

# Revealing the fundamental character of the strong force

**nCTEQ**  
nuclear parton distribution functions

nuclear CTEQ



C T E Q

Coordinated Theoretical-Experimental  
Project on QCD

Fred Olness  
SMU

*Thanks for substantial input  
from my friends & colleagues*

2022 Mitchell Conference  
May 24-27

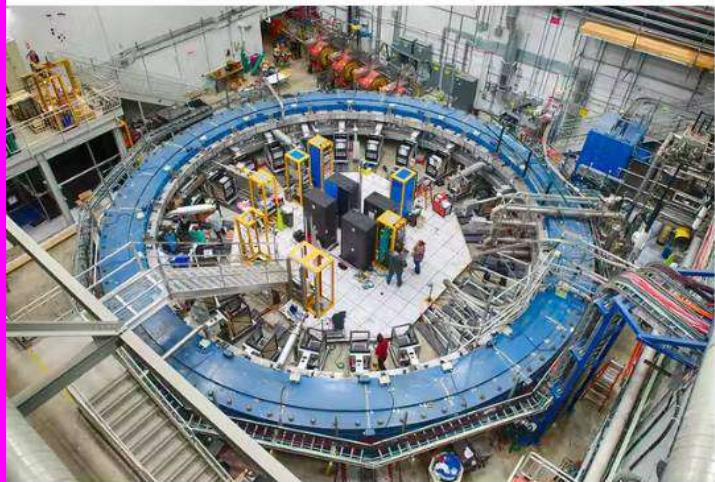
# CERN COURIER

May/June 2022 [cerncourier.com](http://cerncourier.com)

Reporting on international high-energy physics

## LHC RUN 3 BEAMS, DETECTORS, ACTION

### THE CONVERSATION



The storage-ring magnet for the Muon G-2 experiment at Fermilab. Reidar Hahn/wikipedia, CC BY-SA

**The standard model of particle physics may be broken – an expert explains**

Published: May 6, 2022 11.43am EDT

by [Roger Jones](#), Lancaster University

As a physicist working at the Large Hadron Collider (LHC) at Cern, one of the most frequent questions I am asked is “When are you going to find something?”. Resisting the temptation to

HVP  
Hadronic  
Vacuum  
Polarization

**W-Mass  
g-2  
ALICE Dead-Cone**

...

INVERSE

ROGER JONES AND THE CONVERSATION

PHOTOGRAPH BY ROGER JONES FOR INVERSE

## WHY SCIENTISTS THINK PHYSICS COULD BE IN FOR A RECKONING

The evidence seems to be growing that some new physics is needed.

## PHYSICS TODAY

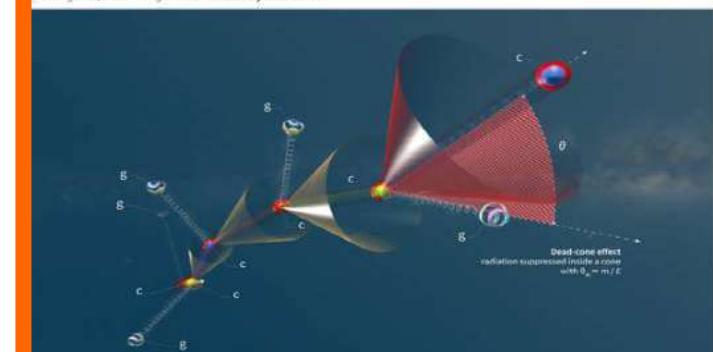
### W-boson mass hints at physics beyond the standard model

Nearly a decade of colliding beams has provided a wealth of data on the fundamental particles that make up our world.

**SCI E&TEC NEWS**

**CERN Physicists Directly Observe Fundamental Phenomenon in Quantum Chromodynamics**

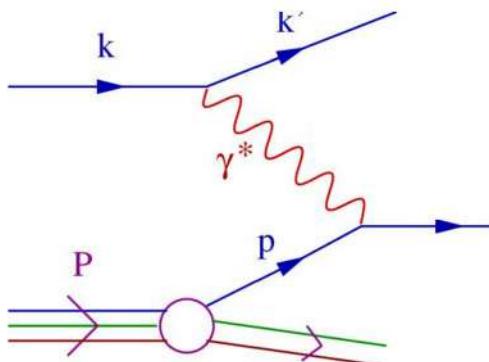
May 19, 2022 by News Staff / Source



A charm quark (c) in a parton shower loses energy by emitting radiation in the form of gluons (g). The shower displays a dead cone of suppressed radiation around the quark for angles smaller than the ratio of the quark's mass (m) and energy (E). The energy decreases at each stage of the shower. Image credit: Daniel Dominguez / CERN.

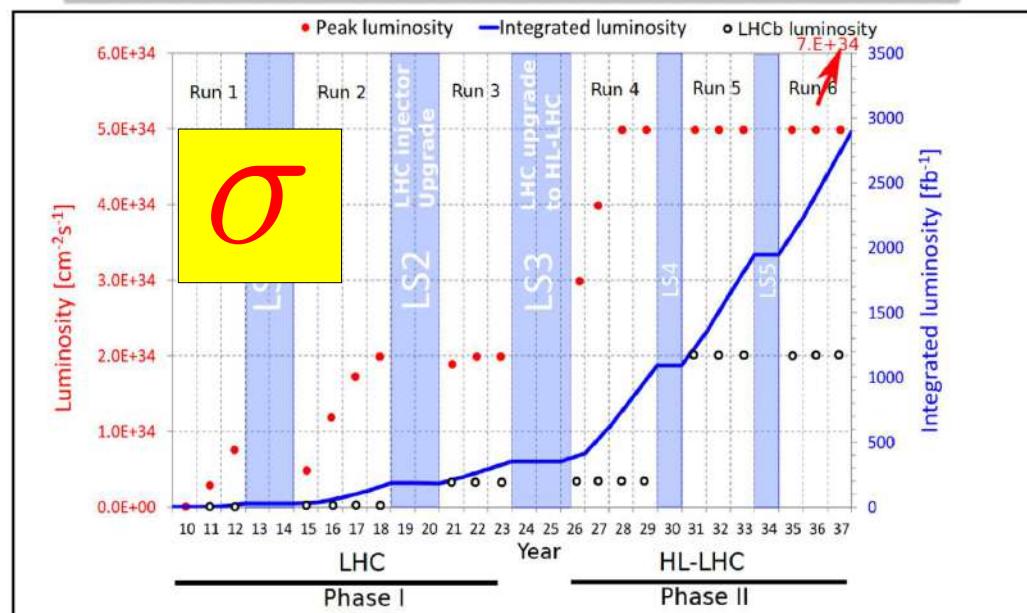
# We are entering the “Precision Era”

3

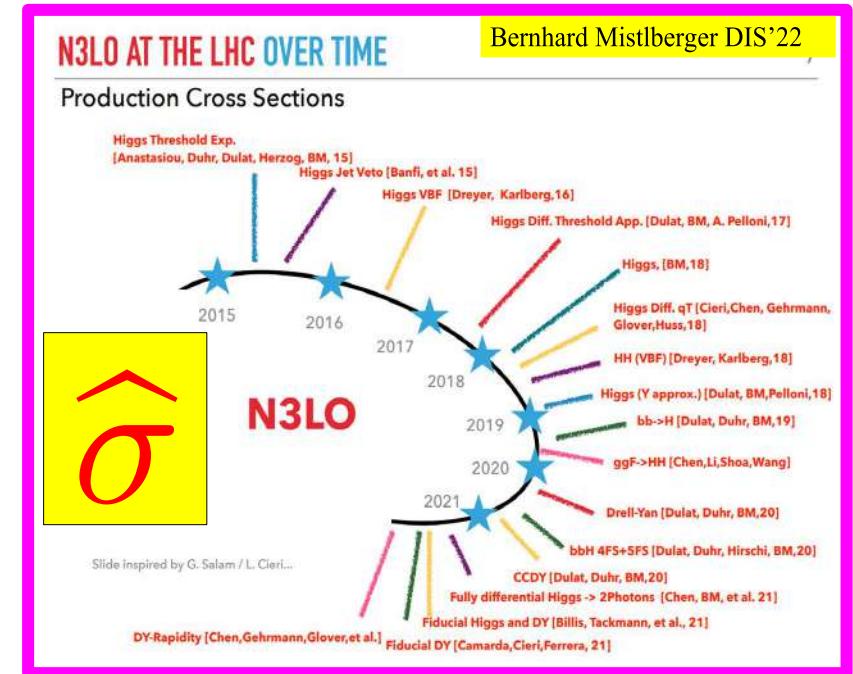


$$\sigma = f \otimes \hat{\sigma}$$

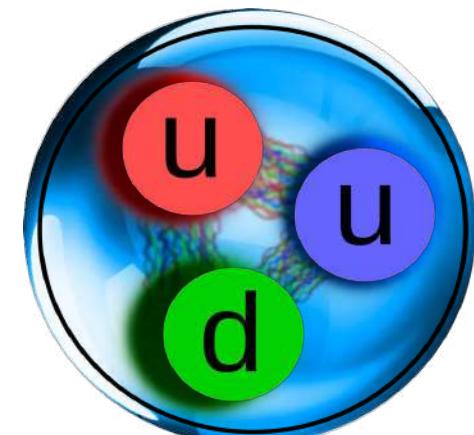
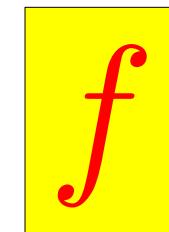
Timeline (LHC/HL-LHC) - Long Shutdowns, Runs, Upgrades

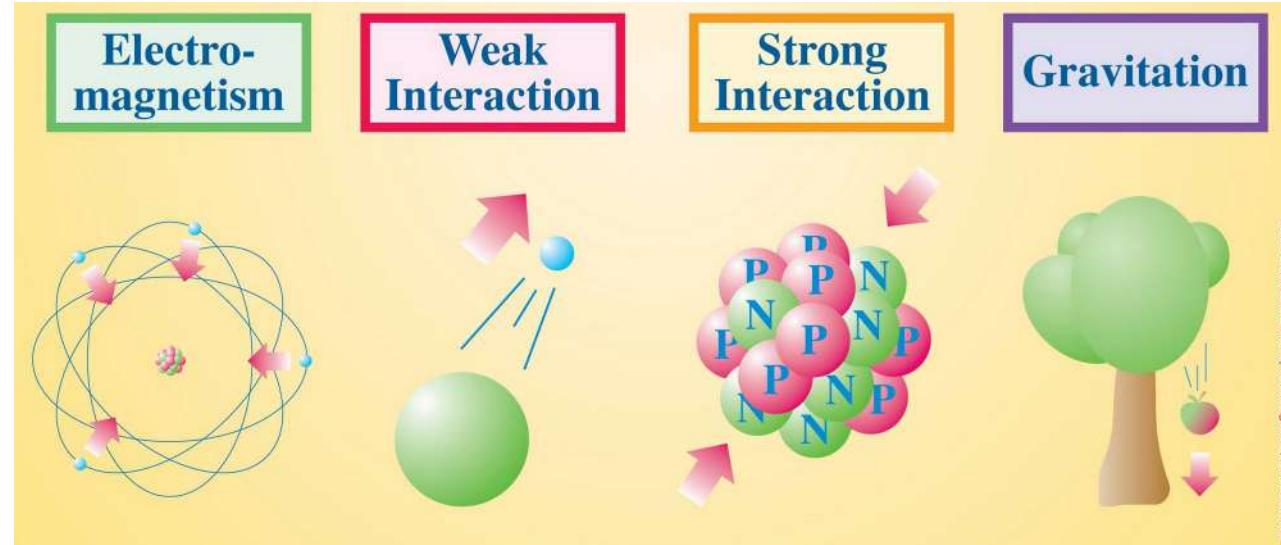
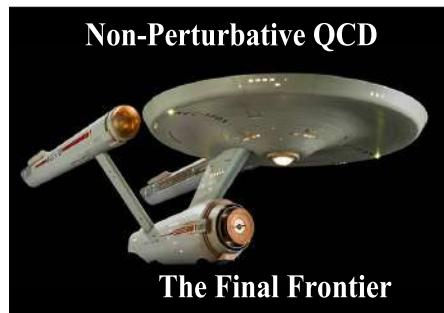


4



Challenge: hadronic component





Nobel Prizes: EW '79,'95,'99,'02,'08,'15   QCD '04   Gravity '11, '17, '20   Higgs '13

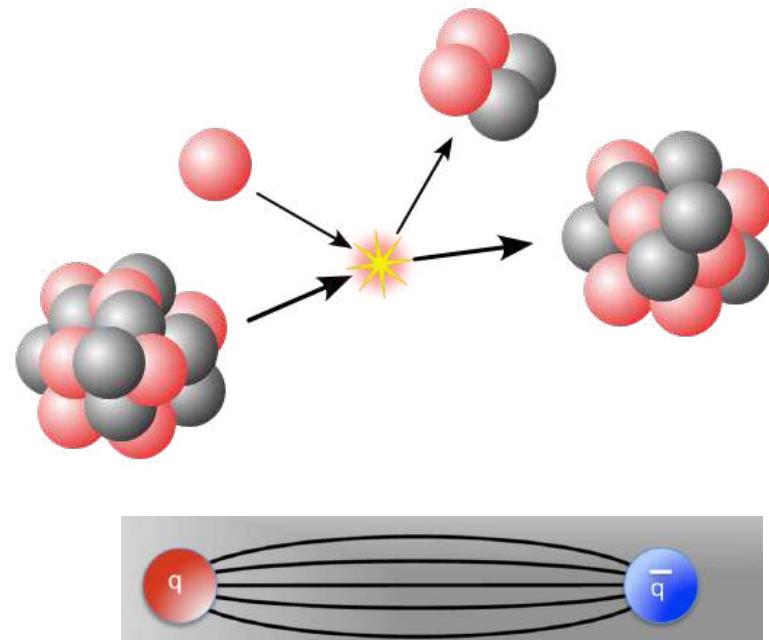
## QCD is our most perfect physical theory

What QCD Tells Us About Nature – and Why We Should Listen. Frank Wilczek

In many respects, our most complex  
asymptotic freedom  
strong color confinement  
... associated manifestations

**Lessons: The Nature of Nature**

“... alien, simple, beautiful, weird, & comprehensible”



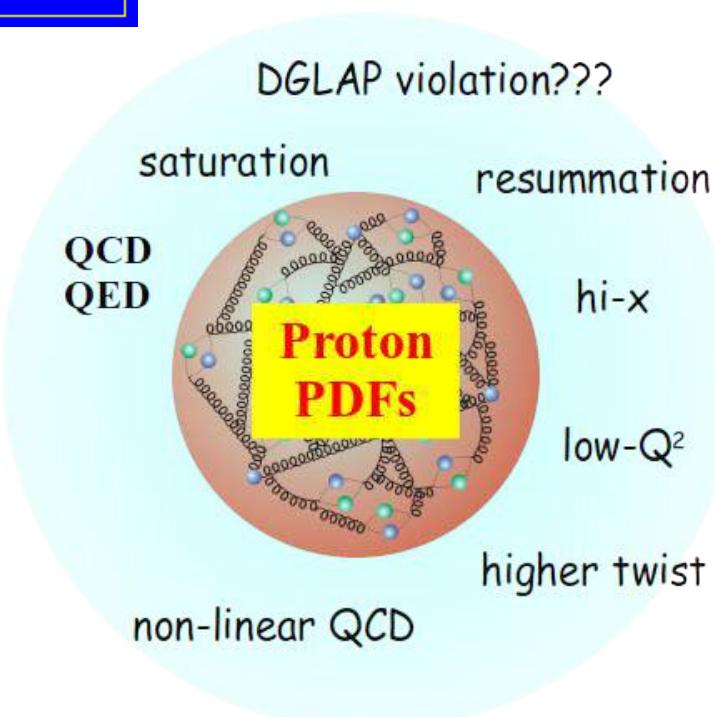
Quark Confinement  
(Asymptotic Freedom)

CTEQ

*Established  
1991*

Foster communication  
between  
experimentalists  
& theorists

HERA  
Tevatron  
*era*

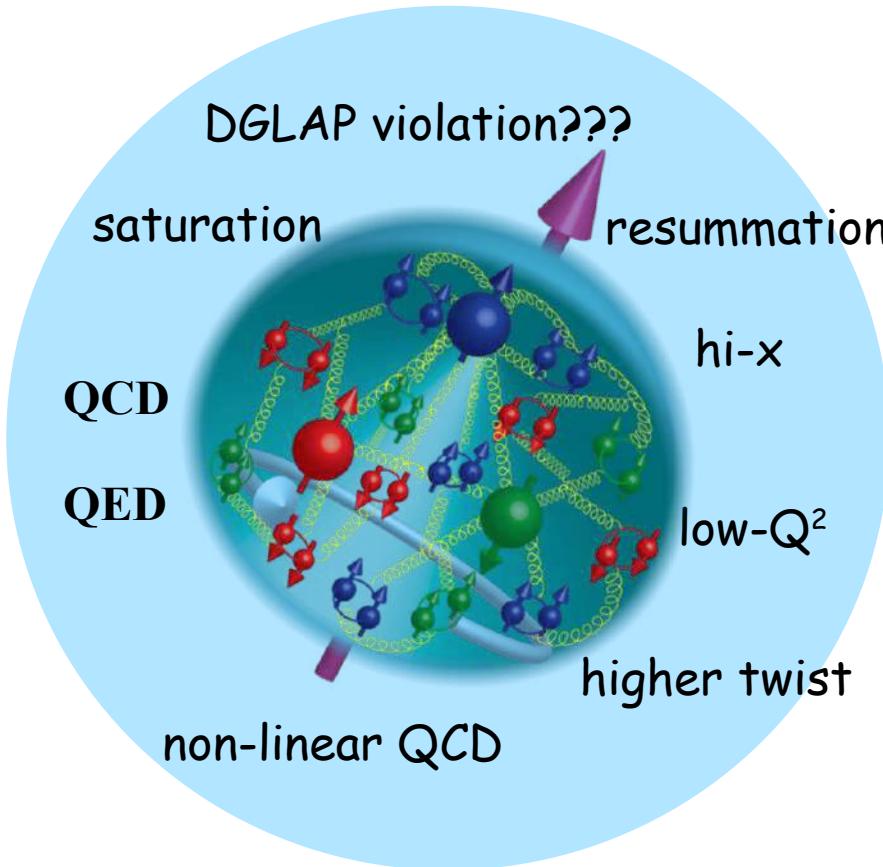


## A History of CTEQ:

The Coordinated Project on  
Theoretical and Experimental  
Studies of QCD

The CTEQ Collaboration  
Editor: Jeff Owens

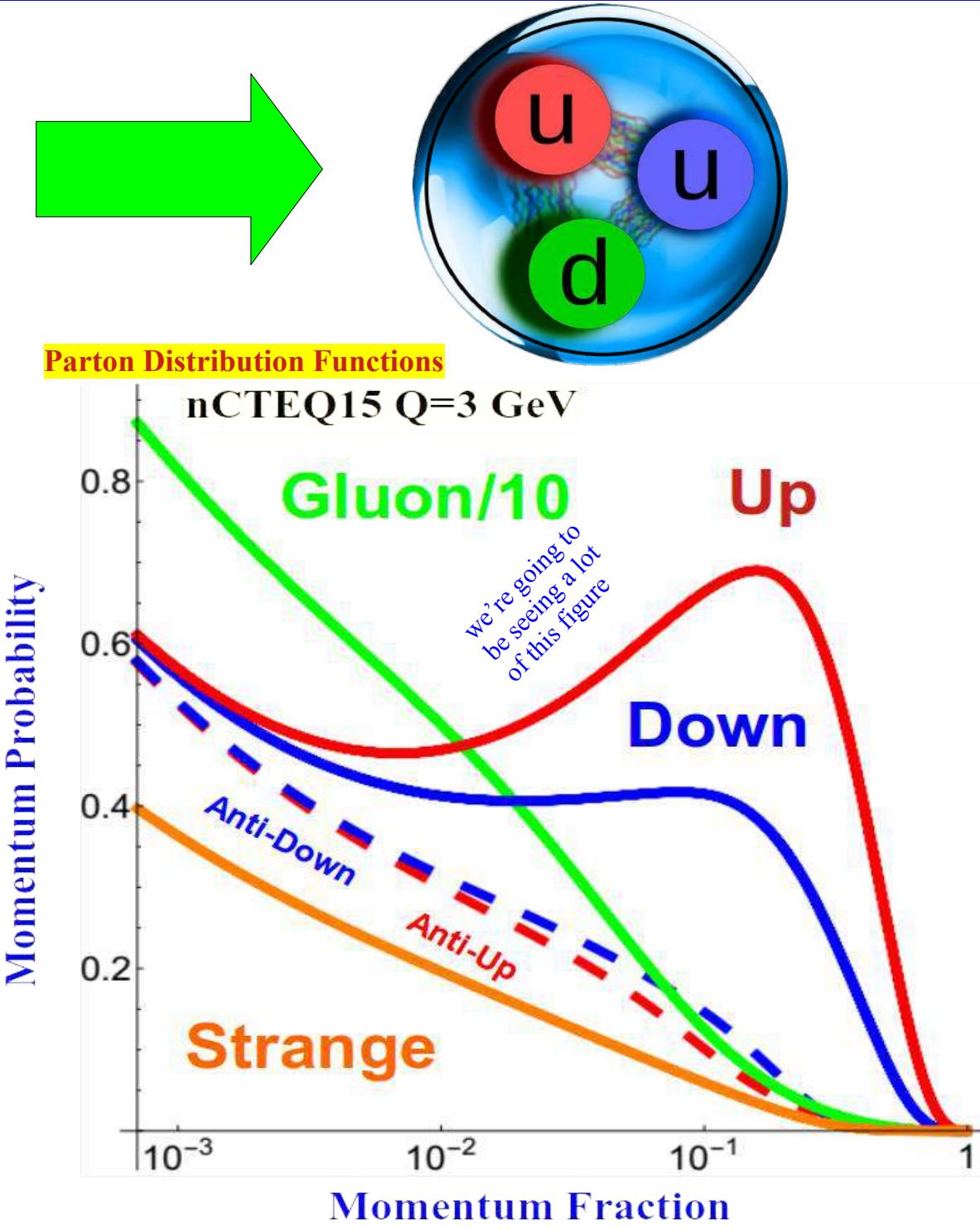




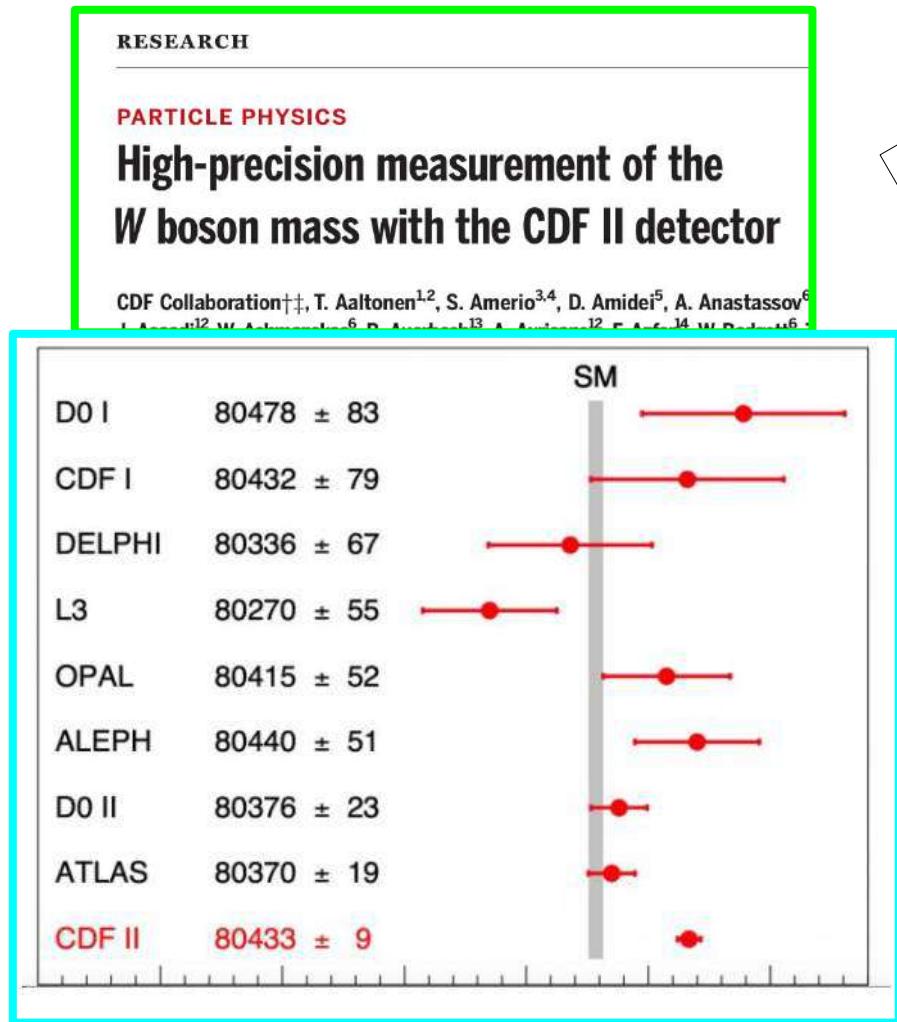
This description is  
**Universal**

*Applies to HERA, LHC, EIC ...*

a consequence of factorization



# Precision Era: High Precision W Boson Mass



**Table 1. Uncertainties in the W mass measurements, in MeV.**

1994 ICHEP'94

	CDF (e)	CDF ( $\mu$ )	DØ(e)
Energy Scale	130	60	260
Resolution	140	120	70
Background	50	50	30
Fitting	20	20	30
PDF	100	100	70
$p_T^W$ and und. evt.	120	145	120
Width	-	-	20
Total Sys.	250	240	307
Statistical	150	200	160
Total (Stat + Sys)	290	300	346

