

NHL'S AND LIGHT OSCILLATING NEUTRINOS IN 2022

Concha Gonzalez-Garcia

(ICREA U. Barcelona & YITP Stony Brook)

FIP's Workshop, CERN, Sept 20, 2022



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OUTLINE

- Introduction: NHL's & Active Neutrino Oscillations
- Status of 3ν global description



Introduction: The SM of Active Neutrinos

The SM is a gauge theory based on the symmetry group

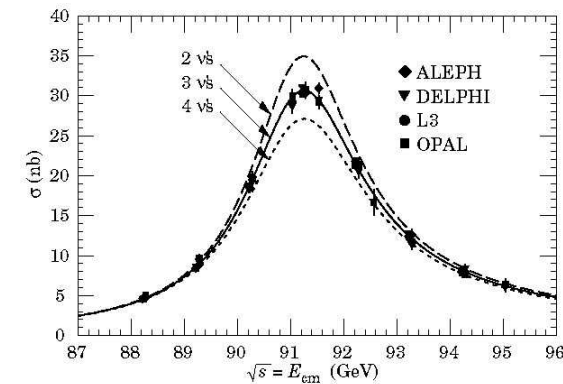
$$SU(3)_C \times SU(2)_L \times U(1)_Y \Rightarrow SU(3)_C \times U(1)_{EM}$$

With three generation of fermions

$(1, 2)_{-\frac{1}{2}}$	$(3, 2)_{\frac{1}{6}}$	$(1, 1)_{-1}$	$(3, 1)_{\frac{2}{3}}$	$(3, 1)_{-\frac{1}{3}}$
$\begin{pmatrix} \nu_e \\ e \end{pmatrix}_L$	$\begin{pmatrix} u^i \\ d^i \end{pmatrix}_L$	e_R	u^i_R	d^i_R
$\begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}_L$	$\begin{pmatrix} c^i \\ s^i \end{pmatrix}_L$	μ_R	c^i_R	s^i_R
$\begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}_L$	$\begin{pmatrix} t^i \\ b^i \end{pmatrix}_L$	τ_R	t^i_R	b^i_R

There is no ν_R

Three and only three



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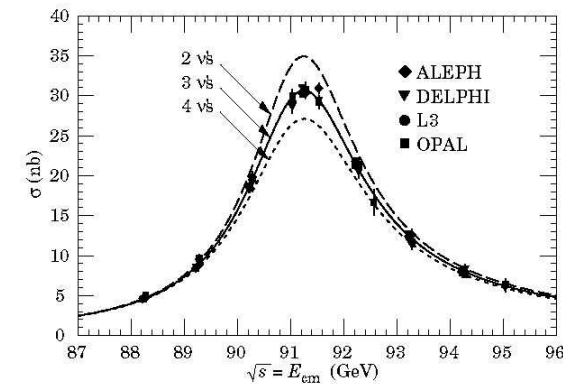


Accidental global symmetry: $B \times L_e \times L_\mu \times L_\tau$ (hence $L = L_e + L_\mu + L_\tau$)



ν strictly massless

Three and only three



Introduction: The need of BSM

- We have confirmed with high/reasonable precision:
 - * Atmospheric ν_μ & $\bar{\nu}_\mu$ disappear most likely to ν_τ (**SK, MINOS, ICECUBE**)
 - * Accel. ν_μ & $\bar{\nu}_\mu$ disappear at $L \sim 300/800$ Km (**K2K, T2K, MINOS, NO ν A**)
 - * Some accelerator ν_μ appear as ν_e at $L \sim 300/800$ Km (**T2K, MINOS, NO ν A**)
 - * Solar ν_e convert to ν_μ/ν_τ (**Cl, Ga, SK, SNO, Borexino**)
 - * Reactor $\bar{\nu}_e$ disappear at $L \sim 200$ Km (**KamLAND**)
 - * Reactor $\bar{\nu}_e$ disappear at $L \sim 1$ Km (**D-Chooz, Daya Bay, Reno**)

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All this implies that L_α are violated \Rightarrow SM needs to be extended

Intro: The Minimal SM Extension

a Gonzalez-Garcia

- Minimal Extension to allow for LFV \Rightarrow give Mass to the Neutrino

* Introduce ν_R AND impose L conservation \Rightarrow Dirac $\nu \neq \nu^c$:

$$\mathcal{L} = \mathcal{L}_{SM} - M_\nu \bar{\nu}_L \nu_R + h.c.$$

* NOT impose L conservation \Rightarrow Majorana $\nu = \nu^c$

$$\mathcal{L} = \mathcal{L}_{SM} - \frac{1}{2} M_\nu \bar{\nu} \nu^C + h.c.$$

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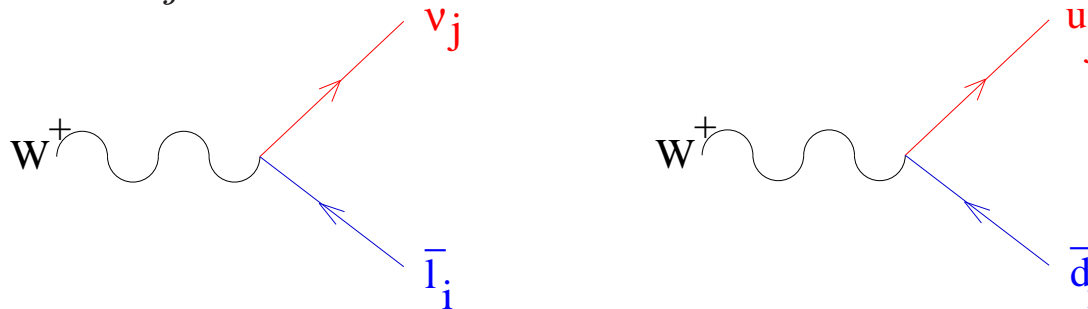
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- Charged current interactions of leptons are not diagonal (*similarly* to quarks)

$$\frac{g}{\sqrt{2}} W_\mu^+ \sum_{ij} (U_{LEP}^{ij} \bar{\ell}^i \gamma^\mu L \nu^j + U_{CKM}^{ij} \bar{U}^i \gamma^\mu L D^j) + h.c.$$



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\Rightarrow Flavour Oscillations:

$$P_{\alpha\beta} = \delta_{\alpha\beta} - 4 \sum_{j \neq i}^n \text{Re}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin^2 \left(\frac{\Delta_{ij}}{2} \right) + 2 \sum_{j \neq i} \text{Im}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin(\Delta_{ij})$$

$$\frac{\Delta_{ij}}{2} = \frac{(E_i - E_j)L}{2} = 1.27 \frac{(m_i^2 - m_j^2)}{\text{eV}^2} \frac{L/E}{\text{Km/GeV}}$$

Intro: Lepton Mixing

- For 3 charged leptons and 3 (ew doublet) + S (ew singlet) neutrinos
the charged current in the mass basis: $\mathcal{L}_{CC} = -\frac{g}{\sqrt{2}} \overline{\ell}_L^i \gamma^\mu U_{\text{LEP}}^{ij} \nu_j W_\mu^+$

$$U_{\text{LEP}}^{ij} = \sum_{k=1}^3 P_{ii}^\ell V_L^{\ell \dagger ik} V^{\nu kj} P_{jj}^\nu \quad 3 \times (3 + S) \text{ matrix}$$

V_L^ℓ : 3×3 Unitary matrix rotating left charged leptons to mass basis

V^ν : $(3 + S) \times (3 + S)$ Unitary matrix rotating neutrinos to mass basis

P_{ii}^ℓ : 3 phases absorbed in l_i

P_{kk}^ν : $S+2$ phases absorbed in ν_i if all ν_i Dirac or $P_{kk}^\nu = \mathbf{I}$ if all ν_i Majorana

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- If no other NP in charge lepton sector we can choose $V_L^\ell = I_{3 \times 3}$

$$\Rightarrow V^\nu = \begin{array}{c|cc} \text{dim} & 3 & S \\ \hline 3 & (K_l & K_h) \equiv U_{\text{LEP}} \\ S & \tilde{K}_h & \tilde{K}_H \end{array} \quad K_{l,3 \times 3} \text{ and } K_{h,3 \times S} \text{ non-unitary}$$

Valle and Schechter PRD22 (1980)

Intro: Lepton Mixing Unitarity

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- The massive neutrino interactions of $\nu_l \equiv 3$ lightest and $N \equiv S$ heavier \equiv NHL's

$$\mathcal{L}_{CC} = -\frac{g}{\sqrt{2}} (\bar{\ell} \gamma^\mu K_l \nu_l + \bar{\ell} \gamma^\mu K_h N) W_\mu^+ + \text{h.c.}$$

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- $V^\nu V^{\nu\dagger} = \begin{pmatrix} K_l K_l^\dagger + K_h K_h^\dagger & \dots \\ \dots & \dots \end{pmatrix} = \begin{pmatrix} I_{3 \times 3} & 0 \\ 0 & I_{S \times S} \end{pmatrix}$

$$\Rightarrow U_{\text{LEP}} U_{\text{LEP}}^\dagger = K_l K_l^\dagger + K_h K_h^\dagger = I_{3 \times 3}$$

$$[\text{But } U_{\text{LEP}}^\dagger U_{\text{LEP}} \neq I_{(3+S) \times (3+S)}]$$

$$K_l K_l^\dagger + K_h K_h^\dagger = I_{3 \times 3} \Rightarrow \text{generic relation between NHL couplings}$$

and **unitarity violation in ν_l oscillations**

- Convenient parametrization:

Xing arXiv:1110.0083; Escribuela *etal* arXiv:1503.08879, Blennow *etal* arXiv:1609.08637

$$K_l = \left[I_{3 \times 3} - \begin{pmatrix} \alpha_{ee} & 0 & 0 \\ \alpha_{e\mu} & \alpha_{\mu\mu} & 0 \\ \alpha_{e\tau} & \alpha_{\mu\tau} & \alpha_{\tau\tau} \end{pmatrix} \right] U_{3 \times 3}$$

$$U_{3 \times 3} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{i\delta_{cp}} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta_{cp}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{21} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\eta_1} & 0 & 0 \\ 0 & e^{i\eta_2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- $$K_l K_l^\dagger + K_h K_h^\dagger = I_{3 \times 3} \Rightarrow K_h K_h^\dagger = \begin{pmatrix} 2\alpha_{ee} & \alpha_{e\mu}^* & \alpha_{e\tau}^* \\ \alpha_{e\mu} & 2\alpha_{\mu\mu} & \alpha_{\mu\tau}^* \\ \alpha_{e\tau} & \alpha_{\mu\tau} & 2\alpha_{\tau\tau} \end{pmatrix} + \mathcal{O}(\alpha^2) \Rightarrow K_h \sim \mathcal{O}(\sqrt{\alpha})$$

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• Canonical type-I see-saw: $M_\nu = \begin{pmatrix} 0 & D_{3 \times S} \\ D_{S \times 3}^T & M_{S \times S} \end{pmatrix} \quad D \equiv \frac{Y^\nu}{\sqrt{2}} v$

Diagonalizing $M_\nu \Rightarrow \begin{cases} 3 \nu'_l \text{'s} : & m_{\nu_l} \sim D^T M^{-1} D \\ S \text{ NHL's} : & M_N \sim M \gg \text{TeV} \\ \alpha \sim \left(\frac{D}{M}\right) \left(\frac{D}{M}\right)^\dagger & \sim \frac{m_{\nu_l}}{M_N} \text{ unobservable} \end{cases}$

Convenient parametrization:

$$K_l = \left[I_{3 \times 3} - \begin{pmatrix} \alpha_{ee} & 0 & 0 \\ \alpha_{e\mu} & \alpha_{\mu\mu} & 0 \\ \alpha_{e\tau} & \alpha_{\mu\tau} & \alpha_{\tau\tau} \end{pmatrix} \right] U_{3 \times 3}(\theta_{12}, \theta_{13}, \theta_{23}, \delta; \eta_1, \eta_2) \quad K_h \sim \mathcal{O}(\sqrt{\alpha})$$

- In more general see-saw-I scenarios: Bounds on α' s depend on NHL mass range

Blennow *etal* arXiv:1609.08637

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- for all $M_N \lesssim 10 \text{ eV}$:
 - 3+S ν' s in oscillation experiments
 - For $10 \text{ eV} \lesssim M_N \ll \text{EW}$ scale :
 - M_N oscillations mostly averaged in osc experiments
 - Searches for N 's at beam-dump experiments
 - For $M_N \gtrsim \text{EW}$ scale \Rightarrow Unitarity and Universality violation in EWPD
- $\Rightarrow \alpha' s \lesssim 10^{-3} - 10^{-4}$

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– for all $M_N \lesssim 10 \text{ eV}$:

- 3+S ν' s in oscillation experiments $\left\{ \begin{array}{l} M_N \sim \text{eV} \Rightarrow \text{some SBL anomaly explained} \\ \text{Fit to all other osc data} \Rightarrow \alpha' s \lesssim 0.1-0.01 \end{array} \right.$

– For $10 \text{ eV} \lesssim M_N \ll \text{EW scale}$:

- M_N oscillations mostly averaged in osc experiments
 - Searches for N 's at beam-dump experiments $\left. \vphantom{\begin{array}{l} - M_N \text{ oscillations mostly averaged in osc experiments} \\ - Searches for } \right\} \Rightarrow \text{stronger bounds on } \alpha' s$

– For $M_N \gtrsim \text{EW scale} \Rightarrow$ Unitarity and Universality violation in EWPD

$$\Rightarrow \alpha' s \lesssim 10^{-3} - 10^{-4}$$

\Rightarrow Unitarity violation can be ignored in present $3\nu_l$ oscillation analysis

Partial 3ν -osc analysis w/o unitarity Hu *etal* 2008.09730; Denton, Gehrlein 2109.14575

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$$K_l K_l^\dagger + K_h K_h^\dagger = I_{3 \times 3} \Rightarrow \text{generic relation between NHL effects and } \nu_l \text{ unit. violat.}$$

– Theoretical prejudice & Experimental bounds:

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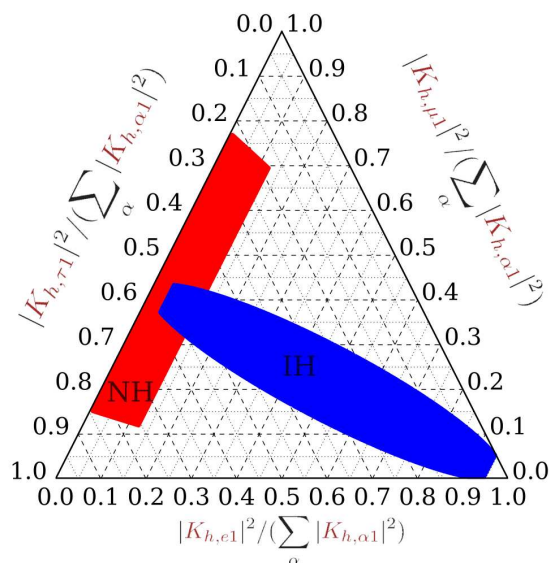
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Minimal (Lepton Flavour Violating) Type I see-saws: Gavela *etal* 0906.1461

$\Rightarrow K_h$ dominantly determined by $3\nu_l$ osc parameters

[up to overall normalization & Maj phase(s)]

\Rightarrow Maximal correlation between $3\nu_l$ osc parameters and expected NHL effects



