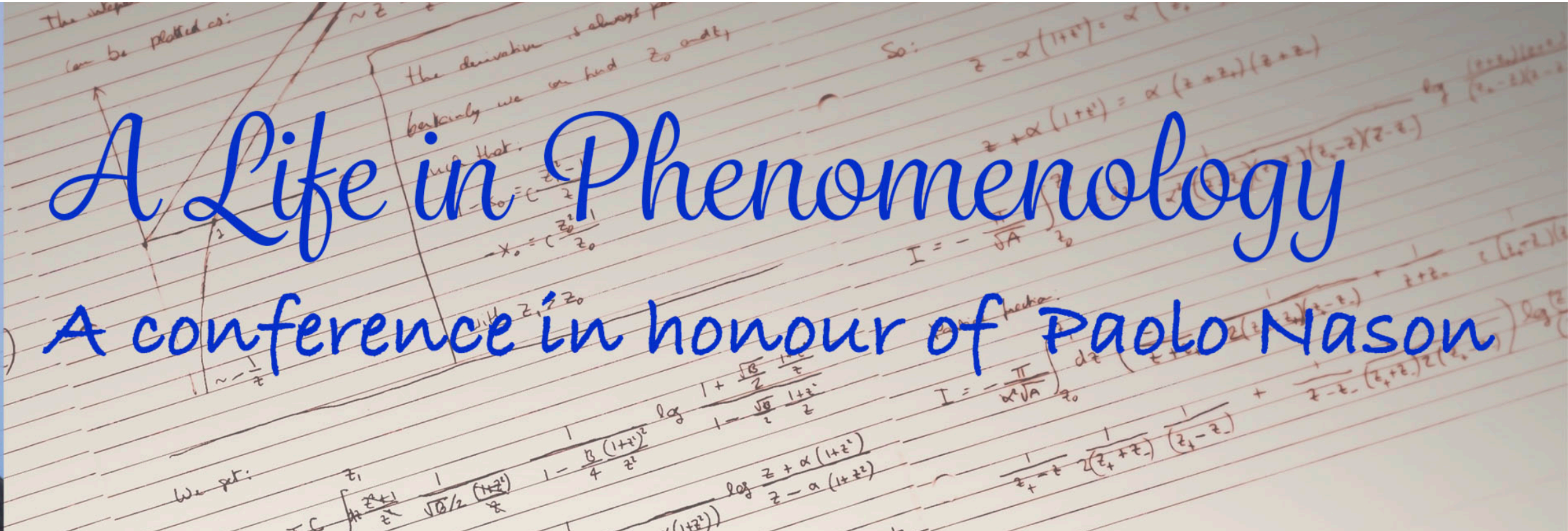
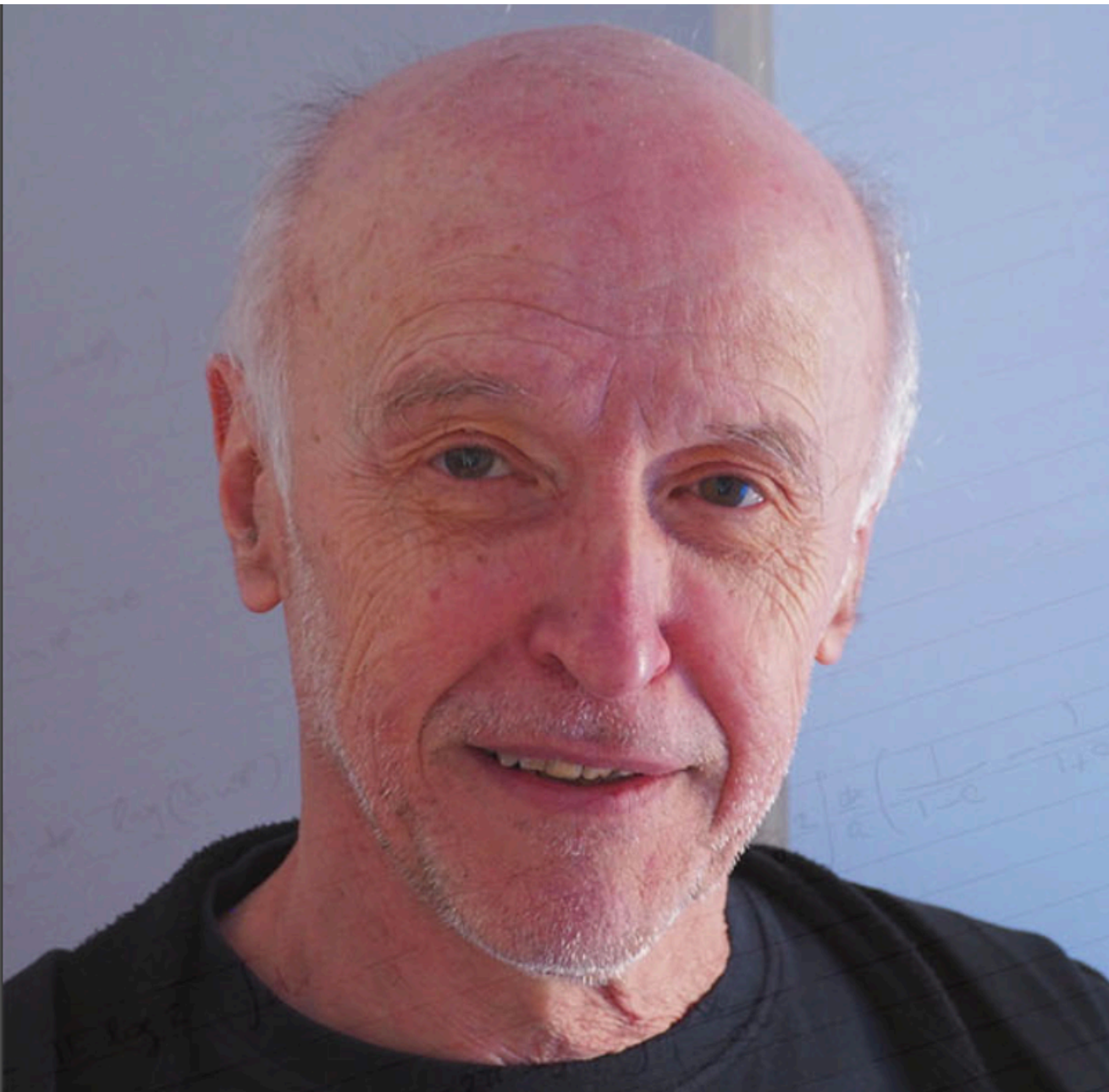


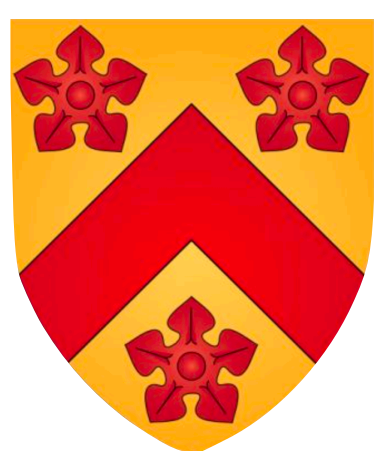
# LIGHT (AND LEPTONS) IN THE PROTON



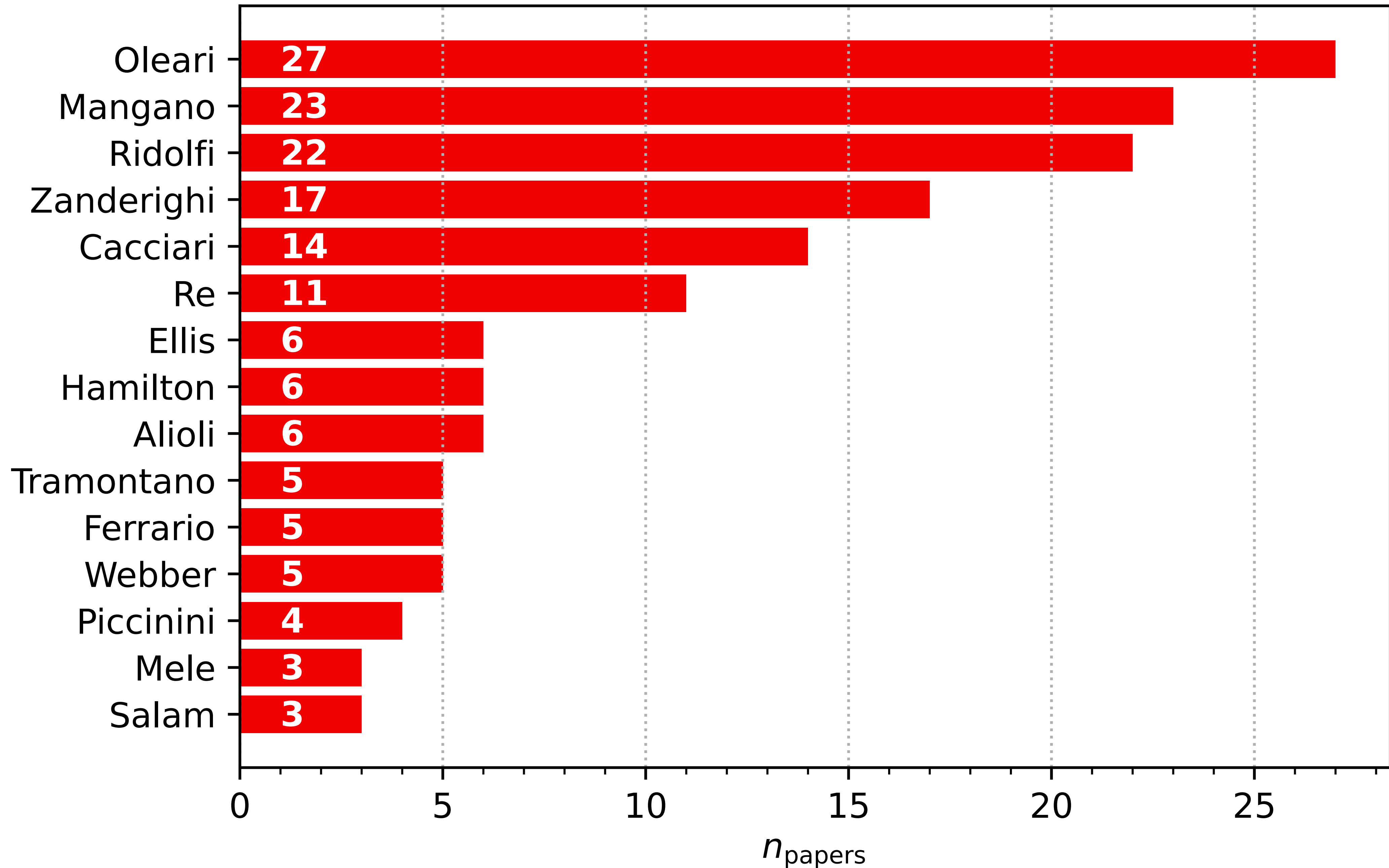
Milano Bicocca, September 2022

Gavin Salam

Rudolf Peierls Centre for Theoretical Physics & All Souls College, University of Oxford



# Paolo's papers with speakers & organisers



# Three papers in common with Paolo

## Multiplicative-accumulative matching of NLO calculations with parton showers

#1

Paolo Nason (INFN, Milan Bicocca and Milan Bicocca U.), Gavin P. Salam (Oxford U., Theor. Phys. and Oxford U.) (Nov 5, 2021)

Published in: *JHEP* 01 (2022) 067 • e-Print: [2111.03553](#) [hep-ph]

 pdf  DOI  cite

 2 citations


## The Photon Content of the Proton

#2

Aneesh V. Manohar (UC, San Diego), Paolo Nason (INFN, Milan Bicocca and Milan Bicocca U.), Gavin P. Salam (CERN), Giulia Zanderighi (CERN and Oxford U., Theor. Phys.) (Aug 3, 2017)

Published in: *JHEP* 12 (2017) 046 • e-Print: [1708.01256](#) [hep-ph]

 pdf  DOI  cite

 180 citations

## How bright is the proton? A precise determination of the photon parton distribution function

#3

Aneesh Manohar (CERN and UC, San Diego), Paolo Nason (INFN, Milan Bicocca), Gavin P. Salam (CERN), Giulia Zanderighi (CERN and Oxford U., Theor. Phys.) (Jul 14, 2016)

Published in: *Phys.Rev.Lett.* 117 (2016) 24, 242002 • e-Print: [1607.04266](#) [hep-ph]

