

SCET Workshop

2022

22 April, 2022

# Radiative corrections to charged-current neutrino scattering at GeV energies

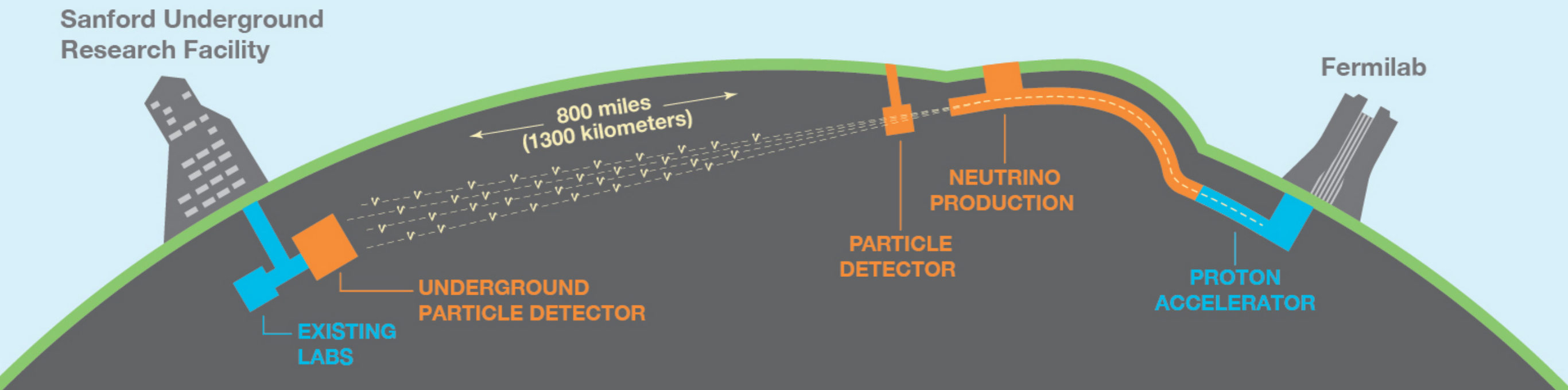


Oleksandr (Sasha) Tomalak

LA-UR-22-23396

# Neutrino experiments

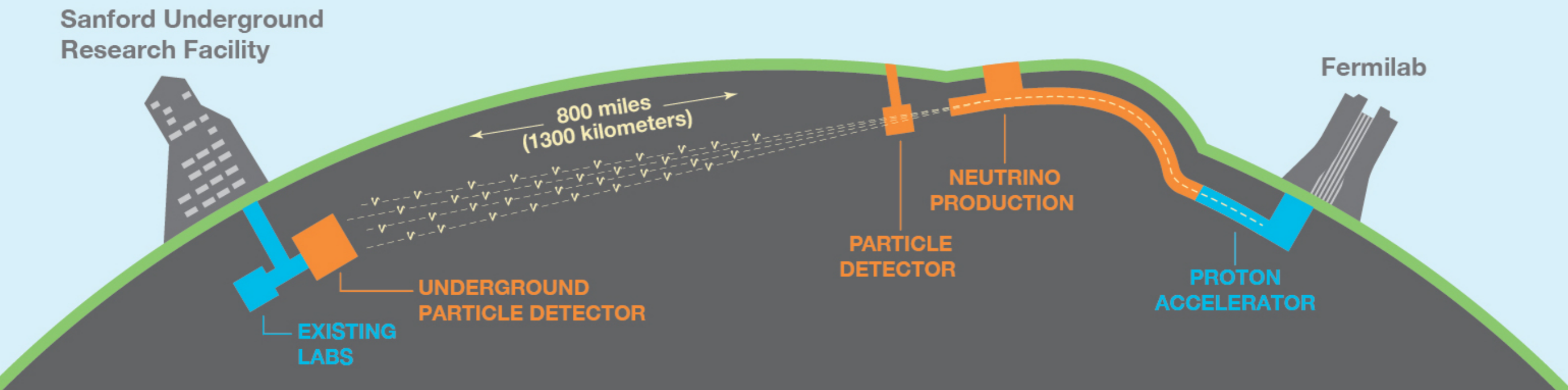
- **DUNE** and Hyper-K: leading-edge  $\nu$  science experiments



- origin of matter-antimatter asymmetry  $\delta_{CP}$
- mass hierarchy and oscillation parameters PMNS matrix,  $\Delta m_{31}^2$
- Grand Unified Theories proton decay
- dynamics of supernova explosion wait for one;)

# Neutrino experiments

- **DUNE** and Hyper-K: leading-edge  $\nu$  science experiments



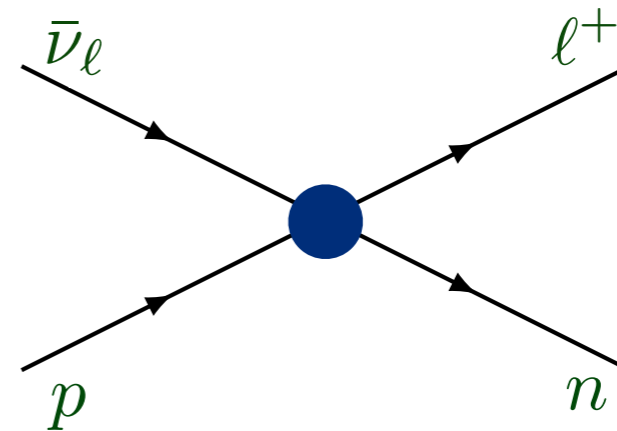
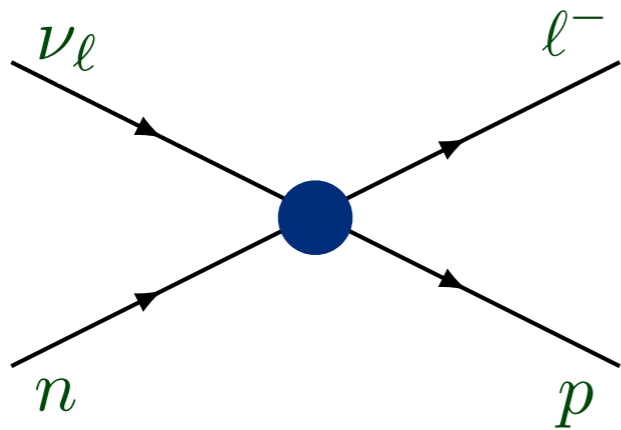
- measurement of  $\nu_\mu$  disappearance and  $\nu_e$  appearance

$$N_\nu \sim \int dE_\nu \Phi_\nu (E_\nu) \times \sigma (E_\nu) \times R (E_\nu, E_\nu^{\text{rec}})$$

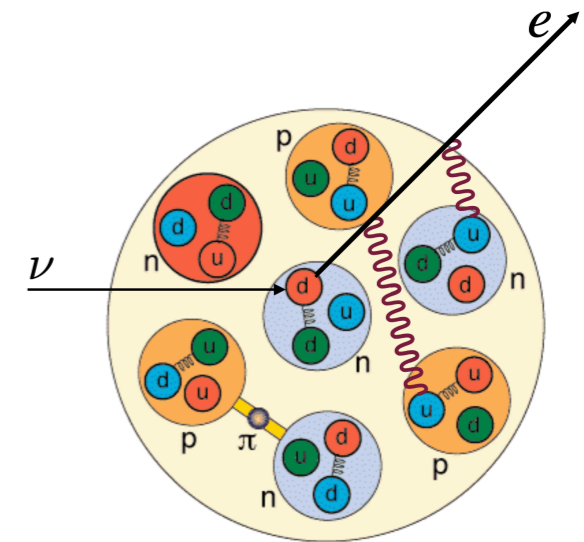
- near detector: determine flux and cross sections

# Outline

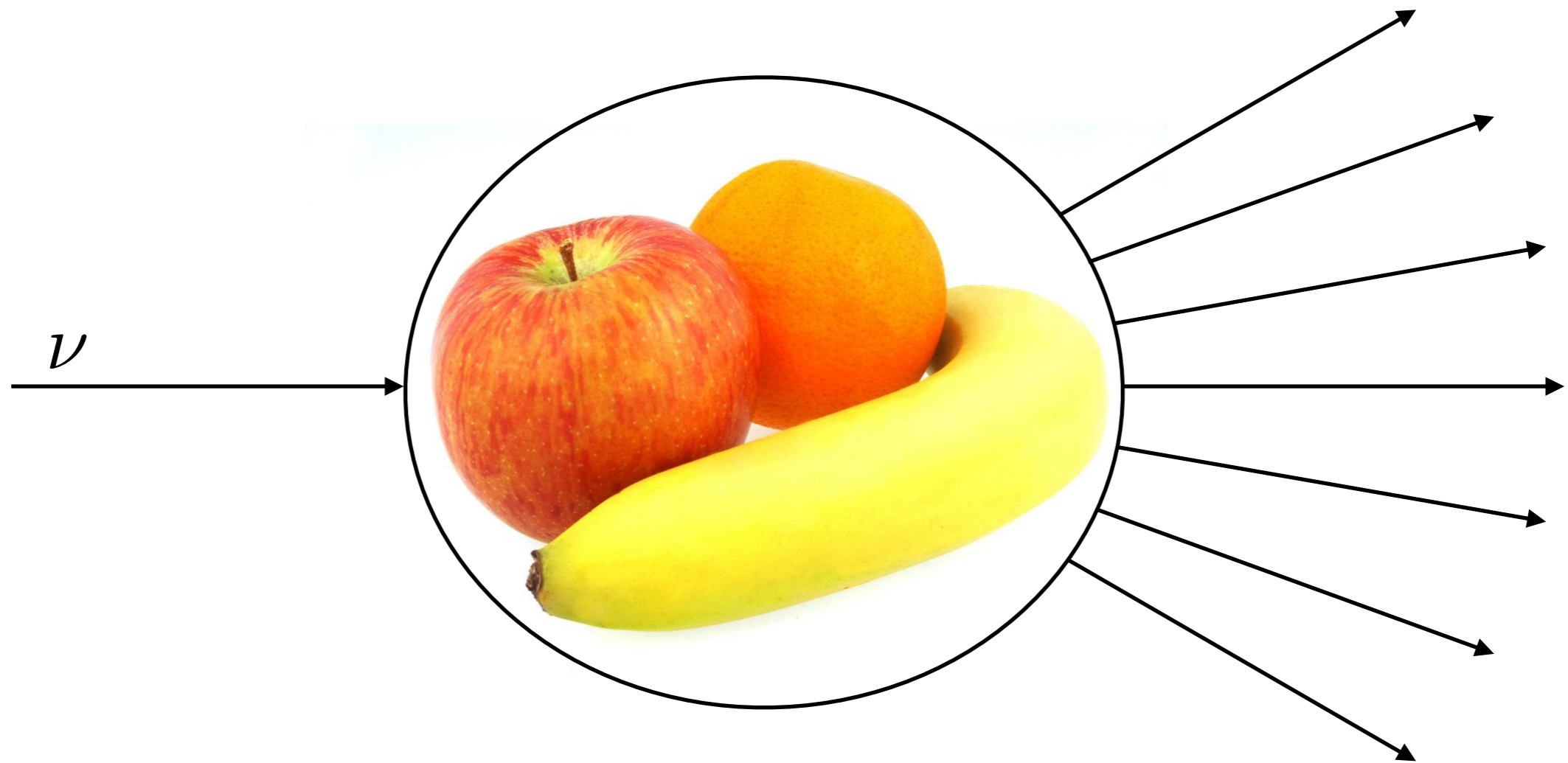
## 1) charged-current elastic scattering on nucleons



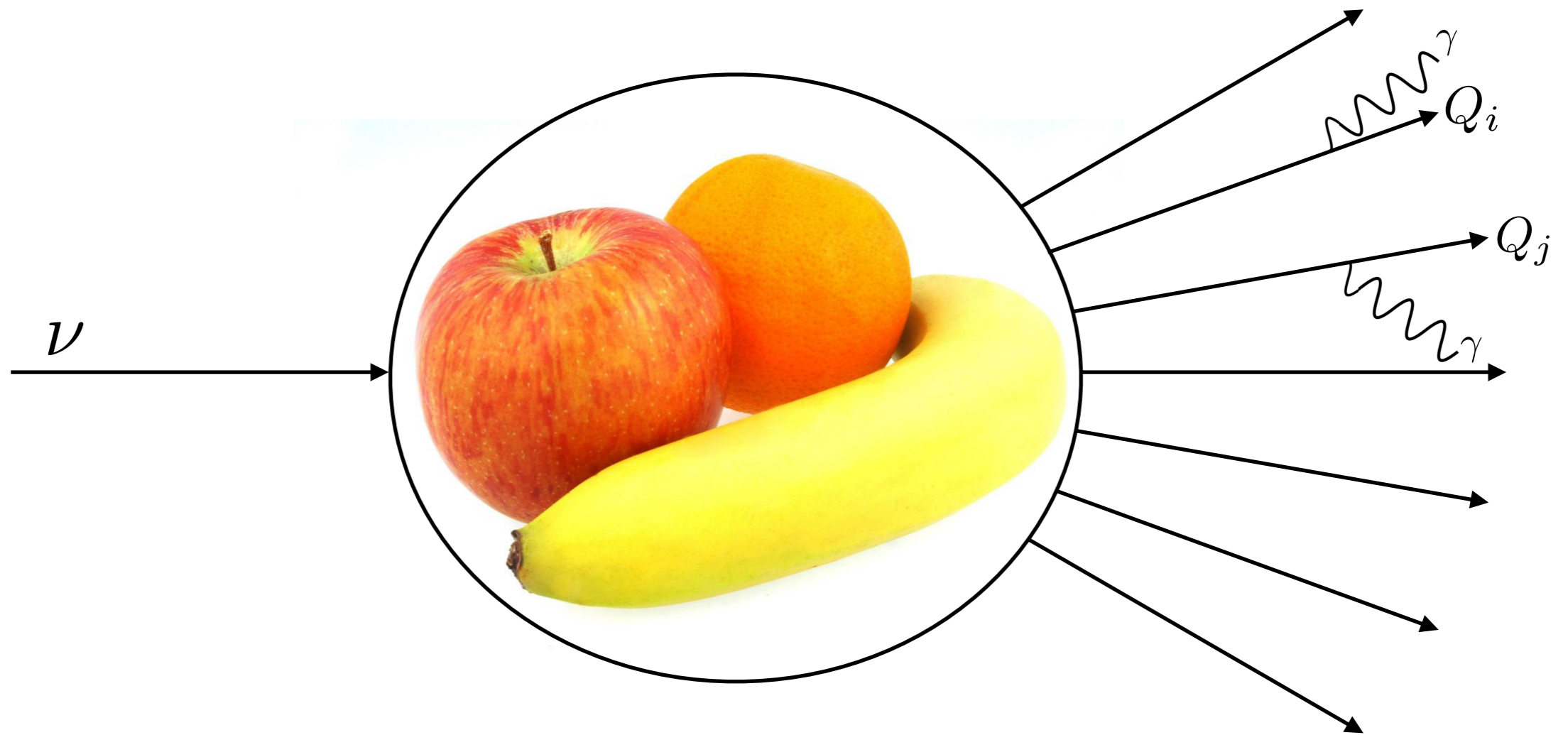
## 2) QED nuclear medium effects in (anti)neutrino-nucleus and electron-nucleus scattering



