

MAP 22: a new global (SIDIS-DY) fit of unpolarised TMDs at N³LL⁽⁻⁾

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(MAP collaboration)

arXiv: 2206.07598 [hep-ph]



Quick facts

Perturbative accuracy: N³LL(-)

2031 SIDIS + (high/low)-energy DY data

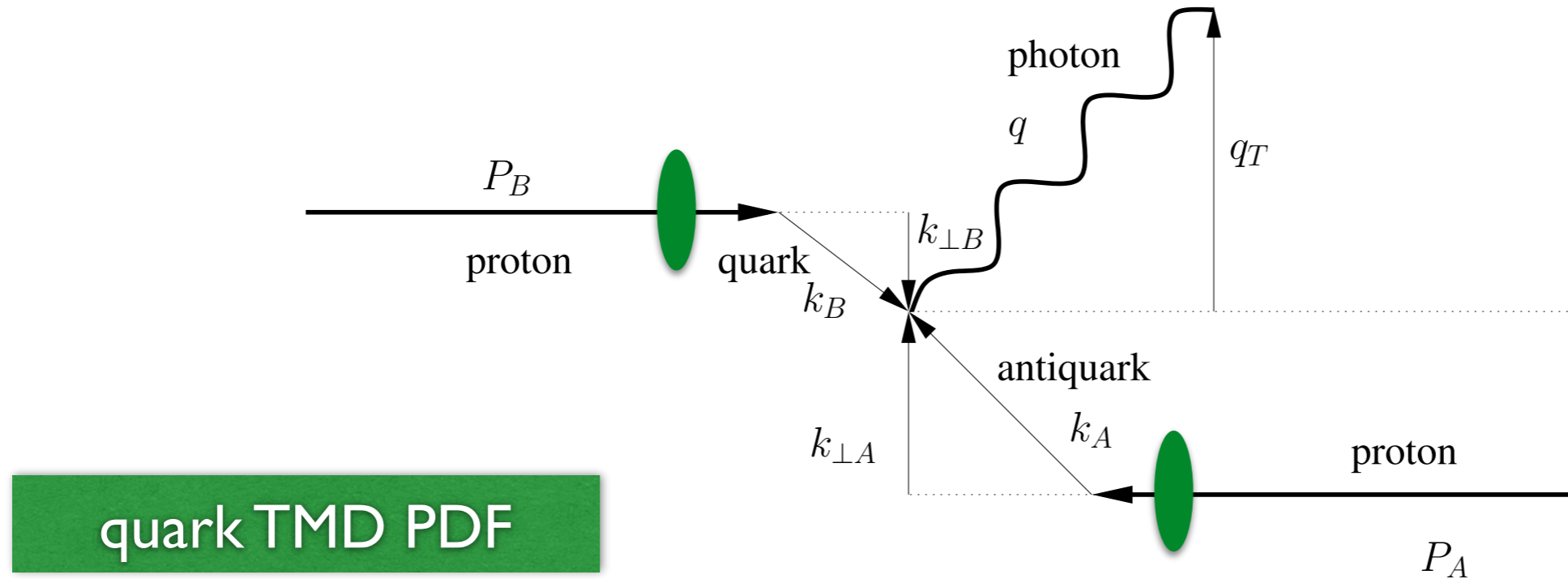


(SIDIS) normalisation factors

21 free parameters

$$\chi^2/N_{data} = 1.06$$

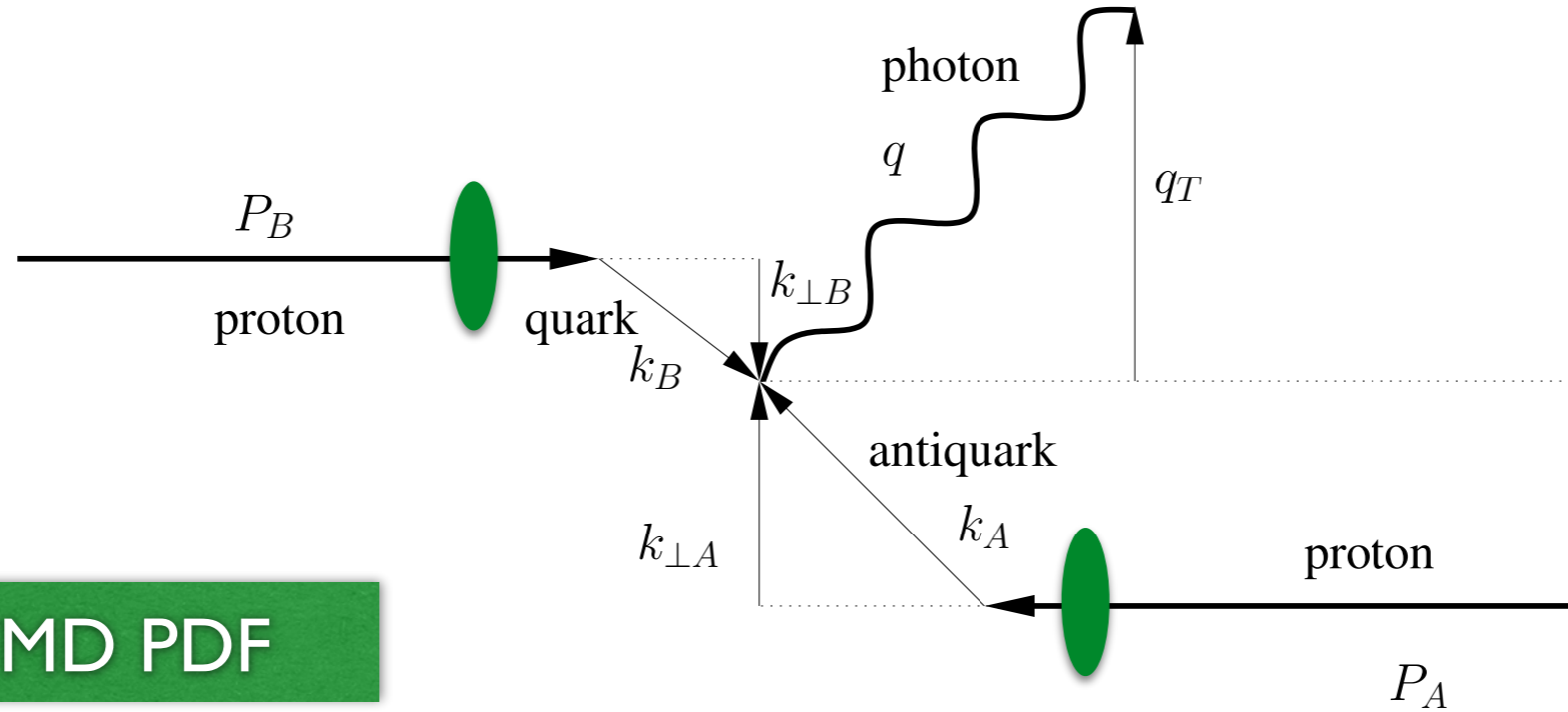
TMD factorisation for DY



quark TMD PDF

$$\frac{d\sigma}{dq_T dy dQ} \propto x_A x_B H^{DY}(Q, \mu) \sum_q c_q(Q^2) \int d^2\mathbf{k}_{\perp A} d^2\mathbf{k}_{\perp B} F^{\bar{q}}(x_A, \mathbf{k}_{\perp A}^2; \mu, \zeta_A) F^q(x_B, \mathbf{k}_{\perp B}^2; \mu, \zeta_B) \delta^{(2)}(\mathbf{k}_{\perp A} + \mathbf{k}_{\perp B} - \mathbf{q}_T)$$

TMD factorisation for DY



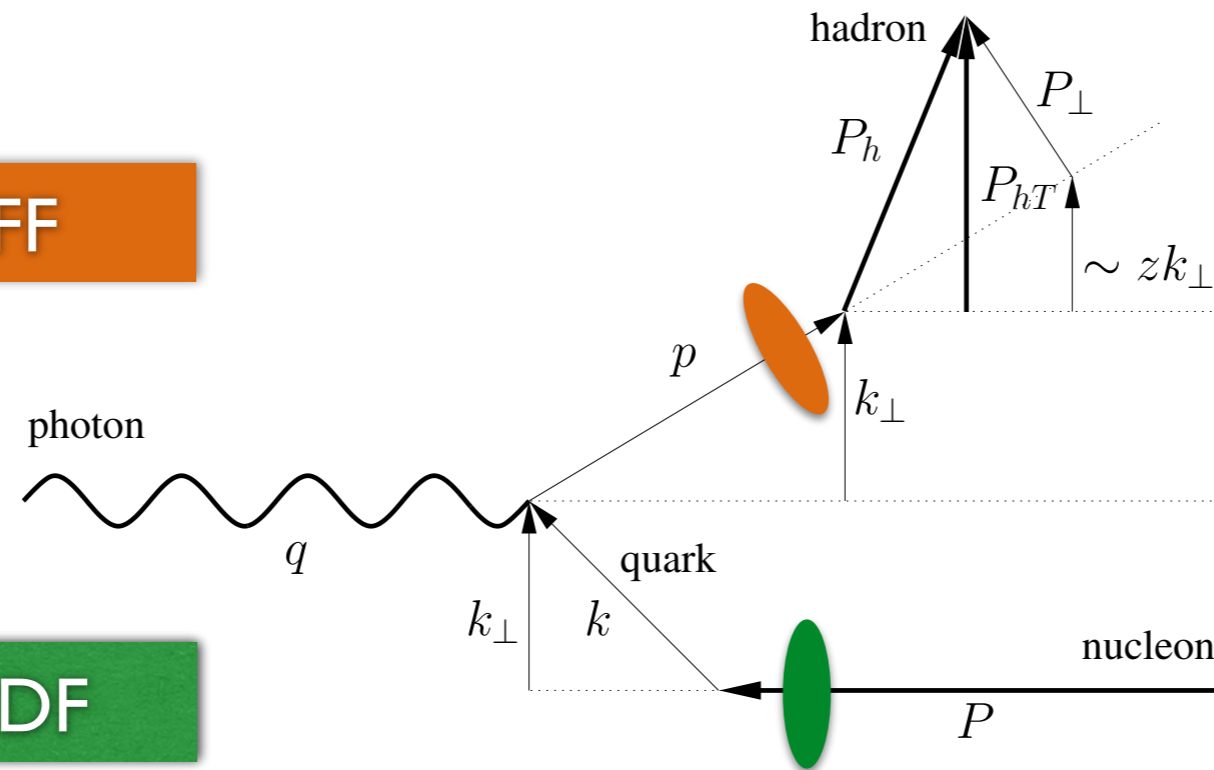
quark TMD PDF

$$\begin{aligned} \frac{d\sigma}{dq_T dy dQ} &\propto x_A x_B H^{DY}(Q, \mu) \sum_q c_q(Q^2) \int d^2\mathbf{k}_{\perp A} d^2\mathbf{k}_{\perp B} \boxed{F^{\bar{q}}(x_A, \mathbf{k}_{\perp A}^2; \mu, \zeta_A)} \boxed{F^q(x_B, \mathbf{k}_{\perp B}^2; \mu, \zeta_B)} \delta^{(2)}(\mathbf{k}_{\perp A} + \mathbf{k}_{\perp B} - \mathbf{q}_T) \\ &= x_A x_B H^{DY}(Q, \mu) \sum_q c_q(Q^2) \int \frac{db_T}{2\pi} b_T J_0(b_T q_T) \boxed{\hat{F}^{\bar{q}}(x_A, b_T^2; \mu, \zeta_A)} \boxed{\hat{F}^q(x_B, b_T^2; \mu, \zeta_B)} \end{aligned}$$

TMD factorisation for SIDIS

quark TMD FF

quark TMD PDF

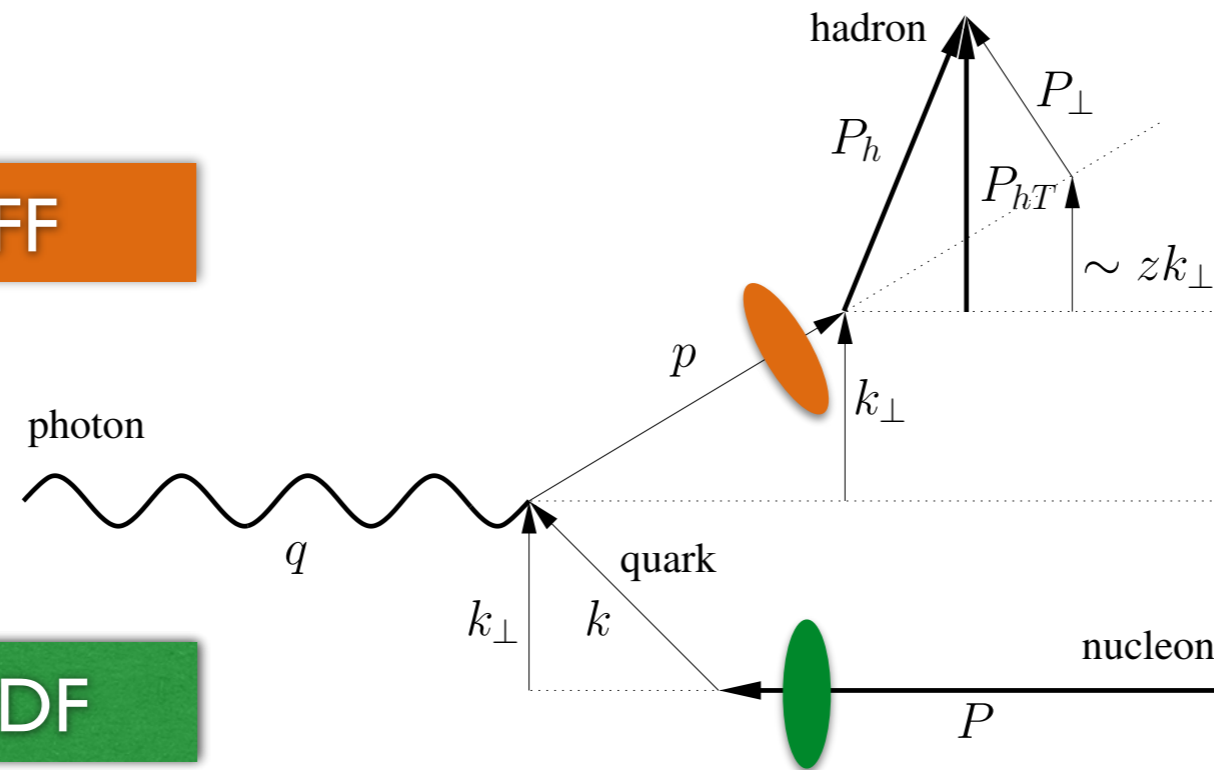


$$\frac{d\sigma}{dx dz dq_T dQ} \propto x H^{SIDIS}(Q, \mu) \sum_q e_q(Q^2) \int d^2\mathbf{k}_\perp \int \frac{d^2\mathbf{P}_\perp}{z^2} F^q(x, \mathbf{k}_\perp^2; \mu, \zeta_A) D^{q \rightarrow h}(z, \mathbf{P}_\perp^2; \mu, \zeta_B) \delta^{(2)}(\mathbf{k}_\perp + \mathbf{P}_\perp/z + \mathbf{q}_T)$$

TMD factorisation for SIDIS

quark TMD FF

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$$\frac{d\sigma}{dx dz dq_T dQ} \propto x H^{SIDIS}(Q, \mu) \sum_q e_q(Q^2) \int d^2\mathbf{k}_{\perp} \int \frac{d^2\mathbf{P}_{\perp}}{z^2} F^q(x, \mathbf{k}_{\perp}^2; \mu, \zeta_A) D^{q \rightarrow h}(z, \mathbf{P}_{\perp}^2; \mu, \zeta_B) \delta^{(2)}(\mathbf{k}_{\perp} + \mathbf{P}_{\perp}/z + \mathbf{q}_T)$$

$$= x H^{SIDIS}(Q, \mu) \sum_q e_q(Q^2) \int \frac{db_T}{2\pi} b_T J_0(b_T q_T) \hat{F}^q(x, b_T^2; \mu, \zeta_A) \hat{D}^q(z, b_T^2; \mu, \zeta_B)$$