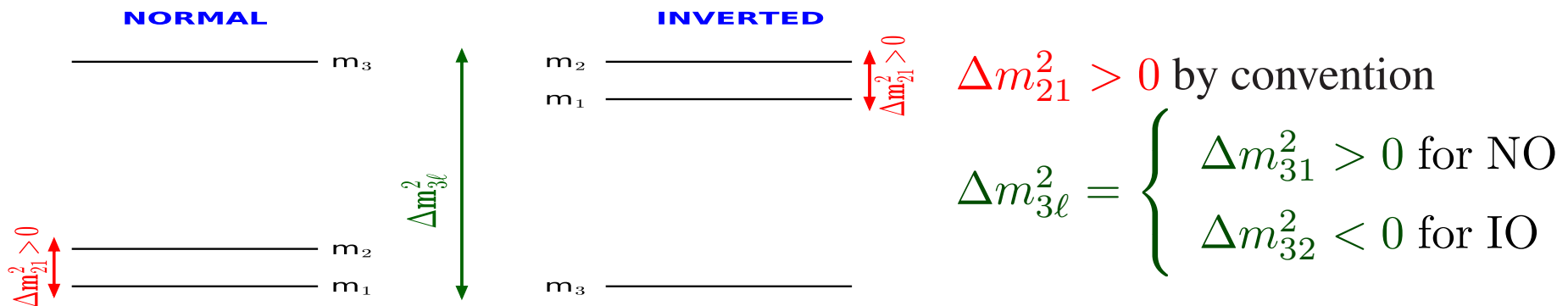
Caputo *etal* 1704.08721

Active 3ν Flavour Parameters

- For 3 ν 's : 3 Mixing angles + 1 Dirac Phase + 2 Majorana Phases

$$U_{\text{LEP}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{i\delta_{\text{CP}}} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta_{\text{CP}}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{21} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\theta_1} & 0 & 0 \\ 0 & e^{i\theta_2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- Convention: $0 \leq \theta_{ij} \leq 90^\circ$ $0 \leq \delta \leq 360^\circ \Rightarrow 2$ Orderings

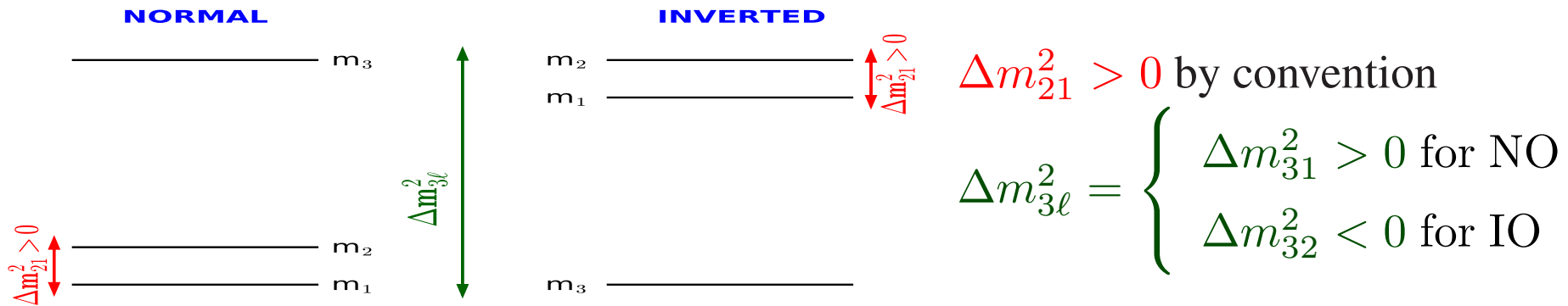


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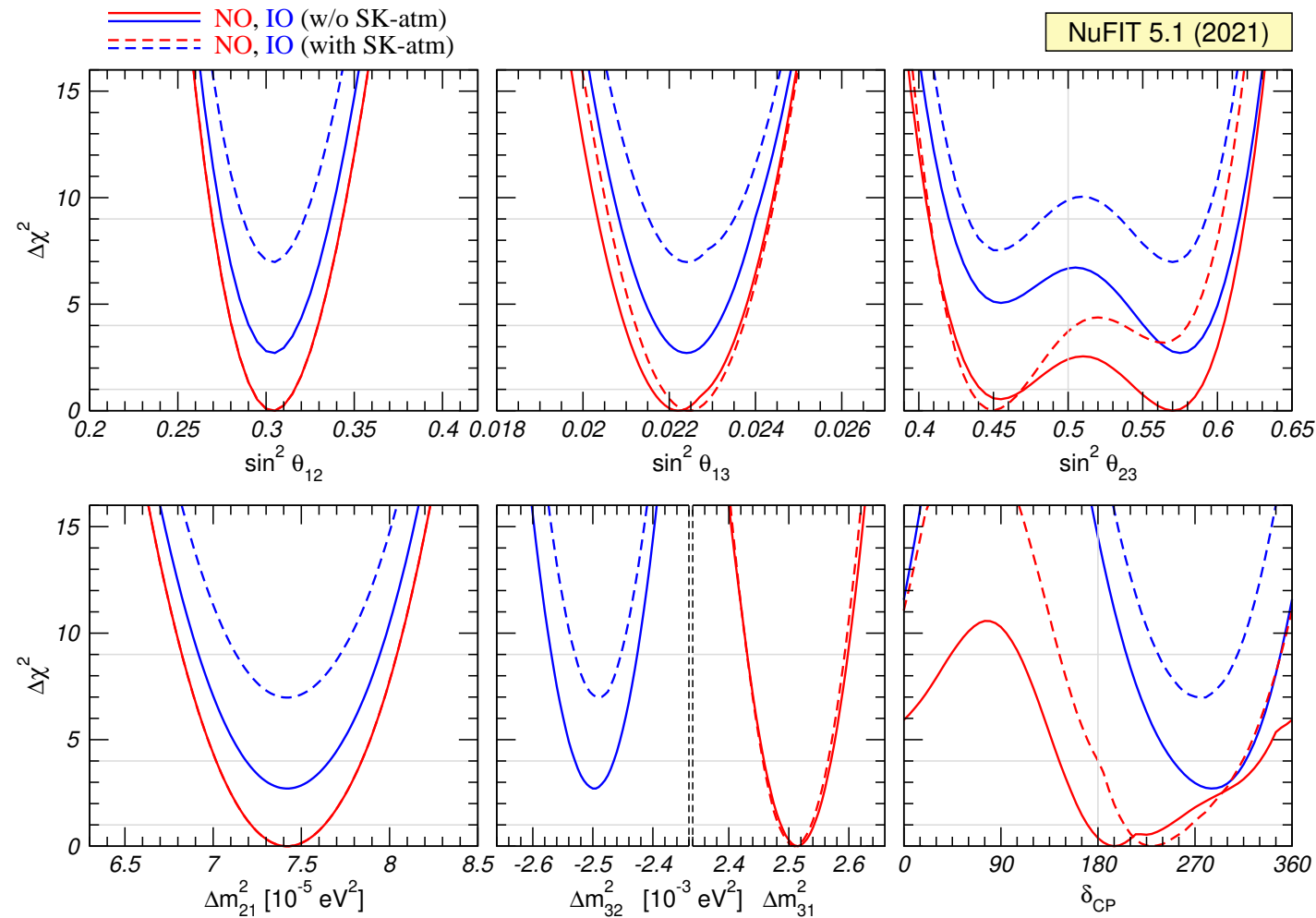


Experiment	Dominant Dependence	Important Dependence
Solar Experiments	θ_{12}	$\Delta m_{21}^2, \theta_{13}$
Reactor LBL (KamLAND)	Δm_{21}^2	θ_{12}, θ_{13}
Reactor MBL (Daya Bay, Reno, D-Chooz)	$\theta_{13}, \Delta m_{3l}^2$	
Atmospheric Experiments (SK, IC)		$\theta_{23}, \Delta m_{3l}^2, \theta_{13}, \delta_{\text{CP}}$
Acc LBL ν_μ Disapp (Minos, T2K, NOvA)	$\Delta m_{3l}^2, \theta_{23}$	
Acc LBL ν_e App (Minos, T2K, NOvA)	δ_{CP}	θ_{13}, θ_{23}

Summary: Global 3 ν Flavour Parameters

Global 6-parameter fit <http://www.nu-fit.org>

Esteban, G-G, Maltoni, Schwetz, Zhou, JHEP'20 [2007.14792], G-G, Maltoni, Schwetz, 2111.03086



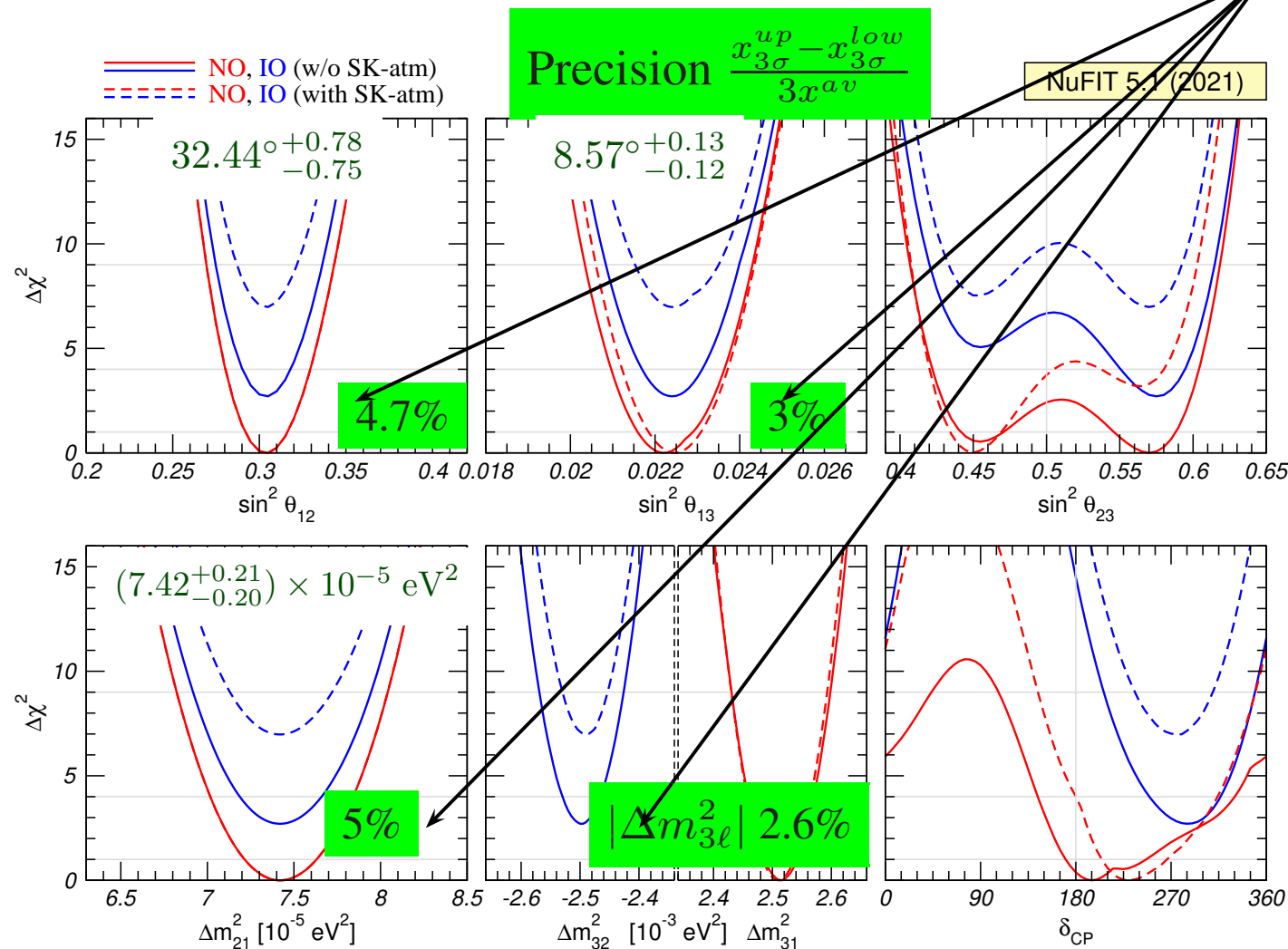
Summary: Global 3 ν Flavour Parameters

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Esteban, G-G, Maltoni, Schwetz, Zhou, JHEP'20 [2007.14792], G-G, Maltoni, Schwetz, 2111.03086

• 4 well-known parameters:

$\theta_{12}, \theta_{13}, \Delta m_{21}^2, |\Delta m_{3\ell}^2|$



Summary: Global 3 ν Flavour Parameters

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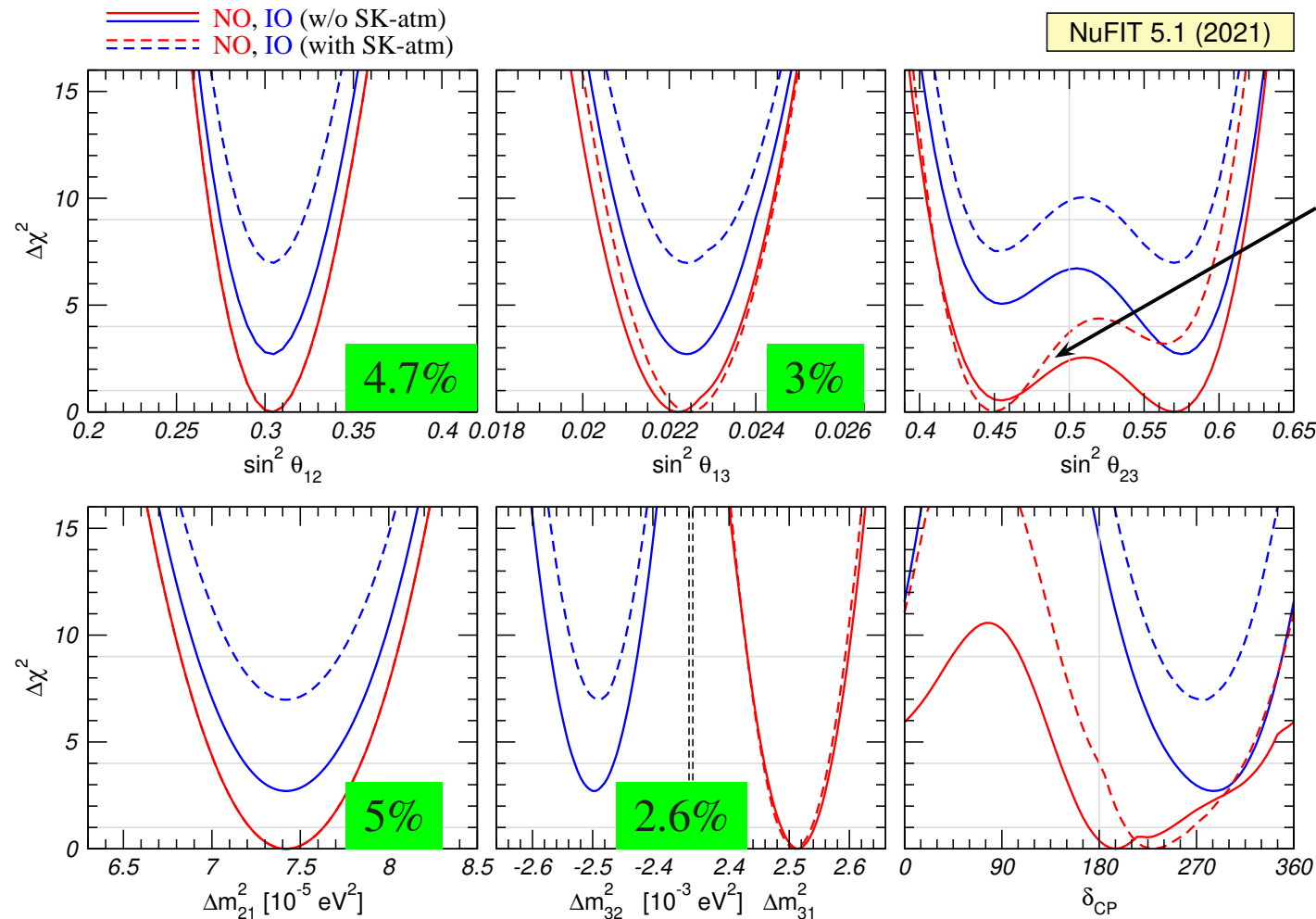
Δm_{21}^2 Solar vs KLAND

Tension Resolved

- θ_{23} : Least known angle

Maximal? Octant?

