

**4<sup>th</sup> Forward Physics Facility Meeting**  
**February 1<sup>st</sup>, 2022**

**Towards precision studies  
of high-energy QCD via a  
FPF+ATLAS tight timing coincidence**

**Francesco Giovanni Celiberto**

**ECT\*/FBK Trento & INFN-TIFPA**



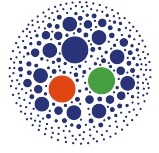
# High-energy resummation at the FPF

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Motivation

Natural  
Stability

FPF+ATLAS  
Coincidence

Towards  
Precision  
Studies



**Collinear factorization** → well-established formalism, successes in QCD pheno



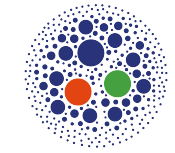
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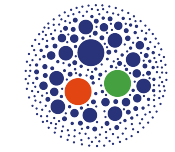
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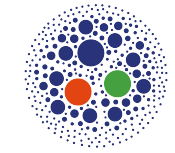
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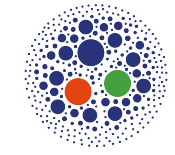
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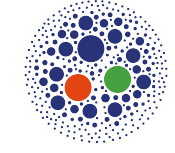
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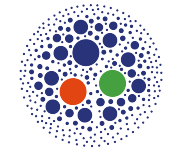


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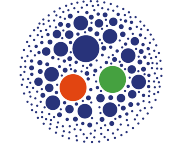
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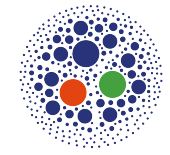
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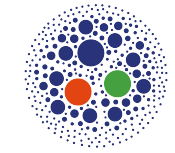
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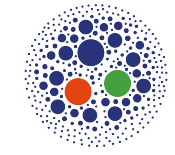
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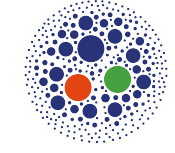
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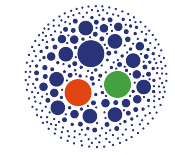
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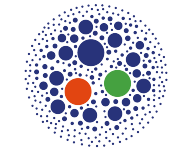
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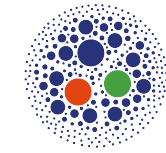
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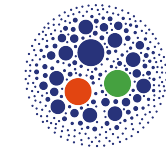
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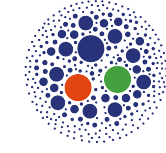
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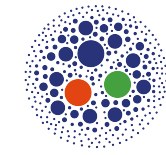
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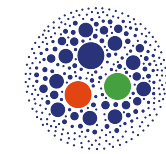
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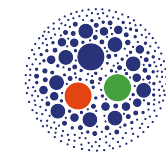
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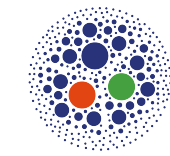
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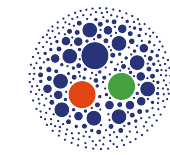
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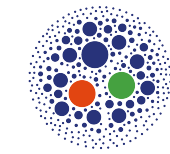
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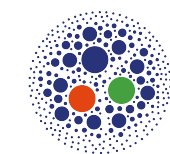
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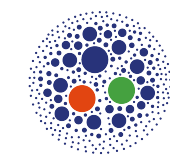
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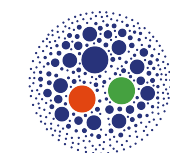
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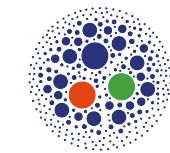
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Parton content of proton at small- $x$  → BFKL UGD, resummed PDFs, small- $x$  TMDs



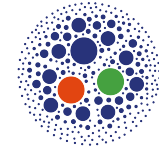
# Mueller-Navelet jets: hybrid factorization

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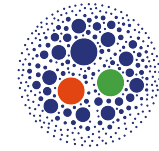
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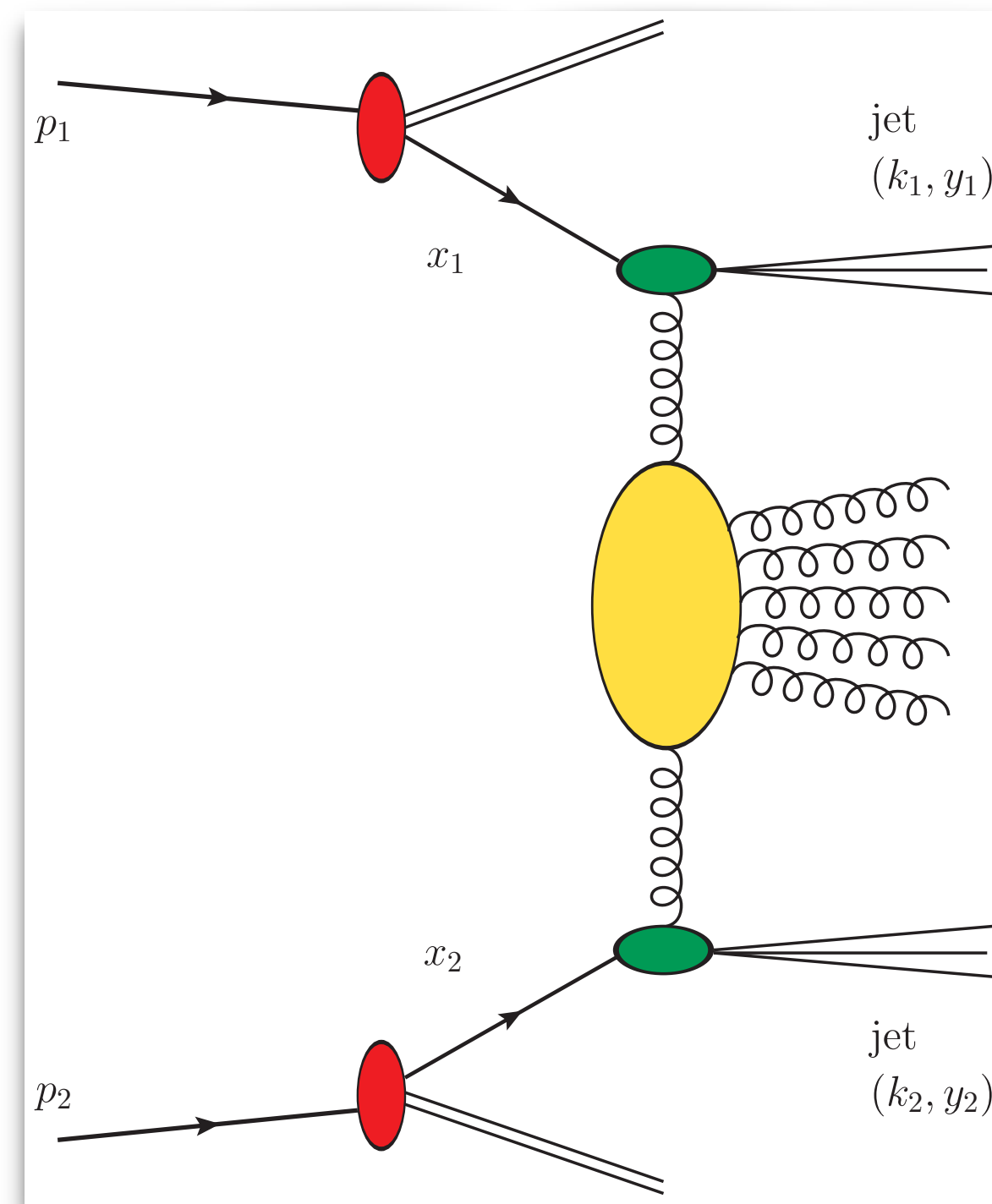


Inclusive hadroproduction of two jets with high  $p_T$  and large rapidity separation,  $\Delta Y$



Moderate  $x$  (*collinear PDFs*), but  $t$ -channel  $p_T$  (*HE factorization*)  $\rightarrow$  **hybrid** approach

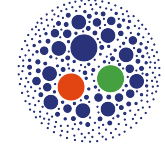
$$\frac{d\sigma}{dy_1 dy_2 d^2\vec{k}_1 d^2\vec{k}_2} = \sum_{r,s=q,g} \int_0^1 dx_1 \int_0^1 dx_2 f_r(x_1, \mu_F) f_s(x_2, \mu_F) \frac{d\hat{\sigma}_{r,s}(x_1 x_2 S, \mu_F)}{dy_1 dy_2 d^2\vec{k}_1 d^2\vec{k}_2}$$



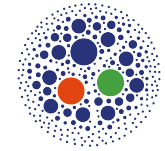


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Introduction & Motivation



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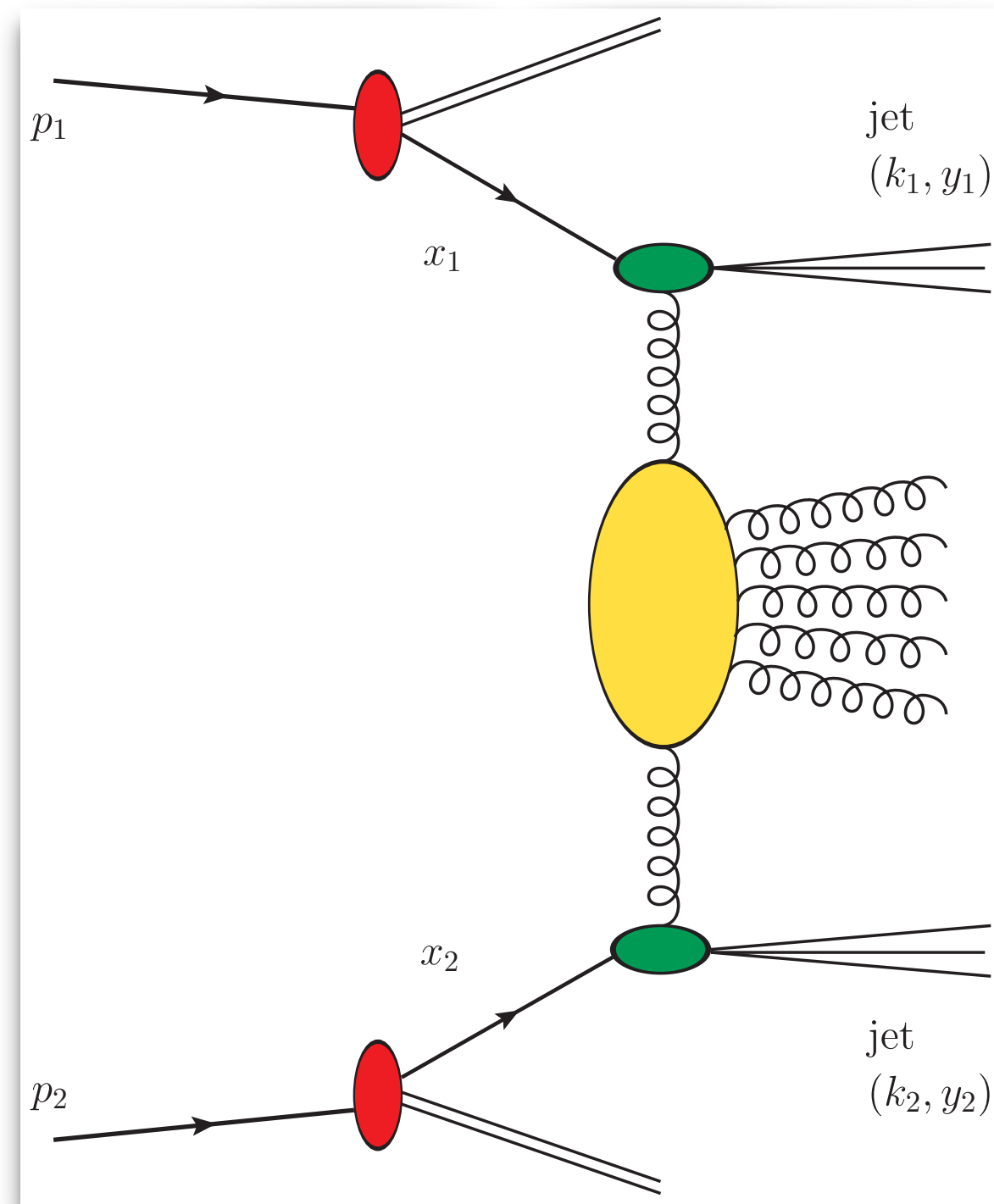
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Natural Stability

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jet vertices  
(off-shell amplitudes)

FPF+ATLAS Coincidence



$$\begin{aligned} \frac{d\hat{\sigma}_{r,s}(x_1 x_2 s, \mu)}{dy_1 dy_2 d^2\vec{k}_1 d^2\vec{k}_2} &= \frac{1}{(2\pi)^2} \\ &\times \int \frac{d^2\vec{q}_1}{\vec{q}_1^2} \mathcal{V}_J^{(r)}(\vec{q}_1, s_0, x_1, \vec{k}_1) \\ &\times \int_{\delta-i\infty}^{\delta+i\infty} \frac{d\omega}{2\pi i} \left(\frac{x_1 x_2 s}{s_0}\right)^\omega \mathcal{G}_\omega(\vec{q}_1, \vec{q}_2) \\ &\times \int \frac{d^2\vec{q}_2}{\vec{q}_2^2} \mathcal{V}_J^{(s)}(\vec{q}_2, s_0, x_2, \vec{k}_2) \end{aligned}$$

BFKL gluon Green's function

Towards Precision Studies

# Mueller-Navelet jets & resummation instabilities

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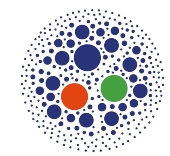
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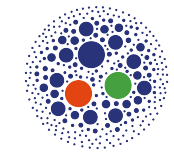
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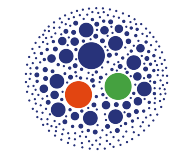
Strong manifestation of higher-order **instabilities** via *scale variation* (i!)

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i At *natural* scales: NLL/LL large, no agreement with data, unphysical values !

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NLA BFKL corrections to cross section with opposite sign with respect to the leading order (LO) result and large in absolute value...

- ◇ ...call for some optimization procedure...
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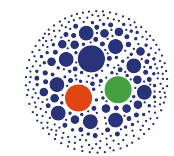
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- ✓ preserve the conformal invariance of an observable...
- ✓ ...by making vanish its  $\beta_0$ -dependent part

\* "Exact" BLM:

suppress NLO IFs + NLO Kernel  $\beta_0$ -dependent factors

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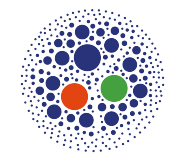
**BLM** scales, theory vs experiment: CMS @7TeV with **symmetric**  $p_T$ -ranges, **only!**

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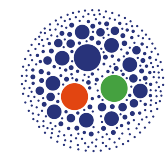
$\mu_R^{\text{BLM}} \gg \mu_R^{\text{nat.}} \Rightarrow d\sigma^{\text{BLM}}/d\sigma^{\text{nat.}} \sim 10^{-(1\div 2)} \Rightarrow$  precision studies hampered



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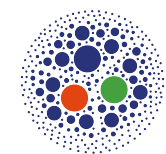
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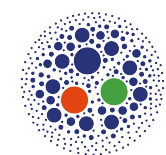
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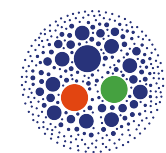
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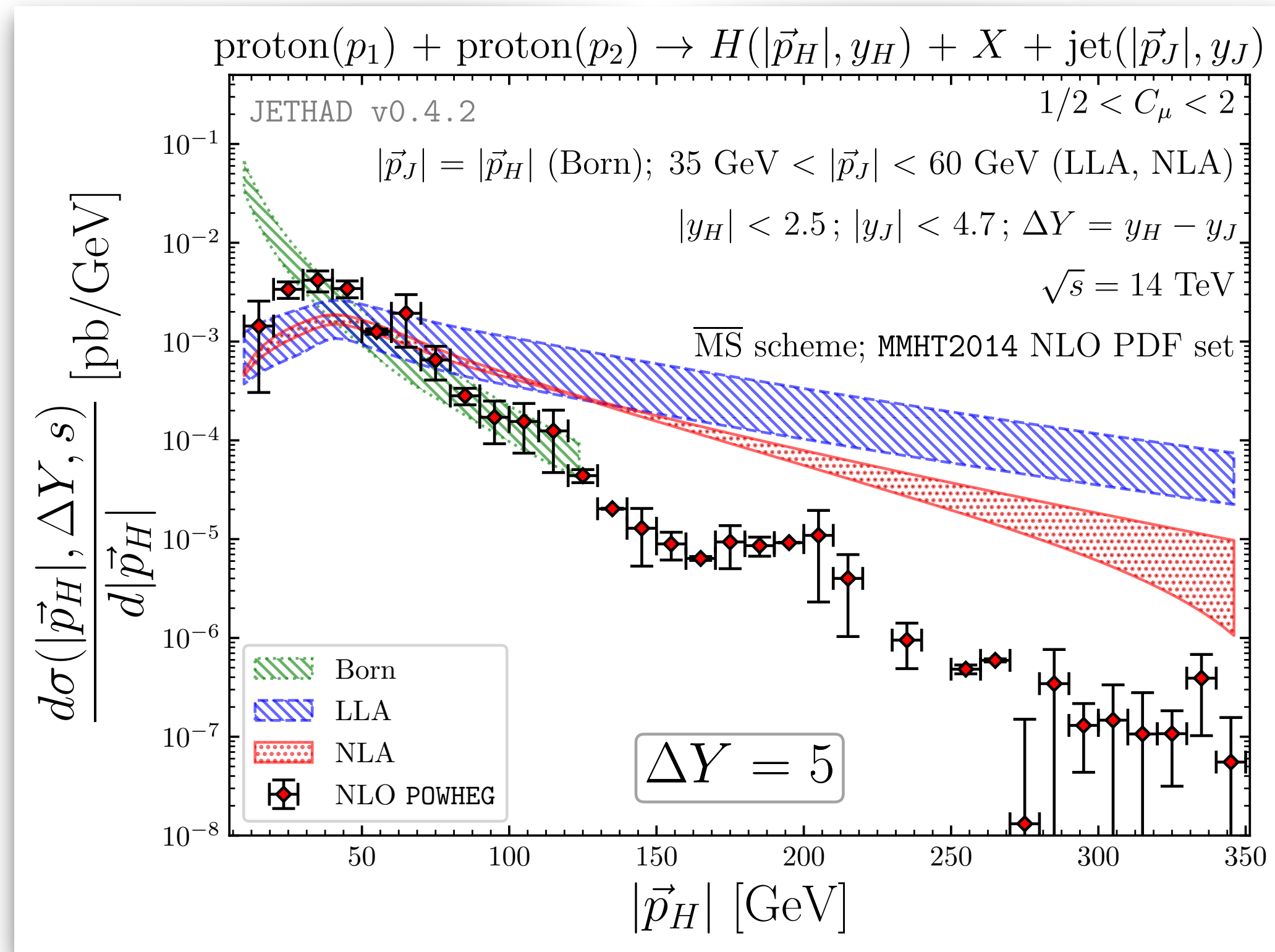
*Unsuccessful* scale optimization  $\rightarrow$  processes featuring *natural stability* (i?)



