Applied Landau damping



Dr. Xavier Buffat

Beams Department – Accelerator and Beam Physics Collective Effects and Impedances

CERN, Switzerland, Geneva

CERN Accelerator School – 15th November 2022



Copyright statement and speaker's release for video publishing

The author consents to the photographic, audio and video recording of this lecture at the CERN Accelerator School. The term "lecture" includes any material incorporated therein including but not limited to text, images and references.

The author hereby grants CERN a royalty-free license to use his image and name as well as the recordings mentioned above, in order to post them on the CAS website.

The material is used for the sole purpose of illustration for teaching or scientific research. The author hereby confirms that to his best knowledge the content of the lecture does not infringe the copyright, intellectual property or privacy rights of any third party. The author has cited and credited any third-party contribution in accordance with applicable professional standards and legislation in matters of attribution.



Recap

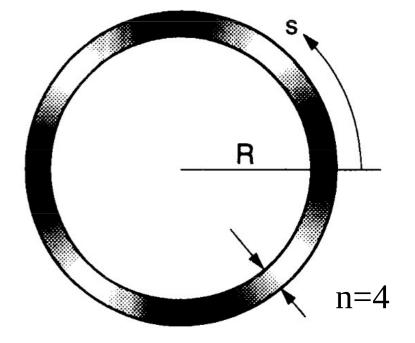
- Landau damping stems from the interaction of single particles with waves
 - A necessary condition for Landau damping is the a comparable velocity / frequency of the wave and the particles motion
- While collective forces such as wake fields or electron clouds tend to generate unstable modes of oscillation, Landau damping stabilises them without emittance growth
 - An external perturbation may also decay through a similar phenomenon, we rather talk about decoherence or filamentation. This mechanism leads to emittance growth
- Landau damping originates in the spread of oscillation frequencies of the particles in the beam
 - It is a linear mechanism, as in plasmas. However in accelerators the frequency spread often originates from non-linear forces

Content

- Part I (concept)
 - Wave particle interaction
 - Van Kampen approach
 - Stability diagram and beam transfer function
- Part II (applications)
 - Longitudinal and transverse Landau damping in unbunched and bunched beams
 - Non-linear collective forces
 - Advanced Landau damping techniques

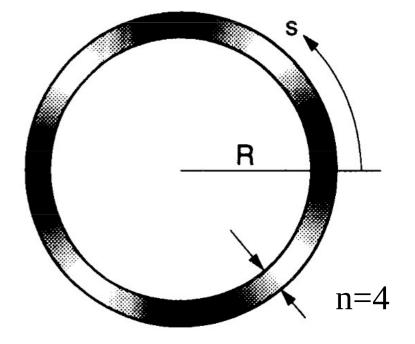
[Chao]

• In unbunched beam, density modulations may self-enhances under the influence an impedance (e.g. Negative mass instability)

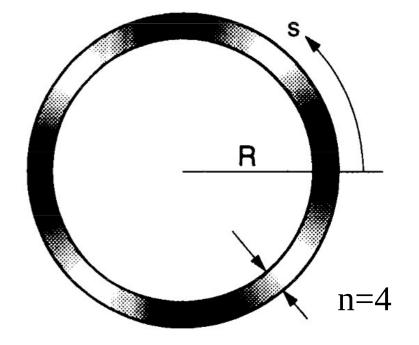




- In unbunched beam, density modulations may self-enhances under the influence an impedance (e.g. Negative mass instability)
- Landau damping of such instabilities originiates in the spread in revolution frequencies for particles with different momentum
 - The dispersion relation takes a special form:

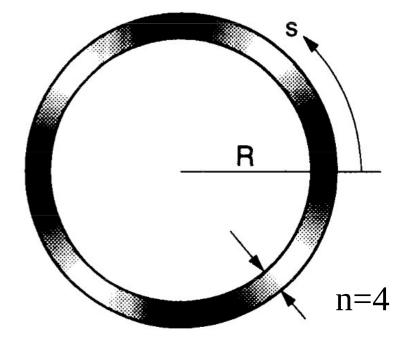


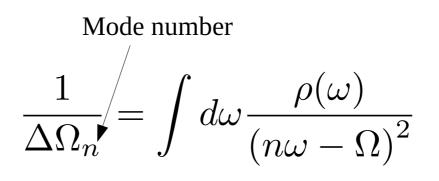
- In unbunched beam, density modulations may self-enhances under the influence an impedance (e.g. Negative mass instability)
- Landau damping of such instabilities originiates in the spread in revolution frequencies for particles with different momentum
 - The dispersion relation takes a **special form**:



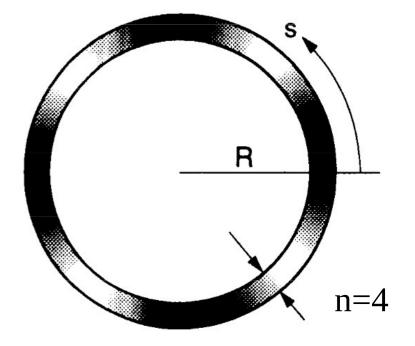
$$\frac{1}{\Delta\Omega_n} = \int d\omega \frac{\rho(\omega)}{\left(n\omega - \Omega\right)^2}$$

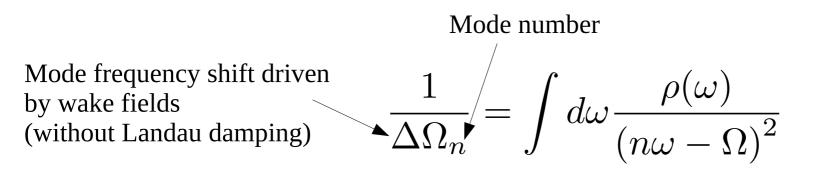
- In unbunched beam, density modulations may self-enhances under the influence an impedance (e.g. Negative mass instability)
- Landau damping of such instabilities originiates in the spread in revolution frequencies for particles with different momentum
 - The dispersion relation takes a **special form**:



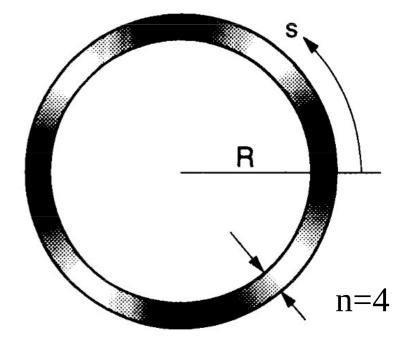


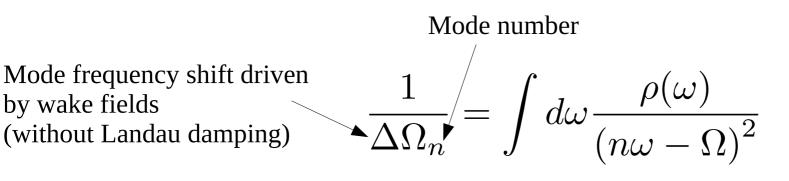
- In unbunched beam, density modulations may self-enhances under the influence an impedance (e.g. Negative mass instability)
- Landau damping of such instabilities originiates in the spread in revolution frequencies for particles with different momentum
 - The dispersion relation takes a special form:





- In unbunched beam, density modulations may self-enhances under the influence an impedance (e.g. Negative mass instability)
- Landau damping of such instabilities originiates in the spread in revolution frequencies for particles with different momentum
 - The dispersion relation takes a special form:

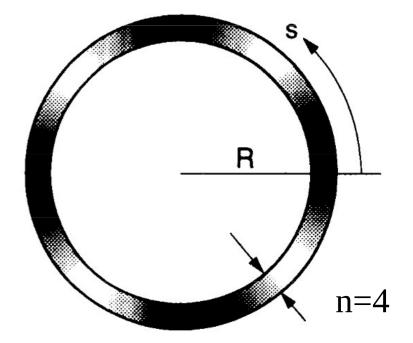


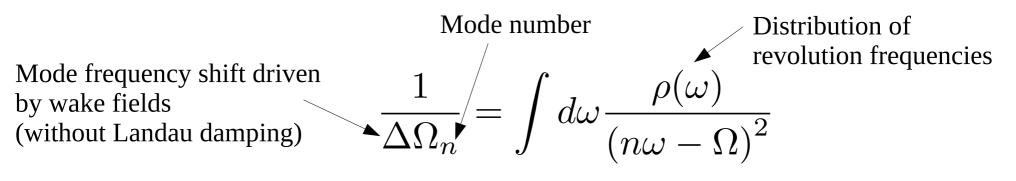


e.g. from perturbation theory:

$$\Delta\Omega_n = i \frac{2\pi N r_0 n\eta}{\gamma T_0^3} Z^{\parallel}(n\omega_0)$$

- In unbunched beam, density modulations may self-enhances under the influence an impedance (e.g. Negative mass instability)
- Landau damping of such instabilities originiates in the spread in revolution frequencies for particles with different momentum
 - The dispersion relation takes a special form:

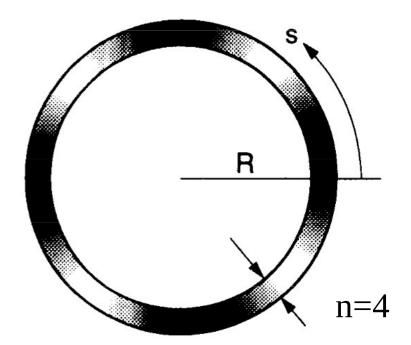


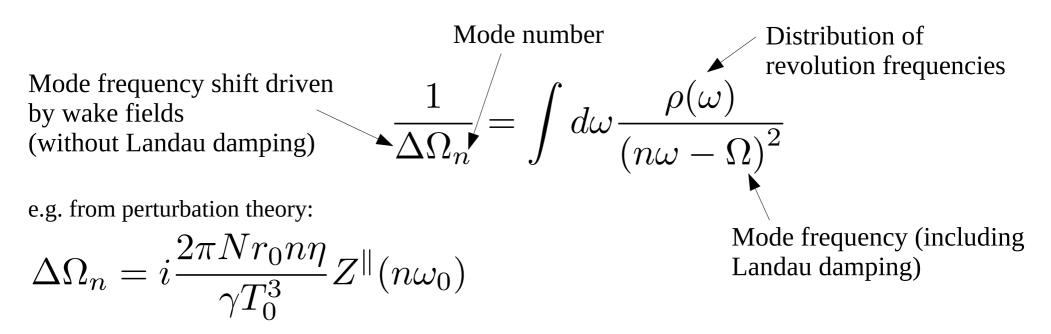


e.g. from perturbation theory:

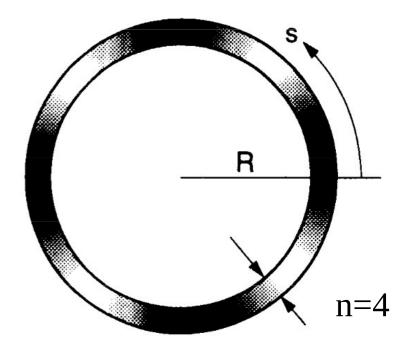
$$\Delta \Omega_n = i \frac{2\pi N r_0 n\eta}{\gamma T_0^3} Z^{\parallel}(n\omega_0)$$

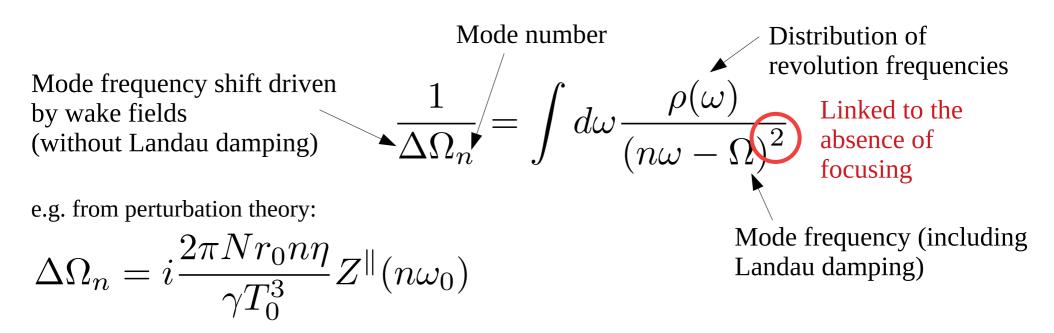
- In unbunched beam, density modulations may self-enhances under the influence an impedance (e.g. Negative mass instability)
- Landau damping of such instabilities originiates in the spread in revolution frequencies for particles with different momentum
 - The dispersion relation takes a special form:

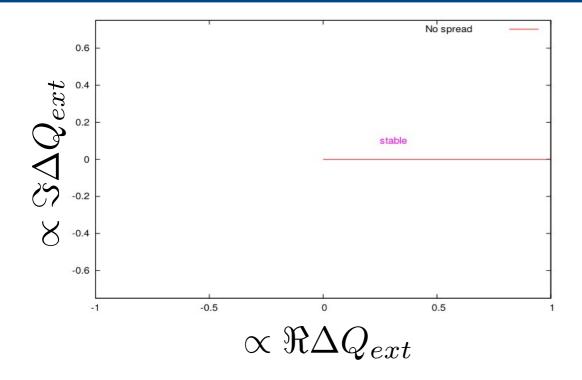




- In unbunched beam, density modulations may self-enhances under the influence an impedance (e.g. Negative mass instability)
- Landau damping of such instabilities originiates in the spread in revolution frequencies for particles with different momentum
 - The dispersion relation takes a special form:

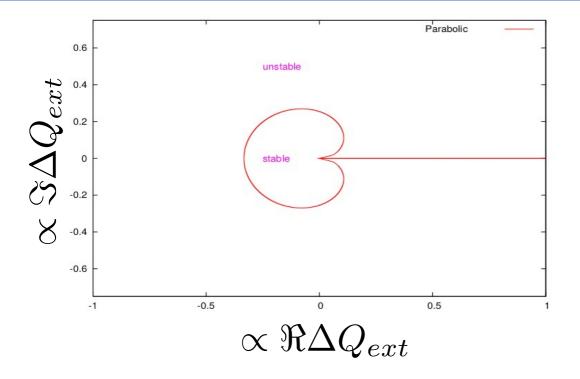






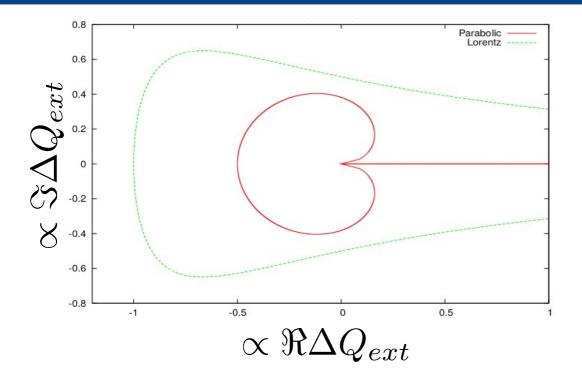
• The beam is always unstable without energy spread

[Chao,



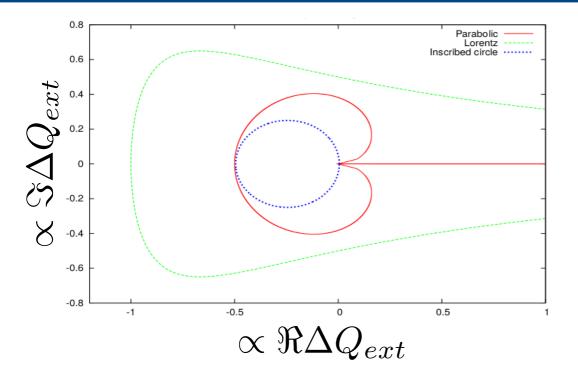
• The beam is always unstable without energy spread

[Chao,



- The beam is always unstable without energy spread
- The stability diagram is strongly impacted by the assumed frequency distribution

[Chao,

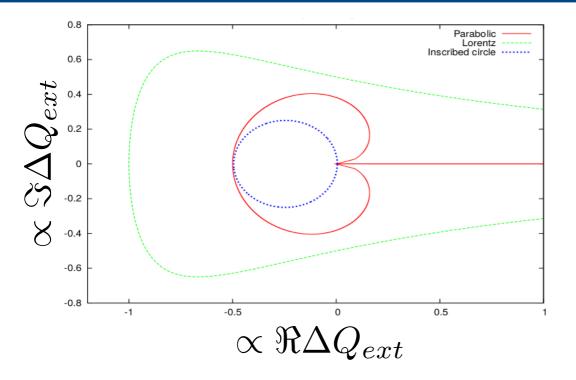


- The beam is always unstable without energy spread
- The stability diagram is strongly impacted by the assumed frequency distribution

