

The space-time electromagnetic structure of hadrons

IWHSS-2022

Egle Tomasi-Gustafsson

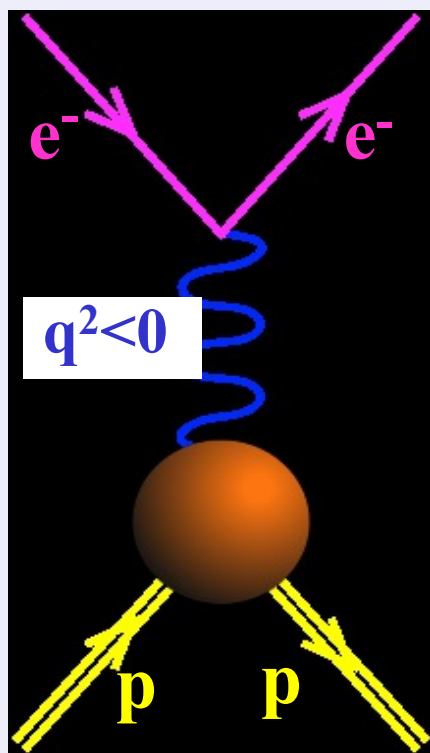
*CEA, IRFU, DPhN and
Université Paris-Saclay, France*

*In collaboration with
Simone Pacetti (INFN & Università di Perugia) and
Andrea Bianconi (INFN & Università di Brescia)*

*International Workshop on Hadron Structure and Spectroscopy (IWHSS-2022)
CERN, Geneva, Switzerland, August 29-31, 2022.*



Nucleon Charge and Magnetic Distributions

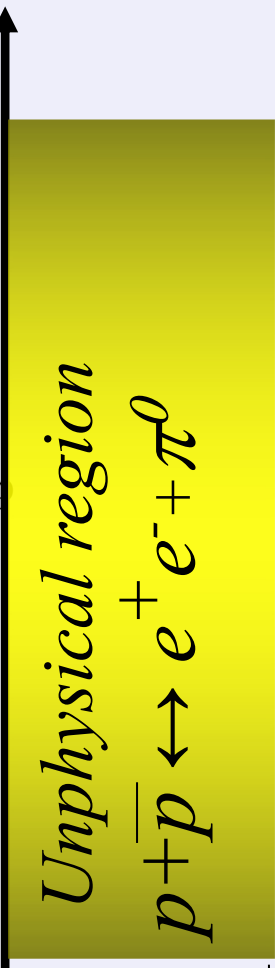


$q^2 < 0$

$G_E(0) = 1$

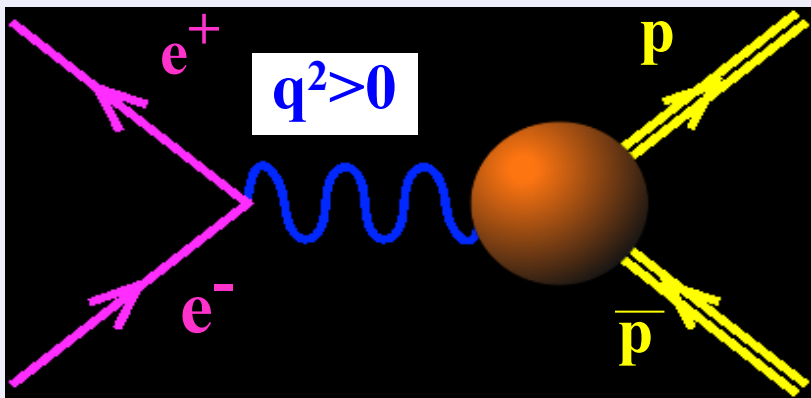
$G_M(0) = \mu_N$

*Space-like
FFs are real*



Unphysical region
 $p + \bar{p} \leftrightarrow e^+ e^- + \pi^0$

Asymptotics
- QCD
- analyticity



$q^2 > 0$

*Time-Like
FFs are complex*

$e + p \rightarrow e + p$

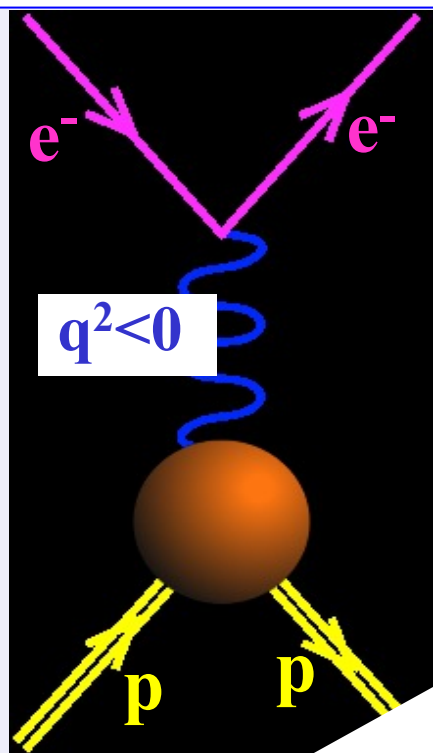
$0 \quad q^2 = 4m_p^2$
 $G_E = G_M$

$p + \bar{p} \leftrightarrow e^+ + e^-$

q^2

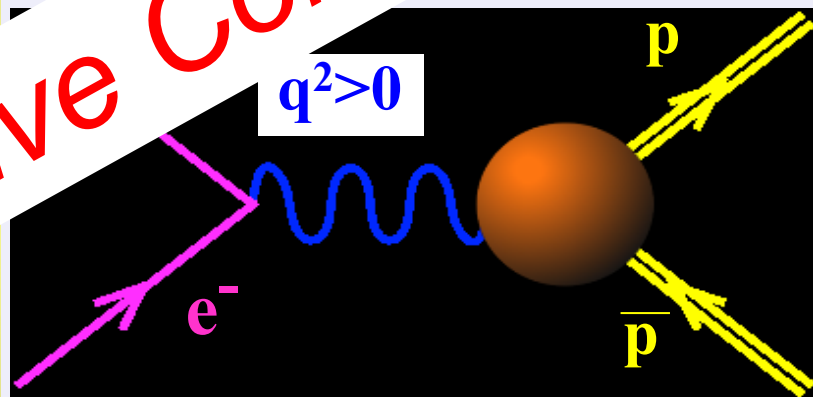


Nucleon Charge and Magnetic Distributions



$G_E(0) = 1$
 $G_M(0) = \mu_N$

Asymptotics
 - QCD



What about Radiative Corrections?

Space-Like
 FFs are real

Unphysical region
 $p + \bar{p} \leftrightarrow e^+ + e^-$

Time-Like
 FFs are complex

$e + p \rightarrow e + p$

$0 \quad q^2 = 4m_p^2$
 $GE = GM$

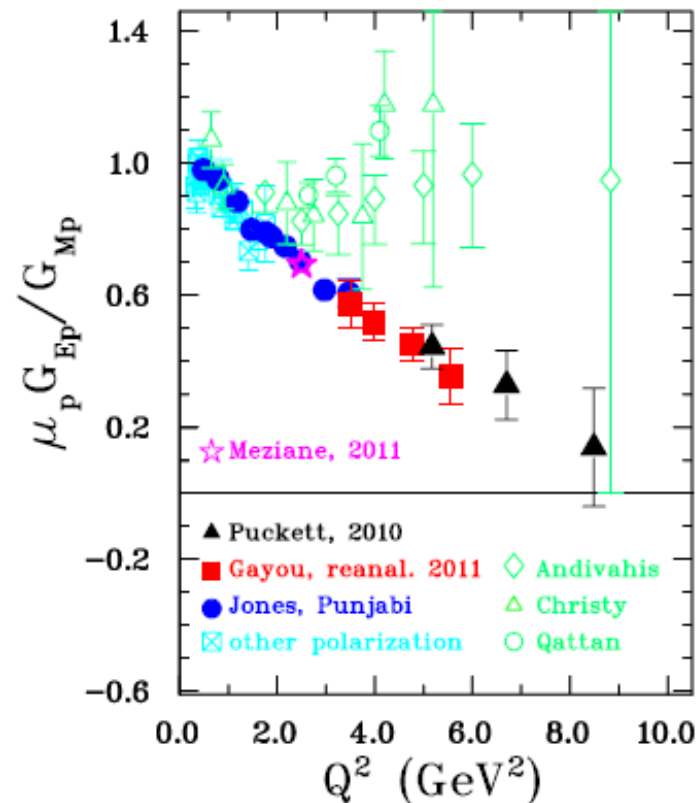
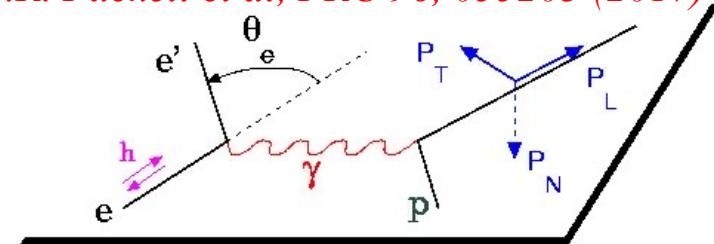
$p + \bar{p} \leftrightarrow e^+ + e^- \quad q^2$

Experimental fact 1 (SL): $ep \rightarrow ep$

- Precise data on the proton space-like form factors by the Akhiezer-Rekalo recoil proton polarization method show that the electric and magnetic distributions in the proton are different, suggesting a steeper Q^2 -monopole-like decrease of the ratio and eventually a zero-crossing of G_E .
- It is well accepted today that the polarization method gives THE reliable measurement of the EM FF ratio at large Q^2 (compared to the Rosenbluth method).
- The difference has been attributed to radiative corrections (including 2γ ?)
- Applying radiative corrections at first order in α brings a % uncertainty in cross section measurements. Not applied to the polarization ratio (cancel)

JLab-GEp Collaboration

J.R. Puckett et al, PRC 96, 055203 (2017)

