



# Recent development in understanding of hadron spectra

MISHA MIKHASENKO

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IWHSS 2022  
CERN Globe

# Variety of the hadronic states

QCD at low-energy regime:

- color interaction confined
- effective d.o.f. - **constituent** quarks (gluons?)

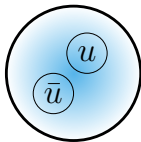
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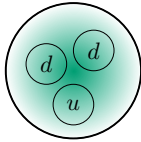
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Ordinary matter:

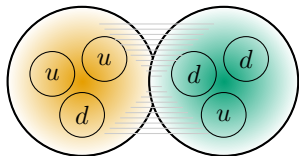
QUARKS	mass →	~2.3 MeV/c <sup>2</sup>	~1.275 GeV/c <sup>2</sup>	~173.07 GeV/c <sup>2</sup>
	charge →	2/3	2/3	2/3
	spin →	1/2	1/2	1/2
		<b>u</b>	<b>c</b>	<del><b>t</b></del>
		up	charm	top
	mass →	~4.8 MeV/c <sup>2</sup>	~95 MeV/c <sup>2</sup>	~4.18 GeV/c <sup>2</sup>
	charge →	-1/3	-1/3	-1/3
	spin →	1/2	1/2	1/2
		<b>d</b>	<b>s</b>	<b>b</b>
		down	strange	bottom



meson



baryon



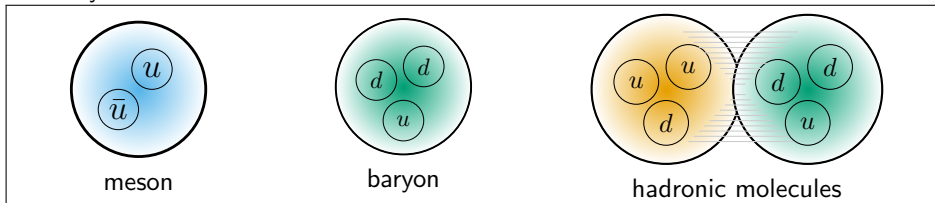
hadronic molecules

# Variety of the hadronic states

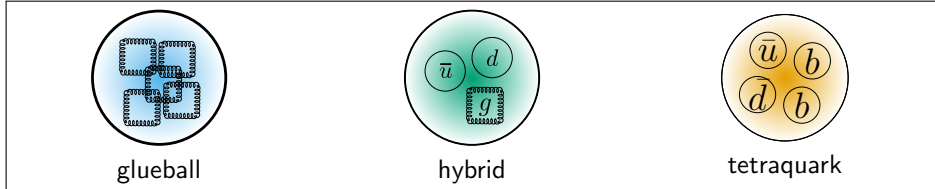
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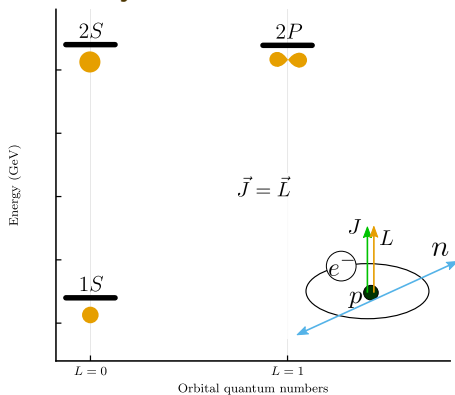
Exotic matter:



	mass $\rightarrow$ $\approx 2.3$ MeV/c <sup>2</sup>	$\approx 1.275$ GeV/c <sup>2</sup>	$\approx 173.07$ GeV/c <sup>2</sup>
charge $\rightarrow$	$2/3$	$2/3$	$2/3$
spin $\rightarrow$	$1/2$	$1/2$	$1/2$
	<b>u</b> up	<b>c</b> charm	<del><b>t</b></del> top
<b>QUARKS</b>	$\approx 4.8$ MeV/c <sup>2</sup>	$\approx 95$ MeV/c <sup>2</sup>	$\approx 4.18$ GeV/c <sup>2</sup>
	$-1/3$	$-1/3$	$-1/3$
	$1/2$	$1/2$	$1/2$
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom

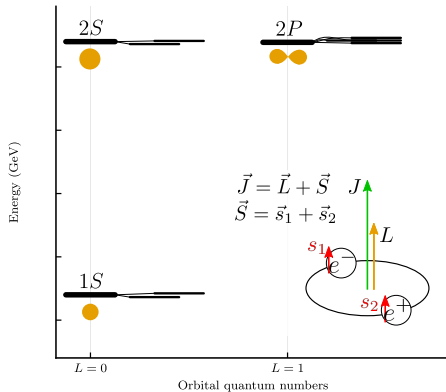
# Why there are so many hadrons?

QED



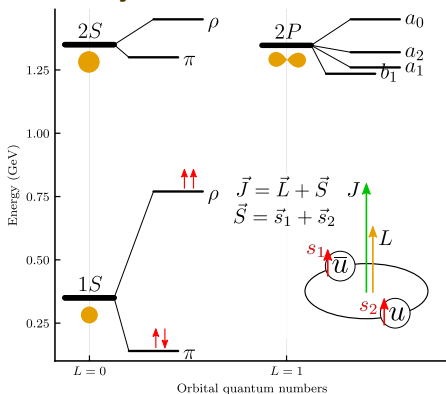
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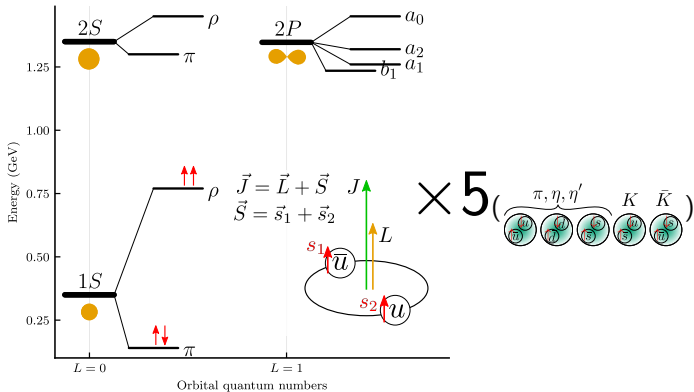
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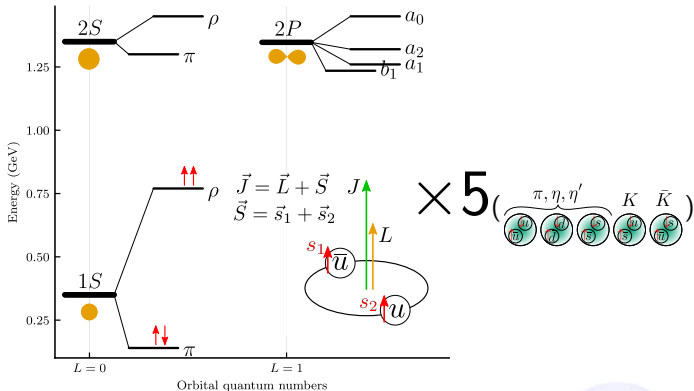
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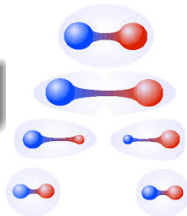
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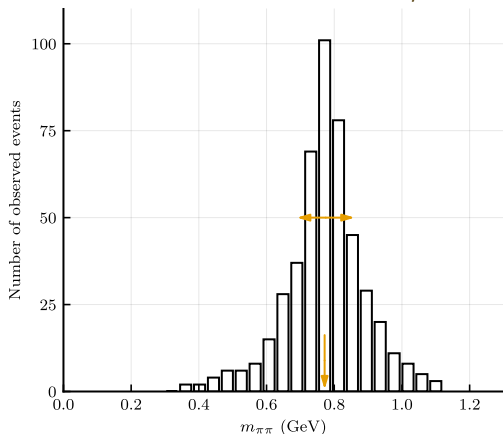


- $(\pi, \rho), (K, K^*), (\eta_c, J/\psi)$  are the lowest  $1S$  states ( $\downarrow\uparrow, \uparrow\uparrow$ ) of the families.