• Usually the frequency distribution is poorly known, Keil-Schnell derived a conservative criterion based on the inscribed circle:

$$|\Delta\Omega_n| \lessapprox \frac{1}{4} n^2 \Delta\omega^2$$

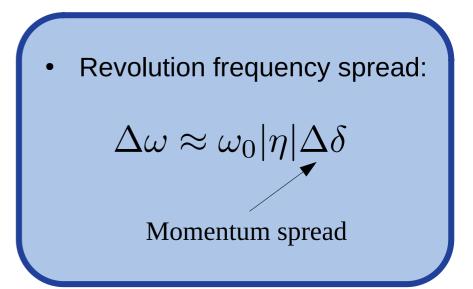
[Chao,



- The beam is always unstable without energy spread
- The stability diagram is strongly impacted by the assumed frequency distribution

 Usually the frequency distribution is poorly known, Keil-Schnell derived a conservative criterion based on the inscribed circle:

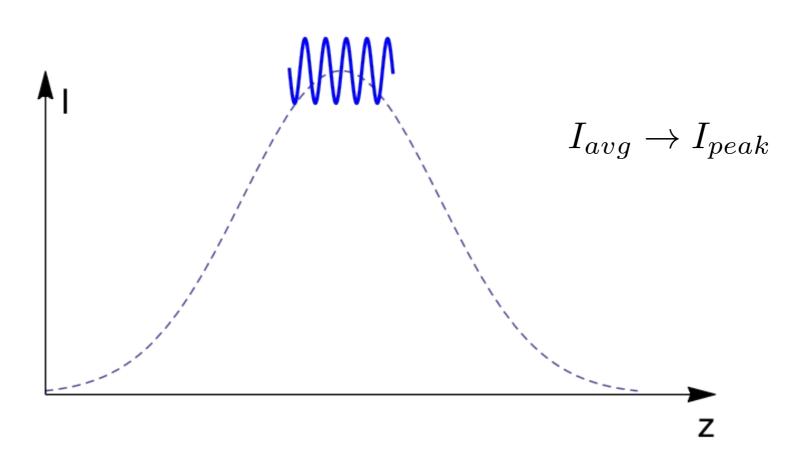
$$|\Delta\Omega_n| \lessapprox \frac{1}{4} n^2 \Delta\omega^2$$



[Chao,

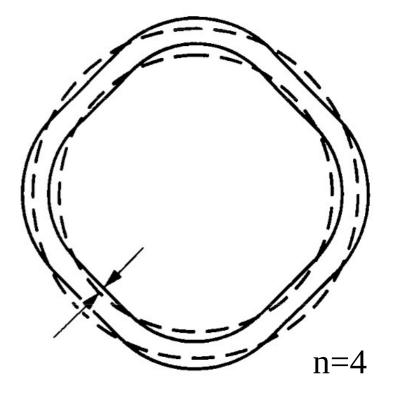
Microwave instability in bunched beams

- The KS criterion also provides a good indication of the requirement to stabilise the **microwave instability** in bunched beams
 - \rightarrow Keil-Schnell-Boussard criterion



[Micro]

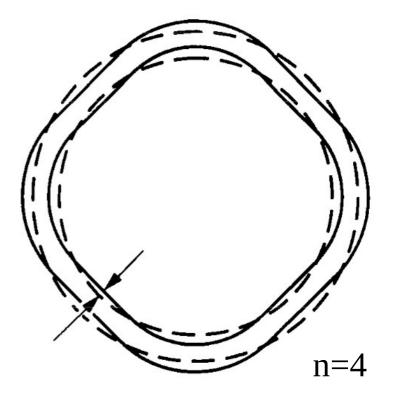
• Transverse oscillations of unbunched beams can also be driven unstable by the interaction with an impedance





- Transverse oscillations of unbunched beams can also be driven unstable by the interaction with an impedance
- The dispersion integral takes the form:

$$\frac{-1}{\Delta\Omega_n} = \int d\omega \frac{\rho(\omega)}{\omega - n\omega_0 - \Omega}$$

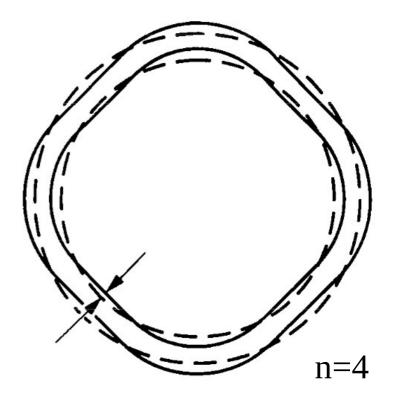


- Transverse oscillations of unbunched beams can also be driven unstable by the interaction with an impedance
- The dispersion integral takes the form:

$$\frac{-1}{\Delta\Omega_n} = \int d\omega \frac{\rho(\omega)}{\omega - n\omega_0 - \Omega}$$

Transverse frequency shift caused by the impedance, e.g. from perturbation theory:

$$\Delta\Omega_n = -i\frac{Nr_0c^2\eta}{2\gamma\omega_\beta T_0}Z^{\perp}(n\omega_0 + \omega_\beta)$$

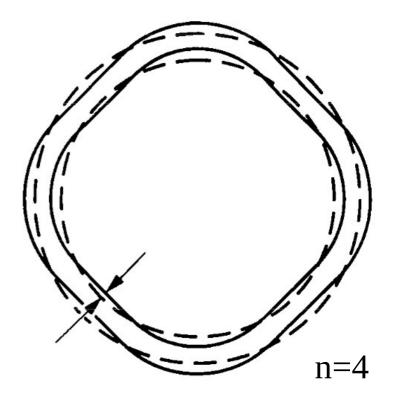


- Transverse oscillations of unbunched beams can also be driven unstable by the interaction with an impedance
- The dispersion integral takes the form:

Transverse frequency spread
$$\frac{-1}{\Delta\Omega_n} = \int d\omega \frac{\rho(\omega)}{\omega - n\omega_0 - \Omega}$$

Transverse frequency shift caused by the impedance, e.g. from perturbation theory:

$$\Delta\Omega_n = -i\frac{Nr_0c^2\eta}{2\gamma\omega_\beta T_0}Z^{\perp}(n\omega_0 + \omega_\beta)$$

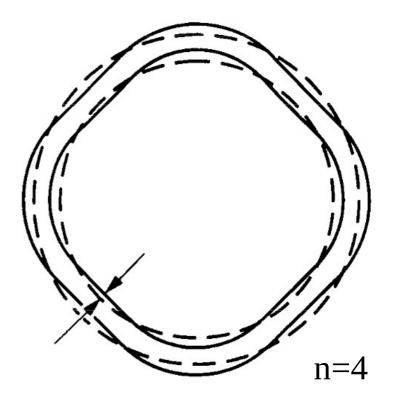


- Transverse oscillations of unbunched beams can also be driven unstable by the interaction with an impedance
- The dispersion integral takes the form:

Transverse frequency spread $\frac{-1}{\Delta\Omega_n} = \int d\omega \frac{\rho(\omega)}{\omega - n\omega_0 - \Omega}$

Transverse frequency shift caused by the impedance, e.g. from perturbation theory:

$$\Delta\Omega_n = -i\frac{Nr_0c^2\eta}{2\gamma\omega_\beta T_0}Z^{\perp}(n\omega_0 + \omega_\beta)$$



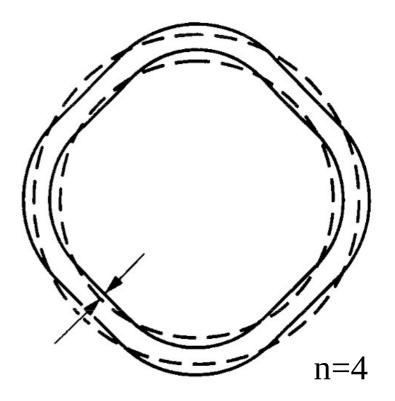
- Transverse oscillations of unbunched beams can also be driven unstable by the interaction with an impedance
- The dispersion integral takes the form:

Transverse frequency spread $\frac{-1}{\Delta\Omega_n} = \int d\omega \frac{\rho(\omega)}{\omega - n\omega_0 - \Omega}$

Transverse frequency shift caused by the impedance, e.g. from perturbation theory:

$$\Delta\Omega_n = -i\frac{Nr_0c^2\eta}{2\gamma\omega_\beta T_0}Z^{\perp}(n\omega_0 + \omega_\beta)$$

• Simplified criterion: $|\Delta\Omega_n| \lessapprox \Delta\omega$



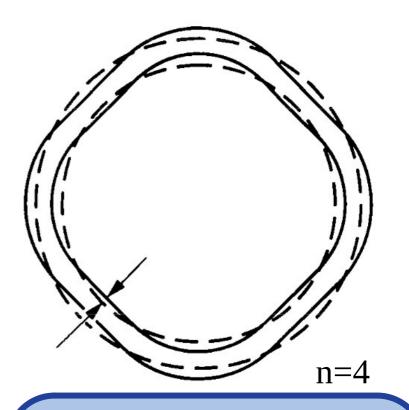
- Transverse oscillations of unbunched beams can also be driven unstable by the interaction with an impedance
- The dispersion integral takes the form:

Transverse frequency spread $\frac{-1}{\Delta\Omega_n} = \int d\omega \frac{\rho(\omega)}{\omega - n\omega_0 - \Omega}$

Transverse frequency shift caused by the impedance, e.g. from perturbation theory:

$$\Delta\Omega_n = -i\frac{Nr_0c^2\eta}{2\gamma\omega_\beta T_0}Z^{\perp}(n\omega_0 + \omega_\beta)$$

• Simplified criterion: $|\Delta\Omega_n| \lessapprox \Delta \omega$



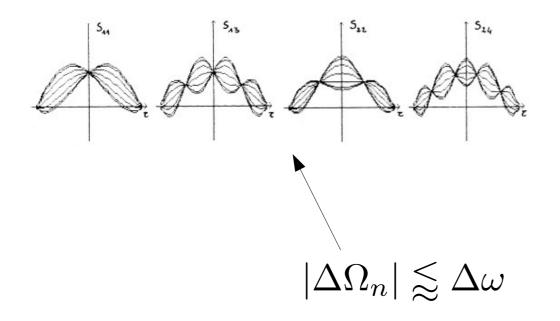
- Sources of transverse frequency spread:
 - Revolution frequency
 - Chromaticity (Q')

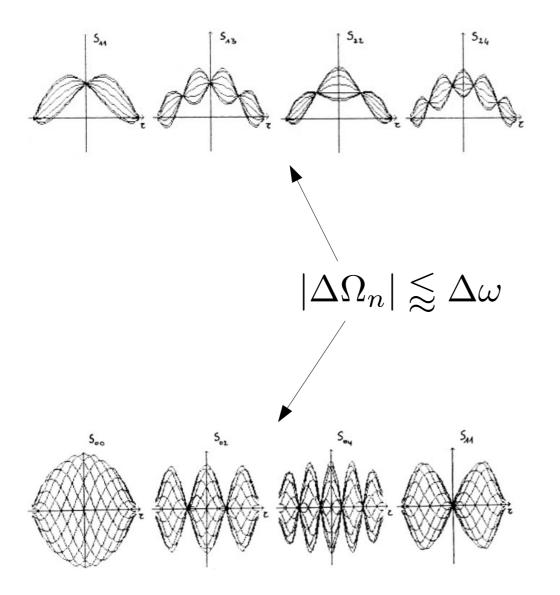
$$\Delta \omega = \omega_0 |Q' - n\eta| \Delta \delta$$

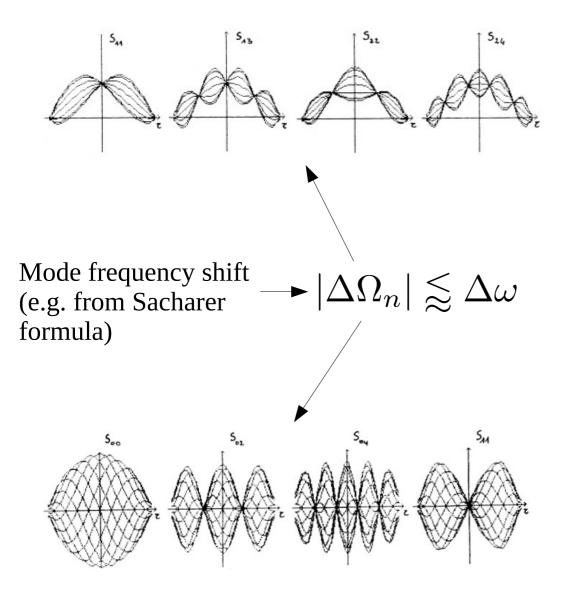
15.11.2022

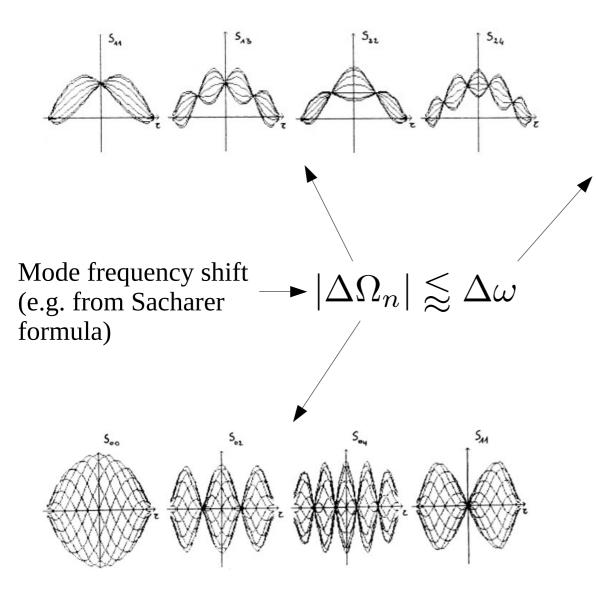
 $|\Delta\Omega_n| \lessapprox \Delta\omega$



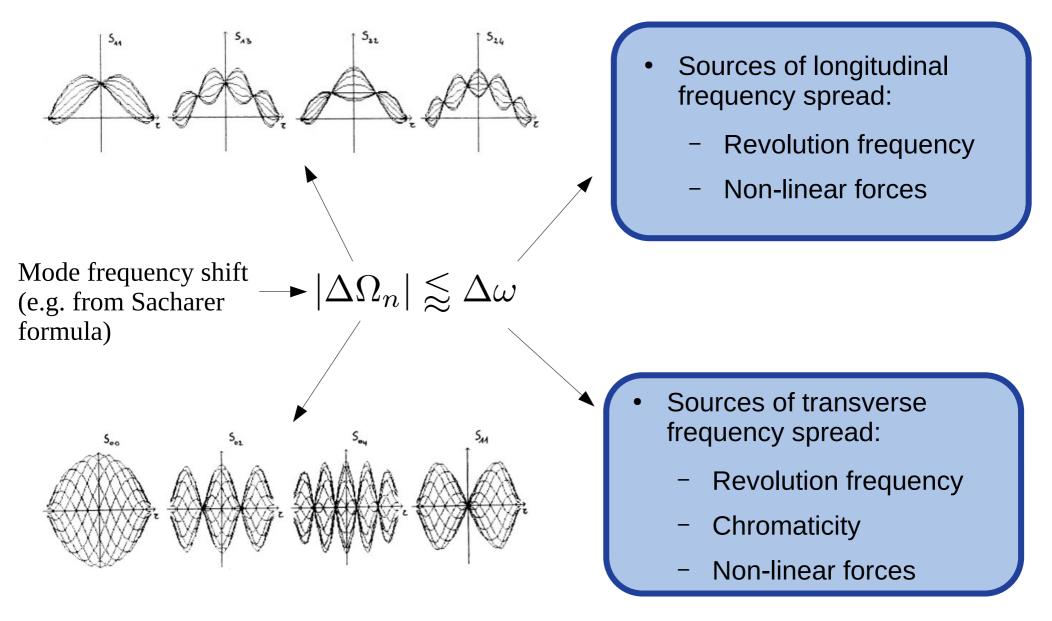




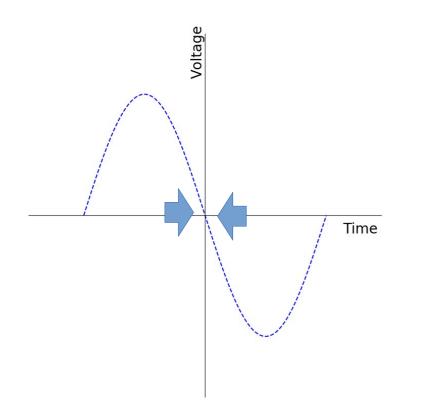




- Sources of longitudinal frequency spread:
 - Revolution frequency
 - Non-linear forces

