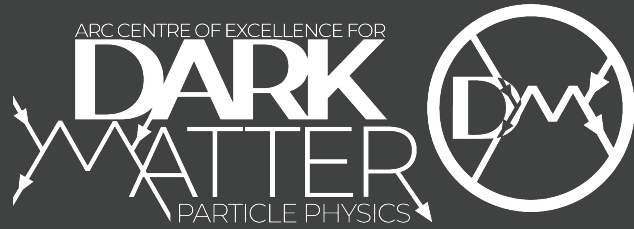


# The Migdal effect in liquid noble dark matter experiments

Mitchell Institute Workshop 2022

**Jayden Newstead**  
*ARC Centre for Dark Matter Particle Physics  
The University of Melbourne*



# The Migdal effect in liquid noble dark matter experiments

Mitchell Institute Workshop 2022

## **Collaborators:**

Nicole Bell (Uni Melb)

James Dent (SHSU)

Rafael Lang (Purdue)

Alexander Ritter (Uni Melb)

Jason Kumar (Hawaii U.)

Bhaskar Dutta (TAMU)

Sumit Ghosh (TAMU)

arXiv:[2112.08514](https://arxiv.org/abs/2112.08514) - Calibrating the Migdal effect

arXiv:[2103.05890](https://arxiv.org/abs/2103.05890) - The Migdal effect from inelastic scattering

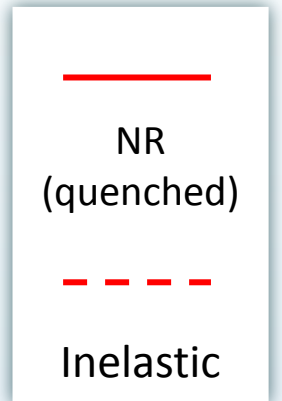
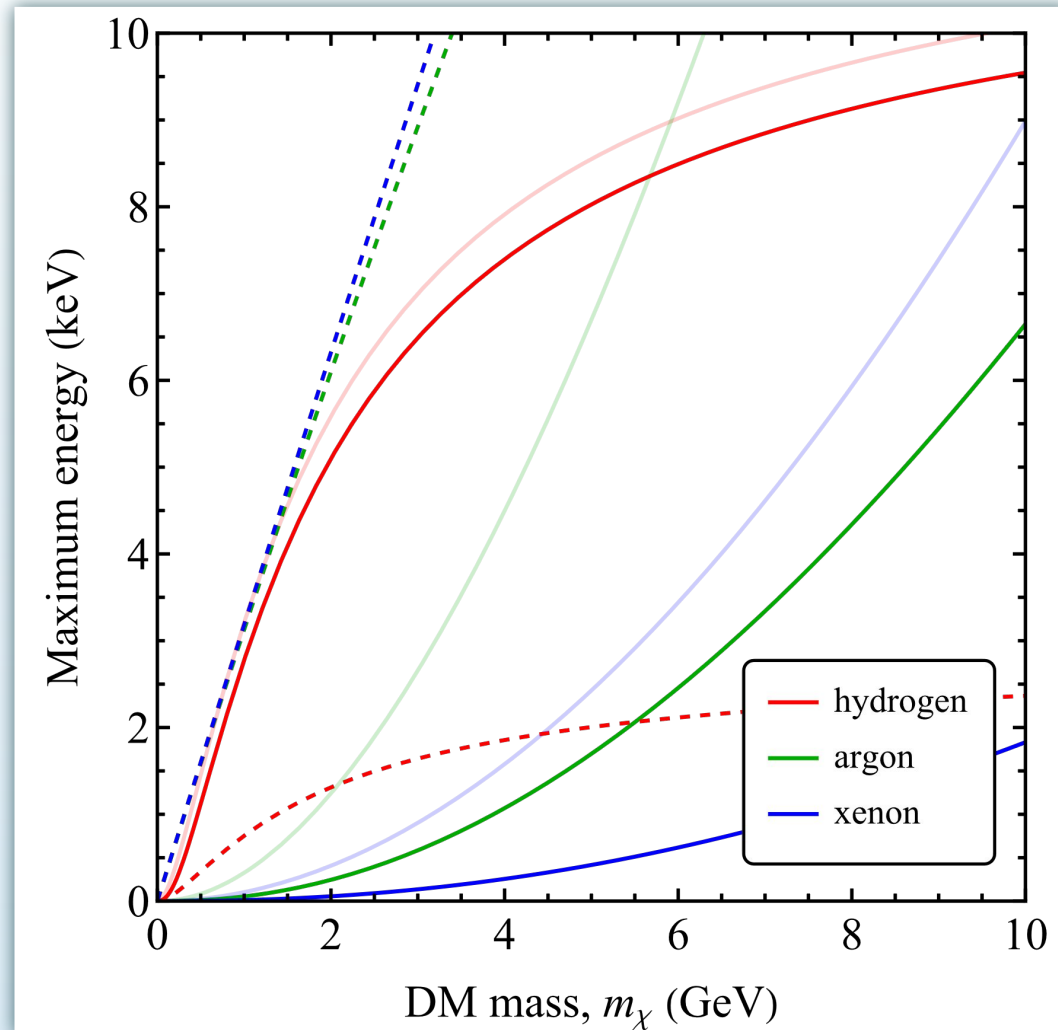
# Direct detection's kinematic problem

- Light dark matter does not pack much of a punch:

$$E_{R_{\max}} = \frac{2\mu_T^2}{m_T} v_{\max}^2$$

$$E_{EM_{\max}} = \frac{\mu_T}{2} v_{\max}^2$$

take  $v_{\max} = 760$  km/s

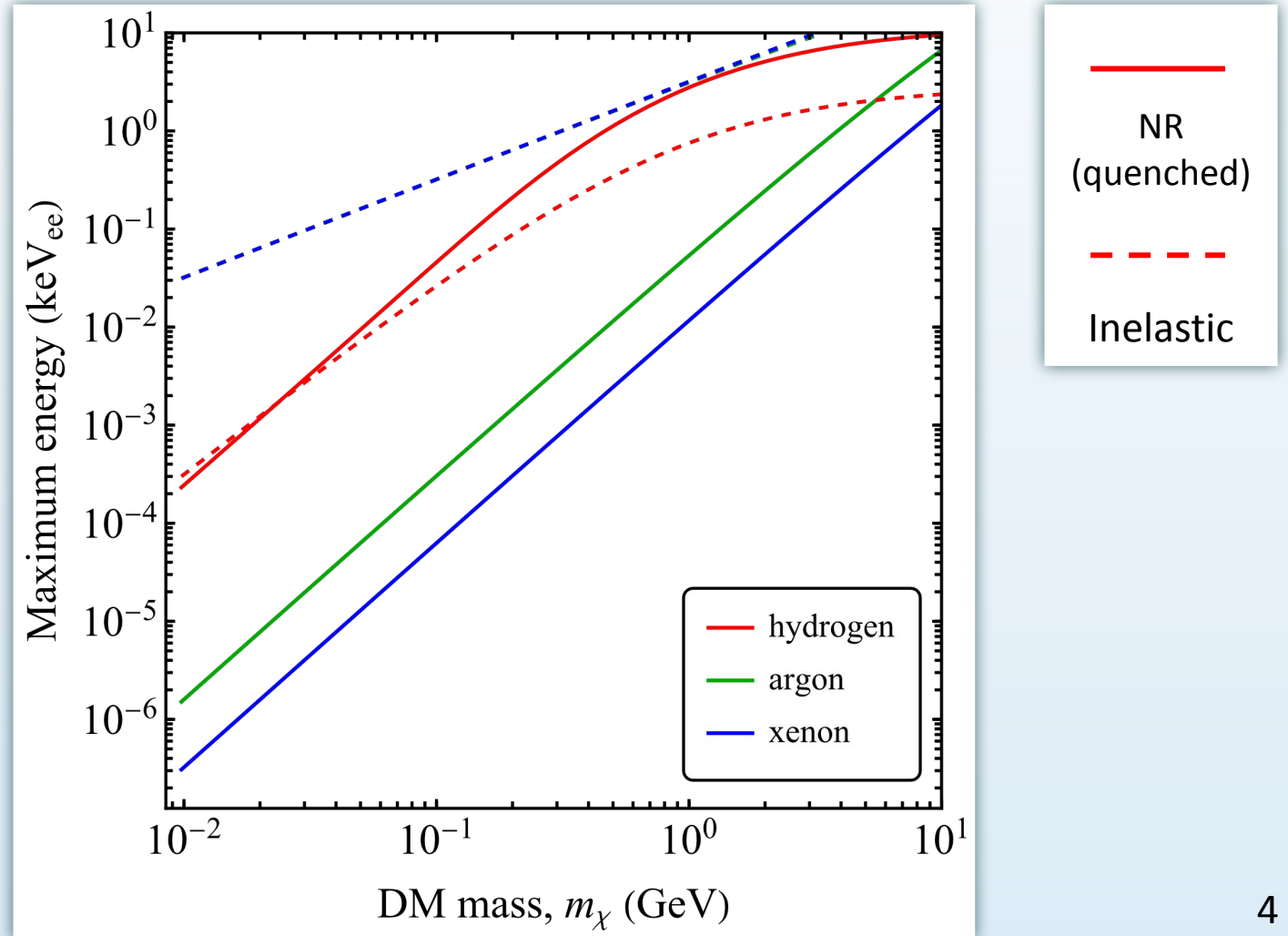


# Direct detection's kinematic problem

- Light dark matter does not pack much of a punch:

$$E_{R_{\max}} = \frac{2\mu_T^2}{m_T} v_{\max}^2$$
$$E_{EM_{\max}} = \frac{\mu_T}{2} v_{\max}^2$$

take  $v_{\max} = 760$  km/s



# A brief history of the Migdal effect

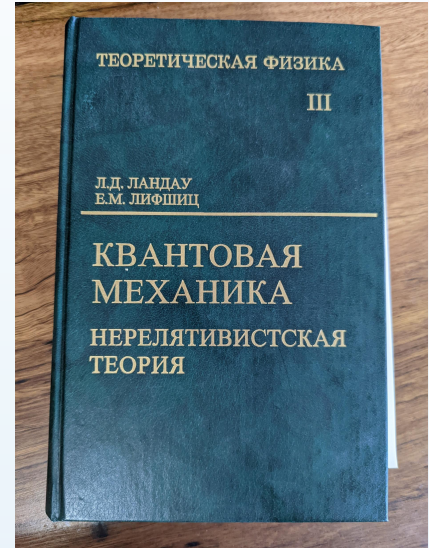
**1939:** A.B. Migdal, J. Phys. USSR 4 449

**1958:** Landau and Lifshitz Vol. 3: Quantum Mechanics, sec. 41:

2. Ядро атома, находящегося в нормальном состоянии, испытывает внезапный толчок, в результате которого оно приобретает скорость  $v$ , длительность толчка  $\tau$  предполагается малой как по сравнению с электронными периодами, так и по сравнению с  $a/v$ , где  $a$  — атомные размеры. Определить вероятность возбуждения атома под влиянием такого «встряхивания» (А. Б. Мигдал, 1939).

**2005:** J.D. Vergados and H. Ejiri, Phys. Lett. B 606, 313, [[hep-ph/0401151](https://arxiv.org/abs/hep-ph/0401151)]

**2018:** M. Ibe, W. Nakano, Y. Shoji and K. Suzuki, JHEP 1803 (2018) 194 [arXiv:1707.07258]



# A brief history of the Migdal effect

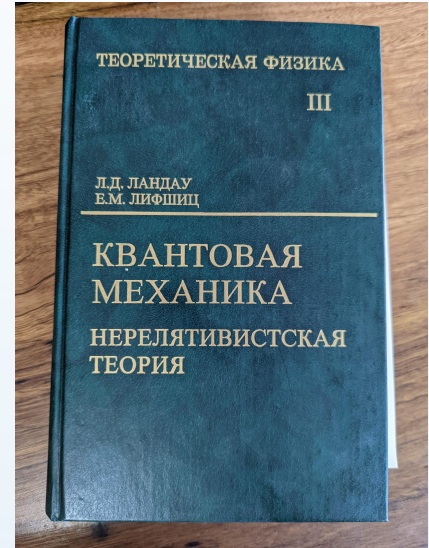
**1939:** A.B. Migdal, J. Phys. USSR 4 449

**1958:** Landau and Lifshitz Vol. 3: Quantum Mechanics, sec. 41:

**PROBLEM 2.** The nucleus of an atom in the normal state receives an impulse which gives it a velocity  $v$ ; the duration  $\tau$  of the impulse is assumed short in comparison both with the electron periods and with  $a/v$ , where  $a$  is the dimension of the atom. Determine the probability of excitation of the atom under the influence of such a “jolt” (A. B. MIGDAL 1939).

**2005:** J.D. Vergados and H. Ejiri, Phys. Lett. B 606, 313, [[hep-ph/0401151](https://arxiv.org/abs/hep-ph/0401151)]

**2018:** M. Ibe, W. Nakano, Y. Shoji and K. Suzuki, JHEP 1803 (2018) 194 [arXiv:1707.07258]



# Migdal rate calculation

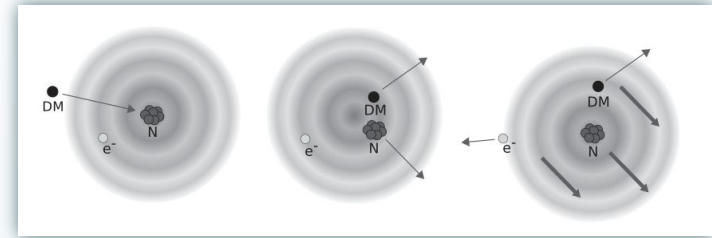
- What goes into the rate calculation?

$$\frac{d^2 R}{dE_{NR} dE_i} = \frac{d^2 R_{iT}}{dE_{NR} dE_i} \times |Z_{ion}|^2$$

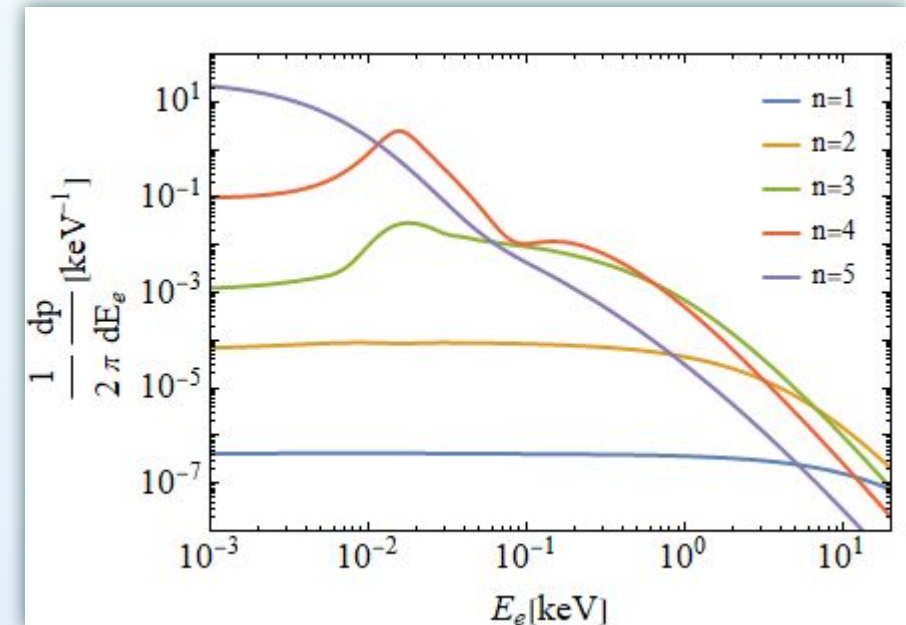
$$|Z_{ion}|^2 = \frac{1}{2\pi} \sum_{n,l} \int dE_e \frac{d}{dE_e} p_{qe}^c(nl \rightarrow (E_e))$$

- What does such an event look like?

