

LMU

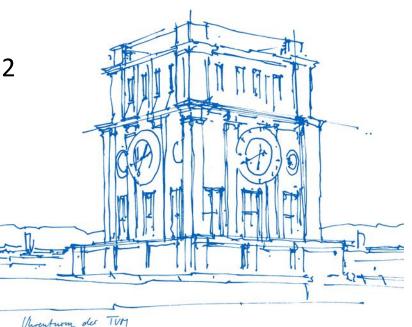
ТΠ

# Testing the chiral anomaly and measuring the radiative width of the $\rho(770)$ at COMPASS New result on $F_{3\pi}$ and $\Gamma_{\rho \to \pi \gamma}!$

Dominik Ecker for the COMPASS collaboration (dominik.ecker@tum.de)

International Workshop on Hadron Structure and Spectroscopy - 2022

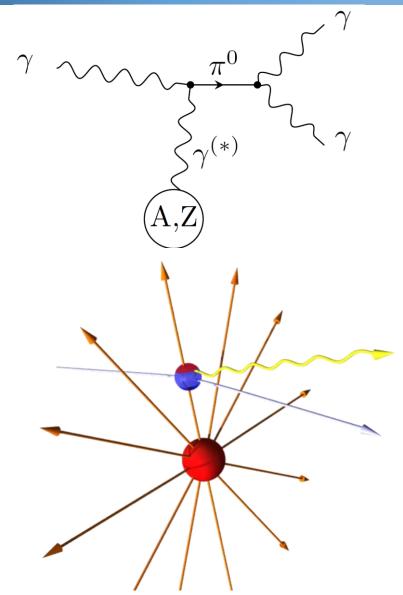




# **Primakoff reactions**

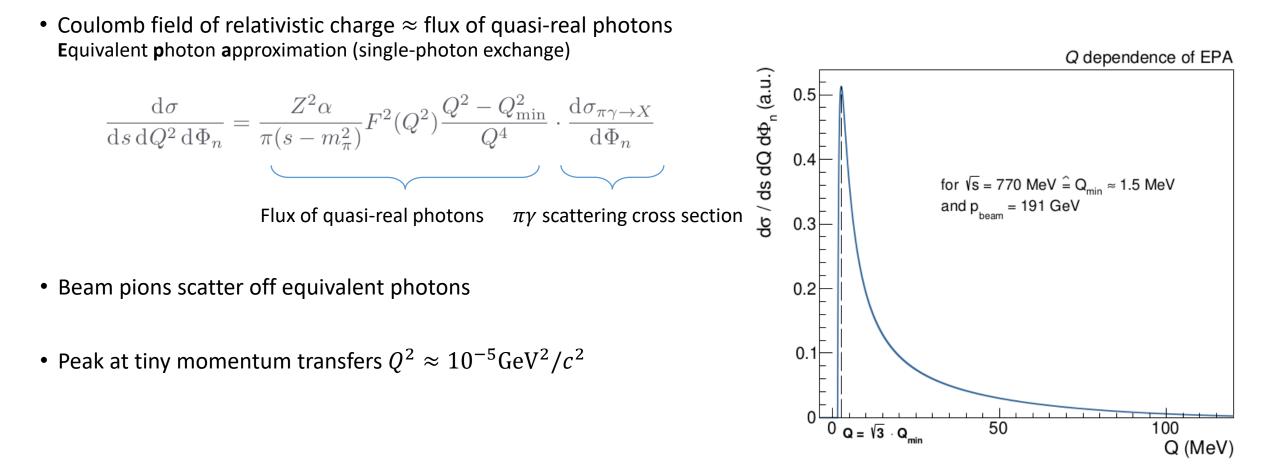


- Idea dates back to Henry Primakoff ("photon target")
- Photon is provided by the strong Coulomb field of a nucleus (typical field strength at  $d = 5R_{Ni}$ :  $E \approx 300 \text{ kV/fm}$ )
- Coulomb field of nucleus is a source of quasireal ( $P_{\gamma}^2 \ll m_{\pi}^2$ ) photons
- Large impact parameters (ultra-peripheral scattering)



### Weizsäcker-Williams approximation





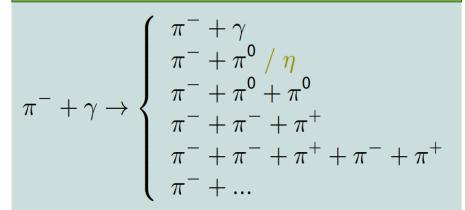
# Primakoff Program at COMPASS



#### **Requirements for Primakoff**

- Fixed target setup with nuclear target (*Z*-dependence of WW approximation)
- Good  $Q^2$ -resolution to separate Coulomb processes (Primakoff) from other processes (strong processes)
- Neutral particles in final state  $\rightarrow$  calorimetry with good position/energy resolution for good  $Q^2$ -resolution.

#### Interesting $\pi + \gamma$ reactions:



2004	$\pi^+\pi^-\pi^-$ : published result	→ PRL 108 (2012) 192001
2009	$\pi^-\gamma$ : pion polarizabilities $\pi^-\pi^0$ : chiral anomaly $\pi^-\pi^0\pi^0$ : chiral dynamics	PRL 114 (2015) 06002     Topic of this talk
2012	$\pi^-\gamma$ : pion polarizabilities $\pi^-\pi^0$ : chiral anomaly $\pi^-\pi^0\pi^0$ : chiral dynamics	4x larger data set compared to 2009

### Quantum Chromodynamics



- Quantum Chromodynamics (QCD) as true theory of strong interaction
- Lagrange density of QCD:

- Flavor symmetries? -> only approximate symmetries
  - $SU(2): m_u \approx m_d$  -> isospin symmetry
  - $SU(3): m_u \approx m_d \approx m_s$
- - -> the eightfold way

## Chiral symmetry of QCD



- Quantum Chromodynamics (QCD) as true theory of strong interaction
- Lagrange density of QCD:

$$\mathscr{L}_{QCD} = \sum_{\substack{f = \{u,d, \\ c,s,t,b\}}} \sum_{i,j=1}^{N_c} \overline{\psi}_{f,j} (i\gamma^{\mu} D_{i,\mu}^{j} - m_f \delta_i^{j}) \psi^{f,i} - \frac{1}{4} \sum_{a=1}^{N_c^2 - 1} G_{\mu\nu}^a G_a^{\mu\nu}$$

• Approximate flavor symmetries in chiral limit  $(m_u = m_d = m_s = 0)$ :

