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Scenarios

Matrix Theory Cosmology

Conclusions

Emergent Early Universe Cosmology

Robert Brandenberger
Physics Department, McGill University

PPC 2022, June 6 - 10, 2022

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Scenarios

Matrix Theory Cosmology

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- Inflationary Scenario is the current paradigm of early Universe cosmology.
- Inflation is usually analyzed using an effective field theory (EFT) framework.
- Fundamental conceptual problems for an EFT description of a rapidly expanding universe.
- Unitarity problem, inconsistency with the 2nd law of thermodynamics.
- We need to look beyond an EFT description of the early universe!
- Matrix Theory Cosmology: Emergent time, space and early universe from the BFSS matrix model.

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Outline

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Scenario

Matrix Theory Cosmology

- 1 Trans-Planckian Censorship
- 2 Scenarios for a Successful Early Universe Cosmology
- 3 Emergent Cosmology from Matrix Theory
- 4 Conclusions

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Trans-Planckian Problem

J. Martin and R.B., *Phys. Rev. D63, 123501 (2002)*

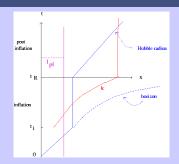
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- Success of inflation: At early times scales are inside the Hubble radius → causal generation mechanism is possible.
- **Problem:** If time period of inflation is more than $70H^{-1}$, then $\lambda_D(t) < I_{Dl}$ at the beginning of inflation.
- → breakdown of effective field theory; new physics
 MUST be taken into account when computing
 observables from inflation.

Trans-Planckian Censorship Conjecture (TCC)

A. Bedroya and C. Vafa., arXiv:1909.11063

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conclusions

No trans-Planckian modes exit the Hubble horizon.

$$ds^2 = dt^2 - a(t)^2 d\mathbf{x}^2$$

$$H(t) \equiv \frac{\dot{a}}{a}(t)$$

$$\frac{a(t_R)}{a(t_i)} I_{pl} \, < \, H(t_R)^{-1}$$

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Justification B.B. arXiv:1911.06056

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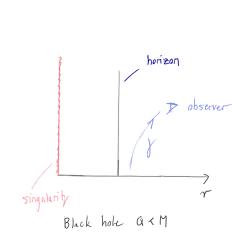
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Cosmology

Analogy with Penrose's Cosmic Censorship Hypothesis:



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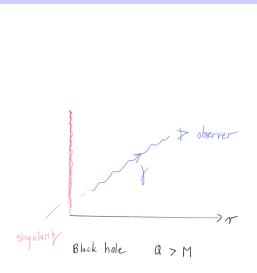
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Justification

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Matrix Theory Cosmology

- Effective field theory of General Relatiivty allows for solutions with timelike singularities: super-extremal black holes.
- Cauchy problem not well defined for observer external to black holes.
- Evolution non-unitary for external observer.
- Conjecture: ultraviolet physics → external observer shielded from the singularity and non-unitarity by horizon.

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Cosmological Version of the Censorship Conjecture

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Conclusion:

Translation

- Position space → momentum space.
- Singularity → trans-Planckian modes.
- Black Hole horizon → Hubble horizon.

Observer measuring super-Hubble horizon modes must be shielded from trans-Planckian modes.

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Why Hubble Horizon?

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Matrix Theory Cosmology

- Recall: Fluctuations only oscillate on sub-Hubble scales.
- Recall: Fluctuations freeze out, become squeezed states and classicalize on super-Hubble scales.
- Demand: classical region be insensitive to trans-Planckian region.
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- $m{\mathcal{H}}$ is the product Hilbert space of a harmonic oscillator Hilbert space for all **comoving** wave numbers k
- UV cutoff: time dependent k_{max} : $k_{max}(t)a(t)^{-1} = m_{pl}$
- Ontinuous mode creation → non-unitarity.
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Effective Field Theory (EFT) and the CC Problem

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Matrix Theory

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- EFT: expand **fields** in comoving Fourier space.
- Quantize each Fourier mode like a harmonic oscillator

 → ground state energy.
- Add up ground state energies → CC problem.
- The usual quantum view of the CC problem is an artefact of an EFT analysis!

