

# Exclusive Processes and GPDs with CLAS/CLAS12



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For the CLAS Collaboration

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**UConn** | UNIVERSITY OF  
CONNECTICUT

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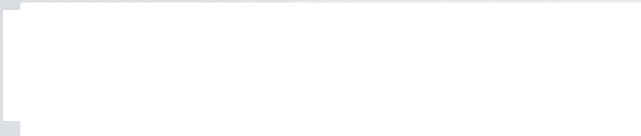
**Jefferson Lab**



# 3-Dimensional Imaging of Quarks and Gluons

Wigner distributions

$$\rho(x, \vec{k}_T, \vec{b}_T)$$



Longitudinal momentum

$$k^+ = xP^+$$

$x$ : longitudinal momentum fraction carried by struck parton



Transverse position

$\vec{k}_T$

Transverse momentum

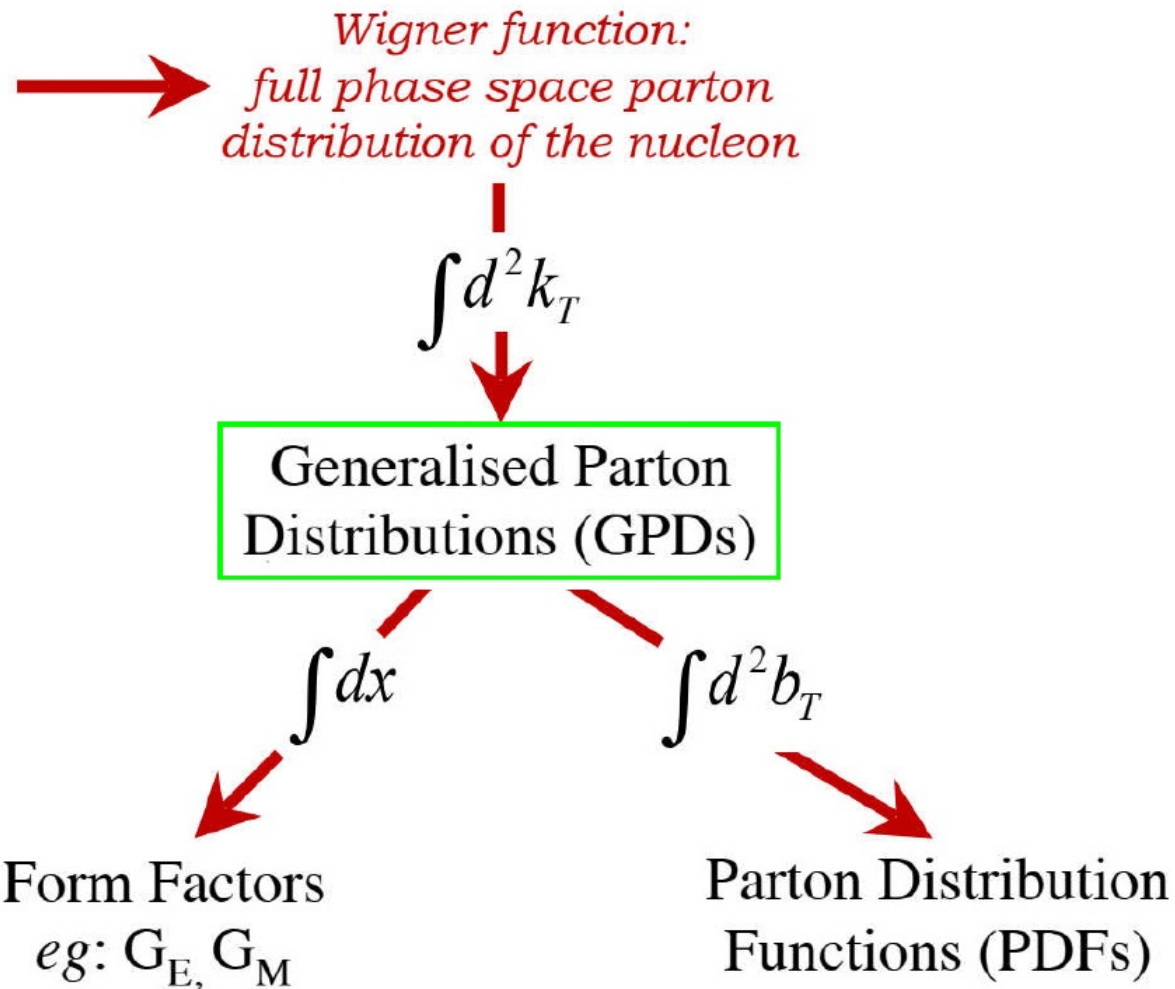
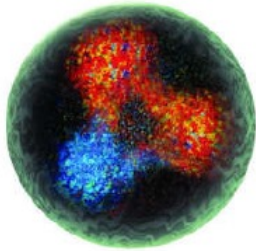
$\vec{b}_T$

partons

Transverse plane

A. Bacchetta

# 3-Dimensional Imaging of Quarks and Gluons



## Generalized Parton Distributions (GPDs)

$$W_{\Gamma}(\mathbf{r}, k) = \frac{1}{2M_N} \int \frac{d^3\mathbf{q}}{(2\pi)^3} e^{-i\mathbf{q}\cdot\mathbf{r}} \left\langle \mathbf{q}/2 \left| \hat{\mathcal{W}}_{\Gamma}(0, k) \right| -\mathbf{q}/2 \right\rangle$$

Integrate over transverse  
*momentum* space

Generalized Parton Distributions  
(GPD)

3-D nucleon images in the  
transverse coordinate and  
longitudinal momentum space

quark pol.

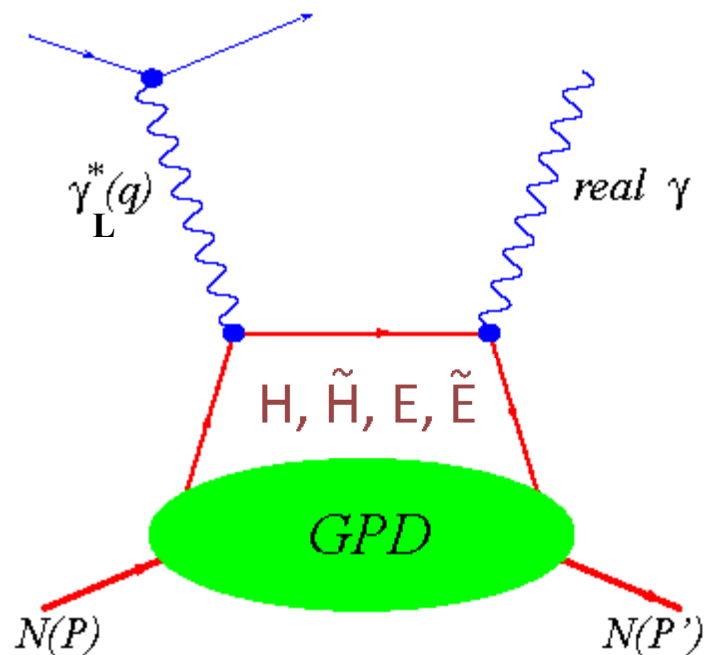
N/q	$U$	$L$	$T$
$U$	$H$		$\bar{E}_T$
$L$		$\tilde{H}$	$\tilde{E}_T$
$T$	$E$	$\tilde{E}$	$H_T, \tilde{H}_T$

nucleon pol.

$$\bar{E}_T = 2\tilde{H}_T + E_T$$

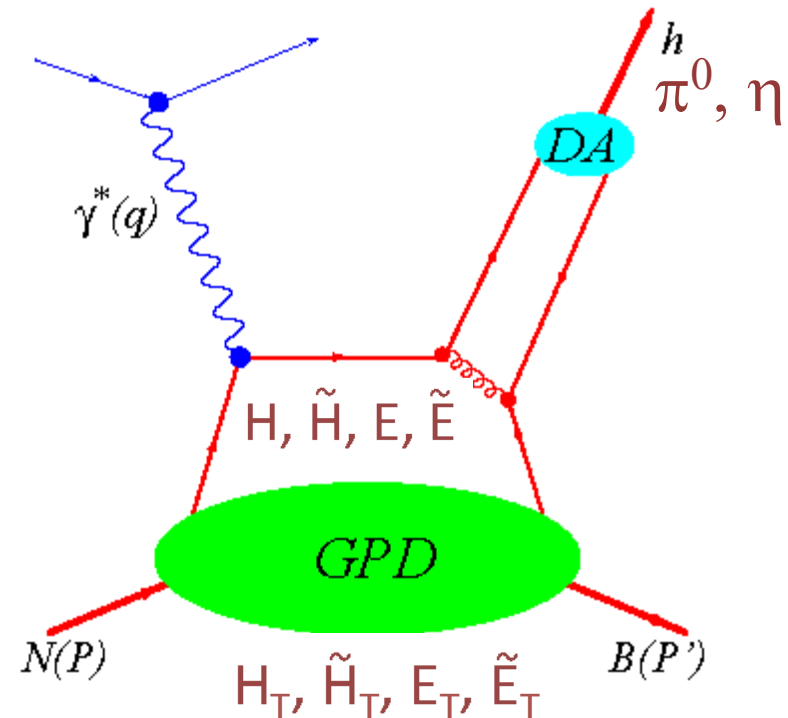
# Study GPDs: Deeply Virtual Exclusive Processes

## Deeply Virtual Compton Scattering (DVCS)



- + Clean process
- Only sensitive to chiral even GPDs

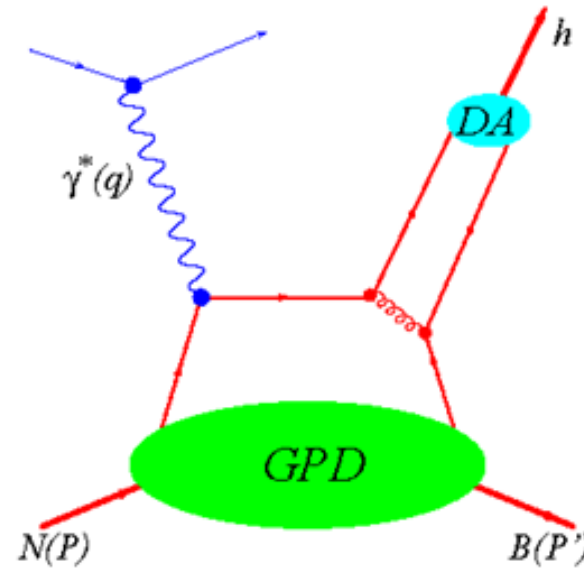
## Deeply Virtual Meson Production (DVMP)



- + Enables Flavour decomposition of GPDs
- + Access to transversity degrees of freedom described by chiral-odd GPDs
- Distribution Amplitude (DA) is involved as additional soft non pert. quantity

## Deeply Virtual Meson Production in the GPD regime

	Meson	Flavor
$\mathcal{H}_T, \bar{\mathcal{E}}_T$ $\tilde{\mathcal{H}}, \tilde{\mathcal{E}}$	$\pi^+$	$\Delta u - \Delta d$
	$\pi^0$	$2\Delta u + \Delta d$
	$\eta$	$2\Delta u - \Delta d + 2\Delta s$
$\mathcal{H}, \mathcal{E}$	$\rho^+$	$u - d$
	$\rho^0$	$2u + d$
	$\omega$	$2u - d$
	$\phi$	$g$



$$\kappa_T^u = \int dx \bar{E}_T^u(x, \xi, t=0)$$

$$\kappa_T^d = \int dx \bar{E}_T^d(x, \xi, t=0)$$

$\bar{\mathcal{E}}_T$  is related to the proton's  
anomalous tensor magnetic moment

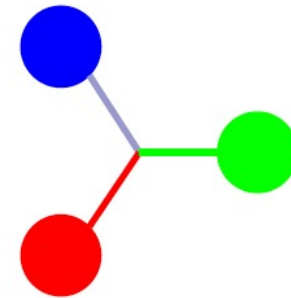
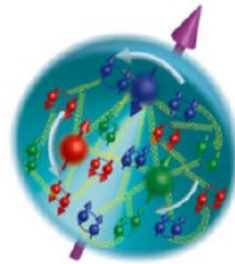
$$\delta_T^u = \int dx H_T^u(x, \xi, t=0)$$

$$\delta_T^d = \int dx H_T^d(x, \xi, t=0)$$

$\mathcal{H}_T$  is related to the proton's tensor charge  
→ Absolute magnitude of transversely polarized  
valence quarks inside a transv. polarized nucleon