TMD structure

$$\begin{aligned} F_{f/P}(x, \mathbf{b}_T; \mu, \zeta) &= \sum_j C_{f/j}(x, b_*; \mu_b, \zeta_F) \otimes f_{j/P}(x, \mu_b) && : A \\ &\times \exp \left\{ K(b_*; \mu_b) \ln \frac{\sqrt{\zeta_F}}{\mu_b} + \int_{\mu_b}^{\mu} \frac{d\mu'}{\mu'} \left[\gamma_F - \gamma_K \ln \frac{\sqrt{\zeta_F}}{\mu'} \right] \right\} && : B \\ &\times \exp \left\{ g_{j/P}(x, b_T) + g_K(b_T) \ln \frac{\sqrt{\zeta_F}}{\sqrt{\zeta_{F,0}}} \right\} && : C \end{aligned}$$

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- matching to collinear PDF at $b_T \ll 1/\Lambda_{\text{QCD}}$
- **perturbative**

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Accuracy	H and C	K and γ_F	γ_K	PDF and α_s evolution
LL	0	-	1	-
NLL	0	1	2	LO
NLL'	1	1	2	NLO
NNLL	1	2	3	NLO
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N ³ LL	2	3	4	NNLO

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$N^3LL^- = N^3LL$ with NLO FF

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- **perturbative**

$$(\mu_b = 2e^{-\gamma_E} / b_*)$$

- CS and RGE evolution to large b_T
- **perturbative**

- b_* prescription to avoid Landau pole

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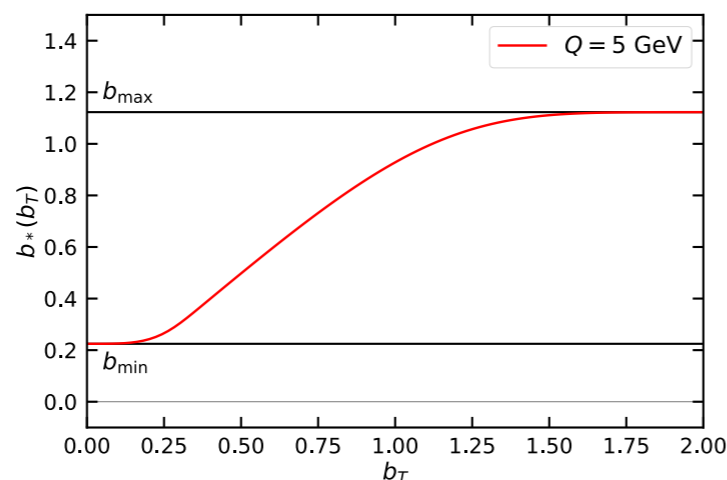
- matching to collinear PDF at $b_T \ll 1/\Lambda_{\text{QCD}}$
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$$(\mu_b = 2e^{-\gamma_E} / b_*)$$

$$b_*(b) = b_{\text{max}} \left(\frac{1 - \exp\left(-\frac{b^4}{b_{\text{max}}^4}\right)}{1 - \exp\left(-\frac{b^4}{b_{\text{min}}^4}\right)} \right)^{\frac{1}{4}}$$

$$b_{\text{max}} = 2e^{-\gamma_E}$$

$$b_{\text{min}} = 2e^{-\gamma_E} / Q$$



- CS and RGE evolution to large b_T
- **perturbative**

- b_* prescription to avoid Landau pole

$N^3LL^- = N^3LL$ with NLO FF

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 &\times \exp \left\{ g_{j/P}(x, b_T) + g_K(b_T) \ln \frac{\sqrt{\zeta_F}}{\sqrt{\zeta_{F,0}}} \right\} f_{NP} && : C
 \end{aligned}$$

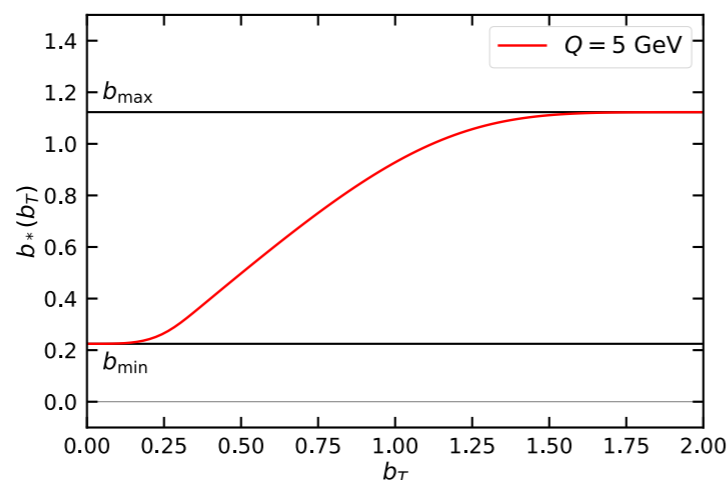
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$$b_{\text{max}} = 2e^{-\gamma_E}$$

$$b_{\text{min}} = 2e^{-\gamma_E}/Q$$



- CS and RGE evolution to large b_T
- **perturbative**

- b_* prescription to avoid Landau pole
- f_{NP} “parametrises” the **non-perturbative** transverse modes
- **fit** f_{NP} to data

$N^3LL^- = N^3LL$ with NLO FF

Non-perturbative: \mathbf{f}_{NP}

$$F(x, b; \mu, \zeta) = \left[\frac{F(x, b; \mu, \zeta)}{F(x, b_*(b); \mu, \zeta)} \right] F(x, b_*(b); \mu, \zeta)$$

Non-perturbative: f_{NP}

$$F(x, b; \mu, \zeta) \stackrel{f_{\text{NP}}}{=} \left[\frac{F(x, b; \mu, \zeta)}{F(x, b_*(b); \mu, \zeta)} \right] F(x, b_*(b); \mu, \zeta)$$

- depends on choice of b^* and collinear PDFs
- requires definition of a functional form

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- depends on choice of b^* and collinear PDFs
- requires definition of a functional form

Our functional form

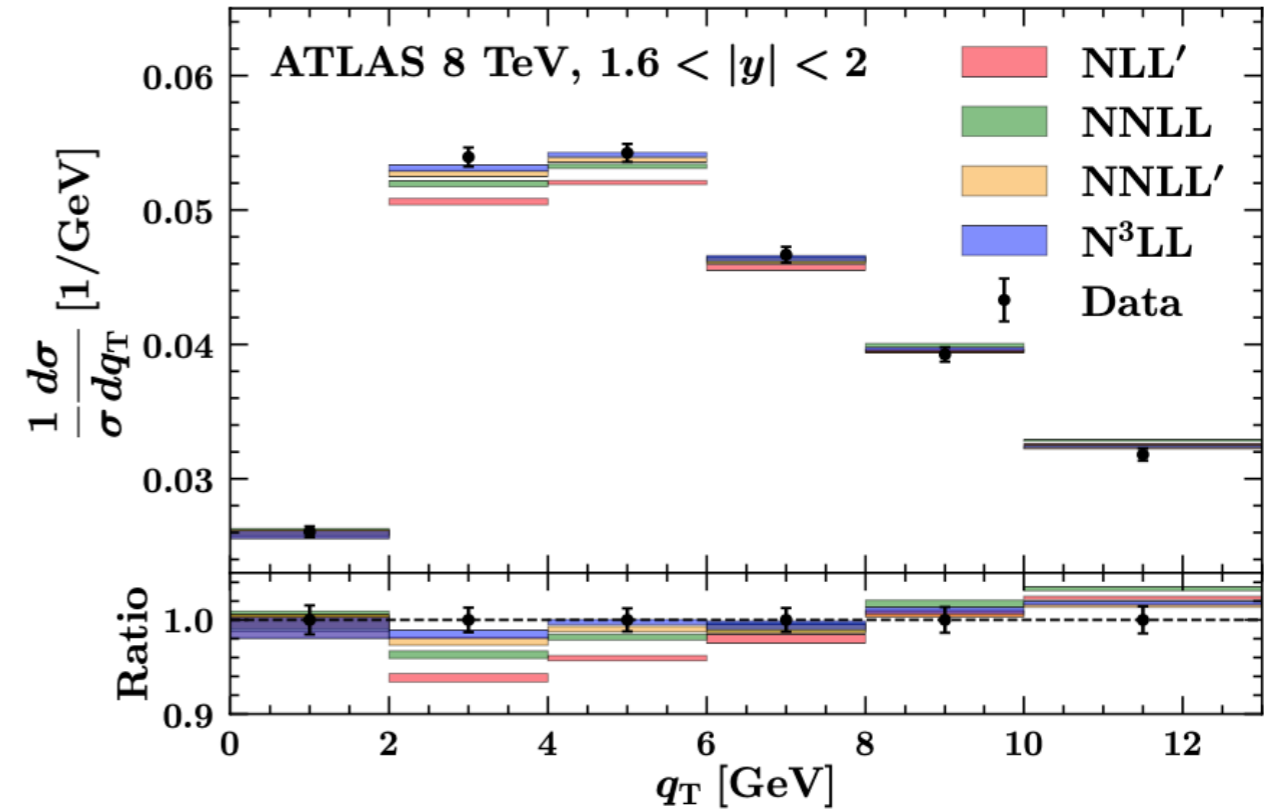
$$f_{1\text{NP}}(x, b_T^2) \propto \text{F.T. of } \left(e^{-\frac{k_T^2}{g1}} + \lambda^2 k_T^2 e^{-\frac{k_T^2}{g1B}} + \lambda_2^2 e^{-\frac{k_T^2}{g1C}} \right)$$

$$g_{\{1,1B,1C\}}(x) = N_{\{1,1B,1C\}} \frac{x^{\sigma_{\{1,2,3\}}} (1-x)^{\alpha_{\{1,2,3\}}^2}}{\hat{x}^{\sigma_{\{1,2,3\}}} (1-\hat{x})^{\alpha_{\{1,2,3\}}^2}}$$

