



# CP violation in heavy flavour decays

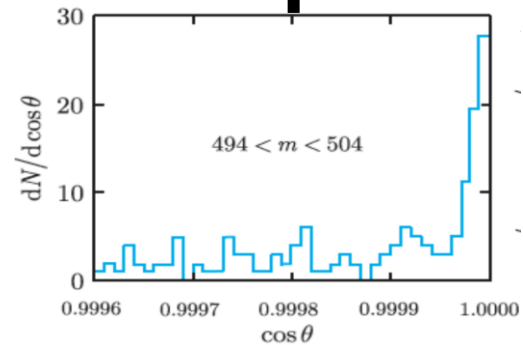
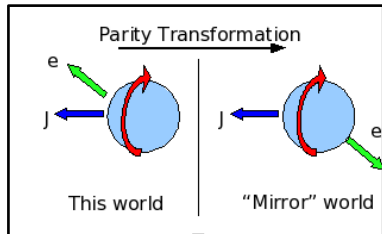
**Yuehong Xie, Central China Normal University**  
**(on behalf of LHCb & Belle II Collaborations)**



**31st International Symposium on Lepton Photon Interactions at High Energies**  
Melbourne, Australia, 17-21 July 2023

# Sixty years of CP violation

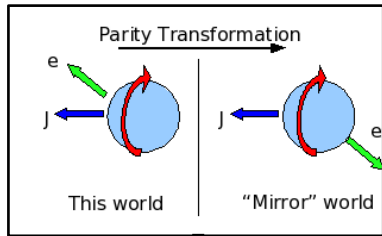
**P violation**  
1956, Wu et al.



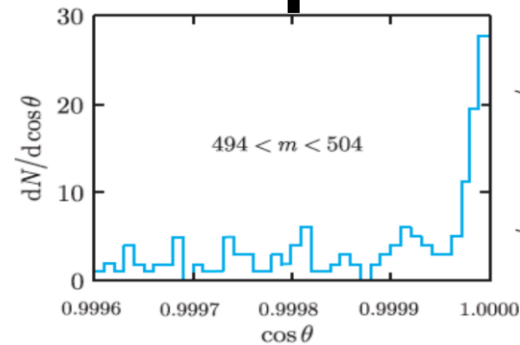
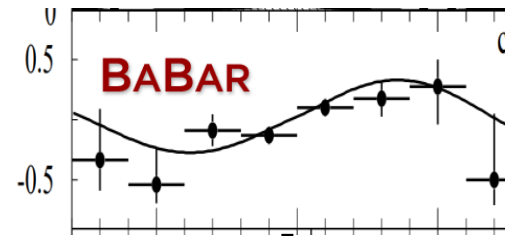
**CP violation in  $K^0$  mixing**  
1964, Cronin, Fitch et al.

# Sixty years of CP violation

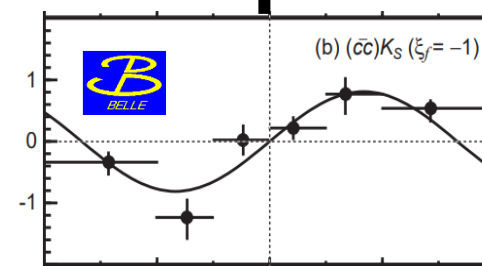
**P violation**  
1956, Wu et al.



**Time-dependent CP violation in  $B^0$  decays**  
2001, BaBar & Belle

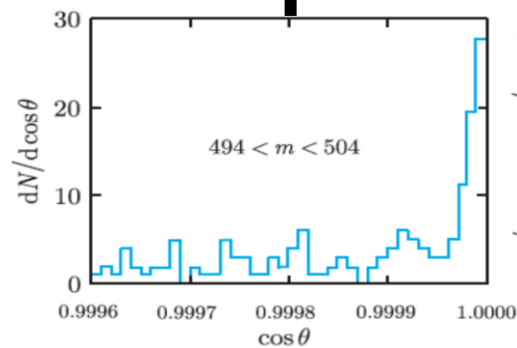
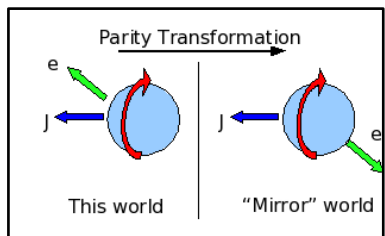


**CP violation in  $K^0$  mixing**  
1964, Cronin, Fitch et al.



# Sixty years of CP violation

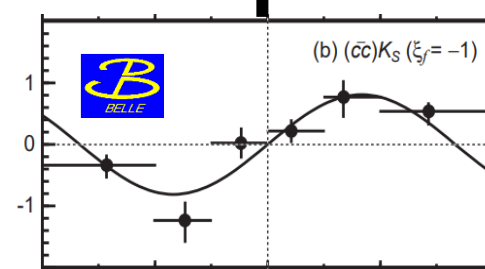
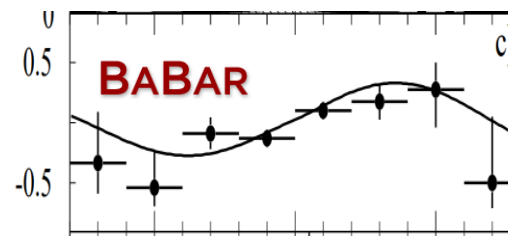
**P violation**  
**1956, Wu et al.**



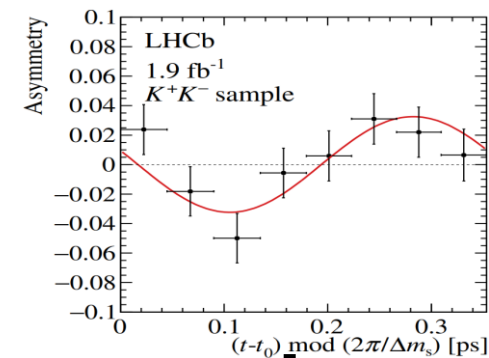
**CP violation in  $K^0$  mixing**  
1964, Cronin, Fitch et al.

# Time-dependent CP violation in $B^0$ decays

## 2001, BaBar & Belle



# Time-dependent CP violation in $B_s^0$ decays



## CP violation in $D^0$ decay



# CKM mechanism: the current theory

□ EWSB & diagonalisation of Yukawa mass matrix  $\Rightarrow$  quark mixing matrix

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = V_{CKM} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$\mathcal{L}_{W\pm} = \frac{g}{\sqrt{2}} (\bar{U}_L \gamma^\mu W_\mu^+ V_{CKM} D_L + \bar{D}_L \gamma^\mu W_\mu^- V_{CKM}^+ U_L)$$

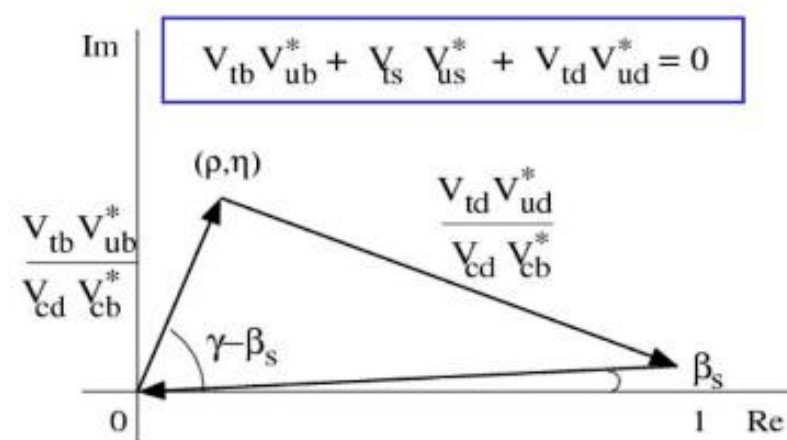
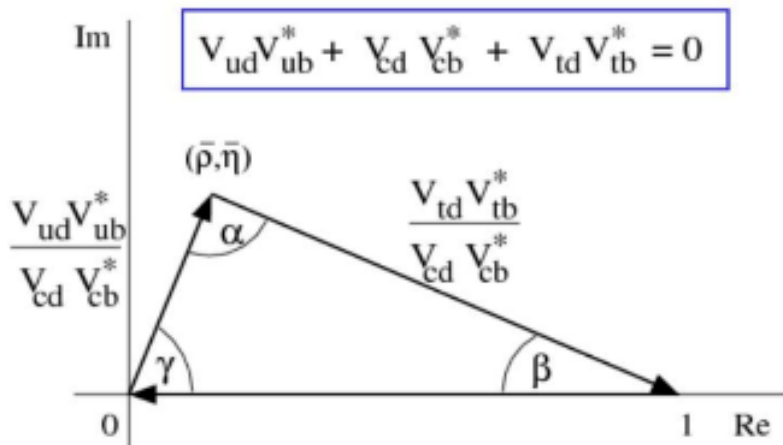
$$V_{CKM} = \begin{pmatrix} 1 - \frac{|^2}{2} & | & A|^3 (r - ih) \\ -| & 1 - \frac{|^2}{2} & A|^2 \\ A|^3 (1 - r - ih) & -A|^2 & 1 \end{pmatrix}$$

L.Wolfenstein PRL 51 (1983) 1945

$(A, \lambda, \rho, \eta)$  to be measured in data

$\eta \neq 0 \Rightarrow$  CP violation

□ Unitarity of the CKM matrix:  $V^\dagger V = I$

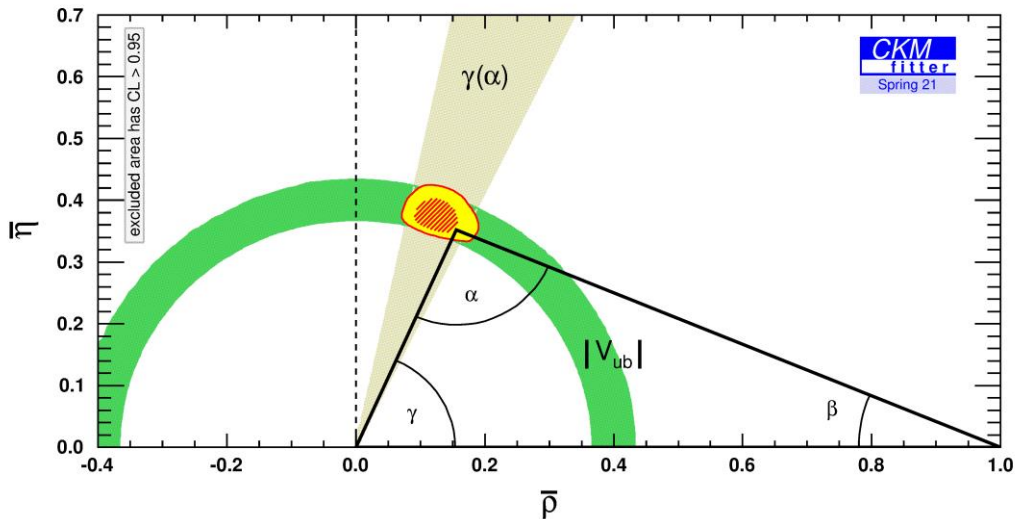


# Test of CKM unitarity

Test the CKM mechanism via over-constraining the four parameters

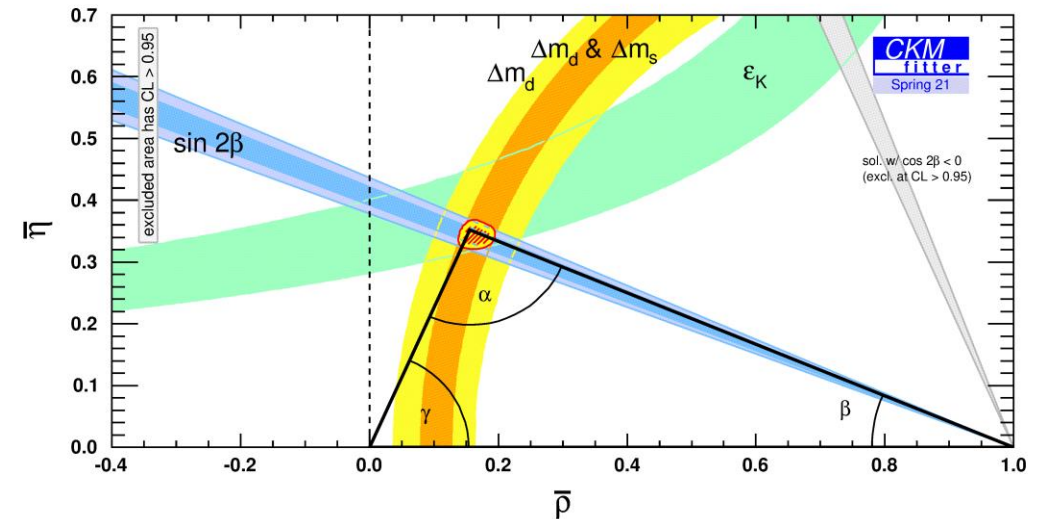
## □ Tree quantities

- $\gamma$  from  $B \rightarrow Dh$
- $V_{ub}$  from  $B \rightarrow \rho/\pi l^- \bar{\nu}$
- ...

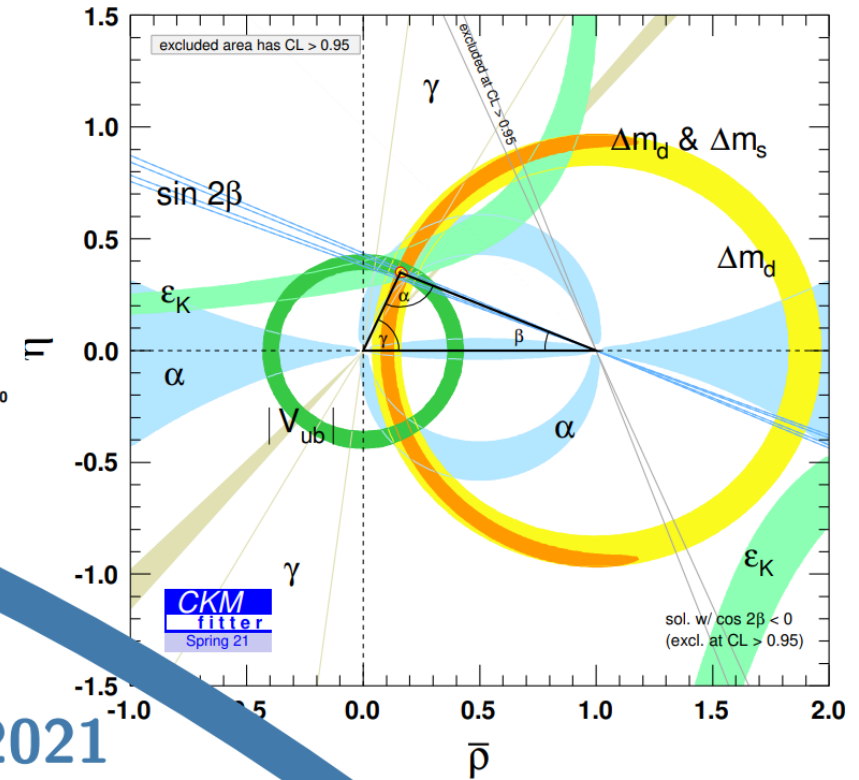
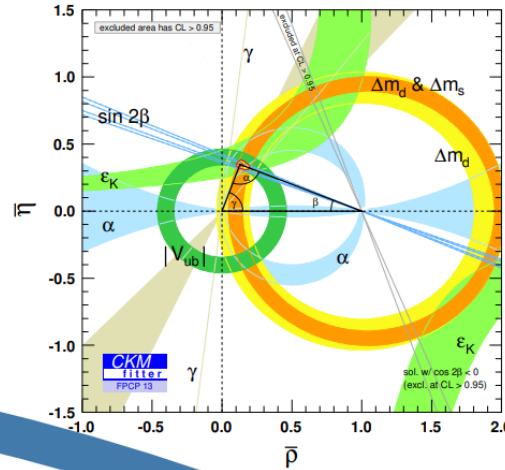
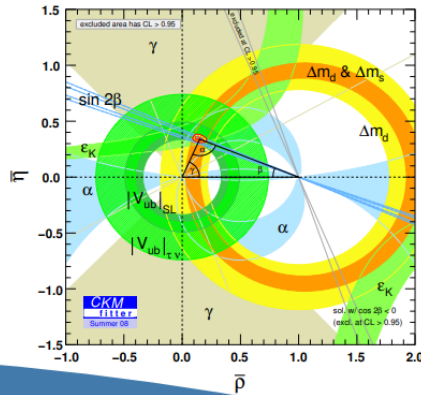
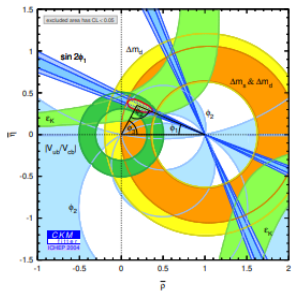


## □ Loop quantities

- $B^0$  mixing phase  $2\beta$
- $B$  mixing frequencies  $\Delta m_d$  &  $\Delta m_s$
- CPV in kaon mixing  $\epsilon_K$
- ...



# Great successes but ...



Particle Masses in MeV/c<sup>2</sup>

Leptons		
neutrinos ~ 0.0005	neutrinos ~ 0.0005	neutrinos ~ 0.0005
electron 0.5	muon 106	tau 1777
Quarks		
up 2	charm 1275	top 172000
down 5	strange 95	bottom 4185

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

Origin?



2023

# Selected highlights for today

- ❑ Significant improvements of  $\beta, \beta_s, \gamma$  by LHCb
- ❑ Belle II early measurements of  $\beta, \gamma, \alpha$
- ❑ Intriguing results in direct CP violation ( $B \rightarrow 3h, B \rightarrow K\pi, D \rightarrow hh$ )

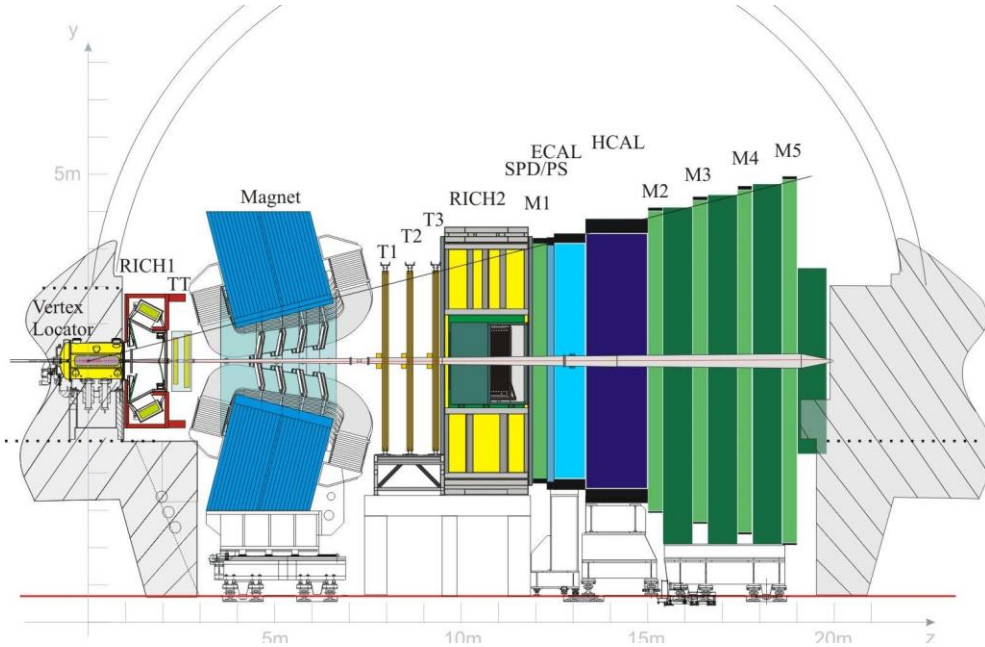
Apologize for the biased selection of topics due to limited time.