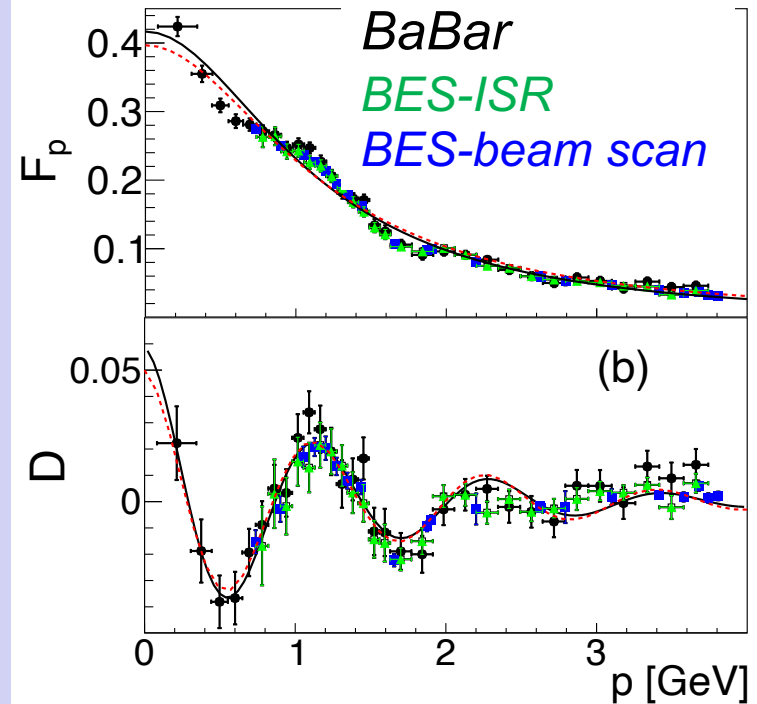


Ch. Perdrisat, V. Punjabi



Experimental fact 2 (TL): $e^+e^- \rightarrow \bar{p}p$

- BaBar and BESIII data on the proton time-like effective form factor show a systematic sinusoidal modulation in terms of the $p\bar{p}$ relative 3-momentum in the near-threshold region.
- $\sim 10\%$ size oscillations on the top of a regular background (dipole x monopole)
- The periodicity and the simple shape of the oscillations point to an interference of mechanisms of scale 0.2 and ~ 1 fm.
- The hadronic matter is distributed in non-trivial way.
- High order radiative corrections are applied (structure functions method)



$$F_p^{\text{fit}}(s) = F_{3p}(s) + F_{\text{osc}}(p(s))$$

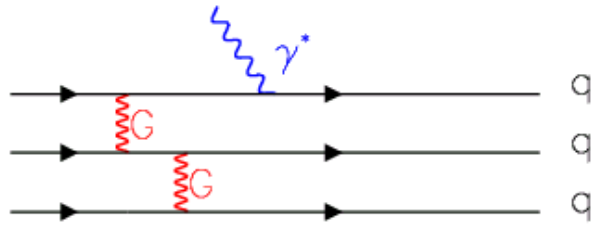
$$F_{3p}(s) = \frac{F_0}{\left(1 + \frac{s}{m_a^2}\right) \left(1 - \frac{s}{m_0^2}\right)^2},$$

$$F_{\text{osc}}(p(s)) = A e^{-Bp} \cos(Cp + D).$$

A. Bianconi, E. T-G. Phys. Rev. Lett. 114,232301 (2015)



The Time-like Region

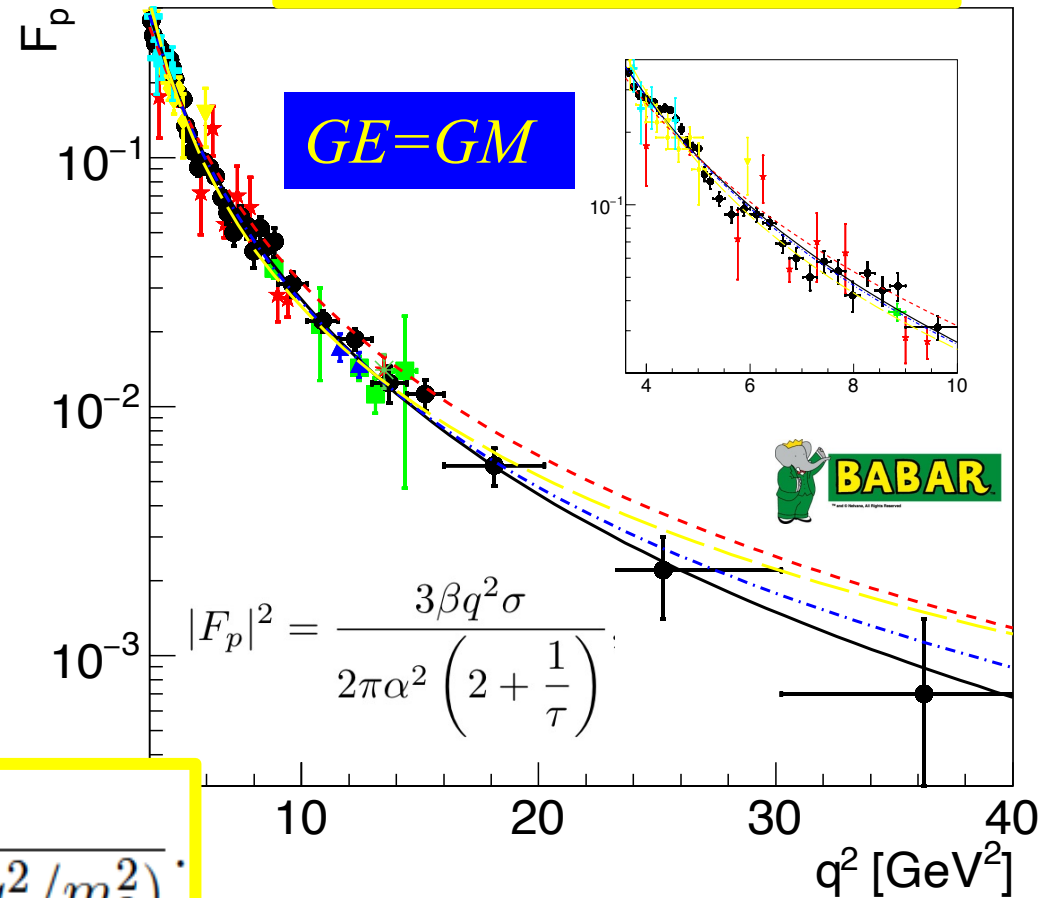
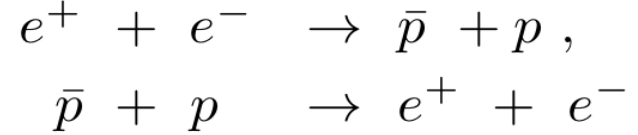


Expected QCD scaling $(q^2)^2$

$$|F_{scaling}(q^2)| = \frac{\mathcal{A}}{(q^2)^2 \log^2(q^2/\Lambda^2)}$$

$$\frac{\mathcal{A}}{(1 + q^2/m_a^2) [1 - q^2/0.71]^2},$$

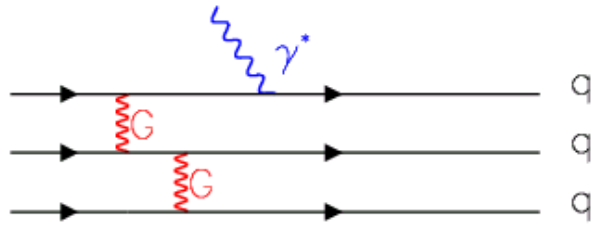
$$|F_{T3}(q^2)| = \frac{\mathcal{A}}{(1 - q^2/m_1^2)(2 - q^2/m_2^2)}.$$



A. Bianconi, E. T-G. Phys. Rev. Lett. 114,232301 (2015)



The Time-like Region

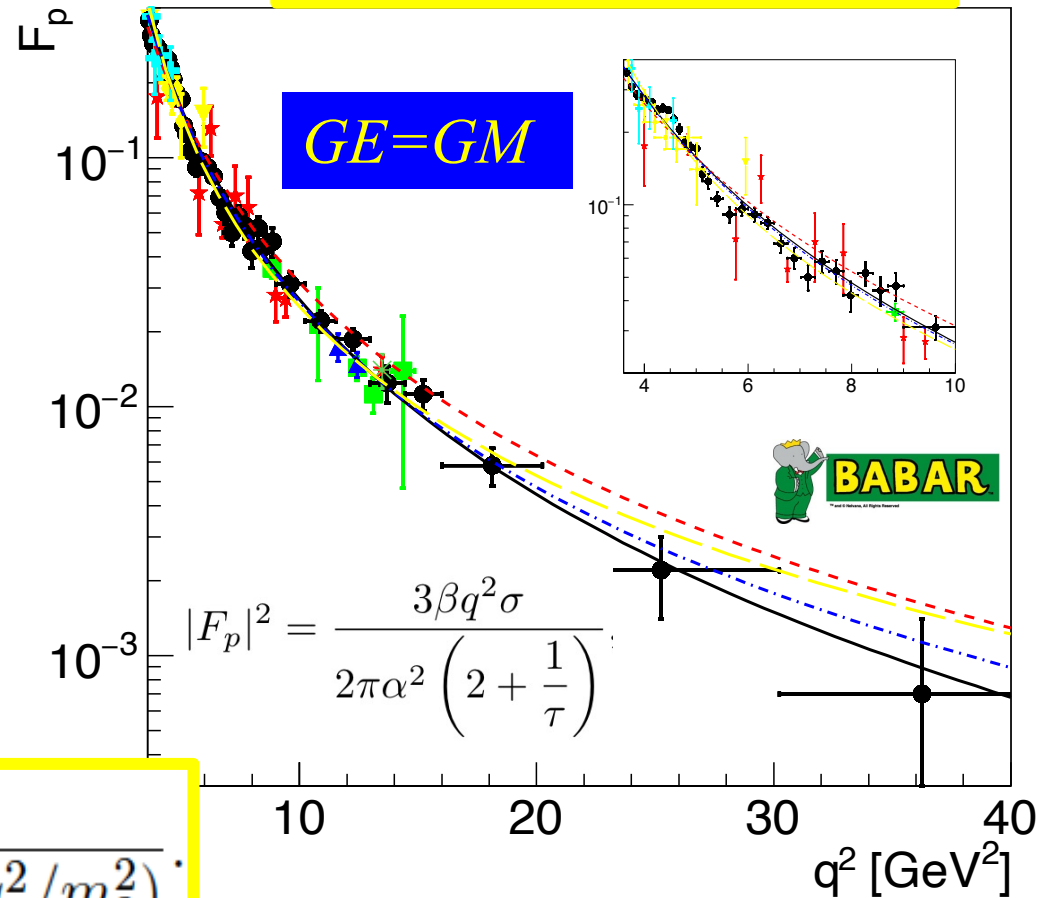
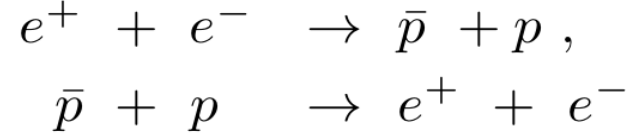


Expected QCD scaling $(q^2)^2$

$$\frac{A}{(q^2)^2 [\log^2(q^2/\Lambda^2) + \pi^2]}$$

$$\frac{A}{(1 + q^2/m_a^2) [1 - q^2/0.71]^2}$$

$$|F_{T3}(q^2)| = \frac{A}{(1 - q^2/m_1^2)(2 - q^2/m_2^2)}$$



A. Bianconi, E. T-G. Phys. Rev. Lett. 114,232301 (2015)



10 years ago a generalization of FFs in SL and TL was proposed

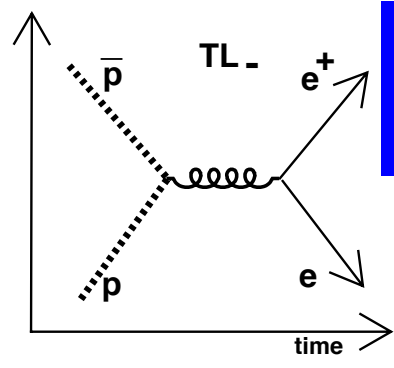
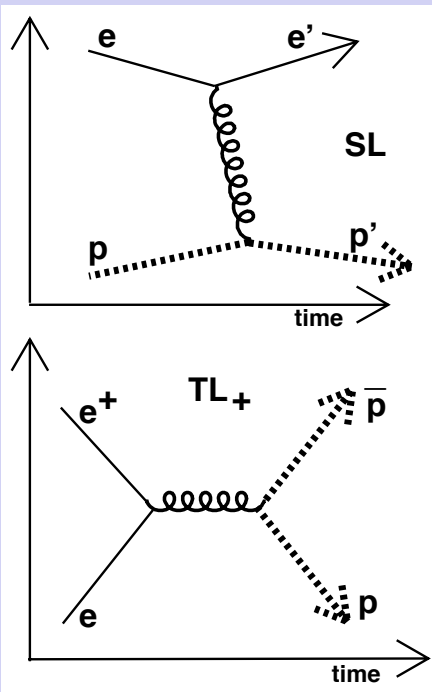
$$F(q^2) = \int_{\mathcal{D}} d^4x e^{iq_\mu x^\mu} \rho(x), \quad q_\mu x^\mu = q_0 t - \vec{q} \cdot \vec{x}$$

$\rho(x) = \rho(\vec{x}, t)$ space-time distribution of the electric charge in the space-time volume \mathcal{D} .