**Goal:** identify excitation of ordinary systems, find exotic formations



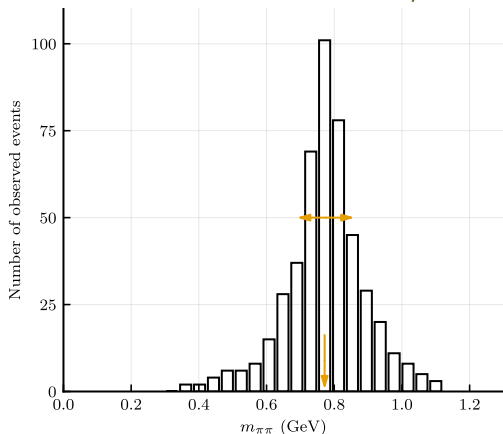
# Invariant-mass distribution, resonances



Hadronic state is a particle

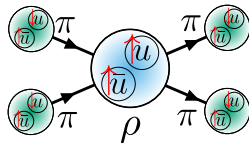
- charact. by **mass** (energy) and **width** (lifetime)

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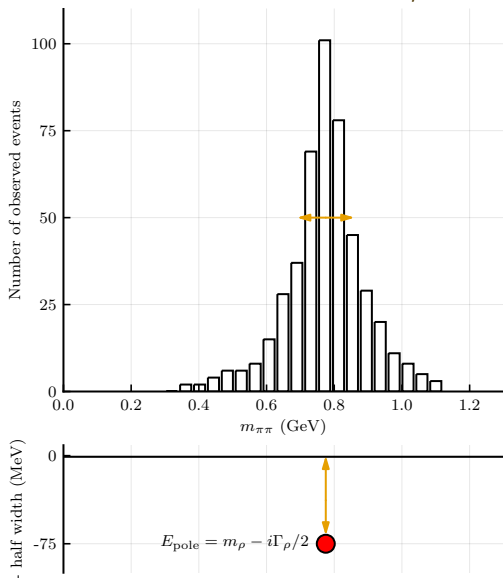
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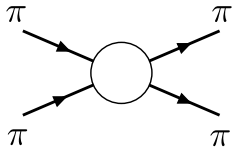
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- Read  $m$ ,  $\Gamma$  from spectrum

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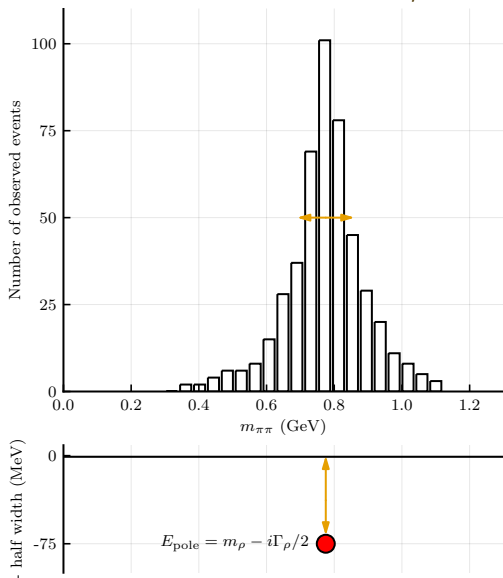
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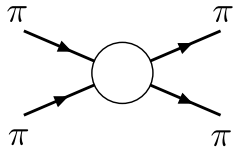
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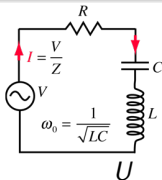


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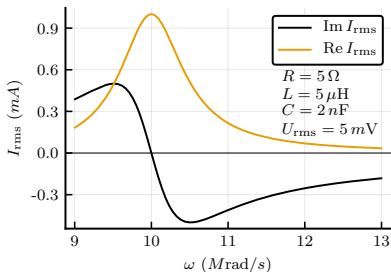
- resonances are **poles** of scattering amplitude.

# Hadron resonances are resonances

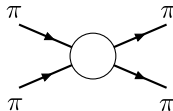
## Electric circuit



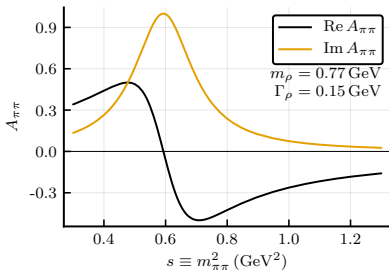
$$I_{\text{rms}} = \frac{U}{R + iL\omega - \frac{i}{C\omega}}$$

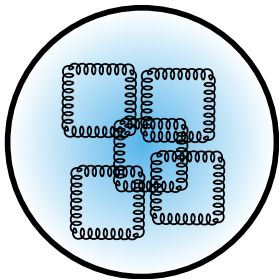


## Scattering



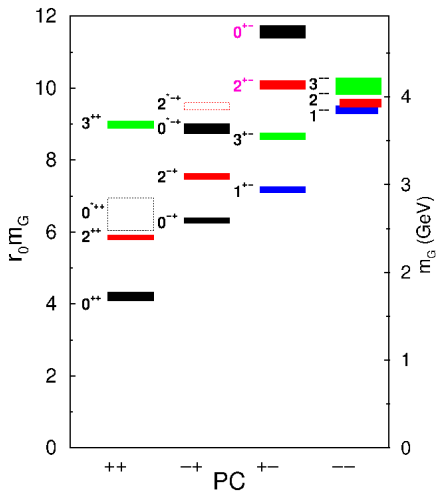
$$A_{\pi\pi} = \frac{m\Gamma}{m^2 - s - im\Gamma}$$





# Glueballs

# States in pure Yang-Mills



[Morningstar-Pearson, PRD60 (1999) 034509]

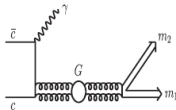
$$\mathcal{L}_{\text{YM}} = -\frac{1}{4} F_{\mu\nu}^2$$

- The self-interaction between gluons leads to the prediction of glueballs
- $0^{++}$  is the lowest state,  $m(G) \sim 1.7 - 2 \text{ GeV}$   
[Chen et al., PRD73 (2006) 014516],  
[Huber et al., EPJC 80 (2020) 1077],  
[Szczepaniak-Swanson, PLB (2003) 577]
- The clearest sign of the confinement
- The worst state to search in real life due to large mixing with quark states



$$J/\psi \rightarrow \gamma \pi^0 \pi^0 \text{ and } \rightarrow \gamma K_S^0 K_S^0$$

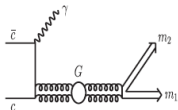
[JPAC, EPJC 82 (2022) 1, 80]



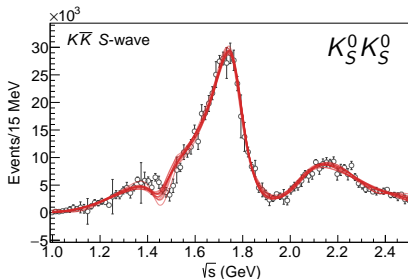
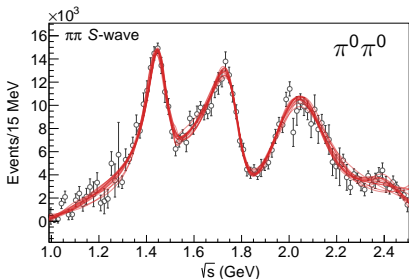
- Gluon-rich process, expected to be the golden channel for the search of the scalar glueball
- BESIII data [PRD98 (2018) 072003; PRD92 (2015) 052003]

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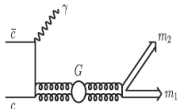
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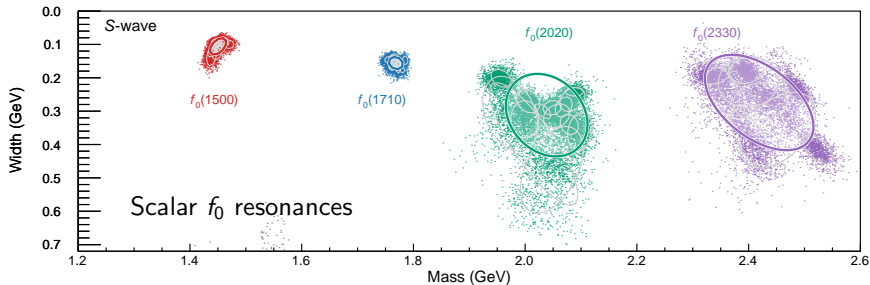
Large production coupling of  $f_0(1710)$  suggests it to have sizable glueball components

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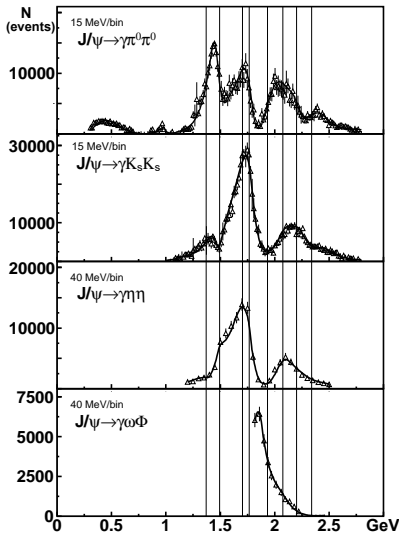
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# Production of scalar mesons via glueball component

