

IWHSS 2022

International Workshop on
Hadron Structure and Spectroscopy
CERN — August 29-31, 2022

HERMES view on the nucleon's spin & 3d structure

The word "Congratulations!" is written in a large, black, cursive script. The letter 'C' is particularly large and features a long, sweeping tail that curves under the word. There are ten hand-drawn stars scattered around the text: three in the upper left, three in the upper right, and four in the lower half. The stars are drawn in two styles: some are solid black outlines, while others are grey outlines. The overall style is casual and celebratory.

Congratulations!

2022 — so many anniversaries!

- 25 years of COMPASS approval
- 20 years of COMPASS data taking



2022 — so many anniversaries!

- 25 years of COMPASS approval
- 20 years of COMPASS data taking
- 35 years of spin crisis/puzzle
- 30 years of HERA and (conditional) HERMES approval
- 15 years of HERA shutdown



[GetDrawings.com]

#123359585

HERMES (1995-2007) @ HERA

27.6 GeV polarized e^+/e^- beam scattered off ...

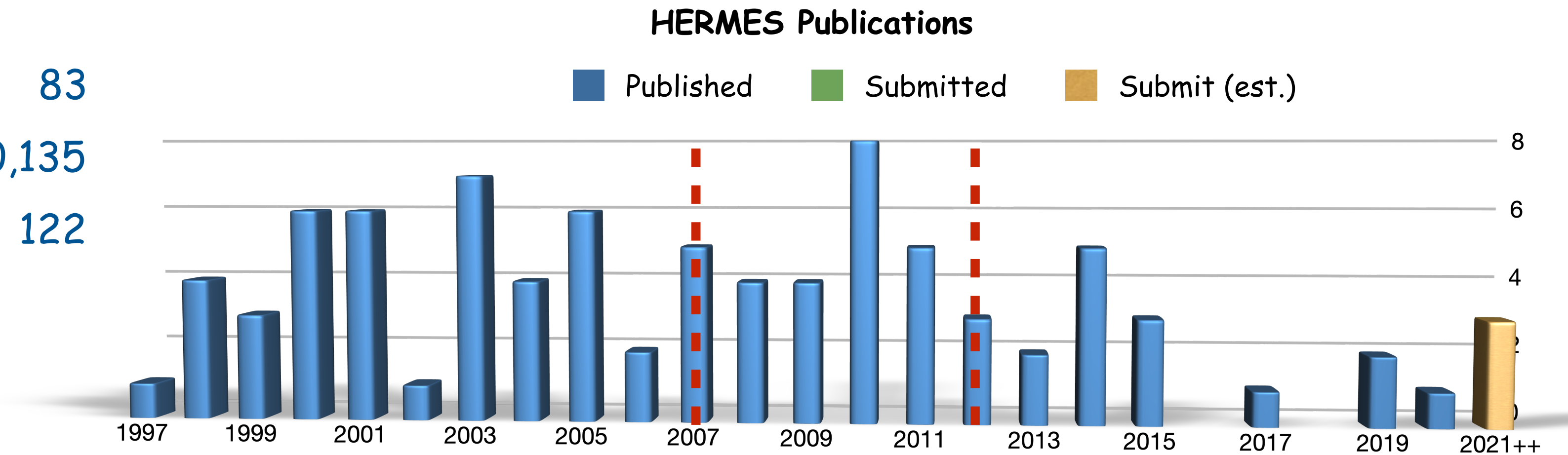


- unpolarized (H, D, He,..., Xe) as well as
 - transversely (H) or
 - longitudinally (H, D, He) polarized
- pure gas targets**



HERMES publication statistics (08/2022)

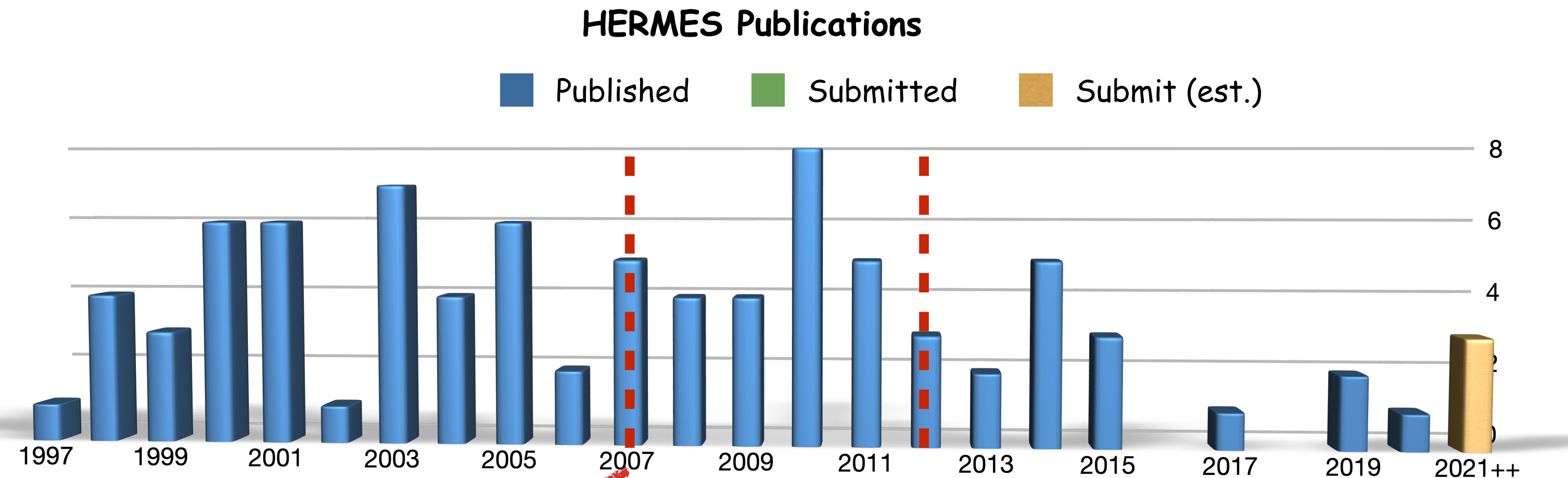
- Total number of published HERMES papers: 83
 - Total number of citations: 10,135
 - Average citations per paper: 122
 - 2 top-cite 500+ & 9 topcite 250+
- [inspirehep.net as of Aug. 28, 2022]



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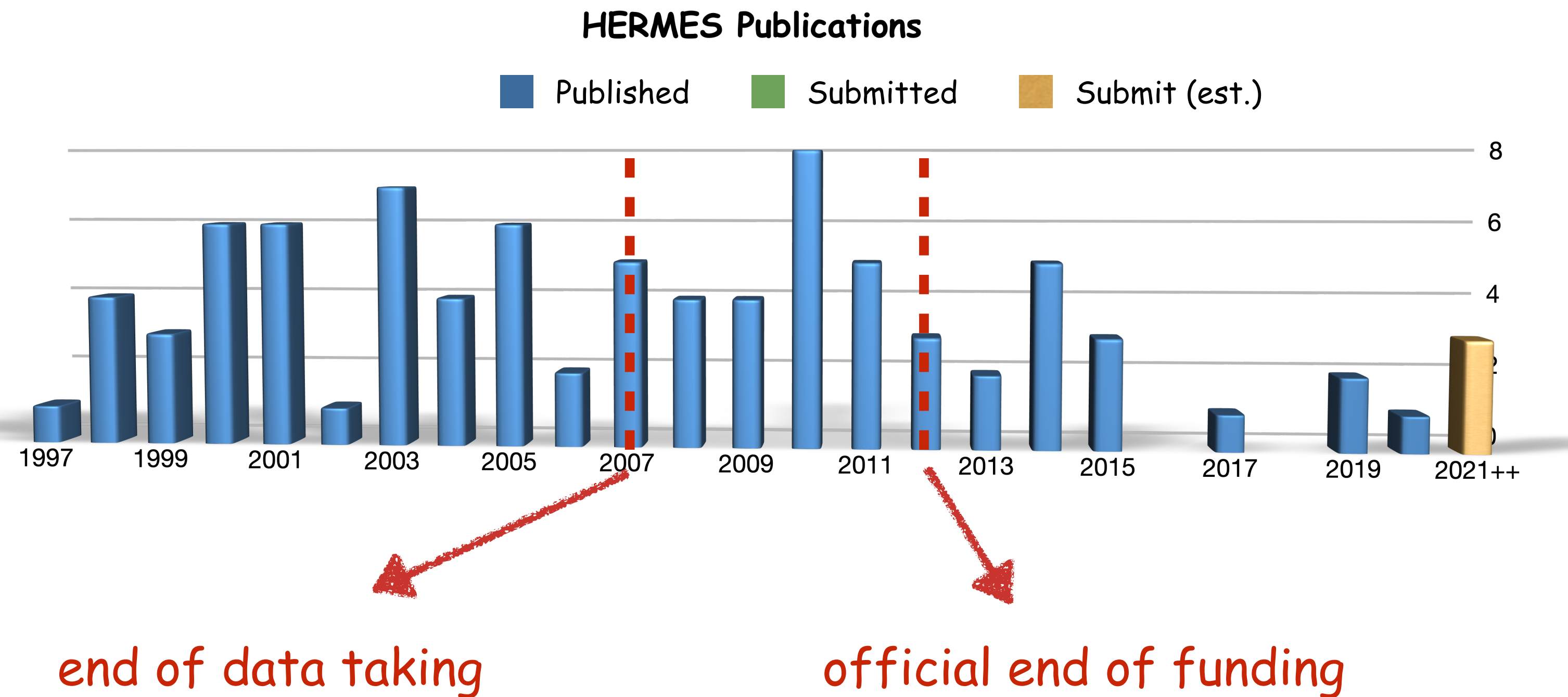


end of data taking

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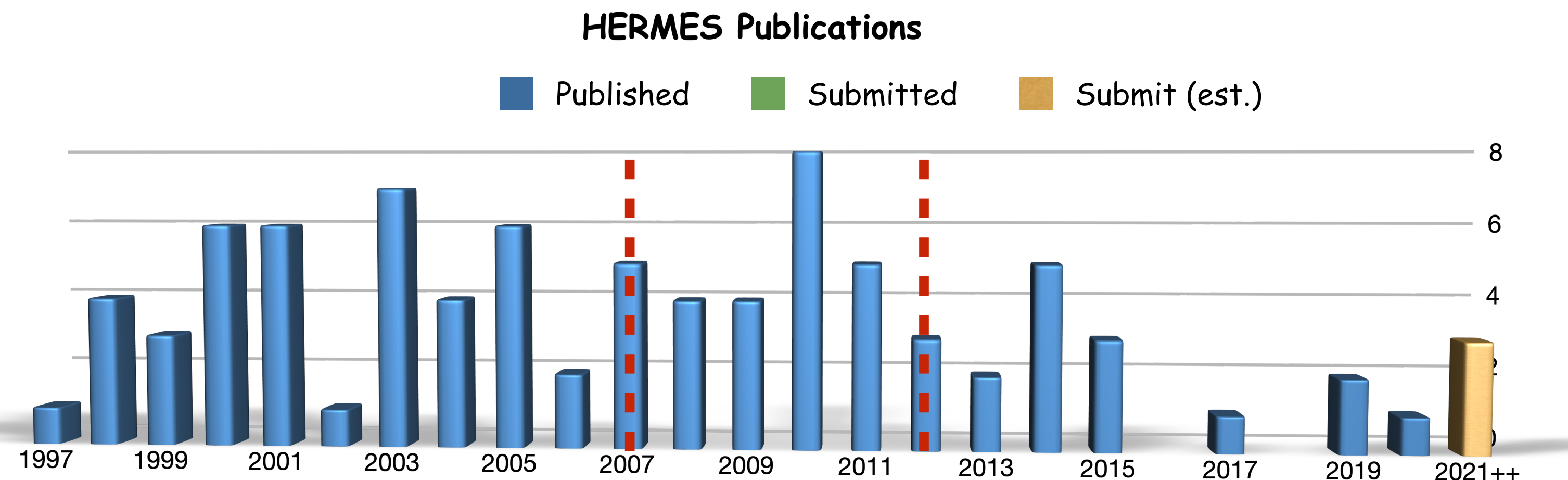
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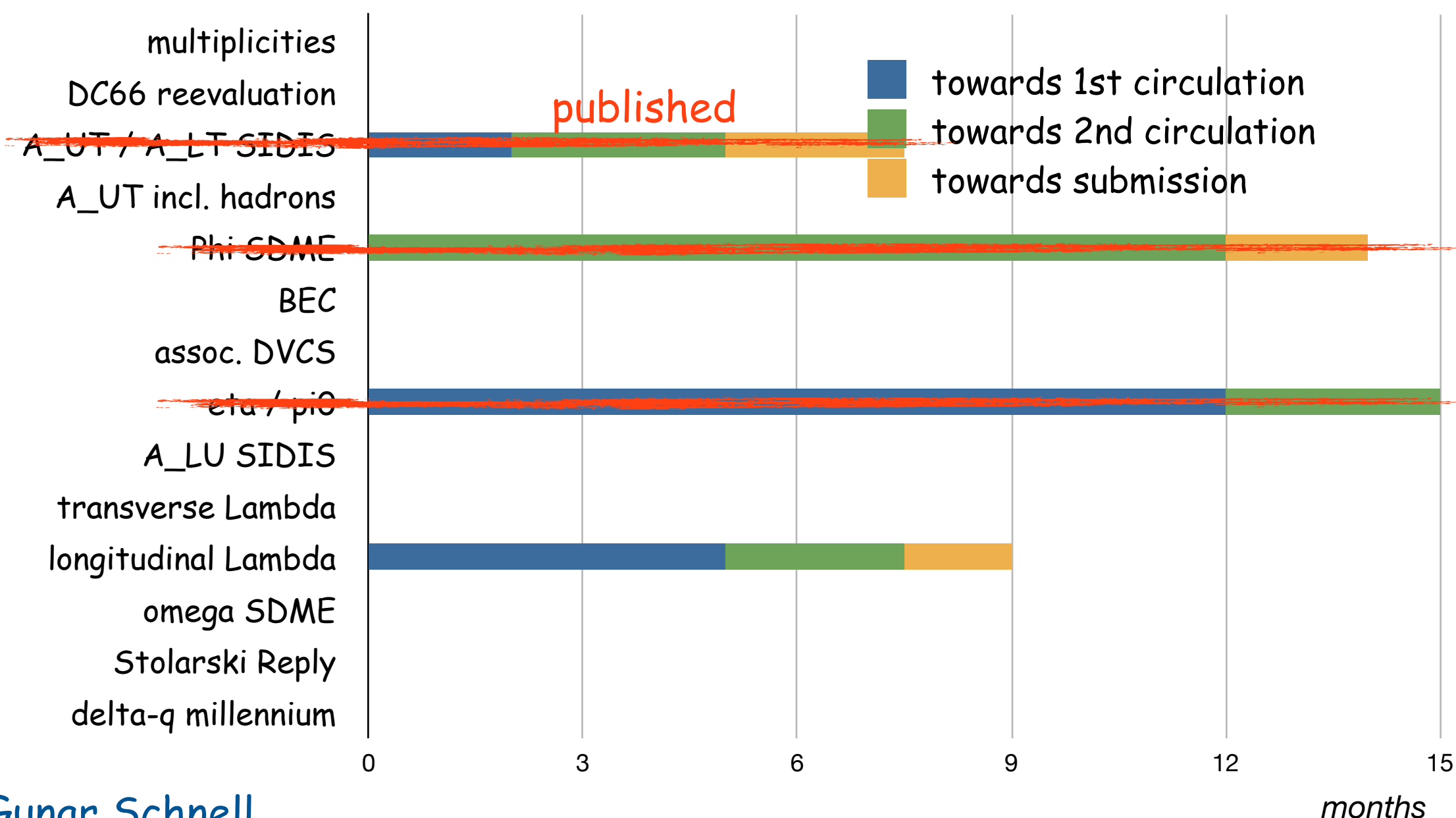
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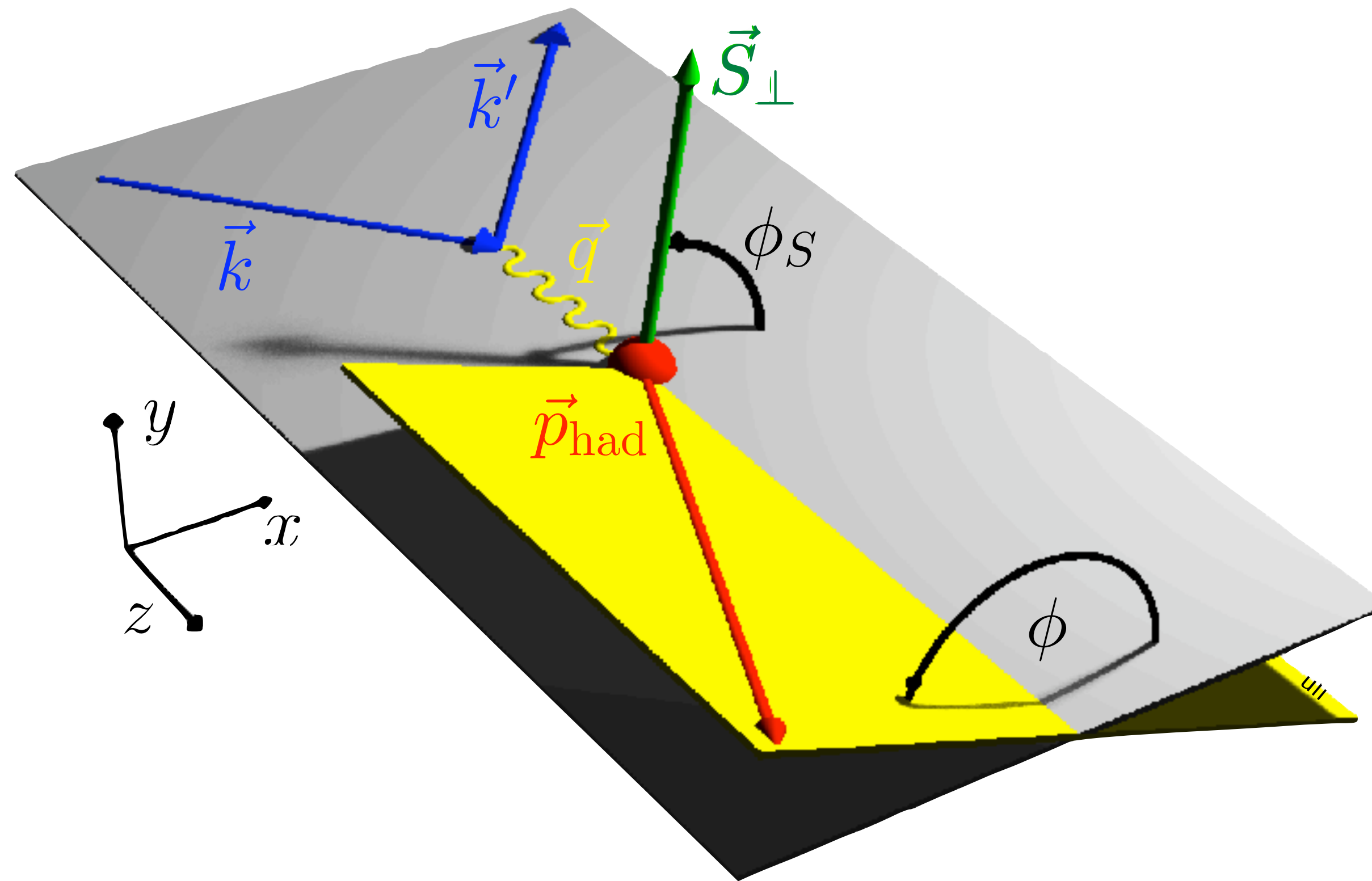


Publication schedule for 2012 priority analyses (08/2022)



- despite tremendous drop in analysis manpower, almost all priority analyses identified finished
 - two analyses dropped
 - one still ongoing in advanced state
- at same time **new ideas**; partially already published, others ... **waiting for manpower**
- only possible thanks to tremendous data-preservation efforts

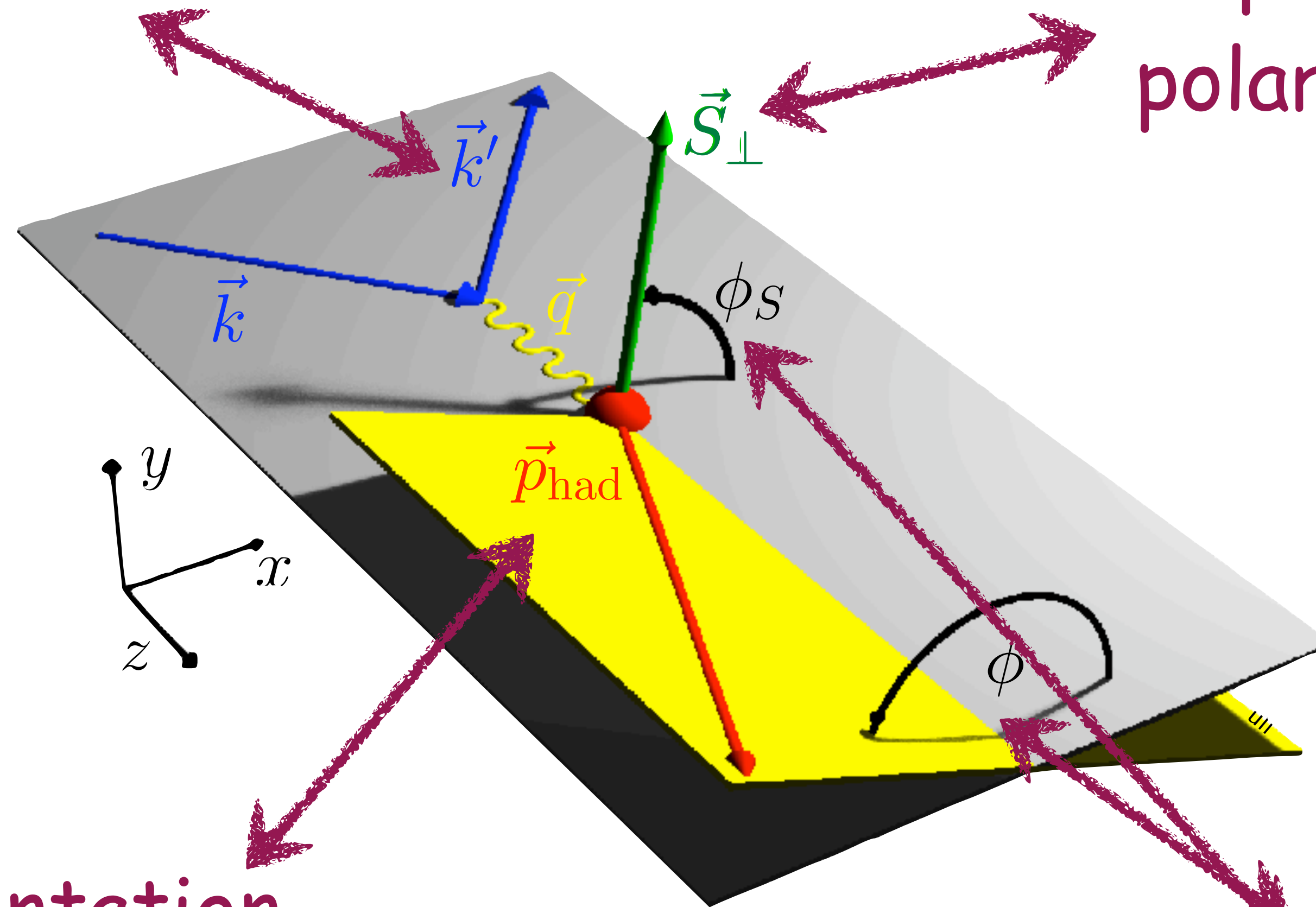
semi-inclusive one-hadron production ($ep \rightarrow ehX$)



semi-inclusive one-hadron production ($ep \rightarrow ehX$)

parton kinematics

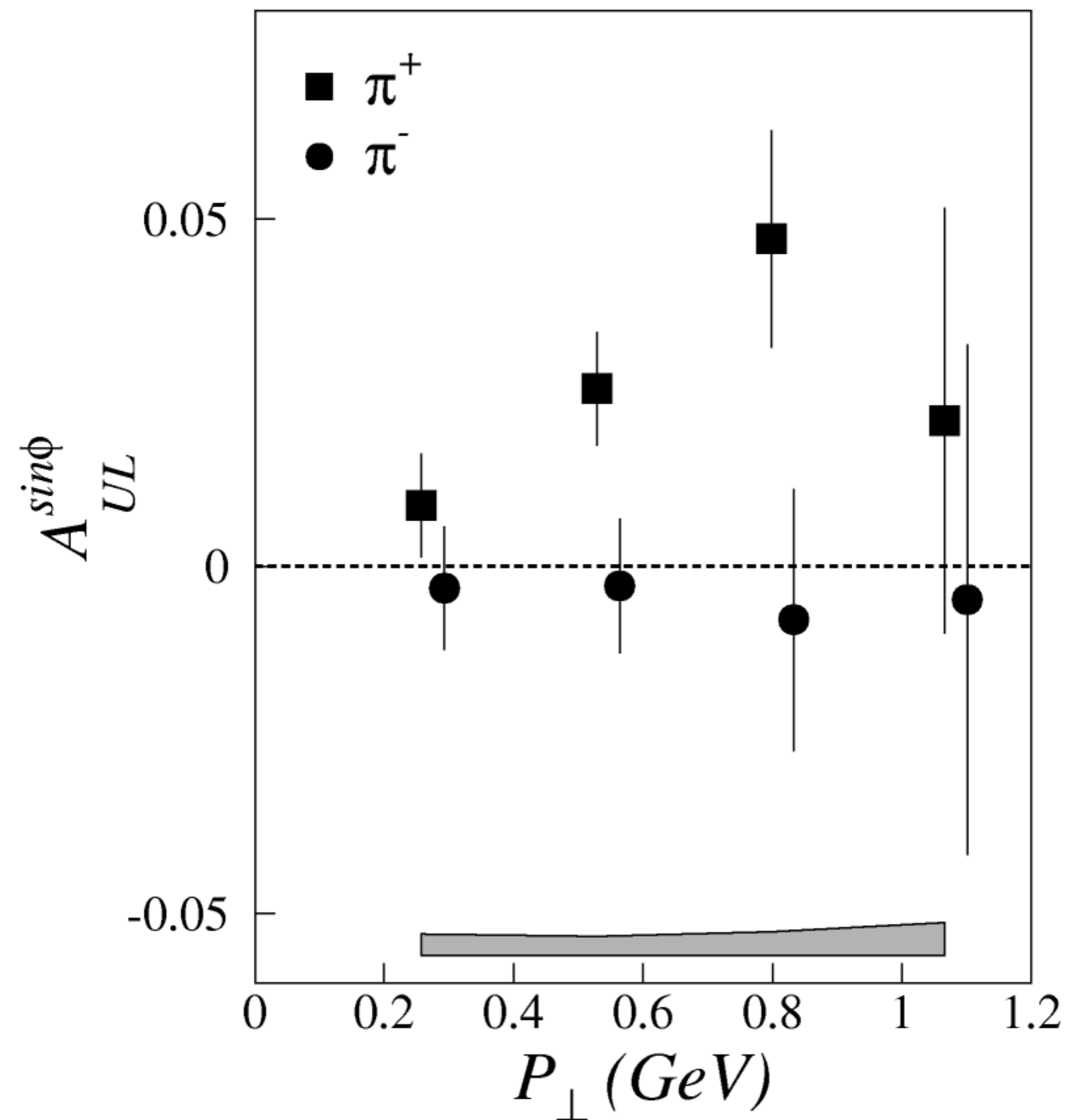
parton
polarization



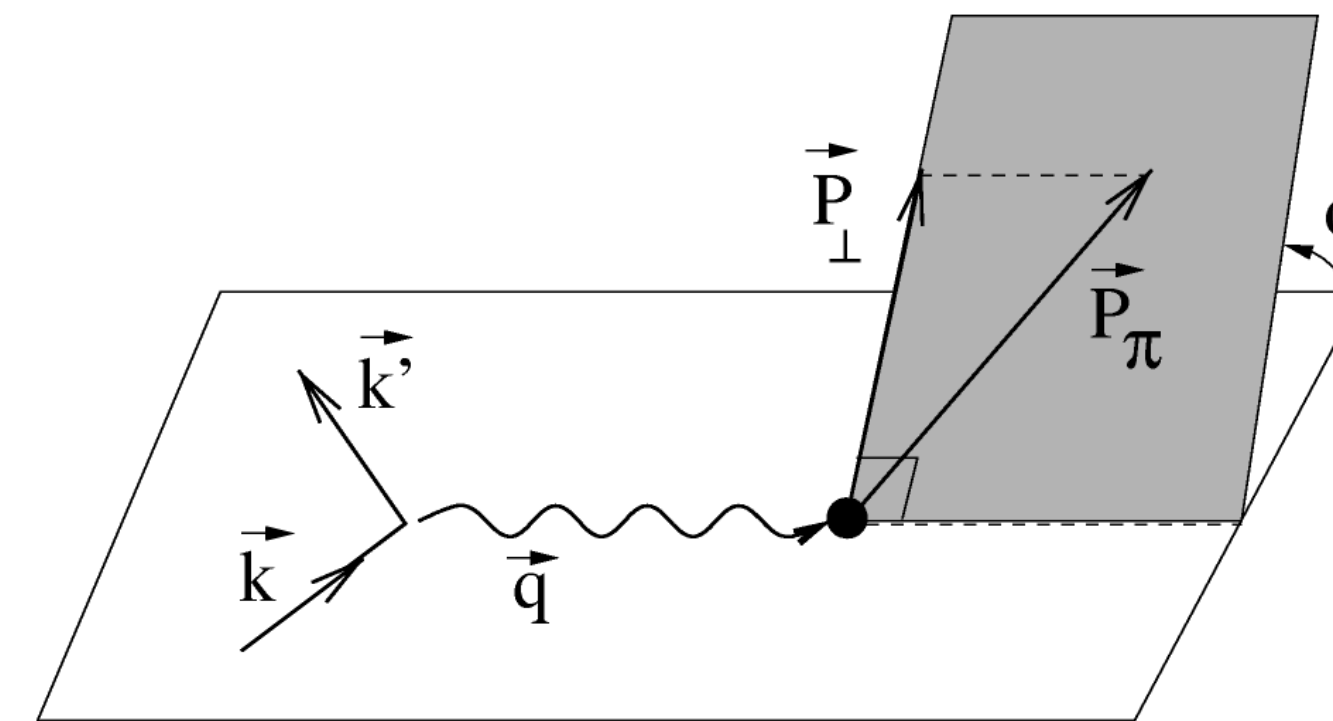
fragmentation
kinematics

fragmentation
fct. selector

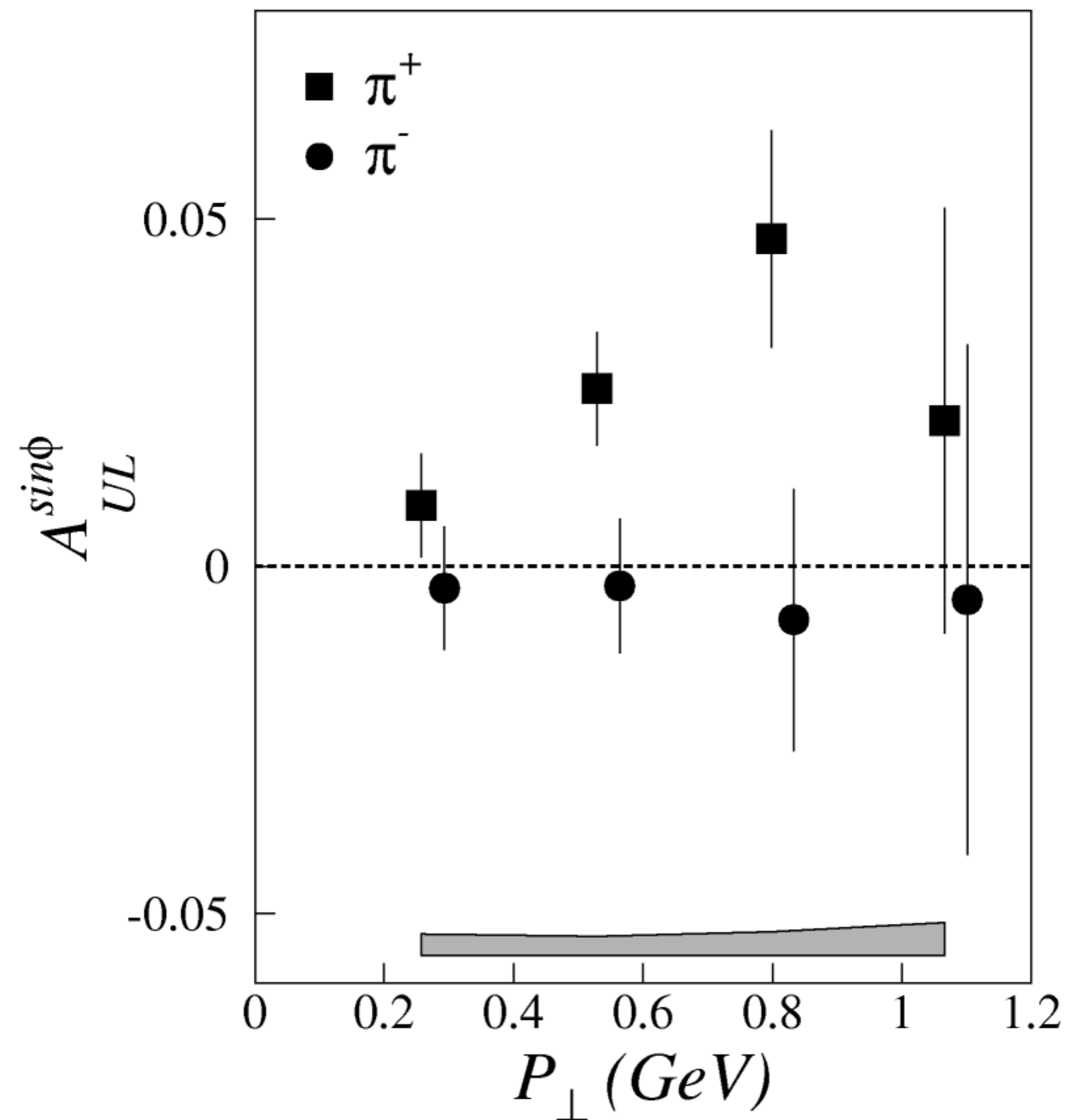
Evidence for a Single-Spin Azimuthal Asymmetry in Semi-inclusive Pion Electroproduction



$$A_{UL} = \frac{1}{|P_B|} \frac{N^{\rightarrow}(\phi) - N^{\leftarrow}(\phi)}{N^{\rightarrow}(\phi) + N^{\leftarrow}(\phi)}$$

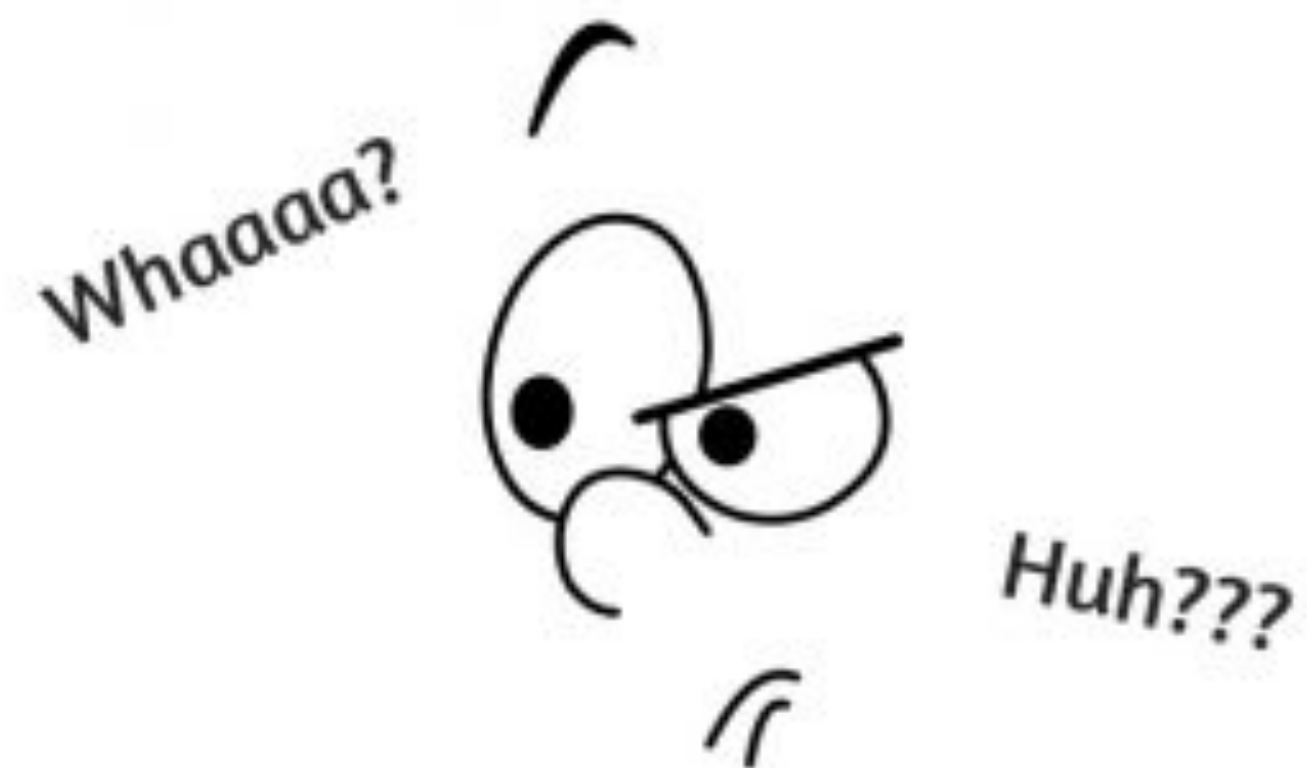


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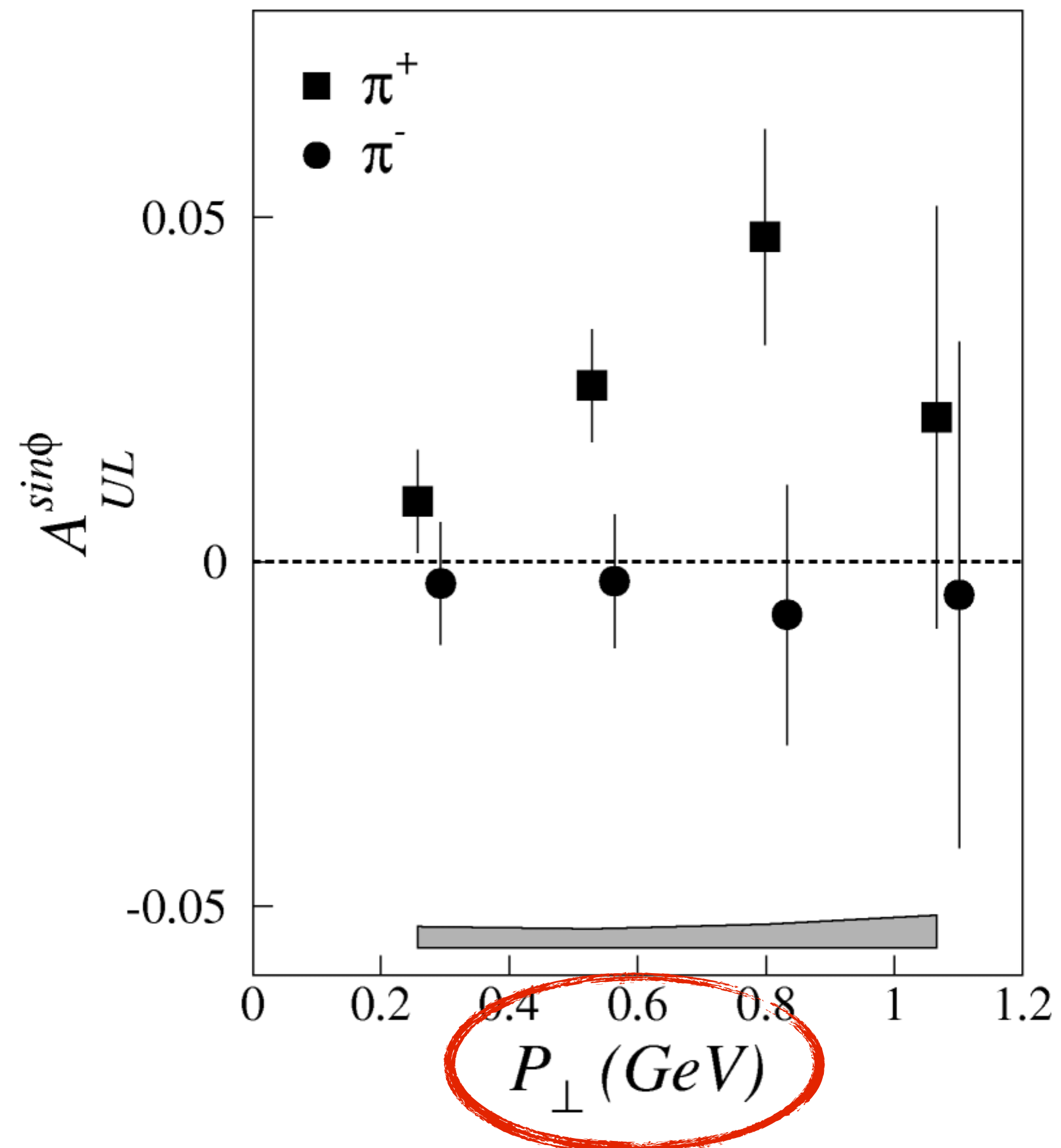


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$\sim \sin \phi$?

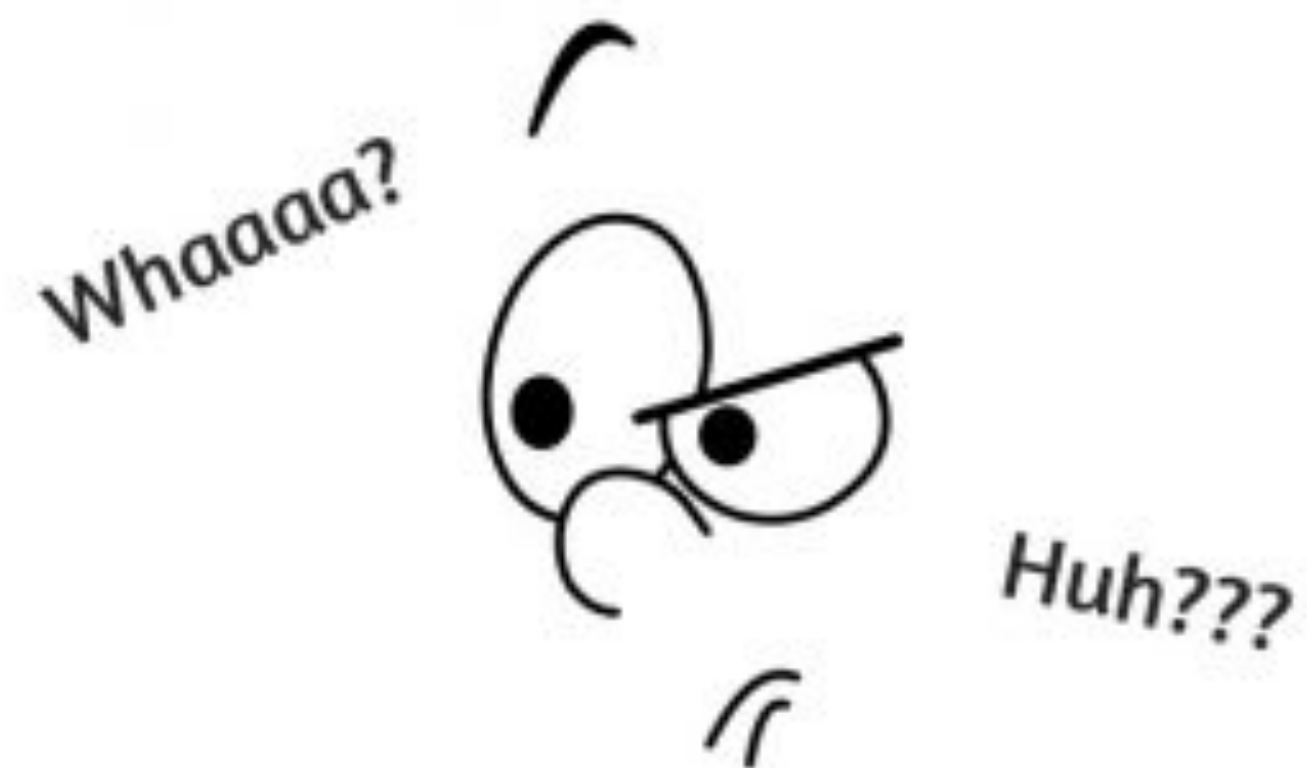


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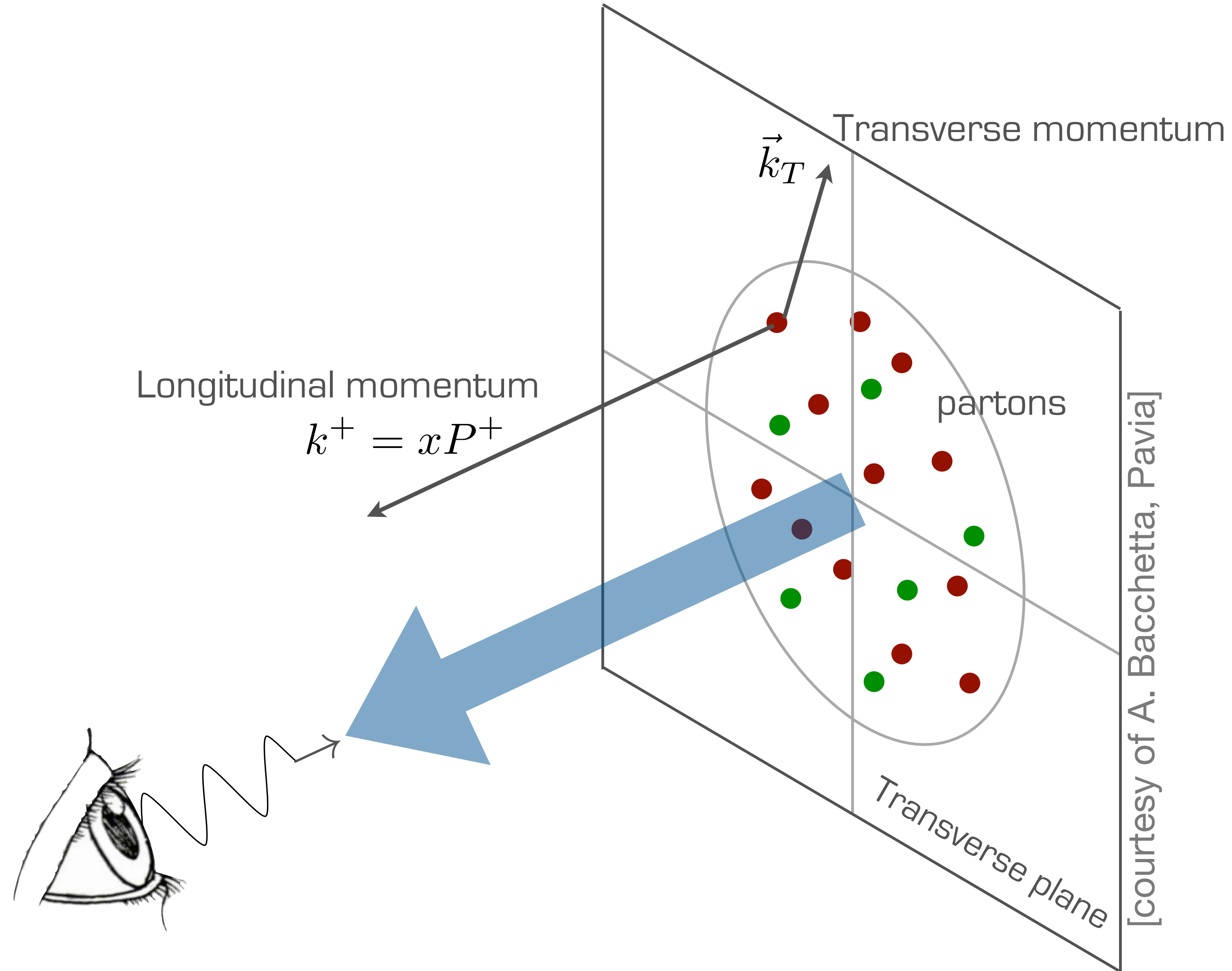


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$\sim \sin \phi ?$



transverse-momentum distributions (TMDs)



3d spin-momentum structure of the nucleon

$$\frac{1}{2}\text{Tr}\left[(\gamma^+ + \lambda\gamma^+\gamma_5)\Phi\right] = \frac{1}{2}\left[f_1 + S^i\epsilon^{ij}k^j\frac{1}{m}f_{1T}^\perp + \lambda\Lambda g_1 + \lambda S^i k^i\frac{1}{m}g_{1T}\right]$$

$$\begin{aligned} \frac{1}{2}\text{Tr}\left[(\gamma^+ - s^j i\sigma^{+j}\gamma_5)\Phi\right] &= \frac{1}{2}\left[f_1 + S^i\epsilon^{ij}k^j\frac{1}{m}f_{1T}^\perp + s^i\epsilon^{ij}k^j\frac{1}{m}h_1^\perp + s^i S^i h_1 \right. \\ &\quad \left. + s^i(2k^i k^j - \mathbf{k}^2\delta^{ij})S^j\frac{1}{2m^2}h_{1T}^\perp + \Lambda s^i k^i\frac{1}{m}h_{1L}^\perp\right] \end{aligned}$$

quark pol.

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

nucleon pol.

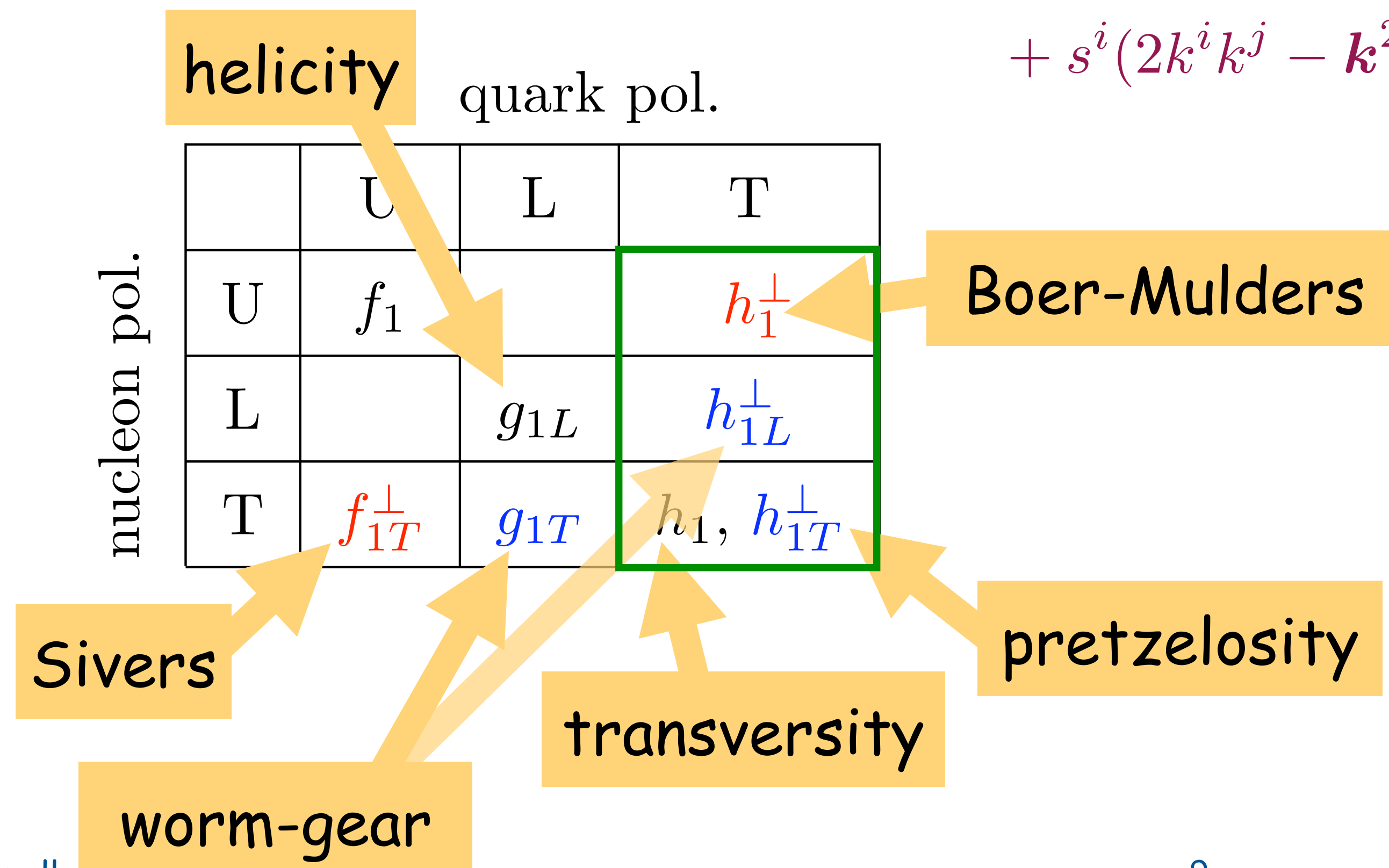
- each TMD describes a particular spin-momentum correlation
- functions in black survive integration over transverse momentum
- functions in green box are chirally odd
- functions in red are naive T-odd

3d spin-momentum structure of the nucleon

$$\frac{1}{2}\text{Tr}\left[(\gamma^+ + \lambda\gamma^+\gamma_5)\Phi\right] = \frac{1}{2}\left[f_1 + S^i\epsilon^{ij}k^j\frac{1}{m}f_{1T}^\perp + \lambda\Lambda g_1 + \lambda S^ik^i\frac{1}{m}g_{1T}\right]$$

$$\frac{1}{2}\text{Tr}\left[(\gamma^+ - s^ji\sigma^{+j}\gamma_5)\Phi\right] = \frac{1}{2}\left[f_1 + S^i\epsilon^{ij}k^j\frac{1}{m}f_{1T}^\perp + s^i\epsilon^{ij}k^j\frac{1}{m}h_1^\perp + s^iS^ih_1\right]$$

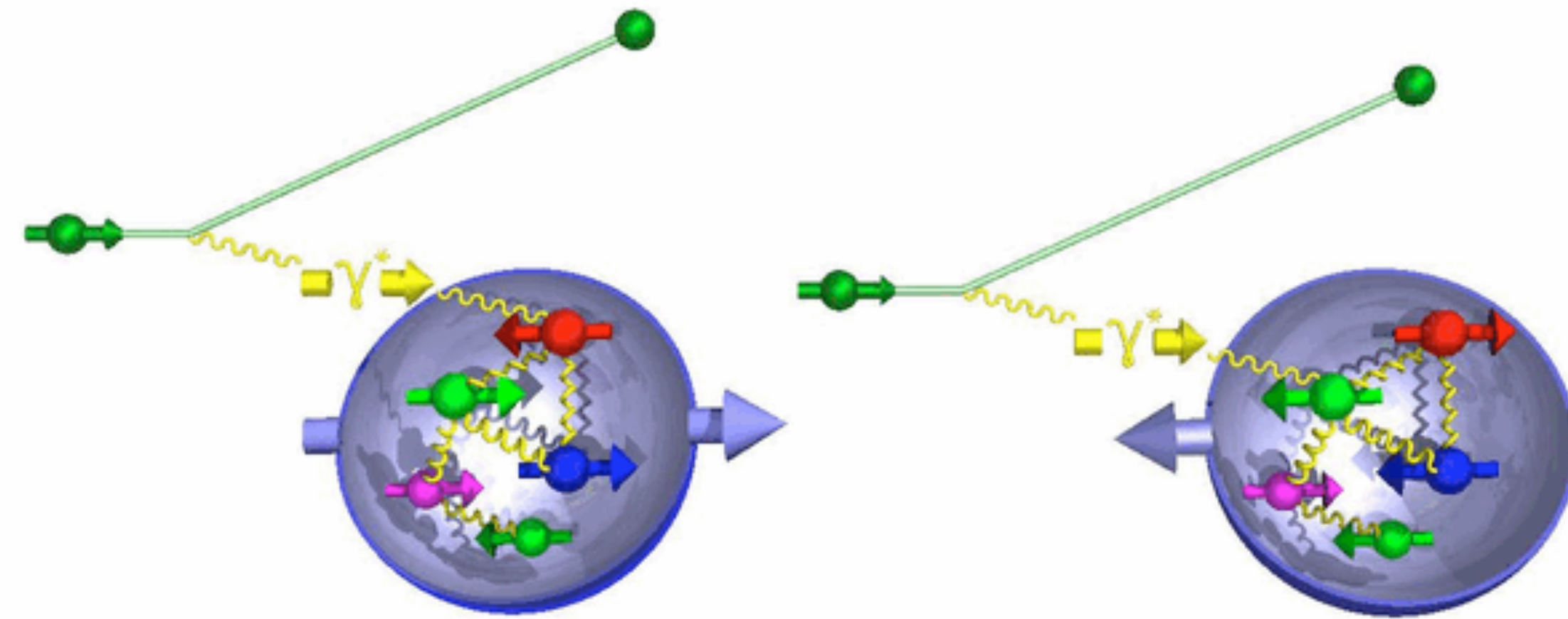
$$+ s^i(2k^ik^j - \mathbf{k}^2\delta^{ij})S^j\frac{1}{2m^2}h_{1T}^\perp + \Lambda s^ik^i\frac{1}{m}h_{1L}^\perp\right]$$



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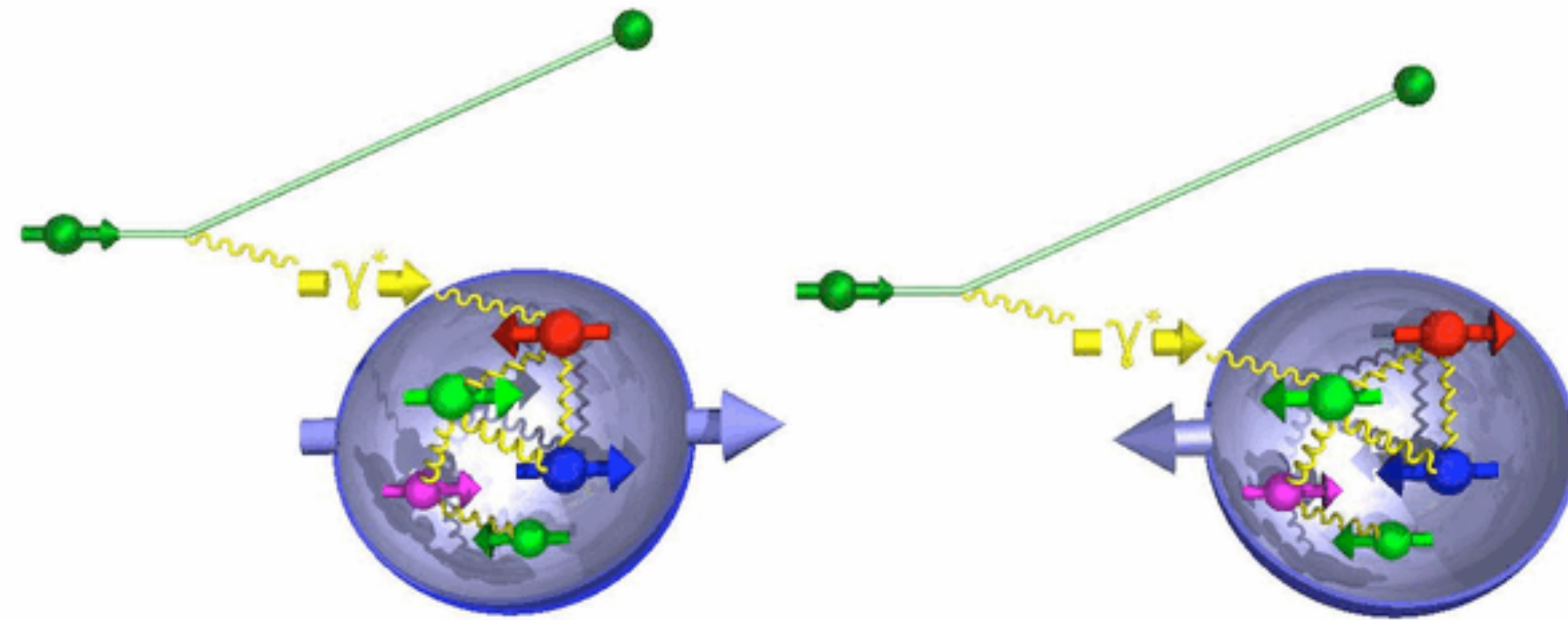
quark polarimetry

- unpolarized quarks: easy - "just" hit them (and count)
- longitudinally polarized quarks: use polarized beam

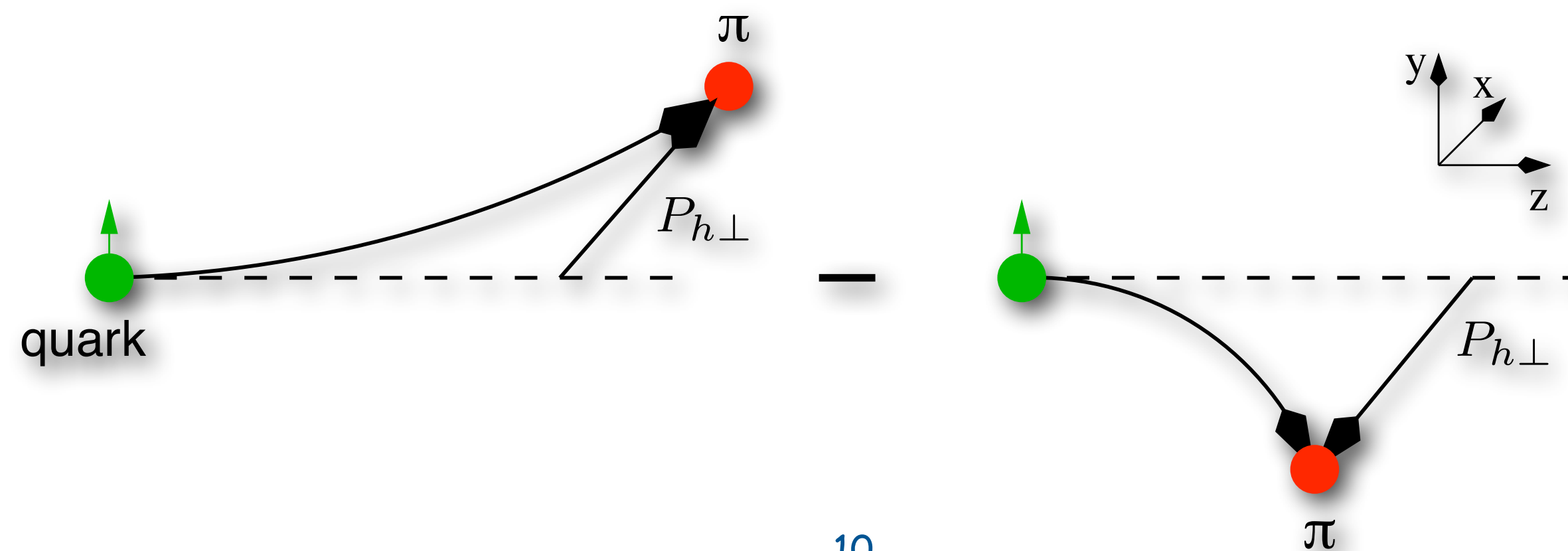


quark polarimetry

- unpolarized quarks: easy - "just" hit them (and count)
- longitudinally polarized quarks: use polarized beam



- transversely polarized quarks: need final-state polarimetry, e.g.



