

Bounds on Right-Handed Neutrino Parameters from Observable Leptogenesis

Based on [[2207.01651](#)]

Pilar Hernandez, Jacobo López-Pavón, Nuria Rius and [Stefan Sandner](#)*

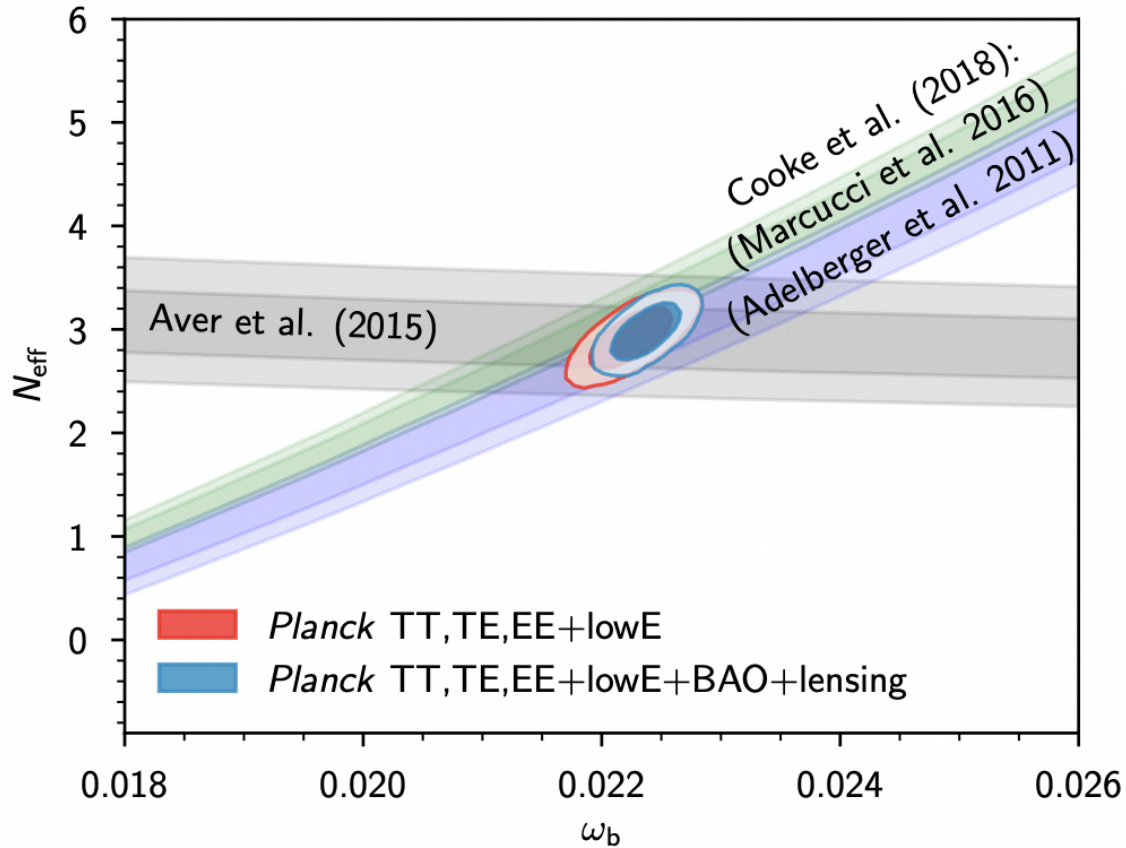
*stefan.sandner@ific.uv.es

Feebly-Interacting Particles, October 17 - 21 2022

Prerequisite I - baryon asymmetry

Baryon asymmetry

Quantified via baryon to entropy density: $Y_B \equiv n_B/s = \frac{6.95 \times 10^{-9}}{2 + 0.8375 \times N_{eff}^{3/4}} \omega_b$



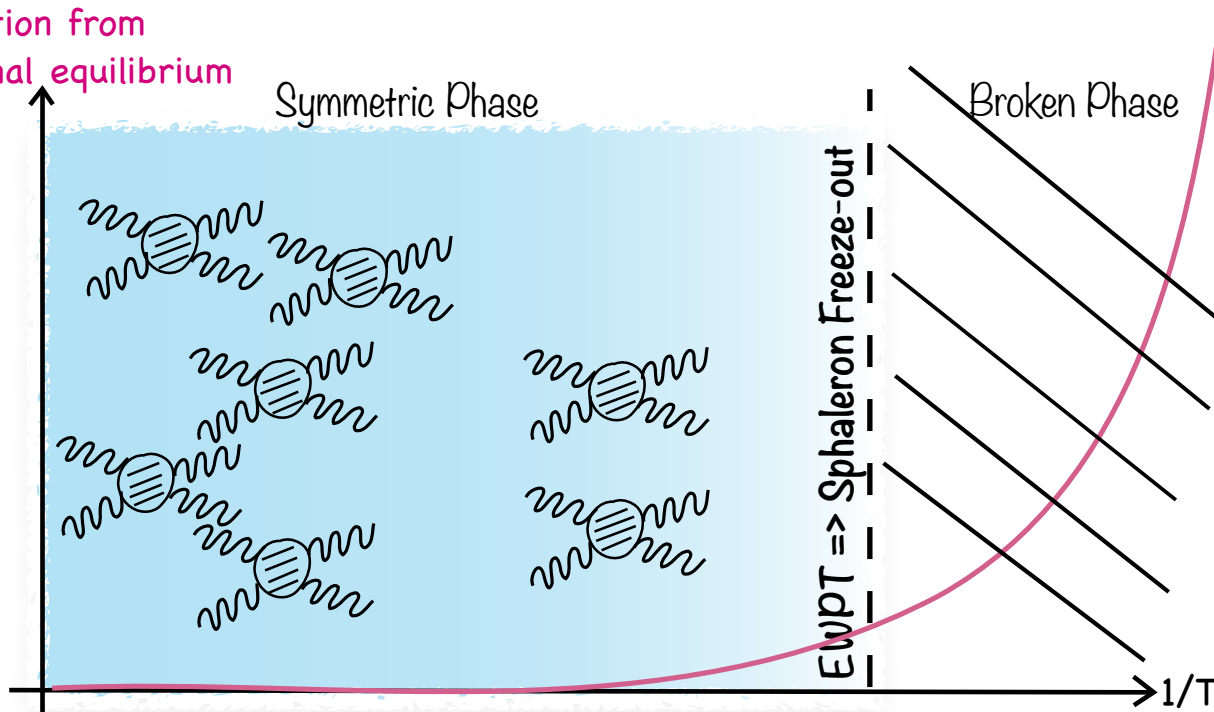
Every (dynamical) model needs to explain $Y_B|_{\text{today}} = (8.66 \pm 0.01) \times 10^{-11}$