#### $SU(3)_R \times SU(3)_L$

- Left- and right-handed fields decouple for massless particles
- Chirality can directly be translated to parity of particle
   → mass-degenerate doublets of states with opposite parity

## Chiral symmetry of QCD

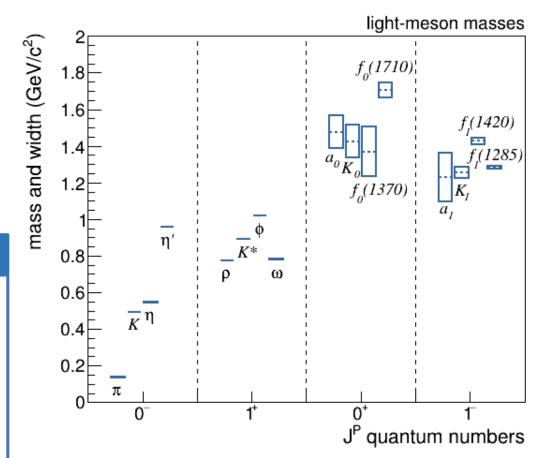
• Lagrange density of QCD:

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• Approximate flavor symmetries in chiral limit  $(m_u = m_d = m_s = 0)$ :

#### $SU(3)_R \times SU(3)_L$

- Left- and right-handed fields decouple for massless particles
- Chirality can directly be translated to parity of particle
   → mass-degenerate doublets of states with opposite parity
- Why does chiral symmetry not manifest itself in the spectrum (in contrast to isospin and eightful way)?
  - → Nambu-Goldstone mechanism for spontaneous/dynamic breakdown of chiral symmetry



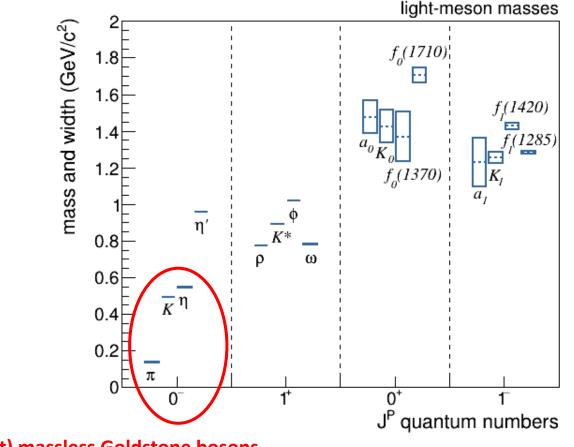




Spontaneous symmetry breaking ⇒ Eight massless, spinless Goldstone bosons

 $(\pi^{\pm}, \pi^{0}, K^{\pm}, K^{0}, \bar{K}^{0}, \eta)$ 

- ⇒ Explicit breaking of chiral symmetry due to the small quark masses -> Goldstone bosons acquire mass
- $\Rightarrow SU(3)_R \times SU(3)_L \rightarrow SU(3)_V$
- ⇒ Chiral Perturbation Theory: effective Lagrangian with power-counting scheme as low-energy theory for QCD makes use of chiral symmetry



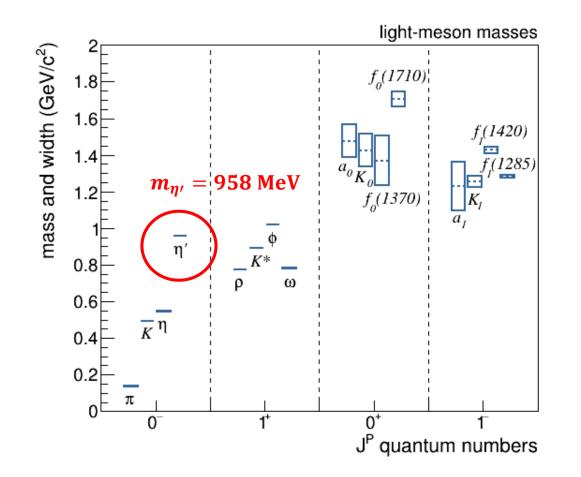
(almost) massless Goldstone bosons

# The chiral anomaly

• Lagrange density of QCD:

$$\mathcal{L}_{QCD} = \sum_{\substack{f = \{u,d, \\ c,s,t,b\}}} \sum_{i,j=1}^{N_c} \overline{\psi}_{f,j} (i\gamma^{\mu} D_{i,\mu}^{j} - m_f \delta_i^{j}) \psi^{f,i} - \frac{1}{4} \sum_{a=1}^{N_c^2 - 1} G_{\mu\nu}^{a} G_a^{\mu\nu}$$

- Features axial U(1)-symmetry in chiral limit:  $\psi(x) \rightarrow e^{i\theta\gamma_5}\psi(x)$
- No ninth "unnaturally light" meson
- Anomalous symmetry breaking: symmetry of the Lagrangian does not lead to conserved Noether currents
- Anomaly: Symmetry of classical Lagrangian violated at quantum level





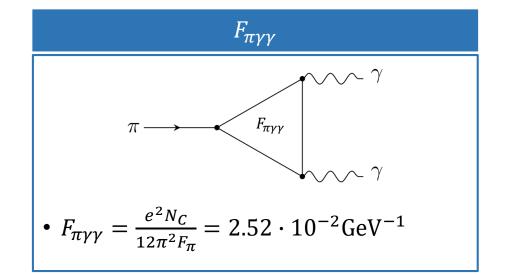
#### Wess-Zumino-Witten term

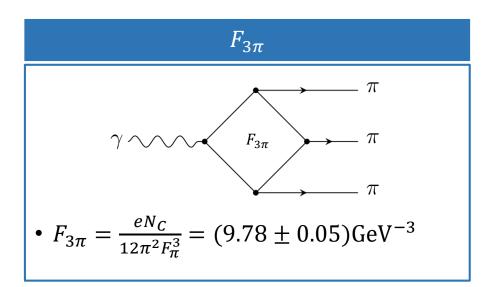


- Chiral anomaly in ChPT taken into account by Wess-Zumino-Witten (WZW) term
- Describes coupling of odd number of Goldstone bosons:

SU(2) flavor	SU(3) flavor
$\pi^0 \to \gamma \gamma$	$K^+K^- \! \to \pi^+\pi^-\pi^0$
$\gamma \pi^- \rightarrow \pi^- \pi^0$	$\eta \!  ightarrow \! \pi^+ \pi^- \gamma$
$\pi^+ \rightarrow e^+ \nu_e \gamma$	$K^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$
etc.	etc.