Effective Field Theory (EFT) and the CC Problem

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Application of the Second Law of Thermodynamics

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- Consider entanglement entropy density $s_E(t)$ between sub- and super-Hubble modes.
- Consider an phase of inflationary expansion.
- $s_E(t)$ increases in time since the phase space of super-Hubble modes grows.
- **Demand**: $s_E(t)$ remain smaller than the post-inflationary thermal entropy.
- Duration of inflation is bounded from above, consistent with the TCC.

Application to EFT Description of Inflation

A. Bedroya, R.B., M. Loverde and C. Vafa., arXiv:1909.11106

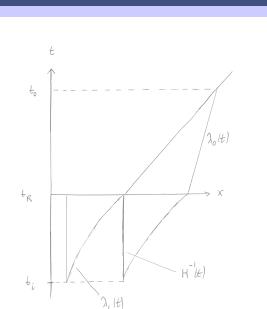
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Application to EFT Descriptions of Inflation

A. Bedroya, R.B., M. Loverde and C. Vafa., arXiv:1909.11106

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TCC implies:

$$\frac{a(t_R)}{a(t_*)}I_{pl} < H(t_R)^{-1}$$

Demanding that inflation yields a causal mechanism for generating CMB anisotropies implies:

$$H_0^{-1} \frac{a(t_0)}{a(t_R)} \frac{a(t_R)}{a(t_*)} < H^{-1}(t_*)$$

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Implications

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Conclusion

Upper bound on the energy scale of inflation:

$$V^{1/4} < 3 \times 10^9 \text{GeV}$$

 \rightarrow upper bound on the primordial tensor to scalar ratio r:

$$r < 10^{-30}$$

Note: Secondary tensors will be larger than the primary ones.

Implications for Dark Energy

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onclusions.

Dark Energy cannot be a bare cosmological constant.

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Angular Power Spectrum of CMB Anisotropies

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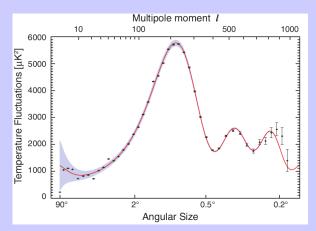
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Credit: NASA/WMAP Science Team

Early Work

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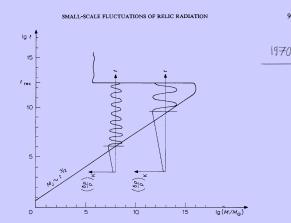


Fig. 1a. Diagram of gravitational instability in the 'big-bang' model. The region of instability is located to the right of the line $M_I(t)$; the region of stability to the left. The two additional lines of the graph demonstrate the temporal evolution of density perturbations of matter: growth until the moment when the considered mass is smaller than the Jeans mass and oscillations thereafter. It is apparent that at the moment of recombination perturbations corresponding to different masses correspond to different phases.

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Key Realization

R. Sunyaev and Y. Zel'dovich, Astrophys. and Space Science **7**, 3 (1970); P. Peebles and J. Yu, Ap. J. **162**, 815 (1970).

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Scenarios

Matrix Theory Cosmology

- Given a scale-invariant power spectrum of adiabatic fluctuations on "super-horizon" scales before t_{eq} , i.e. standing waves.
- ullet --- "correct" power spectrum of galaxies.
- → acoustic oscillations in CMB angular power spectrum.

Early Work

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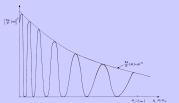


Fig. 1b. The dependence of the square of the amplitude of density perturbations of matter on scale. The fine line designates the usually assumed dependence $(\delta g(\phi)_F \sim M^{-\alpha}$. It is apparent that fluctuations of relic radiation should depend on scale in a similar manner.