SL photon 'sees' a charge density

TL photon can NOT test a space distribution

How to connect and understand the amplitudes?



E.A. Kuraev, A. Dbeyssi, E. T-G. Phys. Lett. 712, 240 (2012)
A.Bianconi, E. T-G. Phys. Rev. Lett. 114,232301 (2015)

Photon-Charge coupling

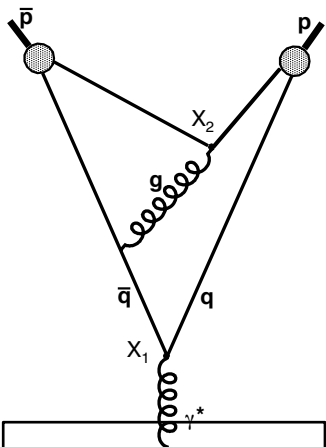
...access projections of $F(q^2)$

$$\rho(\vec{x})$$

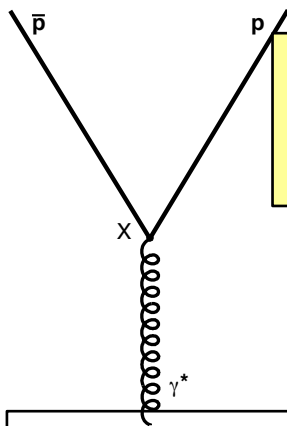
SL: Fourier transform of a stationary charge and current distribution (*Breit frame*)

$$R(t)$$

TL: Amplitude for creating *charge-anticharge pairs* at time t (*CMS frame*)



Resolved



Unresolved

Charge distribution: distribution in time of $\gamma^* \rightarrow$ *charge-anticharge vertices*

The simplest picture: $q\bar{q}$ pair + compact di-quark

representation

Fourier Transform

A. Bianconi, E. T-G., Phys. Rev. Lett. 114, 232301 (2015)

$$F_0(p) \equiv \int d^3\vec{r} \exp(i\vec{p} \cdot \vec{r}) M_0(r)$$

$$F(p) = F_0(p) + F_{osc}(p) \equiv \int d^3\vec{r} \exp(i\vec{p} \cdot \vec{r}) M(r).$$

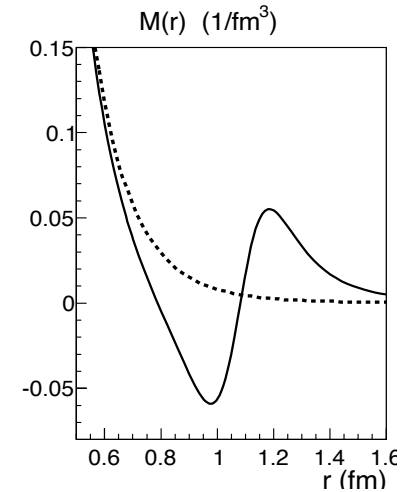
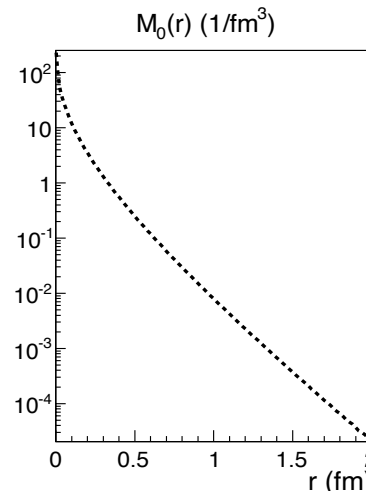
p: relative momentum

r: distance between the center of the forming hadrons

(p,r) conjugate variables, $r \leftrightarrow t$

$$F_0 = \frac{A}{(1 + q^2/m_a^2) [1 - q^2/0.71]^2},$$

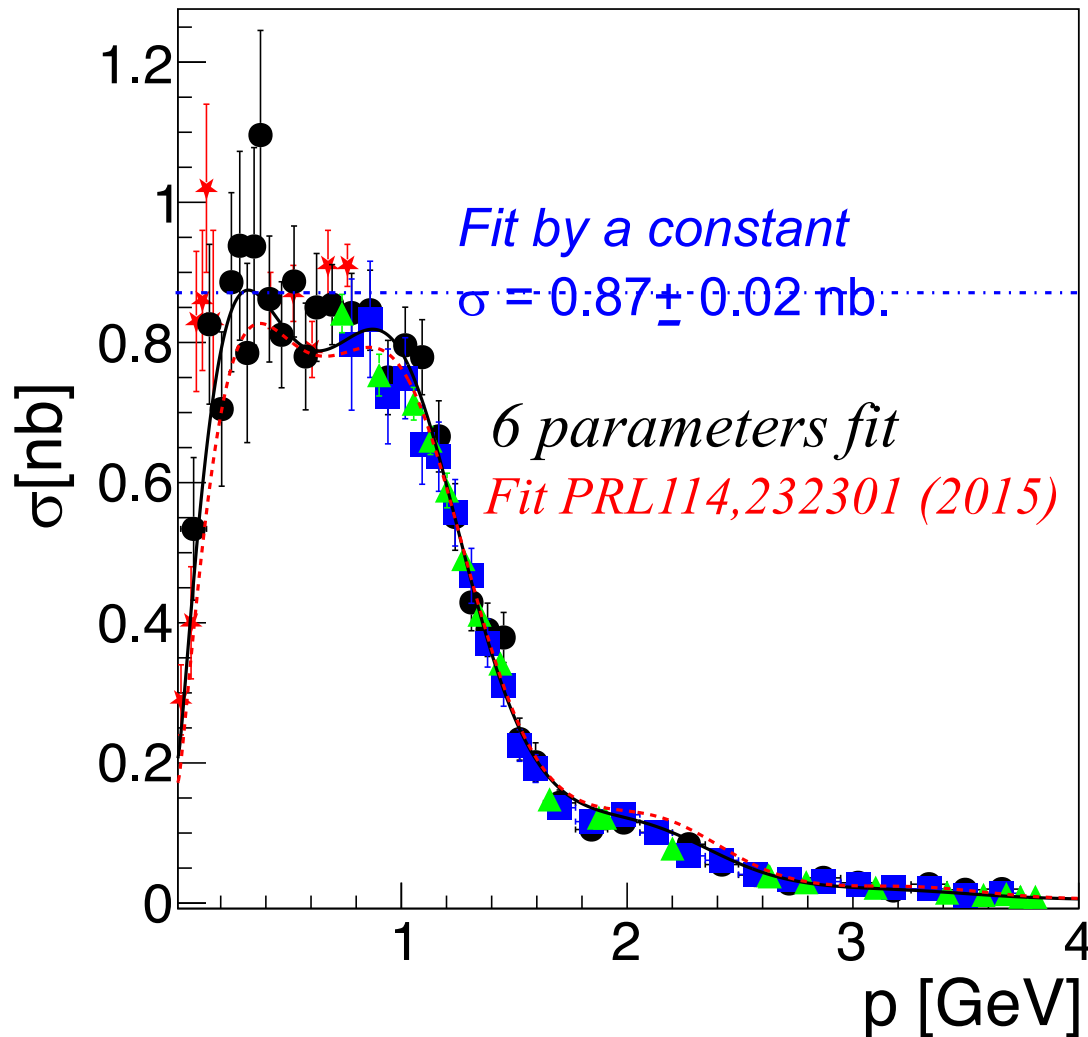
$$F_{osc}(p) \equiv A \exp(-Bp) \cos(Cp + D).$$



- Rescattering processes
- Large imaginary part
- Related to the time evolution of the charge density?
(E.A. Kuraev, E. T-G., A. Dbeyssi, PLB712 (2012) 240)
- Consequences for the SL region?
- Data from BESIII, expected from PANDA



Cross section from $e^+e^- \rightarrow p\bar{p}$



Novosibirsk 38pt
 $1.9 < 2E < 4.5$
PLB794,64 (2019)

BaBar 85pt
 $1.9 < 2E < 4.5$
PRD87,092005 (2013)

ISR-ISR-SA 30pt
 $2 < 2E < 3.6$
PRD99,092002 (2019)

ISR-Scan 22pt
 $2 < 2E < 3.1$
PRL124,042001 (2020)



Generalized Form Factor

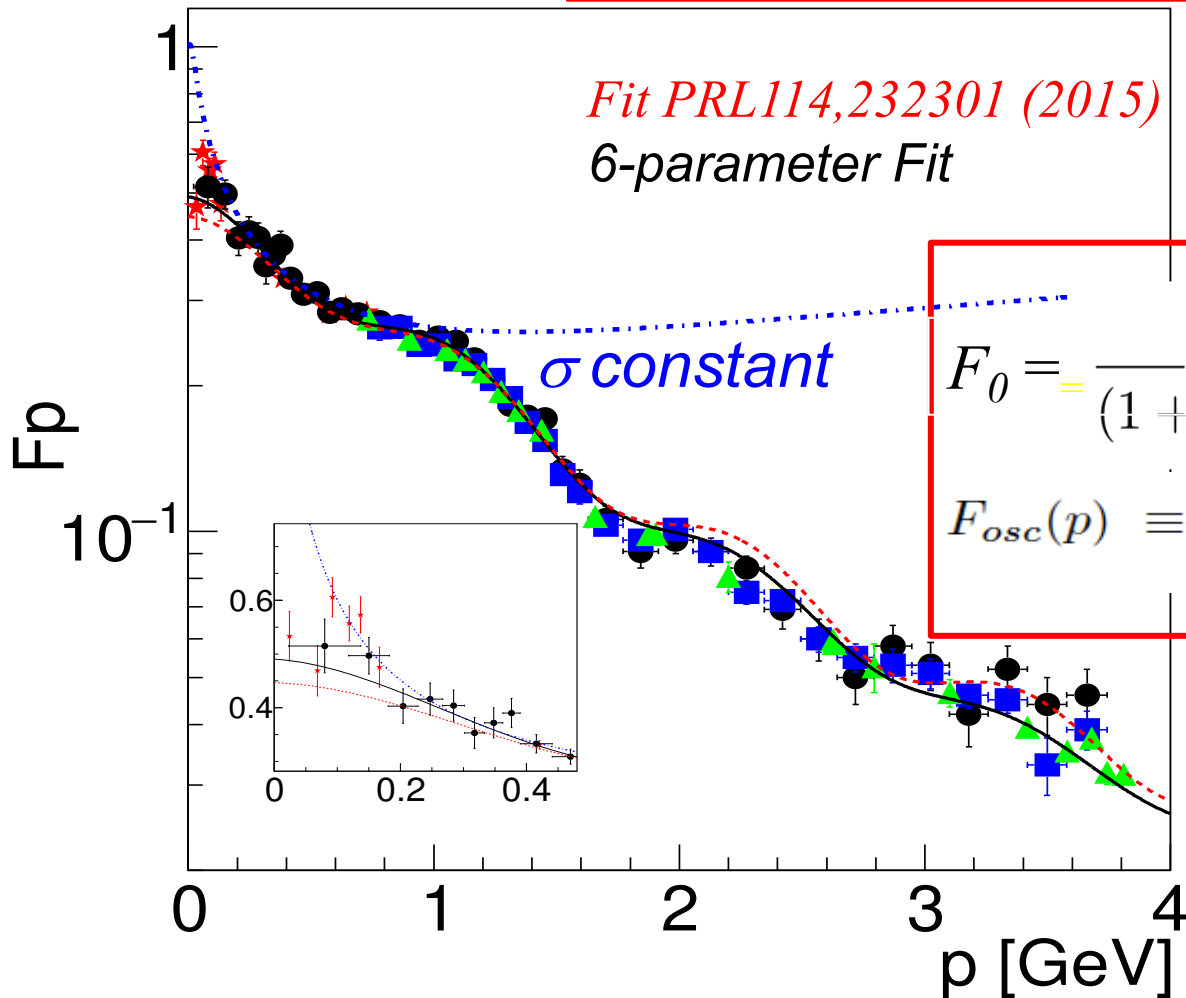
$$F_p(s)^2 = \frac{2\tau |G_M(s)|^2 + |G_E(s)|^2}{2\tau + 1}$$