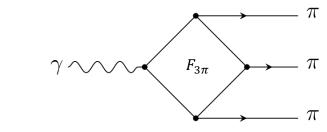
• Effective theory -> pion decay constant measured from leptonic decays of the charged pion ( $\pi^{\pm} \rightarrow \mu^{\pm} + \nu$ )

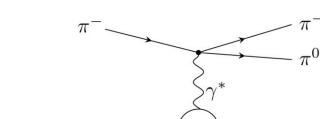


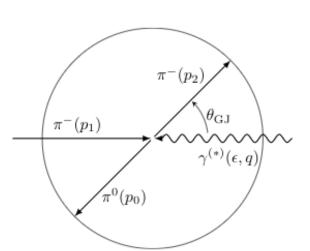


# Testing the chiral anomaly - $F_{3\pi}$









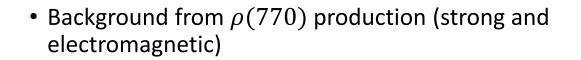
- $F_{3\pi}$ : Direct coupling of  $\gamma$  to  $3\pi$  process proceeds primarily via the chiral anomaly => one of the most definitive tests of low-energy QCD
- Accessible in Primakoff reactions via:  $\pi^-\gamma^* \rightarrow \pi^-\pi^0$
- Challenges:
  - 1. Explicit chiral symmetry breaking:

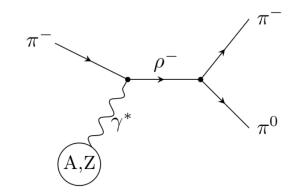
$$F_{3\pi} = \frac{eN_C}{12\pi^2 F_{\pi}^3} = (9.78 \pm 0.05) \text{GeV}^{-3} = F(s = t = u = 0)$$

2. Coherent background from  $\rho(770)$  production

# Coherent background from $\rho(770)$ meson





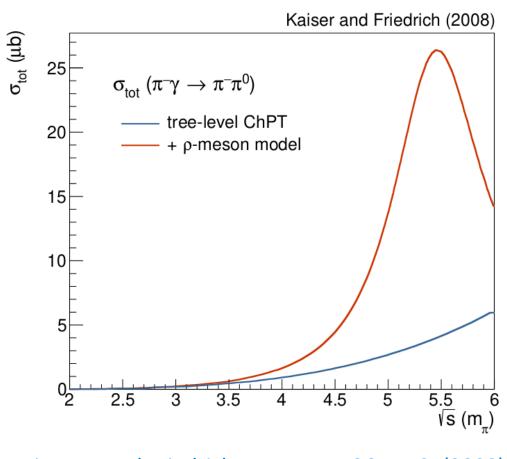


 $\Rightarrow$  possibility of extraction of radiative width of  $\rho$ -meson:

$$\Gamma_{(\rho \to \pi \gamma)} / \Gamma_{\text{tot}} \approx 4.5 \cdot 10^{-4}$$

 $\pi^0, \eta$ 

⇒ contributes to hadronic vacuum polarization terms in calculations of g - 2 of e and  $\mu$ 

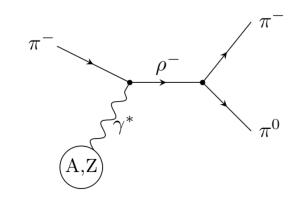


Kaiser, N. and Friedrich, J. M., EPJA 36 no. 2, (2008) 181–188

# Radiative width of $\rho(770)$ meson



• Background from  $\rho(770)$  production (strong and electromagnetic)



 $\Rightarrow$  possibility of extraction of radiative width of  $\rho\text{-}$  meson:

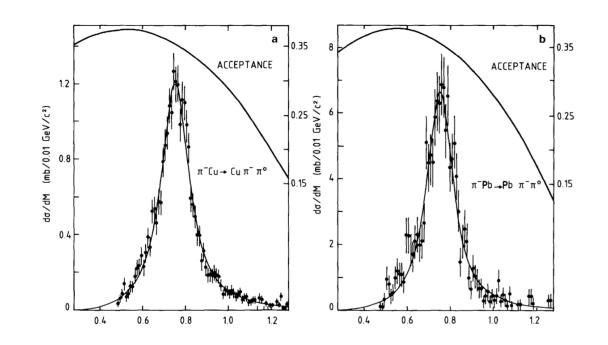
$$\Gamma_{(\rho \to \pi \gamma)} / \Gamma_{\text{tot}} \approx 4.5 \cdot 10^{-4}$$

 $\pi^0, \eta$ 

⇒ contributes to hadronic vacuum polarization terms in calculations of g - 2 of e and  $\mu$ 

<u>Capraro, L. *et al.* NPB 288 (1987) 659-680</u> at CERN (SPS):

• From fit of  $d\sigma/dt$  for  $\rho$  production:  $\Gamma(\rho \rightarrow \pi \gamma) = (81 \pm 4 \pm 4) \text{ keV}$ 



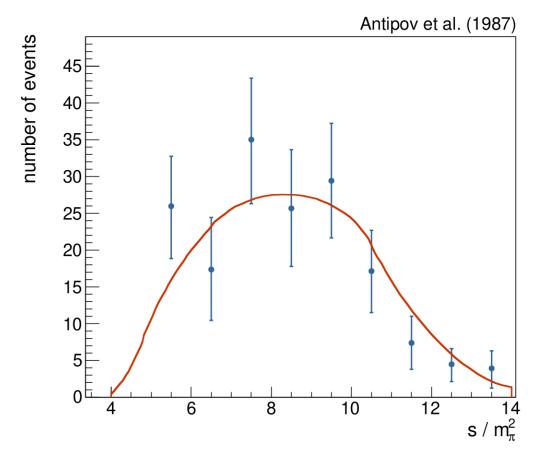


Antipov, Y. et al. PRD 36 (1987) 101103 using data from Serpukhov experiments

Problem of explicit chiral symmetry breaking:

As previously noted, the value  $F^{3\pi}$  is supposed to vary slowly with  $s,t,q^2 \ll m_{\rho}^2$  so that  $F^{3\pi} \simeq F^{3\pi}(0)$ .