**Table 2. Uncertainties on the combined  $M_W$  result.**

2022

Source	Uncertainty (MeV)
Lepton energy scale	3.0
Lepton energy resolution	1.2
Recoil energy scale	1.2
Recoil energy resolution	1.8
Lepton efficiency	0.4
Lepton removal	1.2
Backgrounds	3.3
$p_T^Z$ model	1.8
$p_T^W/p_T^Z$ model	1.3
Parton distributions	3.9
QED radiation	2.7
W boson statistics	6.4
Total	9.4

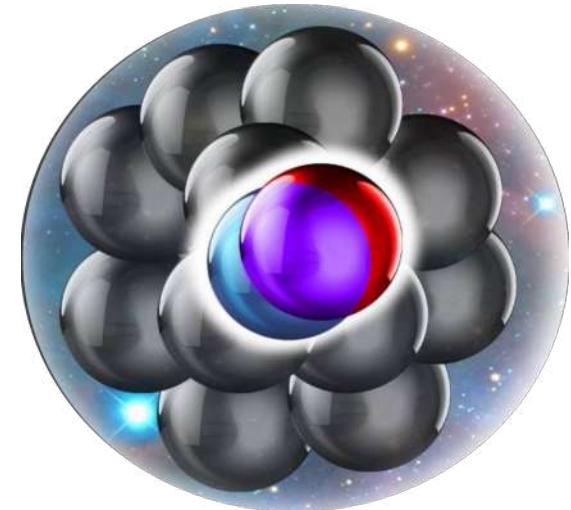
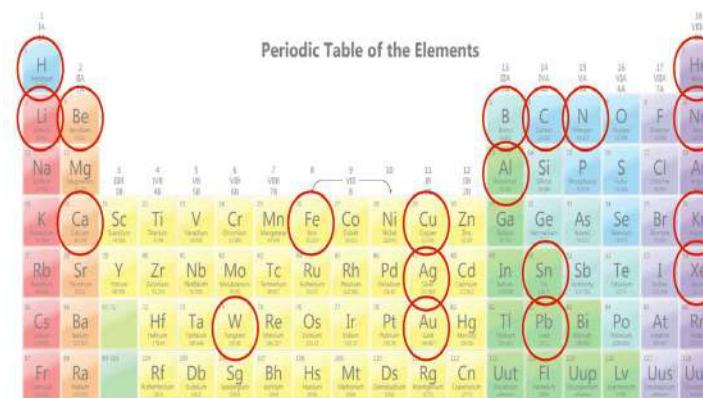
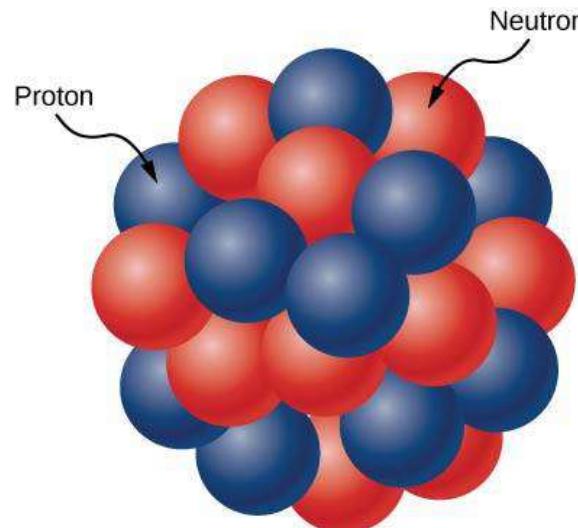
**CSS Resummation**

**Strange PDF**

**PDF Precision**

# Nuclear PDFs

Parton Distribution Functions

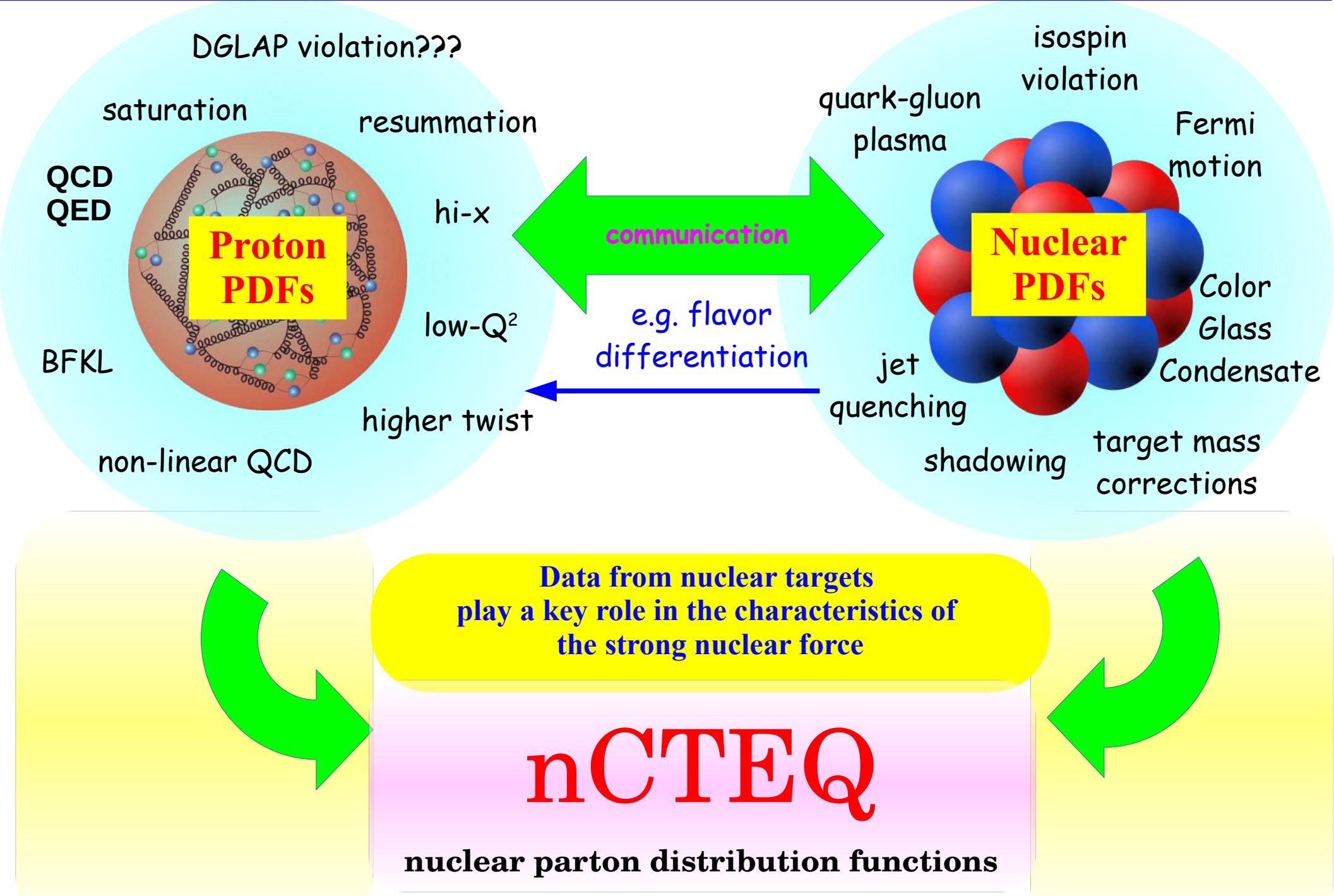


**nCTEQ**

nuclear parton distribution functions

**nuclear Coordinated Theoretical-Experimental Project on QCD**

# ... the ultimate goal for nCTEQ



# nCTEQ Projects

**✓ DIS:** Muzakka, Kovarik, Klasen, ...

**W/Z:** Jezo, Kusina, Olness, ...

**Gluons:** Duwentaster, Klasen, ...

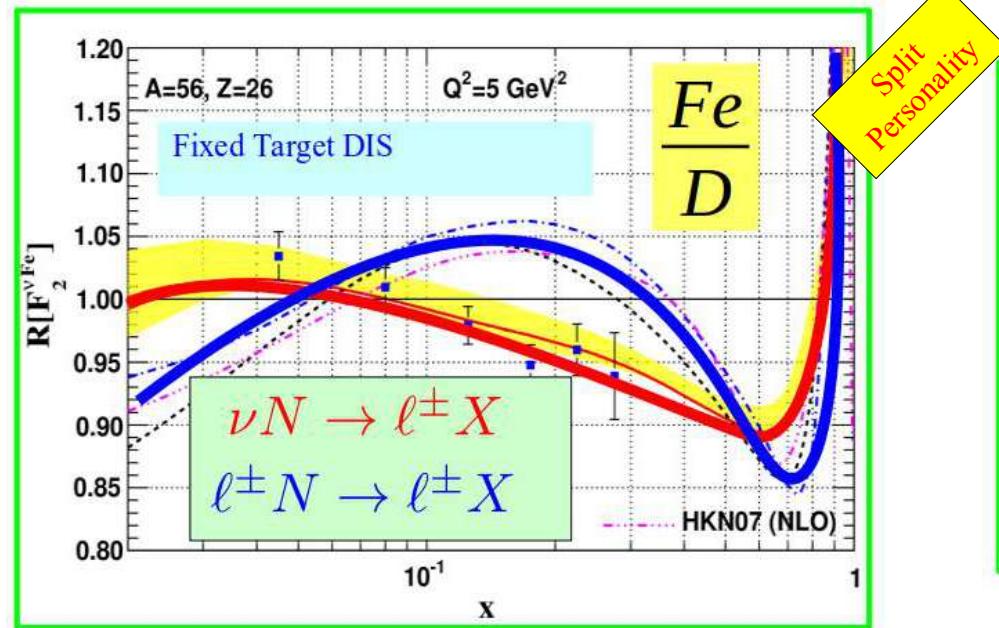
**SRC:** Jezo, Kusina, Olness, ...

**Masses:** Schienbein, Leger, Ruiz, ...

**nCTEQ++:** Jezo, Risse, Muzakka, Duwentaster, Wissmann...

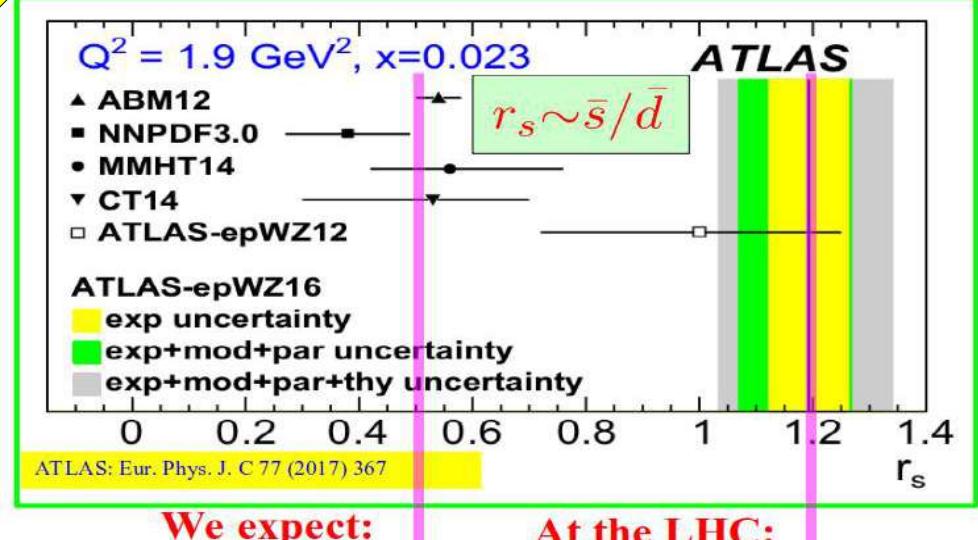
multifaceted  
approach

# nCTEQ15 $\nu$



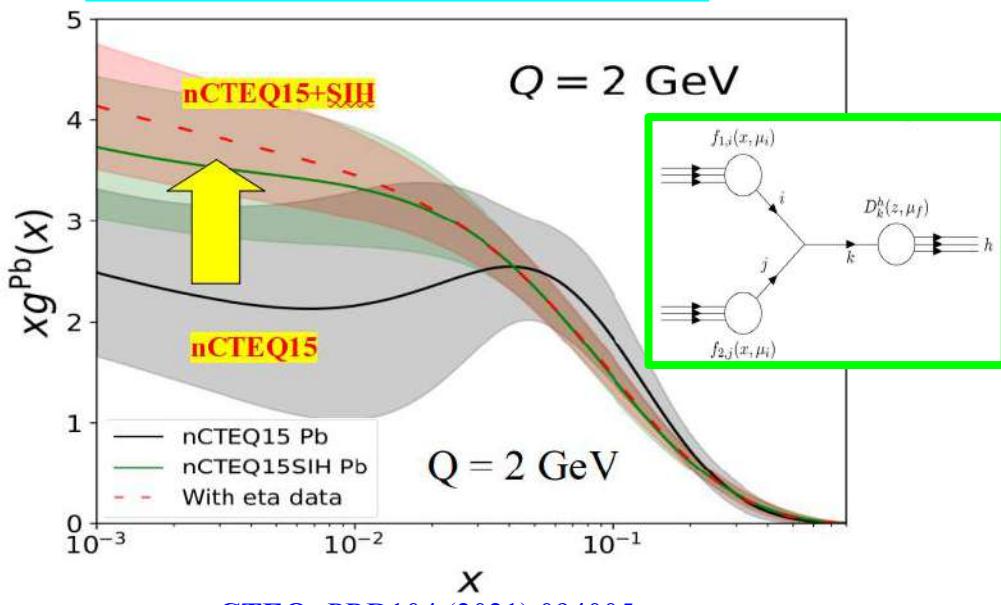
nCTEQ: arXiv: 2204.13157

# nCTEQ15WZ



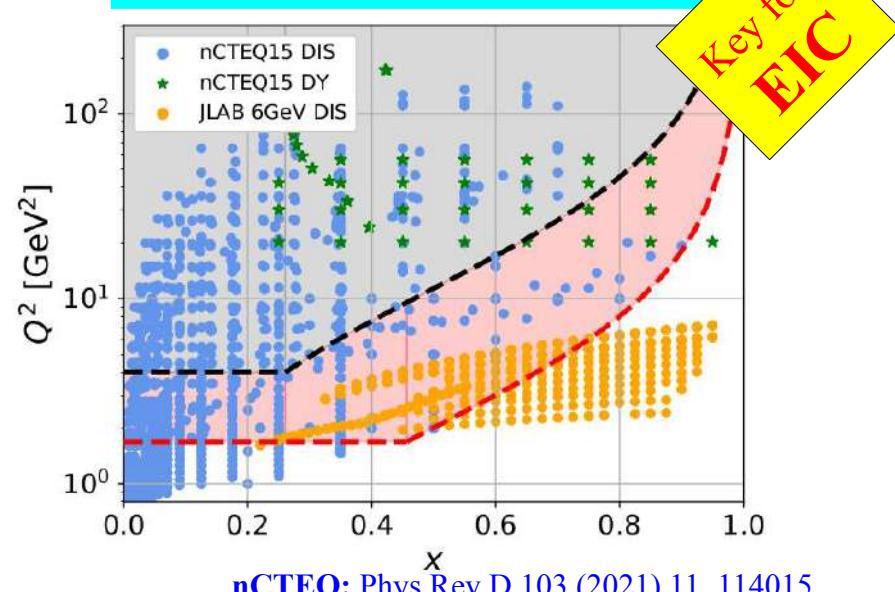
nCTEQ: Phys.Rev.D 104 (2021) 094005

# nCTEQ15WZ+SIH



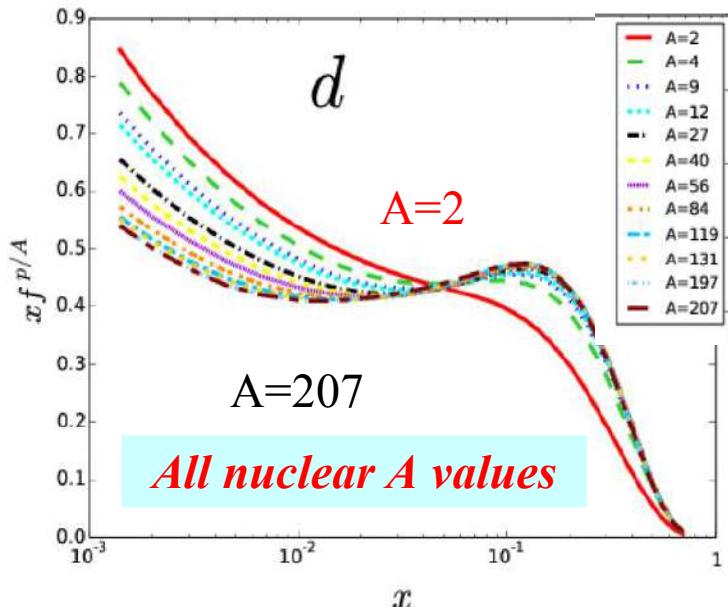
nCTEQ: PRD104 (2021) 094005.

# nCTEQ15HIX



nCTEQ: Phys.Rev.D 103 (2021) 11, 114015

# Short Range Correlations (SRC)

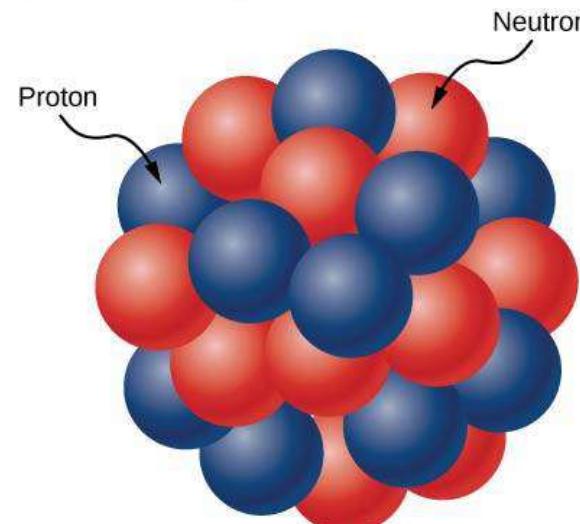


$$f_A = (1 - c_A) f_p + c_A f_{SRC}$$

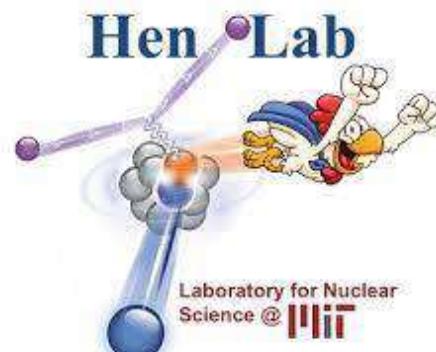
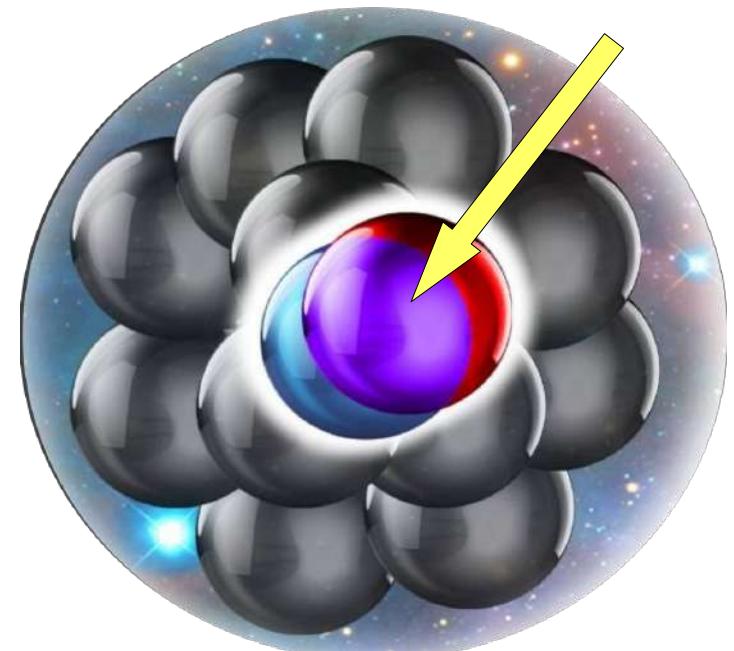
nuclear  
PDF

