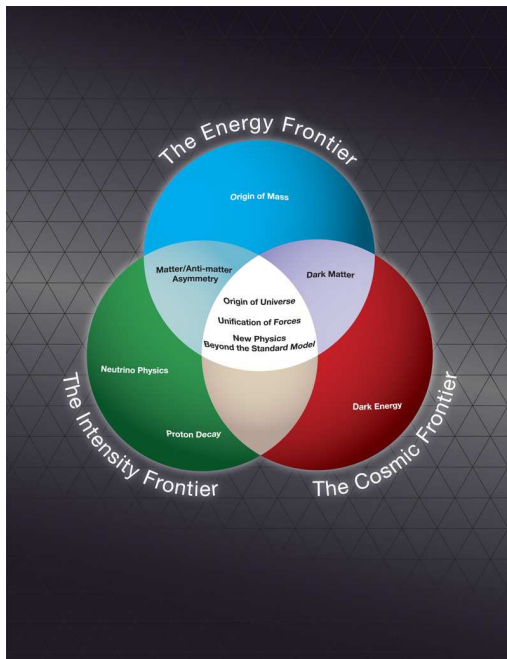


# Sterile neutrinos as dark matter

Oleg RUCHAYSKIY

CERN

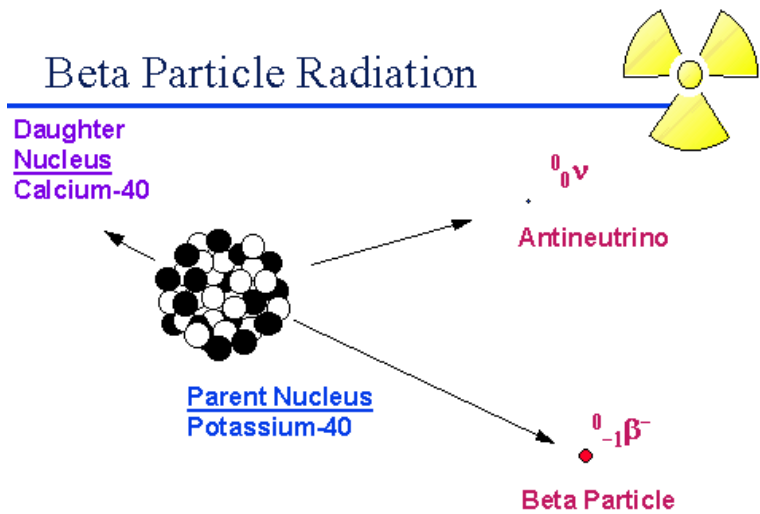


**Dark matter underground  
and in the heavens**

# Higgs - last unseen element of the SM

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The quest that started from attempts to explain atomic and nuclear physics, taking into account Quantum Mechanics and Relativity resulted in construction of the **Standard Model of elementary particles**



## BSM physics

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Already now we know a number of observational **beyond the Standard Model phenomena**:

- **Neutrino oscillations**: transition between neutrinos of different flavours ( $\nu_e, \nu_\mu, \nu_\tau$ ) means violation of lepton flavour symmetries (but not total lepton number!)
- existence of **dark matter** (why observed gravity of galaxies and clusters is so strong?)
- the **absence of anti-matter** in the Universe
- inflation (homogeneity of the observed Universe seem to require correlated initial conditions for causally non-connected regions)
- dark energy (If it will be shown that accelerated expansion of the Universe is caused not by a small cosmological constant, but by some other unknown substance – what is this substance?)

## Fine-tuning problems

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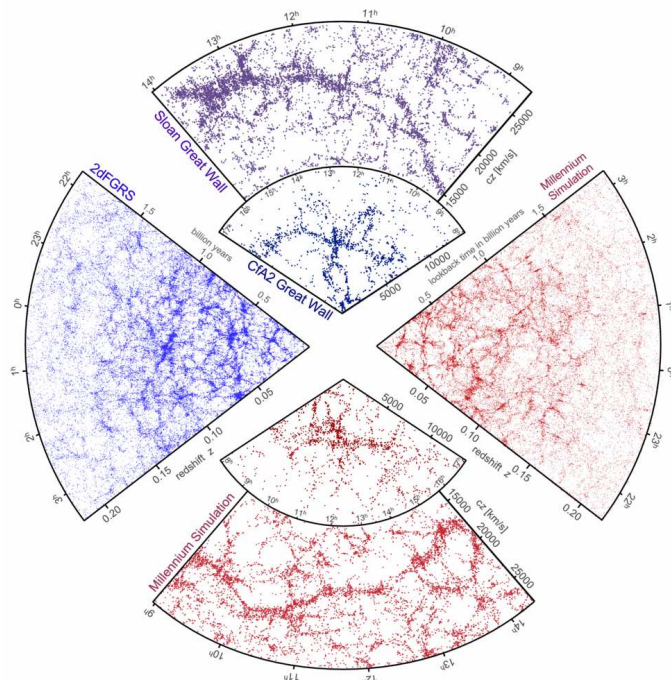
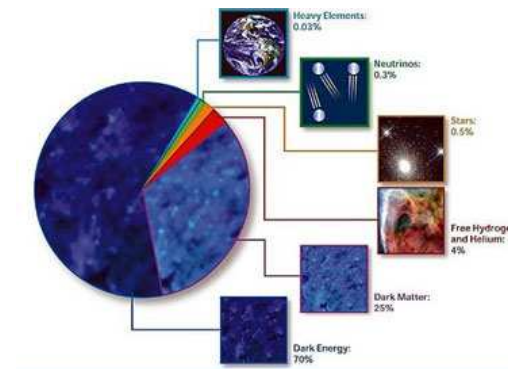
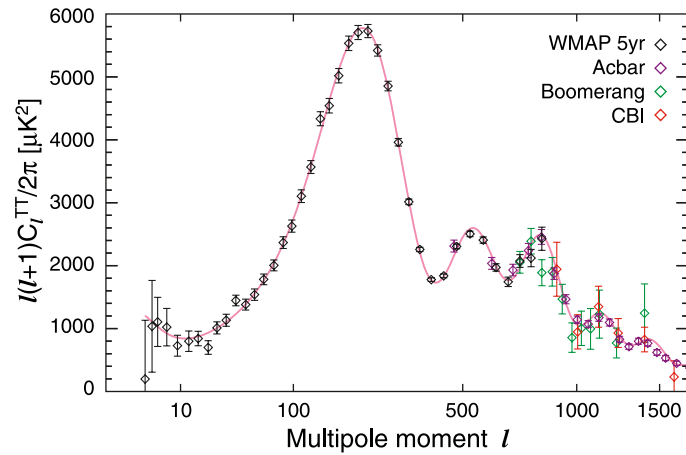
- Important direction of the theoretical particle physics research of the last decades is the problem of “naturalness” – understanding the structure of the Standard Model, small values of some parameters, symmetries, etc:
  - **Gauge hierarchy** problem (why the Higgs mass is small and stable against radiative corrections)
  - **CP problem** (why neutron electrical dipole moment is so small?)
  - **Cosmological constant** problem (why is cosmological constant zero or almost zero?)

## Where can we expect new physics?

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- **Neutrino oscillations**  $m_\nu \sim \sqrt{\Delta m_{\text{atm}}^2} \sim 10^{-2}$  eV.  
**See-saw mechanism**  $m_\nu \sim v^2/\Lambda$ , where  $v = \langle H \rangle = 174$  GeV and  
**new scale**  $\Lambda \sim 10^{15}$  GeV
- **Dark matter**
  - particles with weak cross-section will have correct abundance  $\Omega_{\text{DM}}$  (“WIMP miracle”). **New scale**  $\sim 1$  TeV
  - Axions. **New scale**  $10^{10} - 10^{12}$  GeV.
- **Fine-tuning problems:**
  - hierarchy problem:  $\sim 1$  TeV
  - grand unification:  $\sim 10^{15}$  GeV
  - CP-problem:  $10^{10} - 10^{12}$  GeV (if provided by axion)
- ...

# Dark matter in the Universe



- $\Lambda$ CDM: about 20% of total energy density is in the form of **non-baryonic** matter
- This dark matter is **scale-free** (non-interacting, “cold”, ...)

# Sterile neutrino dark matter

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- Massive neutrinos – probably the first DM candidate. Did not work – particles remain relativistic for too long.  $\Rightarrow$  **Standard Model neutrinos** do not contribute significantly to the Universe mass balance at matter-dominated epoch (CMB, LSS, ...)
- Sterile neutrinos (right-handed counterparts of SM neutrinos): heavier (“colder”) than ordinary neutrinos and couple to the Standard Model super-weakly.  $\Rightarrow$  **Dark matter candidate**
- DM sterile neutrino does not contribute to the neutrino oscillations  $\Rightarrow$  two more particles are needed.
- To be a DM candidate sterile neutrino should couple super-weakly to the Standard Model particles  $\Rightarrow$  its properties (abundance, primordial velocities, etc.) are sensitive to the content of primordial plasma

Dodelson & Widrow (1993)

Shi & Fuller (1998)

Abazajian et al. 2001-2005

Asaka, Shaposhnikov et al. 2005-...

# Standard Model

	I	II	III		
mass →	2.4 MeV	1.27 GeV	171.2 GeV	0	
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	
name →	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>g</b> gluon	
	Left Right	Left Right	Left Right		
	4.8 MeV	104 MeV	4.2 GeV	0	
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	
Quarks	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b><math>\gamma</math></b> photon	
	Left Right	Left Right	Left Right		
	0 eV	0 eV	0 eV	91.2 GeV	
	0	0	0	0	
	<b><math>\nu_e</math></b> electron neutrino	<b><math>\nu_\mu</math></b> muon neutrino	<b><math>\nu_\tau</math></b> tau neutrino	<b>Z<sup>0</sup></b> weak force	<b>H</b> Higgs boson
	Left Right	Left Right	Left Right		spin 0
	0.511 MeV	105.7 MeV	1.777 GeV	80.4 GeV	
	-1	-1	-1	$\pm 1$	
Leptons	<b>e</b> electron	<b><math>\mu</math></b> muon	<b><math>\tau</math></b> tau	<b>W<sup>±</sup></b> weak force	
	Left Right	Left Right	Left Right		

Standard Model neutrinos are **strictly massless**



## Right-chiral particles

---

- Massless fermions can be left and right-chiral (left and right moving):

$$(i\gamma^\mu \partial_\mu - \cancel{m})\psi = \begin{pmatrix} \cancel{m}^0 & i(\partial_t + \vec{\sigma} \cdot \vec{\nabla}) \\ i(\partial_t - \vec{\sigma} \cdot \vec{\nabla}) & \cancel{m}^0 \end{pmatrix} \begin{pmatrix} \psi_L \\ \psi_R \end{pmatrix} = 0$$

where  $\gamma_5 \psi_{R,L} = \pm \psi_{R,L}$  and  $\gamma_5 = i\gamma_0\gamma_1\gamma_2\gamma_3$

- Mass term mixes left and right movers
- To make neutrinos massive, we can add **right-chiral** counterparts  $N_I$

$$\mathcal{L}_{\text{neutrino mass}} = i\bar{N}_I \not{\partial} N_I + \underbrace{\begin{pmatrix} \bar{\nu}_e - N_I \\ \bar{\nu}_\mu - N_J \\ \dots \end{pmatrix}}_{\text{left-right mixing}} + \text{????}$$

# Right-chiral neutrino counterparts?

	I	II	III		
mass →	2.4 MeV	1.27 GeV	171.2 GeV	0	0
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
name →	Left <b>u</b> Right up	Left <b>c</b> Right charm	Left <b>t</b> Right top	<b>g</b> gluon	
	4.8 MeV	104 MeV	4.2 GeV	0	0
Quarks	Left $-\frac{1}{3}$ <b>d</b> Right down	Left $-\frac{1}{3}$ <b>s</b> Right strange	Left $-\frac{1}{3}$ <b>b</b> Right bottom	<b><math>\gamma</math></b> photon	
	$<0.0001$ eV / $\sim 10$ keV	$\sim 0.01$ eV / $\sim$ GeV	$\sim 0.04$ eV / $\sim$ GeV	91.2 GeV	$>114$ GeV
	Left $0$ <b><math>\nu_e</math></b> Right electron neutrino	Left $0$ <b><math>\nu_\mu</math></b> Right muon neutrino	Left $0$ <b><math>\nu_\tau</math></b> Right tau neutrino	$0$ <b><math>Z^0</math></b> weak force	$0$ <b>H</b> Higgs boson
Leptons	Left $-1$ <b>e</b> Right electron	Left $-1$ <b><math>\mu</math></b> Right muon	Left $-1$ <b><math>\tau</math></b> Right tau	80.4 GeV	spin 0
				$\pm 1$ <b><math>W^\pm</math></b> weak force	

The most natural explanation of neutrino experiments – adding right-chiral counterparts to the Standard Model

# Properties of right-chiral neutrinos

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- Charges of right neutrinos?
  - SU(3) : **singlets**
  - SU(2) : **singlets** ( $\nu = L\tilde{H}$  – singlet combination)
  - U<sub>Y</sub>(1) : **singlets** ( $Y(\nu) = Y(\text{Higgs})$ )
- Right-chiral neutrinos **carry no charge** under the Standard Model interactions  $\Rightarrow$  **sterile neutrinos**
- Can add for them a **Majorana mass**

$$\mathcal{L}_{\text{see-saw}} = i\bar{N}_I \not{\partial} N_I + \underbrace{\begin{pmatrix} \text{mixing matrix} \\ \bar{\nu}_e - N_I \\ \bar{\nu}_\mu - N_J \\ \dots \end{pmatrix}}_{\text{Dirac mass } M_D} + \underbrace{\begin{pmatrix} N - N \\ \text{mixing} \end{pmatrix}}_{\text{Majorana mass } M_I}$$

- See-saw Lagrangian violate **flavour** and **total** lepton numbers

## See saw Lagrangian

---

$$\mathcal{L}_{\text{see-saw}} = i\bar{N}_I \not{\partial} N_I + \underbrace{\begin{pmatrix} \bar{\nu}_e - N_I \\ \bar{\nu}_\mu - N_J \\ \dots \end{pmatrix}}_{\text{Dirac mass } M_D} + \underbrace{\begin{pmatrix} N - N \\ \text{mixing} \end{pmatrix}}_{\text{Majorana mass } M_I}$$

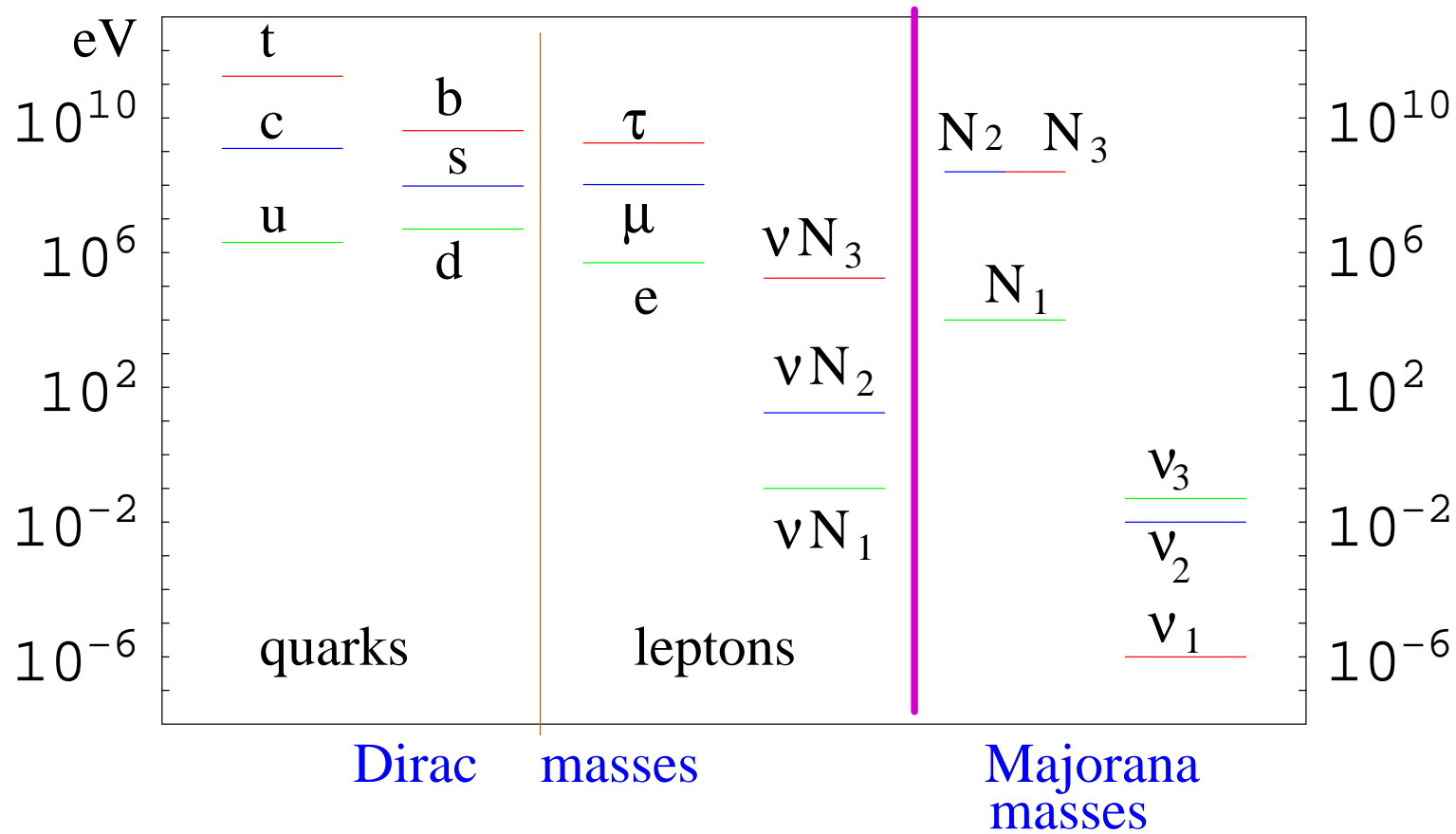
- Standard Model neutrino masses are given by **see-saw formula**:

$$\text{Neutrino mass matrix} = -M_{\text{Dirac}} \frac{1}{M_{\text{Majorana}}} M_{\text{Dirac}}^T$$

- Neutrino mass matrix – **9 parameters**. Dirac+Majorana mass matrix – **11 (18) parameters** for 2 (3) sterile neutrinos.
- **Two** sterile neutrinos are enough to fit the neutrino oscillations data.

**Scale of Dirac and Majorana masses is not fixed!**

# Neutrino Minimal Standard Model



## Mass spectrum of the $\nu$ MSM

Yukawa couplings of sterile neutrinos  $\ll 1$

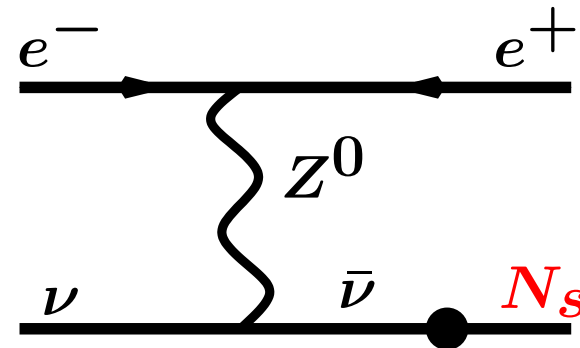
# Some general properties of sterile neutrino

Sterile neutrinos behave as **superweakly interacting** heavy neutrinos

$M_I < 1 \text{ MeV}$	$M_I \gtrsim 1 \text{ MeV}$	$M_I \gtrsim 140 \text{ MeV}$	...
$N_I \rightarrow \nu\nu\bar{\nu}$	$N_I \rightarrow \nu e^+ e^-$	$N_I \rightarrow \pi^\pm e^\mp$	
$N_I \rightarrow \nu\gamma$		$N_I \rightarrow \pi^0\nu$	

Mixing angle with usual neutrinos  $\theta_I$ :

$$\theta_I^2 = \sum_{\alpha=e,\mu,\tau} \frac{M_{\text{Dirac},\alpha I}^2}{M_{\text{Majorana},I}^2} \ll 1$$



Fermi constant:  $G_F \rightarrow \theta G_F$

Lifetime  $\tau \propto \theta_I^{-2} M_I^{-5}$ . Can be cosmologically long

Mixing angle  $\theta \ll 1$  means that sterile neutrinos can be out of equilibrium in the early Universe

# Entire history of the Universe

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## Neutrino Minimal Standard Model ( $\nu$ MSM) solves several *beyond the Standard Model* problems

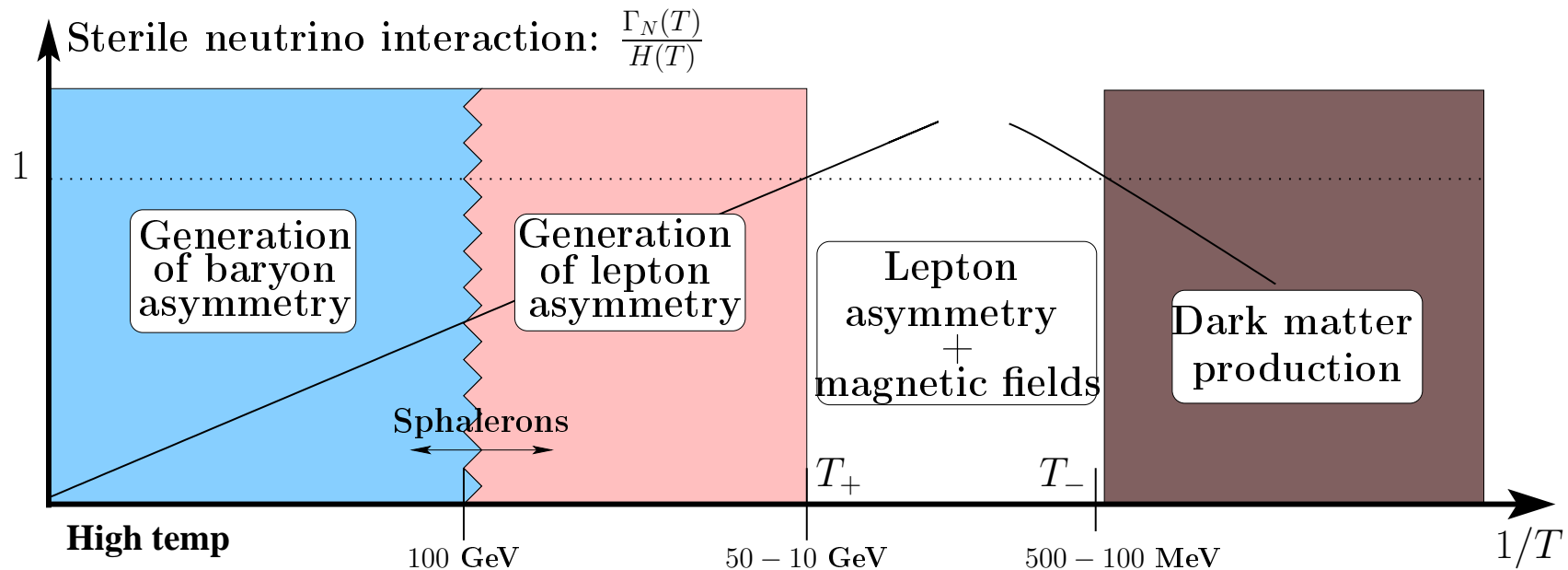
Asaka,  
Shaposhnikov  
(2005)

- ✓ ... explains neutrino oscillations
- ✓ ... matter-antimatter asymmetry of the Universe
- ✓ ... provides a viable dark matter candidate that can be cold, **warm** or **mixed** (cold+warm)
- The  $\nu$ MSM is self-consistent and does not require any other particles  $\Rightarrow$  we have a **complete description of the Universe** from the time of reheating
- Coupled with Higgs inflation the  $\nu$ MSM is a complete and self-consistent theory up to the Planck scale

Bezrukov &  
Shaposhnikov  
(2008)

# Thermal history of the $\nu$ MSM

- Two sterile neutrinos are responsible for neutrino oscillations.
- They determine the properties of the third (DM) sterile neutrino
- Physics of the early Universe with (out-of-equilibrium) sterile neutrinos





## Sakharov conditions in the SM

---

Quick reminded: necessary conditions for generation of baryon asymmetry of the Universe (**Sakharov conditions**):

⊕ B-number violation → sphalerons

⊕ CP (and C) non-conservation → phase of the CKM matrix

⊖ Out-of-equilibrium processes → no phase transition in the SM for  $m_H > 72 \text{ GeV!}$

Sakharov  
(1967)

Kuzmin,  
Rubakov,  
Shaposhnikov  
(1985)

Farrar &  
Shaposhnikov  
(1994)

Kajantie et al.  
(1996)

# What changes in the $\nu$ MSM?

## Sakharov conditions in the ( $\nu$ )MSM

---

Necessary conditions for generation of baryon asymmetry of the Universe (**Sakharov conditions**):

⊕ B-number violation  $\rightarrow$  sphalerons

Sakharov  
(1967)

Kuzmin,  
Rubakov,  
Shaposhnikov  
(1985)

⊕ CP (and C) non-conservation  $\rightarrow$  phase of the CKM matrix **plus additional CP phases in the Dirac mass matrix of sterile neutrinos**

Farrar &  
Shaposhnikov  
(1994)

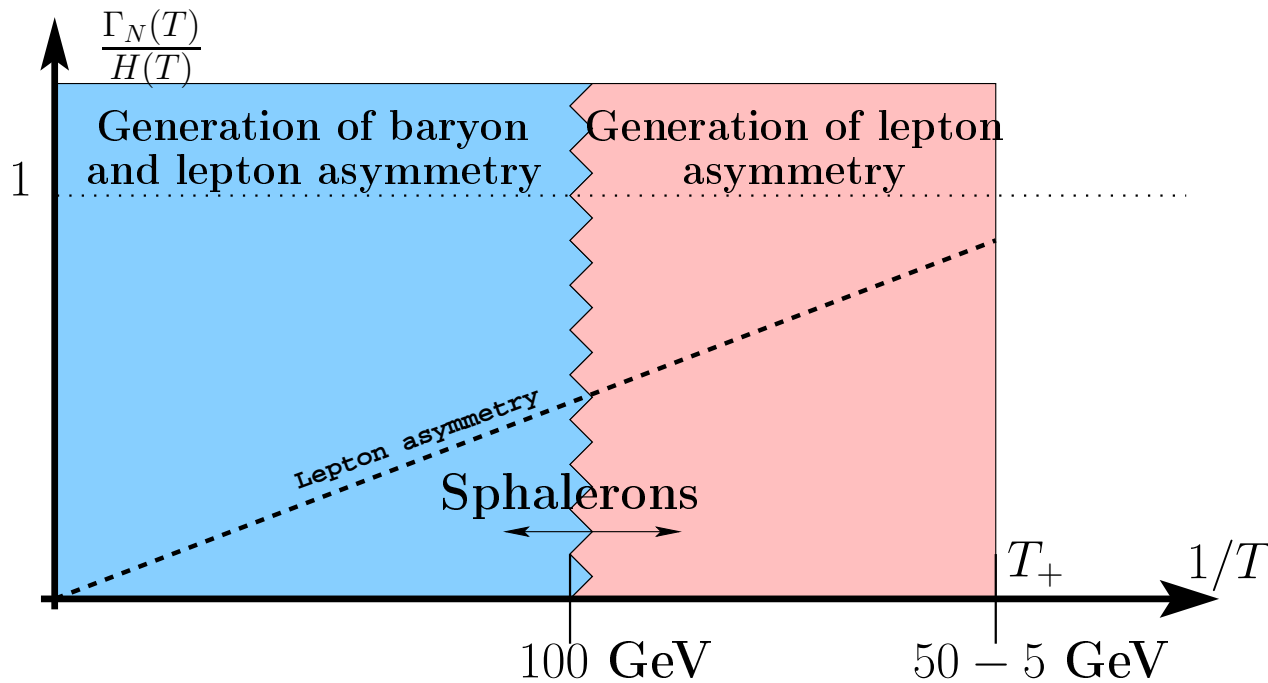
⊕ Out-of-equilibrium processes  $\rightarrow$  no phase transition in the  $\nu$ MSM for  $m_H > 72$  GeV! **but Yukawa couplings of sterile neutrinos are small enough to keep them out of thermal equilibrium at  $T \sim 100$  GeV**