$$E_{det} = \mathcal{L}E_R + E_e + E_{nl}$$



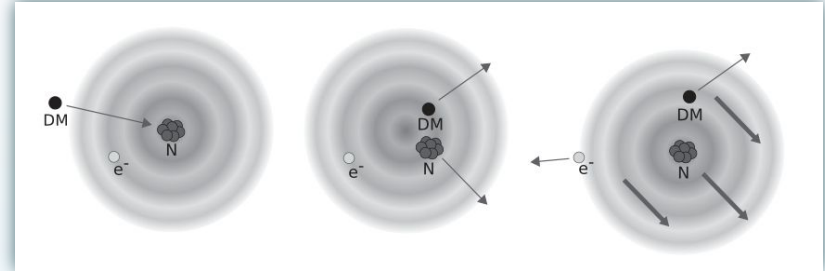
Dolan et al. PRL 2017



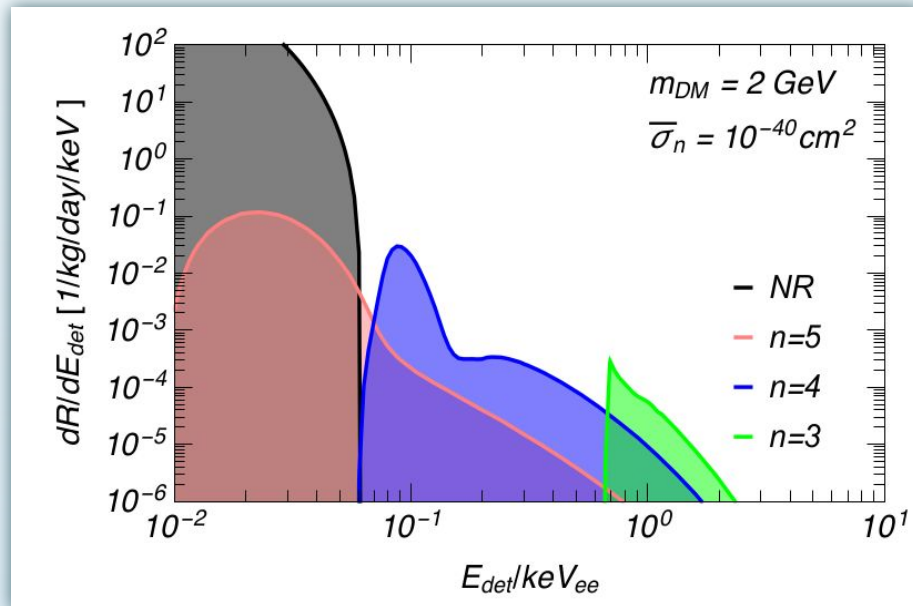
M. Ibe, W. Nakano, Y. Shoji, and K. Suzuki,  
arXiv:1707.07258

# Migdal rates and Limits

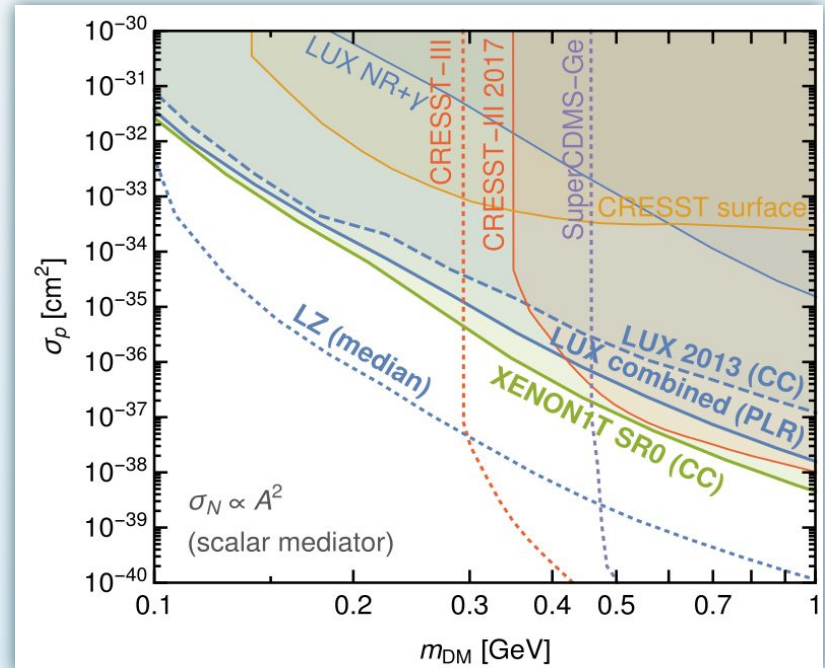
- The Migdal effect is atomic ionization or excitation due to a nuclear recoil
- Electron shakeoff has been observed during nuclear decay, but not due to scattering



Dolan et al.



M. Ibe, W. Nakano, Y. Shoji, and K. Suzuki,  
arXiv:1707.07258



M. J. Dolan, F. Kahlhoefer, and C. McCabe, (PRL)  
arXiv:1711.09906

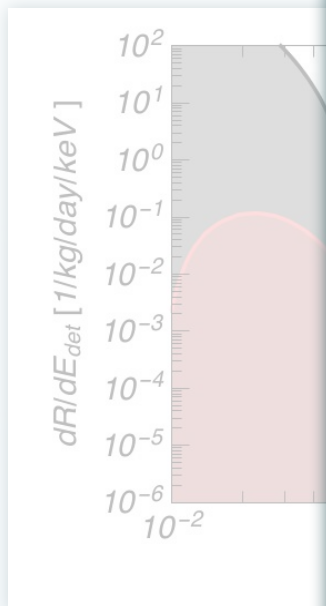


# Migdal rates and Limits

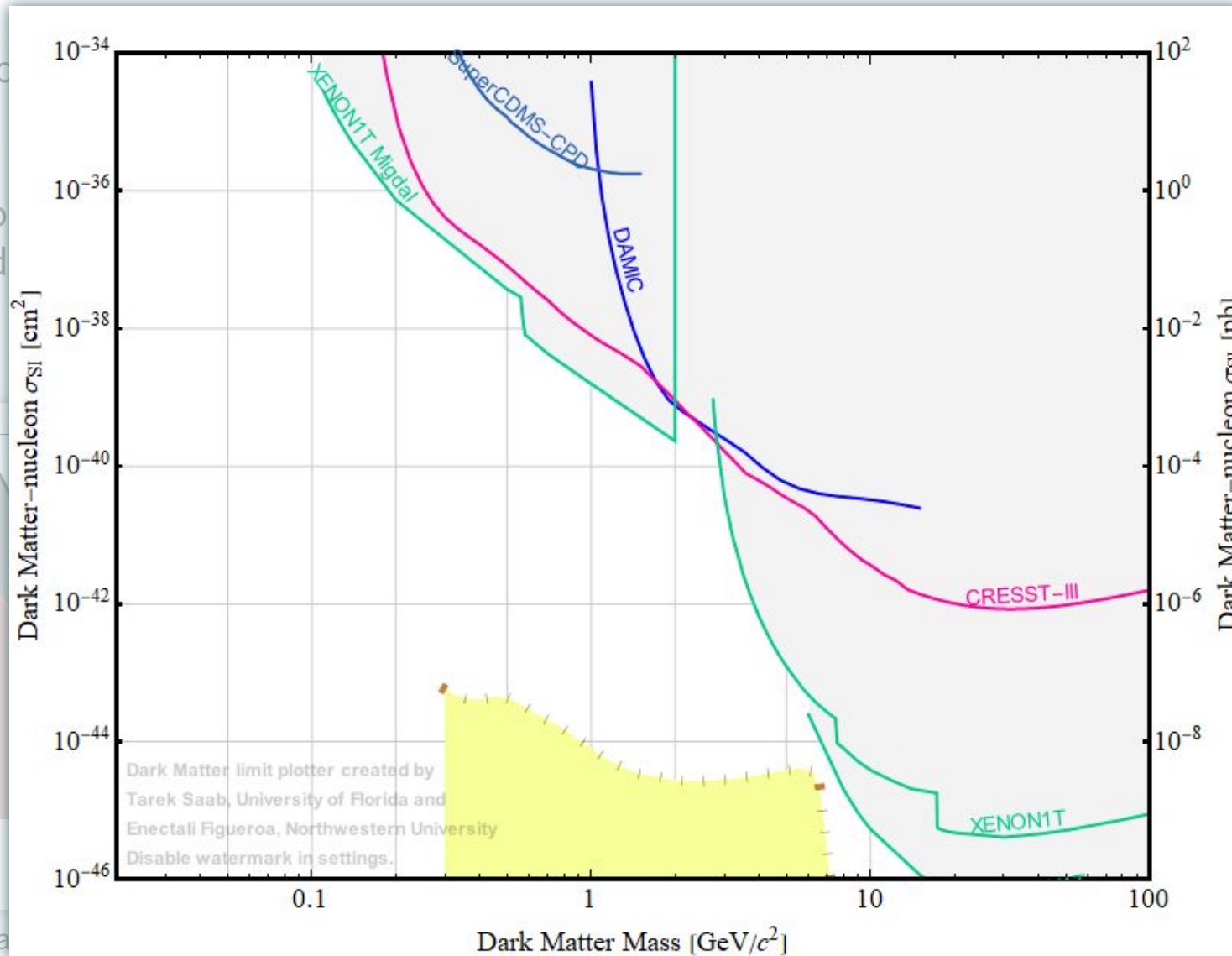
- The Migdal effect produces a nuclear recoil
- Electron shakeoff leads to electron decay, but not d



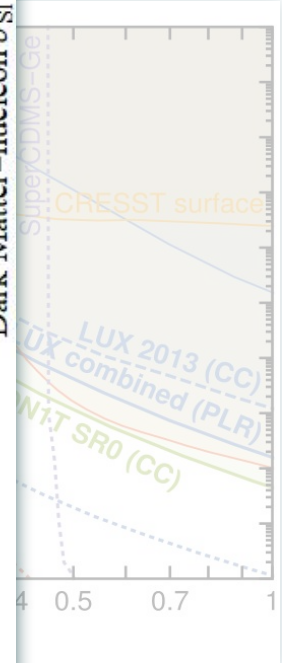
Dolan et al.



M. Ibe, W. Na  
arXiv:1707.07258



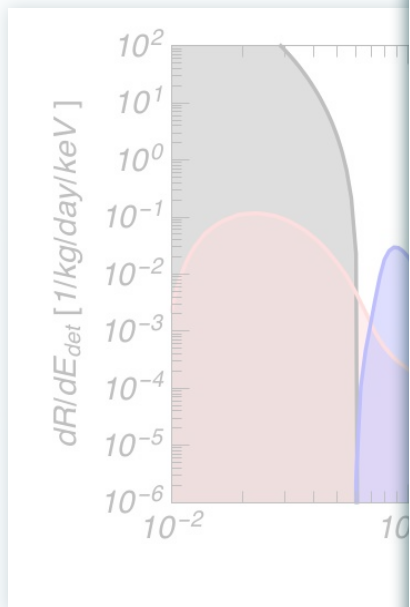
arXiv:1711.09906



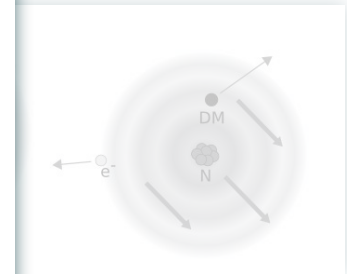
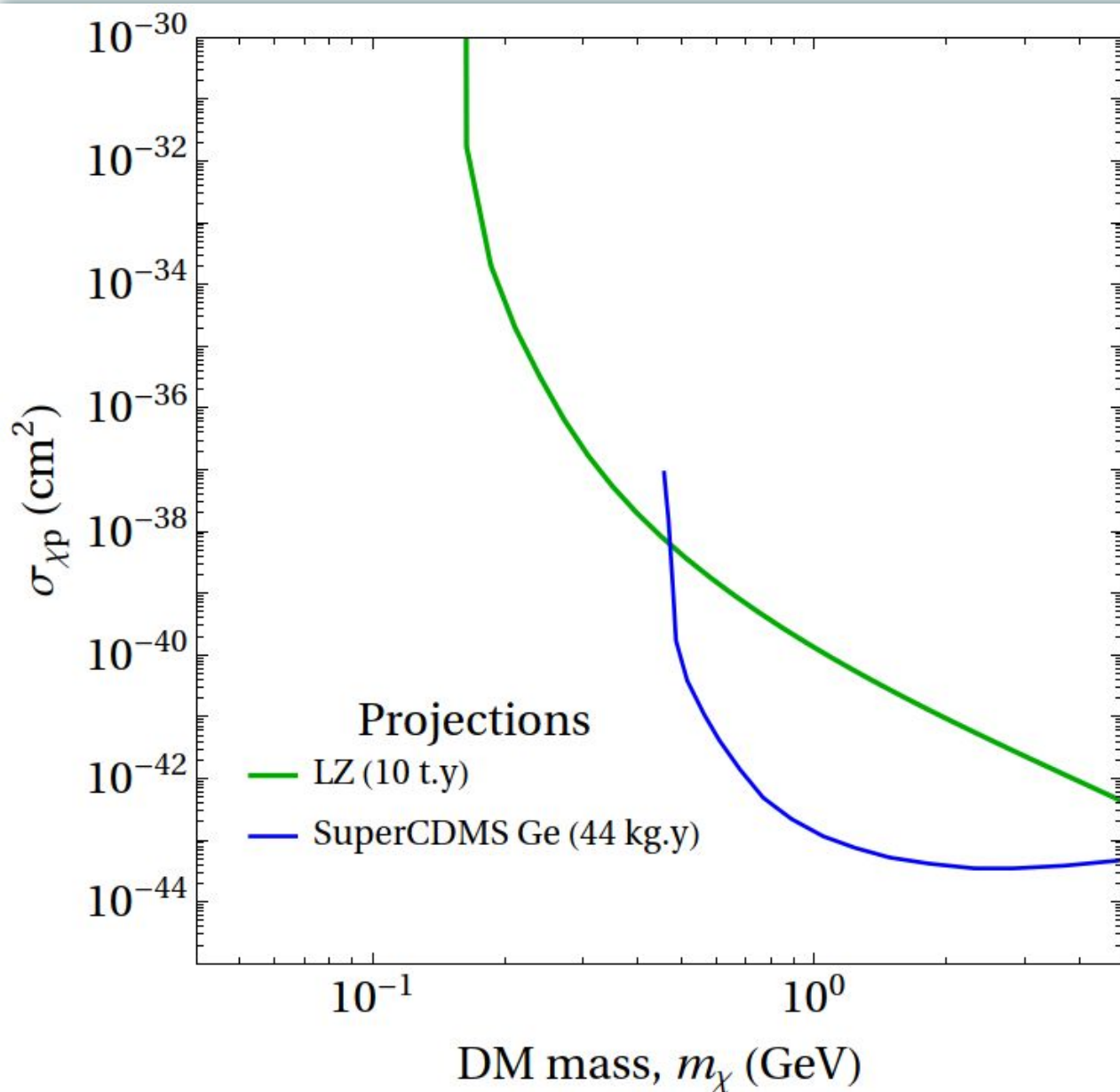
McCabe, (PRL)

# Migdal rates and Limits

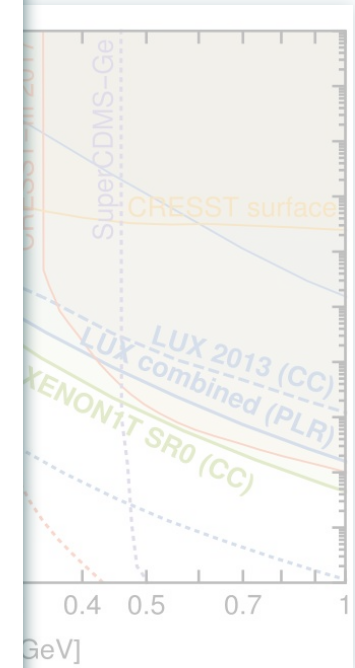
- The Migdal effect is a nuclear recoil
- Electron shakeoff has a decay, but not due to



M. Ibe, W. Nakano  
arXiv:1707.07258



Dolan et al.