normal  
proton  
PDF

SRC  
modified  
PDF

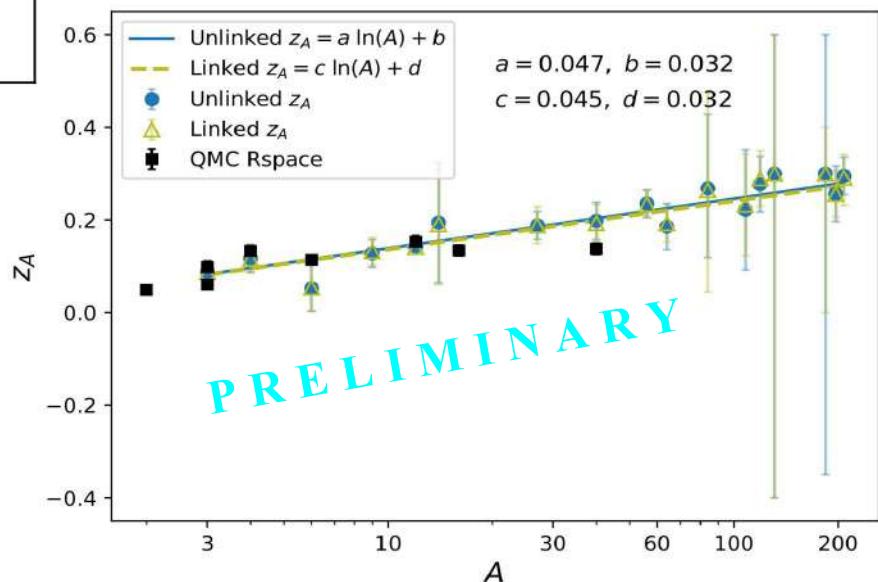
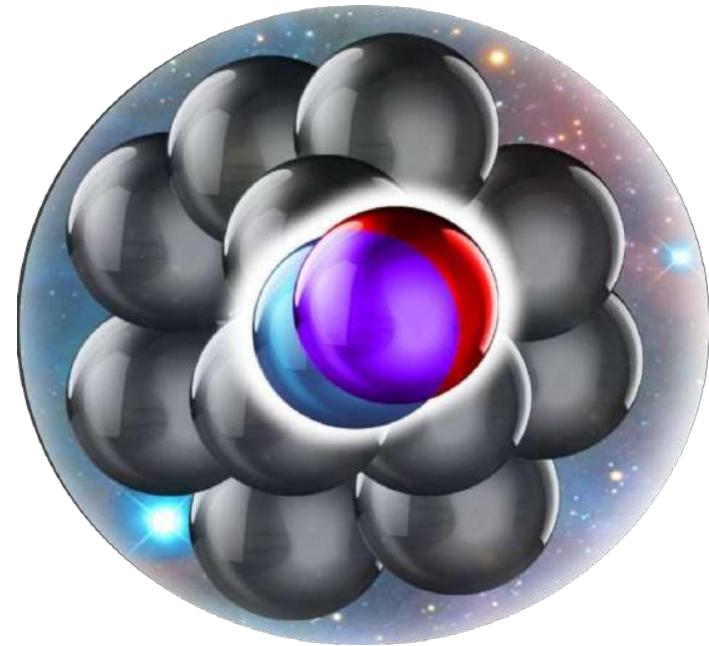
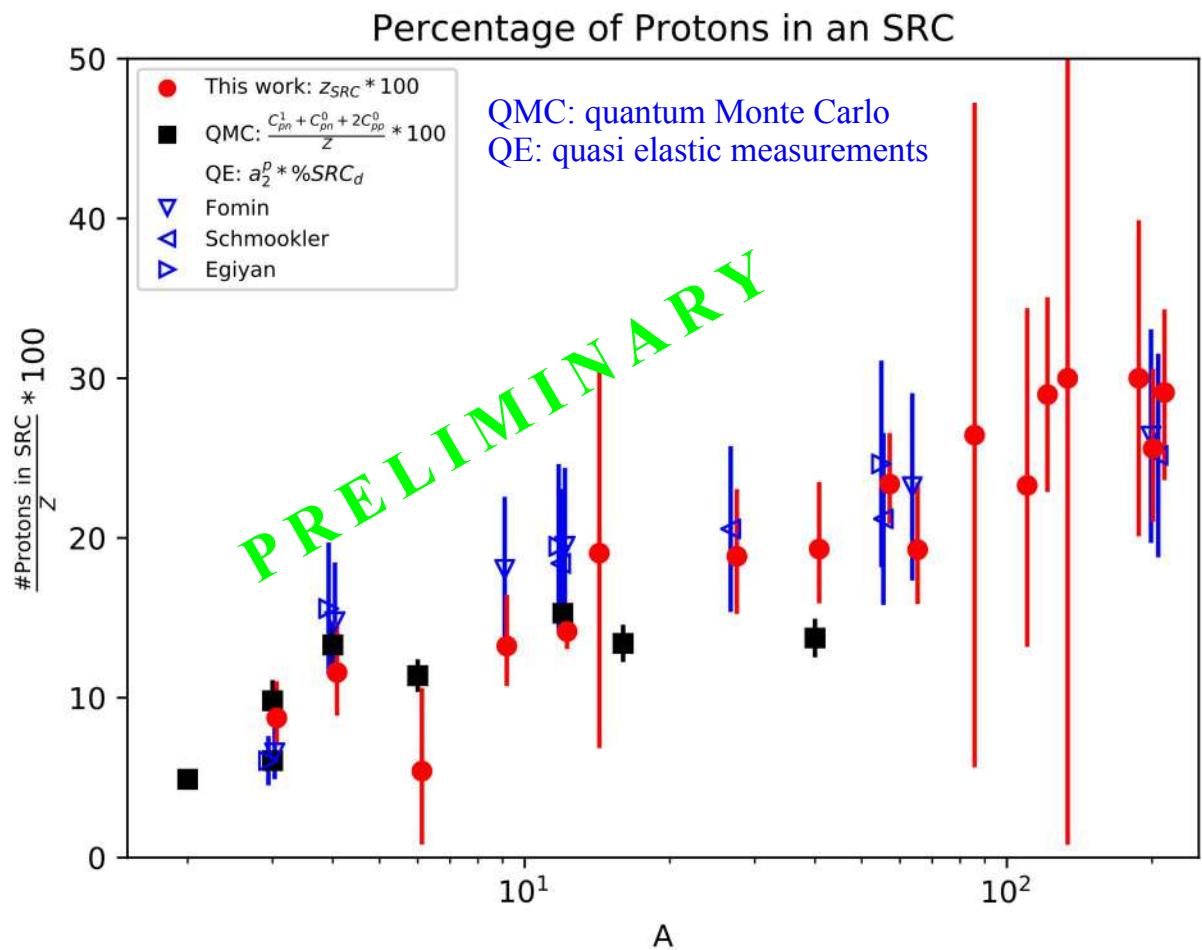


Short Range Correlations (SRC)



# Short Range Correlations (SRC)

13



## Preliminary results:

- Yields good fit:  $\chi^2/N \sim 0.80$  vs. 0.85
- Compatible with (pn) SRC pairs



xFitter Collaboration Meeting February 2020, DESY

[www.xFitter.org](http://www.xFitter.org)

# xFitter



[www.xFitter.org](http://www.xFitter.org)



## Sample data files:

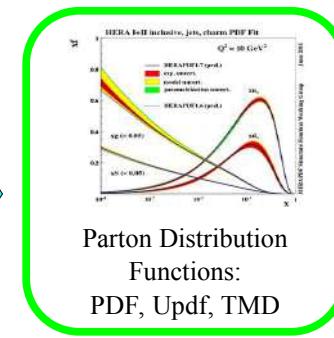
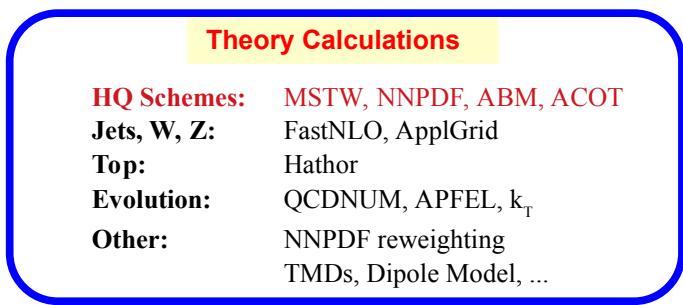
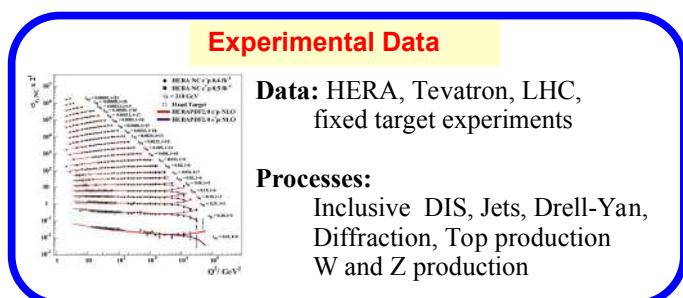
LHC: ATLAS, CMS, LHCb

Tevatron: CDF, D0

HERA: H1, ZEUS, Combined

Fixed Target: ...

User Supplied: ...



- $\alpha_s(M_Z)$ ,  $m_c, m_b, m_t, \dots$
- Theoretical Cross Sections
- Comparisons to other PDFs (LHAPDF)



## Features & Recent Updates:

Photon PDF & QED  
Pole & MS-bar masses  
Profiling and Re-Weighting

Heavy Quark Variable Threshold  
Improvements in  $\chi^2$  and correlations  
TMD PDFs (uPDFs)  
... and many other

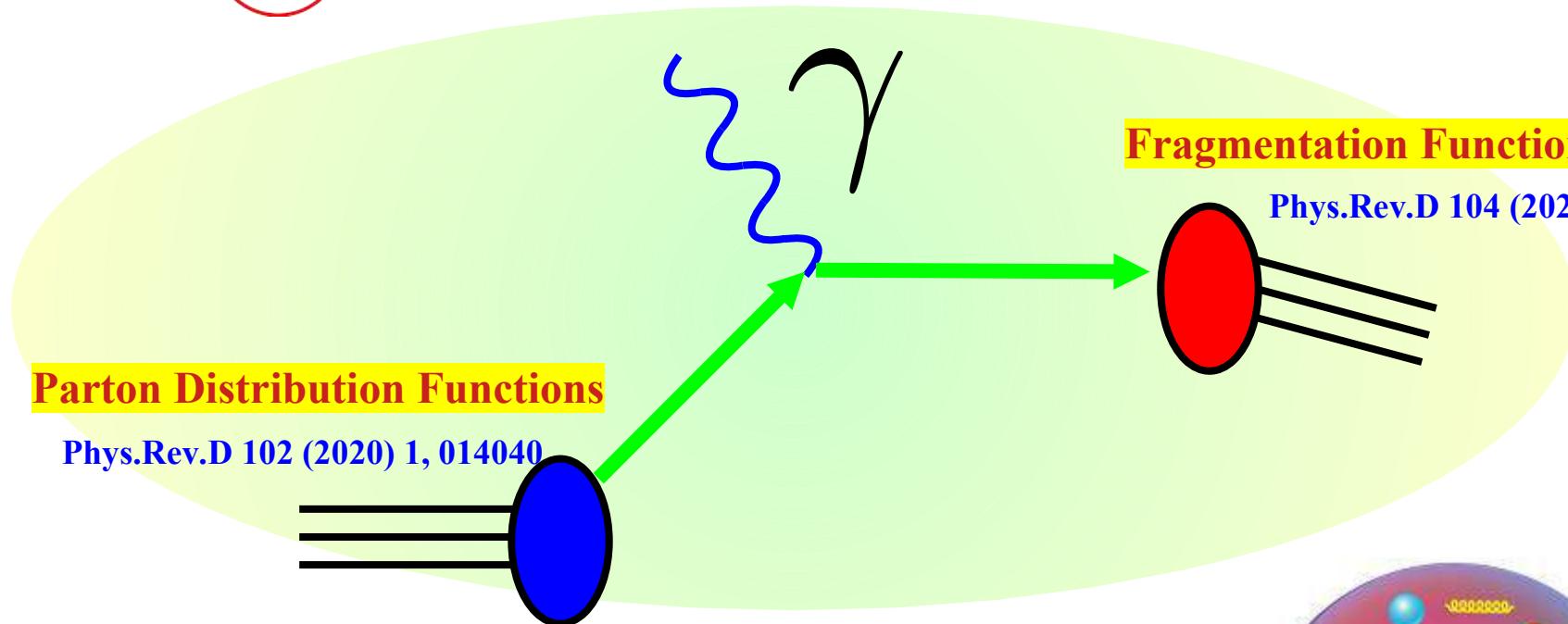
**xFitter 2.2.0  
Future Freeze**

# Pion PDFs & FFs

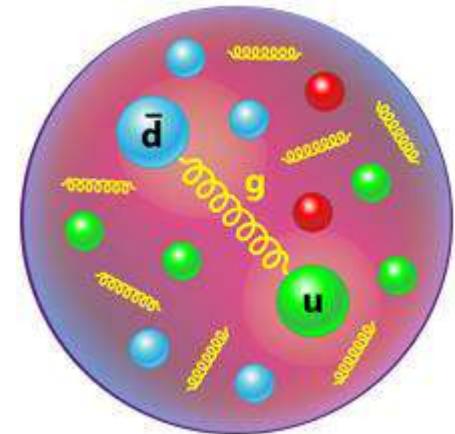
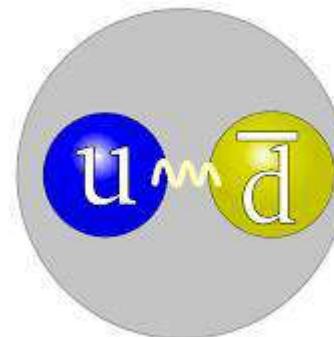


**Parton Distribution Functions**

**Fragmentation Functions**



$$\text{Pion } \pi^+ = u\bar{d}$$



***Input from L-QCD***

Article

## Direct observation of the dead-cone effect in quantum chromodynamics

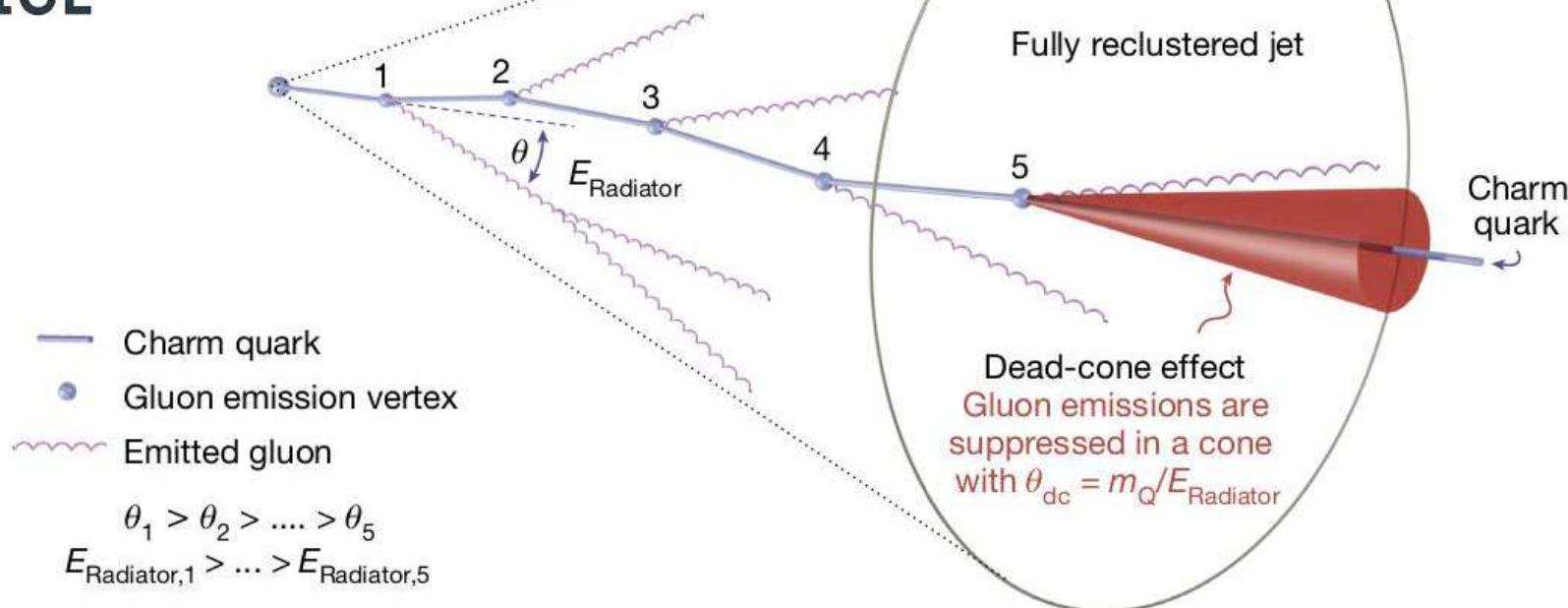
<https://doi.org/10.1038/s41586-022-04572-w>

ALICE Collaboration\*

- Detailed heavy quark shower reconstruction
- Dead Cone Observation
- Sensitive to **QUARK** mass (*not meson mass*)



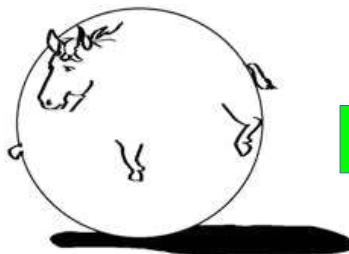
ALICE



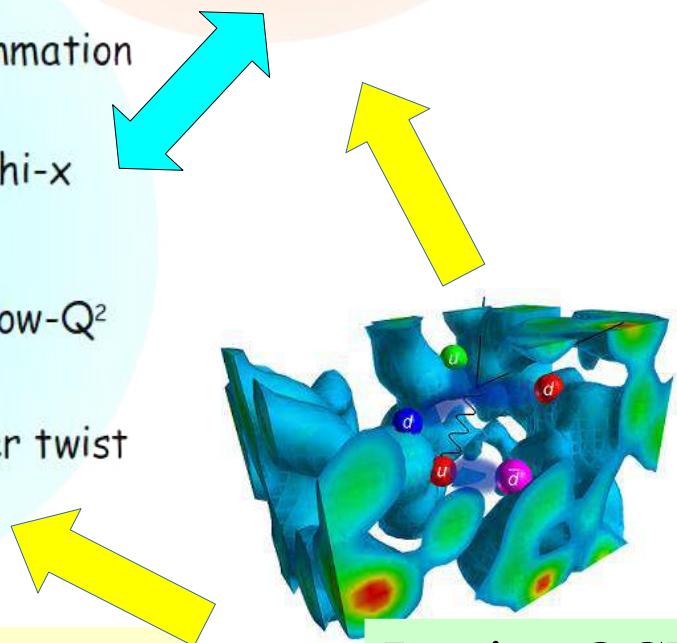
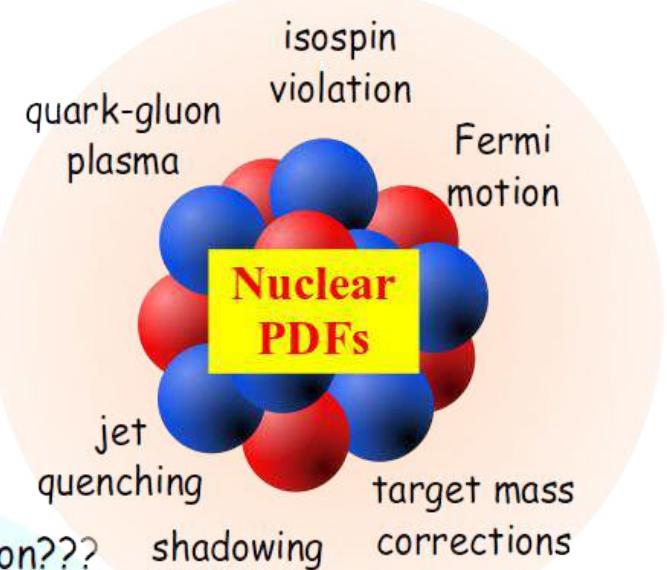
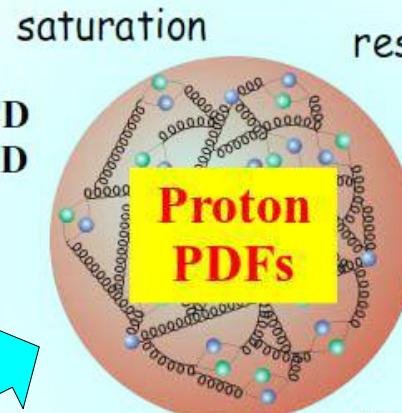
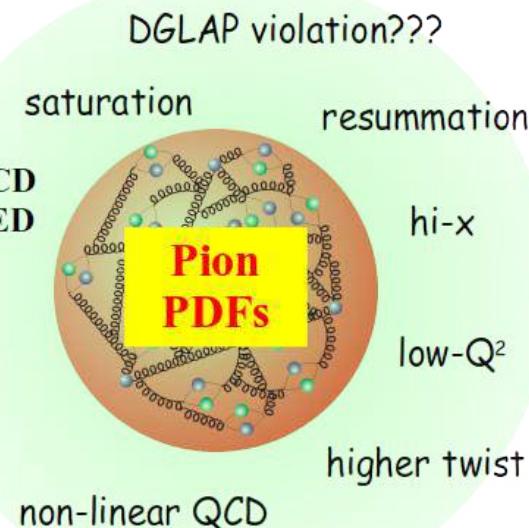
$$d\sigma \sim \frac{\theta^2}{(\theta^2 + \theta_D^2)^2} \quad \theta_D \sim \frac{m}{E}$$

# CONCLUSIONS

**QCD**  
Lagrangian



$$\mathcal{L}_{QCD} = \bar{\psi}_q (i\gamma_\mu D^\mu - m_q) \psi_q - \frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu}$$



