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Selected topics in exclusive meson production

International Workshop on Hadron Structure
and Spectroscopy
CERN, August 29th 31st 2022

Outline

- Brief Overview

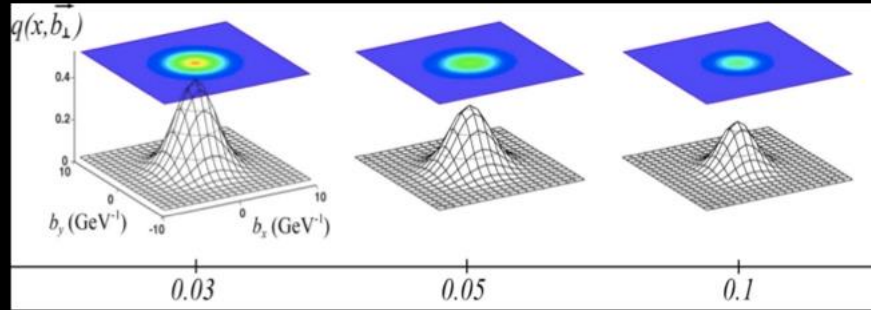
- Selected topics:
 - Pseudoscalar meson production
 - toward higher CoM energies: charmed mesons
 - Scale dependence
- What I will not cover:
 - Specifics of vector mesons
 - Nuclear targets



a framework with benchmarks for ML and DNN analyses of deeply virtual exclusive scattering cross sections

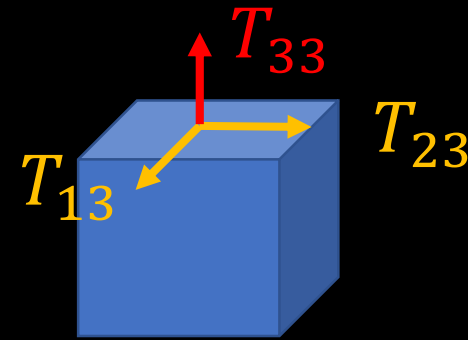
M.Almaeen, J.Grigsby, J.Hoskins, B.Kriesten, Y. Li, H. W. Lin and SL, arXiv:2207.10766

- Quark and Gluon Imaging

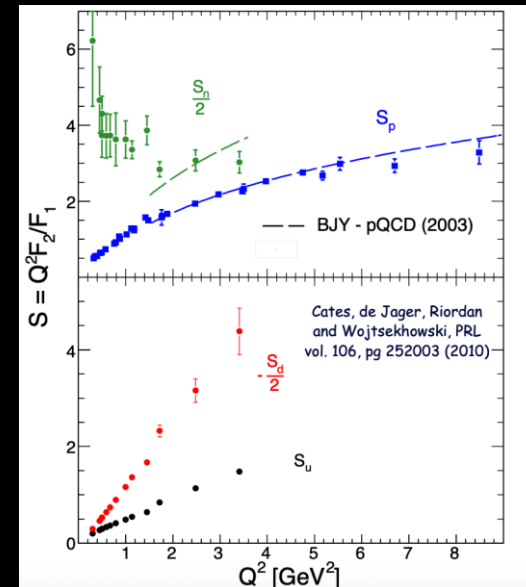


M. Defurne

- What generates the proton spin, mass and its internal forces (dynamics)

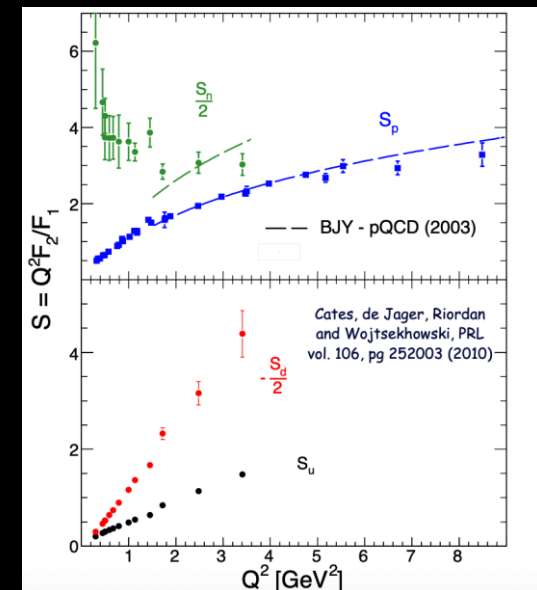
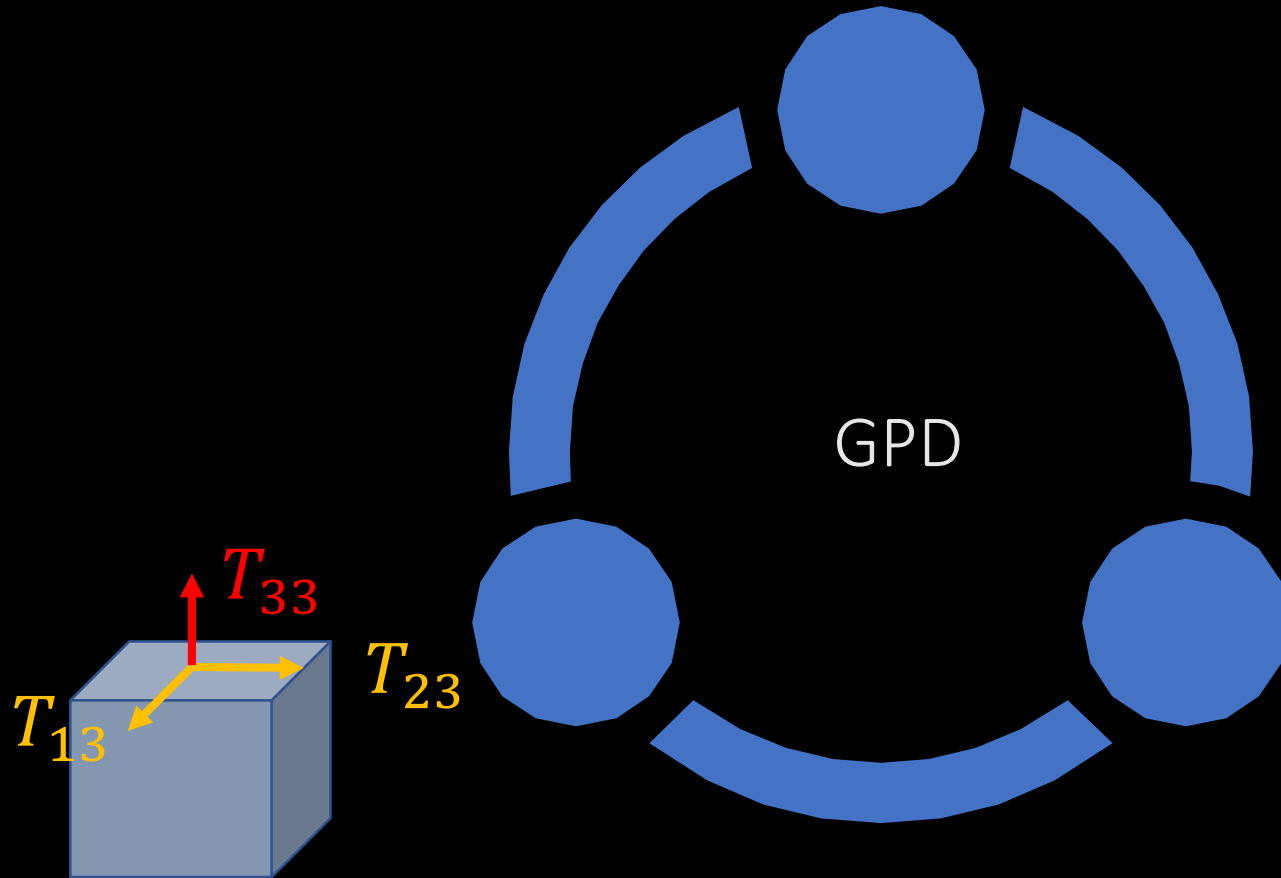
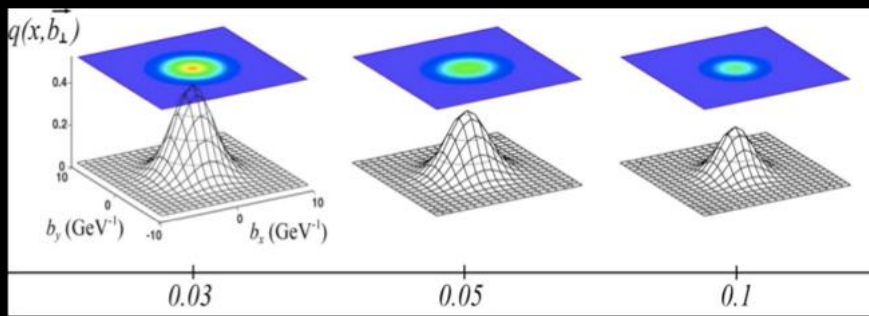