$$\Rightarrow \bar{F}_{3\pi} = (12.9 \pm 0.9 \pm 0.5) \text{ GeV}^{-3}$$





#### Ametller, L. et al. PRD 64 (2001) 094009

PHYSICAL REVIEW D, VOLUME 64, 094009

Electromagnetic corrections to  $\gamma \pi^{\pm} \rightarrow \pi^0 \pi^{\pm}$ 

Ll. Ametller Dept. de Física i Enginyeria Nuclear, UPC, E-08034 Barcelona, Spain

M. Knecht and P. Talavera Centre de Physique Théorique, CNRS-Luminy, Case 907, F-13288 Marseille Cedex 9, France (Received 11 July 2001; published 3 October 2001)

The amplitude for the anomalous transitions  $\gamma \pi^{\pm} \rightarrow \pi^0 \pi^{\pm}$  is analyzed within chiral perturbation theory including electromagnetic interactions. The presence of a *t*-channel one-photon exchange contribution induces sizable  $\mathcal{O}(e^2)$  corrections which enhance the cross section in the threshold region and bring the theoretical prediction into agreement with available data. In the case of the crossed reaction  $\gamma \pi^0 \rightarrow \pi^+ \pi^-$ , the same contribution appears in the *s* channel and its effects are small.

DOI: 10.1103/PhysRevD.64.094009 PACS number(s): 12.39.Fe, 11.30.Rd, 13.60.Le, 13.75.-n

Reanalysis of Serpukhov data using chiral expansion:

$$F_{3\pi}(s,t,u) = F_{3\pi}(f^{(0)}(s,t,u) + f^{(1)}(s,t,u) + f^{(2)}(s,t,u) + \dots)$$

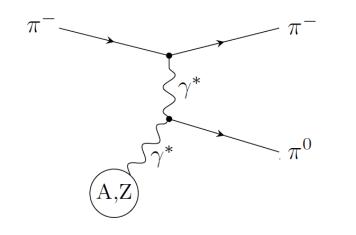
• Extrapolation using one loop and two loop corrections:

$$F_{3\pi} = (11.4 \pm 1.3) \text{ GeV}^{-3}$$

### Previous measurement of $F_{3\pi}$ - Reanalysis



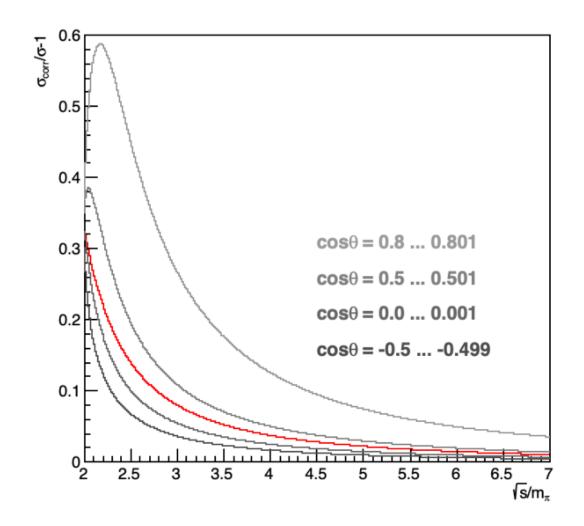
 Electro-magnetic corrections => significant contribution to f<sup>(0)</sup>(s, t, u) when isospin breaking effect are taken into account.



• Integrated correction amounts to 32% at threshold

 $\Rightarrow F_{3\pi} = (10.7 \pm 1.2) \text{ GeV}^{-3}$ 

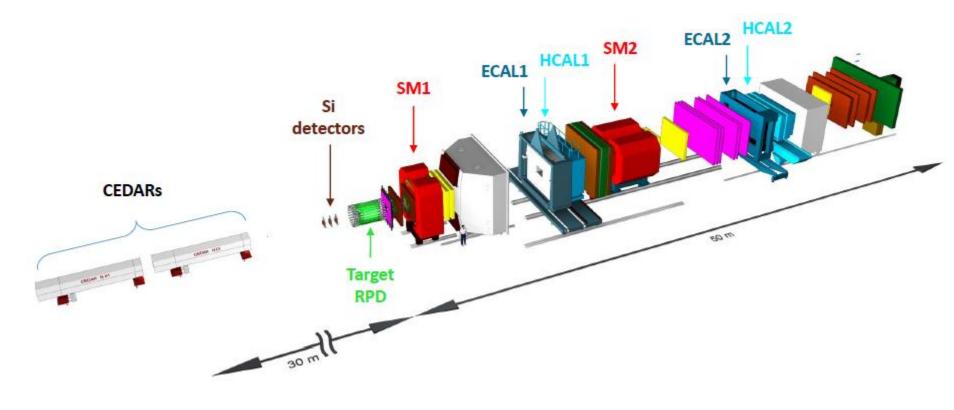
- Precision of previous measurements: O(10%)
  - $\Rightarrow$  More precise experimental determination desirable



Ametller, L. et al. PRD 64 (2001) 094009

#### The COMPASS experiment at CERN



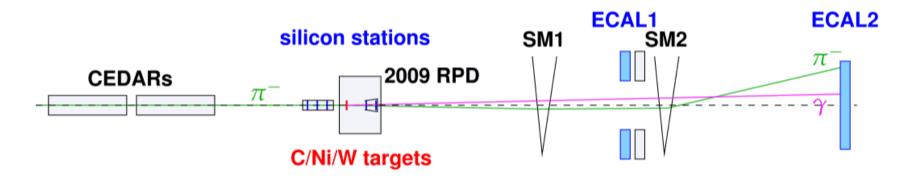


Abbon, P. et al. NIM A 779 (2014) 69–115

- 190 GeV negative hadron beam
- Beam PID
- Nuclear target(s): Ni and W
- Calorimetric trigger on neutrals
- Two stage spectrometer (LAS and SAS) with tracking and calorimeter

### Principle of Measurement





- 190 GeV negative hadron beam: 96.8%  $\pi^-$ , 2.4%  $K^-$ , 0.8%  $\bar{p}$
- Beam particle identification by Cherenkov detectors
- 4mm Ni target disk ( $\approx 25\% X/X_0$ )
- Measure scattered  $\pi^-$  and produced photons (number of photons depends on final state)
- Select exclusive events at very low  $Q^2$
- For absolute cross-section measurements:

Luminosity determination via free Kaon decays

$$(K^- \rightarrow \pi^- \pi^0 \text{ or } K^- \rightarrow \pi^- \pi^0 \pi^0)$$

#### **COMPASS** measurement



• Dispersive framework to deduce  $F_{3\pi}$  from a fit to the  $\pi^{-}\pi^{0}$  mass distribution up to 1.0 GeV including the  $\rho(770)$ -resonance:

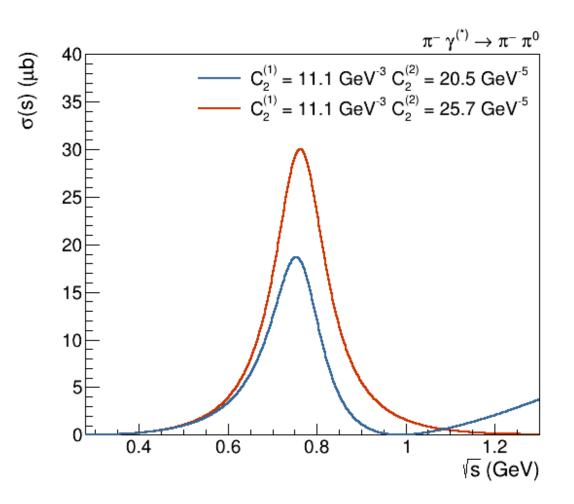
$$\sigma(s) = \frac{(s - 4m_{\pi}^2)^{3/2}(s - m_{\pi}^2)}{1024\pi\sqrt{s}} \int_{-1}^{1} dz (1 - z^2) |\mathcal{F}(s, t, u)|^2$$

With

$$\mathcal{F}(s,t,u) = C_2^{(1)} \mathcal{F}_2^{(1)}(s,t,u) + C_2^{(2)} \mathcal{F}_2^{(2)}(s,t,u) - \frac{2e^2 F_\pi^2 F_{3\pi}}{t}$$

 $C_2^{(1)}$ ,  $C_2^{(2)}$ : fit parameters

 $\mathcal{F}_{2}^{(1)}(s, t, u), \mathcal{F}_{2}^{(2)}(s, t, u)$ : provided by theory colleagues (Kubis, Hoferichter)



<u>M. Hoferichter, B. Kubis, and D. Sakkas, PRD 86 (2012)</u> 116009

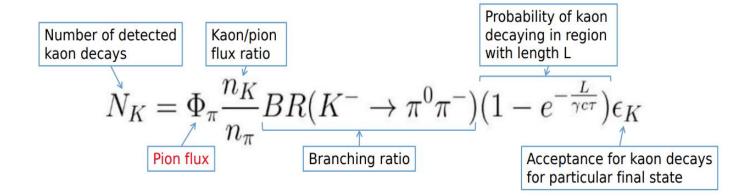
#### Luminosity determination



• Needed for absolute cross section measurement: effective integrated luminosity (DAQ dead time taken into account)

Effective luminosity:  $L_{eff} = L \cdot (1 - \epsilon_{DAQ})$ 

- Luminosity can be determined via free decays of beam kaons in the beam:
  - Use CEDARs to tag kaons
  - Measure free decays where no material
  - Exclusive events with zero momentum transfer





Decay channel	$\Gamma_i/\Gamma$	Remark
$K^- \to \mu^- \bar{\nu}_\mu$	$(63.56 \pm 0.11)$ %	Does not deposit energy in ECAL2 (Primakoff-trigger)
$K^-  o \pi^- \pi^0$	$(20.67 \pm 0.08)$ %	Similar systematics as Primakoff $\pi^- \rightarrow \pi^- \pi^0$ channel
$K^- \rightarrow \pi^- \pi^- \pi^+$	(5.583 ± 0.024) %	Does not deposit energy in ECAL2 (Primakoff-trigger)
$K^-  ightarrow e^- \pi^0 \overline{ u}_e$	$(5.07 \pm 0.08)$ %	Non exclusive, missing energy
$K^-  ightarrow \mu^- \pi^0 \overline{ u}_\mu$	$(3.352 \pm 0.033)$ %	Non exclusive, missing energy
$K^-  ightarrow \pi^- \pi^0 \pi^0$	$(1.760 \pm 0.023)$ %	Used to determine $\pi/K$ -ratio in the beam
others	$< 10^{-4}$	No significant contribution to background expected

 Different channels may form background for each other, but give possibility to crosscheck results

Used for luminosity determination Considered as background process

### Effective integrated luminosity



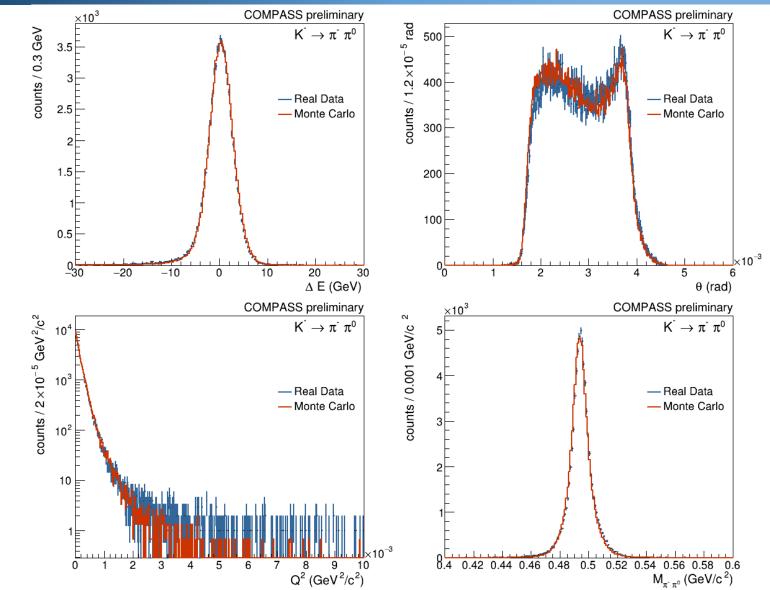
 $L_{2\pi,eff} = 5.21 \pm 0.04_{stat} \text{ nb}^{-1}$  $L_{3\pi,eff} = 5.06 \pm 0.12_{stat} \text{ nb}^{-1}$ 

Largest contributions to systematic uncertainty:

- CEDAR tag efficiency: 7%
- ECAL reconstruction: 5%
- kaon/pion beam ratio: 2.5%

