

Low energy SUSY in light of current experiments

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Outline

- 1 SUSY confronted with LHC and dark matter
- 2 SUSY confronted with muon $g-2$
- 3 Can SUSY jointly explain muon $g-2$ and W -mass
- 4 Summary

1 SUSY confronted with LHC and dark matter

LHC

- LHC discovered a 125 GeV Higgs boson

A great triumph of SUSY !

SUSY predicts 5 Higgs bosons

At tree level: $m_h < m_Z |\cos 2\beta| < m_Z$

At loop-level:
$$M_t^2 = \begin{pmatrix} M_Q^2 + m_Z^2 \cos 2\beta (\frac{1}{2} - \frac{2}{3}s_W^2) + m_t^2 & m_t(A_t - \mu \cot \beta) \\ m_t(A_t - \mu \cot \beta) & M_U^2 + \frac{2}{3}m_Z^2 \cos 2\beta s_W^2 + m_t^2 \end{pmatrix}$$
$$\equiv \begin{pmatrix} m_{t_L}^2 & m_t X_t \\ m_t X_t & m_{t_R}^2 \end{pmatrix}$$

$$m_{t_{1,2}}^2 = \frac{1}{2} (m_{t_L}^2 + m_{t_R}^2) \mp \frac{1}{2} \sqrt{(m_{t_L}^2 - m_{t_R}^2)^2 + 4m_t^2 X_t^2}$$

$$M_S^2 \equiv (m_{t_1}^2 + m_{t_2}^2) / 2$$

$$m_h^2 \leq m_Z^2 + \epsilon = m_Z^2 + \frac{3m_t^4}{2\pi^2 v^2} \left[\log \frac{M_S^2}{m_t^2} + \frac{X_t^2}{M_S^2} \left(1 - \frac{X_t^2}{12M_S^2} \right) \right]$$

$$\leq 135 \text{ GeV} \quad (\text{for } M_S \leq 2\text{TeV})$$

LHC

- LHC discovered a 125 GeV Higgs boson

A great triumph of SUSY!

Require top squarks (colored sparticles) above TeV

- LHC direct search not seen any sparticles

Push colored sparticles above TeV

LHC

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Push colored sparticles above TeV

Consistent

DM

lightest neutralino $\tilde{\chi}_1^0$ $\left\{ \begin{array}{l} \text{weak coupling } g \sim 0.5 \\ \text{massive } g \sim 500 \text{ GeV} \end{array} \right.$

→ WIMP

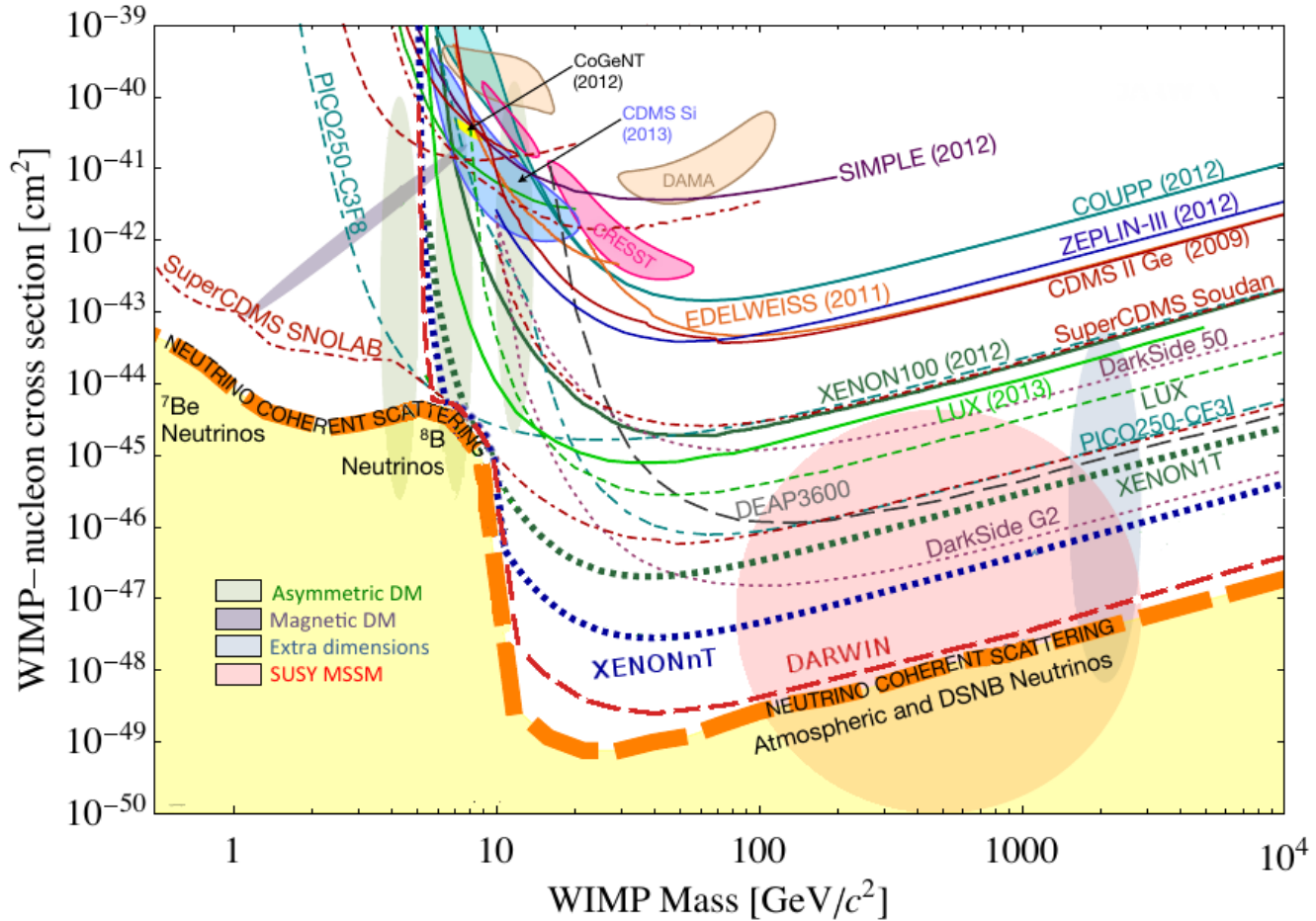
WIMP miracle for dark matter

$$\Omega_{DM} h^2 \equiv \frac{\rho_{DM}}{\rho_{tot}} h^2 \simeq \frac{3 \times 10^{-27} \text{cm}^3 \text{s}^{-1}}{\langle \sigma v \rangle} \quad 0.1199 \pm 0.0027$$

$$\langle \sigma v \rangle \sim \frac{g^4}{16\pi} \frac{1}{M^2} \simeq (6 \times 10^{-26} \text{cm}^3 \text{s}^{-1}) \left(\frac{g}{0.5} \right)^4 \left(\frac{500 \text{ GeV}}{M} \right)^2$$

