

Model building in relation to recent flavour anomalies

Admir Greljo



19.05.2022, LHCP

Flavour Anomalies

Test of lepton universality in beauty-quark decays

#NaN

LHCb Collaboration • Roel Aaij (NIKHEF, Amsterdam) et al. (Mar 22, 2021)

Published in: *Nature Phys.* 18 (2022) 3, 277-282 • e-Print: [2103.11769](https://arxiv.org/abs/2103.11769) [hep-ex]
[pdf](#) [links](#) [DOI](#) [cite](#) [datasets](#)

336 citations

CERN News article

3

4

5

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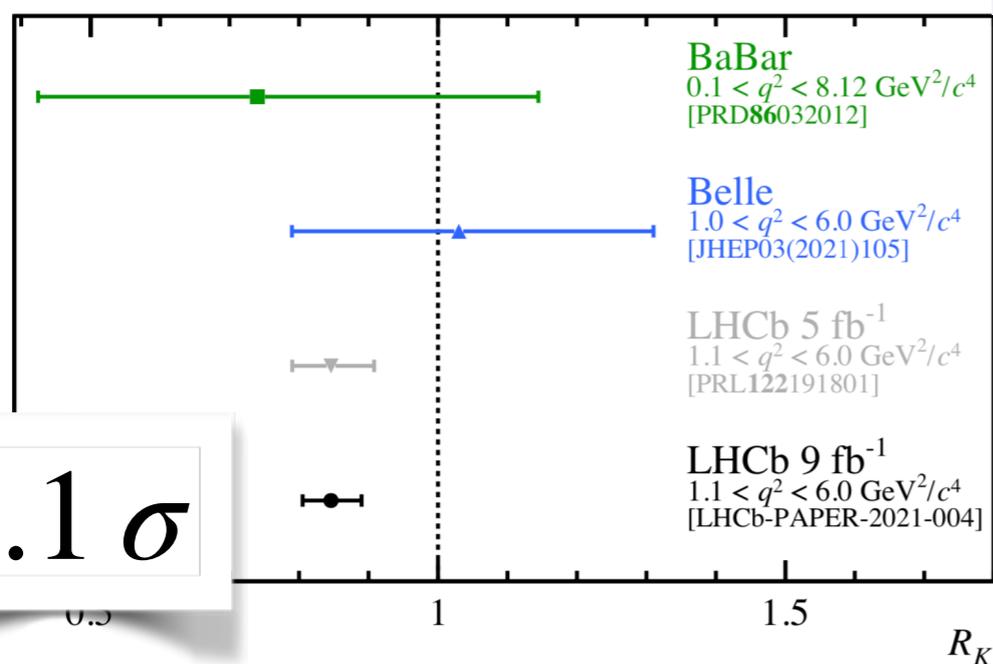
25 / page

LHCb News article

Interactions.org article

BBC News article

Scientific American article



3.1 σ

LHCb, [2103.11769](https://arxiv.org/abs/2103.11769)

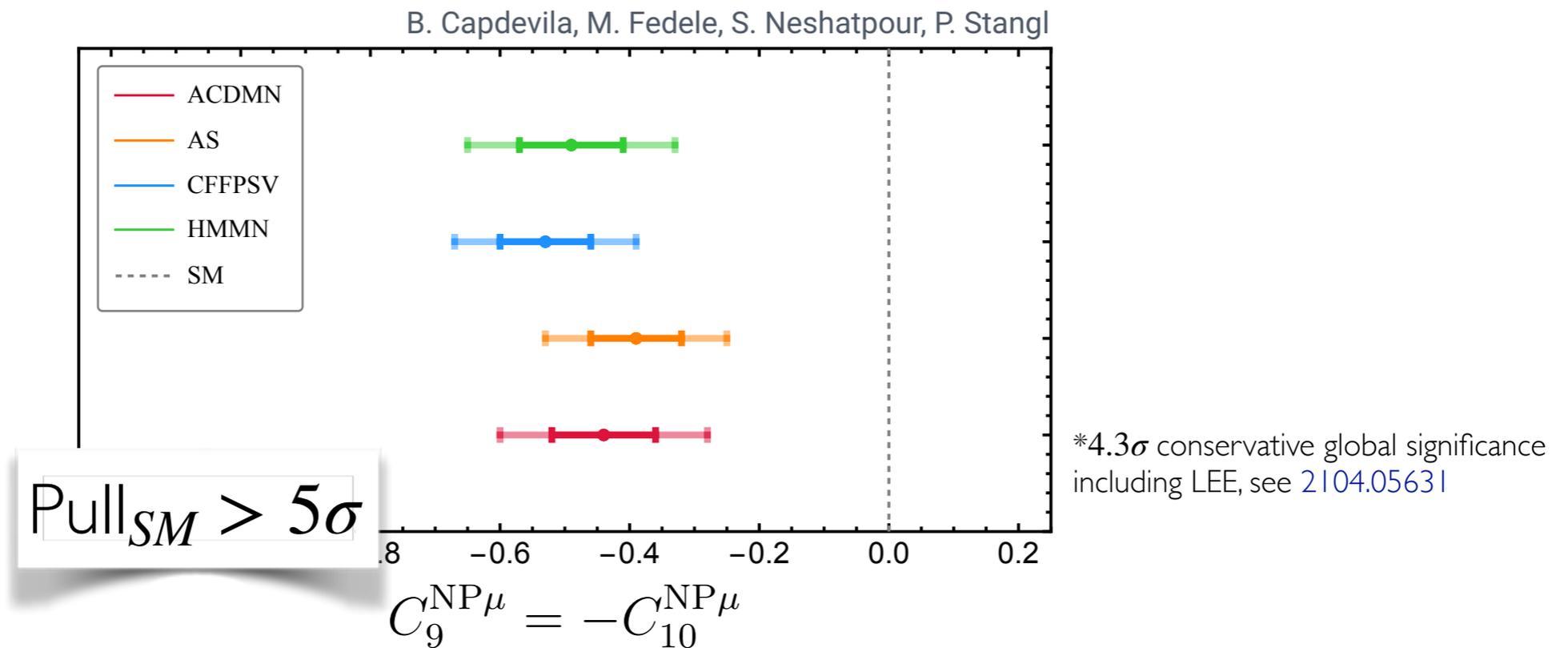
- R_K - Evidence for μ/e universality violation in $B \rightarrow K$

Flavour Anomalies

++ other anomalous observables with the underlying quark-level transition $b \rightarrow s \mu \mu$

Coherent EFT picture

See Planary III: Flavour Physics
See Flavour 2 & 3 parallel sessions



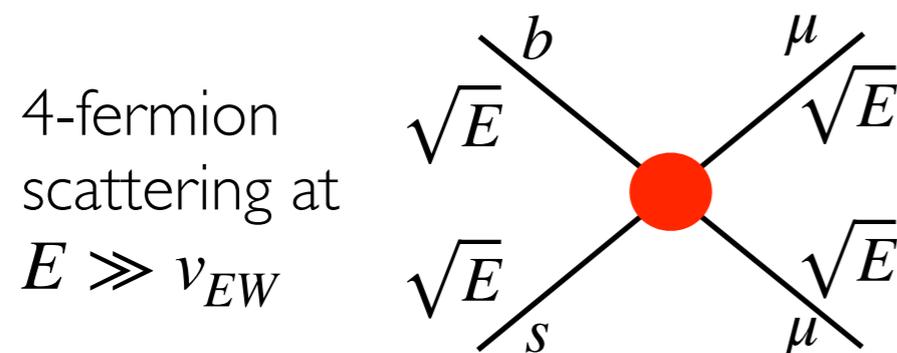
$$\mathcal{L}_{NP} \supset (40 \text{ TeV})^{-2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

$$\approx 10^{-4} G_F/2$$

Bonus: $b \rightarrow c \tau \nu, (g - 2)_\mu$

New mass scale?

- **IF** $b \rightarrow s\ell^+\ell^-$ anomalies are a genuine new physics effect
 \implies **Major Revolution in HEP**



$$\mathcal{A} \sim \frac{E^2}{(40 \text{ TeV})^2}$$

Observational evidence!

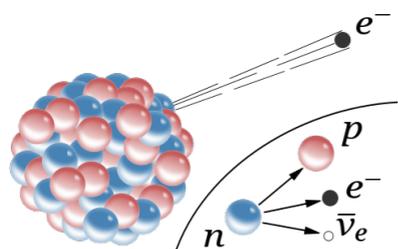
$$\implies M_X \lesssim 100 \text{ TeV}$$

Violation of perturbative unitarity
 Di Luzio, Nardecchia; 1706.01868

- In many realistic models, the mediator is typically much lighter!
 \implies **opportunities for a discovery at the LHC**
- A bright long-term future for collider physics! [Backup]
 - Stronger than the EW naturalness!
 - Other observational evidence: *Neutrino oscillations, Dark Matter, Baryon asymmetry, Inflation, etc* could be a physics of a very high (or different) energy scale.

Mediators?

Phenomena



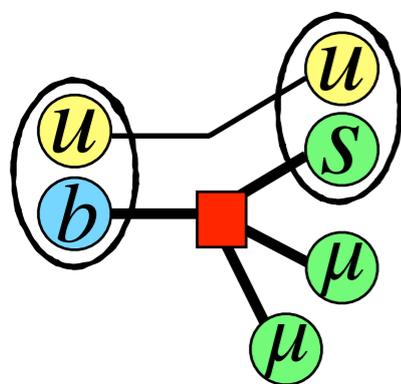
EFT

$$G_F$$

$$\Rightarrow M_X \lesssim 1 \text{ TeV}$$

Mediator

$$W^\pm$$

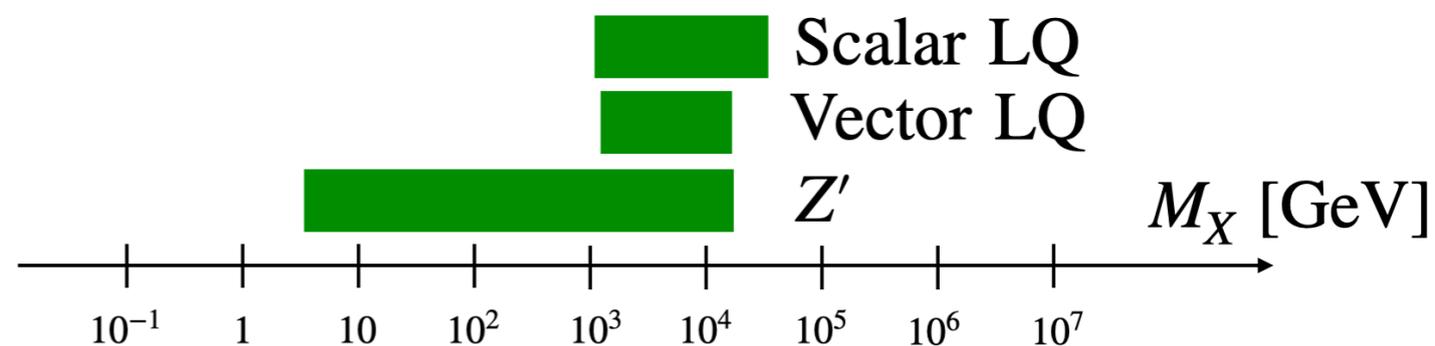
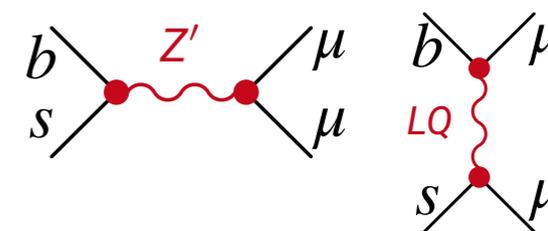


$$\mathcal{O}(10^{-4}) G_F$$

$$\Rightarrow M_X \lesssim 100 \text{ TeV}$$

See also talk by M. Blanke

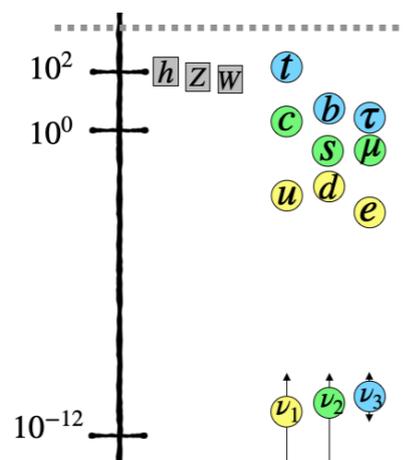
$$Z', LQ, ?$$



Directions in model building

*some examples,
not a review

Any connections with the big open questions?



Flavour puzzle,
Higgs mass,
Charge quantisation,
...

