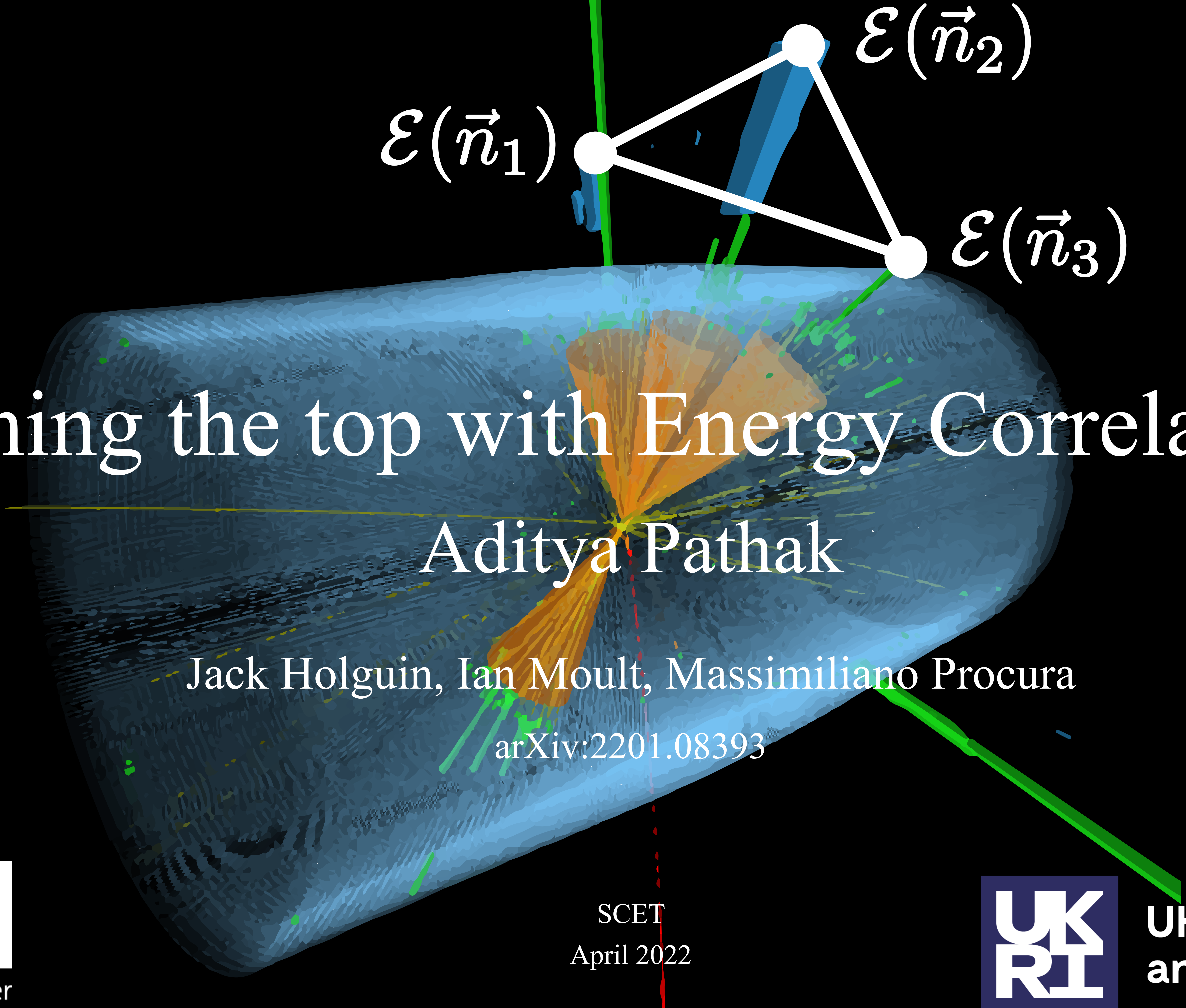


Weighing the top with Energy Correlators

Aditya Pathak

Jack Holguin, Ian Moult, Massimiliano Procura

arXiv:2201.08393

SCET
April 2022

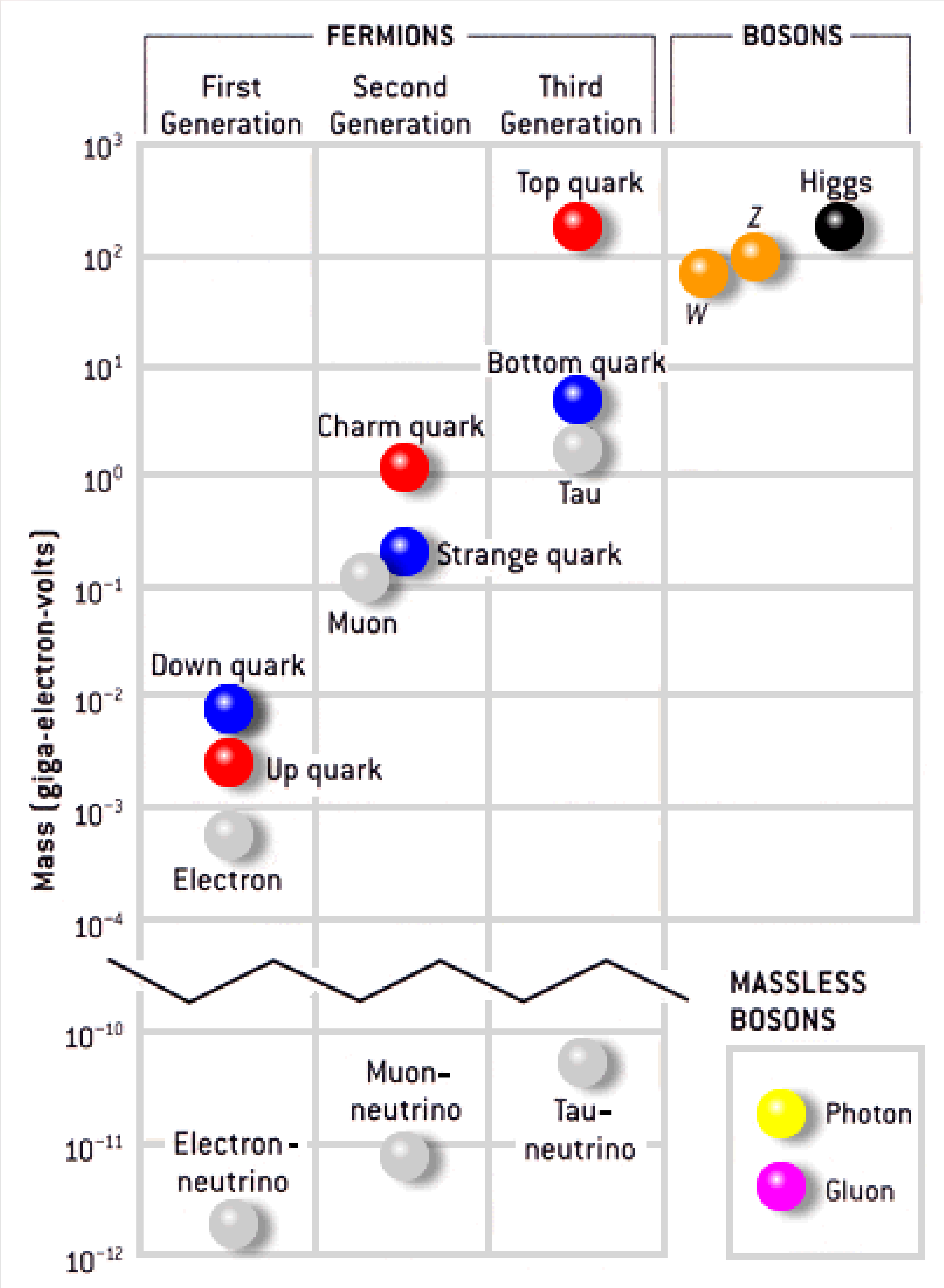
MANCHESTER
1824
The University of Manchester

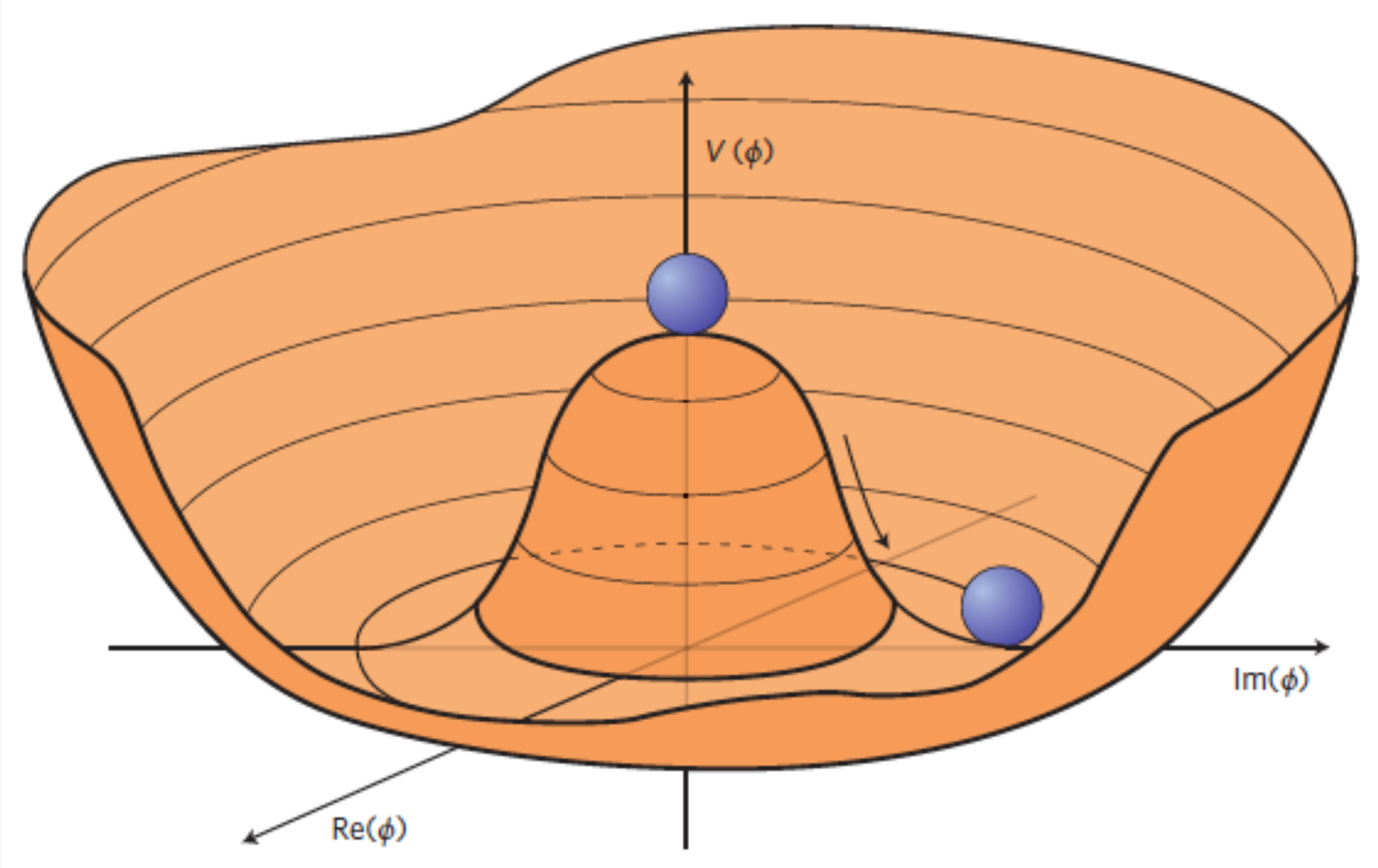
UK Research and Innovation

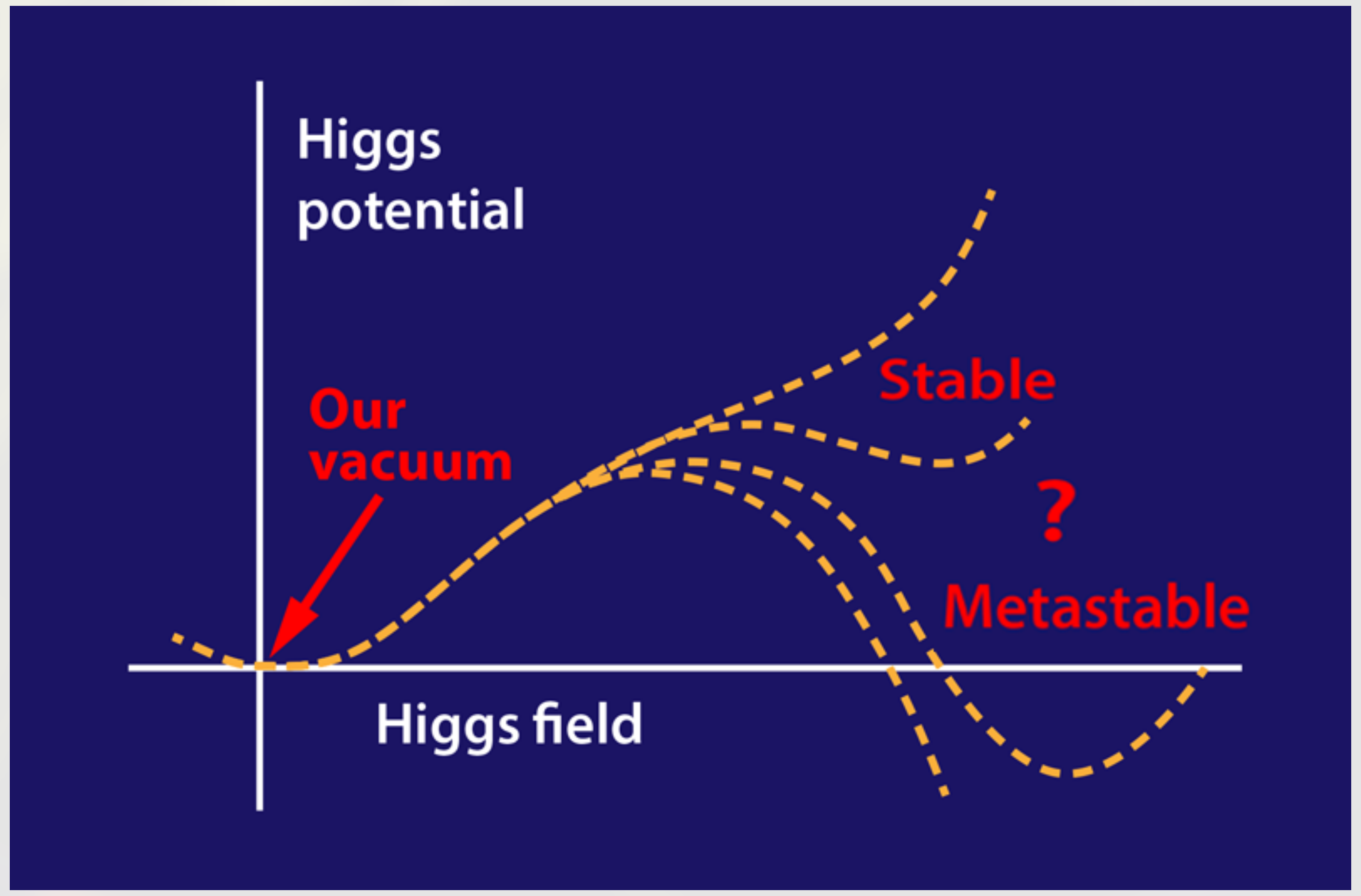
Stability of the electroweak vacuum

Much ado about nothing

Quantum corrections modify the effective potential and can make the EW Vacuum unstable



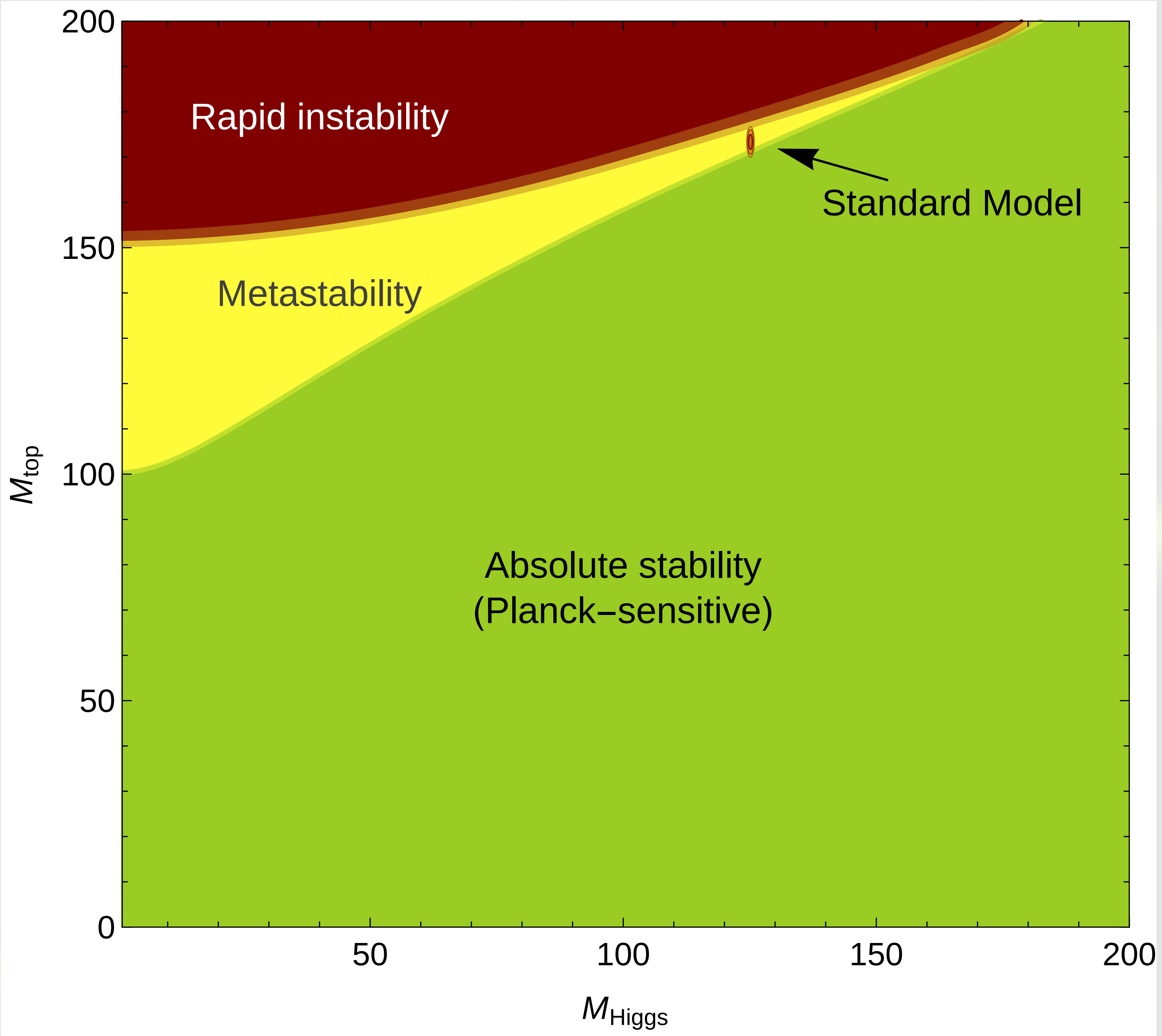


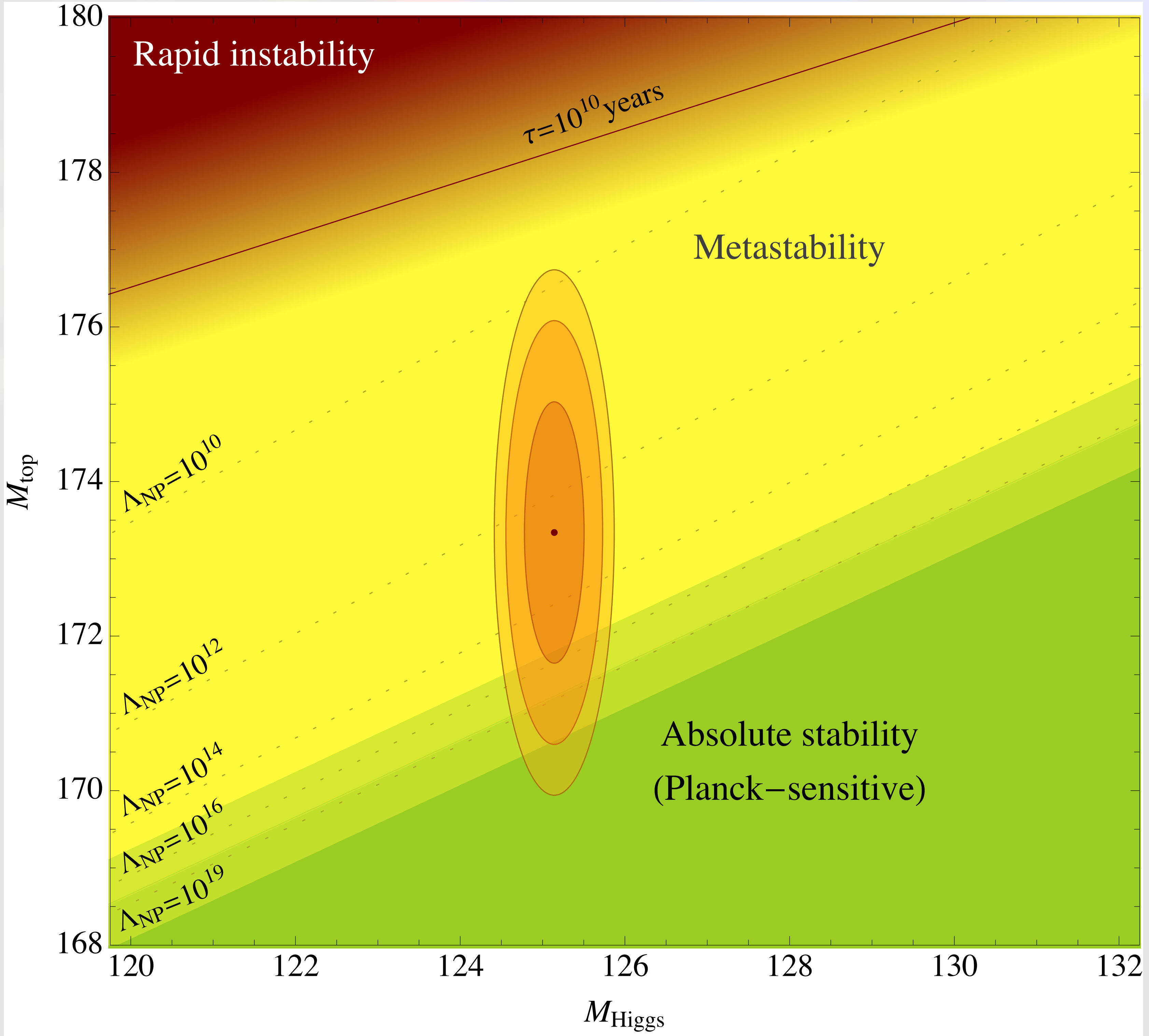


Background: CMS

Why the top mass?

Top quark Yukawa: $y_t = 0.94$





Astonishing result: SM right on the boundary of absolute stability and metastability!

Buttazzo, et al., 2013; Andreassen, et al. 2014

Status of top mass measurements

Current world average (HL-LHC projection ~ 200 MeV)

$$m_t = 172.76 \pm 0.3\,\mathrm{GeV}$$ PDG

An impressive uncertainty ~ 0.2 %!

Some of the numbers that enter this world average:

$$m_t^{\mathrm{MC}} = 172.69 \pm 0.48\,\mathrm{GeV}$$

ATLAS, 1810.01772

$$m_t^{\mathrm{MC}} = 172.26 \pm 0.61\,\mathrm{GeV}$$

CMS, 1812.06489

Compare with Tevatron:

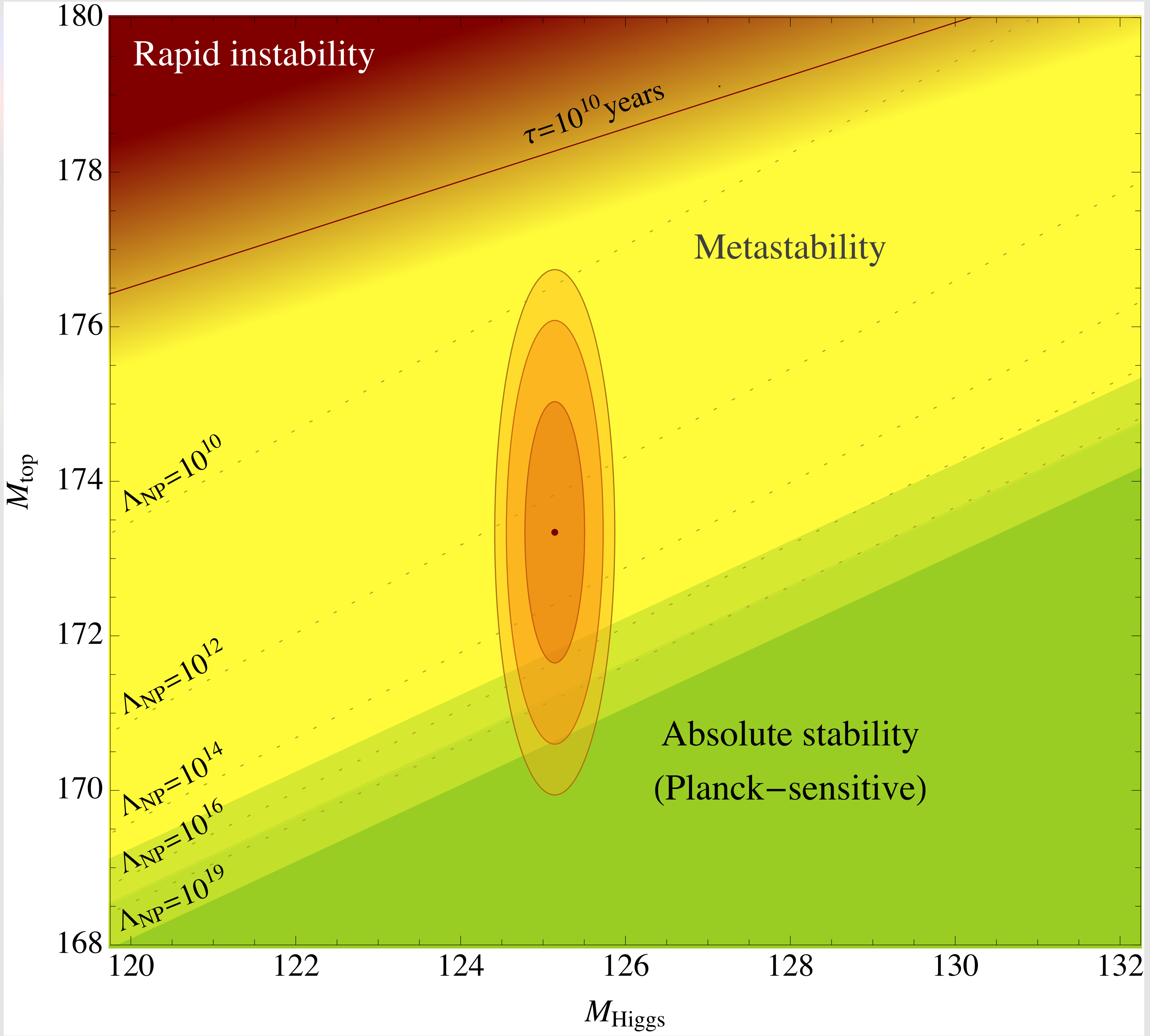
$$m_t^{\mathrm{MC}} = 174.34 \pm 0.64\,\mathrm{GeV}$$

Tevatron, 1407.2682

A recent CMS analysis yielded:

$$m_t^{\mathrm{pole}} = 170.5 \pm 0.8\,\mathrm{GeV}$$

CMS, 1904.05237



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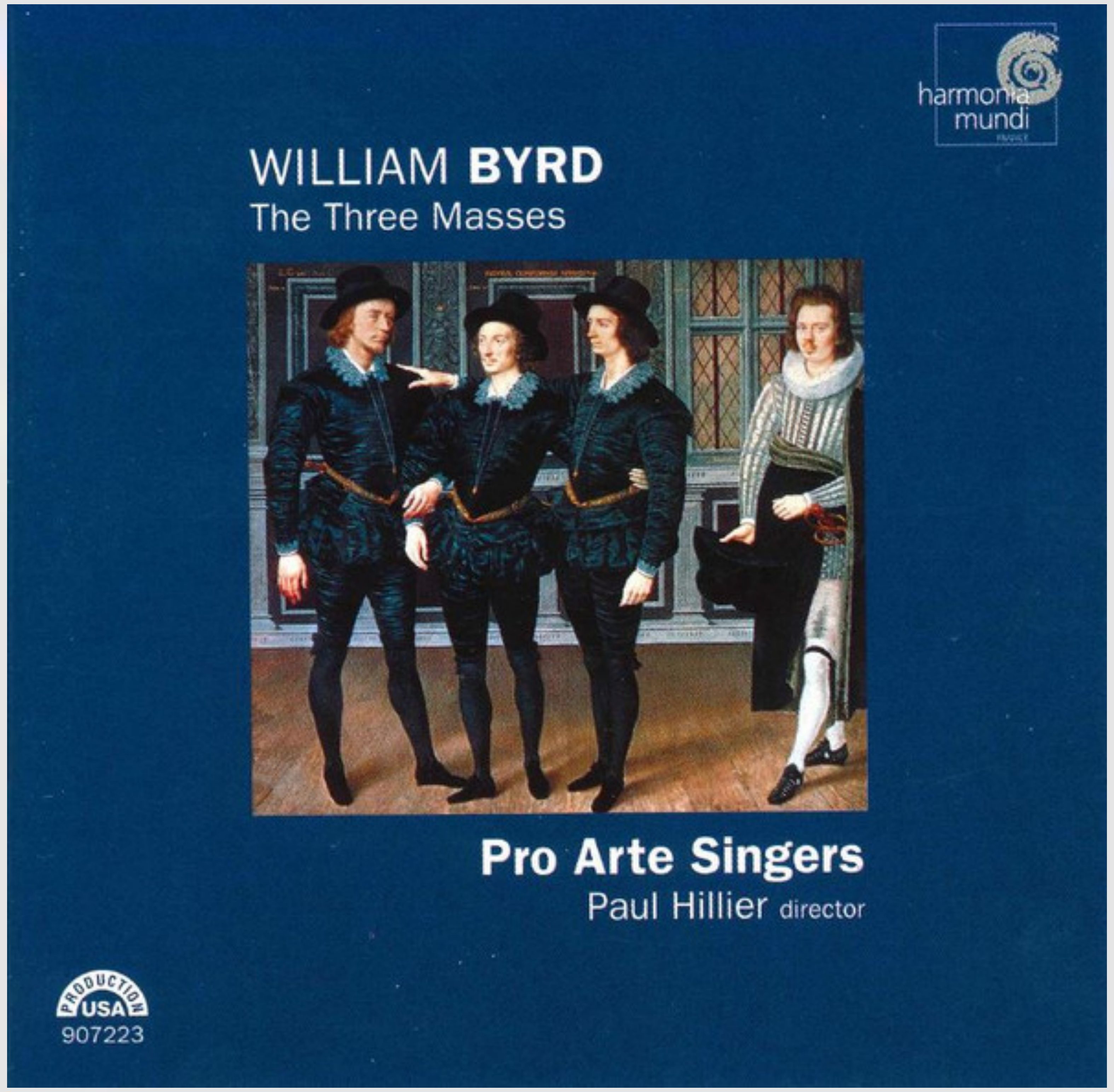
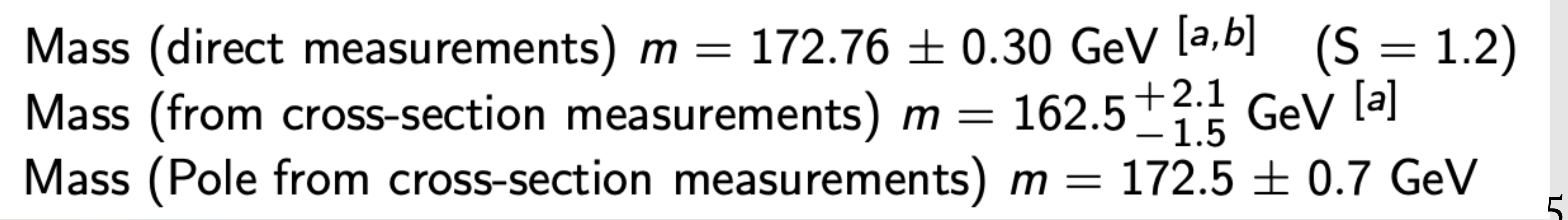


The only quark with three masses in PDG:

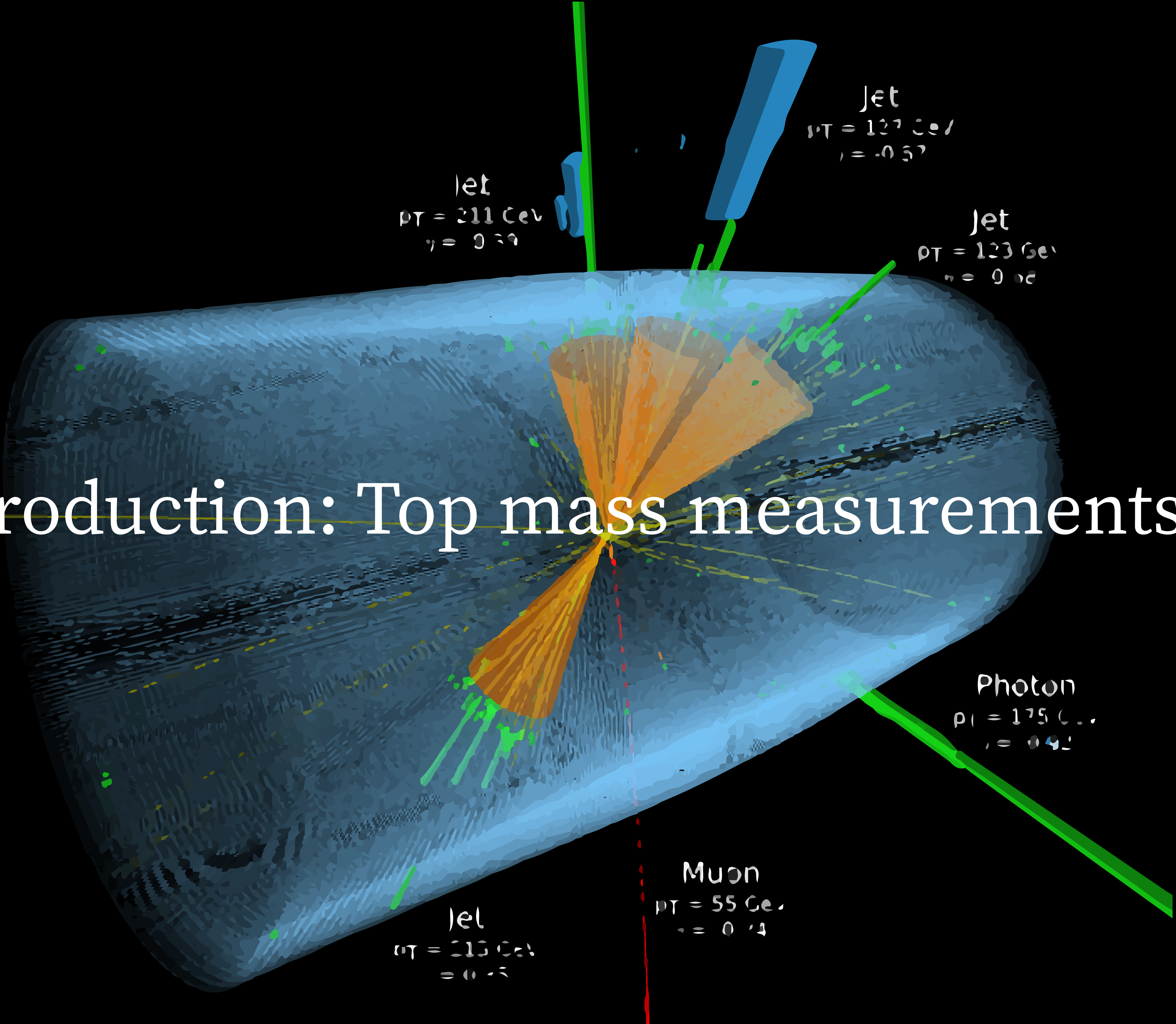


Mass (direct measurements) $m = 172.76 \pm 0.30$ GeV [a,b] (S = 1.2)

Mass (from cross-section measurements) $m = 162.5^{+2.1}_{-1.5}$ GeV [a]

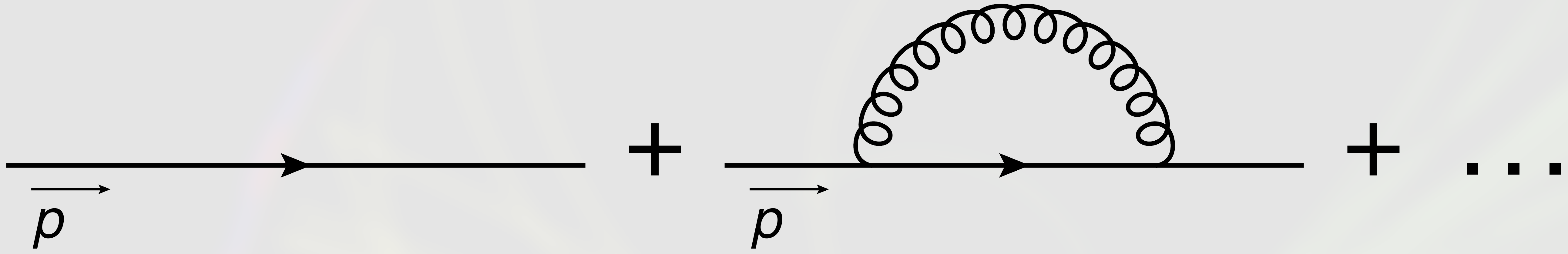
Mass (Pole from cross-section measurements) $m = 172.5 \pm 0.7$ GeV

Introduction: Top mass measurements



How to measure the top mass?

The top quark mass is not a physical observable but a Lagrangian parameter,



$$\sim \quad \frac{i}{\not{p} - m_t^0 - \Sigma(p, m_t^0, \mu)},$$

and must be renormalized in a definite *mass scheme.*

Use a physical observable sensitive to top mass:

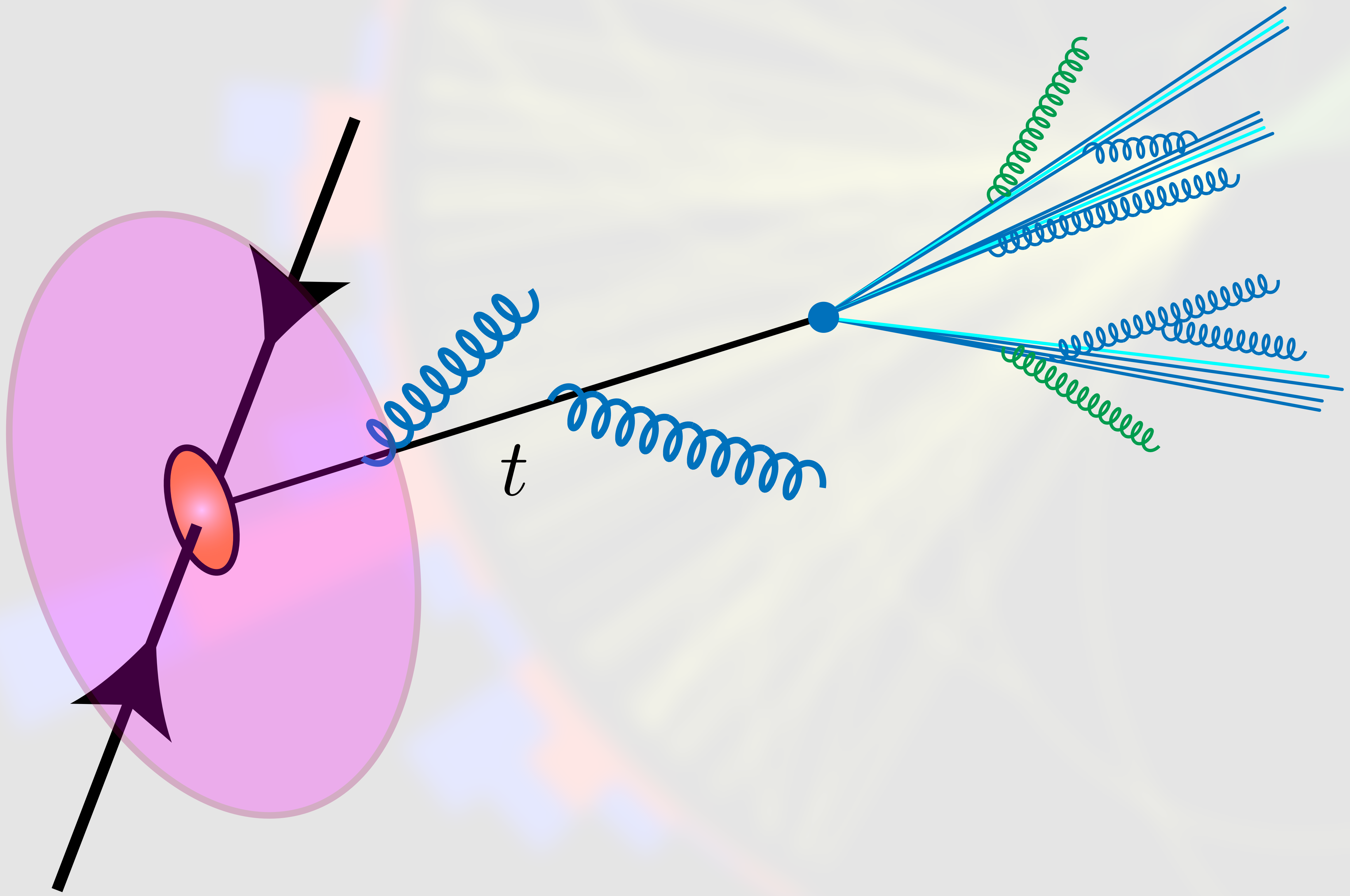
$$\sigma^{\text{exp}}(m_t^X, \Lambda_{\text{QCD}}, Y) = \sigma^{\text{pert}}(m_t^X, \alpha_s, Y, \ldots) + \sigma^{\text{NP}}(\Lambda_{\text{QCD}}, Y, \ldots)$$

$$m_t^{\text{pole}} = m_t^X + \delta m_t^X$$

Andre Hoang: What is the top quark mass? 2004.12915

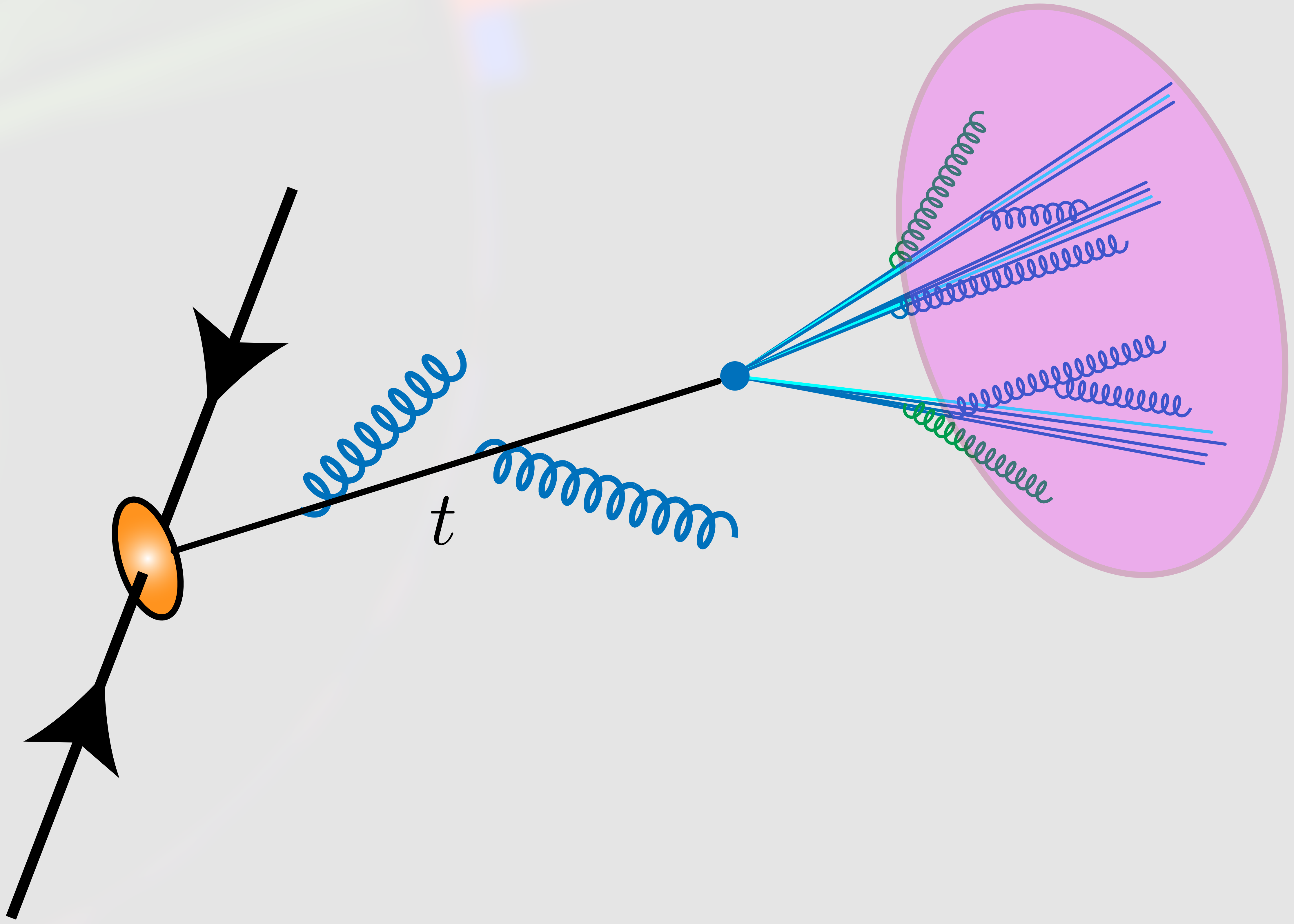
How to measure the top mass?

1. Exploit the production mechanism



(inclusive over final state)

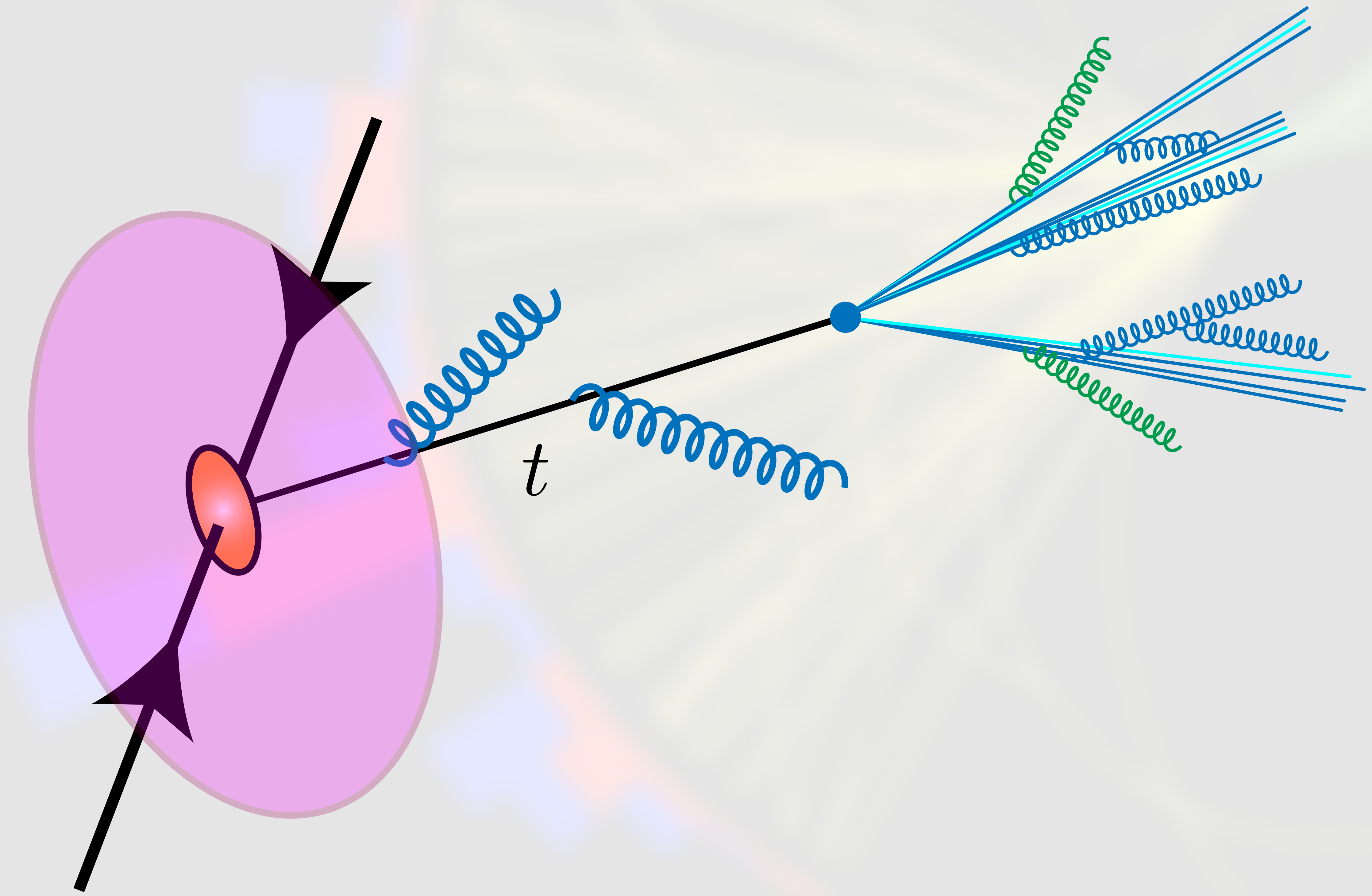
2. Exploit the final state decay products



(insensitive to the production)

How to measure the top mass?