Kajantie et al.  
(1996)

Asaka,  
Shaposhnikov  
(2005)

**Baryogenesis in the  $\nu$ MSM goes through leptogenesis**

# Baryo- and lepto-genesis in the $\nu$ MSM



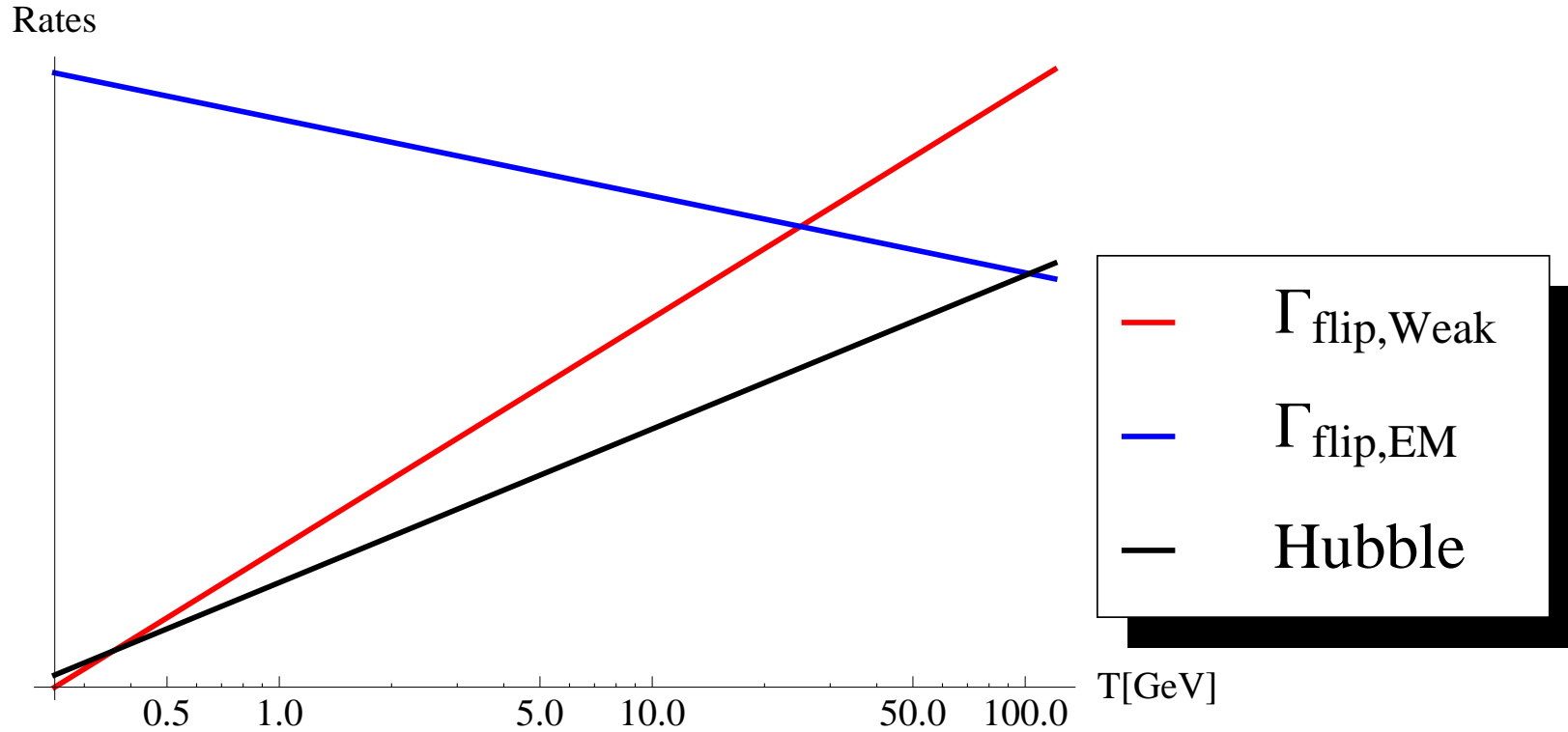
- At  $T > T_{\text{sph}}$  lepton asymmetry **gets converted** “on-the-fly” to baryon asymmetry by sphalerons — **baryogenesis**
- At  $T_{\text{sph}} > T > T_+$  lepton asymmetry **continues to be generated**  
(where  $|F|^2 T_+ = \frac{T_+^2}{M}$  and the Yukawa coupling  $|F|^2 \sim \frac{M m_{\text{atm}}}{v^2}$ )
- $\Rightarrow$  In the  $\nu$ MSM  $L_{\text{tot}}(T_+) \gg B_{\text{tot}}(T_{\text{sph}})$

## Left-right asymmetry in primordial plasma

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- Classically, the number of **left** and **right** massless fermions is conserved **independently** (in particular, number of left and right **electrons** at high temperatures)
- Introduce a **chemical potential**  $\mu_{L,R}$  for each conserved quantity. The **density matrix** is  $\hat{\rho} = \exp\left(-\frac{\hat{H}}{T} + \mu_R \hat{N}_R + \mu_L \hat{N}_L\right)$  Equilibrium value of *any* quantity is determined by these numbers  $(T, \mu_L, \mu_R)$
- Left-handed **electrons**  $e_L, \bar{e}_L$  – inherit lepton asymmetry  $n_{e_L} \neq n_{\bar{e}_L}$  from active neutrinos through weak processes ( $\Gamma_{\text{Weak}} \gg \text{Hubble}$ )
- The **difference of chemical potentials**  $\Delta\mu = \mu_L - \mu_R$  in the electron sector **appears**

# Chirality flipping rates in the SM



$$\Gamma_{\text{EM}} \propto \alpha^2 T \left( \frac{m}{3T} \right)^2 \quad \Gamma_{\text{W}} \propto G_F^2 T^5 \left( \frac{m}{3T} \right)^2 \quad H(T) = \frac{T^2}{M_*}$$

$$\frac{\partial \Delta\mu}{\partial t} = -\Gamma_{\text{flip}} \Delta\mu \Rightarrow \Delta\mu \propto e^{-\Gamma_{\text{flip}} t}$$

## Source of asymmetry?

---

- Evolution of the **difference** of chemical potential:

$$\frac{\partial \Delta\mu}{\partial t} = -\Gamma_{\text{flip}} \Delta\mu + \mathcal{S}(t) + \dots$$

Chirality flipping rate

Source of left-right asymmetry

- The situation when  $\Gamma \gg H$  implies **source-tracking solution** (system forgets initial conditions)

$$\Delta\mu \approx \frac{\mathcal{S}(t)}{\Gamma}$$

works if  $\frac{\partial \log \mathcal{S}(t)}{\partial t} \ll \Gamma_{\text{flip}}$  – the faster chirality flipping the better

# Maxwell equations

- The presence of different number of left and right fermions leads to additional terms in the effective Lagrangian for gauge fields

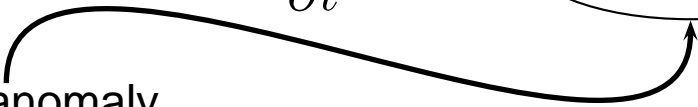
- As a result Maxwell equations get term current, proportional to  $\Delta\mu$ : Vilenkin (1978)

$$\text{curl } \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\text{curl } \vec{B} = \sigma \vec{E} + \frac{e^2}{4\pi} \Delta\mu \vec{B}$$

$$\frac{\partial \Delta\mu}{\partial t} \propto \left( \frac{e^2}{16\pi^2} \vec{E} \cdot \vec{B} \right) - \Gamma_{\text{flip}} \Delta\mu$$

Chiral anomaly



Redlich & Wjewardhana (1985);

Fröhlich et al. (2000–2001)

- If  $\Delta\mu$  is a function of  $t$  **only** Maxwell equations have an **exponentially growing solution** for **one of the two** circular polarizations  $\Rightarrow$  **helical magnetic fields**

Joyce & Shaposhnikov

Giovannini & Shaposhnikov (1998)

## CMF instability in the $\nu$ MSM

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- At  $T \geq T_+$  lepton asymmetry in the left neutrino + left-electron sector  $\Rightarrow \Delta\mu$  between left and right electrons appears...

- ...and instability quickly develops:  $B \propto e^{\lambda_k(t)}$  with

$$\lambda_{\max} = \left( \frac{\alpha \bar{\mu}/T}{2\pi} \right)^2 \frac{\eta(T)}{\sigma/T} \approx 5 \left( \frac{\bar{\mu}/T}{10^{-4}} \right)^2 \frac{100 \text{ GeV}}{T}$$

- ...generating **maximally helical** magnetic fields ...

- ...with the total energy

$$\frac{\rho_B}{T^4} = \left( \frac{\bar{\mu}}{T} \right)^3 \frac{\pi^{3/2}}{\lambda_{\max}^{1/2}} e^{\lambda_{\max}/4}$$

- ...in the wide range of length scales



## Magnetic fields in the $\nu$ MSM

---

- Magnetic fields, generated in the  $\nu$ MSM *below* 100 GeV are:
  - Maximally helical (sign of helicity determined by the sign of baryon asymmetry)
  - Energetic (magnetic energy density can be  $\sim$  total radiation density)
  - The generation occurs on subhorizon scales, but modes up to  $10^{-4}$  of the horizon (at  $T \sim 10$  GeV) can be generated)
- Their survival until today is a matter of complicated magneto-hydrodynamical evolution

The leptogenesis in the  $\nu$ MSM thus leads to the **baryogenesis** and generation of **potentially observable** cosmological magnetic fields

# Evidence for magnetic fields in voids?

Our **very preliminary** estimates show that the fields with  $B \sim 10^{-16} - 10^{-13}$  G and correlation scale 1 pc – 1 kpc can survive in the  $\nu$ MSM

Banerjee & Jedamzik (2004)

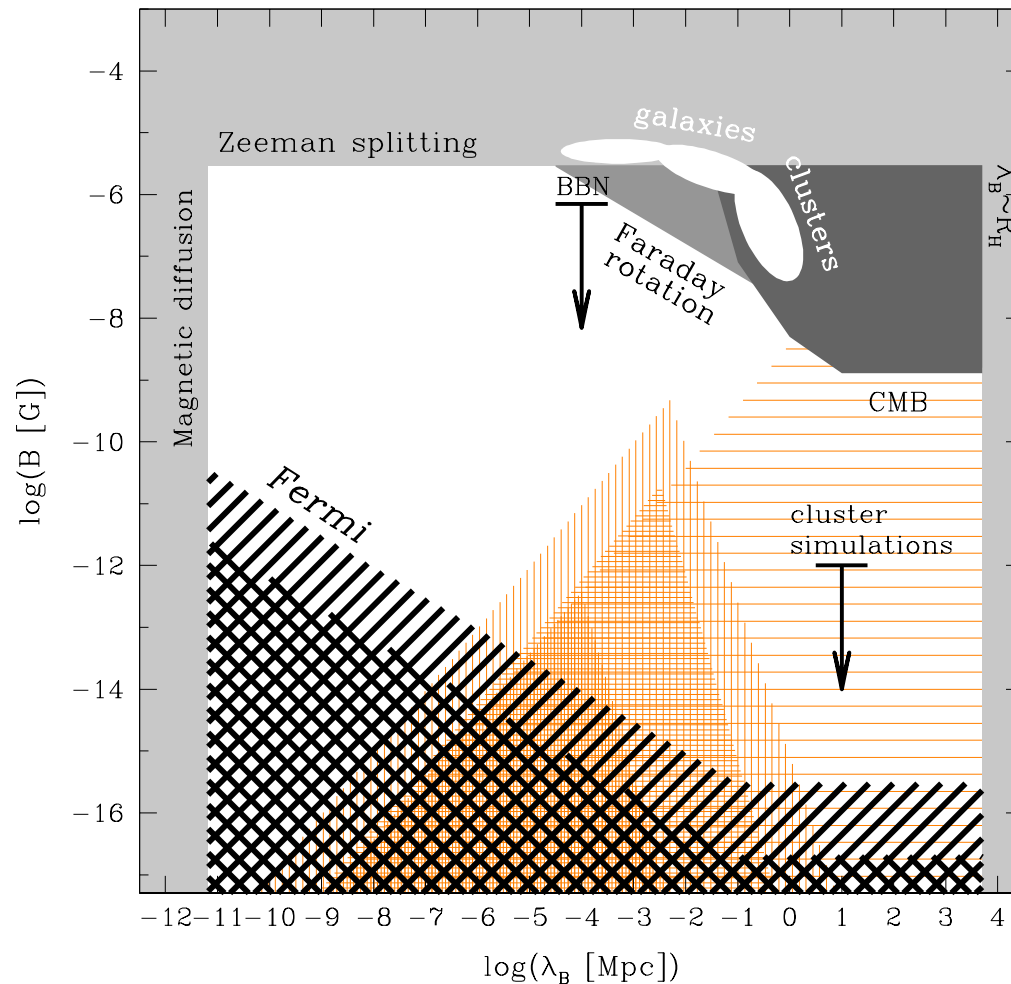
Jedamzik & Sigl (2010)

Boyarsky, O.R. *in progress*

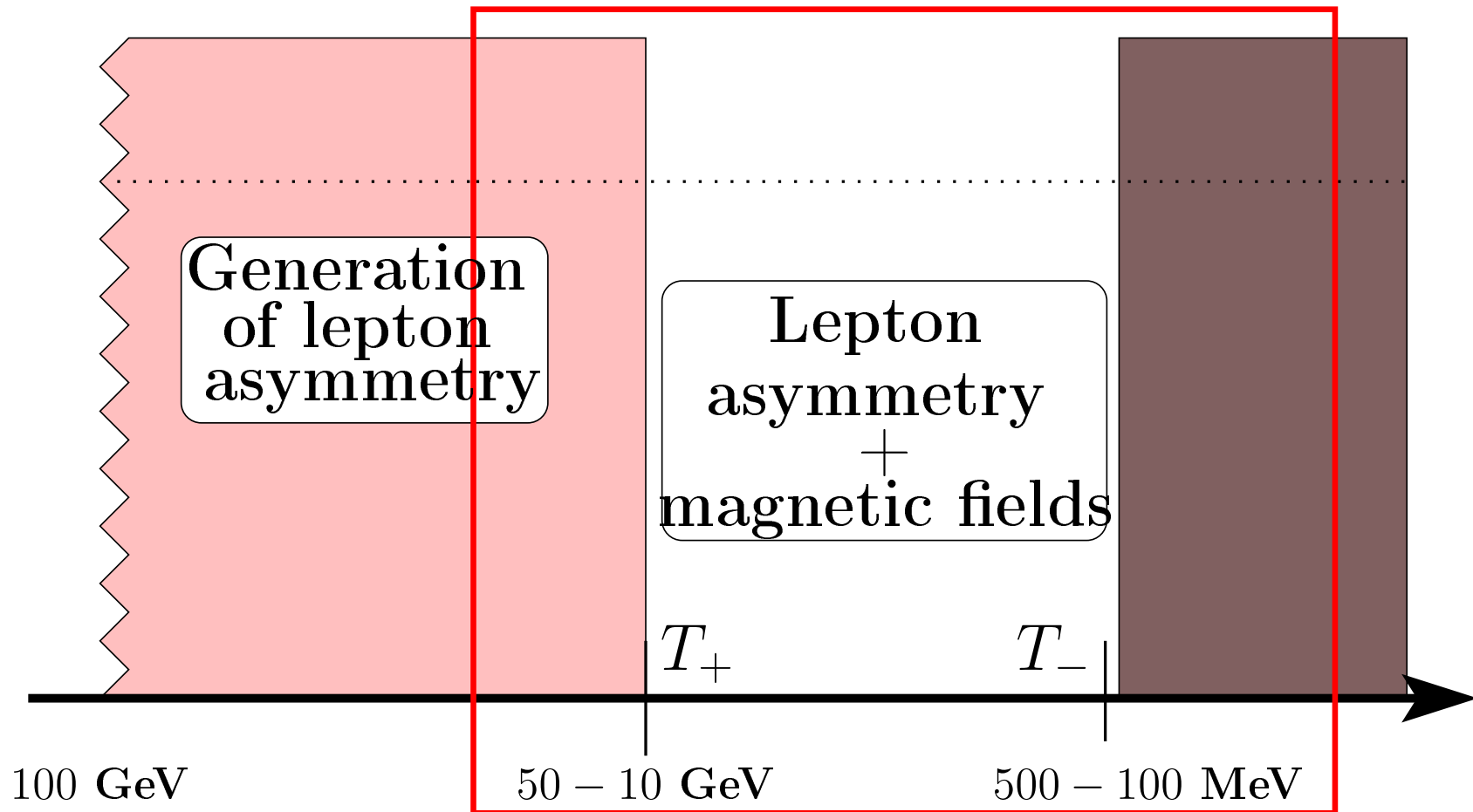
Neronov & Vovk, Science (2010);

Dolag et al. (2010);

Tavecchio et al. (2011)



# Magnetic fields and chiral asymmetry



## Magnetic fields and chiral asymmetry

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- At  $T = T_+ \sim \mathcal{O}(1)$  GeV sterile neutrino enter equilibrium with primordial plasma and the source of lepton asymmetry disappears
- The presence of **helical magnetic fields** re-generates lepton asymmetry in plasma

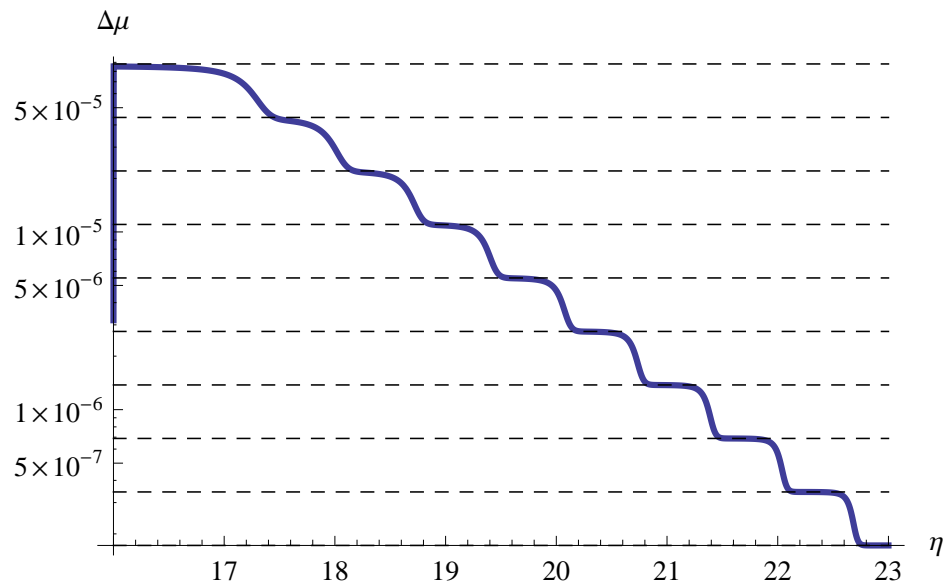
$$\begin{aligned}\frac{\partial B}{\partial t} &= \frac{1}{\sigma} \nabla^2 B + \frac{\alpha \Delta \mu}{\sigma} \text{curl } B \\ \frac{\partial \Delta \mu}{\partial t} &\propto \frac{1}{\alpha} \frac{B \times \text{curl } B}{\sigma} - \frac{\alpha \Delta \mu B^2}{\sigma} - \Delta \mu \Gamma_{\text{flip}}\end{aligned}$$

- Chemical potential settles at the level

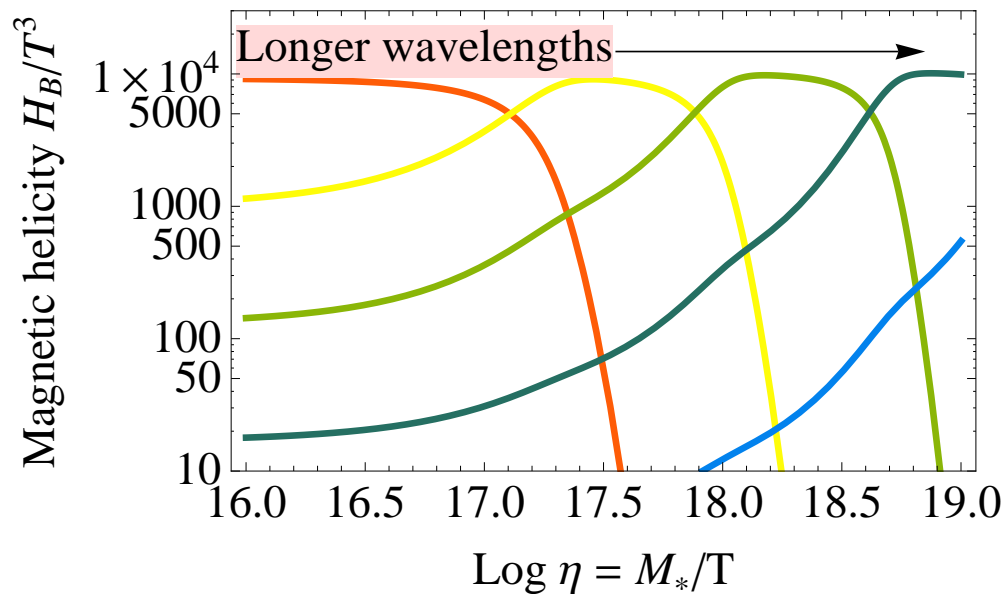
$$\Delta \mu \approx \frac{B \times \text{curl } B}{B^2 + \sigma \Gamma_{\text{flip}}}$$

- Creates **negative feedback loop** – opposes magnetic diffusion

# Chemical potential/helicity evolution

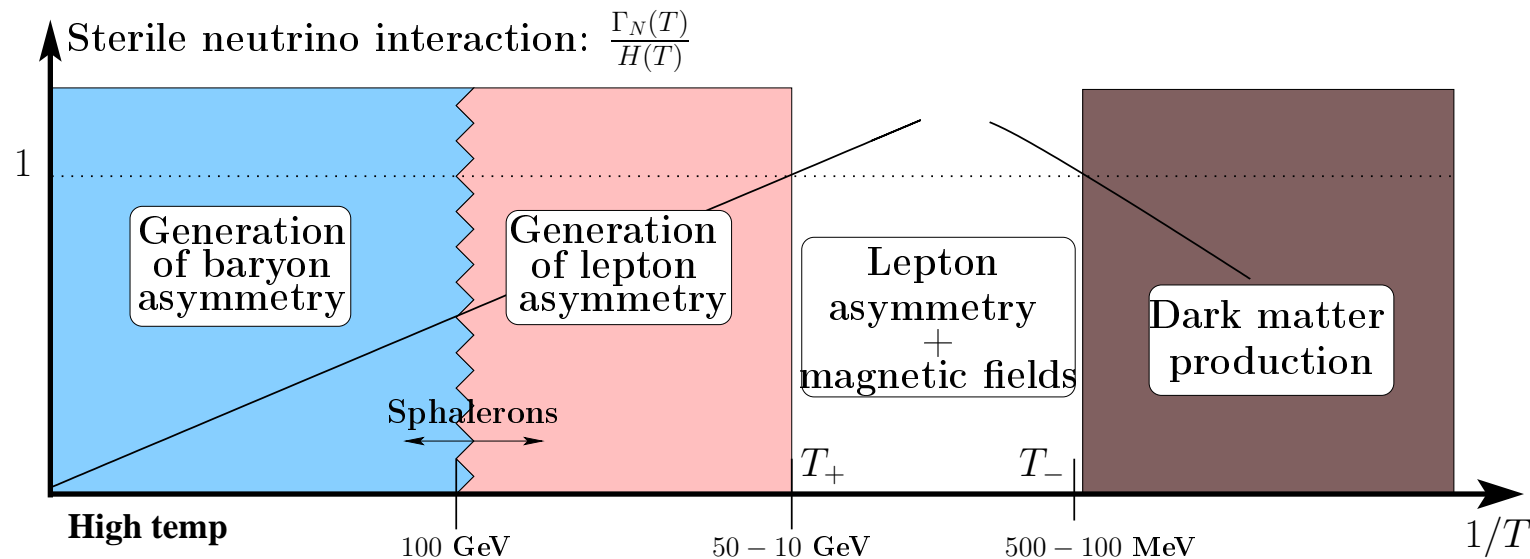


- Chemical potential is generated fast from  $\Delta\mu \approx 0$
- Then it decreases slowly in time
- Its presence undoes effects of *magnetic diffusion*



Helicity gets pumped into longer and longer modes (from red to blue colors)

# Chemical potential/helicity evolution



- Chemical potential is generated from helical magnetic fields and **survives** till temperatures  $\mathcal{O}(100)$  MeV
- Dissipation due to magnetic diffusion is **much slower than exponential**  $\Rightarrow$  Helicity and magnetic energy survive for longer. The magnetic energy/helicity spectrum **reddens**
- This whole process stops when **chirality flipping reactions** become too fast (as compared to magnetic energy density)

## Properties of sterile neutrino DM

---

- The third sterile neutrino is a **dark matter** particle in the  $\nu$ MSM
- Mass can be **anything** higher than  $\sim 300$  eV
- Can **decay** into the SM particles (with the lifetime at least  $10^{26}$  sec)
- Sterile neutrino DM never been in thermal equilibrium in the early Universe (Has a non-universal **non-thermal** spectrum of primordial velocities)
- Production sensitive to the presence of **lepton asymmetry** in plasma
- Modifies formation of structures at **sub-Mpc scales** (warm dark matter)

Tremaine &  
Gunn (1979)

Boyarsky, O.R.  
et al. (2008)

# Lifetime of sterile neutrino DM candidate

- Dominant decay channel for sterile neutrino (for  $M_s < 1$  MeV) is  $N \rightarrow 3\nu$ .