- **Polarized PDFs**
- **GPDs & TMDs**
- **Fragmentation**



# BACKUP

# New Tools

PDFSense  
&  
... borrowing from AI

## Artificial Intelligence Tools: Projector tool of Google TensorFlow

### Embedding Projector

#### DATA

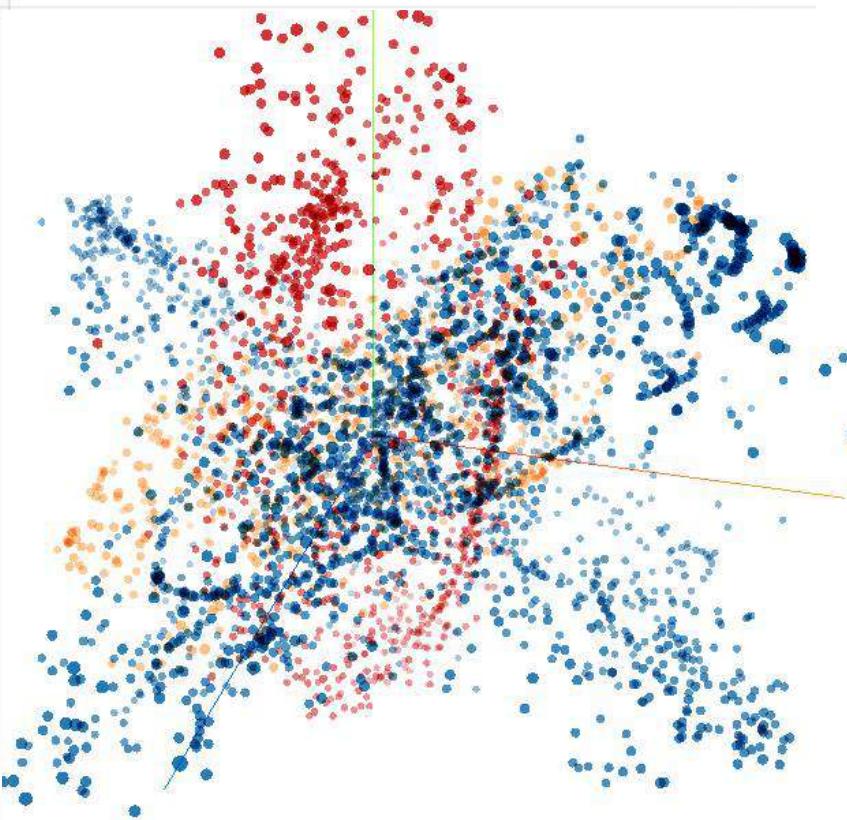
5 tensors found

Word2Vec 10K



A

Points: 4021 | Dimension: 56



Label by

Type

Color by

Type

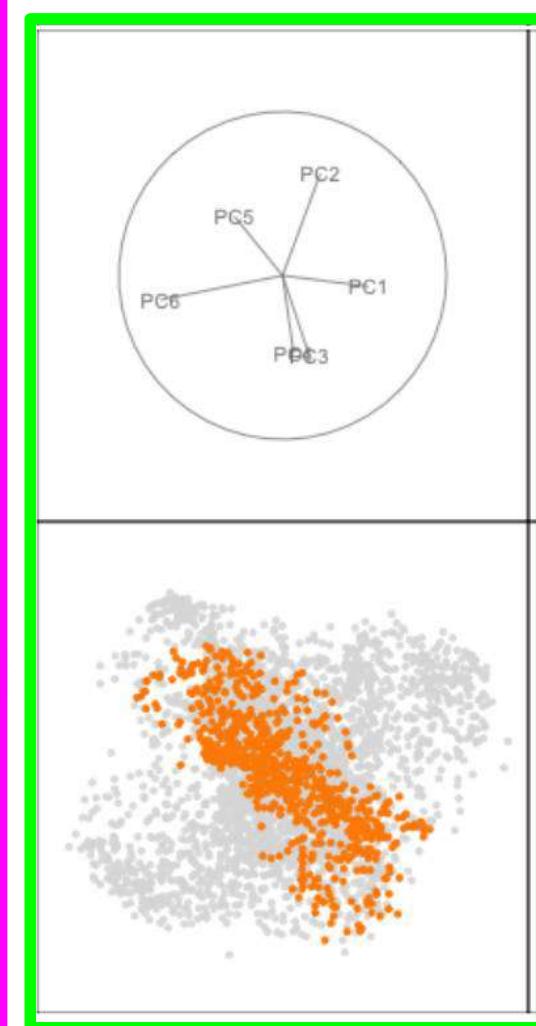
Sphereize data

Load data

Publish

Checkpoint: residual\_all\_norm\_-1\_RawData.tsv

Metadata: metadata\_RawData.tsv

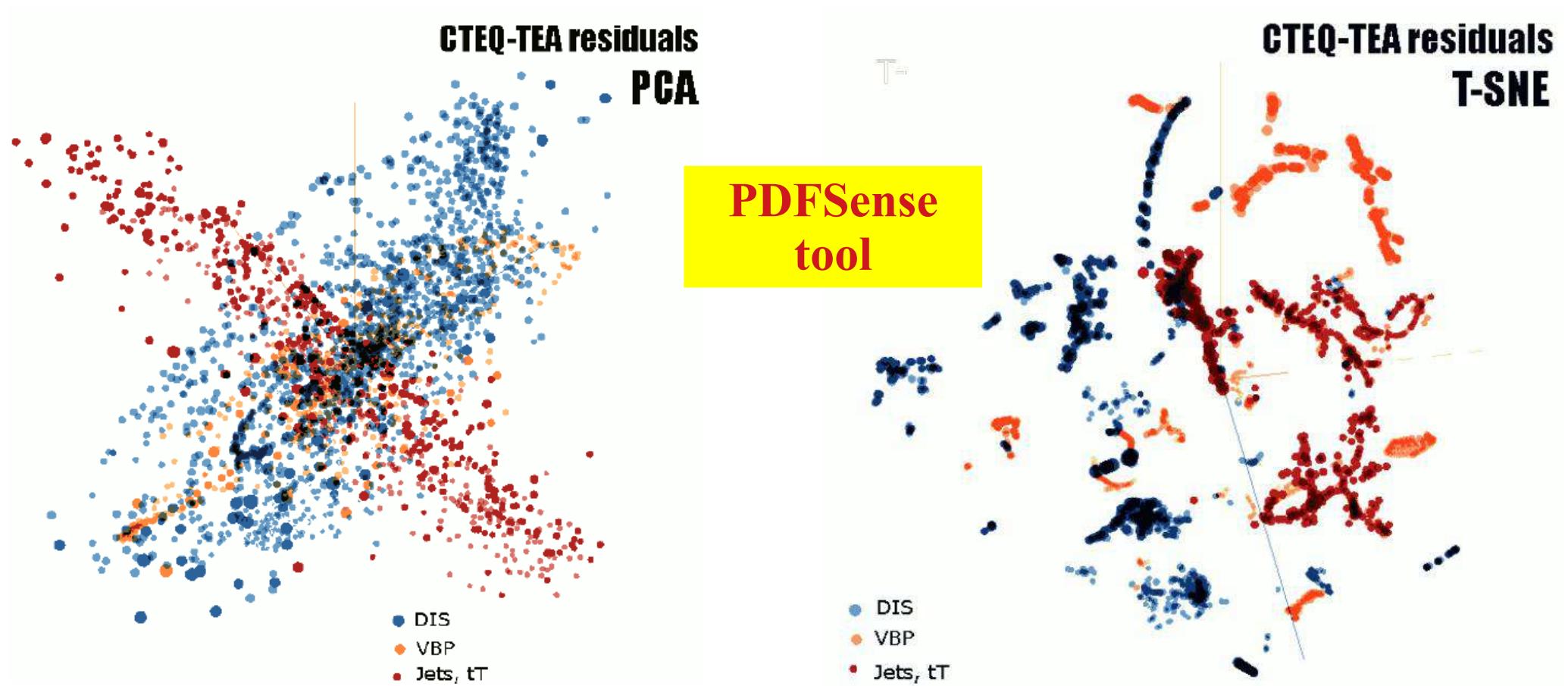


Dynamical projections for the visualization of PDFSense data

Dianne Cook, Ursula Laa, German Valencia arXiv:1806.09742

# TensorFlow Embedding Projector

<https://metapdf.hepforge.org/PDFSense/>



Principal Component Analysis (PCA) visualizes the 56-dim. manifold by reducing it to 10 dimensions  
(à la META PDFs)

<http://projector.tensorflow.org>

t-distributed stochastic neighbor embedding (t-SNE) sorts vectors according to their similarity

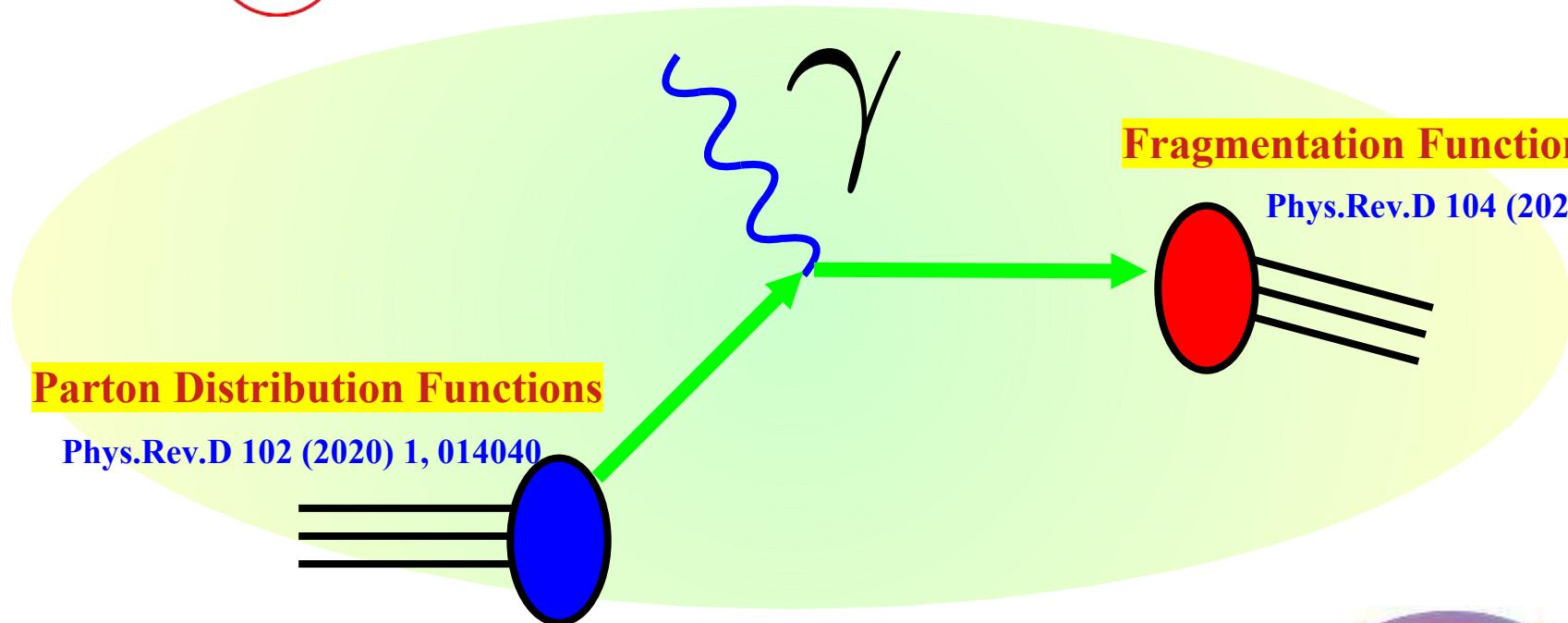
$$r_i(\vec{a}) = \frac{1}{s_i} (T_i(\vec{a}) - D_{i,sh}(\vec{a})).$$

# Pion PDFs & FFs

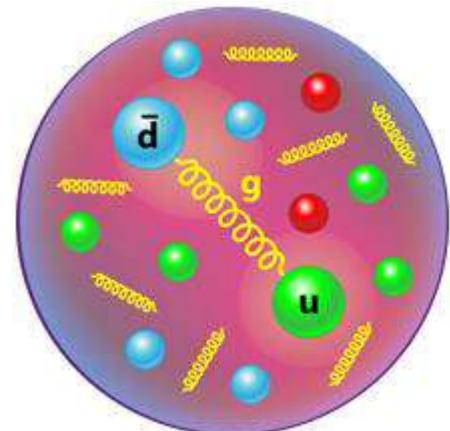
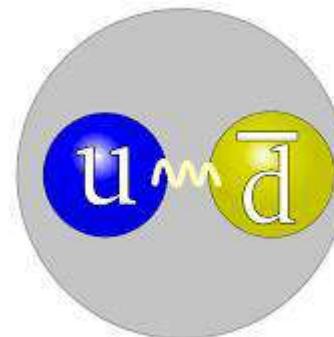


**Parton Distribution Functions**

**Fragmentation Functions**

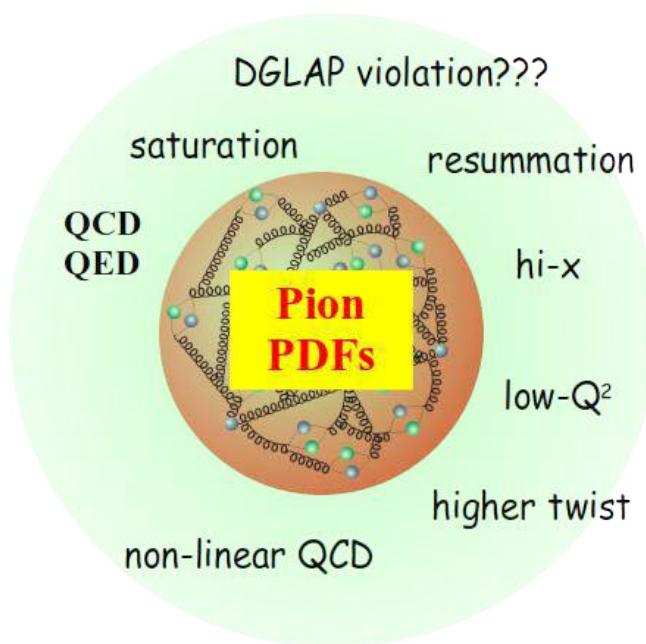


$$\text{Pion } \pi^+ = u\bar{d}$$



# xFitter Pion Fit

[Phys.Rev.D 102 \(2020\) 1, 014040](#)



Special thanks to: Ivan Novikov,  
Alexander Glazov, Oleksandr Zenaiev

## Parton Distribution Functions of the Charged Pion Within The xFitter Framework

xFitter Developers' team: Ivan Novikov,<sup>1, 2,\*</sup> Hamed Abdolmaleki,<sup>3</sup> Daniel Britzger,<sup>4</sup> Amanda Cooper-Sarkar,<sup>5</sup> Francesco Giuli,<sup>6</sup> Alexander Glazov,<sup>2,†</sup> Aleksander Kusina,<sup>7</sup> Agnieszka Luszczak,<sup>8</sup> Fred Olness,<sup>9</sup> Pavel Starovoitov,<sup>10</sup> Mark Sutton,<sup>11</sup> and Oleksandr Zenaiev<sup>12</sup>

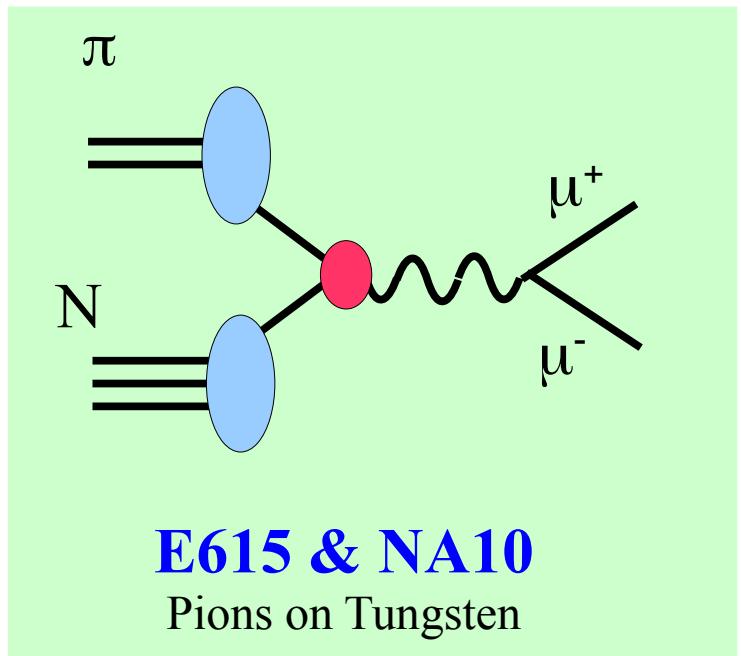
e-Print: 2002.02902 [hep-ph]

# xFitter Meson PDFs

*xFitter: open-source framework for global fits to meson PDFs*

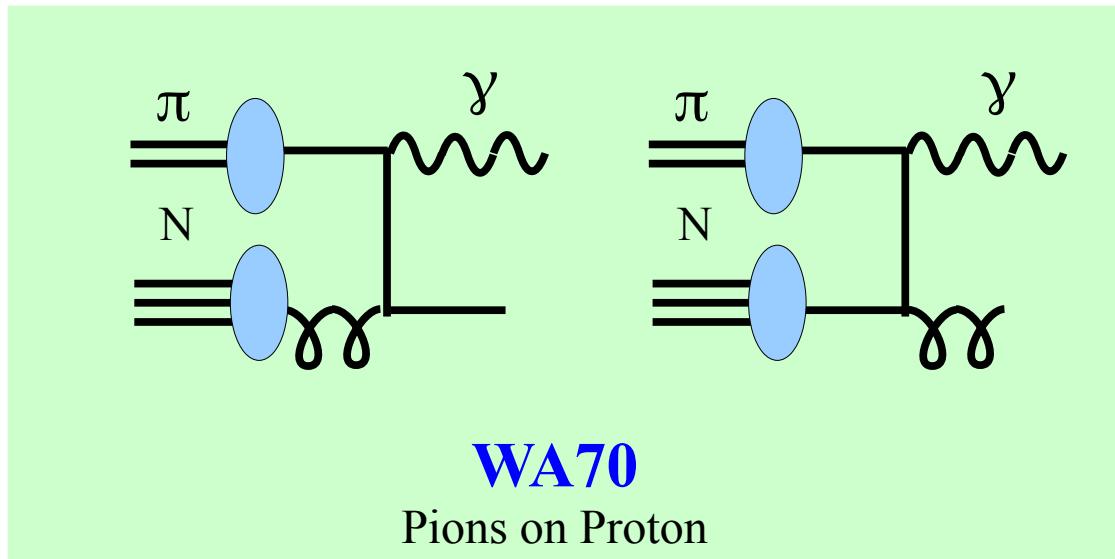


<https://www.xfitter.org/>



Experiment  $\chi^2/N_{\text{points}}$

E615	206/140
NA10 (194 GeV)	107/67
NA10 (286 GeV)	95/73
WA70	64/99

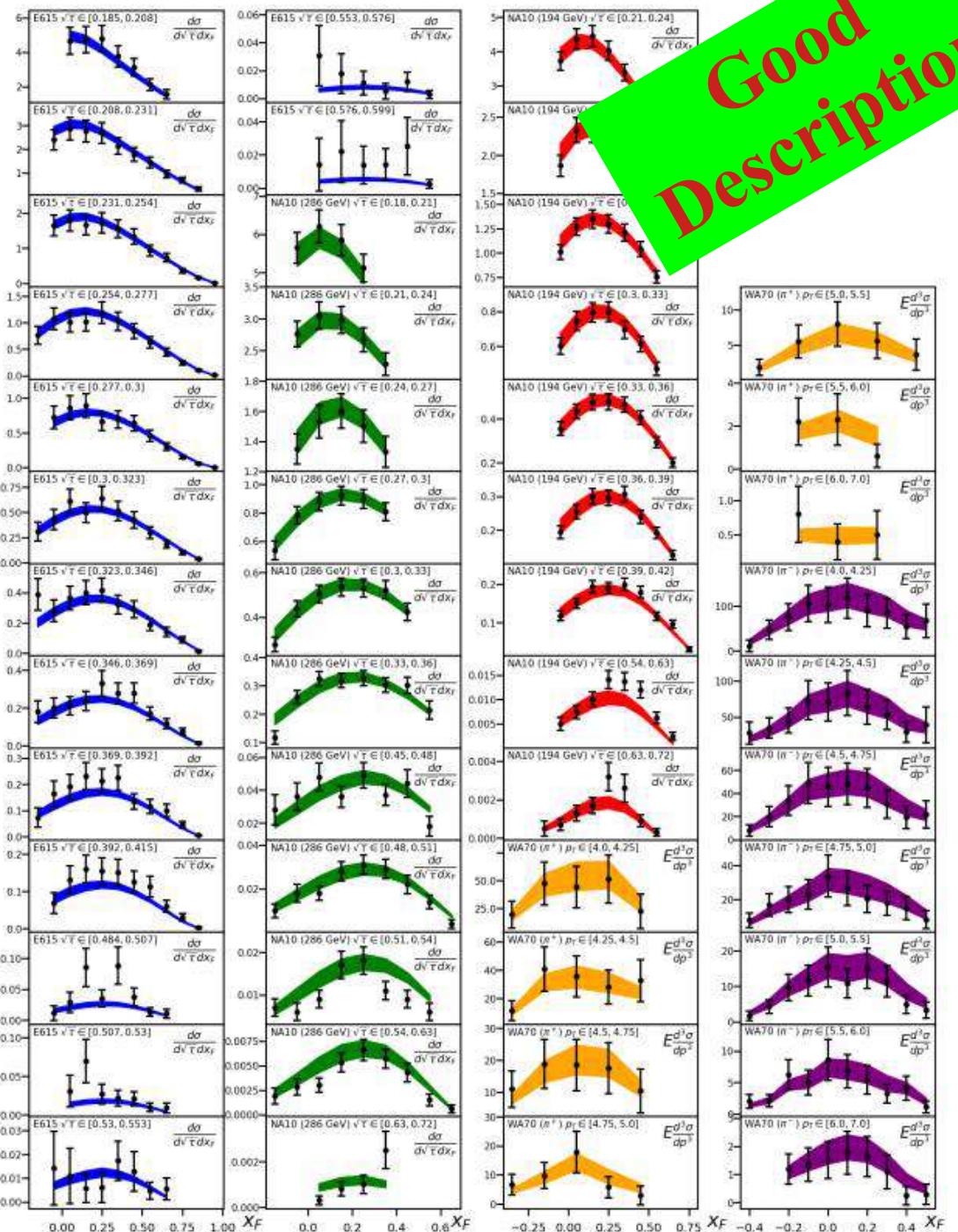


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e-Print: 2002.02902 [hep-ph]

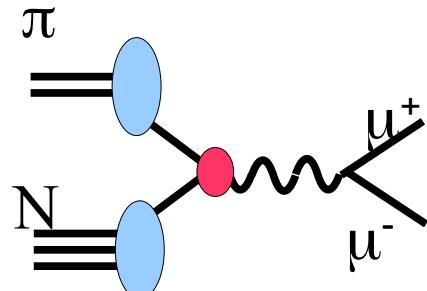
## Pion Data:



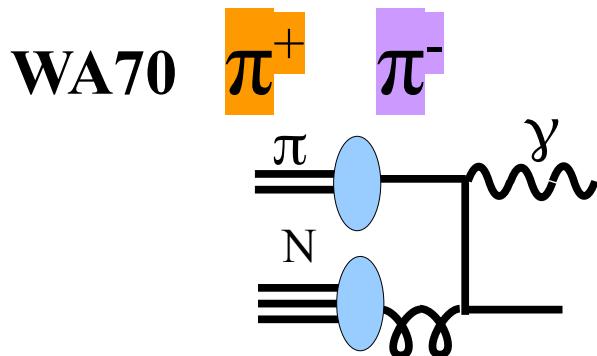
## Pions ( $\pi^-$ ) on Tungsten

**E615**  $E_\pi = 252 \text{ GeV}$

**NA10**  $E_\pi = 194 \text{ GeV}$  &  $286 \text{ GeV}$



## Pions ( $\pi^\pm$ ) on Proton



## NLO computation with MCFM / APPLGRID

- theory errors from  $\alpha_s$ , and nPDF uncertainties
- uncertainties include scale variations.
- for factorization scale variation

modify APPLGRID for two PDFs

# xFitter Pion PDFs

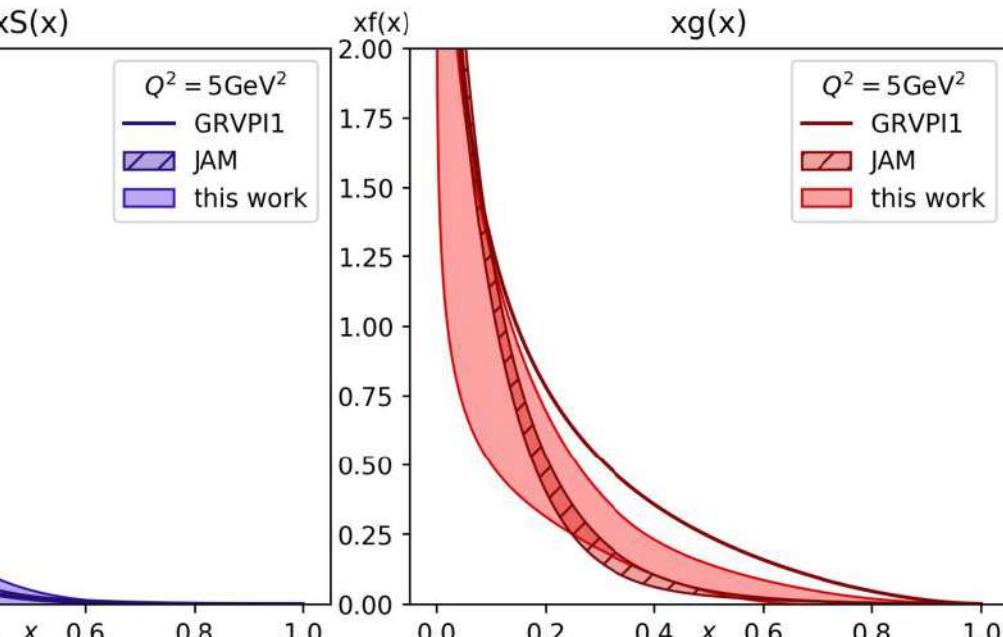
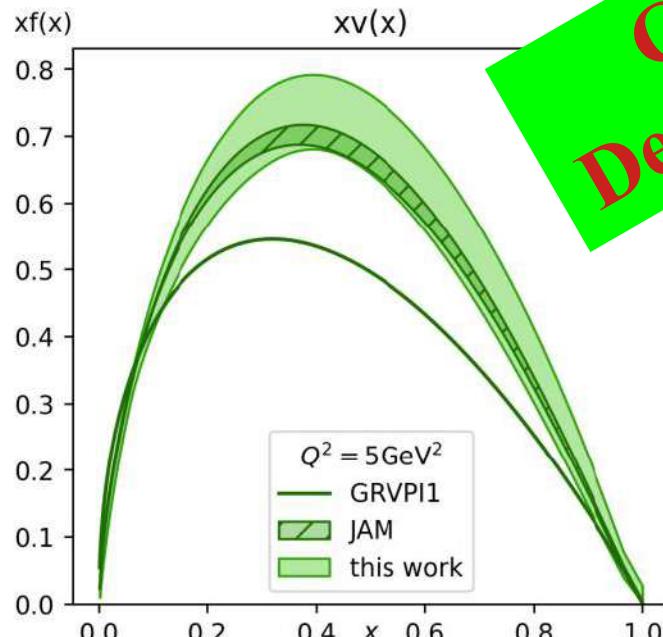
Experiment	Normalization uncertainty	$\chi^2/N_{\text{points}}$
E615	15 %	206/140
NA10 (194 GeV)	6.4%	107/67
NA10 (286 GeV)	6.4%	95/73
WA70	32%	64/99

$$xv(x) = A_v x^{B_v} (1-x)^{C_v} (1 + D_v x^\alpha),$$

$$xS(x) = A_S x^{B_S} (1-x)^{C_S} / \mathcal{B}(B_S + 1, C_S + 1),$$

$$xg(x) = A_g (C_g + 1) (1-x)^{C_g},$$

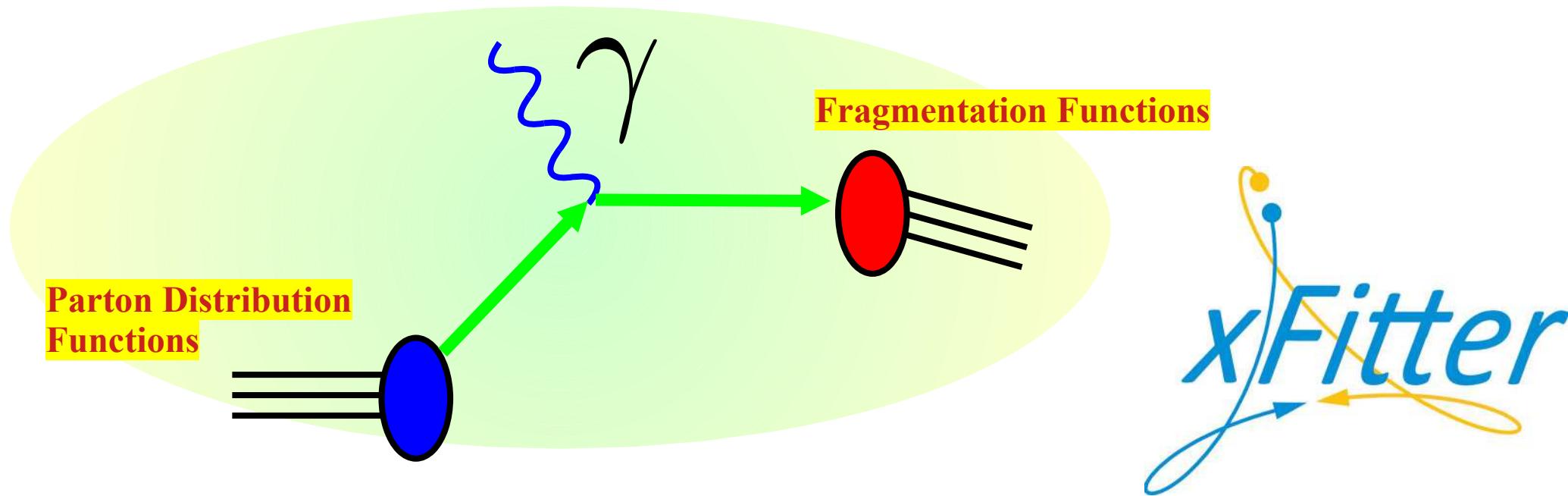
Good Description



	$\langle xv \rangle$	$\langle xS \rangle$	$\langle xg \rangle$	$Q^2$ (GeV <sup>2</sup> )
JAM [31]	$0.54 \pm 0.01$	$0.16 \pm 0.02$	$0.30 \pm 0.02$	1.69
JAM (DY)	$0.60 \pm 0.01$	$0.30 \pm 0.05$	$0.10 \pm 0.05$	1.69
this work	$0.55 \pm 0.06$	$0.26 \pm 0.15$	$0.19 \pm 0.16$	1.69
Lattice-3 [18]	$0.428 \pm 0.030$			4
SMRS [25]	0.47			4
Han et al. [44]	$0.51 \pm 0.03$			4
GRVPI1 [27]	0.39	0.11	0.51	4
Ding et al. [11]	$0.48 \pm 0.03$	$0.11 \pm 0.02$	$0.41 \pm 0.02$	4
this work	$0.50 \pm 0.05$	$0.25 \pm 0.13$	$0.25 \pm 0.13$	4
JAM	$0.48 \pm 0.01$	$0.17 \pm 0.01$	$0.35 \pm 0.02$	5
this work	$0.49 \pm 0.05$	$0.25 \pm 0.12$	$0.26 \pm 0.13$	5
Lattice-1 [16]	$0.558 \pm 0.166$			5.76
Lattice-2 [17]	0.48	0.04		5.76
this work	$0.48 \pm 0.05$	$0.25 \pm 0.12$	$0.27 \pm 0.13$	5.76
WRH [26]	$0.434 \pm 0.022$			27
ChQM-1 [13]	0.428			27
ChQM-2 [15]	0.46			27
this work	$0.42 \pm 0.04$	$0.25 \pm 0.10$	$0.32 \pm 0.10$	27
SMRS [25]	$0.49 \pm 0.02$			49
this work	$0.41 \pm 0.04$	$0.25 \pm 0.09$	$0.34 \pm 0.09$	49

# Pion Fragmentation Functions

Phys.Rev.D 104 (2021) 5, 056019



*Hamed Abdolmaleki, Maryam Soleymaninia, Hamzeh Khanpour*

PHYSICAL REVIEW D 104, 056019 (2021)

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## QCD analysis of pion fragmentation functions in the xFitter framework

Hamed Abdolmaleki,<sup>1,\*</sup> Maryam Soleymaninia,<sup>1,†</sup> Hamzeh Khanpour<sup>1,2,3,‡</sup> Simone Amoroso<sup>4,§</sup> Francesco Giulio<sup>4,||</sup>, Alexander Glazov<sup>4,¶</sup> Agnieszka Luszczak<sup>6,\*\*</sup> Fredrick Olness<sup>7,††</sup> and Oleksandr Zenaiev<sup>8,‡‡</sup>

(xFITTER Developers' Team:)

# xFitter: Multiple fits with a vast array of data sets

HAMED ABDOLMALEKI *et al.*PHYS. REV. D **104**, 056019 (2021)

TABLE I. The Single Inclusive electron-positron Annihilation (SIA) datasets used in the pion FFs analysis. The values of  $\chi^2$  per  $N$  data points for the individual SIA experiments are shown. The  $z$  range for each experiment is displayed in Fig. 8. The measured observable is also listed where  $\sqrt{s}$  is the total CMS energy,  $\beta = p_h/E_h$ , and  $z = 2E_h/\sqrt{s}$ .

Observable	Experiment	$\sqrt{s}$ [GeV]	$\chi^2/\text{number of points}$					
			Fit A (NLO)	Fit A (NNLO)	Fit B (NNLO)	Fit C (NNLO)	Fit D (NNLO)	Fit E (NNLO)
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}$	SLD	91.20	57/34	41/34	41/34	48/34	39/34	45/34
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}  _{\text{uds}}$	SLD <sub>uds</sub>	91.20	66/34	52/34	56/34	44/34	43/34	45/34
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}  _c$	SLD <sub>c</sub>	91.20	35/34	33/34	32/34	32/34	32/34	32/34
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}  _b$	SLD <sub>b</sub>	91.20	25/34	24/34	24/34	24/34	23/34	24/34
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dp_h}$	OPAL	91.20	42/24	41/24	41/24	39/24	39/24	39/24
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dp_h}$	DELPHI	91.20	37/21	41/21	41/21	44/21	44/21	43/21
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dp_h}  _{\text{uds}}$	DELPHI <sub>uds</sub>	91.20	25/21	27/21	26/21	30/21	31/21	30/21
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dp_h}  _b$	DELPHI <sub>b</sub>	91.20	20/21	20/21	21/21	19/21	20/21	19/21
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}$	ALEPH	91.20	21/23	14/23	14/23	11/23	11/23	12/23
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}$	TASSO44	44.00	15/6	17/6	15/6	18/6	16/6	18/6
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}$	TASSO34	34.00	6.8/9	8.0/9	6.8/9	9.3/9	7.3/9	8.3/9
$\frac{1}{\beta\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}$	TPC	29.00	6.3/13	11/13	11/13	11/13	7.1/13	9.2/13
$\frac{s}{\beta} \frac{d\sigma^h}{d\beta}$	TASSO22	22.00	5.7/8	5.5/8	5.6/8	6.1/8	5.9/8	5.8/8
$\frac{s}{\beta} \frac{d\sigma^h}{d\beta}$	TASSO14	14.00	11/9	11/9	11/9	9.9/9	11/9	9.8/9
$\frac{s}{\beta} \frac{d\sigma^h}{d\beta}$	TASSO12	12.00	1.4/4	1.4/4	1.3/4	0.96/4	1.4/4	1.1/4
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dp_h}$	BABAR	10.52	71/40	53/40	77/40	...	...	33/37
$\frac{d\sigma^h}{dz}$	BELLE13	10.54	21/70	14/70	...	...	...	...
$\frac{d\sigma^h}{dz}$	BELLE20	10.58	...	...	82/32	32/32	9.2/28	17/28
Correlated $\chi^2$			11	9.4	8.4	16	9.4	12
Log penalty $\chi^2$			+4.2	+3.0	+4.2	+7.7	+5.6	+6.8
Total $\chi^2/\text{dof}$			480/386	427/386	518/348	404/308	357/304	410/341

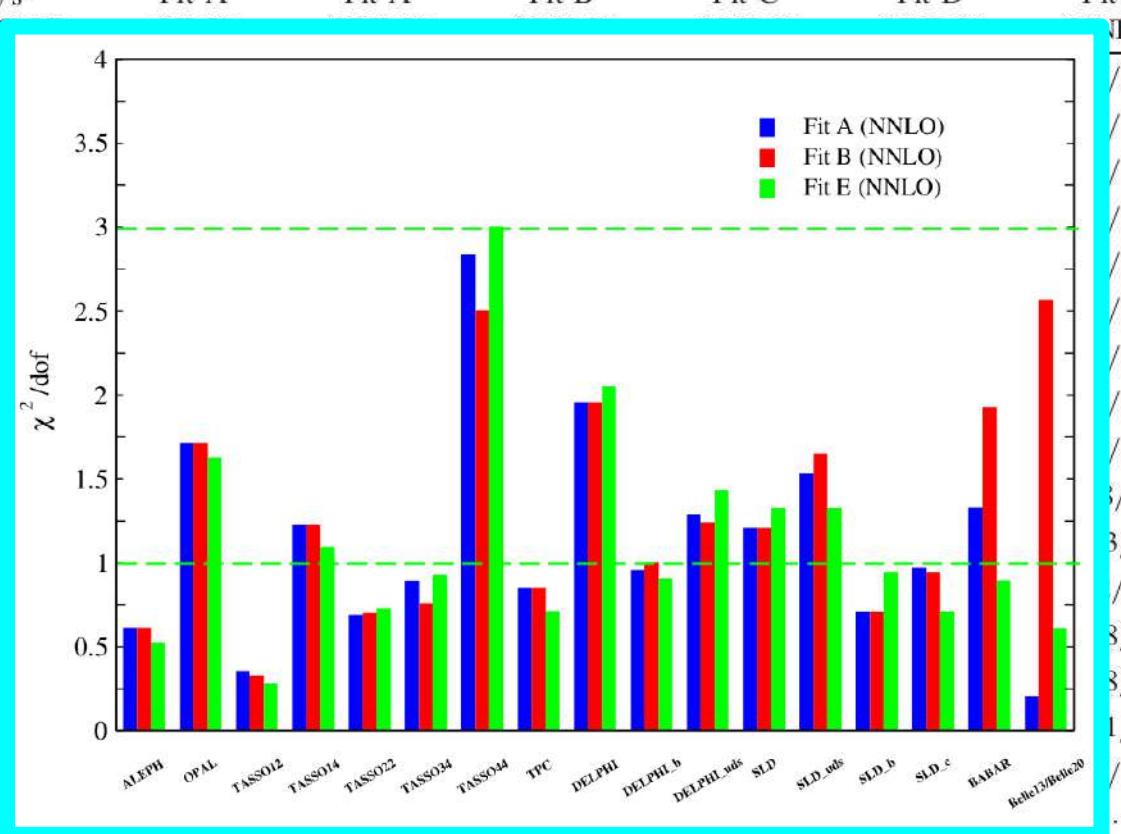
# xFitter: Multiple fits with a vast array of data sets

HAMED ABDOLMALEKI *et al.*

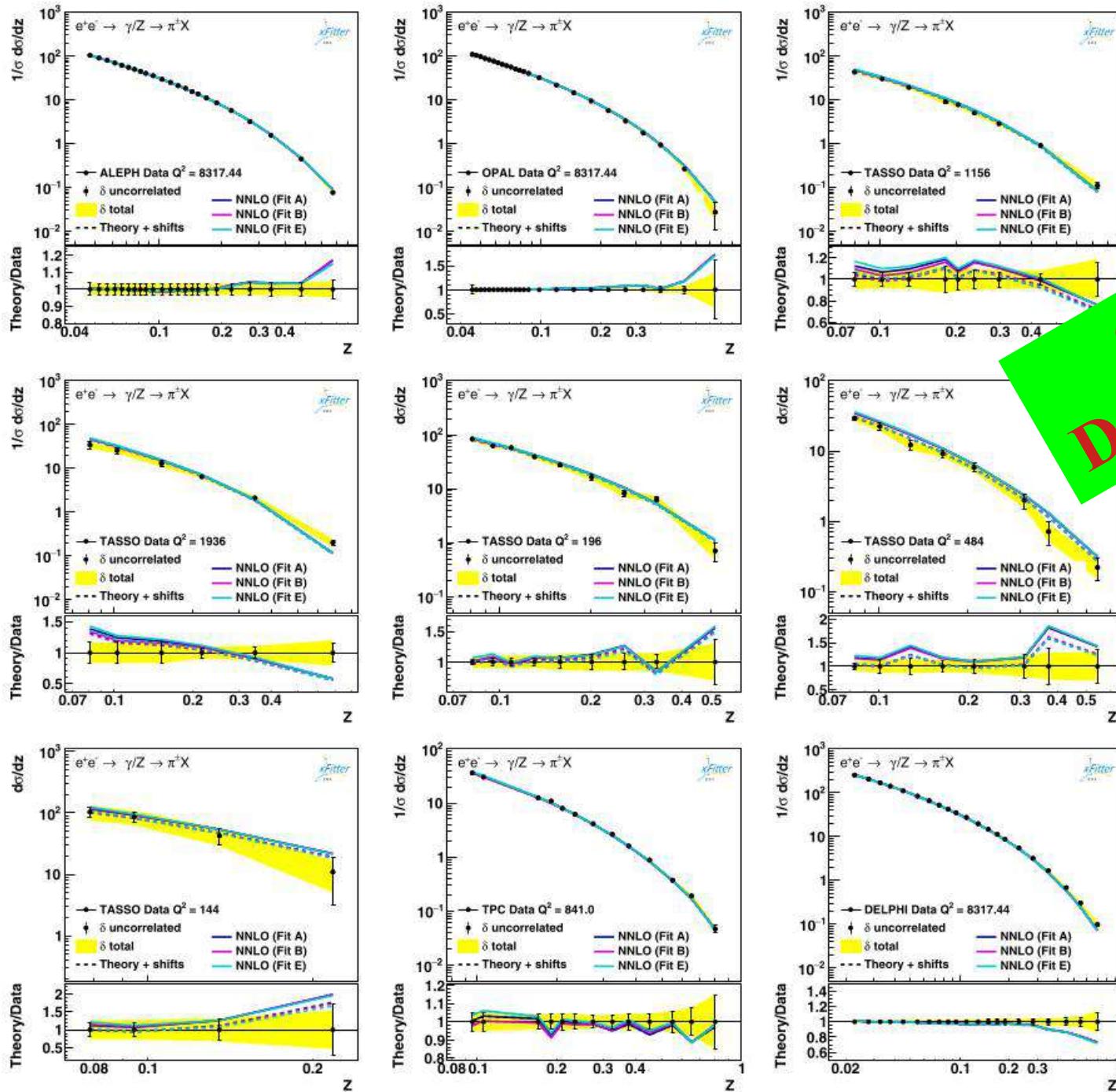
PHYS. REV. D 104, 056019 (2021)

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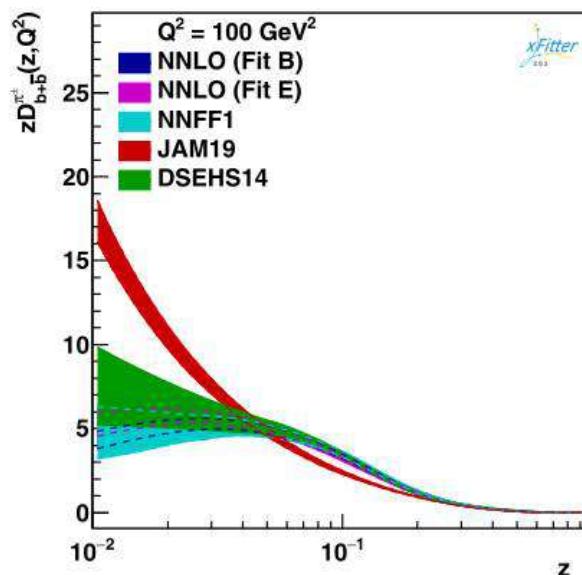
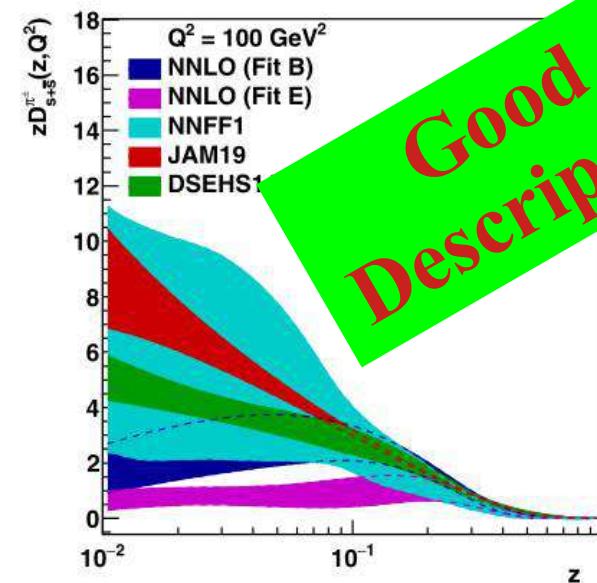
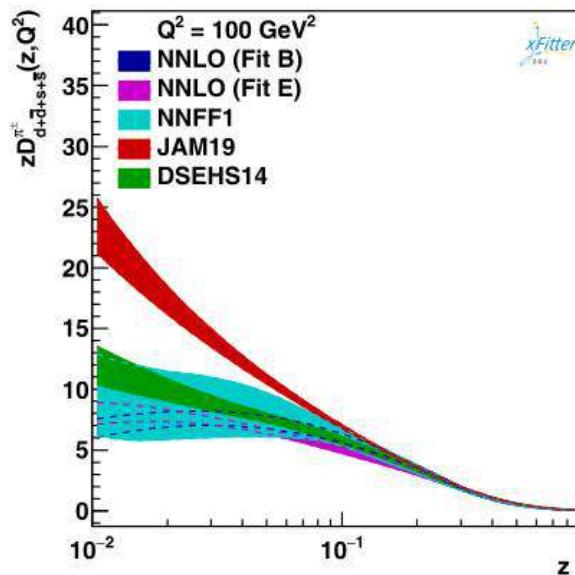
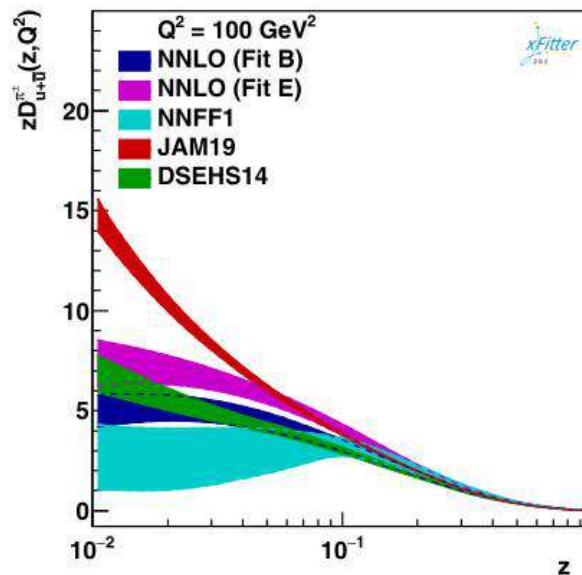
Observable	Experiment	$\sqrt{s}$ [GeV]	$\chi^2/\text{number of points}$					
			Fit A	Fit A	Fit B	Fit C	Fit D	Fit E
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}$	SLD	9						
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}  _{uds}$	SLD <sub>uds</sub>	9						
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}  _c$	SLD <sub>c</sub>	9						
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}  _b$	SLD <sub>b</sub>	9						
$\frac{1}{\sigma_{\text{tot}}} \frac{dp_h}{dp_h}$	OPAL	9						
$\frac{1}{\sigma_{\text{tot}}} \frac{dp_h}{dp_h}$	DELPHI	9						
$\frac{1}{\sigma_{\text{tot}}} \frac{dp_h}{dp_h}  _{uds}$	DELPHI <sub>uds</sub>	9						
$\frac{1}{\sigma_{\text{tot}}} \frac{dp_h}{dp_h}  _b$	DELPHI <sub>b</sub>	9						
$\frac{1}{\sigma_{\text{tot}}} \frac{dp_h}{dp_h}$	ALEPH	9						
$\frac{1}{\sigma_{\text{tot}}} \frac{dp_h}{dp_h}$	TASSO44	9						
$\frac{1}{\sigma_{\text{tot}}} \frac{dp_h}{dp_h}$	TASSO34	4						
$\frac{1}{\beta\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}$	TPC	4						
$\frac{s}{\beta} \frac{d\sigma^h}{dz}$	TASSO22	2						
$\frac{s}{\beta} \frac{d\sigma^h}{dz}$	TASSO14	1						
$\frac{s}{\beta} \frac{d\sigma^h}{dz}$	TASSO12	1						
$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dp_h}$	BABAR	1						
$\frac{d\sigma^h}{dz}$	BELLE13	1						
$\frac{d\sigma^h}{dz}$	BELLE20	10.58	...	...	82/32	32/32	9.2/28	17/28
Correlated $\chi^2$			11	9.4	8.4	16	9.4	12
Log penalty $\chi^2$			+4.2	+3.0	+4.2	+7.7	+5.6	+6.8
Total $\chi^2/\text{dof}$			480/386	427/386	518/348	404/308	357/304	410/341