1. Exploit the production mechanism



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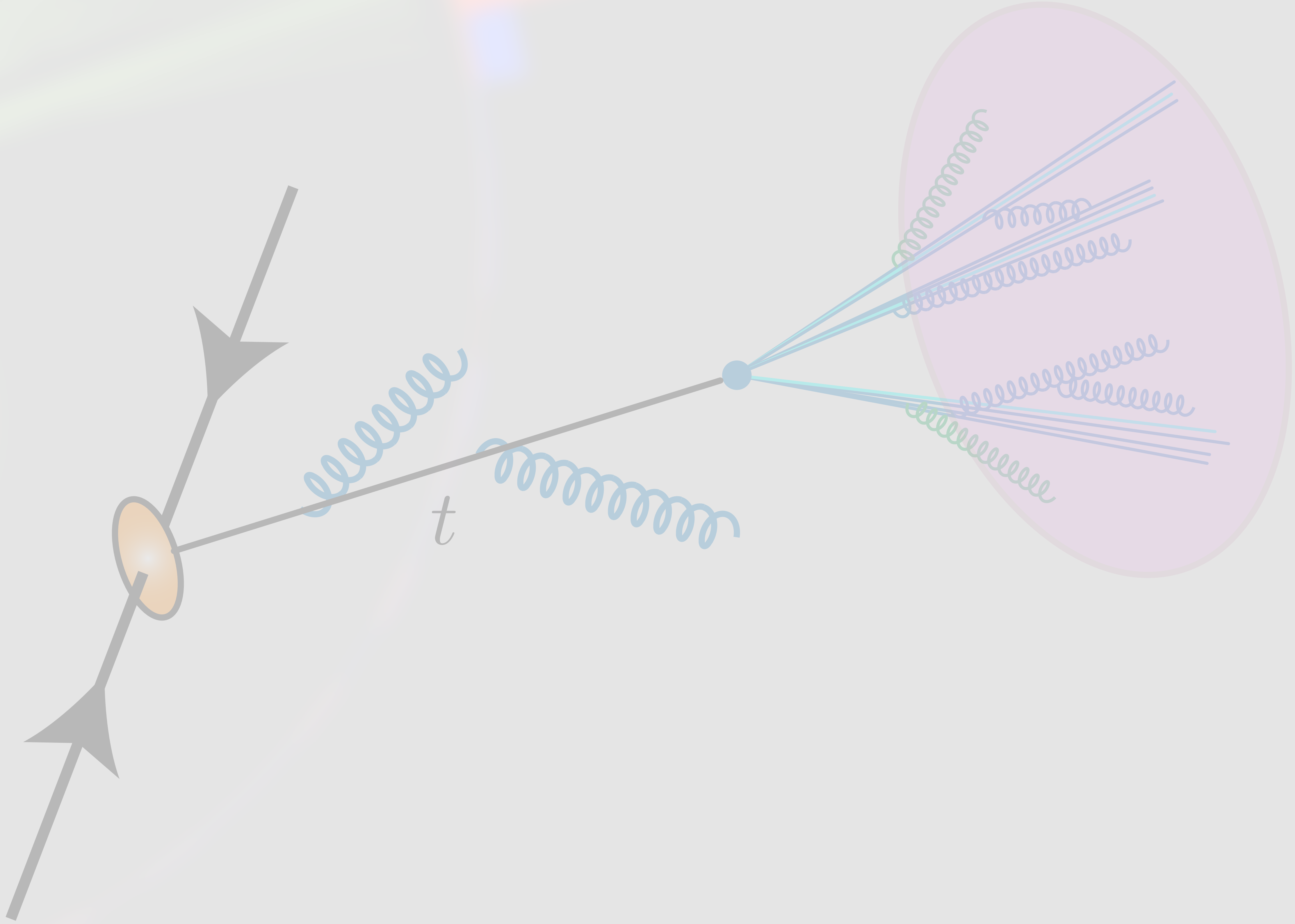

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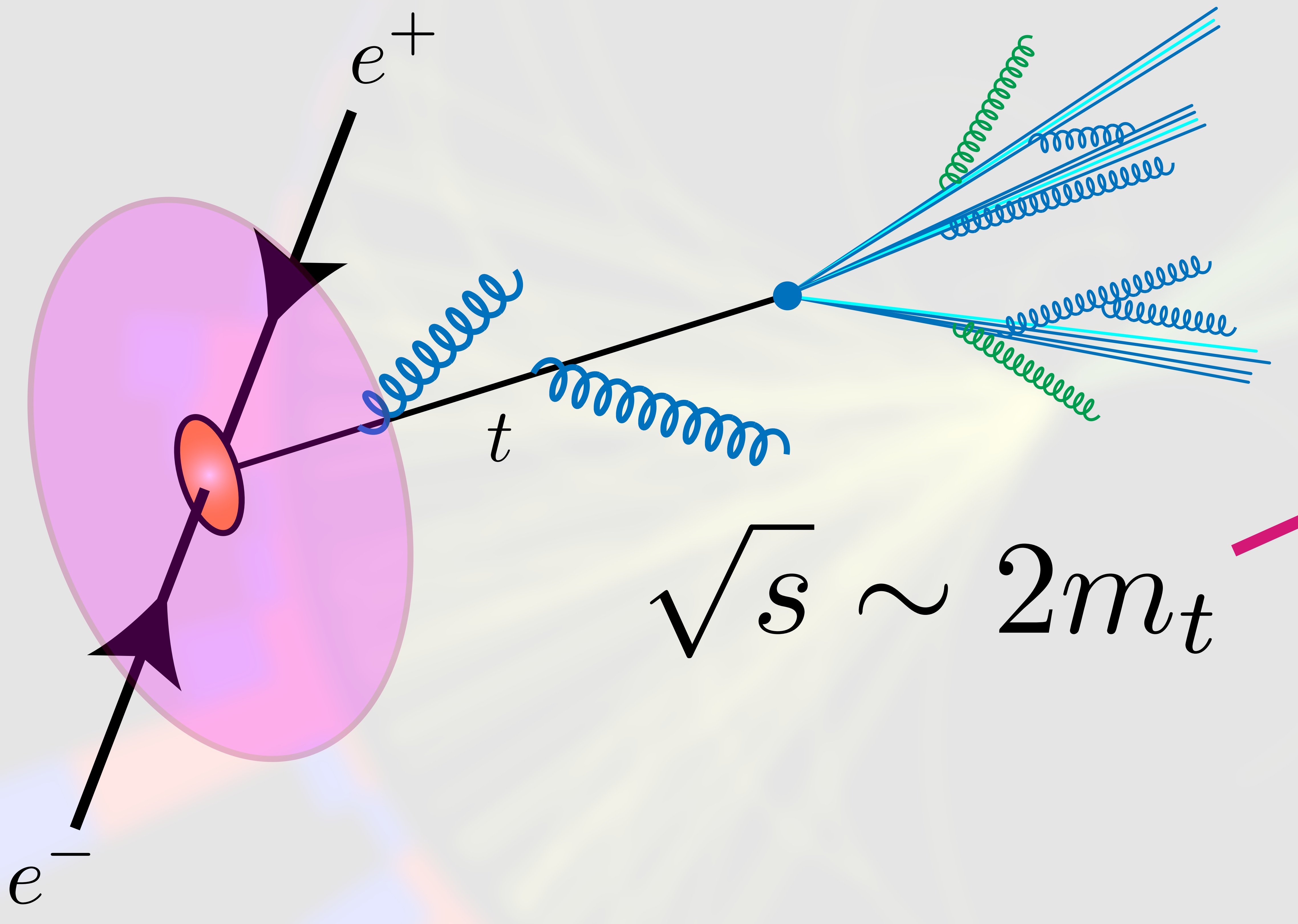
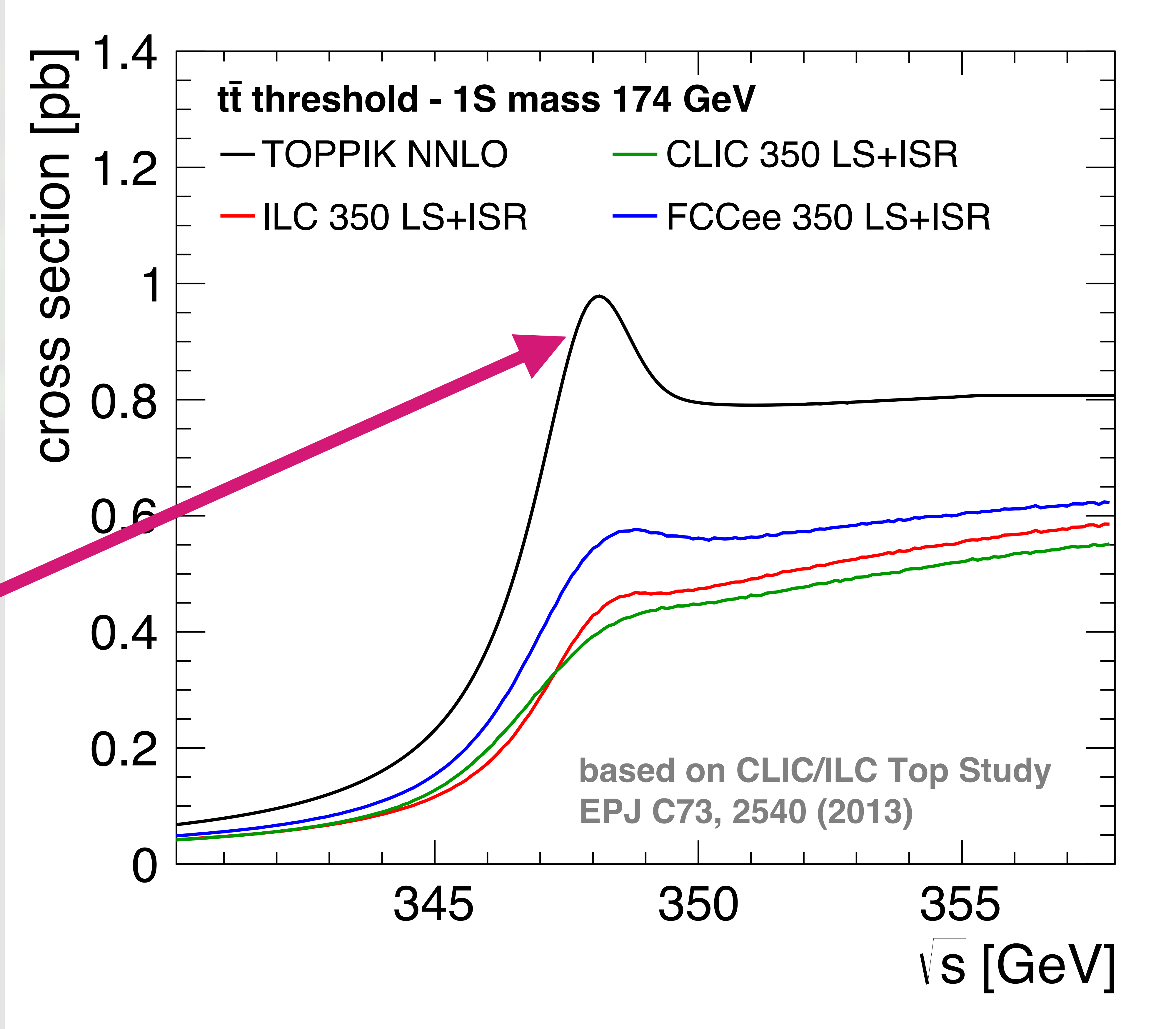


$$\sqrt{s} \sim 2m_t$$

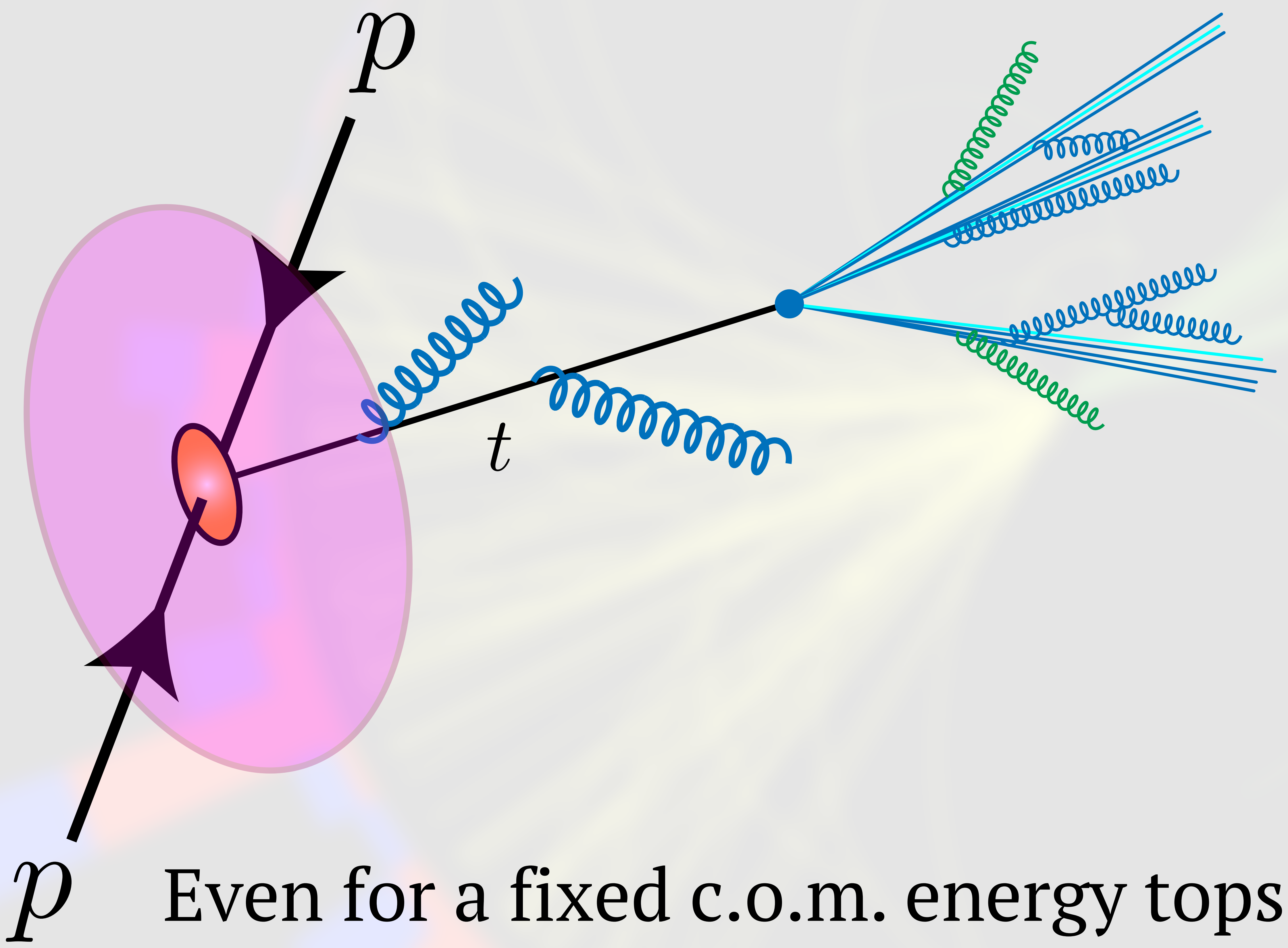


based on CLIC/ILC Top Study
EPJ C73, 2540 (2013)

Threshold scan in e+e- colliders: < 50 MeV precision

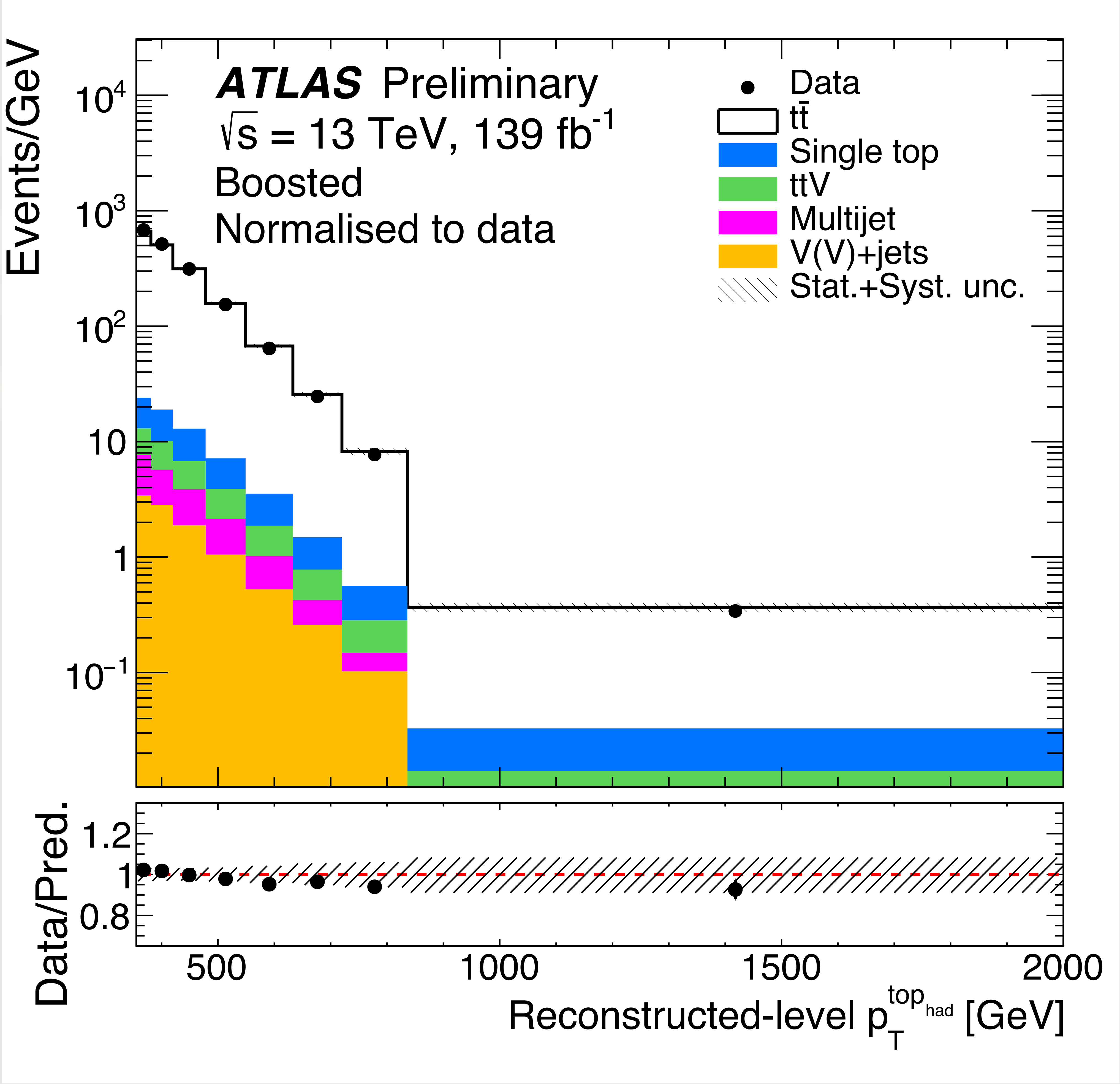
1. Exploit the production mechanism

Challenging to exploit in *pp* collisions



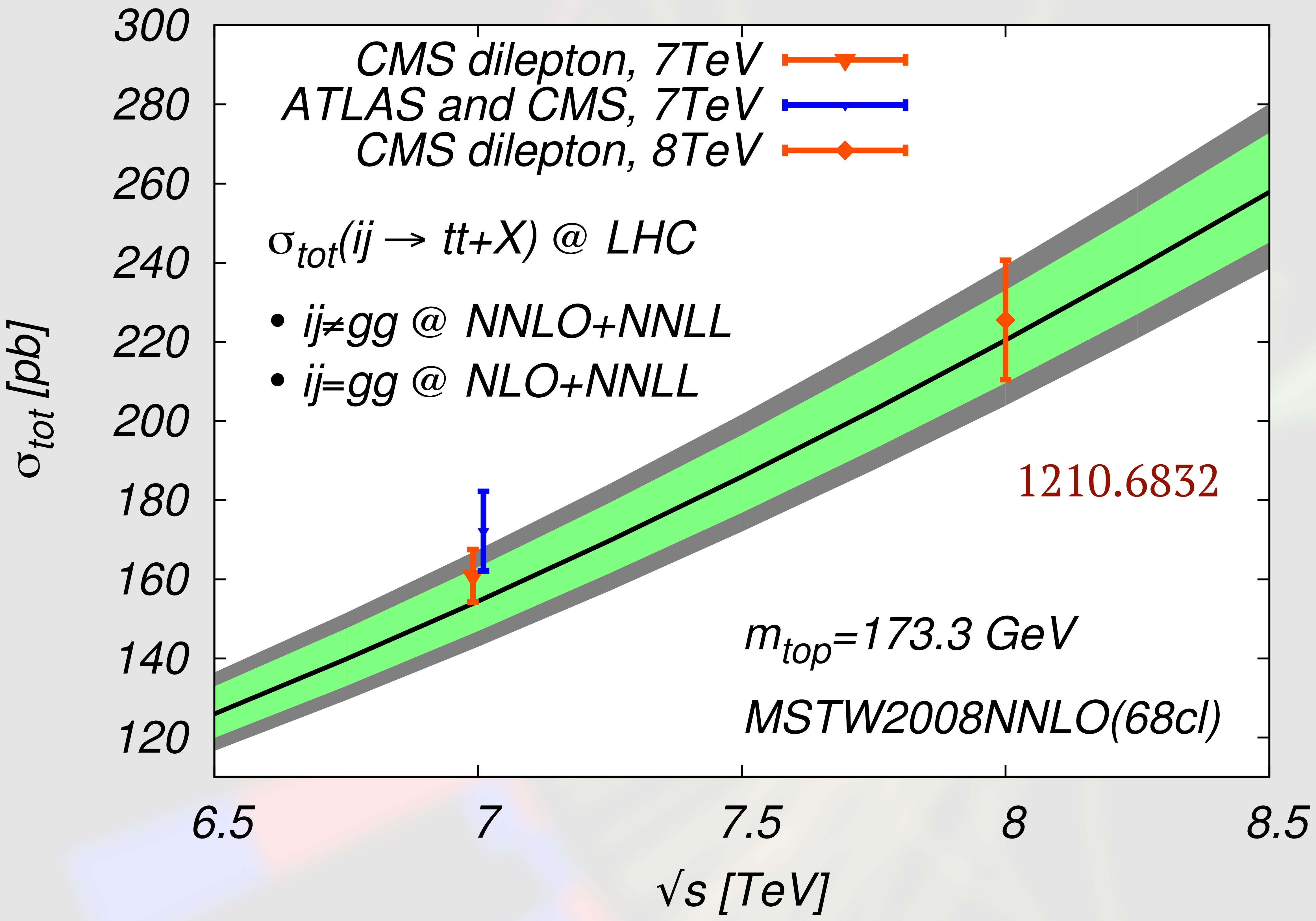
Even for a fixed c.o.m. energy tops are produced with a distribution of p_T

I will come back to this

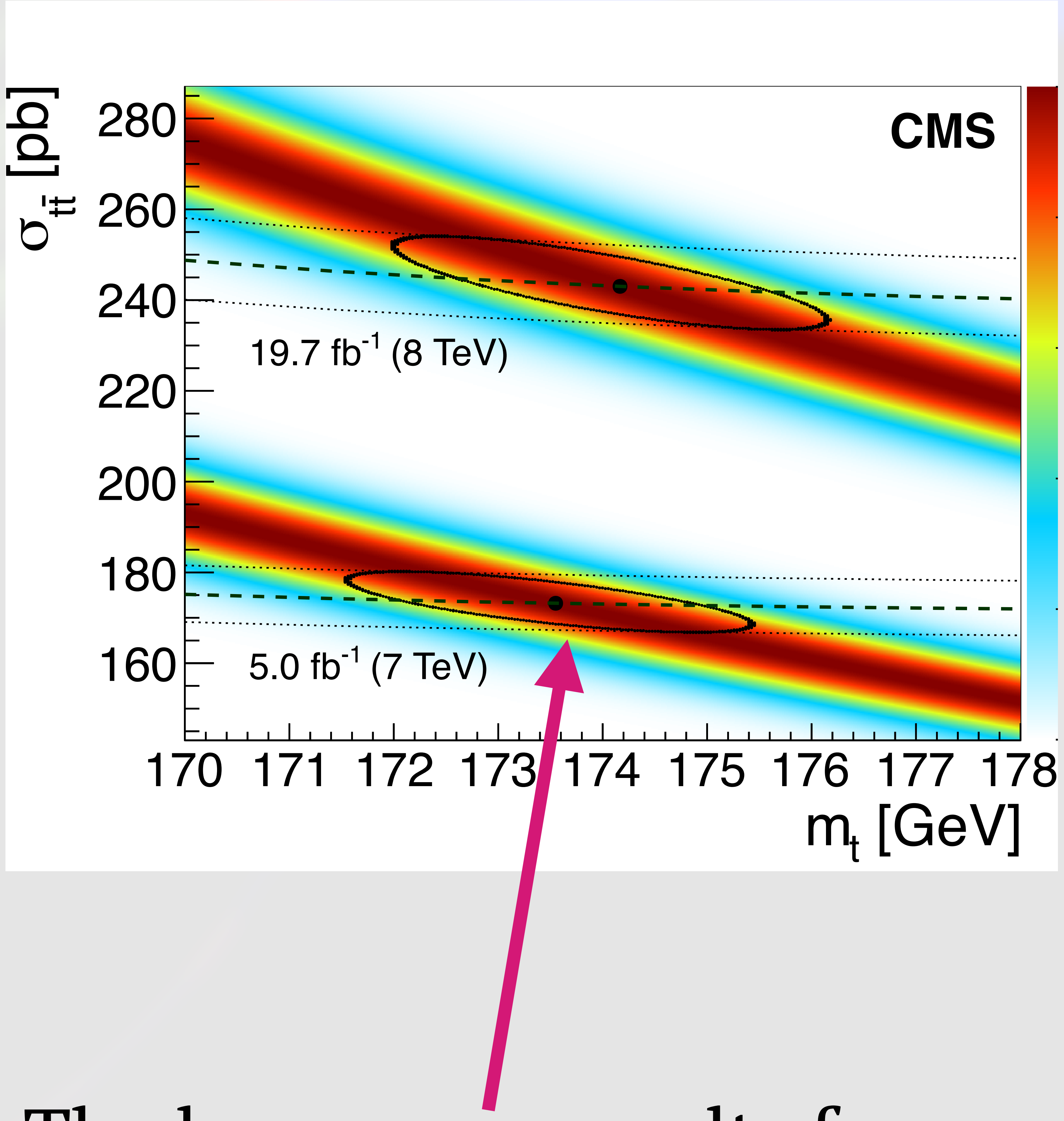


Theoretically cleanest way: Count the tops

Czakon, Mitov 2012, 2013; Aliev et al. 1007.1327



1210.6832



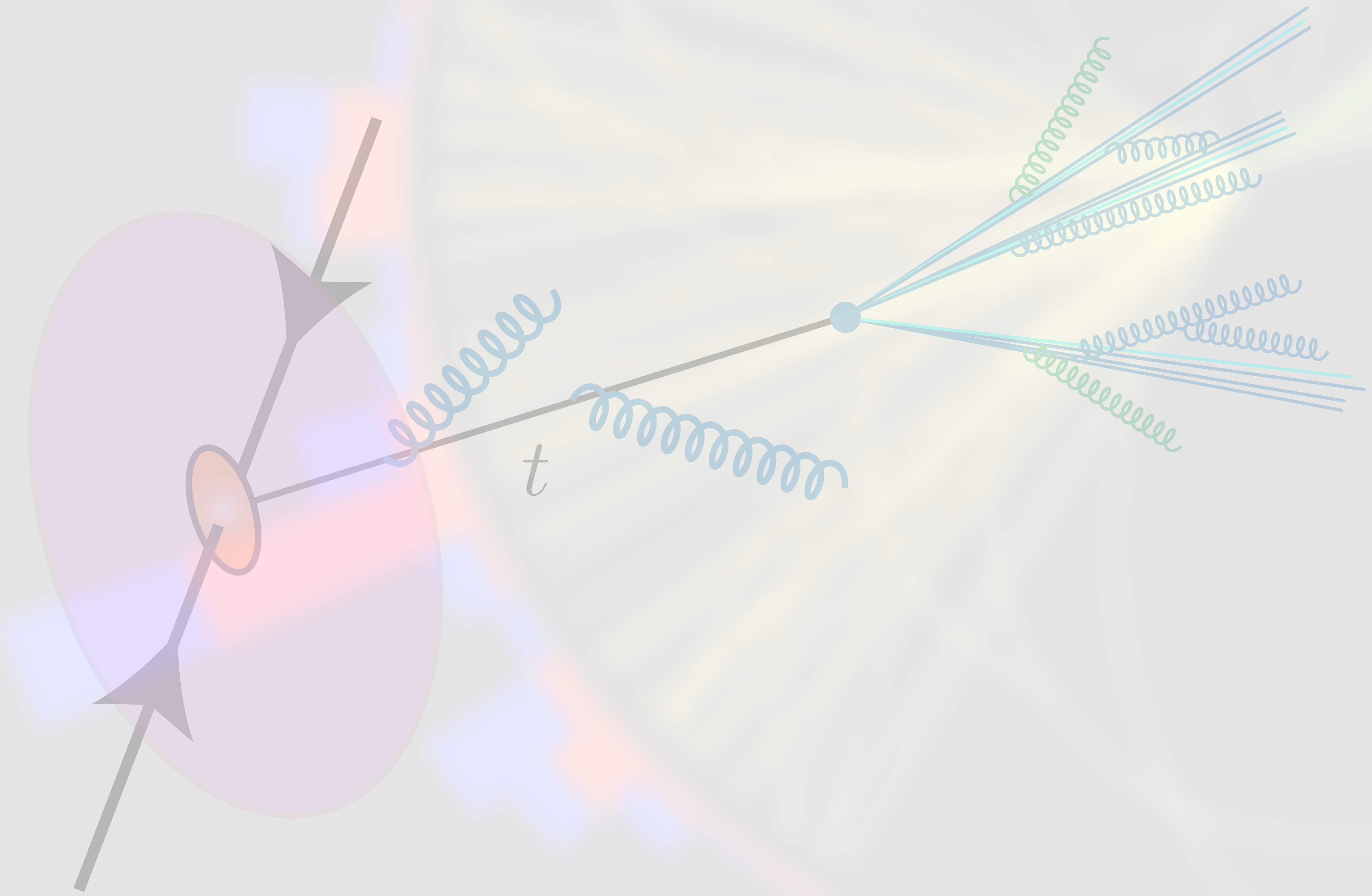
$$m_t^{\text{pole}} = 172.9^{+2.5}_{-2.6}\ \text{GeV}$$ ATLAS, 1406.5375

$$m_t^{\text{pole}} = 172.7^{+2.4}_{-2.7}\ \text{GeV}$$ CMS, 1701.06228

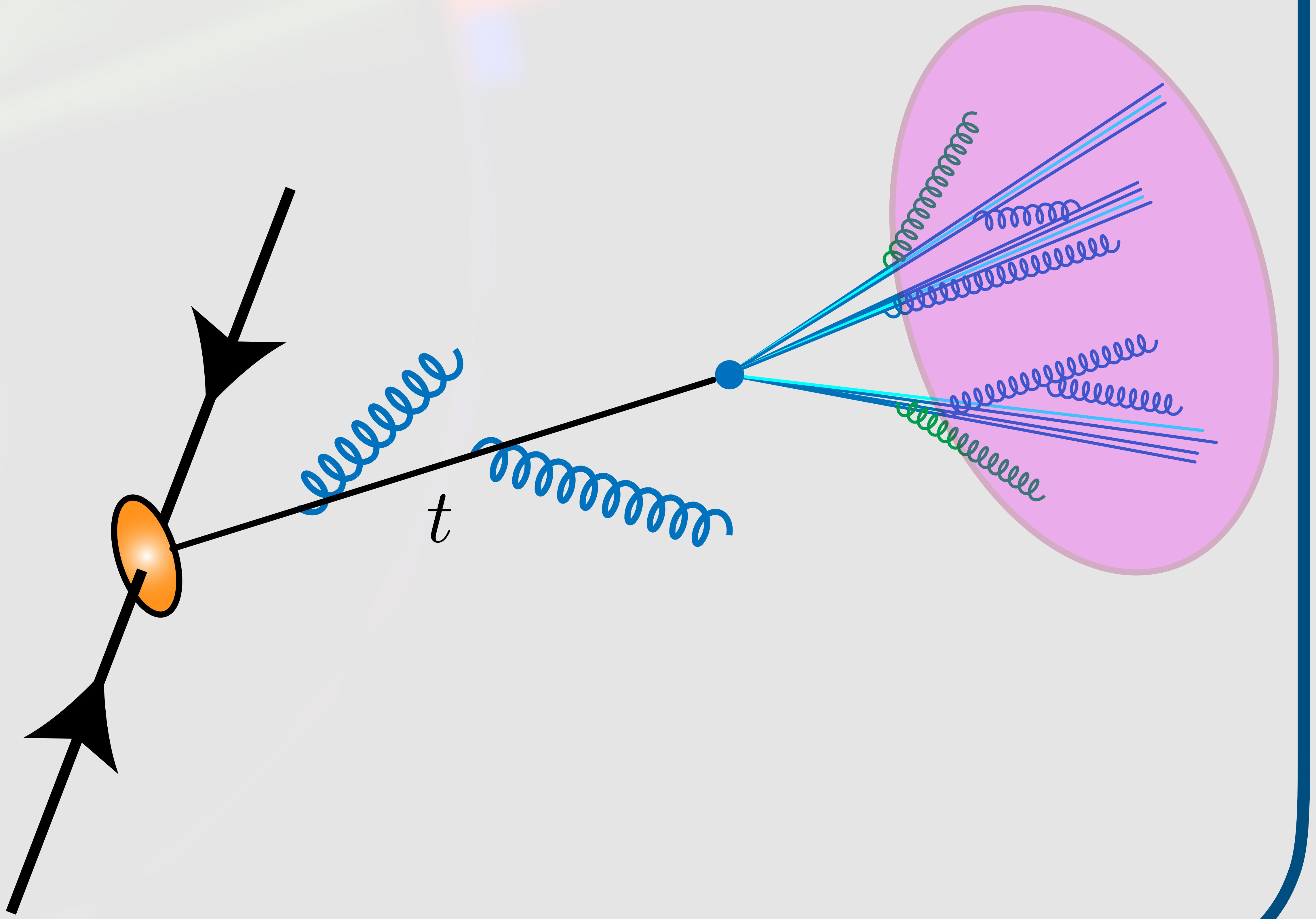
The large error results from normalization uncertainty

How to measure the top mass?

1. Exploit the production mechanism



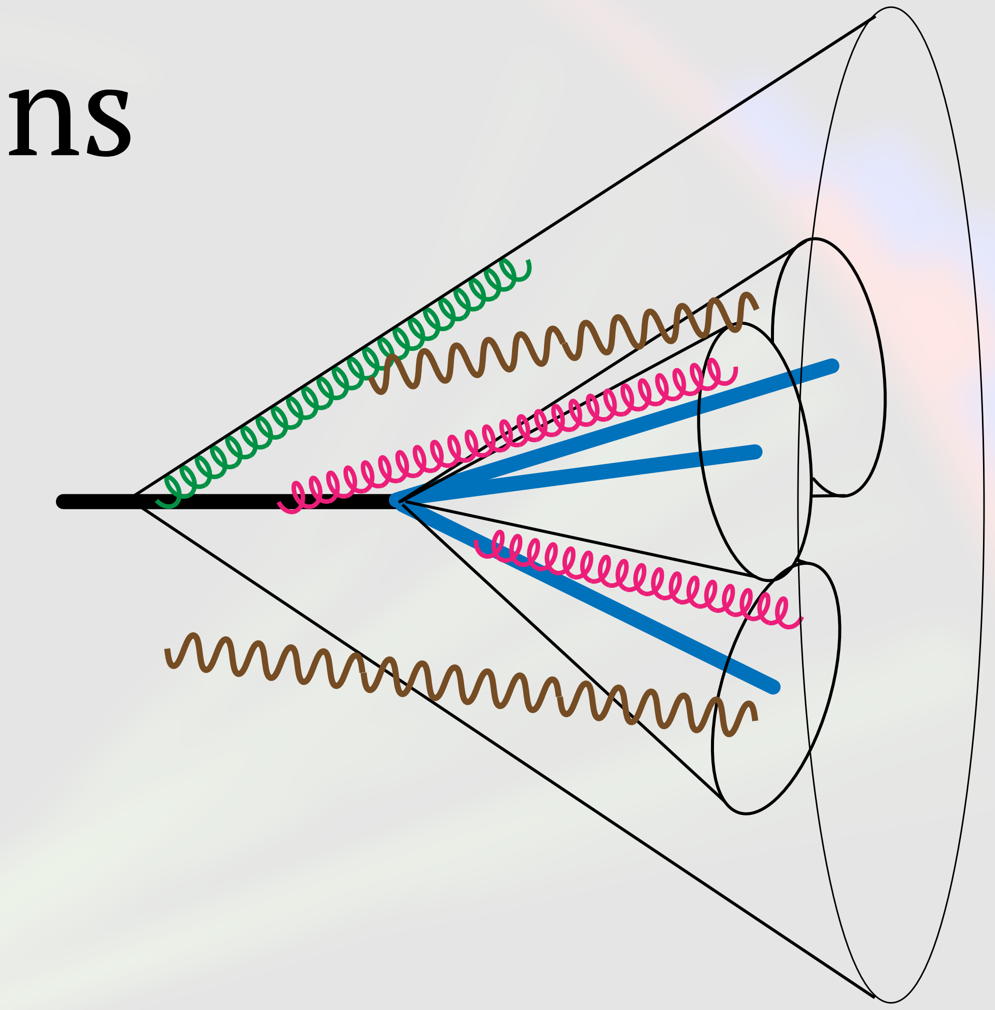
2. Exploit the final state decay products

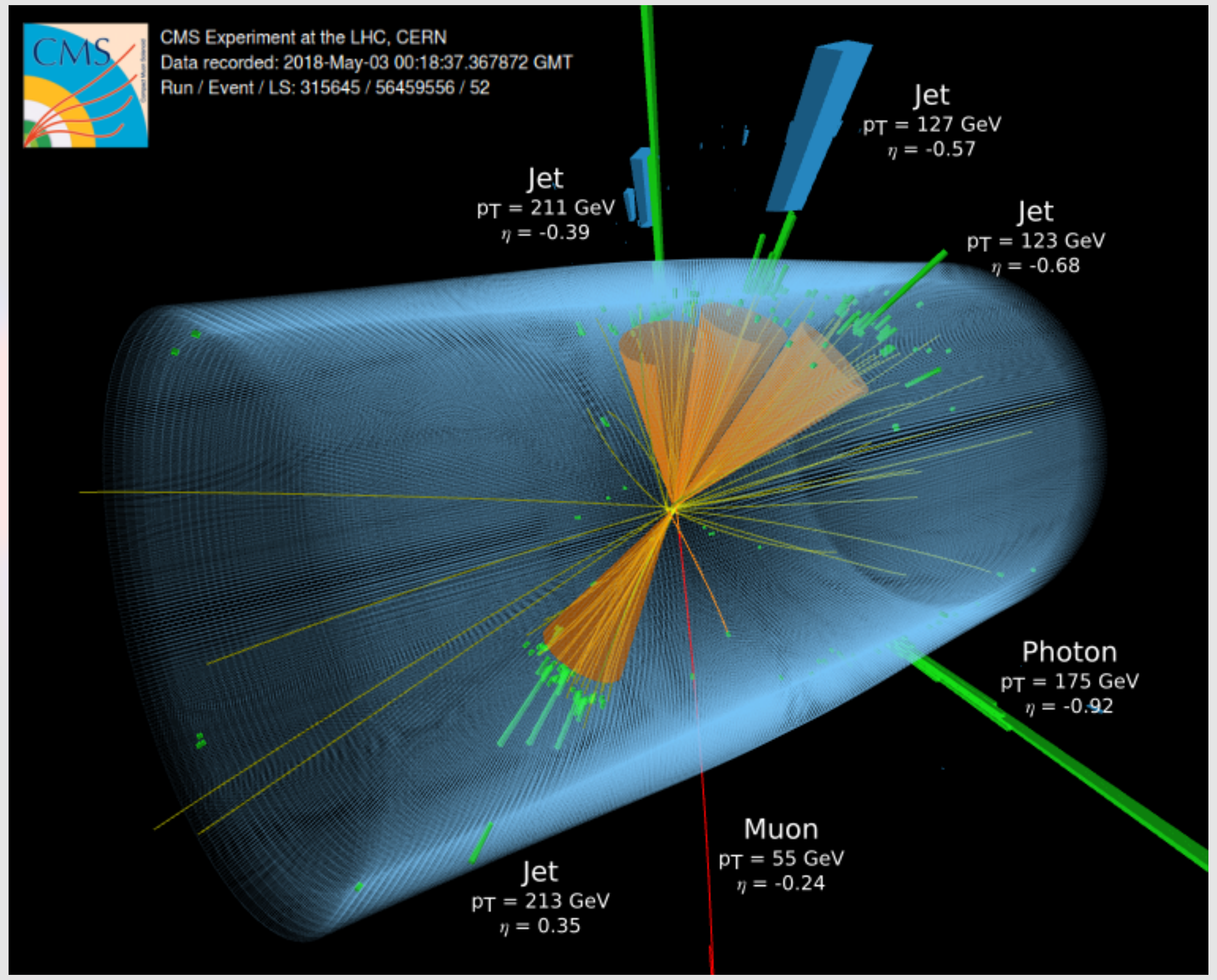


2. Exploit the final state decay products

Measure all sorts of differential distributions on top decay products:

$$\frac{d\sigma}{dm_t^{\mathrm{reco}}}, \quad \frac{d\sigma}{dM_{bl}}, \quad \frac{d\sigma}{dM_{t\bar{t}}}, \quad \frac{d\sigma}{dM_{t\bar{t}j}}$$





Use $E = mc^2$

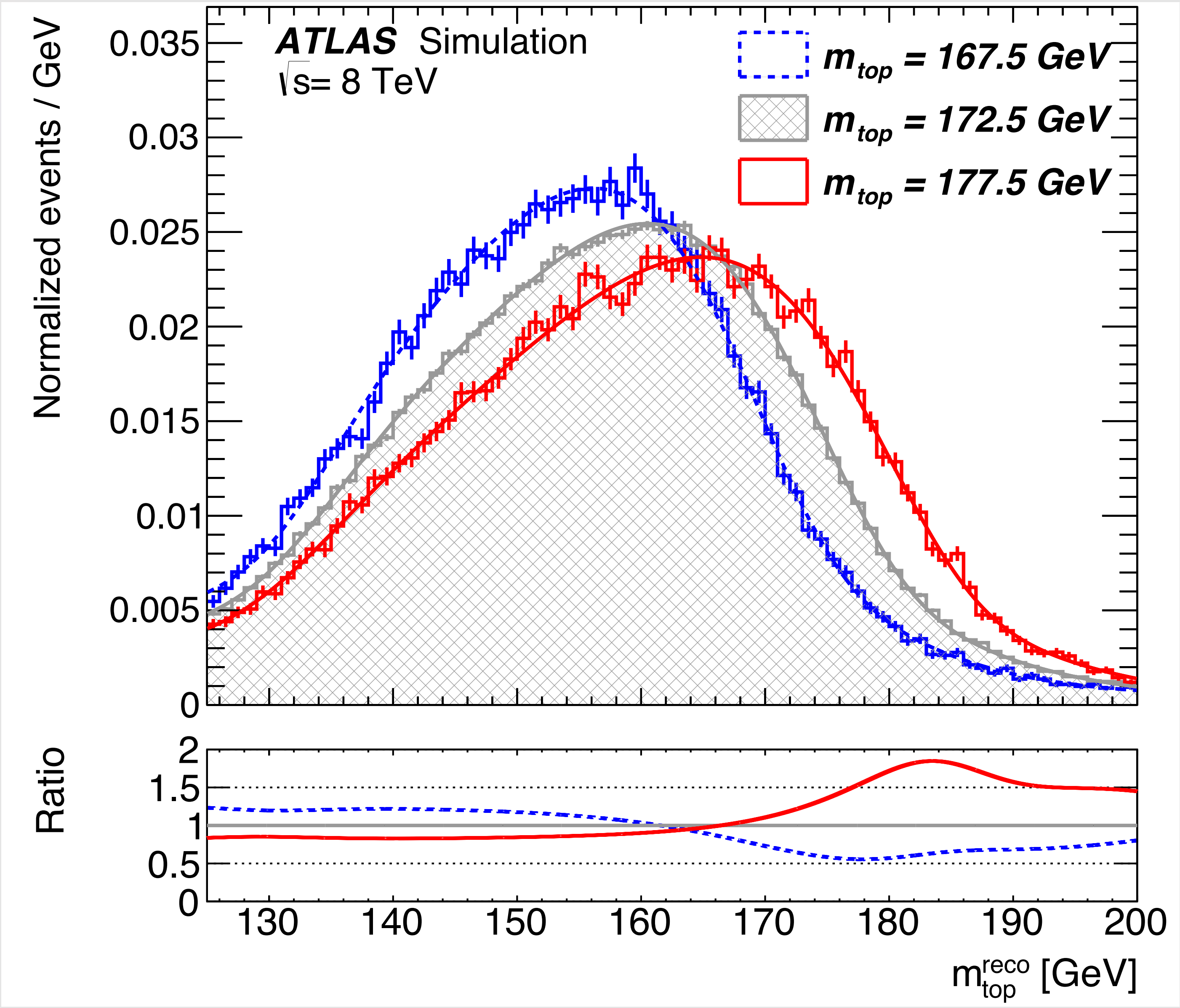
This approach has yielded the most precise measurements:

$$m_t^{\mathrm{MC}} = 172.69 \pm 0.48\,\mathrm{GeV}$$ ATLAS, 1810.01772

$$m_t^{\mathrm{MC}} = 172.26 \pm 0.61\,\mathrm{GeV}$$ CMS, 1812.06489

Conceptual problem: ***What mass is m_t^{MC}?***

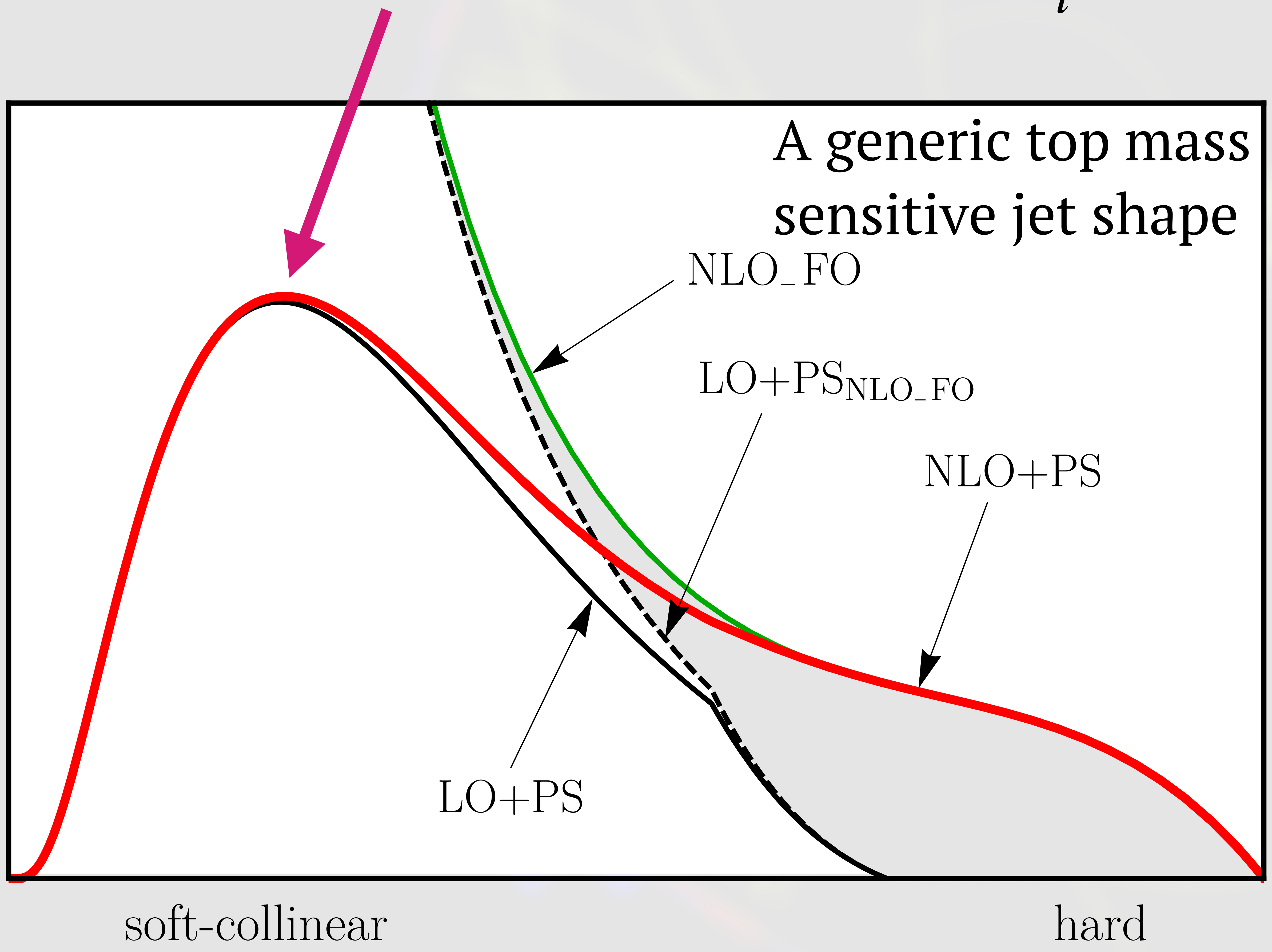
Simulating the top as a particle with a definite mass ignores $\mathcal{O}(1\,\mathrm{GeV})$ long-distance effects