Wolfenstein  
Pal (1982)

- Life-time  $\tau = 5 \times 10^{26} \text{sec} \times \left(\frac{\text{keV}}{M_s}\right)^5 \left(\frac{10^{-8}}{\theta^2}\right)^2$

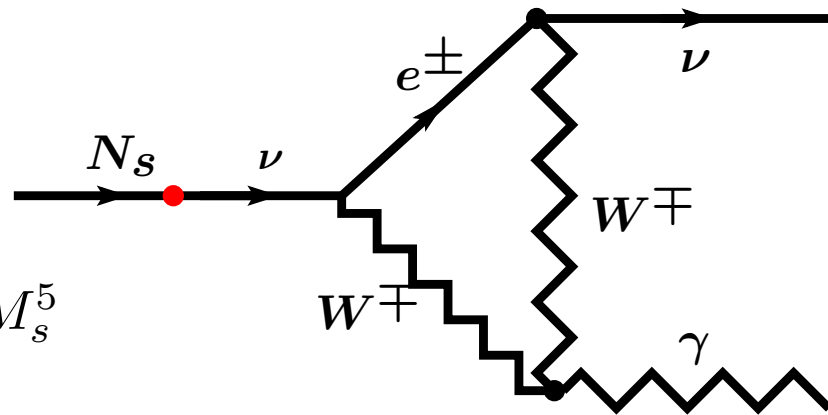
Barger Phillips  
Sarkar (1995)

- Subdominant **radiative decay channel**

– Photon energy:  $E_\gamma = \frac{M_s}{2}$

– Radiative decay width:

$$\Gamma_{\text{rad}} = \frac{9 \alpha_{\text{EM}} G_F^2}{256 \cdot 4\pi^4} \sin^2(2\theta) M_s^5$$



Dolgov  
Hansen (2000)

Abazajian  
Fuller Tucker  
(2001)

- Sterile neutrino DM **is not completely dark**. Its decay signal can be searched for in the spectra of astrophysical objects.

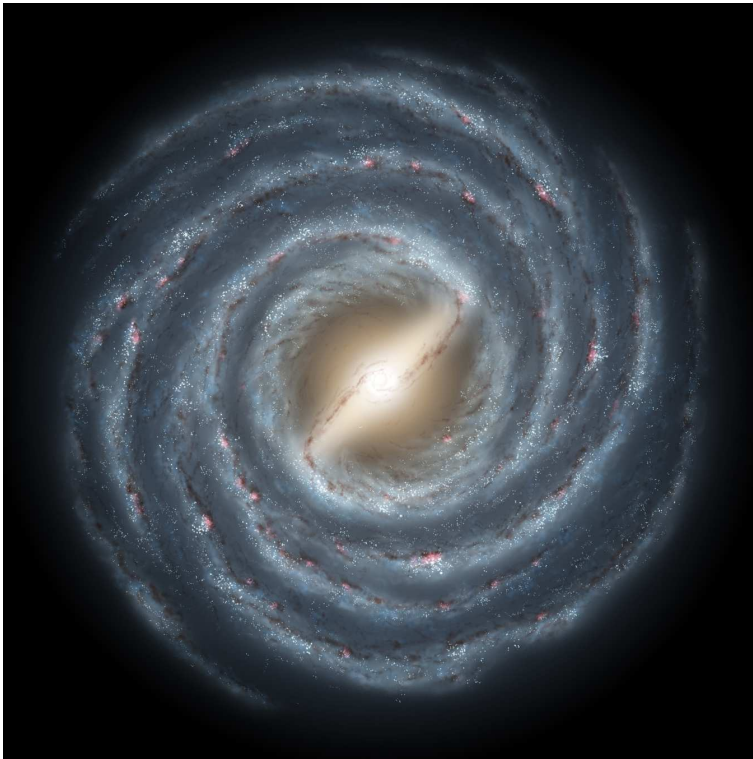
Boyarsky, O.R.  
et al.  
(2006-2009)



## Decay of sterile neutrino DM

---

- DM may be decaying with a cosmologically long life-time (age of the Universe or even longer). Can we detect such decay?
- **Yes!** if you multiply a small number (probability of decay) with a large number (typical amount of DM particles in a galaxy  $\sim 10^{70}-10^{100}$ )



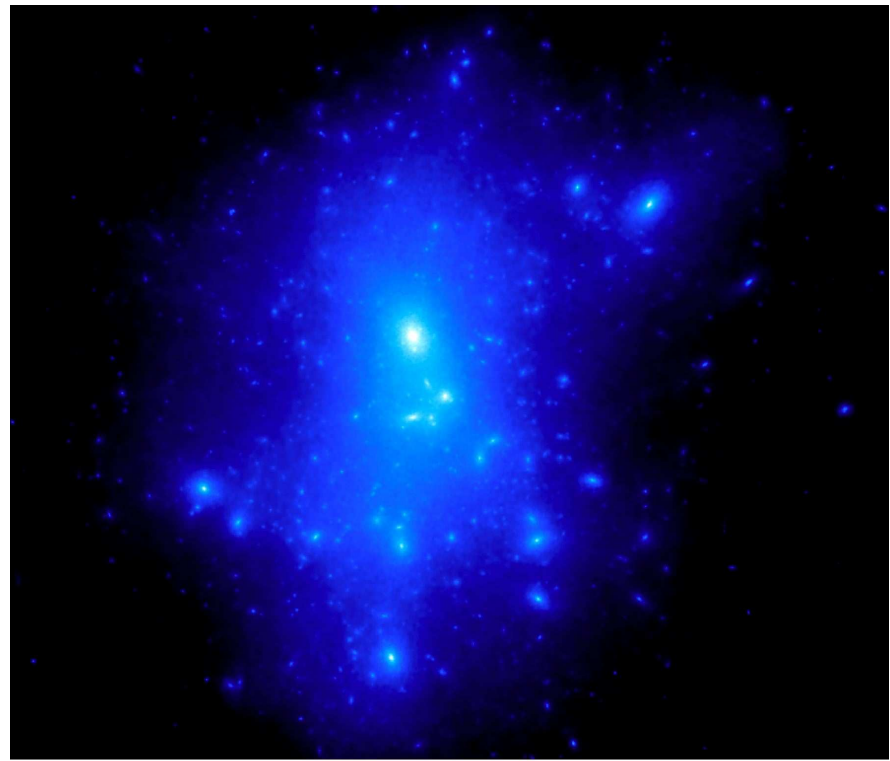
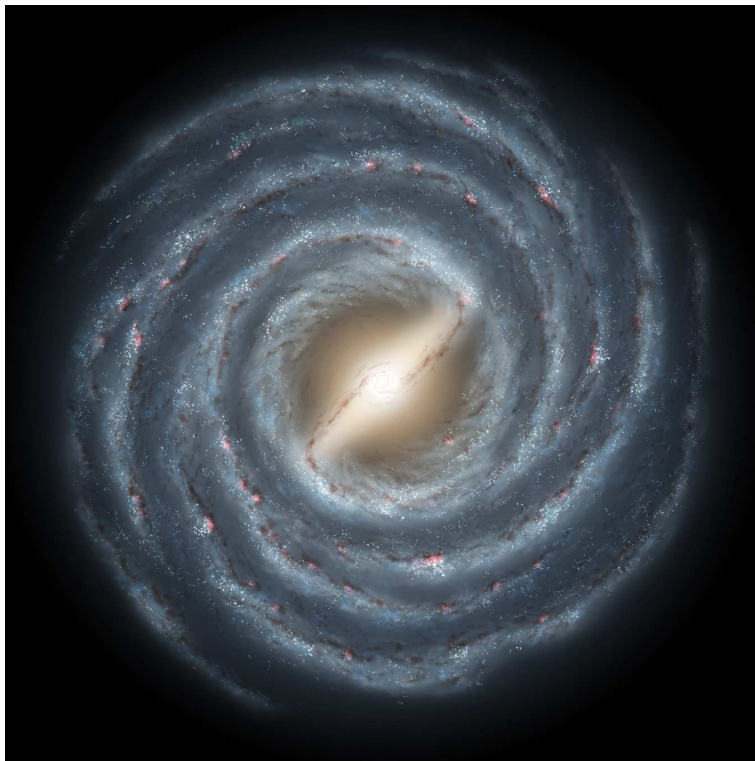
$$\text{Signal} \propto \int_{\text{line of sight}} \rho_{\text{DM}}(r) dl$$

Expected signal from the galaxy at a particular energy

## Decay of sterile neutrino DM

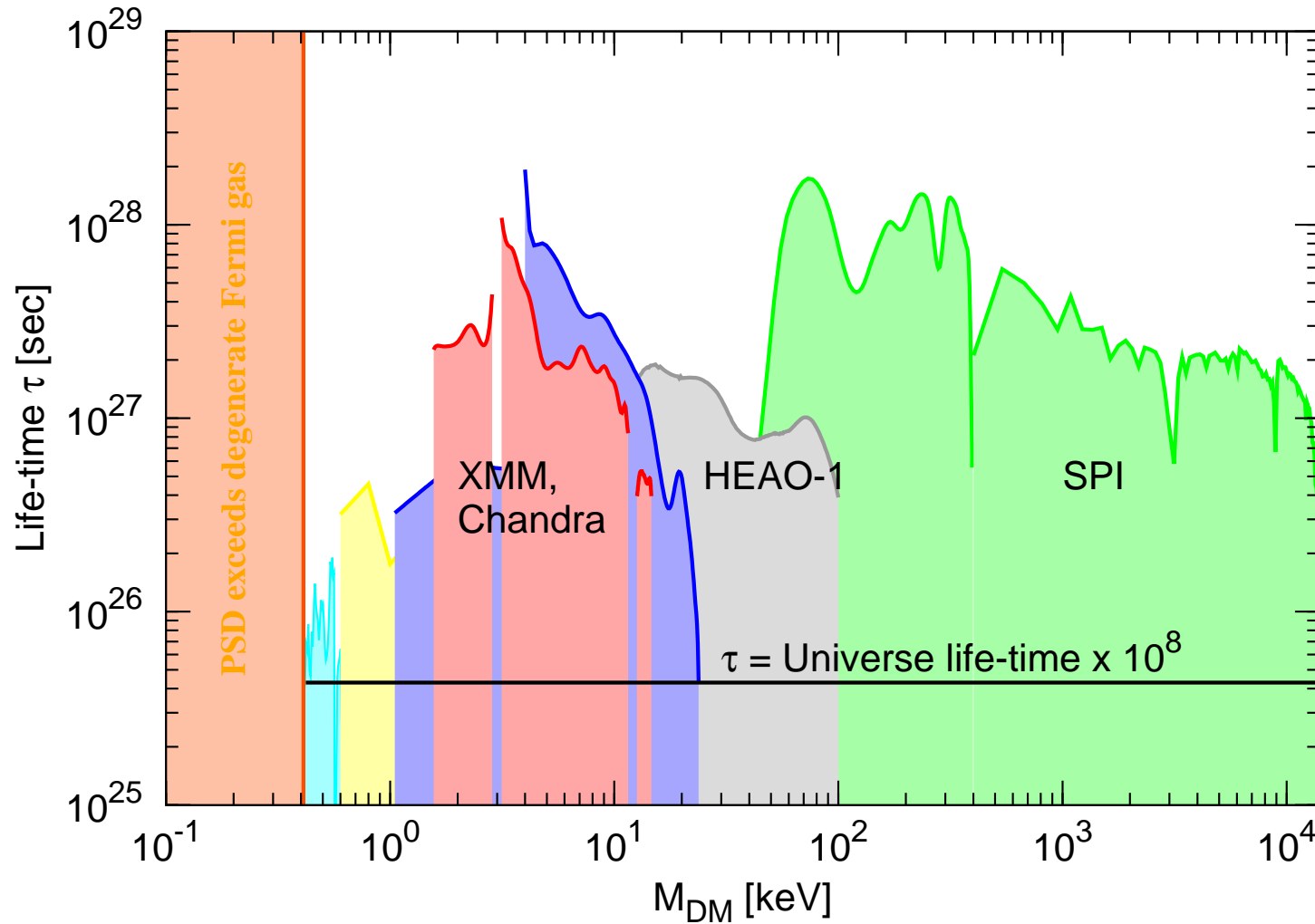
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- DM may be decaying with a cosmologically long life-time (age of the Universe or even longer). Can we detect such decay?
- **Yes!** if you multiply a small number (probability of decay) with a large number (typical amount of DM particles in a galaxy  $\sim 10^{70}-10^{100}$ )



Expected signal from a galaxy at a particular energy (simulation from B. Moore)

# Restrictions on life-time of decaying DM



**MW (HEAO-1)**  
 Boyarsky, O.R.  
 et al. 2005

**Coma and Virgo clusters**  
 Boyarsky, O.R.  
 et al.

**Bullet cluster**  
 Boyarsky, O.R.  
 et al. 2006

**LMC+MW(XMM)**  
 Boyarsky, O.R.  
 et al. 2006

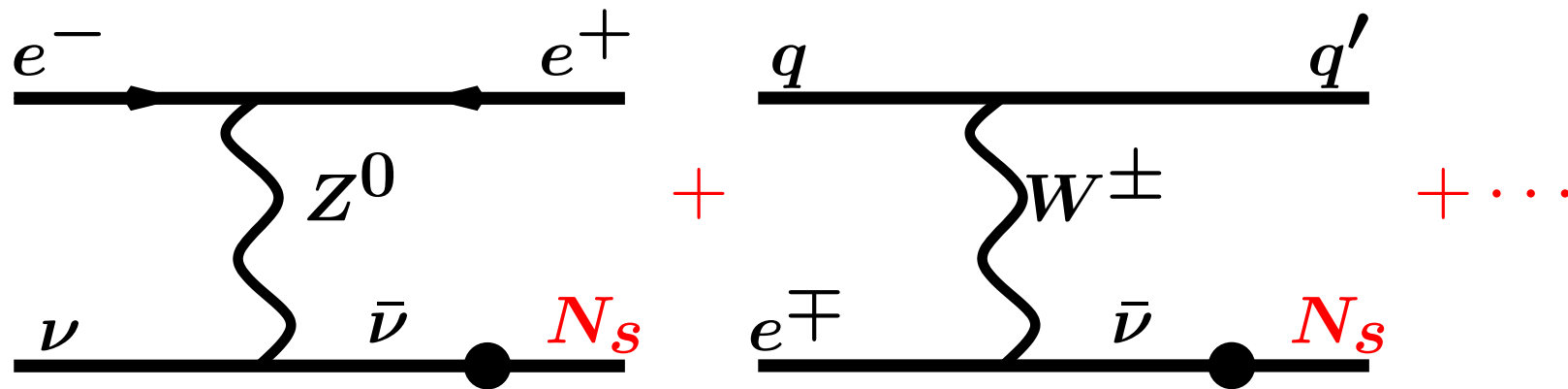
**MW Riemer-Sørensen et al.; Abazajian et al.**

**MW (XMM)**  
 Boyarsky, O.R.  
 et al. 2007

**M31 Watson et al. 2006; Boyarsky et al. 2007**

Results of almost **20** published works.

## Production through mixing



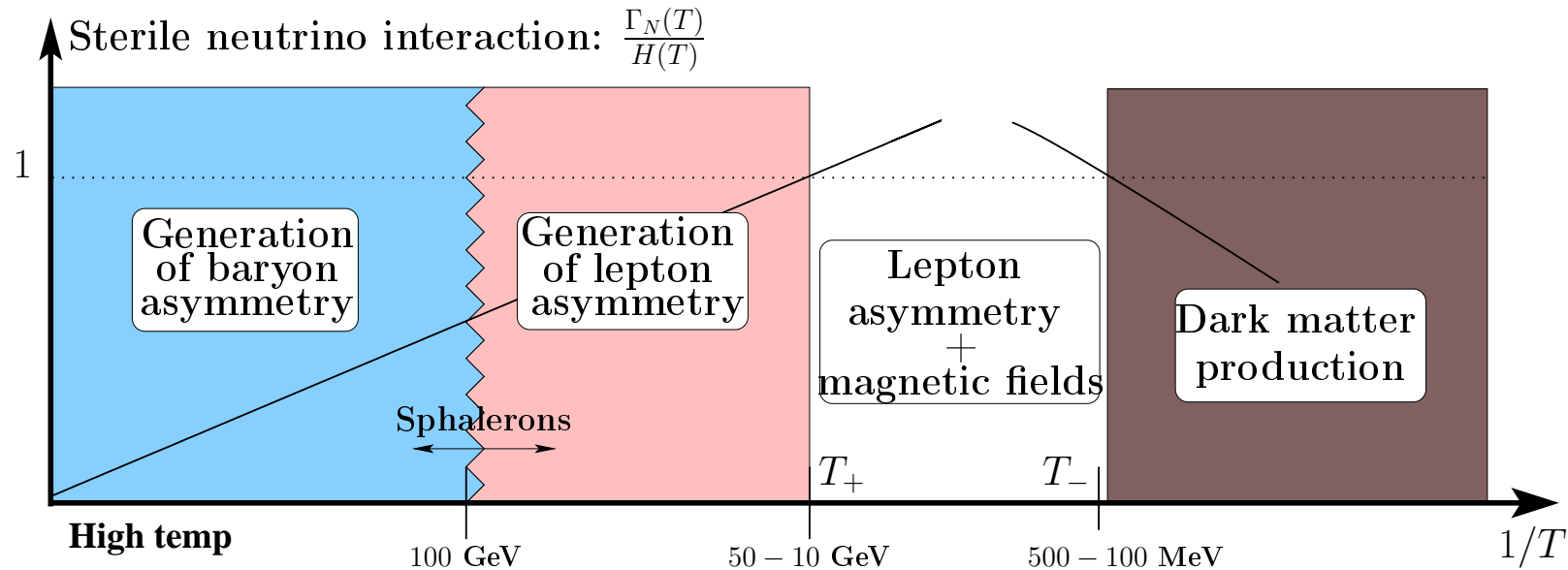
- Sterile neutrinos have **non-equilibrium spectrum of primordial velocities**, roughly proportional to the spectrum of active neutrinos

$$f_s(p) \propto \frac{\theta^2}{\exp\left(\frac{p}{T_\nu(t)}\right) + 1}$$

- Production is sharply peaked at

$$T_{\max} \simeq 130 \left( \frac{M_s}{\text{keV}} \right)^{1/3} \text{ MeV}$$

# Resonant production

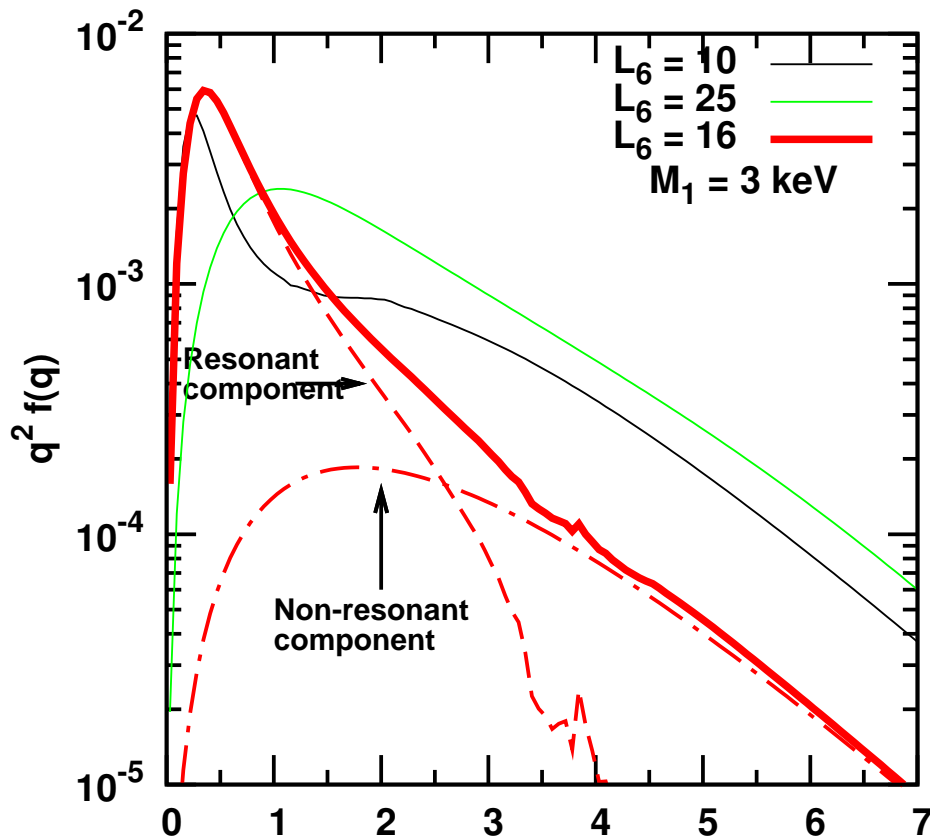


- The lepton asymmetry gets carried over to by magnetic fields
- The presence of lepton asymmetry in primordial plasma at  $T \sim \mathcal{O}(100)$  MeV makes active-sterile mixing much more effective – Shi Fuller'98  
**resonant production** of sterile neutrino dark matter  
 Laine, Shaposhnikov

# RP sterile neutrino spectra

In the minimal model explaining neutrino oscillations and dark matter (3 sterile neutrinos and nothing more), sterile neutrino DM has spectrum with **two components**:

Laine,  
Shaposhnikov  
Boyarsky,  
O.R.,  
Shaposhnikov



- Maximal amount of DM produced resonantly:

$$\Omega_{\text{RP}} h^2 \propto M_{\text{DM}} \times \frac{n_\nu - n_{\bar{\nu}}}{n_\nu + n_{\bar{\nu}}}$$

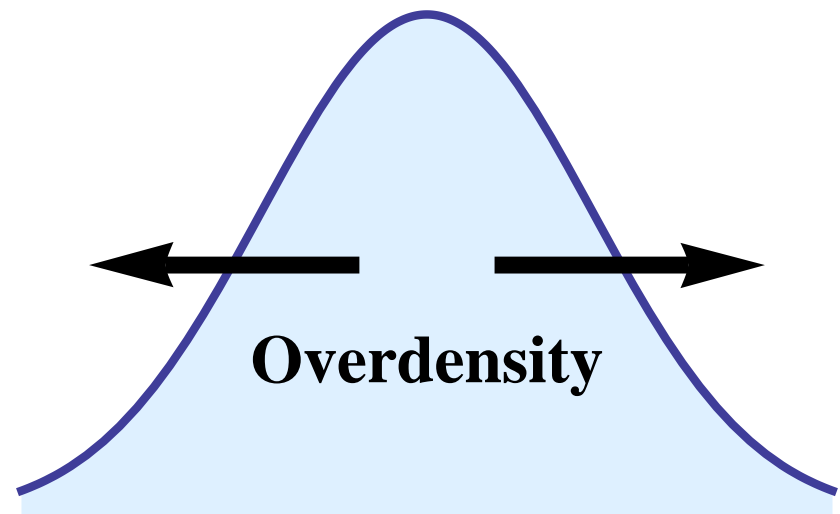
- Colder (**resonant**) component with  $\langle p \rangle \ll T_\nu$
- Warmer (**non-resonant**) component with  $\langle p \rangle \sim 3T_\nu$

# Free-streaming

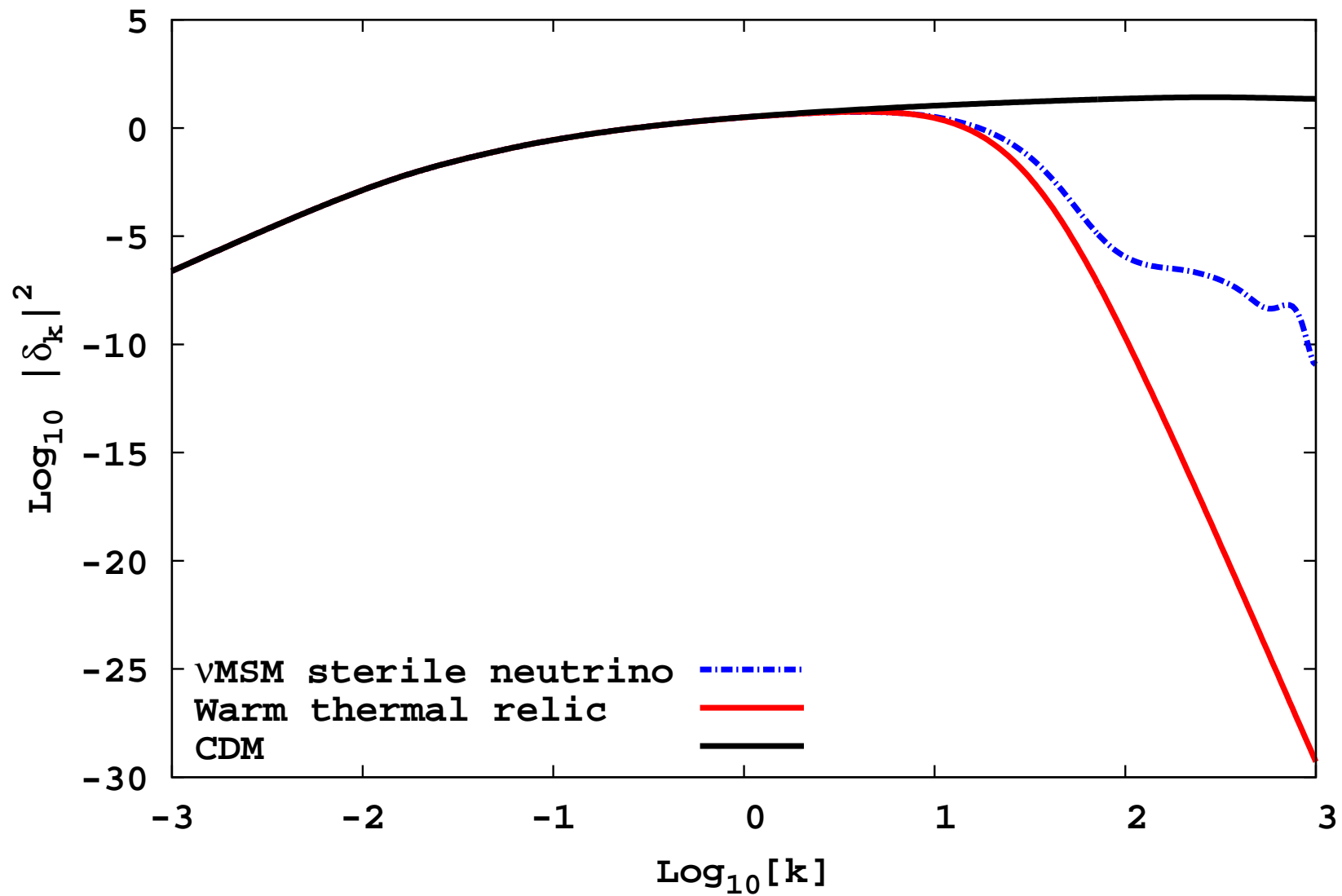
- Sterile neutrino DM is produced at temperatures  $T \sim 100$  MeV (for masses  $\sim$  keV – created relativistic  $\Rightarrow$  **warm dark matter**)
- Relativistic particles **free stream** out of overdense regions and smooth primordial inhomogeneities
- Power spectrum of primordial density perturbations is suppressed at scales below **free-streaming horizon**
- Scales of interest:

$$\lambda_{FS}^{co} \sim 1 \text{ Mpc} \left( \frac{\text{keV}}{M_{\text{sterile}}} \right)$$

$$\lambda_{FS}^{co} = \int_0^t \frac{v(t') dt'}{a(t')}$$



# Suppression of power spectrum





# How to probe primordial velocities?

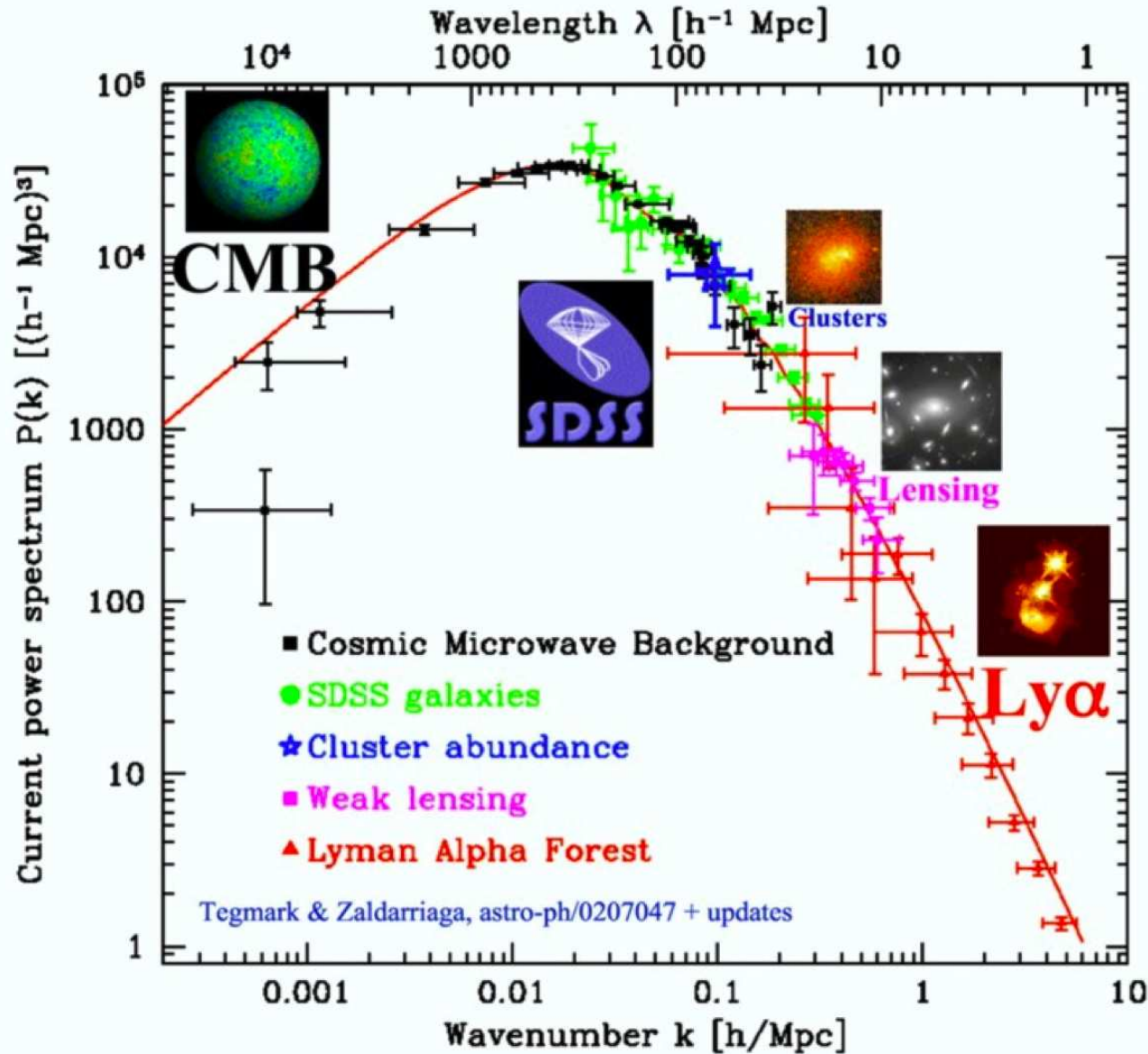
---

- Primordial velocities **affect**:
  - **Power-spectrum** of density fluctuations (suppress normalization at large scale)
  - **Halo mass function** (number of halos of small mass decreases)
  - Dark matter **density profiles** in individual objects
- Scales probed by CMB and LSS experiments (linear regime of perturbation growth)

$$k \simeq \ell \times \frac{H_0}{2} = \frac{\ell}{6000} \frac{h}{\text{Mpc}}$$

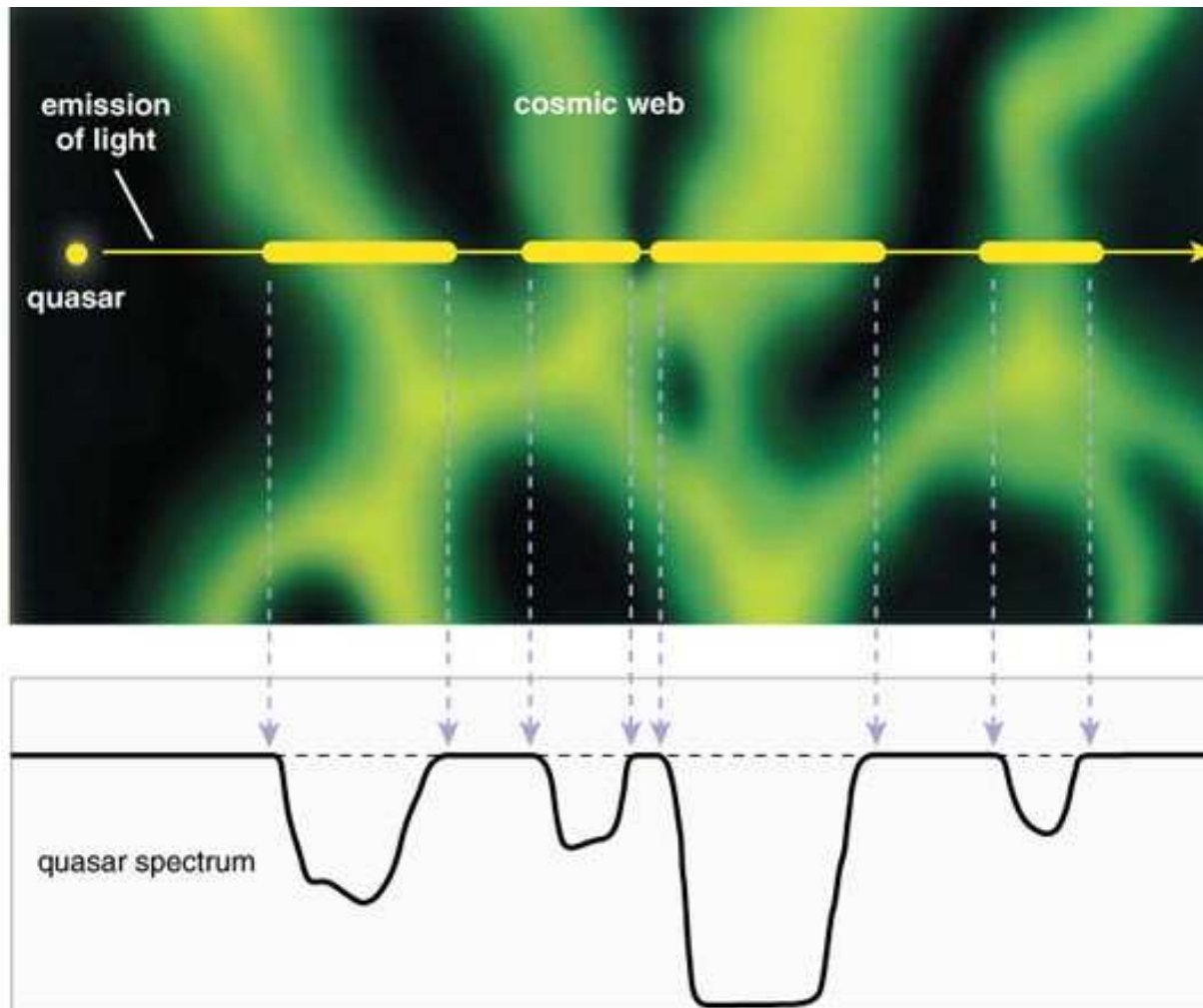
- Is sensitive up to scales  $k \lesssim 0.1 h / \text{Mpc}$
- Smaller scales? Non-linear stage of structure formation

# How to measure power spectrum



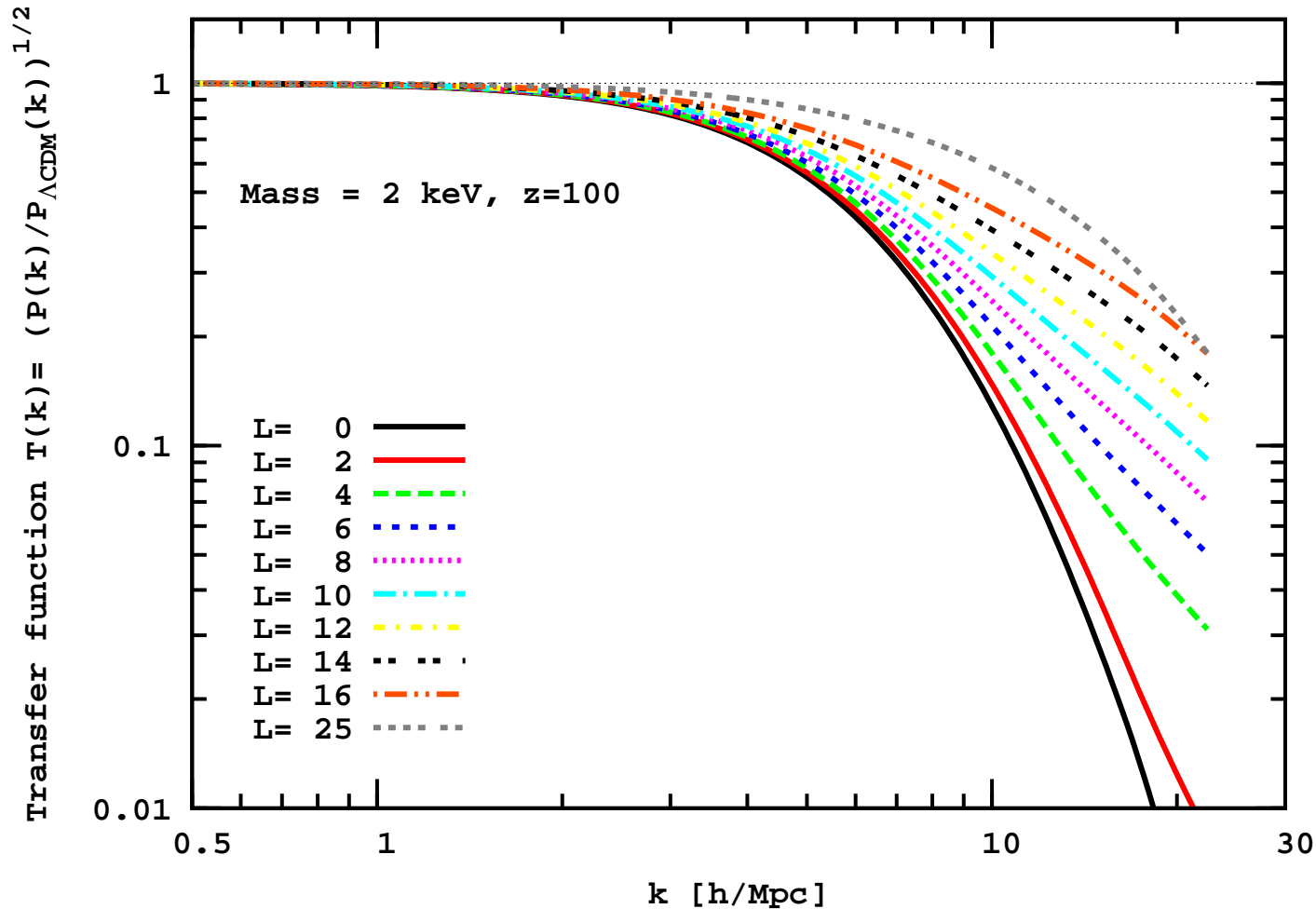
Max Tegmark  
Univ. of Pennsylvania  
max@physics.upenn.edu  
TAUP 2003  
September 5, 2003

# Lyman- $\alpha$ forest and cosmic web



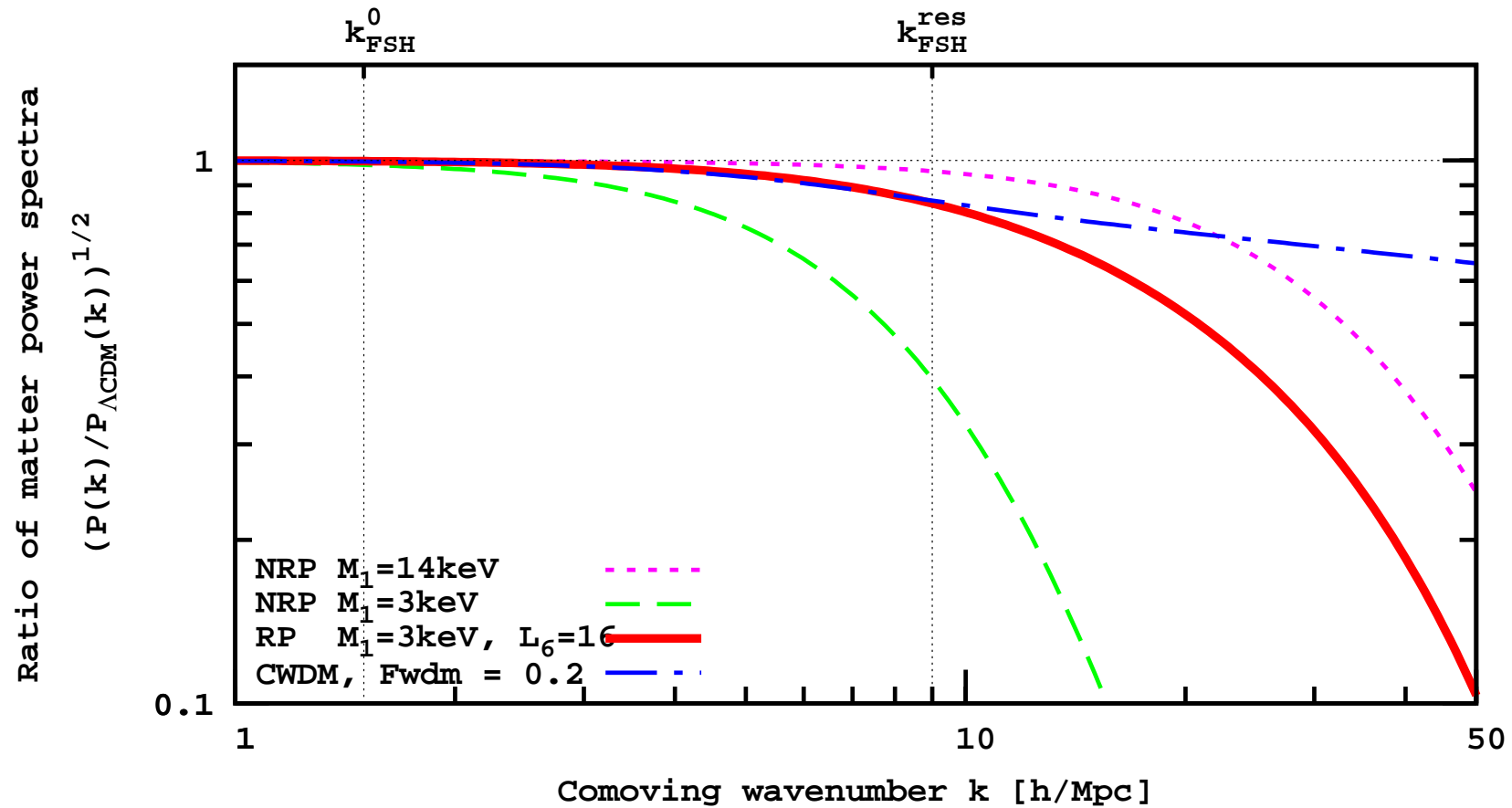
Neutral hydrogen in intergalactic medium is a tracer of overall matter density. Scales  $0.3h/\text{Mpc} \lesssim k \lesssim 3h/\text{Mpc}$

# Free-streaming of sterile neutrino DM



**Transfer functions** of resonantly produce sterile neutrinos with the mass 2 keV, produced at different lepton asymmetries

# Power spectrum for sterile neutrinos



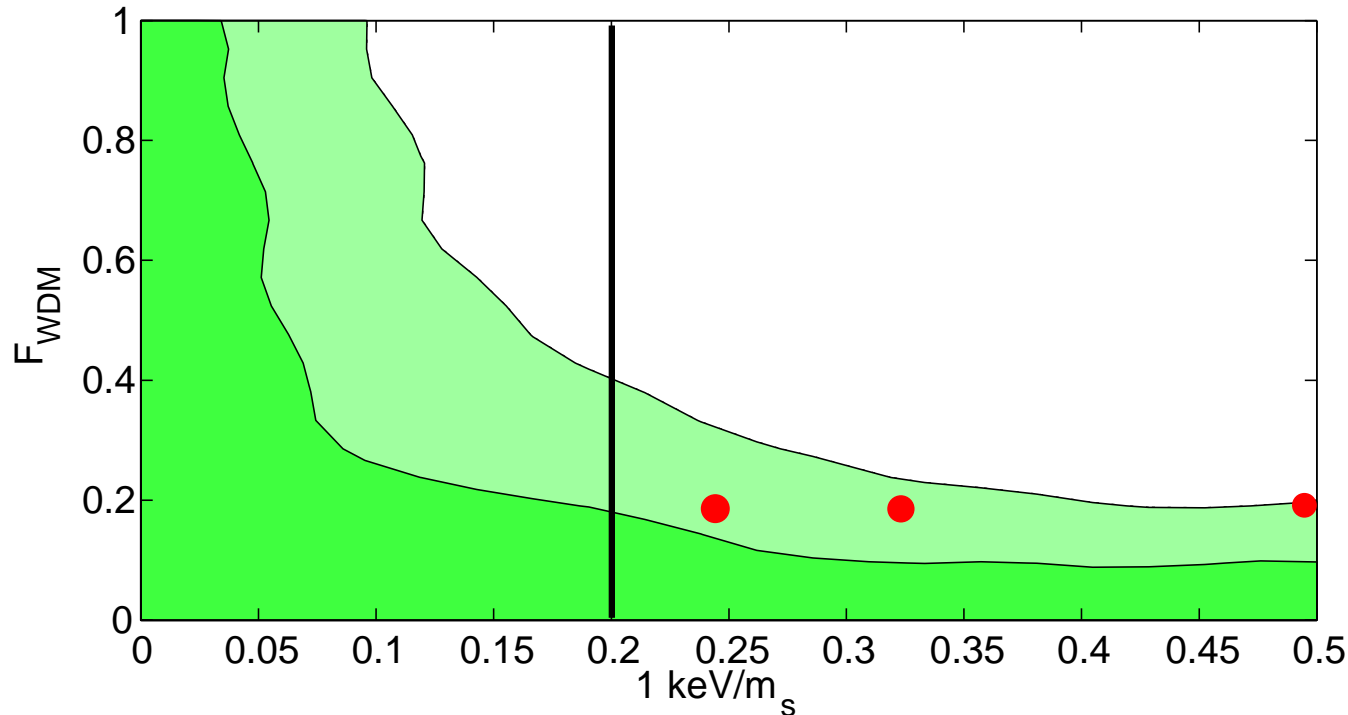
Boyarsky, Lesgourgues, **O.R.**, Viel JCAP, PRL 2009;

Boyarsky, **O.R.**, Shaposhnikov Ann. Rev. Nucl. Part. Sci. 2009

# Lyman- $\alpha$ bounds for sterile neutrinos

- Revised version of these bounds in CDM+WDM (mixed, CWDM) models demonstrates that
  - The primordial spectra **are not described by free-streaming**
  - There exist viable models with the masses as low as 2 keV

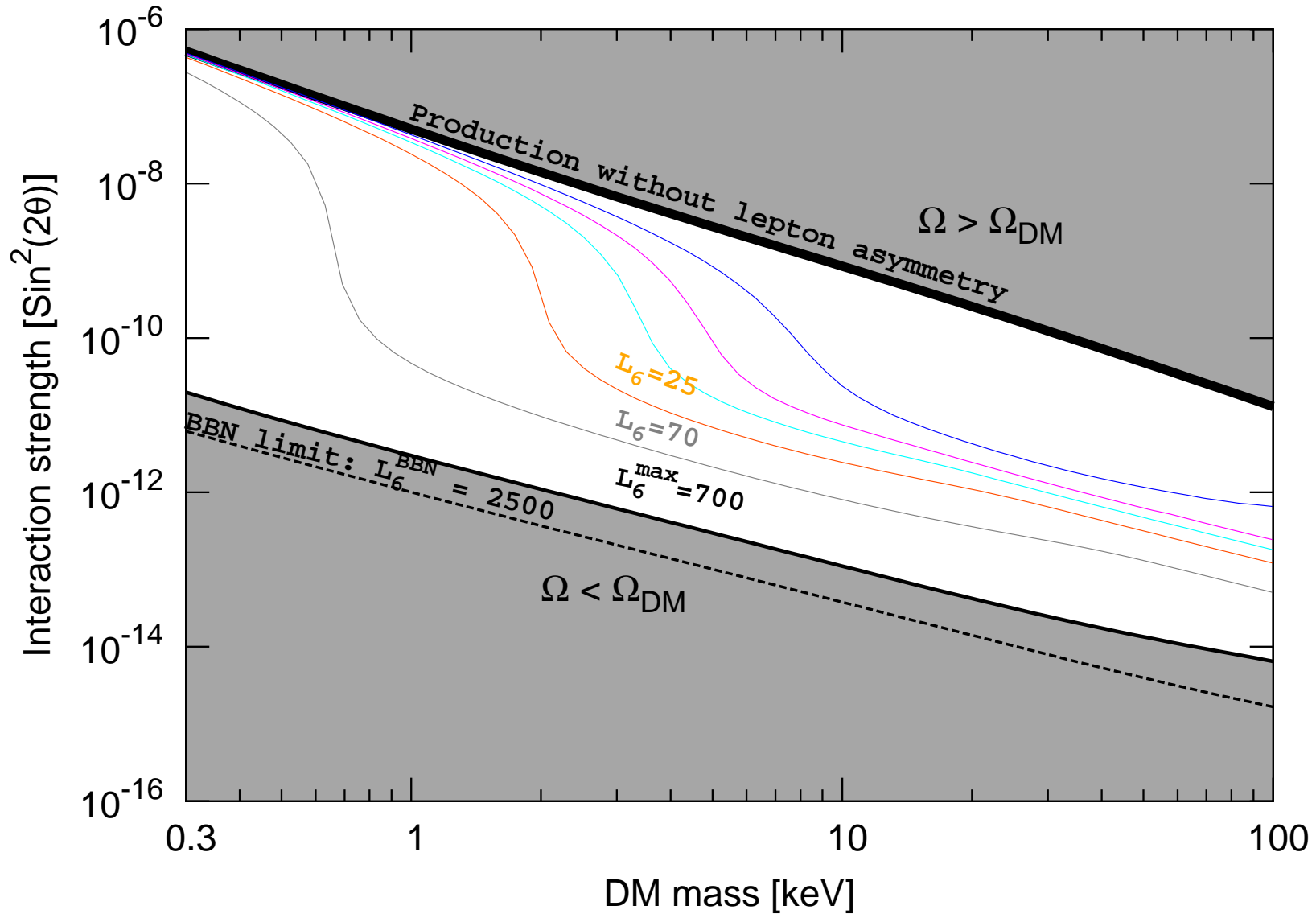
Boyarsky,  
O.R.,  
Lesgourgues,  
Viel JCAP &  
PRL (2009)