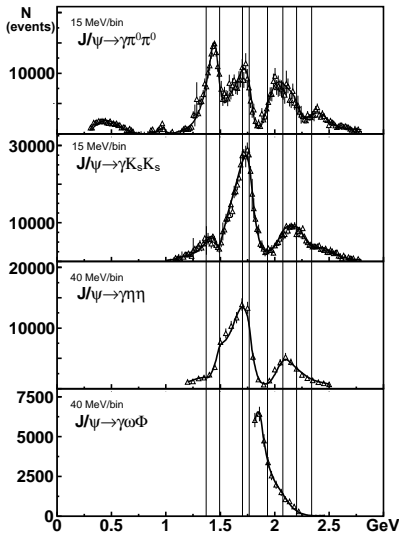
[Bonn-Gatchina group, PLB816 (2021) 136227]



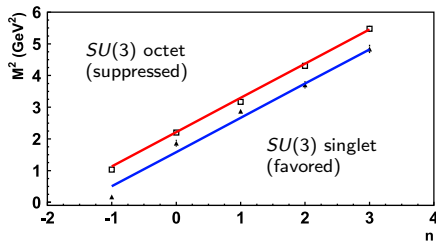
- Combined analysis of enormous dataset:  $\pi\pi$ ,  $K\bar{K}$ ,  $\eta\eta$ , and  $\phi\omega$ , + 15  $\bar{p}N$  annihilation reactions.

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[Bonn-Gatchina group, PLB816 (2021) 136227]

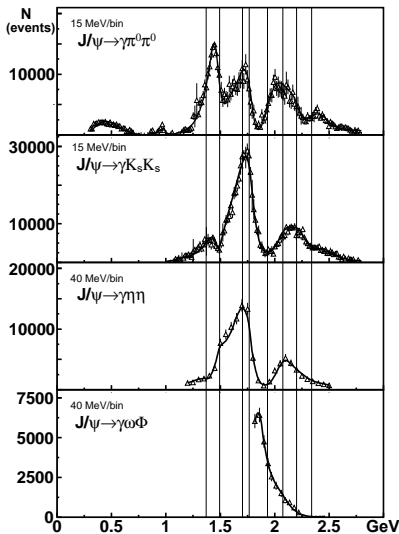


- Combined analysis of enormous dataset:  $\pi\pi$ ,  $K\bar{K}$ ,  $\eta\eta$ , and  $\phi\omega$ , + 15  $\bar{p}N$  annihilation reactions.
- 10 scalar mesons guided by the radial-exc. trajectories

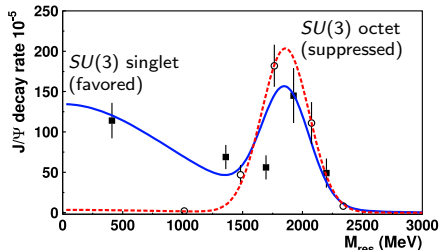


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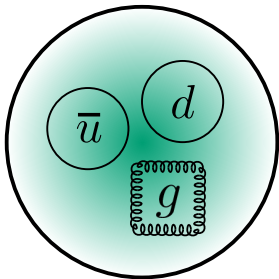
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“Fragmented glueball”:

- No extra state, shares scalar-resonance w.functions

# Hybrids

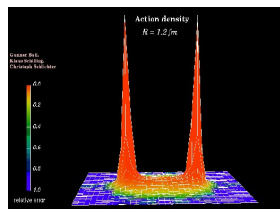
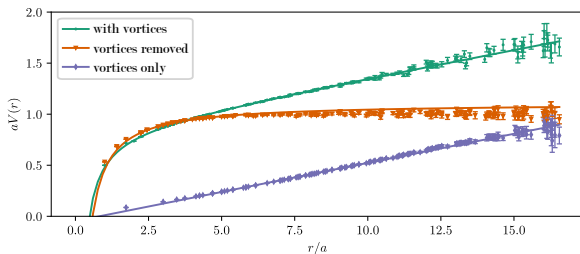


# Hybrids

# Vortices and QCD confinement

[Greensite, PPNP51 (2003) 1]

- The self-interactions of gluons cause formation of  $q\bar{q}$  and  $g$  condensates
- Many structures in QCD vacuum fields:
  - ▶ instantons, merons, abelian monopoles, **centre vortices**



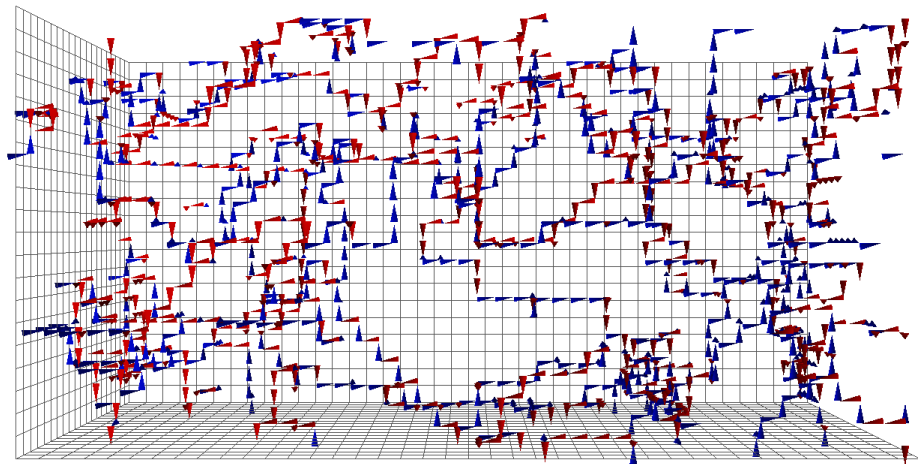
**Centre vortices** capture the essence of nonperturbative QCD:

- cause the confinement
- lead to dynamical generation of the mass



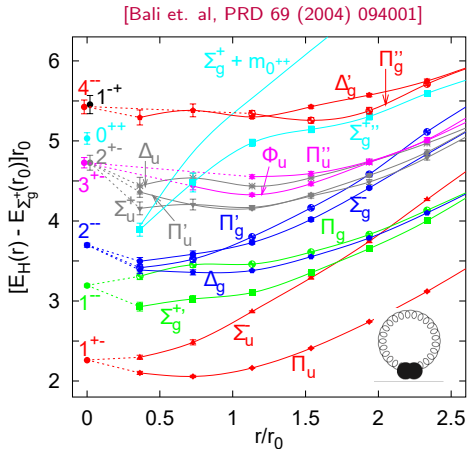
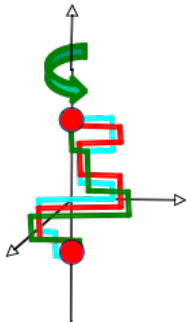
# Vortices flow in QCD vacuum

[Adelaide group]



# Constituent gluons

- Physical quarks appear to move in the gluon-field condensate
- The condensate can be **excited** leading to effective (constituent) gluons



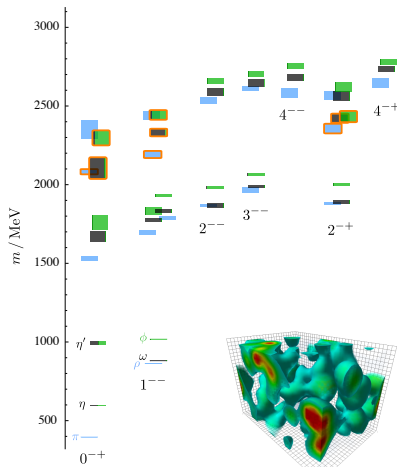
The lowest state is  $J^{PC} = 1^{+-}$

Gluons behave as quasiparticles with  $1^{+-}$

[Krupinski-Szczepaniak, PRD73 (2006) 116002]

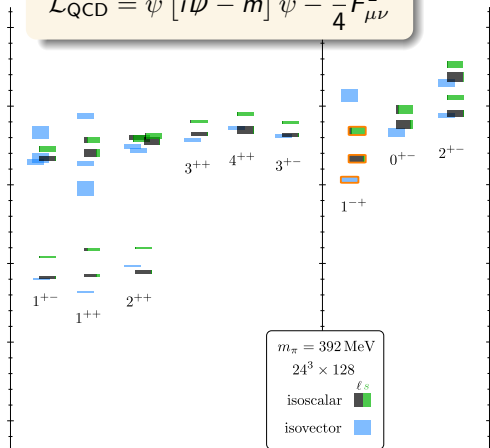
# Hybrid multiplets from Lattice

[Dudek et al., PRD 88, 094505 (2013)]