Why top mass interpretation problem?

$$\left(\frac{d\sigma}{dm_t^{\mathrm{reco}}}, \quad \frac{d\sigma}{dM_{bl}}, \quad \frac{d\sigma}{dM_{t\bar{t}}}, \quad \frac{d\sigma}{dM_{t\bar{t}j}}\right)$$

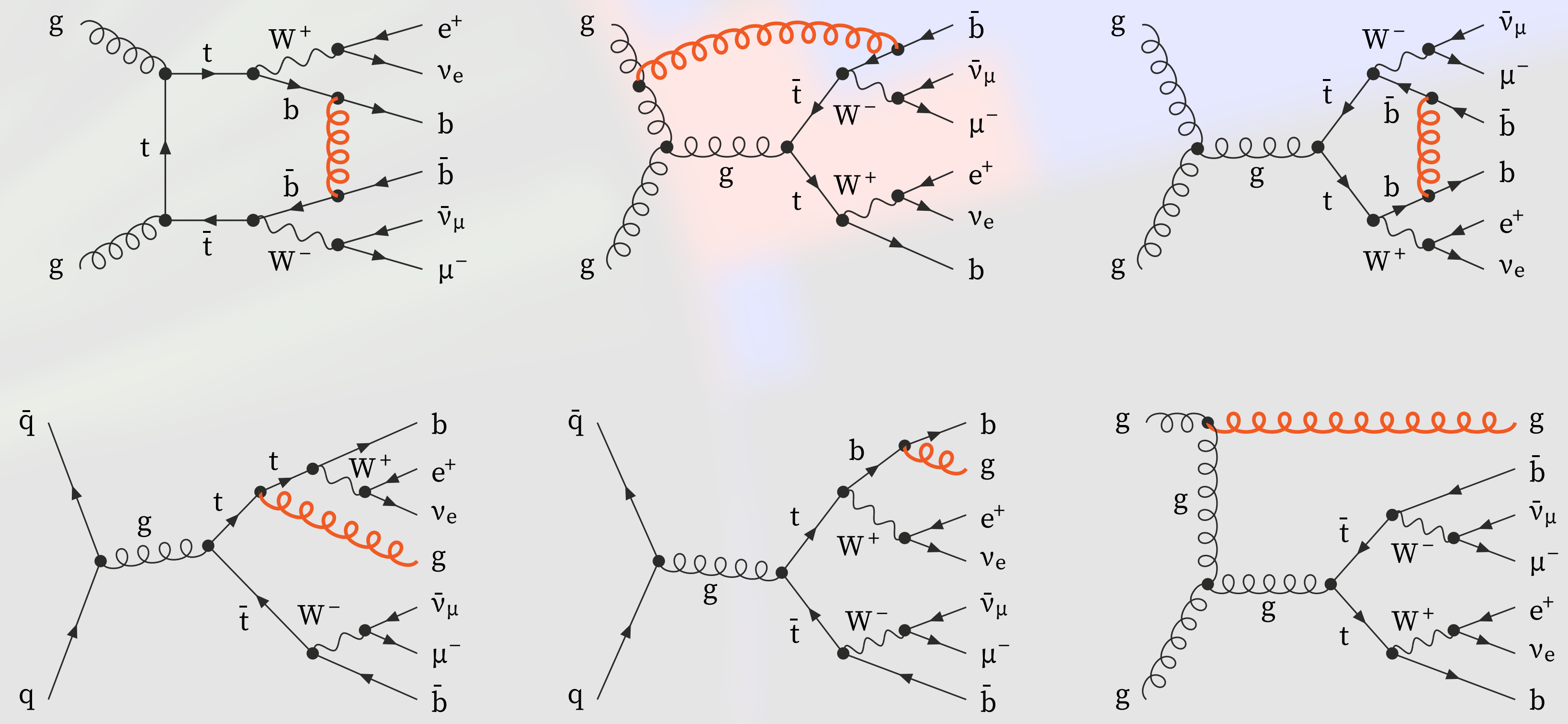
Threshold structure sensitive to m_t



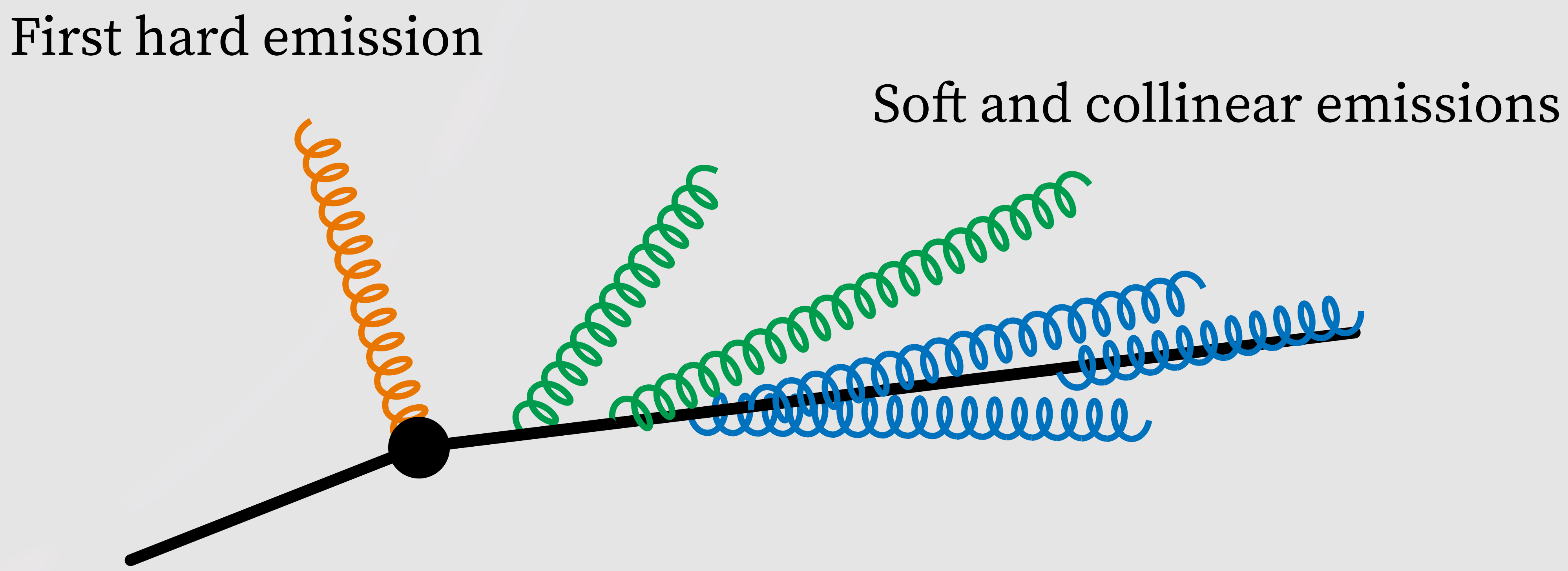
Hoang 2004.12915 + S. Plätzer

Top Production and decay at NLO, NNLO

Mazzitelli et al. 2012.14267; Cormier et al. 1810.06493; Frederix et al. 1603.01178; Jezo et al. 1607.04538; Hoeche et al. 1402.6293



Denner et al. 1207.5018



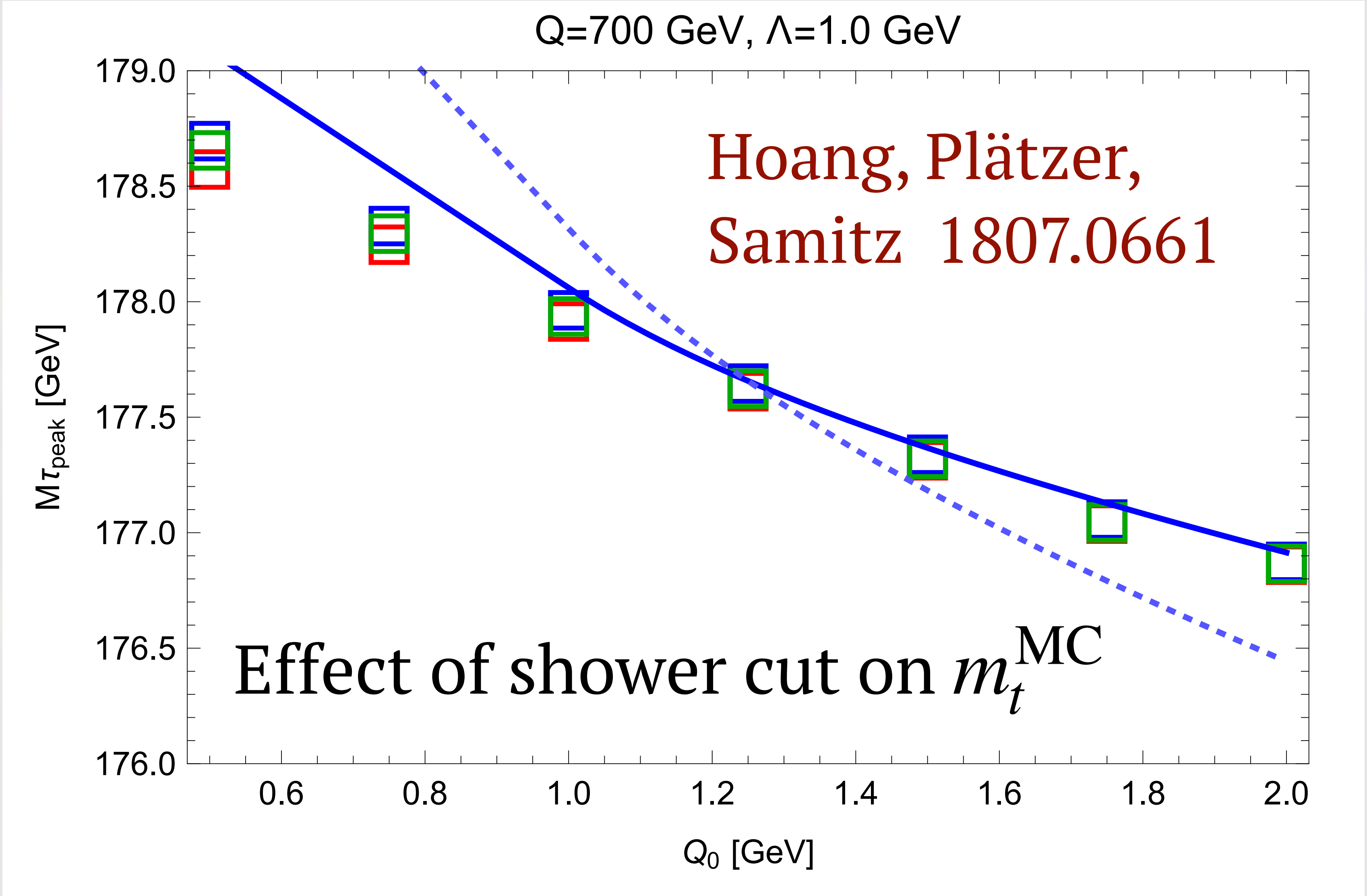
First hard emission

Soft and collinear emissions

Why top mass interpretation problem?

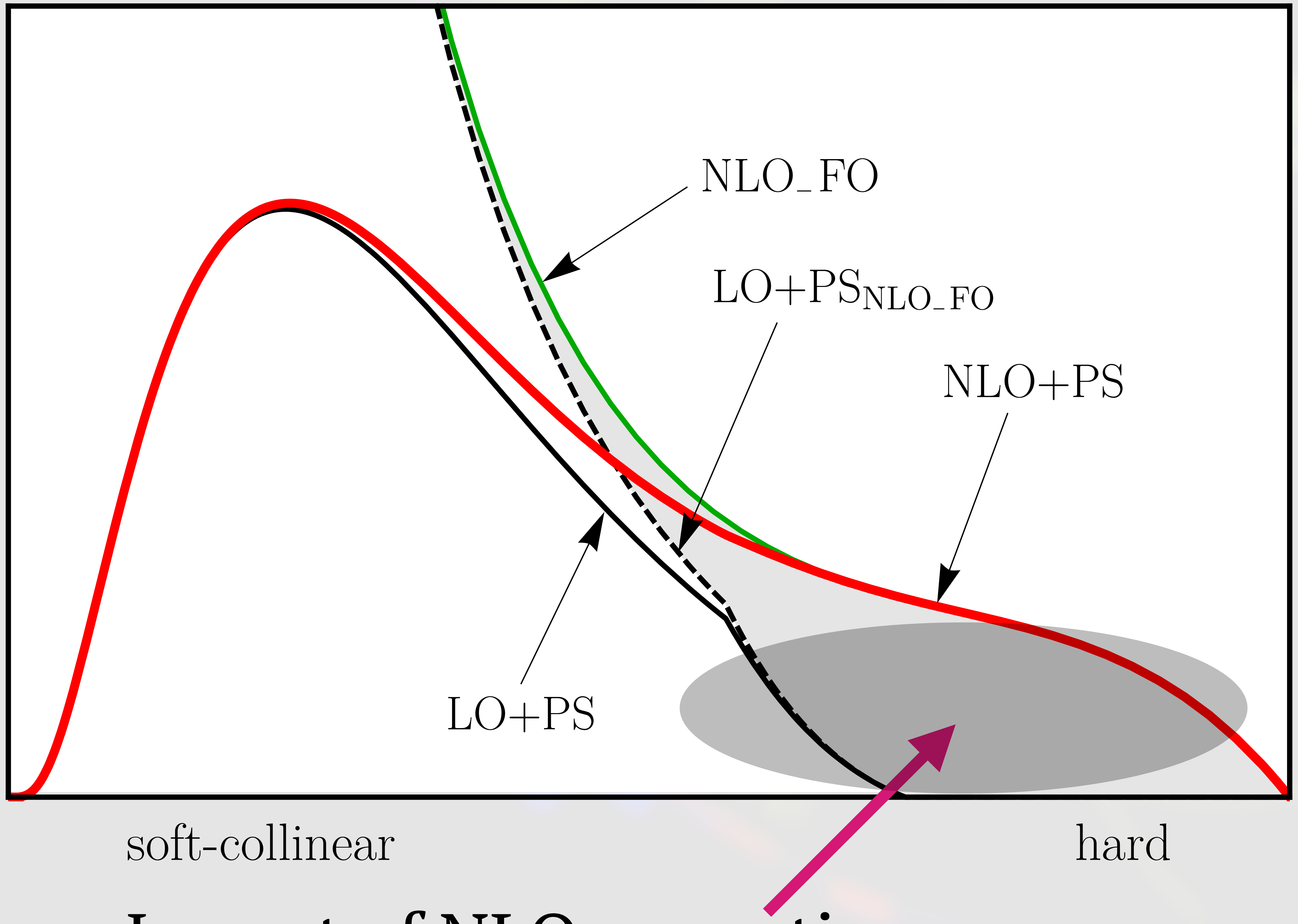
Observations:

1. Threshold structure appears in the soft-collinear region
2. NLO corrections make an impact only in the tail



Hoang, Plätzer, Samitz 1807.0661

Effect of shower cut on m_t^{MC}



Impact of NLO corrections

*Implications for **direct measurements:***

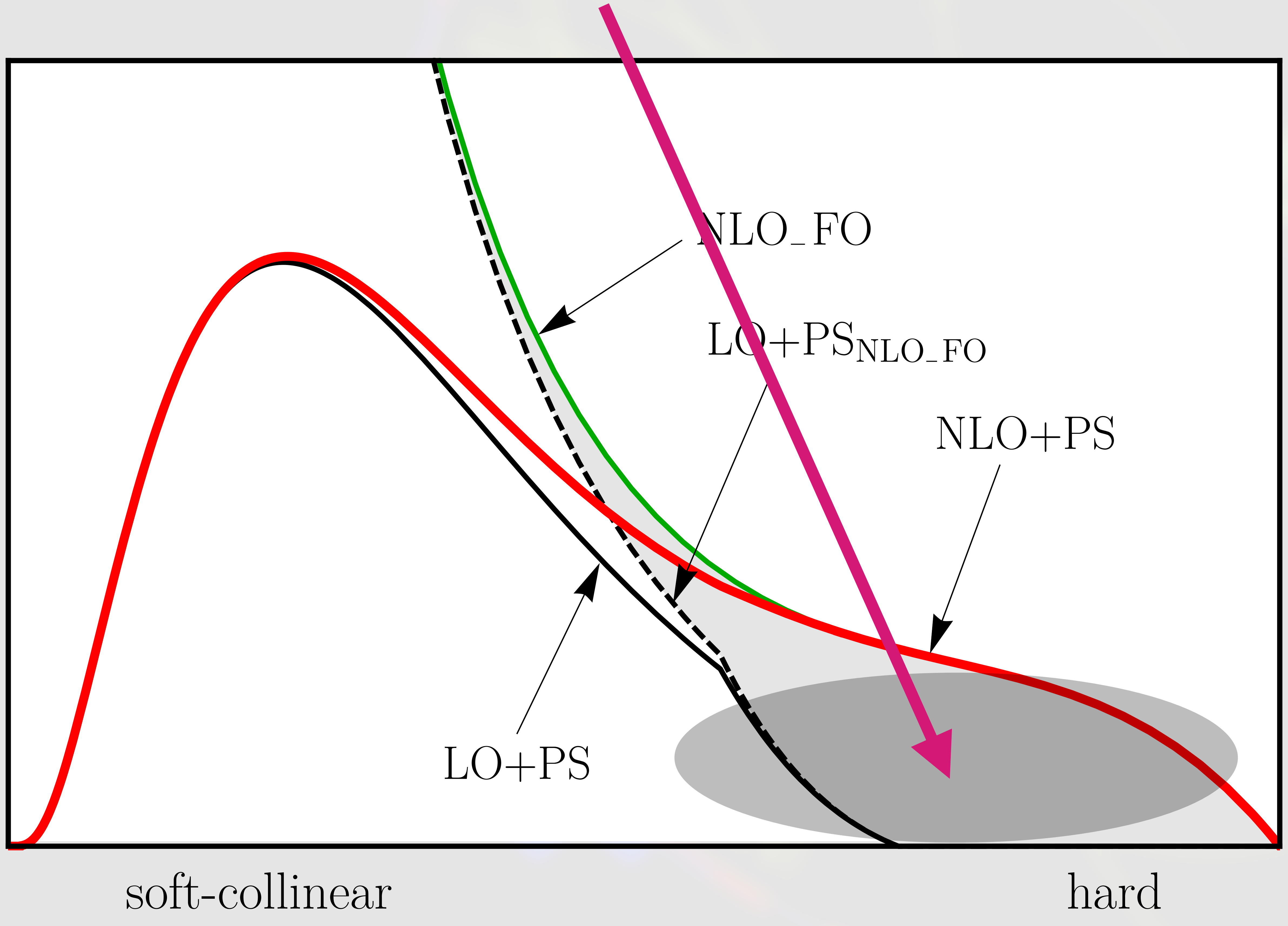
1. Very challenging to improve PS beyond NLL. Hadronization models make up for inadequacies of the PS: poor theoretical control.
2. PS impacts the meaning of the MC top mass parameter: effects as large as 0.5 GeV.

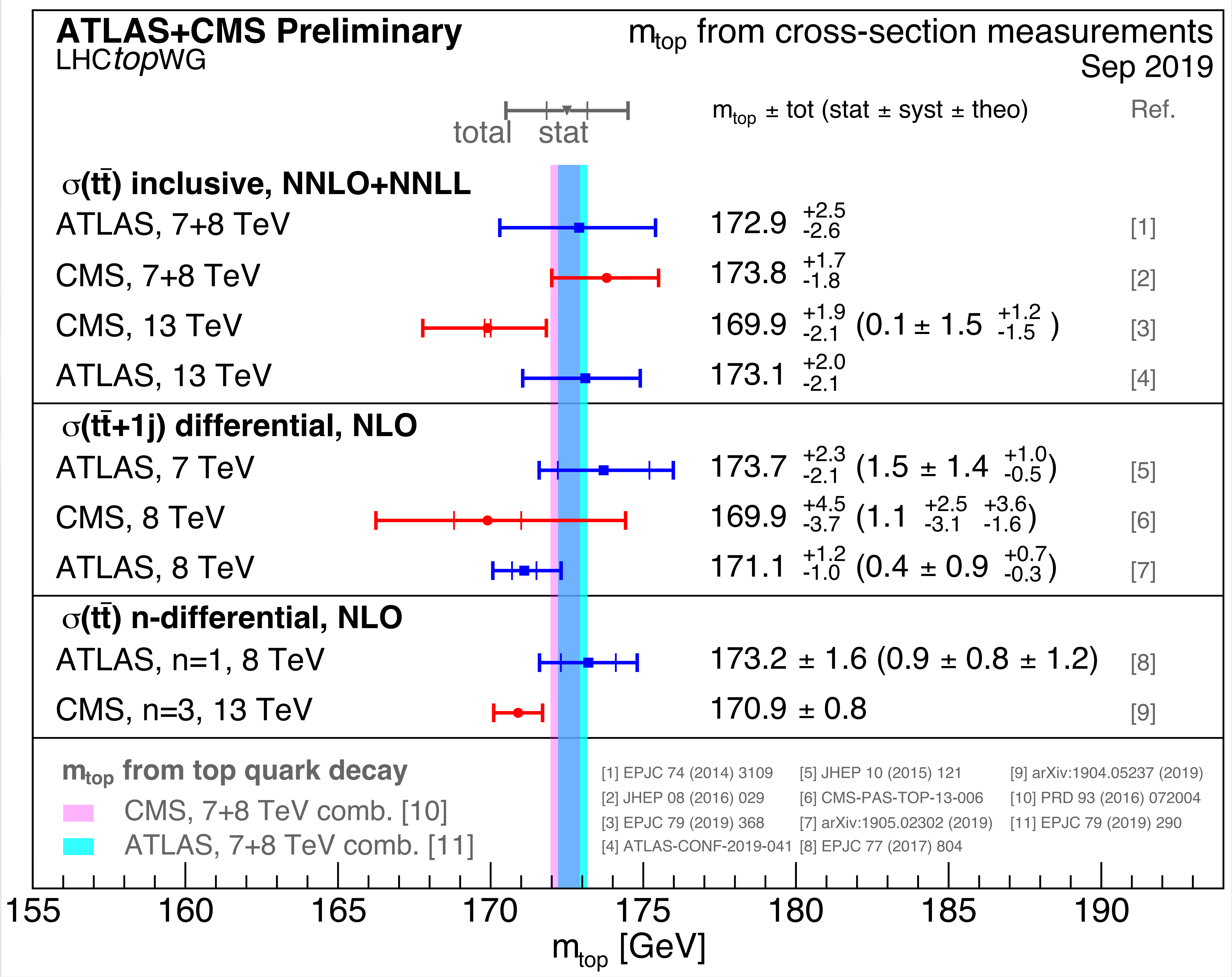
Hoang, Plätzer, Samitz 1807.0661

Avoid threshold region: indirect measurements

Away from threshold NLO matched MC are reliable

Focus here for good theoretical control

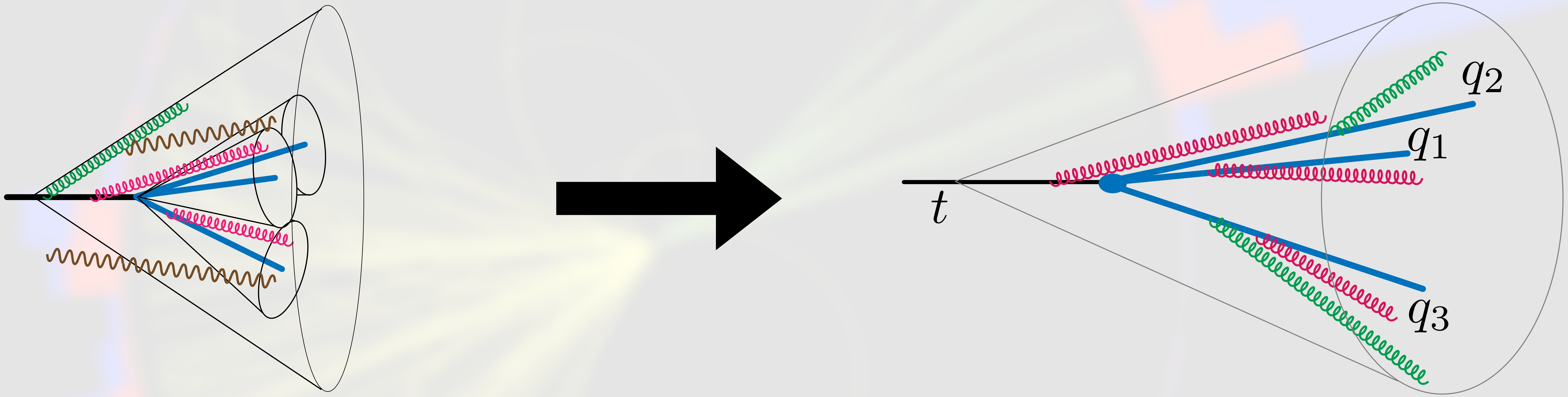




Unfortunately, poor sensitivity when not leveraging the threshold

Analytical resummation

Resummation of observables such as m_t^{reco} is extremely complicated so consider a simpler observable: the jet mass



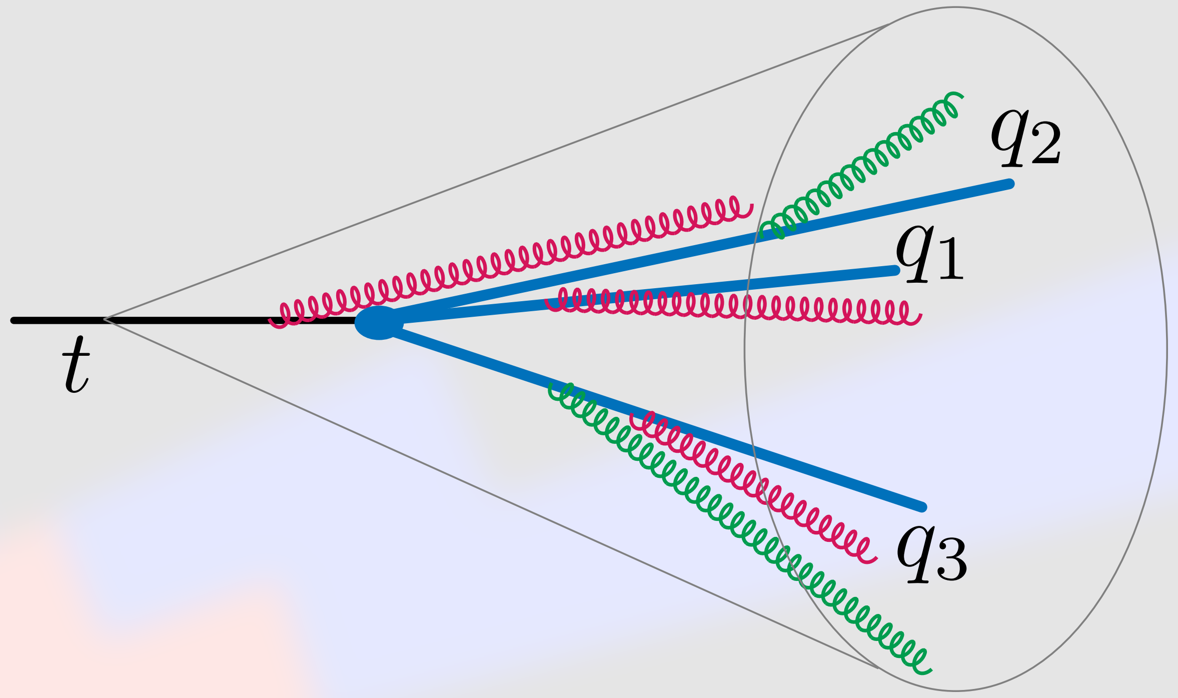
$$M_J^2 = \left(\sum_{i \in J} p_i^\mu \right)^2 \simeq m_t^2 + \Gamma_t m_t + \ldots$$

Fleming et al. hep-ph/0703207, 0711.2079

Goal is to compute an analytical prediction which can be compared with data to extract the top mass.

Analytical resummation

Consider the jet mass:

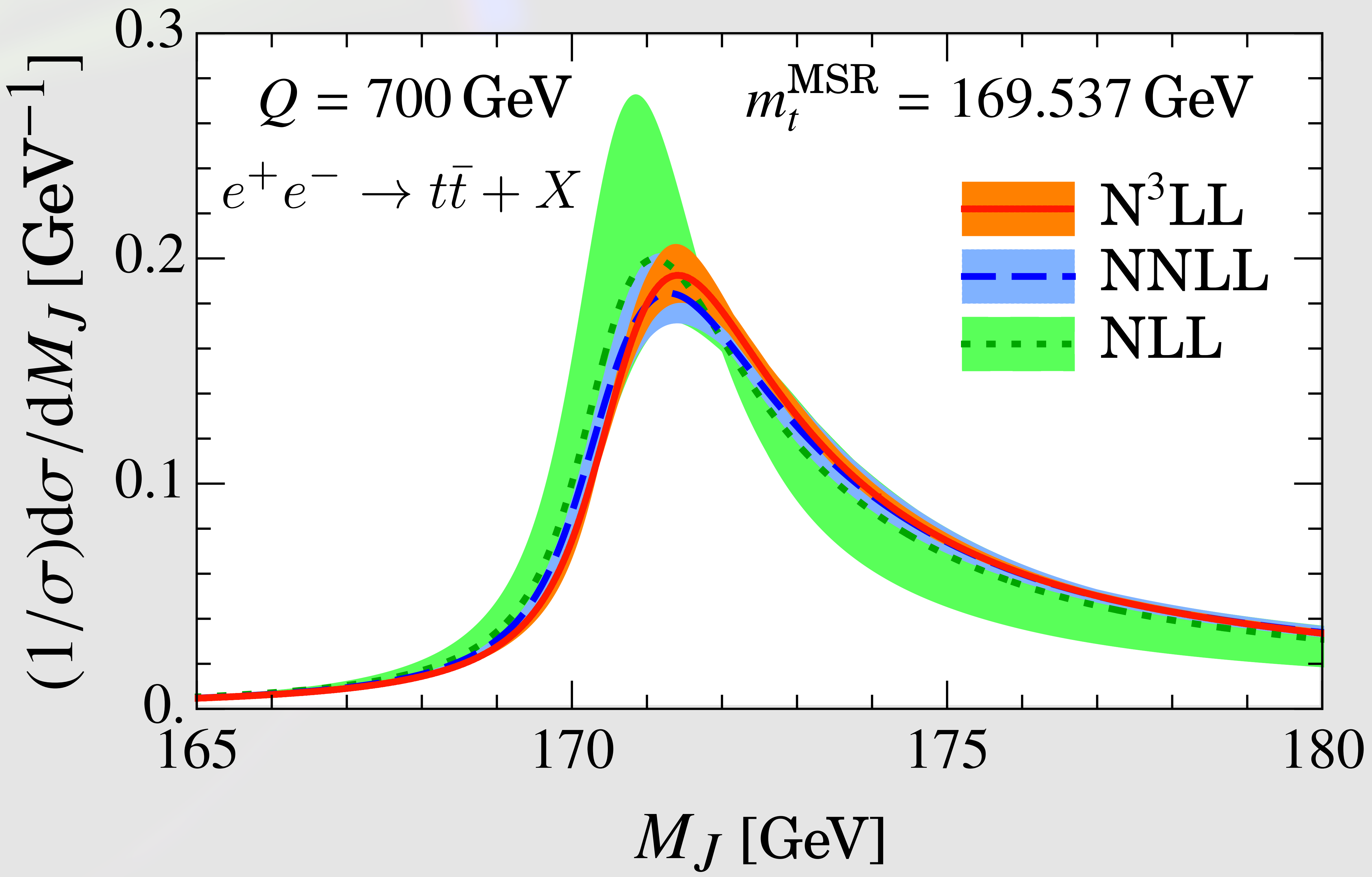


$$M_J^2 = \Big(\sum_{i\in J} p_i^\mu\Big)^2 \simeq m_t^2 + \Gamma_t m_t + \dots$$

Resummation using SCET and HQET

$$\frac{1}{\sigma_0}\frac{\mathrm{d}\sigma}{\mathrm{d}\tau_2} = m_t\, Q^2 H_{\mathrm{evol}}^{(5,6)}(Q, m_t, \varrho, \mu; \mu_H, \mu_m)$$
$$\times \int \mathrm{d}\ell\, \mathrm{d}\hat{s}\, U_B^{(5)}(\hat{s}_\tau - \varrho\ell - \hat{s}, \mu, \mu_B)\, J_{B,\tau_2}^{(5)}(\hat{s}, \Gamma_t, \delta m, \mu_B)$$
$$\times \int \mathrm{d}\ell' \mathrm{d}k\, U_S^{(5)}(\ell - \ell', \mu, \mu_S) \hat{S}_{\tau_2}^{(5)}(\ell' - k, \bar{\delta}, \mu_S) F(k - 2\Delta)\,,$$

Calculate in your favorite top mass scheme δ_m

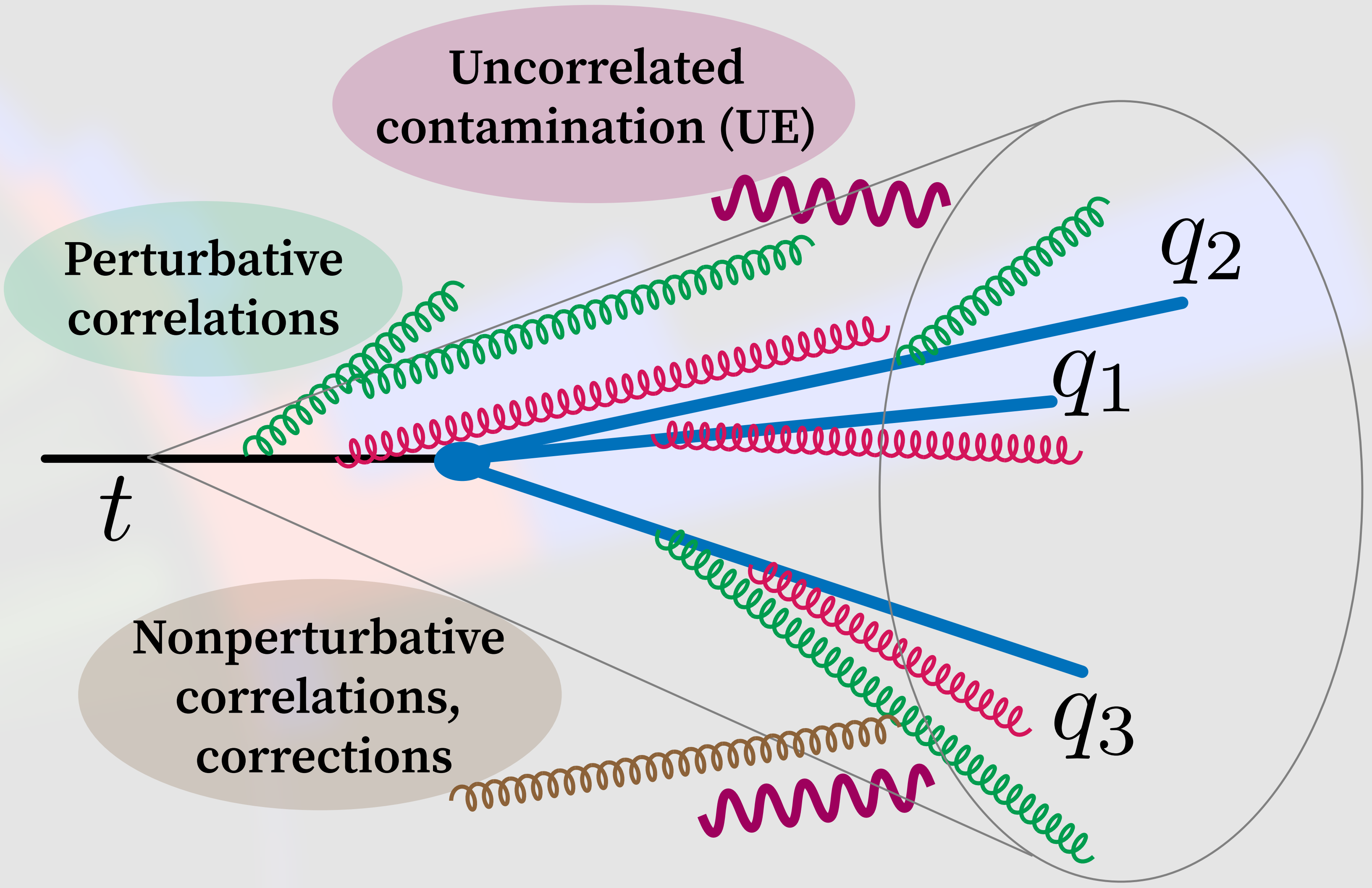


Bachu, Hoang, AP, Mateu, Stewart 2012.12304

Analytical resummation

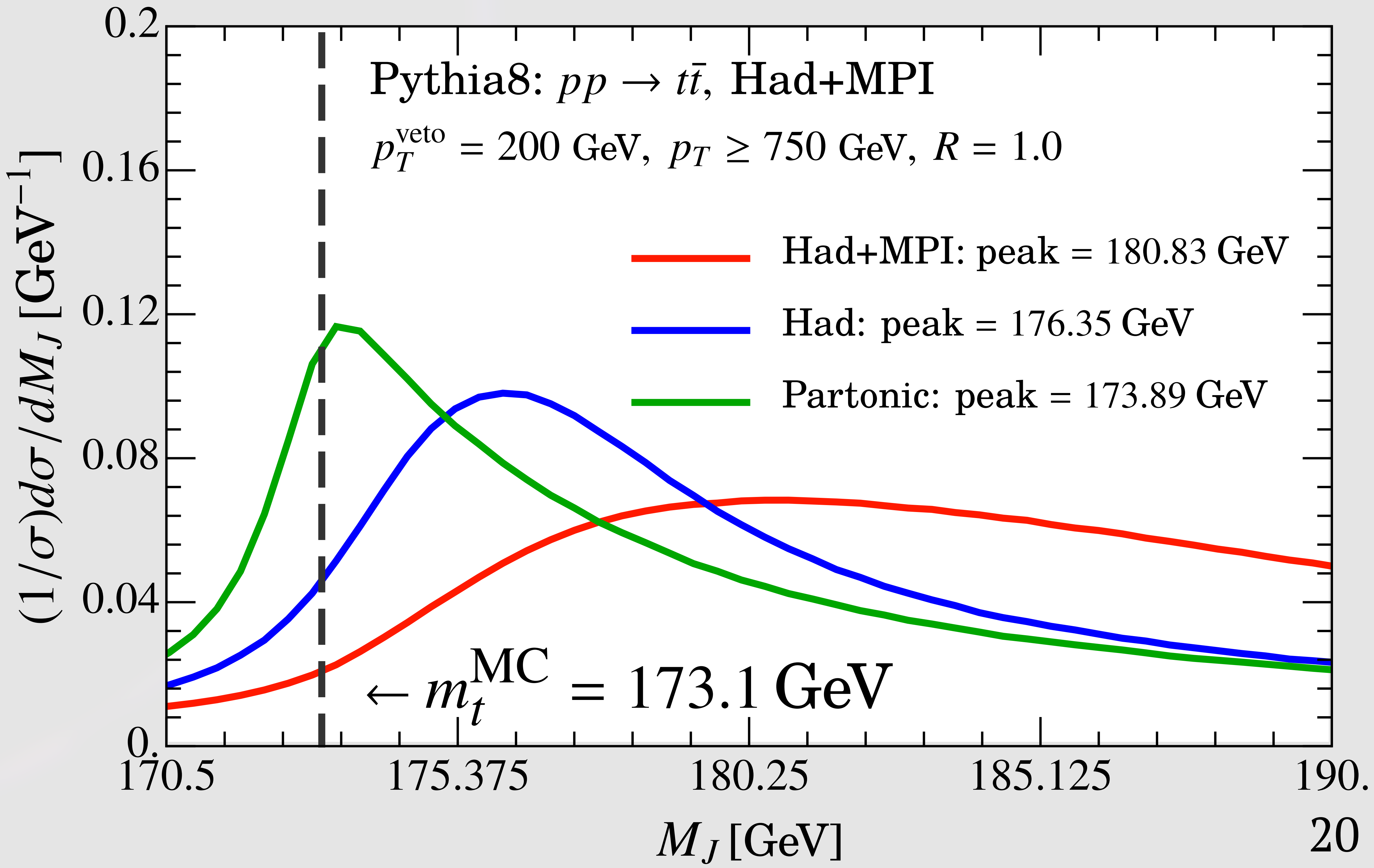
Consider the jet mass:

$$M_J^2 = \left(\sum_{i \in J} p_i^\mu \right)^2 \simeq m_t^2 + \Gamma_t m_t + \ldots$$



Challenges in pp

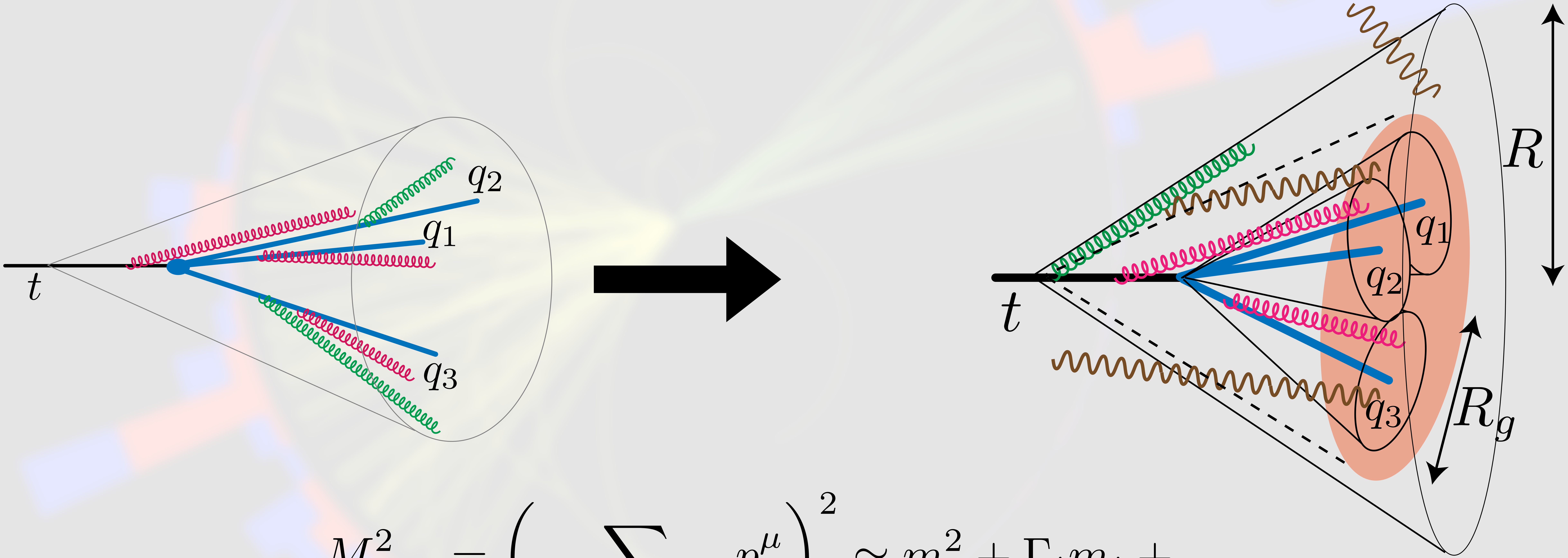
- Strongly correlated with outside radiation
- Precision spoiled by uncorrelated contamination



Soft drop jet mass

Dasgupta et al. 1307.0007; Larkoski, Marzani, Soyez, Thaler 1402.2657

Improve robustness for the LHC by considering the soft drop jet mass



$$M^2_{J,\mathrm{sd}} = \Bigg(\sum_{i \in J^{\mathrm{groomed}}} p_i^\mu \Bigg)^2 \simeq m_t^2 + \Gamma_t m_t + \ldots$$

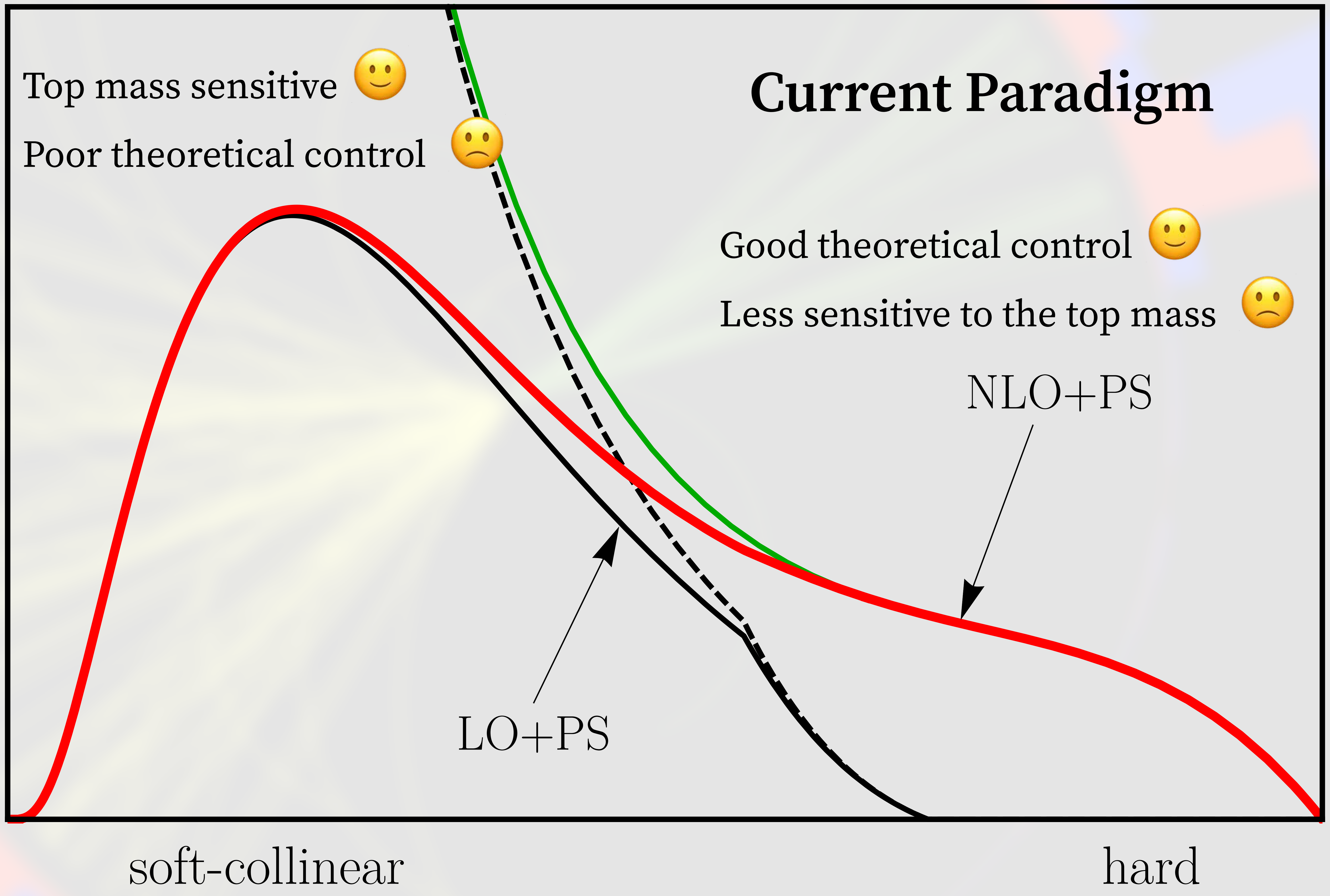
Soft drop jet mass

Soft drop improves resilience of the peak against hadronization and the UE

A challenging task to account for residual shifts

Hoang, AP, Mantry, Stewart 1906.11843;
AP, Stewart, Vaidya, Zoppi 2012.15568
Hoang, Mantry, AP, Stewart 1708.02586;
Hoang, Mantry, AP, Stewart and ATLAS,
ATL-PHYS-PUB-2021-034