- similar form for TMD FF
- 21 free parameters

SIDIS normalisation

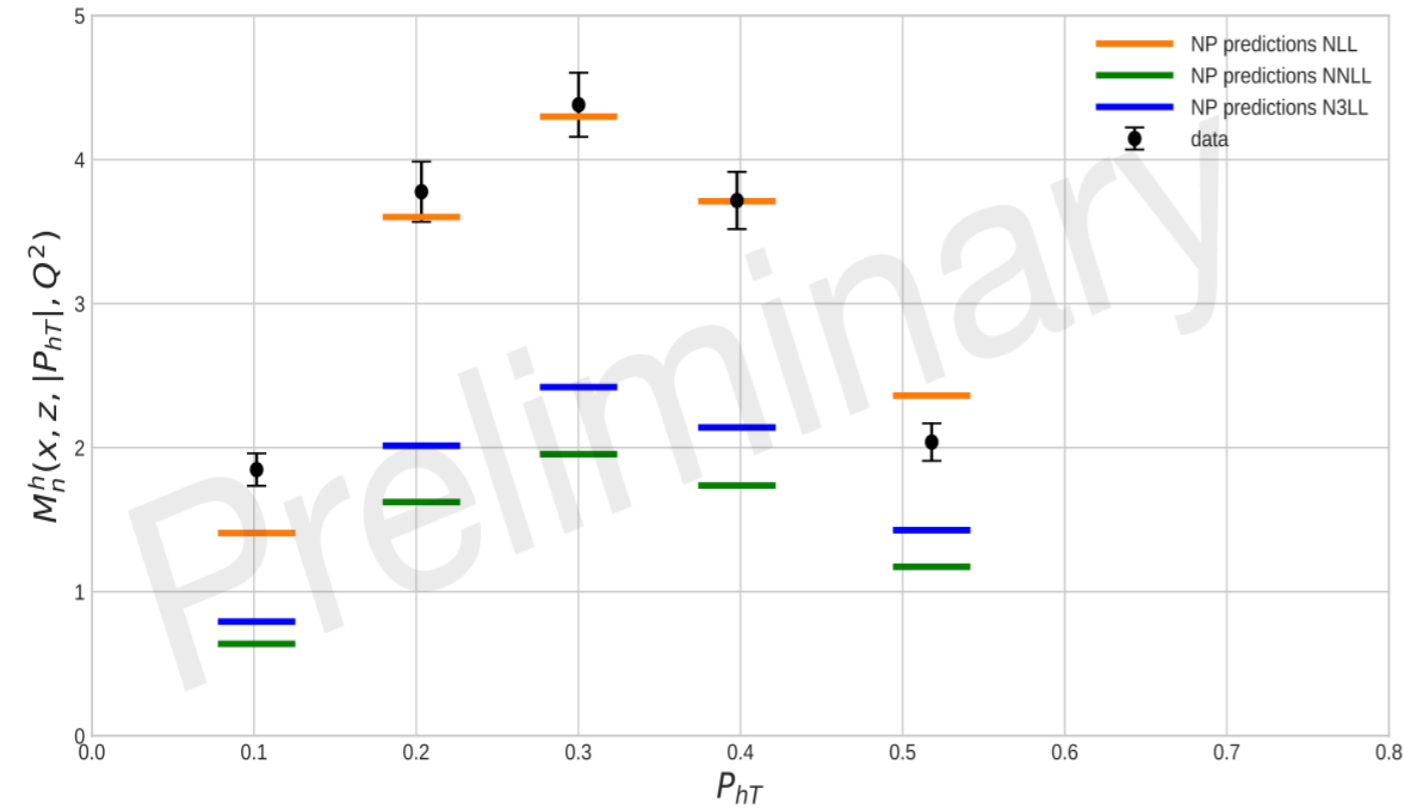
DY beyond NLL



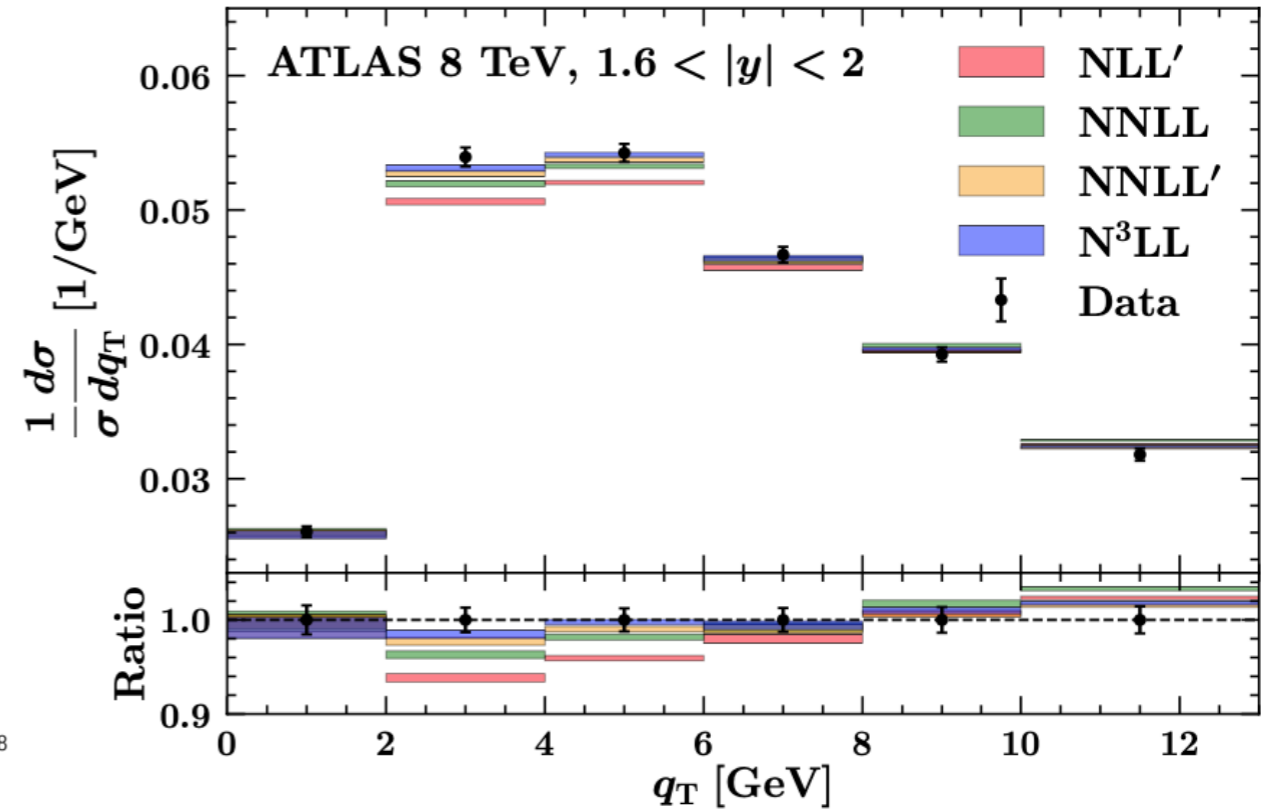
SIDIS normalisation

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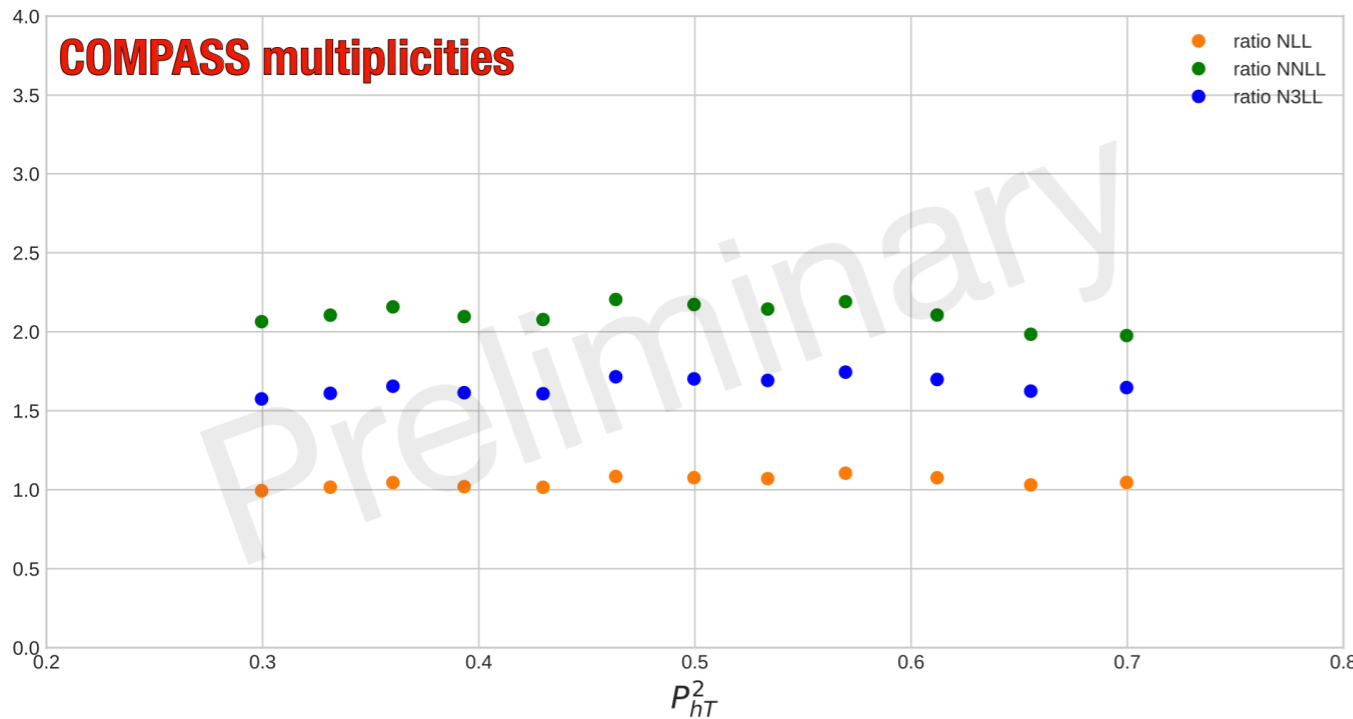
HERMES



DY beyond NLL



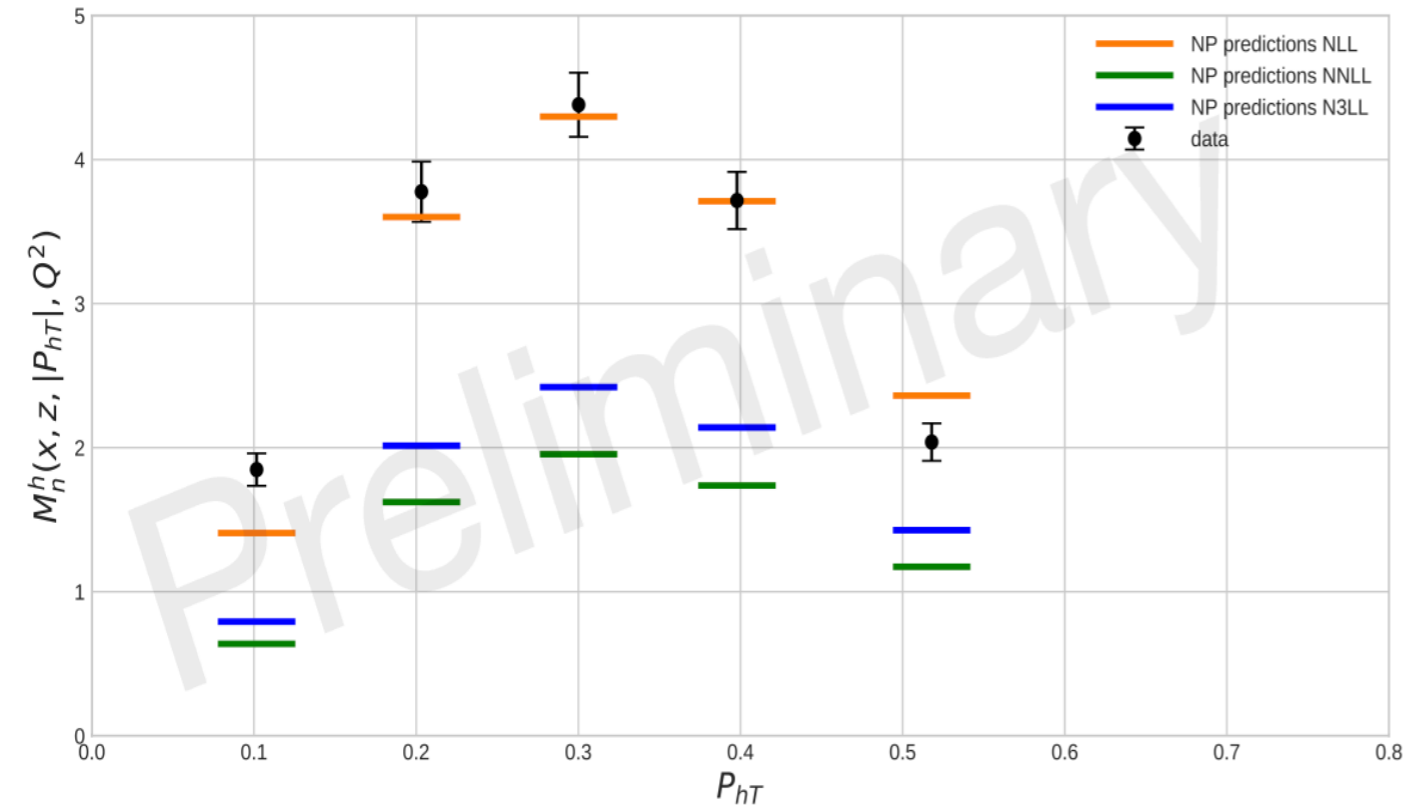
COMPASS multiplicities



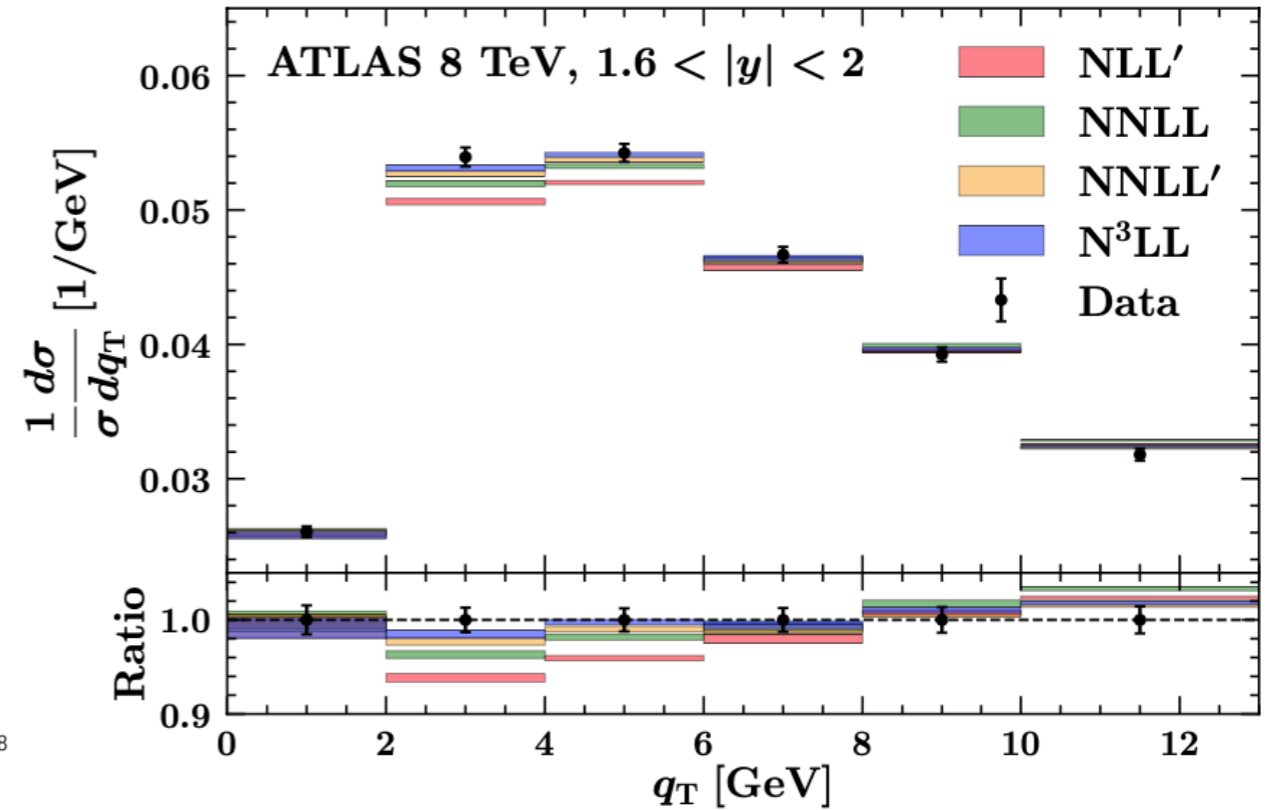
SIDIS normalisation

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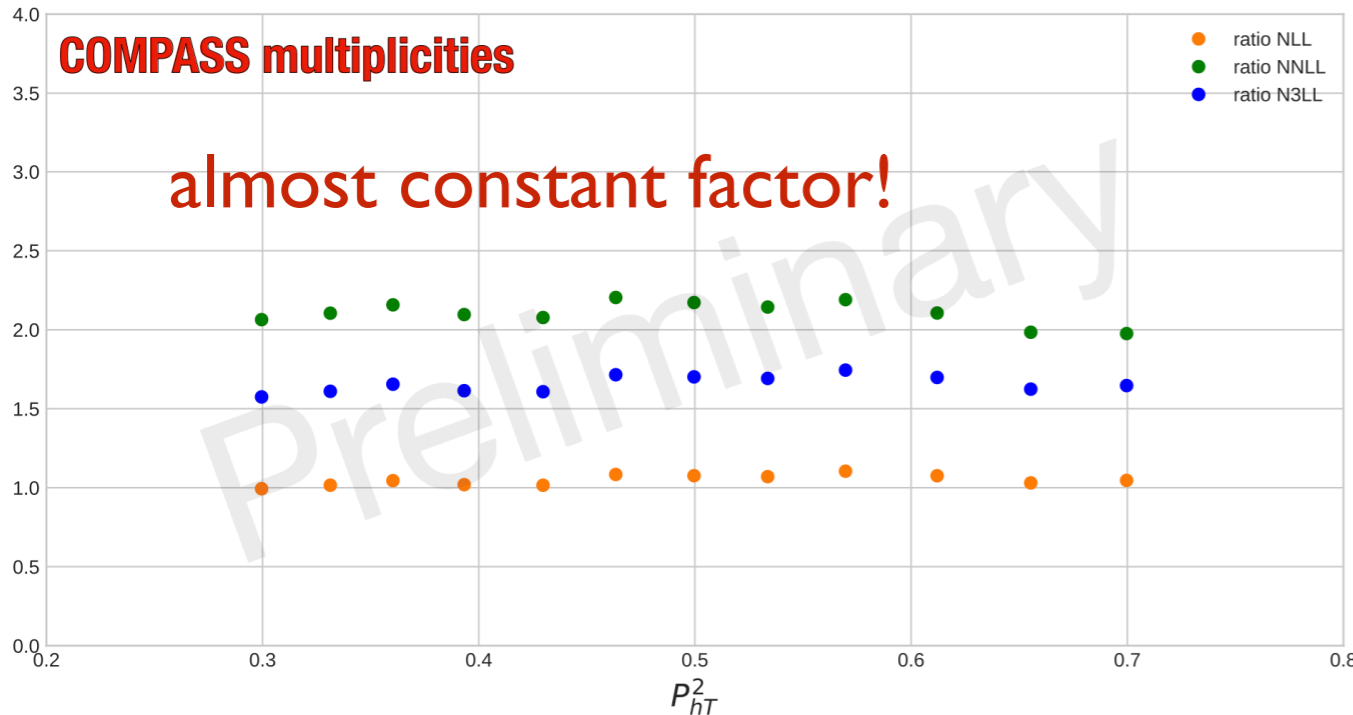


DY beyond NLL



COMPASS multiplicities

almost constant factor!