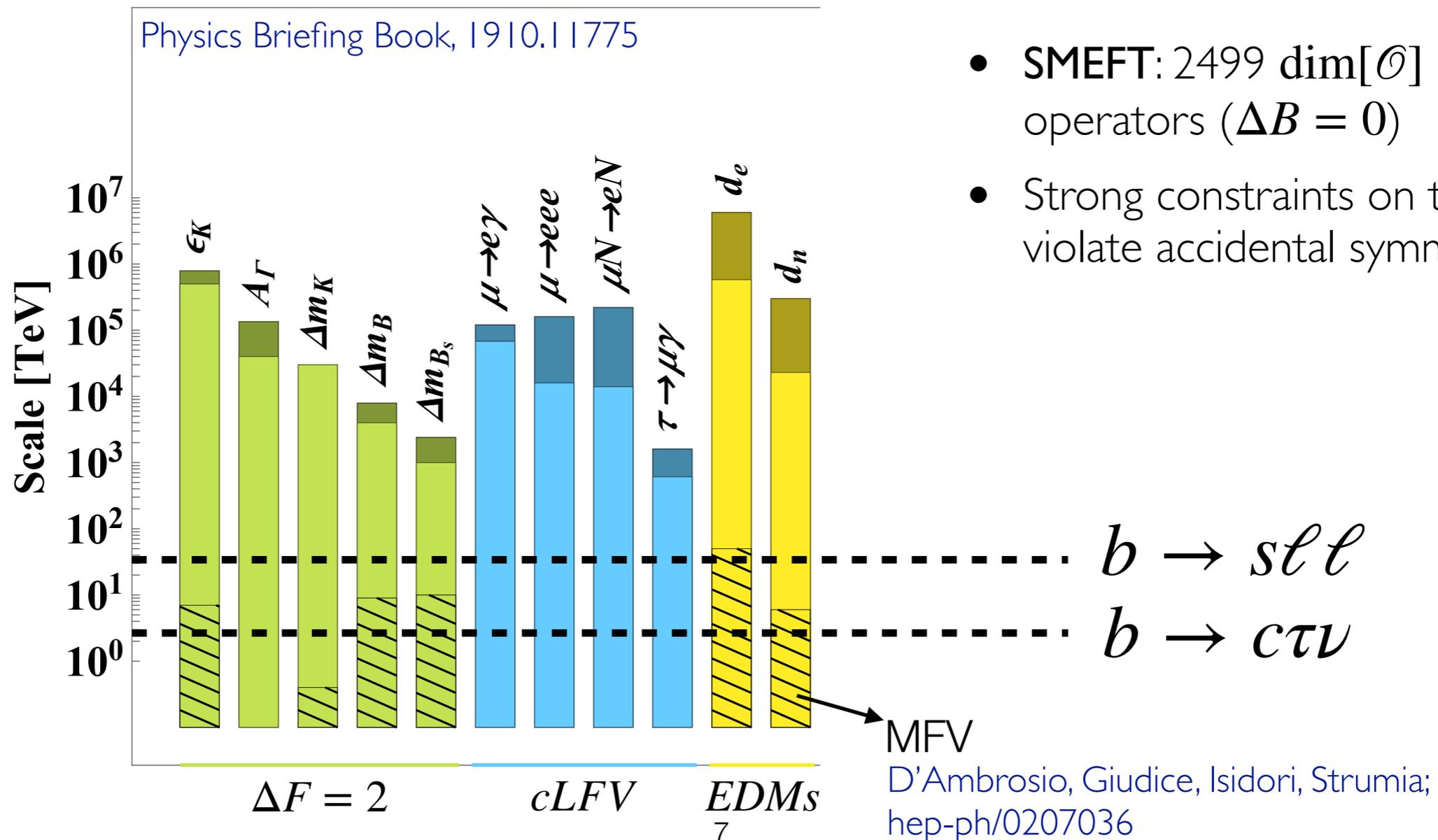


Flavour Symmetries

- Exact and approximate accidental symmetries carefully revisited

Consistency game

Explain the anomalies while passing other constraints



Flavour Symmetries

- MFV doesn't work well for B anomalies!
- Other flavour symmetries and their breaking patterns to be explored
- The winner in the quark sector: $U(2)^3$ [Barbieri et al; 1105.2296](#)
[Buttazzo et al; 1706.07808](#)

$$Y_{u,d} \sim \begin{pmatrix} \boxed{\Delta_{u,d}} & \boxed{V} \\ 0 & 0 & \textcircled{1} \end{pmatrix} \quad \begin{aligned} \Delta &\ll V \ll 1 \\ V^\dagger &\propto (V_{td}, V_{ts}) \end{aligned}$$

Flavour Symmetries

- MFV doesn't work well for B anomalies!
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[Buttazzo et al; 1706.07808](#)

Charting the space of SMEFT with flavour symmetries

[Faroughy, Isidori, Wilsch, Yamamoto; 2005.05366](#)
[AG, Thomsen, Palavric; 2203.09561](#)

SMEFT $\mathcal{O}(1)$ terms (dim-6, $\Delta B = 0$)		Lepton sector							
		MFV _L	U(3) _V	U(2) ² × U(1) ²	U(2) ²	U(2) _V	U(1) ⁶	U(1) ³	No symm.
Quark sector	MFV _Q	47	54	65	71	80	87	111	339
	U(2) ² × U(3) _d	82	93	105	115	128	132	168	450
	U(2) ³ × U(1) _{b_R}	96	107	121	128	144	150	186	480
	U(2) ³	110	123	135	147	162	164	206	512
	No symm.	1273	1334	1347	1407	1470	1425	1611	2499

(*) Terms relevant for the high- p_T physics: Top, Higgs & electroweak

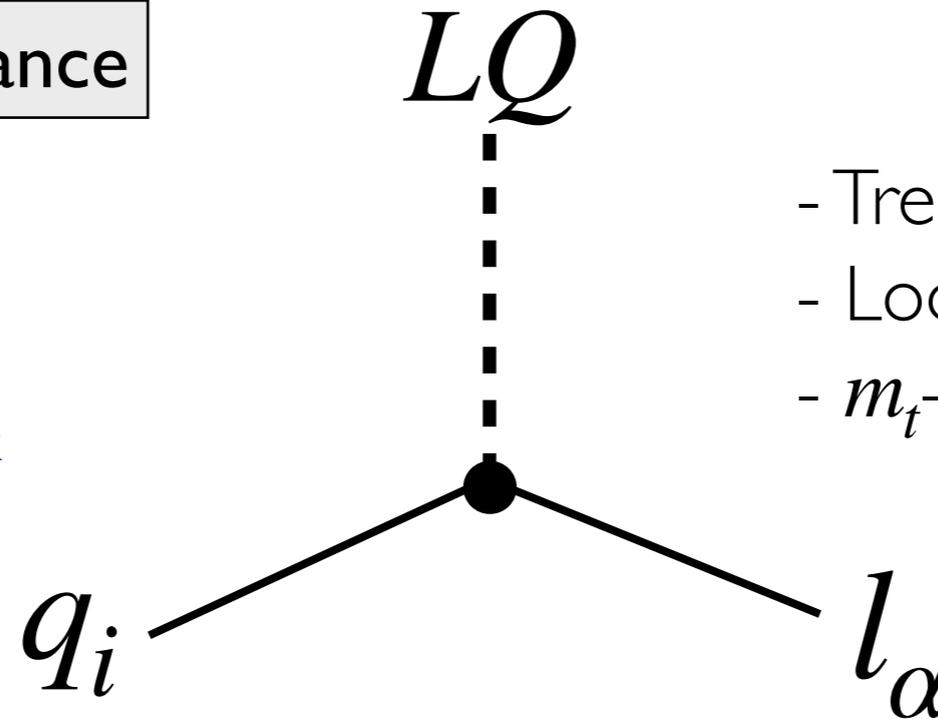
See talks by Juan Rojo and Tevong You. See also the Top 2 parallel session

The LHC EFT WG: the flavour structure compatible with B anomalies?

TeV-scale Leptoquarks

The leptoquark renaissance

[Phys.Rept. 641 (2016) 1-68]
Doršner, Fajfer, AG, Kamenik, Košnik



- Tree-level $2q2\ell$,
- Loop-suppressed $4q$ and 4ℓ ,
- m_t -enhanced $(g - 2)_\mu$.

Flavour symmetries + Leptoquarks

$$U(2)_q \times U(2)_\ell$$

$$\mathcal{L} \supset q_3 \ell_3 \mathcal{S}$$

$$U(2)_q \times U(1)_\mu$$

$$\mathcal{L} \supset q_3 \ell_2 \mathcal{S}$$

(Small breaking gives $b \rightarrow s\mu\mu$)

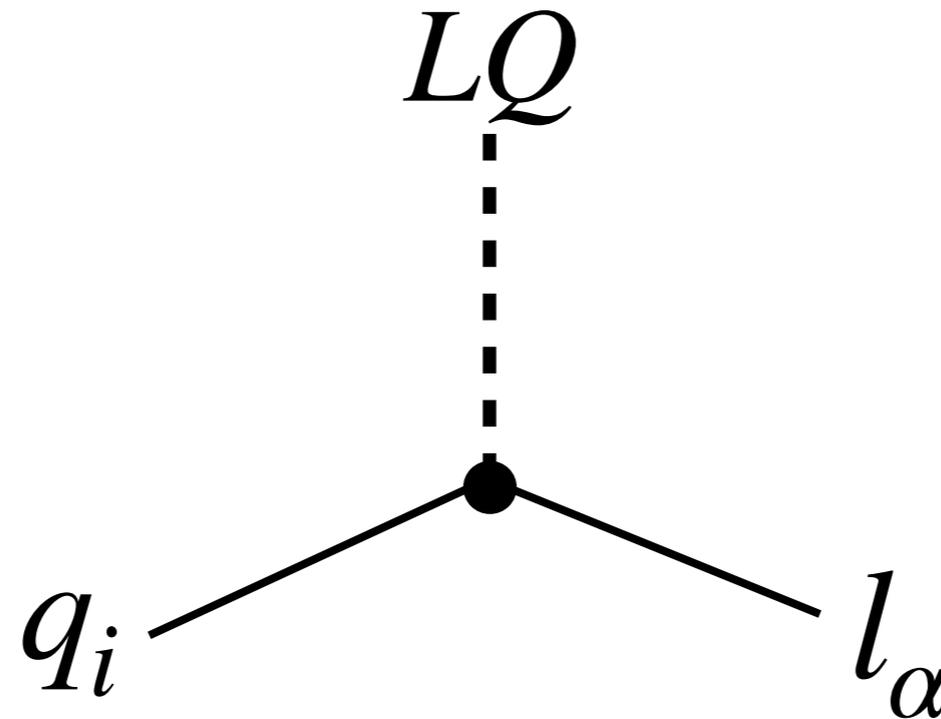
$$+b \rightarrow c\tau\nu$$

Buttazzo et al; 1706.07808

$$+(g - 2)_\mu$$

AG, Stangl, Thomsen; 2103.13991

TeV-scale Leptoquarks



Two thriving model-building directions:

Quark-Lepton Unification

- Variations of the original Pati-Salam idea

$$SU(4) \times SU(3)' \times SU(2)_L \times U(1)'$$

e.g. Di Luzio, AG, Nardecchia; 1708.08450
AG, Stefanek; 1802.04274

The Composite Higgs

- If Higgs was a π ,
LQ would be a K , ...

e.g. Marzocca; 1803.10972
Gripaios, Nardecchia, Renner; 1412.1791

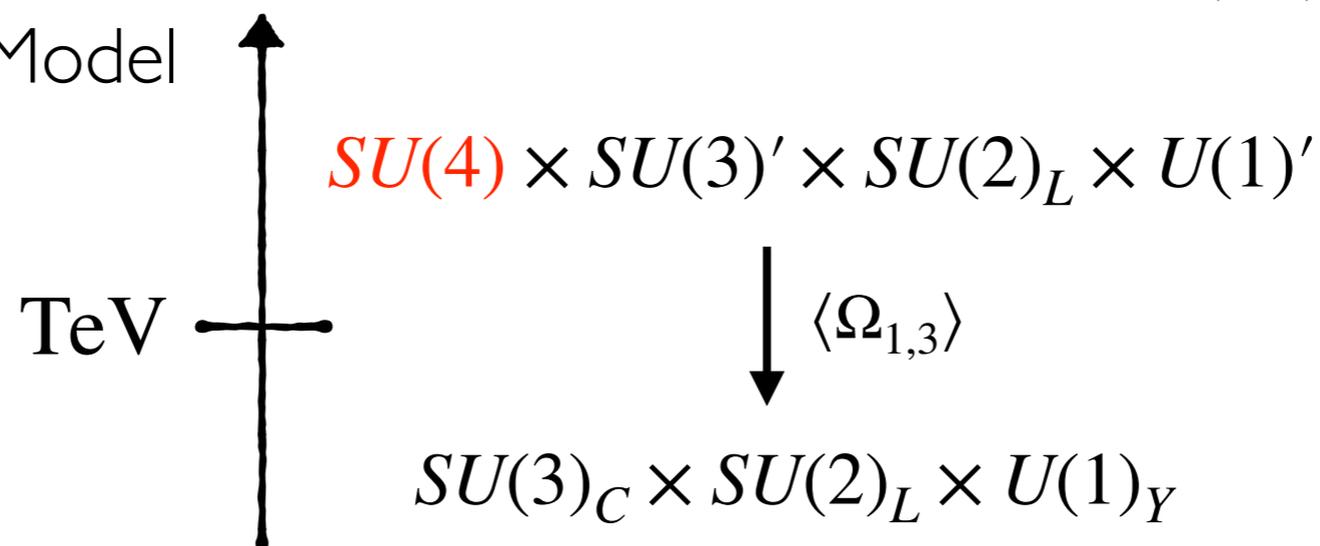


Fuentes-Martin, Stangl; 2004.11376

The 4321 model

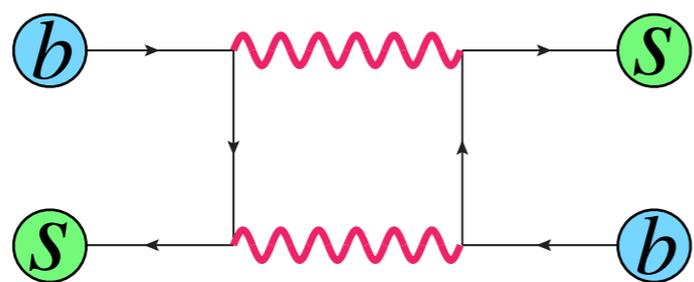
- New gauge extension of the Standard Model

Di Luzio, AG, Nardecchia; 1708.08450



- Comprehensive investigation:

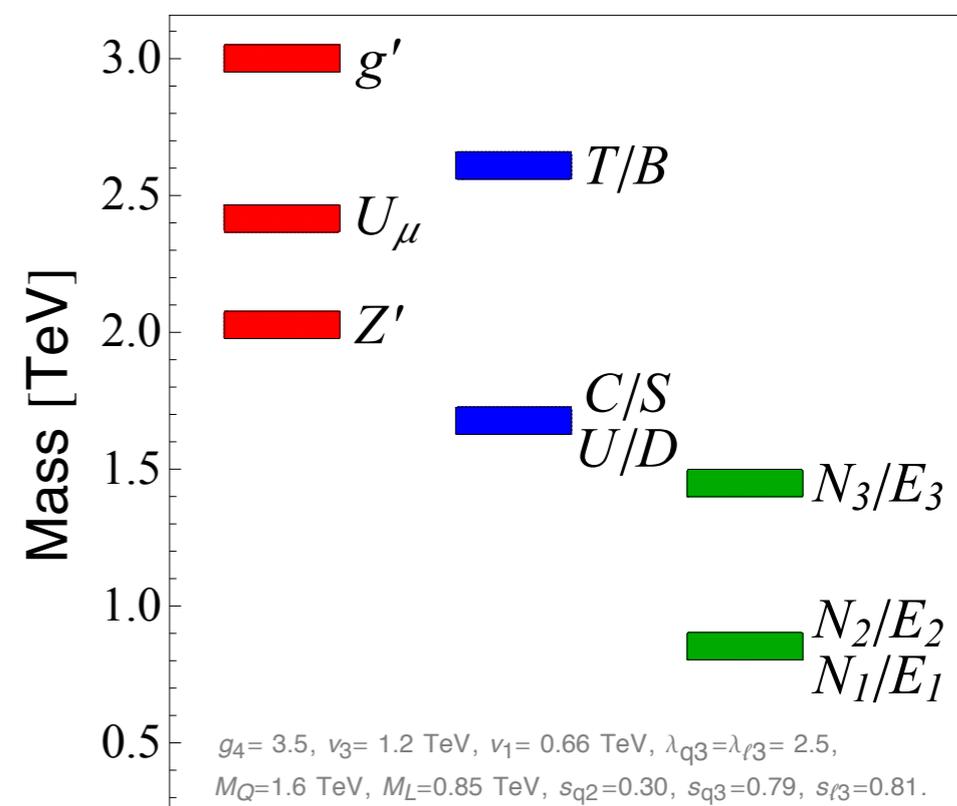
Di Luzio, Fuentes-Martin, AG, Nardecchia, Renner; 1708.08450



$$C_{bs}^{LL} \sim \Delta R_{D^{(*)}}^2 M_L^2$$

The lightest new states are vector-like leptons!

