

# Vector-Boson Scattering at the LHC – recent theory developments

Barbara Jäger  
University of Tübingen

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# outline

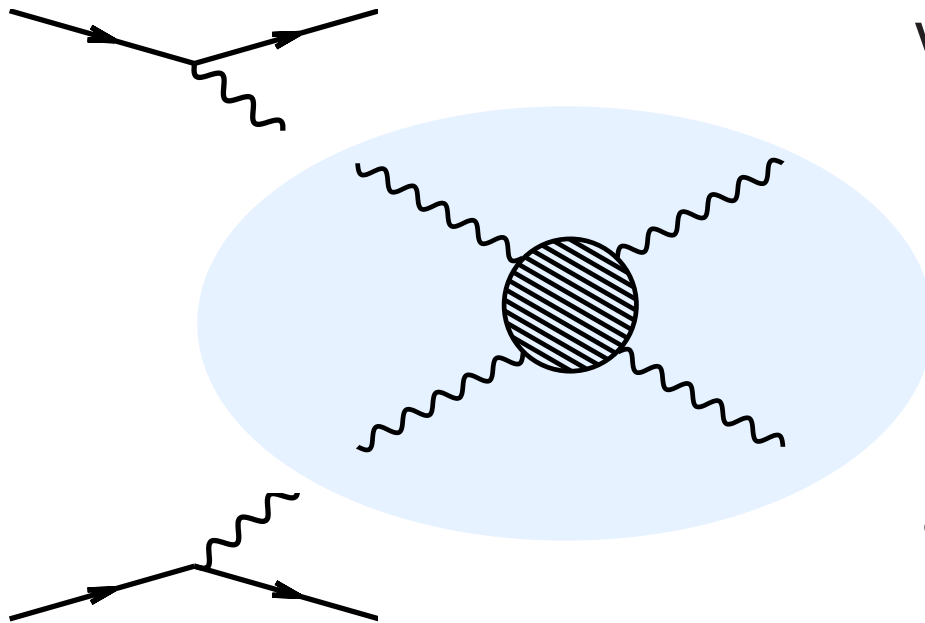
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- ◆ definition of the VBS signature
- ◆ precision calculations for VBS processes
- ◆ matching to parton showers
- ◆ tools
- ◆ polarization observables

# vector boson scattering: $VV \rightarrow VV$

weak boson and Higgs sector intimately linked

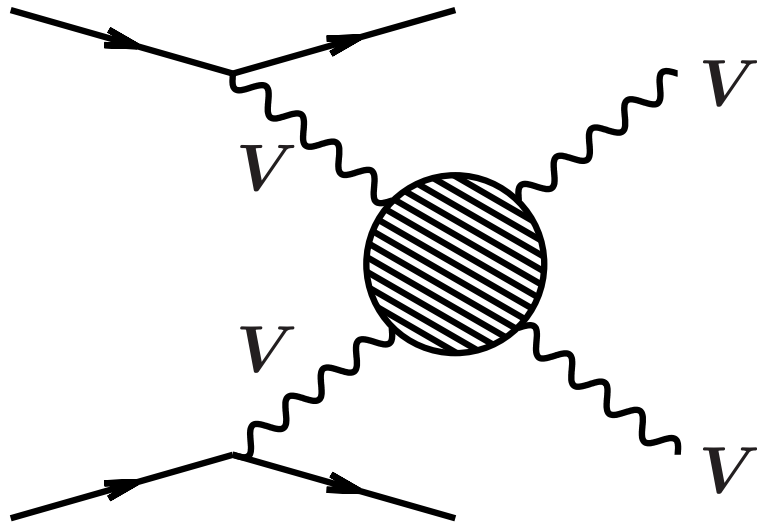
electroweak symmetry breaking: Higgs mechanism gives masses to  $W^\pm$ ,  $Z$  ( $\rightarrow$  longitudinal modes)



vector-boson scattering processes are extremely **sensitive to new interactions in the gauge boson sector**

👉 search for new resonances, anomalous (quartic) gauge-boson couplings, ...

# vector boson scattering at colliders: $pp \rightarrow VV + 2 \text{ jets}$



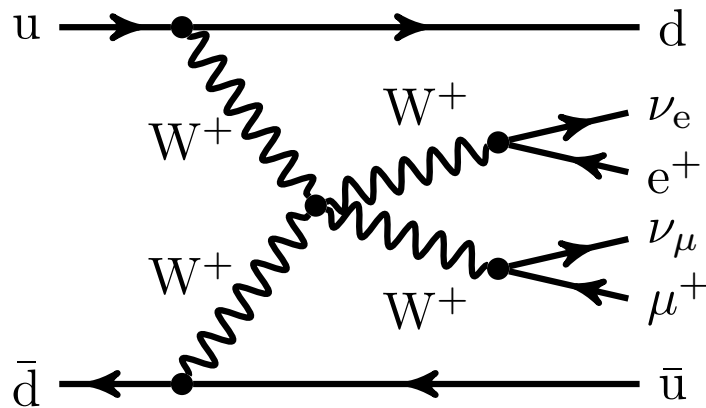
make use of unique VBS topology:

- ◆ jets in forward regions of detector,
- ◆ decay products of weak bosons at central rapidities

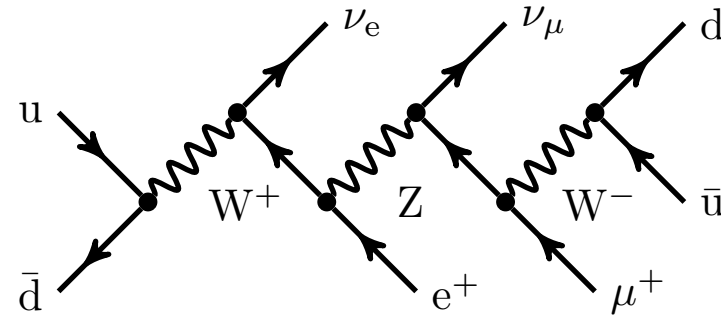
experiment: don't observe gauge bosons of the  $VVjj$  final state, but their (hadronic or) leptonic decay products

☞ need predictions for final state with 4 leptons and 2 jets

# the $W^+W^+$ channel: $pp \rightarrow \mu^+\nu_\mu e^+\nu_e jj$ at $\mathcal{O}(\alpha^6)$



$t$ -channel



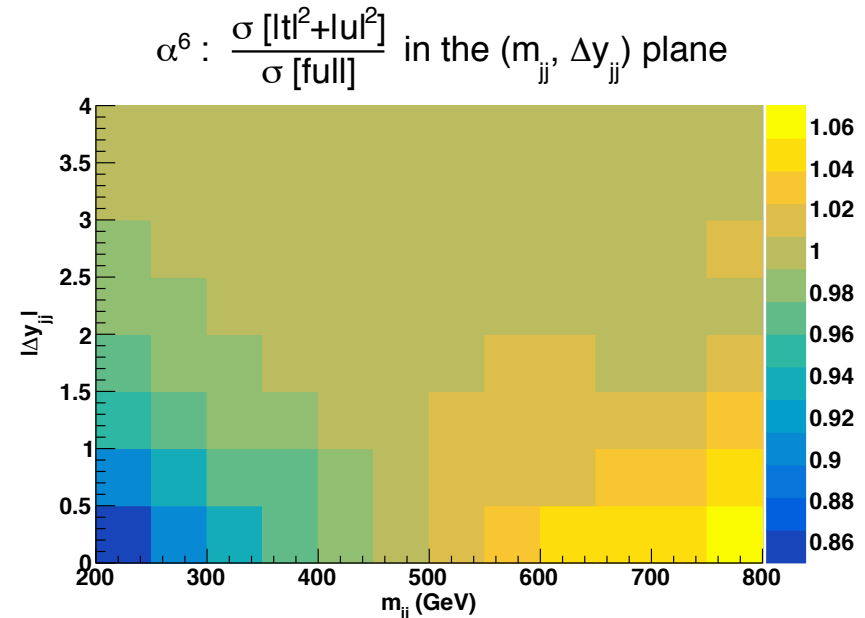
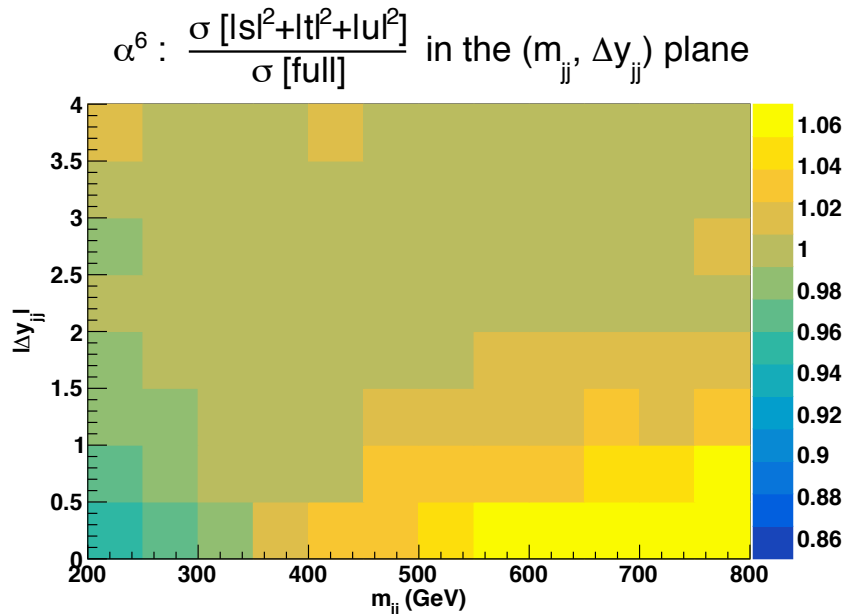
$s$ -channel