[D. Leinweber et al,  
CSSM Visualisation]

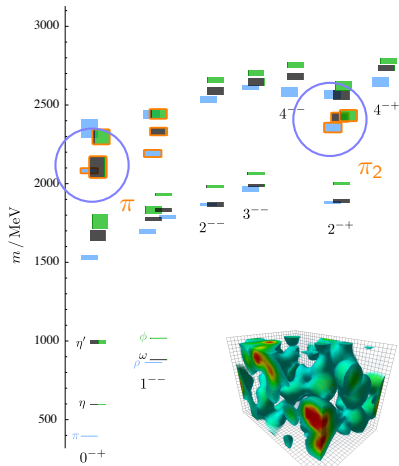
$$\mathcal{L}_{\text{QCD}} = \bar{\psi} [i\not{D} - m] \psi - \frac{1}{4} F_{\mu\nu}^2$$



mass of pion is 391 MeV

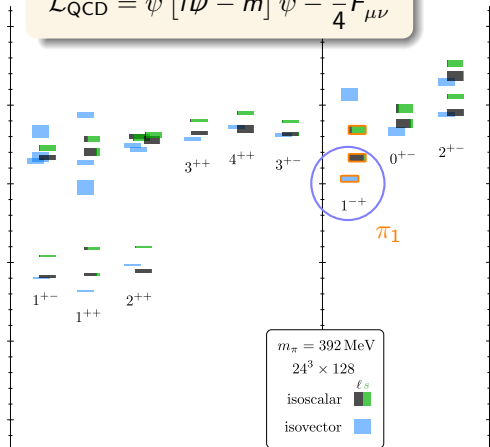
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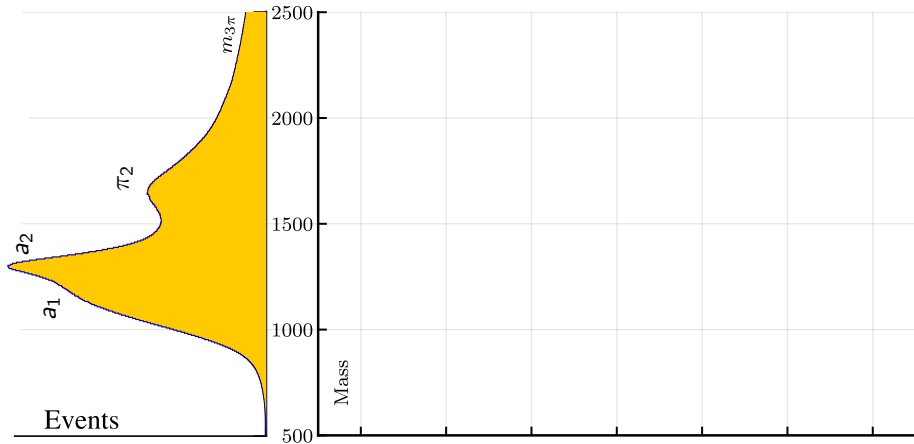
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# Diffractive production of $3\pi$ states

[COMPASS, PRD95 (2017) 032004]

The results of the  $3\pi$  PWA at COMPASS

— 14 interfering waves  $\times$  11  $t'$ -slices simultaneously.

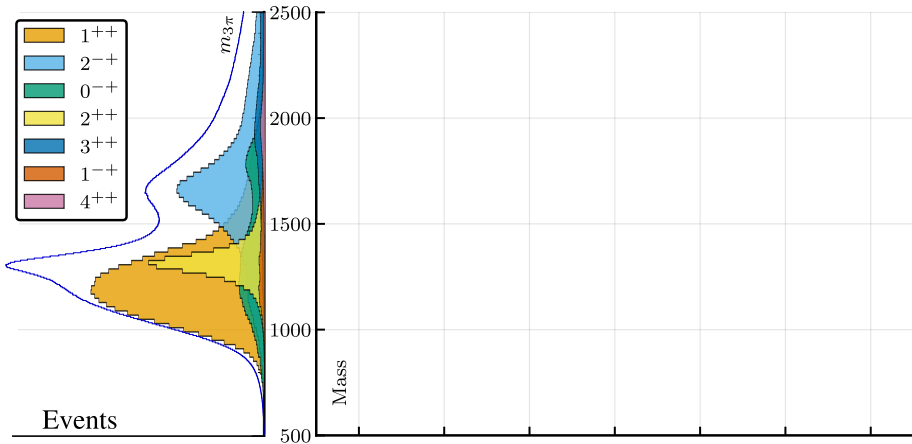


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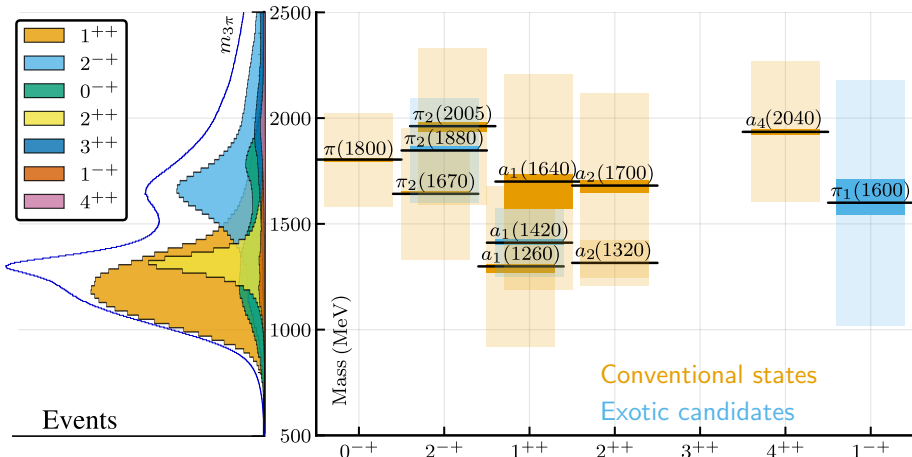


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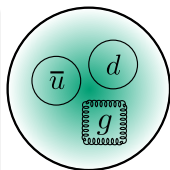
- Simultaneous fit for 11 resonances including hybrid candidates,  $\pi_1(1600)$  and  $\pi_2(1880)$ .

# Experimental evidence for the hybrid mesons

## Evidence for $1^{-+}$ hybrid

- Established in decays to  $\eta^{(\prime)}\pi$  by COMPASS [COMPASS, JPAC]
- Established in decays to  $3\pi$  by COMPASS [COMPASS]
- See in  $\bar{p}N$  annihilation with the Crystal Ball data [Kopf et al.,]

More details in [Stephan's talk](#) (today), [Vincent's talk](#) (tomorrow)



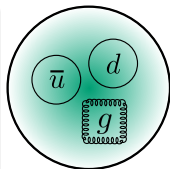


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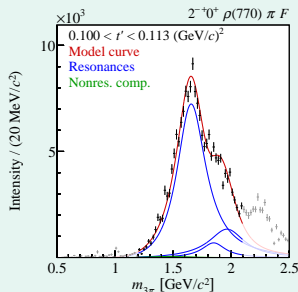
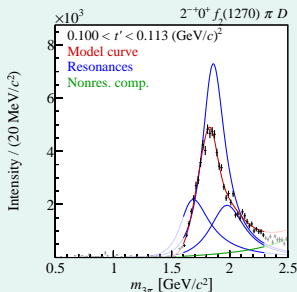
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## Hits for $2^{-+}$ hybrid

- $\pi_2(1880)$  is required in COMPASS fits [COMPASS, PRD95 (2017) 032004]
- **Challenge:** overlapping resonances!