- Mechanisms of flavor dependence in nucleons and nuclei and BSM explorations

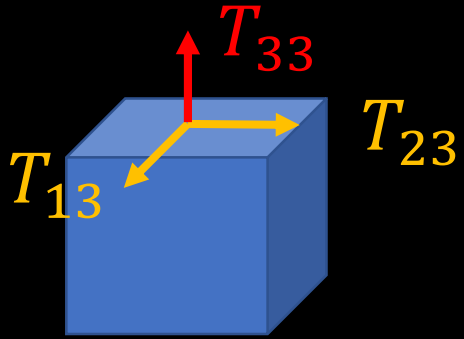


G. Cates et al. (2010)

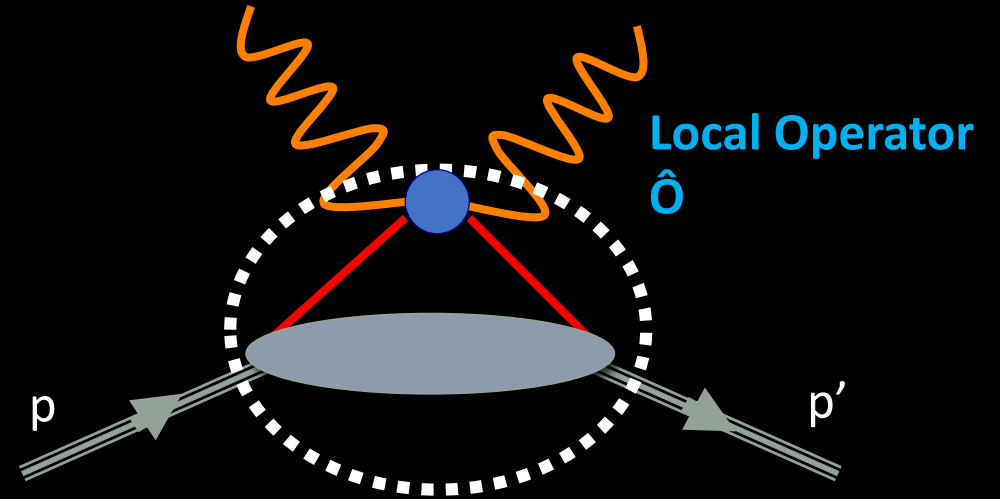
Common thread



Proton spin: quark longitudinal angular momentum, J_Z^q



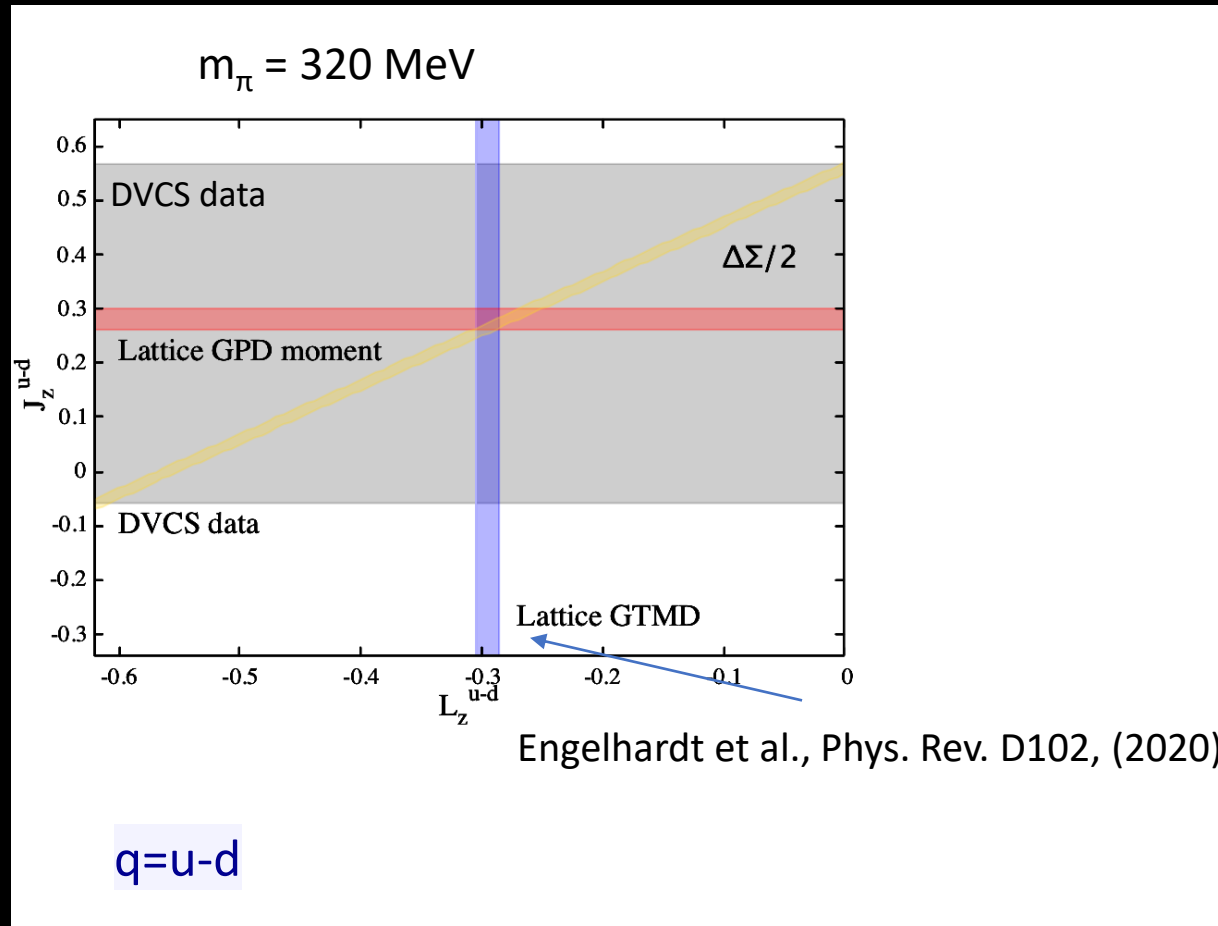
$$J_Z^q = \int_0^1 dx x (H_q + E_q)$$



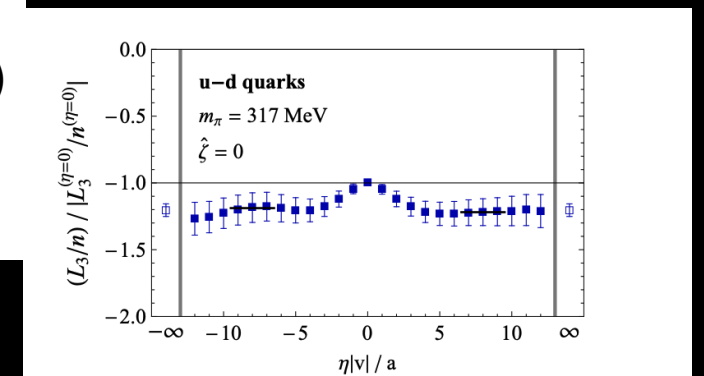
GPD Moments \rightarrow EMT Form Factors

X. Ji (1997)

What we know from measurements and lattice



$$J_q = L_q + \frac{1}{2} \Delta \Sigma_q$$



- Do we need to measure a GTMD to learn about OAM?

Connecting the two pictures using **QCD Equations of Motion** and **Lorentz symmetry**

$$\begin{aligned} J_L &= L_L + S_L \\ \frac{1}{2} \int dx x(H + E) &= \int dx x(\tilde{E}_{2T} + H + E) + \frac{1}{2} \int dx \tilde{H} \\ &= - \int dx F_{14}^{(1)} + \frac{1}{2} \int dx \tilde{H} \end{aligned}$$

- A. Rajan, A. Courtoy, M. Engelhardt, S.L., PRD (2016)
- A. Rajan, M. Engelhardt, S.L., PRD (2018)

*Twist 3 GPD notation from Meissner, Metz and Schlegel, JHEP(2009)

Quark Spin Orbit: $L \cdot S$

$$\frac{1}{2} \int dx x \tilde{H} + \frac{m_q}{2M} \kappa_T^q = \int dx x (2\tilde{H}'_{2T} + E'_{2T} + \tilde{H}) + \frac{1}{2} e_q$$

$J_z S_z$

$L_z S_z$

$S_z S_z$

- A. Rajan, A. Courtoy, M. Engelhardt, S.L., PRD (2016)
- A. Rajan, M. Engelhardt, S.L., PRD (2018)

*Twist 3 GPD notation from Meissner, Metz and Schlegel, JHEP(2009)

A closer look to $J_z S_z$

$$2(J_z S_z)_q \equiv 2[(J \cdot S)_q - (J_T \cdot S_T)_q] = \frac{1}{2} \int dx x \tilde{H} + \frac{m_q}{2M} \kappa_T^q$$

$$\kappa_T^q = \int dx (E_T + 2\tilde{H}_T) , \quad e_q = \int dx H$$

Quark transverse anomalous magnetic moment
(M. Burkardt, PRD72 (2005))

A closer look to $J_z S_z$

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Quark transverse anomalous magnetic moment
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Transverse Angular Momentum Sum Rule

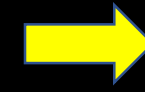
O. Alkassasbeh, M. Engelhardt, SL and A. Rajan, (2022) soon on arXiv

$$\frac{1}{2} \int dx x (H + E) - \frac{1}{2} \int dx \mathcal{M}_T = \int dx x (\tilde{E}_{2T} + H + E + \frac{H_{2T}}{\xi}) + \frac{1}{2} \int dx g_T - \frac{1}{2} \int dx x \mathcal{A}_T$$

J_T L_T S_T

Twist 3 GPDs Physical Interpretation

GPD	$P_q P_p$	TMD	Ref. 1
H^\perp	UU	f^\perp	$2\tilde{H}_{2T} + E_{2T}$
\tilde{H}_L^\perp	LL	g_L^\perp	$2\tilde{H}'_{2T} + E'_{2T}$
H_L^\perp	UL	$f_L^\perp^{(*)}$	$\tilde{E}_{2T} - \xi E_{2T}$
\tilde{H}^\perp	LU	$g^\perp^{(*)}$	$\tilde{E}'_{2T} - \xi E'_{2T}$
$H_T^{(3)}$	UT	$f_T^{(*)}$	$H_{2T} + \tau \tilde{H}_{2T}$
$\tilde{H}_T^{(3)}$	LT	g'_T	$H'_{2T} + \tau \tilde{H}'_{2T}$



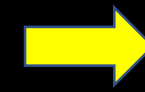
1/Q correction to H



1/Q correction to \tilde{H} $\mathbf{L} \cdot \mathbf{S}$

NEW!! OAM \mathbf{L}_z

NEW!!