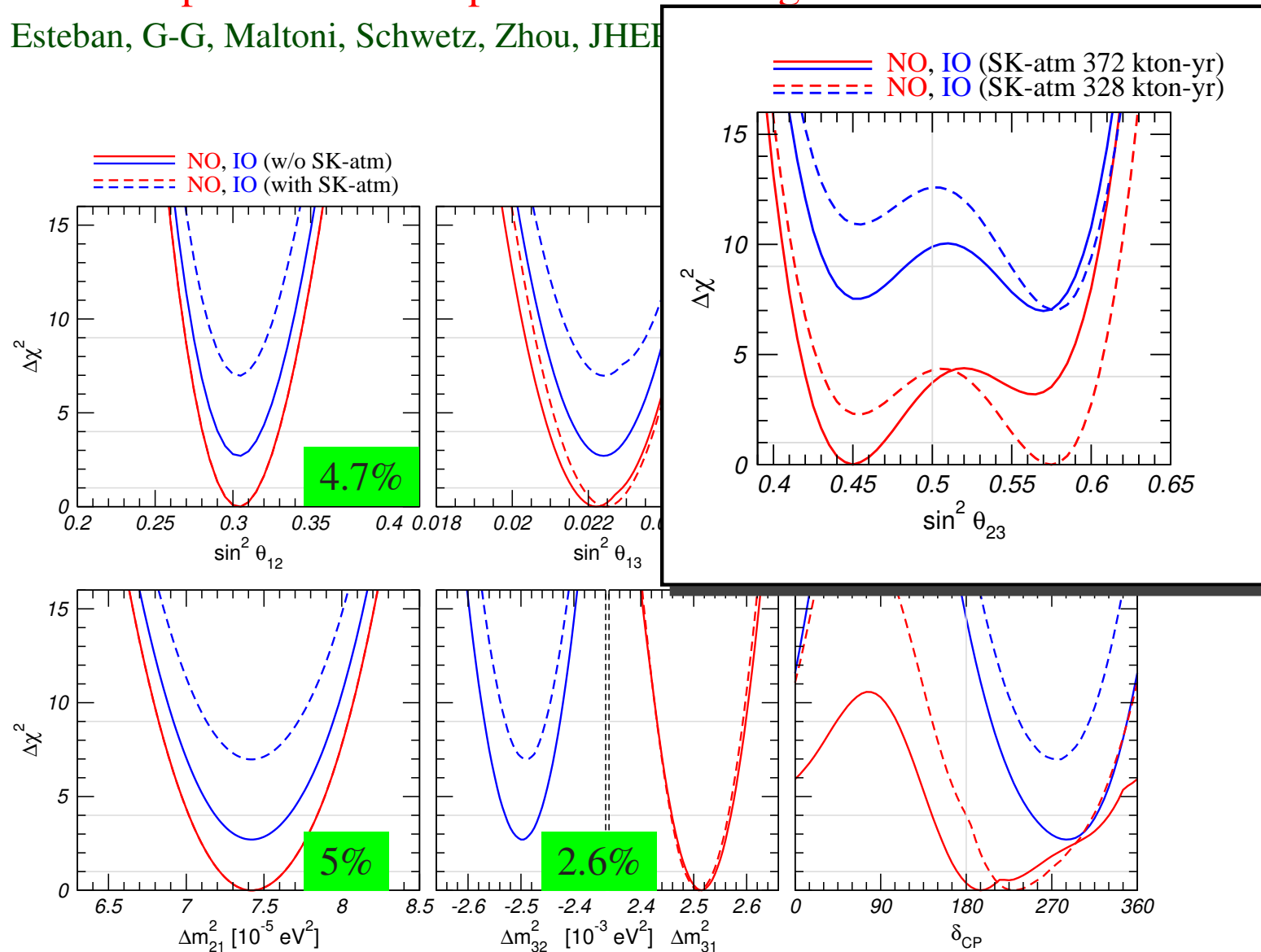
non-robust wrt ATM



Summary: Global 3 ν Flavour Parameters

Global 6-parameter fit <http://www.nu-fit.org>

Esteban, G-G, Maltoni, Schwetz, Zhou, JHEP



2111.03086
 1-known parameters:
 θ_{13} , Δm_{21}^2 , $|\Delta m_{3\ell}^2|$
 Solar vs KLAND
 on Resolved
 Least known angle
 normal? Octant?
 robust wrt ATM

Summary: Global 3 ν Flavour Parameters

Global 6-parameter fit <http://www.nu-fit.org>

Esteban, G-G, Maltoni, Schwetz, Zhou, JHEP'20 [2007.14792], G-G, Maltoni, Schwetz, 2111.03086

- 4 well-known parameters:

$$\theta_{12}, \theta_{13}, \Delta m_{21}^2, |\Delta m_{3\ell}^2|$$

Δm_{21}^2 Solar vs KLAND

Tension Resolved

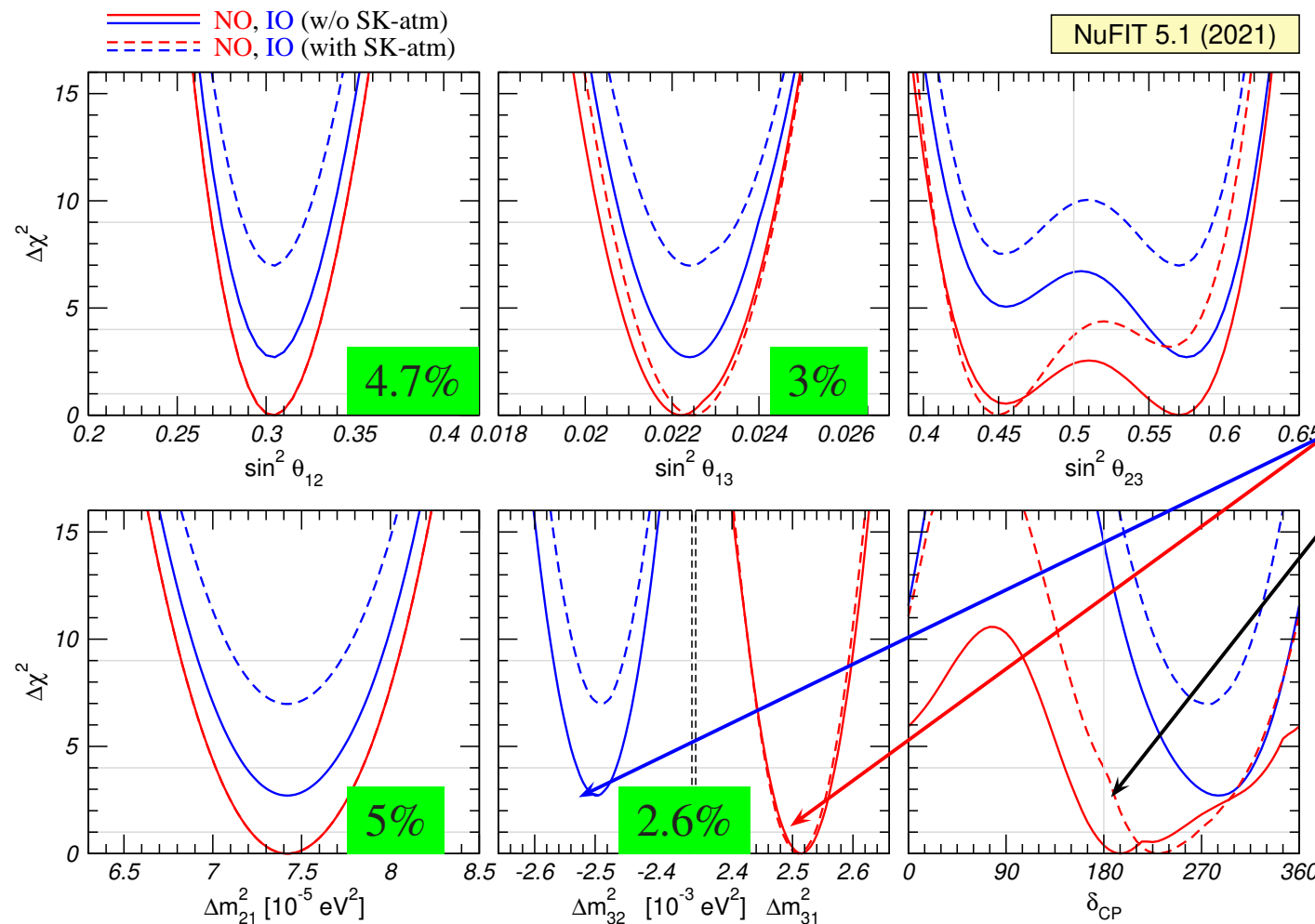
- θ_{23} : Least known angle

Maximal? Octant?

non-robust wrt ATM

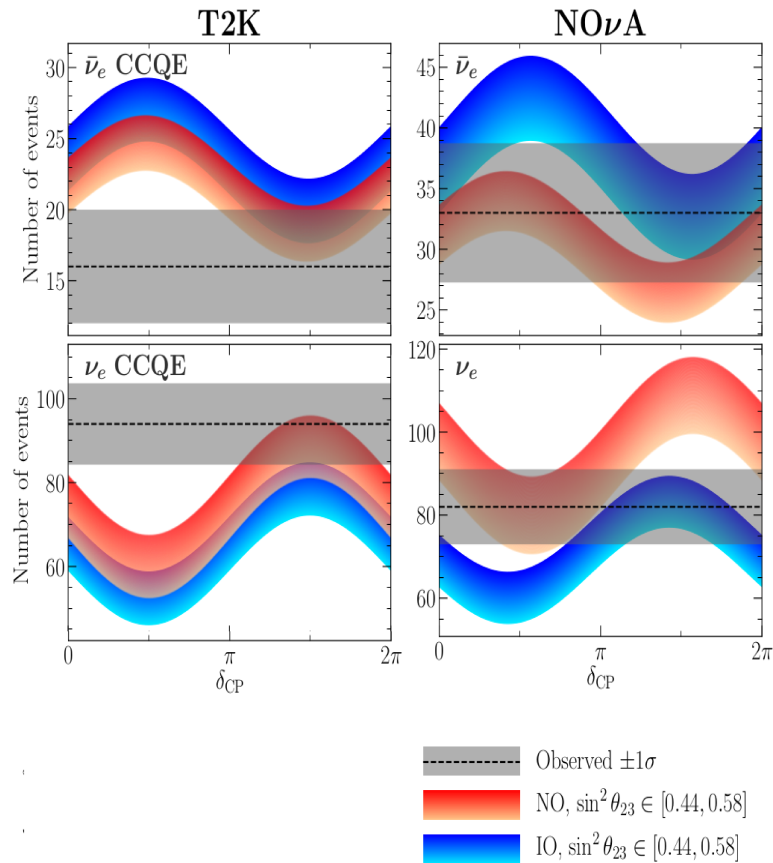
- Ordering **NO** or **IO**?

CPV?:



CPV and Ordering in LBL: ν_e appearance

ν_e and $\bar{\nu}_e$ appearance events

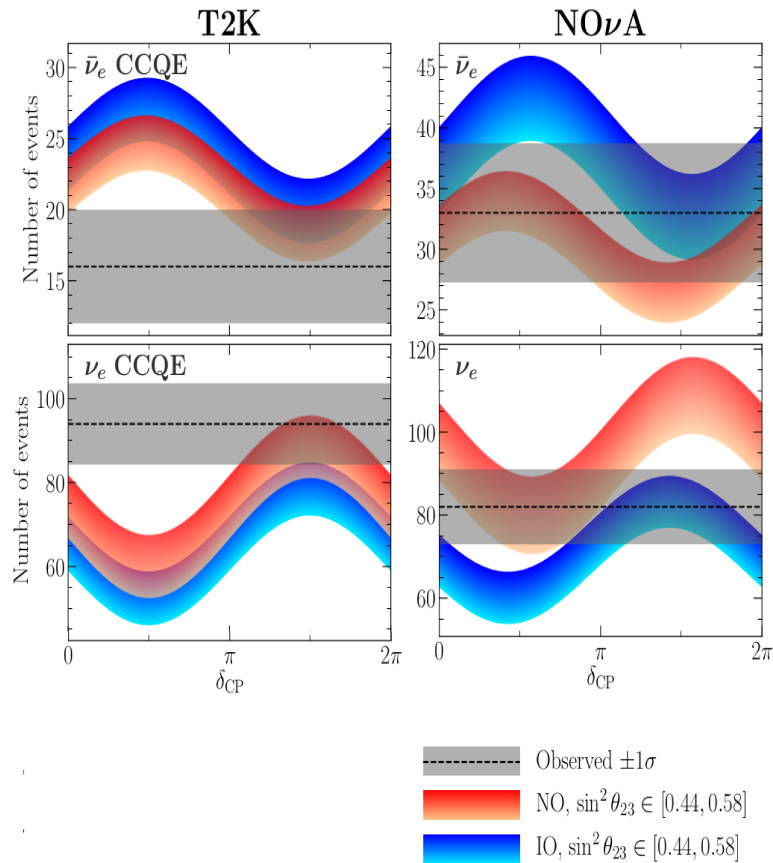


\Rightarrow Each T2K and NO ν A favour **NO**

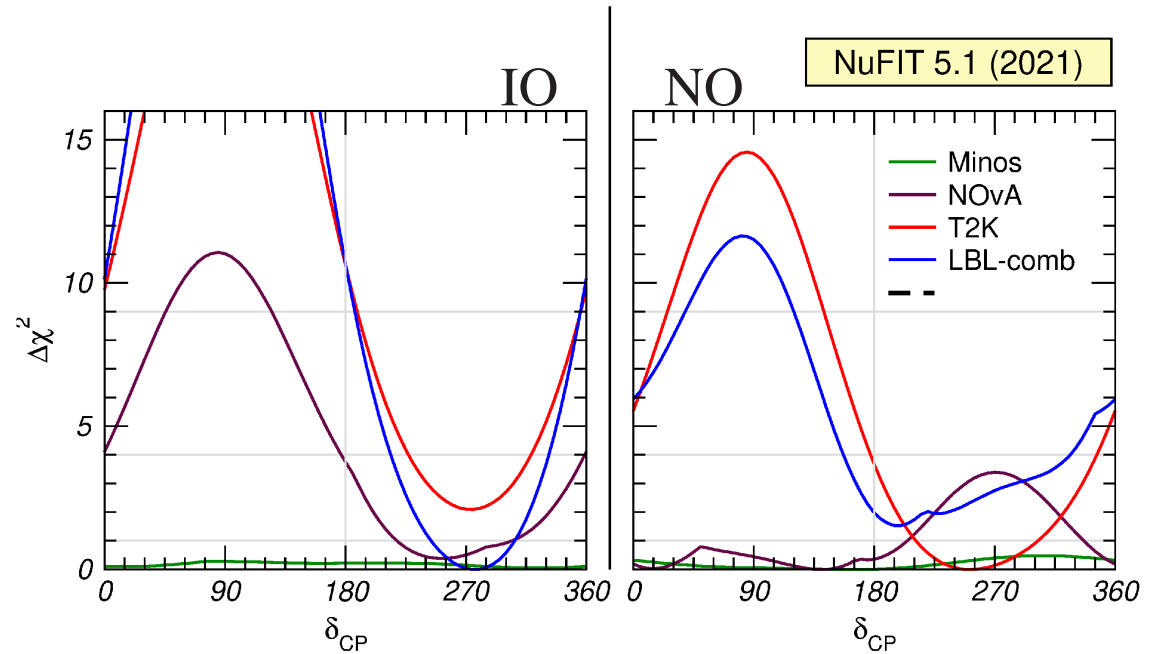
CPV and Ordering in LBL: ν_e appearance

Sanchez-Garcia

ν_e and $\bar{\nu}_e$ appearance events



But tension in favoured values of δ_{CP} in NO



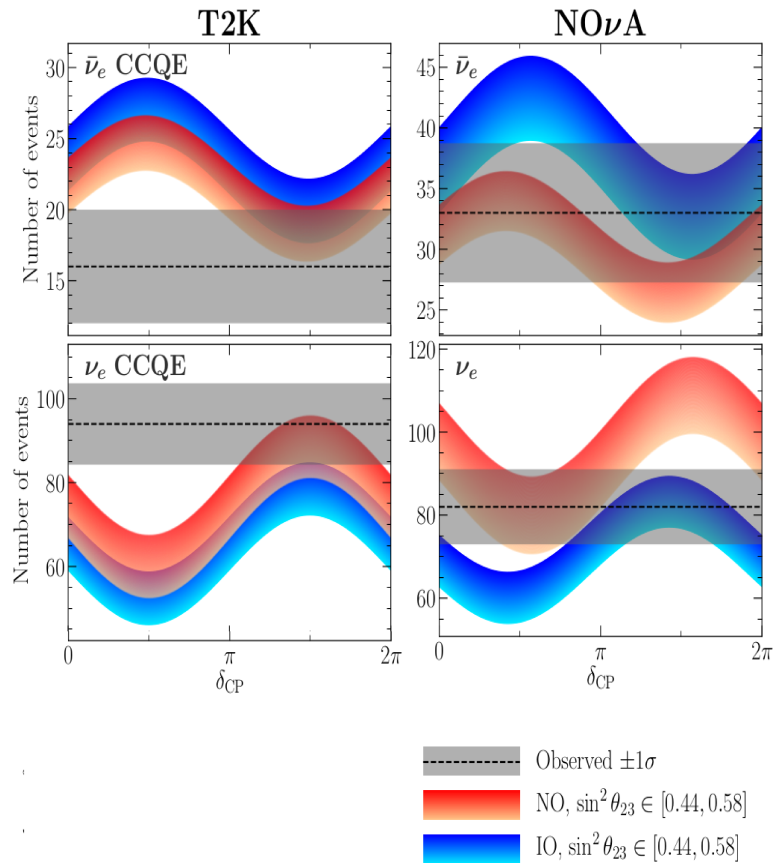
\Rightarrow IO best fit in LBL combination

