Higgs

Judith Katzy, DESY

10 years of Higgs discovery 4.7.2012



Happy birthday!





Higgs

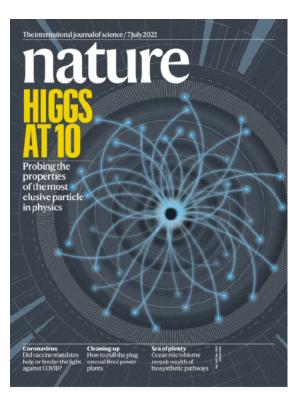
Judith Katzy, DESY

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Happy birthday!





Higgs

- > Higgs mechanism predicted by Englert, Higgs and Brout in the 1960s
- > Nobel prize in 2013 to Francois Englert and Peter Higgs

Higgs discovery seminar at CERN on 4.7.2012









The Higgs boson turns ten



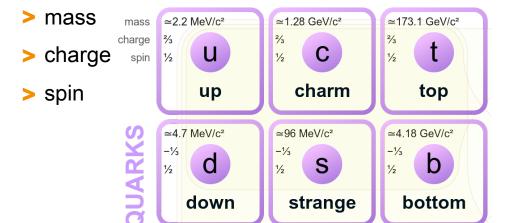
Wise Old Owl - a day ago

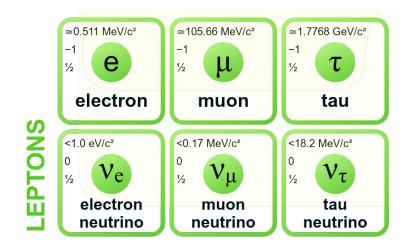
I'm not a particle physicist but I believe the headline is fundamentally flawed as the Higgs Boson has, I suspect, been around for rather longer than 10 years..

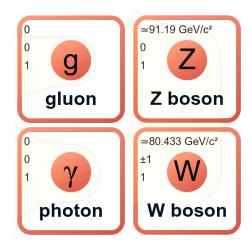
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Observed particles of the Standard Model of Particle physics in 2011

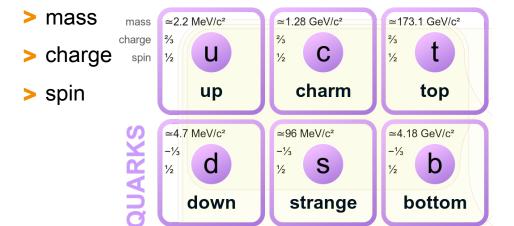


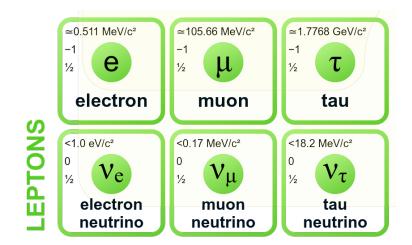


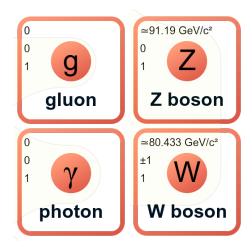




Observed particles of the Standard Model of Particle physics in 2011







Fundamental particles well structured in terms of charge, spin and interactions

mass



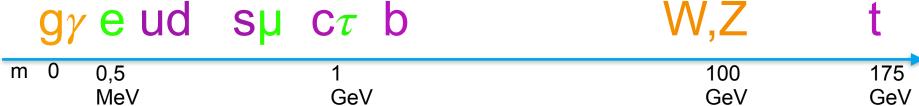
≃2.2 MeV/c²

≃1.28 GeV/c²

С

≃173.1 GeV/c²

t



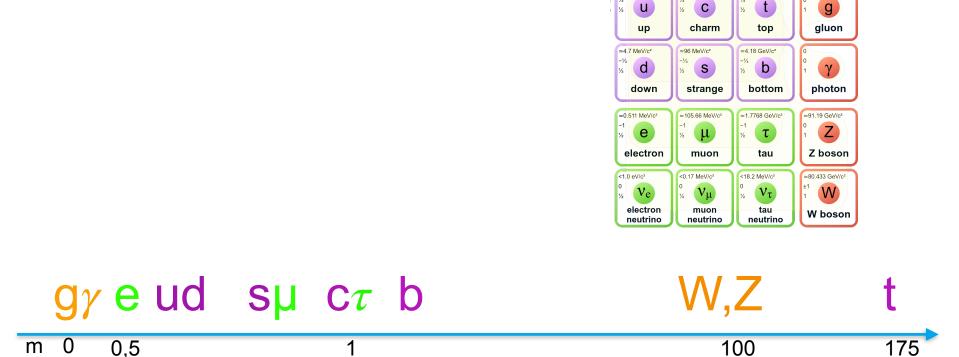
But mass is a mess.....



Mass of gauge bosons: W, Z

- > Observation: weak force is much weaker than em force
- Description: interactions are mediated by gauge bosons:
 - > EM interaction:
 - long range transmitted by massless gauge bosons (photons)
 - No exchange of charge gauge boson is neutral (photons)
 - Weak interaction:
 - Short range transmitted by massive gauge bosons (W,Z)
 - With and without exchange of charge neutral (Z) and charged (W) gauge bosons





≃1.28 GeV/c2

GeV

GeV

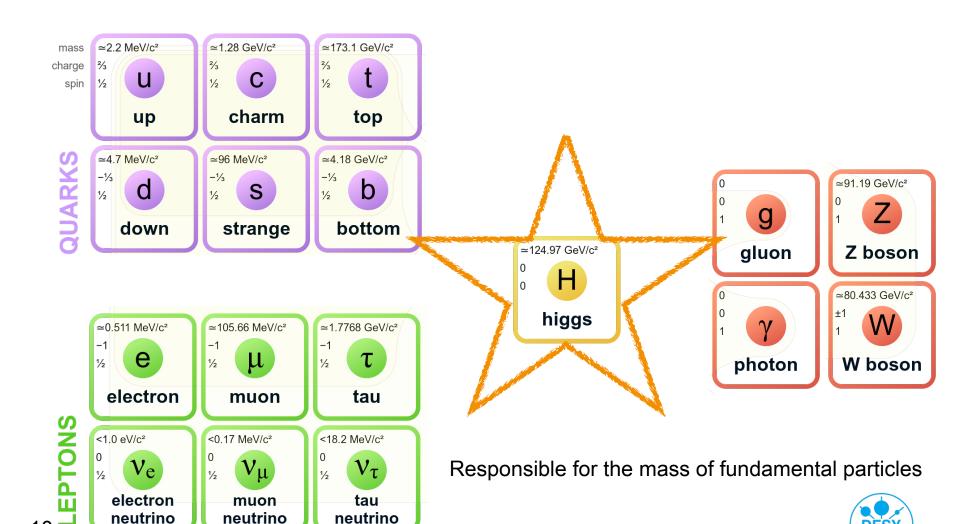
How do get particles mass?

GeV

0.5

MeV

Complete Standard Model of Particle physics in 2012



Higgs field & Higgs boson

- > Higgs field
 - New type of fundamental field ("5th force")
 - > Higgs field is non-zero everywhere all the time
 - Independent of a source being present in the Universe
 - Reminiscent of Aether concept, but now consistent with special relativity
 - Strength of interaction between particles and the Higgs field causes their mass
- > Higgs boson detected = proof of Higgs field exist



Indirect:

- > Predict size of atoms:
 - > Atomic radius proportional to 1/me
 - > A different radius would modify energy levels and chemical reactions of all elements



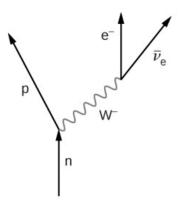
Indirect:

- > Predict size of atoms:
 - > Atomic radius proportional to 1/me
 - > A different radius would modify energy levels and chemical reactions of all elements
- > Makes protons stable
 - \rightarrow Difference in quark masses (m_{up} < m_{down}) contribute to protons being lighter than neutrons
 - > Protons are stable



Indirect:

- > Predict size of atoms:
 - > Atomic radius proportional to 1/m_e
 - A different radius would modify energy levels and chemical reactions of all elements
- Makes protons stable
 - \rightarrow Difference in quark masses ($m_{up} < m_{down}$) contribute to protons being lighter than neutrons
 - > Protons are stable
- > Sets timescale of radioactive β decays
 - Many radioactive decays involve the W boson
 - > examples: fusion reaction in the Sun; life time of stars
 - Mass of W influences the rate of these reactions





Direct:

- Perturb the Higgs field a bit so that it jumps by a quantum and decays by emitting its field quant: the Higgs Boson
- Measure interaction of the Higgs Boson with the SM particles in proton proton collisions at the LHC

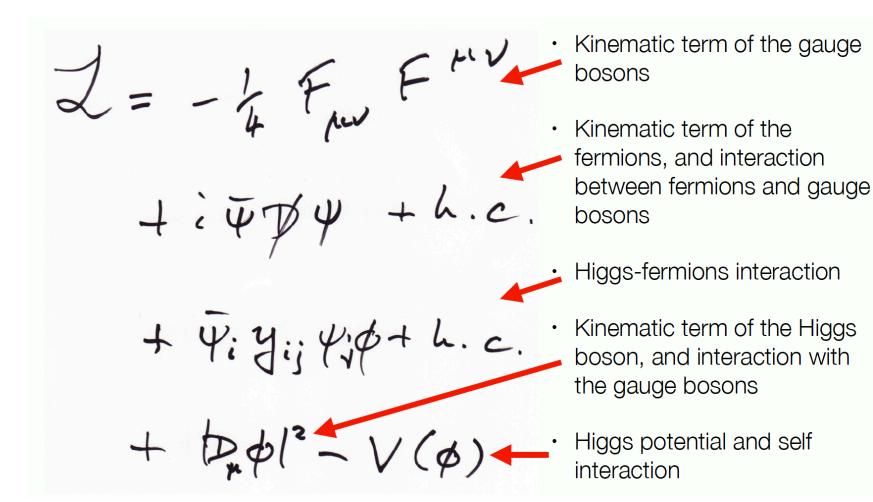


The Higgs Boson

- Powerful tool to study how the underlying Higgs field affects fundamental particles of the Standard Model. Measure
 - > Higgs production
 - > Higgs decay
 - > Higgs mass
 - > Higgs spin
- Since Higgs is everywhere use it to search for signatures of particles or effects hithero unkown and outside the Standard Model
 - > Portal to dark matter
 - Explanation for Baryon asymmetry
 - **>** . . .