1/Q correction to E: OAM, \mathbf{L}_T

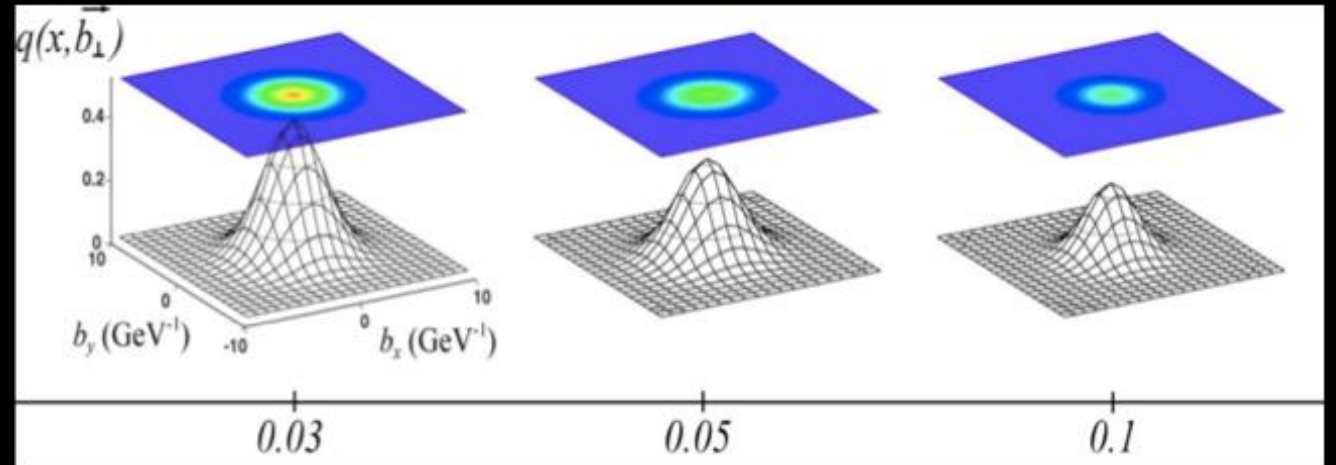


1/Q correction to \tilde{E}

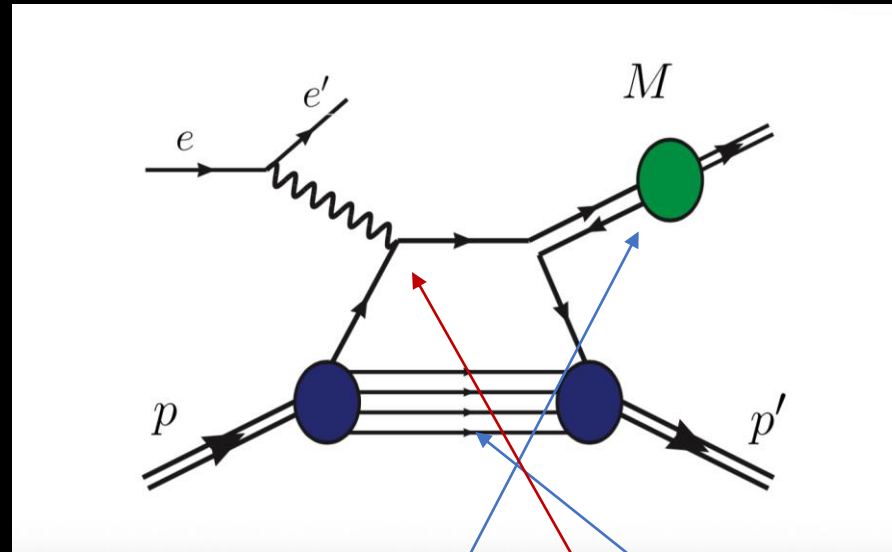
(*) T-odd

[1] Meissner, Metz and Schlegel, JHEP(2009)

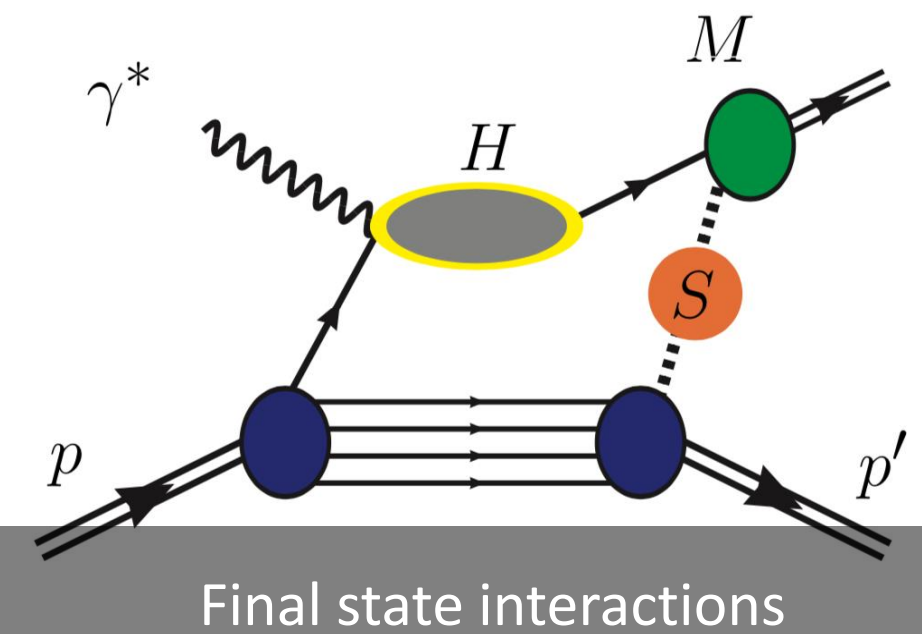
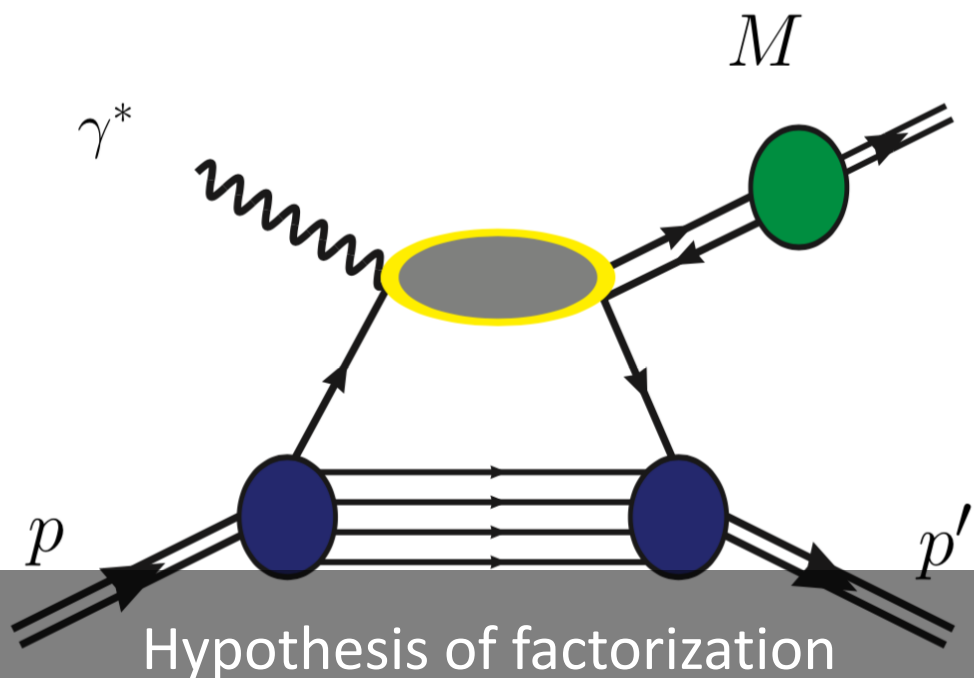
Measuring All This:
from Jlab@12 GeV,
Jlab@12+ GeV, COMPASS to
the EIC



Role of meson production



$$A = \int_0^1 dz \text{ (DA)} \int_{-1}^1 dx \text{ (PQCD)} \text{ (GPD)}$$



Factorization Theorem for meson production

Collins, Frankfurt & Strikman (PRD, 1997)

1) When the virtual photon is longitudinally polarized the end-point contributions in the meson wave function are power suppressed.

(Due to helicity conservation polarization transfers directly from the photon to the produced vector meson)

3) γ_L^* singles out small size configurations compared to γ_T^* .

4) “Non small size” configurations are less likely to factorize and are power suppressed.

This is the underlying physics idea that has all to be proven!

In this working hypothesis ...

$$\rho_L^0 \rightarrow \int_{-1}^1 dx \left[\frac{1}{x - \xi + i\epsilon} + \frac{1}{x + \xi - i\epsilon} \right] (e_u H_u - e_d H_d)$$

$$\rho_L^+ \rightarrow \int_{-1}^1 dx \left[\frac{e_u}{x - \xi + i\epsilon} + \frac{e_d}{x + \xi + i\epsilon} \right] (H_u - H_d)$$

$$\omega_L \rightarrow \int_{-1}^1 dx \left[\frac{1}{x - \xi + i\epsilon} + \frac{1}{x + \xi + i\epsilon} \right] (e_u H_u + e_d H_d)$$

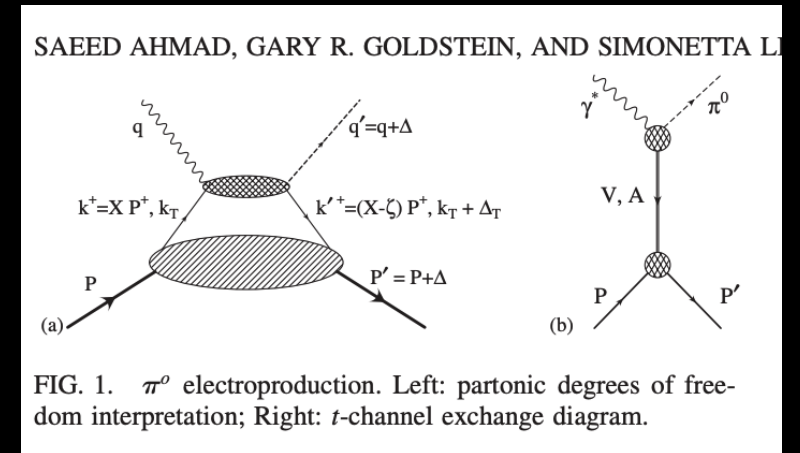
$$\pi^0 \rightarrow \int_{-1}^1 dx \left[\frac{1}{x - \xi + i\epsilon} + \frac{1}{x + \xi - i\epsilon} \right] (e_u \tilde{H}_u - e_d \tilde{H}_d)$$

$$\pi^+ \rightarrow \int_{-1}^1 dx \left[\frac{e_u}{x - \xi + i\epsilon} + \frac{e_d}{x + \xi + i\epsilon} \right] (\tilde{H}_u - \tilde{H}_d)$$

$$\eta \rightarrow \frac{1}{\sqrt{6}} \int_{-1}^1 dx \left[\frac{1}{x - \xi + i\epsilon} + \frac{1}{x + \xi + i\epsilon} \right] (e_u \tilde{H}_u + e_d \tilde{H}_d - 2e_s \tilde{H}_s)$$