\Rightarrow Each T2K and NO ν A favour **NO**

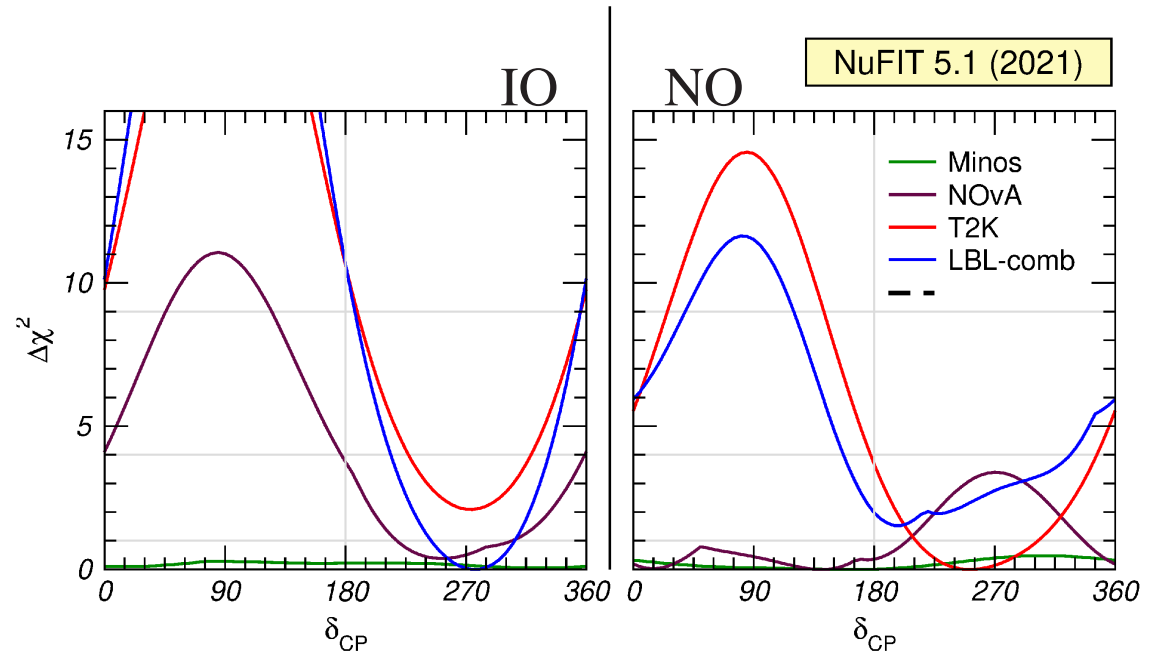
CPV and Ordering in LBL: ν_e appearance

Sanchez-Garcia

ν_e and $\bar{\nu}_e$ appearance events



But tension in favoured values of δ_{CP} in NO



⇒ IO best fit in LBL combination

● Parameter goodness-of-fit (PG) test:

	normal ordering			inverted ordering		
	χ_{PG}^2/n	p -value	$\#\sigma$	χ_{PG}^2/n	p -value	$\#\sigma$
T2K vs NOνA (θ_{13} free)	6.7/4	0.15	1.4 σ	3.6/4	0.46	0.7 σ
T2K vs NOνA (θ_{13} fix)	6.5/3	0.088	1.7 σ	2.8/3	0.42	0.8 σ

⇒ Each T2K and NOνA favour **NO**

No significant incompatibility

Ordering in LBL & Reactors

- At LBL determined in ν_μ and $\bar{\nu}_\mu$ disappearance spectrum

$$\Delta m_{\mu\mu}^2 \simeq \Delta m_{3l}^2 + \frac{c_{12}^2 \Delta m_{21}^2}{s_{12}^2 \Delta m_{21}^2} \begin{matrix} \text{NO} \\ \text{IO} \end{matrix} + \dots$$

- At MBL Reactors (Daya-Bay, Reno, D-Chooz) determined in $\bar{\nu}_e$ disapp spectrum

$$\Delta m_{ee}^2 \simeq \Delta m_{3l}^2 + \frac{s_{12}^2 \Delta m_{21}^2}{c_{12}^2 \Delta m_{21}^2} \begin{matrix} \text{NO} \\ \text{IO} \end{matrix} \quad \text{Nunokawa, Parke, Zukanovich (2005)}$$

⇒ Contribution to NO/IO from combination of LBL with reactor data

Ordering in LBL & Reactors

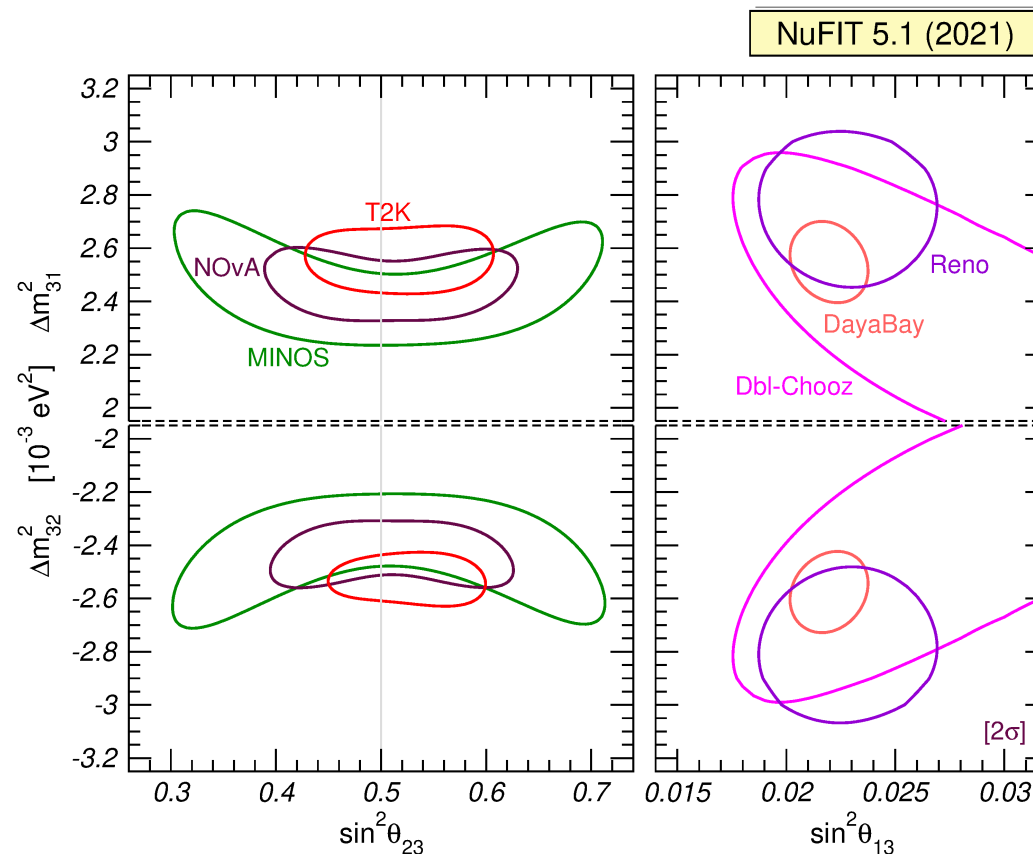
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⇒ Contribution to NO/IO from combination of LBL with reactor data



Ordering: LBL + Reactors

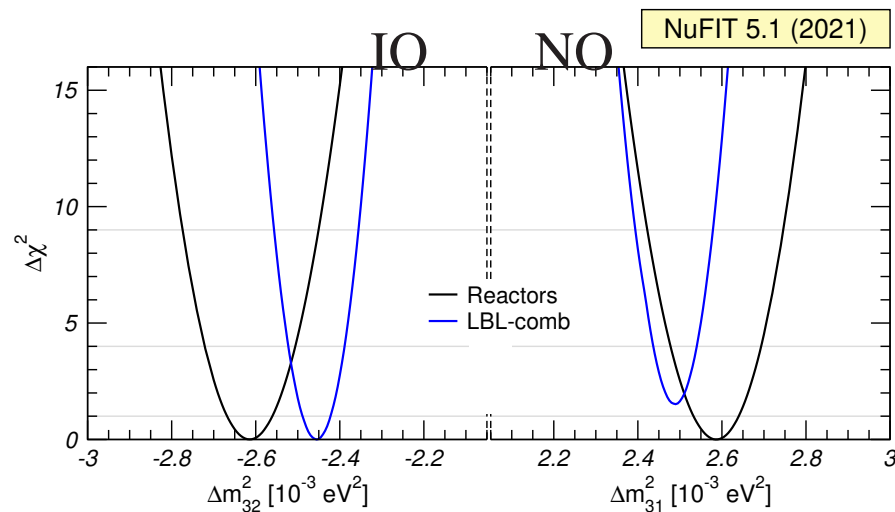
- At LBL determined in ν_μ and $\bar{\nu}_\mu$ disappearance spectrum

$$\Delta m_{\mu\mu}^2 \simeq \Delta m_{3l}^2 + \frac{c_{12}^2 \Delta m_{21}^2}{s_{12}^2 \Delta m_{21}^2} \begin{matrix} \text{NO} \\ \text{IO} \end{matrix} + \dots$$

- At MBL Reactors (Daya-Bay, Reno, D-Chooz) determined in $\bar{\nu}_e$ disapp spectrum

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⇒ Contribution to NO/IO from combination of LBL with reactor data



- T2K and $\text{NO}\nu\text{A}$ more compatible in IO ⇒ **IO** best fit in LBL combination
- LBL/Reactor complementarity in $\Delta m_{3\ell}^2$ ⇒ **NO** best fit in LBL+Reactors

Ordering & CPV: LBL + Reactors

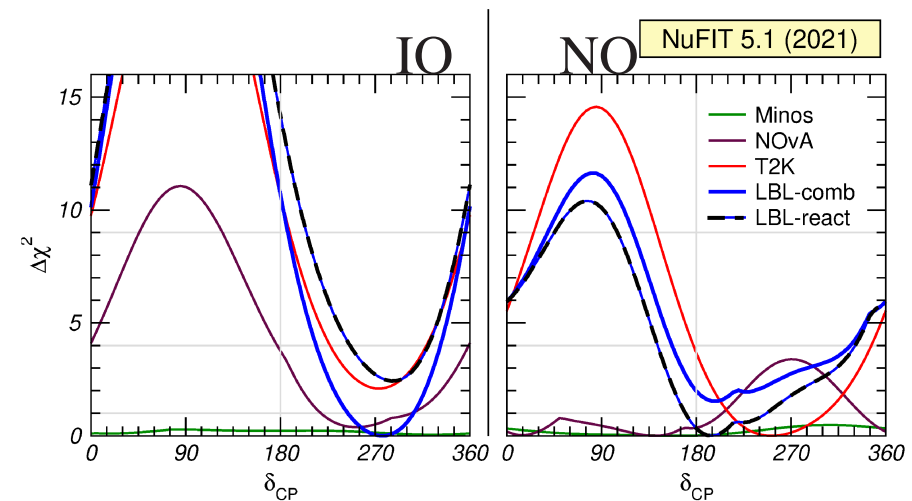
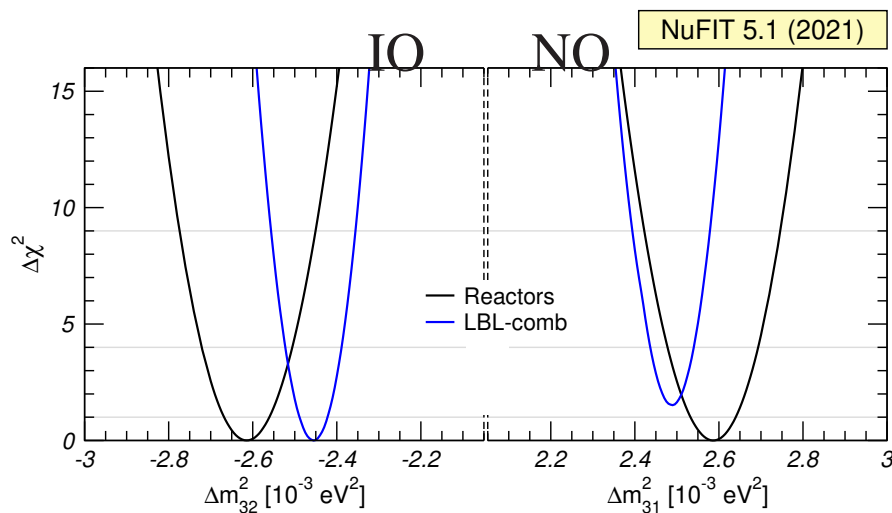
- At LBL determined in ν_μ and $\bar{\nu}_\mu$ disappearance spectrum

$$\Delta m_{\mu\mu}^2 \simeq \Delta m_{3l}^2 + \begin{matrix} c_{12}^2 \Delta m_{21}^2 & \text{NO} \\ s_{12}^2 \Delta m_{21}^2 & \text{IO} \end{matrix} + \dots$$

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$$\Delta m_{ee}^2 \simeq \Delta m_{3l}^2 + \begin{matrix} s_{12}^2 \Delta m_{21}^2 & \text{NO} \\ c_{12}^2 \Delta m_{21}^2 & \text{IO} \end{matrix} \quad \text{Nunokawa, Parke, Zukanovich (2005)}$$