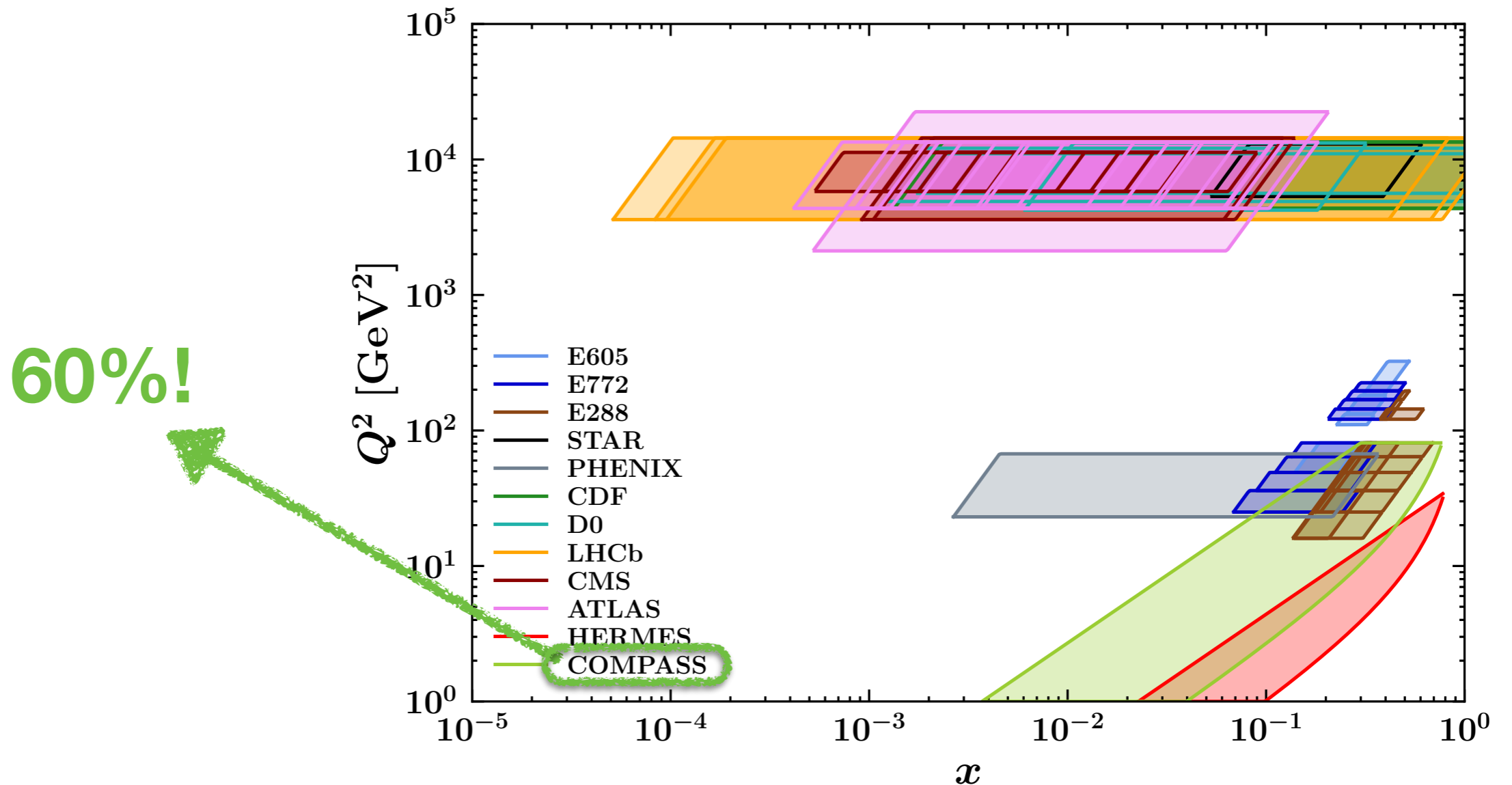
normalisation factor for SIDIS

- computed a priori, before the fit
- independent on the fitting parameters
- dependent on collinear PDFs

TMD global fits

	Accuracy	HERMES	COMPASS	DY fixed target	DY collider	N of points	χ^2/N_{points}
Pavia 2017 arXiv:1703.10157	NLL	✓	✓	✓	✓	8059	1.55
SV 2019 arXiv:1912.06532	N ³ LL ⁻	✓	✓	✓	✓	1039	1.06
MAP22 arXiv:2206.07598	N ³ LL ⁻	✓	✓	✓	✓	2031	1.06

Datasets

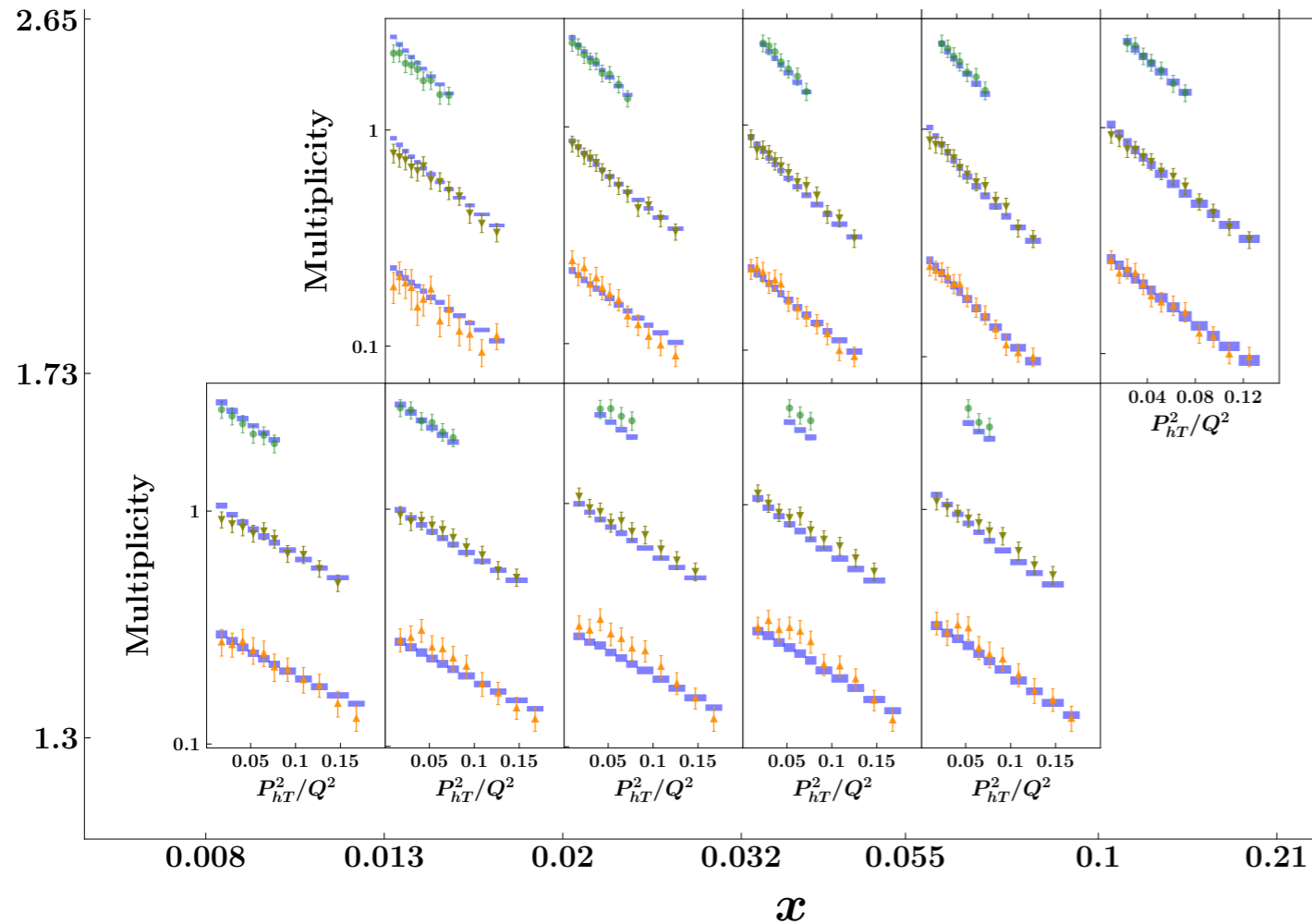


Cuts on kinematics

- $\langle Q \rangle > 1.3$ GeV
- $0.2 < \langle z \rangle < 0.7$
- $q_T/Q \leq 0.2$ (Drell-Yan)
- $P_{hT}|_{max} = \min[\min[0.2Q, 0.5zQ] + 0.3 \text{ GeV}, zQ]$ (SIDIS)

Fit quality: SIDIS

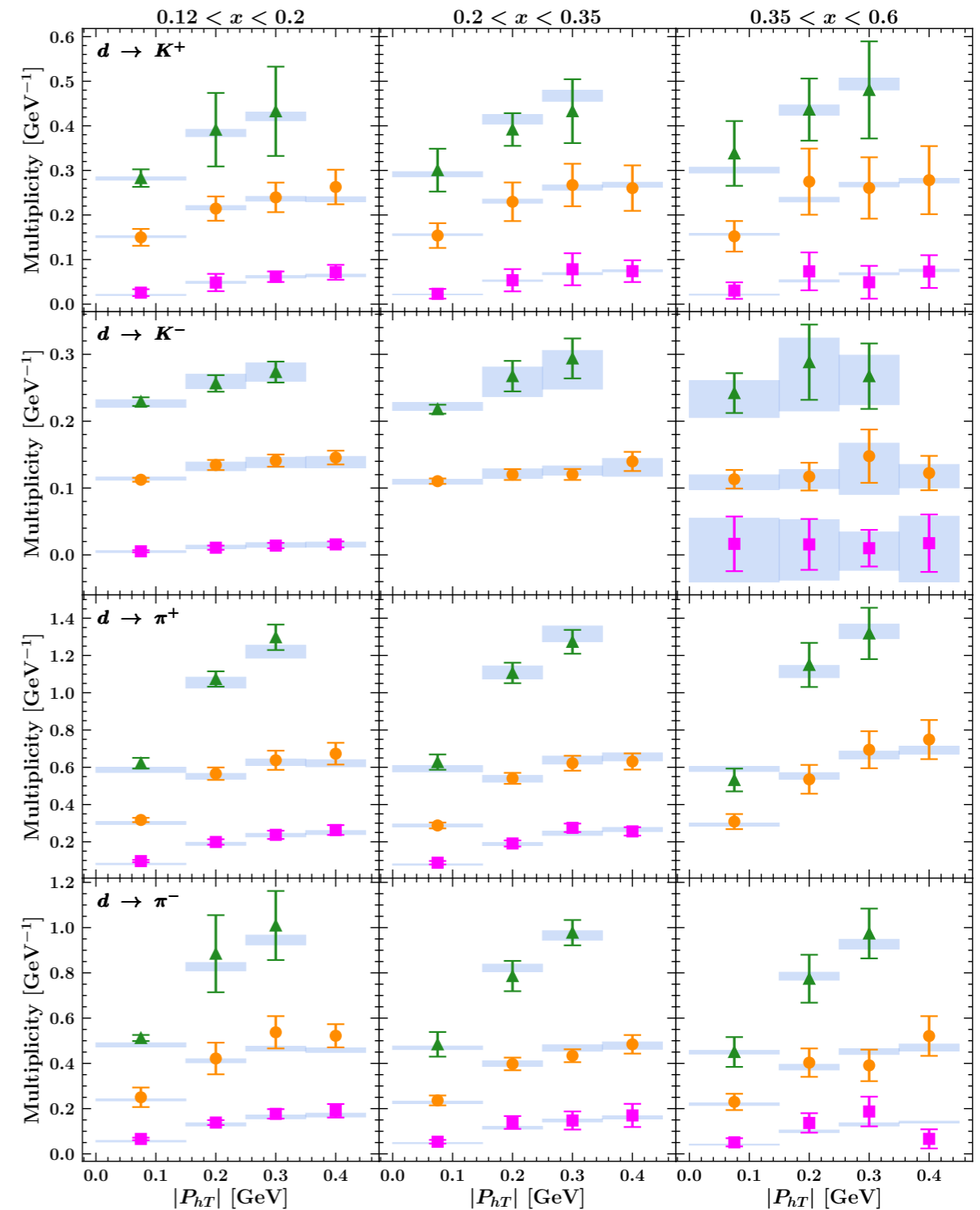
COMPASS



Good agreement for almost all bins

$$\chi^2/N_{data} = 0.87 \text{ (SIDIS total)}$$

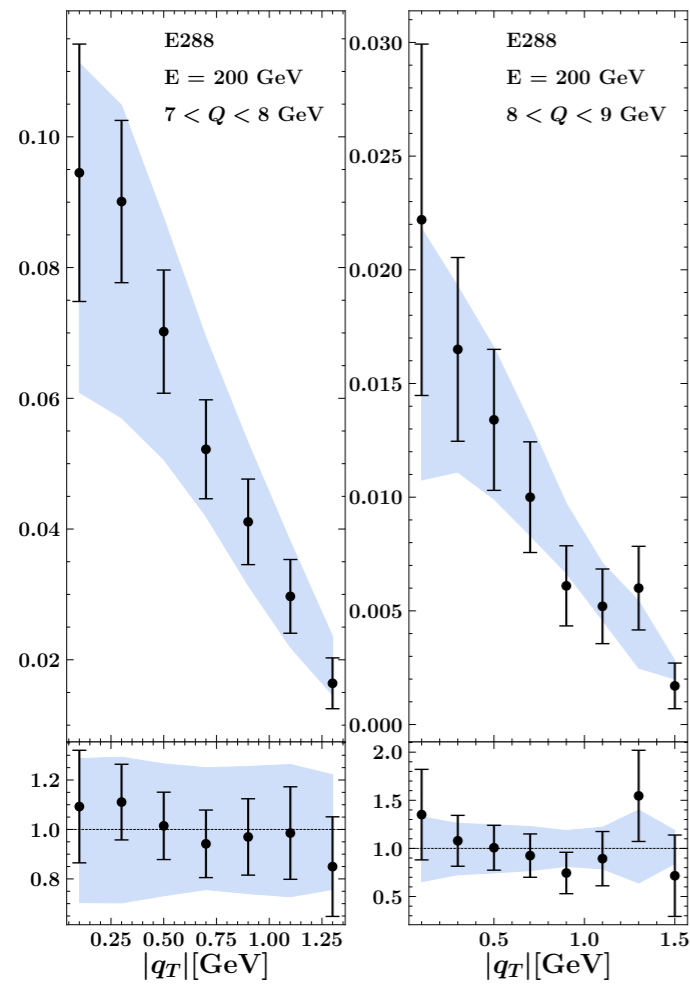
HERMES



▲ $0.375 < z < 0.475$ (offset = 0.2)
● $0.475 < z < 0.6$ (offset = 0.1)
■ $0.6 < z < 0.8$ (offset = 0)

Fit quality: Drell-Yan

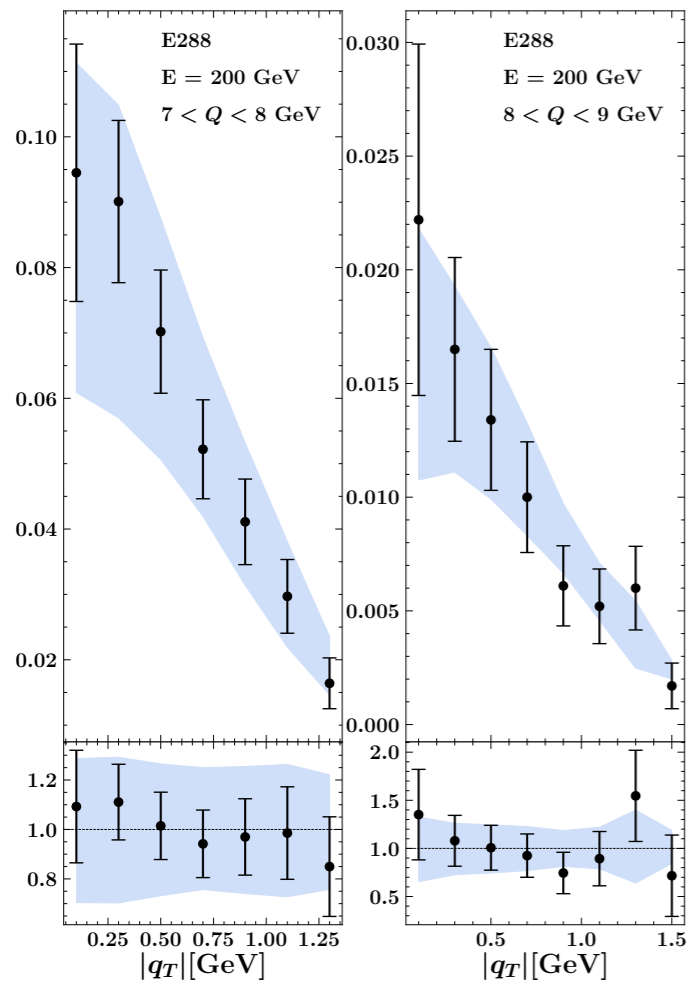
E288



$\chi^2/N_{data} = 1.24$
(DY fixed-target)