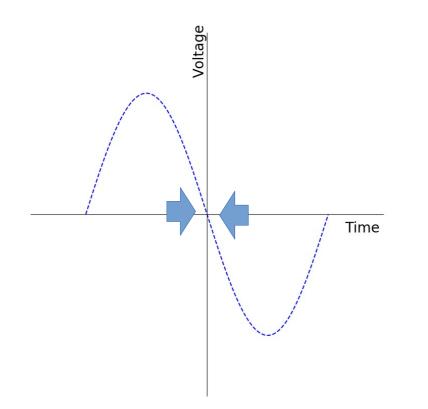


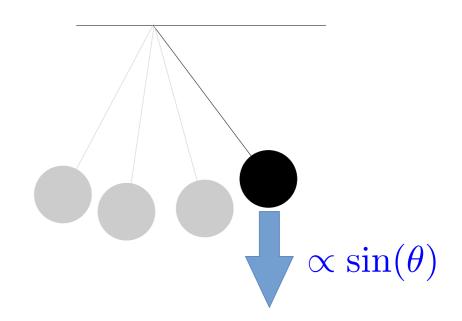
- For bunched beams, the longitudinal focusing provokes oscillations around the fixed point with $\,\omega_s$
 - \rightarrow As RF cavities function with sine wave, the focusing force is non-linear





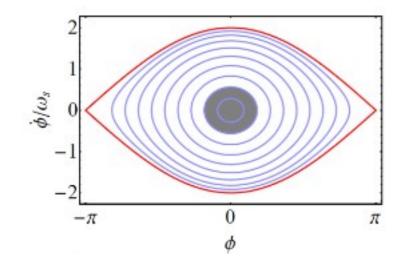
- For bunched beams, the longitudinal focusing provokes oscillations around the fixed point with $\,\omega_s$
 - \rightarrow As RF cavities function with sine wave, the focusing force is non-linear





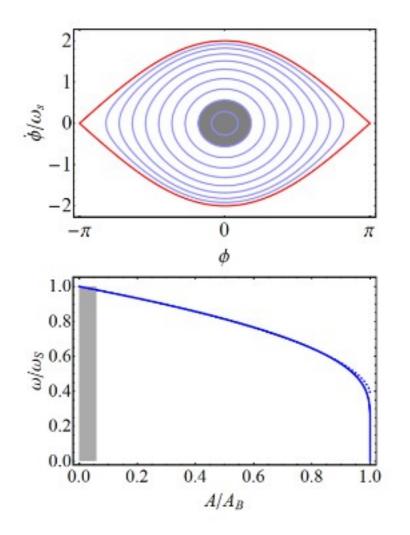
• The behaviour is identical to the pendulum without the small angle approximations

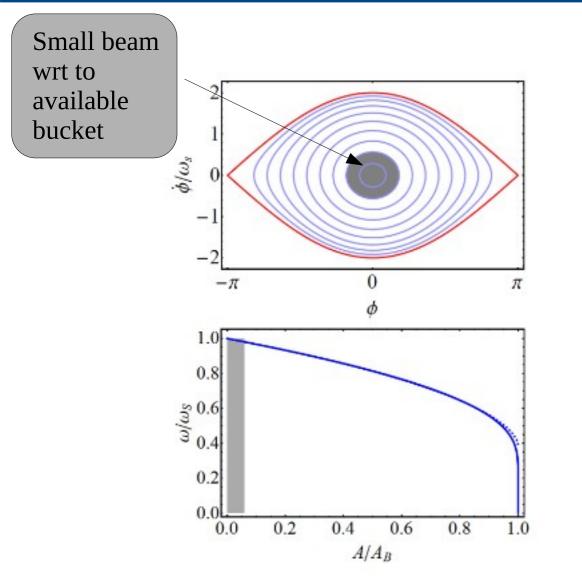
[Damerau]



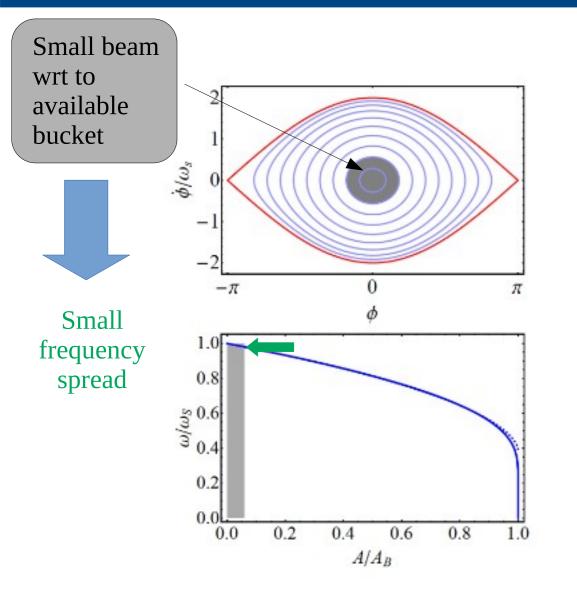


[Damerau]

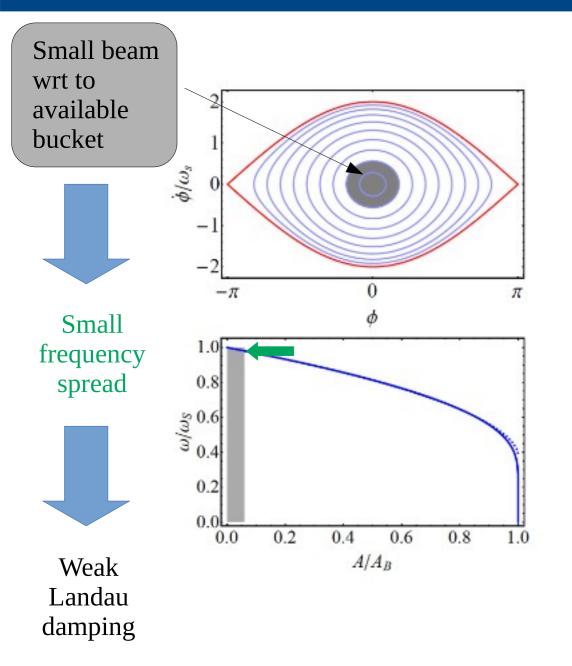




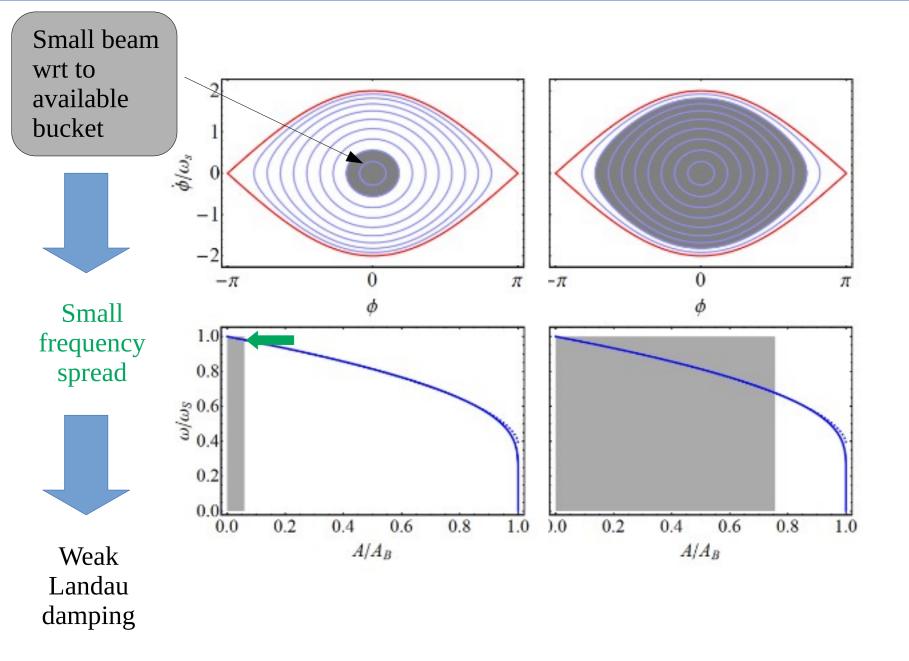
[Damerau]

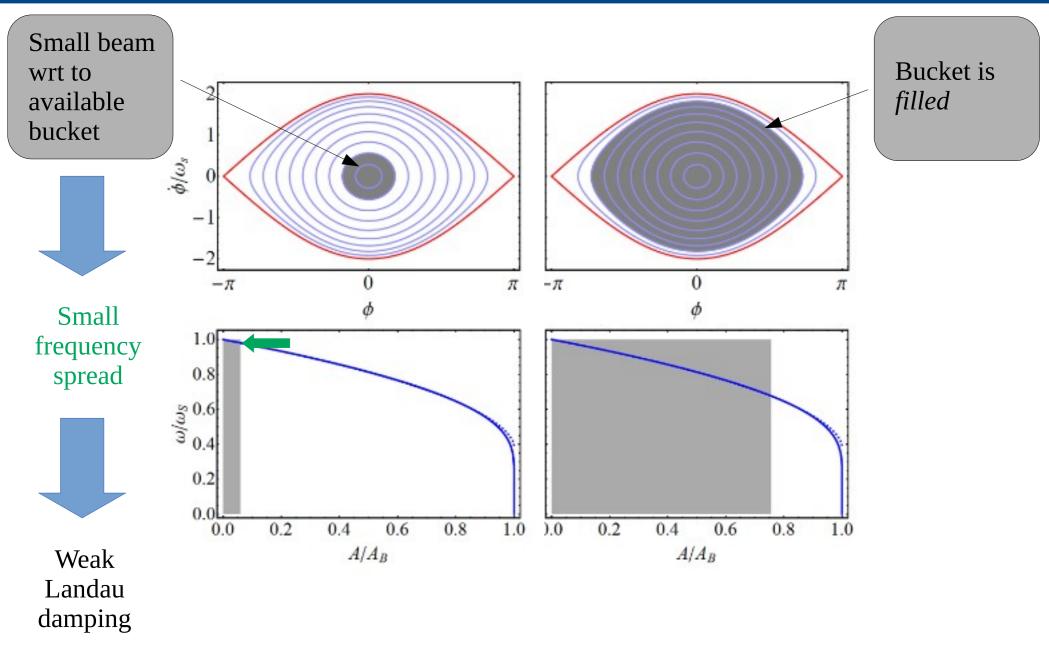


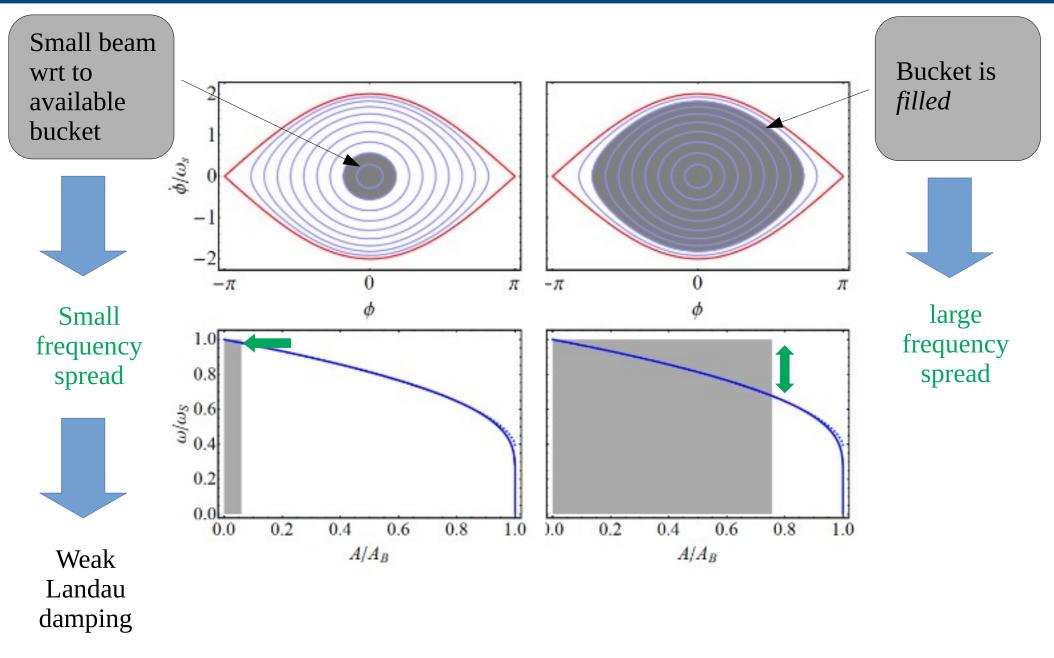
[Damerau]

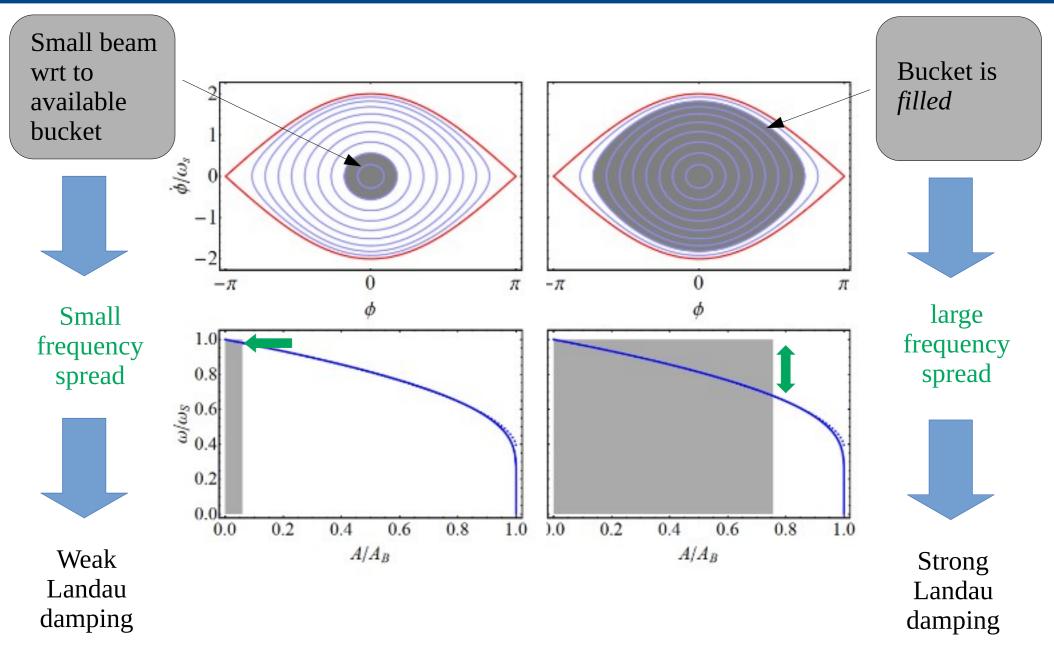


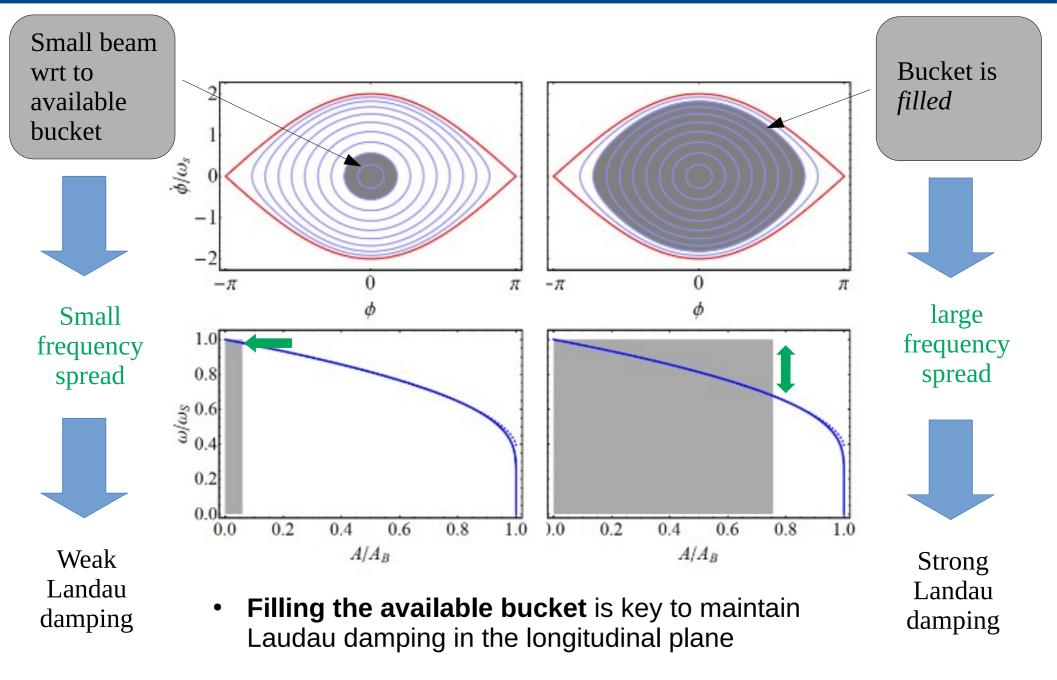
[Damerau]