Fit PRL114,232301 (2015)
6-parameter Fit

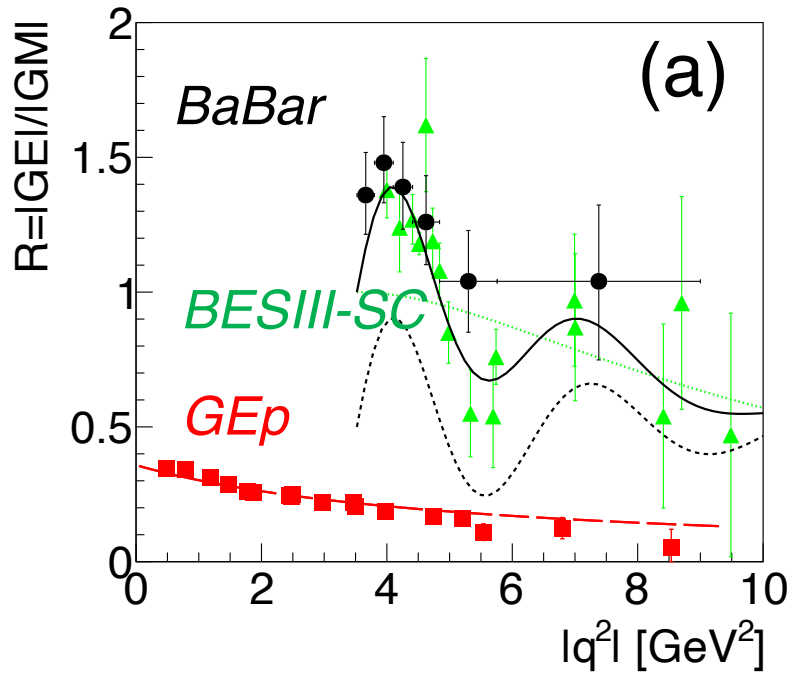
σ constant

$$F_0 = \frac{A}{(1 + q^2/m_a^2) [1 - q^2/0.71]^2},$$

$$F_{osc}(p) \equiv A \exp(-Bp) \cos(Cp + D).$$



Form Factor Ratio $R=|GE|/|GM|$



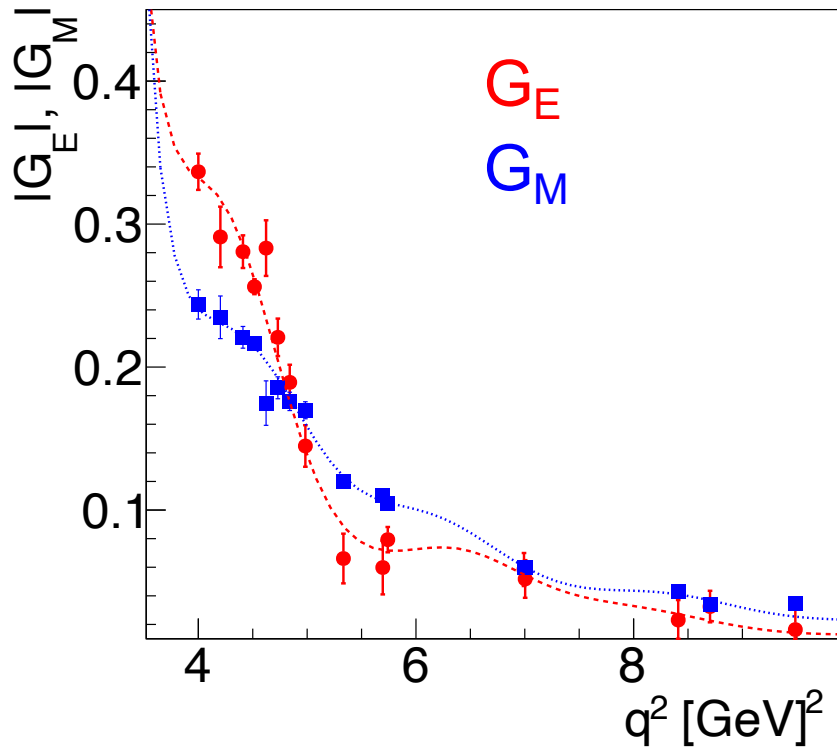
- Precise data from BESIII
- Dip at $|q^2| \sim 5.8$ GeV²
- Comparison with SL (Jlab-GEp data) – *fitted by a monopole*
- Oscillations on top of a monopole: from GE or GM?

$$F_R(\omega(s)) = \frac{1}{1 + \omega^2/r_0} [1 + r_1 e^{-r_2 \omega} \sin(r_3 \omega)], \quad \omega = \sqrt{s} - 2m_p,$$



Sachs form factors: $|G_E|$, $|G_M|$

From the fit on F_p and the fit on R ,
the Sachs FFs (moduli) can be reconstructed



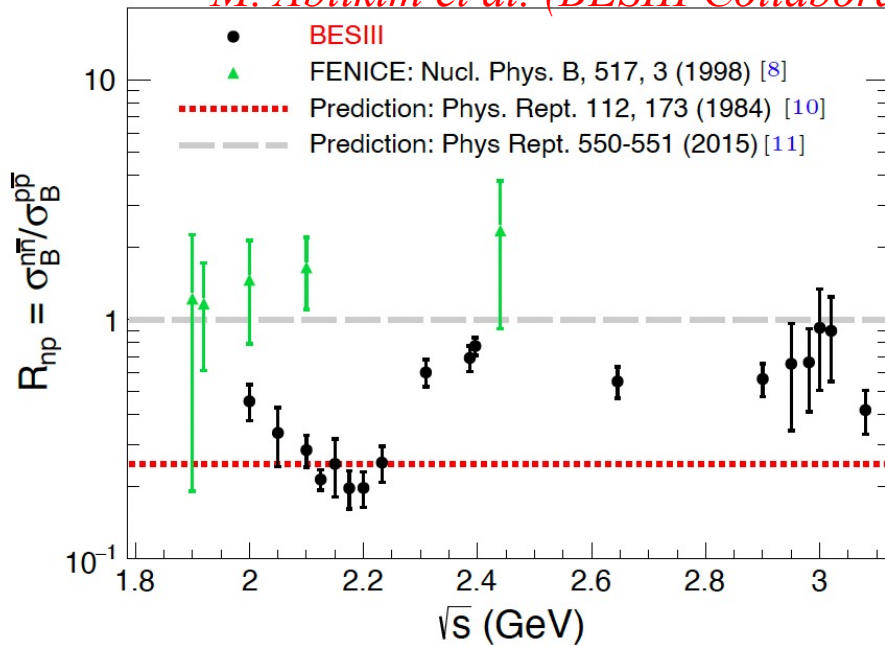
$$|G_E(s)| = F_p(s) \sqrt{\frac{1 + 2\tau}{R^2(s) + 2\tau/R^2(s)}}$$
$$|G_M(s)| = F_p(s) \sqrt{\frac{1 + 2\tau}{R^2(s) + 2\tau}}$$

Threshold constrain $R=1$ for $\tau=1$
The fit gives :
 $|G_E| = |G_M| = 0.48$



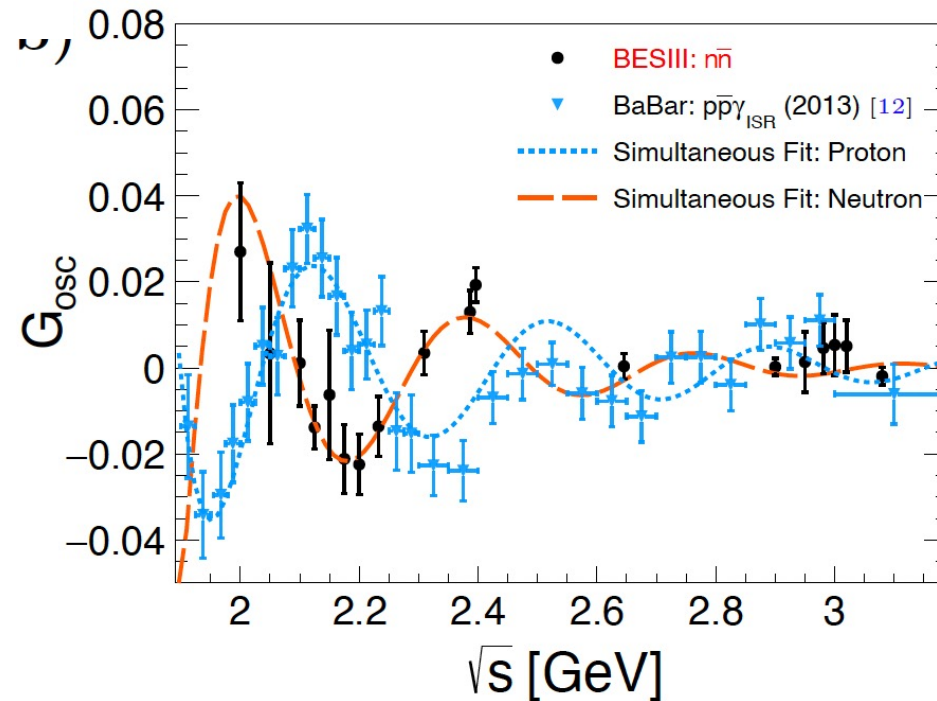
Neutron time-like form factor

M. Ablikim et al. (BESIII Collaboration), Nature Phys. 17, 1200 (2021)



$$R(n/p) < 1$$

Same 6 parameter fit
 Simultaneous fit p & n
 Same parameters but
 $\Delta\phi = 125^\circ \pm 12^\circ$



- Interfering amplitudes?