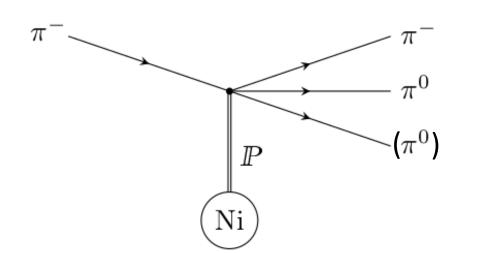
Result:

$$L_{eff} = 5.21 \pm 0.48_{syst} \pm 0.04_{stat}$$



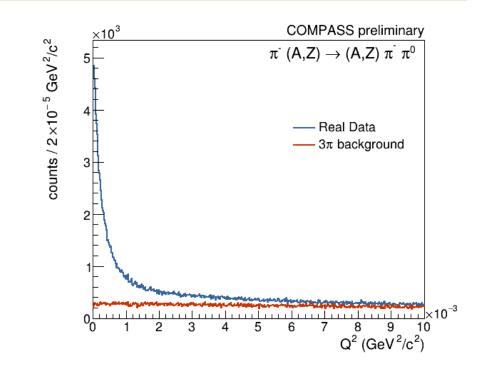
### Main Background





•  $\pi^{-}\pi^{0}$ -final state forbidden by *G*-parity conservation

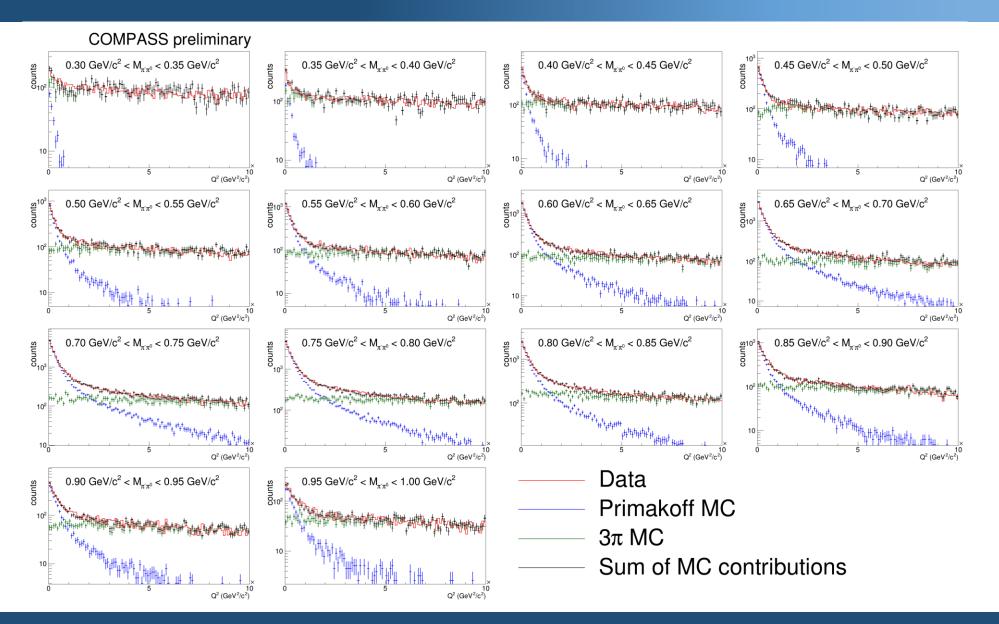
- Large cross section for  $\pi^{-}\pi^{0}\pi^{0}$  final state  $\Rightarrow$  loss of one (soft)  $\pi^{0}$
- Approach: determine leakage from 3pi MC data with 2pi event selection



Approach for  $3\pi$  leakage:

- Select diffractive  $3\pi$  events
- Develop partial-wave model
- Weight  $3\pi$  Monte Carlo data set according to model
- Subtract from  $2\pi$  event sample

# Scaling of $3\pi$ Monte Carlo background prediction



Dominik Ecker | IWHSS | 30/08/2022

#### Results of dispersive fits



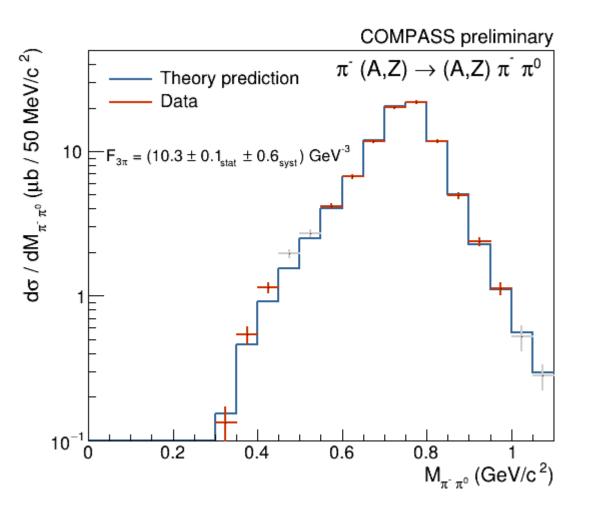
• Selection:  $Q^2 < 1.296 \cdot 10^{-3} \,\text{GeV}^2/c^2$ 

$$C_{2}^{(1)} = (10.5 \pm 0.1_{stat} \pm 0.6_{syst}) \text{GeV}^{-3}$$
$$C_{2}^{(2)} = (24.5 \pm 0.1_{stat})^{+1.6} \text{GeV}^{-5}$$

$$F_{3\pi} = (10.3 \pm 0.1_{stat} \pm 0.6_{syst}) \text{GeV}^{-3}$$

$$\Gamma_{\rho \to \pi \gamma} = \left(76 \pm 1_{stat-8 syst}^{+10}\right) \text{keV}$$

- Preliminary result for  $F_{3\pi}$  in agreement with theory prediction from ChPT
- Lower systematics to be expected



#### Comparison to previous measurements



• COMPASS: First combined measurement of  $F_{3\pi}$  and  $\Gamma_{\rho \to \pi \gamma}$ 

$$F_{3\pi} = (10.3 \pm 0.1_{stat} \pm 0.6_{syst}) \text{GeV}^{-3}$$
$$\Gamma_{\rho \to \pi\gamma} = \left(76 \pm 1_{stat} + 10_{-8} + 10_{syst}\right) \text{keV}$$

- Intensive test of systematics:
  - Different  $K^-$  decay channels
  - Studies on different background contributions ( $\omega$  and  $\pi$  exchange)
- Accompanied with intensive analysis of  $\pi^-\text{Ni} \rightarrow \pi^-\pi^0\pi^0\text{Ni}$  for background estimation

<u>Capraro, L. *et al.* NPB 288 (1987) 659-680</u> at CERN (SPS):