Beyond longitudinally polarized photon

- G. R. Goldstein, J. O. Gonzalez Hernandez and S. Liuti, [arXiv:1401.0438 [hep-ph]].
- Courtoy, S. Baessler, M. Gonzalez-Alonso and S. Liuti, Phys. Rev. Lett. 115 , 162001 (2015)
- G.R. Goldstein, J. O. Gonzalez Hernandez and S. Liuti, Phys. Rev. D 91114013 (2015)
- G. R. Goldstein, J. O. Gonzalez Hernandez and S. Liuti, J. Phys. G 39, 115001 (2012)
- S. Liuti and G. R. Goldstein, [arXiv:1009.1334 [hep-ph]].
- S. Ahmad, G. R. Goldstein and S. Liuti, Phys. Rev. D 79, 054014 (2009)



Focus on pseudoscalar mesons

Pseudoscalar meson production gives access to:

- the tensor charge, g_T
- the tensor anomalous magnetic moment, κ_T

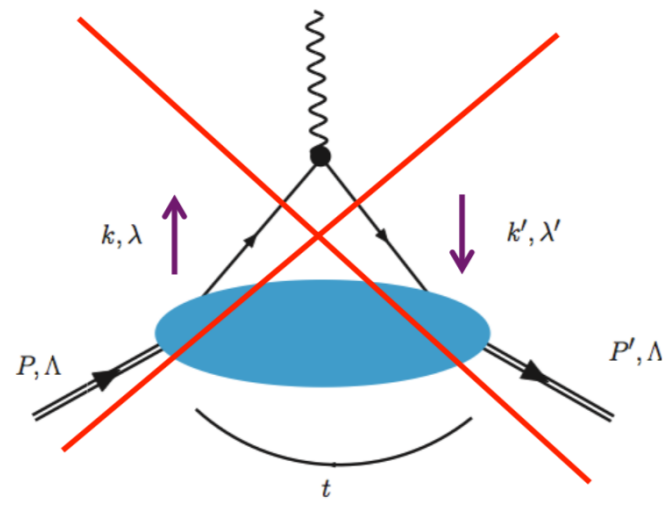
Opportunity for BSM studies

The most general form of gauge interactions with the exchange of a spin-1 particle is a linear combination of

VECTOR $\bar{\psi} \gamma_{\mu} \psi$ and **AXIAL-VECTOR** $\bar{\psi} \gamma_{\mu} \gamma_5 \psi$

Courtoy, Baessler,
Gonzalez Alonso, Liuti
(PRL, 2015)

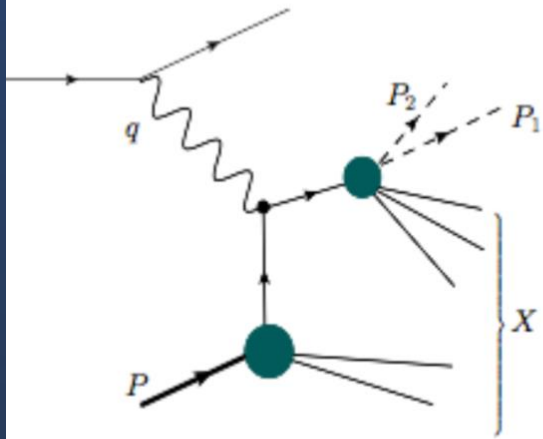
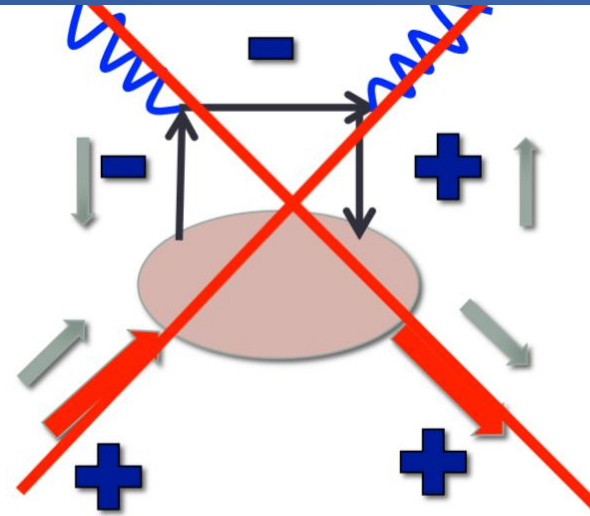
- ✓ The tensor charge is not “fundamental”
- ✓ A “tensor form factor” cannot be measured in elastic scattering type processes mediated by either one or two photons



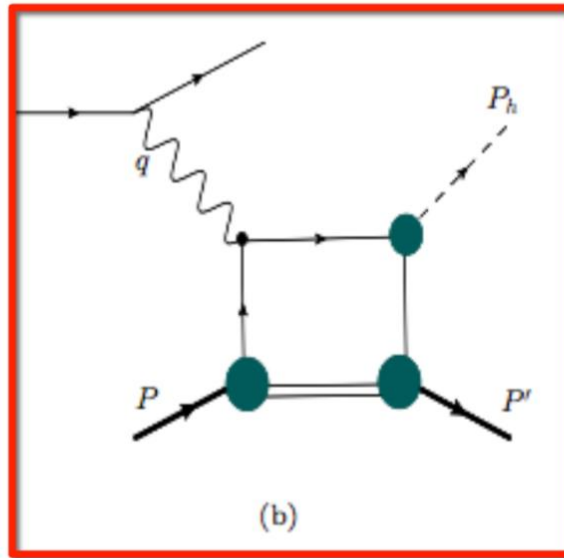
$$\langle p', \Lambda' | \underbrace{\pm i \bar{\psi}(0) (\sigma^{+1} \pm i \sigma^{+2}) \psi(0)} | p, \Lambda \rangle$$

The operator is chiral-odd: only connects quarks with opposite helicity

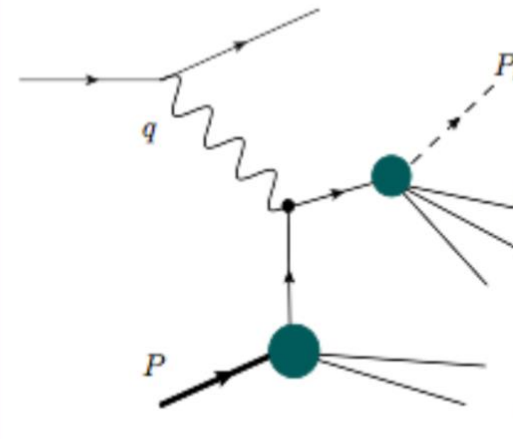
To detect chiral odd distributions we need another distinct hadronic blob



(a)
dihadron



(b)
DV π^0 P, DV η P

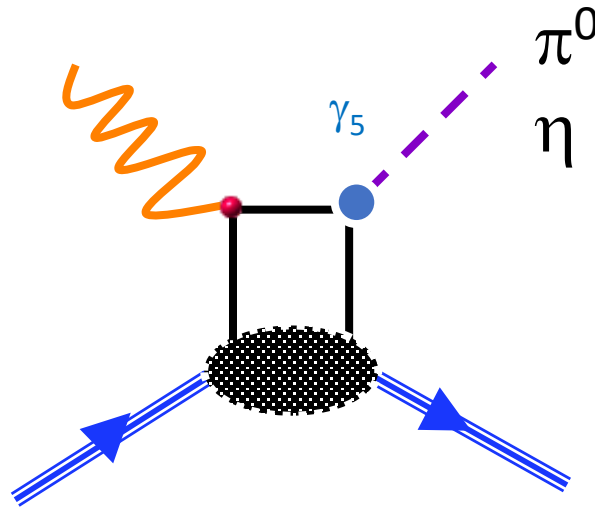
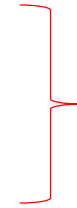


(c)
SIDIS

collinear

$$J^{PC} = 1^{--} \quad \gamma, \rho, \omega, \dots$$

$$J^{PC} = 1^{+-} \quad \mathbf{b}_1, \mathbf{h}_1$$


 D^0
 η_c


New! Charmed mesons

chiral-odd structure

$$\begin{aligned} \gamma_5 (\not{k} + \not{q}) \gamma^\mu &= (k_\nu + q_\nu) \frac{\gamma_5}{2} ([\gamma^\nu, \gamma^\mu] + \{\gamma^\nu, \gamma^\mu\}) = (k_\nu + q_\nu) \gamma_5 (i\sigma^{\mu\nu} + g^{\mu\nu}) \\ &\propto i\gamma_5 \sigma^{\mu\nu} \end{aligned}$$

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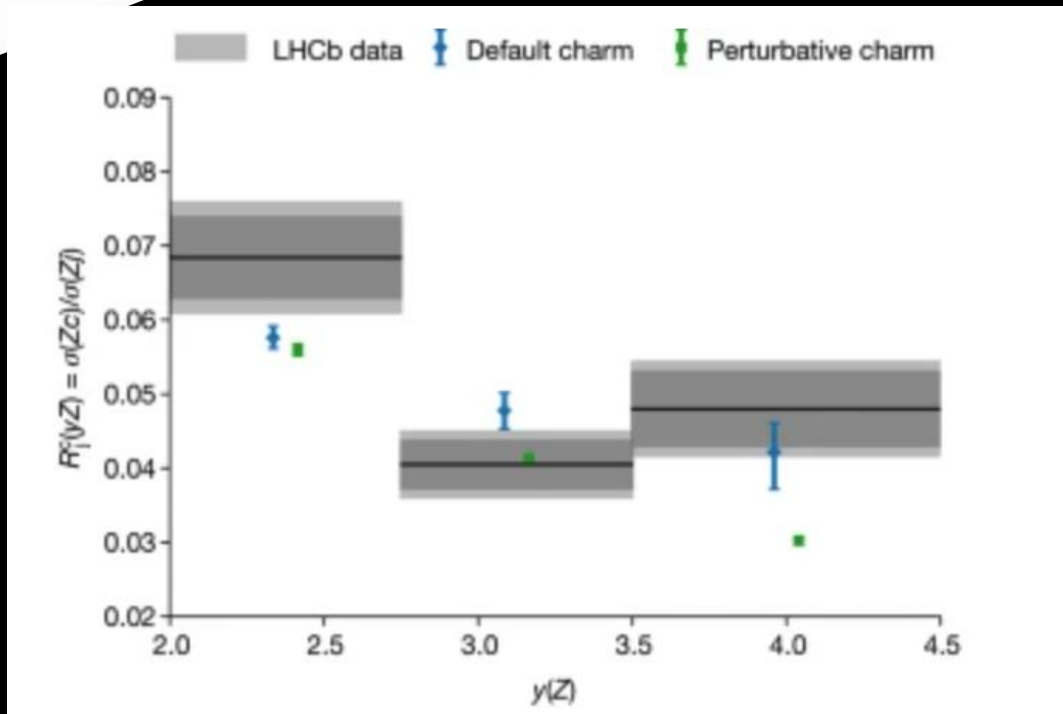
Evidence for intrinsic charm quarks in the proton