A. Bianconi, E.T-G., PRL 114,232301 (2015)

- $I=0,1$ channel mixing?

*X. Cao, J.-P. Dai, and H. Lenske
PRD 105 (2022) L071503*

- Resonances?

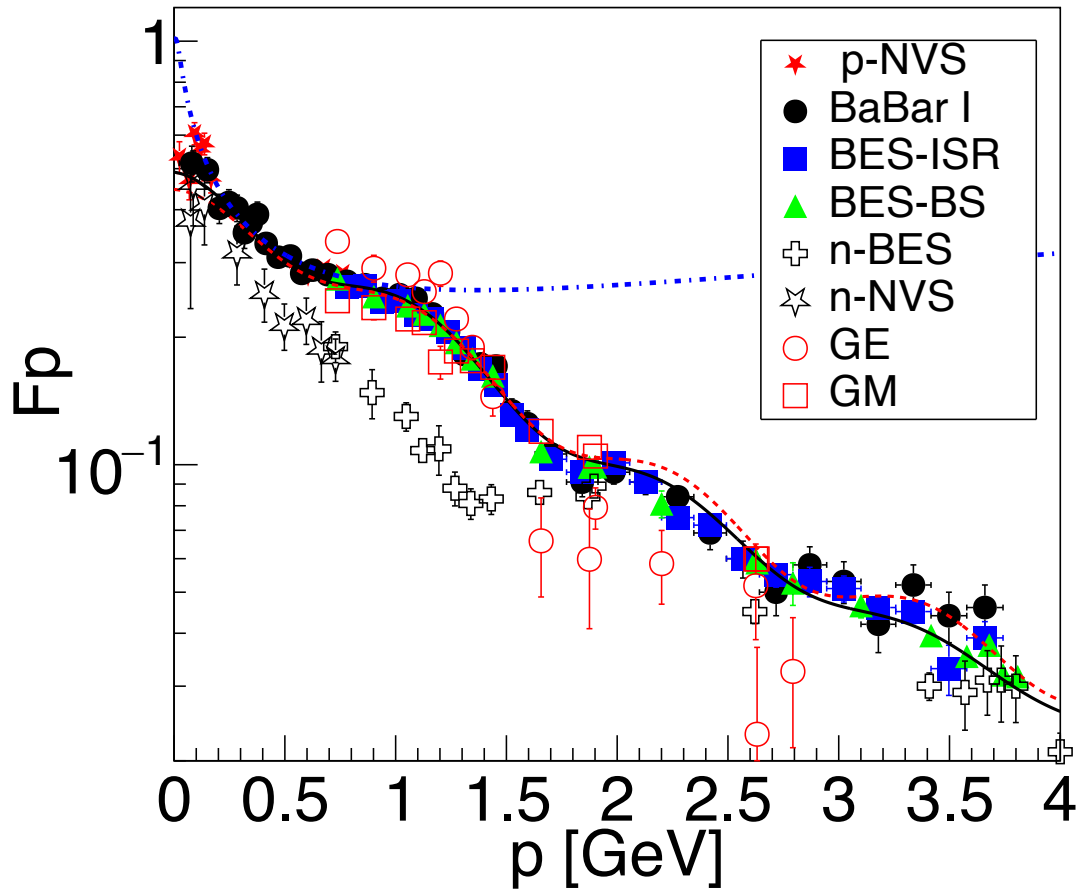
*H. Lin, H.-W. Hammer, and U.-G. Meissner,
P.R.L. 128, 052002 (2022)*



Proton & Neutron

Similar 6-parameter fit for p & n with a different phase

M. Ablikim et al. (BESIII Collaboration), Nature Phys. 17, 1200 (2021)

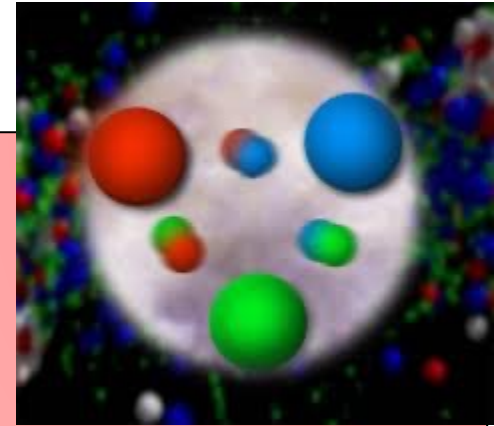


- Depends on background
- Gap between the points
- n-fit without Novosibirsk data



The nucleon according to *Арбуз*

It is generally assumed that the nucleon is composed by 3 valence quarks and a neutral sea of $q\bar{q}$ pairs



Nucleon: antisymmetric state of colored quarks

$$|p\rangle \sim \epsilon_{ijk} |u^i u^j d^k\rangle$$
$$|n\rangle \sim \epsilon_{ijk} |u^i d^j d^k\rangle$$

Main assumption of the *Арбуз* model:

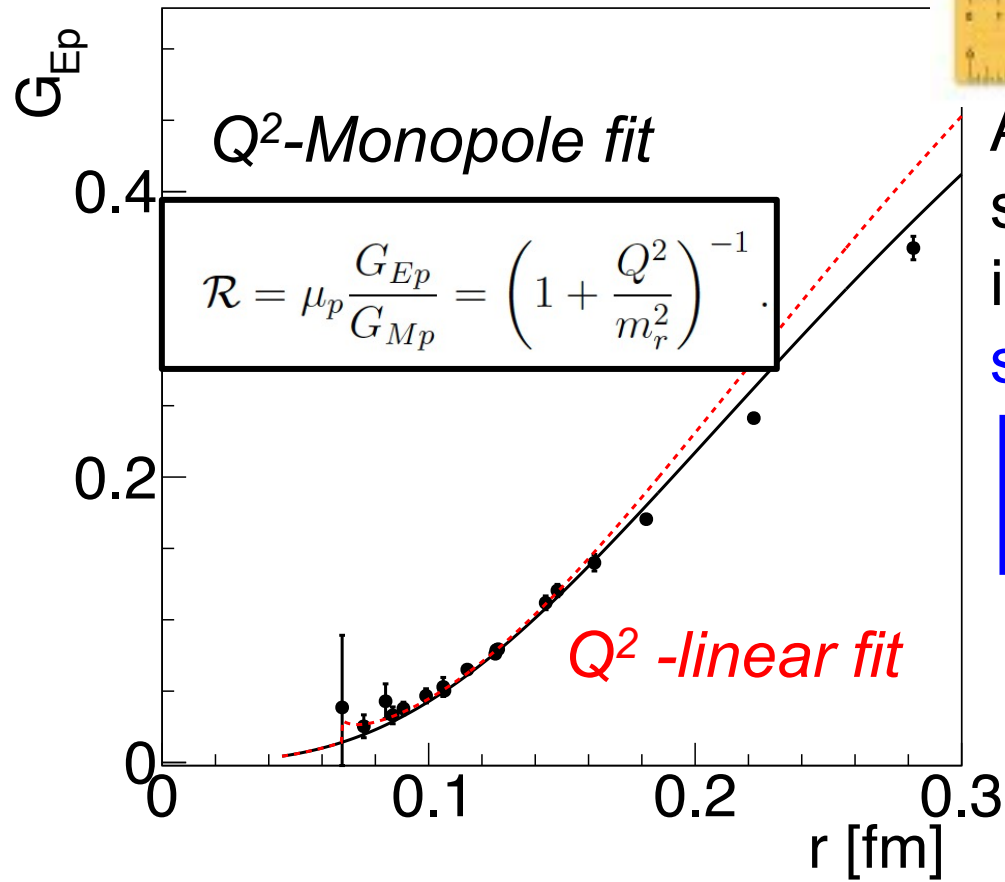
Does not hold in the spatial center of the nucleon: the center of the nucleon *is electrically neutral*, due to the strong gluonic field

Inner region: gluonic condensate of clusters with randomly oriented chromo-magnetic field (Vainshtein, 1982)

The color quantum number of quarks does not play any role, due to stochastic averaging. Pauli principle applies.



SL- the most precise ruler



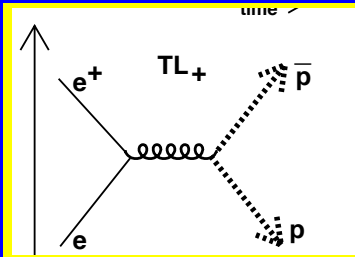
Additional suppression for the scalar part due to colorless internal region: “charge screening in a plasma”:

$$G_E(Q^2) = \frac{G_M(Q^2)}{\mu} \left(1 + Q^2/q_1^2\right)^{-1}$$

Zero crossing?
Prediction: NO

The photon ‘sees’ the neutral, screened region
 $G_{Ep} \approx 0$ for $r < 0.06$ fm

$$r \text{ [fm]} = \lambda = \hbar c / \sqrt{Q^2} = 0.197 \text{ [GeV fm]} / \sqrt{Q^2 \text{ [GeV]}},$$



Time-like region

Арбуз

Antisymmetric state
of colored quarks



Colorless quarks:
Pauli principle

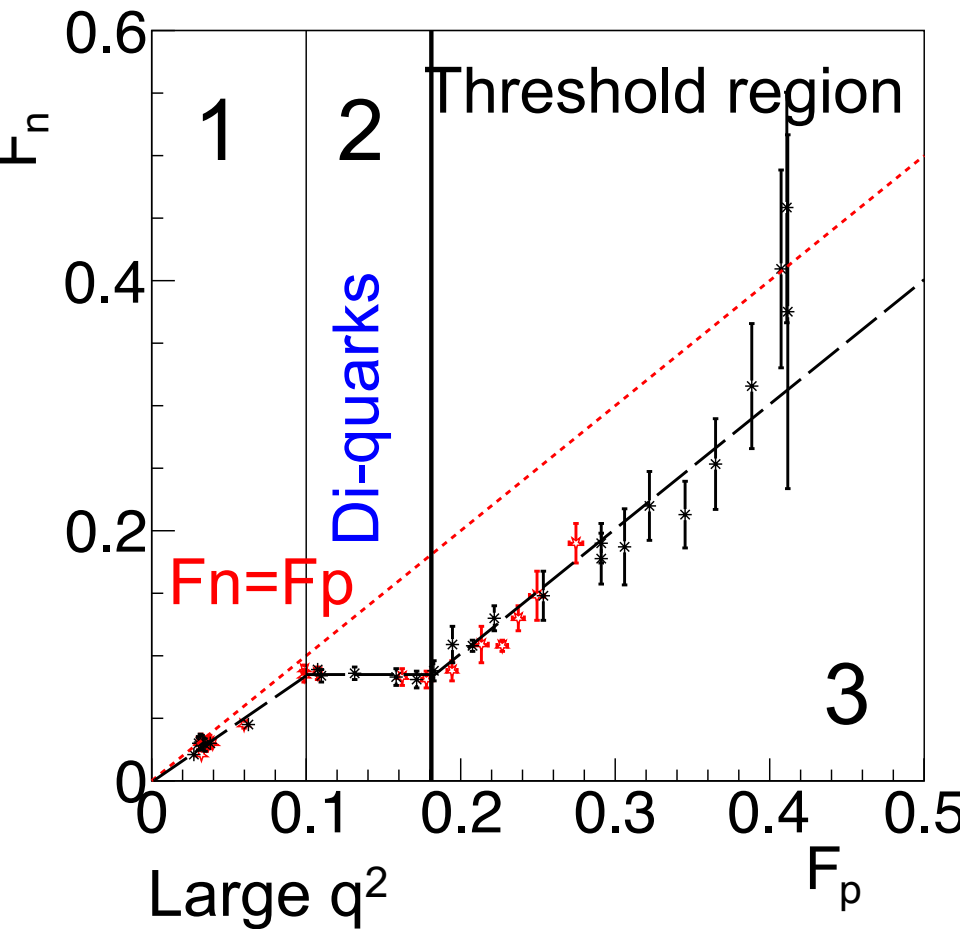
The vacuum state transfers all the released energy to a state of matter consisting at least of 6 massless valence quarks, a set of gluons, sea of $\bar{q}q$ with $q_0 > 2M_p$, $J=1$, dimensions $\hbar/(2M_p) \sim 0.1 \text{ fm}$.

