

Longitudinal Beam Profile Measurements

T. Lefevre, CERN

- Longitudinal beam profile in Accelerators
- Bunch Length measurement techniques

“When you are courting a nice girl an hour seems like a second. When you sit on a red-hot cinder a second seems like an hour. That's relativity. ”

Albert Einstein



How to accelerate Particles

DC Accelerator



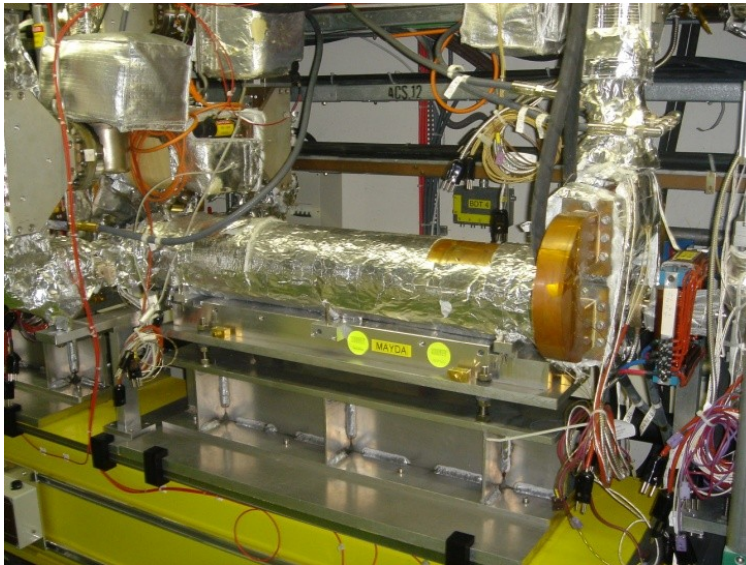
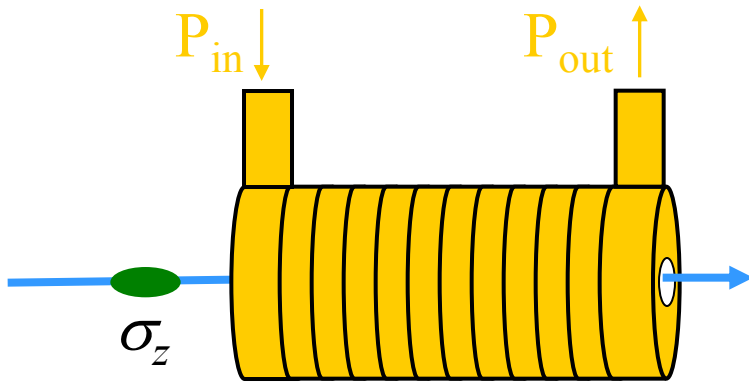
RF Accelerator



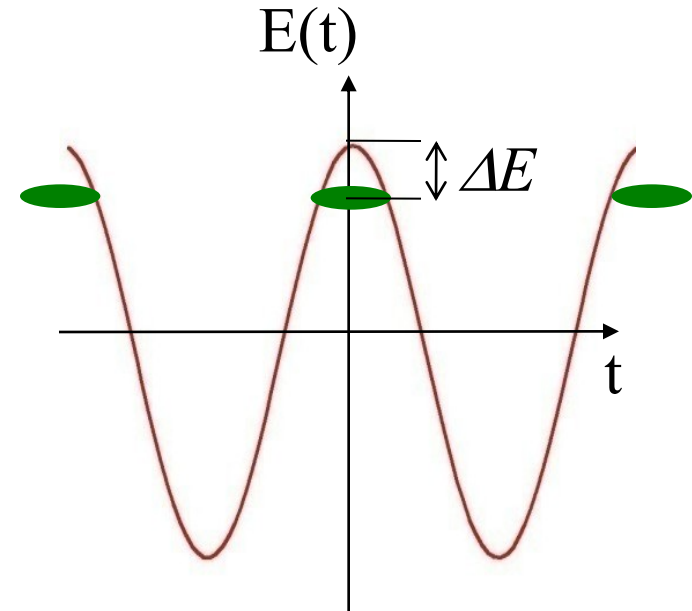
synchronize particle
with an
electromagnetic wave!

How to accelerate Particles

RF Accelerating structures



RF Accelerating Field



At 3GHz

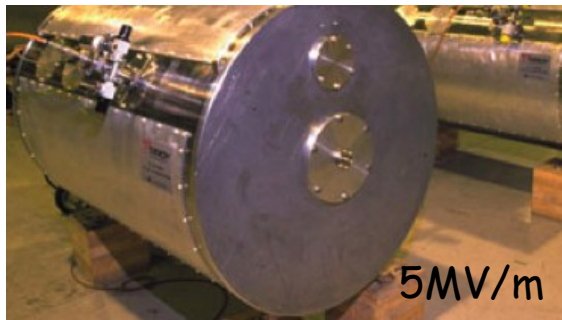
1 period = 333ps : Bunch spacing
Typical bunch length : few deg ~ few ps

Accelerating Cavities



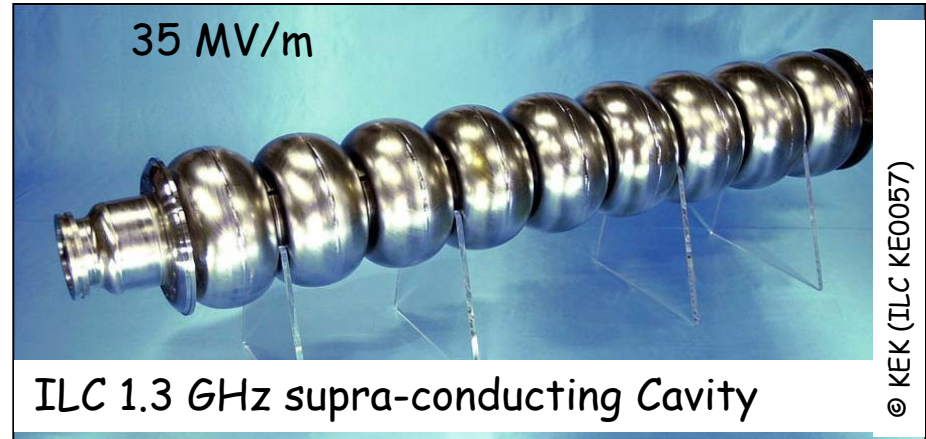
CERN PS 19 MHz Cavity (prototype 1966)

© CERN



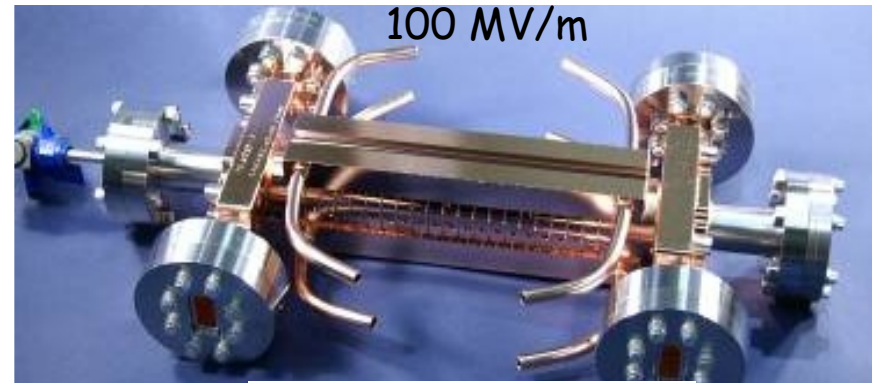
5MV/m

400MHz LHC Cavity in its cryo-module



ILC 1.3 GHz supra-conducting Cavity

© KEK (ILC KE0057)



CLIC 12 GHz Cavity

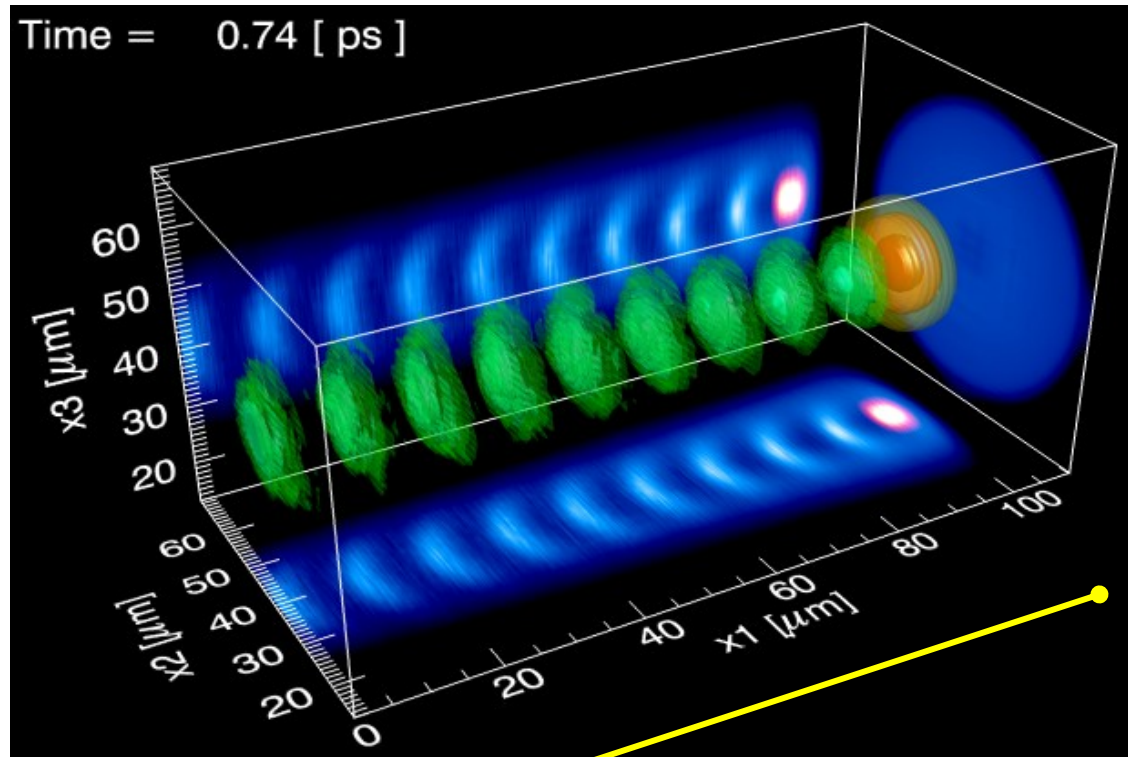
Longitudinal profile in accelerators

- Develop machine with the aim to improve luminosity for a linear collider or brightness for a radiation source or neutron source

H ⁻ @ SNS	100ps
H ⁺ @ LHC	230ps
e ⁻ @ ILC	500fs
e ⁻ @ CLIC	130fs
e ⁻ @ XFEL	80fs
e ⁻ @ LCLS	75fs

What is the next frontier ?

Courtesy of W. Mori & L. da Silva



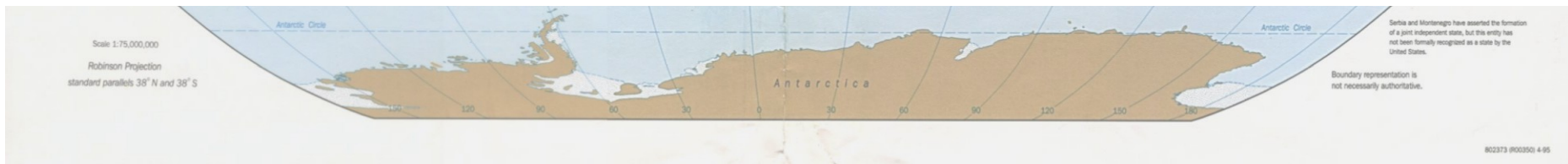
100 μm

Plasma cavity

What is the next frontier ?



ELI will be the first infrastructure dedicated to the fundamental study of laser-matter interaction in a new and unsurpassed regime of laser intensity: the ultra-relativistic regime ($I > 10^{23} \text{ W/cm}^2$). **At its centre will be an exawatt class laser** ~1000 times more powerful than either the Laser Mégajoule in France or the National Ignition Facility (NIF) in the US. In contrast to these projects, ELI will attain its extreme power from the shortness of its pulses (femtosecond and attosecond). The infrastructure will serve to investigate a new generation of **compact accelerators delivering energetic particle and radiation beams of femtosecond (10^{-15} s) to attosecond (10^{-18} s) duration**. Relativistic compression offers the potential of intensities exceeding $I > 10^{25} \text{ W/cm}^2$, which will challenge the vacuum critical field as well as provide a new avenue to ultrafast **attosecond to zeptosecond (10^{-21} s) studies of laser-matter interaction**. ELI will afford wide benefits to society ranging from improvement of oncology treatment, medical imaging, fast electronics and our understanding of aging nuclear reactor materials to development of new methods of nuclear waste processing.



Beam instrumentation

1- Longitudinal Profile



RMS or FWHM values

- *More precise information on the beam characteristic*

2- Single shot measurements



Sampling measurements

- *Do not care about the beam reproducibility*
- *No additional problem due to timing jitter*

3- Non interceptive



Destructive Devices

- *Can be used for beam study and beam control for on-line monitoring*
- *Beam Power : No risk of damage by the beam itself*

Beam instrumentation

Simplicity and Reliability

'Beam diagnostics should help you to understand the beam properties, it should not be the opposite'

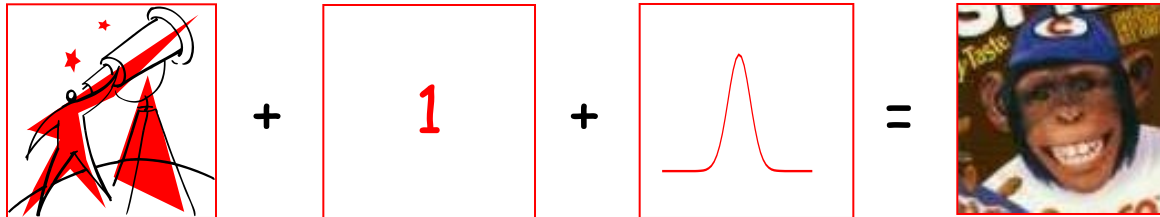


A detector, what for ?

- Online Beam stability → Non-intercepting and reliable
Only have access to a partial information (RMS values,..)
- Beam characterization and beam physics study → Full information
Complexity and time consuming

Beam instrumentation

Can we do non intercepting, single shot, beam profile measurement in an easy way ?



All in red → 'perfect system'

Bunch length measurement techniques

Short bunch length measurements

Optical Method

1. Produce visible light
2. Analyse the light pulse using dedicated instruments

Bunch Frequency Spectrum

The shorter the bunches, the broader the bunch frequency spectrum

RF manipulation

Use RF techniques to convert time information into spatial information

Laser-based beam diagnostic

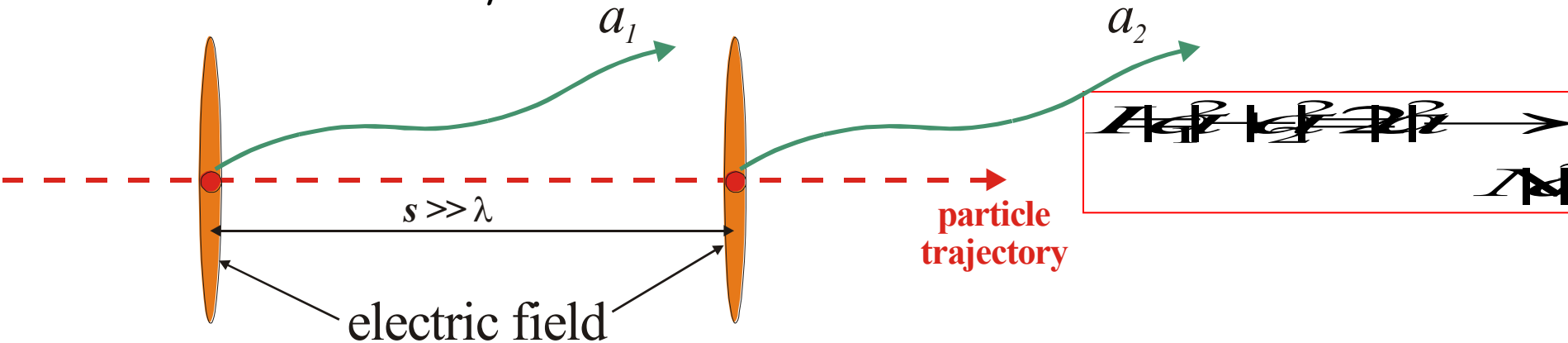
Using short laser pulses and sampling techniques

Radiative techniques

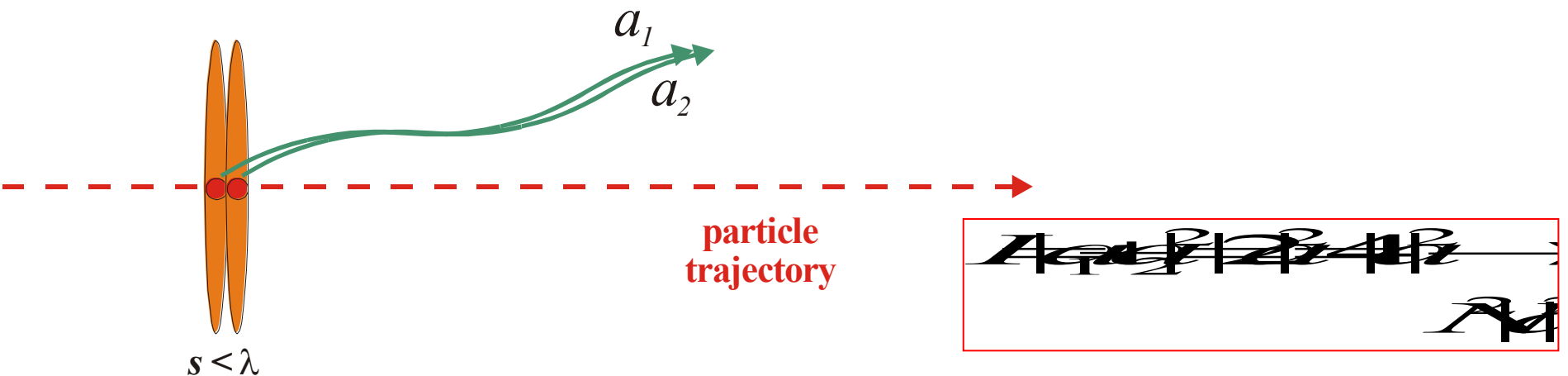
'Convert particles into photons'

Coherent / Incoherent Radiation

- At wavelength much shorter than the bunch length, the radiation is emitted incoherently because each electron emits its radiation independently from the others without a defined phase relation



- A coherent enhancement occurs at wavelengths which are equal to or longer than the bunch length, where fixed phase relations are existing, resulting in the temporal coherence of the radiation



Radiation Spectrum

Incoherent term

Coherent term

$$S(\omega) = S_p(\omega) [N + N(N-1)F(\omega)]$$

$S(\omega)$ – radiation spectrum

$S_p(\omega)$ – single particle spectrum

N – number of electrons in a bunch

$F(\omega)$ – longitudinal bunch form factor

$$F(\omega) = \int_{-\infty}^{\infty} \rho(s) e^{i\omega s/c} ds$$

$\rho(s)$ – Longitudinal particle distribution in a bunch

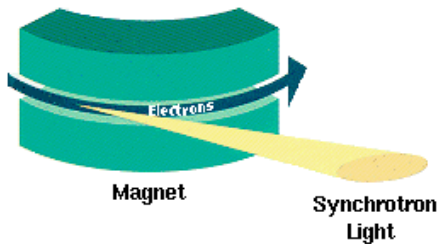
Optical method with Incoherent radiation