[The NNPDF Collaboration](#)

[Nature](#) **608**, 483–487 (2022) | [Cite this article](#)

21k Accesses | 321 Altmetric | [Metrics](#)

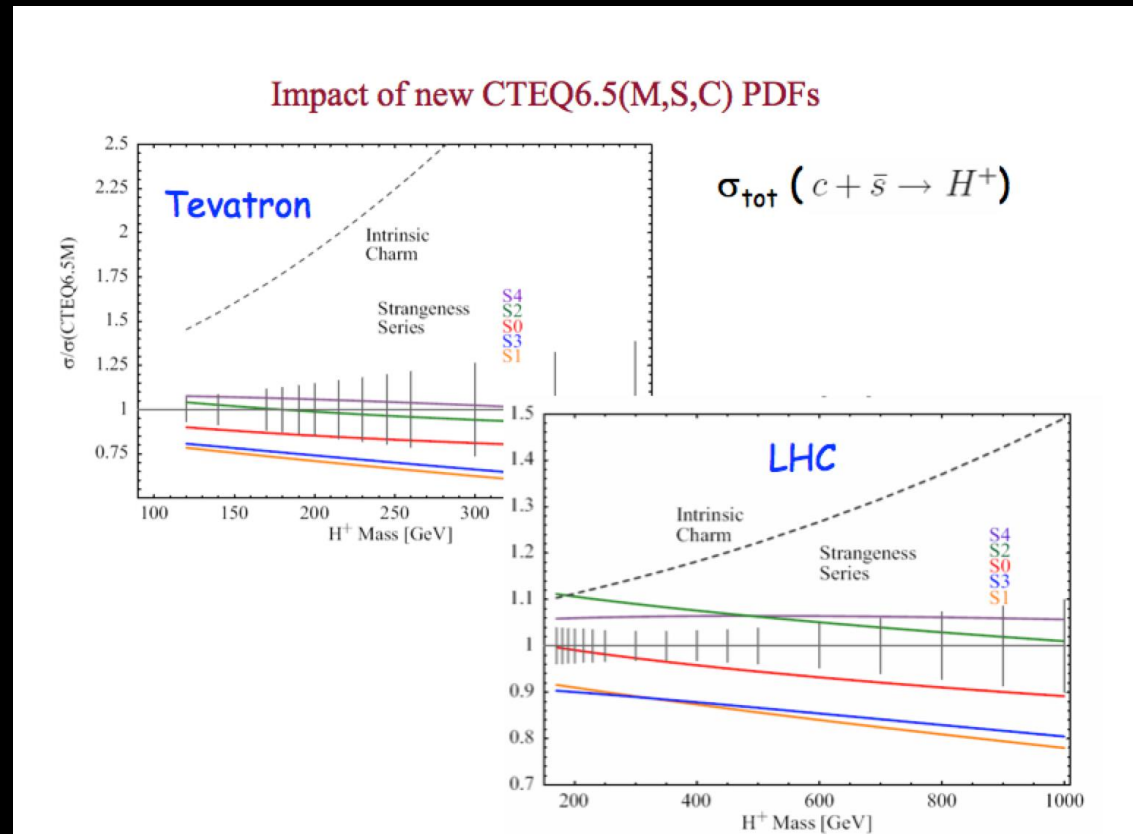
LHCb measurement of Z-boson production in association with charm-tagged jets



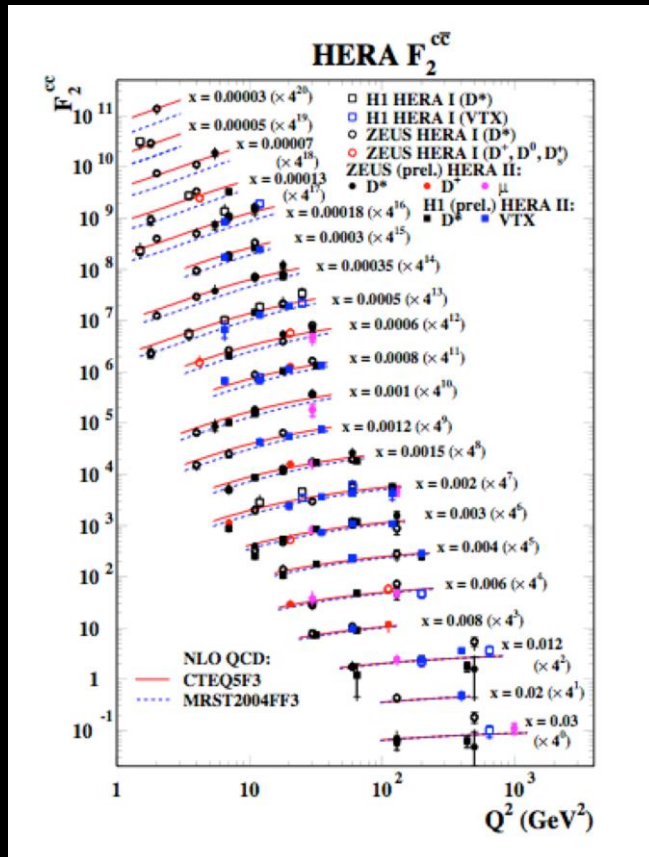
Heavy quark pseudoscalar meson exclusive electroproduction to access intrinsic charm

LHC processes are sensitive to charm content of the proton

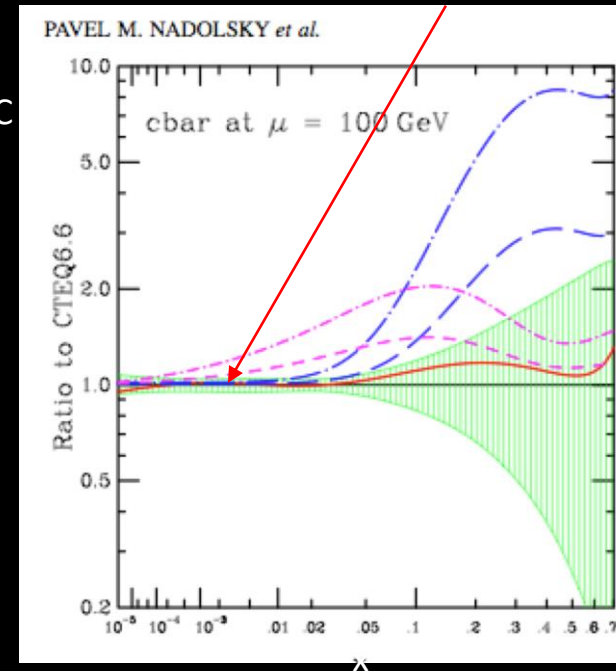
- ⇒ Higgs production: SM Higgs, charged Higgs,
- ⇒ Precision physics (CKM matrix elements, V_{tb} ...): single top production, ...



Most data are at very low x where they cannot discriminate whether IC is there



IC/no-IC



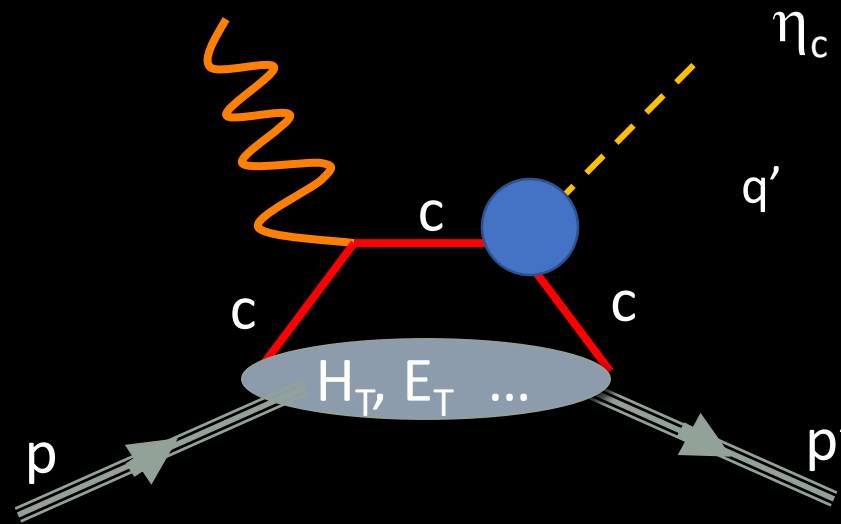
(see also P. Di Nezza's talk)

In exclusive electroproduction η_c , D^0 , and \bar{D}^0 is governed by chiral-odd soft matrix elements which cannot evolve from gluons

η_c , D^0 , and \bar{D}^0 can be used as triggers of “intrinsic charm content”

Gold plated signal: η_c exclusive production

$$\gamma^* p \rightarrow \eta_c p$$

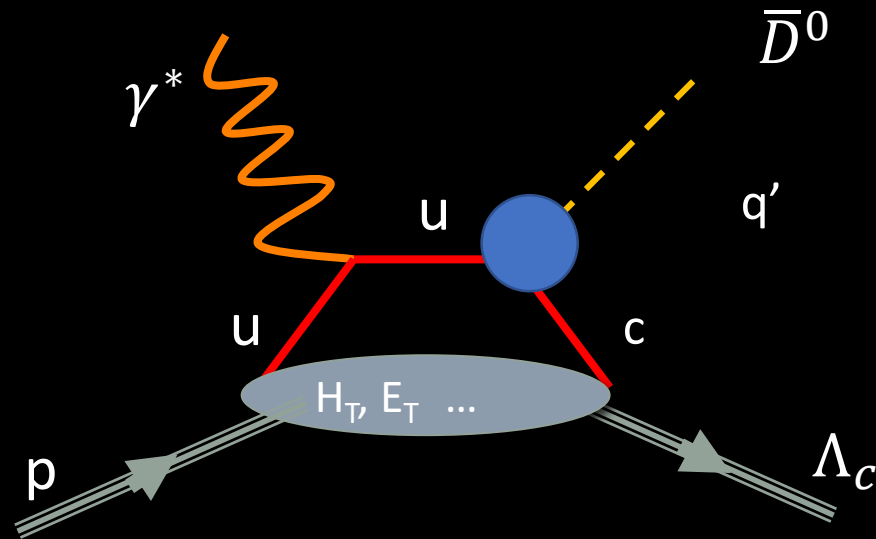


flavor content of string

$$p \rightarrow c + (c\text{-bar } uud) + c \rightarrow p$$

Other interesting channel

$$\gamma^* p \rightarrow \bar{D}^0 \Lambda_c$$



flavor content of string

$$p \rightarrow u + (ud) + c \rightarrow \Lambda_c$$

Cross Section

G.R. Goldstein, J. O. Gonzalez Hernandez and SL, Phys. Rev. D 91114013 (2015)