# Neutrino interactions

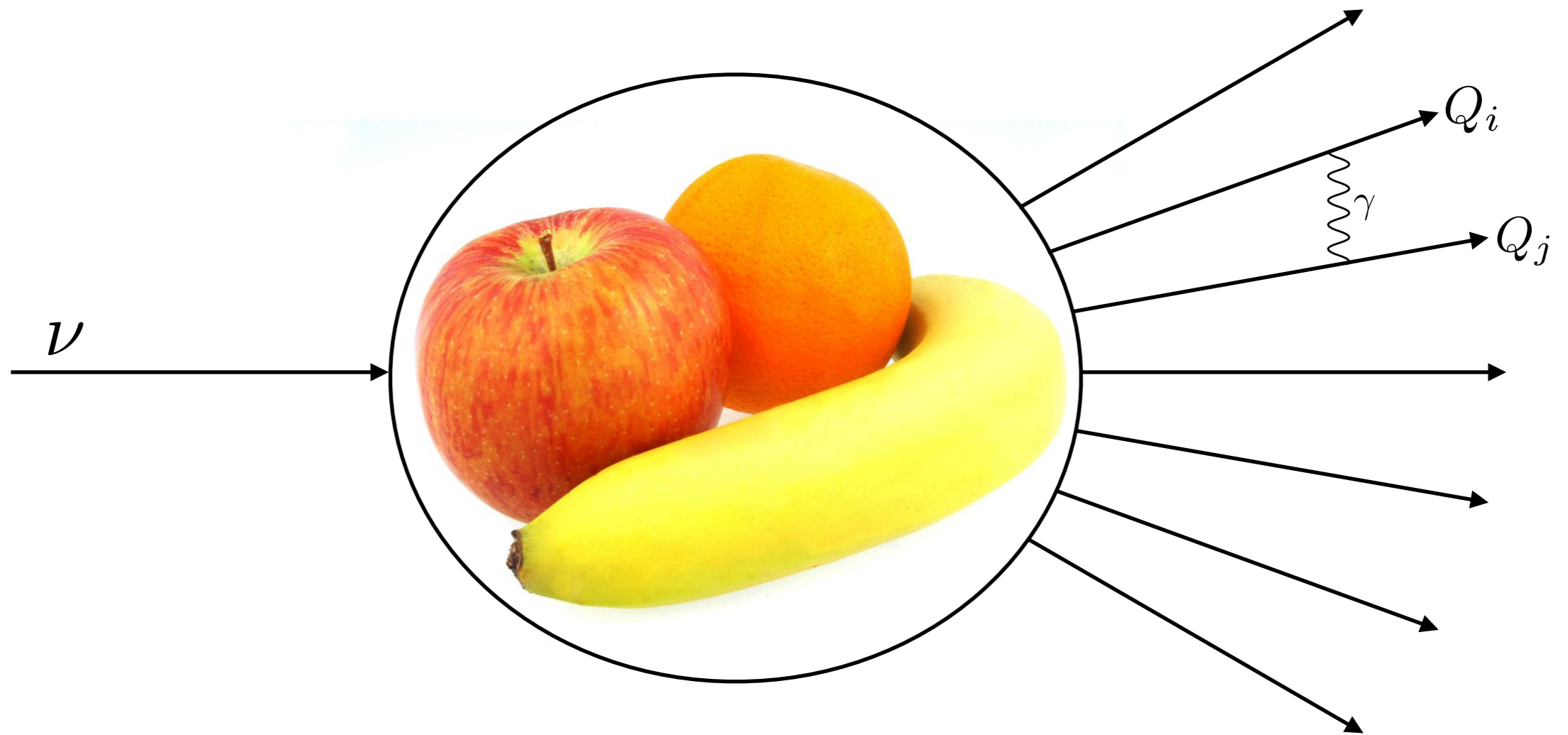


# QED corrections



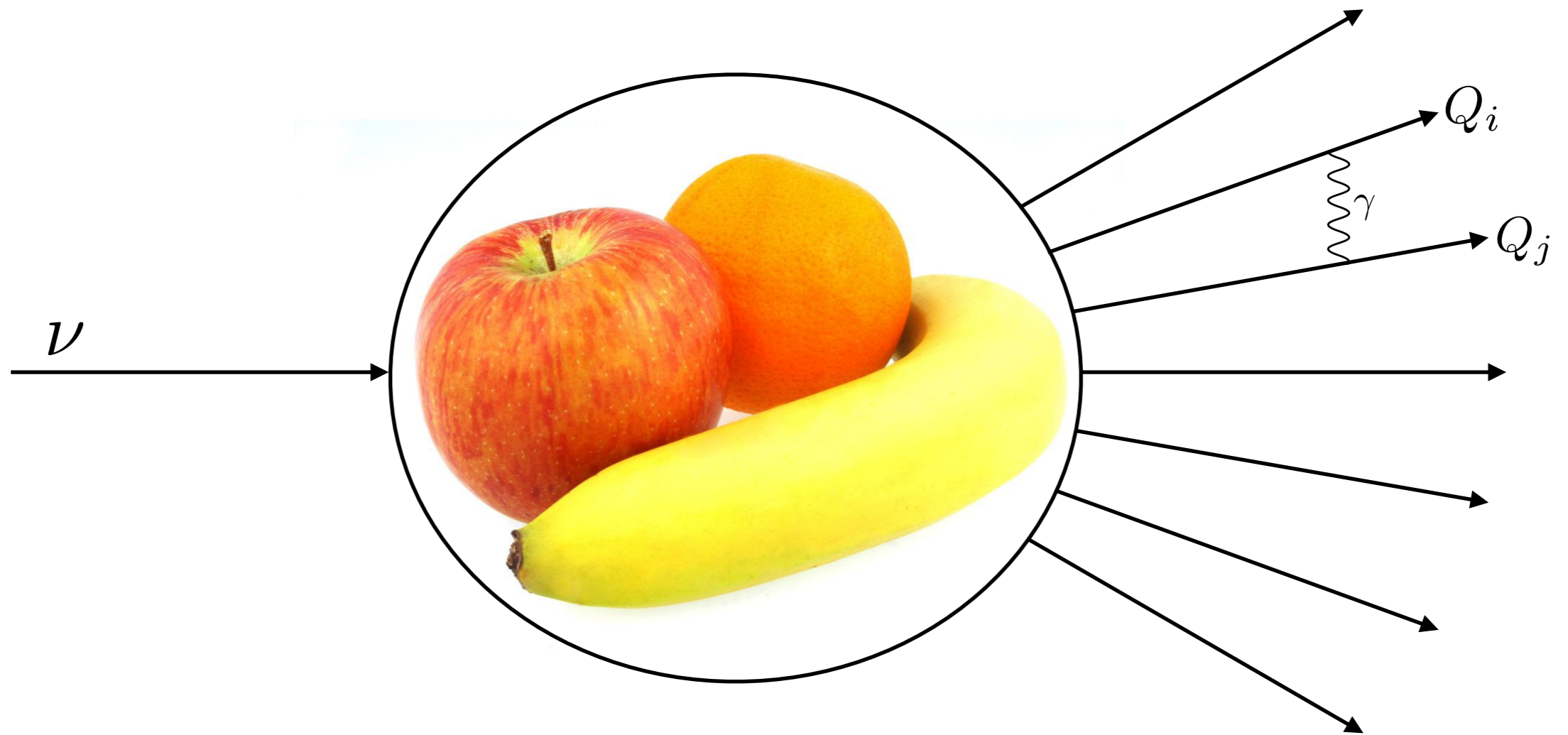
- all charged particles couple to real and virtual photons

# QED corrections



- all charged particles couple to real and virtual photons

# QED corrections

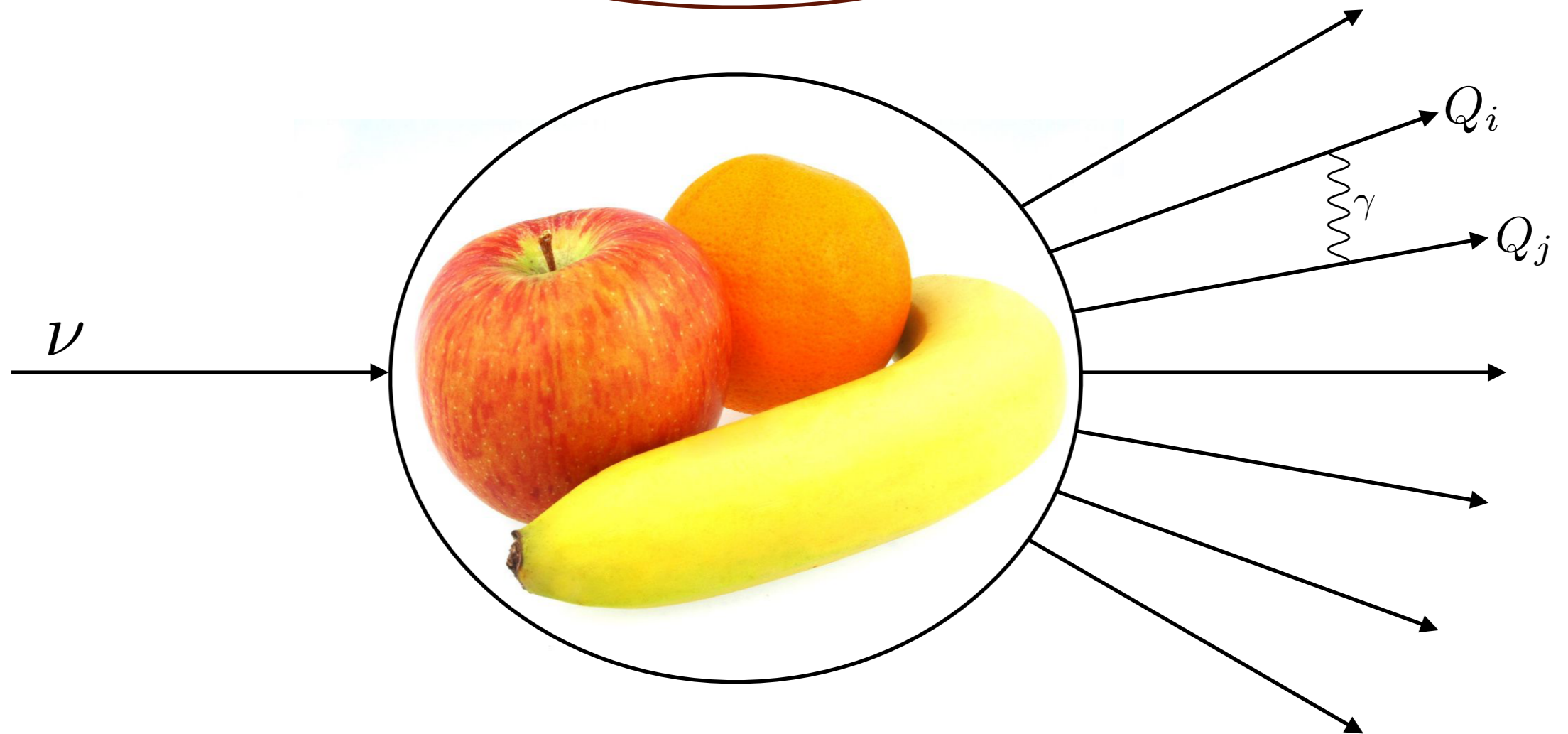


-  $\frac{\alpha}{\pi} \sim 0.2\%$  suppression by electromagnetic coupling constant



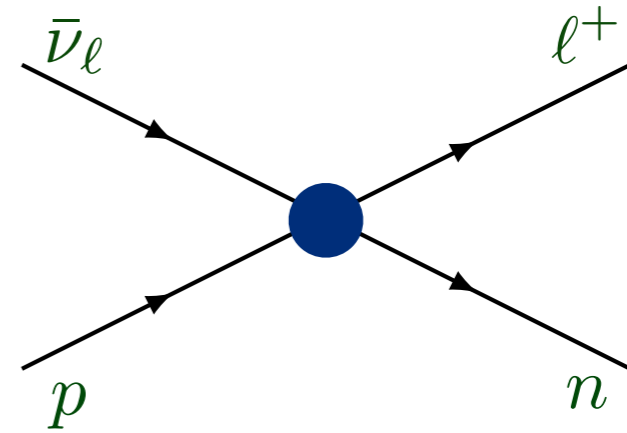
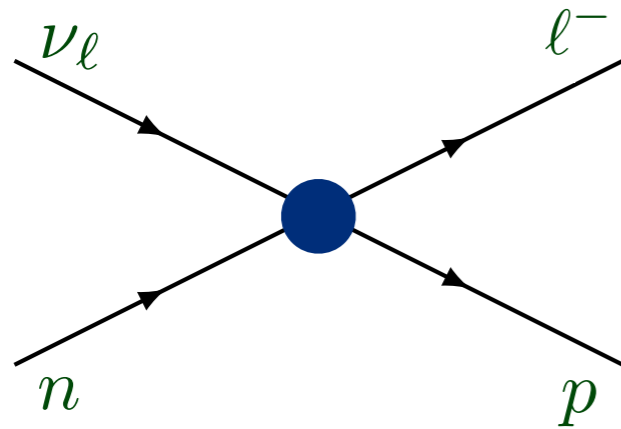
# QED corrections

$$m_e \ll m_\mu \ll E_\nu$$



$$\frac{\alpha}{\pi} \sim 0.2 \% \text{ multiplied by } \ln \frac{E_\nu}{m_e} \sim 6 - 10 \text{ or } \ln^2 \frac{E_\nu}{m_e} \sim 36 - 100$$

- scale separation introduces large flavor-dependent QED logarithms



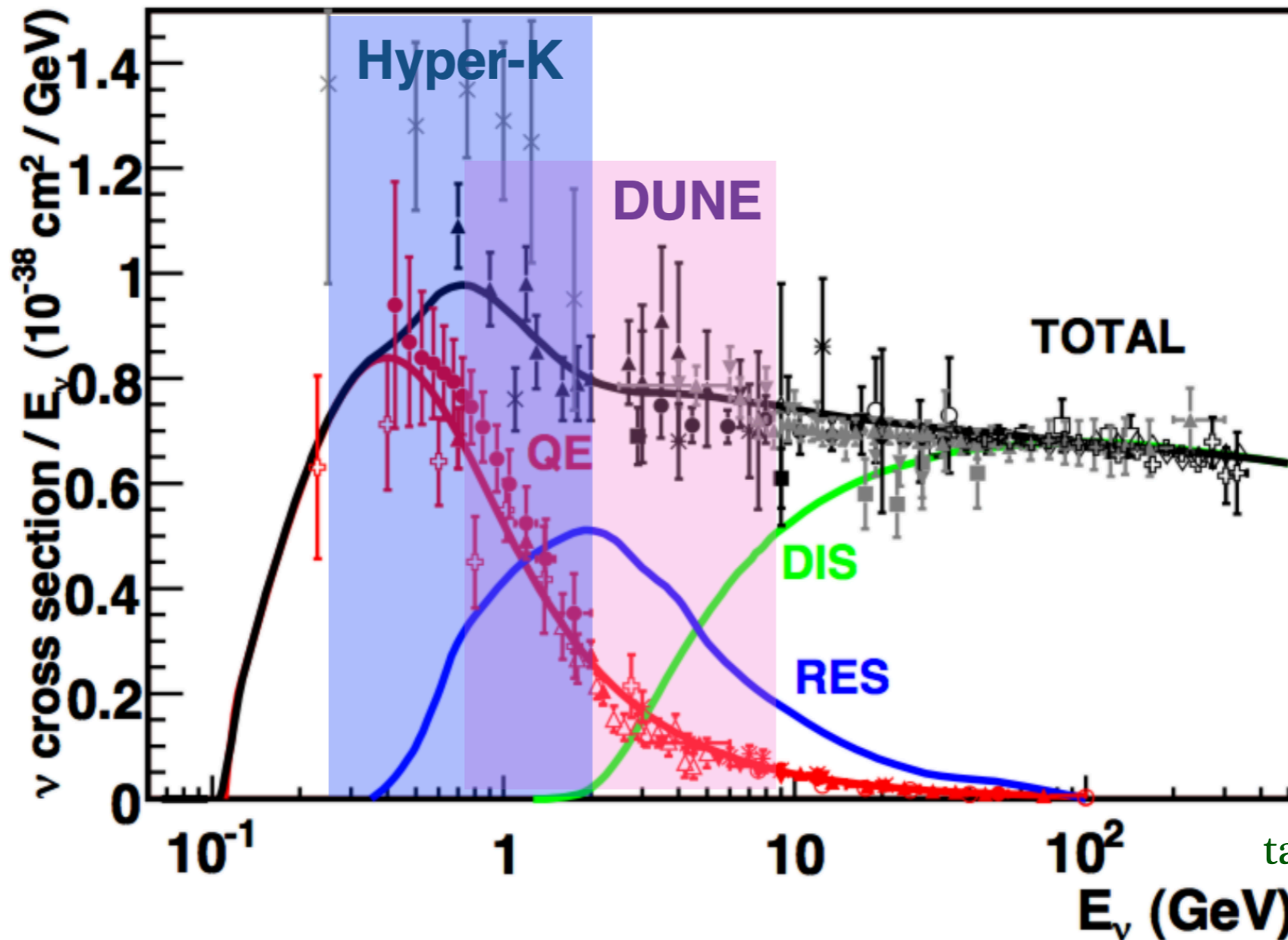
# Radiative corrections in charged-current elastic scattering on free nucleons

O. T., Qing Chen, Richard J. Hill and Kevin S. McFarland, arXiv: 2105.07939

O. T., Qing Chen, Richard J. Hill, Kevin S. McFarland and Clarence Wret (arXiv: to appear)

# CCQE. Why should we care?

- neutrino-nucleus cross sections and future accelerator-based fluxes

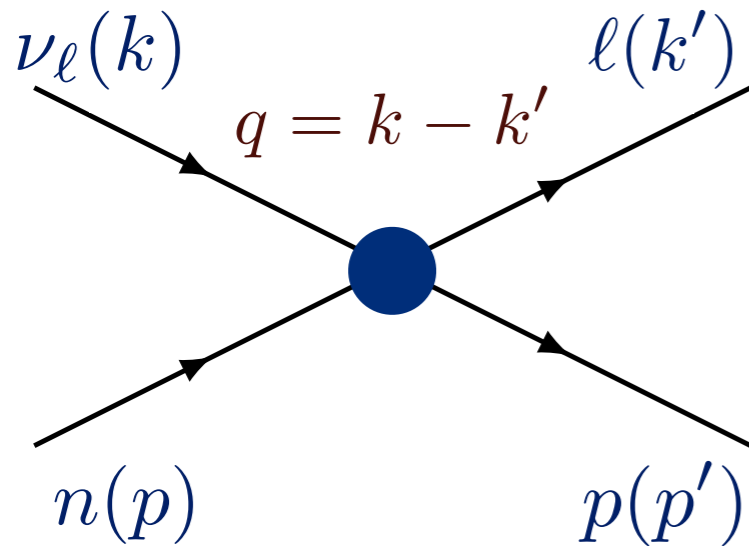


Formaggio  
and Zeller  
(2013)

Noemi Rocco  
talk at Neutrino 2020

- basic process: bulk of events at Hyper-K and DUNE
- channel for reconstruction of neutrino energy

# CCQE scattering on free nucleon



neutrino energy

$$E_\nu$$

momentum transfer

$$Q^2 = -q^2$$

contact interaction at GeV energies

- assuming isospin symmetry, nucleon current:

$$\Gamma^\mu(Q^2) = \langle p | \bar{u} (\gamma^\mu - \gamma^\mu \gamma_5) d | n \rangle$$

$$\Gamma^\mu(Q^2) = \gamma^\mu F_D^V(Q^2) + \frac{i\sigma^{\mu\nu} q_\nu}{2M} F_P^V(Q^2) + \gamma^\mu \gamma_5 F_A(Q^2) + \frac{q^\mu}{M} \gamma_5 F_P(Q^2)$$

form factors: isovector Dirac and Pauli      axial and pseudoscalar

$$F_{D,P}^V = F_{D,P}^p - F_{D,P}^n$$

tree-level amplitude

$$T = \frac{G_F V_{ud}}{\sqrt{2}} (\bar{\ell}(k') \gamma_\mu (1 - \gamma_5) \nu_\ell(k)) (\bar{p}(p') \Gamma^\mu(Q^2) n(p))$$

# Elastic scattering on free nucleon

- only 3 experiments performed with deuterium bubble chamber
- direct access to form-factor shape