'Convert particles into visible
photons'

Optical Synchrotron Radiation



SR appears when a charged particle is bent in a magnetic field



$$P_{\gamma} = \frac{1}{6\pi\epsilon_0} \frac{q^2 c^3}{4\pi} \frac{1}{\rho^2 \gamma^3}$$

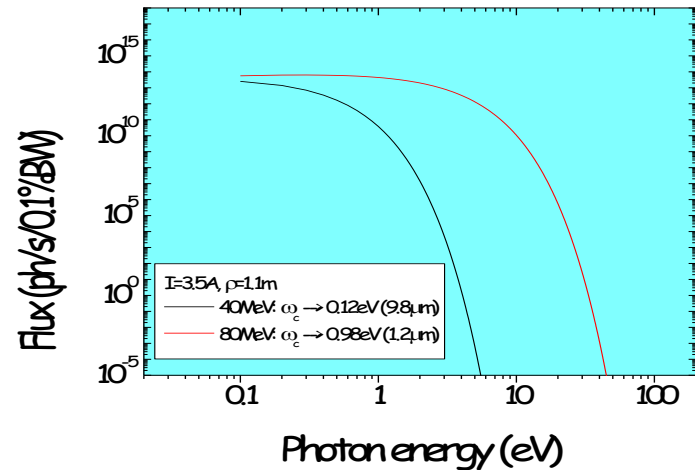
γ charged particle Lorentz-factor

ρ is the bending radius

Critical frequency:

$$\omega_c = \frac{3}{2} \frac{c}{\rho} \gamma^3$$

Beam energy $\rightarrow \gamma$ Beam curvature $\rightarrow \rho$



Limitations:

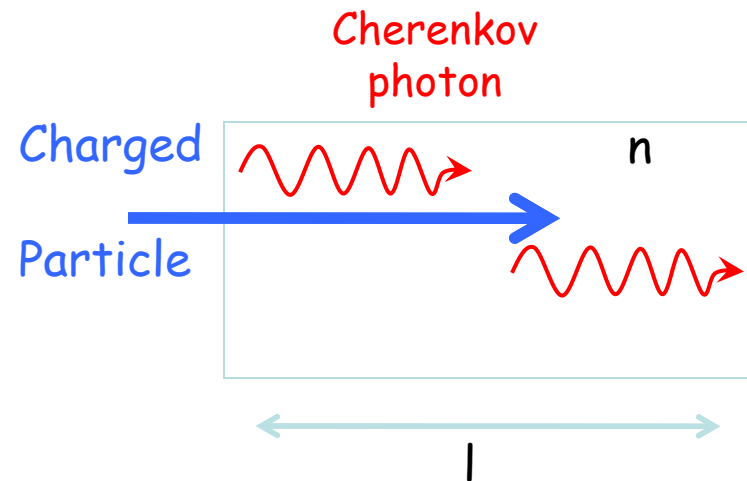
- Use a lot on electrons (for visible light: $E > 150$ MeV)
- Limited to very high energy proton or heavy ion beams

Cherenkov radiation



'Equivalent to the supersonic boom but for photons'

Threshold process: Particles go faster than light $\beta > 1/n$



- n is the index of refraction ($n > 1$)
- β is the relative particle velocity

- θ_c is the Cherenkov light emission angle

$$\cos(\theta_c) = \frac{1}{\beta n}$$

- l the length of the cherenkov radiator

The total number of photons proportional to the thickness of the Cherenkov radiator



Limitations :

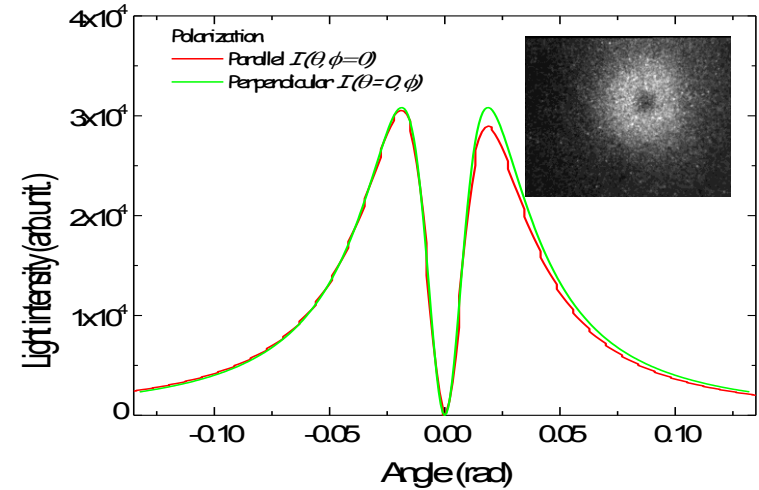
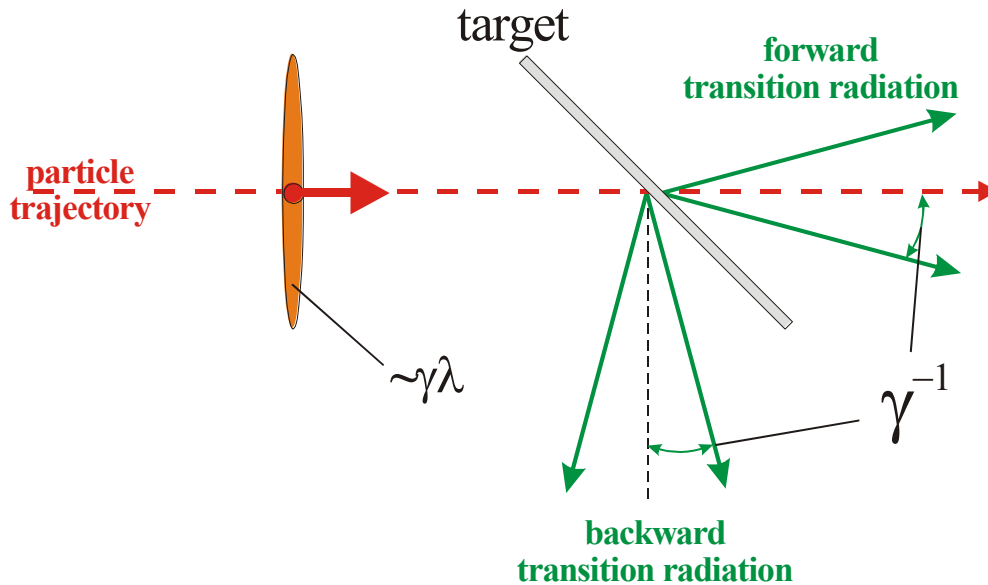
- Using transparent material (Glass $n=1.46$)
- Time resolution limited by the length of the radiator

$$\Delta t = l \left(\frac{n}{c} - \frac{1}{\beta c} \right)$$

Optical Transition Radiation



'TR is generated when a charged particle passes through the interface between two materials with different permittivity (screen in vacuum)'



Number of OTR photons per charge particle



$\sim 5 \cdot 10^{-3}$ in $[400-600]nm$

Radiation wavelength

Beam energy

Using good reflecting material

The thermal limit for 'best' screens (C, Be, SiC) is $\sim 1 \cdot 10^6$ nC/cm²

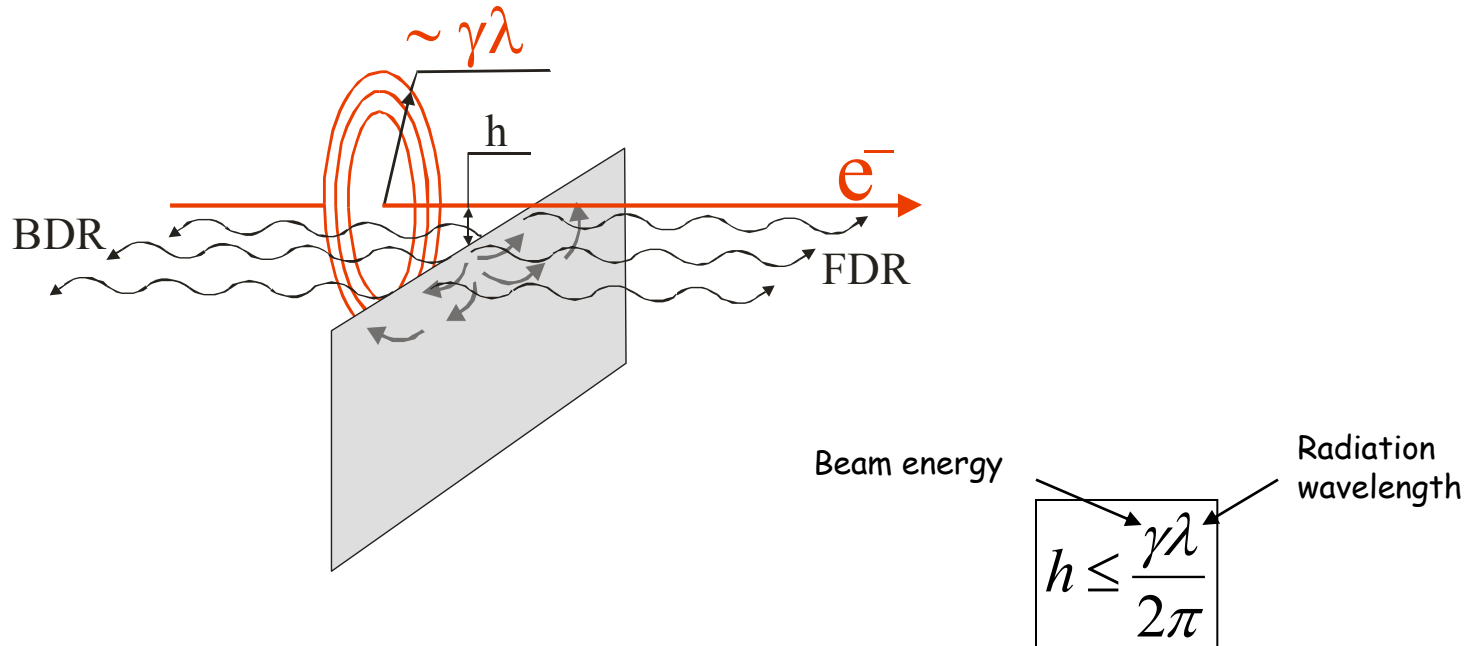
$$\Delta T(r) = \frac{dE}{dx} \frac{N_{tot}}{2\pi\sigma^2 c_p \rho} e^{-\frac{r^2}{2\sigma^2}}$$

M. Castellano and V. Verzilov, *Phys. Rev. ST-AB* 1, 062801 (1998)

Optical Diffraction Radiation



'DR is generated when a charged particle passes through an aperture or near an edge of dielectric materials, if the distance to the target h (impact parameter) satisfies the condition :

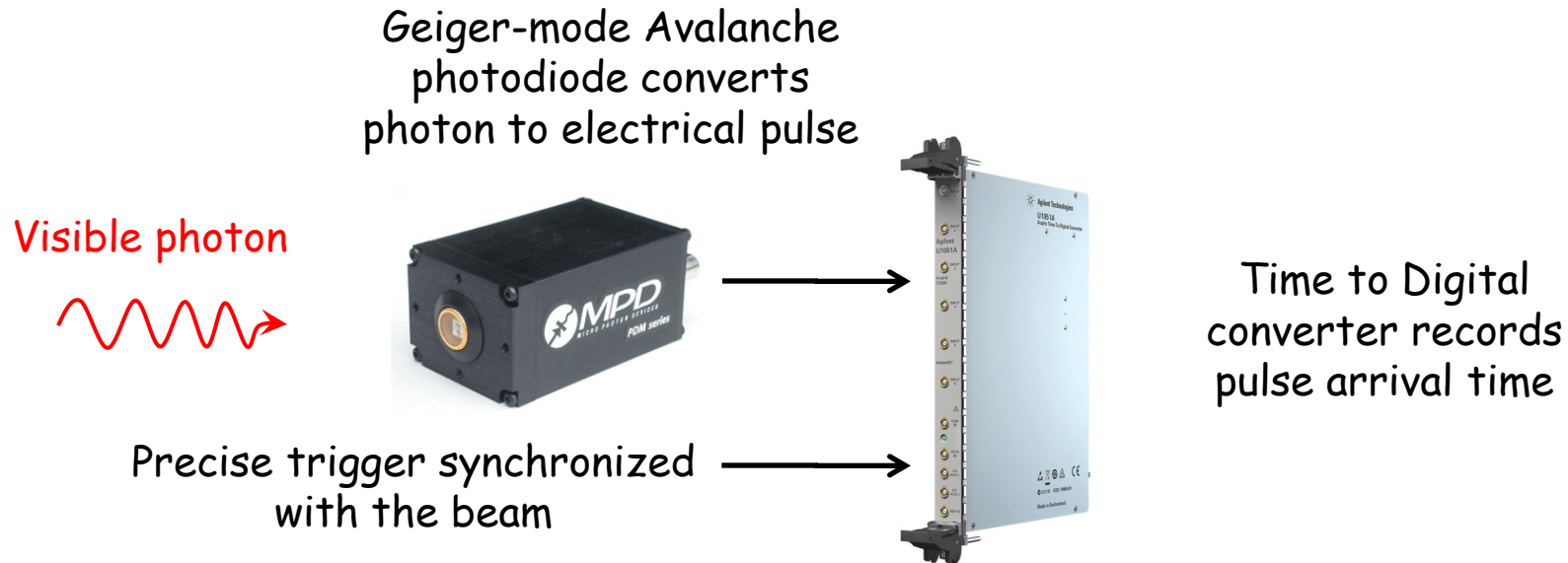


Limitations :

- Not enough photons in the visible for low energy particles : $E < 1 \text{ GeV}$ for a decent impact parameter ($100\mu\text{m}$)

T. Muto et al, Physical Review Letters 90 (2003) 104801

Time Correlated Single Photon Counting

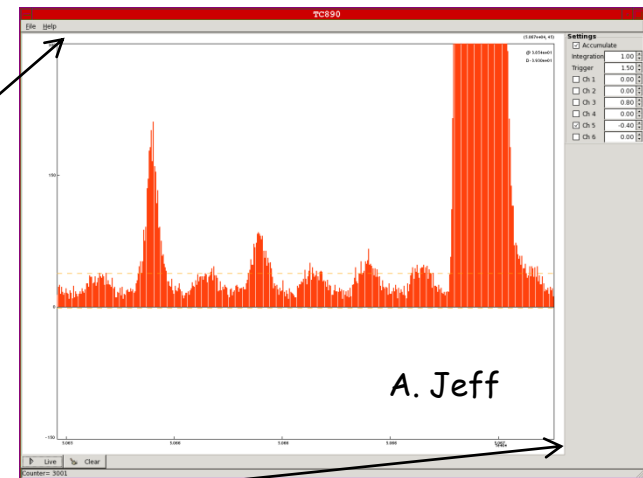
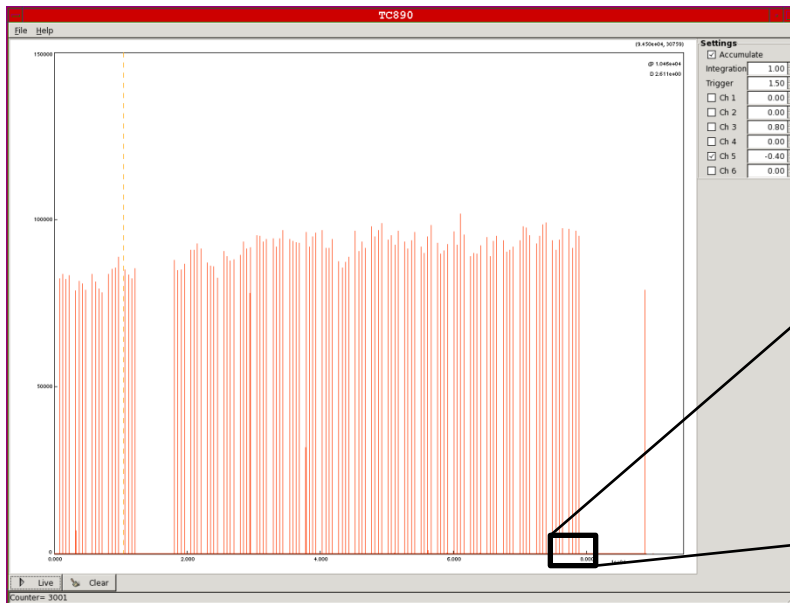


- Sampling Method allowing very high dynamic range if you measure long enough
- Avalanche photodiode have deadtime and are subject to afterpulsing
- State of the art TDC typically limited to 10ps sampling

D.V. O'Connor, D. Phillips, Time-correlated Single Photon Counting, Academic Press, London, 1984
C.A. Thomas et al., Nucl. Instr. and Meth. A566 (2006) p.762

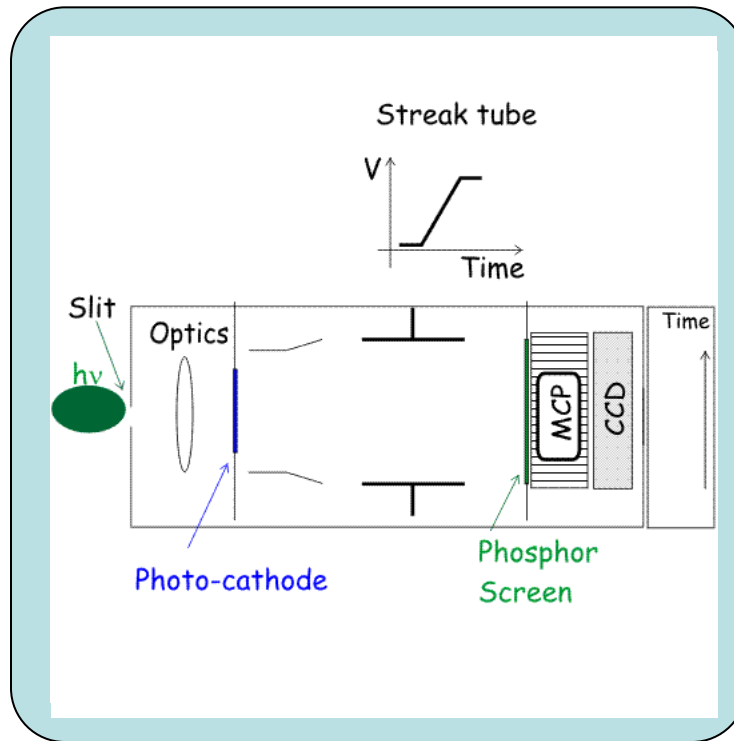
Time Correlated Single Photon Counting

Longitudinal profile of the entire LHC ring (89us)
with 50ps resolution using SR light



A very large dynamic range should make it possible to see ghost bunches as small as $5e5$ protons / 50ps with long integration

Streak Camera



'Streak cameras uses a time dependent deflecting electric field to convert time information in spatial information on a CCD'

