GTMDs & Wigner functions

25 years

Shohini Bhattacharya

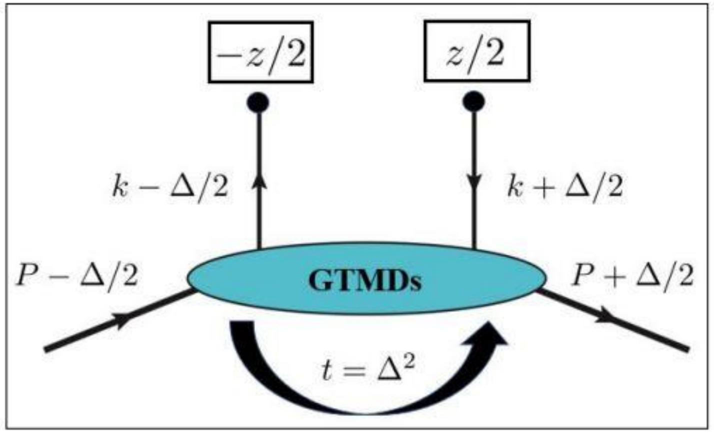
BNL

30 August 2022

Outline

- Generalized TMDs (GTMDs)
- Wigner functions
- Observables for GTMDs: State of the art
- Summary

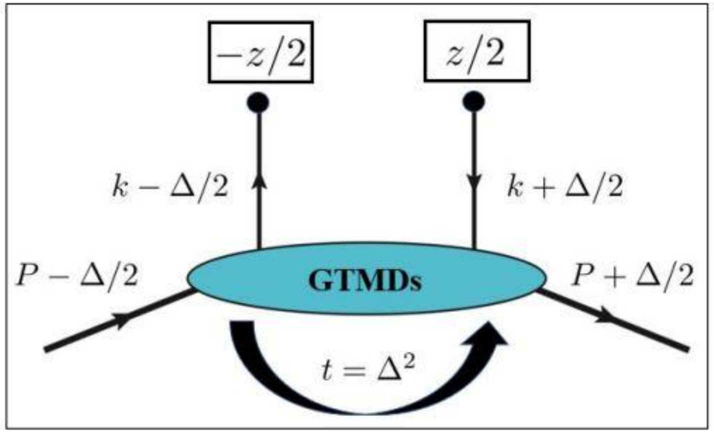
Generalized **T**ransverse **M**omentum dependent **D**istributions (GTMDs)



Definition of a (quark) GTMD correlator:

$$W^{q[\Gamma]}_{\lambda,\lambda'} = \frac{1}{2}\int \frac{dz^- d^2\vec{z}_\perp}{(2\pi)^3}\, e^{ik.z} < p', \lambda' | \bar{\psi}^q(-\tfrac{z}{2})\,\Gamma\,\mathcal{W}(-\tfrac{z}{2},\tfrac{z}{2})\psi^q(\tfrac{z}{2})|p,\lambda > \Big|_{z^+=0}$$

Generalized **T**ransverse **M**omentum dependent **D**istributions (GTMDs)



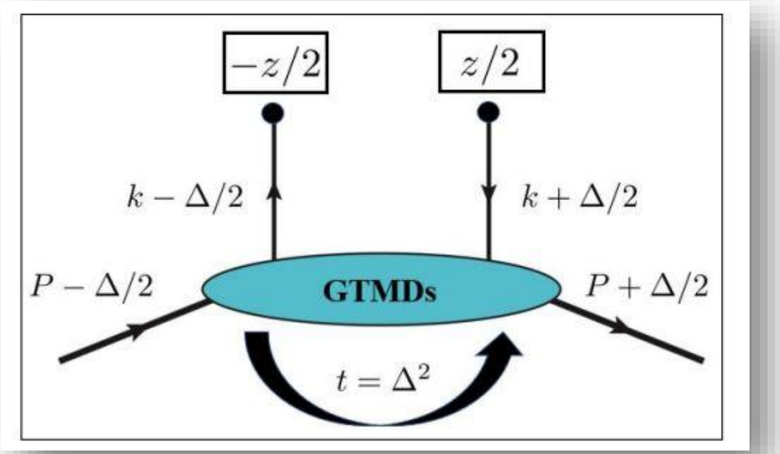
Definition of a (quark) GTMD correlator:

$$W^{q[\Gamma]}_{\lambda,\lambda'} = \frac{1}{2}\int \frac{dz^- d^2\vec{z}_\perp}{(2\pi)^3}\, e^{ik.z} < p',\lambda'|\bar{\psi}^q(-\tfrac{z}{2})\,\Gamma\,\mathcal{W}(-\tfrac{z}{2},\tfrac{z}{2})\psi^q(\tfrac{z}{2})|p,\lambda > \Big|_{z^+=0}$$

Parameterization of correlator through GTMDs:

$$\boxed{X^q(x,\xi,\vec{k}^2_\perp,\vec{\Delta}^2_\perp,\vec{k}_\perp\cdot\vec{\Delta}_\perp)}$$

Generalized Transverse Momentum dependent Distributions (GTMDs)



Definition of a (quark) GTMD correlator:

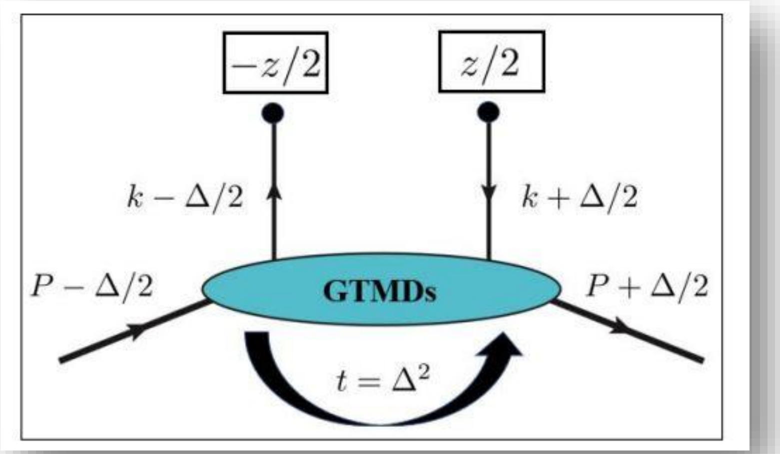
$$W^{q[\Gamma]}_{\lambda,\lambda'} = \frac{1}{2}\int \frac{dz^- d^2\vec{z}_\perp}{(2\pi)^3}\, e^{ik.z} < p',\lambda'|\bar{\psi}^q(-\tfrac{z}{2})\,\Gamma\,\mathcal{W}(-\tfrac{z}{2},\tfrac{z}{2})\psi^q(\tfrac{z}{2})|p,\lambda > \Big|_{z^+=0}$$

Parameterization of correlator through GTMDs:

$$\boxed{X^q(x,\xi,\vec{k}_\perp^2,\vec{\Delta}_\perp^2,\vec{k}_\perp\cdot\vec{\Delta}_\perp)}$$

x : **"average" longitudinal momentum fraction of quark**

Generalized Transverse Momentum dependent Distributions (GTMDs)



Definition of a (quark) GTMD correlator:

$$W^{q[\Gamma]}_{\lambda,\lambda'} = \frac{1}{2}\int \frac{dz^- d^2\vec{z}_\perp}{(2\pi)^3}\, e^{ik.z} < p',\lambda'|\bar{\psi}^q(-\tfrac{z}{2})\,\Gamma\,\mathcal{W}(-\tfrac{z}{2},\tfrac{z}{2})\psi^q(\tfrac{z}{2})|p,\lambda > \Big|_{z^+=0}$$

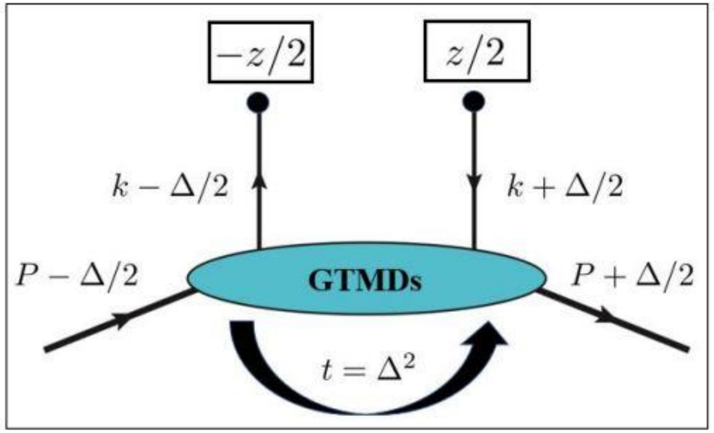
Parameterization of correlator through GTMDs:

$$\boxed{X^q(x,\xi,\vec{k}^2_\perp,\vec{\Delta}^2_\perp,\vec{k}_\perp\cdot\vec{\Delta}_\perp)}$$

x : "average" longitudinal momentum fraction of quark

$\xi = \frac{p^+ - p'^+}{p^+ + p'^+} = -\frac{\Delta^+}{2P^+}$: longitudinal momentum transfer to nucleon

Generalized Transverse Momentum dependent Distributions (GTMDs)



Definition of a (quark) GTMD correlator:

$$W^{q[\Gamma]}_{\lambda,\lambda'} = \frac{1}{2}\int \frac{dz^- d^2\vec{z}_\perp}{(2\pi)^3}\, e^{ik.z} < p',\lambda'|\bar{\psi}^q(-\tfrac{z}{2})\,\Gamma\,\mathcal{W}(-\tfrac{z}{2},\tfrac{z}{2})\psi^q(\tfrac{z}{2})|p,\lambda > \Big|_{z^+=0}$$

Parameterization of correlator through GTMDs:

$$\boxed{X^q(x,\xi,\vec{k}^2_\perp,\vec{\Delta}^2_\perp,\vec{k}_\perp\cdot\vec{\Delta}_\perp)}$$

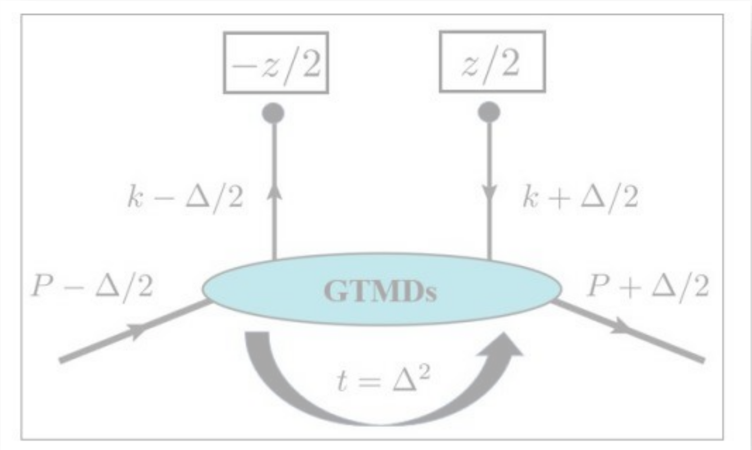
$\Delta_\perp$: transverse momentum transfer to nucleon

x : "average" longitudinal momentum fraction of quark

$\vec{k}_\perp$: "average" transverse momentum of quark

$\xi = \frac{p^+ - p'^+}{p^+ + p'^+} = -\frac{\Delta^+}{2P^+}$: longitudinal momentum transfer to nucleon

Generalized Transverse Momentum dependent Distributions (GTMDs)



Definition of a (quark) GTMD correlator:

$$W^{q[\Gamma]}_{\lambda,\lambda'} = \frac{1}{2}\int \frac{dz^- d^2\vec{z}_\perp}{(2\pi)^3}\, e^{ik.z} < p',\lambda' | \bar{\psi}^q(-\tfrac{z}{2})\,\Gamma\,\mathcal{W}(-\tfrac{z}{2},\tfrac{z}{2})\psi^q(\tfrac{z}{2})|p,\lambda > \Big|_{z^+=0}$$

General results:

i. **16 leading-twist GTMDs for quarks (Meissner, Metz, Schlegel, arXiv: 0906.5323)**

ii. **16 leading-twist GTMDs for gluons (Lorcé, Pasquini, arXiv: 1307.4497)**

iii. **GTMDs are complex functions**

Why are GTMDs interesting?

Why are GTMDs interesting?

GTMDs are the “Mother Functions”

(Meissner, Metz, Schlegel, 2009)

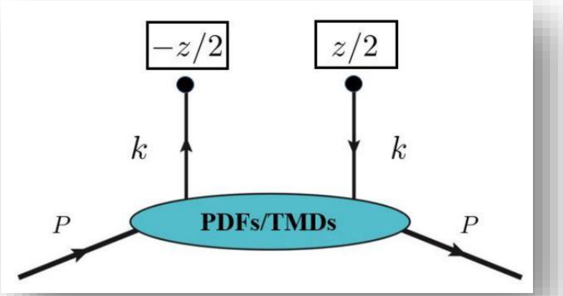
GTMDs $(x, \vec{k}_\perp, \Delta)$

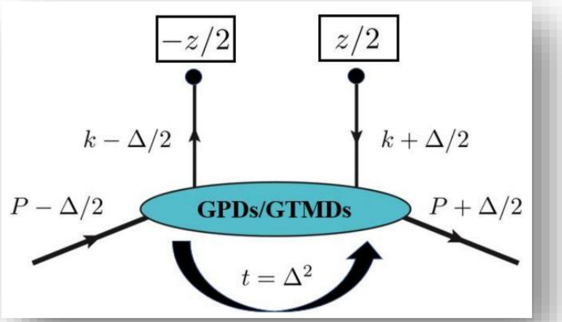
$\Delta = 0$ $\quad\quad$ $\int d^2\vec{k}_\perp$

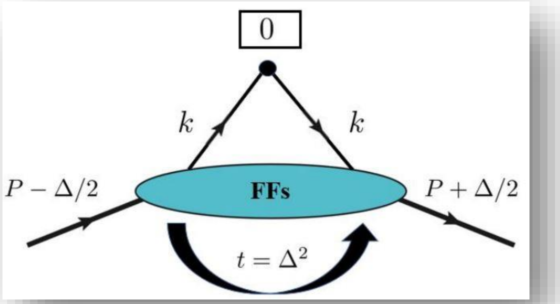
TMDs $(x, \vec{k}_\perp)$ $\quad\quad$ **GPDs** (x, Δ)

$\int d^2\vec{k}_\perp$ $\quad\quad$ $\Delta = 0$ $\quad\quad$ $\int dx$

PDFs (x) $\quad\quad$ **FFs** (Δ)







Why are GTMDs interesting?

GTMDs are the "Mother Functions"

GTMDs contain physics beyond TMDs & GPDs

(Meissner, Metz, Schlegel, 2009)

GTMDs $(x, \vec{k}_\perp, \Delta)$

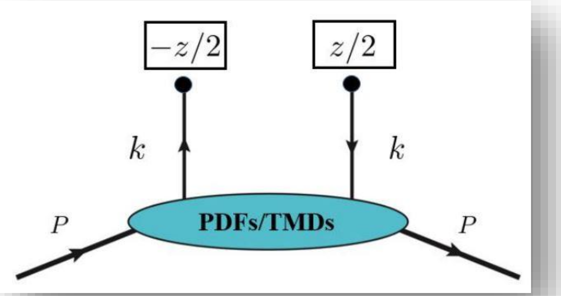
$\Delta = 0$ → **TMDs** $(x, \vec{k}_\perp)$

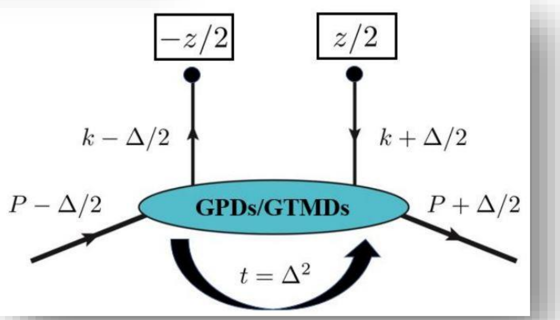
$\int d^2\vec{k}_\perp$ → **GPDs** (x, Δ)

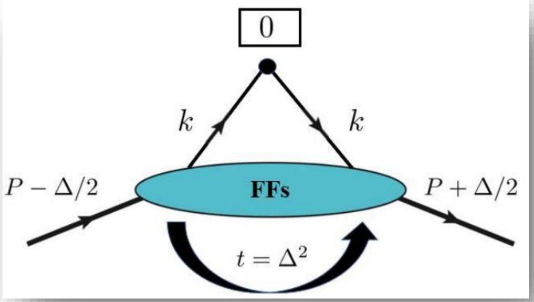
TMDs $(x, \vec{k}_\perp)$ — $\int d^2\vec{k}_\perp$ → **PDFs** (x)

GPDs (x, Δ) — $\Delta = 0$ → **PDFs** (x)

GPDs (x, Δ) — $\int dx$ → **FFs** (Δ)







Why are GTMDs interesting?

Connection to Wigner functions

Wigner Distribution $(x, \vec{k}_\perp, \vec{b}_\perp)$ **(Belitsky, Ji, Yuan, 2003)**

2-D Fourier Transform $(\vec{\Delta}_\perp)$ ↑ $\xi = 0$

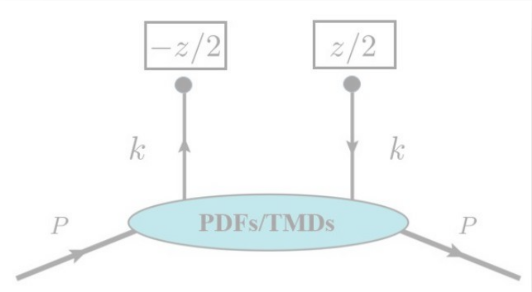
(Meissner, Metz, Schlegel, 2009) **GTMDs** $(x, \vec{k}_\perp, \Delta)$

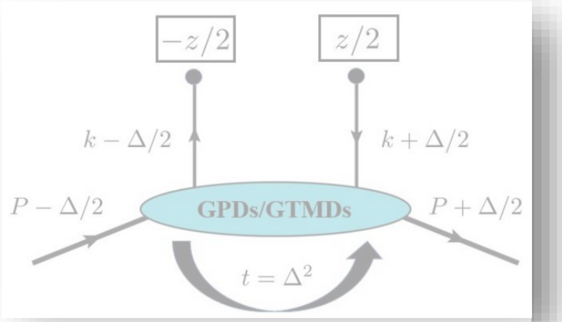
$\Delta = 0$ $\quad$ $\int d^2\vec{k}_\perp$

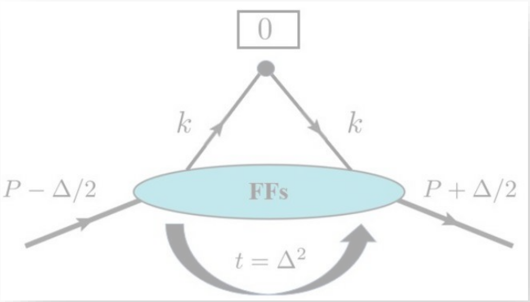
TMDs $(x, \vec{k}_\perp)$ $\quad$ **GPDs** (x, Δ)

$\int d^2\vec{k}_\perp$ $\quad$ $\Delta = 0$ $\quad$ $\int dx$

PDFs (x) $\quad$ **FFs** (Δ)







Why are GTMDs interesting?

Wigner functions & connection to parton Orbital Angular Momentum

- **Recap from NRQM:**

Expectation value of observables $\langle \mathcal{O} \rangle = \int dx \int dk \mathcal{O}(x,k) W(x,k)$

Why are GTMDs interesting?