Baryon asymmetry

Dynamical creation is fundamentally constrained => **Sakharov Conditions**

- * Baryon number violation
- * C & CP violation
- * Deviation from thermal equilibrium

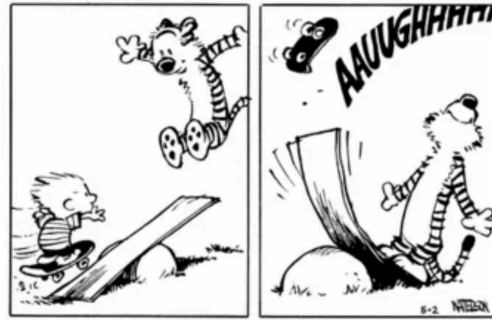
Deviation from
thermal equilibrium



Prerequisite II - neutrino masses

Neutrino masses

light active neutrino



heavy neutral leptons

The possible Majorana nature of the neutrinos leads to the **See-Saw** framework!
 We will focus on the minimal scenario with 2 heavy neutral leptons (HNLs)

Large mixings (U^2) between active neutrinos and HNLs are achieved via an **approximate lepton number** symmetry

$$Y = (\underline{y}, \underline{0}) + (\underline{0}, \underline{y}')$$

$$M = \begin{pmatrix} 0 & \Lambda \\ \Lambda & 0 \end{pmatrix} + \text{diag}(\mu)$$