Mitsuru Uesaka et al, NIMA 406 (1998) 371

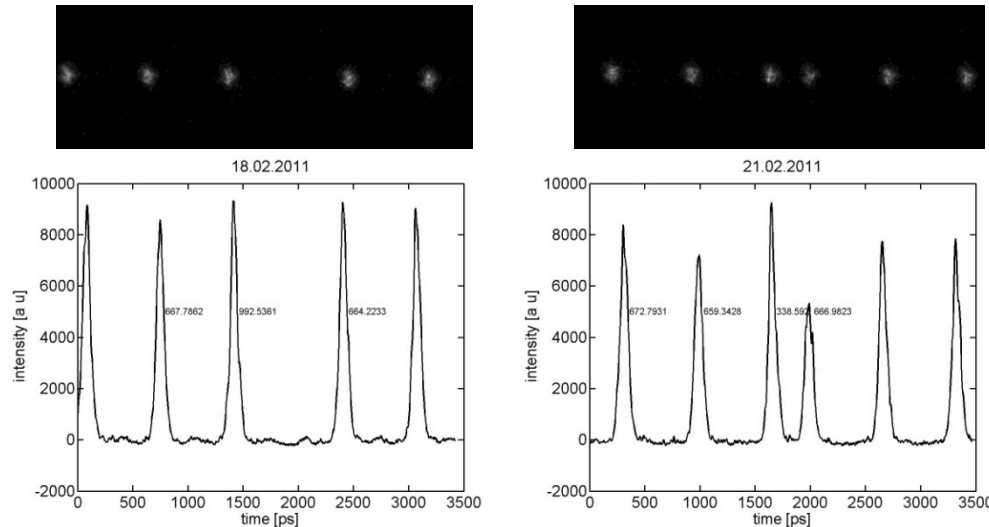
200fs time resolution obtained using reflective optics and 12.5nm bandwidth optical filter (800nm) and the Hamamatsu FESCA 200

Limitations : Time resolution of the streak camera :

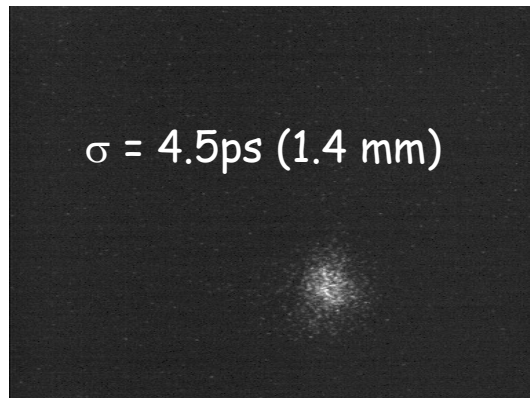
- (i) Initial velocity distribution of photoelectrons : *narrow bandwidth optical filter*
- (ii) Spatial spread of the slit image: *small slit width*
- (iii) Dispersion in the optics

Streak camera examples

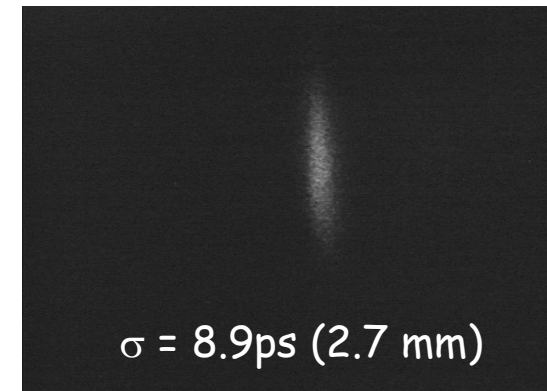
Observation of 5MeV electron bunch train using cherenkov
Sweep speed of 250ps/mm



Measure of bunch length using OTR and OSR



*Sweep
speed of
10ps/mm*



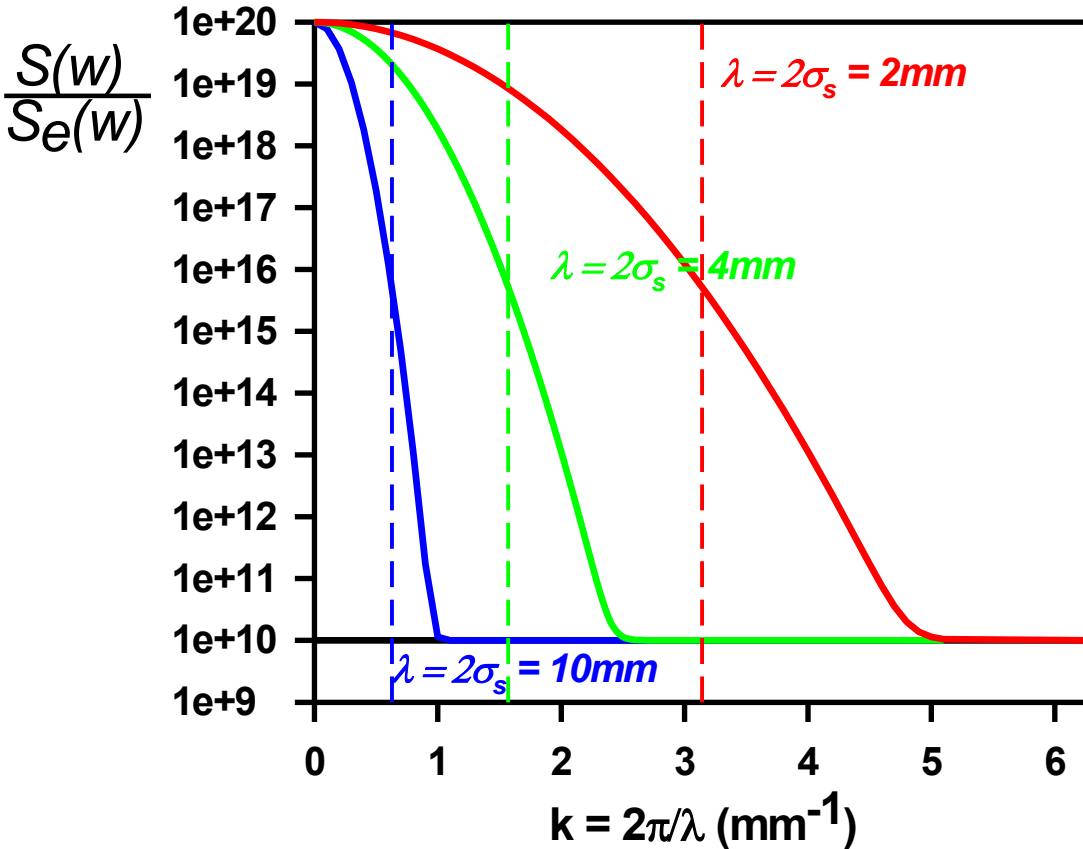
Bunch Length measurement with Coherent Radiation

'The shorter in time, The broader in frequency'

Bunch Form Factor for Gaussian distribution



Assume $N = 10^{10}$ e/bunch



Coherent radiation appears when the bunch length is comparable to or shorter than the emitted radiation wavelength

Measuring Radiation Spectrum

$$S(\omega) \approx N^2 S_p(\omega) F(\omega)$$

- ✓ $S(\omega)$ – radiation spectrum ((known in the experiment))
- ✓ N – number of electrons on the bunch (known from the experiment)
- ✓ $F(\omega)$ – bunch form factor (what you want to find out)
- ✓ $S_p(\omega)$ – single particle spectrum (should be known)



Coherent Transition Radiation (CTR)

P. Kung et al, *Physical review Letters* 73 (1994) 96



Coherent Diffraction (CDR) or Coherent Synchrotron (CSR)

B. Feng et al, *NIM A* 475 (2001) 492-497 ; A.H. Lumpkin et al, *NIM A* 475 (2001) 470-475 ; C. Castellano et al, *Physical Review E* 63 (2001) 056501

T. Watanabe et al, *NIM A* 437 (1999) 1-11 & *NIM A* 480 (2002) 315-327

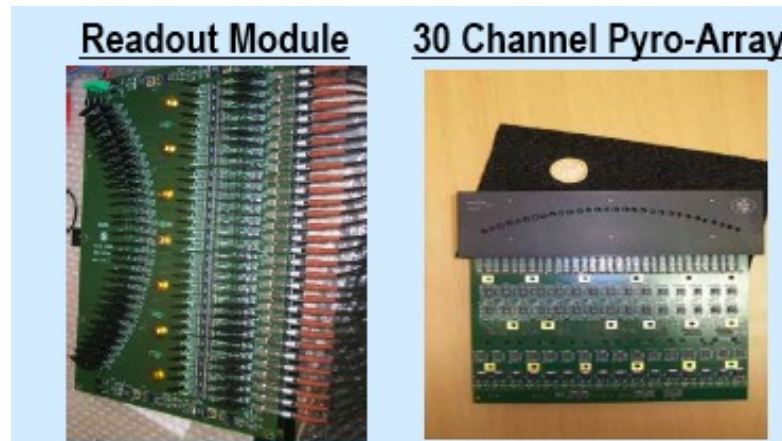
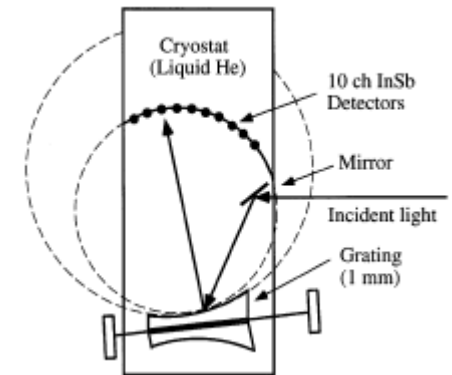
Bunch Frequency Spectrum by Coherent Radiation

1

'The polychromator enables to get the spectrum directly by a single shot. The radiation is deflected by a grating and resolved by a multi-channels detector array'

T. Wanatabe et al., NIM-A 480 (2002) 315-327

H. Delsim-Hashemiet al., Proc. FLS, Hamburg 2006, WG512



B. Schmidt, DESY

Bunch Frequency Spectrum by Coherent Radiation

Frequency Domain

Spectral Intensity
 $A(\omega)$

Extrapolation
(high and low frequencies)

Correction

(transfer function of detection system)

Long Form Factor
 $|F(\omega)|$

Inverse Fourier Transform for
symmetric bunch distribution

Long. Bunch profile
 $S(z)$

Kramers-Kronig relation
for non symmetric bunches

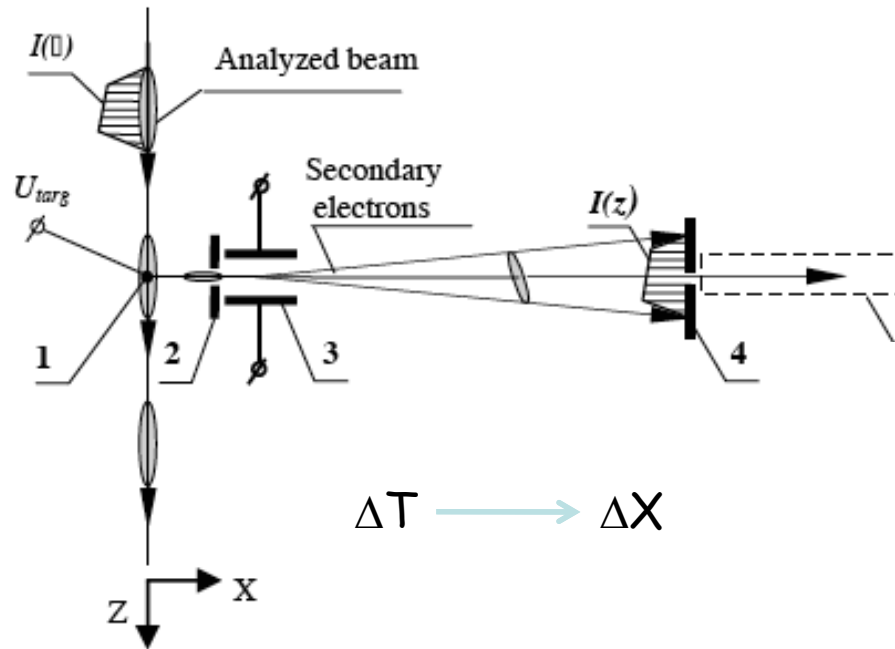
Time Domain

R. Lai and A.J. Sievers, NIM-A 397 (1997) 221 -231

RF techniques

'Transforming time information into
spatial information'

Bunch Shape Monitor - Feschenko monitor



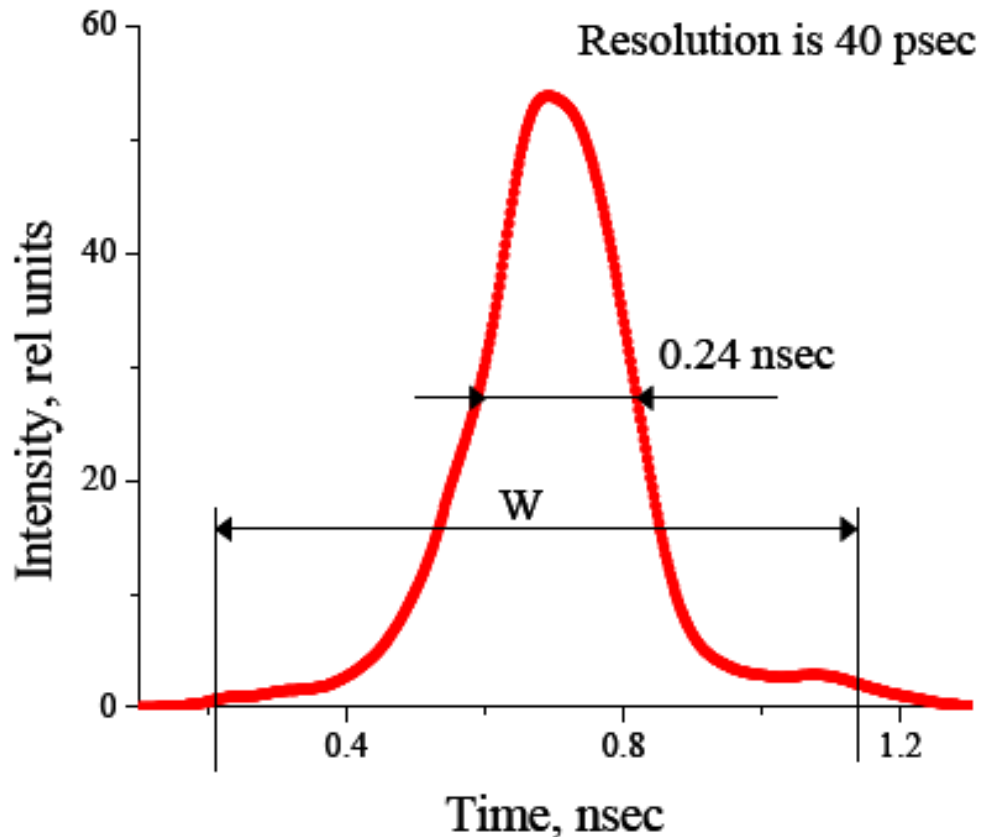
- 1 - Target (wire, screen, laser for H^-) : Source of secondary electrons
- 2 - Input collimator
- 3 - RF deflector (100MHz, 10kV) combined with electrostatic lens
- 4 - Electron Beam detector (electron multiplier, ..)



1

Bunch Shape monitor - Feschenko monitor

Longitudinal Bunch profile @ SNS

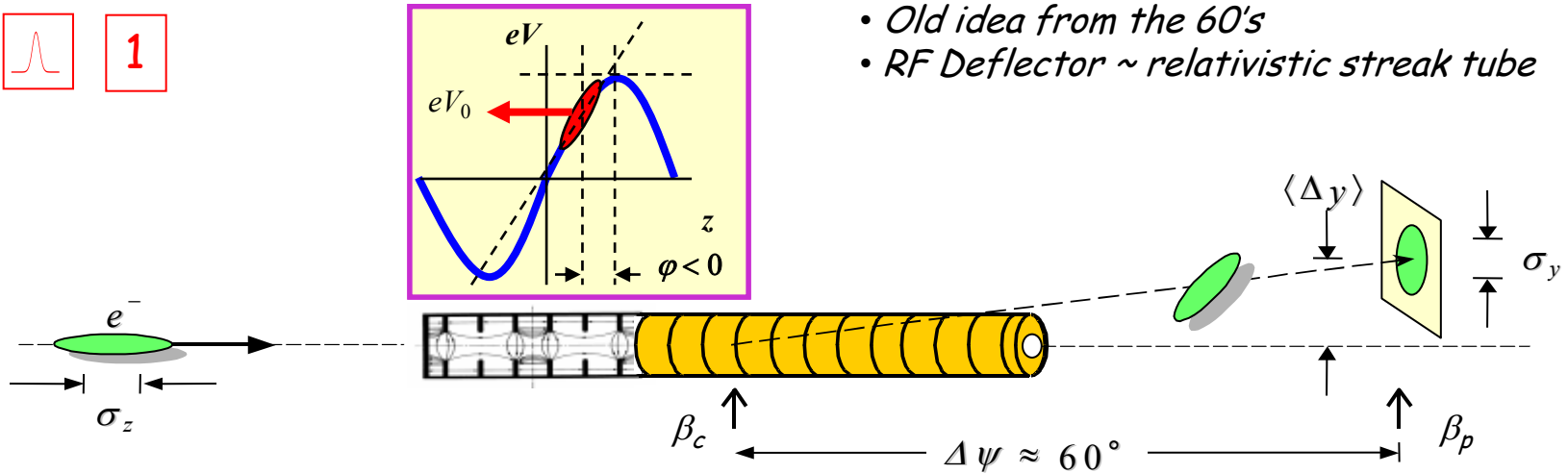


A. Feschenko *et al*, Proceedings of LINAC 2004, Lübeck, p408

RF Deflecting Cavity



1



- Old idea from the 60's
- RF Deflector ~ relativistic streak tube

Beam profile RF on

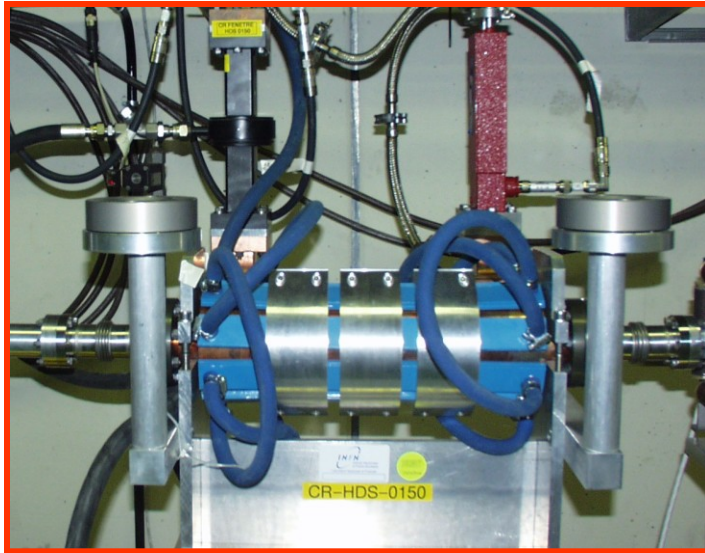
$$\sigma_y = \sqrt{\sigma_{y_0}^2 + \sigma_z^2 \beta_c \beta_p \left(\frac{2\pi eV_0}{\lambda E_0} \sin(\Delta\Psi) \cos(\varphi) \right)^2}$$

Beam profile RF off (points to $\sigma_{y_0}^2$)
 Deflecting Voltage (points to eV_0)
 Bunch length (points to σ_z)
 Beta function at cavity and profile monitor (points to $\beta_c \beta_p$)
 RF deflector wavelength (points to λ)
 Beam energy (points to E_0)
 Betatron phase advance (cavity-profile monitor) (points to $\sin(\Delta\Psi) \cos(\varphi)$)