 $\Gamma_{\rho \to \pi \gamma} = (81 \pm 4 \pm 4) \text{ keV}$ 

Obtained by fitting  $d\sigma/dt$  distribution (separation of nuclear and Coulomb processes)

- Neglecting chiral production of  $\pi^-\pi^0$
- Presumably underestimation of systematics  $(3\pi \text{ leakage, beam composition})$

$\Gamma(\pi^{\pm}\gamma)$					Гз
VALUE (keV)	DOCUMENT ID		TECN	CHG	COMMENT
68 ±7 OUR FIT	Error includes sca	le fact	or of 2.3	3.	
68 ±7 OUR AVE	RAGE Error inclu	des sca	ale facto	r of 2.2	2. See the ideogram below.
$81$ $\pm 4$ $\pm 4$	CAPRARO	87	SPEC	_	$200 \pi^- A \rightarrow \pi^- \pi^0 A$
$59.8 \pm 4.0$	HUSTON	86	SPEC	+	202 $\pi^+ A \rightarrow \pi^+ \pi^0 A$
$71 \pm 7$	JENSEN	83	SPEC	_	156–260 $\pi^- A \rightarrow \pi^- \pi^0 A$

#### Comparison to previous measurements



• COMPASS: First combined measurement of  $F_{3\pi}$  and  $\Gamma_{\rho \to \pi \gamma}$ 

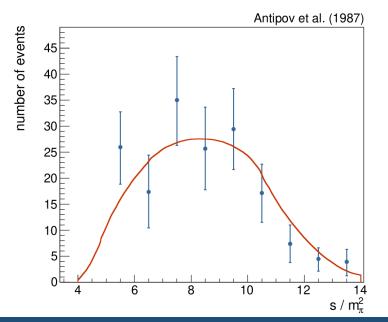
$$F_{3\pi} = (10.3 \pm 0.1_{stat} \pm 0.6_{syst}) \text{GeV}^{-3}$$
$$\Gamma_{\rho \to \pi\gamma} = \left(76 \pm 1_{stat} + 10_{-8} + 10_{syst}\right) \text{keV}$$

- Intensive test of systematics:
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Antipov, Y. et al. PRD 36 (1987) 101103 and reanalyzed by Ametller, L. et al. PRD 64 (2001) 094009

 $F_{3\pi} = (10.7 \pm 1.2) \text{ GeV}^{-3}$ 

- Neglecting s-channel production of  $\rho$  meson
- No proper consideration of systematics



#### Thank you for your attention



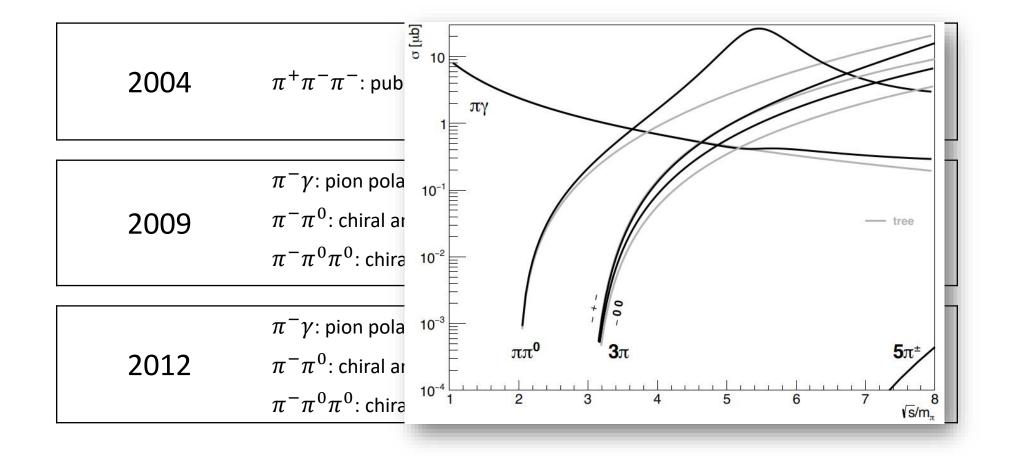
# 2004 $\pi^+\pi^-\pi^-$ : published result $\implies$ PRL 108 (2012) 192001

	$\pi^-\gamma$ : pion polarizabilities $\implies$ Phys. Rev. Lett. 114	(2015) 06002
2009	$\pi^{-}\pi^{0}$ : chiral anomaly Presented in this ta	lk
	$\pi^{-}\pi^{0}\pi^{0}$ : chiral dynamics	

	$\pi^-\gamma$ : pion polarizabilities
2012	$\pi^{-}\pi^{0}$ : chiral anomaly Ax larger data set compared to 2009 No results yet, MC still incomplete
	$\pi^{-}\pi^{0}\pi^{0}$ : chiral dynamics

#### Primakoff data sets at COMPASS



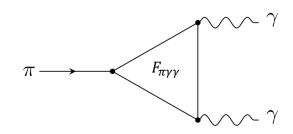


# Discovery of the chiral anomaly – $\pi^0$ lifetime



• First definitive measurement of  $\pi^0$ -lifetime in 1963:

 $\tau_{\exp}(\pi^0) = (9.5 \pm 1.5) \cdot 10^{-17} s \neq \tau_{PCAC}(\pi^0) \approx 10^{-13} s$ 

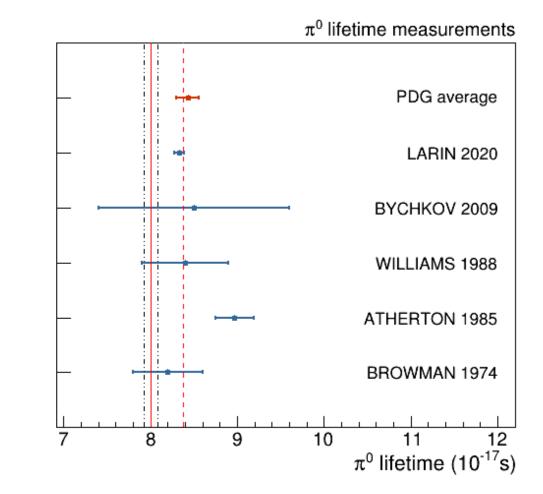


• Adler, Bell, Jackiw, Bardeen 1969: calculation of triangle diagram

$$\Gamma^{\text{anom}}(\pi^{0} \to \gamma \gamma) = F_{\pi \gamma \gamma}^{2} \cdot \frac{m_{\pi^{0}}^{3}}{64\pi} = \left(\frac{e^{2}N_{c}}{12\pi^{2}F_{\pi}}\right)^{2} \frac{m_{\pi^{0}}^{3}}{64\pi} = 7.75 \,\text{eV}$$
$$\tau(\pi^{0}) = \text{BR}(\pi^{0} \to \gamma \gamma) \cdot \frac{\hbar}{\Gamma^{\text{anom}}(\pi^{0} \to \gamma \gamma)}$$
$$= 8.38 \cdot 10^{-17} \,\text{s}$$