Wigner functions & connection to parton Orbital Angular Momentum

- **Recap from NRQM:**

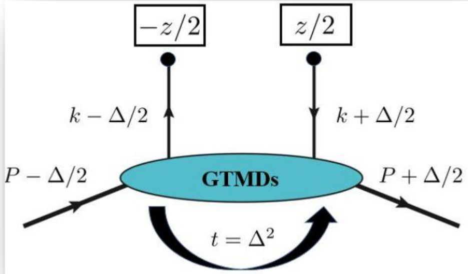
Expectation value of observables $\langle \mathcal{O} \rangle = \int dx \int dk \mathcal{O}(x,k) W(x,k)$

- **OAM as a moment of Wigner distribution** **: (Lorcé, Pasquini, 2011 / Hatta, 2011 / Ji, Xiong, Yuan, 2012)**

$$L_z^q = \int dx \int d^2k_\perp d^2b_\perp (\vec{b}_\perp \times \vec{k}_\perp)_z W^q (x, \vec{b}_\perp, \vec{k}_\perp)$$

Intuitive definition of OAM

Parameterization of a GTMD correlator **(Meissner, Metz, Schlegel, arXiv: 0906.5323):**

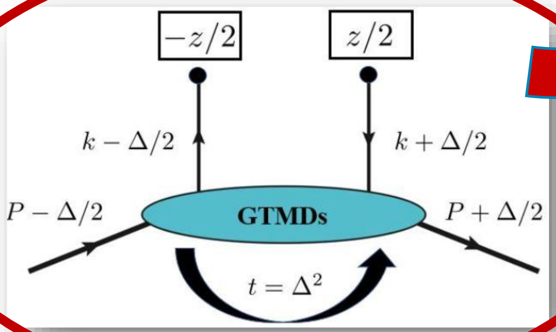


$$= \frac{1}{2M}\,\bar{u}(p',\lambda')\left[F_{1,1} + \frac{i\sigma^{i+}k_\perp^i}{P+}F_{1,2} + \frac{i\,\sigma^{i+}\Delta_\perp^i}{P+}F_{1,3} + \frac{i\sigma^{ij}k_\perp^i\Delta_\perp^j}{M^2}F_{1,4}\right]u(p,\lambda)$$

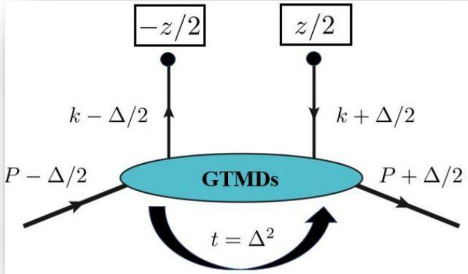
Same equation holds for gluons (Hatta, 1111.3547)

- **OAM as a moment of Wigner distribution/GTMD: (Lorcé, Pasquini, 2011 / Hatta, 2011 / Ji, Xiong, Yuan, 2012)**

$$L_z^q = \int dx \int d^2k_\perp d^2b_\perp (\vec{b}_\perp \times \vec{k}_\perp)_z \left\{ \int e^{i\vec{b}_\perp\cdot\vec{\Delta}_\perp} \right.$$



Parameterization of a GTMD correlator (Meissner, Metz, Schlegel, arXiv: 0906.5323):



$$= \frac{1}{2M}\,\bar{u}(p',\lambda')\left[\boldsymbol{F_{1,1}} + \frac{i\sigma^{i+}k_\perp^i}{P^+}\boldsymbol{F_{1,2}} + \frac{i\,\sigma^{i+}\Delta_\perp^i}{P^+}\boldsymbol{F_{1,3}} + \frac{i\sigma^{ij}k_\perp^i\Delta_\perp^j}{M^2}\boldsymbol{F_{1,4}}\right]u(p,\lambda)$$

Same equation holds for gluons (Hatta, 1111.3547)

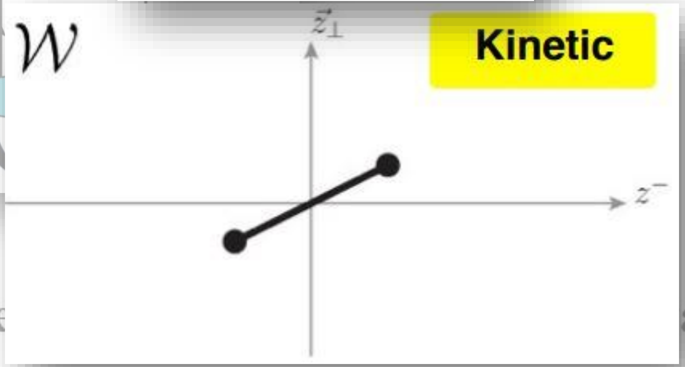
- **OAM as a moment of Wigner distribution/GTMD:** (Lorcé, Pasquini, 2011 / Hatta, 2011 / Ji, Xiong, Yuan, 2012)

$$L_z^{q,g} = -\int dx \int d^2\vec{k}_\perp \frac{\vec{k}_\perp^2}{M^2}\, \boldsymbol{F_{1,4}^{q,g}(x,\vec{k}_\perp^2)}$$

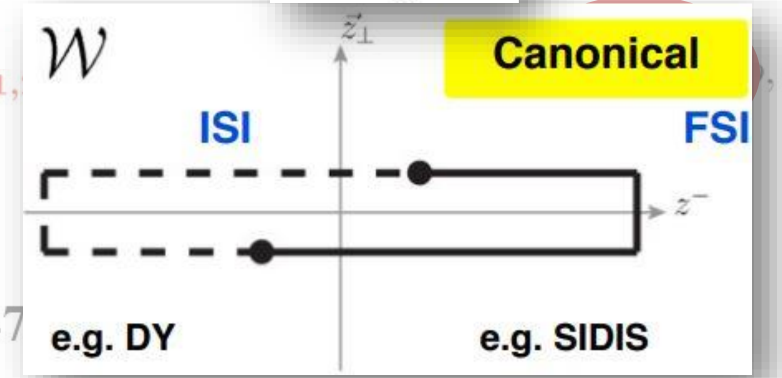
Relation between GTMD $F_{1,4}^{q,g}$ & OAM

Gauge-invariant extension

Ji, Xiong, Yuan, 2012



Hatta, 2011



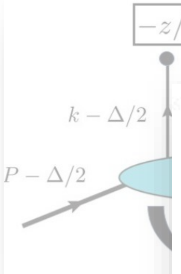
- **OAM as a moment of Wigner distribution/GTMD:** (Lorcé, Pasquini, 2011 / Hatta, 2011 / Ji, Xiong, Yuan, 2012)

$$\boxed{L_z^{q,g} = -\int dx \int d^2\vec{k}_\perp \frac{\vec{k}_\perp^2}{M^2} \boldsymbol{F_{1,4}^{q,g}(x, \vec{k}_\perp^2)}}$$

Relation between GTMD $F_{1,4}^{q,g}$ & OAM

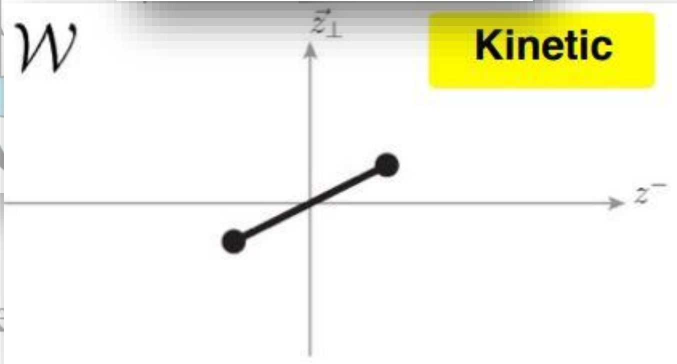
Gauge-invariant extension

Parameterization of a ... 23):

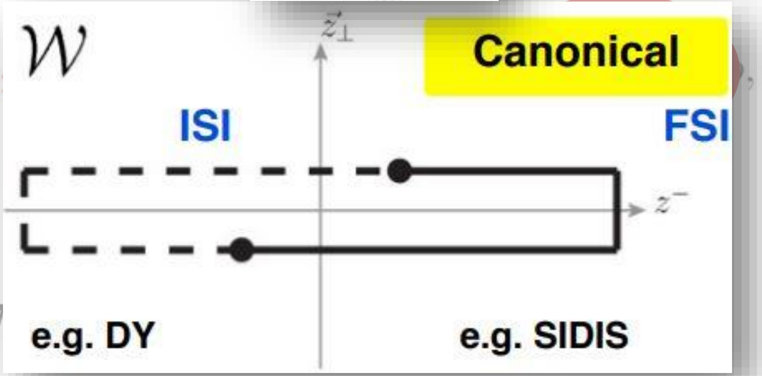


$+\ \frac{i\sigma^{i+}k_\perp^i}{P^+} F_{1,} \ldots, \lambda)$

Ji, Xiong, Yuan, 2012



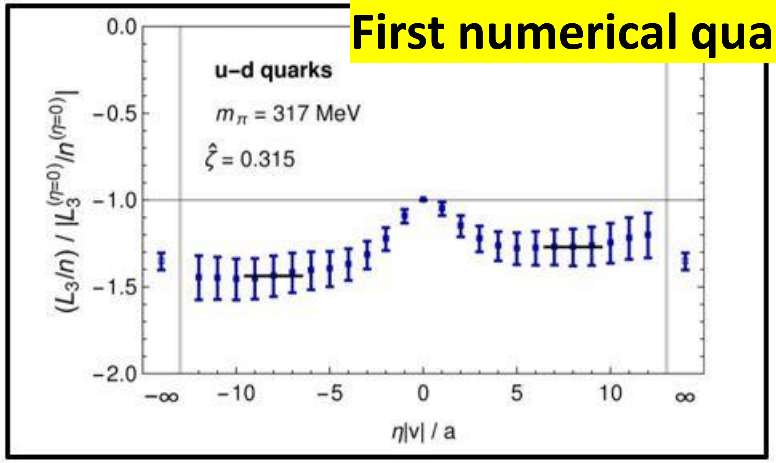
Hatta, 2011



Same e ... a, 1111.3547

- O ... Xiong, Yuan, 2012) ... OAM

First numerical quantification of differences between Ji & JM OAM



First lattice calculation of $L_{\rm JM}$ vs. $L_{\rm Ji}$
(Engelhardt, 1701.01536)

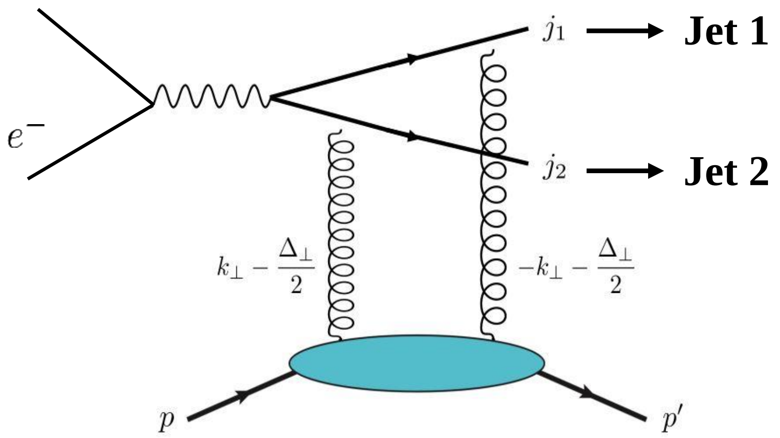
i. **Figure shows** $L^{u-d}_{\rm JM}/L^{u-d}_{\rm Ji}$

ii. **Significant numerical differences between** $L_{\rm JM}$ **&** $L_{\rm Ji}$

Observables for GTMDs: State of the art

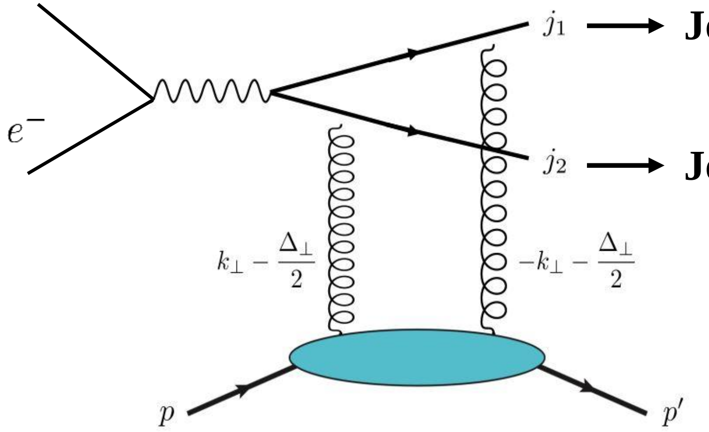
Observables for GTMDs

Exclusive dijet production in lepton-ion collisions at small-x (Hatta, Xiao, Yuan, arXiv: 1601.01585)



Observables for GTMDs

Exclusive dijet production in lepton-ion collisions at small-x (Hatta, Xiao, Yuan, arXiv: 1601.01585)



$j_1 \rightarrow$ **Jet 1**

$j_2 \rightarrow$ **Jet 2**

“Elliptic” Wigner distribution:

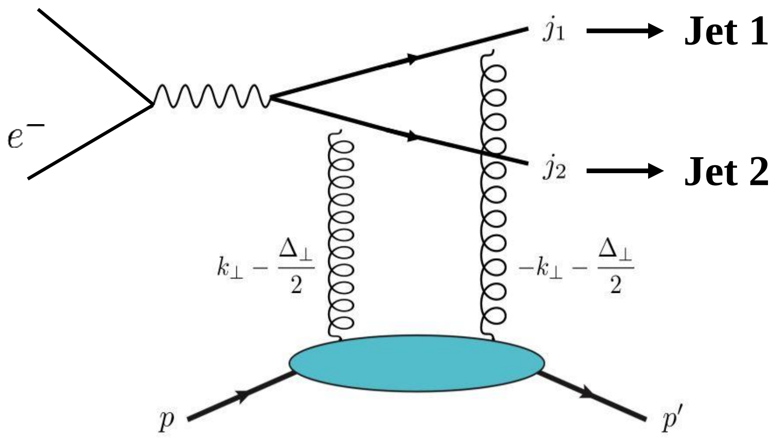
Symmetric part

$$W(x, \vec{k}_\perp, \vec{b}_\perp) \approx W_0(x, |\vec{k}_\perp|, |\vec{b}_\perp|) + 2\cos 2(\phi_k - \phi_b)\, W_1(x, |\vec{k}_\perp|, |\vec{b}_\perp|)$$

Elliptic part

Observables for GTMDs

Exclusive dijet production in lepton-ion collisions at small-x (Hatta, Xiao, Yuan, arXiv: 1601.01585)



"Elliptic" Wigner distribution:

$$W(x, \vec{k}_\perp, \vec{b}_\perp) \approx W_0(x, |\vec{k}_\perp|, |\vec{b}_\perp|) + 2\cos 2\,(\phi_k - \phi_b)\, W_1(x, |\vec{k}_\perp|, |\vec{b}_\perp|)$$

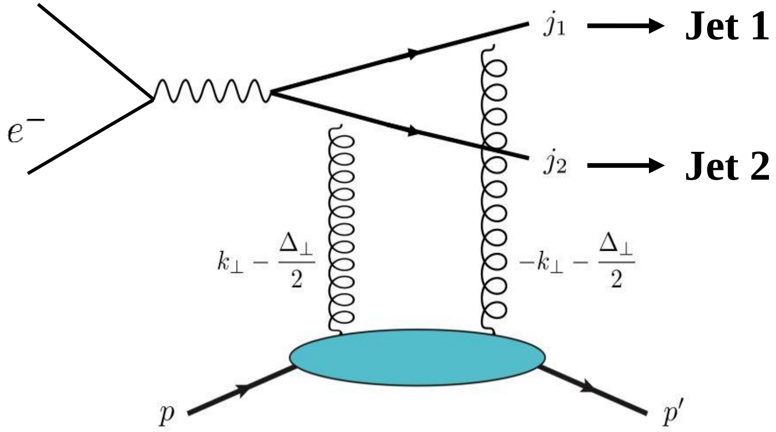
Main result:

$$\frac{d\sigma}{dy_1 dy_2 d^2\vec{\Delta}_\perp d^2\vec{P}_\perp} \propto z(1-z)[z^2 + (1-z)^2] \int d^2k_\perp d^2k'_\perp S(k_\perp, \Delta_\perp) S(k'_\perp, \Delta_\perp) \times \left[\frac{\vec{P}_\perp}{P_\perp^2 + \epsilon^2} - \frac{\vec{P}_\perp - \vec{k}_\perp}{(P_\perp - k_\perp)^2 + \epsilon^2}\right] \cdot \left[\frac{\vec{P}_\perp}{P_\perp^2 + \epsilon^2} - \frac{\vec{P}_\perp - \vec{k}'_\perp}{(P_\perp - k'_\perp)^2 + \epsilon^2}\right]$$

$$\approx d\sigma_0 + 2\cos 2\,(\phi_{P_\perp} - \phi_{\Delta_\perp}) d\tilde{\sigma}$$

Observables for GTMDs

Exclusive dijet production in lepton-ion collisions at small-x (Hatta, Xiao, Yuan, arXiv: 1601.01585)



"Elliptic" Wigner distribution:

$$W(x, \vec{k}_\perp, \vec{b}_\perp) \approx W_0(x, |\vec{k}_\perp|, |\vec{b}_\perp|) + 2\cos 2(\phi_k - \phi_b)\, W_1(x, |\vec{k}_\perp|, |\vec{b}_\perp|)$$

Main result:

$$\frac{d\sigma}{dy_1 dy_2 d^2\vec{\Delta}_\perp d^2\vec{P}_\perp} \propto z(1-z)[z^2 + (1-z)^2] \int d^2k_\perp d^2k'_\perp S(k_\perp, \Delta_\perp) S(k'_\perp, \Delta_\perp)$$

Cosine angular modulation

$$\left[\frac{\vec{P}_\perp}{P_\perp^2 + \epsilon^2} - \frac{\vec{P}_\perp - \vec{k}_\perp}{(P_\perp - k_\perp)^2 + \epsilon^2}\right] \cdot \left[\frac{\vec{P}_\perp}{P_\perp^2 + \epsilon^2} - \frac{\vec{P}_\perp - \vec{k}'_\perp}{(P_\perp - k'_\perp)^2 + \epsilon^2}\right]$$

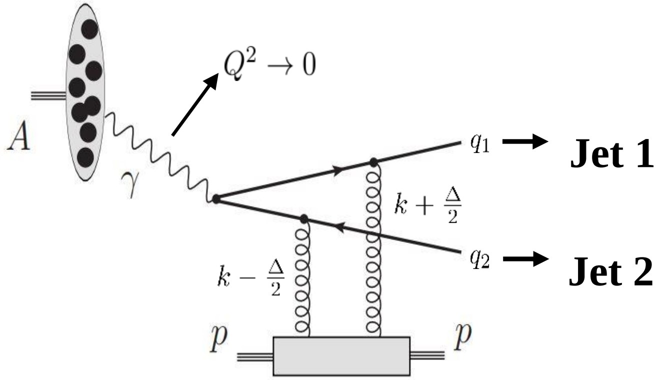
$$\approx d\sigma_0 + 2\cos 2(\phi_{P_\perp} - \phi_{\Delta_\perp})\, d\tilde{\sigma}$$

$$\vec{P}_\perp = \frac{1}{2}(\vec{j}_{2\perp} - \vec{j}_{1\perp})$$

Observables for GTMDs

Exclusive dijet production in lepton-ion collisions at small-x (Hatta, Xiao, Yuan, arXiv: 1601.01585)

Exclusive dijet production in ultra-peripheral collisions at small-x (Hagiwara et al., arXiv: 1706.01765)



Same cosine angular correlation observed in UPC

Main result:

$$\frac{d\sigma}{dy_1 dy_2 d^2\vec{\Delta}_\perp d^2\vec{P}_\perp} \propto z(1-z)[z^2+(1-z)^2]\int d^2k_\perp d^2k'_\perp S(k_\perp,\Delta_\perp)S(k'_\perp,\Delta_\perp)$$