For a complete picture, see LHCb and Belle II talks in parallel sessions

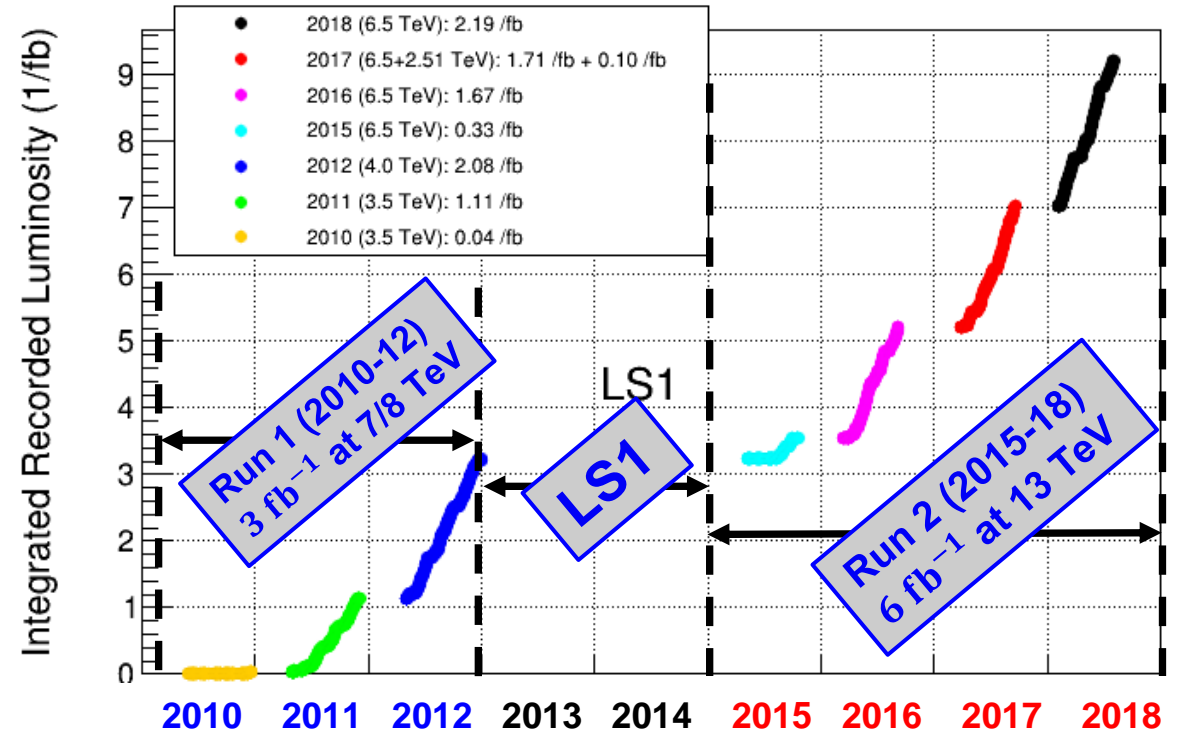
- [Charmless b-hadron decays at LHCb](#), Rongrong Song, 07/17
- [Measurements of the CKM angle gamma at LHCb](#), Fidan Suljik, 07/18
- [Mixing and CPV in charm decays at LHCb](#), Tom Hadavizadeh, 07/18
- [Recent Belle II results on time-dependent CP violation and charm physics](#), Michele Veronesi, 07/18
- [Recent Belle II results on hadronic B decays](#), Xiaodong Shi, 07/18



# LHCb experiment

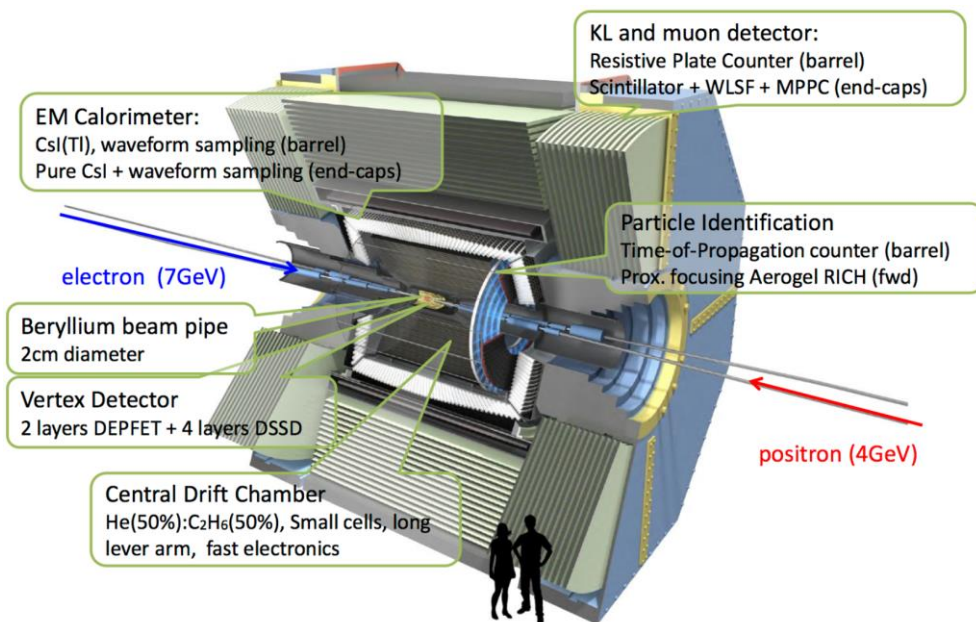


- Flavour physics experiment at LHC
- Unique strength to study all  $b$  and  $c$  hadron species, particularly  $B_s^0$
- $9 \text{ fb}^{-1}$  @ 7, 8, 13 TeV



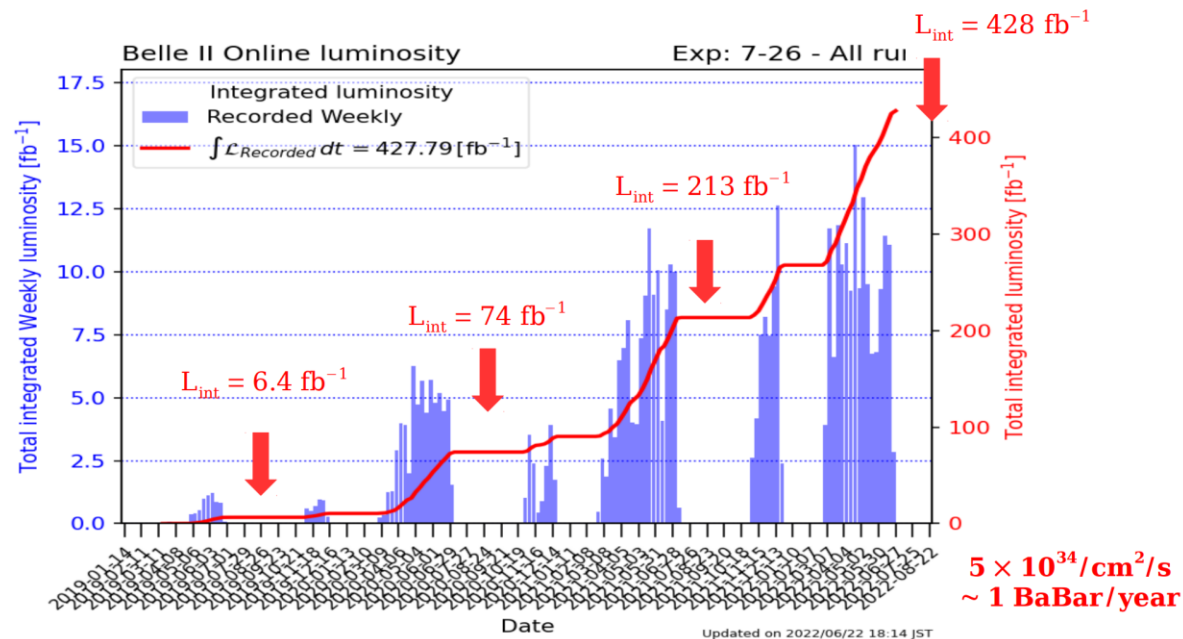
Results shown today based on full Run1 and Run2 data samples

# Belle II experiment



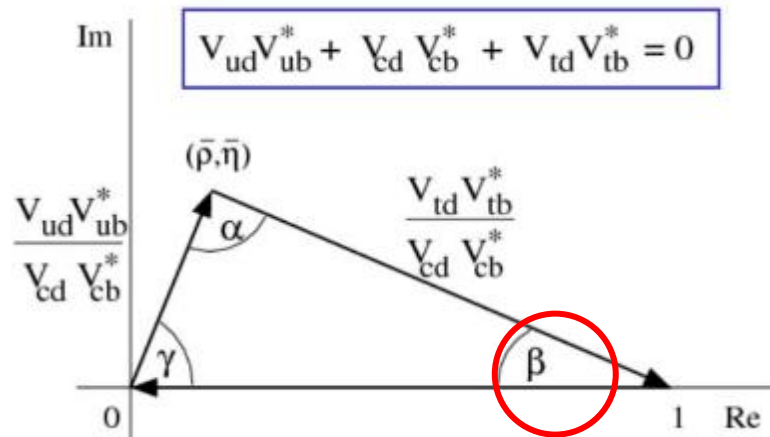
- SuperB factory at SuperKEKB
- Unique strength to study final states with neutrinos and neutral particles
- $362 \text{ fb}^{-1}$  @  $\Upsilon(4S)$  for study of  $B^0, B^\pm$

arXiv:1011.0352

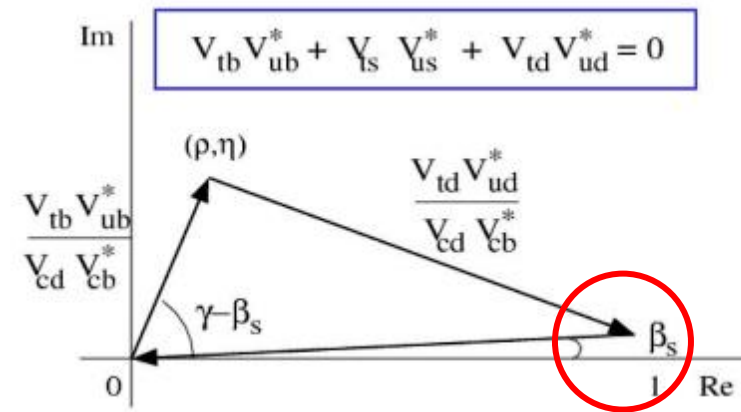


**Results shown today mainly based on data taken before 2022**

# Time-dependent CP violation in beauty



$$\phi_d = 2\beta^{\text{eff}}$$

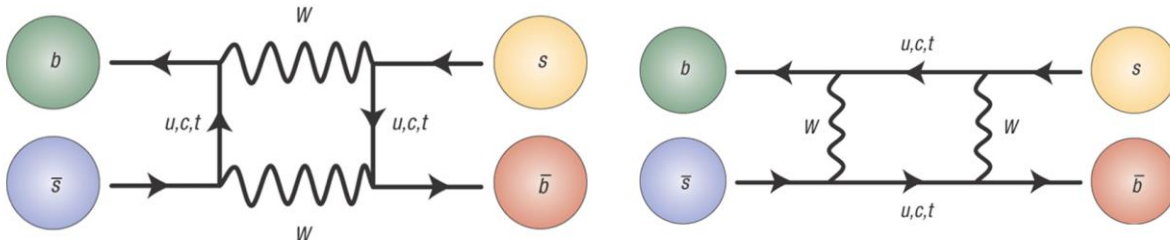


$$\phi_s = -2\beta_s^{\text{eff}}$$

# Neutral $B$ mixing and CPV

□ Neutral  $B$  mesons:  $B^0 = (\bar{b}d)$     $\bar{B}^0 = (b\bar{d})$     $B_s^0 = (\bar{b}s)$     $\bar{B}_s^0 = (b\bar{s})$

□  $B_q^0 - \bar{B}_q^0$  ( $q = d, s$ ) oscillation

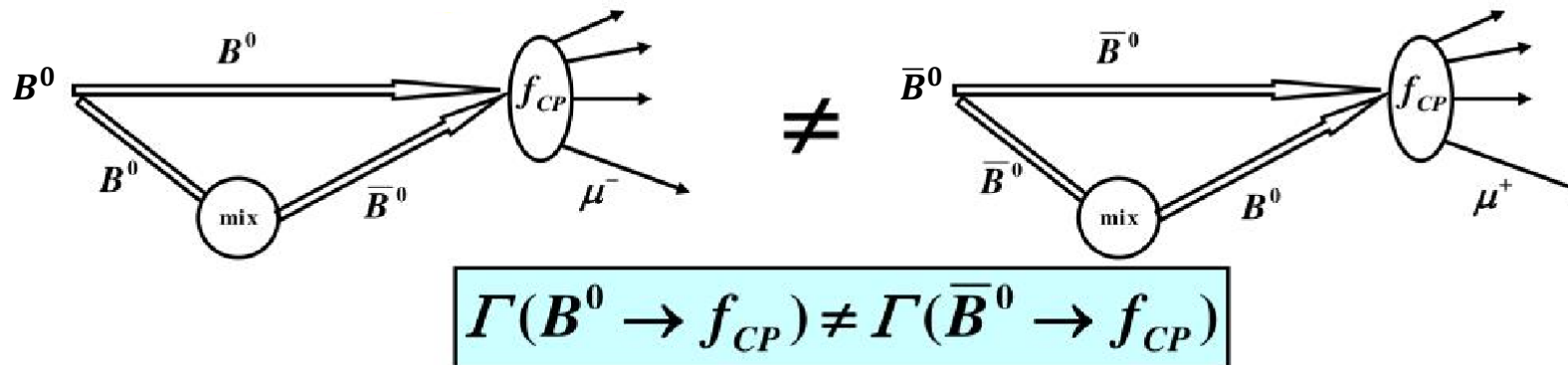


$$B_L = p|B_q\rangle + q|\bar{B}_q\rangle$$

$$B_H = p|B_q\rangle - q|\bar{B}_q\rangle$$

$$\Delta m_q = m_H - m_L, \Delta \Gamma_q = \Gamma_L - \Gamma_H$$

□ CPV in interference of  $B_q^0$  decay to CP eigenstate with and w/o mixing





# Measuring time-dependent (TD) CPV

$$A_{CP}(t) = \frac{\Gamma(\bar{B}_q^0(t) \rightarrow f_{CP}) - \Gamma(B_q^0(t) \rightarrow f_{CP})}{\Gamma(\bar{B}_q^0(t) \rightarrow f_{CP}) + \Gamma(B_q^0(t) \rightarrow f_{CP})} = \frac{-C_f \cos(\Delta m_q t) + S_f \sin(\Delta m_q t)}{\cosh \frac{\Delta \Gamma_q t}{2} - D_f \sinh \frac{\Delta \Gamma t}{2}}$$

$$\lambda_f \equiv \frac{q}{p} \frac{\bar{A}_f}{A_f} = \eta_f \frac{q}{p} \frac{\bar{A}_{\bar{f}}}{A_f}, \quad C_f = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2}, \quad S_f = \frac{2\Im \lambda_f}{1 + |\lambda_f|^2}, \quad D_f = \frac{2\Re \lambda_f}{1 + |\lambda_f|^2}$$

$S_f \neq 0$ : mixing induced CPV

$\eta_f$ : CP eigen-value, affecting sign of  $S_f$

$C_f \neq 0$ : direct CPV in decay

## Requirements on experiments

- Identify the initial flavour  $B$  or  $\bar{B}$
- Reconstruct the proper decay time  $t$
- Understand experimental dilutions on  $S_f$  and  $C_f$

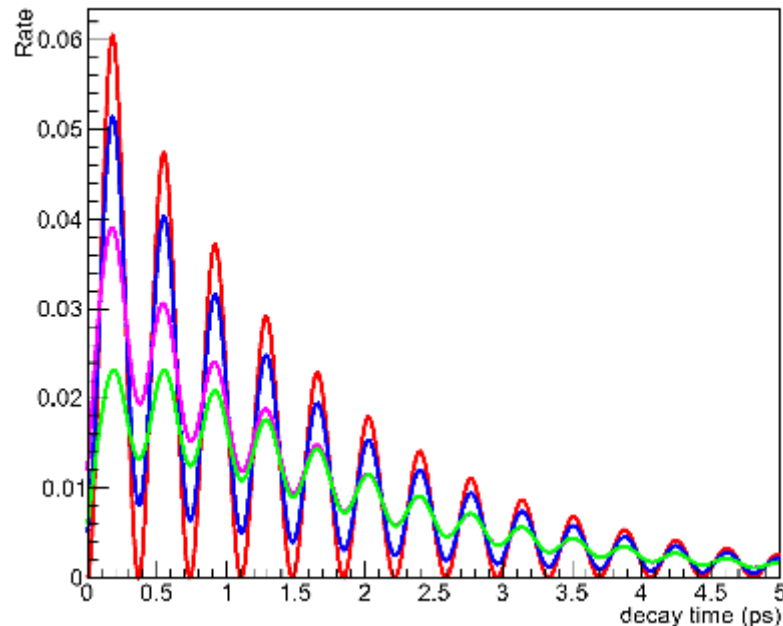
# Experimental effects

$$\Delta m_s = 17.7 \text{ ps}^{-1}$$

$$\sigma_t = 50 \text{ fs}$$

$$\omega = 0.2$$

$$\epsilon(t) = 1/(1 + \exp(-2t))$$



## □ Time resolution $\sigma_t$

$$S \rightarrow e^{-\frac{(\Delta m \sigma_t)^2}{2}} S = D_{\text{time}} S$$

$$D_{\text{time}} \sim 0.7 \text{ for } \Delta m_s = 17.7 \text{ ps}^{-1} \text{ with } \sigma_t = 50 \text{ fs}$$
$$\sim 0.7 \text{ for } \Delta m_d = 0.5 \text{ ps}^{-1} \text{ with } \sigma_t = 1.5 \text{ ps}$$