Predictions from 1970

R. Sunyaev and Y. Zel'dovich, Astrophys. and Space Science **7**, 3 (1970); P. Peebles and J. Yu, Ap. J. **162**, 815 (1970).

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Criteria for a Successful Early Universe Scenario

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- Horizon >> Hubble radius in order for the scenario to solve the "horizon problem" of Standard Big Bang Cosmology.
- Scales of cosmological interest today originate inside the Hubble radius at early times in order for a causal generation mechanism of fluctuations to be possible.
- Mechanism for producing a scale-invariant spectrum of curvature fluctuations on super-Hubble scales.

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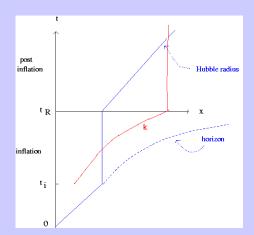
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Inflation as a Solution

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Bouncing Cosmology as a Solution

F. Finelli and R.B., *Phys. Rev.* D65, 103522 (2002), D. Wands, *Phys. Rev.* D60 (1999)

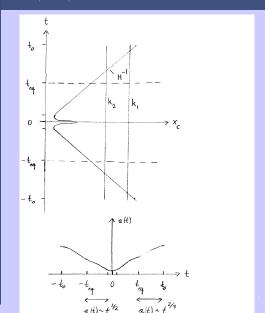


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Emergent Universe

R.B. and C. Vafa, *Nucl. Phys. B316:391 (1989)*

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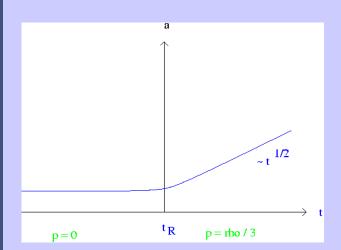
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Emergent Universe as a Solution

A. Nayeri, R.B. and C. Vafa, *Phys. Rev. Lett.* 97:021302 (2006)

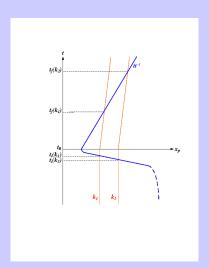
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Trans-Planckian Censorship and Cosmological Scenarios

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Matrix Theory Cosmology

- Bouncing cosmologies are consistent with the TCC provided that the energy scale at the bounce is lower than the Planck scale.
- Emergent cosmologies are consistent with the TCC provided that the energy scale of the emergence phase is lower than the Planck scale.
- Inflationary cosmologies are inconsistent with the TCC unless the energy scale of inflation is fine tuned.

All early universe scenarios require going beyond EFT.

Trans-Planckian Censorship and Cosmological Scenarios

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S. Brahma, R.B. and S. Laliberte, arXiv:2108.1152

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Scenario:

Matrix Theory Cosmology

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Starting point: BFSS matrix model at high temperatures.

- BFSS model is a quantum mechanical model of 10
 N × N Hermitean matrices.
- Note: no space!
- Note: no singularities!
- Note: BFSS matrix model is a proposed non-perturbative definition of M-theory: 10 dimensional superstring theory emerges in the $N \to \infty$ limit.

BFSS Model (bosonic sector)

T. Banks, W. Fischler, S. Shenker and L. Susskind, Phys. Rev. D **55**, 5112 (1997)

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conclusions

$$L \, = \, \frac{1}{2 g^2} \big[{\rm Tr} \big(\frac{1}{2} (D_t X_i)^2 - \frac{1}{4} [X_i, X_j]^2 \big) \big]$$

- X_i , i = 1, ...9 are $N \times N$ Hermitean matrices.
- D_t : gauge covariant derivative (contains a matrix A_0)

't Hooft limit: $N \to \infty$ with $\lambda \equiv g^2 N = g_s l_s^{-3} N$ fixed.