The Standard Model Lagrangian



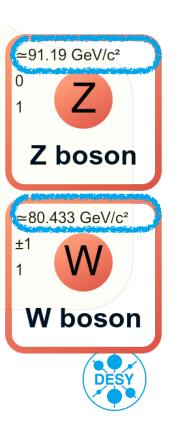


Higgs mechanism for gauge bosons

Modify electroweak part of the Lagrangian to give mass to W and Z but leaving photons and gluons massless







Higgs mechanism for gauge bosons

- Soal: modify electroweak part of the Lagrangian to give mass to W and Z but leaving photons and gluons massless
 - Introduce a (complex) doublet scalar field φ (= 4 real scalar fields related to gauge bosons)

$$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix},$$



Higgs mechanism for gauge bosons

- Goal: modify electroweak part of the Lagrangian to give mass to W and Z but leaving photons and gluons massless
 - > Introduce a (complex) doublet scalar field φ (= 4 real scalar fields related to W+/-, Z, photon)
 - > Generate a mass term from kinetic energy term of φ (by breaking its symmetry)
- > Add a Potential for the scalar field φ

$$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix},$$
 $\mathcal{L}_{\mathrm{Higgs}} = (D_\mu \Phi)^\dagger (D^\mu \Phi) - V \left(\Phi^\dagger \Phi\right)$ Kinetic energy term Potential



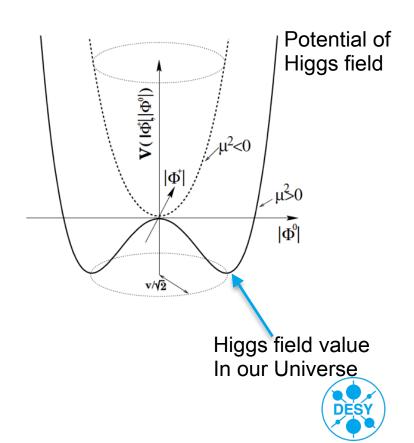
The Higgs Potential

$$V\left(\Phi^{\dagger}\Phi\right) = -\mu^{2}\Phi^{\dagger}\Phi + \lambda\left(\Phi^{\dagger}\Phi\right)^{2}, \qquad \mu^{2}, \lambda > 0$$

Notice the "wrong" mass sign.

$$V\left(\Phi^{\dagger}\Phi\right)$$
 is $SU(2)_L \times U(1)_Y$ symmetric.

- > Higgs field at φ=0 is not the minimum
 - > instable configuration!
- Higgs field has a constant value in vacuum corresponding to the minimum of the potential
 - > "vacuum expectation value" v or vev
 - Higgs field at minimum of potential is non-zero
 - Higgs must be spin 0 to avoid violation of space-time symmetry
 - > Higgs is the only fundamental particle with spin 0



Higgs field is a scalar field

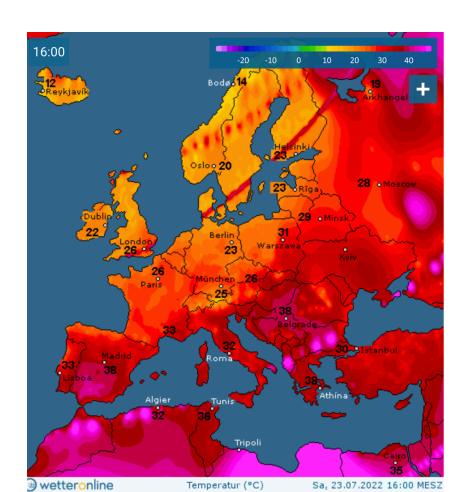
- > Assign a number (scalar) to each point in space
 - > Example: temperature map
- Here: value of Higgs field at minimum of Higgs potential (in vacuum)
- > We can derive this value:

$$m_W^2=rac{g^2v^2}{4}$$
 and $rac{G_F}{\sqrt{2}}=\left(rac{g}{2\sqrt{2}}
ight)^2rac{1}{m_W^2}$ Charged currents

$$v = \sqrt{\frac{1}{\sqrt{2}G_F}}$$
 :

Fermi G_F measured precisely from muon lifetime (with muon beam@PSI)

$$v = \sqrt{\frac{1}{\sqrt{2}G_F}} \approx 246.22 \text{ GeV}$$



Consequences for the scalar field H

The scalar potential

$$V\left(\Phi^{\dagger}\Phi\right) = -\mu^{2}\Phi^{\dagger}\Phi + \lambda\left(\Phi^{\dagger}\Phi\right)^{2}$$

expanded around the vacuum state

$$\Phi(x) = \frac{1}{\sqrt{2}} \left(\begin{array}{c} 0 \\ v + H(x) \end{array} \right)$$

becomes

$$V = \frac{1}{2} \left(\frac{2\lambda v^2}{4} \right) H^2 + \lambda v H^3 + \frac{\lambda}{4} H^4 - \frac{\lambda}{4} v^4$$

 \bullet the scalar field H gets a mass

$$m_H^2 = 2\lambda v^2$$

- there is a term of cubic and quartic self-coupling.
- a constant term: the cosmological constant (irrelevant in the Standard Model)

$$\rho_H \equiv \frac{\lambda}{4} v^4 = \frac{v^2 m_H^2}{8}$$



Consequences: the masses of the bosons

Two massive charged vector bosons

$$m_W^2 = \frac{g^2 v^2}{4}$$

g: weak isospin g':weak hypercharge

One massless vector boson

$$m_{\gamma} = 0$$

One massive neutral vector boson Z

$$m_Z^2 = (g^2 + g'^2)v^2/4$$

One massive scalar particle: The Higgs Boson

$$m_H^2 = \frac{4\lambda(v)m_W^2}{q^2} \quad = \ \lambda \ \mathrm{v^2}$$

Whose mass is an unknown parameter of the theory as the quartic coupling λ

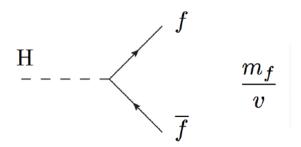
-> Higgs mass is not predicted by the model!



Fermion mass - Yukawa interaction

- > Direct mass term not invariant under SU(2)_L or U(1)_Y gauge transformation
- Generate masses through Yukawa-type interaction terms
 - Lorentz invariant, gauge invariant and renormalizable

Coupling directly proportional to mass





Higgs as a "fifth force" - how does it act?

- > Particles acquire mass by exchanging Higgs boson
 - > Force is stronger for heavier particles
 - > reminiscent of gravity
- Other forces in SM: interaction strength comes in multiples of some basic unit of charge
 - > Electron charge for electric force

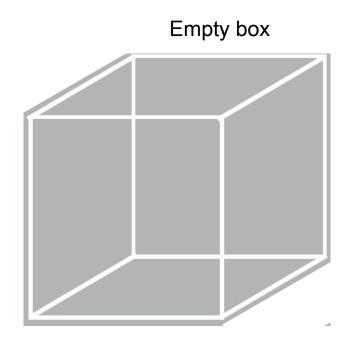


- > Isn't Gravity the force that acts on mass?
- > Does Higgs explain the mass of matter?



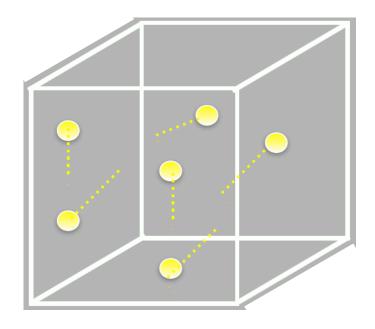
Going back: what is mass?