# Window of parameters of sterile neutrino DM

Asaka, Laine,  
Shaposhnikov

Laine,  
Shaposhnikov

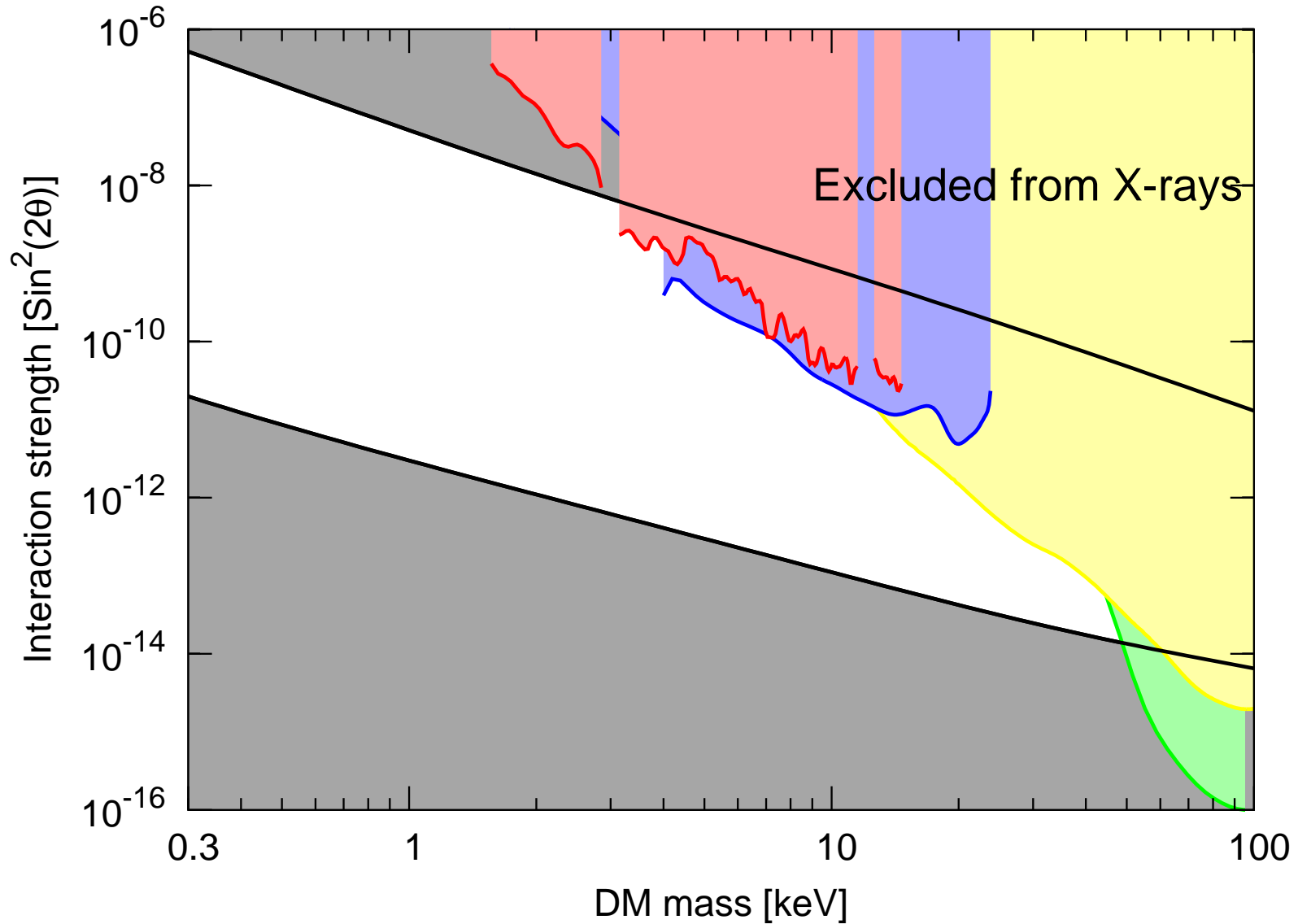


# Window of parameters of sterile neutrino DM

Asaka, Laine,  
Shaposhnikov

Laine,  
Shaposhnikov

**O.R.** and  
many others  
2005-2010



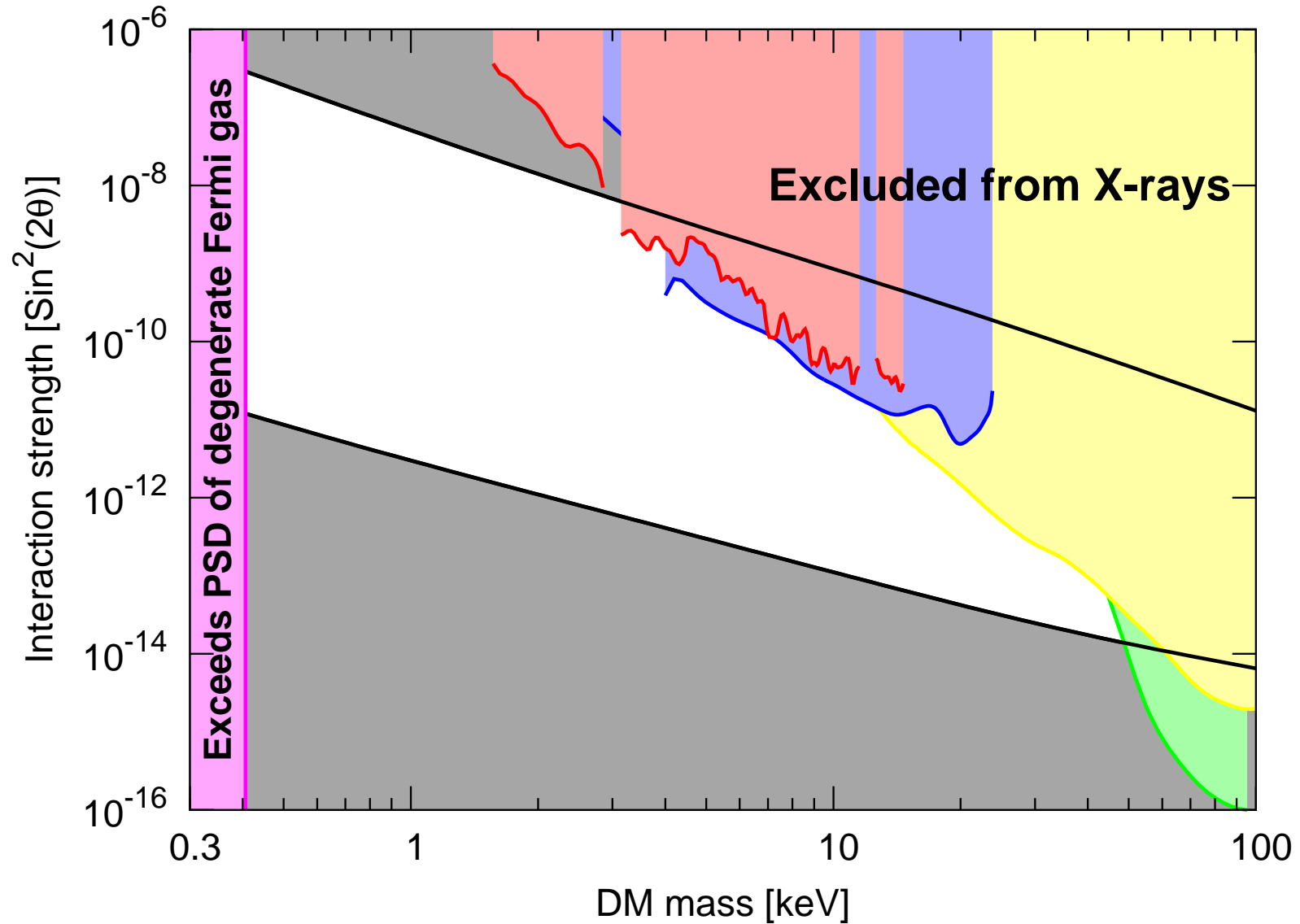


# Window of parameters of sterile neutrino DM

Asaka, Laine,  
Shaposhnikov

Laine,  
Shaposhnikov

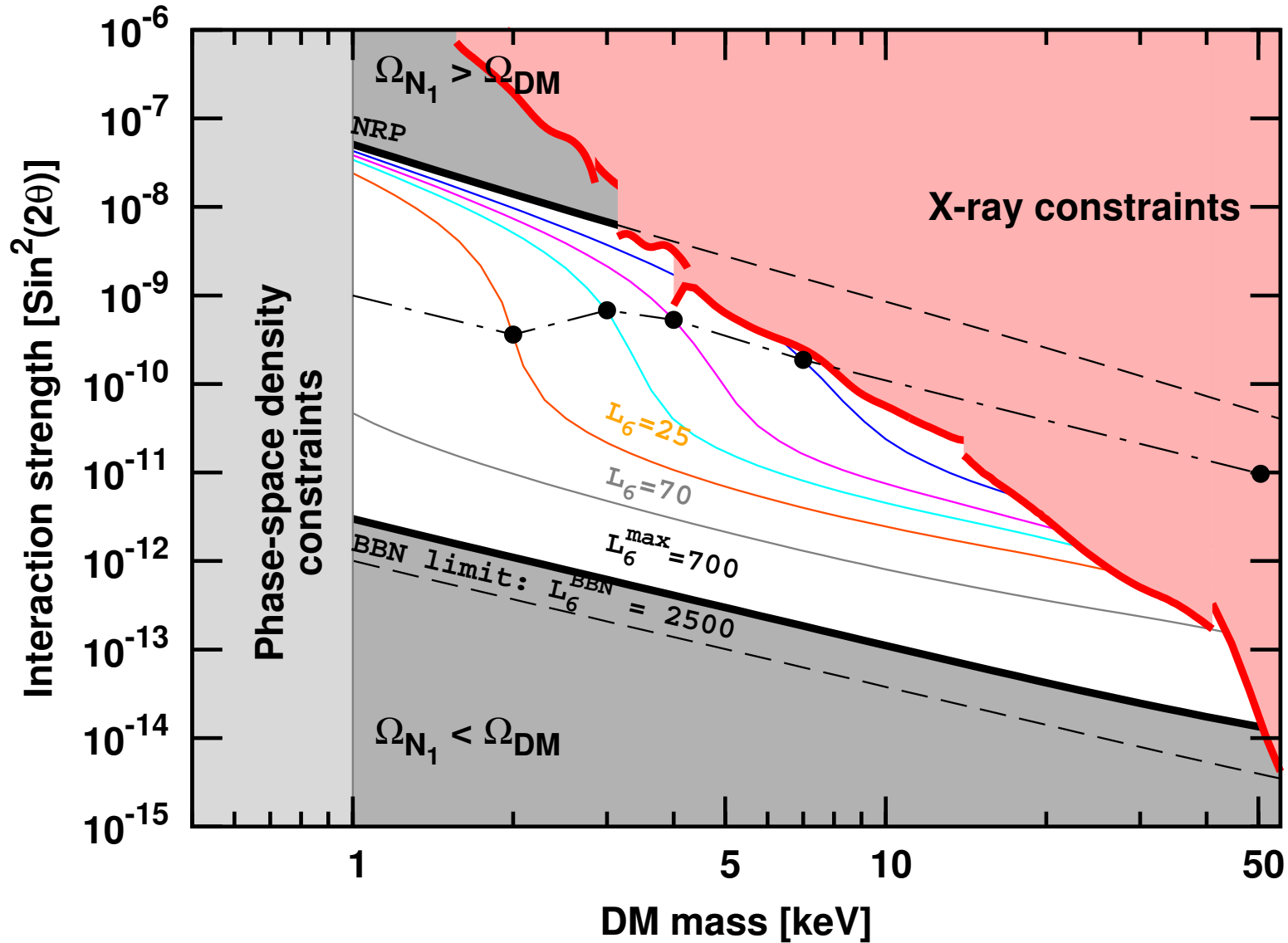
O.R. and  
many others  
2005-2010



# Sterile neutrino DM in the $\nu$ MSM

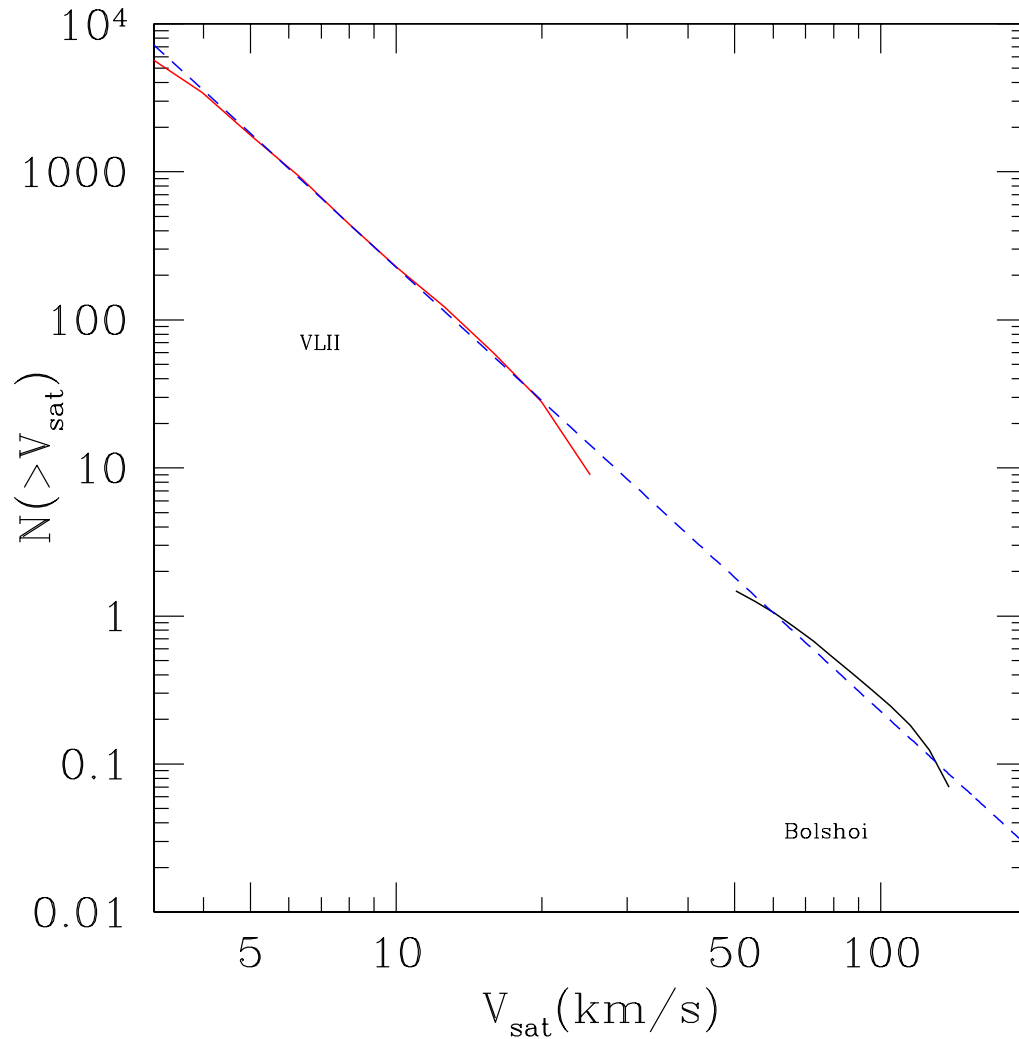
Boyarsky,  
O.R.,  
Lesgourgues,  
Viel  
[0812.3256]

Boyarsky,  
O.R.,  
Shaposhnikov  
[0901.0011]



Number of small dark matter halos  
((Sub)Halo mass function)

# CDM scale-free structures

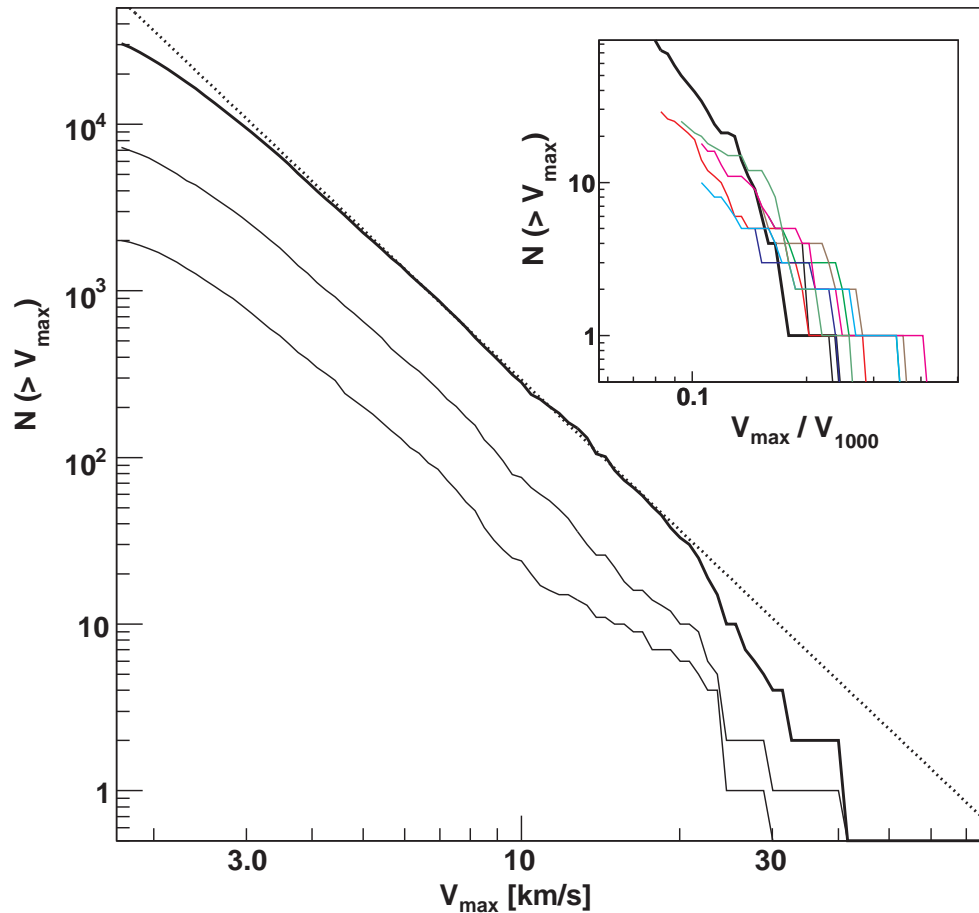


- **CDM** structures form in a scale-free manner

$$\frac{dn}{dM} \propto M^{-2}$$

- *Bolshoi* + *Via Lactea-II* simulations
- Subhlo mass function

# CDM scale-free structures

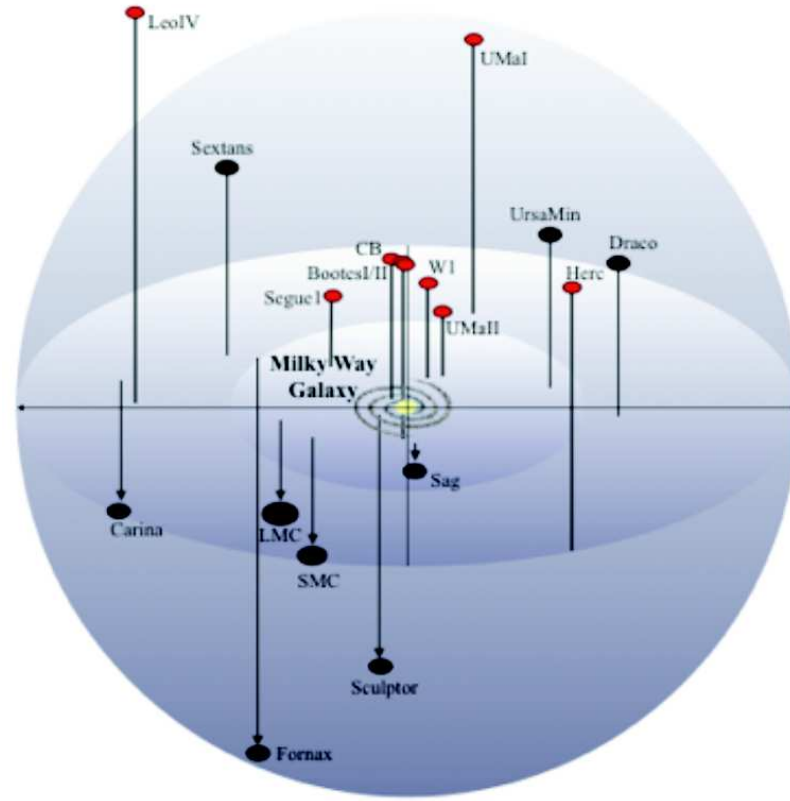
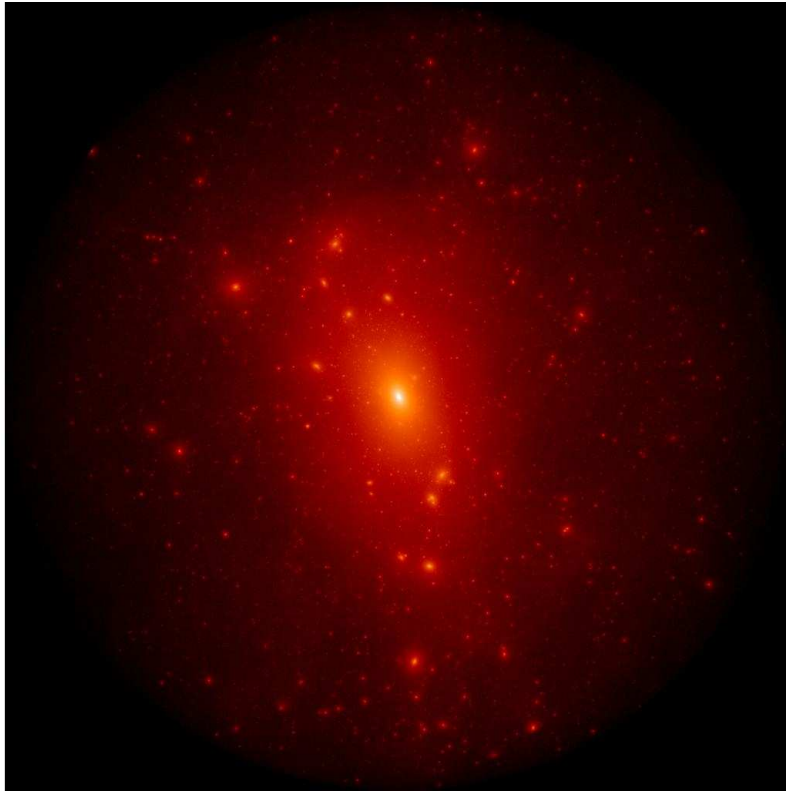


- **CDM** structures form in a scale-free manner

$$\frac{dn}{dM} \propto M^{-\alpha}, \quad \alpha \approx 2$$

- *Via Lactea-II* simulations
- Subhalo mass function
- Sub-subhalo mass function is the same as for subhalos

# Halo substructure in "cold" DM universe

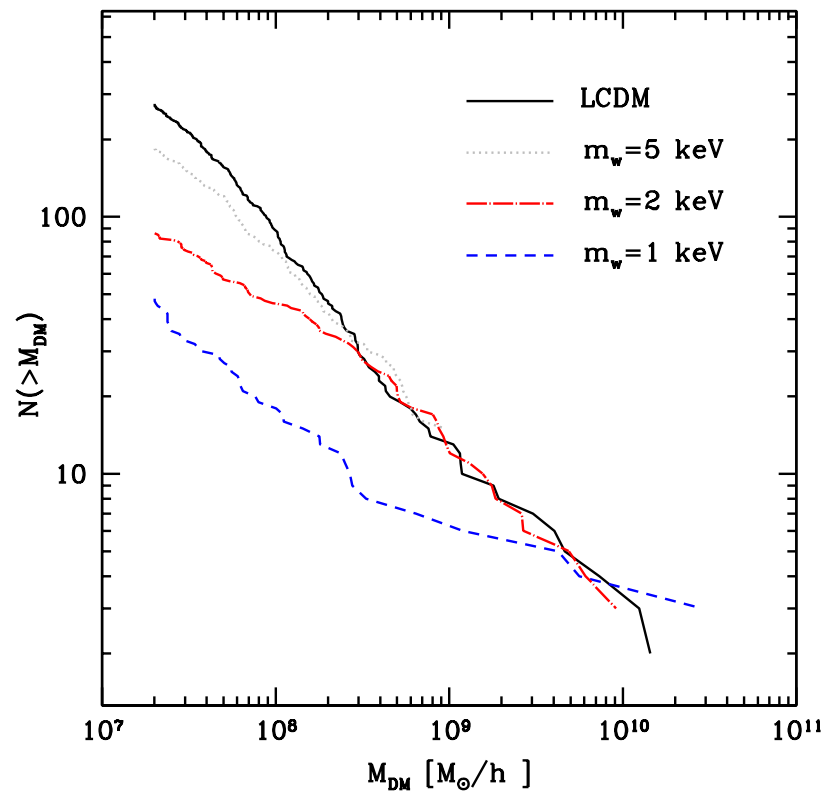


$45 \times 10^3$  substructures (Aquarius  $\sim 30$  observed substructures within our simulation) Galaxy. M. Geha 2010

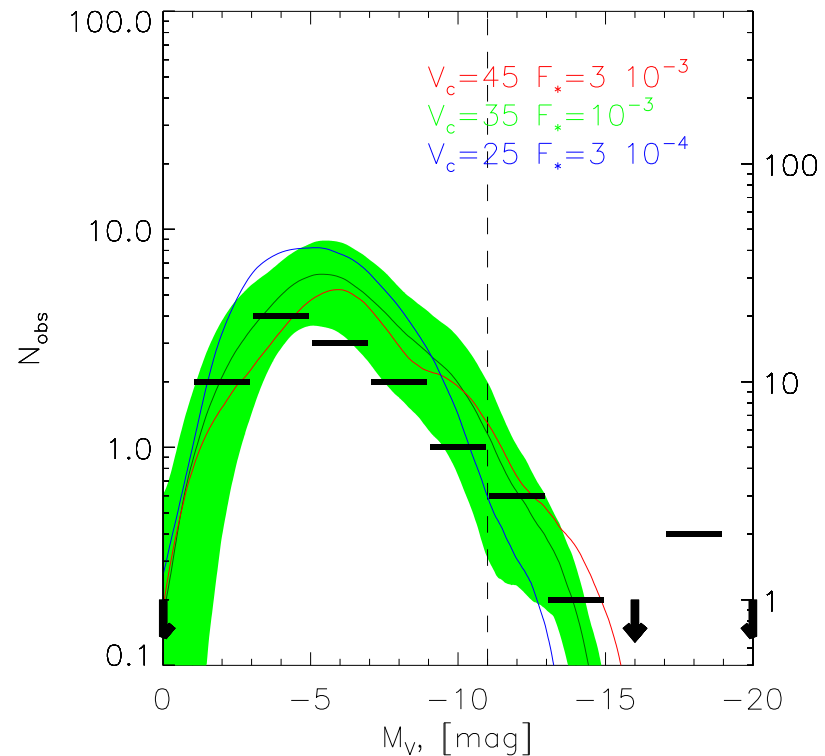
**Is small number of observed substructures due to dark matter free-streaming?** Moore et al. (1999), Klypin et al. (1999) and many others

# Mass vs. luminosity function

There can be a large bias between satellite **luminosity function** and satellite **mass function** in  $\Lambda$ CDM? [Bullock et al. \(2000\);](#)



[Benson et al. \(2002\)](#)



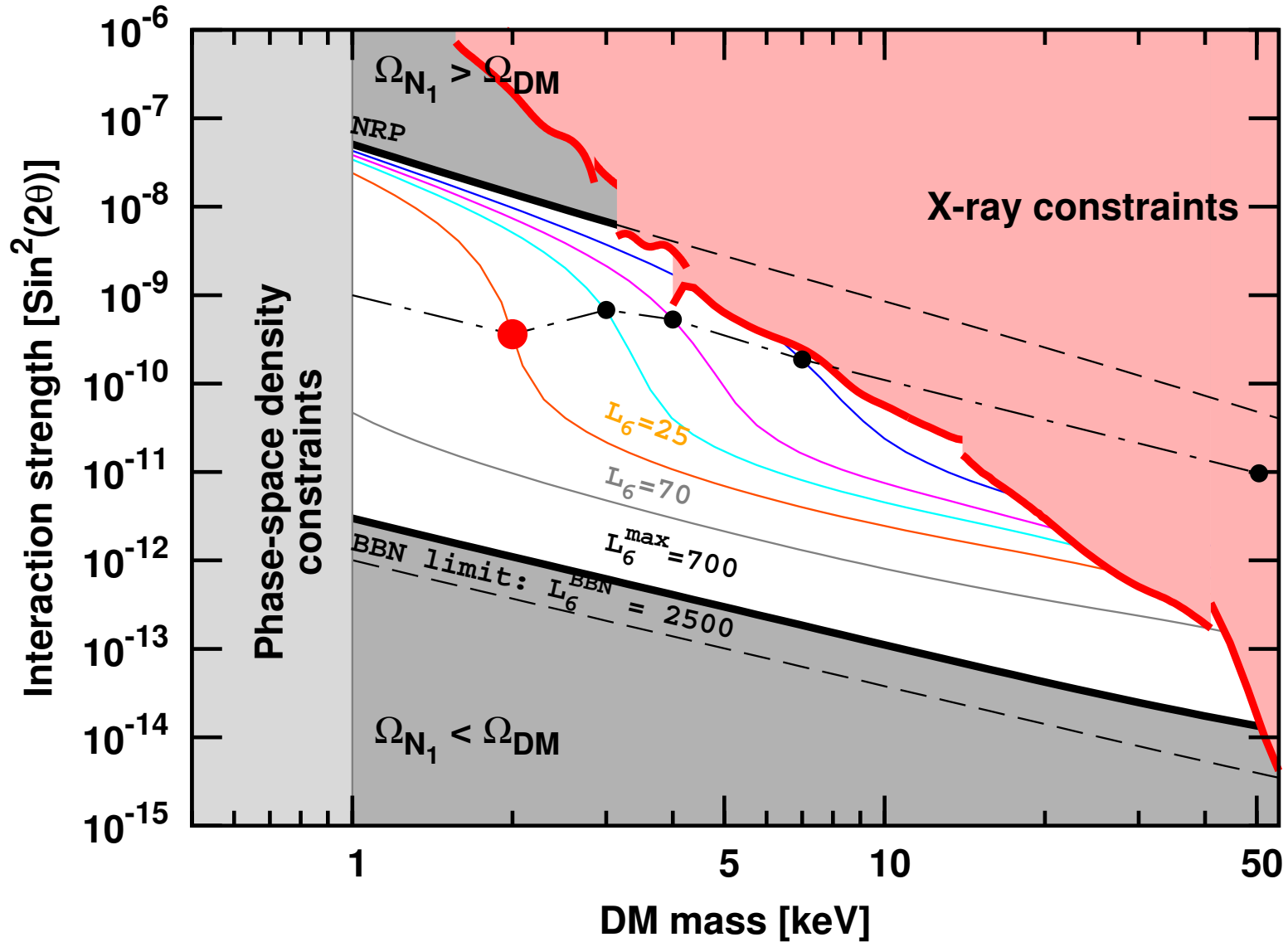
[Macciò & Fontanot'09](#)