$$y' \ll y, \mu \ll \Lambda$$

$$U^2 \simeq y^2 \frac{v^2}{M^2}$$

$$m_\nu = f(y'/y, \mu/\Lambda)$$

$$\Delta M = 2\mu$$

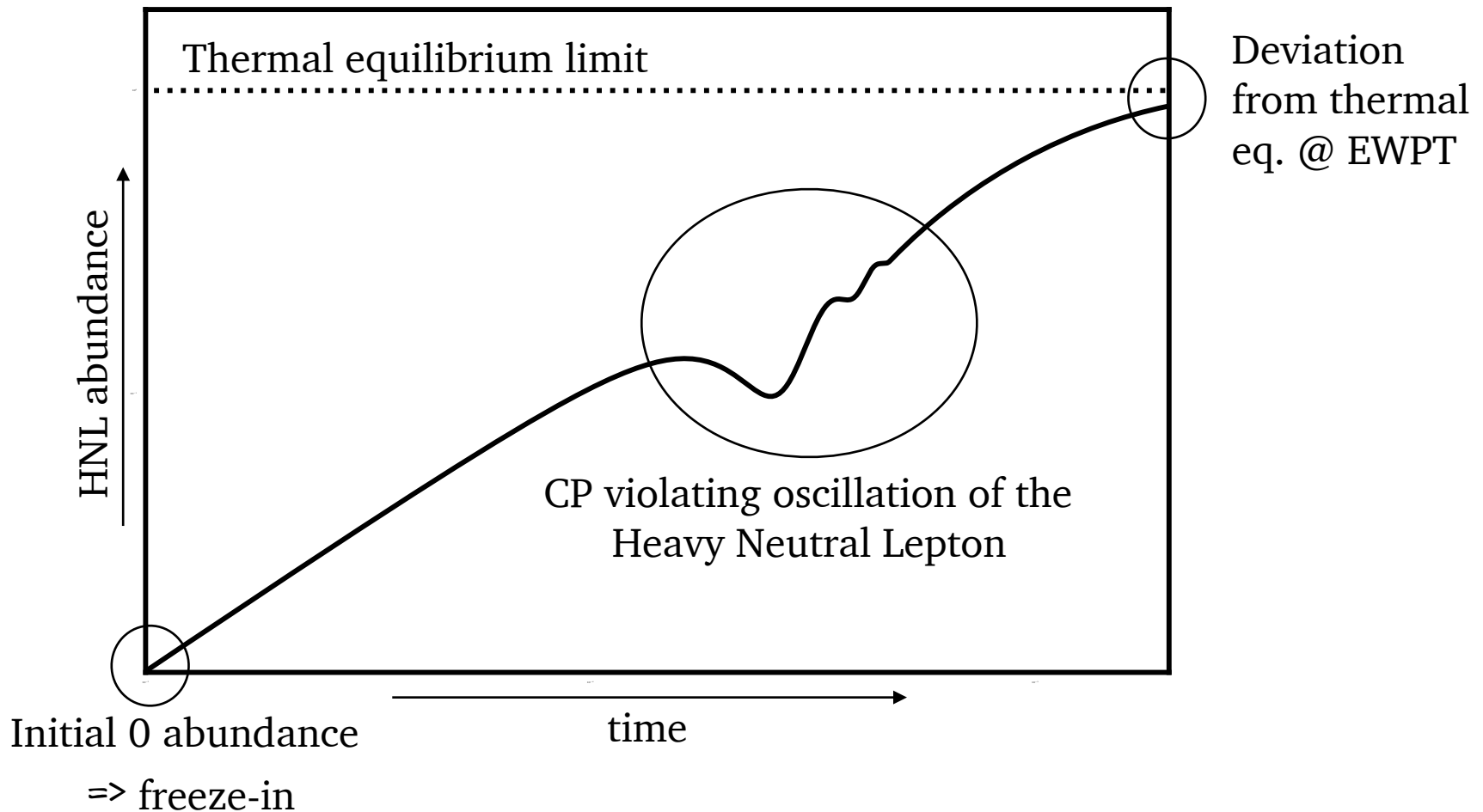
Leptogenesis

Baryon asymmetry

Neutrino masses



Leptogenesis via oscillations



Leptogenesis via oscillations

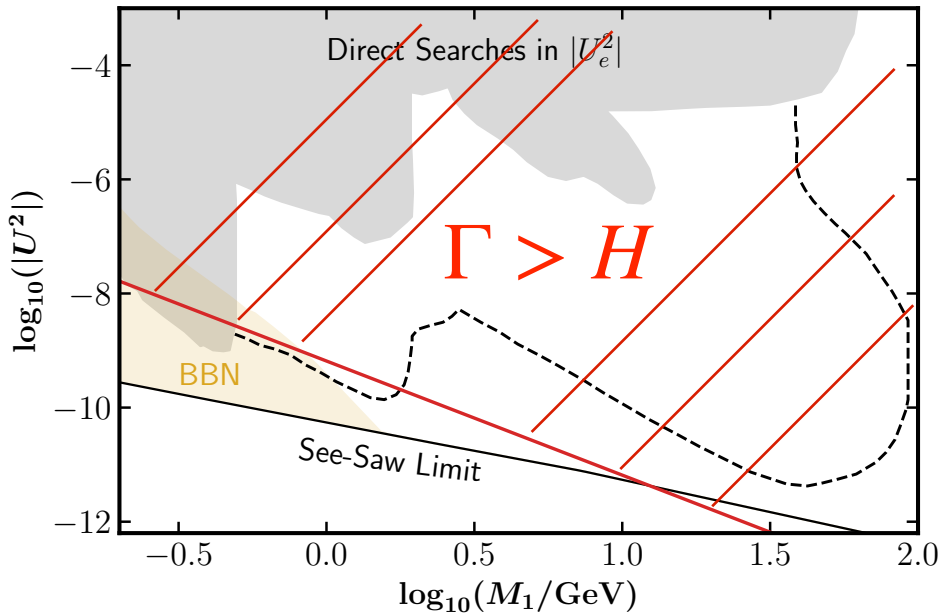
Quantification of the asymmetry via quantum Boltzmann equation

$$\dot{\rho} = -i[H, \rho] - \frac{1}{2}\{\Gamma^a, \rho\} + \frac{1}{2}\{\Gamma^p, \rho_{eq} - \rho\}$$