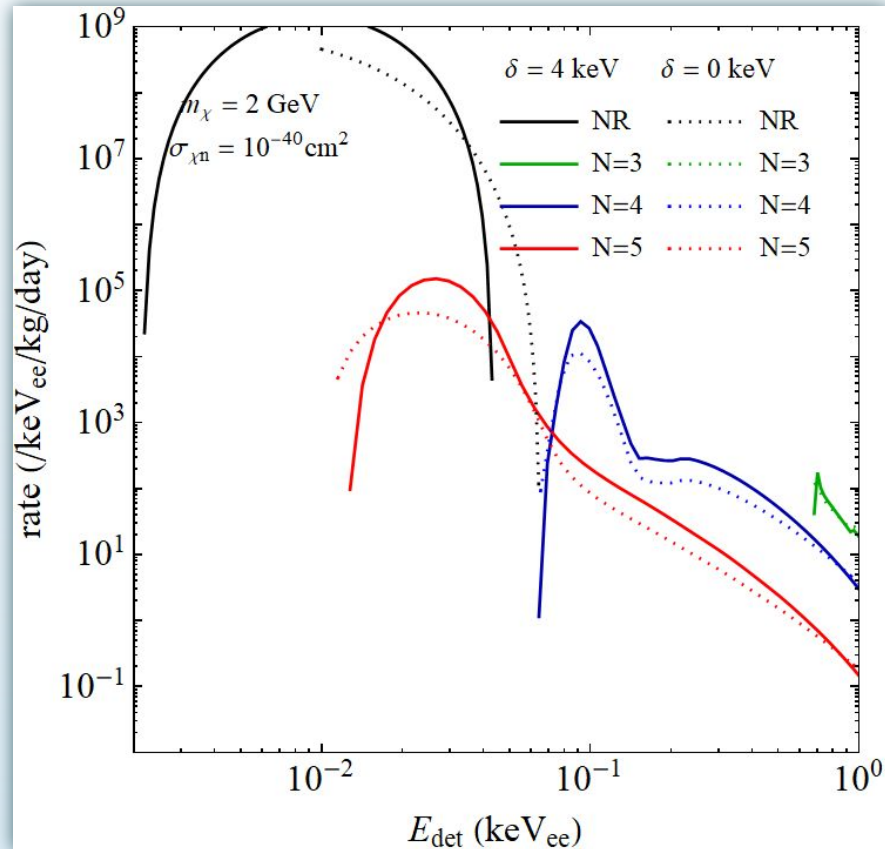


and C. McCabe, (PRL)

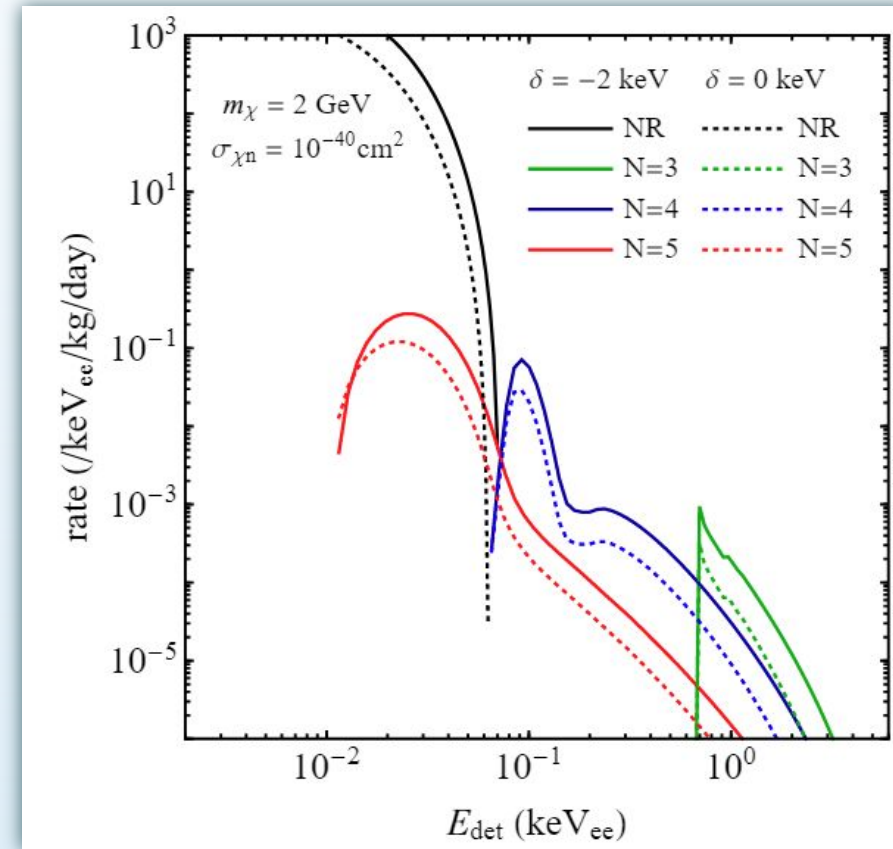
# The Migdal effect with inelastic DM

- Keeping mass and cross section constant, the largest effect is on the kinematic endpoint

endothermic

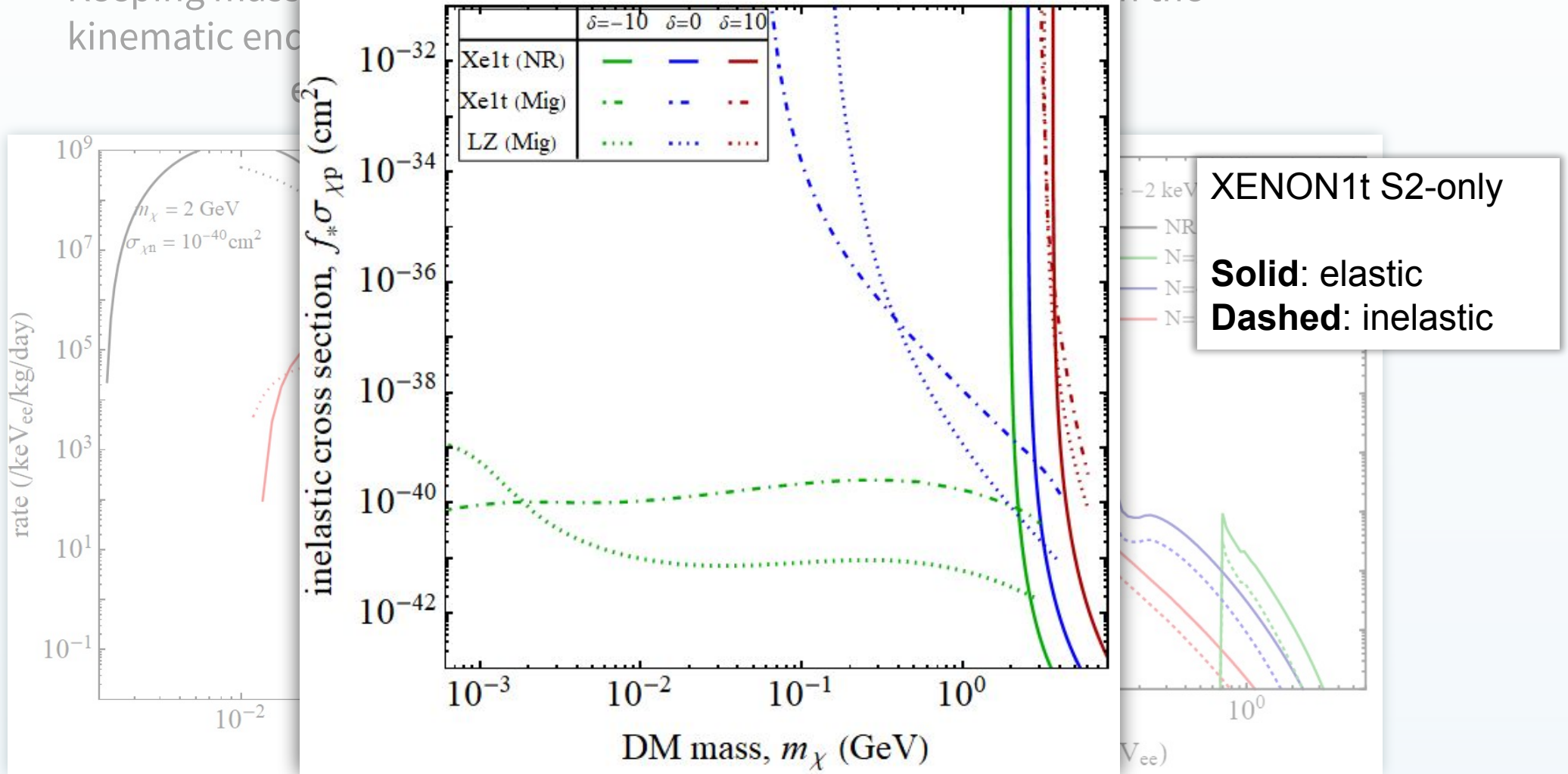


exothermic

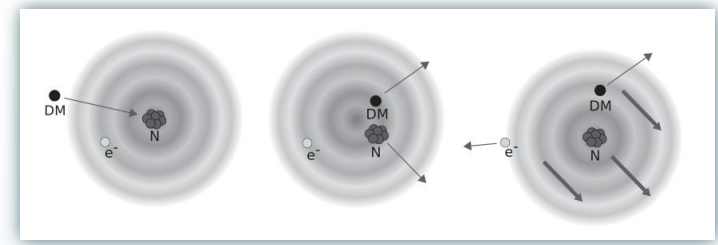


# The Migdal effect with inelastic DM

- Keeping mass and cross section constant, the largest effect is on the kinematic end



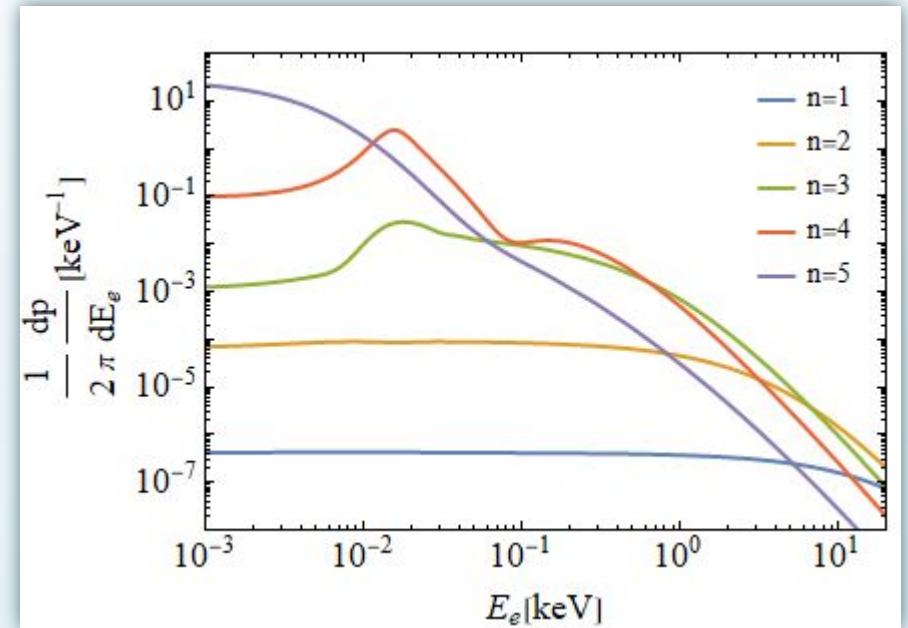
# Migdal rate calibration



Two components of the calculation we want to calibrate:

1. The atomic ionization factors  
(Data driven methods exist for solid state targets via the EELS)
2. The detector response to a Migdal event

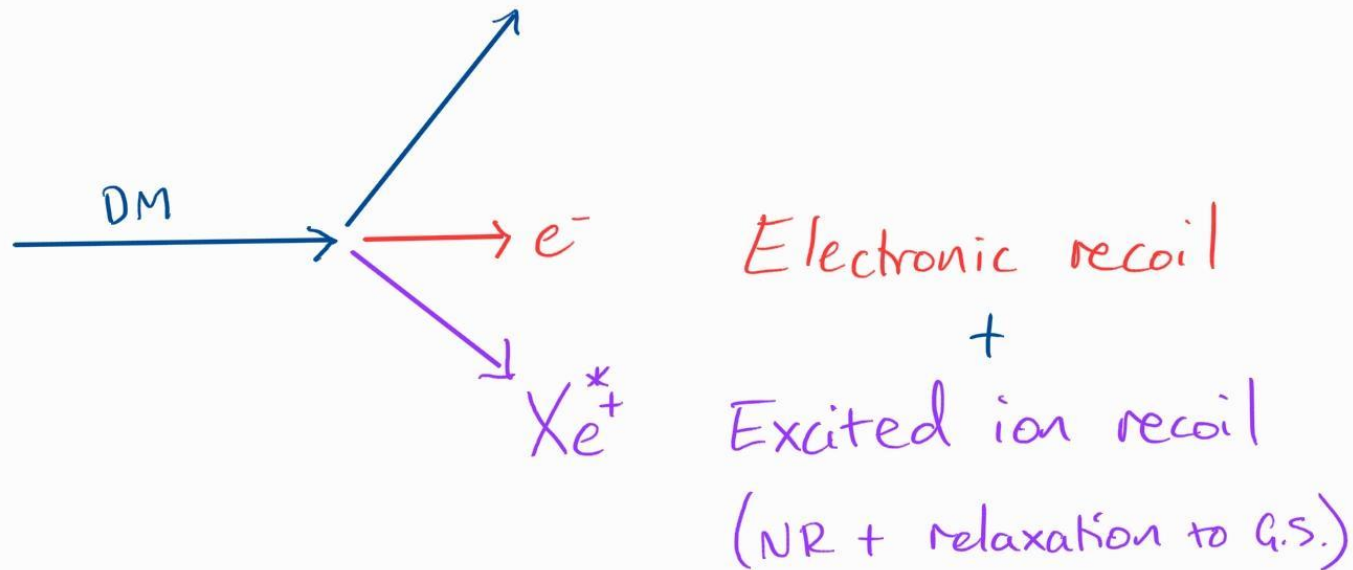
$$E_{\text{det}} = \mathcal{L}E_R + E_e + E_{nl}$$



M. Ibe, W. Nakano, Y. Shoji, and K. Suzuki,  
arXiv:1707.07258

# Quanta production for a Migdal event

How does a Migdal event change the signal production process?



**→ A calibration is needed**

# Calibrating the Migdal effect

- Use nuclear recoils from neutral particles:

**neutrons:**

$$E_{R,\max} = \frac{4\mu_T^2 E_n}{m_n m_T}$$

$$E_{\text{EM},\max} = \frac{\mu_T E_n}{m_n}$$

**neutrinos:**

$$E_{R,\max} = \frac{2E_\nu^2}{m_T + 2E_\nu^2}$$

$$E_{\text{EM},\max} = E_\nu - E_R$$

Two proposals (that I'm aware of):

- The MIGDAL experiment will attempt to observe Migdal events with neutrons from a DD generator (2.5 MeV) in a gaseous  $\text{CF}_4$  optical TPC
- Kentaro Miuchi et al. who suggest using a LiBe reaction at AIST, producing 565 keV neutrons, and gaseous xenon and argon targets

# Calibrating the Migdal effect

- Use nuclear recoils from neutral particles:

**neutrons:**

$$E_{R,\max} = \frac{4\mu_T^2 E_n}{m_n m_T}$$

**neutrinos:**

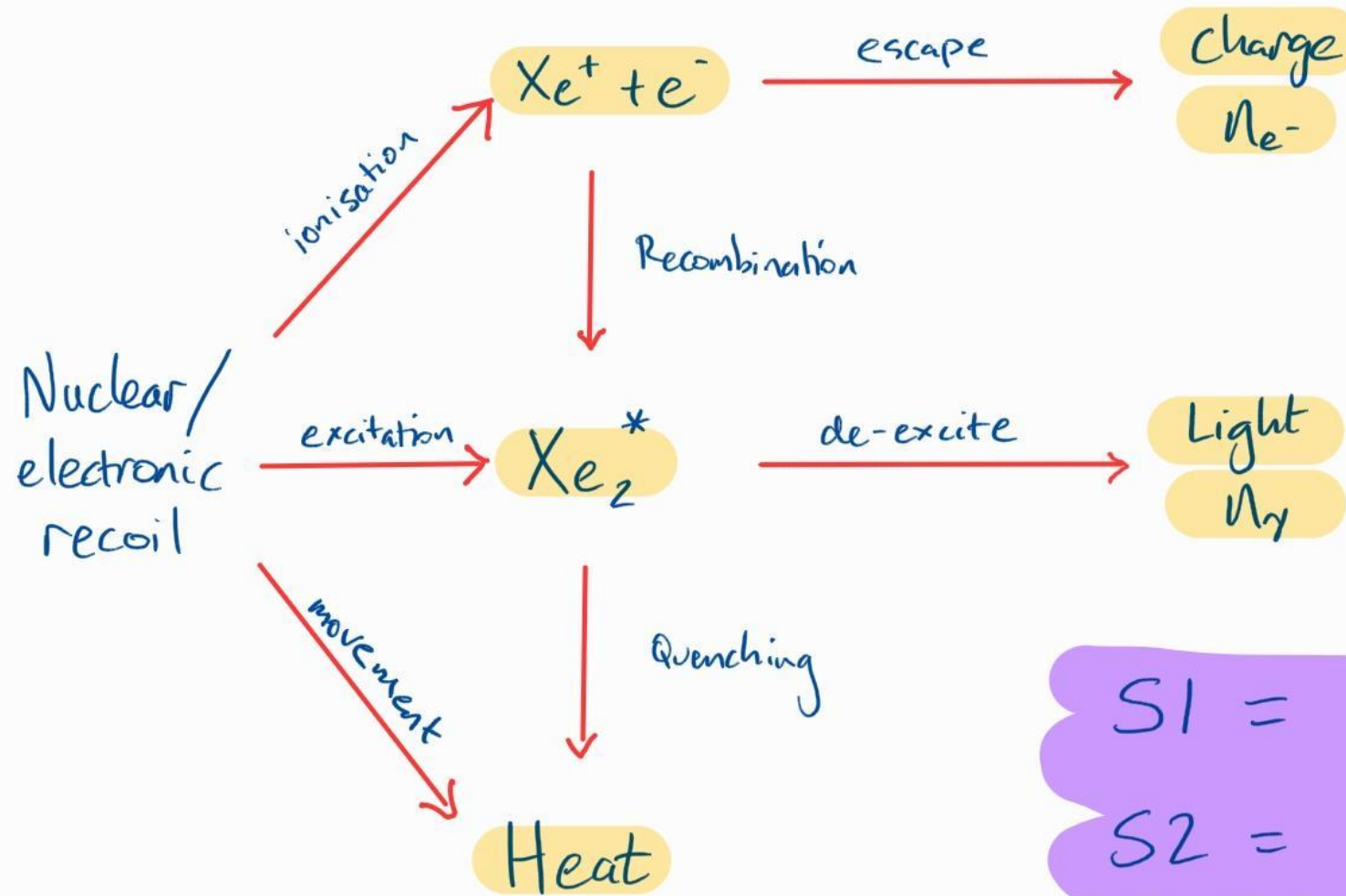
$$E_{R,\max} = \frac{2E_\nu^2}{m_T + 2E_\nu}$$