Summary of challenges in the current paradigm



Current Paradigm

Top mass sensitive 🙂

Poor theoretical control 🙁

Good theoretical control 🙂

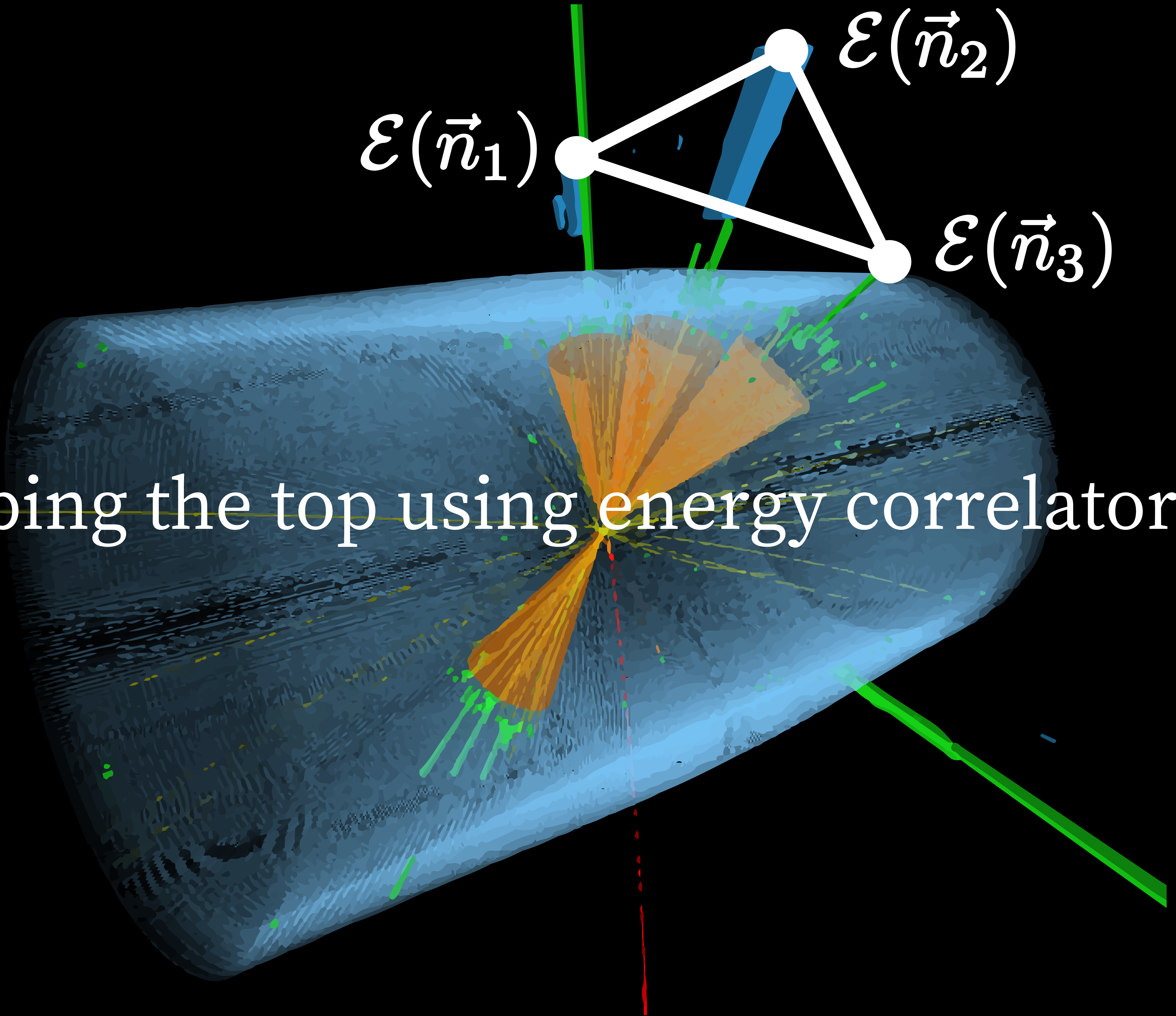
Less sensitive to the top mass 🙁

Overcome challenges in the new paradigm

To overcome these challenges we need:

1. Top mass sensitivity in the hard region
2. Insensitivity to soft physics and contamination from the underlying event

Probing the top using energy correlators



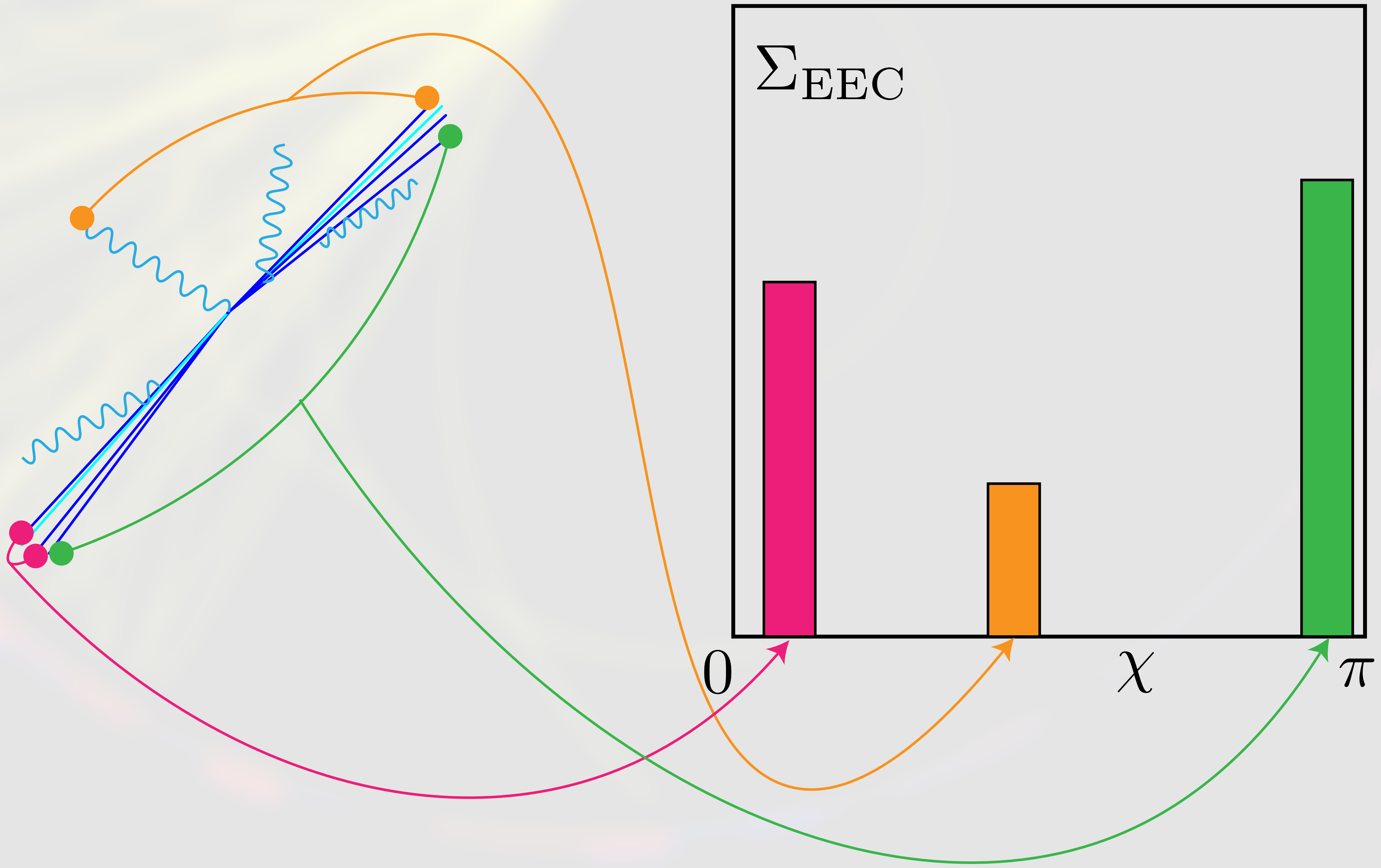
The 2-point correlator

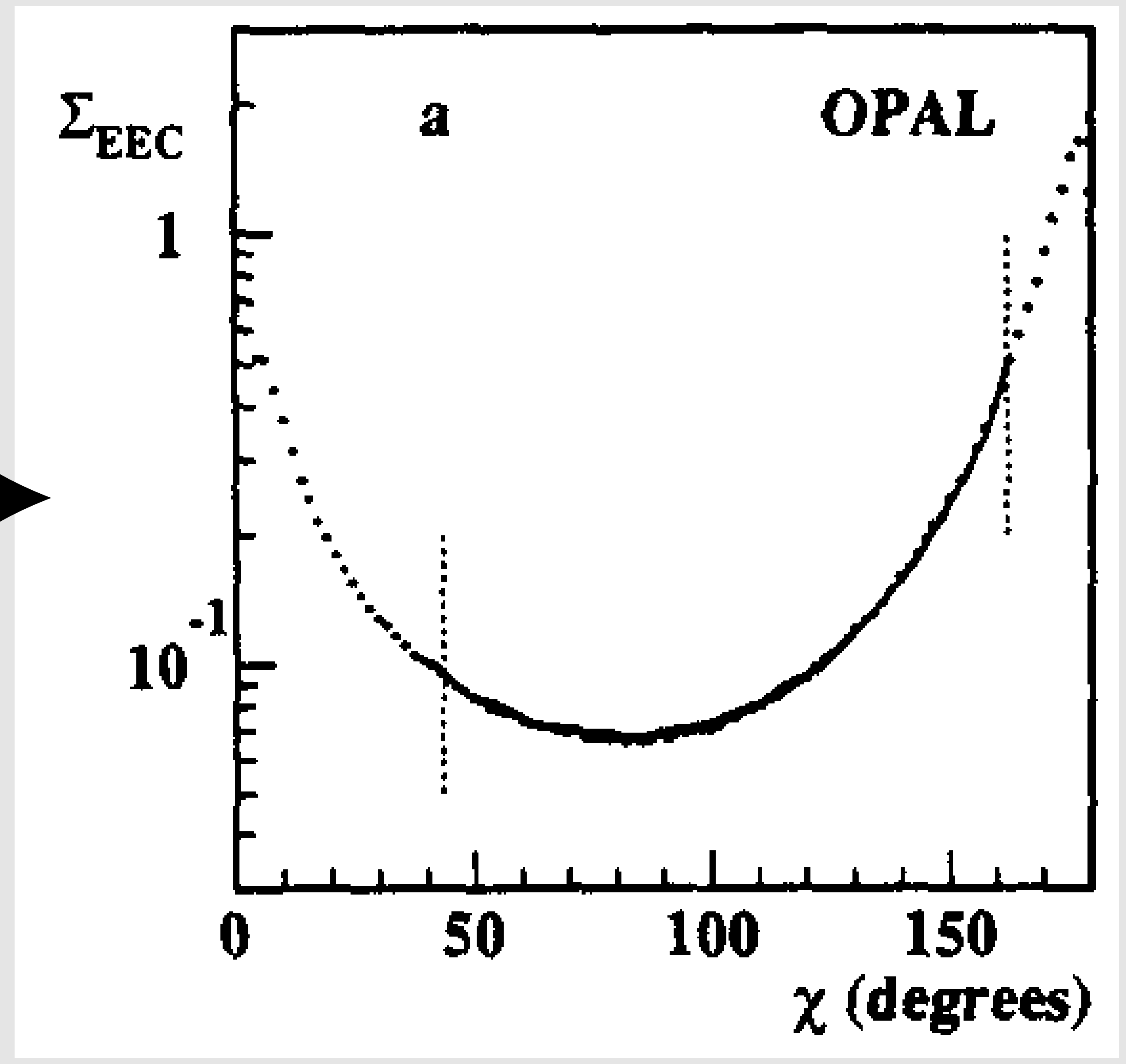
$$\langle \mathcal{E}(\vec{n}_1)\mathcal{E}(\vec{n}_2)\rangle = \sum_{ij}\int \frac{\mathrm{d}\sigma_{ij}}{\mathrm{d}^2\vec{n}_i\mathrm{d}^2\vec{n}_j} E_iE_j\delta^2(\vec{n}_1-\vec{n}_i)\delta^2(\vec{n}_2-\vec{n}_j)$$

Inclusive cross section to produce particles *i* and *j* + anything else!

$$\frac{\mathrm{d}\Sigma}{\mathrm{d}\cos\chi} = \int \mathrm{d}^2n_1\mathrm{d}^2n_2\,\delta(\vec{n}_1\cdot\vec{n}_2-\cos\chi)\frac{\langle \mathcal{E}(\vec{n}_1)\mathcal{E}(\vec{n}_2)\rangle}{Q^2}$$

Not event by event:



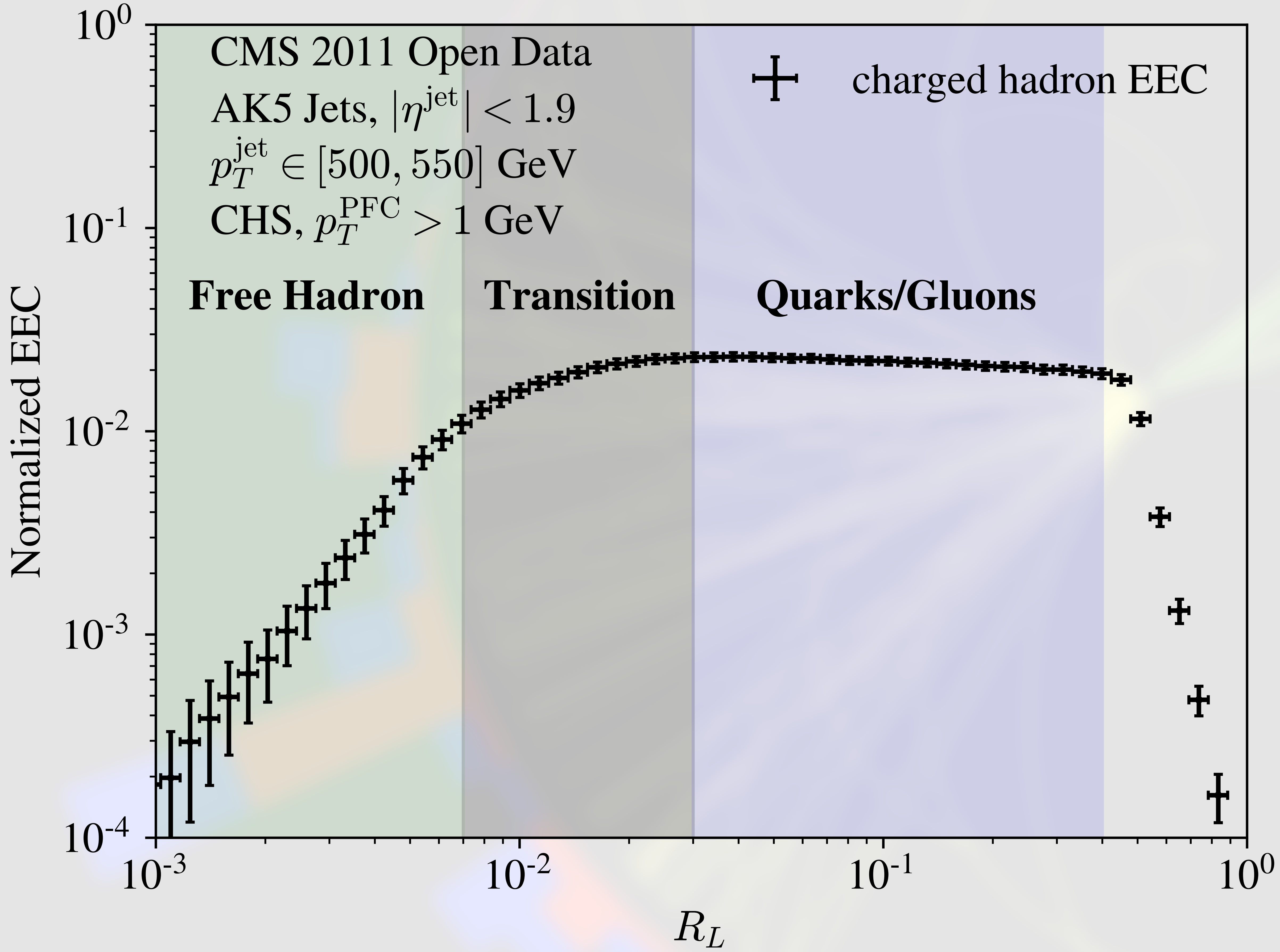


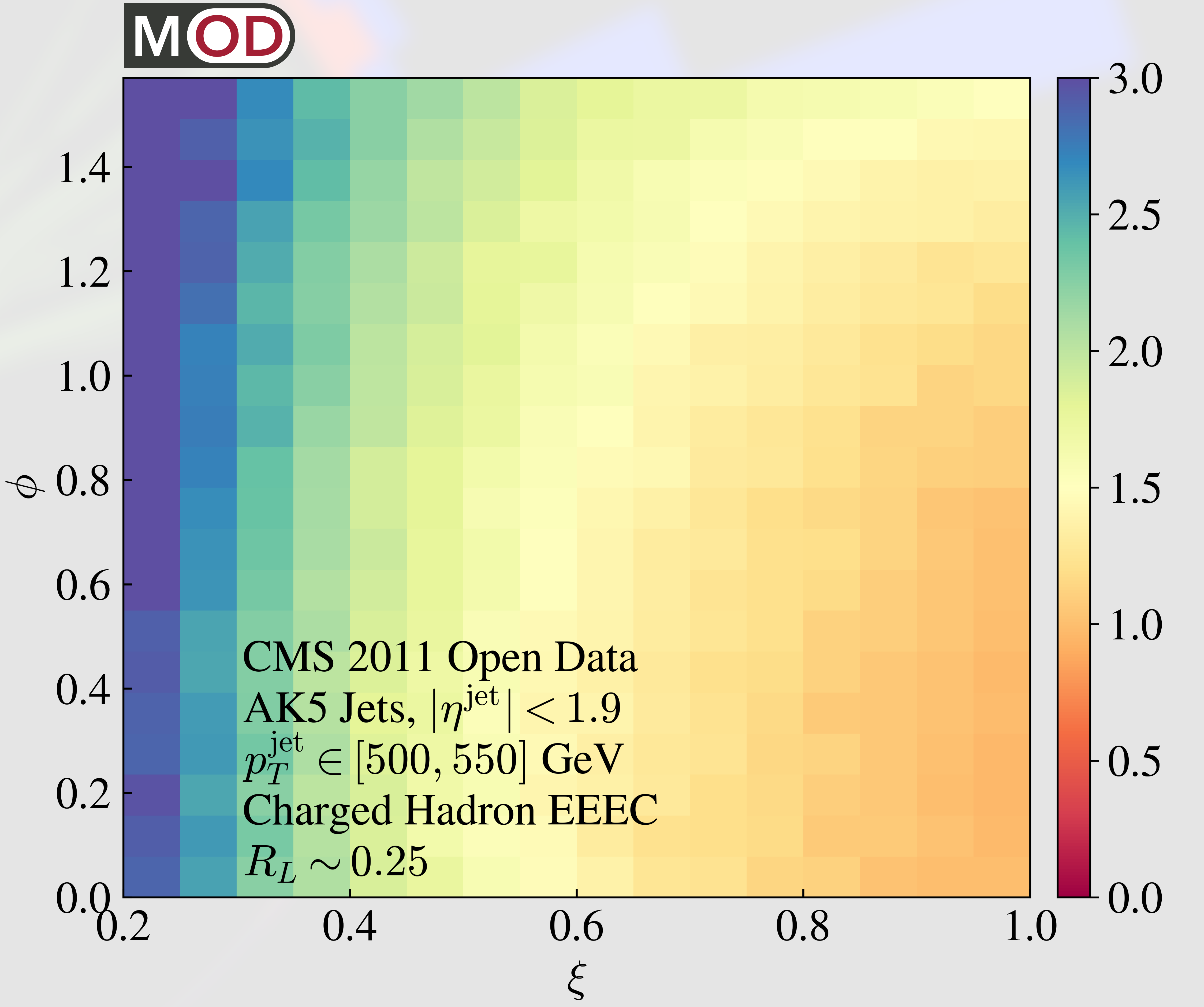
[Opal collboration, Z. Phys. C59 (1993) 21]

Progress in recent years

Energy correlators map transition from perturbative to free hadron phase

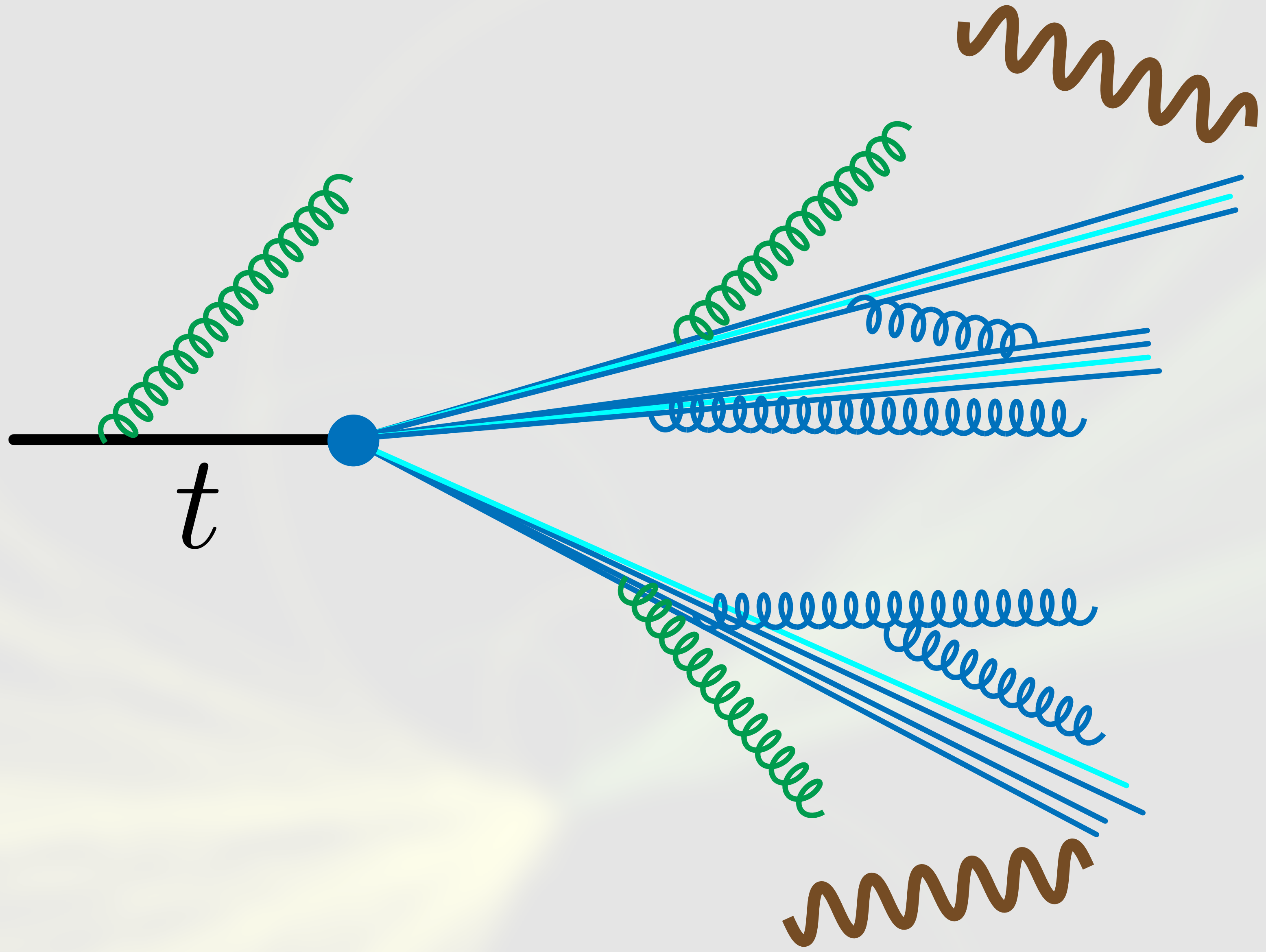
Komiske, Moult, Thaler, Zhu 2201.07800



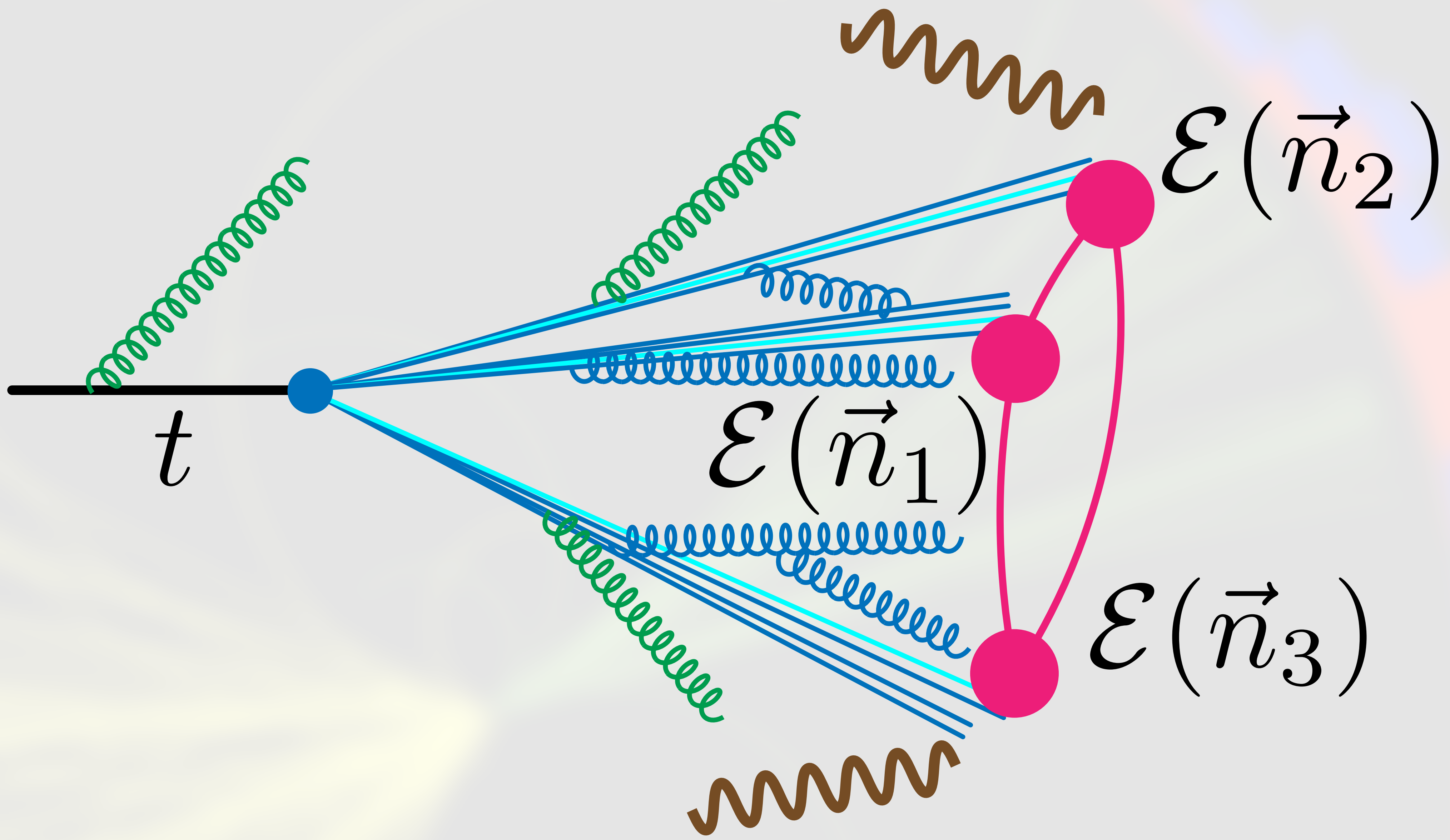


This talk: first time applying them to top quarks

Which correlator will well characterize the top decay?



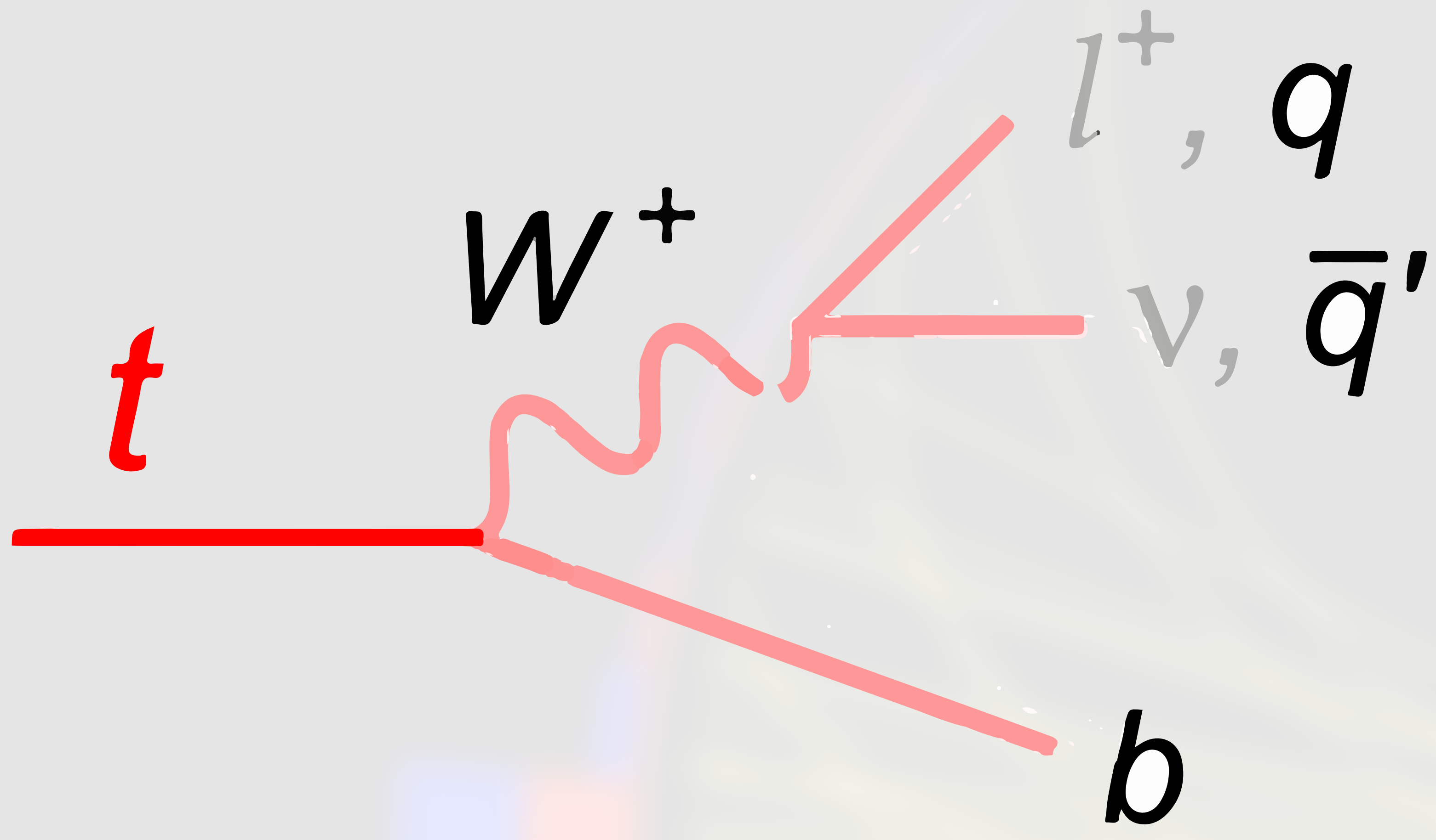
Which correlator will well characterize the top decay?



$$\langle\mathcal{E}(\vec{n}_1)\mathcal{E}(\vec{n}_2)\mathcal{E}(\vec{n}_3)\rangle$$

$$= \sum_{ij} \int \frac{d\sigma_{ijk}}{d^2\vec{n}_i d^2\vec{n}_j d^2\vec{n}_k} E_i E_j E_k \, \delta^2(\vec{n}_1 - \vec{n}_i)\delta^2(\vec{n}_2 - \vec{n}_j)\delta^2(\vec{n}_3 - \vec{n}_k)$$

What do we expect to see at leading order?



The correlator is sensitive to angles between the decay products.

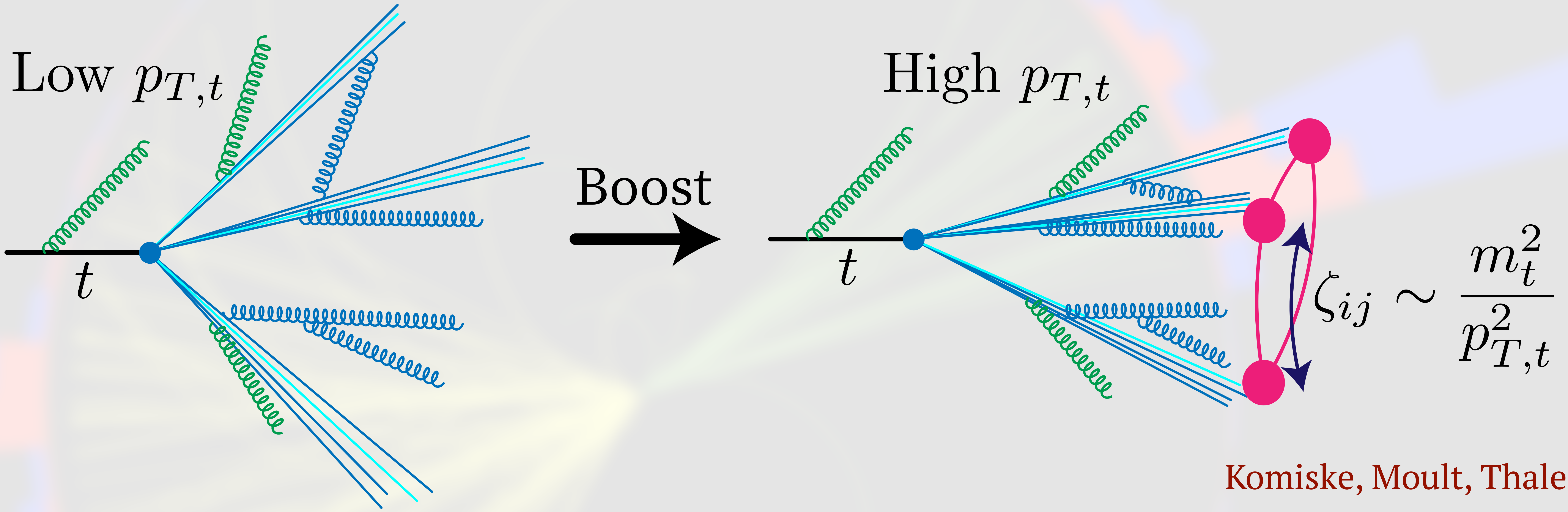
$$\zeta_{ij} = \frac{1 - \cos\theta_{ij}}{2}$$

In the top rest frame: $\tilde{\zeta}_{12} + \tilde{\zeta}_{23} + \tilde{\zeta}_{31} \in [2, 2.25]$

Lab frame angles: $\zeta \equiv \sum_{i<j} \zeta_{ij} \approx \left(\frac{m_t}{Q}\right)^2 \sum_{i<j} \tilde{\zeta}_{ij}$

$$\boxed{\langle \zeta \rangle \approx \frac{3m_t^2}{Q^2}}$$

Top mass imprinted at a characteristic angle

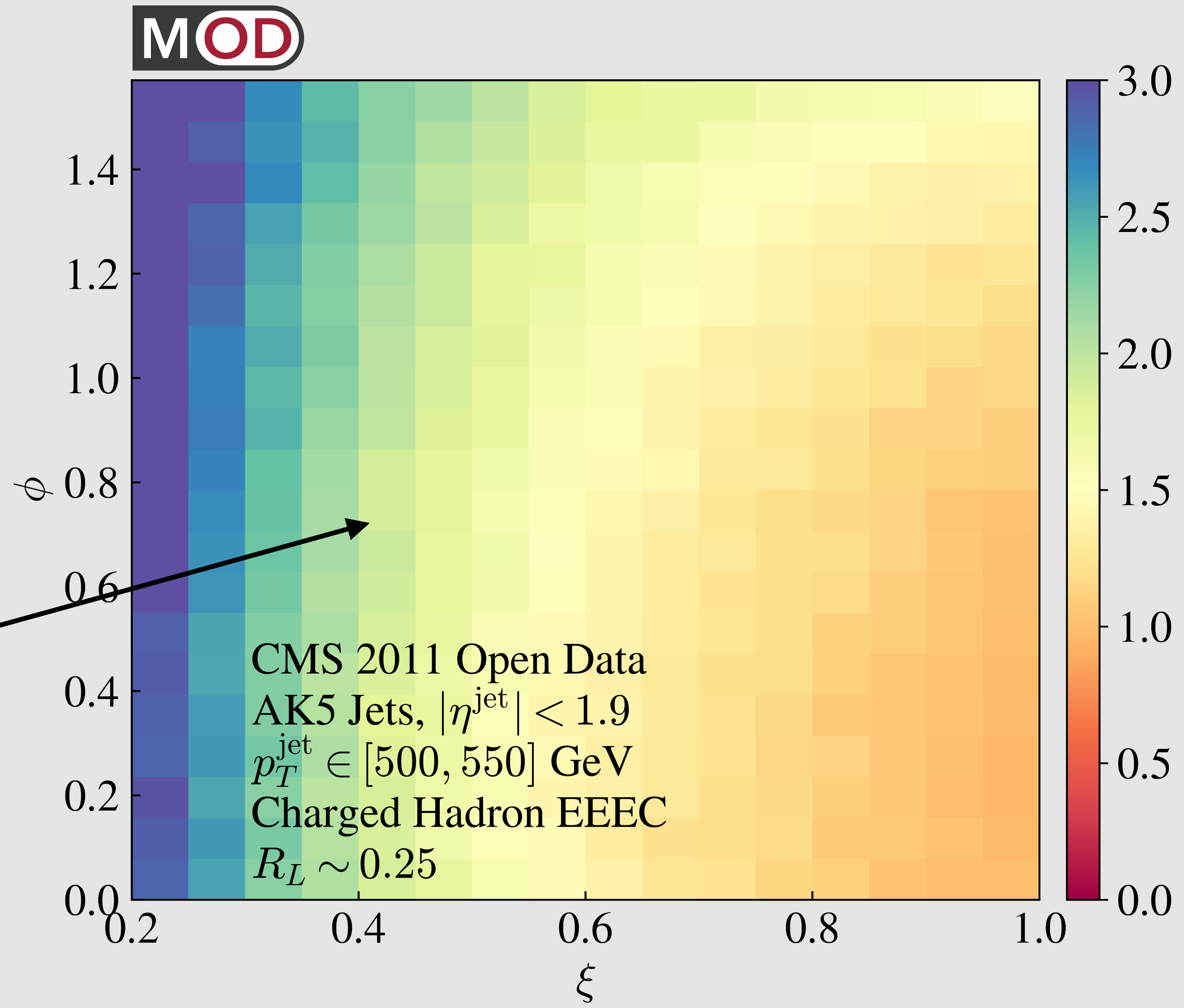


Komiske, Moult, Thaler, Zhu 2201.07800

In contrast, in the CFT limit EEEC exhibits a featureless power law:

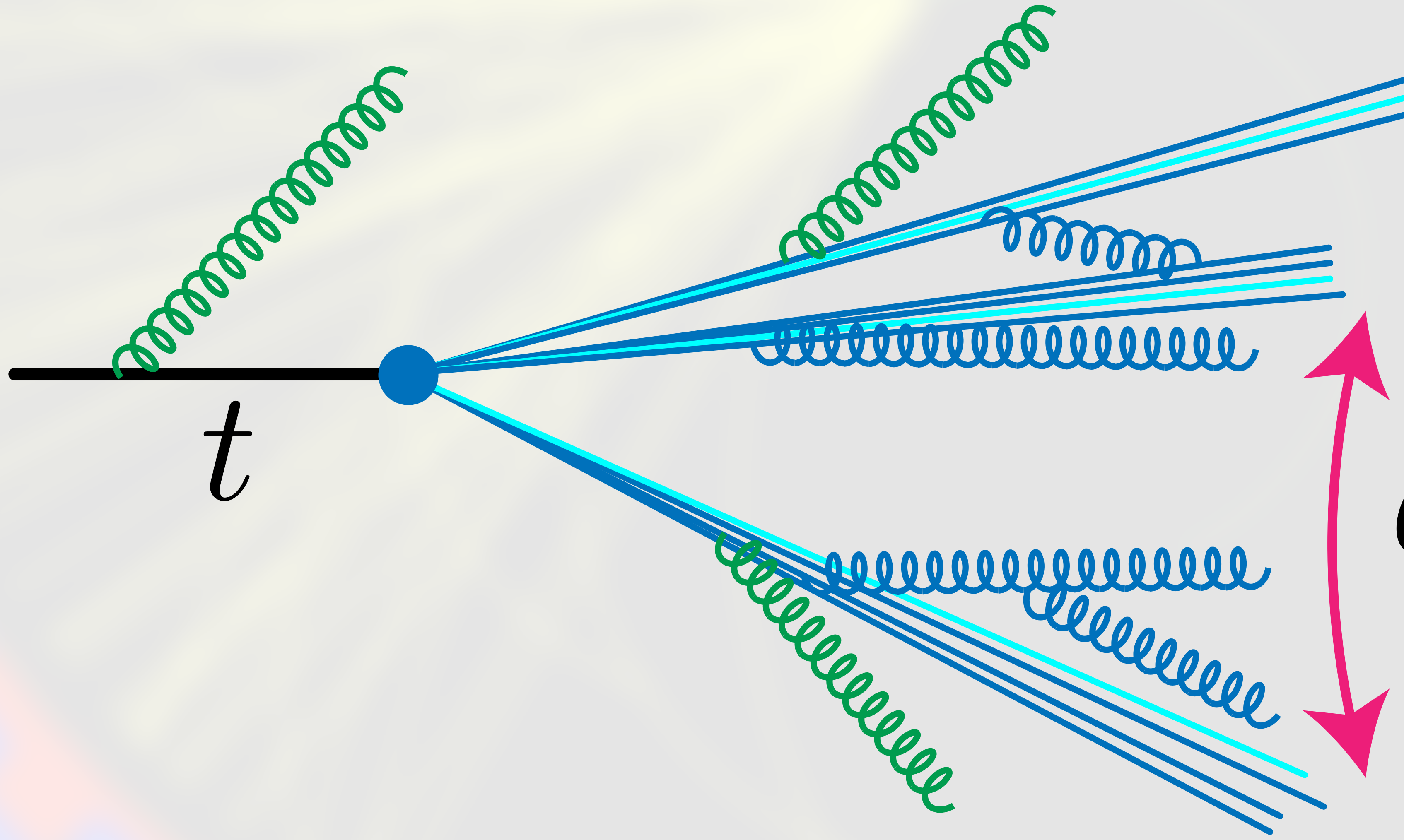
$$G^{(1)}(\zeta_{12}, \zeta_{23}, \zeta_{31}) \xrightarrow{\text{CFT}} \zeta_{31}^{-1+\gamma(4)} G(z, \bar{z})$$

light quark/gluon jets



Suppress contribution from collinear splittings

We want to preserve the $\langle\zeta\rangle \sim 3m_t^2/Q^2$ dependence but $\zeta = \sum_{i<j} \zeta_{ij}$ will also pick up collinear splittings



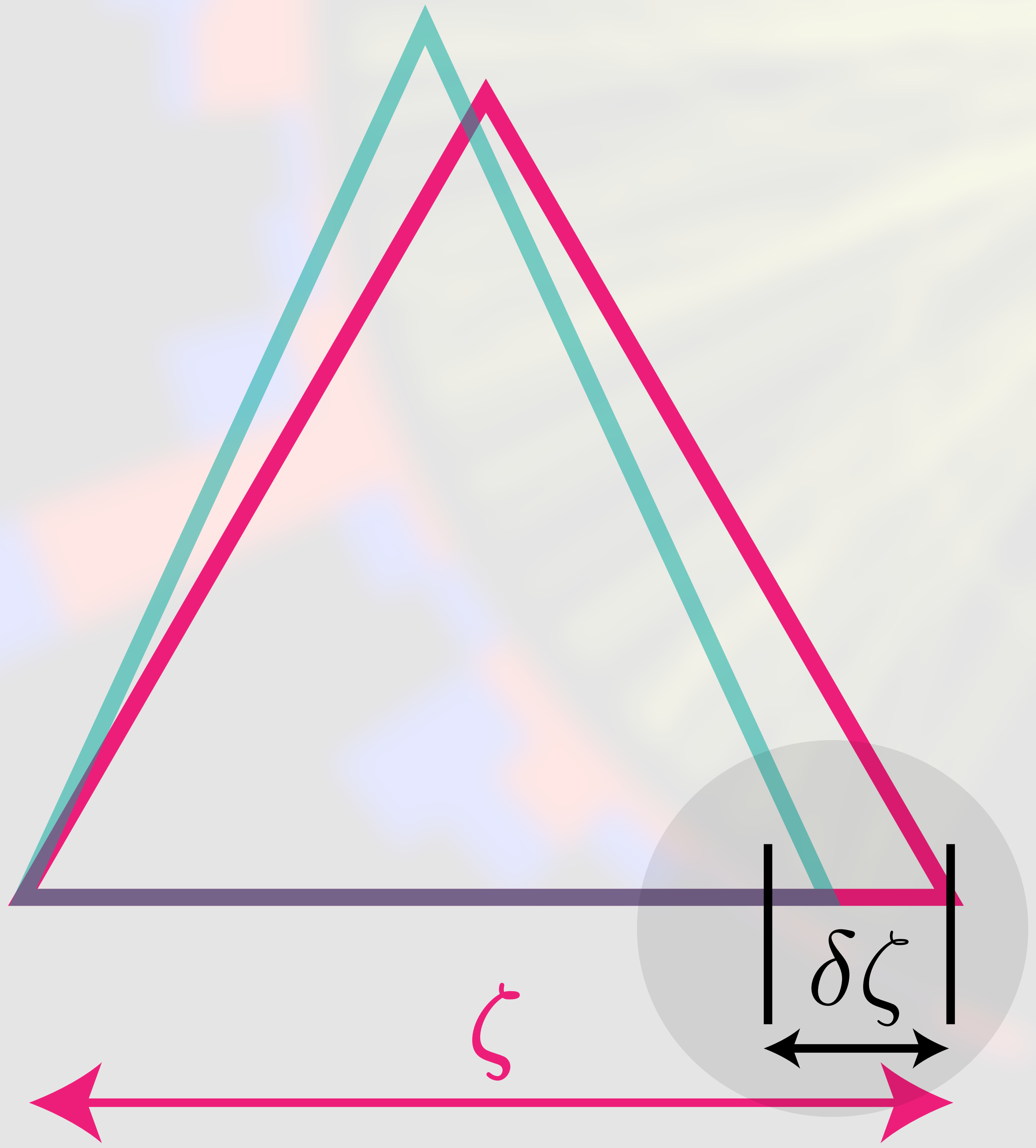
$\zeta_{ij} \ll m_t^2/p_{T,t}^2$

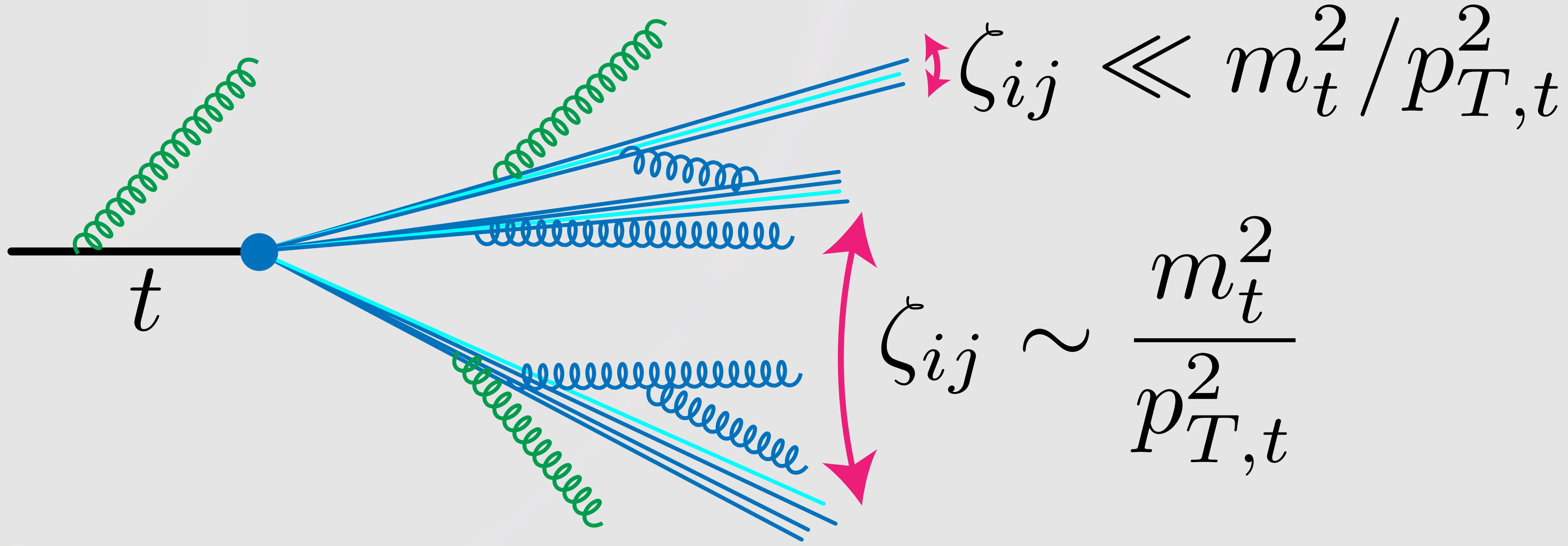
$\zeta_{ij} \sim \dfrac{m_t^2}{p_{T,t}^2}$