ANL 1982: 1737 events

BNL 1981: 1138 events

FNAL 1983: 362 events

world data: ~3200 events



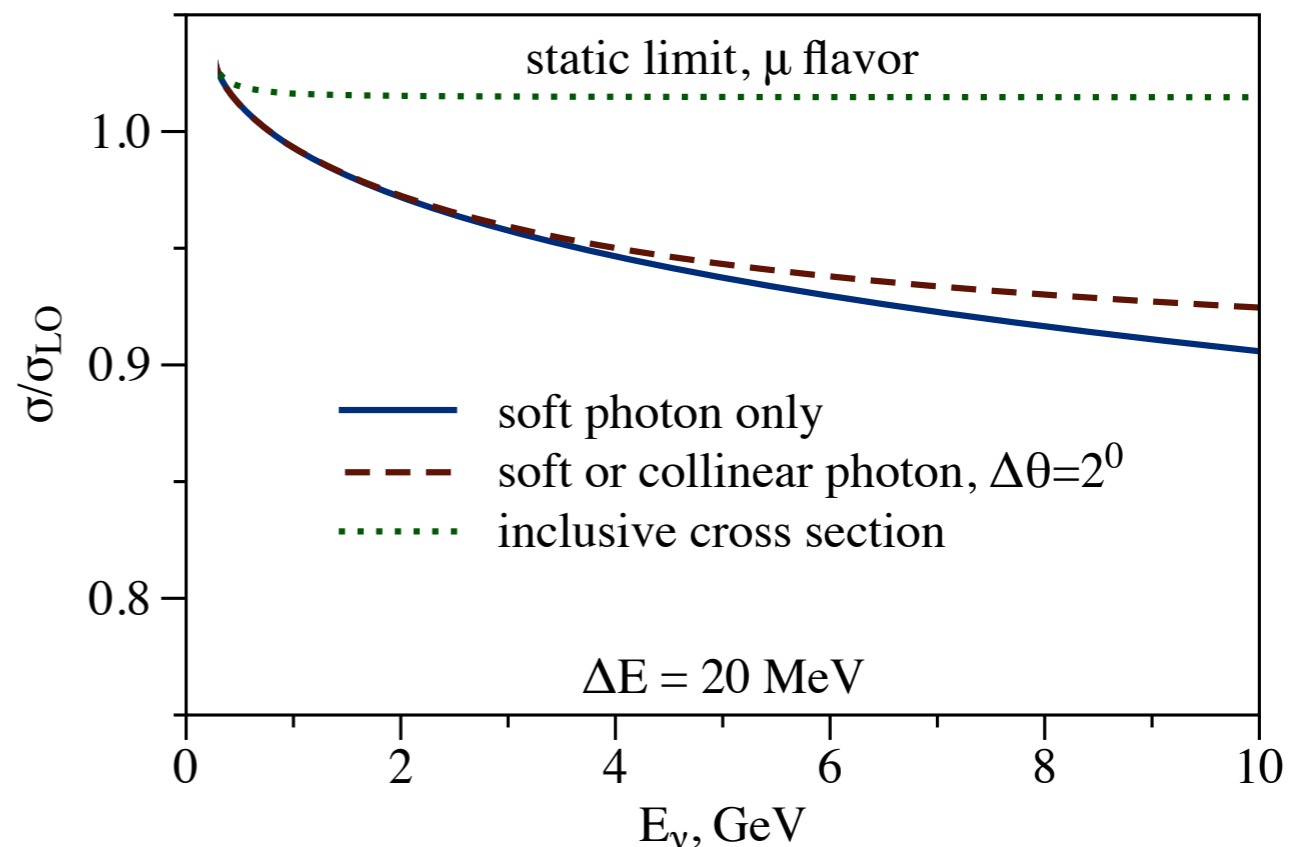
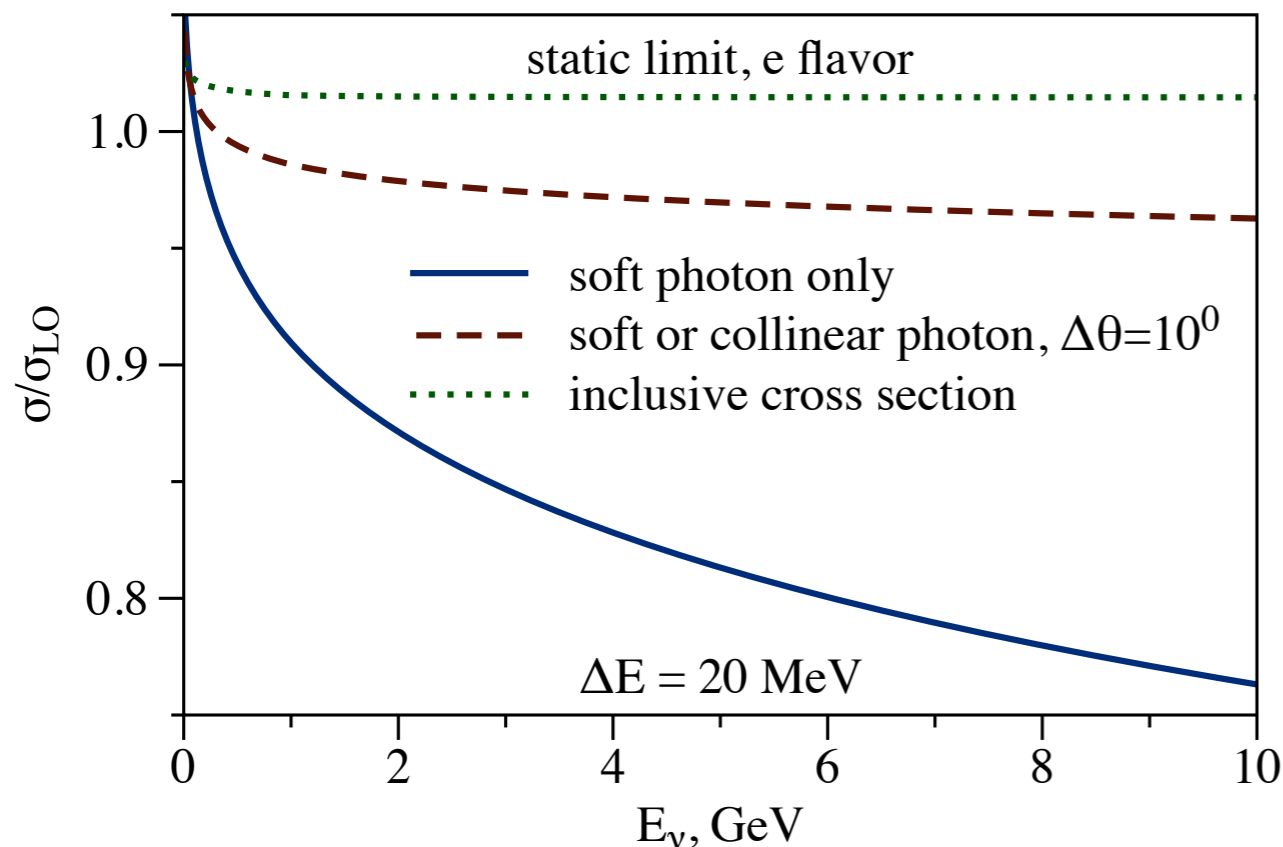
Fermilab bubble chamber, Richard Drew

- axial form factor extracted based on electromagnetic structure

A.S. Meyer, M. Betancourt, R. Gran and R.J. Hill (2016)

# Static nucleon limit

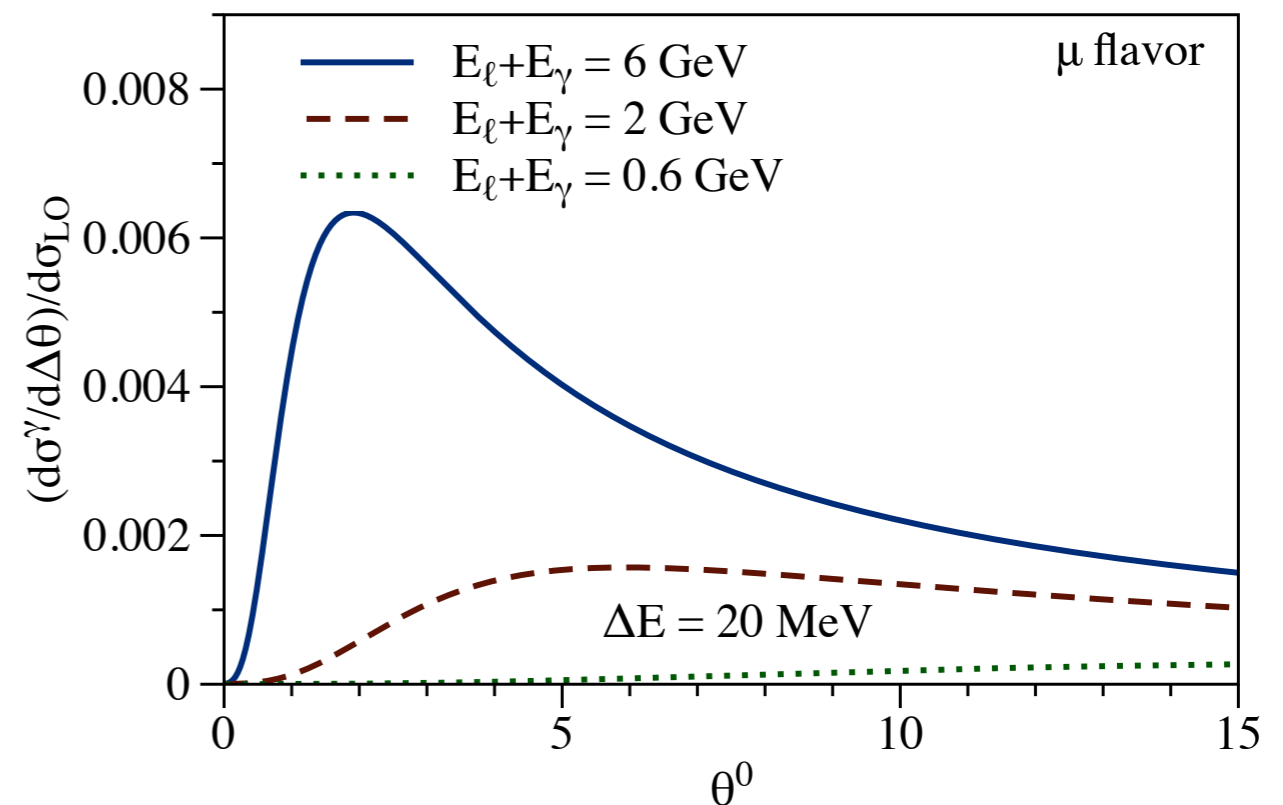
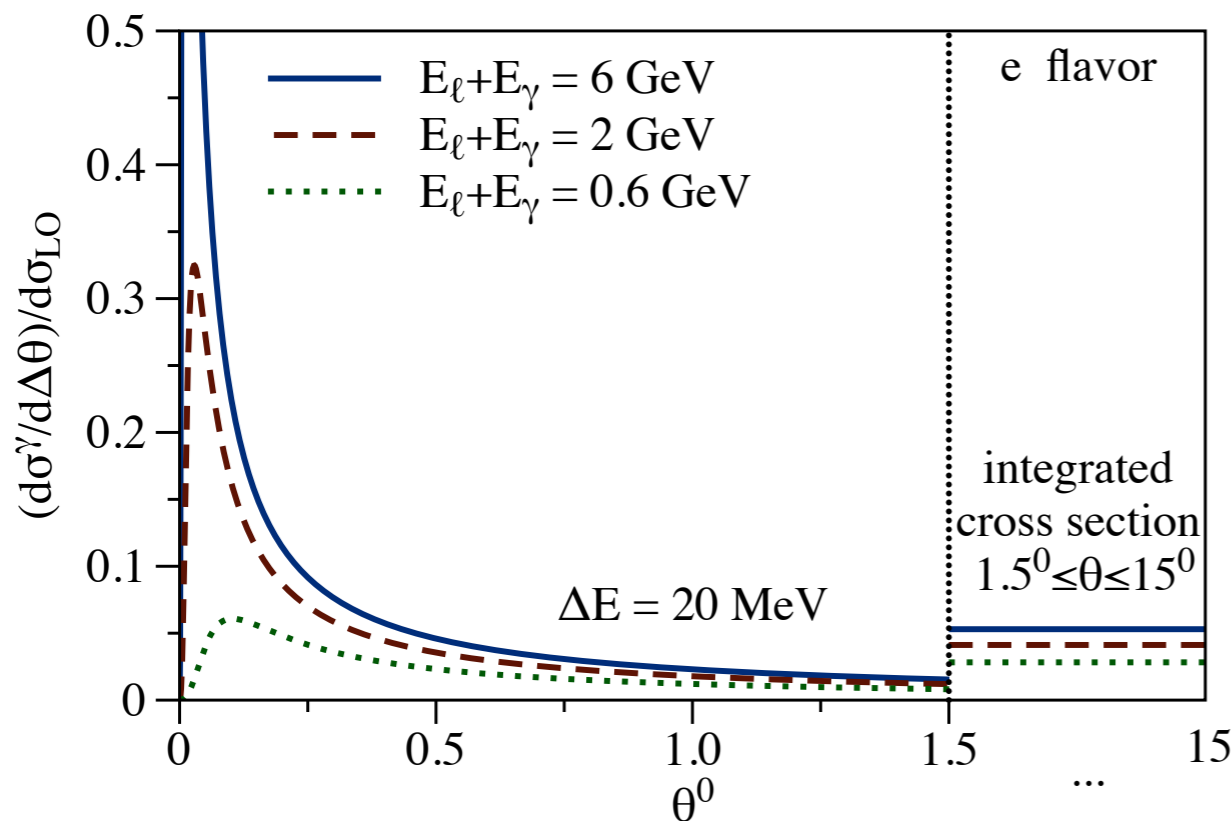
- formal limit of infinitely heavy nucleus  $m_\ell \ll E_\ell \ll M$
- provides correct soft and collinear logarithms
- soft-photon energy  $< 20$  MeV, jet size:  $10^\circ$  for electron and  $2^\circ$  for muon



- flavor-dependent effect, same for  $\nu_\ell n \rightarrow \ell^- p$  vs  $\bar{\nu}_\ell p \rightarrow \ell^+ n$
- collinear observable: cancellation of virtual vs real logs
- inclusive observables (+ $\gamma$ ): few % level, flavor independent

# Electron vs muon jets

- factorization for radiation of collinear photons
- cone angle is defined to lepton direction
- photons of energy  $> 20$  MeV, fixed energy in the cone



- flavor-dependent effect, same for  $\nu_\ell n \rightarrow \ell^- p$  vs  $\bar{\nu}_\ell p \rightarrow \ell^+ n$
- forward-peaked radiation for electron flavor
- negligible radiation for muons with shifted peak position

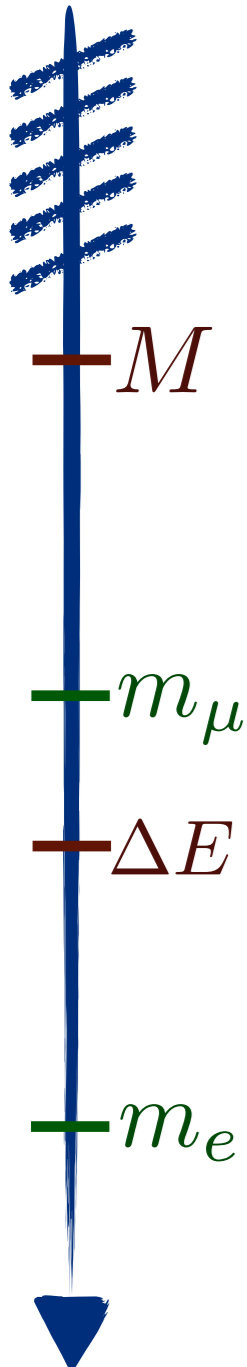
# Factorization approach

- cross section is given by **factorization formula**

$$d\sigma \sim S \left( \frac{\Delta E}{\mu} \right) J \left( \frac{m_\ell}{\mu} \right) H \left( \frac{M}{\mu} \right)$$

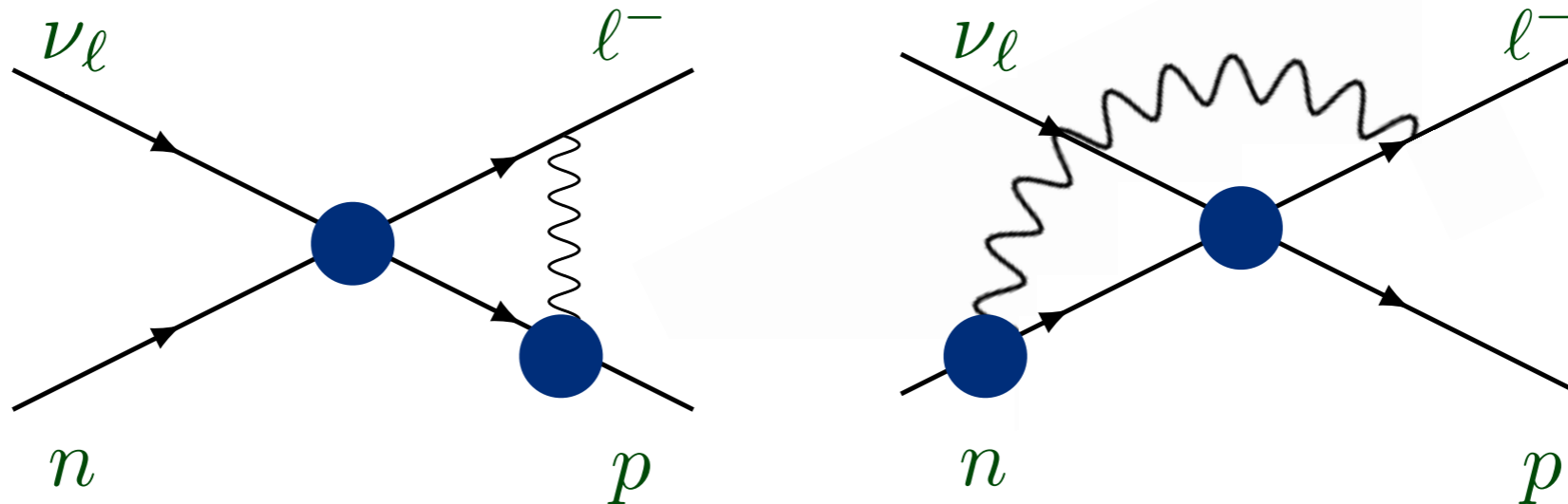
- determine **hard function** at hard scale by matching experiment or hadronic model to the theory with heavy nucleon

- soft and collinear functions are evaluated **perturbatively**





# Hadronic model at GeV scale



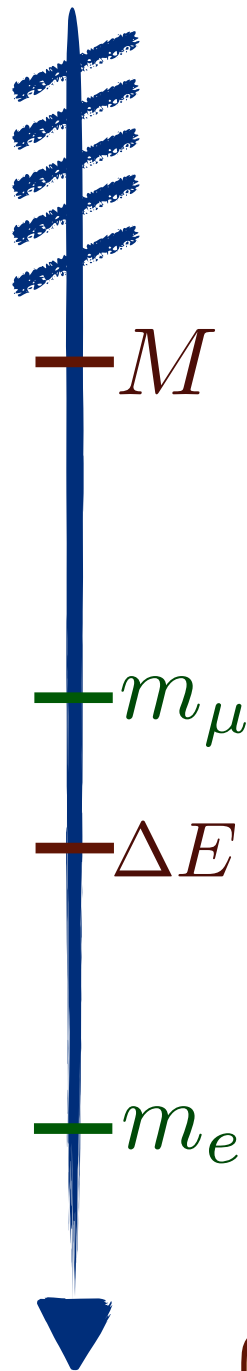
- exchange of photon between the charged lepton and nucleons
- assume **onshell form** for each interaction with dipole form factors  
discussed for neutrino-nucleon scattering: Graczyk (2013)
- add **self energy** for charged particles
- reproduce soft and collinear regions of SCET