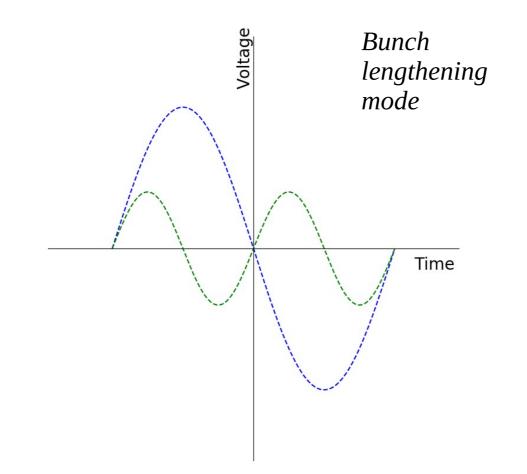


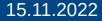


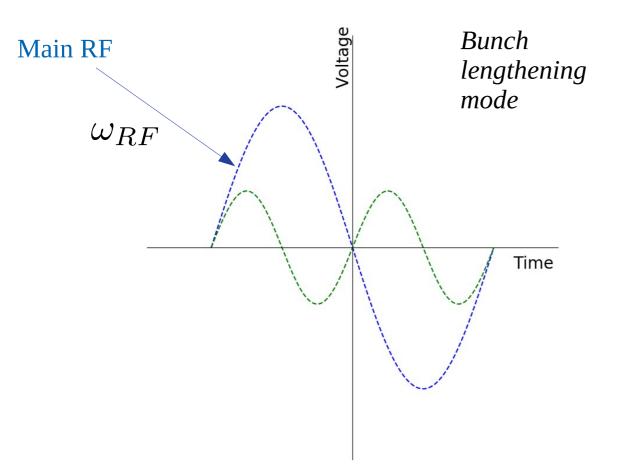


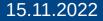


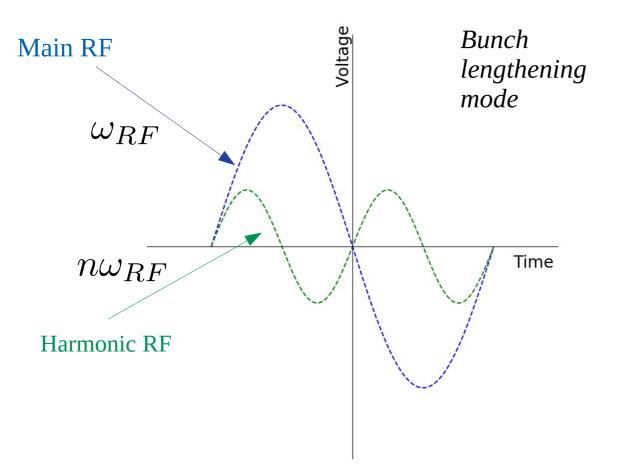




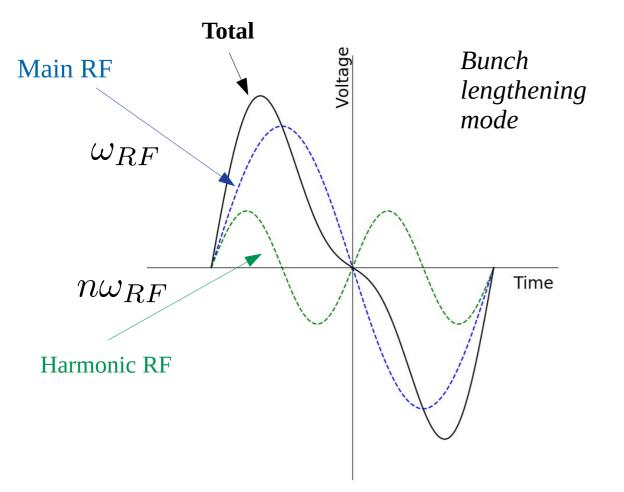


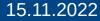


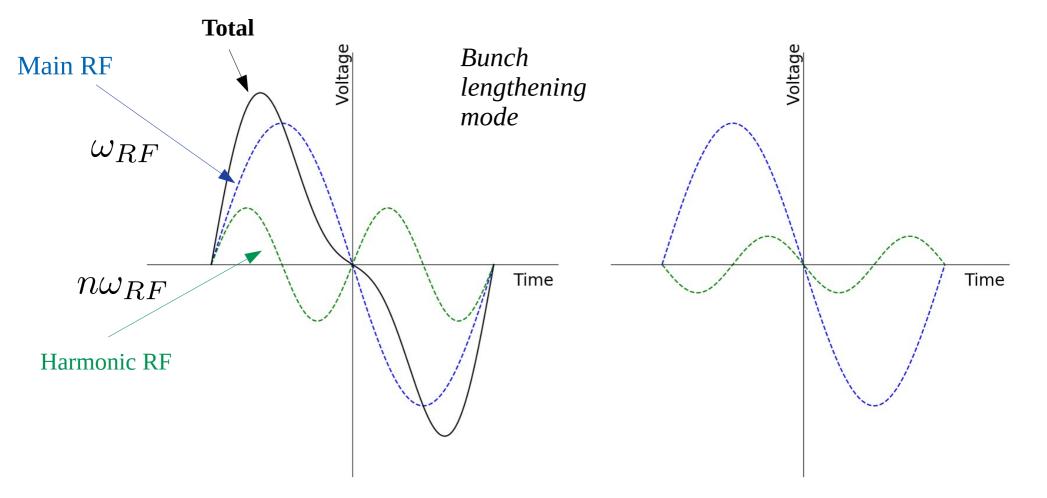


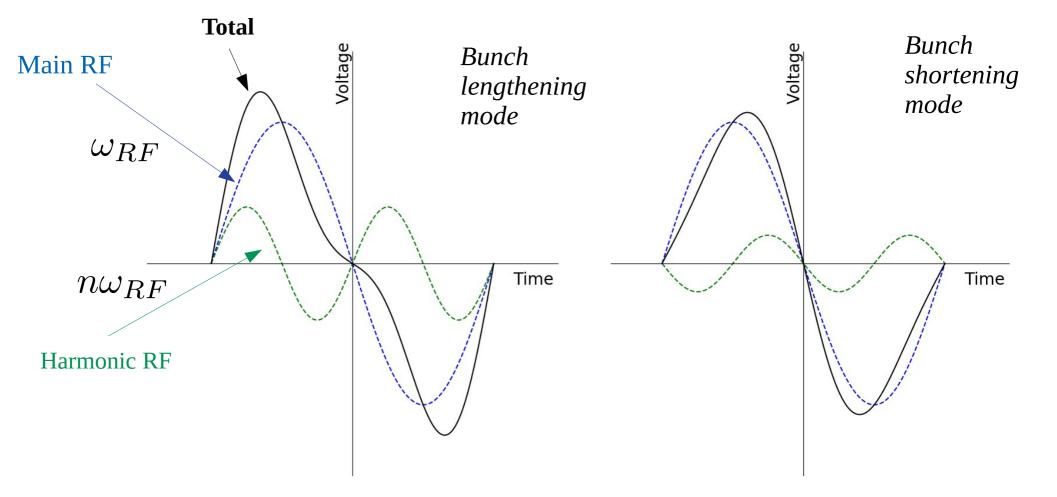


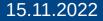


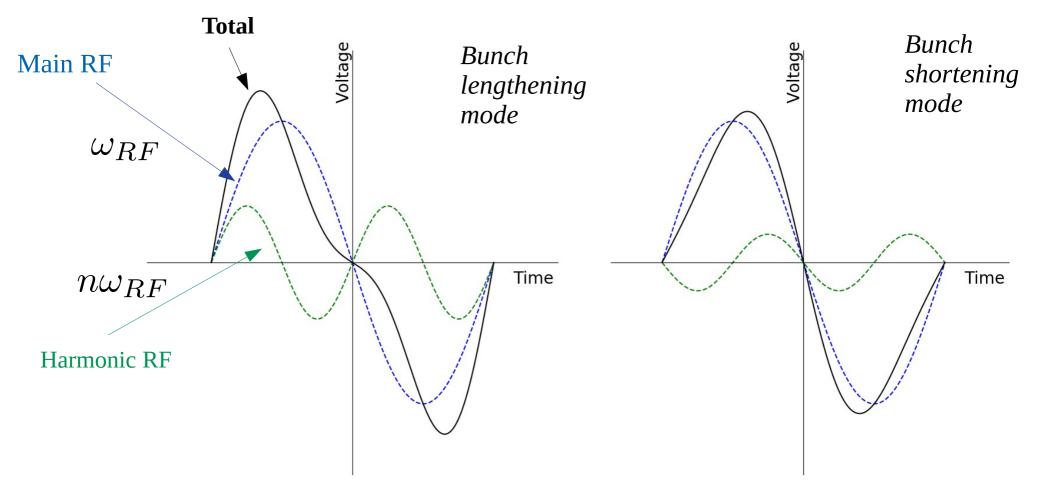








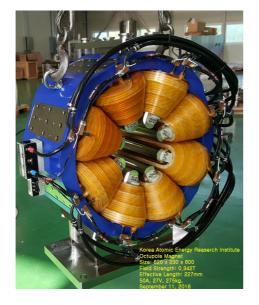


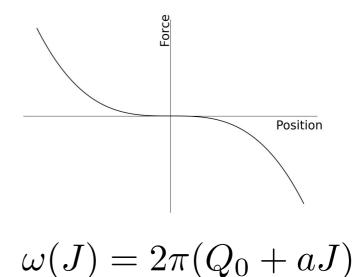


- The tune spread can be enhanced (or reduced) depending on the relative phase and voltage of the two RF systems
 - \rightarrow Improve / deteriorate Landau damping

Transverse stability

- In high energy machines, the frequency spread linked to revolution frequency and the chromaticity is usually small
- Chromatic sextupole magnets are non-linear, yet to first order they don't contribute to the transverse tune spread
 - → Dedicated octupole magnets (aka Landau octupoles)





[Octupole]

Optics

Slippage factor chromaticity correction

Optics

Slippage factor chromaticity correction **RF cavities** Frequency, voltage, harmonic systems



Optics

Slippage factor chromaticity correction **RF cavities** Frequency, voltage, harmonic systems

Magnets

Chromatic sextupoles, Landau octupoles

Optics

Slippage factor chromaticity correction

RF cavities Frequency, voltage, harmonic systems

Magnets

Chromatic sextupoles, Landau octupoles

Impedance

Beam pipe dimensions, Beam equipment designs (e.g. instrumentation, collimator, Vacuum valves), Material choices, transistions

Optics Slippage factor

chromaticity correction

RF cavities Frequency, voltage, harmonic systems

Magnets

Chromatic sextupoles, Landau octupoles

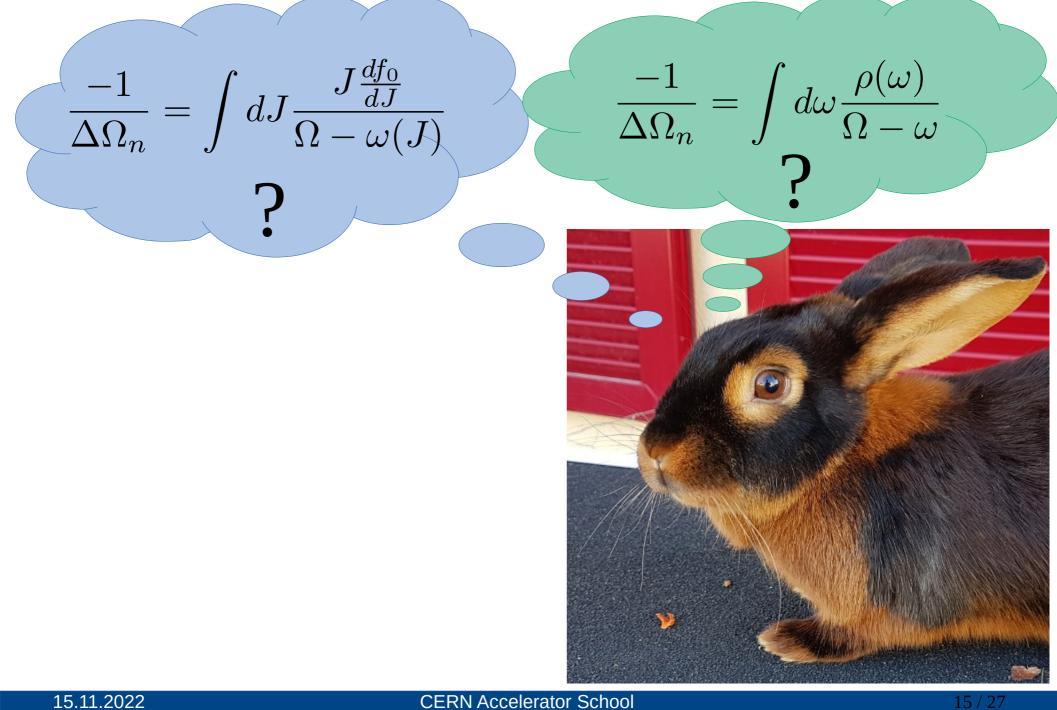
Impedance

Beam pipe dimensions, Beam equipment designs (e.g. instrumentation, collimator, Vacuum valves), Material choices, transistions

Operation

Adiabatic damping during energy ramp (RF voltage functions, longitudinal blowup)

Fuego's theoretical catch



Fuego's theoretical catch

 In plasmas, only the density of velocity matters

 $\frac{-1}{\Delta\Omega_n} = \int dJ \frac{J \frac{df_0}{dJ}}{\Omega - \omega(J)}$

→ A treatment based on the frequency distribution remains a **reasonable approximation** for many applications in accelerator



Fuego's theoretical catch

 In plasmas, only the density of velocity matters

 $\frac{-1}{\Delta\Omega_n} = \int dJ \frac{J \frac{df_0}{dJ}}{\Omega - \omega(J)}$

→ A treatment based on the frequency distribution remains a **reasonable approximation** for many applications in accelerator

• When the frequency spread arise from non-linear forces, the treatment is slighty different

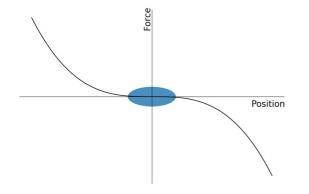
$$\omega(J) = \frac{\partial H}{\partial J}$$

15 / 27

 $\frac{-1}{\Delta\Omega_n} = \int d\omega \frac{\rho(\omega)}{\Omega - \omega}$

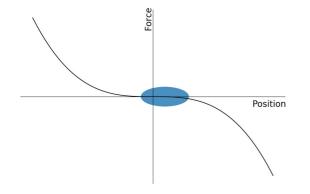
- Some collective forces are non-linear, they have an impact on Landau damping
 - Due to their dynamic nature, they lead to different behaviours
 - \rightarrow Different dispersion relations

External forces



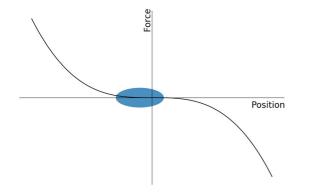
- Some collective forces are non-linear, they have an impact on Landau damping
 - Due to their dynamic nature, they lead to different behaviours
 - \rightarrow Different dispersion relations

External forces

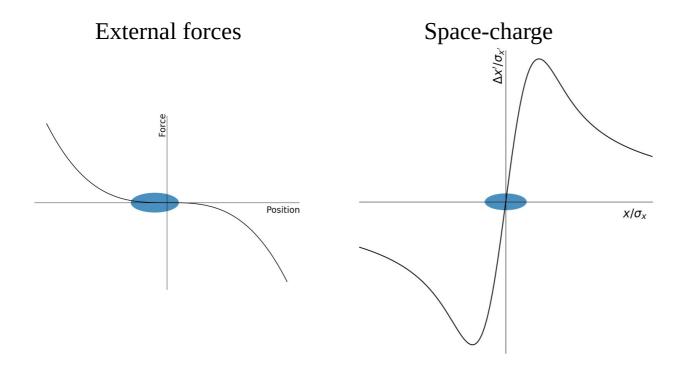


- Some collective forces are non-linear, they have an impact on Landau damping
 - Due to their dynamic nature, they lead to different behaviours
 - \rightarrow Different dispersion relations