DM

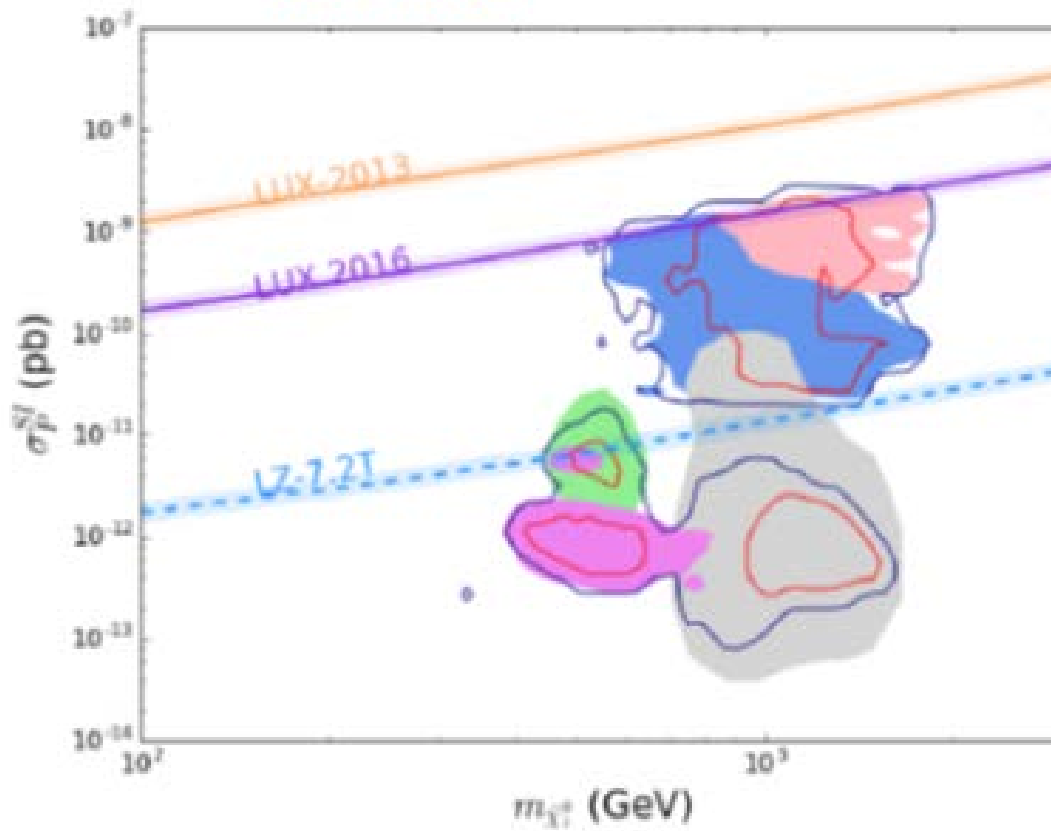
MSSM



DM

Run-1 + Run-2
LUX-2016

1612.02296
Han, Hikasa, Wu, Yang, Zhang



CMSSM
mSUGRA

DM

SUSY neutralino as dark matter is ok !

- **Relic density is ok**
- **Direct detection limits satisfied**

2 SUSY confronted with muon g-2

Muon g-2 is a probe to new physics

$$\delta a_\ell \propto \frac{\alpha}{\pi} \frac{m_\ell^2}{M^2} \quad (M \gg m_\ell)$$

$$(m_\mu/m_e)^2 \simeq 4 \times 10^4$$

muon g-2 is a best probe to NP
(tau lepton is too short-lived)

$$\tau_e = \infty$$

$$\tau_\mu = 2.197 \times 10^{-6} \text{ s}$$

$$\tau_\tau = 2.906 \times 10^{-13} \text{ s}$$

Recent measurement of muon g-2

$$a_{\mu}^{\text{QED}} = 116\,584\,718.9(1) \times 10^{-11}$$

$$a_{\mu}^{\text{EW}} = 153.6(1.0) \times 10^{-11}$$

$$a_{\mu}^{\text{HVP, LO}} = 6931(40) \times 10^{-11}$$

$$a_{\mu}^{\text{HVP, NLO}} = -98.3(7) \times 10^{-11}$$

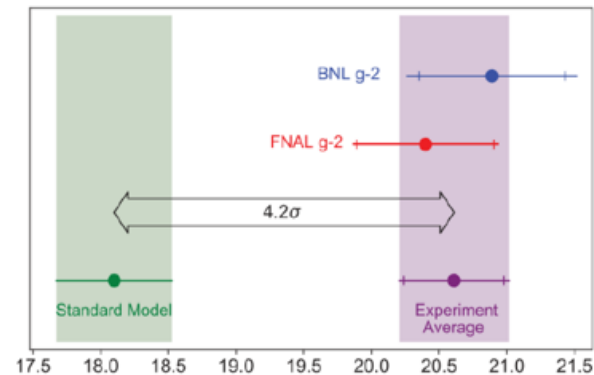
$$a_{\mu}^{\text{HVP, NNLO}} = 12.4(1) \times 10^{-11}$$