These proposals could provide a validation of theoretical calculation of the atomic ionization probabilities, **however:**

- It is *higher energy recoils* than a low mass DM would induce
- Theoretical calculations of a '*molecular*' Migdal effect have not been performed (and would be difficult)
- Does not calibrate the *detector response* of Migdal event in a dark matter detector



# Signal production



Use:  
**Nobel**  
**Element**  
**Simulation**  
**Technique**  
to model this process

$$S1 = g_1 n_\gamma$$

$$S2 = g_2 n_{e^-}$$

# Anatomy of a dual-phase xenon detector

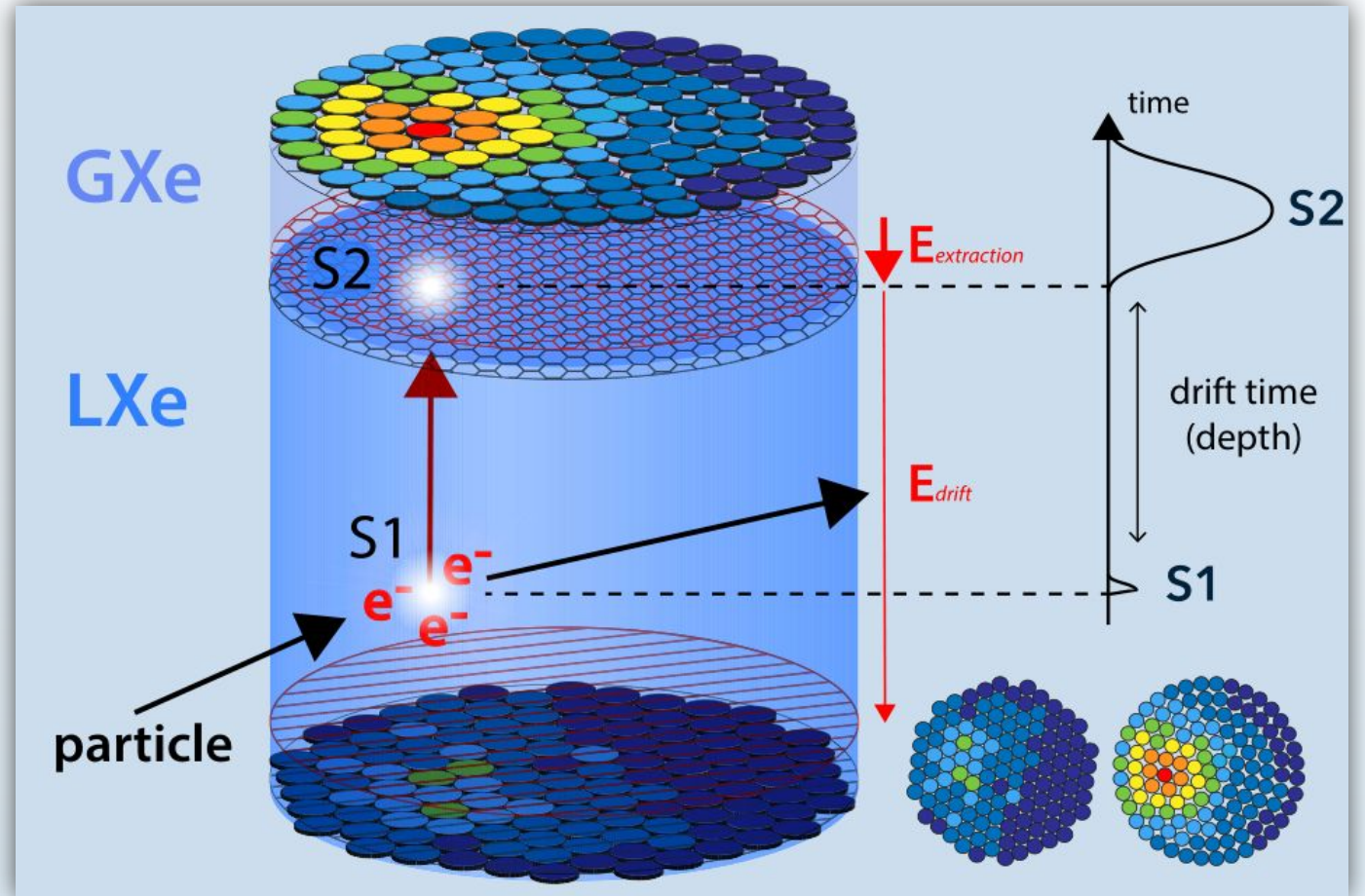
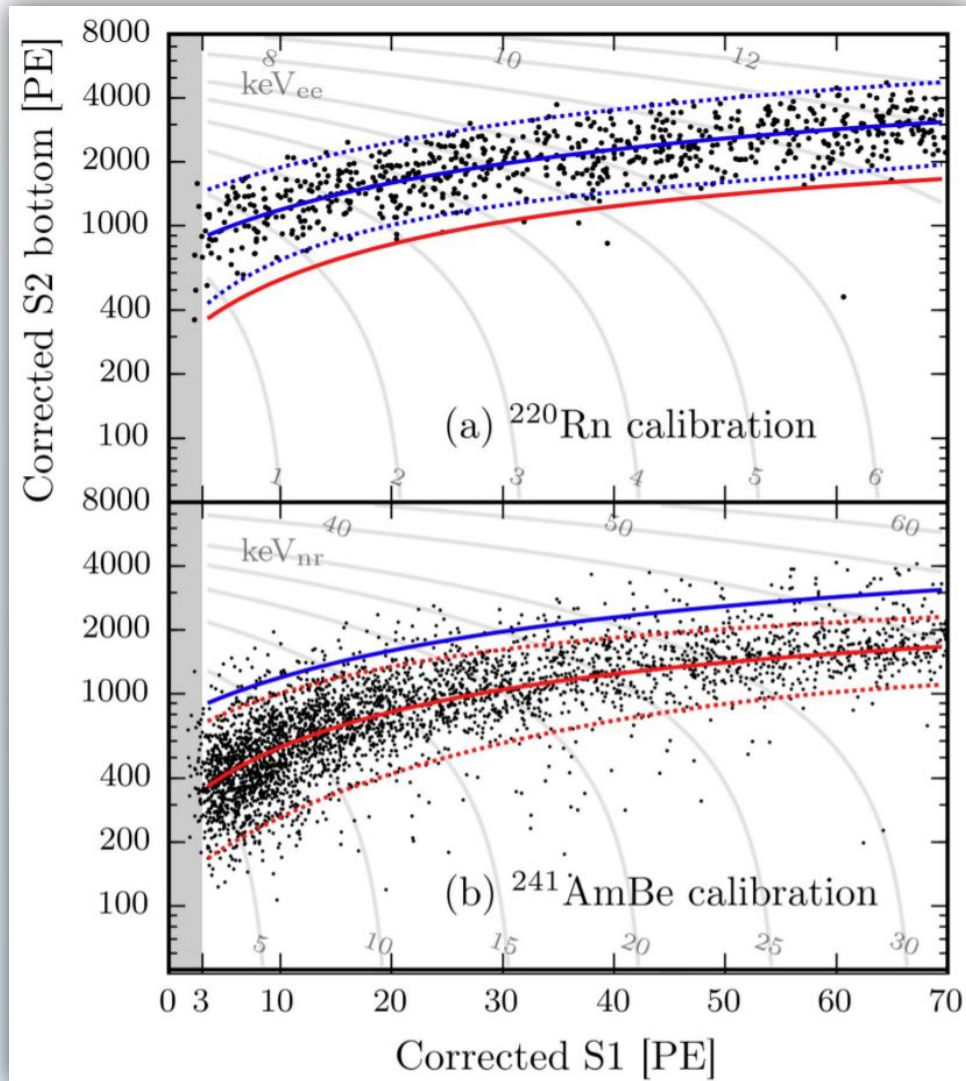
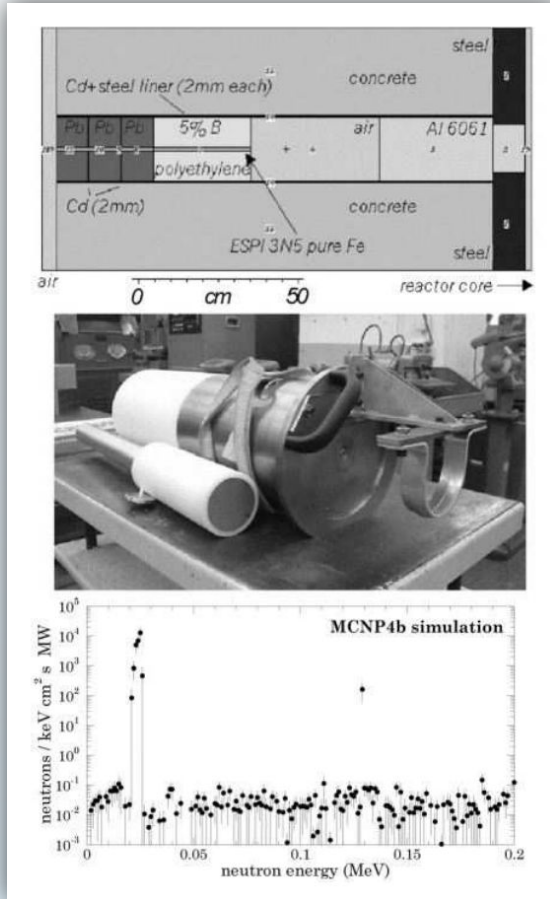


Image: XENON1t collaboration

# Potential low-energy neutron sources

## Nuclear reactor + filter



arXiv:nucl-ex/0701011

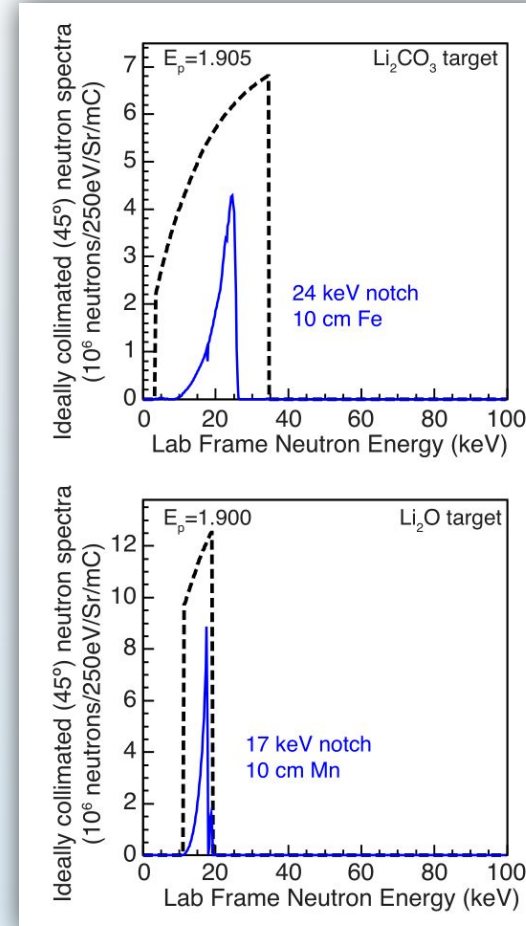
### Pros:

- Large flux
- Continuous operation

### Cons:

- Gamma backgrounds

## Li + p near threshold + filter



arXiv:1403.1285

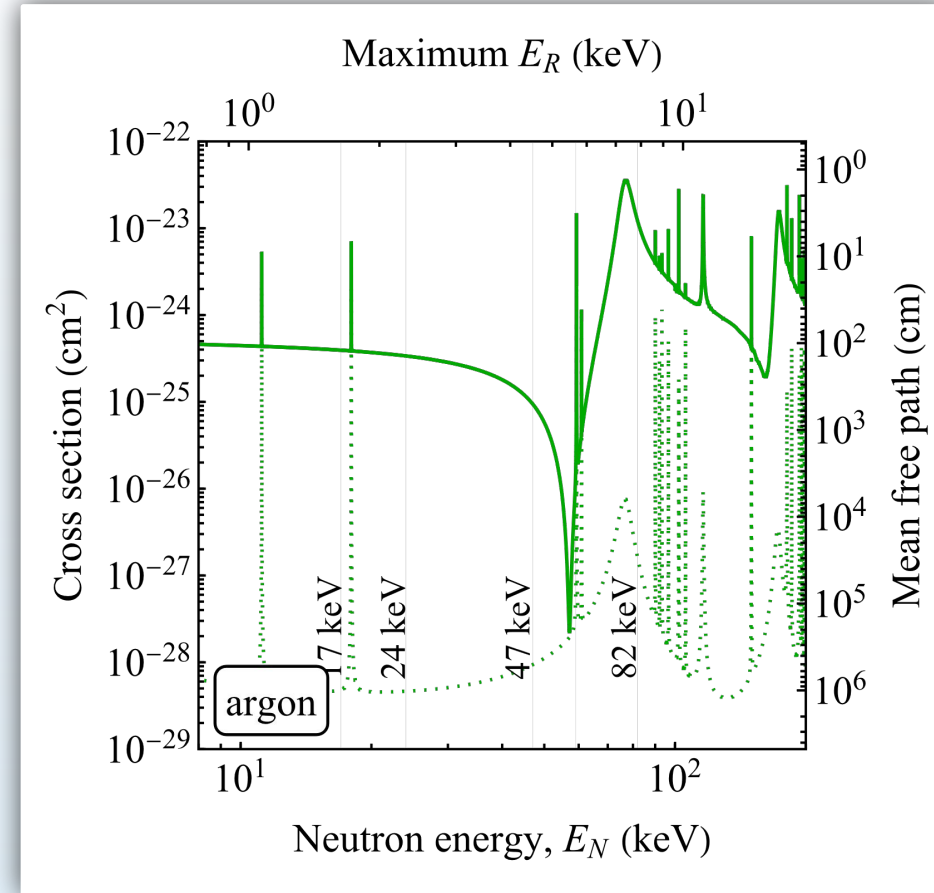
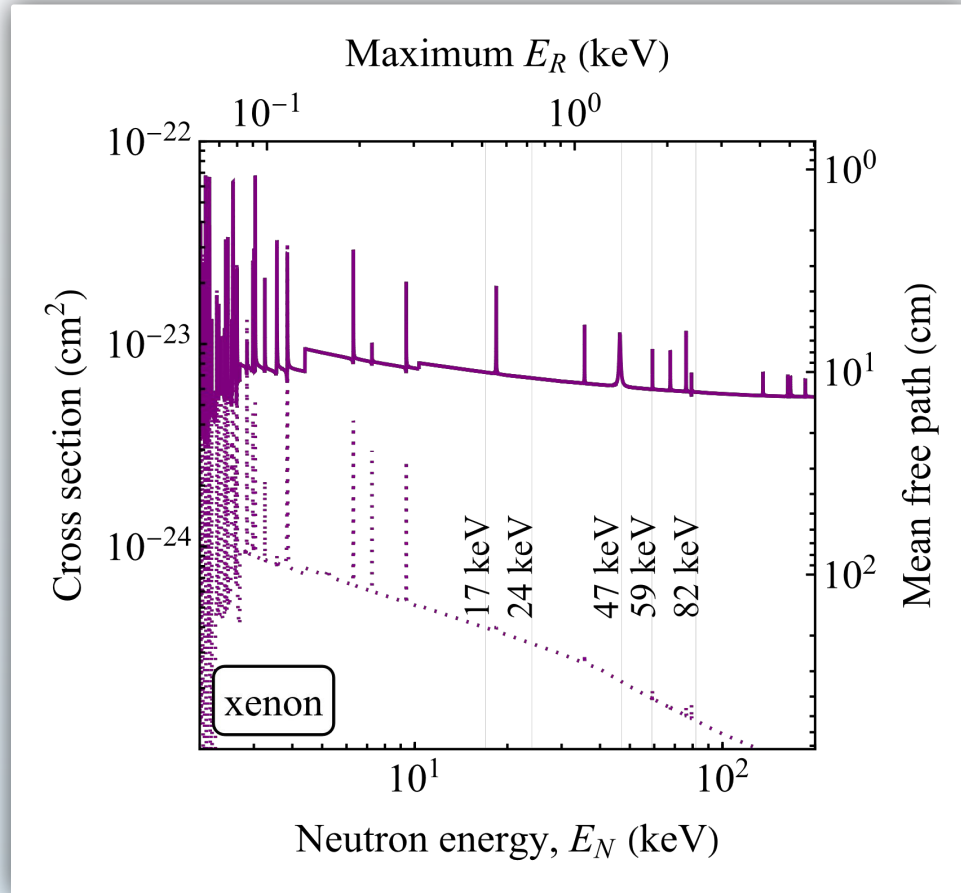
### Pros:

- Pulsed operation

### Cons:

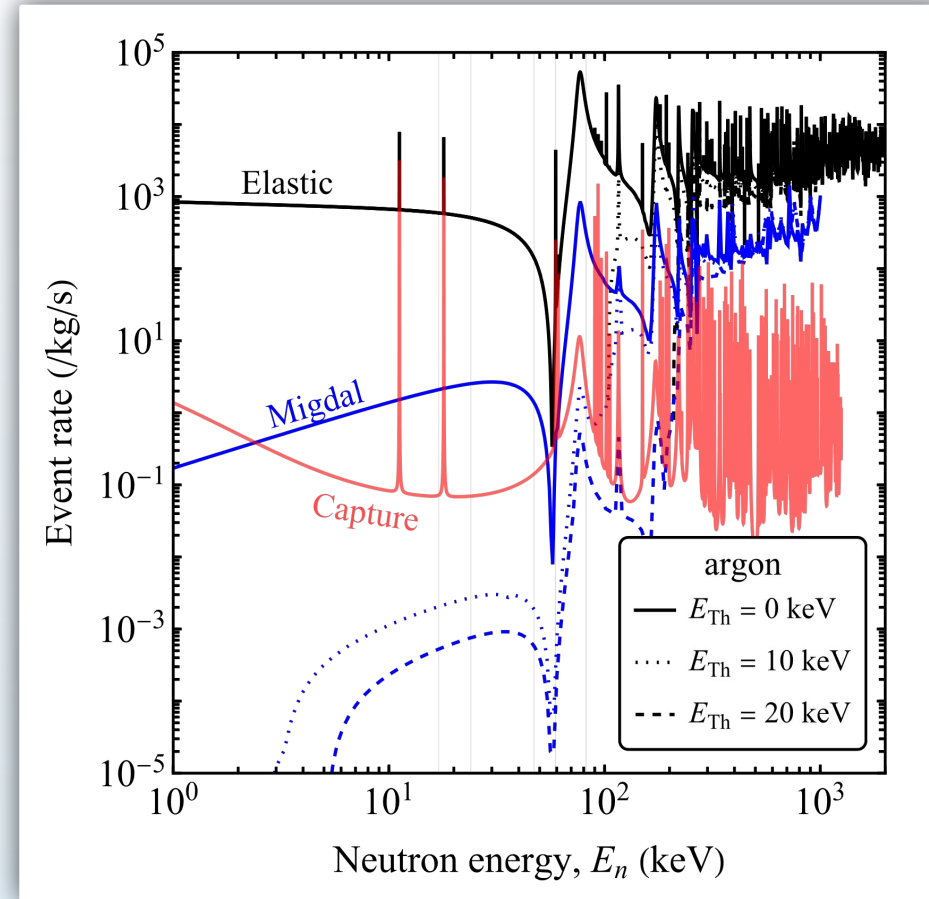
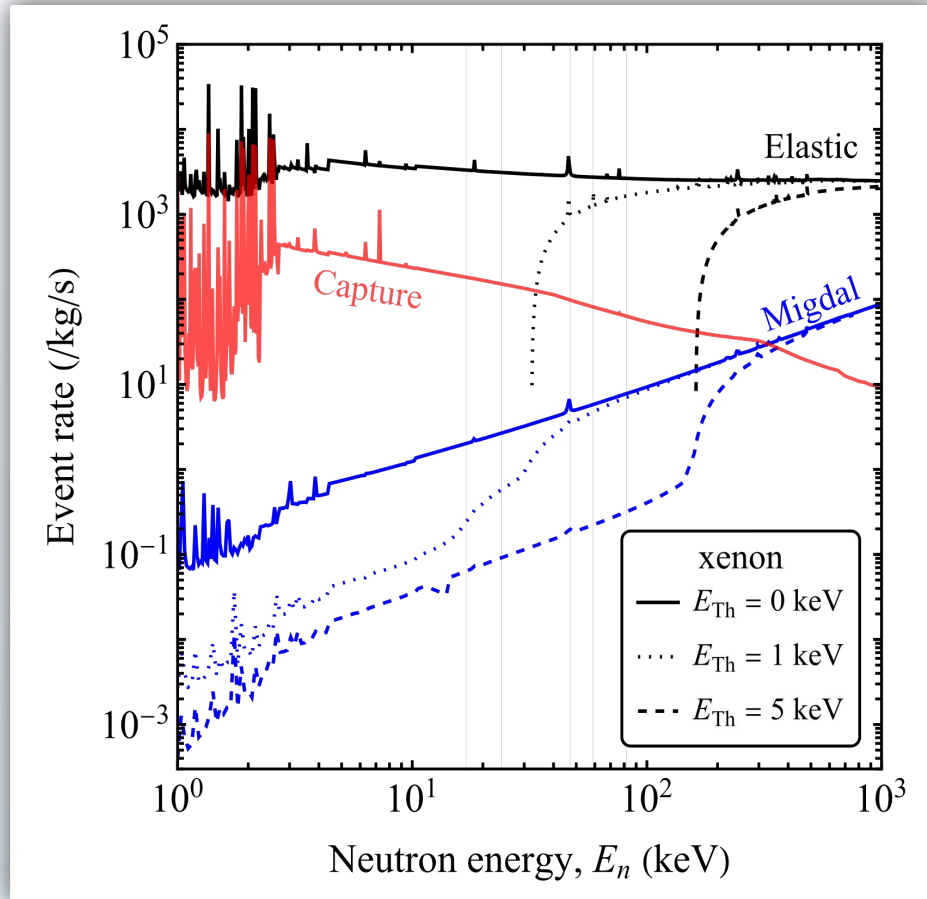
- Larger fluxes may require large/cooled targets

# The neutron scattering landscape



- Radiative capture of neutrons will be a significant background
- Inelastic scattering is  $>100$  keV threshold for all but xenon-129

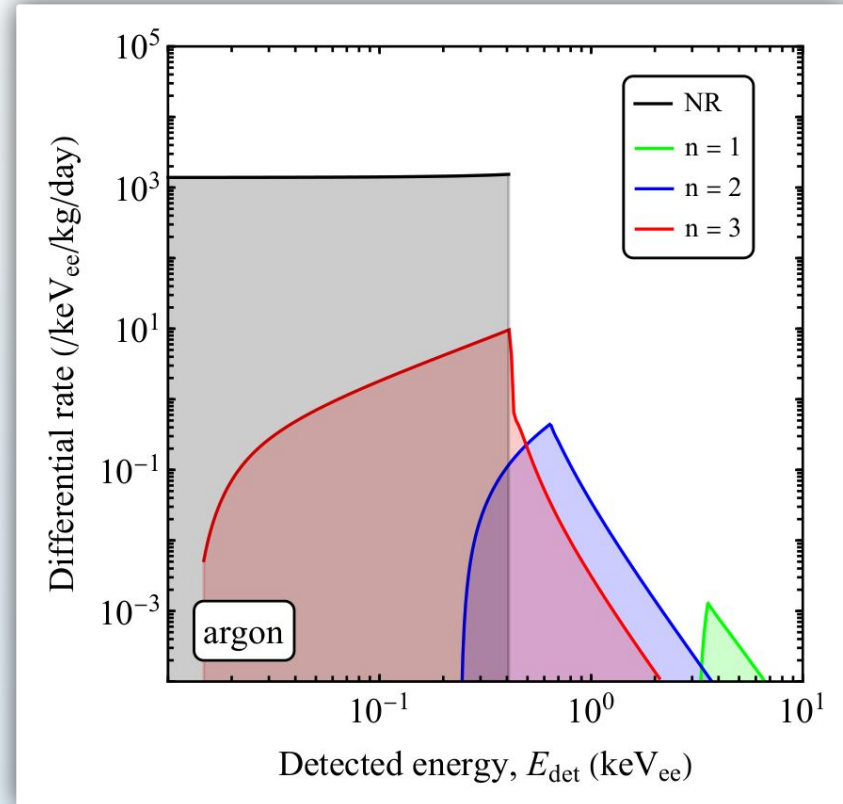
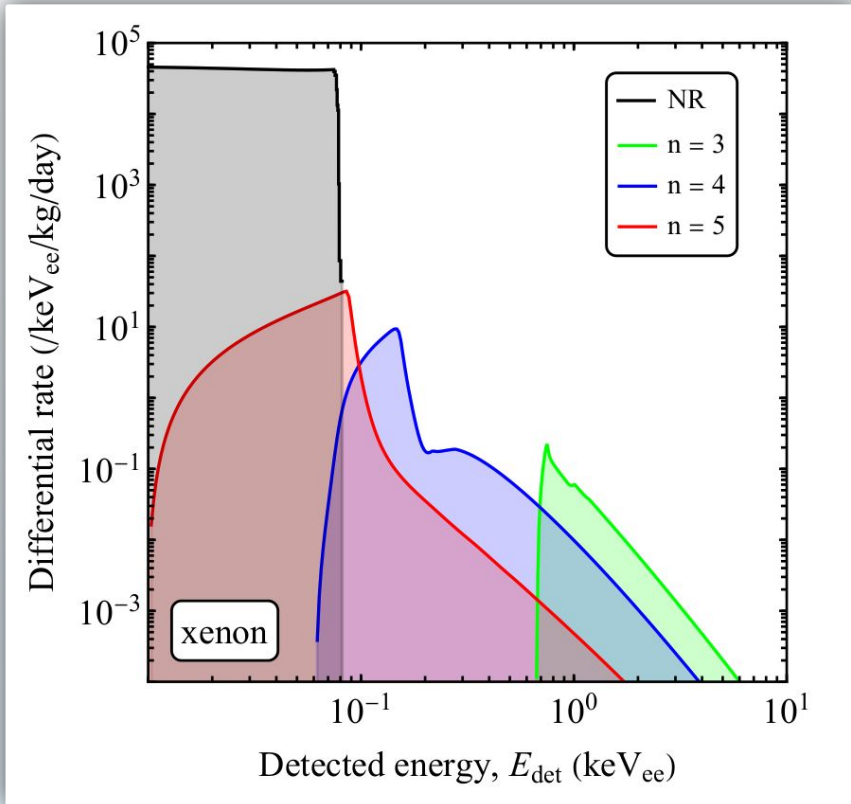
# The neutron scattering landscape



- Radiative capture of neutrons will be a significant background
- Inelastic scattering is  $>100$  keV threshold for all but xenon-129

# Low-energy neutron Migdal rates

$E = 17 \text{ keV}$  neutrons, flux =  $100 \text{ n/cm}^2/\text{s}$



## Total rates (raw):

Nuclear:  $3,300 \text{ events/kg/s}$

Migdal:  $2 \text{ events/kg/s}$

$600 \text{ events/kg/s}$

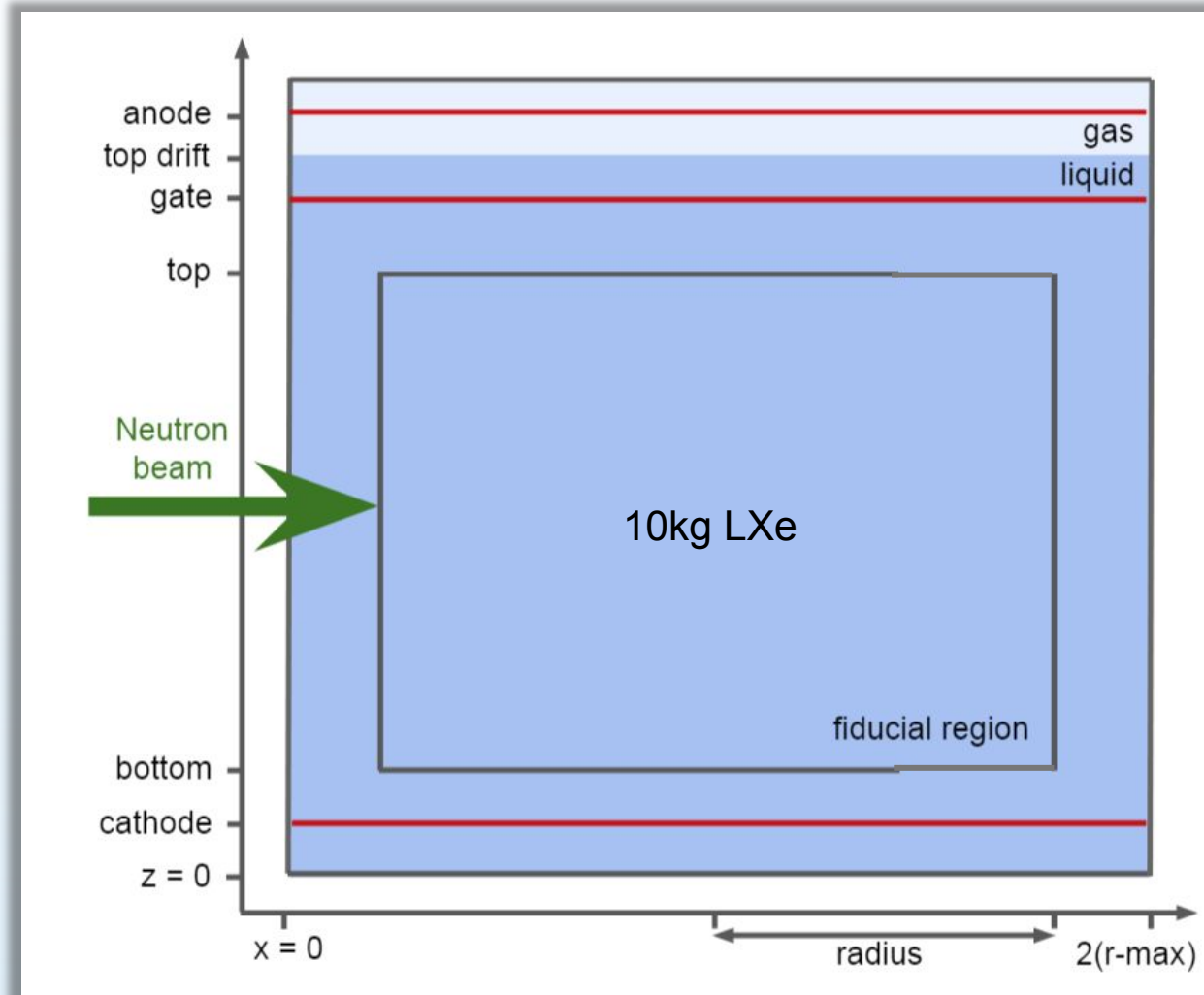
$2 \text{ events/kg/s}$

# Simulation of a neutron beam source

Gaussian  
neutron beam:

FWHM = 6cm  
Peak flux =  $10^8$ n/hr  
(avg 100n/cm<sup>2</sup>/s)

Modelled on Barbeau  
et al.