Quantum
density matrix

CP violating
oscillations $H \propto \Delta M_{ij}^2/k_0$

Thermalization
efficiency $\Gamma^{a,p} \propto YY^\dagger T$



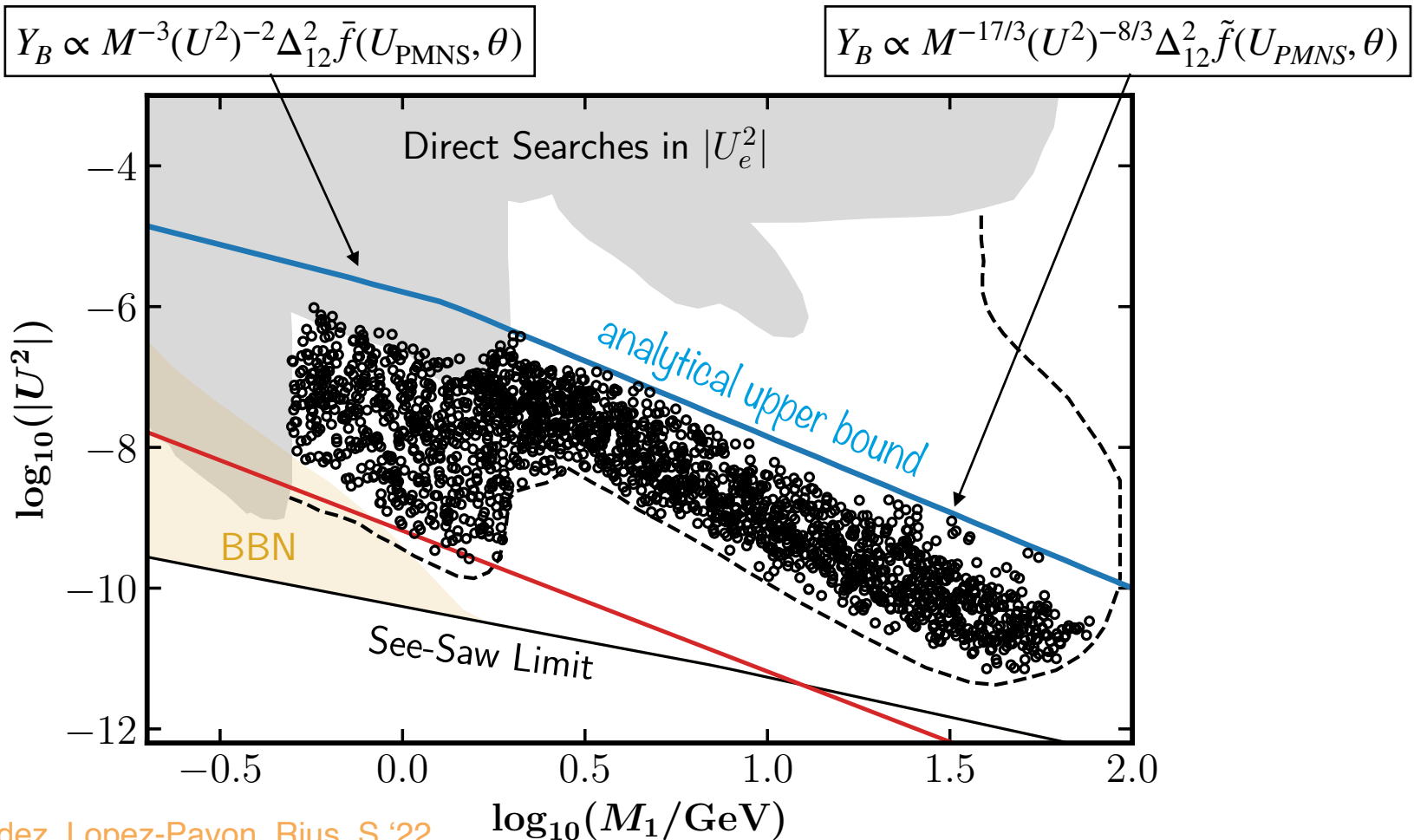
Estimated equilibration rate at EWPT

$$\Gamma \propto U^2 \frac{M^2}{v^2} T_{EW} \lesssim H = T_{EW}^2 / M_p^*$$

Damped oscillations

If oscillations are damped $\Gamma_{osc}^{slow} \simeq P_{osc} \Gamma \lesssim H$ is realizable until EWPT

Adiabatic perturbation around $\Gamma_{osc}/\Gamma \ll 1$ leads to **analytical upper bound**

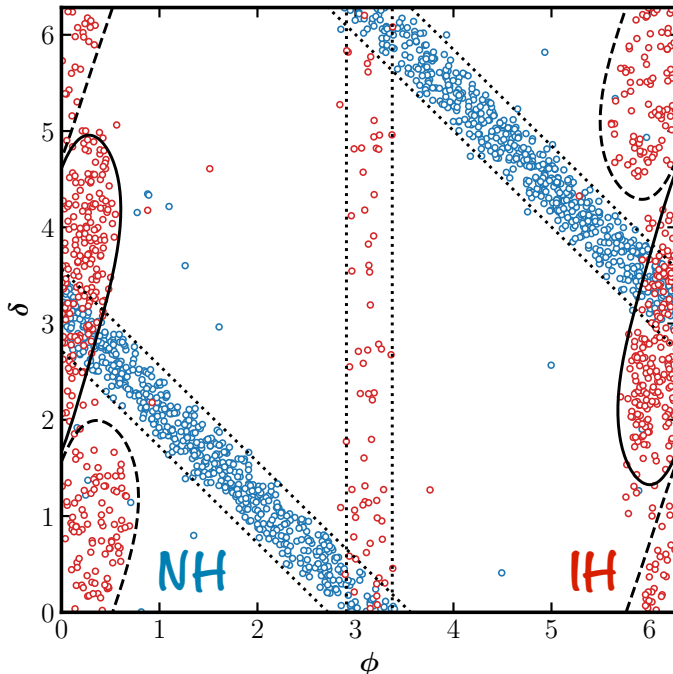


Fast oscillations

If $\Gamma_{\text{osc}}/\Gamma \gg 1$ the analytic solution can predict the PMNS phases, flavour mixing and implications on neutrinoless double beta decay