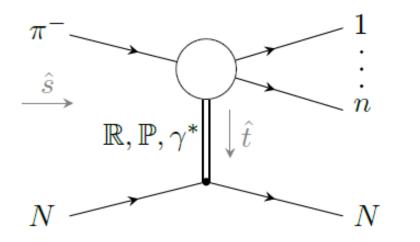
• Moussalam and Kampf 2009: NLO-calculation in chiral perturbation theory

$$\tau_{\rm NLO}(\pi^0) = (8.04 \pm 0.11) \cdot 10^{-17} \,\mathrm{s}$$



### Production mechanisms for mesons at COMPASS

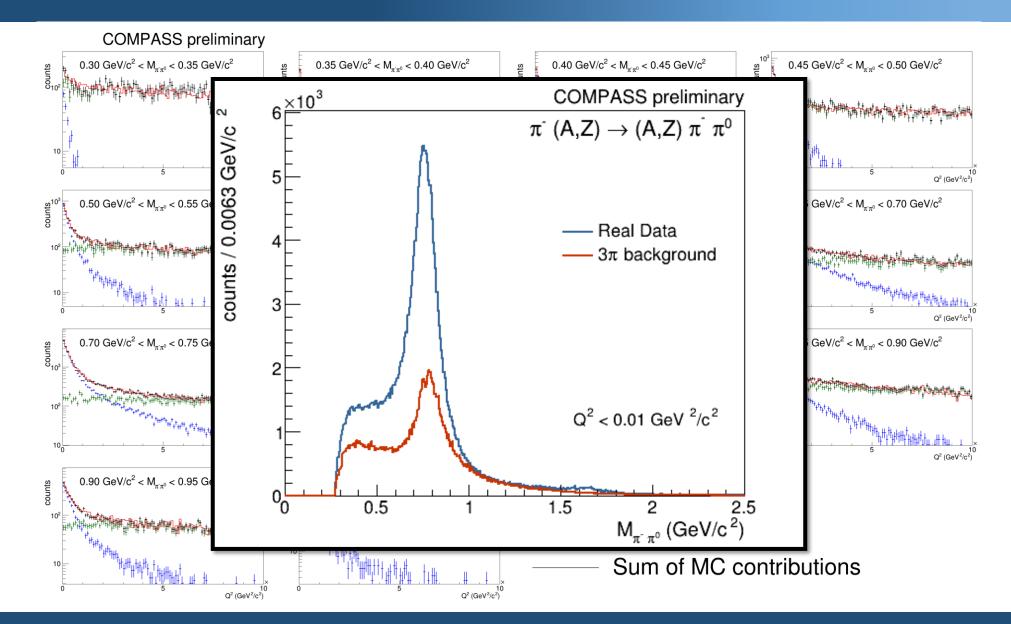




- Strong and electromagnetic production of mesons
- Electromagnetic production via Primakoff effect with sharp  $Q^2$  distribution
- Pomeron exchange:  $\pi^{-}\pi^{0}$  final state forbidden due to *G*parity conservation, but: large cross-section for  $\pi^{-}\pi^{0}\pi^{0}$ final state  $\rightarrow$  loss of one (soft)  $\pi^{0}$  as main background

	Primakoff	₽ (strong)	$\mathbb{R}$ (strong)
$\sigma(s)$	$\propto \ln(\sqrt{s})$	$\propto$ const.	$\propto 1/\sqrt{s}$
$\sigma(A_{\text{target}})$	$\propto$ const.	$\propto A^{2/3}$	$\propto A^{2/3}$
$\sigma(Z_{\text{target}})$	$\propto Z^2$	$\propto$ const.	$\propto$ const.
$\sigma(t)$	$\propto \frac{Q^2 - Q_{\min}^2}{Q^4} = \frac{\hat{t}'}{\hat{t}^2}$	$\propto e^{-b\hat{t}'}$	$\propto g(\hat{t}) \cdot e^{-b\hat{t}'}$ for small $\hat{t}$

# Scaling of $3\pi$ Monte Carlo background prediction

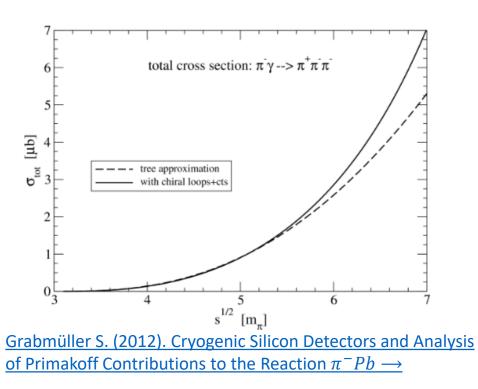


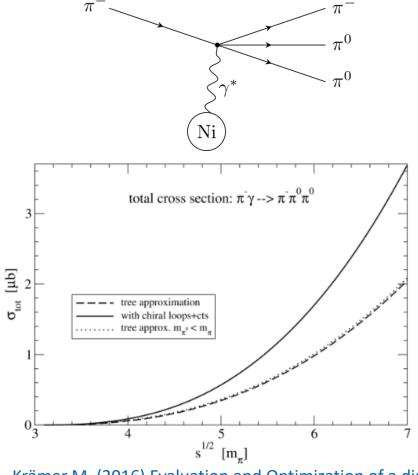
/ | | |

#### Chiral Tree, Chiral Loop



- Direct (point-like) coupling of photon to 4 pions
- Prediction from ChPT at tree- and loop-level available





<u>Krämer M. (2016) Evaluation and Optimization of a digital</u> <u>calorimetric trigger and analysis of  $\pi^-Ni \rightarrow$ </u>



- Selection:  $Q^2 < 1.296 \cdot 10^{-3} \, {\rm GeV}^2/c^2$
- Trigger on energy deposit in central part of electromagnetic calorimeter ( $E_{\text{trig}} > 68 \text{ GeV}$ )
- Minimum energy of  $\pi^0 \rightarrow$  maximum scattering angle of  $\pi^-$  in Gottfried-Jackson frame