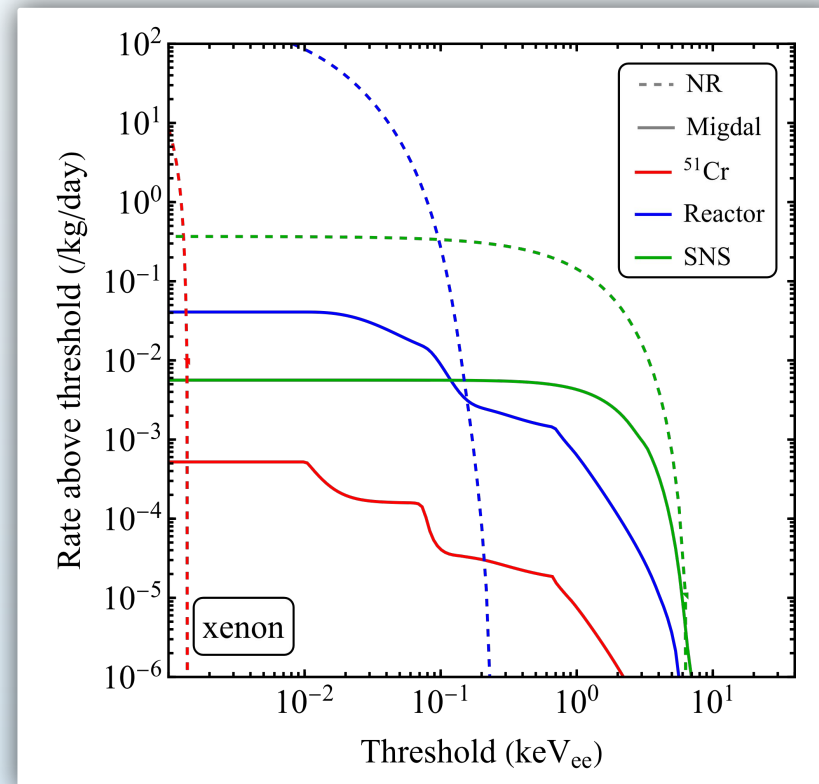
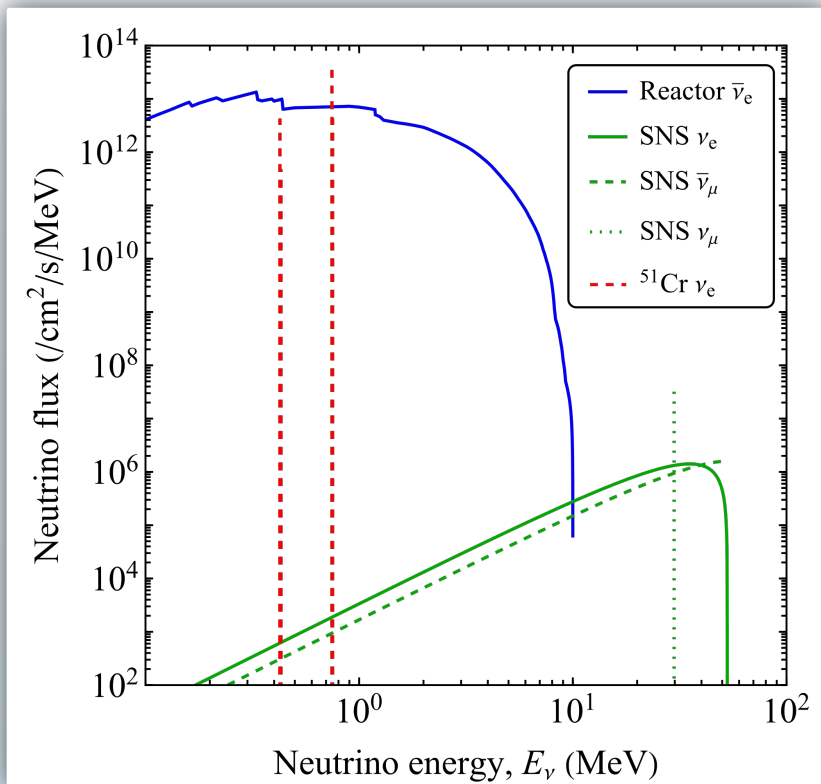


dimension	position (mm)
$r_{\max}$	120.
radius	100.
cathode	20.0
bottom	40.0
top	160.
gate	190.
top drift	195.
anode	200.

parameter	value
$g_1$	0.15 PE/ $\gamma$
$g_2$	24 PE/ $e^-$
field	300 V/cm
$e^-$ lifetime	350. $\mu$ s
min S1	2 phd
min S2	250 phd
no. PMTs	60

# Low-energy neutrino sources

source	flux (/cm <sup>2</sup> /s)	max $E_\nu$ (MeV)	max $E_R^{\text{Xe}}$ (keV)
nuclear reactor	$1.5 \times 10^{13}$	10	1.7
SNS	$4.2 \times 10^6$	52.8	47
<sup>51</sup> Cr	$4.8 \times 10^{13}$	0.746	0.01



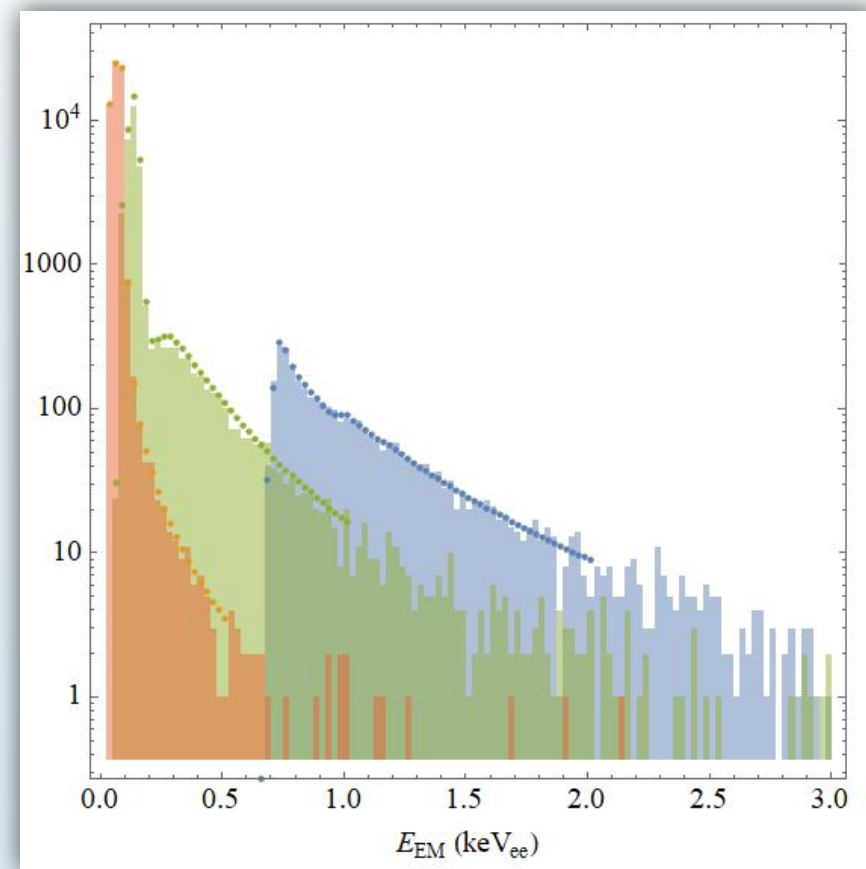
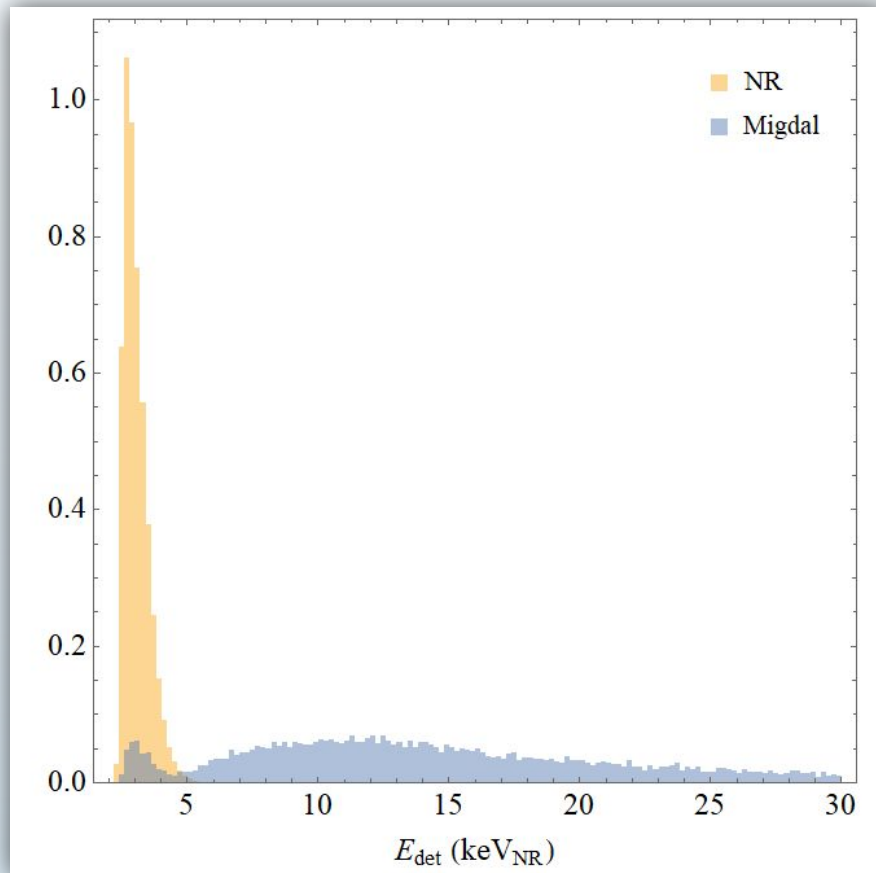


# Simulating NR + Migdal events with NEST

1. Select NR energy from distribution,  $E_R$  calculate max. allowed  $E_{EM}$
2. Loop over atomic shells,  $E_{nl}$ , and randomly (MC) ionize an electron with  $E_e$  distributed as shown earlier (with prob. scaled by the atomic recoil velocity)
3. Calculate the yields of ions and excitons produced by  $E_R$ ,  $E_e$  and  $E_{nl}$ , using NEST models for NR,  $\beta$  and  $\beta$  respectively
4. Calculate the quanta from the summed yields and the subsequent S1 & S2

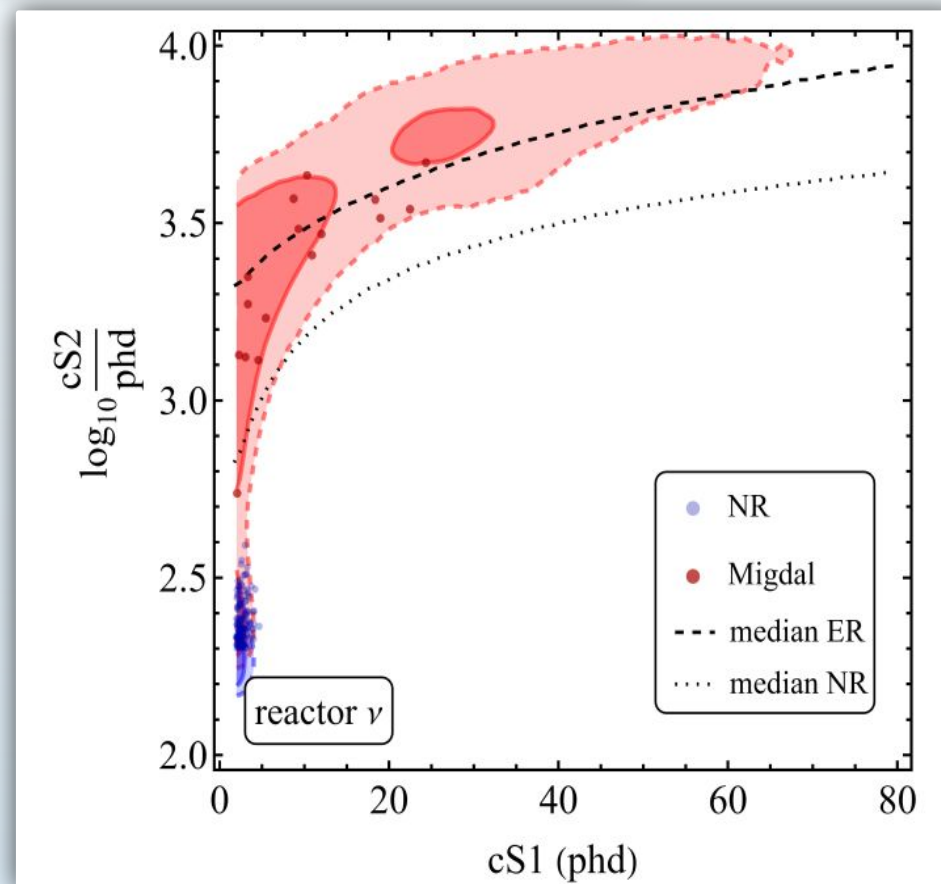
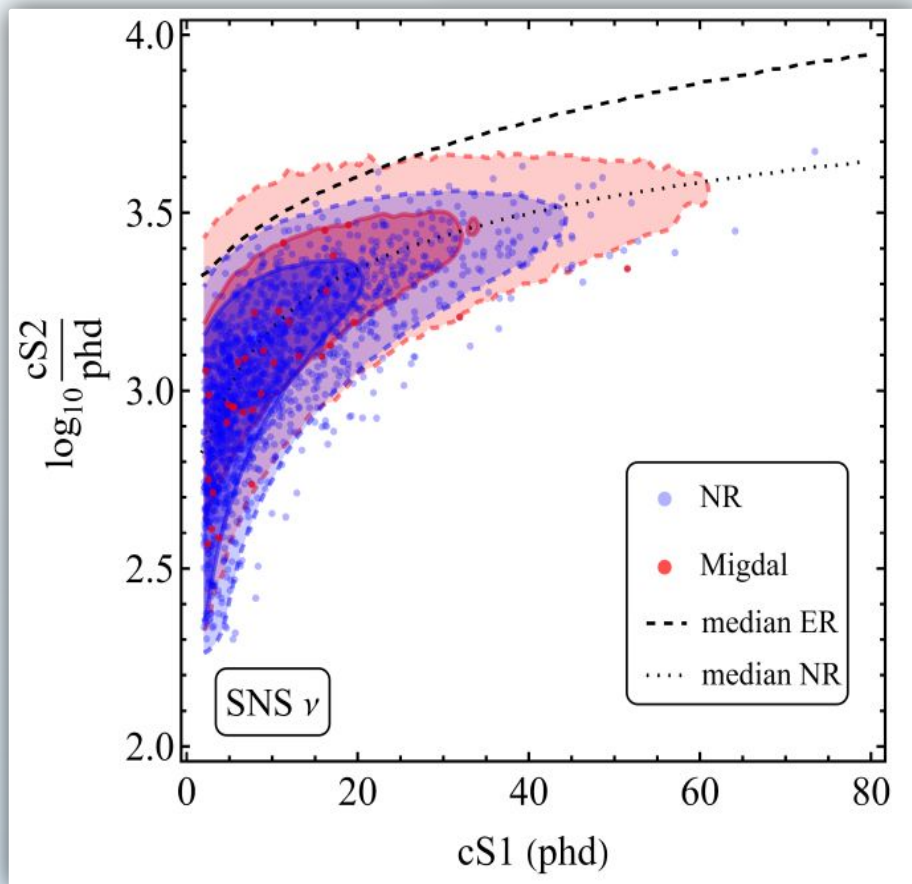
# Simulation with NEST

