

CONSISTENT KINETIC MIXING

Based on <u>arXiv:2207.00023</u> with Martin Bauer (published yesterday: <u>Phys. Rev. Lett. 129, 171801 (2022)</u>)

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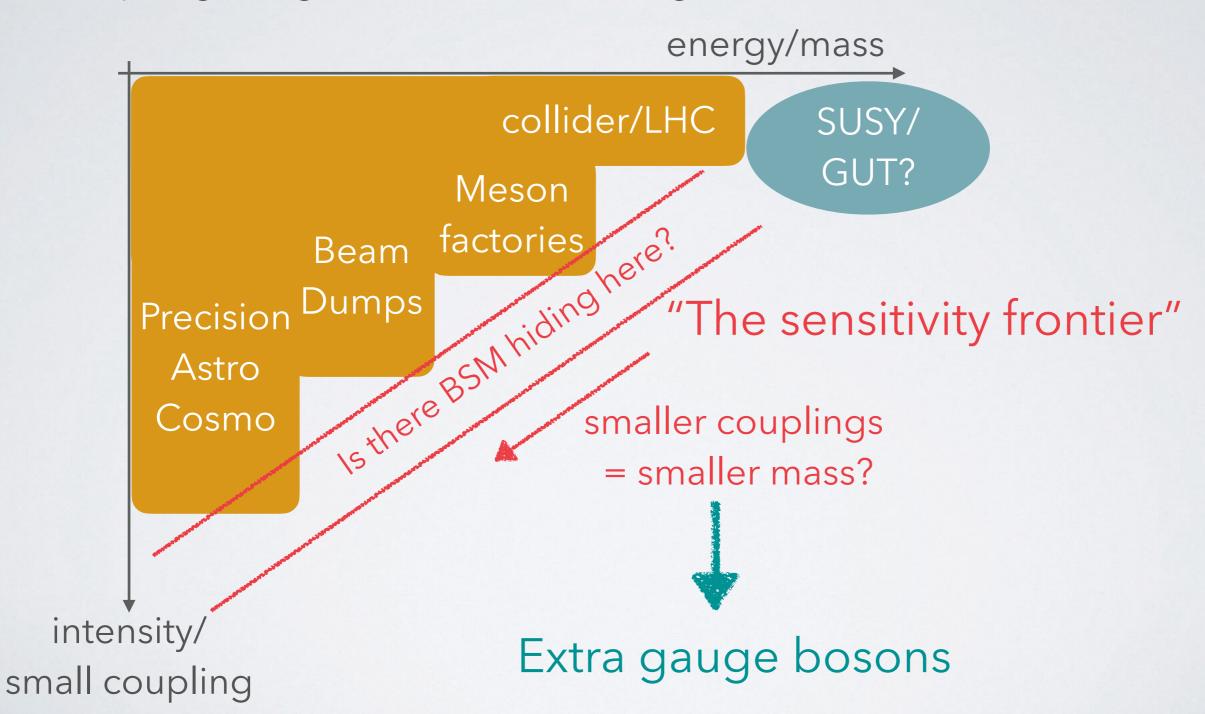


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WHERE TO LOOK FOR BSM

 Many UV theories predict heavy new states with sizeable couplings (e.g. SUSY, GUTs, String Models, ...)



HIDDEN PHOTONS

$$\mathcal{L}\supset -rac{\epsilon_A}{2}\,F_{\mu
u}X^{\mu
u}$$
 [Okun '82; Holdom '86]

• For light mediators $M_X \ll M_Z$ kinetic terms can be diagonalised by simple field redefinition:

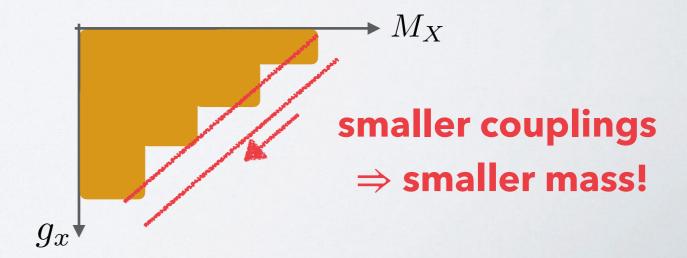
$$A^{\mu} \rightarrow A^{\mu} - \epsilon_A X^{\mu}$$
 \longrightarrow $eA_{\mu}J^{\mu}_{EM} - \epsilon_A eX_{\mu}J^{\mu}_{EM}$ \longrightarrow

Coupling to EM current suppressed by ϵ_A , where typically $\epsilon_A \propto g_\chi/16\pi^2$