Cosine angular modulation

$$\left[\frac{\vec{P}_\perp}{P_\perp^2+\epsilon^2} - \frac{\vec{P}_\perp - \vec{k}_\perp}{(P_\perp - k_\perp)^2+\epsilon^2}\right] \cdot \left[\frac{\vec{P}_\perp}{P_\perp^2+\epsilon^2} - \frac{\vec{P}_\perp - \vec{k}'_\perp}{(P_\perp - k'_\perp)^2+\epsilon^2}\right]$$

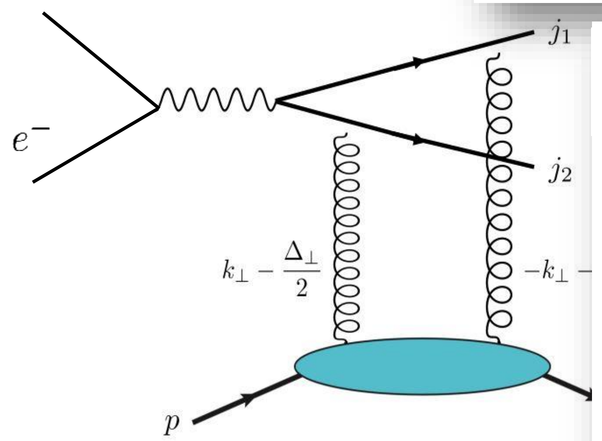
$$\approx d\sigma_0 + 2\cos 2(\phi_{P_\perp} - \phi_{\Delta_\perp})d\tilde{\sigma}$$

$$\vec{P}_\perp = \frac{1}{2}(\vec{j}_{2\perp} - \vec{j}_{1\perp})$$

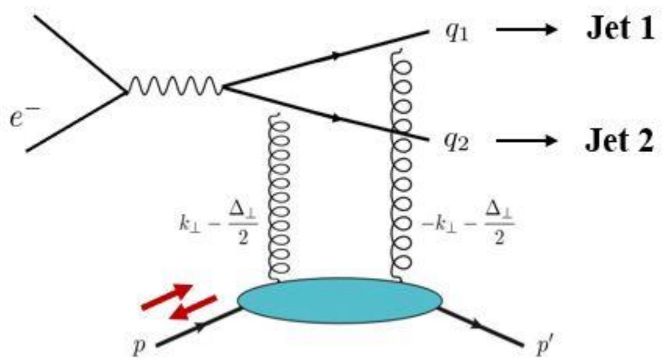
Observables for GTMDs

Exclusive dijet production in lepton-ion collisions at small-x (Hatta, Xiao, Yuan, arXiv: 1601.01585)

Coming up:



What happens if target is polarized?



arXiv: 1612.02438 (2016)

Hunting the Gluon Orbital Angular Momentum at the Electron-Ion Collider

Xiangdong Ji,[1,2] Feng Yuan,[3] and Yong Zhao[1,3]

Main result:

$$\frac{d\sigma}{dy_1 dy_2 d^2\vec{\Delta}_\perp d^2\vec{P}_\perp} \propto z(1-z)[z^2+(1-z)^2]\int d^2k_\perp d^2k'_\perp S(k_\perp,\Delta_\perp)S(k'_\perp,\Delta_\perp)$$

Cosine angular modulation

$$\frac{\vec{P}_\perp}{P_\perp^2+\epsilon^2} - \frac{\vec{P}_\perp - \vec{k}_\perp}{(P_\perp - k_\perp)^2+\epsilon^2}\Bigg] \cdot \Bigg[\frac{\vec{P}_\perp}{P_\perp^2+\epsilon^2} - \frac{\vec{P}_\perp - \vec{k}'_\perp}{(P_\perp - k'_\perp)^2+\epsilon^2}\Bigg]$$

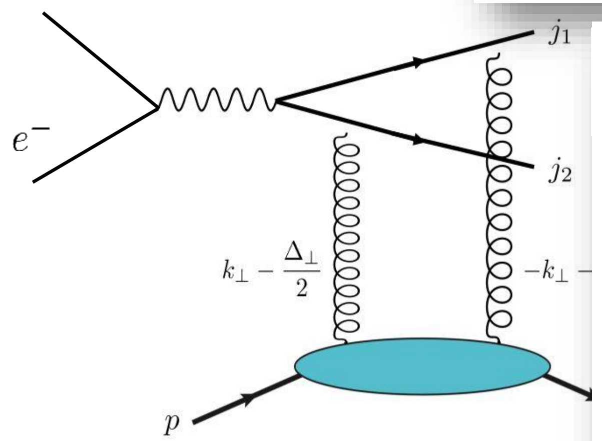
$$\approx d\sigma_0 + 2\cos 2\left(\phi_{P_\perp} - \phi_{\Delta_\perp}\right) d\tilde{\sigma}$$

$$\vec{P}_\perp = \frac{1}{2}(\vec{j}_{2\perp} - \vec{j}_{1\perp})$$

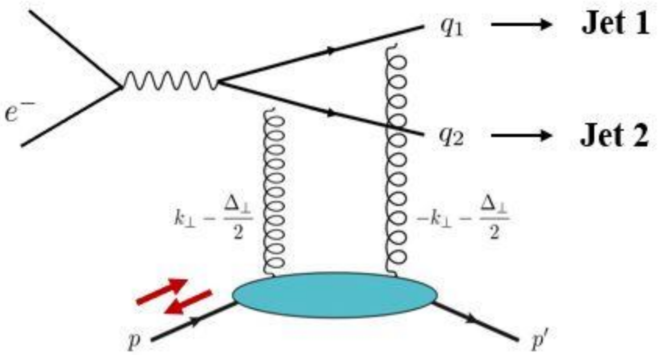
Observables for GTMDs

Exclusive dijet production in lepton-ion collisions at small-x (Hatta, Xiao, Yuan, arXiv: 1601.01585)

Coming up:



What happens if target is polarized?



arXiv: 1612.02438 (2016)

Hunting the Gluon Orbital Angular Momentum at the Electron-Ion Collider

Xiangdong Ji,[1,2] Feng Yuan,[3] and Yong Zhao[1,3]

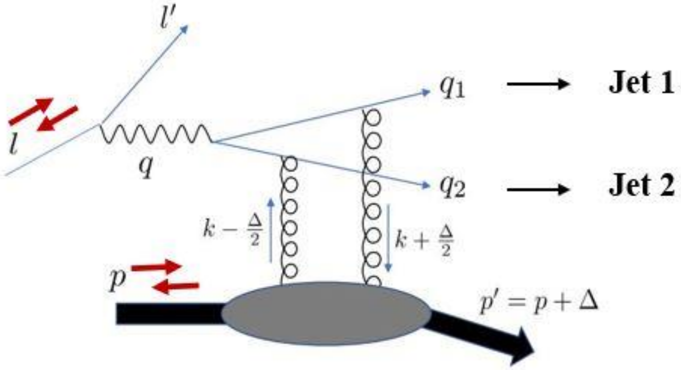
Main result:

$$\frac{d\sigma}{dy_1 dy_2 d^2\vec{\Delta}_\perp d^2\vec{P}_\perp} \propto z(1$$

Cosine angul

$$\approx d\sigma_0$$

What happens if in addition lepton is polarized?



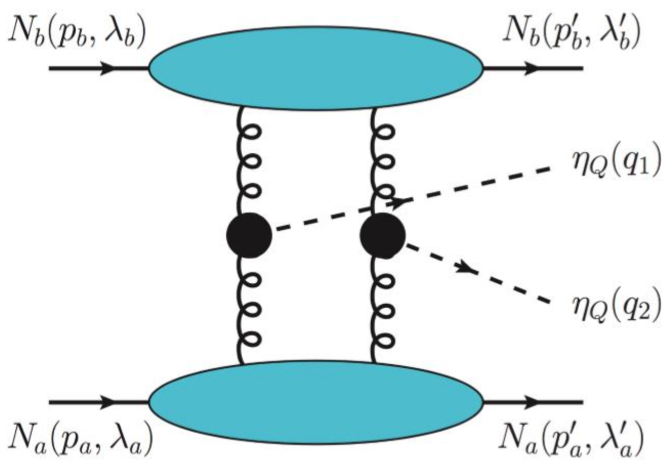
arXiv: 2201.08709 (2022)

Signature of the gluon orbital angular momentum

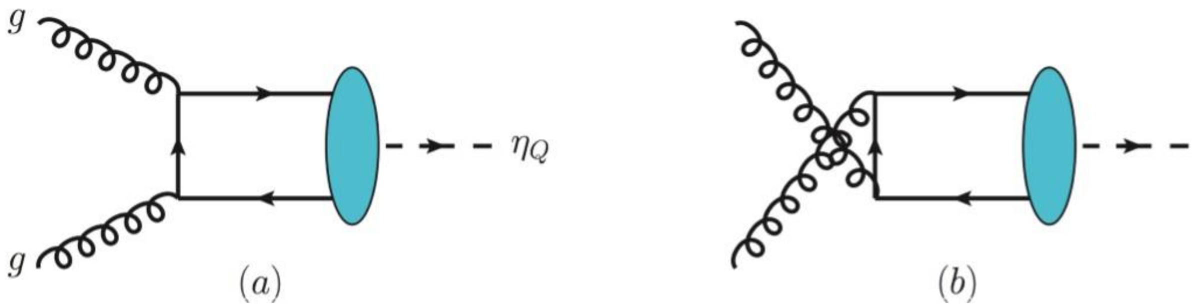
Shohini Bhattacharya,[1,*] Renaud Boussarie,[2,†] and Yoshitaka Hatta[1,3,‡]

Observables for GTMDs

Exclusive double quarkonium production (SB, Metz, Ojha, Tsai, Zhou, arXiv: 1802.10550)



Color Singlet Model: (Kuhn et. al., 1979, …)

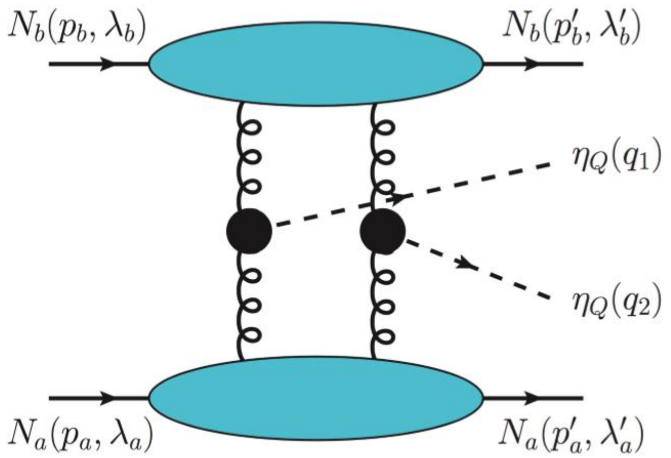


Main result:

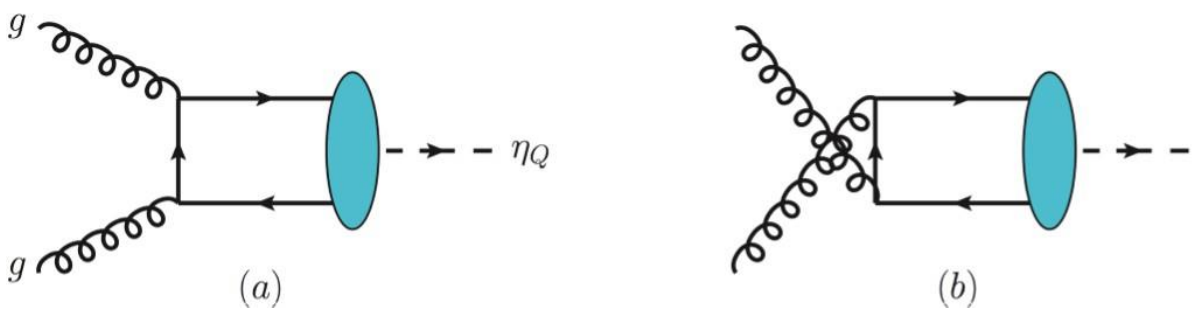
$$\frac{1}{2}\left(\tau_{XY} - \tau_{YX}\right) \approx 2\,\mathrm{Re.}\left\{ -\frac{\varepsilon_\perp^{ij}\Delta_{a\perp}^j}{M}\, C\left[\frac{k_{a\perp}^i}{M} F_{1,4}(x_a, \vec{k}_{a\perp})\, F_{1,1}(x_b, \vec{k}_{b\perp})\right] C\left[F_{1,1}^*(x_a, \vec{p}_{a\perp})\, F_{1,1}^*(x_b, \vec{p}_{b\perp})\right]\right\}$$

Observables for GTMDs

Exclusive double quarkonium production (SB, Metz, Ojha, Tsai, Zhou, arXiv: 1802.10550)



Color Singlet Model: (Kuhn et. al., 1979, …)



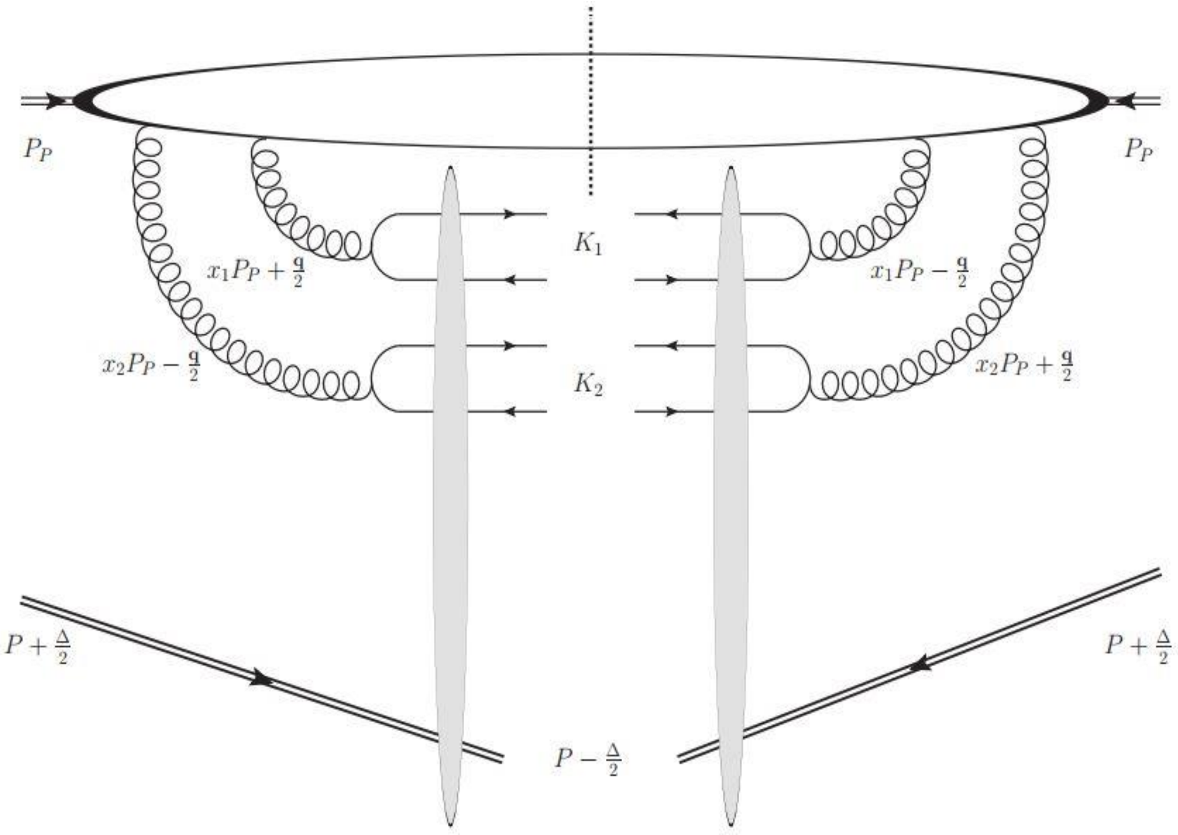
Main result:

$$\frac{1}{2}\left(\tau_{XY} - \tau_{YX}\right) \approx 2\,\mathrm{Re.}\left\{ -\frac{\varepsilon_{\perp}^{ij}\Delta_{a\perp}^{j}}{M}\, C\left[\frac{k_{a\perp}^{i}}{M} F_{1,4}(x_a, \vec{k}_{a\perp})\, F_{1,1}(x_b, \vec{k}_{b\perp})\right] C\left[F_{1,1}^{*}(x_a, \vec{p}_{a\perp})\, F_{1,1}^{*}(x_b, \vec{p}_{b\perp})\right]\right\}$$

This linear combination of polarization observables is sensitive to gluon OAM

Observables for GTMDs

Single-exclusive pp collisions (Boussarie, Hatta, Xiao, Yuan, arXiv: 1807.08697)



Main result:

Access Weiszacker-Williams gluon GTMD

Example: Result for $\chi_1 \, \chi_1$ production

Double PDF

$$d\sigma \approx F(x_1, x_2)$$
$$\times \left(G_1(\vec{K}_\perp, \vec{\Delta}_\perp) + \frac{\vec{K}_\perp^2}{2M^2} G_2(\vec{K}_\perp, \vec{\Delta}_\perp) \right)^2$$

Unpolarized & Linearly-polarized GTMDs

More developments …

$$Im.\, \boldsymbol{F_{1,2}}\Big|_{\Delta=0} = -f_{1T}^{\perp}$$

arXiv: 1912.08182 (2019)

Probing the gluon Sivers function with an unpolarized target: GTMD distributions and the Odderons

Renaud Boussarie,[1] Yoshitaka Hatta,[1] Lech Szymanowski,[2] and Samuel Wallon[3,4]

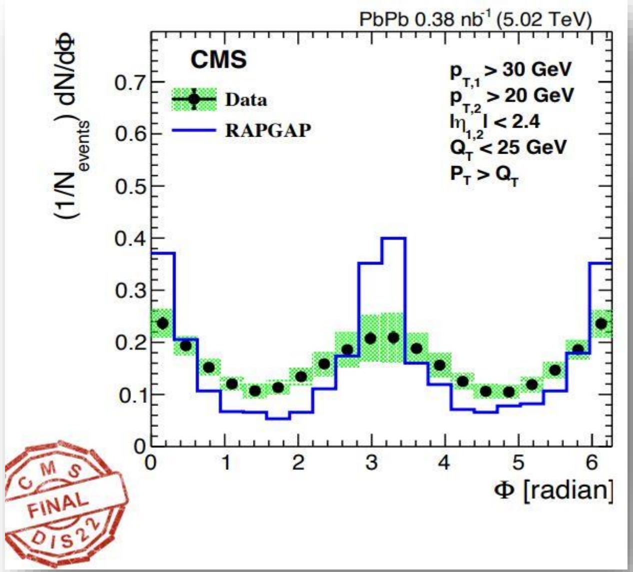
More developments …

$$Im.\, \boldsymbol{F_{1,2}}\Big|_{\Delta=0} = -f_{1T}^{\perp}$$

arXiv: 1912.08182 (2019)

Probing the gluon Sivers function with an unpolarized target: GTMD distributions and the Odderons

Renaud Boussarie,[1] Yoshitaka Hatta,[1] Lech Szymanowski,[2] and Samuel Wallon[3,4]



The CMS Collaboration **Michael Murray's talk, DIS 2022**

Angular correlations in exclusive dijet photoproduction in ultra-peripheral PbPb collisions at $\sqrt{s_{NN}} = 5.02$ TeV