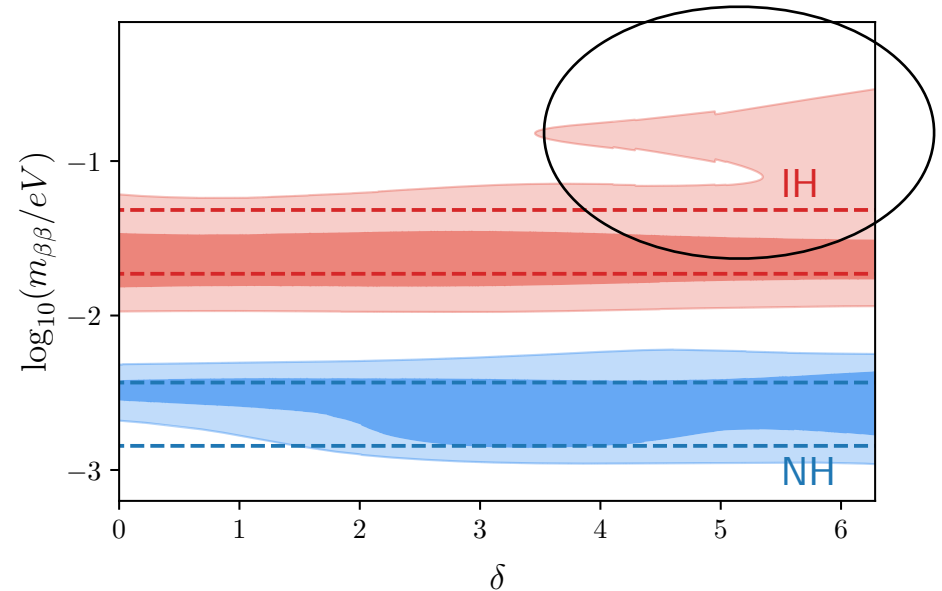
Flavour selection

$\Delta M/M = 10^{-2}$ within FCC



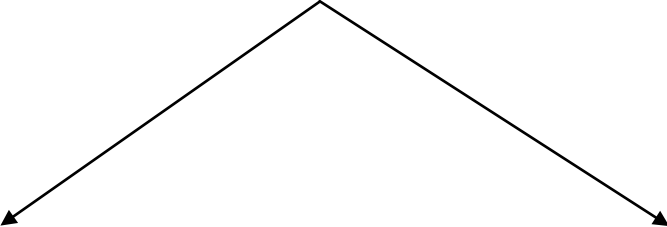
$m_{\beta\beta}$ enhancement

$\Delta M/M = 10^{-2}$ within SHiP



Conclusions and Outlook

- * Developed analytical approximation reveals correlation of Leptogenesis with other observables



Upper bound on the right-handed neutrino interaction with the SM content!

Right-handed neutrinos with $\Delta M/M \rightarrow 1$ need to realize a concrete flavour composition & impact the neutrinoless double-beta decay rate!

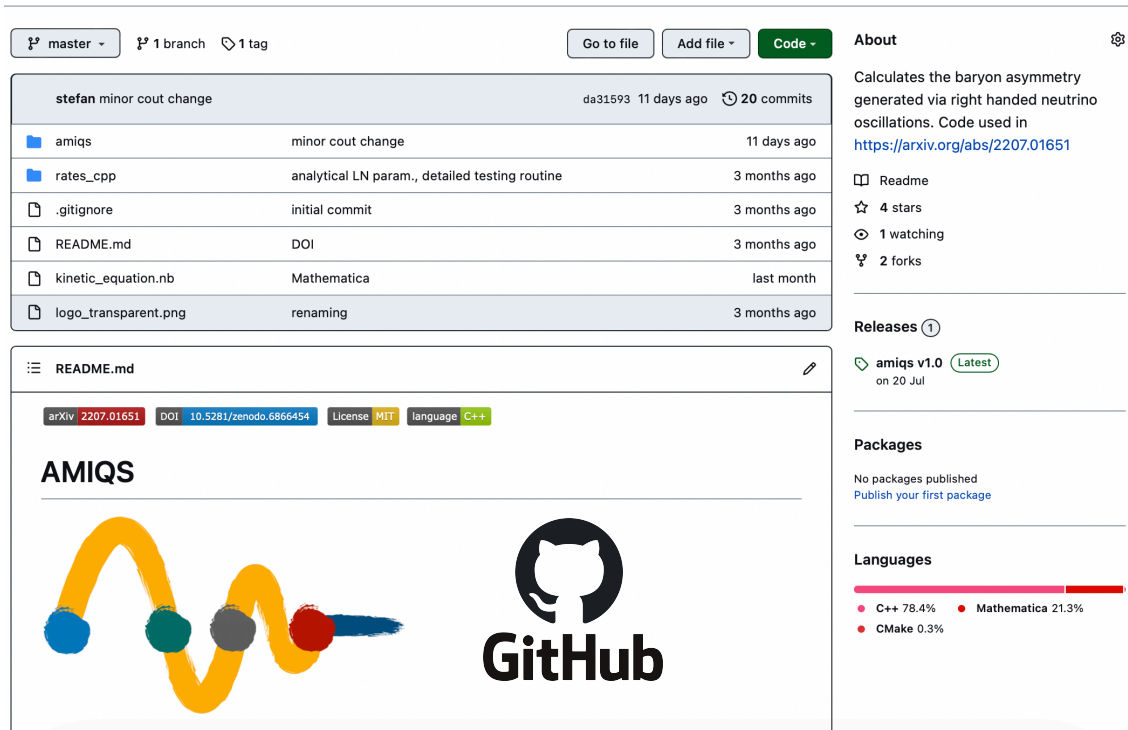
- * Method developed can help to explore non-minimal scenarios

- * Check out [[2207.01651](#)] for more details

Bonus



* Numerical code available on GitHub





The screenshot shows a GitHub repository page for a user named 'stefan'. The repository is titled 'minor cout change' and has 20 commits. The file list includes 'amiqs', 'rates_cpp', '.gitignore', 'README.md', 'kinetic_equation.nb', and 'logo_transparent.png'. The README.md file is open, showing the title 'AMIQS' and a GitHub logo. The repository description states: 'Calculates the baryon asymmetry generated via right handed neutrino oscillations. Code used in <https://arxiv.org/abs/2207.01651>'. The repository has 4 stars, 1 watching, and 2 forks. The latest release is 'amiqs v1.0' on 20 Jul. The language statistics are: C++ 78.4%, Mathematica 21.3%, and CMake 0.3%.