TMDs in hadronization

quark pol.

	U	L	T
U	D_1		H_1^\perp
L		G_1	H_{1L}^\perp
T	D_{1T}^\perp	G_{1T}^\perp	$H_1 H_{1T}^\perp$

hadron pol.

TMDs in hadronization

quark pol.

	U	L	T
hadron pol.	U	D_1	H_1^\perp
	L		G_1 H_{1L}^\perp
	T	D_{1T}^\perp	G_{1T}^\perp H_1 H_{1T}^\perp

➡ relevant for unpolarized final state

TMDs in hadronization

quark pol.

hadron pol.

	U	L	T
U	D_1		H_1^\perp
L		G_1	H_{1L}^\perp
T	D_{1T}^\perp	G_{1T}^\perp	$H_1 H_{1T}^\perp$

relevant for unpolarized final state

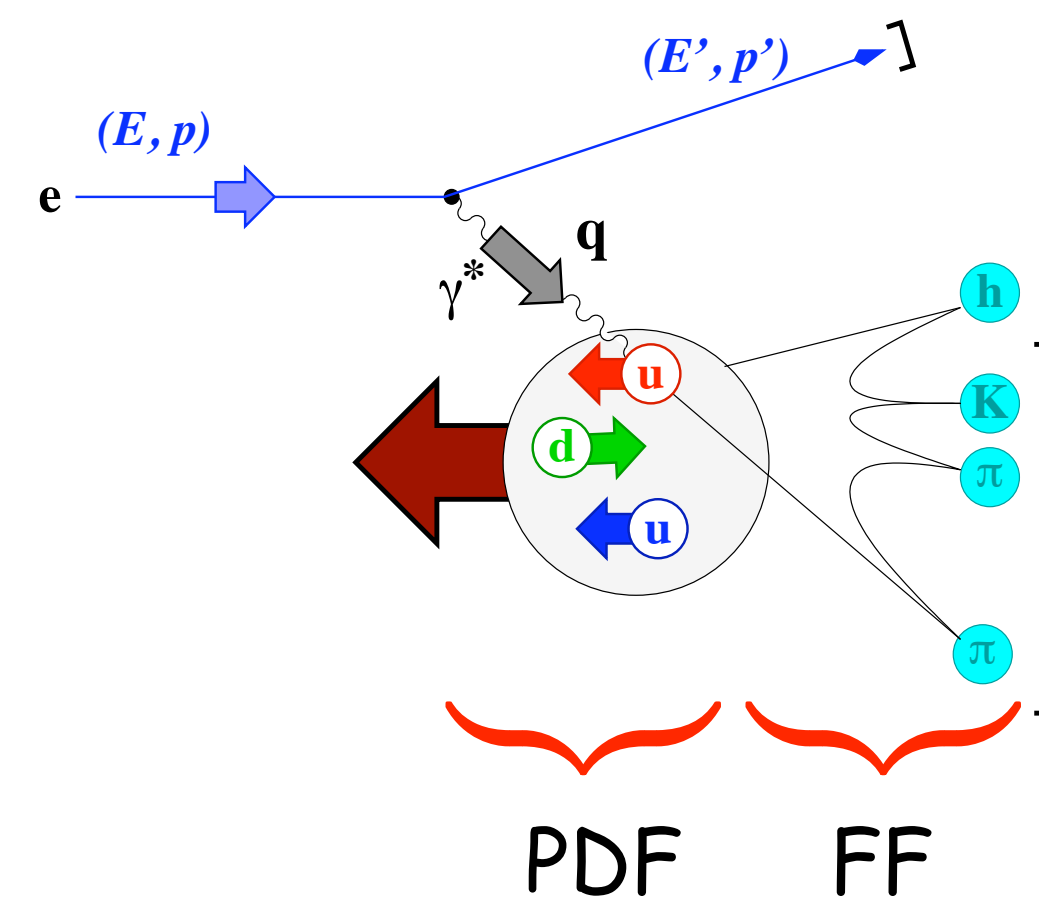
Collins FF: $H_1^{\perp, q \rightarrow h}$

ordinary FF: $D_1^{q \rightarrow h}$

TMDs in hadronization

		quark pol.				
		U	L	T		
hadron pol.	U	D_1		H_1^\perp	} relevant for unpolarized final state	polarized final-state hadrons (e.g., hyperons)
	L		G_1	H_{1L}^\perp		
	T	D_{1T}^\perp	G_{1T}^\perp	H_1 H_{1T}^\perp		

probing TMDs in semi-inclusive DIS



		quark pol.		
		U	L	T
nucleon pol.	U	f_1		h_1^\perp
	L		g_{1L}	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

in SIDIS*) couple PDFs to:

Collins FF: $H_1^\perp, q \rightarrow h$

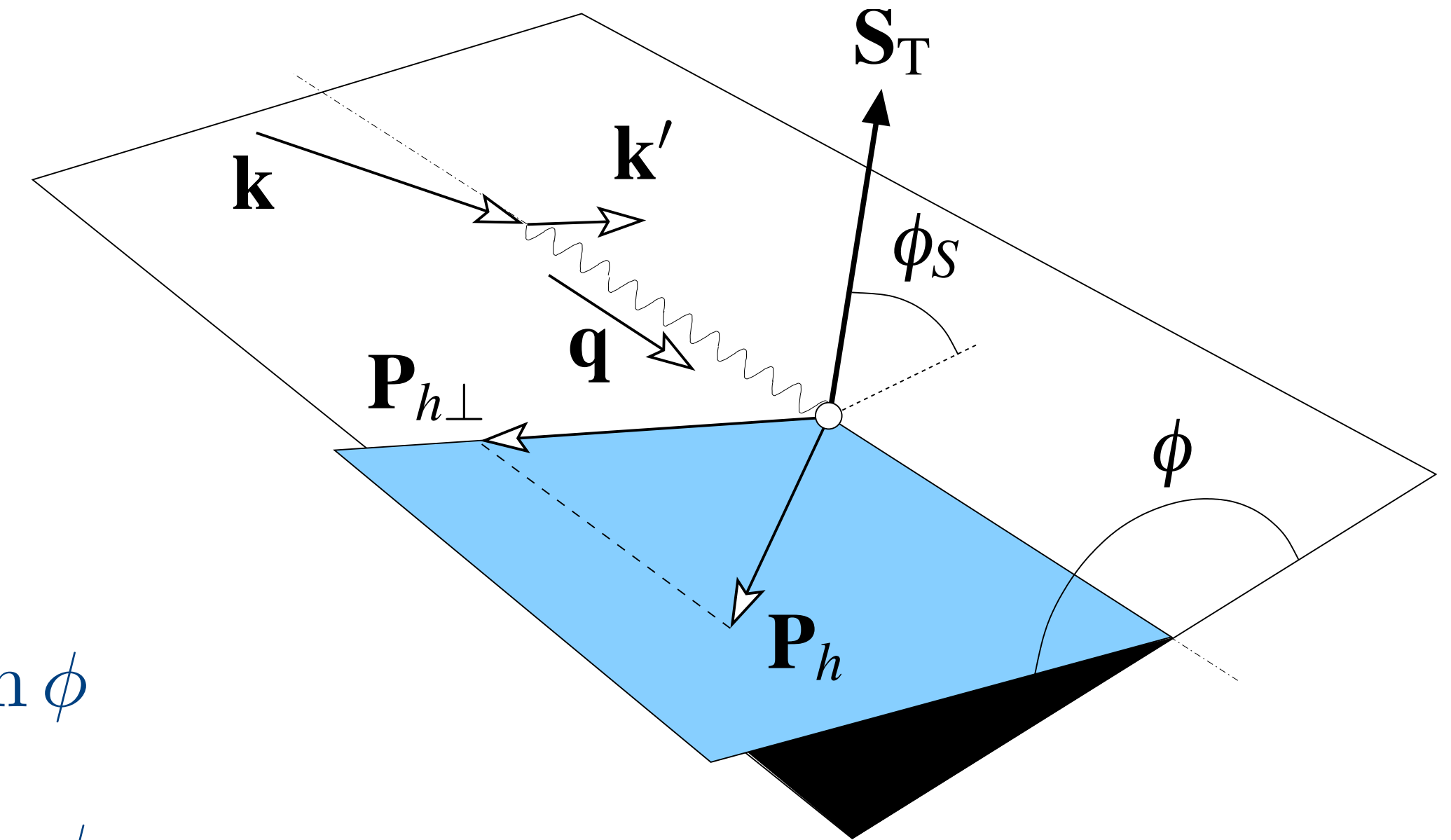
ordinary FF: $D_1^{q \rightarrow h}$

⇒ give rise to characteristic azimuthal dependences

*) semi-inclusive DIS with unpolarized final state

- excluding transverse polarization:

$$\frac{d\sigma^h}{dx dy dz dP_{h\perp}^2 d\phi} = \frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \left\{ F_{UU,T}^h + \epsilon F_{UU,L}^h + \lambda\Lambda\sqrt{1-\epsilon^2} F_{LL}^h \right. \\ \left. + \sqrt{2}\epsilon \left[\lambda\sqrt{1-\epsilon} F_{LU}^{h,\sin\phi} + \Lambda\sqrt{1+\epsilon} F_{UL}^{h,\sin\phi} \right] \sin\phi \right. \\ \left. + \sqrt{2}\epsilon \left[\lambda\Lambda\sqrt{1-\epsilon} F_{LL}^{h,\cos\phi} + \sqrt{1+\epsilon} F_{UU}^{h,\cos\phi} \right] \cos\phi \right. \\ \left. + \Lambda\epsilon F_{UL}^{h,\sin 2\phi} \sin 2\phi + \epsilon F_{UU}^{h,\cos 2\phi} \cos 2\phi \right\}$$

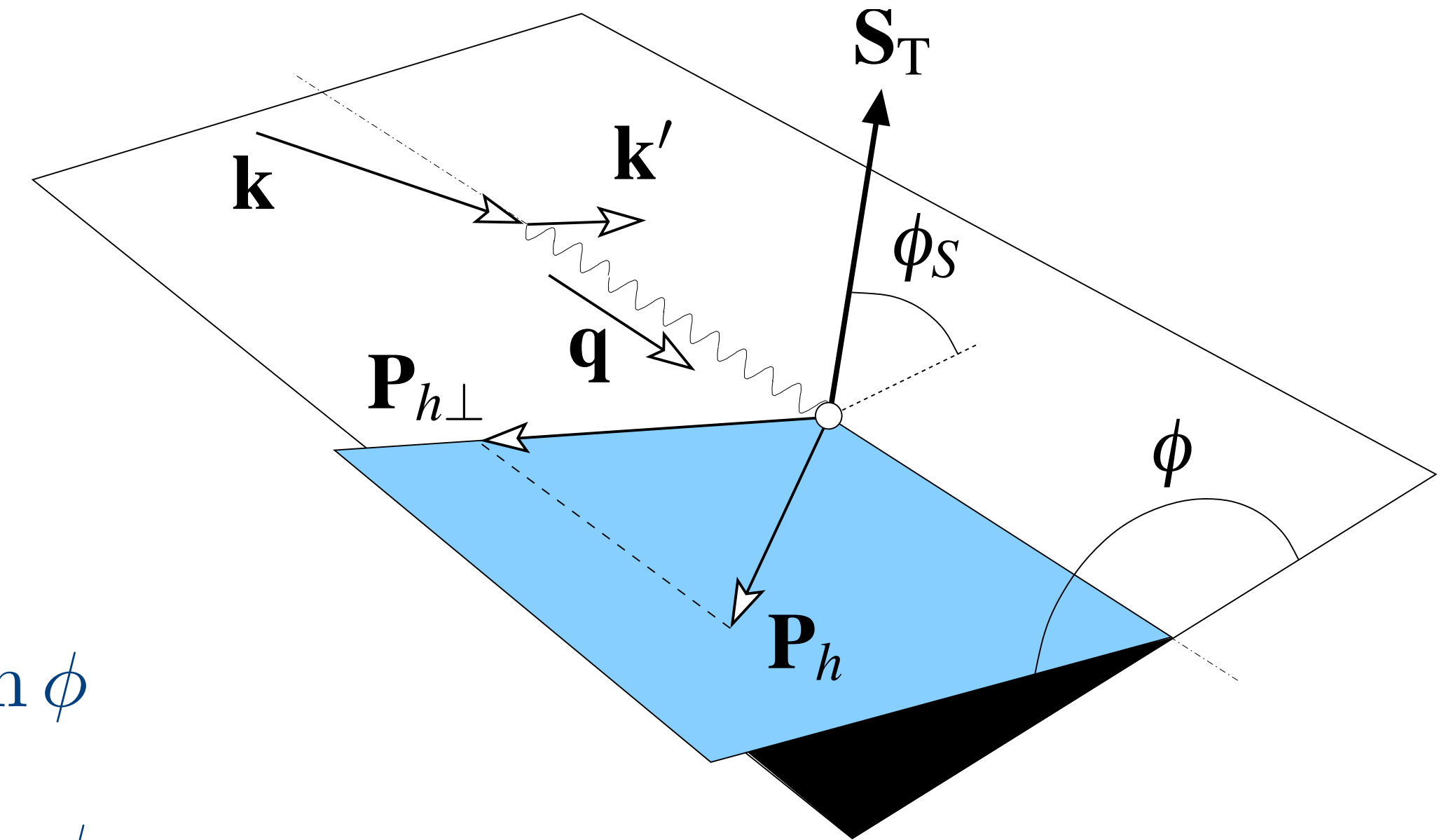


$$F_{XY}^{h,\text{mod}} = F_{XY}^{h,\text{mod}}(x, Q^2, z, P_{h\perp})$$

$\swarrow \quad \searrow$
 Beam (λ) / Target (Λ)
 helicities

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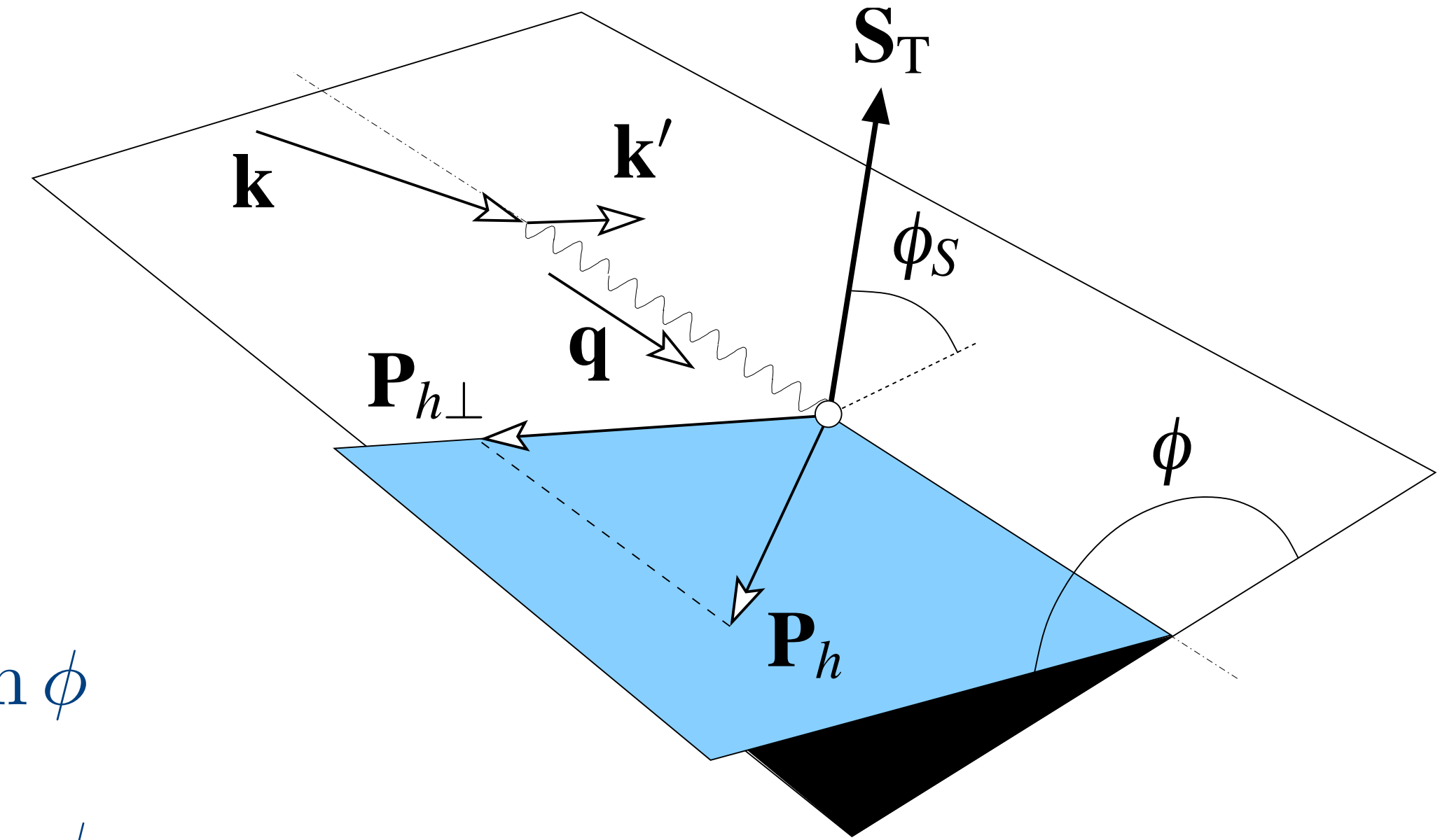


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- double-spin asymmetry:

$$A_{LL}^h \equiv \frac{\sigma_{++}^h - \sigma_{+-}^h + \sigma_{--}^h - \sigma_{-+}^h}{\sigma_{++}^h + \sigma_{+-}^h + \sigma_{--}^h + \sigma_{-+}^h}$$

- excluding transverse polarization:

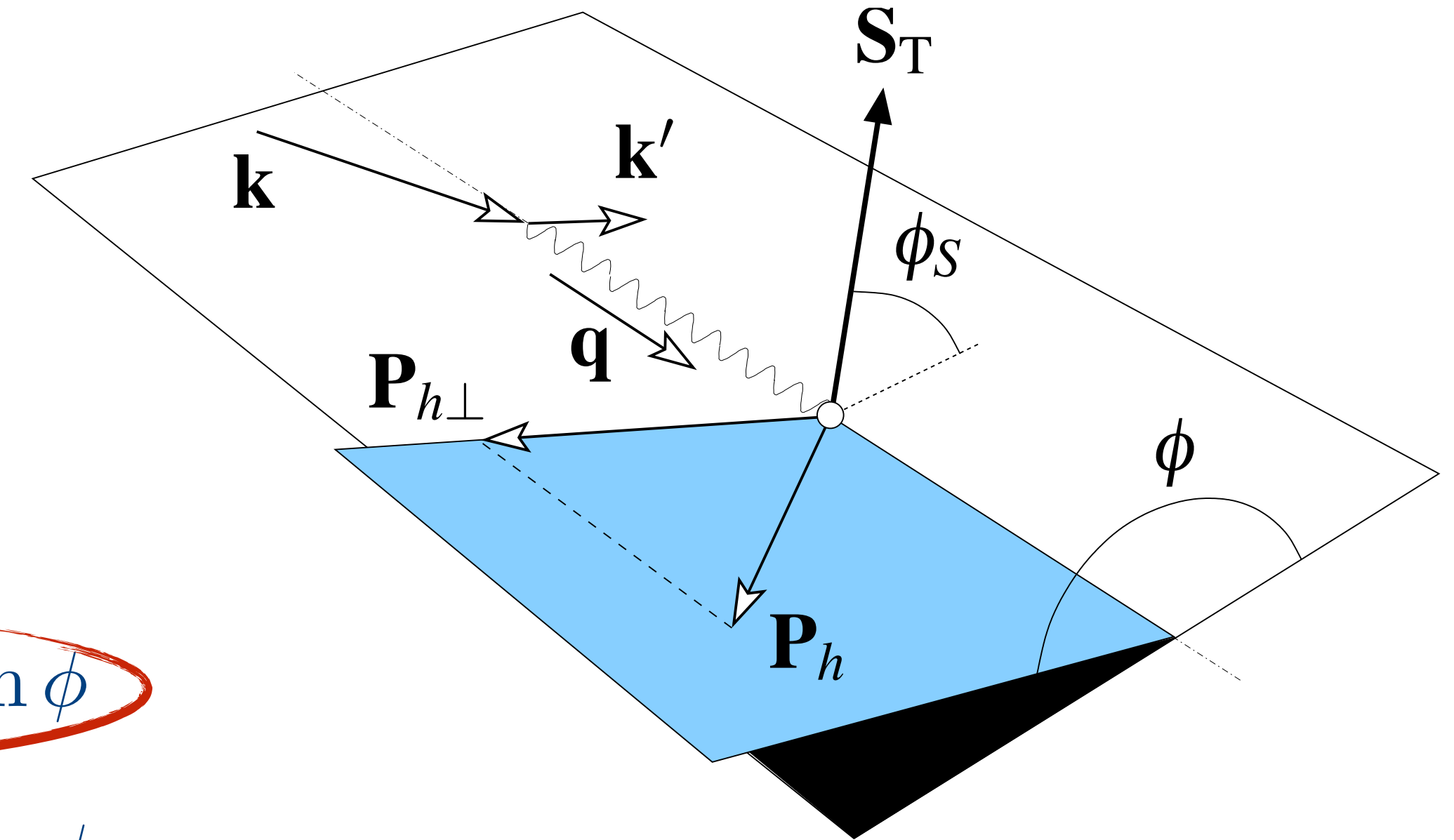
$$\frac{d\sigma^h}{dx dy dz dP_{h\perp}^2 d\phi} = \frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right)$$

$$\left\{ F_{UU,T}^h + \epsilon F_{UU,L}^h + \lambda\Lambda\sqrt{1-\epsilon^2} F_{LL}^h \right.$$

$$+ \sqrt{2}\epsilon \left[\lambda\sqrt{1-\epsilon} F_{LU}^{h,\sin\phi} + \Lambda\sqrt{1+\epsilon} F_{UL}^{h,\sin\phi} \right] \sin\phi$$

$$+ \sqrt{2}\epsilon \left[\lambda\Lambda\sqrt{1-\epsilon} F_{LL}^{h,\cos\phi} + \sqrt{1+\epsilon} F_{UU}^{h,\cos\phi} \right] \cos\phi$$

$$\left. + \Lambda\epsilon F_{UL}^{h,\sin 2\phi} \sin 2\phi + \epsilon F_{UU}^{h,\cos 2\phi} \cos 2\phi \right\}$$



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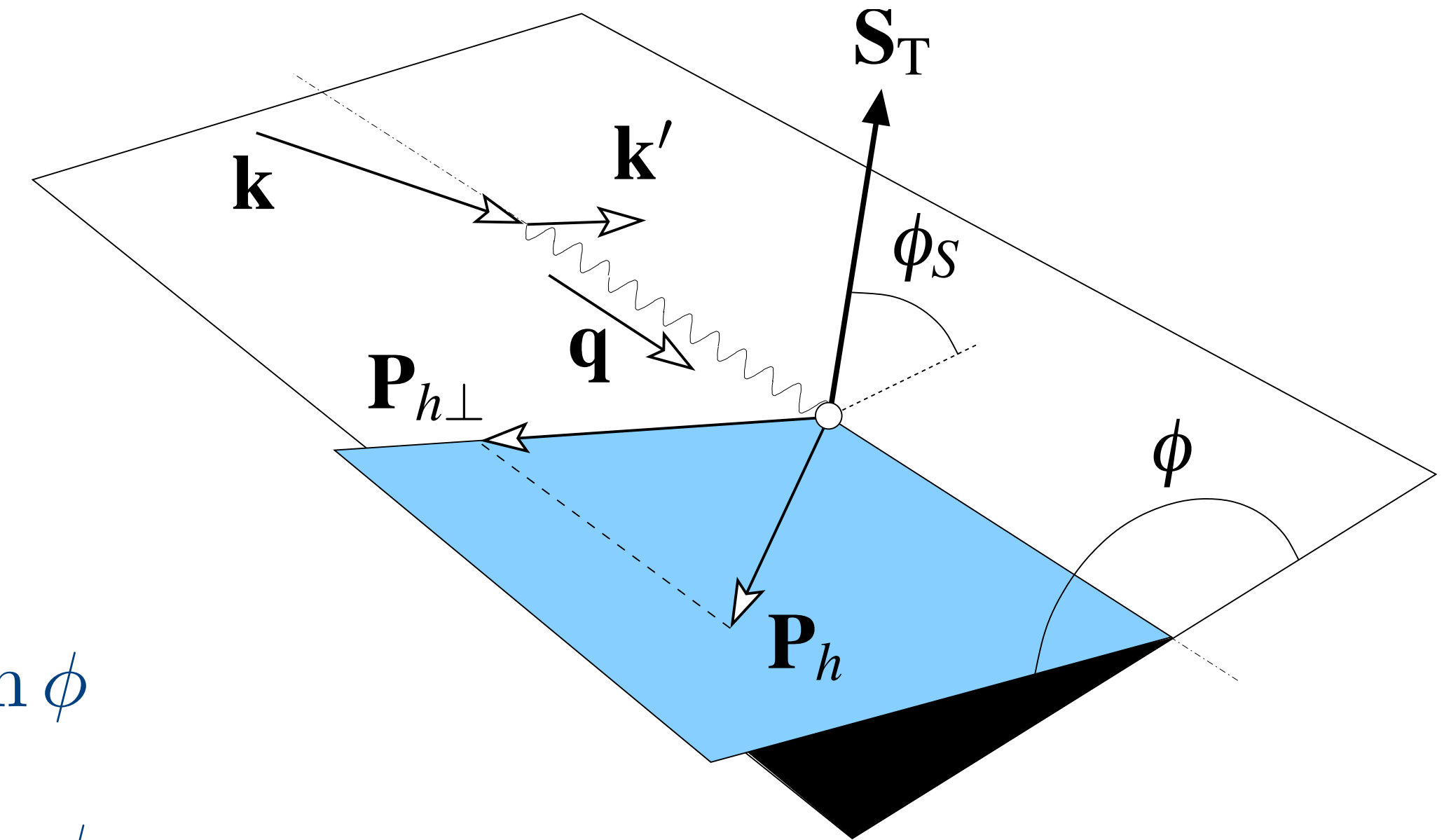
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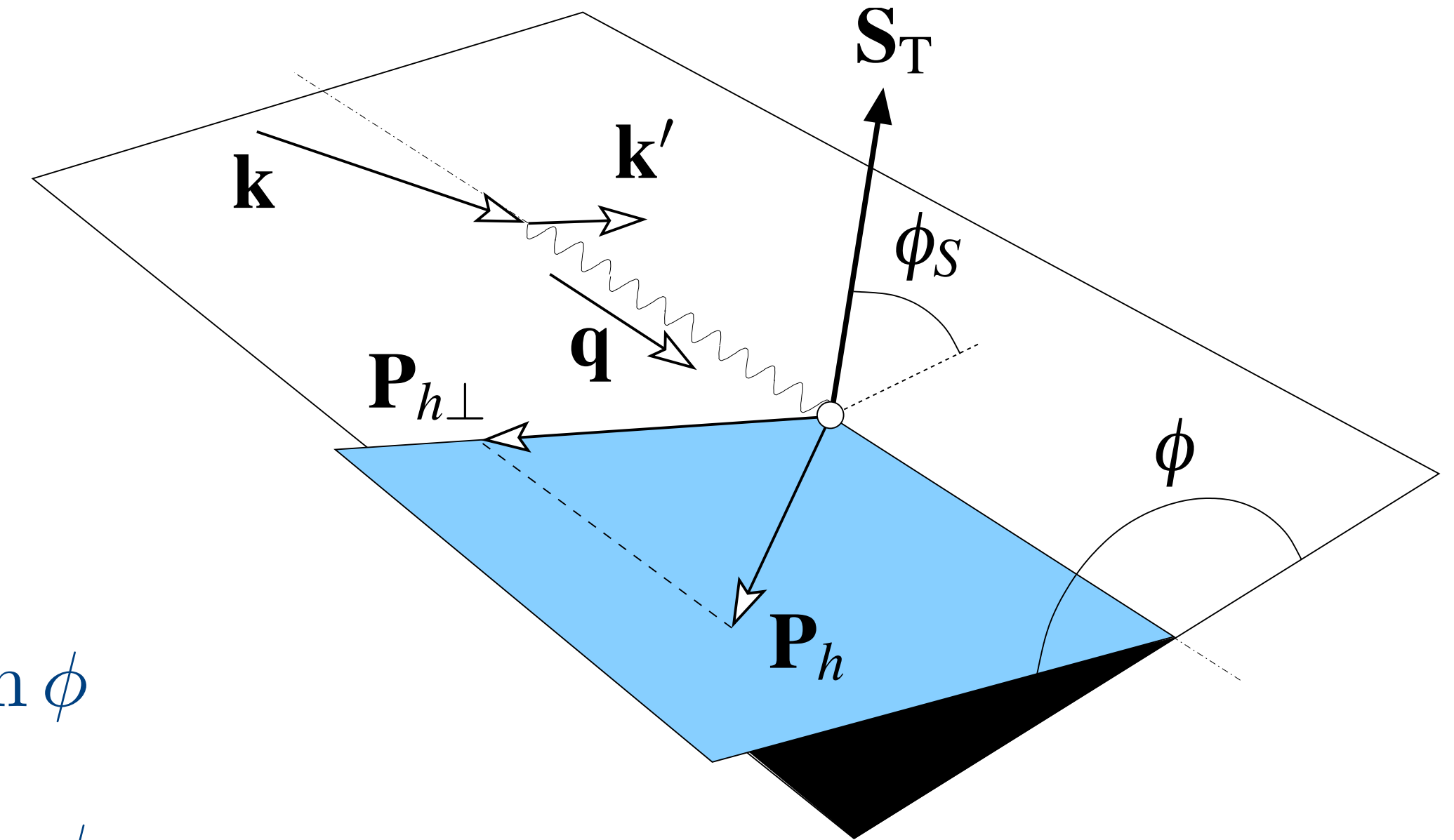
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- excluding transverse polarization:

$$\frac{d\sigma^h}{dx dy dz dP_{h\perp}^2 d\phi} = \frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \left\{ F_{UU,T}^h + \epsilon F_{UU,L}^h + \lambda\Lambda\sqrt{1-\epsilon^2} F_{LL}^h \right. \\ \left. + \sqrt{2}\epsilon \left[\lambda\sqrt{1-\epsilon} F_{LU}^{h,\sin\phi} + \Lambda\sqrt{1+\epsilon} F_{UL}^{h,\sin\phi} \right] \sin\phi \right. \\ \left. + \sqrt{2}\epsilon \left[\lambda\Lambda\sqrt{1-\epsilon} F_{LL}^{h,\cos\phi} + \sqrt{1+\epsilon} F_{UU}^{h,\cos\phi} \right] \cos\phi \right. \\ \left. + \Lambda\epsilon F_{UL}^{h,\sin 2\phi} \sin 2\phi + \epsilon F_{UU}^{h,\cos 2\phi} \cos 2\phi \right\}$$



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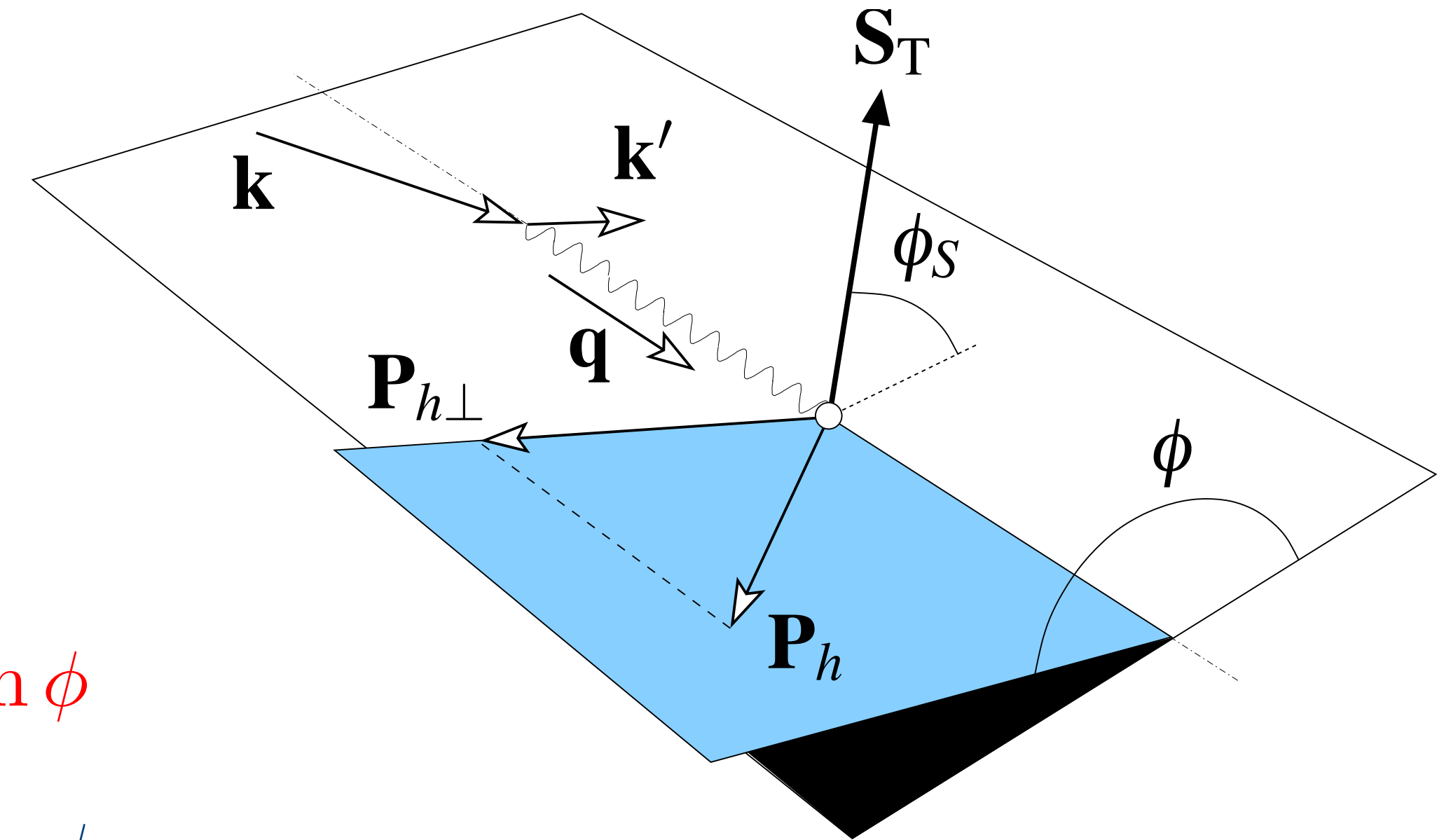
semi-inclusive DIS

- excluding transverse polarization:

$$\frac{d\sigma^h}{dx dy dz dP_{h\perp}^2 d\phi} = \frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \left\{ F_{UU,T}^h + \epsilon F_{UU,L}^h + \lambda\Lambda\sqrt{1-\epsilon^2} F_{LL}^h \right. \\ \left. + \sqrt{2}\epsilon \left[\lambda\sqrt{1-\epsilon} F_{LU}^{h,\sin\phi} + \Lambda\sqrt{1+\epsilon} F_{UL}^{h,\sin\phi} \right] \sin\phi \right. \\ \left. + \sqrt{2}\epsilon \left[\lambda\Lambda\sqrt{1-\epsilon} F_{LL}^{h,\cos\phi} + \sqrt{1+\epsilon} F_{UU}^{h,\cos\phi} \right] \cos\phi \right. \\ \left. + \Lambda\epsilon F_{UL}^{h,\sin 2\phi} \sin 2\phi + \epsilon F_{UU}^{h,\cos 2\phi} \cos 2\phi \right\}$$

- single-spin asymmetry:

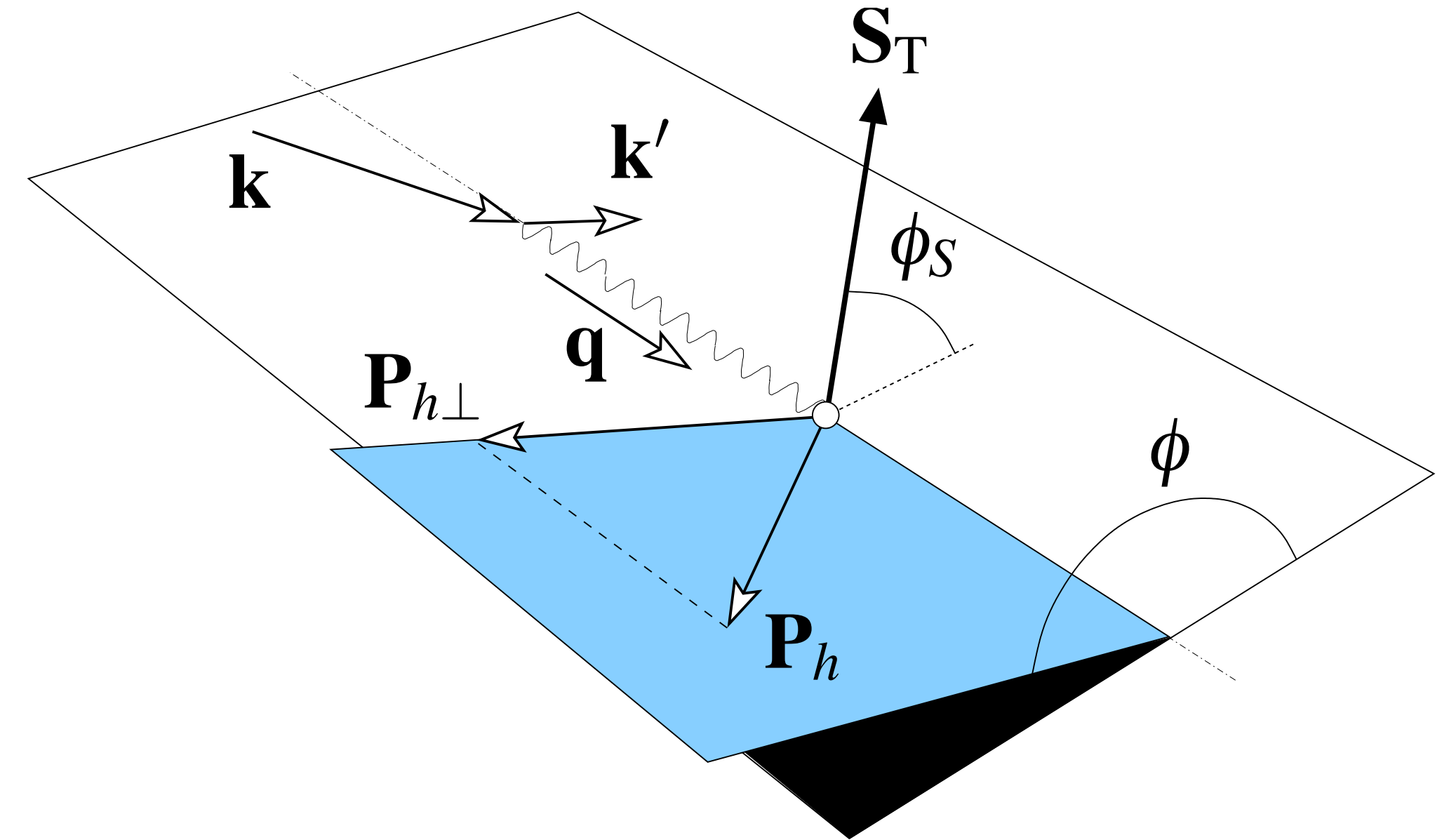
- explicit angular dependence to be analyzed



$$A_{LU}^h \equiv \frac{\sigma_{+-}^h + \sigma_{++}^h - \sigma_{-+}^h - \sigma_{--}^h}{\sigma_{+-}^h + \sigma_{++}^h + \sigma_{-+}^h + \sigma_{--}^h}$$

- with transverse target polarization:

$$\begin{aligned}
 \frac{d\sigma^h}{dx dy dz dP_{h\perp}^2 d\phi d\phi_s} &= \frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \\
 &\left\{ F_{UU,T}^h + \epsilon F_{UU,L}^h + \text{terms not involving transv. polarization} \right. \\
 &\quad + S_T \left[\left(F_{UT,T}^{h,\sin(\phi-\phi_s)} + \epsilon F_{UT,L}^{h,\sin(\phi-\phi_s)} \right) \sin(\phi - \phi_s) \right. \\
 &\quad \quad + \epsilon F_{UT}^{h,\sin(\phi+\phi_s)} \sin(\phi + \phi_s) + \epsilon F_{UT}^{h,\sin(3\phi-\phi_s)} \sin(3\phi - \phi_s) \\
 &\quad \quad \left. + \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{h,\sin\phi_s} \sin\phi_s + \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{h,\sin(2\phi-\phi_s)} \sin(2\phi - \phi_s) \right] \\
 &\quad + S_T \lambda \left[\sqrt{1-\epsilon^2} F_{LT}^{h,\cos(\phi-\phi_s)} \cos(\phi - \phi_s) \right. \\
 &\quad \quad \left. \left. + \sqrt{2\epsilon(1-\epsilon)} F_{LT}^{h,\cos\phi_s} \cos\phi_s + \sqrt{2\epsilon(1-\epsilon)} F_{LT}^{h,\cos(2\phi-\phi_s)} \cos(2\phi - \phi_s) \right] \right\}
 \end{aligned}$$



- with transverse target polarization:

$$\frac{d\sigma^h}{dx dy dz dP_{h\perp}^2 d\phi d\phi_s} = \frac{2\pi\alpha^2}{(1-\epsilon)} \frac{y^2}{\left(1 + \frac{\gamma^2}{2x}\right)}$$

Sivers

$$\left\{ F_{UU,T}^h + \epsilon F_{UU,L}^h + \text{terms not involving transv. polarization} \right.$$

$$+ S_T \left[\left(F_{UT,T}^{h,\sin(\phi-\phi_s)} + \epsilon F_{UT,L}^{h,\sin(\phi-\phi_s)} \right) \sin(\phi - \phi_s) \right.$$

pretzelosity

$$+ \epsilon F_{UT}^{h,\sin(\phi+\phi_s)} \sin(\phi + \phi_s) + \epsilon F_{UT}^{h,\sin(3\phi-\phi_s)} \sin(3\phi - \phi_s)$$

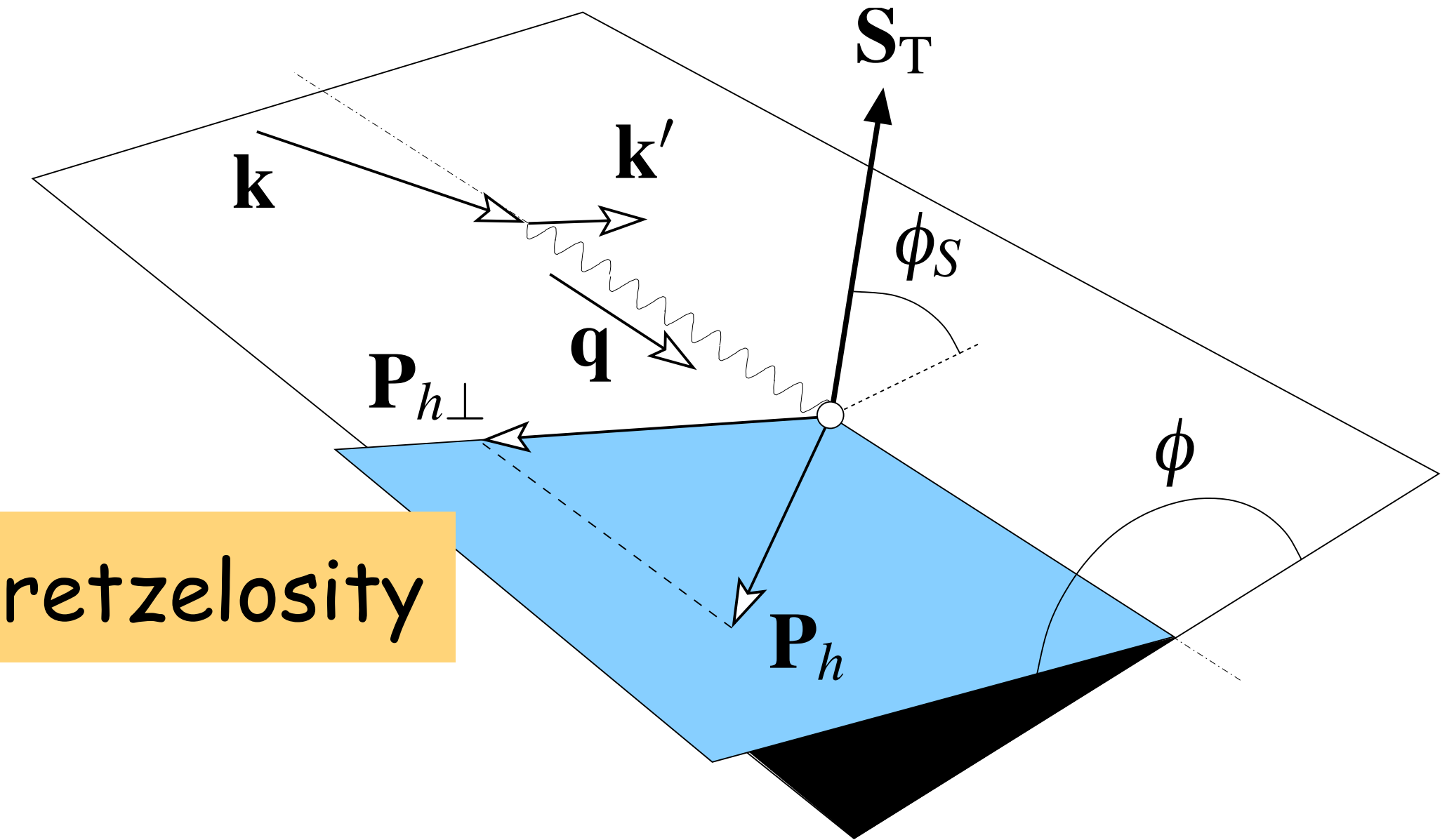
transversity

$$+ \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{h,\sin\phi_s} \sin\phi_s + \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{h,\sin(2\phi-\phi_s)} \sin(2\phi - \phi_s) \left. \right]$$

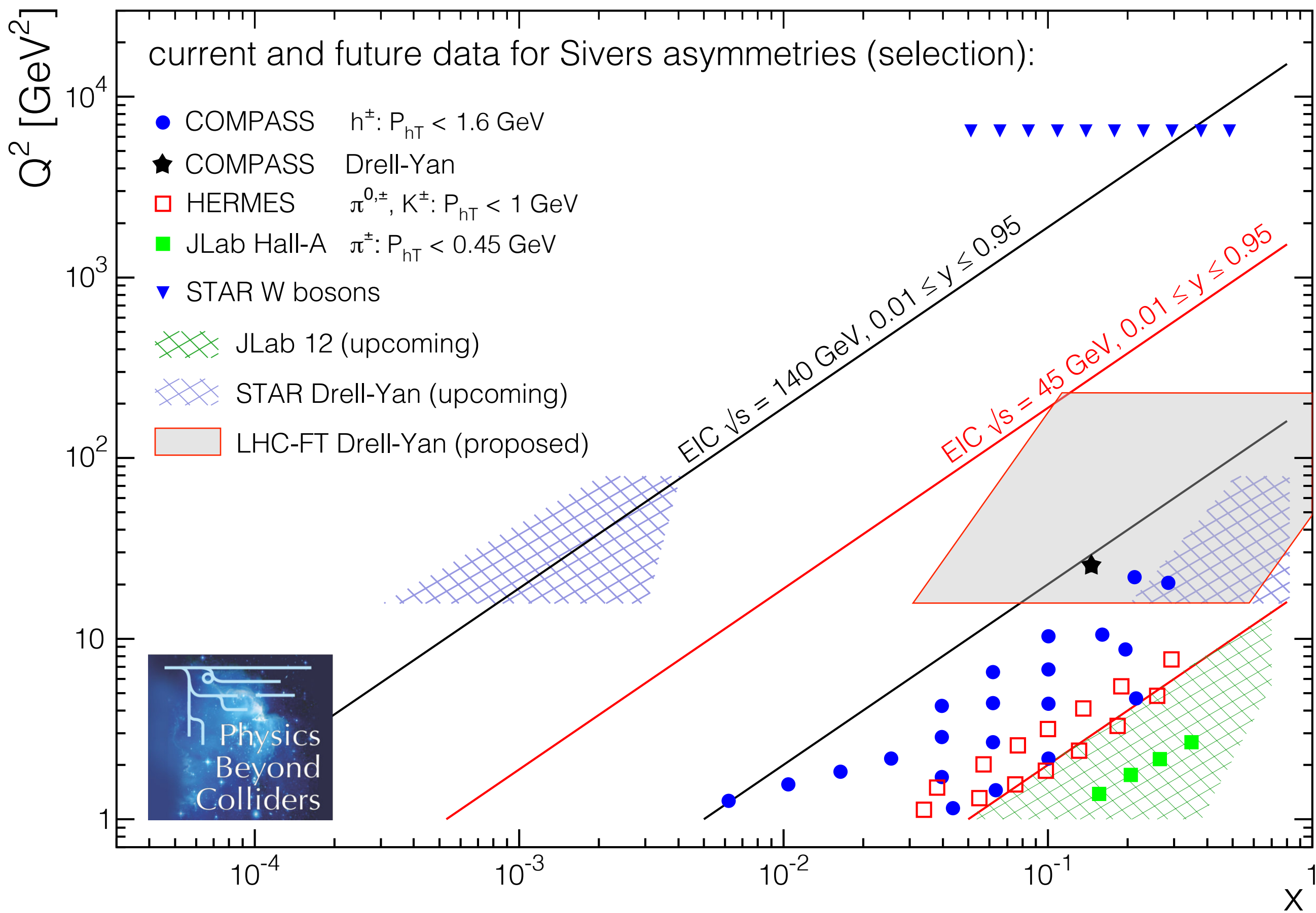
$$+ S_T \lambda \left[\sqrt{1-\epsilon^2} F_{LT}^{h,\cos(\phi-\phi_s)} \cos(\phi - \phi_s) \right.$$

worm-gear

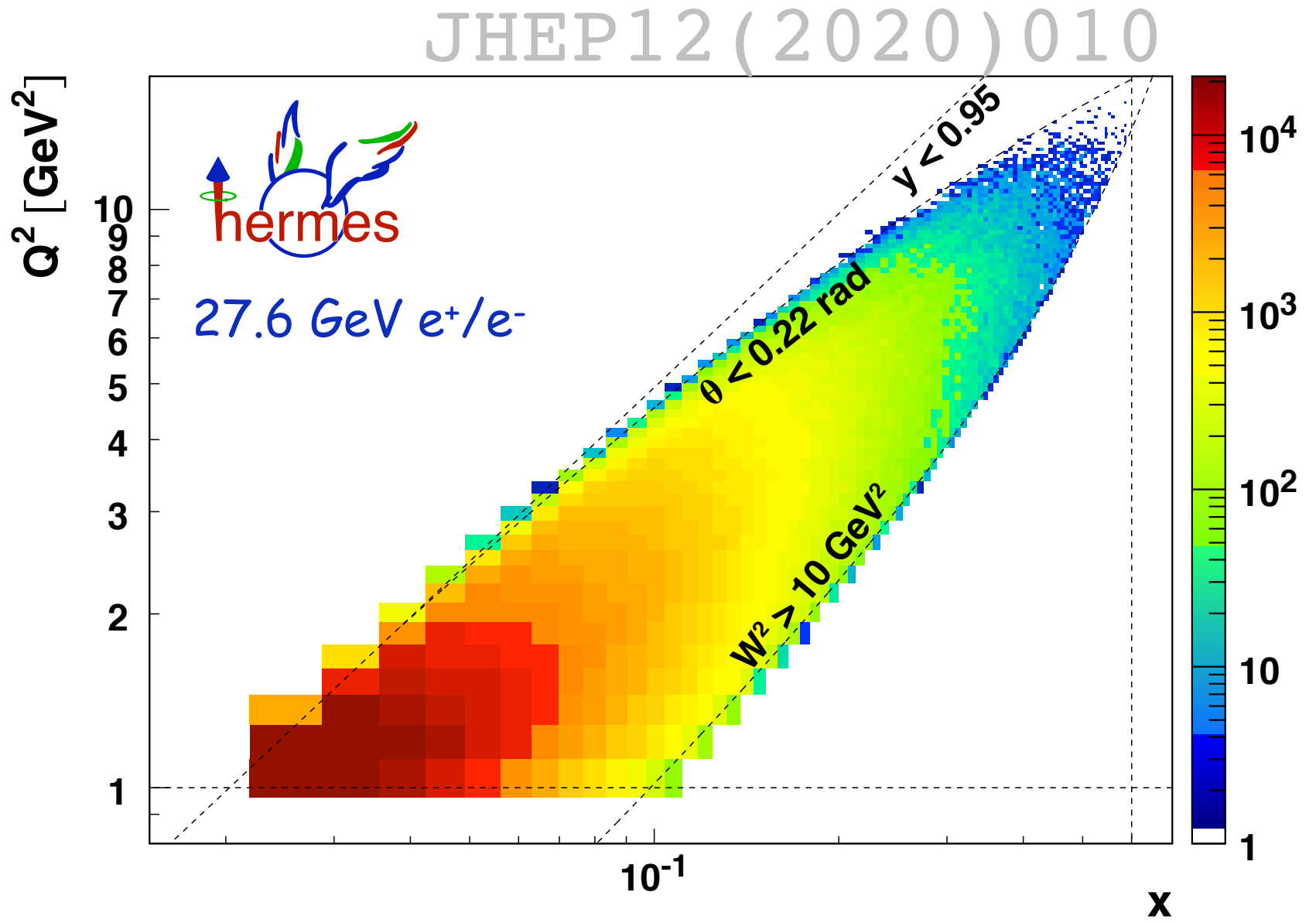
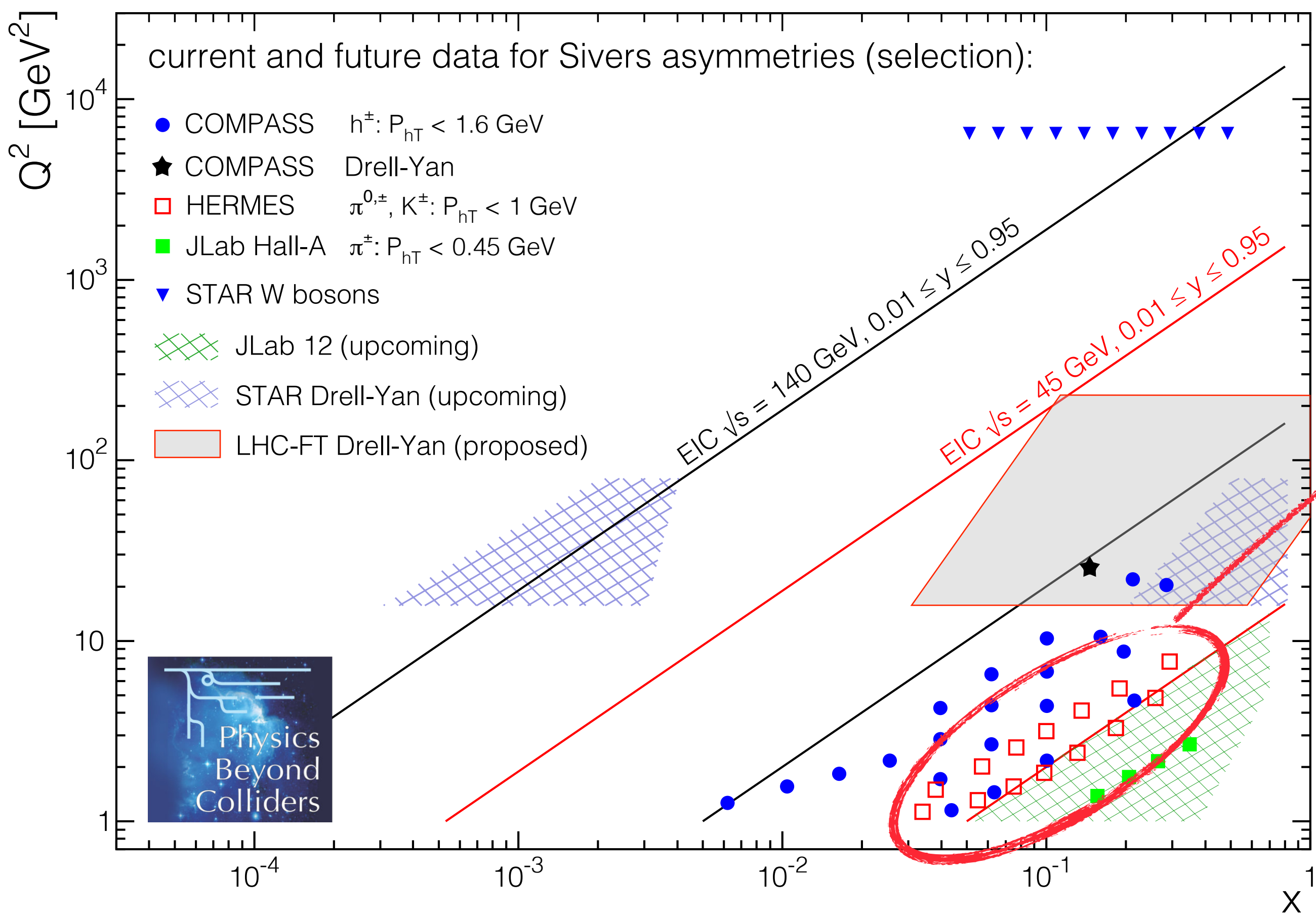
$$+ \sqrt{2\epsilon(1-\epsilon)} F_{LT}^{h,\cos\phi_s} \cos\phi_s + \sqrt{2\epsilon(1-\epsilon)} F_{LT}^{h,\cos(2\phi-\phi_s)} \cos(2\phi - \phi_s) \left. \right\}$$