## □ Wrong tag probability $\omega$

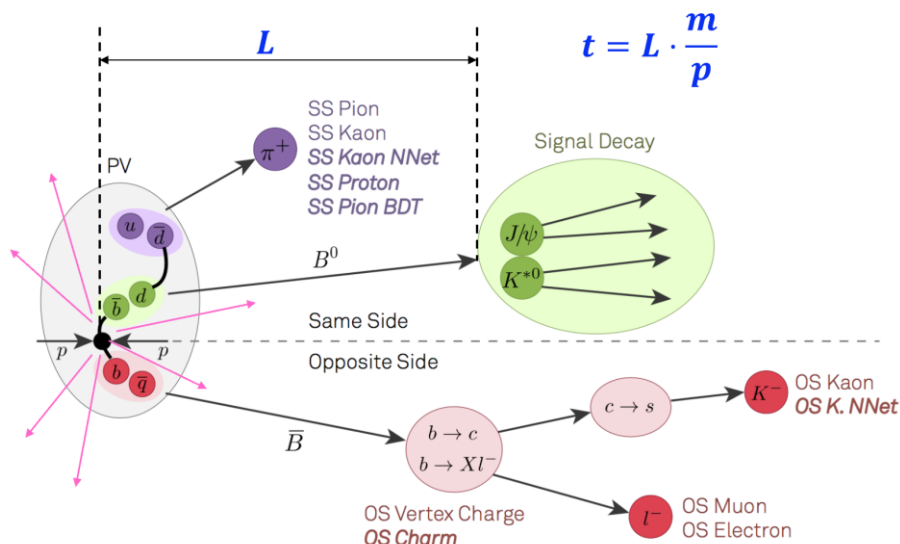
$$S \rightarrow (1 - 2\omega) S$$

## □ Decay-time dependent efficiency $\epsilon(t)$

$$P(t) \rightarrow \epsilon(t) P(t)$$

Obtain info on  $\sigma_t$ ,  $\omega$  and  $\epsilon(t)$  from data using control channels

# LHCb method for TD study



- Flavour tagging: info from other  $B$  & fragmentation particles

$$\epsilon_{\text{tag}}(1 - 2\omega)^2 \sim 5\%$$

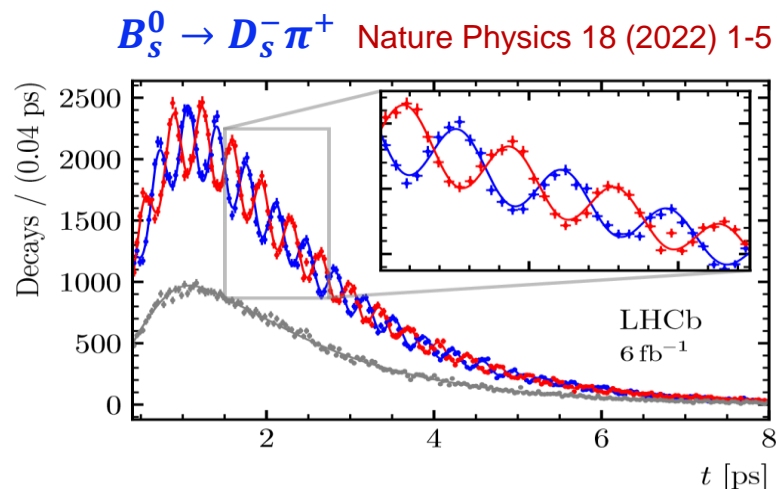
- Large boost from  $pp$  collision

$$\beta\gamma \sim 10, L \sim 1 \text{ cm}$$

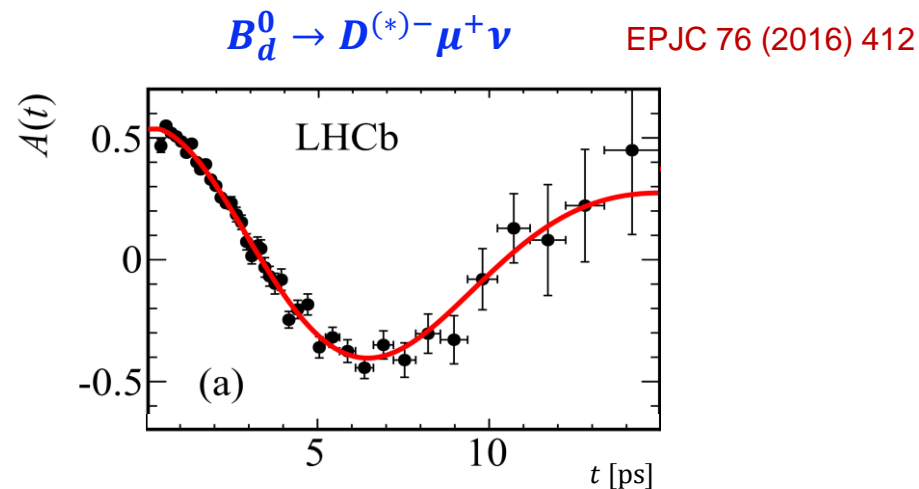
- Silicon vertex system

$$\sigma_t \sim 45 \text{ fs}$$

Int. J. Mod. Phys. A30 (2015) 1530022

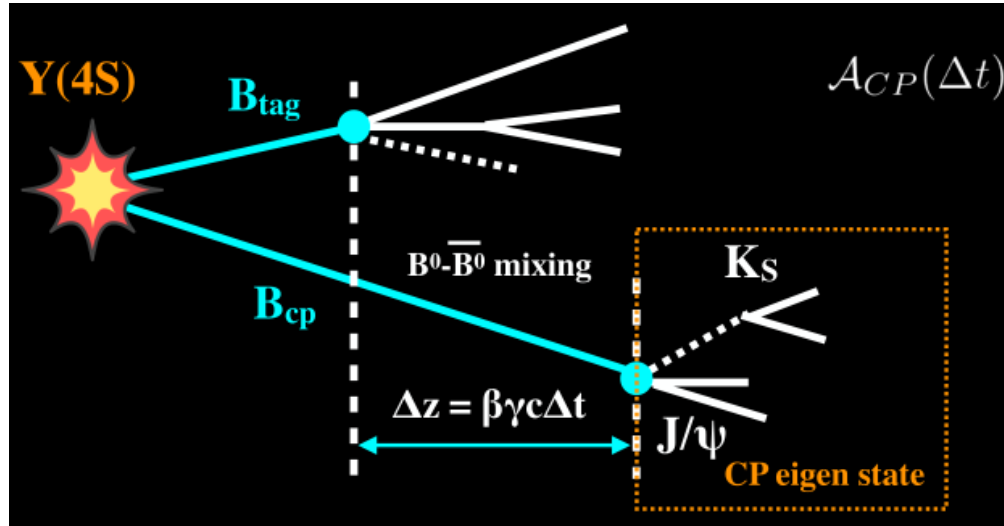


$$\Delta m_s = 17.7656 \pm 0.0057(\text{comb}) \text{ ps}^{-1}$$



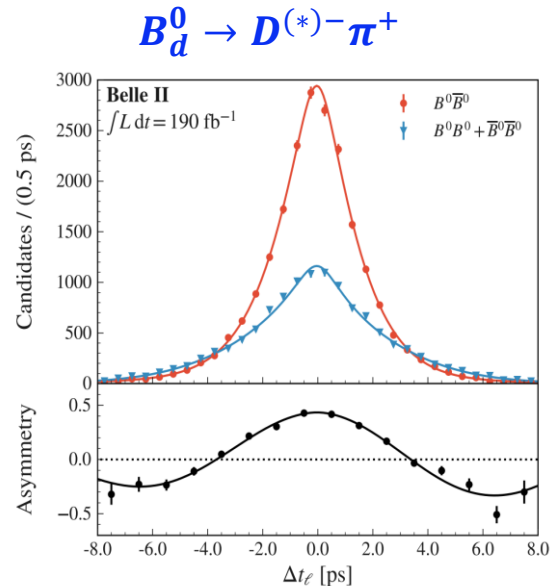
$$\Delta m_d = 0.5050 \pm 0.0021(\text{stat}) \pm 0.0010(\text{syst}) \text{ ps}^{-1}$$

# Belle II method for TD study



- Flavour tagging: info from other  $B$   
 $\epsilon_{\text{tag}}(1 - 2\omega)^2 \sim 30\%$
- Asymmetric  $e^+e^-$  collision  
 $\beta\gamma = 0.28, \Delta z \sim 200 \mu\text{m}$
- Silicon vertex detector  
 $\sigma_t \sim 1.5 \text{ ps}$

arXiv: 1808.10567



PRD 107 (2023) L091102

$$\Delta m_d = 0.516 \pm 0.008 \pm 0.005 \text{ ps}^{-1}$$

$$\tau_{B^0} = 1.499 \pm 0.013 \pm 0.005 \text{ ps}$$

Belle:  $\Delta m_d = 0.509 \pm 0.004 \pm 0.005 \text{ ps}^{-1}$

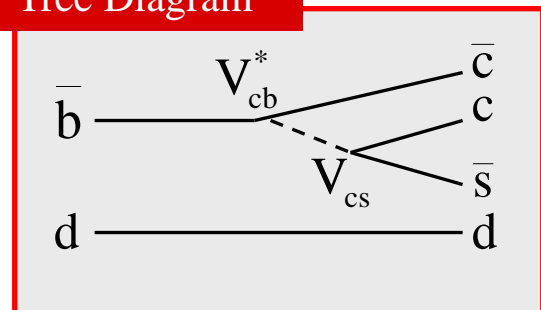


# $B^0$ mixing phase $\phi_d = 2\beta^{\text{eff}}$

B factory flagship!

Tree-dominated  $b \rightarrow c\bar{c}s$  processes (e.g.  $B^0 \rightarrow J/\psi K_S^0$ )

Tree Diagram



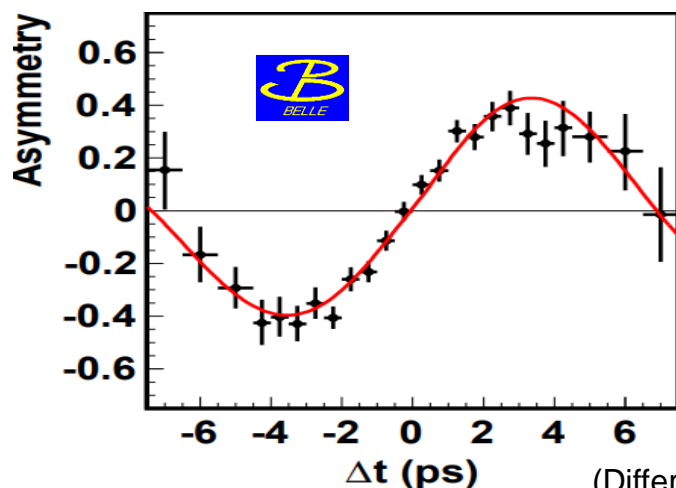
$$\lambda_f = \frac{q}{p} \frac{\bar{A}}{A} = \eta_f e^{-2i\beta}$$

$$S_f = -\eta_f \sin 2\beta$$

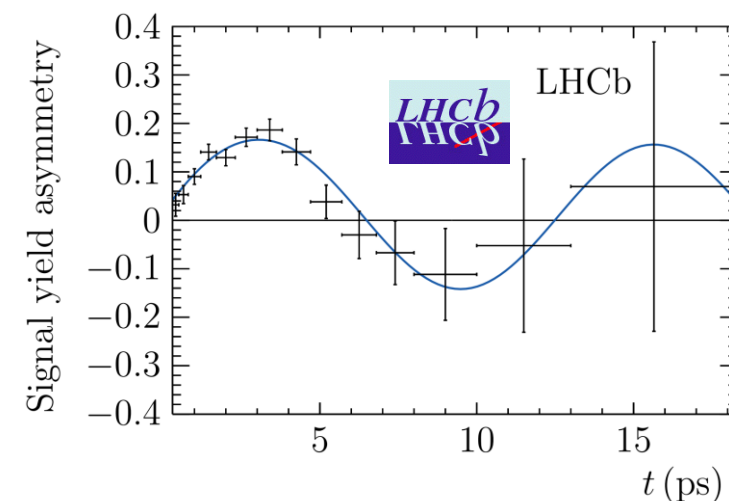
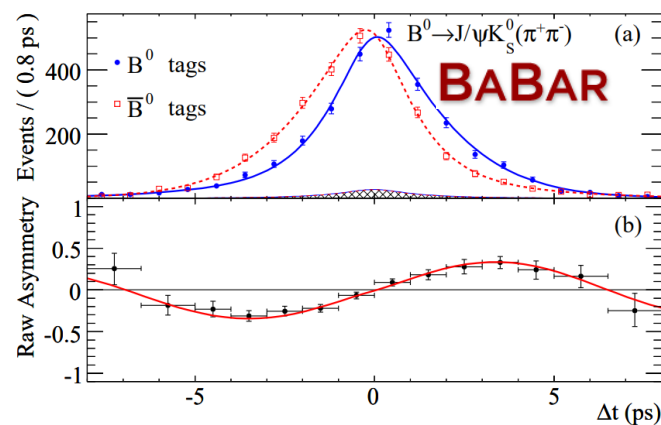
$$C_f = 0$$

- Belle:  $\sin 2\phi_1 = 0.667 \pm 0.023 \pm 0.012$   
PRL 108 (2012) 171802
- BaBar:  $\sin 2\beta = 0.687 \pm 0.028 \pm 0.012$   
PRD 79 (2009) 072009
- LHCb Run 1:  $\sin 2\beta = 0.760 \pm 0.034$   
PRL 115 (2015) 031601, JHEP 11 (2017) 170

$$A_{CP}(t) = -\eta_f \sin 2\beta \sin(\Delta m_d t)$$



(Different sign convention than LHCb)



## □ Three CP-odd $b \rightarrow c\bar{c}s$ modes

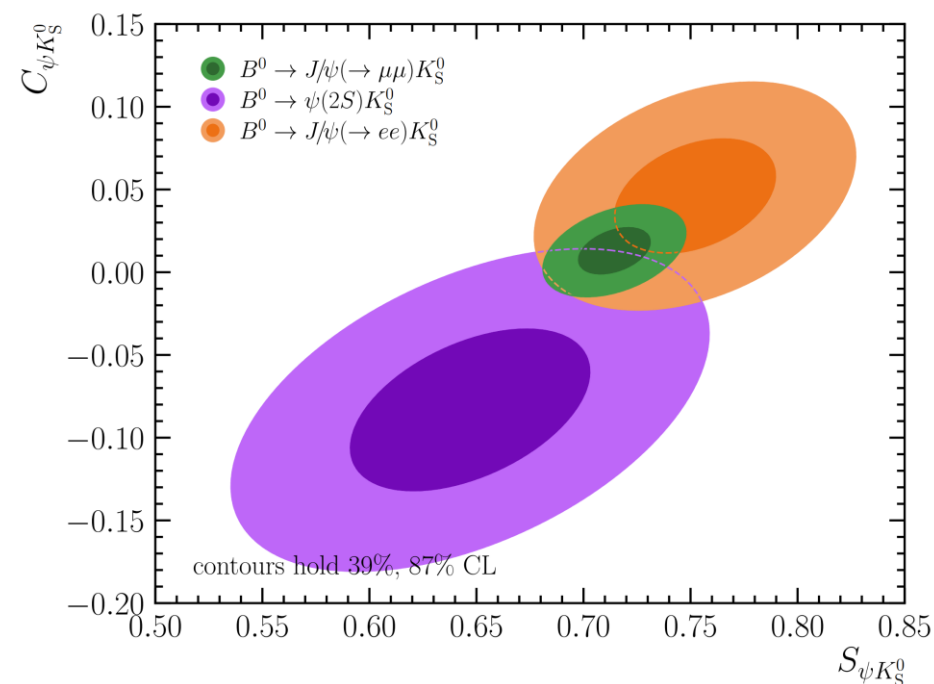
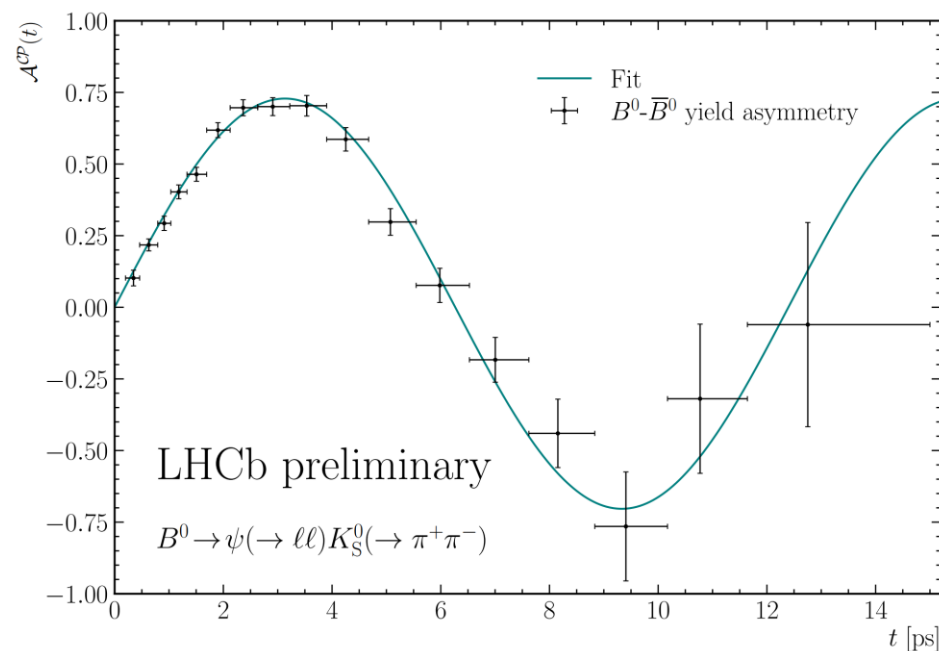
- $B^0 \rightarrow J/\psi(\rightarrow \mu\mu)K_S^0$  (~306k signals)
- $B^0 \rightarrow J/\psi(\rightarrow ee)K_S^0$  (~24k signals)
- $B^0 \rightarrow \psi(2S)K_S^0$  (~43k signals)