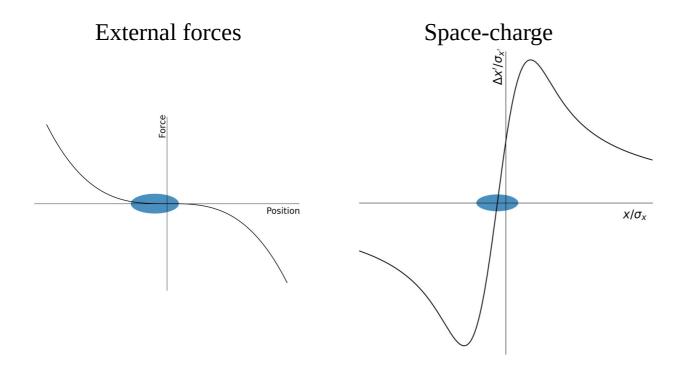
External forces



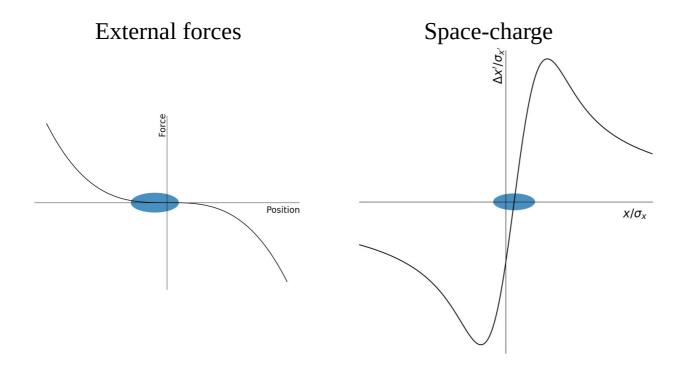
- Some collective forces are non-linear, they have an impact on Landau damping
 - Due to their dynamic nature, they lead to different behaviours
 - \rightarrow Different dispersion relations



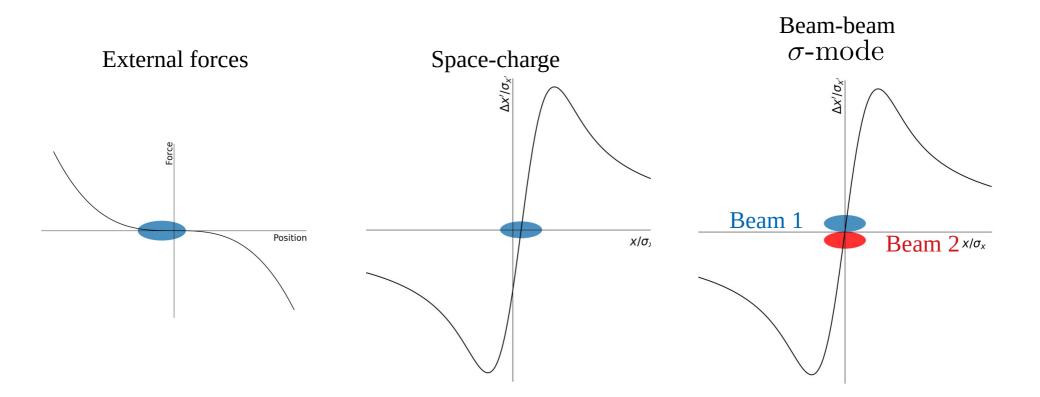
- Some collective forces are non-linear, they have an impact on Landau damping
 - Due to their dynamic nature, they lead to different behaviours
 - \rightarrow Different dispersion relations



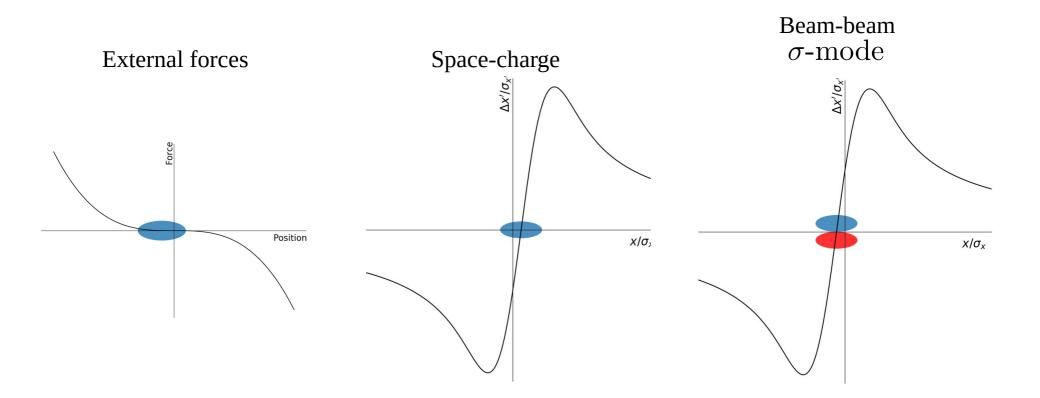
- Some collective forces are non-linear, they have an impact on Landau damping
 - Due to their dynamic nature, they lead to different behaviours
 - \rightarrow Different dispersion relations



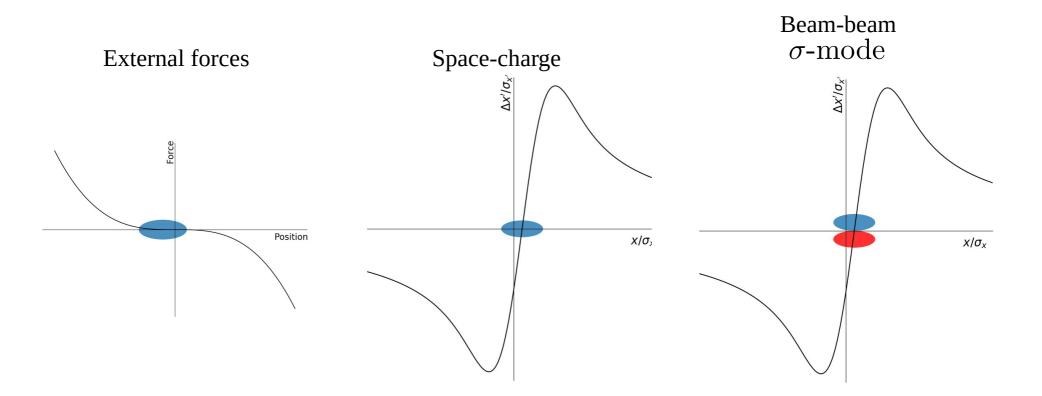
- Some collective forces are non-linear, they have an impact on Landau damping
 - Due to their dynamic nature, they lead to different behaviours
 - \rightarrow Different dispersion relations



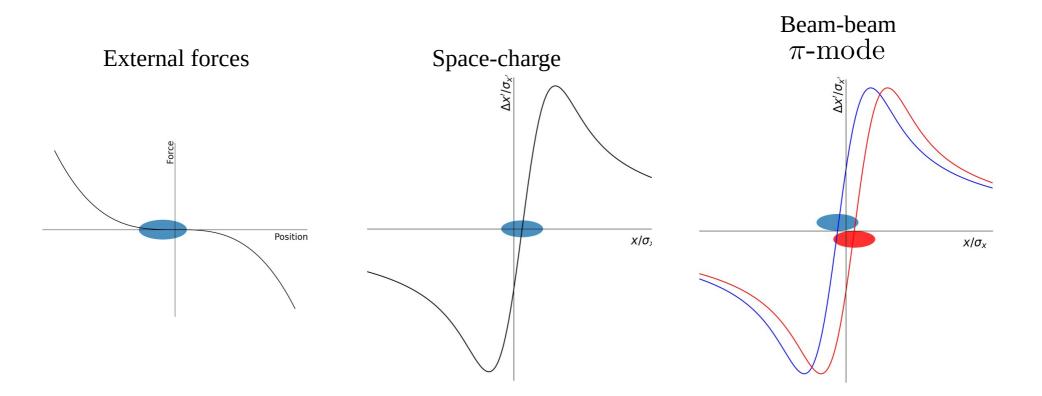
- Some collective forces are non-linear, they have an impact on Landau damping
 - Due to their dynamic nature, they lead to different behaviours
 - \rightarrow Different dispersion relations



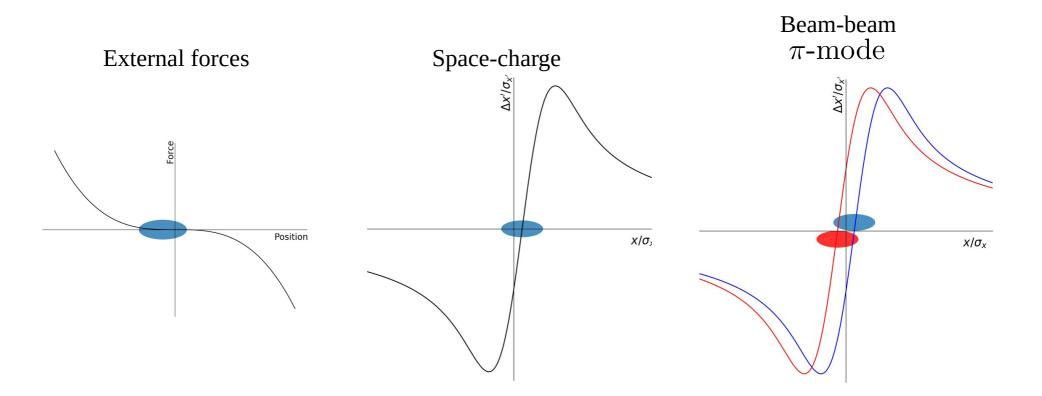
- Some collective forces are non-linear, they have an impact on Landau damping
 - Due to their dynamic nature, they lead to different behaviours
 - \rightarrow Different dispersion relations



- Some collective forces are non-linear, they have an impact on Landau damping
 - Due to their dynamic nature, they lead to different behaviours
 - \rightarrow Different dispersion relations

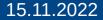


- Some collective forces are non-linear, they have an impact on Landau damping
 - Due to their dynamic nature, they lead to different behaviours
 - \rightarrow Different dispersion relations



Stability of the rigid bunch mode with space-charge [Metral, Kornilov]

$$\int dJ_x dJ_y \frac{\partial f_0}{\partial J_x} \left(\Delta Q_n^x - \Delta Q_{SC}^x (J_x, J_y) \right) \\ \frac{\int dJ_x dJ_y}{Q^x - Q_0^x - \Delta Q_0^x (J_x, J_y) - \Delta Q_{SC}^x (J_x, J_y) - nQ_s} = -1$$



Stability of the rigid bunch mode with space-charge [Metral, Kornilov]

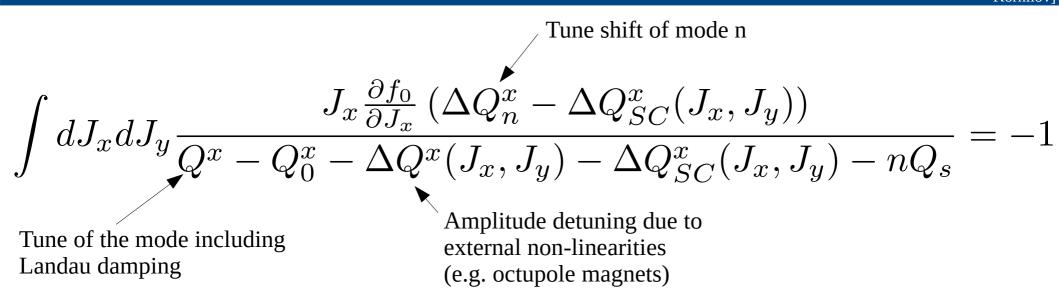
$$\int dJ_x dJ_y \frac{J_x \frac{\partial f_0}{\partial J_x} \left(\Delta Q_n^x - \Delta Q_{SC}^x (J_x, J_y) \right)}{Q^x - Q_0^x - \Delta Q^x (J_x, J_y) - \Delta Q_{SC}^x (J_x, J_y) - nQ_s} = -1$$

Stability of the rigid bunch mode with space-charge [Metral, Kornilov]

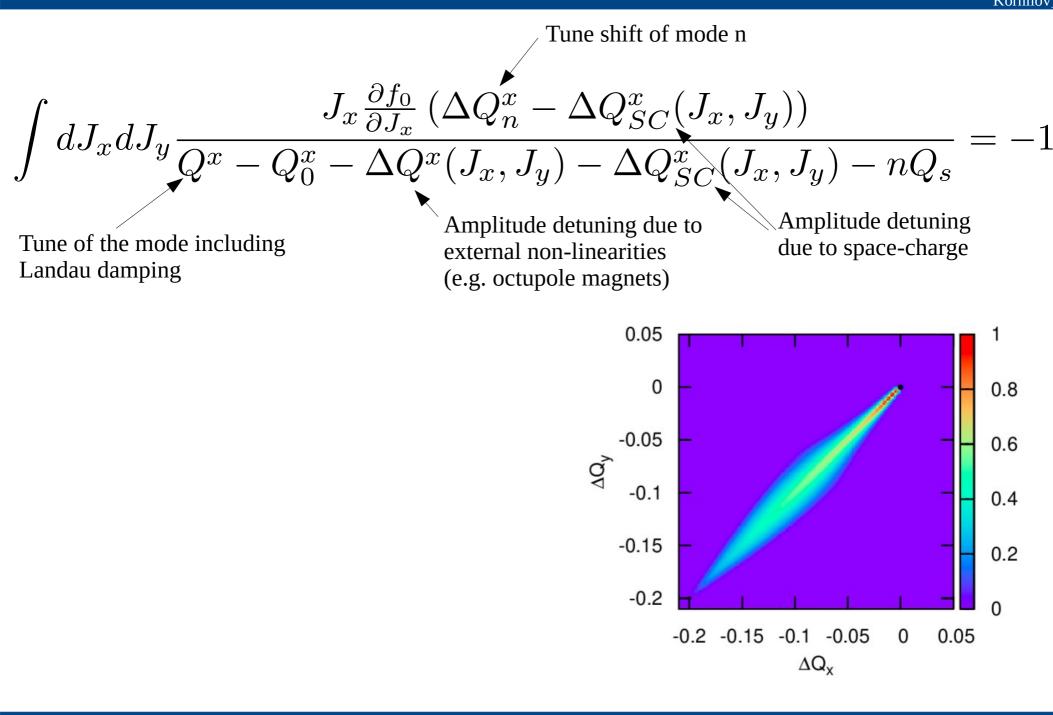
$$\int dJ_x dJ_y \frac{J_x \frac{\partial f_0}{\partial J_x} \left(\Delta Q_n^x - \Delta Q_{SC}^x (J_x, J_y) \right)}{Q^x - Q_0^x - \Delta Q^x (J_x, J_y) - \Delta Q_{SC}^x (J_x, J_y) - nQ_s} = -1$$

Tune of the mode including Landau damping

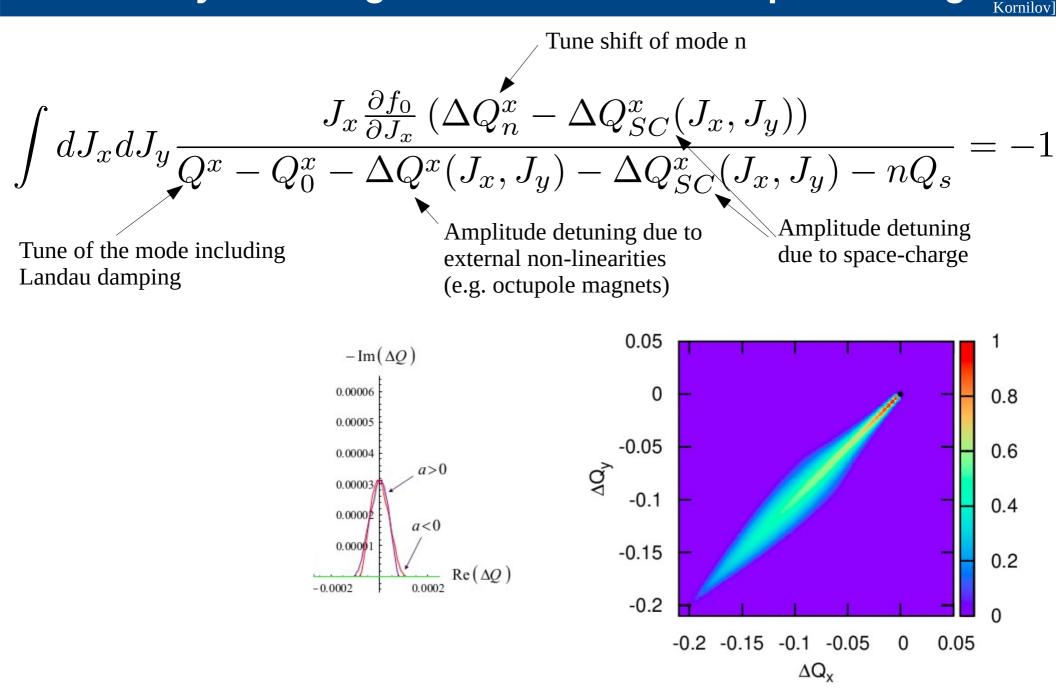
Stability of the rigid bunch mode with space-charge [Metral, Korpilov]