$$\begin{aligned}
 \frac{d^4\sigma}{dx_{Bj}dyd\phi dt} = & \Gamma \left\{ \boxed{F_{UU,T} + \epsilon F_{UU,L} + \epsilon \cos 2\phi F_{UU}^{\cos 2\phi} + \sqrt{2\epsilon(\epsilon+1)} \cos \phi F_{UU}^{\cos \phi} + h \sqrt{2\epsilon(1-\epsilon)} \sin \phi F_{LU}^{\sin \phi}} \right. \\
 & + S_{||} \left[\sqrt{2\epsilon(\epsilon+1)} \sin \phi F_{UL}^{\sin \phi} + \epsilon \sin 2\phi F_{UL}^{\sin 2\phi} + h \left(\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos \phi F_{LL}^{\cos \phi} \right) \right] \\
 & + S_{\perp} \left[\sin(\phi - \phi_S) \left(F_{UT,T}^{\sin(\phi-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi-\phi_S)} \right) + \epsilon \left(\sin(\phi + \phi_S) F_{UT}^{\sin(\phi+\phi_S)} + \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi-\phi_S)} \right) \right. \\
 & + \left. \sqrt{2\epsilon(1+\epsilon)} \left(\sin \phi_S F_{UT}^{\sin \phi_S} + \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi-\phi_S)} \right) \right] \\
 & \left. + S_{\perp} h \left[\sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi-\phi_S)} + \sqrt{2\epsilon(1-\epsilon)} \left(\cos \phi_S F_{LT}^{\cos \phi_S} + \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \right) \right] \right\}
 \end{aligned}$$

Helicity amplitudes

$$F_{UU,T} = \mathcal{N} [|f_{10}^{++}|^2 + |f_{10}^{+-}|^2 + |f_{10}^{-+}|^2 + |f_{10}^{--}|^2]$$

$$F_{UU,L} = \mathcal{N} [|f_{00}^{++}|^2 + |f_{00}^{+-}|^2]$$

$$F_{UU}^{\cos 2\phi} = -\mathcal{N} 2\Re [(f_{10}^{++})^* (f_{10}^{--}) - (f_{10}^{+-})^* (f_{10}^{-+})]$$

$$F_{UU}^{\cos \phi} = -\mathcal{N} \Re [(f_{00}^{+-})^* (f_{10}^{+-} + f_{10}^{-+}) + (f_{00}^{++})^* (f_{10}^{++} - f_{10}^{--})]$$

$$F_{LU}^{\sin \phi} = \mathcal{N} \Im [(f_{00}^{+-})^* (f_{10}^{+-} + f_{10}^{-+}) + (f_{00}^{++})^* (f_{10}^{++} - f_{10}^{--})]$$

κ_T

$$f_{10}^{++} \propto \Delta \left(2\tilde{\mathcal{H}}_T + (1 - \xi)\mathcal{E}_T - (1 - \xi)\tilde{\mathcal{E}}_T \right)$$

 g_T

$$f_{10}^{+-} \propto \mathcal{H}_T + \frac{t_0 - t}{4M^2} \tilde{\mathcal{H}}_T + \frac{\xi^2}{1 - \xi^2} \mathcal{E}_T + \frac{\xi}{1 - \xi^2} \tilde{\mathcal{E}}_T$$

$$f_{10}^{-+} \propto \Delta^2 \tilde{\mathcal{H}}_T$$

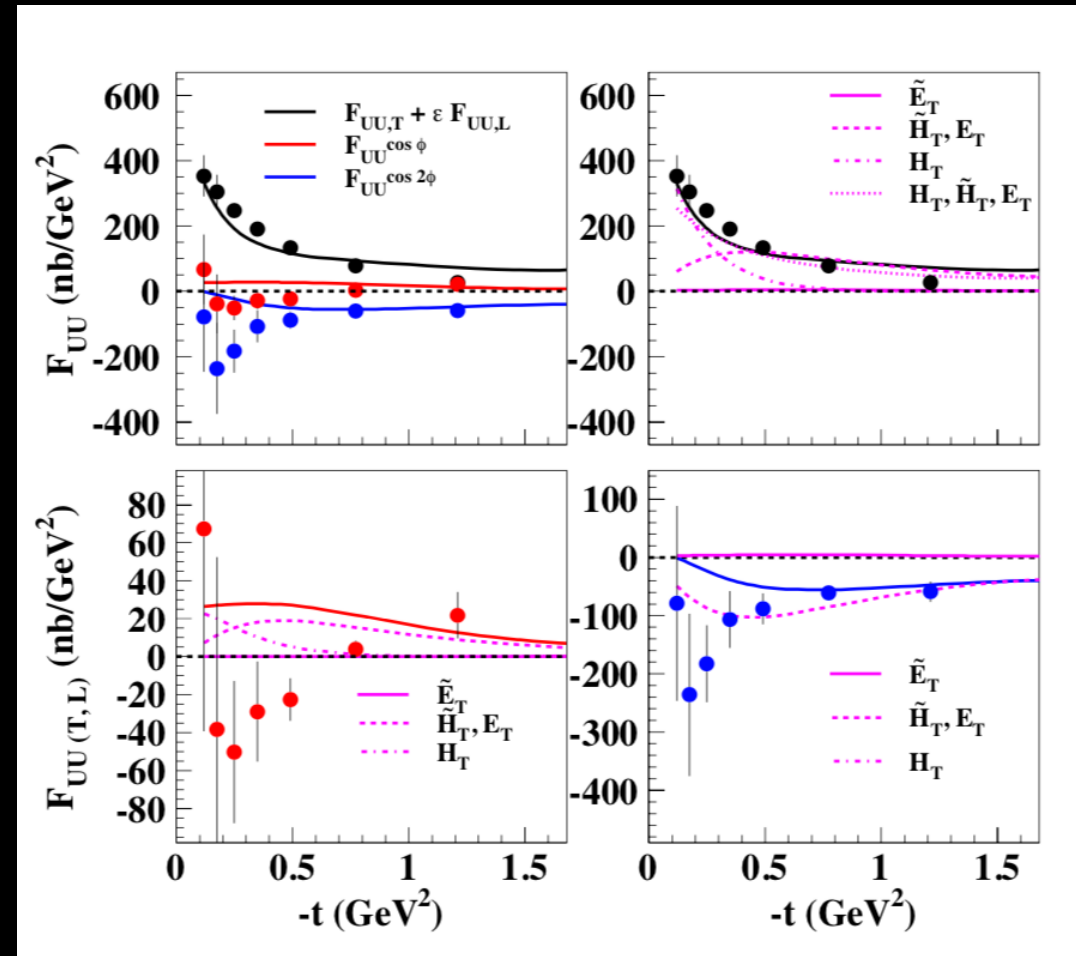
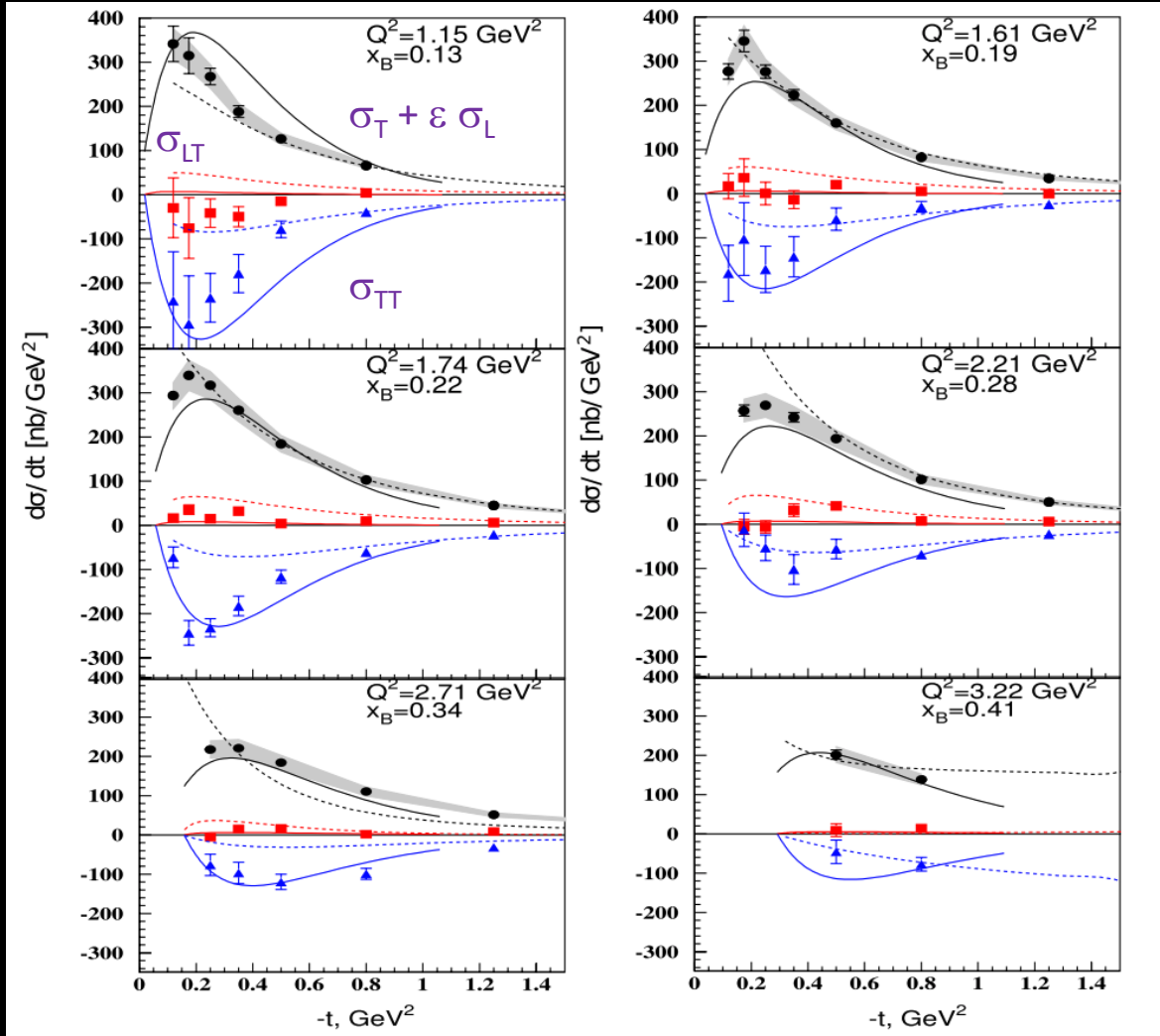
 κ_T

$$f_{10}^{--} \propto \Delta \left(2\tilde{\mathcal{H}}_T + (1 + \xi)\mathcal{E}_T + (1 + \xi)\tilde{\mathcal{E}}_T \right),$$