File	Description	Last Commit
amiqs	minor cout change	11 days ago
rates_cpp	analytical LN param., detailed testing routine	3 months ago
.gitignore	initial commit	3 months ago
README.md	DOI	3 months ago
kinetic_equation.nb	Mathematica	last month
logo_transparent.png	renaming	3 months ago

arXiv [2207.01651](https://arxiv.org/abs/2207.01651) DOI [10.5281/zenodo.6866454](https://doi.org/10.5281/zenodo.6866454) License [MIT](#) language [C++](#)

AMIQS

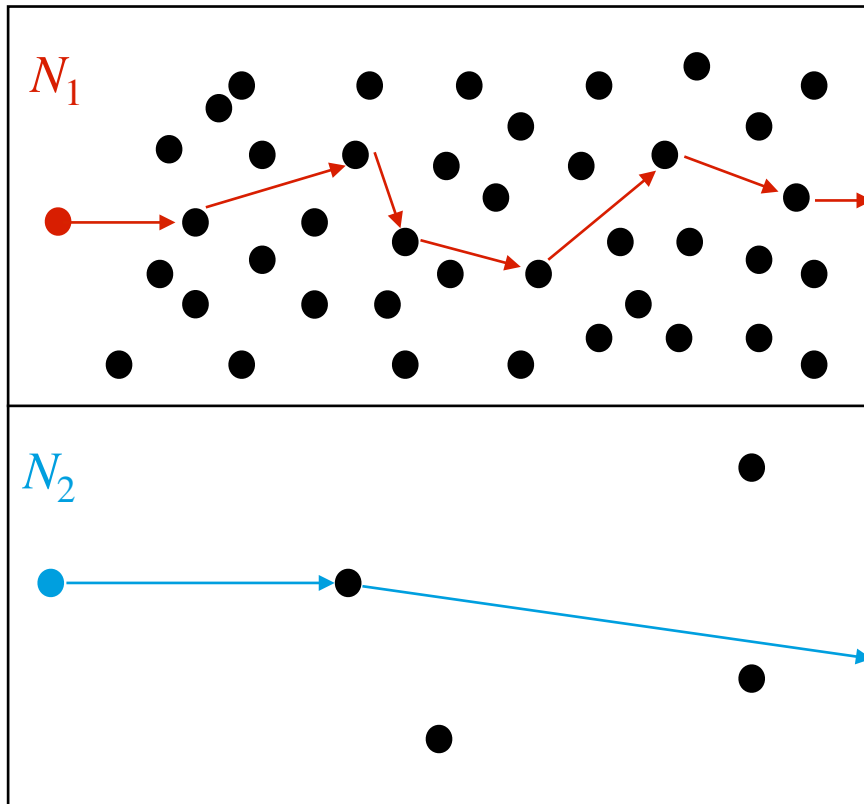


* Check out [[2207.01651](https://arxiv.org/abs/2207.01651)] for more details

Damped oscillations

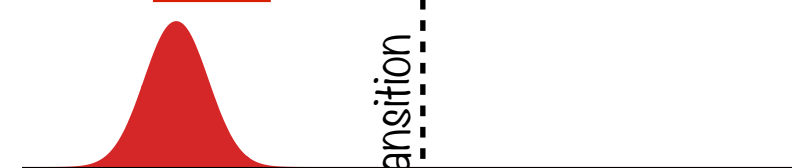
If oscillations are damped $\Gamma_{osc}^{slow} \simeq P_{osc} \Gamma \lesssim H$ is realizable until EWPT