$$a_{\mu}^{\text{HLBL}} + a_{\mu}^{\text{HLBL, NLO}} = 92(18) \times 10^{-11}$$

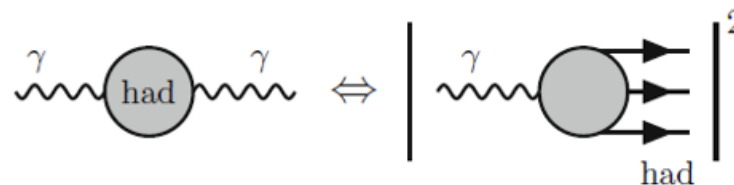
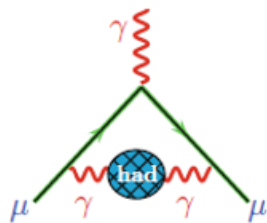
$$a_{\mu}^{\text{SM}} = 116\,591\,810(43) \times 10^{-11}$$

$$a_{\mu}^{\text{Exp}} = 116\,592\,061(41) \times 10^{-11}$$

$$a_{\mu}^{\text{Exp}} - a_{\mu}^{\text{SM}} = 251(59) \times 10^{-11}$$



Theory uncertainty mainly from HVP



Recent measurement of muon $g-2$

Naturalness and the muon magnetic moment

2021年6月11日 上午9:50

40m

Zoom

报告人

Nima Arkani-Hamed (IAS)

M_j Take

* $\sim 10\%$ chance it's new phys.
(Much more plausible than other anom.!) \downarrow

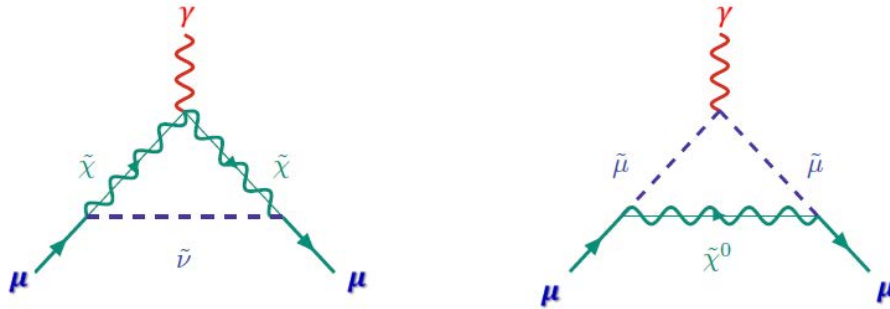
* Lattice QCD groups should converge
on $\sim 1-2$ year timescale

* ... But not easy to mess with disp.
relation results!

* FNAL should reduce error bars by $\sim \times 4$

* JPARC indep exp. by ~ 2025

SUSY can explain muon g-2, **but** not so easy

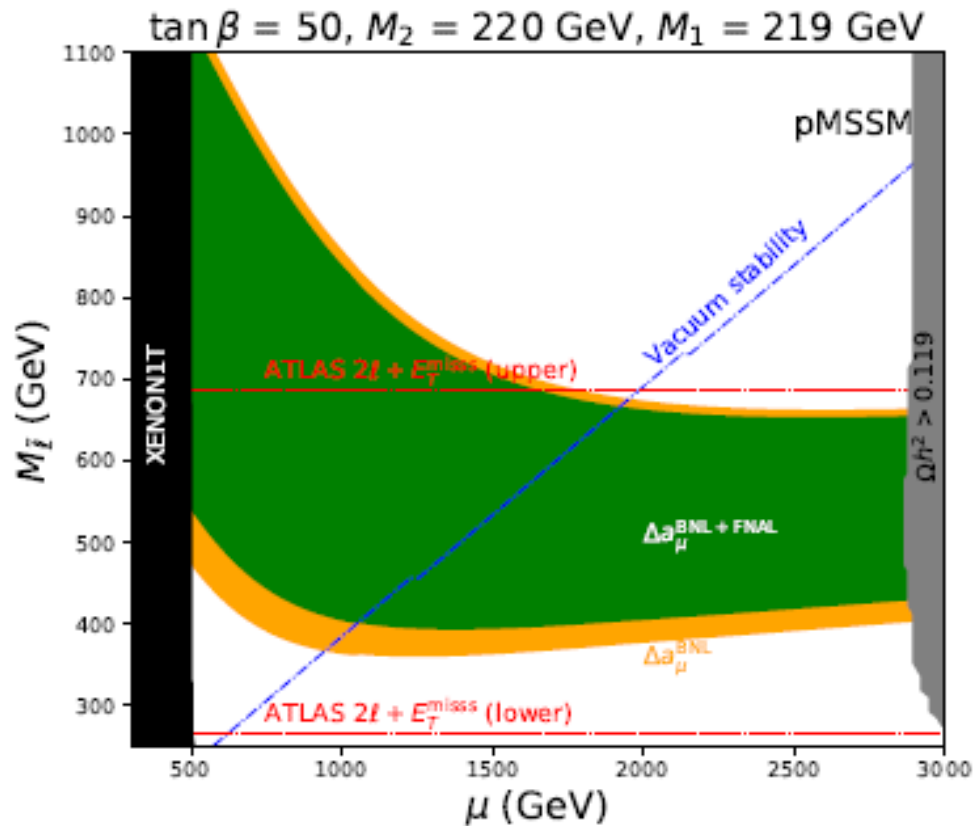


$$\delta a_{\mu}^{\text{SUSY}} = 14 \tan \beta \left(\frac{100 \text{ GeV}}{M_{\text{SUSY}}} \right)^2 10^{-10}$$

See, e. g.,
Moroi, hep-ph/9512396

Require light slepton, light electroweakino
(uncolored sparticles are light)

**MSSM:
g-2 is OK**



2104. 03262

Wang, Wu, Xiao, Yang, Zhang

Figure 2. FNAL+BNL and BNL Δa_μ constraints for the BW scenario in the pMSSM. The orange and dark green regions can explain the BNL and the FNAL+BNL Δa_μ measurements at 2σ CL. The black region is excluded by Xenon-1T at 90% CL, while in the brown region the LSP is not bino-like neutralino. The areas between the two ATLAS $2\ell + E_T^{\text{miss}}$ limits (red dash lines) are excluded by 13 TeV LHC searches for slepton-pair production at 95% CL. The regions on the right of blue dash lines spoil stability of the electroweak vacuum.