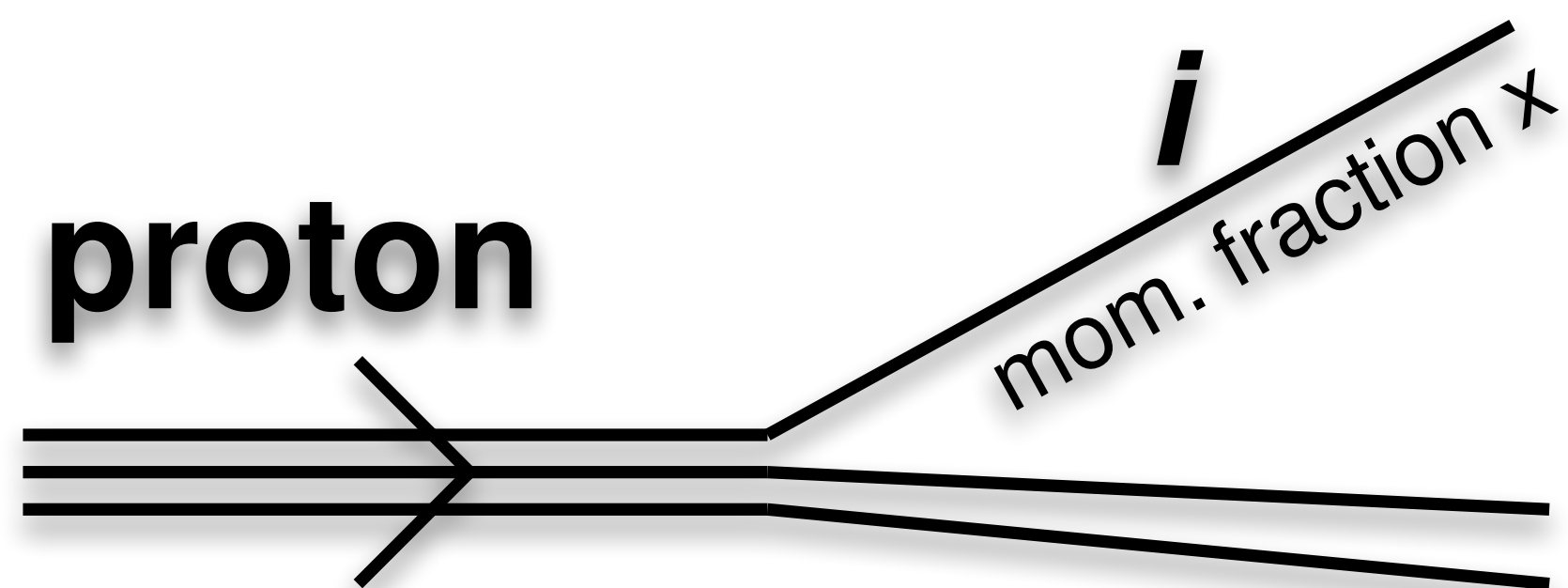
 pdf  DOI  cite

 272 citations

# Paolo's papers with $\geq 250$ citations

	ncit	/yr	jrn	nAu	title
1.	0709.2092	4059	271	jhp	3 Matching NLO QCD computations with Parton Shower simulations: the POWHEG method
2.	1002.2581	3776	300	jhp	4 A general framework for implementing NLO calculations in shower Monte Carlo programs: the POWHEG BOX
3.	0409146hp	3448	192	jhp	1 A New method for combining NLO QCD with shower Monte Carlo algorithms
4.	87-12	1644	47	npb	3 The Total Cross-Section for the Production of Heavy Quarks in Hadronic Collisions
5.	89-04	1204	36	npb	3 The One Particle Inclusive Differential Cross-Section for Heavy Quark Production in Hadronic Collisions
6.	0707.3088	1149	76	jhp	3 A Positive-weight next-to-leading-order Monte Carlo for heavy flavour hadroproduction
7.	0305252hp	1127	58	jhp	3 Matching NLO QCD and parton showers in heavy flavor production
8.	91-09-24	985	32	npb	3 Heavy quark correlations in hadron collisions at next-to-leading order
9.	9803400hp	936	38	jhp	3 The P(T) spectrum in heavy flavor hadroproduction
10.	1111.5869	886	82	plb	5 Top-pair production at hadron colliders with next-to-next-to-leading logarithmic soft-gluon resummation
11.	0907.4076	860	65	jhp	4 NLO single-top production matched with shower in POWHEG: s- and t-channel contributions
12.	0306211hp	806	42	jhp	4 Soft gluon resummation for Higgs boson production at hadron colliders
13.	9801375hp	686	28	npb	4 NLL resummation of the heavy quark hadroproduction cross-section
14.	1205.6344	610	59	jhp	6 Theoretical predictions for charm and bottom production at the LHC
15.	0911.5299	601	47	jhp	2 NLO Higgs boson production via vector-boson fusion matched with shower in POWHEG
16.	0303085hp	590	30	jhp	5 The t anti-t cross-section at 1.8-TeV and 1.96-TeV: A Study of the systematics due to parton densities and scale dependence
17.	0805.4802	589	41	jhp	4 NLO vector-boson production matched with shower in POWHEG
18.	0812.0578	581	42	jhp	4 NLO Higgs boson production via gluon fusion matched with shower in POWHEG
19.	0502203hp	509	29	prl	3 QCD predictions for charm and bottom production at RHIC
20.	9604351hp	507	19	npb	4 The Resummation of soft gluons in hadronic collisions
21.	88-02	468	14	npb	4 Total Cross-Sections for Heavy Flavor Production in Hadronic Collisions and QCD
22.	1107.5051	466	42	jhp	4 W+W-, WZ and ZZ production in the POWHEG BOX
23.	0102134hp	458	21	jhp	3 The p(T) spectrum in heavy flavor photoproduction
24.	1206.3572	370	36	jhp	3 MINLO: Multi-Scale Improved NLO
25.	0804.2800	370	26	jhp	5 Updated predictions for the total production cross sections of top and of heavier quark pairs at the Tevatron and at the LHC
26.	1012.3380	327	28	jhp	5 Jet pair production in POWHEG
27.	9702287hp	321	13	p	4 Heavy quark production
28.	1309.0017	321	35	jhp	4 NNLOPS simulation of Higgs boson production
29.	1306.2542	301	33	jhp	4 $\sigma_{HW^{\pm}}/HZ + 0$ and 1 jet at NLO with the POWHEG BOX interfaced to GoSam and their merging within MiNLO
30.	88-06	283	8	npb	2 QCD Radiative Corrections to the Photoproduction of Heavy Quarks
31.	9602208hp	283	11	plb	4 The Top cross-section in hadronic collisions
32.	90-12	277	9	npb	2 The Fragmentation function for heavy quarks in QCD
33.	1607.04266	272	44	prl	4 How bright is the proton? A precise determination of the photon parton distribution function
34.	9510350np	269	9	ptb	4 Improving the weizsacker-williams approximation in electron - proton collisions
35.	0312132hp	265	14	jhp	5 QCD analysis of first $\sigma_b$ cross-section data at 1.96-TeV
36.	1001.2312	262	21	npb	4 Heavy quarks in deep-inelastic scattering

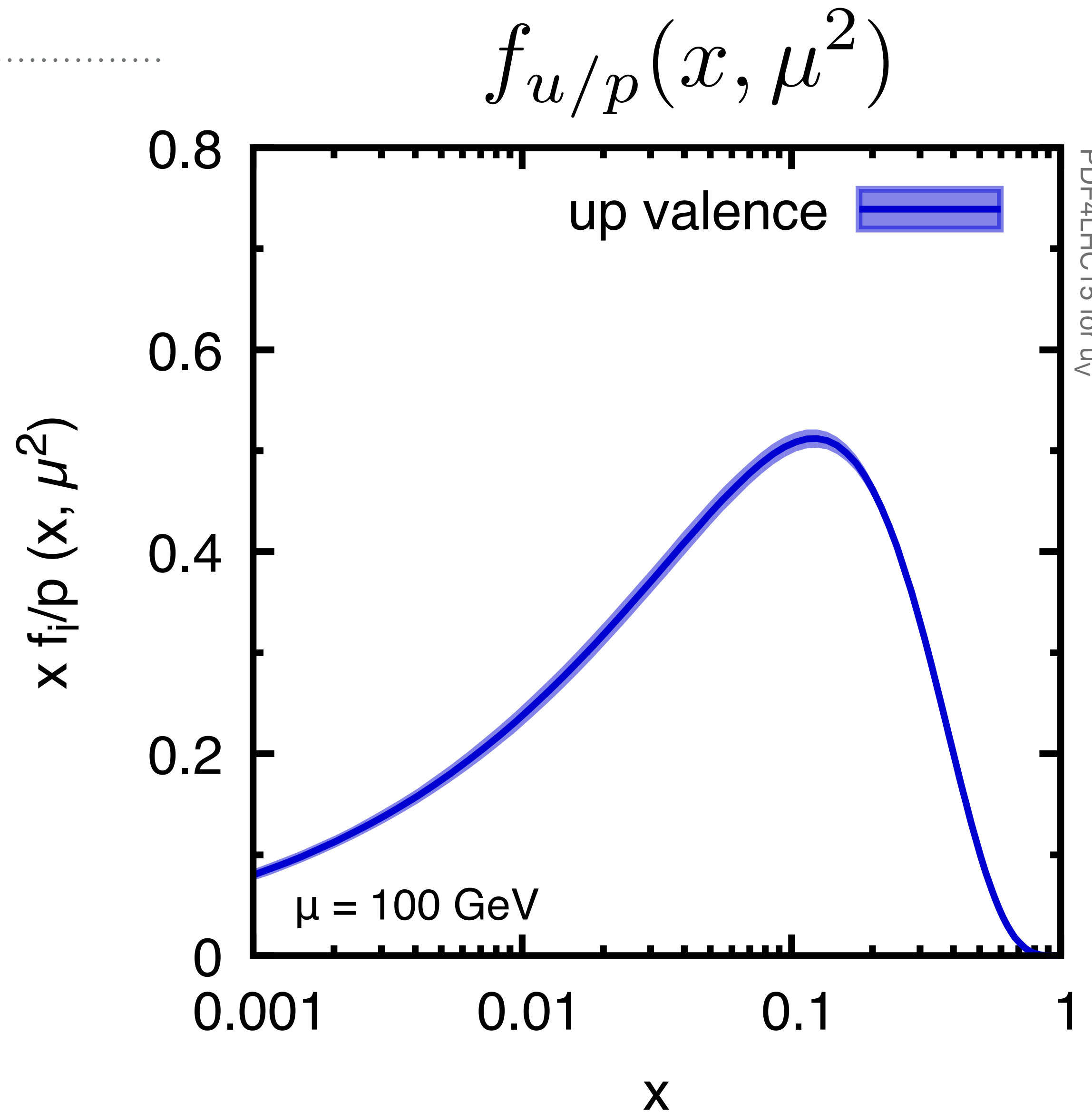
# parton distribution functions (PDFs)



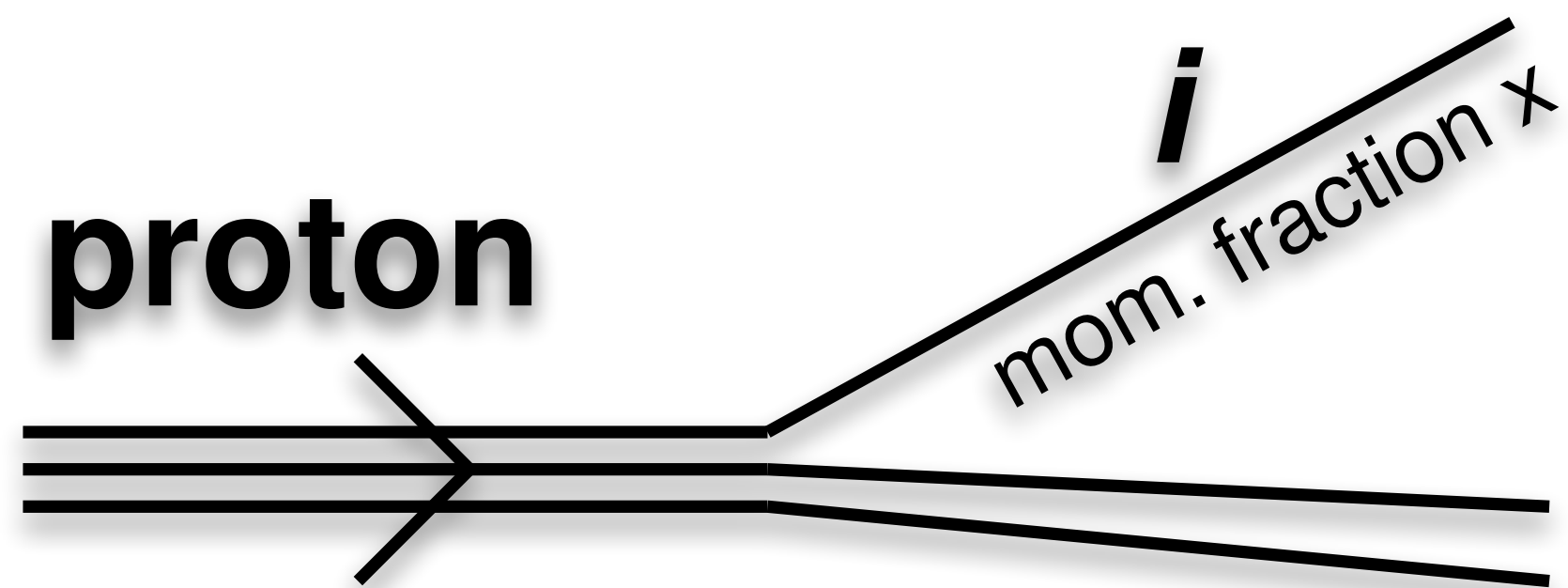
LHC physics  
needs PDFs in region  
 $\sim 10^{-3} - 0.5$