2d kinematic phase space



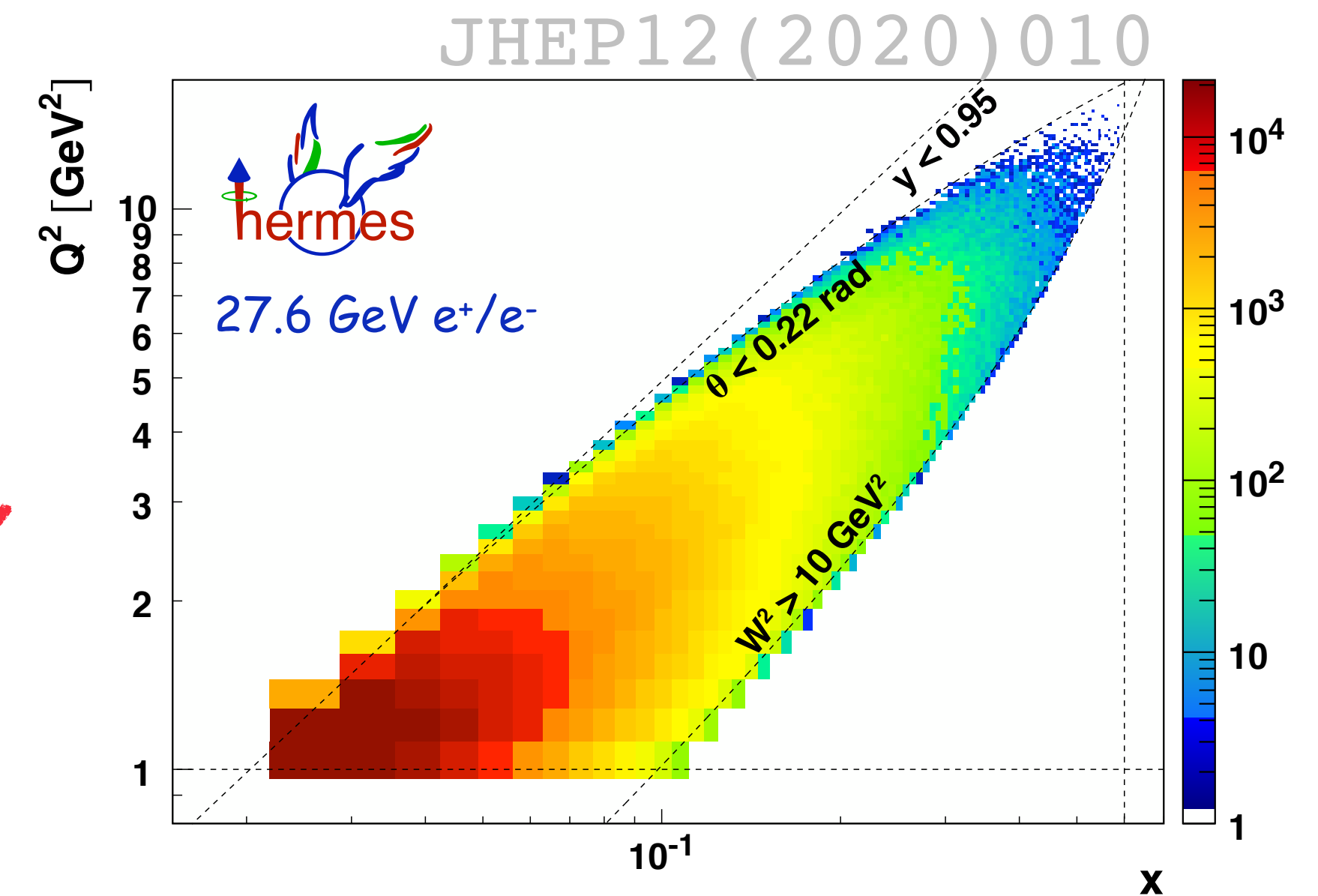
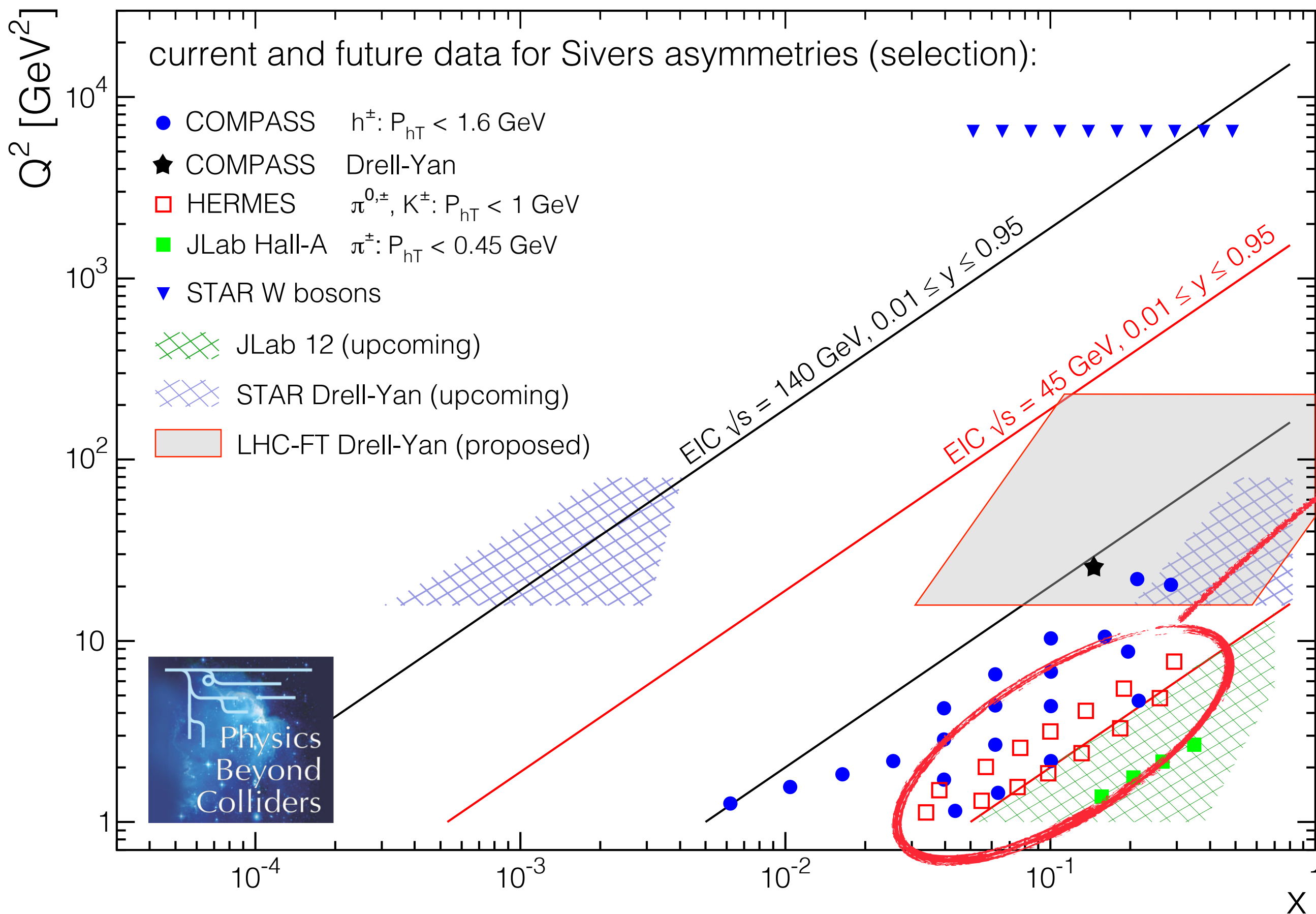
2d kinematic phase space



Scattered lepton:	Q^2	$> 1 \text{ GeV}^2$
	W^2	$> 10 \text{ GeV}^2$
Detected hadrons:	$0.023 < x$	< 0.6
	$0.1 < y$	< 0.95
	$2 \text{ GeV} < \mathbf{P}_h $	$< 15 \text{ GeV}$ charged mesons
	$4 \text{ GeV} < \mathbf{P}_h $	$< 15 \text{ GeV}$ (anti)protons
	$ \mathbf{P}_h $	$> 2 \text{ GeV}$ neutral pions
	$P_{h\perp}$	$< 2 \text{ GeV}$
	$0.2 < z$	< 0.7 (1.2 for the “semi-exclusive” region)

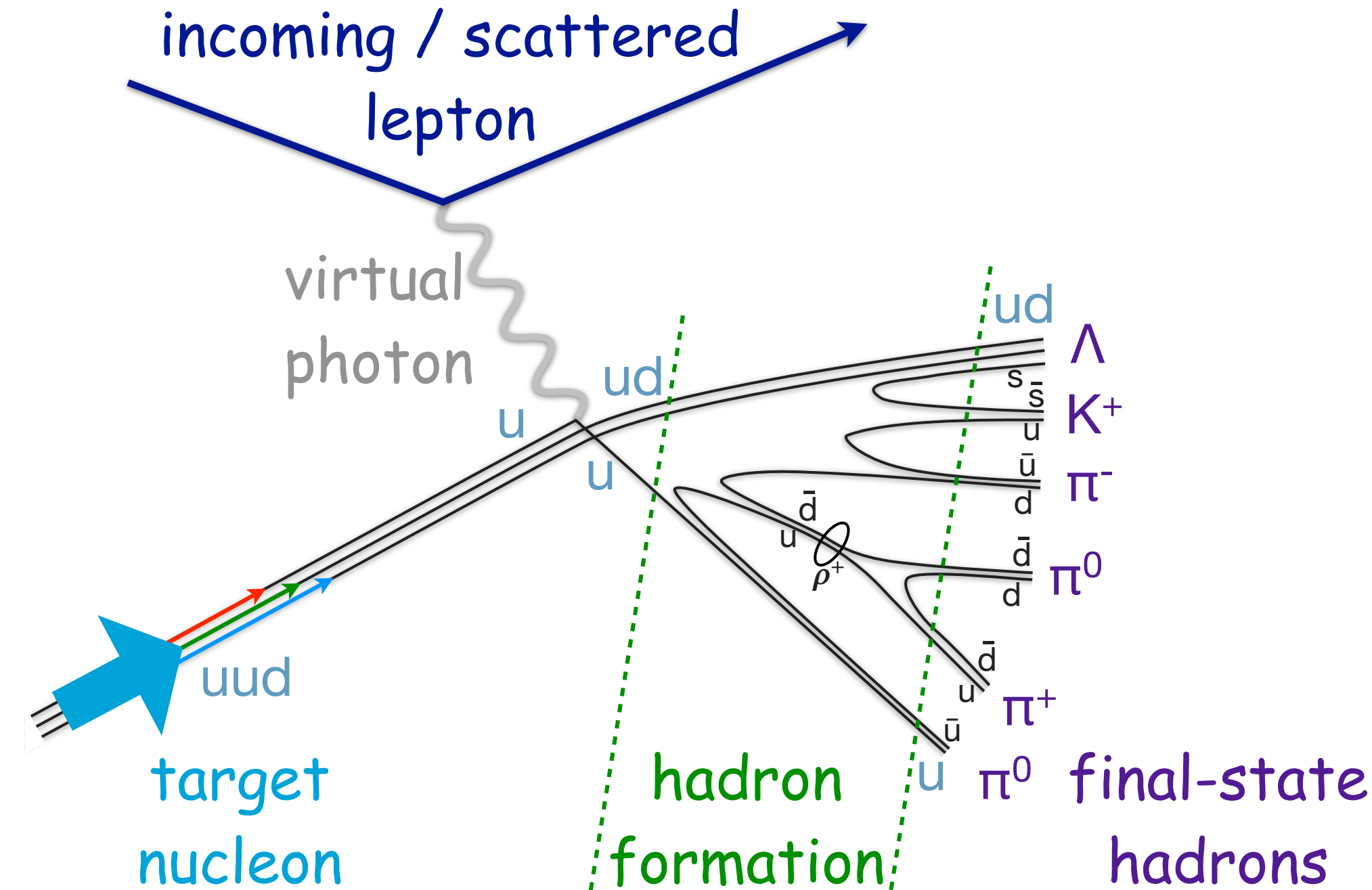
Table 3. Restrictions on selected kinematics variables. The upper limit on z of 1.2 applies only to the analysis of the z dependence.

2d kinematic phase space

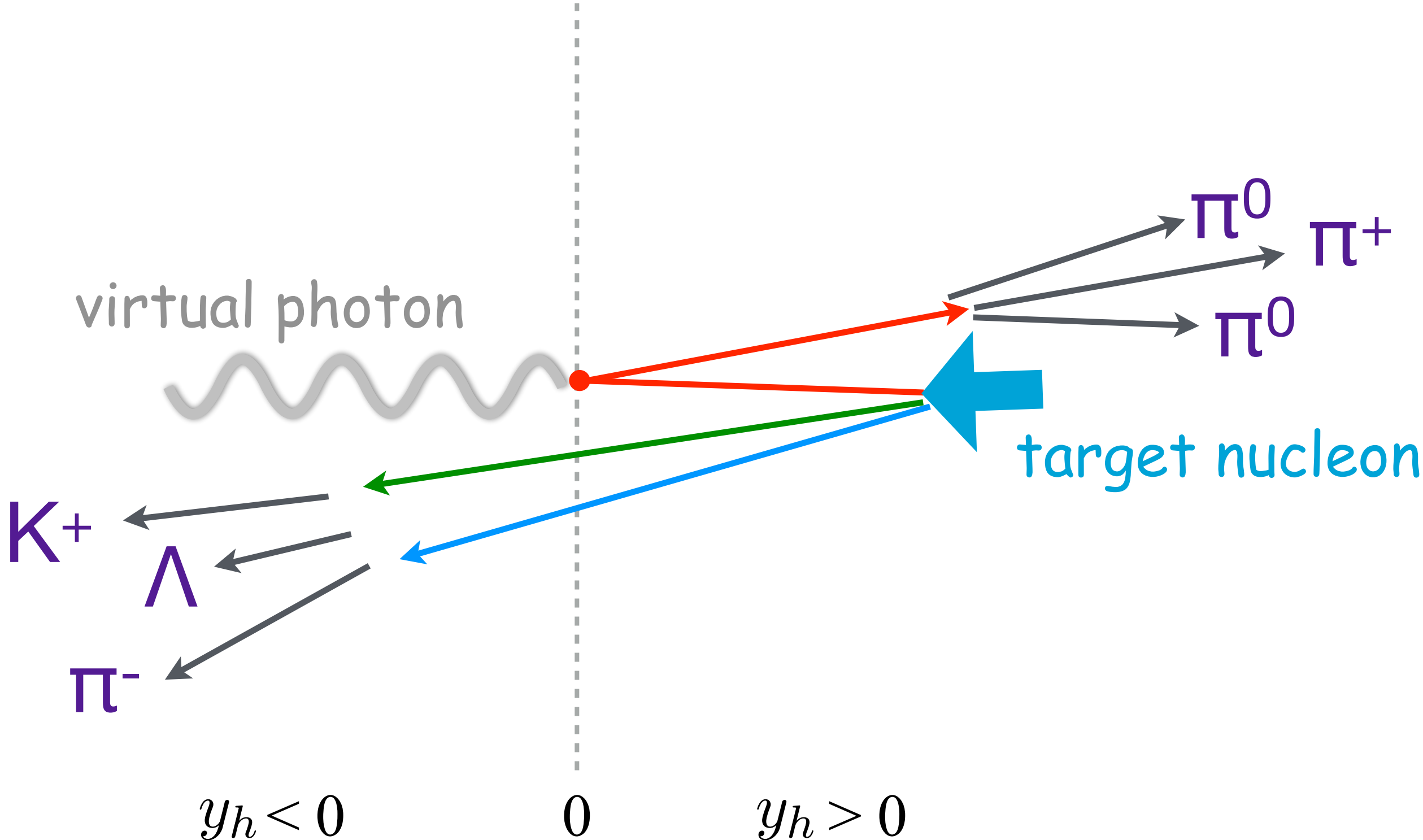


2d (x - Q^2) kinematic space not
the only relevant one for
SIDIS interpretation

current vs. target fragmentation



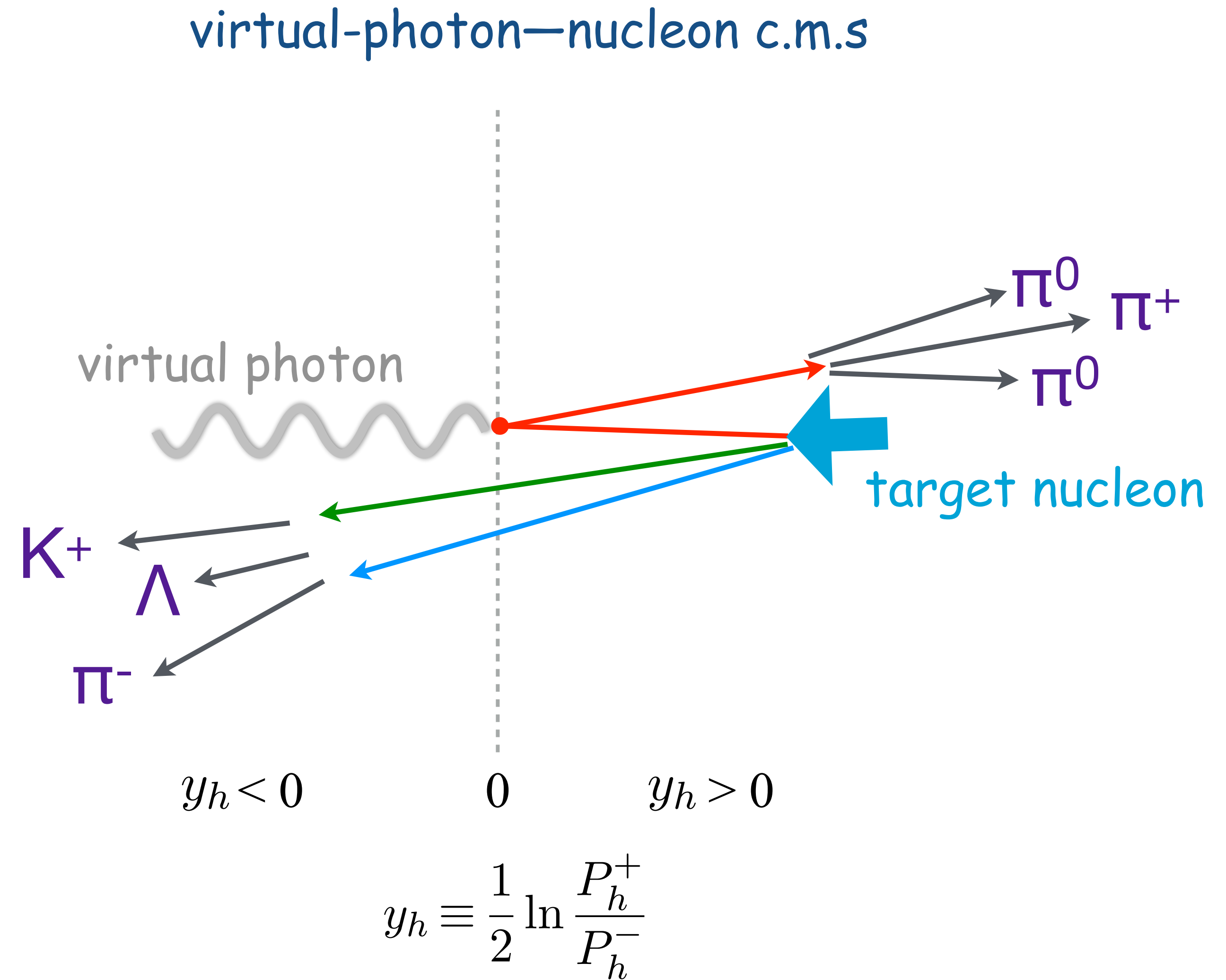
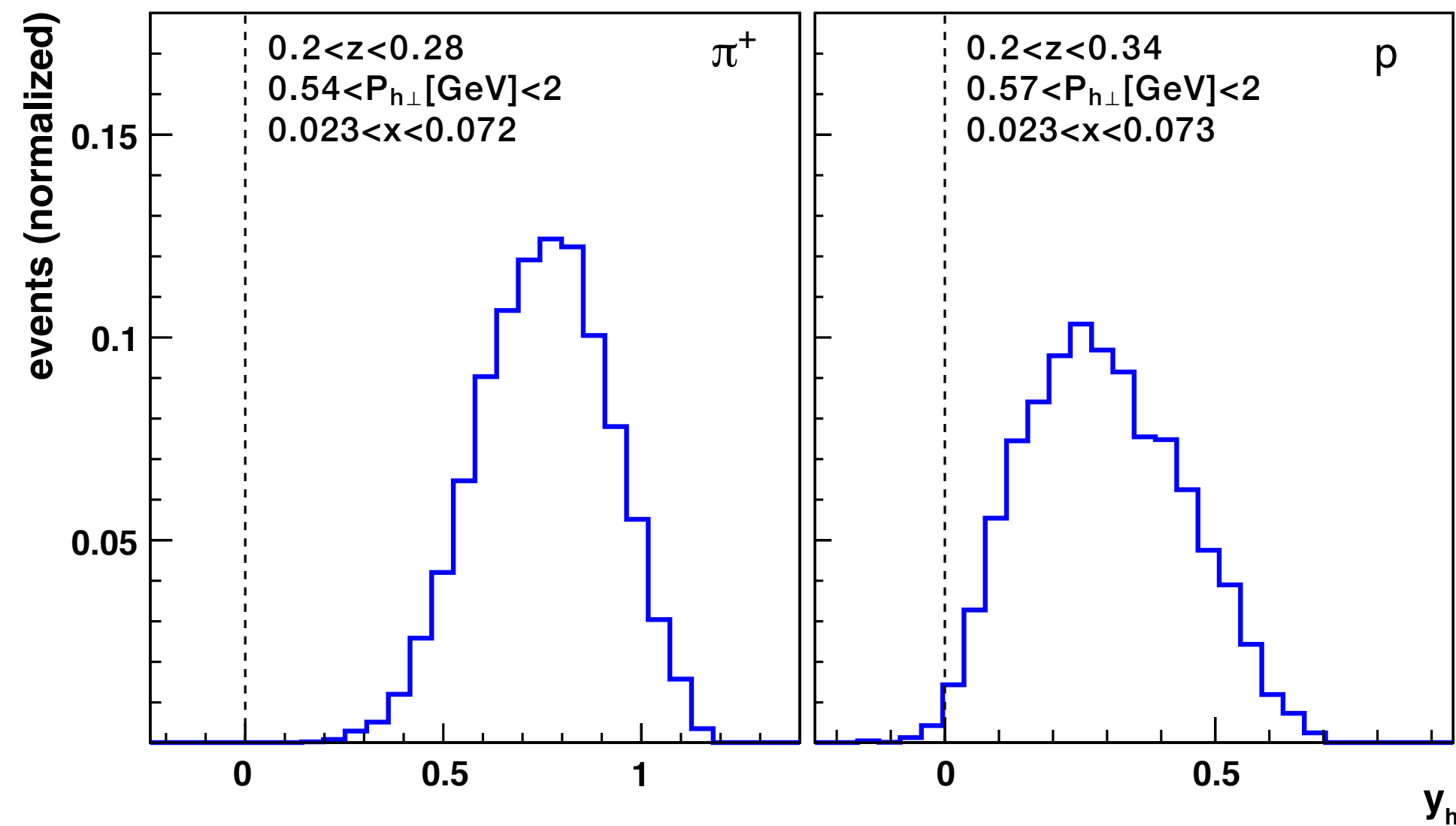
virtual-photon—nucleon c.m.s



$$y_h \equiv \frac{1}{2} \ln \frac{P_h^+}{P_h^-}$$

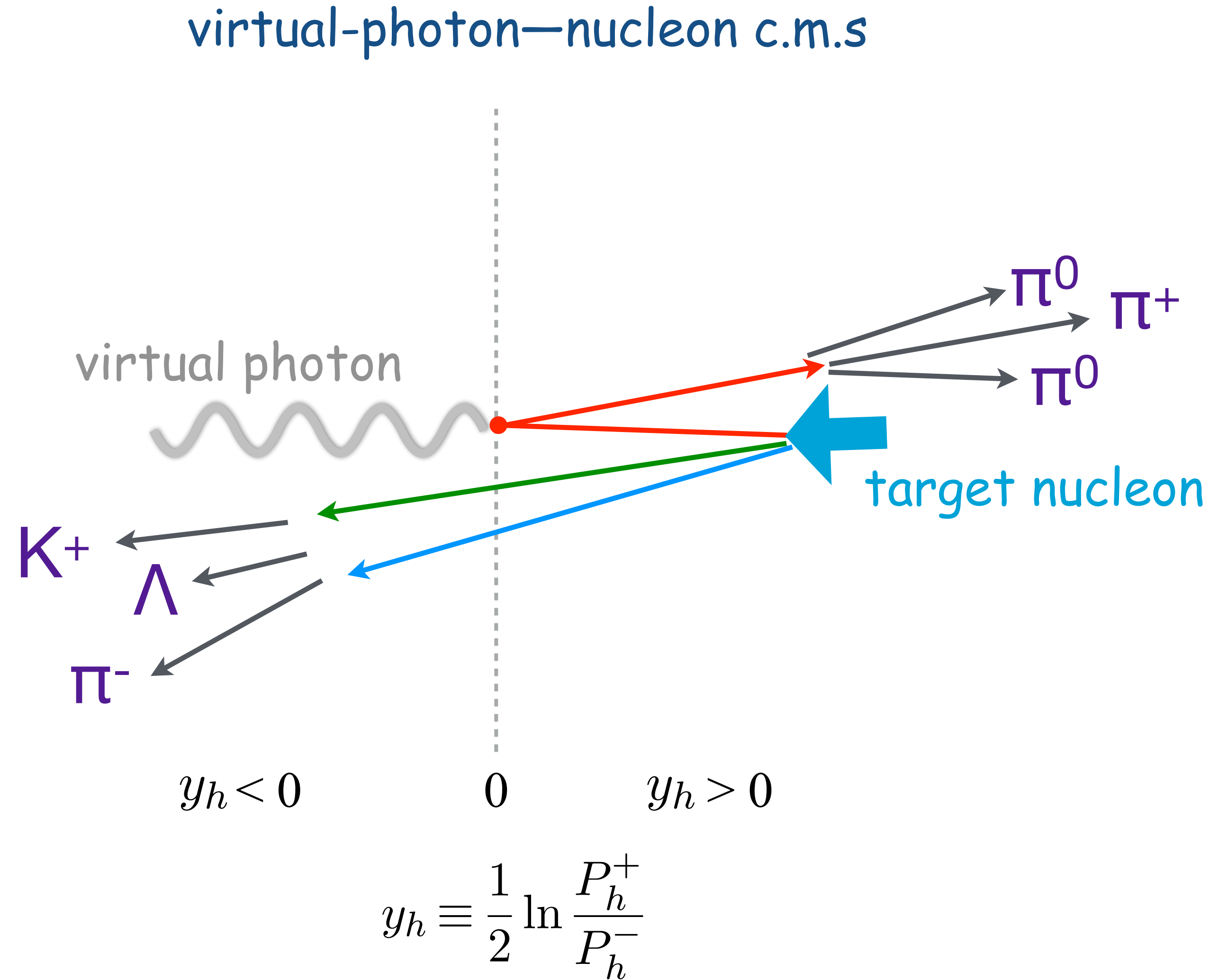
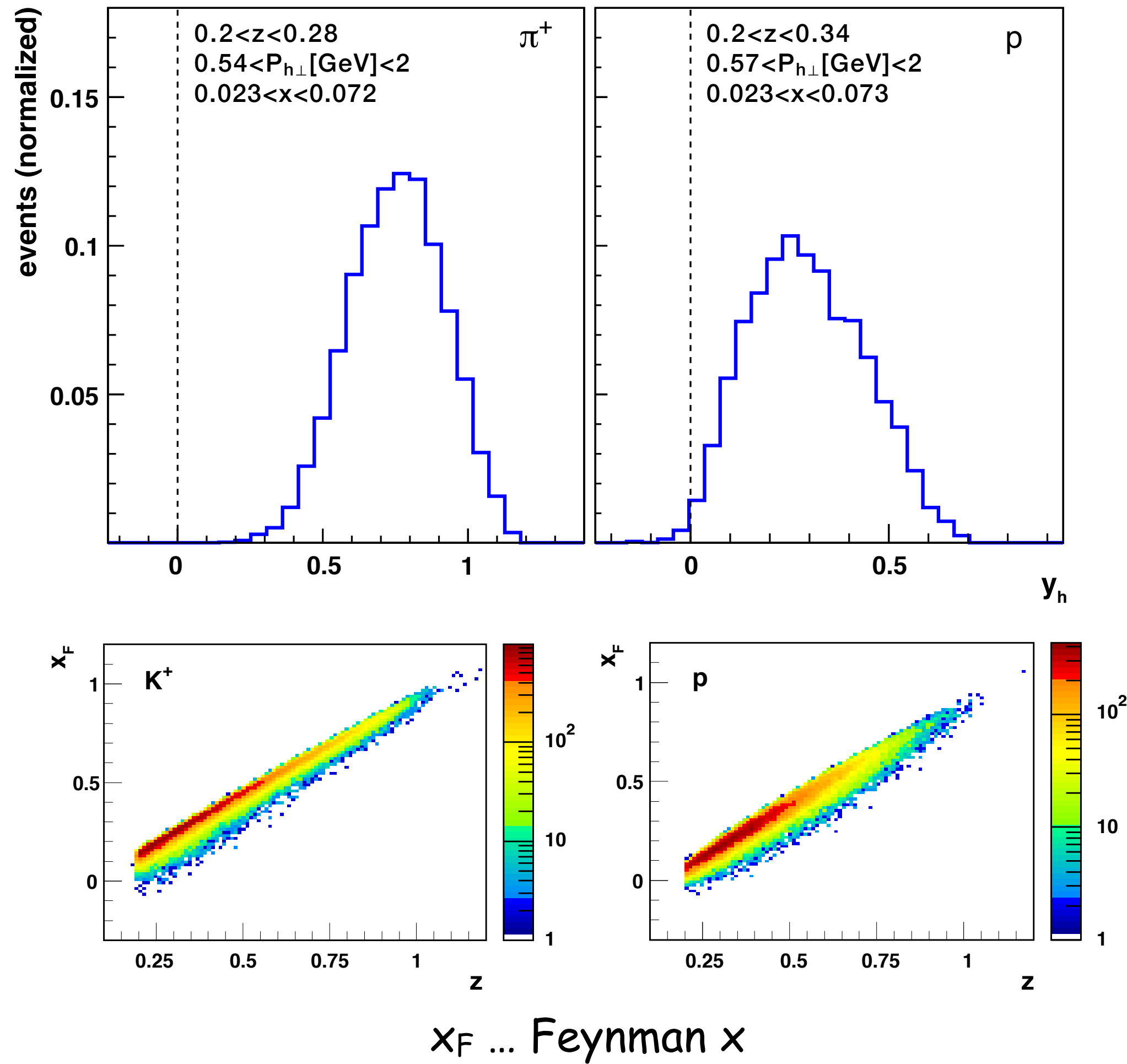
P_h^\pm ... light-cone momenta

current vs. target fragmentation



P_h^\pm ... light-cone momenta

current vs. target fragmentation



selected hadrons at HERMES mainly
forward-going in photon-nucleon c.m.s.

$P_h^\pm \dots$ light-cone momenta

Longitudinal double-spin asymmetries in semi-inclusive deep-inelastic scattering of electrons and positrons by protons and deuterons

A. Airapetian,^{13,16} N. Akopov,²⁶ Z. Akopov,⁶ E. C. Aschenauer,⁷ W. Augustyniak,²⁵ R. Avakian,²⁶ A. Avetissian,²⁶
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 S. I. Manaenkov,¹⁹ Y. Mao,³ B. Marianski,²⁵ H. Marukyan,²⁶ Y. Miyachi,²³ A. Movsisyan,^{10,26} V. Muccifora,¹¹
 A. Mussgiller,^{6,9} Y. Naryshkin,¹⁹ A. Nass,⁹ G. Nazaryan,²⁶ W.-D. Nowak,⁷ L. L. Pappalardo,¹⁰ R. Perez-Benito,¹³
 A. Petrosyan,²⁶ P. E. Reimer,¹ A. R. Reolon,¹¹ C. Riedl,^{7,15} K. Rith,⁹ G. Rosner,¹⁴ A. Rostomyan,⁶ J. Rubin,¹⁵
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 J. J. M. Steijger,¹⁸ S. Taroian,²⁶ A. Terkulov,¹⁷ R. Truty,¹⁵ A. Trzcinski,^{25,*} M. Tytgat,¹² P. B. van der Nat,¹⁸
 Y. Van Haarlem,¹² C. Van Hulse,^{4,12} D. Veretennikov,^{4,19} V. Vikhrov,¹⁹ I. Vilardi,² C. Vogel,⁹ S. Wang,³
 S. Yaschenko,⁹ B. Zihlmann,⁶ and P. Zupranski²⁵

(The HERMES Collaboration)

re-analysis of longitudinal double-spin asymmetries

- revisited [PRD 71 (2005) 012003] A_1 analysis at HERMES in order to
 - exploit slightly larger data set (less restrictive momentum range)
 - provide A_{\parallel} in addition to A_1

$$A_1^h = \frac{1}{D(1 + \eta\gamma)} A_{\parallel}^h \quad D = \frac{1 - (1 - y)\epsilon}{1 + \epsilon R}$$

R (ratio of longitudinal-to-transverse cross-sec'n) still to be measured!
[only available for inclusive DIS data, e.g., used in g_1 SF measurements]

- correct for D-state admixture (deuteron case) on asymmetry level
- correct better for azimuthal asymmetries coupling to acceptance
- look at multi-dimensional (x , z , $P_{h\perp}$) dependences
- extract twist-3 cosine modulations

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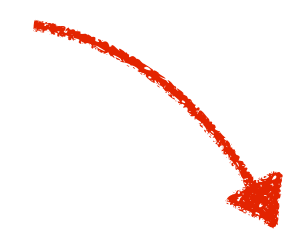
- correct for D-state admixture (deuteron case) on asymmetry level
- correct better for azimuthal asymmetries coupling to acceptance
- look at multi-dimensional (x , z , $P_{h\perp}$) dependences
- extract twist-3 cosine modulations ... consistent with zero

double-spin asymmetry $A_{||}$

$$A_{||}^h \equiv \frac{C_{\phi}^h}{f_D} \left[\frac{L_{\Rightarrow} N_{\Leftarrow}^h - L_{\Leftarrow} N_{\Rightarrow}^h}{L_{P,\Rightarrow} N_{\Leftarrow}^h + L_{P,\Leftarrow} N_{\Rightarrow}^h} \right]_B$$

double-spin asymmetry $A_{||}$

azimuthal
correction


$$A_{||}^h \equiv \frac{C_{\phi}^h}{f_D} \left[\frac{L_{\Rightarrow} N_{\Leftarrow}^h - L_{\Leftarrow} N_{\Rightarrow}^h}{L_{P,\Rightarrow} N_{\Leftarrow}^h + L_{P,\Leftarrow} N_{\Rightarrow}^h} \right]_B$$

double-spin asymmetry $A_{||}$

azimuthal correction

nucleon-in-nucleus depolarization factor
(0.926 for deuteron due to D-state admixture)

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double-spin asymmetry $A_{||}$

azimuthal correction

luminosities

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nucleon-in-nucleus
depolarization factor
(0.926 for deuteron due
to D-state admixture)

double-spin asymmetry $A_{||}$

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luminosities

$$A_{||}^h \equiv \frac{C_{\phi}^h}{f_D} \left[\frac{L_{\Rightarrow} N_{\Leftarrow}^h - L_{\Leftarrow} N_{\Rightarrow}^h}{L_{P,\Rightarrow} N_{\Leftarrow}^h + L_{P,\Leftarrow} N_{\Rightarrow}^h} \right]_B$$

nucleon-in-nucleus depolarization factor (0.926 for deuteron due to D-state admixture)

polarization-weighted luminosities

double-spin asymmetry $A_{||}$

azimuthal correction

luminosities

nucleon-in-nucleus depolarization factor (0.926 for deuteron due to D-state admixture)

polarization-weighted luminosities

unfolded for QED radiation to Born level

$$A_{||}^h \equiv \frac{C_{\phi}^h}{f_D} \left[\frac{L_{\Rightarrow} N_{\Leftarrow}^h - L_{\Leftarrow} N_{\Rightarrow}^h}{L_{P,\Rightarrow} N_{\Leftarrow}^h + L_{P,\Leftarrow} N_{\Rightarrow}^h} \right]_B$$

double-spin asymmetry $A_{||}$

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- dominated by statistical uncertainties

double-spin asymmetry $A_{||}$

$$A_{||}^h \equiv \frac{C_{\phi}^h}{f_D} \left[\frac{L_{\Rightarrow} N_{\Leftarrow}^h - L_{\Leftarrow} N_{\Rightarrow}^h}{L_{P,\Rightarrow} N_{\Leftarrow}^h + L_{P,\Leftarrow} N_{\Rightarrow}^h} \right]_B$$

- dominated by statistical uncertainties
- main systematics arise from
 - polarization measurements [6.6% for hydrogen, 5.7% for deuterium]
 - azimuthal correction [$O(\text{few } \%)$]

azimuthal-asymmetry corrections

measured

"polarized Cahn" effect etc.

$$\tilde{A}_{\parallel}^h(x, Q^2, z, P_{h\perp}) = \frac{\int d\phi \sigma_{\parallel}^h(x, Q^2, z, P_{h\perp}, \phi) \xi(\phi)}{\int d\phi \sigma_{UU}^h(x, Q^2, z, P_{h\perp}, \phi) \xi(\phi)}$$

Boer-Mulders and Cahn effects etc.

azimuthal acceptance

- both numerator and in particular denominator ϕ dependent
 - in theory integrated out
 - in praxis, detector acceptance also ϕ dependent
 - convolution of physics & acceptance leads to bias in normalization of asymmetries

azimuthal-asymmetry corrections

measured

"polarized Cahn" effect etc.

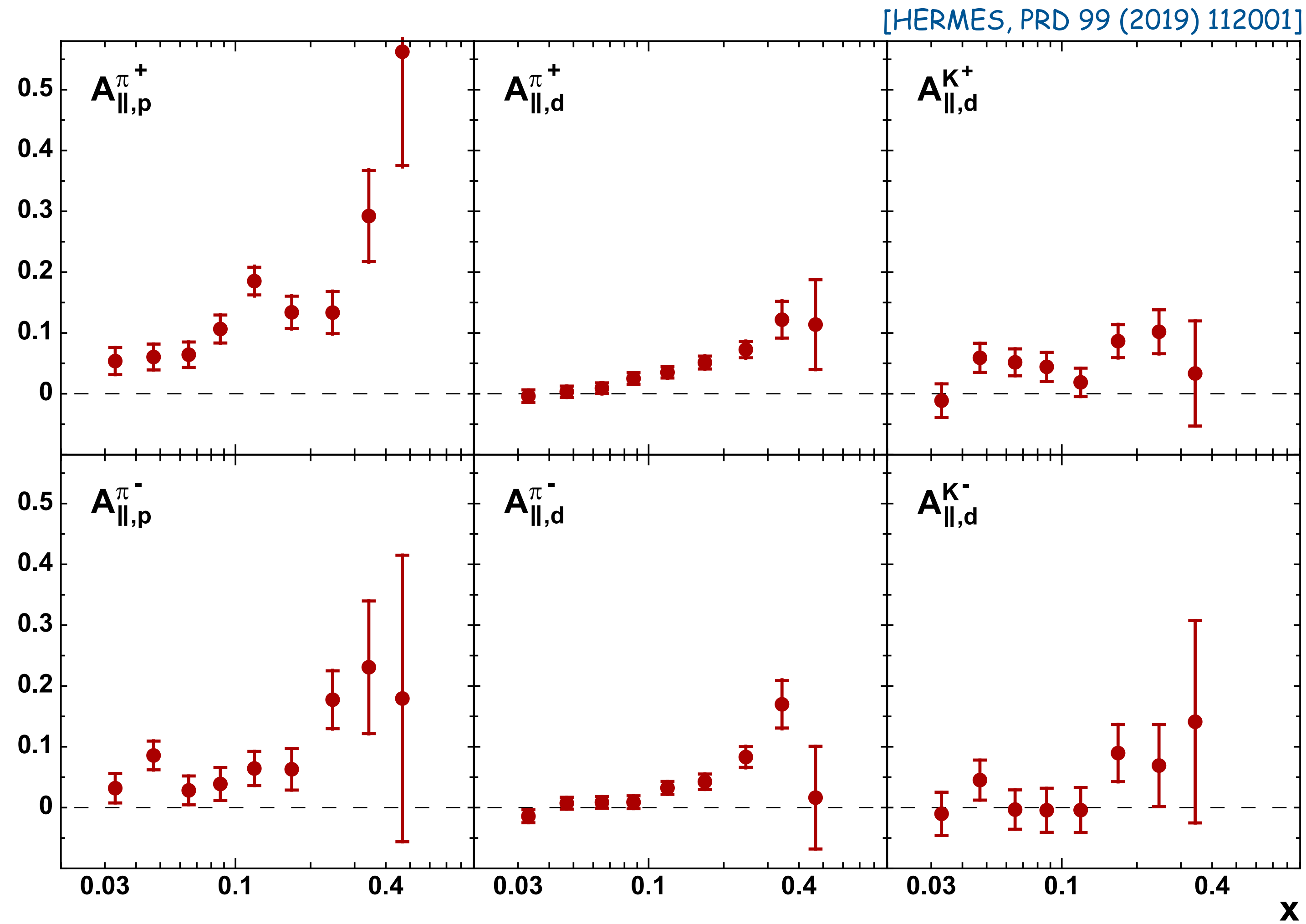
$$\tilde{A}_{\parallel}^h(x, Q^2, z, P_{h\perp}) = \frac{\int d\phi \sigma_{\parallel}^h(x, Q^2, z, P_{h\perp}, \phi) \xi(\phi)}{\int d\phi \sigma_{UU}^h(x, Q^2, z, P_{h\perp}, \phi) \xi(\phi)}$$

Boer-Mulders and Cahn effects etc.

azimuthal acceptance

- both numerator and in particular denominator ϕ dependent
 - in theory integrated out
 - in praxis, detector acceptance also ϕ dependent
 - convolution of physics & acceptance leads to bias in normalization of asymmetries
- implemented data-driven model for azimuthal modulations [PRD 87 (2013) 012010] into MC
 - 👉 extract correction factor & apply to data

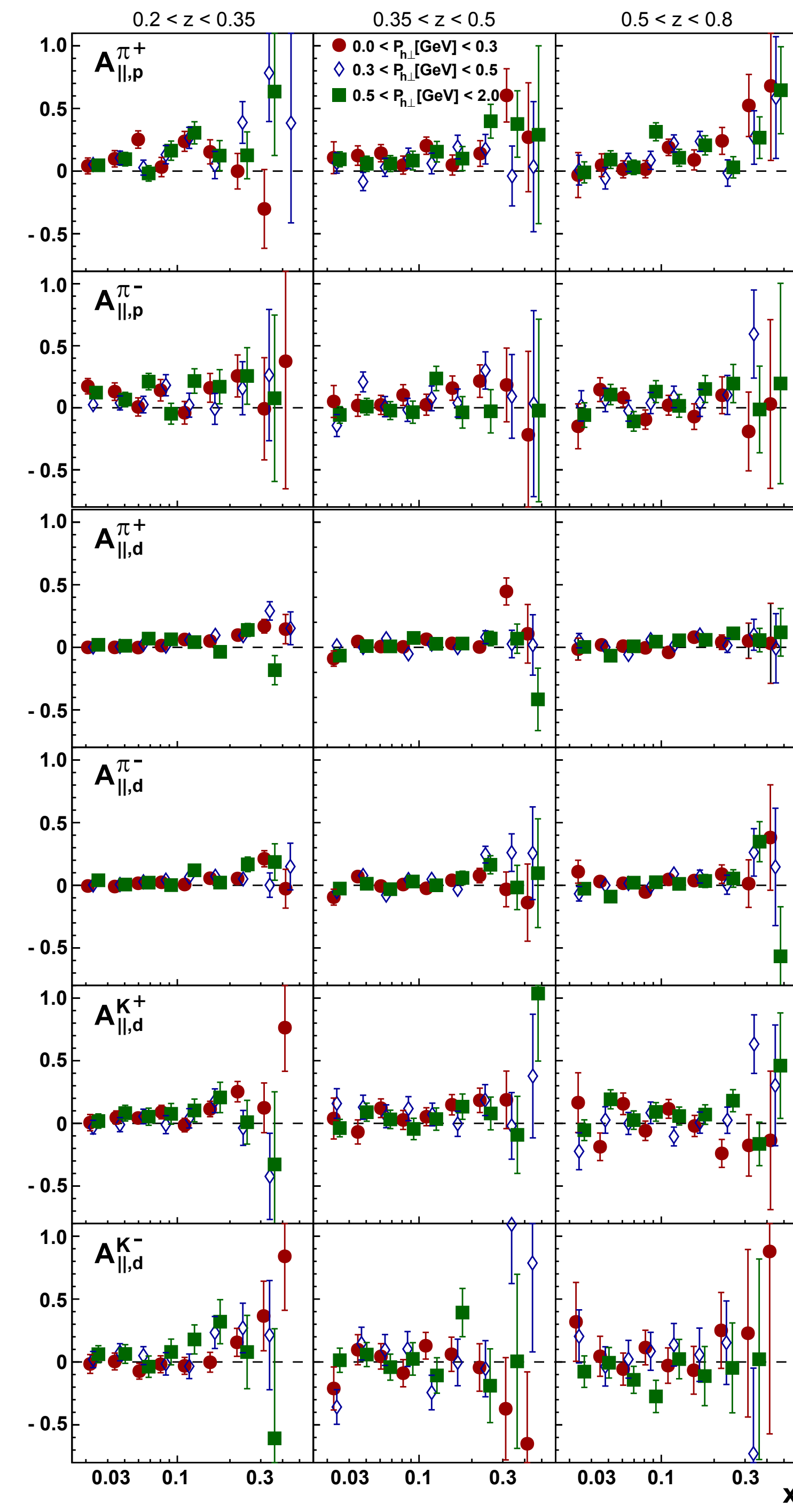
x dependence of $A_{||}$



☑ fully consistent with previous HERMES publication [PRD 71 (2005) 012003]

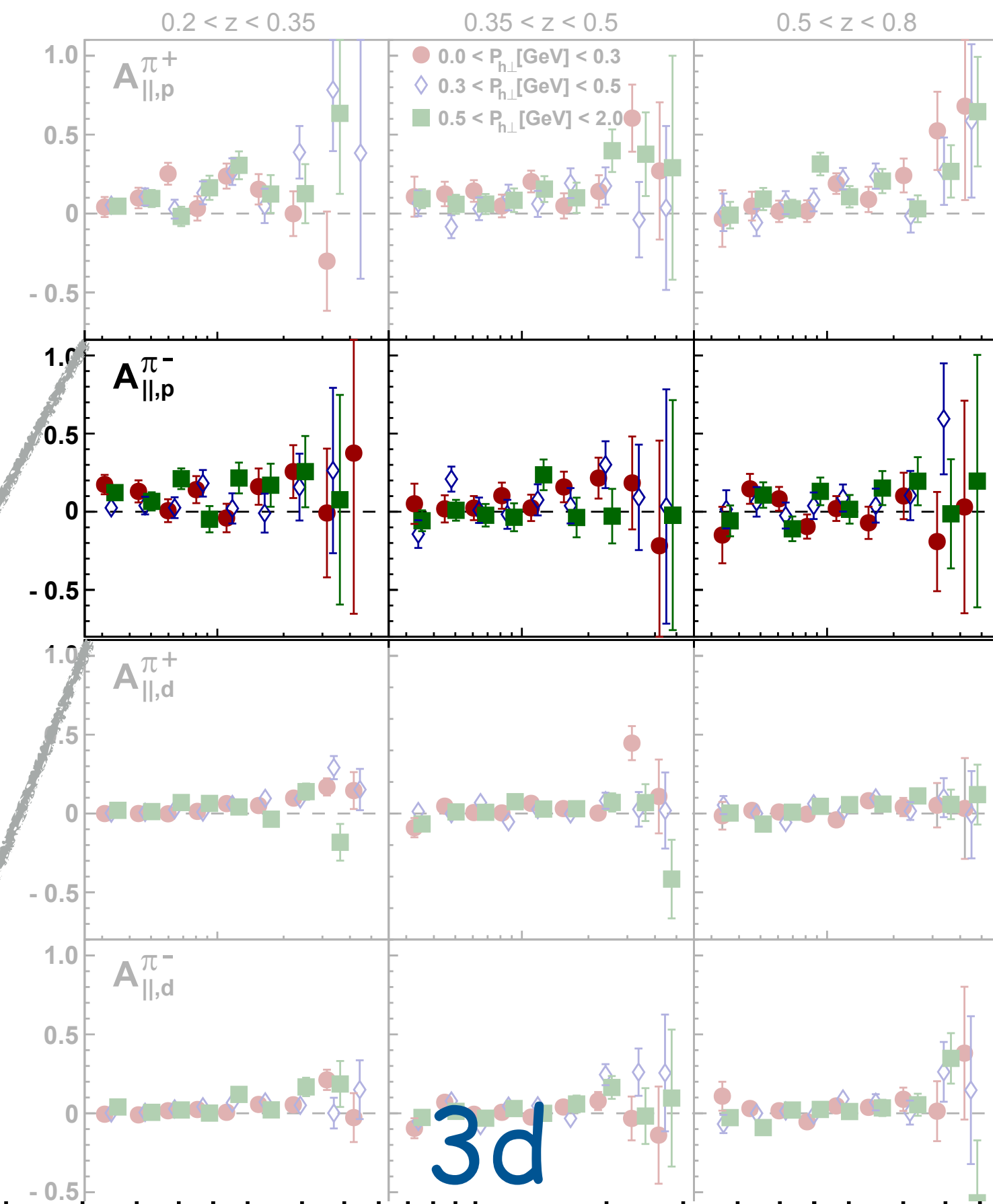
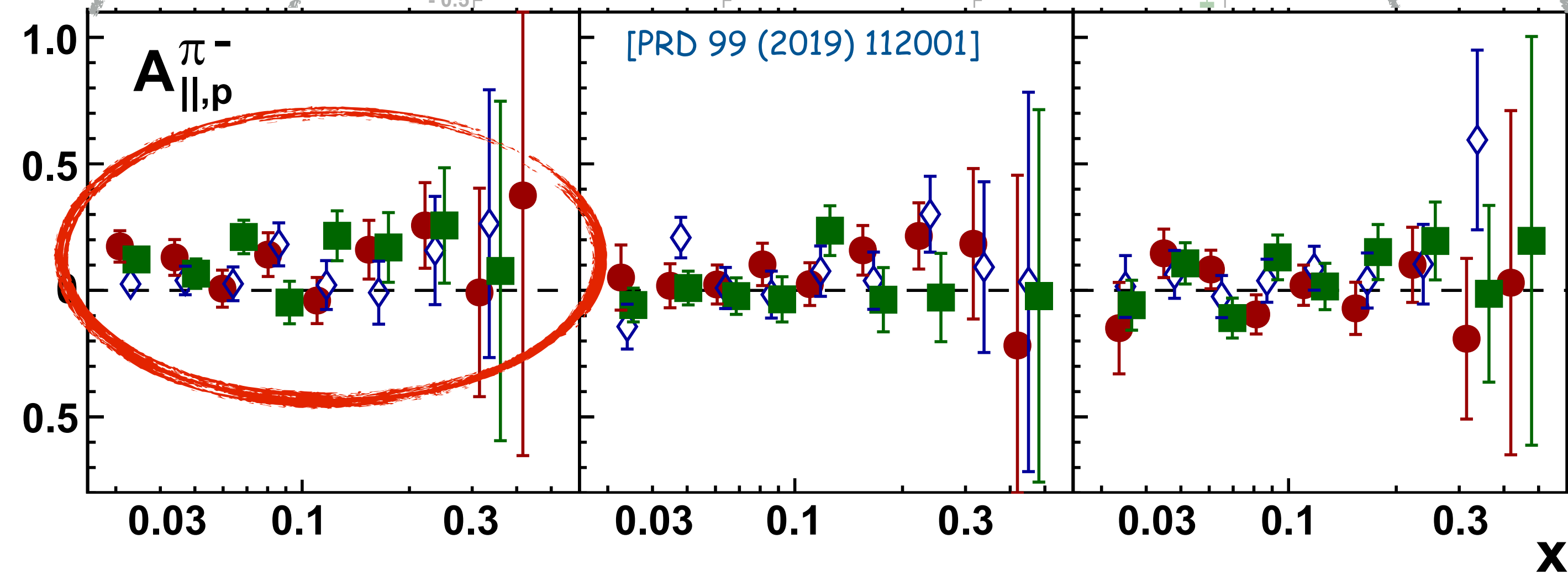
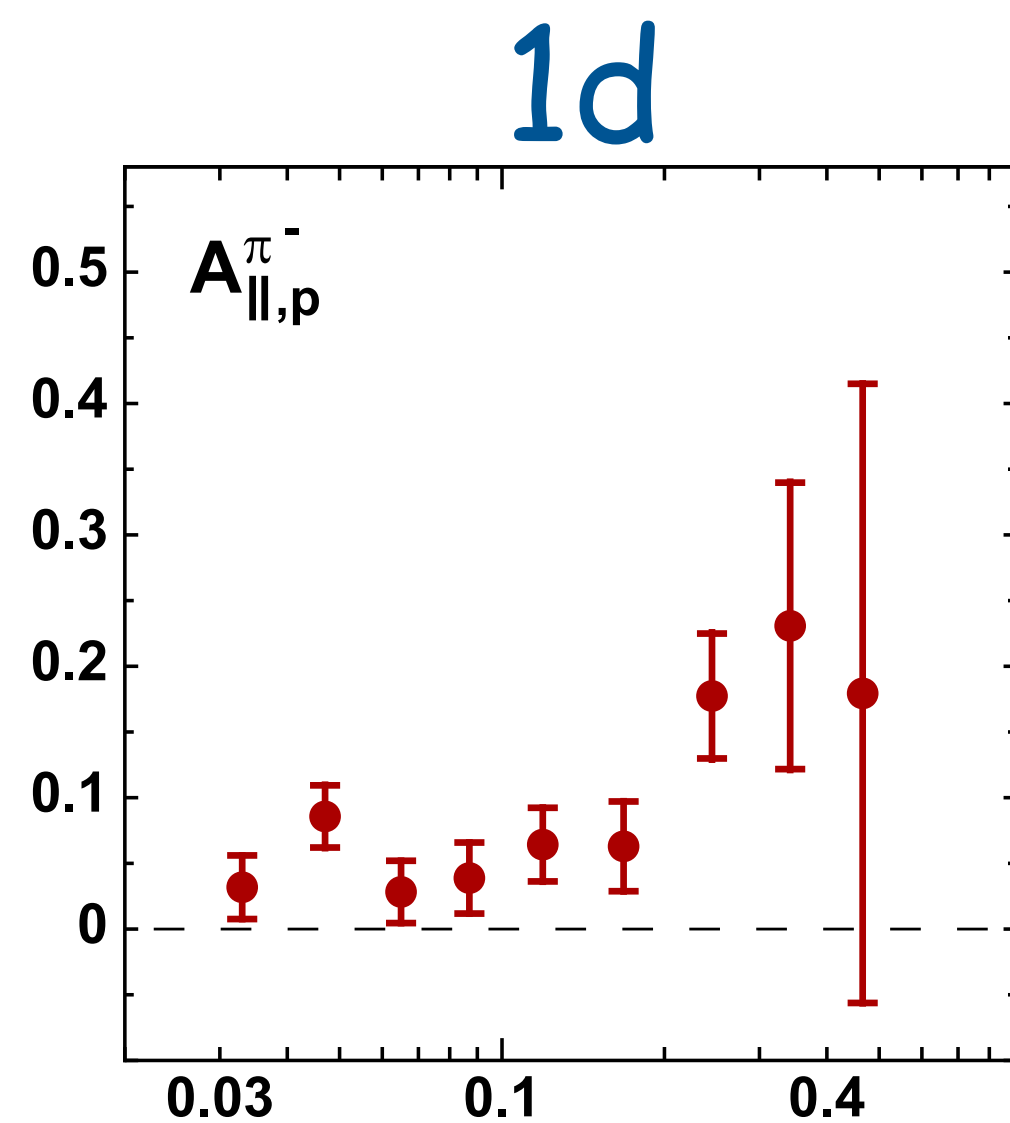
3-dimensional binning

- first-ever 3d binning provides transverse-momentum dependence



3-dimensional binning

- first-ever 3d binning provides transverse-momentum dependence
- but also extra flavor sensitivity, e.g.,
 - π^- asymmetries mainly coming from **low- z** region where disfavored fragmentation large and thus sensitivity to the large positive up-quark polarization



hadron-charge difference asymmetries

$$A_1^{h^+ - h^-}(x) \equiv \frac{\left(\sigma_{1/2}^{h^+} - \sigma_{1/2}^{h^-}\right) - \left(\sigma_{3/2}^{h^+} - \sigma_{3/2}^{h^-}\right)}{\left(\sigma_{1/2}^{h^+} - \sigma_{1/2}^{h^-}\right) + \left(\sigma_{3/2}^{h^+} - \sigma_{3/2}^{h^-}\right)}$$

hadron-charge difference asymmetries

$$A_1^{h^+ - h^-}(x) \equiv \frac{\left(\sigma_{1/2}^{h^+} - \sigma_{1/2}^{h^-}\right) - \left(\sigma_{3/2}^{h^+} - \sigma_{3/2}^{h^-}\right)}{\left(\sigma_{1/2}^{h^+} - \sigma_{1/2}^{h^-}\right) + \left(\sigma_{3/2}^{h^+} - \sigma_{3/2}^{h^-}\right)}$$

- at leading-order and leading-twist, assuming charge conjugation symmetry for fragmentation functions:

$$A_{1,d}^{h^+ - h^-} \stackrel{\text{LO} = \text{LT}}{=} \frac{g_1^{u_v} + g_1^{d_v}}{f_1^{u_v} + f_1^{d_v}}$$

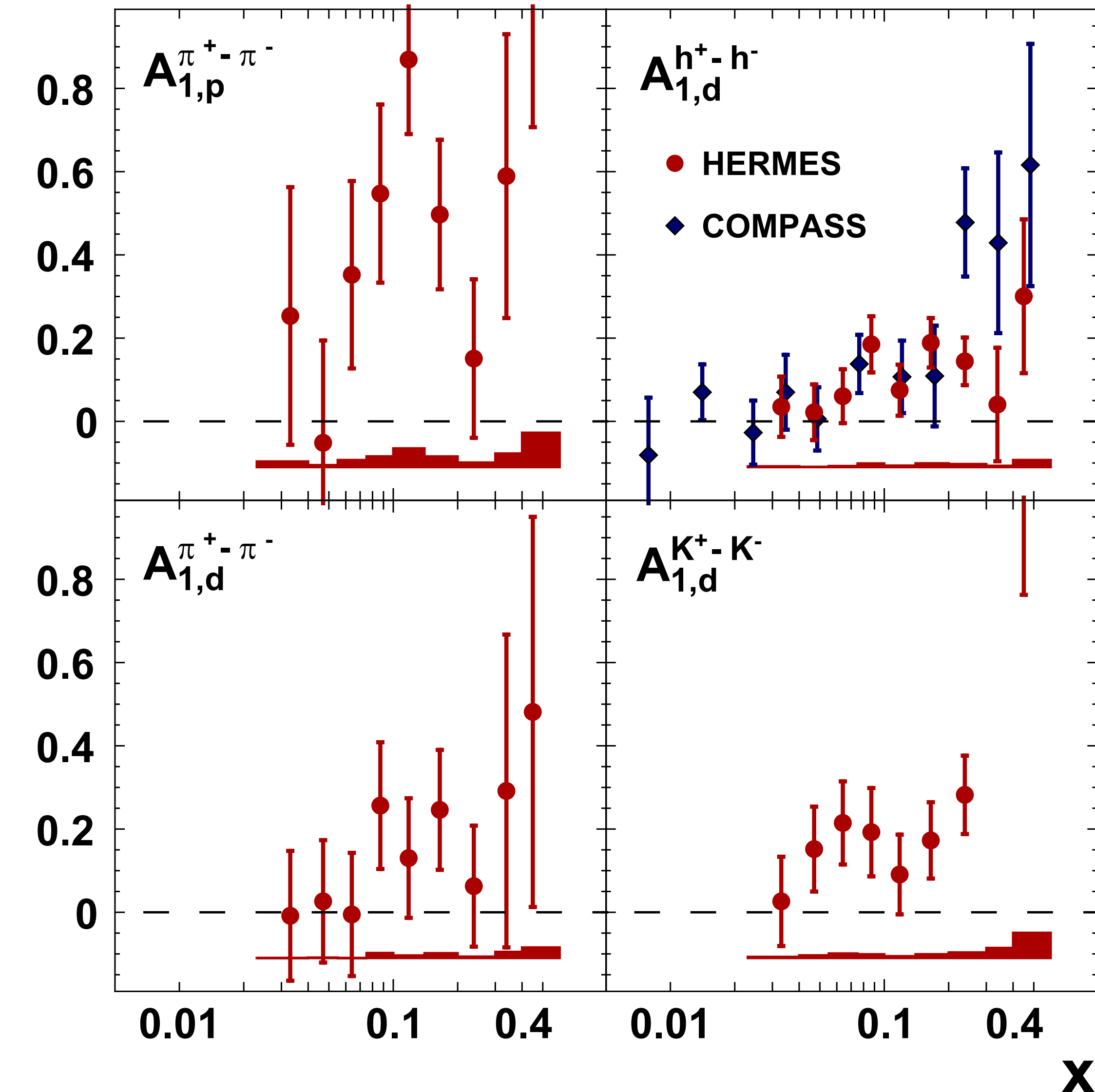
- assuming also isospin symmetry in fragmentation:

$$A_{1,p}^{h^+ - h^-} \stackrel{\text{LO} = \text{LT}}{=} \frac{4g_1^{u_v} - g_1^{d_v}}{4f_1^{u_v} - f_1^{d_v}}$$