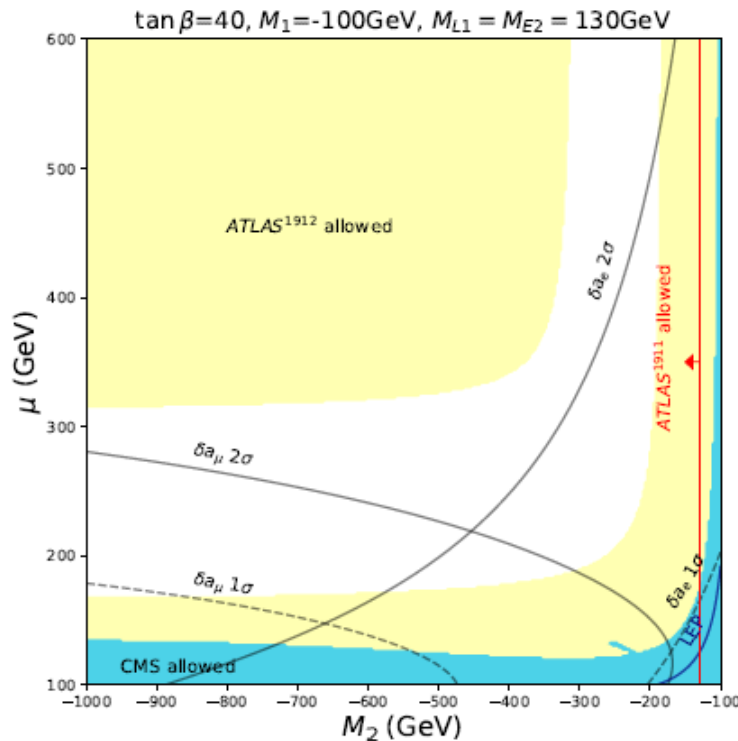
MSSM: muon g-2 and electron g-2 simultaneously OK !

$$\Delta a_e^{\text{Exp-SM}} = a_e^{\text{Exp}} - a_e^{\text{SM}}(\text{Cs}) = (-8.8 \pm 3.6) \times 10^{-13}$$

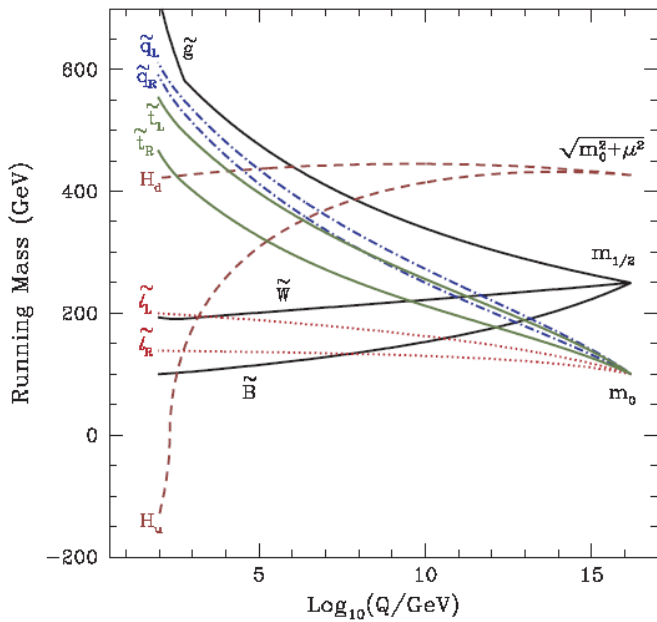
2107.04962

Li, Xiao, Yang

from measurement of fine-structure constant using ^{133}Cs atoms at Berkeley is 2.4σ below SM prediction



CMSSM/mSUGRA, GMSB, AMSB: g-2 not OK



125 GeV Higgs \rightarrow heavy top squarks

$\rightarrow m_0$ is large

\rightarrow heavy sleptons

\rightarrow cannot explain g-2

GMSB/AMSB: $g-2$ not OK

See, e. g.,

Baer, Barger, Mustafayev, 1202.4038

To give a 125 GeV Higgs, SUSY particles are above 10 TeV

→ $g-2$ cannot be explained

GMSB/AMSB: $g-2$ not OK

Extend GMSB:

For example,

See, e.g.,

Kang, Li, Liu, Tong, Yang, 1203.2336

A Heavy SM-like Higgs and a Light Stop from Yukawa-Deflected
Gauge Mediation

$$W_1 = \lambda_u S \bar{\Phi}_L H_u + \lambda_d \bar{S} \Phi_L H_d,$$

can have large A_t , giving 125 GeV Higgs without very heavy stops

→ $g-2$ can be explained

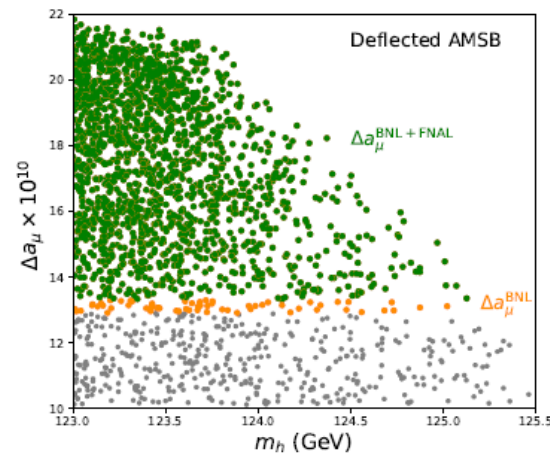
GMSB/AMSB: $g-2$ not OK

Extend AMSB:

For example,

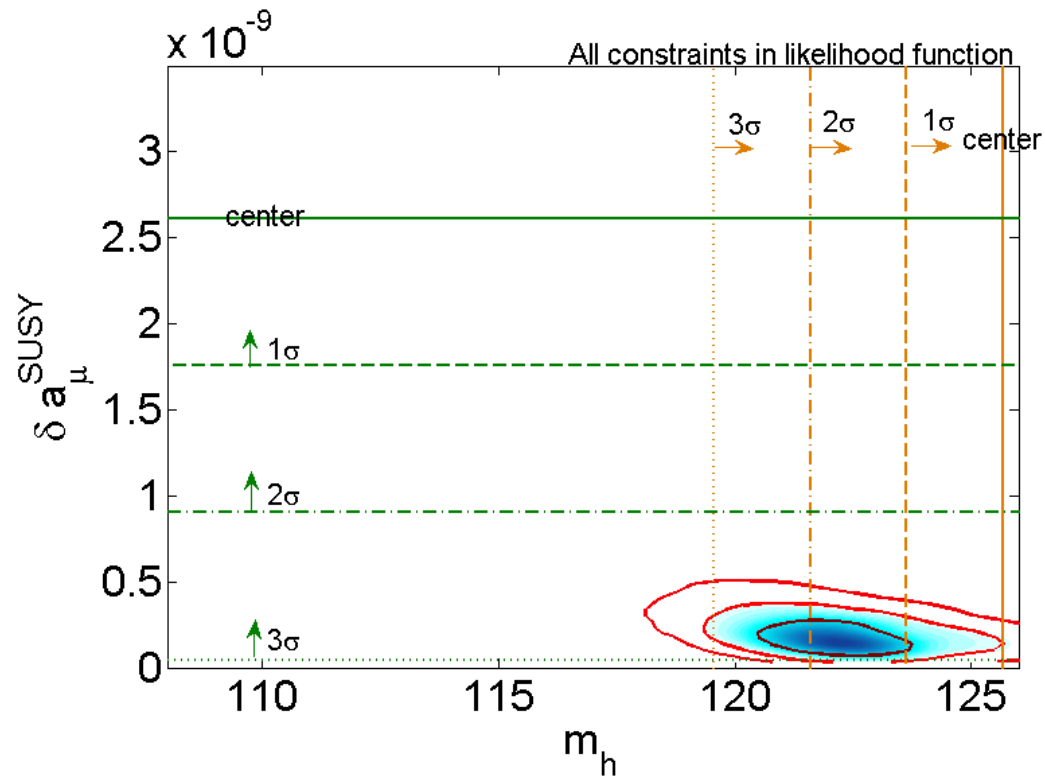
Wang, Wang, Yang, Zhang, 1505.02785

Heavy colored SUSY partners from deflected anomaly mediation



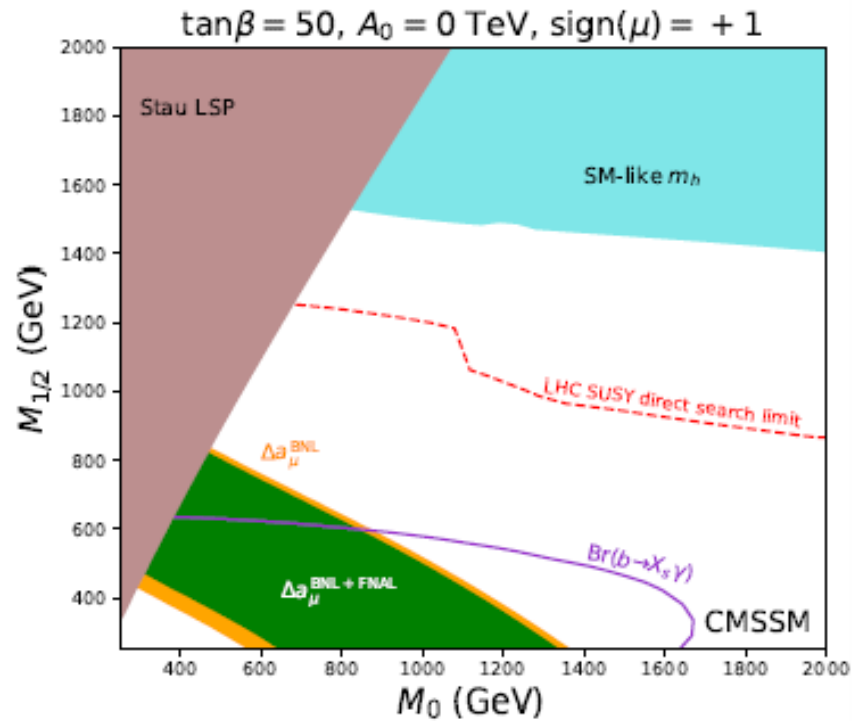
→ $g-2$ can be explained

CMSSM/mSUGRA: $g-2$ not OK



Han, Hikasa, Wu, Yang, Zhang,
1612.02296

CMSSM/mSUGRA: $g-2$ not OK



Wang, Wu, Xiao, Yang, Zhang,
2104.03262

CMSSM/mSUGRA: g-2 not OK

Extend CMSSM/mSUGRA:

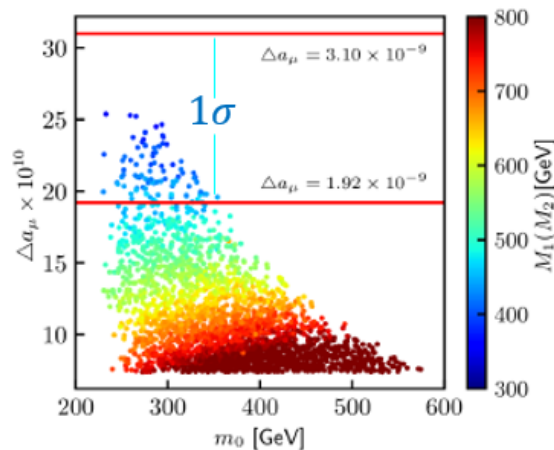
For example,

Reconcile muon g-2 anomaly with LHC data in
SUGRA with generalized gravity mediation