# From the ground state nucleon to resonances

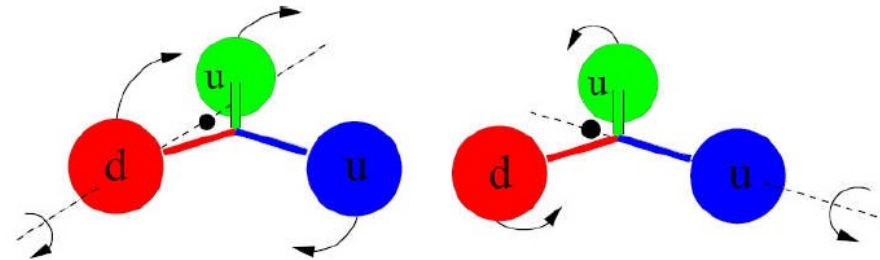
Ground state nucleon:  
(proton, neutron)



Nucleon resonances:

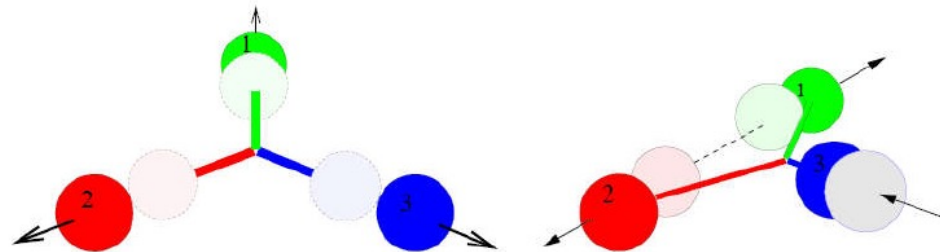
➤ Orbital excitations

i.e N(1535)



➤ Radial excitations

i.e N(1440)



# From classical GPD to transition GPDs

**Past:** Extensive studies of transition form factors (**2D picture** of transv. position)

**But:** How does the excitation affect the **3D structure** of the Nucleon?

→ Pressure distributions, tensor charge, ... of resonances?

→ Information encoded in **transition GPDs**

→ More difficult theoretical description due to additional degrees of freedom

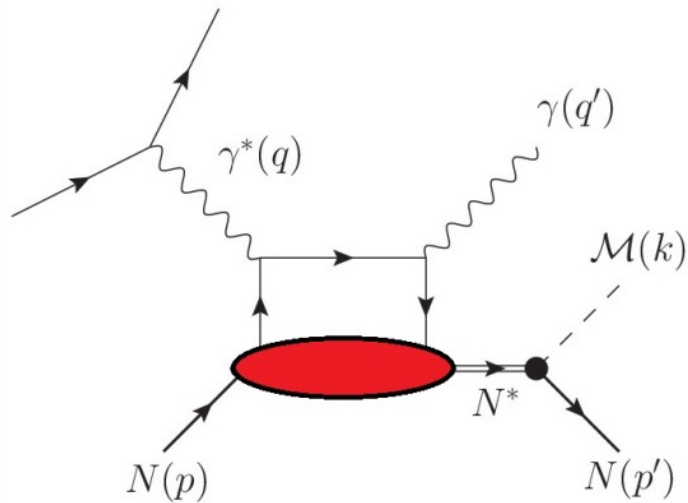
Simplest case:  $N \rightarrow \Delta$  transition

→ **16 transition GPDs**

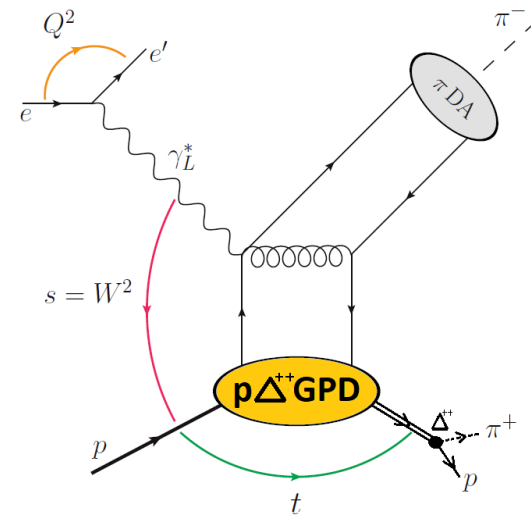
- 8 helicity non-flip transition GPDs (twist 2)
- 8 helicity flip transition GPDs



# Studies of Transition GPDs



**non-diag. DVCS**



**non-diag. DVMP**

- **8 helicity non-flip trans. GPDs (twist 2)**

- 3 are dominating in the large  $N_c$  limit

- Connection to proton-proton GPDs via symmetry considerations

- Description of leading twist effects / longitudinal photons →  $\sigma_L$

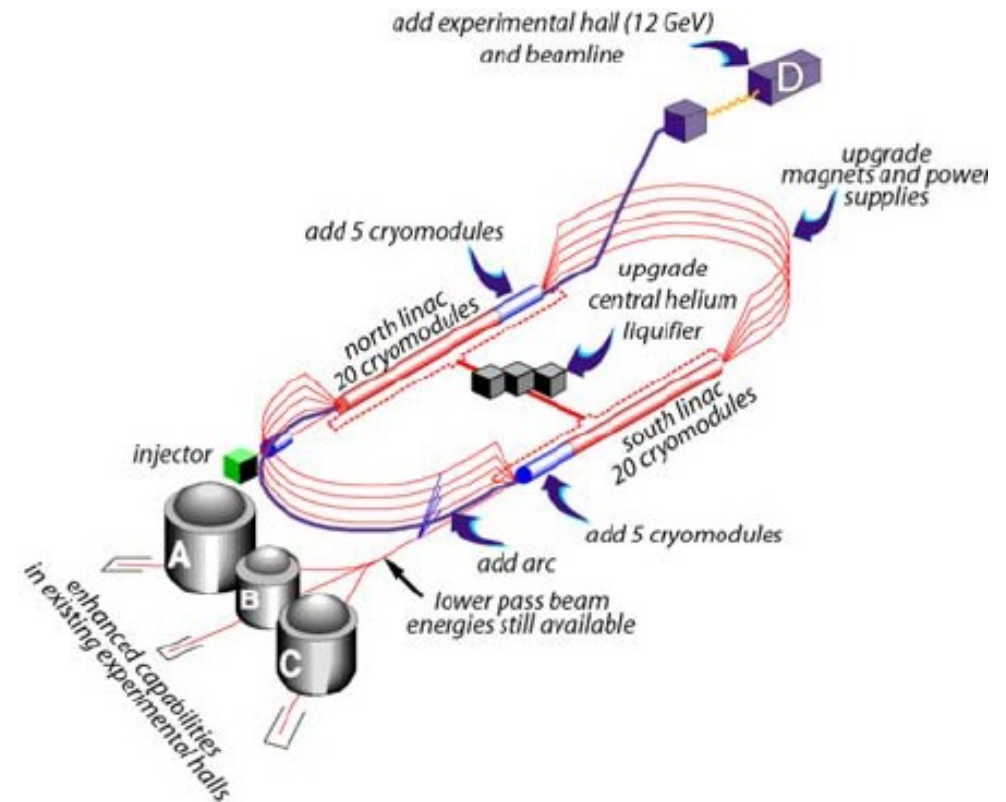
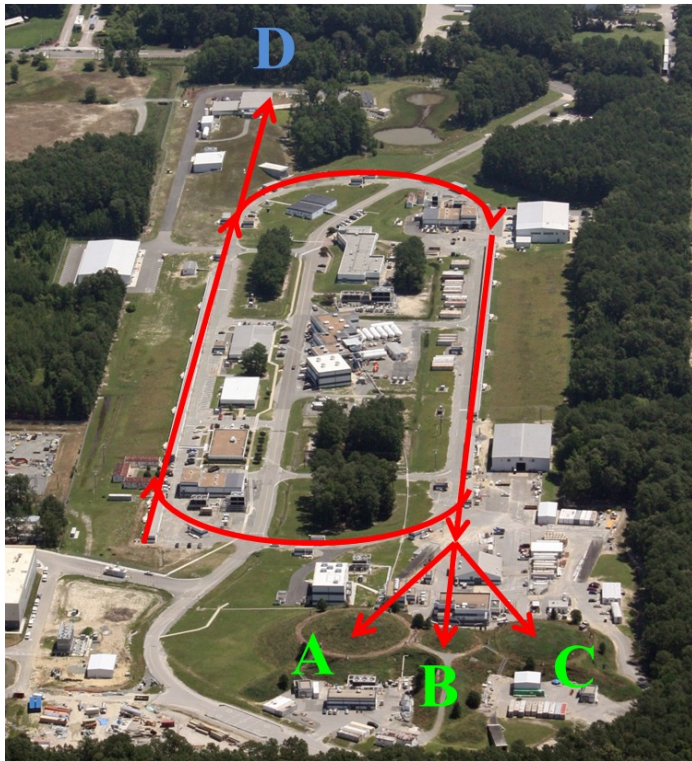
- First theoretical works available

- **8 helicity flip trans. GPDs**

- Needed for twist-3 sector (non-diag DVMP)

- Theory in progress (no publ. so far)

# Thomas Jefferson National Accelerator Facility (Jefferson Lab)



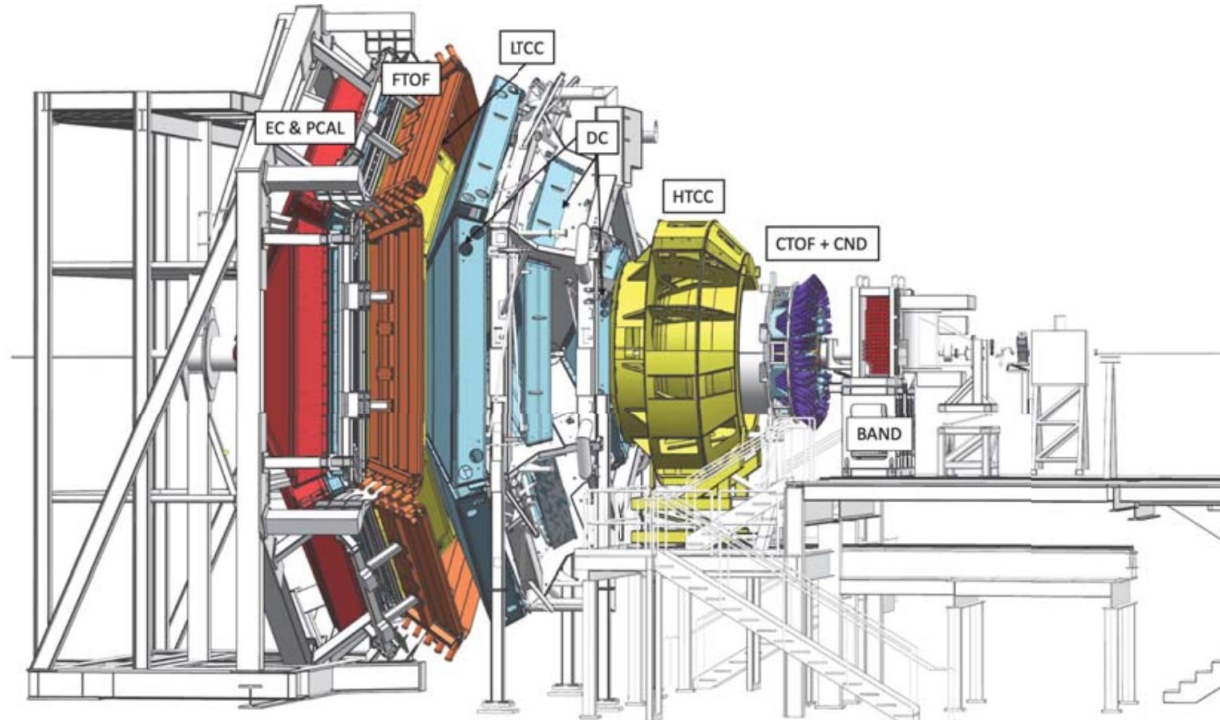
## CEBAF Upgrade completed in September 2017

- electron beam
- $E_{\max} = 12 \text{ GeV}$
- $I_{\max} = 90 \mu\text{A}$
- $\text{Pol}_{\max} \sim 90\%$

## Physics Operation

- 4 halls running simultaneously since January 2018

# CLAS12 Experimental Setup in Hall B at JLAB



V. Burkert et al., Nucl. Instrum. Meth.A 959 (2020) 163419

- Data recorded with CLAS12 during fall 2018 and spring 2019
- 10.6 / 10.2 GeV  $e^-$  beam
- $\sim 87\%$  average polarization
- liquid  $H_2$  target