Typically known with good  
**precision  $\sim 1-3\%$**

*E.g. NNPDF, MMHT, CT & PDF4LHC working group (+ also HERAPDF, ABM, ...)*



# parton distribution functions (PDFs)



LHC physics  
needs PDFs in  
 $\sim 10^{-3} -$

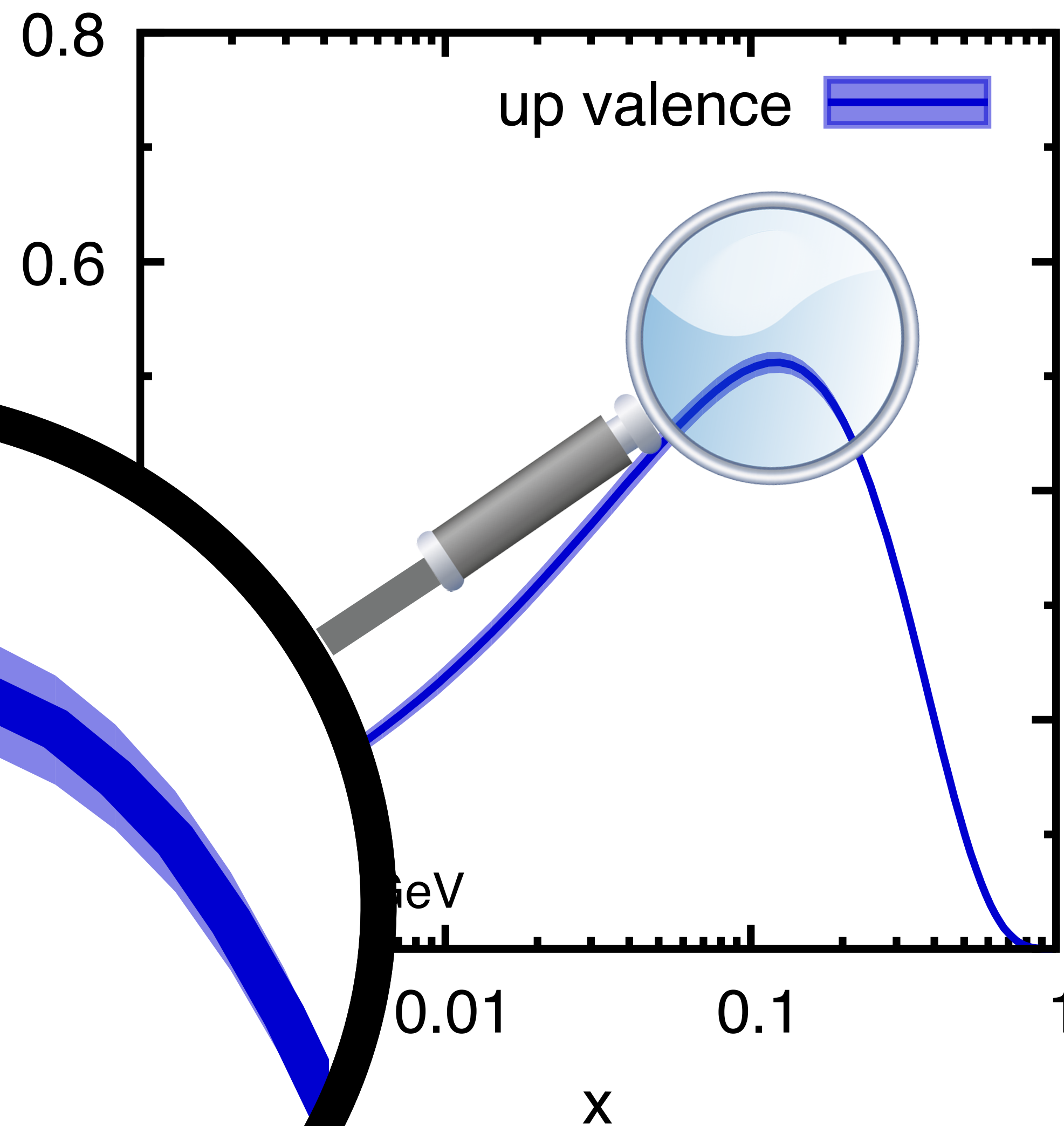
Typically known  
**precision**  $\sim$

$\pm 2\%$

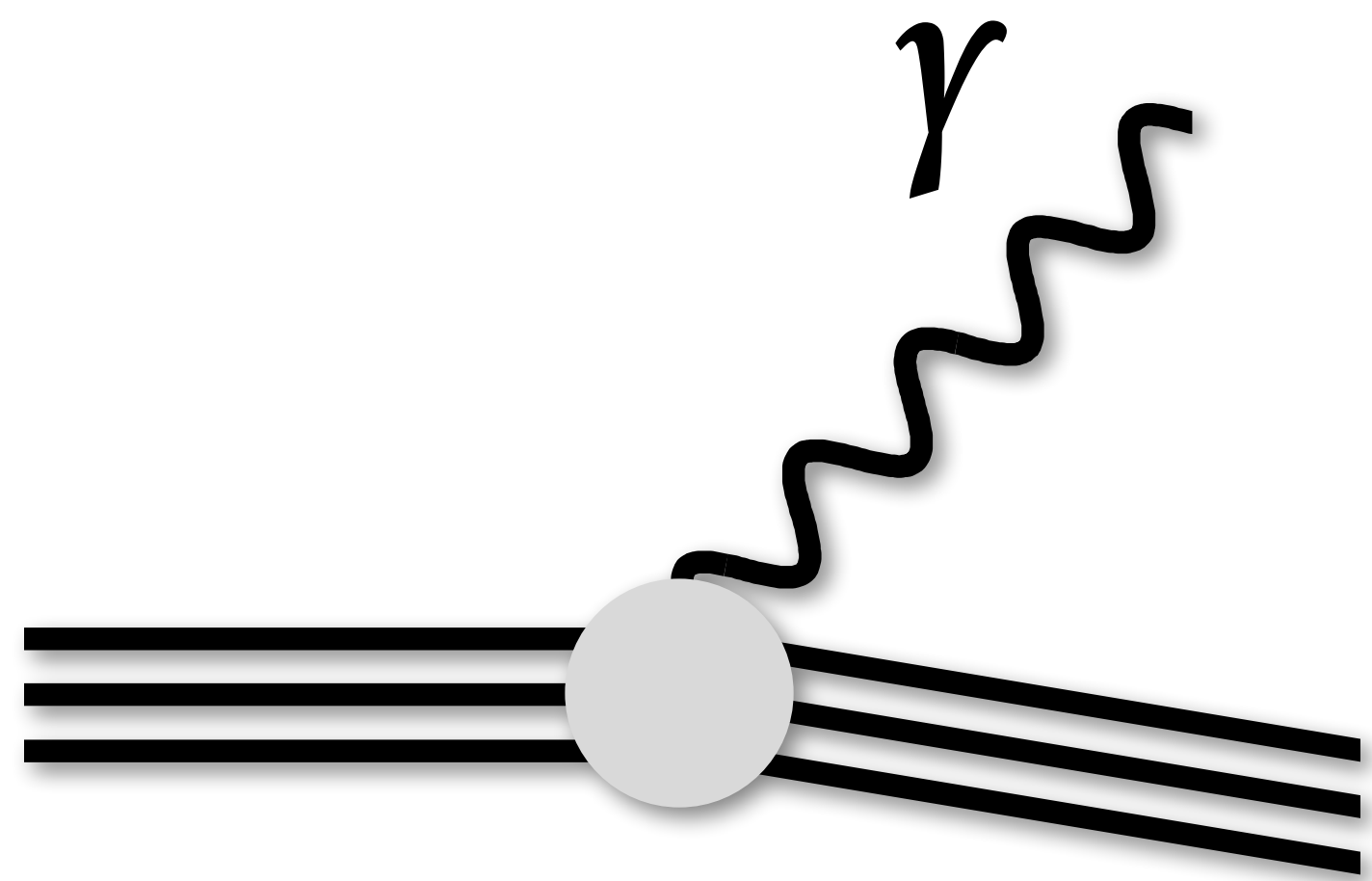
E.g. NNPDF, MMHT, CT & PDF

(PDF, ABM, ...)

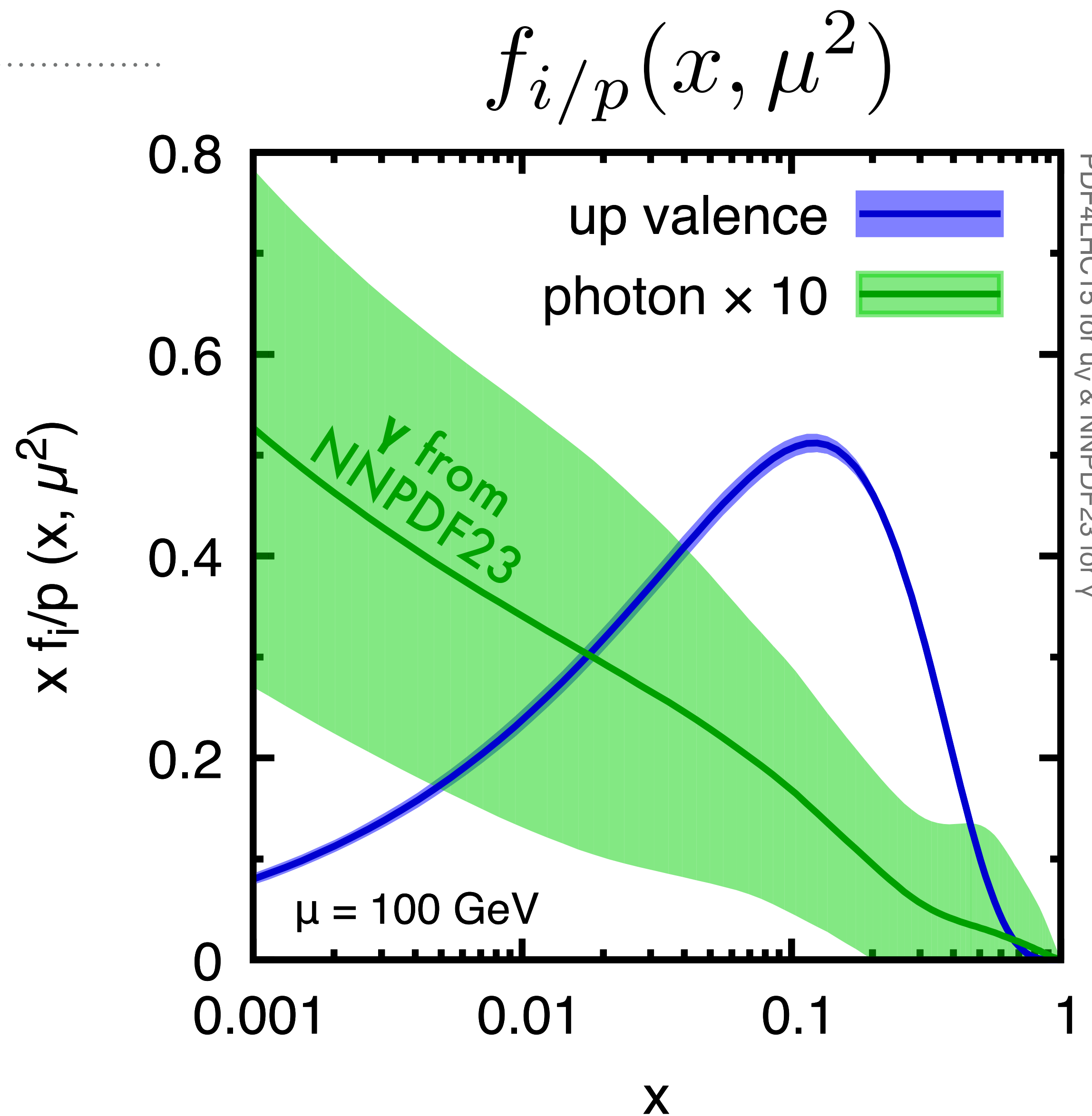
$$f_{u/p}(x, \mu^2)$$



# parton distribution functions (PDFs)

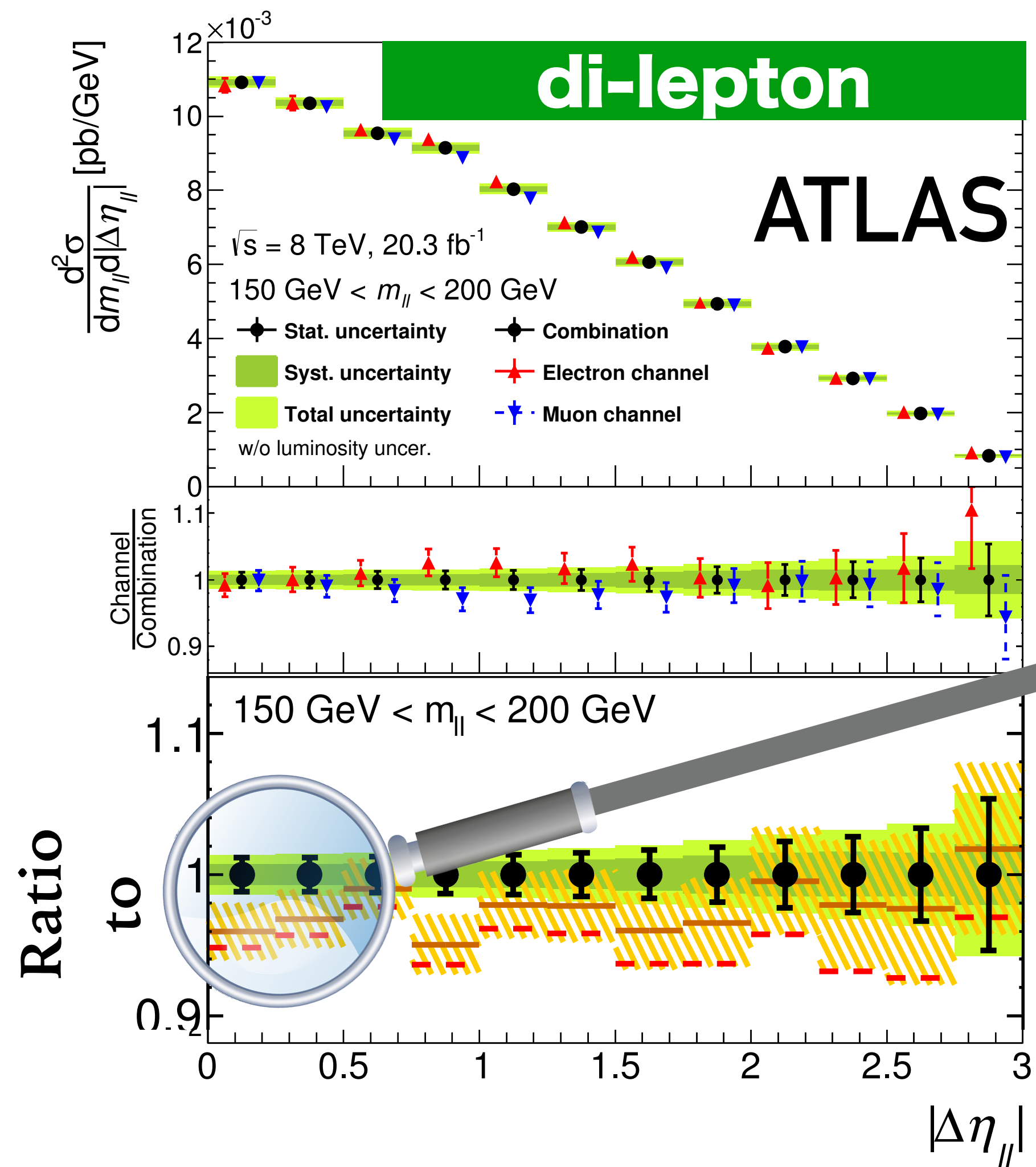


One exception:  
 the photon distribution  
 inside the proton  
 (had up to 100% uncertainty)



# model-independent $\gamma$ PDF fit (c. 2013)

status 2015

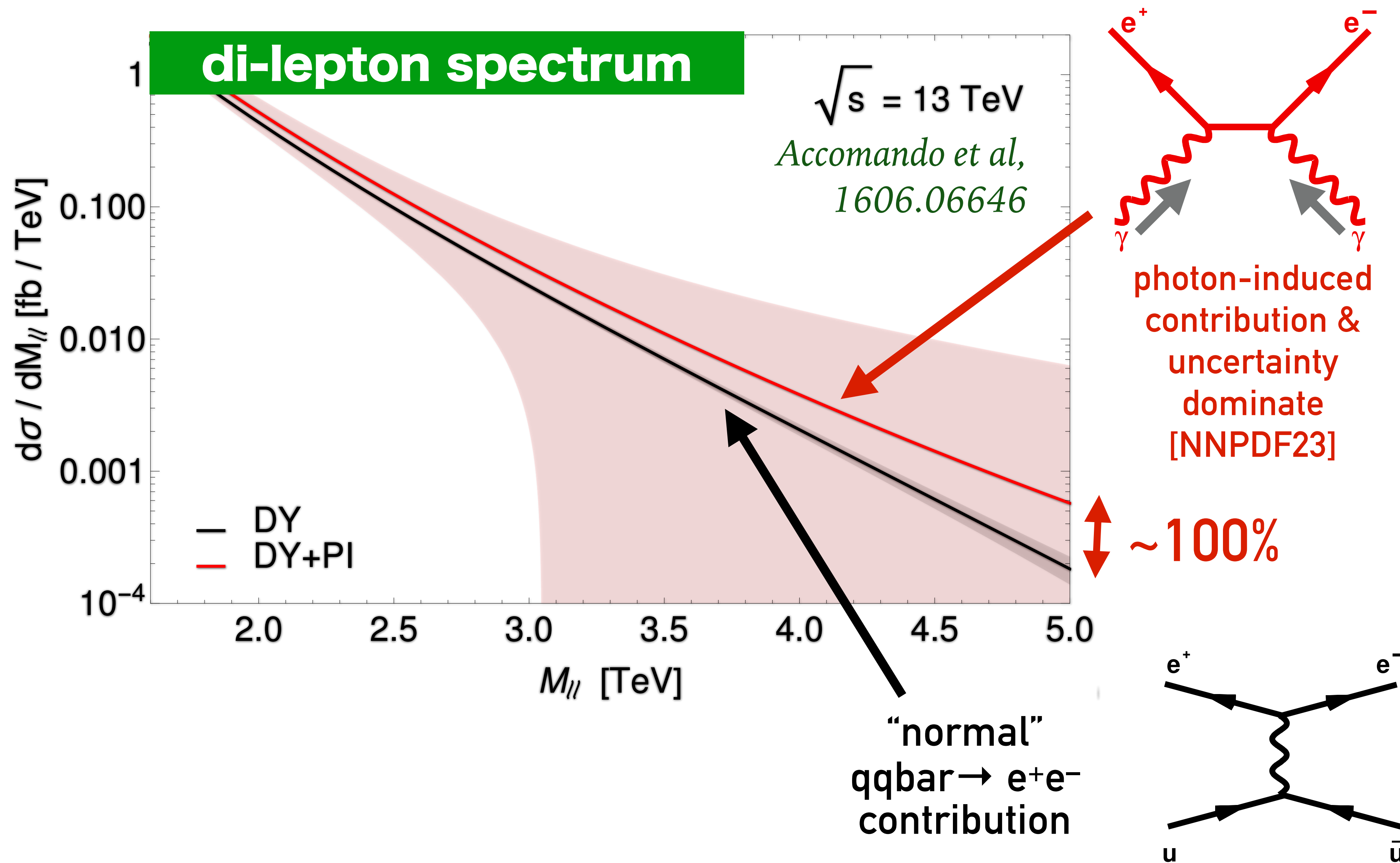


95-99% from  
 $q\bar{q} \rightarrow e^+e^-$

+ few % from  
 $\gamma\gamma \rightarrow e^+e^-$



it mattered for di-lepton, di-boson, ttbar, EW higgs, etc.