- best determination of hard function

# Factorization approach

- cross section is given by **factorization formula**

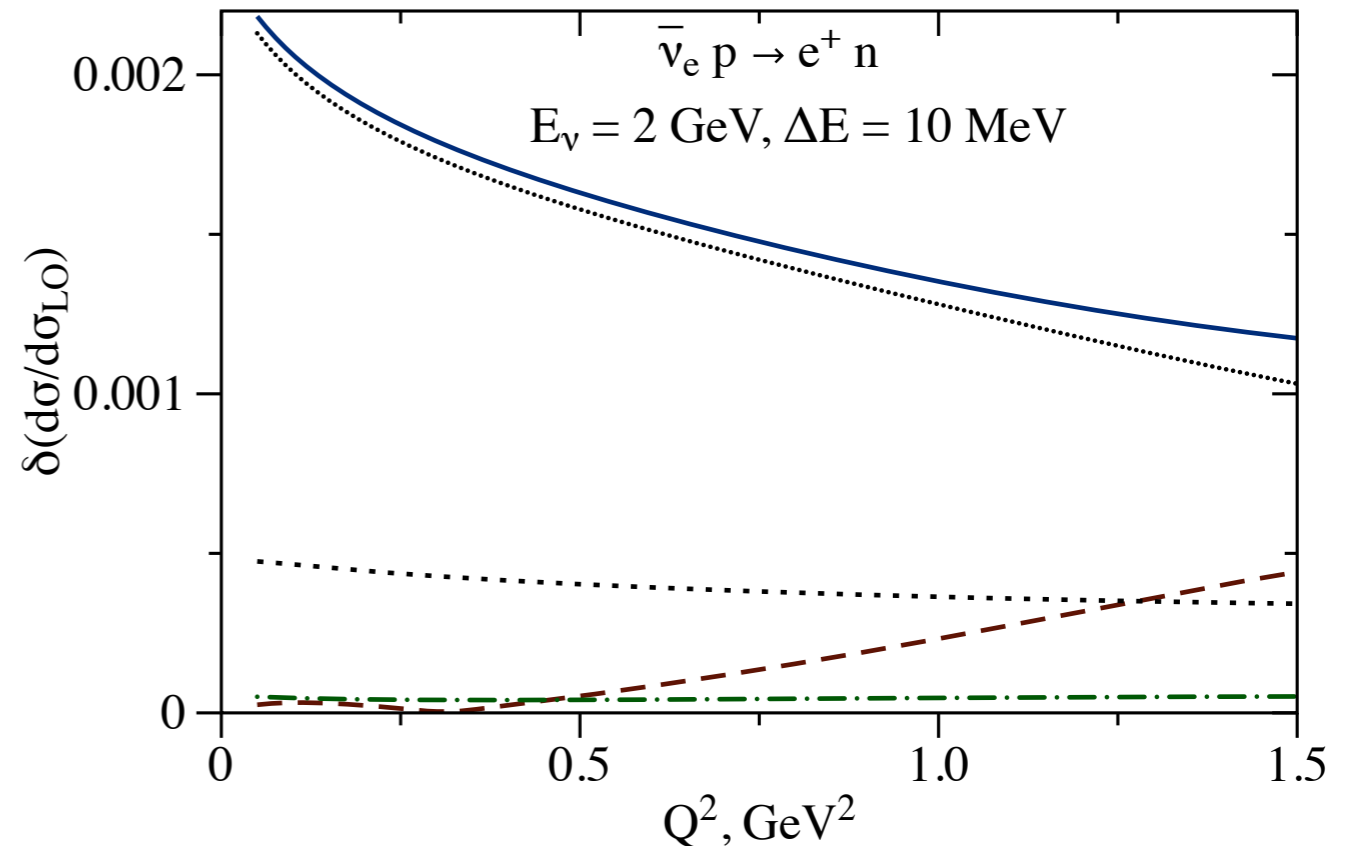
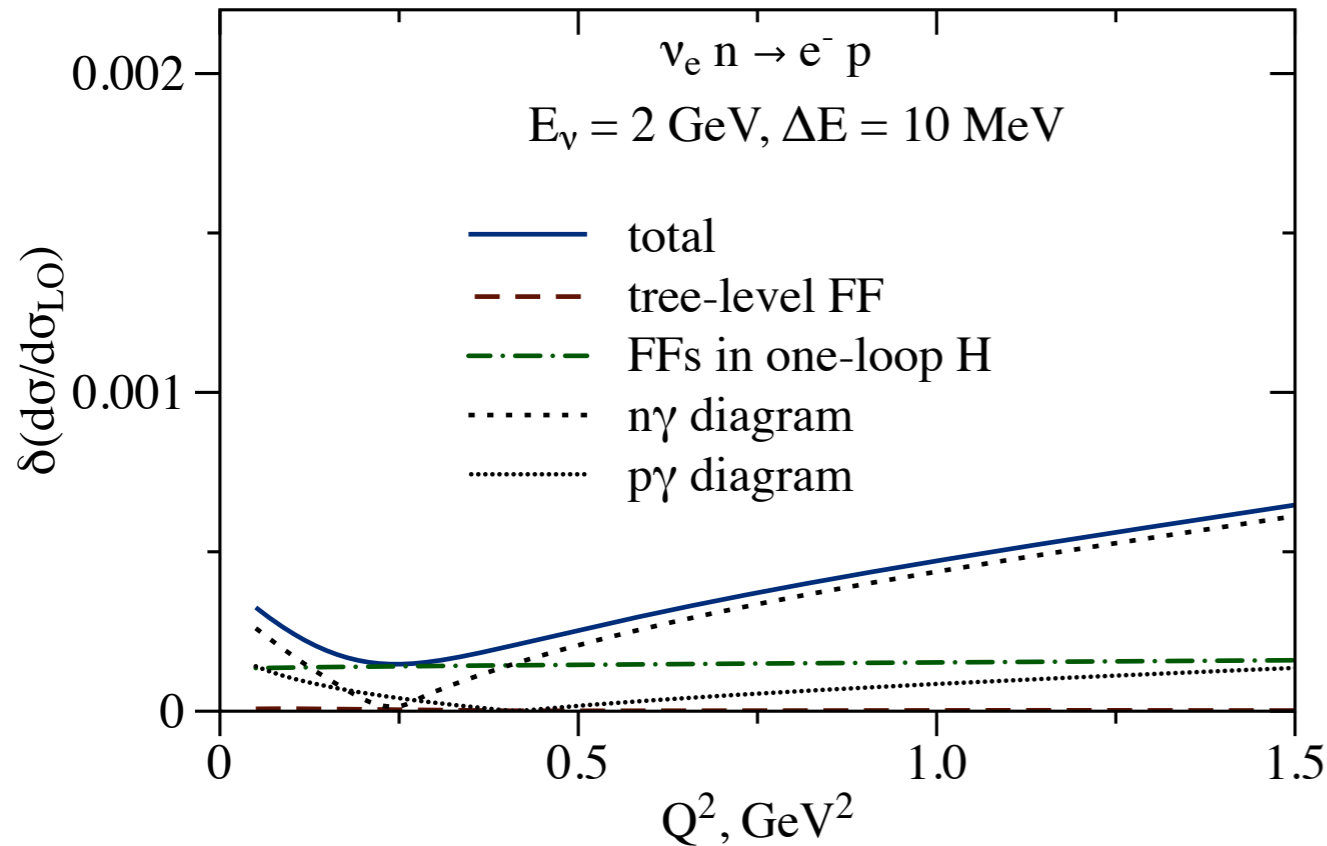
$$d\sigma \sim S \left( \frac{\Delta E}{\mu} \right) J \left( \frac{m_\ell}{\mu} \right) H \left( \frac{M}{\mu} \right)$$

- 
- determine **hard function** at hard scale by matching experiment or **hadronic model** to the theory with heavy nucleon
  - **RGE evolution** of the hard function to scales  $\Delta E, m_\ell$
  - **soft and collinear functions** are evaluated **perturbatively**
  - calculate cross section at low energies accounting for **all large logs**  
ep scattering with soft radiation only: Richard J. Hill (2016)

- **soft and collinear functions** determined **analytically**
- **hard function** describes physics at GeV energies

# Error budget

- uncertainties from hard function



Meyer, Betancourt, Gran and Hill (2016)

- nucleon form factors

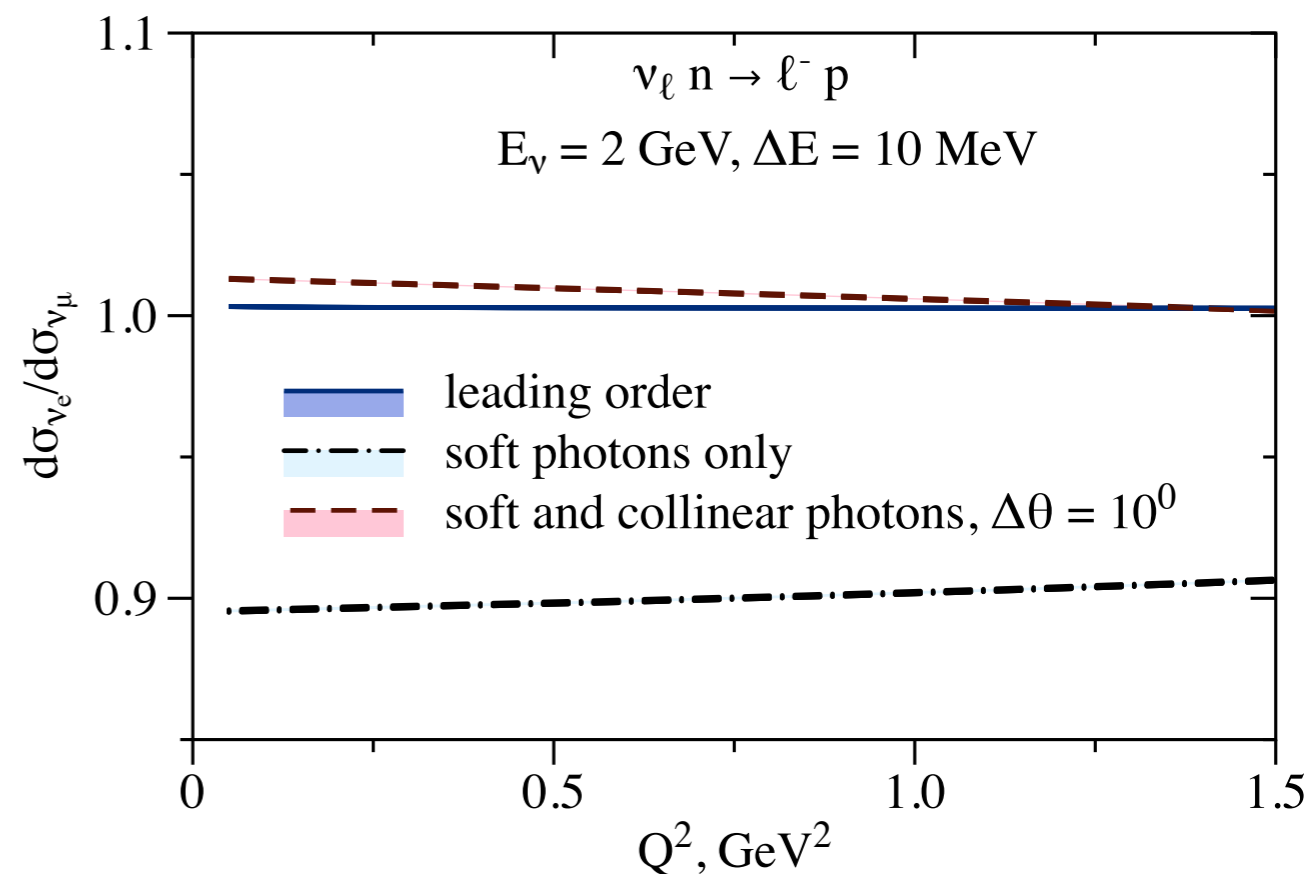
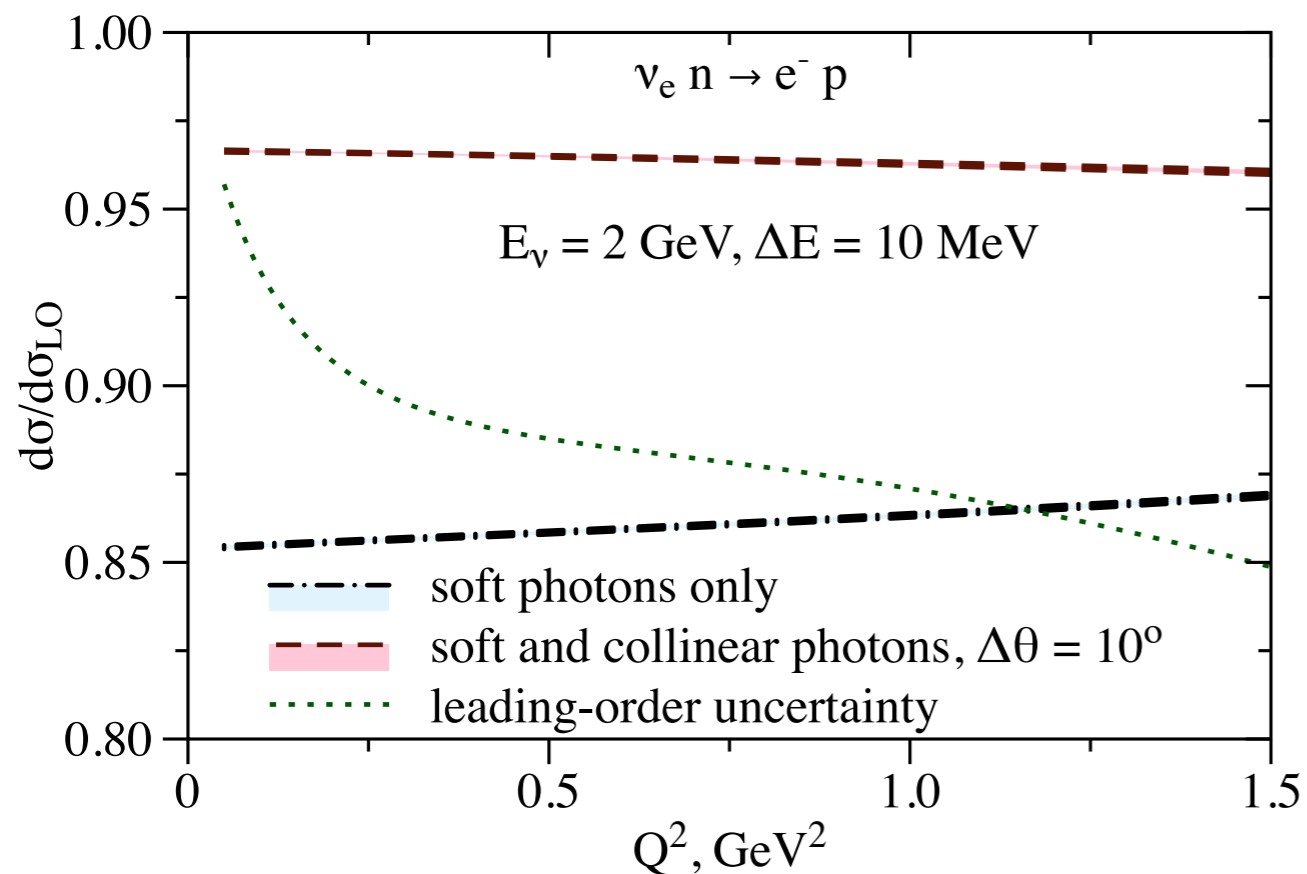
Kaushik Borah, Gabriel Lee, Richard J. Hill and O.T. (2020)

- add perturbative uncertainty by variation of scale

- uncertainty of permille level for the ratio to LO result

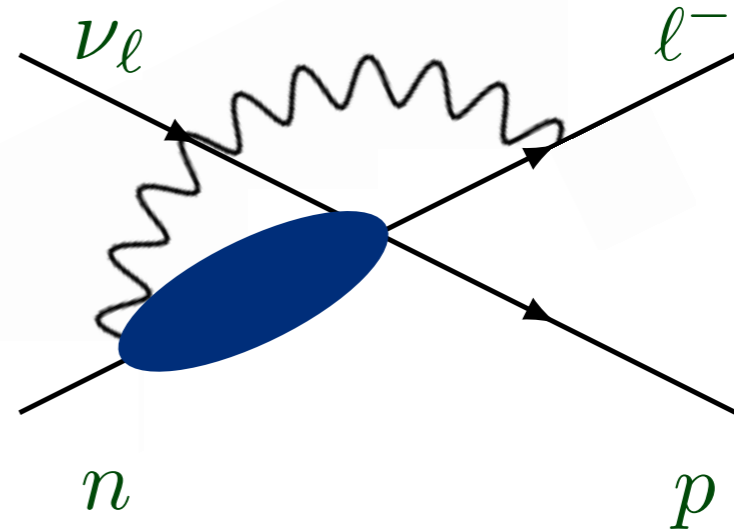
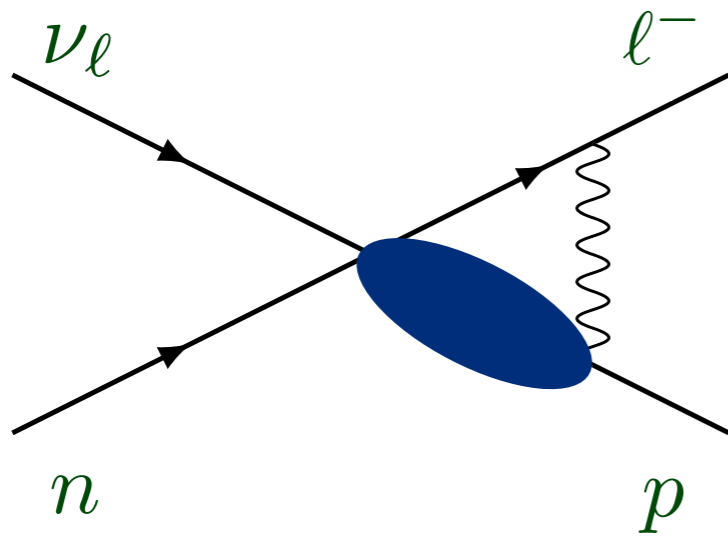
# Exclusive observables