dominant in VBS  
fiducial region

small when VBS cuts  
are applied

# impact of VBS approximation

“VBS approximation”: only  $t$ - and  $u$ -channel contributions,  
no  $s$ -channel, no  $u \cdot t$  interference

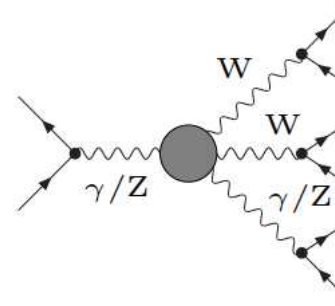
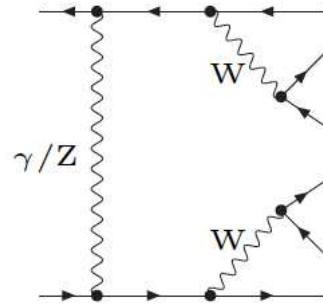
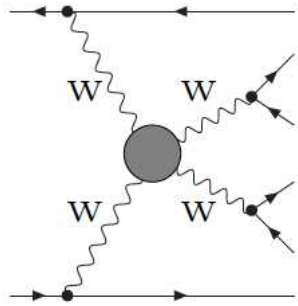


Ballestrero et al. (2018)

typical VBS search region ( $m_{jj} > 500$  GeV,  $|\Delta y_{jj}| > 2.5$ ):  
VBS approximation works well (better than 5%)

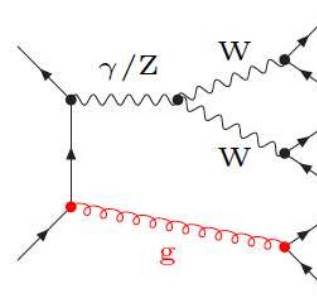
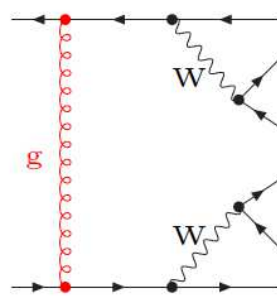
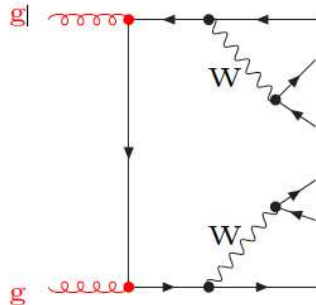
# the various contributions to the VVjj final state

EW channels:



$$|\mathcal{M}_{EW}|^2 \propto \alpha^6$$

QCD channels:



$$|\mathcal{M}_{QCD}|^2 \propto \alpha_s^2 \alpha^4$$

interference between QCD and EW channels:

possible, but suppressed



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# fixed-order calculations: state of the art

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- ◆ **NLO-QCD corrections** to 4 lepton+2 jet final state at  $\mathcal{O}(\alpha^6\alpha_s)$ , using the VBS approximation:  
*Bozzi, Oleari, Zeppenfeld, B. J. (2006-2009) → VBFNLO*  
*Denner, Hosekova, Kallweit (2012)*
- ◆ **NLO-QCD corrections** to 4 lepton+2 jet final state at  $\mathcal{O}(\alpha^4\alpha_s^3)$ : (QCD-induced production = irreducible background to VBS signal)  
*Melia, Melnikov, Röntsch, Zanderighi (2010-2011)*  
*Greiner, Heinrich, Mastrolia, Ossola, Reiter, Tramontano (2012)*  
*Campanario, Kerner, Ninh, Zeppenfeld (2013-14) → VBFNLO*
- ◆ **NLO-QCD and EW corrections** to 4 lepton+2 jet final state:  
*Biedermann, Dittmaier, Denner, Maierhöfer, Pellen, Schwan (2016-19)*  
*Denner, Franken, Pellen, Schmidt (2020-22)*

# EW corrections: why worry?

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- ◆ LHC-2 was operating at 13 TeV
  - energy range sensitive to EW effects;  
EW corrections can reach some 10%
- ◆ integrated LHC luminosity will reach several  $100 \text{ fb}^{-1}$ 
  - many measurements at few-percent level  
(= typical size of EW corrections)
- ◆ planned high-precision measurements:
  - EW parameters, (anomalous) couplings,...
  - EW corrections are crucial ingredient

# large electroweak corrections in VBS

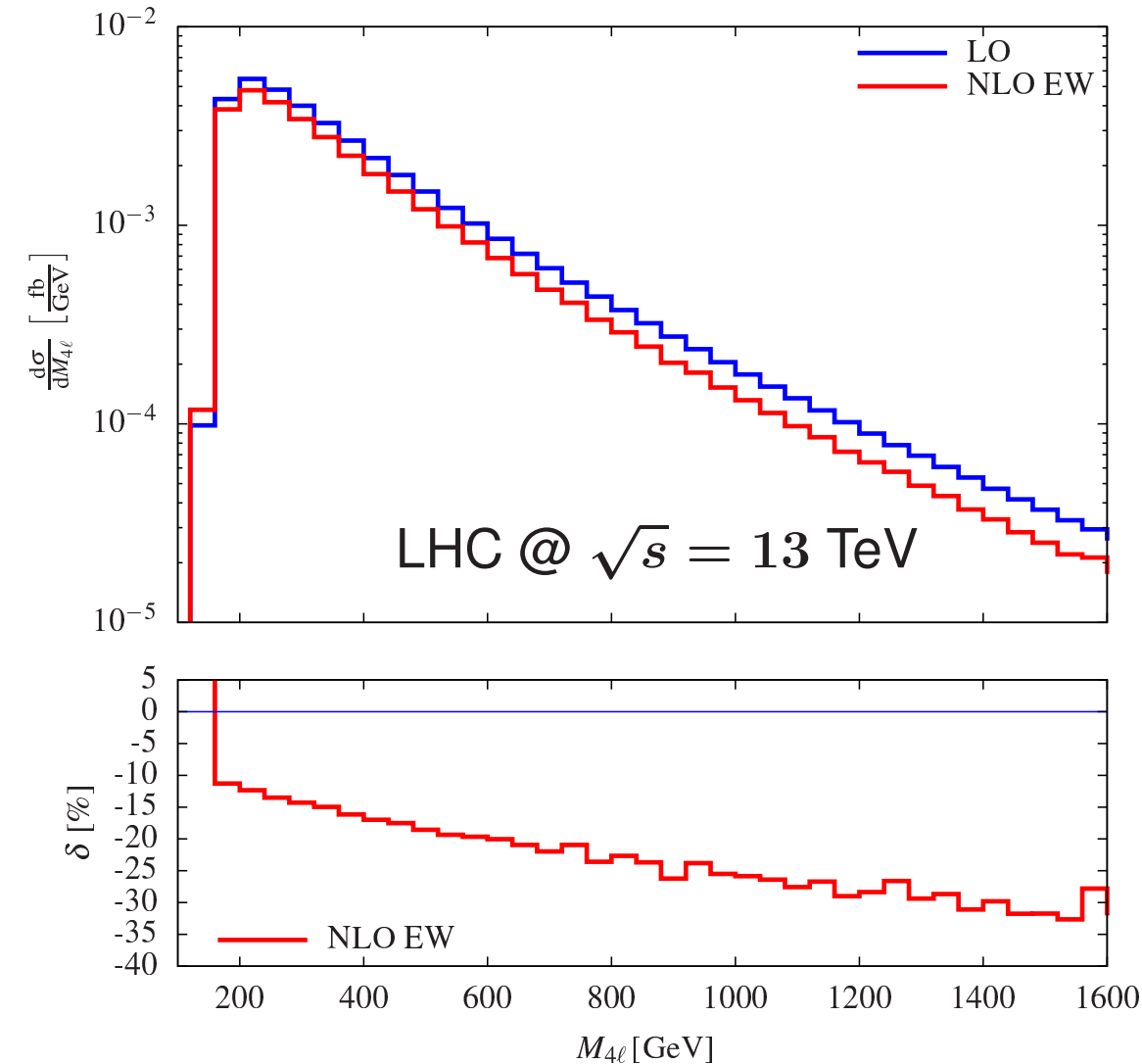
origin of large EW corrections to  $W^+W^+ \rightarrow W^+W^+$ :  
double and single **Sudakov logarithms** of the form