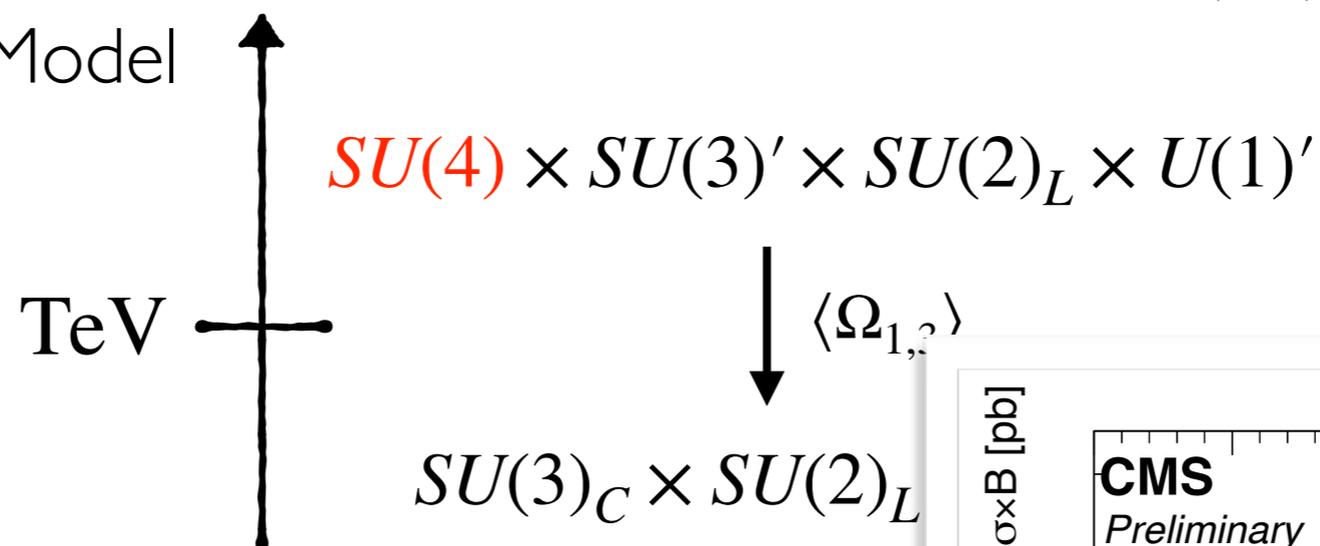
Benchmark spectrum



The 4321 model

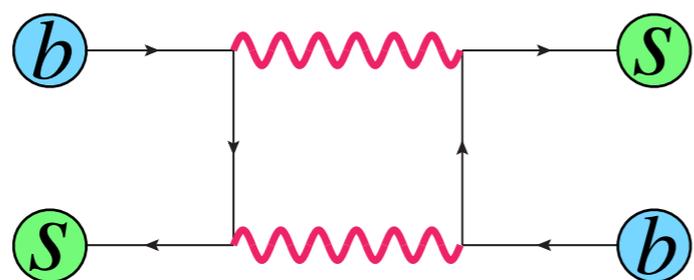
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Di Luzio, AG, Nardecchia; 1708.08450



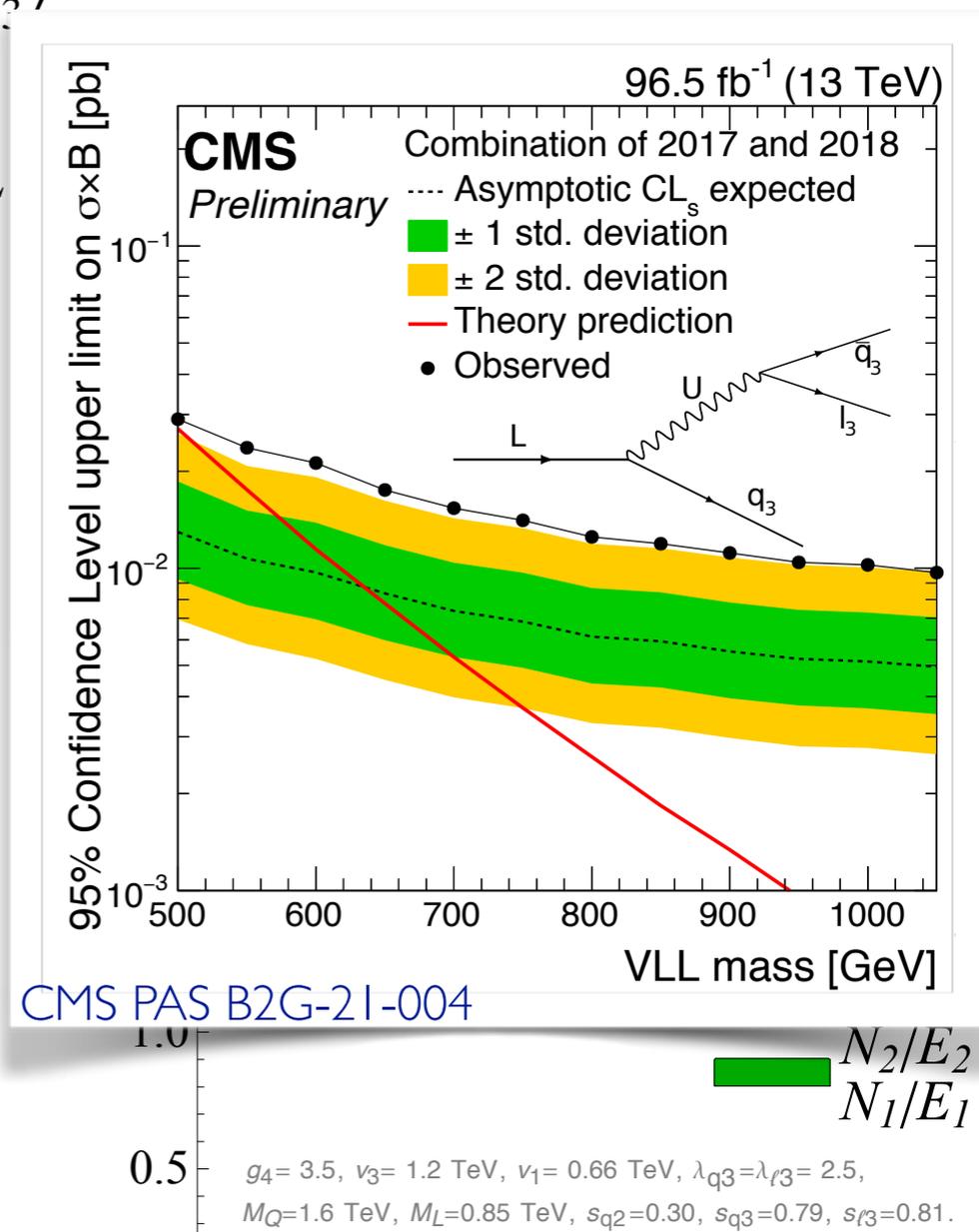
- Comprehensive investigation:

Di Luzio, Fuentes-Martin, AG, Nardecchia, Renner; 1708.08450



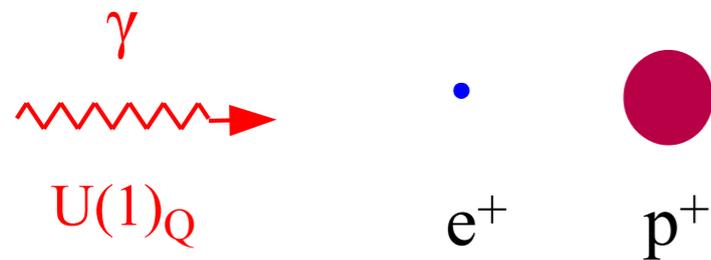
$$C_{bs}^{LL} \sim \Delta R_{D^{(*)}}^2 M_L^2$$

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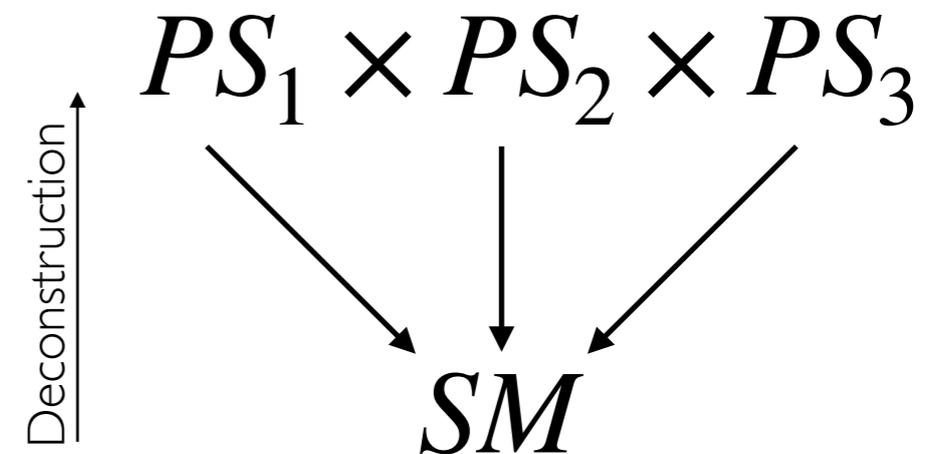
Non-universal gauge interactions

Bordone, Cornella, Fuentes-Martin, Isidori; 1712.01368



Far apart at short distances!

Universality of gauge interactions:
Only a **low-energy property**?

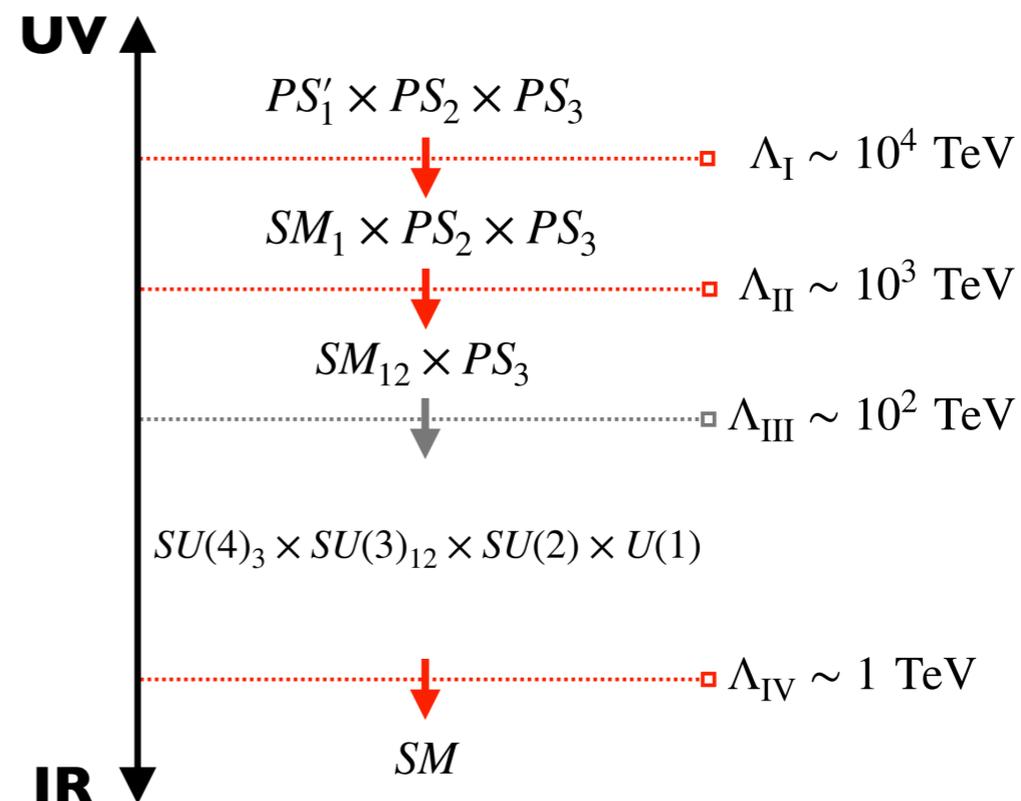


Flavour hierarchies

Bordone, Cornella, Fuentes-Martin, Isidori; 1712.01368

Multi-scale flavour

- Series of hierarchical SSBs
 \implies Flavour hierarchies



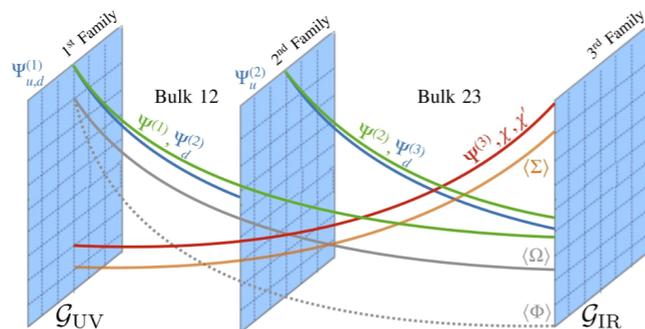
Flavour hierarchies

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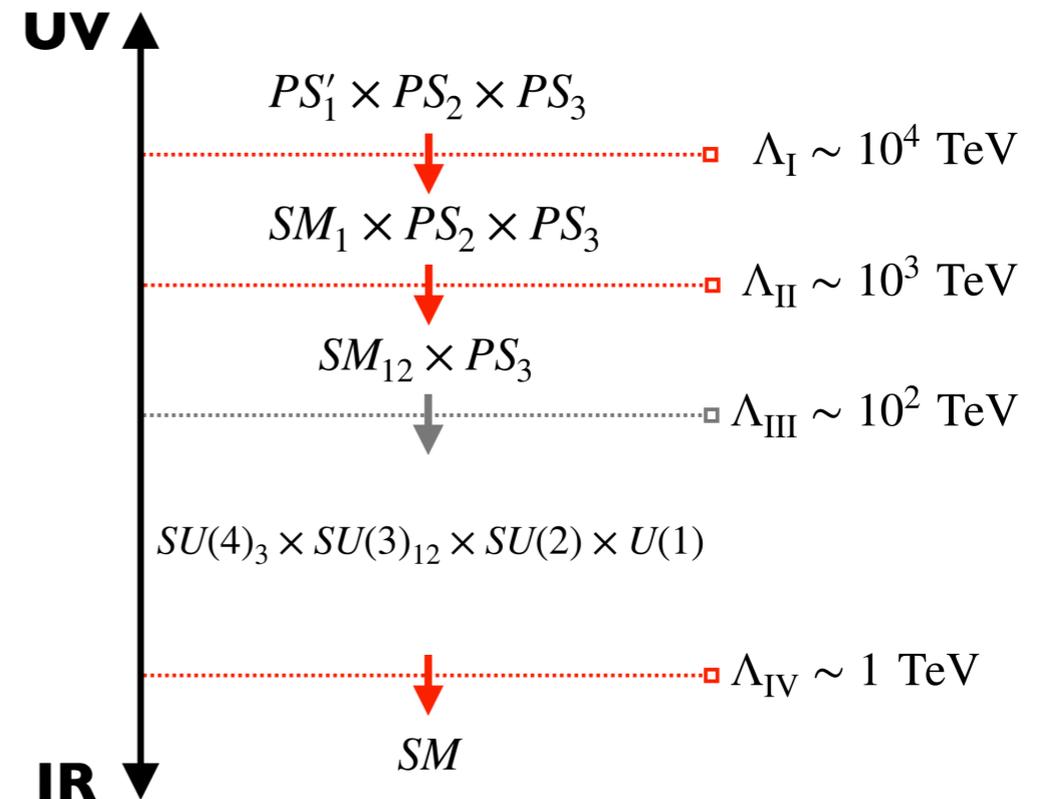
Flavour as a topological defect