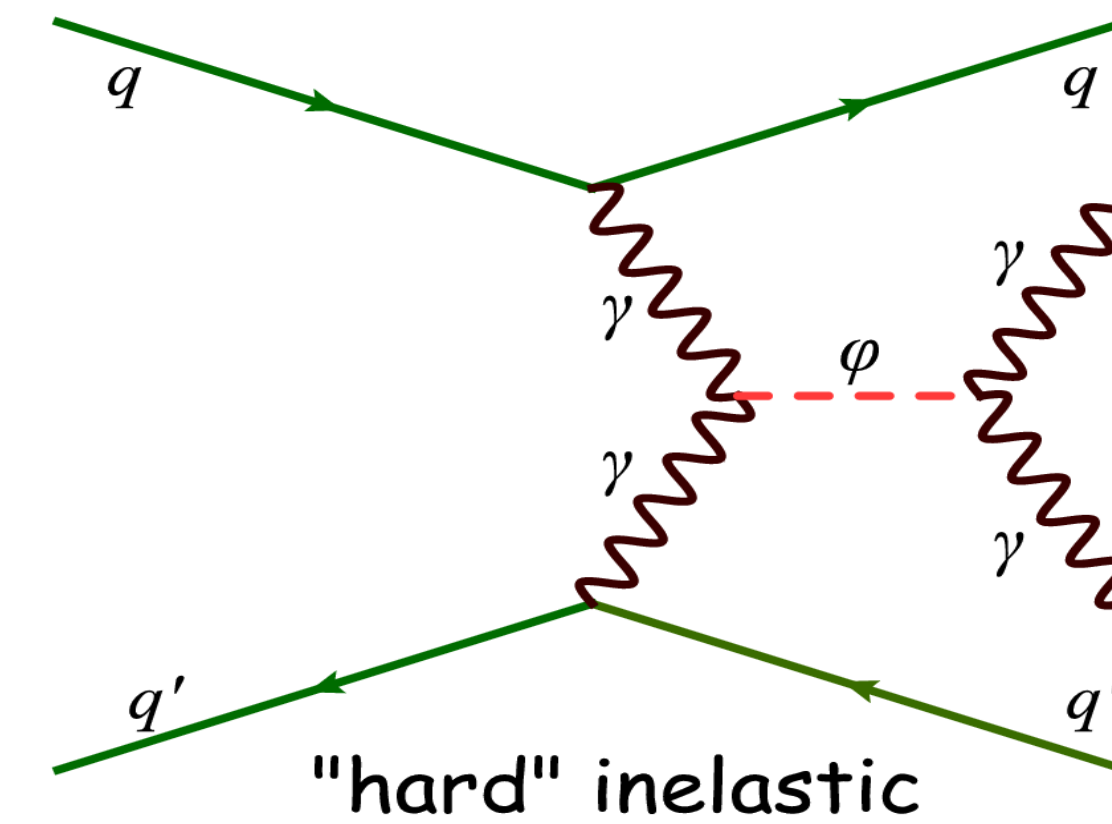
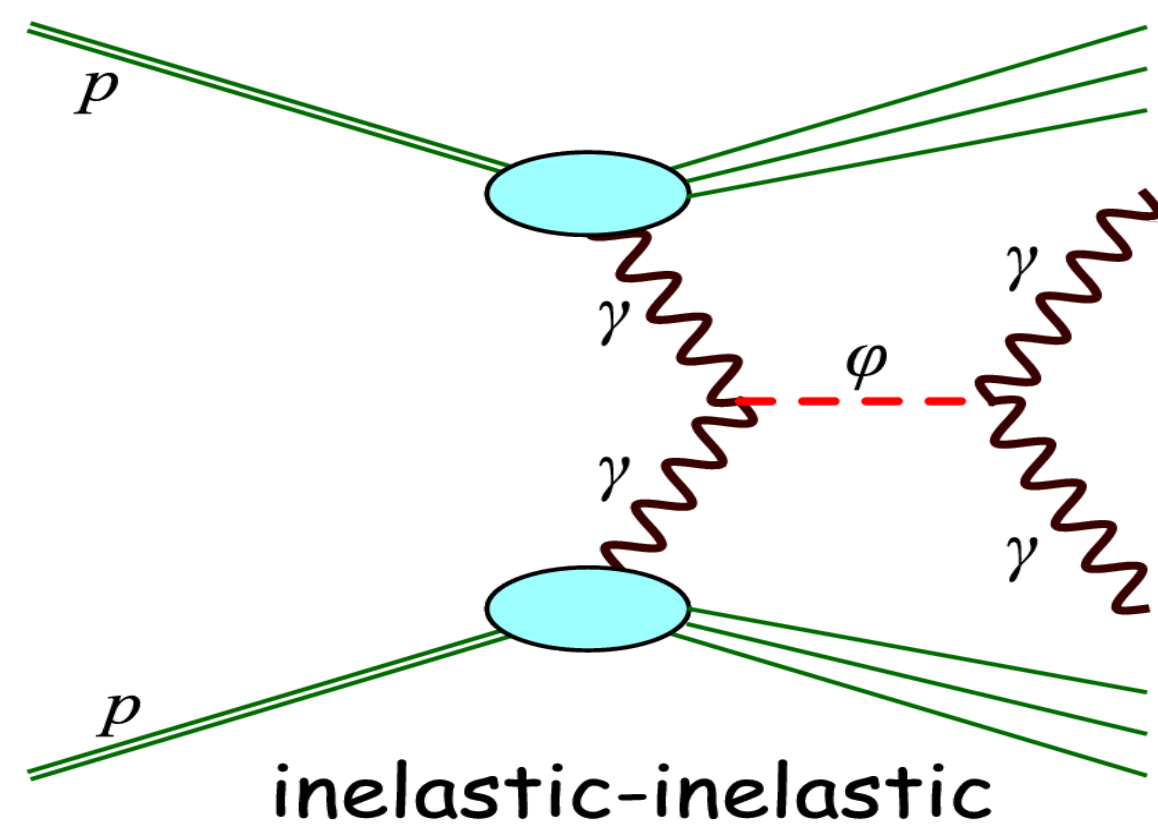
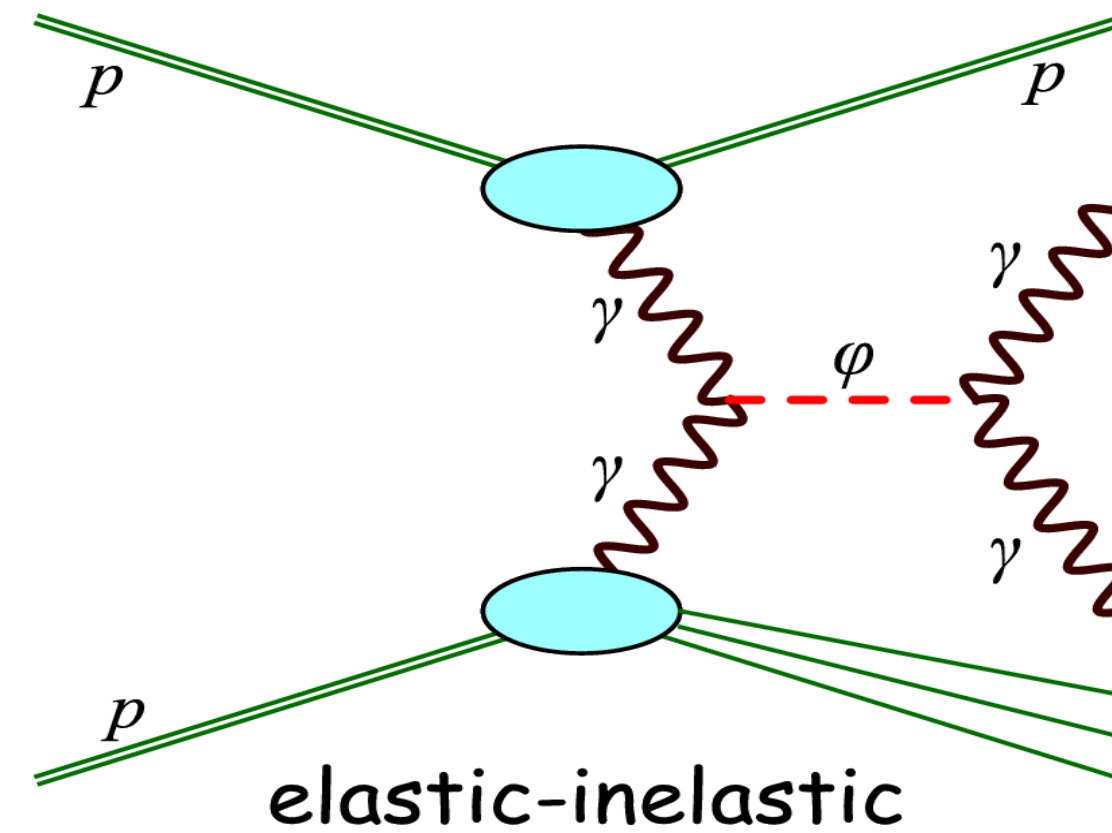
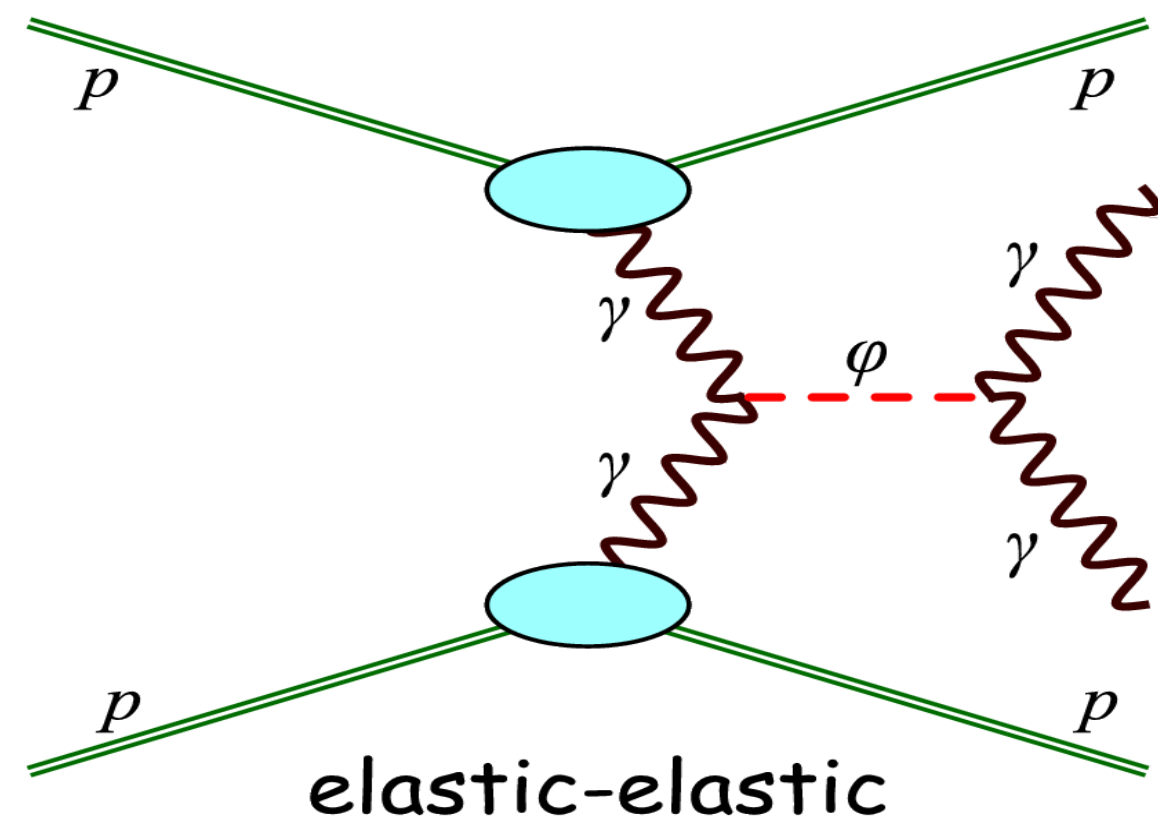


# Photon fusion

The 750 GeV excess from photon-photon and quark-quark processes

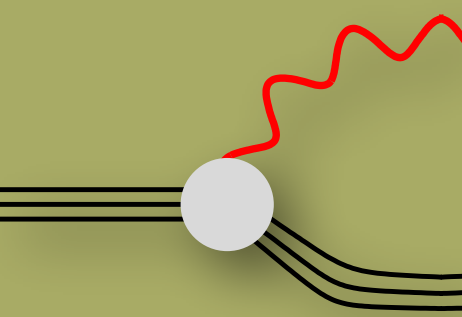
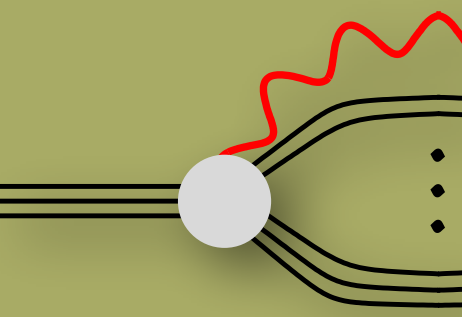
Tanumoy Mandal

(Moriond QCD, March 20, 2016)



1512.05751;1512.05776;1512.08502;1601.00386;1601.00638;1601.01144;1601.01571;1601.01712;  
1601.03772;1601.07167;1601.07187;1602.02380;1602.07574;1601.07774;1603.00287 ... more

# Widely discussed photon-PDF estimates

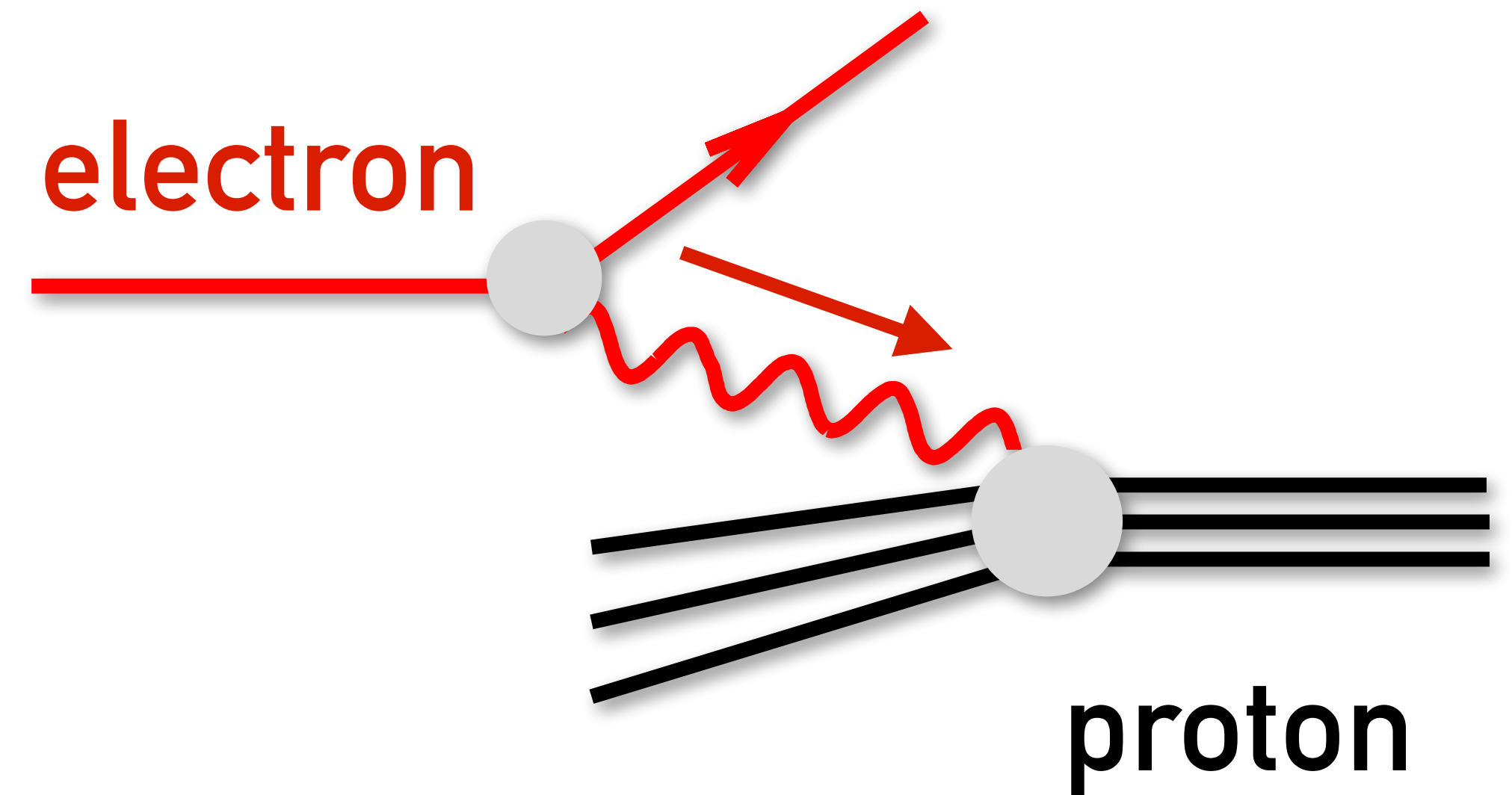
	 elastic	 inelastic	LHAPDF public computer-readable form?
Gluck Pisano Reya 2002	dipole	model	✗
MRST2004qed	✗	model	✓
CT14qed_inc	dipole	model (data-constrained)	✓
Martin Ryskin 2014	dipole (only electric part)	model	✗
Harland-Lang, Khoze Ryskin 2016	dipole	model	✗
NNPDF23qed (& NNPDF30qed)	no separation; fit to data		