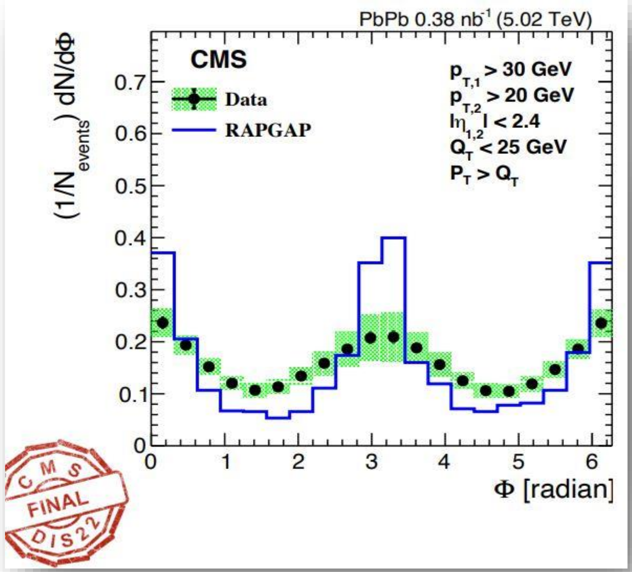
More developments …

$$Im.\ \boldsymbol{F_{1,2}}\Big|_{\Delta=0} = -f_{1T}^{\perp}$$

arXiv: 1912.08182 (2019)

Probing the gluon Sivers function with an unpolarized target: GTMD distributions and the Odderons

Renaud Boussarie,[1] Yoshitaka Hatta,[1] Lech Szymanowski,[2] and Samuel Wallon[3,4]



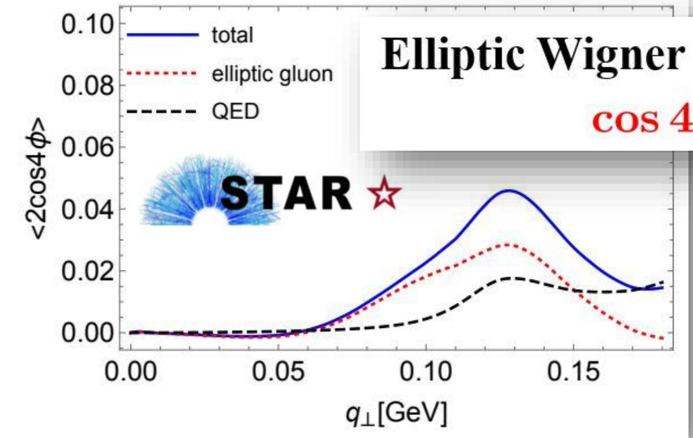
The CMS Collaboration **Michael Murray's talk, DIS 2022**

Angular correlations in exclusive dijet photoproduction in ultra-peripheral PbPb collisions at $\sqrt{s_{NN}} = 5.02$ TeV

arXiv: 2106.13466 (2021)

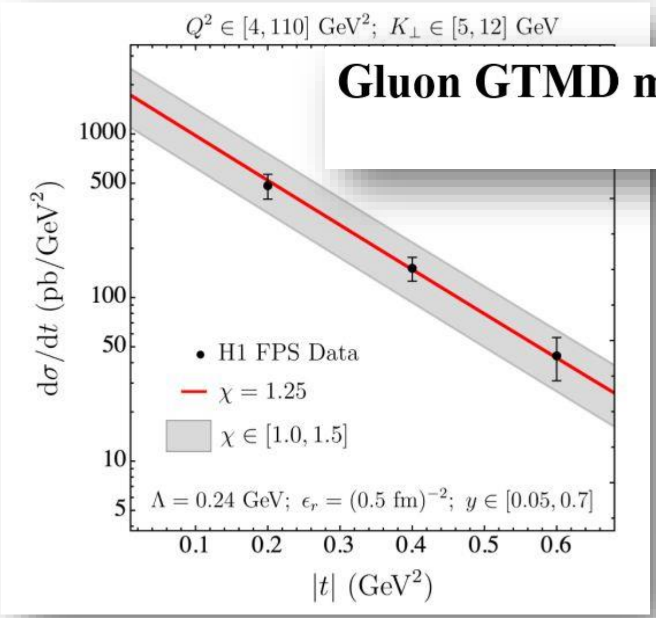
Probing the gluon tomography in photoproduction of di-pions

Yoshikazu Hagiwara, Cheng Zhang, Jian Zhou, and Ya-jin Zhou



Elliptic Wigner distribution contributes to $\cos 4\phi$ asymmetry

More developments …



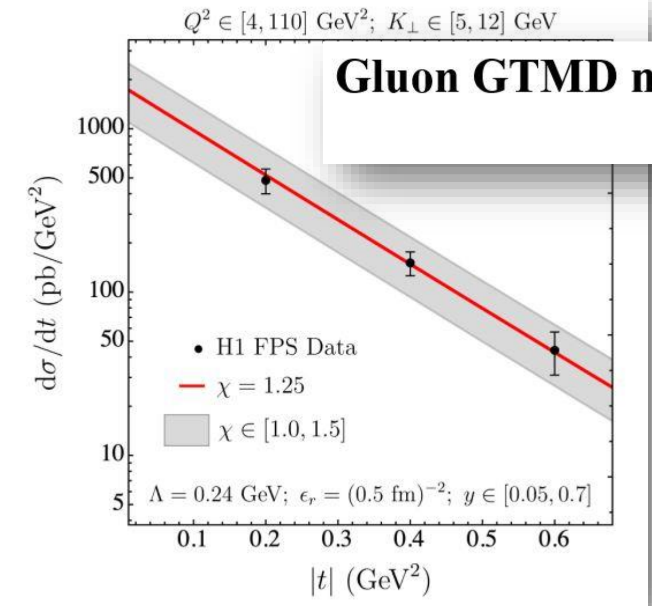
Gluon GTMD model based on MV model can describe HERA-H1 data

arXiv: 2106.15148 (2021)

GTMD model predictions for diffractive dijet production at EIC

Daniël Boer[1,*] and Chalis Setyadi[1,2,†]

More developments …



Gluon GTMD model based on MV model can describe HERA-H1 data

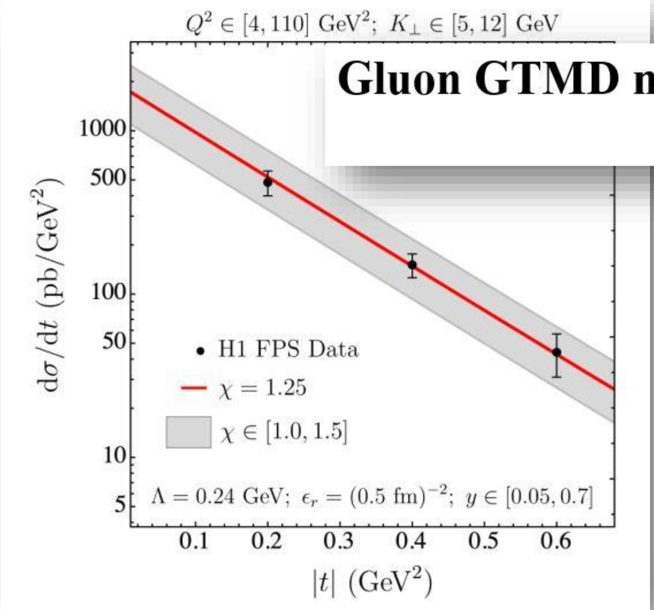
arXiv: 2106.15148 (2021)

GTMD model predictions for diffractive dijet production at EIC

Daniël Boer[1,*] and Chalis Setyadi[1,2,†]

Impact of JIMWLK evolution: See Mantysaari, Mueller, Schenke, 1902.05087

More developments …



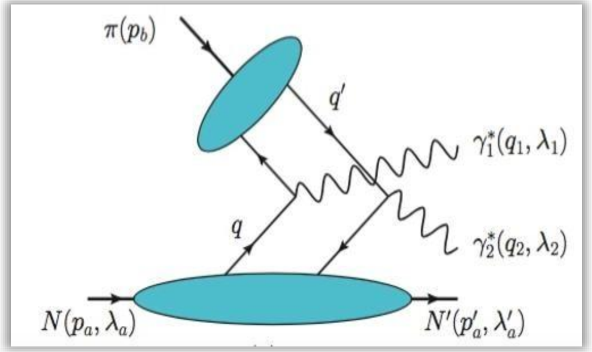
Gluon GTMD model based on MV model can describe HERA-H1 data

arXiv: 2106.15148 (2021)

GTMD model predictions for diffractive dijet production at EIC

Daniël Boer[1,*] and Chalis Setyadi[1,2,†]

Impact of JIMWLK evolution: See Mantysaari, Mueller, Schenke, 1902.05087



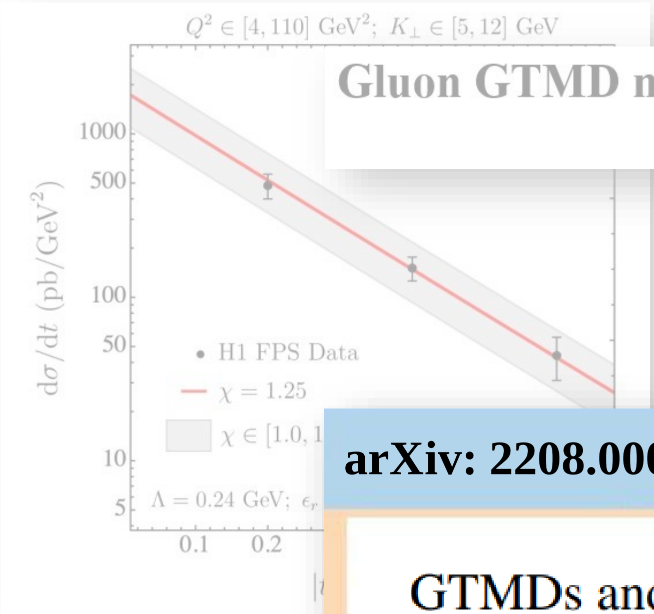
arXiv: 1702.04387 (2017)

Generalized TMDs and the exclusive double Drell-Yan process

Shohini Bhattacharya,[1] Andreas Metz,[1] and Jian Zhou[2]

First & only process sensitive to quark GTMDs

More developments …



Gluon GTMD model based on MV model can describe HERA-H1 data

arXiv: 2106.15148 (2021)

GTMD model predictions for diffractive dijet production at EIC

ri, Mueller, Schenke, 1902.05087

arXiv: 2208.00021 (2022)

First proof of factorization

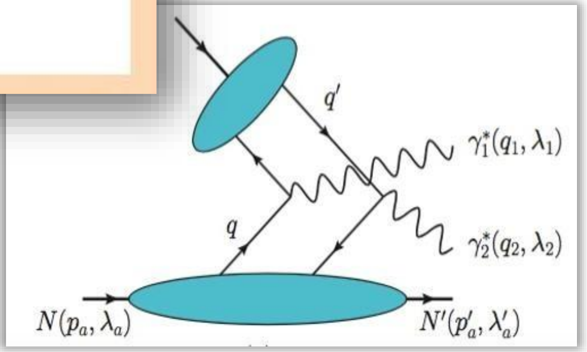
GTMDs and the factorization of exclusive double Drell-Yan

Miguel G. Echevarria[a,b], Patricia A. Gutierrez Garcia[c], Ignazio Scimemi[c]

arXiv: 1702.04387 (2017)

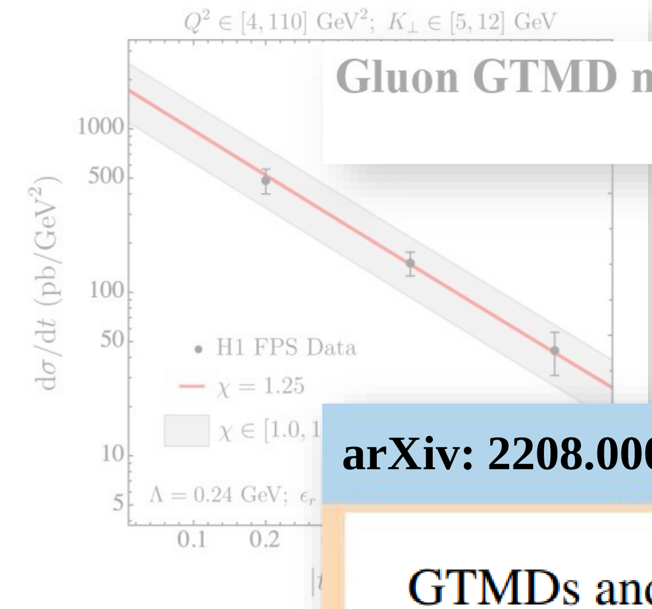
Generalized TMDs and the exclusive double Drell-Yan process

Shohini Bhattacharya,[1] Andreas Metz,[1] and Jian Zhou[2]



First & only process sensitive to quark GTMDs

More developments …



Gluon GTMD model based on MV model can describe HERA-H1 data

arXiv: 2106.15148 (2021)

GTMD model predictions for diffractive dijet production at EIC

ri, Mueller, Schenke, 1902.05087

arXiv: 2208.00021 (2022) **First proof of factorization**

GTMDs and the factorization of exclusive double Drell-Yan

Miguel G. Echevarria[a,b], Patricia A. Gutierrez Garcia[c], Ignazio Scimemi[c]

arXiv: 2207.09526 (2022) **Evolution**

Matching generalised transverse-momentum-dependent distributions onto generalised parton distributions at one loop

Valerio Bertone

arXiv: 1702.04387 (2017)

Generalized TMDs and the exclusive double I

Shohini Bhattacharya,[1] Andreas Metz,[1] and Ji

GTMDs

Our recent work

Signature of the gluon orbital angular momentum

Shohini Bhattacharya,[1,*] Renaud Boussarie,[2,†] and Yoshitaka Hatta[1,3,‡]

In Collaboration with:

Renaud Boussarie (CPHT, CNRS)

Yoshitaka Hatta (BNL)

Based on:

PRL 128, 182002 (arXiv: 2201.08709)

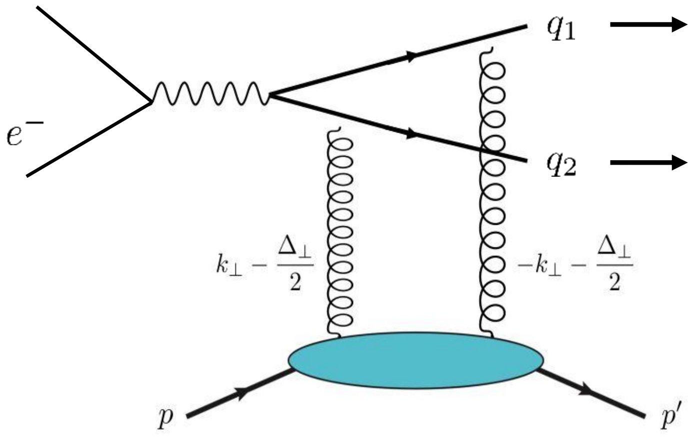
Probing gluon OAM through exclusive dijet production

Inspiration

arXiv: 1612.02438 (2016)

Hunting the Gluon Orbital Angular Momentum at the Electron-Ion Collider

Xiangdong Ji,[1,2] Feng Yuan,[3] and Yong Zhao[1,3]



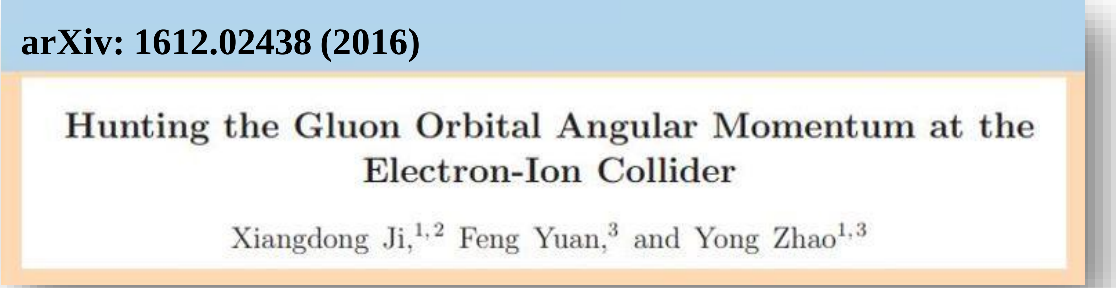
$\longrightarrow$ **Jet 1**

$\longrightarrow$ **Jet 2**

We took a fresh look at this 2016 paper

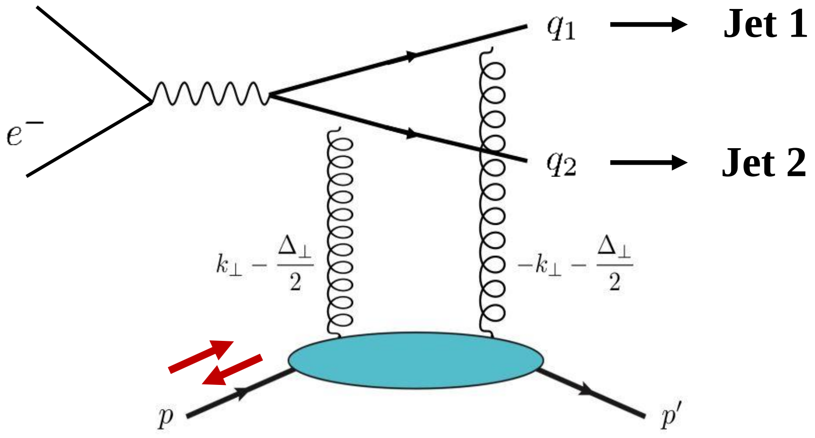
Probing gluon OAM through exclusive dijet production

Summary of the 2016 paper


arXiv: 1612.02438 (2016)

Hunting the Gluon Orbital Angular Momentum at the Electron-Ion Collider

Xiangdong Ji,[1,2] Feng Yuan,[3] and Yong Zhao[1,3]



Longitudinal single spin asymmetry (SSA):

$$\frac{d\Delta\sigma}{dy dQ^2 d\Omega} = \sigma_0 h_p \frac{2(\bar{z}-z)(q_\perp \times \Delta_\perp)}{q_\perp^2 + \mu^2}\Big[16\beta(1-y)\mathfrak{Im}[F_g^* + 4\xi^2\bar{\beta}F_g'^*][\mathcal{L}_g + 8\xi^2\bar{\beta}\mathcal{L}_g'] + (1+(1-y)^2)\,\mathfrak{Im}[F_g^* + 2\xi^2(1-2\beta)F_g'^*][\mathcal{L}_g + 2\bar{\beta}(1/z\bar{z}-2)(\mathcal{L}_g + 4\xi^2(1-2\beta)\mathcal{L}_g')]\Big]$$

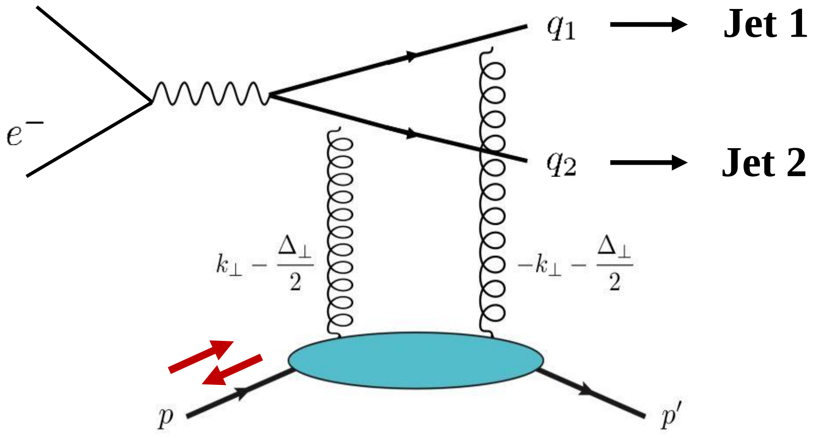
Probing gluon OAM through exclusive dijet production