> Einstein: E = m / c^2 <=> m = E / c^2





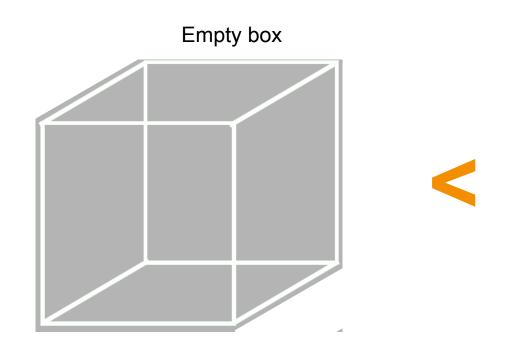
box filled with photons

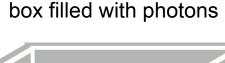


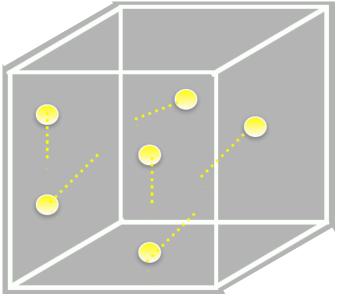


Going back: what is mass?

> Einstein: $E = m / c^2$ <=> $m = E / c^2$





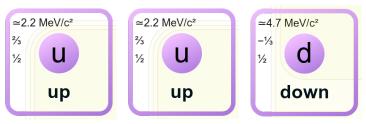


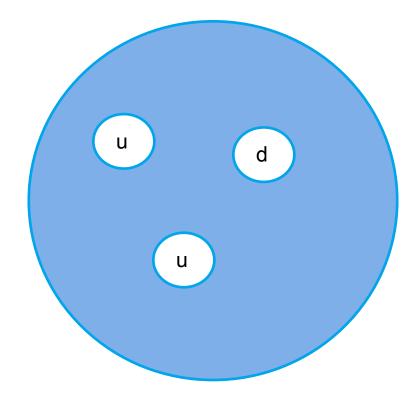
> A system of massless constituents can have a mass



In the real world

> Mass of valence quarks is 9.1 MeV / 1 GeV ~ 1% of the mass of the proton





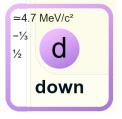


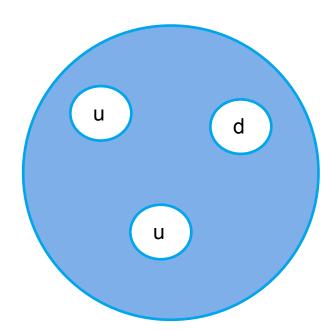
In the real world

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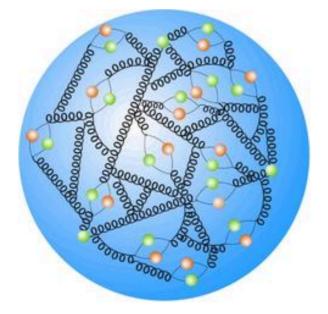








Picture of proton taken by the HERA accelerator



99% of the total mass is dynamically emerging from strong interactions! Gravity couples to the total mass Higgs only couples to mass of fundamental particles.

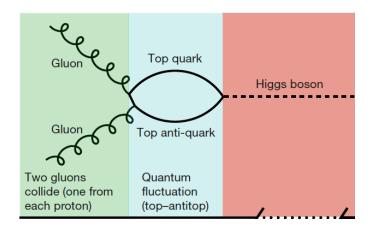


- > What we know so far
 - > Measurements of (with) the Higgs boson



Higgs boson production at the LHC

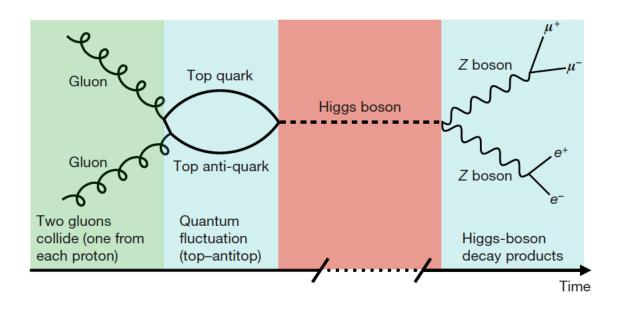
- Higgs boson coupling increases with mass -> use heavy particles to study Higgs-particle interaction
- LHC: proton-proton collider
- Colliding (up and down) quarks and gluons are light
 - Only weak coupling to Higgs field
 - First produce heavy particles which than interact with the Higgs field
 - Quantum fluctuation into a top-antitop pair
 - mass of top: 172 GeV





Measurement of Higgs - example

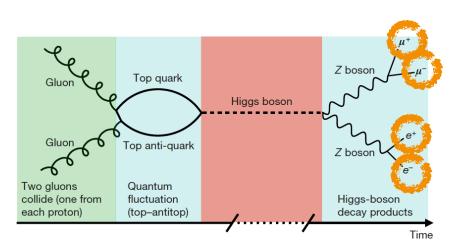
- > ~2.6% of Higgs decay to a pair of Z-bosons
 - Z-bosons decay into pairs of electron and muons which can be detected by the experiments

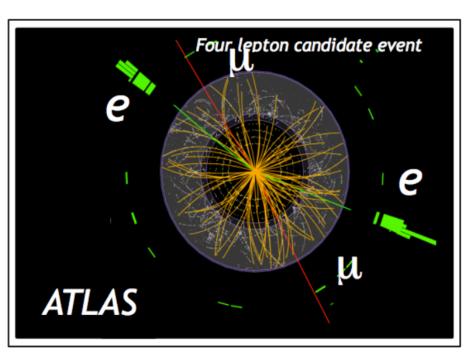




Measurement of Higgs

- > ~2.6% of Higgs decay to a pair of Z-bosons
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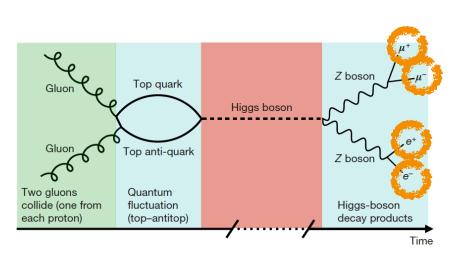


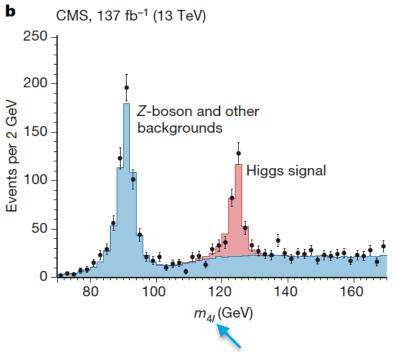


Reconstruct electron and muon four momentum From measured tracks and calorimeter clusters

Measurement of Higgs

- > ~2.6% of Higgs decay to a pair of Z-bosons
 - > Z-bosons decay into pairs of electron and muons which can be detected by the experiments

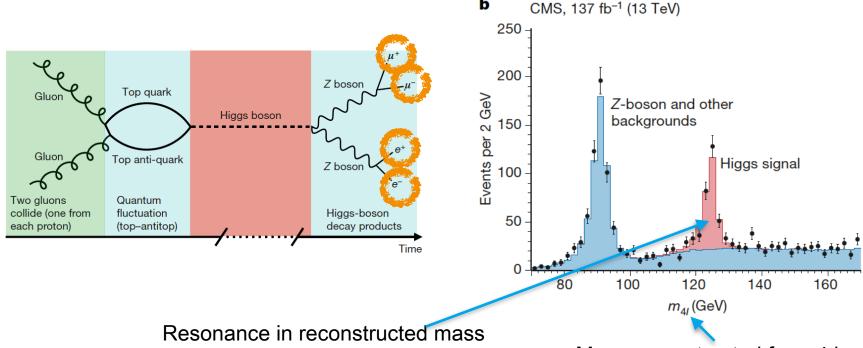




Mass reconstructed from 4 leptons $(e^+e^-\mu^+\mu^- \text{ or } e^+e^-e^+e^- \text{ or } \mu^+\mu^-\mu^+\mu^-)$

Measurement of Higgs

- > ~2.6% of Higgs decay to a pair of Z-bosons
 - > Z-bosons decay into pairs of electron and muons which can be detected by the experiments

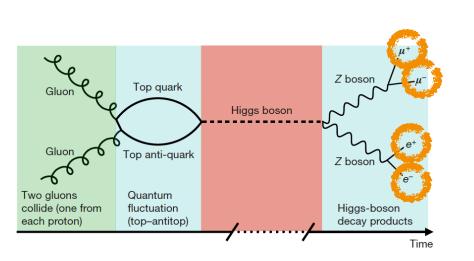


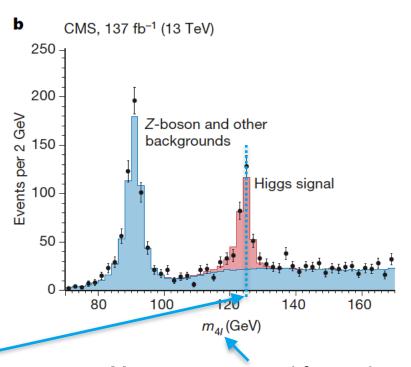
= there is a particle decaying into leptons

Mass reconstructed from 4 leptons $(e^+e^-\mu^+\mu^- \text{ or } e^+e^-e^+e^- \text{ or } \mu^+\mu^-\mu^+\mu^-)$

Measurement of Higgs

- > ~2.6% of Higgs decay to a pair of Z-bosons
 - Z-bosons decay into pairs of electron and muons which can be detected by the experiments





Particle has mass of ~125 GeV

Not shown: relative angular distribution of leptons sensitive to spin of particle => confirmed Higgs is Spin-0