- cancellation of uncertainties from hard function for  $e/\mu$  and ratio to LO

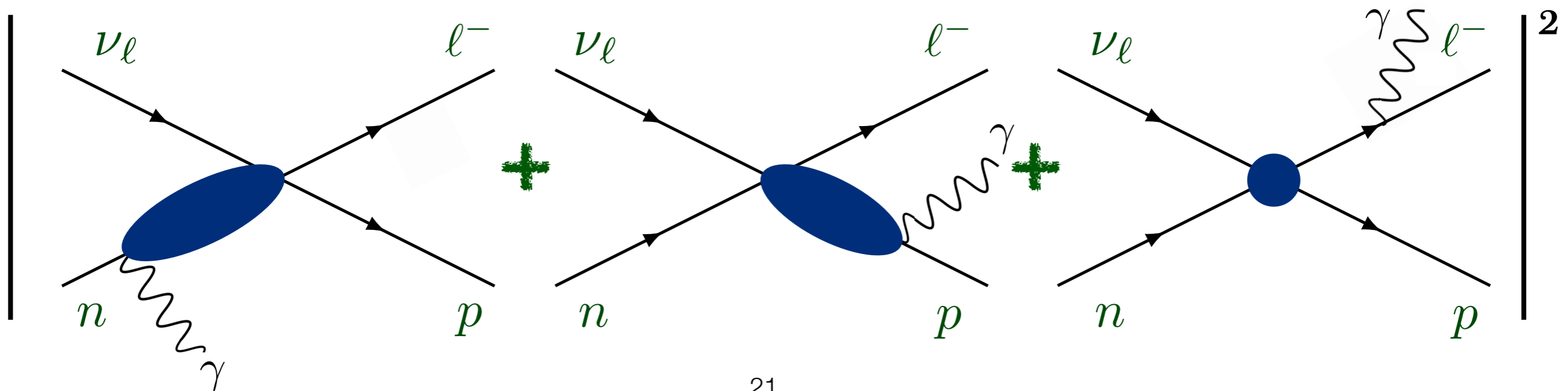


- ratios: cancellation of uncertainty from hard function

# Inclusive observables

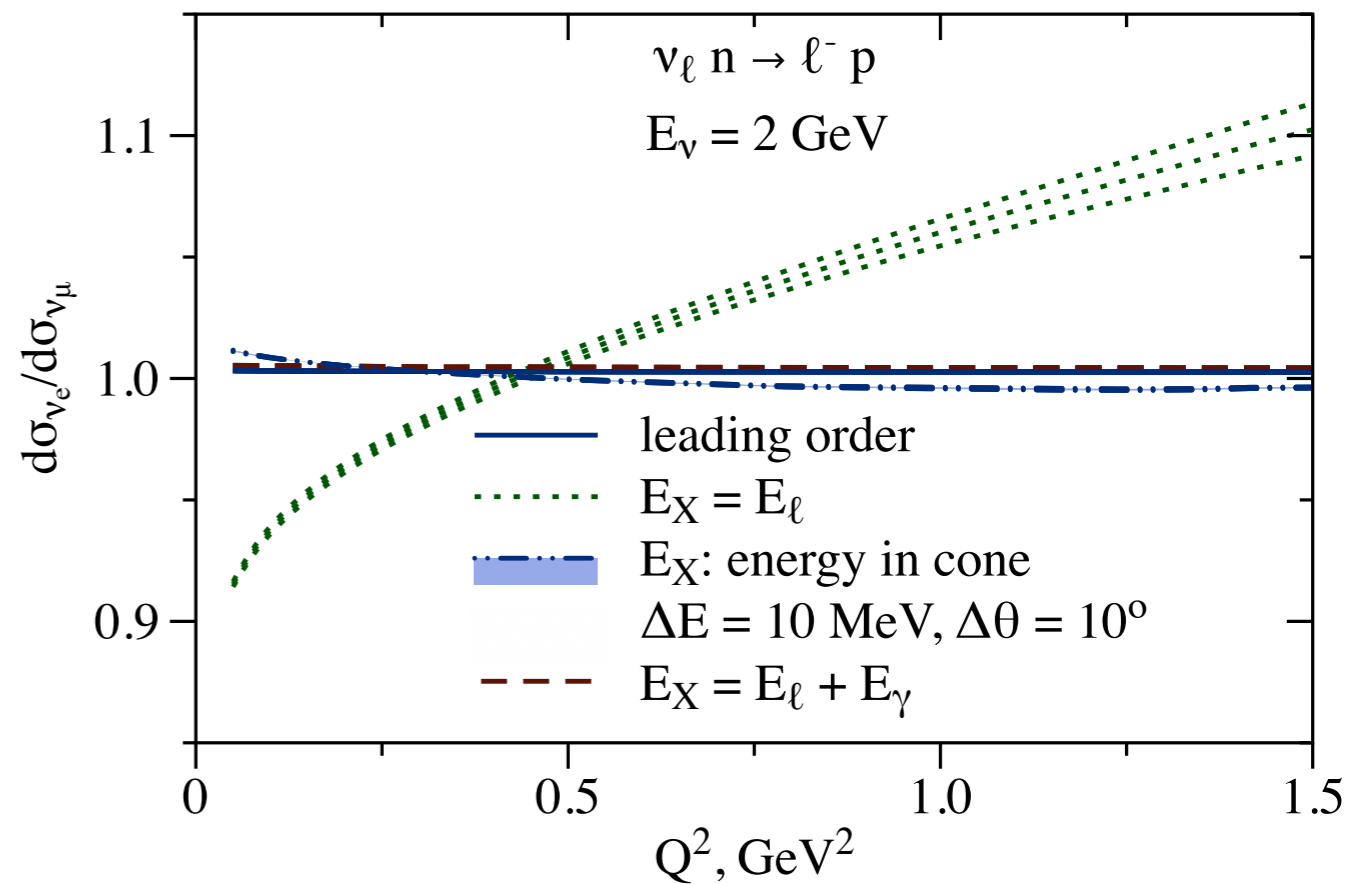
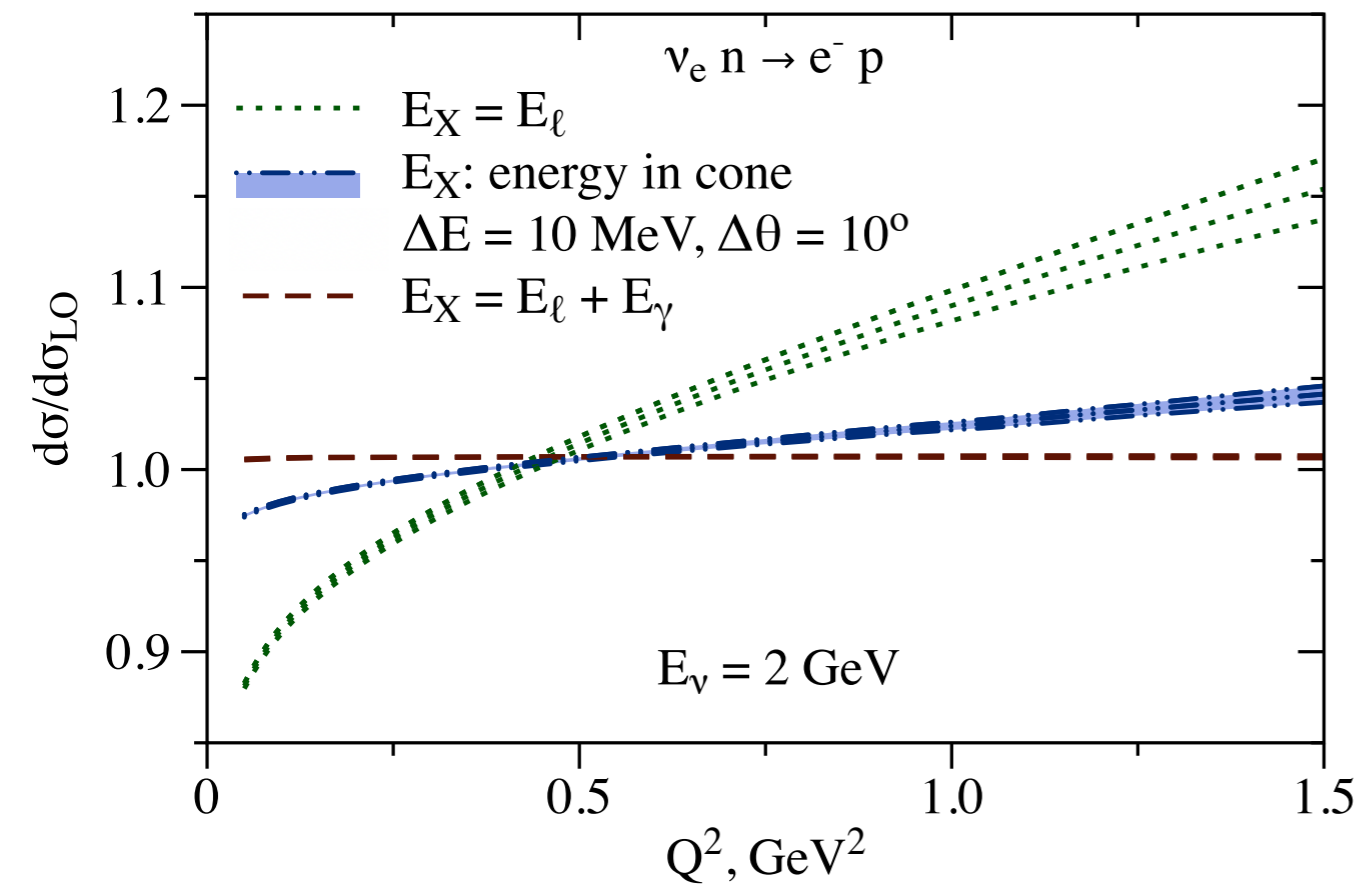


- the same gauge-invariant model for the real radiation
- arbitrary hard photons are part of the observable



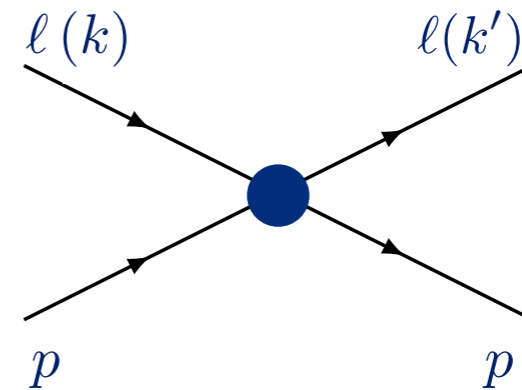
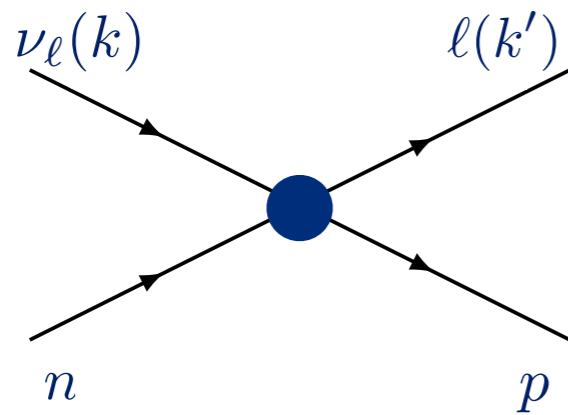
# Inclusive observables

- kinematics  $Q^2 = 2M(E_\nu - E_X)$  is reconstructed with 3 different  $E_X$



- dependence on reconstruction of kinematics and cuts
- predict  $\sigma_{\nu_e}$  from  $\sigma_{\nu_\mu}$  measurements with neutrino beam

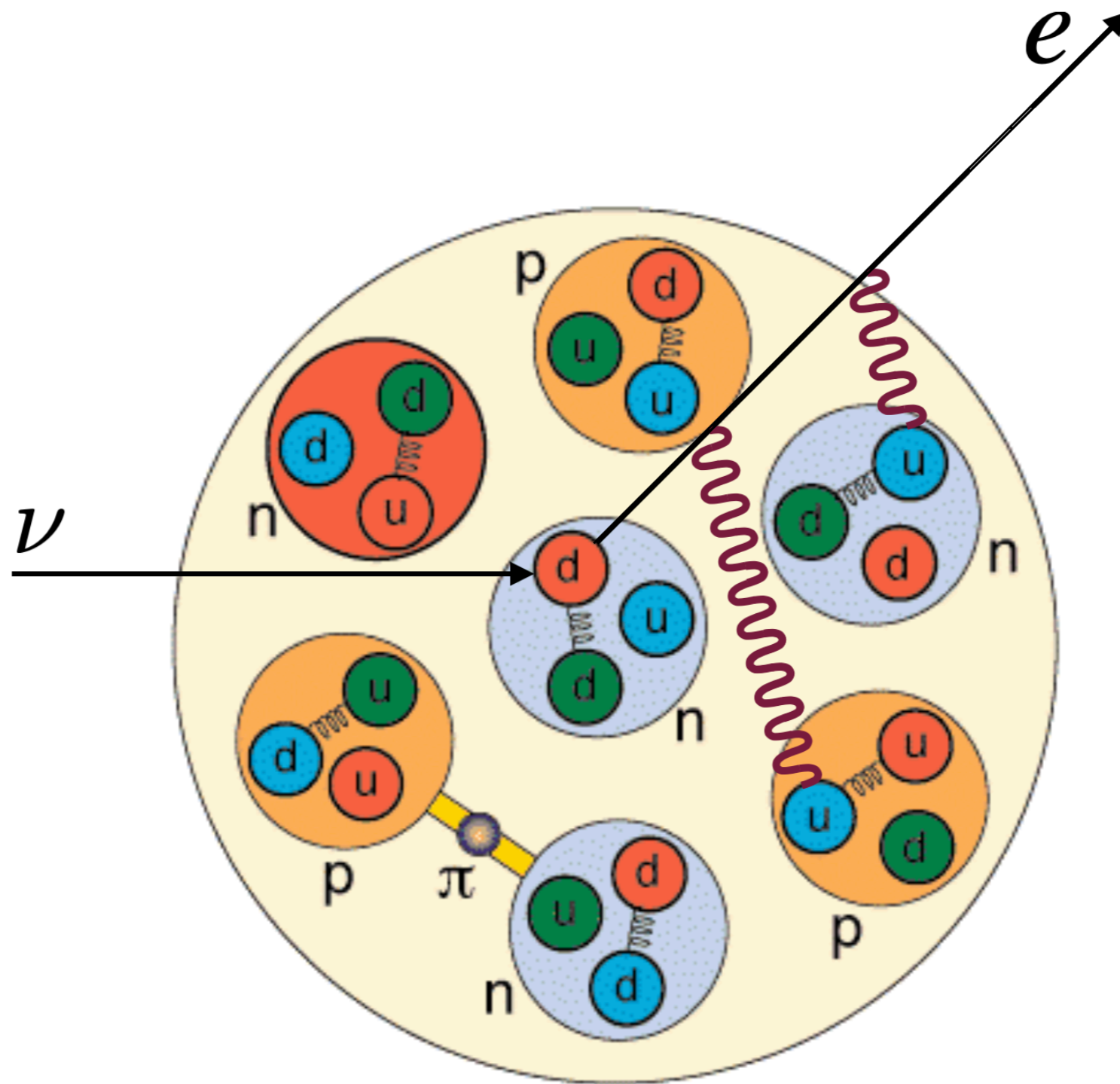




# QED nuclear medium effects in neutrino-nucleus and electron-nucleus scattering

O. T. and Ivan Vitev (arXiv: to appear)

# QED medium effects



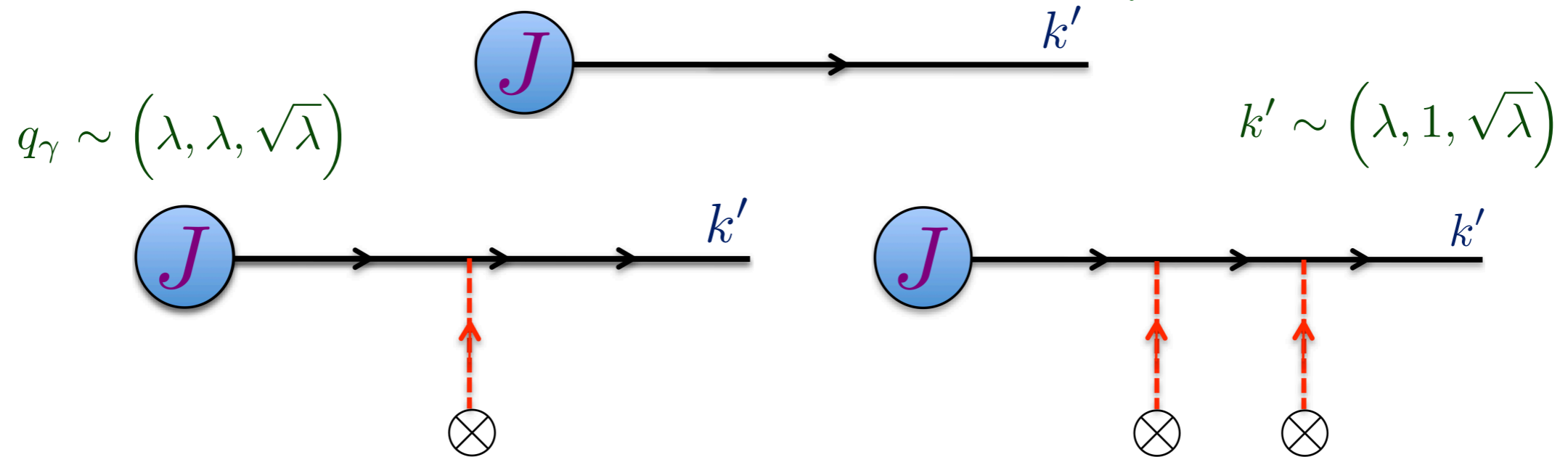
- charged lepton exchanges photons with nuclear medium



# SCET<sub>G</sub> formulation

- forward scattering is dominant process
- Glauber photons exchanged with a nuclear charge distribution

QCD: G. Ovanesyan and I. Vitev, JHEP (2011)