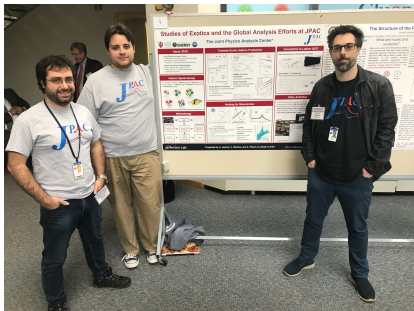


# Towards more theory-sound model

[JPAC, PPNP (2022) 103981]

**JPAC:** tight collaboration between theory and experiment

- How to model 3-body resonances?  
[JPAC, JHEP 08 (2019) 080]
- How to incorporate spin?  
[JPAC, PRD101 (2020), 034033]
- How to add background?
- Test case:  $a_1(1260) \rightarrow 3\pi$   
[JPAC, PRD98 (2018), 096021]

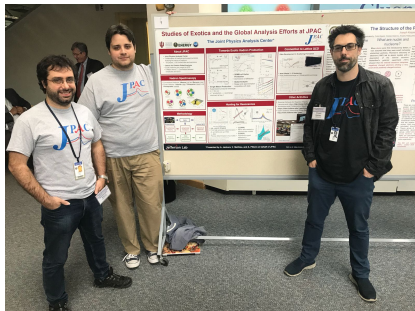


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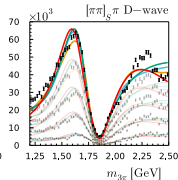
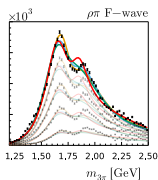
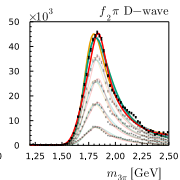
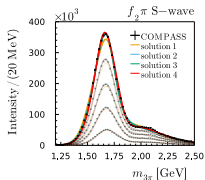
[JPAC, PPNP (2022) 103981]

**JPAC:** tight collaboration between theory and experiment

- How to model 3-body resonances?  
[JPAC, JHEP 08 (2019) 080]
- How to incorporate spin?  
[JPAC, PRD101 (2020), 034033]
- How to add background?
- Test case:  $a_1(1260) \rightarrow 3\pi$   
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$2^{-+}$  fits  
require  
 $\pi_2(1880)$

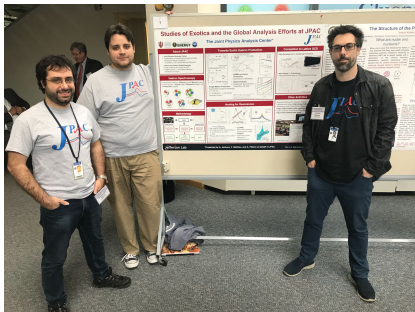


# Towards more theory-sound model

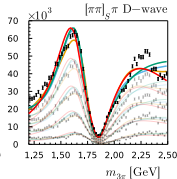
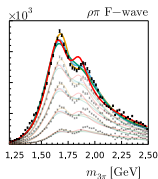
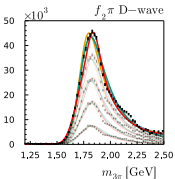
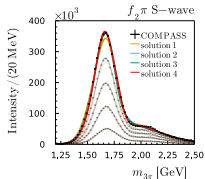
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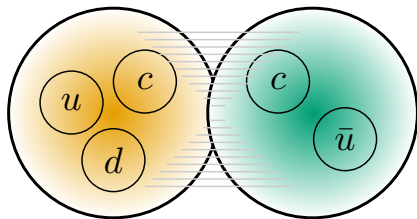
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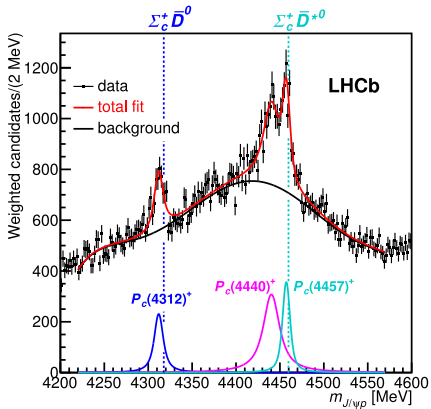
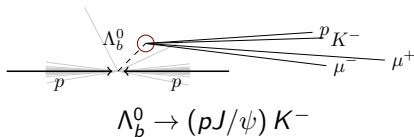


See talk of **Vincent** tomorrow.

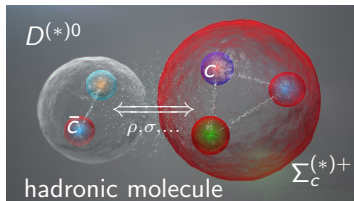


# Exotic molecules

# Pentaquarks in $p^{(uud)} J/\psi^{(c\bar{c})}$ mass spectrum [PRL 122 (2019) 22]

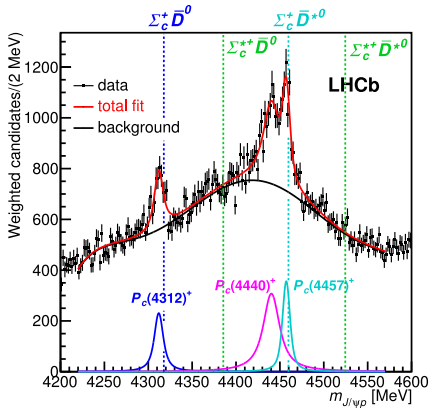
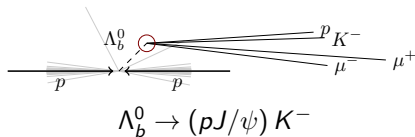


- Narrow peaks in  $\rightarrow p J/\psi$
- Right near  $\Sigma_c^{*+} \bar{D}^{*0}$  threshold
- The most plausible interpretation is hadronic molecules

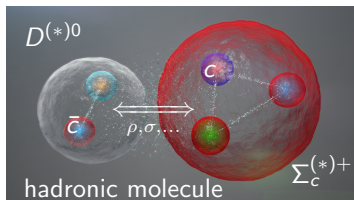


- Would be an exotic nuclei
- No analogue of the Meson-Baryon system in nuclear physics

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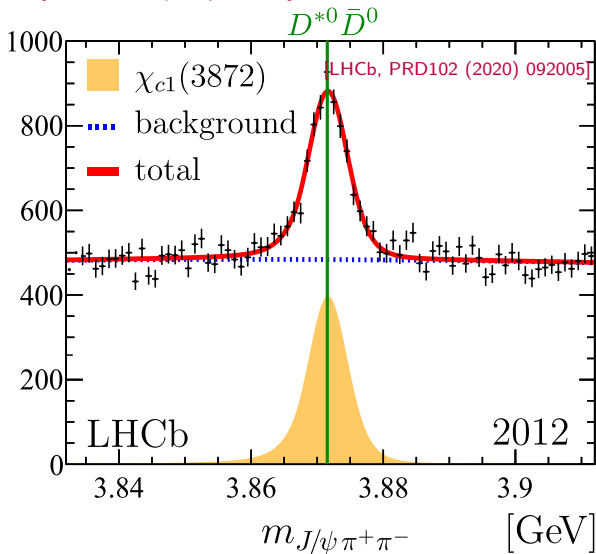
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[Du et al., PRL 124 (2020) 7], [Liu et al., PRL 122 (2019) 24]

# $\chi_{c1}(3872)$ : charmonium state right at the $D^{*0}\bar{D}^0$ mass

Nature is highly debated from 2003 [Belle, PRL91 (2003), 262001]

- Charmonium state ( $c\bar{c}$ ),  $\chi_{c1}(2P)$  is expected 70 MeV above
- The peak right at the  $D^{*0}\bar{D}^0$  threshold
- Large isospin violation in the strong decays to  $J/\psi\pi^+\pi^-$  [LHCb 2022, 2204.12597]

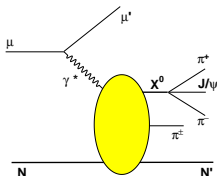




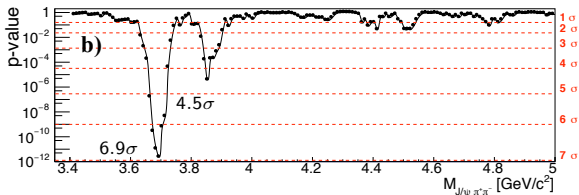
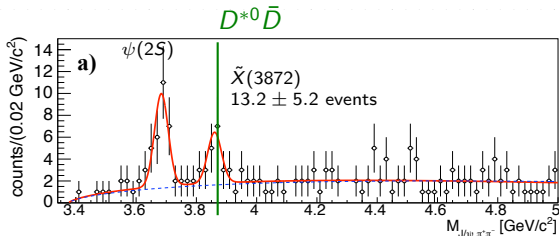
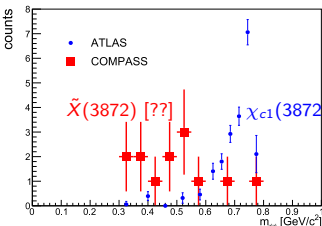
# Puzzles from the muoproduction of $\chi_{c1}(3872)$

[COMPASS, PLB 783 (2018) 334]