Use approximate LN symmetry to ensure: i) $\Delta M \ll M$ & ii) $y' \ll y$



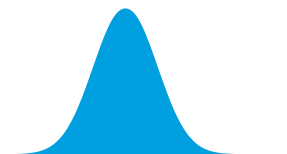
Thermalization probability

100% before EWPT



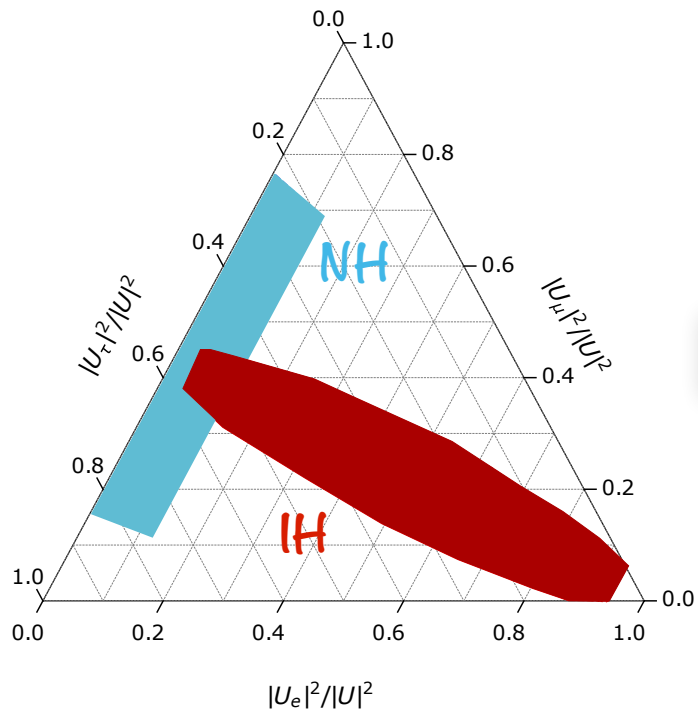
Electroweak phase transition

100% after EWPT

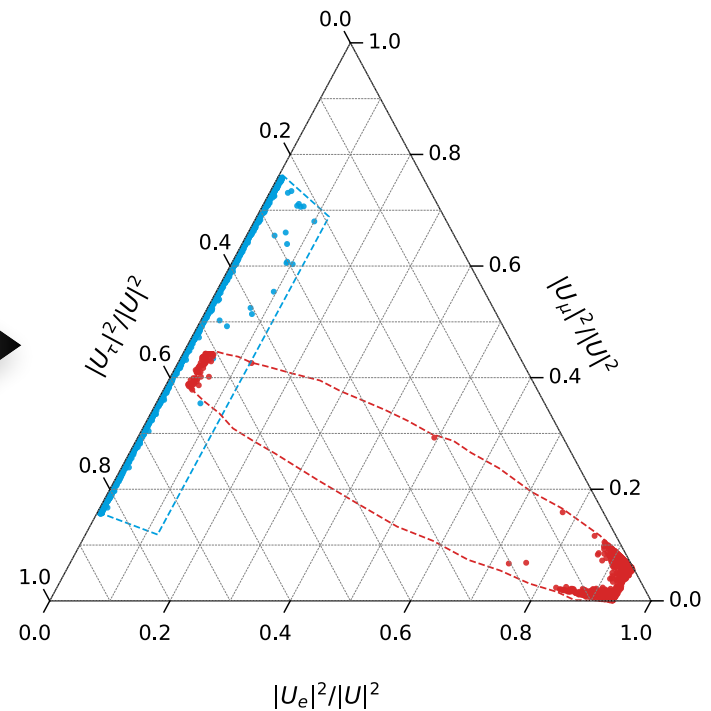


Fast oscillations

Neutrino Oscillation data

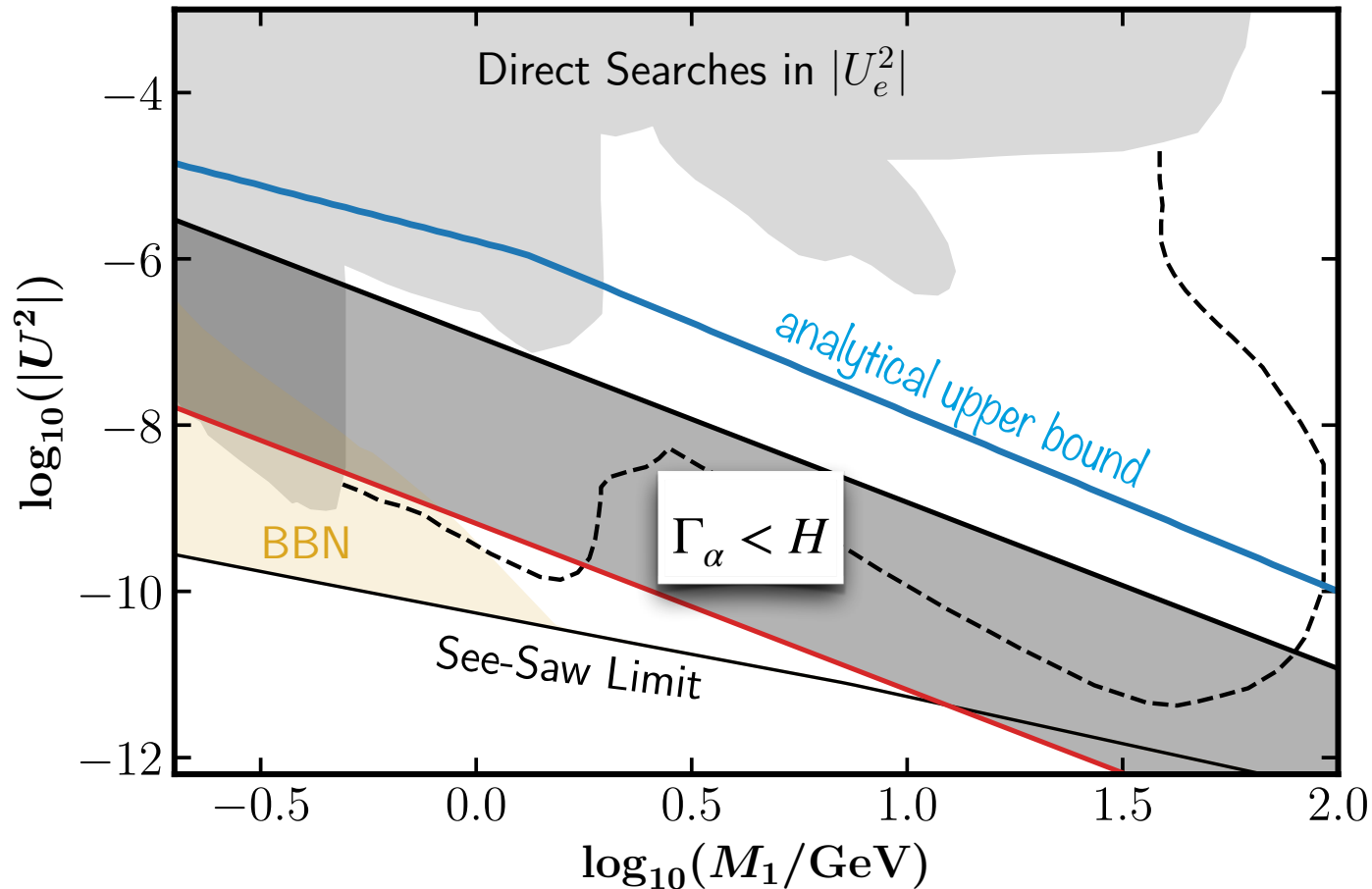


Flavour selection via Leptogenesis
with $\Delta M/M = 10^{-2}$ within FCC



Fast oscillations

One mode can remain weak only via flavour hierarchical interactions



CP Invariants

NORMAL HIERARCHY

$$\begin{aligned}
 \frac{\Delta_{\text{LNC}}^{\text{ov}}}{M_2^2 - M_1^2} &\approx -\frac{v^2 \sqrt{\Delta m_{\text{atm}}^2}}{8M^3 U^4} s_\theta, \\
 \frac{\Delta_{\text{LNC}}^{\text{int(e)}}}{M_2^2 - M_1^2} &= \frac{\Delta_{\text{LNC}}^{\text{osc(e)}}}{g(M_1, M_2)} \approx U^2 M^3 \frac{\sqrt{\Delta m_{\text{atm}}^2}}{v^4} r s_{12}^2 s_\theta, \\
 \frac{\Delta_{\text{LNC}}^{\text{int}(\mu)}}{M_2^2 - M_1^2} &= \frac{\Delta_{\text{LNC}}^{\text{osc}(\mu)}}{g(M_1, M_2)} \approx \frac{U^2 M^3}{2} \frac{\sqrt{\Delta m_{\text{atm}}^2}}{v^4} \sqrt{r} c_{12} \sin(\theta - \phi), \\
 \frac{\Delta_{\text{LNC}}^{\text{int}(\tau)}}{M_2^2 - M_1^2} &= \frac{\Delta_{\text{LNC}}^{\text{osc}(\tau)}}{g(M_1, M_2)} \approx -\frac{\Delta_{\text{LNC}}^{\text{int}(\mu)}}{M_2^2 - M_1^2}, \\