- change: integral along final lepton direction over charge and potential

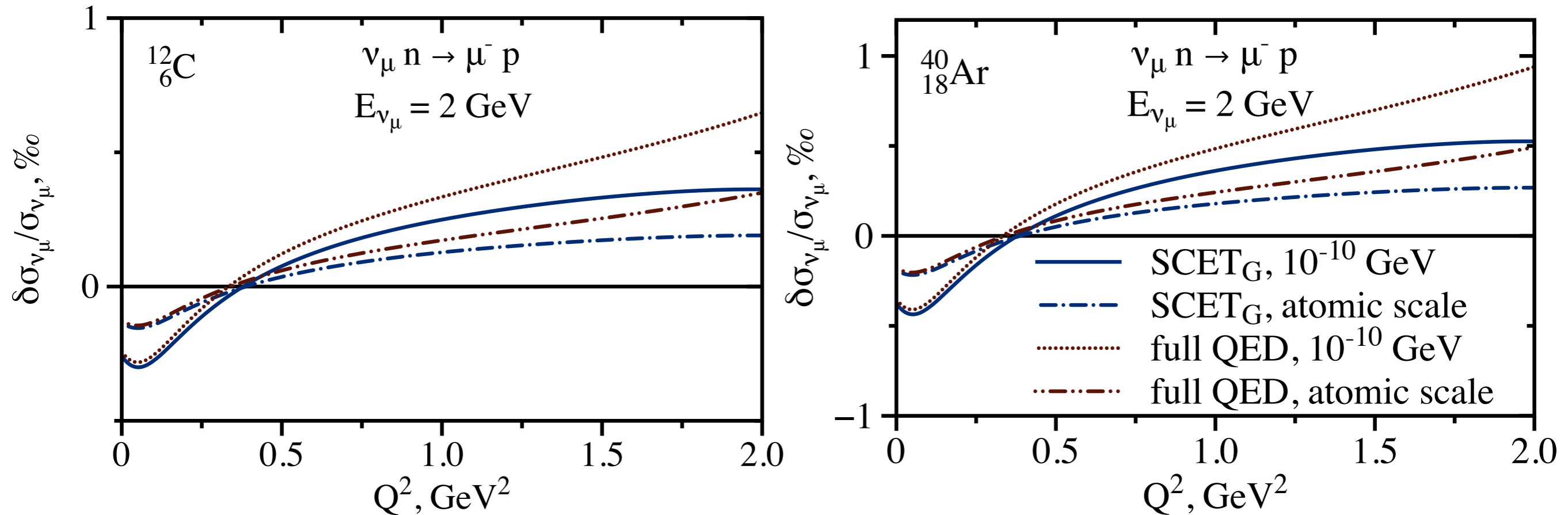
$$\delta\sigma_f \sim \int_{\text{lepton line}}^{\text{final}} \rho(z) dz \int \frac{d^2\vec{q}_\perp}{(2\pi)^2} |v(\vec{q}_\perp)|^2 \left( \sigma_0(\vec{k}, \vec{k}' - \vec{q}_\perp) - \sigma_0(\vec{k}, \vec{k}') \right)$$

- leading-order cross sections are distorted
- EFT and full QED calculations are performed

# Neutrino scattering

- relative correction per nucleon

$$v(q_{\perp}^2) = \frac{e^2}{q_{\perp}^2 + \lambda^2}$$



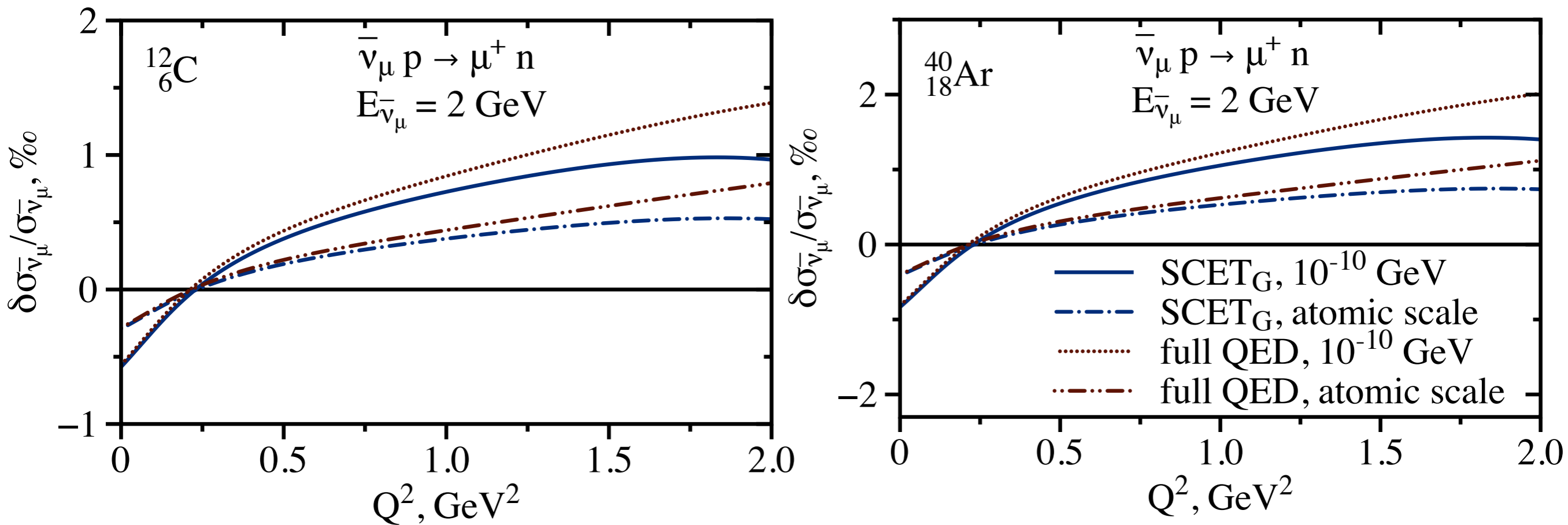
preliminary

- **permille-level** distortion of cross sections:  $\mathcal{O}(\alpha^2)$  correction
- smaller correction to inclusive cross section

# Antineutrino scattering

- relative correction per nucleon

$$v(q_{\perp}^2) = \frac{e^2}{q_{\perp}^2 + \lambda^2}$$



preliminary

- permille-level distortion of cross sections:  $\mathcal{O}(\alpha^2)$  correction
- larger correction than for neutrino scattering

# SCET<sub>G</sub> formulation

- forward scattering is dominant process
- Glauber photons exchanged with a nuclear charge distribution
- add initial-state exchanges, no interference with final-state exchanges
- change: integral along initial lepton direction over charge and potential

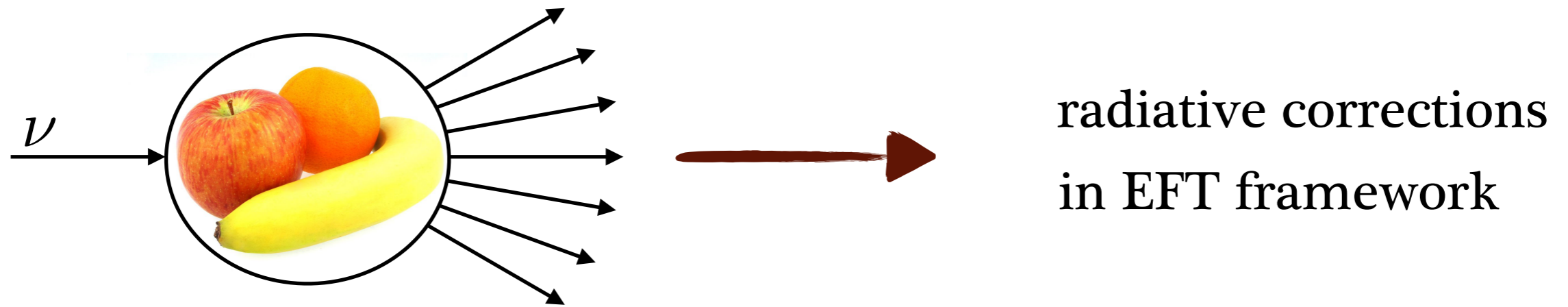
$$\delta\sigma_i \sim \int_{\text{lepton line}}^{\text{initial}} \rho(z) dz \int \frac{d^2\vec{q}_\perp}{(2\pi)^2} |v(\vec{q}_\perp)|^2 \left( \sigma_0(\vec{k} + \vec{q}_\perp, \vec{k}') - \sigma_0(\vec{k}, \vec{k}') \right)$$

- change: integral along final lepton direction over charge and potential

$$\delta\sigma_f \sim \int_{\text{lepton line}}^{\text{final}} \rho(z) dz \int \frac{d^2\vec{q}_\perp}{(2\pi)^2} |v(\vec{q}_\perp)|^2 \left( \sigma_0(\vec{k}, \vec{k}' - \vec{q}_\perp) - \sigma_0(\vec{k}, \vec{k}') \right)$$

- leading-order cross sections are distorted
- EFT and full QED calculations are ongoing

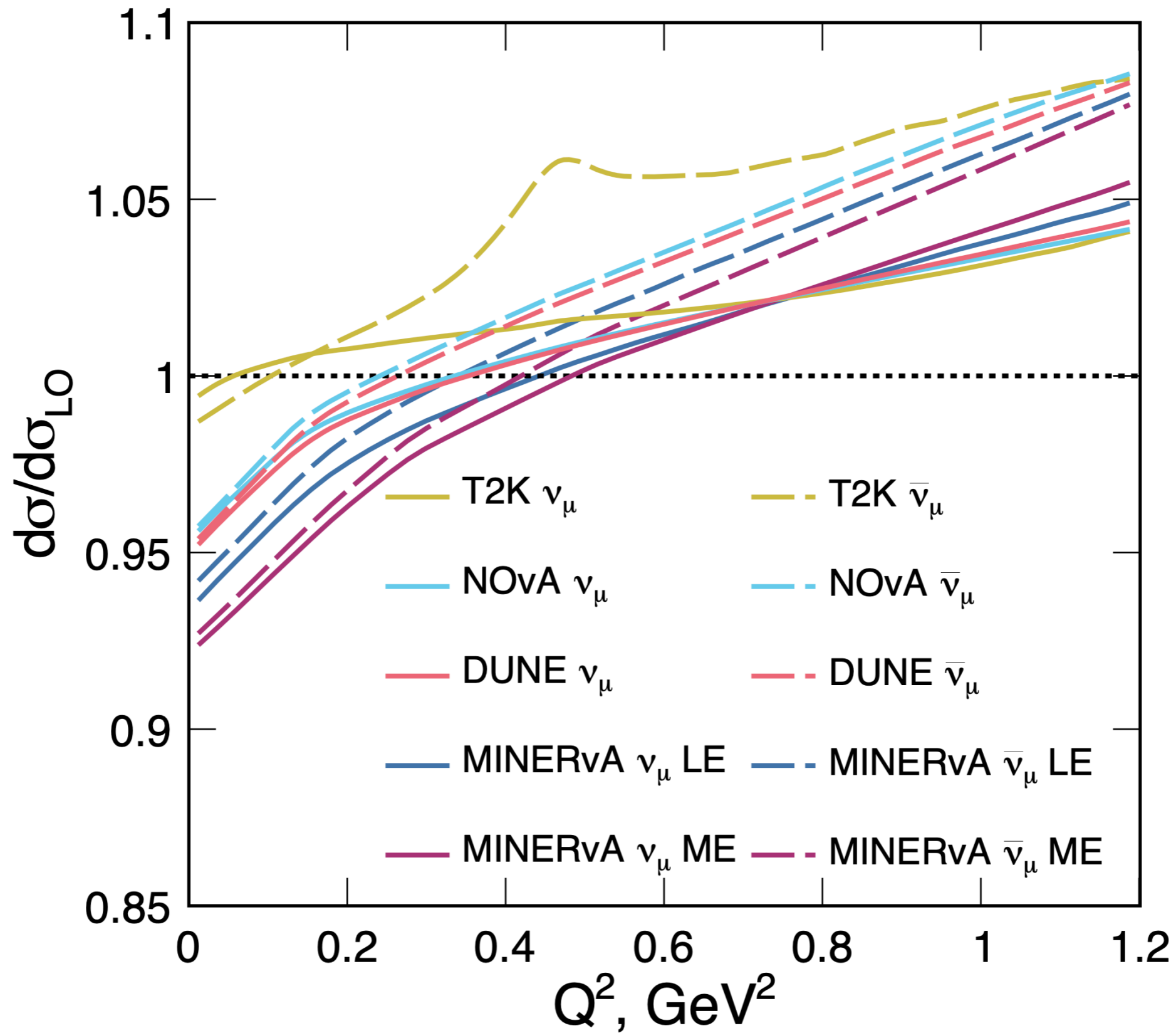
# Conclusions



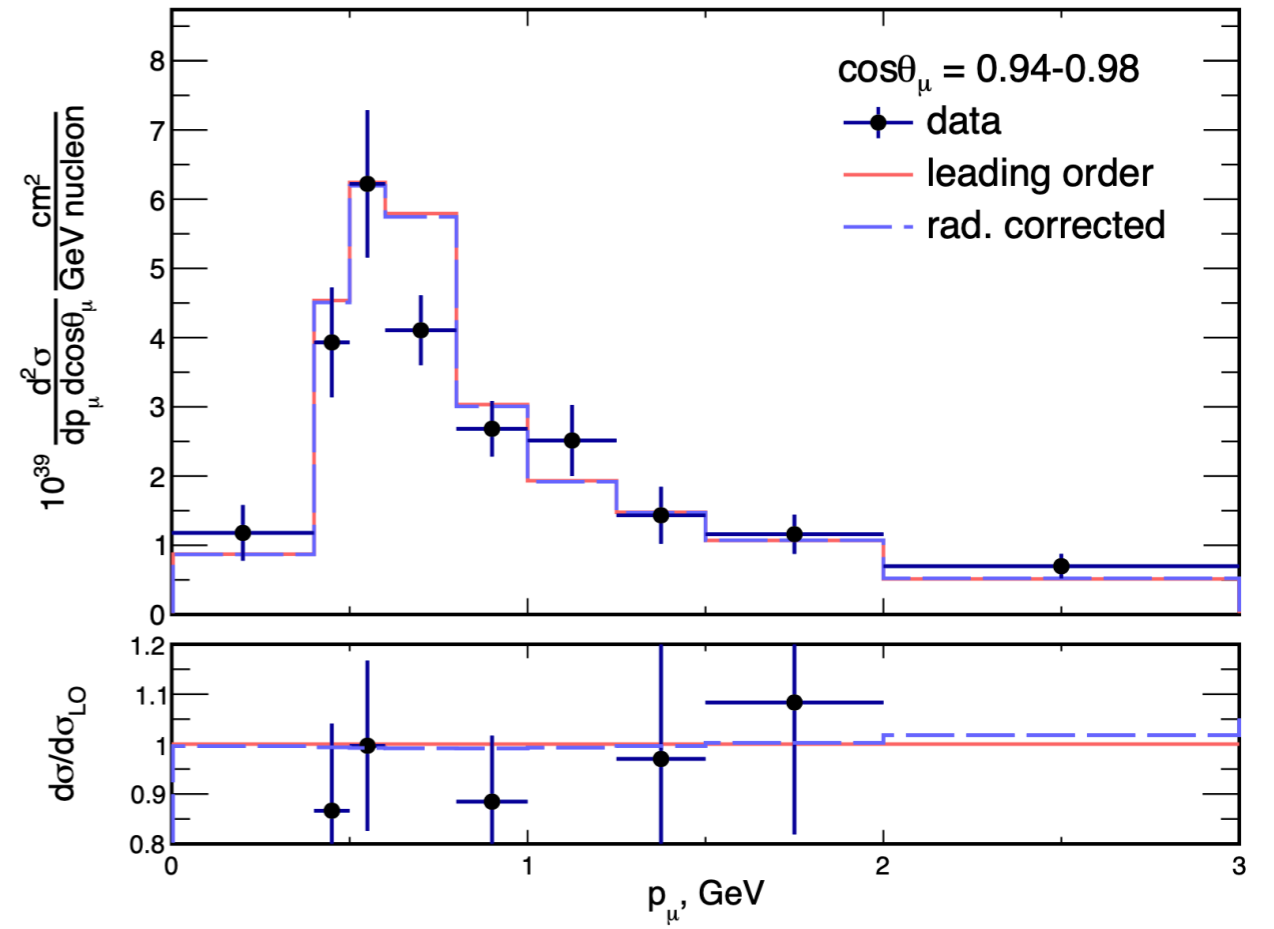
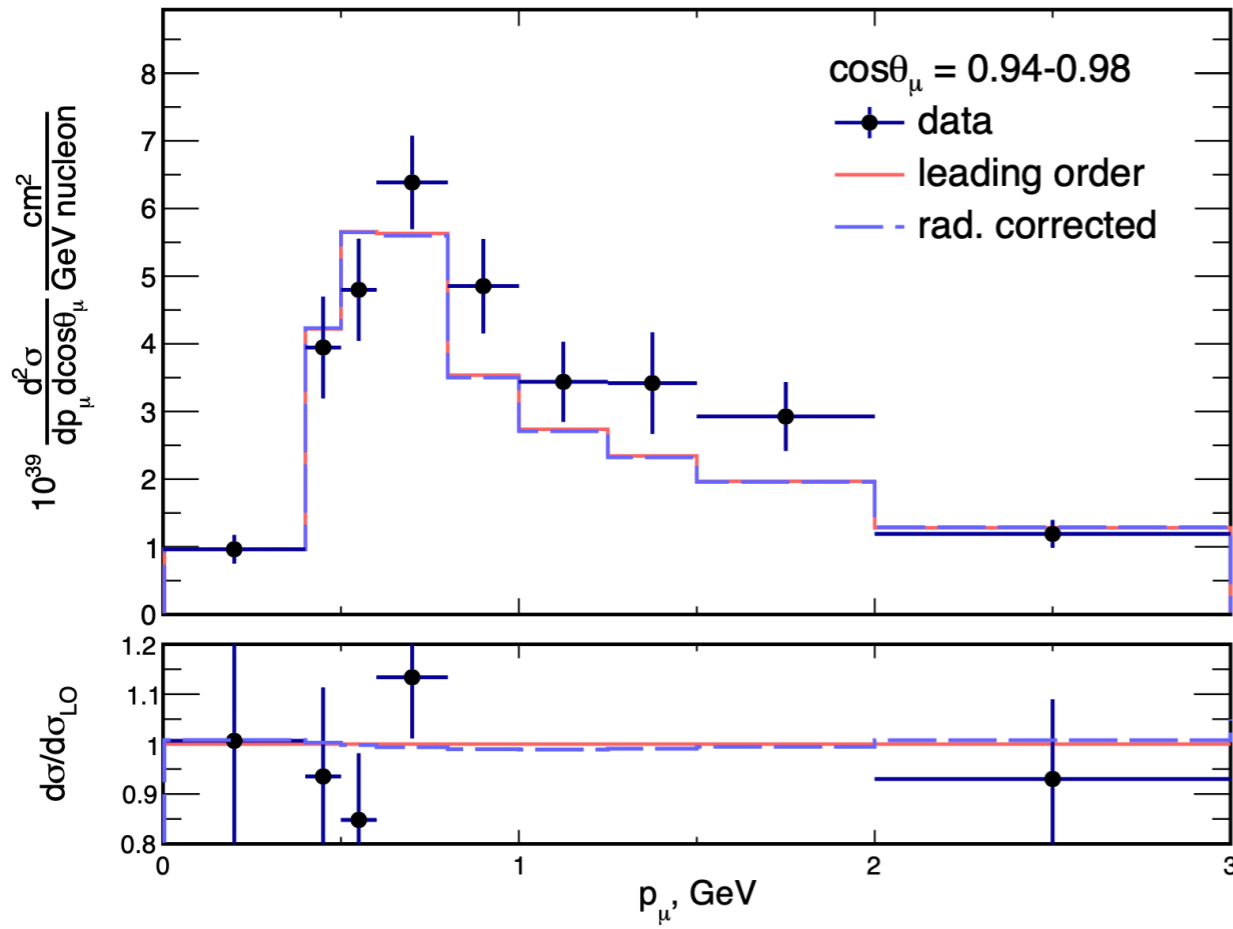
- radiative corrections to neutrino-nucleon cross sections formulated in factorization framework
- charged-current elastic electron vs muon cross-section ratios evaluated from theory with sub-percent uncertainty
- permille-level QED nuclear medium effects in lepton-nucleus scattering with SCET<sub>G</sub> and full QED treatments

Thanks for your attention !!!