## □ New LHCb results

Run2  $\sin 2\beta = 0.716 \pm 0.013 \pm 0.008$   
 $C = 0.012 \pm 0.012 \pm 0.003$

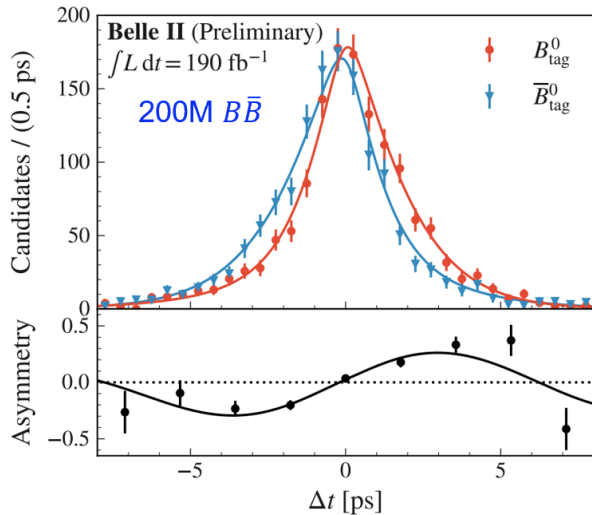
Run 1  $\sin 2\beta = 0.760 \pm 0.034$

Run1+2  $\sin 2\beta = 0.724 \pm 0.014$

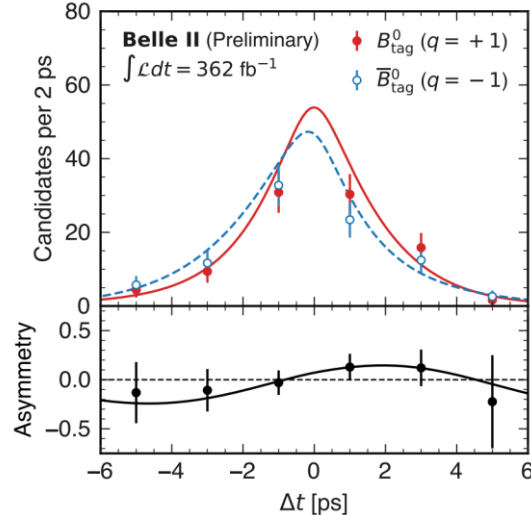


# Belle II results of $\sin 2\beta$

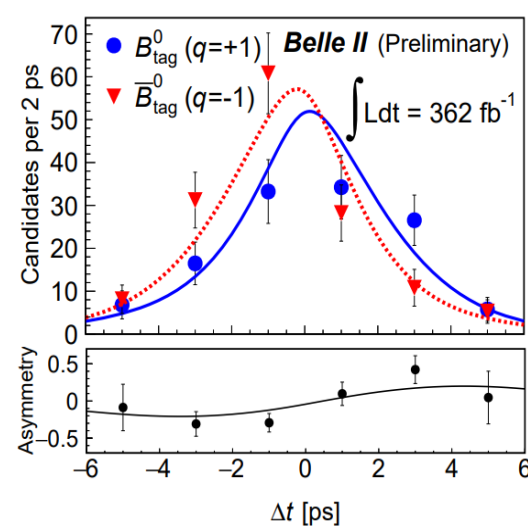
$$B^0 \rightarrow J/\psi K_S^0$$



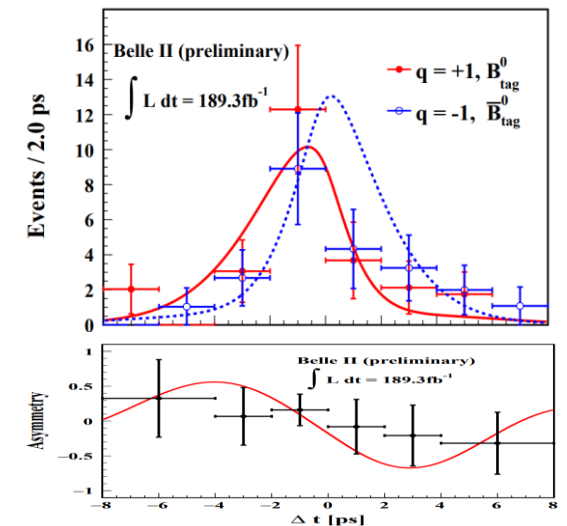
$$B^0 \rightarrow \phi K_S^0$$



$$B^0 \rightarrow K_S^0 \pi^0$$



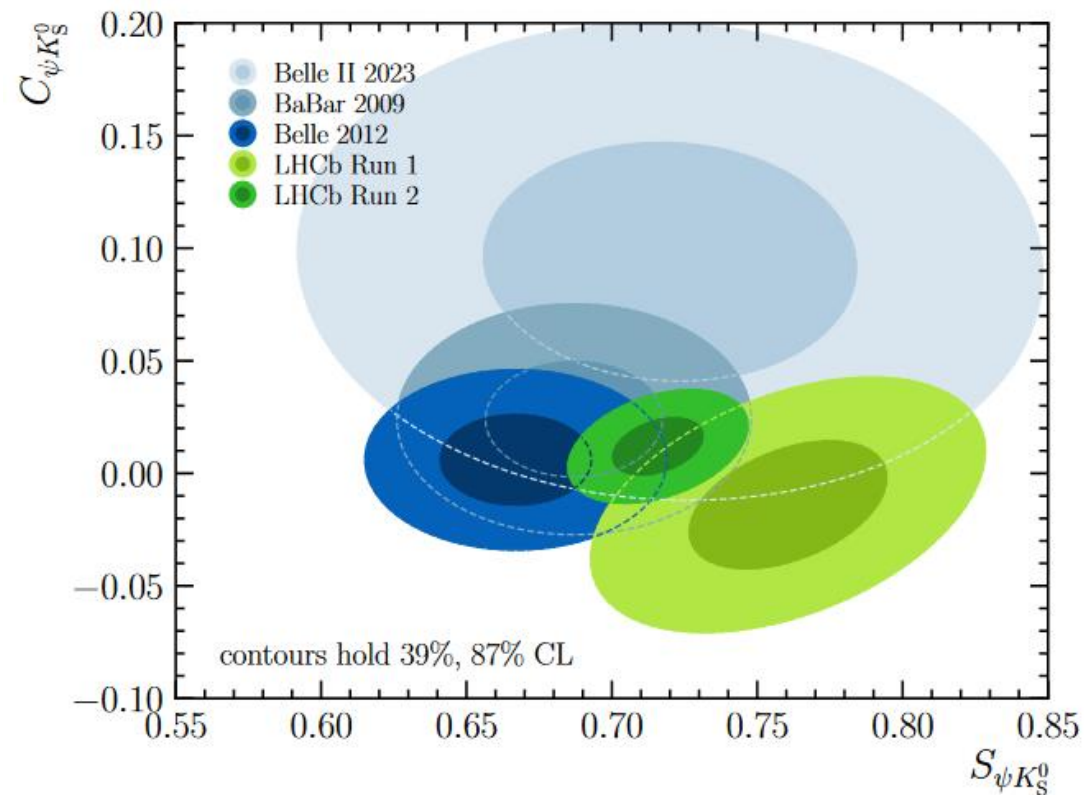
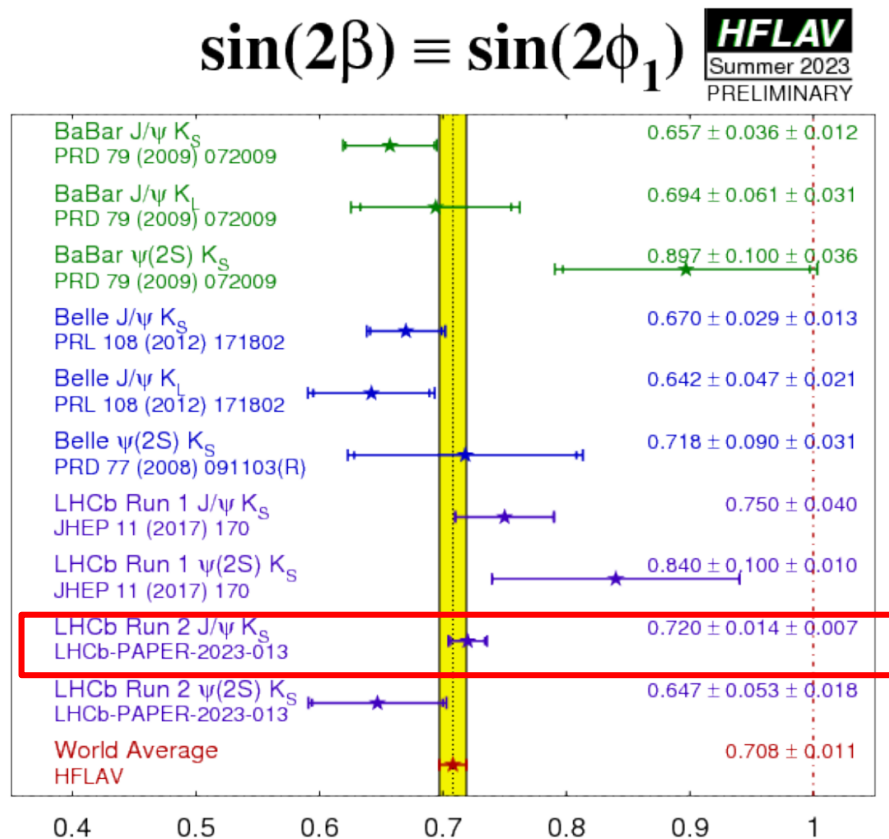
$$B^0 \rightarrow K_S^0 K_S^0 K_S^0$$



Type	Mode	$\sin 2\phi^{\text{eff}} = -\eta_f S$	$A = -C$	Ref.
$b \rightarrow c\bar{c}s$	$B^0 \rightarrow J/\psi K_S^0$	$0.720 \pm 0.062 \pm 0.016$	$0.094 \pm 0.044 \pm_{-0.017}^{+0.042}$	<a href="#">arXiv:2302.12898</a>
$b \rightarrow s\bar{s}s$	$B^0 \rightarrow \phi K_S^0$	$0.54 \pm 0.25^{+0.06}_{-0.08}$	$0.31 \pm 0.20 \pm 0.05$	<a href="#">arXiv:2307.02802</a>
$b \rightarrow s\bar{d}d$	$B^0 \rightarrow K_S^0 \pi^0$	$0.74^{+0.20}_{-0.23} \pm 0.04$	$0.04^{+0.15}_{-0.14} \pm 0.05$	<a href="#">arXiv:2305.07555</a>
$b \rightarrow s\bar{d}d$	$B^0 \rightarrow K_S^0 K_S^0 K_S^0$	$1.86^{+0.91}_{-0.46} \pm 0.09$	$-0.22^{+0.30}_{-0.27} \pm 0.04$	<a href="#">arXiv:2209.09547</a>

Belle:  $\sin 2\phi_1 = 0.667 \pm 0.023 \pm 0.012$  (772M  $B\bar{B}$ )

# World average of $\sin 2\beta$



- With Run2 data, LHCb overtakes B factories in the  $\sin 2\beta$  measurement
- New W.A. improved by 35% in precision:  $\sin 2\beta = 0.708 \pm 0.011$  (W.A.)
- Consistent with SM prediction:  $\sin 2\beta = 0.731^{+0.029}_{-0.016}$  (CKMFitter)



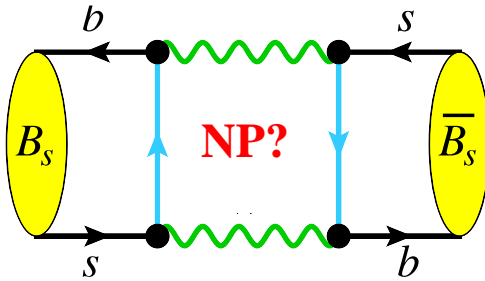
# $B_s^0$ mixing phase $\phi_s = -2\beta_s^{\text{eff}}$

LHC flagship!

- $\phi_s$ : precisely predicted in SM

$$\phi_s^{\text{SM}} \approx -2\beta_s = -0.0368_{-0.009}^{+0.006} \text{ rad (CKMFitter)}$$

- Sensitive to NP in mixing



- Golden mode:  $B_s^0 \rightarrow J/\psi\phi$

$$A_{CP}(t) \approx -\eta_f \sin \phi_s \sin(\Delta m_s t)$$

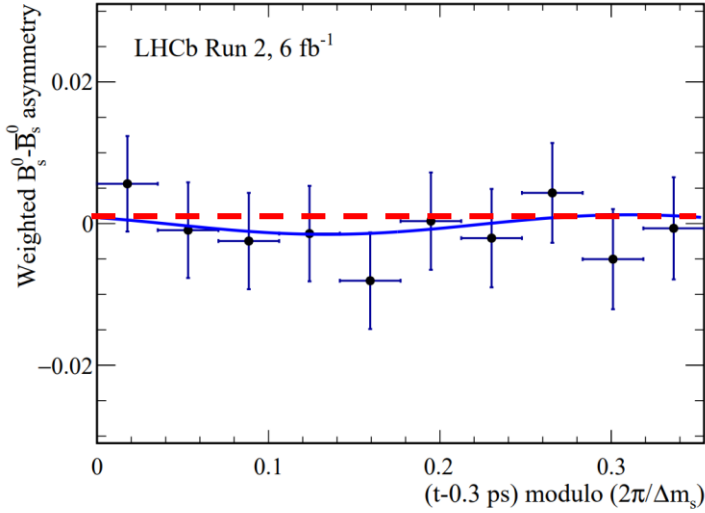
Angular analysis to separate CP even ( $\eta_f = 1$ ) and odd ( $\eta_f = -1$ ) states

- Major players: LHCb, ATLAS, CMS

Collab.	$\phi_s$ (rad)
LHCb early Run2 (all $b \rightarrow c\bar{c}s$ )	$-0.042 \pm 0.025$
LHCb early Run 2 ( $B_s^0 \rightarrow J/\psi\phi$ )	$-0.081 \pm 0.032$
ATLAS ( $B_s^0 \rightarrow J/\psi\phi$ )	$-0.087 \pm 0.041$
CMS ( $B_s^0 \rightarrow J/\psi\phi$ )	$-0.021 \pm 0.045$
HFLAV	$-0.049 \pm 0.019$

LHCb, EPJC 79 (2019) 706  
 ATLAS, EPJC 81 (2021) 342  
 CMS, PLB 816 (2021) 136188

## No sign of CP violation



## No sign of polarization dependence

$$\phi_s^0 \text{ [rad]} = -0.034 \pm 0.023$$

$$\phi_s^{\parallel} - \phi_s^0 \text{ [rad]} = -0.002 \pm 0.021$$

$$\phi_s^{\perp} - \phi_s^0 \text{ [rad]} = -0.001^{+0.020}_{-0.021}$$

$$\phi_s^S - \phi_s^0 \text{ [rad]} = 0.022^{+0.027}_{-0.026}$$

$$|\lambda^0| = 0.969^{+0.025}_{-0.024}$$

$$|\lambda^{\parallel}/\lambda^0| = 0.982^{+0.055}_{-0.052}$$

$$|\lambda^{\perp}/\lambda^0| = 1.107^{+0.082}_{-0.076}$$

$$|\lambda^S/\lambda^0| = 1.121^{+0.084}_{-0.078}$$

## New LHCb results

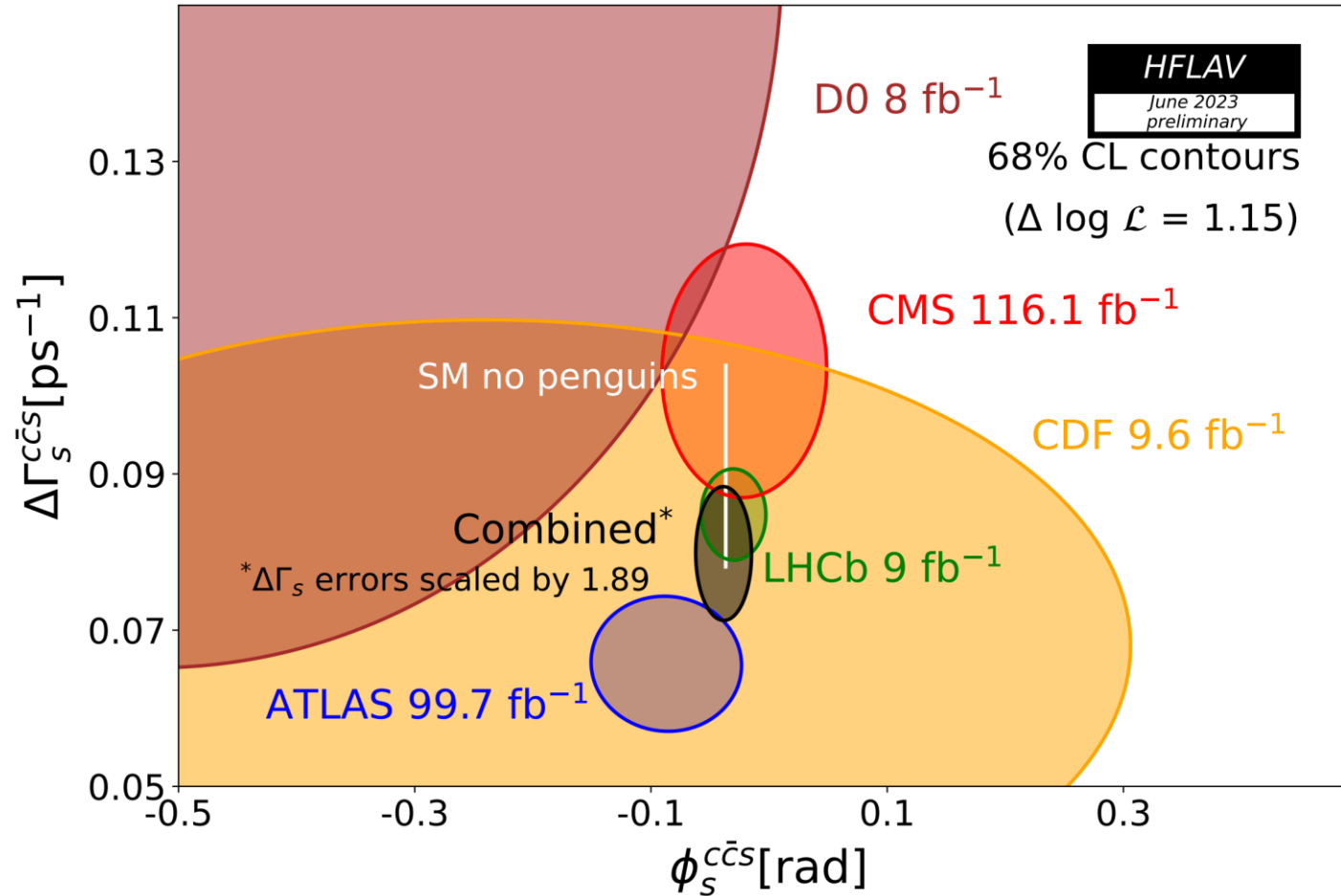
Parameter	Values
$\phi_s$ [rad]	$-0.039 \pm 0.022 \pm 0.006$
$ \lambda $	$1.001 \pm 0.011 \pm 0.005$
$\Gamma_s - \Gamma_d$ [ps <sup>-1</sup> ]	$-0.0056^{+0.0013}_{-0.0015} \pm 0.0014$
$\Delta\Gamma_s$ [ps <sup>-1</sup> ]	$0.0845 \pm 0.0044 \pm 0.0024$
$\Delta m_s$ [ps <sup>-1</sup> ]	$17.743 \pm 0.033 \pm 0.009$
$ A_{\perp} ^2$	$0.2463 \pm 0.0023 \pm 0.0024$
$ A_0 ^2$	$0.5179 \pm 0.0017 \pm 0.0032$
$\delta_{\perp} - \delta_0$ [rad]	$2.903^{+0.075}_{-0.074} \pm 0.048$
$\delta_{\parallel} - \delta_0$ [rad]	$3.146 \pm 0.060 \pm 0.052$