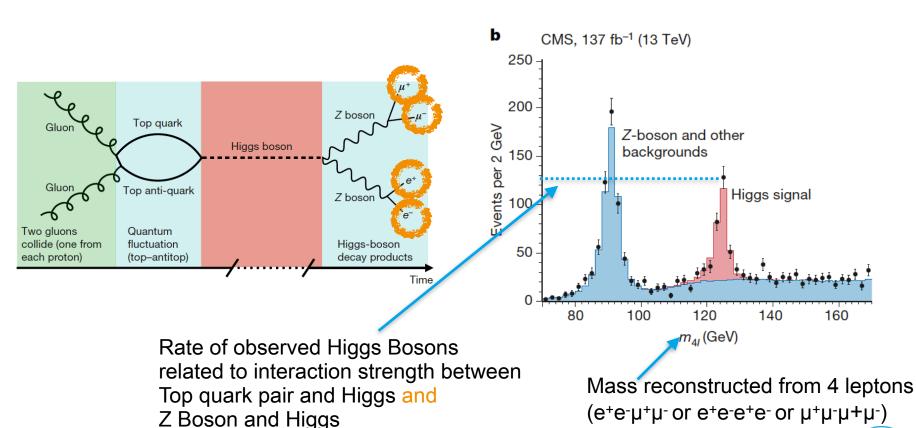
Mass reconstructed from 4 leptons (e+e-μ+μ- or e+e-e+e- or μ+μ-μ+μ-)

Measurement of Higgs

> ~2.6% of Higgs decay to a pair of Z-bosons

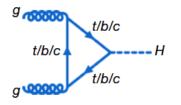
Both are predicted by SM

Z-bosons decay into pairs of electron and muons which can be detected by the experiments



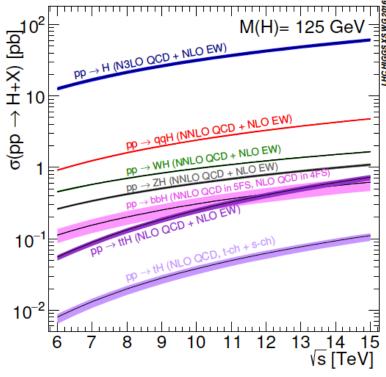
- Interaction in one measurement related to Higgs interaction in production * decay
- To get interactions separately per particle probe all possible decay and production modes with complementary sensitivity
 - > Each mode has special experimental challenges





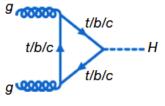
Gluon Fusion (ggF) 7M Higgs produced



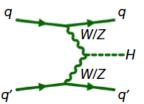


LHC center of mass energy

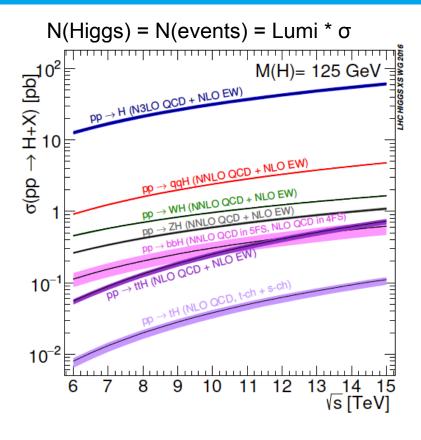




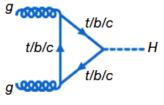
Gluon Fusion (ggF) 7M Higgs produced



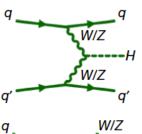
Vector Boson Fusion (qqH) ~0.5M Higgs produced







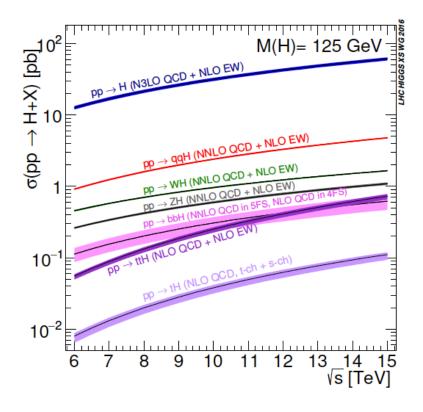
Gluon Fusion (ggF) 7M Higgs produced



W/Z

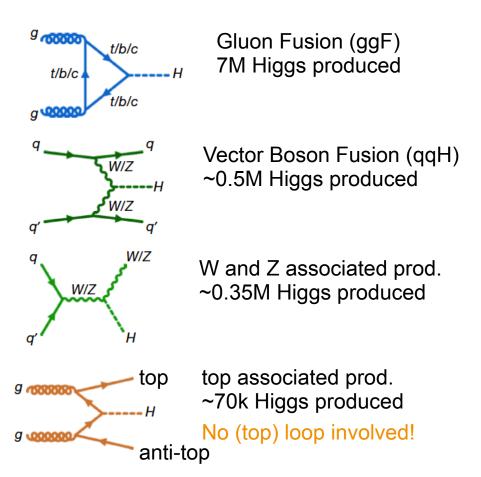
Vector Boson Fusion (qqH) ~0.5M Higgs produced

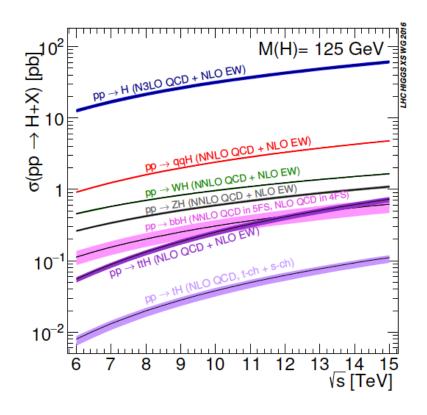
W and Z associated prod. ~0.35M Higgs produced





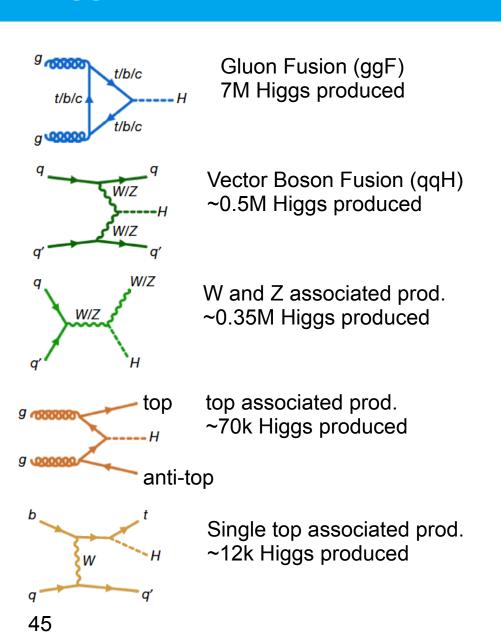
Higgs production modes at the LHC

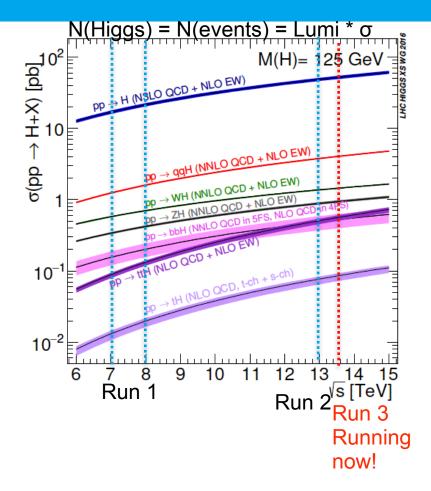






Higgs production modes at the LHC



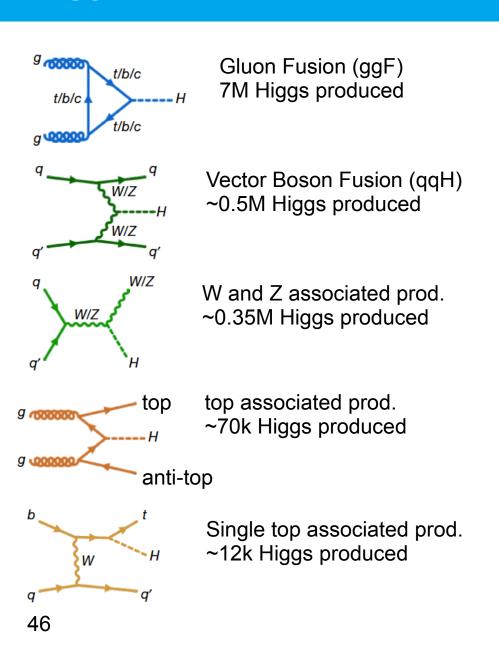


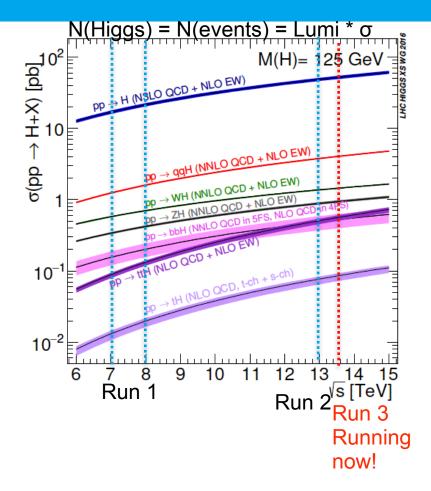
Cross sections increase with center of mass energy