Wang, Wang, Yang, 1504.00505

Wang, Wang, Yang, Zhu, 1808.10851

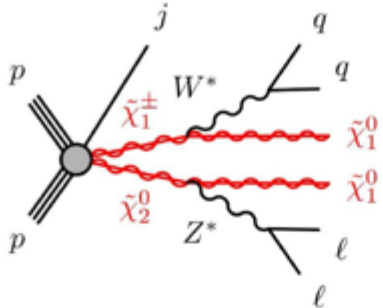
Glينو-SUGRA scenarios in light of FNAL muon g-2



Akula, Nath, 1304.5526

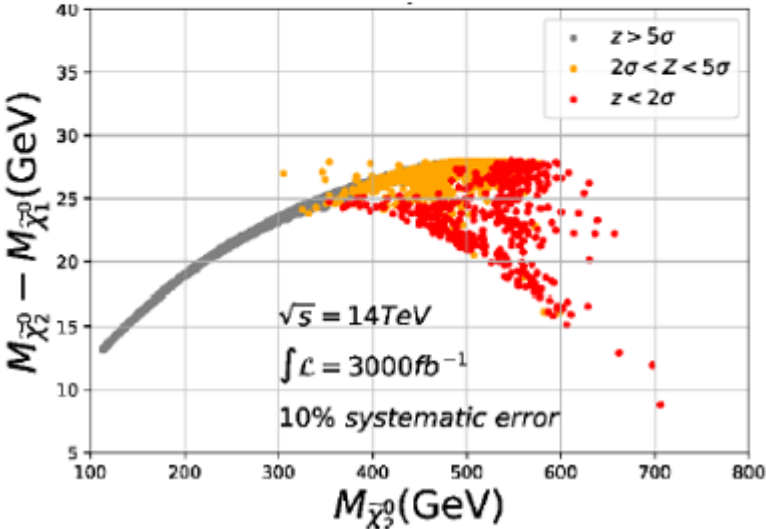
Li, Liu, Wang, Yang, Zhang, 2106.04466

Implication for MSSM search at LHC



1909.07792

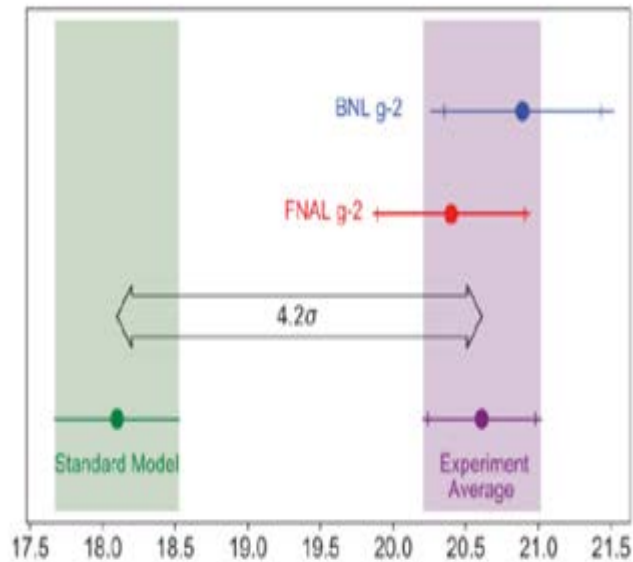
Abdughani, Hikasa, Wu, Yang, Zhao



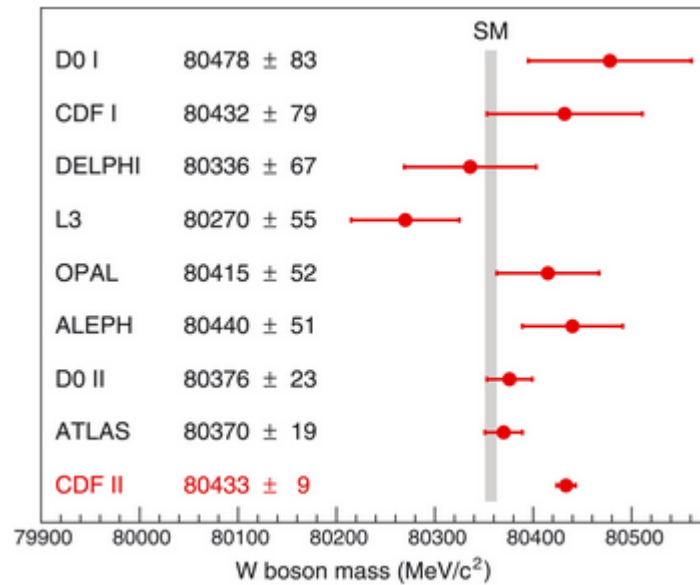
3 Can SUSY jointly explain muon g-2 and W-mass ?

JMY, Y. Zhang, arXiv: 2204.04202

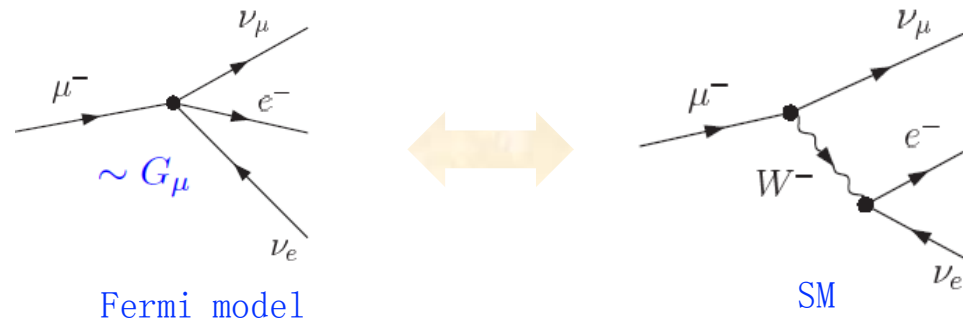
muon g-2



W-mass



W-mass:



$$M_W^2 \left(1 - \frac{M_W^2}{M_Z^2} \right) = \frac{\pi\alpha}{\sqrt{2}G_\mu} (1 + \Delta r)$$

\updownarrow
 loop corrections

$$\Delta r = \Delta\alpha - \frac{\cos^2 \theta_W}{\sin^2 \theta_W} \Delta\rho + \dots$$