# xFitter: Detailed comparison with data sets



Good Description



Good description of the data in general

Deviations in the low-z region

BELLE and BaBar data pull in opposite directions

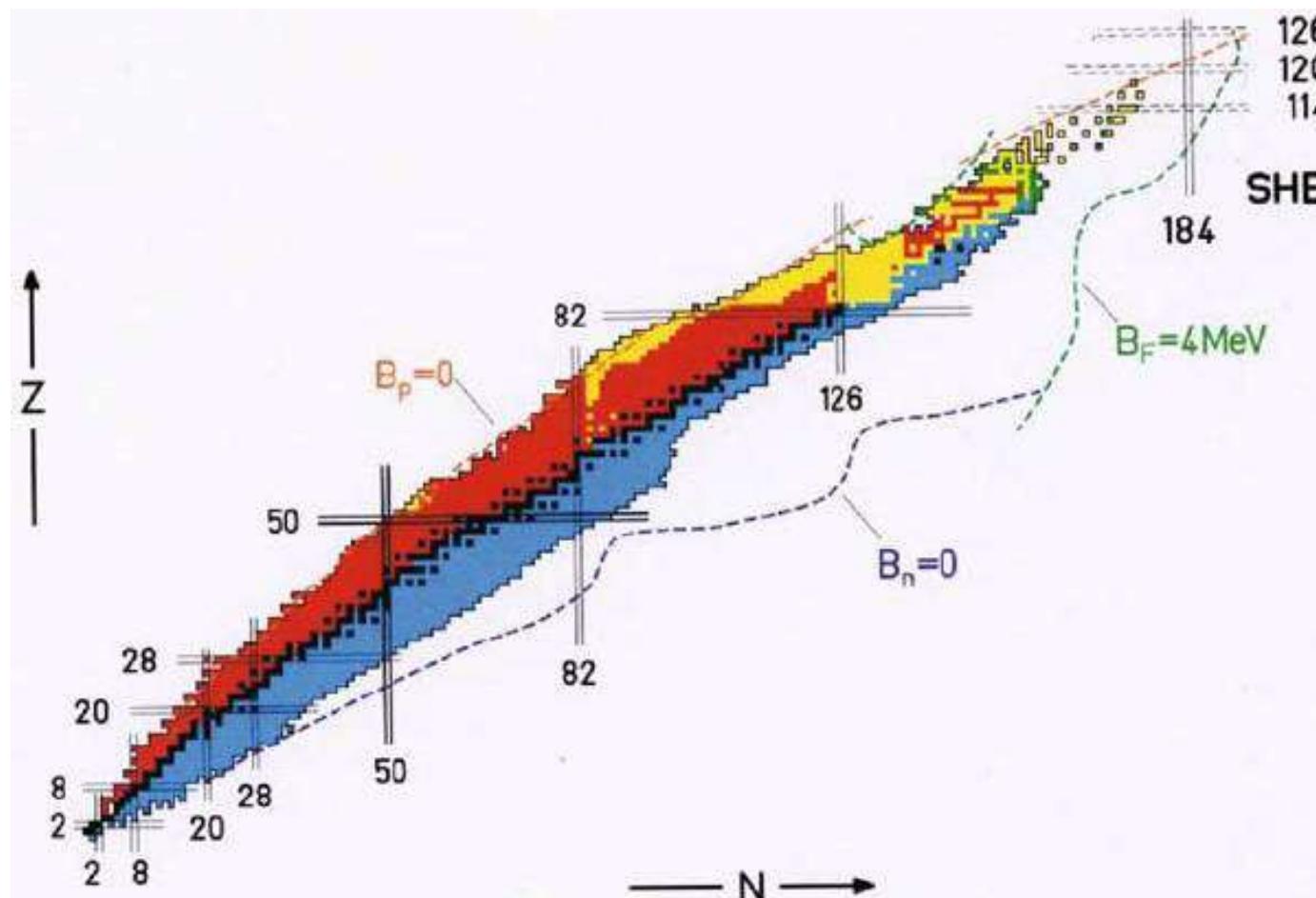
Clearly further investigation is warranted

# Target Mass Corrections (TMC)

*The challenge of a multi-scale problem*

...

Ingo Schienbein, Chloe Leger, Richard Ruiz ...



## Example #2: Multi-Scale Problems are Challenging

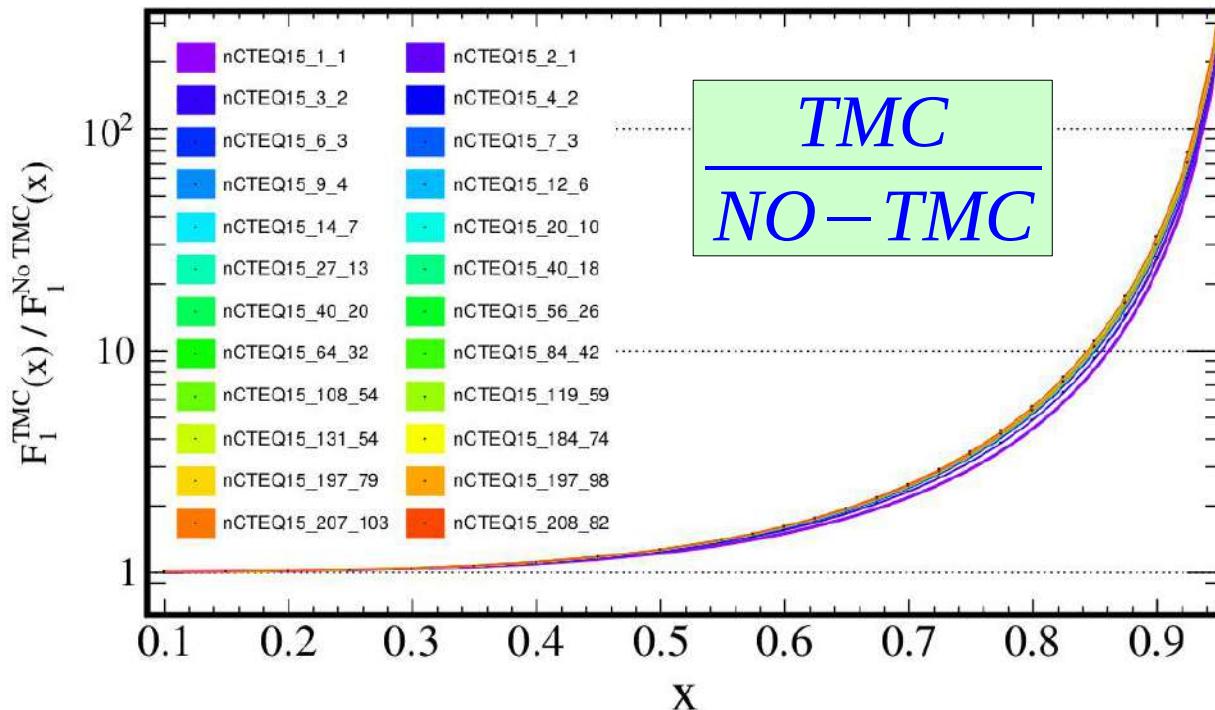
### Two-Loop Total Cross Section: One Scale

$$\sigma(Q^2) = \sigma_0 \left\{ 1 + \frac{\alpha_s(Q^2)}{4\pi} (3C_F) + \left( \frac{\alpha_s(Q^2)}{4\pi} \right)^2 \left[ -C_F^2 \left( \frac{3}{2} \right) + C_F C_A \left( \frac{123}{2} - 44\zeta(3) \right) + C_F T n_f (-22 + 16\zeta(3)) \right] \right\}$$

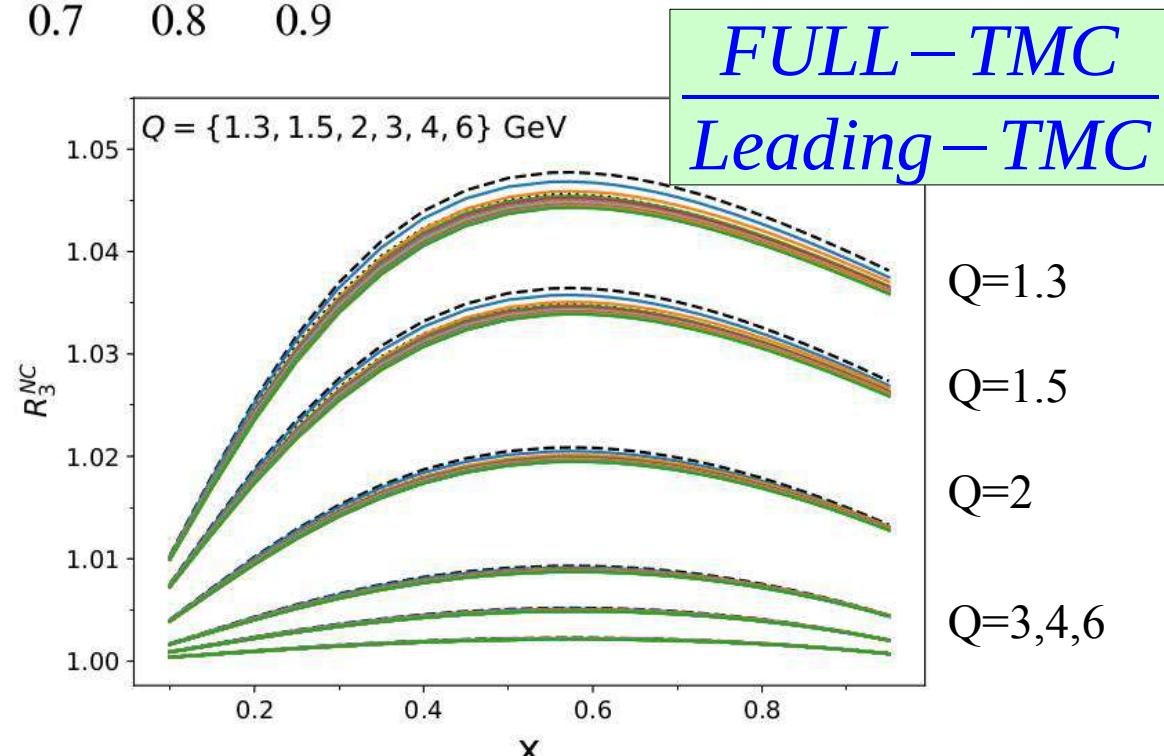
### Two-Loop Drell-Yan Cross Section: Two Scales

$$\begin{aligned}
H_{q\bar{q}}^{(2), S+V}(z) = & \left( \frac{\alpha_s}{4\pi} \right)^2 \delta(1-z) \left\{ C_A C_F \left[ [\frac{193}{3} - 24\zeta(3)] \ln \left( \frac{Q^2}{M^2} \right) - 11 \ln^2 \left( \frac{Q^2}{M^2} \right) - \frac{12}{5} \zeta(2)^2 + \frac{592}{9} \zeta(2) + 28\zeta(3) - \frac{1535}{12} \right] \right. \\
& + C_F^2 \left[ [18 - 32\zeta(2)] \ln^2 \left( \frac{Q^2}{M^2} \right) + [24\zeta(2) + 176\zeta(3) - 93] \ln \left( \frac{Q^2}{M^2} \right) \right. \\
& \quad \left. \left. + \frac{8}{5} \zeta(2)^2 - 70\zeta(2) - 60\zeta(3) + \frac{511}{4} \right] \right\} \\
& + n_f C_F \left[ 2 \ln^2 \left( \frac{Q^2}{M^2} \right) - \frac{34}{3} \ln \left( \frac{Q^2}{M^2} \right) + 8\zeta(3) - \frac{112}{9} \zeta(2) + \frac{127}{6} \right] \\
& + C_A C_F \left[ -\frac{44}{3} \mathcal{D}_0(z) \ln^2 \left( \frac{Q^2}{M^2} \right) + \{[\frac{536}{9} - 16\zeta(2)] \mathcal{D}_0(z) - \frac{176}{3} \mathcal{D}_1(z)\} \ln \left( \frac{Q^2}{M^2} \right) \right. \\
& \quad \left. - \frac{176}{3} \mathcal{D}_2(z) + [\frac{1072}{9} - 32\zeta(2)] \mathcal{D}_1(z) + [56\zeta(3) + \frac{176}{3} \zeta(2) - \frac{1616}{27}] \mathcal{D}_0(z) \right] \\
& + C_F^2 \left[ [64\mathcal{D}_1(z) + 48\mathcal{D}_0(z)] \ln^2 \left( \frac{Q^2}{M^2} \right) + \{192\mathcal{D}_2(z) + 96\mathcal{D}_1(z) - [128 + 64\zeta(2)] \mathcal{D}_0(z)\} \ln \left( \frac{Q^2}{M^2} \right) \right. \\
& \quad \left. + 128\mathcal{D}_3(z) - (128\zeta(2) + 256) \mathcal{D}_1(z) + 256\zeta(3) \mathcal{D}_0(z) \right] \\
& + n_f C_F \left[ \frac{8}{3} \mathcal{D}_0(z) \ln^2 \left( \frac{Q^2}{M^2} \right) + [\frac{32}{3} \mathcal{D}_1(z) - \frac{80}{9} \mathcal{D}_0(z)] \ln \left( \frac{Q^2}{M^2} \right) + \frac{32}{3} \mathcal{D}_2(z) - \frac{160}{9} \mathcal{D}_1(z) + [\frac{224}{27} - \frac{32}{3} \zeta(2)] \mathcal{D}_0(z) \right].
\end{aligned}$$

Ref:  
CTEQ  
Handbook



TMCs can be large



Corrections are nearly universal

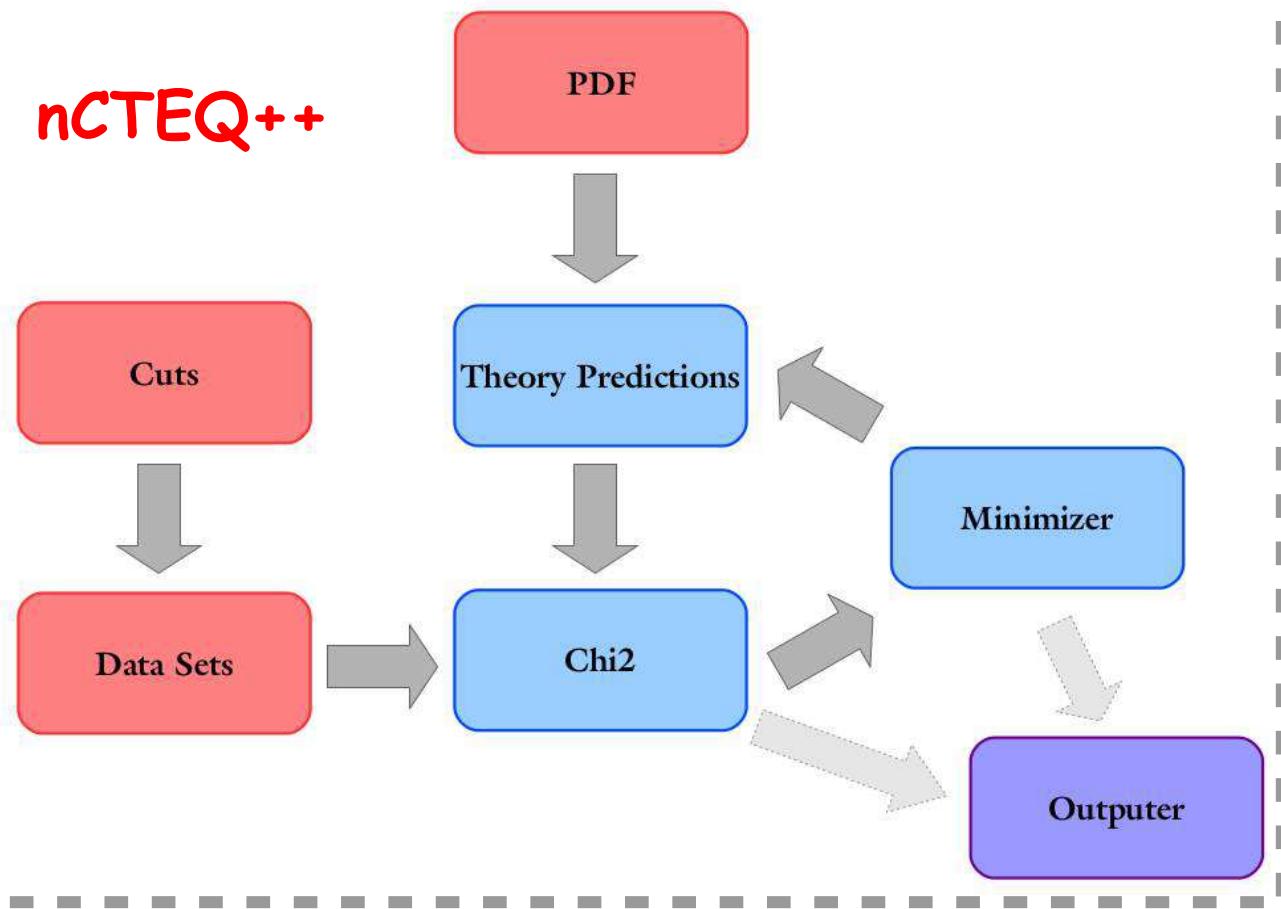


# nCTEQ++

*a modern, modular code base*

Top level C++, modular structure, output to YAML & Python scripts

## nCTEQ++



Special thanks to:

Tomas Jezo  
Eric Godat  
Florian Lyonnet  
Aleksander Kusina

Use external programs

- Minuit
- HOPPET
- MCFM
- APPLgrid



## Pre-Computed Grids

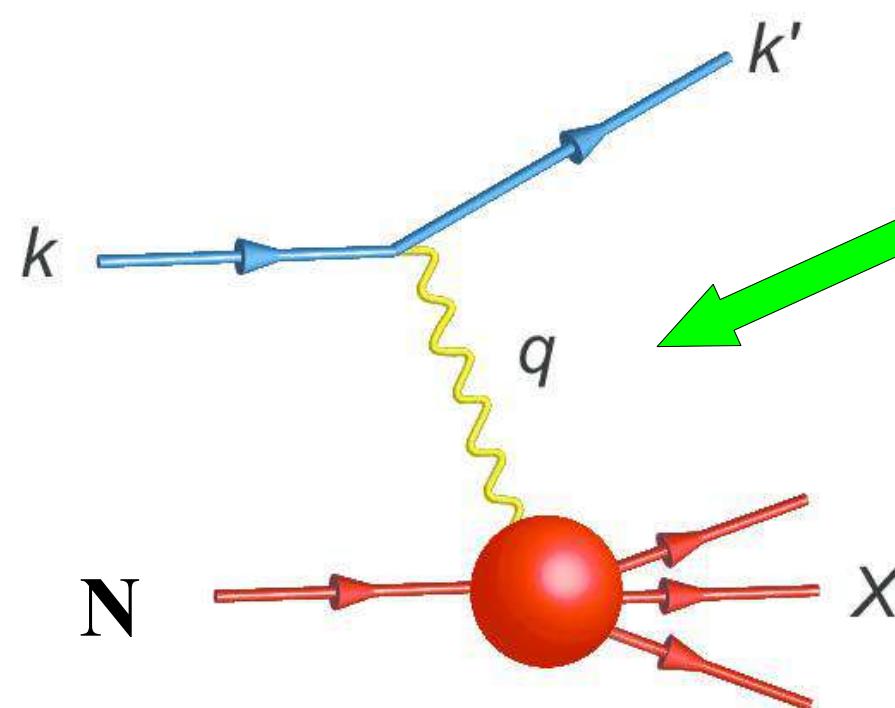
Tremendous speed-up for higher order calculation

... for example ...

High order DIS processes  
(Peter Risse)

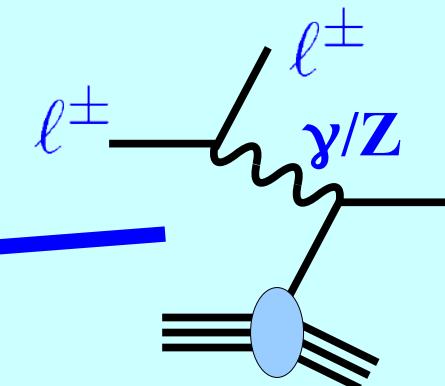
# Neutrino Deep Inelastic Scattering (DIS)

Faiq Muzakka, Karol Kovarik, ...