Run2  $\phi_s^{J/\psi\phi} = -0.039 \pm 0.022 \pm 0.006$  rad

Run1+2  $\phi_s^{J/\psi\phi} = -0.044 \pm 0.020$  rad

Run1+2  $\phi_s^{c\bar{c}s} = -0.038 \pm 0.018$  rad

# World average of $\phi_s$ vs $\Delta\Gamma_s$



Tention in  $\Delta\Gamma_s$  remains

LHCb

$$\Delta\Gamma_s = 0.0845 \pm 0.0044 \pm 0.0024 \text{ ps}^{-1}$$

ATLAS

$$\Delta\Gamma_s = 0.0657 \pm 0.0043 \pm 0.0037 \text{ ps}^{-1}$$

CMS

$$\Delta\Gamma_s = 0.1032 \pm 0.0095 \pm 0.0048 \text{ ps}^{-1}$$

W.A. of  $\phi_s$  improved by 15%:  $\phi_s^{ccs} = -0.039 \pm 0.016 \text{ rad (W.A.)}$

Consistent with SM:  $\phi_s^{\text{SM}} = -0.0368^{+0.006}_{-0.009} \text{ rad (CKMFitter)}$

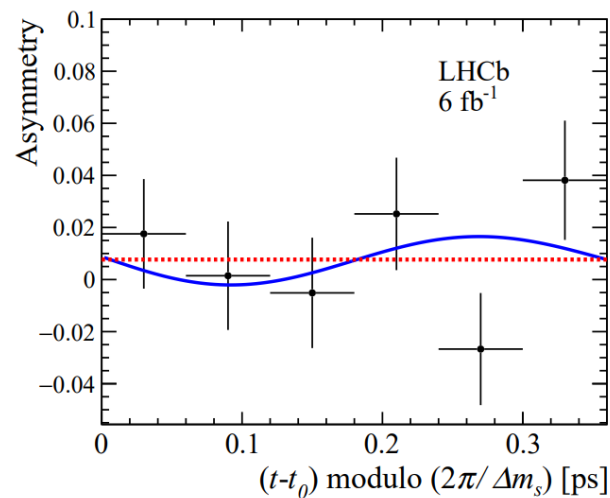
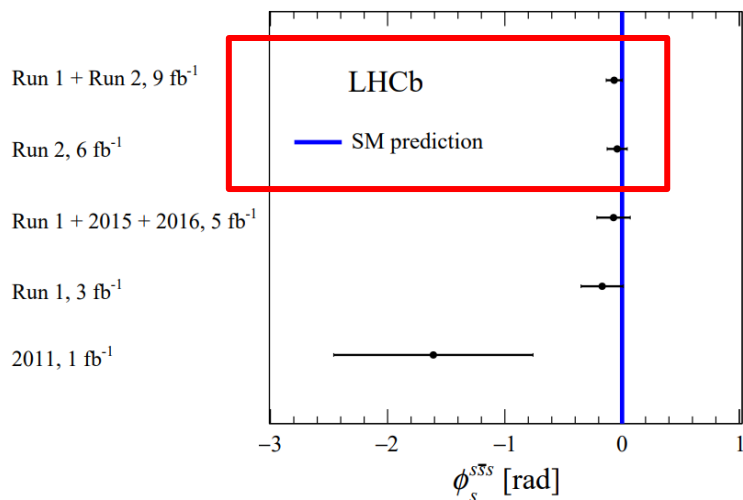
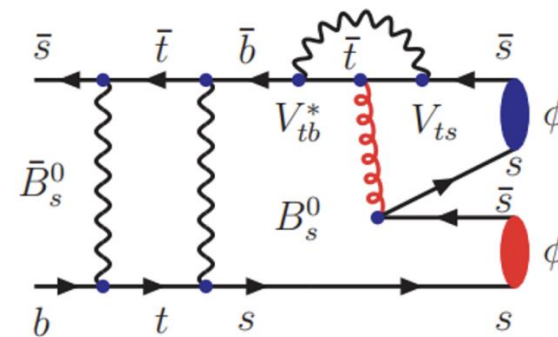
# CPV in penguin-dominated $B_s^0 \rightarrow \phi\phi$

- Tiny CPV expected in SM:  $\phi_s^{s\bar{s}s} = 0.00 \pm 0.02$  rad
- Sensitive to NP in mixing and penguin diagrams
- New LHCb results

Run2  $\phi_s^{s\bar{s}s} = -0.042 \pm 0.075 \pm 0.009$  rad

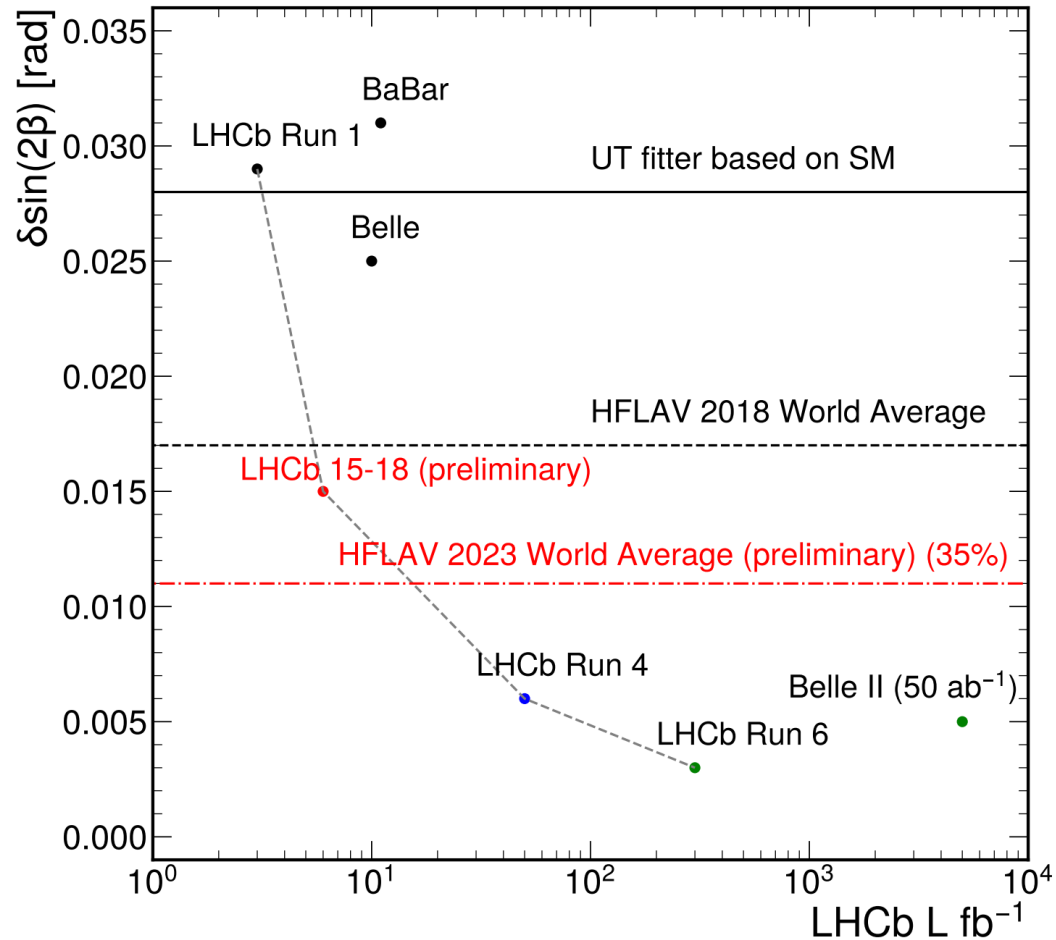
Run1+2  $\phi_s^{s\bar{s}s} = -0.074 \pm 0.069$  rad

arXiv:2304.06198

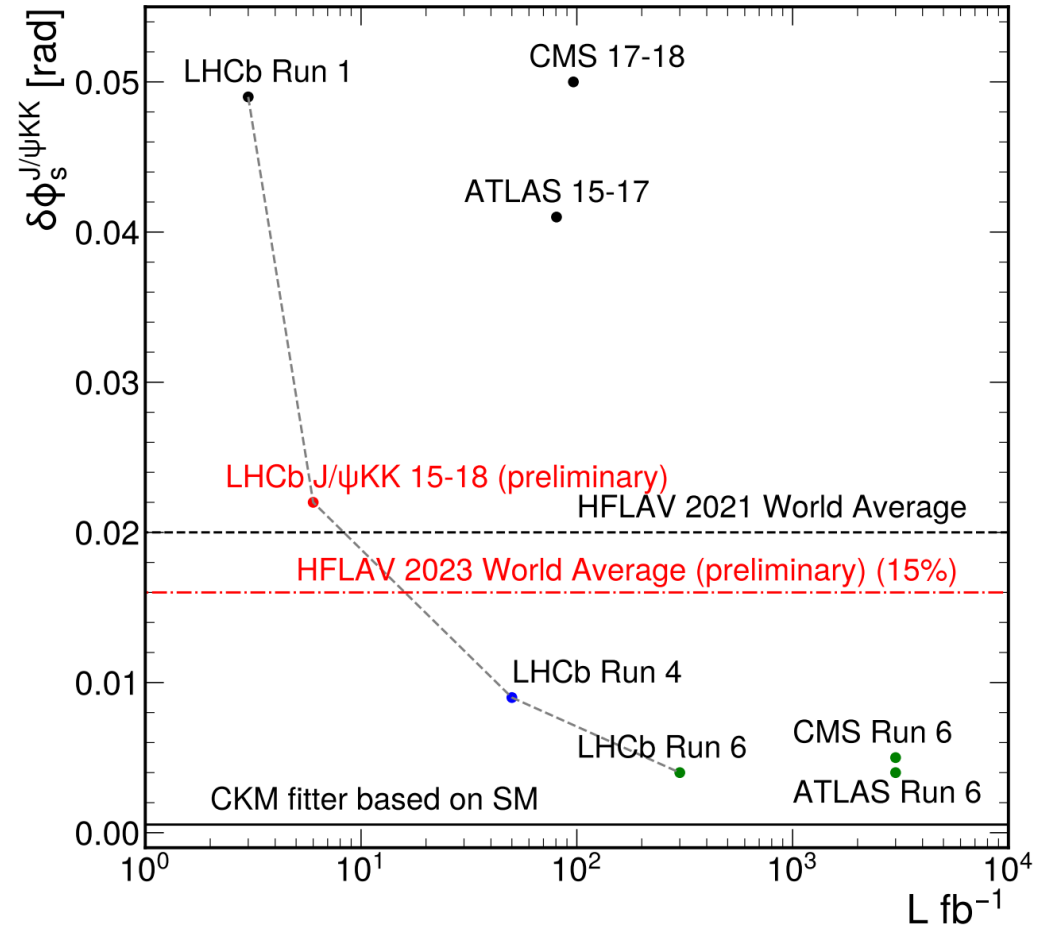


No sign of CP violation & result consistent with SM

# Projections for $\sin 2\beta$ and $\phi_s$

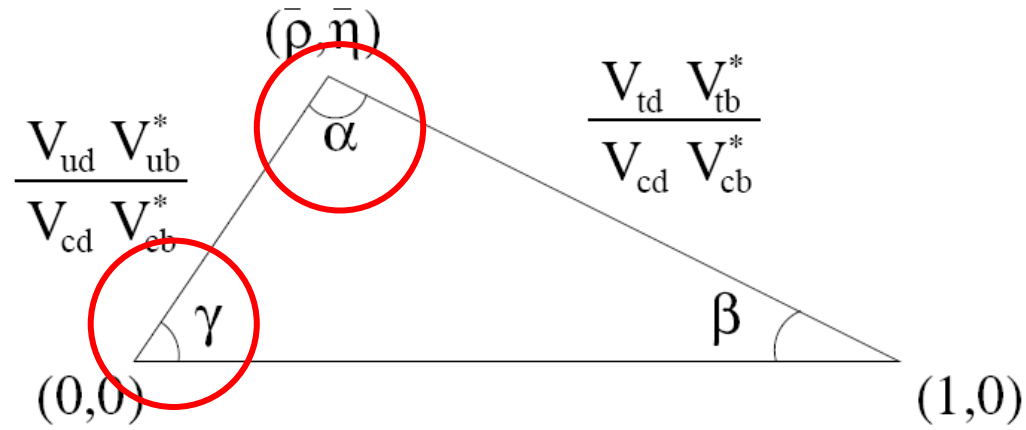


$\sin 2\beta$ :  $\sigma^{\text{exp}}$  already better than  $\sigma^{\text{SM}}$



$\phi_s$ :  $\sigma^{\text{exp}} \gg \sigma^{\text{SM}}$ , with large room for improvement

## CKM angles $\gamma$ and $\alpha$





# CKM angle $\gamma$

LHCb dominating!

- Access  $\gamma$  from interference of  $b \rightarrow u$  &  $b \rightarrow c$  transitions in  $B^\pm \rightarrow Dh^\pm$  decays

$$\Gamma(B^\pm \rightarrow Dh^\pm) \propto |r_D e^{-i\delta_D} + r_B e^{i(\delta_B \pm \gamma)}|^2$$

$\gamma, \delta_B, r_B$ : to be measured

$\delta_D, r_D$ : external inputs

- Each B factory:  $\sigma_\gamma \approx 15^\circ$

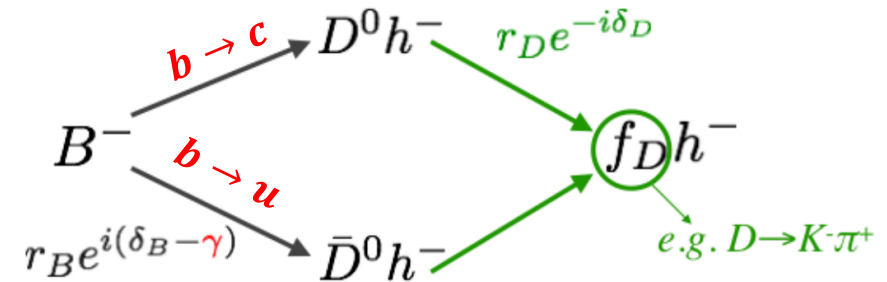
BaBar:  $\gamma = (70 \pm 18)^\circ$  PRD 87 (2015) 052 015

BELLE:  $\gamma = (73_{-15}^{+13})^\circ$  arXiv: 1301.2033

- Previous LHCb combination :  $\sigma_\gamma \approx 4^\circ$

LHCb:  $\gamma = (65.4_{-4.2}^{+3.8})^\circ$  JHEP 12 (2021) 141

Recent updated to include several new  $\gamma$  measurements



## ■ B decay modes

- $B^+ \rightarrow Dh^+, B^+ \rightarrow D^* h^+, B^+ \rightarrow DK^{*+}, B^+ \rightarrow Dh^+ \pi^+ \pi^-$
- $B^0 \rightarrow DK^{*0}, B^0 \rightarrow D^\mp \pi^\pm$
- $B_s^+ \rightarrow D_s^\mp K^\pm, B_s^+ \rightarrow D_s^\mp K^\pm \pi^+ \pi^-$

## ■ $D^0$ decay modes

- 2-body:  $D^0 \rightarrow K^+ \pi^-, D^0 \rightarrow h^+ h^-$
- 3-body:  $D^0 \rightarrow K_S^0 h^+ h'^-, D^0 \rightarrow h^+ h'^- \pi^0$
- 4-body:  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+, D^0 \rightarrow K^- K^+ \pi^- \pi^+, D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0, D^0 \rightarrow \pi^- \pi^+ \pi^- \pi^+$

# New $\gamma$ results with $B \rightarrow Dh$ decays

□  $\gamma$  in  $B^\pm \rightarrow D[K^\mp \pi^\pm \pi^\pm \pi^\mp] h^\pm$

arXiv:2209.03692

- Decay rates measured in bins of  $K3\pi$  phase space
- Per bin strong-phase differences and coherences factor from CLEO and BESIII

$$\gamma = (54.8^{+3.8}_{-5.8} {}^{+0.6}_{-0.6} {}^{+6.7}_{-4.3})^\circ$$

Uncertainty of external inputs dominates!