- can be used to extract valence helicity distributions

hadron-charge difference asymmetries

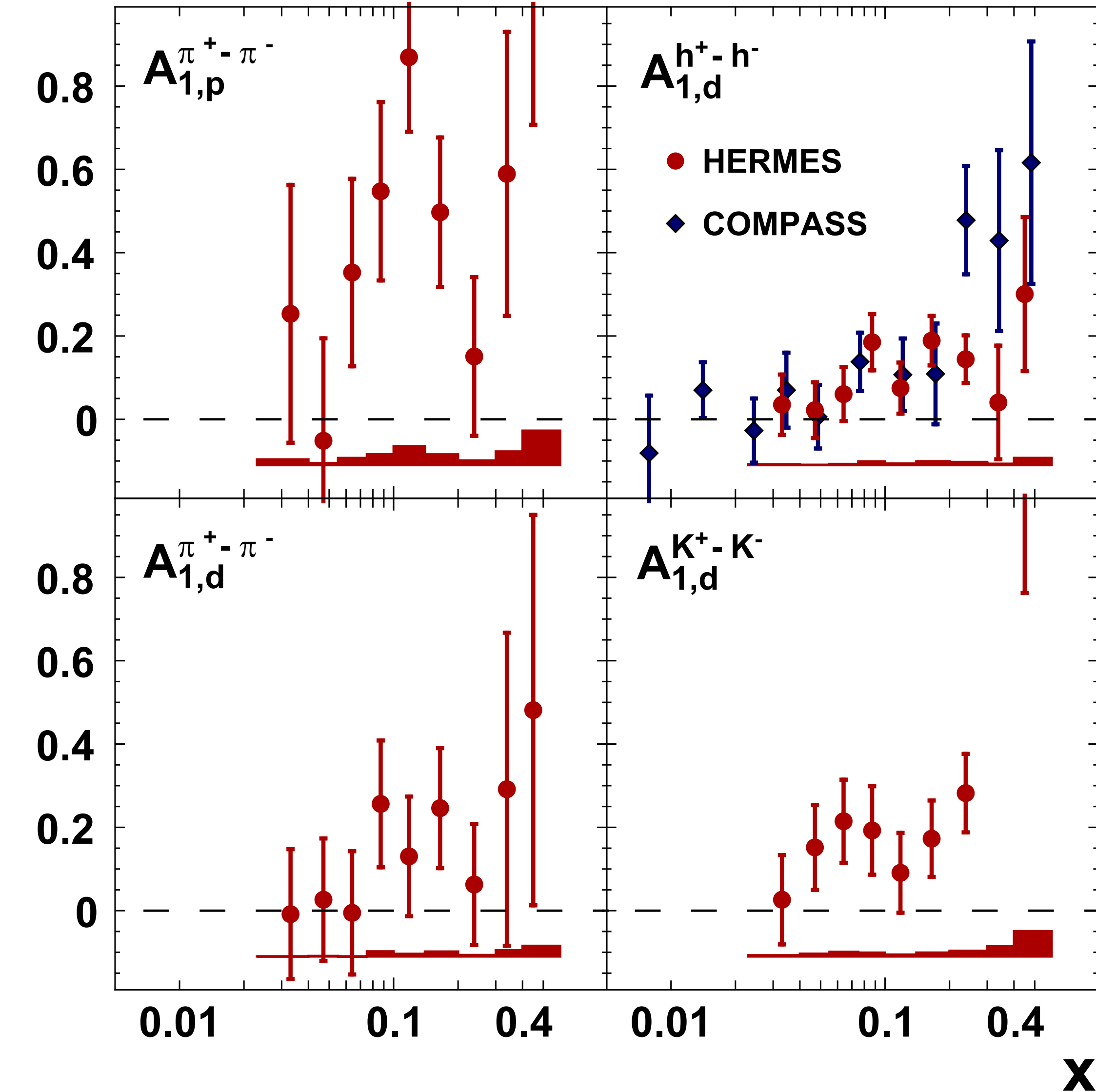
[arXiv:1810.07054]



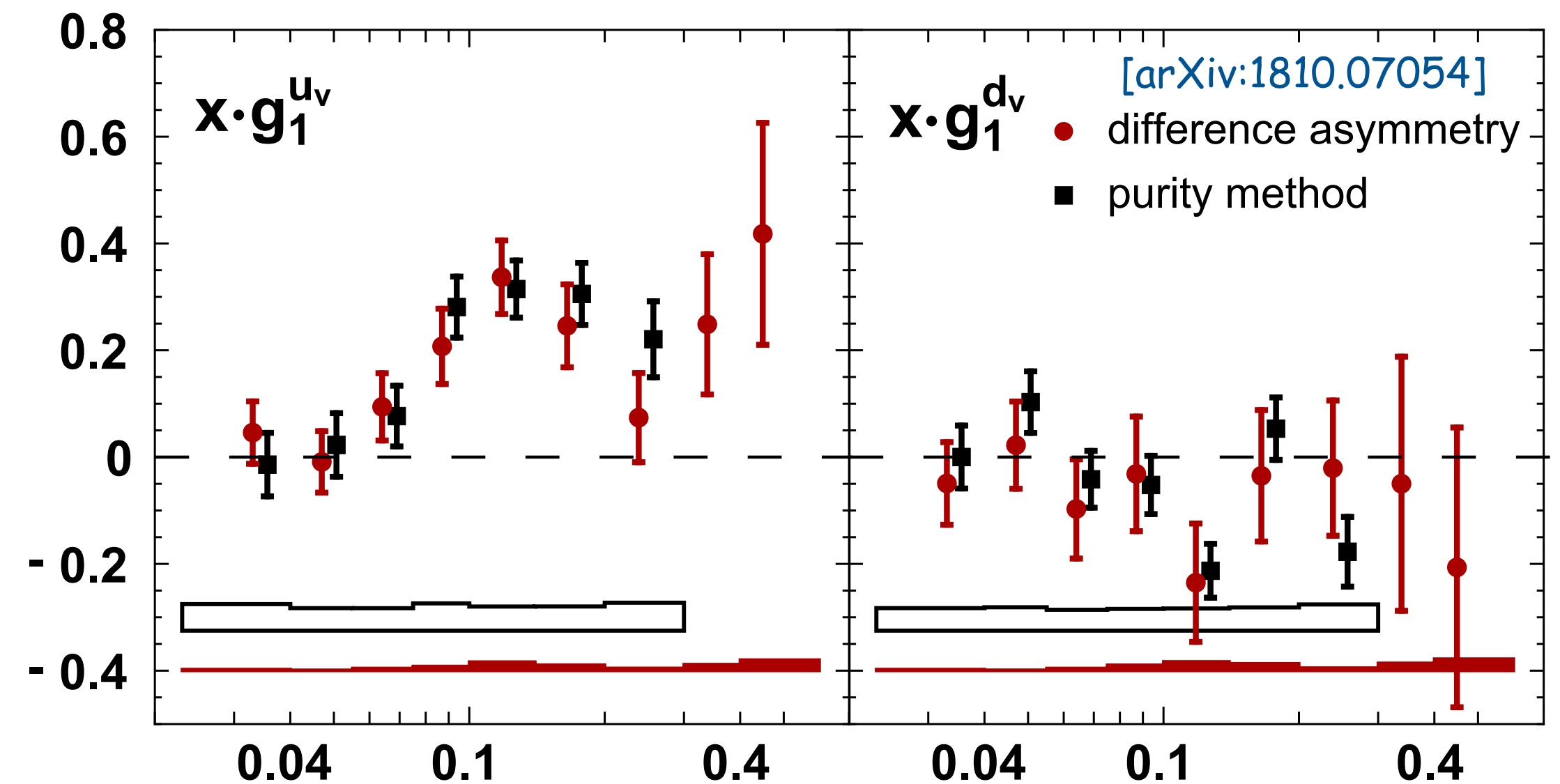
- no significant hadron-type dependence for deuterons
- deuteron results (unidentified hadrons) consistent with COMPASS

hadron-charge difference asymmetries

[arXiv:1810.07054]



- no significant hadron-type dependence for deuterons
- deuteron results (unidentified hadrons) consistent with COMPASS
- valence distributions consistent with JETSET-based extraction:



Azimuthal single- and double-spin asymmetries in semi-inclusive deep-inelastic lepton scattering by transversely polarized protons



The HERMES Collaboration

A. Airapetian,^{13,16} N. Akopov,²⁶ Z. Akopov,⁶ E.C. Aschenauer,⁷ W. Augustyniak,²⁵ R. Avakian,^{26,a} A. Bacchetta,²¹ S. Belostotski,^{19,a} V. Bryzgalov,²⁰ G.P. Capitani,¹¹ E. Cisbani,²² G. Ciullo,¹⁰ M. Contalbrigo,¹⁰ W. Deconinck,⁶ R. De Leo,² E. De Sanctis,¹¹ M. Diefenthaler,⁹ P. Di Nezza,¹¹ M. Düren,¹³ G. Elbakian,²⁶ F. Ellinghaus,⁵ A. Fantoni,¹¹ L. Felawka,²³ G. Gavrilov,^{6,19,23} V. Gharibyan,²⁶ D. Hasch,¹¹ Y. Holler,⁶ A. Ivanilov,²⁰ H.E. Jackson,^{1,a} S. Joosten,¹² R. Kaiser,¹⁴ G. Karyan,^{6,26} E. Kinney,⁵ A. Kisselev,¹⁹ V. Kozlov,¹⁷ P. Kravchenko,^{9,19} L. Lagamba,² L. Lapikás,¹⁸ I. Lehmann,¹⁴ P. Lenisa,¹⁰ W. Lorenzon,¹⁶ S.I. Manaenkov,¹⁹ B. Marianski,^{25,a} H. Marukyan,²⁶ Y. Miyachi,²⁴ A. Movsisyan,^{10,26} V. Muccifora,¹¹ Y. Naryshkin,¹⁹ A. Nass,⁹ G. Nazaryan,²⁶ W.-D. Nowak,⁷ L.L. Pappalardo,¹⁰ P.E. Reimer,¹ A.R. Reolon,¹¹ C. Riedl,^{7,15} K. Rith,⁹ G. Rosner,¹⁴ A. Rostomyan,⁶ J. Rubin,¹⁵ D. Ryckbosch,¹² A. Schäfer,²¹ G. Schnell,^{3,4,12} B. Seitz,¹⁴ T.-A. Shibata,²⁴ V. Shutov,⁸ M. Statera,¹⁰ A. Terkulov,¹⁷ M. Tytgat,¹² Y. Van Haarlem,¹² C. Van Hulse,¹² D. Veretennikov,^{3,19} I. Vilardi,² S. Yaschenko,⁹ D. Zeiler,⁹ B. Zihlmann⁶ and P. Zupranski²⁵

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⁶DESY, 22603 Hamburg, Germany

⁷DESY, 15738 Zeuthen, Germany

⁸Joint Institute for Nuclear Research, 141980 Dubna, Russia

^aDeceased.

Azimuthal modulation		Significant non-vanishing Fourier amplitude					
		π^{+}	π^{-}	K^{+}	K^{-}	p	π^0 \bar{p}
$\sin(\phi + \phi_S)$	[Collins]	✓	✓	✓		✓	
$\sin(\phi - \phi_S)$	[Sivers]	✓		✓	✓	✓	(✓) ✓
$\sin(3\phi - \phi_S)$	[Pretzelosity]						
$\sin(\phi_S)$		(✓)	✓		✓		
$\sin(2\phi - \phi_S)$							(✓)
$\sin(2\phi + \phi_S)$				✓			
$\cos(\phi - \phi_S)$	[Worm-gear]	✓	(✓)	(✓)			
$\cos(\phi + \phi_S)$							
$\cos(\phi_S)$				✓			
$\cos(2\phi - \phi_S)$							

Azimuthal single- and double-spin asymmetries in semi-inclusive deep-inelastic lepton scattering by transversely polarized protons



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$\sin(\phi - \phi_S)$	[Sivers]	✓		✓	✓	✓	(✓)	✓
$\sin(3\phi - \phi_S)$	[Pretzelosity]							
$\sin(\phi_S)$		(✓)	✓		✓			
$\sin(2\phi - \phi_S)$								(✓)
$\sin(2\phi + \phi_S)$				✓				
$\cos(\phi - \phi_S)$	[Worm-gear]	✓	(✓)	(✓)				
$\cos(\phi + \phi_S)$								
$\cos(\phi_S)$				✓				
$\cos(2\phi - \phi_S)$								

90%

95%

Azimuthal single- and double-spin asymmetries in semi-inclusive deep-inelastic lepton scattering by transversely polarized protons



The HERMES Collaboration

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⁶DESY, 22603 Hamburg, Germany

⁷DESY, 15738 Zeuthen, Germany

⁸Joint Institute for Nuclear Research, 141980 Dubna, Russia

^aDeceased.

3d

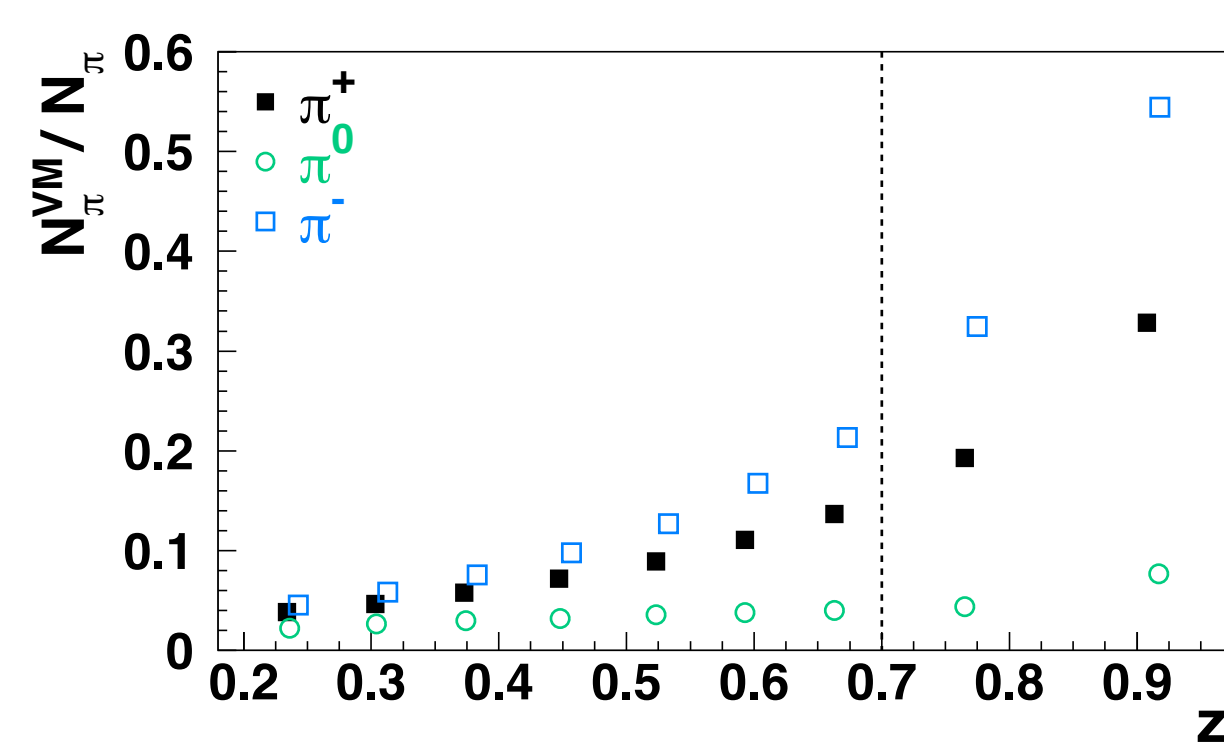
1d

Azimuthal modulation		Significant non-vanishing Fourier amplitude						
		π^+	π^-	K^+	K^-	p	π^0	\bar{p}
$\sin(\phi + \phi_S)$	[Collins]	✓	✓	✓		✓		
$\sin(\phi - \phi_S)$	[Sivers]	✓		✓	✓	✓	(✓)	✓
$\sin(3\phi - \phi_S)$	[Pretzelosity]							
$\sin(\phi_S)$		(✓)	✓		✓			
$\sin(2\phi - \phi_S)$								(✓)
$\sin(2\phi + \phi_S)$				✓				
$\cos(\phi - \phi_S)$	[Worm-gear]	✓	(✓)	(✓)				
$\cos(\phi + \phi_S)$								
$\cos(\phi_S)$				✓				
$\cos(2\phi - \phi_S)$								

90%

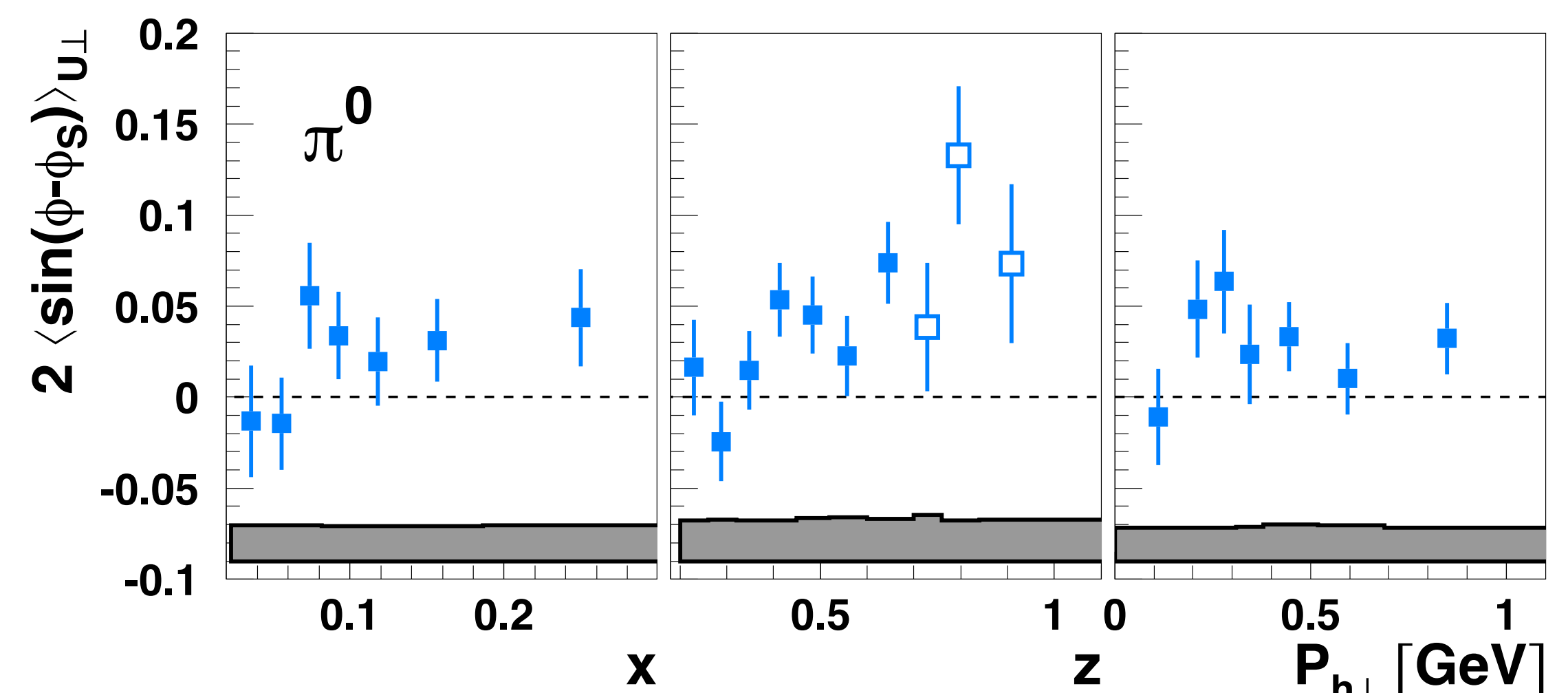
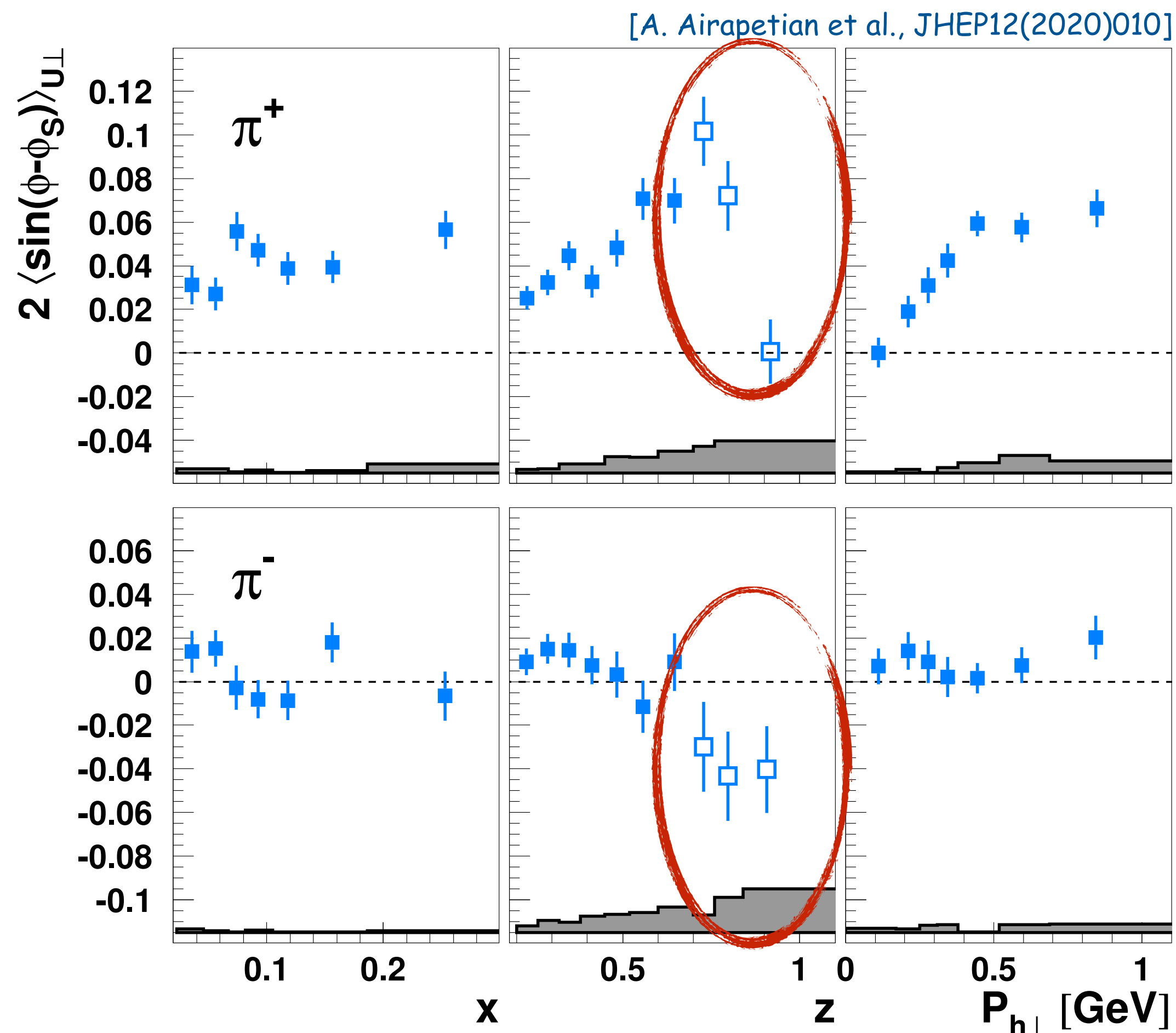
95%

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp



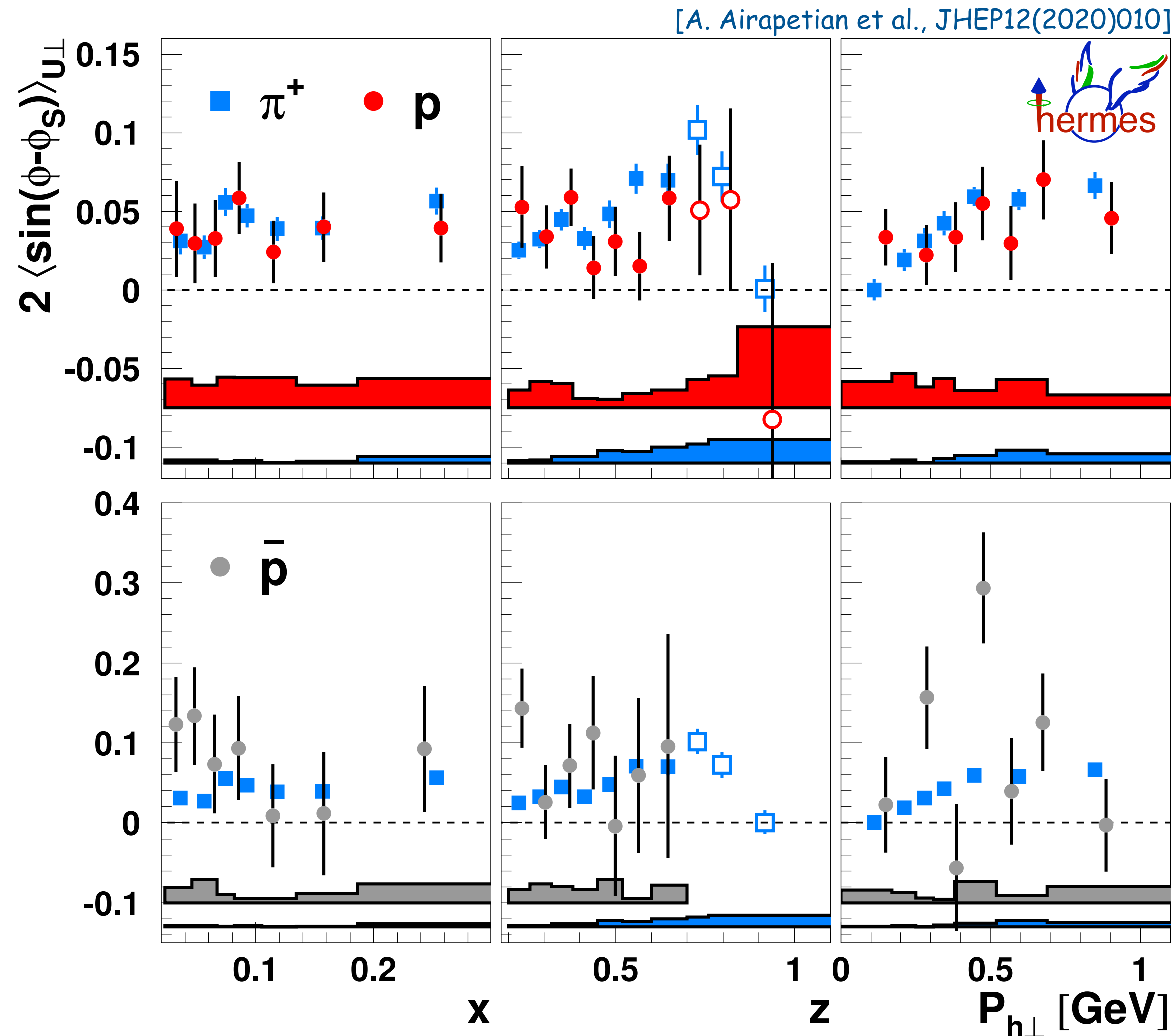
Sivers amplitudes for pions

- high- z data probes region of increased flavor sensitivity to struck quark (but also where contributions from exclusive vector-meson production becomes significant)
- only last z bin shows indication of sizable ρ^0 contribution (decaying into charged pions)



Sivers amplitudes pions vs. (anti)protons

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp



similar-magnitude asymmetries for (anti)**protons** and
pions

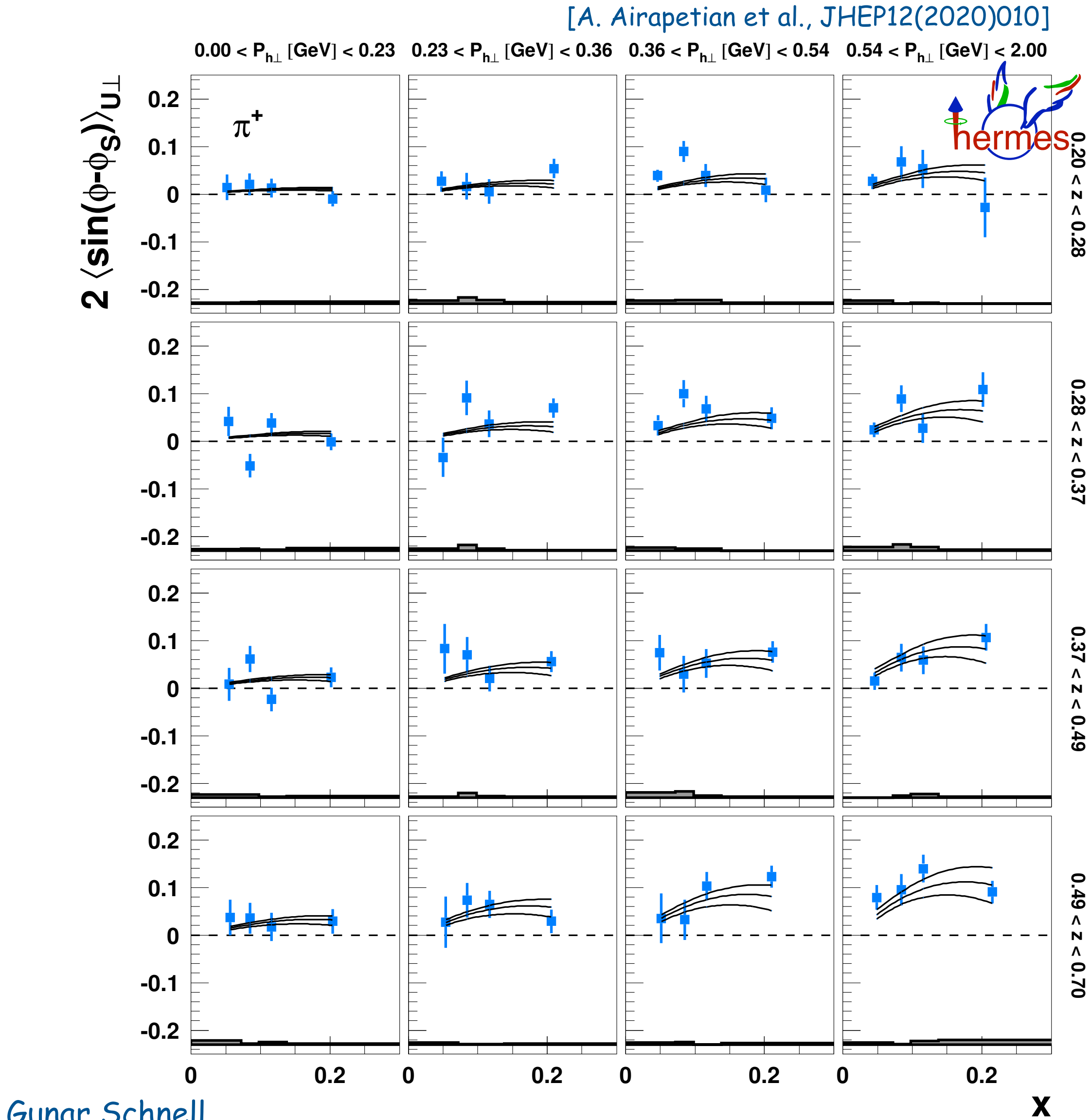
→ consequence of u-quark dominance in both cases?

$$2\langle \sin(\phi - \phi_S) \rangle_{\text{UT}} = - \frac{\sum_q e_q^2 f_{1T}^{\perp,q}(x, p_T^2) \otimes_{\mathcal{W}} D_1^q(z, k_T^2)}{\sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^q(z, k_T^2)}$$

$$\approx -\mathcal{C} \frac{f_{1T}^{\perp,u}(x, p_T^2)}{f_1^u(x, p_T^2)}$$

Sivers amplitudes multi-dimensional analysis

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

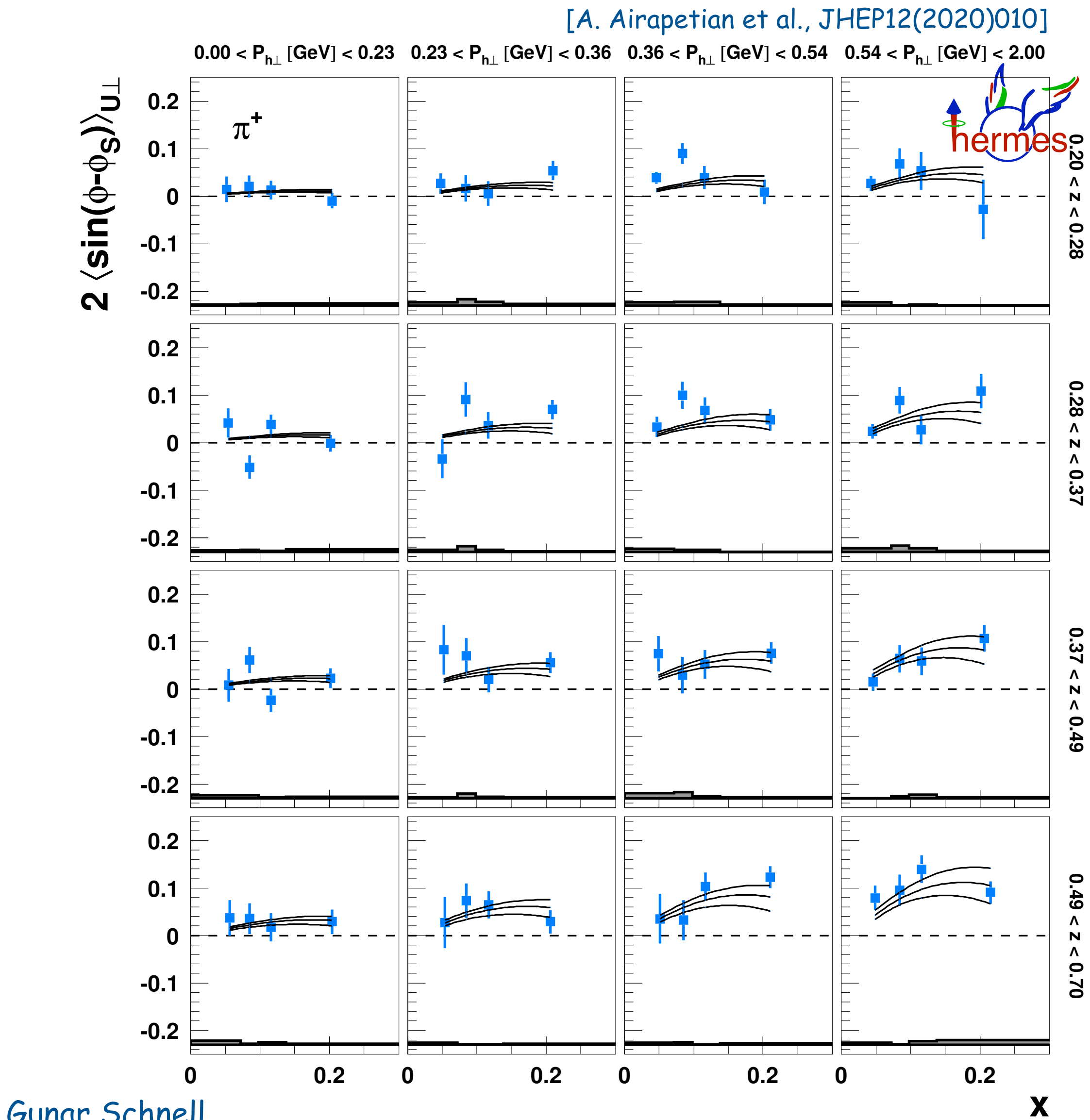


- 3d analysis: 4x4x4 bins in (x,z, P_{h⊥})

Sivers amplitudes

multi-dimensional analysis

	U	L	T
U	f_1		h_1^\perp
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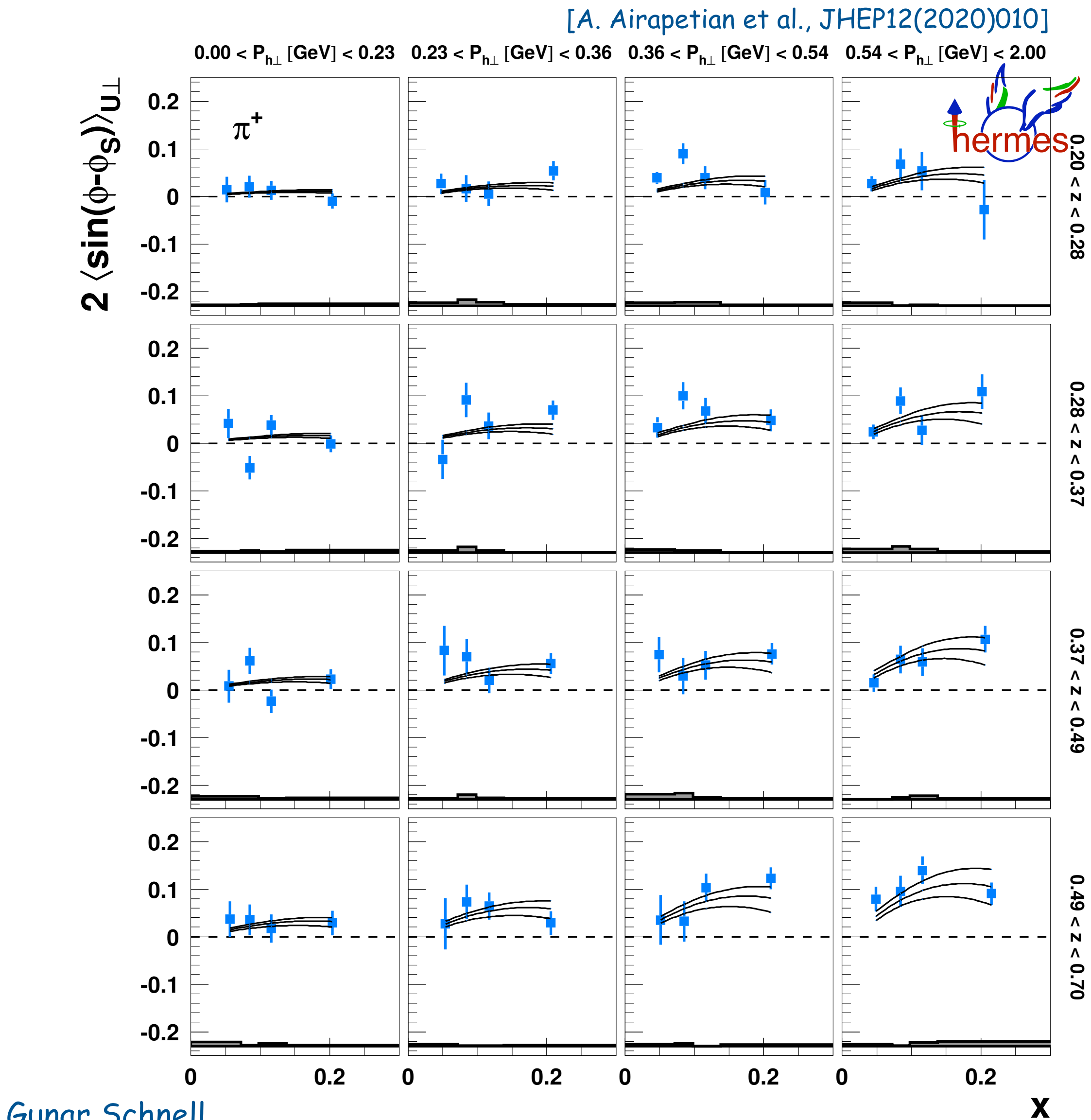


- 3d analysis: 4x4x4 bins in ($x, z, P_{h\perp}$)
- reduced systematics
- disentangle correlations
- isolate phase-space region with large signal strength

Sivers amplitudes

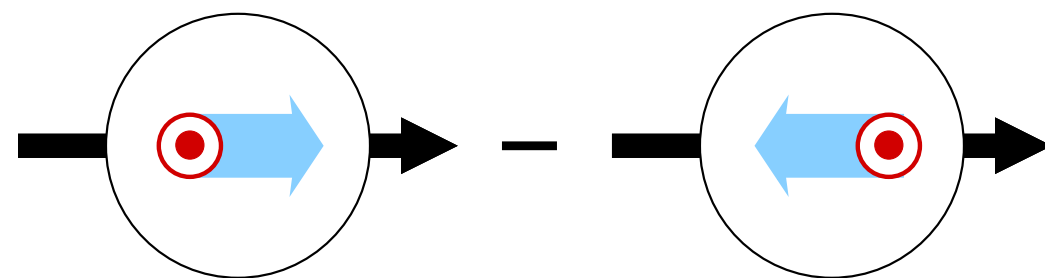
multi-dimensional analysis

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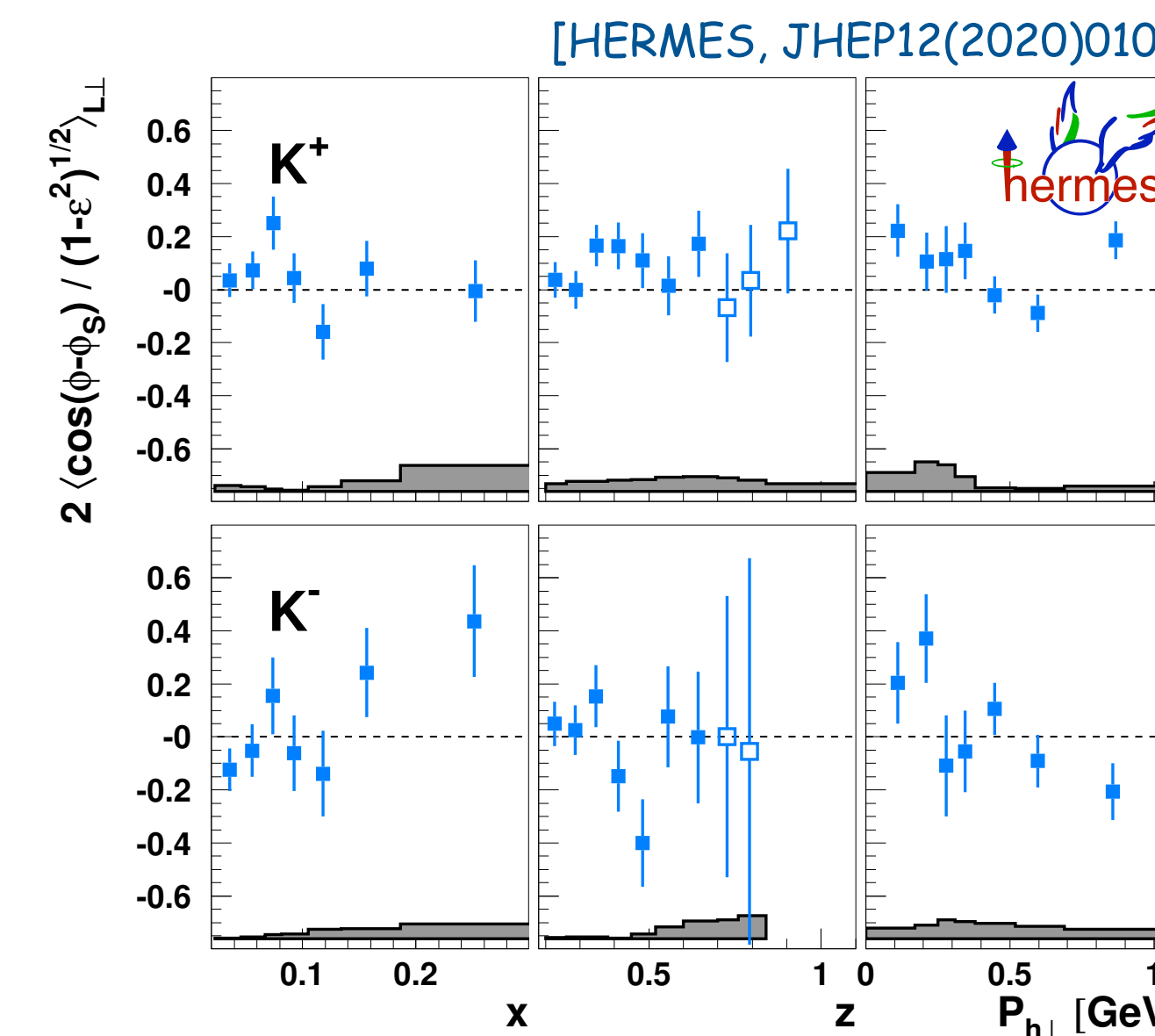
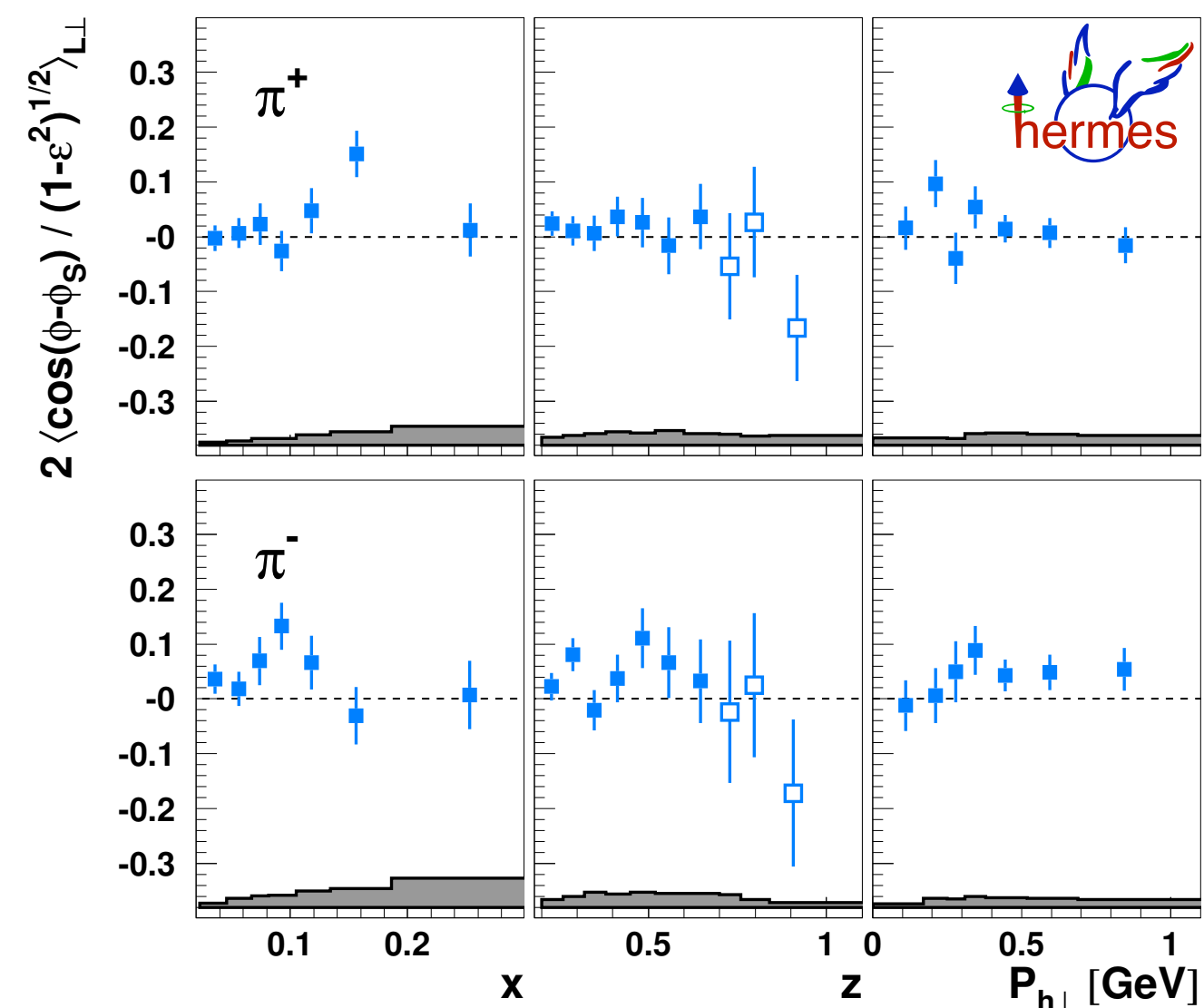
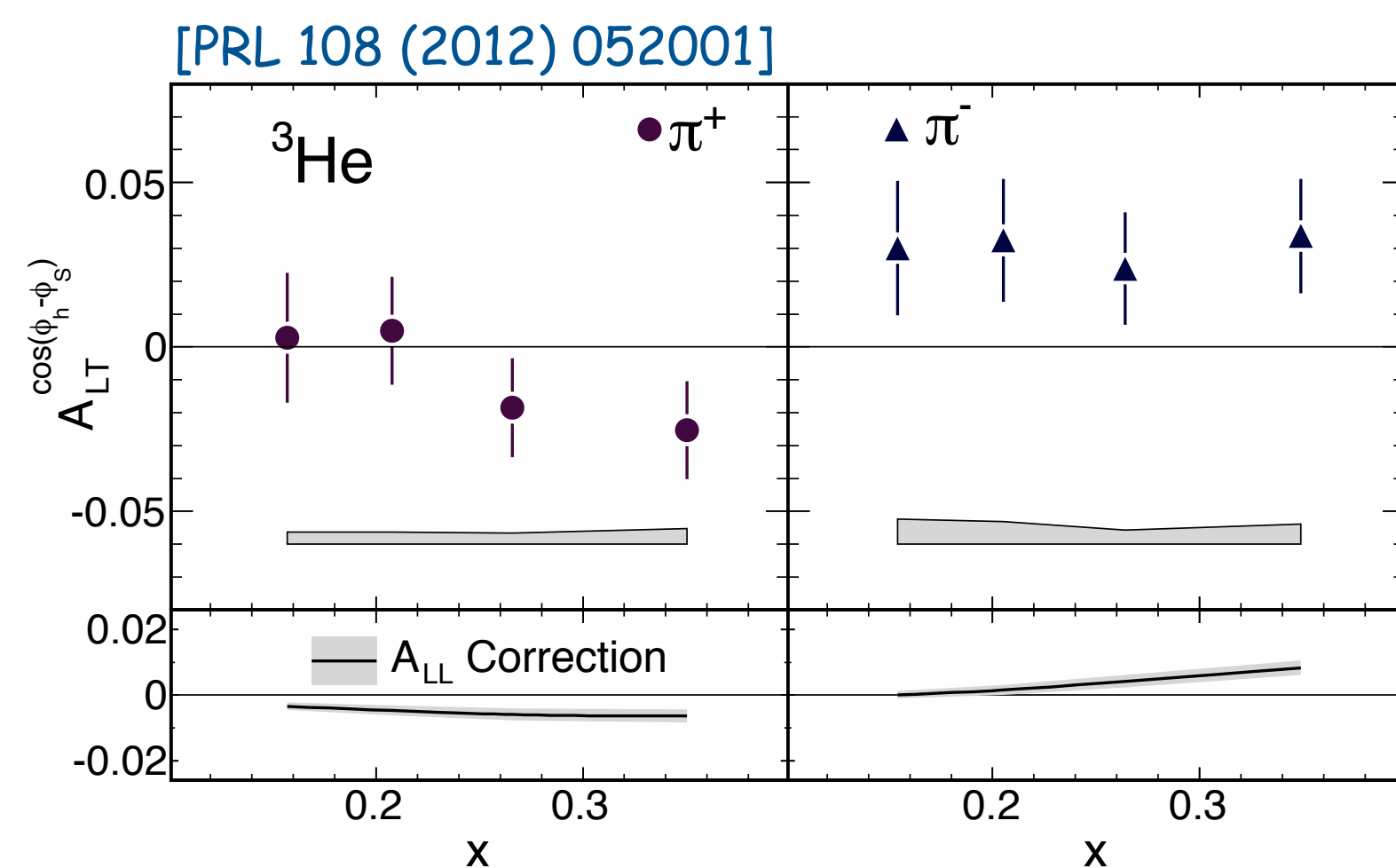
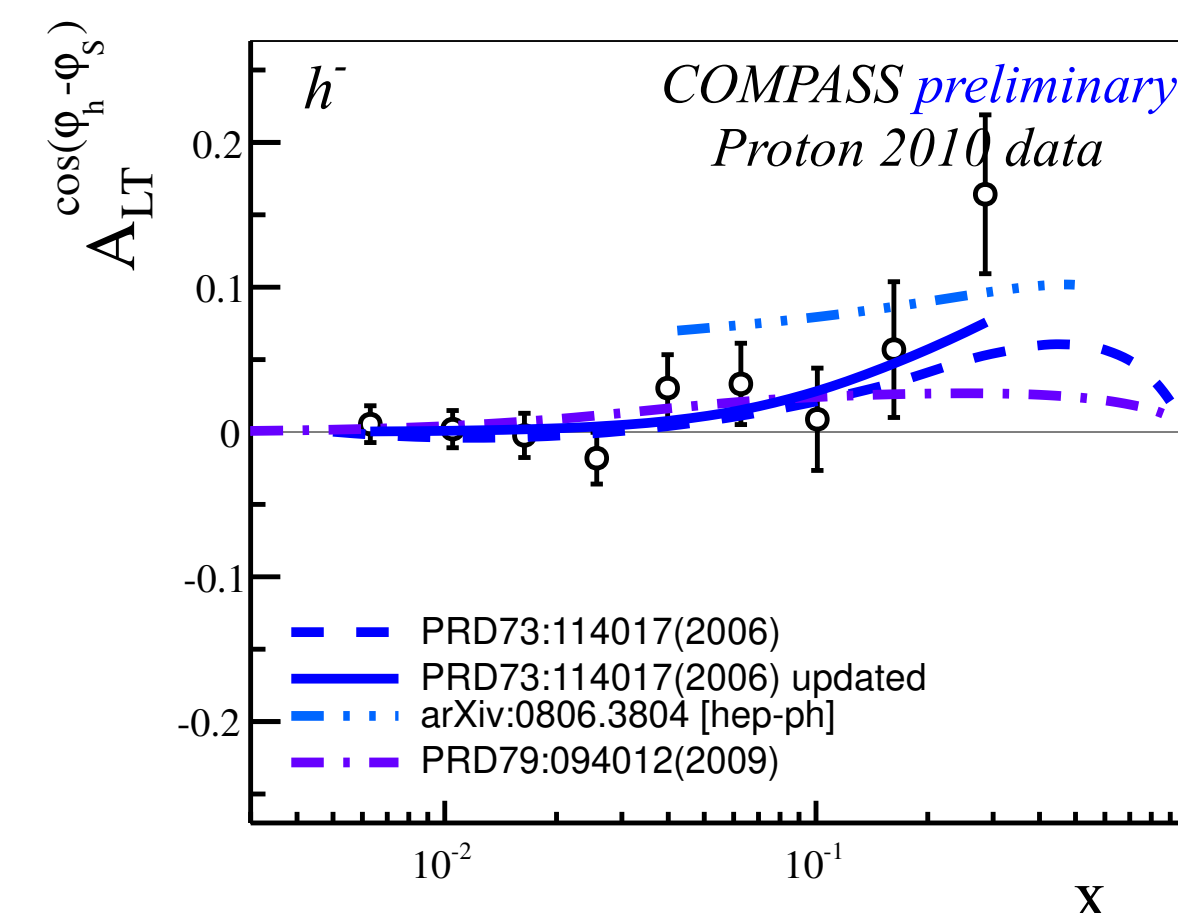
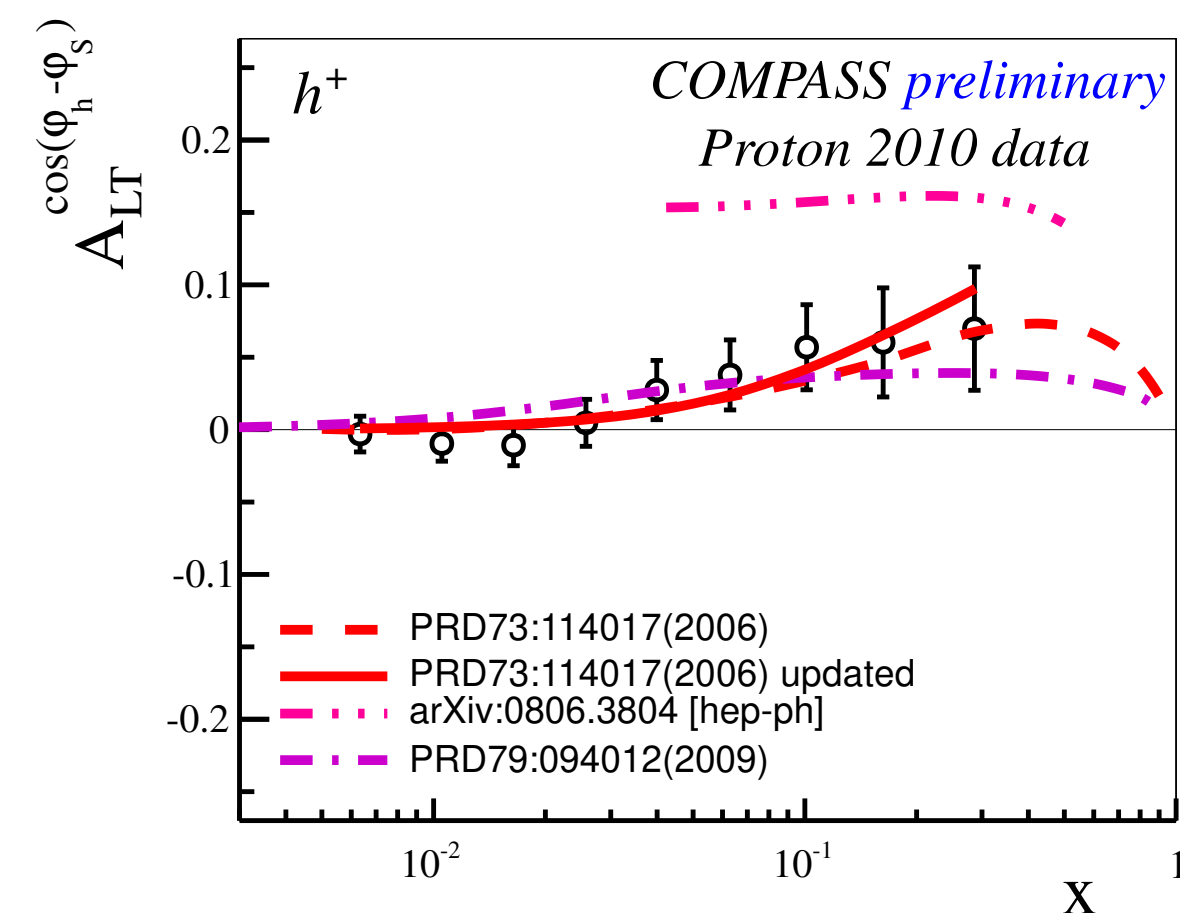
- 3d analysis: 4x4x4 bins in ($x, z, P_{h\perp}$)
- reduced systematics
- disentangle correlations
- isolate phase-space region with large signal strength
- allows more detailed comparison with calculations
- accompanied by kinematic distribution to guide phenomenology

	U	L	T
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L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp



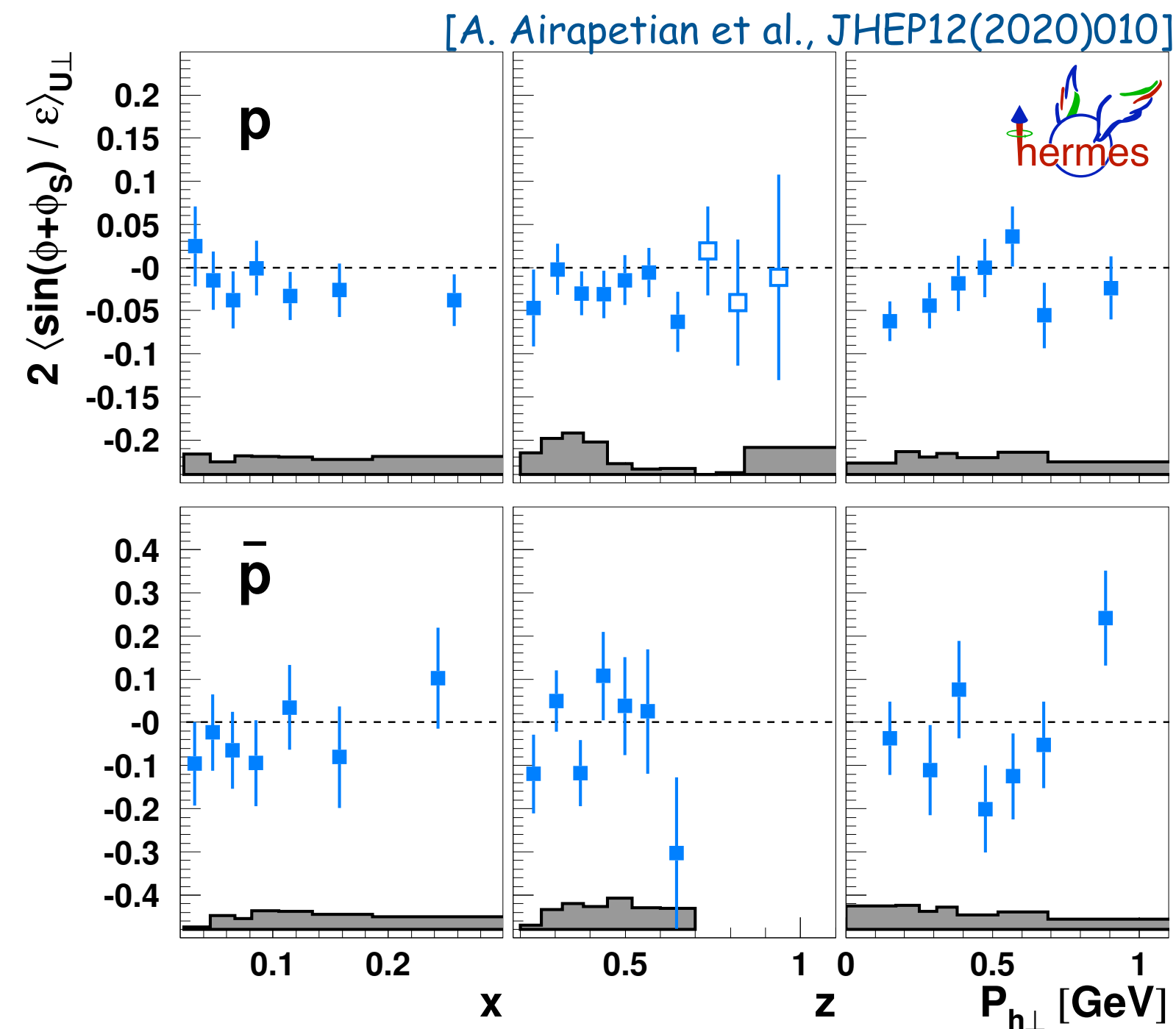
worm-gear II

- quark-helicity asymmetry in transversely polarized nucleon
- evidences from
 - ^3He target at JLab
 - H target at COMPASS & HERMES



new HERMES results on Collins amplitudes

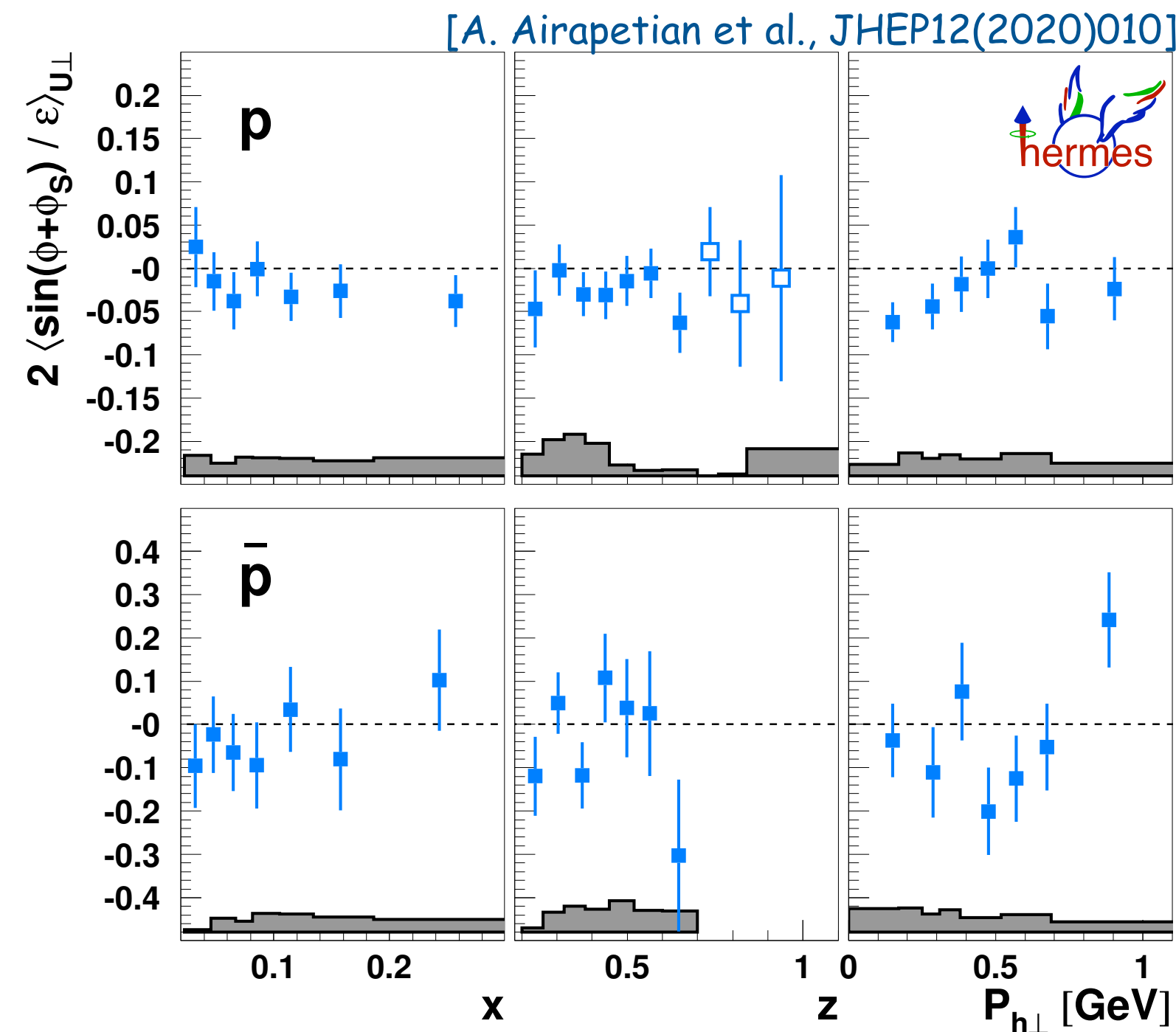
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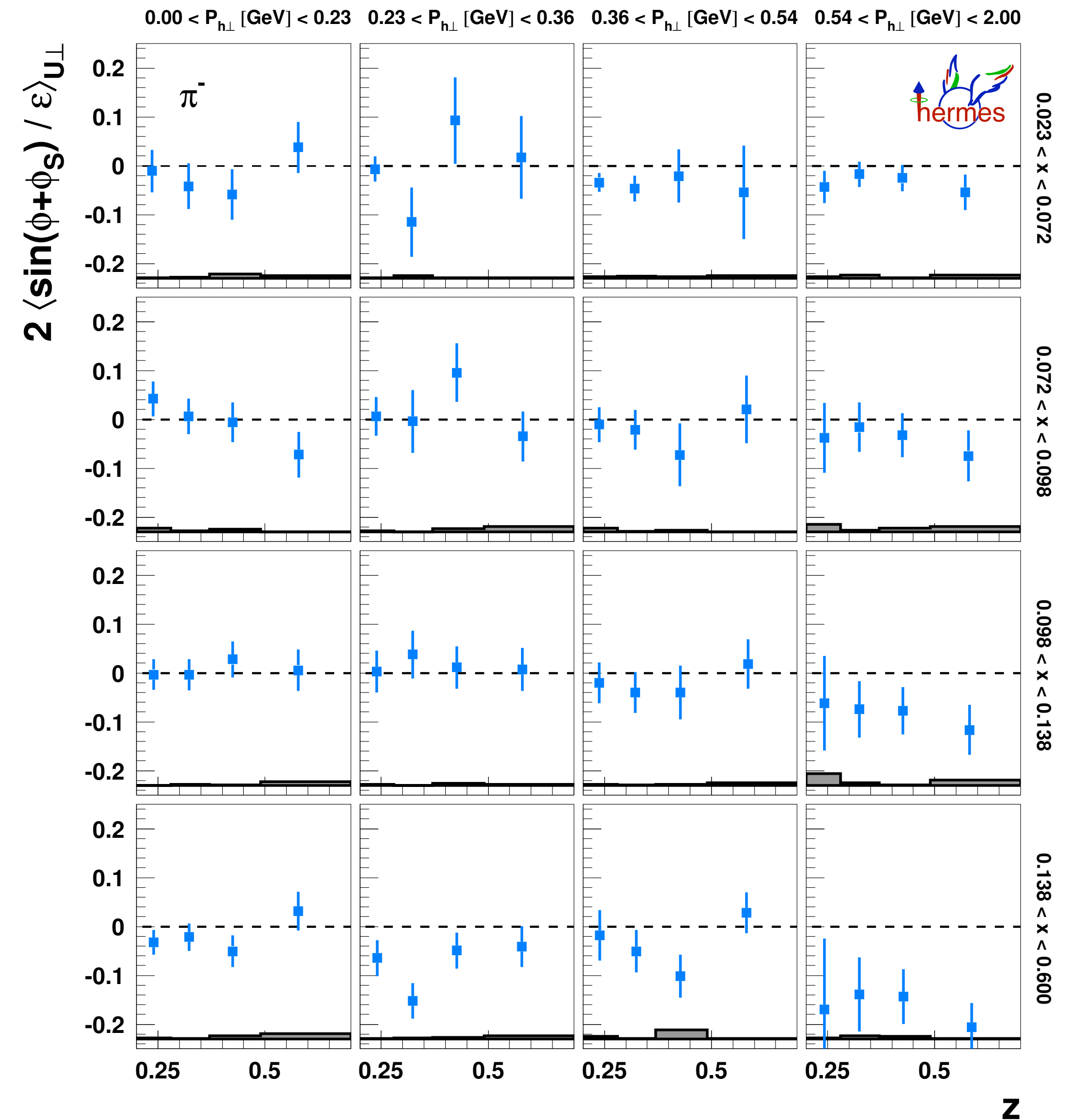
- first-ever results for (anti-)protons consistent with zero
 ➡ vanishing Collins effect for (spin-1/2) baryons?