- uu (dd) quarks are repulsed from the inner region
- The 3rd quark u (p) or d (n) is attracted by one of the identical quarks, forming *a compact di-quark: competition between attraction force and stochastic force of the gluon field*
- The color state is restored: the 'point-like' hadron expands and cools down: *the current quarks and antiquarks absorb gluons and transform into constituent quarks*

E.A. Kuraev, A. Dbeyssi, E. T-G. Phys. Lett. 712, 240 (2012)



TL - np-correlation : 3 steps



Experimental points at
the same P_L

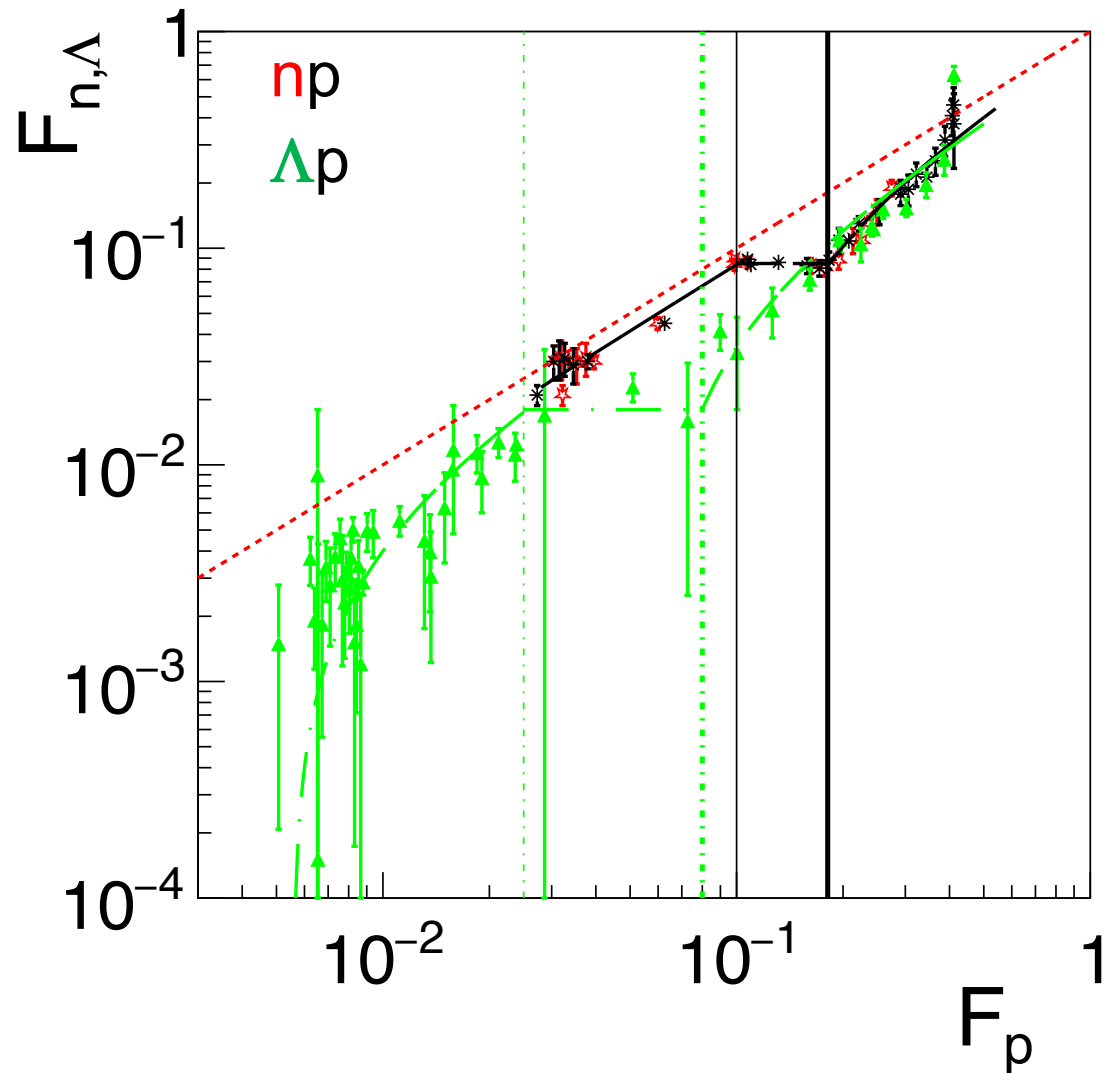
Proton values calculated
from the 6-parameter fit

- 1) pQCD applies
- 2) di-quark phase
charge redistributed
- 3) The hadron is formed

E.A. Kuraev, A. Dbeyssi, E. T-G. Phys. Lett. 712, 240 (2012)

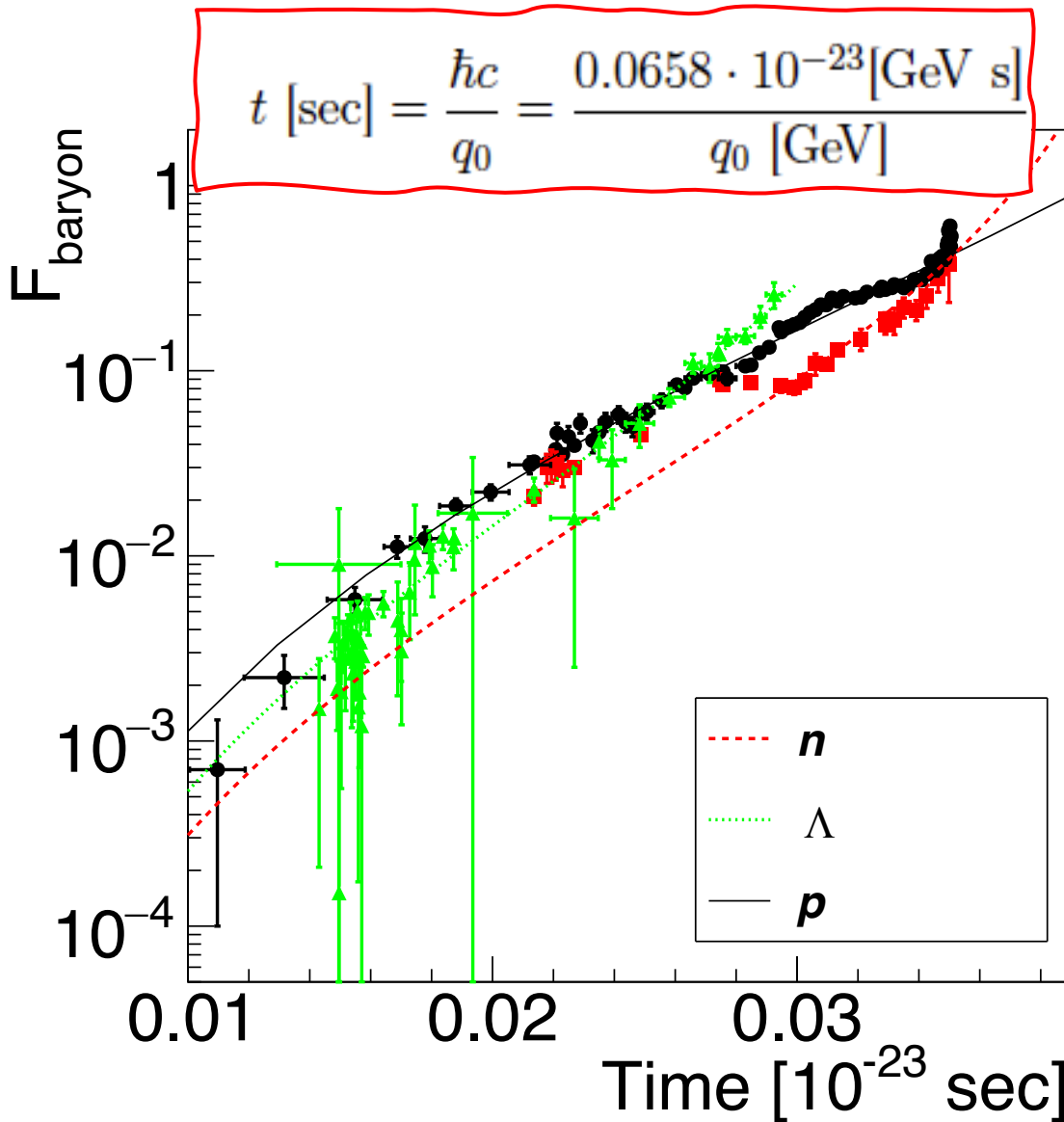


np Λ -correlation



Quark pairs created by quantum vacuum fluctuations: all quark flavors are equally probable, but, due to Heisenberg principle, the associated time depends on the energy (baryon mass)

TL- the most precise clock



10^{-23} s is the time for
light to cross a proton

Di-quark phase dominant
at $t \sim 0.02-0.03$ [10^{-23} s]



Summary & Conclusions

- BESIII new data on TL n & p FFs, their ratio and *first determination of individual proton TL FFs ($|G_E|$ and $|G_M|$)*
- *FFs ratio: damped oscillations around a monopole decrease*
- Oscillations more pronounced in $|G_E|$
- Origin of oscillatory phenomena :
Di-quark as a necessary step towards hadron creation?
- *Main features of the SL and TL FFs data qualitatively explained by the **Арбуз** model:*
 - The monopole-like decrease of the FF ratio
 - The formation of a di-quark component in the nucleon
 - The $np\Delta$ FFs correlation
- Predicts
 - similarities between n & p , SL & TL, non zero crossing in SL

Deepen quantitative aspects!