- 5D warped compactification
 \implies Flavour + Higgs



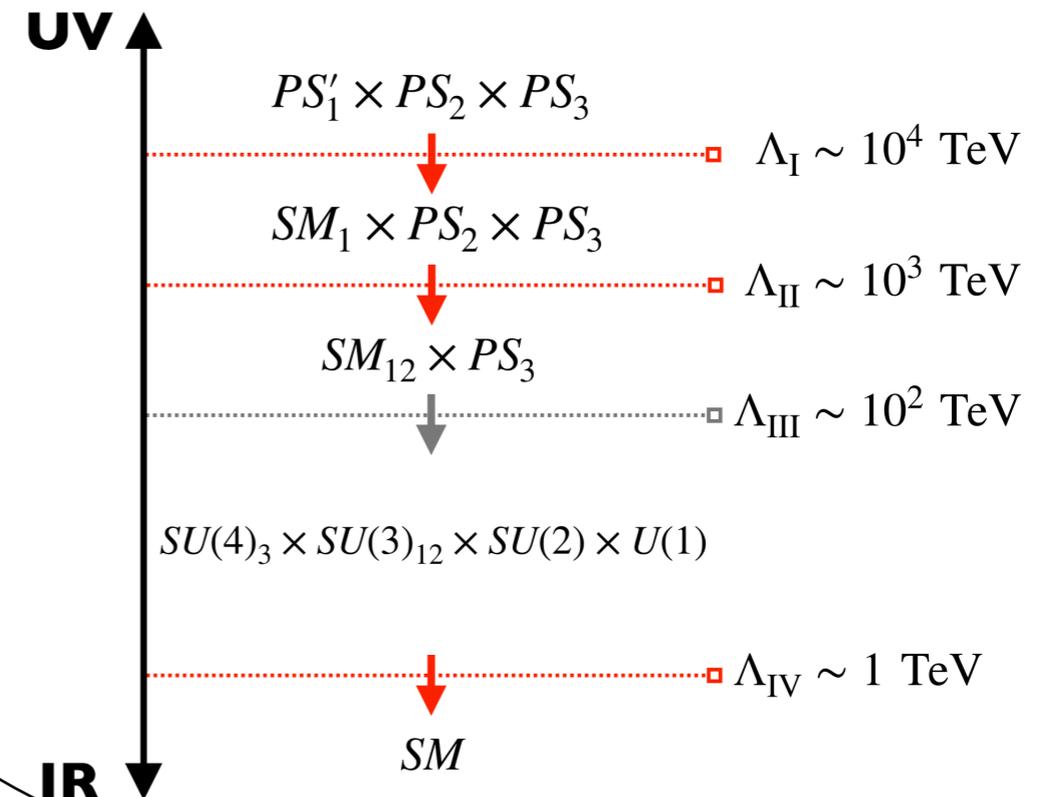
Fuentes-Martin et al; 2203.01952

Bordone, Cornella, Fuentes-Martin, Isidori; 1712.01368



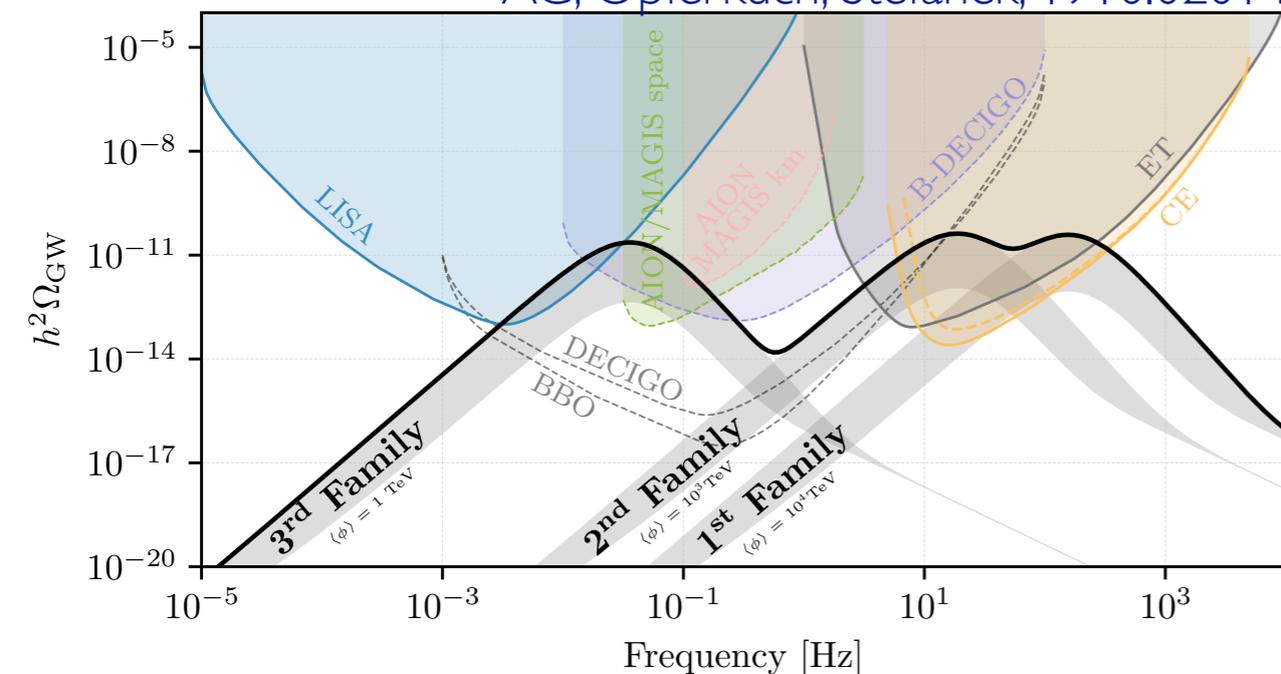
Cosmological implications

Bordone, Cornella, Fuentes-Martin, Isidori; 1712.01368



- Novel connections
GW astronomy & Flavour physics

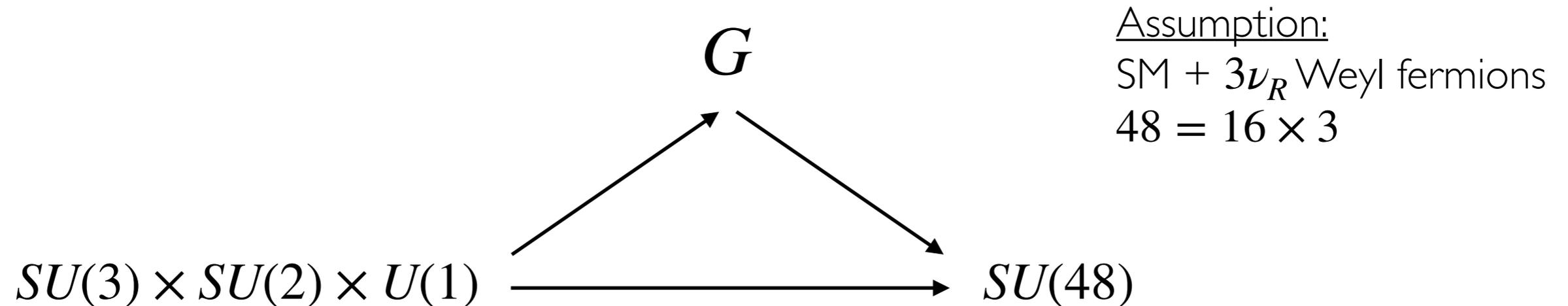
AG, Opferkuch, Stefanek; 1910.02014



Stochastic gravitational wave radiation with the characteristic **three-peaked** signature.

$$\begin{array}{lll} \sqrt{m_t m_b} & : & \sqrt{m_s m_c} & : & \sqrt{m_u m_d} \\ 1 & : & 10^{-2} & : & 10^{-4} \\ f_{\text{LISA}}^{-1} & : & \dots & : & f_{\text{ET}}^{-1} \end{array}$$

(Partial) Unification

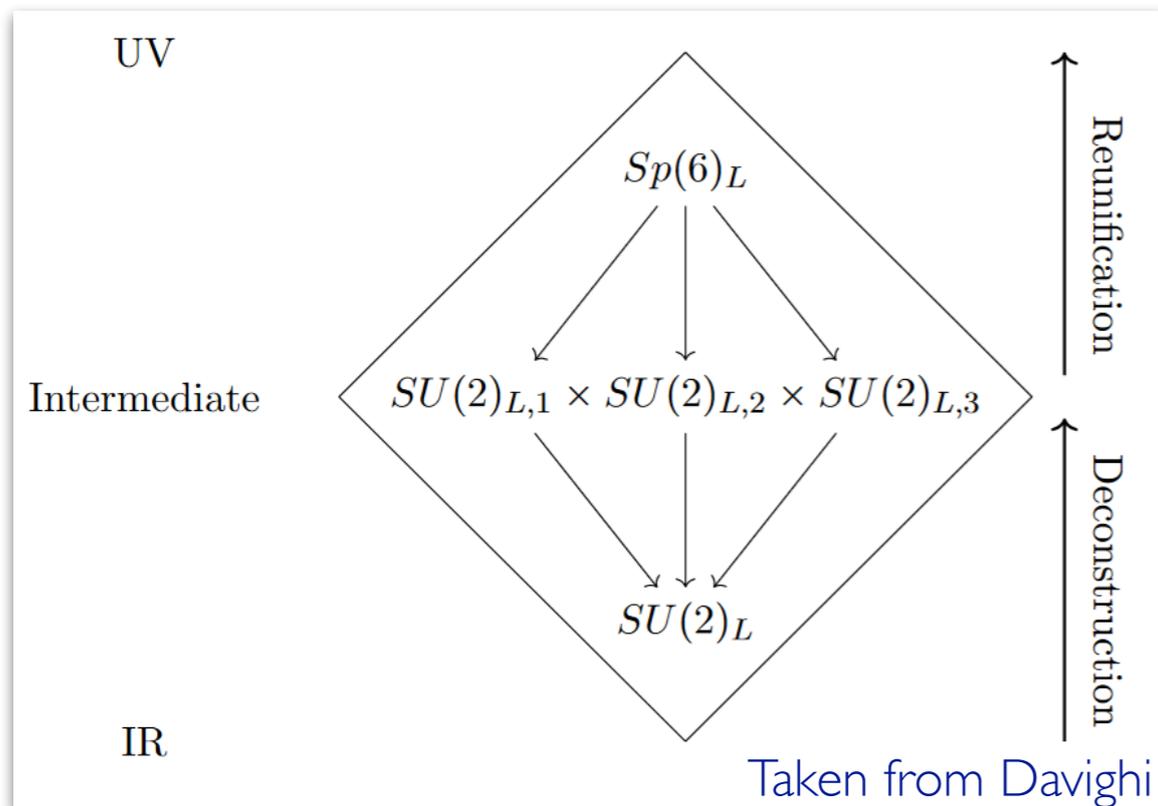


Allanach, Gripaos, Tooby-Smith; 2104.14555

- Classification of anomaly-free semisimple algebras containing the SM
- Novel ‘GUTs’ beyond the universal PS , $SU(5)$ or $SO(10)$
- An example is $G = PS_1 \times PS_2 \times PS_3$ Bordone et al; 1712.01368