$$\sigma_{\text{LL}} = \sigma_{\text{LO}} \left[ 1 - \frac{\alpha}{4\pi} \frac{8}{\sin^2 \theta_W} \log^2 \left( \frac{Q^2}{M_W^2} \right) + \frac{\alpha}{4\pi} \frac{19}{3 \sin^2 \theta_W} \log \left( \frac{Q^2}{M_W^2} \right) \right],$$

... with scale  $Q$  characteristic for VBS  $\leftrightarrow m_{4\ell}$   
at LHC-13:  $\langle m_{4\ell} \rangle$  of order 390 GeV

*[Biedermann, Denner, Pellen (2016) ]*

# $pp \rightarrow W^+W^+jj$ : electroweak corrections



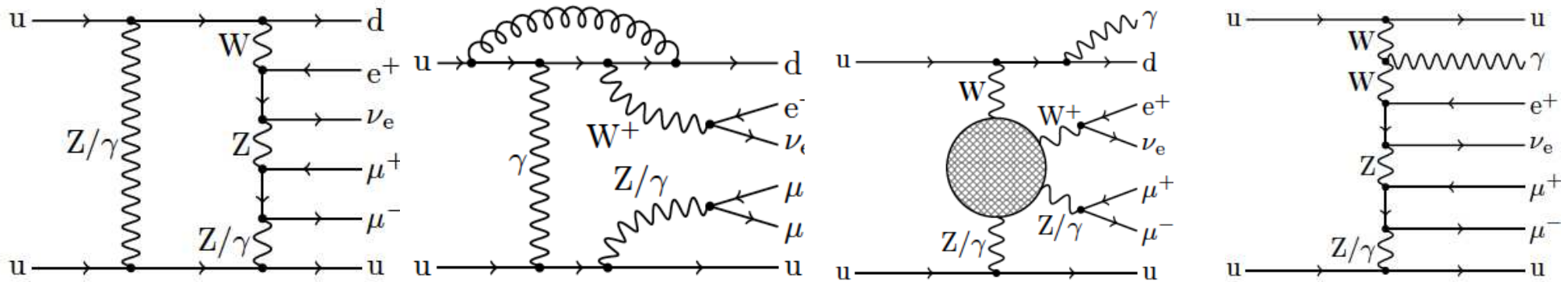
first calculation of NLO-EW  
corrections to same-sign VBS  
in fully leptonic decay mode

$$pp \rightarrow \mu^+ \nu_\mu e^+ \nu_e jj$$

dominant EW corrections of  
about -16% on fiducial xsec  
and even more ( $\sim -30\%$ )  
in tails of distributions

[Biedermann, Denner, Pellen (2016)]

# $pp \rightarrow WZjj$ : strong and EW corrections



systematic expansion in strong and electroweak couplings

☞ NLO corrections:  $\mathcal{O}(\alpha_s \alpha^6)$  and  $\mathcal{O}(\alpha^7)$ ;

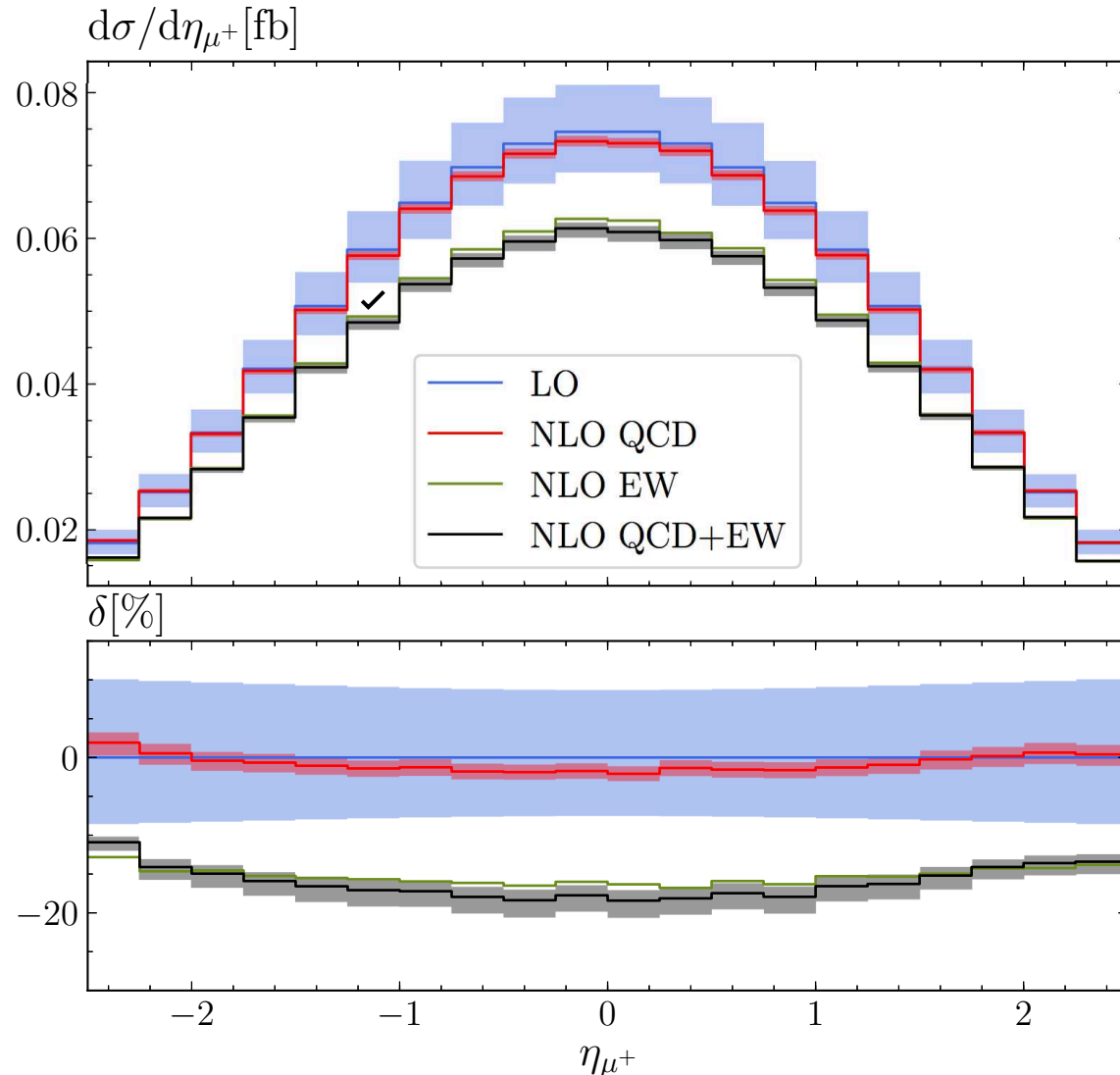
including loop diagrams and real photon or parton emission

very large number of diagrams: computed with the help of **automated amplitude generators** (OpenLoops and Recola)