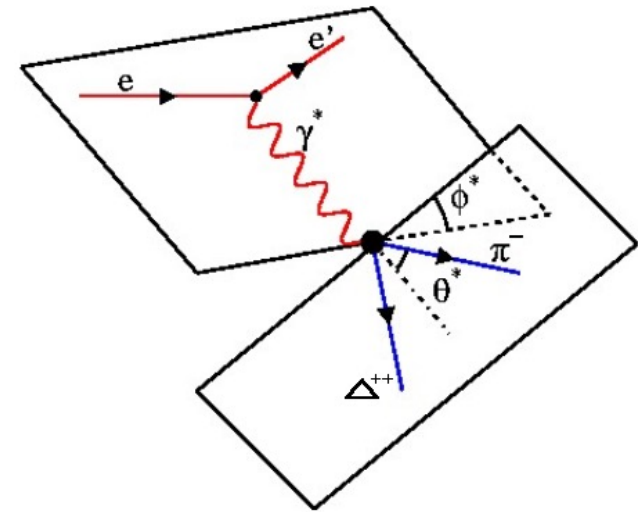
**1. Hard exclusive pseudoscalar / vector meson  
Electroproductions (GPDs)**

**2.  $ep \rightarrow e\Delta^{++}\pi^- \rightarrow ep\pi^+\pi^-$  (N- $\rightarrow$  $\Delta$  transition  
GPDs)**

# Hard Exclusive Meson Electroproduction and Beam Spin Asymmetries (BSA)

Cross section (longitudinally pol. beam and unpol. target):

$$2\pi \frac{d^2\sigma}{dt d\phi} = \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} + \epsilon \cdot \cos(2\phi) \frac{d\sigma_{TT}}{dt} \\ + \sqrt{2\epsilon(1+\epsilon)} \cdot \cos(\phi) \frac{d\sigma_{LT}}{dt} \\ + h \cdot \sqrt{2\epsilon(1-\epsilon)} \cdot \sin(\phi) \frac{d\sigma_{LT'}}{dt}$$



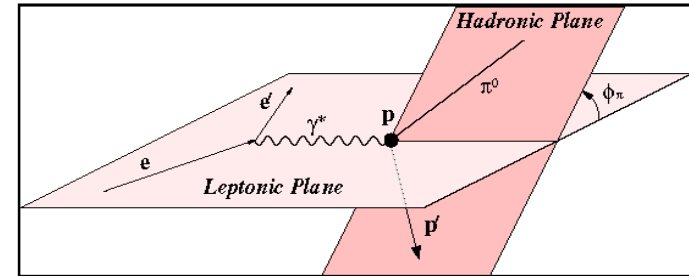
Beam Spin Asymmetry:

$$BSA(t, \phi, x_B, Q^2) = \frac{d\sigma^+ - d\sigma^-}{d\sigma^+ + d\sigma^-} = \frac{\sqrt{2\epsilon(1-\epsilon)} \frac{\sigma_{LT'}}{\sigma_0} \sin \phi}{1 + \sqrt{2\epsilon(1+\epsilon)} \frac{\sigma_{LT}}{\sigma_0} \cos \phi + \epsilon \frac{\sigma_{TT}}{\sigma_0} \cos 2\phi}$$

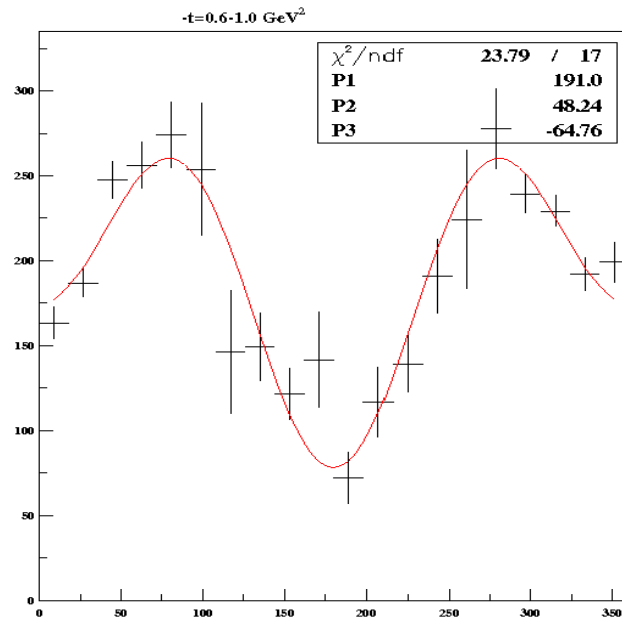
# Differential Cross Sections for $ep \rightarrow ep\pi^0$

Structure Functions

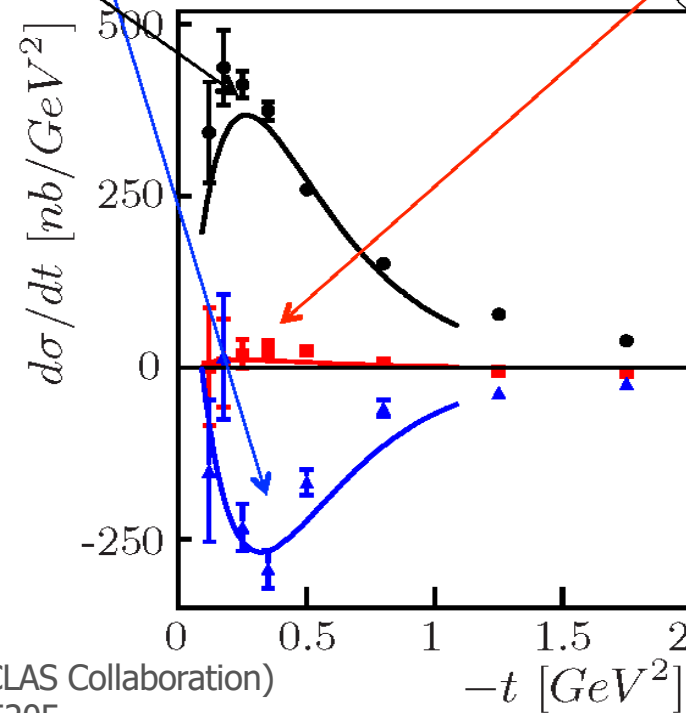
$$\sigma_U = \sigma_T + \epsilon \sigma_L \quad \sigma_{TT} \quad \sigma_{LT}$$



$$\frac{d\sigma}{dt d\phi}(Q^2, x, t, \phi) = \frac{1}{2\pi} \left( \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt} \cos \phi$$



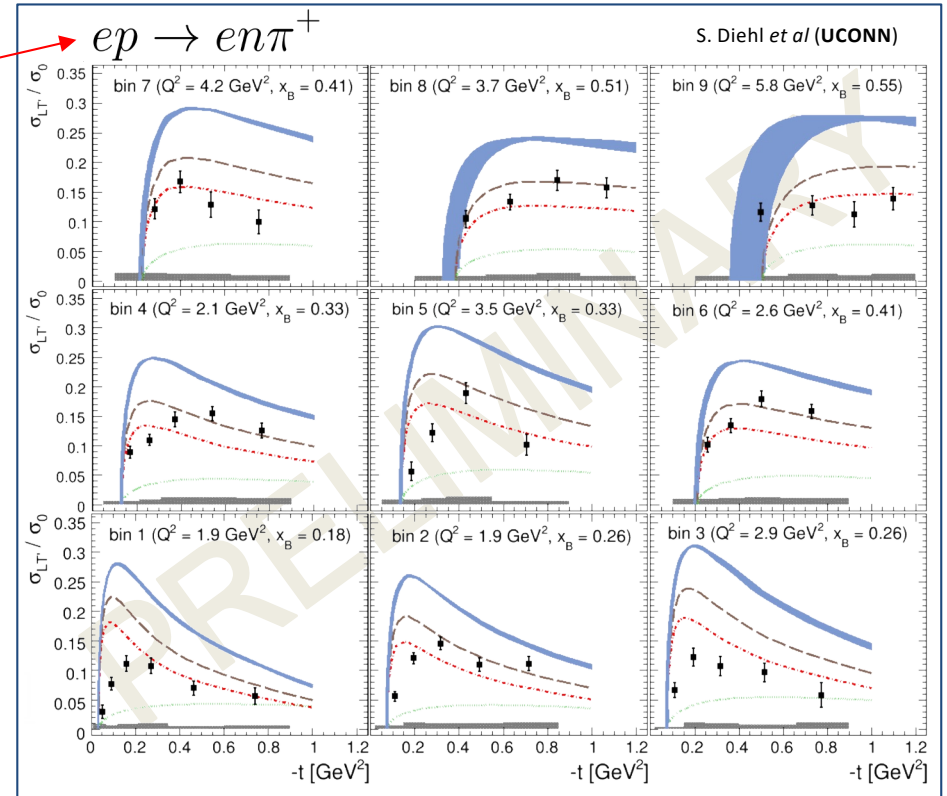
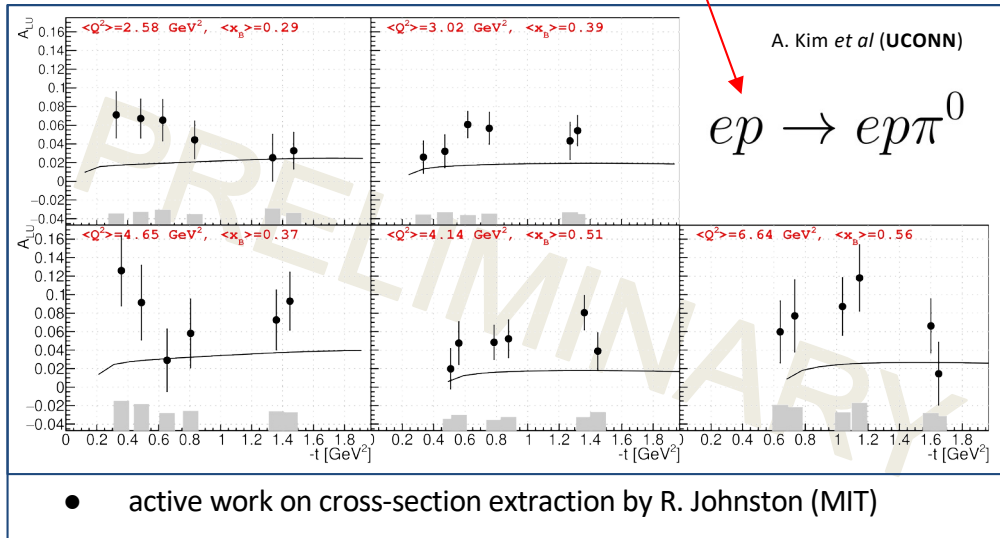
$\phi$  distribution



I. Bedlinskiy *et al.* (CLAS Collaboration)  
Phys. Rev. C **90**, 025205

# Pseudoscalar meson electroproduction with CLAS12

$$\sigma_{LT'} = \xi \sqrt{1 - \xi^2} \frac{\sqrt{-t'}}{2m} \times \text{Im} \left[ \langle H_T \rangle^* \langle \tilde{E} \rangle + \langle \tilde{E}_T \rangle^* \langle \tilde{H} \rangle \right]$$