-> note in particular for ttH and tH



Higgs production modes at the LHC



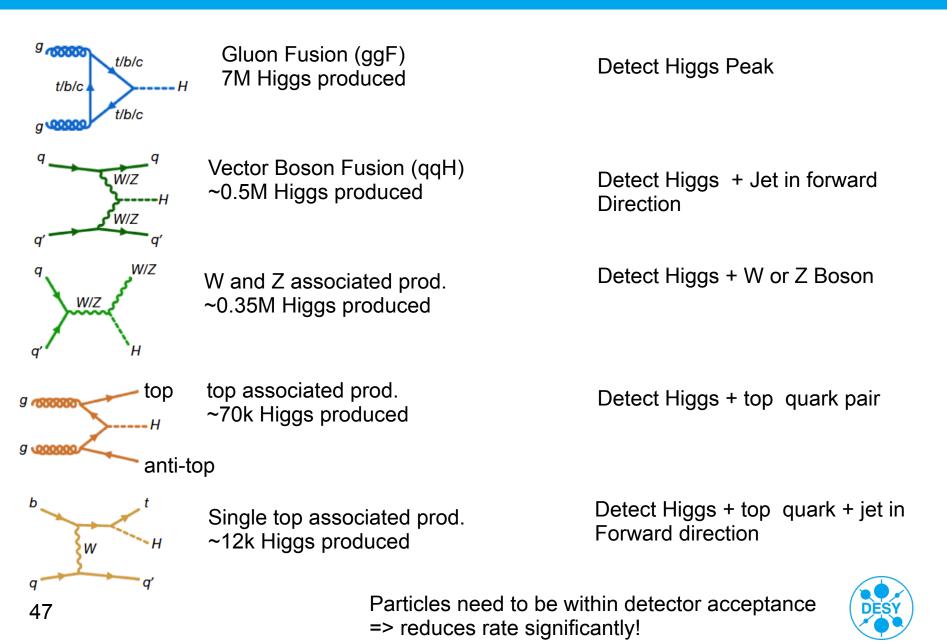


Cross sections increase with center of mass energy

-> note in particular for ttH and tH

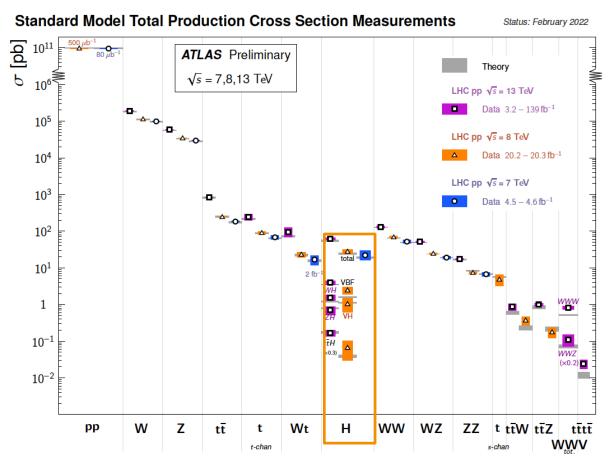


Measure Higgs production modes at the LHC



Rate of Physics processes at the LHC



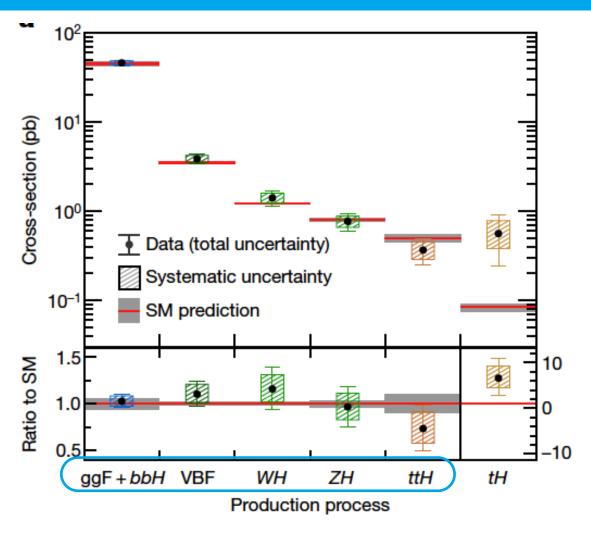


Lots of background to suppress!

-> stringent requirements to select events fast during data taking (trigger) and during offline data analysis

Reduce rate of selected Higgs events significantly! In total ~27000 Higgs events recorded

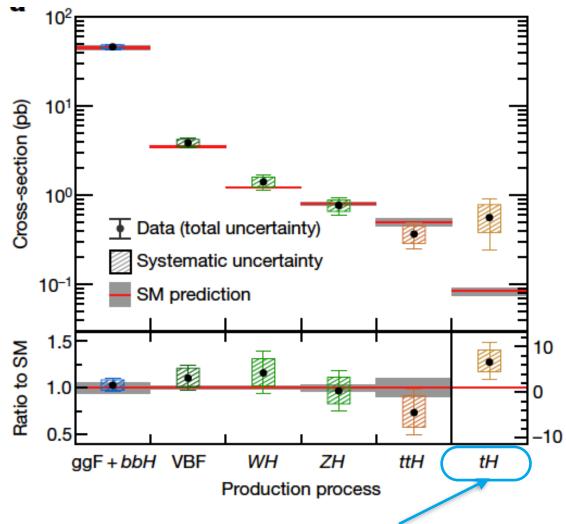
Measured production cross section



Processes observed



Measured production cross section



Processes not yet observed
Rate of the process < 8 times SM prediction
(so maybe it is equal to SM prediction?)
Something to discover with LHC Run 3

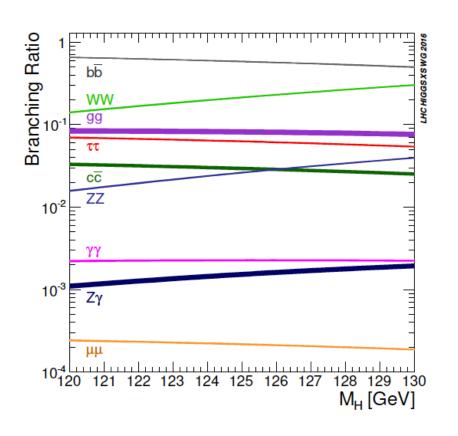


Higgs decays - third generation quarks

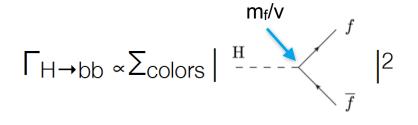
> Higgs lifetime 10⁻²² sec -> total decay width Γ_{tot}: 4.1 MeV

 $BR_{i}=\Gamma_{i}/\Gamma_{tot}$ $\Gamma_{tot}=\Sigma \Gamma_{i}$

> Higgs decays into a pair of fermions or bosons



Example decay to bb:



Decay mode	Expected BR for m _H =125 GeV
bb	57%

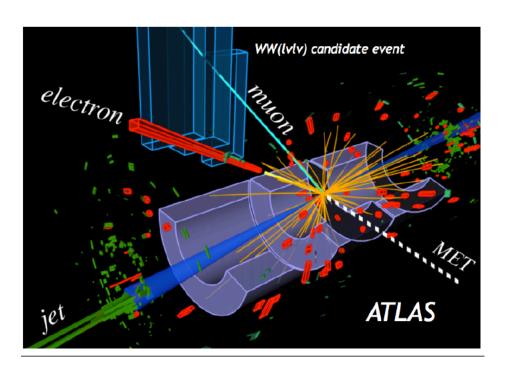


Higgs decays - W-bosons

> Higgs lifetime 10⁻²² sec -> total decay width Γ_{tot}: 4.1 MeV

 $BR_{i}=\Gamma_{i}/\Gamma_{tot}$ $\Gamma_{tot}=\Sigma \Gamma_{i}$

> Higgs decays into a pair of fermions or bosons



Decay mode	Expected BR for m _H =125 GeV
bb	57%
WW	22%

Question round: why is WW BR lower than bb? After all, W is much heavier?