# Natural stability of the HE resummation

**Higgs + jet**  $\Leftrightarrow$  large transverse masses, partial NLL

[\[F. G. C. et al. \(2021\)\]](#)



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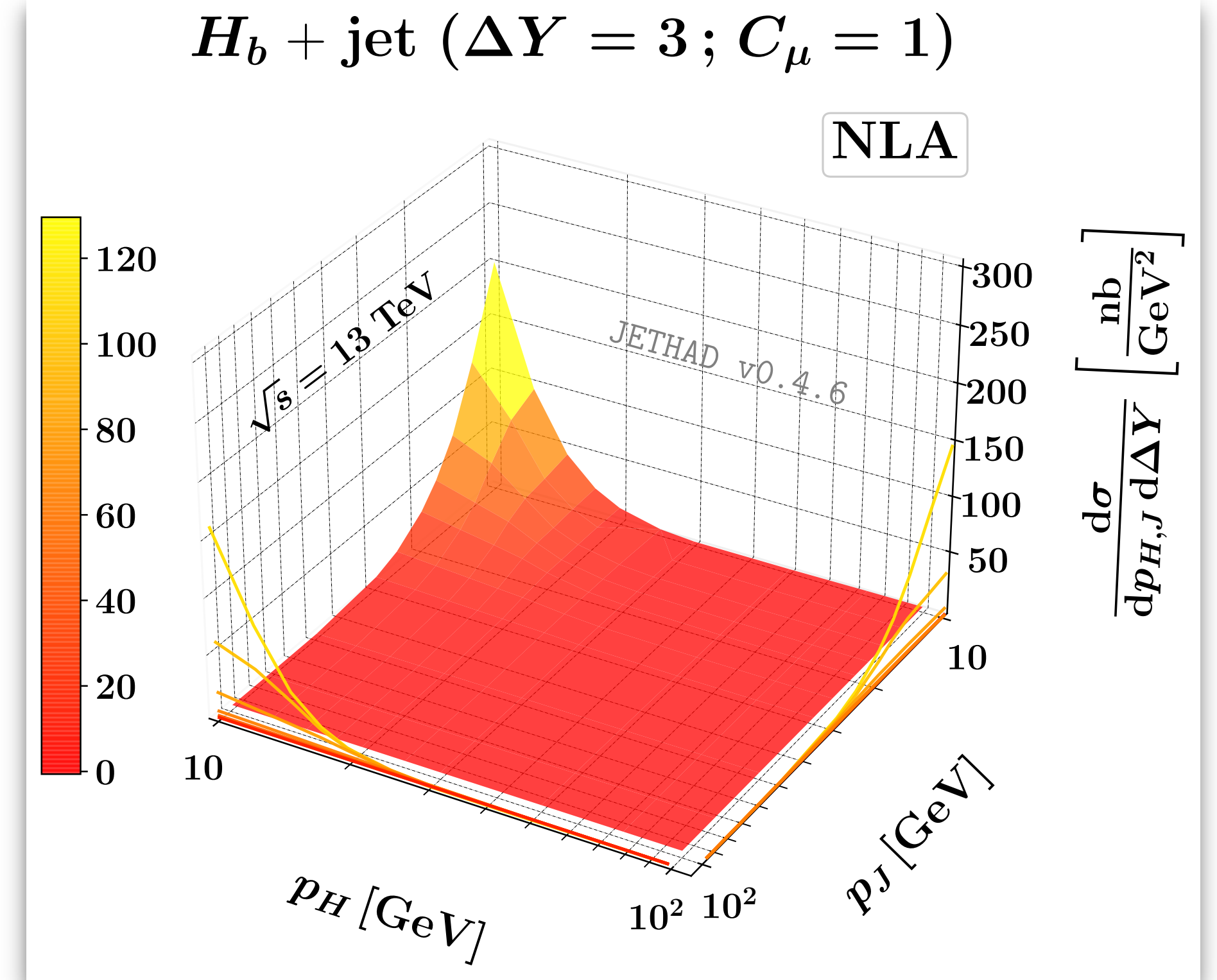
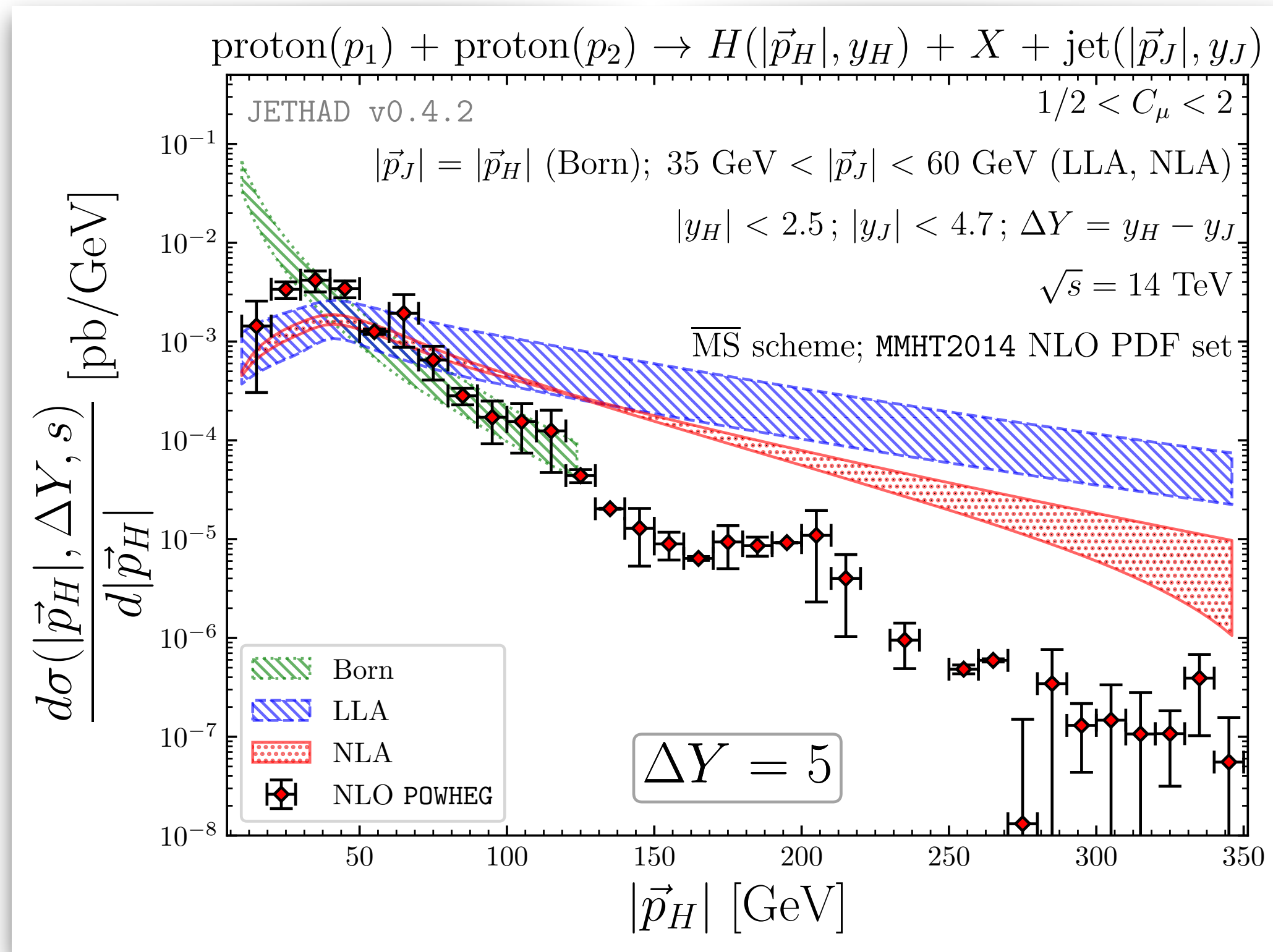
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[F. G. C. et al. (2021)]

**Heavy flavor**  $\Leftrightarrow$   $D^*/\Lambda_c/H_b$  VFNS FFs, full NLL

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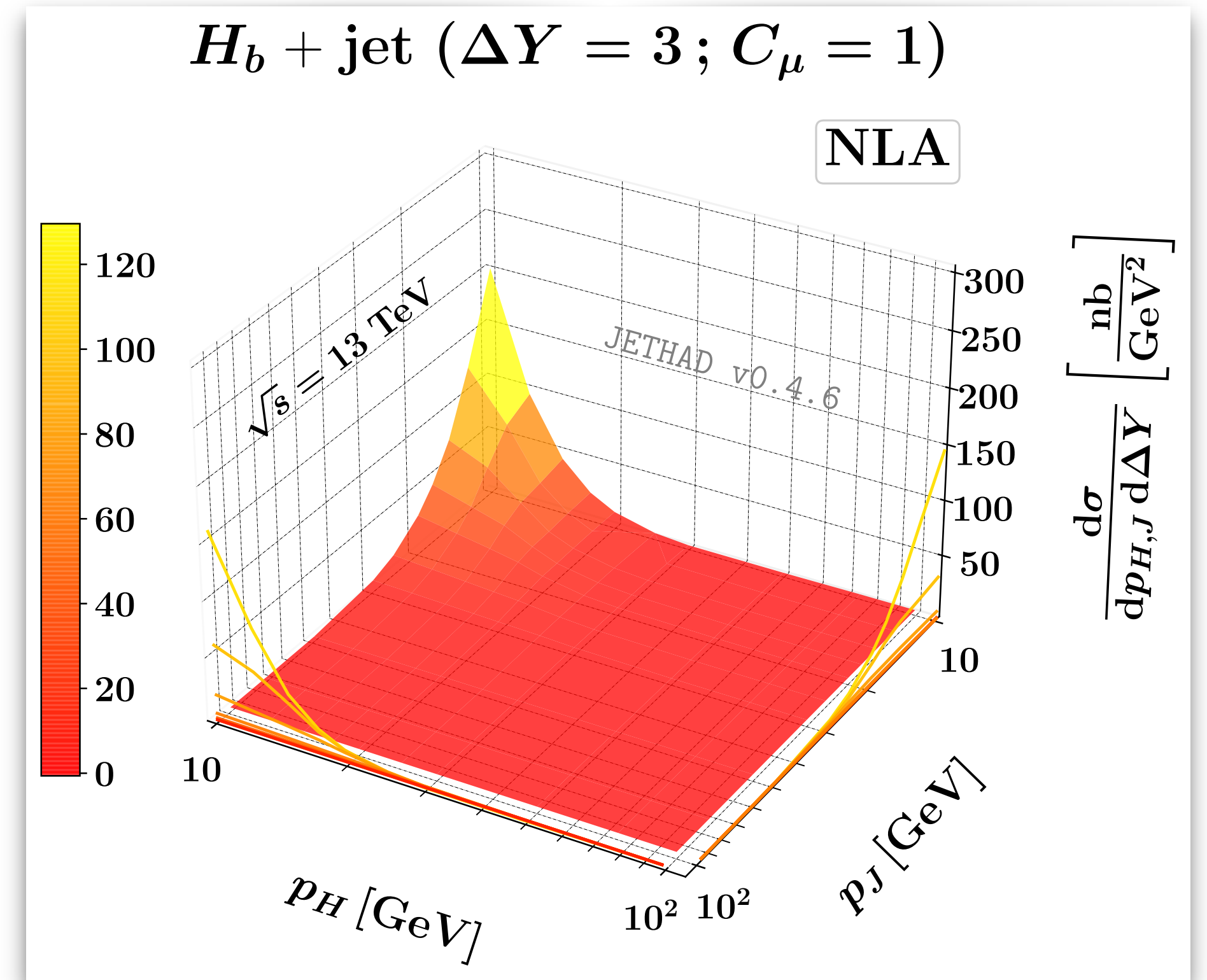
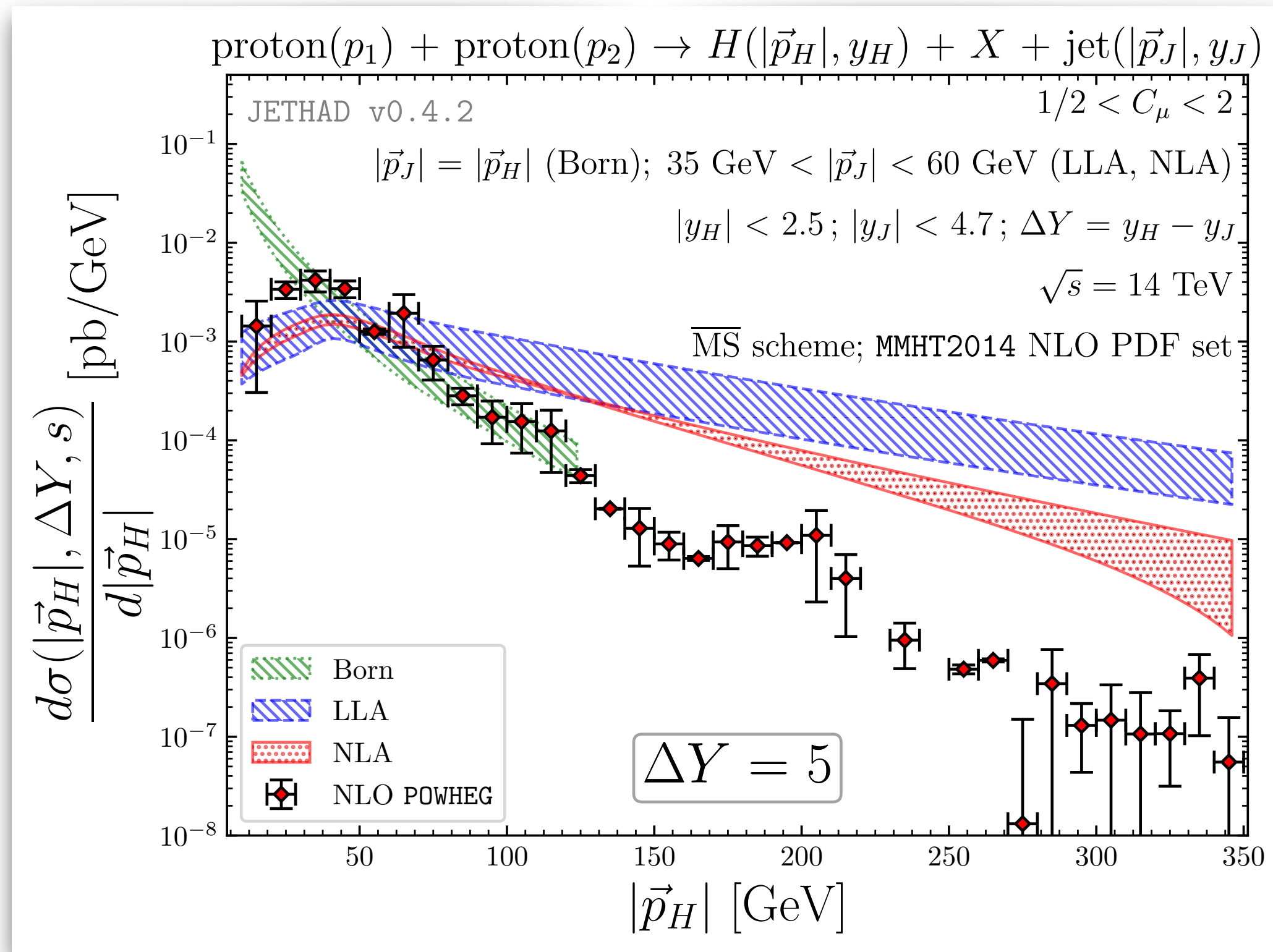
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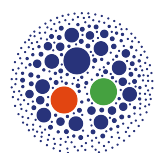


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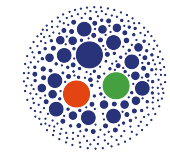
Towards Precision Studies



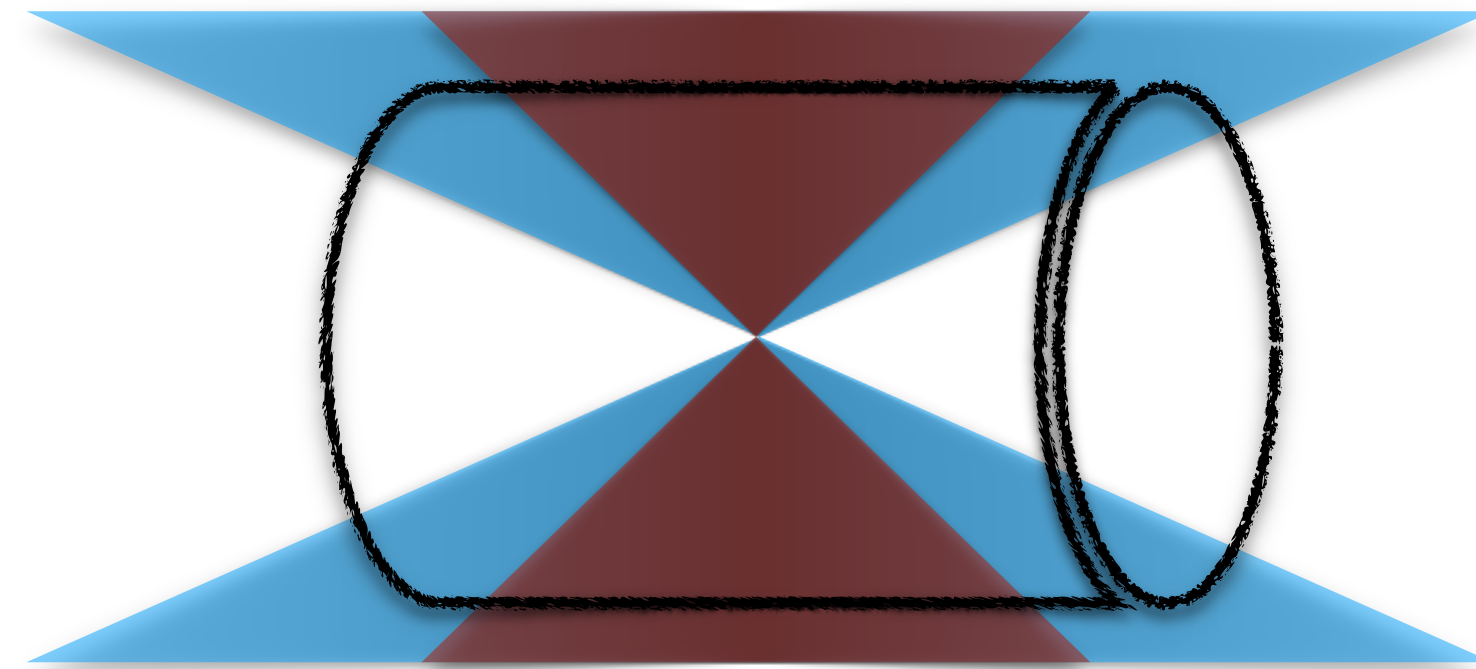
**Natural stability** as a tool to investigate HE dynamics of QCD at the **FPF**



# Light mesons @FPF + heavy flavor @ATLAS



Forward + backward CMS detections: Mueller-Navelet, hadron-jet, di-hadron



$$|y_{\text{jet}}| < 4.7$$

barrel + endcap

$$|y_{\text{hadron}}| < 2.4$$

barrel

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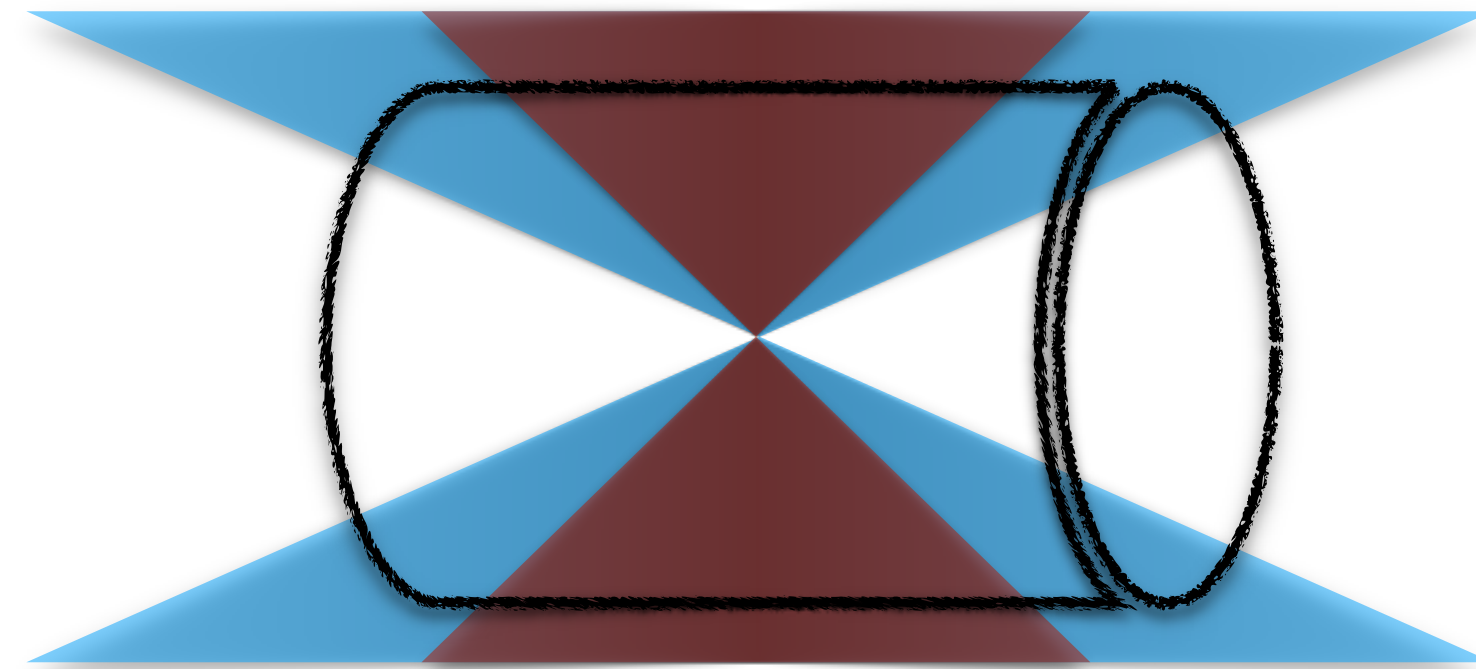
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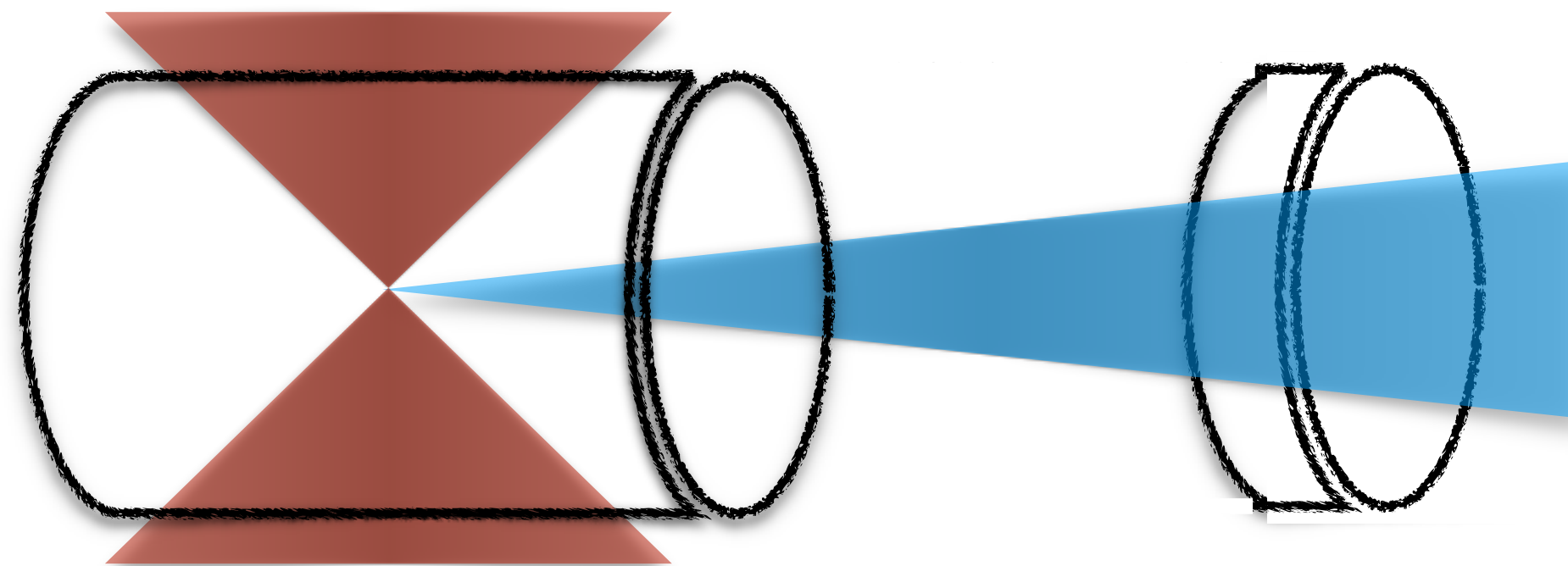
$$|y_{\text{jet}}| < 4.7$$