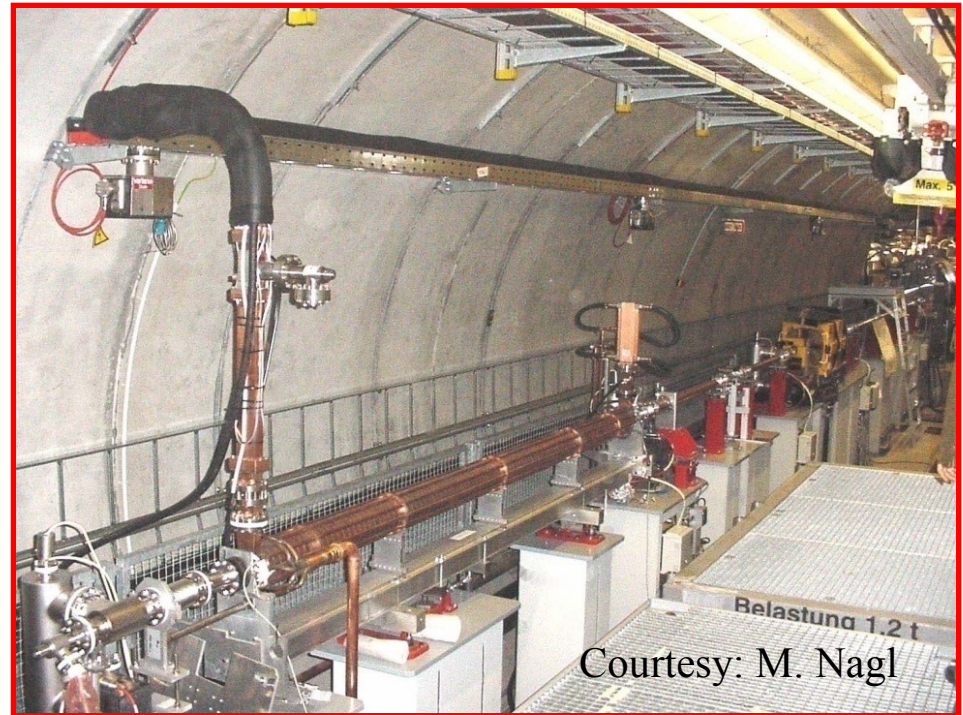
$\sin\Delta\Psi = 1, \beta_p$ small
Make β_c large

RF Deflecting Cavity

CTF3



LOLA @ Flash

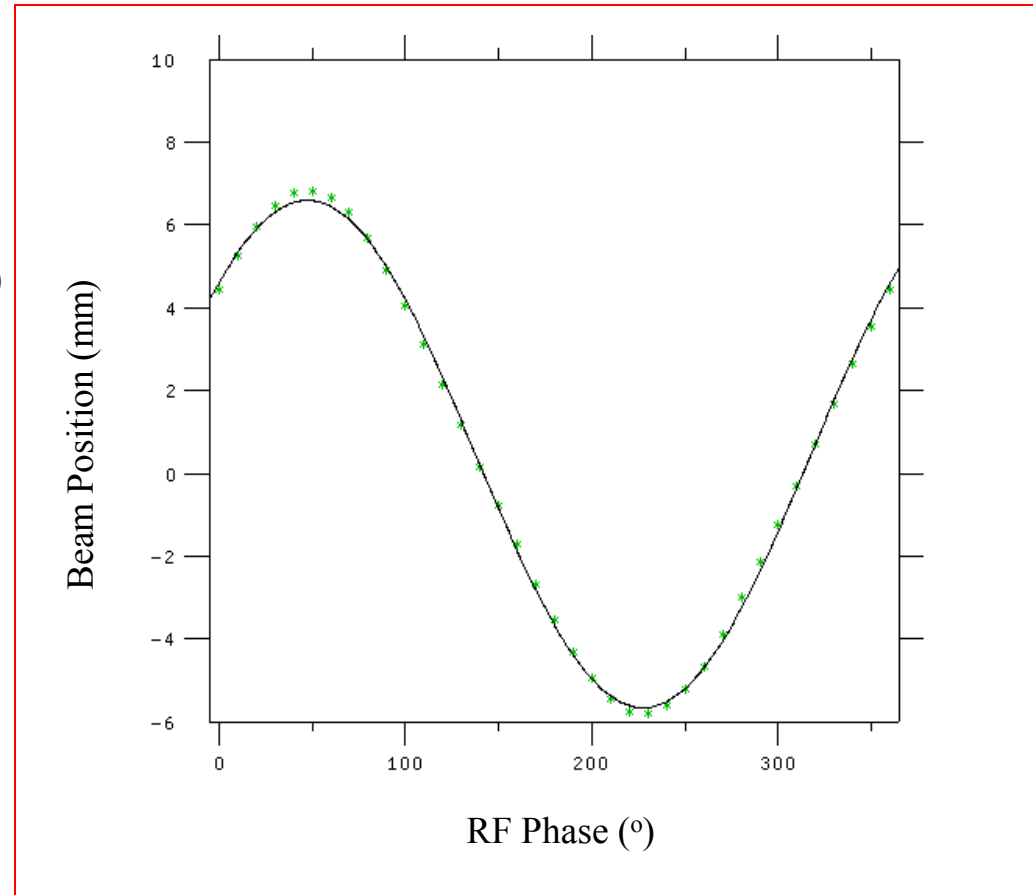


RF Deflecting Cavity

Calibration of RF Deflector

$$\Delta X(\text{mm}) \longrightarrow \begin{matrix} \Delta\varphi(^{\circ}) \\ \Delta T(\text{ps}) \end{matrix}$$

Monitor the Beam Position on (or close to) the Profile monitor to calibrate the deflection angle

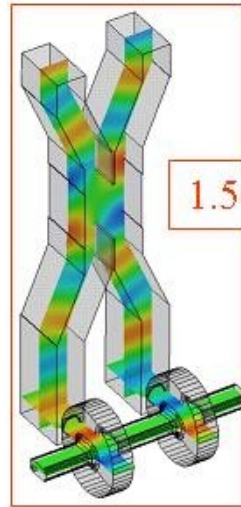


Beam offset on the screen

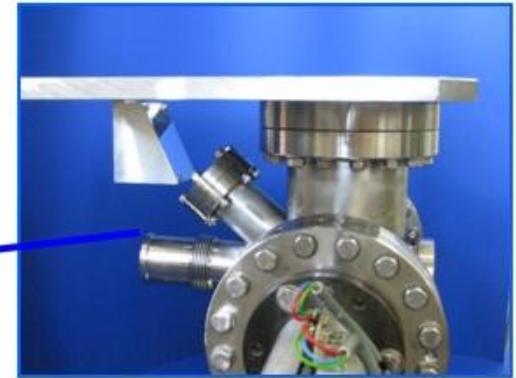
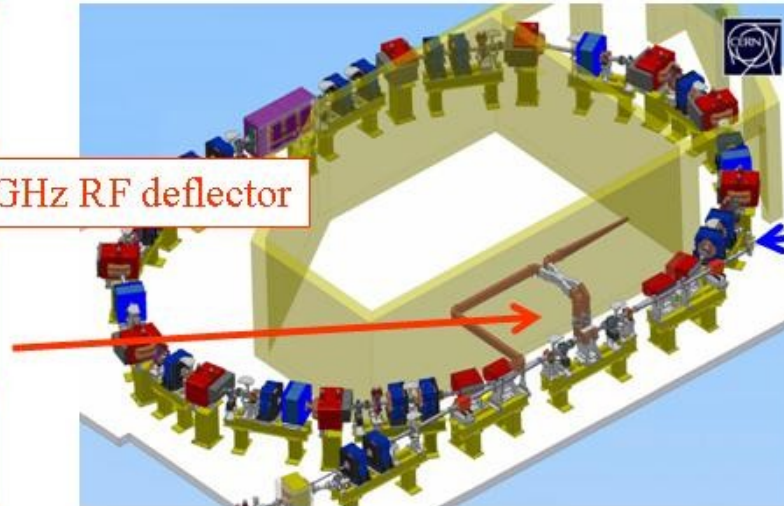
$$\Delta y(z) \approx \frac{eV_0}{E_0} \cdot \sqrt{\beta_c \beta_p} \sin(\Delta\Psi) \left(\frac{2\pi}{\lambda} - z \cos(\varphi) + \sin(\varphi) \right)$$

RF deflector phase

RF by Deflecting Cavity



1.5GHz RF deflector



OTR screen

RF deflector off

$$\sigma_{\text{noRF}} = 0.35\text{mm}$$

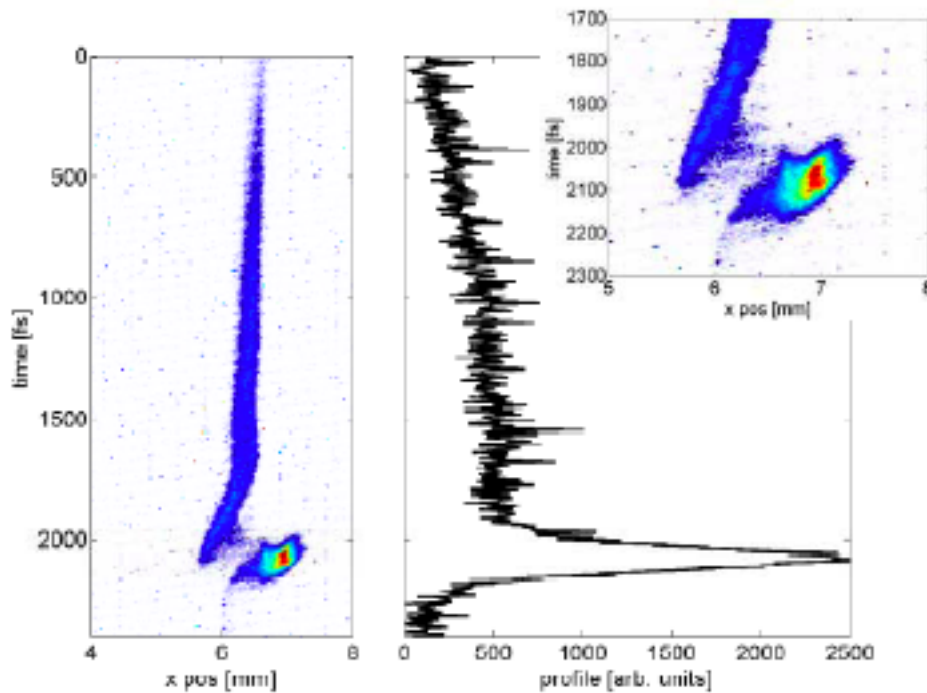
$$\sigma_z = 2\text{ps}$$

RF deflector on : 0 Xing

$$\sigma_{0\text{Xing}} = 2.9\text{mm}$$

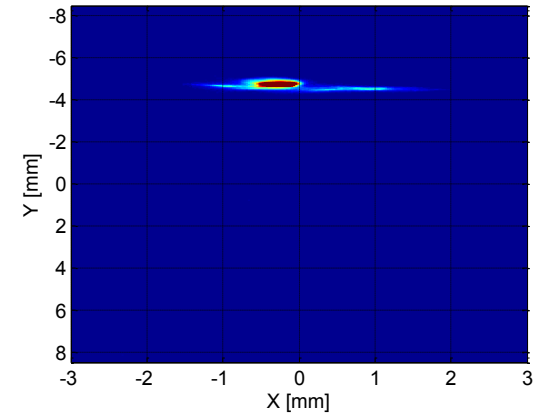
RF by Deflecting Cavity

Bunch length measurement @ Flash

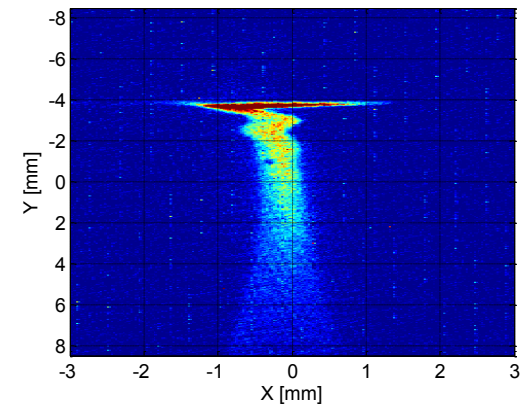


→ Resolution of 4fs/pixels

LOLA off:



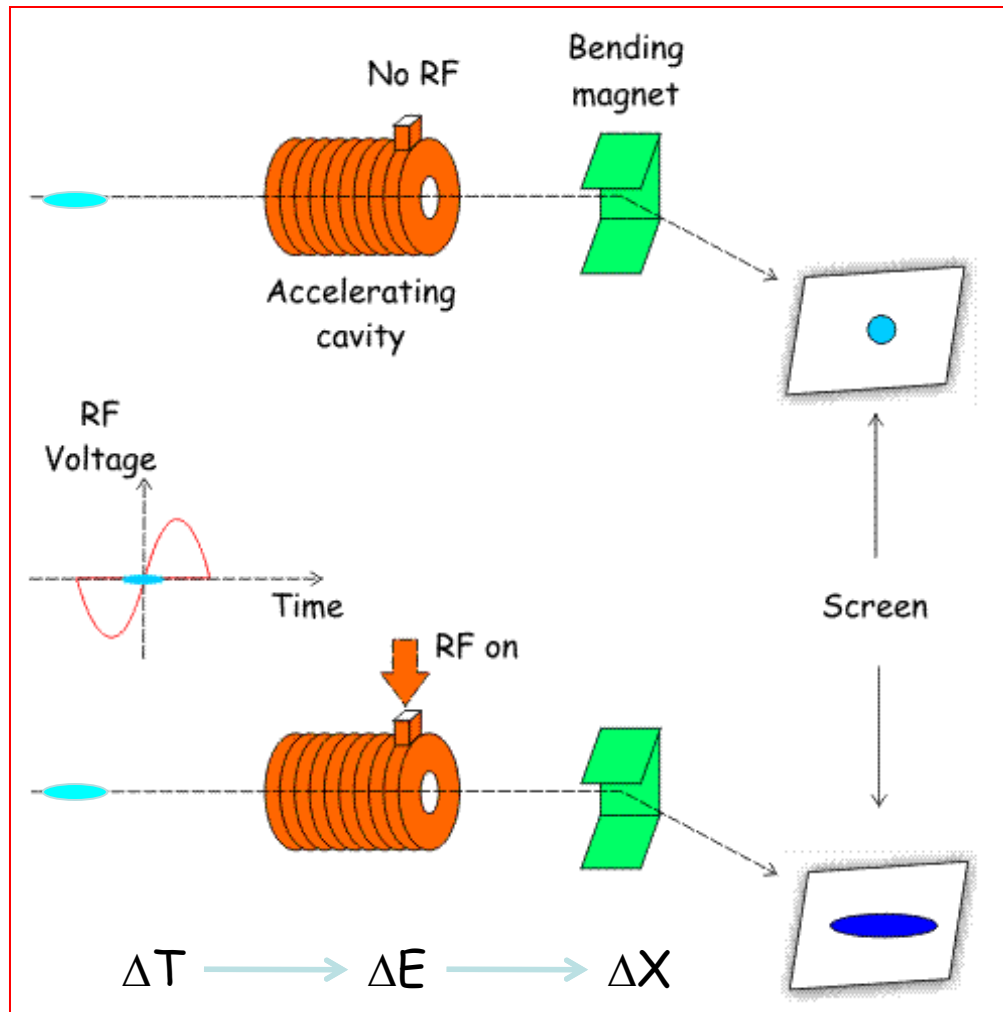
LOLA on:



M. Hüning *et al*, Proceeding of the 27th FEL conference, Stanford, 2005, pp538

RF accelerating structures

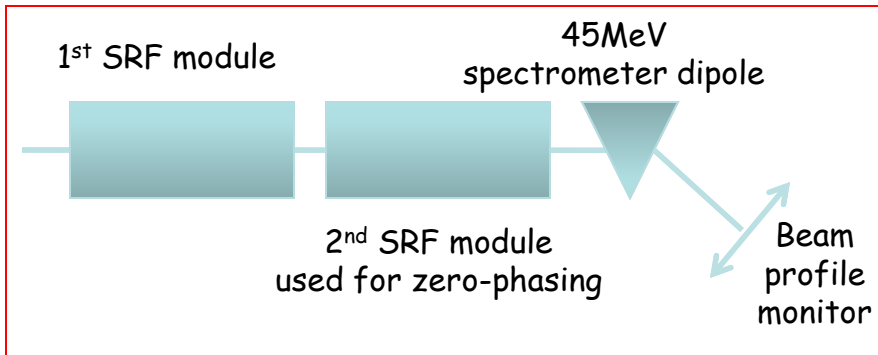
'The electron energy is modulated by the zero-phasing RF accelerating field and the bunch distribution is deduced from the energy dispersion measured downstream using a spectrometer line'



1

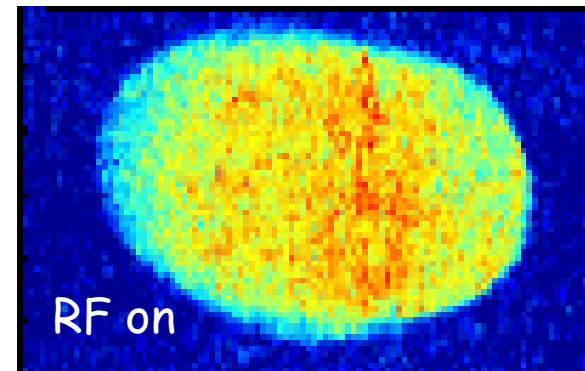
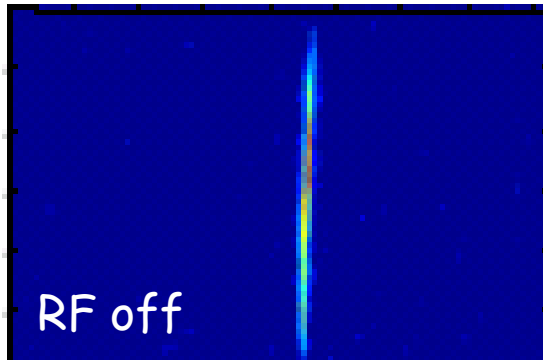
RF accelerating structures