Constrain angles in equilateral configuration

$$\frac{\mathrm{d}\Sigma(\delta\zeta)}{\mathrm{d}Q\,\mathrm{d}\zeta} = \int \mathrm{d}\zeta_{12}\mathrm{d}\zeta_{23}\mathrm{d}\zeta_{31} \int \mathrm{d}\sigma \widehat{\mathcal{M}}^{(n)}_{\triangle}(\zeta_{12},\zeta_{23},\zeta_{31},\zeta,\delta\zeta)$$

$$\widehat{\mathcal{M}}^{(n)}_{\triangle}(\zeta_{12},\zeta_{23},\zeta_{31},\zeta,\delta\zeta) = \sum_{i,j,k} \frac{E_i^n E_j^n E_k^n}{Q^{3n}} \delta\left(\zeta_{12}-\frac{\theta_{ij}^2}{4}\right)\delta\left(\zeta_{31}-\frac{\theta_{ik}^2}{4}\right)\delta\left(\zeta_{23}-\frac{\theta_{jk}^2}{4}\right)$$
$$\times\, \delta(3\zeta-\zeta_{12}-\zeta_{23}-\zeta_{31}) \prod_{l,m,n\in\{1,2,3\}} \Theta(\delta\zeta - |\zeta_{lm}-\zeta_{mn}|).$$

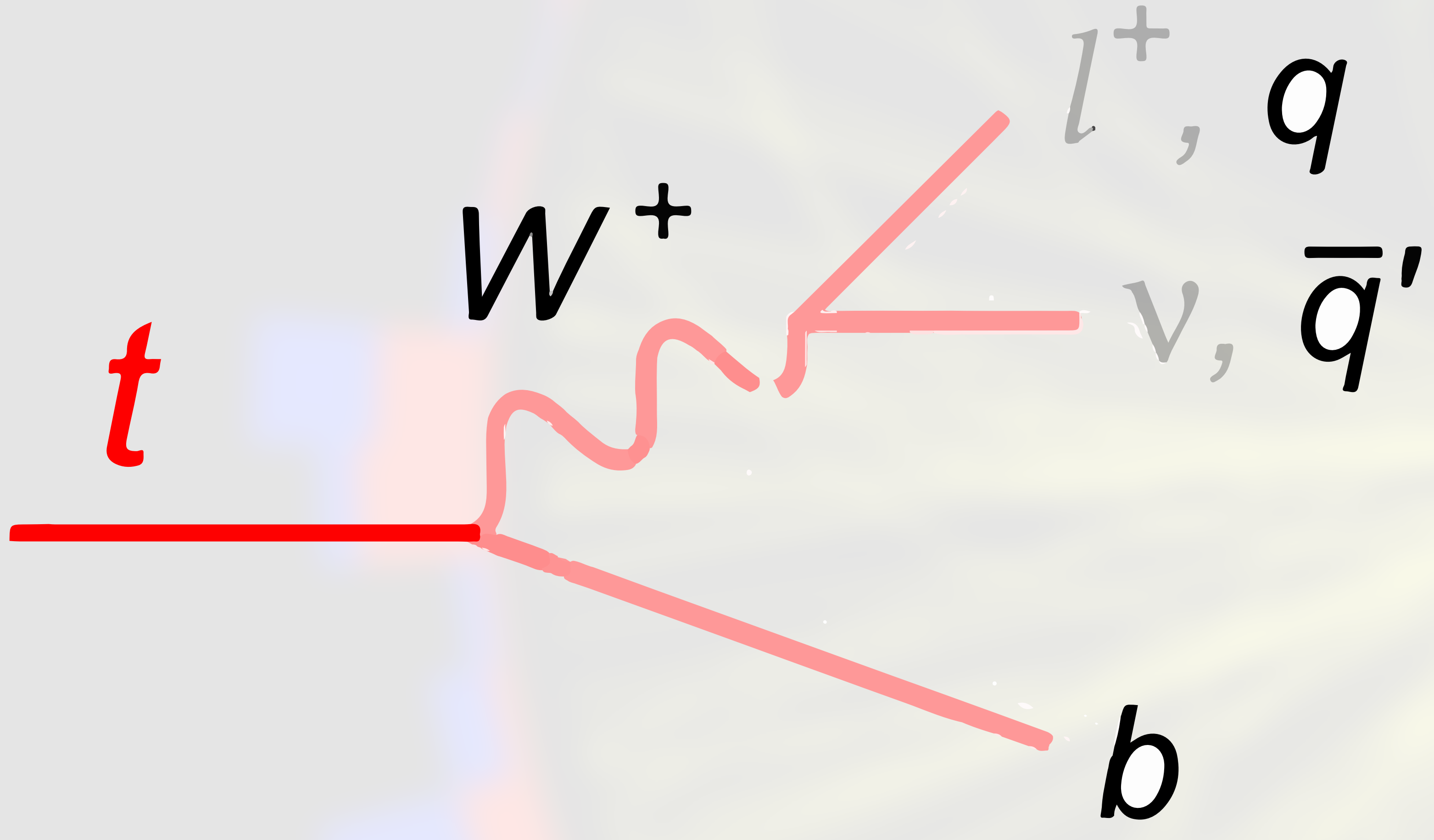


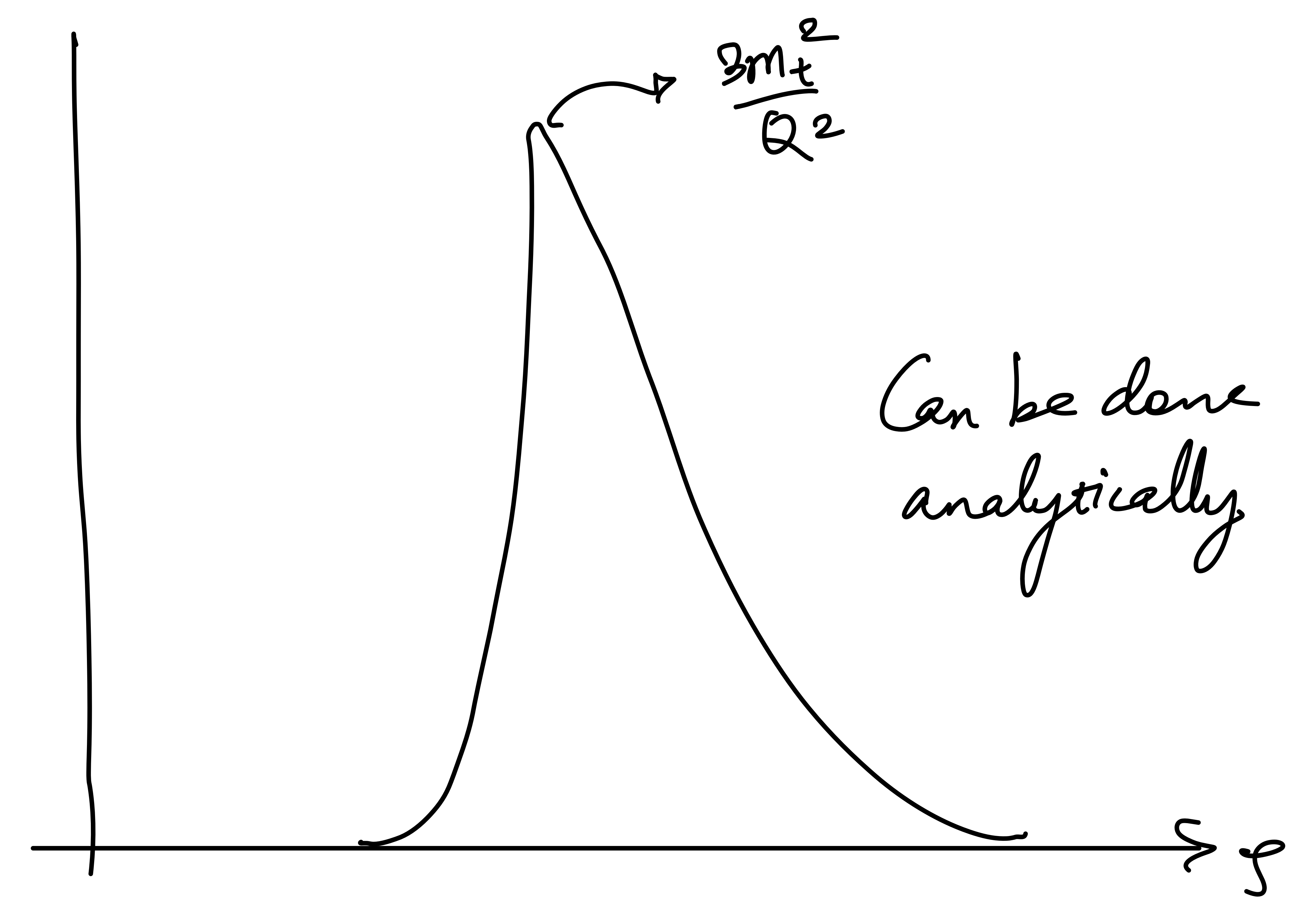


Allow for some small asymmetry

Understanding the distribution

What does the distribution look like at leading order?

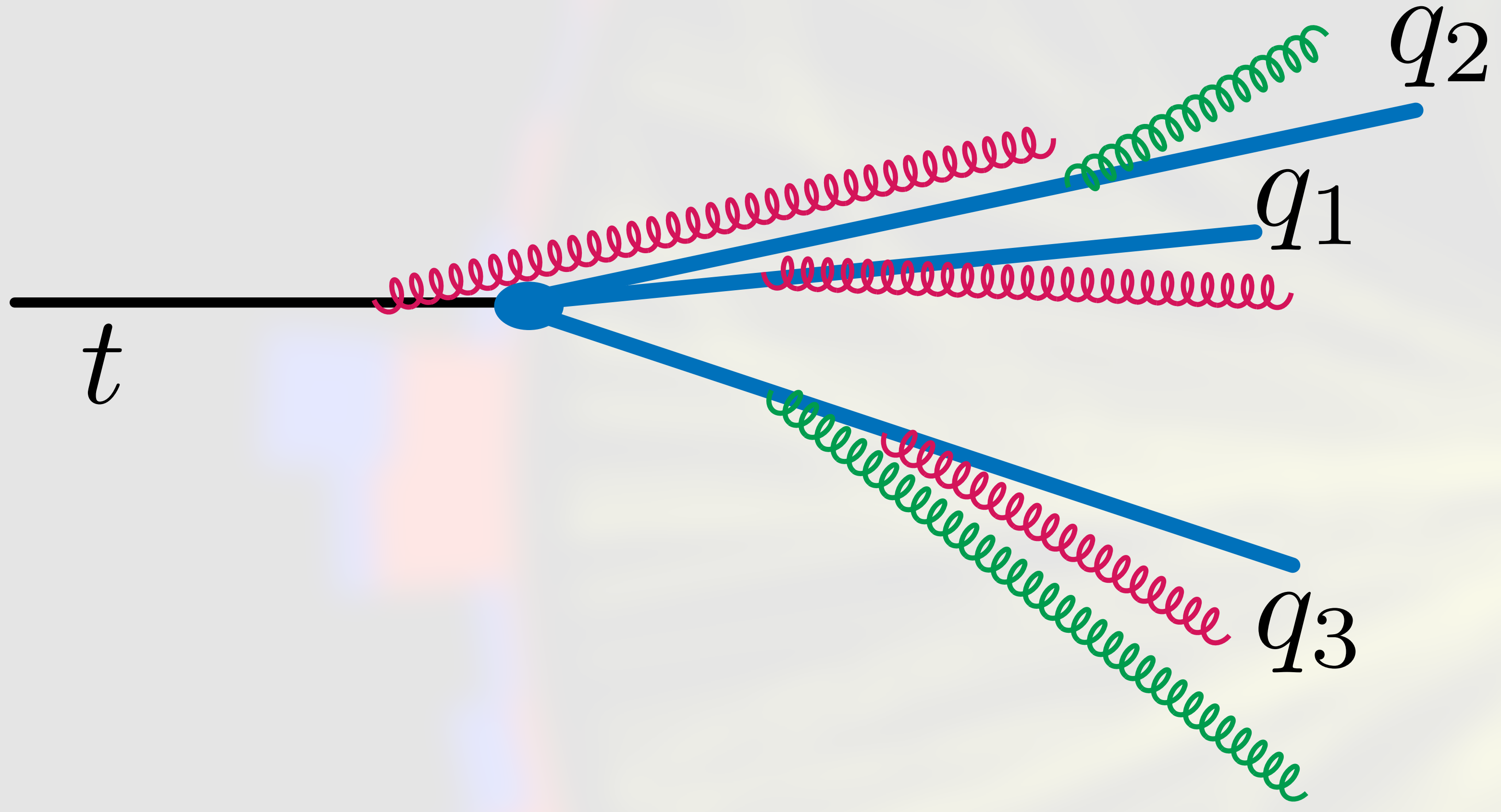


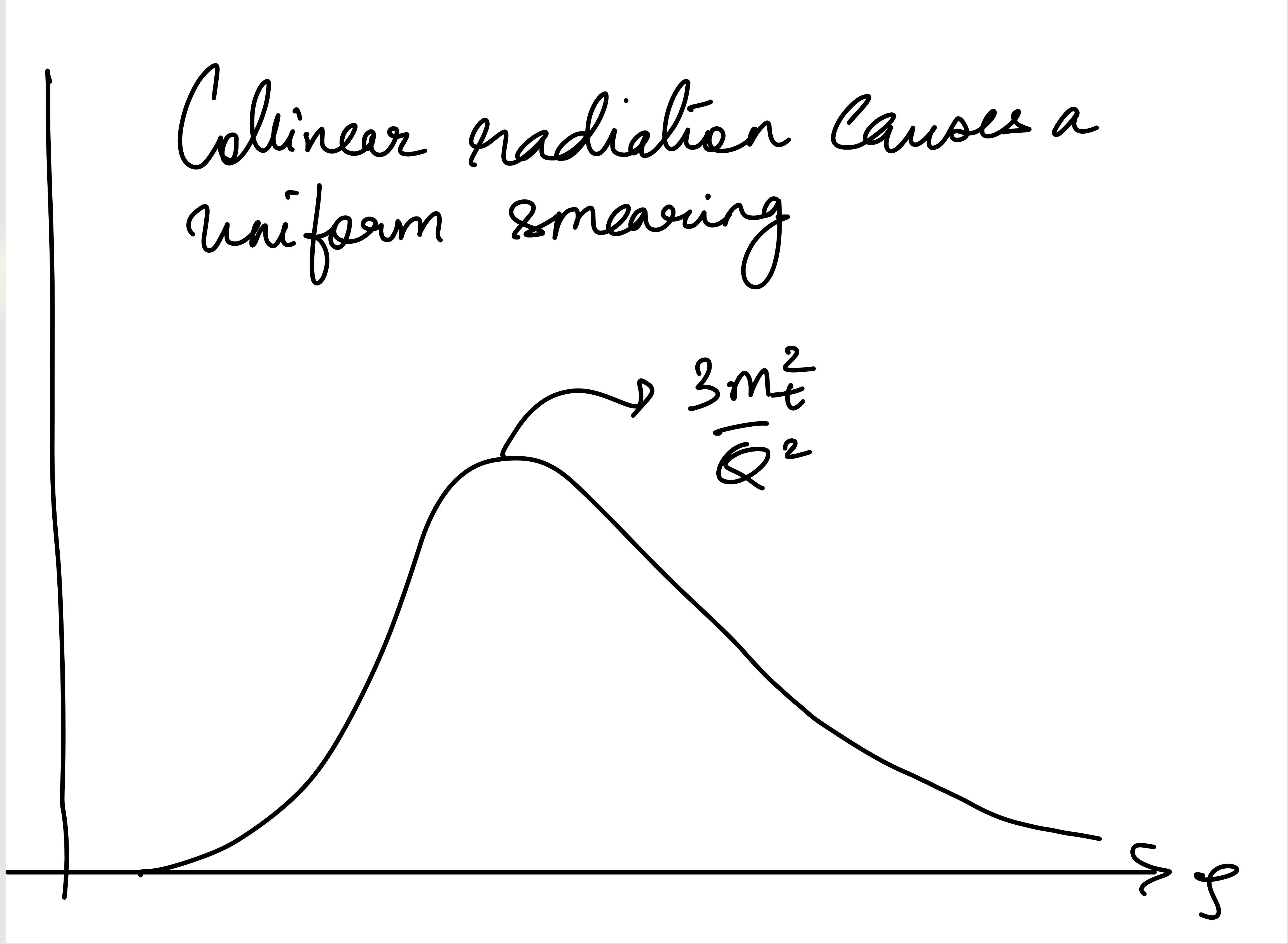


Can be done analytically

Understanding the distribution

What does the distribution look like with higher order corrections?

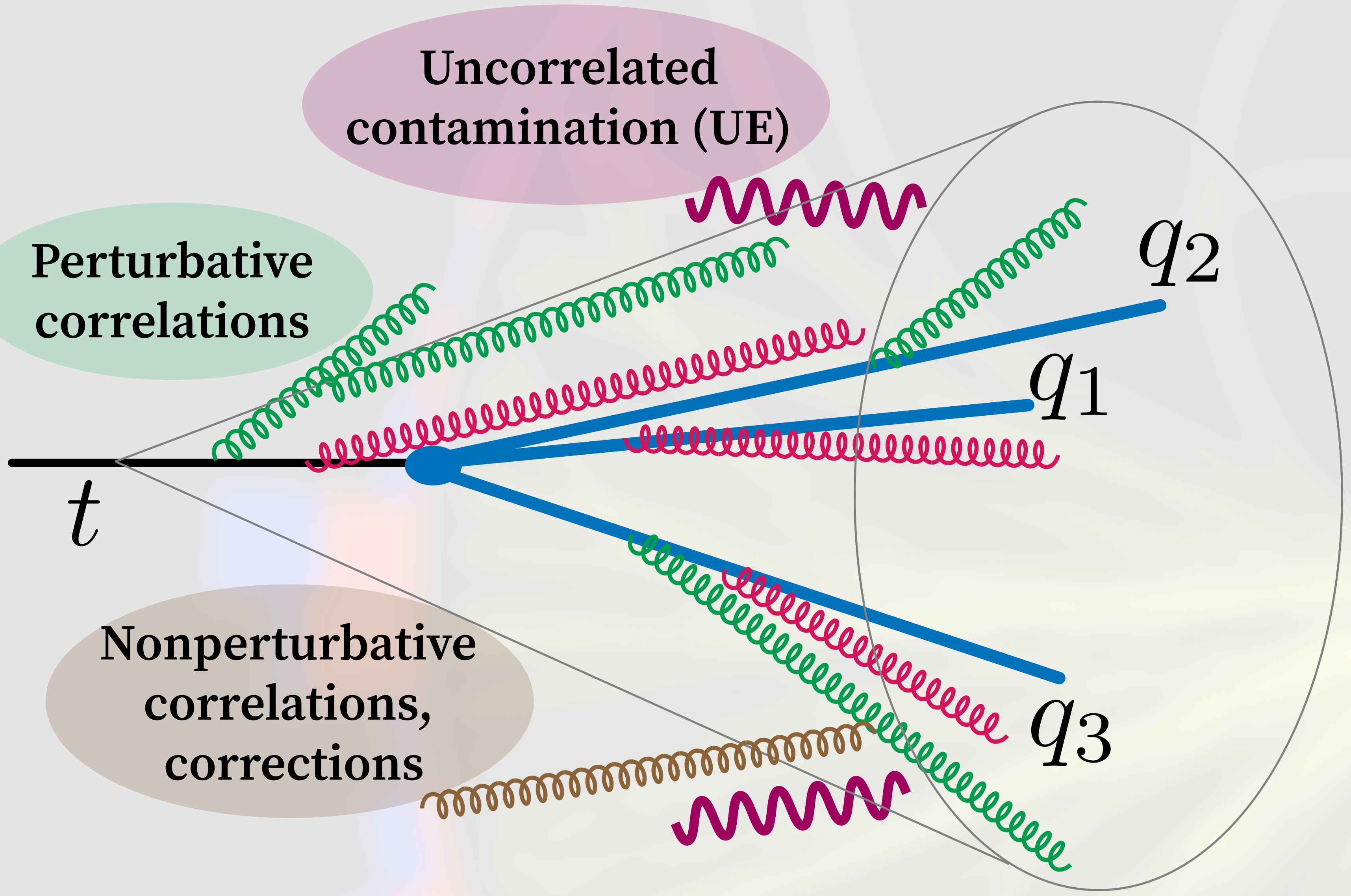




Collinear radiation causes a uniform smearing

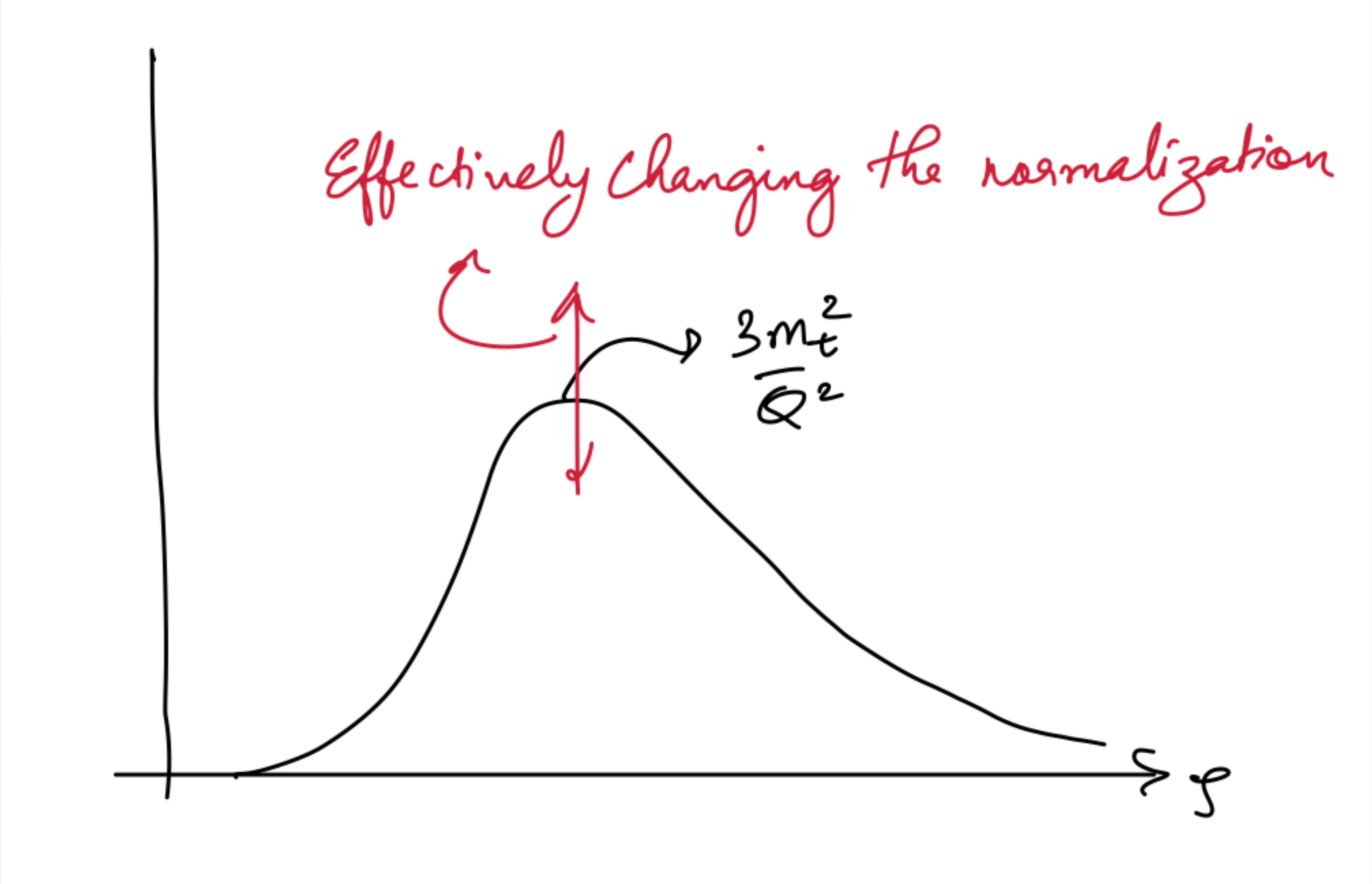
Understanding the distribution

What does the distribution look like with nonperturbative corrections?


Uncorrelated contamination (UE)

Perturbative correlations

Nonperturbative correlations, corrections

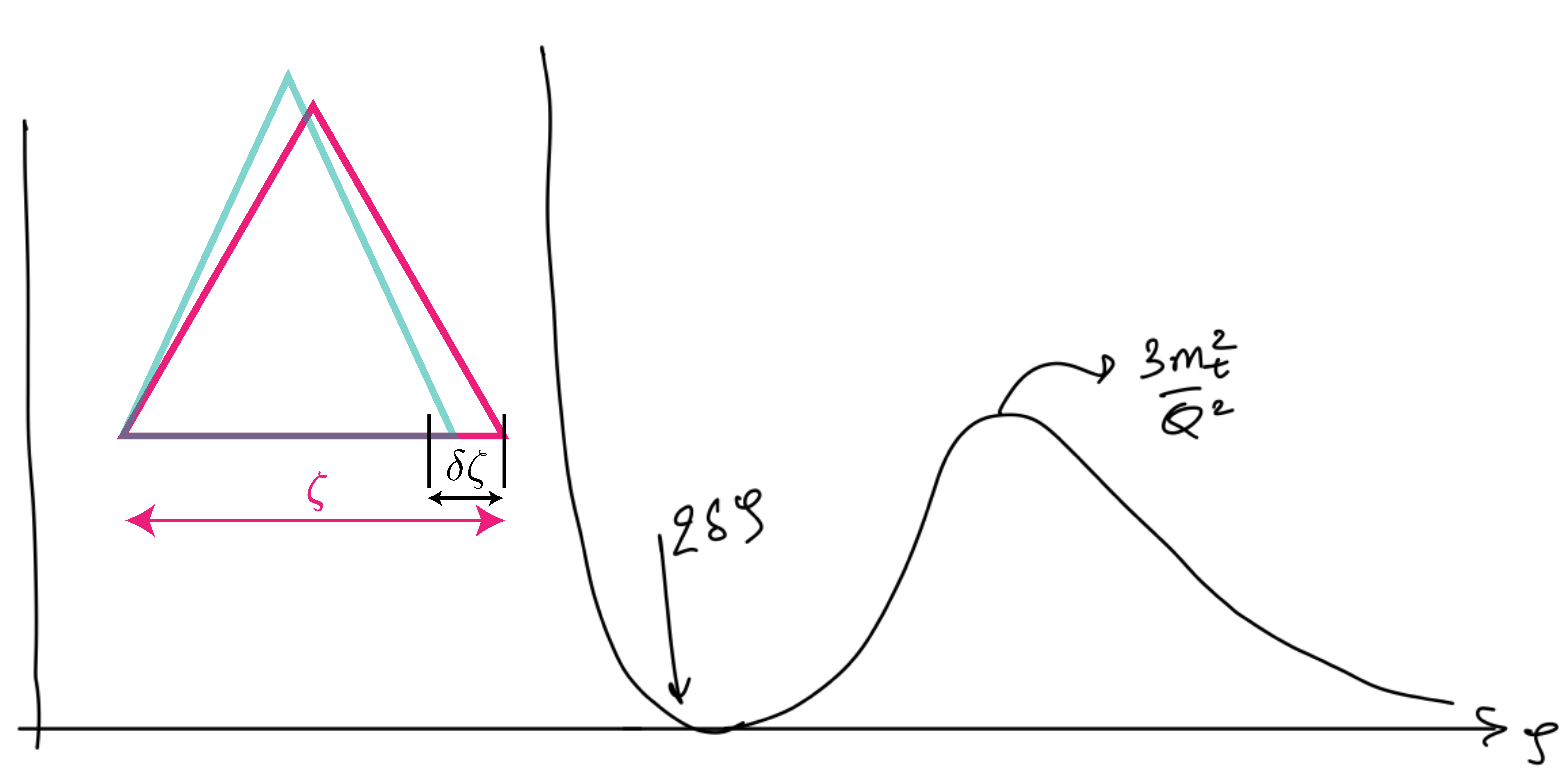


We know from other studies of energy correlators that NP corrections are an additive power law

hep-ph/9902341
hep-ph/9411211
hep-ph/9708346

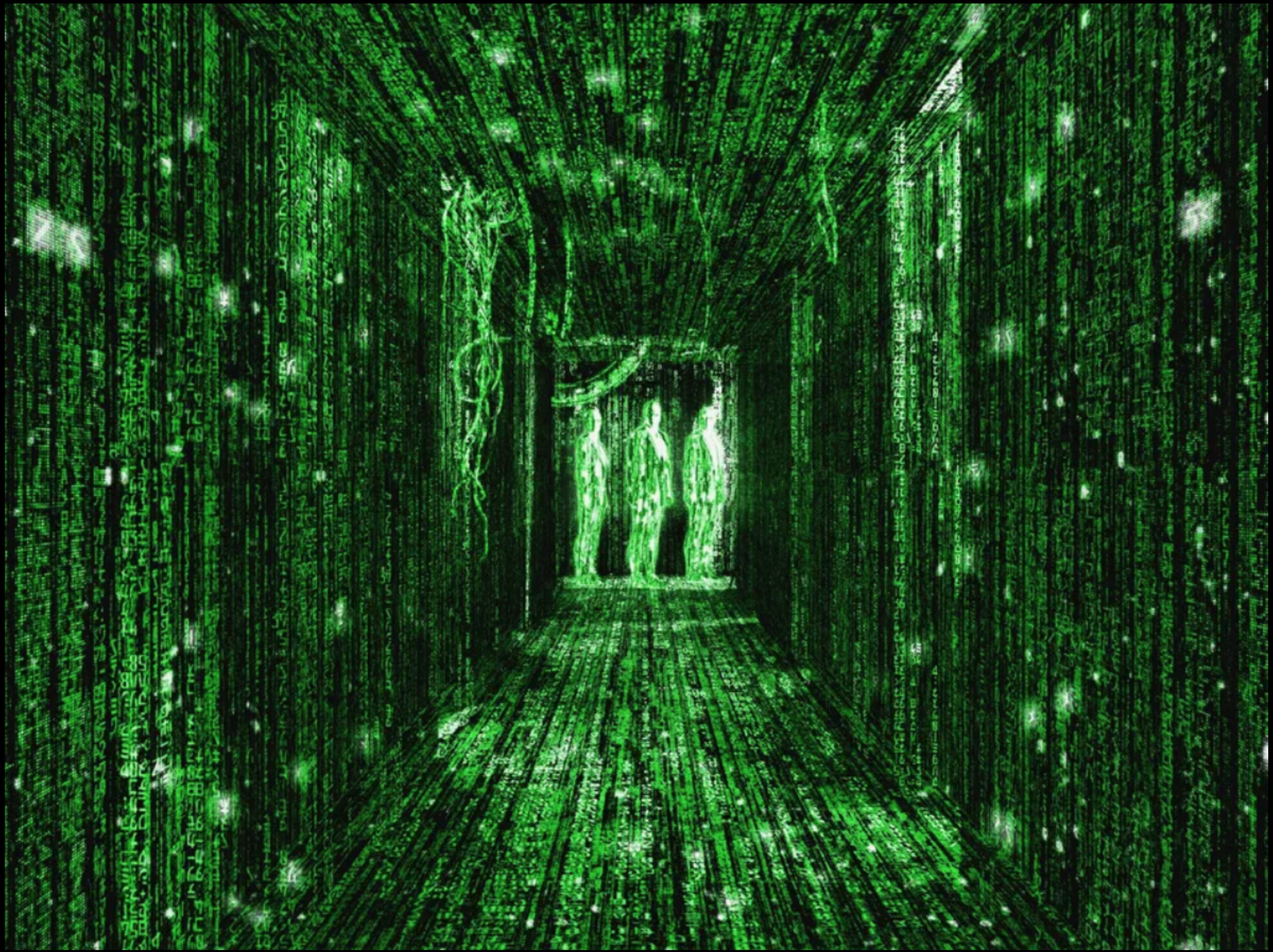
Understanding the distribution

What is the effect of asymmetry cut?

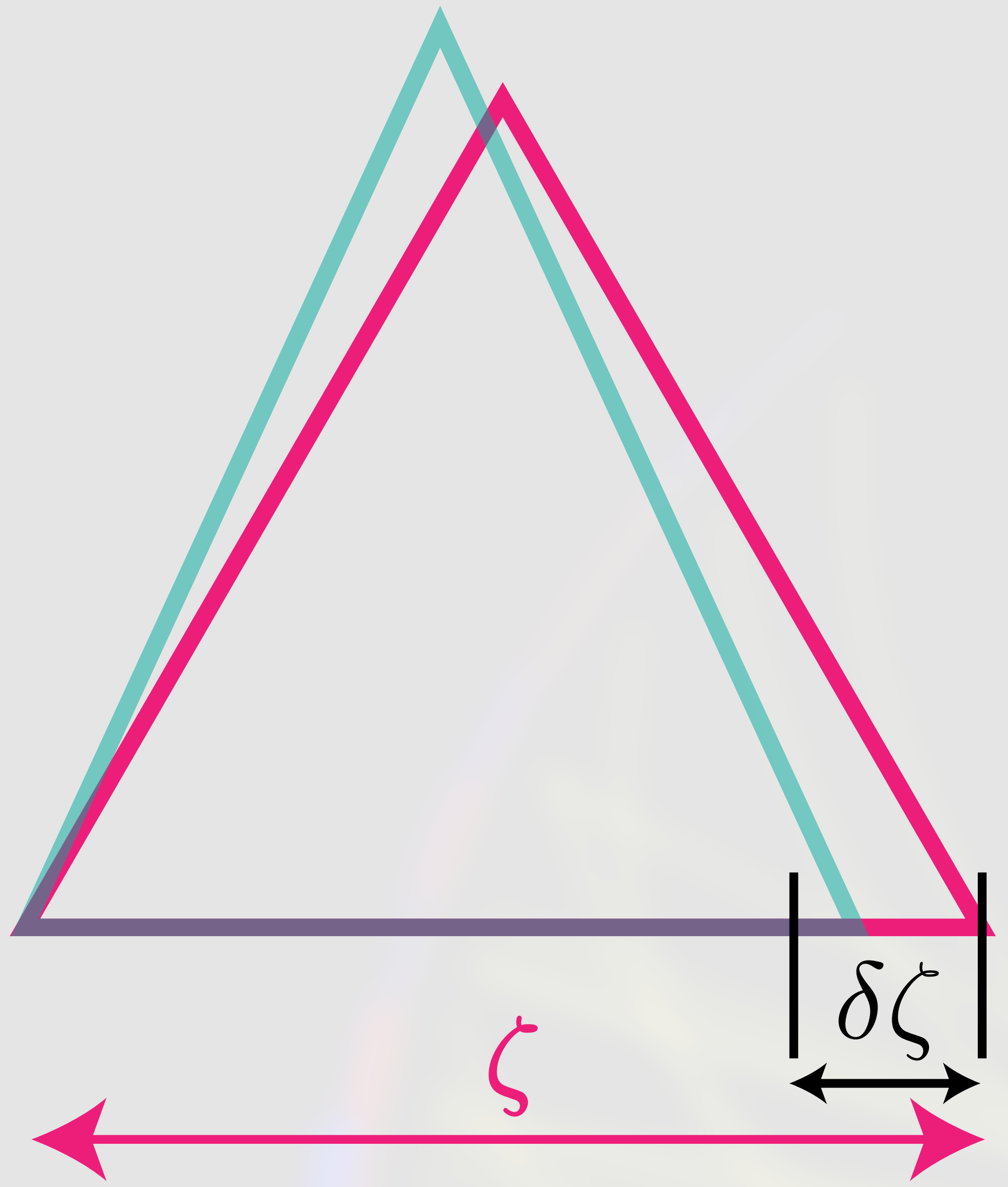


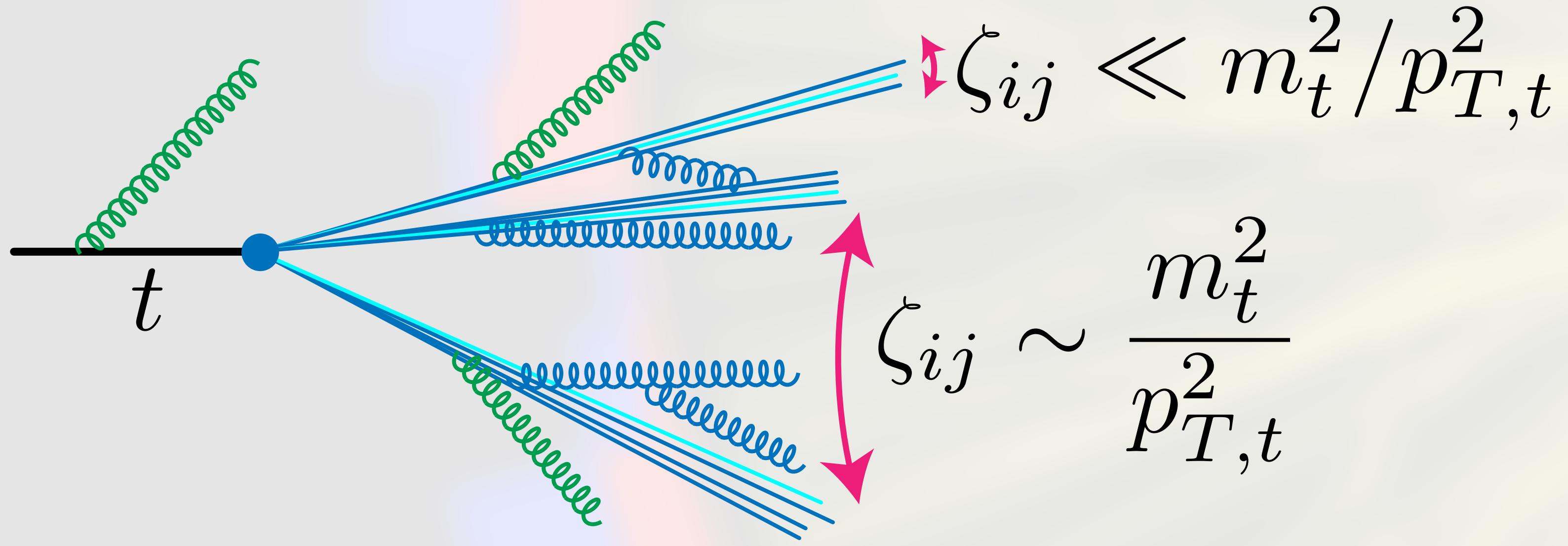
Enough sketching!

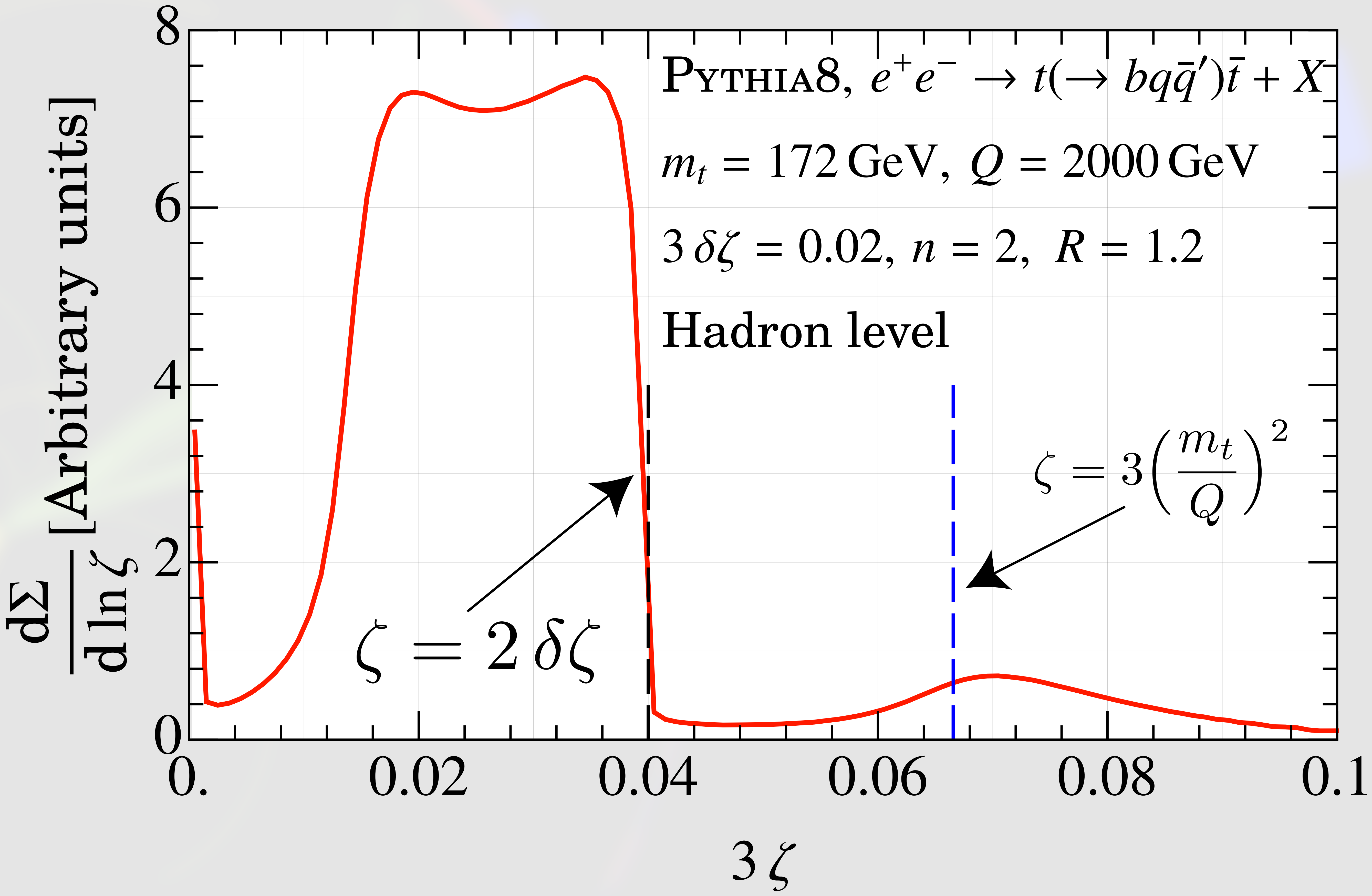
Let us simulate



Simulation in PYTHIA8

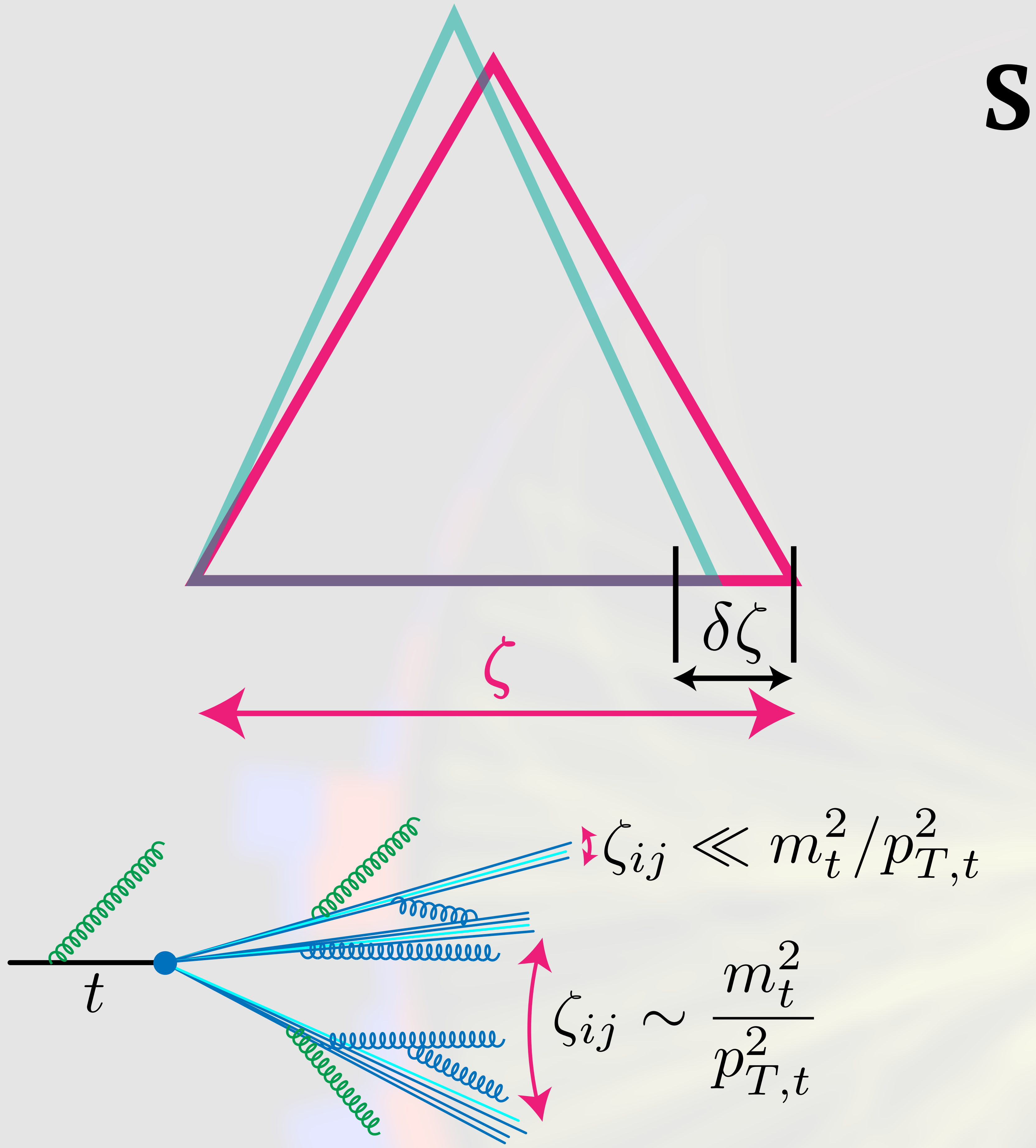


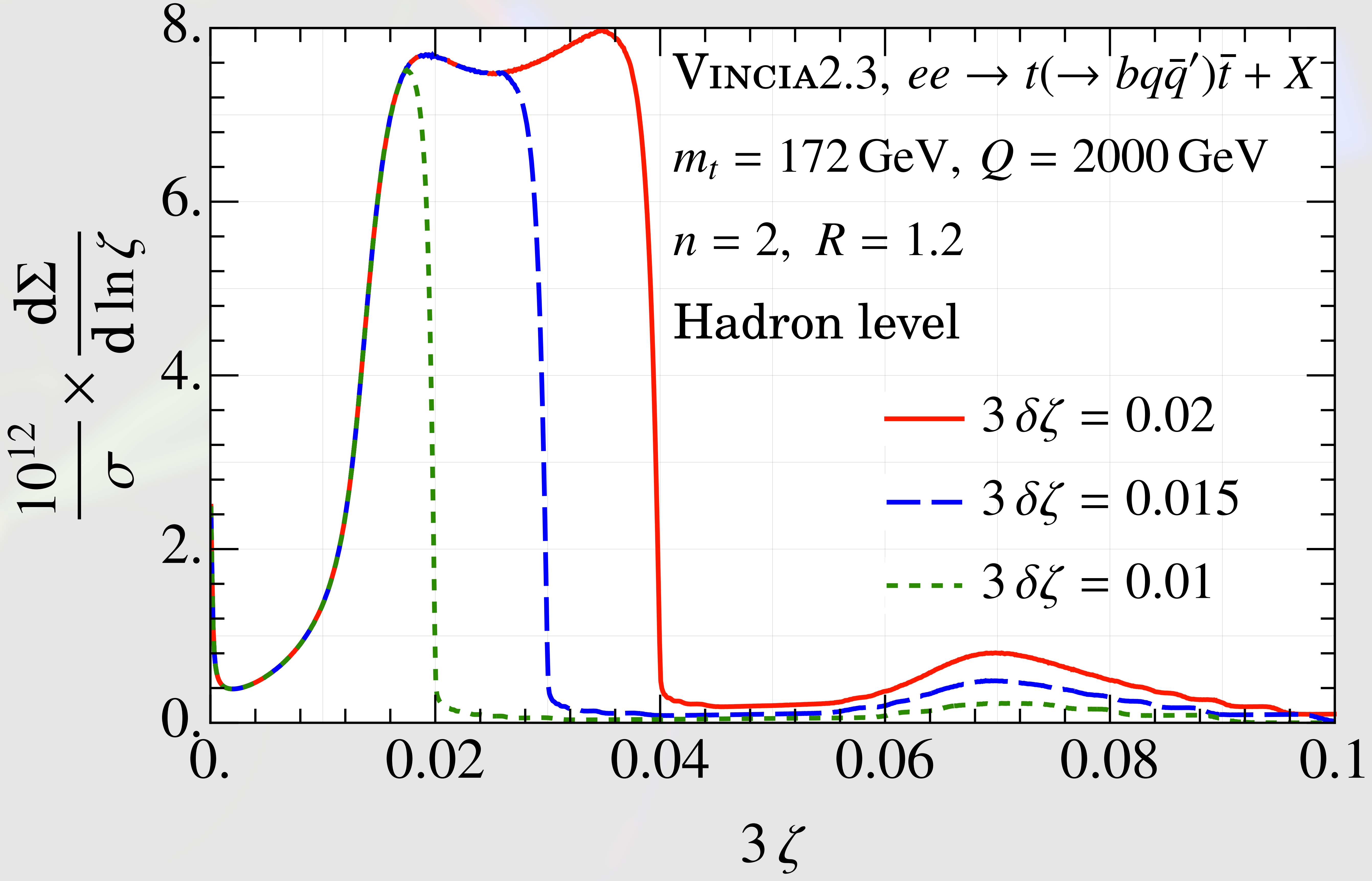




1. Distinct peak at $\zeta \sim 3(m_t/Q)^2$: peak dominated by hard decay of the top
2. Resilient to collinear radiation, $\alpha_s \ln \zeta_{\text{peak}} < 1$: fixed order perturbation theory sufficient