# Integrated over flux lepton energy spectra

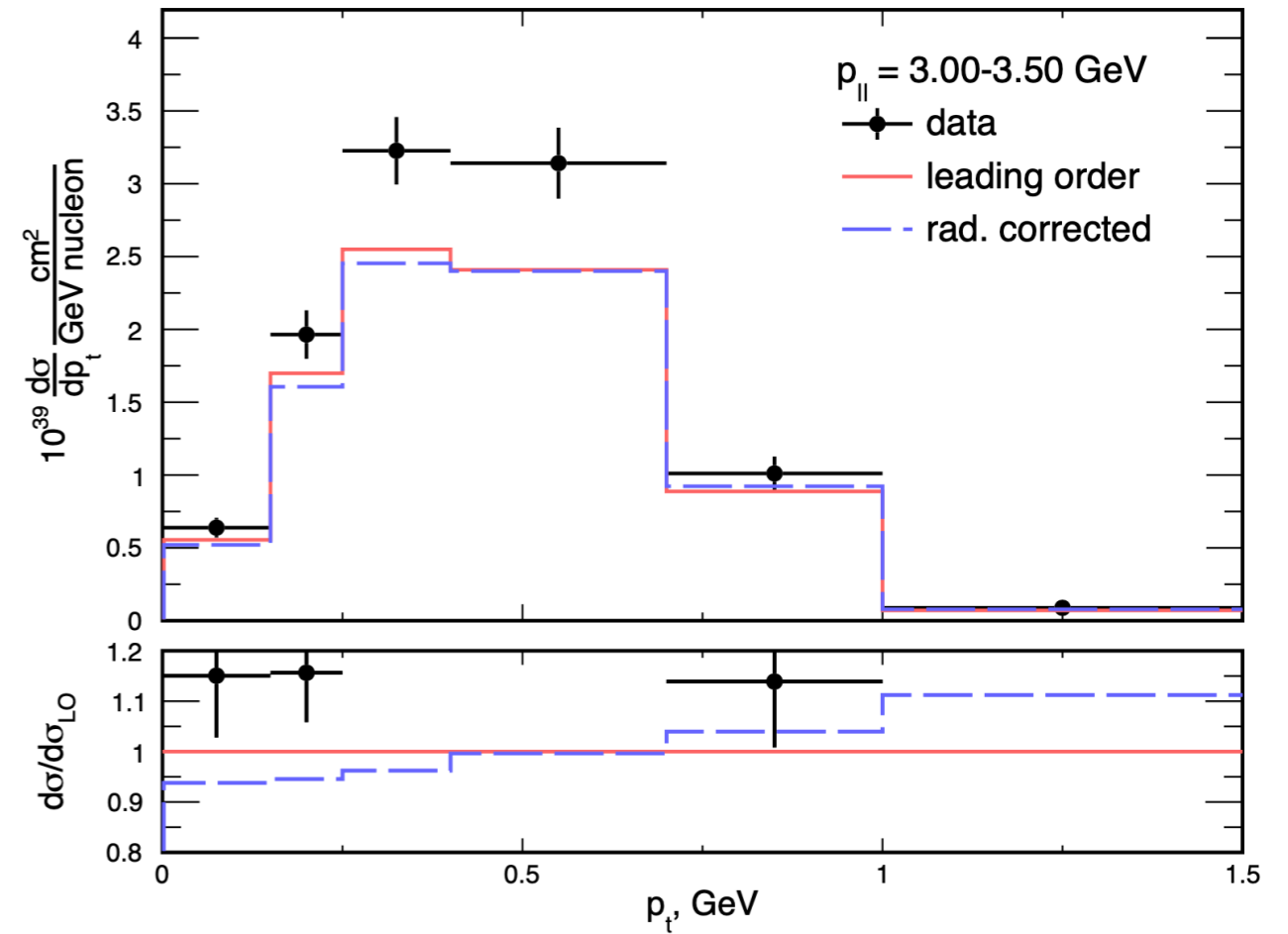
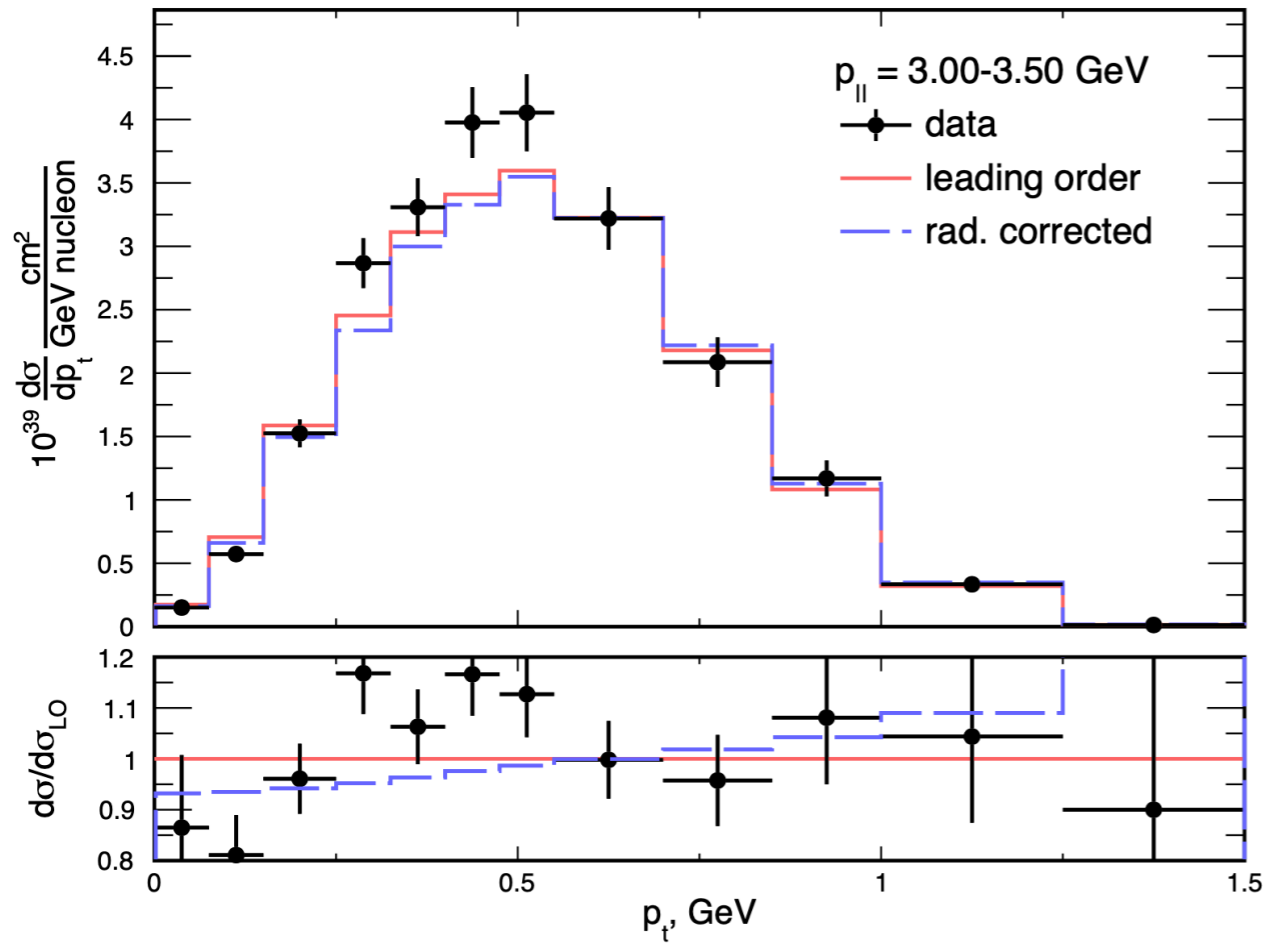


# T2K ND280 data

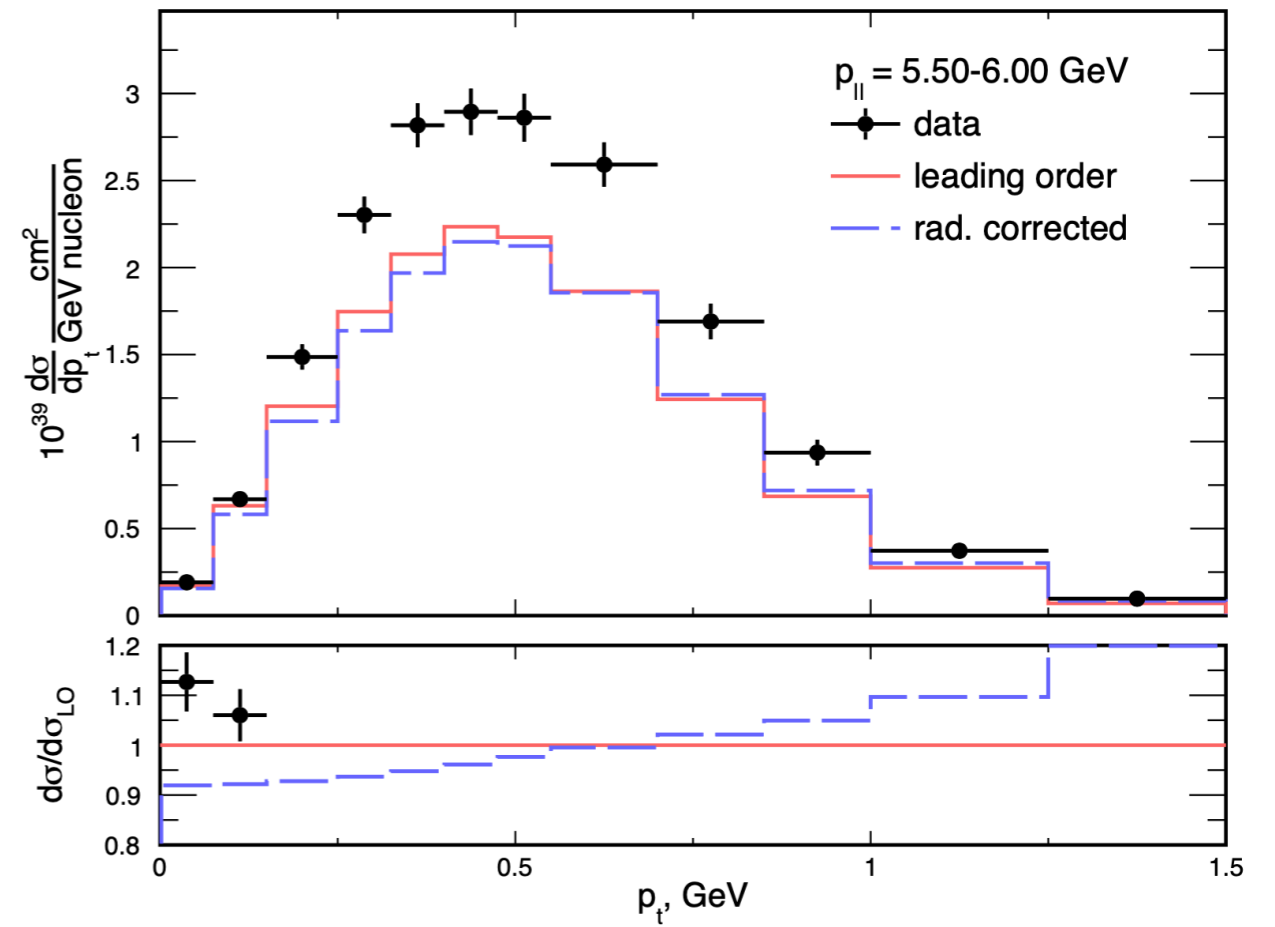
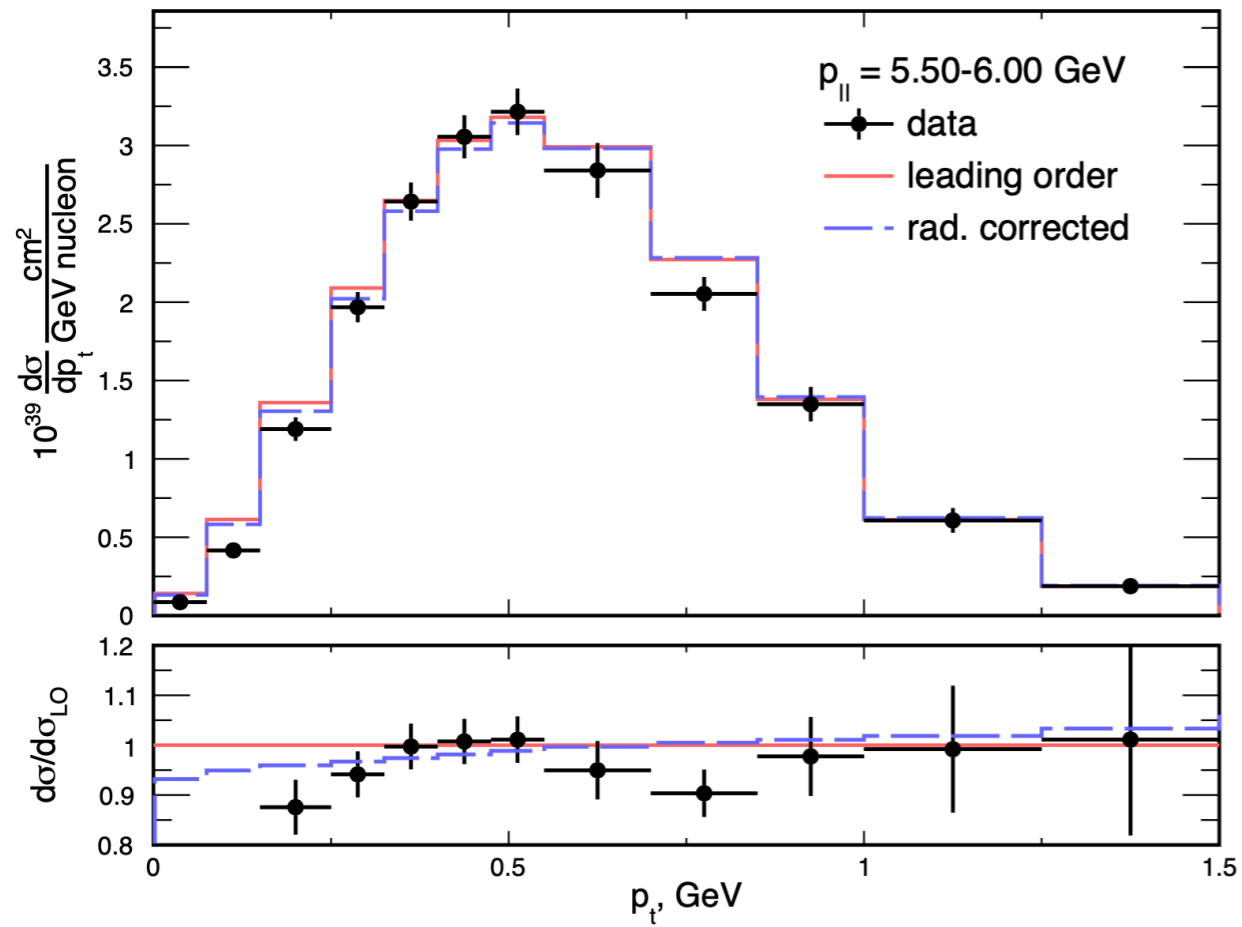