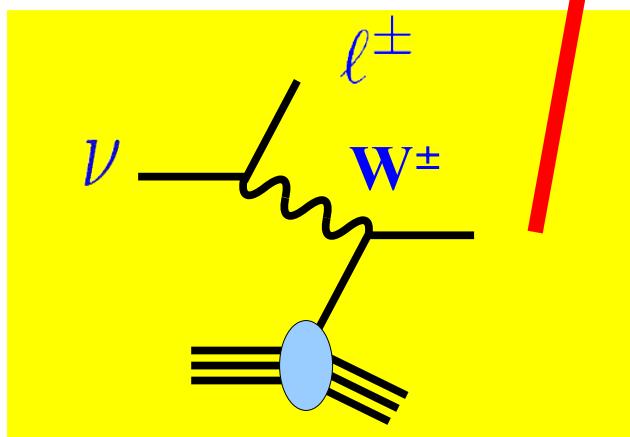
Could be:  
neutral photon  $\gamma$   
or charged  $W^\pm$

## Charged Lepton DIS



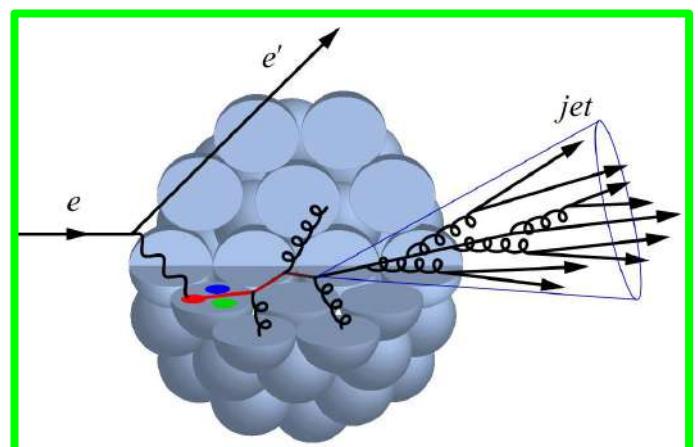
some caveats  
... correlated errors

Ingo Schienbein, ... (2007)  
Karol Kovarik, ... (2010)



## Neutrino DIS

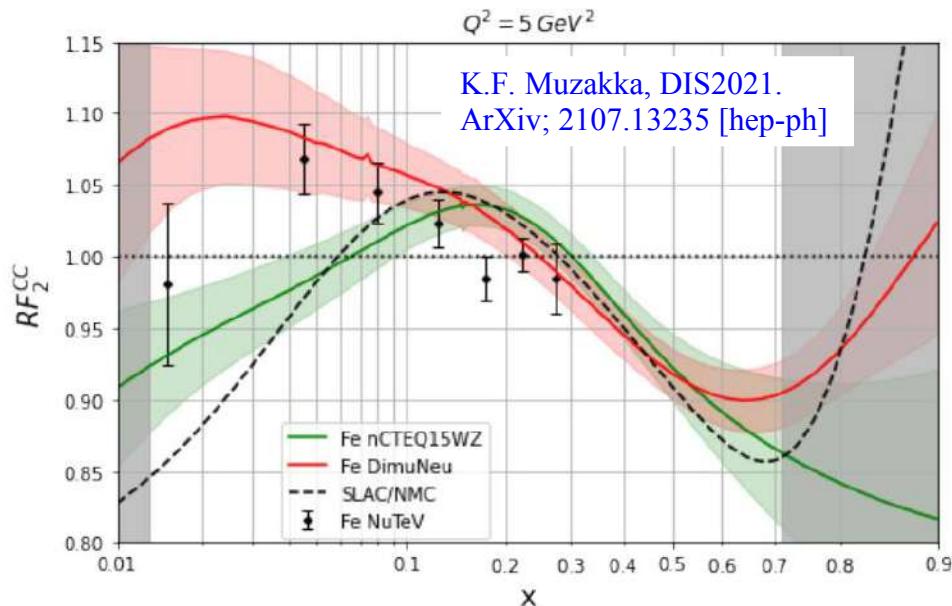
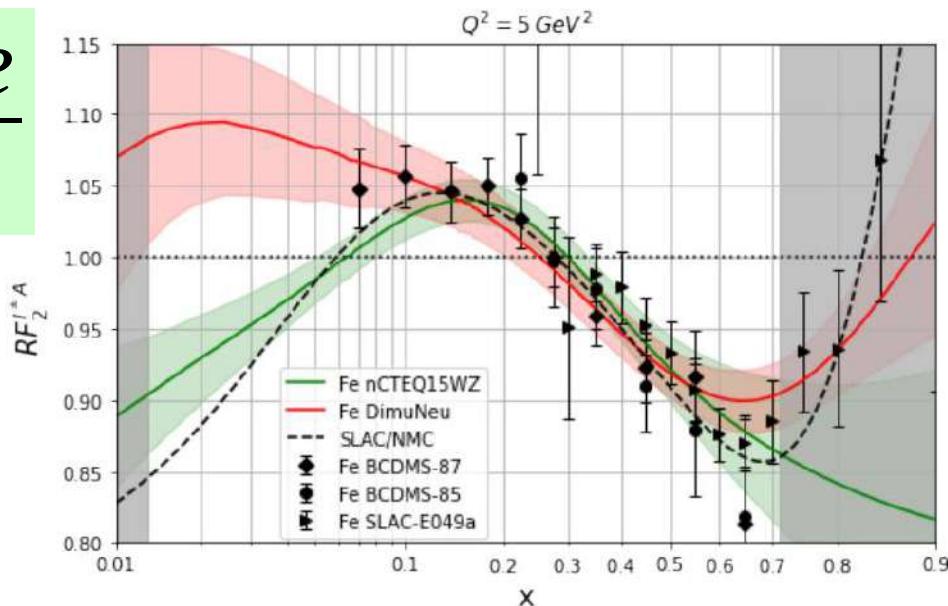
Depends on nuclear corrections



Propagation of  $\gamma/W$  thru nuclei

Faiq Muzakka, Karol Kovarik, ...

$\frac{Fe}{D}$



*Iron*  


---

 $(proton + neutron)$

What is the correct nuclear correction ???  
 Are these data sets compatible???

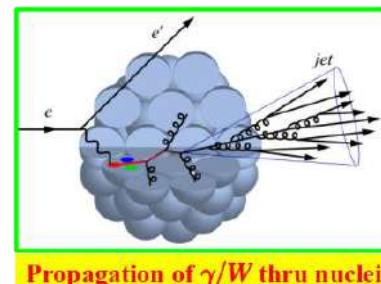
STAY TUNED!



### Compatibility of neutrino DIS data and its impact on nuclear parton distribution functions

K.F. Muzakka <sup>1,\*</sup>, P. Duwentäster <sup>1,†</sup>, T.J. Hobbs <sup>2,3,4</sup>, T. Ježo <sup>5,‡</sup>, M. Klasen <sup>1,§</sup>, K. Kovářík <sup>1,¶</sup>, A. Kusina <sup>6,\*\*</sup>, J.G. Morfin <sup>7,††</sup>, F. I. Olness <sup>2,††</sup>, R. Ruiz <sup>6</sup>, I. Schienbein <sup>8,§§</sup>

<sup>1</sup> Institut für Theoretische Physik, Westfälische Wilhelms-Universität Münster.



Propagation of  $\gamma/W$  thru nuclei

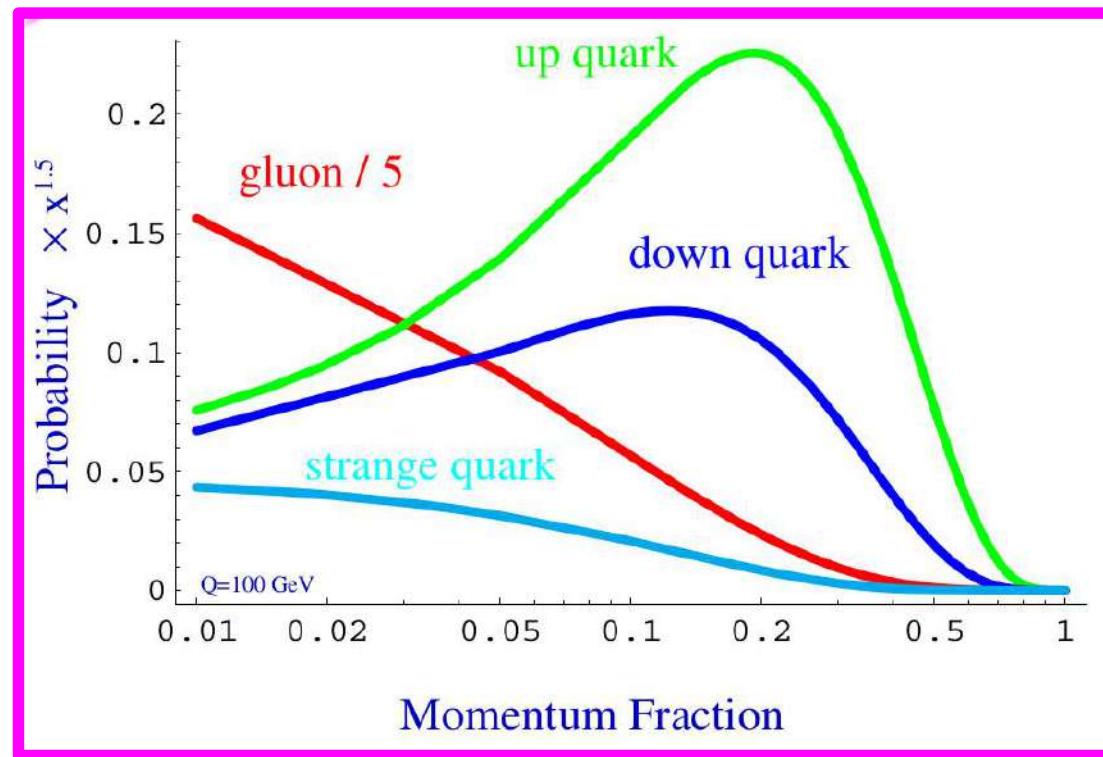
# Strange PDF

Parton Distribution Functions



*... this has a significant impact on the strange quark PDF*

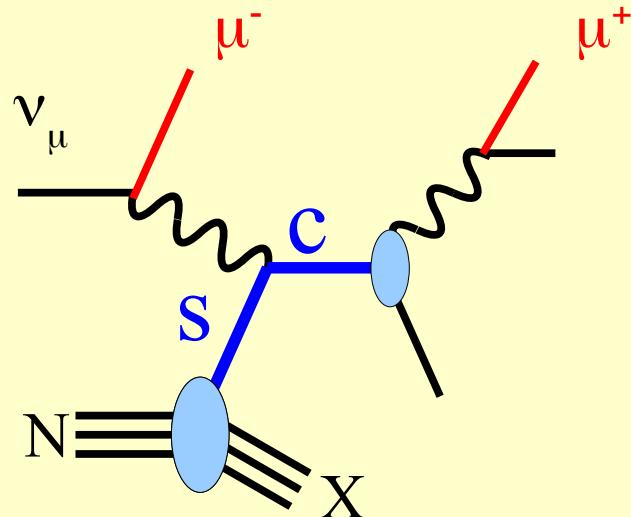
Need to “dig out”  
 $s(x)$  underneath  $d(x)$



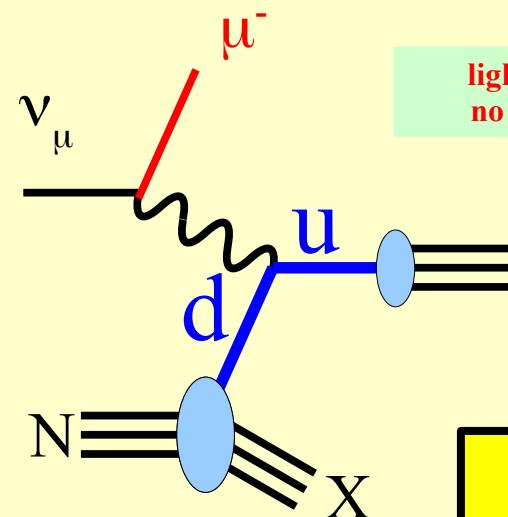
**Result:**

$$\bar{s}(x) \sim \frac{1}{2} \bar{d}(x)$$

## Strange Quark



## Down Quark

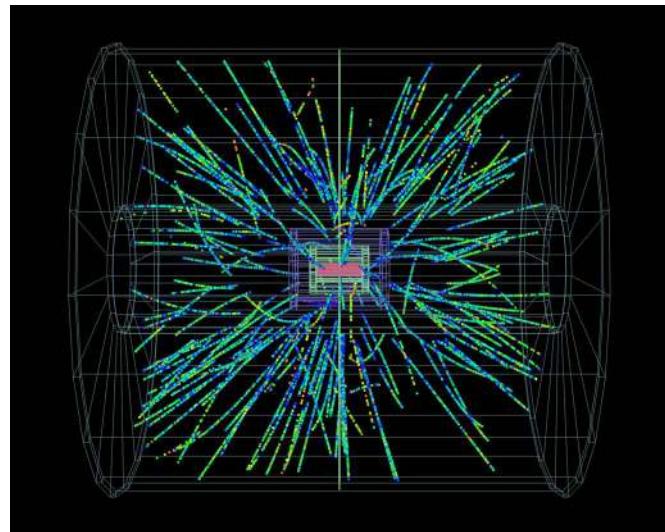


light u mass  
no isolated  $\mu$

Depends on  
nuclear PDFs

# W and Z Boson Production at the Large Hadron Collider (LHC)

Tomas Jezo, Aleksander Kusina, Fred Olness, ...

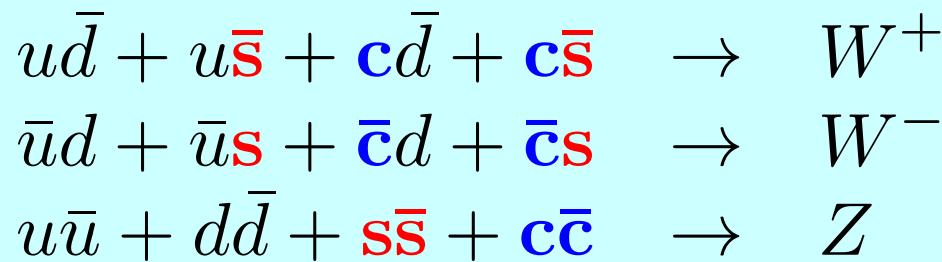


$$\begin{aligned} p \ p &\rightarrow W, Z \\ p \ Pb &\rightarrow W, Z \end{aligned}$$

**LHC Heavy Ion**

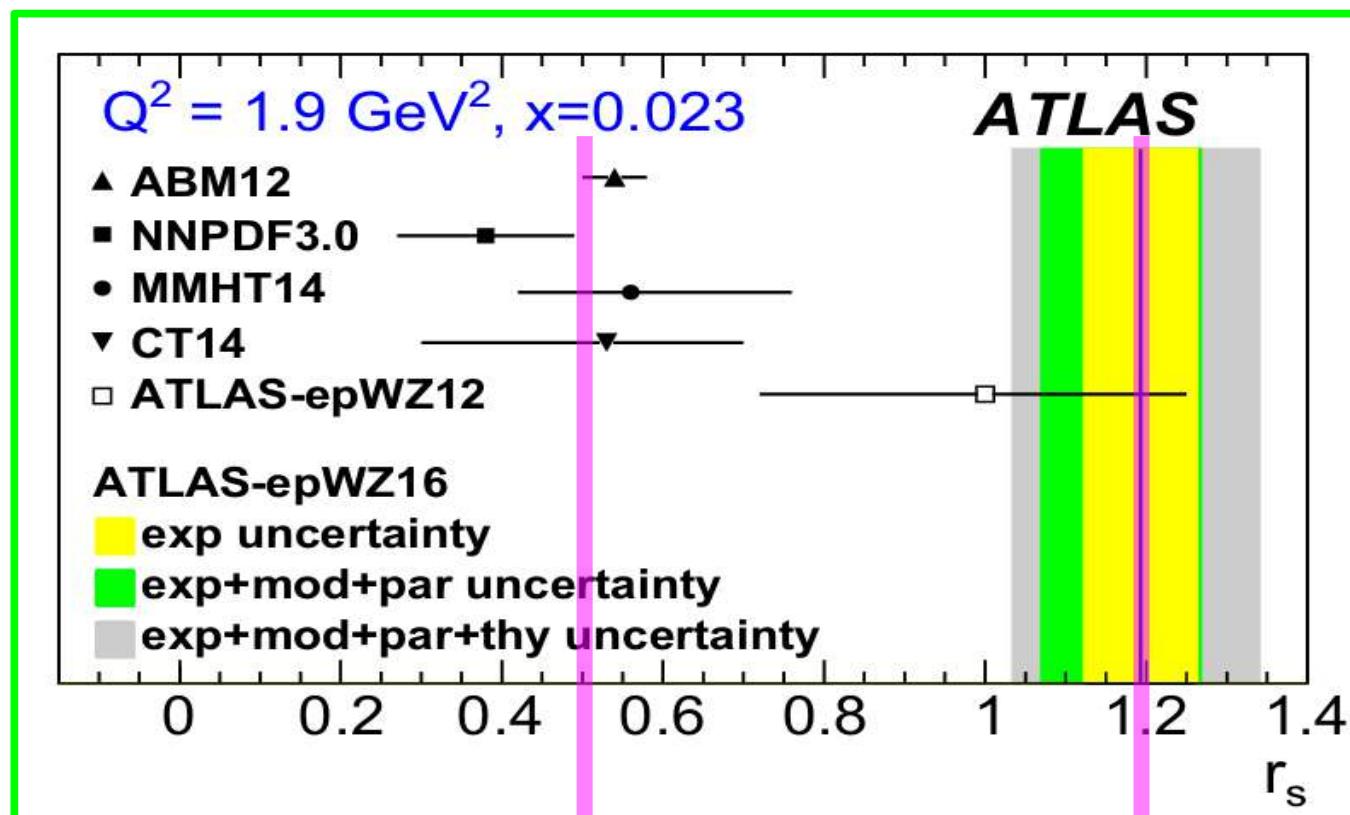
... there's another  
way to measure the  
strange quark

nCTEQ: Eur.Phys.J.C 80 (2020) 10, 968



**Surprise:**

We expected  $r_s = 1/2$   
LHC finds  $r_s > 1$



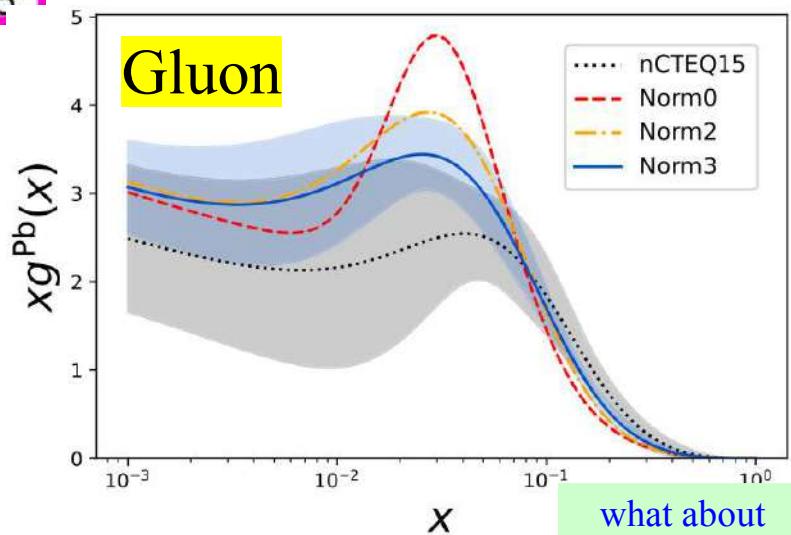
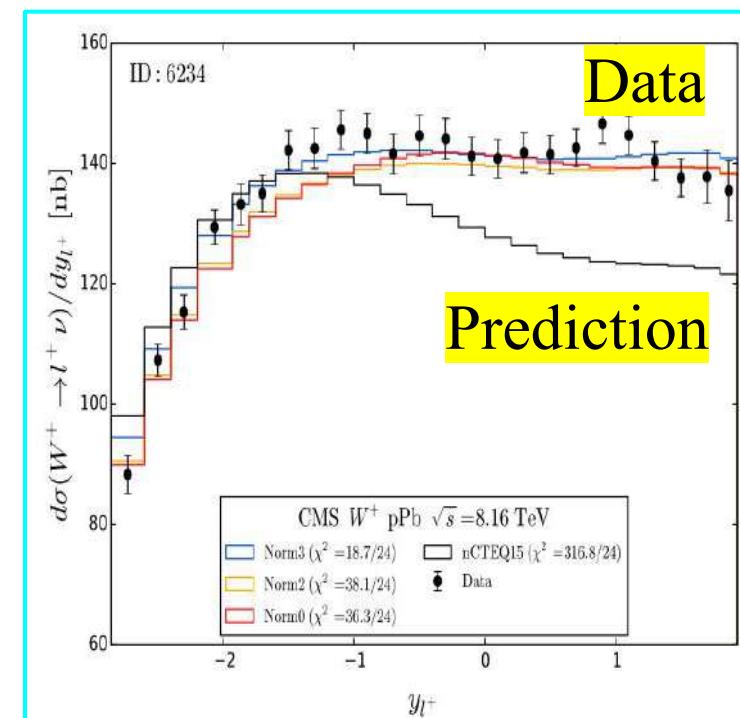
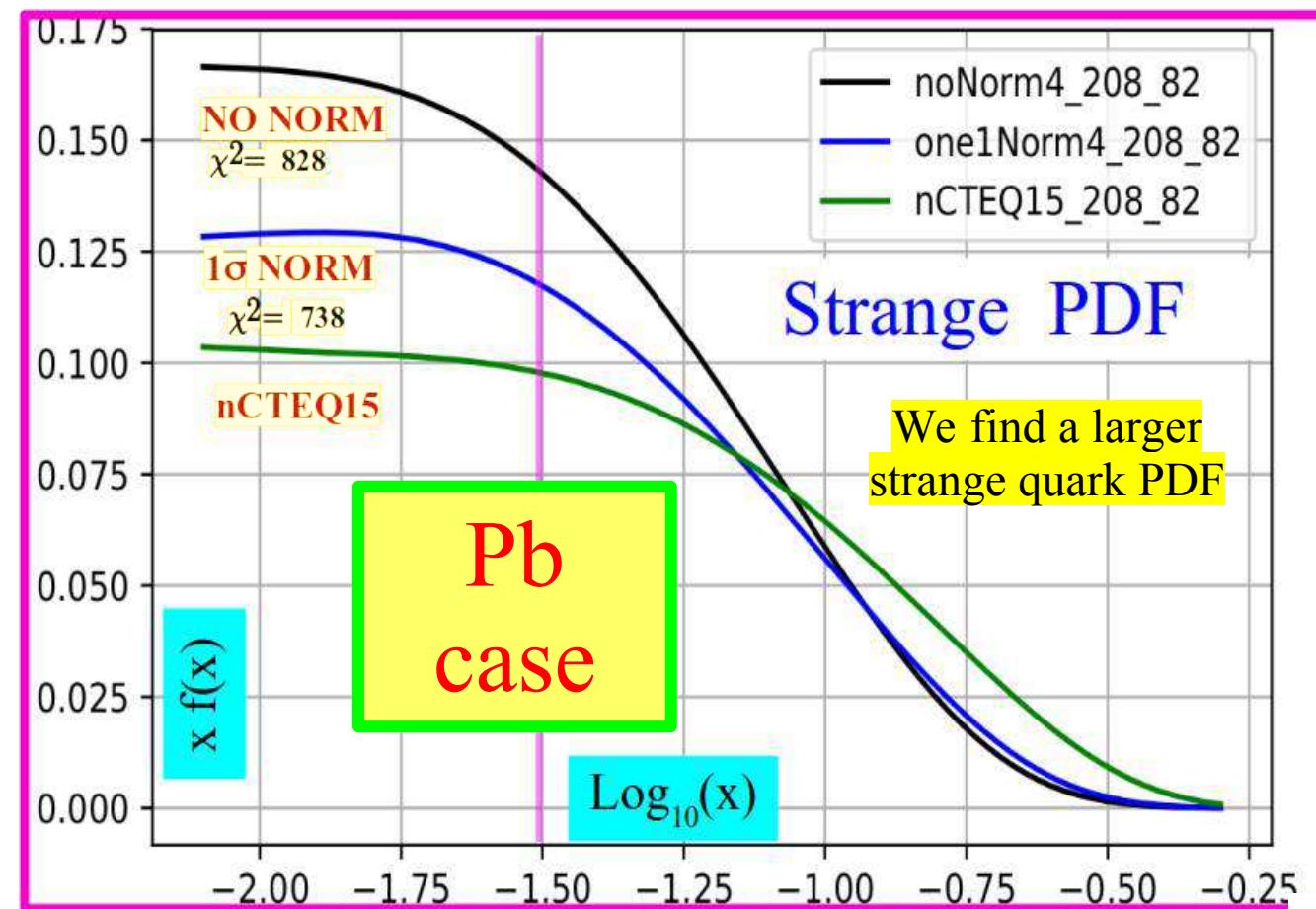
$$r_s \sim \bar{s}/\bar{d}$$