Simulation in PYTHIA8

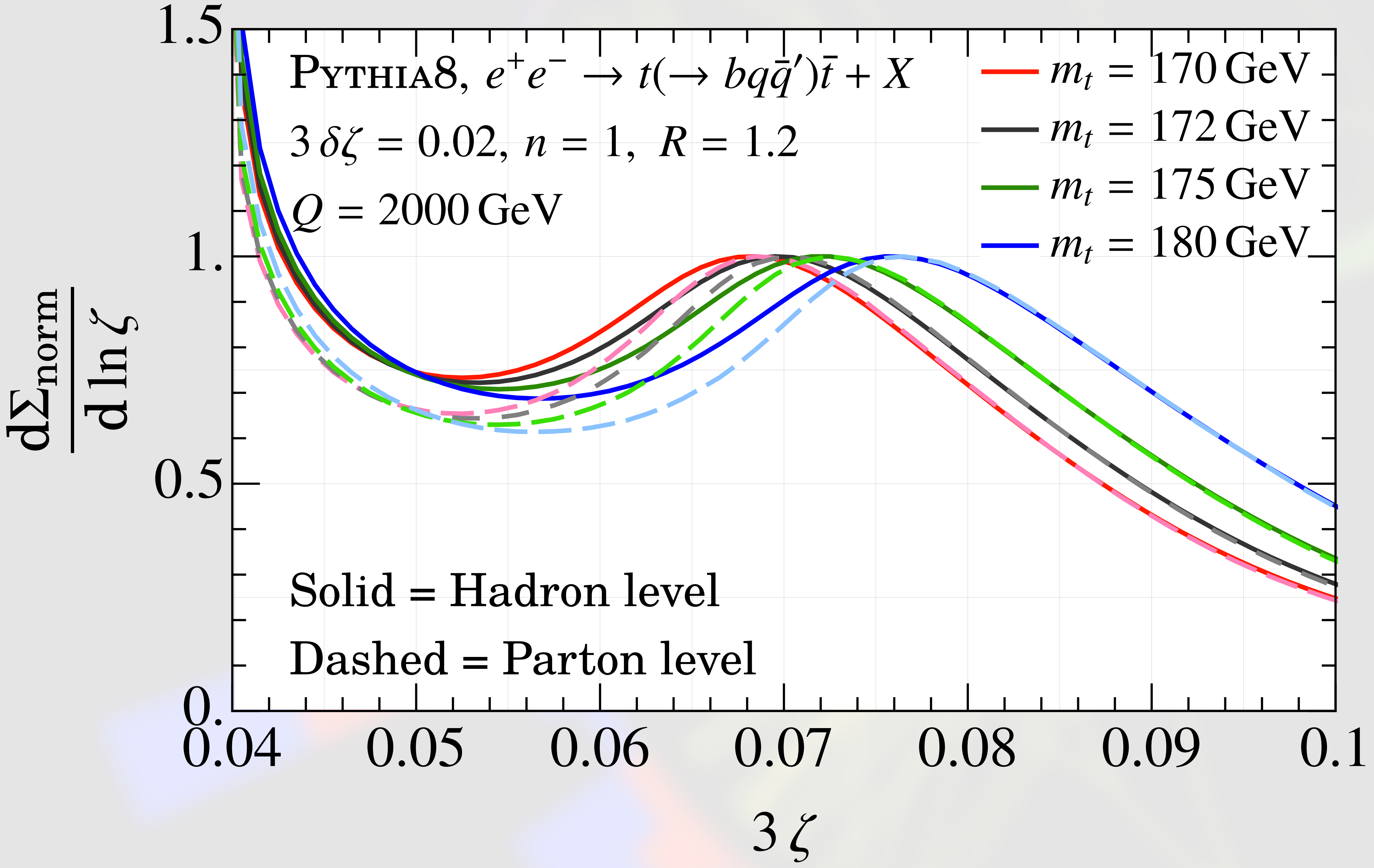


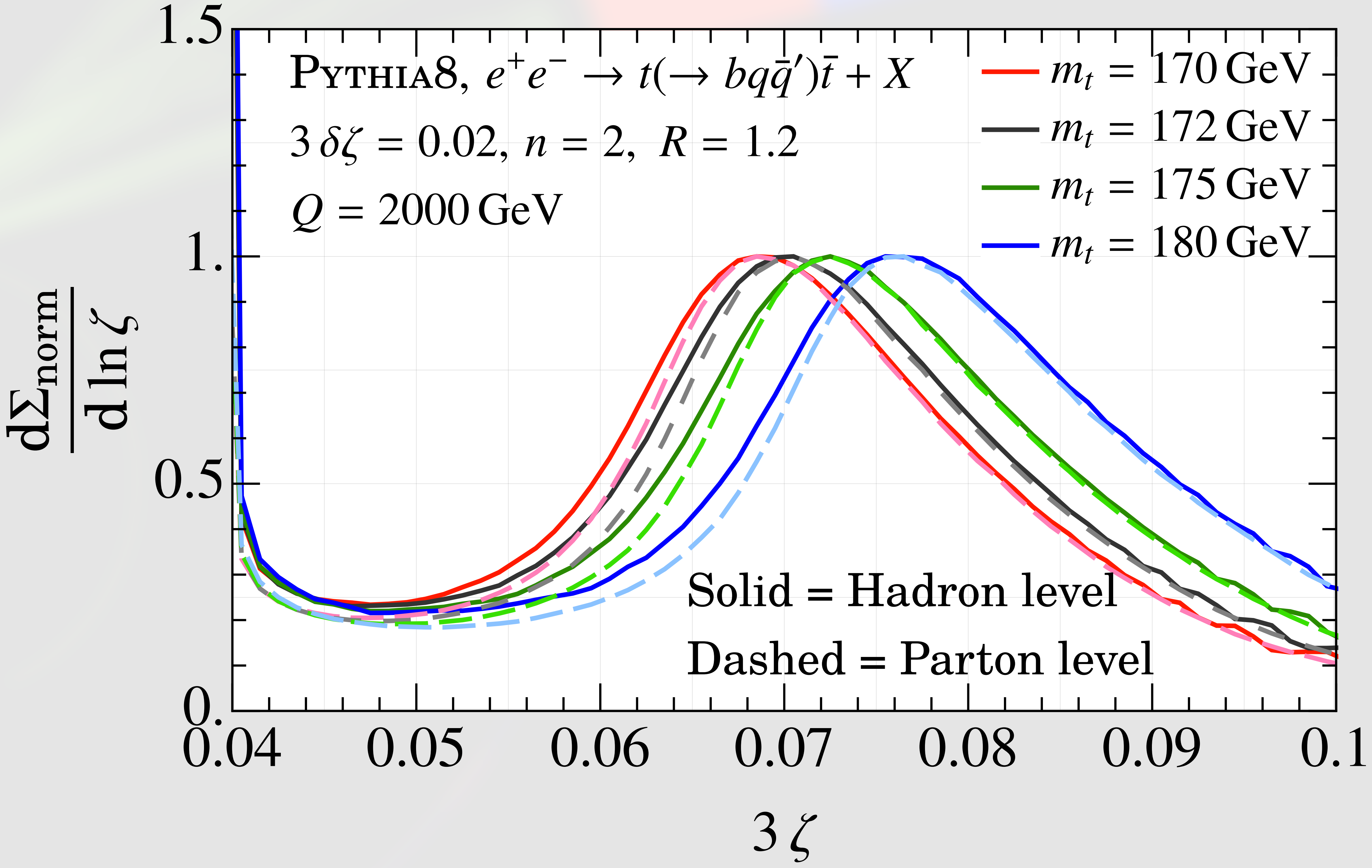


1. Asymmetry cut creates a sharp cutoff and makes the top peak visible. No hierarchy required.
2. Impact on statistics: $d\Sigma/d\zeta \approx 4(\delta\zeta)^2 G^{(n)}(\zeta, \zeta, \zeta; m_t)$

Excellent top mass sensitivity

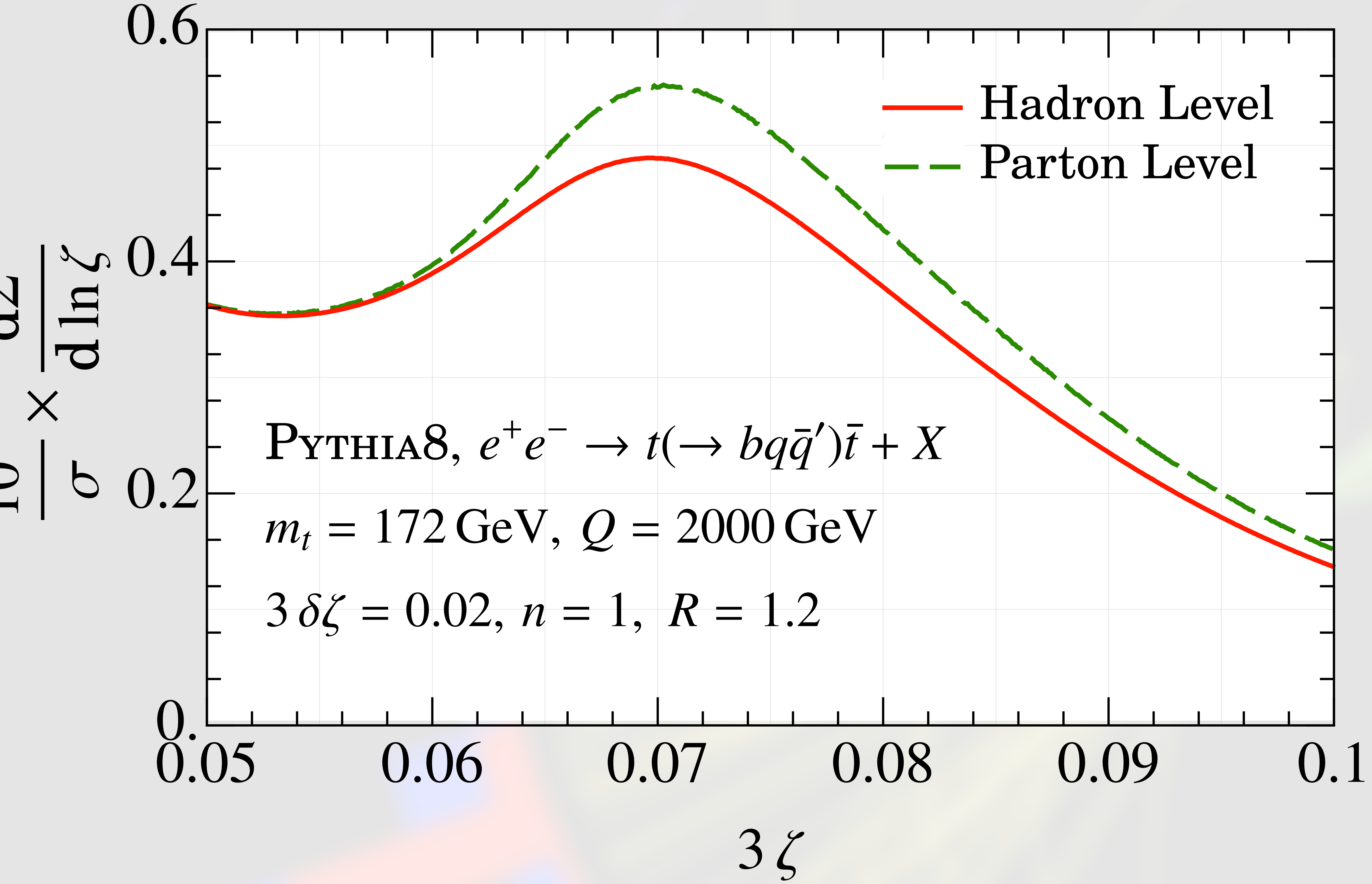
$$\widehat{\mathcal{M}}^{(n)}(\zeta_{12},\zeta_{23},\zeta_{31}) = \sum_{i,j,k} \frac{E_i^n E_j^n E_k^n}{Q^{3n}} \delta\left(\zeta_{12}-\hat{\zeta}_{ij}\right) \delta\left(\zeta_{23}-\hat{\zeta}_{ik}\right) \delta\left(\zeta_{31}-\hat{\zeta}_{jk}\right)$$

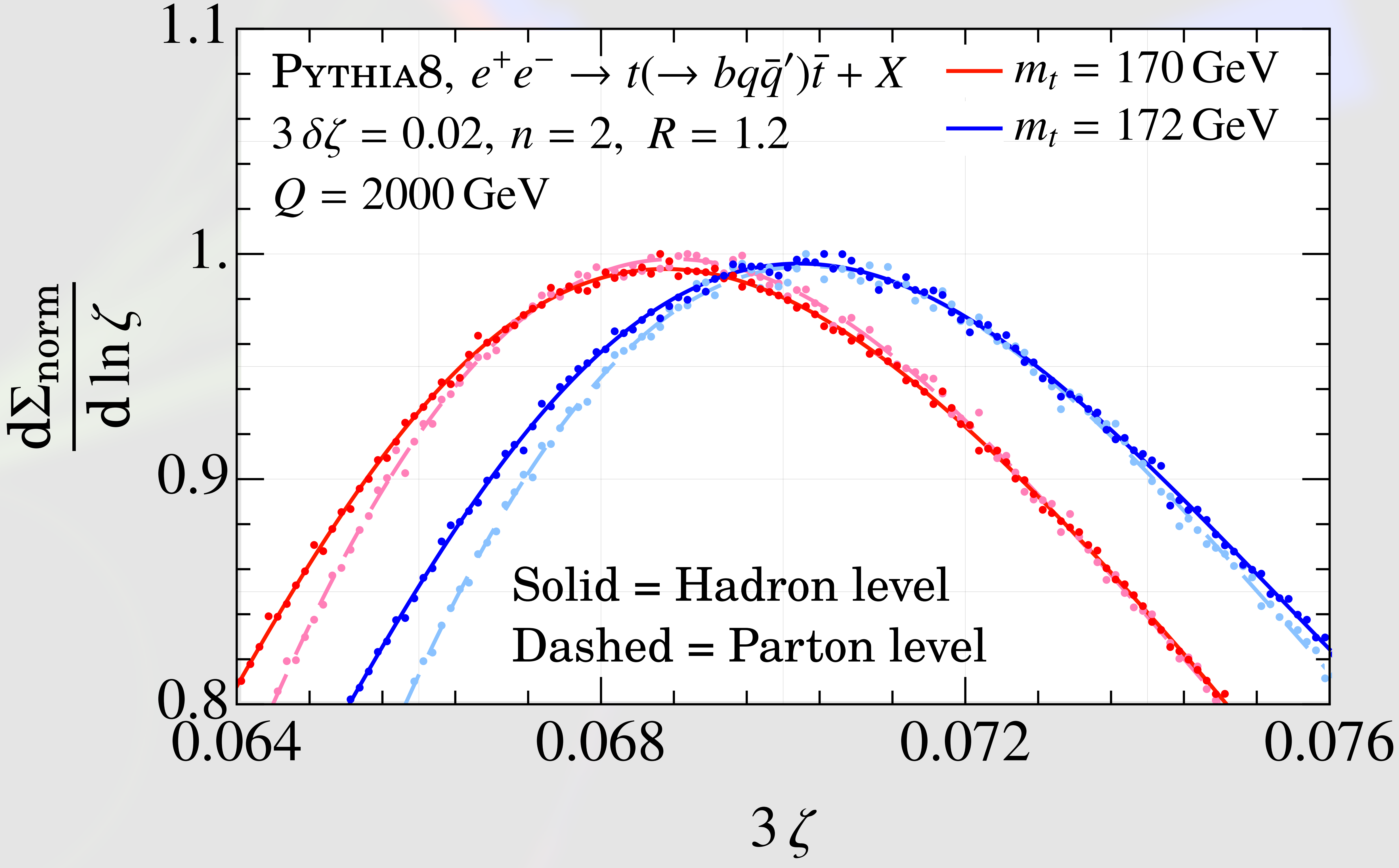




$n = 2$ is not IRC safe: absorb IRC sensitive pieces in moments of fragmentation function

Hadronization corrections



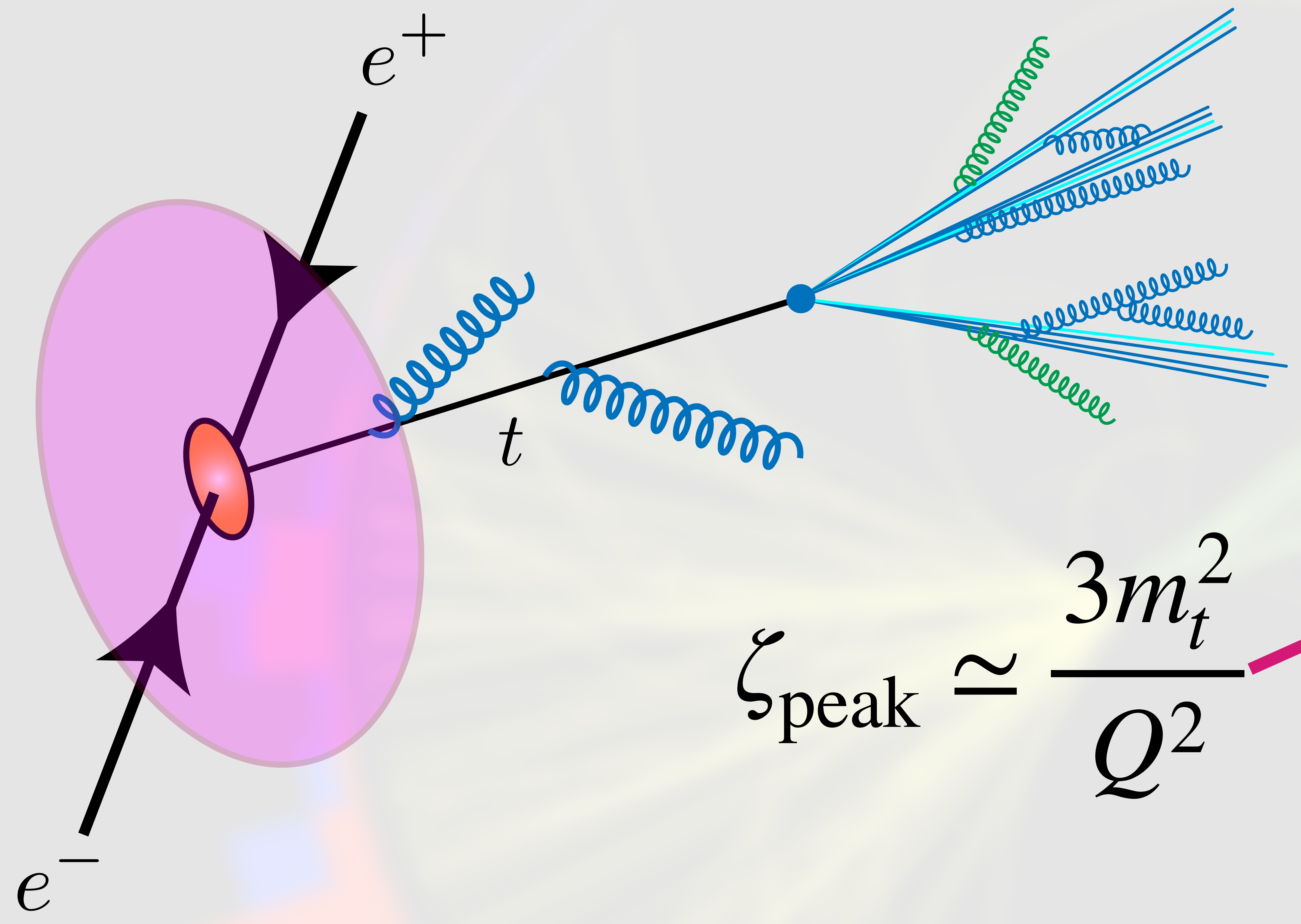


1. Nonperturbative effects enter as an additive power law: not a shift as in the case of jet mass

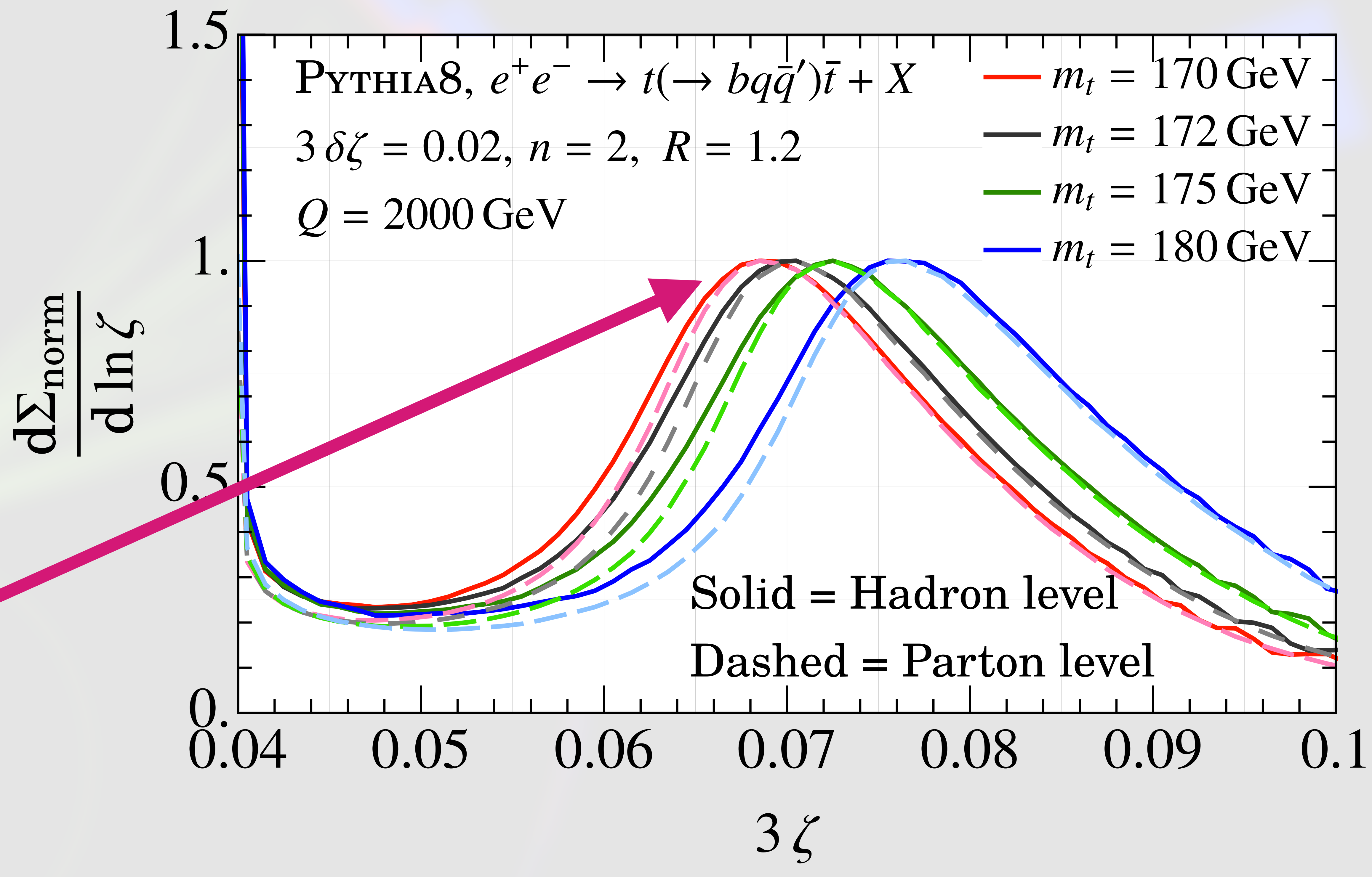
2. Normalized distribution: small effect on the peak, $\Delta m_t^{\text{Had}} \approx 150 \pm 50\,\text{MeV}$

EEEC on tops at the LHC

We are in fact sensitive to the production mechanism



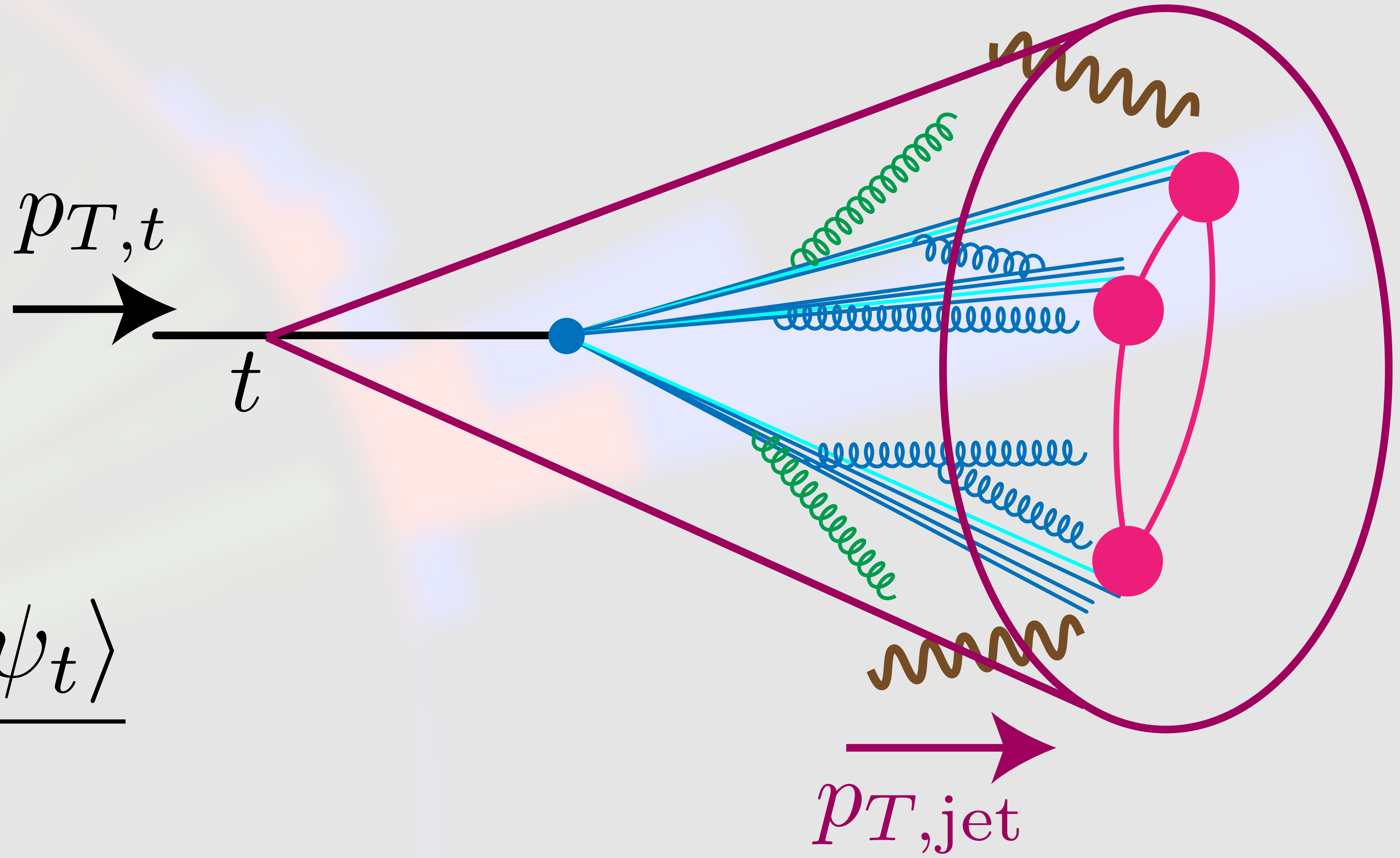
$$\zeta_{\text{peak}} \simeq \frac{3m_t^2}{Q^2}$$



$$\langle \mathcal{E}(\vec{n}_1)\mathcal{E}(\vec{n}_2)\mathcal{E}(\vec{n}_3)\rangle_t \equiv \frac{\langle \psi_t | \mathcal{E}(\vec{n}_1)\mathcal{E}(\vec{n}_2)\mathcal{E}(\vec{n}_3) | \psi_t \rangle}{\langle \psi_t | \psi_t \rangle}$$

For e^+e^- collisions we can define a state via a local operator $\mathcal{O}$: $|\psi_t\rangle = \mathcal{O}\,|0\rangle$, and produce tops with definite velocity Q/m_t

Energy correlators at hadron colliders



Let us take a closer look at the definition of the correlator:

$$\langle \mathcal{E}(\vec{n}_1)\mathcal{E}(\vec{n}_2)\mathcal{E}(\vec{n}_3)\rangle_t \equiv \frac{\langle \psi_t | \mathcal{E}(\vec{n}_1)\mathcal{E}(\vec{n}_2)\mathcal{E}(\vec{n}_3) | \psi_t \rangle}{\langle \psi_t | \psi_t \rangle}$$

At hadron colliders we have something like:

$$|\psi_t\rangle_{pp} = \left| \text{An anti-}k_T \text{ jet with } R = 1.2 \text{ and } p_{T,\text{jet}} \in [600{,}650] \text{ GeV} \right\rangle$$

Here we need jets to specify the state

Implications for hadron colliders

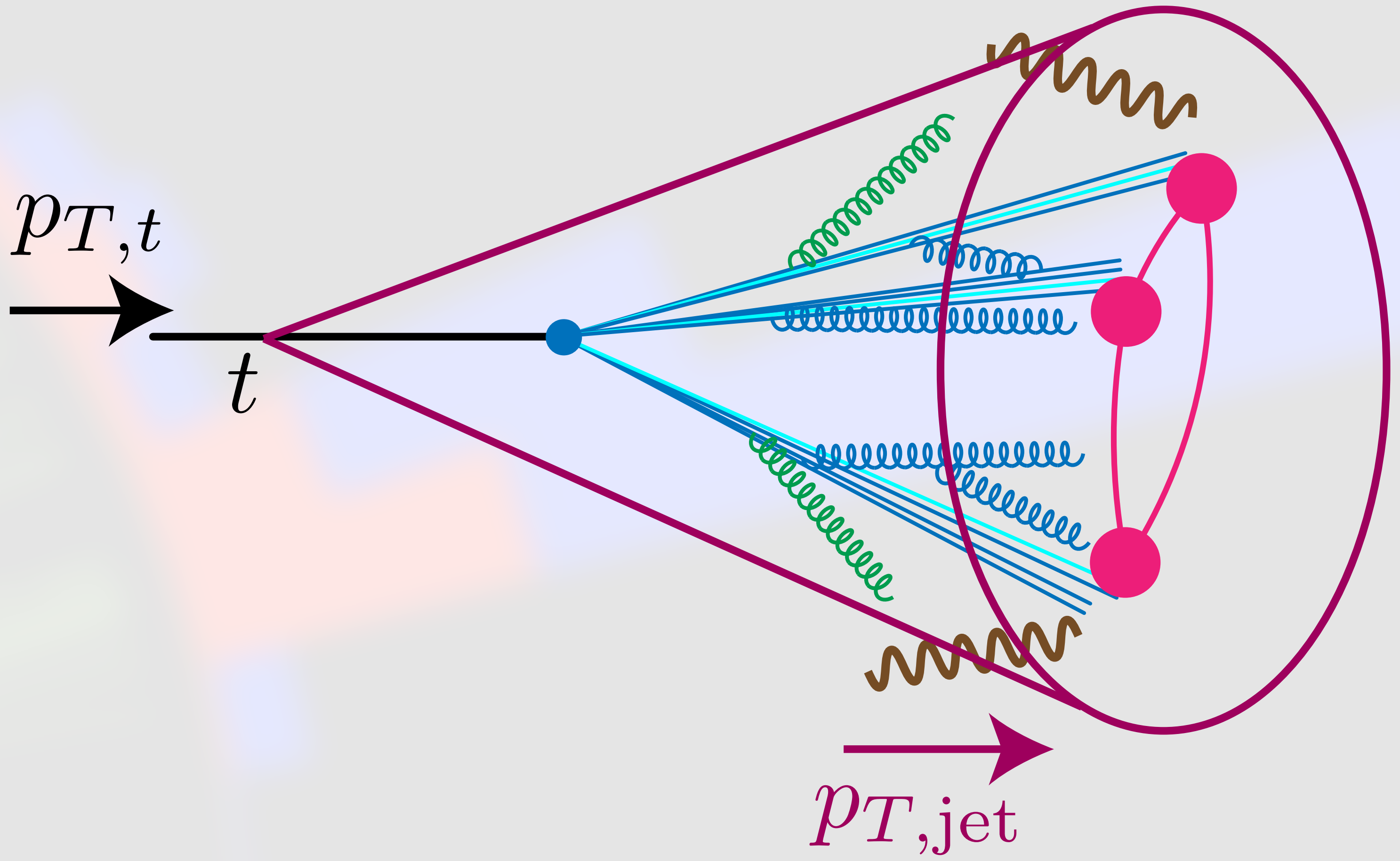
At the LHC we also have soft junk from the underlying event

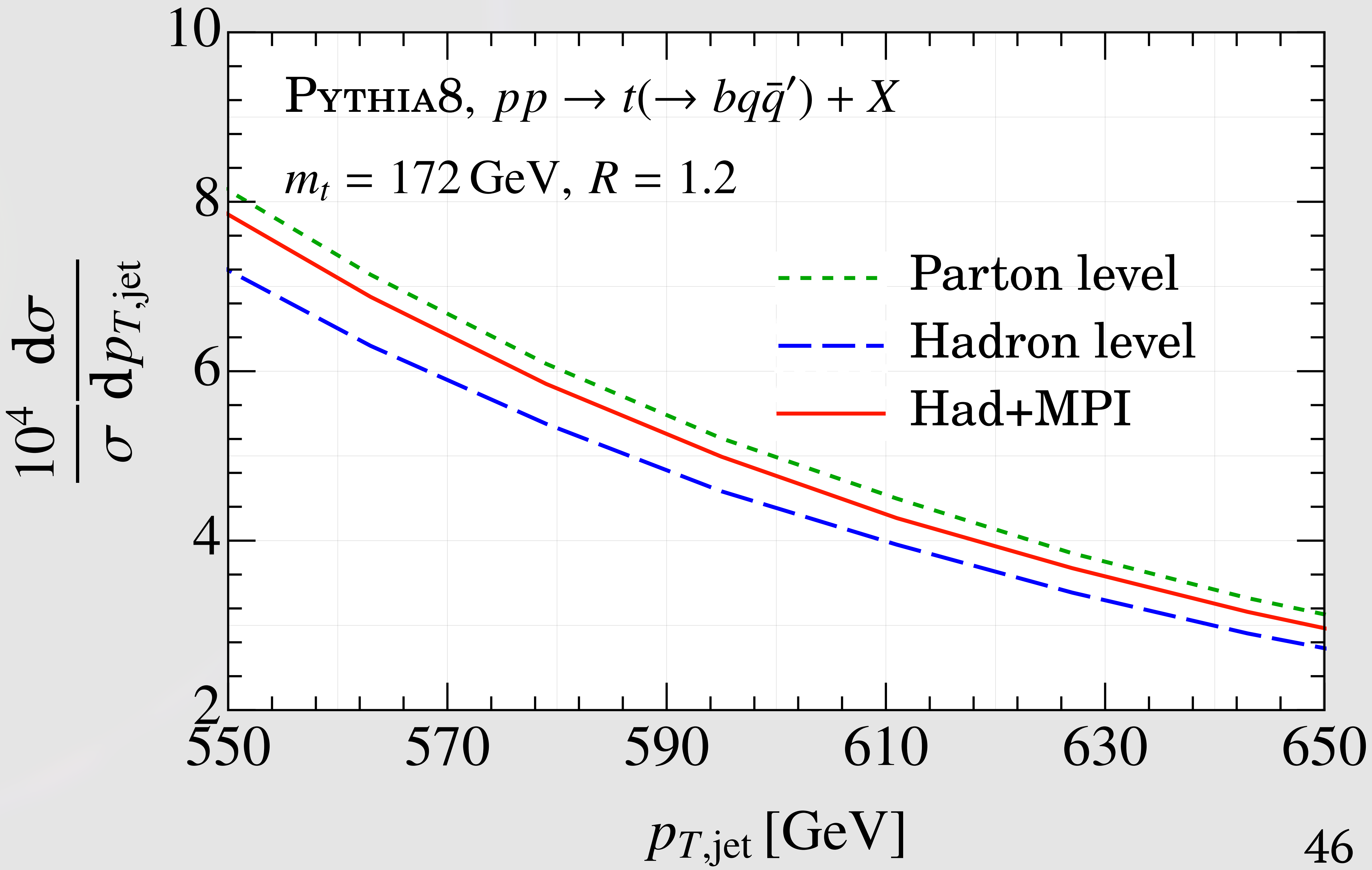
Q1. How does adding UE impact the observable?

We can only indirectly constrain top velocity through $p_{T,\mathrm{jet}}$

Q2. How do shifts in $p_{T,\mathrm{jet}}$ impact the state $|\psi_t\rangle$ and the EEEC measurement?

$$\frac{\langle\psi_t|\mathcal{E}(\vec{n}_1)\mathcal{E}(\vec{n}_2)\mathcal{E}(\vec{n}_3)|\psi_t\rangle}{\langle\psi_t|\psi_t\rangle}$$

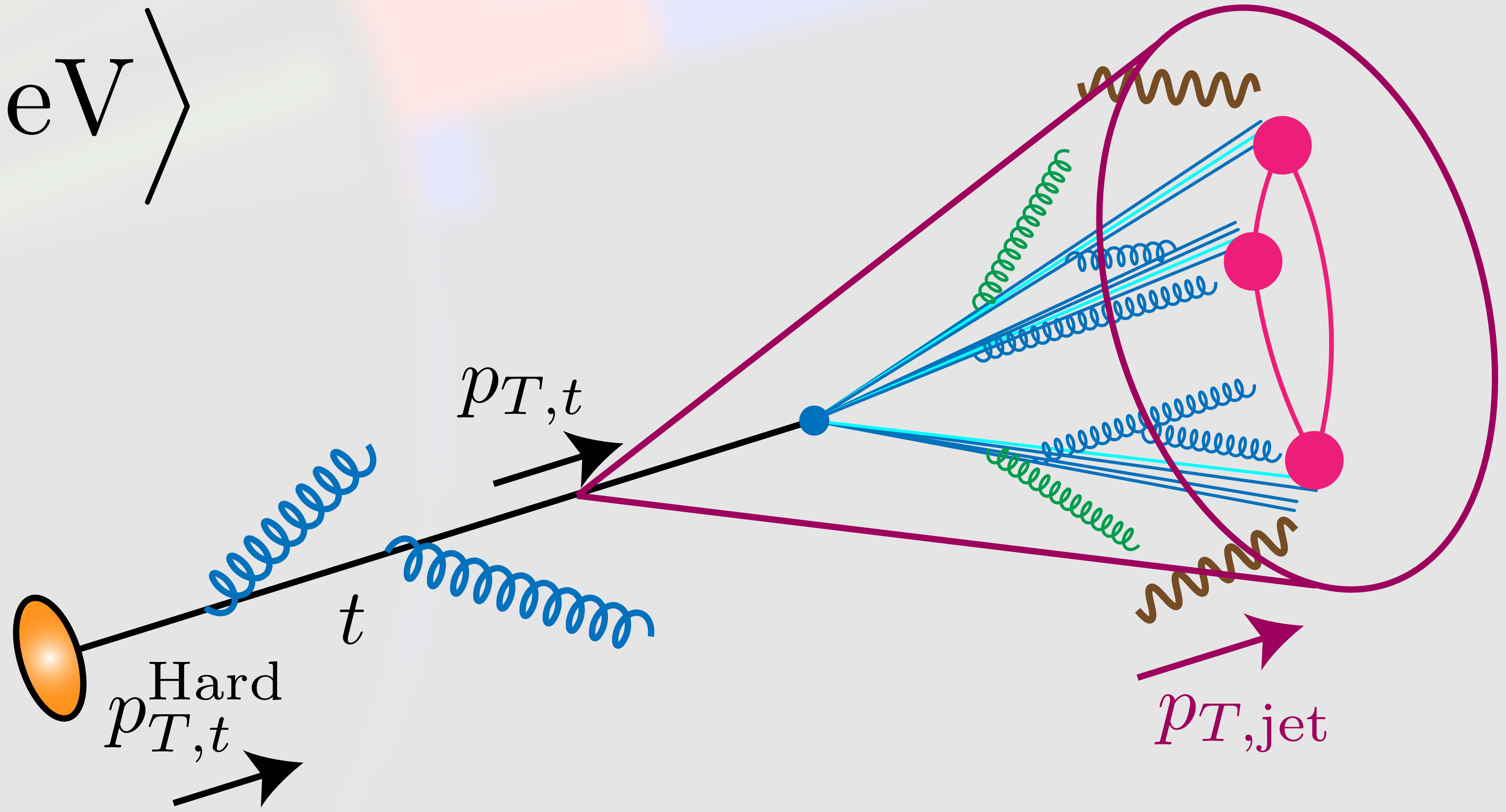




Q1: What is the impact of the underlying event?

For now fix the top quark velocity in *pp* but include underlying event and consider a *(unphysical)* state of hard tops with a definite velocity:

$$|\psi_t\rangle_{pp} = \left|\text{Tops produced with } p_{T,t}^{\text{hard}} = 600 \text{ GeV}\right\rangle$$

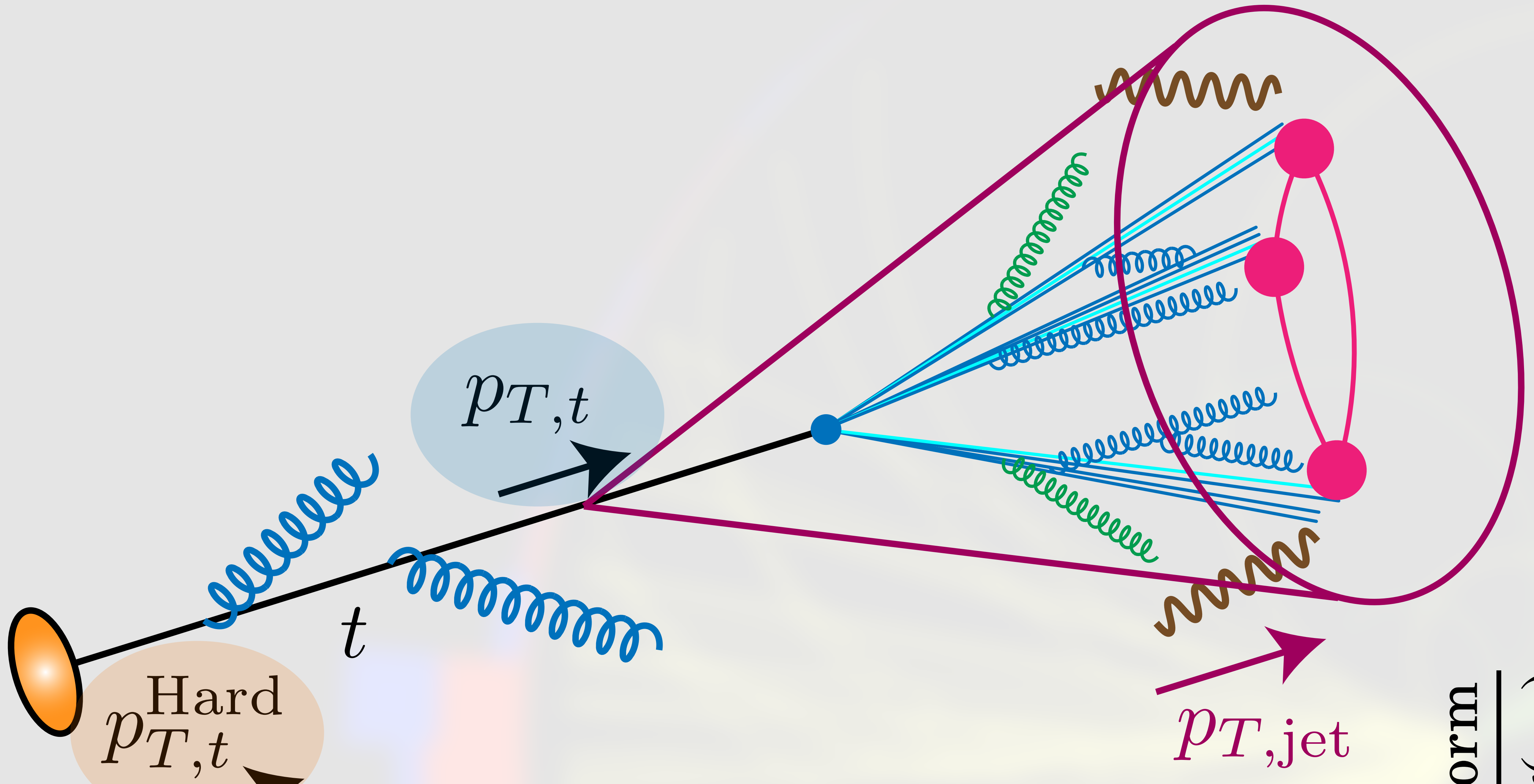


The underlying event still impacts the $p_{T,\text{jet}}$ and adds additional uncorrelated soft radiation to the measurement.