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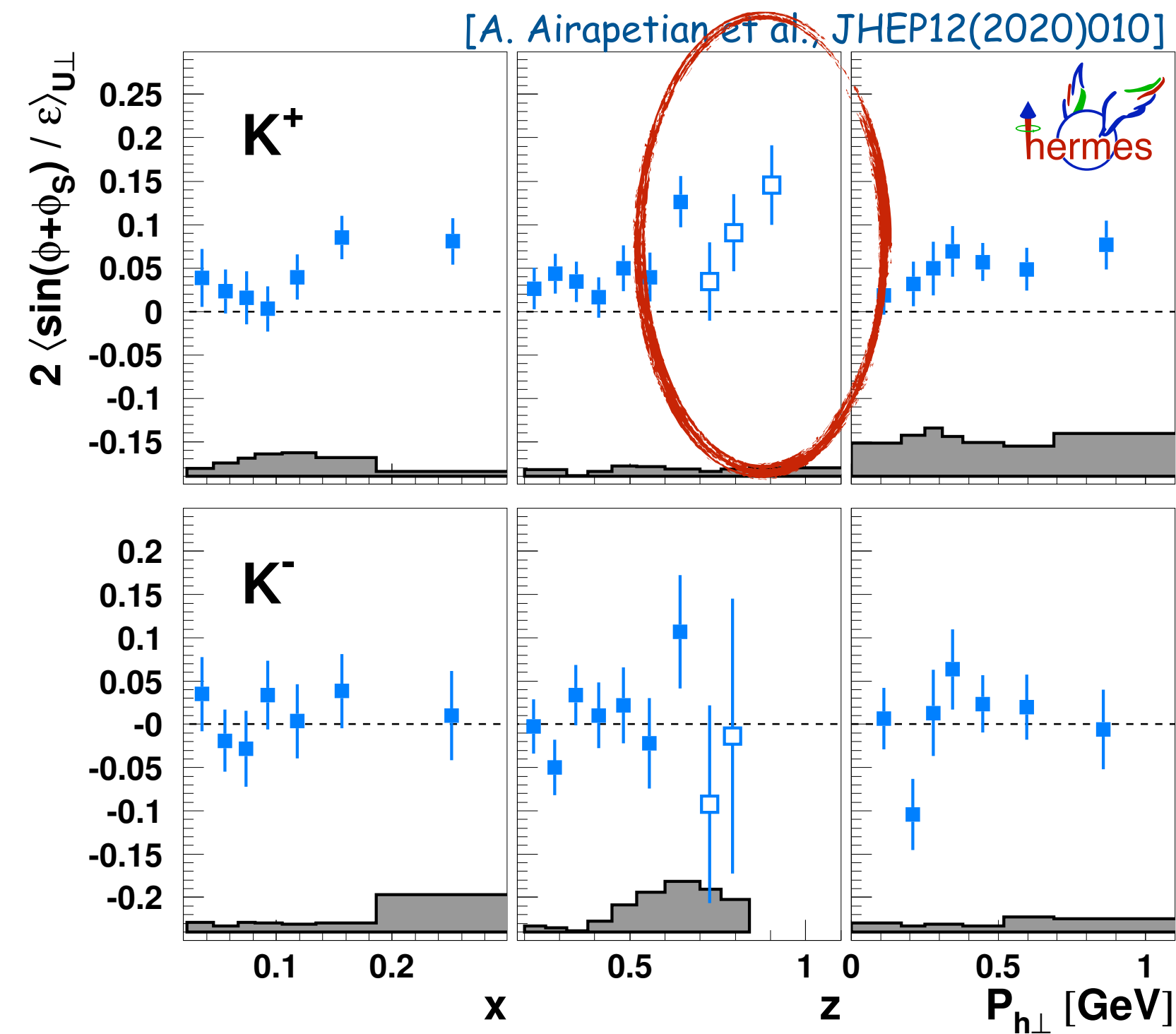
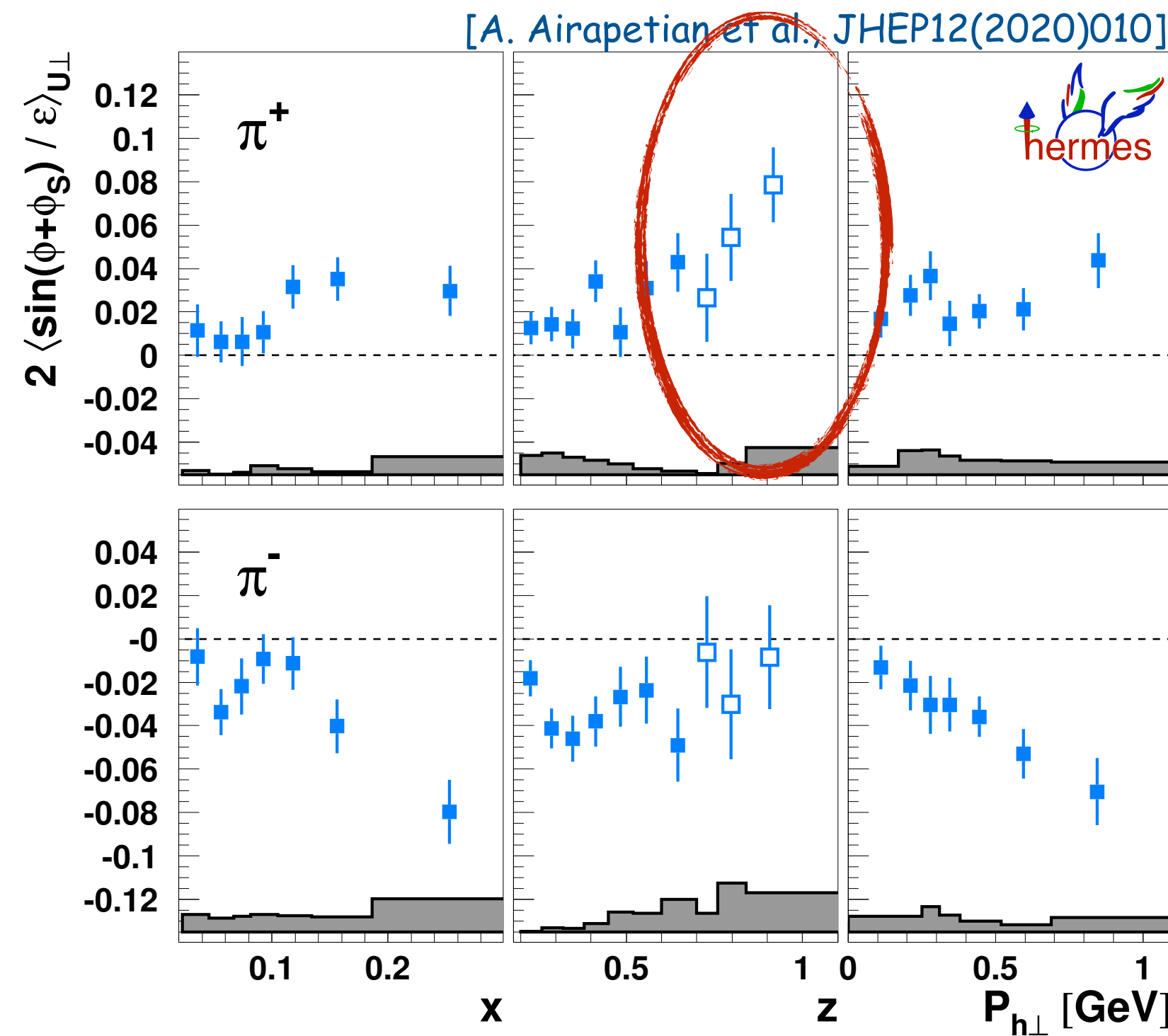


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- analysis now performed in 3d, both including or not including kinematic "depolarization" prefactor



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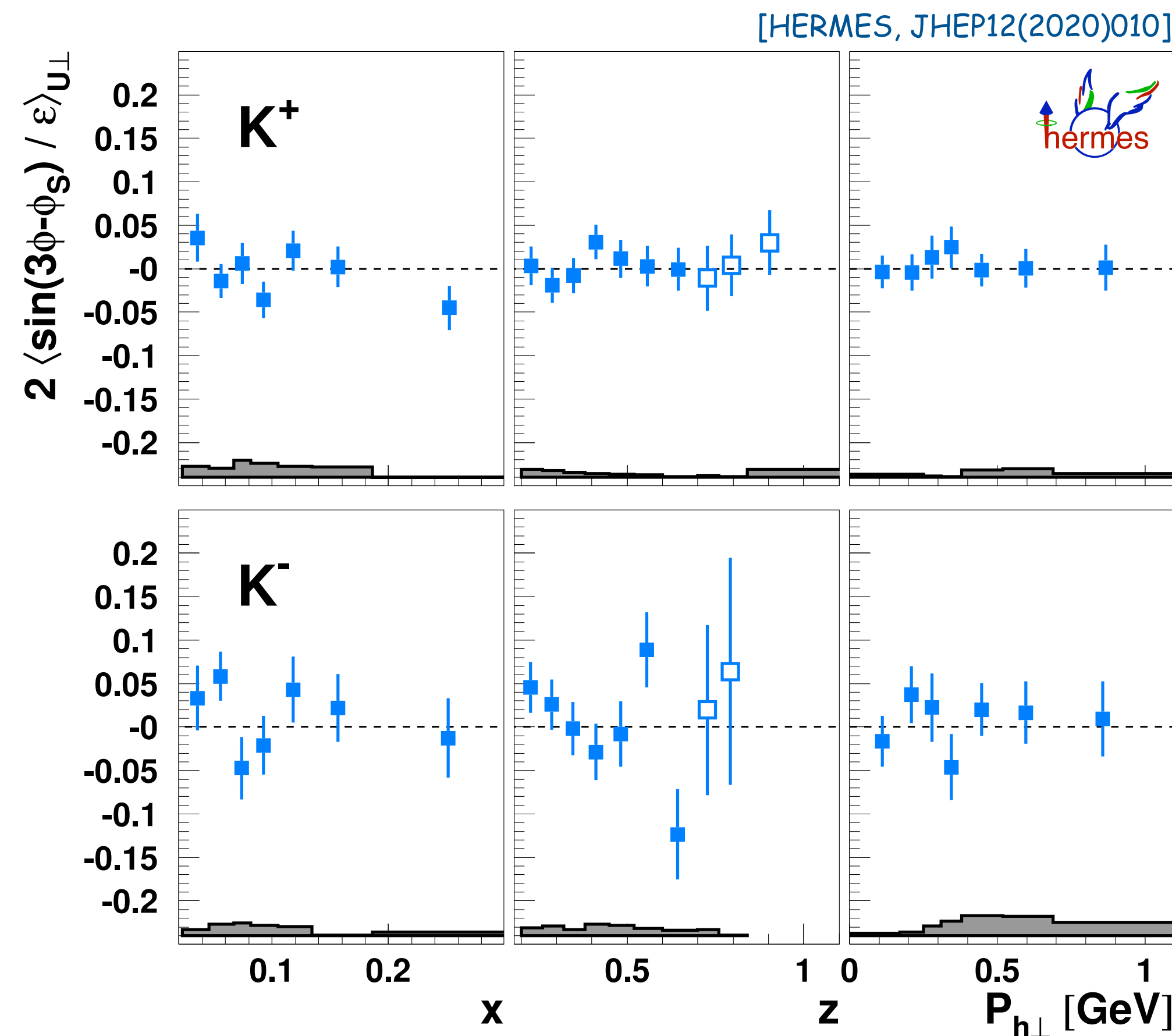
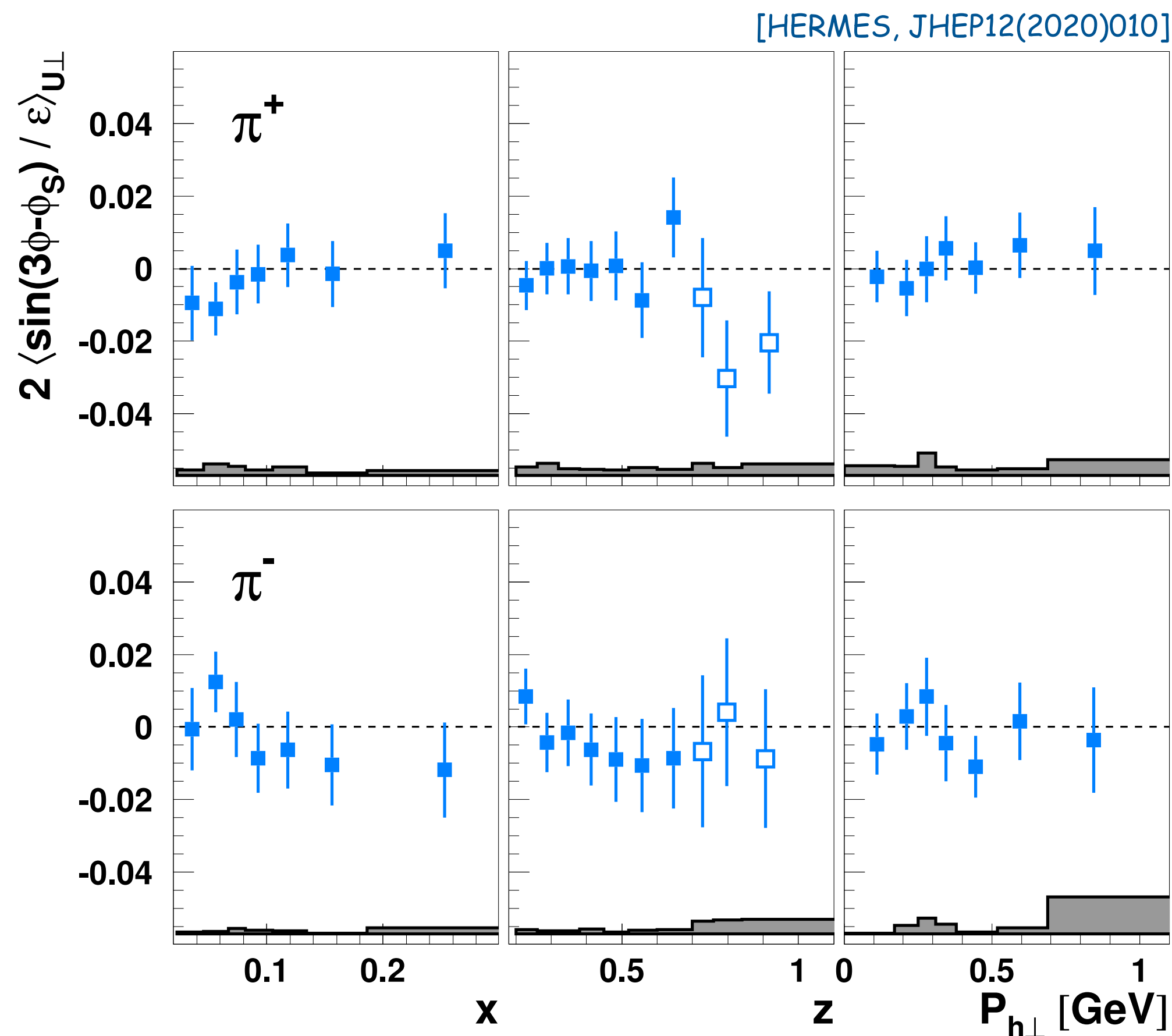


- first-ever results for (anti-)protons consistent with zero
 ➔ vanishing Collins effect for (spin-1/2) baryons?
- analysis now performed in 3d, both including or not including kinematic "depolarization" prefactor
- high- z region with larger quark-flavour sensitivity, with increasing amplitudes for positive pions and kaons

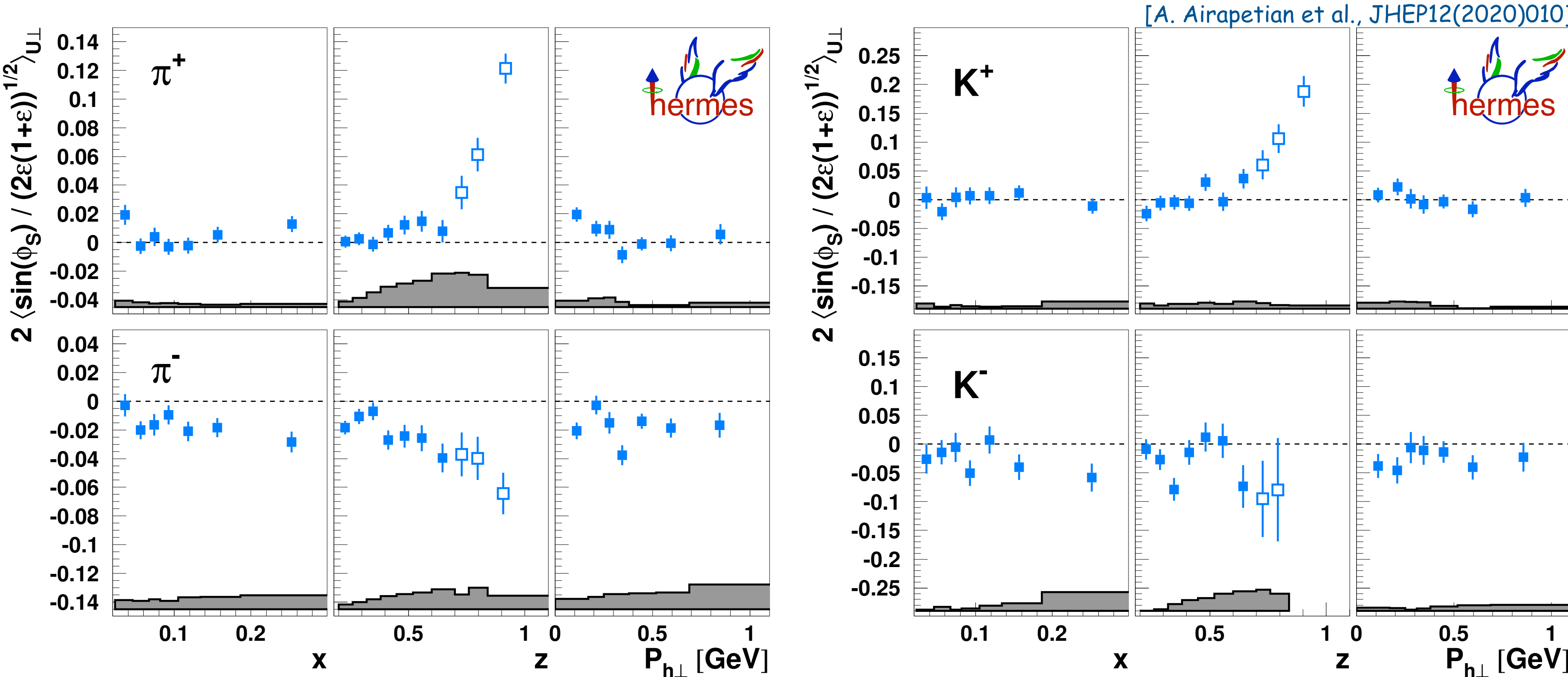
Pretzelosity

- quadrupole deformation in momentum space
- chiral-odd \Rightarrow needs Collins FF (or similar)
- ^1H , ^2H & ^3He data from various experiments consistently small/vanishing
- cancelations? pretzelosity=zero? or just the additional general suppression of the asymmetry by two powers of $P_{h\perp}/M_N$

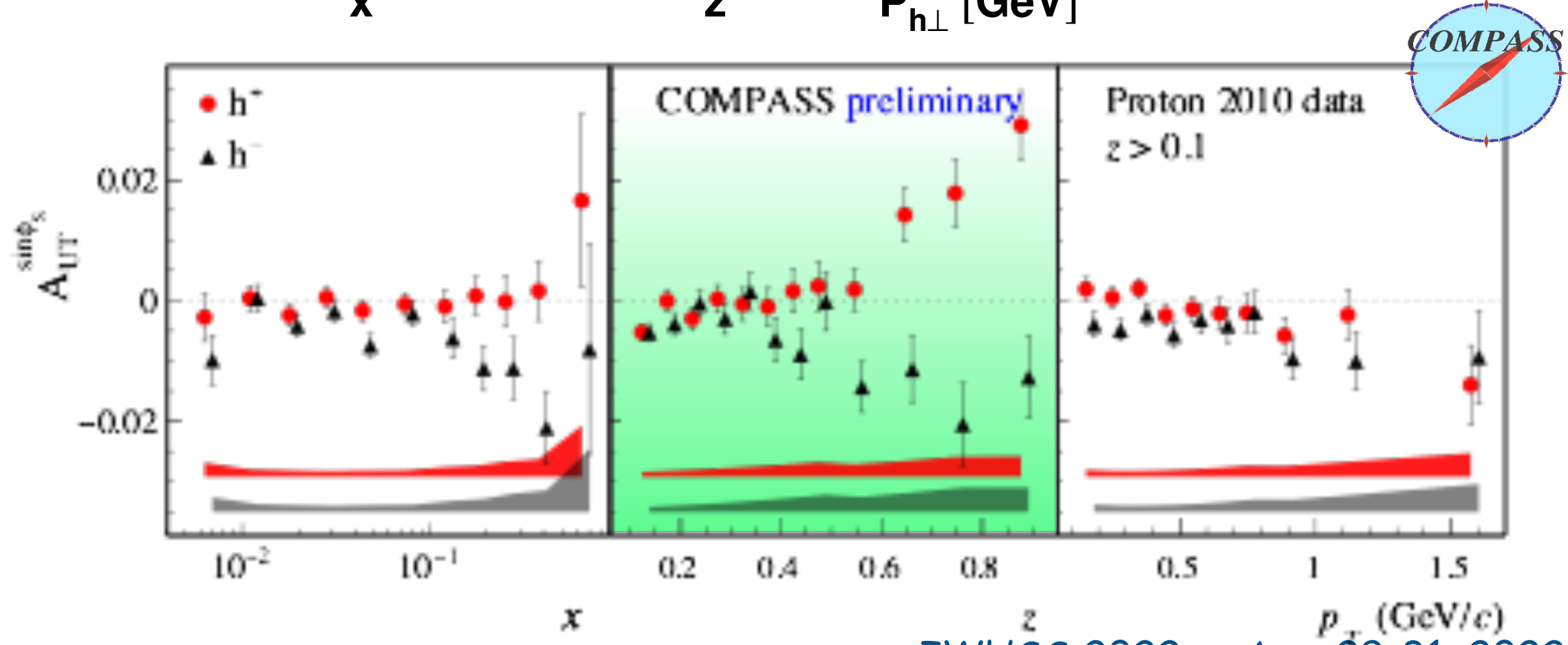
	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp



surprises: subleading twist, e.g., $\langle \sin(\phi_s) \rangle_{UT}$



- clearly non-zero asymmetries
- opposite sign for charged pions (Collins-like behavior)
- striking z dependence and in particular magnitude
- similar observation at COMPASS





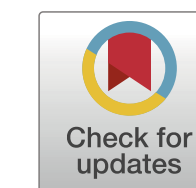
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Beam-helicity asymmetries for single-hadron production in semi-inclusive deep-inelastic scattering from unpolarized hydrogen and deuterium targets

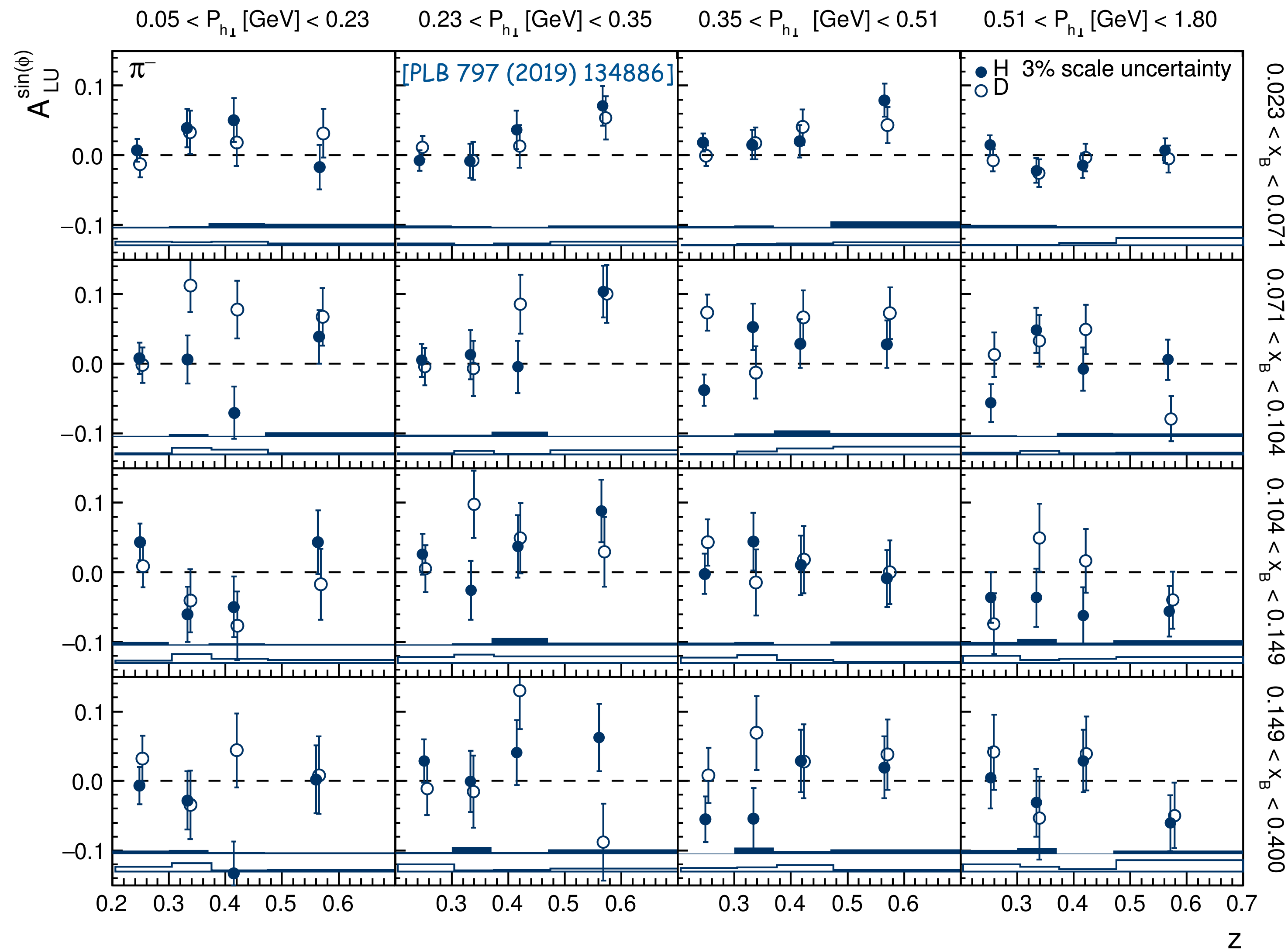


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subleading twist II - $\langle \sin(\phi) \rangle_{LU}$

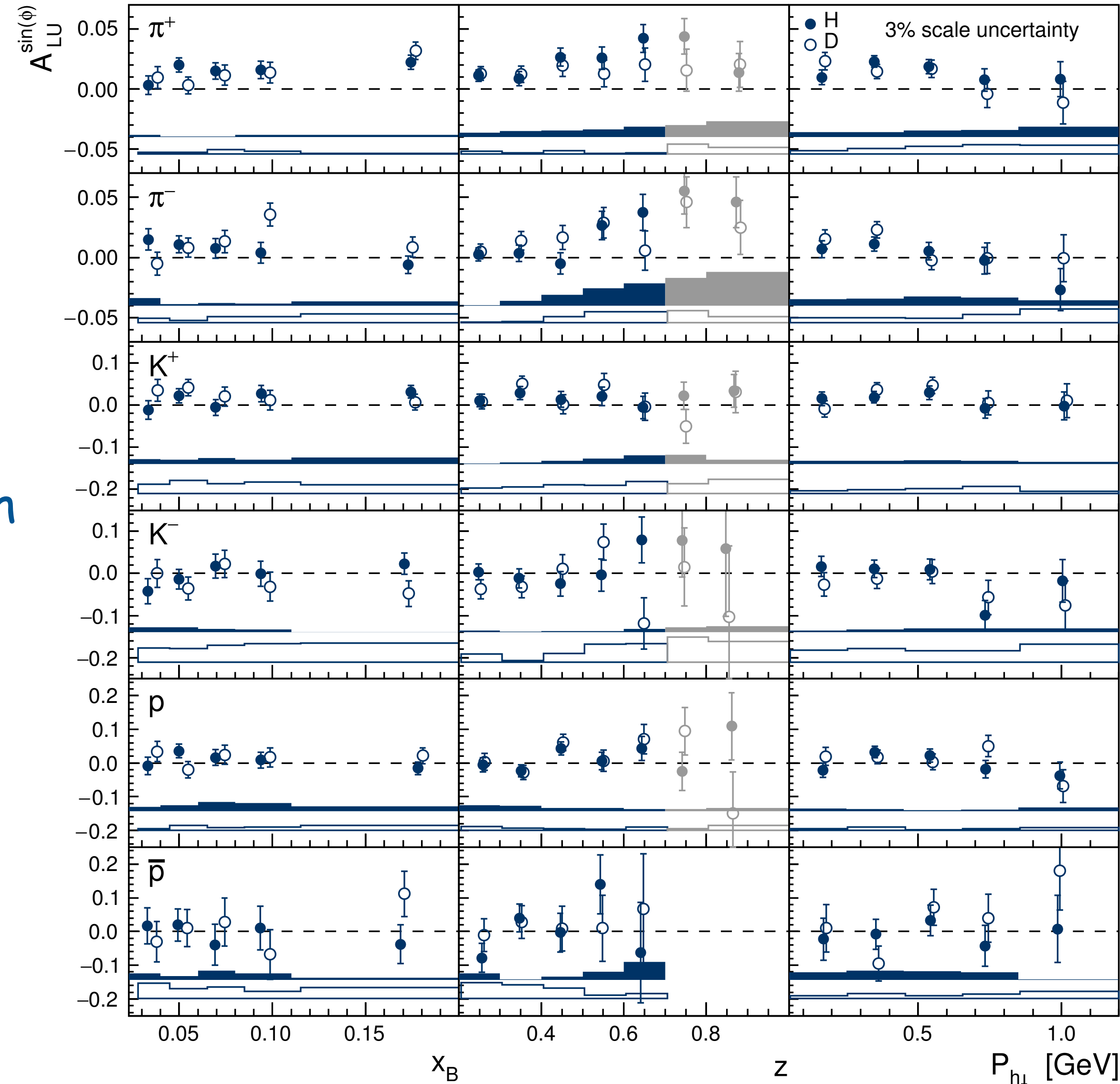
HERMES 3d analysis



most comprehensive presentation; use 1d binning for discussion

$$\frac{M_h}{M_z} h_1^\perp \tilde{E} \oplus x g^\perp D_1 \oplus \frac{M_h}{M_z} f_1 \tilde{G}^\perp \oplus x e H_1^\perp$$

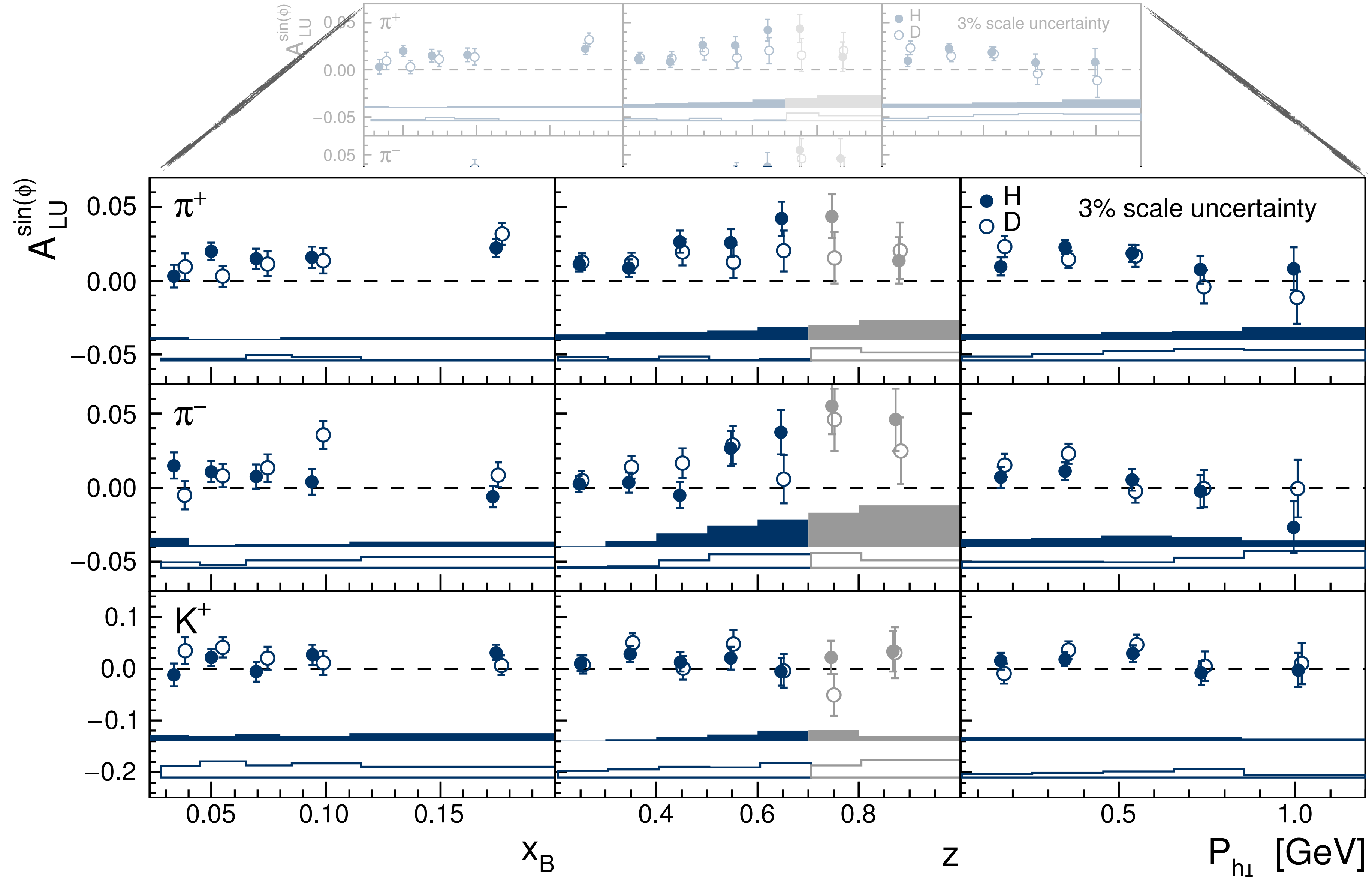
[HERMES, PLB 797 (2019) 134886]



- p & d targets
- π , K, p & \bar{p} final-state h
- SIDIS and high- z transition regions

$$\frac{M_h}{M_z} h_1^\perp \tilde{E} \oplus x g^\perp D_1 \oplus \frac{M_h}{M_z} f_1 \tilde{G}^\perp \oplus x e H_1^\perp$$

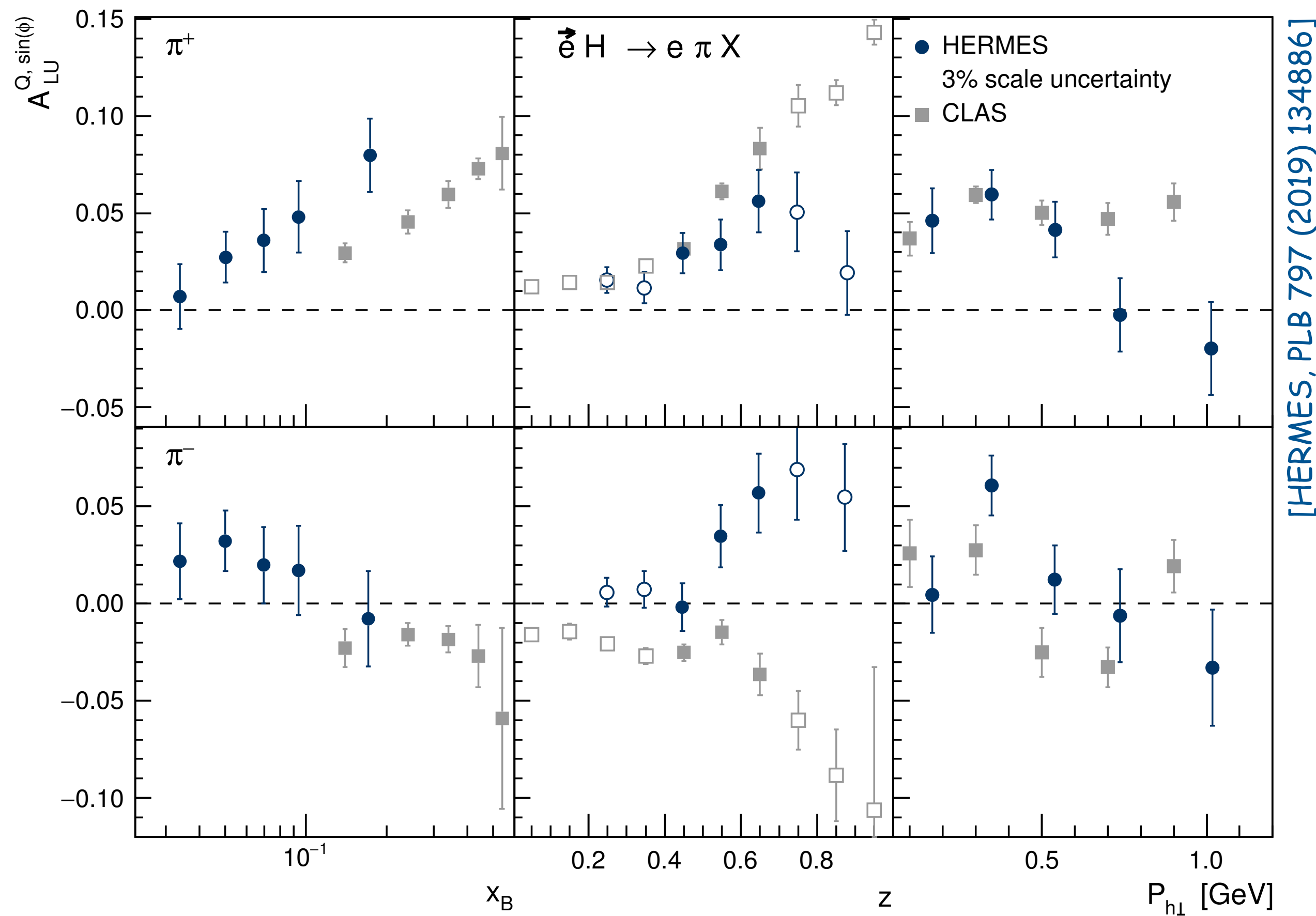
[HERMES, PLB 797 (2019) 134886]



subleading twist II - $\langle \sin(\phi) \rangle_{LU}$

HERMES & CLAS

$$\frac{M_h}{M_z} h_1^\perp \tilde{E} \oplus x g^\perp D_1 \oplus \frac{M_h}{M_z} f_1 \tilde{G}^\perp \oplus \textcolor{red}{x e H_1^\perp}$$



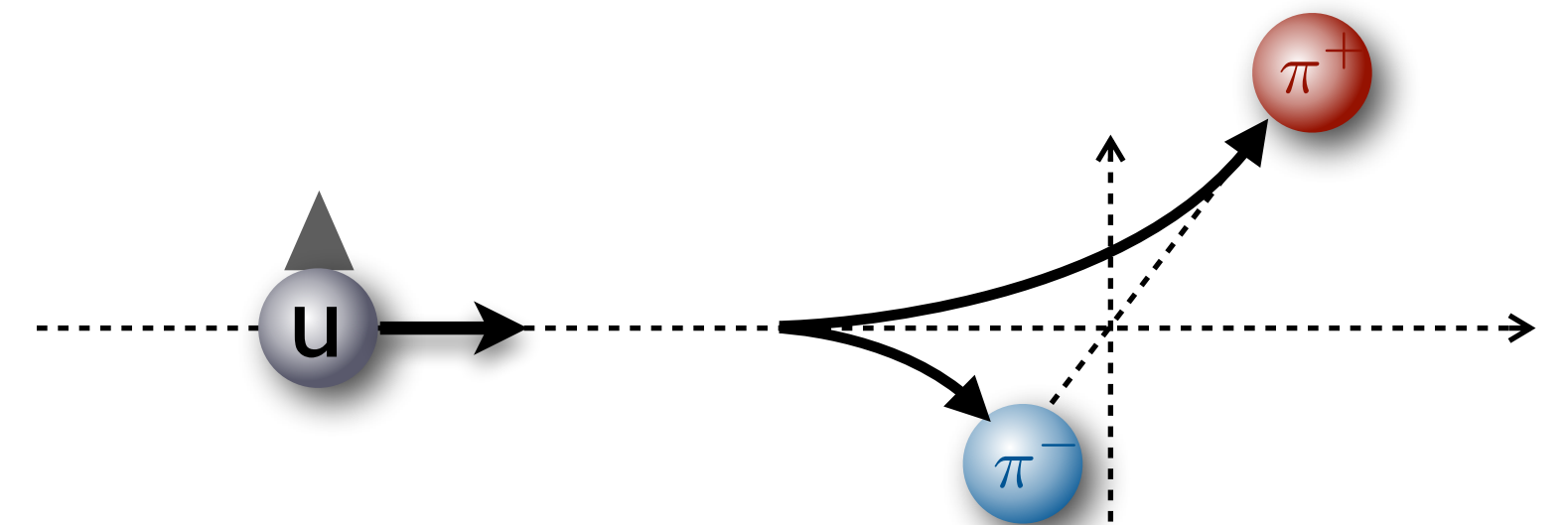
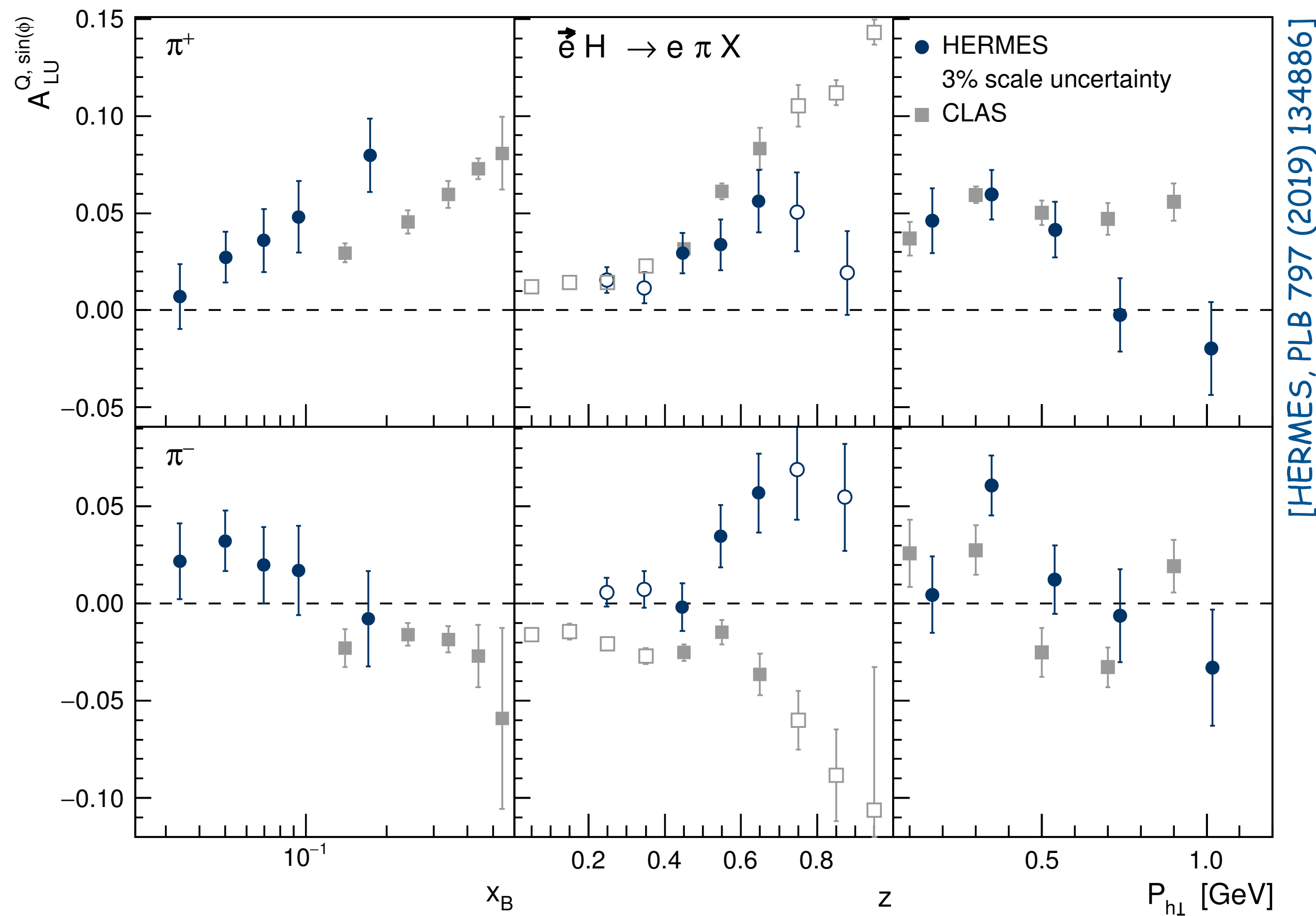
[HERMES, PLB 797 (2019) 134886]

- opposite behavior at HERMES/CLAS of negative pions in z projection due to different x -range probed

subleading twist II - $\langle \sin(\phi) \rangle_{LU}$

HERMES & CLAS

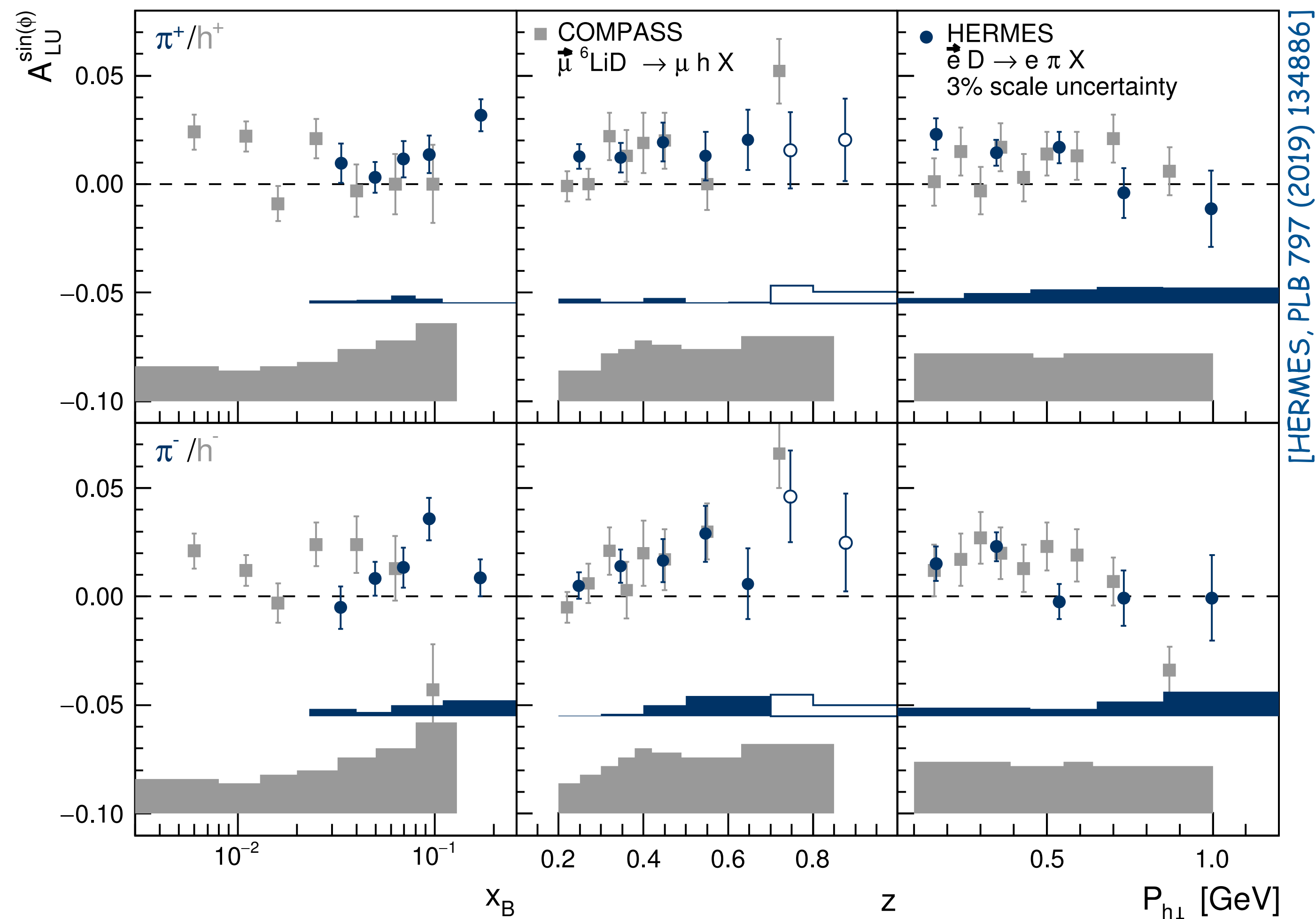
$$\frac{M_h}{M_z} h_1^\perp \tilde{E} \oplus x g^\perp D_1 \oplus \frac{M_h}{M_z} f_1 \tilde{G}^\perp \oplus \textcolor{red}{x e H_1^\perp}$$



- opposite behavior at HERMES/CLAS of negative pions in z projection due to different x -range probed
- CLAS more sensitive to $e(x)$ Collins term due to higher x probed?

subleading twist II - $\langle \sin(\phi) \rangle_{LU}$ HERMES & COMPASS

$$\frac{M_h}{M_z} h_1^\perp \tilde{E} \oplus x g^\perp D_1 \oplus \frac{M_h}{M_z} f_1 \tilde{G}^\perp \oplus x e H_1^\perp$$



consistent behavior for charged pions / hadrons at HERMES / COMPASS for isoscalar targets

- HERMES continues producing results long after its shut-down
 - latest pub's providing 3d presentations of longitudinal & transverse SSA & DSA
 - completes the TMD analyses of single-hadron production
 - several significant leading-twist spin-momentum correlations (Sivers, Collins, worm-gear) but no sign for pretzelosity => clear dipole but no quadrupole deformations
 - surprisingly large twist-3 effects
 - by now, basically all asymmetries (except one: A_{UL}) extracted simultaneously in three or even four dimensions — a rich data set on transverse-momentum distributions
- complementary to data from other facilities
- equally important are studies of generalized parton distributions (see DVCS summary in backup) and many other results not related to 3d structure (e.g., nuclear effects)

PRD 87 (2013) 074029
PRD 87 (2013) 012010

PRD 87 (2013) 012010

quark pol.

nucleon pol.