CEBAF injector, Newport News



D. X. Wang *et al*, Physical Review E57 (1998) 2283

84fs, 45MeV beam but low charge beam



Limitations

RF non linearities
Beam loading and wakefield for high charge beam

Laser based techniques

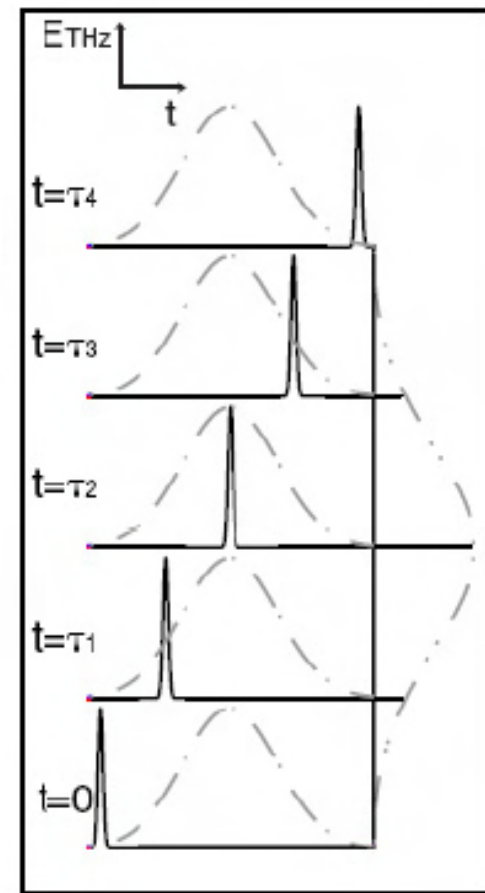
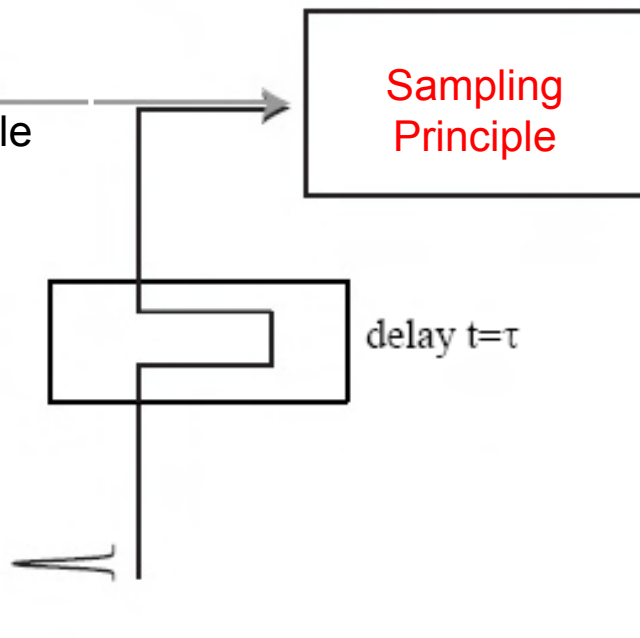
Sampling Techniques

Using a short laser pulse to scan through the beam profile

Longitudinal

Beam profile

probe pulse

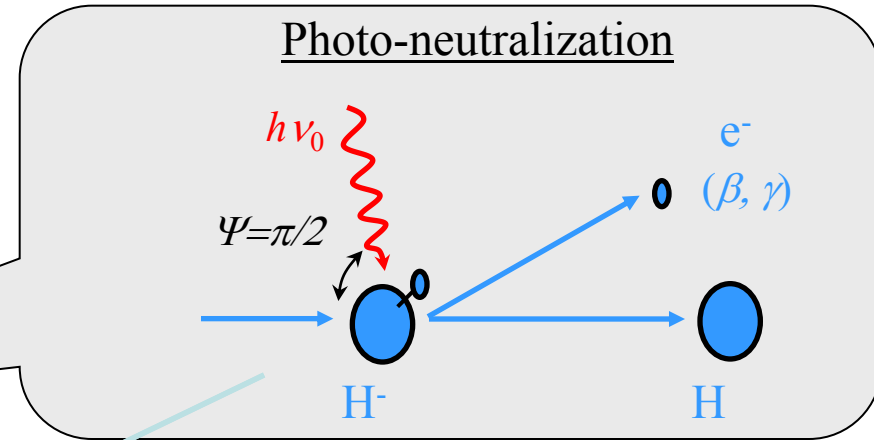
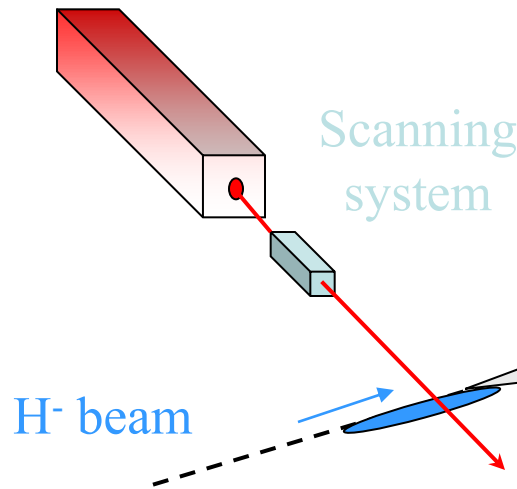


Limitation

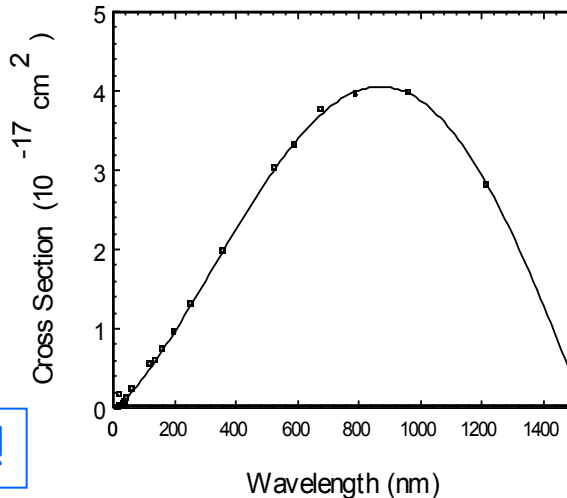
Laser-beam synchronization jitter (50fs)

Laser Wire Scanner : Photo-neutralization

High power laser



- First ionization potential for H^- ions is 0.75eV
- Photo-neutralization cross section : $\sigma \sim 4 \cdot 10^{-17} \text{ cm}^2$



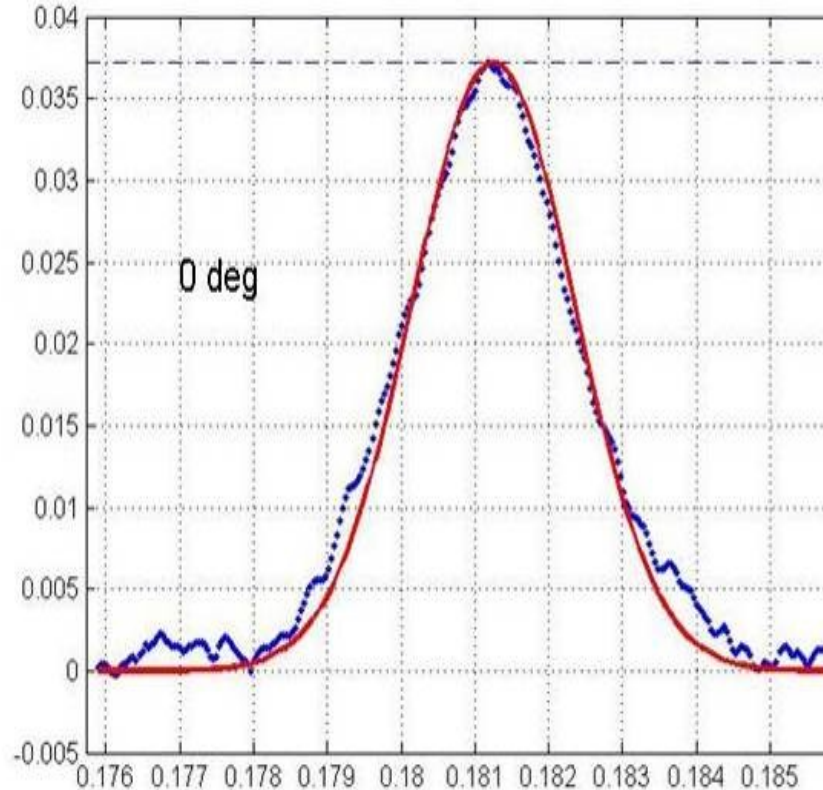
- Detection system based on**
- The measurement of released electrons using a magnet and a collector (faraday cup, MCP,..)
 - Measured the conversion of H^- into H with a current monitor



Laser Wire Scanner : Photo-neutralization

Mode Locked Laser Longitudinal Measurements @ SNS

2.5 MeV H^- , 402.5 MHz bunching freq, Ti-Sapphire laser phase-locked @ $1/5^{\text{th}}$ bunching frequency



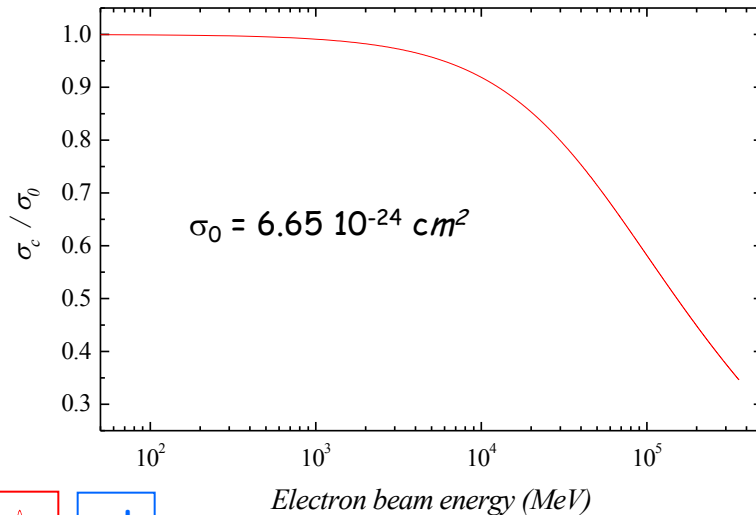
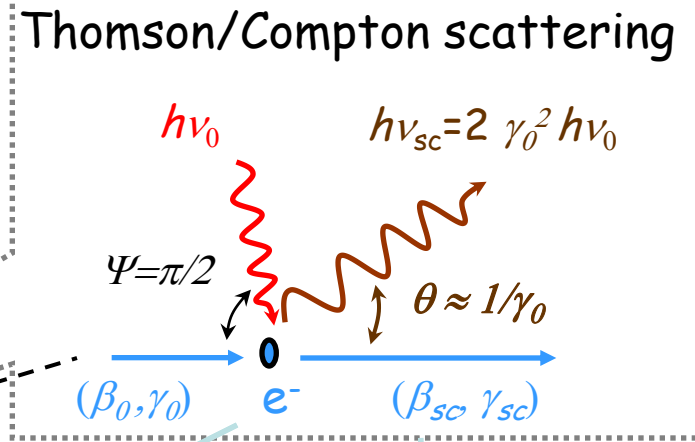
Collected electron signal plotted vs. phase

Laser Wire Scanner - Compton scattering

High power laser

Scanning system

e^- beam



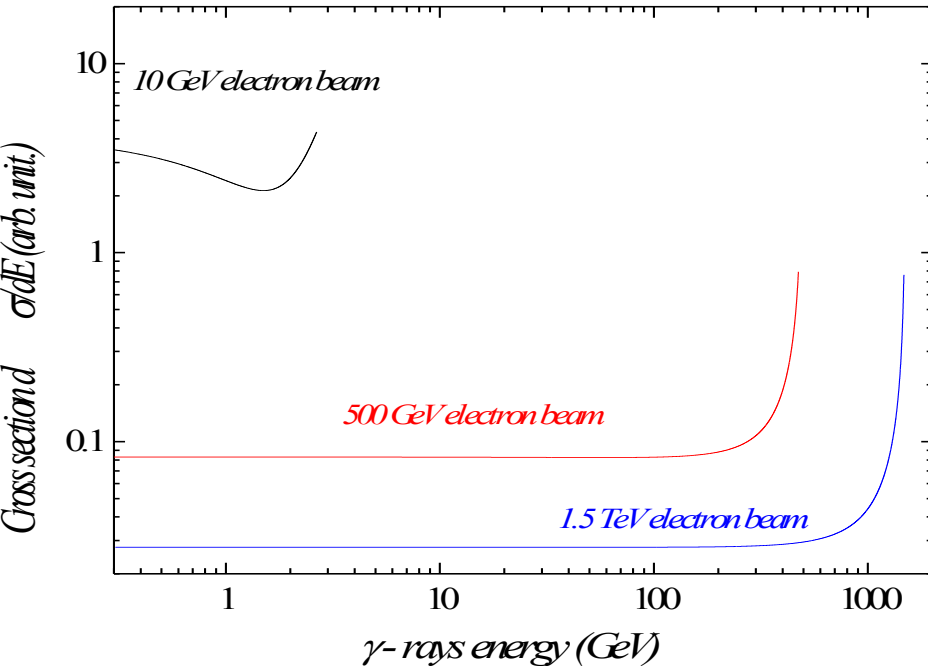
- Detection system based on**
- The measurement of the scattered photons
 - The measurement of degraded electrons



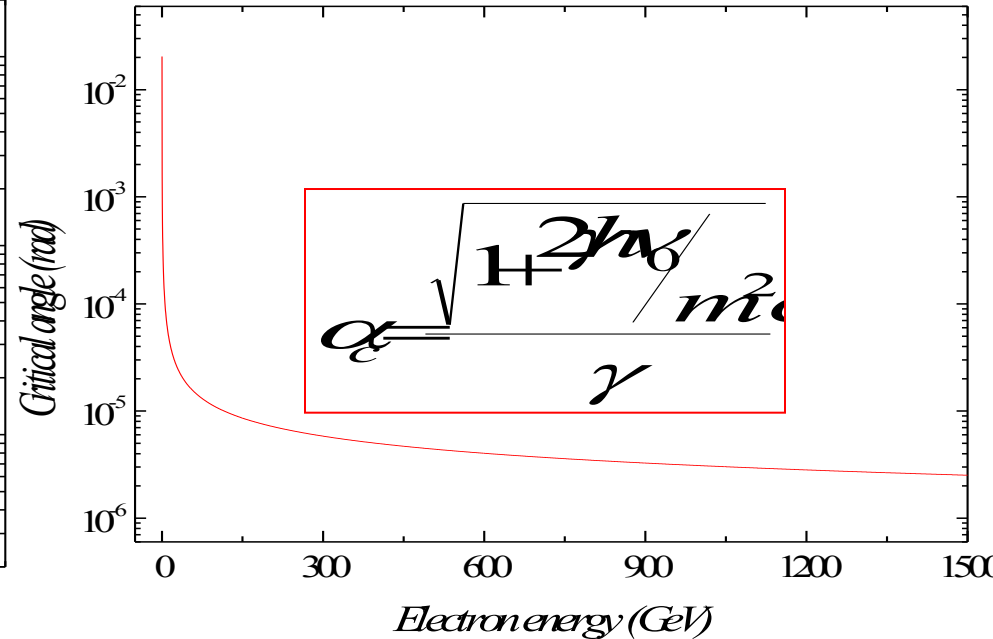
Laser Wire Scanner - Compton scattering

Energy spectrum of scattered photons

Using a 266nm wavelength laser



Emission angle of the scattered photons

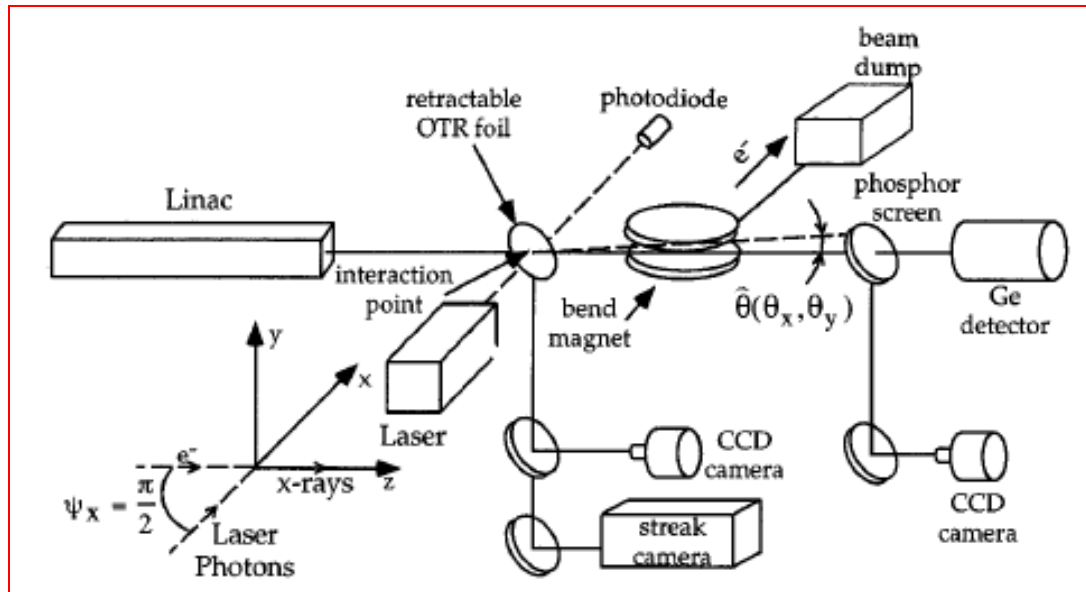


At very high energy

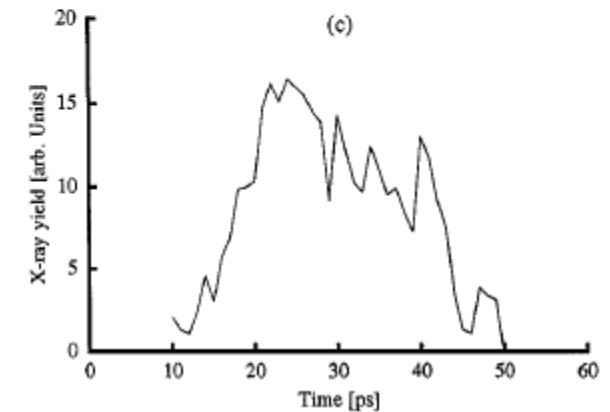
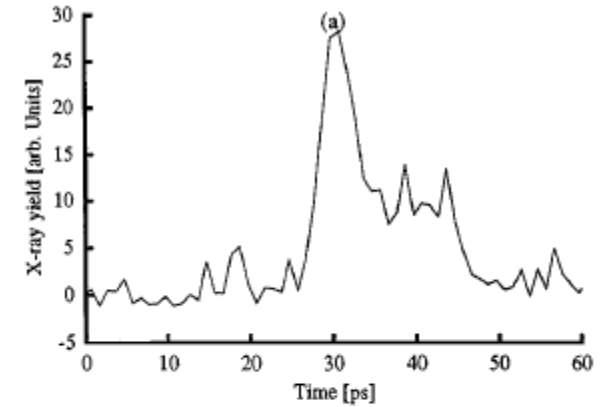
- The photons steal most of the electron energy (*electron recoil becomes extremely important*)
- The photons are emitted within a very small angle (a few μrad) in the forward direction
 - Measurement of degraded electrons only feasible at high energies