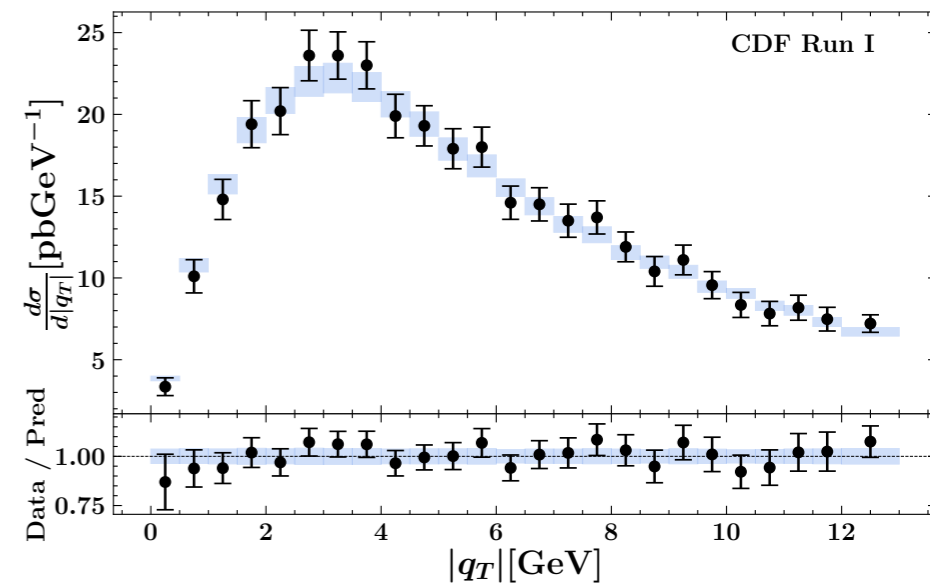
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E288



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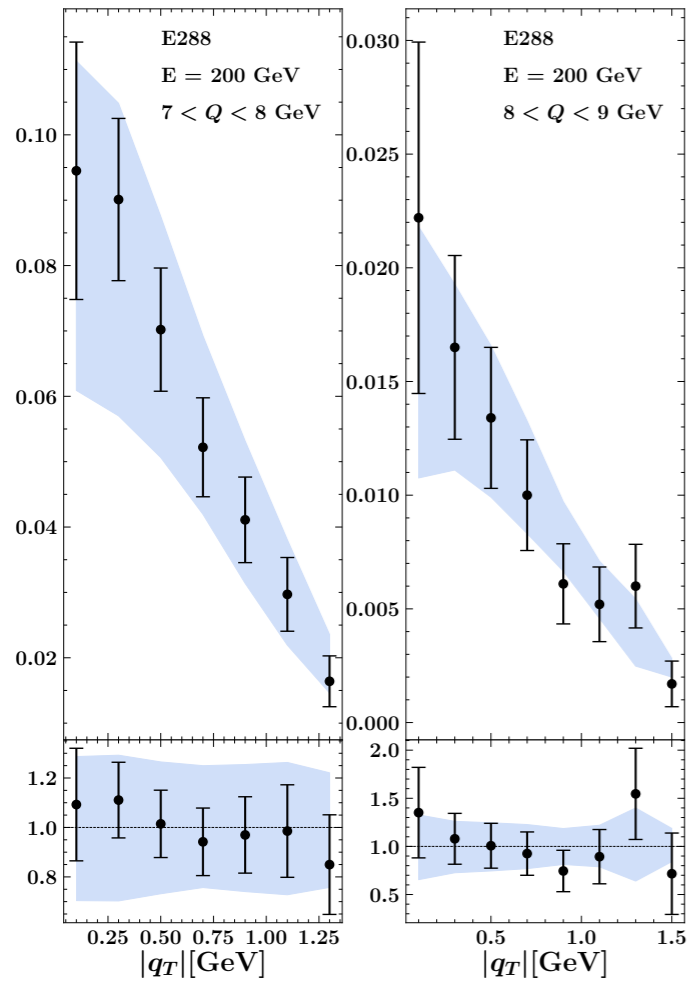
CDF



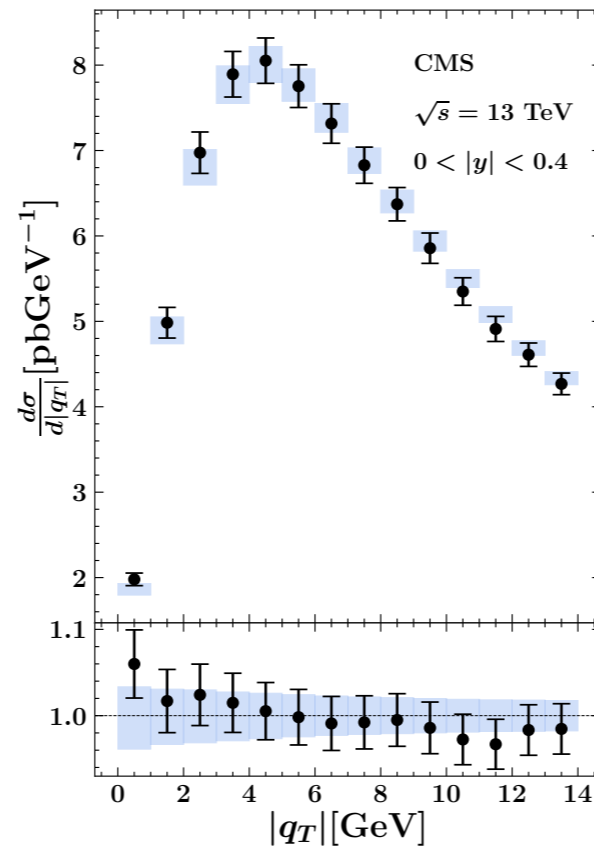
$\chi^2/N_{data} = 0.93$
(DY Tevatron)

Fit quality: Drell-Yan

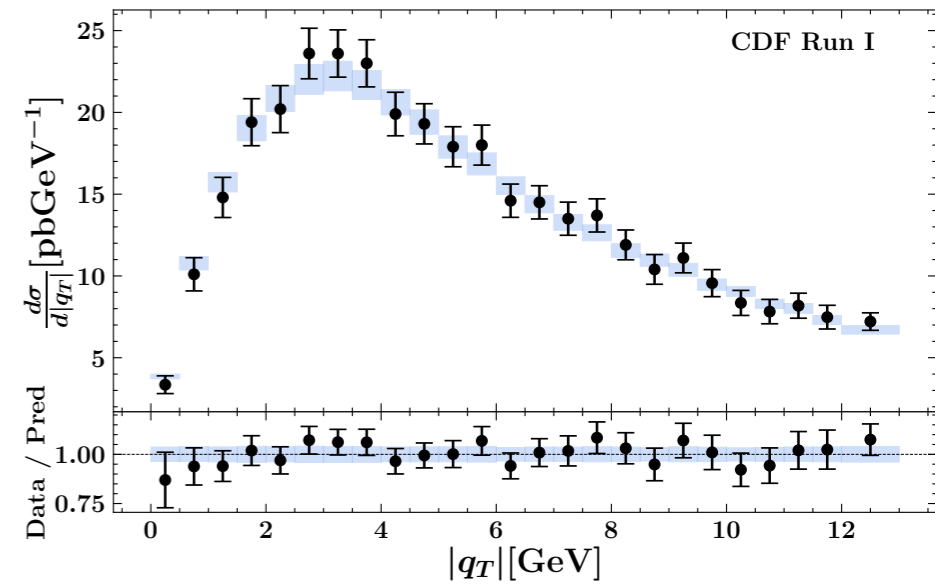
E288



CMS

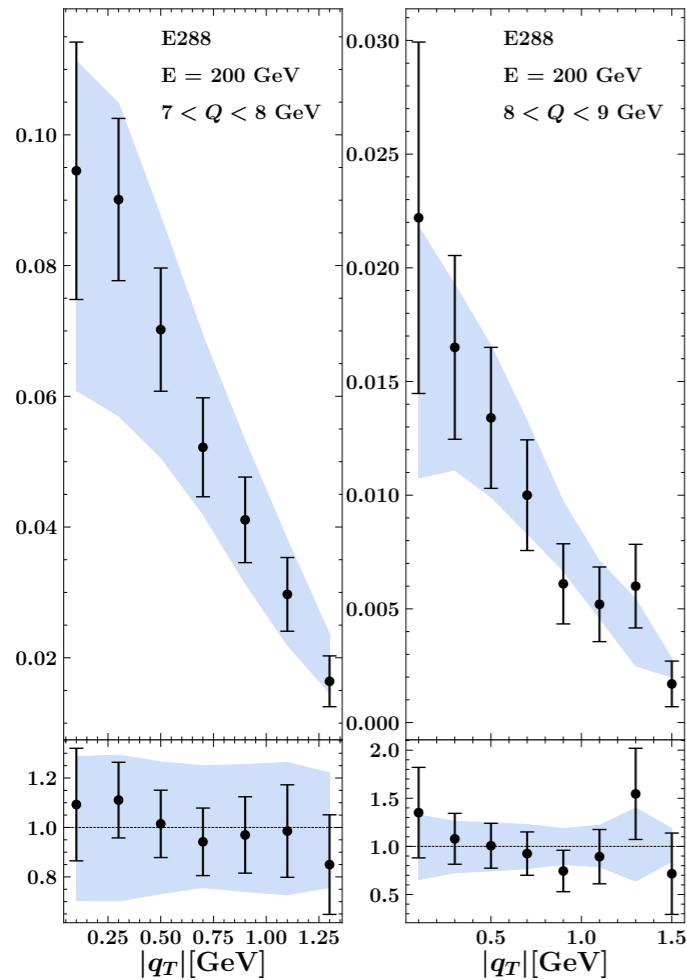


CDF



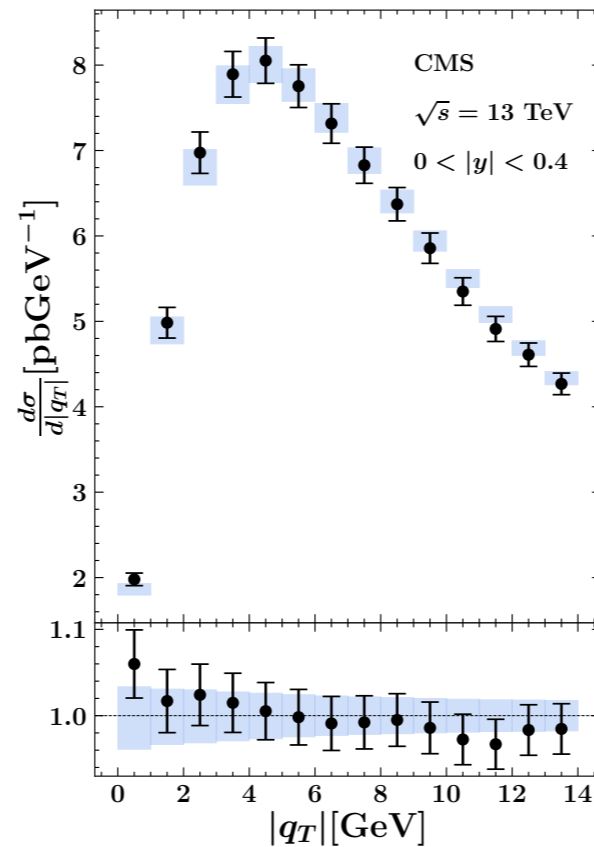
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E288



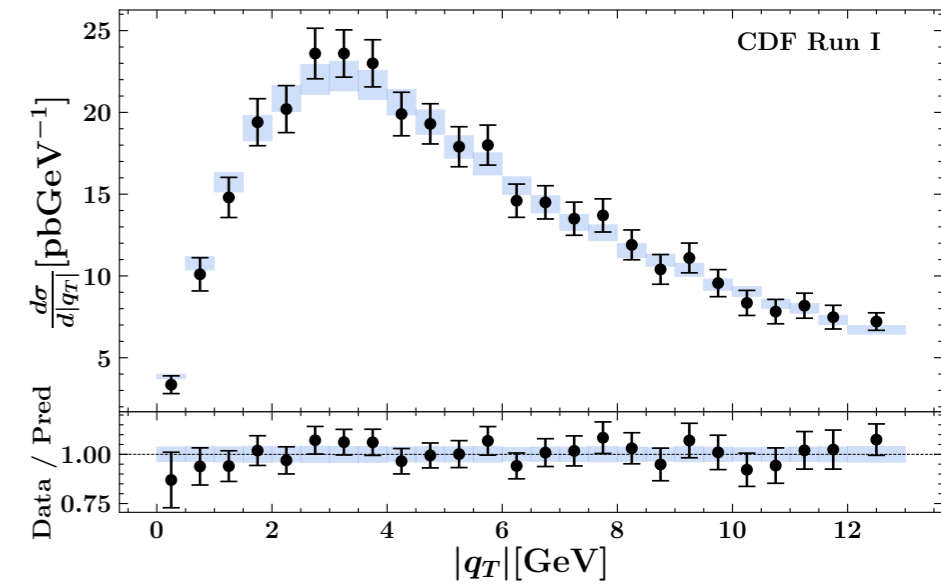
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CMS



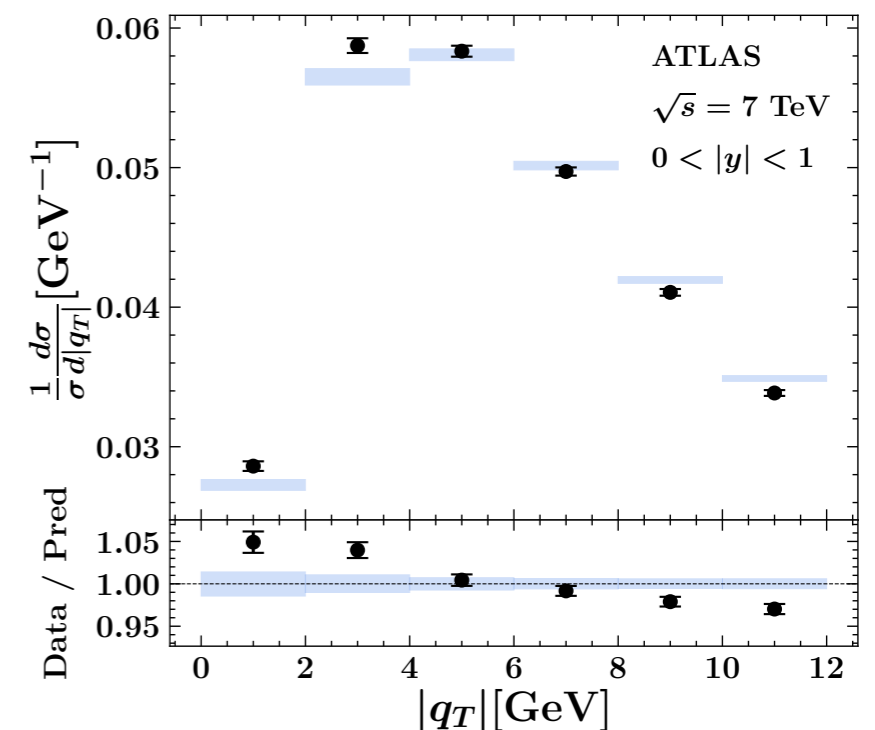
$\chi^2/N_{data} = 0.55$
(DY CMS)

CDF



$\chi^2/N_{data} = 0.93$
(DY Tevatron)