□  $\gamma$  in  $B^\pm \rightarrow D[h^\pm h'^\mp \pi^0] h^\pm$

JHEP 07 (2022) 099

- Evidence for CPV in  $B^\pm \rightarrow [\pi^\pm K^\mp \pi^0]_D K^\pm$

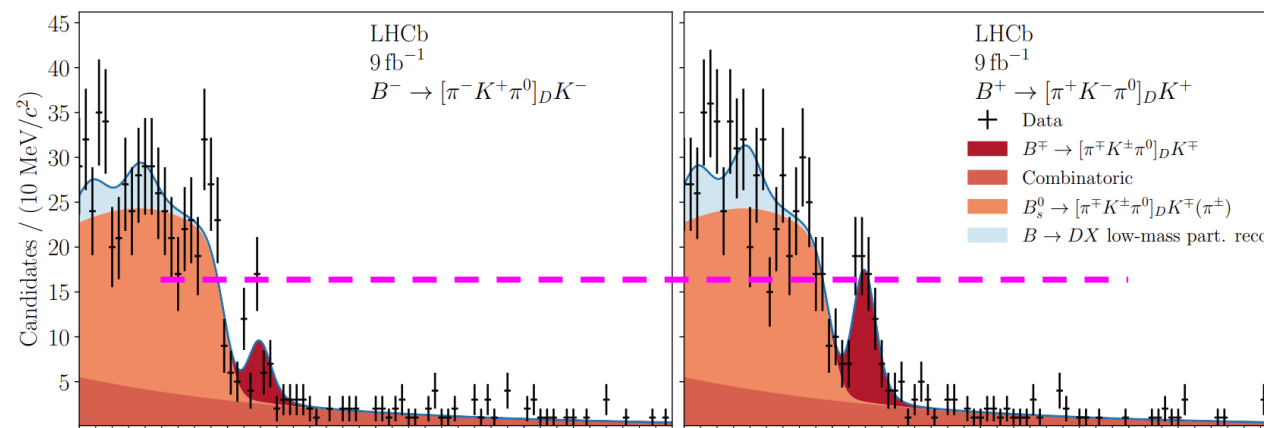
$$\gamma = (56^{+24}_{-19})^\circ$$

□  $\gamma$  in  $B^\pm \rightarrow D[K^+ K^- \pi^+ \pi^-] h^\pm$

- Currently using  $D^0$  amplitude model, expecting measurement of  $D$  parameters from BESIII

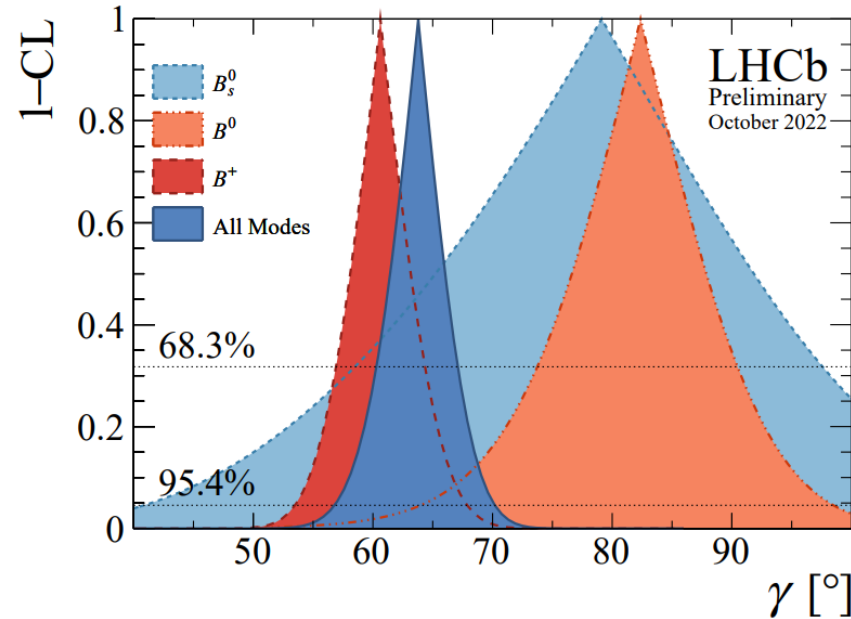
$$\gamma = (116^{+12}_{-14})^\circ$$

EPJC 83 (2023) 547

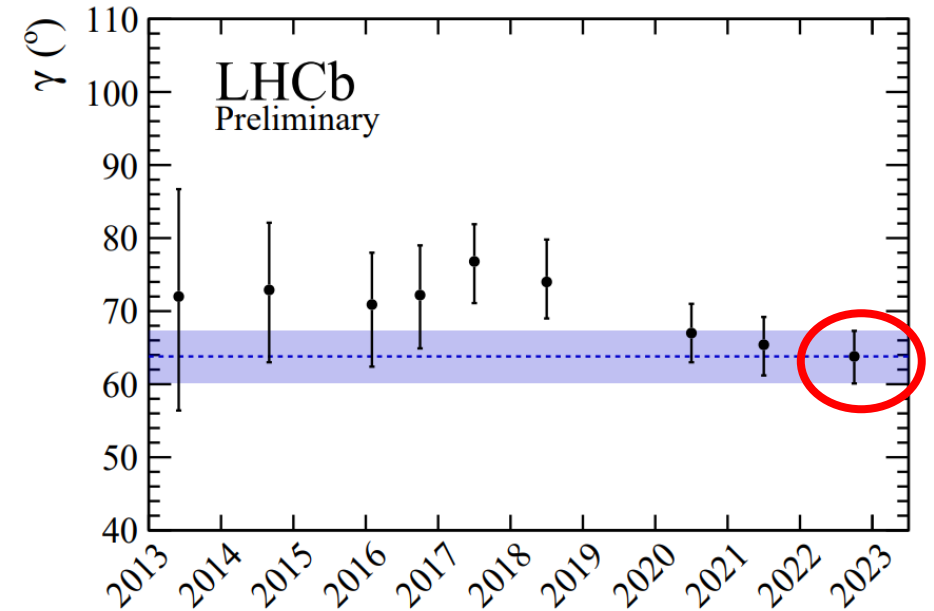


## □ New LHCb combination of many $B$ and $D$ decay modes

$B^\pm \rightarrow DK^{(*)\pm}$   
 $B^0 \rightarrow DK^{*0}$   
 $B^0 \rightarrow D^\mp \pi^\pm$   
 $B_s^0 \rightarrow D_s^\mp K^\pm (\pi\pi)$   
 $D \rightarrow K^+ \pi^-$   
 $D \rightarrow K^+ \pi^-$   
 $D \rightarrow h^+ h^- \pi^0$   
 $D \rightarrow \pi^+ \pi^- \pi^+ \pi^-$   
 $D \rightarrow K^+ \pi^- \pi^0$   
 $D \rightarrow K^\pm \pi^\mp \pi^+ \pi^-$   
 $D \rightarrow K_S^0 K^\pm \pi^\mp$   
 $D \rightarrow K_S^0 K^\pm \pi^\mp$



LHCb:  $\gamma = (63.8^{+3.5}_{-3.7})^\circ$



10% improvement

Consistent with SM prediction:  $\gamma = (65.5^{+1.1}_{-2.7})^\circ$  (CKMFitter)



# $\gamma/\phi_3$ measurements at Belle II

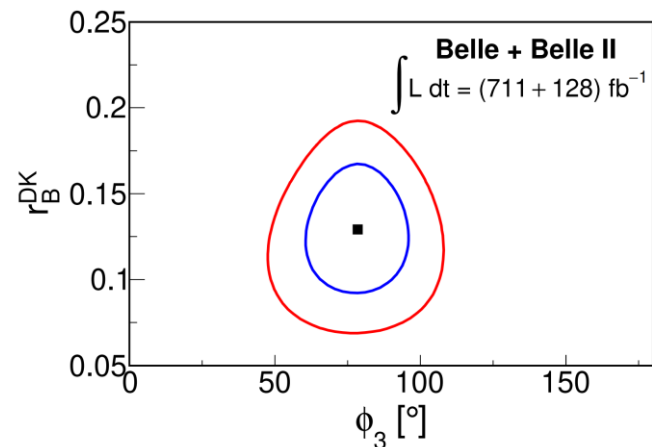
Several efforts to improve  $\gamma$  by adding Belle II early data to Belle data

- **Model-independent binned analysis of  $B^\pm \rightarrow D[K_S^0 h^+ h^-] h^\pm$**

Per bin  $D^0$  strong-phase parameter from CLEO and BESIII using

$$\gamma = \phi_3 = (78.4 \pm 11.4(\text{stat}) \pm 0.5(\text{syst}) \pm 1.0(\text{ext}))^\circ$$

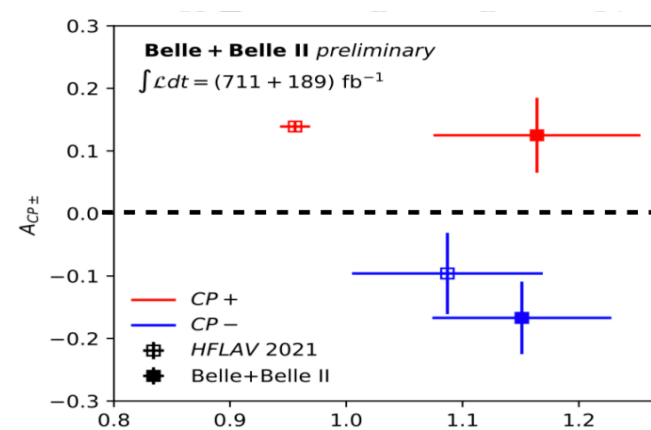
JHEP 02 (2022) 063



- **CPV and BFs in  $B \rightarrow DK$  with  $D^0 \rightarrow K^+ K^-$  and  $D^0 \rightarrow K_S^0 \pi^0$**

- CP-odd accessible only to B-factories
- Evidence of opposite  $A_{CP}$  for even and odd states

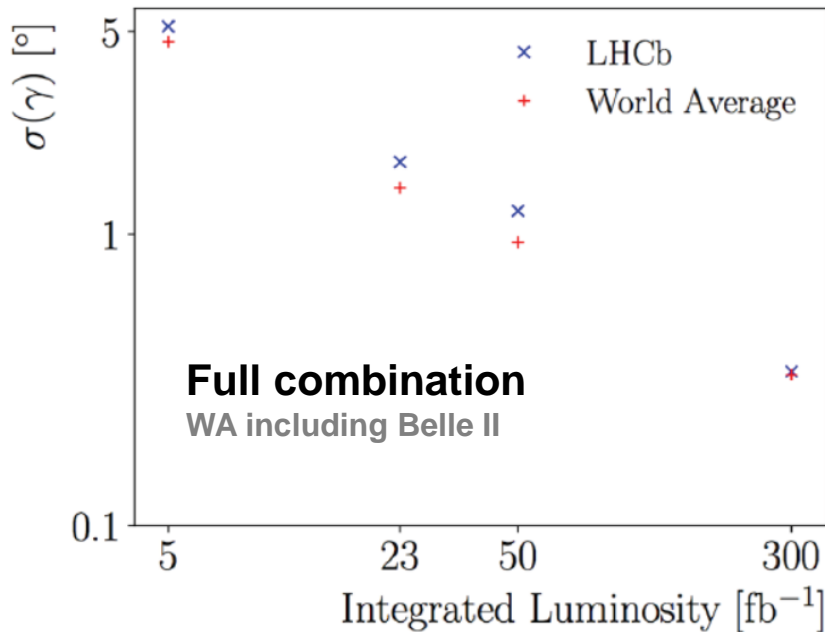
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- **CPV and BFs in  $B \rightarrow Dh$  with  $D^0 \rightarrow K_S^0 K \pi$**

arXiv:2306.02940

# Future prospect for $\gamma$



## □ Status now

- LHCb Run 2:  $\sigma_\gamma \approx 4^\circ$
- BESIII 3 fb<sup>-1</sup>  $D\bar{D}$ : error from strong phase  $\sim 1^\circ$

## □ ~2030

- LHCb upgrade I:  $\sigma_\gamma < 1^\circ$
- BESIII 20 fb<sup>-1</sup>  $D\bar{D}$ : error from strong phase  $< 0.5^\circ$

## □ ~2040

- LHCb upgrade II:  $\sigma_\gamma < 0.4^\circ$
- Need future charm factory

Data source	Integrated Lumi	year	$\gamma$ sensitivity
<b>LHCb Run1 (7, 8TeV)</b>	3 fb <sup>-1</sup>	2012	8°
<b>LHCb Run2 (13TeV)</b>	6 fb <sup>-1</sup>	2018	4°
<b>Belle II Run</b>	50 ab <sup>-1</sup>	2025	1-2°
<b>LHCb upgrade I</b>	50 fb <sup>-1</sup>	2030	<1°
<b>LHCb upgrade II</b>	200 fb <sup>-1</sup>	2040	<0.4°

# Belle II potential for $\alpha/\phi_2$

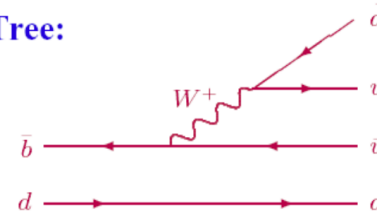
□ Access  $\alpha$  from TD-CPV in  $B^0 \rightarrow \pi\pi, \rho\rho$  decays

$$\alpha = (85.2^{+4.8}_{-4.3})^\circ \text{ (HFLAV)}$$

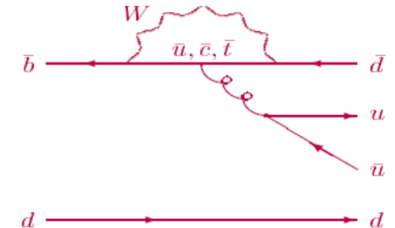
$$A_{CP}(t) = \textcolor{red}{C} \cos(\Delta m_d t) - \textcolor{red}{S} \sin(\Delta m_d t)$$

$$\textcolor{red}{S} = \sin 2\alpha + 2 r \cos \delta \sin(\alpha + \beta) \cos 2\alpha$$

Tree:



Penguin:



$$A(B^0 \rightarrow \pi^+ \pi^-) = T e^{i\gamma} + P e^{i\delta}, r = |P|/|T|$$

□ Control hadronic parameter  $r$  and  $\delta$  using BFs and CPV of all isospin-related  $B \rightarrow \pi\pi$  ( $B \rightarrow \rho\rho$ ) channels, which are all accessible at Belle II

$$\mathcal{B}(\rho^+ \rho^-) = (2.67 \pm 0.28 \pm 0.28) \times 10^{-5}, f_L = 0.956 \pm 0.035 \pm 0.033$$

[arXiv:2206.12362](#)

$$\mathcal{B}(\rho^+ \rho^0) = (2.32 \pm 0.22 \pm 0.27) \times 10^{-5}, f_L = 0.943 \pm 0.035 \pm 0.060$$

[arXiv:2208.03554](#)

$$A_{CP} = -0.069 \pm 0.068 \pm 0.060$$

$$\mathcal{B}(\pi^+ \pi^-) = (5.83 \pm 0.22 \pm 0.17) \times 10^{-6},$$

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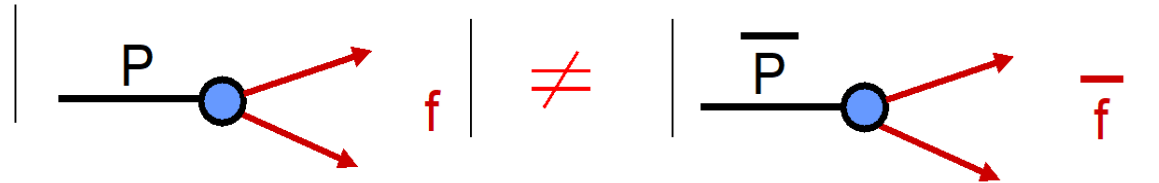
$$\mathcal{B}(\pi^+ \pi^0) = (5.10 \pm 0.29 \pm 0.32) \times 10^{-6}, A_{CP} = -0.081 \pm 0.054 \pm 0.008$$

$$\mathcal{B}(\pi^0 \pi^0) = (1.38 \pm 0.27 \pm 0.22) \times 10^{-6}, A_{CP} = 0.14 \pm 0.46 \pm 0.07$$

[PRD 107\(2023\)112009](#)



## Some results in direct CP violation



$$A_{CP} = \frac{\Gamma(P \rightarrow f) - \Gamma(\bar{P} \rightarrow \bar{f})}{\Gamma(P \rightarrow f) + \Gamma(\bar{P} \rightarrow \bar{f})} \propto \sin(\delta_2 - \delta_1) \sin(\varphi_2 - \varphi_1)$$

# CPV in charmless 3-body $B$ decay

- Large local CPV observed in  $B^\pm \rightarrow h^+ h^- \pi^\pm$  decays using Run 1 data PRD 90 (2014) 112004
- Analysis of Run 2 data reveals new findings

- Observation of inclusive  $A_{CP}$  in two modes

$$A_{CP}(K^\pm K^+ K^-) = -0.037 \pm 0.002 \pm 0.002 \pm 0.003$$

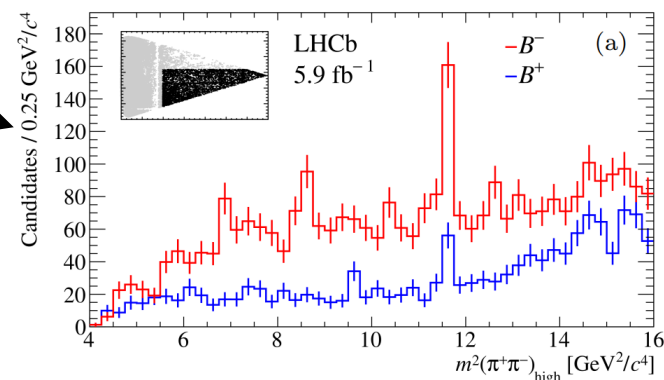
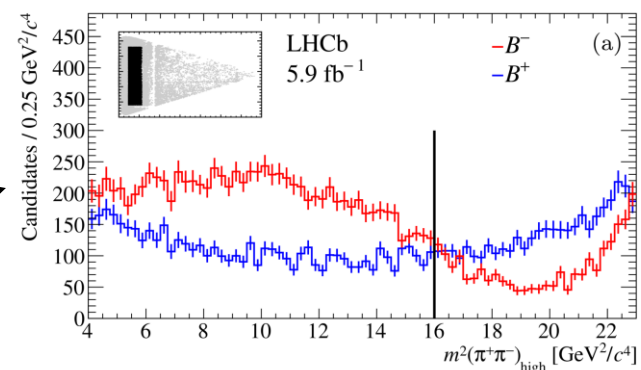
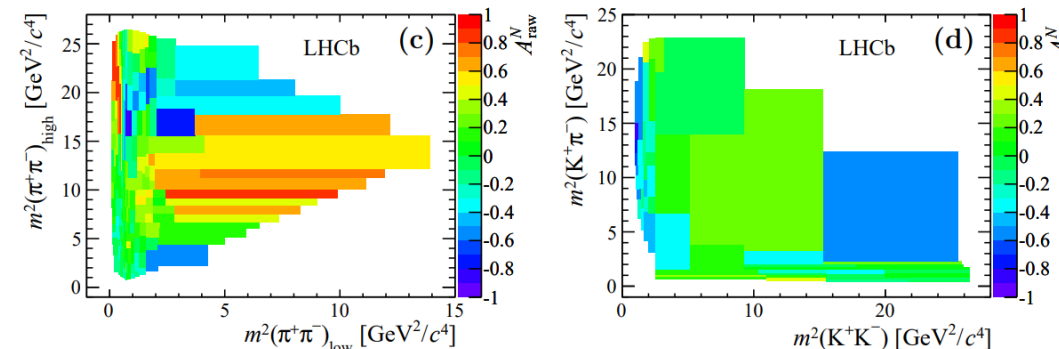
$$A_{CP}(\pi^\pm \pi^+ \pi^-) = +0.080 \pm 0.004 \pm 0.003 \pm 0.003$$