Laser Wire Scanner - Compton scattering

ALS @ LBNL

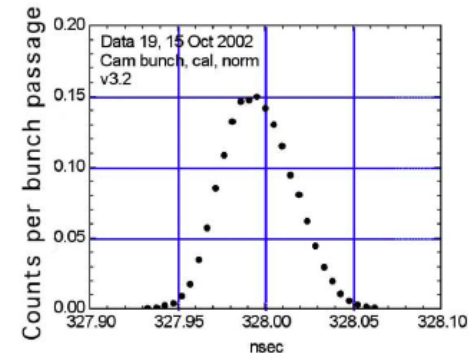
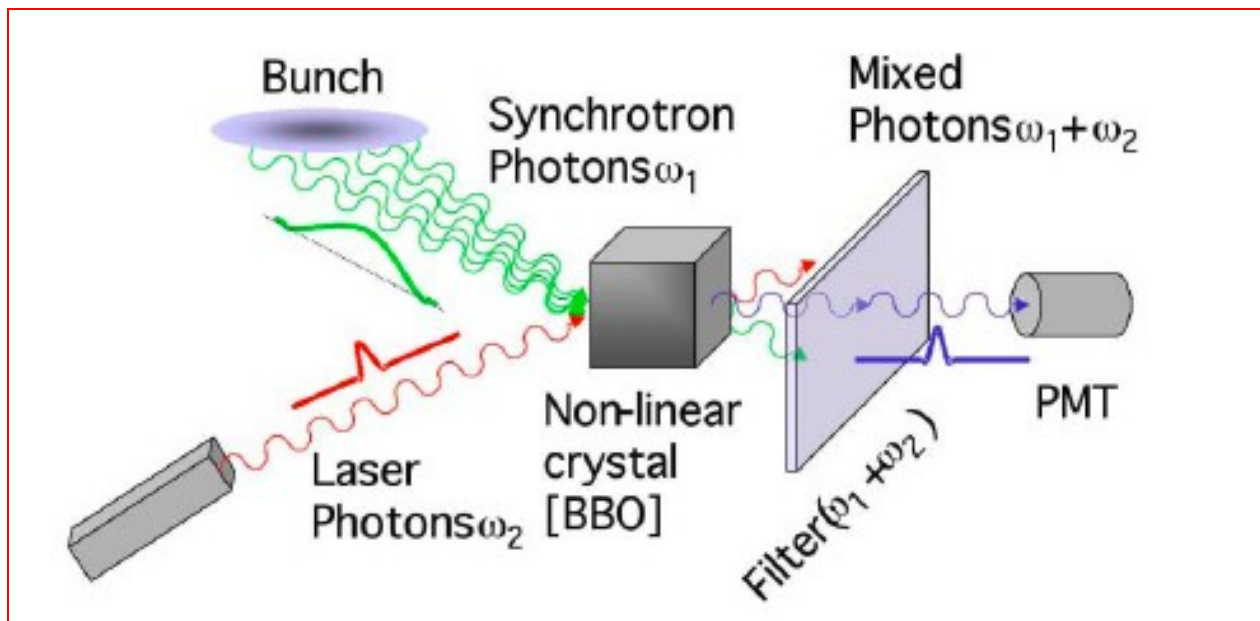


Using a 10TW Ti:Al₂O₃ laser system. Detecting 5.10⁴ 10-40 keV X-rays using either an X-ray CCD and Ge detector



Non linear mixing

'Non linear mixing uses beam induced radiation, which is mixed with a short laser pulse in a doubling non linear crystal (BBO,..). The resulting up frequency converted photons are then isolated and measured'



M. Zolotorev *et al*, *Proceeding of the PAC 2003*, pp.2530

15-30ps electron bunches (ALS, LBNL) scanned by a 50fs Ti:Al₂O₃ laser

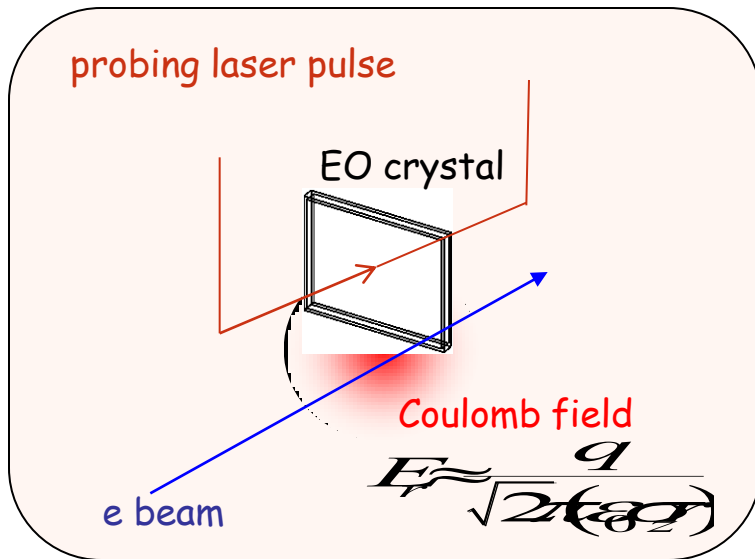


n!

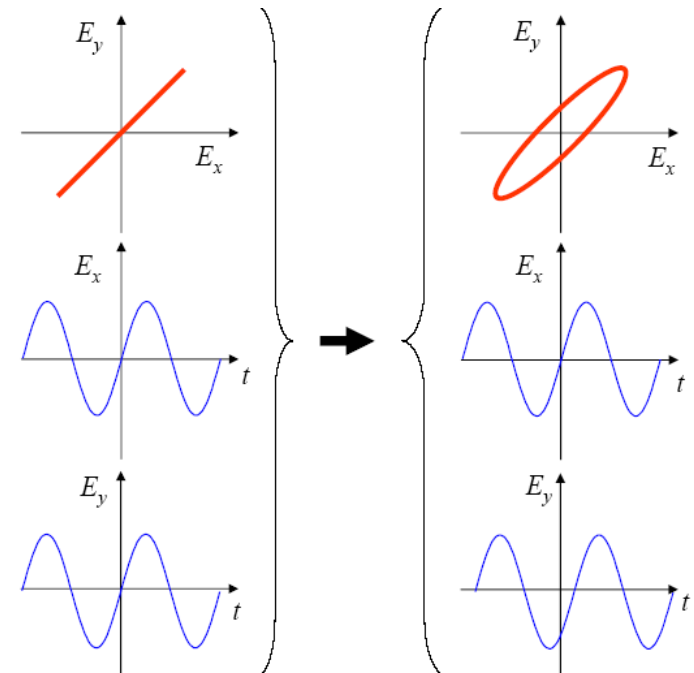
Electro Optic Sampling

'This method is based on the polarization change of a laser beam which passes through a crystal itself polarized by the electrons electric field'

E-field induced birefringence in EO-crystal : Pockels effect

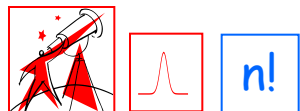


- Polarization diagram
- electric field of the horizontal polarization
- electric field of the vertical polarization



$$\Gamma = \frac{2\pi d}{\lambda_0} (n_x - n_y) = \frac{2\pi d}{\lambda_0} n_0^3 r_{41} E_r$$

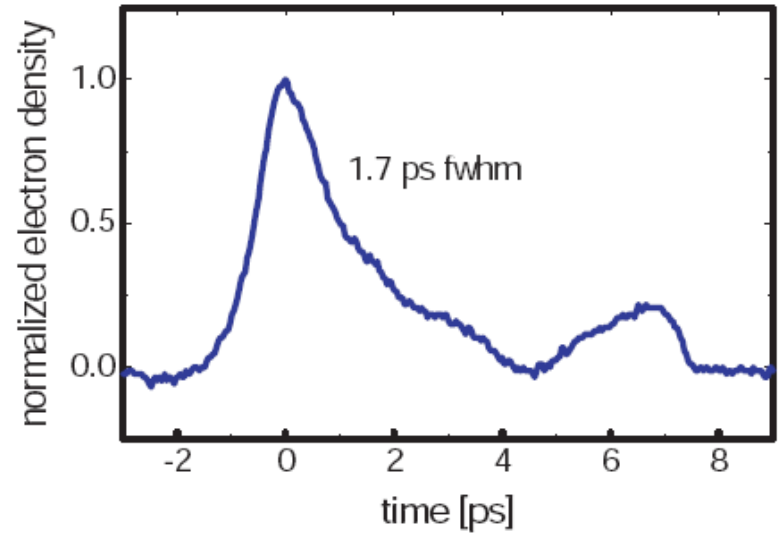
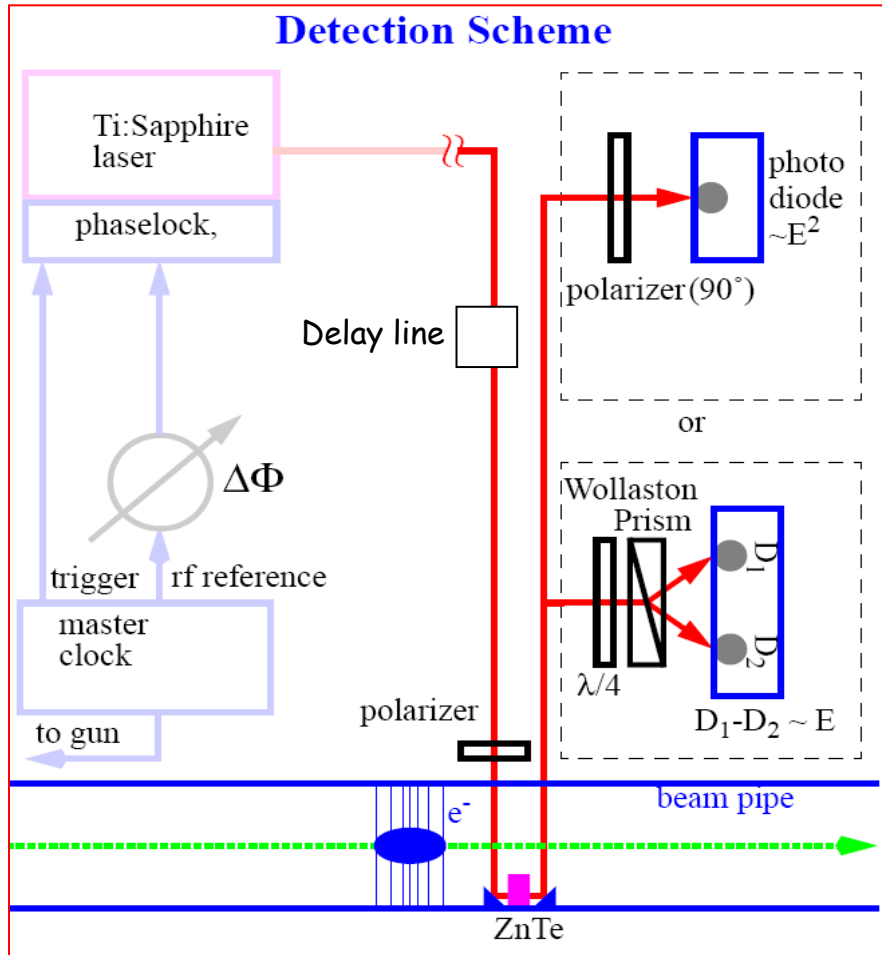
Relative phase shift between polarizations increases with the beam electric field



Electro Optic Sampling

EOS @ FELIX

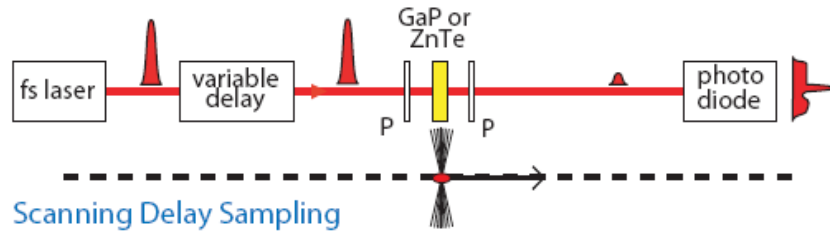
Detection Scheme



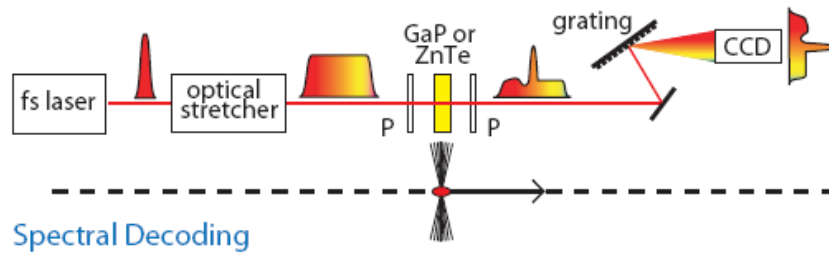
Using 12fs Ti:Al₂O₃ laser at 800nm and ZnTe crystal 0.5mm thick and a beam of 46MeV, 200pC, 2ps.

X. Yan *et al*, PRL 85, 3404 (2000)

Electro Optic based bunch length monitors

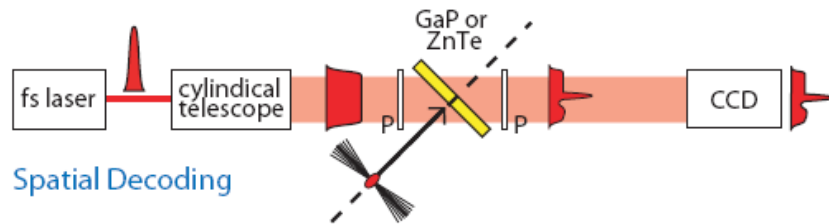


1. Sampling:
 - multi-shot method
 - arbitrary time window possible



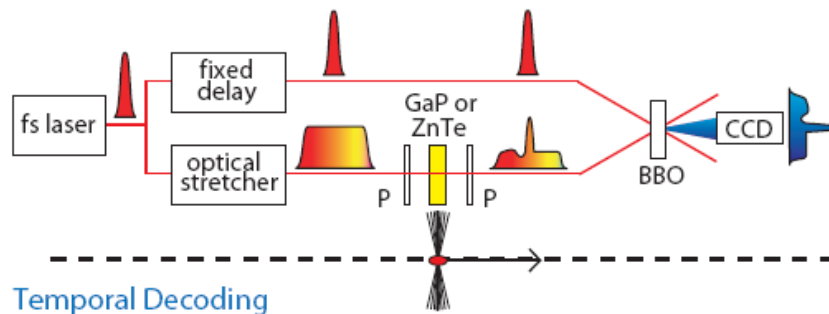
2. Chirp laser method, spectral encoding
 - laser bandwidth limited ~ 250 fs

Wilke *et al.*, PRL 88 (2002) 124801



3. Spatial encoding:
 - imaging limitation ~ 30 – 50 fs

Cavalieri *et al.*, PRL 94 (2005) 114801
 Jamison *et al.*, Opt. Lett. 28 (2003) 1710
 Van Tilborg *et al.*, Opt. Lett. 32 (2007) 313






4. Temporal encoding:
 - laser pulse length limited ~ 30 fs

Berden *et al.*, PRL 93 (2004) 114802

1

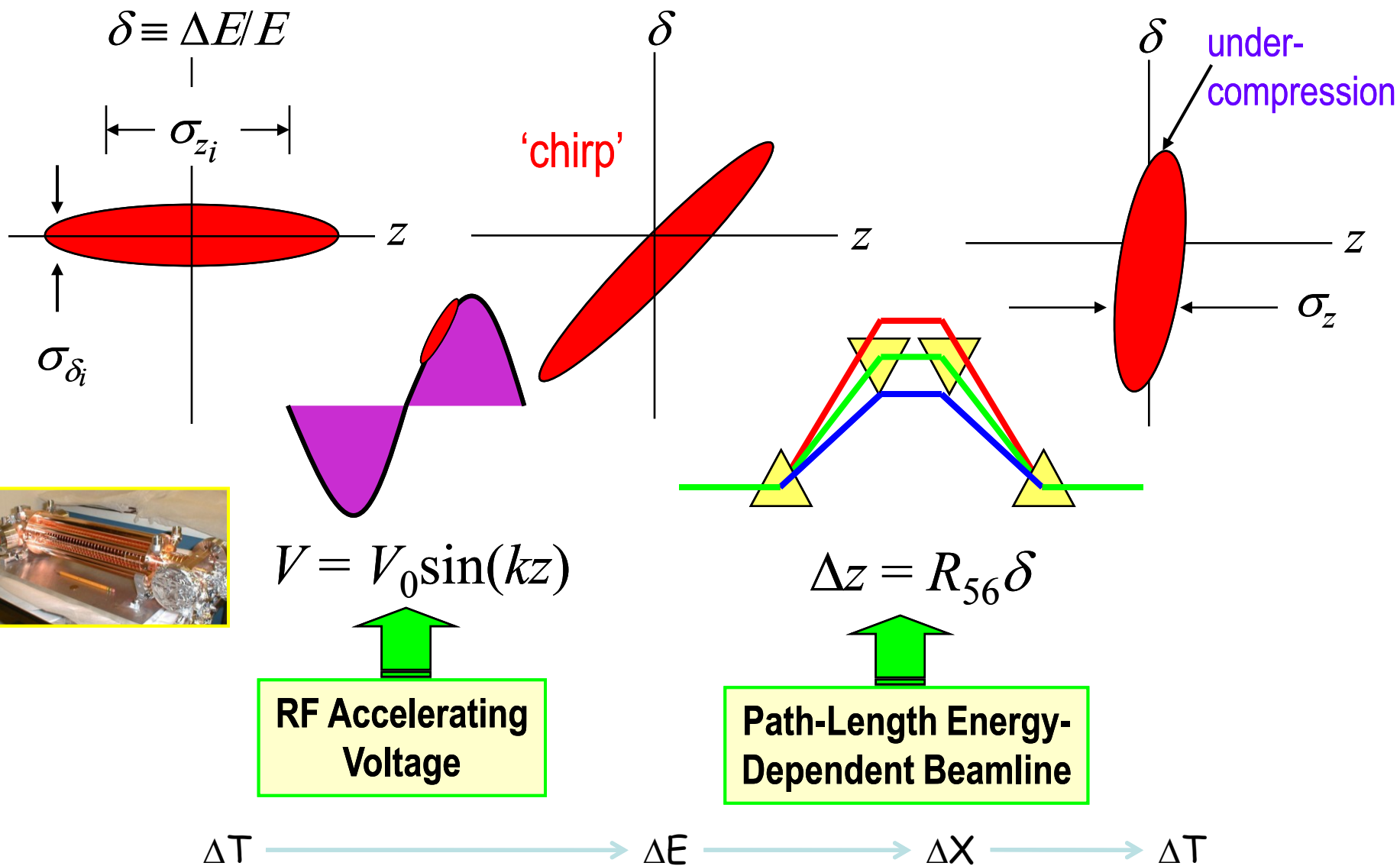
Summary

				σ	1	n!	Limitations
• Optical radiation							
• Cherenkov / OTR radiation	X						
• ODR / OSR Radiation	X						
• TCSPC			X				10ps
• Streak camera			X				200fs
• Coherent radiation : Bunch spectrum							
• Interferometry			X		X		
• Polychromator			X		X		
• RF techniques							
• 'Feschenko' monitor	X		X		X		Hadron, 20ps
• RF Deflector	X		X		X		10fs
• Zero phasing techniques	X		X		X		10fs
• Laser based Method							
• Sampling					X		Jitter (50fs)
• Non linear mixing			X				
• Thomson/Compton scattering	X		X				Electron
• Photo-neutralization	X		X				H ⁻
• Electro-Optic Sampling	X		X				
• E-O Spectral decoding	X		X		X		~ 200fs
• E-O Spatial decoding	X		X		X		~ 50fs
• E-O Temporal decoding	X		X		X		~ 50fs