⇒ Contribution to NO/IO from combination of LBL with reactor data

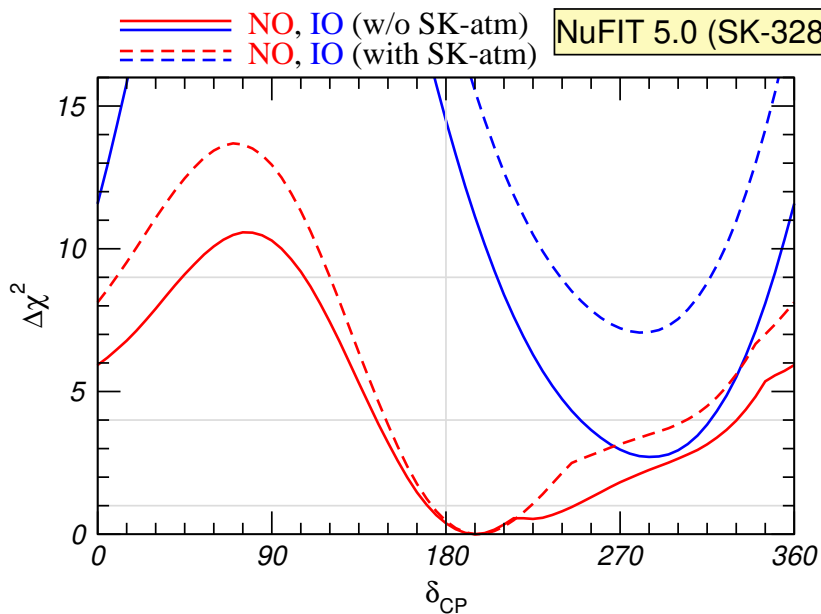


- T2K and NOνA more compatible in IO ⇒ **IO** best fit in LBL combination
- LBL/Reactor complementarity in Δm_{3l}^2 ⇒ **NO** best fit in LBL+Reactors
- **in NO**: b.f $\delta_{CP} = 195^\circ$ ⇒ CPC allowed at 0.6 σ
- **in IO**: b.f $\delta_{CP} \sim 270^\circ$ ⇒ CPC disfavoured at 3 σ

Ordering & CPV including ATM

ATM results added to global fit using SK χ^2 tables

- NUFIT 5.0: included SK I-IV 328 kton-years table
- NUFIT 5.1: include SK I-IV 372.8 kton-years table



Add SK-atm table \Rightarrow favouring of NO:

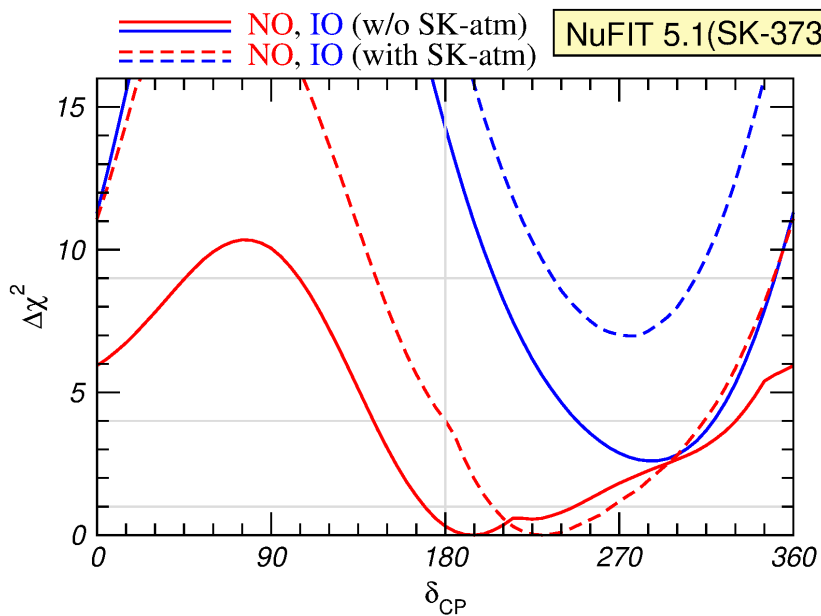
$$\Delta\chi_{\text{NO-IO}, \text{w/o SK-atm}}^2 = 2.7$$

$$\Delta\chi_{\text{NO-IO}, \text{with SK-atm}}^2 = 7.1$$

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- NUFIT 5.0: included SK I-IV 328 kton-years table
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Add either SK-atm table \Rightarrow favouring of NO:

$$\Delta\chi_{\text{NO-IO}, \text{w/o SK-atm}}^2 = 2.7$$

$$\Delta\chi_{\text{NO-IO}, \text{with SK-atm}}^2 = 7.1$$

Add new table \Rightarrow slight increase of significance of CPV in NO

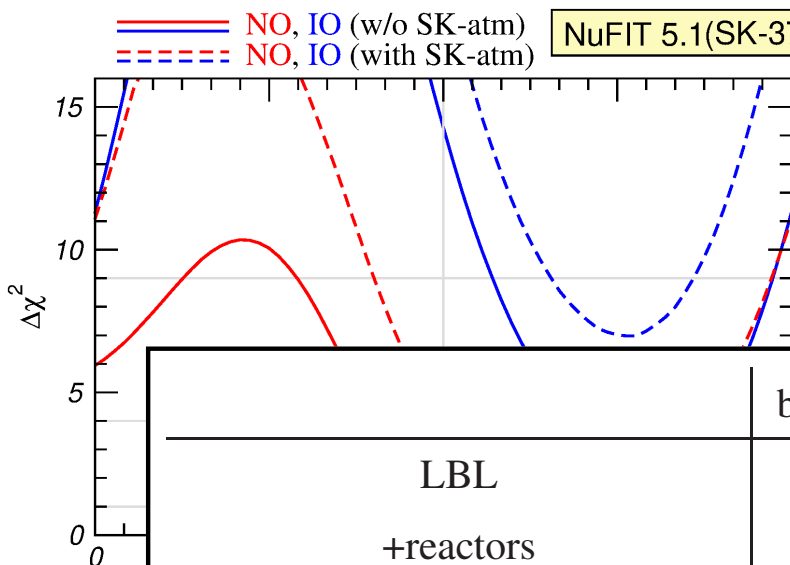
w/o SK-Atm b.f $\delta_{\text{CP}} = 195^\circ$ CPC at 0.6σ

with SK-Atm: b.f $\delta_{\text{CP}} = 230^\circ$ CPC at 2σ

Ordering & CPV including ATM

ATM results added to global fit using SK χ^2 tables

- NUFIT 5.0: included SK I-IV 328 kton-years table
- NUFIT 5.1: include SK I-IV 372.8 kton-years table



Add either SK-atm table \Rightarrow favouring of NO:

$$\Delta\chi_{\text{NO-IO, w/o SK-atm}}^2 = 2.7$$

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	best fit MO	$\Delta\chi^2(\text{MO})$	best fit δ_{CP}	$\Delta\chi^2(\text{CPC})$	oct. θ_{23}	$\Delta\chi^2(\text{oct})$
LBL	IO	1.5	275°	2.0	2nd	2.2
+reactors	NO	2.7	195°	0.4	2nd	0.5
+ SK-Atm 328 kt-y (NuFIT 5.0)	NO	7.1	197°	0.5	2nd	2.5
+ SK-Atm 373 kt-y (NuFIT 5.1)	NO	7.0	230°	4.0	1st	3.2

Near Future for CP and Ordering: Strategies

- $\nu/\bar{\nu}$ comparison with or without Earth matter effects in $\nu_\mu \rightarrow \nu_e$ & $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ at LBL: DUNE (wide band beam, L=1300 km), HK (narrow band beam, L=300 km)

$$P_{\mu e} \simeq s_{23}^2 \sin^2 2\theta_{13} \left(\frac{\Delta_{31}}{\Delta_{31} \pm V} \right)^2 \sin^2 \left(\frac{\Delta_{31} \pm V L}{2} \right) + 8 J_{CP}^{\max} \frac{\Delta_{12}}{V} \frac{\Delta_{31}}{\Delta_{31} \pm V} \sin \left(\frac{V L}{2} \right) \sin \left(\frac{\Delta_{31} \pm V L}{2} \right) \cos \left(\frac{\Delta_{31} L}{2} \pm \delta_{CP} \right)$$

$$J_{CP}^{\max} = c_{13}^2 s_{13} c_{23} s_{23} c_{12} s_{12}$$

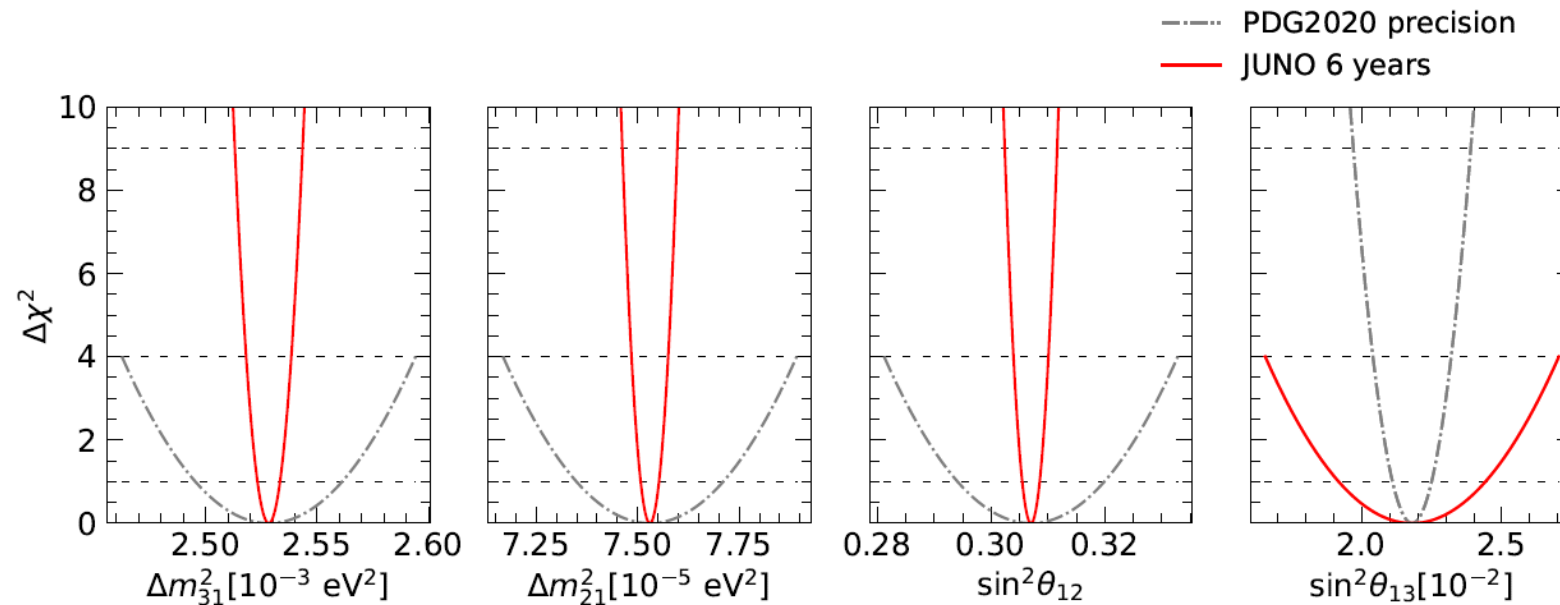
- Challenge: Parameter degeneracies, Normalization uncertainty, E_ν reconstruction
- Reactor experiment at $L \sim 50$ km (vacuum) able to observe the difference between oscillations with Δm_{31}^2 and Δm_{32}^2 : JUNO

$$P_{\nu_e, \nu_e} = 1 - c_{13}^4 \sin^2 2\theta_{12} \sin^2 \left(\frac{\Delta m_{21}^2 L}{4E} \right) - \sin^2 2\theta_{13} \left[c_{12}^2 \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right) + s_{12}^2 \sin^2 \left(\frac{\Delta m_{32}^2 L}{4E} \right) \right]$$

- Challenge: Energy resolution/scale
- Earth matter effects in large statistics ATM ν_μ disapp : HK, INO, PINGU, ORCA ...
- Challenge: ATM flux contains both ν_μ and $\bar{\nu}_\mu$, ATM flux uncertainties

JUNO: Sensitivity to Oscillation Parameters

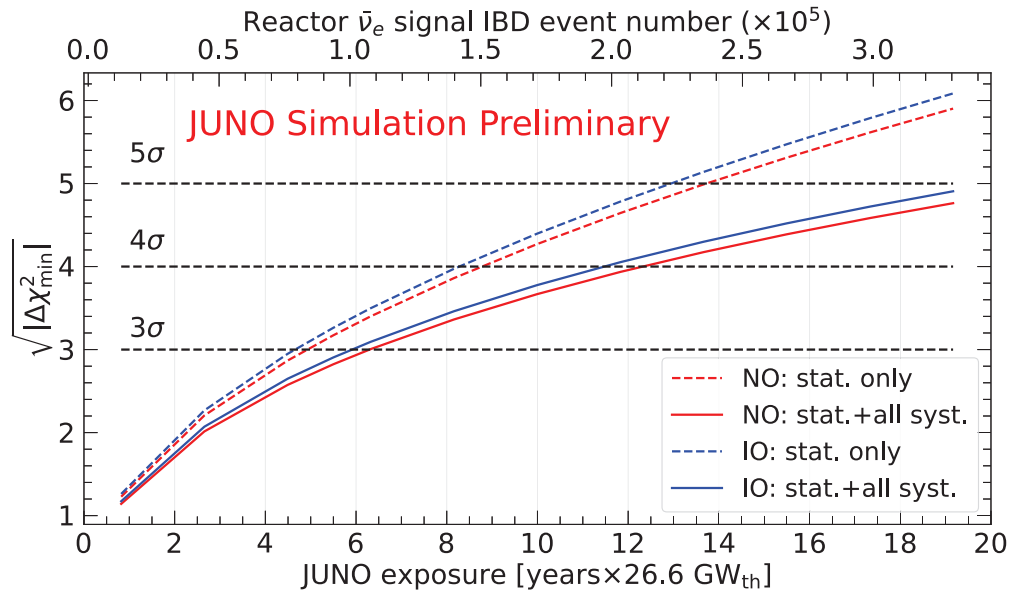
	Central Value	PDG2020	100 days	6 years	20 years
$\Delta m_{31}^2 (\times 10^{-3} \text{ eV}^2)$	2.5283	± 0.034 (1.3%)	± 0.021 (0.8%)	± 0.0047 (0.2%)	± 0.0029 (0.1%)
$\Delta m_{21}^2 (\times 10^{-5} \text{ eV}^2)$	7.53	± 0.18 (2.4%)	± 0.074 (1.0%)	± 0.024 (0.3%)	± 0.017 (0.2%)
$\sin^2 \theta_{12}$	0.307	± 0.013 (4.2%)	± 0.0058 (1.9%)	± 0.0016 (0.5%)	± 0.0010 (0.3%)
$\sin^2 \theta_{13}$	0.0218	± 0.0007 (3.2%)	± 0.010 (47.9%)	± 0.0026 (12.1%)	± 0.0016 (7.3%)



2204.13249



SENSITIVITY TO NEUTRINO MASS ORDERING



- ✓ JUNO+TAO, 6 years × 26.6 GW exposure: $\sim 3\sigma$
- ✓ +1% external constrain on Δm_{32}^2 : $> 4\sigma$
- ✓ combined with accelerator/atmospheric experiment: $> 5\sigma$
 ↳ sensitivity boost due to tension for wrong ordering

Impact of systematics:

	$\Delta\chi^2_{\min}$	stat. + 1 syst.
Statistics	11.3	
Stat.+Flux error	-0.6	
Stat.+Backgrounds	-1.4	
Stat.+Nonlinearity	-0.4	
Stat.+Others	< -0.05	
Total	9.0	

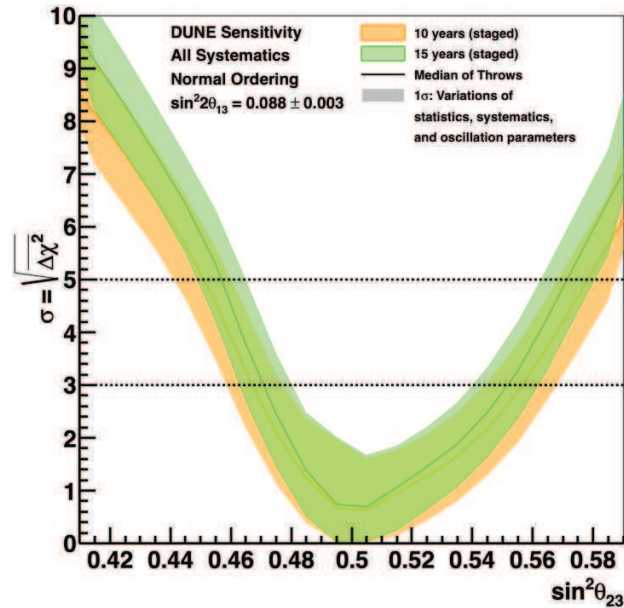
JUNO Simulation Preliminary

- Paper under preparation.
- Combination of reactor and atmospheric channels within JUNO is investigated.