Gauge-Flavour unification

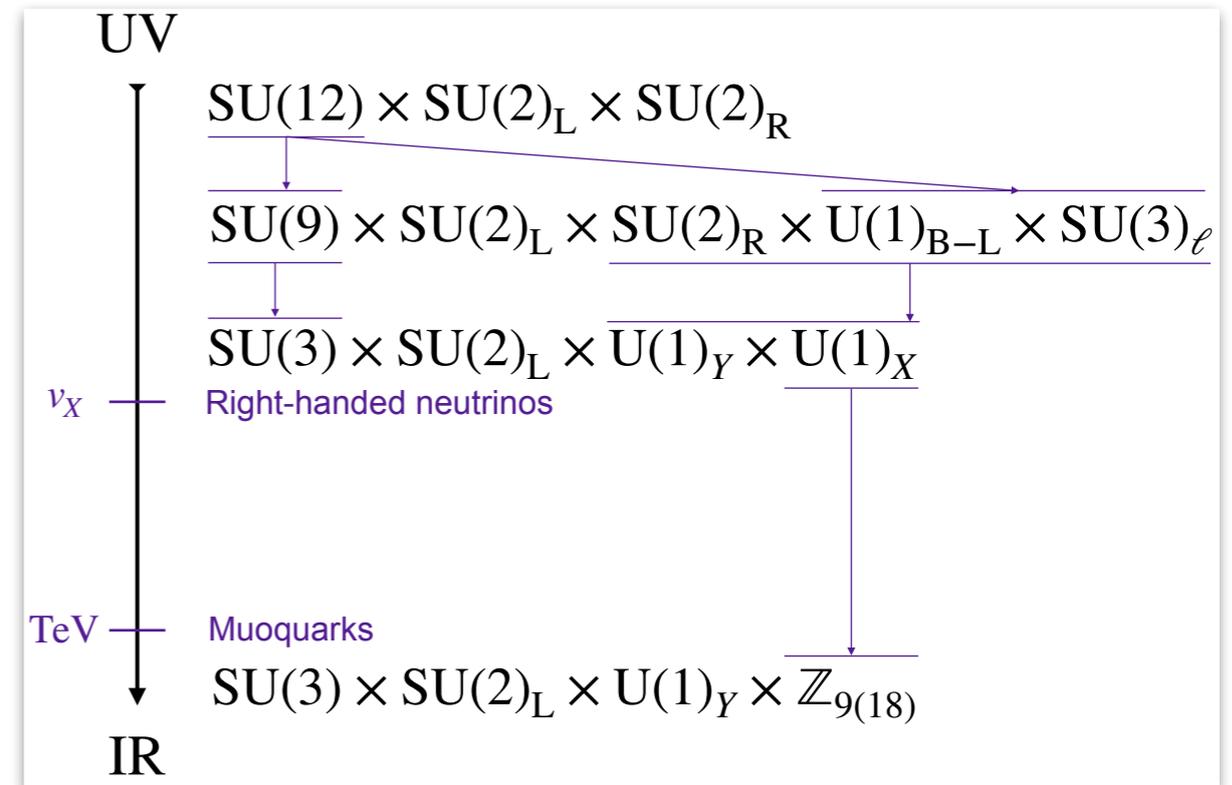
$$G = SU(4) \times Sp(6) \times Sp(6)$$



Electroweak flavour unification

Davighi, Tooby-Smith; 2201.07245

$$G = SU(12) \times SU(2) \times SU(2)$$



Color flavour unification

Davighi, AG, Thomsen; 2202.05275

Summary

- Flavour anomalies triggered flourishing model building directions:
 - *Flavour Symmetries*
 - *TeV-scale Leptoquarks*
 - *Non-universal gauge extensions*
 - *Multi-scale flavour*
 - *Quark-lepton unification*
 - *Gauge-flavour unification*
- Valuable results even if the anomalies go away
- If the anomalies 'stay' \implies
a major boost for the existing and future collider physics program



Backup

Non-universal gauged $U(1)$

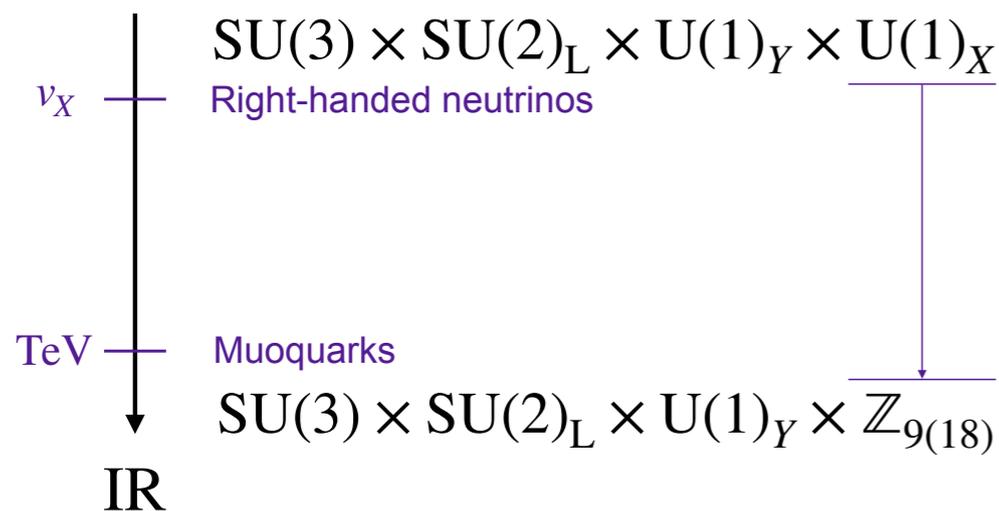
Lepton non-universal $U(1)$

- The prime example: $U(1)_{L_\mu - L_\tau}$ Altmannshofer et al, 1403.1269, 1406.2332
- Classification of anomaly-free $U(1)$ extensions Allanach, Davighi, Melville; 1812.04602
- Selection rules for leptoquarks and deriving accidental $U(1)^3$ AG, Soreq, Stangl, Thomsen, Zupan; 2107.07518

Lepton non-universal

Davighi, AG, Thomsen; 2202.05275

$$X = 3m(B - L) - n(2L_\mu - L_e - L_\tau)$$



$$(m, n) = (3a + r, 9b + 3r), \quad \text{for } r \in \{1, 2\},$$

$$(a, b) \in \mathbb{Z}^2, \text{ and } \gcd(3a + r, b - a) = 1.$$

Novel mechanism

Exact proton stability!

(to all orders in the SMEFT)

$$\Delta B = 0 \pmod{3}$$

~~p decay~~
 ~~$n \leftrightarrow \bar{n}$~~

✓ sphaleron

Similar mechanisms shortly after:

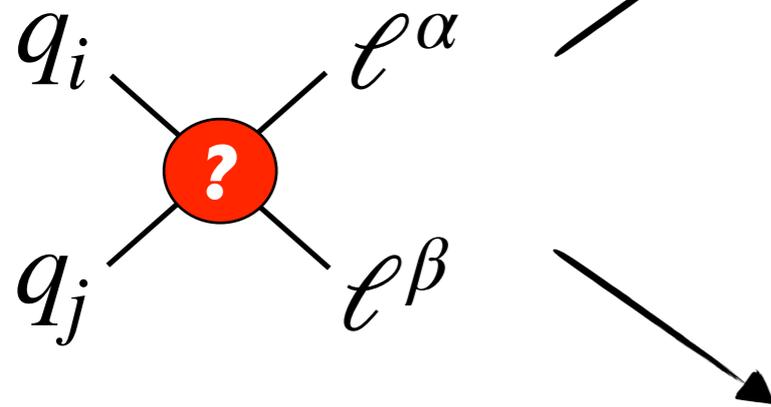
Koren; 2204.01741,

Wang, Wan, You; 2204.08393

Flavour Physics in High- p_T Tails

 for flavor-sensitive interactions

$$pp \rightarrow \ell_\alpha^+ \ell_\beta^- (j), \dots$$



Scale

TeV 0.1 am



GeV 0.1 fm



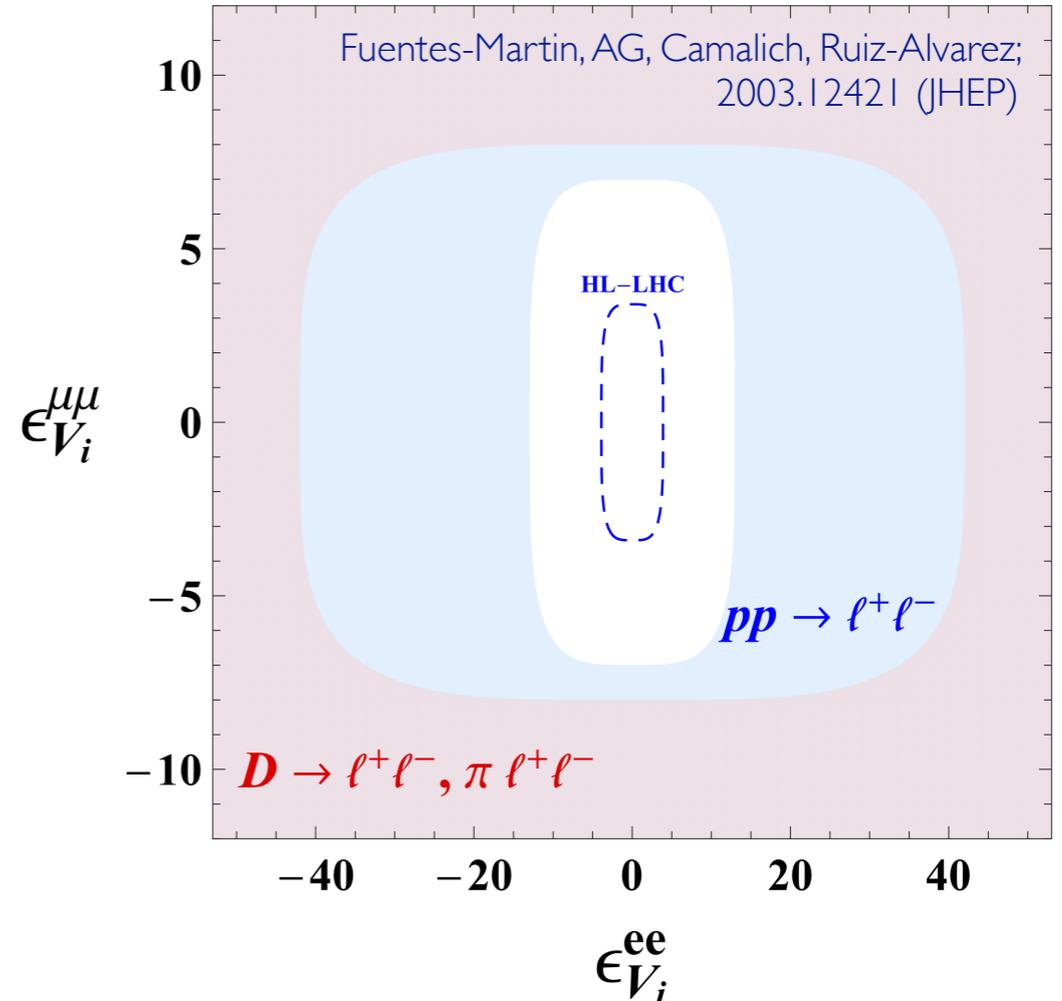
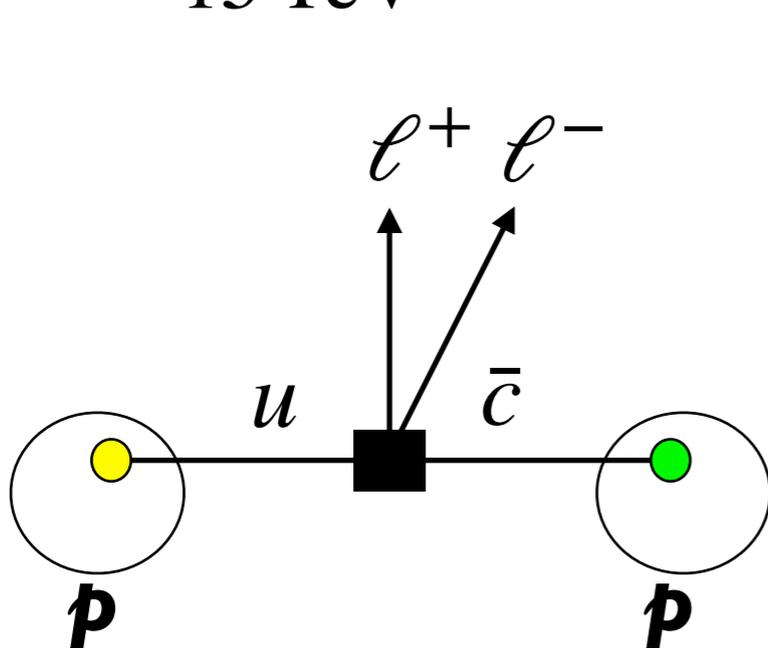
 A wealth of information for flavour physics, **complementary** to hadron decays.

Flavour Physics in High- p_T Tails

Example: Rare $c \rightarrow u\ell^+\ell^-$ decays

- Tiny SM rates: $BR(D^0 \rightarrow \mu^+\mu^-) \sim \mathcal{O}(10^{-13})$
short-distance contribution negligible (efficient GIM suppression), long-distance dominated
- Already strong experimental upper limits: $BR(D^0 \rightarrow \mu^+\mu^-) \lesssim 6 \times 10^{-9}$ LHCb, 1305.5059
- **Null test of the SM** sensitive to New Physics

$$\mathcal{L}_{NP} \approx \frac{\epsilon_V^{\ell\ell}}{15 \text{ TeV}} (\bar{u}_R \gamma^\mu c_R) (\bar{\ell}_R \gamma^\mu \ell_R)$$