 \frac{\Delta_{\text{LNV}}^{\text{ov}}}{M_1 M_2 (M_2^2 - M_1^2)} &= \frac{v^2}{2U^2 M^2} \frac{\Delta_{\text{LNV}}^{\text{osc}}}{g_M(M_1, M_2)} \approx -\frac{\sqrt{\Delta m_{\text{atm}}^2}}{4MU^2} s_\theta.
 \end{aligned}$$

INVERTED HIERARCHY

$$\begin{aligned}
 \frac{\Delta_{\text{LNC}}^{\text{ov}}}{M_2^2 - M_1^2} &\approx \frac{v^2 \sqrt{\Delta m_{\text{atm}}^2}}{8M^3 U^4} \frac{(1 + 3c_\phi \sin 2\theta_{12})(c_\theta s_\phi \sin 2\theta_{12} + s_\theta \cos 2\theta_{12})}{-1 + c_\phi^2 \sin^2 2\theta_{12}}, \\
 \frac{\Delta_{\text{LNC}}^{\text{int(e)}}}{M_2^2 - M_1^2} &= \frac{\Delta_{\text{LNC}}^{\text{osc(e)}}}{g(M_1, M_2)} \approx \frac{U^2 M^3}{2} \frac{\sqrt{\Delta m_{\text{atm}}^2}}{v^4} (\sin 2\theta_{12} s_\phi c_\theta + \cos 2\theta_{12} s_\theta), \\
 \frac{\Delta_{\text{LNC}}^{\text{int}(\mu)}}{M_2^2 - M_1^2} &= \frac{\Delta_{\text{LNC}}^{\text{osc}(\mu)}}{g(M_1, M_2)} \approx \frac{\Delta_{\text{LNC}}^{\text{int}(\tau)}}{M_2^2 - M_1^2} = \frac{\Delta_{\text{LNC}}^{\text{osc}(\tau)}}{g(M_1, M_2)} \approx -\frac{1}{2} \frac{\Delta_{\text{LNC}}^{\text{int(e)}}}{M_2^2 - M_1^2}, \\
 \frac{\Delta_{\text{LNV}}^{\text{ov}}}{M_1 M_2 (M_2^2 - M_1^2)} &= \frac{v^2}{2U^2 M^2} \frac{\Delta_{\text{LNV}}^{\text{osc}}}{g_M(M_1, M_2)} \approx -\frac{\sqrt{\Delta m_{\text{atm}}^2}}{8MU^2} r^2 s_\theta.
 \end{aligned}$$