barrel + endcap

$$|y_{\text{hadron}}| < 2.4$$

barrel

- Ultra-forward FPF + central ATLAS detections: light mesons + heavy flavor



$$5 < y_{\pi, K} < 7$$

FPF

$$|y_{D^*, \Lambda_c, H_b}| < 2.4$$

ATLAS barrel

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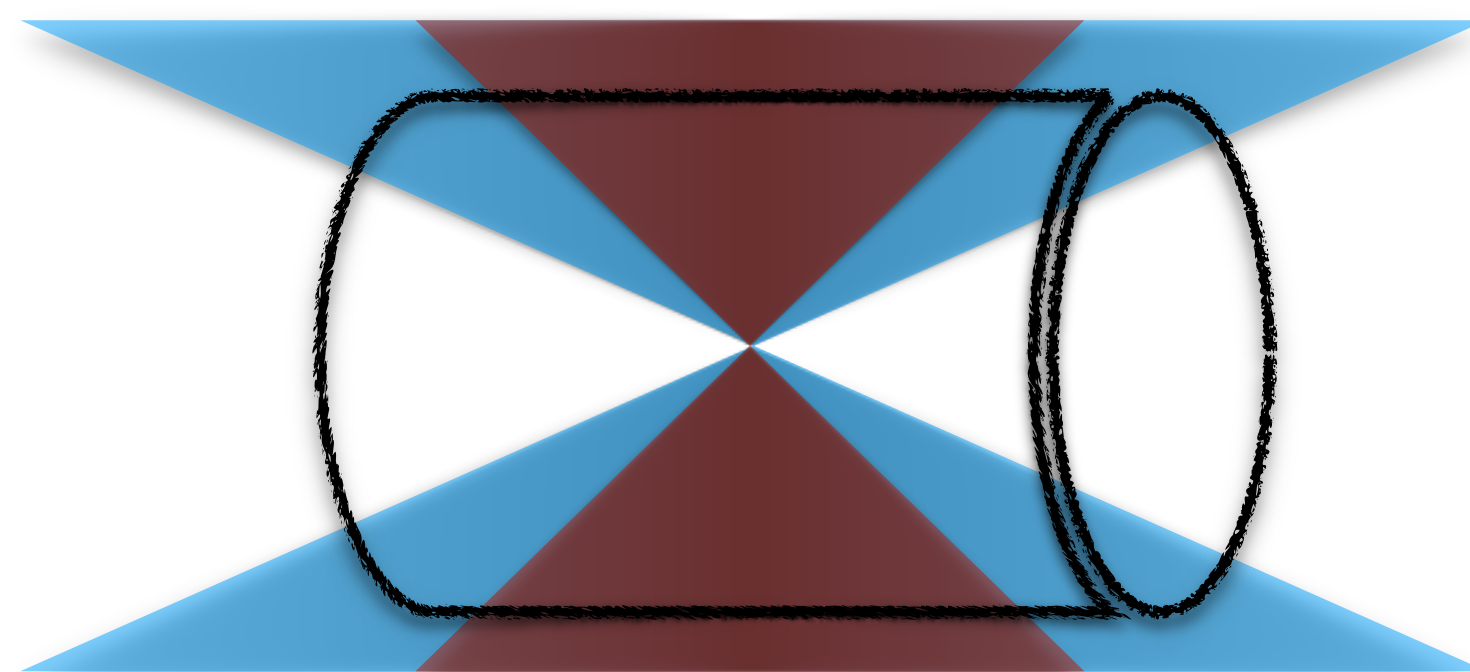
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# Light mesons @FPF + heavy flavor @ATLAS

- Forward + backward CMS detections: Mueller-Navelet, hadron-jet, di-hadron



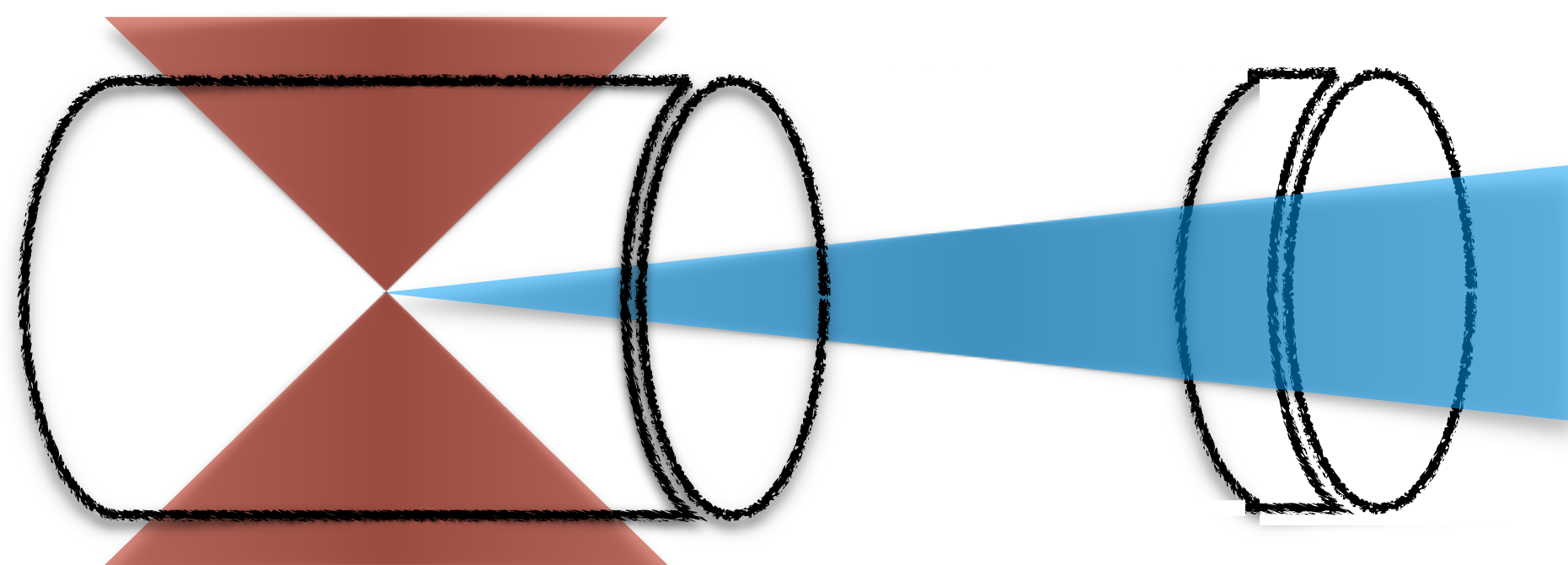
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ATLAS barrel

- Hybrid NLL/collinear factorization vs HE-NLO via the JETHAD method [\[F. G. C. \(2021\)\]](#)

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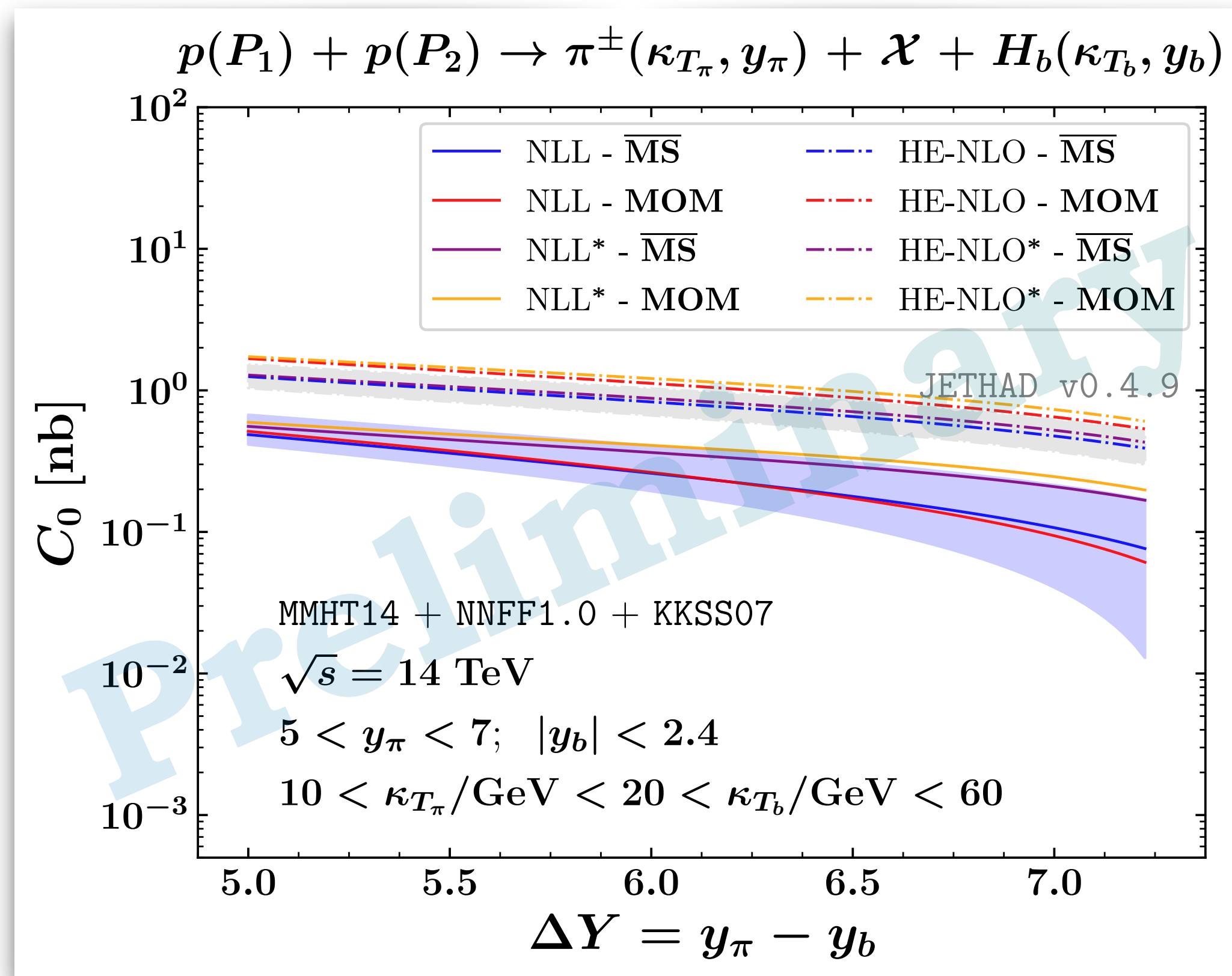
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# Rapidity distribution @FPF+ATLAS

Inclusive  $\pi^\pm$  (FPF) +  $H_b$  (ATLAS) production

[F. G. C. (in preparation)]



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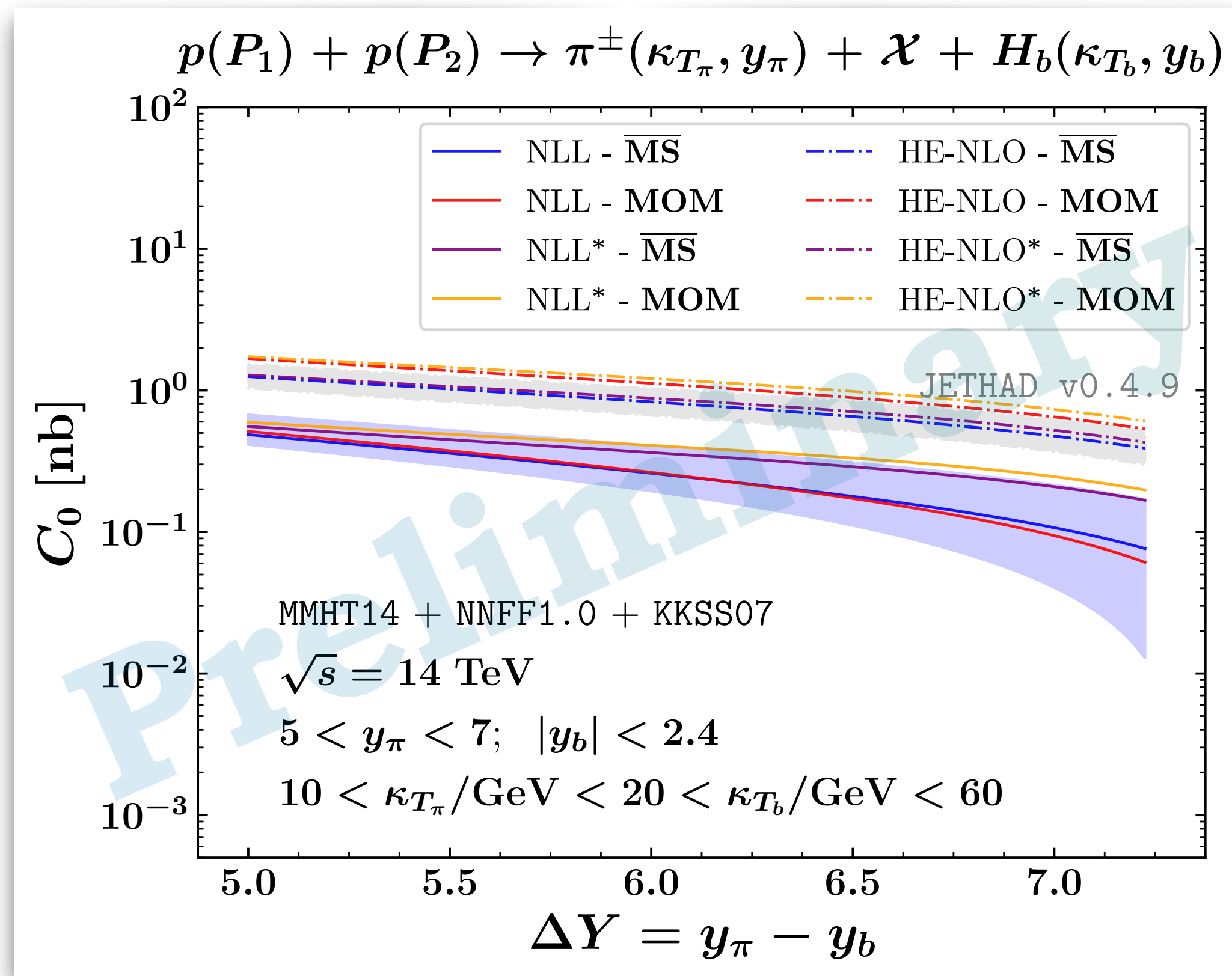
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Inclusive  $\pi^\pm$  (FPF) +  $H_b$  (ATLAS) production

\* ; Natural stability at work !

[F. G. C. (in preparation)]



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# Rapidity distribution @FPF+ATLAS

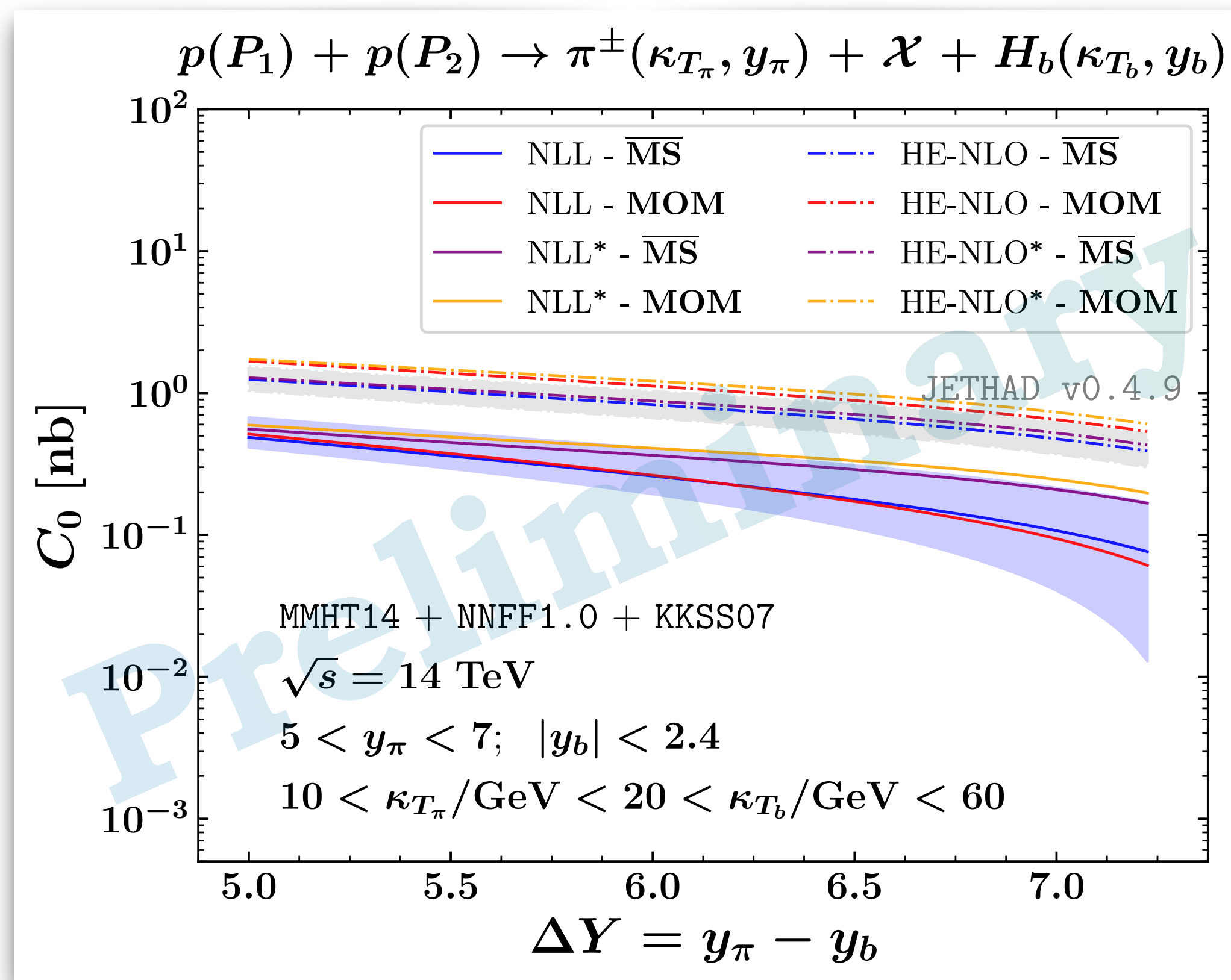
Inclusive  $\pi^\pm$  (FPF) +  $H_b$  (ATLAS) production

[F. G. C. (in preparation)]

\* ; **Natural stability** at work !

\* Scale-variation studies feasible

\* NLL and HE-NLO clearly disengaged



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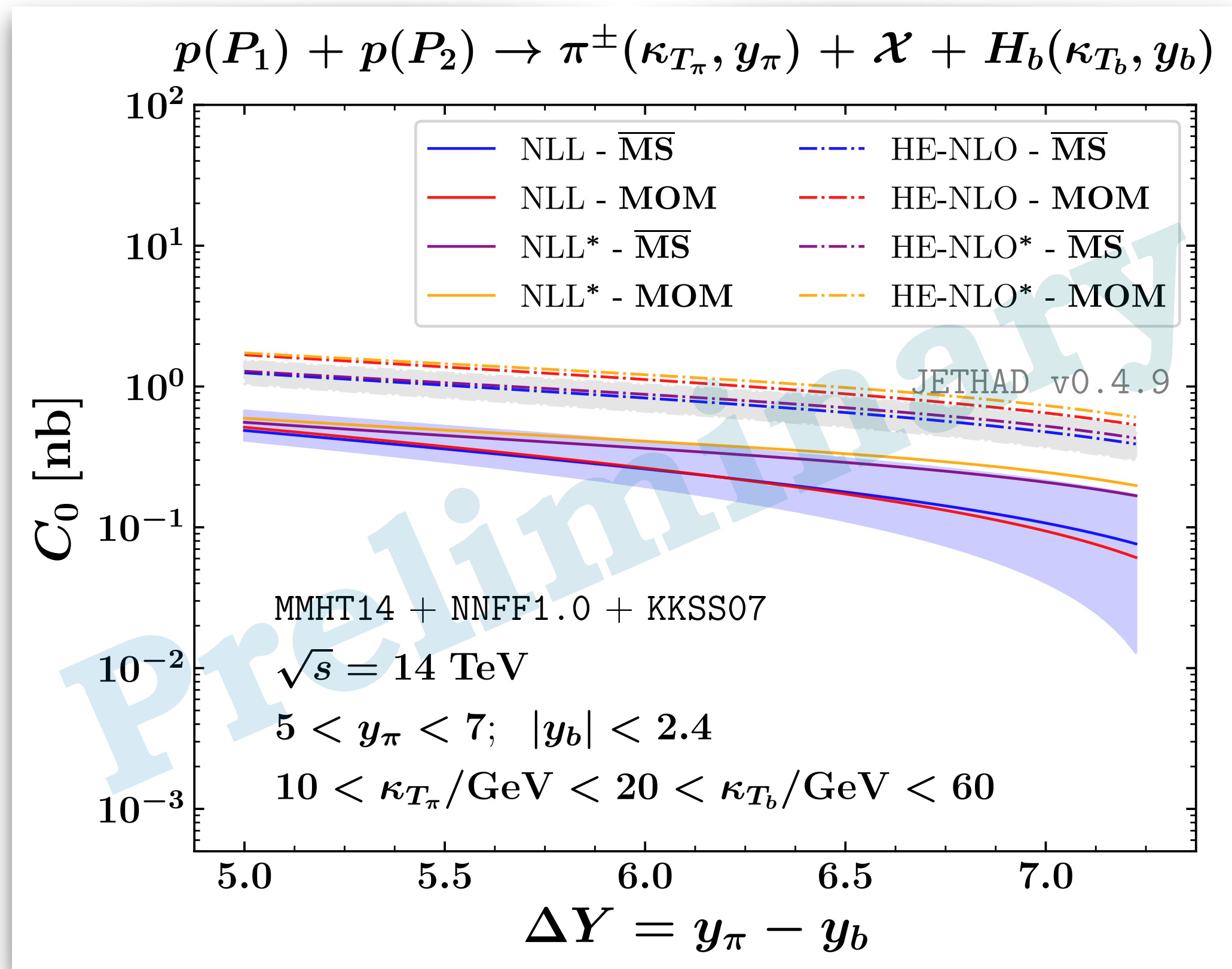
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Inclusive  $\pi^\pm$  (FPF) +  $H_b$  (ATLAS) production

[F. G. C. (in preparation)]



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\* Scale-variation studies feasible

\* NLL and HE-NLO clearly disengaged

\* Systematic uncertainties

NLL\*: NNLL effects via BFKL repres.