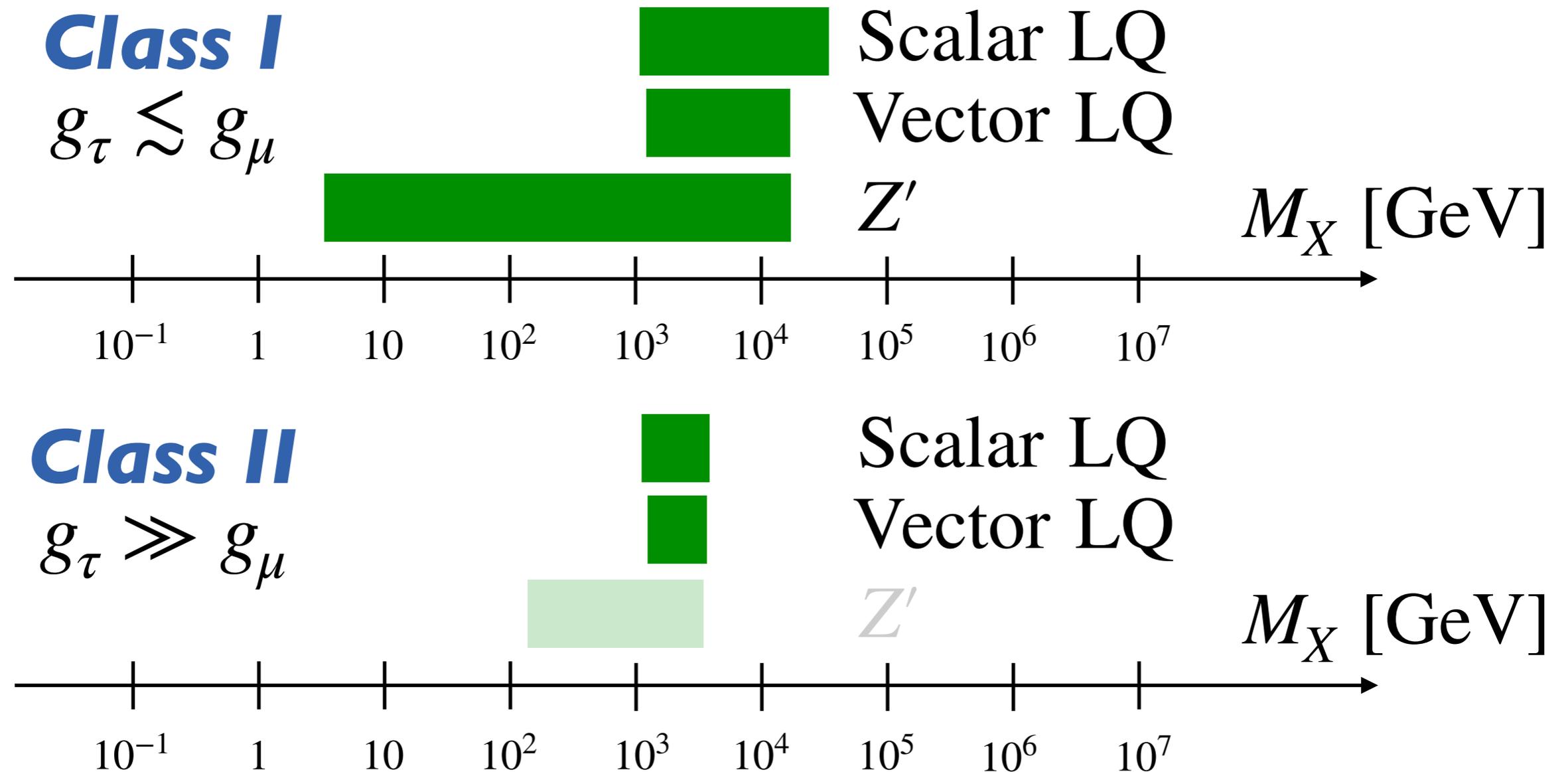


Low- p_T roadmap

1. $b \rightarrow s\ell\ell$: Only μ ? LH or vectorial? Universal contribution?
2. $b \rightarrow c\tau\nu$: Yes or No?
If yes, $\Lambda \lesssim 10$ TeV, $U(2)_\ell$ preferred, $g_\tau \gg g_\mu$. Eg $LQ \rightarrow \tau b$.
3. $(g - 2)_\mu$: Yes or No? Leptonic $U(1)^3$.
4. $b \rightarrow s\nu\nu$ & $b \rightarrow s\tau\tau$:
 $SU(2)_L$ prediction. If large $\gg 10\%$, $U(2)_\ell$ again.
5. $b \rightarrow d\ell\ell(\nu\nu)$: Test $U(2)_q$, also in $s \rightarrow d\nu\nu$
6. LFV in b decays: Leptonic flavour, e.g. $U(2)_\ell$ vs $U(1)^3$
7. cLFV ($e_i \rightarrow e_j$), τ LFU, $\Delta F = 2$, EDMs, EWPO: Z and W pole physics, ...

The high- p_T targets

- $b \rightarrow s\ell\ell$: Tree-level



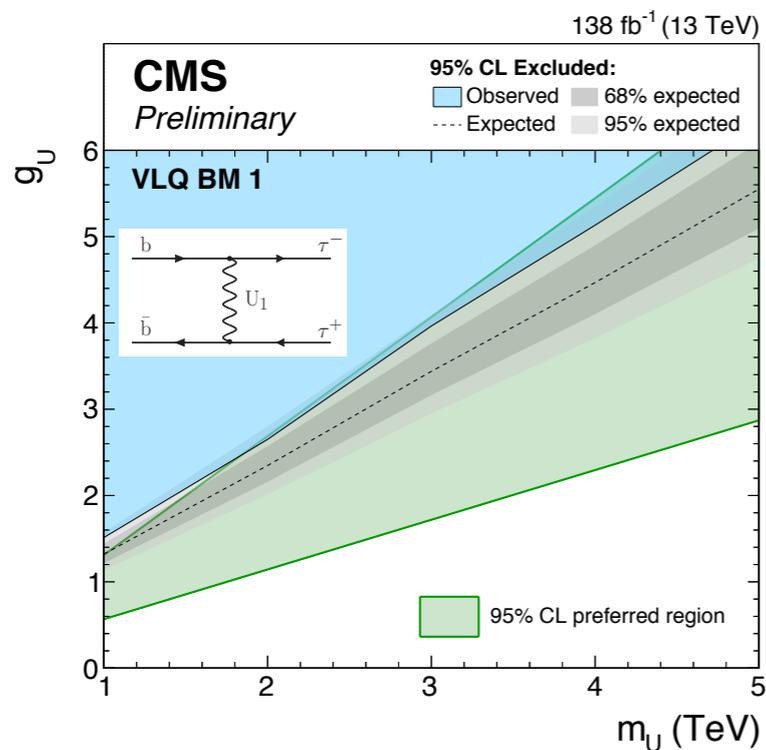
- Loop-level mediators $\gtrsim 0.1$ TeV and \lesssim few TeV

High- p_T LHC

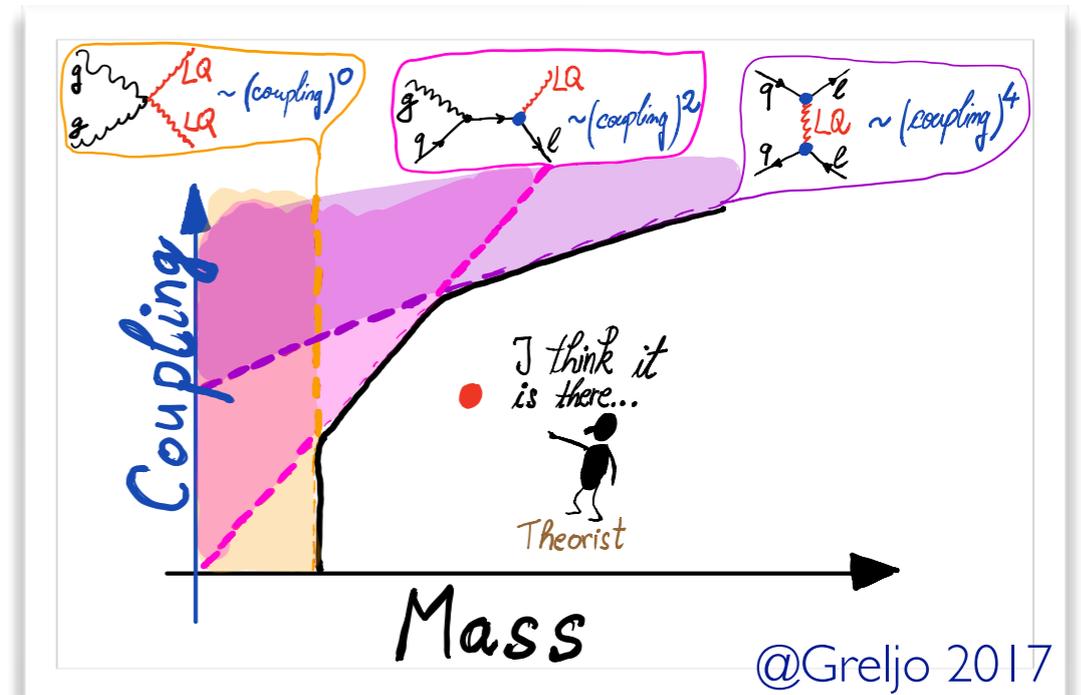
- Resonances and tails in:

- $\tau\tau(b)$, Faroughy, AG, Kamenik; 1609.07138
- $\tau\nu(b)$, AG, Camalich, Ruiz-Alvarez; 1811.07920
Marzocca, Min, Son; 2008.07541
- $\mu\mu(b)$, AG, Marzocca; 1704.09015
Afik et al; 1805.11402, 1912.00425
- ...

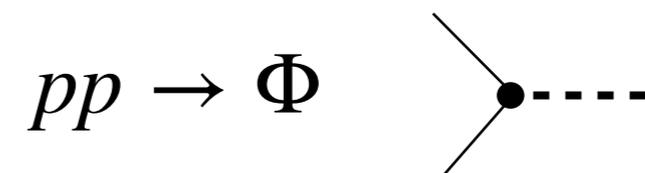
- Leptoquark searches



CMS PAS HIG-21-001



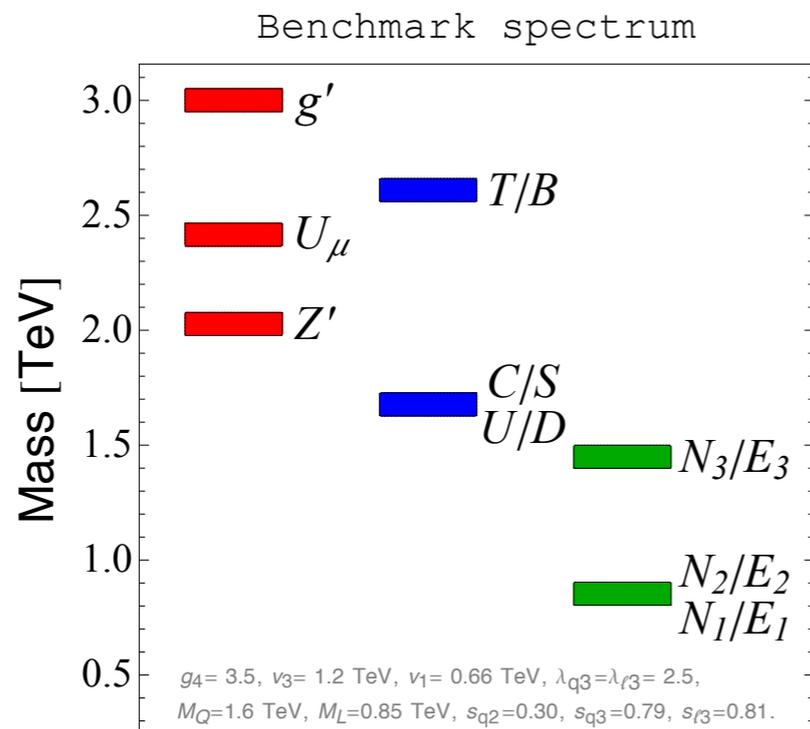
Novel mechanism
 Resonant LQ production



Buonocore, Haisch, Nason,
 Tramontano, Zanderighi; 2005.06475
 Haisch, Polesello; 2012.11474
 AG, Selimovic; 2012.02092

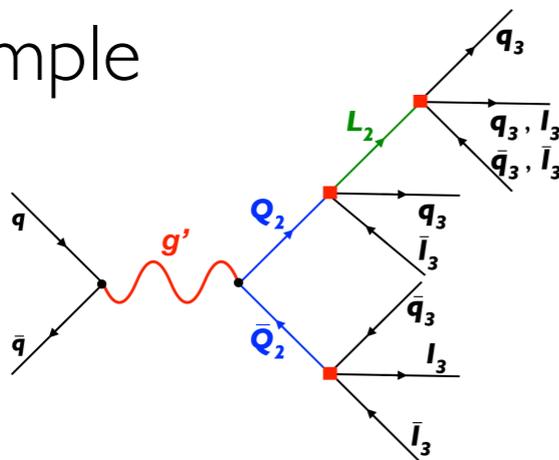
High- p_T LHC

- Explicit models:
The 4321 model

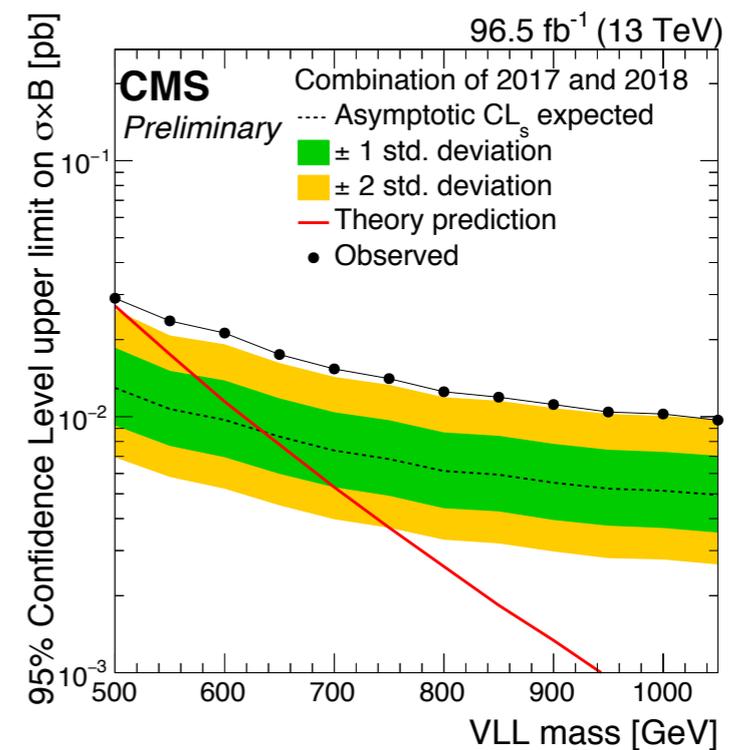
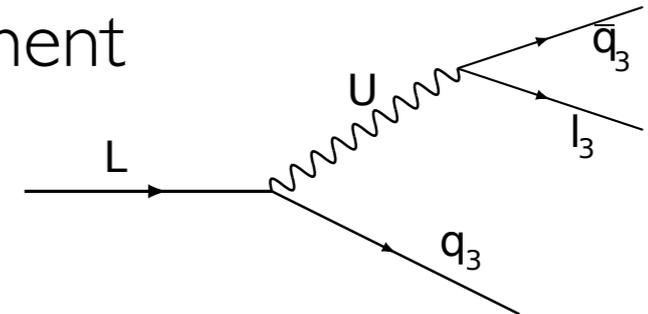