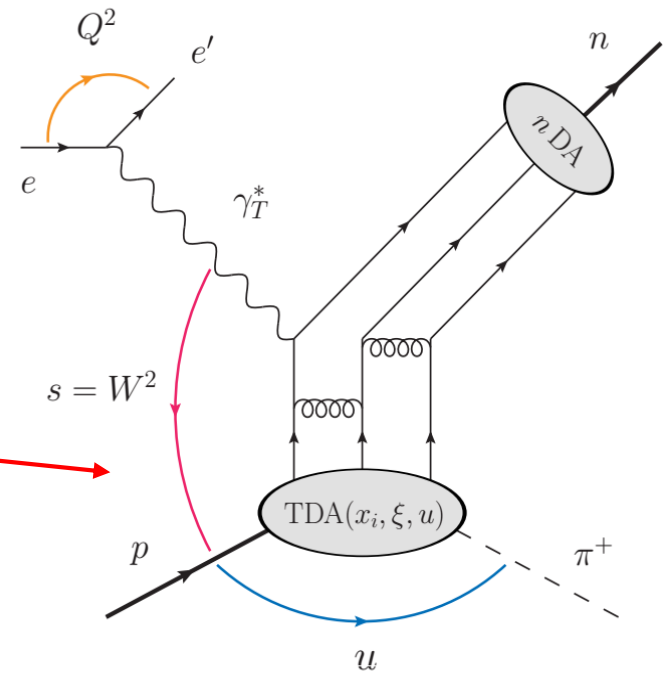
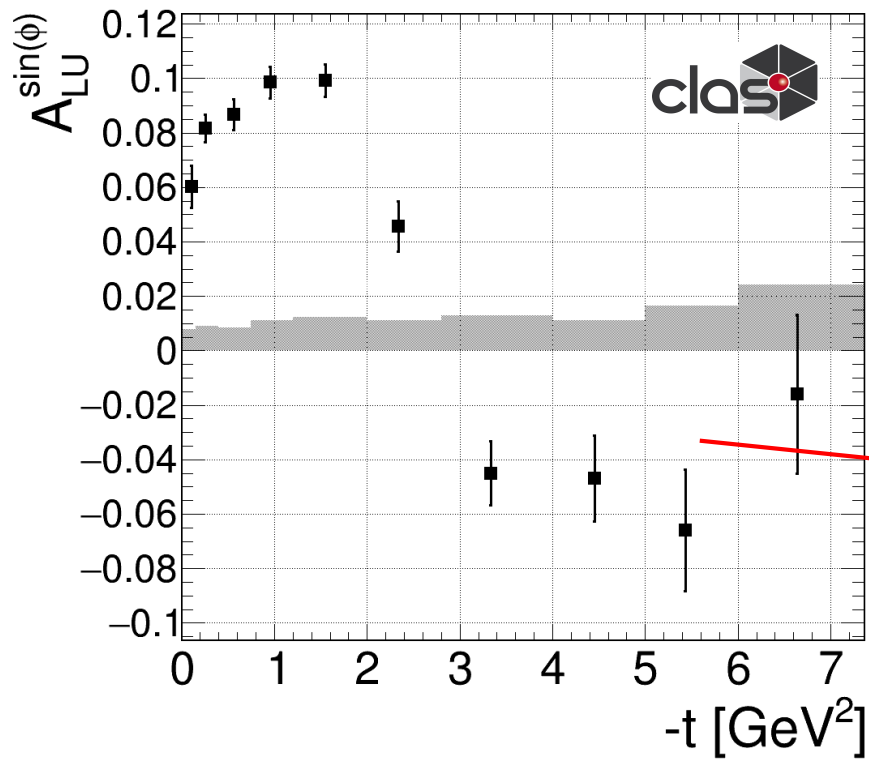
GK model

Additionally active work on  $\eta$  beam spin asymmetry and cross-section extraction

# Beam spin asymmetry for $ep \rightarrow en\pi^+$

$$BSA_i = \frac{1}{P_e} \cdot \frac{N_i^+ - N_i^-}{N_i^+ + N_i^-}$$

$$BSA = \frac{A_{LU}^{\sin \phi} \sin \phi}{1 + A_{UU}^{\cos \phi} \cos \phi + A_{UU}^{\cos(2\phi)} \cos(2\phi)}$$



S. Diehl et al. (CLAS collaboration),  
**Phys. Rev. Lett. 125, 182001 (2020)**

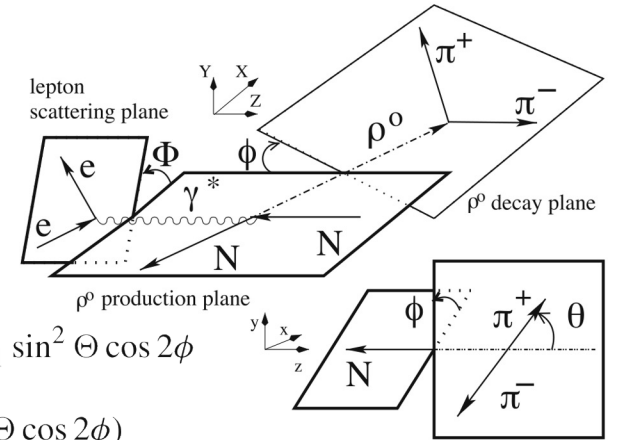


# Vector meson production: Spin Density Matrix Elements (SDME)

$$\frac{d\sigma}{d\phi d\Phi d\Theta dQ^2 dx_B dt} = \Gamma(Q^2, x_B, E) \frac{1}{2\pi} \left\{ \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right\} \mathcal{W}^{U+L}(\Phi, \phi, \cos \Theta)$$

$$\mathcal{W}^{U+L}(\Phi, \phi, \cos \Theta) = \mathcal{W}^U(\Phi, \phi, \cos \Theta) + P_b \mathcal{W}^L(\Phi, \phi, \cos \Theta),$$

$$\begin{aligned} \mathcal{W}^U(\Phi, \phi, \cos \Theta) = & \frac{3}{8\pi^2} \left[ \frac{1}{2}(1 - r_{00}^{04}) + \frac{1}{2}(3r_{00}^{04} - 1) \cos^2 \Theta - \sqrt{2} \text{Re}\{r_{10}^{04}\} \sin 2\Theta \cos \phi - r_{1-1}^{04} \sin^2 \Theta \cos 2\phi \right. \\ & - \epsilon \cos 2\Phi (r_{11}^1 \sin^2 \Theta + r_{00}^1 \cos^2 \Theta - \sqrt{2} \text{Re}\{r_{10}^1\} \sin 2\Theta \cos \phi - r_{1-1}^1 \sin^2 \Theta \cos 2\phi) \\ & - \epsilon \sin 2\Phi (\sqrt{2} \text{Im}\{r_{10}^2\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^2\} \sin^2 \Theta \sin 2\phi) \\ & + \sqrt{2\epsilon(1+\epsilon)} \cos \Phi (r_{11}^5 \sin^2 \Theta + r_{00}^5 \cos^2 \Theta - \sqrt{2} \text{Re}\{r_{10}^5\} \sin 2\Theta \cos \phi - r_{1-1}^5 \sin^2 \Theta \cos 2\phi) \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \sin \Phi (\sqrt{2} \text{Im}\{r_{10}^6\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^6\} \sin^2 \Theta \sin 2\phi) \right], \\ \mathcal{W}^L(\Phi, \phi, \cos \Theta) = & \frac{3}{8\pi^2} [\sqrt{1-\epsilon^2} (\sqrt{2} \text{Im}\{r_{10}^3\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^3\} \sin^2 \Theta \sin 2\phi) \\ & + \sqrt{2\epsilon(1-\epsilon)} \cos \Phi (\sqrt{2} \text{Im}\{r_{10}^7\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^7\} \sin^2 \Theta \sin 2\phi) \\ & + \sqrt{2\epsilon(1-\epsilon)} \sin \Phi (r_{11}^8 \sin^2 \Theta + r_{00}^8 \cos^2 \Theta - \sqrt{2} \text{Re}\{r_{10}^8\} \sin 2\Theta \cos \phi - r_{1-1}^8 \sin^2 \Theta \cos 2\phi)] \end{aligned}$$



# Vector meson production: Spin Density Matrix Elements (SDME)

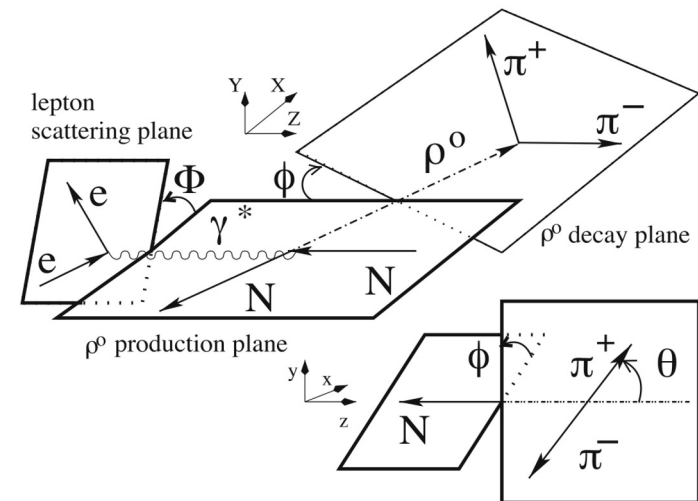
$$\frac{d\sigma}{d\phi d\Phi d\Theta dQ^2 dx_B dt} = \Gamma(Q^2, x_B, E) \frac{1}{2\pi} \left\{ \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right\} \mathcal{W}^{U+L}(\Phi, \phi, \cos \Theta)$$

After simplifications from Eur. Phys. J. C (2014):

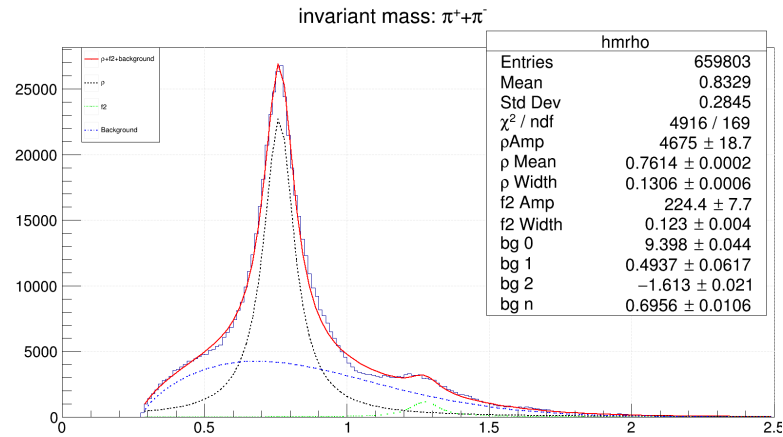
$$r_{00}^1 \sigma_0 \sim |\bar{E}_T|^2$$

$$r_{00}^5 \sigma_0 \sim \text{Re} [\langle \bar{E}_T \rangle \langle H \rangle + \langle H_T \rangle \langle E \rangle]$$

$$r_{00}^8 \sigma_0 \sim \text{Im} [\langle \bar{E}_T \rangle \langle H \rangle + \langle H_T \rangle \langle E \rangle]$$

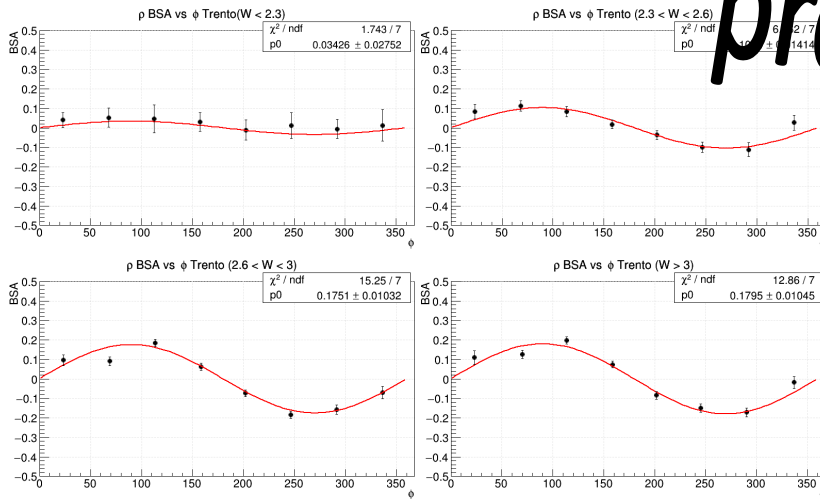


# Exclusive $\rho$ production with CLAS12

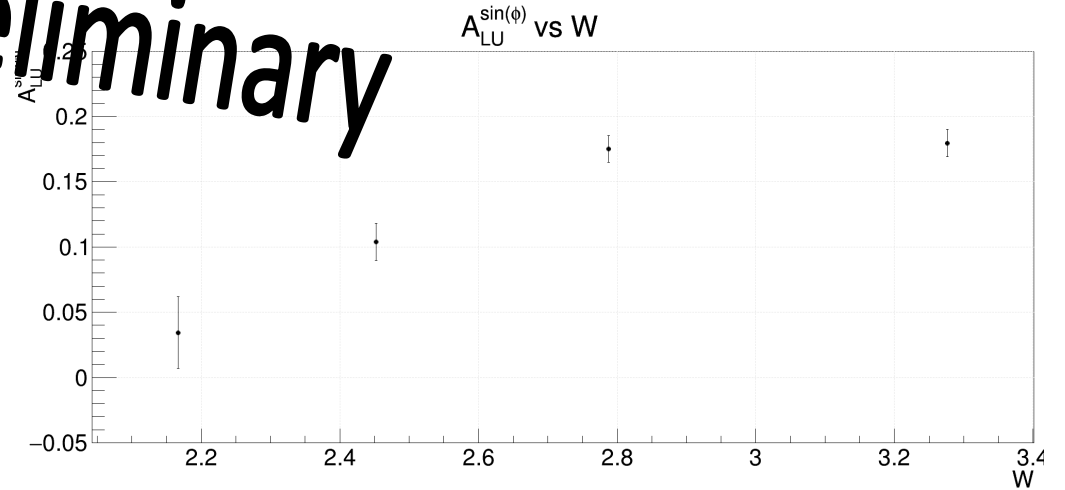


$$\sigma_{LT'} \sim r_{00}^8 \sim \text{Im} \left[ \langle H_T \rangle^* \langle E \rangle + \langle \bar{E}_T \rangle^* \langle H \rangle \right]$$

$$BSA = \frac{A_{LU}^{\sin \phi} \sin \phi}{1 + A_{UU}^{\cos \phi} \cos \phi + A_{UU}^{\cos(2\phi)} \cos(2\phi)}$$