[Denner, Dittmaier, Maierhöfer, Pellen, Schwan (2019)]

# $pp \rightarrow W Z j j$ : strong and EW corrections

[Denner, Dittmaier, Maierhöfer, Pellen, Schwan (2019)]



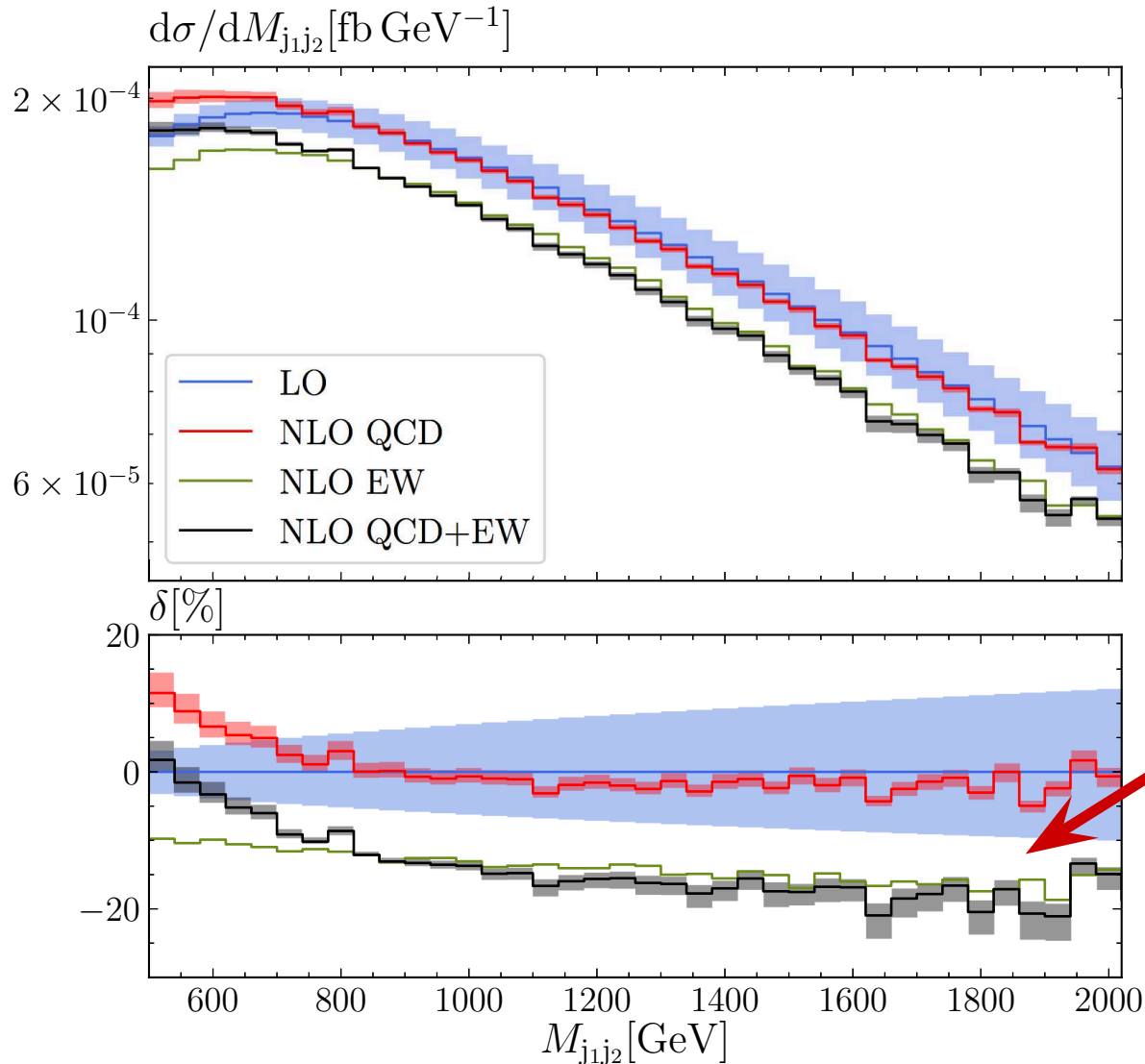
EW corrections larger than QCD corrections, shift xsec by  $\sim -16\%$

(compare size of QCD scale uncertainty

↕  
width of band)

# $pp \rightarrow W Z j j$ : strong and EW corrections

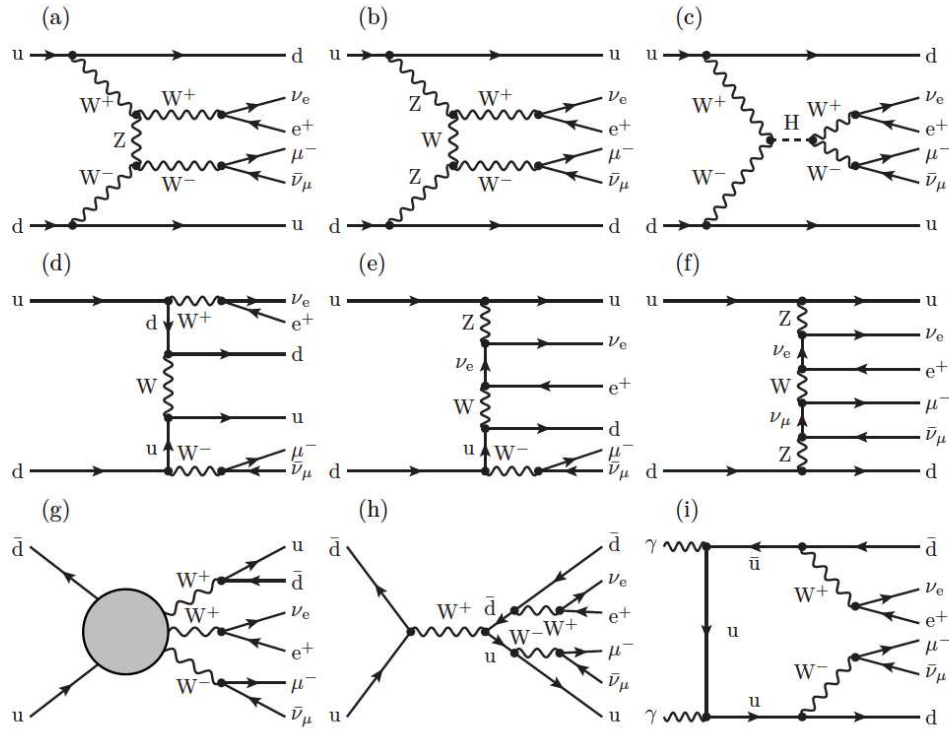
[Denner, Dittmaier, Maierhöfer, Pellen, Schwan (2019)]



typical **Sudakov behavior**  
of EW corrections in  
high-energy **tails**



$$pp \rightarrow W^+W^-jj$$



*Denner, Franken, Schmidt, Schwan  
(02/2022)*

impact of various contributions  
depends on selection cuts:

**VBS scenario**

versus

**Higgs search scenario**



different topologies and  
production modes

# $pp \rightarrow W^+W^-jj$ : impact of contributions at LO

*Denner et al. (2022)*

order	$\mathcal{O}(\alpha^6)$	$\mathcal{O}(\alpha_s\alpha^5)$	$\mathcal{O}(\alpha_s^2\alpha^4)$	$\mathcal{O}(\alpha_s^4\alpha^4)$	sum
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## VBS setup

$\sigma_{\text{LO}}[(\text{fb})]$	2.6988	0.06491	6.9115	0.1952	9.8704
fraction [%]	27.3	0.7	70.0	2.0	100

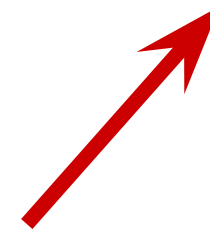
## Higgs setup

$\sigma_{\text{LO}}[(\text{fb})]$	1.5322	0.008996	1.6923	0.1057	3.3392
fraction [%]	45.9	0.3	50.7	3.2	100

# $pp \rightarrow VVjj$ : size of NLO EW corrections

*Denner et al. (2022)*

process	$W^+W^+$	$W^+Z$	$ZZ$	$W^+W^-$ (VBS setup)	$W^+W^-$ (Higgs setup)
$\sigma_{\text{LO}}^{\alpha^6}$ [fb]	1.4178	0.25511	0.097683	2.6988	1.5322
$\delta^{\text{EW}}$ [%]	-15.3	-16.0	-15.9	-11.4	-6.7



size of EW corrections depends  
on channel and cuts

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# parton shower matching: dedicated implementations