Di Luzio, Fuentes-Martin, AG,
Nardecchia, Renner; 1708.08450

- Example



- Experiment



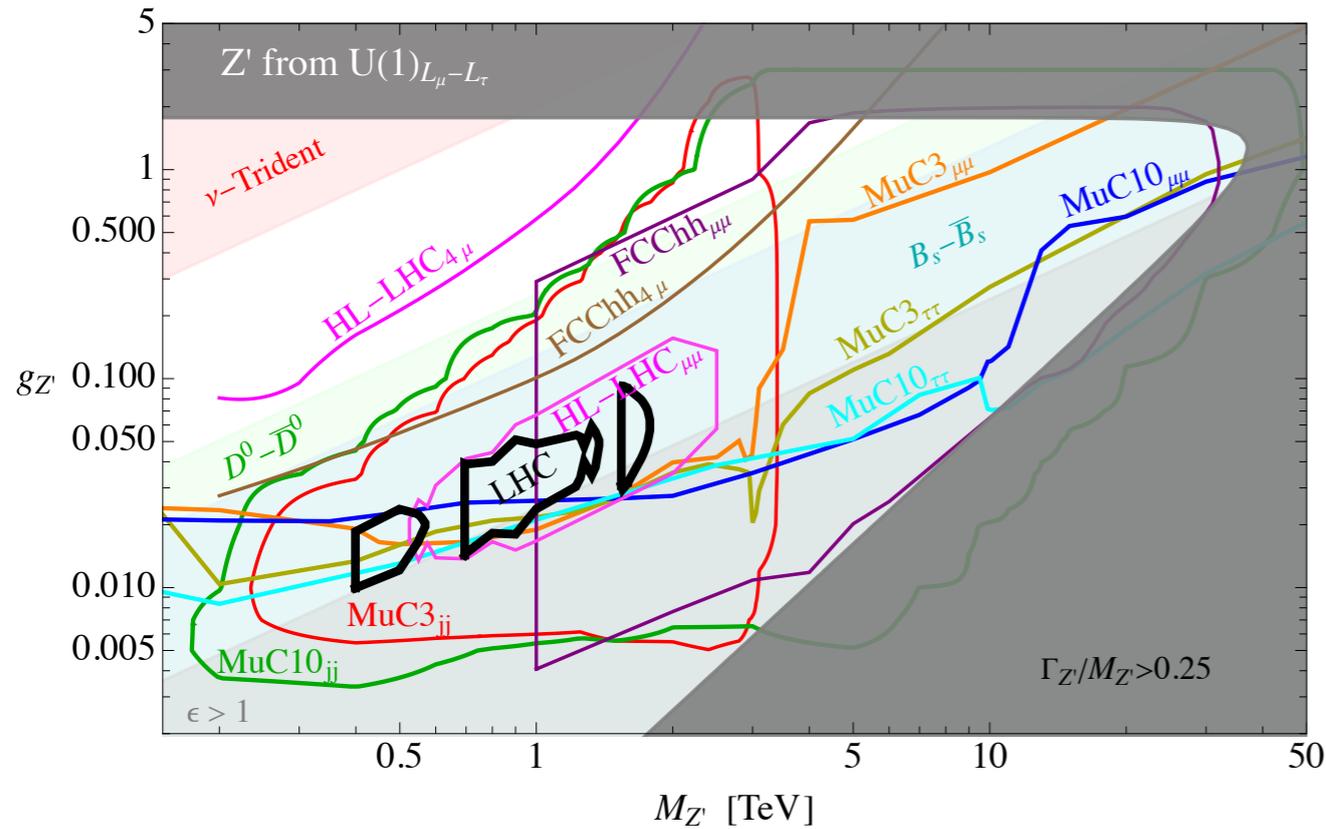
CMS PAS B2G-21-004

The CMS quote:

“The observed excess is consistent with the presence of VLLs in the context of the 4321 model, and the excess of events over the background-only hypothesis corresponds to a significance of 2.8σ .”