Thank you for your attention



Decreasing of the ratio G_E/G_M

Арбуз

Additional suppression for the scalar part due to colorless internal region: “charge screening in a plasma”:

$$\Delta\phi = -4\pi e \sum Z_i n_i, \quad n_i = n_{i0} \exp\left[-\frac{Z_i e \phi}{kT}\right]$$

Neutrality condition: $\sum Z_i n_{i0} = 0$

$$\Delta\phi - \chi^2 \phi = 0, \quad \phi = \frac{e^{-\chi r}}{r}, \quad \chi^2 = \frac{4\pi e^2 Z_i^2 n_{i0}}{kT}$$

Additional suppression
(Fourier transform)

$$G_E(Q^2) = \frac{G_M(Q^2)}{\mu} \left(1 + Q^2/q_1^2\right)^{-1}$$

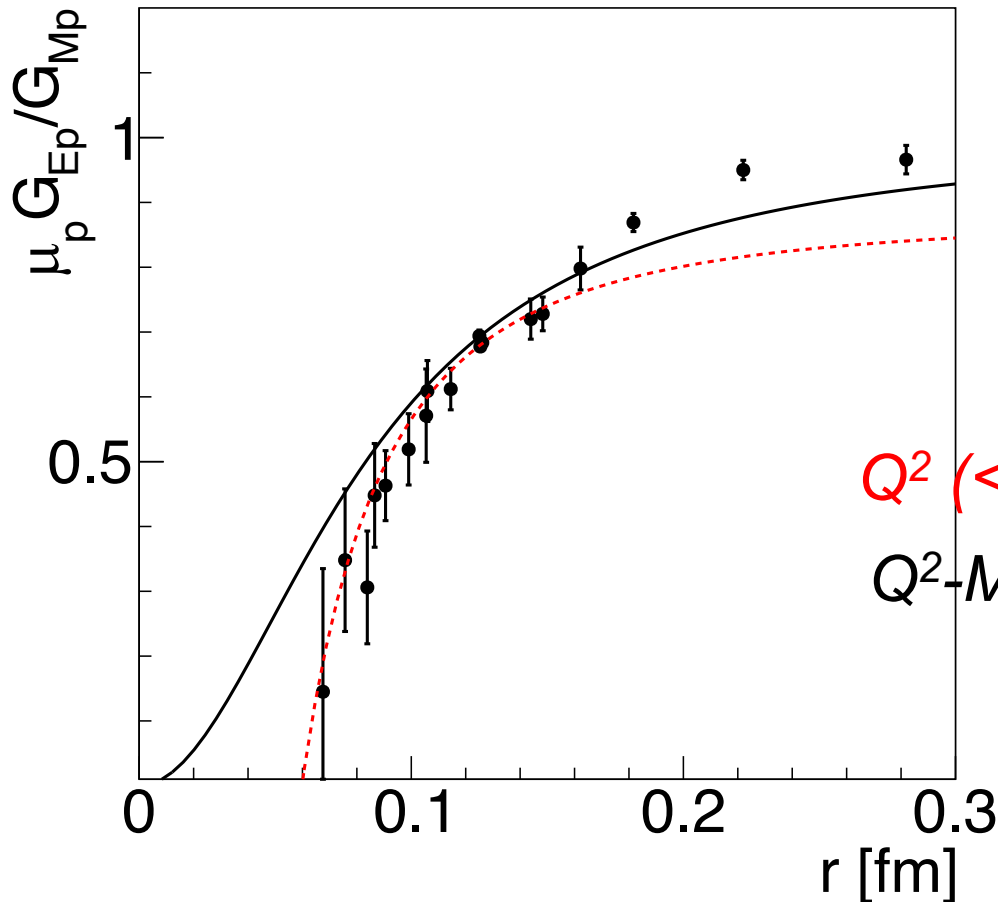
$q_1 (\equiv \chi)$

fitting parameter



SL Form Factors Ratio

Large $Q^2 \rightarrow$ Small r



$$\mathcal{R} = \mu_p \frac{G_{Ep}}{G_{Mp}} = \left(1 + \frac{Q^2}{m_r^2}\right)^{-1}.$$

$Q^2 (< 0.15 \text{ GeV}^2)$ – linear fit

Q^2 -Monopole fit

$$r \text{ [fm]} = \lambda = \hbar c / \sqrt{Q^2} = 0.197 \text{ [GeV fm]} / \sqrt{Q^2 \text{ [GeV]}},$$



The nucleon

Inner region: gluonic condensate of clusters with randomly oriented chromo-magnetic field (Vainshtein, 1982, instanton model)

Intensity of the gluon field in vacuum:

$$\langle 0 | \alpha_s / \pi (G_{\mu\nu}^a)^2 | 0 \rangle \sim E^2 - B^2 \sim E^2 = 0.012 \text{ GeV}^4.$$

$$G^2 \simeq 0.012 \pi / \alpha_s \text{ GeV}^4, \text{ i.e., } E \simeq 0.245 \text{ GeV}^2, \quad \alpha_s / \pi \sim 0.1$$

In the internal region of strong chromo-magnetic field, **the color quantum number of quarks does not play any role**, due to stochastic averaging

$$\langle G | u^i u^j | G \rangle \sim \delta_{ij} \begin{array}{l} \text{proton} \\ \text{neutron} \end{array}$$

$d^i d^j$

*Colorless quarks:
Pauli principle*



Antisymmetric state
of colored quarks



*Colorless quarks:
Pauli principle*

- 1) uu (dd) quarks are repulsed from the inner region
- 2) The 3rd quark is attracted by one of the identical quarks, forming a compact di-quark
- 3) The color state is restored

Formation of di-quark: competition between attraction force and stochastic force of the gluon field

$$\frac{Q_q^2 e^2}{r_0^2} > e|Q_q| E.$$

isolated quark

proton: (u) $Q_q = +1/3$
neutron: (d) $Q_q = -2/3$

attraction force > stochastic force of the gluon field



QCD-Counting rules

V. A. Matveev, R.M. Muradian, A.N. Tavkhelidze, Nuovo Cimento Lett. 7 (1973) 719
S.J. Brodsky, G.R. Farrar, Phys. Rev. Lett. 31 (1973) 1153.

$$G_M^{(p,n)}(Q^2) = \mu G_E(Q^2);$$

$$G_E^{(p,n)}(Q^2) = G_D(Q^2) = \left[1 + Q^2/(0.71 \text{ GeV}^2)\right]^{-2}$$

Normalization: $G_E^{(p,n)}(0) = 1, 0, G_M^{(p,n)}(0) = \mu_{p,n}$

Quark counting rules apply to the vector part of the potential



The annihilation channel:

$$e^+ + e^- \rightarrow \gamma^*(q) \rightarrow p + \bar{p}$$

1) Creation of a $p\bar{p}$ state through $^3S_1 = \langle 0 | J^\mu | p\bar{p} \rangle$ intermediate state with $q = (\sqrt{q^2}, 0, 0, 0)$.

2) The vacuum state transfers all the released energy to a state of matter consisting of:

- 6 massless valence quarks
- Set of gluons
- Sea of current ($q\bar{q}$) -pairs of quarks- with energy $q_0 > 2M_p$, $J=1$, dimensions $\hbar/(2M_p) \sim 0.1 \text{ fm}$.

3) Pair of p and \bar{p} formed by three bare quarks:

- Structureless
- Colorless



pointlike FFs !!!



The annihilation channel: $e^+ + e^- \rightarrow \gamma^*(q) \rightarrow p + \bar{p}$.

- The point-like hadron pair expands and cools down: the current quarks and antiquarks absorb gluon and transform into constituent quarks

- The residual energy turns into kinetic energy of the motion with relative velocity $2\beta = 2 \sqrt{1 - 4M_p^2/q_0^2}$.

- The strong chromo-EM field leads to an effective loss of color. Fermi statistics: identical quarks are repulsed. The remaining quark of different flavor is attracted to one of the identical quarks, creating a compact diquark (du -state)



The annihilation channel: $e^+ + e^- \rightarrow \gamma^*(q) \rightarrow p + \bar{p}$.

The repulsion of p and \bar{p} with kinetic energy

Арбуз

$$T = \sqrt{q^2} - 2M_p c^2$$

is balanced by the confinement potential

$$q_0 - 2M_p c^2 = (k/2)R^2$$

- The long range color forces create a stable colorless state of proton and antiproton
- The initial energy is dissipated from current to constituent quarks originating on shell $\bar{p}p$ separated by a distance R .



The annihilation channel: $e^+ + e^- \rightarrow \gamma^*(q) \rightarrow p + \bar{p}$.

At larger distances, the inertial force exceeds the confinement force: p and \bar{p} start to move apart with relative velocity β

p and \bar{p} leave the interaction region: at larger distances the integral of $Q(t)$ must vanish

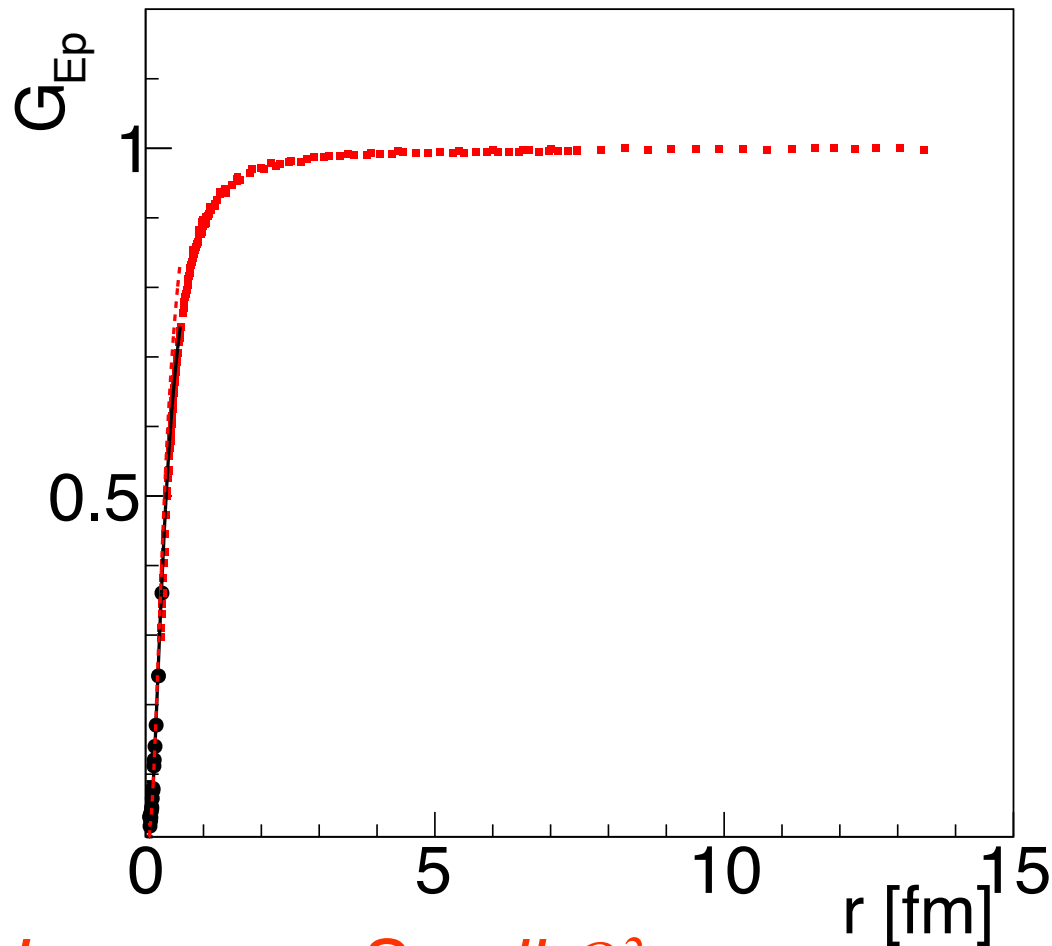
For very small values of the velocity $\alpha\pi/\beta \simeq 1$ FSI lead to the creation of a bound $N\bar{N}$ system