We expect:

At the LHC:

$$r_s = \frac{\bar{s} + s}{2\bar{d}}$$

Proton  
case

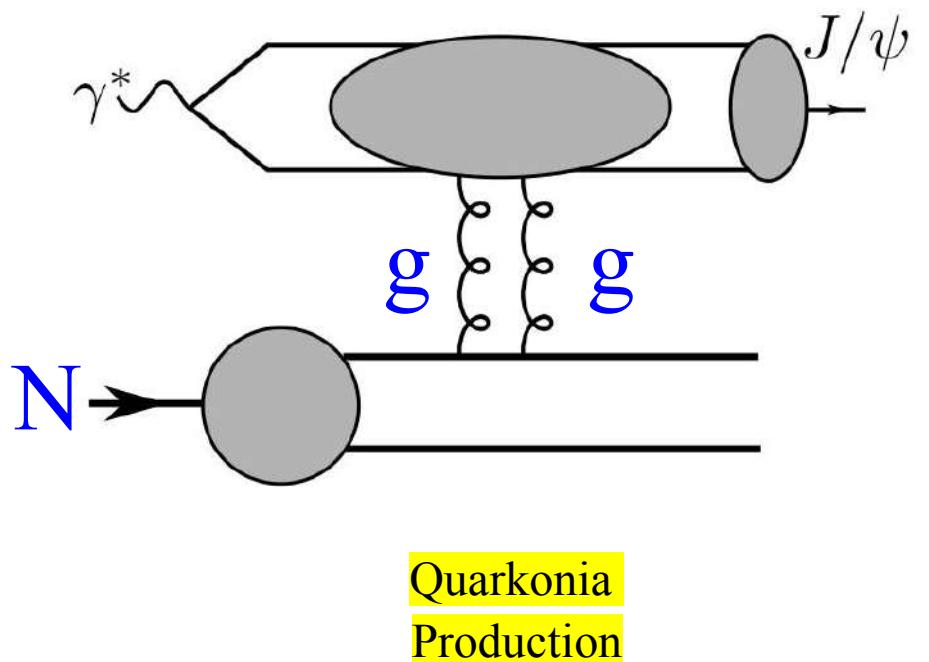
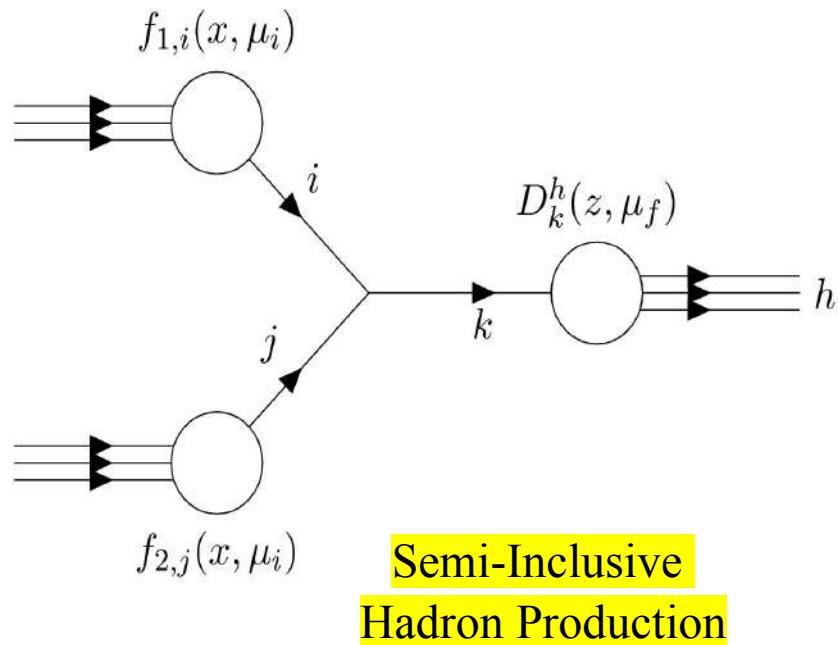


# Measuring the nuclear Gluon PDF

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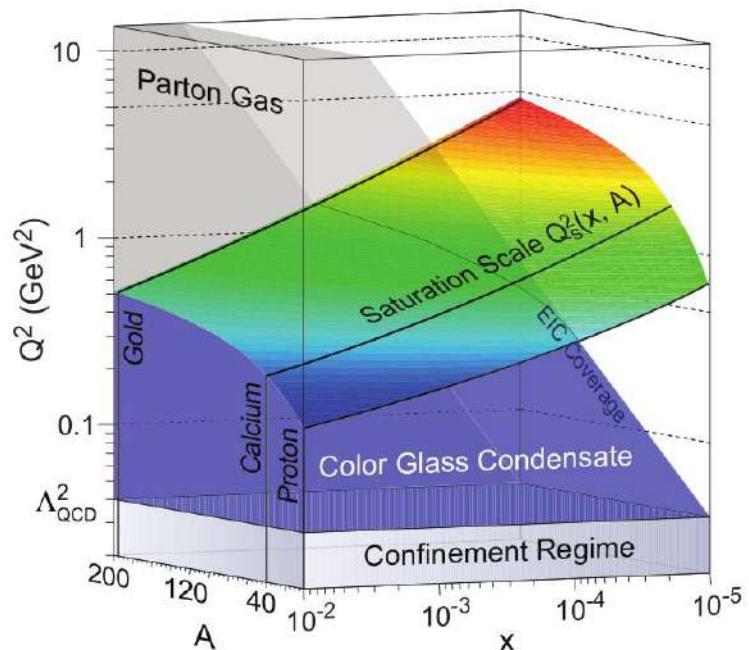
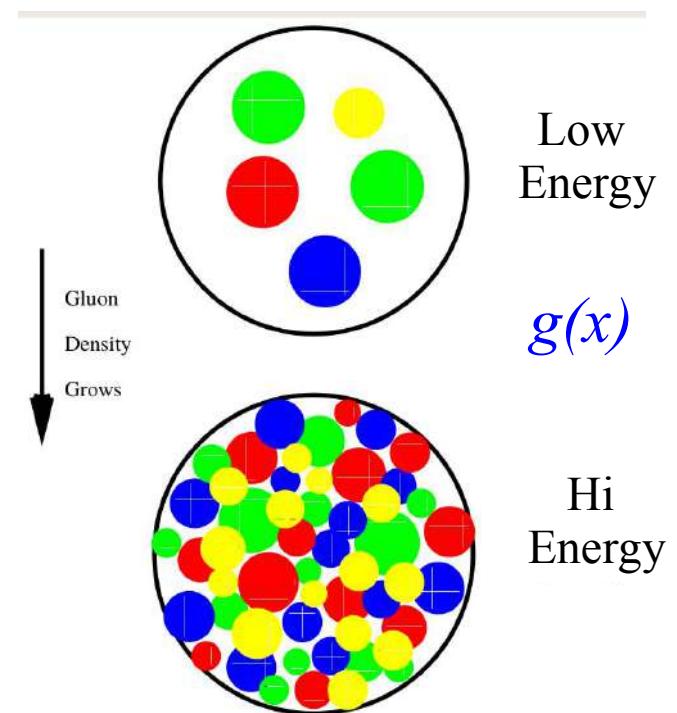
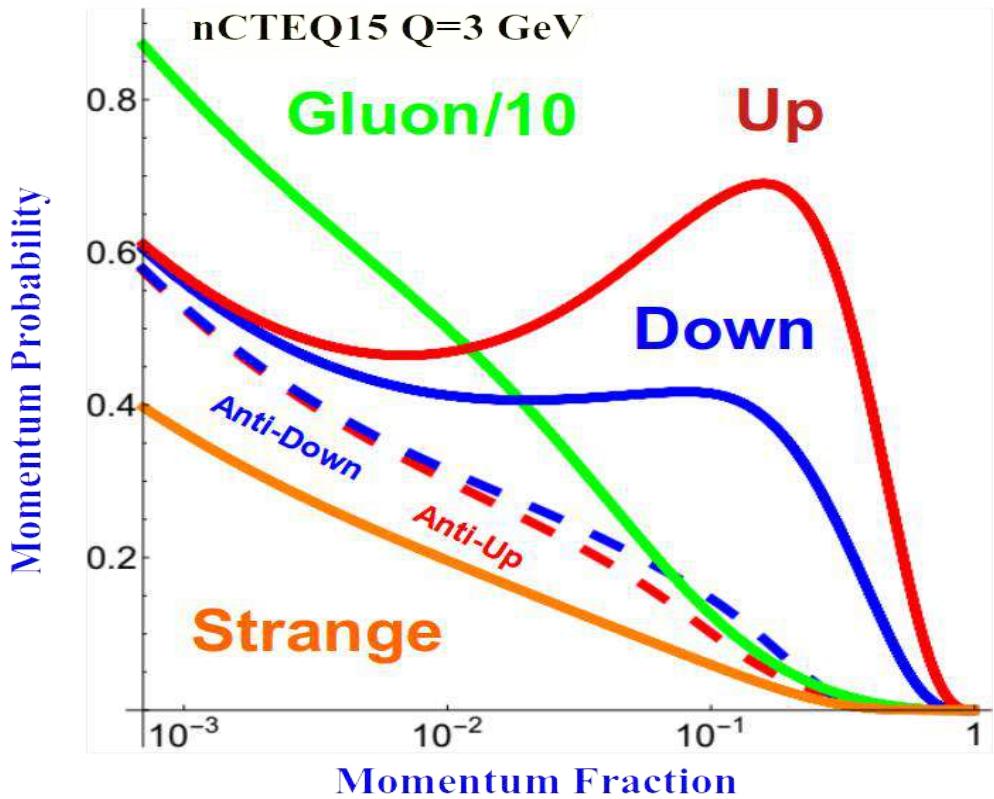
Parton Distribution Functions

Pit Duwentaster, Michael Klasen, ...



how can we determine  
the gluon

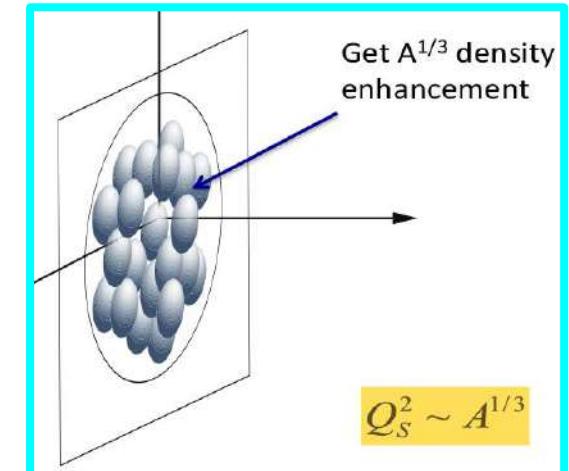
# Nuclear Medium Effects at small momentum fraction ( $x$ )



## Nuclear medium effects:

- Quark Gluon Plasma
- Color Glass Condensate
- Recombination
- Saturation
- Resummation
- ... *your theory here*

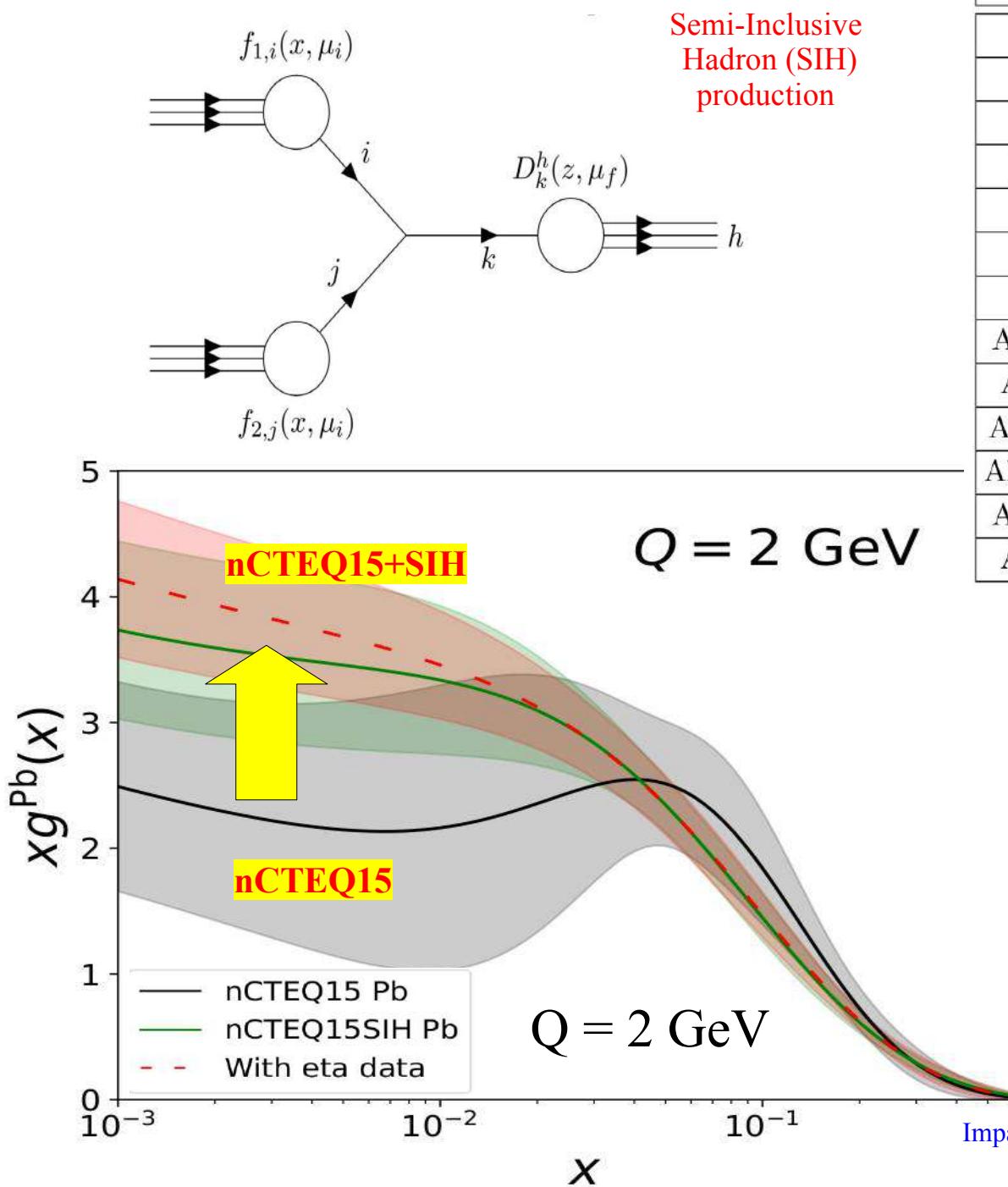
We gain a geometric factor of  $A^{1/3}$



# Precision Gluon can help study nuclear medium effects

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Pit Duwentaster, Michael Klasen, ...



Data set	$\sqrt{s_{NN}}$ [GeV]	Observ.	No. points
PHENIX $\pi^0$	200	$R_{dAu}$	21
PHENIX $\eta$	200	$R_{dAu}$	12
PHENIX $\pi^\pm$	200	$R_{dAu}$	20
PHENIX $K^\pm$	200	$R_{dAu}$	15
STAR $\pi^0$	200	$R_{dAu}$	13
STAR $\eta$	200	$R_{dAu}$	7
STAR $\pi^\pm$	200	$R_{dAu}$	23
ALICE 5 TeV $\pi^0$	5020	$R_{pPb}$	31
ALICE 5 TeV $\eta$	5020	$R_{pPb}$	16
ALICE 5 TeV $\pi^\pm$	5020	$R_{pPb}$	58
ALICE 5 TeV $K^\pm$	5020	$R_{pPb}$	58
ALICE 8 TeV $\pi^0$	8160	$R_{pPb}$	30
ALICE 8 TeV $\eta$	8160	$R_{pPb}$	14

Semi-Inclusive  
Hadron (SIH)  
production

*Determines gluon  
in small  $x$  region*

Impact of inclusive hadron production data on nuclear gluon PDFs  
nCTEQ: P. Duwentäster, et al., PRD104 (2021) 094005.

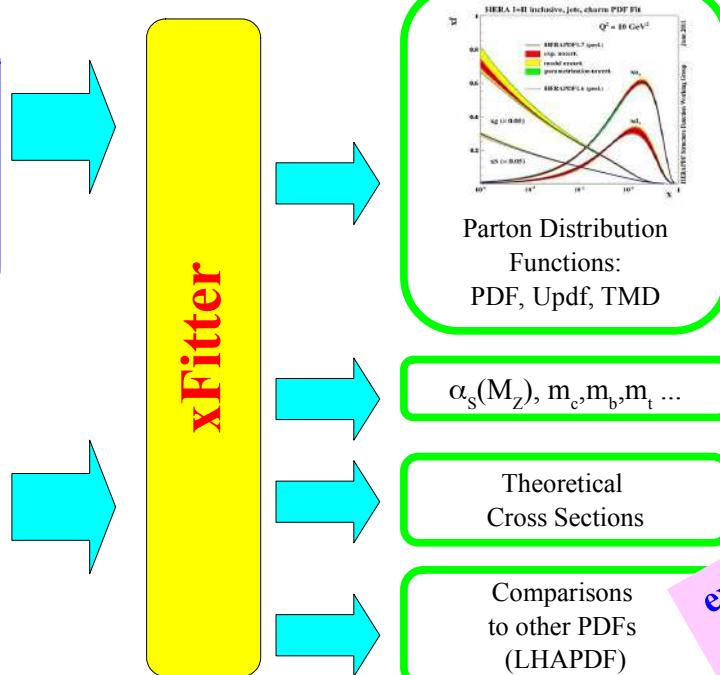
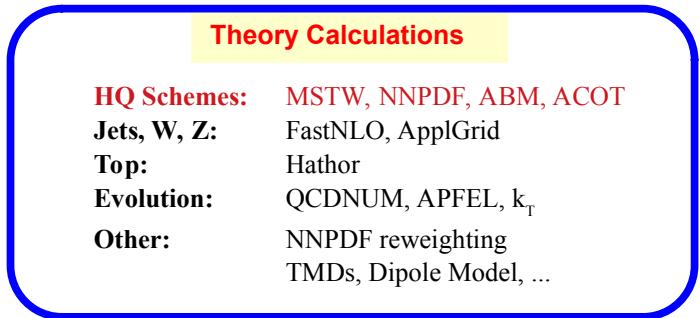
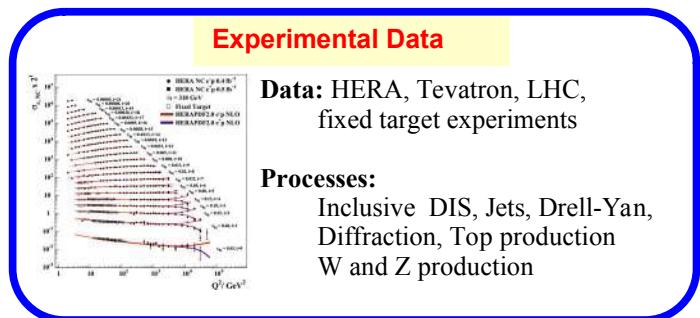


## Features & Recent Updates:

- Photon PDF & QED
- Pole & MS-bar masses
- Profiling and Re-Weighting
- Heavy Quark Variable Threshold
- Update  $\chi^2$  and correlations
- TMD PDFs (uPDFs)
- ... and many other

## Sample data files:

- LHC: ATLAS, CMS, LHCb
- Tevatron: CDF, D0
- HERA: H1, ZEUS, Combined
- Fixed Target: ...
- User Supplied: ...



extensions include  
nuclear PDFs



**xFitter 2.0.1**  
*Old Fashioned*

Date	Version
	2.0.1N Nuclear Daiquiri 02/2020



# nCTEQ: A Deeper Understanding of the strong nuclear force

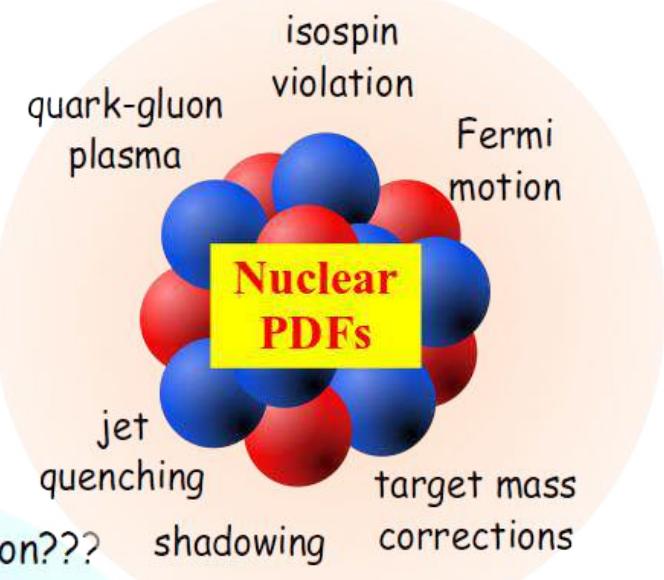
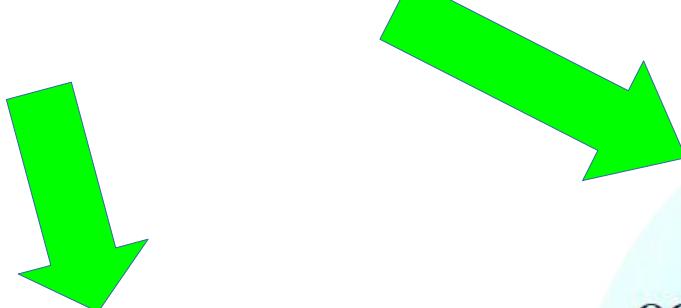
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Quantum ChromoDynamics

**QCD**  
Lagrangian



$$\mathcal{L}_{QCD} = \bar{\psi}_q (i\gamma_\mu D^\mu - m_q) \psi_q - \frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu}$$



DGLAP violation???

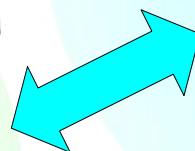
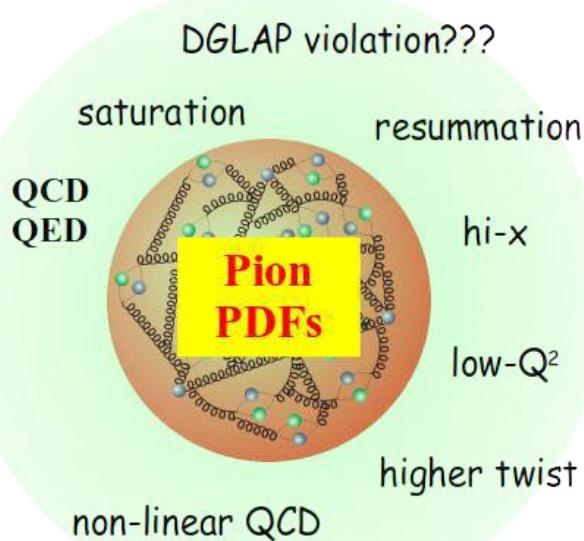
resummation

hi-x

saturation

QCD  
QED

**Proton  
PDFs**



non-linear QCD

low- $Q^2$

higher twist



**Conjecture:** A theory can't be fundamental unless it fits on a coffee mug.