- Exclusive production



- In association with  $\pi^\pm$
- Large rate w.r.t.  $\psi(2S)$



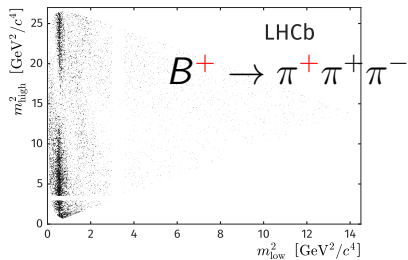
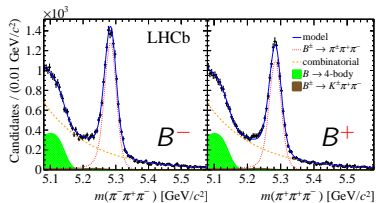
- $\pi\pi$  spectrum should show be the tail of the  $\rho$
- The signal in  $4.7\sigma$  tension with  $\chi_{c1} \rightarrow J/\psi\rho$  decay

# Precision studies of resonance line shapes

CP violation in  $B \rightarrow 3\pi$ 

[PAPER-2019-017 (LHCb), PAPER-2019-018 (LHCb)]

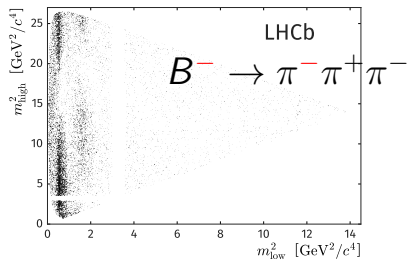
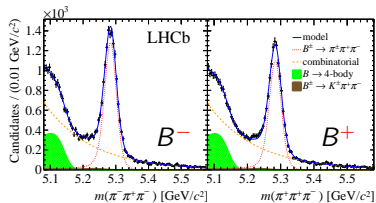
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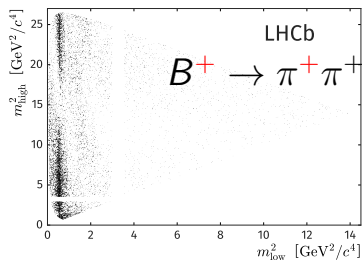
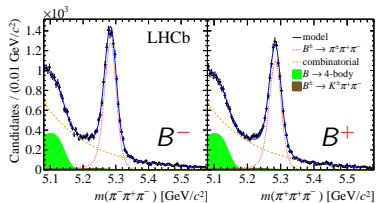
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# CP violation in $B \rightarrow 3\pi$

## Model-independent analysis



[PAPER-2019-017 (LHCb), PAPER-2019-018 (LHCb)]

- $\text{Br}(B^\pm \rightarrow \pi^\pm \pi^+ \pi^-)$  are significantly different
- However, CPT implies same lifetime of  $B^+$  and  $B^-$

The main mechanism of CPV is **final-state interaction**

[Dedonder et al., APPB42 (2011), 2013]

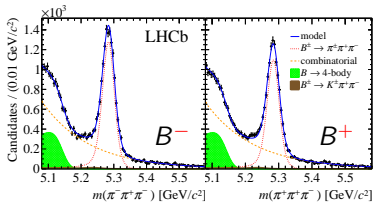
[Nogueira et al., PRD92, 054010 (2015)]

- Decay probability is distributed between various channels.
- $\pi\pi \leftrightarrow K\bar{K}$  ensures distribution of CP between  $B \rightarrow 3\pi$  and  $B \rightarrow \pi K\bar{K}$

⇒ Precise studies of  $\pi\pi/K\bar{K}$  amplitudes are needed

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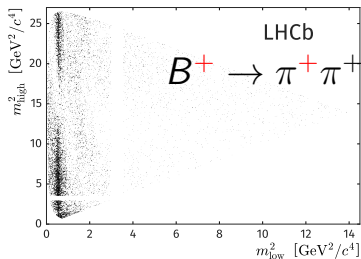
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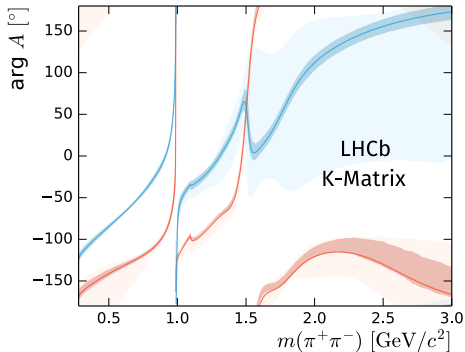
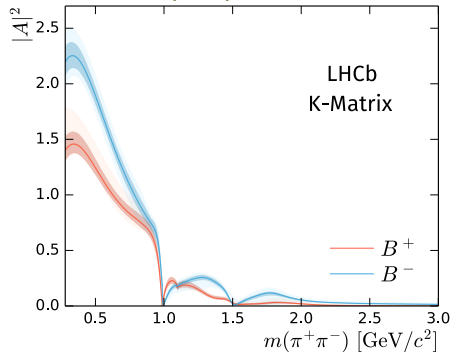


⇒ Precise studies of  $\pi\pi/K\bar{K}$  amplitudes are needed

Recent results of  $\pi\pi$  amplitude in  $D$  decays [PAPER-LHCb-2022-0XX], see [Liupan's talk](#).

# Extracted $(\pi\pi)_S$ production amplitude

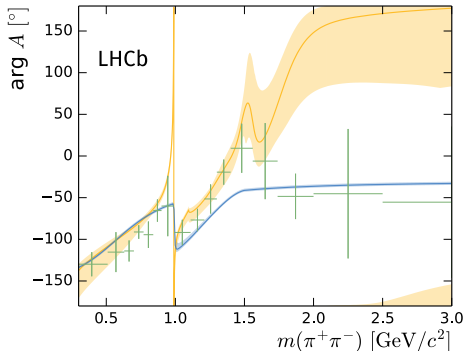
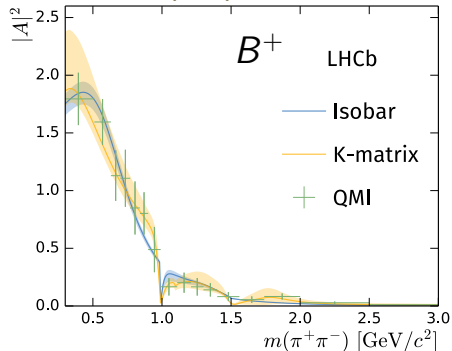
[PAPER-2019-017 (LHCb)]



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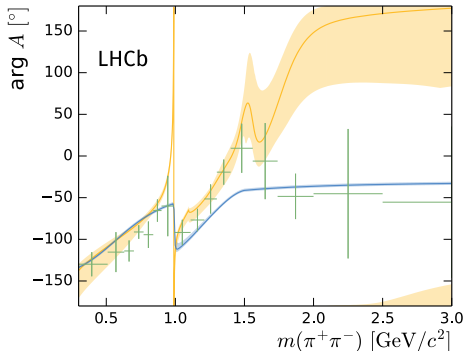
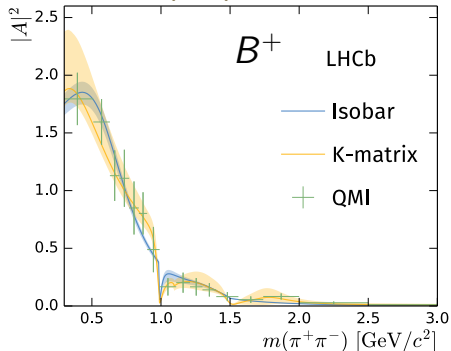


- Clear difference in  $(\pi\pi)_S$  amplitude in  $B^+$  and in  $B^-$
- Different parametrizations are broadly consistent to each other



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[PAPER-2019-017 (LHCb)]



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- Different parametrizations are broadly consistent to each other

Many sources of the CP violation:

- $(\pi\pi)_S$ -wave
- $\rho(770)/(\pi\pi)_S$  interference
- $f_2(1260)$

Convolved with **three-body dynamics**

# Three-body final-state interaction

For multibody decays, several decay chains lead to the same final state

$$\sim \text{white circle} = \sim \text{yellow circle} + \sim \text{blue circle} + \sim \text{green circle}$$

$$\sim \text{yellow circle} = \sim \text{wavy line} + \sim \text{wavy line}$$

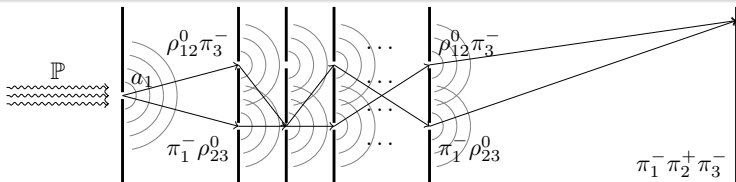
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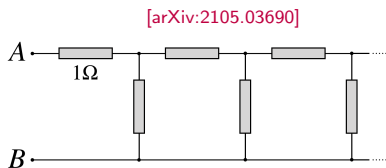
$$+ \dots$$

Hadronic double-slit experimental with infinite # of barriers



# Infinite Resistor Ladder Puzzle

Equivalent resistance of the infinite ladder of the chains:



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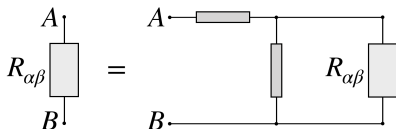
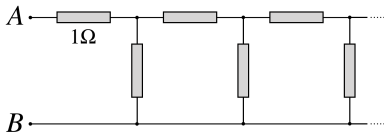
Equivalent resistance of the infinite ladder of the chains:

- Solved by adding one more unit cell

$$R_{\alpha\beta} = 1 + \frac{R_{\alpha\beta}}{1 + R_{\alpha\beta}}$$

- The answer is the golden ratio

[arXiv:2105.03690]



# Infinite Resistor Ladder Puzzle

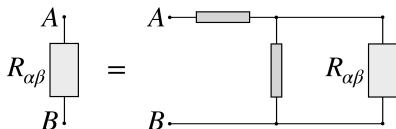
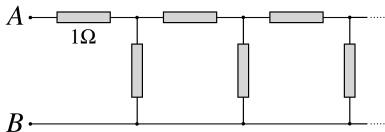
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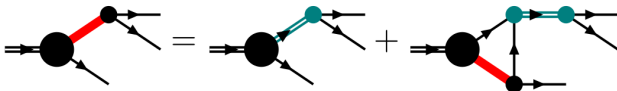
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## Infinite Rescattering Ladder



- Unitarity and analyticity are imposed (Khuri-Treiman equations)
- Solved by one more cell (a virtual loop integral)

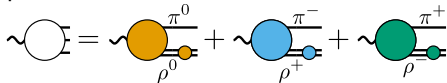
# One applications of the rescattering equations

$$\phi/\omega \rightarrow 3\pi$$

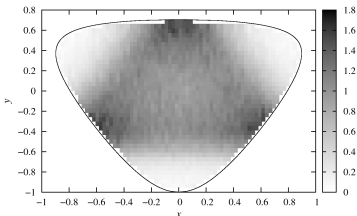
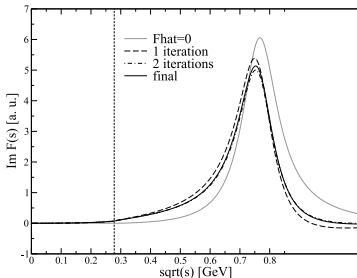
[Niecknig et al., EPJC72 (2012) 2014]

[I. Danilkin et al., PRD91 (2015), 094029]

- proceeds via three coherent chains



- KT to sum the infinite ladder
- The solution converges with three iterations



- $2 \times 10^6$  decays  $\phi \rightarrow \pi^+\pi^-\pi^0$  by KLOE
- Excellent agreement with the data:  
 $\chi^2/\text{ndf} = 1.02$
- Proves importance of the  $3b$  rescattering corrections.

# Probability re-distribution

$$X \rightarrow \pi\pi\pi$$

$$\left\langle \pi\pi \leftrightarrow K\bar{K} \right\rangle$$

$$X \rightarrow \pi K\bar{K}$$

- Plays nicely for  $B$  decays making CPV consistent with CPT
- What is tuning the mass of  $X$  to light-meson sector?

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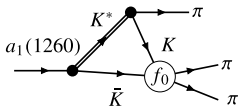
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## Triangle Singularity



- Couplings between  $3\pi$  and  $\pi K\bar{K}$  is enhanced at 1.42 GeV
- Resonance-like effect, however, not exotic state
- Long-thought theoretical concept
- Observed by COMPASS for the first time  
[COMPASS, PRL 115 (2015) 082001]  
[COMPASS, PRL(2021)]



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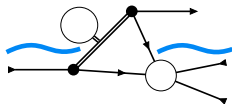
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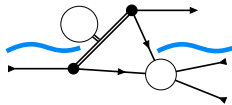
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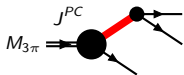
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Ongoing effort to compute the effect in the KT approach.

# Mode precise data on $\pi\pi$ scattering

freed-isobar analysis in COMPASS

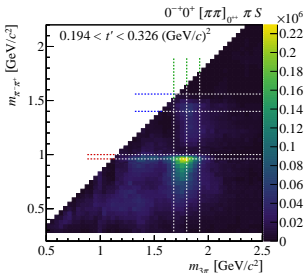
$\pi\pi$ -interaction



in presence of  
third particle

Large set of different  $\pi\pi$   $S$ -waves:

- The lineshape depends on:
  - ▶ Total invariant mass  $M_{3\pi}$
  - ▶ Cross channel amplitudes (other waves in sector  $J^{PC}$ )
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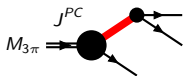


Several ongoing efforts to interpret the data, calibrate th. frameworks

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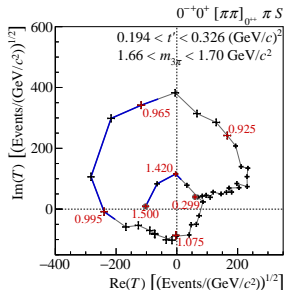
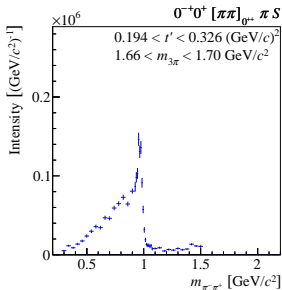
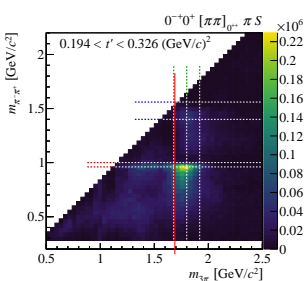
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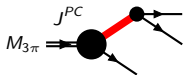


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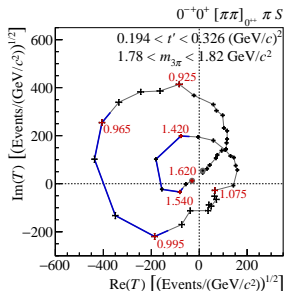
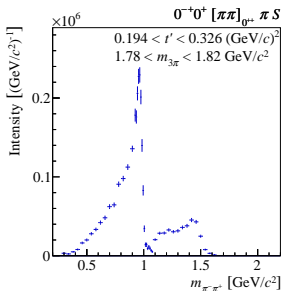
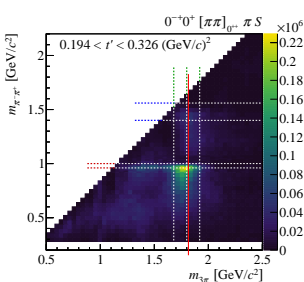
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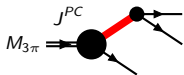


Several ongoing efforts to interpret the data, calibrate th. frameworks

# Mode precise data on $\pi\pi$ scattering

freed-isobar analysis in COMPASS

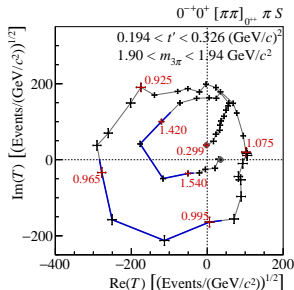
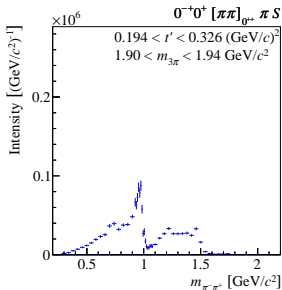
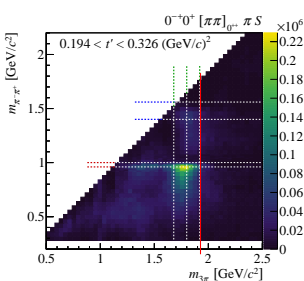
$\pi\pi$ -interaction



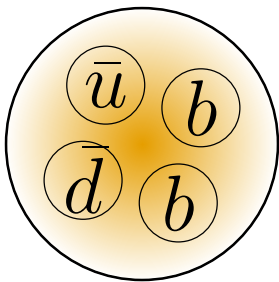
in presence of  
third particle

Large set of different  $\pi\pi$   $S$ -waves:

- The lineshape depends on:
  - ▶ Total invariant mass  $M_{3\pi}$
  - ▶ Cross channel amplitudes (other waves in sector  $J^{PC}$ )
  - ▶ Total quantum numbers  $J^{PC}$



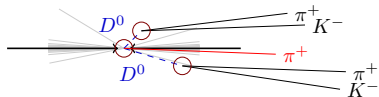
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# Tetraquarks