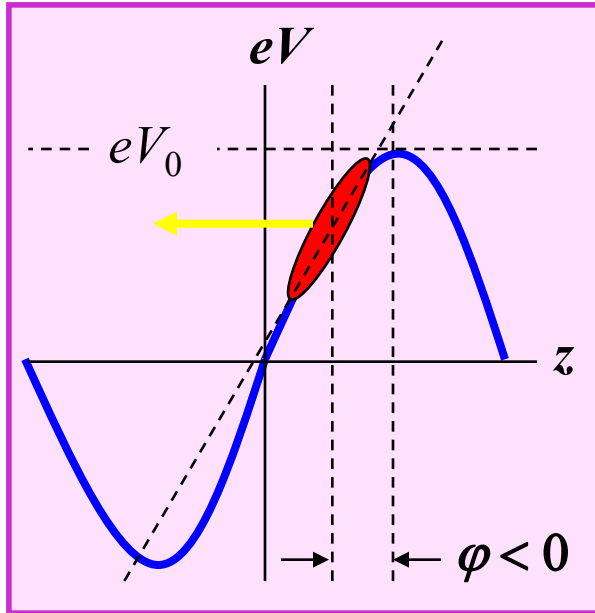
Bunch length manipulation

- Magnetic Compression
- Ballistic Compression

Short bunches by Magnetic Compression



Short bunches by Magnetic Compression



$$E(z) = E_0 + eV_0 \cos(\varphi + 2\pi z/\lambda)$$

$$\delta \equiv \frac{\Delta E}{E} \approx \dots$$

$$\delta_0 \frac{E_0}{E} + \left(1 - \frac{E_0}{E}\right) \left[\frac{\cos(\varphi + \Delta\varphi) - (2\pi z/\lambda) \sin(\varphi + \Delta\varphi)}{\cos(\varphi)} - 1 \right]$$

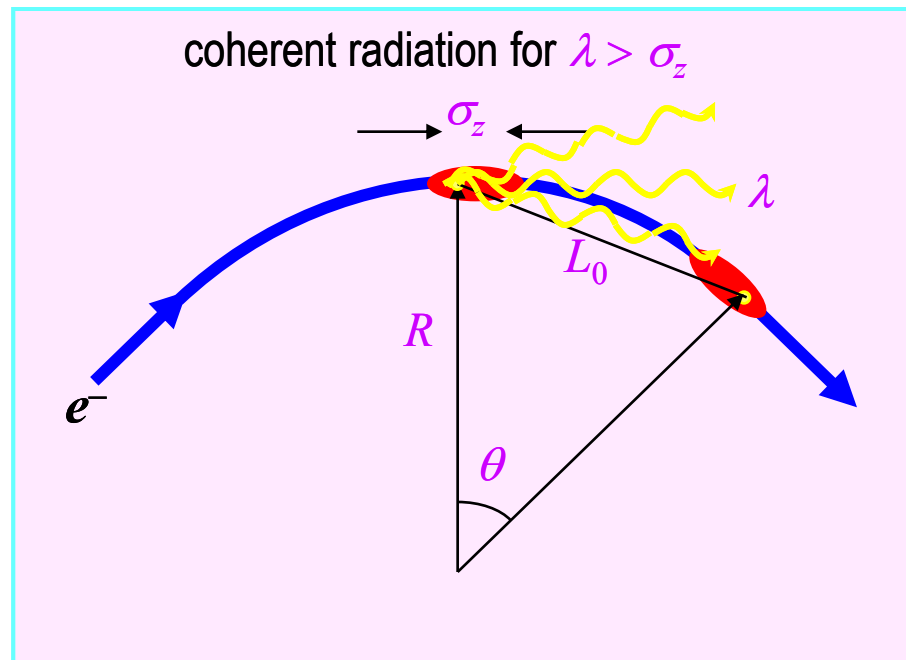
$$k(\varphi) \equiv \frac{\partial \delta}{\partial z} = -\frac{2\pi}{\lambda} \left(1 - \frac{E_0}{E}\right) \frac{\sin(\varphi + \Delta\varphi)}{\cos(\varphi)} \quad \text{'chirp'}$$

final bunch length and energy spread...

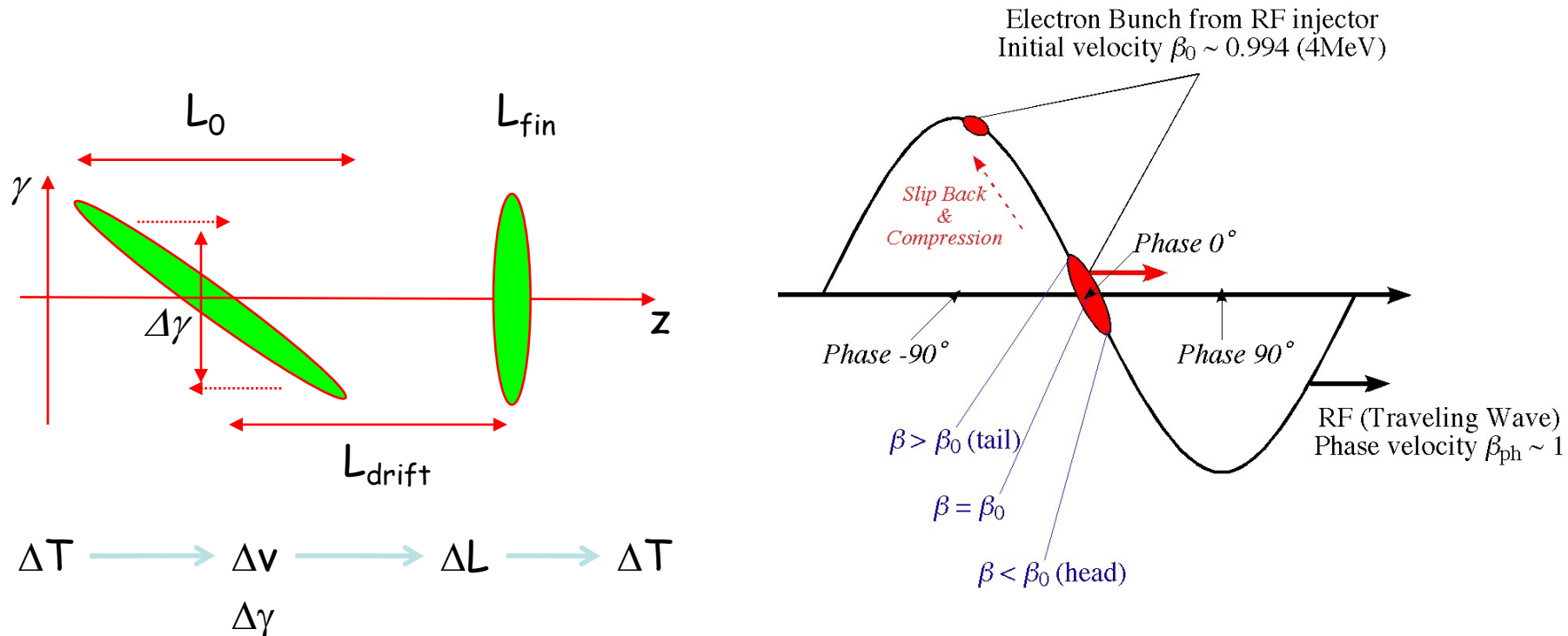
$$\sigma_z = \sqrt{(1 + kR_{56})^2 \sigma_{z0}^2 + R_{56}^2 \sigma_{\delta_0}^2 E_0^2 / E^2} \quad , \quad \sigma_\delta = \sqrt{k^2 \sigma_{z0}^2 + \sigma_{\delta_0}^2 E_0^2 / E^2}$$

Coherent Synchrotron Radiation in Magnetic Chicane

- Powerful radiation generates energy spread in bends
- Causes bend-plane emittance growth (short bunch worse)



Short bunches by Ballistic/Velocity Compression

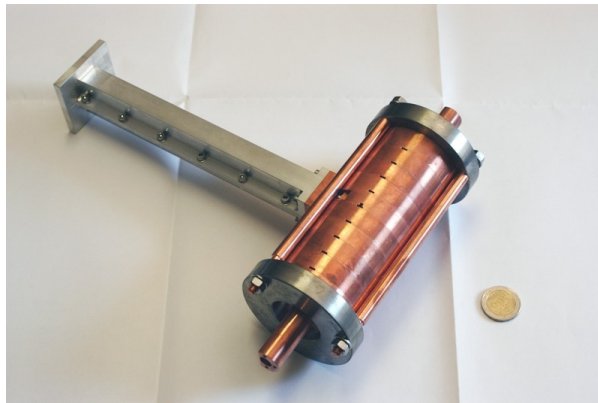
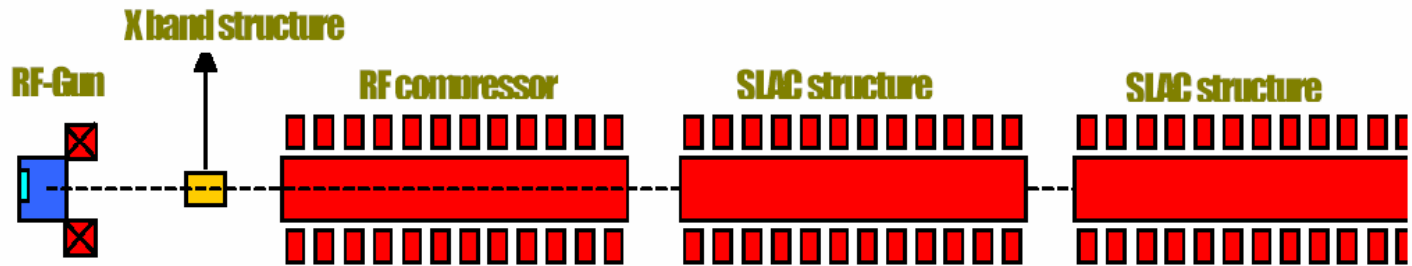


Provide a correlated velocity spread enough to produce, in a drift of length L_{drift} a path difference equal to ΔL

$$\Delta L = \left[\frac{L_{drift}}{\bar{\gamma}^2} \right] \frac{\Delta\gamma}{\bar{\gamma}}$$

P. Piot *et al*, PRSTAB 6 (2003) 033503
S.G. Anderson *et al*, PRSTAB 8 (2005) 014401

Short bunches by Ballistic Compression



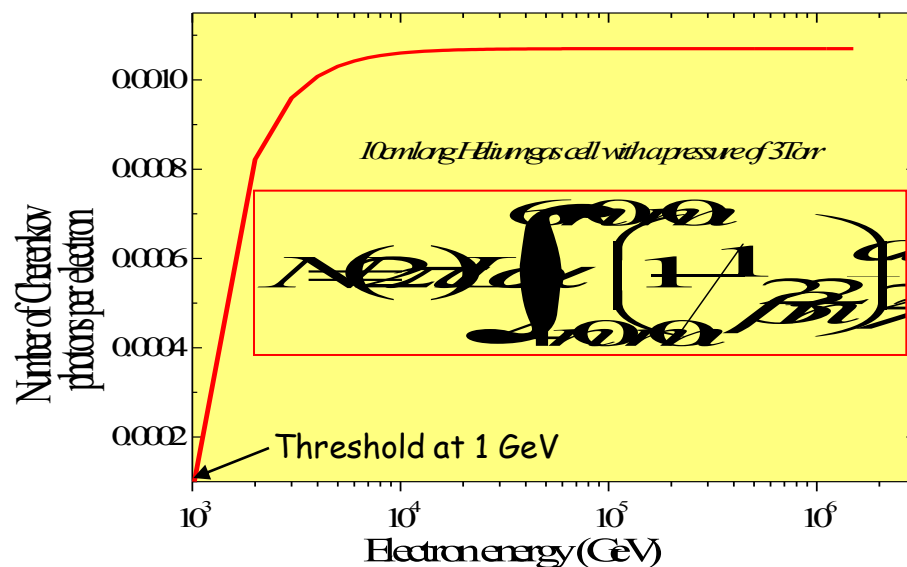
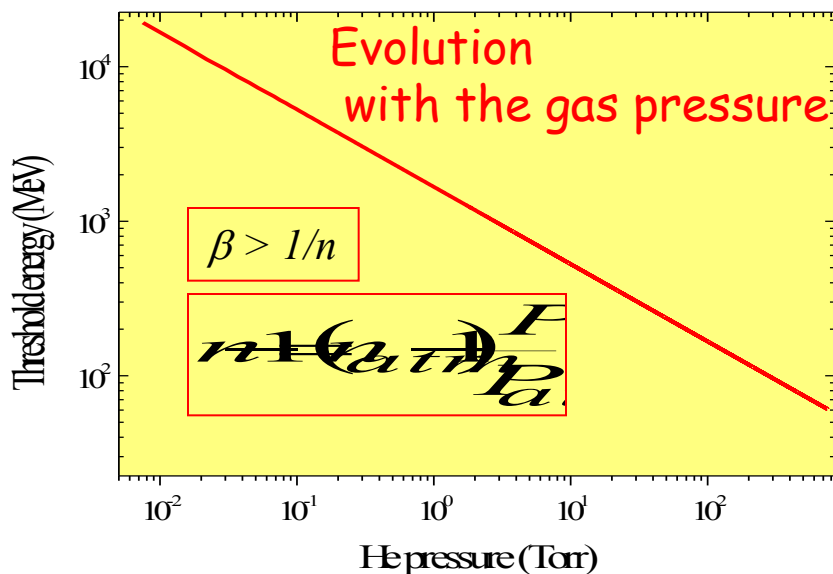
- Works well for non ultra-relativistic beam energies
- no Coherent Synchrotron Radiation effect and bend-plane emittance growth
- Longitudinal emittance growth due to RF non linearities

Reserved Slides

Cherenkov in gases

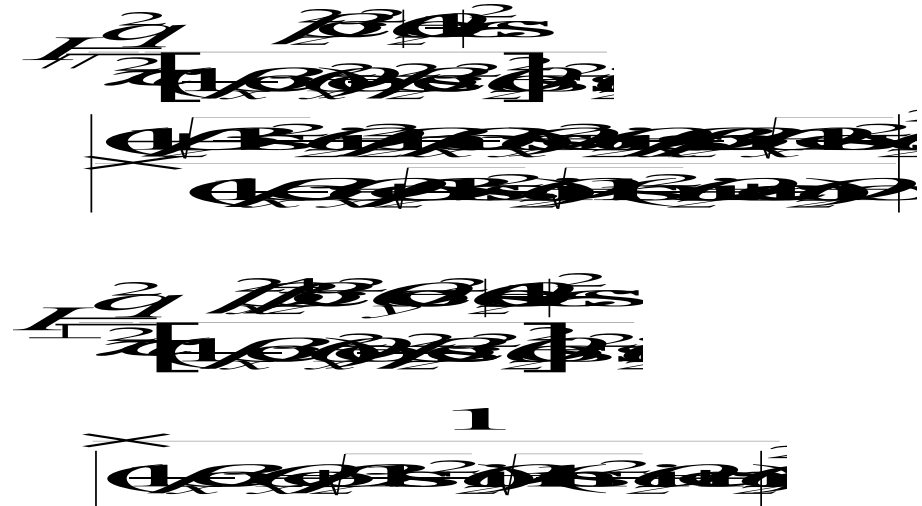
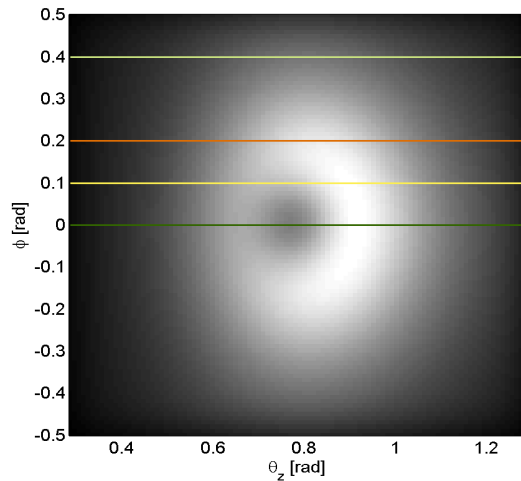
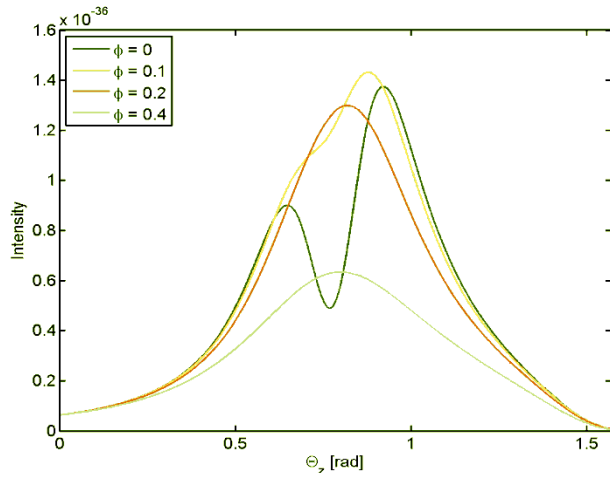
Threshold Cherenkov detector : $\beta > 1/n$

Cherenkov radiator (1atm)	Silica aerogel	Pentane C_5H_{12}	Ethane C_2H_6	Argon Ar	Neon Ne	Helium He
Index of refraction (n-1)	$8.4 \cdot 10^{-3}$	$1.7 \cdot 10^{-3}$	$7.1 \cdot 10^{-4}$	$2.8 \cdot 10^{-4}$	$6.7 \cdot 10^{-5}$	$3.5 \cdot 10^{-5}$
Cherenkov threshold (MeV)	3.5	8.2	13.1	20.9	43.5	60.4



Optical Transition Radiation

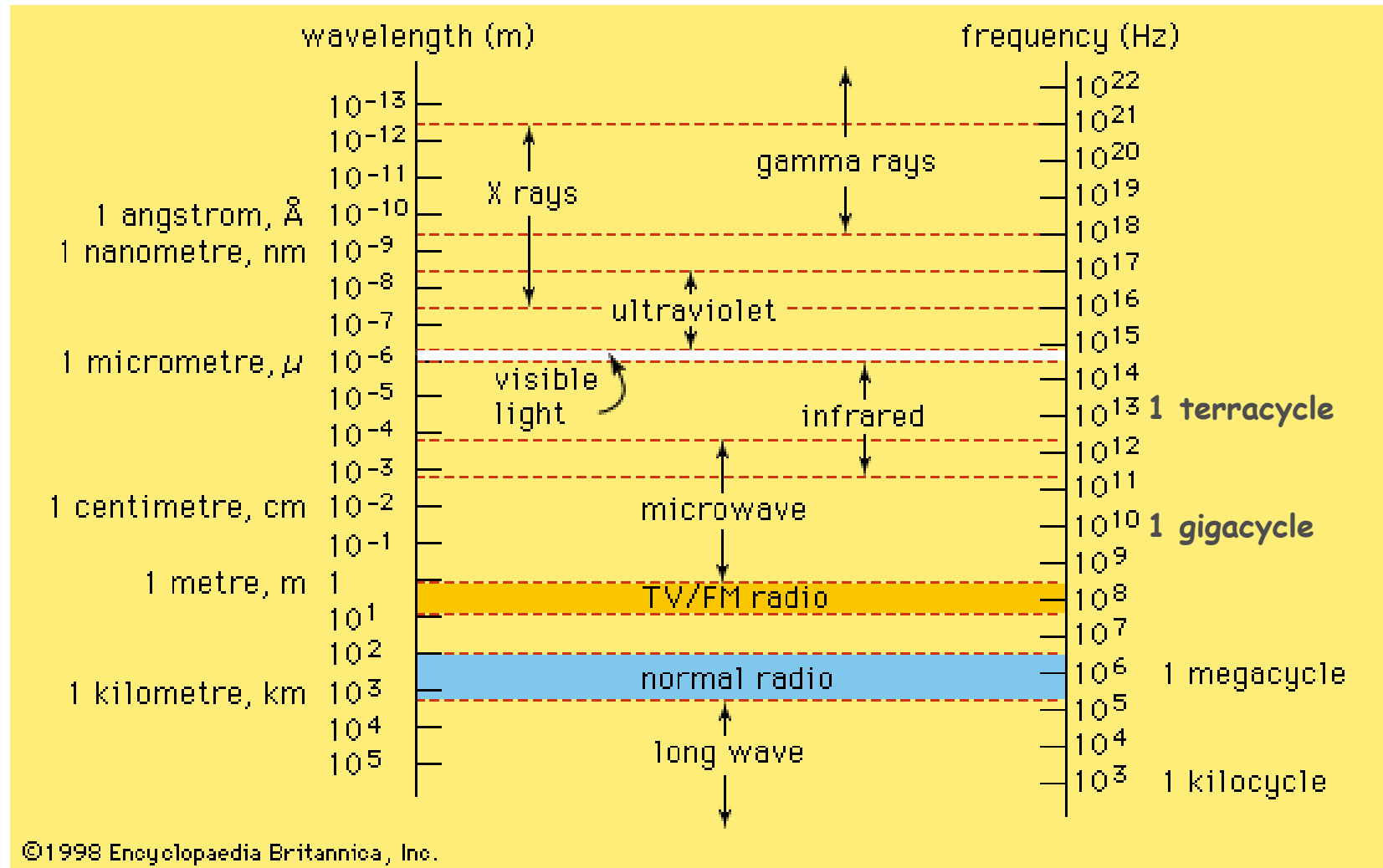
The angular intensity distribution is given by:



The actual angular intensity distribution becomes:



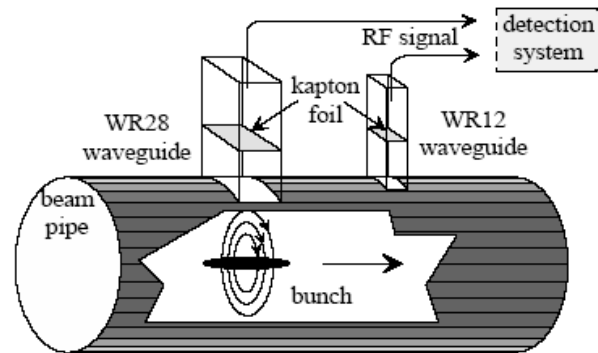
Bunch Frequency Spectrum



Bunch frequency spectrum by RF Pick-up



σ



'Based on the measurement of the bunch spectrum which is picked-up by a rectangular waveguide coupled to the beam pipe'

1

- Simple diode detectors and fixed frequency filters

n!