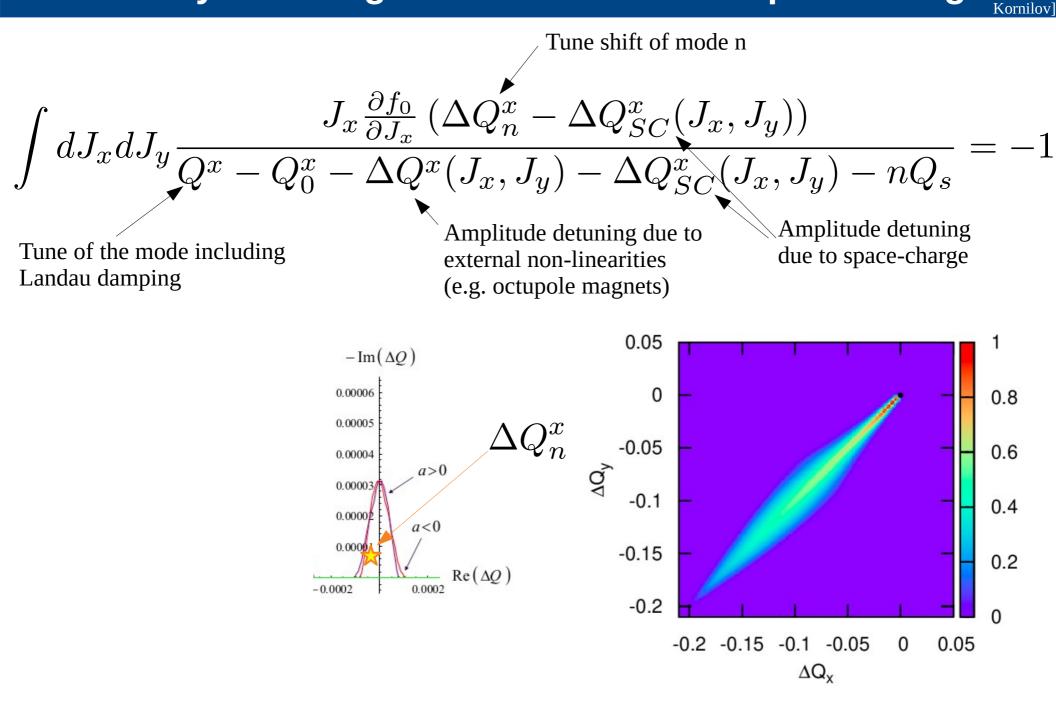
Stability of the rigid bunch mode with space-charge [Metral, Komilov]



Stability of the rigid bunch mode with space-charge [Metral,

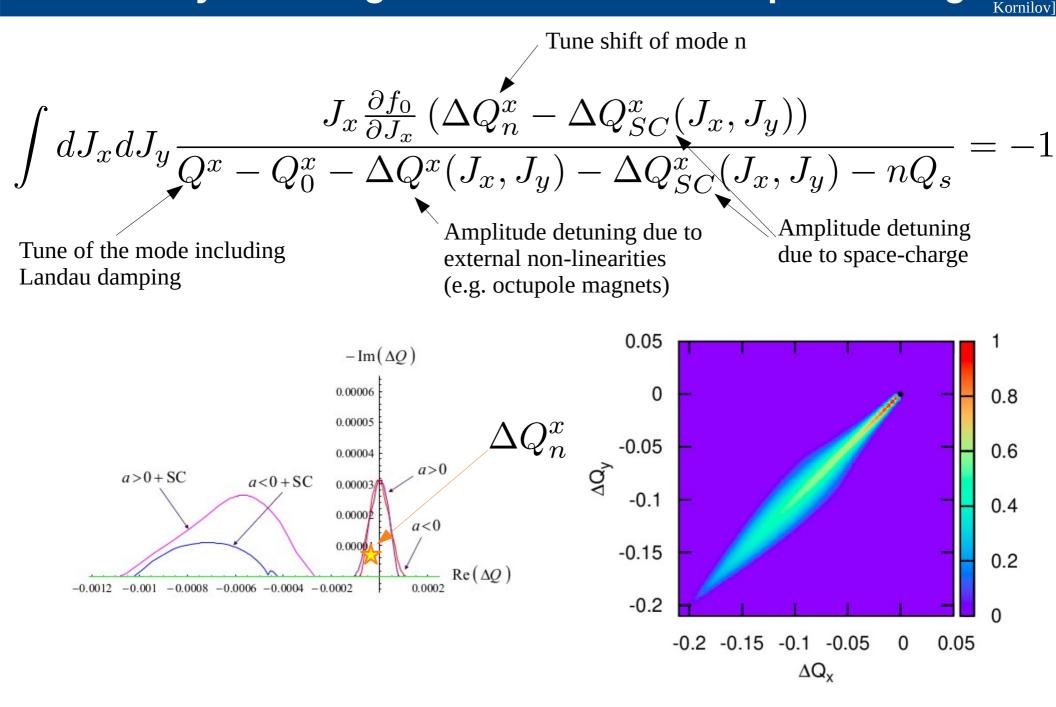


Stability of the rigid bunch mode with space-charge [Metral,

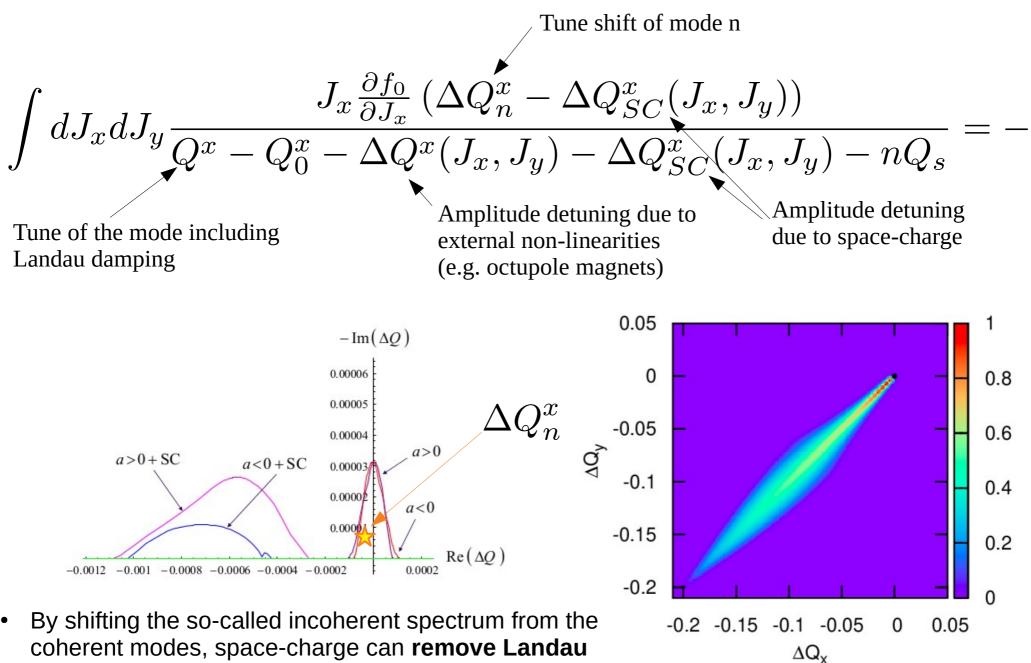


15.11.2022

Stability of the rigid bunch mode with space-charge [Metral,

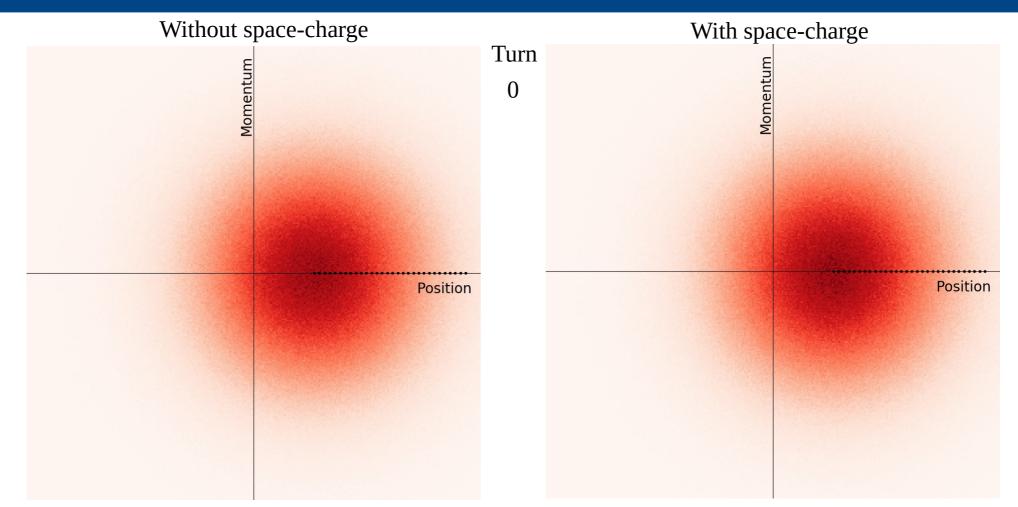


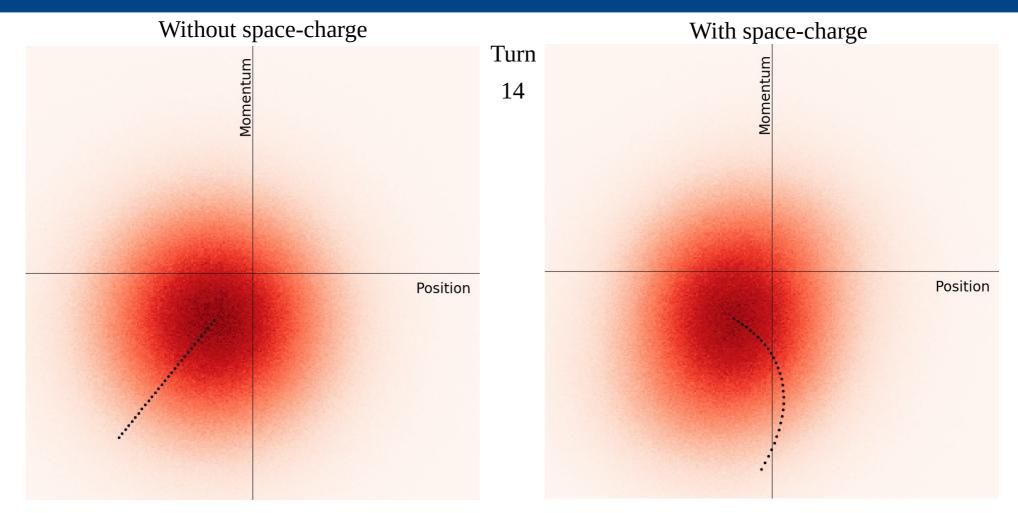
Stability of the rigid bunch mode with space-charge [Metral, Komilov]

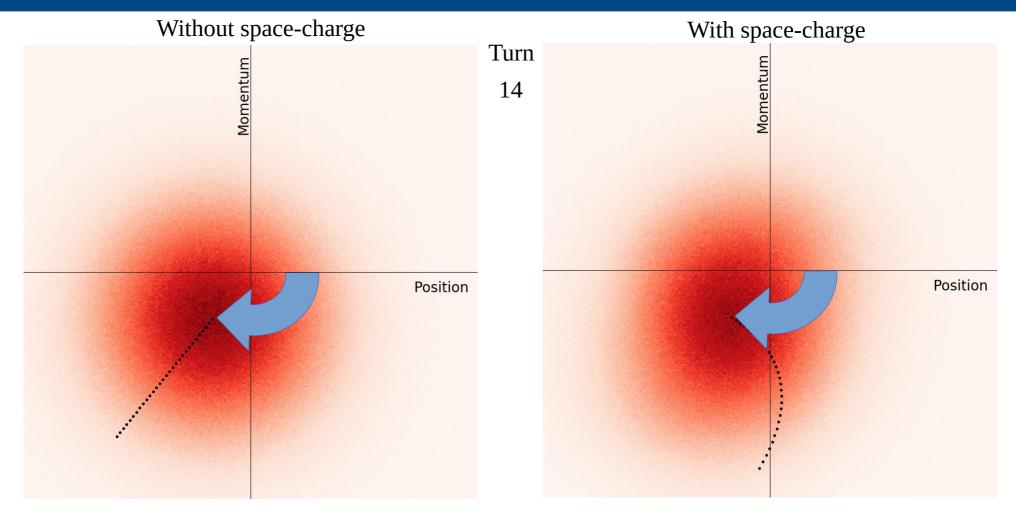


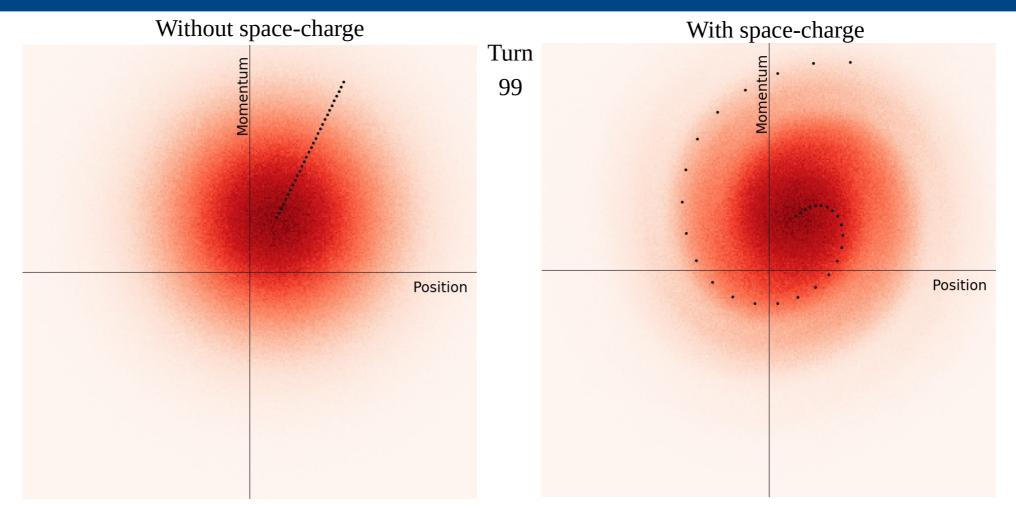
damping for modes otherwise stabilised e.g. by octupoles