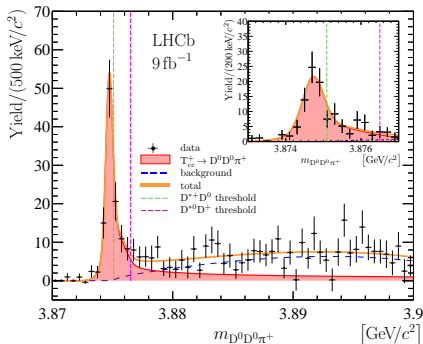
# The landmark of 2021 – double-charm tetraquark, $T_{cc}^+$

[NP 18 (2022) 7, 751-754, NC 13 (2022) 1, 3351]



Two models: Native & Th.-motivated

- The peak position is well constrained.
- The width is not, limit to the coupling:  $|g| > 7.7(6.2) \text{ GeV}$  at 90(95)% CL



Parameter	Value
$N$	$117 \pm 16$
$\delta m_{\text{BW}}$	$-273 \pm 61 \text{ keV}/c^2$
$\Gamma_{\text{BW}}$	$410 \pm 165 \text{ keV}$

Naive BW

Parameter	Value
$N$	$186 \pm 24$
$\delta m_{\text{U}}$	$-359 \pm 40 \text{ keV}/c^2$
$ g $	$3 \times 10^4 \text{ GeV (fixed)}$

Advanced Model  
(developed for  $3\pi$  at  
COMPASS)

Excellent agreement with the data. Reaction amplitude is fully fixed.



Fundamental parameters of  $T_{cc}^+$ 

[interactive]

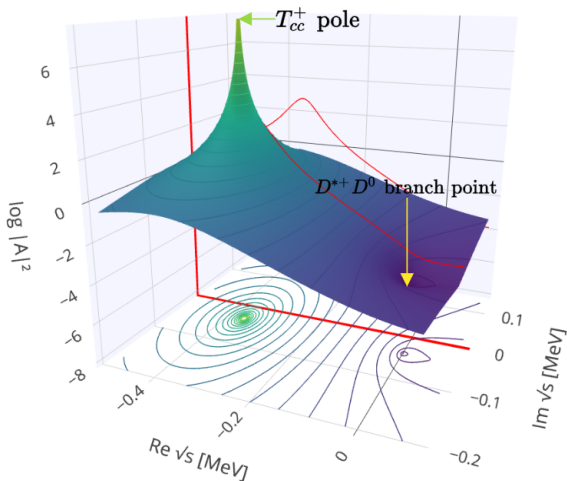
Mass and width – position of the complex pole of the reaction amplitude

- Analytic continuation is non-trivial due to three-body decays [MM et al. (JPAC), PRD 98 (2018) 096021]

The pole parameters:

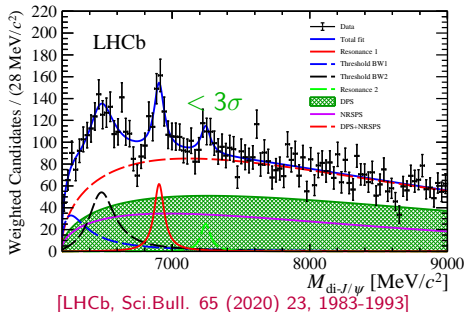
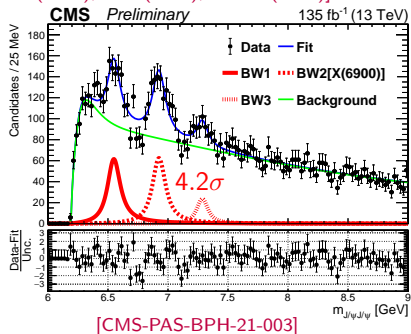
$$\delta m_{\text{pole}} = -360 \pm 40_{-0}^{+4} \text{ keV},$$

$$\Gamma_{\text{pole}} = 48 \pm 2_{-14}^{+0} \text{ keV}.$$



# States in $J/\psi J/\psi$ spectrum – four-charm tetraquarks, $T_{\psi\psi}$

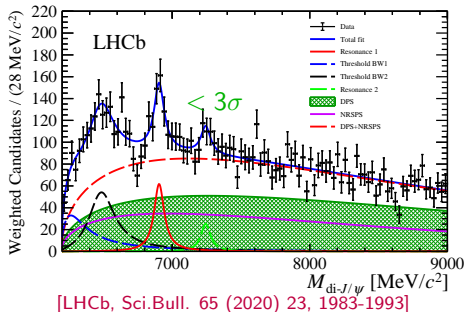
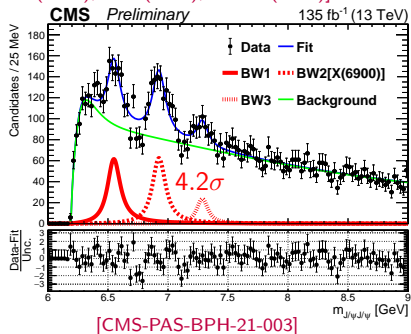
[LHCb(2020), CMS(2022), ATLAS(2022)]



- Rapid raise at the threshold followed by the three peaks.

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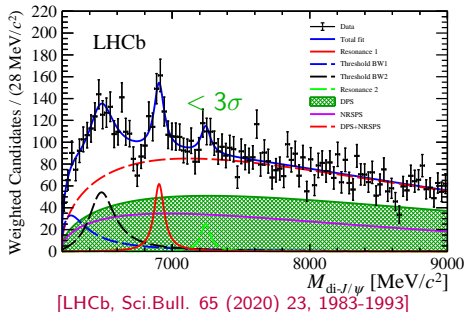
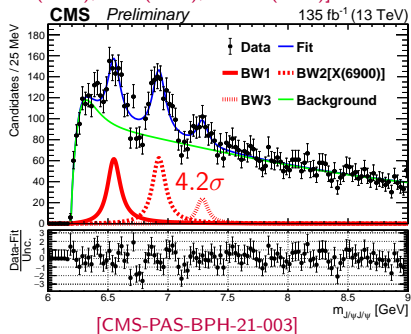
[LHCb(2020), CMS(2022), ATLAS(2022)]



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- Clear dips at 6.8 GeV makes the fit struggle

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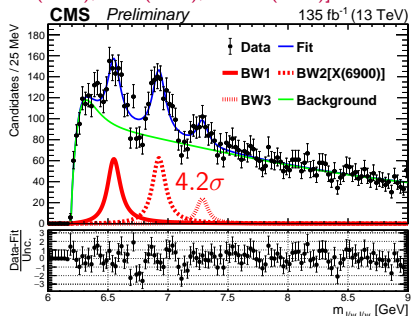
[LHCb(2020), CMS(2022), ATLAS(2022)]



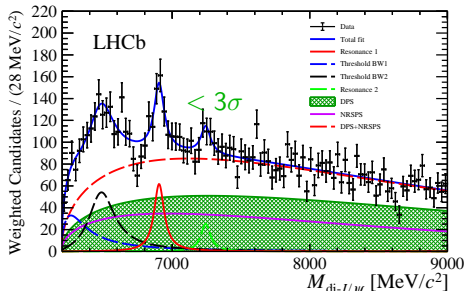
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- Background is a continuum production process with many  $J^{PC}$ . Similar to Deck process in diffractive reactions

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[LHCb(2020), CMS(2022), ATLAS(2022)]



[CMS-PAS-BPH-21-003]



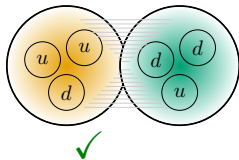
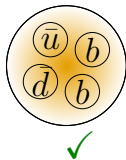
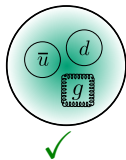
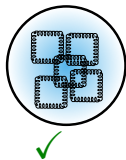
[LHCb, Sci.Bull. 65 (2020) 23, 1983-1993]

- Rapid raise at the threshold followed by the three peaks.
- Clear dips at 6.8 GeV makes the fit struggle
- Background is a continuum production process with many  $J^{PC}$ . Similar to Deck process in diffractive reactions
- Ideas to improve the analysis adding angular variables

[MM, L. An, R. McNulty, arXiv:2007.05501]

# Summary

- Spectroscopy is one of the most developing field of fundamental physics
- New large data samples from modern experiments
- Great effort of exp. and th groups
- Am amazing rate of discoveries:
  - ▶ New clues for the scalar glueball
  - ▶ Hybrid meson is established in several decay modes
  - ▶ Long-thought triangle singularity is observed
  - ▶ New classes of hadrons,  $QQ\bar{q}\bar{q}'$  and  $QQ\bar{Q}\bar{Q}$
  - ▶ New types of atoms, hadronic molecules.



Thank you for the attention