Summary of the 2016 paper

arXiv: 1612.02438 (2016)

Hunting the Gluon Orbital Angular Momentum at the Electron-Ion Collider

Xiangdong Ji,[1,2] Feng Yuan,[3] and Yong Zhao[1,3]



Schematic structure of SSA (oversimplified):

$$\boxed{\frac{d\sigma}{dy dQ^2 d\Omega} \sim \sigma_0 h_p \sin(\phi_{q_\perp} - \phi_{\Delta_\perp})\,(\bar{z} - z)\left[\mathfrak{Im}\Big(F_g^*(\xi)\mathcal{L}_g(\xi)\Big)\right]}$$

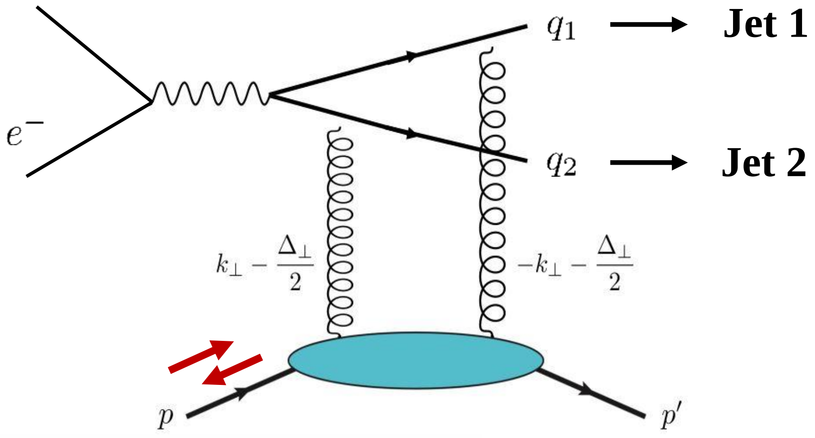
Probing gluon OAM through exclusive dijet production

Summary of the 2016 paper

arXiv: 1612.02438 (2016)

Hunting the Gluon Orbital Angular Momentum at the Electron-Ion Collider

Xiangdong Ji,[1,2] Feng Yuan,[3] and Yong Zhao[1,3]



Signature of OAM is sinusoidal angular modulation

$q_\perp = q_{1\perp} - q_{2\perp}$

Moment of GPD

$$\boxed{\frac{d\sigma}{dydQ^2d\Omega} \sim \sigma_0 h_p \sin(\phi_{q_\perp} - \phi_{\Delta_\perp})(\bar{z} - z)\left[\Im\mathfrak{m}\left(F_g^*(\xi)\mathcal{L}_g(\xi)\right)\right]}$$

Moment of OAM

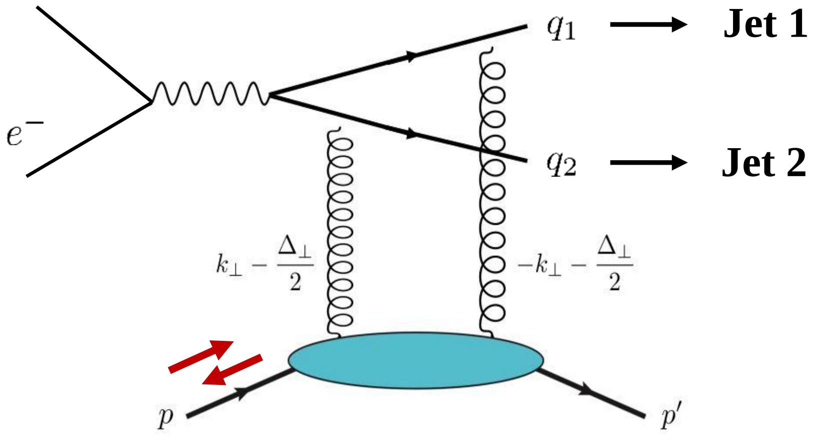
Probing gluon OAM through exclusive dijet production

Summary of the 2016 paper

arXiv: 1612.02438 (2016)

Hunting the Gluon Orbital Angular Momentum at the Electron-Ion Collider

Xiangdong Ji,[1,2] Feng Yuan,[3] and Yong Zhao[1,3]



Issues with SSA:

$$q_\perp = q_{1\perp} - q_{2\perp}$$

$$\frac{d\sigma}{dydQ^2d\Omega} \sim \sigma_0 h_p \sin(\phi_{q_\perp} - \phi_{\Delta_\perp})\,(\bar{z} - z)\left[\mathfrak{Im}\Big(F_g^*(\xi)\mathcal{L}_g(\xi)\Big)\right]$$

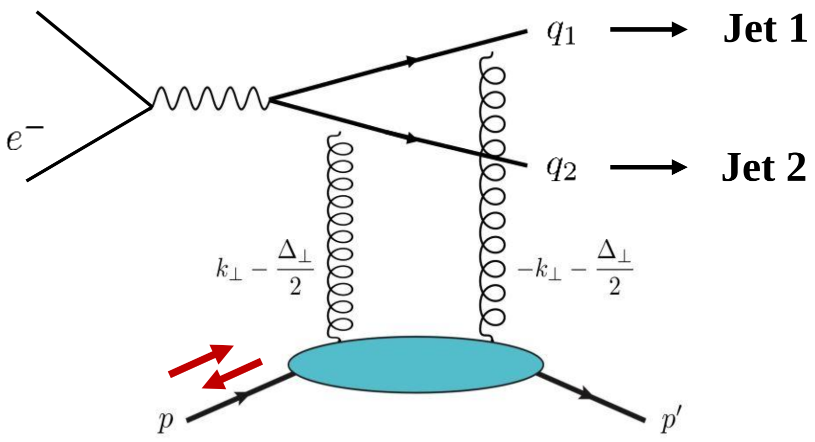
Probing gluon OAM through exclusive dijet production

Summary of the 2016 paper

arXiv: 1612.02438 (2016)

Hunting the Gluon Orbital Angular Momentum at the Electron-Ion Collider

Xiangdong Ji,[1,2] Feng Yuan,[3] and Yong Zhao[1,3]



Issues with SSA:

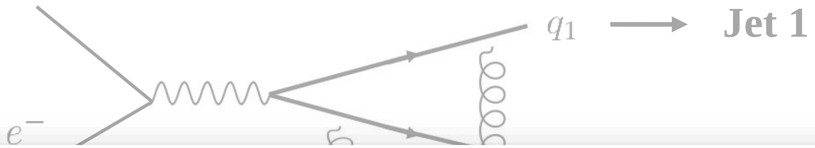
$$q_\perp = q_{1\perp} - q_{2\perp}$$

$$\frac{d\sigma}{dy dQ^2 d\Omega} \sim \sigma_0 h_p \sin(\phi_{q_\perp} - \phi_{\Delta_\perp})(\bar{z} - z)\left[\Im\mathrm{m}\left(F_g^*(\xi)\mathcal{L}_g(\xi)\right)\right]$$

SSA vanishes for symmetric jet configurations $z = \bar{z} = \frac{1}{2}$

Probing gluon OAM through exclusive dijet production

Summary of the 2016 paper



arXiv: 1612.02438 (2016)

Hunting the Gluon Orbital Angular Momentum
Electron-Ion Collider

Xiangdong Ji,[1,2] Feng Yuan,[3] and Yong Zhao[1,3]

"Compton Form Factor":

$$\boxed{\mathcal{L}_g(\xi) = \int dx \frac{x^2 \xi L_g(x,\xi)}{(x^2 - \xi^2 + i\xi\epsilon)^3}}$$

Third pole at $x = \pm\xi$ ⟶ potentially dangerous for collinear factorization

(See Cui, Hu, Ma, 1804.05293)

Issues with SSA:

$$q_\perp = q_{1\perp} - q_{2\perp}$$

$$\frac{d\sigma}{dy dQ^2 d\Omega} \sim \sigma_0 h_p \sin(\phi_{q_\perp} - \phi_{\Delta_\perp}) (\bar{z} - z) \left[\Im m \left(F_g^*(\xi) \mathcal{L}_g(\xi) \right) \right]$$

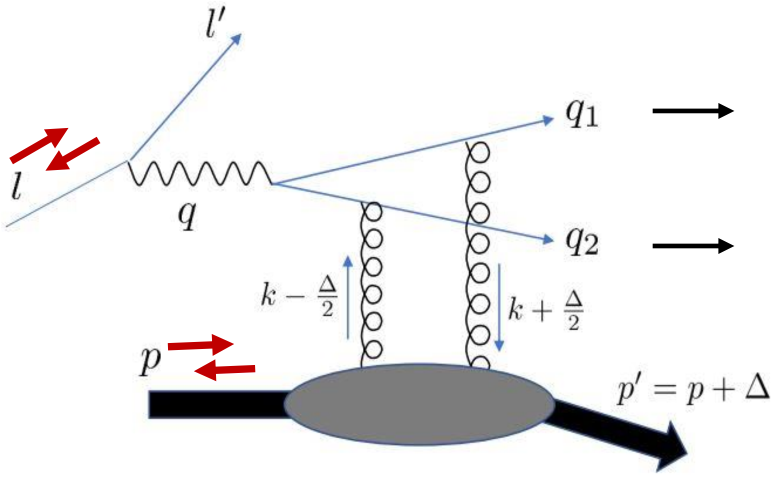
SSA vanishes for symmetric jet configurations $z = \bar{z} = \frac{1}{2}$

Probing gluon OAM through exclusive dijet production

Our work

Signature of the gluon orbital angular momentum

Shohini Bhattacharya,[1,*] Renaud Boussarie,[2,†] and Yoshitaka Hatta[1,3,‡]



$q_1 \longrightarrow$ **Jet 1**

$q_2 \longrightarrow$ **Jet 2**

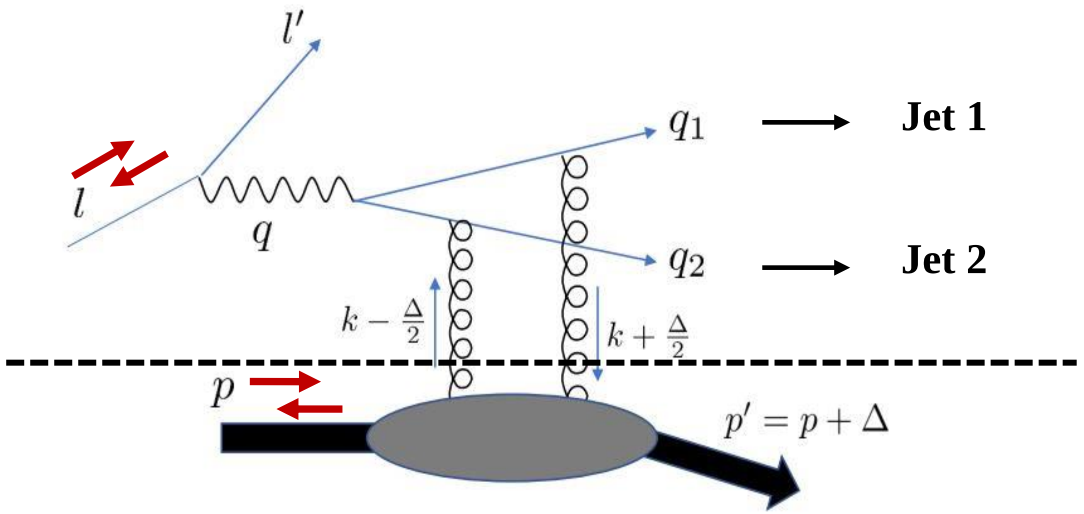
Distinct feature in our work

Double spin asymmetry (DSA):-

Both electron & incoming proton are longitudinally polarized

Probing gluon OAM through exclusive dijet production

Scattering amplitude



- **6 leading-order Feynman diagrams**
- **Scattering amplitude:**

$$\boxed{A \propto \int dx \int d^2k_\perp \, \mathcal{H}(x, \xi, q_\perp, k_\perp, \Delta_\perp) \, x f_g(x, \xi, k_\perp, \Delta_\perp)}$$

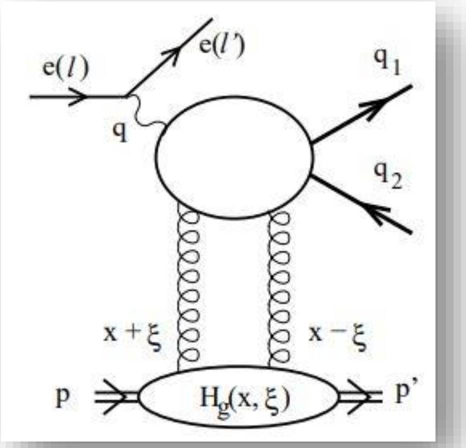
Hard part Soft part

Probing gluon OAM through exclusive dijet production

Scattering amplitude

Twist expansion:

- **Twist-2 amplitude:** **Proportional to gluon GPD**



Braun, Ivanov, 0505263

$$A_T^2 = \frac{i g_s^2 e_{em} e_q}{N_c} \frac{1}{q_\perp^2 + \mu^2} \left(\bar{u}(q_1) \not{\epsilon}_\perp v(q_2)\right) \int dx \frac{1}{(x+\xi-i\varepsilon)(x-\xi+i\varepsilon)}$$
$$\times \left(1 + \frac{2\xi^2(1-2\beta)}{(x+\xi-i\varepsilon)(x-\xi+i\varepsilon)}\right) \boxed{\int d^2k_\perp x f_g(x,\xi,k_\perp,\Delta_\perp)}$$

$$A_L^2 = \frac{i g_s^2 e_{em} e_q}{N_c} \frac{1}{(q_\perp^2 + \mu^2)^2} 4\xi z\bar{z} QW \left(\bar{u}(q_1)\gamma^- v(q_2)\right) \int dx \frac{1}{(x+\xi-i\varepsilon)(x-\xi+i\varepsilon)}$$
$$\times \left(1 + \frac{4\xi^2\bar{\beta}}{(x+\xi-i\varepsilon)(x-\xi+i\varepsilon)}\right) \boxed{\int d^2k_\perp x f_g(x,\xi,k_\perp,\Delta_\perp)}$$

Probing gluon OAM through exclusive dijet production

Scattering amplitude

Twist expansion:

- **Twist-3 amplitude:** **Proportional to gluon OAM**

$$A_T^3 = -\frac{ig_s^2 e_{em} e_q}{N_c} \frac{2(\bar{z}-z)}{(q_\perp^2+\mu^2)^2} \bar{u}(q_1)\epsilon_\perp \cdot \gamma_\perp v(q_2) \int dx \frac{x}{(x^2-\xi^2+i\xi\varepsilon)^2} \left(2\xi + \frac{(2\xi)^3(1-2\beta)}{(x^2-\xi^2+i\xi\varepsilon)}\right) \boxed{\int d^2k_\perp q_\perp \cdot \boldsymbol{k}_\perp \, x f_g(x,\xi,k_\perp,\Delta_\perp)}$$
$$- \frac{ig_s^2 e_{em} e_q}{N_c} \frac{2(2\xi)^2 z\bar{z}W}{(q_\perp^2+\mu^2)^2} \bar{u}(q_1)\gamma^- v(q_2) \int dx \frac{x}{(x^2-\xi^2+i\xi\varepsilon)^2} \boxed{\int d^2k_\perp \epsilon_\perp \cdot \boldsymbol{k}_\perp \, x f_g(x,\xi,k_\perp,\Delta_\perp)}$$

$$A_L^3 = \frac{ig_s^2 e_{em} e_q}{N_c} \frac{16\xi^2(\bar{z}-z)z\bar{z}QW}{(q_\perp^2+\mu^2)^3} \bar{u}(q_1)\gamma^- v(q_2) \int dx \frac{x}{(x^2-\xi^2+i\xi\varepsilon)^2} \left(1 + \frac{8\xi^2(1-\beta)}{(x^2-\xi^2+i\xi\varepsilon)}\right) \boxed{\int d^2k_\perp q_\perp \cdot \boldsymbol{k}_\perp \, x f_g(x,\xi,k_\perp,\Delta_\perp)}$$

Probing gluon OAM through exclusive dijet production

Scattering amplitude

Twist expansion:

- **Twist-3 amplitude:** Proportional to gluon OAM

$$A_T^3 = -\frac{ig_s^2 e_{em} e_q}{N_c}\frac{2(\bar z - z)}{(q_\perp^2+\mu^2)^2}\bar u(q_1)\epsilon_\perp\cdot\gamma_\perp v(q_2)\int dx \frac{x}{(x^2-\xi^2+i\xi\varepsilon)^2}\left(2\xi + \frac{(2\xi)^3(1-2\beta)}{(x^2-\xi^2+i\xi\varepsilon)}\right)\int d^2k_\perp q_\perp\cdot \boldsymbol{k}_\perp\, x f_g(x,\xi,k_\perp,\Delta_\perp)$$

$$-\frac{ig_s^2 e_{em} e_q}{N_c}\frac{2(2\xi)^2 z\bar z W}{(q_\perp^2+\mu^2)^2}\bar u(q_1)\gamma^- v(q_2)\int dx\, x \int d^2k_\perp \epsilon_\perp\cdot \boldsymbol{k}_\perp\, x f_g(x,\xi,k_\perp,\Delta_\perp)$$

Factorization-breaking third poles at $x = \pm\xi$

$$A_L^3 = \frac{ig_s^2 e_{em} e_q}{N_c}\frac{16\xi^2(\bar z - z)z\bar z QW}{(q_\perp^2+\mu^2)^3}\bar u(q_1)\gamma^- v(q_2)\int dx \frac{x}{(x^2-\xi^2+i\xi\varepsilon)^2}\left(1 + \frac{8\xi^2(1-\beta)}{(x^2-\xi^2+i\xi\varepsilon)}\right)\int d^2k_\perp q_\perp\cdot \boldsymbol{k}_\perp\, x f_g(x,\xi,k_\perp,\Delta_\perp)$$

Probing gluon OAM through exclusive dijet production

Note: Gluon GPDs may contain $\sim \theta(\xi - |x|)(x^2 - \xi^2)^2$

(See Radyushkin, 9805342)

Hence, integrals containing third poles are divergent

Twist expansion:

- **Twist-3 amplitude:** Proportion

$$A_T^3 = -\frac{i g_s^2 e_{em} e_q}{N_c} \frac{2(\bar z - z)}{(q_\perp^2 + \mu^2)^2} \bar u(q_1) \epsilon_\perp \cdot \gamma_\perp v(q_2) \int dx \frac{x}{(x^2 - \xi^2 + i\xi\varepsilon)^2} \left(2\xi + \frac{(2\xi)^3 (1 - 2\beta)}{(x^2 - \xi^2 + i\xi\varepsilon)} \right) \int d^2 k_\perp q_\perp \cdot \boldsymbol{k}_\perp \, x f_g(x, \xi, k_\perp, \Delta_\perp)$$

$$- \frac{i g_s^2 e_{em} e_q}{N_c} \frac{2(2\xi)^2 z \bar z W}{(q_\perp^2 + \mu^2)^2} \bar u(q_1) \gamma^- v(q_2) \int dx \frac{x}{\cdots} \int d^2 k_\perp \epsilon_\perp \cdot \boldsymbol{k}_\perp \, x f_g(x, \xi, k_\perp, \Delta_\perp)$$

Factorization-breaking third poles at $x = \pm\xi$

$$A_L^3 = \frac{i g_s^2 e_{em} e_q}{N_c} \frac{16\xi^2 (\bar z - z) z \bar z Q W}{(q_\perp^2 + \mu^2)^3} \bar u(q_1) \gamma^- v(q_2) \int dx \frac{x}{(x^2 - \xi^2 + i\xi\varepsilon)^2} \left(1 + \frac{8\xi^2 (1 - \beta)}{(x^2 - \xi^2 + i\xi\varepsilon)} \right) \int d^2 k_\perp \, q_\perp \cdot \boldsymbol{k}_\perp \, x f_g(x, \xi, k_\perp, \Delta_\perp)$$