▶ Extra [2008.11280], JUNO+IceCube [1911.06745]

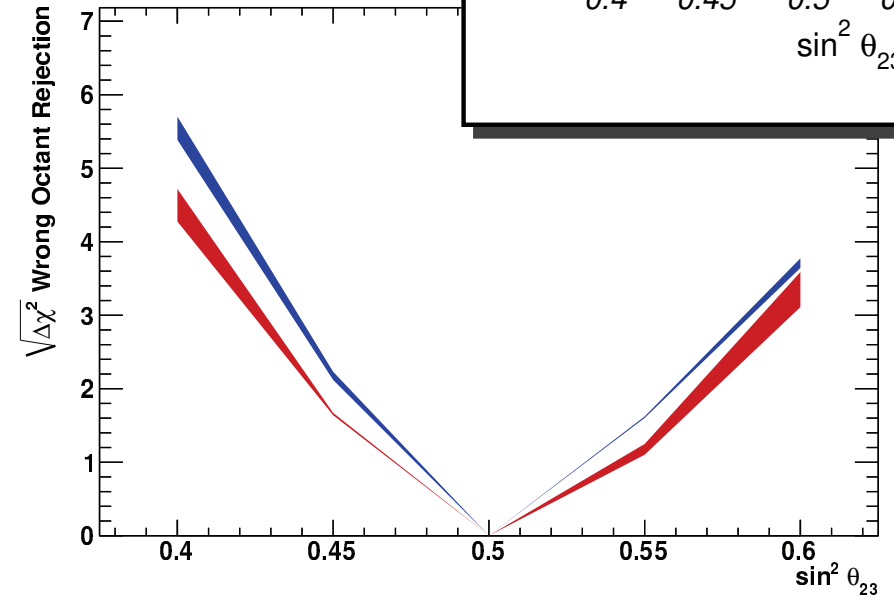
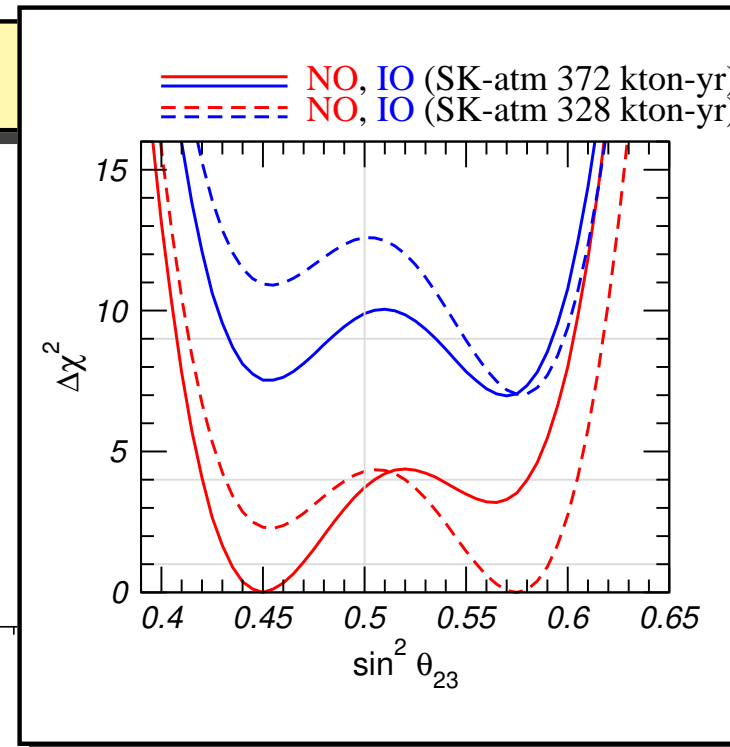
DUNE & Hyper-Kamiokande: θ_{23}

θ_{23} octant: future sensitivities



$\sim 3 - 5\sigma$

DUNE 2002.03005



Beam+Atm $\Rightarrow \sim 3 - 6\sigma$

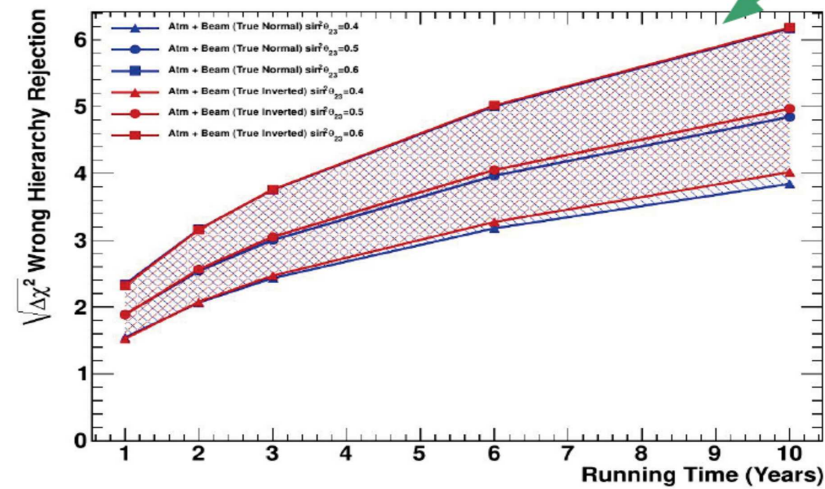
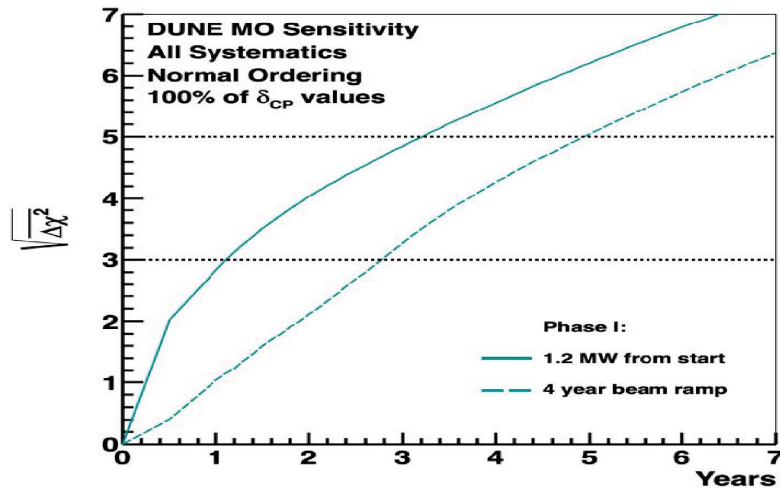
HK 1805.04163

DUNE & Hyper-Kamiokande: CPV and MO

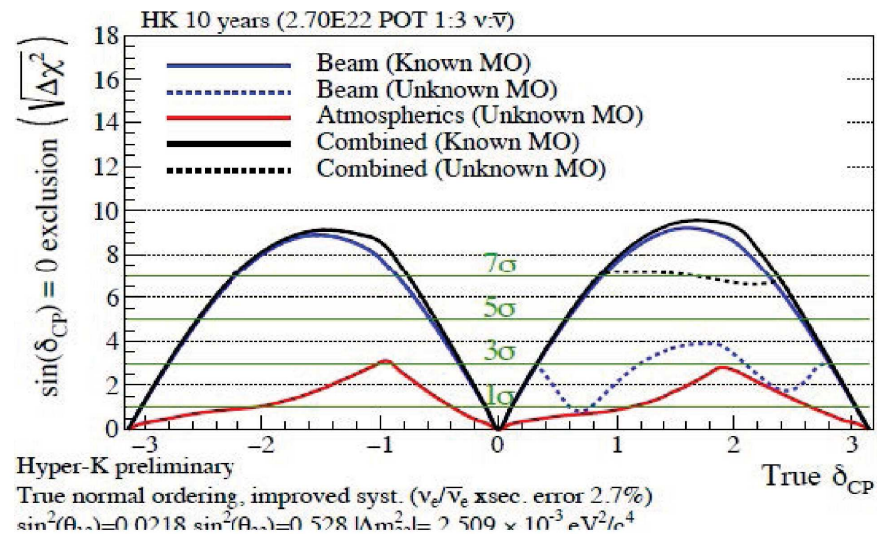
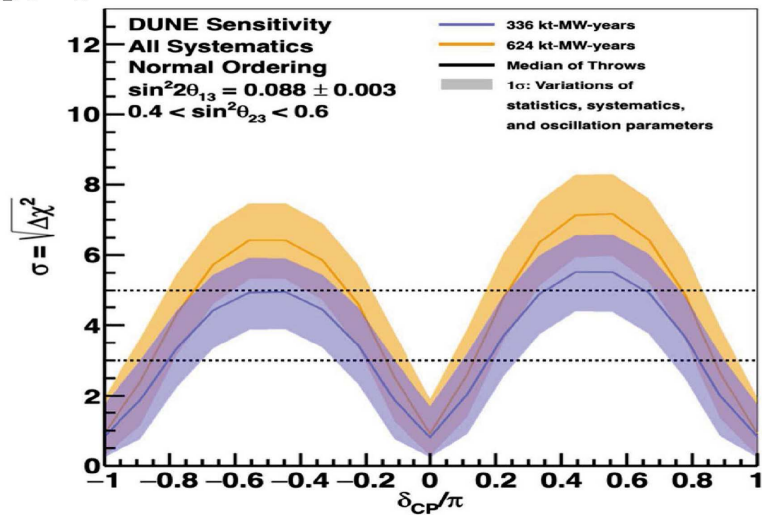
Mass Ordering

DUNE

Hyper-Kamiokande



CPV



- SM extension with additional singlets

- Lepton-mixing Unitarity: $K_l K_l^\dagger + K_h K_h^\dagger = I_{3 \times 3} \Rightarrow$ generic relation between NHL couplings (K_h) and flavour param. and unit. violation of active ν_l (K_l)
- Canonical see-saw: Unitarity violation in the light sector unobservably small
- In more general see-saw-I scenarios: Experimental bounds
 - \Rightarrow Unitarity violation can still be ignored in present $3\nu_l$ oscillation analysis
- Model dependent correlation between $3\nu_l$ parameters and NHL couplings
Maximal correlation in minimal (Lepton Flavour Violating) See-saws

- Status of 3ν fit

- Robust determination of $\theta_{12}, \theta_{13}, \Delta m_{21}^2, |\Delta m_{3\ell}^2|$
- Mass ordering, θ_{23} Octant, CPV depend on subdominant 3ν -effects
 \Rightarrow interplay of LBL/reactor/ATM results

	best fit MO	$\Delta\chi^2(\text{MO})$	best fit δ_{CP}	$\Delta\chi^2(\text{CPC})$	oct. θ_{23}	$\Delta\chi^2(\text{oct})$
LBL	IO	1.5	275°	2.0	2nd	2.2
+reactors	NO	2.7	195°	0.4	2nd	0.5
+ SK-Atm 328 kt-y (NuFIT 5.0)	NO	7.1	197°	0.5	2nd	2.5
+ SK-Atm 373 kt-y (NuFIT 5.1)	NO	7.0	230°	4.0	1st	3.2

\Rightarrow not statistically significant yet

\Rightarrow definitive answer from upcoming experiments

Summary: Global 3 ν Flavour Parameters

Evolution of global 3 flavour fit

Gonzalez-Garcia, Maltoni, TS [arXiv:2111.03086]

	2012	2014	2016	2018	2021	
	NuFIT 1.0	NuFIT 2.0	NuFIT 3.0	NuFIT 4.0	NuFIT 5.1	
θ_{12}	15%	14%	14%	14%	14%	1.07
θ_{13}	30%	15%	11%	8.9%	9.0%	3.3
θ_{23}	43%	32%	32%	27%	27%	1.6
Δm_{21}^2	14%	14%	14%	16%	16%	0.88
$ \Delta m_{3\ell}^2 $	17%	11%	9%	7.8%	6.7% [6.5%]	2.5
δ_{CP}	100%	100%	100%	100% [92%]	100% [83%]	1 [1.2]
$\Delta\chi_{IO-NO}^2$	± 0.5	-0.97	+0.83	+4.7 [+9.3]	+2.6 [+7.0]	

w/o [w] SK atm data

relat. precision at 3σ : $\frac{2(x^+ - x^-)}{(x^+ + x^-)}$

improvement factor from 2012 to 2021

Summary: Global 3 ν Flavour Parameters

Global 6-parameter fit <http://www.nu-fit.org>

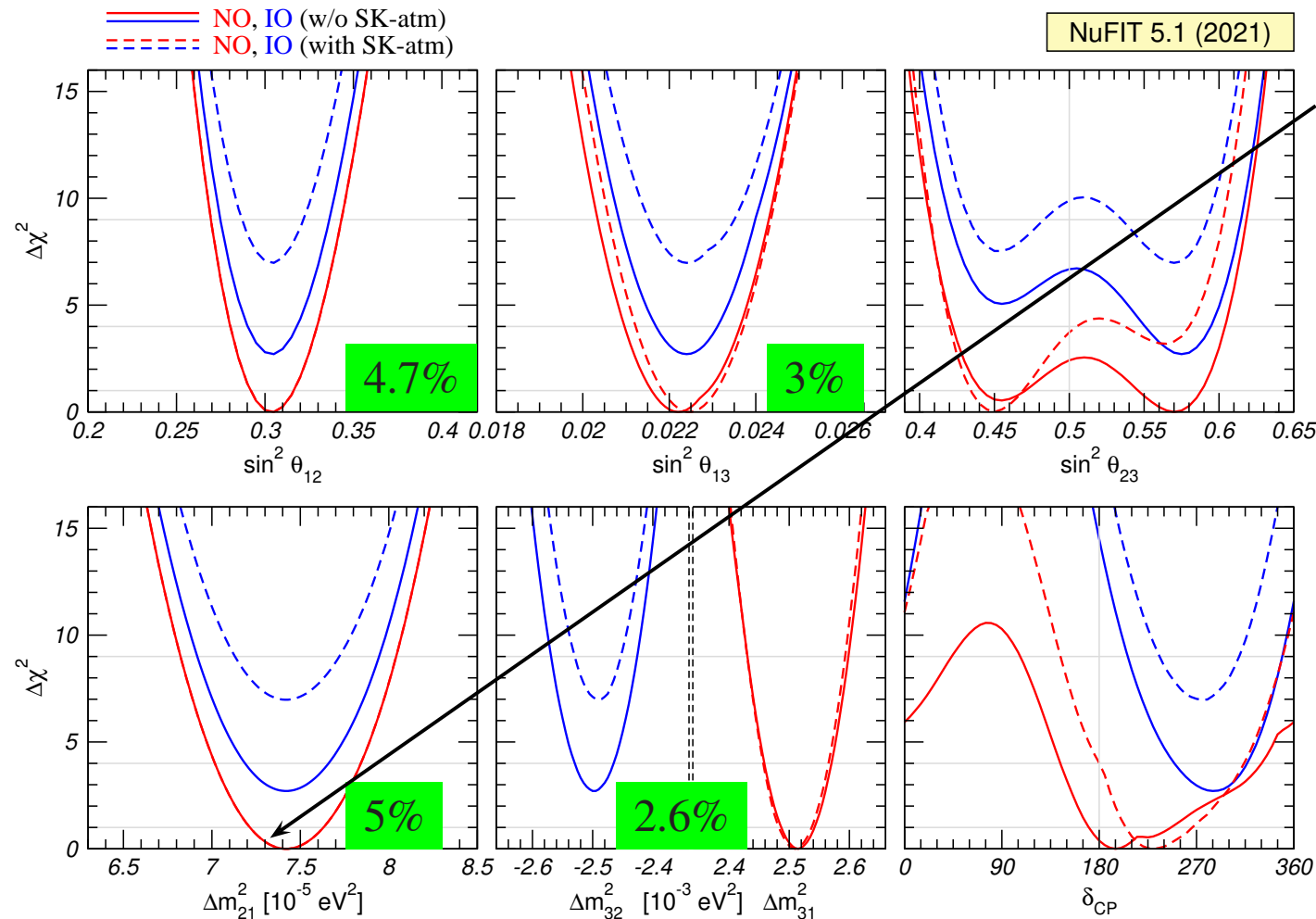
Esteban, G-G, Maltoni, Schwetz, Zhou, JHEP'20 [2007.14792], G-G, Maltoni, Schwetz, 2111.03086