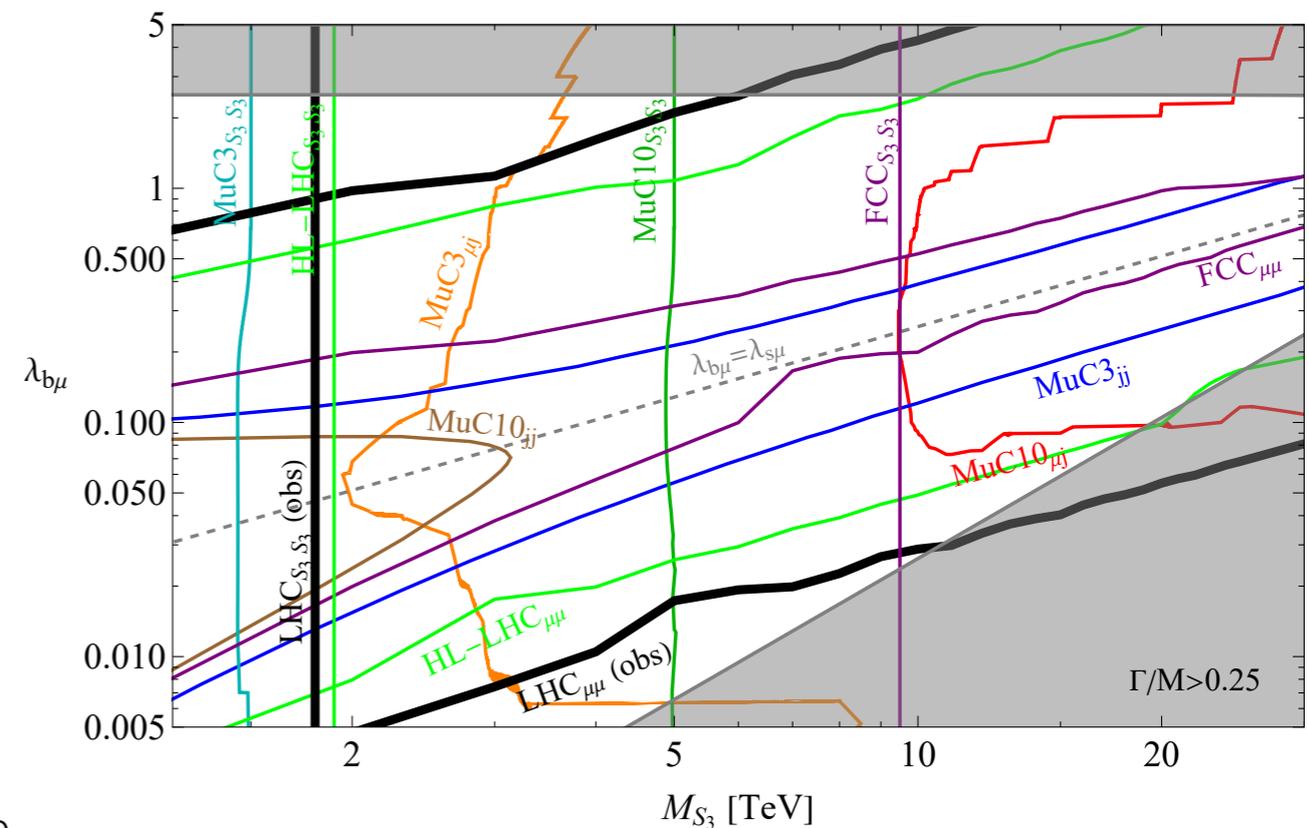
FCC-hh versus MuC

Azotov, Garosi, AG, Marzocca, Salko, Trifinopoulos; w.i.p



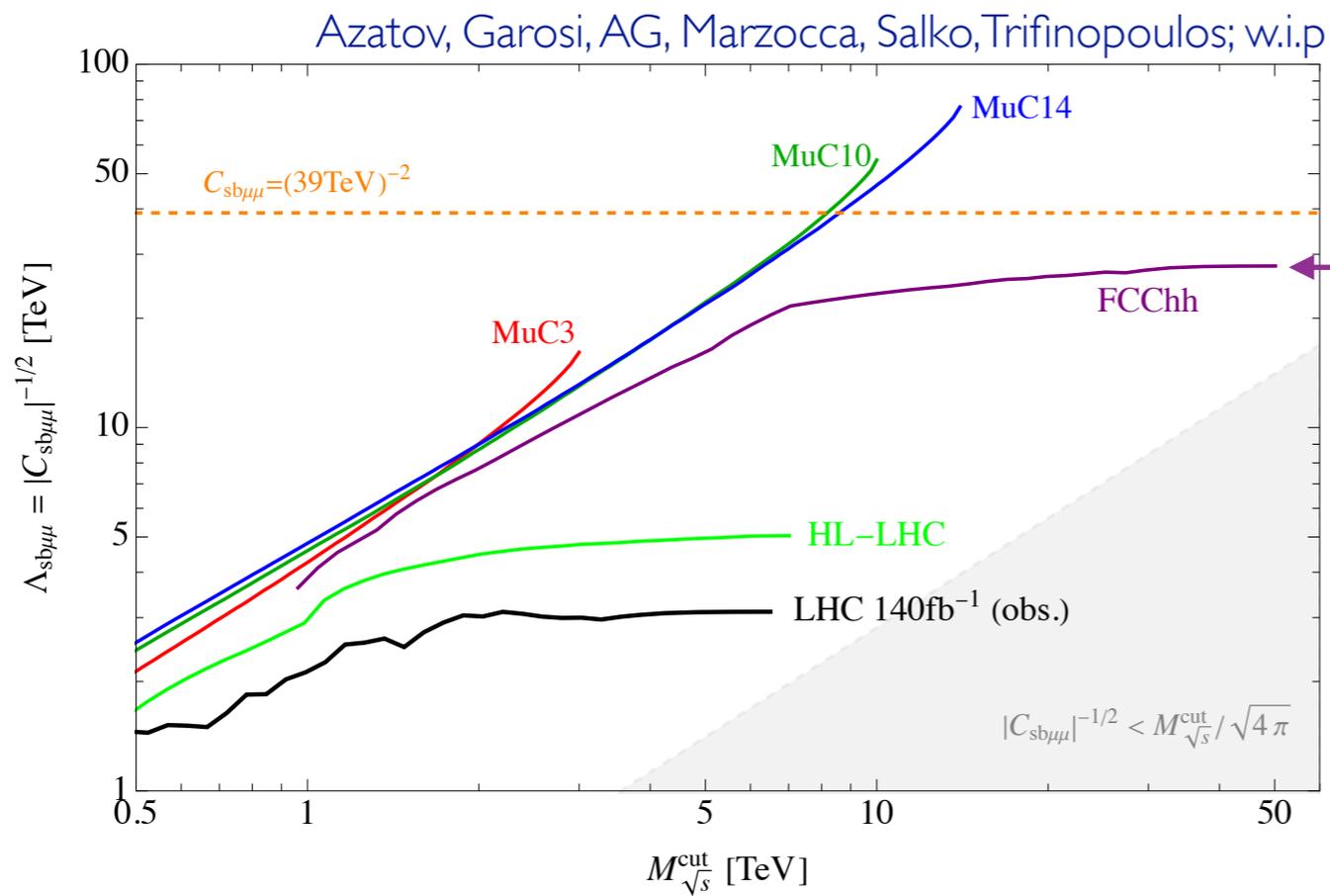
Minimalistic LQ model $>$

$<$ Minimalistic Z' model

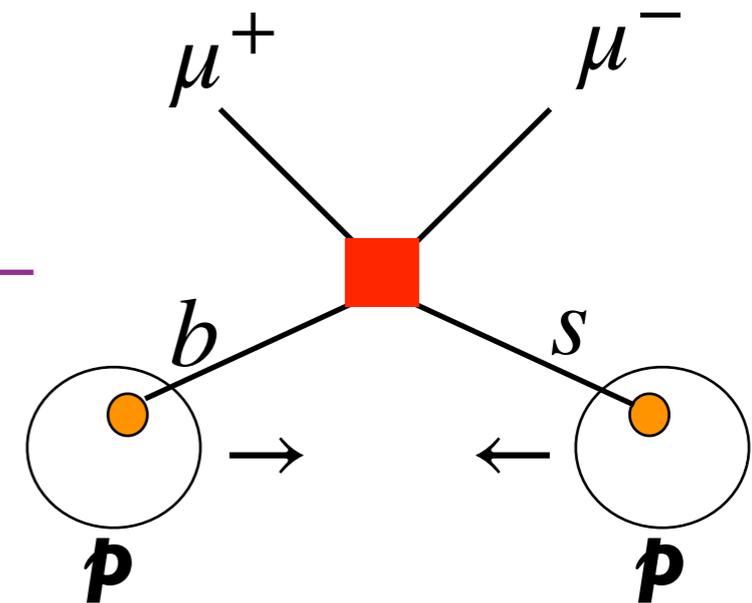


FCC-hh versus MuC

Minimalistic EFT >

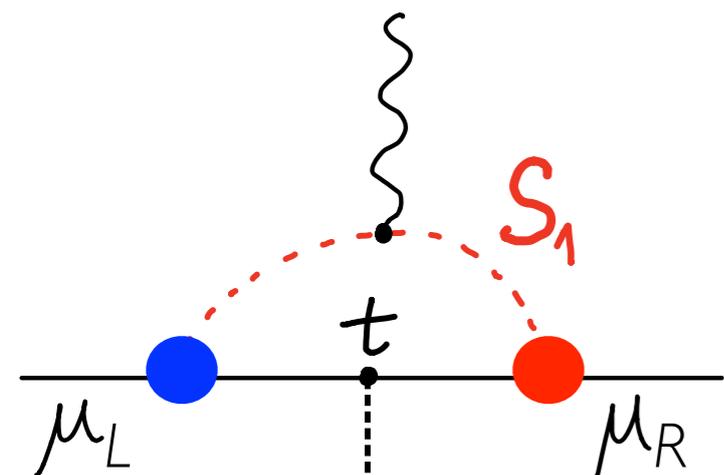


High-mass tails



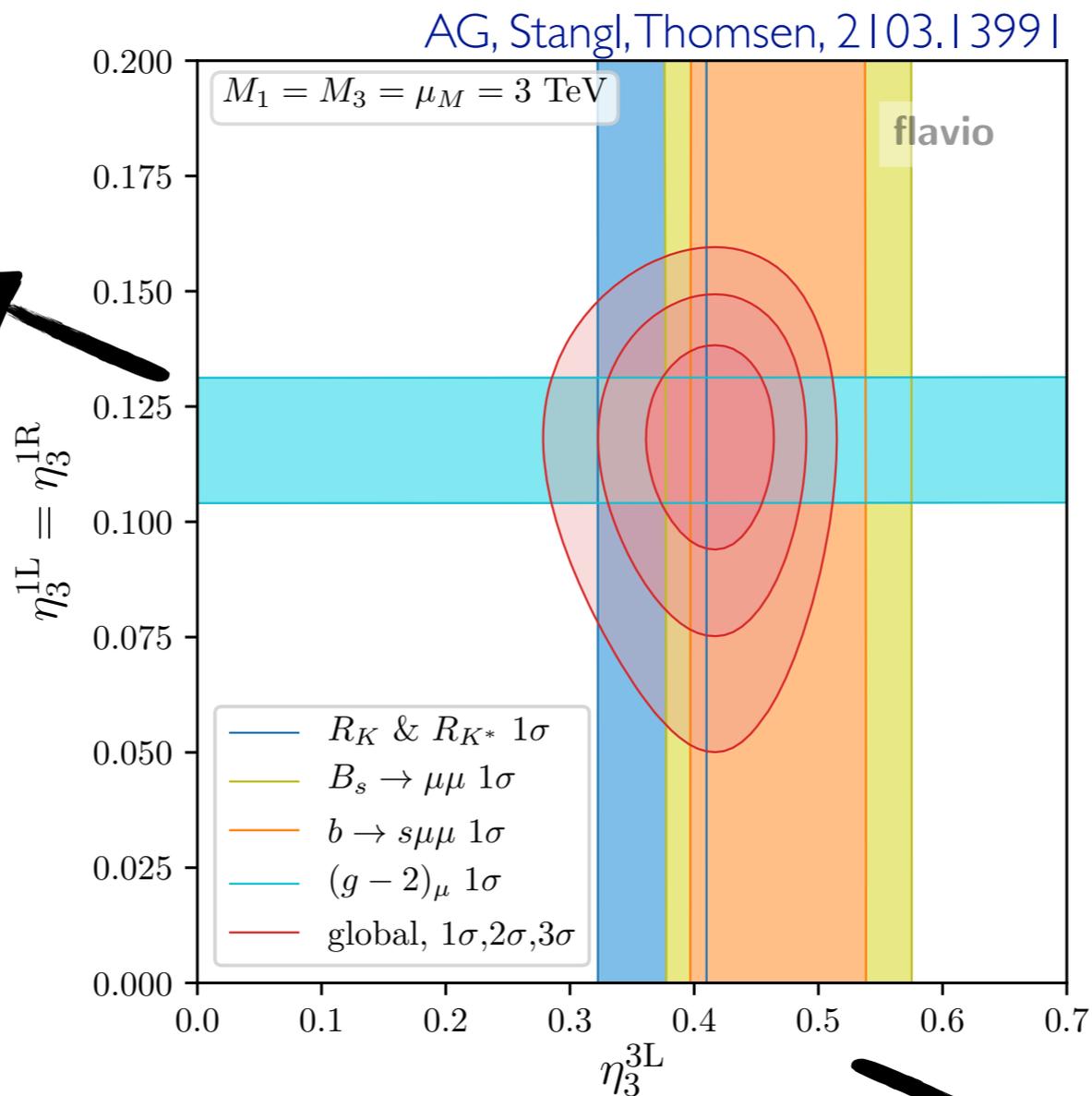
AG, Marzocca; 1704.09015

LQ model example



* m_t/m_μ enhancement

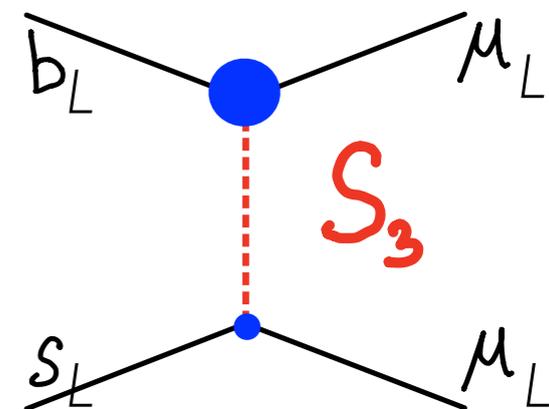
- Queiroz, Shepherd; 1403.2309,
- Dorsner, Fajfer, AG, Kamenik, Kosnik; 1603.04993,
- Coluccio Leskow, Crivellin, D'Ambrosio, Müller; 1612.06858
- Dorsner, Fajfer, Sumensari; 1910.03877
- Gherardi, Marzocca, Venturini; 2008.09548
- + many more



$$\eta_i^{3L} = (V_{td}, V_{ts}, 1) \eta_3^{3L}$$

* V-A structure

- Hiller, Schmaltz, 1408.1627,
- Dorsner, Fajfer, AG, Kamenik, Kosnik; 1603.04993,
- Buttazzo, AG, Isidori, Marzocca; 1706.07808,
- Gherardi, Marzocca, Venturini; 2008.09548
- + many more



- One-loop matching to SMEFT from 2003.12525
- 399 observables in **smelli** 1810.07698
- EW and flavor observables, LFV, LFU, magnetic moments, neutral meson mixing, semileptonic and rare B, D, K decays, etc.

A $U(1)$ story

■ Lepton non-universal gauge extensions:

Davighi, AG, Thomsen; 2202.05275
AG, Stangl, Thomsen; 2103.13991 (PLB)

- Chiral fermions: SM + $3\nu_R$

- A class of chiral anomaly-free $U(1)_X$ gauge extensions:

$$X = 3m(B - L) - n(2L_\mu - L_e - L_\tau) , \quad \text{gcd}(m, n) = 1$$

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 symmetry
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 rules:



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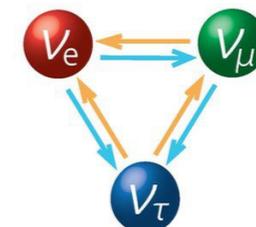


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- *LFV is observed in nature!* The PMNS is full of $\mathcal{O}(1)$ elements.



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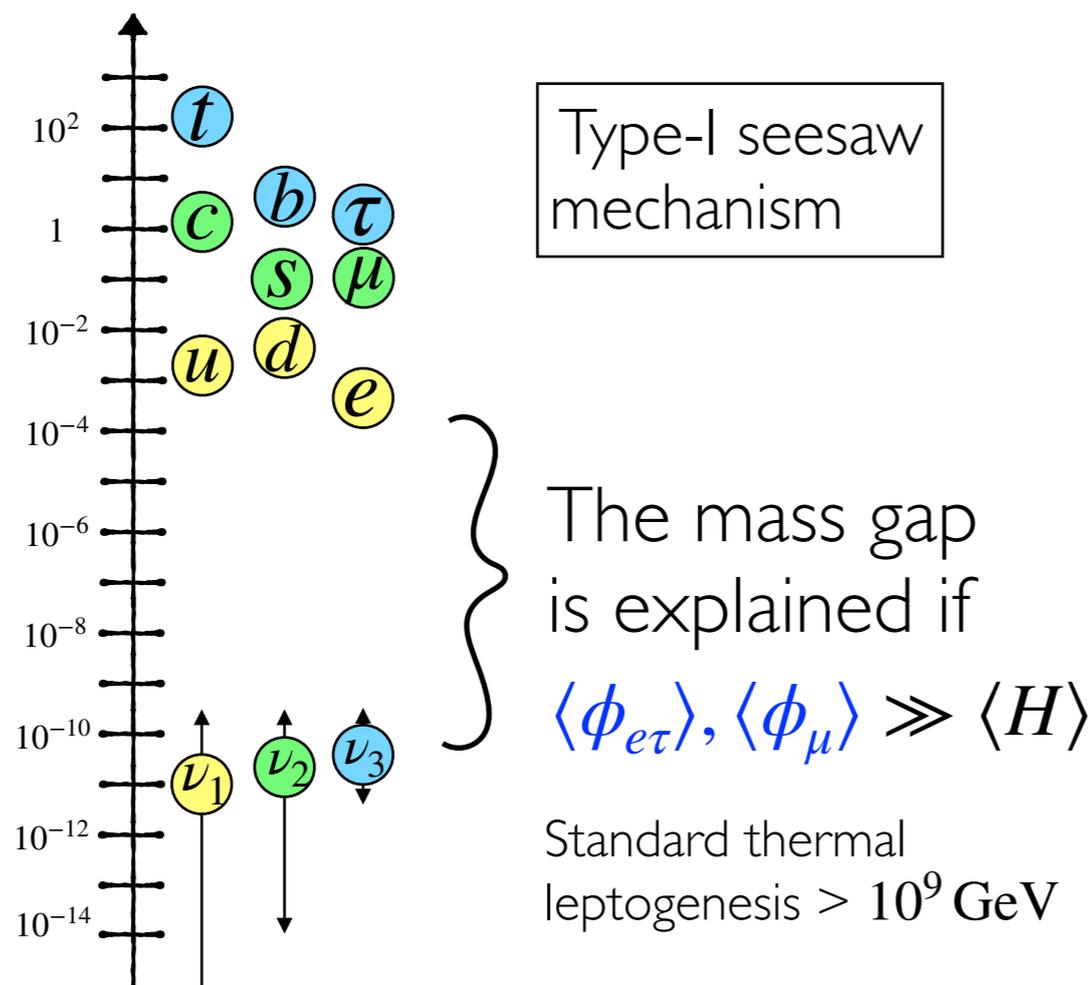
- The correct neutrino masses and mixings dictate the $U(1)_X$ breaking!
- A *dense* Majorana mass matrix needs two SM-singlet scalar fields with charges $6m - 2n$ and $6m + n$ to get a VEV $(n_i n_j \phi)$

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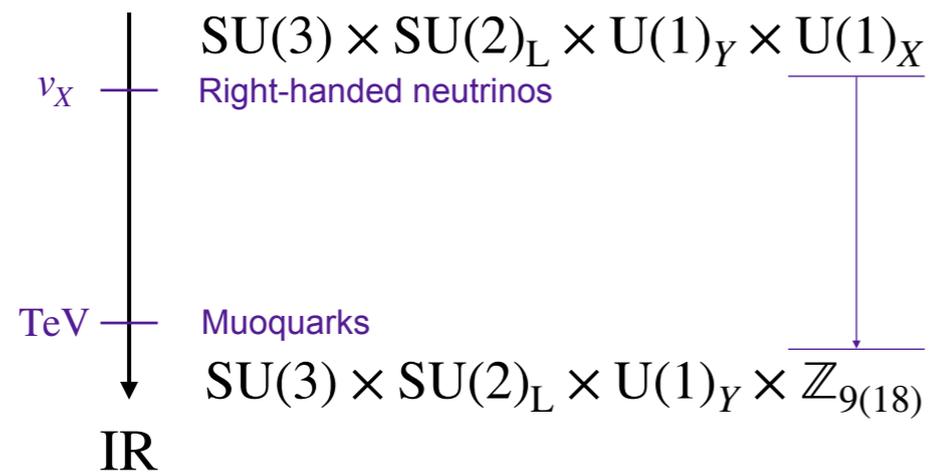
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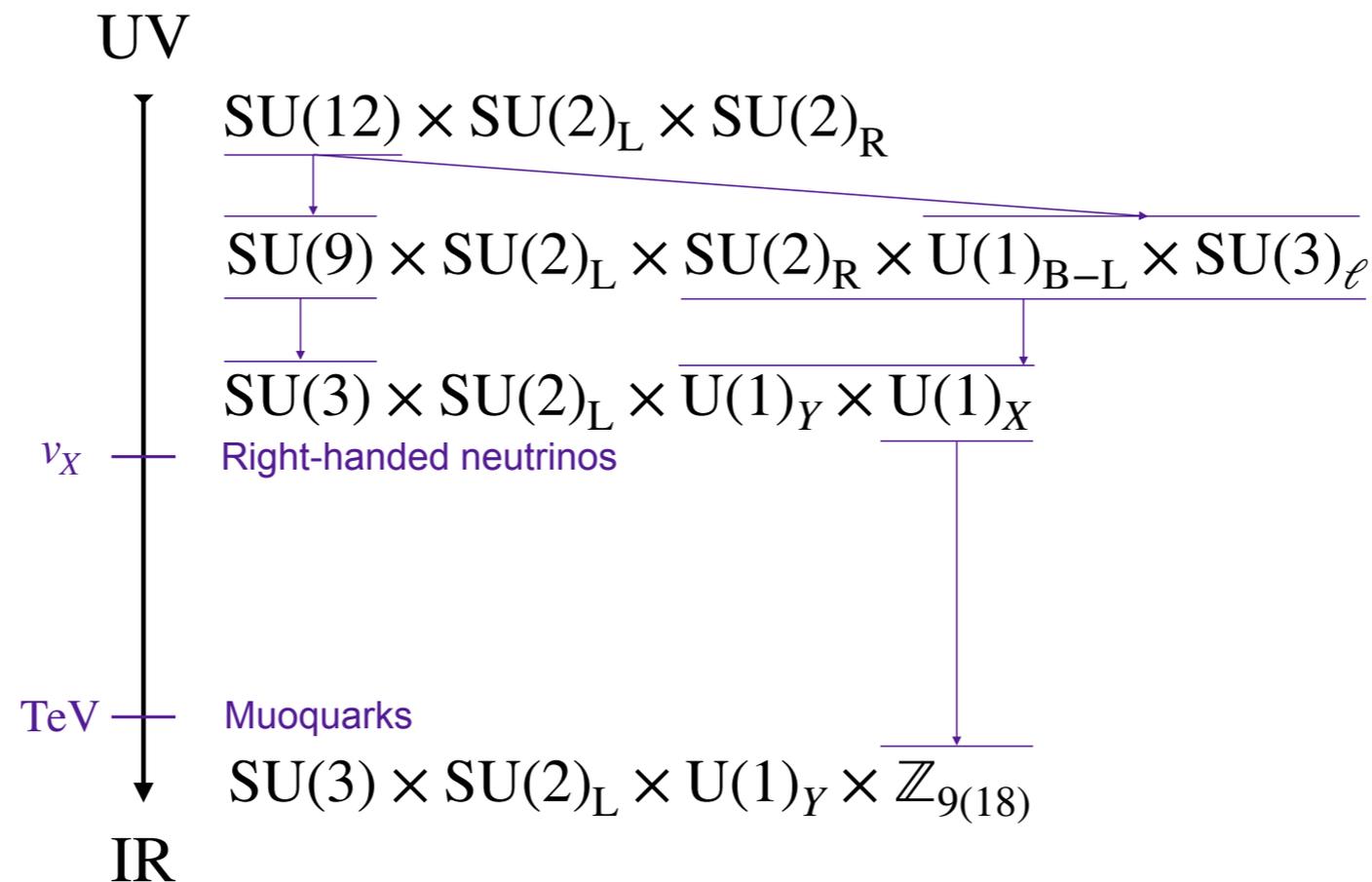
- Residual unbroken discrete subgroup $\Gamma \subset U(1)_X$ remarkably forbids proton decay to all orders in the EFT.
- Approximate $U(1)_\ell^3$ in S interactions

$$\begin{aligned}
 (m, n) &= (3a + r, 9b + 3r), \quad \text{for } r \in \{1, 2\}, \\
 (a, b) &\in \mathbb{Z}^2, \text{ and } \gcd(3a + r, b - a) = 1.
 \end{aligned}$$

A $U(1)$ story

Davighi, AG, Thomsen; 2202.05275

■ Lepton non-universal gauge extensions:



Gauge-flavour unification