Thermal Initial State

N. Kawahara, J. Nishimura and S. Takeuchi, JHEP 12, 103 (2007)

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Matrix Theory Cosmology

- Consider a high temperature state.
- At high temperatures, the bosonic sector of the (Euclidean) BFSS model is well approximated by the bosonic sector of the (Euclidean) IKKT matrix model.
- Matsubara expansion:

$$X_i(t) = \sum_n X_i^n e^{2\pi i Tt}$$

$$A_i \equiv T^{-1/4} X_i^0$$

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IKKT Matrix Model

N. Ishibashi, H. Kawai, Y. Kitazawa and A. Tsuchiya, Nucl. Phys. B **498**, 467 (1997).

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Proposed as a non-perturbative definition of the IIB Superstring theory.

Action:

$$\mathcal{S}_{IKKT} \,=\, -rac{1}{g^2} \mathrm{Tr}ig(rac{1}{4}[A^a,A^b][A_a,A_b] + rac{i}{2}ar{\psi}_lpha(\mathcal{C}\Gamma^a)_{lphaeta}[A_a,\psi_eta]ig)\,,$$

Partition function:

$$Z = \int dAd\psi e^{iS}$$

Y. Ito, J. Nishimura and A. Tsuchiya, arXiv:1506.04795

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Matrix Theory Cosmology

Conclusions

- Eigenvalues of A_0 become emergent time.
- Work in the basis in which A_0 is diagonal.
- Numerical studies: $\frac{1}{N}\langle {\rm Tr} A_0^2 \rangle \sim \kappa N$

$$ullet$$
 o $t_{max} \sim \sqrt{N}$

$$\bullet \to \Delta t \sim \frac{1}{\sqrt{N}}$$

ullet \rightarrow infinite continuous time.

Y. Ito, J. Nishimura and A. Tsuchiya, arXiv:1506.04795

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→ infinite continuous time.

Y. Ito, J. Nishimura and A. Tsuchiya, arXiv:1506.04795

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Scenarios

Matrix Theory Cosmology

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- Eigenvalues of A_0 become emergent time, continuous in $N \to \infty$ limit.
- Work in the basis in which A_0 is diagonal: A_i matrices elements decay when going away from the diagonal.
- $\sum_{i}\langle |A_{i}|_{ab}^{2}\rangle$ decays when $|a-b|>n_{c}$
- $\sum_{i} \langle |A_i|_{ab}^2 \rangle \sim \text{constant when } |a-b| < n_c$
- $n_c \sim \sqrt{N}$

S. Kim, J. Nishimura and A. Tsuchiya, arXiv:1108.1540

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- Eigenvalues of A_0 become emergent time, continuous in $N \to \infty$ limit.
- Work in the basis in which A_0 is diagonal: A_i matrices elements decay when going away from the diagonal.
- Pick $n \times n$ blocks $\tilde{A}_i(t)$ about the diagonal $(n < n_c)$

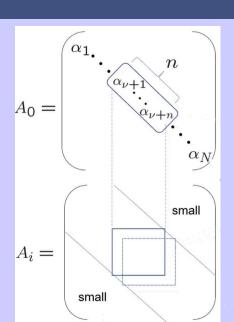
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J. Nishimura, PoS CORFU 2019, 178 (2020) [arXiv:2006.00768 [hep-lat]].

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- Work in the basis in which A_0 is diagonal.
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- Extent of space in direction i

$$x_i(t)^2 \equiv \left\langle \frac{1}{n} \text{Tr}(\bar{A}_i)(t))^2 \right\rangle$$

In a thermal state there is spontaneous symmetry breaking: SO(9) → SO(6) × SO(3): three dimensions of space become larger, the others are confined.
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S. Brahma, R.B. and S. Laliberte, in preparation

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Scenario:

Matrix Theory Cosmology

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- Eigenvalues of A_0 become emergent time, continuous in $N \to \infty$ limit.
- Work in the basis in which A_0 is diagonal: pick n (comoving spatial coordinate) and consider the block matrix $\tilde{A}_i(t)$.
- Physical distance between n = 0 and n (emergent space):

$$I_{phys,i}^2(n) \equiv \left\langle \text{Tr}(\bar{A}_i)(t))^2 \right\rangle$$

- $I_{phys,i}(n) \sim n$ (for $n < n_c$)
- Emergent infinite and continuous space in $N \to \infty$ limit.
- Emergent metric (S. Brahma, R.B. and S. Laliberte, in preparation).