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- ◆ **matching to parton showers** for EW production mode:

*Jäger, Karlberg, Scheller, Zanderighi (2011-18)* → POWHEG-BOX

*Rauch, Plätzer (2016)* → HERWIG

- ◆ **matching to parton showers** for QCD production mode:

*Melia, Nason, Röntsch, Zanderighi (2011)* → POWHEG-BOX

- ◆ **matching to EW showers:**

*Chiesa, Denner, Lang, Pellen (2019)* → POWHEG-BOX

# parton shower matching: multi-purpose tools

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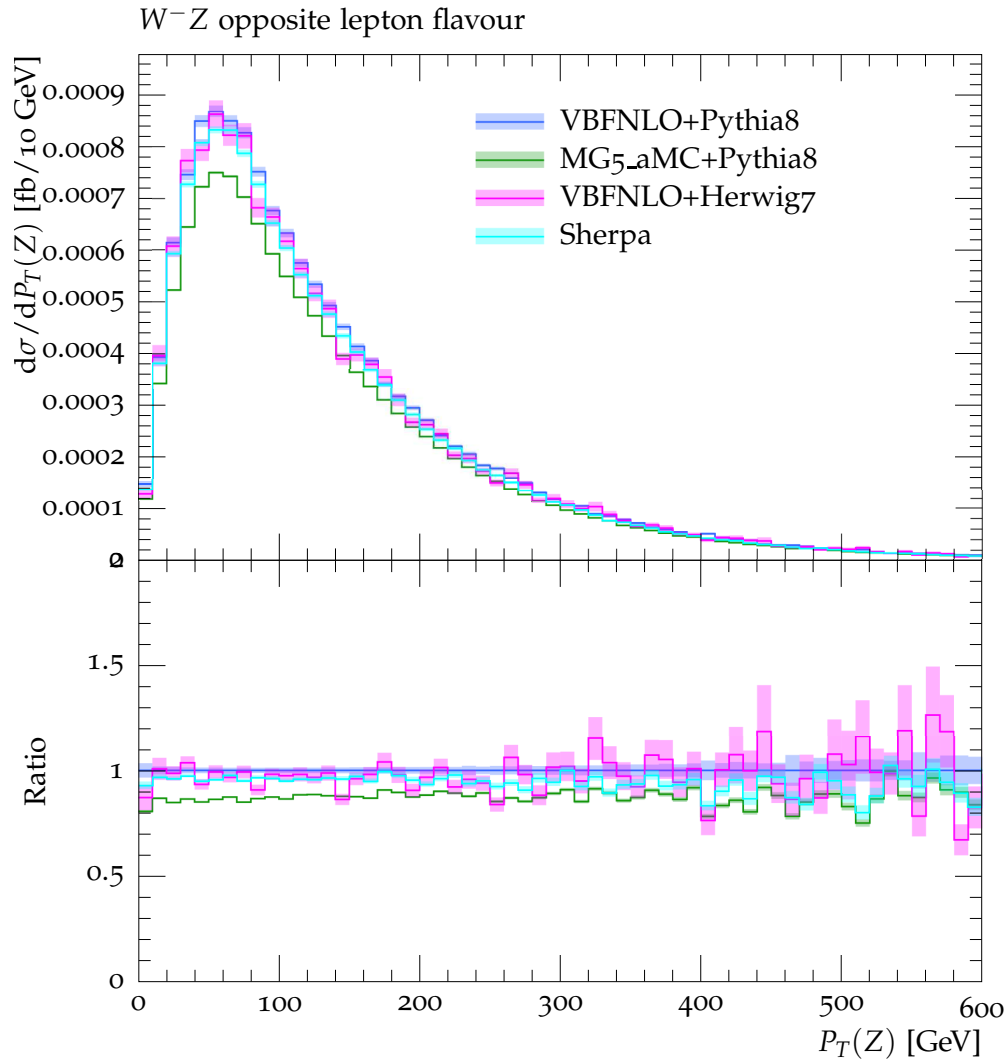
- ◆ **Madgraph5aMC@NLO:**

can in principle do NLO-QCD, but is typically used by experiments at LO with **factorized on-shell decays of  $V$  bosons**

- ◆ **Sherpa:**

LO for  $VVjj$ , but can provide **merged samples** with up to two extra jets

# $pp \rightarrow WZjj$ matched to parton showers at LO



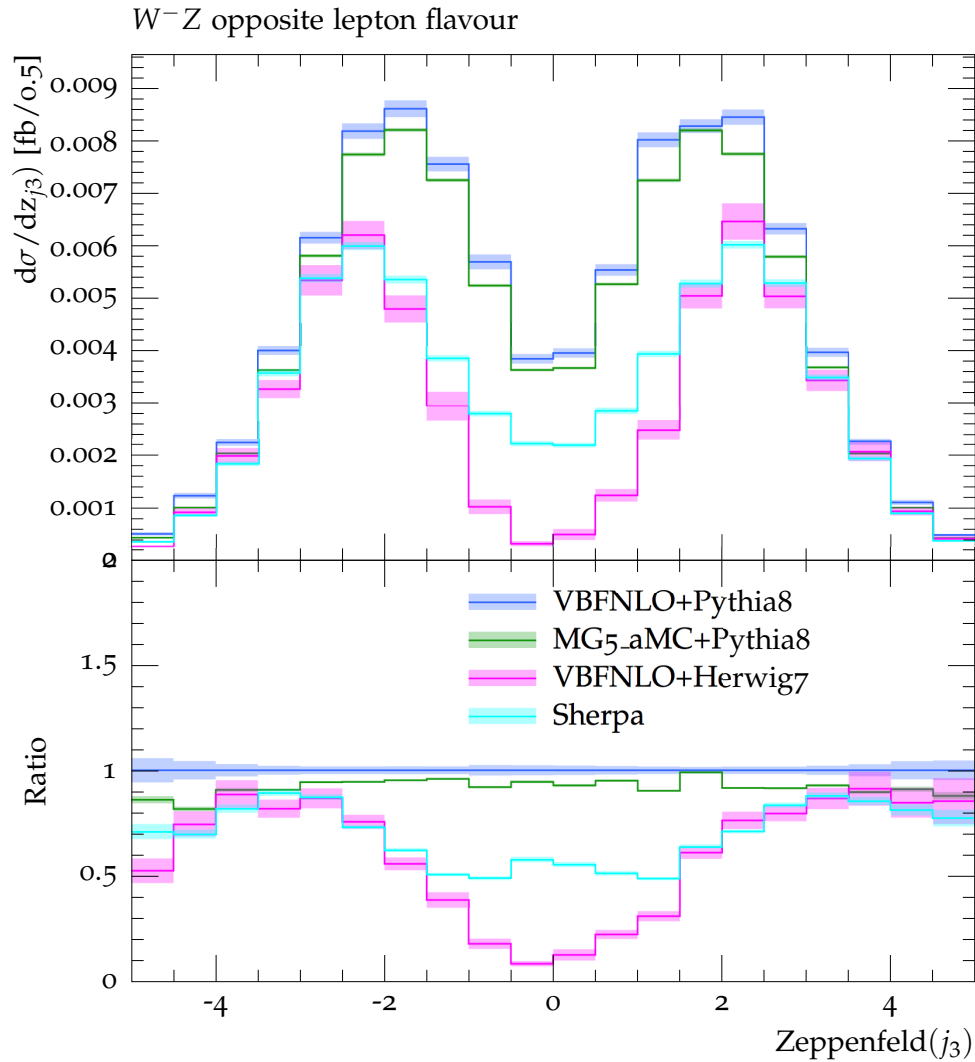
[Les Houches (2018)]

systematic comparison of existing tools matched to parton showers at LO:

- ◆ significant discrepancies even for distributions of particles already present at Born level