	U	L	T
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PRD 99 (2019) 112001

PRL 84 (2000) 4047
PRD 64 (2001) 097101
PLB 562 (2003) 182

JHEP 12(2020)010

PRL 94 (2005) 012002
PRL 103 (2009) 152002
JHEP 12(2020)010

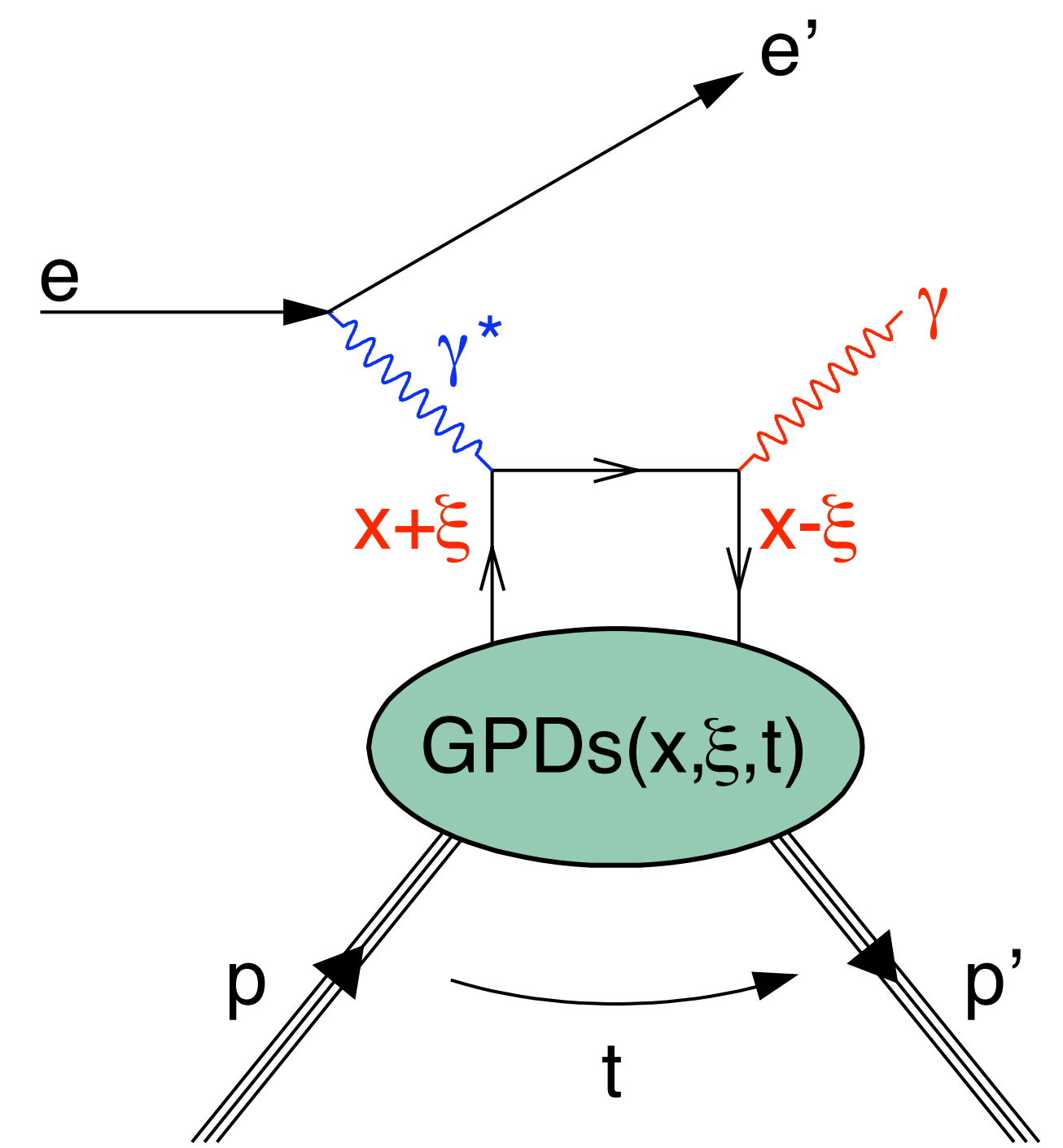
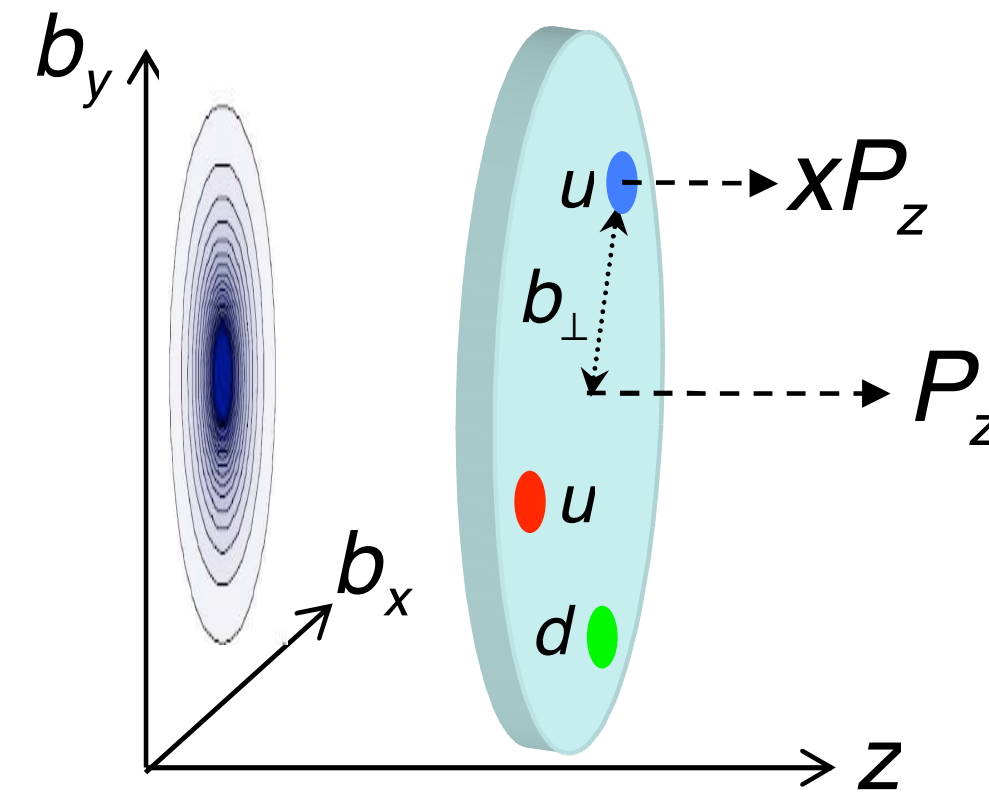
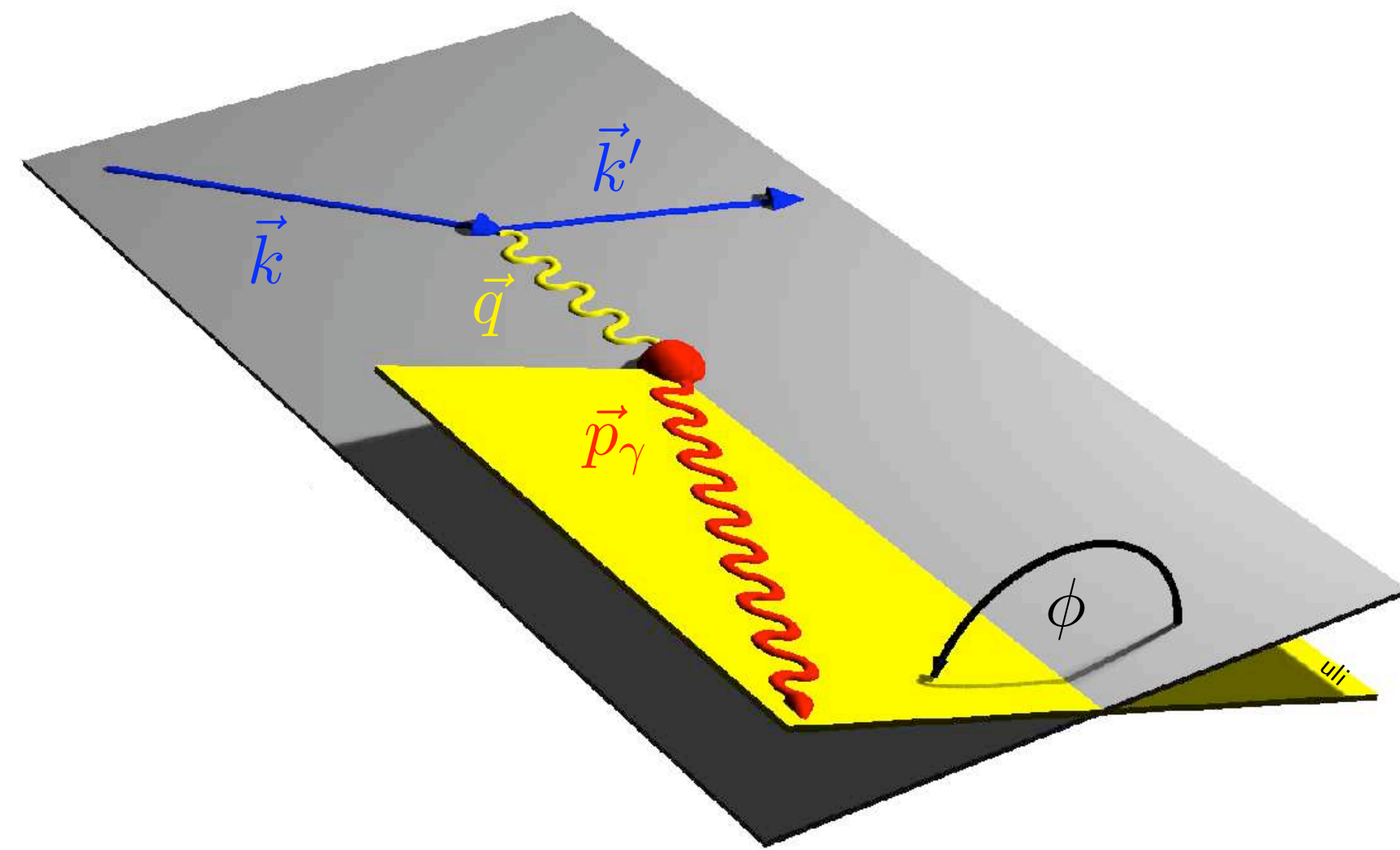
JHEP 12(2020)010

PRL 94 (2005) 012002
JHEP 06(2008)017
PLB 693 (2010) 11
JHEP 12(2020)010

backup slides

deeply virtual Compton
scattering (DVCS)

DVCS

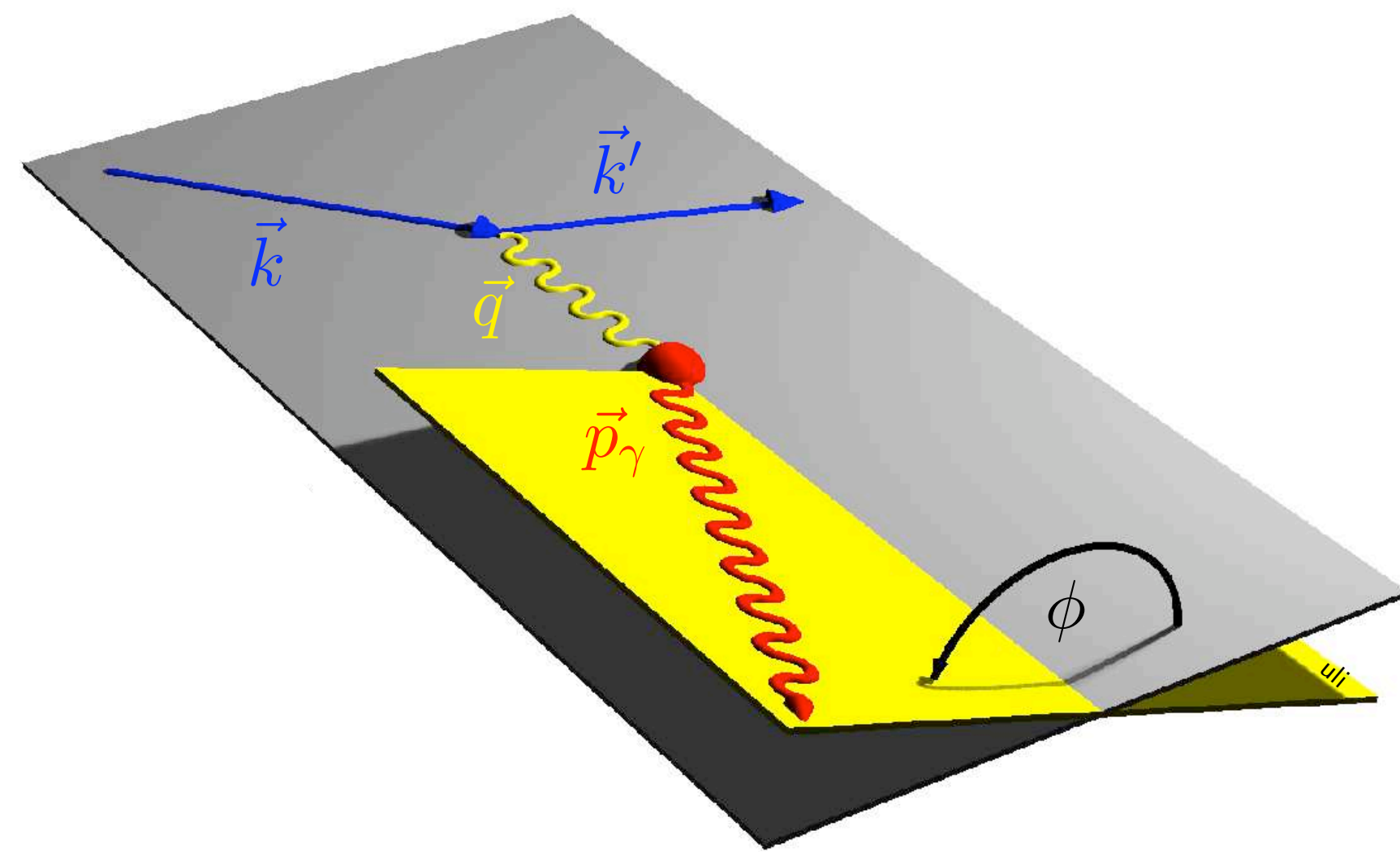


- beam polarization P_B
- beam charge C_B
- here: unpolarized target
(many more modulations
for polarized targets)

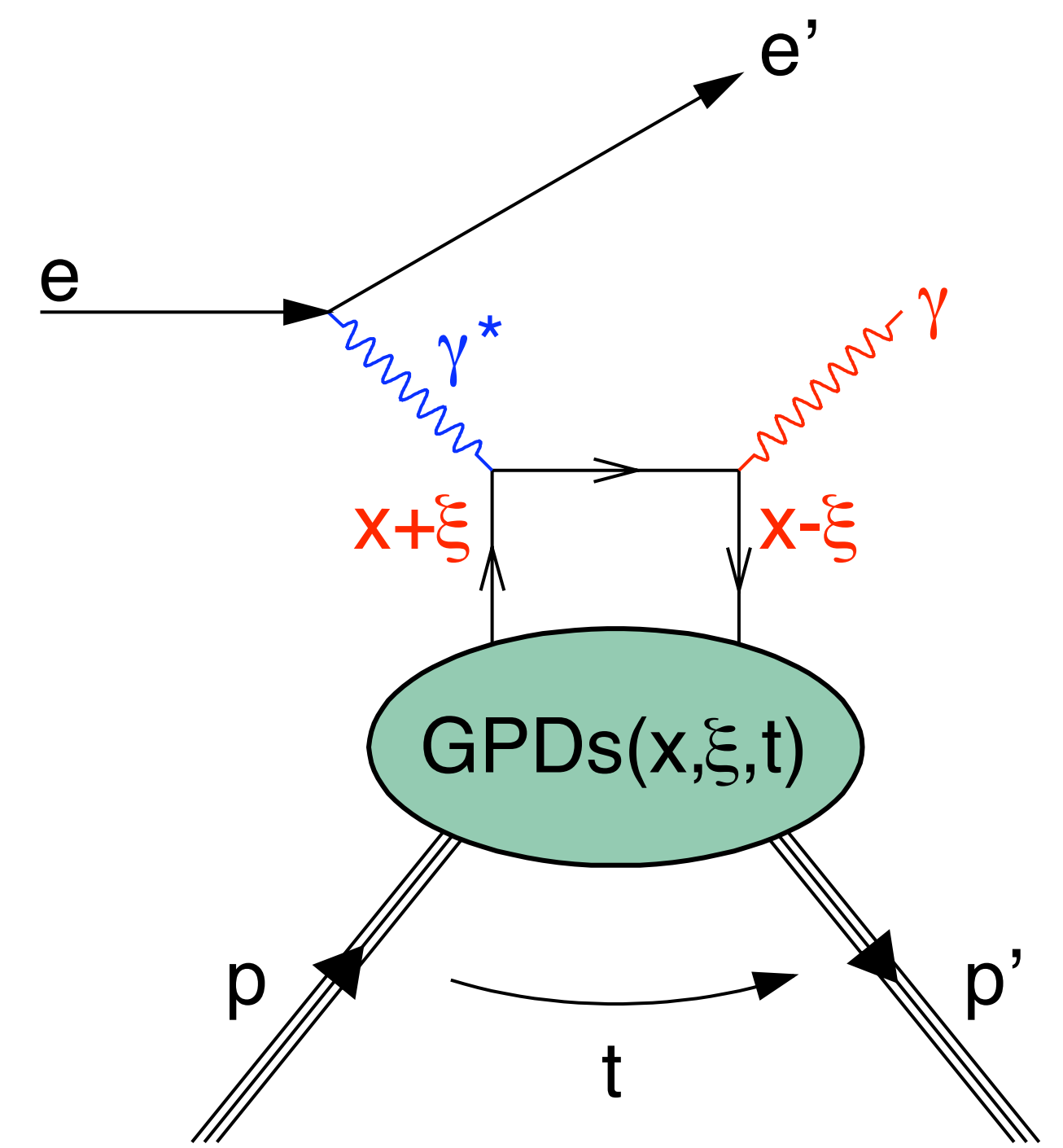
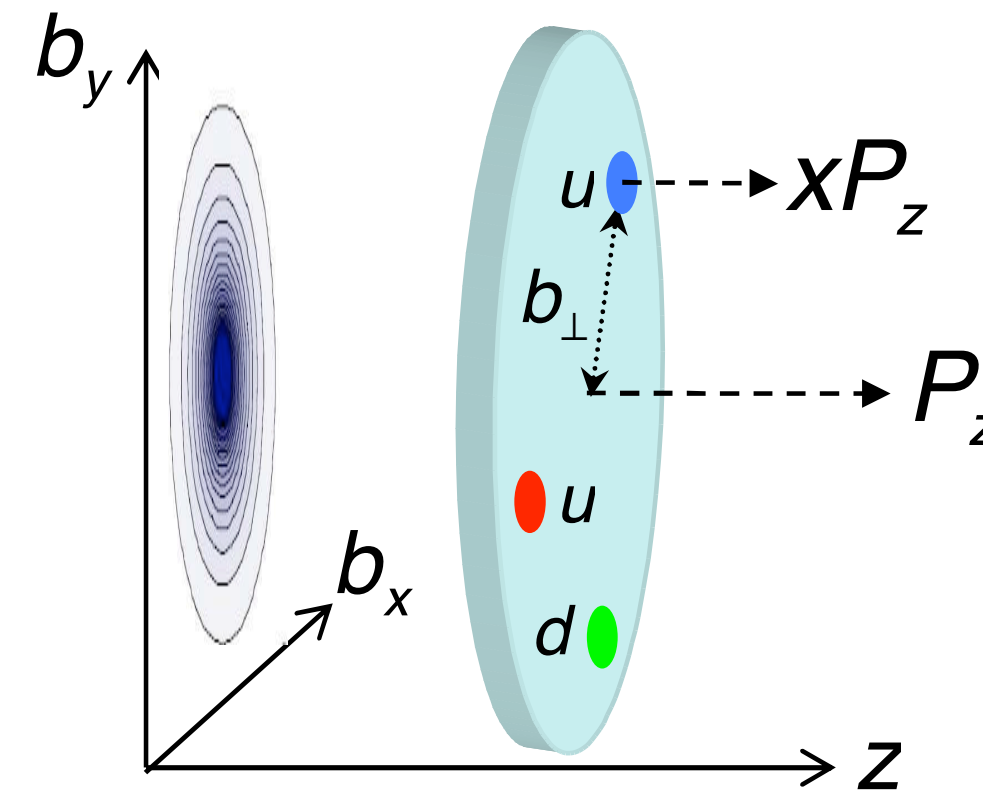
Fourier expansion for ϕ :

$$|\mathcal{T}_{BH}|^2 = \frac{K_{BH}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \sum_{n=0}^2 c_n^{BH} \cos(n\phi)$$

calculable in QED
(using form-factor measurements)



DVCS

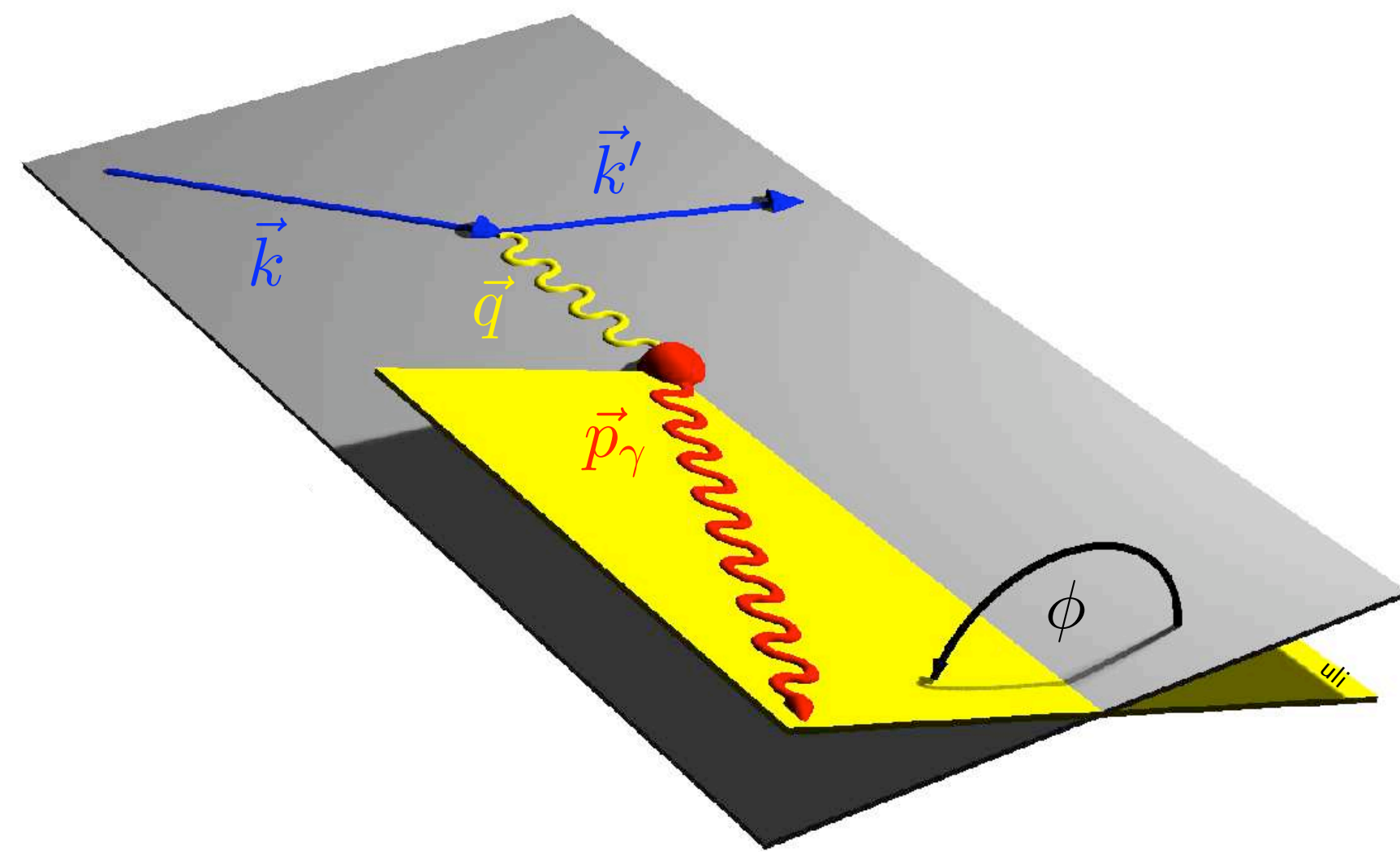


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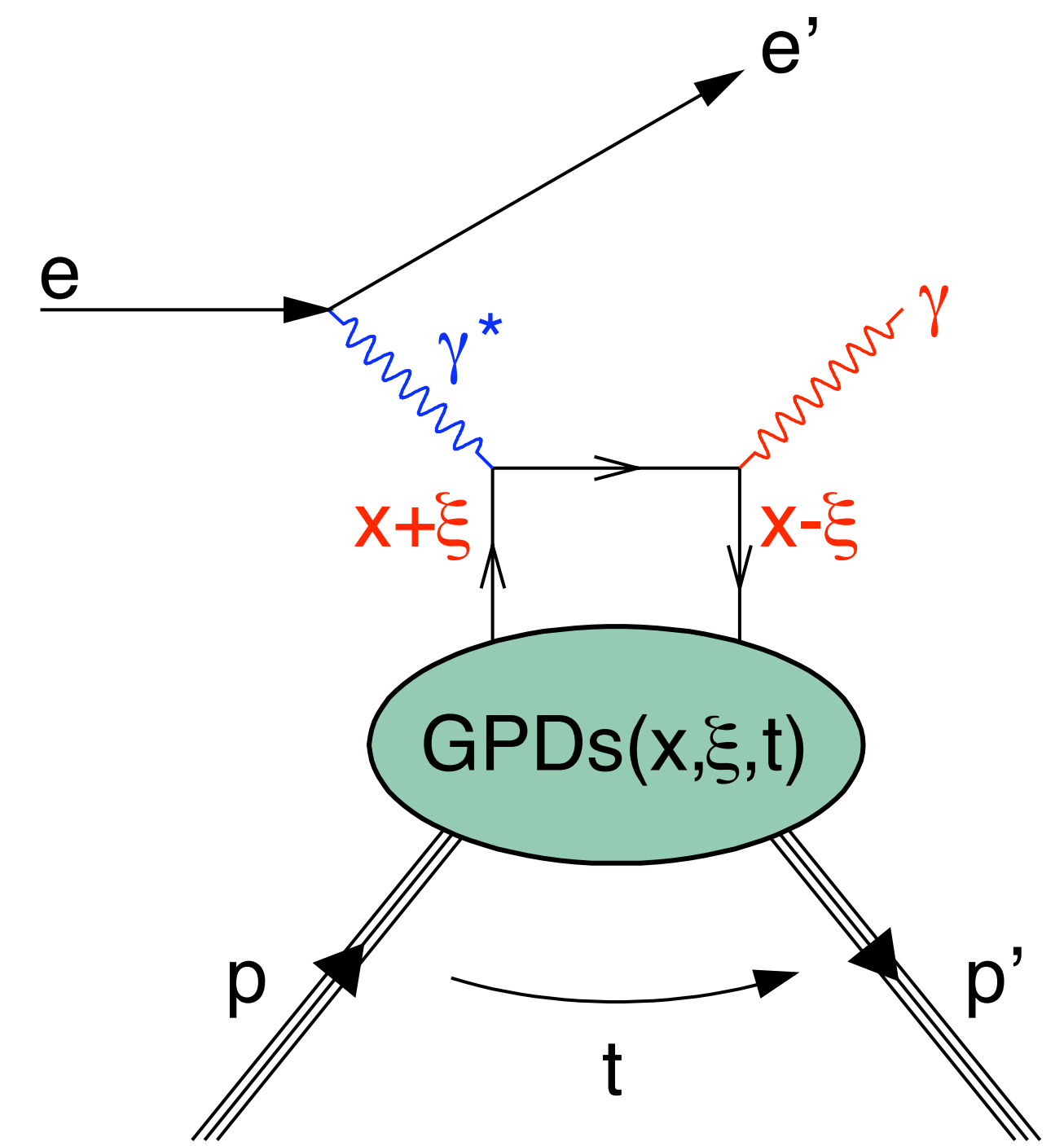
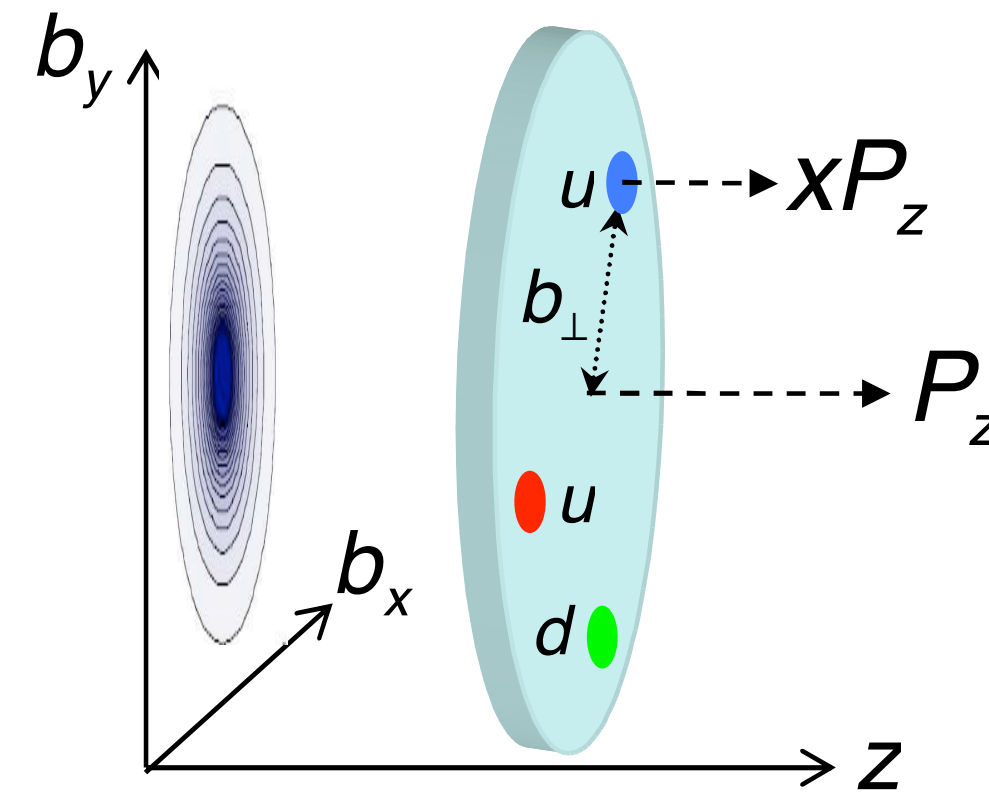
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$$|\mathcal{T}_{\text{DVCS}}|^2 = K_{\text{DVCS}} \left[\sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi) + P_B \sum_{n=1}^1 s_n^{\text{DVCS}} \sin(n\phi) \right]$$



DVCS



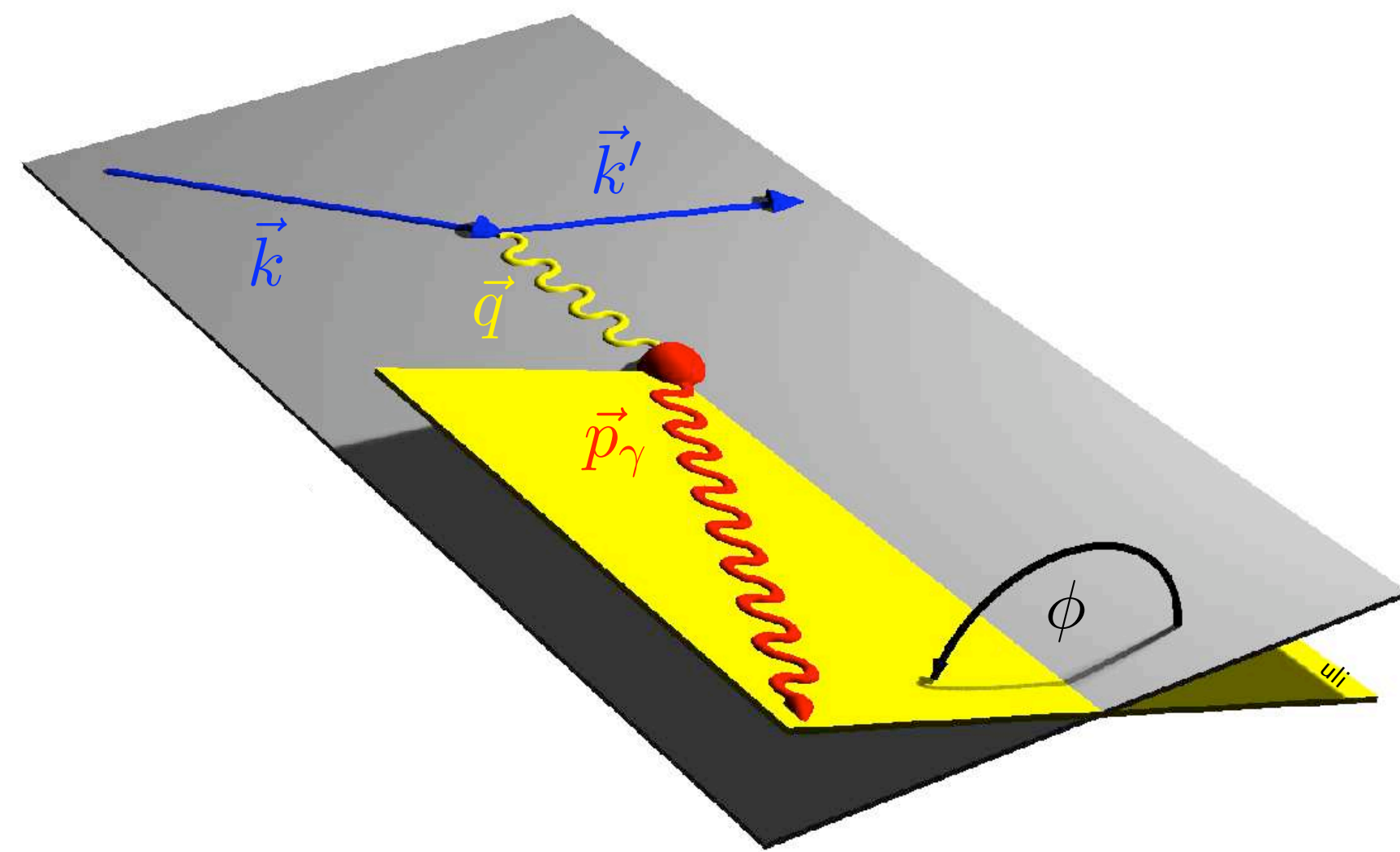
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(many more modulations for polarized targets)

Fourier expansion for ϕ :

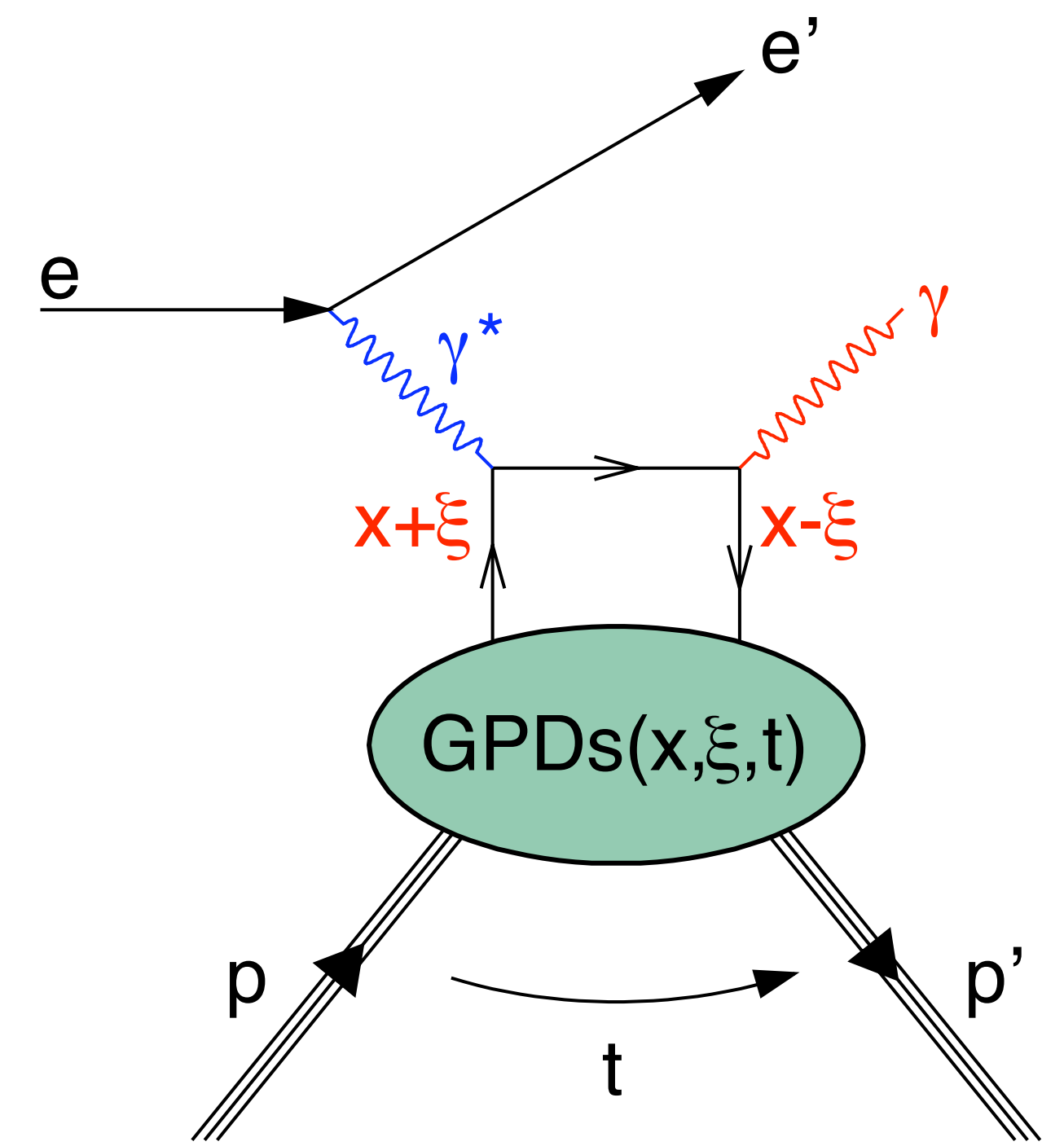
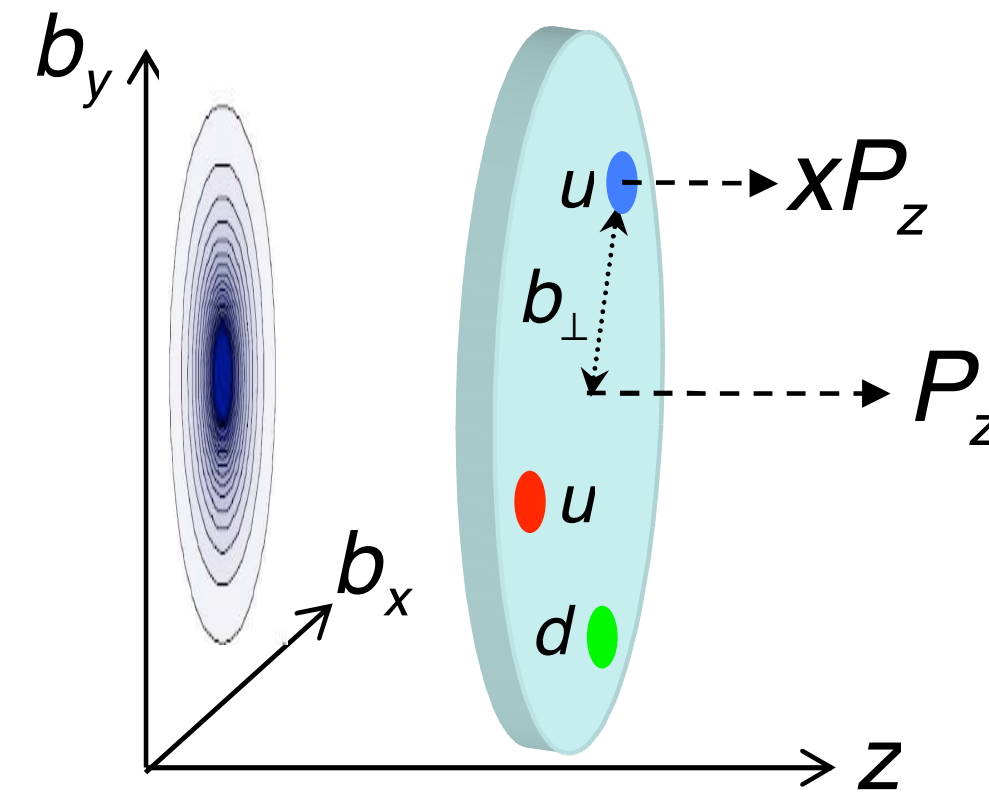
$$|\mathcal{T}_{\text{BH}}|^2 = \frac{K_{\text{BH}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \sum_{n=0}^2 c_n^{\text{BH}} \cos(n\phi)$$

$$|\mathcal{T}_{\text{DVCS}}|^2 = K_{\text{DVCS}} \left[\sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi) + P_B \sum_{n=1}^1 s_n^{\text{DVCS}} \sin(n\phi) \right]$$

$$\mathcal{I} = \frac{C_B K_{\mathcal{I}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left[\sum_{n=0}^3 c_n^{\mathcal{I}} \cos(n\phi) + P_B \sum_{n=1}^2 s_n^{\mathcal{I}} \sin(n\phi) \right]$$



DVCS



- beam polarization P_B
- beam charge C_B
- here: unpolarized target (many more modulations for polarized targets)

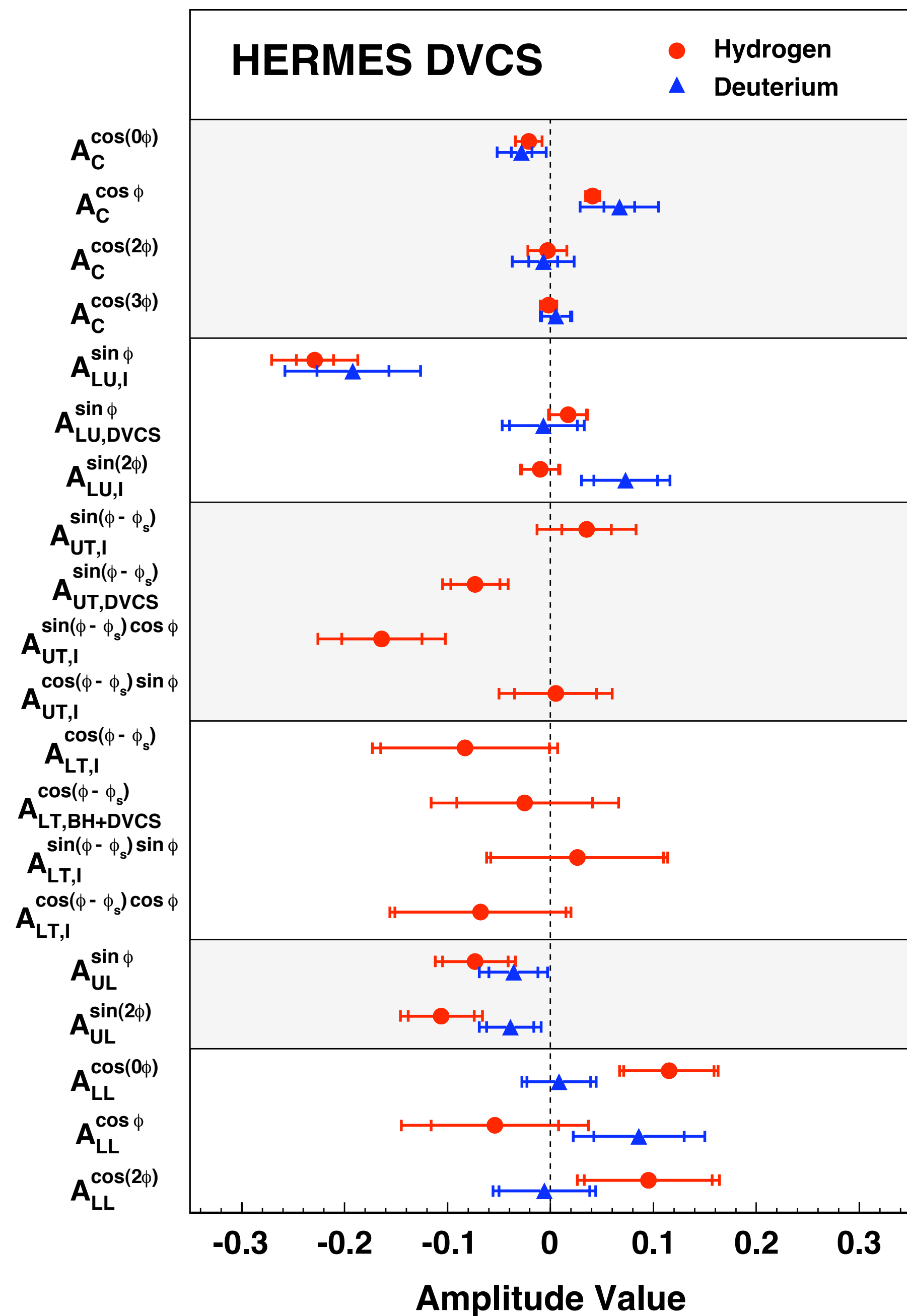
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bilinear ("DVCS") or linear in GPDs



Beam-charge asymmetry:

$GPD\ H$

PRD 75 (2007) 011103

NPB 829 (2010) 1

JHEP 11 (2009) 083

Beam-helicity asymmetry:

$GPD\ H$

PRC 81 (2010) 035202

PRL 87 (2001) 182001

JHEP 07 (2012) 032

Transverse target spin asymmetries:

$GPD\ E$ from proton target

JHEP 06 (2008) 066

PLB 704 (2011) 15

Longitudinal target spin asymmetry:

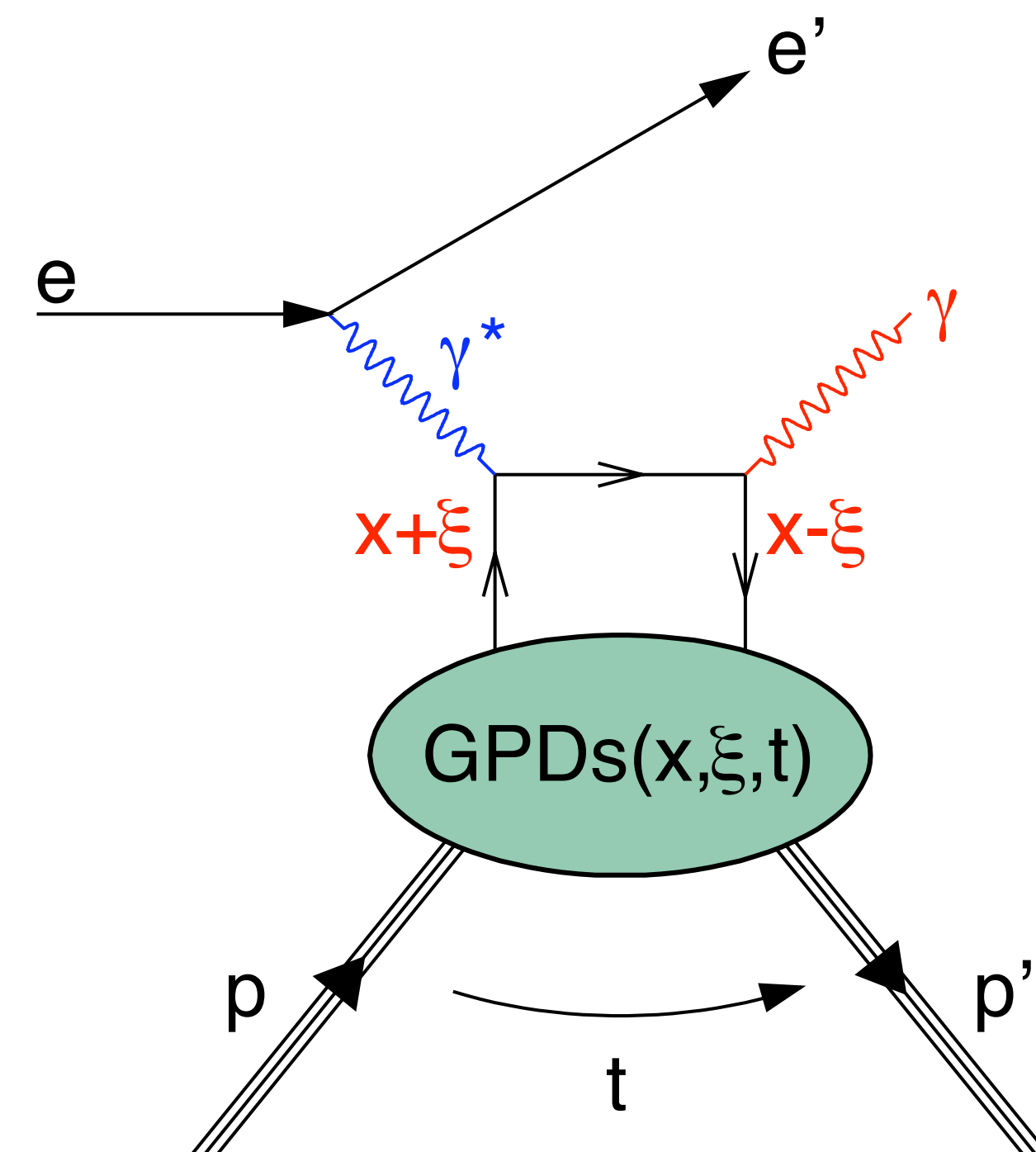
$GPD\ \tilde{H}$

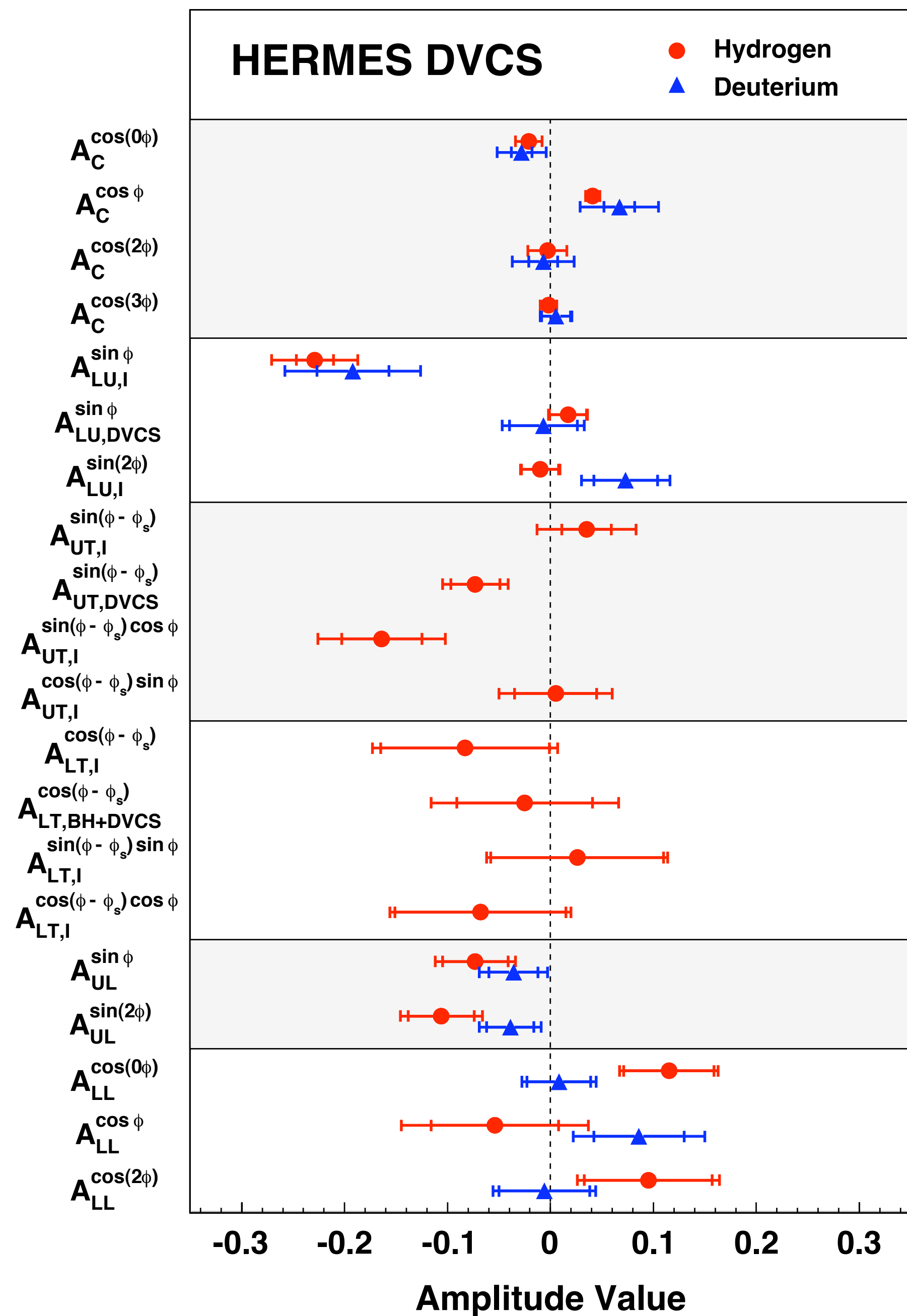
JHEP 06 (2010) 019

Double-spin asymmetry:

$GPD\ \tilde{H}$

NPB 842 (2011) 265





Beam-charge asymmetry:

$GPD\ H$

PRD 75 (2007) 011103

NPB 829 (2010) 1

JHEP 11 (2009) 083

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PLB 704 (2011) 15

Longitudinal target spin asymmetry:

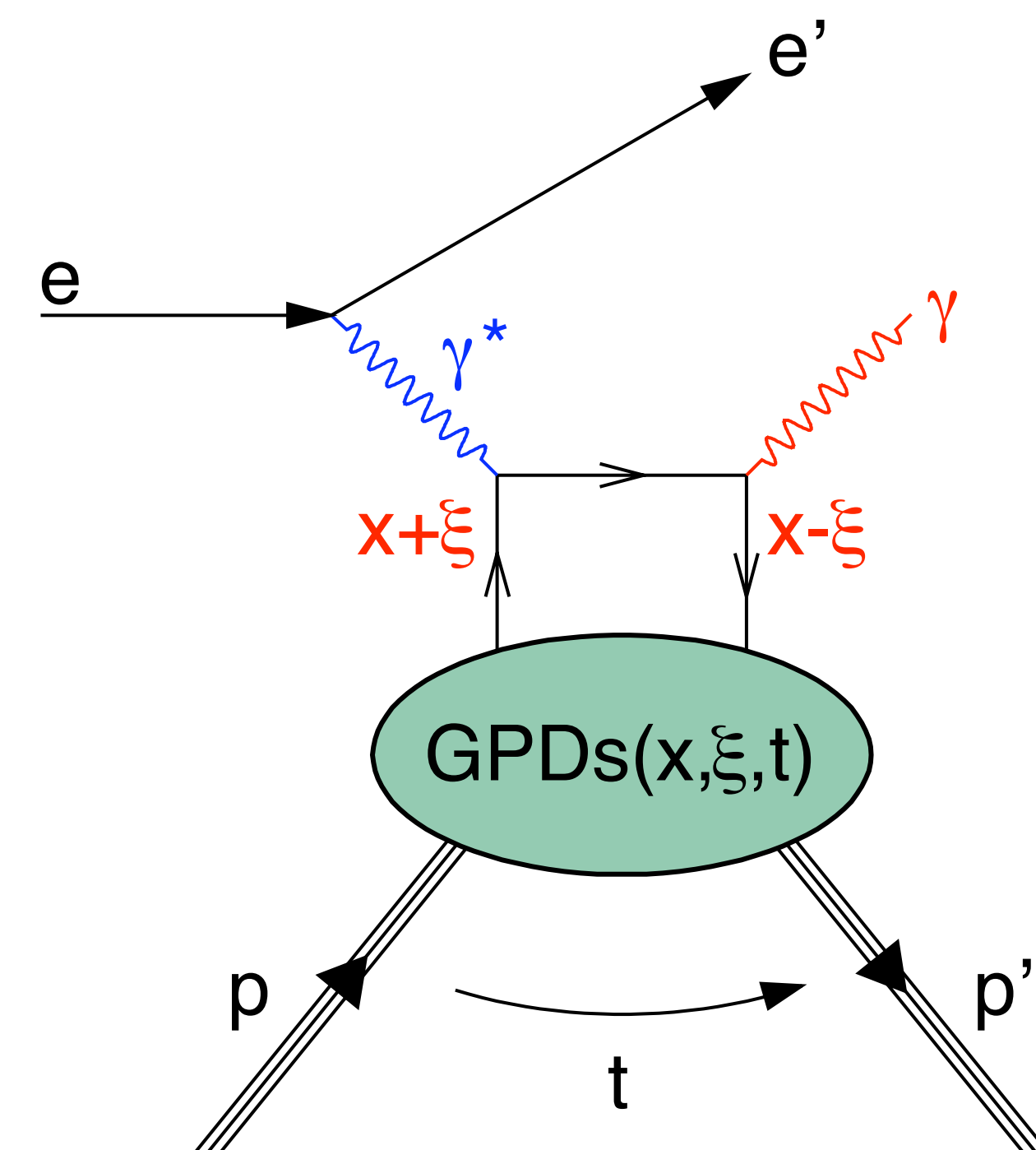
$GPD\ \tilde{H}$

JHEP 06 (2010) 019

Double-spin asymmetry:

$GPD\ \tilde{H}$

NPB 842 (2011) 265

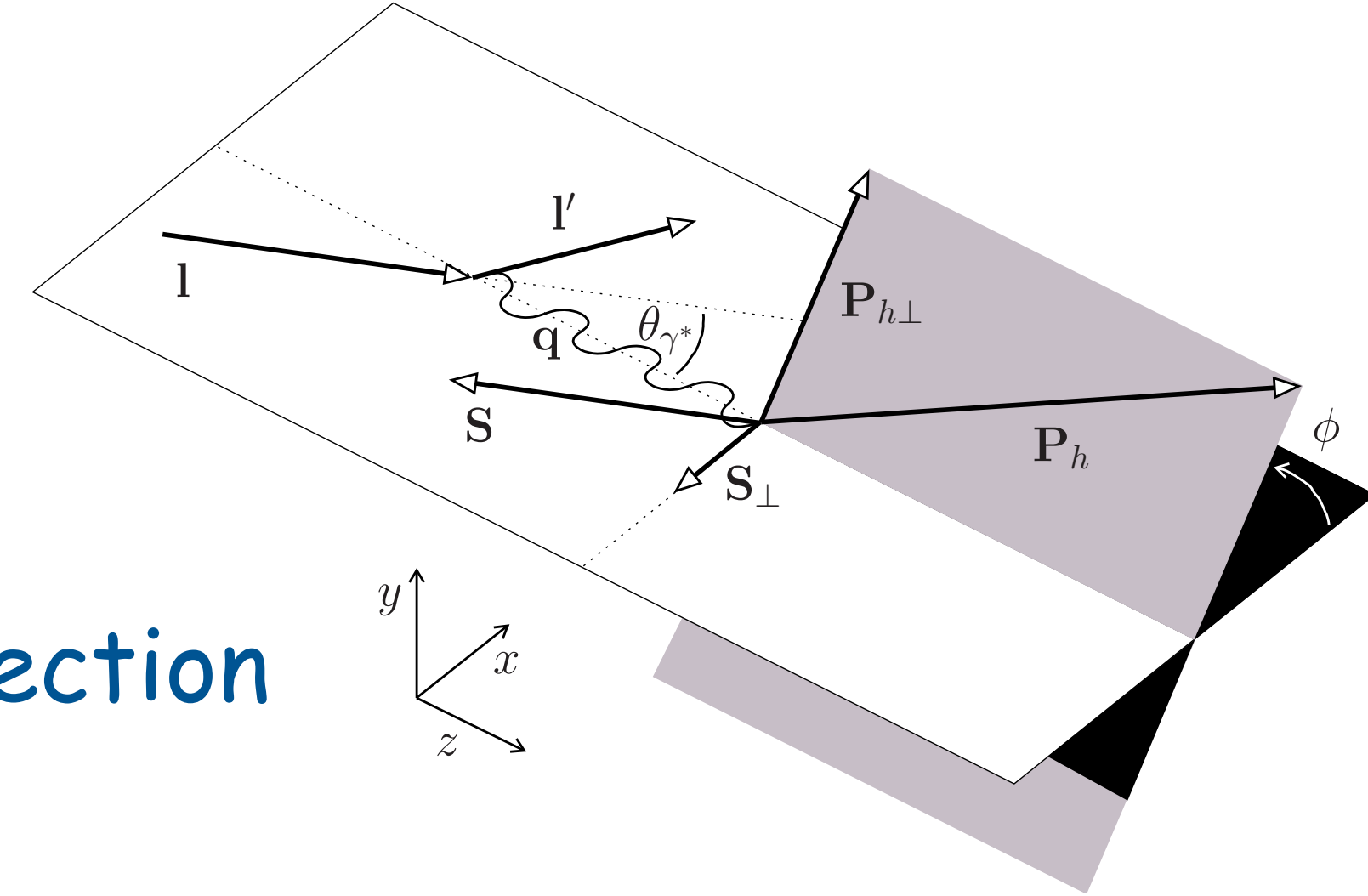


however, no cross-section measurement so far at HERMES kinematics!