- Use of RF mixers with a sweeping oscillator

By sweeping over some given frequency range, the frequency spectrum amplitude is measured

C. Martinez et al, CLIC note 2000-020

700fs bunch length on a 40MeV beam

Limitations :

- Sensitive to beam position and beam charge
- Limited to some 300-500fs bunch length (>170GHz)

Bunch frequency spectrum by RF Pick-up



Filters, Horns and mixers

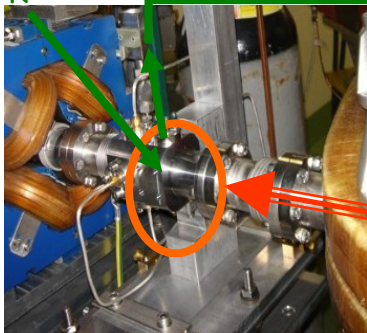
- Reflecting low pass filter - 4 frequency-band detection stages
- Series of 2 down mixing stages at each detection station.

Acqiris DC282 Compact PCI Digitizer

4 channels, 2 GHz bandwidth, 2-8 GS/s sampling rate



BPR



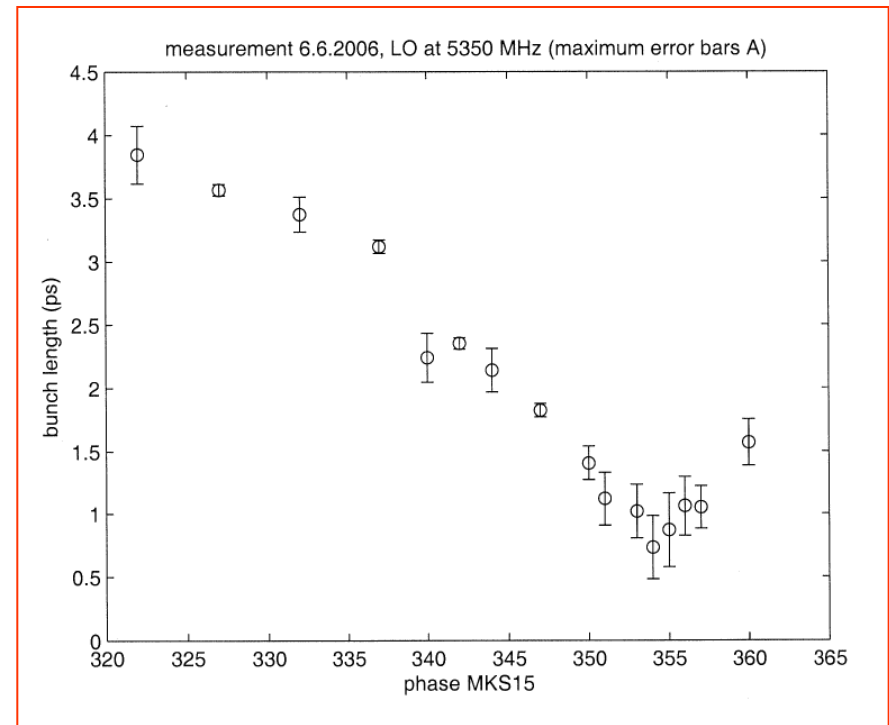
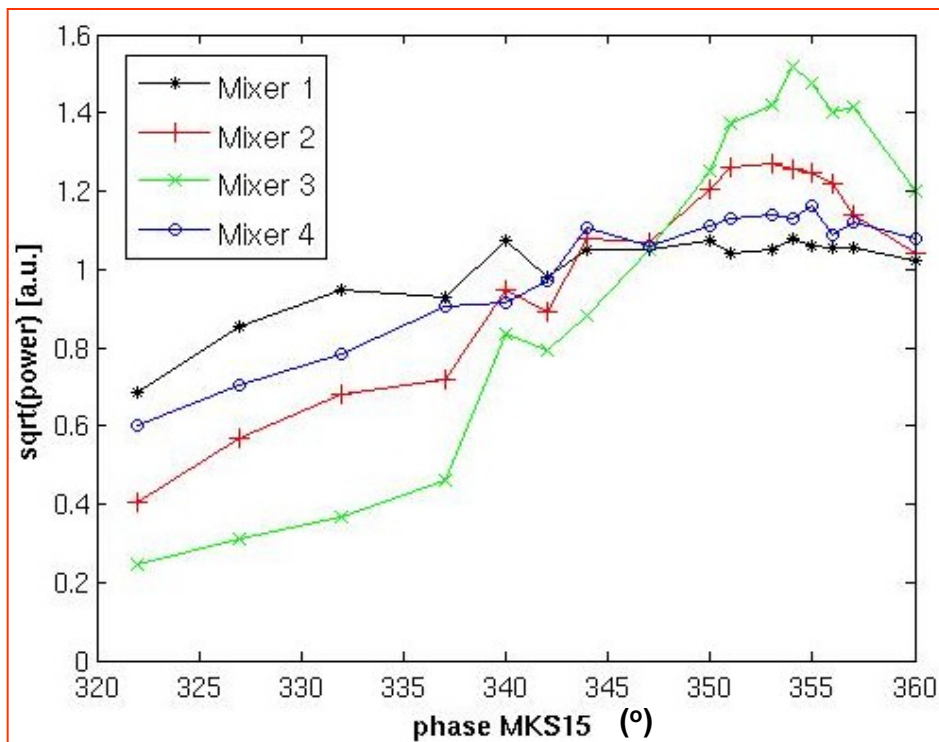
WR-28 Waveguide ~20m long

Beam

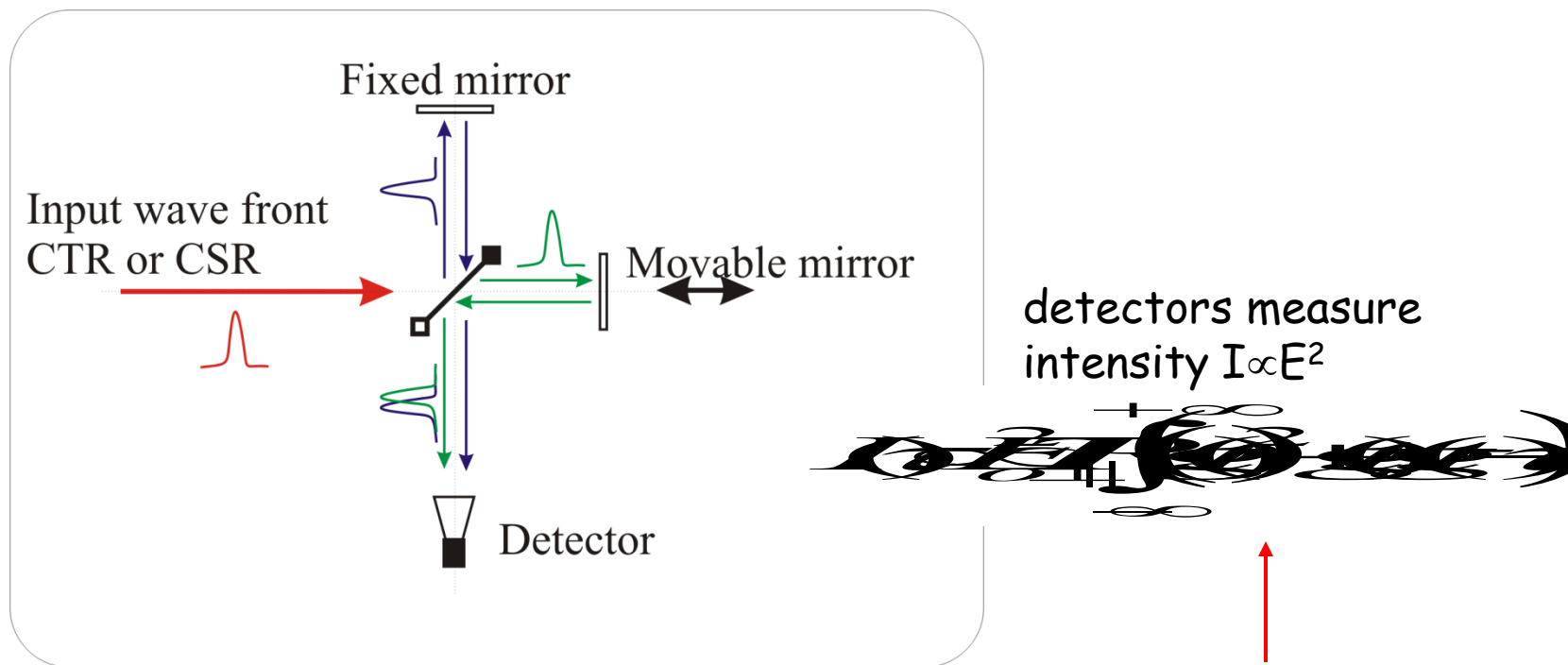
Data acquisition controlled by a Labview program, with built in Matlab FFT analysis routine

Bunch Frequency Spectrum by RF Pick-up

' Changing the phase of a klystron and measuring bunch compression on the pick-up '



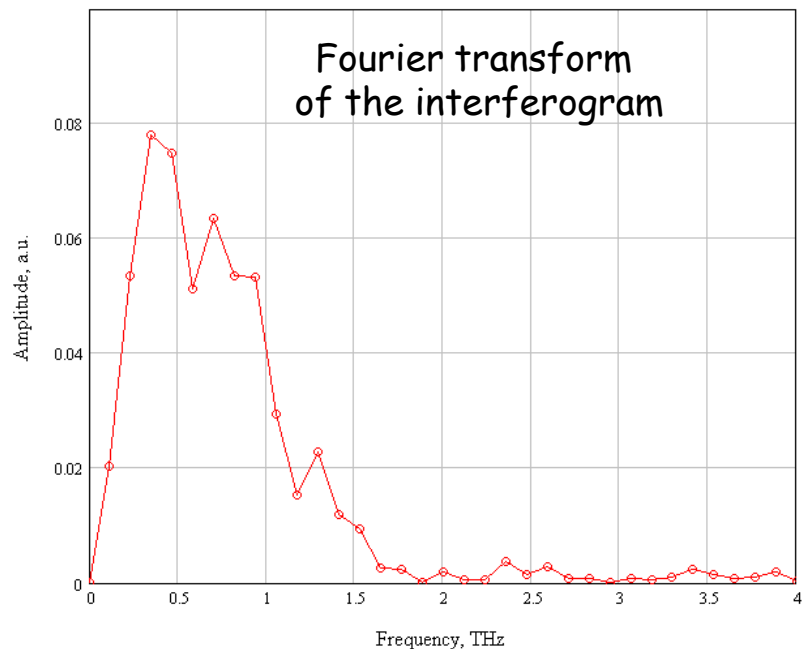
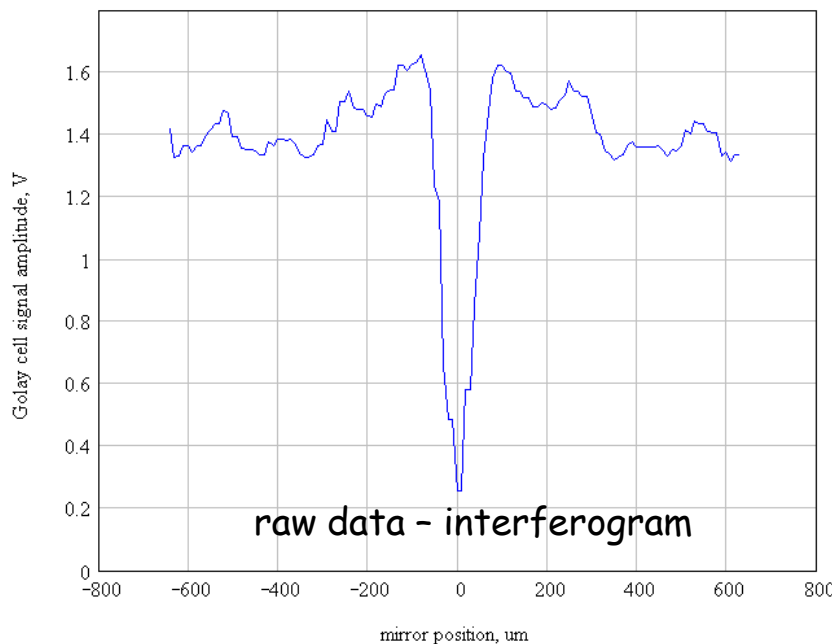
Bunch Frequency Spectrum by Coherent Radiation



the autocorrelation function is
measured with the help of an
interferometer

The Wiener-Khintchine theorem says:
"the Fourier transform of the autocorrelation function
is the power spectrum".

Bunch Frequency Spectrum by Coherent Radiation



- the Gaussian shape of the bunch is assumed

$$f(t) = \frac{Q}{\sqrt{2\pi}} e^{-\left(\frac{t}{\sigma}\right)^2}$$

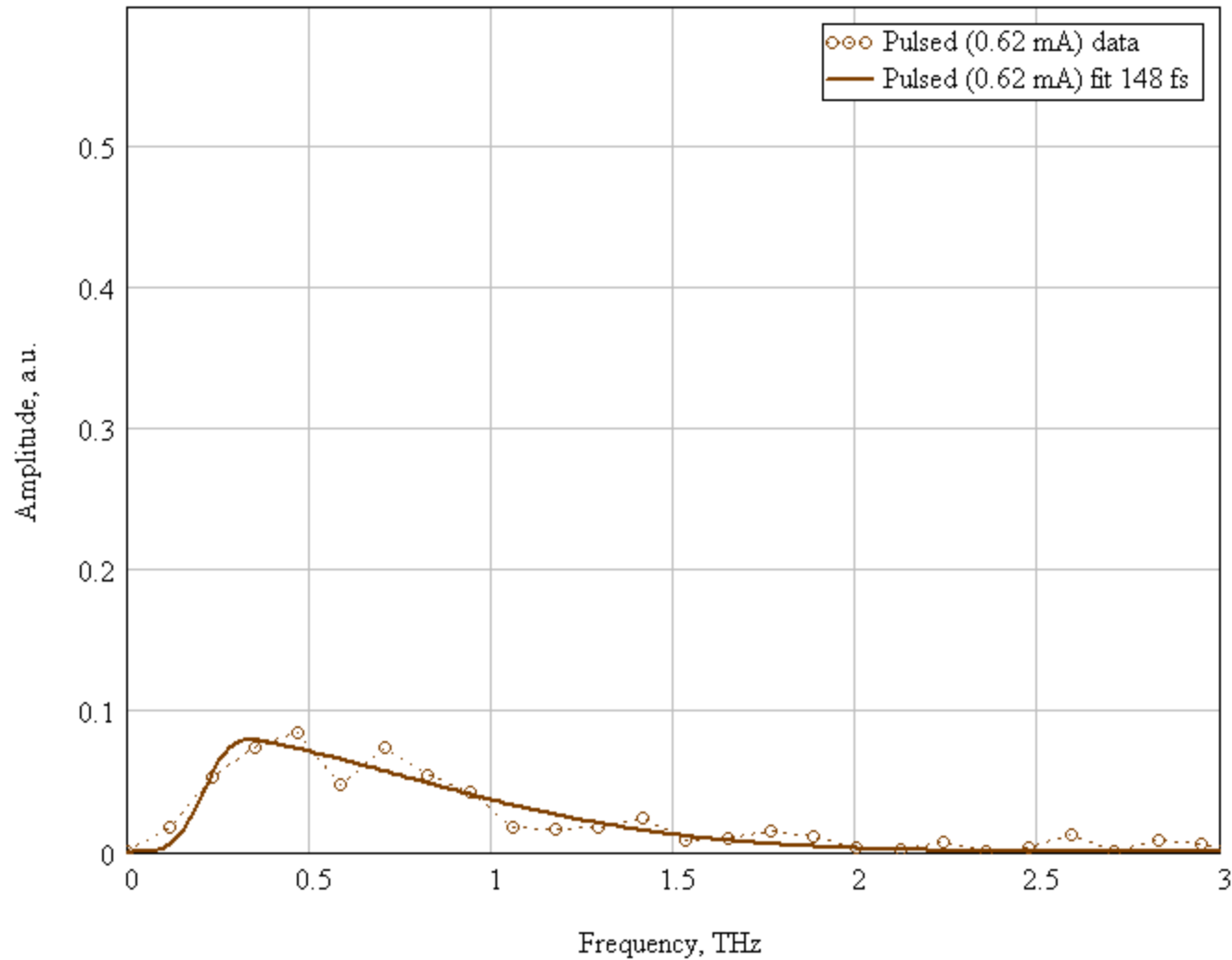
- its power spectrum is also Gaussian

$$|f(\omega)|^2 = \frac{Q^2}{2\pi\sigma^2} e^{-\frac{\omega^2}{2\sigma^2}}$$

- The fit function is used

$$f(\omega) = \frac{Q}{\sqrt{2\pi}} e^{-\frac{\omega^2}{2\sigma^2}}$$

Bunch Frequency Spectrum by Coherent Radiation



RF by Deflecting Cavity

Calibration curves @ Flash

- For fixed power: measurement of the vertical beam position for different phases ϕ

$$\Delta y \approx const \cdot \phi, \quad \phi = \omega_{LOLA} \cdot \Delta t$$

- For arbitrary power:

$$\frac{\Delta y}{\Delta t} = const \cdot \sqrt{P_0}$$