MOM scheme: upper limit (overestimate)

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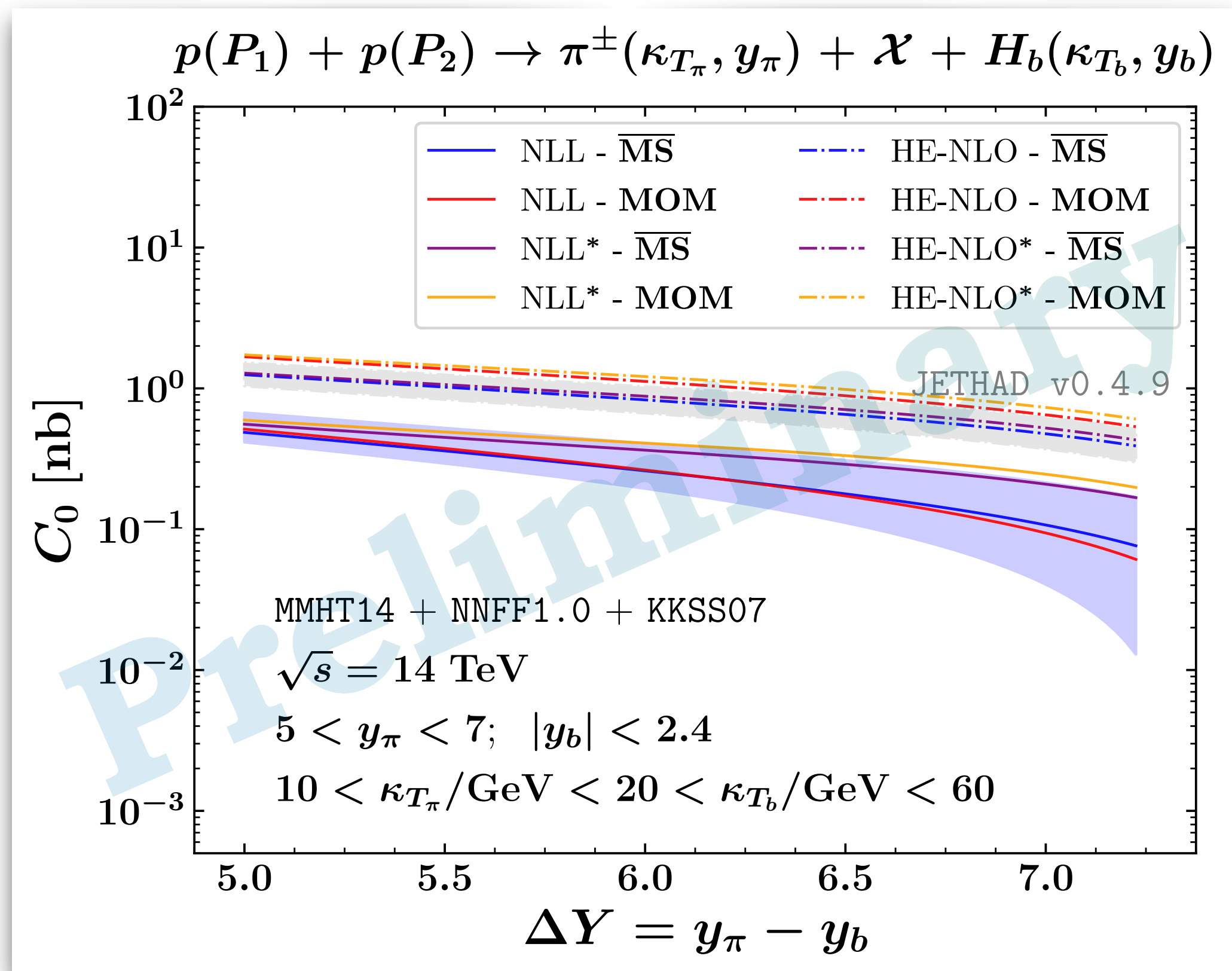
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# Rapidity distribution @FPF+ATLAS

Inclusive  $\pi^\pm$  (FPF) +  $H_b$  (ATLAS) production

[F. G. C. (in preparation)]



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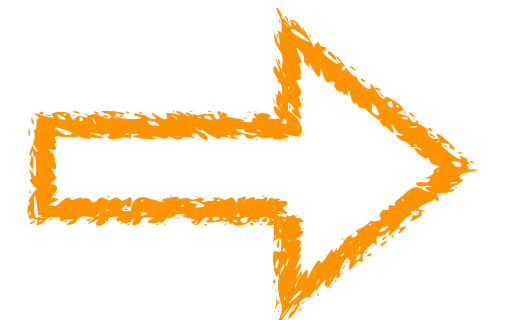
\* Systematic uncertainties

NLL\*: NNLL effects via BFKL repres.

MOM scheme: upper limit (overestimate)

\* **HE resummation** plays a **key role**

\* **Chance to probe PDFs and FFs**



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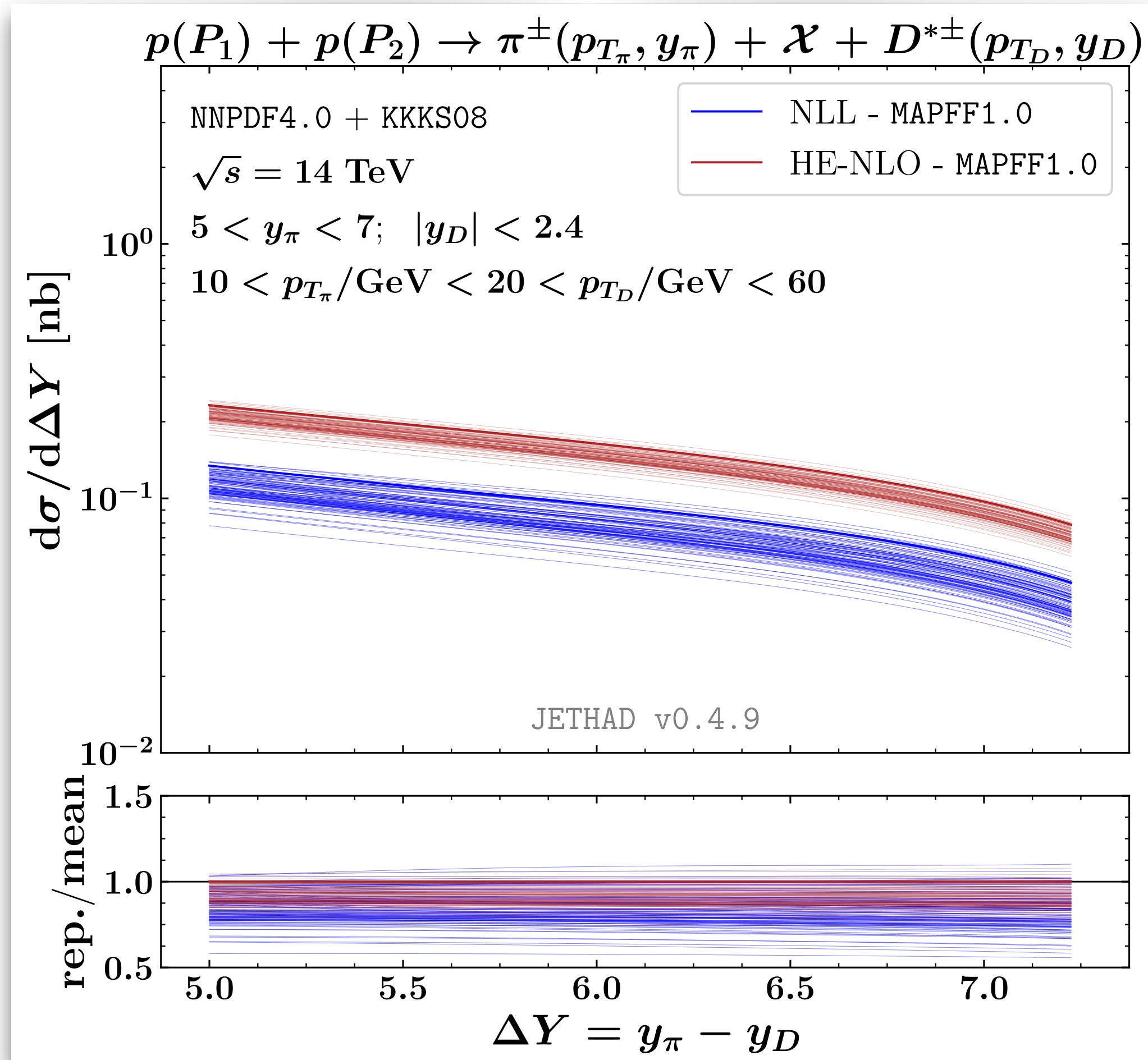
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# Rapidity distribution @FPF+ATLAS

Inclusive  $\pi^\pm$  (FPF) +  $D^{*\pm}$  (ATLAS) production

[FPF Snowmass Whitepaper]



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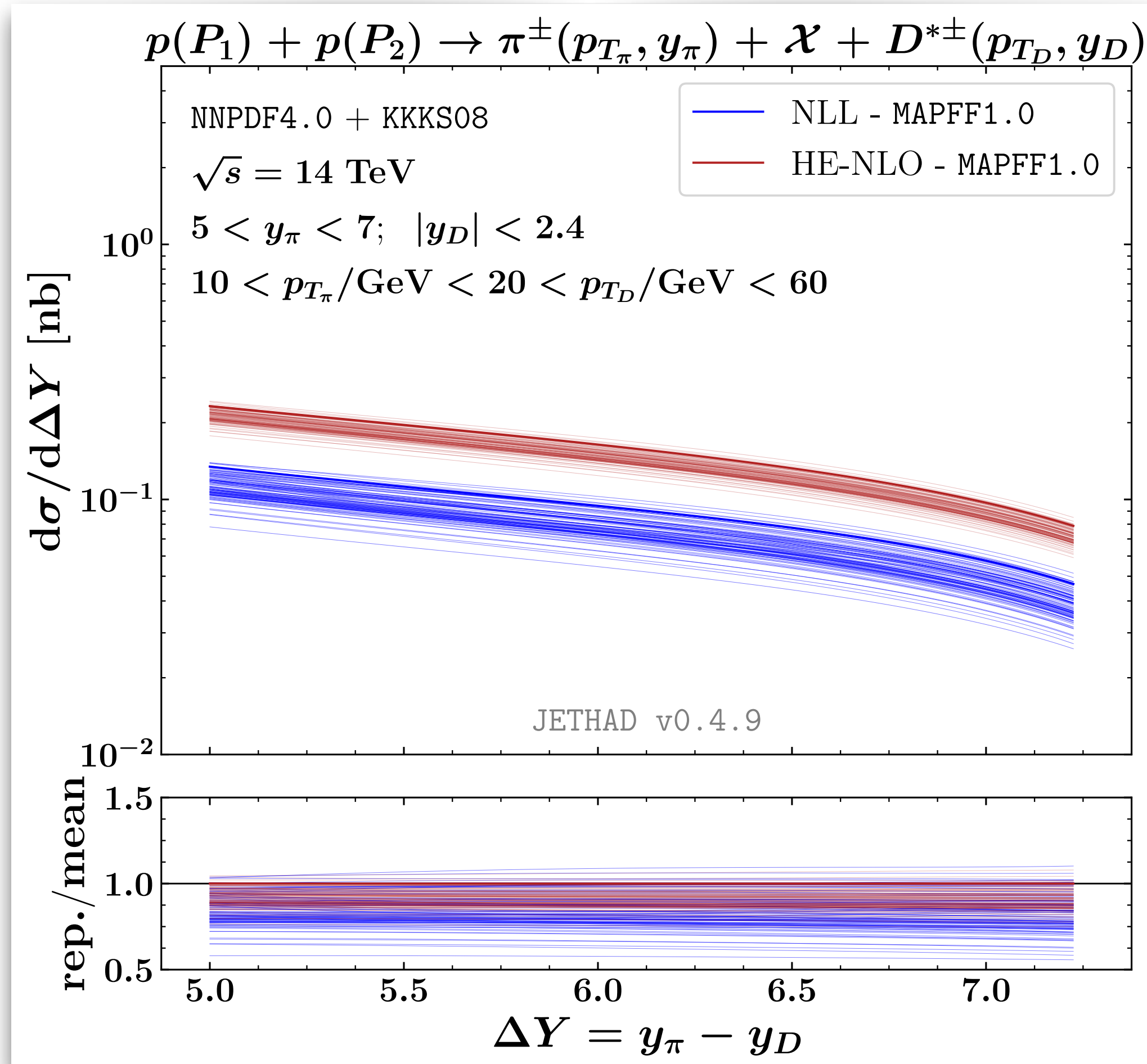
# Rapidity distribution @FPF+ATLAS

**Inclusive  $\pi^\pm$  (FPF) +  $D^{*\pm}$  (ATLAS) production**

[FPF Snowmass Whitepaper]

\* Impact of collinear FFs on  $\Delta Y$ -distribution

\* **Replica method** at work



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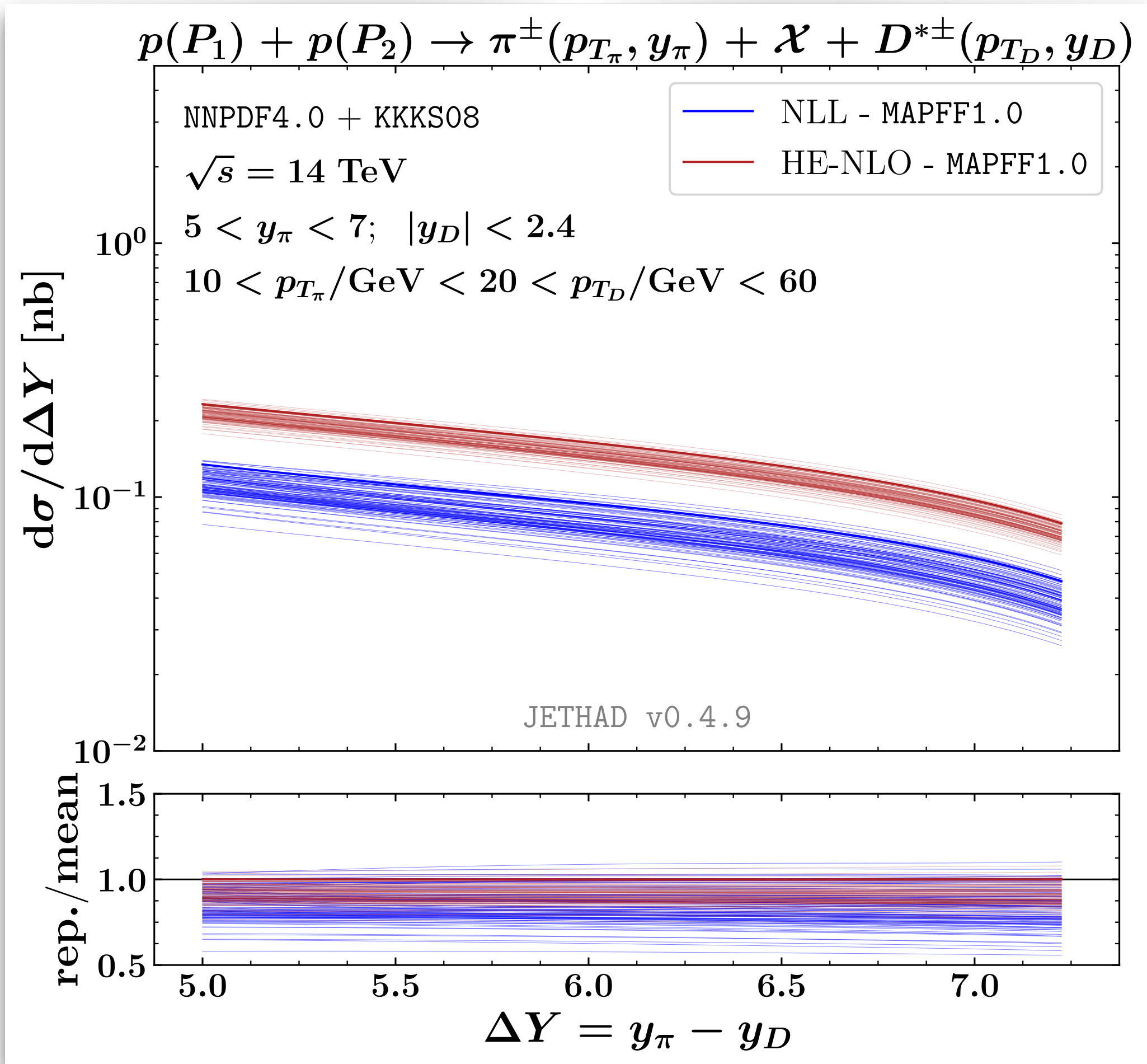
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# Rapidity distribution @FPF+ATLAS

**Inclusive  $\pi^\pm$  (FPF) +  $D^{*\pm}$  (ATLAS) production**

[FPF Snowmass Whitepaper]



\* Impact of collinear FFs on  $\Delta Y$ -distribution

\* **Replica method** at work

\* Larger spread of replicas at NLL

\* Probe FFs in complementary ranges

Weight of FF replicas in the same set

Different sets via *functional correlation*?

\* **Complementary studies on FFs**

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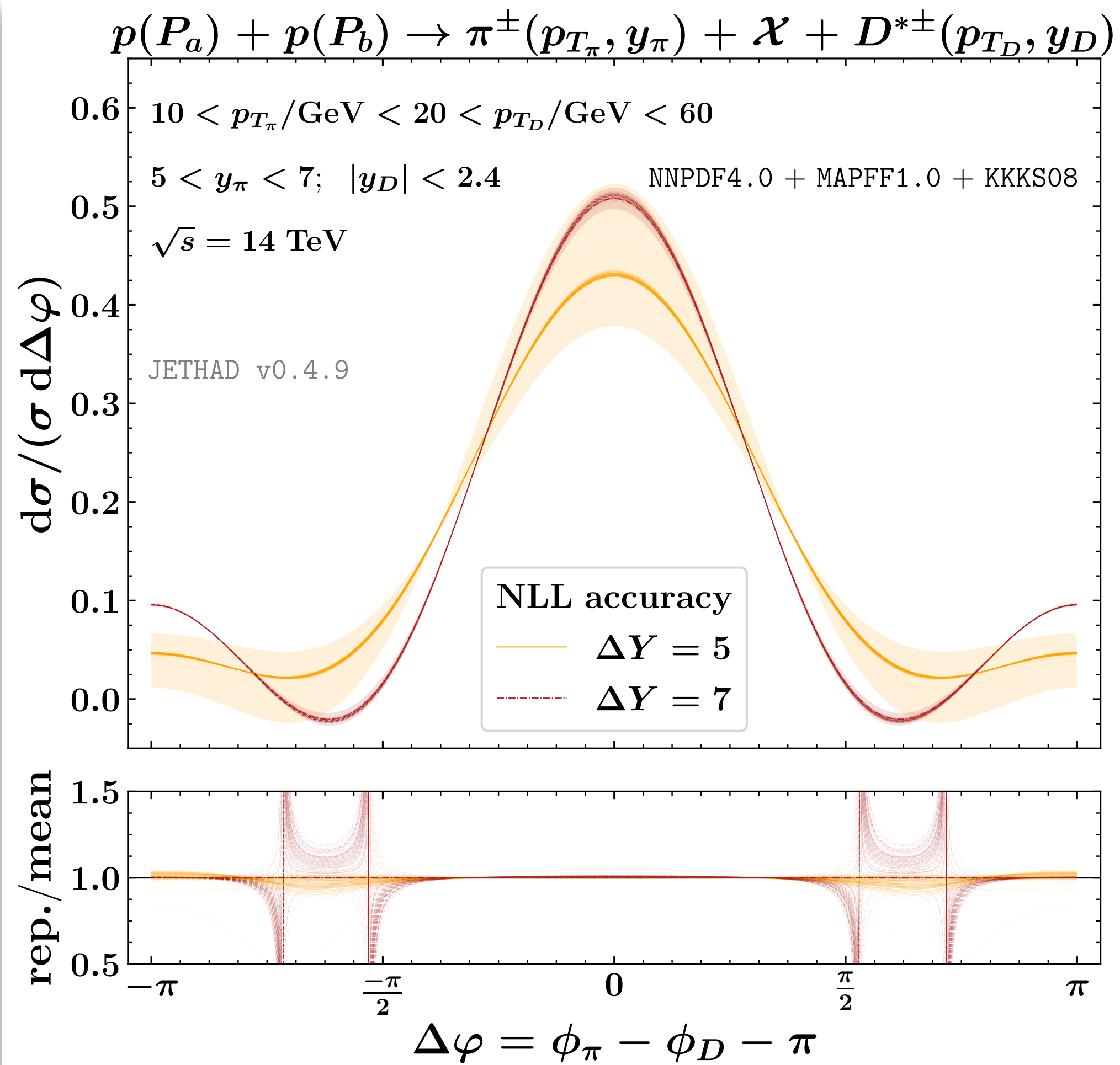
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# Azimuthal distribution @FPF+ATLAS

Inclusive  $\pi^\pm$  (FPF) +  $D^{*\pm}$  (ATLAS) production

[FPF Snowmass Whitepaper]