non-vanishing twist-3

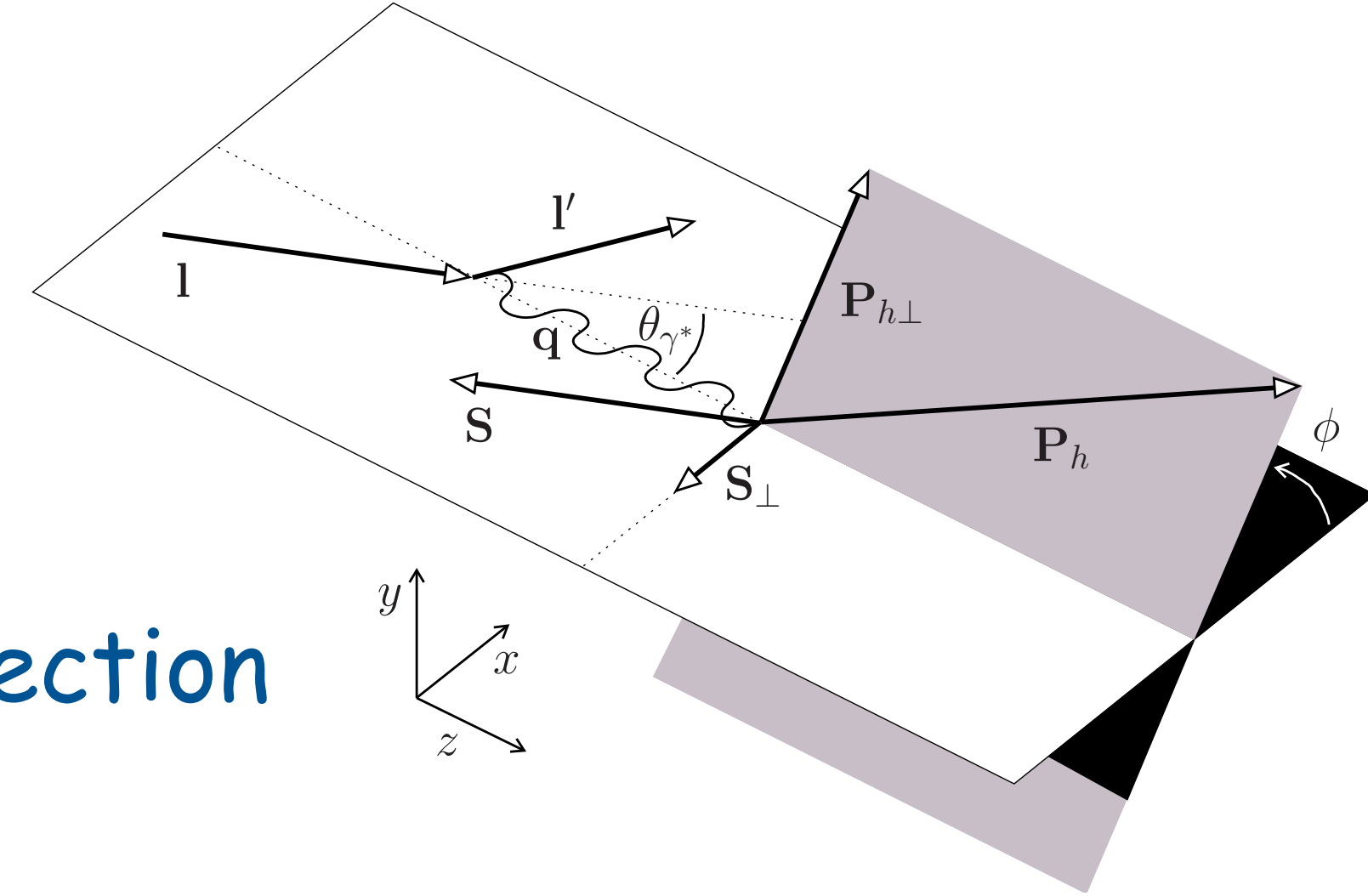
subleading twist I - $\langle \sin(\phi) \rangle_{UL}$

- theory done w.r.t. virtual-photon direction
- experiments use targets polarized w.r.t. lepton-beam direction



subleading twist I - $\langle \sin(\phi) \rangle_{UL}$

- theory done w.r.t. virtual-photon direction
 - experiments use targets polarized w.r.t. lepton-beam direction
- ➔ mixing of longitudinal and transverse polarization effects
[Diehl & Sapeta, EPJ C 41 (2005) 515], e.g.,

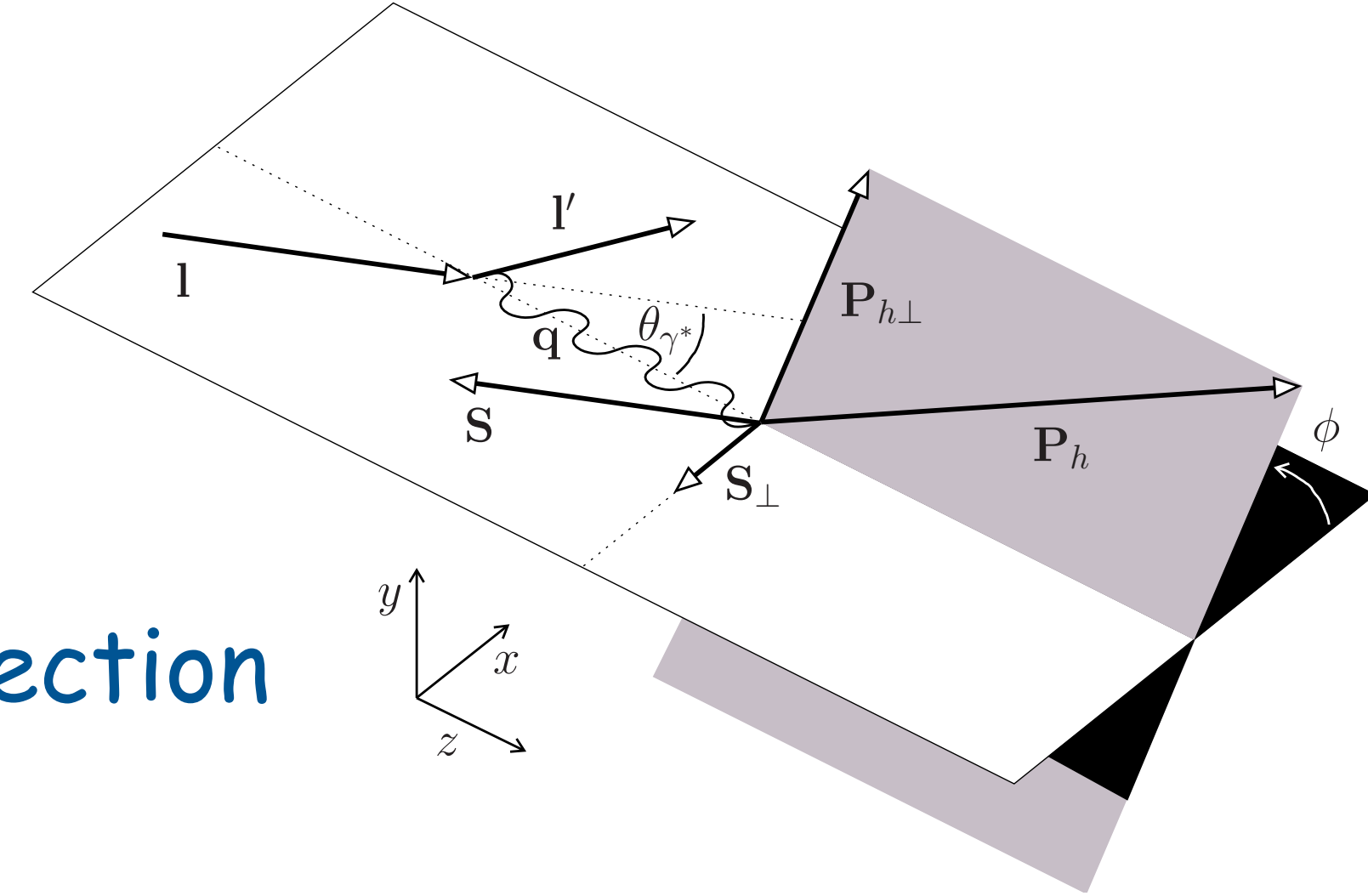


$$\begin{pmatrix} \langle \sin \phi \rangle_{UL}^I \\ \langle \sin(\phi - \phi_S) \rangle_{UT}^I \\ \langle \sin(\phi + \phi_S) \rangle_{UT}^I \end{pmatrix} = \begin{pmatrix} \cos \theta_{\gamma^*} & -\sin \theta_{\gamma^*} & -\sin \theta_{\gamma^*} \\ \frac{1}{2} \sin \theta_{\gamma^*} & \cos \theta_{\gamma^*} & 0 \\ \frac{1}{2} \sin \theta_{\gamma^*} & 0 & \cos \theta_{\gamma^*} \end{pmatrix} \begin{pmatrix} \langle \sin \phi \rangle_{UL}^q \\ \langle \sin(\phi - \phi_S) \rangle_{UT} \\ \langle \sin(\phi + \phi_S) \rangle_{UT} \end{pmatrix}$$

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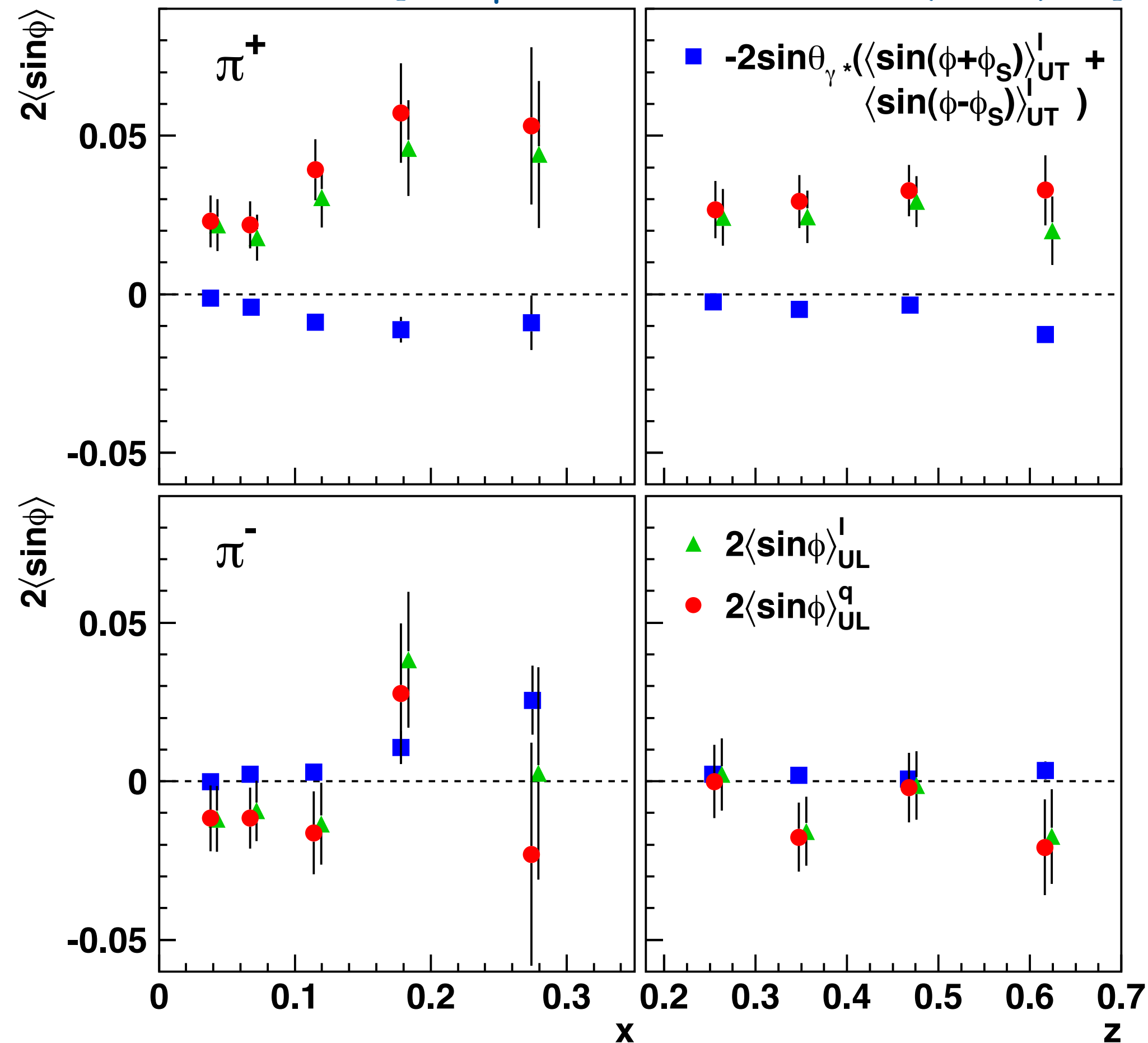
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➔ need data on same target for both polarization orientations!

subleading twist I - $\langle \sin(\phi) \rangle_{UL}$

$$\langle \sin \phi \rangle_{UL}^q = \langle \sin \phi \rangle_{UL}^I + \sin \theta_{\gamma^*} \left(\langle \sin(\phi + \phi_S) \rangle_{UT}^I + \langle \sin(\phi - \phi_S) \rangle_{UT}^I \right)$$

[Airapetian et al., PLB 622 (2005) 14]

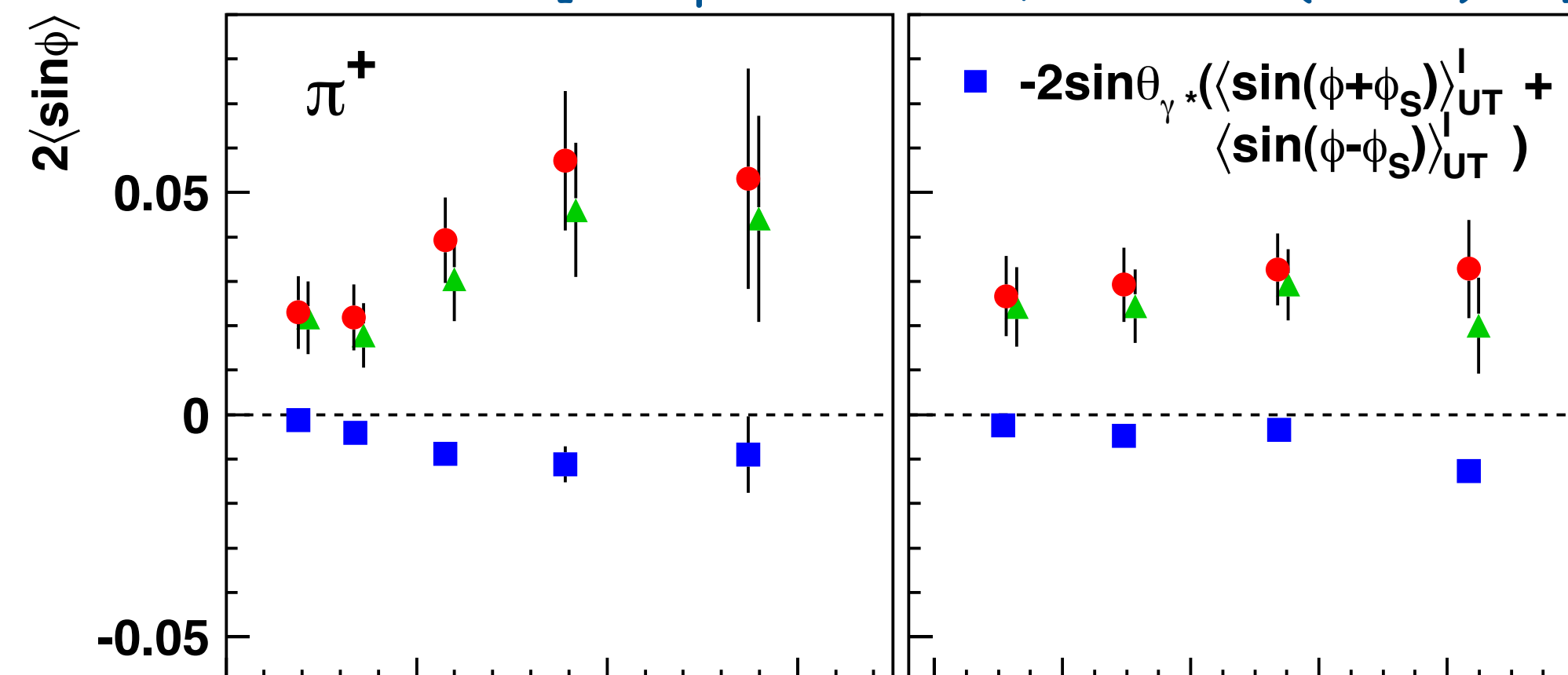


- experimental A_{UL} dominated by twist-3 contribution
- correction for A_{UT} contribution **increases** the longitudinal asymmetry for positive pions
- consistent with zero for π^-

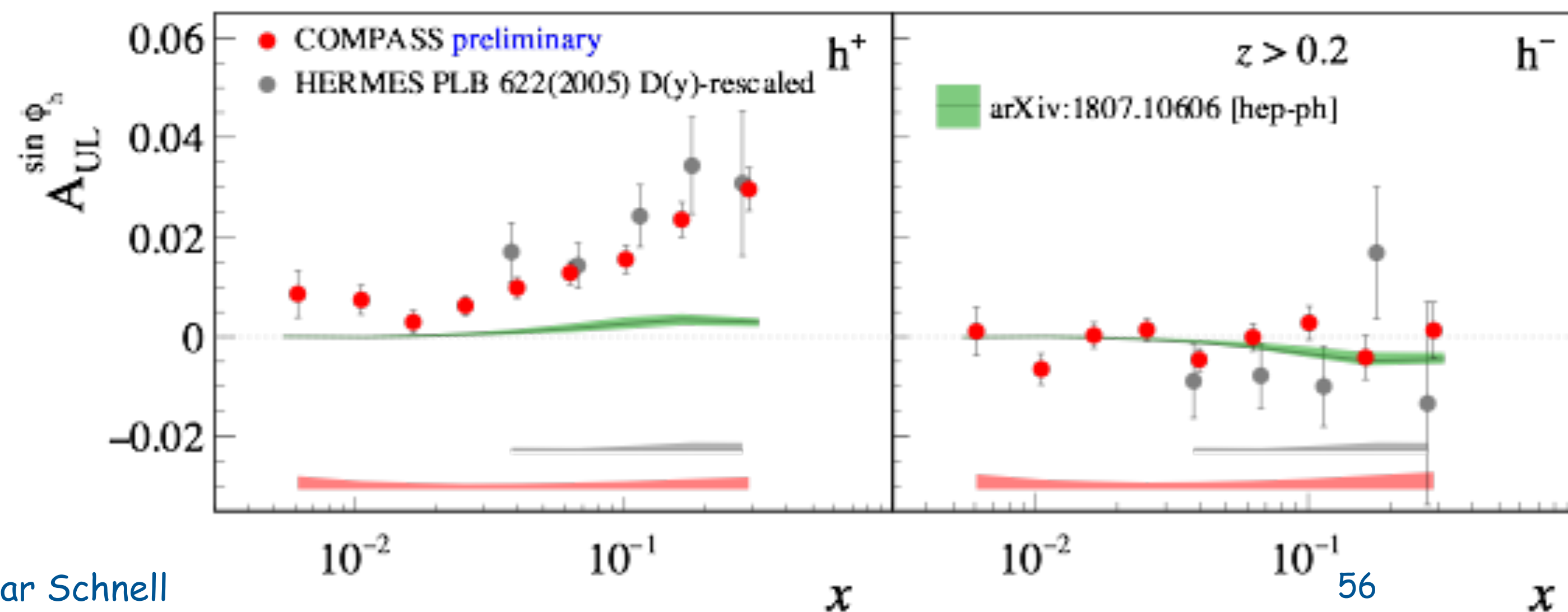
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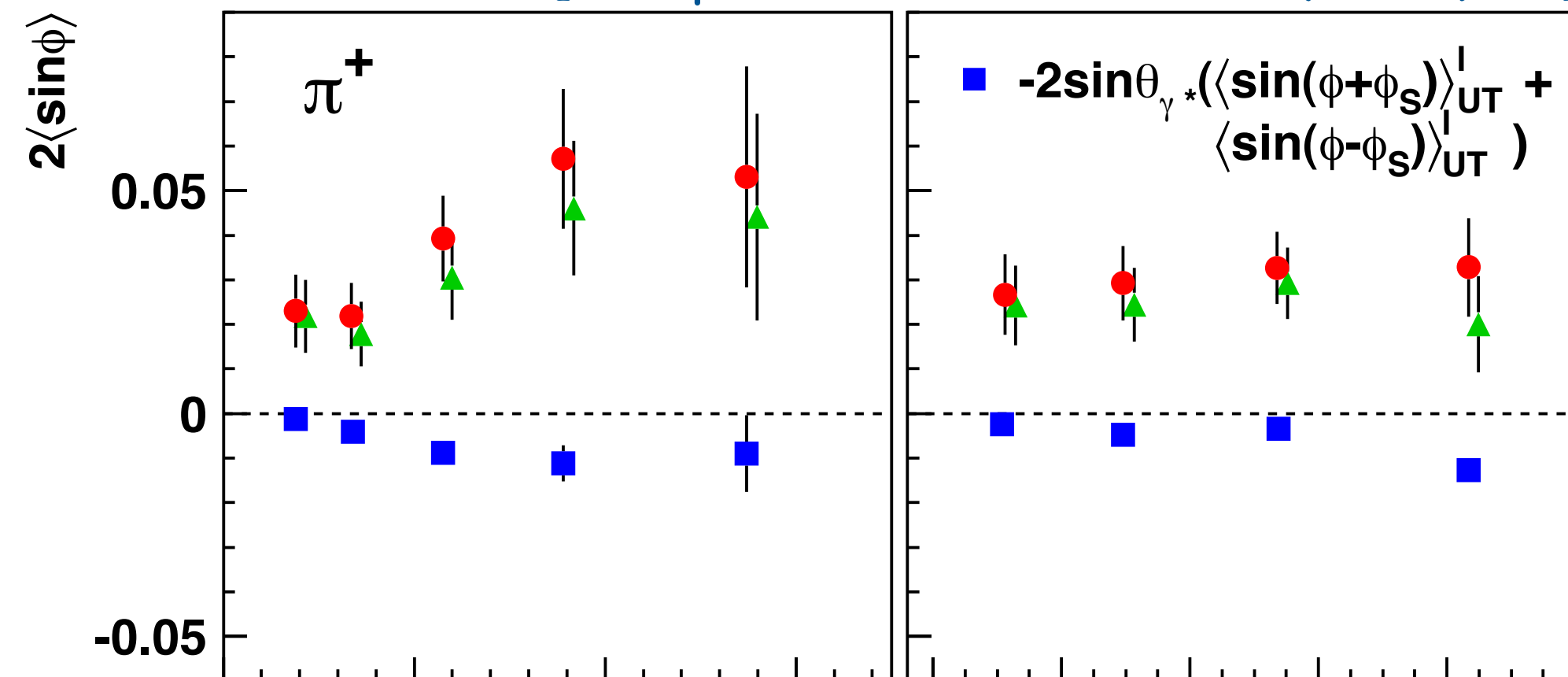
- experimental A_{UL} dominated by twist-3 contribution
- in contrast to WW-type approximation [1807.10606] (both COMPASS and HERMES data)



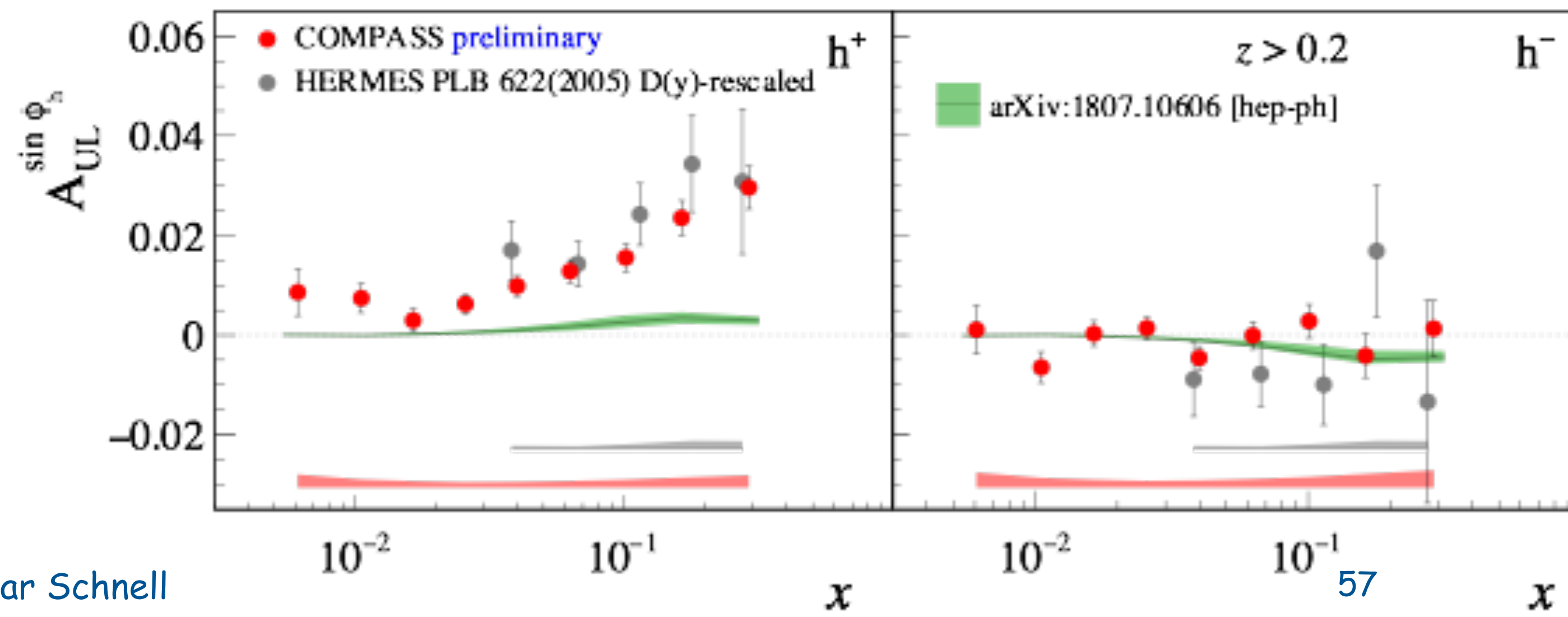
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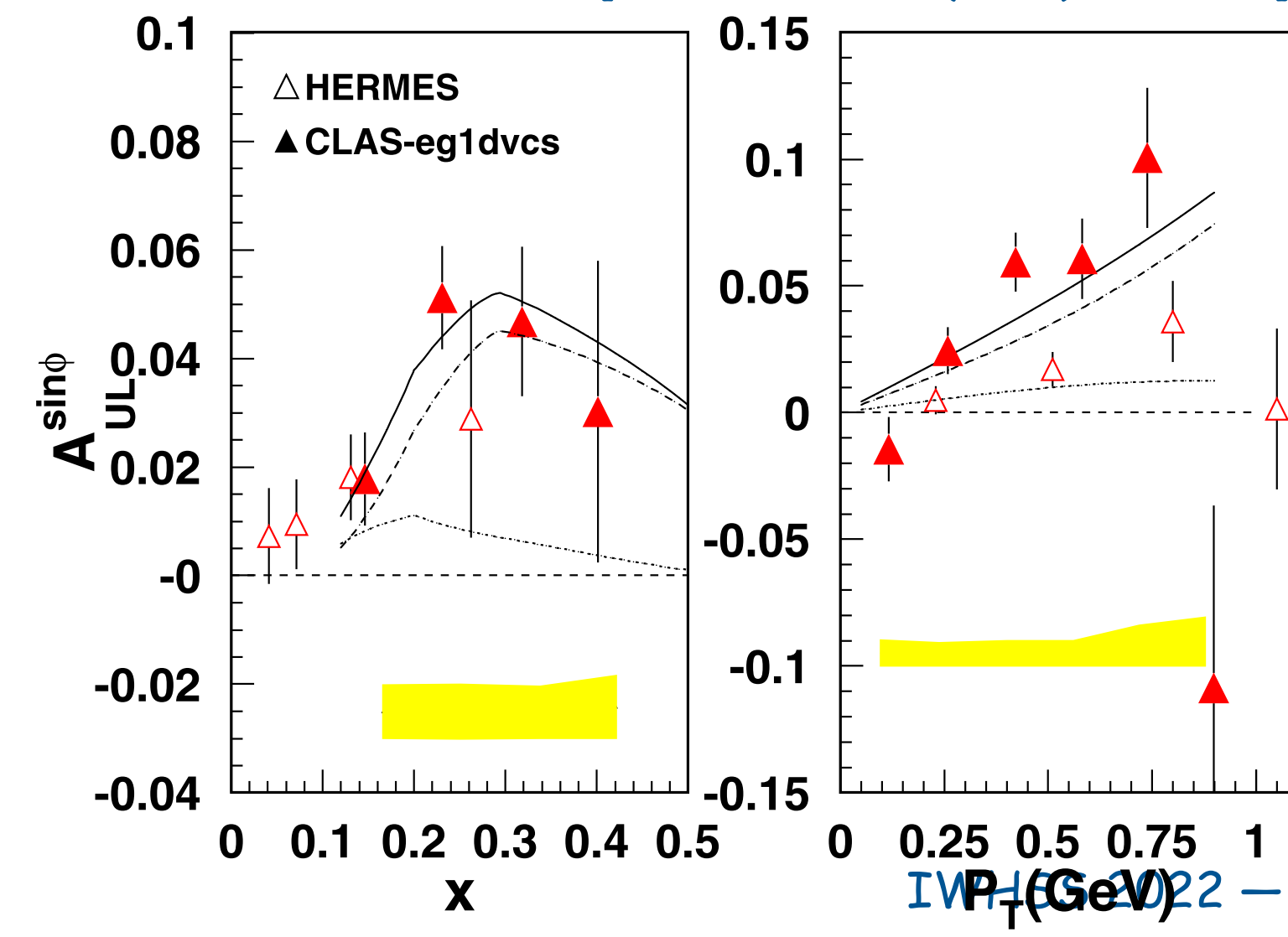
[Airapetian et al., PLB 622 (2005) 14]



- experimental A_{UL} dominated by twist-3 contribution
- in contrast to WW-type approximation [1807.10606] (for both COMPASS and HERMES data)
- sizable also for new CLAS neutral-pion data



[CLAS, PLB 782 (2018) 662-667]



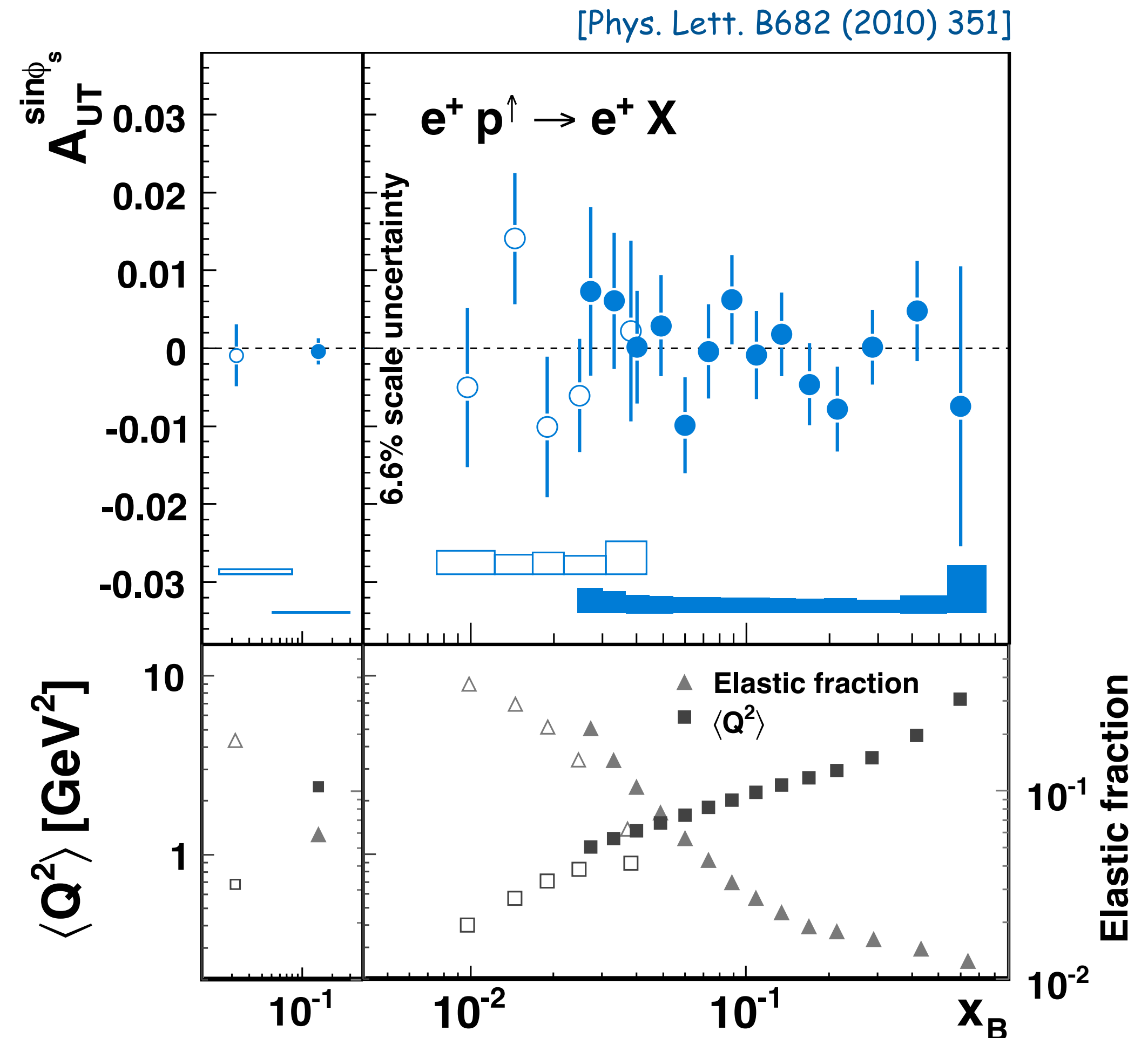
subleading twist II - $\langle \sin(\phi) \rangle_{LU}$

$$\frac{M_h}{M_z} h_1^\perp \tilde{E} \oplus x g^\perp D_1 \oplus \frac{M_h}{M_z} f_1 \tilde{G}^\perp \oplus x e H_1^\perp$$

- naive-T-odd Boer-Mulders (BM) function coupled to a twist-3 FF
 - signs of BM from unpolarized SIDIS
 - little known about interaction-dependent FF
- little known about naive-T-odd g^\perp ; singled out in A_{LU} in jet production
- large unpolarized f_1 , coupled to interaction-dependent FF
- twist-3 e survives integration over $P_{h\perp}$; here coupled to Collins FF
 - e linked to the pion-nucleon σ -term
 - interpreted as color force (from remnant) on transversely polarized quarks at the moment of being struck by virtual photon
- all terms vanish in WW-type approximation

subleading twist III - $\langle \sin(\phi_s) \rangle_{UT}$

- vanishes in inclusive limit, e.g. after integration over $P_{h\perp}$ and z , and summation over all hadrons
- tested to permille level at HERMES:



subleading twist III - $\langle \sin(\phi_S) \rangle_{UT}$

- vanishes in inclusive limit, e.g. after integration over $P_{h\perp}$ and z , and summation over all hadrons
- various contributing terms related to transversity, worm-gear, Sivers etc.:

$$\propto \left(\mathbf{x} \mathbf{f}_T^\perp \mathbf{D}_1 - \frac{M_h}{M} \mathbf{h}_1 \frac{\tilde{\mathbf{H}}}{z} \right) - \mathcal{W}(\mathbf{p}_T, \mathbf{k}_T, \mathbf{P}_{h\perp}) \left[\left(\mathbf{x} \mathbf{h}_T \mathbf{H}_1^\perp + \frac{M_h}{M} \mathbf{g}_{1T} \frac{\tilde{\mathbf{G}}^\perp}{z} \right) - \left(\mathbf{x} \mathbf{h}_T^\perp \mathbf{H}_1^\perp - \frac{M_h}{M} \mathbf{f}_{1T}^\perp \frac{\tilde{\mathbf{D}}^\perp}{z} \right) \right]$$

- non-vanishing collinear limit:

$$F_{UT}^{\sin(\phi_S)}(x, Q^2, z) = \int d^2 \mathbf{P}_{h\perp} F_{UT}^{\sin(\phi_S)}(x, Q^2, z, P_{h\perp}) = -x \frac{2M_h}{Q} \sum_q e_q^2 h_1^q \frac{\tilde{H}^q(z)}{z}$$

subleading twist III - $\langle \sin(\phi_S) \rangle_{UT}$

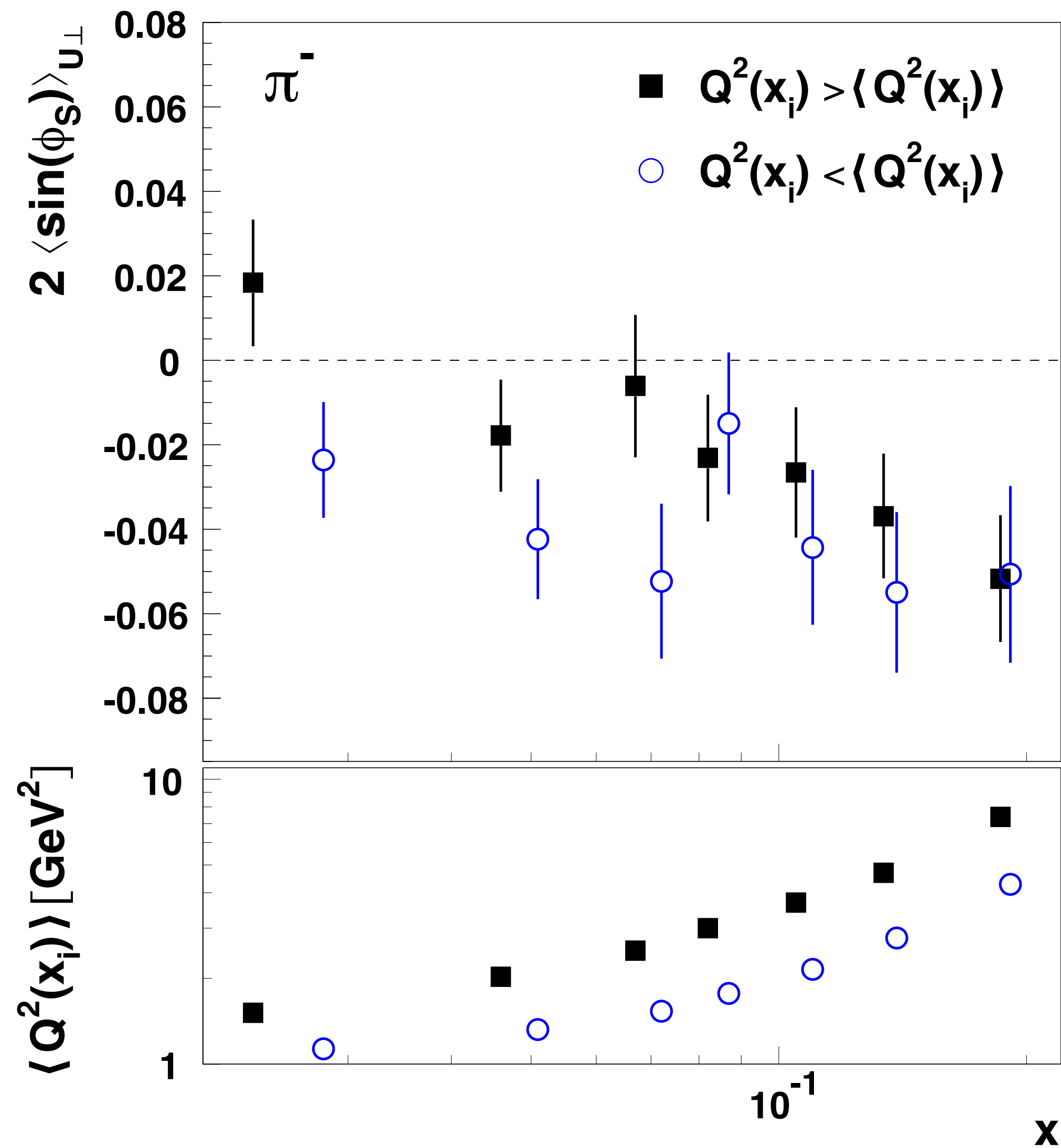
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subleading twist III - $\langle \sin(\phi_s) \rangle_{UT}$

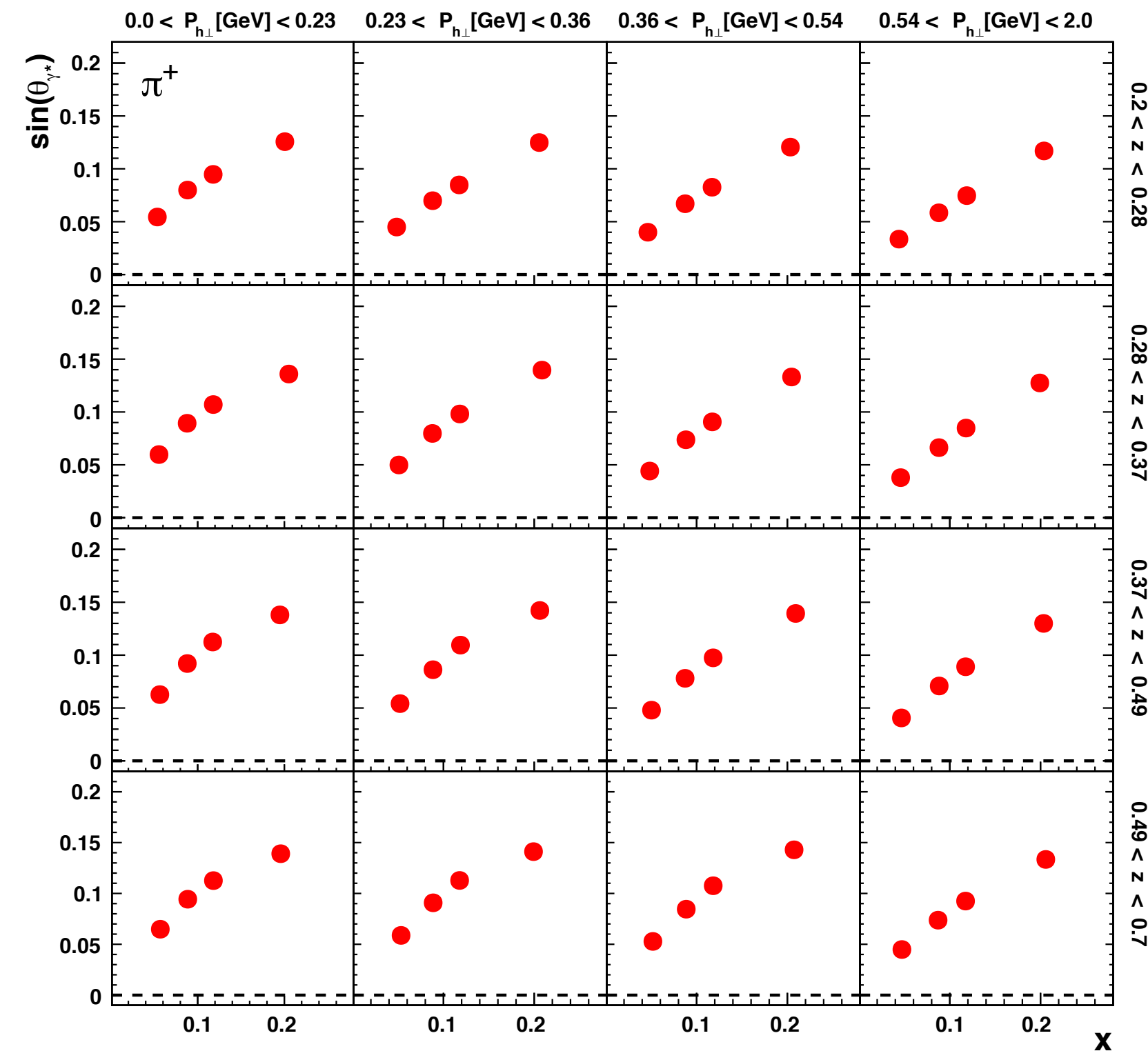
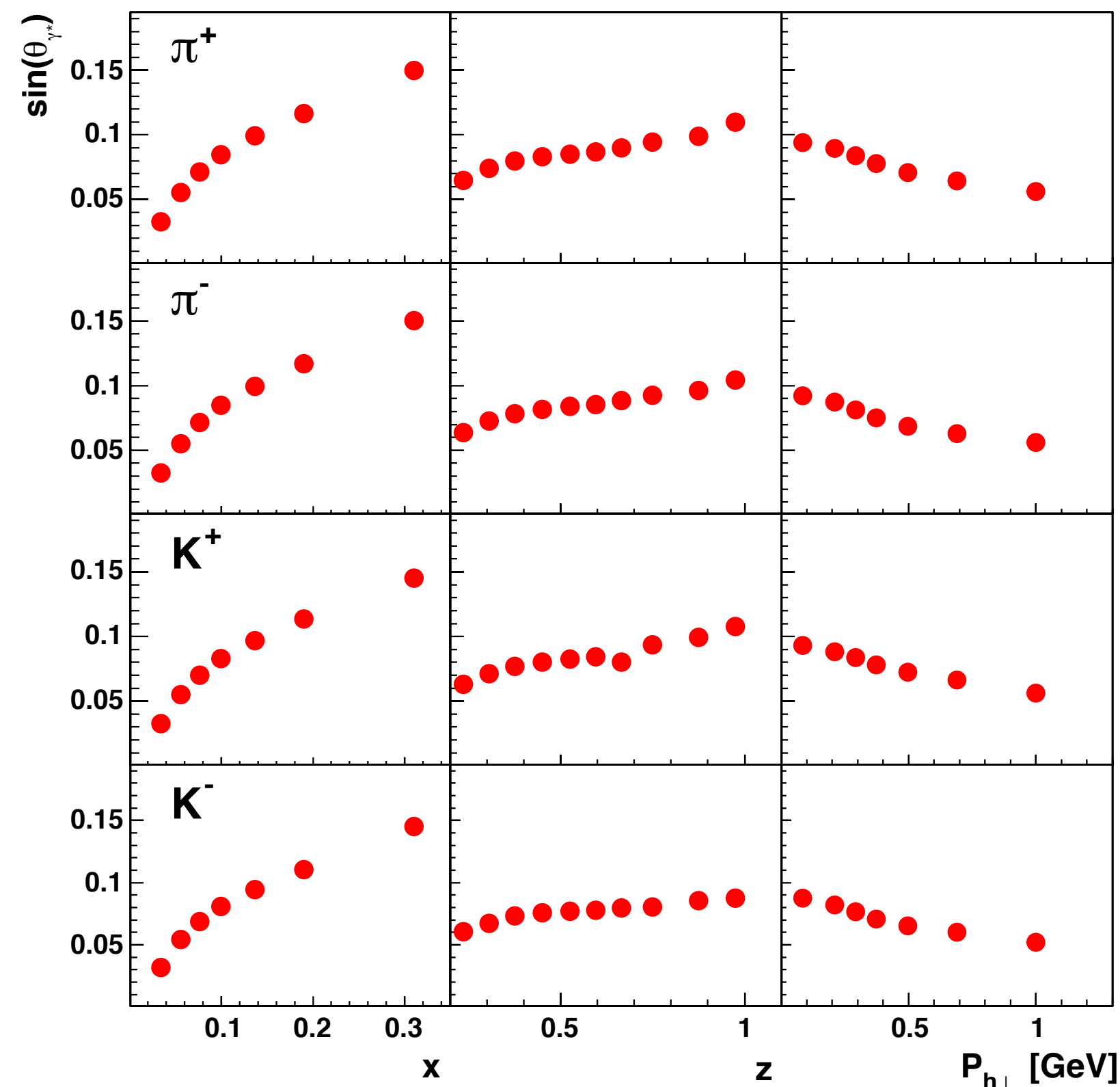
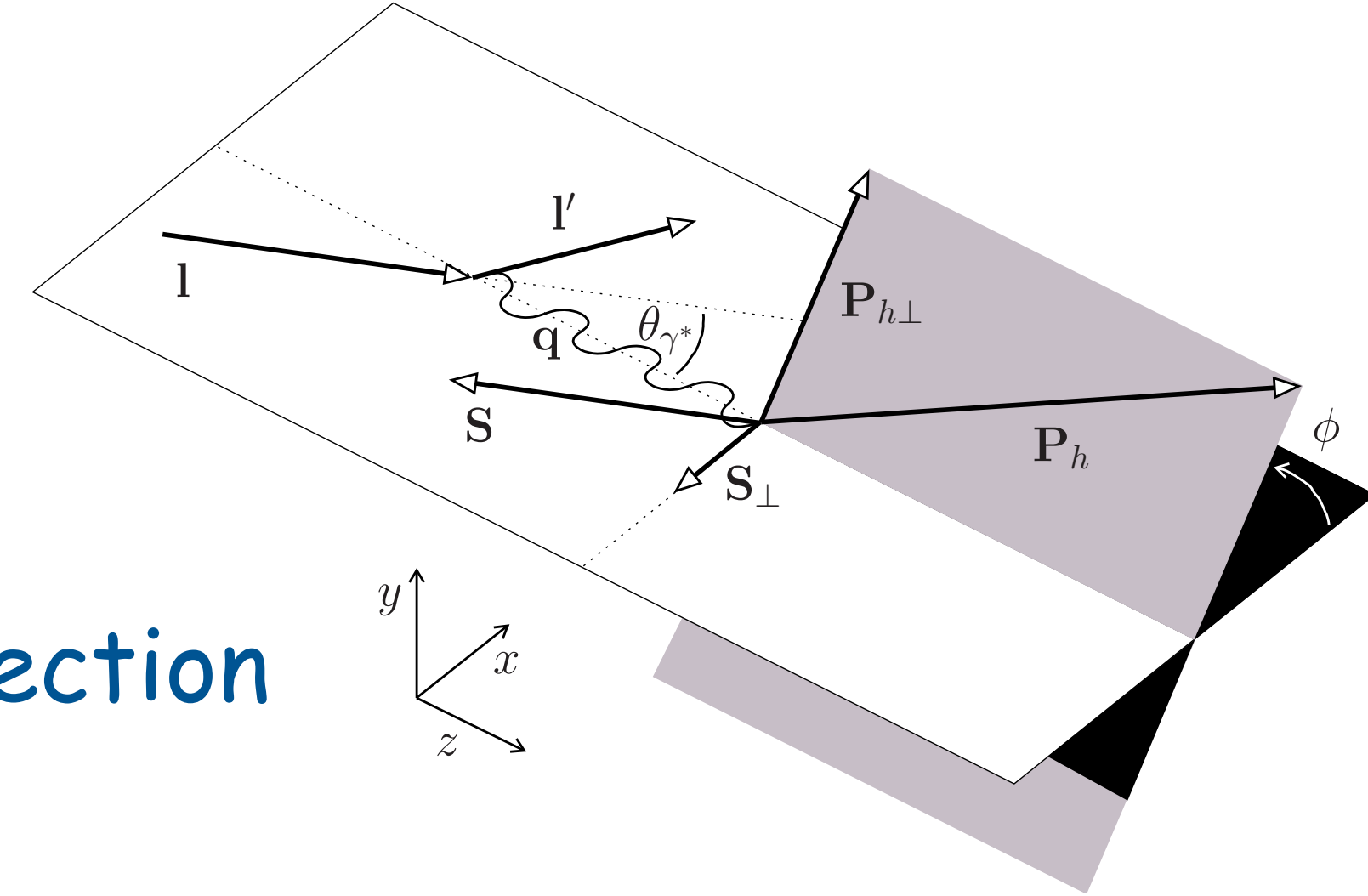


● hint of Q^2 dependence seen in signal for negative pions

devil in the details &
lessons learnt on the way

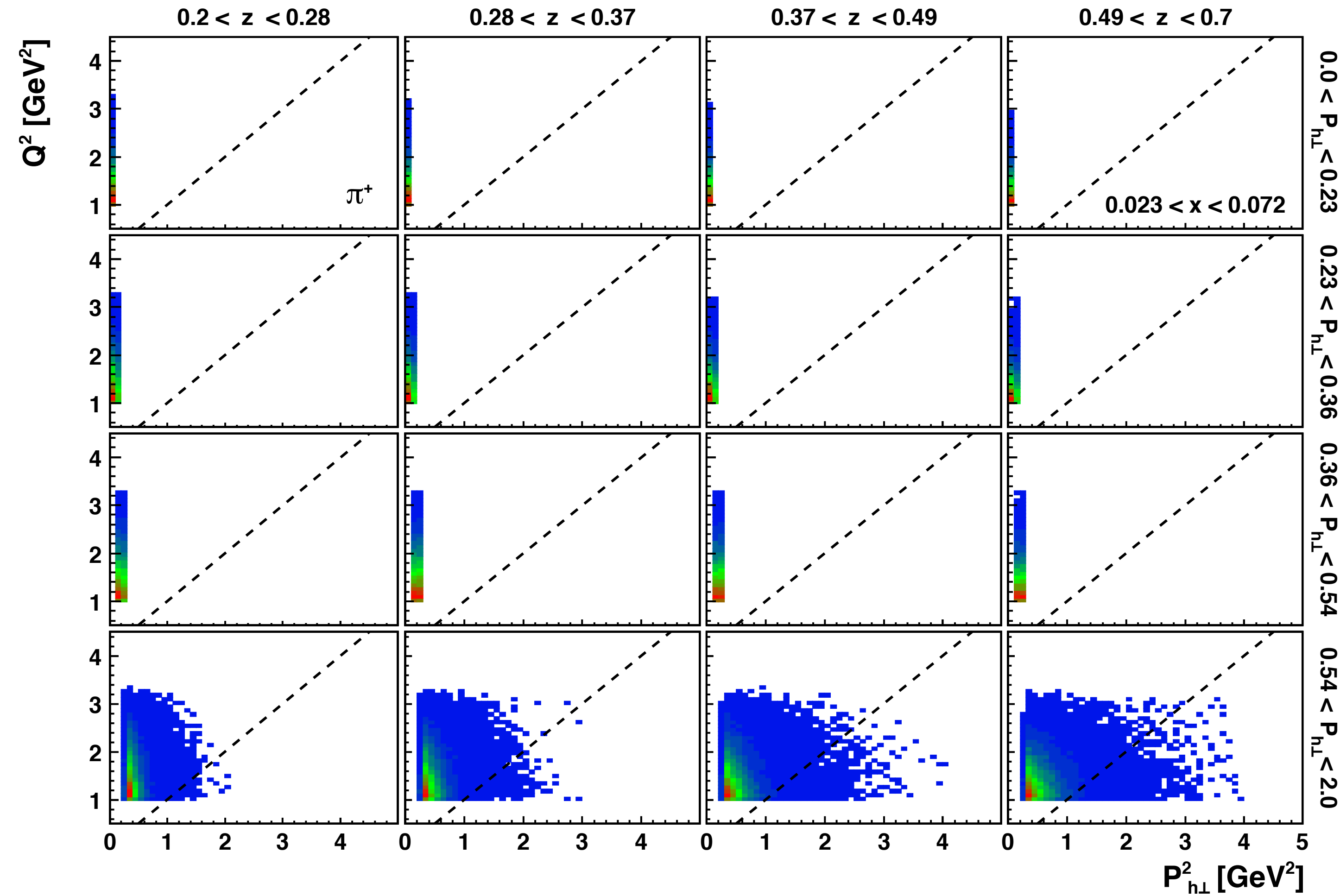
mixing of target polarizations

- theory done w.r.t. virtual-photon direction
 - experiments use targets polarized w.r.t. lepton-beam direction
- ➔ mixing of longitudinal and transverse polarization effects



TMD factorization: a 2-scale problem

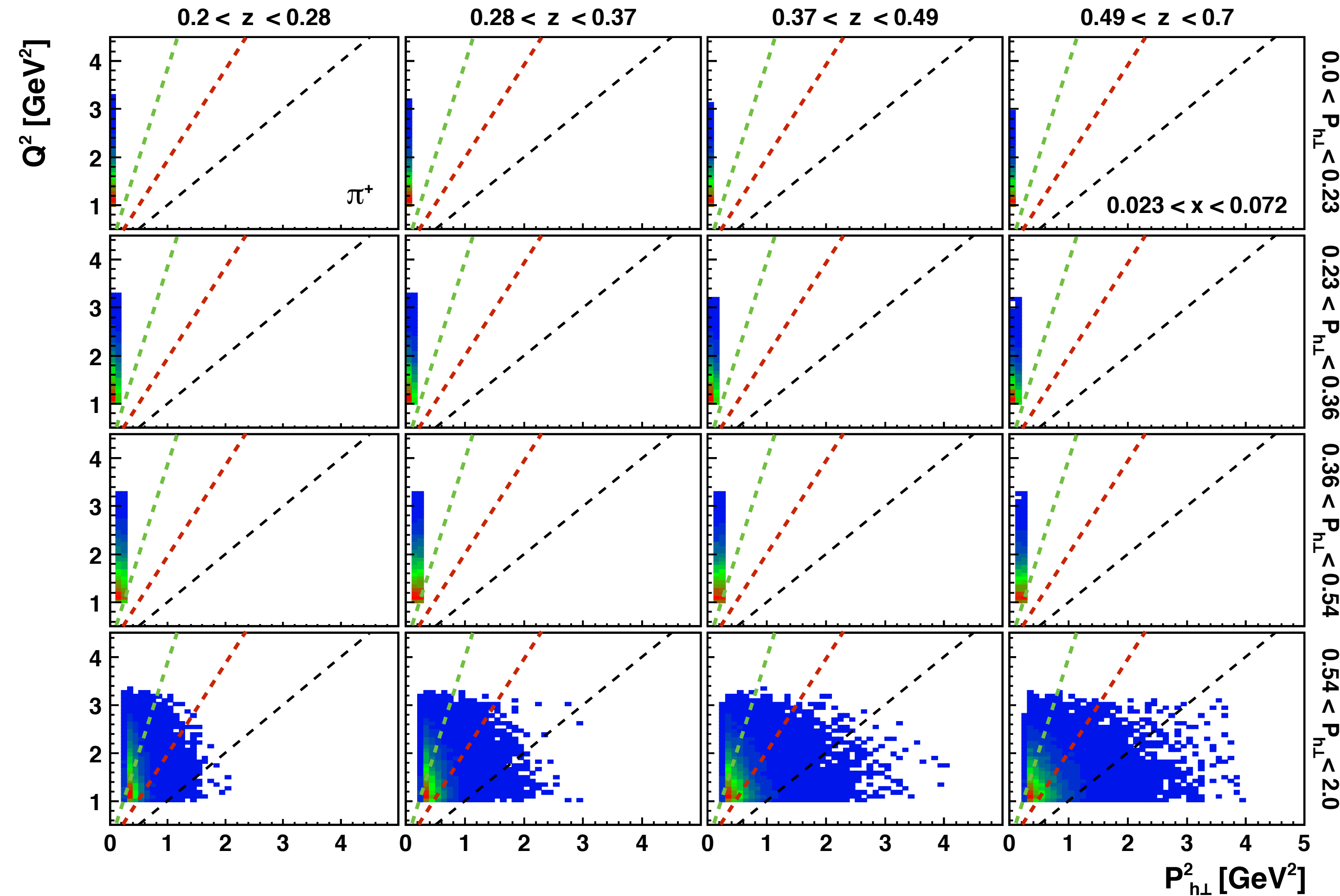
lowest x bin



--- $Q^2 = P_{h\perp}^2$

TMD factorization: a 2-scale problem

lowest x bin



--- $Q^2 = P_{h\perp}^2$

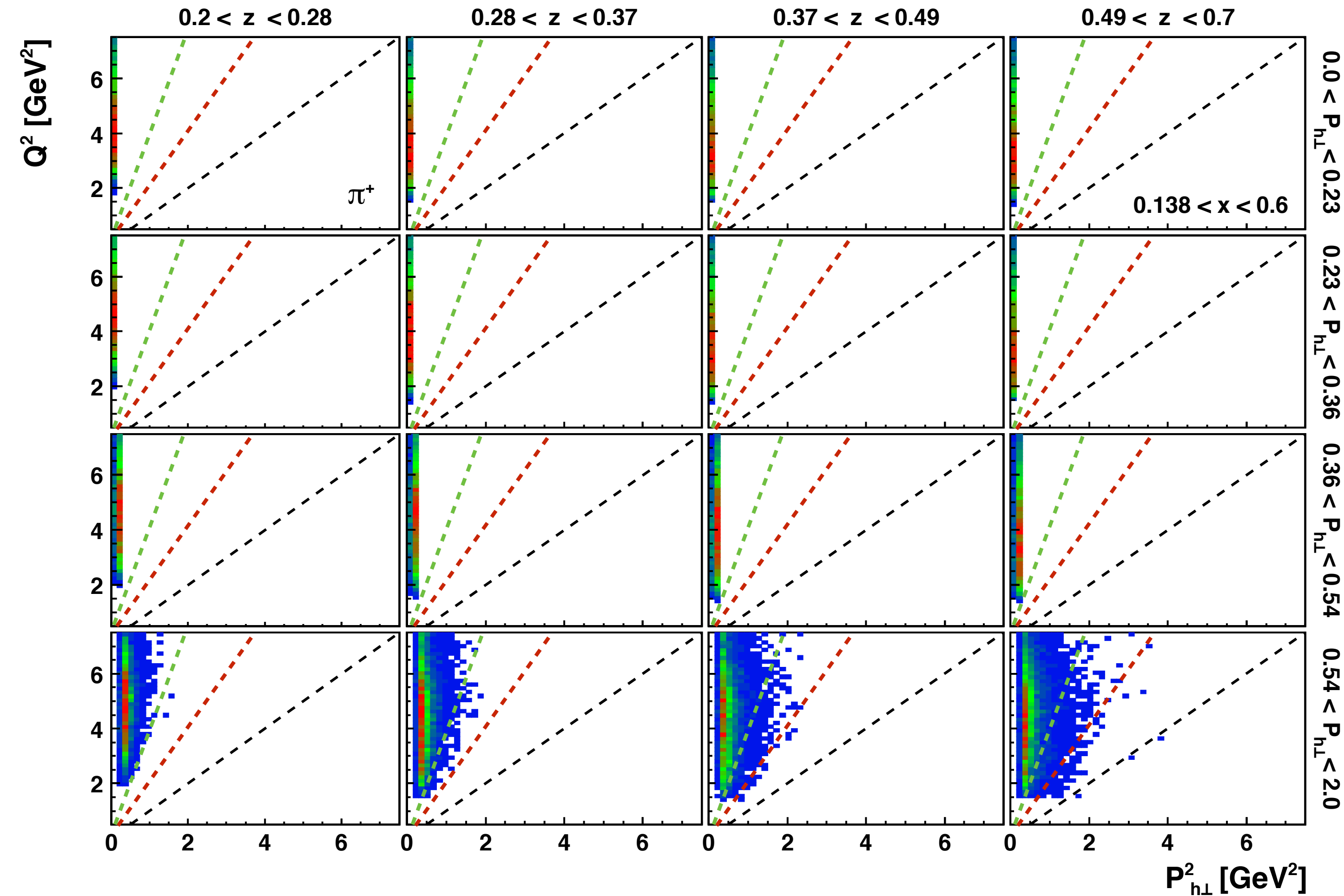
--- $Q^2 = 2 P_{h\perp}^2$

--- $Q^2 = 4 P_{h\perp}^2$

disclaimer: coloured lines drawn by hand

TMD factorization: a 2-scale problem

highest x bin



--- $Q^2 = P_{h\perp}^2$

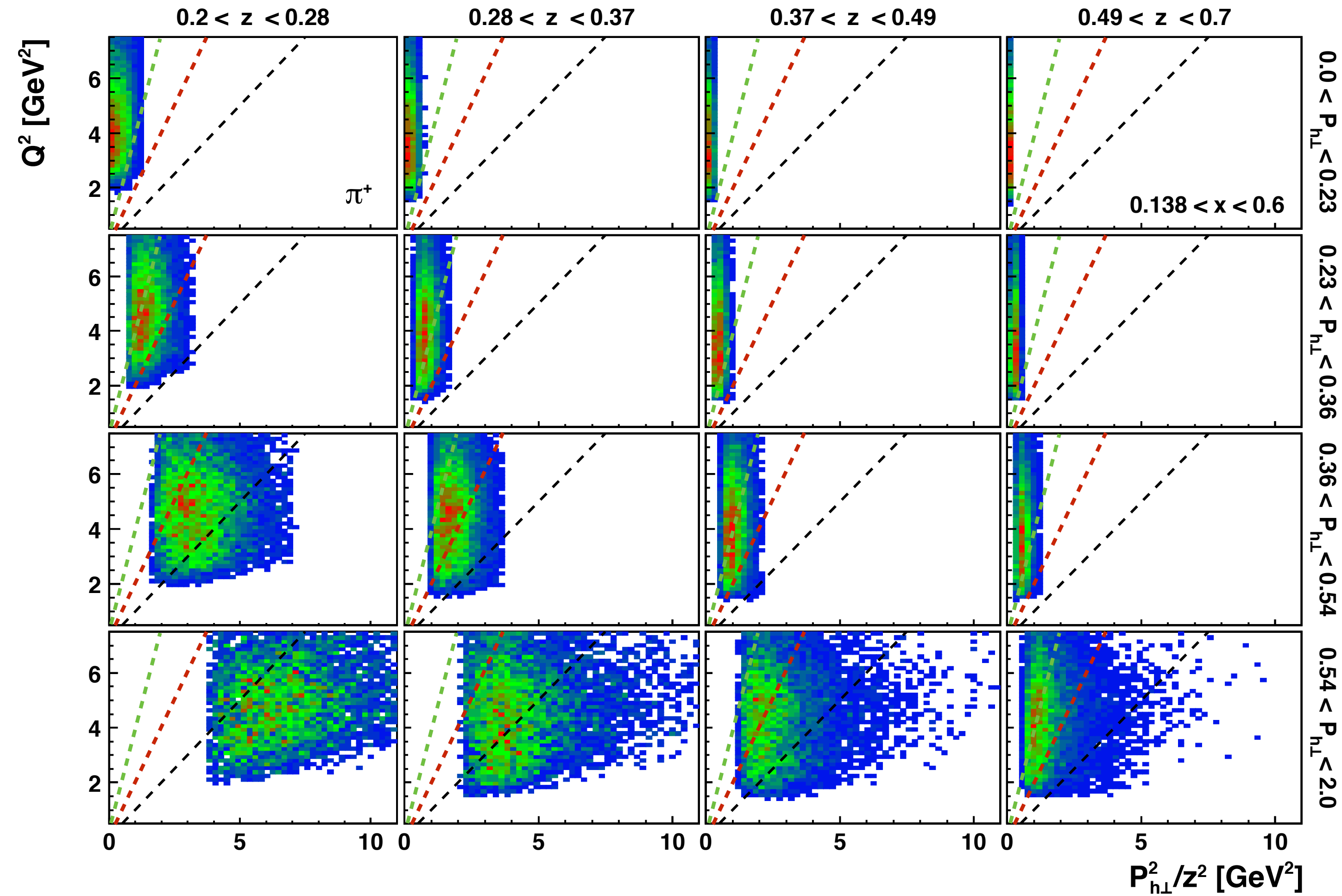
--- $Q^2 = 2 P_{h\perp}^2$

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disclaimer: coloured lines drawn by hand