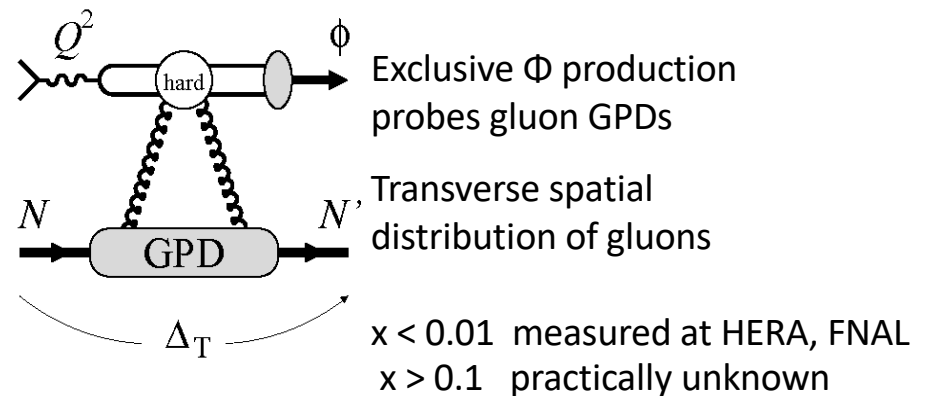
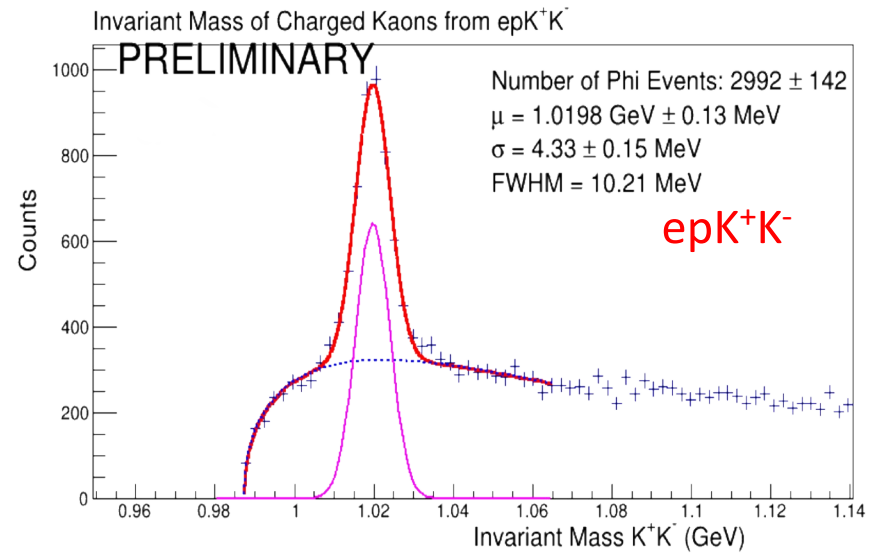
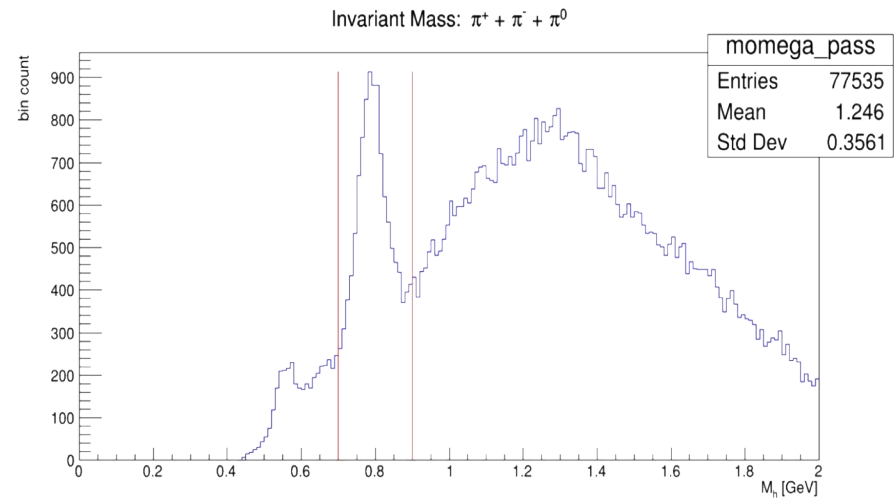
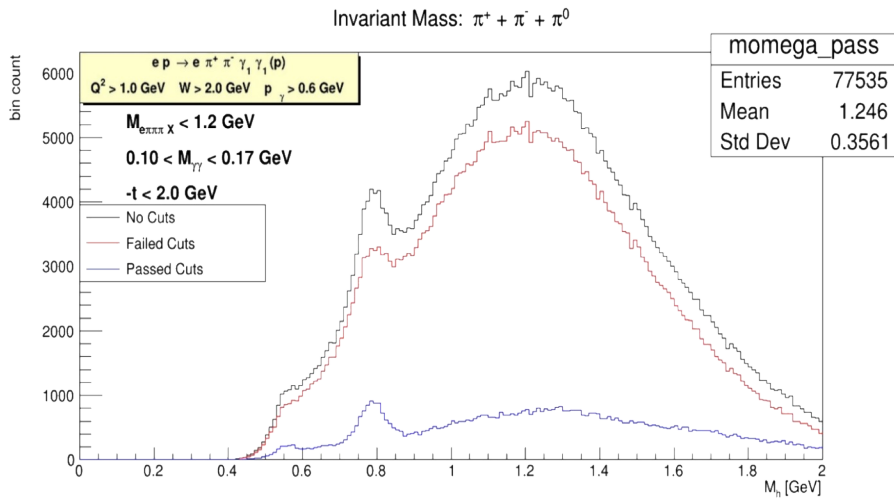


preliminary

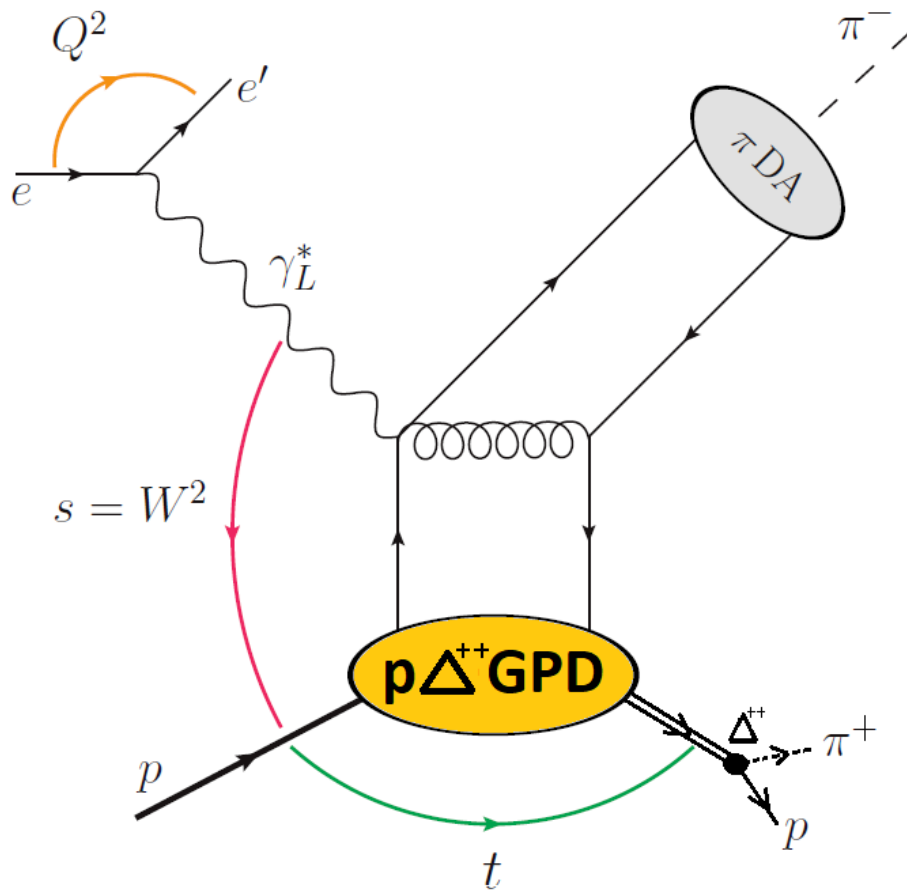


$$BSA_i = \frac{1}{P_e} \cdot \frac{N_i^+ - N_i^-}{N_i^+ + N_i^-}$$

# Exclusive $\omega$ , $\phi$ production with CLAS12



$$ep \rightarrow e\Delta^{++}\pi^{-} \rightarrow ep\pi^{+}\pi^{-}$$



**Factorization expected for:**

$$-t / Q^2 \ll 1 \text{ and } Q^2 > M_{\Delta}^2$$

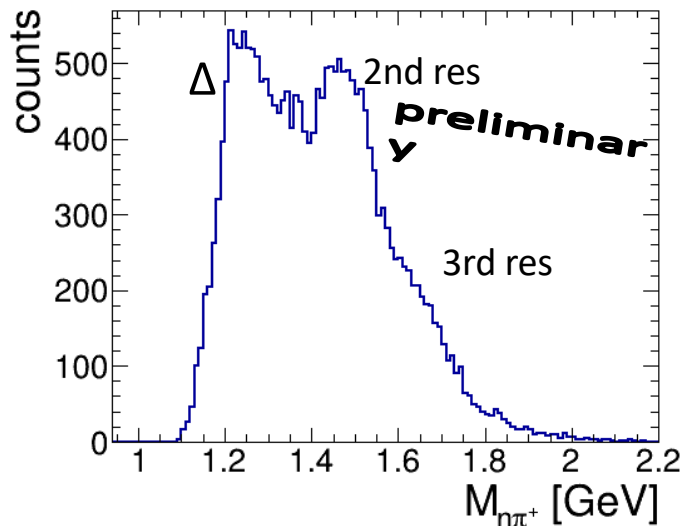
$x_B$  fixed

- ➔ Provides access to p- $\Delta$  transition GPDs
- ➔ 3D structure of the  $\Delta$  resonance and of the excitation process
- $\pi^{\pm}$  is expected to be especially sensitive to the tensor charge of the resonance

# Why is $\pi^-\Delta^{++}$ special?

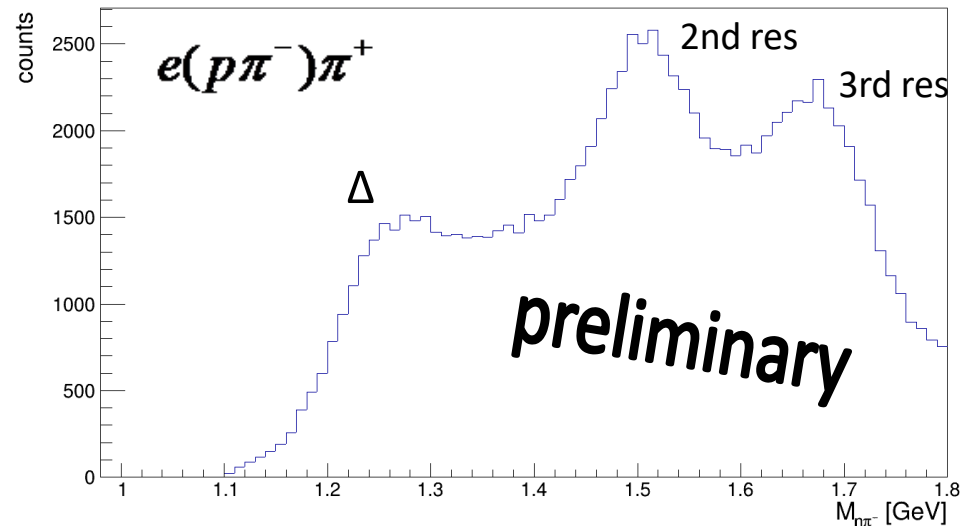
non-diagonal DVCS

$$\gamma^* p \rightarrow N^* \gamma \rightarrow p \text{ meson } \gamma$$



other non-diagonal DVMP channels

$$ep \rightarrow e\Delta^0\pi^+ \rightarrow e(p\pi^-\pi^+)$$



$$ep \rightarrow e\Delta^{++}\pi^- \rightarrow \underbrace{ep\pi^+\pi^-}_{I_z = +3/2}$$