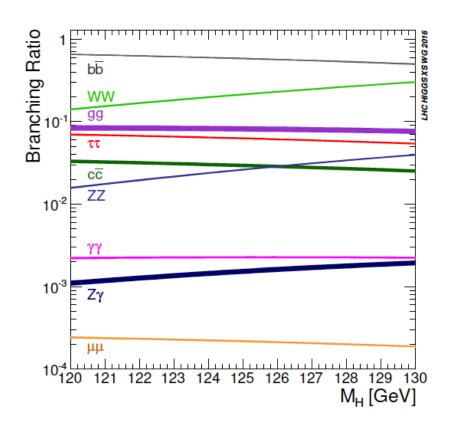


Higgs decays - third generation leptons

> Higgs lifetime 10⁻²² sec -> total decay width Γ_{tot}: 4.1 MeV

 $BR_{i}=\Gamma_{i}/\Gamma_{tot}$ $\Gamma_{tot}=\Sigma \Gamma_{i}$

> Higgs decays into a pair of fermions or bosons

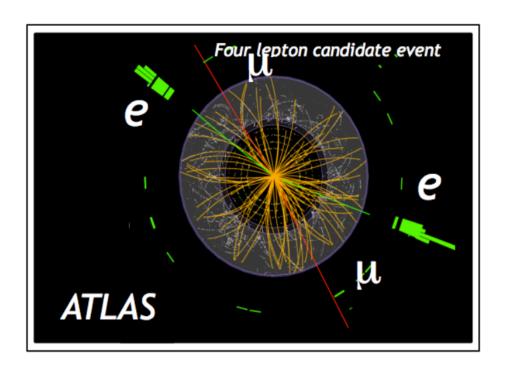


Decay mode	Expected BR for m _H =125 GeV
bb	57%
WW	22%
ττ	6.3 %



Higgs decays - Z-bosons

- > Higgs lifetime 10⁻²² sec -> total decay width Γ_{tot}: 4.1 MeV
- > Higgs decays into a pair of fermions or bosons



Decay mode	Expected BR for m _H =125 GeV
bb	57%
WW	22%
π	6.3 %
ZZ	3%

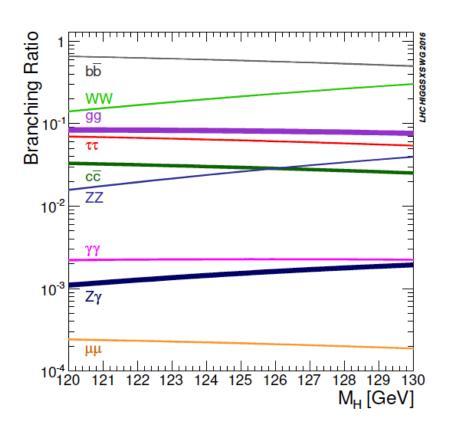


Higgs decays - 2nd generation quarks

> Higgs lifetime 10⁻²² sec -> total decay width Γ_{tot}: 4.1 MeV

 $BR_{i}=\Gamma_{i}/\Gamma_{tot}$ $\Gamma_{tot}=\Sigma \Gamma_{i}$

> Higgs decays into a pair of fermions or bosons

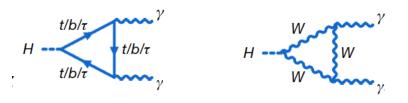


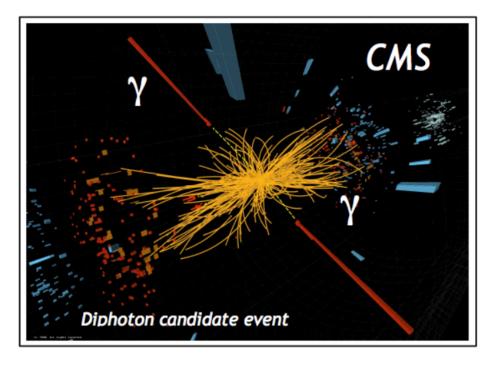
Decay mode	Expected BR for m _H =125 GeV
bb	57%
WW	22%
π	6.3 %
ZZ	3%
CC	3%

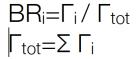


Higgs decays - photons

How? - Loop again!



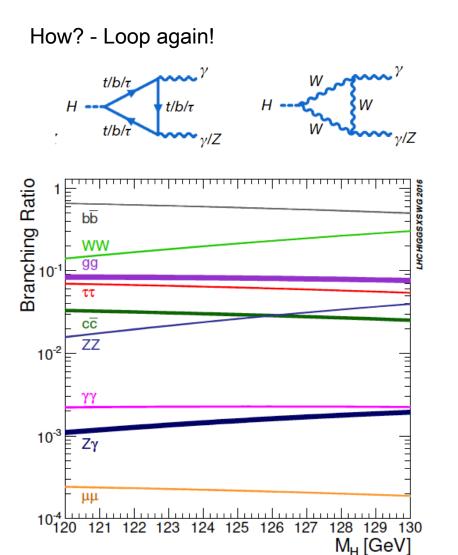




Decay mode	Expected BR for m _H =125 GeV
bb	57%
WW	22%
π	6.3 %
ZZ	3%
СС	3%
γγ	0.2 %



Higgs decays - Z + photon

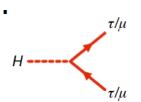


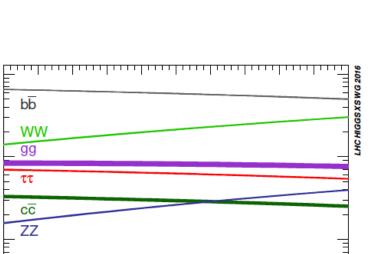
$BR_i = \Gamma_i / \Gamma$	tot
$\Gamma_{tot} = \Sigma \Gamma_i$	

Decay mode	Expected BR for m _H =125 GeV
bb	57%
WW	22%
ττ	6.3 %
ZZ	3%
CC	3%
γγ	0.2 %
Ζγ	0.2 %

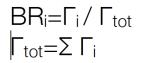
7 Question: why do the BR for WW, ZZ and Zgamma depend more on Higgs mass than the other BR?

Higgs decays - 2nd generation fermions





M_H [GeV]



Decay mode	Expected BR for m _H =125 GeV
bb	57%
WW	22%
ττ	6.3 %
ZZ	3%
СС	3%
γγ	0.2 %
Ζγ	0.2 %
μμ	0.02 %



Branching Ratio

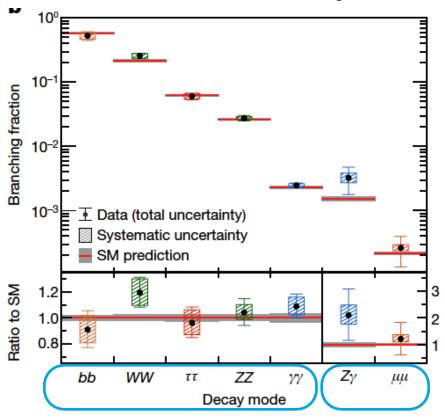
10⁻²

10⁻³

Ζγ

Measured Higgs branching ratios

Assume Higgs production follows. Standard Model -> get BR from data

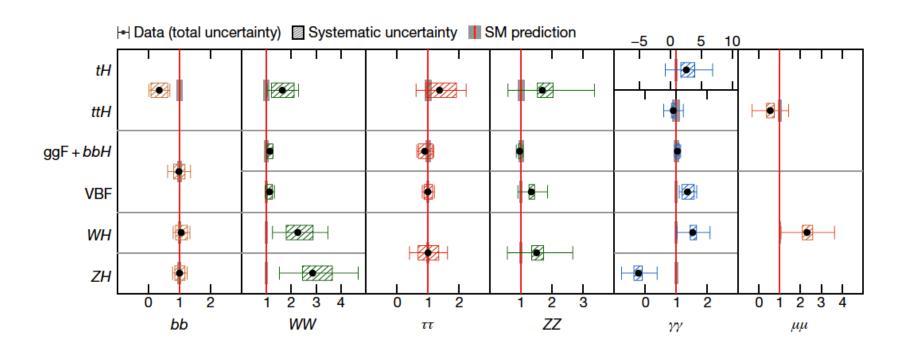


Measured to be in agreement with SM within ~20%

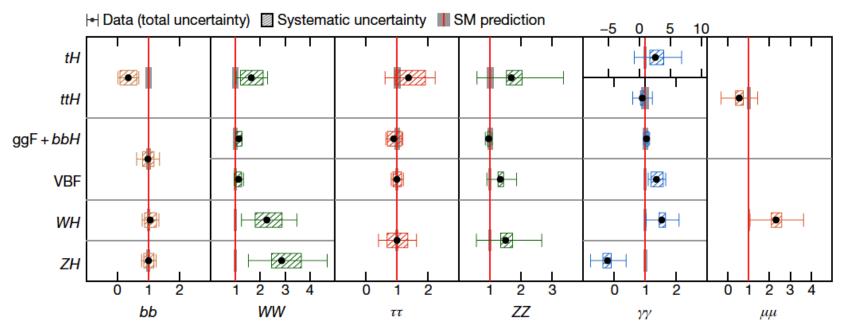
Very rare decays measured with SM within 2-300%

Many decay modes experimentally proven to exist = strong evidence to establish resonance at m=125 GeV as Higgs









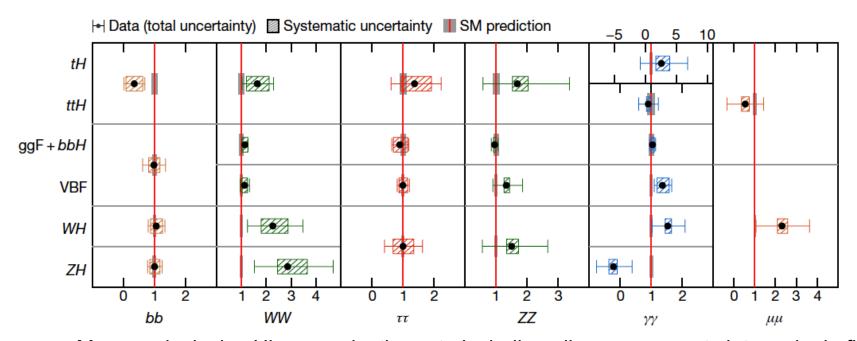
Measure inclusive Higgs production rate including all measurements into a single fit Parameterising each individual production and decay mode as

$$\mu_{if} = (\sigma_i/\sigma_i^{SM})(B_f/B_f^{SM})$$

$$\mu = 1.05 \pm 0.06$$

= $1.05 \pm 0.03(\text{stat.}) \pm 0.03(\text{exp.}) \pm 0.04(\text{sig. th.}) \pm 0.02(\text{bkg. th.}).$