*elastic part long known: Budnev, Ginzburg, Meledin & Serbo, Phys.Rept. 1974*

# How do you do better? → Use electron–proton scattering

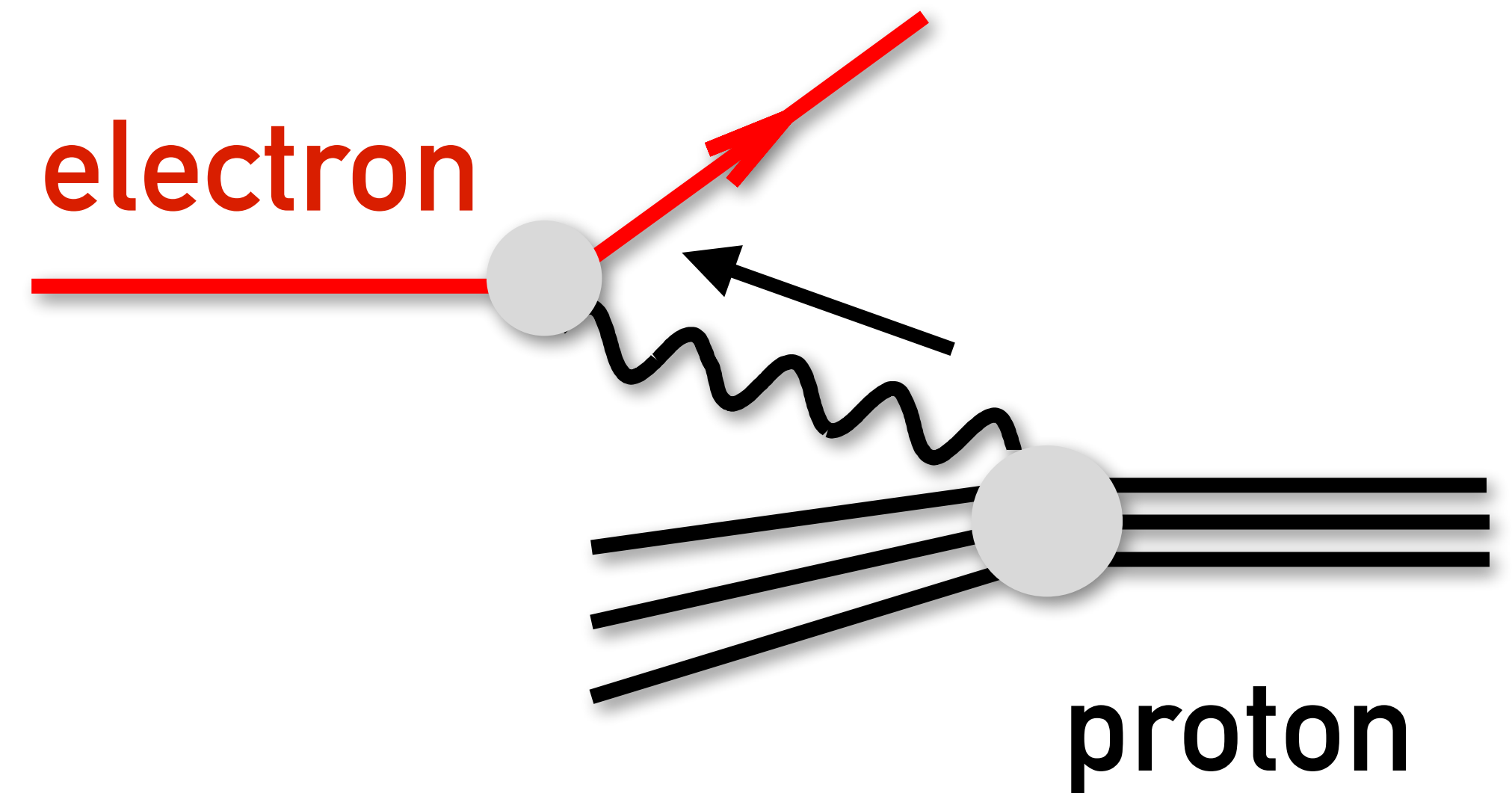
---

- ▶ Experiments have been going on for decades
- ▶ Usually seen as photons from electron probing proton structure



# How do you do better? → Use electron–proton scattering

- ▶ Experiments have been going on for decades
- ▶ Usually seen as photons from electron probing proton structure
- ▶ But **can be viewed as electron probing proton’s photonic field**
- ▶ Everything about unpolarized EM electron–proton interaction encoded in two “structure functions”  $F_2(x, Q^2)$  &  $F_L(x, Q^2)$



$$\frac{d\sigma}{dx dQ^2} = \frac{4\pi\alpha^2}{xQ^4} \left( \left( 1 - y + \frac{y^2}{2} \left( 1 + 2x^2 \frac{m_p^2}{Q^2} \right) \right) F_2(x, Q^2) - \frac{y^2}{2} F_L(x, Q^2) \right)$$

# February 2016

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**Gian Giudice**

Congratulations, Paolo!

Import-3 19 February 2016 at 21:32

[Hide](#)



On behalf of the CERN Theory Department, I wish to congratulate our colleague and former TH staff member, Paolo Nason, on his appointment to the Accademia Nazionale dei Lincei. Paolo joins in this prestigious academy our Director General, Fabiola Gianotti, and three other former TH staff members, Luciano Maiani, Guido Martinelli, and Gabriele Veneziano.

--

Gian Francesco Giudice  
Theoretical Physics Department, CERN  
CH 1211 Geneva 23, Switzerland  
Tel. +41 22 767 3203

# Most of the world uses Mathematica...

---



**Paolo Nason**

Maxima

To: Gavin Salam,

Cc: g.zanderighi1@physics.ox.ac.uk, Aneesh Manohar,

Resent-From: Gavin Salam

Import 8 March 2016 at 16:51

[Hide](#)



svn co <svn+ssh://nason@pcte15.mib.infn.it/Maxima>

read the README and follow the instruction.

# Part A: getting the core formula

---

- ▶ expect photon distribution to be an integral over standard DIS structure functions,  $F_2$  and  $F_L$

$$f_{\gamma/p}(x, \mu^2) = \int dx' \int dQ^2 [c_2(\dots)F_2(x', Q^2) + c_L(\dots)F_L(x', Q^2)]$$

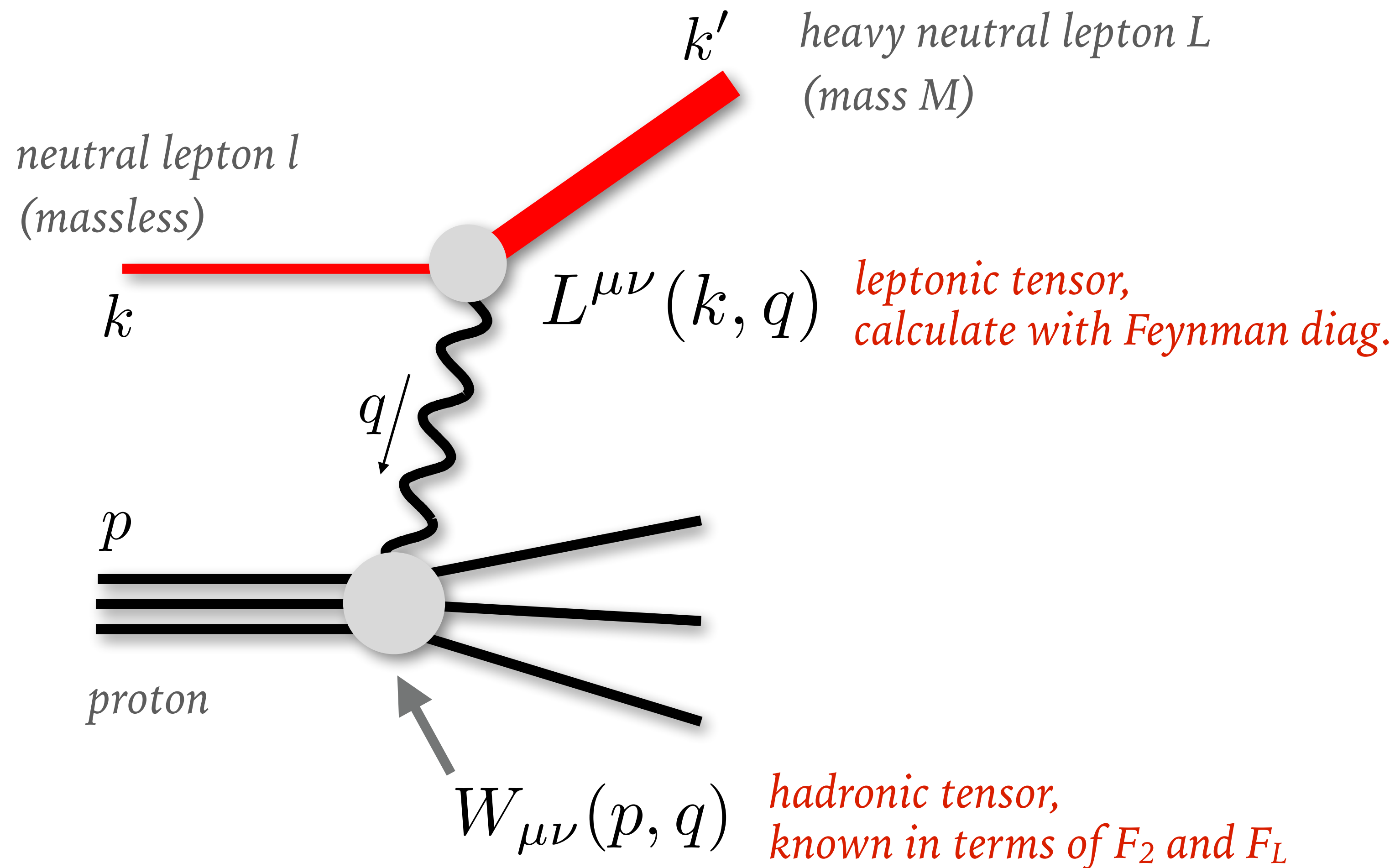
- ▶ **Our task: figure out the coefficients  $c_2(\dots)$  and  $c_L(\dots)$  multiplying  $F_2$  and  $F_L$**

Manohar, Nason, GPS & Zanderighi, arXiv:1607.04266  
(use of BSM inspired by Drees & Zeppenfeld, PRD39(1989)2536)



# Heavy-lepton cross section in terms of structure functions

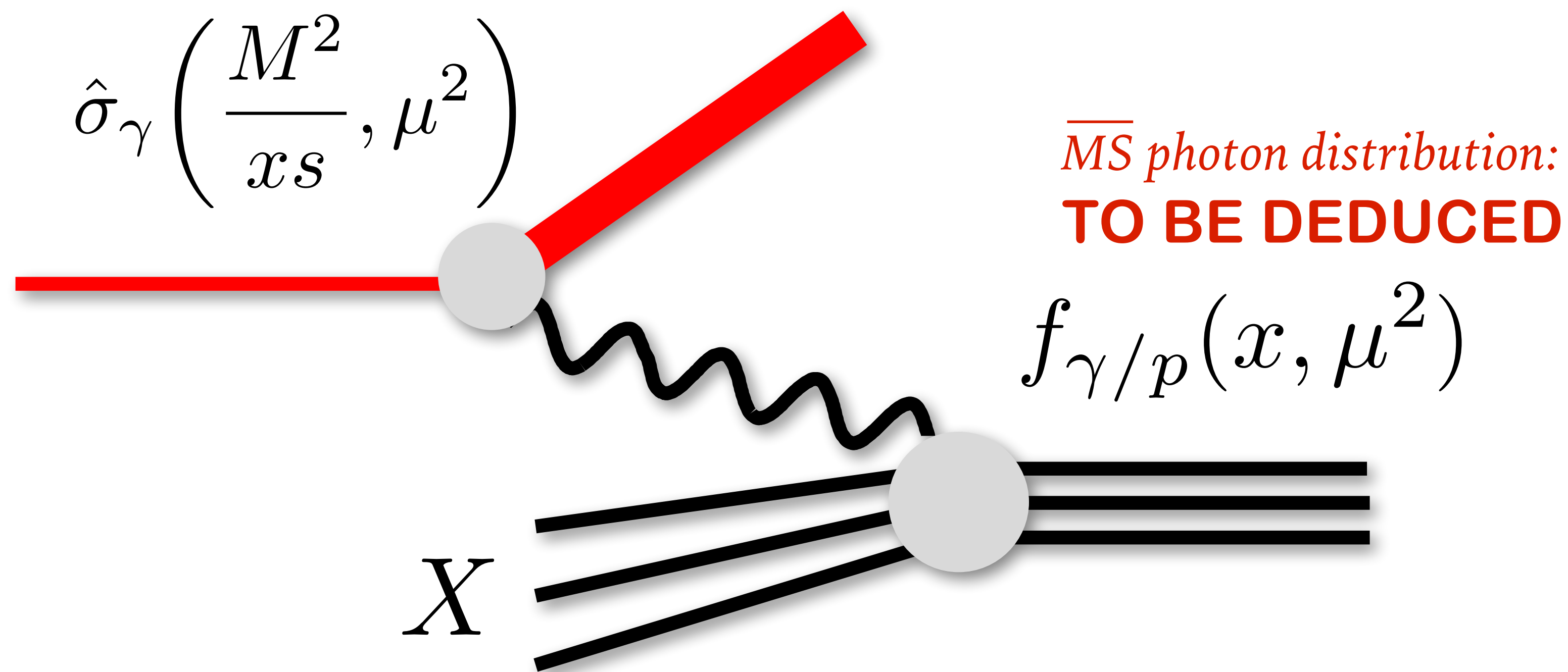
(use of BSM inspired by  
Drees & Zeppenfeld,  
PRD39(1989)2536)



$$\sigma = \frac{1}{4p \cdot k} \int \frac{d^4 q}{(2\pi)^4 q^4} e_{\text{ph}}^2(q^2) [4\pi W_{\mu\nu} L^{\mu\nu}(k, q)] \times 2\pi \delta((k - q)^2 - M^2)$$