# MINERvA LE data

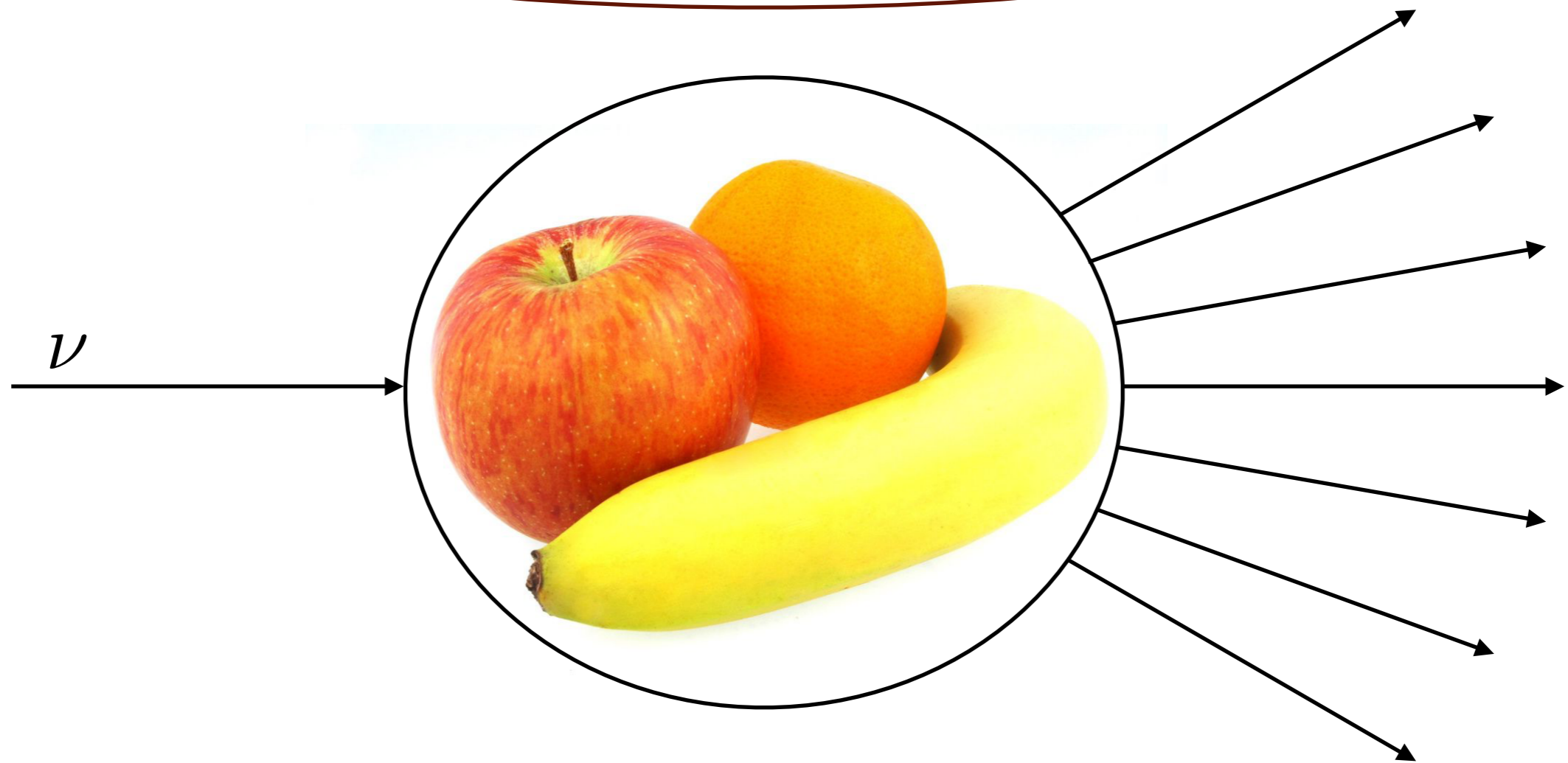


# MINERvA ME data



# Electroweak corrections

$$m_e, m_\mu, M, E_\nu \ll M_W, M_Z, m_t, m_H$$



$$\frac{\alpha}{\pi} \sim 0.2 \% \text{ multiplied by } \frac{1}{\sin^2 \theta_W}, \ln \frac{M_Z}{M}, \ln \frac{M_t}{M}, \dots$$

- electroweak corrections can be included in low-energy interactions

---

couplings of **effective Lagrangian** are precisely determined

$$\mathcal{L}_{\text{eff}}^{\text{NC}} = -\bar{\nu}_l \gamma_\mu P_L \nu_l \cdot \bar{f} \gamma^\mu (c_L^{\nu_l f} P_L + c_R^{\nu_l f} P_R) f$$

$$\mathcal{L}_{\text{eff}}^{\text{CC}} = -2\sqrt{2}G_F \sum_{l \neq l'} \bar{\nu}_{l'} \gamma^\mu P_L \nu_l \bar{l} \gamma_\mu P_L l' - c^{qq'} \sum_{q \neq q'} \bar{l} \gamma^\mu P_L \nu_l \bar{q} \gamma_\mu P_L q'$$

# Neutrino-lepton, neutrino-quark scattering

O.T. and Richard J Hill, Phys. Lett. B 805, 3, 135466 (2020)

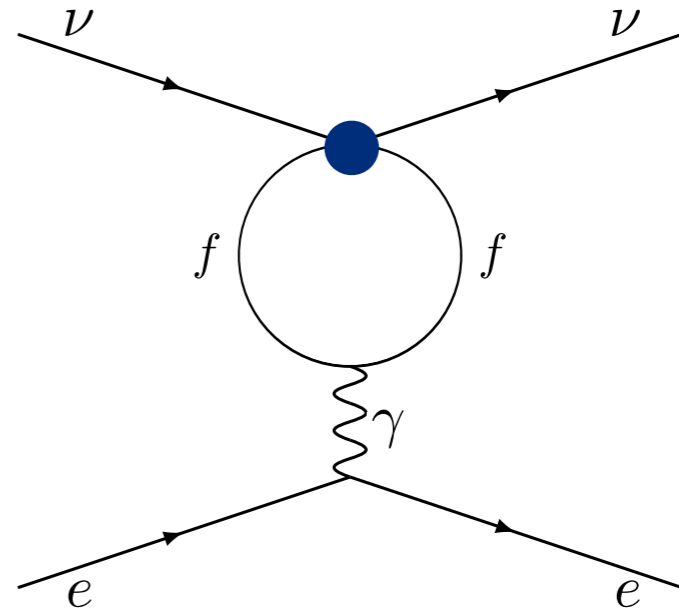
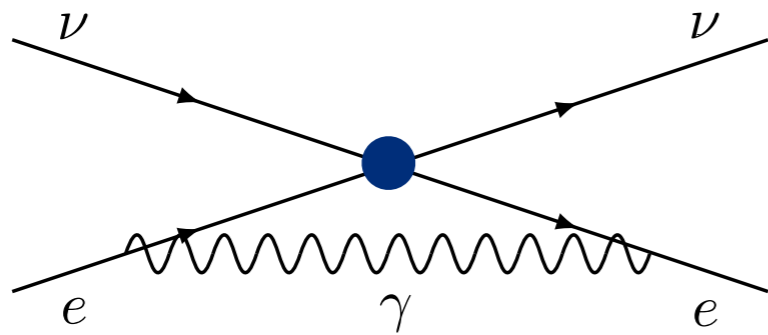
known at permille level



leading in  $G_F$  terms with loop expansion in  $\alpha, \alpha_s$  within Standard Model

poster at Neutrino 2020:

<https://youtu.be/mrW4aYjP57w>

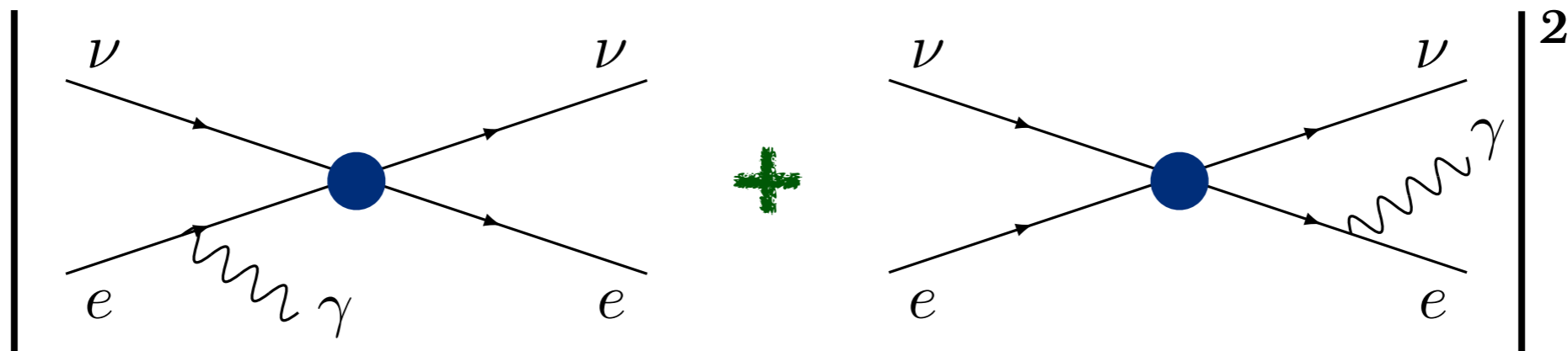


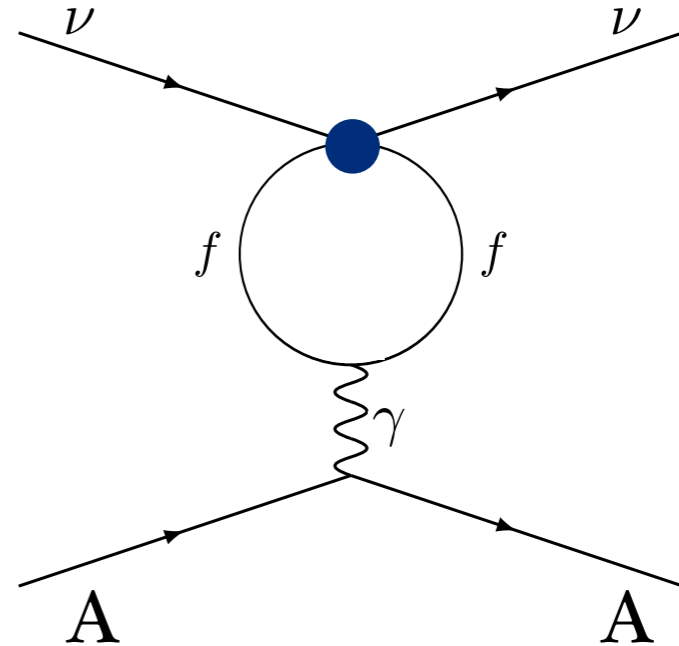
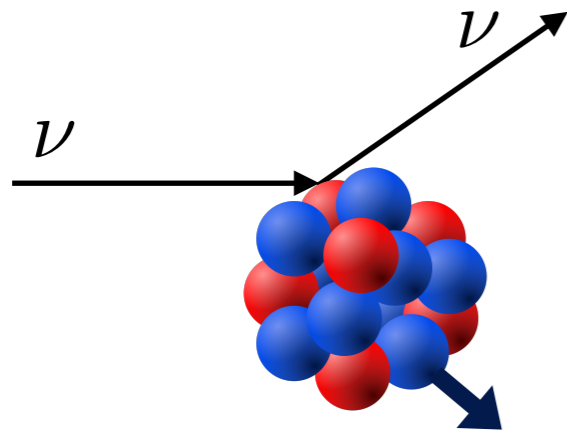
# Neutrino-electron scattering

O.T. and Richard J Hill, Phys. Rev. D 101 3, 033006 (2020)

percent-level predictions for MINERvA

known analytically at permille level for NOvA and DUNE





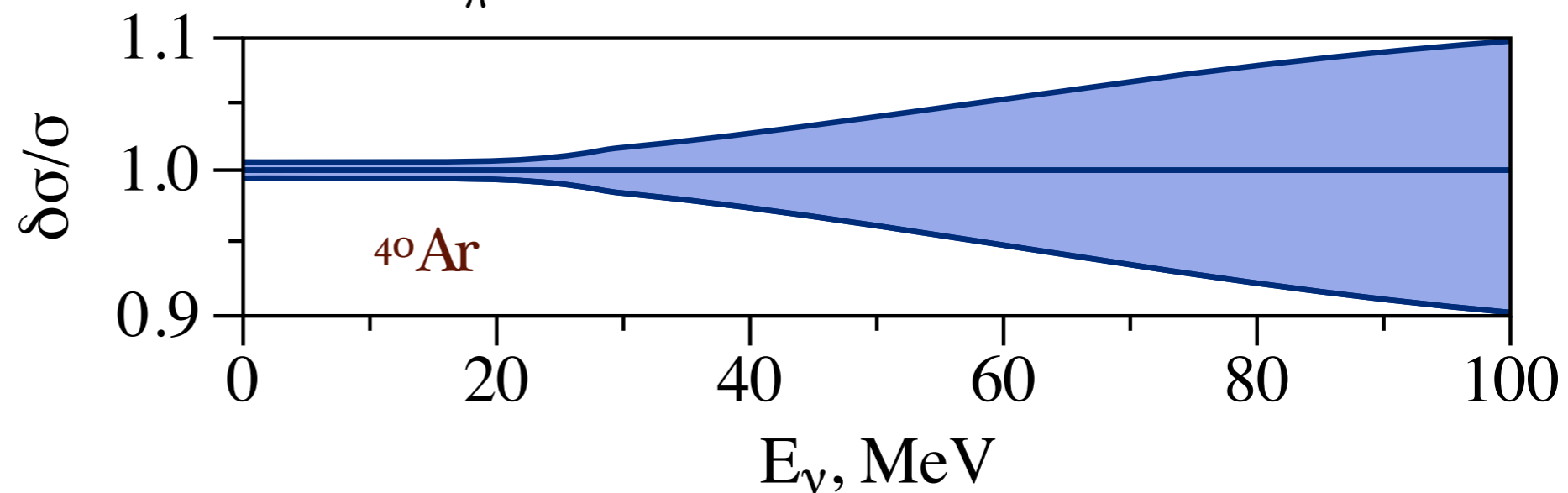
# Coherent elastic neutrino-nucleus scattering

O.T., Pedro Machado, Vishvas Pandey and Ryan Plestid, JHEP 2102, 097 (2021)

$$F_W(Q^2) \rightarrow F_W(Q^2) + \frac{\alpha}{\pi} [\delta^{\nu e} + \delta^{\text{QCD}}] F_{\text{ch}}(Q^2)$$

flavor-dependent  
at percent level

for Coherent and CCM

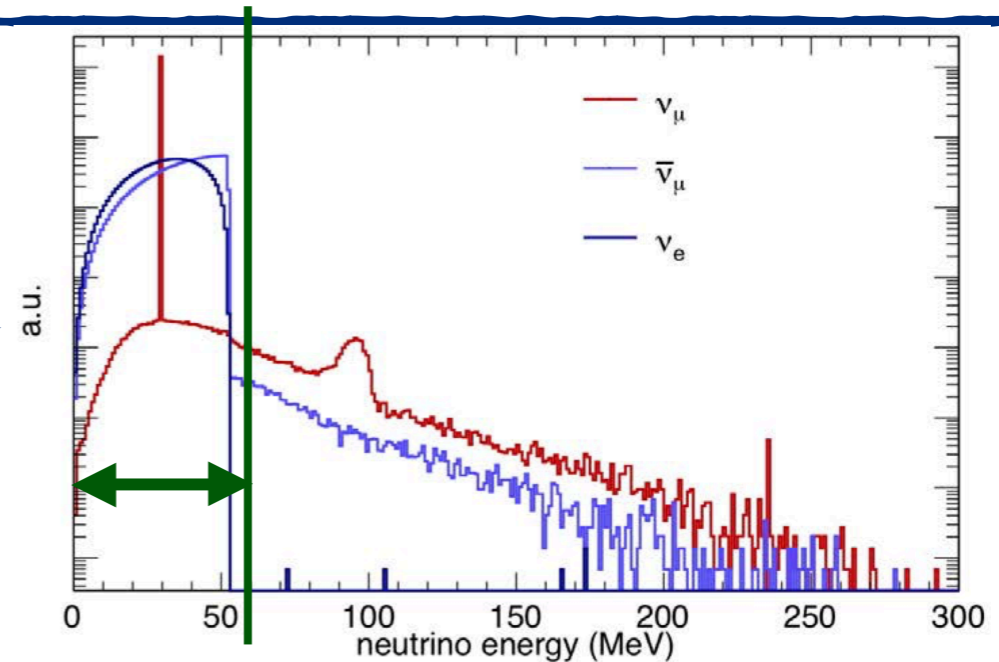


flavor-dependence at tree-level

energy spectra from  $\pi$ DAR  $\rightarrow$

$$\pi^+ \rightarrow \mu^+ \nu_\mu$$

$$\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$$



Akimov et al., Science 357 6356, 1123-1126 (2017)

# Neutrinos from muon, pion and kaon decays

O. T., arXiv: 2112.12395

$$\pi^+ \rightarrow \mu^+ \nu_\mu \gamma$$

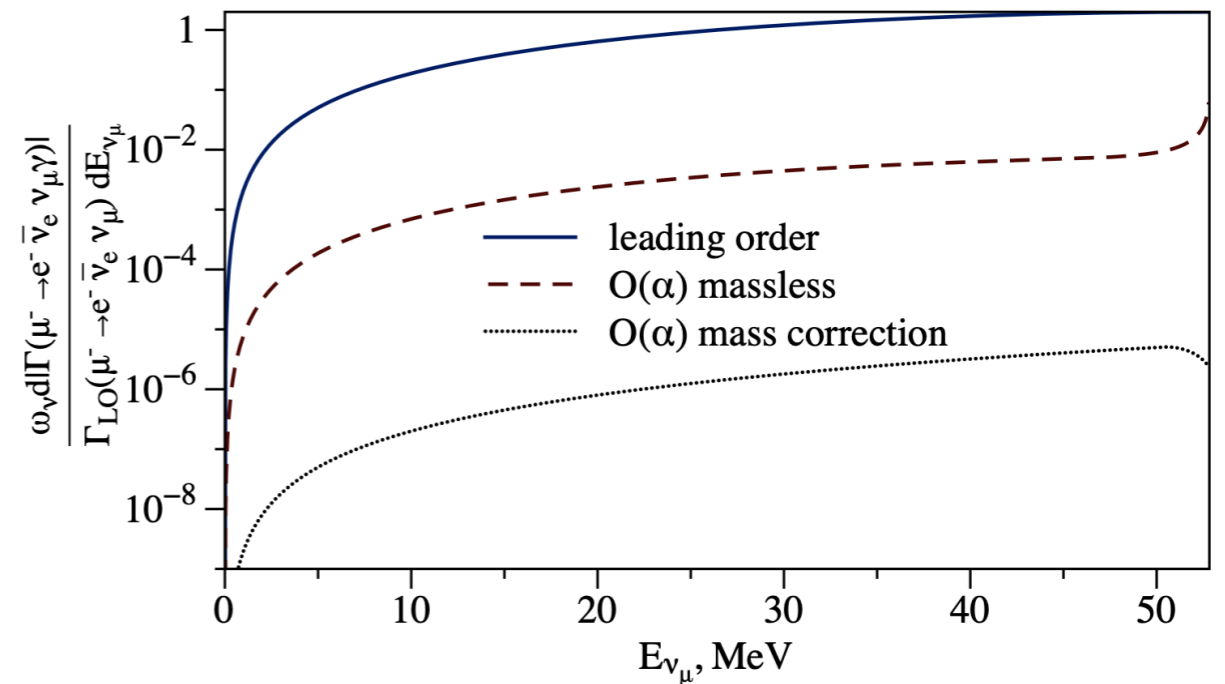
< 0.1 ‰

$$K^+ \rightarrow \mu^+ \nu_\mu \gamma$$

flavor-dependence is clarified to permille level analytically



$$\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu \gamma \quad 3-4 \text{ ‰}$$



first QED/EW form factors with different mass