➔ The  $p\pi^+$  final state can **only** be populated by  **$\Delta$ -resonances**

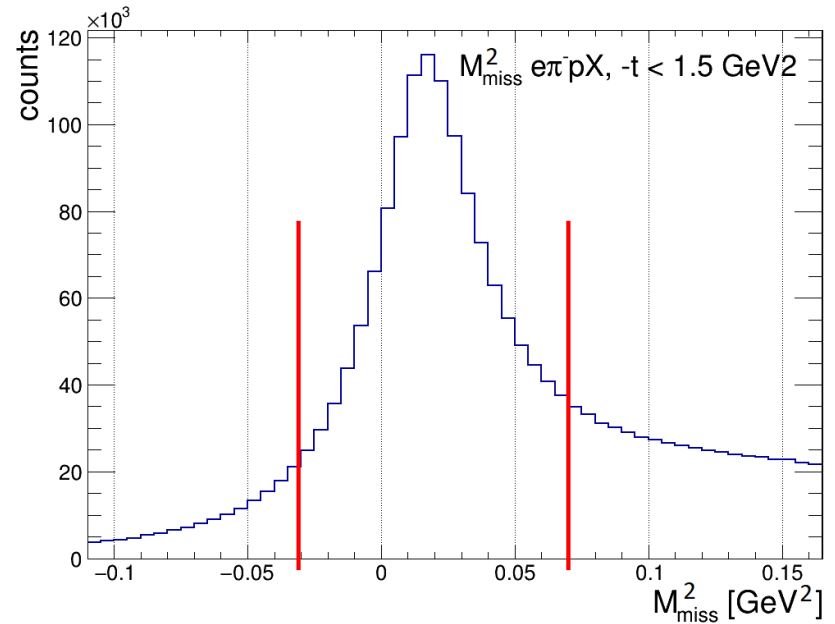
- Large gap between  $\Delta(1232)$  and higher resonances

## Event Selection and Kinematic Cuts

$$ep \rightarrow e\Delta^{++}\pi^{-} \rightarrow ep\pi^{-}X$$

$$X = \pi^{+}$$

- 2  $\sigma$  cut around the missing  $\pi^{+}$

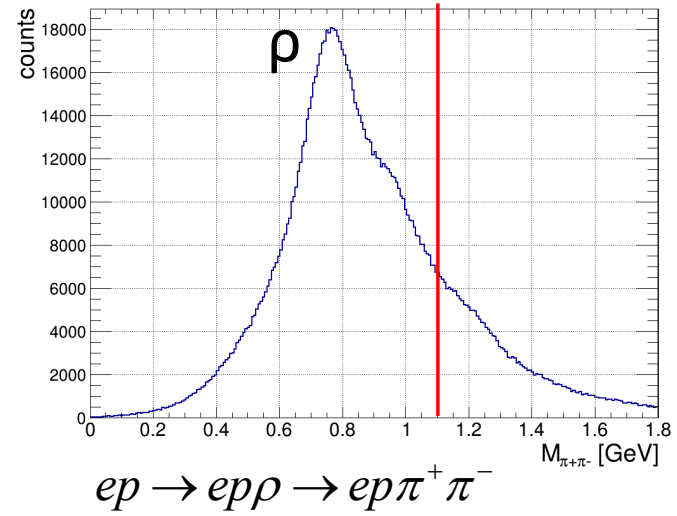
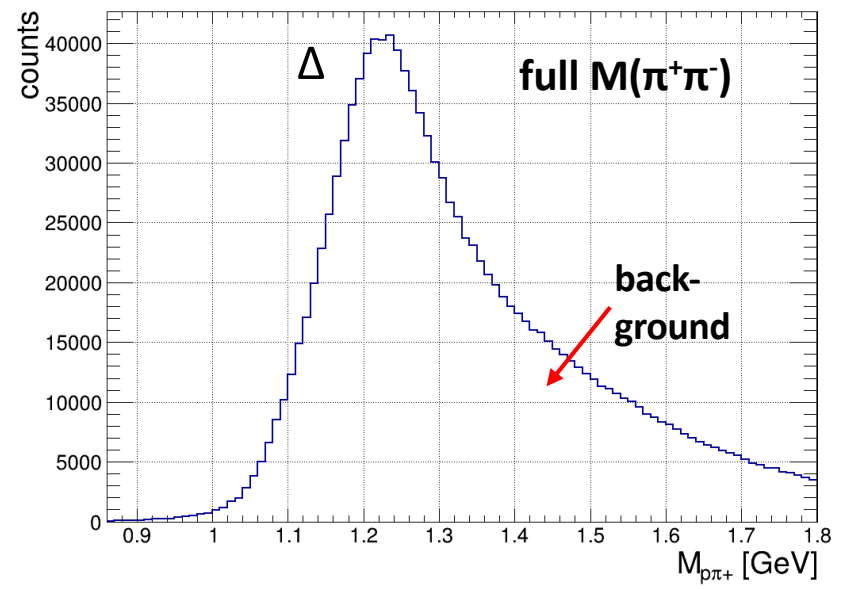
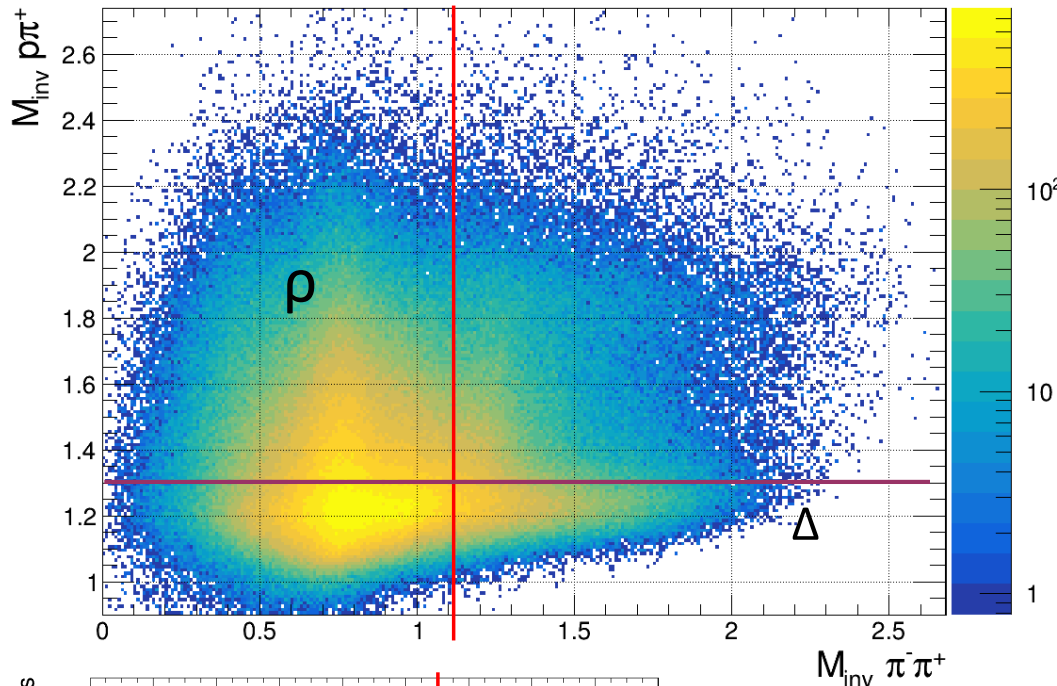


### Kinematic cuts:

$$Q^2 > 1.5 \text{ GeV}^2 \quad W > 2 \text{ GeV} \quad y < 0.75$$

$$-t < 1.5 \text{ GeV}^2 \text{ (only the forward region)}$$

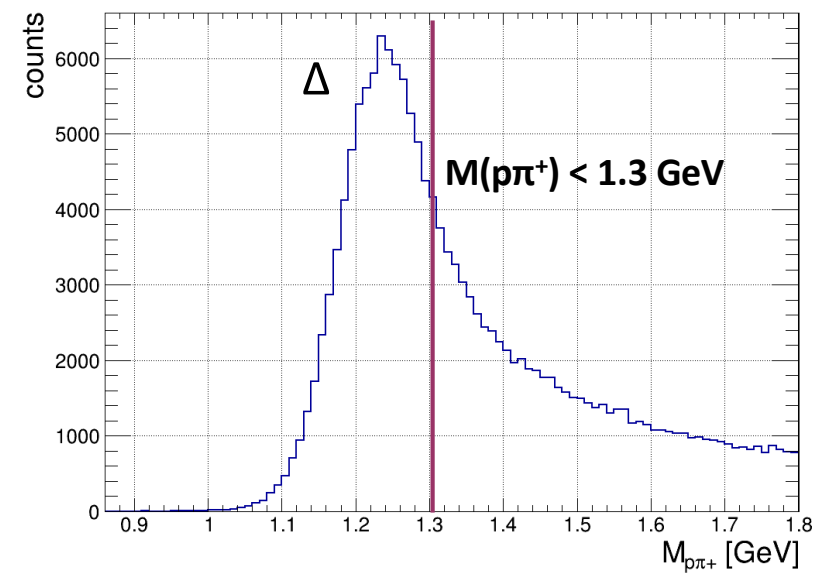
# Event Selection and Background Rejection



$M(\pi^+\pi^-) > 1.1 \text{ GeV}$

**rho contamination**

**< 0.8 %**





# Monte Carlo Simulations

## 2 MC samples have been used:

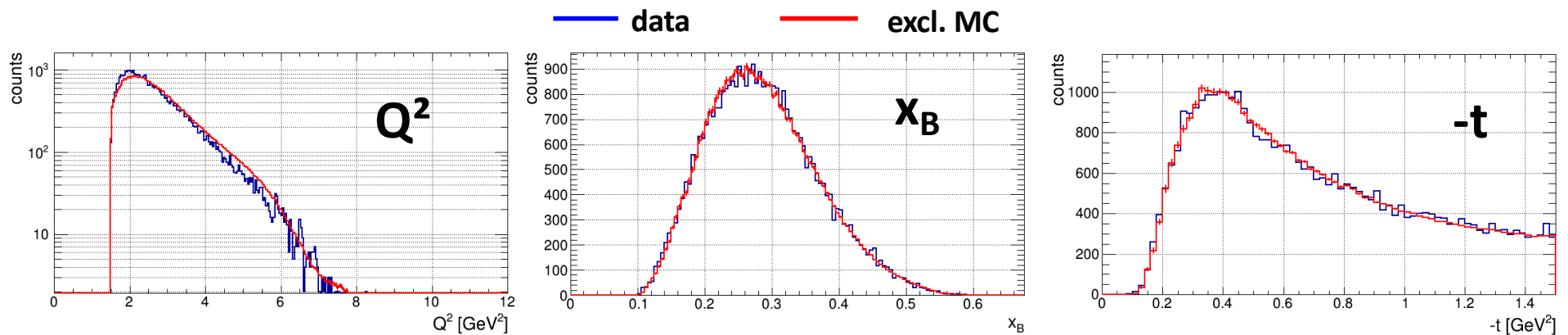
### a) Semi-inclusive DIS MC

- ☐ Does not contain the  $\pi^-\Delta^{++}$  production in „forward“ kinematics
- ☐ Contains nonres. background as well as  $\rho$  production and other potential BG channels
- ☐ Used to estimate background shape and contaminations