Event by event simulation:  
NR + electron + de-excitation



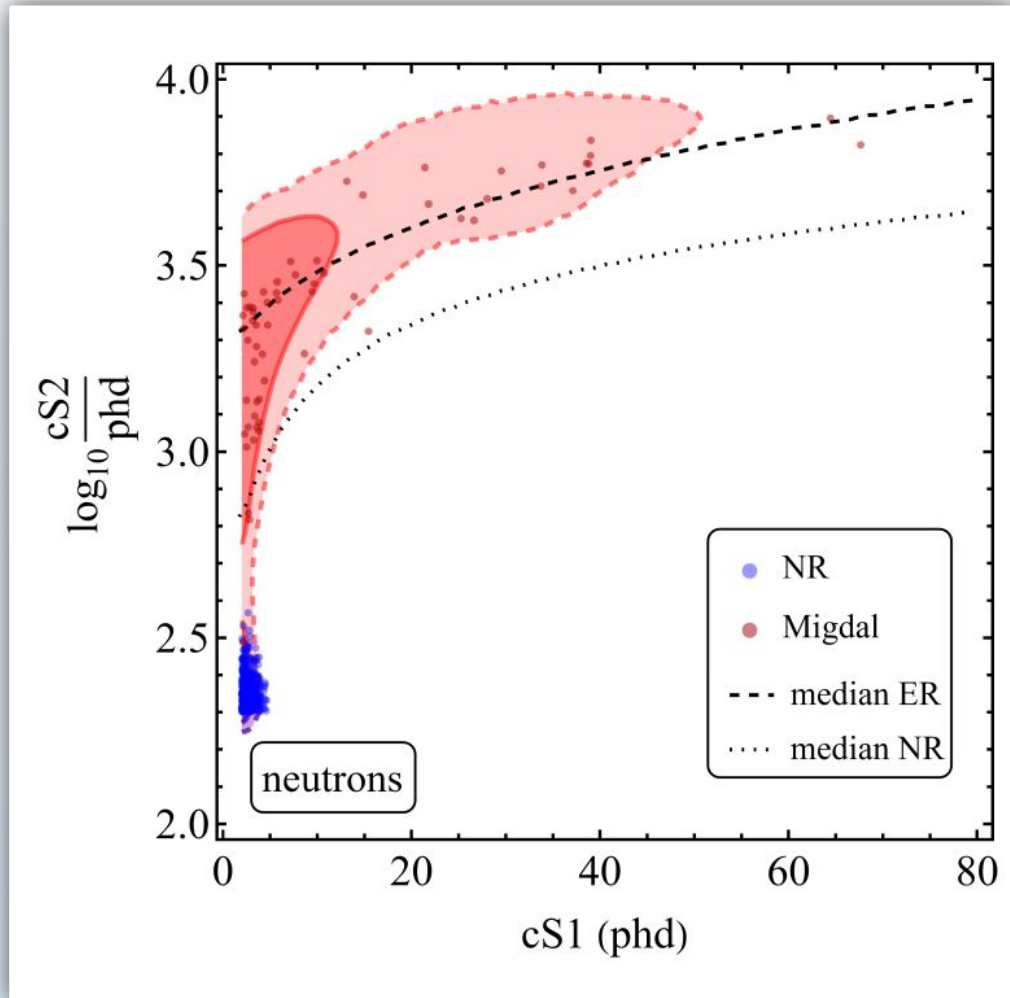
# Low-energy neutrino sources

source	flux (/cm <sup>2</sup> /s)	max $E_\nu$ (MeV)	max $E_R^{Xe}$ (keV)
nuclear reactor	$1.5 \times 10^{13}$	10	1.7
SNS	$4.2 \times 10^6$	52.8	47
<sup>51</sup> Cr	$4.8 \times 10^{13}$	0.746	0.01



# Simulation with NEST (xenon)

S1 vs S2 signal (17 keV neutrons):



Source	Calc. ratio	Sim. ratio	Sim. rate/kg/day
neutron (17 keV)	$6.0 \times 10^{-4}$	0.1	600
reactor neutrinos	$1.7 \times 10^{-4}$	0.1	$4.3 \times 10^{-4}$
SNS neutrinos	$1.5 \times 10^{-2}$	0.02	$8.8 \times 10^{-3}$
$^{51}\text{Cr}$ neutrinos	$5.4 \times 10^{-6}$	$\infty$	$8.2 \times 10^{-6}$

- Neutrons are the only viable candidate

# Summary and open questions:

- The Migdal effect is a powerful tool to extend the reach of xenon DM experiments
- A calibration of the Migdal effect directly in a liquid xenon target is desirable
- How do we model the quanta production? (is it necessary?)
- Low-energy beams of neutrons appear to be a viable option
- Background mitigation will be key

~/code\$

<https://zenodo.org/record/5587760>

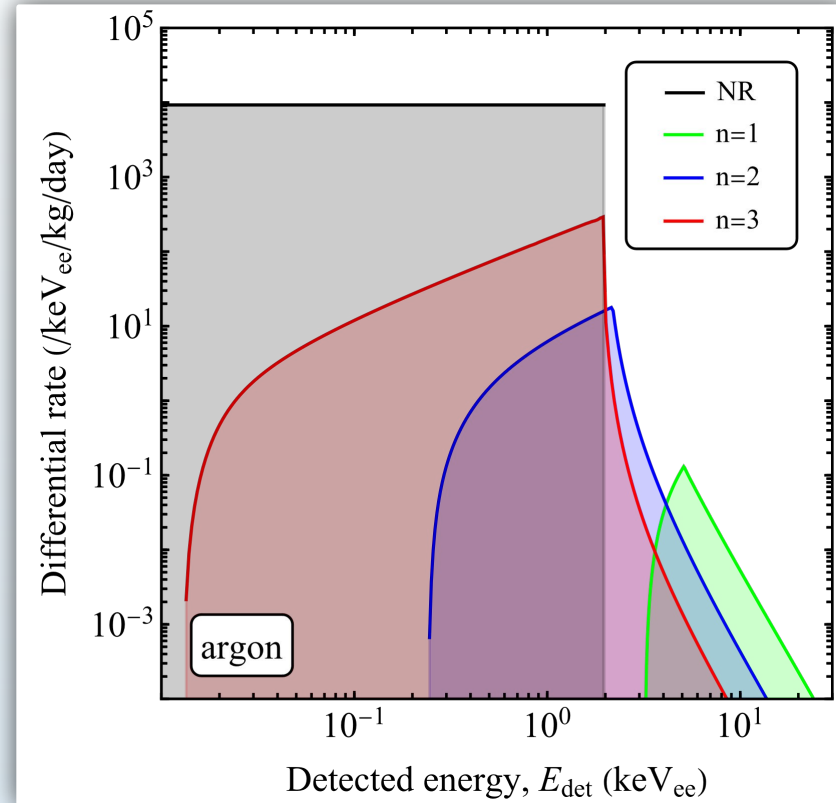
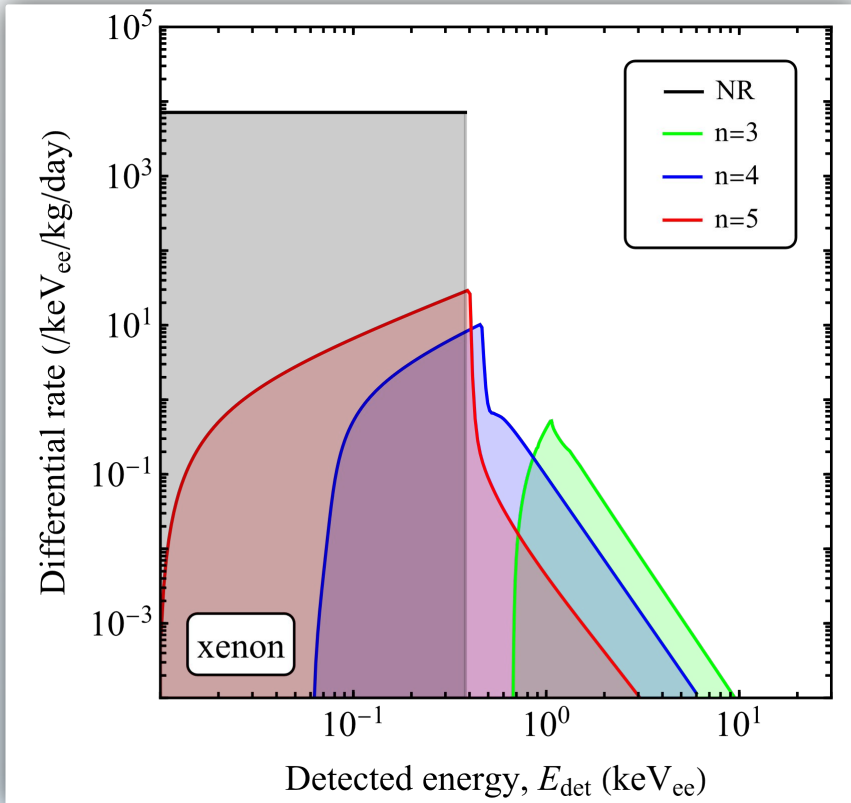
<https://github.com/jaydenn/nuMigdalCalc>