TMD factorization: a 2-scale problem

highest x bin



--- $Q^2 = P_{h\perp}^2/z^2$

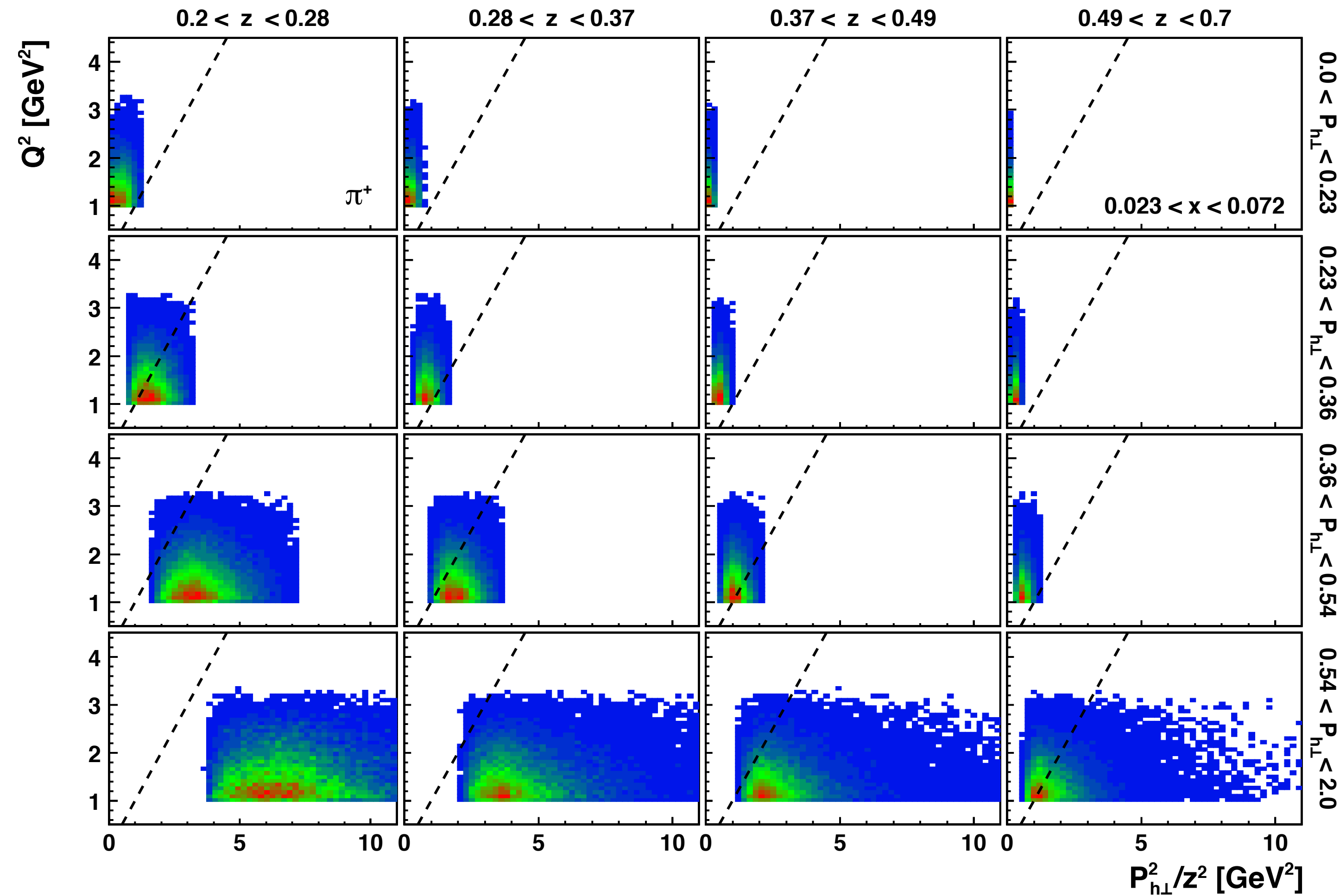
--- $Q^2 = 2 P_{h\perp}^2/z^2$

--- $Q^2 = 4 P_{h\perp}^2/z^2$

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TMD factorization: a 2-scale problem

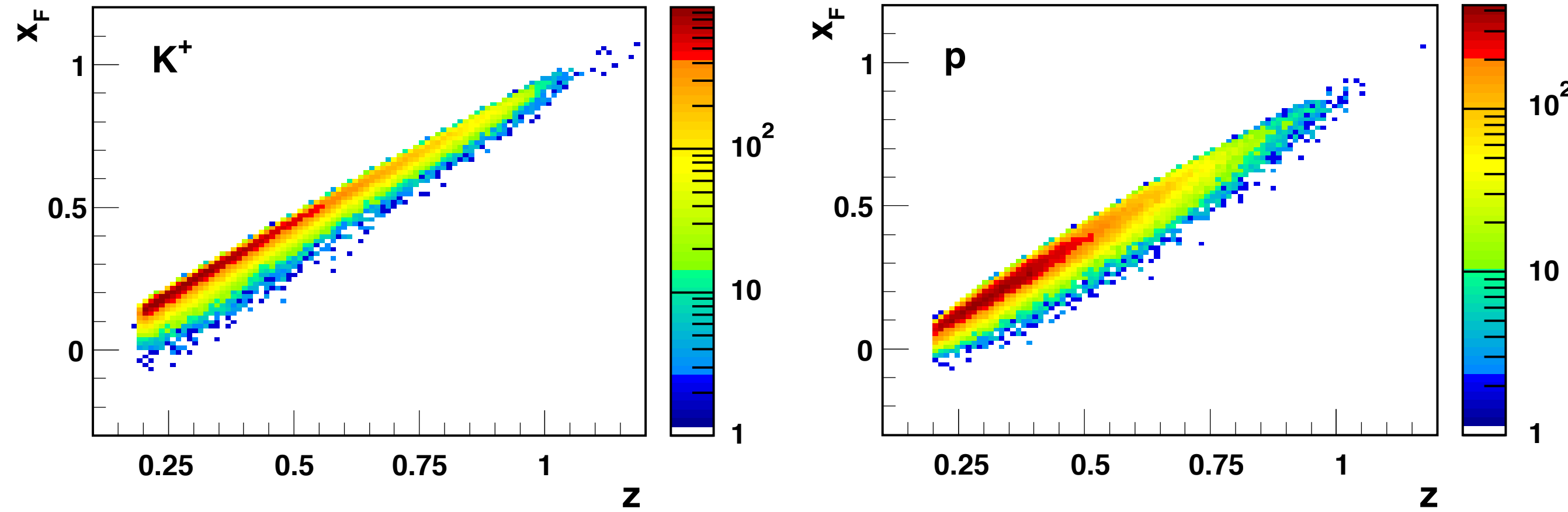
lowest x bin



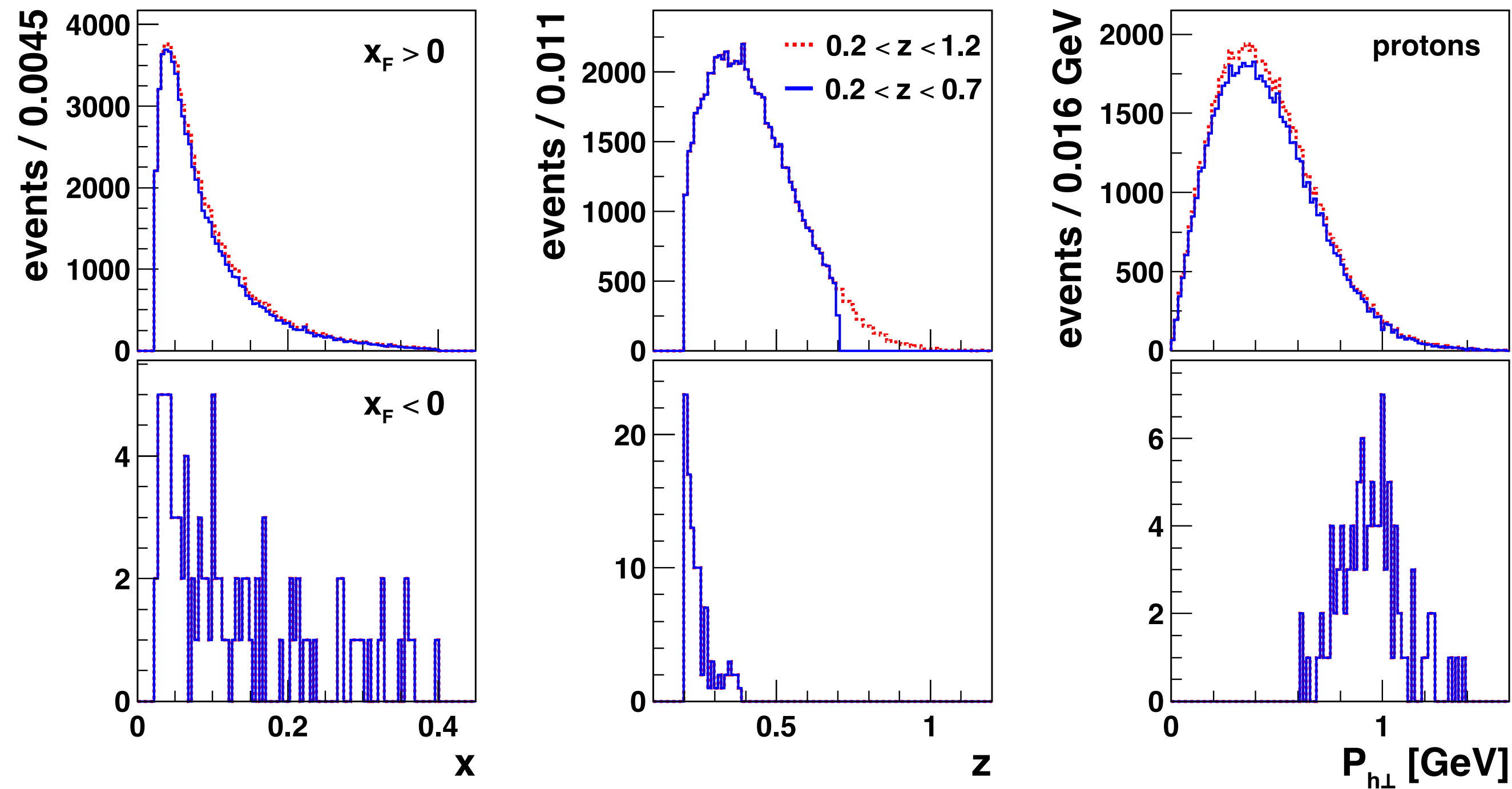
--- $Q^2 = P_{h\perp}^2/z^2$

all other x-bins included in the
Supplemental Material of
JHEP12(2020)010

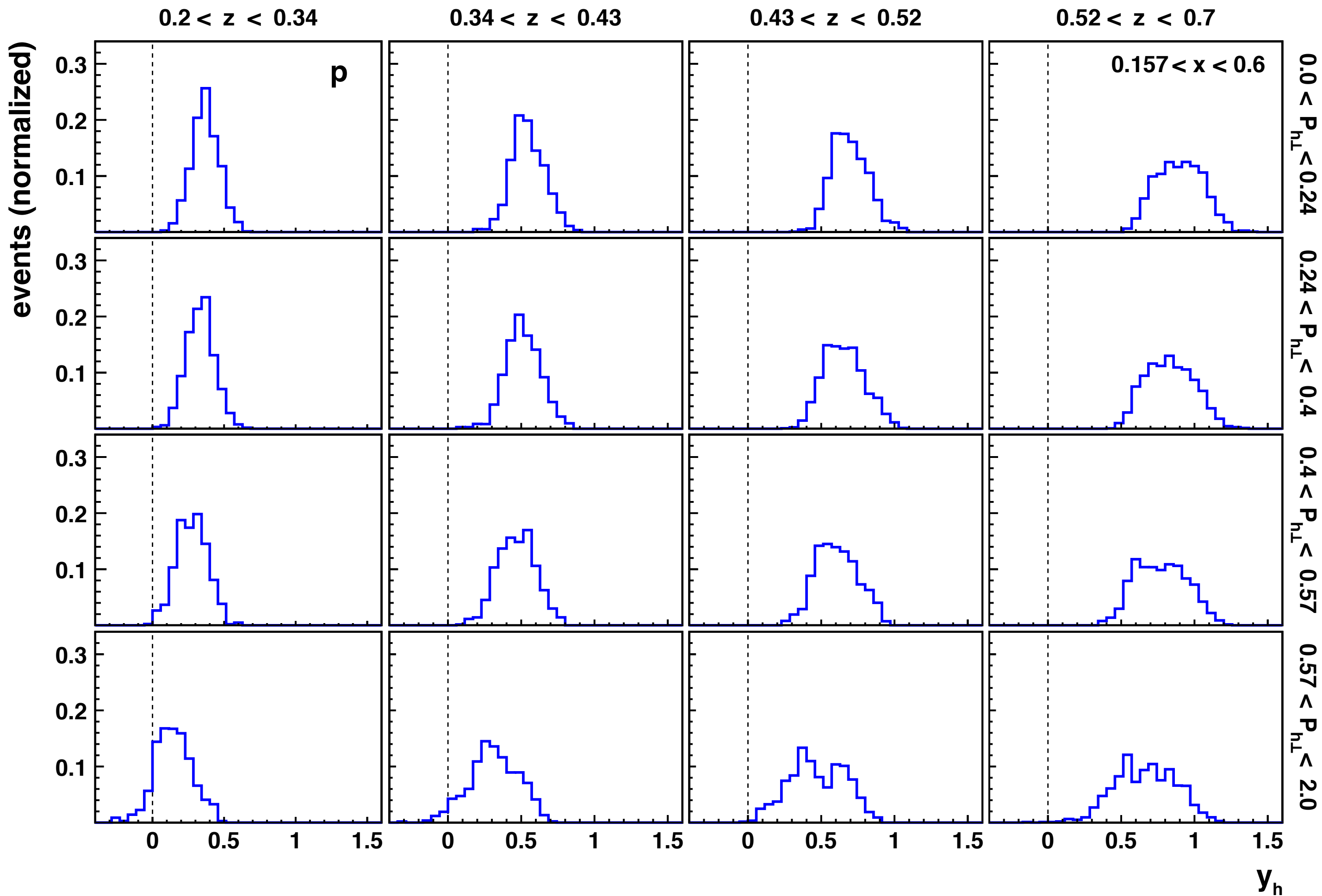
hadron production at HERMES



- forward-acceptance favors current fragmentation
- backward rapidity populates large- $P_{h\perp}$ region [as expected]



hadron production at HERMES

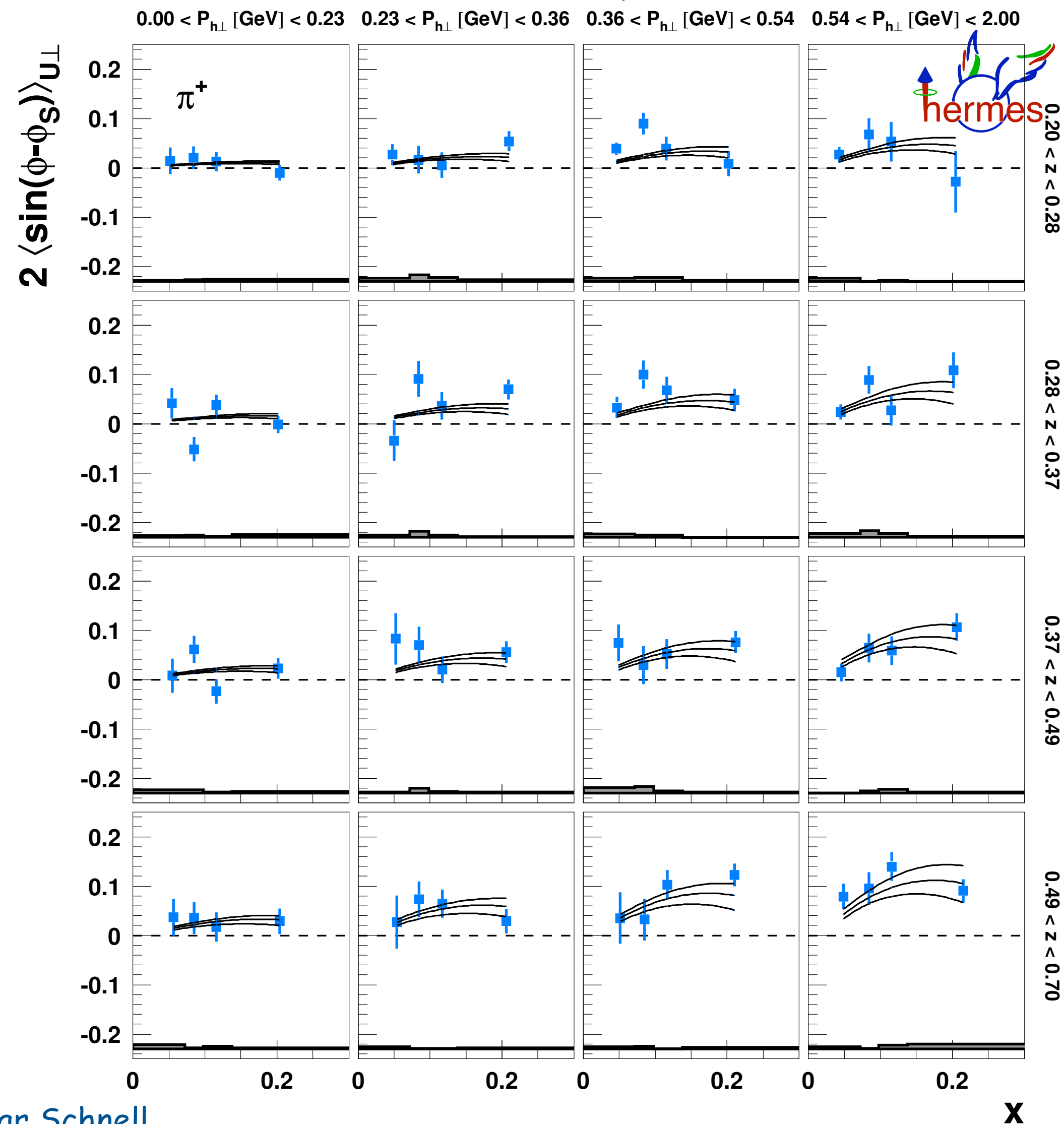


- forward-acceptance favors current fragmentation
- backward rapidity populates large- $P_{h\perp}$ region [as expected]
- rapidity distributions available for all kinematic bins (e.g., highest-x bin protons)

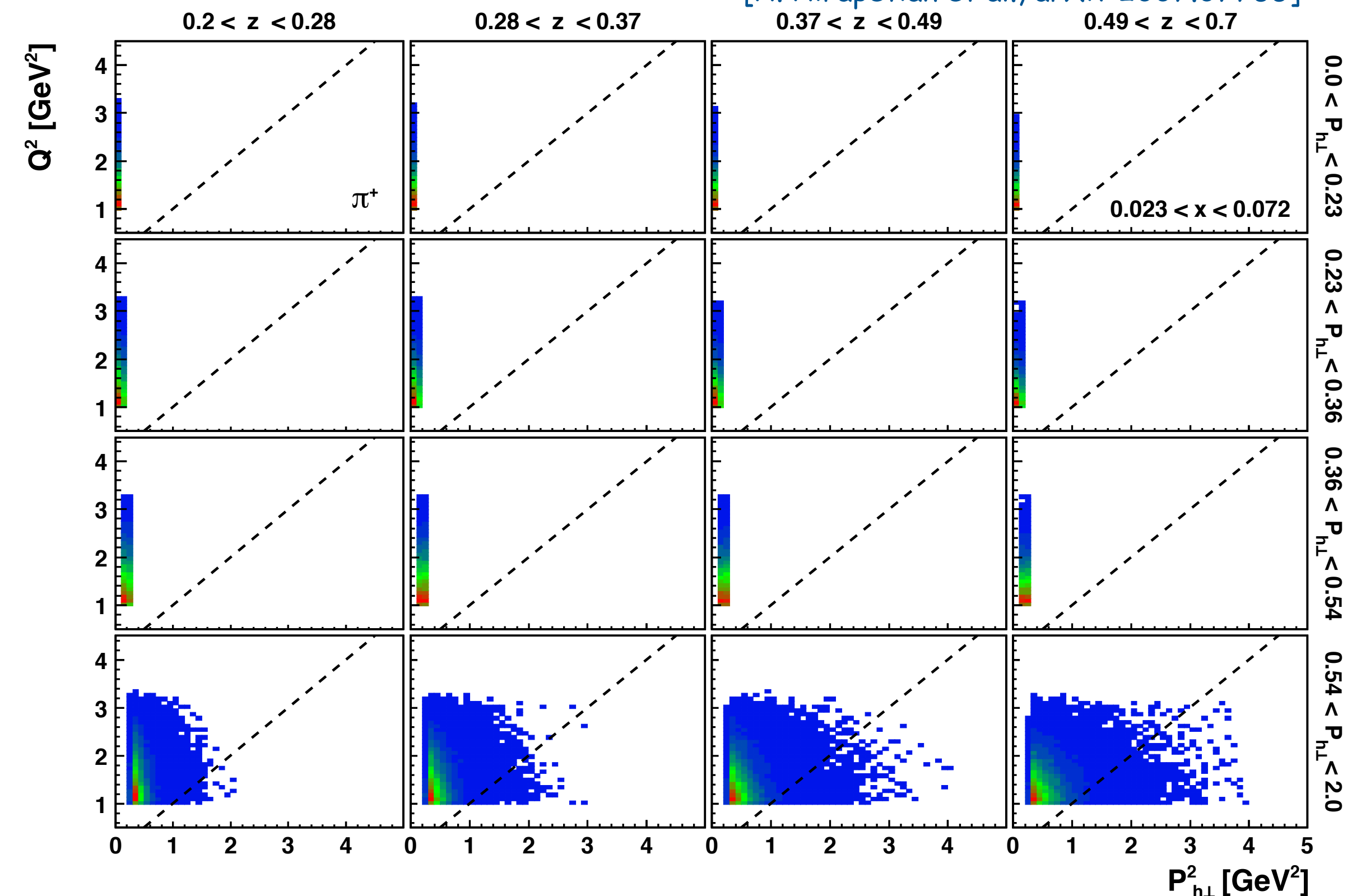
	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

Sivers amplitudes multi-dimensional analysis

[A. Airapetian et al., arXiv:2007.07755]



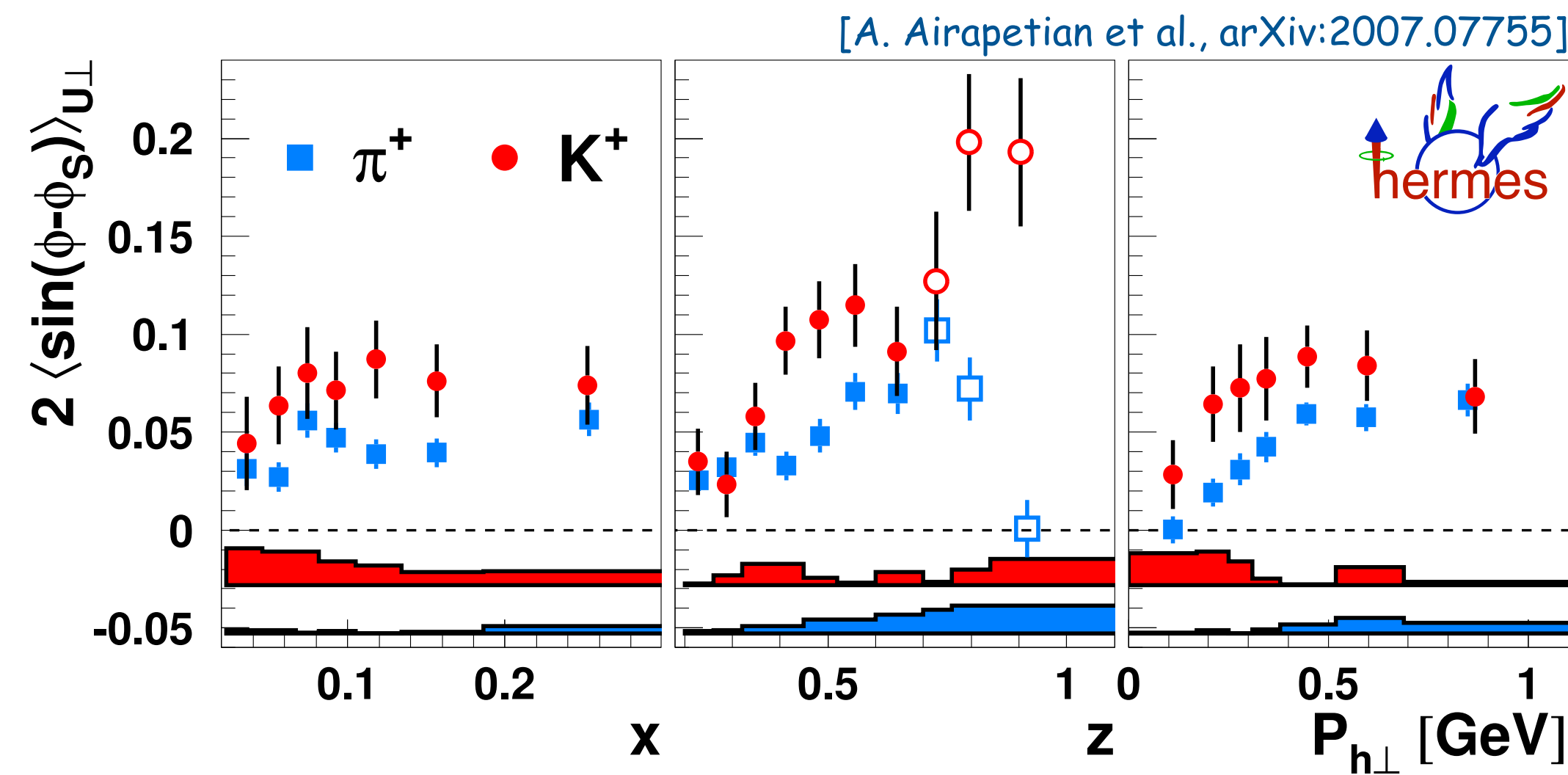
[A. Airapetian et al., arXiv:2007.07755]



multi-d dependence and kinematical distribution
should facilitate analyses within TMD formalism

Sivers amplitudes pions vs. kaons

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp



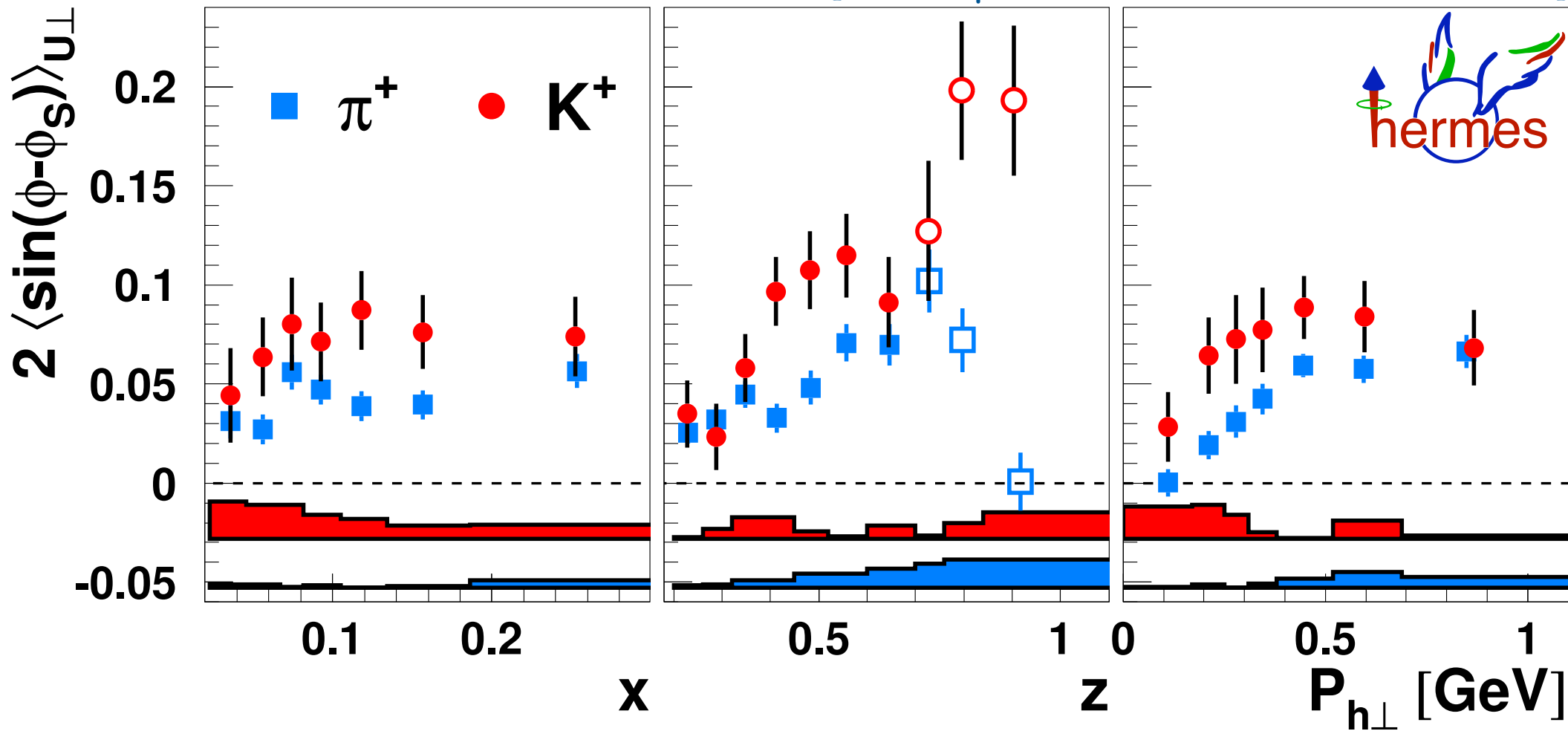
somewhat unexpected if dominated
by scattering from u-quarks:

$$\simeq - \frac{f_{1T}^{\perp,u}(x, p_T^2) \otimes_{\mathcal{W}} D_1^{u \rightarrow \pi^+/K^+}(z, k_T^2)}{f_1^u(x, p_T^2) \otimes D_1^{u \rightarrow \pi^+/K^+}(z, k_T^2)}$$

Sivers amplitudes pions vs. kaons

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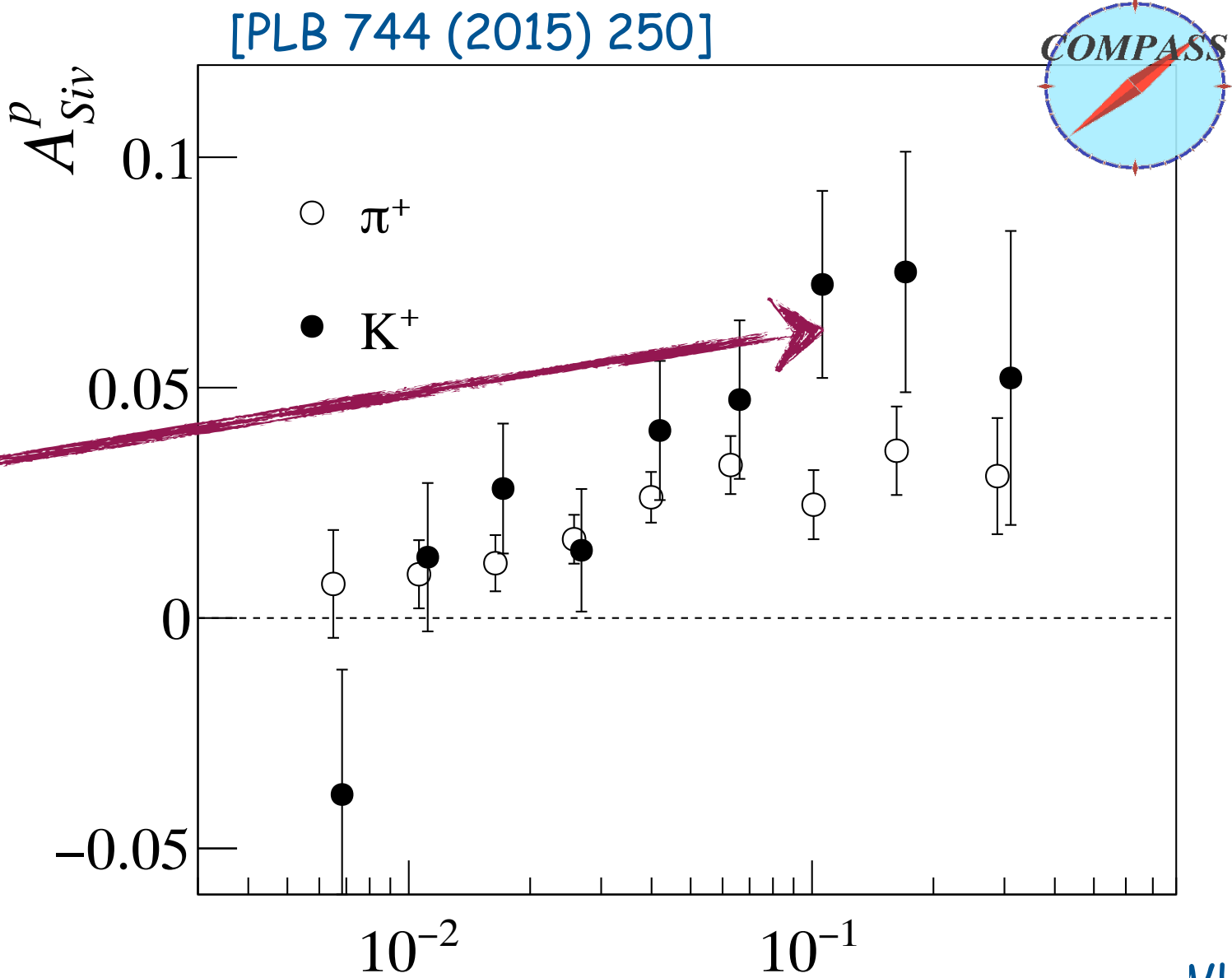
[A. Airapetian et al., arXiv:2007.07755]



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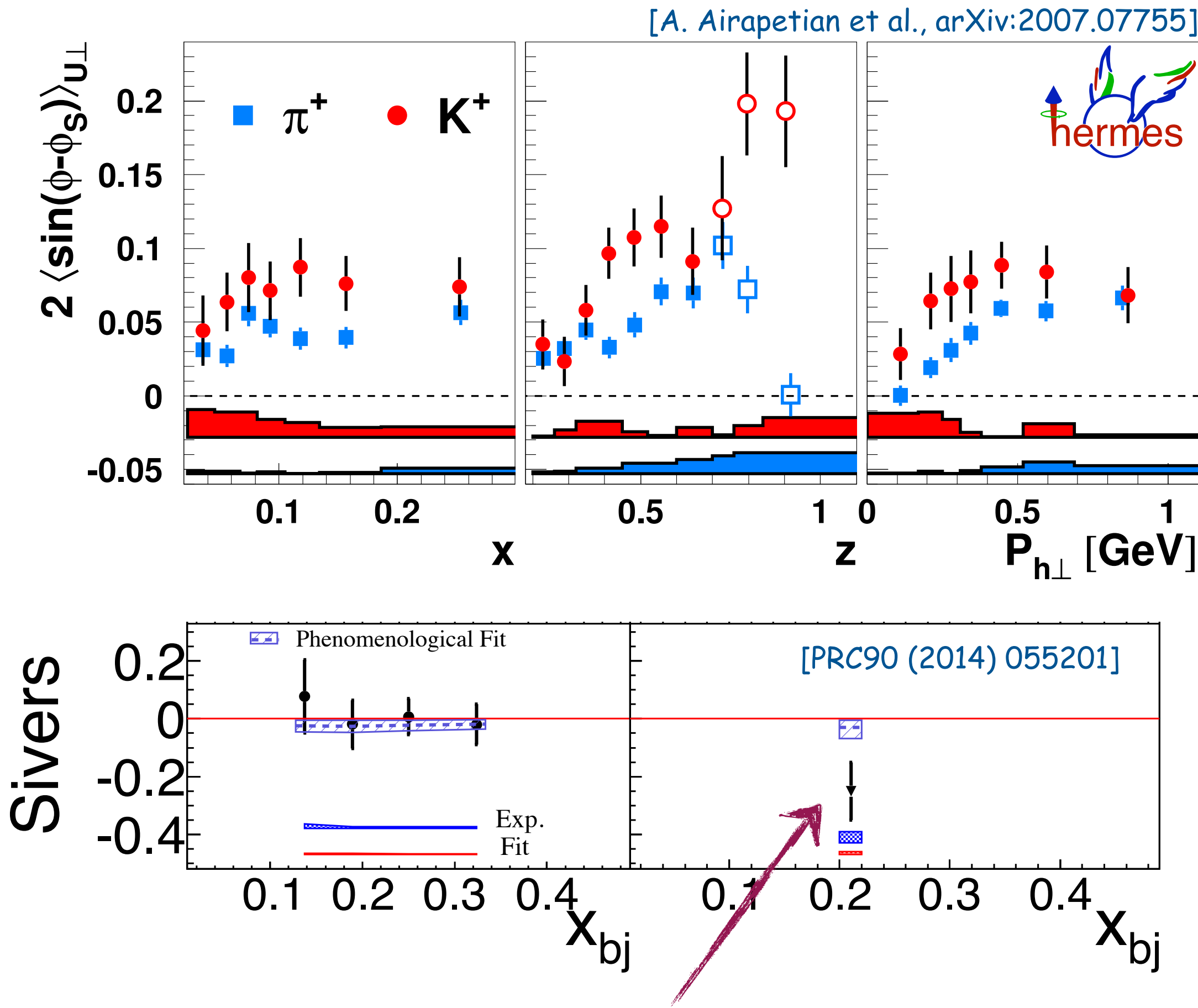
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larger amplitudes seen also by COMPASS



Sivers amplitudes pions vs. kaons

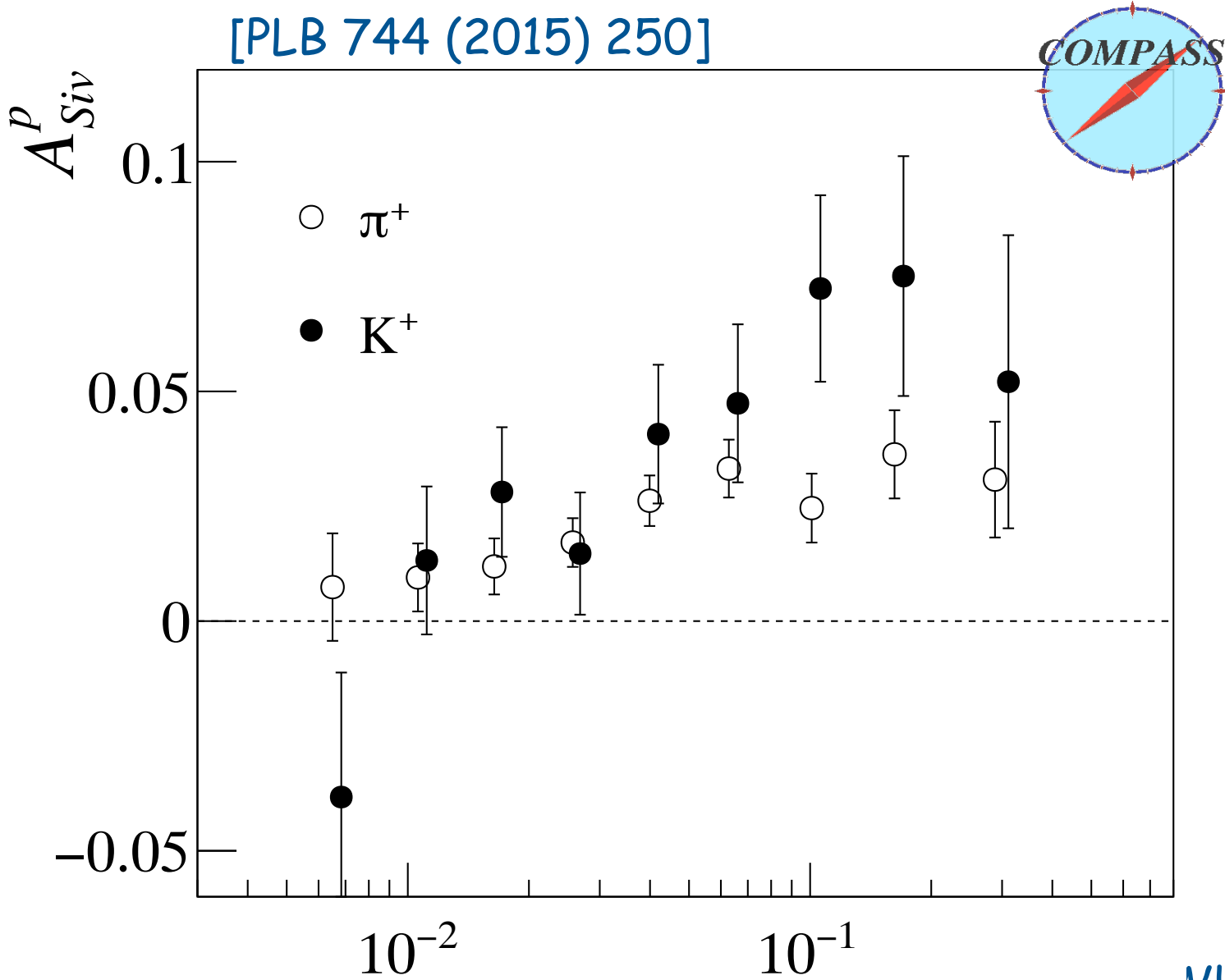
	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp



surprisingly large K- asymmetry for ^3He target
(but zero for K^+ ?!)

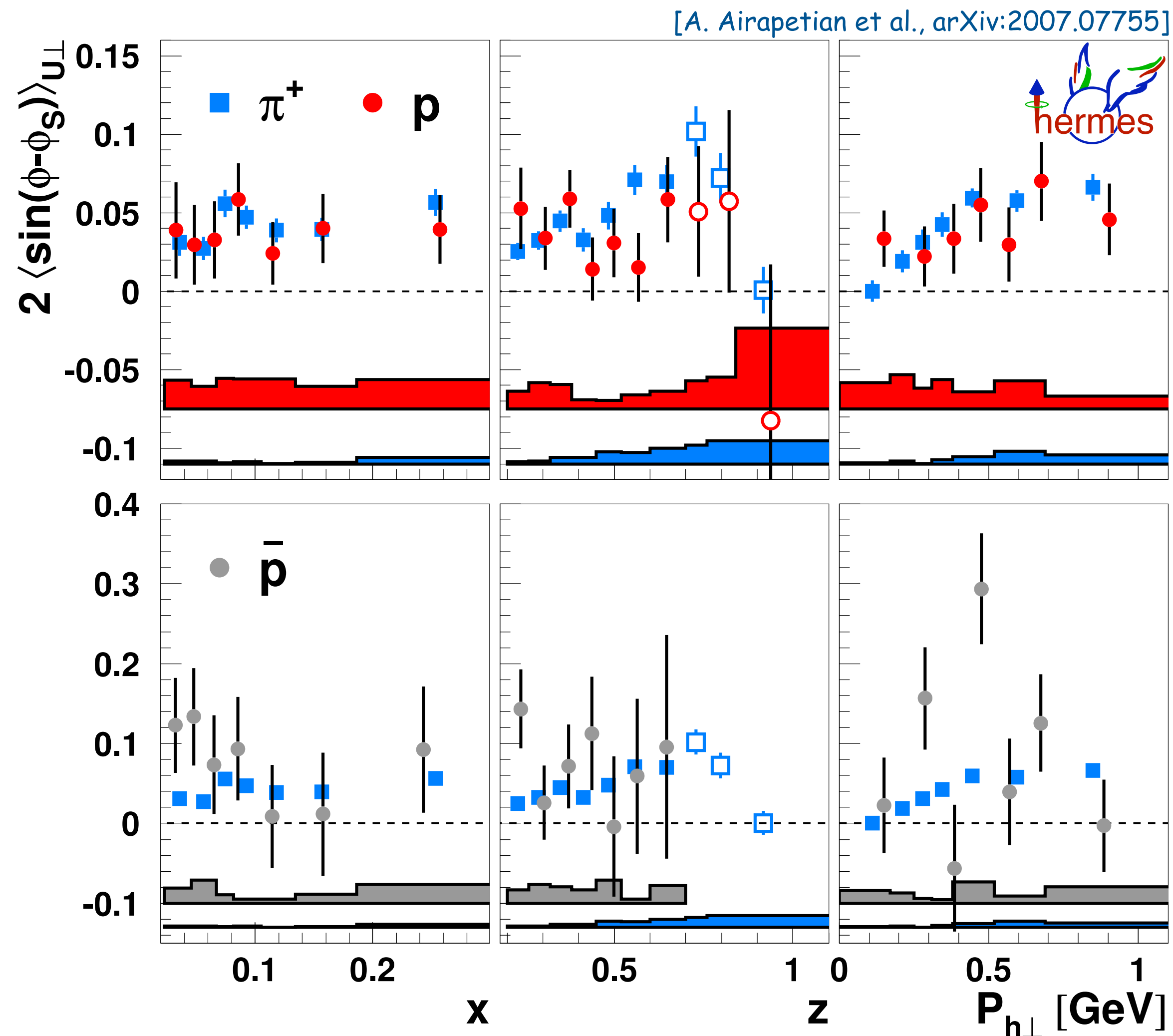
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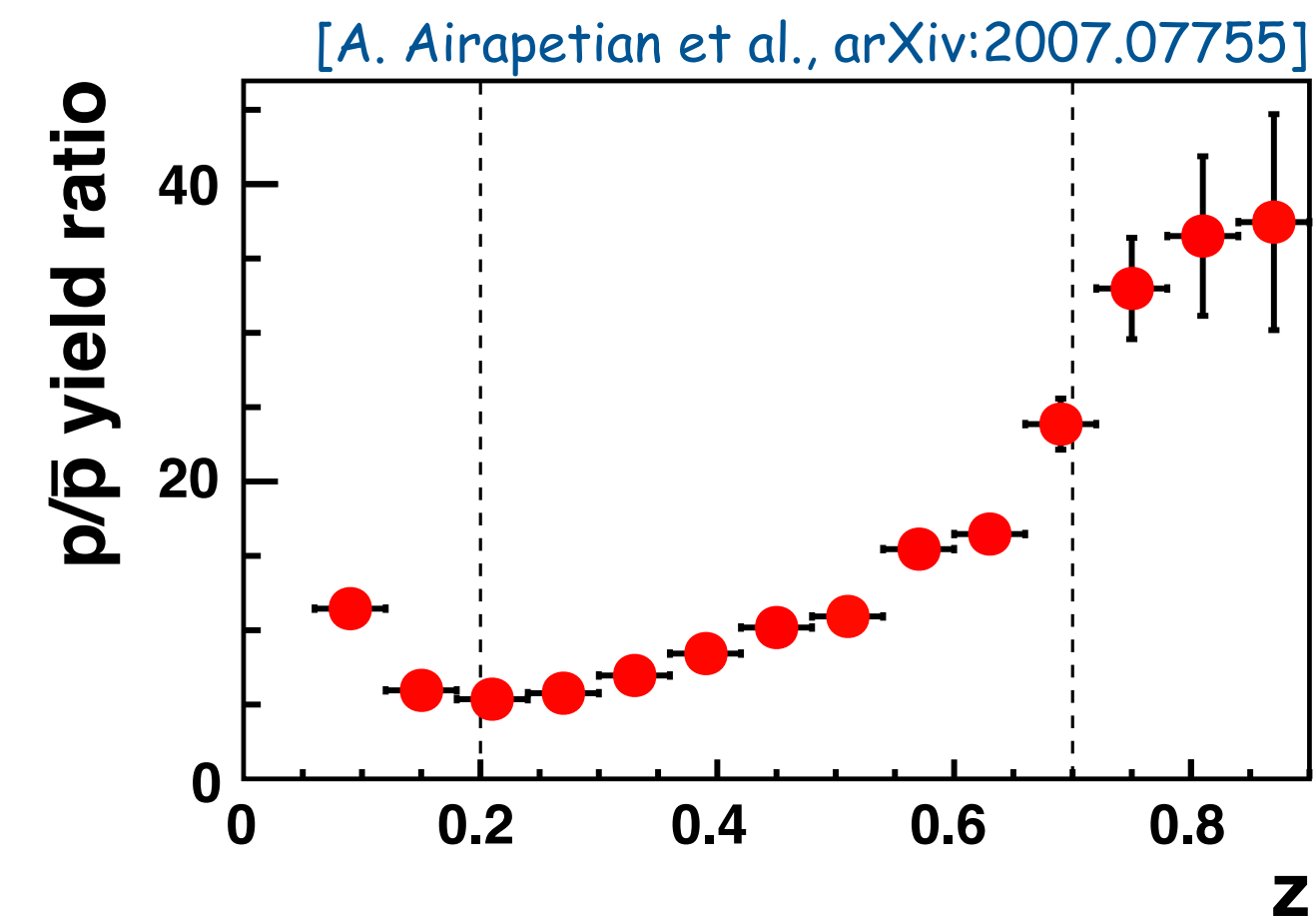
Sivers amplitudes pions vs. (anti)protons

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp



similar-magnitude asymmetries for (anti)protons and pions

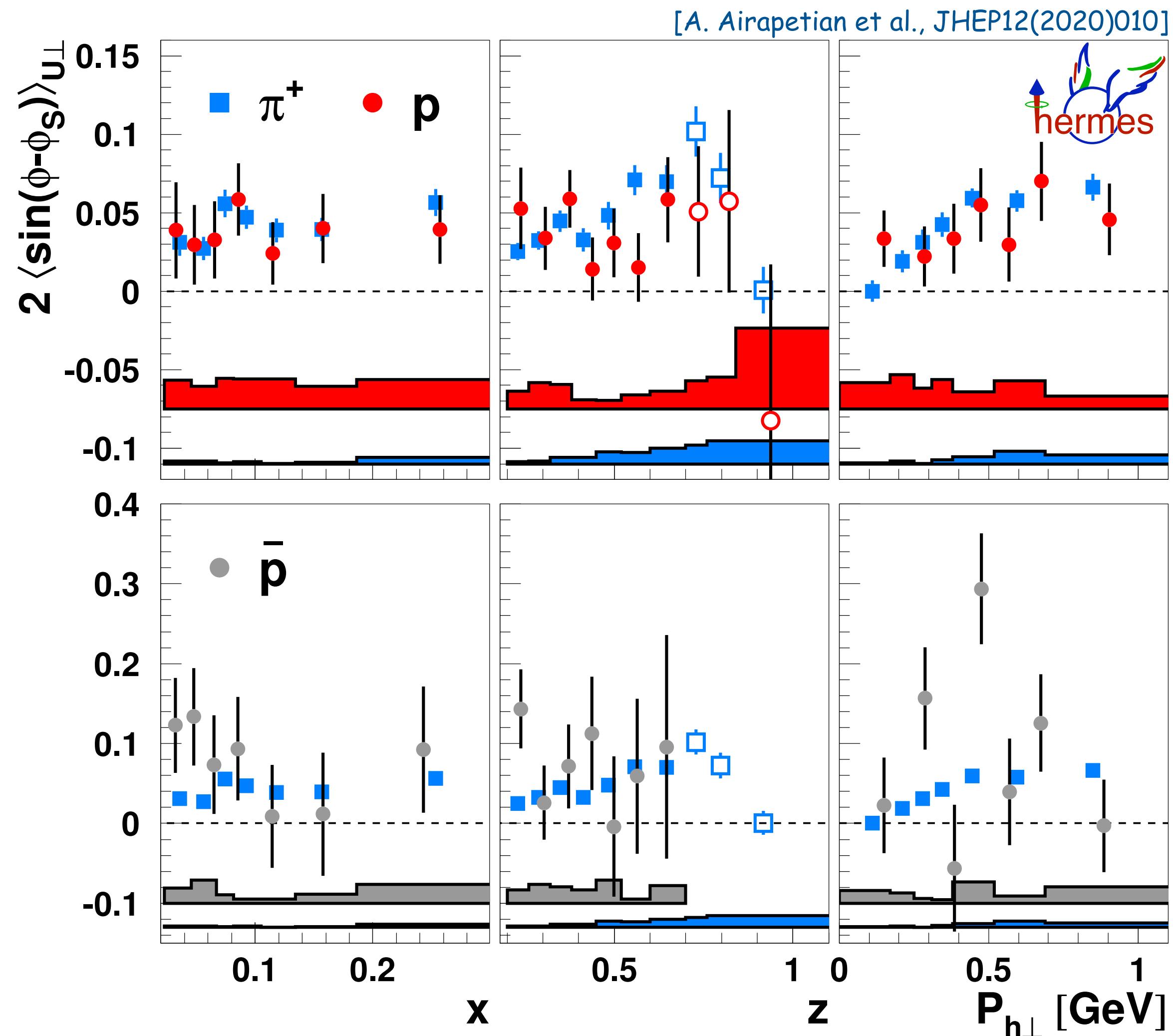
→ consequence of u-quark dominance in both cases?



possibly, onset of target fragmentation only at lower z

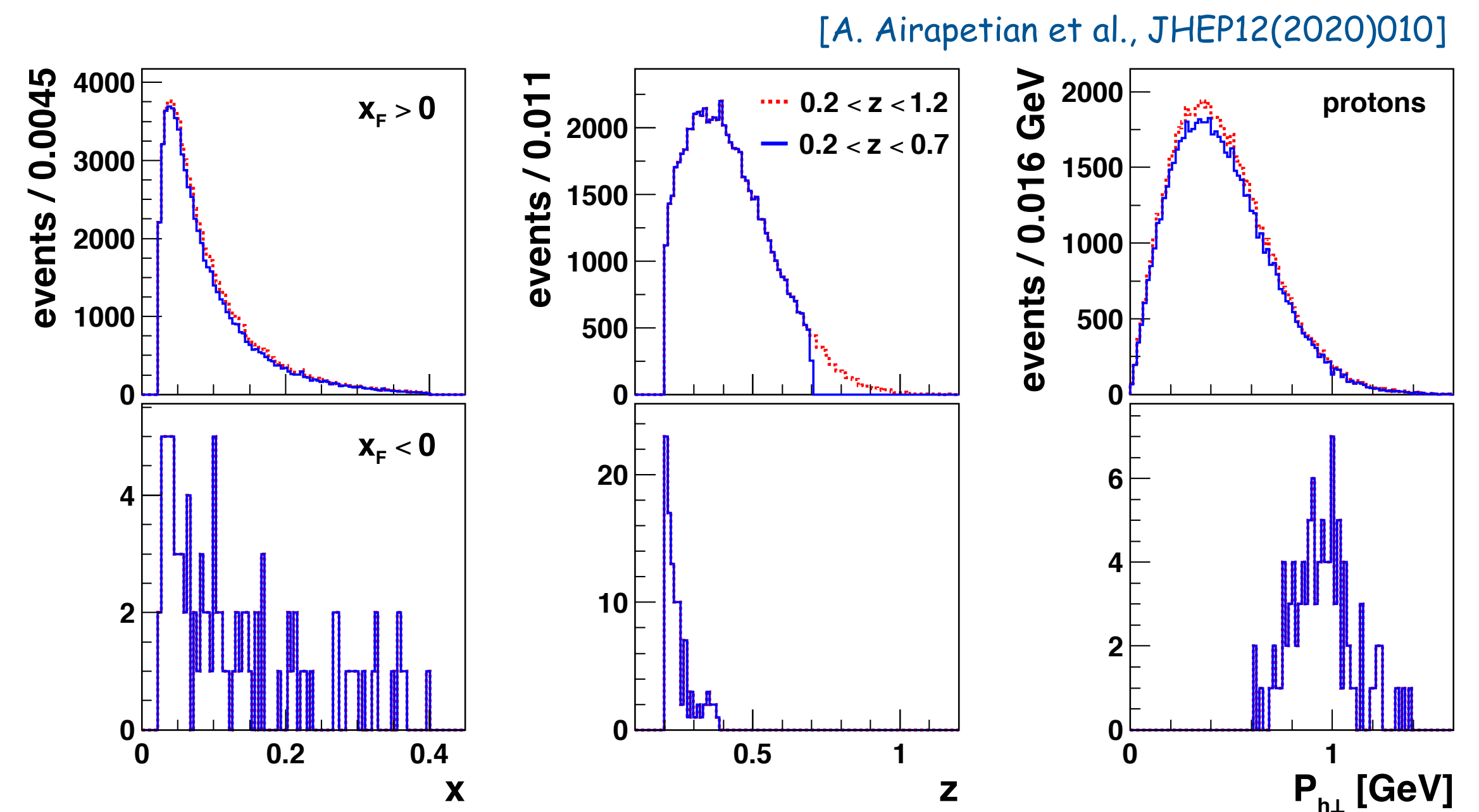
	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

Sivers amplitudes pions vs. (anti)protons



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