Probing gluon OAM through exclusive dijet production

Scattering amplitude

Twist expansion:

Switch off the factorization-breaking third poles by setting $z=\bar{z}=\frac{1}{2}$

$$A_T^3 = -\frac{ig_s^2 e_{em} e_q}{N_c} \boxed{\frac{2(\bar{z}-z)}{(q_\perp^2+\mu^2)^2}} \bar{u}(q_1)\epsilon_\perp \cdot \gamma_\perp v(q_2) \int dx \frac{x}{(x^2-\xi^2+i\xi\varepsilon)^2}\left(2\xi + \frac{(2\xi)^3(1-2\beta)}{(x^2-\xi^2+i\xi\varepsilon)}\right) \int d^2k_\perp q_\perp \cdot \boldsymbol{k}_\perp \, x f_g(x,\xi,k_\perp,\Delta_\perp)$$

Recall: Not possible in SSA

Factorization-breaking third poles at $x=\pm\xi$

$$A_L^3 = \frac{ig_s^2 e_{em} e_q}{N_c} \frac{16\xi^2 (\bar{z}-z) z\bar{z} QW}{(q_\perp^2+\mu^2)^3} \bar{u}(q_1)\gamma^- v(q_2) \int dx \frac{x}{(x^2-\xi^2+i\xi\varepsilon)^2}\left(1 + \frac{8\xi^2(1-\beta)}{(x^2-\xi^2+i\xi\varepsilon)}\right) \int d^2k_\perp q_\perp \cdot \boldsymbol{k}_\perp \, x f_g(x,\xi,k_\perp,\Delta_\perp)$$

Probing gluon OAM through exclusive dijet production

Scattering amplitude

Main result $(z=1/2)$**:**

DSA is sensitive to OAM through an interference between L & T amplitudes:

$$\boxed{\begin{aligned}\int d\phi_{q_\perp} L^{\mu\nu}A^*_\mu A_\nu = -\frac{2^{10}\pi^4}{N_c} h_l h_p \alpha_s^2 \alpha_{em} e_q^2 \frac{(1+\xi)\xi Q^2}{(q_\perp^2+\mu^2)^2}|l_\perp||\Delta_\perp|\cos(\phi_{l_\perp}-\phi_{\Delta_\perp}) \\ \times \mathfrak{Re}\left[\left\{\mathcal{H}_g^{(1)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(1)*} + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\left(\mathcal{H}_g^{(2)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(2)*}\right)\right\}\mathcal{L}_g + \left(\mathcal{E}_g^{(1)*} + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\mathcal{E}_g^{(2)*}\right)\frac{\mathcal{O}}{2}\right]\end{aligned}}$$

DSA does not vanish for symmetric jet configurations $z=\bar{z}=\dfrac{1}{2}$

Probing gluon OAM through exclusive dijet production

Scattering amplitude

Main result $(z = 1/2)$**:**

DSA is sensitive to OAM through an interference between L & T amplitudes:

$$\int d\phi_{q_\perp} L^{\mu\nu} A^*_\mu A_\nu = -\frac{2^{10}\pi^4}{N_c} h_l h_p \alpha_s^2 \alpha_{em} e_q^2 \frac{(1+\xi)\xi Q^2}{(q_\perp^2+\mu^2)^2} |l_\perp||\Delta_\perp| \cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$
$$\times \Re\mathfrak{e}\left[\left\{\mathcal{H}_g^{(1)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(1)*} + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\left(\mathcal{H}_g^{(2)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(2)*}\right)\right\}\mathcal{L}_g + \left(\mathcal{E}_g^{(1)*} + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\mathcal{E}_g^{(2)*}\right)\frac{\mathcal{O}}{2}\right]$$

Signature of gluon OAM is cosine angular modulation

Probing gluon OAM through exclusive dijet production

Scattering amplitude

Main result $(z = 1/2)$**:**

DSA is sensitive to OAM through an interference between L & T amplitudes:

$$\int d\phi_{q_\perp} L^{\mu\nu} A^*_\mu A_\nu = -\frac{2^{10}\pi^4}{N_c} h_l h_p \alpha_s^2 \alpha_{em} e_q^2 \frac{(1+\xi)\xi Q^2}{(q_\perp^2+\mu^2)^2} |l_\perp||\Delta_\perp| \cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$
$$\times \Re\mathfrak{e}\left[\left\{\mathcal{H}_g^{(1)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(1)*} + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\left(\mathcal{H}_g^{(2)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(2)*}\right)\right\}\mathcal{L}_g + \left(\mathcal{E}_g^{(1)*} + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\mathcal{E}_g^{(2)*}\right)\frac{\mathcal{O}}{2}\right]$$

"Compton Form Factors":

$$\mathcal{L}_g(\xi) = \int_{-1}^{1} dx \frac{x^2 L_g(x,\xi)}{(x-\xi+i\epsilon)^2(x+\xi-i\epsilon)^2}$$

$$\mathcal{H}_g^{(1)}(\xi) = \int_{-1}^{1} dx \frac{H_g(x,\xi)}{(x-\xi+i\epsilon)(x+\xi-i\epsilon)} \qquad \mathcal{H}_g^{(2)}(\xi) = \int_{-1}^{1} dx \frac{\xi^2 H_g(x,\xi)}{(x-\xi+i\epsilon)^2(x+\xi-i\epsilon)^2}$$

Probing gluon OAM through exclusive dijet production

Scattering amplitude

Main result $(z = 1/2)$**:**

DSA is sensitive to OAM through an interference between L & T amplitudes:

$$\int d\phi_{q_\perp} L^{\mu\nu} A^*_\mu A_\nu = -\frac{2^{10}\pi^4}{N_c} h_l h_p \alpha_s^2 \alpha_{em} e_q^2 \frac{(1+\xi)\xi Q^2}{(q_\perp^2+\mu^2)^2} |l_\perp||\Delta_\perp| \cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$
$$\times \mathfrak{Re}\left[\left\{\mathcal{H}_g^{(1)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(1)*} + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\left(\mathcal{H}_g^{(2)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(2)*}\right)\right\}\mathcal{L}_g + \left(\mathcal{E}_g^{(1)*} + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\mathcal{E}_g^{(2)*}\right)\frac{\mathcal{O}}{2}\right]$$

"Compton Form Factors":

$$O(x,\xi) \equiv \int d^2\widetilde{k}_\perp \frac{\widetilde{k}_\perp^2}{M^2} F_{1,2}(x,\xi,\widetilde{\Delta}_\perp = 0)$$

$$\mathcal{O}(\xi) = \int_{-1}^{1} dx \frac{xO(x,\xi)}{(x-\xi+i\epsilon)^2(x+\xi-i\epsilon)^2}$$

Probing gluon OAM through exclusive dijet production

Scattering amplitude

Not the end of the story:

Probing gluon OAM through exclusive dijet production

Scattering amplitude

Not the end of the story:

- **Interference between unpolarized & helicity GPD** $(z = 1/2)$**:**

Helicity GPD

$$\int d\phi_{q_\perp} L^{\mu\nu} A_\mu A_\nu = \frac{2^{10}\pi^4}{N_c} h_l h_p \alpha_s^2 \alpha_{em} e_q^2 \frac{(1-\xi^2)\xi Q^2}{(q_\perp^2+\mu^2)^2} |l_\perp||\Delta_\perp| \cos(\phi_{l_\perp} - \phi_{\Delta_\perp}) \mathfrak{Re}\left[\left(\mathcal{H}_g^{(1)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(1)*}\right)\left(\tilde{\mathcal{H}}_g^{(2)} - \frac{\xi^2}{1-\xi^2}\tilde{\mathcal{E}}_g^{(2)}\right)\right]$$

- **Analogous contribution should enter SSA**

Probing gluon OAM through exclusive dijet production

Scattering amplitude

Not the end of the story:

- **Interference between unpolarized & helicity GPD** $(z=1/2)$**:**

Helicity GPD

$$\int d\phi_{q_\perp} L^{\mu\nu} A_\mu A_\nu = \frac{2^{10}\pi^4}{N_c} h_l h_p \alpha_s^2 \alpha_{em} e_q^2 \frac{(1-\xi^2)\xi Q^2}{(q_\perp^2+\mu^2)^2} |l_\perp||\Delta_\perp| \cos(\phi_{l_\perp}-\phi_{\Delta_\perp}) \mathfrak{Re}\left[\left(\mathcal{H}_g^{(1)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(1)*}\right)\left(\tilde{\mathcal{H}}_g^{(2)} - \frac{\xi^2}{1-\xi^2}\tilde{\mathcal{E}}_g^{(2)}\right)\right]$$

Helicity contributes to the same angular modulation as that of OAM

Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

See backup slides for details on how we modelled GPDs and OAM

Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

Realistic EIC kinematics

$\sqrt{s}$ [GeV]	Q^2 [GeV^2]	y	ξ
120	2.7	0.7	$\lesssim 10^{-3}$
	4.8		
	10.0		

Focus on:

$$z = \bar{z} = \frac{1}{2}$$

Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

Realistic EIC kinematics

$\sqrt{s}$ [GeV]	Q^2 [GeV^2]	y	ξ
120	2.7	0.7	$\lesssim 10^{-3}$
	4.8		
	10.0		

Focus on:

$$z = \bar{z} = \frac{1}{2}$$

Cross section:

$$\boxed{\frac{d\sigma}{dy dQ^2 d\phi_{l_\perp} dz dq_\perp^2 d^2\Delta_\perp} = \frac{\alpha_{em} y}{2^{11}\pi^7 Q^4} \frac{\int d\phi_{q_\perp} L^{\mu\nu} A_\mu^* A_\nu}{(W^2+Q^2)(W^2-M_J^2)z\bar{z}}}$$

Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

Realistic EIC kinematics

$\sqrt{s}$ [GeV]	Q^2 [GeV^2]	y	ξ
120	2.7	0.7	$\lesssim 10^{-3}$
	4.8		
	10.0		

Focus on:

$$z = \bar{z} = \frac{1}{2}$$

Study cross section as differential in the skewness variable

$$\frac{d\sigma}{dy\,dQ^2\,dz\,d\xi\,d\delta\phi}$$

Cross section:

$$\frac{d\sigma}{dy\,dQ^2\,d\phi_{l_\perp}\,dz\,dq_\perp^2\,d^2\Delta_\perp} = \frac{\alpha_{em}y}{2^{11}\pi^7 Q^4}$$

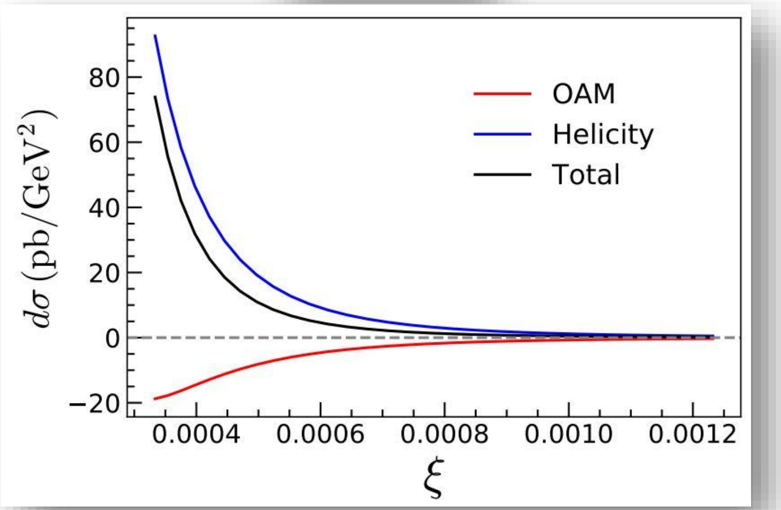
Relation between skewness & jet momenta:

$$\boxed{\xi = \frac{q_\perp^2 + z\bar{z}Q^2}{-q_\perp^2 + z\bar{z}(Q^2 + 2W^2)}}$$

Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

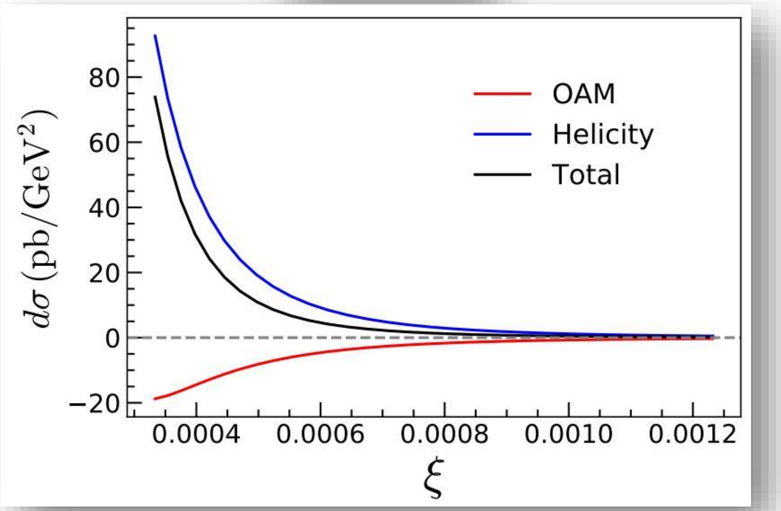
$Q^2 = 2.7$



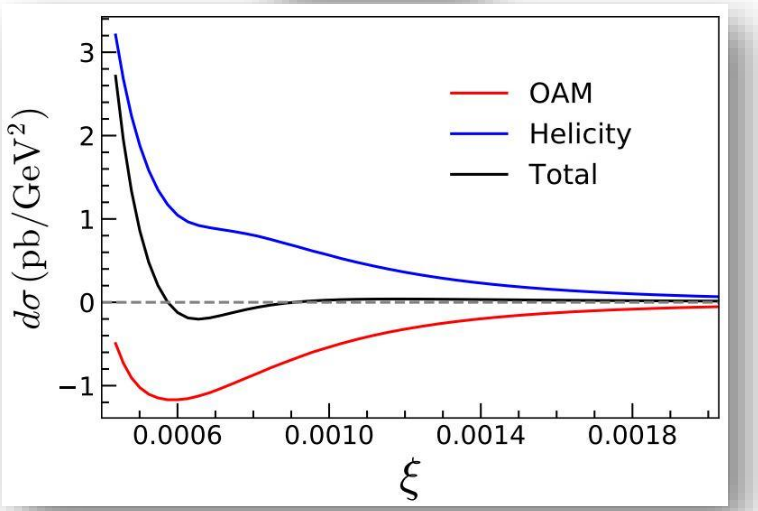
Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

$Q^2 = 2.7$



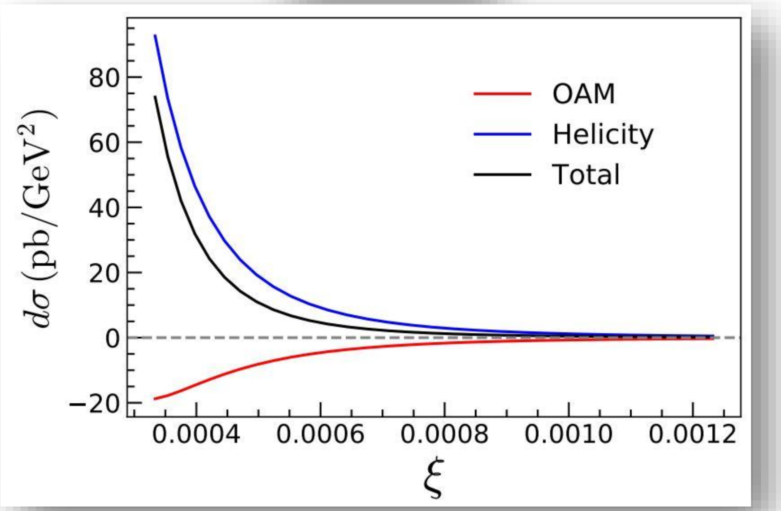
$Q^2 = 4.8$



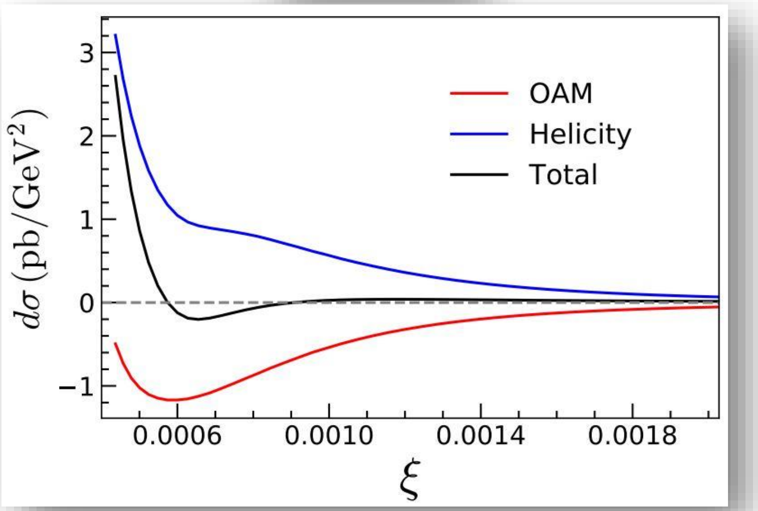
Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