Suppression of number of structures in [Koposov et al.'09](#)  
WDM Universe

# Sterile neutrino DM in the $\nu$ MSM

Boyarsky,  
**O.R.**,  
 Lesgourgues,  
 Viel  
 [0812.3256]

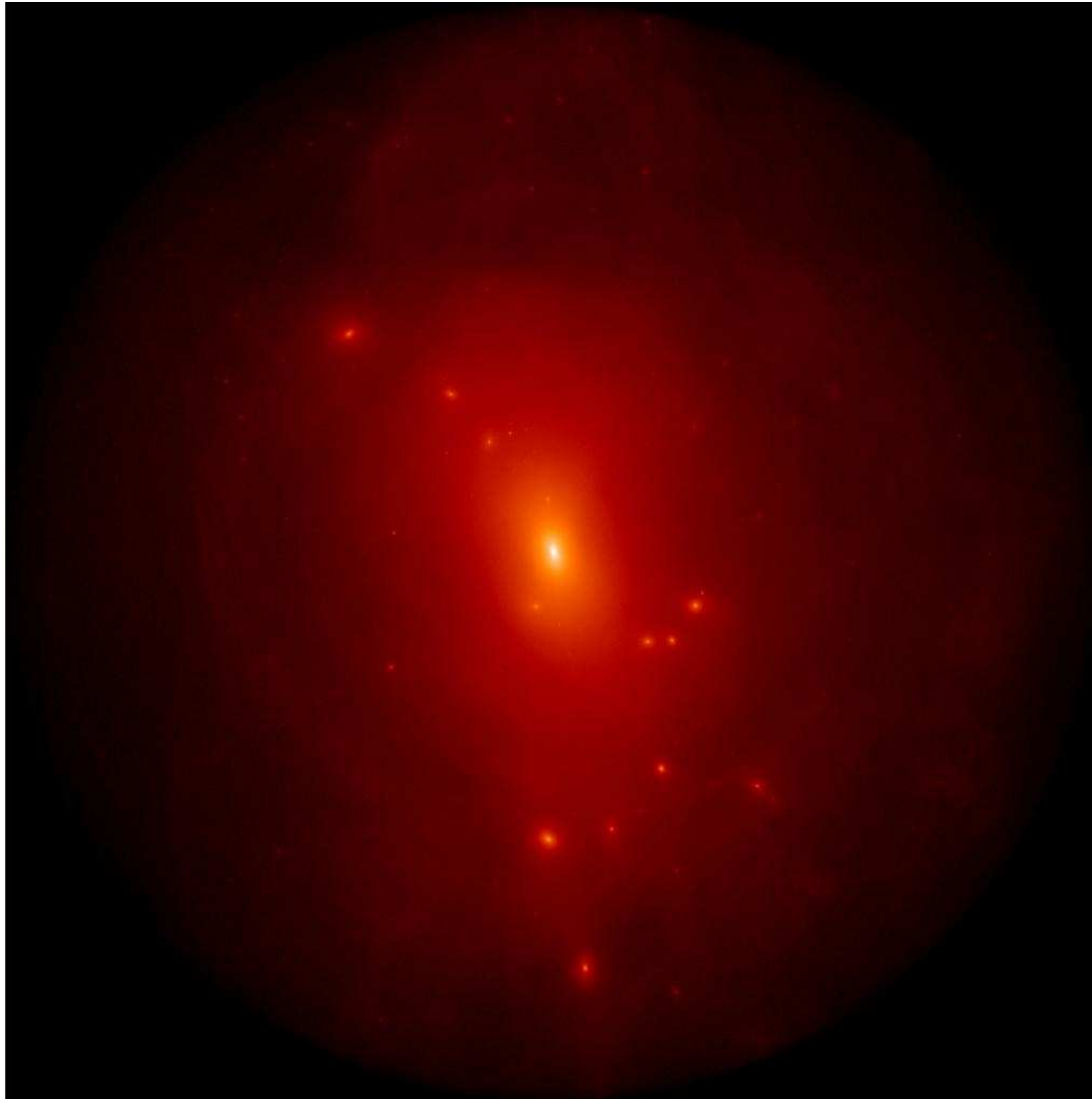
Boyarsky,  
**O.R.**,  
 Shaposhnikov  
 [0901.0011]





# Halo substructure with sterile neutrino DM

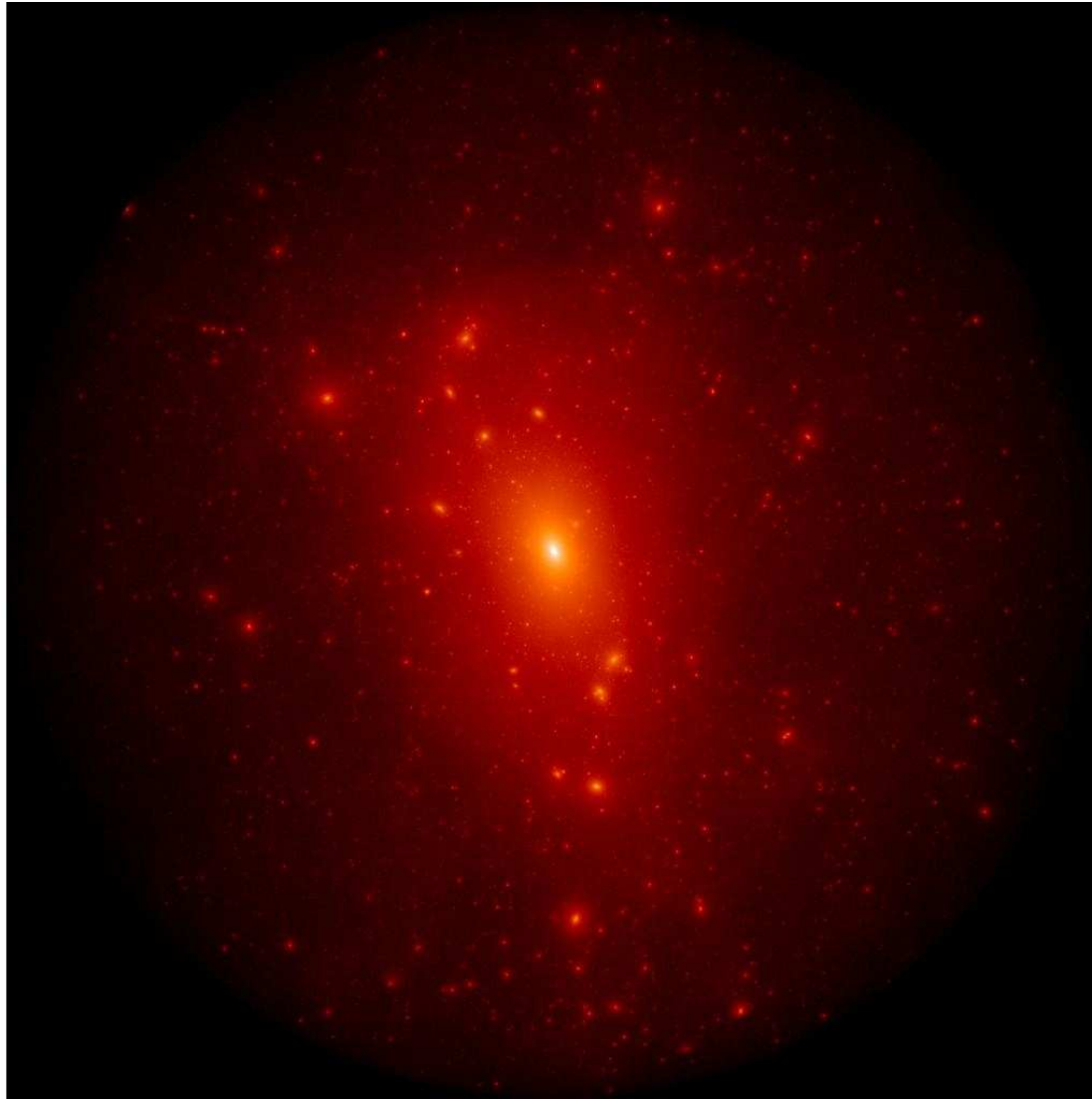
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Lovell, Frenk,  
Eke, . . . ,  
Boyarsky, **O.R.**  
1104.2929  
[astro-ph.CO]

## Halo substructure with CDM

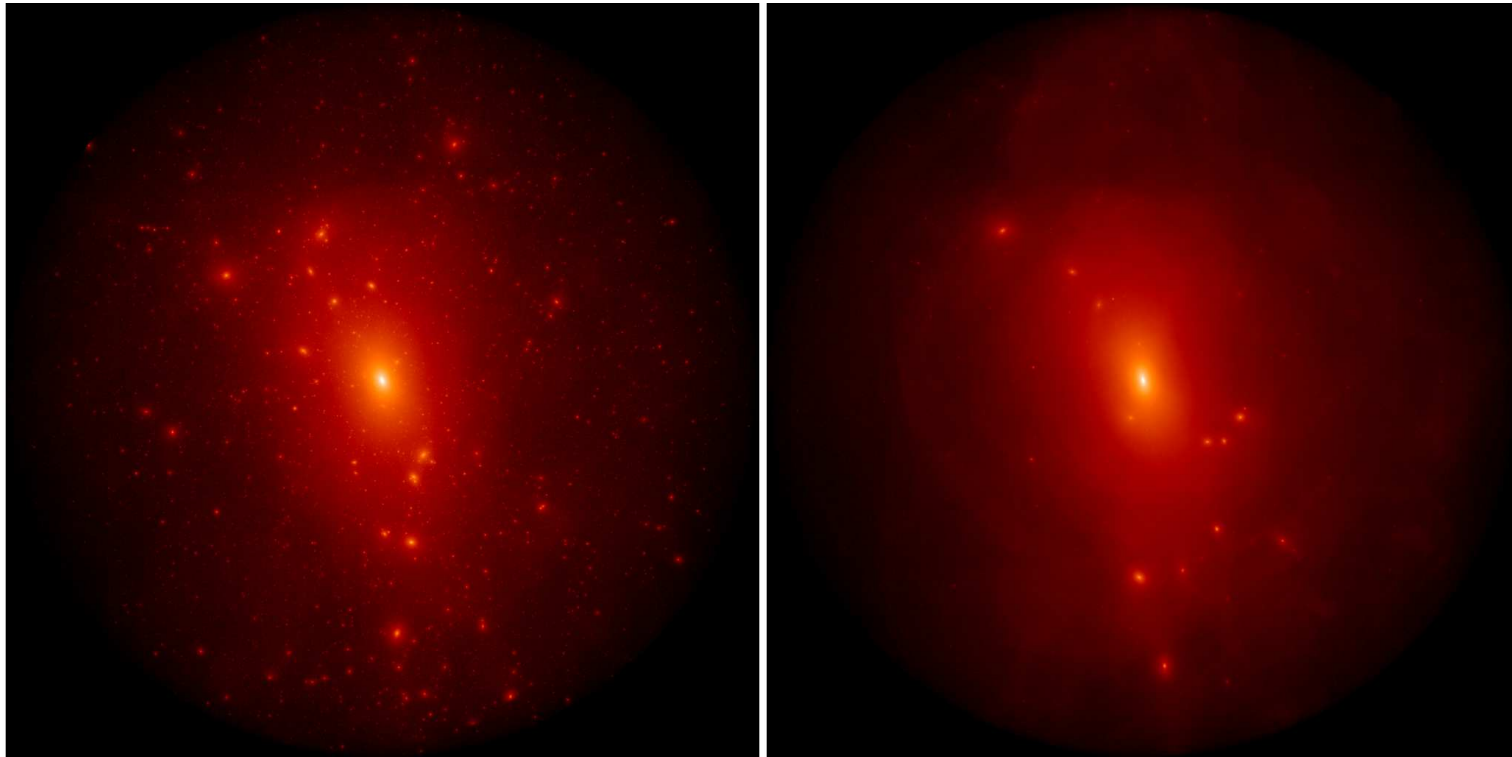
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Aq-A2 halo

# Halo substructure with sterile neutrino DM

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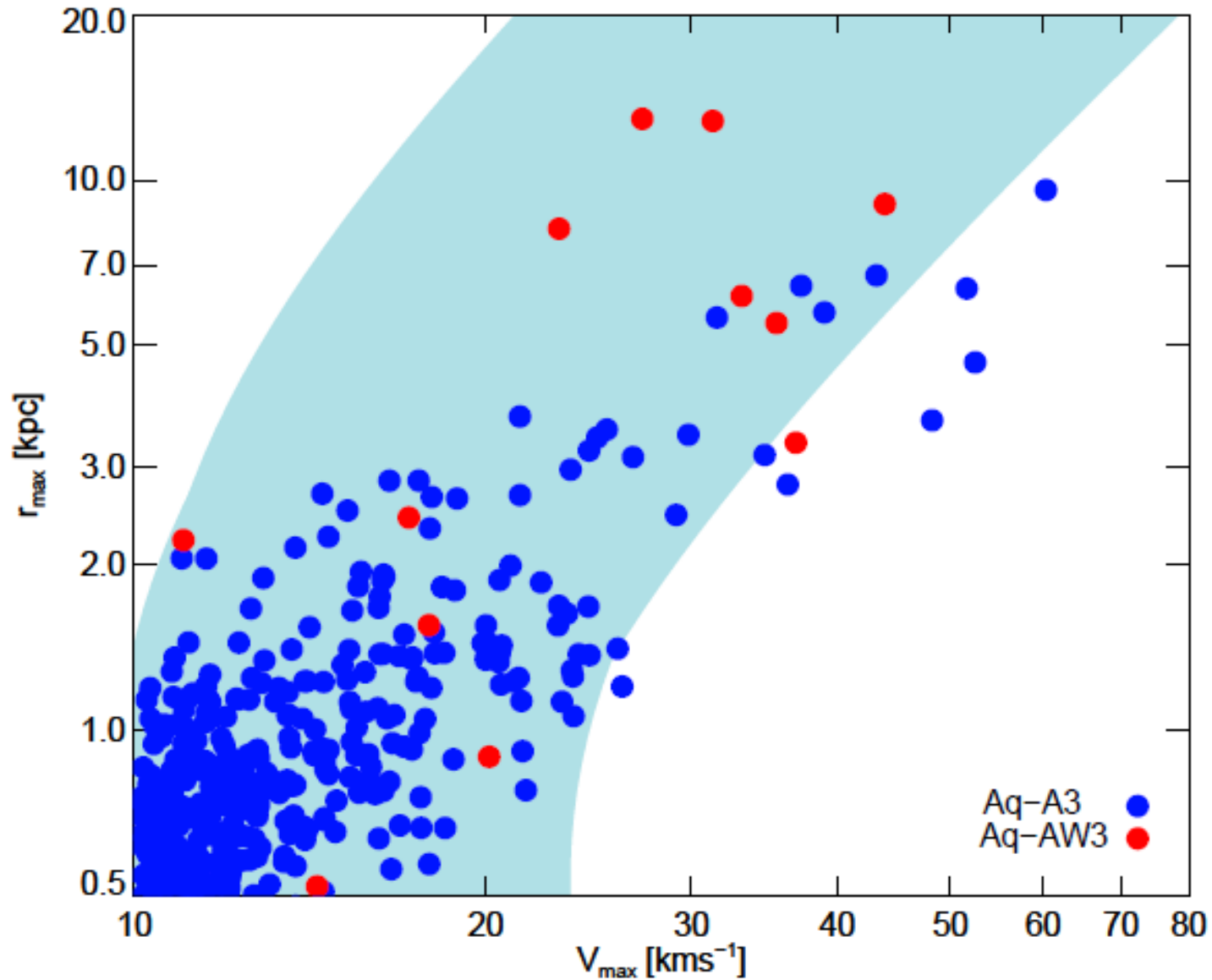


*Aq-A-2 CDM halo*

*Aq-AW-2 halo* made of sterile neutrino DM (Gao, Theuns, Frenk, O.R., ...)

- Simulated sterile neutrino DM halo (right) is fully compatible with the Lyman- $\alpha$  forest data but provides a structure of Milky way-size halo different from CDM

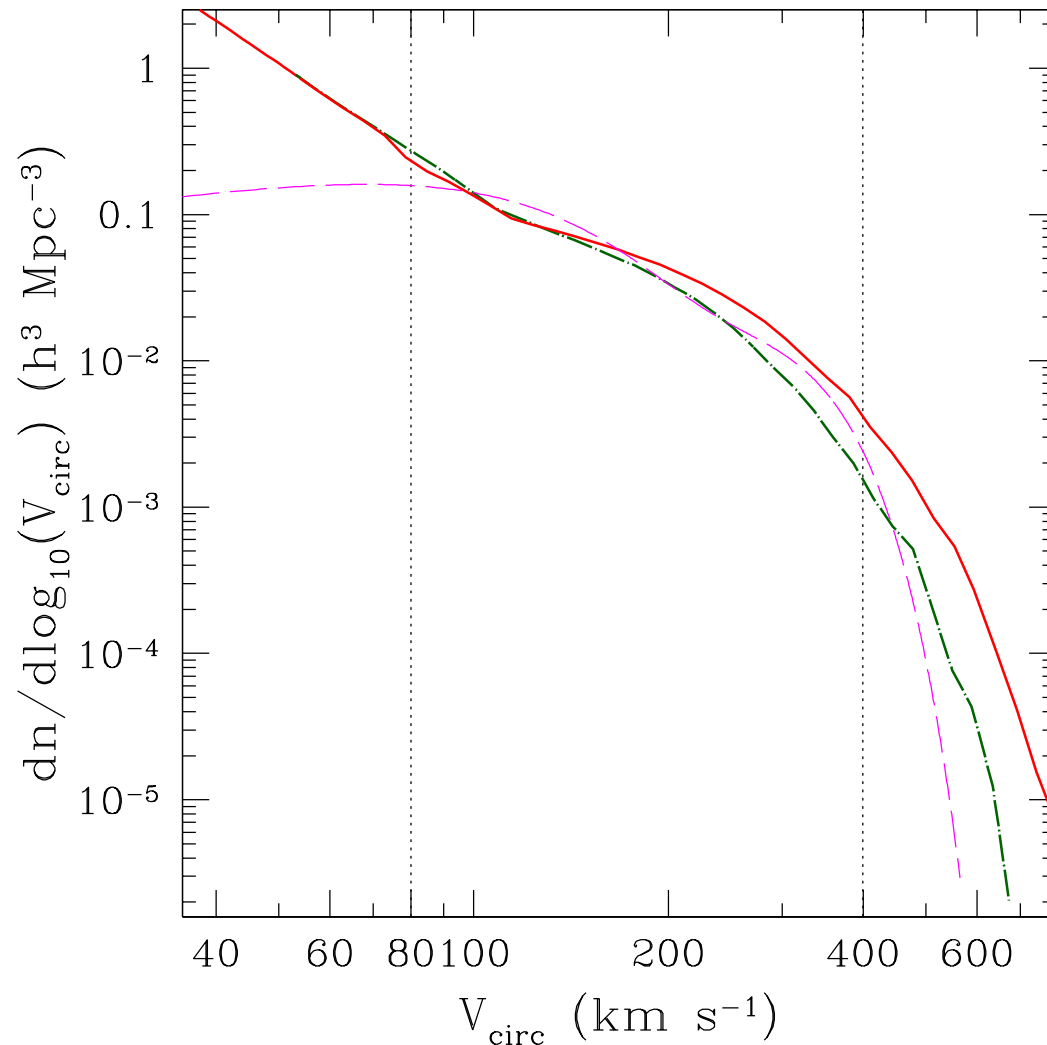
# Abundance of large satellites



Strigari, Frenk  
White (2011)

Lovell, Frenk,  
Eke, ...,  
Boyarsky, O.R.  
1104.2929  
[astro-ph.CO]

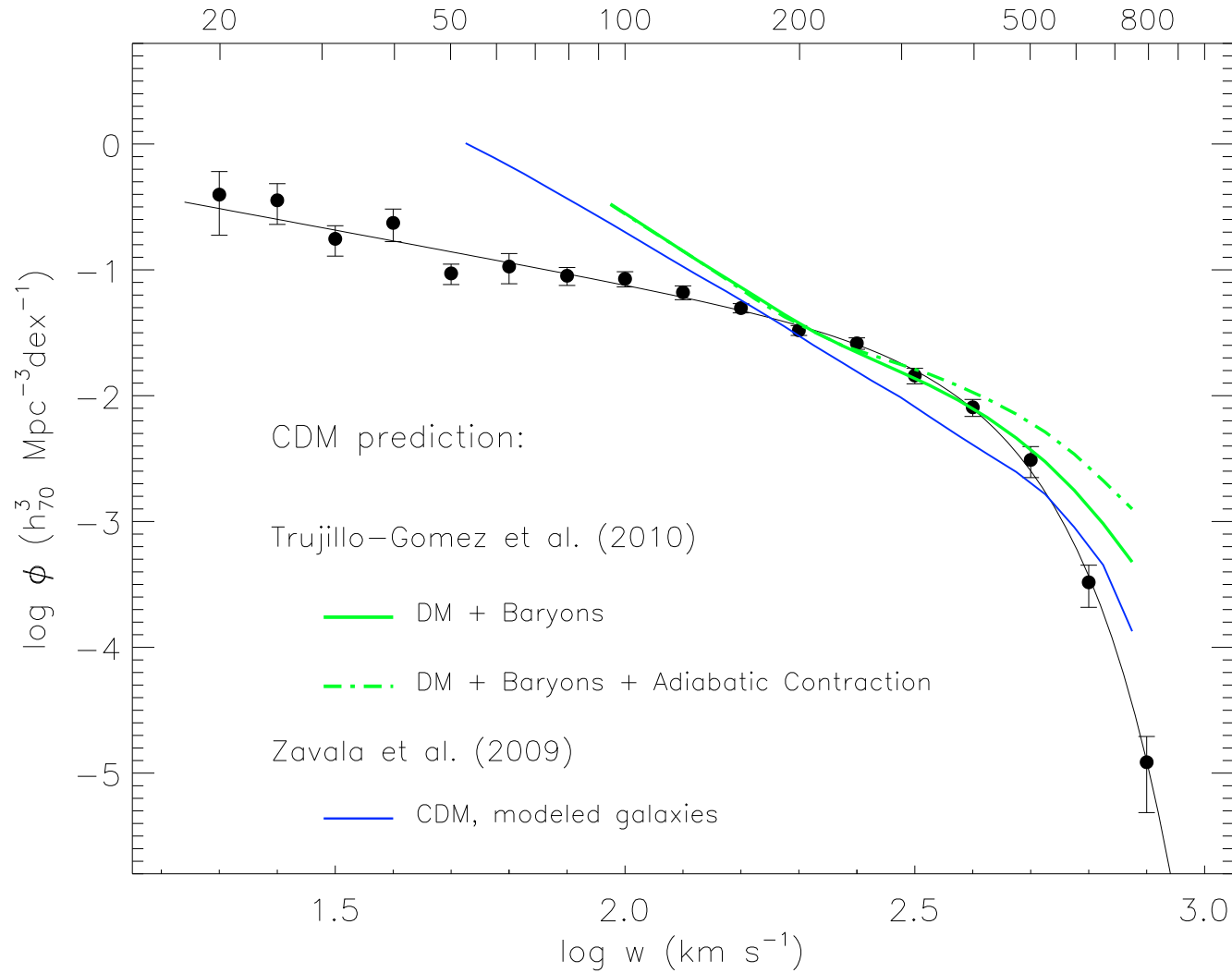
## Another overabundance problem



Observed number of **isolated** halos with circular velocities below  $\sim 100 \text{ km/sec}$  is smaller than predicted by  $\Lambda\text{CDM}$  simulations, assuming *linear bias*

Trujillo-Gomez, Klypin, Primack et al. 2010-2011

# ALFALFA Velocity width function vs. CDM

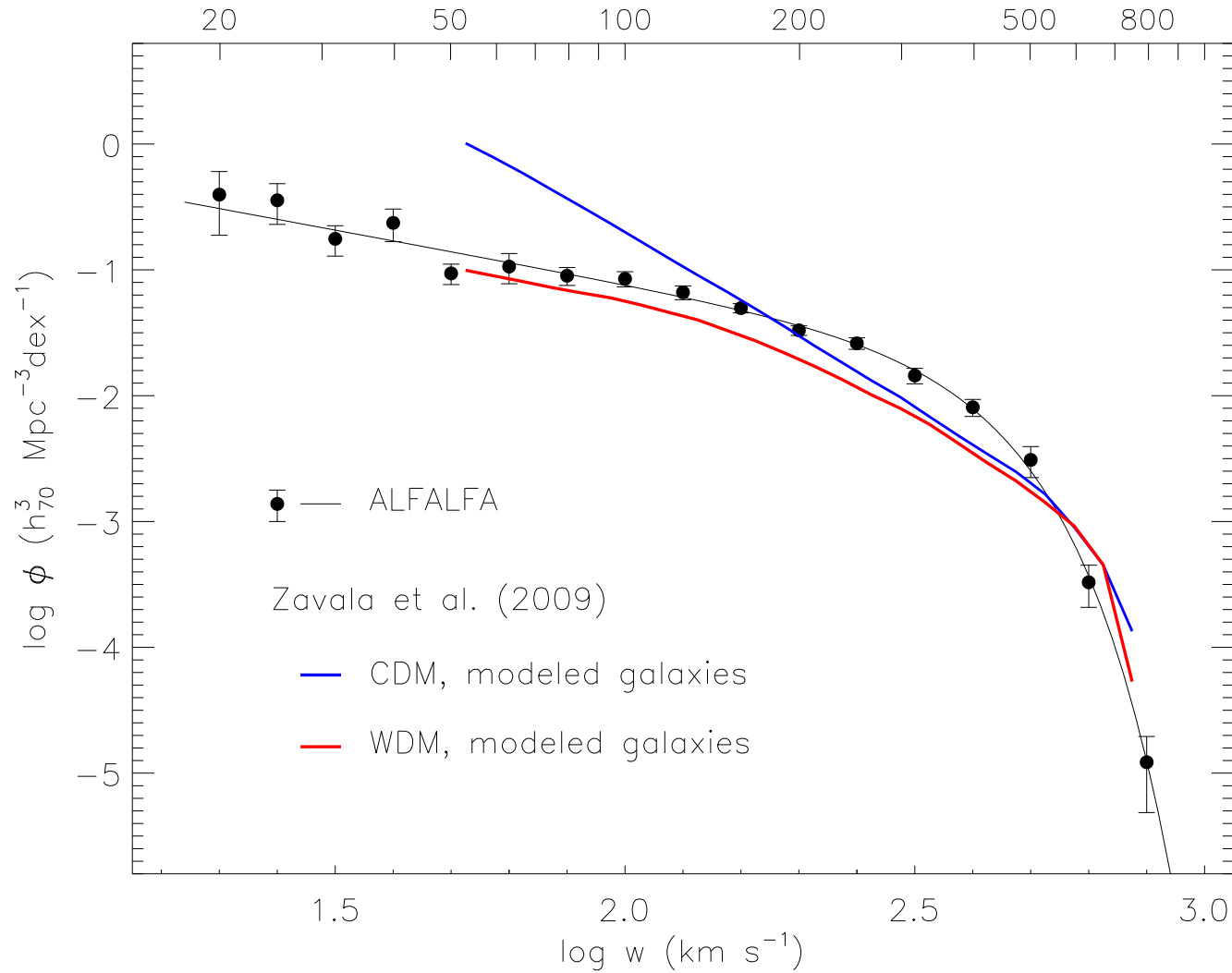


Papastergis+  
[1106.0710]