Use $p_{T,\text{jet}}$ in the energy weights

$$\widehat{\mathcal{M}}_{(pp)}^{(n)}(\zeta_{12},\zeta_{23},\zeta_{31}) = \sum_{i,j,k\,\in\,\text{jet}} \frac{(p_{T,i})^n (p_{T,j})^n (p_{T,k})^n}{(p_{T,\text{jet}})^{3n}} \delta\left(\zeta_{12}-\hat{\zeta}_{ij}^{(pp)}\right)\delta\left(\zeta_{23}-\hat{\zeta}_{ik}^{(pp)}\right)\delta\left(\zeta_{31}-\hat{\zeta}_{jk}^{(pp)}\right)$$

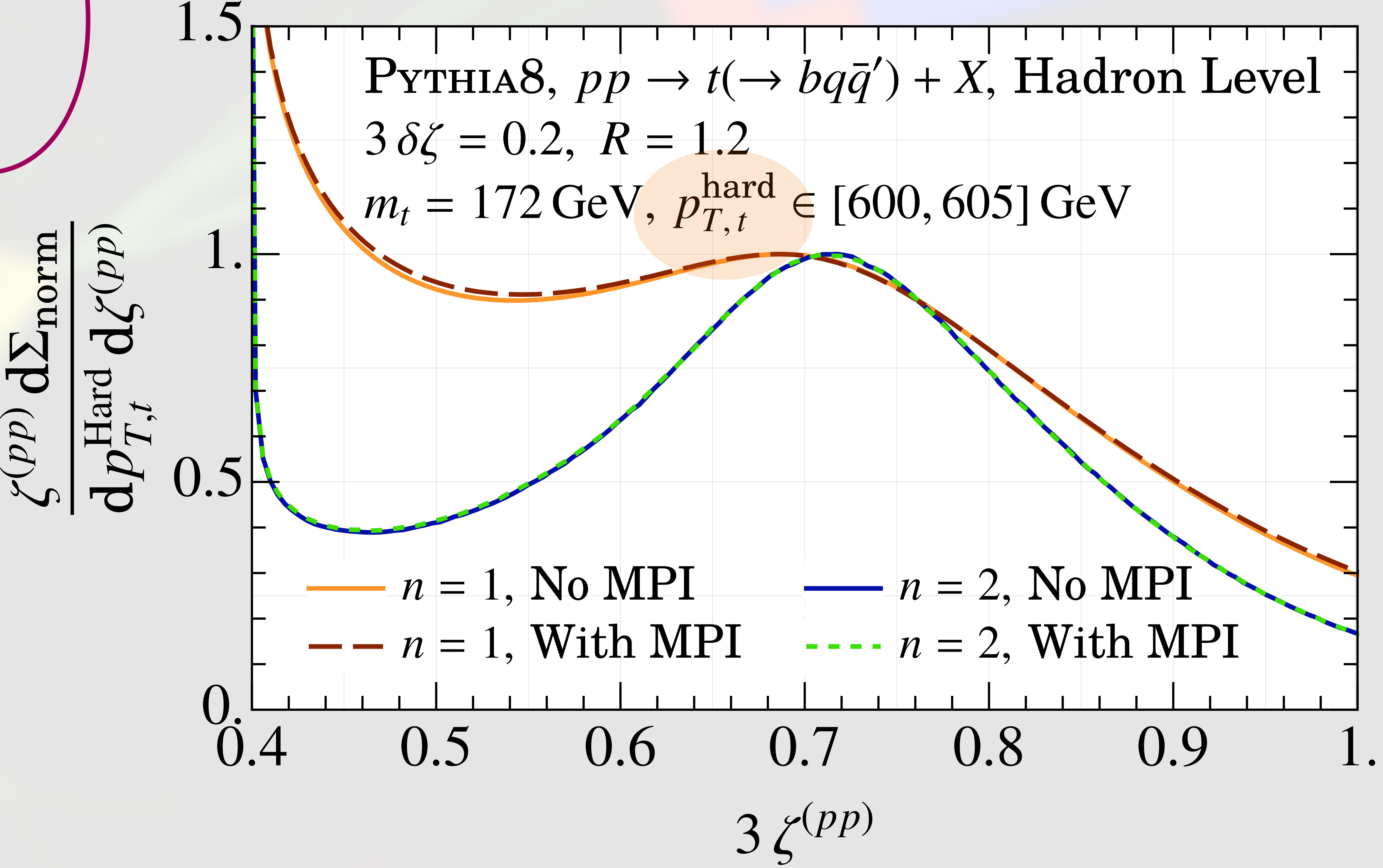
A: Correlators themselves are insensitive to the UE!



$$\zeta^{(pp)}_{\text{peak}} \approx 3\left(\frac{m_t}{p_{T,t}}\right)^2$$

Not $p_{T,\text{jet}}$!

$$|\psi_t\rangle_{pp} = \left|\text{Tops produced with } p^{\text{hard}}_{T,t} = 600\text{ GeV}\right\rangle$$

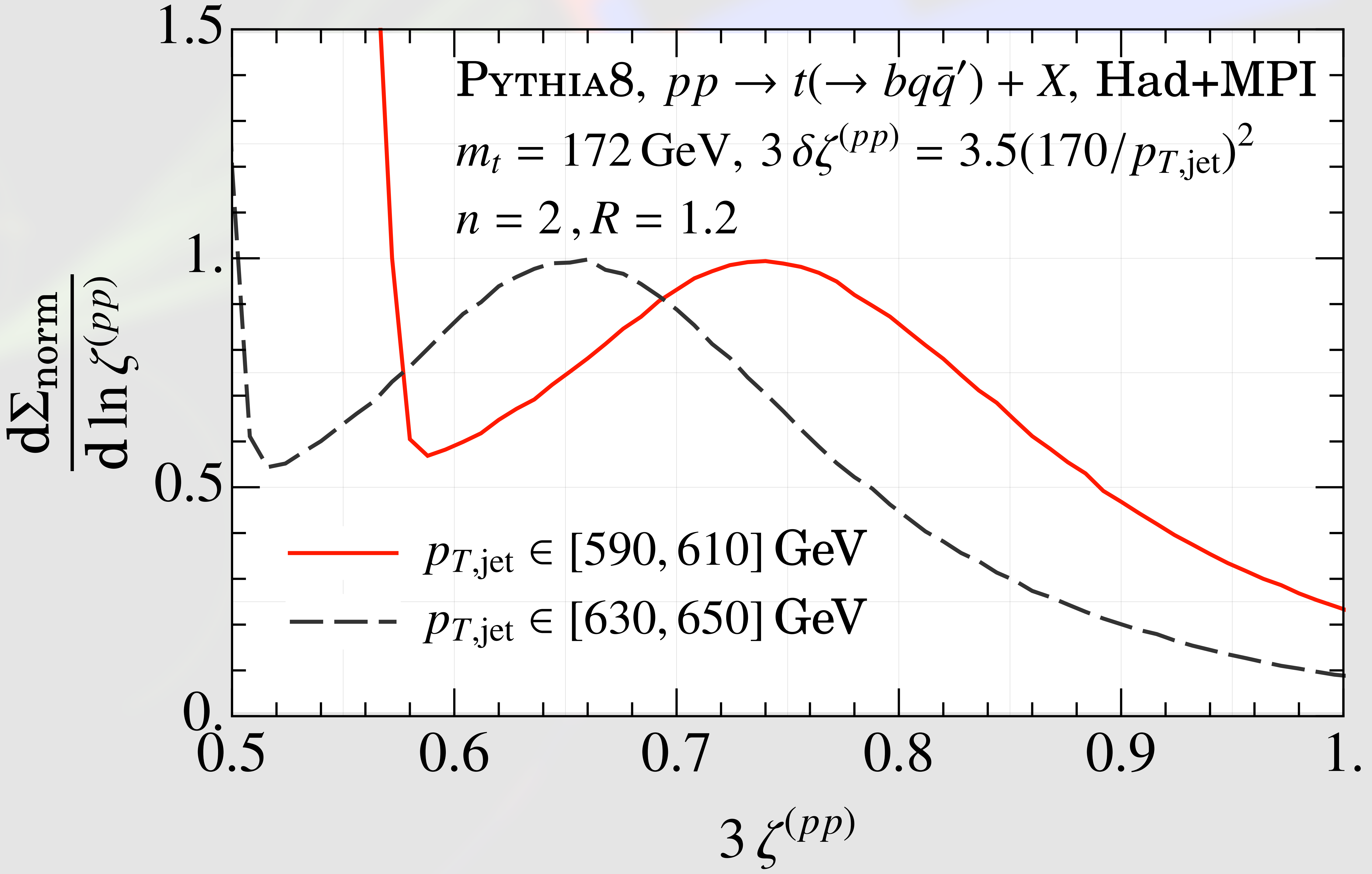


Q2. How to deal with shifts in jet p_T impacting $|\psi_t\rangle$?

Write the measurement as

$$\frac{d\Sigma(\delta\zeta)}{dp_{T,\mathrm{jet}}\,d\zeta} = \boxed{\frac{d\Sigma(\delta\zeta)}{dp_{T,t}\,d\zeta}}\,\frac{dp_{T,t}}{dp_{T,\mathrm{jet}}}$$

Completely insensitive to the underlying event



Only need to characterize the nonperturbative effects on the hard scale $p_{T,\mathrm{jet}}$

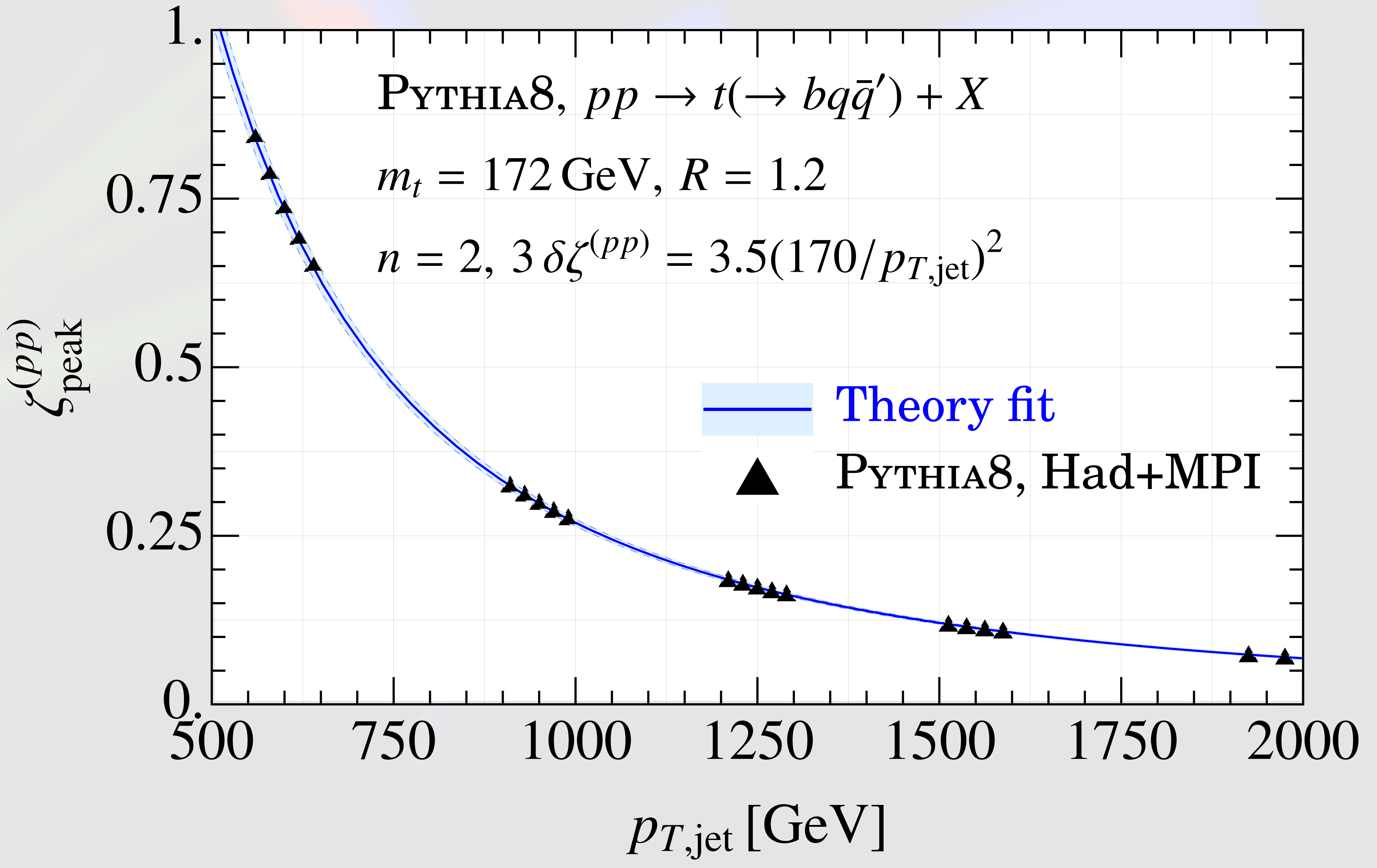
A: Disentangle by considering multiple p_T bins

Unlike jet mass, $p_{T,\mathrm{jet}}$ shifts impact the peak nonlinearly

$$\zeta^{(pp)}_{\mathrm{peak}} = \frac{3F_{\mathrm{pert}}(m_t, p_{T,\mathrm{jet}}, \alpha_s, R)}{\left(p_{T,\mathrm{jet}} + \Delta_{\mathrm{NP}}(R) + \Delta_{\mathrm{MPI}}(R)\right)^2}$$

At leading order $F^{\mathrm{LO}}_{\mathrm{pert}} = m_t^2$

Determine $\Delta_{\mathrm{NP}}(R)$ and $\Delta_{\mathrm{MPI}}(R)$ independently from the $p_{T,\mathrm{jet}}$ spectrum



Pythia8 m_t	Parton $\sqrt{F_{\mathrm{pert}}}$	Hadron + MPI $\sqrt{F_{\mathrm{pert}}}$
172 GeV	172.6 ± 0.3 GeV	$172.3 \pm 0.2 \pm 0.4$ GeV
173 GeV	173.5 ± 0.3 GeV	$173.6 \pm 0.2 \pm 0.4$ GeV
175 GeV	175.5 ± 0.4 GeV	$175.1 \pm 0.3 \pm 0.4$ GeV
173 – 172	0.9 ± 0.4 GeV	1.3 ± 0.6 GeV
175 – 172	2.9 ± 0.5 GeV	2.8 ± 0.6 GeV

A promising evidence for complete theoretical control of the top mass up to errors $\lesssim 1$ GeV!

Outlook

Future improvements:

1. Improve the MC analysis by optimizing for $\Delta\zeta$, binning of $p_{T,\text{jet}}$ and exploring configurations other than equilateral triangle
2. A systematic study of statistical power including HL-LHC projections

Factorization theorem:

Mele, Nason 1990,1991;
Czakon et al 2102.08267

$$\frac{\mathrm{d}\Sigma}{\mathrm{d}p_{T,\text{jet}}\mathrm{d}\eta\,\mathrm{d}\zeta} = f_i \otimes f_j \otimes H_{i,j\to t}\left(z_J; p_{T,t} = \frac{p_{T,\text{jet}}}{z_J}, \eta\right)$$

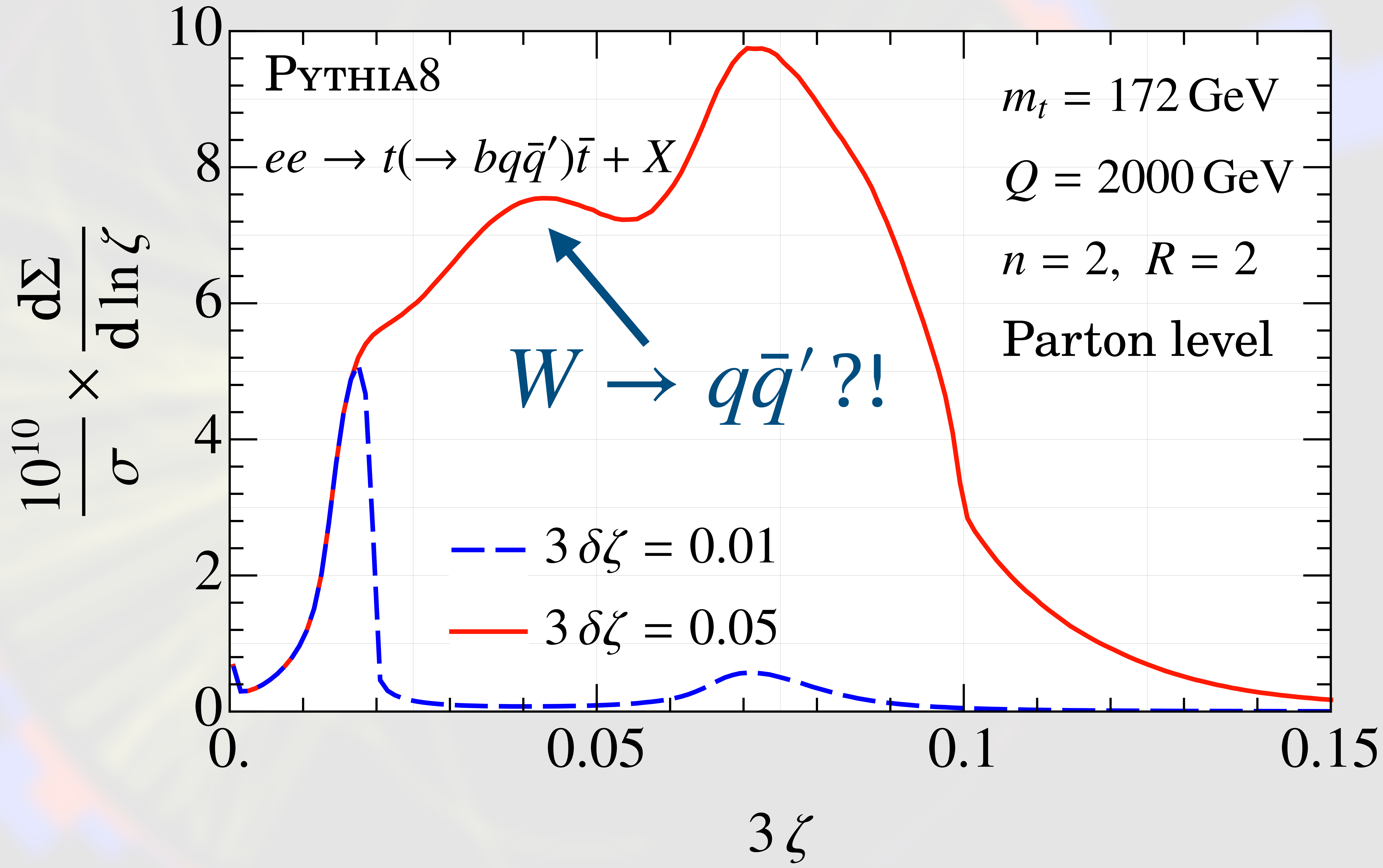
$$\otimes J_{t\to t}(z_J, z_h; R) \otimes J^{[\text{tracks}]}_{\text{EEEC}}(n, z_h, \zeta; m_t; \Gamma_t)$$

Kang, Ringer, Vitev 1606.07063

Energy correlator jet function

Outlook

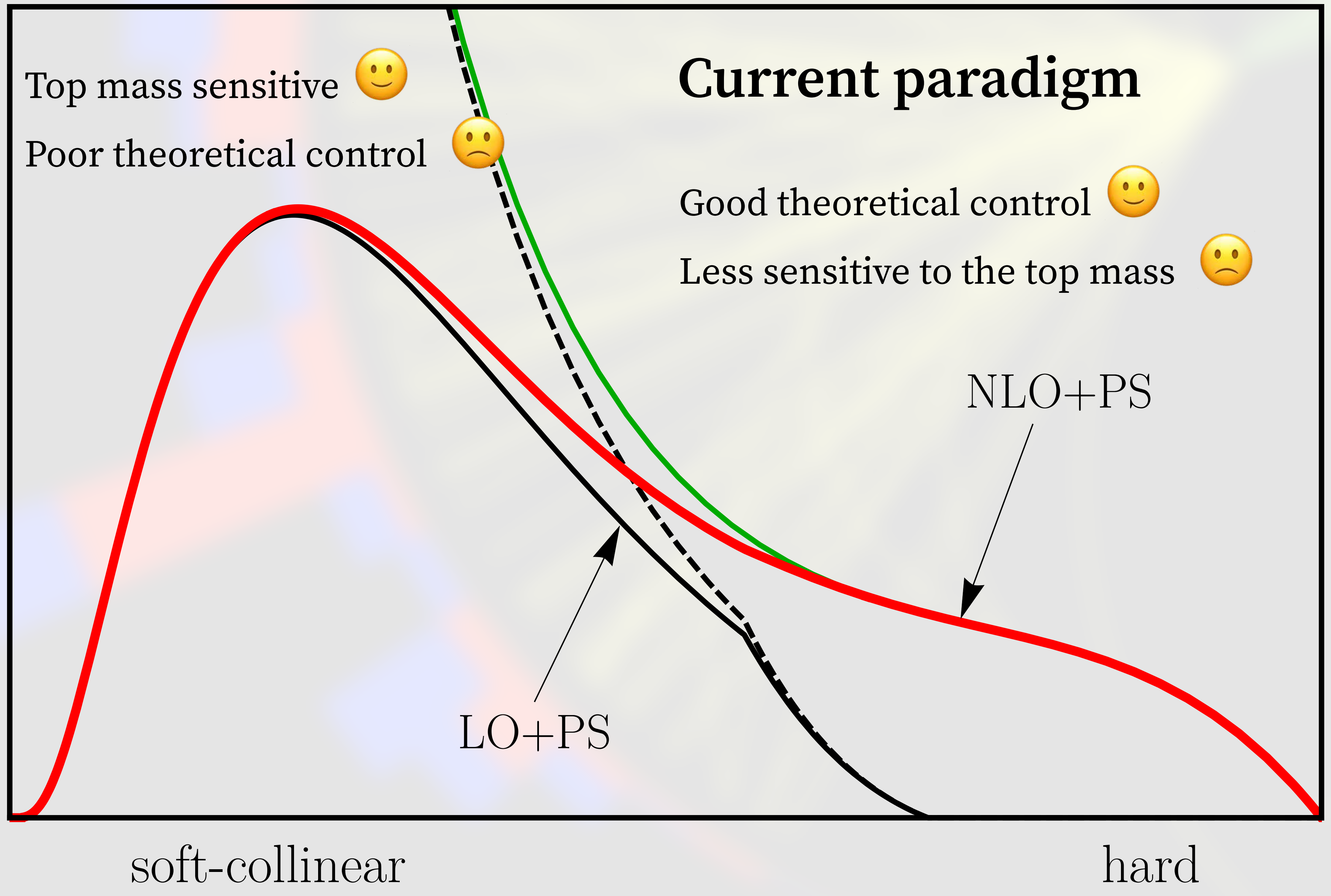
Can we exploit the imprint of 2-body W decay in tops in the 3-point correlator?!

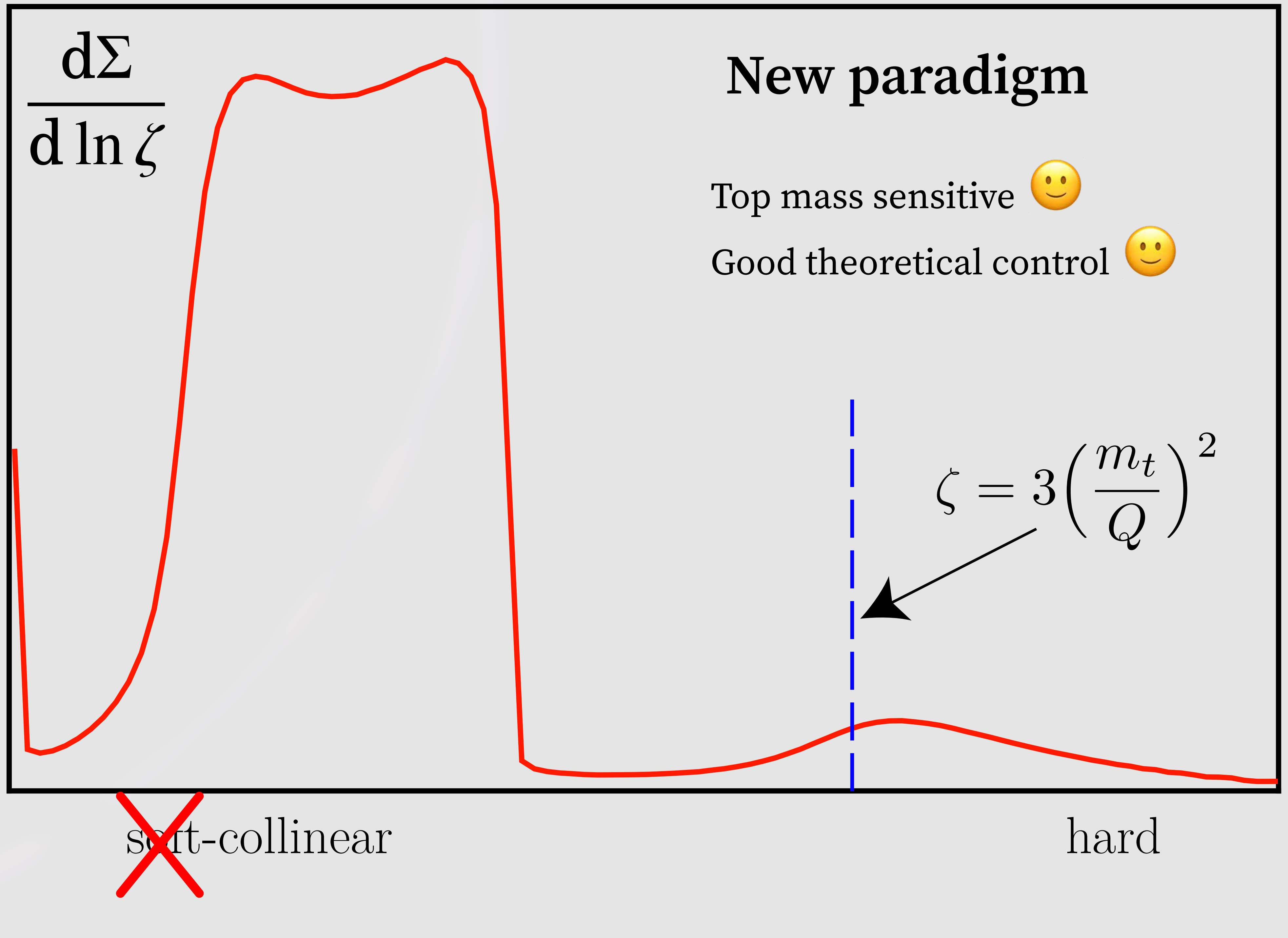


Possibly a way to overcome the systematics of $p_{T,\mathrm{jet}}$ shifts due to the underlying event?

Conclusions

1. The 3-point correlation function gives a kinematic structure in the hard region
2. Very tiny hadronization corrections to the normalized spectrum
3. Impact on $p_{T,\text{jet}}$ can be independently studied quantified.





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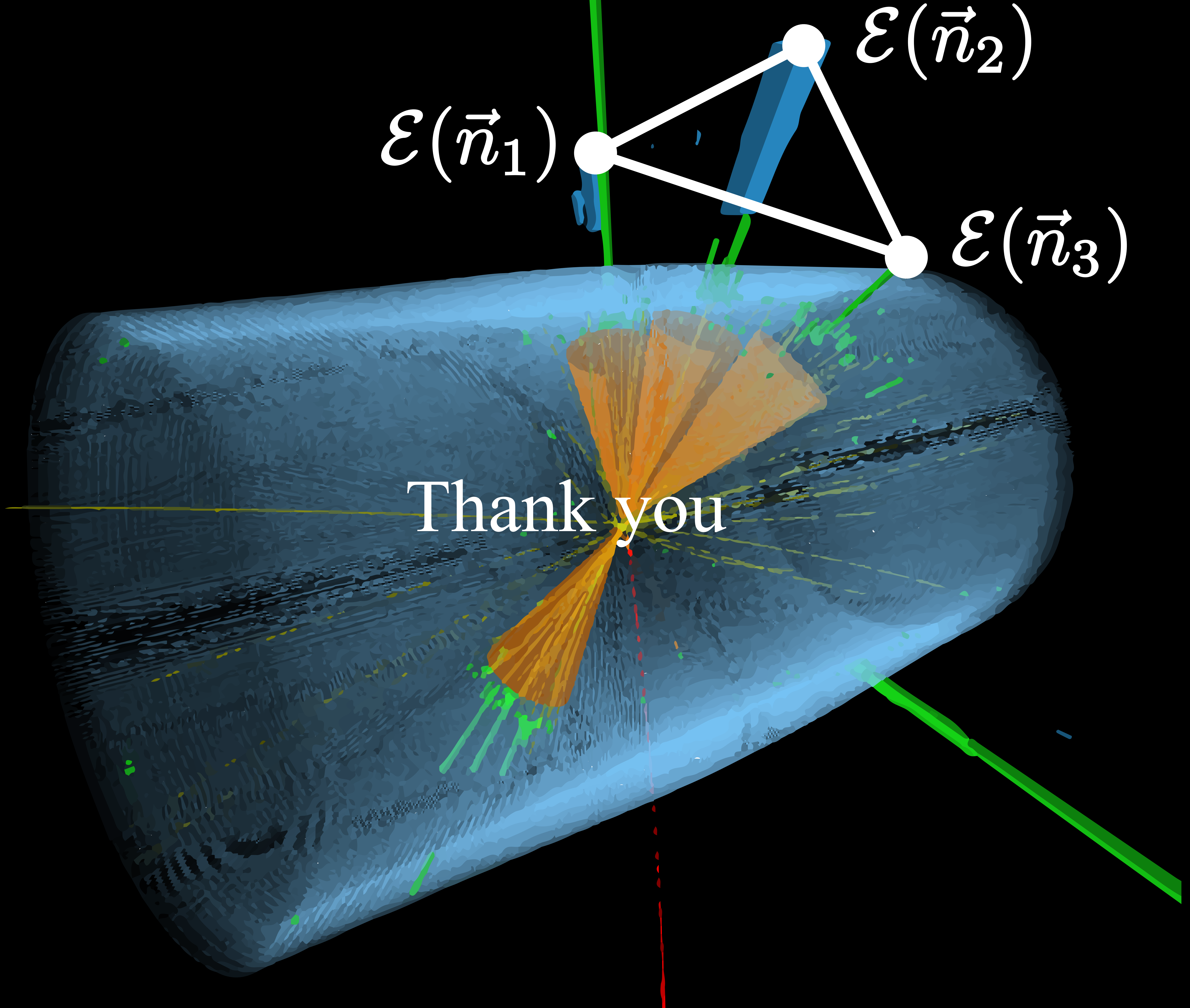
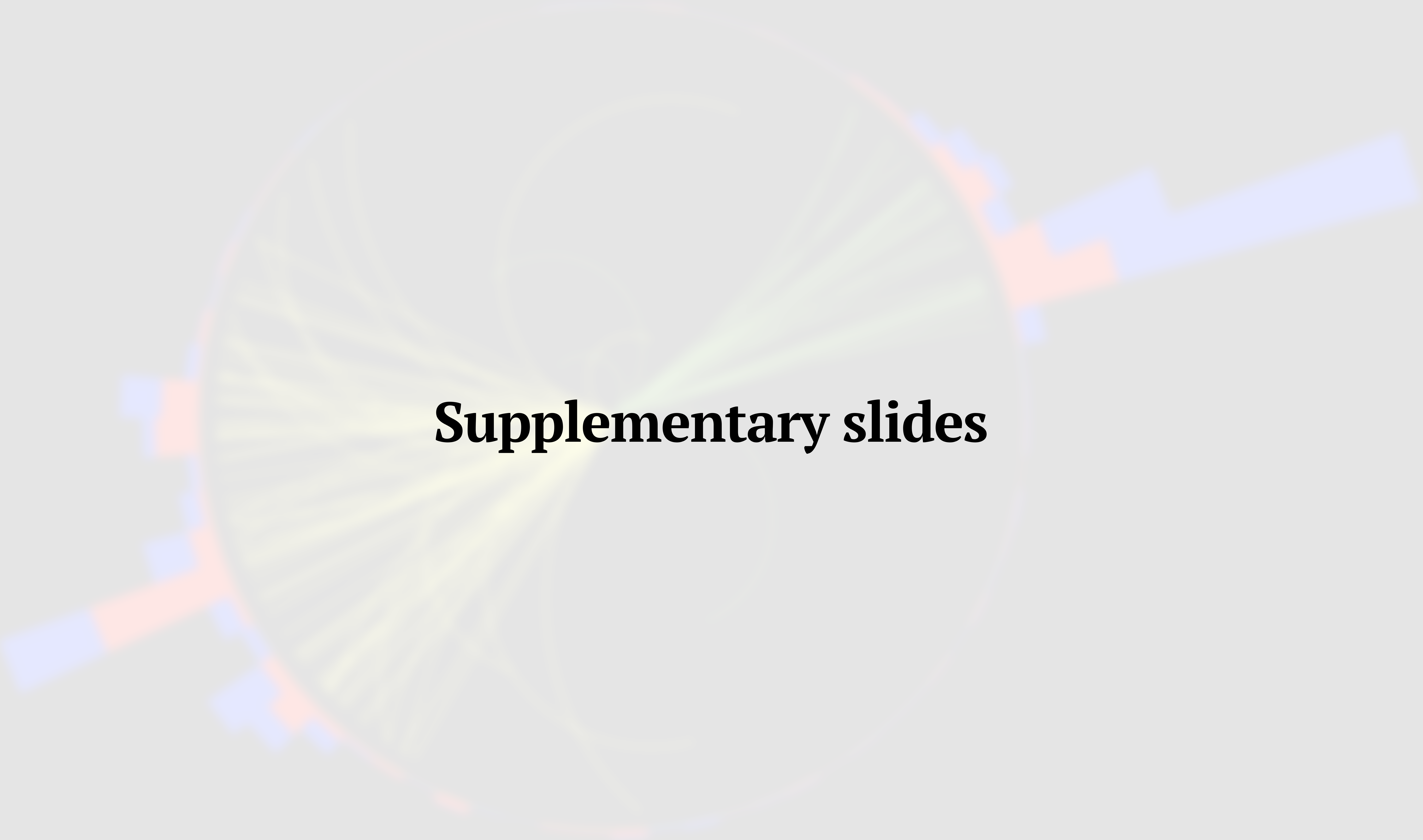


Thank you



Supplementary slides

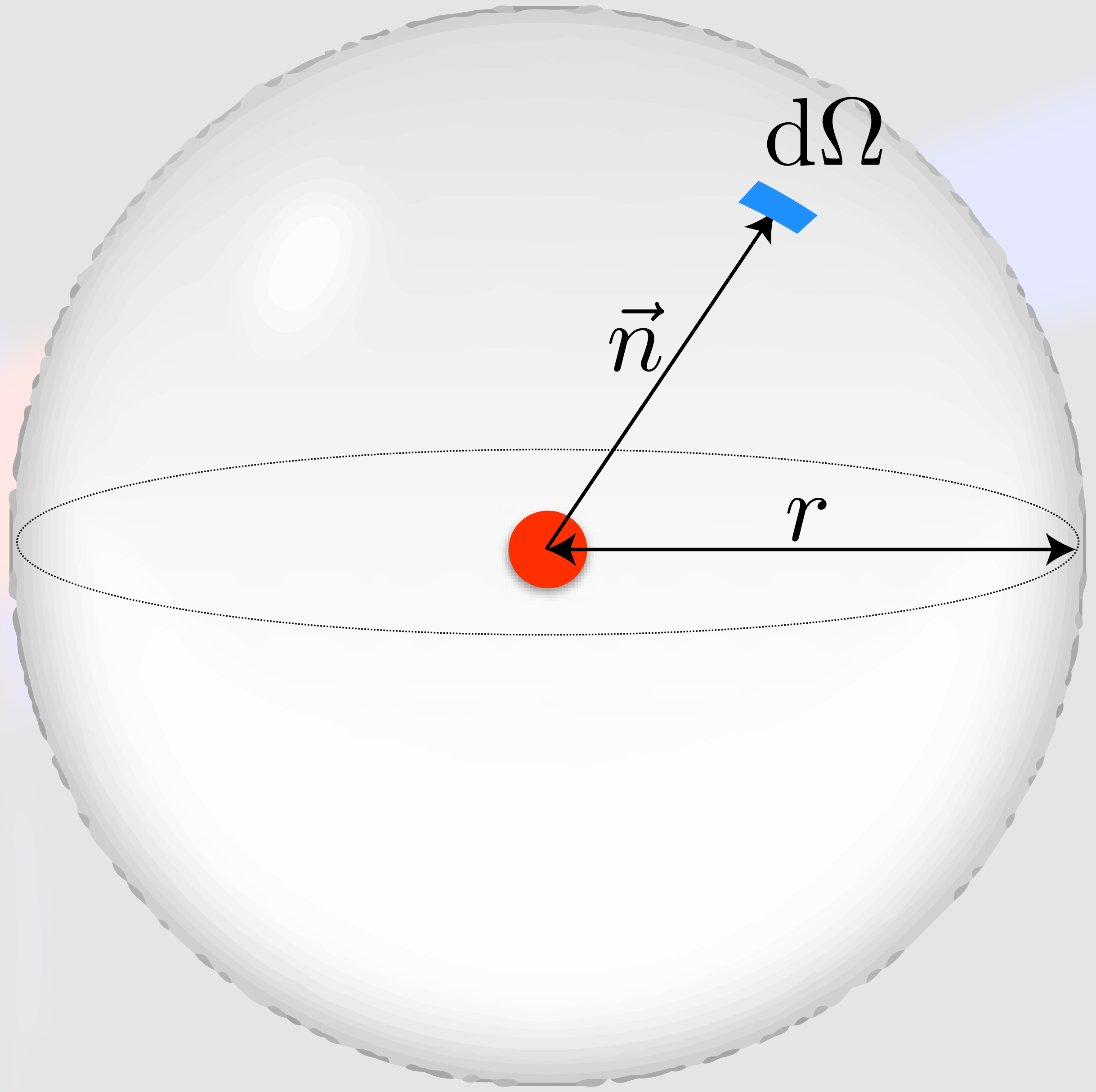
Light Ray Operators

Need light ray operators for Lorentzian signature

Sveshnikov, Tkachov hep-ph/9512370, Hofman, Maldacena; 0803.1467

$$\mathcal{E}(\vec{n}) = \int_0^\infty dt \lim_{r\to\infty} r^2 n^i T_{0i}(t, r\vec{n})$$

$$\mathcal{E}(\vec{n}) \simeq \int_0^\infty \mathrm{d}t \left(\text{Energy flux through } \mathrm{d}\Omega \right)$$



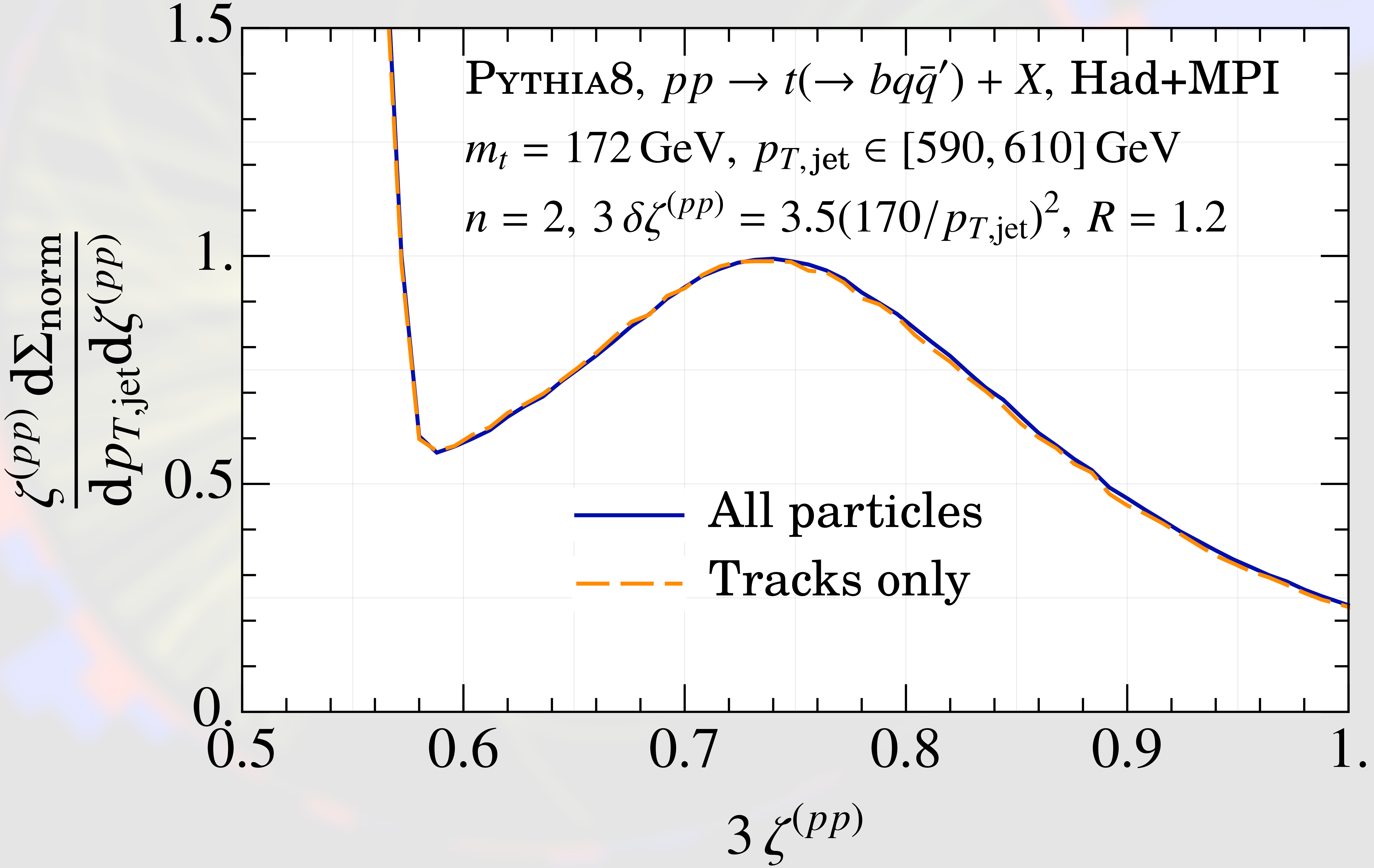
Consider correlation functions of energy flow operators:

$$\langle\psi|\mathcal{E}(\vec{n}_1)\mathcal{E}(\vec{n}_2)\ldots\mathcal{E}(\vec{n}_N)|\psi\rangle$$

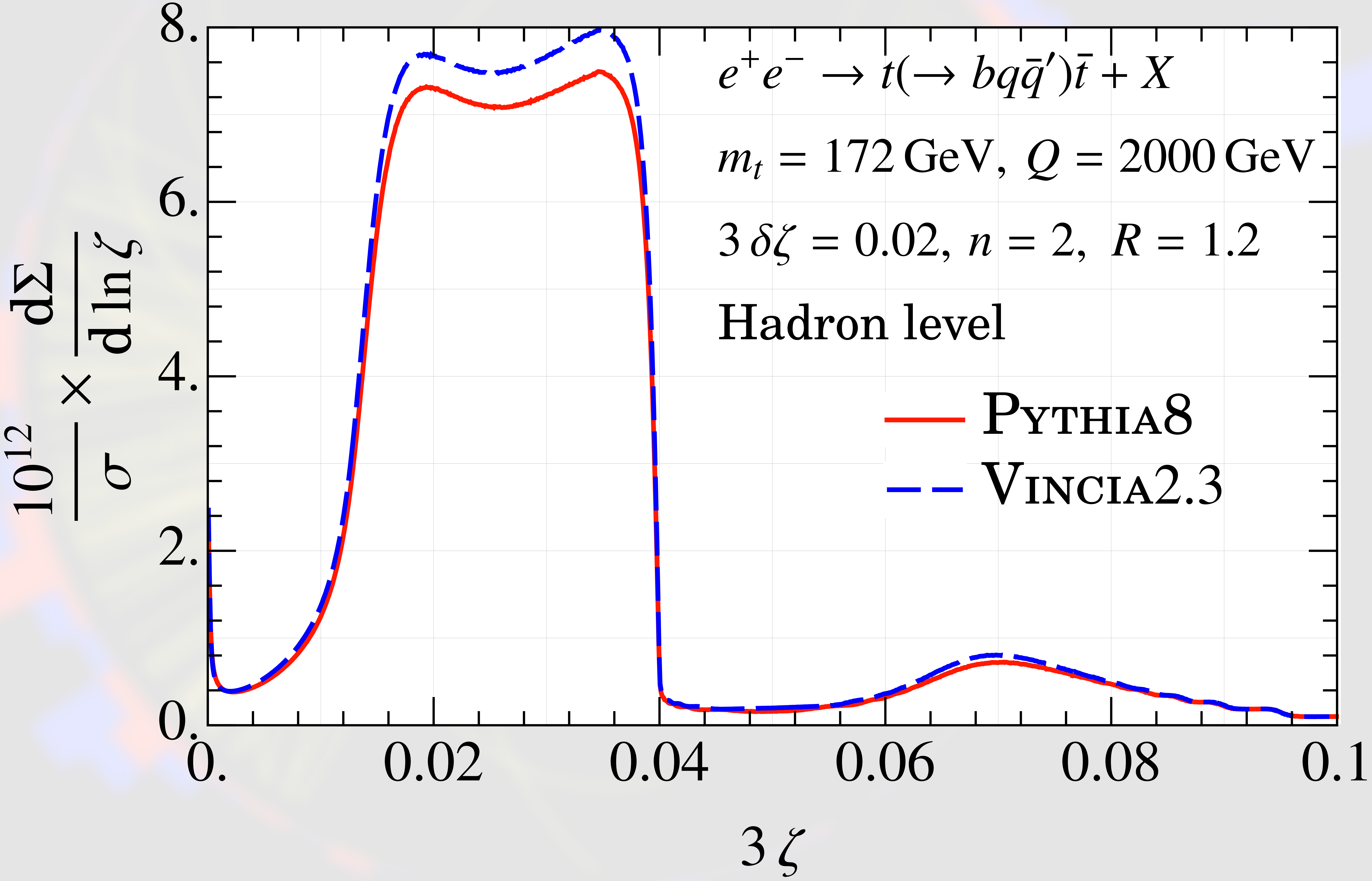
$|\psi\rangle$ specifies the state on which we measure the correlator

Measurement on tracks

The measurement is insensitive to the usage of tracks, allowing for high angular resolution.

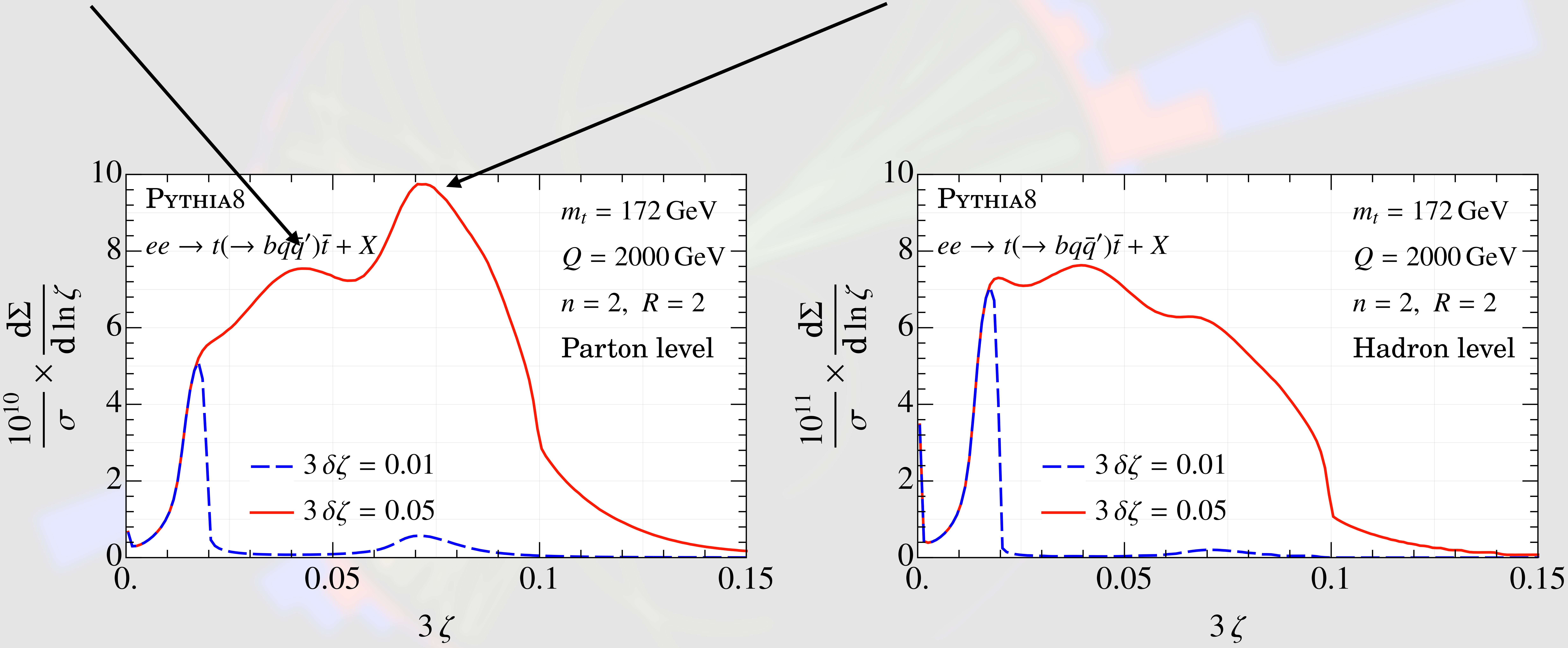


Comparison with Vincia



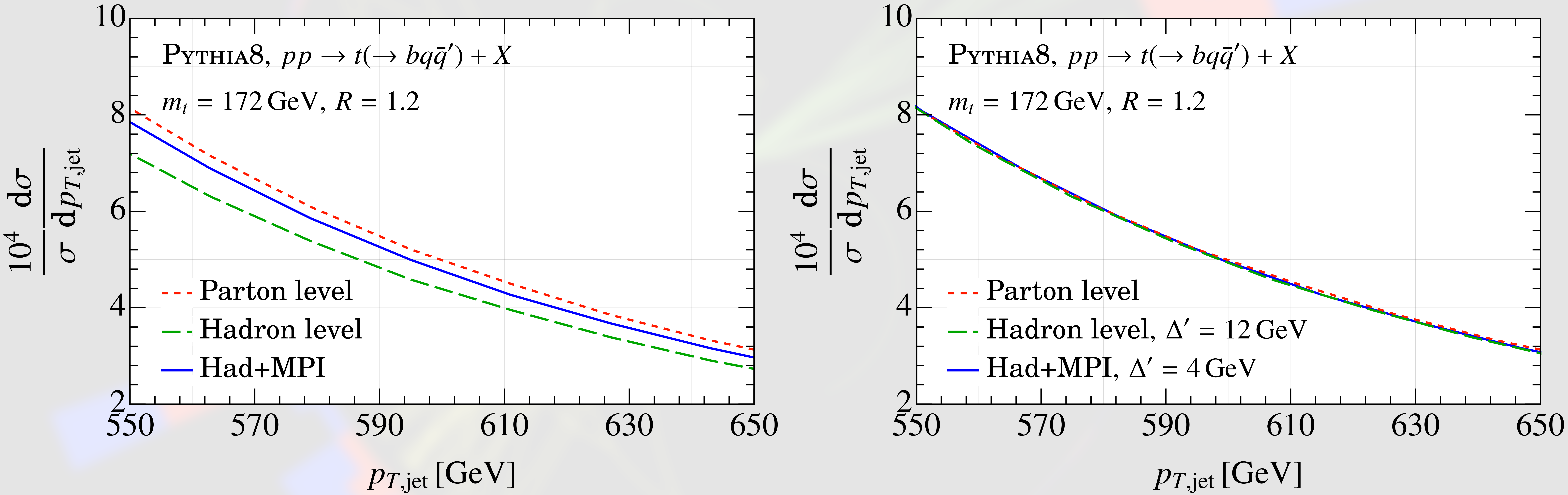
Relaxing asymmetry cut at parton and hadron level

This peak ($W \to q\bar{q}'$?) persists at hadron level, while this one ($t \to bq\bar{q}'$) requires asymmetry cut.