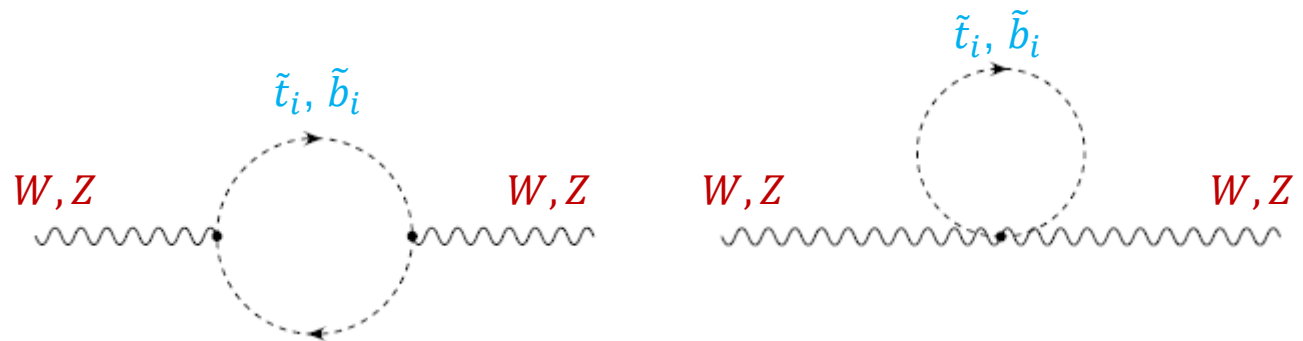
$$\delta M_W \simeq \frac{M_W}{2} \frac{\cos^2 \theta_W}{\cos^2 \theta_W - \sin^2 \theta_W} \Delta\rho$$

$$\Delta\rho = \frac{\Sigma^Z(0)}{M_Z^2} - \frac{\Sigma^W(0)}{M_W^2}$$

W-mass:

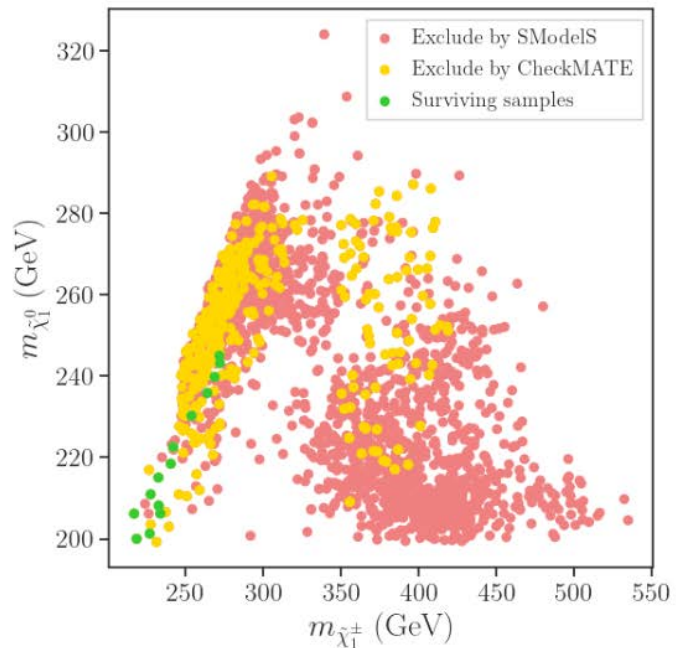
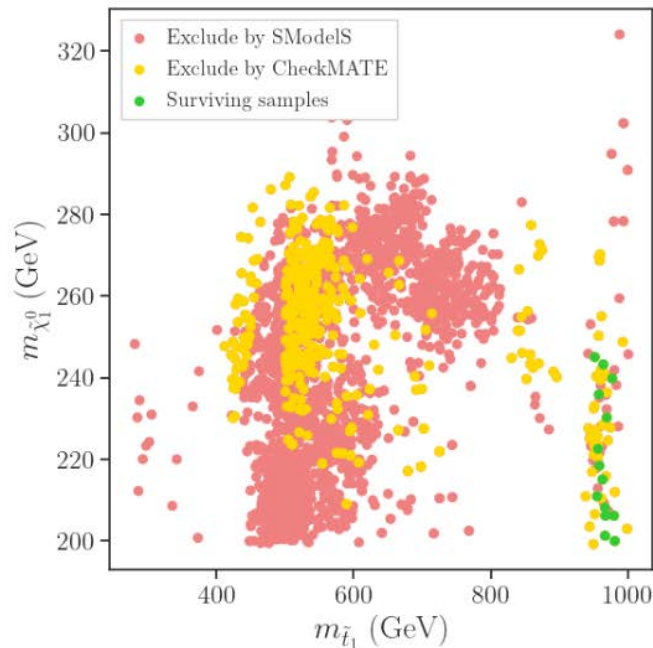
$$\delta M_W \simeq \frac{M_W}{2} \frac{\cos^2 \theta_W}{\cos^2 \theta_W - \sin^2 \theta_W} \Delta\rho$$