ALFALFA (HI) survey. Deviations from  $\Lambda$ CDM predictions for  $v_{rot} \lesssim 100$  km/sec

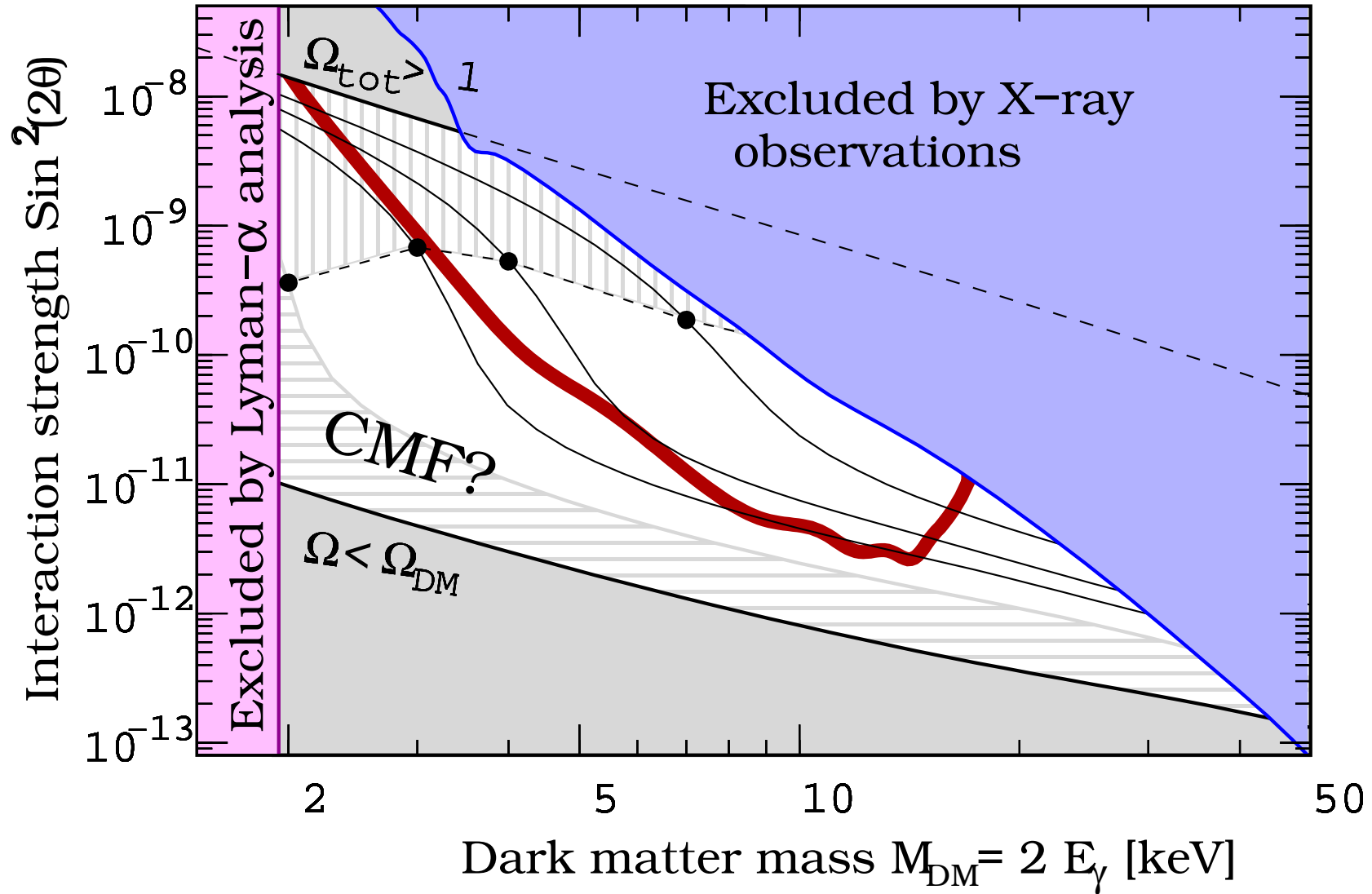
# Velocity width function vs. WDM

Papastergis+  
[1106.0710]



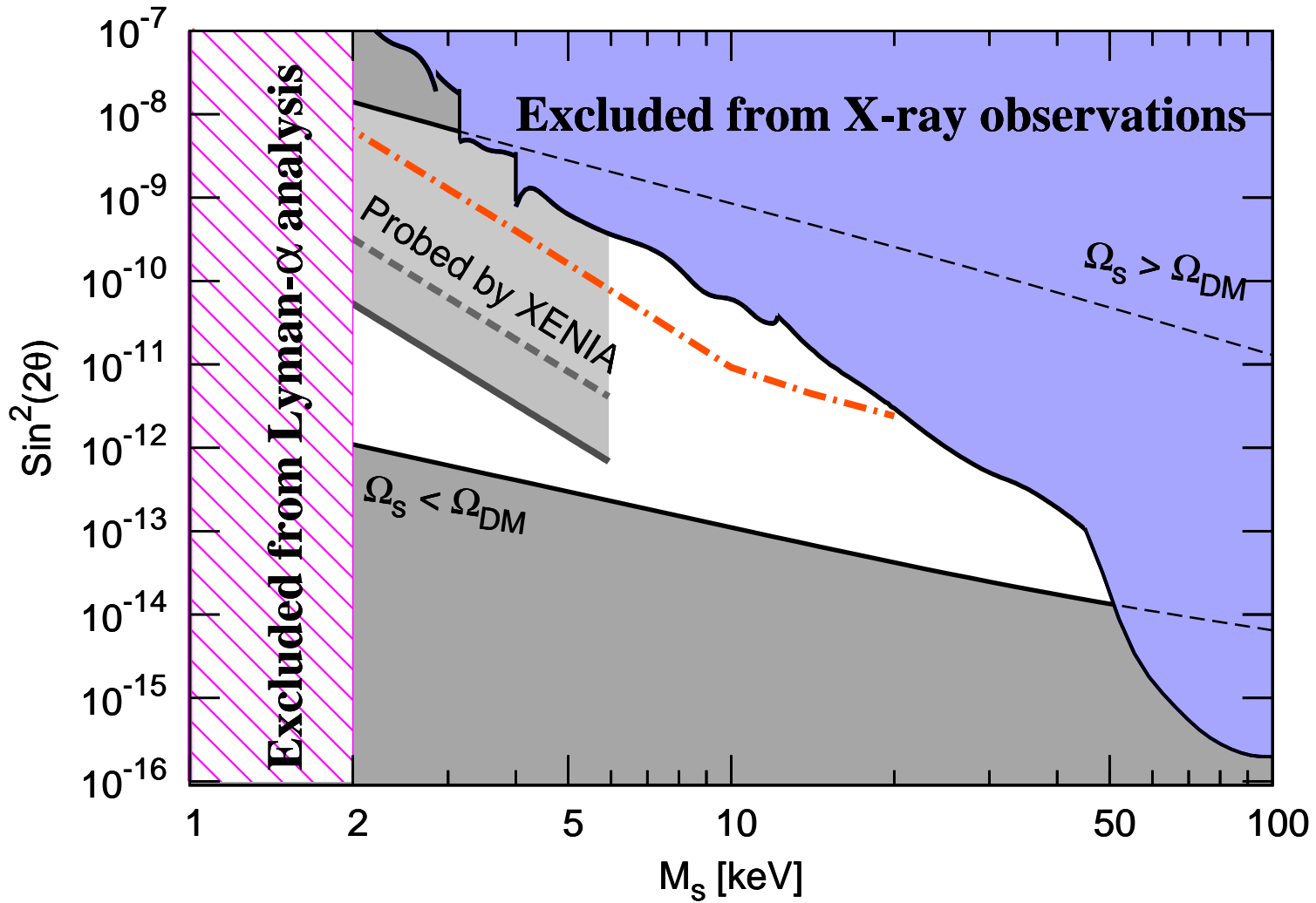
ALFALFA (HI) survey. Deviations from  $\Lambda$ CDM predictions for  $v_{rot} \lesssim 100$  km/sec

# Future?





# Improved bounds on DM decay

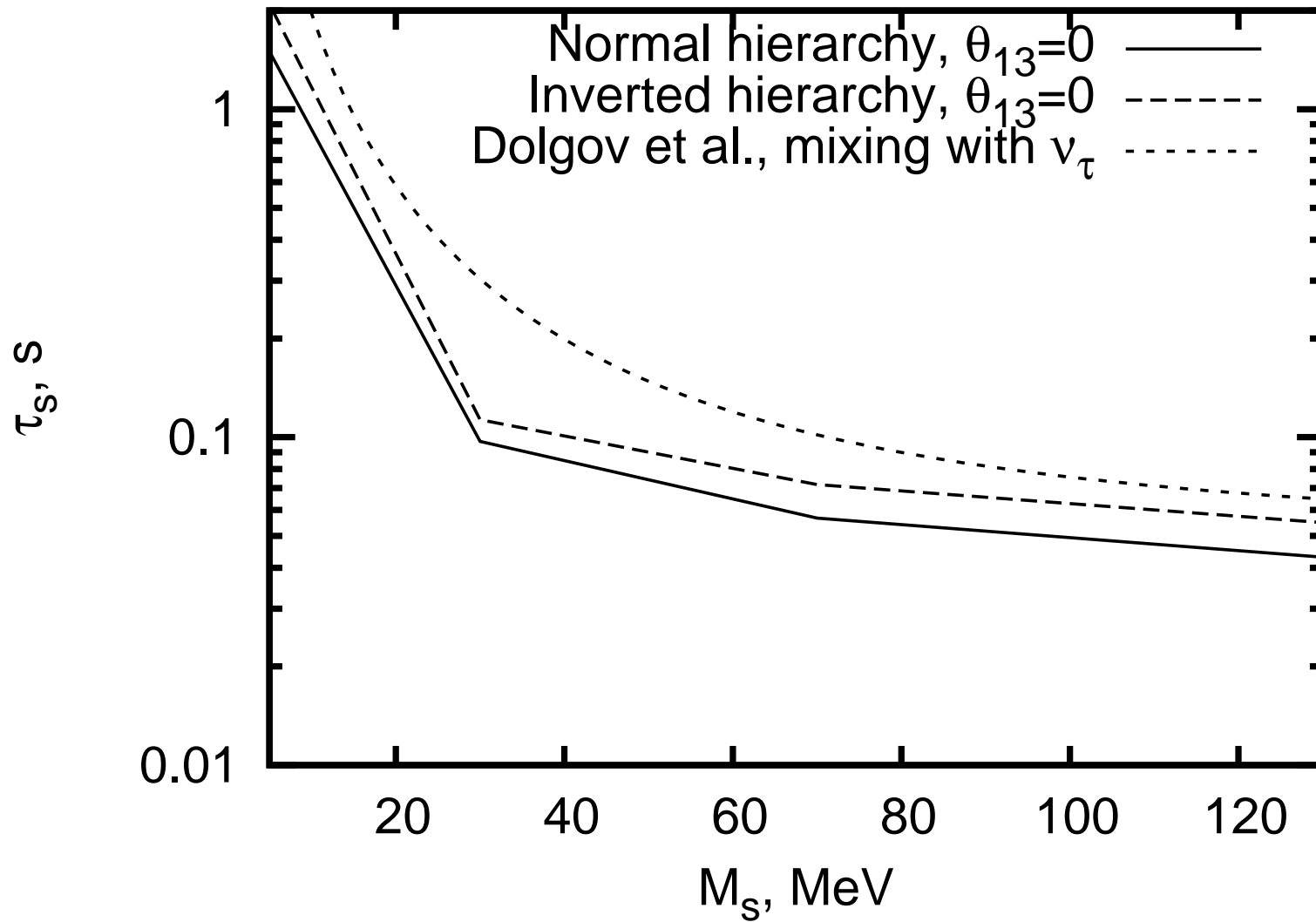


Proposal  
submitted for  
ESA M3  
mission

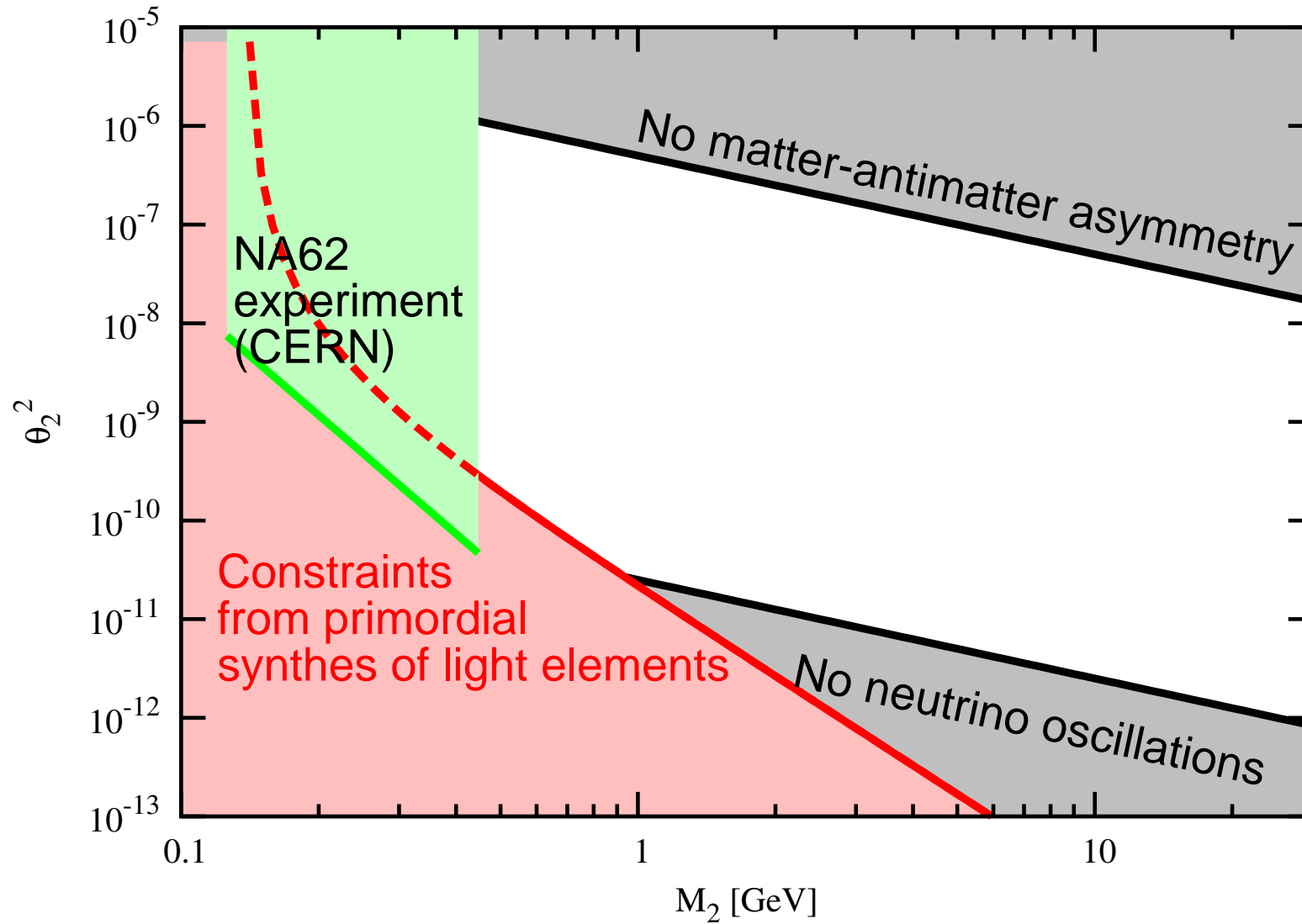
# BBN constraints

Dolgov,  
Semikoz et al.  
(2000–2001);

O.R., Ivashko  
et al. (2011)



# Probing other sterile neutrinos



## Conclusion

---

- $\nu$ MSM demonstrates that the BSM phenomena can find their explanation without introduction of new energy scale
- Neutrino Minimal Standard Model ( $\nu$ **MSM**) provides resolution of all major observational BSM problems and gives a **complete history of the Universe** from inflationary era till today
- Sterile neutrino dark matter can leave its imprints on formation of structures and can be detected via its monochromatic decays to photons
- Heavier sterile neutrino particles can be probed with this generation of **intensity frontier** experiments

---

Thank you for your attention!

## Thermal relics

---

- The simplest WDM model – **thermal relics**. Particles that freeze-out relativistic at temperature  $T_d$

Bode et al.  
(2001)

$$f(v) = \frac{1}{\exp\left\{\frac{M_{\text{DM}}v}{T_d(t)}\right\} + 1}$$

- Decoupling temperature determines abundance:

$$\Omega_{\text{DM}}h^2 = \left(\frac{T_d}{T_\nu}\right)^3 \frac{M_{\text{DM}}}{94 \text{ eV}} \quad \text{where} \quad \left(\frac{T_d}{T_\nu}\right)^3 = \frac{10.75}{g_*(T_d)}$$

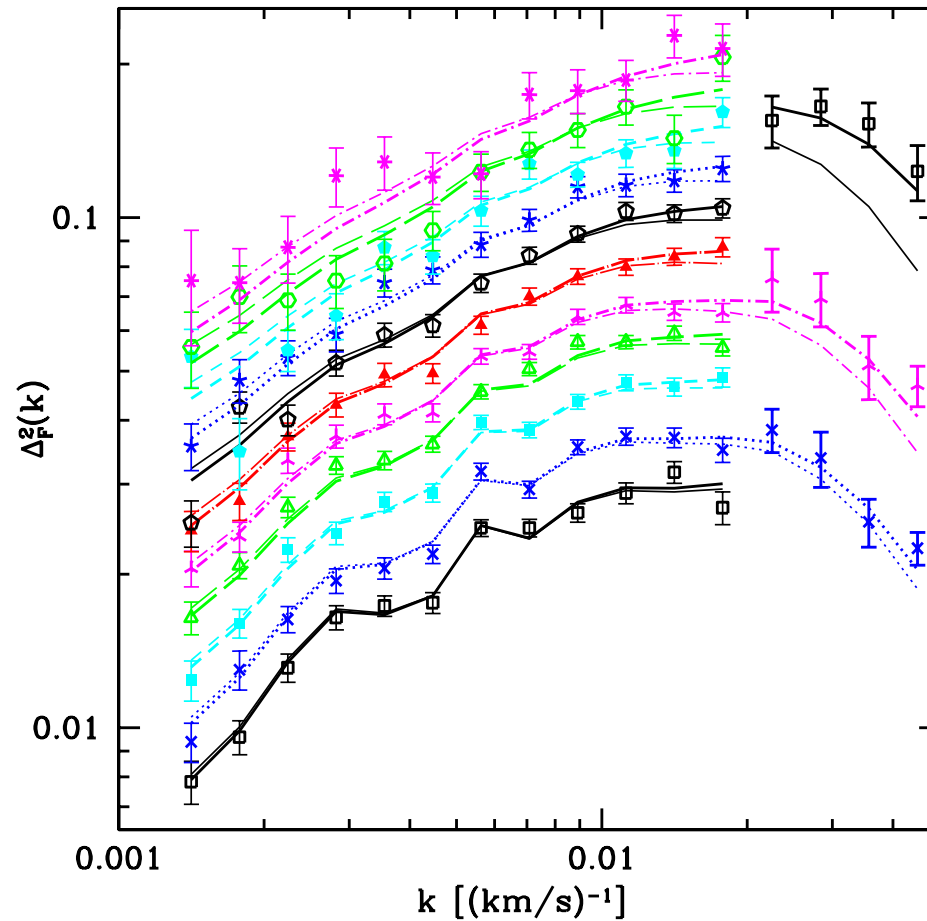
- The suppression of the power-spectrum is strong

Viel et al.  
(2005)

$$T(k) \equiv \sqrt{\frac{P(k)}{P_{\Lambda\text{CDM}}(k)}} \propto \left(\frac{k_c}{k}\right)^{10} \quad k_c \sim 20 \frac{h}{\text{Mpc}} \frac{M_{\text{DM}}}{\text{keV}}$$

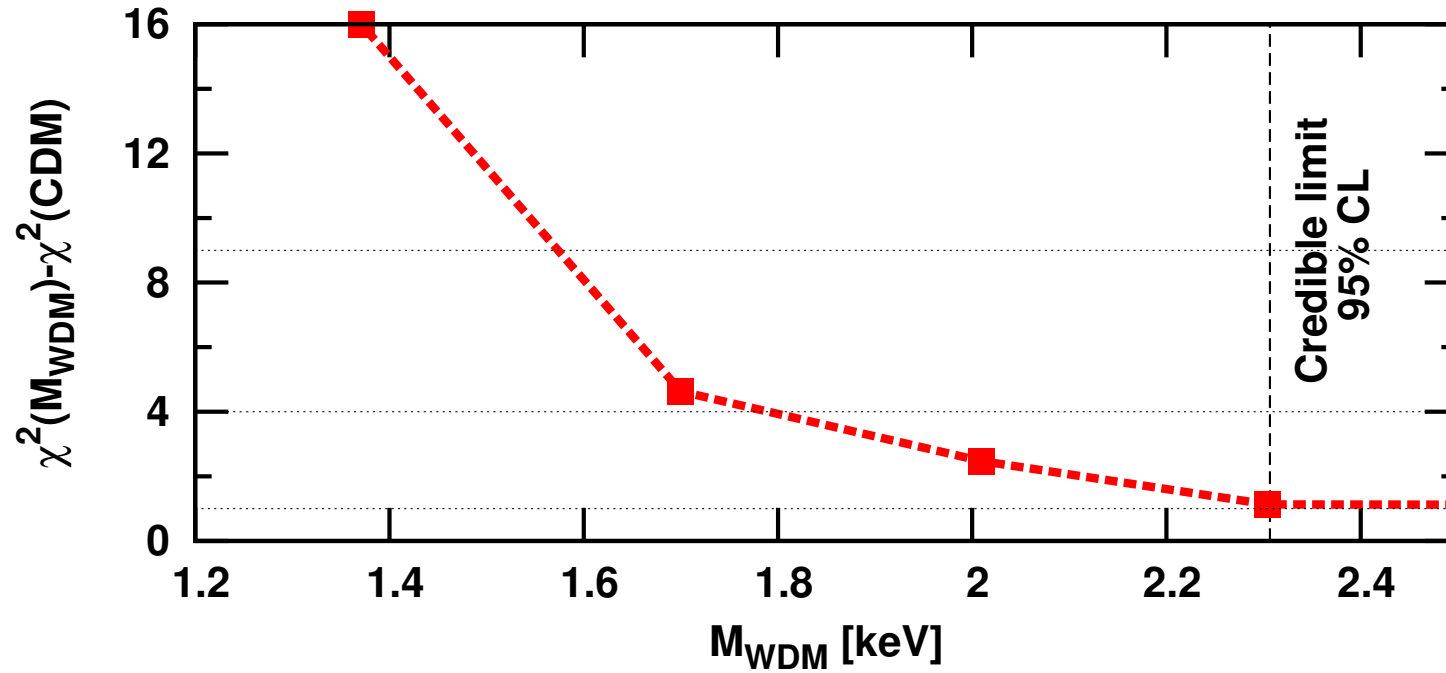
# Lyman- $\alpha$ forest flux power spectrum

Seljak et al.  
'06



Measured flux power spectrum is compared against CDM and non-CDM models

# Ly- $\alpha$ and thermal relics



Boyarsky,  
Lesgourgues,  
**O.R.**, Viel  
[0812.0010]  
(JCAP 2009)

Also Viel et al.  
2005-2007;

Seljak et al.  
(2006)

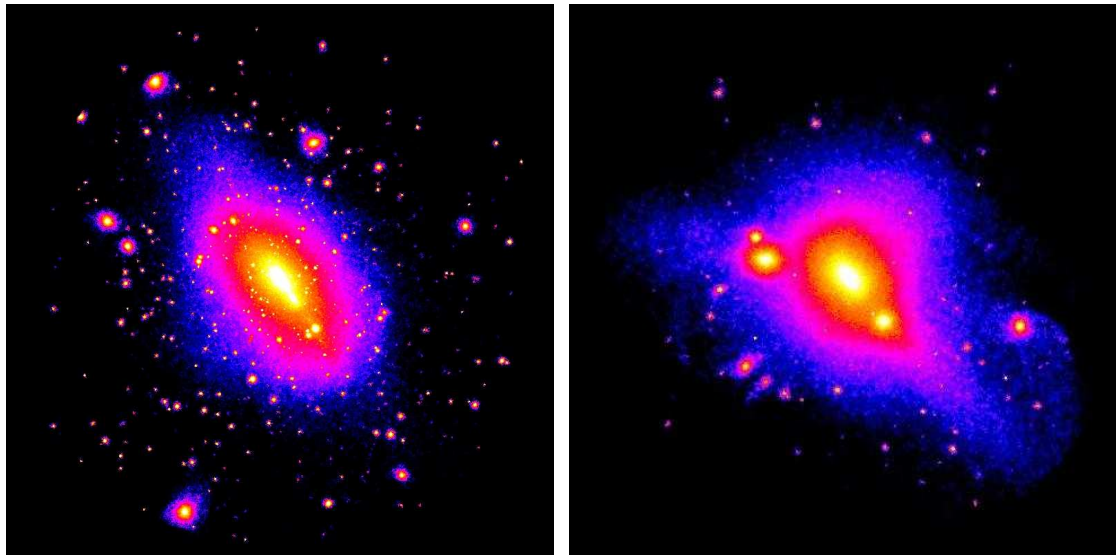
*These bounds are for **thermal relics** only!*