Analysis of $p_{T,\text{jet}}$ shifts

Here we show $p_{T,\text{jet}}$ shifts relative to parton level:



Obtaining the top mass from multiple $p_{T,\text{jet}}$ bins

1. Parameterize the all orders peak position:

$$\zeta_{\text{peak}}^{(pp)} = 3(1+\mathcal{O}(\alpha_s))\frac{m_t^2}{f(p_{T,\text{jet}}, m_t, \alpha_s, \Lambda_{\text{QCD}})^2} \equiv 3(1+\mathcal{O}(\alpha_s))\frac{m_t^2}{\left(p_{T,\text{jet}} + \Delta(p_{T,\text{jet}}, m_t, \alpha_s, \Lambda_{\text{QCD}})\right)^2}$$

2. Work with

$$\rho^2(\zeta_{\text{peak}}^{(pp)\text{v}}, p_{T,\text{jet}}^{\text{v}}) = \left(\zeta_{\text{peak}}^{(pp)\text{ref}} - \zeta_{\text{peak}}^{(pp)\text{v}}\right)\left(\frac{3(1+\mathcal{O}(\alpha_s))}{(p_{T,\text{jet}}^{\text{v}})^2} - \frac{3(1+\mathcal{O}(\alpha_s))}{(p_{T,\text{jet}}^{\text{ref}})^2}\right)^{-1},$$

3. Define

$$\Delta^{\text{ref}} \equiv \Delta(p_{T,\text{jet}}^{\text{ref}}, m_t, \alpha_s, \Lambda_{\text{QCD}}), \qquad \Delta^{\text{v}}(p_{T,\text{jet}}^{\text{v}} - p_{T,\text{jet}}^{\text{ref}}, m_t, \alpha_s, \Lambda_{\text{QCD}}) \equiv \Delta(p_{T,\text{jet}}^{\text{v}}, m_t, \alpha_s, \Lambda_{\text{QCD}}) - \Delta^{\text{ref}}$$

4. Solve for ρ

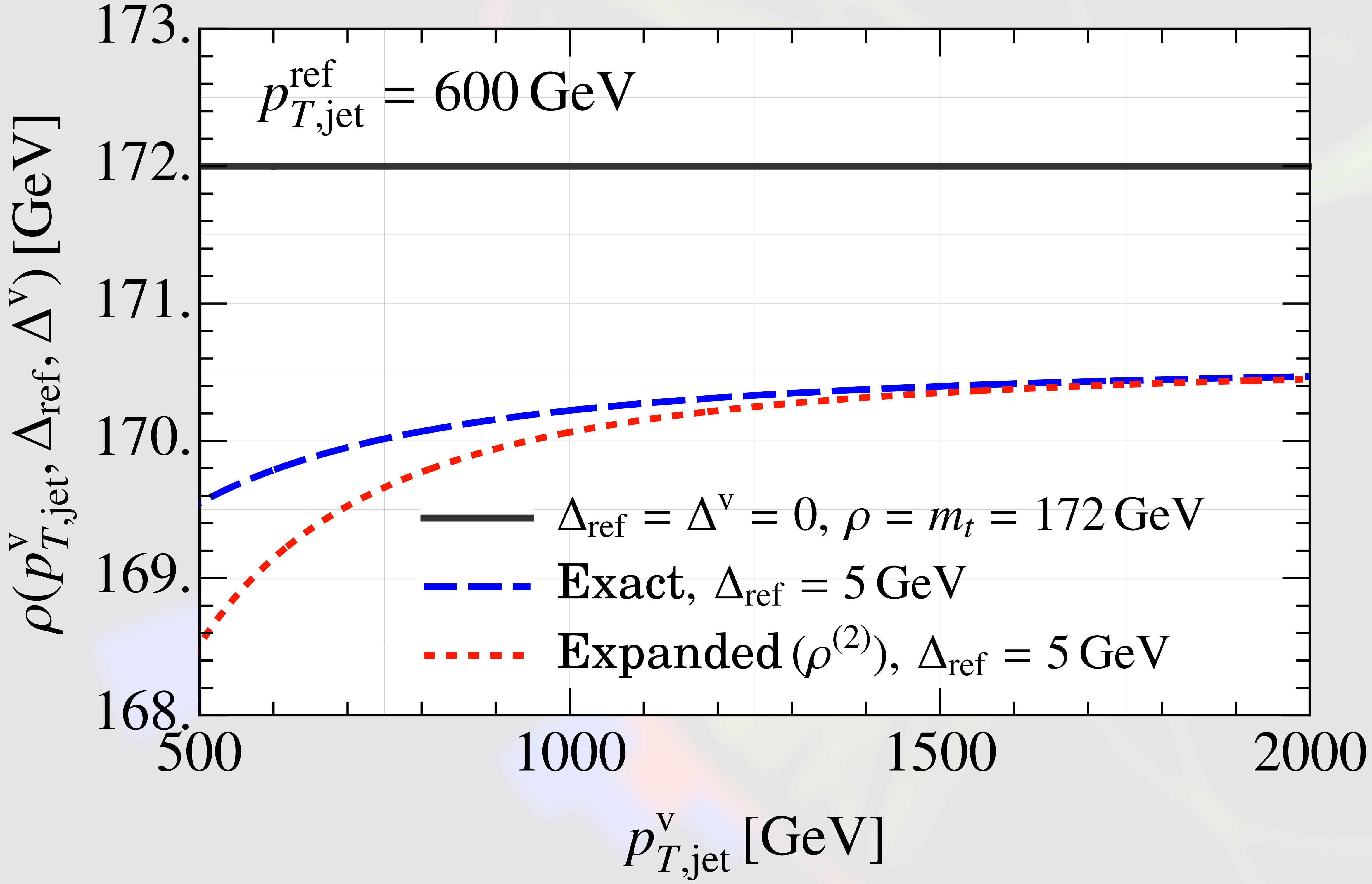
$$\rho(p_{T,\text{jet}}^{\text{v}}, \Delta^{\text{ref}}, \Delta^{\text{v}}) = \sqrt{F_{\text{pert}}}\,\frac{p_{T,\text{jet}}^{\text{ref}}}{p_{T,\text{jet}}^{\text{ref}} + \Delta^{\text{ref}}}\left(1 - \frac{2p_{T,\text{jet}}^{\text{ref}}\Delta^{\text{ref}} + (\Delta^{\text{ref}})^2}{2(p_{T,\text{jet}}^{\text{v}})^2} + \frac{\left(p_{T,\text{jet}}^{\text{ref}} + \Delta^{\text{ref}}\right)^2\left(\Delta^{\text{ref}} + \Delta^{\text{v}}\right)}{8(p_{T,\text{jet}}^{\text{v}})^3} + \ldots\right)$$

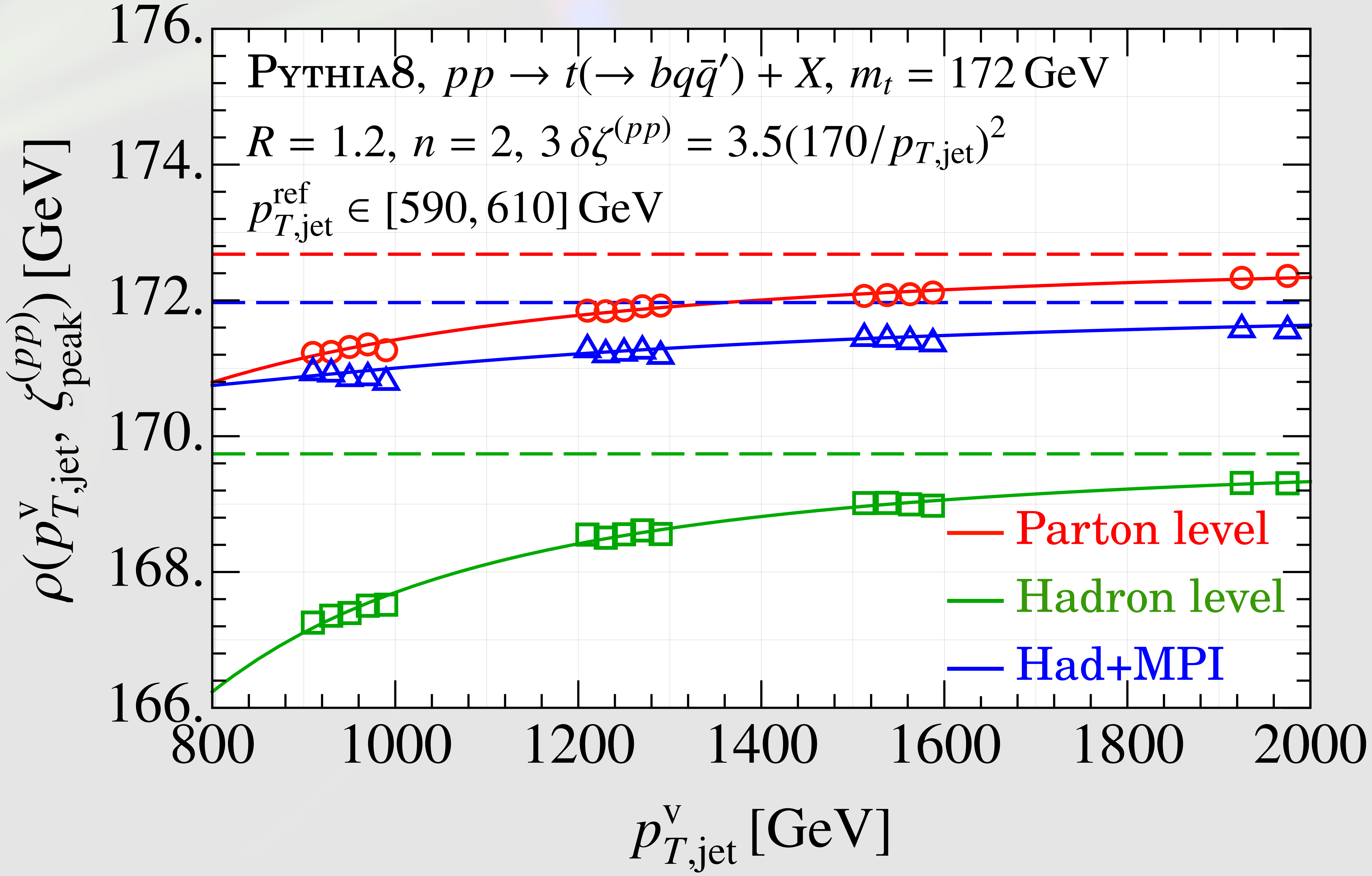
5. The asymptotic value for $p_{T,\text{jet}}^{\text{v}}$ depends only on m_t and Δ^{ref}.

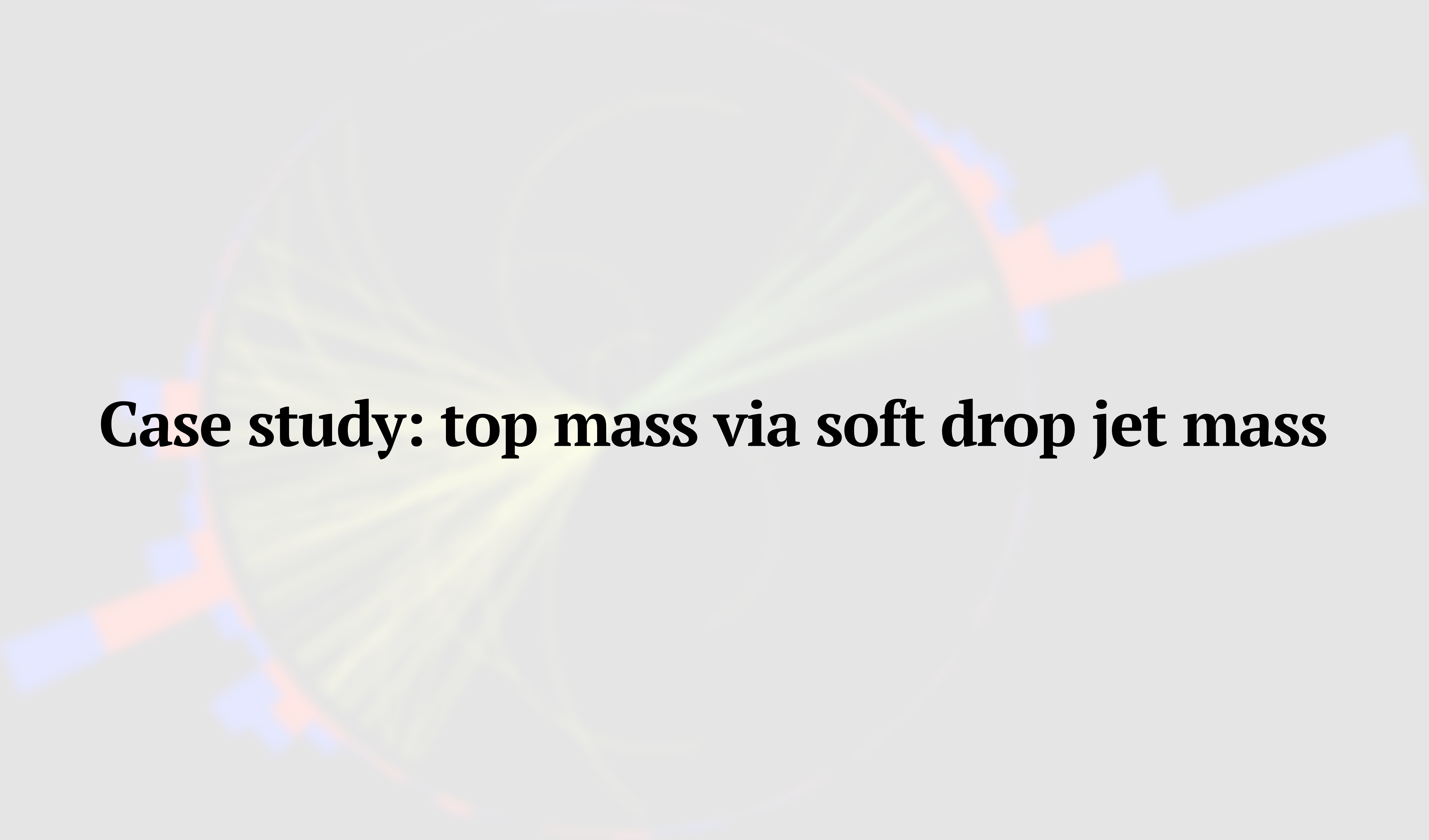
Obtaining the top mass from multiple $p_{T,\mathrm{jet}}$ bins

Fit function:

$$\rho = \rho_{\mathrm{asy}} + c_2 (p^{\mathrm{v}}_{T,\mathrm{jet}})^{-2} + c_3 (p^{\mathrm{v}}_{T,\mathrm{jet}})^{-3}$$



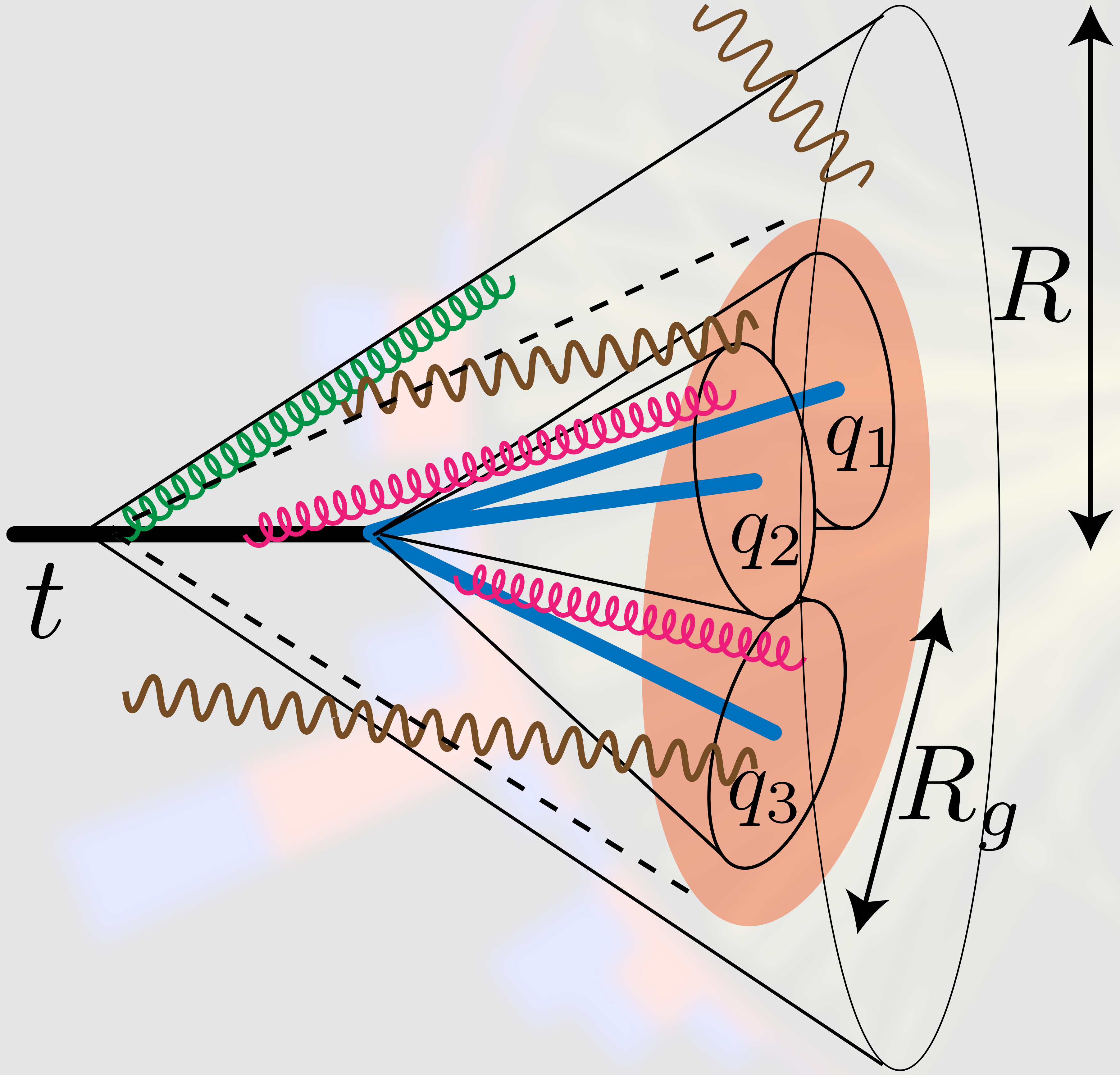




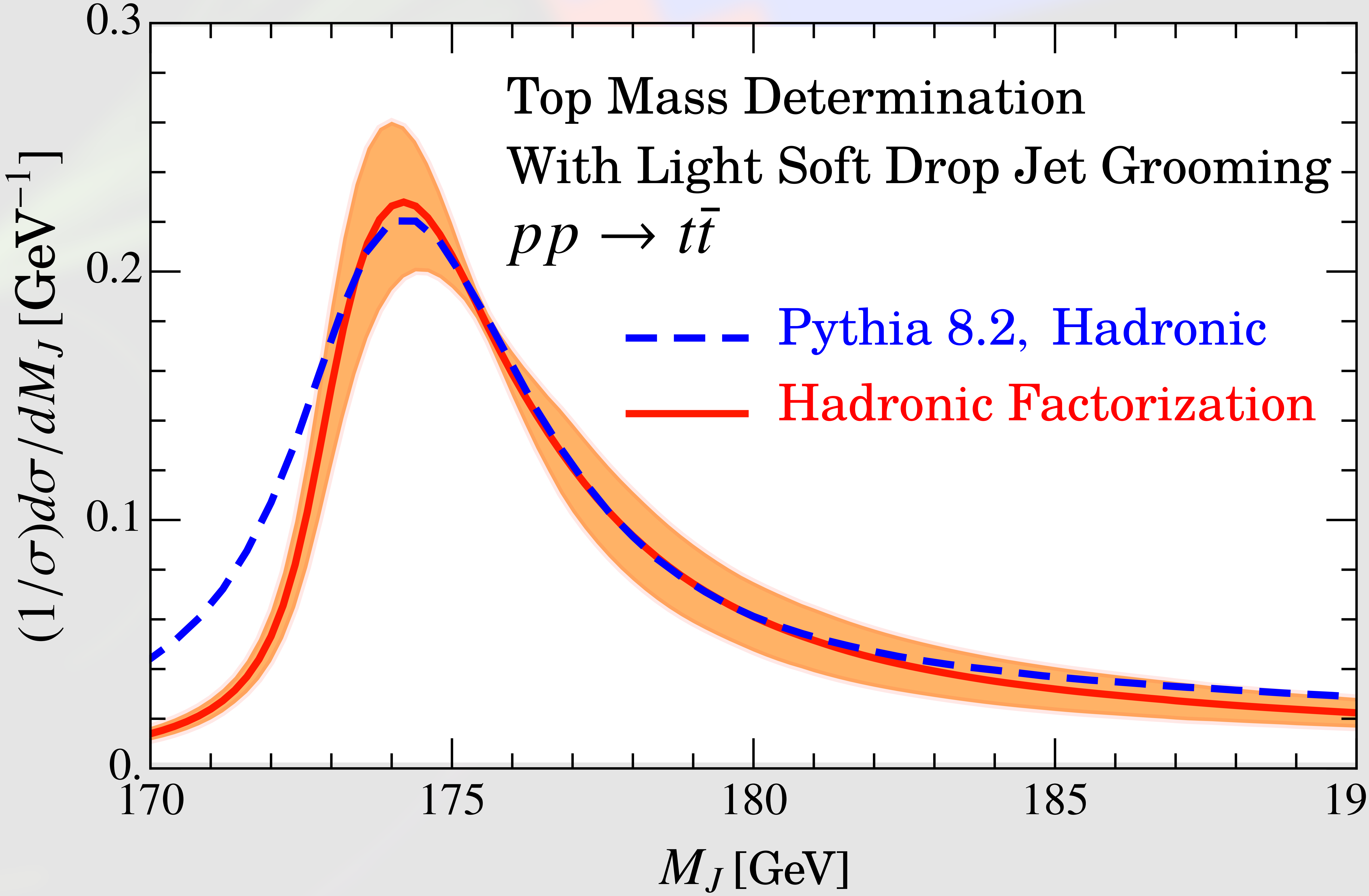
Case study: top mass via soft drop jet mass

Soft drop jet mass

Soft drop jet mass can be analytically resummed as well

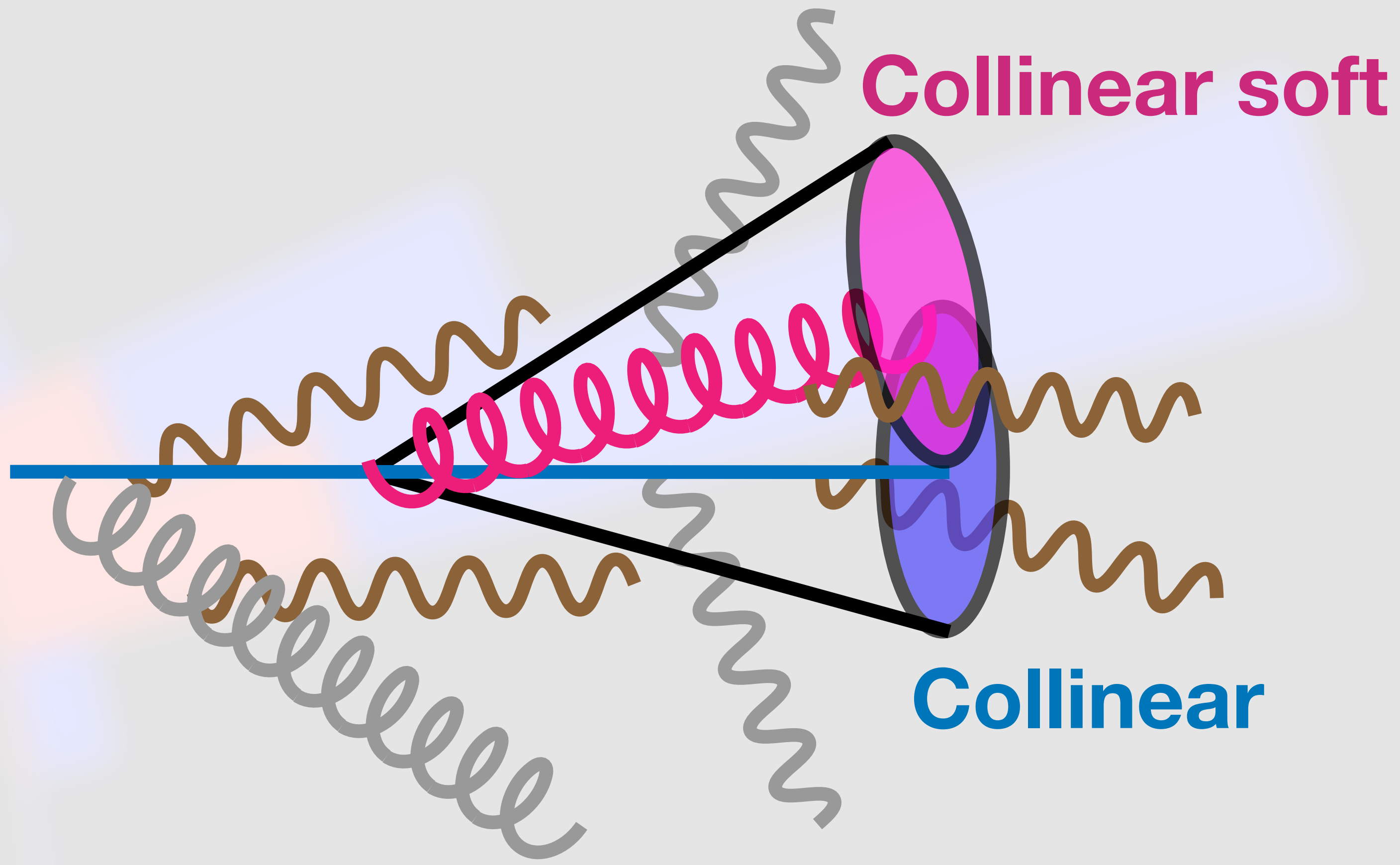


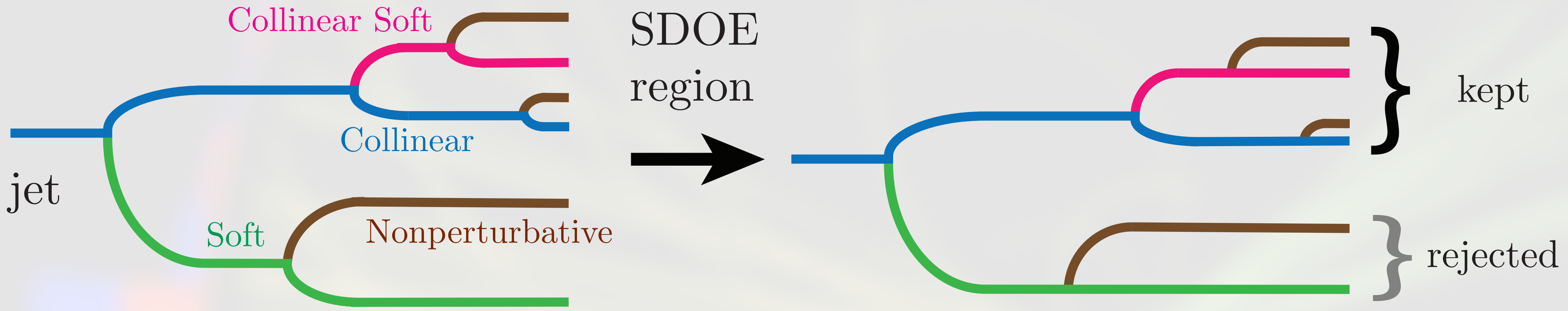
Hoang, Mantry, AP, Stewart 1708.02586



Hadronization corrections

To describe the hadronization corrections we looked closely into the effects of clustering and two-pronged geometry of the groomed jet

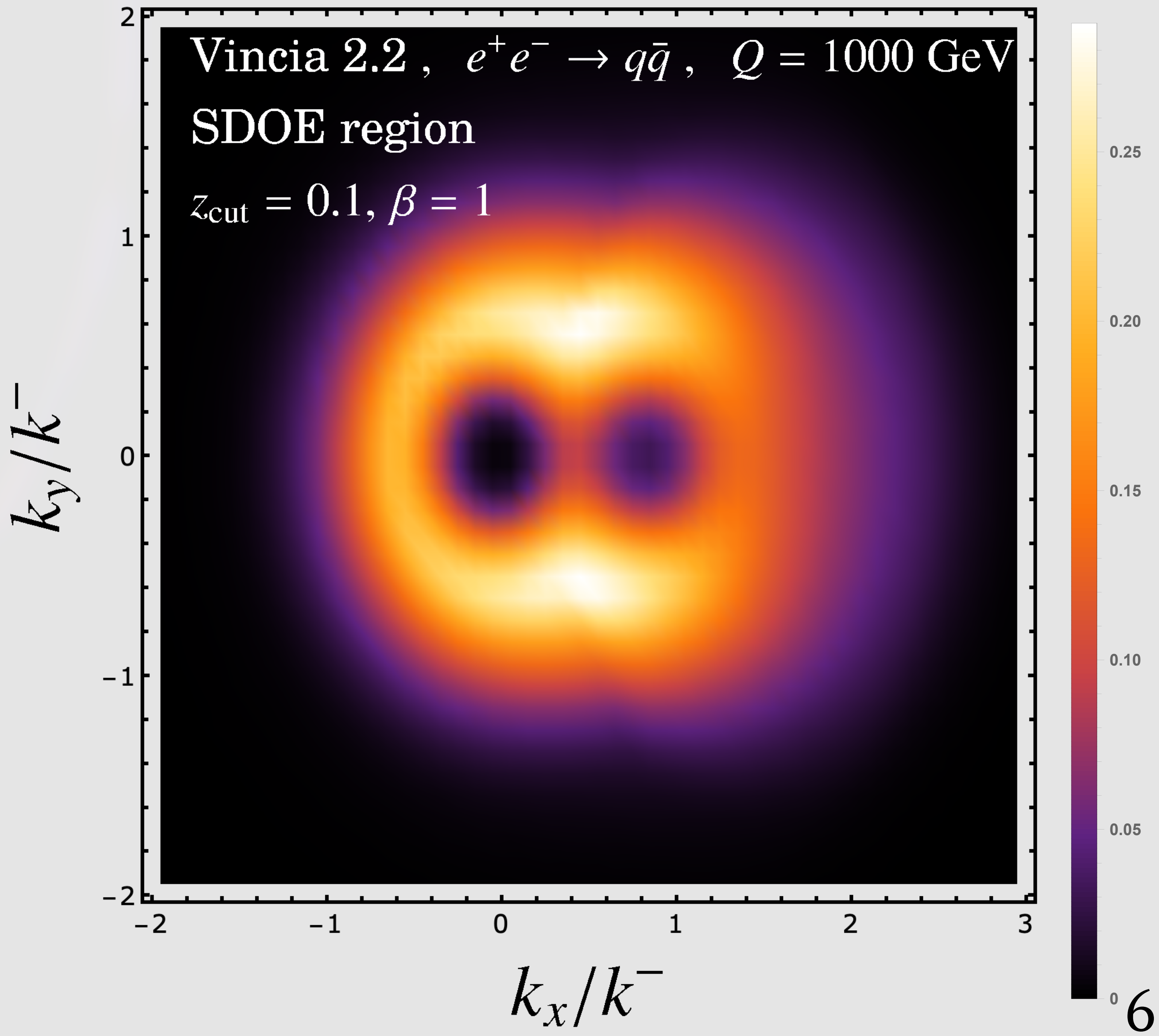




Hoang, AP, Mantry, Stewart 1906.11843; AP, Stewart, Vaidya, Zoppi 2012.15568

Factorization of NP corrections:

$$\frac{d\sigma_\kappa^{\text{had}}}{dm_J^2} = \frac{d\sigma_\kappa^{\text{part}}}{dm_J^2} - Q\,\Omega_{1\kappa}^{\circledcirc}\,\frac{d}{dm_J^2}\left(C_1^\kappa(m_J^2, Q, z_{\text{cut}}, \beta, R)\,\frac{d\hat{\sigma}_\kappa}{dm_J^2}\right) + \frac{Q\Upsilon_{1,0}^\kappa + \beta\Upsilon_{1,1}^\kappa}{m_J^2}\,C_2^\kappa(m_J^2, Q, z_{\text{cut}}, \beta, R)\,\frac{d\sigma_\kappa^{\text{part}}}{dm_J^2}$$

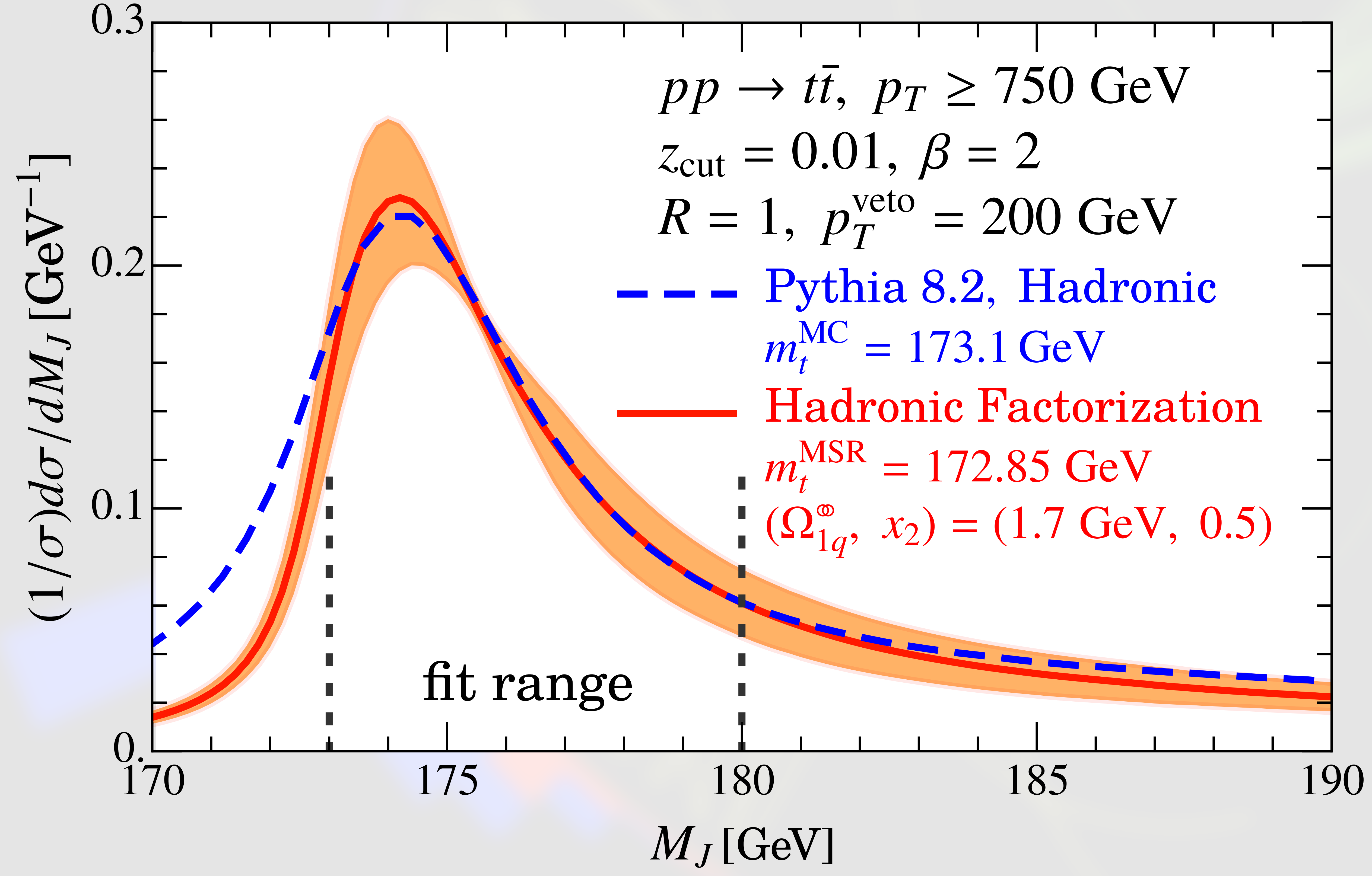


NP corrections governed by 3 universal constants

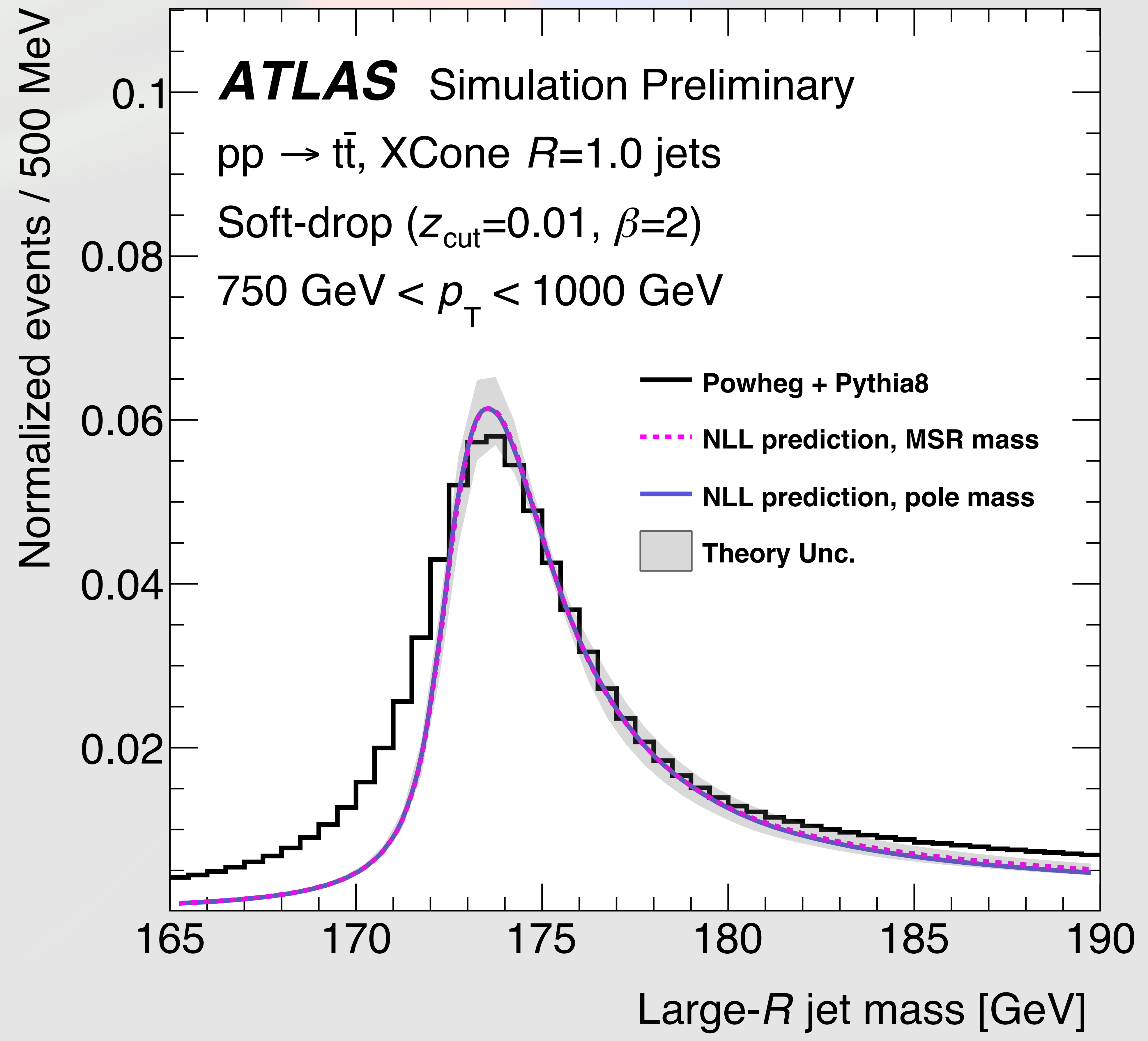
Calibration of Monte Carlo Top Mass

Comparing theory prediction with MC simulations enable m_t^{MC} calibration

Hoang, Mantry, AP, Stewart
1708.02586; Hoang, Mantry, Michel,
AP, Stewart (soon)



Hoang, Mantry, AP, Stewart and
ATLAS, ATL-PHYS-PUB-2021-034



Simultaneously fit for m_t and Ω_1°

Calibration of Monte Carlo Top Mass

Uncertainty breakdown:

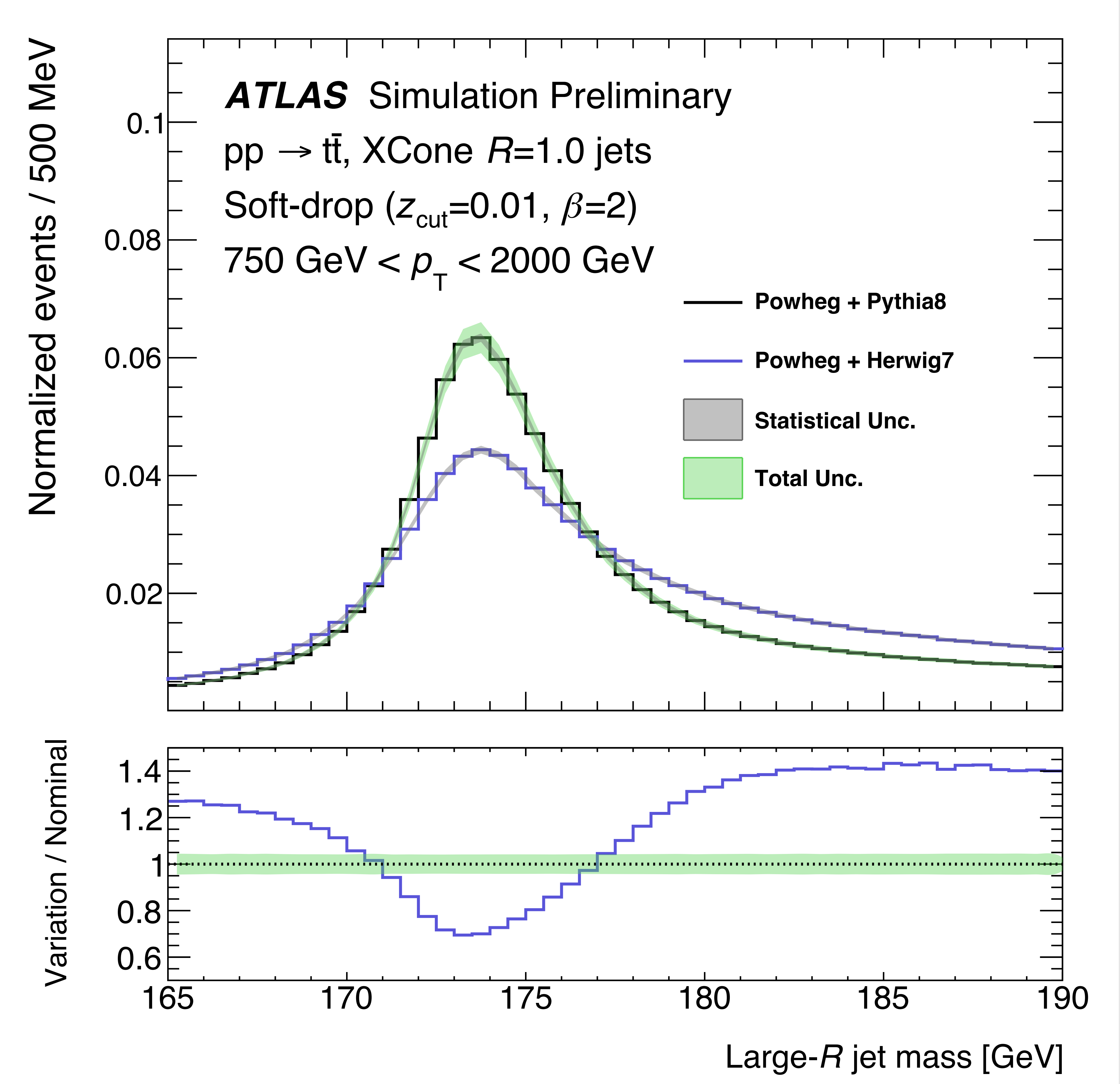
Source of Uncertainty	**size [MeV]**	**comment**
Theory	+ 230/-310	Envelope of NLL scale variations
Fit methodology	± 190	fit range, p_T bins
UE model	± 155	A14 eigentune variations, CR models
Observable definition	± 200	$z_{\mathrm{cut}} = 0.01, 0.005, 0.02,\ \beta = 1, 2,$ Anti-k$_t$ / XCone jets

$$m_t^{\mathrm{MSR,P8}}(R = 1\,\mathrm{GeV}) = 172.42 \pm 0.1\,\mathrm{GeV}$$

$$m_t^{\mathrm{MSR,H7}}(R = 1\mathrm{GeV}) = 172.27 \pm 0.09\,\mathrm{GeV}$$

$$\Omega_{1q}^{\infty,\,\mathrm{P8}} = 1.49 \pm 0.03\,\mathrm{GeV}\,, \qquad x_2^{\mathrm{P8}} = 0.52 \pm 0.09$$

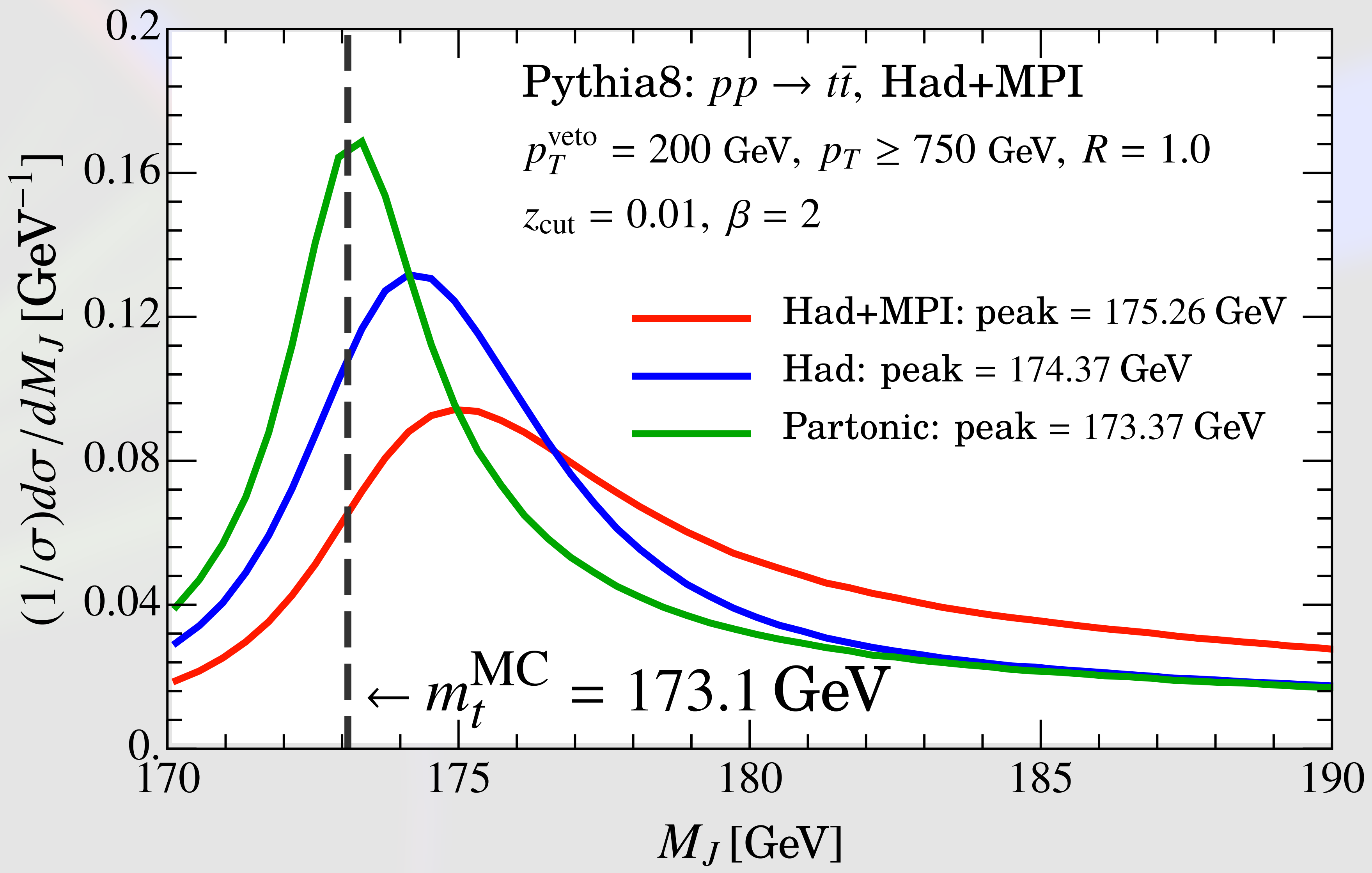
$$\Omega_{1q}^{\infty,\mathrm{H7}} = 1.9 \pm 0.07\,\mathrm{GeV}\,, \qquad x_2^{\mathrm{H7}} = 0.98 \pm 0.12$$



Calibration for Herwig consistent with Pythia despite very different shapes

Lessons learned

$$M_{J,\mathrm{sd}}^2 = \Big(\sum_{i\in J^{\mathrm{groomed}}} p_i^\mu\Big)^2 \simeq m_t^2 + \Gamma_t m_t + \ldots$$



1. Successful Hadron level calibration but challenges ahead: Describing Underlying Event will require additional parameters

Ferdinand, Lee, AP (in progress)

2. Need hadronization models for anything more complicated than soft drop jet mass with no systematic method to assess the uncertainties.