# $pp \rightarrow WZjj$ matched to parton showers at LO



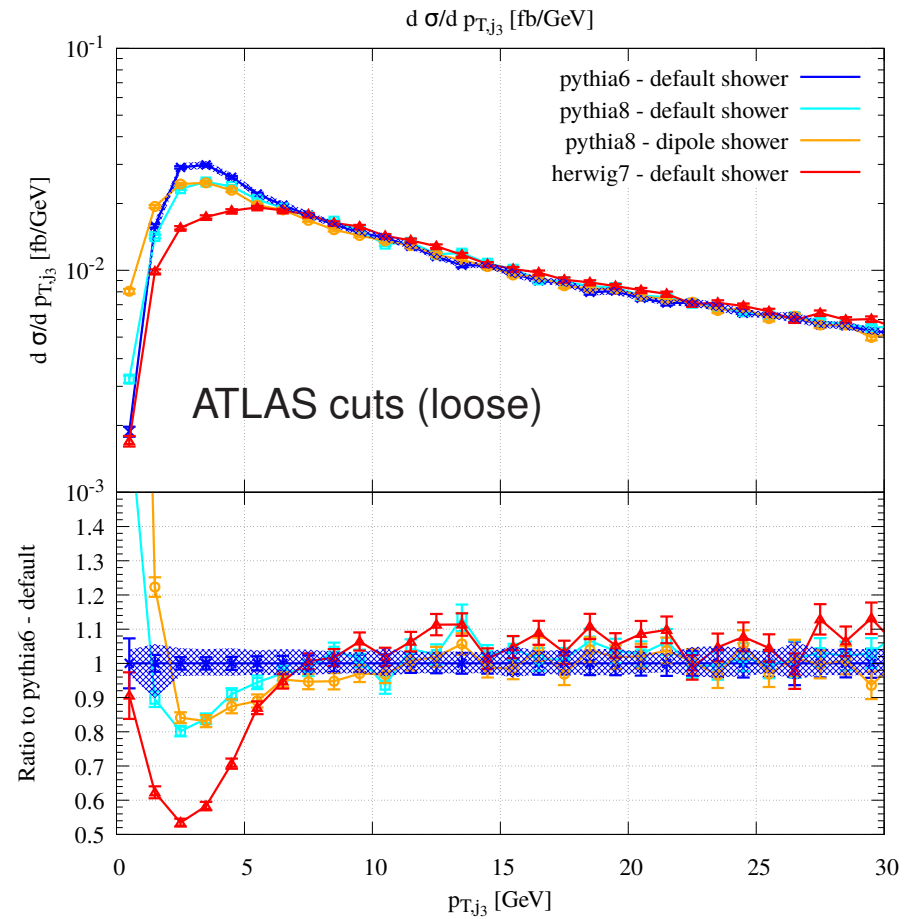
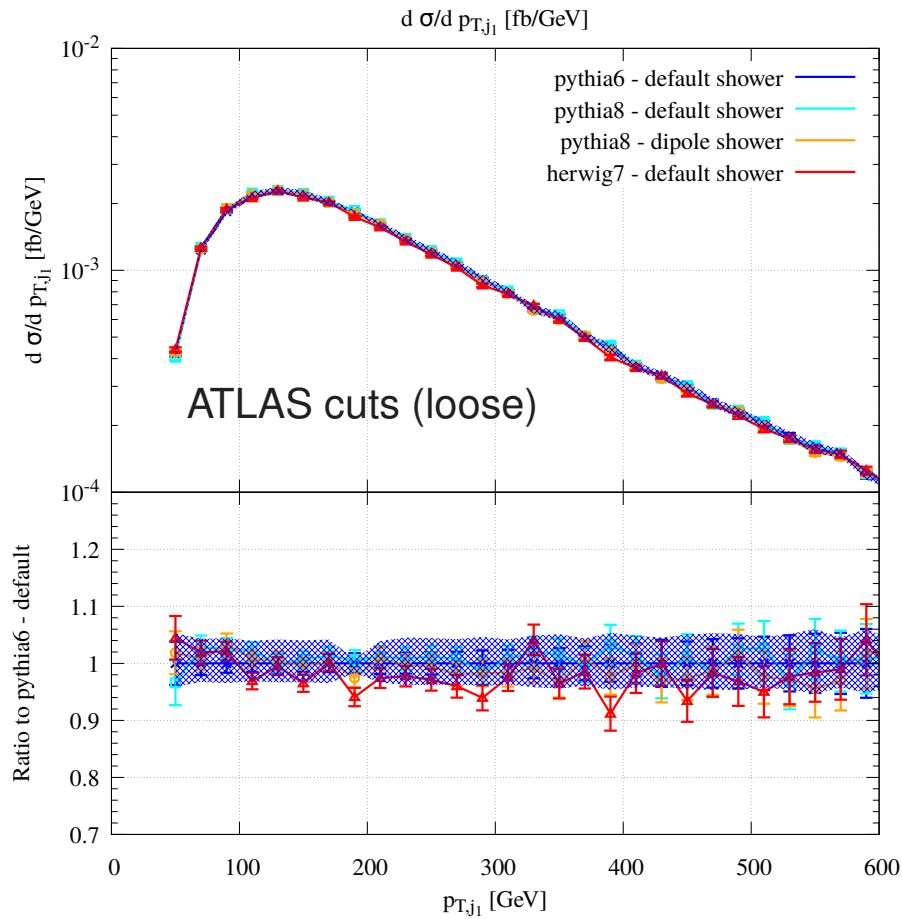
[Les Houches (2018)]

systematic comparison of existing tools matched to parton showers at LO:

- ◆ significant discrepancies even for distributions of particles already present at Born level
- ◆ up to 100% differences in distributions of 3rd jet, like

$$z = \frac{y_{j3} - \frac{y_{j1} + y_{j2}}{2}}{|y_{j1} - y_{j2}|}$$

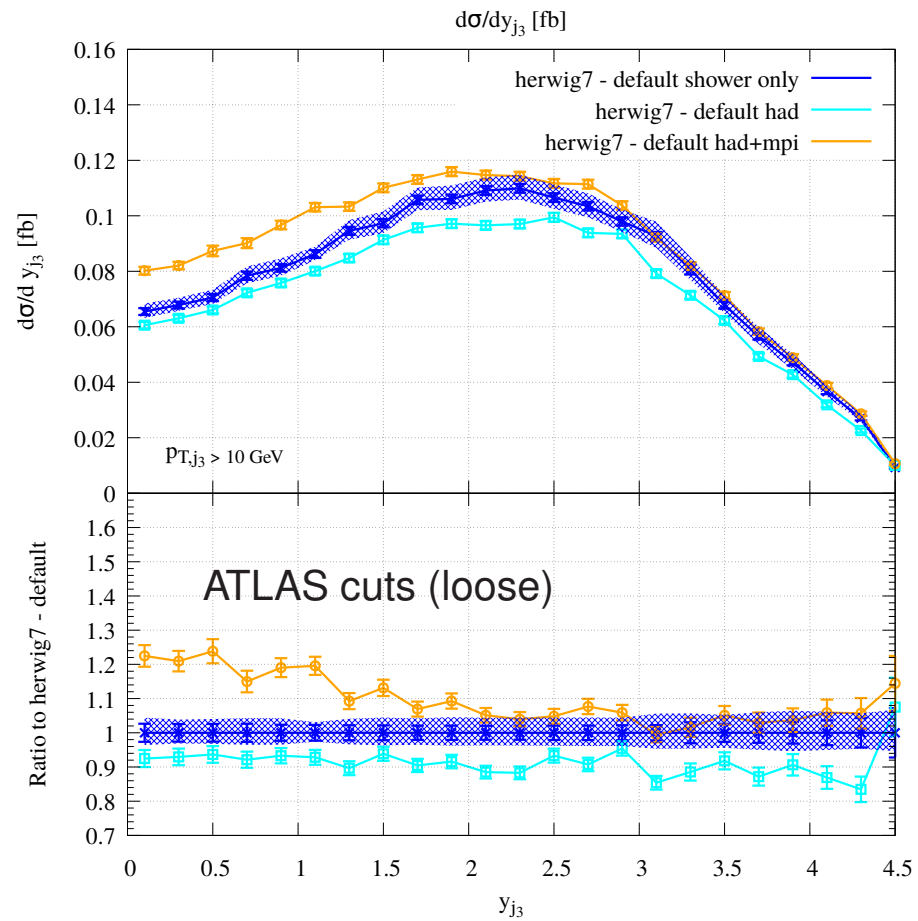
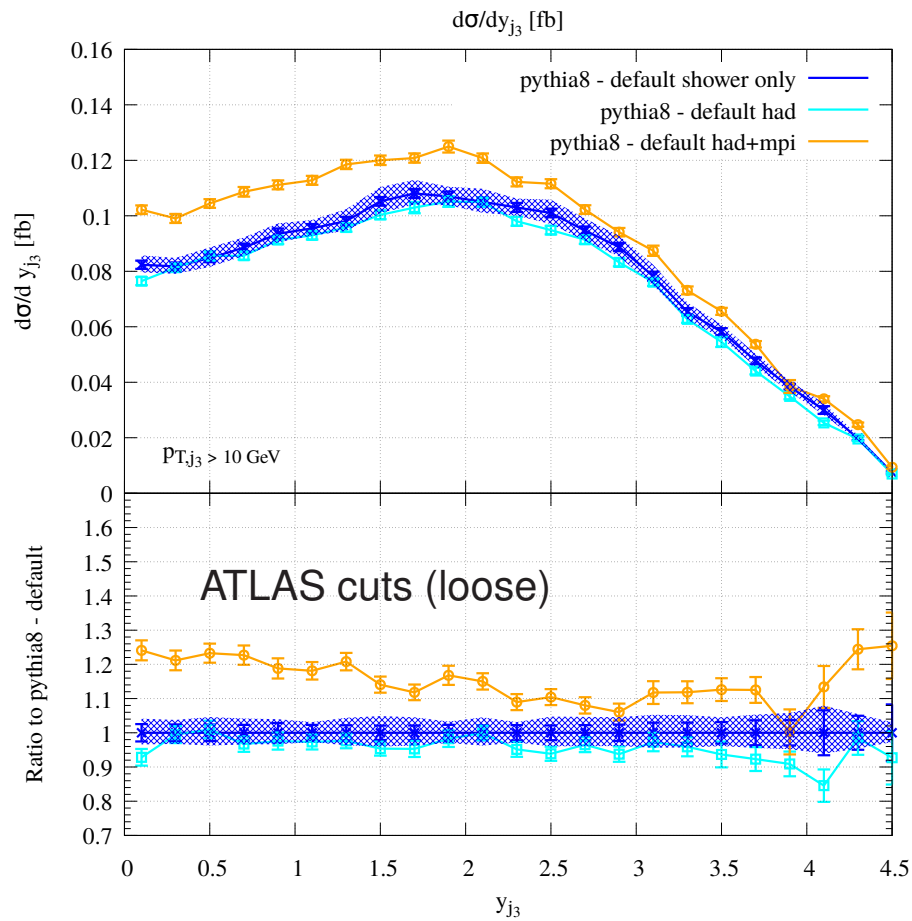
# $pp \rightarrow W Z j j$ matched to parton showers at NLO-QCD