## Lyman- $\alpha$ forest and warm DM

---

- Previous works put bounds on free-streaming  $\lambda_{FS} \lesssim 150$  kpc (“WDM mass”  $> 2.3$  keV) Viel et al. 2005-2007; Seljak et al.(2006)
- The simplest **WDM** with such a free-streaming would not modify visible substructures:



Maccio & Fontanot (2009);

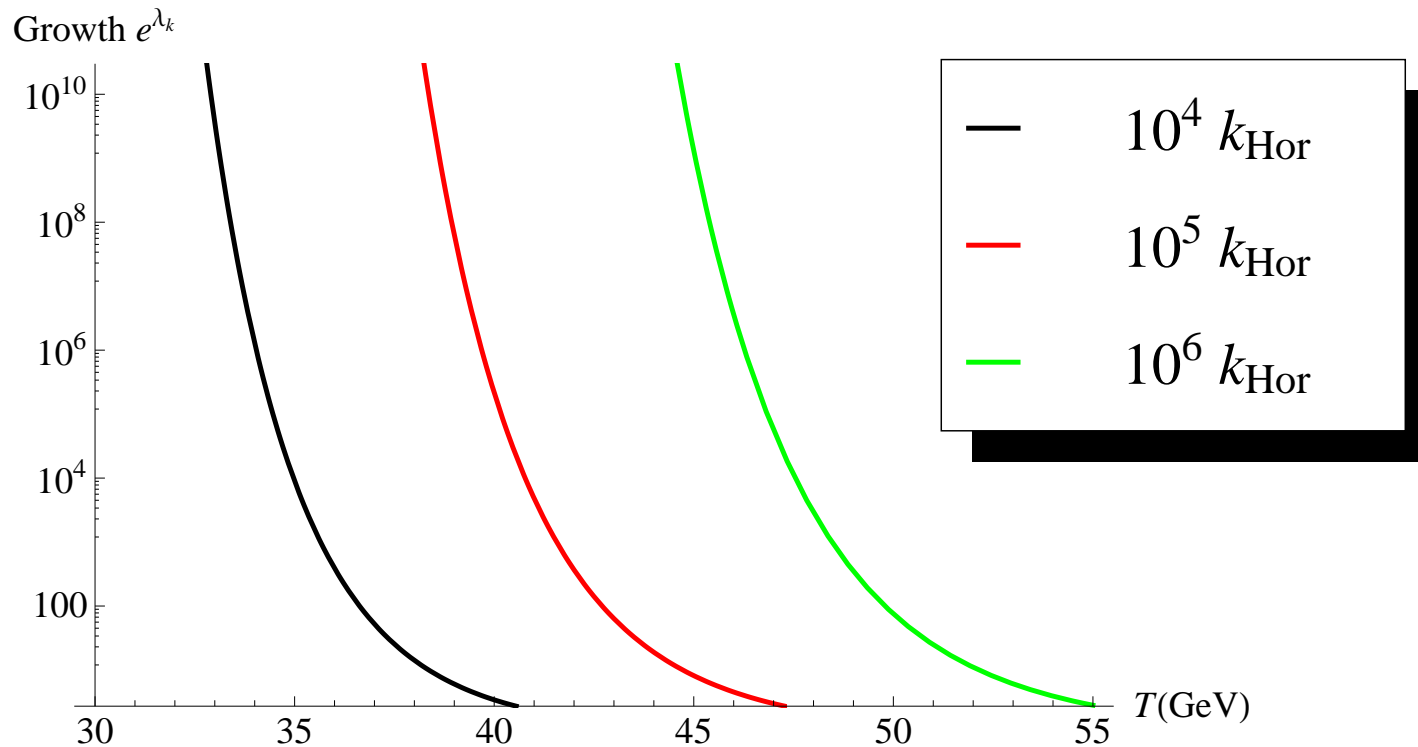
Polisensky & Ricotti (2010)

- **Thermal relic** with exponential cut-off  $\sim 1$  Mpc would erase **too many substructures**. Anything “colder” would produce enough structures to explain observed Milky Way structures

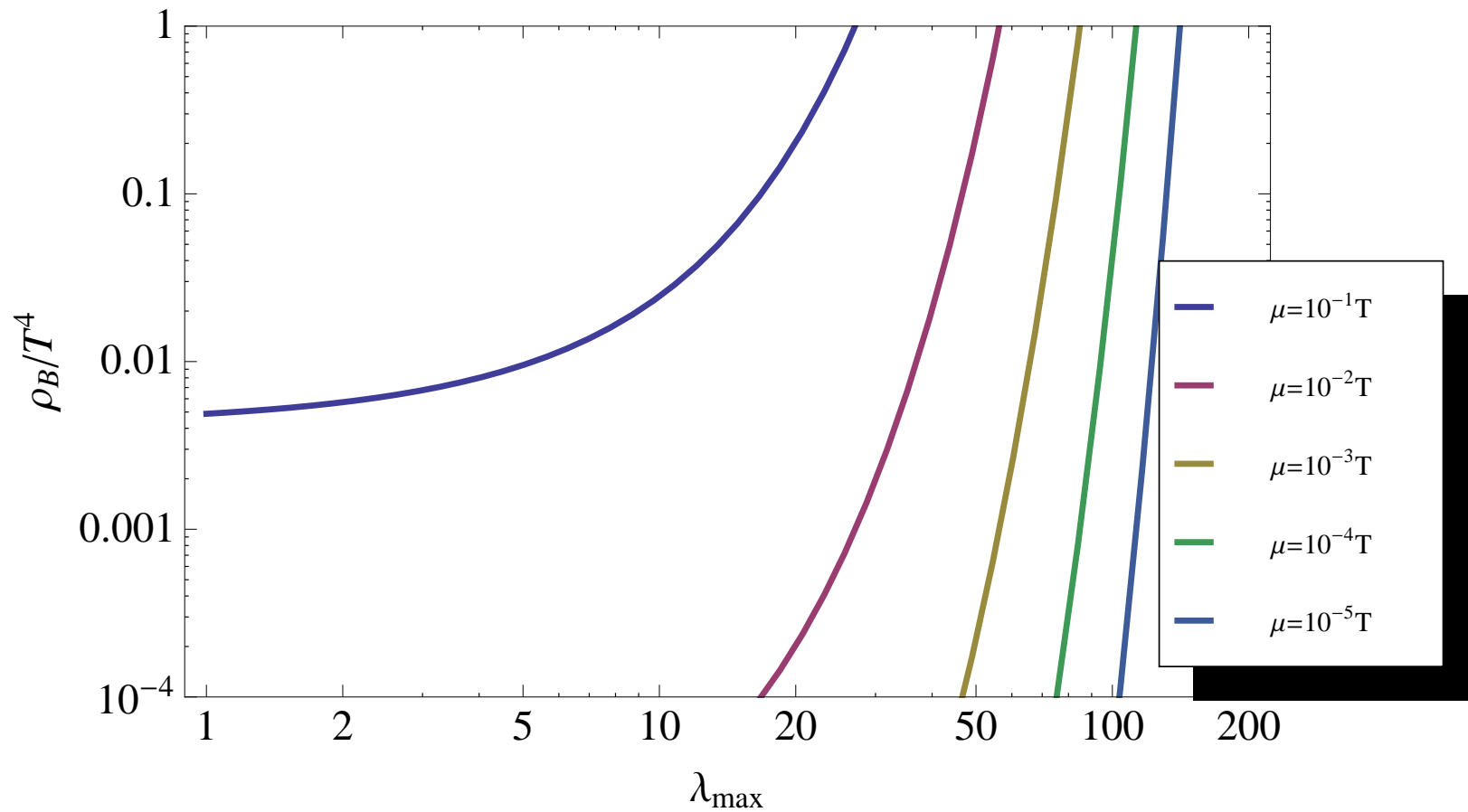
## CMF instability in the $\nu$ MSM

The **longest wave-length** that has experienced instability at temperature  $T$  is

$$k_{min} = H(T) \frac{\sigma}{\alpha \bar{\mu}} \sim \frac{H(T)}{\alpha^2 \log(1/\alpha) \bar{\mu}(T)}$$

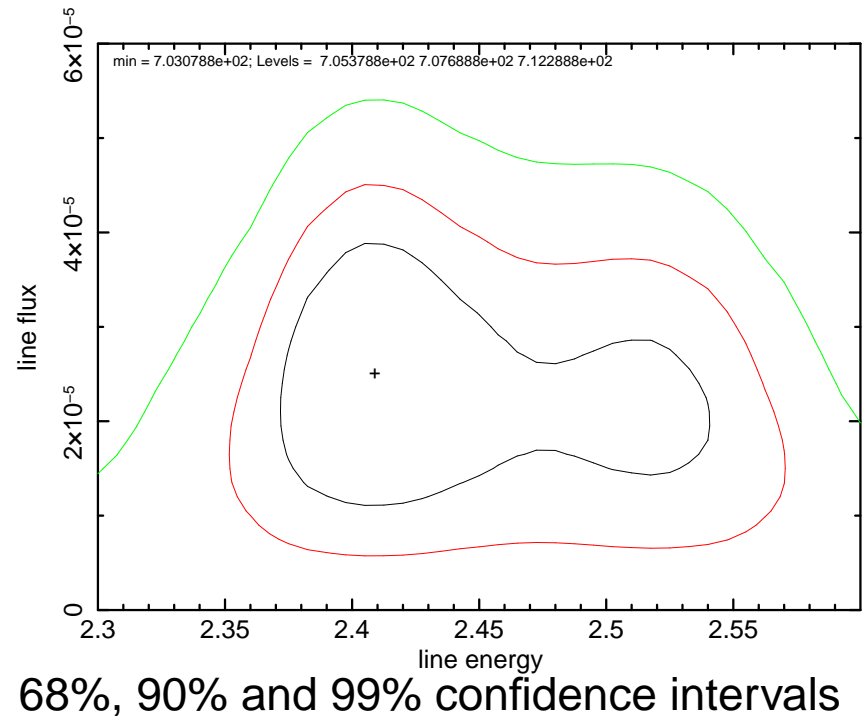
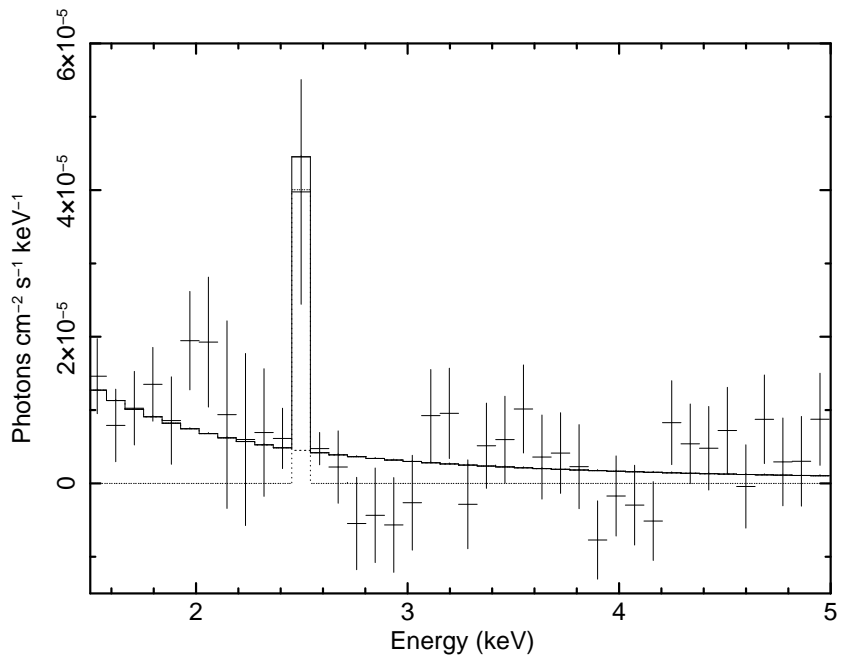


# Energy in the magnetic field



## Checking DM origin of a line

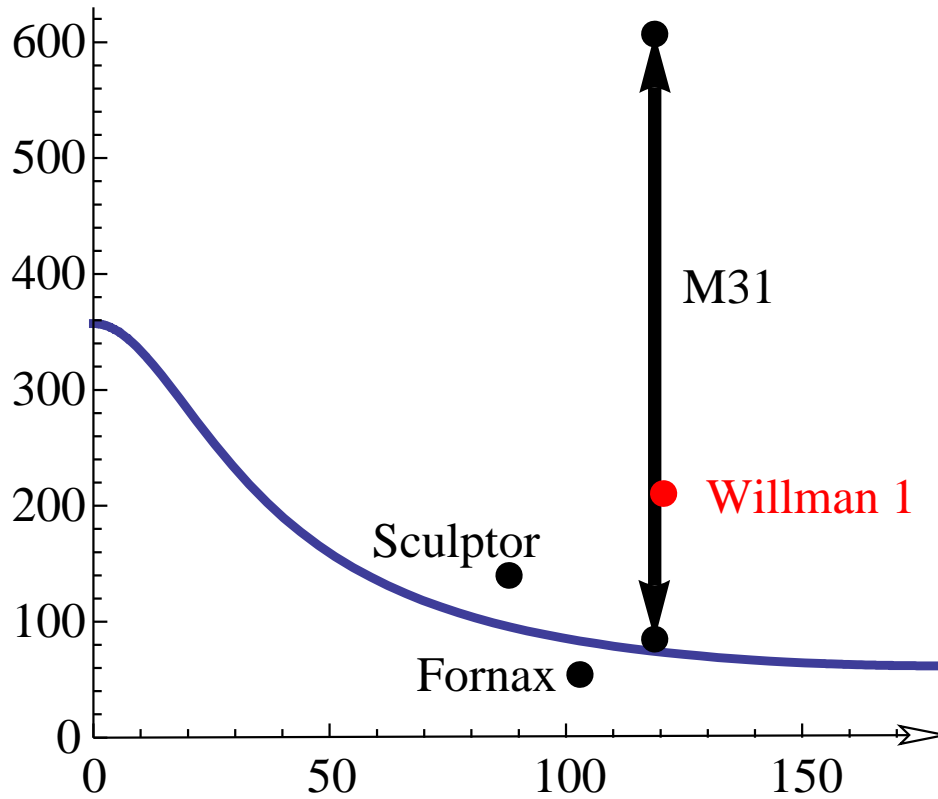
- *Dark Matter Search Using Chandra Observations of Willman 1, and a Spectral Feature Consistent with a Decay Line of a 5 keV Sterile Neutrino* Loewenstein & Kusenko (Dec'2009)



- *Can the excess in the FeXXVI Ly gamma line from the Galactic Center provide evidence for 17 keV sterile neutrinos?* Prokhorov & Silk (Jan'2010)

## Do we see this line anywhere else?

$S_{MW}$  Msun/pc<sup>2</sup>



Objects with comparable expected signal for which archival data is available

■ **Fornax dSph (XMM)**

$$S_F = 54.4 M_{\odot} \text{pc}^{-2}$$

■ **Sculptor dSph (Chandra)**

$$S_{Sc} = 140 M_{\odot} \text{pc}^{-2}$$

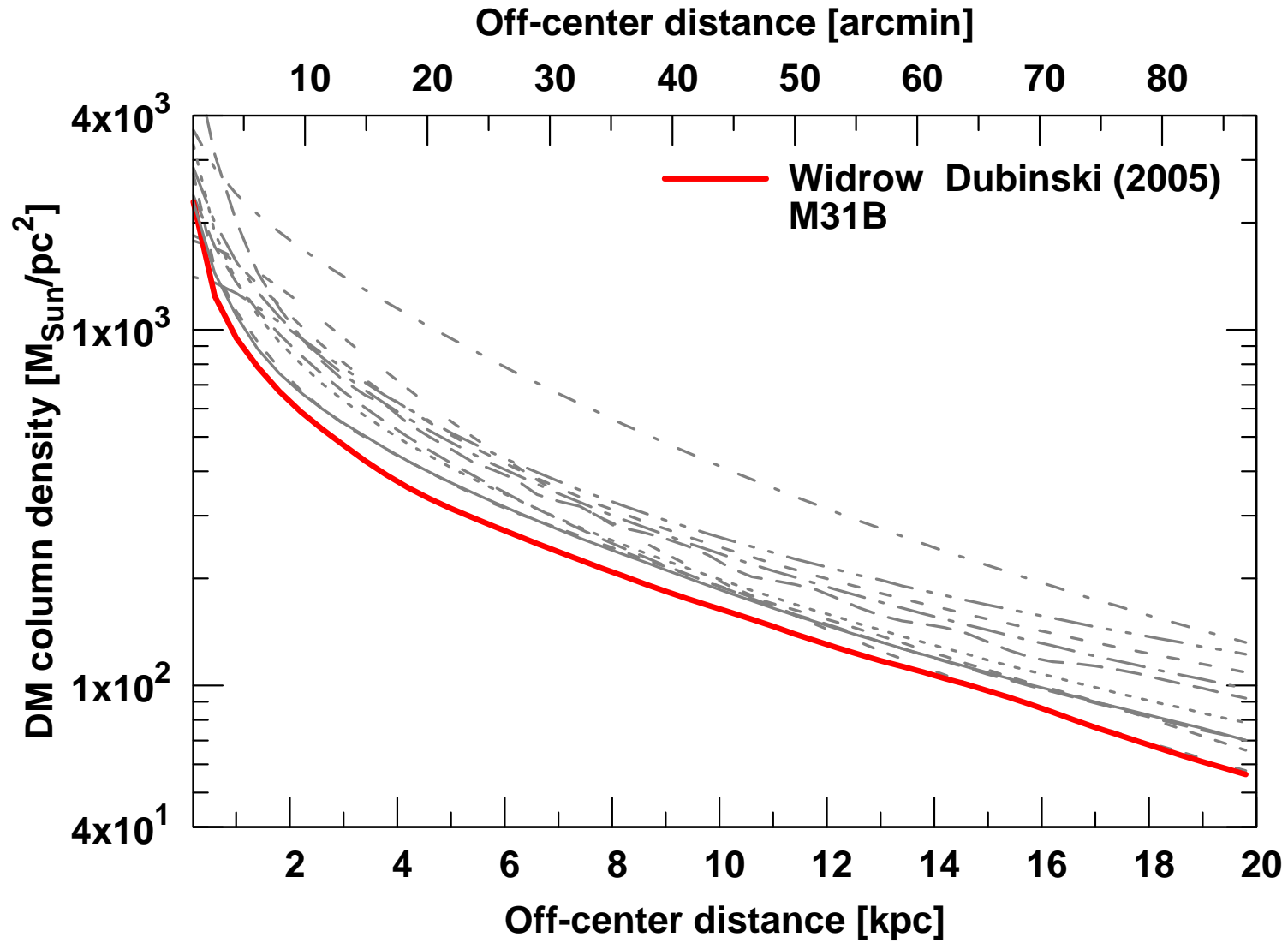
■ **Andromeda galaxy (M31) :**

$$S_{M31} \sim 100 - 600 M_{\odot} / \text{pc}^2$$

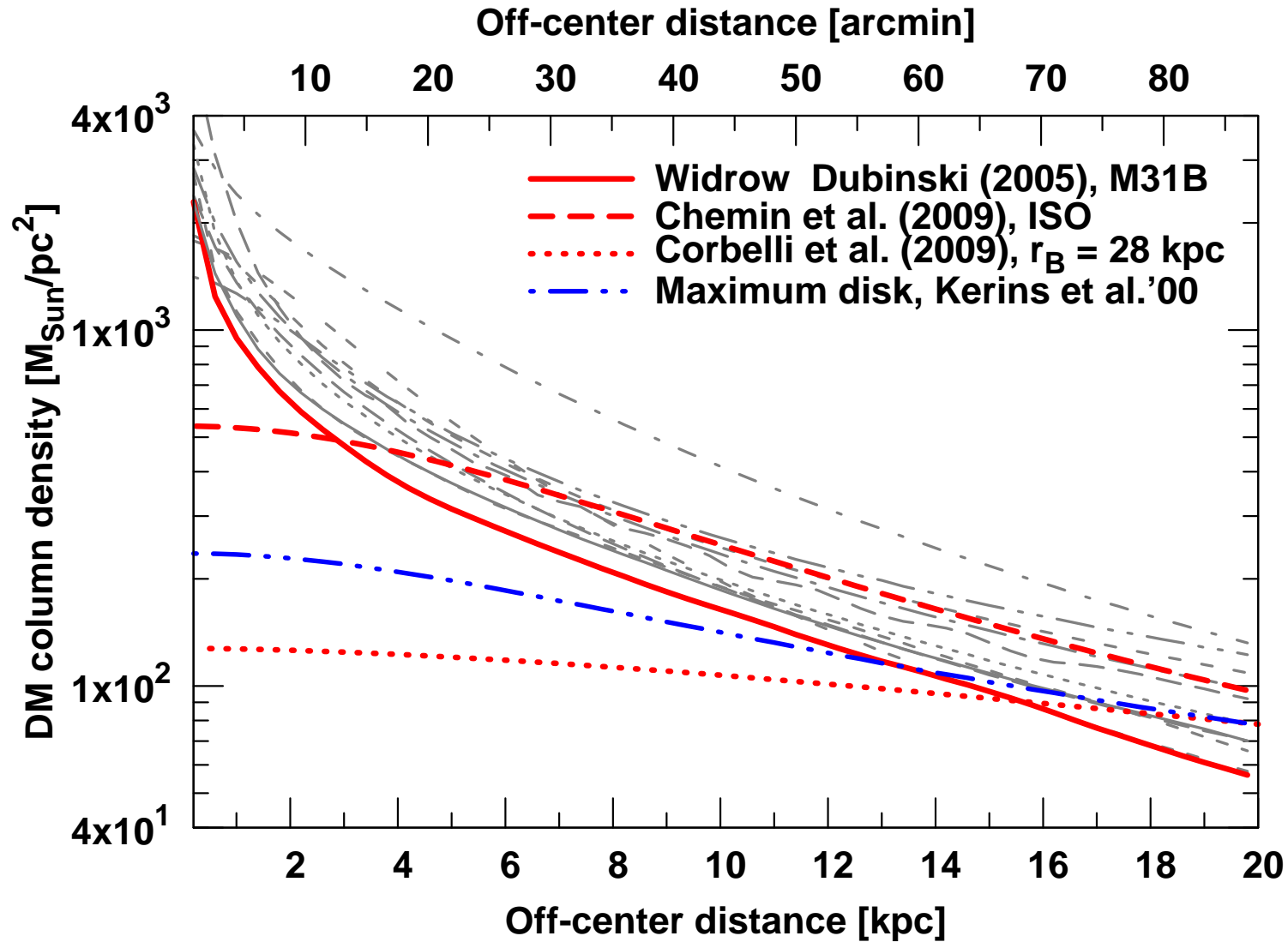
**Do we see this 2.5 keV line?**

# DM in Andromeda galaxy (2008)

Boyarsky,  
O.R. et al.  
MNRAS'08



# DM in Andromeda galaxy (2010)



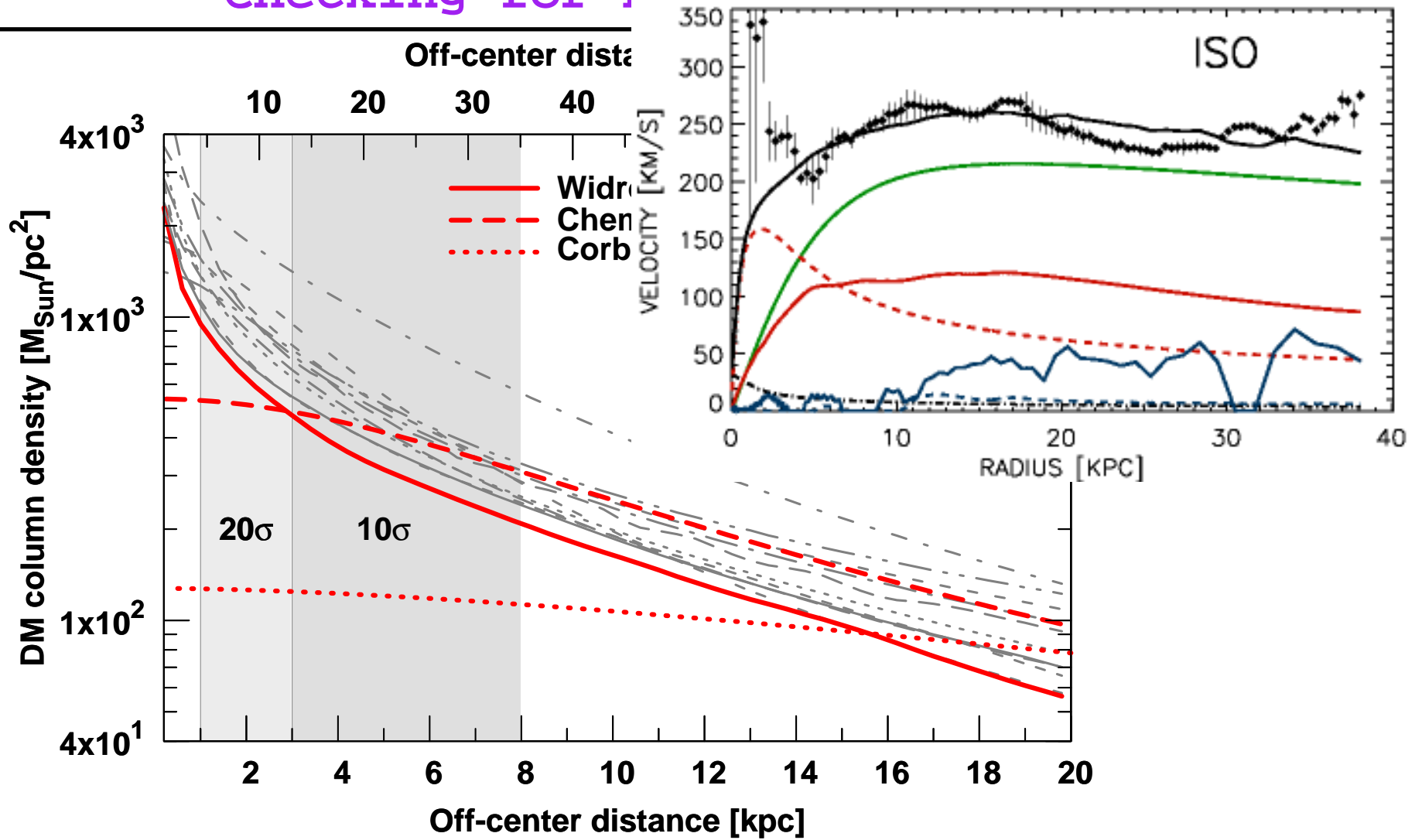
Boyarsky,  
O.R. et al.  
MNRAS'08

Chemin et al.  
0909.3846

Corbelli et al.  
0912.4133

Kusenko &  
Loewenstein  
1001.4055

# Checking for $\tilde{\nu}_m$ lines in M31



Willman 1 spectral feature excluded with high significance from archival observations of M31 and Fornax and Sculptor dSphs