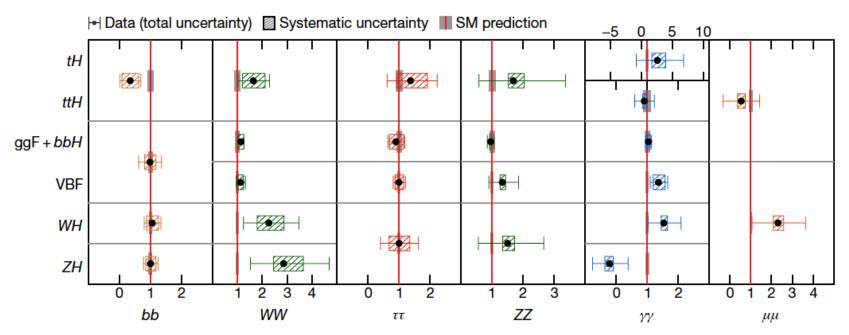
Measure inclusive Higgs production rate including all measurements into a single fit Parameterising each individual production and decay mode as

$$\mu_{if} = (\sigma_i/\sigma_i^{SM})(B_f/B_f^{SM})$$

Room for better theory
$$\mu = 1.05 \pm 0.06$$

$$= 1.05 \pm 0.03 (\text{stat.}) \pm 0.03 (\text{exp.}) \pm 0.04 (\text{sig. th.}) \pm 0.02 (\text{bkg. th.}).$$



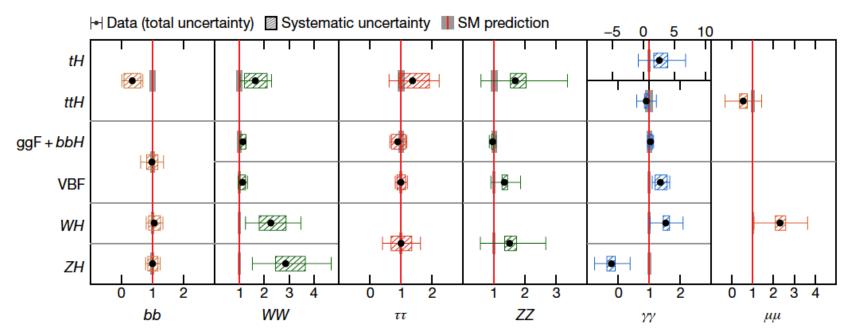


Measure inclusive Higgs production rate including all measurements into a single fit Parameterising each individual production and decay mode as

$$\mu_{if} = (\sigma_i/\sigma_i^{SM})(B_f/B_f^{SM})$$

$$\mu$$
 = More data will help
= 1.05 ± 0.03(stat.) ± 0.03(exp.) ± 0.04(sig. th.) ± 0.02(bkg. th.).



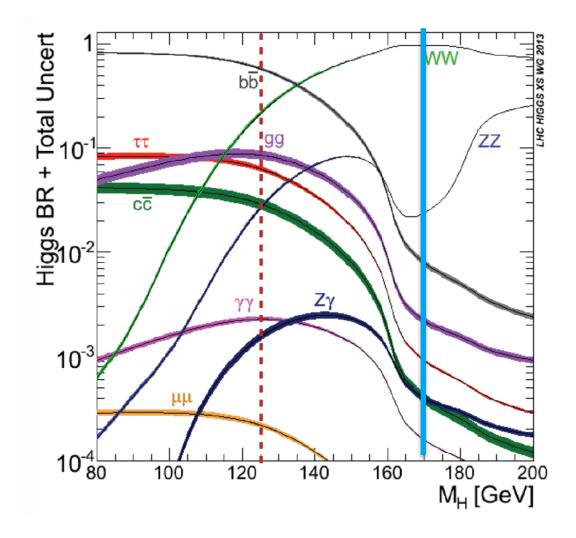


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$$\mu_{if} = (\sigma_i/\sigma_i^{SM})(B_f/B_f^{SM})$$

$$\mu$$
=1.05±0.06 Room for improved calibrations and object reconstruction =1.05±0.03(stat.)±0.03(exp.)±0.04(sig. th.)±0.02(bkg. th.).

What if....?



If Higgs were 50 GeV heavier, most of the decay channels would have been Out of reach for current LHC data. In particular $\gamma\gamma$ channel!



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- > Technical implementation: κ framework



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p: particle, e.g. γ , b, W, Z,...

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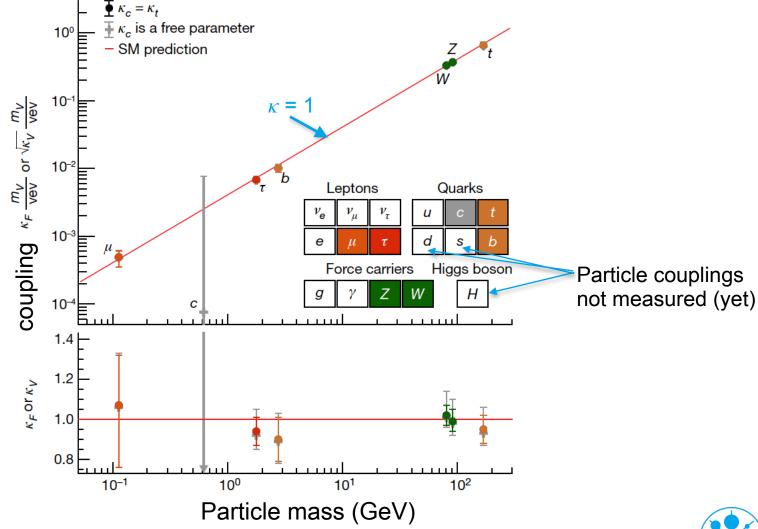
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- K = 1 means agreement with SM
- > Coupling of vector bosons and fermions follow Higgs mechanism
- Make assumptions on the other couplings not being probed
 - > Being SM or being free
 - > fermions couple the same way (one modifier for $\kappa_c = \kappa_t$)
 - **>** ...

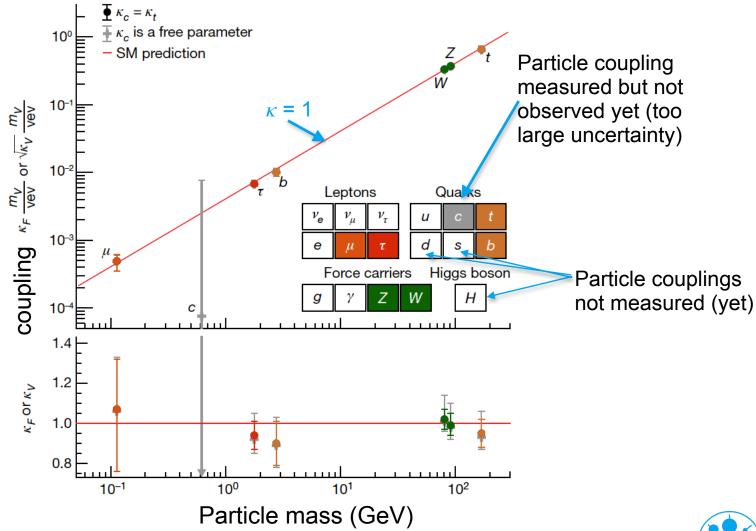


Measure coupling strength as function of mass



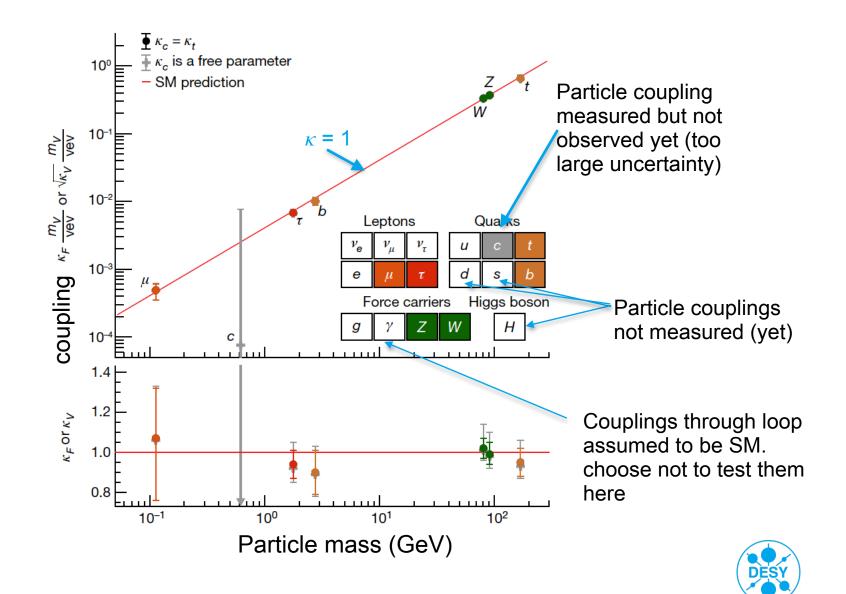


Measure coupling strength as function of mass

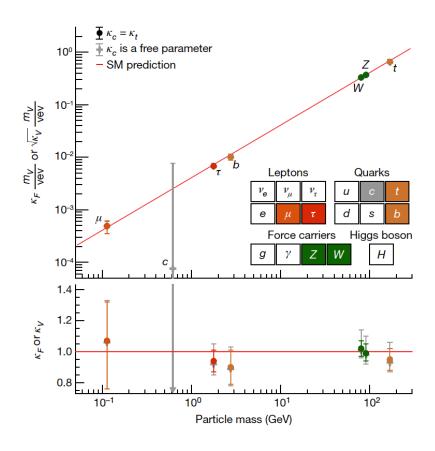




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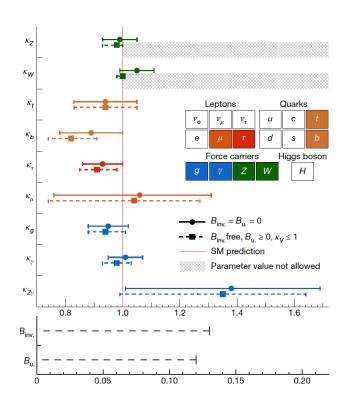