• 4 well-known parameters:

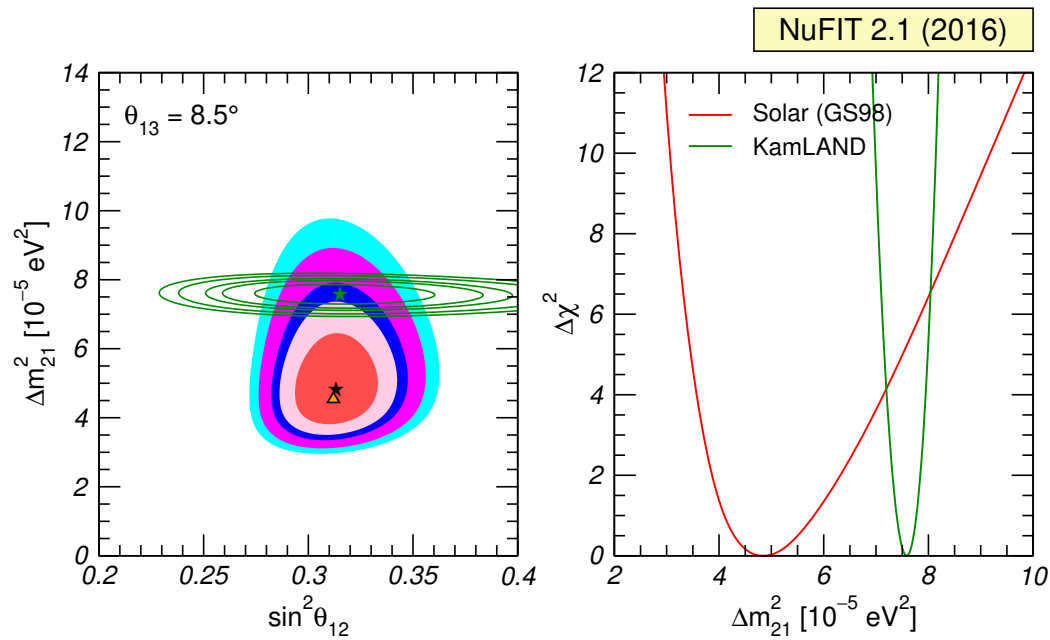
$\theta_{12}, \theta_{13}, \Delta m_{21}^2, |\Delta m_{3\ell}^2|$

Δm_{21}^2 Solar vs KLAND

Tension Resolved



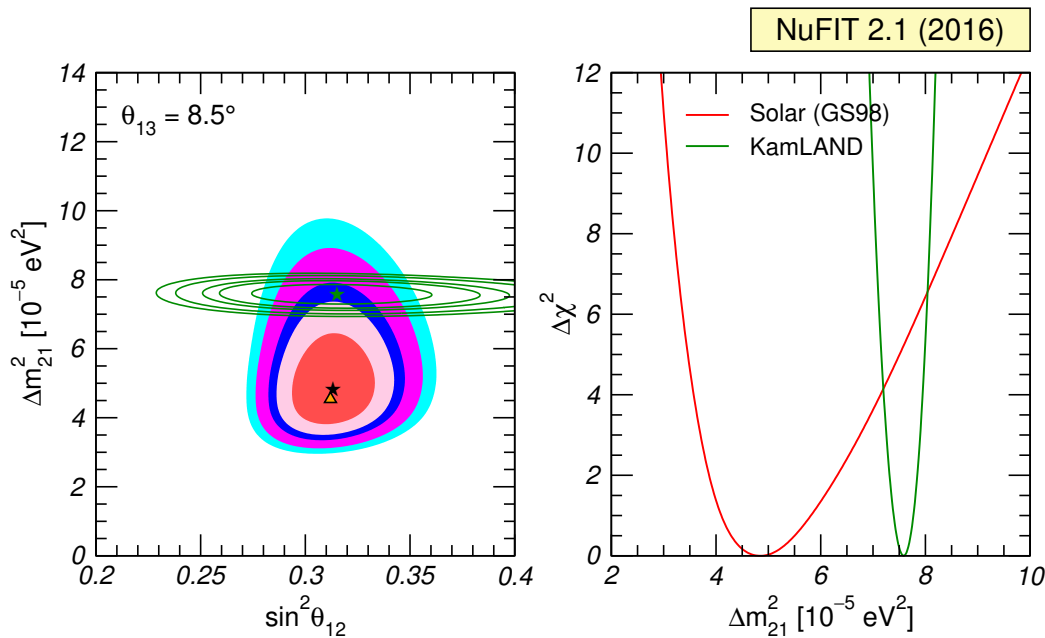
- Last decade: after including $\theta_{13} \simeq 9^\circ$ the comparison of KamLAND vs Solar



θ_{12} better than 1σ agreement

But $\sim 2\sigma$ tension on Δm_{12}^2

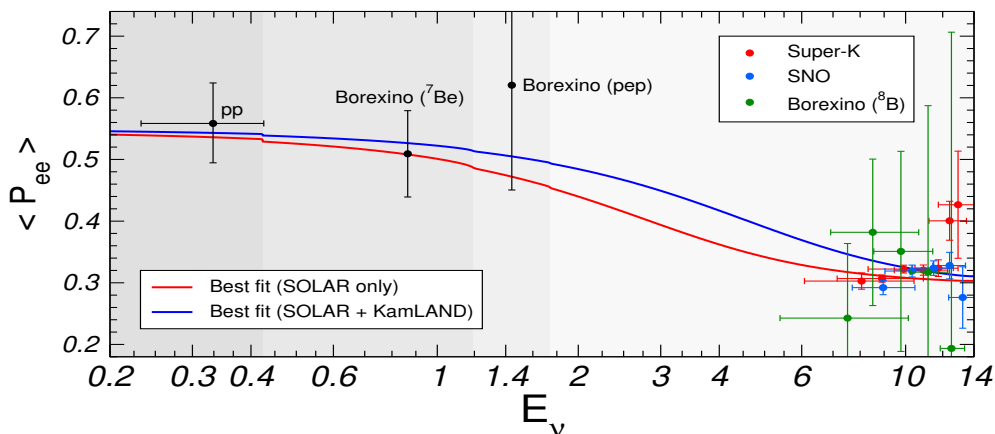
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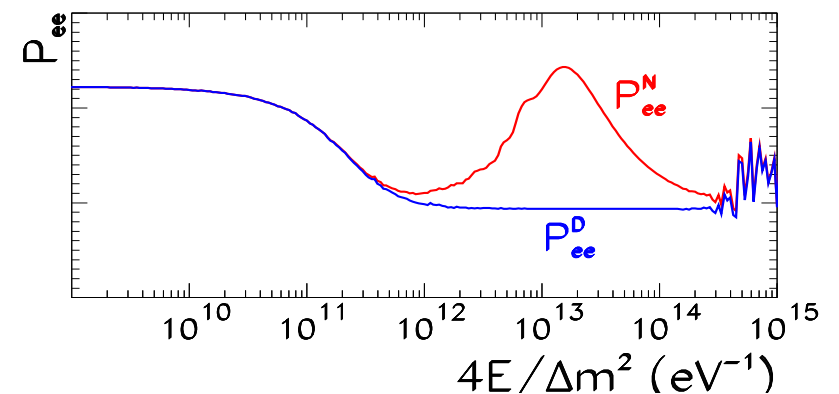
- Tension arising from:

Smaller-than-expected MSW low-E turn-up
 in SK/SNO spectrum at global b.f.

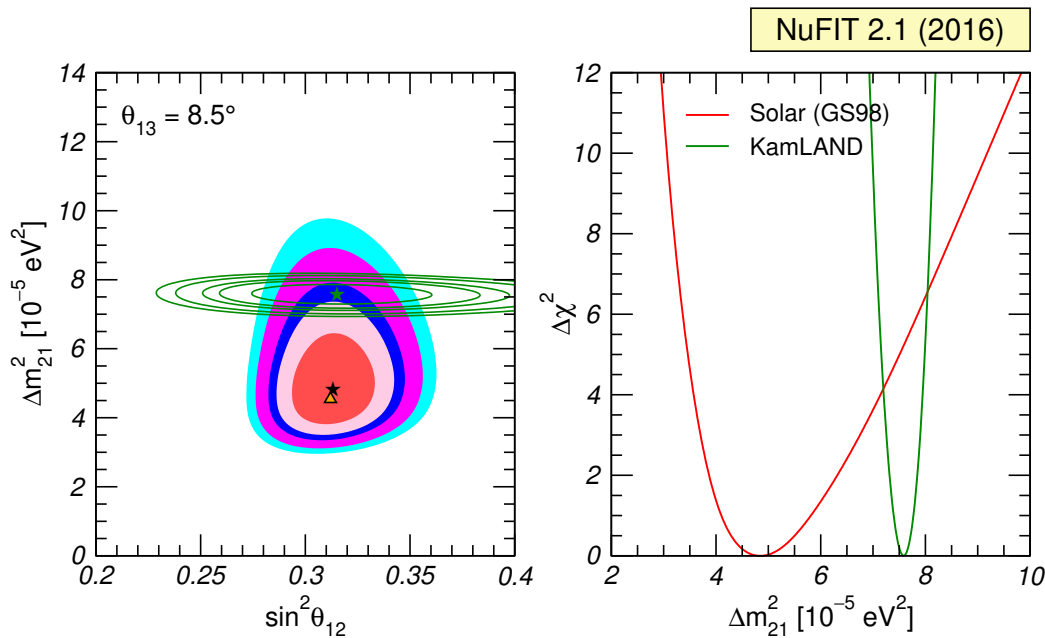


“too large” of Day/Night at SK

$$A_{D/N,SK4-2055} = [-3.1 \pm 1.6(\text{stat.}) \pm 1.4(\text{sys.})]\%$$



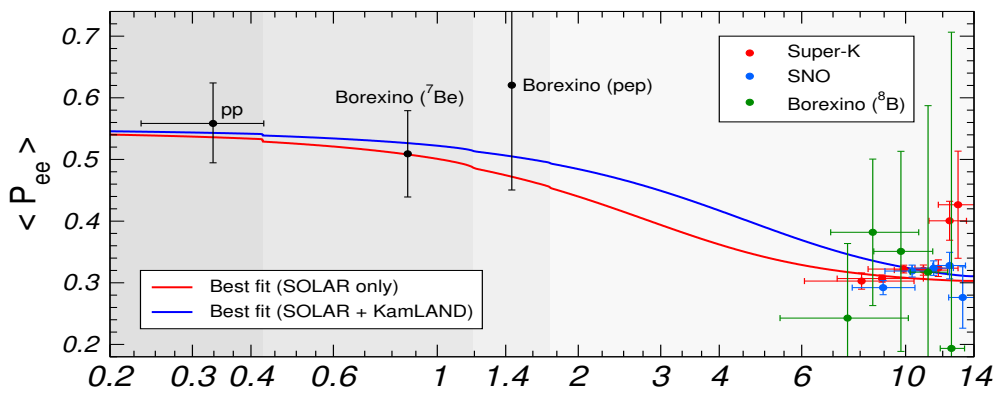
- Last decade: after including $\theta_{13} \simeq 9^\circ$ the comparison of KamLAND vs Solar



θ_{12} better than 1σ agreement
 But $\sim 2\sigma$ tension on Δm_{12}^2

- Tension arising from:

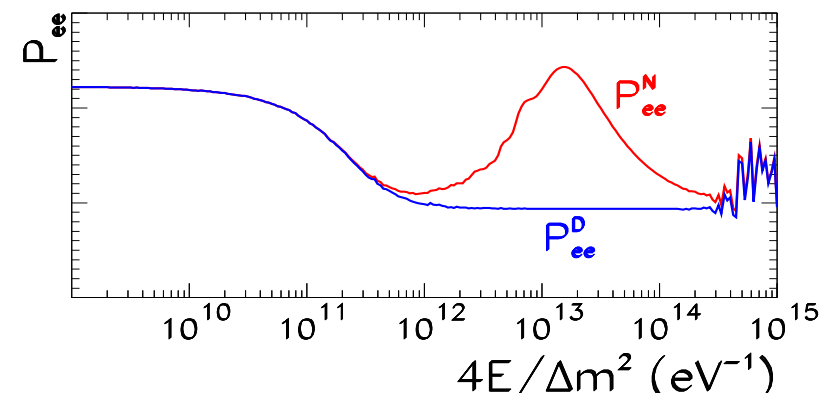
Smaller-than-expected MSW low-E turn-up in SK/SNO spectrum at global b.f.



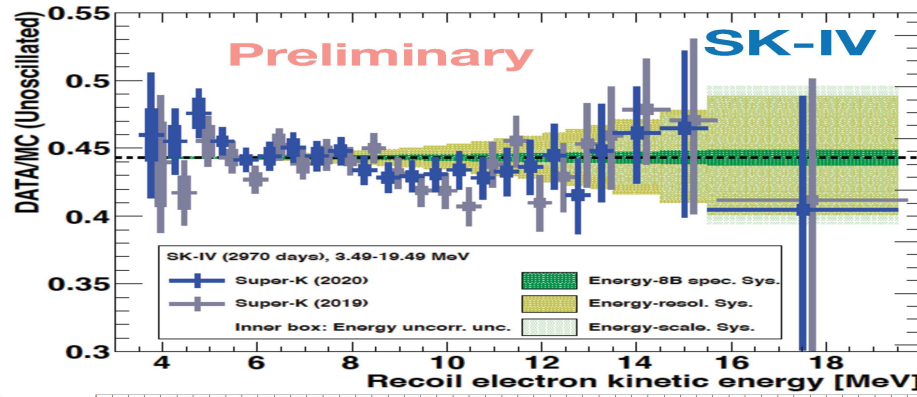
\Rightarrow “hint” of NP in propagation: NSI?