ATLAS



$\chi^2/N_{data} = 5.05$
(DY ATLAS)

Fitting parameters

Parameter	Average over replicas
g_2 [GeV]	0.248 ± 0.008
N_1 [GeV ²]	0.316 ± 0.025
α_1	1.29 ± 0.19
σ_1	0.68 ± 0.13
λ [GeV ⁻¹]	1.82 ± 0.29
N_3 [GeV ²]	0.0055 ± 0.0006
β_1	10.23 ± 0.29
δ_1	0.0094 ± 0.0012
γ_1	1.406 ± 0.084
λ_F [GeV ⁻²]	0.078 ± 0.011
N_{3B} [GeV ²]	0.2167 ± 0.0055
N_{1B} [GeV ²]	0.134 ± 0.017
N_{1C} [GeV ²]	0.0130 ± 0.0069
λ_2 [GeV ⁻¹]	0.0215 ± 0.0058
α_2	4.27 ± 0.31
α_3	4.27 ± 0.13
σ_2	0.455 ± 0.050
σ_3	12.71 ± 0.21
β_2	4.17 ± 0.13
δ_2	0.167 ± 0.006
γ_2	0.0007 ± 0.0110

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- $\lambda \sim 2$: weighted Gaussian important

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N_{1B} [GeV ²]	0.134 ± 0.017
N_{1C} [GeV ²]	0.0130 ± 0.0069
λ_2 [GeV ⁻¹]	0.0215 ± 0.0058
α_2	4.27 ± 0.31
α_3	4.27 ± 0.13
σ_2	0.455 ± 0.050
σ_3	12.71 ± 0.21
β_2	4.17 ± 0.13
δ_2	0.167 ± 0.006
γ_2	0.0007 ± 0.0110

- $\lambda \sim 2$: weighted Gaussian important
- $\lambda_2 \neq 0$: third Gaussian non-negligible

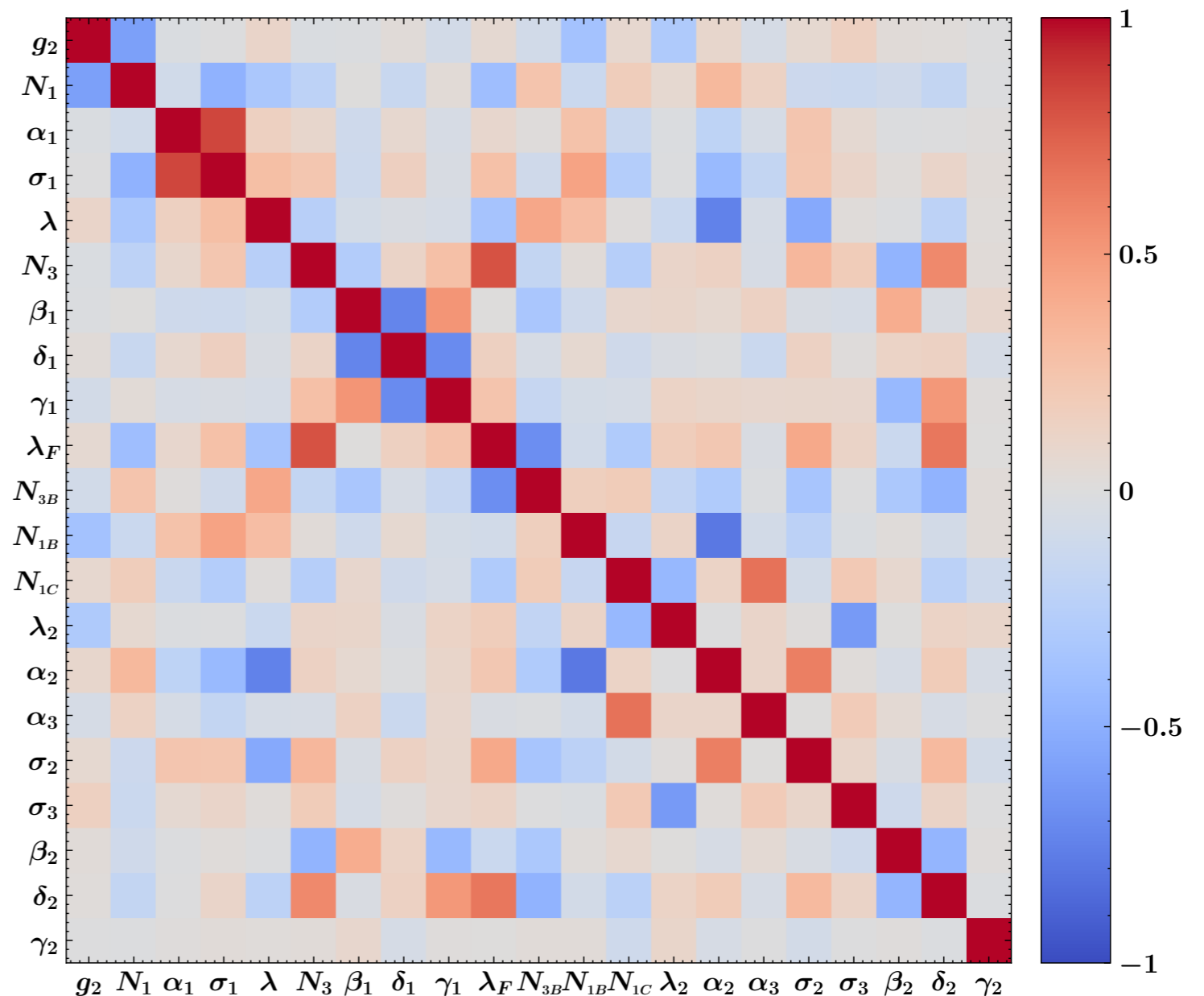
Fitting parameters

Parameter	Average over replicas
g_2 [GeV]	0.248 ± 0.008
N_1 [GeV ²]	0.316 ± 0.025
α_1	1.29 ± 0.19
σ_1	0.68 ± 0.13
λ [GeV ⁻¹]	1.82 ± 0.29
N_3 [GeV ²]	0.0055 ± 0.0006
β_1	10.23 ± 0.29
δ_1	0.0094 ± 0.0012
γ_1	1.406 ± 0.084
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- $\lambda \sim 2$: weighted Gaussian important
- $\lambda_2 \neq 0$: third Gaussian non-negligible
- g_2 very small standard deviation

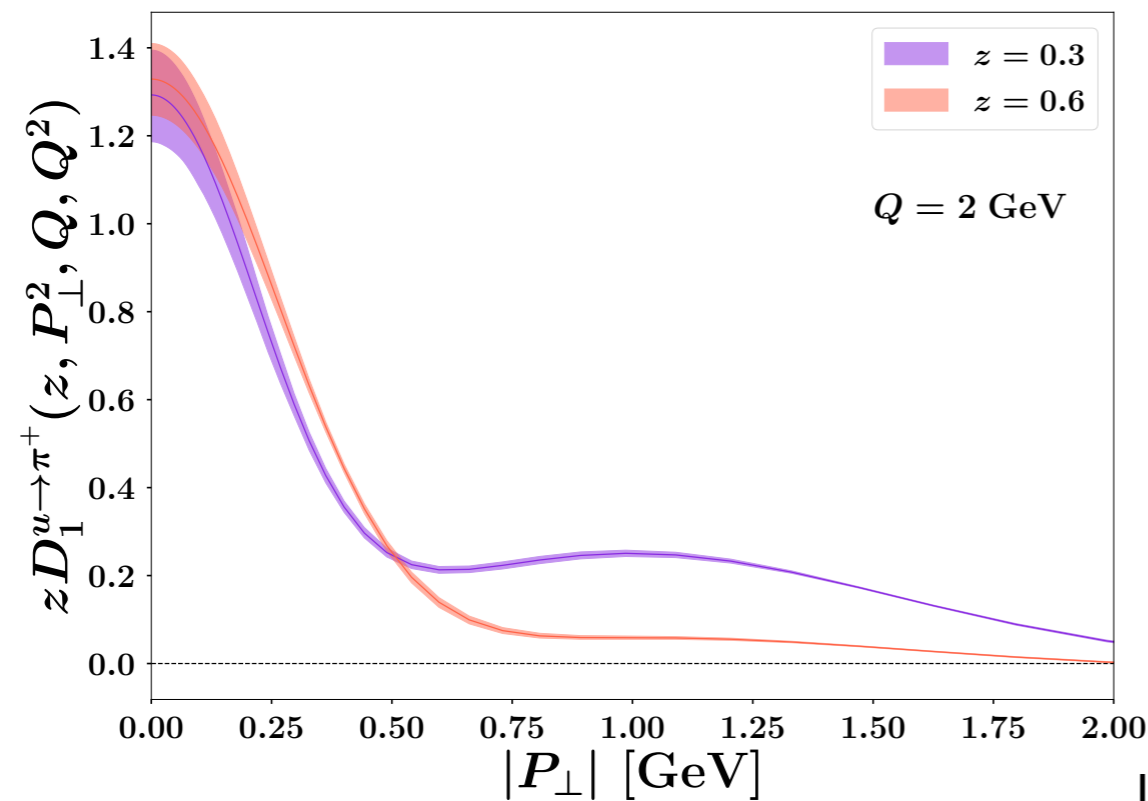
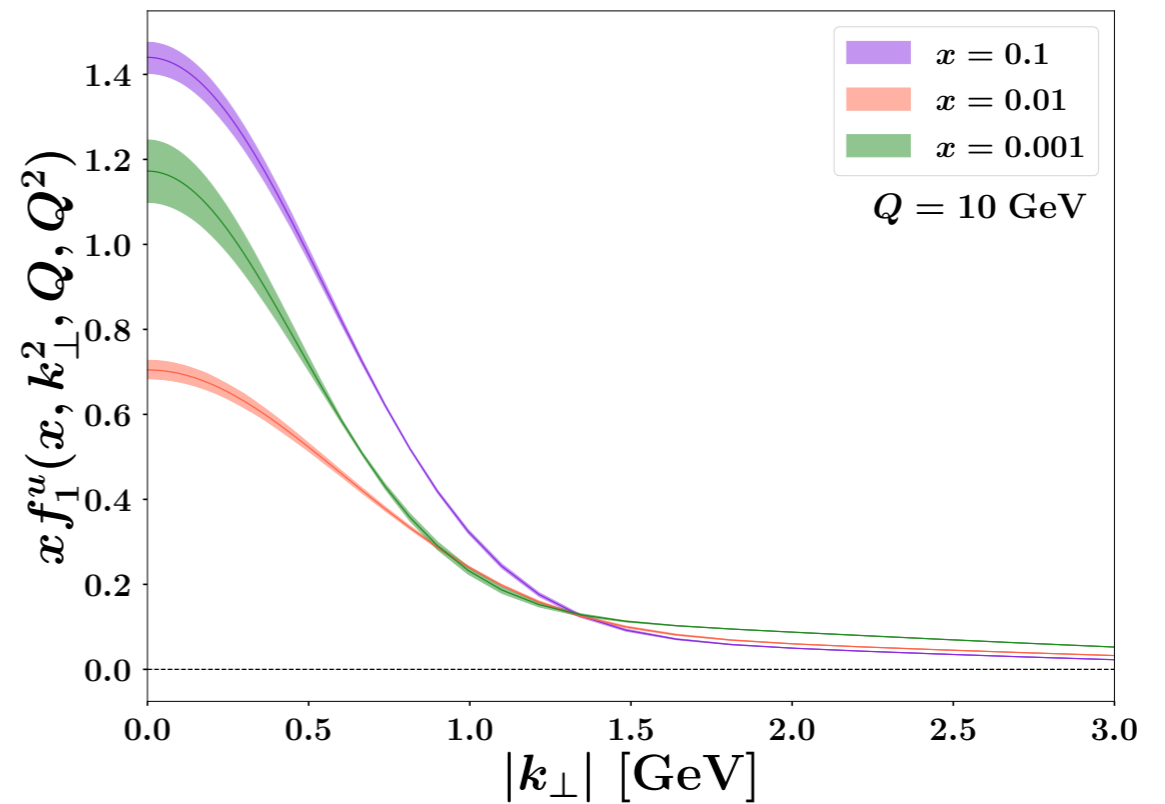
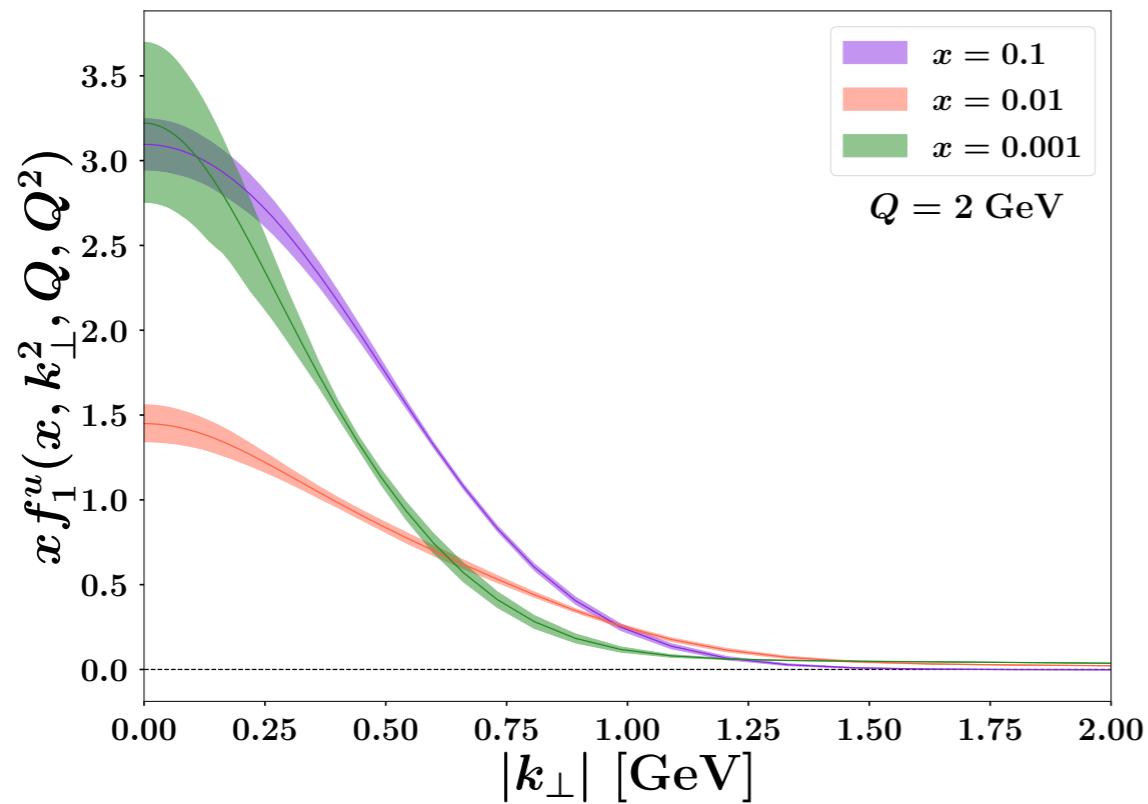
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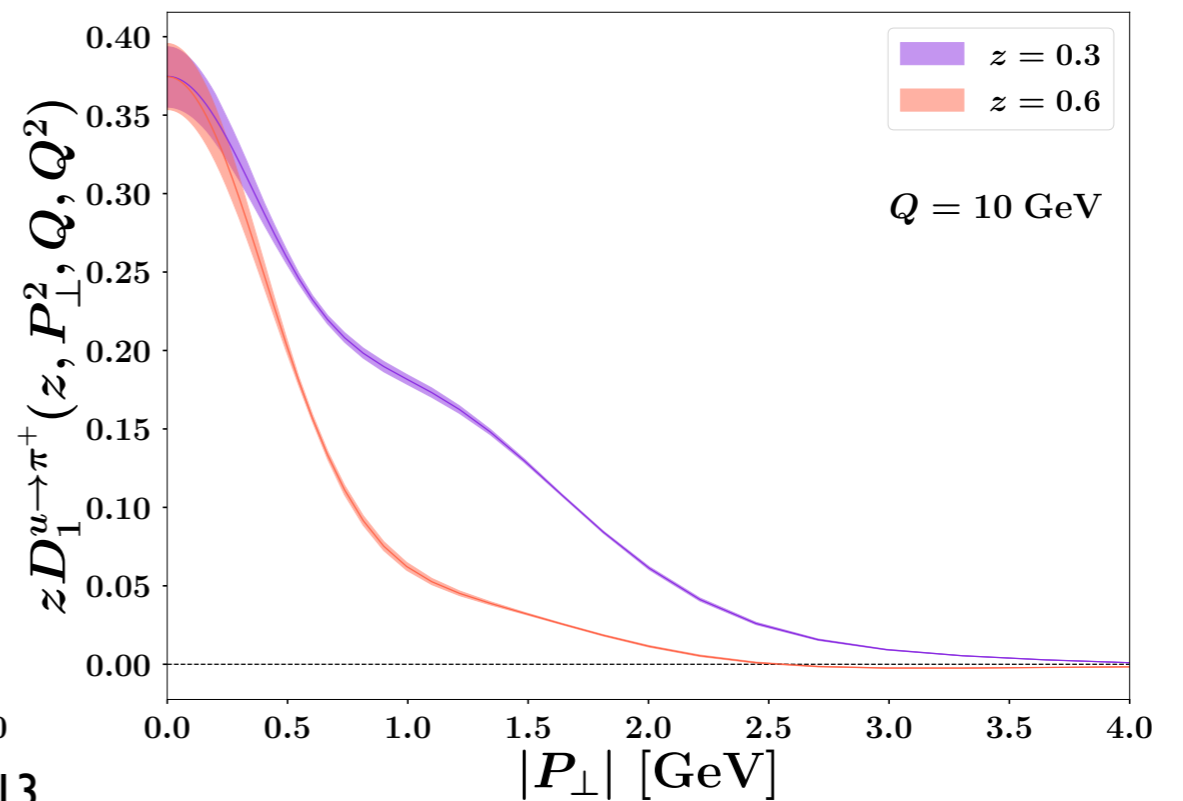