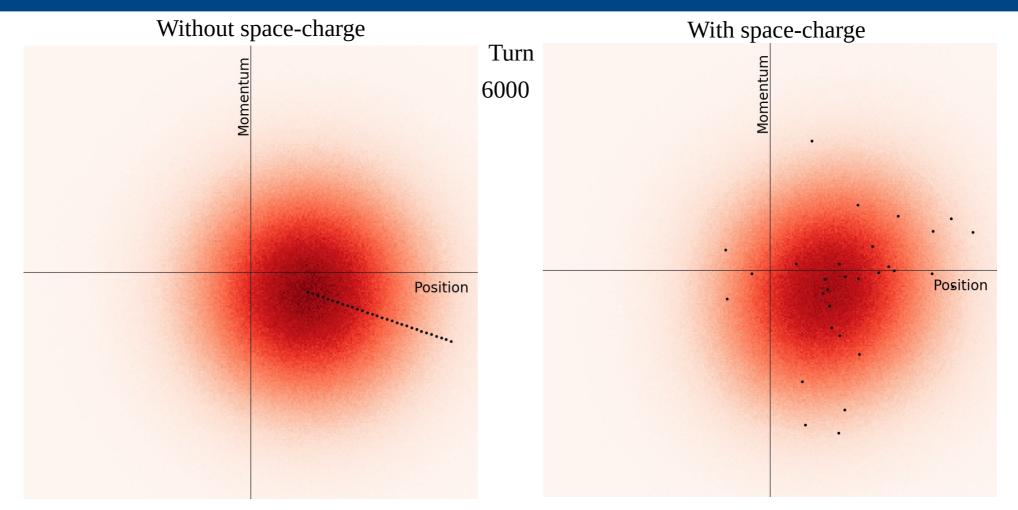
CERN Accelerator School

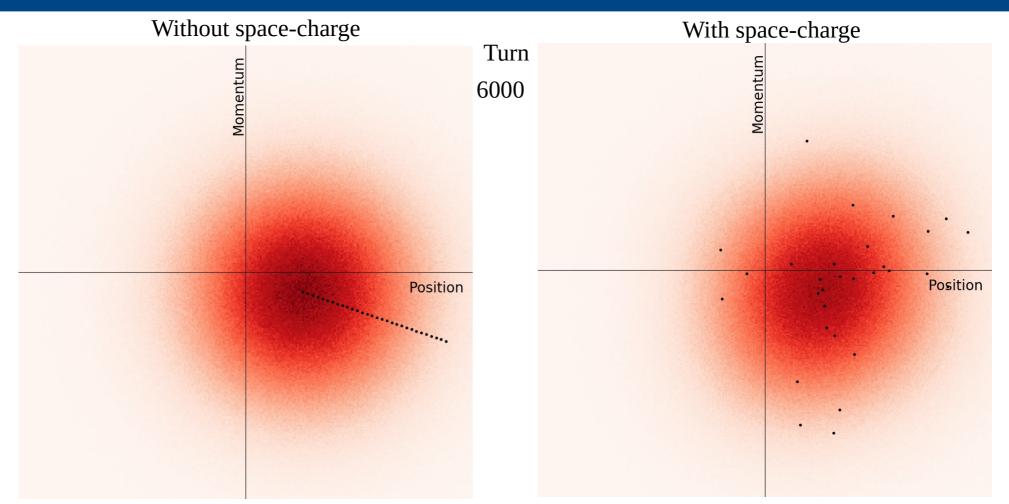








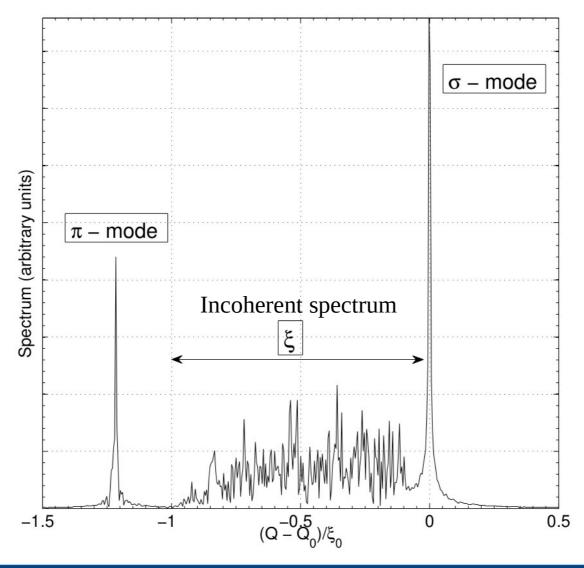




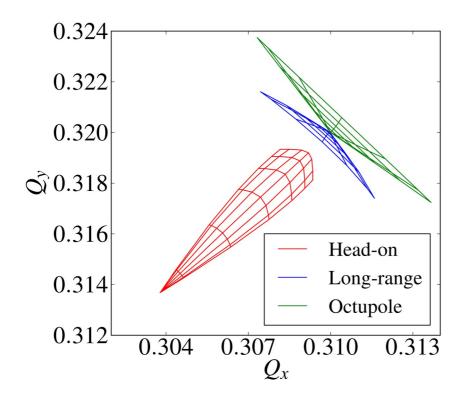
- The motion of the centroid is not affected by space-charge
 - → Coherent mode
- The motion of single particles around the centroid is affected
 - \rightarrow Incoherent tune spread

Stability of the rigid bunch mode with beam-beam [Pieloni]

- A similar effect occurs with the coherent modes generated by beam-beam interactions
 - \rightarrow They are outside of the incoherent spectrum, Landau damping is lost



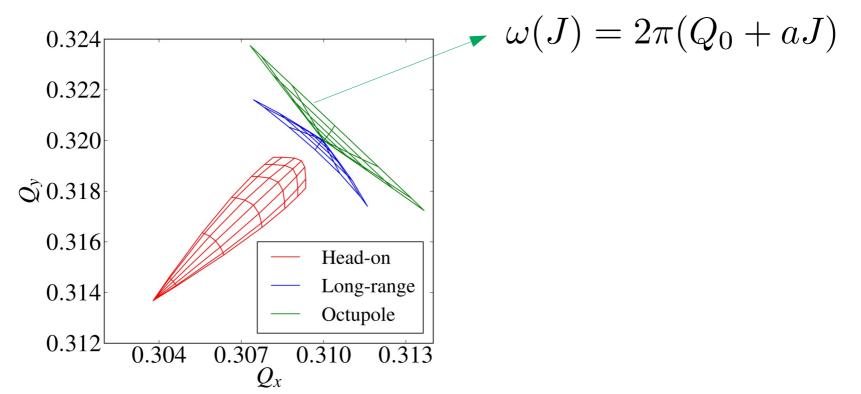
• If the coherent modes are suppressed (e.g. with an active feedback), the remaining tune spread can be beneficial for other modes



[Buffat,

Stability diagrams with beam-beam

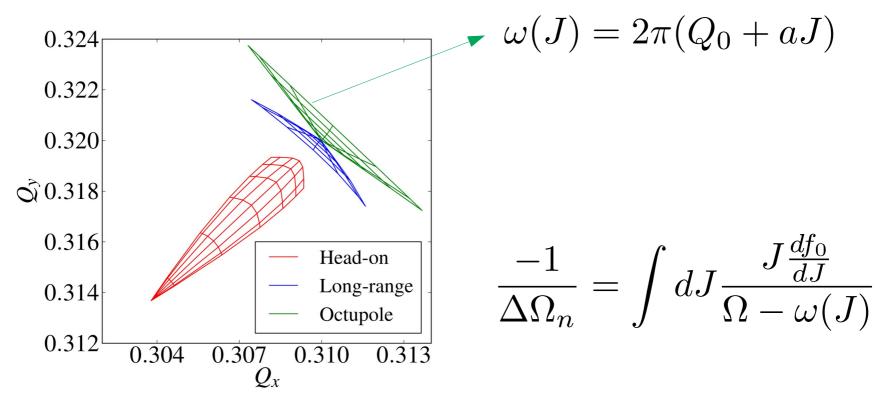
• If the coherent modes are suppressed (e.g. with an active feedback), the remaining tune spread can be beneficial for other modes



[Buffat,

Stability diagrams with beam-beam

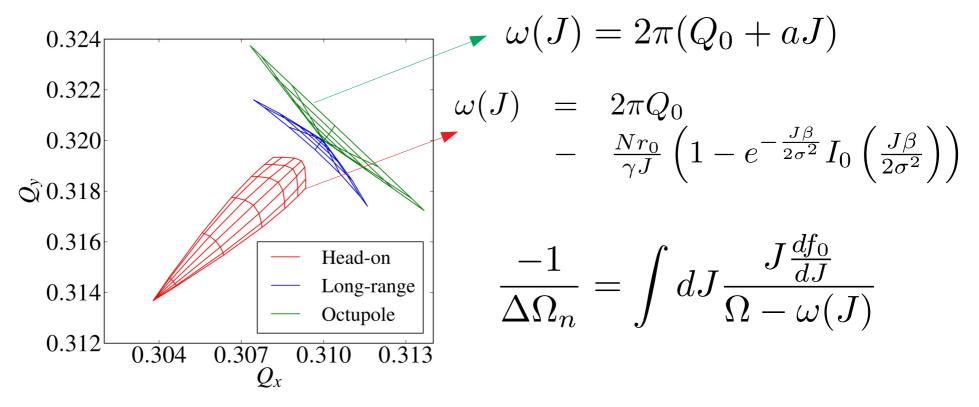
• If the coherent modes are suppressed (e.g. with an active feedback), the remaining tune spread can be beneficial for other modes



[Buffat,

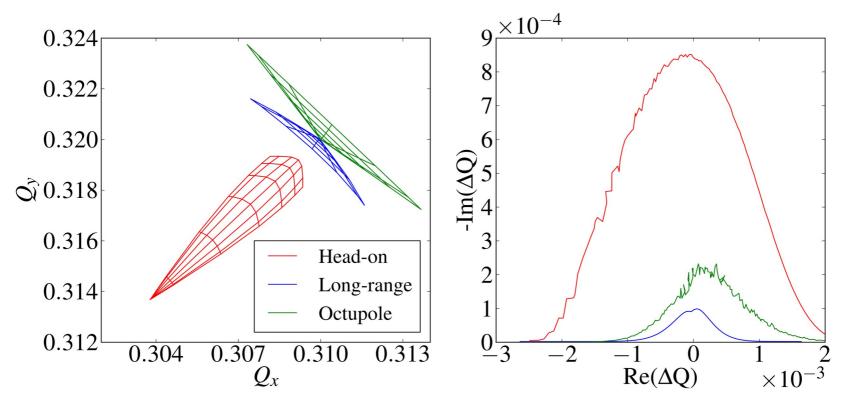
Stability diagrams with beam-beam

• If the coherent modes are suppressed (e.g. with an active feedback), the remaining tune spread can be beneficial for other modes



[Buffat,

• If the coherent modes are suppressed (e.g. with an active feedback), the remaining tune spread can be beneficial for other modes

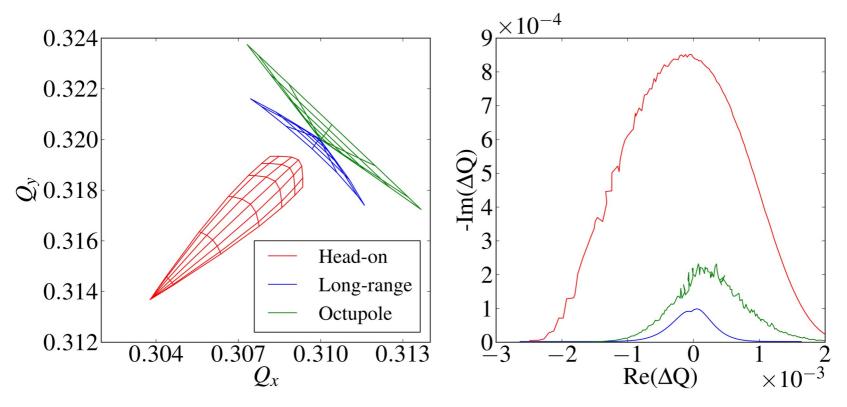


 Due to its different dependence on the action, the amplitude detuning due to headon beam-beam interactions is more efficient at producing Landau damping than octupoles!

[Buffat,

Chao21

• If the coherent modes are suppressed (e.g. with an active feedback), the remaining tune spread can be beneficial for other modes

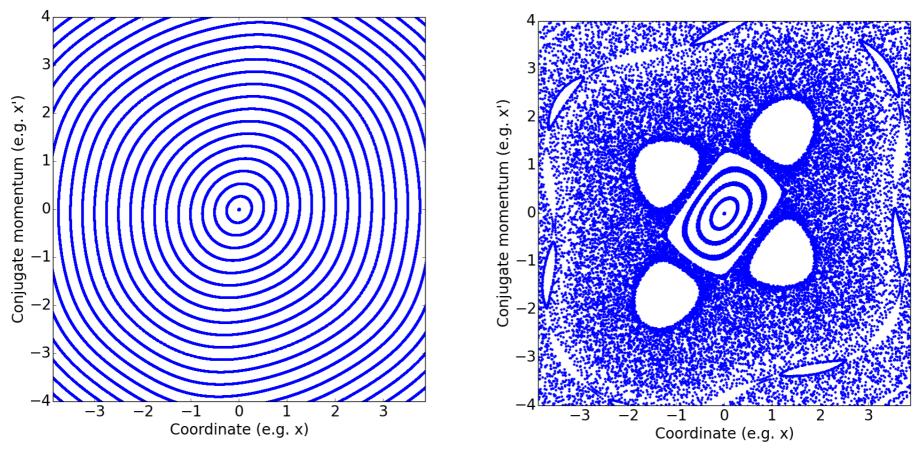


- Due to its different dependence on the action, the amplitude detuning due to headon beam-beam interactions is more efficient at producing Landau damping than octupoles!
 - \rightarrow Maybe we should be inspired ?

[Buffat,

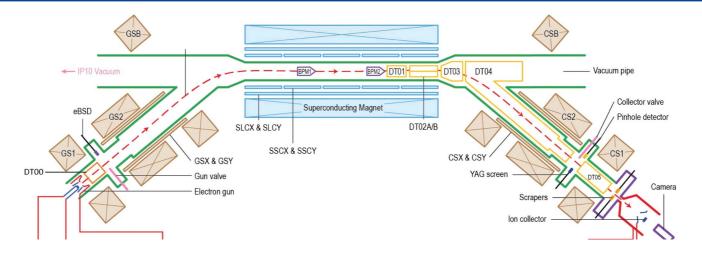
Chao21

The issue with non-linear forces

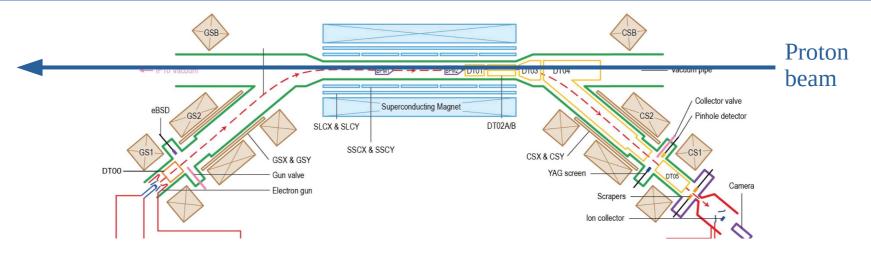


- Along with the tune spread required for Landau damping, non-linearities come with detrimental effect for the single particle trajectories:
 - Resonances, chaotic motion and eventually beam quality degradation (particles losses, emittance growth)

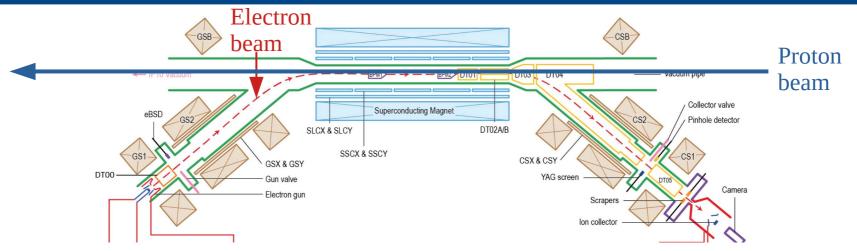
 \rightarrow The **amount of Landau** damping that can be obtained with octupoles is **limited** by their impact on beam losses