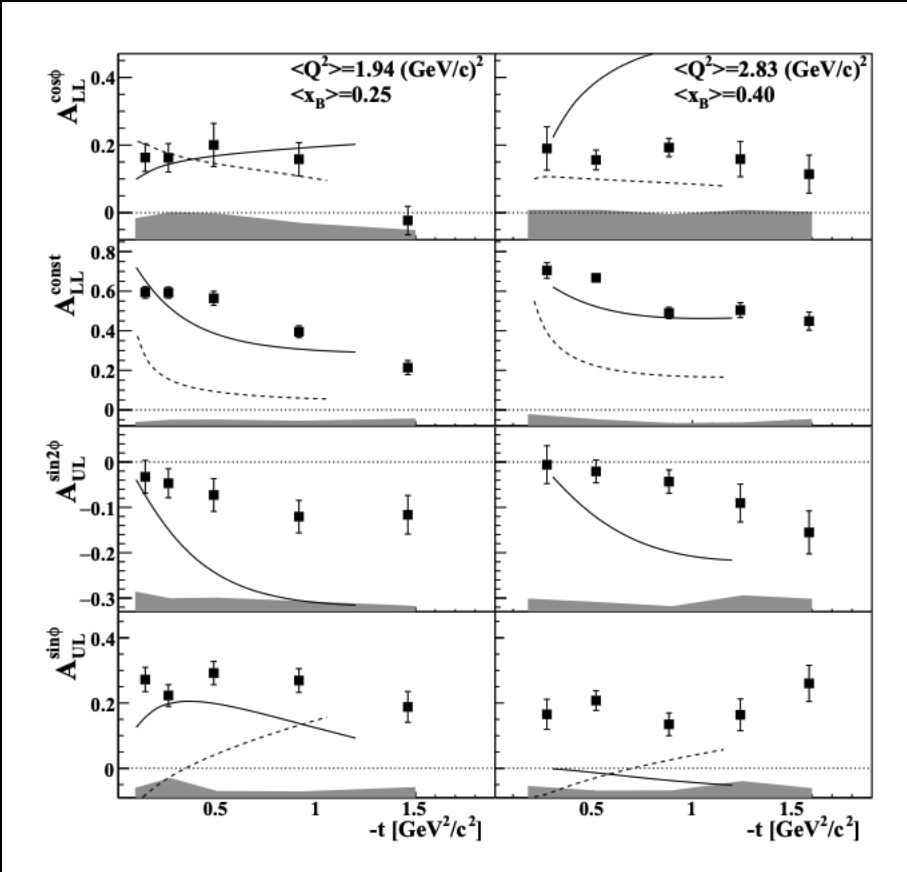
Unpolarized Cross Section initial data

G. Goldstein, O. Gonzalez-Hernandez, SL

Phys.Rev.D 91 (2015)