- $\lambda \sim 2$: weighted Gaussian important
- $\lambda_2 \neq 0$: third Gaussian non-negligible
- g_2 very small standard deviation
- correlation matrix nearly diagonal

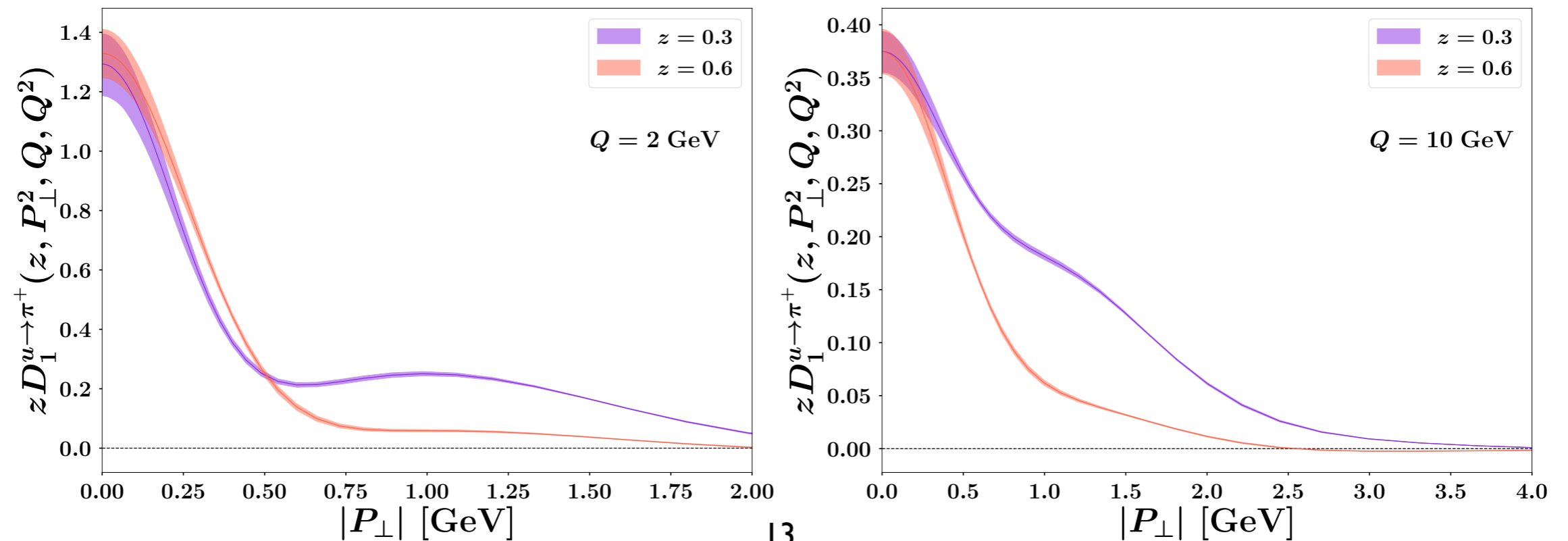
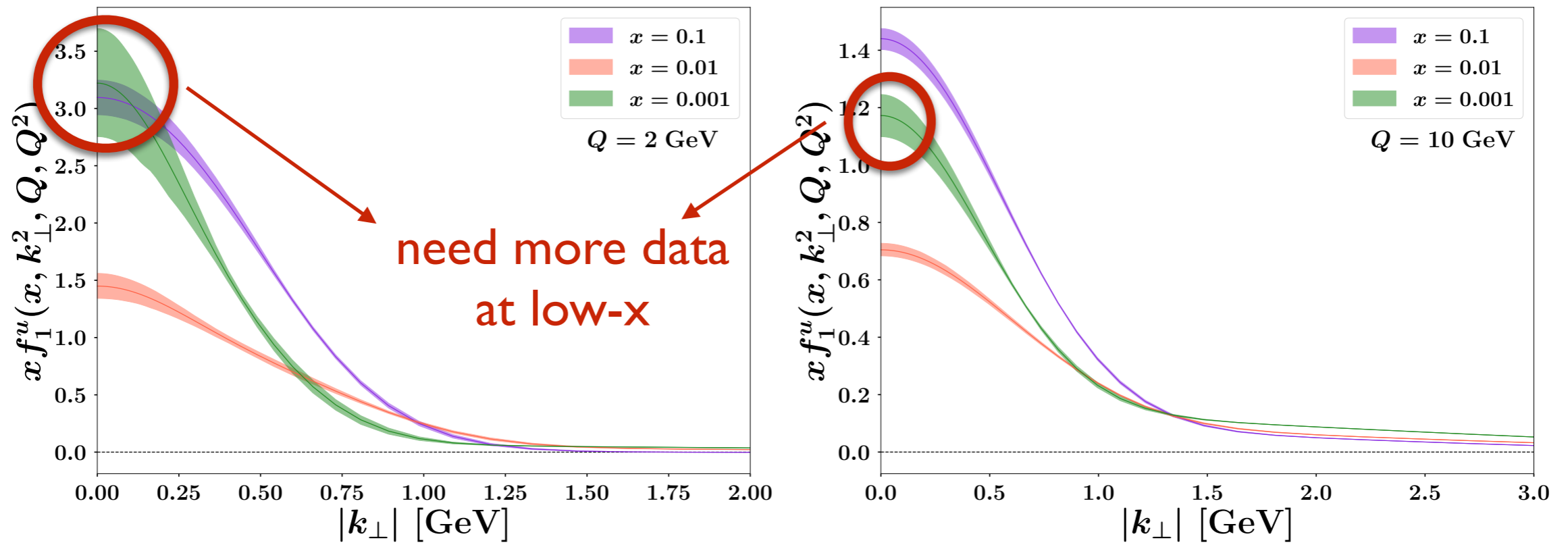
TMD PDFs and FFs



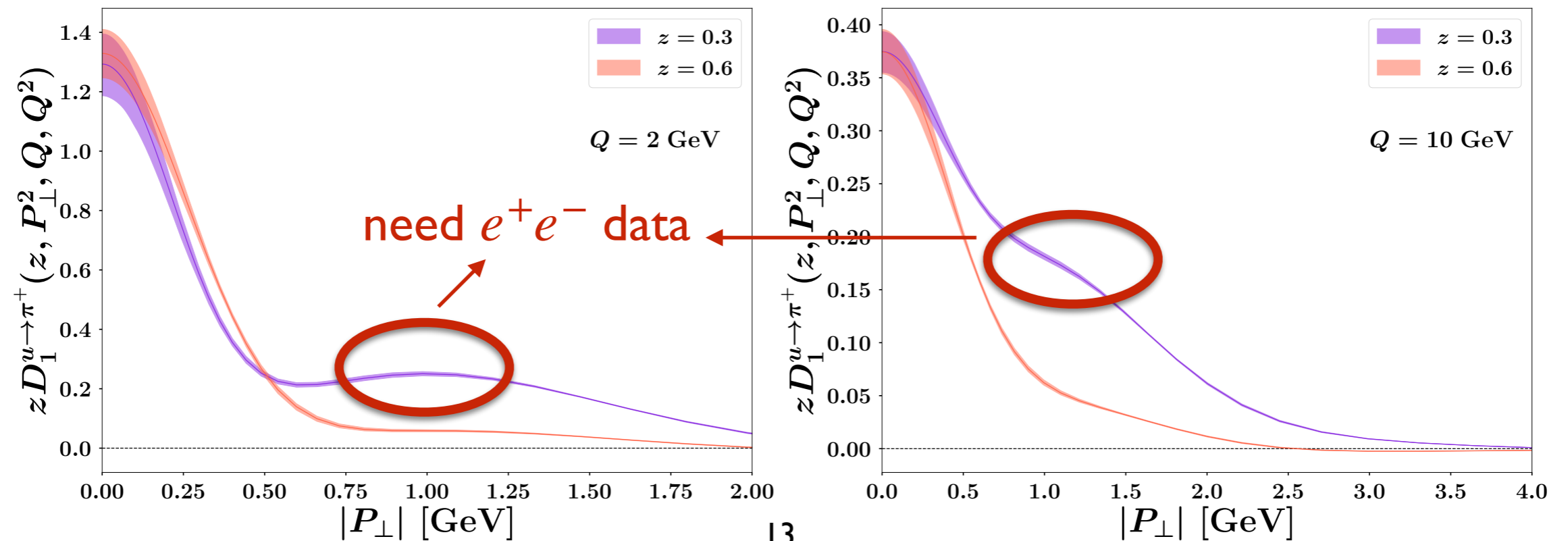
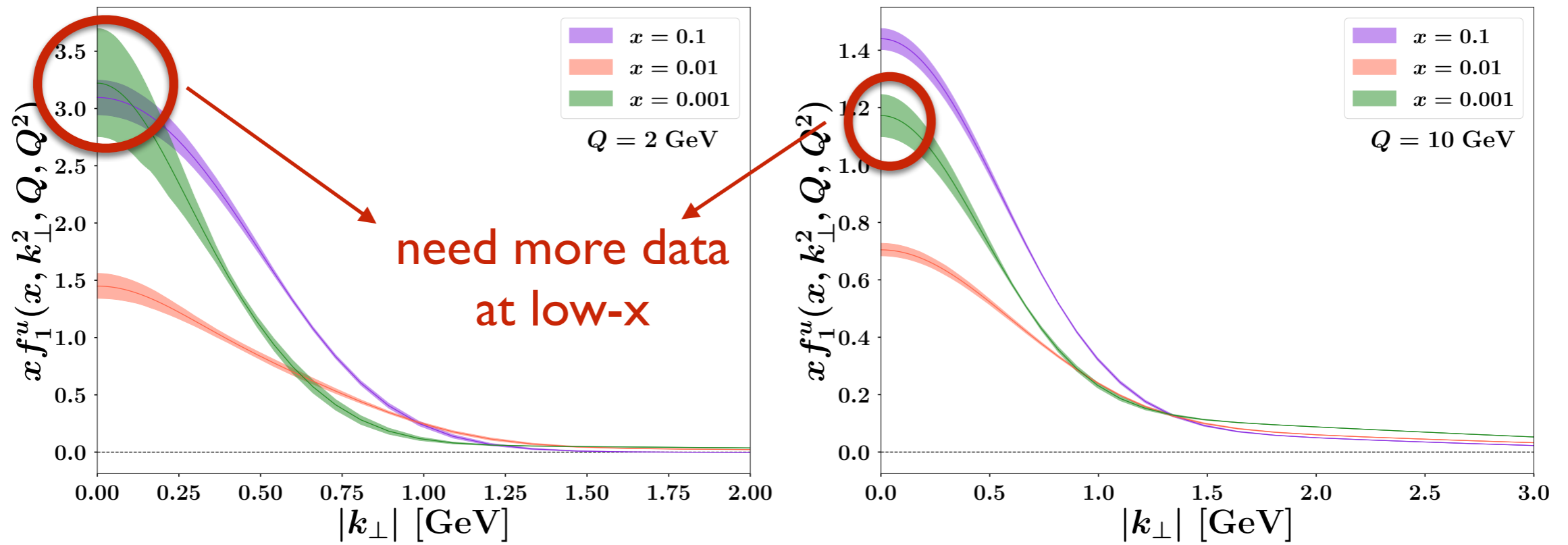
13



TMD PDFs and FFs



TMD PDFs and FFs



The Nanga Parbat framework



Nanga Parbat: a TMD fitting framework

Nanga Parbat is a fitting framework aimed at the determination of the non-perturbative component of TMD distributions.

Download

You can obtain NangaParbat directly from the github repository:

<https://github.com/MapCollaboration/NangaParbat>

For the last development branch you can clone the master code:

```
git clone git@github.com:MapCollaboration/NangaParbat.git
```

Conclusions

- Extraction of **TMD PDFs and FFs** from DY and SIDIS data at **N³LL(-)**
- 484 DY (Fermilab, LHC, RHIC) + 1547 SIDIS (COMPASS, Hermes): **2031 data points**
- **Normalisation factors** used for SIDIS data
- Very good description of entire dataset ($\chi^2 = 1.06$) **except for ATLAS data**
- **Code and TMD grids** available at the NangaParbat website
- **Plans for the future:**
 - improve perturbative accuracy
 - matching with fixed order
 - include theoretical uncertainties
 - flavour dependence

Backup

Normalisation of SIDIS multiplicities

Introduction of a normalisation prefactor

$$\text{PREFACTOR}(x, z, Q) = \frac{\frac{d\sigma^h}{dx dQ^2 dz} \Big|_{\text{nonmix.}}}{\int W d^2 q_T}$$

$$\frac{d\sigma^h}{dx dQ^2 dz} \Big|_{O(\alpha_S)} = \sigma_0 \sum_{f, f'} \frac{e_f^2}{z^2} (\delta_{f'f} + \delta_{f'g}) \frac{\alpha_S}{\pi} \left\{ [D_1^{h/f'} \otimes C_1^{f'f} \otimes f_1^{f/N}](x, z, Q) \right\} \Big|_{\text{nonmix.}}$$

$$\int W \Big|_{O(\alpha_S)} = \sigma_0 \sum_{f, f'} \frac{e_f^2}{z^2} (\delta_{f'f} + \delta_{f'g}) \frac{\alpha_S}{\pi} [D_1^{h/f'} \otimes C_{\text{TMD}}^{f'f} \otimes f_1^{f/N}](x, z, Q)$$

Independent of the fitting parameters!!