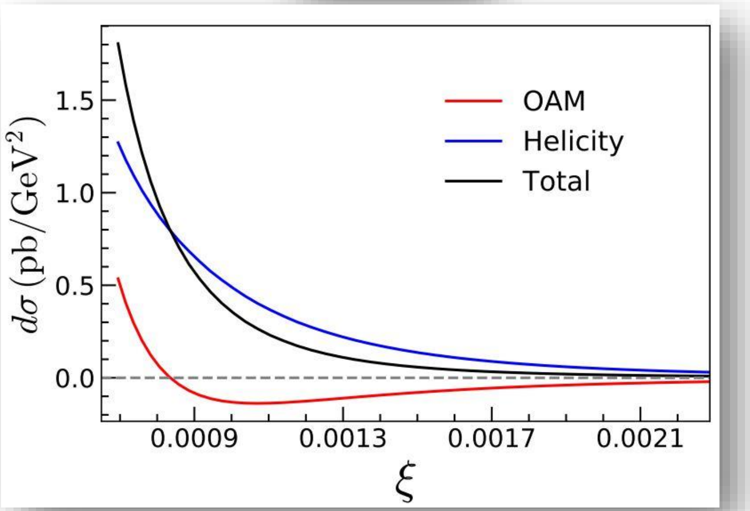
$Q^2 = 2.7$



$Q^2 = 4.8$



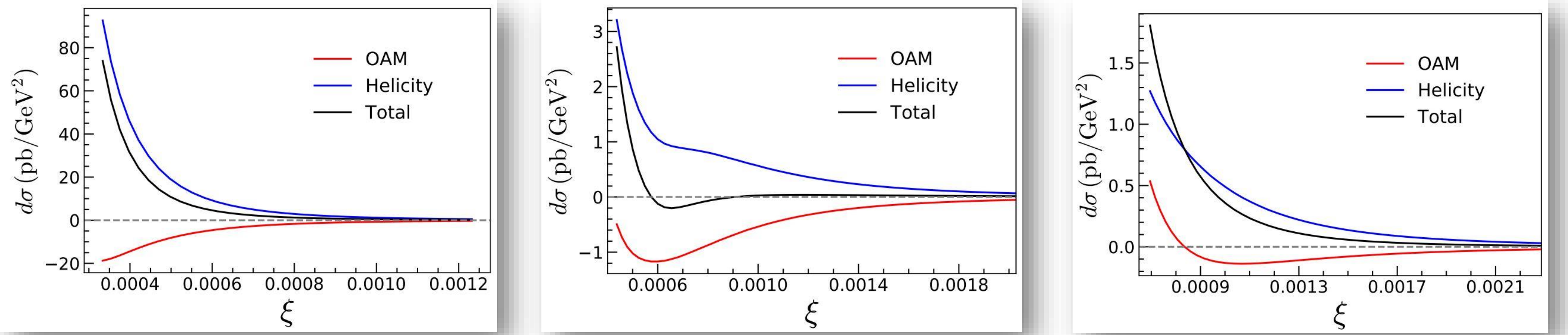
$Q^2 = 10$



Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

$Q^2 = 2.7$ $\qquad$ $Q^2 = 4.8$ $\qquad$ $Q^2 = 10$

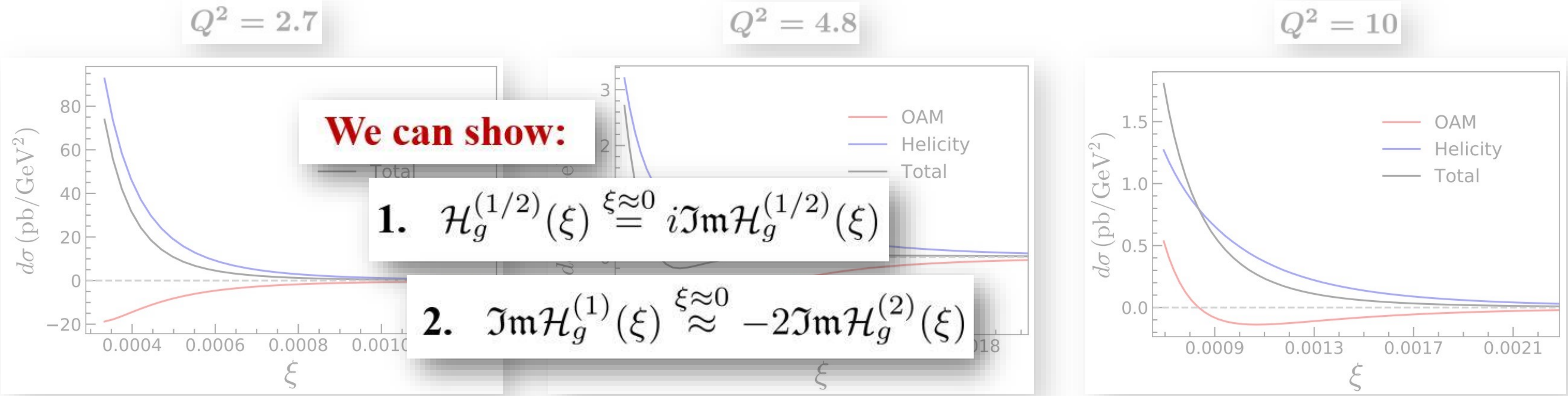


DSA:

$$\int d\phi_{q_\perp} L^{\mu\nu} A^*_\mu A_\nu \Big|_{\delta\phi=0} \sim \mathfrak{Re}\left[\mathcal{H}_g^{(1)*}(\xi)\, \tilde{\mathcal{H}}_g^{(2)}(\xi)\right] - \mathfrak{Re}\left[\left\{\mathcal{H}_g^{(1)*}(\xi) + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\mathcal{H}_g^{(2)*}(\xi)\right\}\mathcal{L}_g(\xi)\right]$$

Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section



We can show:

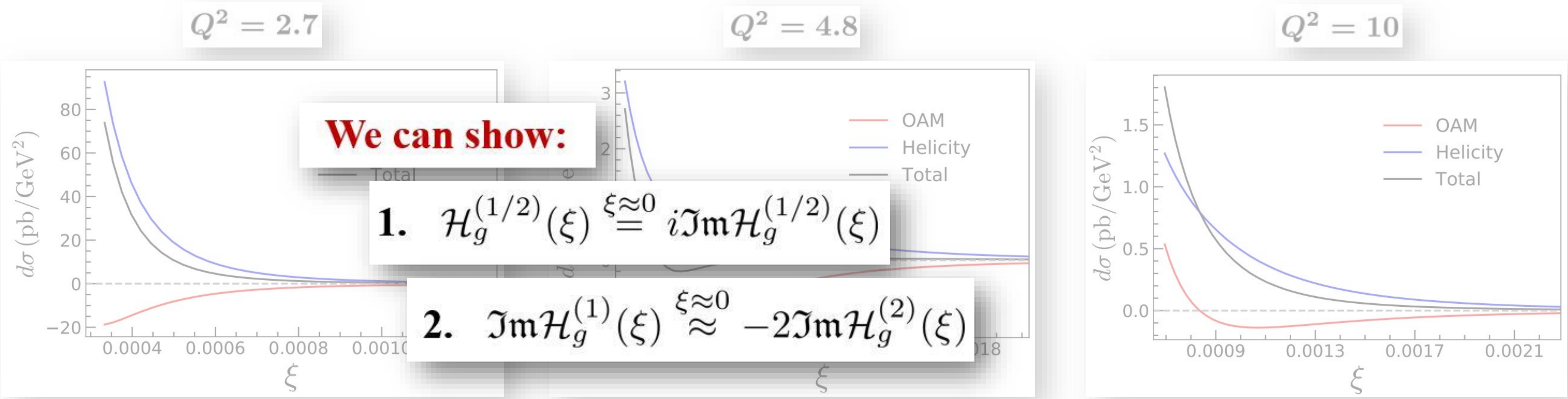
1. $\mathcal{H}_g^{(1/2)}(\xi) \overset{\xi\approx 0}{=} i\mathfrak{Im}\mathcal{H}_g^{(1/2)}(\xi)$

2. $\mathfrak{Im}\mathcal{H}_g^{(1)}(\xi) \overset{\xi\approx 0}{\approx} -2\mathfrak{Im}\mathcal{H}_g^{(2)}(\xi)$

DSA: $$\int d\phi_{q_\perp} L^{\mu\nu} A_\mu^* A_\nu \Big|_{\delta\phi=0} \sim \mathfrak{Re}\left[\mathcal{H}_g^{(1)*}(\xi)\,\tilde{\mathcal{H}}_g^{(2)}(\xi)\right] - \mathfrak{Re}\left[\left\{\mathcal{H}_g^{(1)*}(\xi) + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\mathcal{H}_g^{(2)*}(\xi)\right\}\mathcal{L}_g(\xi)\right]$$

Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section



We can show:

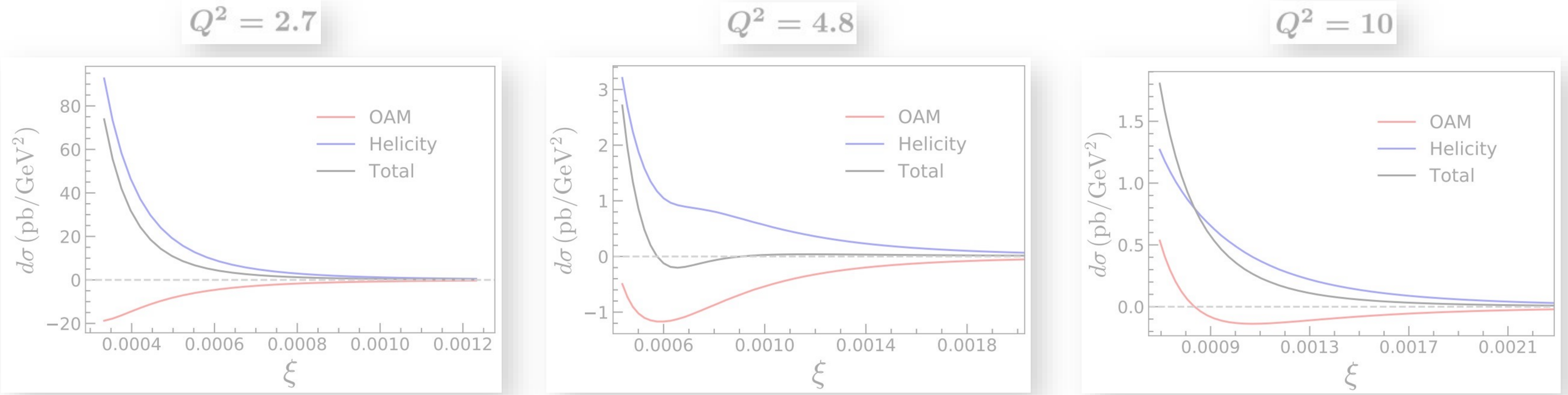
1. $\mathcal{H}_g^{(1/2)}(\xi) \overset{\xi\approx 0}{=} i\mathfrak{Im}\mathcal{H}_g^{(1/2)}(\xi)$

2. $\mathfrak{Im}\mathcal{H}_g^{(1)}(\xi) \overset{\xi\approx 0}{\approx} -2\mathfrak{Im}\mathcal{H}_g^{(2)}(\xi)$

DSA: $$\int d\phi_{q_\perp} L^{\mu\nu} A^*_\mu A_\nu \Big|_{\delta\phi=0} \sim \mathcal{H}_g^{(1)*}(\xi)\left(\tilde{\mathcal{H}}_g^{(2)}(\xi) + \frac{q_\perp^2 - Q^2/4}{q_\perp^2 + Q^2/4}\,\mathcal{L}_g(\xi)\right)$$

Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

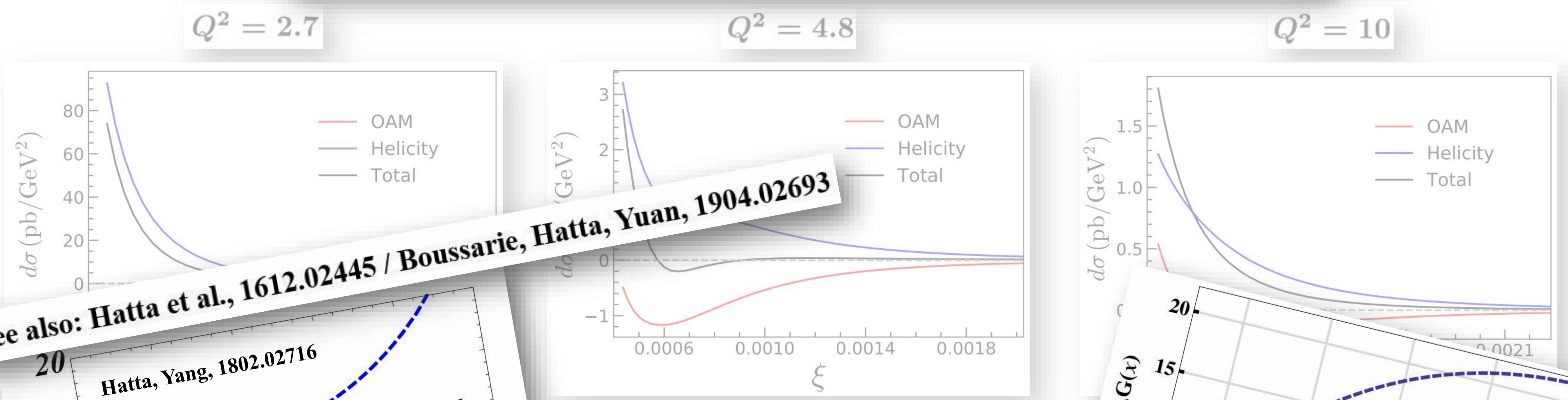


DSA: $$\int d\phi_{q_\perp} L^{\mu\nu} A^*_\mu A_\nu \Big|_{\delta\phi=0} \sim \mathcal{H}_g^{(1)*}(\xi)\left(\tilde{\mathcal{H}}_g^{(2)}(\xi) + \frac{q_\perp^2 - Q^2/4}{q_\perp^2 + Q^2/4}\mathcal{L}_g(\xi)\right)$$

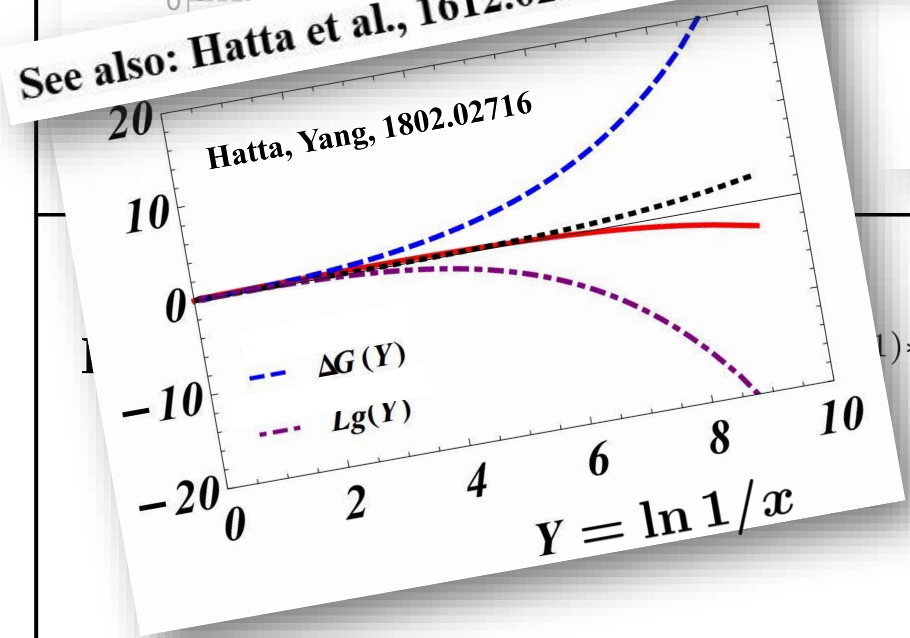
$\tilde{\mathcal{H}}_g^{(2)}$ & $\mathcal{L}_g$ **interfere positively/negatively depending upon sign of** $q_\perp^2 - \dfrac{Q^2}{4}$

Cancellation expected between Helicity & OAM at small x

$$\Delta G(x) \approx -L_g(x)$$

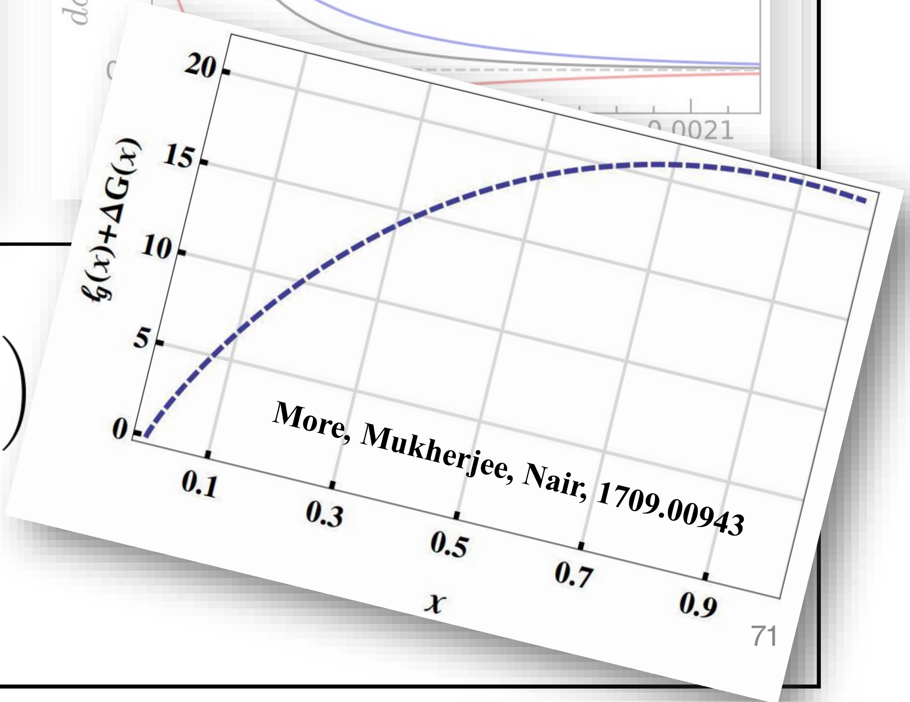


See also: Hatta et al., 1612.02445 / Boussarie, Hatta, Yuan, 1904.02693



$$\ldots)^*(\xi)\left(\tilde{\mathcal{H}}_g^{(2)}(\xi) + \frac{q_\perp^2 - Q^2/4}{q_\perp^2 + Q^2/4}\mathcal{L}_g(\xi)\right)$$

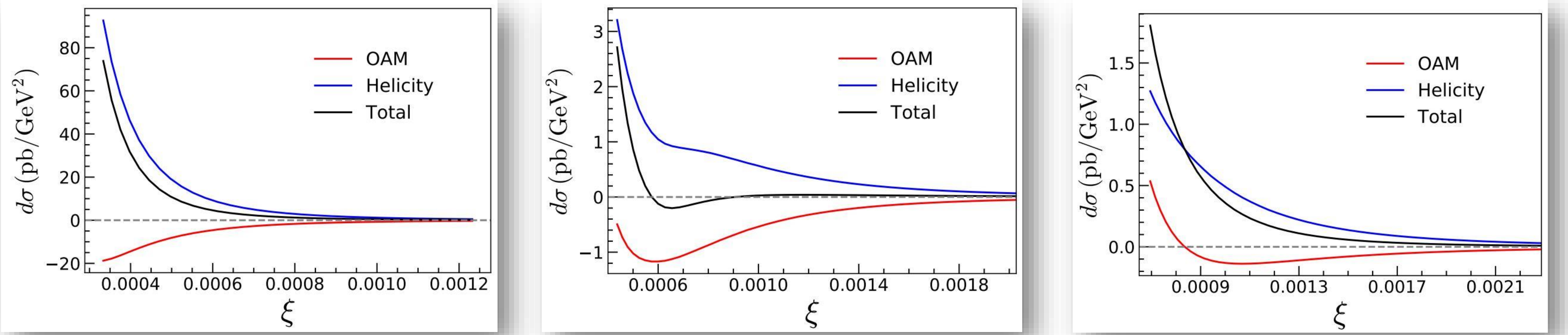
$\Delta G(x)$ $\qquad$ $L_g(x)$



Cancellation expected between Helicity & OAM at small x

$$\Delta G(x) \approx -L_g(x)$$

$Q^2 = 2.7$ $Q^2 = 4.8$ $Q^2 = 10$



Unique opportunity to study interplay between

$\Delta G(x)$ & $L_g(x)$

which has been so far only studied theoretically!

$$\left(\tilde{\mathcal{H}}_g^{(2)}(\xi) + \frac{q_\perp^2 - Q^2/4}{q_\perp^2 + Q^2/4} \mathcal{L}_g(\xi) \right)$$

$$\tilde{\mathcal{H}}_g^{(2)}(\xi) \downarrow \Delta G(x) \qquad \mathcal{L}_g(\xi) \downarrow L_g(x)$$

Summary

Summary of our work

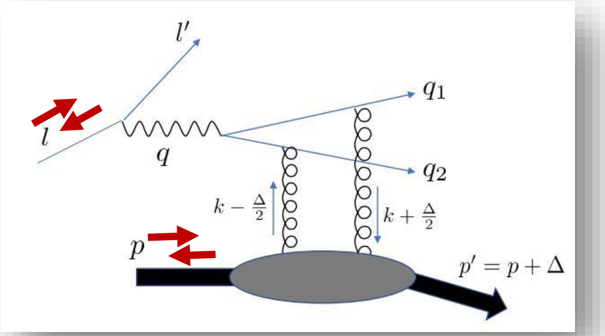
- **Gluon OAM related to the Wigner distribution**

Summary

Summary of our work

- **Gluon OAM related to the Wigner distribution**

- **DSA in exclusive dijet production is a unique observable to access the gluon OAM @ EIC:**