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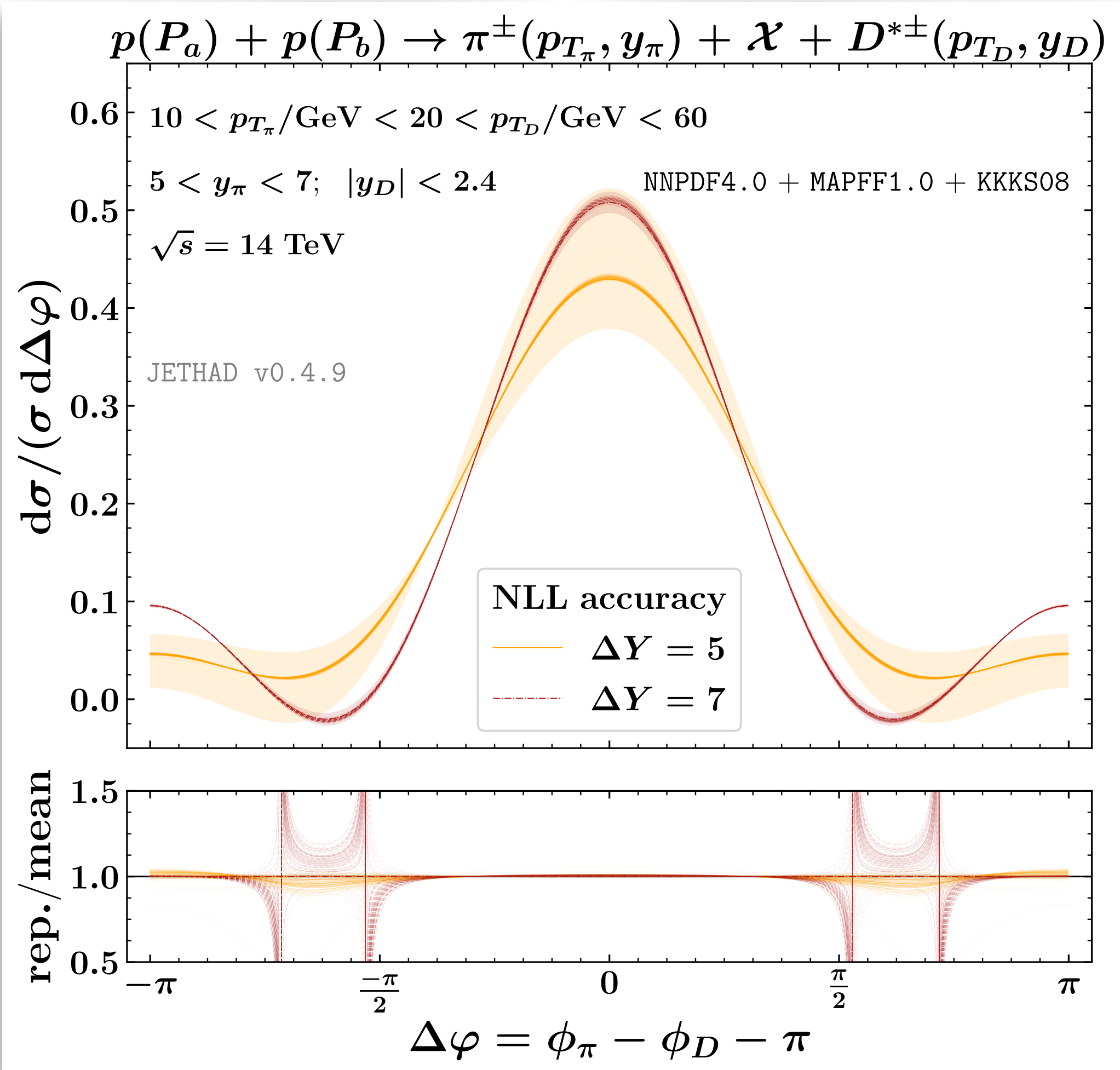
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# Azimuthal distribution @FPF+ATLAS

**Inclusive  $\pi^\pm$  (FPF) +  $D^{*\pm}$  (ATLAS) production**

[FPF Snowmass Whitepaper]

- \* Signals from *all azimuthal modes*
- \* Easy to be analyzed from data
- \* **Multiplicity:** PDF/FF effects quenched



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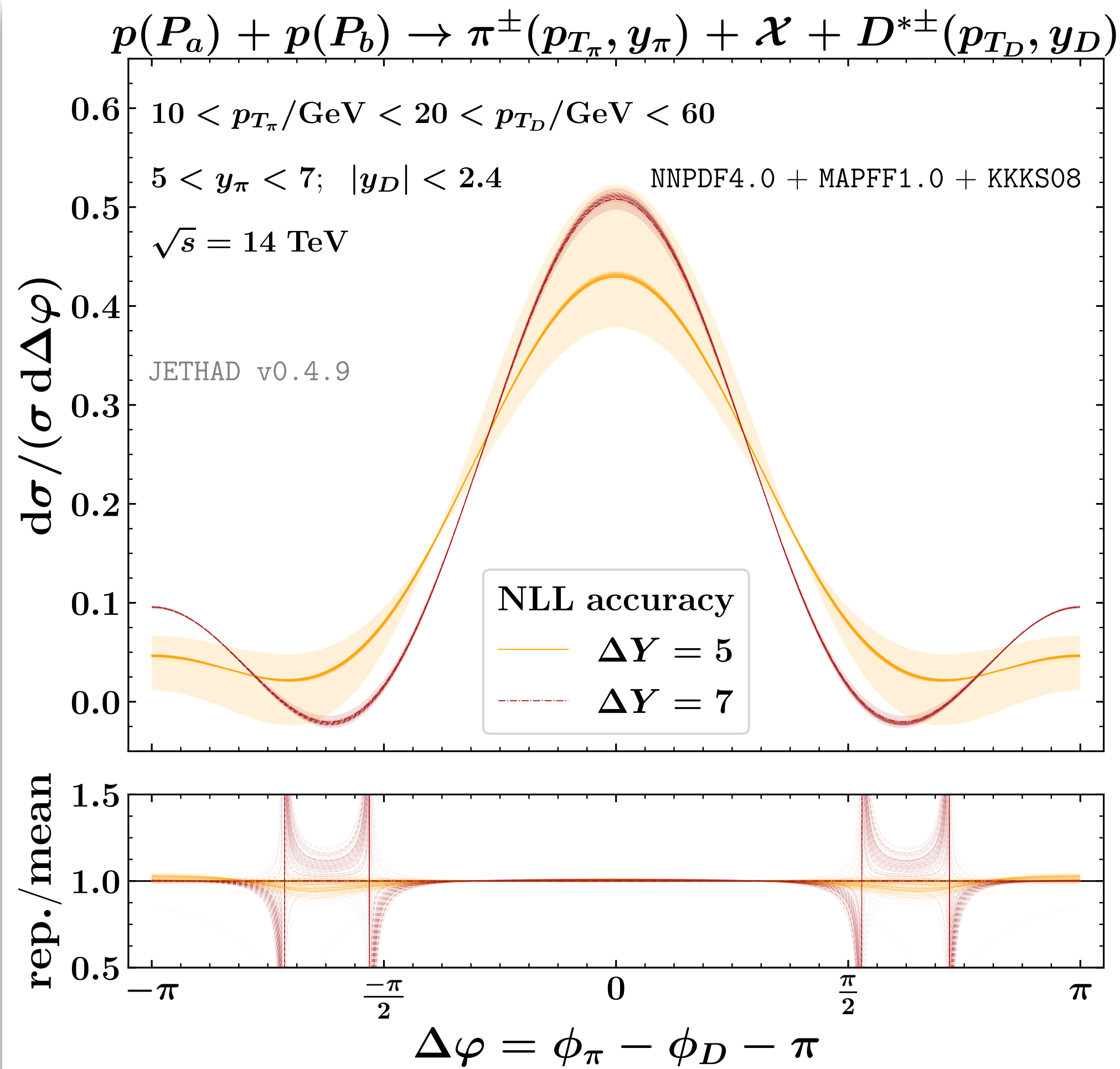


# Azimuthal distribution @FPF+ATLAS

Inclusive  $\pi^\pm$  (FPF) +  $D^{*\pm}$  (ATLAS) production

[FPF Snowmass Whitepaper]

- \* Signals from *all azimuthal modes*
  - \* Easy to be analyzed from data
  - \* **Multiplicity:** PDF/FF effects quenched
  - \* *Novel and unexpected* features
- Peak behavior  $\rightarrow$  **re-correlation** pattern
- Possible **threshold** contamination



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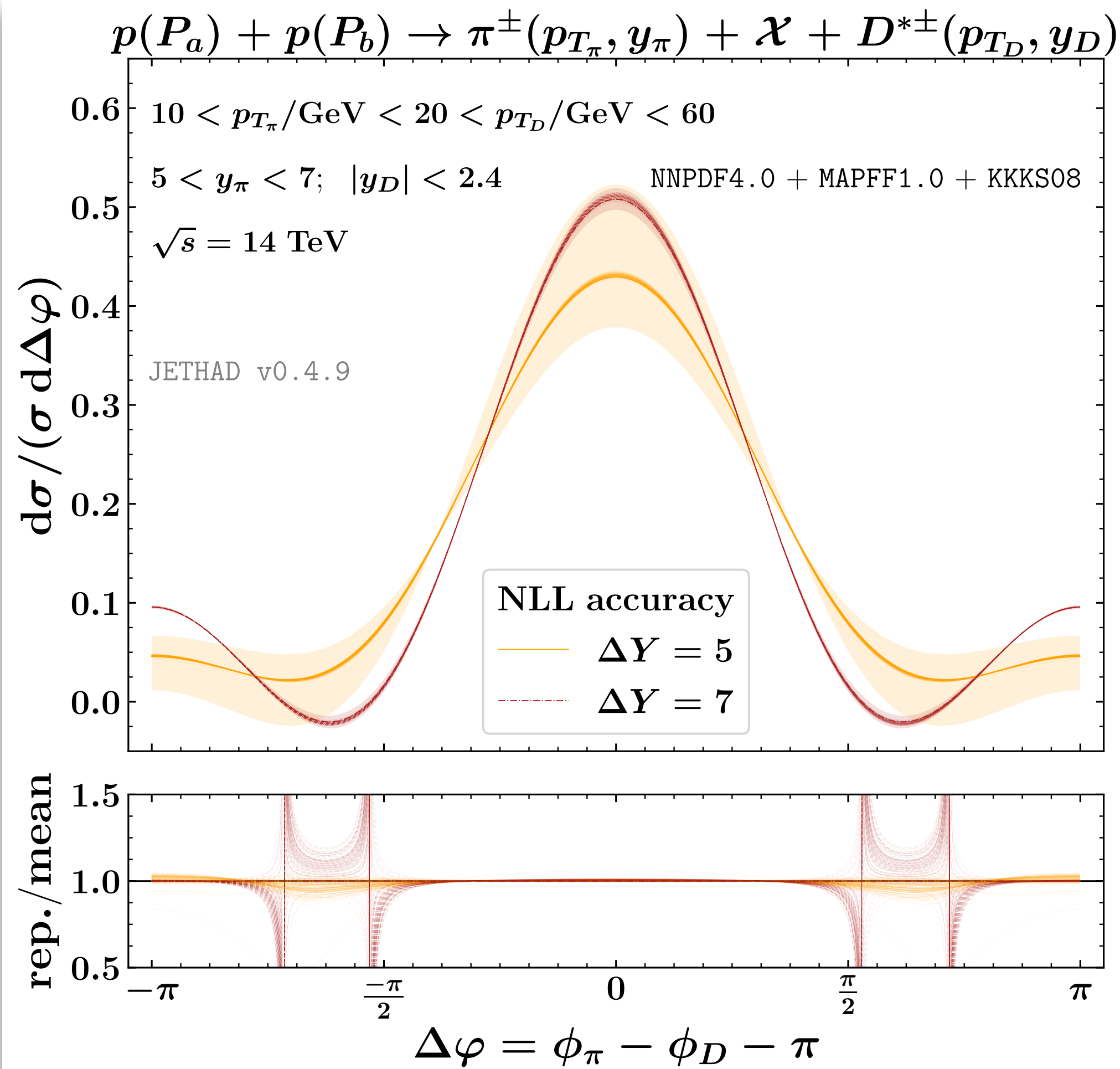
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# Azimuthal distribution @FPF+ATLAS

Inclusive  $\pi^\pm$  (FPF) +  $D^{*\pm}$  (ATLAS) production

[FPF Snowmass Whitepaper]



\* Signals from *all azimuthal modes*

\* Easy to be analyzed from data

\* **Multiplicity:** PDF/FF effects quenched

\* *Novel and unexpected* features

Peak behavior → **re-correlation** pattern

Possible **threshold** contamination

\* *Stringent* tests of **HE resummation**

\* **Chance to explore other resummations**

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# Towards new directions

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- ☑ *FPF + ATLAS coincidence* → **high discovery potential** of QCD
- ☑ **Significant impact** of *HE dynamics* on *fixed-order* calculations
- ☑ *Rapidity distribution* → **constrain FFs** in **complementary** ranges
- ☑ *Azimuthal distribution* → **hunt** for **novel HE features**  
→ **explore interplay** with other **resummations**



# Towards new directions

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- FPF + ATLAS coincidence* → **high discovery potential** of QCD
- Significant impact** of *HE dynamics* on *fixed-order* calculations
- Rapidity distribution* → **constrain FFs** in **complementary** ranges
- Azimuthal distribution* → **hunt** for **novel HE features**  
→ **explore interplay** with other **resummations**
- Theory: *multi-lateral formalism* → **encode** those resummations
- Pheno: *Heavy-hadron* production at the FPF → **flavor** studies  
*Hadronic structure* at the FPF → **HE/coll./TMD interplay**

**Backup  
slides**

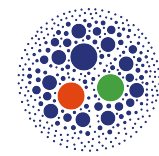
# Inclusive Higgs + jet: azimuthal coefficients

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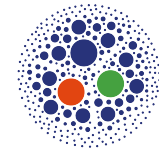
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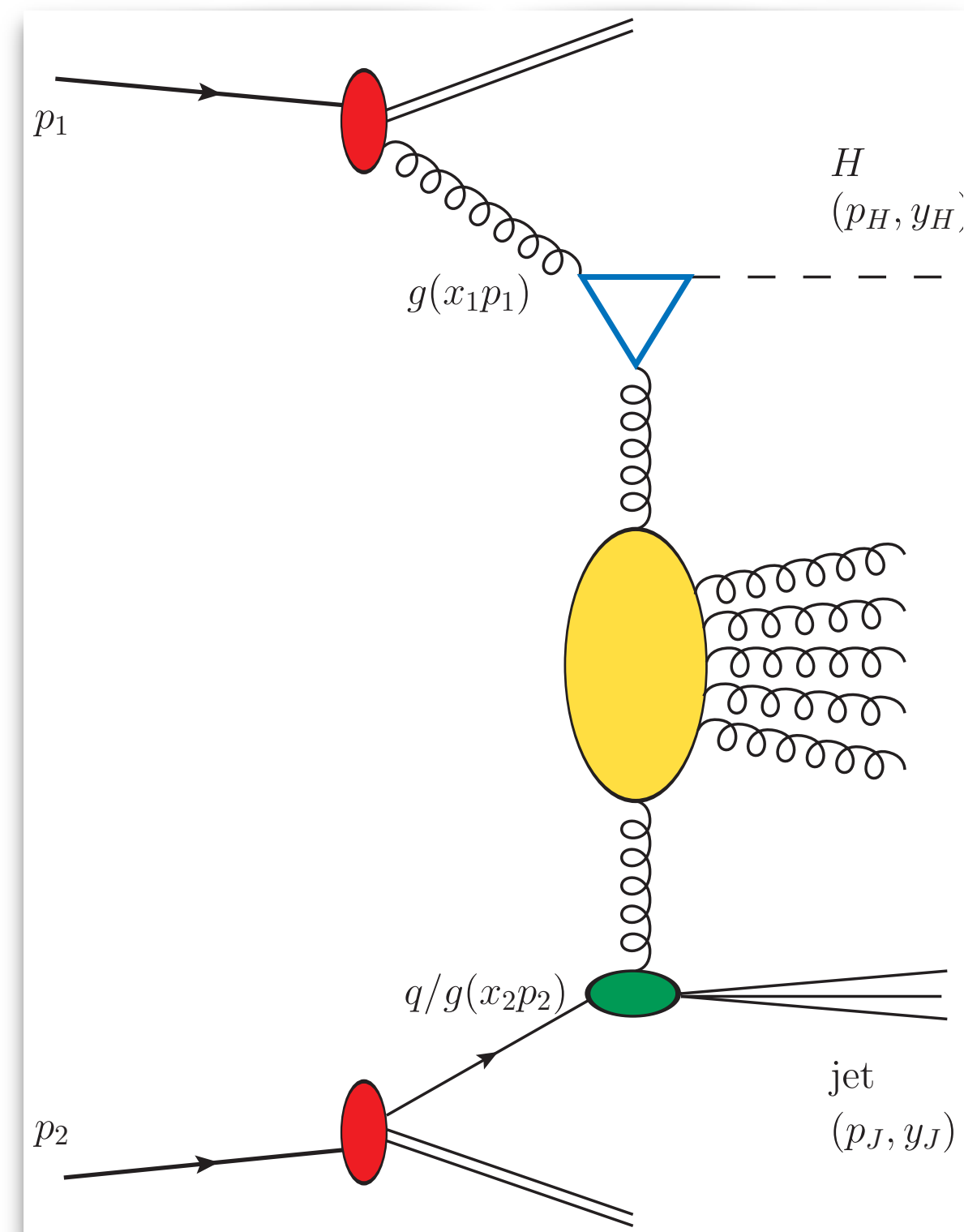
Inclusive h.p. of a Higgs + jet system with high  $p_T$  and large rapidity separation,  $\Delta Y$



Large energy scales expected to **stabilize** the high-energy resummed series

$$\frac{d\sigma}{dx_1 dx_2 d|\vec{p}_H| d|\vec{p}_J| d\varphi_H d\varphi_J} = \frac{1}{(2\pi)^2} \left[ \mathcal{C}_0 + \sum_{n=1}^{\infty} 2 \cos(n\varphi) \mathcal{C}_n \right]$$

$$\varphi = \varphi_H - \varphi_J - \pi$$

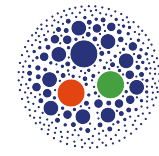


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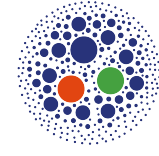


# Inclusive Higgs + jet: azimuthal coefficients

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Inclusive h.p. of a Higgs + jet system with high  $p_T$  and large rapidity separation,  $\Delta Y$



Large energy scales expected to **stabilize** the high-energy resummed series

Natural Stability

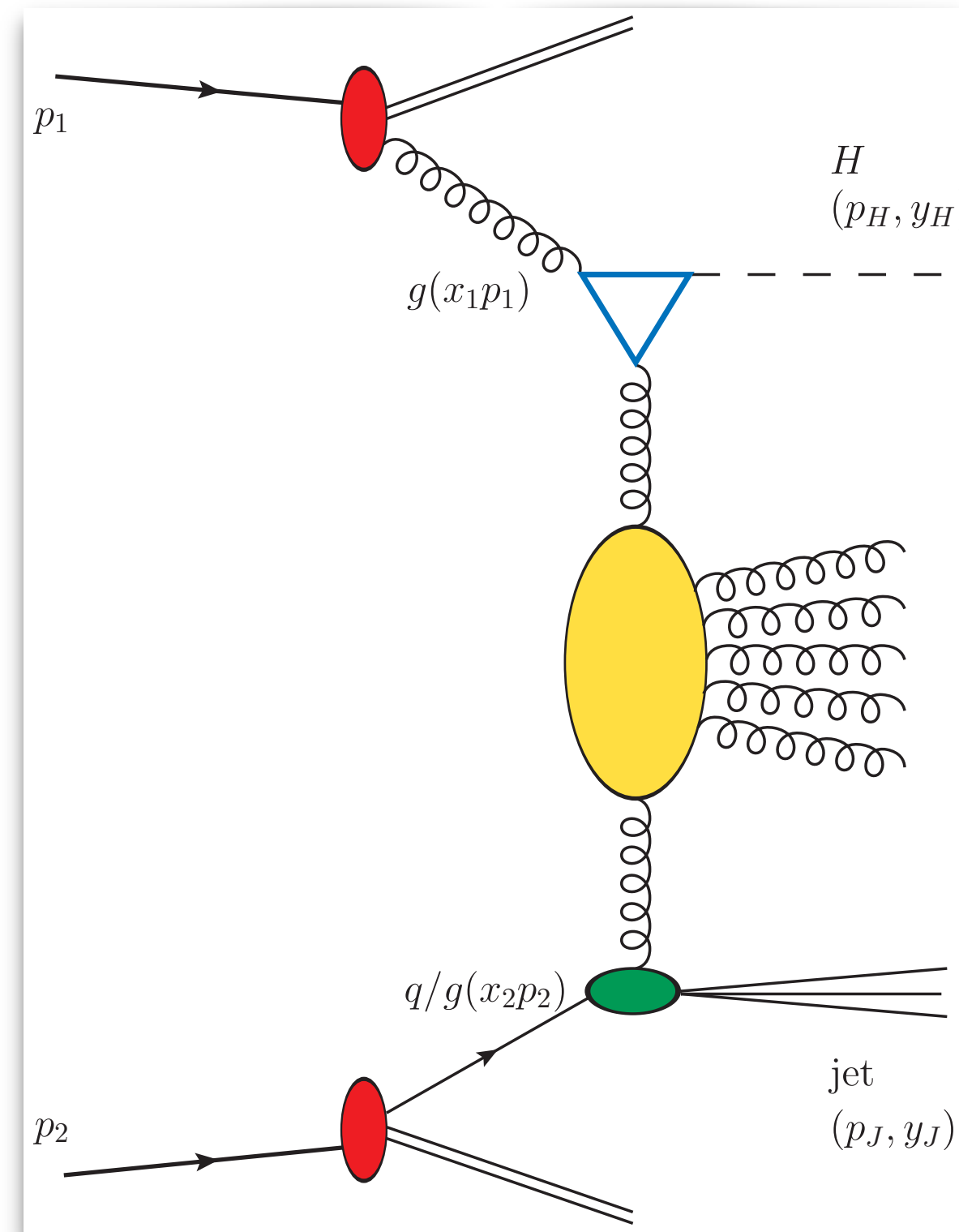
$$\frac{d\sigma}{dx_1 dx_2 d|\vec{p}_H| d|\vec{p}_J| d\varphi_H d\varphi_J} = \frac{1}{(2\pi)^2} \left[ \mathcal{C}_0 + \sum_{n=1}^{\infty} 2 \cos(n\varphi) \mathcal{C}_n \right]$$