[B.J., Karlberg, Scheller (2018)]

parton-shower settings have little impact on tagging jets;  
larger differences for non-tagging jets

# $pp \rightarrow W Z j j$ matched to parton showers at NLO-QCD

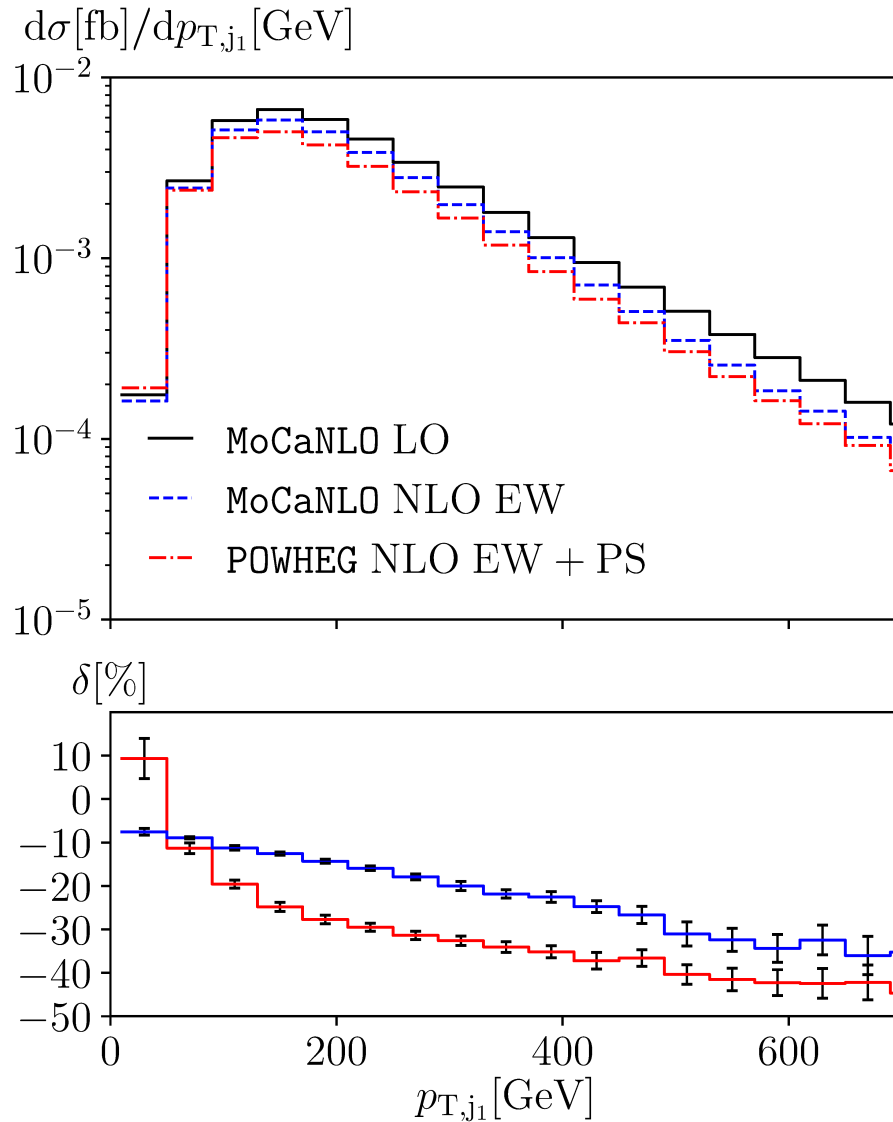


[B.J., Karlberg, Scheller (2018)]

parton-shower settings modify rapidity distribution of 3rd jet

# $pp \rightarrow W^+W^+jj$ at NLO-EW matched to a QED shower

[Chiesa, Denner, Lang, Pellen (2019)]



matching of NLO EW  
calculation to QED shower:

- ◆ typical Sudakov suppression in tails because of EW corrections
- ◆ extra shower radiation: additional decrease
- ✓ implementation available in the POWHEG-BOX

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# LO comparison for $pp \rightarrow W^+W^+jj$

VBS-typical cuts:

$$p_{T,\ell} > 20 \text{ GeV}, |y_\ell| < 2.5, \Delta R_{\ell\ell} > 0.3$$

$$p_{T,miss} > 40 \text{ GeV},$$

$$p_{T,j} > 30 \text{ GeV}, |y_j| < 4.5, \Delta R_{j\ell} > 0.3$$

$$m_{jj} > 500 \text{ GeV}, |\Delta y_{jj}| > 2.5$$

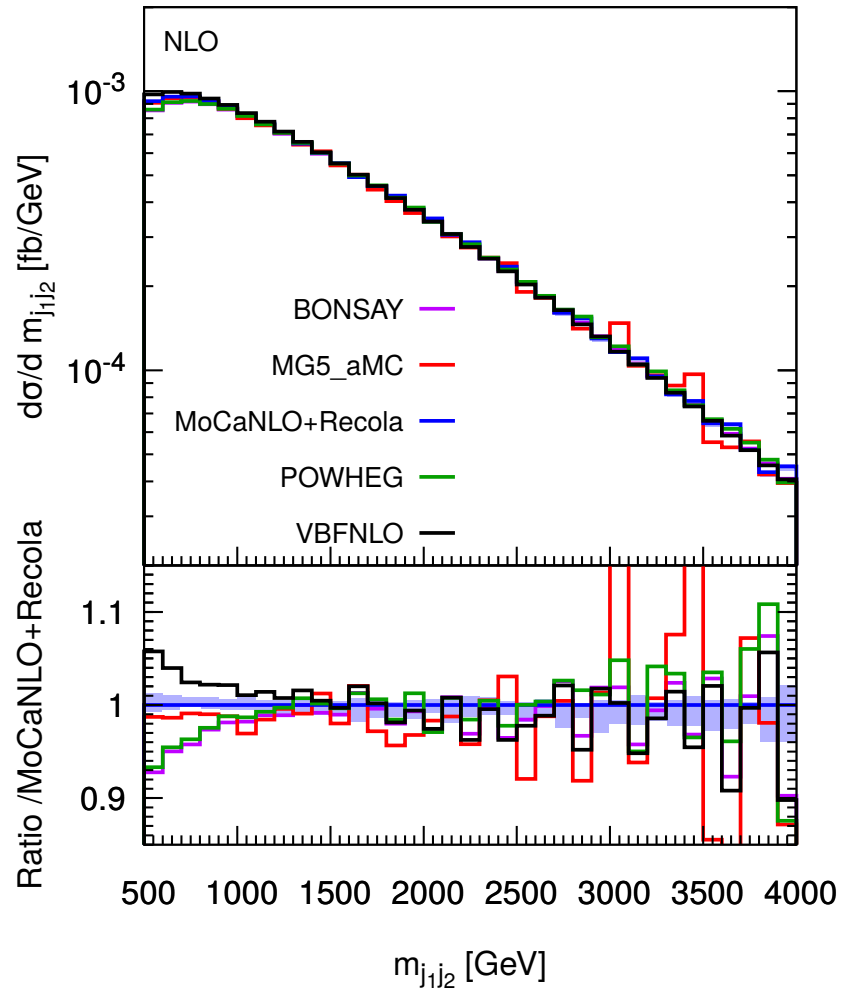
**tuned comparison** of existing tools performed in context of VBS-COST action

*[Ballestrero et al. (2018)]*

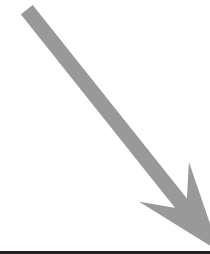
Code	$\sigma$ [fb]
BONSAY	$1.43636 \pm 0.00002$
POWHEG-BOX	$1.44092 \pm 0.00009$
VBFNLO	$1.43796 \pm 0.00005$
PHANTOM	$1.4374 \pm 0.0006$
WHIZARD	$1.4381 \pm 0.0002$
MG5_AMC	$1.4304 \pm 0.0007$
MoCANLO+RECOLA	$1.43476 \pm 0.00009$

# NLO-QCD comparison for $pp \rightarrow W^+W^+jj$

*Ballestrero et al. (2018)*



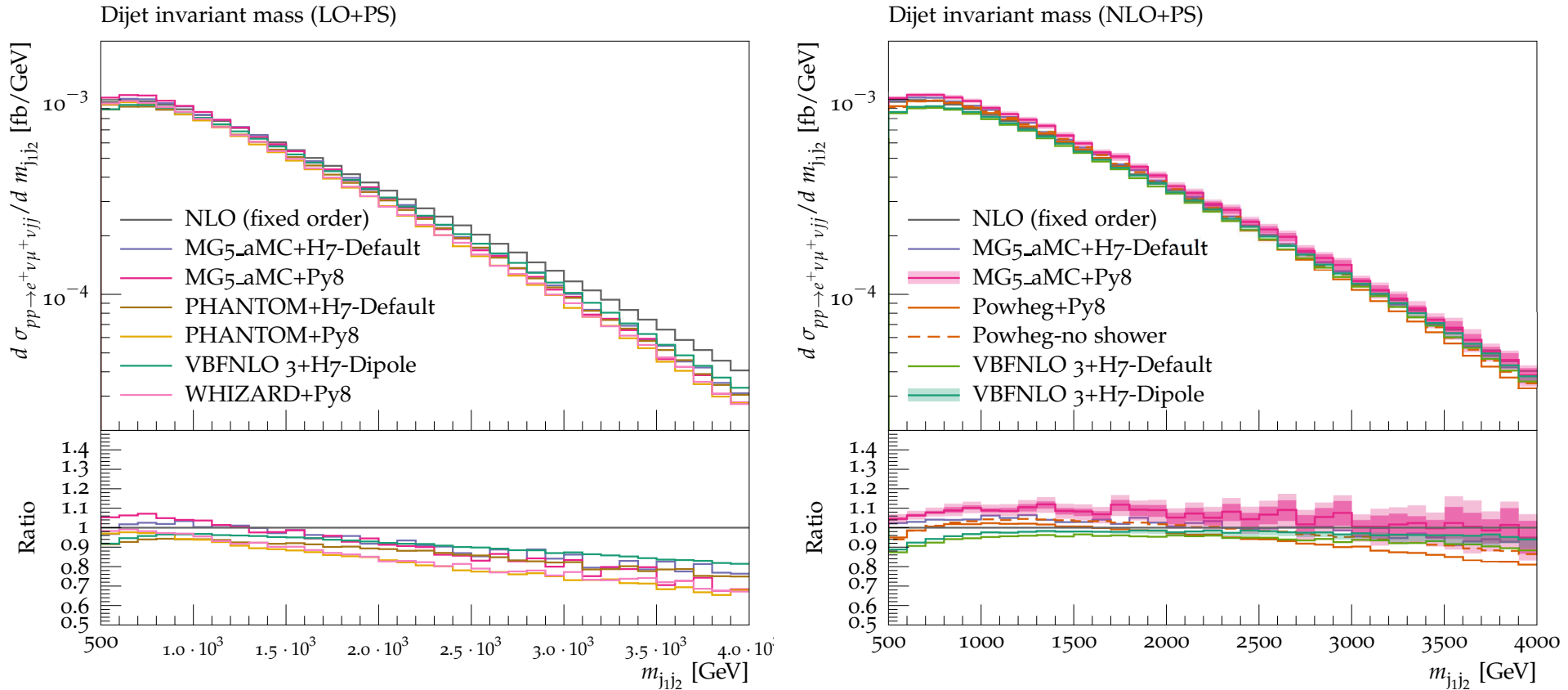
good agreement at  
NLO-QCD



Code	$\sigma$ [fb]
BONSAY	$1.35039 \pm 0.00006$
POWHEG-BOX	$1.3605 \pm 0.0007$
VBFNLO	$1.3916 \pm 0.0001$
MG5_AMC	$1.363 \pm 0.004$
MoCANLO+RECOLA	$1.378 \pm 0.001$



# parton-shower comparison for $pp \rightarrow W^+W^+jj$



Ballestrero et al. (2018)

differences between various simulations reduced when going from LO+PS to NLO+PS

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# polarization effects in $VV$ scattering

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recall: longitudinal gauge boson modes  $W_L^\pm, Z_L$   
intimately linked to Higgs mechanism



can we isolate longitudinal polarization modes of the gauge bosons in VBS processes?

major obstacle: experimentally accessible process is

$pp \rightarrow 4 \text{ fermions} + 2 \text{ jets}$ , not  $VV \rightarrow VV$ !

- ✗ initial state: collider does not provide polarized gauge bosons
- ✗ final state contains contributions from non-resonant diagrams

# polarized $VV$ scattering: Monte-Carlo tools

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tools featuring (approximate) methods to treat spin correlations and off-shell effects for processes involving weak bosons:

## ◆ MG5\_aMC@NLO:

- polarized on-shell  $V$  bosons (up to NLO+PS) in SM and several BSM models;
- spin-correlated decays in NWA (with `MadSpin` or via decay chain)

## ◆ WHIZARD:

polarized on shell  $V$  bosons (NWA, cascade decay), within SM or SMEFT

## ◆ PHANTOM:

generation of polarized  $V$  bosons in  $2 \rightarrow 6$  processes, including all spin correlations and off-shell effects at LO in SM, Higgsless and Singlet Extension

## ◆ WZDECAY:

generator-independent package for decaying polarized  $V$  bosons in NWA

# take-home message

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impressive number of **experimental results** on VBS . . .

. . . but also status of **theoretical work** is very advanced:

◆ theorists provide **precision calculations and tools**:

NLO QCD, NLO EW, NLO QCD+EW,

matching to parton showers, . . .

◆ new line of investigation: **polarization effects** in VBS processes

**tools are on the market** which allow for

simulations at **high degree of accuracy**

☞ they can only unfold their potential if used



...for your attention