$$g_{ii}(n)^{1/2} = \frac{d}{dn}I_{phys,i}(n)$$

S. Brahma, R.B. and S. Laliberte, in preparation

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Scenario

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Canaluciana

Emergent metric:

$$g_{ii}(n)^{1/2} = \frac{d}{dn} I_{phys,i}(n)$$

Result:

$$g_{ii}(n,t) = \mathcal{A}(t)\delta_{ii}$$
 $i = 1,2,3$

SO(3) symmetry -

$$g_{ii}(n,t) = \mathcal{A}(t)\delta_{ii}$$
 $i = 1, 2, 3$

→ spatially flat

Note: Local Lorentz invariance emerges in $N \to \infty$ limit.

S. Brahma, R.B. and S. Laliberte, in preparation

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Late Time Dynamics

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Scenario

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onclusions:

$$\mathcal{A}(t) \sim t^{1/2}$$

Note: no sign of a cosmological constant.

S. Brahma, R.B. and S. Laliberte, arXiv:2108.1152

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Scenario

Matrix Theory Cosmology

- We assume that the spontaneous symmetry breaking observed in the IKKT model also holds in the BFSS model.
- Method: generalize the Gaussian approximation method used to demonstrate the existence of the phase transition in the IKKT model to the BFSS theory (S. Brahma et al, in preparation).
- Thermal correlation functions in the three large spatial dimensions calculated in the high temperature state of the BFSS model (following the formalism developed in String Gas Cosmology).
- curvature fluctuations and gravitational waves.

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Matrix Theory Cosmology: Thermal Fluctuations

S. Brahma, R.B. and S. Laliberte, arXiv:2108.1152

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Scenarios

Matrix Theory Cosmology

Conclusions

Method:

- Consider BFSS finite temperature partition function
- Take partial derivatives with respect to T and R_i
- Obtain energy density and pressure fluctuations.

S. Brahma, R.B. and S. Laliberte, arXiv:2108.1152

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Matrix Theory Cosmology

Conclusions

Thermal fluctuations in the emergent phase \rightarrow

- Scale-invariant spectrum of curvature fluctuations
- With a Poisson contribution for UV scales.
- Scale-invariant spectrum of gravitational waves.

→ BFSS matrix model yields emergent infinite space, emergent infinite time, emergent spatially flat metric and an emergent early universe phase with thermal fluctuations leading to scale-invariant curvature fluctuations and gravitational waves.

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Open Problems

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Scenario

Matrix Theory Cosmology

- Understand phase transition to the expanding phase of Big Bang Cosmology.
- Spectral indices?
- What about Dark Energy?

Plan

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Scenario

Matrix Theory Cosmology

- 1 Trans-Planckian Censorship
- 2 Scenarios for a Successful Early Universe Cosmology
- 3 Emergent Cosmology from Matrix Theory
- 4 Conclusions

Conclusions

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Scenarios

Matrix Theory Cosmology

- Inflation is not the only scenario of early universe cosmology consistent with current data.
- In light of the TCC and other conceptual problems effective field theory models of inflation are not viable.
- In light of the TCC and other conceptual problems Dark Energy cannot be a cosmological constant.
- We need to go beyond point particle EFT in order to describe the very early universe.

Conclusions

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Matrix Theory
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Conclusions

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Cosmology

- BFSS matrix model is a proposal for a non-perturbative definition of superstring theory. Consider a high temperature state of the BFSS model.
- → emergent time, space and metric. Emergent space is spatially flat and infinite.
- Thermal fluctuations of the BFSS model → scale-invariant spectra of cosmological perturbations and gravitational waves.
- Transition from an emergent phase to the radiation phase of expansion. No cosmological constant.