arXiv:2206.07622

- Significant  $A_{CP}$  in  $KK \leftrightarrow \pi\pi$  rescattering region, with a sign change across phase space
- Indication of  $\chi_{c0}(1P)$  contribution, with a large  $A_{CP}$
- Observation of  $A_{CP}$  in  $B \rightarrow PV$  modes through angular analysis

arXiv:2202.02038

$$A_{CP}(B^\pm \rightarrow \rho(770)^0 K^\pm) = 0.150 \pm 0.019$$



# $K\pi$ isospin sum rule

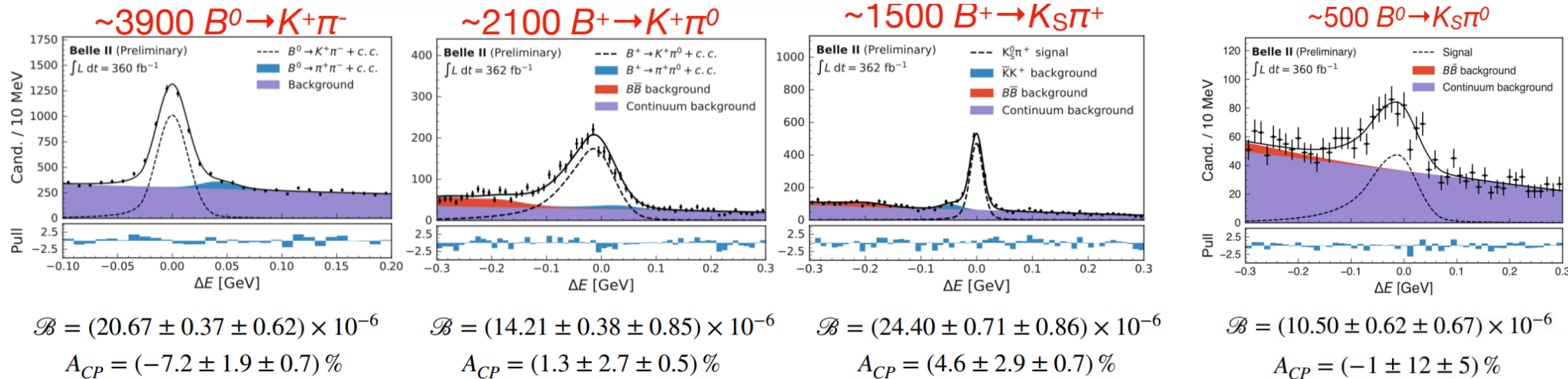
□ SM predicts  $I_{K\pi} = 0$  with  $O(1)\%$  theoretical uncertainty

$$I_{K\pi} = \mathcal{A}_{K^+\pi^-} + \mathcal{A}_{K^0\pi^+} \frac{\mathcal{B}(K^0\pi^+)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^+\pi^0} \frac{\mathcal{B}(K^+\pi^0)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^0\pi^0} \frac{\mathcal{B}(K^0\pi^0)}{\mathcal{B}(K^+\pi^-)}$$

WA:  $I_{K\pi} = (-13 \pm 11)\%$ , precision limited by  $K_S^0\pi^0$

□ Belle II able to access all final states for testing  $K\pi$  isospin sum rule

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$$I_{K\pi} = (-3 \pm 13 \pm 5)\%$$

Consistent with SM and competitive with W.A.

# Direct CPV in charm

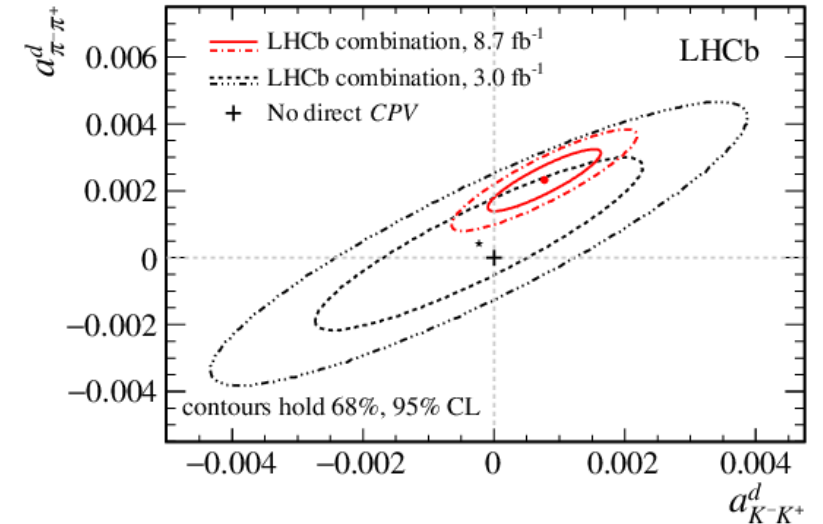
## Evidence of direct CPV in $D^0 \rightarrow \pi^- \pi^+$

arXiv:2209.03179

- CPV observed in  $A_{CP}(K^- K^+) - A(\pi^- \pi^+)$  PRL 122 (2019) 211803
- New measurement of  $A_{CP}(K^- K^+)$  using Run2 data
- Subtracting mixing-related CPV:  $a_f^d = A_{CP}(f) - \frac{\langle t \rangle_f}{\tau_D} \Delta Y_f$

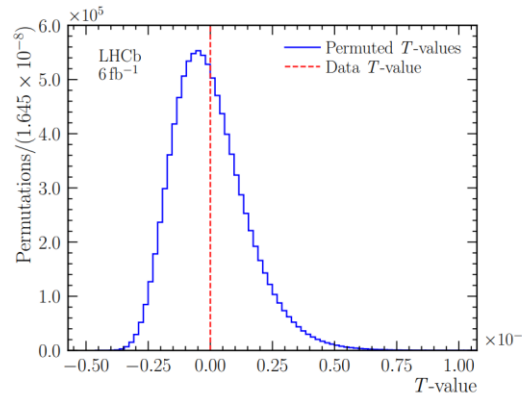
$$a_{K^- K^+}^d = (7.7 \pm 5.7) \times 10^{-4} \quad 1.4\sigma \text{ from zero}$$

$$a_{\pi^- \pi^+}^d = (23.2 \pm 6.1) \times 10^{-4} \quad 3.8\sigma \text{ from zero}$$

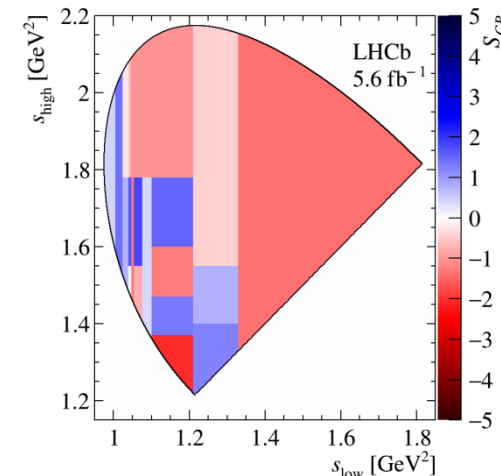


## Search for CPV in multi-body decays

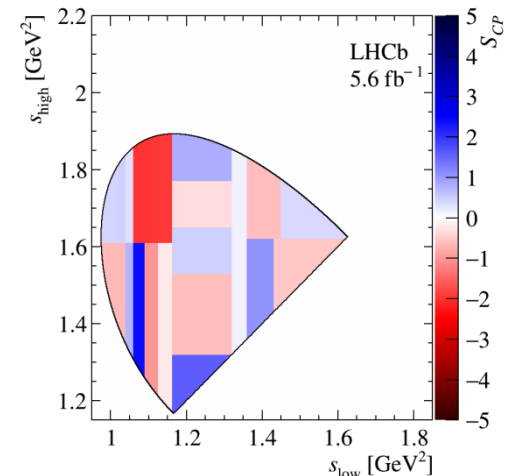
- $D^0 \rightarrow \pi^- \pi^+ \pi^0$ : energy test  
arXiv:2303.04062
- $D_{(s)}^+ \rightarrow K^- K^+ K^+$ : per-bin fit  
arXiv:2306.12746
- $D^0 \rightarrow h^- h^+ \mu^+ \mu^-$ : angular fit  
PRL 128 (2022) 221801
- No evidence for CPV



$D^0 \rightarrow \pi^- \pi^+ \pi^0$



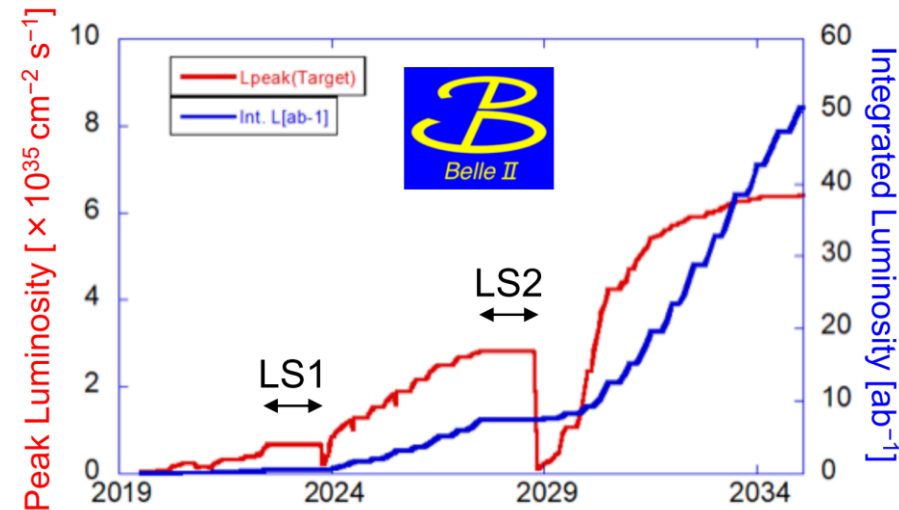
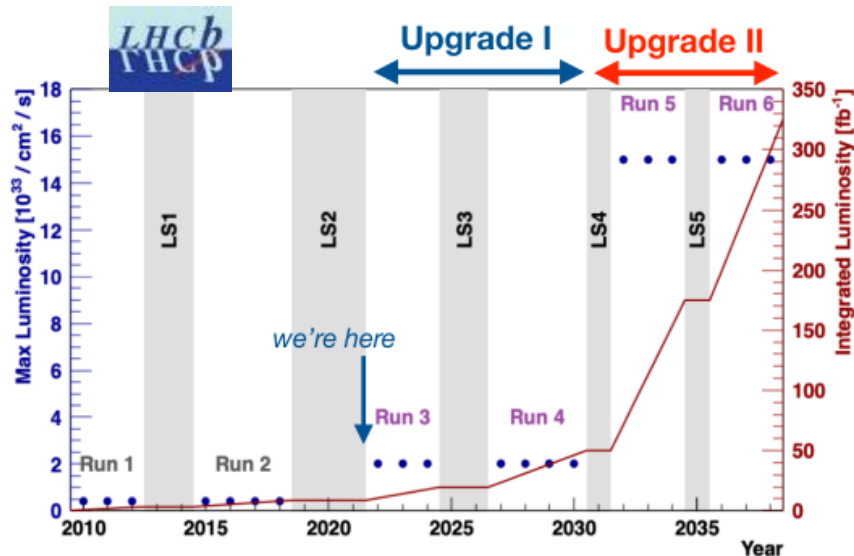
$D_s^+ \rightarrow K^- K^+ K^+$



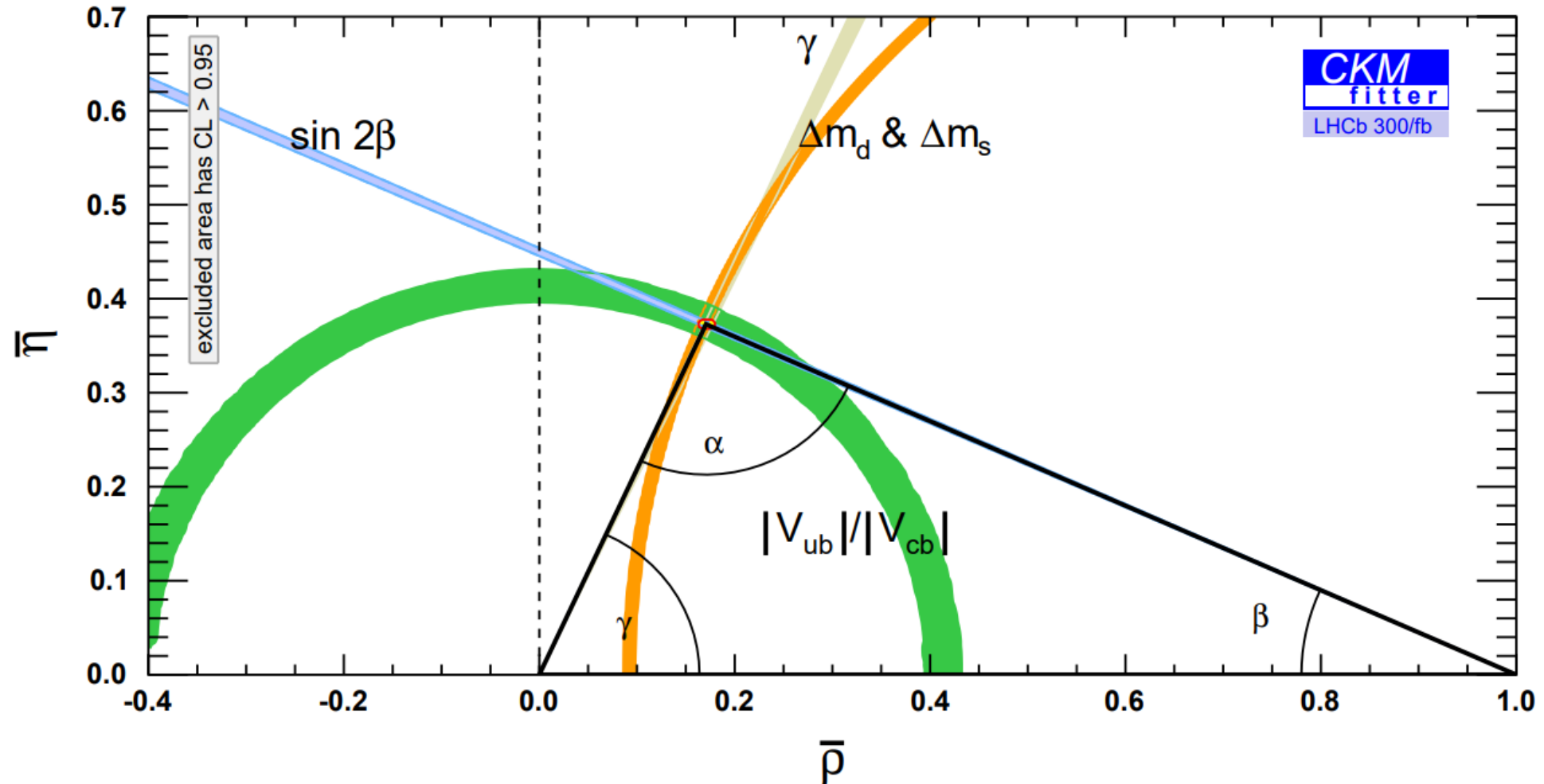
$D^+ \rightarrow K^- K^+ K^+$

# Summary

- ❑ The LHCb experiment has achieved the most precise measurements of the CKM angle  $\beta$ ,  $\beta_s$  and  $\gamma$ , which all agree with the SM predictions.
- ❑ Belle II is ramping up and producing interesting results.
- ❑ A deeper understanding of CP violation is a long term goal that requires synergies of LHCb upgrades, Belle II and future charm experiments.



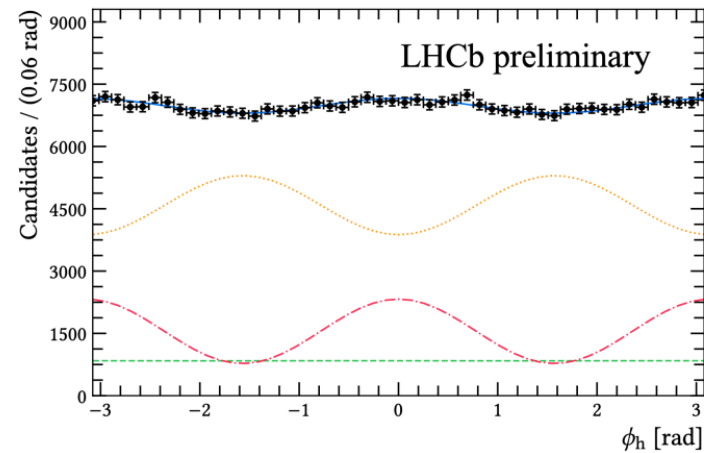
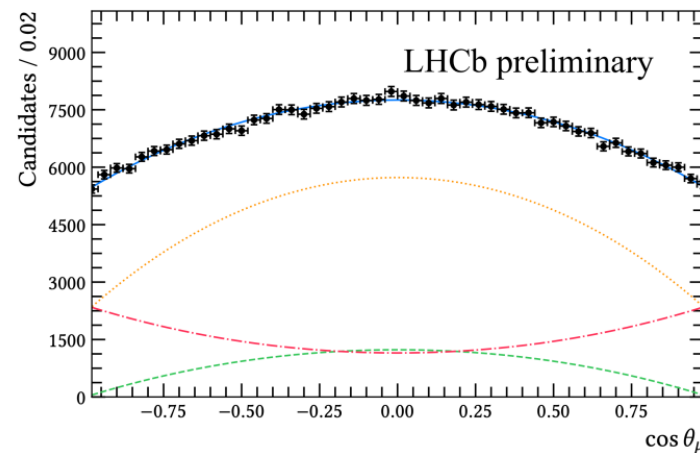
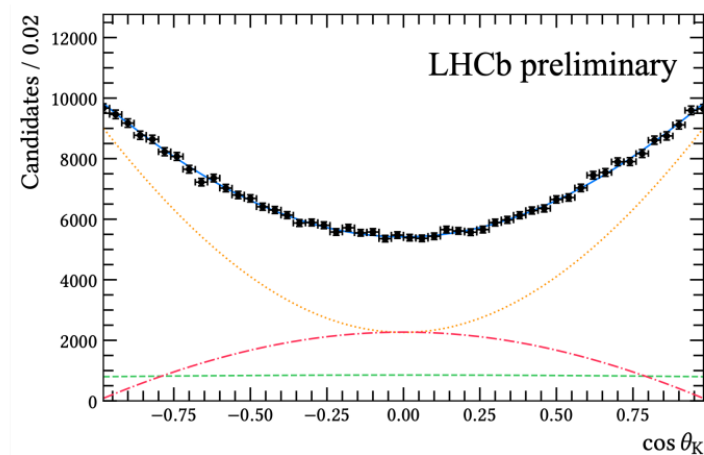
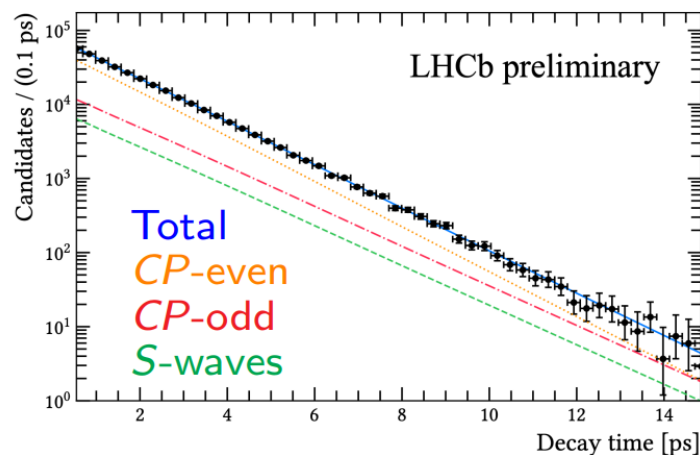
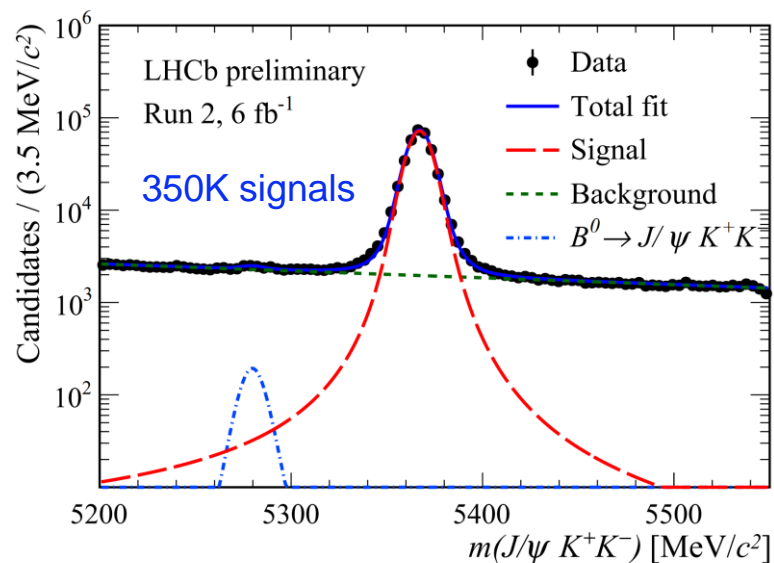
**There will be no place for new physics to hide,  
if it has a non-SM flavour structure!**