<https://github.com/jaydenn/thinNEST>

<https://github.com/jaydenn/MigdalMC>

# Low-energy neutron Migdal rates

$E = 82 \text{ keV}$  neutrons, flux =  $100 \text{ n/cm}^2/\text{s}$



## Total rates:

Nuclear: 2,700 events/kg/s

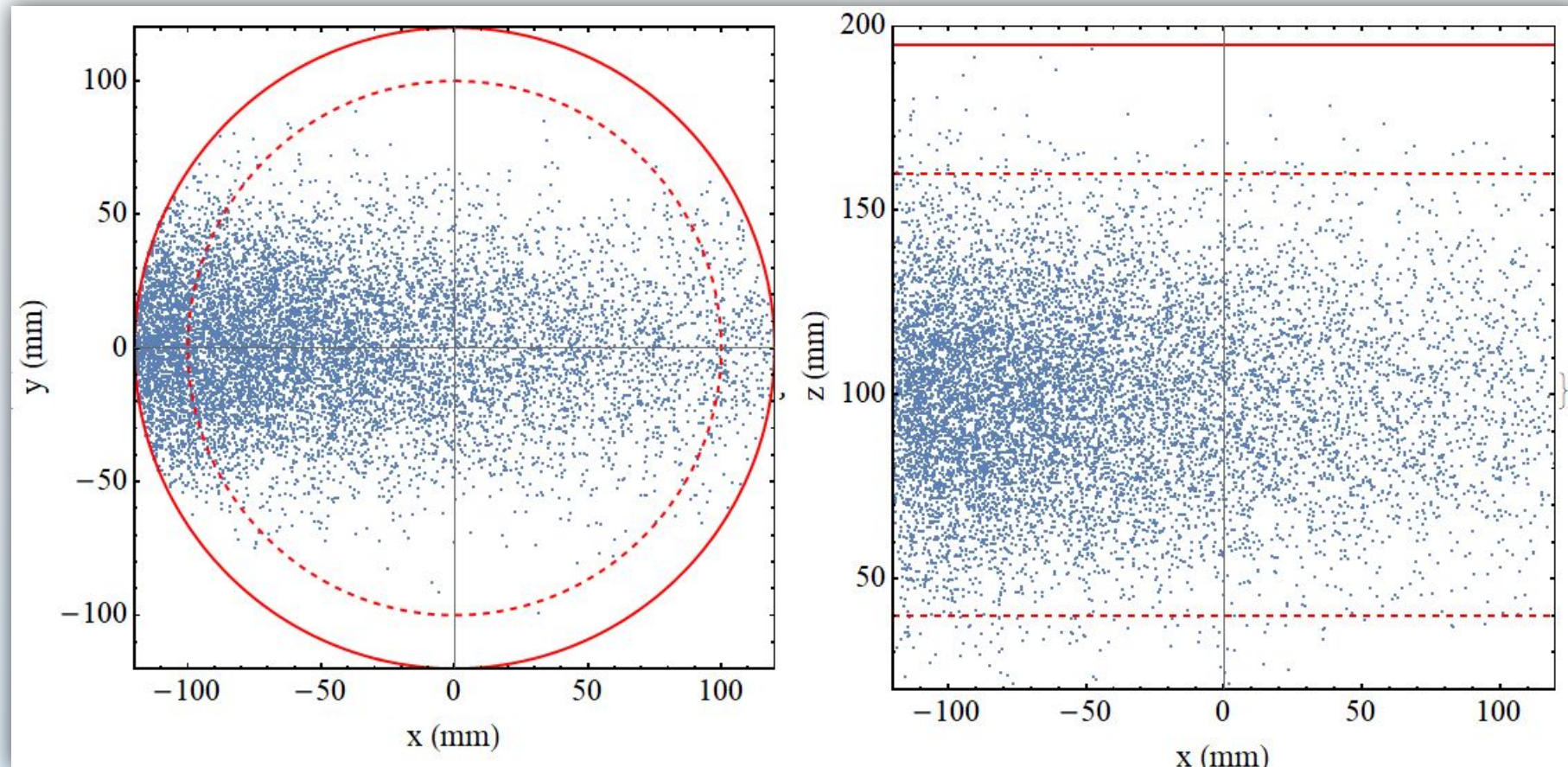
Migdal: 8 events/kg/s

12,300 events/kg/s

320 events/kg/s

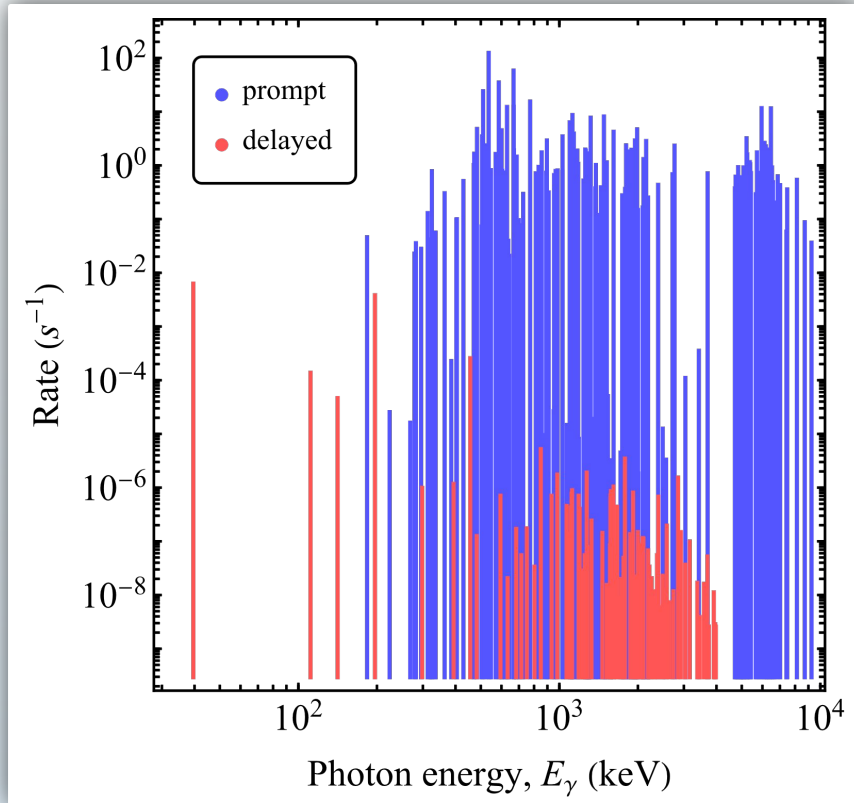
# Simulation of a neutron beam source

- Mean free path of 17 keV neutrons in xenon is  $\sim 10\text{cm}$

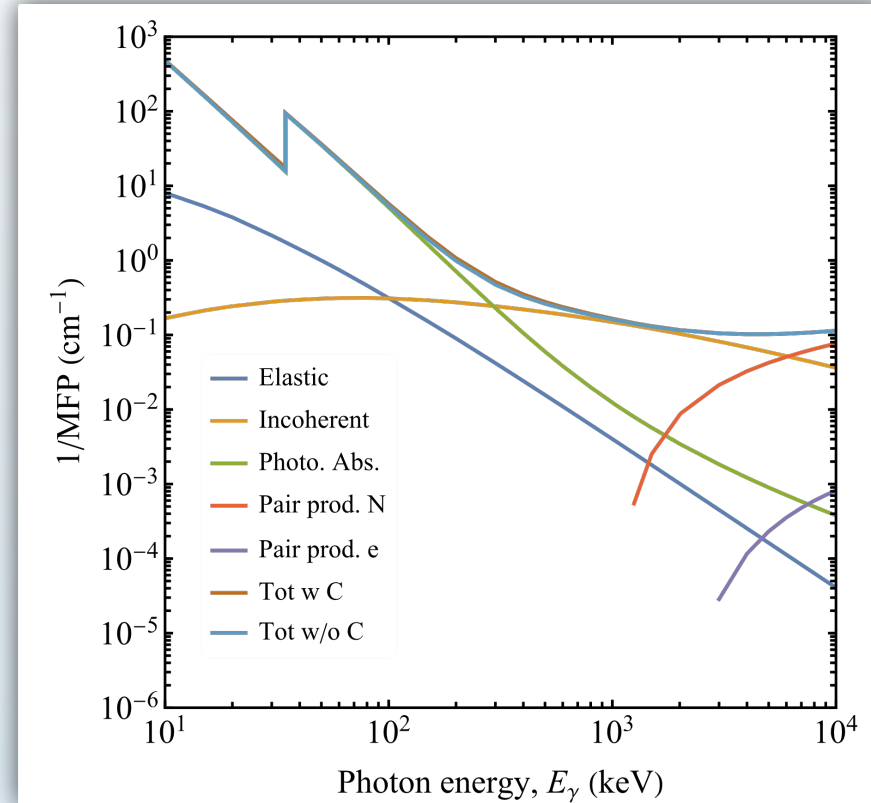


# Neutron capture backgrounds

## Radiative capture



## Photon mean free path

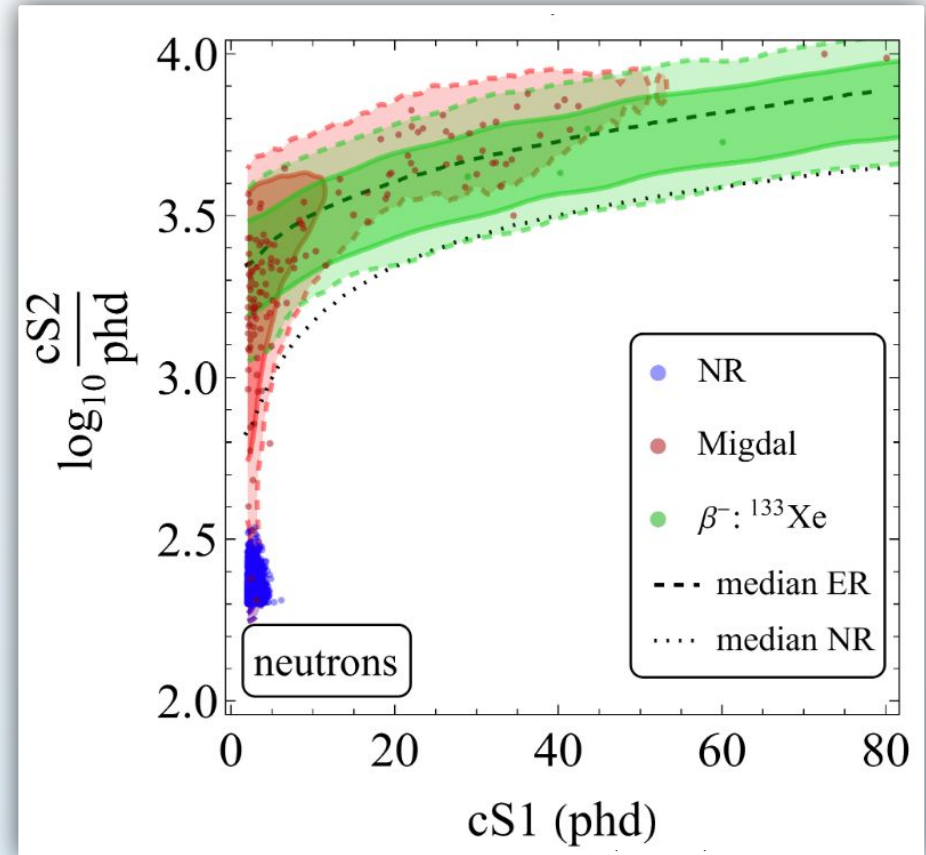




# Neutron capture backgrounds

Subsequent decays:

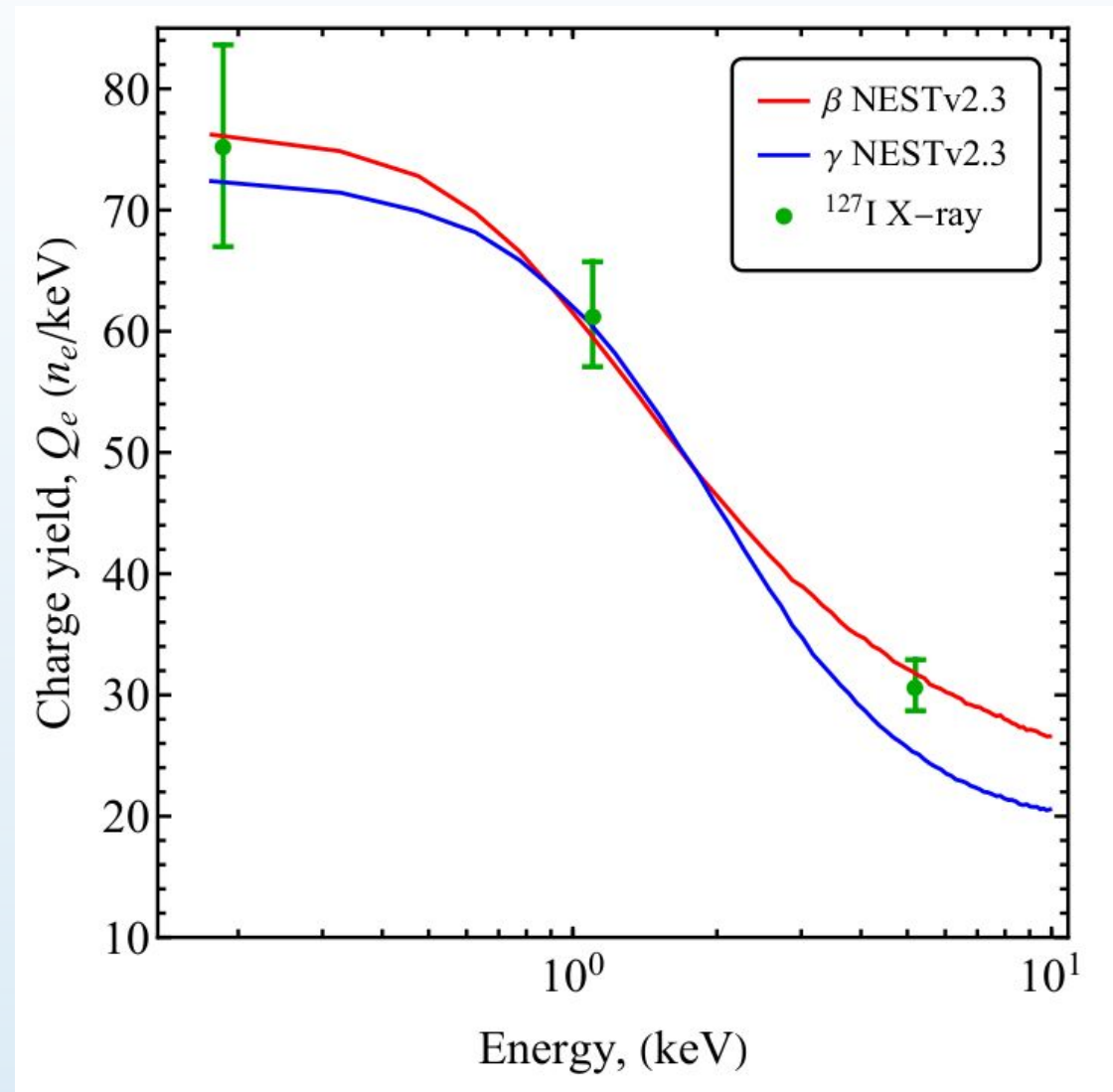
xenon-125 $\rightarrow$ EC + iodine-125	( $t \sim 17$ hrs)
xenon-127 $\rightarrow$ EC + iodine-127	( $t \sim 36$ days)
xenon-133 $\rightarrow$ $\beta^-$ + cesium-133	( $t \sim 5$ days)
xenon-135 $\rightarrow$ $\beta^-$ + cesium-135	( $t \sim 9$ hrs)
xenon-137 $\rightarrow$ $\beta^-$ + cesium-137	( $t \sim 4$ min)



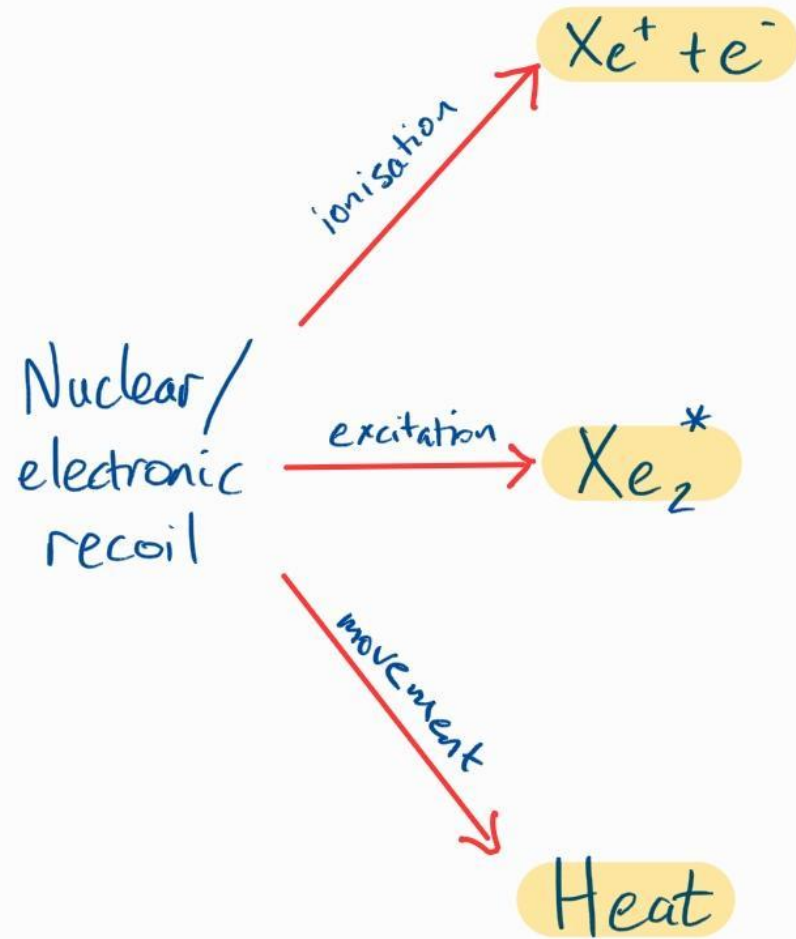
# Background mitigation

	Radiative decay	Subsequent decays	External backgrounds
Multi-scatter	✓	✓	✓
Pulsed beam trigger		✓	✓
'Fiducial' cut on beam		✓	✓
Cycle det on/off		✓	
Extra xenon flow		✓	

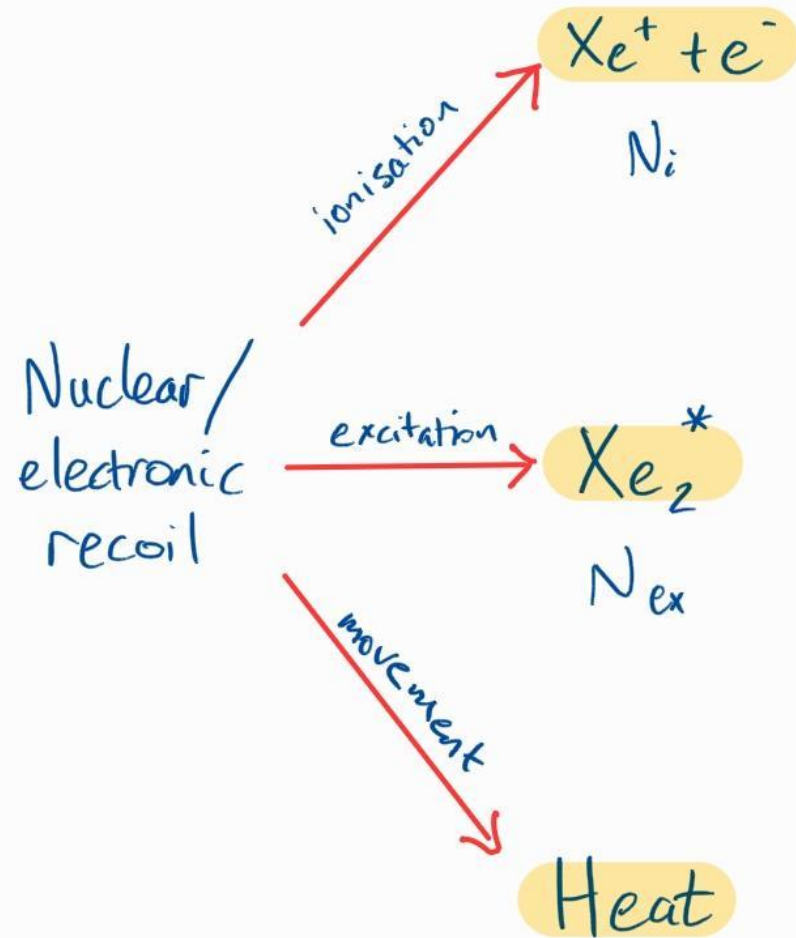
# Charge yields



# Signal production

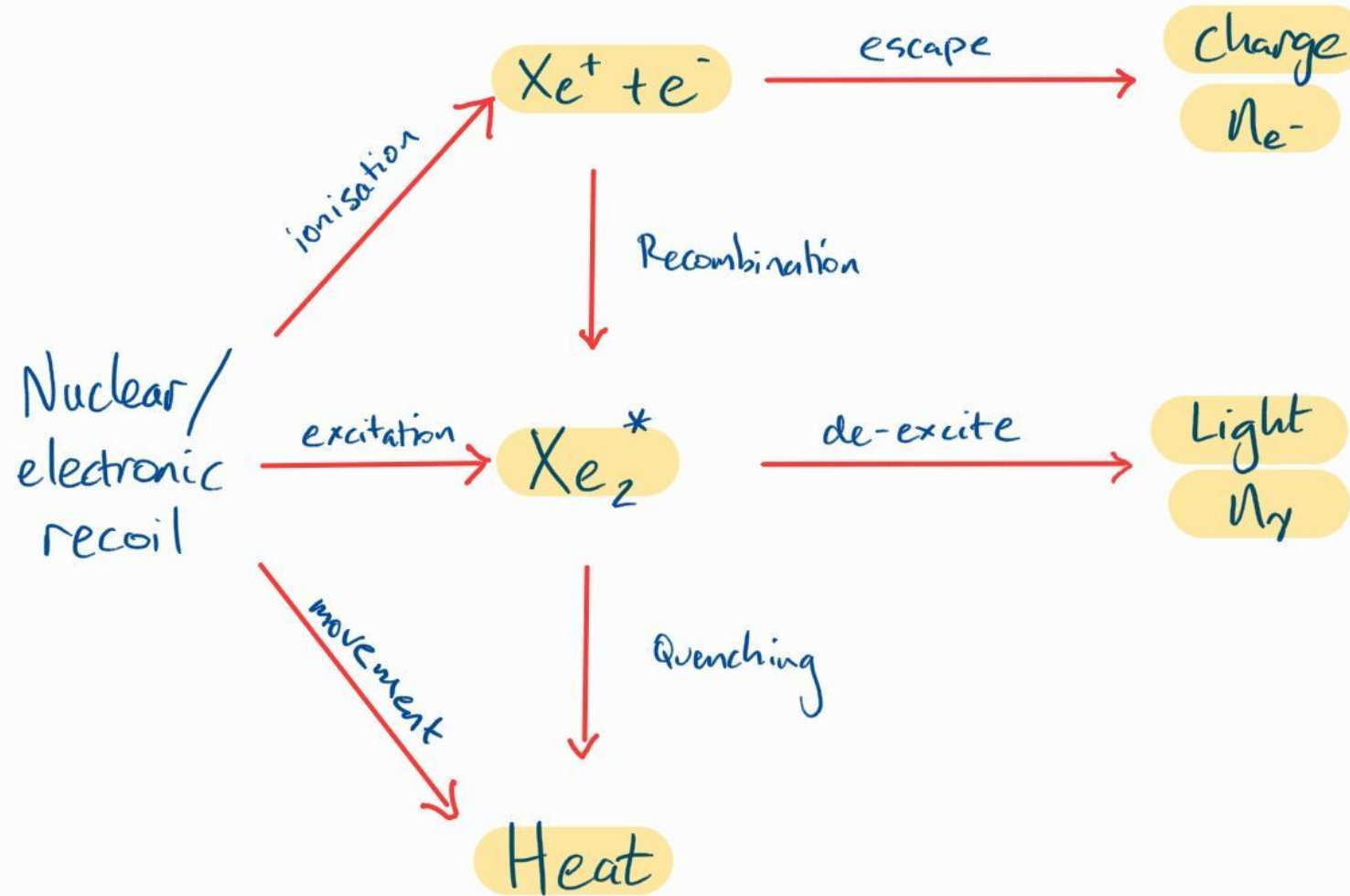


# Signal production



$$\text{ratio} \left( \frac{N_{ex}}{N_i} \right)_{NR} \sim 0.1 > \left( \frac{N_{ex}}{N_i} \right)_{ER}$$

# Signal production



# Signal production