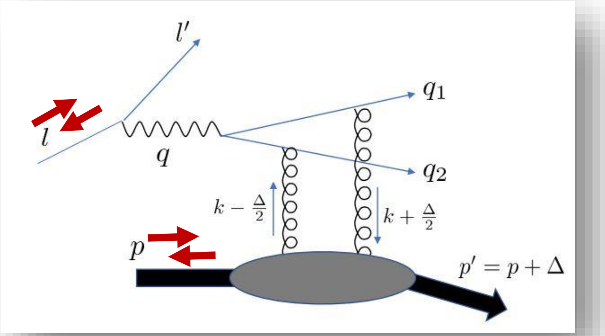
$$\int d\phi_{q_\perp} L^{\mu\nu} A^*_\mu A_\nu \sim -\,\mathfrak{Re}\left[\left\{\mathcal{H}_g^{(1)*}(\xi) + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\mathcal{H}_g^{(2)*}(\xi)\right\}\mathcal{L}_g(\xi)\right]\cos(\phi_{l_\perp}-\phi_{\Delta_\perp})$$

$$+\,\mathfrak{Re}\left[\mathcal{H}_g^{(1)*}(\xi)\,\tilde{\mathcal{H}}_g^{(2)}(\xi)\right]\cos(\phi_{l_\perp}-\phi_{\Delta_\perp})$$

Summary

Summary of our work

- **Gluon OAM related to the Wigner distribution**
- **DSA in exclusive dijet production is a unique observable to access the gluon OAM @ EIC:**



$$\int d\phi_{q_\perp} L^{\mu\nu} A^*_\mu A_\nu \sim -\,\mathfrak{Re}\left[\left\{\mathcal{H}_g^{(1)*}(\xi) + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\mathcal{H}_g^{(2)*}(\xi)\right\}\mathcal{L}_g(\xi)\right]\cos(\phi_{l_\perp}-\phi_{\Delta_\perp})$$

$$+\,\mathfrak{Re}\left[\mathcal{H}_g^{(1)*}(\xi)\,\tilde{\mathcal{H}}_g^{(2)}(\xi)\right]\cos(\phi_{l_\perp}-\phi_{\Delta_\perp})$$

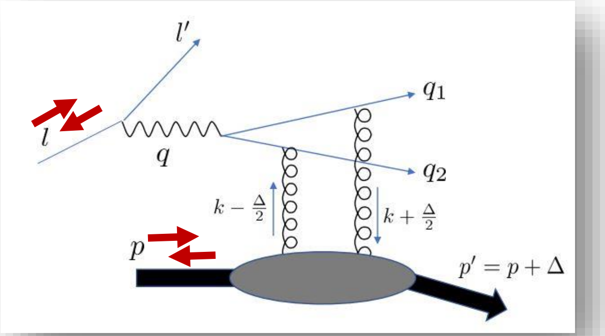
Signature of gluon OAM is cosine angular modulation

Summary

Summary of our work

DSA does not vanish for symmetric jet configurations $z = \bar{z} = \dfrac{1}{2}$

- **DSA in exclusive dijet production is a unique observable to access the gluon OAM @ EIC:**



$$\int d\phi_{q_\perp} L^{\mu\nu} A^*_\mu A_\nu \sim -\,\mathfrak{Re}\left[\left\{\mathcal{H}_g^{(1)*}(\xi) + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\mathcal{H}_g^{(2)*}(\xi)\right\}\mathcal{L}_g(\xi)\right]\cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$

$$+\,\mathfrak{Re}\left[\mathcal{H}_g^{(1)*}(\xi)\,\tilde{\mathcal{H}}_g^{(2)}(\xi)\right]\cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$

Signature of gluon OAM is cosine angular modulation

Summary

Summary of our work

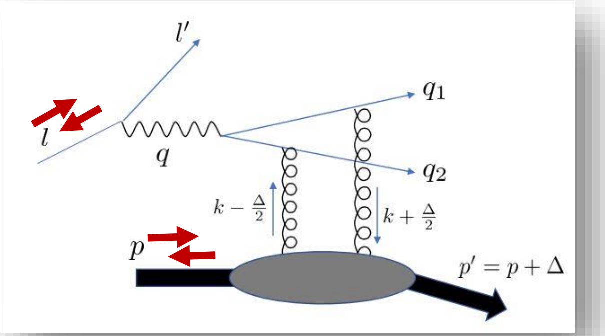
DSA does not vanish for symmetric jet configurations $z = \bar{z} = \frac{1}{2}$

Gluon OAM related to the higher ...

- DSA in exclusive dijet production is ...

Consequence:

Elimination of factorization-breaking third poles at $x = \pm\xi$



$$\int d\phi_{q_\perp} L^{\mu\nu} A^*_\mu A_\nu \sim -\Re\mathfrak{e}\left[\left\{\mathcal{H}_g^{(1)*}(\xi) + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\mathcal{H}_g^{(2)*}(\xi)\right\}\mathcal{L}_g(\xi)\right]\cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$

$$+\Re\mathfrak{e}\left[\mathcal{H}_g^{(1)*}(\xi)\tilde{\mathcal{H}}_g^{(2)}(\xi)\right]\cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$

Signature of gluon OAM is cosine angular modulation

Summary

Summary of our work

DSA does not vanish for symmetric jet configurations $z = \bar{z} = \frac{1}{2}$

Gluon OAM related to the Wigner

Consequence:

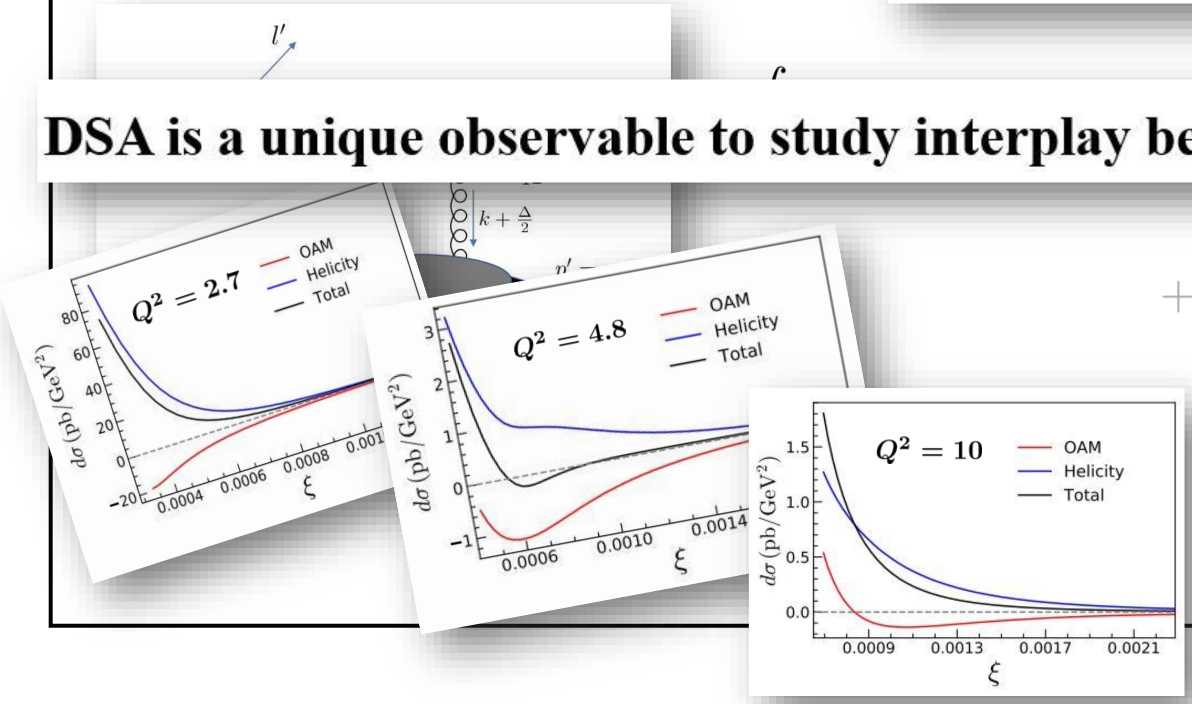
Elimination of factorization-breaking third poles at $x = \pm\xi$

- DSA in exclusive dijet production is

DSA is a unique observable to study interplay between gluon OAM & helicity

$$\mathcal{L}_g(\xi) \Big] \cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$

$$+ \Re\mathfrak{e}\Big[\mathcal{H}_g^{(1)*}(\xi)\, \tilde{\mathcal{H}}_g^{(2)}(\xi)\Big] \cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$



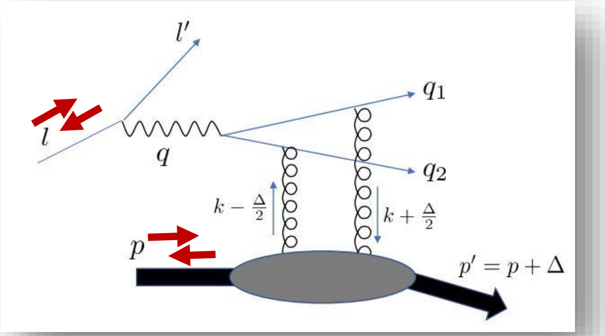
Signature of gluon OAM is cosine angular modulation

Summary

Summary of our work

- **Gluon OAM related to the Wigner distribution**

- **DSA in exclusive dijet production is a unique observable to access the gluon OAM @ EIC:**



$$\int d\phi_{q_\perp} L^{\mu\nu} A_\mu^* A_\nu \sim -\,\mathfrak{Re}\left[\left\{\mathcal{H}_g^{(1)*}(\xi) + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\mathcal{H}_g^{(2)*}(\xi)\right\}\mathcal{L}_g(\xi)\right]\cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$

$$+\,\mathfrak{Re}\left[\mathcal{H}_g^{(1)*}(\xi)\,\tilde{\mathcal{H}}_g^{(2)}(\xi)\right]\cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$

- **First realistic numerical calculation of observable sensitive to OAM @ EIC**

Backup slides

Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

Ingredients for non-perturbative functions

OAM

$$\int d\phi_{q_\perp} L^{\mu\nu} A^*_\mu A_\nu = -\frac{2^{10}\pi^4}{N_c} h_l h_p \alpha_s^2 \alpha_{em} e_q^2 \frac{(1+\xi)\xi Q^2}{(q_\perp^2+\mu^2)^2} |l_\perp||\Delta_\perp| \cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$
$$\times \mathfrak{Re}\left[\left\{\mathcal{H}_g^{(1)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(1)*} + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\left(\mathcal{H}_g^{(2)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(2)*}\right)\right\}\mathcal{L}_g + \left(\mathcal{E}_g^{(1)*} + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\mathcal{E}_g^{(2)*}\right)\frac{\mathcal{O}}{2}\right]$$

Helicity

$$\int d\phi_{q_\perp} L^{\mu\nu} A_\mu A_\nu = \frac{2^{10}\pi^4}{N_c} h_l h_p \alpha_s^2 \alpha_{em} e_q^2 \frac{(1-\xi^2)\xi Q^2}{(q_\perp^2+\mu^2)^2} |l_\perp||\Delta_\perp| \cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$
$$\times \mathfrak{Re}\left[\left(\mathcal{H}_g^{(1)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(1)*}\right)\left(\tilde{\mathcal{H}}_g^{(2)} - \frac{\xi^2}{1-\xi^2}\tilde{\mathcal{E}}_g^{(2)}\right)\right]$$

Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

Ingredients for non-perturbative functions

- **Neglect contributions from** $(E_g,\, \tilde{E}_g)\,,\; F_{1,2}$ $\longrightarrow$ **Very simple formula**

OAM

$$\int d\phi_{q_\perp} L^{\mu\nu} A_\mu^* A_\nu = -\frac{2^{10}\pi^4}{N_c} h_l h_p \alpha_s^2 \alpha_{em} e_q^2 \frac{(1+\xi)\xi Q^2}{(q_\perp^2+\mu^2)^2} |l_\perp||\Delta_\perp| \cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$
$$\times \mathfrak{Re}\left[\left\{\mathcal{H}_g^{(1)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(1)*} + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\left(\mathcal{H}_g^{(2)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(2)*}\right)\right\}\mathcal{L}_g + \left(\mathcal{E}_g^{(1)*} + \frac{4q_\perp^2}{q_\perp^2+\mu^2}\mathcal{E}_g^{(2)*}\right)\frac{\mathcal{O}}{2}\right]$$

Helicity

$$\int d\phi_{q_\perp} L^{\mu\nu} A_\mu A_\nu = \frac{2^{10}\pi^4}{N_c} h_l h_p \alpha_s^2 \alpha_{em} e_q^2 \frac{(1-\xi^2)\xi Q^2}{(q_\perp^2+\mu^2)^2} |l_\perp||\Delta_\perp| \cos(\phi_{l_\perp} - \phi_{\Delta_\perp})$$
$$\times \mathfrak{Re}\left[\left(\mathcal{H}_g^{(1)*} - \frac{\xi^2}{1-\xi^2}\mathcal{E}_g^{(1)*}\right)\left(\tilde{\mathcal{H}}_g^{(2)} - \frac{\xi^2}{1-\xi^2}\tilde{\mathcal{E}}_g^{(2)}\right)\right]$$

Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

Ingredients for non-perturbative functions

- **Neglect contributions from** $(E_g,\, \tilde{E}_g)\,,\, F_{1,2}$ $\longrightarrow$ **Very simple formula**
- **Model** $(H_g,\, \tilde{H}_g)$ **according to the Double distribution approach (see for instance Radyushkin, 9805342)**

$$\boxed{\begin{pmatrix} H_g(x,\xi) \\ \tilde{H}_g(x,\xi) \end{pmatrix} = \int_{-1}^{1} d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha\, \delta(\beta+\xi\alpha - x) \times \frac{15}{16} \frac{[(1-|\beta|)^2-\alpha^2]^2}{(1-|\beta|)^5} \times \begin{cases} \beta\, G(\beta) \\ \beta\, \Delta G(\beta) \end{cases}}$$

Probing gluon OAM through exclusive dijet production

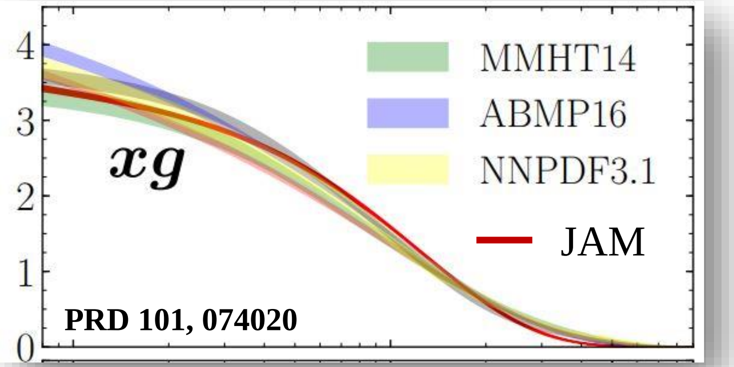
Numerical estimate of cross section

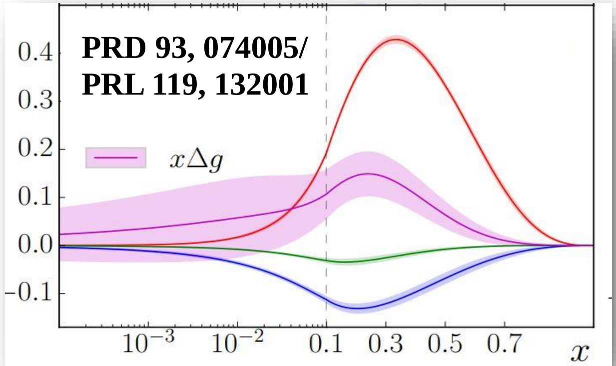
Ingredients for non-perturbative functions

- **Neglect contributions from** $(E_g,\, \tilde{E}_g)\,,\, F_{1,2} \longrightarrow$ **Very simple formula**
- **Model** $(H_g,\, \tilde{H}_g)$ **according to the Double distribution approach (see for instance Radyushkin, 9805342)**

$$\boxed{\begin{pmatrix} H_g(x,\xi) \\ \tilde{H}_g(x,\xi) \end{pmatrix} = \int_{-1}^{1} d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha\, \delta(\beta + \xi\alpha - x) \times \frac{15}{16} \frac{[(1-|\beta|)^2 - \alpha^2]^2}{(1-|\beta|)^5} \times \begin{cases} \beta\, G(\beta) \\ \beta\, \Delta G(\beta) \end{cases}}$$

JAM PDFs





Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

Ingredients for non-perturbative functions

- **Neglect contributions from** $(E_g,\, \tilde{E}_g)\,,\, F_{1,2} \longrightarrow$ **Very simple formula**
- **Model** $(H_g,\, \tilde{H}_g)$ **according to the Double distribution approach (see for instance Radyushkin, 9805342)**
- **Model for OAM:**

Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

Ingredients for non-perturbative functions

- **Neglect contributions from** $(E_g,\, \tilde{E}_g)\,,\, F_{1,2}$ $\longrightarrow$ **Very simple formula**
- **Model** $(H_g,\, \tilde{H}_g)$ **according to the Double distribution approach (see for instance Radyushkin, 9805342)**
- **Model for OAM:**

1. "OAM density": (Hatta, Yoshida, 1207.5332)

$$L^g_{can}(\boldsymbol{x}) \;=\; x\int_x^1 \frac{dx'}{x'^2}\left(H_g(x')+E_g(x')\right) \;-\; 2x\int_x^1 \frac{dx'}{x'^2}\Delta G(x') + \text{ genuine twist-three}$$

Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

Ingredients for non-perturbative functions

- **Neglect contributions from** $(E_g,\, \tilde{E}_g)\,,\, F_{1,2}$ $\longrightarrow$ **Very simple formula**
- **Model** $(H_g,\, \tilde{H}_g)$ **according to the Double distribution approach (see for instance Radyushkin, 9805342)**
- **Model for OAM:**

1. "OAM density": (Hatta, Yoshida, 1207.5332)

$$\boxed{L^g_{can}(x) \overset{\text{WW approx}}{\approx} x\int_x^1 \frac{dx'}{x'^2}\big(\underbrace{H_g(x')}_{H_g(x') = x'G(x')} + \underbrace{E_g(x')}_{\text{Neglect } E_g}\big) - 2x\int_x^1 \frac{dx'}{x'^2}\Delta G(x') + \cancel{\text{genuine twist-three}}}$$

Probing gluon OAM through exclusive dijet production

Numerical estimate of cross section

Ingredients for non-perturbative functions

- **Neglect contributions from** $(E_g,\, \tilde{E}_g)\,,\, F_{1,2}$ $\longrightarrow$ **Very simple formula**
- **Model** $(H_g,\, \tilde{H}_g)$ **according to the Double distribution approach (see for instance Radyushkin, 9805342)**
- **Model for OAM:**

1. "OAM density": (Hatta, Yoshida, 1207.5332)

$$\boxed{L^g_{can}(\boldsymbol{x}) \overset{\text{WW approx}}{\approx} x\int_x^1 \frac{dx'}{x'^2}(H_g(x') + E_g(x')) - 2x\int_x^1 \frac{dx'}{x'^2}\Delta G(x') + \cancel{\text{genuine twist-three}}}$$

2. Use the Double distribution approach to construct $xL_g(x,\boldsymbol{\xi})$ from $xL_g(x)$ (GPD-like approach)

Probing gluon OAM through exclusive dijet production

Cross section

Jet azimuthal angle ($\phi_{q_\perp}$) integrated out

$$\frac{d\sigma}{dy dQ^2 d\phi_{l_\perp} dz dq_\perp^2 d^2\Delta_\perp} = \frac{\alpha_{em} y}{2^{11}\pi^7 Q^4} \frac{\int d\phi_{q_\perp} L^{\mu\nu} A_\mu^* A_\nu}{(W^2+Q^2)(W^2-M_J^2)z\bar{z}}$$

Integrate assuming a Gaussian form factor

$$\sim e^{-b\Delta_\perp^2}$$

Slope = 5

(See Braun, Ivanov, 0505263)