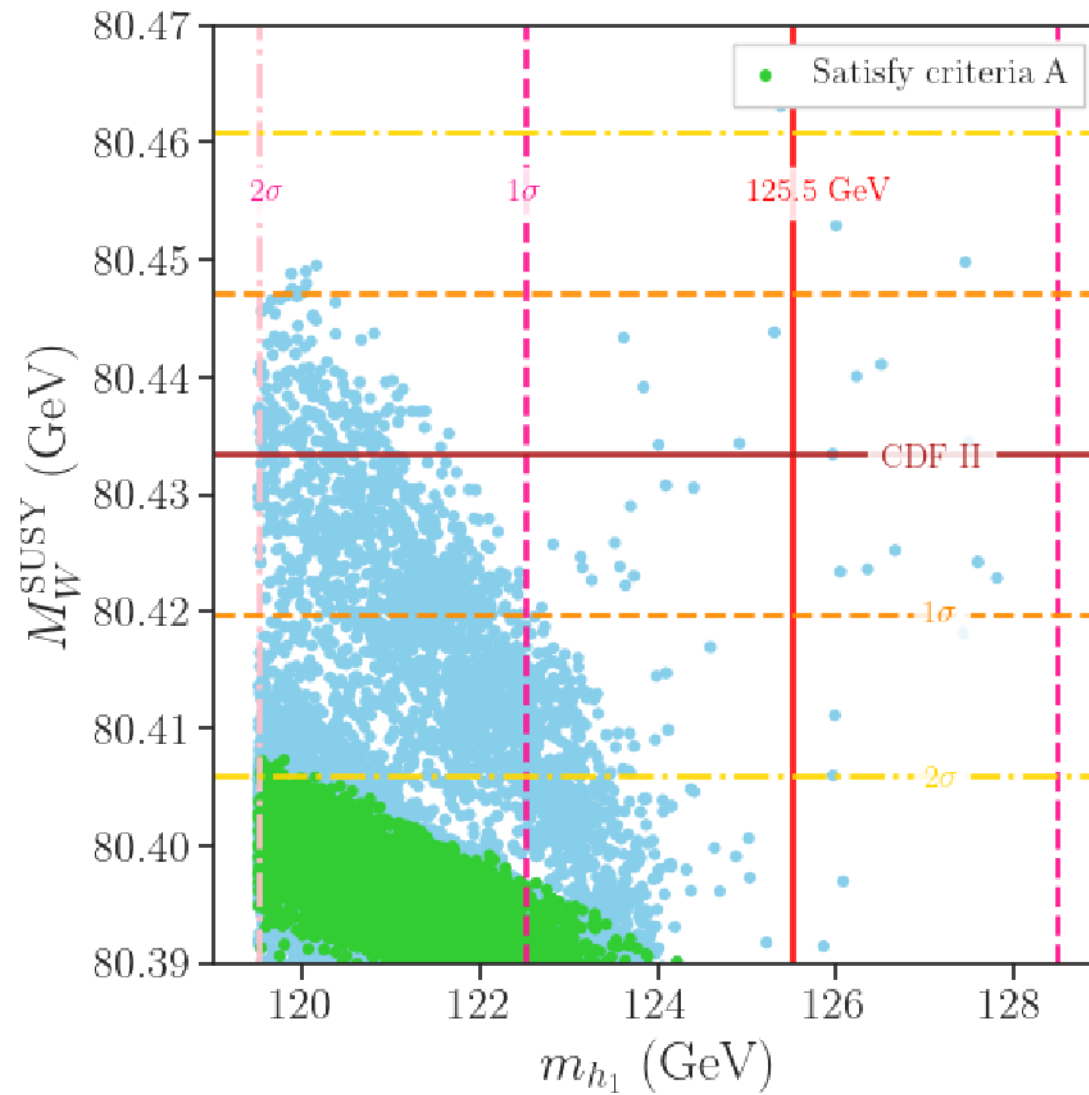
$$\Delta\rho = \frac{\Sigma^Z(0)}{M_Z^2} - \frac{\Sigma^W(0)}{M_W^2}$$



$$\begin{aligned} \Delta\rho_0^{\text{SUSY}} = \frac{3G_F}{8\sqrt{2}\pi^2} [& -\sin^2 \theta_{\tilde{t}} \cos^2 \theta_{\tilde{t}} F_0(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2) - \sin^2 \theta_{\tilde{b}} \cos^2 \theta_{\tilde{b}} F_0(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2) \\ & + \cos^2 \theta_{\tilde{t}} \cos^2 \theta_{\tilde{b}} F_0(m_{\tilde{t}_1}^2, m_{\tilde{b}_1}^2) + \cos^2 \theta_{\tilde{t}} \cos^2 \theta_{\tilde{b}} F_0(m_{\tilde{t}_1}^2, m_{\tilde{b}_2}^2) \\ & + \sin^2 \theta_{\tilde{t}} \cos^2 \theta_{\tilde{b}} F_0(m_{\tilde{t}_2}^2, m_{\tilde{b}_1}^2) + \sin^2 \theta_{\tilde{t}} \cos^2 \theta_{\tilde{b}} F_0(m_{\tilde{t}_2}^2, m_{\tilde{b}_2}^2)] \end{aligned}$$

- In the parameter space allowed by current experimental constraints from colliders and dark matter detections, MSSM can simultaneously explain both measurements at 2σ level.
- The favored parameter space, characterized by a compressed spectrum between (bino, wino, stau), with top-squark around 1 TeV.





4 Summary

SUSY Status (in light of current experiments)

- Fancy models:

GMSB/AMSB: can give 125 GeV Higgs, but with very heavy stop (fine-tuning)

CMSSM/mSUGRA: can give 125 GeV Higgs; but cannot explain muon $g-2$

- Low energy effective models:

MSSM: can fit all data well, but suffer from little fine-tuning

NMSSM:

- Weird-smart models:

Split-SUSY: no problem (give up naturalness)

Stealth SUSY: no problem (can always escape detections)

Compressed SUSY: no problem (can escape detection at LHC)

4 Summary

SUSY Status (in light of current experiments)

Then, what is the problem of SUSY ?

- LHC direct search not seen any sparticles
Push colored sparticles above TeV (stop mass $M_{SUSY} > \text{TeV}$)
- Quadratic divergence cancel, log divergence still exist

$$\Delta m_H^2 \sim (M_{SUSY}^2 - M_{SM}^2) \frac{\lambda_f^2}{16\pi^2} \ln \left(\frac{\Lambda}{M_{SUSY}} \right)$$

$$m_H^2 = m_0^2 - \Delta m_H^2$$

125 GeV bare

little fine-tuning
problem

SUSY is natural if $M_{SUSY} \sim \mathcal{O}(1) \text{ TeV}$

4 Summary

- SUSY confronted with LHC: ok
- SUSY confronted with DM: ok
- Can SUSY explain muon $g-2$ and W -mass ?

CMSSM, mSUGRA, GMSB, AMSB: need to be extended

MSSM: ok

- light electroweakinos
- light sleptons
- light stop

Most hopefully accessible at LHC

Thanks for your attention !