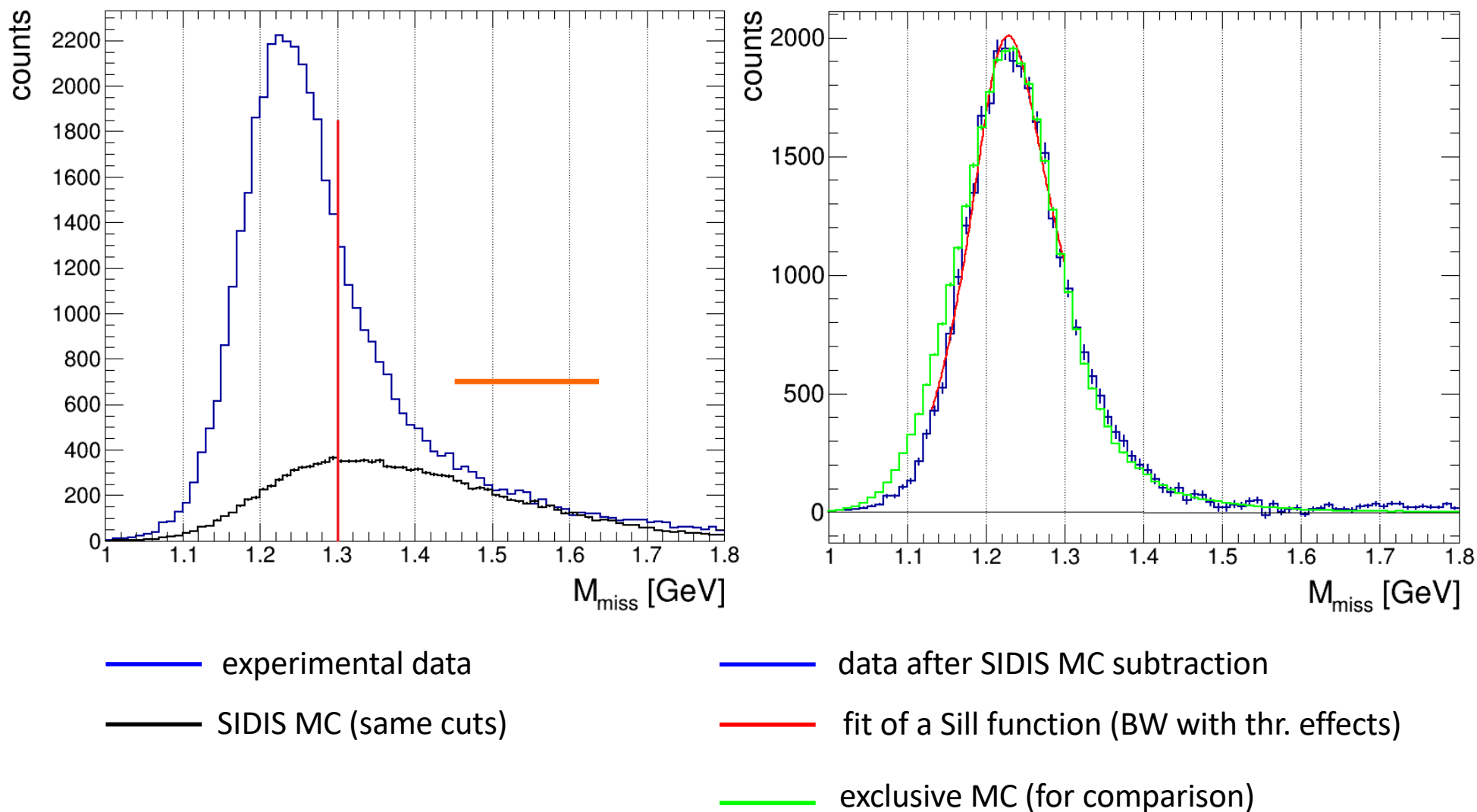
### b) Exclusive $\pi^-\Delta^{++}$ MC

- ☐ Phase space simulation with a weight added to match experimental data
- ☐  $\Delta$  peak with PDG mass and FWHM

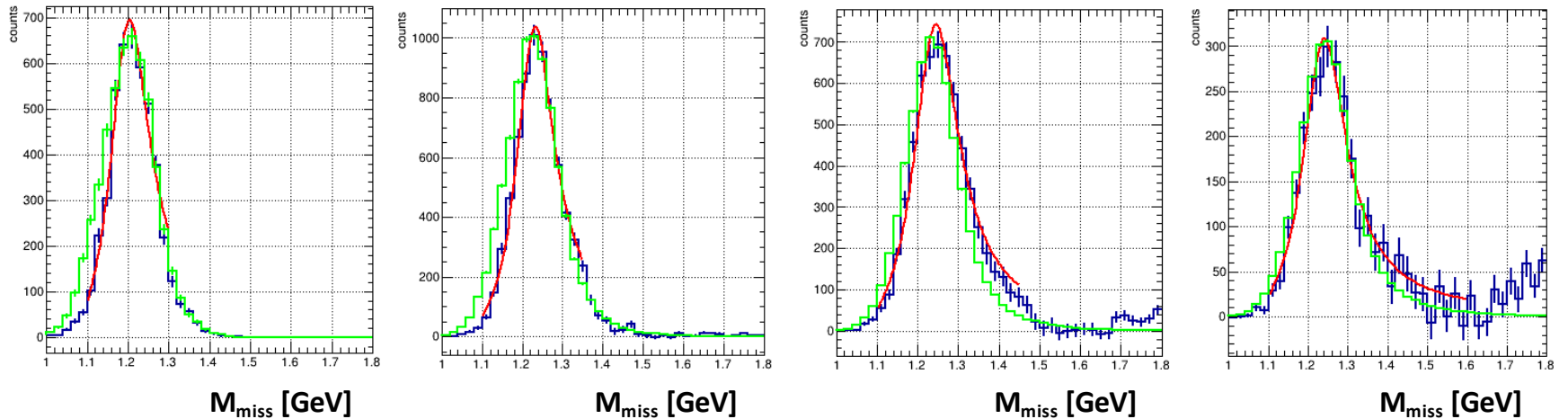
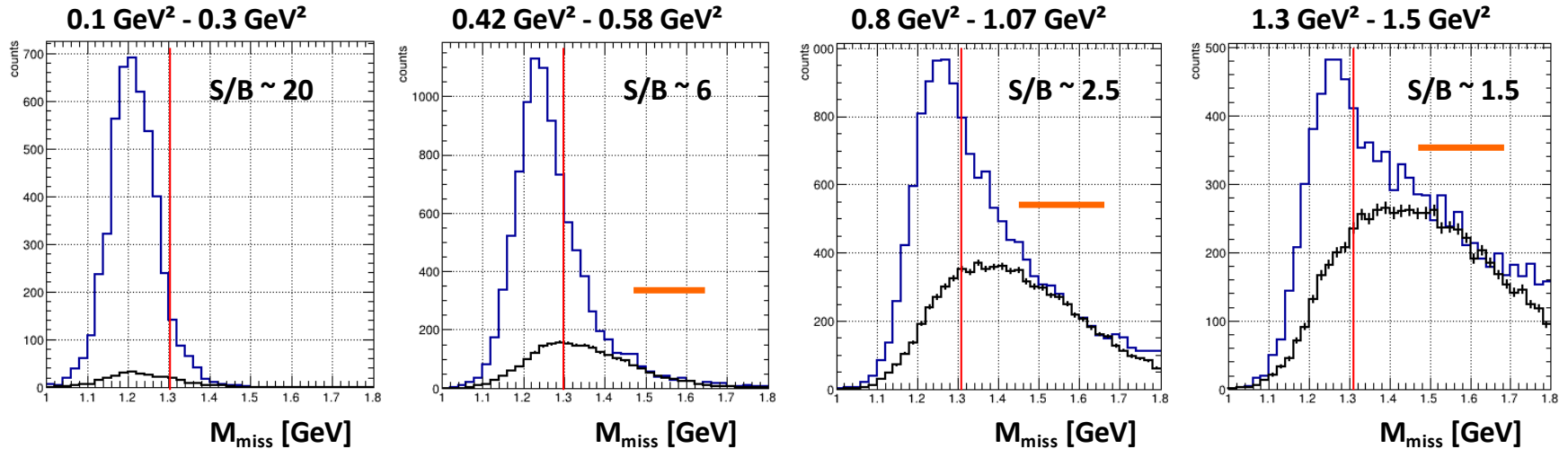
➔ Both MCs are processed through the full simulation and reconstruction chain



# Event Selection and Background Estimate



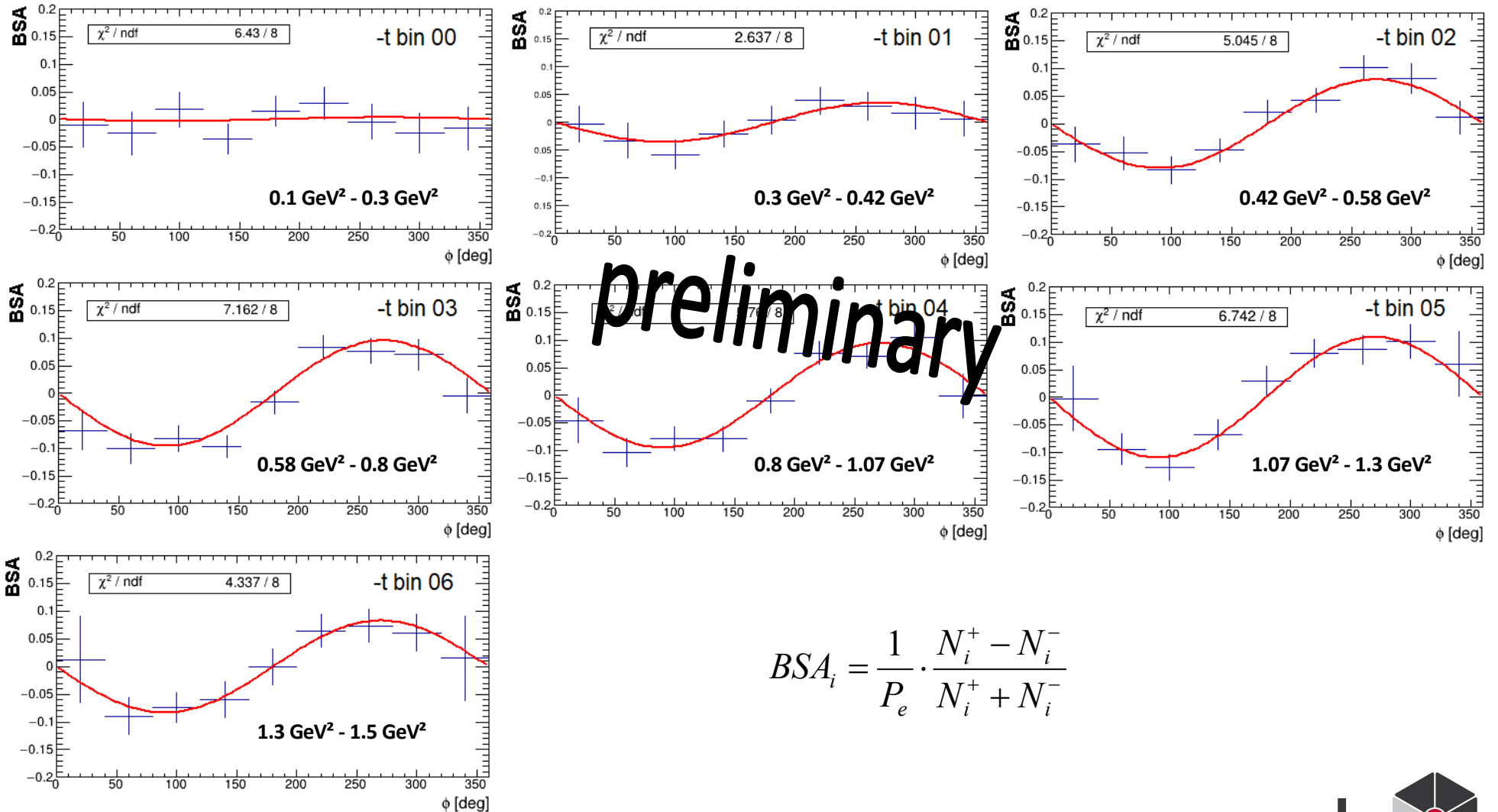
# Event Selection and Background Estimate



— experimental data  
 — SIDIS MC (same cuts)

— data after SIDIS MC subtraction  
 — fit of a Sill function (BW with thr. effects)  
 — exclusive MC (for comparison)