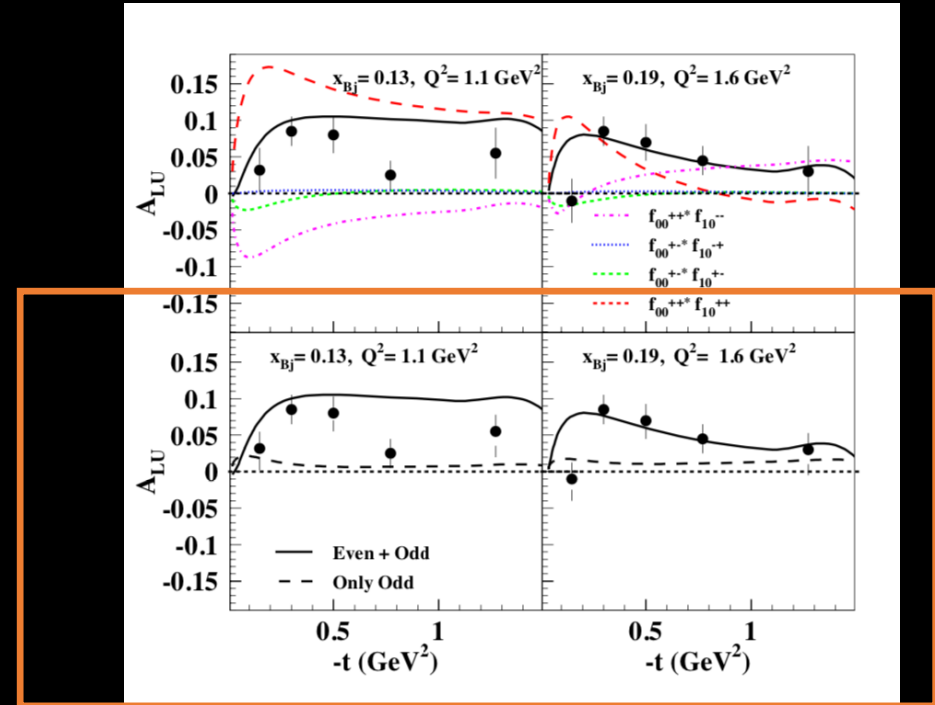


Asymmetries for Longitudinally polarized beam/target



A. Kim, A. Avakian et al, *Phys.Lett.B* 768 (2017)

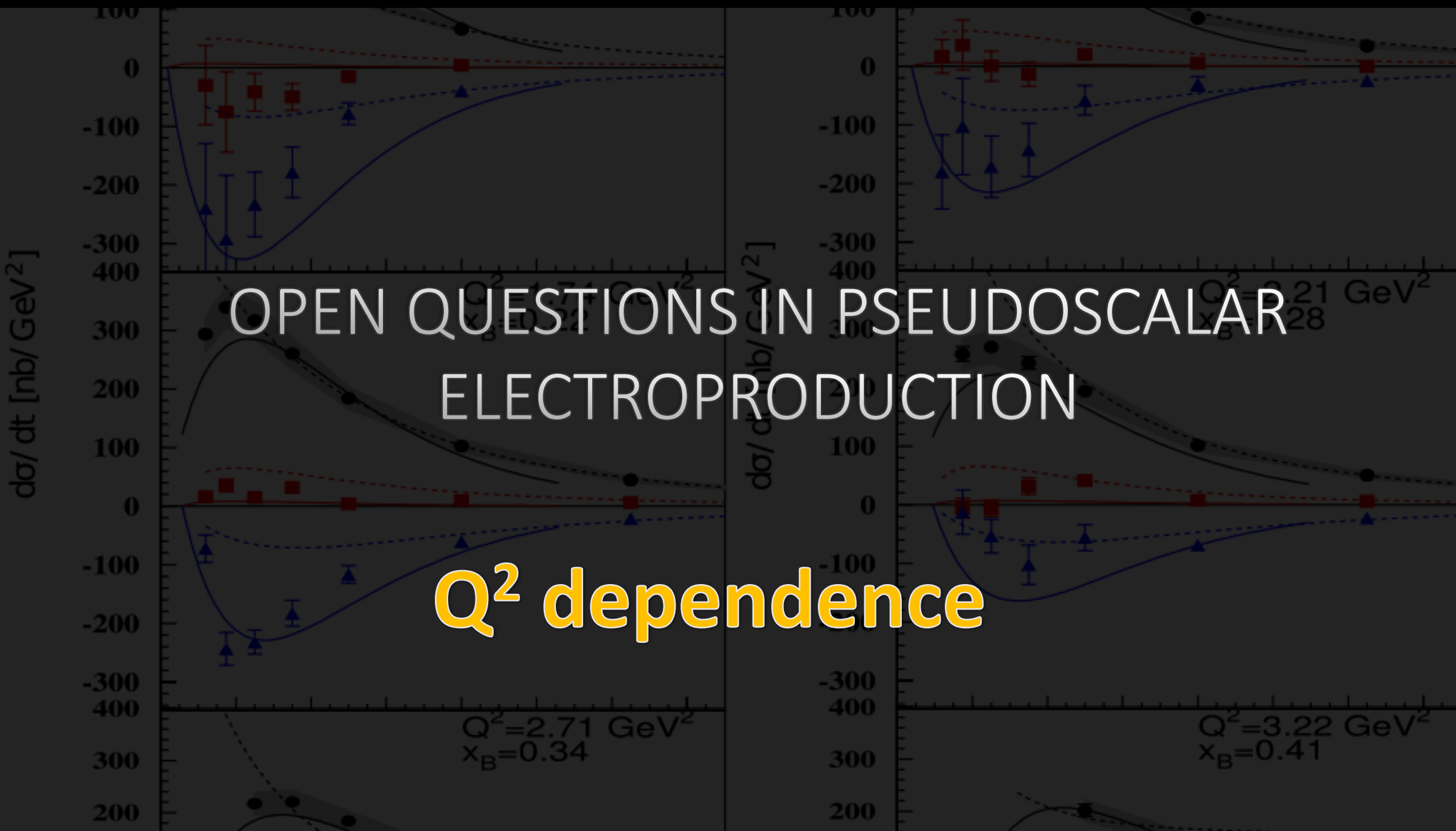
Compounded chiral odd and even effects



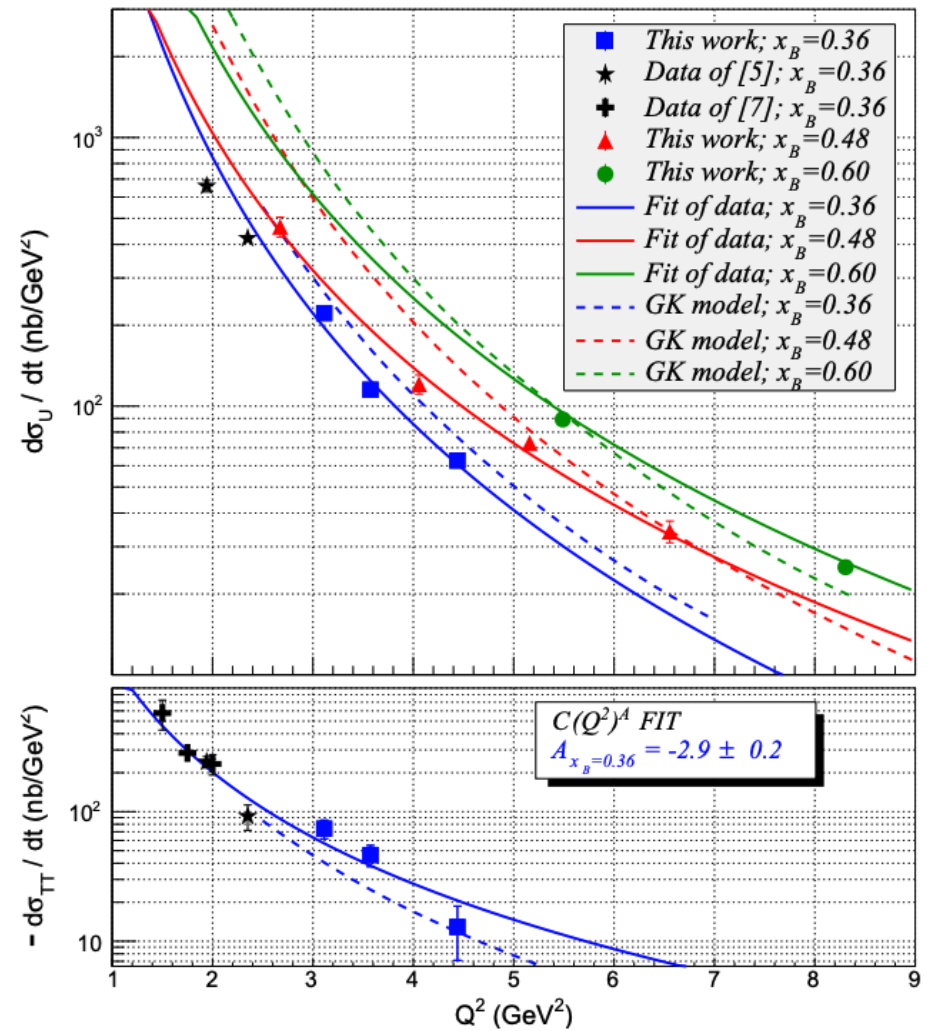
G.Goldstein, J. O. Gonzalez Hernandez and SL
 Phys. Rev. D 91114013 (2015)

OPEN QUESTIONS IN PSEUDOSCALAR ELECTROPRODUCTION

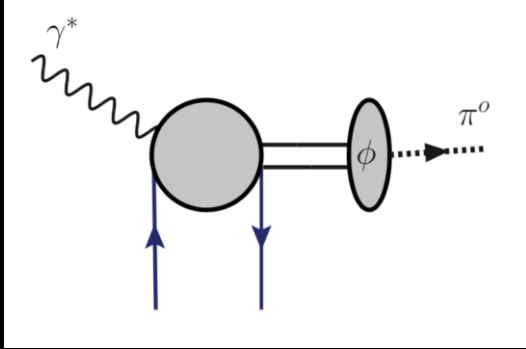
Q^2 dependence



- New data from Hall A seem to indicate that the “standard” Q^2 dependence picture does not fit the data



View DVMP vertex as pseudoscalar-meson transition form factor

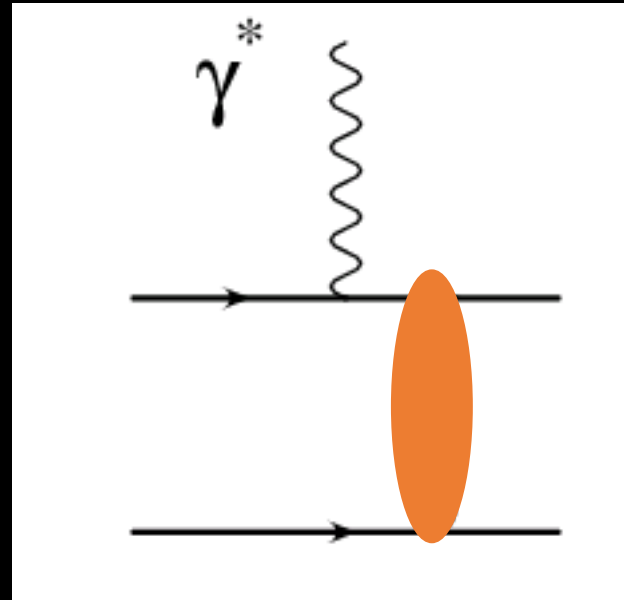


$$J^{PC} = 1^{--} ({}^3S_1)$$

ρ, ω

$$J^{PC} = 1^{+-} ({}^1P_1)$$

b_1, h_1



π^0

$$J^{PC} = 0^{+-}$$

Distinction between ω, ρ (vector) and b_1, h_1 (axial-vector) exchanges

$J^{PC}=1^{--}$ \longrightarrow transition from $\omega, \rho (S=1 L=0)$ to $\pi^0 (S=0 L=0)$ $\Delta L = 0$

$J^{PC}=1^{+-}$ \longrightarrow transition from $b_1, h_1 (S=0 L=1)$ to $\pi^0 (S=0 L=0)$ $\Delta L = 1$

“Vector” exchanges no change in OAM

“Axial-vector” exchanges change 1 unit of OAM!

$$F_{\gamma^* V \pi^0} = \int dx_1 dy_1 \int d^2\mathbf{b} \psi_V(y_1, b) \mathcal{C}K_0(\sqrt{x_1(1-x_1)Q^2}b) \psi_{\pi^0}(x_1, b) \exp(-S)$$

$$F_{\gamma^* A \pi^0} = \int dx_1 dy_1 \int d^2\mathbf{b} \psi_A^{(1)}(y_1, b) \mathcal{C}K_0(\sqrt{x_1(1-x_1)Q^2}b) \psi_{\pi^0}(x_1, b) \exp(-S)$$

Because of OAM axial vector transition involves Bessel J_1

$$\psi_A^{(1)}(y_1, b) = \int d^2 k_T J_1(y_1 b) \psi(y_1, k_T),$$

This yields configurations of larger “radius” in b space (suppressed with Q^2)

Helicity Amplitudes

Hard scattering

$$f_1 = f_4 = \int_{-1+\zeta}^1 dX g_2(X, \zeta, t, Q^2) F_V(Q^2) A_{++,+-}(X, \zeta, t)$$

$$f_2 = \int_{-1+\zeta}^1 dX \underline{g_2(X, \zeta, t, Q^2)} [F_V(Q^2) + F_A(Q^2)] \underline{A_{--,++}(X, \zeta, t)}$$

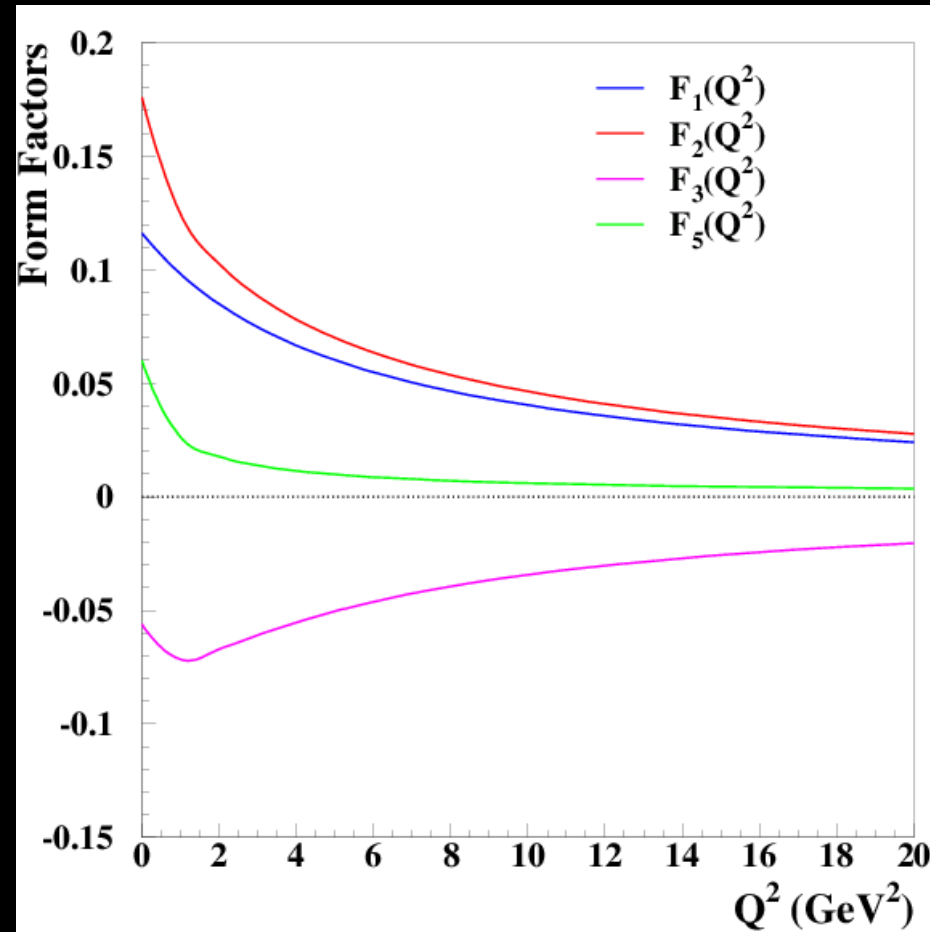
$$f_3 = \int_{-1+\zeta}^1 dX g_2(X, \zeta, t, Q^2) [F_A(Q^2) - F_V(Q^2)] A_{+,-,-+}(X, \zeta, t)$$

$$f_5 = \int_{-1+\zeta}^1 dX g_5(X, \zeta, t, Q^2) F_A(Q^2) A_{--,++}(X, \zeta, t)$$

Q^2 dependence at pion vertex

These are the form factors for the different configurations

Quantitative calculations are in progress



Conclusions

- Pseudoscalar and vector meson production are both essential channels to pin down chiral even and chiral odd GPDs
- There is lots of interesting physics to keep discovering (Q² dependence, BSM, charm ...)
- More synergy between theory and experiment!