Арбуз



Proton radius

*Data from Mainz,
PRC 90, 015206 (2014)*

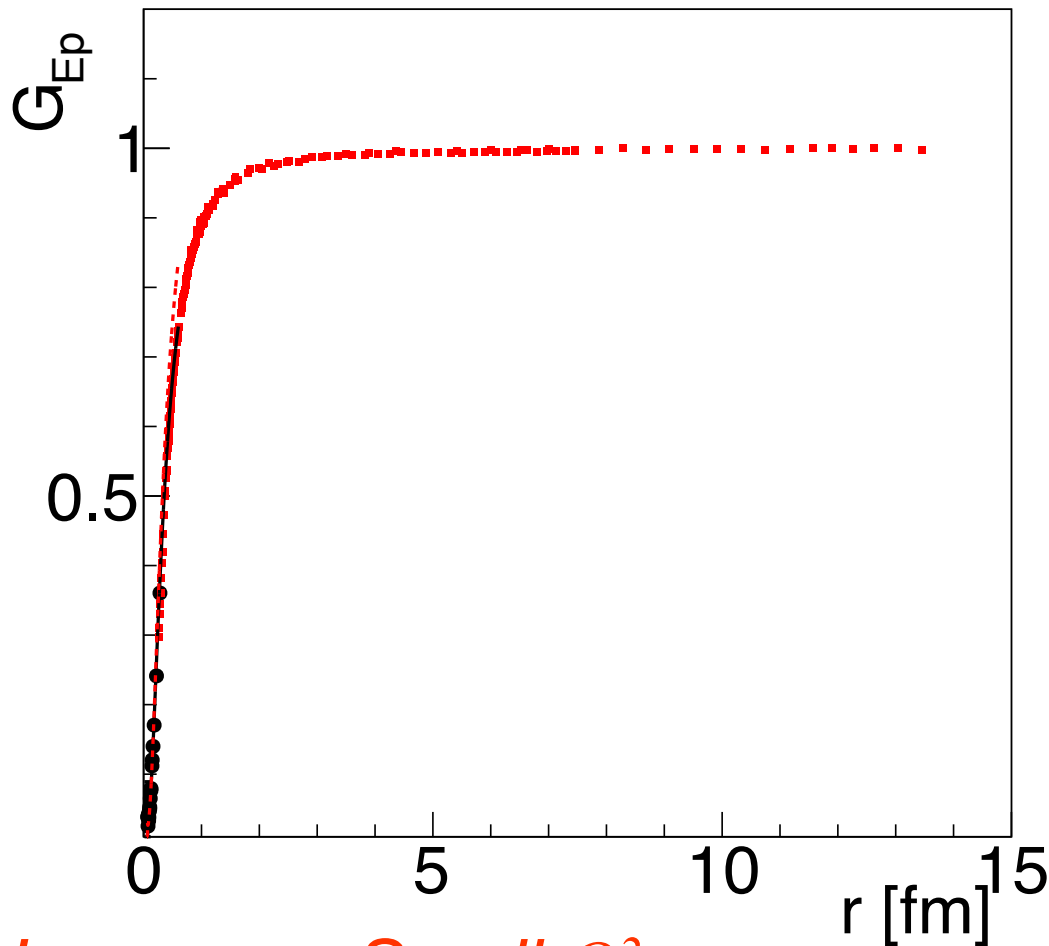


Large $r \rightarrow$ Small Q^2



Proton radius

Data from Mainz, CLAS...



How can a photon with wavelength ~ 15 fm distinguish between a proton size of 0.84 or 0.87 fm?

Large $r \rightarrow$ Small Q^2



Plan

- *Definition of form factors in space and time-like regions*
- *new data in SL and TL*
- Nucleon Structure
- Time **Evolution of hadron formation**
- proton, neutron and hyperon FF correlation

What can we learn from time-like processes?



Symmetry Relations(annihilation)

- Differential cross section at complementary angles:

The SUM cancels the 2γ contribution:

$$\frac{d\sigma_+}{d\Omega}(\theta) = \frac{d\sigma}{d\Omega}(\theta) + \frac{d\sigma}{d\Omega}(\pi - \theta) = 2\frac{d\sigma^{Born}}{d\Omega}(\theta)$$

The DIFFERENCE enhances the 2γ contribution:

$$\frac{d\sigma_-}{d\Omega}(\theta) = \frac{d\sigma}{d\Omega}(\theta) - \frac{d\sigma}{d\Omega}(\pi - \theta) = 4N \left[(1 + x^2) \text{Re}G_M \Delta G_M^* + \right. \\ \left. + \frac{1 - x^2}{\tau} \text{Re}G_E \Delta G_E^* + \sqrt{\tau(\tau - 1)} x (1 - x^2) \text{Re}\left(\frac{1}{\tau} G_E - G_M\right) F_3^* \right]$$

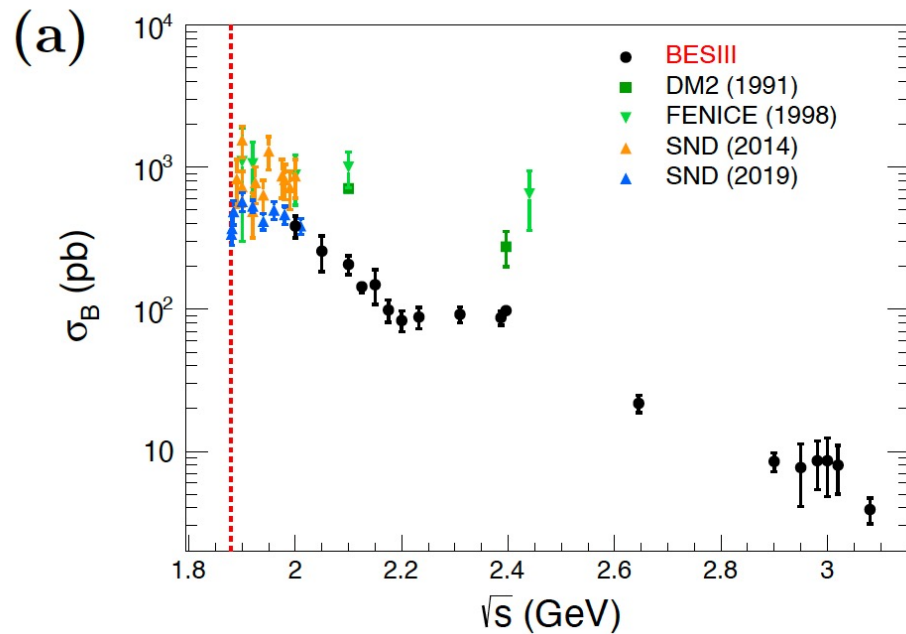
$$\tau = \frac{q^2}{4m^2}, \quad x = \cos\theta$$



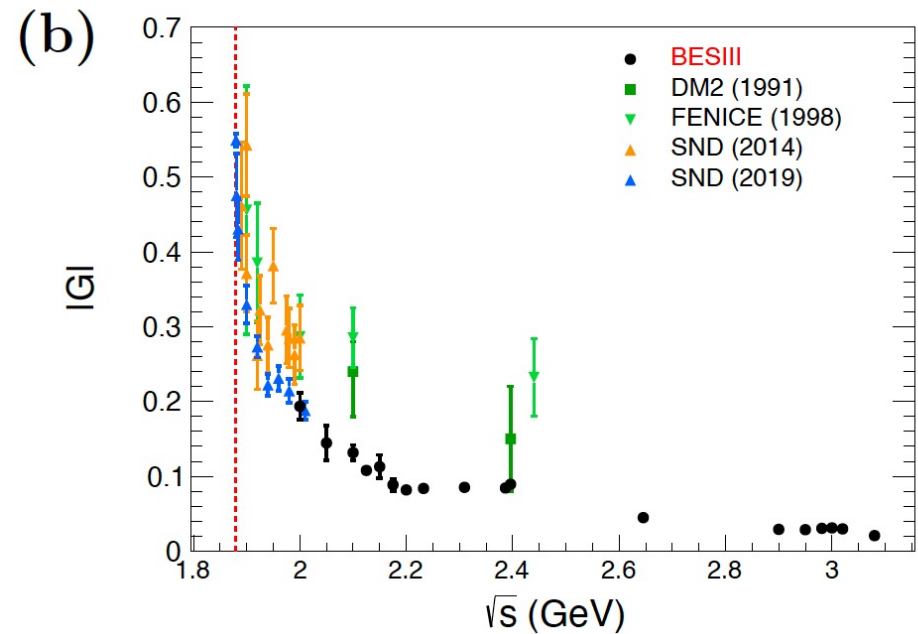
Neutron time-like form factor

M. Ablikim et al. (BESIII Collaboration), Nature Phys. 17, 1200 (2021)

Cross section $e^+e^- \rightarrow n\bar{n}$



Form factor



Time-like observables: $|G_E|^2$ and $|G_M|^2$

-The cross section for $\bar{p} + p \rightarrow e^+ + e^-$ (1 γ -exchange):

$$\frac{d\sigma}{d(\cos\theta)} = \frac{\pi\alpha^2}{8m^2\sqrt{\tau-1}} [\tau|G_M|^2(1 + \cos^2\theta) + |G_E|^2\sin^2\theta]$$

θ : angle between e^- and \bar{p} in cms.

A. Zichichi, S. M. Berman, N. Cabibbo, R. Gatto, Il Nuovo Cimento XXIV, 170 (1962)

B. Bilenkii, C. Giunti, V. Wataghin, Z. Phys. C 59, 475 (1993).

G. Gakh, E.T-G., Nucl. Phys. A761,120 (2005).

As in SL region:

- Dependence on q^2 contained in FFs
- Even dependence on $\cos^2\theta$ (1 γ exchange)
- No dependence on sign of FFs
- Enhancement of magnetic term

but TL form factors are complex!



Conclusions

- *High order radiative corrections* are mandatory to claim a percent precision on the observables
- Effects as *correlations and normalizations* should be carefully scrutinized
see GEp as a parameter
 ε -derivative of the reduced elastic cross section
- *Two photon exchange as K-factor*

Radiative corrections modify not only the absolute values but also the dependence of the observables on the relevant kinematical variables



Unpolarized cross section

-The cross section for $\bar{p} + p \rightarrow e^+ + e^-$ (1 γ -exchange):

$$\frac{d\sigma}{d(\cos\theta)} = \frac{\pi\alpha^2}{8m^2\sqrt{\tau-1}} [\tau|G_M|^2(1 + \cos^2\theta) + |G_E|^2\sin^2\theta]$$

θ : angle between e^- and \bar{p} in cms.

Two Photon Exchange:

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2}{4q^2} \sqrt{\frac{\tau}{\tau-1}} D$$

- Induces four new terms
- Odd function of θ :
- Does not contribute at $\theta=90^\circ$

$$D = (1 + \cos^2\theta)(|G_M|^2 + 2\text{Re}G_M\Delta G_M^*) + \frac{1}{\tau} \sin^2\theta(|G_E|^2 + 2\text{Re}G_E\Delta G_E^*) + 2\sqrt{\tau(\tau-1)} \cos\theta \sin^2\theta \text{Re}\left(\frac{1}{\tau}G_E - G_M\right)F_3^*$$

M.P. Rekalo and E. T.-G., EPJA 22, 331 (2004)

G.I. Gakh and E. T.-G., NPA761, 120 (2005)