“too large” of Day/Night at SK

$$A_{D/N,SK4-2055} = [-3.1 \pm 1.6(\text{stat.}) \pm 1.4(\text{sys.})]\%$$



- AFTER NU2020: With SK4 2970 days data
Slightly more pronounced low-E turn-up

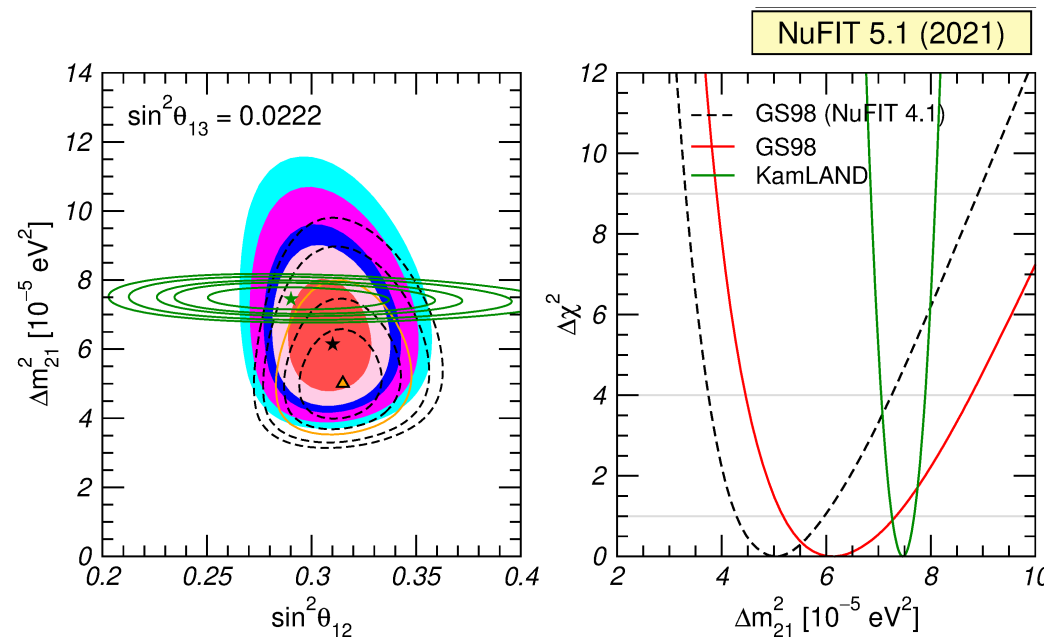


Smaller of Day/Night at

$$A_{D/N,SK4-2055} = [-3.1 \pm 1.6(\text{stat.}) \pm 1.4(\text{sys.})]\%$$

$$A_{D/N,SK4-2970} = [-2.1 \pm 1.1]\%$$

- In NuFIT 5.1

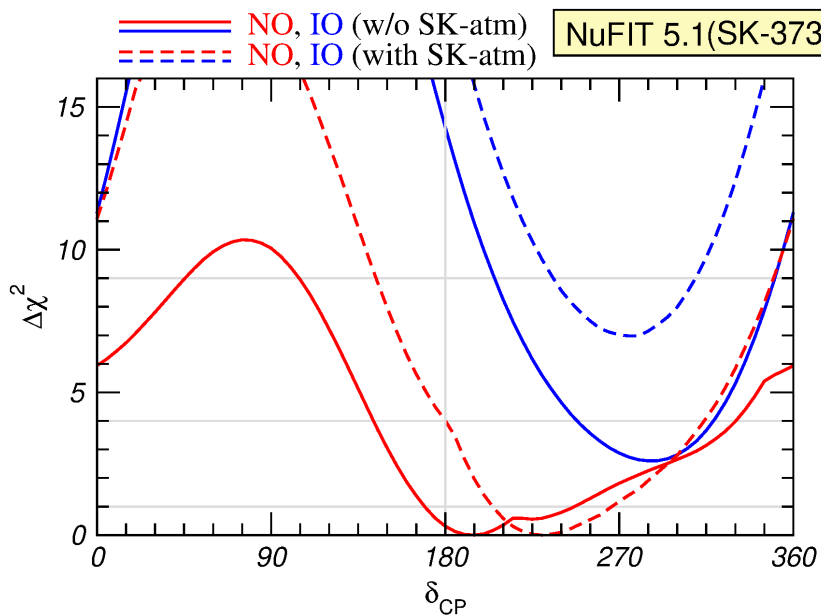


⇒ Agreement of Δm_{21}^2 between solar and KamLAND at 1σ

Ordering & CPV including ATM

ATM results added to global fit using SK χ^2 tables

- NUFIT 5.0: included SK I-IV 328 kton-years table
- NUFIT 5.1: include SK I-IV 372.8 kton-years table



Add either SK-atm table \Rightarrow favouring of NO:

$$\Delta\chi_{\text{NO-IO}, \text{w/o SK-atm}}^2 = 2.7$$

$$\Delta\chi_{\text{NO-IO}, \text{with SK-atm}}^2 = 7.1$$

Add new table \Rightarrow slight increase of significance of CPV in NO

w/o SK-Atm b.f $\delta_{\text{CP}} = 195^\circ$ CPC at 0.6σ

with SK-Atm: b.f $\delta_{\text{CP}} = 230^\circ$ CPC at 2σ

Ordering & CPV including ATM

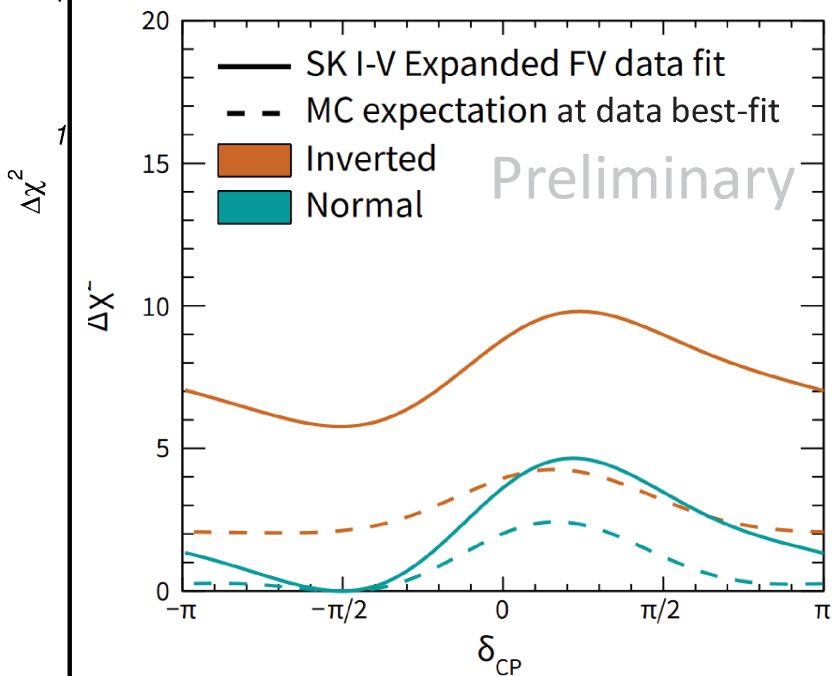
ATM results added to global fit using SK χ^2 tables

- NUFIT 5.0: included SK I-IV 328 kton-years table

- NUFIT 5.1: include SK I-IV 372.8 kton-years table

Expected impact of SK-V

(373 \rightarrow 484 kt.yr)



Favouring of NO and CPV
increases beyond expectation

either SK-atm table \Rightarrow favouring of NO:

$$\Delta\chi_{\text{NO-IO, w/o SK-atm}}^2 = 2.7$$

$$\Delta\chi_{\text{NO-IO, with SK-atm}}^2 = 7.1$$

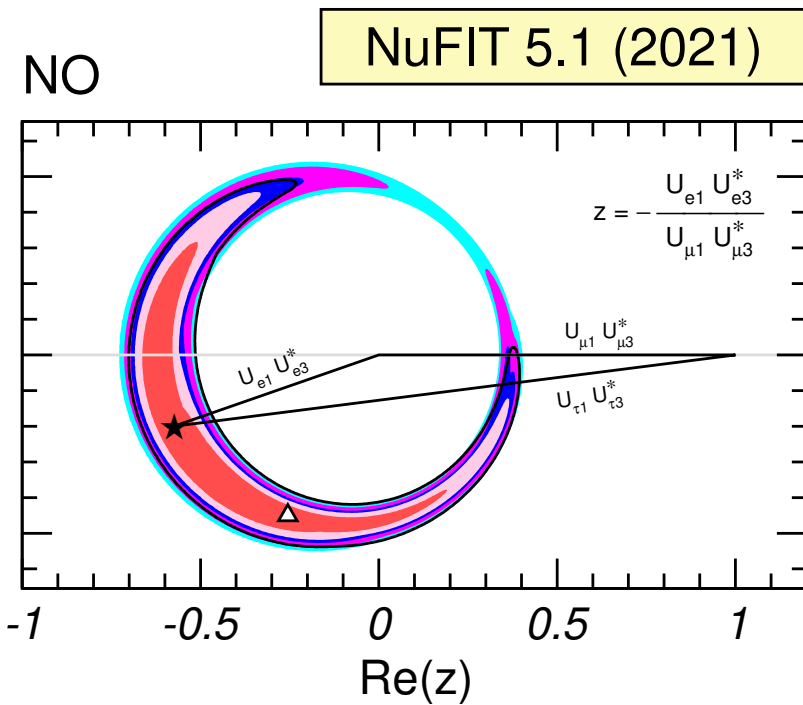
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3ν Mixing: Leptonic Unitarity Triangle

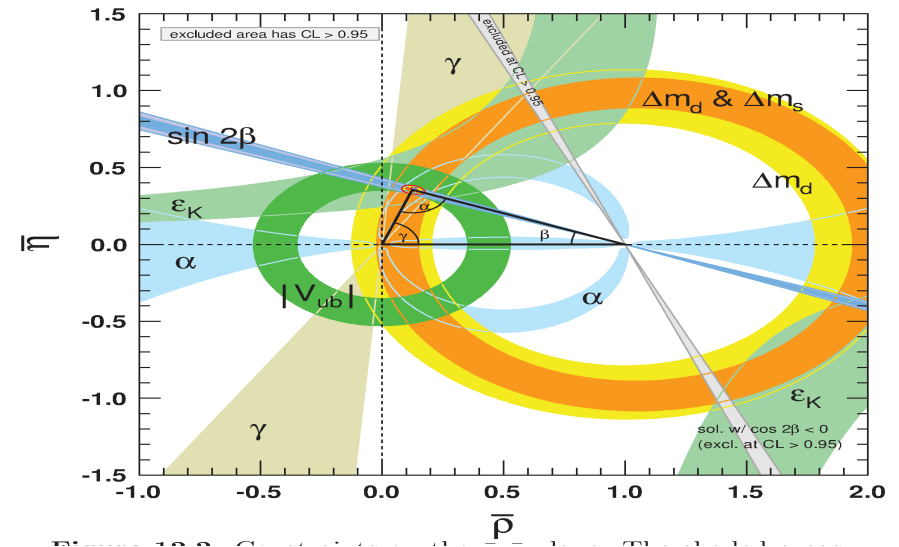
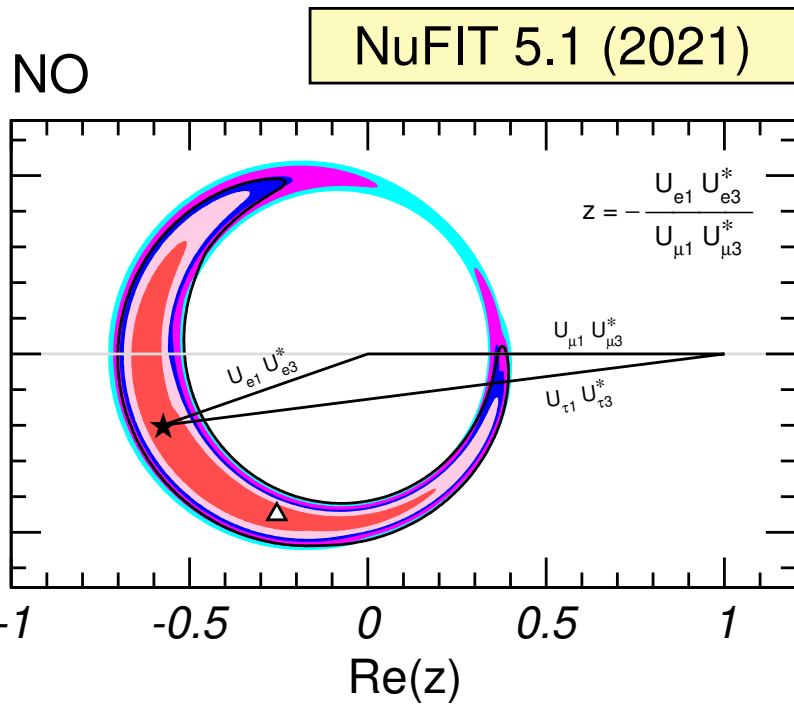
Unitarity triangle in lepton sector



3ν Mixing: Leptonic Unitarity Triangle

Unitarity triangle in lepton sector

The equivalent in the quark sector

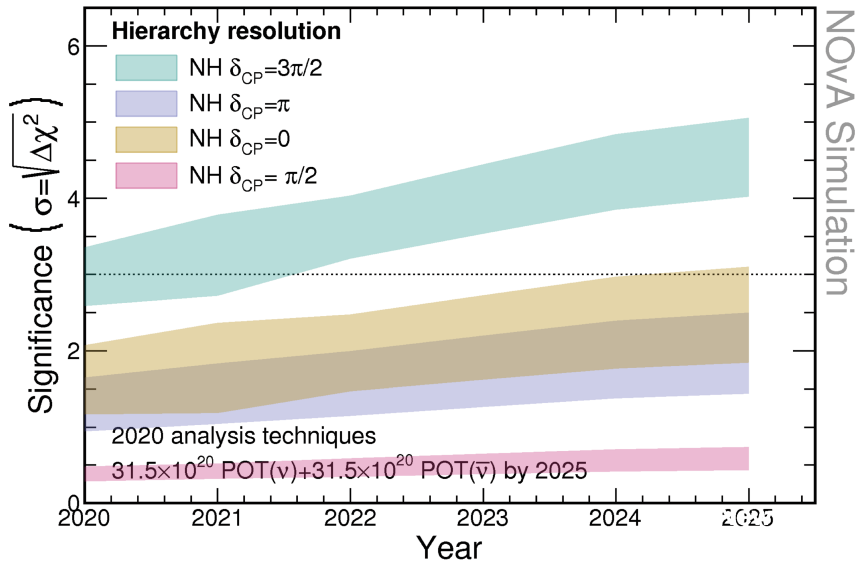


“Near Future” for CPV and Ordering

NOνA: Ordering

A priori NOνA sensitivity to Mass Hierarchy vs. time

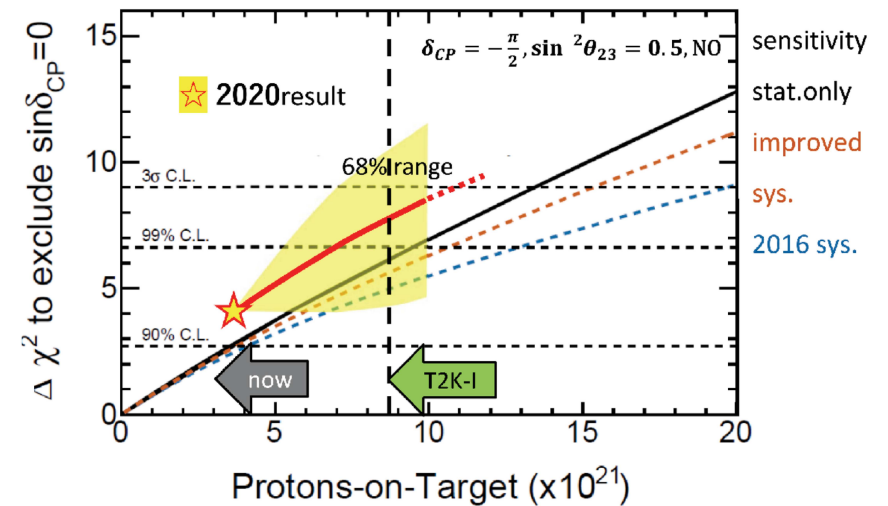
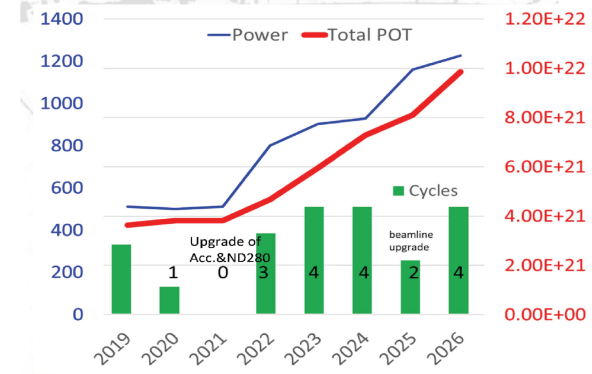
$$\sin^2\theta_{23}=0.45-0.60, \Delta m_{32}^2=+2.40 \times 10^{-3} \text{eV}^2, \sin^2\theta_{13}=0.085$$



NOνA reaches 3 sigma sensitivity for between 30% and 50% of δ_{CP} values, depending on MH and $\sin^2(\theta_{23})$

T2K: CPV

Estimation POT



To be further improved by ND280 upgrade etc. If CP is maximally violated, we have a good chance to reach 3 σ .

From F.Sanchez snowmass talk