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FPF+ATLAS Coincidence

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Higgs vertex  
(off-shell amplitude)

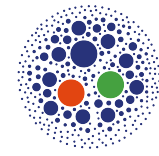
jet vertex  
(off-shell amplitude)

$$\begin{aligned} \frac{d\hat{\sigma}_{r,s}(x_1 x_2 s, \mu)}{dy_H dy_J d^2\vec{p}_H d^2\vec{p}_J} &= \frac{1}{(2\pi)^2} \\ &\times \int \frac{d^2\vec{q}_1}{\vec{q}_1^2} \mathcal{V}_H^{(r)}(\vec{q}_1, s_0, x_1, \vec{p}_H) \\ &\times \int_{\delta-i\infty}^{\delta+i\infty} \frac{d\omega}{2\pi i} \left( \frac{x_1 x_2 s}{s_0} \right)^\omega \mathcal{G}_\omega(\vec{q}_1, \vec{q}_2) \\ &\times \int \frac{d^2\vec{q}_2}{\vec{q}_2^2} \mathcal{V}_J^{(s)}(\vec{q}_2, s_0, x_2, \vec{p}_J) \end{aligned}$$

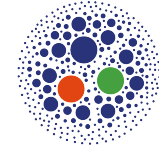
BFKL gluon Green's function

# Inclusive Higgs + jet: azimuthal coefficients

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Inclusive h.p. of a Higgs + jet system with high  $p_T$  and large rapidity separation,  $\Delta Y$



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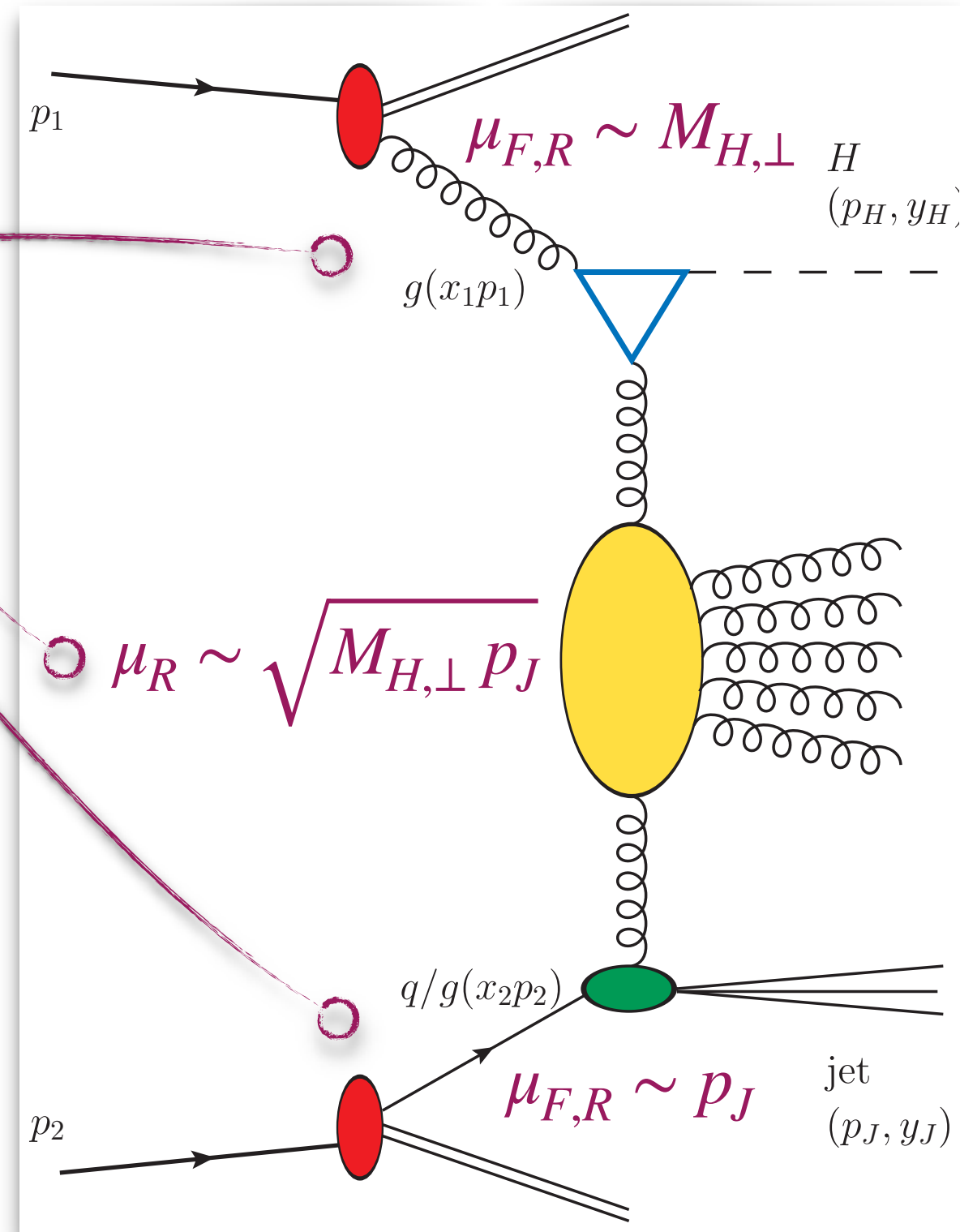
$$\varphi = \varphi_H - \varphi_J - \pi$$

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Higgs vertex  
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jet vertex  
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BFKL gluon Green's function

# Azimuthal correlations: $C_1/C_0 \equiv \langle \cos \varphi \rangle$ Backup

$$\varphi = \varphi_1 - \varphi_2 - \pi$$

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# Azimuthal correlations: $C_1/C_0 \equiv \langle \cos \varphi \rangle$

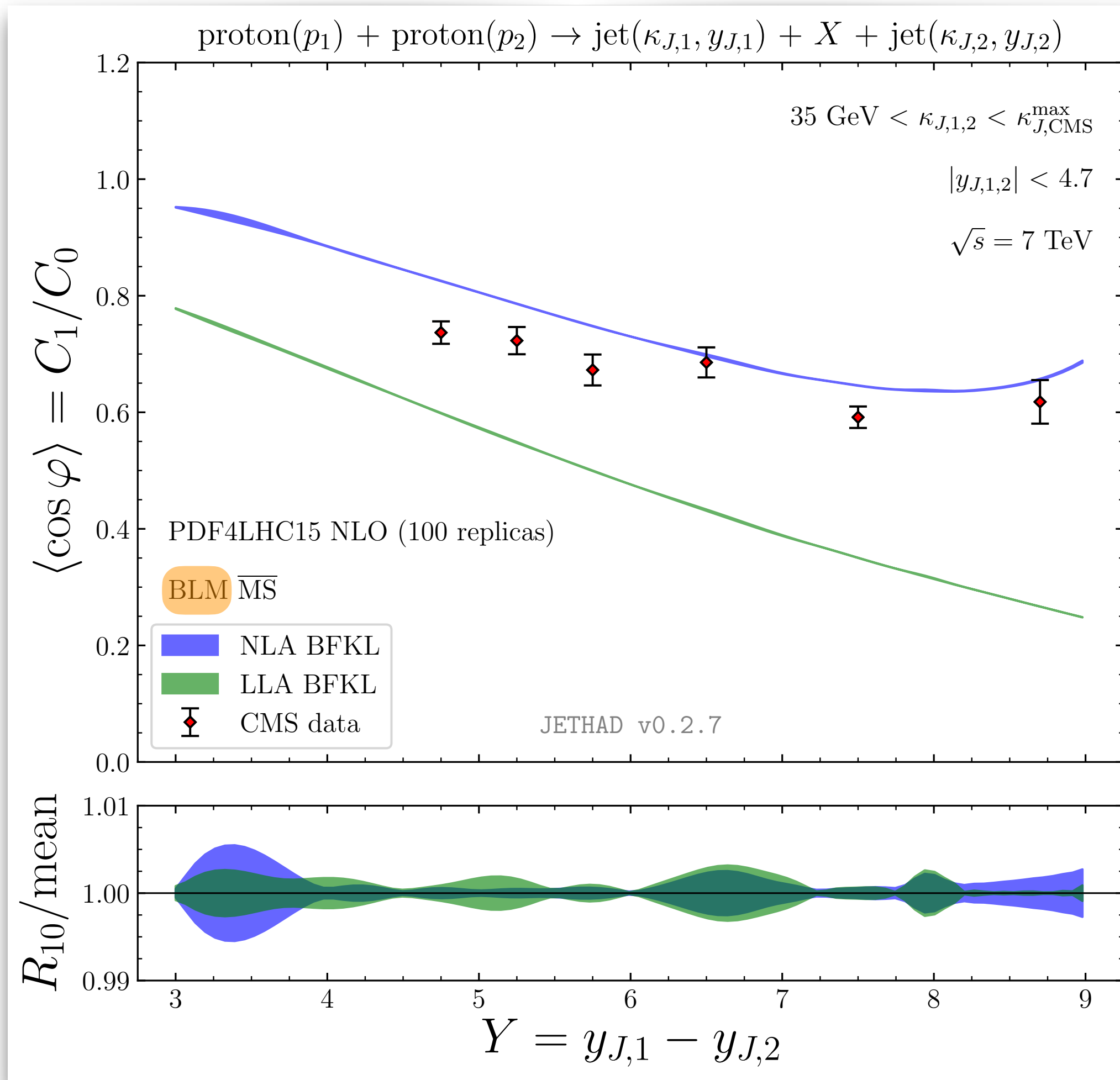
Backup

$$\varphi = \varphi_1 - \varphi_2 - \pi$$

## Mueller-Navelet jets

[B. Ducloué, L. Szymanowski, S. Wallon (2014)]

(figure below) [F. G. C. (2021)]



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# Azimuthal correlations: $C_1/C_0 \equiv \langle \cos \varphi \rangle$

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$$\varphi = \varphi_1 - \varphi_2 - \pi$$

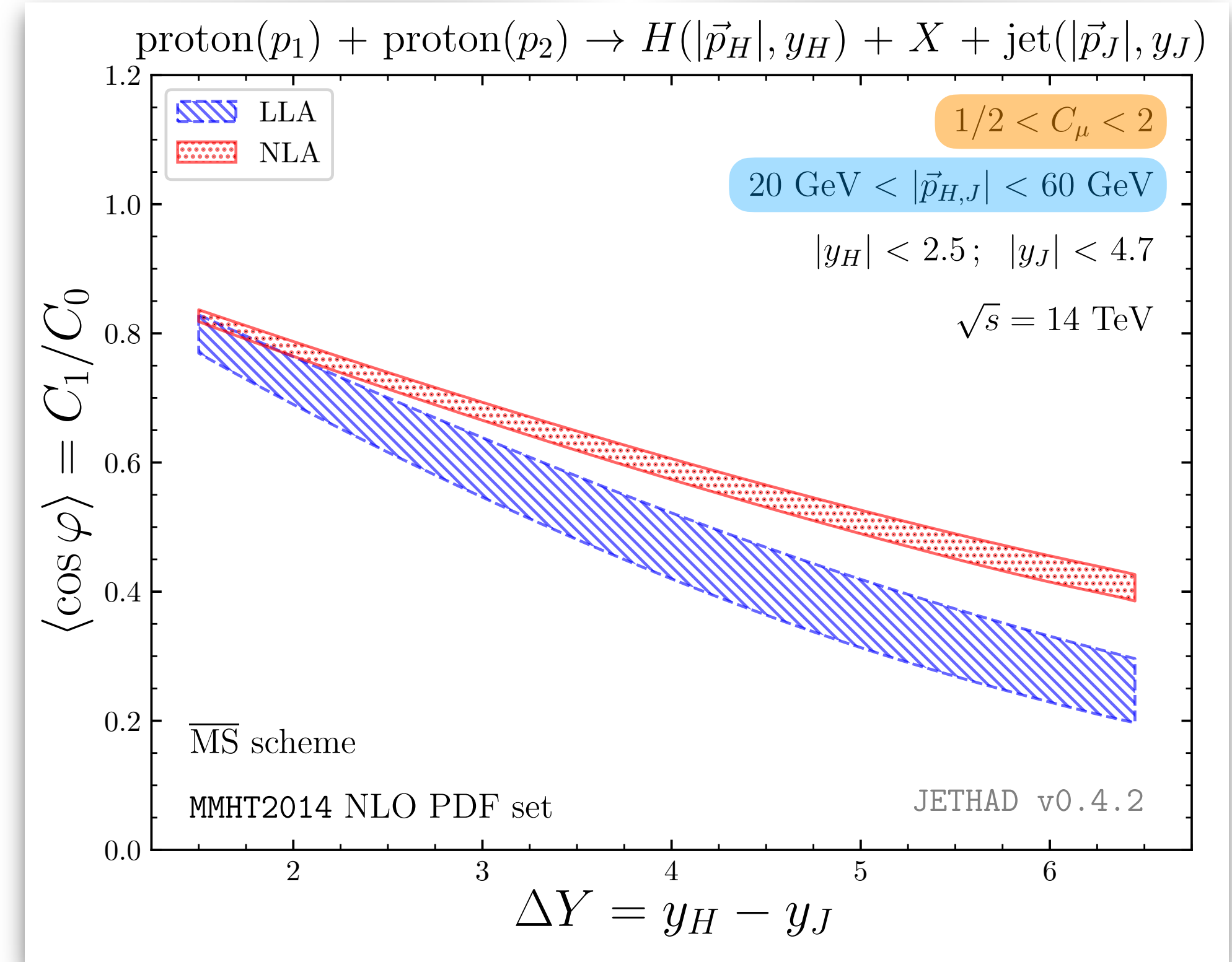
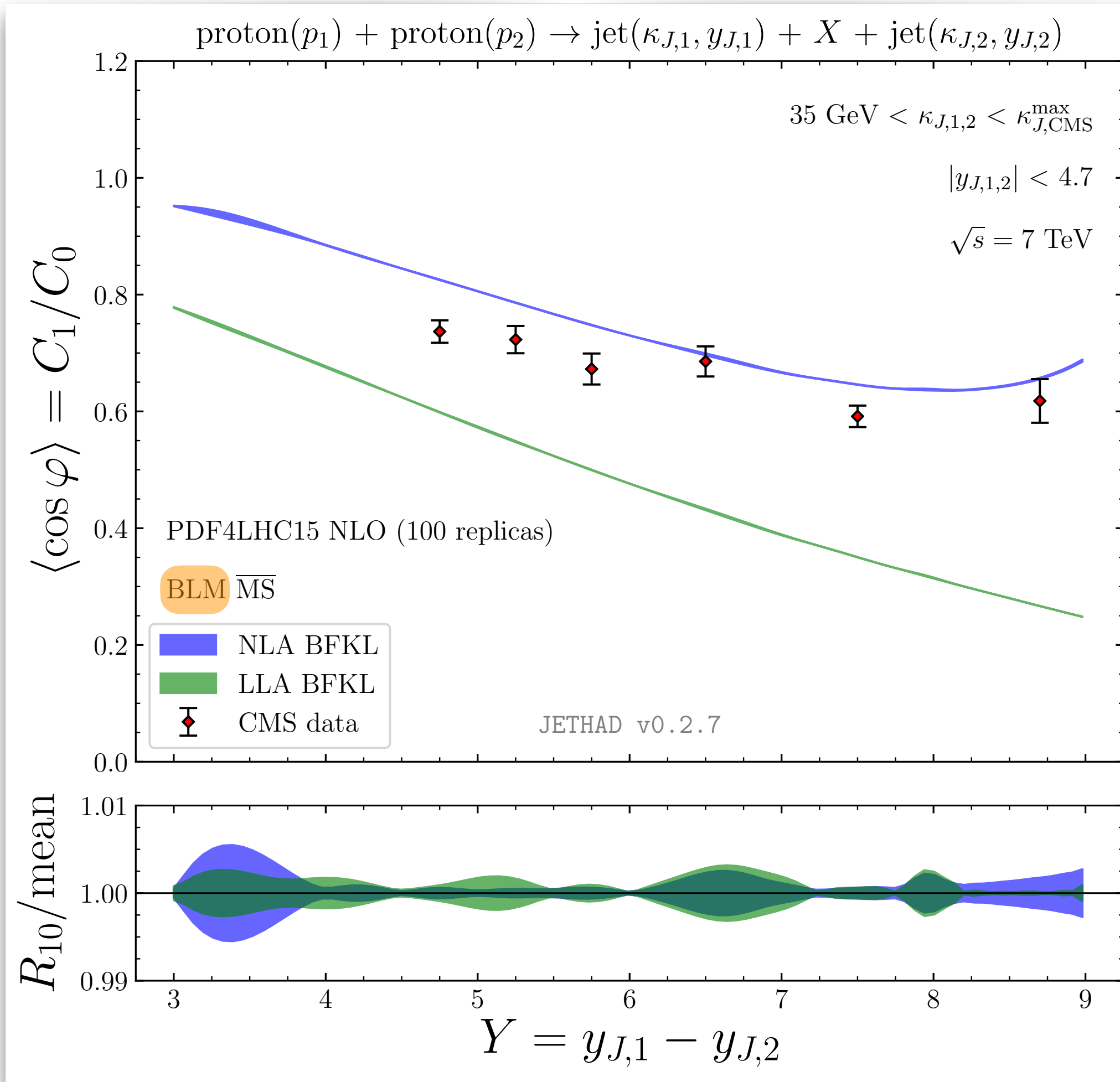
## Mueller-Navelet jets

[B. Ducloué, L. Szymanowski, S. Wallon (2014)]

(figure below) [F. G. C. (2021)]

## Higgs + jet

[F. G. C., D. Yu. Ivanov, M. M. A. Mohammed, A. Papa (2021)]



natural scales  
 symmetric  $p_T$  range

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# $\varphi$ -averaged cross section: $C_0$

$$C_n(\Delta Y, s) = \int_{p_H^{\min}}^{p_H^{\max}} d|\vec{p}_H| \int_{p_J^{\min}}^{p_J^{\max}} d|\vec{p}_J| \int_{y_H^{\min}}^{y_H^{\max}} dy_H \int_{y_J^{\min}}^{y_J^{\max}} dy_J \delta(y_H - y_J - \Delta Y) C_n$$

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# $\varphi$ -averaged cross section: $C_0$

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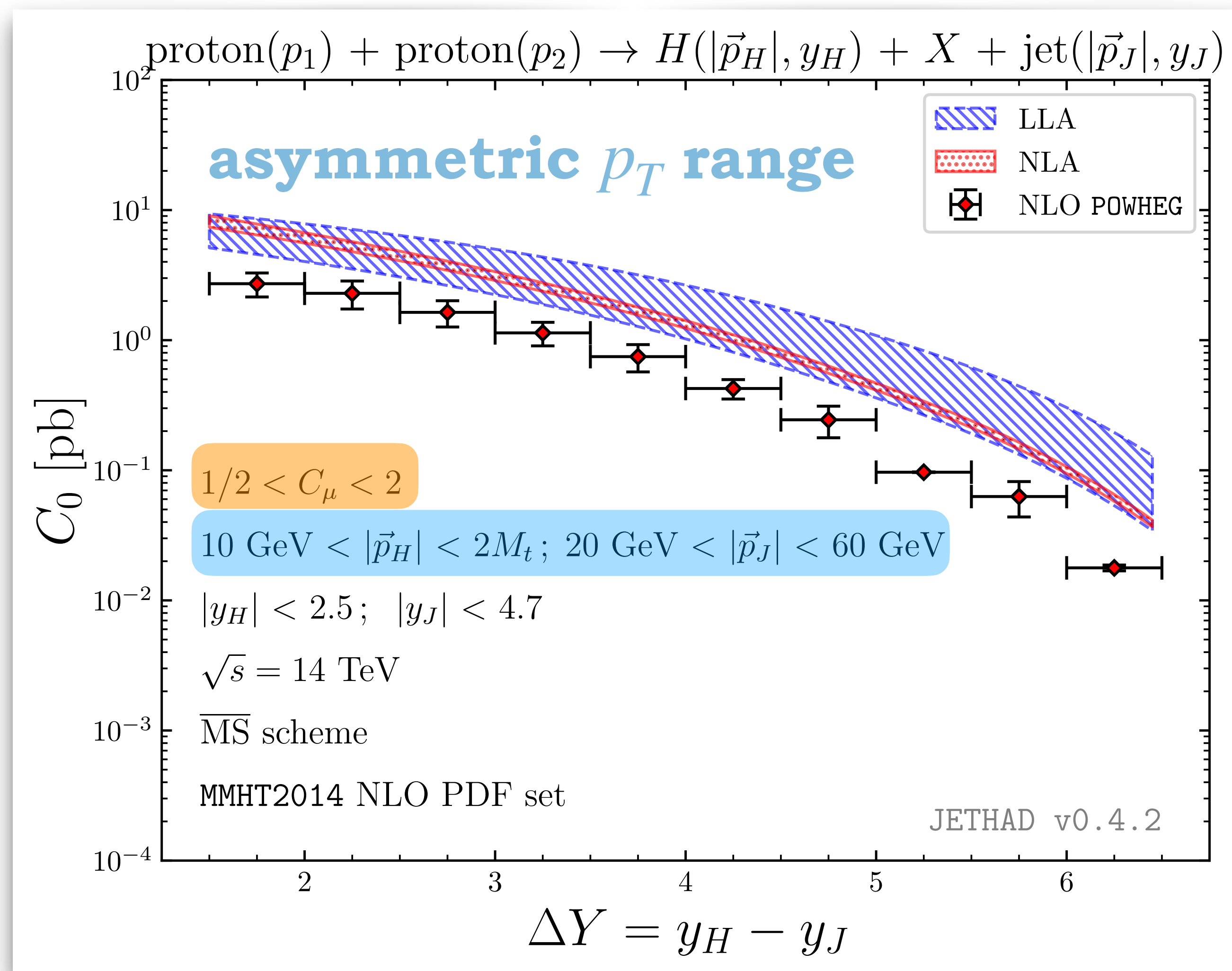
# $\varphi$ -averaged cross section: $C_0$