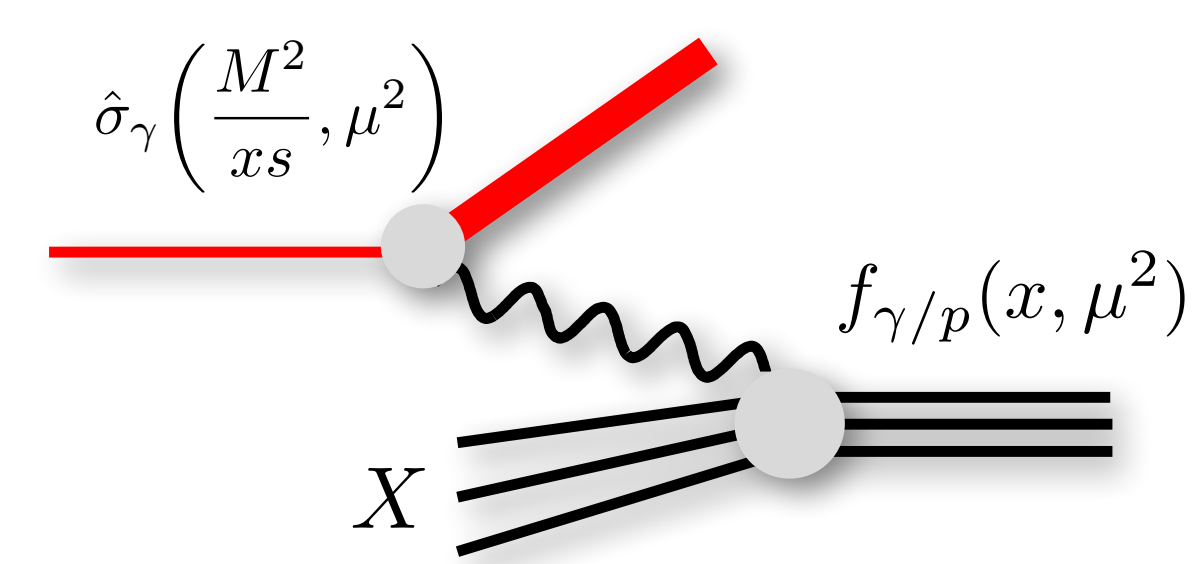
# Cross section in terms of structure functions

*hard-scattering cross section  
calculate in collinear factorisation*



$$\sigma = c_0 \sum_a \int \frac{dx}{x} \hat{\sigma}_a \left( \frac{M^2}{xS}, \mu^2 \right) x f_{a/p}(x, \mu^2)$$

# Cross section in terms of structure functions



Hard cross section driven by the photon distribution at LO



$$\hat{\sigma}_a(z, \mu^2) = \alpha(\mu^2)\delta(1-z)\delta_{a\gamma} + \frac{\alpha^2(\mu^2)}{2\pi} \left[ -2 + 3z + zp_{\gamma q}(z) \ln \frac{M^2(1-z)^2}{z\mu^2} \right] \sum_{i \in \{q, \bar{q}\}} e_i^2 \delta_{ai} + \dots,$$



Quarks and gluons come in at higher orders

# Photon PDF in terms of $F_2$ and $F_L$ — the **LUXqed** approach

$$x f_{\gamma/p}(x, \mu^2) = \frac{1}{2\pi\alpha(\mu^2)} \int_x^1 \frac{dz}{z} \left\{ \int_{\frac{x^2 m_p^2}{1-z}}^{\frac{\mu^2}{1-z}} \frac{dQ^2}{Q^2} \alpha^2(Q^2) \right. \\ \left. \left[ \left( z p_{\gamma q}(z) + \frac{2x^2 m_p^2}{Q^2} \right) F_2(x/z, Q^2) - z^2 F_L\left(\frac{x}{z}, Q^2\right) \right] \right. \\ \left. - \alpha^2(\mu^2) z^2 F_2\left(\frac{x}{z}, \mu^2\right) \right\}$$

This includes terms

$$\alpha L (\alpha_s L)^n$$

$$\alpha (\alpha_s L)^n$$

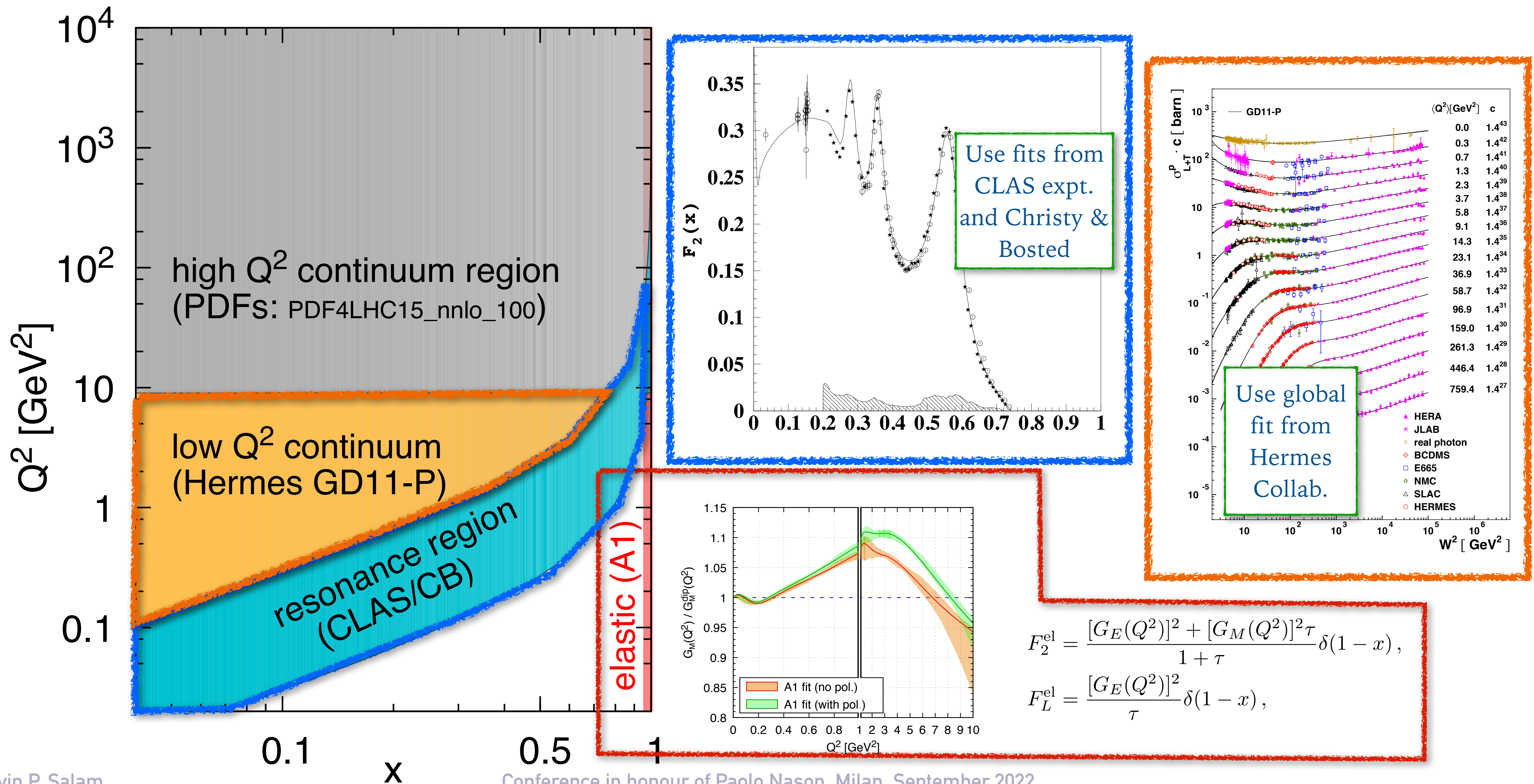
$$\alpha^2 L^2 (\alpha_s L)^n$$

$$(L = \ln \mu^2/\Lambda^2)$$

our 2017 work went one order higher (e.g. extra power of  $\alpha_s$ )

It subsequently emerged that two “forgotten” papers, Anlauf et. al, CPC70(1992)97 Mukherjee & Pisano, [hep-ph/0306275](https://arxiv.org/abs/hep-ph/0306275), had the correct integrand (but not the limits)

# Part B: finding $F_2$ and $F_L$ data to put into the formula



# July 2016: Finishing the paper

---



**Paolo Nason**

Import-2 14 July 2016 at 07:23

**WRONG TITLE !!!!**

[Hide](#)

To: g.zanderighi1@physics.ox.ac.uk, Gavin Salam,  
Aneesh Manohar,  
Resent-From: Gavin Salam



Ha! the title is wrong!

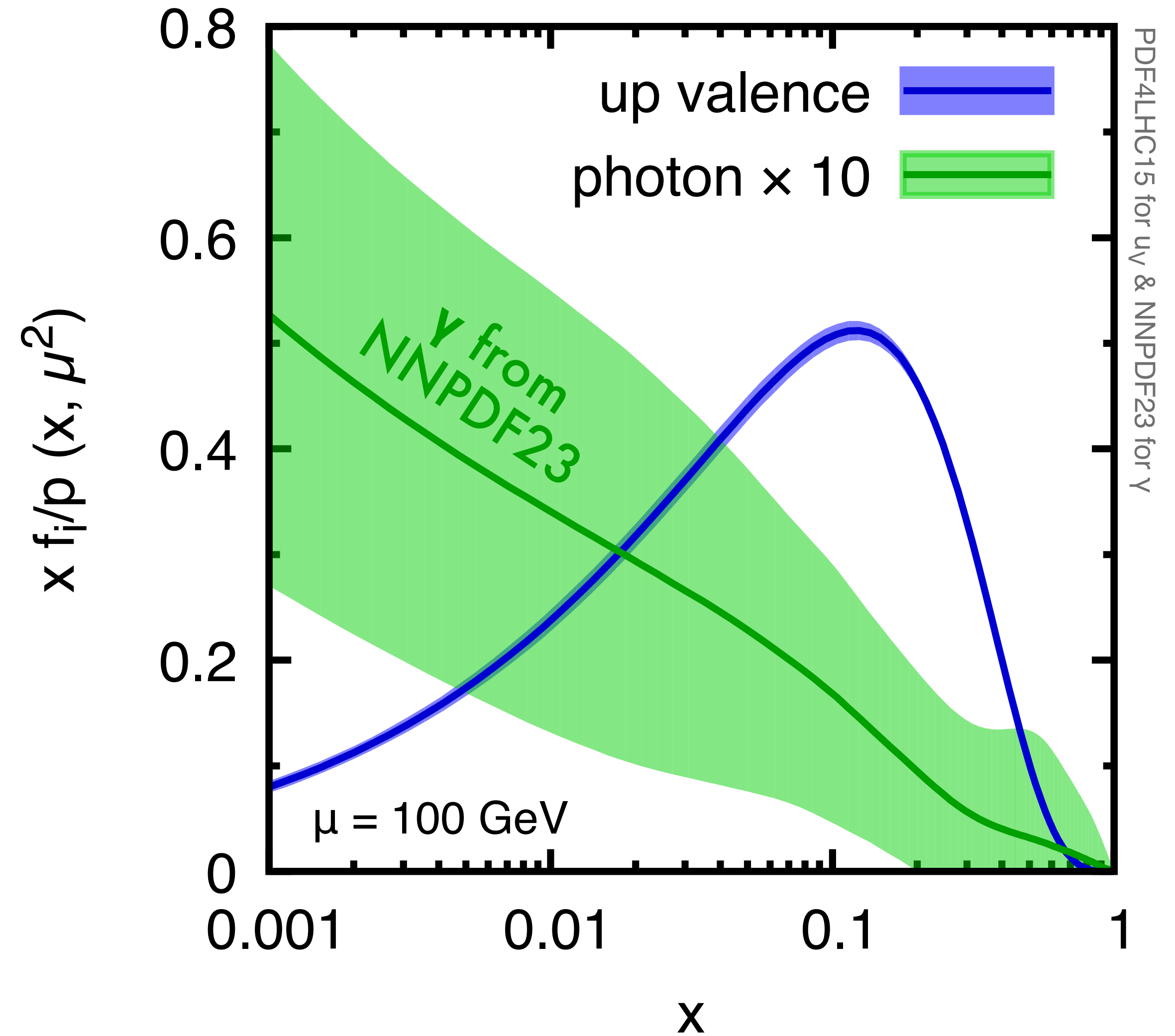
It says how bright is the photon!

How could we miss this?

P.