• If $U(1)_X$ is broken by VEV f of scalar, mass is related to coupling:

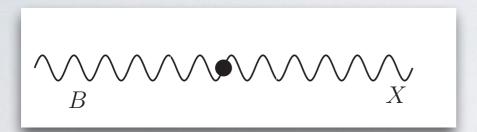
$$\mathcal{L} = (D_{\mu}S)^{\dagger} D^{\mu}S \supset g_x^2 f^2 X_{\mu} X^{\mu}$$

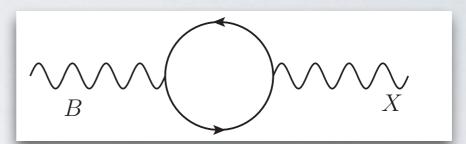
$$\Rightarrow M_X = g_x f$$



KINETIC MIXING — "COMMON LORE"

How does kinetic mixing with photon arise? Cannot be fundamental!





• Kinetic mixing requires either tree-level mixing between the new $U(1)_X$ and the SM hypercharge $U(1)_B$ or is induced at the loop-level if there are fields charged under both $U(1)_B$ and $U(1)_X$

$$\mathcal{L} \supset -\frac{\epsilon_B}{2} B_{\mu\nu} X^{\mu\nu}$$

$$B_{\mu} = c_w A_{\mu} - s_w Z_{\mu}$$

$$\mathcal{L} \supset -c_w \frac{\epsilon_B}{2} F_{\mu\nu} X^{\mu\nu} + s_w \frac{\epsilon_B}{2} Z_{\mu\nu} X^{\mu\nu}$$

$$\Rightarrow \epsilon_A = c_w \epsilon_B$$

KINETIC MIXING — THE FULL PICTURE

• There is a dim-6 operator that induces mixing with the weak bosons (in theories with $SU(2)_L$ multiplets charged under $U(1)_X$ generated at loop level)

$$\mathcal{O}_{WX} = \frac{c_{WX}}{\Lambda^2} H^{\dagger} \sigma^i H W^i_{\mu\nu} X^{\mu\nu}$$

New physics

scale

This operator induces kinetic mixing after EWSB

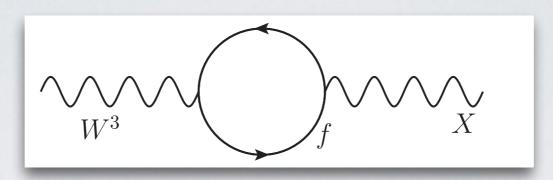
$$\mathcal{O}_{WX}\supset -\frac{\epsilon_W}{2}\,W_{\mu\nu}^3X^{\mu\nu} \qquad \text{with } \epsilon_W=c_{WX}\frac{v^2}{\Lambda^2}$$

$$W_\mu^3=s_w\,A_\mu+c_w\,Z_\mu$$

$$\mathcal{O}_{WX}\supset -s_w\,\frac{\epsilon_W}{2}\,F_{\mu\nu}X^{\mu\nu} -c_w\,\frac{\epsilon_W}{2}\,Z_{\mu\nu}X^{\mu\nu}$$

$$\implies \epsilon_A = c_w \, \epsilon_B + s_w \, \epsilon_W$$

LOOP GENERATION OF ϵ_W



• The operator \mathcal{O}_{WX} captures the $SU(2)_L$ contributions to kinetic mixing of the X boson with W^3 . After EWSB one can identify

$$\Pi_{WX}^{\mu\nu} = \Pi_{WX} [g^{\mu\nu}p_1 \cdot p_2 - p_1^{\mu}p_2^{\nu}] + \Delta_{WX} g^{\mu\nu}$$