Non-mixed terms in collinear SIDIS cross section

$$\frac{d\sigma^h}{dx dQ^2 dz} \Big|_{O(\alpha_s^1)} = \sigma_0 \sum_{ff'} \frac{e_f^2}{z^2} (\delta_{f'f} + \delta_{f'g}) \frac{\alpha_s}{\pi} \left\{ \left[D_1^{h/f'} \otimes C_1^{f'f} \otimes f_1^{f/N} \right] (x, z, Q) \right. \\ \left. + \frac{1-y}{1+(1-y)^2} \left[D_1^{h/f'} \otimes C_L^{f'f} \otimes f_1^{f/N} \right] (x, z, Q) \right\},$$

$$C_1^{qq} = \frac{C_F}{2} \left\{ -8\delta(1-x)\delta(1-z) \right. \\ \left. + \delta(1-x) \left[P_{qq}(z) \ln \frac{Q^2}{\mu_F^2} + L_1(z) + L_2(z) + (1-z) \right] \right. \\ \left. + \delta(1-z) \left[P_{qq}(x) \ln \frac{Q^2}{\mu^2} + L_1(x) - L_2(x) + (1-x) \right] \right. \\ \left. + 2 \frac{1}{(1-x)_+} \frac{1}{(1-z)_+} \frac{1+z}{(1-x)_+} - \frac{1+x}{(1-z)_+} + 2(1+xz) \right\},$$

Experimental uncertainties

$$m_i \pm \sigma_{i,\text{stat}} \pm \sigma_{i,\text{unc}} \pm \sigma_{i,\text{corr}}^{(1)} \pm \dots \pm \sigma_{i,\text{corr}}^{(k)}$$

uncorrelated

correlated

additive

multiplicative

$$\chi^2 = \sum_{i,j=1}^n (m_i - t_i) V_{ij}^{-1} (m_j - t_j)$$

$$\sigma_{i,\text{corr}}^{(l)} \equiv \delta_{i,\text{corr}}^{(l)} m_i$$

covariance matrix

$$V_{ij} = s_i^2 \delta_{ij} + \left(\sum_{l=1}^{k_a} \delta_{i,\text{add}}^{(l)} \delta_{j,\text{add}}^{(l)} + \sum_{l=1}^{k_m} \delta_{i,\text{mult}}^{(l)} \delta_{j,\text{mult}}^{(l)} \right) m_i m_j$$

χ^2 chisquare

systematic shift

$$d_i = \sum_{\alpha=1}^k \lambda_{\alpha} \sigma_{i,\text{corr}}^{(\alpha)}$$

shift

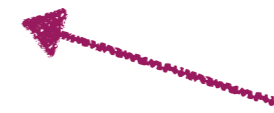


$$\bar{t}_i = t_i + d_i$$

shifted prediction

$$\frac{\partial \chi^2}{\partial \lambda_{\alpha}} = 0$$

nuisance parameters



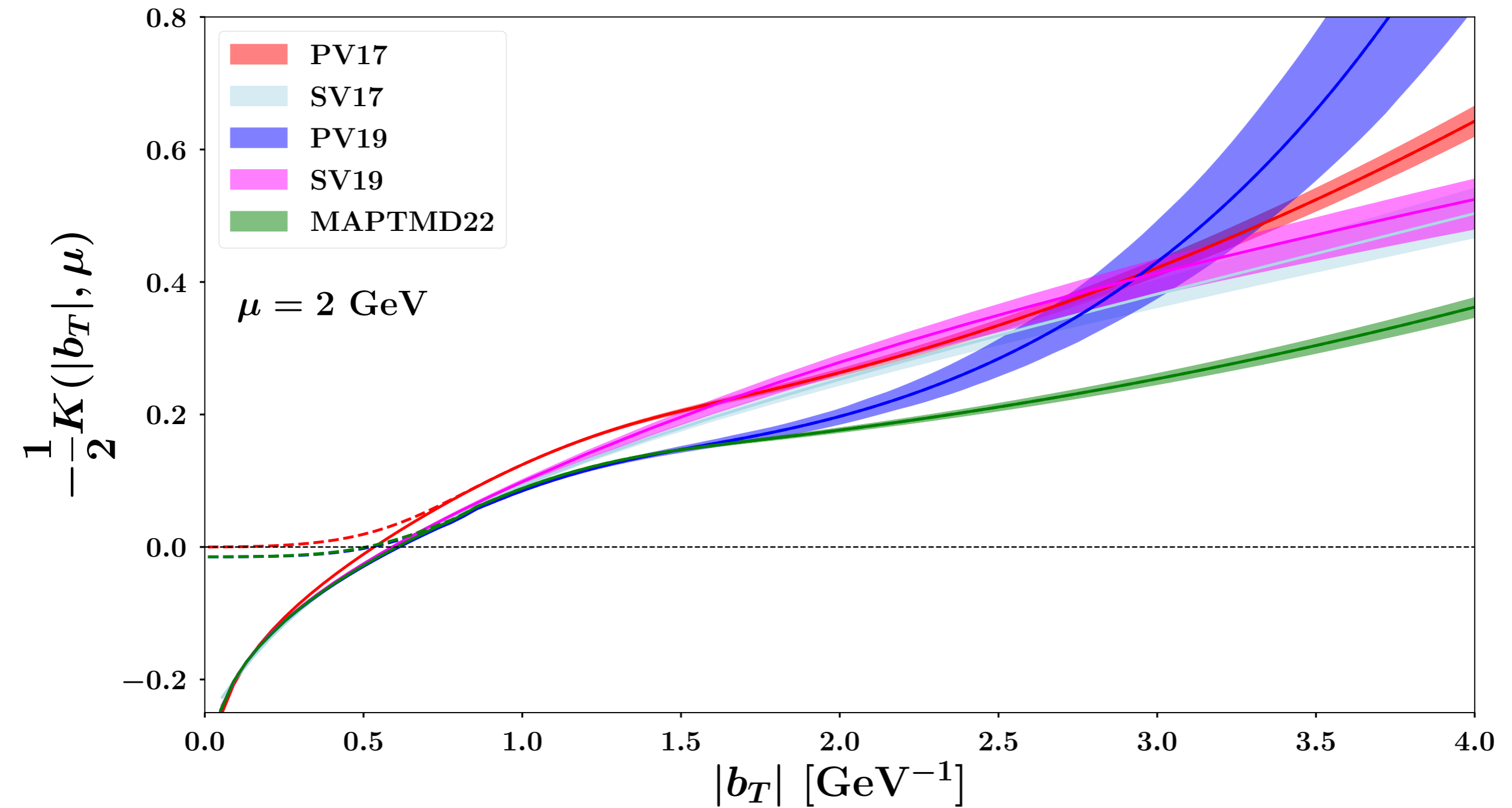
$$\chi^2 = \sum_{i=1}^n \left(\frac{m_i - \bar{t}_i}{s_i} \right)^2 + \sum_{\alpha=1}^k \lambda_{\alpha}^2$$

recover the form of the uncorrelated definition

penalty term



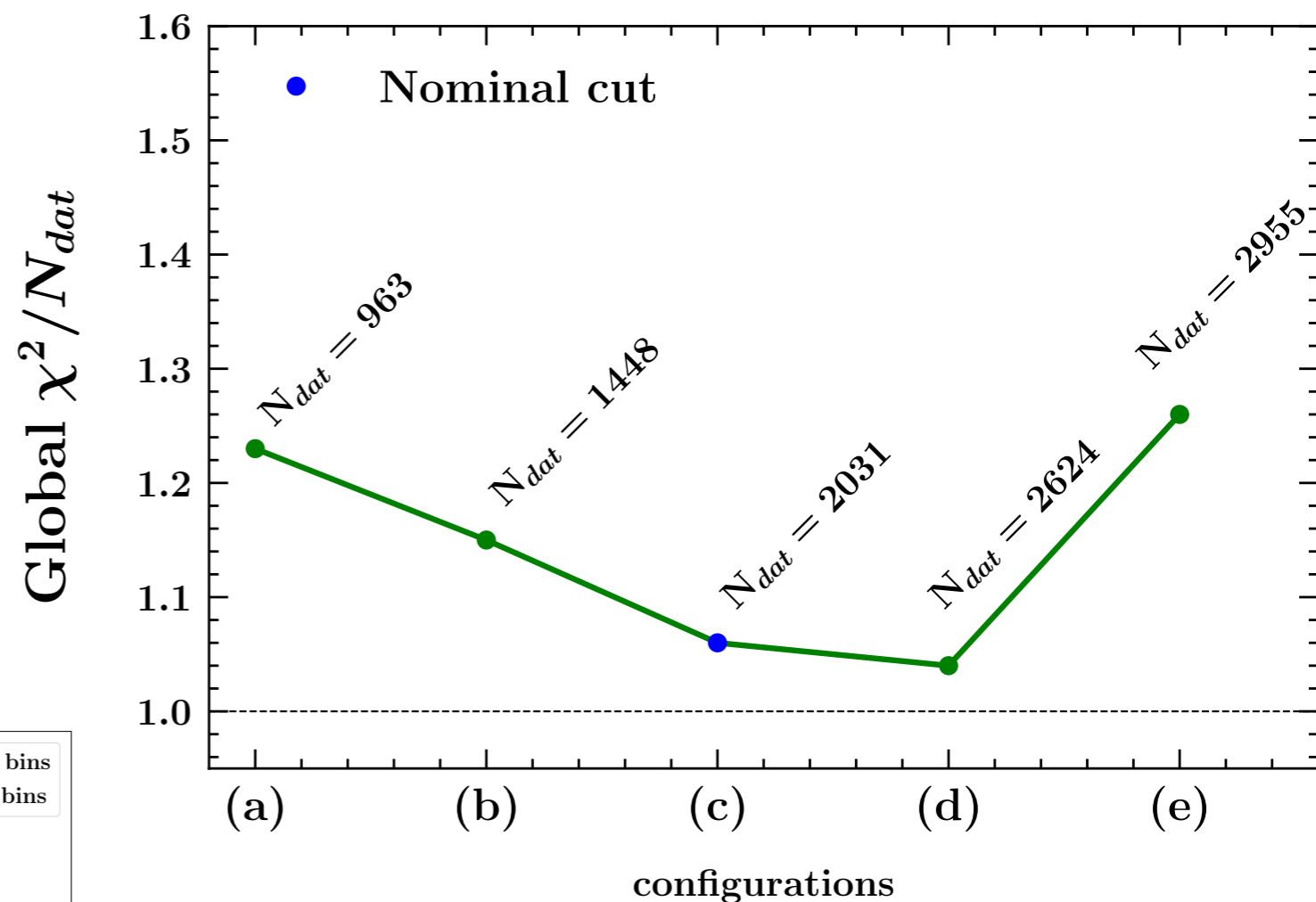
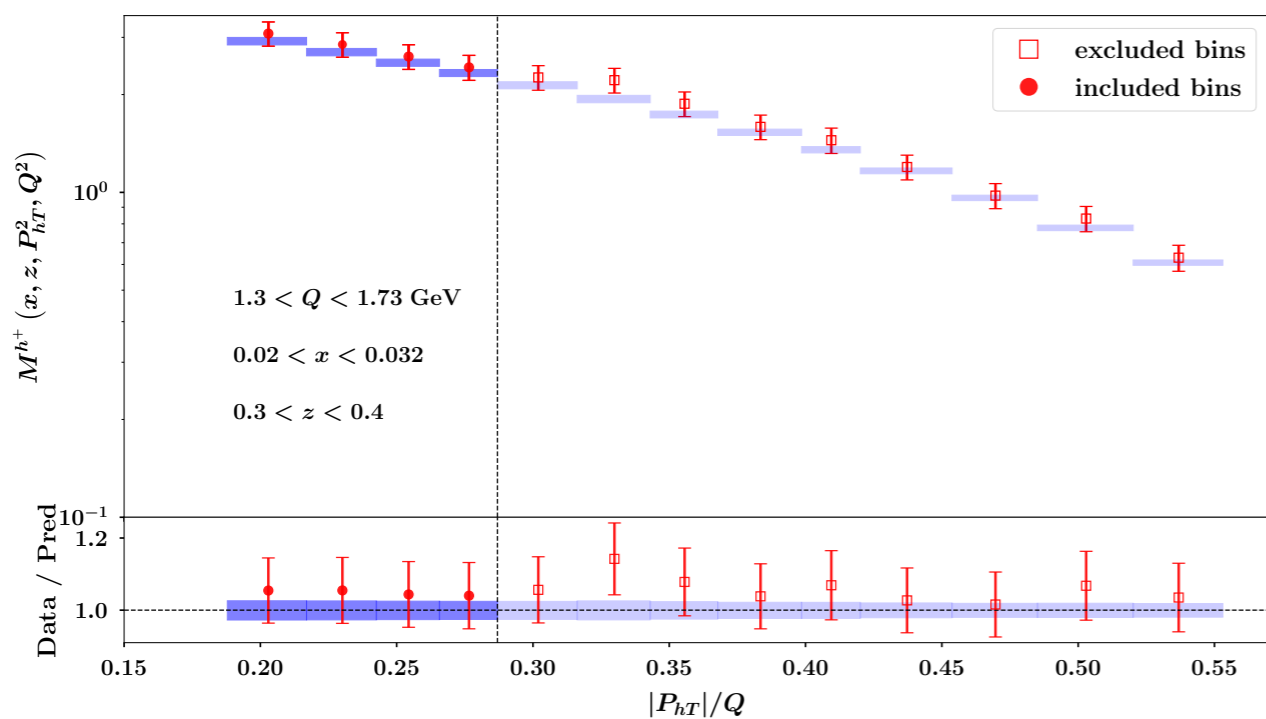
Collins-Soper kernel



Different SIDIS cuts

$$P_{hT}|_{max} = \min[\min[0.2Q, 0.5zQ] + 0.3 \text{ GeV}, zQ]$$

- (a) $c_1 = 0.4, c_2 = 0.4, c_3 = 0$
- (b) $c_1 = 0.15, c_2 = 0.4, c_3 = 0.2$
- (c) $c_1 = 0.2, c_2 = 0.5, c_3 = 0.3$ (baseline)
- (d) $c_1 = 0.2, c_2 = 0.6, c_3 = 0.4$
- (e) $c_1 = 0.2, c_2 = 0.7, c_3 = 0.5$



Different logarithmic orders

Data set	N ³ LL ⁻		NNLL		NLL	
	N_{dat}	$\langle\chi^2\rangle \pm \delta\langle\chi^2\rangle$	N_{dat}	$\langle\chi^2\rangle \pm \delta\langle\chi^2\rangle$	N_{dat}	$\langle\chi^2\rangle \pm \delta\langle\chi^2\rangle$
ATLAS	72	5.01 ± 0.26	/	/	/	/
PHENIX 200	2	3.26 ± 0.31	2	0.81 ± 0.11	/	/
STAR 510	7	1.16 ± 0.04	7	0.99 ± 0.03	/	/
Other sets	170	0.83 ± 0.01	170	2.37 ± 0.11	/	/
DY collider	251	2.06 ± 0.07	179	2.3 ± 0.1	/	/
E772	53	2.48 ± 0.12	53	2.05 ± 0.22	/	/
Other sets	180	0.87 ± 0.04	180	0.71 ± 0.04	180	0.81 ± 0.04
DY fixed-target	233	1.24 ± 0.04	233	1.01 ± 0.05	180	0.81 ± 0.04
HERMES	344	0.71 ± 0.04	344	1.1 ± 0.06	344	0.51 ± 0.02
COMPASS	1203	0.95 ± 0.02	1203	0.6 ± 0.06	1203	0.41 ± 0.01
SIDIS	1547	0.89 ± 0.02	1547	0.71 ± 0.05	1547	0.43 ± 0.01
Total	2031	1.08 ± 0.01	1959	0.89 ± 0.01	1727	0.47 ± 0.01