**Spare slides**

- Maximum-likelihood fit to TD angular distributions of tagged  $B_s^0$  and  $\bar{B}_s^0$  decays



# LHCb $\phi_s$ combination

LHCb-paper-2023-016  
in preparation

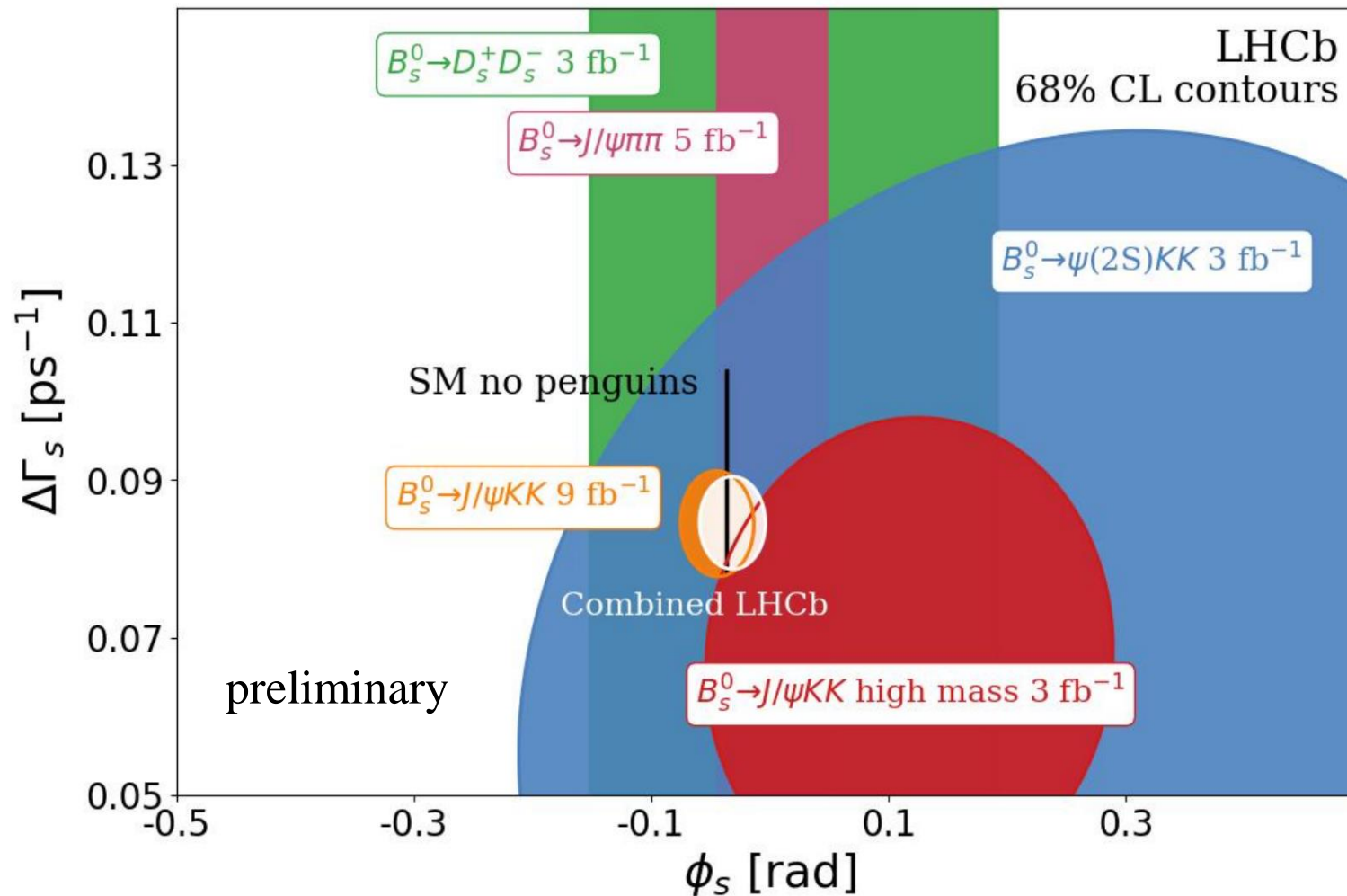
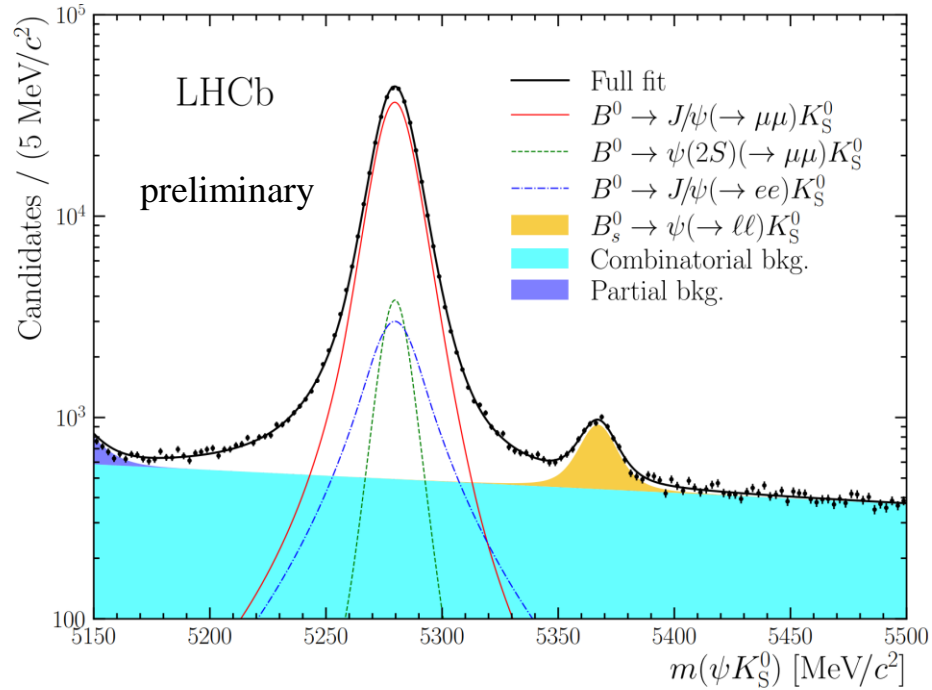


Table 3: Summary of the systematic uncertainties ( $\times 0.01$ ) for the main physics parameters.

Source	$ A_0 ^2$	$ A_\perp ^2$	$\phi_s$ [rad]	$ \lambda $	$\delta_\perp - \delta_0$ [rad]	$\delta_\parallel - \delta_0$ [rad]	$\Gamma_s - \Gamma_d$ [ps $^{-1}$ ]	$\Delta\Gamma_s$ [ps $^{-1}$ ]	$\Delta m_s$ [ps $^{-1}$ ]
Mass parametrization	0.04	0.03	0.03	0.02	0.15	0.12	0.02	0.04	0.03
Mass: shape statistical	0.04	0.04	0.05	0.09	0.62	0.33	0.02	0.01	0.11
Mass factorization	0.11	0.10	0.42	0.19	0.54	0.60	0.12	0.16	0.18
$B_c^+$ contamination <sup>2</sup>	0.04	0.05	—	0.02	—	0.17	(0.07)	(0.03)	—
D-wave component	0.04	0.04	0.02	—	0.07	0.13	0.01	0.03	0.02
Ghost tracks	0.07	0.04	0.02	0.10	0.18	0.18	0.02	—	0.01
Multiple candidates	0.01	—	0.27	0.22	0.90	0.41	0.01	0.01	0.24
Particle identification	0.06	0.09	0.27	0.27	1.31	0.51	0.05	0.15	0.46
$C_{SP}$ factors	—	0.01	0.01	0.03	0.73	0.41	—	0.01	0.04
DTR <sup>3</sup> calibration	—	—	0.03	0.02	0.11	0.07	—	—	0.05
DTR model applicability	—	—	0.08	0.03	0.26	0.09	—	—	0.09
Time bias correction	0.04	0.05	0.06	0.05	0.77	0.11	0.03	0.05	0.44
Angular efficiency	0.05	0.14	0.25	0.32	0.42	0.44	0.01	0.02	0.13
Angular resolution	0.01	0.01	0.02	0.01	0.02	0.08	—	0.01	0.02
Kinematic weighting	0.24	0.09	0.01	0.01	0.98	0.86	0.02	0.03	0.31
Momentum uncertainty	0.08	0.04	0.04	—	0.07	0.11	0.01	—	0.13
Longitudinal scale	0.07	0.04	0.04	—	0.10	0.09	0.02	—	0.31
Neglected correlations	—	—	—	—	4.20	4.96	—	—	—
Total systematic uncertainty	0.32	0.24	0.6	0.5	4.8	5.2	0.14	0.24	0.9
Statistical uncertainty	0.17	0.23	2.2	1.1	7.5	6.0	0.14	0.44	3.3

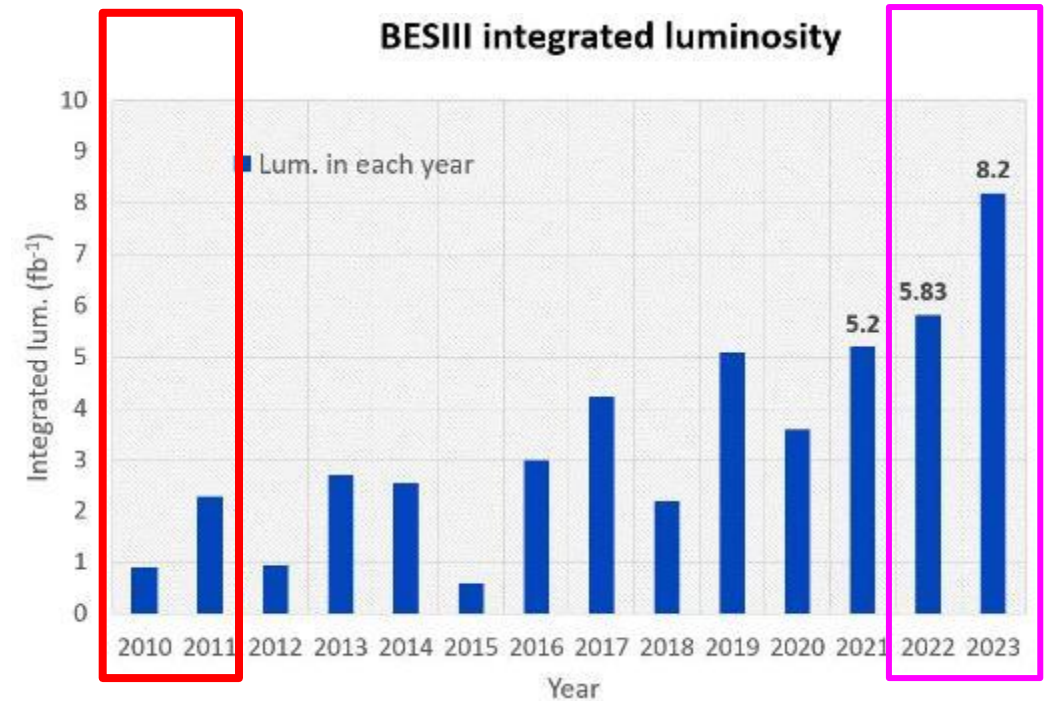


Source	$\sigma(S)$	$\sigma(C)$
Fitter validation	0.0004	0.0006
Decay-time bias model	0.0007	0.0013
FT $\Delta\epsilon_{\text{tag}}$ portability	0.0014	0.0017
FT calibration portability	0.0053	0.0001
$\Delta\Gamma_d$ uncertainty	0.0055	0.0017

mode	Para.	Ref.
$D^0 \rightarrow K_{S,L}^0 \pi^+ \pi^-$	Strong phase	PRD 101 (2020) 112002
$D^0 \rightarrow K_S^0 K^+ K^-$	Strong phase	PRD 102 (2020) 052008
$D^0 \rightarrow K^+ \pi^-$	Strong phase	EPJC 82 (2022) 1009
$D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$	Strong phase	arXiv:2103.05988
$D^0 \rightarrow K^+ K^- \pi^+ \pi^-$	CP-even fraction	arXiv:2212.06489
$D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$	CP-even fraction	arXiv:2305.03975
$D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$	CP-even fraction	arXiv:2208.10098

Used for  $D$  parameters

To be used



- Current BESIII measurements of  $D^0$  strong-phase parameters used  $3 \text{ fb}^{-1}$  of  $\psi(3770) \rightarrow D\bar{D}$  data
- BESIII will accumulate  $20 \text{ fb}^{-1}$  of  $\psi(3770) \rightarrow D\bar{D}$  data this year



# LHCb upgrade II sensitivity

Observable	Current LHCb	LHCb 2025	Belle II	Upgrade II	ATLAS & CMS
<b>EW Penguins</b>					
$R_K$ ( $1 < q^2 < 6 \text{ GeV}^2 c^4$ )	0.1 [274]	0.025	0.036	0.007	—
$R_{K^*}$ ( $1 < q^2 < 6 \text{ GeV}^2 c^4$ )	0.1 [275]	0.031	0.032	0.008	—
$R_\phi, R_{pK}, R_\pi$	—	0.08, 0.06, 0.18	—	0.02, 0.02, 0.05	—
<b>CKM tests</b>					
$\gamma$ , with $B_s^0 \rightarrow D_s^+ K^-$	$(^{+17}_{-22})^\circ$ [136]	$4^\circ$	—	$1^\circ$	—
$\gamma$ , all modes	$(^{+5.0}_{-5.8})^\circ$ [167]	$1.5^\circ$	$1.5^\circ$	$0.35^\circ$	—
$\sin 2\beta$ , with $B^0 \rightarrow J/\psi K_s^0$	0.04 [609]	0.011	0.005	0.003	—
$\phi_s$ , with $B_s^0 \rightarrow J/\psi \phi$	49 mrad [44]	14 mrad	—	4 mrad	22 mrad [610]
$\phi_s$ , with $B_s^0 \rightarrow D_s^+ D_s^-$	170 mrad [49]	35 mrad	—	9 mrad	—
$\phi_s^{s\bar{s}s}$ , with $B_s^0 \rightarrow \phi \phi$	154 mrad [94]	39 mrad	—	11 mrad	Under study [611]
$a_{\text{sl}}^s$	$33 \times 10^{-4}$ [211]	$10 \times 10^{-4}$	—	$3 \times 10^{-4}$	—
$ V_{ub} / V_{cb} $	6% [201]	3%	1%	1%	—
<b><math>B_s^0, B^0 \rightarrow \mu^+ \mu^-</math></b>					
$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-)/\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)$	90% [264]	34%	—	10%	21% [612]
$\tau_{B_s^0 \rightarrow \mu^+ \mu^-}$	22% [264]	8%	—	2%	—
$S_{\mu\mu}$	—	—	—	0.2	—
<b><math>b \rightarrow c \ell^- \bar{\nu}_\ell</math> LUV studies</b>					
$R(D^*)$	0.026 [215, 217]	0.0072	0.005	0.002	—
$R(J/\psi)$	0.24 [220]	0.071	—	0.02	—
<b>Charm</b>					
$\Delta A_{CP}(KK - \pi\pi)$	$8.5 \times 10^{-4}$ [613]	$1.7 \times 10^{-4}$	$5.4 \times 10^{-4}$	$3.0 \times 10^{-5}$	—
$A_\Gamma$ ( $\approx x \sin \phi$ )	$2.8 \times 10^{-4}$ [240]	$4.3 \times 10^{-5}$	$3.5 \times 10^{-4}$	$1.0 \times 10^{-5}$	—
$x \sin \phi$ from $D^0 \rightarrow K^+ \pi^-$	$13 \times 10^{-4}$ [228]	$3.2 \times 10^{-4}$	$4.6 \times 10^{-4}$	$8.0 \times 10^{-5}$	—
$x \sin \phi$ from multibody decays	—	( $K3\pi$ ) $4.0 \times 10^{-5}$	( $K_S^0 \pi\pi$ ) $1.2 \times 10^{-4}$	( $K3\pi$ ) $8.0 \times 10^{-6}$	—