• The kinetic mixing due to $U(1)_X$ charged $SU(2)_L$ multiplets reads

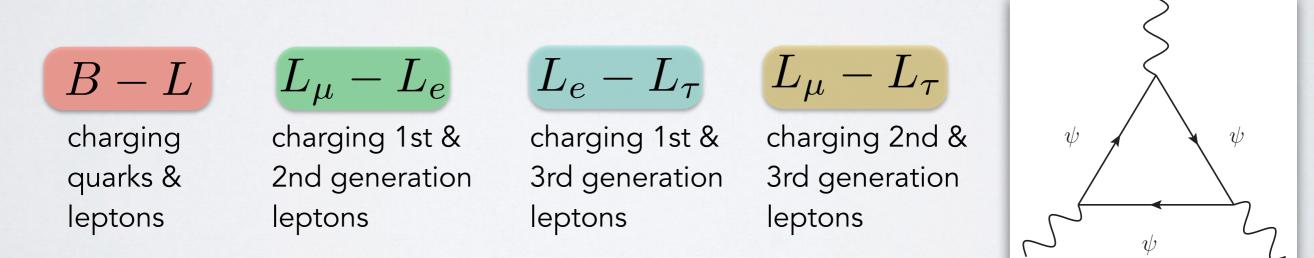
$$\Pi_{WX} = -\frac{g\,g_x}{8\pi^2} \sum_f T_3^f \left(v_X^f + a_X^f\right) \int_0^1 \!\! dx \, x (1-x) \, \log\left(\frac{\mu^2}{m_f^2 - x(1-x)q^2}\right)$$
 Sum over
$$SU(2)_L \, \text{charge} \quad (v_X^f + a_X^f) = 2\,Q_L^f \quad \text{loop function}$$

WHY IS THIS IMPORTANT?

• Beyond kinetic mixing $U(1)_X$ can be coupled to SM by gauge interactions

$${\cal L}_{
m int}=-g_x\,J_X^\mu X_\mu$$
 $SU(2)_L$ multiplets! $J_X^\mu=\sum_\psi ar\psi\,Q_\psi\,\gamma^\mu\psi$ with $\psi=Q,L,u,d,\ell,
u$

Phenomenologically viable anomaly-free combinations are:

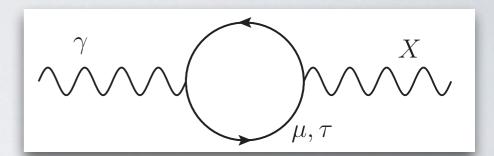


• All of these models charge SM $SU(2)_L$ multiplets, and thus necessarily induce \mathcal{O}_{WX} at the renormalizable level ($\Lambda = \nu$)!

MATCHING EXAMPLE: $U(1)_{L_{\prime\prime}-L_{\tau}}$

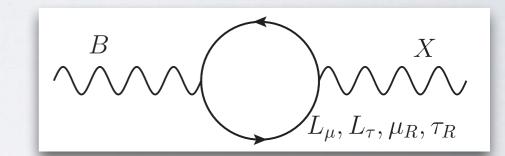
In the IR the loop mixing with the photon is computed to

$$\epsilon_A = \frac{eg_{\mu\tau}}{6\pi^2} \log\left(\frac{m_\mu}{m_\tau}\right)$$



The naive UV computation yields

$$\epsilon_B = \frac{g'g_{\mu\tau}}{24\pi^2} \left[3\log\left(\frac{m_{\mu}}{m_{\tau}}\right) + \log\left(\frac{m_{\nu_{\mu}}}{m_{\nu_{\tau}}}\right) \right]$$



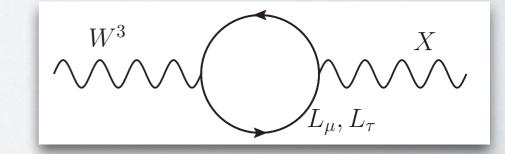


$$\Rightarrow$$
 $\epsilon_A \neq c_w \epsilon_B$



We are missing the mixing with the $SU(2)_L$

$$\epsilon_W = \frac{gg_{\mu\tau}}{24\pi^2} \left[\log\left(\frac{m_{\mu}}{m_{\tau}}\right) - \log\left(\frac{m_{\nu_{\mu}}}{m_{\nu_{\tau}}}\right) \right]$$





$$\Rightarrow \epsilon_A = c_w \, \epsilon_B + s_w \, \epsilon_W$$



HIGGS LOW-ENERGY THEOR

One-loop corrections:

acuum polarization

Starting from the low-energy Lagrangian

$$\mathcal{L} = -\frac{1}{4} \left(F_{\mu\nu}, Z_{\mu\nu}, X_{\mu\nu} \right) \begin{bmatrix} \begin{pmatrix} 1 & 0 & \epsilon_A \\ 0 & 1 & \epsilon_Z \\ \epsilon_A & \epsilon_Z & 1 \end{pmatrix} + \mathbf{\Pi} \end{bmatrix} \begin{pmatrix} F^{\mu\nu} \\ Z^{\mu\nu} \\ X^{\mu\nu} \end{pmatrix}$$

we can derive the Higgs decay amplitudes via the low-energy theorem:

$$\lim_{p_h \to 0} \mathcal{M}(h \to V_i V_j) \to \frac{\partial}{\partial v} \mathcal{M}(V_i \to V_j) = \partial_v [G^T \mathbf{\Pi} G]_{ij}$$