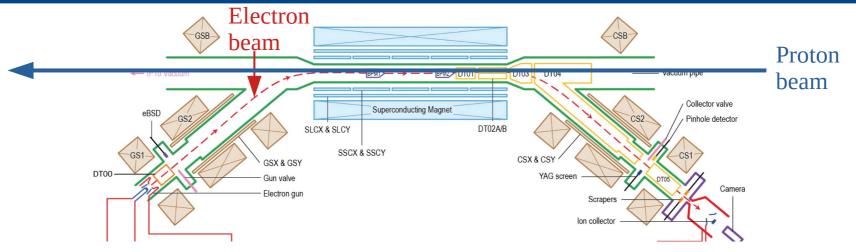


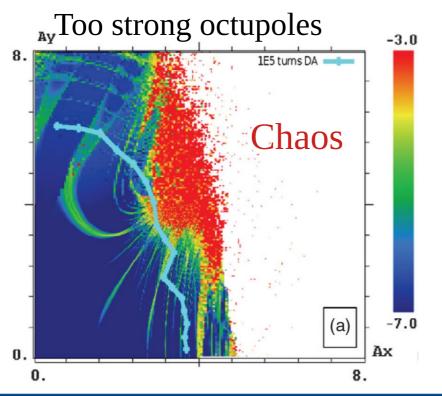




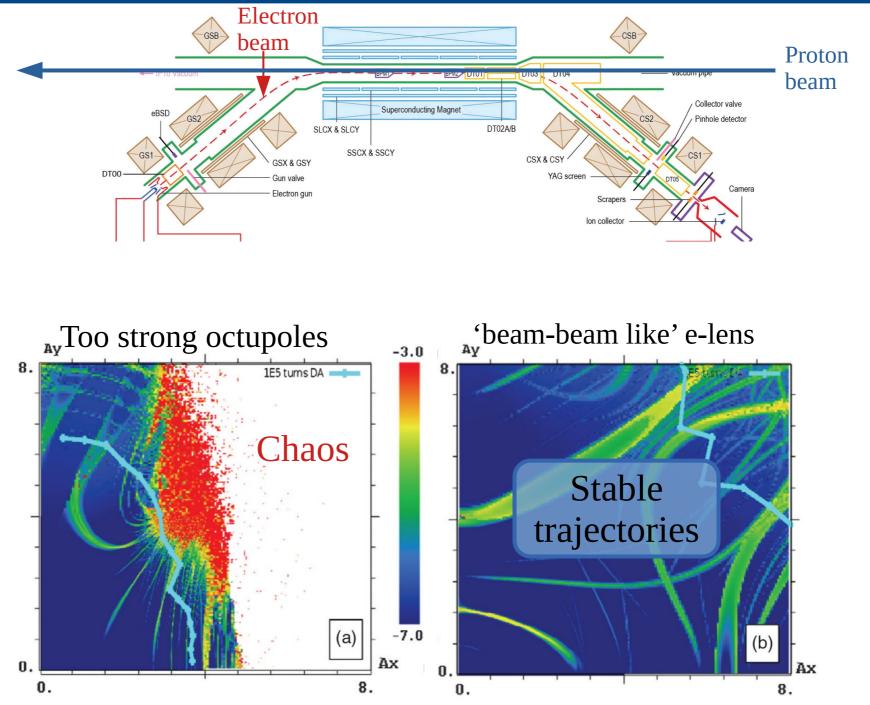






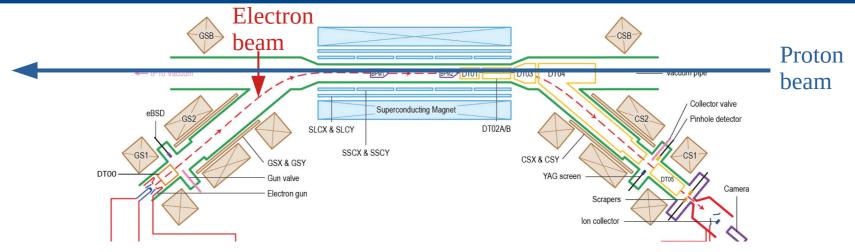


15.11.2022

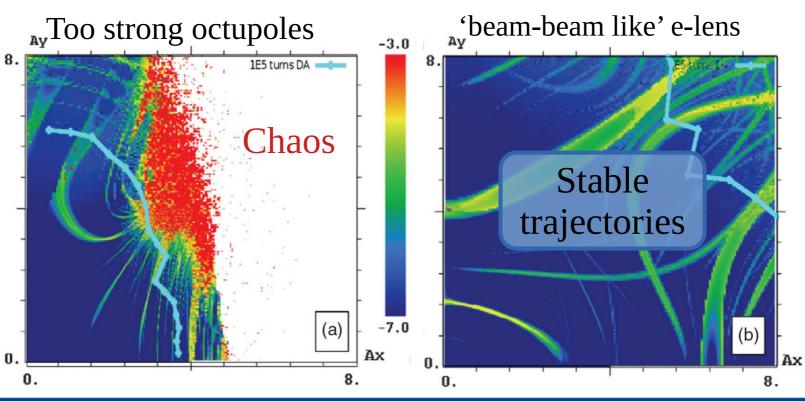


15.11.2022

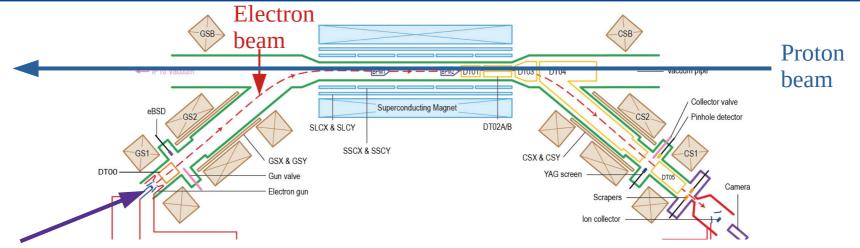
CERN Accelerator School



The gun design allows for various electron beam shapes

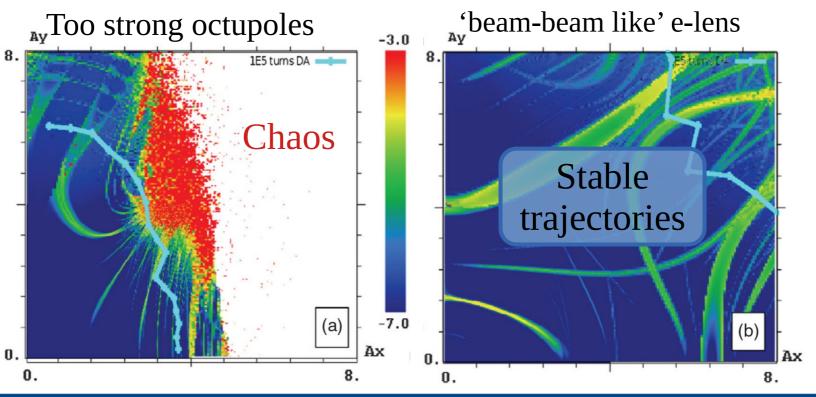


15.11.2022



The gun design allows for various electron beam shapes

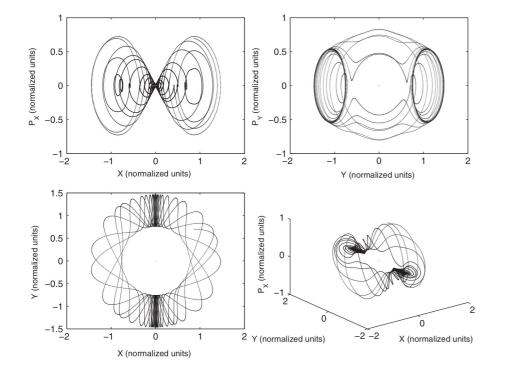
→ Optimise the force to maximise Landau damping with least impact on the beam quality



15.11.2022

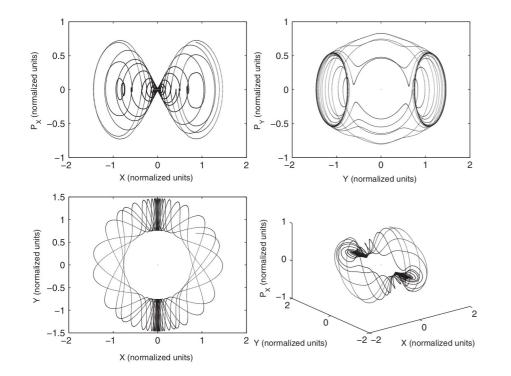
Non-linear integrable optics

- It is possible to introduce 'good' non-linearities that generate a tune spread yet maintaining some invariants of motion
 - \rightarrow Possibly strong Landau damping without deterioration of the beam quality



[NLIO,IOTA, McMillan]

- It is possible to introduce 'good' non-linearities that generate a tune spread yet maintaining some invariants of motion
 - \rightarrow Possibly strong Landau damping without deterioration of the beam quality

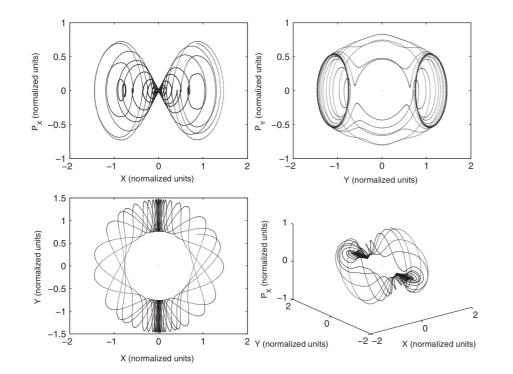


A series of independently powered octupoles to generate a non-linear integrable optics at IOTA

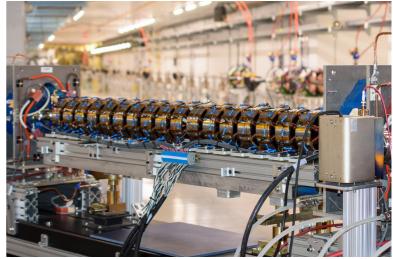


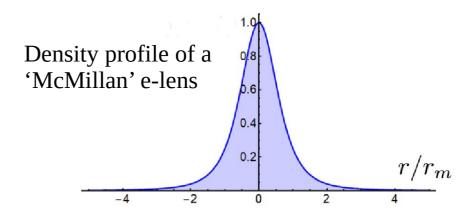
[NLIO,IOTA, McMillan]

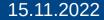
- It is possible to introduce 'good' non-linearities that generate a tune spread yet maintaining some invariants of motion
 - \rightarrow Possibly strong Landau damping without deterioration of the beam quality



A series of independently powered octupoles to generate a non-linear integrable optics at IOTA







23 / 27

[NLIO,IOTA, McMillan]

$$\frac{\int dr r f_0(r) \left| H_l^k(r) \right|^2}{\Delta \Omega_{ext}^{l,k}} = \int dr \frac{r f_0(r) \left| H_l^k(r) \right|^2}{\Omega^{l,k} - \omega(r) - l\omega_s}$$

$$\frac{\int dr r f_0(r) \left| H_l^k(r) \right|^2}{\Delta \Omega_{ext}^{l,k}} = \int dr \frac{r f_0(r) \left| H_l^k(r) \right|^2}{\Omega^{l,k} - \omega(r) - l\omega_s}$$

Transverse frequency shift



$$\frac{\int dr r f_0(r) \left| H_l^k(r) \right|^2}{\Delta \Omega_{ext}^{l,k}} = \int dr \frac{r f_0(r) \left| H_l^k(r) \right|^2}{\Omega^{l,k} - \omega(r) - l\omega_s}$$

Transverse frequency shift

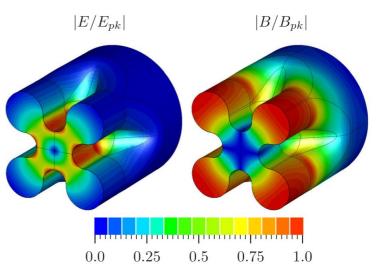
Longitudinal oscillation amplitude

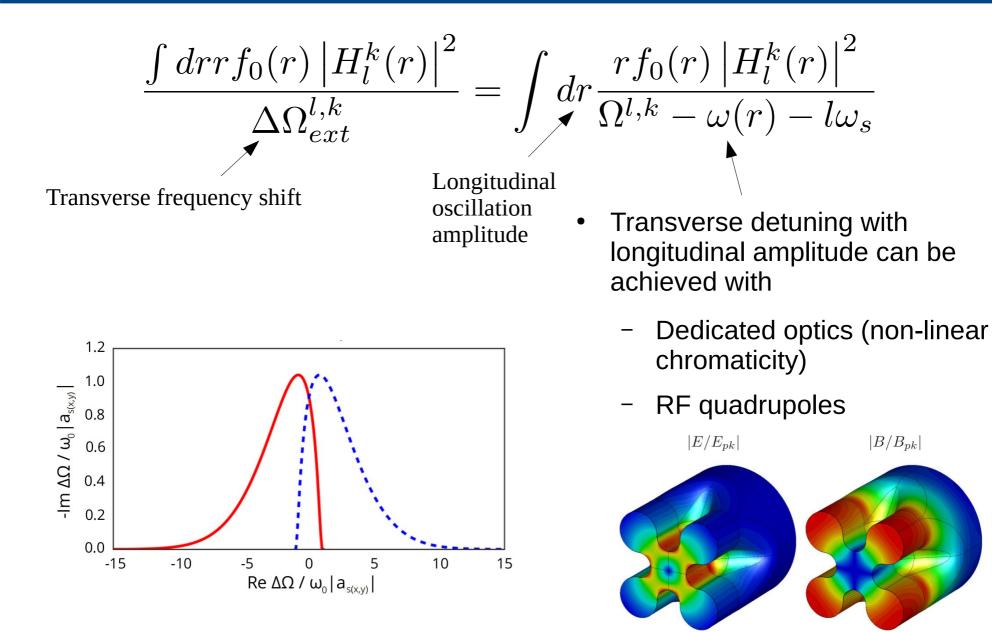
$$\frac{\int drr f_{0}(r) \left| H_{l}^{k}(r) \right|^{2}}{\Delta \Omega_{ext}^{l,k}} = \int dr \frac{r f_{0}(r) \left| H_{l}^{k}(r) \right|^{2}}{\Omega^{l,k} - \omega(r) - l\omega_{s}}$$
Transverse frequency shift Longitudinal oscillation

amplitude

 Transverse detuning with longitudinal amplitude can be achieved with

- Dedicated optics (non-linear chromaticity)
- RF quadrupoles





24 / 27

0.25

0.0

0.5

0.75

1.0

- In some cases Landau damping arise naturally in accelerators
 - Momentum spread
 - Chromatic spread
 - Non-linearity of the longitudinal focusing (RF wave)
 - Non-linearity of collective forces (Space-charge, beam-beam)

- In some cases Landau damping arise naturally in accelerators
 - Momentum spread
 - Chromatic spread
 - Non-linearity of the longitudinal focusing (RF wave)
 - Non-linearity of collective forces (Space-charge, beam-beam)

- If this is not sufficient, specific devices are used
 - Harmonic RF cavities (aka Landau cavities)
 - Landau octupoles
 - More advanced tools (electron-lens, special magnets, RF quadrupoles)

- In some cases Landau damping arise naturally in accelerators
 - Momentum spread
 - Chromatic spread
 - Non-linearity of the longitudinal focusing (RF wave)
 - Non-linearity of collective forces (Space-charge, beam-beam)

- If this is not sufficient, specific devices are used
 - Harmonic RF cavities (aka Landau cavities)
 - Landau octupoles
 - More advanced tools (electron-lens, special magnets, RF quadrupoles)
- Several aspect of accelerator design are driven by the need for Landau damping (Beam parameters, optics, operation, ...)

- In some cases Landau damping arise naturally in accelerators
 - Momentum spread
 - Chromatic spread
 - Non-linearity of the longitudinal focusing (RF wave)
 - Non-linearity of collective forces (Space-charge, beam-beam)

- If this is not sufficient, specific devices are used
 - Harmonic RF cavities (aka Landau cavities)
 - Landau octupoles
 - More advanced tools (electron-lens, special magnets, RF quadrupoles)
- Several aspect of accelerator design are driven by the need for Landau damping (Beam parameters, optics, operation, ...)
- Landau damping is **beneficial** to maintain the beam quality, however the means to generate Landau damping can have a bad impact on the trajectories of single particles, leading to a **deterioration** of the beam quality



References

- [Chao] A. Chao, Theory of Collective Beam Instabilities in Accelerators (Wiley, New York, 1993)
- W. Herr, Introduction to Landau Damping in Proc. of CAS: Advanced Accelerator Physics, Trondheim, Norway, August 2013, CERN-2014-009 (CERN, Geneva, 2014), pp. 377-404
- [Micro] https://uspas.fnal.gov/materials/19Knoxville/lec%2010.pdf
- [Laclare] J.L. Laclare, Bunched beam coherent instabilities, in Proc. of CERN Accelerator School, Oxford, UK 16 27 Sep 1985, pp.264-326
- [Damerau] H. Damerau, Introduction to Non-linear Longitudinal Beam Dynamics, in Proc. of CERN Accelerator School (2019)
- [Octupole] Y.-M. Kim, NIM-A 950 (2020) 162971
- [Metral] E. Metral and F. Ruggiero, Stability diagrams for Landau damping with two-dimensional betatron tune spread from both octupoles and non-linear space-charge, CERN-AB-2004-025 (ABP)
- [Kornilov] V. Kornilov, Landau damping, CERN Accelerator School (2019)
- [Pieloni] T. Pieloni, PhD Thesis 4211, EPFL (2008)
- [Buffat] X. Buffat, et al., Phys. Rev. ST Accel. Beams 17, 111002 (2014)
- [Chao2] A. Chao, Lie Algebra Techniques for Nonlinear Dynamics, https://www.slac.stanford.edu/~achao/lecturenotes.html
- [RHIC] X. Gu, et al., Phys. Rev. Accel. Beams, 20, 023501 (2017)
- [elens] V. Shiltsev, et al., PRL **119**, 134802 (2017)
- [NLIO] V. Danilov and S. Nagaitsev, **13**, 084002 (2010)
- [IOTA] https://news.fnal.gov/2020/12/iota-octupole-channel/
- [McMillan] S. Nagaitsev, et al., 2021 JINST 16 P03047
- [Grudiev] A. Grudiev, Phys. Rev. ST Accel. Beams 17, 011001 (2014)
- [Schenk] M. Schenk, PhD Thesis 9298, EPFL (2019)
- [RFQ] K. Papke and A. Grudiev, Phys. Rev. Accel. Beams 20, 082001 (2014)