# Resulting Beam Spin Asymmtries ( $Q^2$ - $x_B$ integrated)

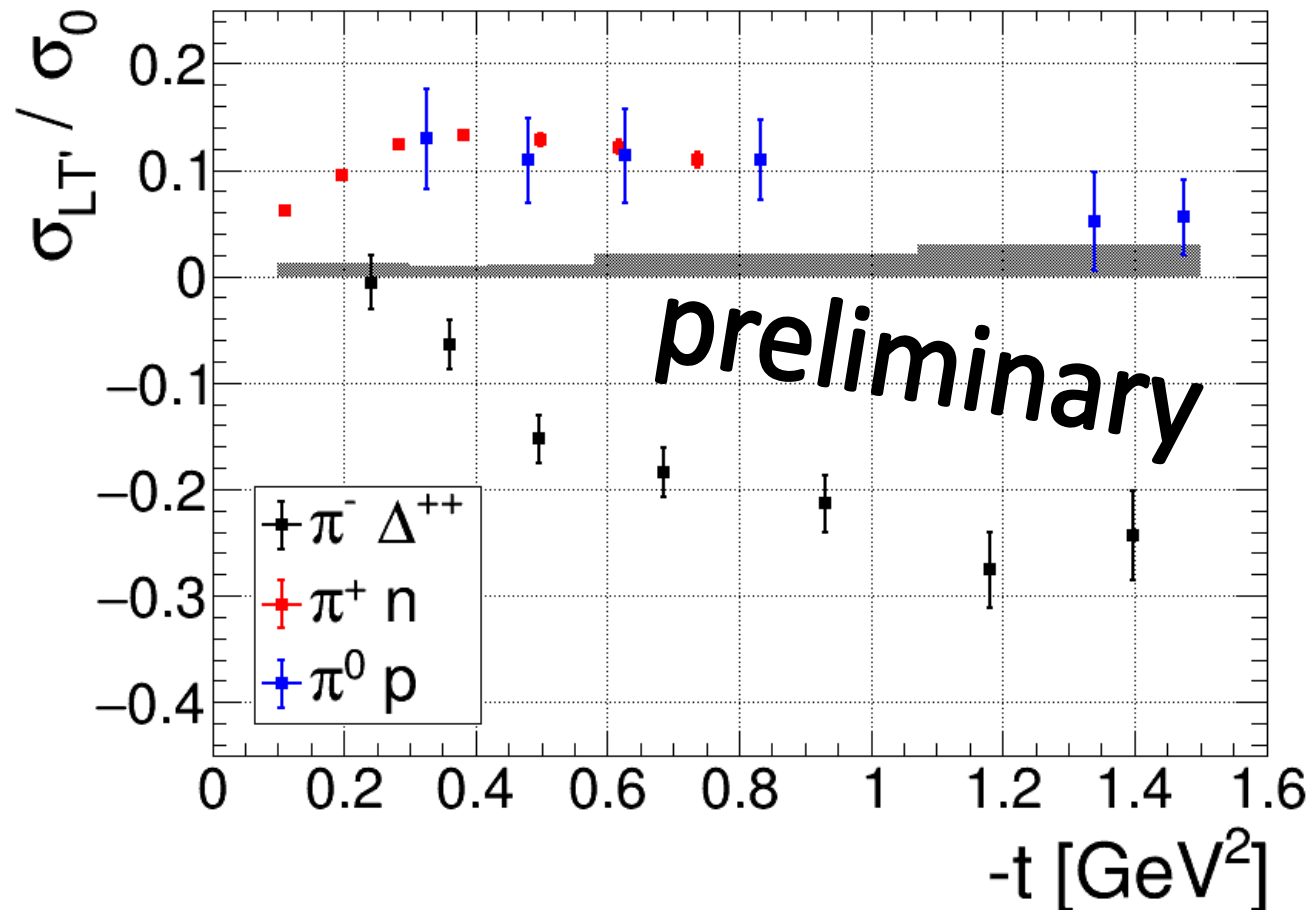


$$BSA_i = \frac{1}{P_e} \cdot \frac{N_i^+ - N_i^-}{N_i^+ + N_i^-}$$



## $Q^2 - x_B$ Integrated Result

$\langle Q^2 \rangle = 2.48 \text{ GeV}^2$ ,  $\langle x_B \rangle = 0.27$

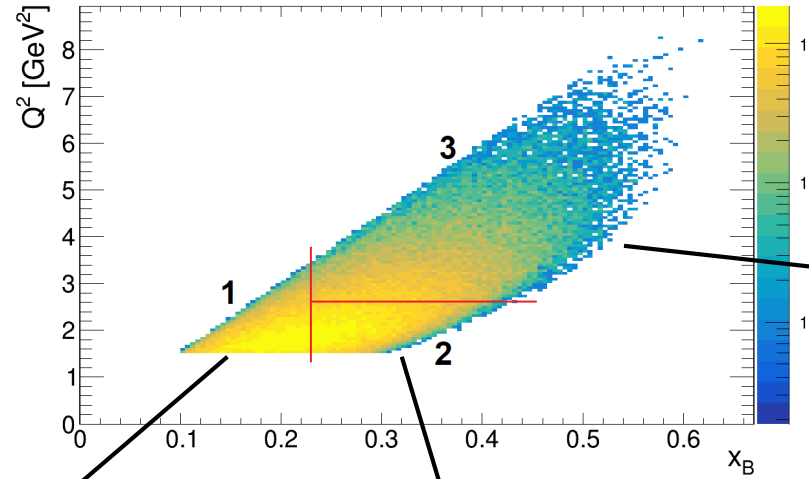


Different sources of systematic uncertainty have been studied:  
beam polarisation, background subtraction, fiducial volume, extraction method,  
acceptance, bin migration, radiative effects

# Multidimensional Results



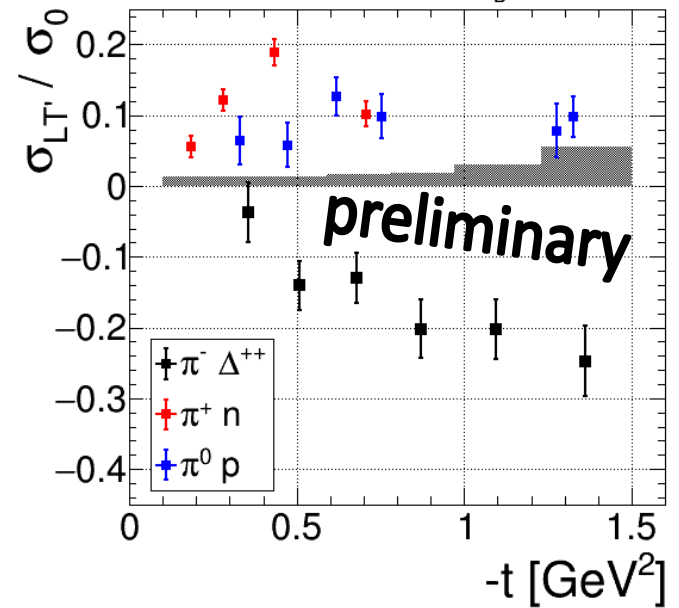
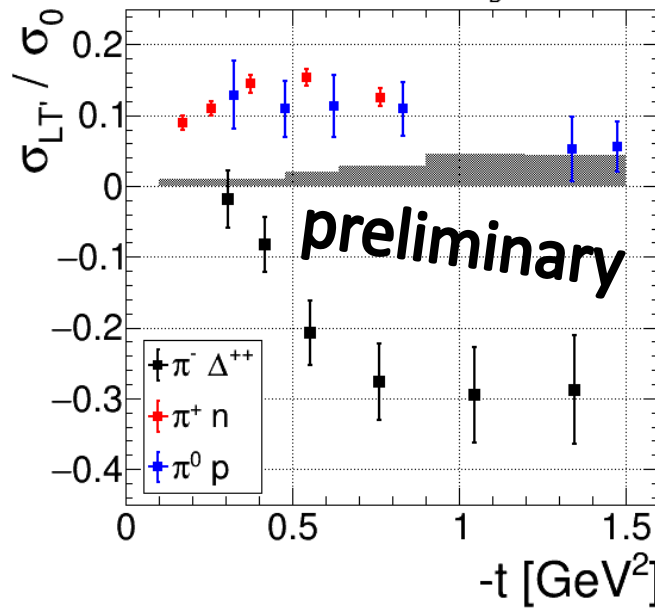
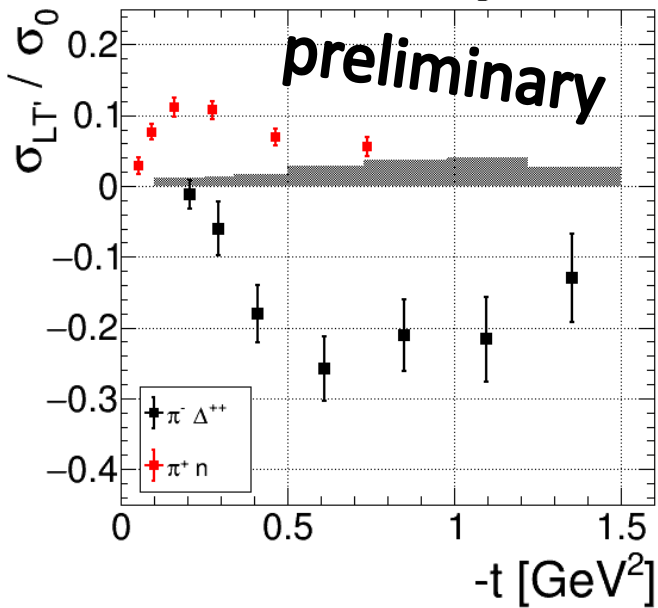
preliminary



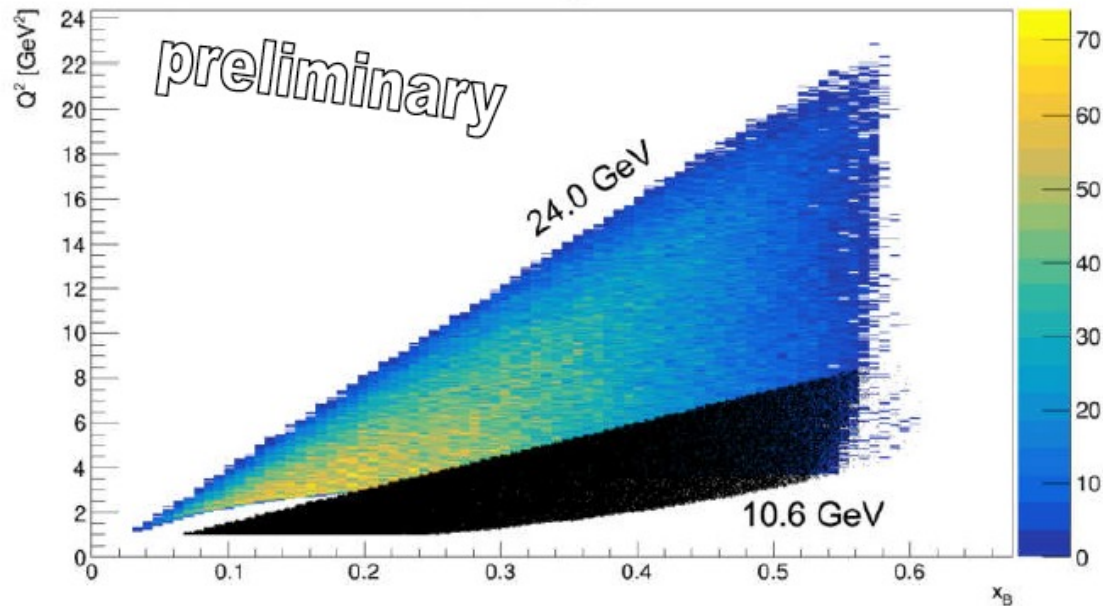
bin 1 ( $Q^2 = 1.95$  GeV<sup>2</sup>,  $x_B = 0.19$ )

bin 2 ( $Q^2 = 2.11$  GeV<sup>2</sup>,  $x_B = 0.28$ )

bin 3 ( $Q^2 = 3.38$  GeV<sup>2</sup>,  $x_B = 0.34$ )



# Perspectives for a 20+ GeV JLAB upgrade



$$ep \rightarrow e\Delta^{++}\pi^{-} \rightarrow ep\pi^{+}\pi^{-}$$

**Extended  $Q^2$  range**

**→ Advantage for factorisation**

- Similar for non-diagonal DVCS

## Conclusion and Outlook

- CLAS12 has a comprehensive program in measuring hard exclusive pseudoscalar and vector meson productions to access GPDs.
- Hard exclusive  $\pi^- \Delta^{++}$  production can be well measured with CLAS12 to study transition GPDs.
- The obtained BSA from  $\pi^- \Delta^{++}$  production is clearly negative and  $\sim 2$  times larger than for the hard exclusive  $\pi^+ / \pi^0$  production.
- The extracted BSA is a potential first "clean" observable sensitive to p- $\Delta$  transition GPDs
- More comprehensive theoretical framework for the exclusive meson productions would be needed.