[Ellis, Gaillard, Nanopoulos '76]

[Shifman, Vainshtein, Voloshin, Zakharov '79]

vacuum polarizations in canonical normalisation

$$\Pi = \begin{pmatrix}
\Pi_{\gamma\gamma} & \Pi_{\gamma Z} & \Pi_{\gamma X} \\
\Pi_{\gamma Z} & \Pi_{Z Z} & \Pi_{Z X} \\
\Pi_{\gamma X} & \Pi_{Z X} & \Pi_{X X}
\end{pmatrix}$$

$$G = \begin{pmatrix}
1 & 0 & -\frac{\epsilon_{A}}{\sqrt{1 - \epsilon_{A}^{2} - \epsilon_{Z}^{2}}} \\
0 & 1 & -\frac{\epsilon_{A}}{\sqrt{1 - \epsilon_{A}^{2} - \epsilon_{Z}^{2}}} \\
0 & 0 & \frac{1}{\sqrt{1 - \epsilon_{A}^{2} - \epsilon_{Z}^{2}}}
\end{pmatrix}$$

$$\Pi = \begin{pmatrix}
\Pi_{\gamma\gamma} & \Pi_{\gamma Z} & \Pi_{\gamma X} \\
\Pi_{\gamma Z} & \Pi_{Z Z} & \Pi_{Z X} \\
\Pi_{\gamma X} & \Pi_{Z X} & \Pi_{X X}
\end{pmatrix}$$

$$G = \begin{pmatrix}
1 & 0 & -\frac{\epsilon_{A}}{\sqrt{1 - \epsilon_{A}^{2} - \epsilon_{Z}^{2}}} \\
0 & 1 & -\frac{\epsilon_{A}}{\sqrt{1 - \epsilon_{A}^{2} - \epsilon_{Z}^{2}}} \\
0 & 0 & \frac{1}{\sqrt{1 - \epsilon_{A}^{2} - \epsilon_{Z}^{2}}}
\end{pmatrix}$$

$$G^{T} \Pi G = \Pi - \begin{pmatrix}
0 & 0 & \epsilon_{A} \Pi_{\gamma\gamma} + \epsilon_{Z} \Pi_{\gamma Z} \\
\cdot & 0 & \epsilon_{A} \Pi_{\gamma Z} + \epsilon_{Z} \Pi_{Z Z} \\
\cdot & \cdot & 2\epsilon_{A} \Pi_{\gamma X} + 2\epsilon_{Z} \Pi_{Z X}
\end{pmatrix}$$

HIGGS LOW-ENERGY THEOREM

• In the SM we find then for mixing with a new $U(1)_X$ in the IR

$$\partial_v \Pi_{\gamma X}(0) = \sum_f N_c^f \frac{e \, g_x}{12 \, \pi^2 \, v} \, Q_f \, v_X^f$$

$$\partial_v \Pi_{ZX}(0) = \sum_f N_c^f \frac{e \, g_x}{24 \, \pi^2 \, v} \, \frac{T_3^f - 2 \, s_w^2 \, Q_f}{s_w c_w} \, v_X^f$$

$$\partial_v \Pi_{XX}(0) = \sum_f N_c^f \frac{g_x^2}{24 \, \pi^2 \, v} \, v_X^{f2}$$

The sums run over all fermions with $m_f \gg m_h$ (i.e. the top quark)

• Allows us to derive universal branching ratios for models gauging B

$$\mathcal{BR}_{h\to\gamma X} \simeq (0.92 g_x^2 + 6.36 g_x \epsilon_A + 11.01 \epsilon_A^2) \cdot 10^{-3}$$

$$\Rightarrow \sim 10^{-8}$$
 (for $g_x \sim 10^{-4}$ and $\epsilon_A \sim 10^{-3}$) in reach of FCC-hh!

CONCLUSIONS

- Hidden Photons are well motivated particles that could hide along the sensitivity frontier (i.e. weaker coupling, smaller mass)
- The commonly quoted matching $\epsilon_A = c_w \, \epsilon_B$ is incomplete!
- There is a dim-6 operator inducing W^3X mixing. In models with $SU(2)_L$ multiplets charged under $U(1)_X$ it is generated at loop level

- The ϵ_W contribution is essential in anomaly-free U(1) models to obtain correct IR mixing!
- Higgs low-energy theorems automatically incorporate all decay amplitudes comprehensively at fixed order in ϵ

BACKUP

HIGGS LOW-ENERGY THEOREM

Have derived the vacuum polarisation amplitudes for kinetic mixing