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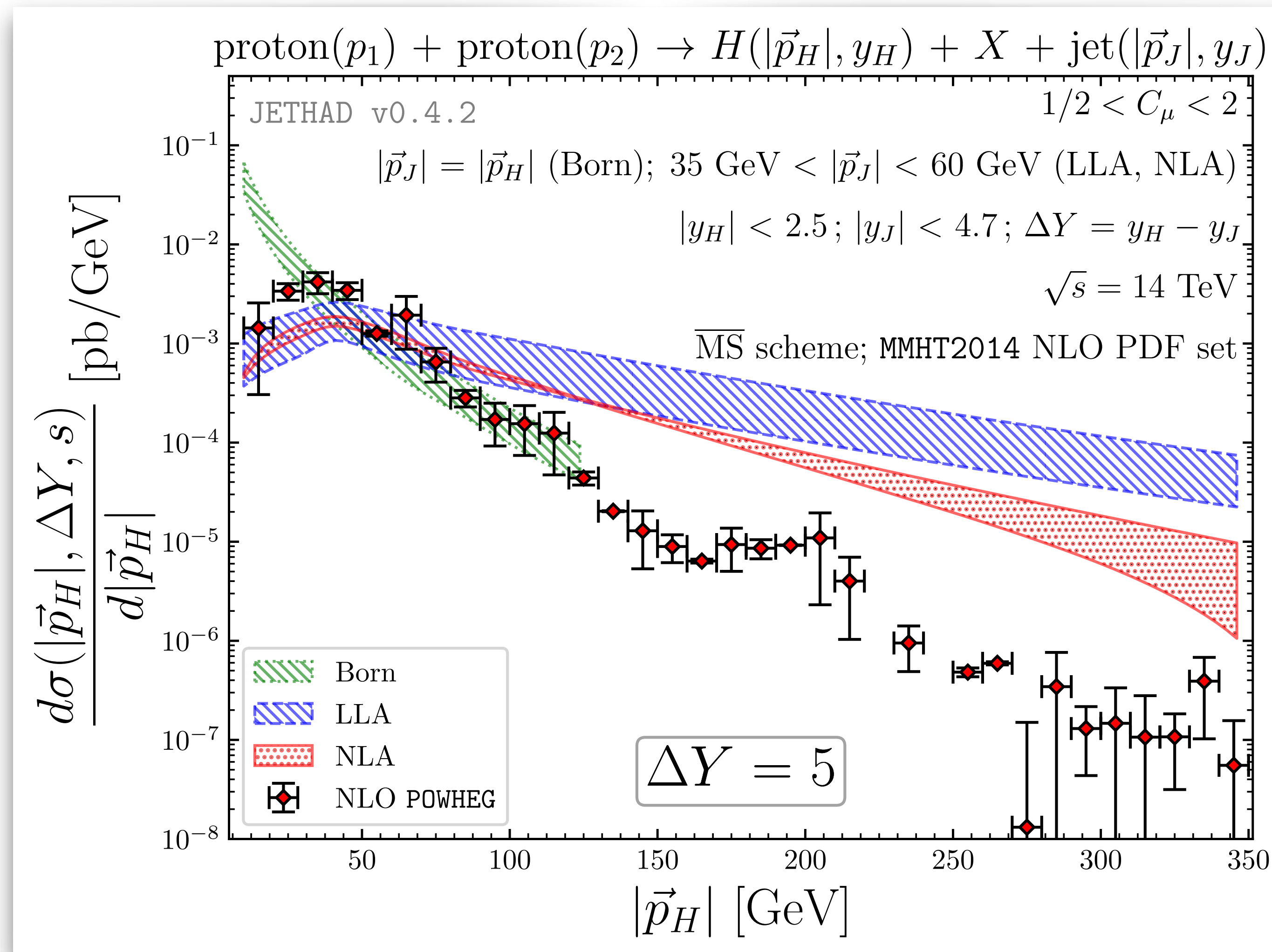
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# $p_H$ -distribution: $dC_0/dp_H$

$$\frac{d\sigma(|\vec{p}_H|, \Delta Y, s)}{d|\vec{p}_H|d\Delta Y} = \int_{p_J^{\min}}^{p_J^{\max}} d|\vec{p}_J| \int_{y_H^{\min}}^{y_H^{\max}} dy_H \int_{y_J^{\min}}^{y_J^{\max}} dy_J \delta(y_H - y_J - \Delta Y) C_0$$





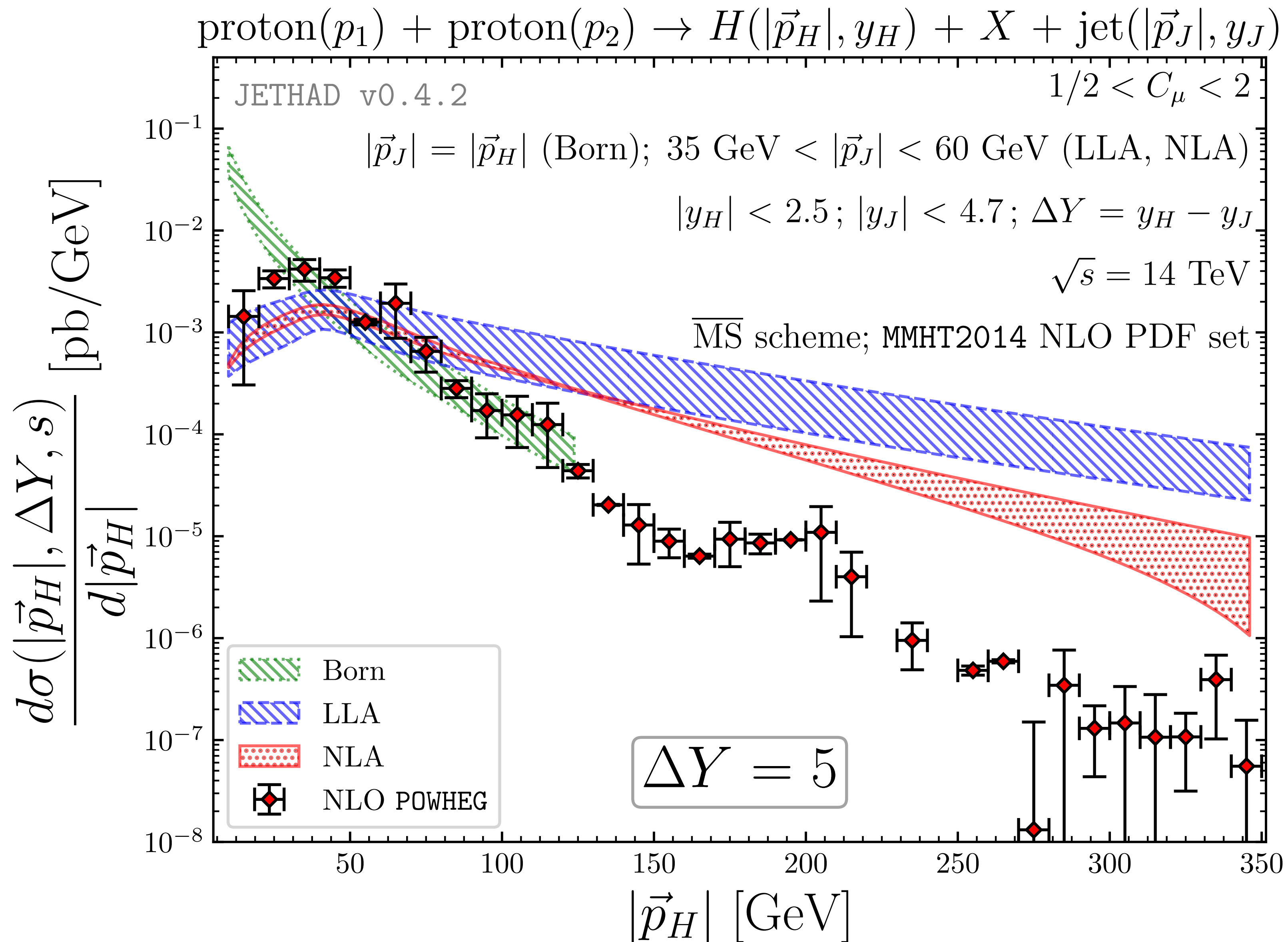
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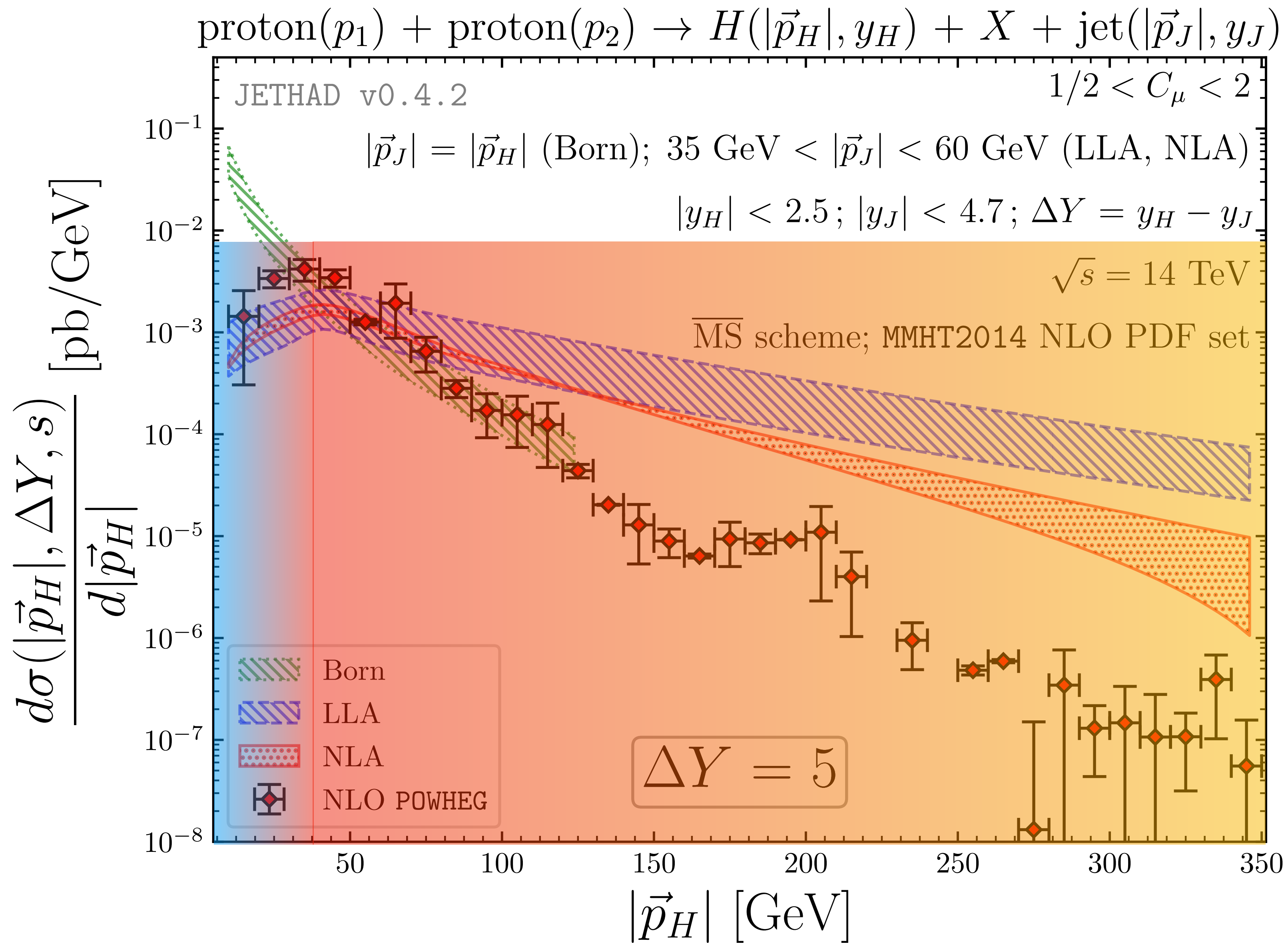
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large  $p_T$  logs  
 $p_T$ -resum. needed

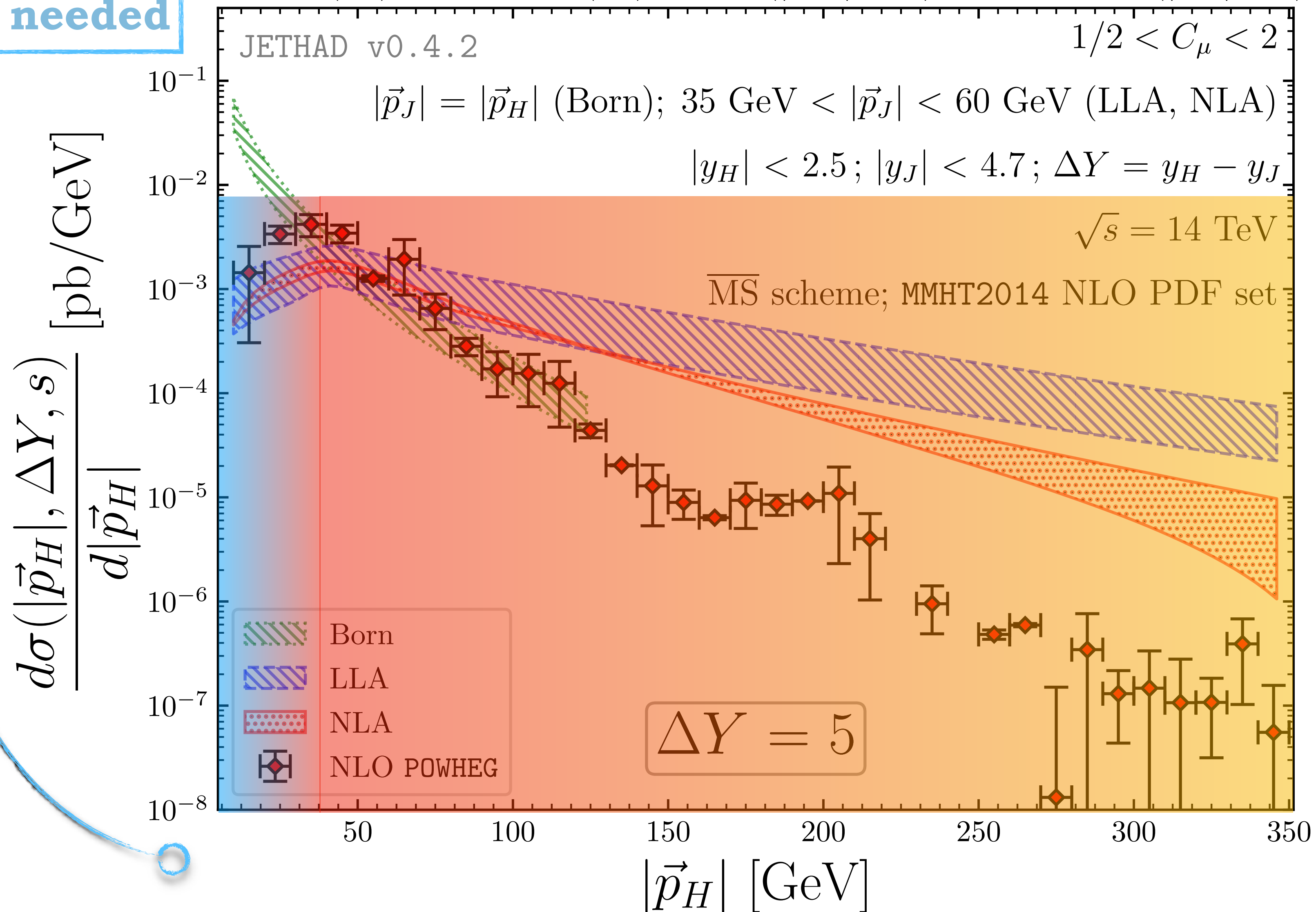
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$$\text{proton}(p_1) + \text{proton}(p_2) \rightarrow H(|\vec{p}_H|, y_H) + X + \text{jet}(|\vec{p}_J|, y_J)$$





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large  $p_T$  logs  
 $p_T$ -resum. needed

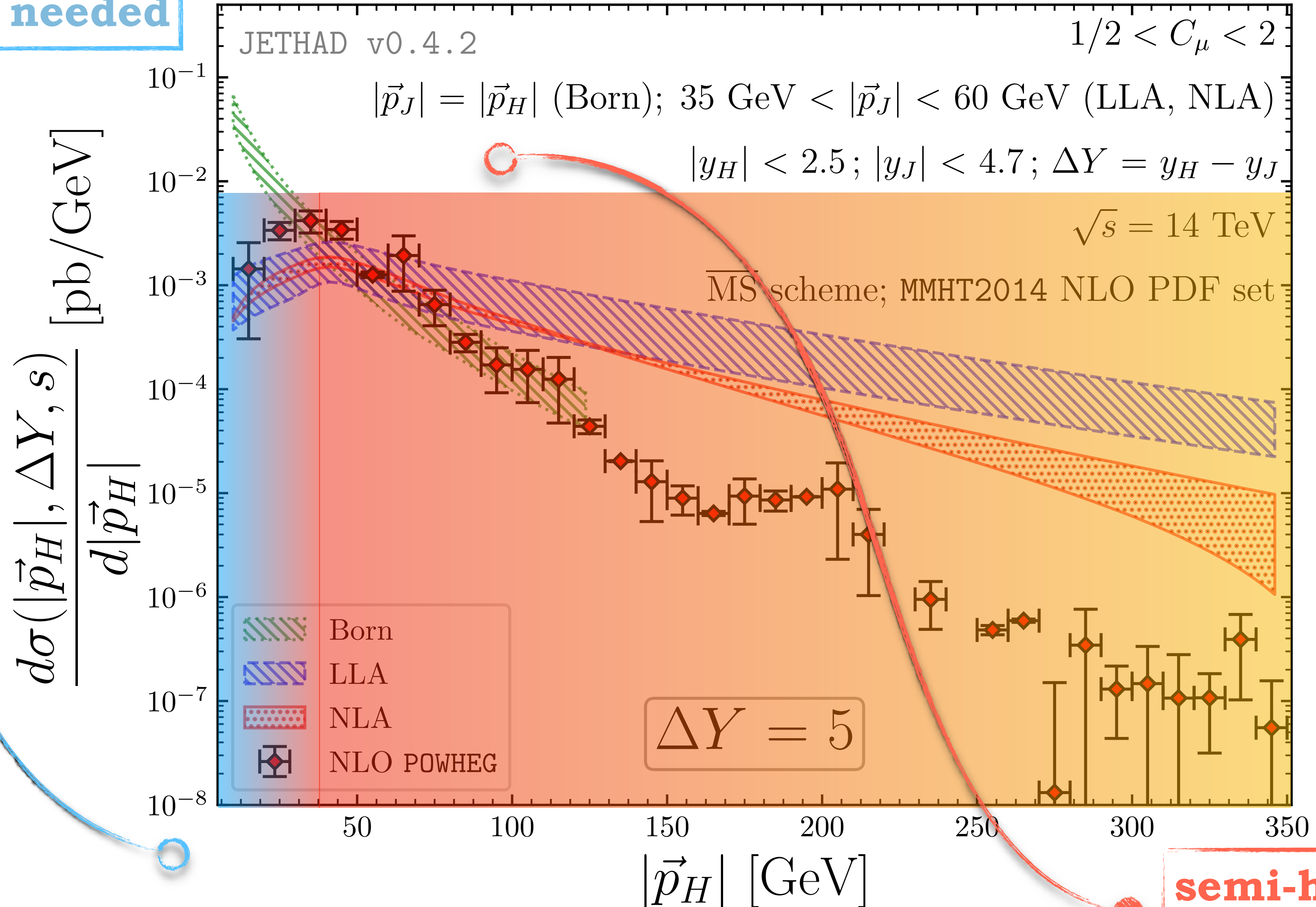
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$$\text{proton}(p_1) + \text{proton}(p_2) \rightarrow H(|\vec{p}_H|, y_H) + X + \text{jet}(|\vec{p}_J|, y_J)$$



semi-hard regime  
BFKL expected

Introduction & Motivation

Natural Stability

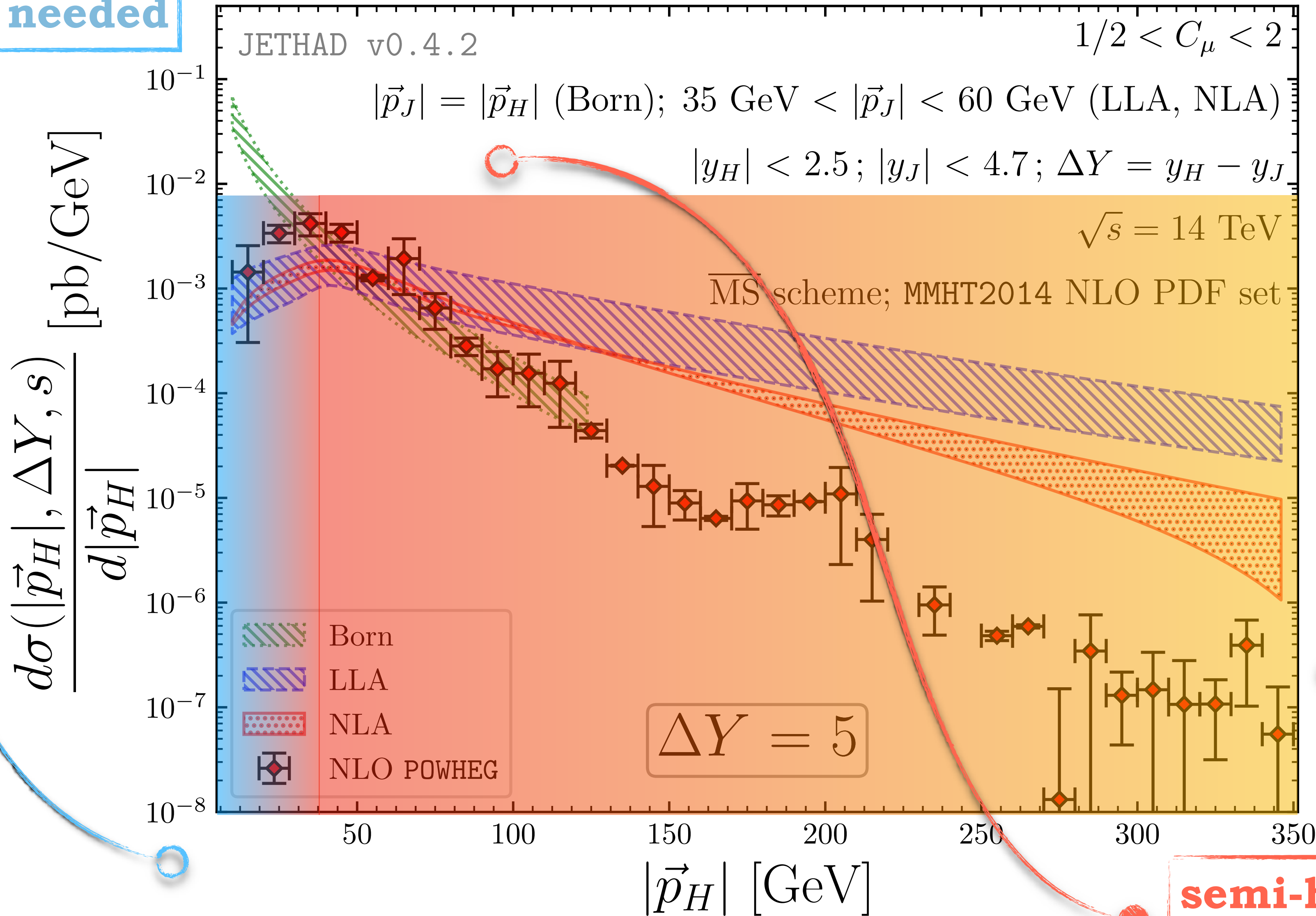
FPF+ATLAS Coincidence

Towards Precision Studies

large  $p_T$  logs  
 $p_T$ -resum. needed

DGLAP-type + threshold logs  $\rightarrow$  BFKL decoupling

$$\text{proton}(p_1) + \text{proton}(p_2) \rightarrow H(|\vec{p}_H|, y_H) + X + \text{jet}(|\vec{p}_J|, y_J)$$



semi-hard regime  
BFKL expected

Backup

[F. G. C., D. Yu. Ivanov, M. M. A. Mohammed, A. Papa (2021)]