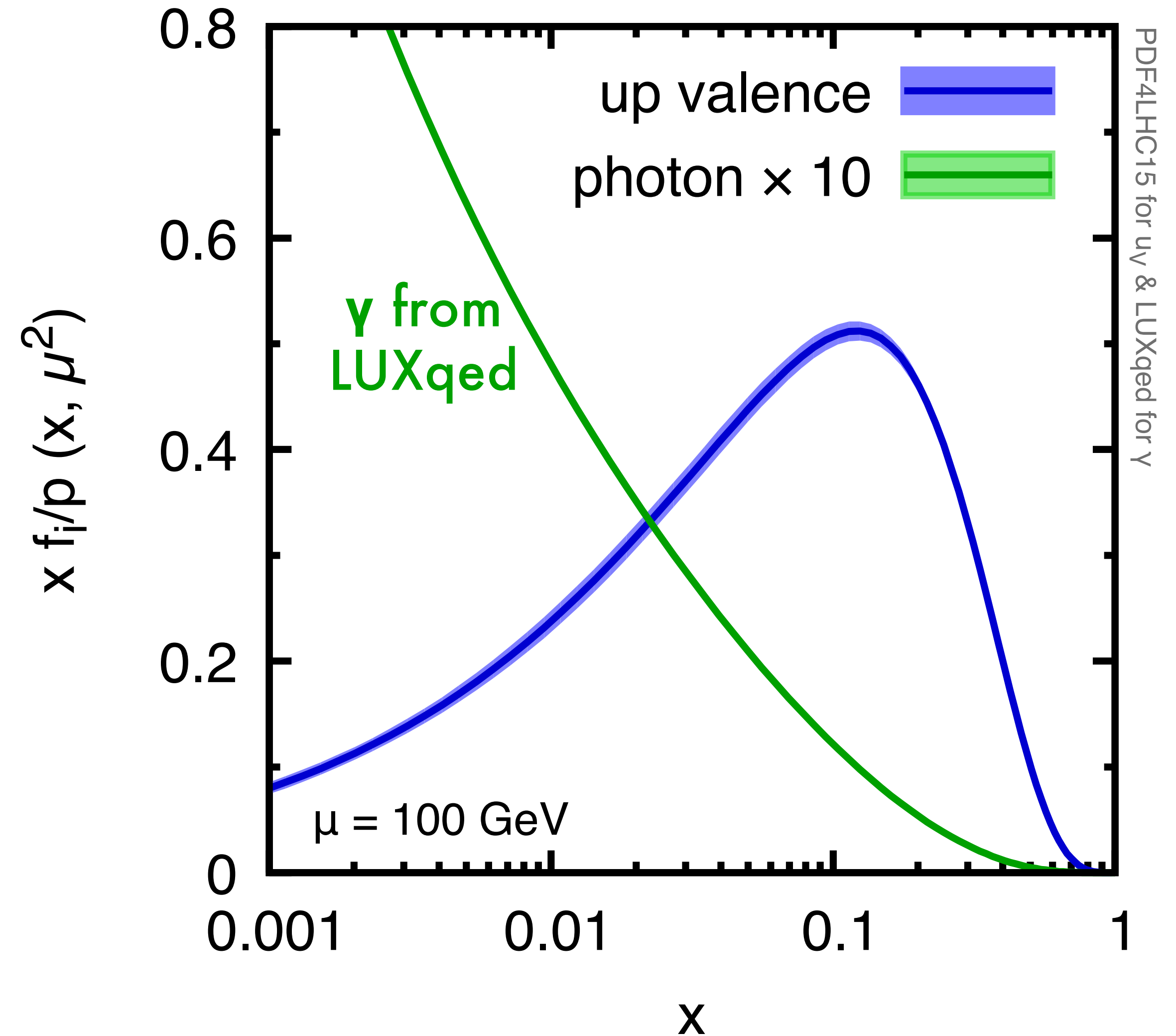
# photon PDF results

- Model-independent uncertainty (NNPDF) was 50–100%



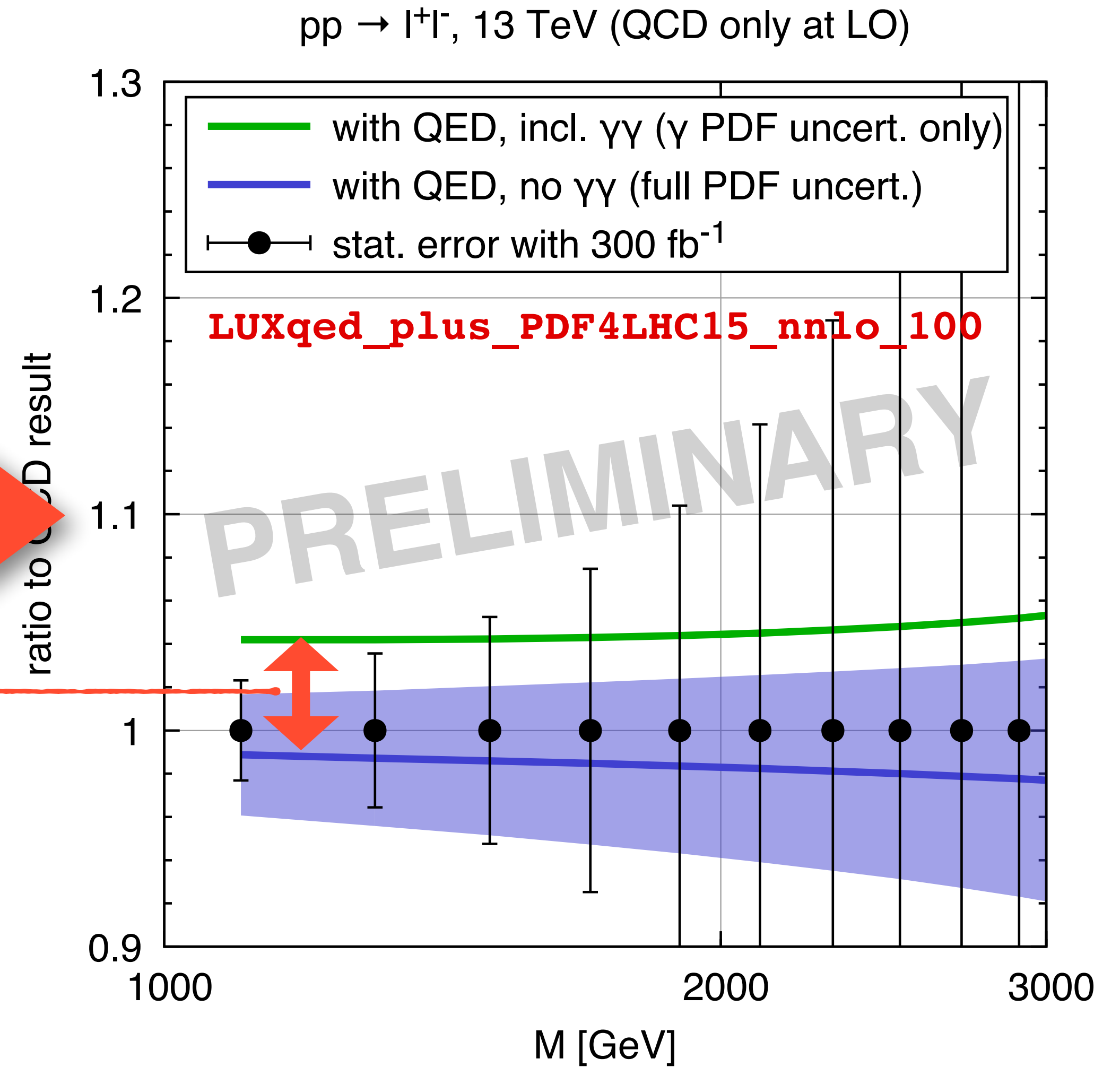
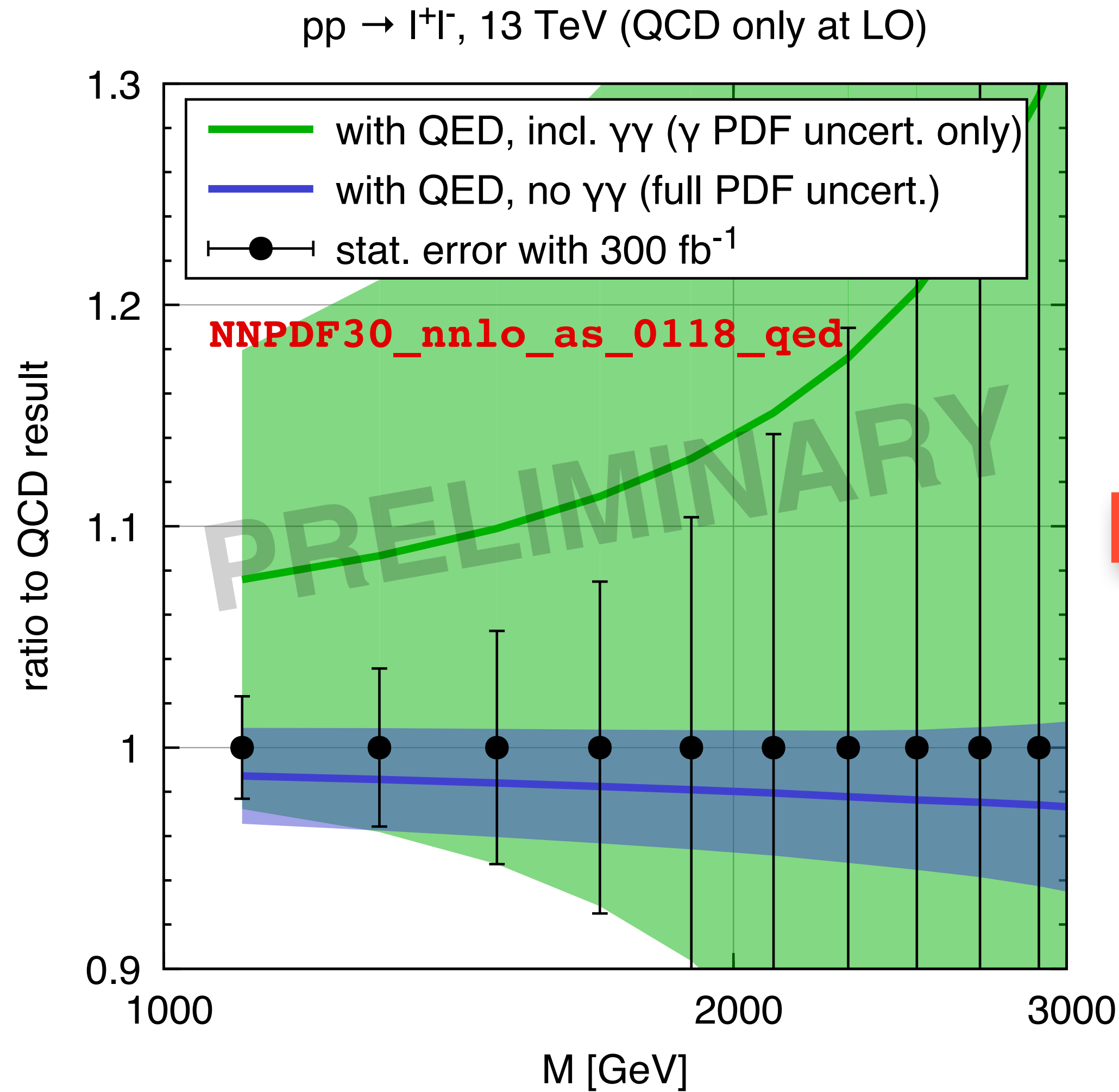
# photon PDF results

- ▶ Model-independent uncertainty (NNPDF) was 50–100%
- ▶ Goes down to  $O(1\%)$  with LUXqed determination



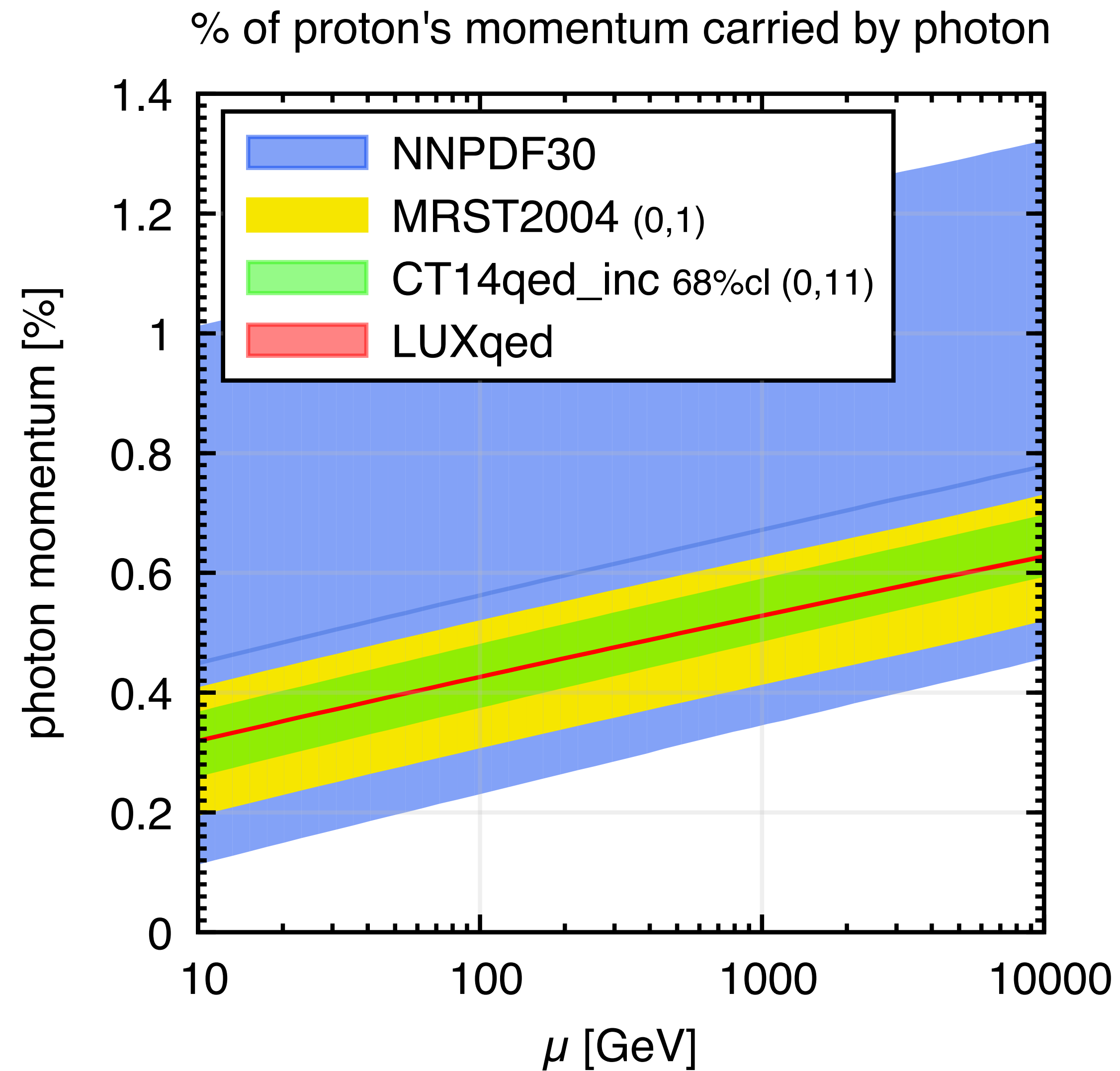


# di-lepton spectrum



$\gamma\gamma$  component has few-% effect on Drell-Yan spectrum; negligible uncertainty

# How bright is the proton? [ $\gamma$ momentum fraction]



momentum ( $\mu = 100$ GeV)	
gluon	$46.8 \pm 0.4\%$
up valence	$18.2 \pm 0.3\%$
down valence	$7.5 \pm 0.2\%$
light sea quarks	$20.7 \pm 0.4\%$
charm	$4.0 \pm 0.1\%$
bottom	$2.5 \pm 0.1\%$
photon	$0.426 \pm 0.003\%$

LUXqed\_plus\_PDF4LHC15\_nnlo\_100

(1+107 members, symmhessian, errors handled by LHAPDF out of the box,

valid for  $\mu > 10$  GeV)

# Where do we submit? → PRL

---

## Referee A

[...]

This work is interesting but it does not meet the criteria of innovation and impact expected for publication in Physical Review Letters.

[...]

Luckily, referees B & C were more positive; paper eventually accepted...