- Higher mass leads to more precise measurements
- Knowledge about Higgs mostly from vector boson couplings (5% precision) and 3rd generation fermions (7-12% precision)
- 2nd generation fermions probed with large uncertainties



Measure coupling strength

- > Maybe there is coupling to a (new) particle that has just not been observed yet?
 - > Probe data under this assumption (B_{inv} free)
 - Some decays might be undetected due to large backgrounds, let's include these as well (B_u >= 0)





Higgs Summary

- Demonstrated Higgs mechanism and what we know today about the resonance observed at ~125 GeV on 4.7.2012
 - > It is spin-0
 - It has mass of 125 GeV
 - It couples to 3rd generation fermions and heavy vector bosons according to the Standard model prediction within (5-12% precision)
 - > It couples to 2nd generation fermions
 - It decays to photons
- It looks like the Higgs in the Standard Model Higgs Boson!



Higgs Outlook

- Room for new physics to appear?
- > Not all couplings have been observed yet:
 - > Decay to charm quarks (hopefully with Run 3 data)
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 - > Decay to up, down, strange quarks
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 - Measure CP properties of Higgs in fermionic interactions
 - Deviation might explain Baryon asymmetry in Universe
 - > First results exists, LHC Run3 will make them more precise



Back-up



MASS TERMS

quadratic in fields with a constant

$$\frac{g_W^2}{8}(W_\mu^1 + iW_\mu^2)(W^{1\mu} - iW^{2\mu})(v+h)^2$$

$$\frac{g_W^2v^2}{8}(W_\mu^1W^{1\mu} + W_\mu^2W^{2\mu}) = \frac{m_W^2}{2}(W_\mu^1W^{1\mu} + W_\mu^2W^{2\mu})$$

$$m_W = \frac{1}{2}g_Wv$$

$$\frac{v^2}{8} (A_{\mu}, Z_{\mu}) \begin{pmatrix} 0 & 0 \\ 0 & g_W^2 + g'^2 \end{pmatrix} \begin{pmatrix} A^{\mu} \\ Z^{\mu} \end{pmatrix}$$

$$m_A = 0 \qquad m_Z = \frac{v}{2} \sqrt{g_W^2 + g'^2}$$



Spontaneous symmetry breaking in the SM

We give mass to the gauge bosons through the Higgs mechanism: generate mass terms from t kinetic energy term of a scalar doublet field Φ that undergoes a broken-symmetry process.

Introduce a complex scalar doublet: four scalar real fields (why will become clear later)

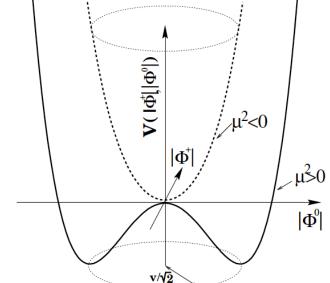
$$\Phi = \begin{pmatrix} \phi^{+} \\ \phi^{0} \end{pmatrix}, \qquad Y(\Phi) = 1$$

$$\mathcal{L}_{\text{Higgs}} = (D_{\mu}\Phi)^{\dagger}(D^{\mu}\Phi) - V(\Phi^{\dagger}\Phi)$$

$$D^{\mu} = \partial^{\mu} - igW_{i}^{\mu}\frac{\sigma^{i}}{2} - ig'\frac{Y(\Phi)}{2}B^{\mu}$$

$$V(\Phi^{\dagger}\Phi) = -\mu^{2}\Phi^{\dagger}\Phi + \lambda(\Phi^{\dagger}\Phi)^{2}, \qquad \mu^{2}, \lambda > 0$$

$$\text{Notice the "wrong" mass sign.}$$



$$V\left(\Phi^{\dagger}\Phi\right)$$
 is $SU(2)_L \times U(1)_Y$ symmetric.

- The reason why $Y(\Phi) = 1$ is not to break electric-charge conservation.
- Charge assignment for the Higgs doublets is done according to $Q = T_3 + Y/2$.



Fermion mass generation

A direct mass term is not invariant under $SU(2)_L$ or $U(1)_Y$ gauge transformation

$$m_f \bar{\psi} \psi = m_f \left(\bar{\psi}_R \psi_L + \bar{\psi}_L \psi_R \right)$$

Generate fermion masses through Yukawa-type interactions terms

$$\mathcal{L}_{\text{Yukawa}} = -\Gamma_d^{ij} \bar{Q}_L^{\prime i} \Phi d_R^{\prime j} - \Gamma_d^{ij*} \bar{d}_R^{\prime i} \Phi^{\dagger} Q_L^{\prime j}$$

$$-\Gamma_u^{ij} \bar{Q}_L^{\prime i} \Phi_c u_R^{\prime j} + \text{h.c.}$$

$$-\Gamma_e^{ij} \bar{L}_L^i \Phi e_R^j + \text{h.c.}$$

$$-\Gamma_\nu^{ij} \bar{L}_L^i \Phi_c \nu_R^j + \text{h.c.}$$

$$-\Gamma_\nu^{ij} \bar{L}_L^i \Phi_c \nu_R^j + \text{h.c.}$$

where Q', u' and d' are quark fields that are generic linear combination of the mass eigenstates u and d and Γ_u , Γ_d and Γ_e are 3×3 complex matrices in generation space, spanned by the indices i and j.

 $\mathcal{L}_{\text{Yukawa}}$ is Lorentz invariant, gauge invariant and renormalizable, and therefore it can (actually it must) be included in the Lagrangian.

Notice: neutrino masses can be implemented via the Γ_{ν} term. Since $m_{\nu} \approx 0$, we neglect it.



Expanding around the vacuum state

In the unitary gauge we have

$$\bar{Q}_{L}^{\prime i} \Phi d_{R}^{\prime j} = \left(\bar{u}_{L}^{\prime i} \ \bar{d}_{L}^{\prime i}\right) \begin{pmatrix} 0 \\ \frac{v+H}{\sqrt{2}} \end{pmatrix} d_{R}^{\prime j} = \frac{v+H}{\sqrt{2}} \, \bar{d}_{L}^{\prime i} \, d_{R}^{\prime j}$$

$$\bar{Q}_{L}^{\prime i} \Phi_{c} u_{R}^{\prime j} = \left(\bar{u}_{L}^{\prime i} \ \bar{d}_{L}^{\prime i}\right) \begin{pmatrix} \frac{v+H}{\sqrt{2}} \\ 0 \end{pmatrix} u_{R}^{\prime j} = \frac{v+H}{\sqrt{2}} \, \bar{u}_{L}^{\prime i} \, u_{R}^{\prime j}$$

and we obtain

$$\mathcal{L}_{\text{Yukawa}} = -\Gamma_{d}^{ij} \frac{v + H}{\sqrt{2}} \bar{d}_{L}^{'i} d_{R}^{'j} - \Gamma_{u}^{ij} \frac{v + H}{\sqrt{2}} \bar{u}_{L}^{'i} u_{R}^{'j} - \Gamma_{e}^{ij} \frac{v + H}{\sqrt{2}} \bar{e}_{L}^{i} e_{R}^{j} + \text{h.c.}$$

$$= -\left[M_{u}^{ij} \bar{u}_{L}^{'i} u_{R}^{'j} + M_{d}^{ij} \bar{d}_{L}^{'i} d_{R}^{'j} + M_{e}^{ij} \bar{e}_{L}^{i} e_{R}^{j} + \text{h.c.} \right] \left(1 + \frac{H}{v} \right)$$

$$M^{ij} = \Gamma^{ij} \frac{v}{\sqrt{2}}$$



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W and Z masses and Weinberg angle θ_W

Electroweak mixing angle (rotating W0 and B0 vector boson plane to get Z0 and photon)

Gives relationship between W and Z Boson masses

$$\cos heta_{
m W} = rac{m_{
m W}}{m_{
m Z}}$$

$$\cos heta_{
m W} = rac{g}{\sqrt{g^2 + g'^2}}$$