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# $p_H$ -distribution: $dC_0/dp_H (M_t \rightarrow +\infty)$

$$\frac{d\sigma(|\vec{p}_H|, \Delta Y, s)}{d|\vec{p}_H|d\Delta Y} = \int_{p_J^{\min}}^{p_J^{\max}} d|\vec{p}_J| \int_{y_H^{\min}}^{y_H^{\max}} dy_H \int_{y_J^{\min}}^{y_J^{\max}} dy_J \delta(y_H - y_J - \Delta Y) C_0$$

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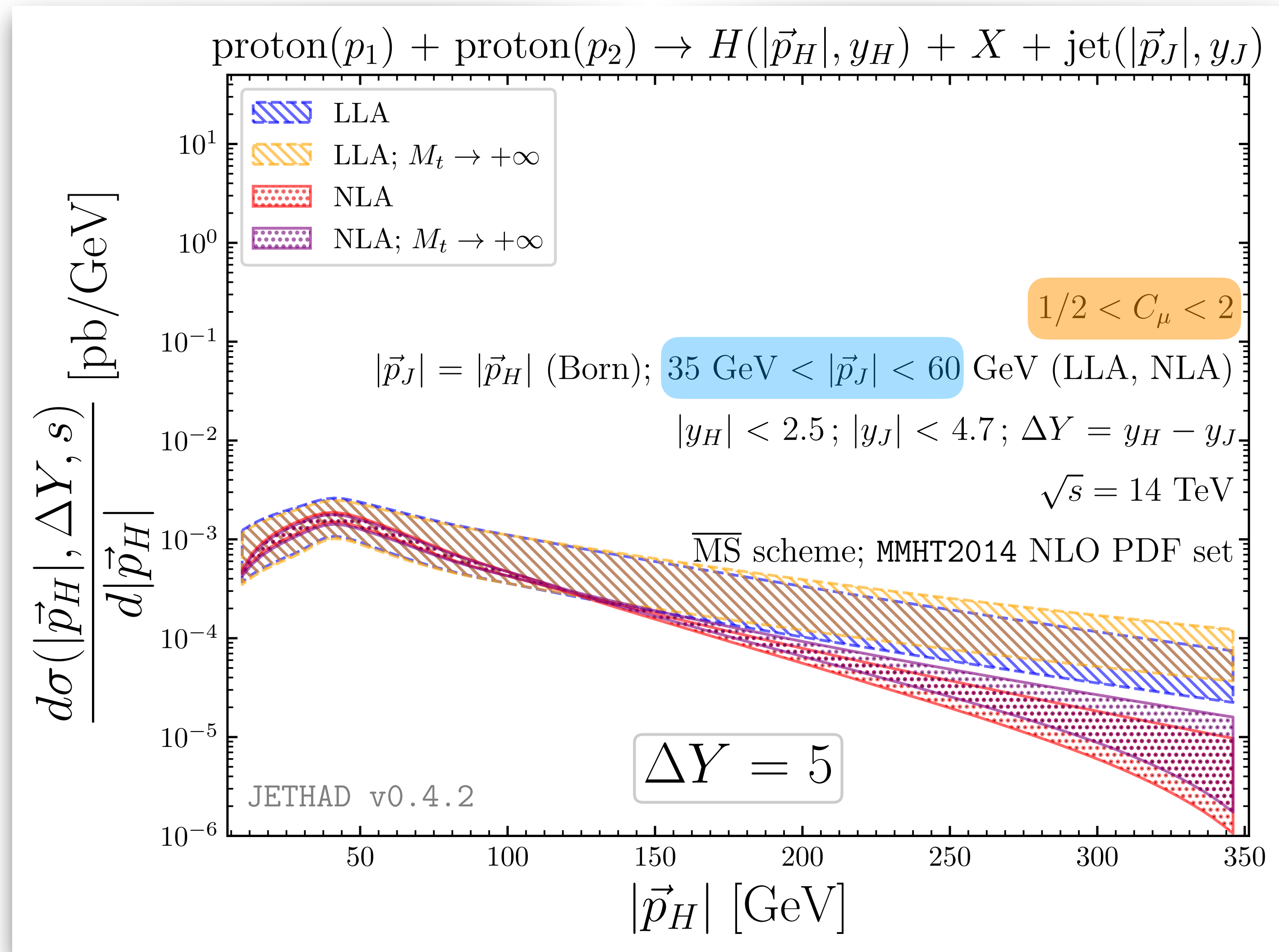
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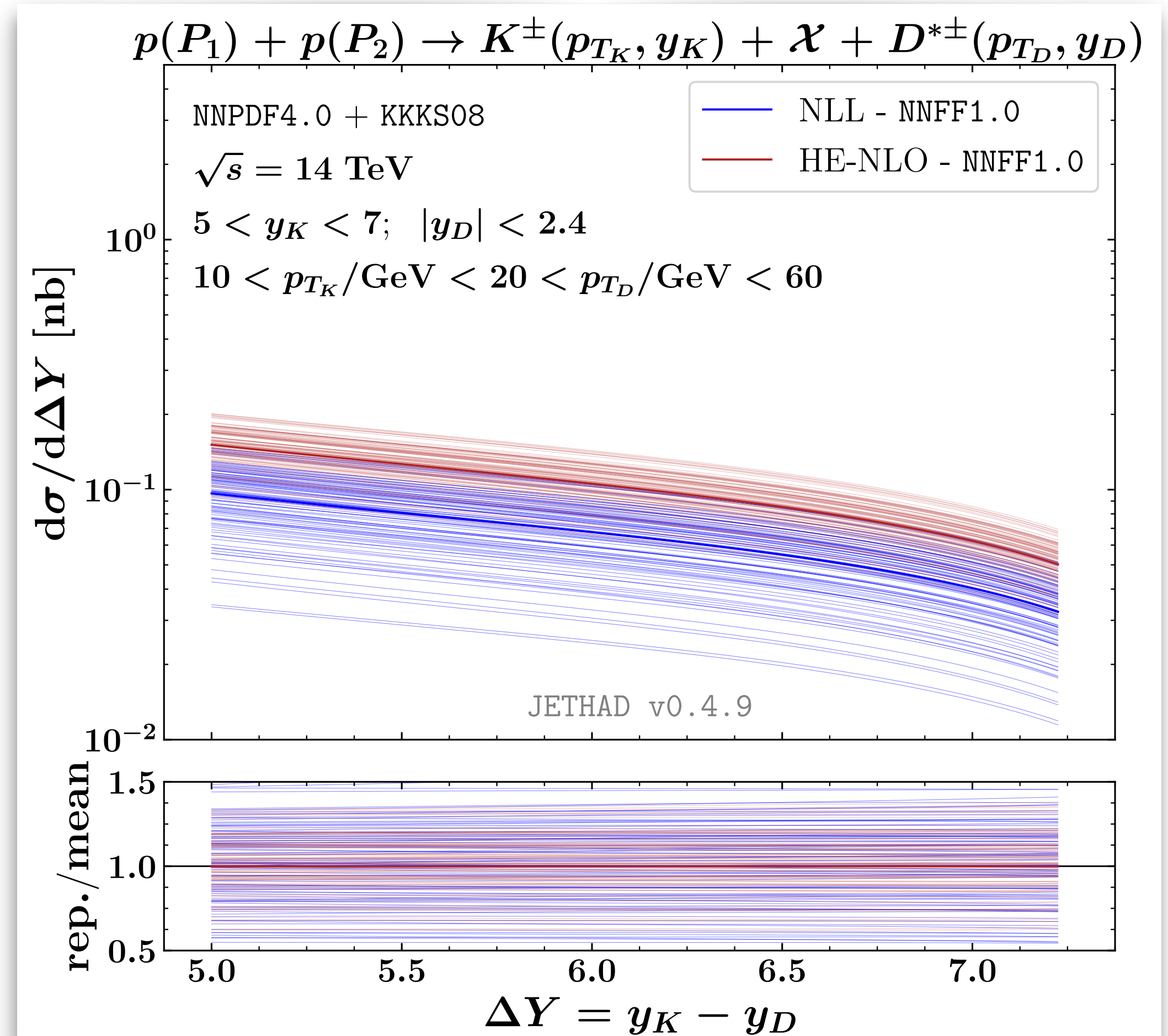
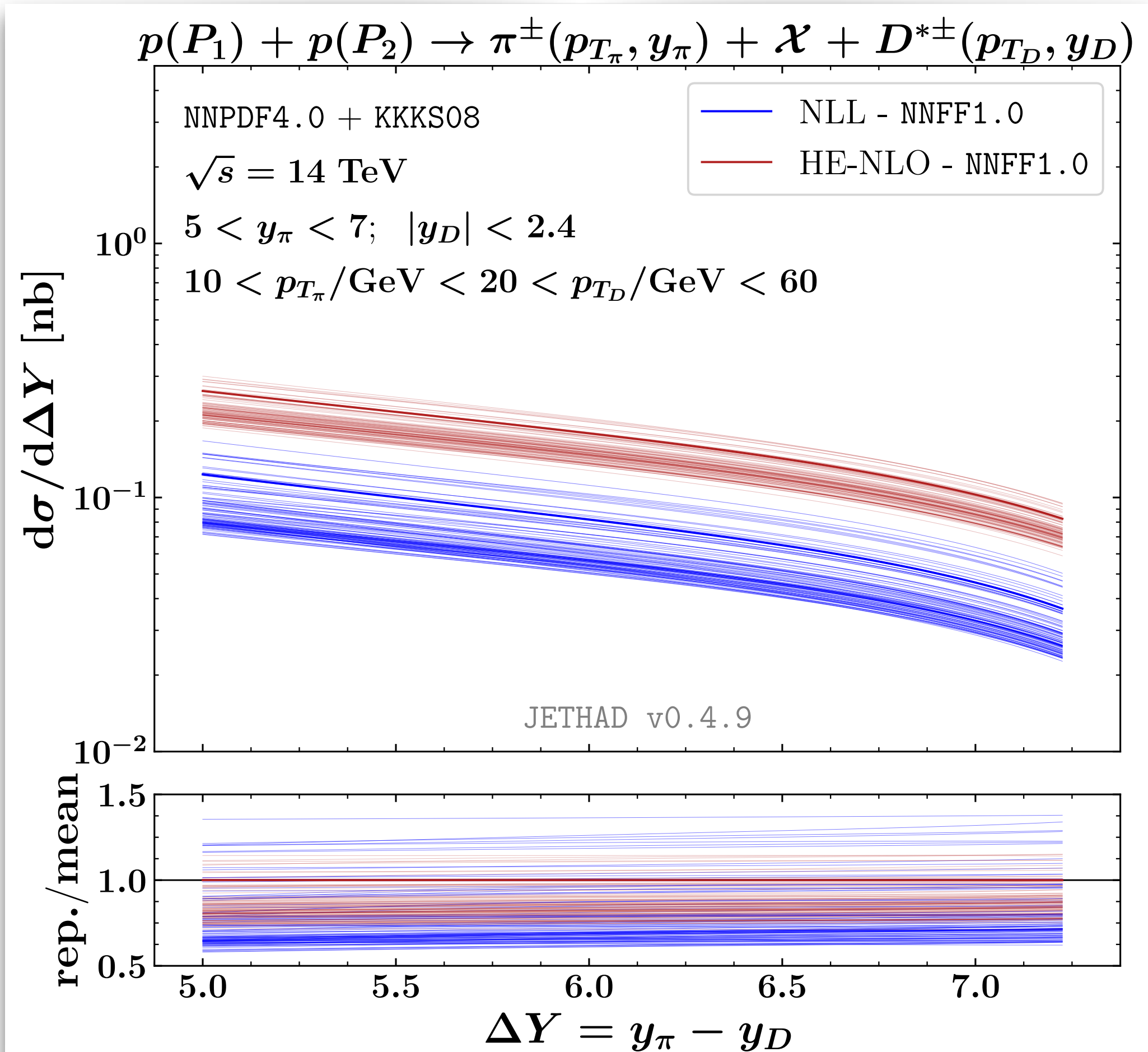
# Rapidity distribution @FPF+ATLAS

Inclusive  $\pi^\pm$  (FPF) +  $D^{*\pm}$  (ATLAS) production

[FPF Snowmass Whitepaper]

Inclusive  $K^\pm$  (FPF) +  $D^{*\pm}$  (ATLAS) production

[FPF Snowmass Whitepaper]



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# Azimuthal distribution @FPF+ATLAS

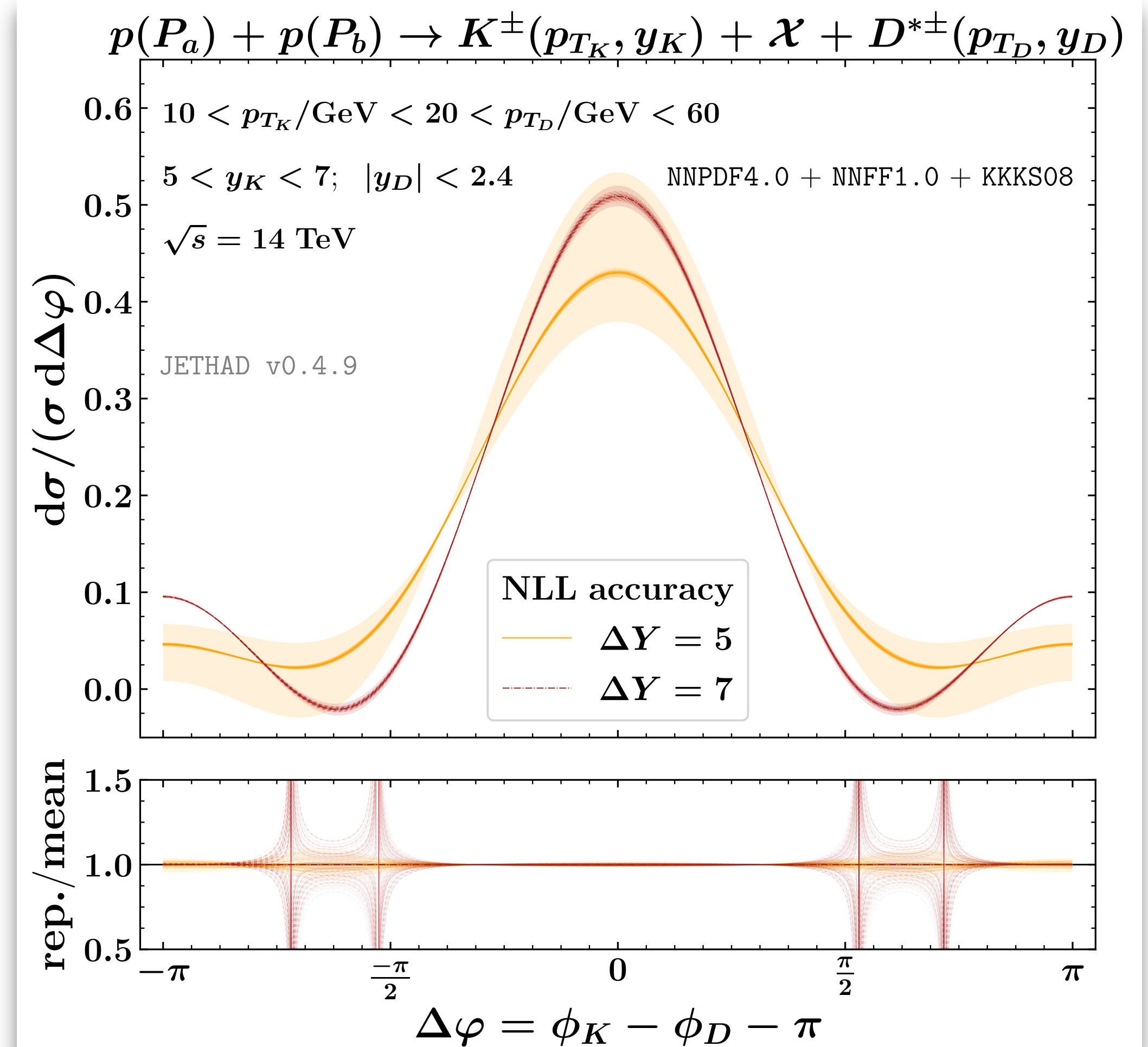
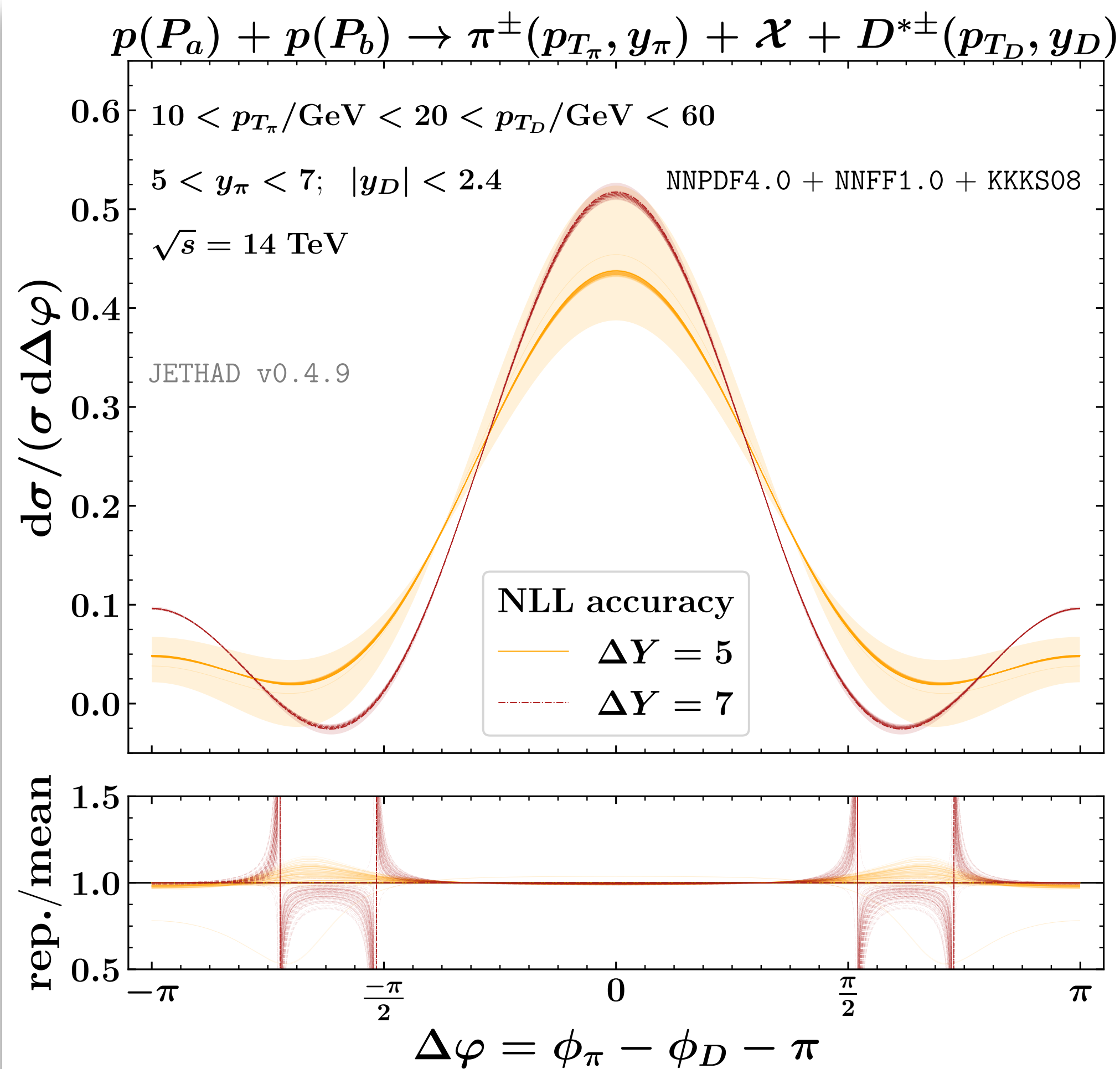
Backup

Inclusive  $\pi^\pm$  (FPF) +  $D^{*\pm}$  (ATLAS) production

[FPF Snowmass Whitepaper]

Inclusive  $K^\pm$  (FPF) +  $D^{*\pm}$  (ATLAS) production

[FPF Snowmass Whitepaper]



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