# Where do we submit? → PRL

---

**Subject:**To\_author LU16377 Manohar PRL Editors' Suggestion

**Date:**Wed, 26 Oct 2016 16:01:04 -0400

**From:**[prl@aps.org](mailto:prl@aps.org)

**Reply-To:**[prl@aps.org](mailto:prl@aps.org)

**To:**[g.zanderighi1@physics.ox.ac.uk](mailto:g.zanderighi1@physics.ox.ac.uk)

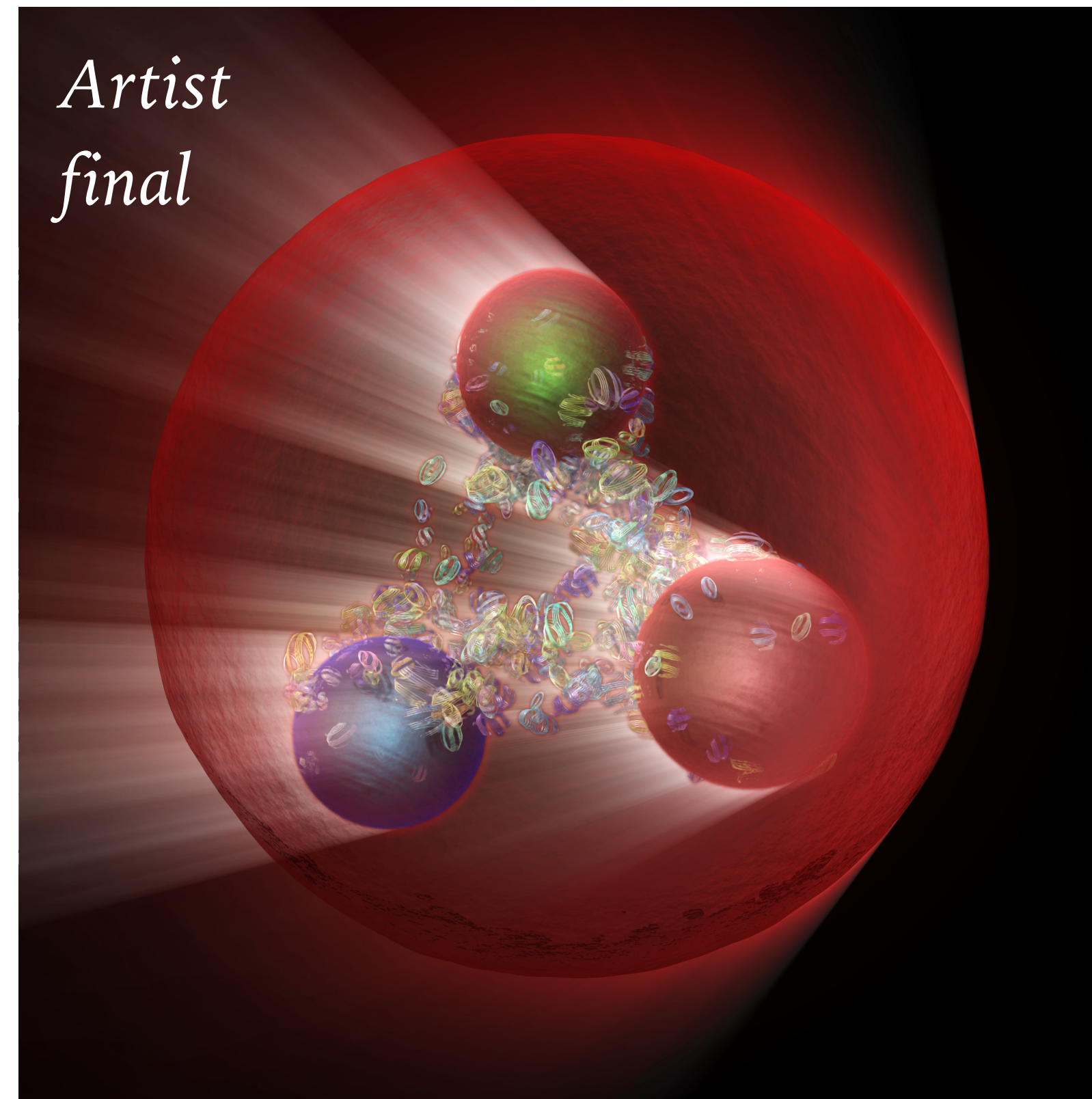
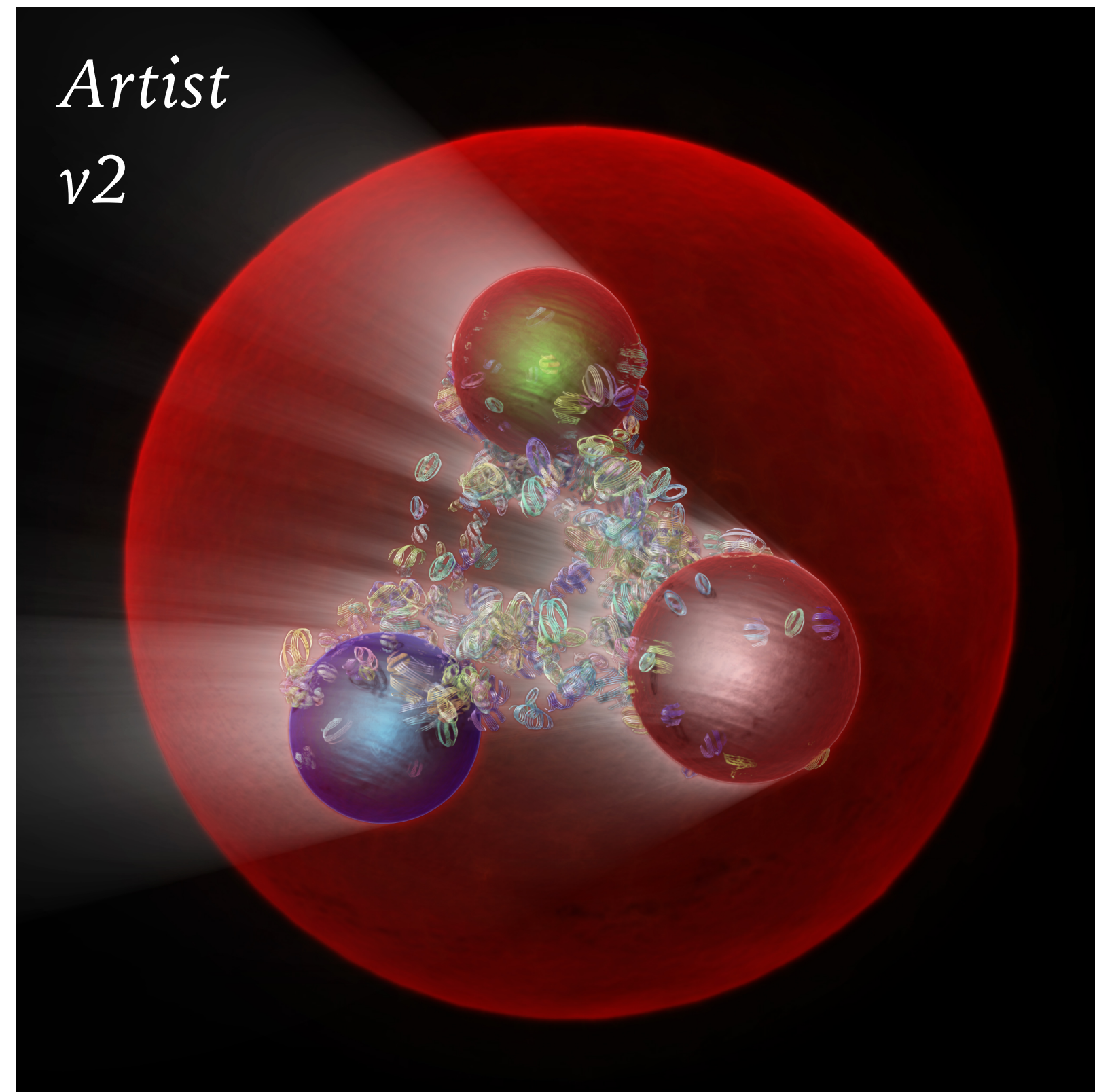
Dear Dr. Zanderighi,

We are pleased to inform you that we have selected your recently accepted manuscript to be a PRL Editors' Suggestion. [...]

Please reply to this email with an image that meets the criteria appended below.

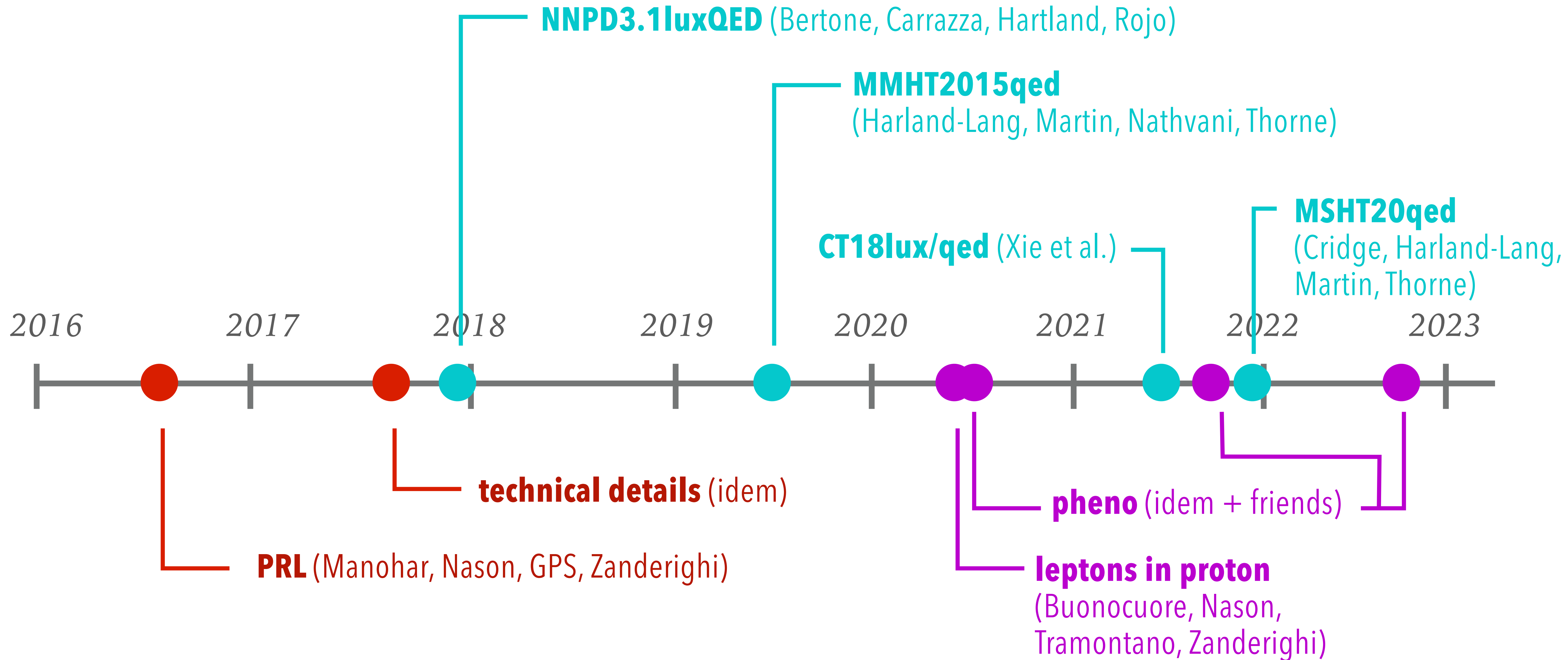
# October 2016 — Getting CERN's help for an image

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*with thanks to CERN artist Daniel Dominguez for his patience with us!*

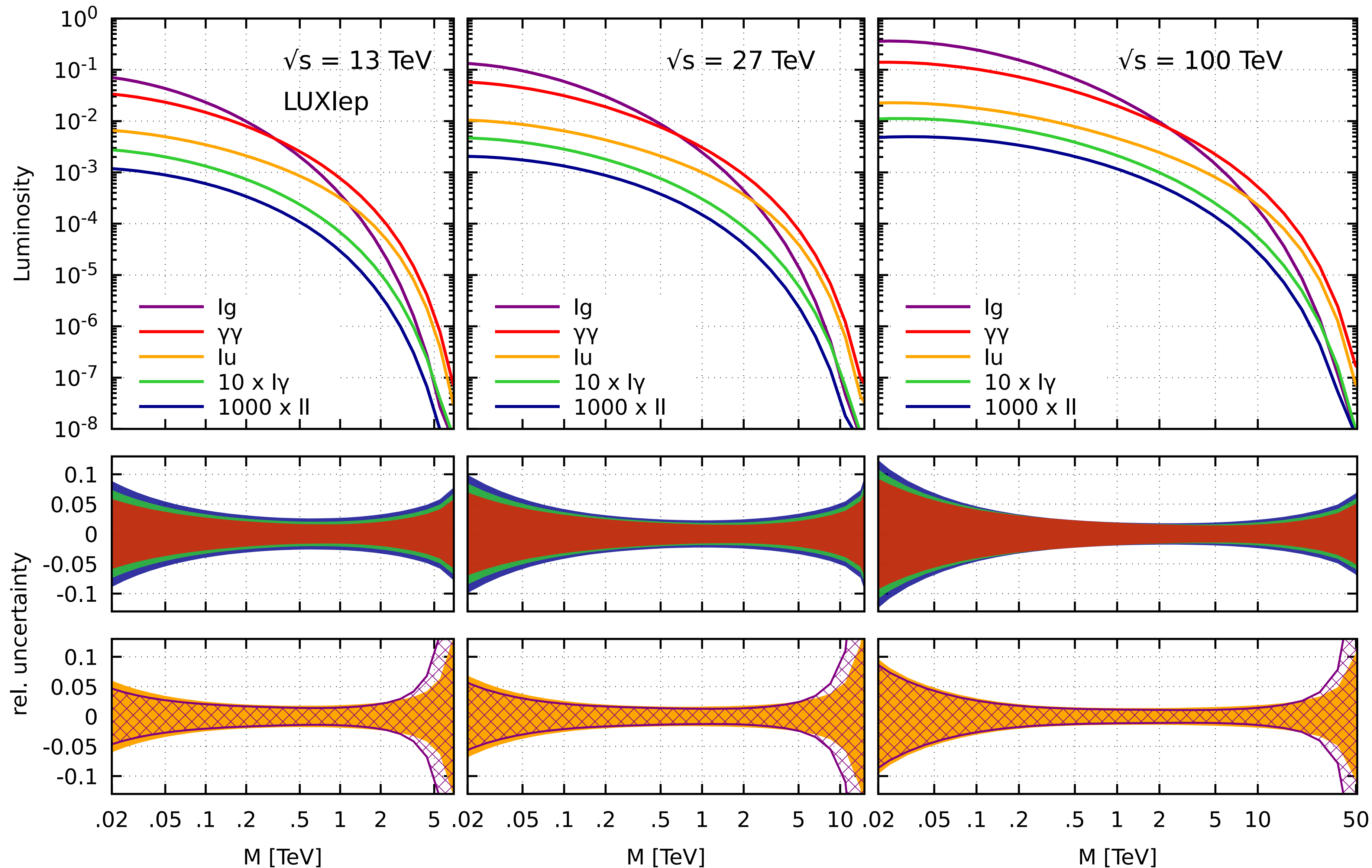
# Key subsequent developments



# Leptons in the proton: 2005.06477 (Buonocore, Nason, Tramontano, Zanderighi)

$$\begin{aligned}
 x_\ell f_\ell(x_\ell, \mu_F^2) = & \left( \frac{1}{2\pi} \right)^2 \int_{x_\ell}^1 \frac{dx}{x} z_\ell \int_x^1 \frac{dz}{z} \int_{\frac{m_p^2 x^2}{1-z}}^{\frac{\mu_F^2}{1-z}} \frac{dQ^2}{Q^2} \alpha^2(Q^2) \\
 & \left\{ P_{l\gamma}(z_\ell) \log \frac{\mu_F^2}{(1-z_\ell)z_\ell \left( Q^2 + \frac{m_\ell^2}{z_\ell(1-z_\ell)} \right)} \left[ F_2 \left( z P_{\gamma q}(z) + \frac{2m_p^2 x^2}{Q^2} \right) - F_L z^2 \right] \right. \\
 & + F_2 \left[ 4(z-2)^2 z_\ell(1-z_\ell) - (1+4z_\ell(1-z_\ell)) z P_{\gamma q}(z) \right] \\
 & + F_L z^2 P_{l\gamma}(z_\ell) - \frac{2m_p^2 x^2}{Q^2} F_2 - \left( F_2 \frac{2m_p^2 x^2}{Q^2} - z^2 F_L \right) 4z_\ell(1-z_\ell) \\
 & + \frac{m_\ell^2 F_2}{m_\ell^2 + Q^2 z_\ell(1-z_\ell)} \left[ z P_{\gamma q}(z) - 8z_\ell(1-z_\ell) \left( 1 - z - \frac{m_p^2 x^2}{Q^2} \right) + \frac{2m_p^2 x^2}{Q^2} \right] \\
 & \left. - \frac{m_\ell^2 F_L z^2}{m_\ell^2 + Q^2 z_\ell(1-z_\ell)} [2 - P_{l\gamma}(z_\ell)] \right\}. \tag{2.25}
 \end{aligned}$$

# Leptons in the proton: 2005.06477 (Buonocore, Nason, Tramontano, Zanderighi)



partonic  
luminosities  
with leptons and  
photons



# Conclusions

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As usual, when Paolo touches something,  
chances are it will come out fundamentally changed

(And then he takes it through to the end)

I look forward to many more such fundamental advances from you, Paolo!