

# Universality of high- $p_T$ hadron suppression from radiative energy loss in AA collisions

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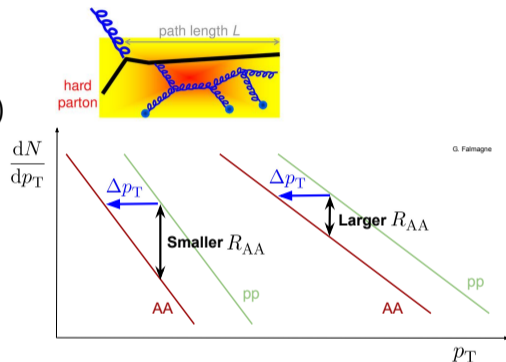


QGP France, Tours

May 3rd, 2022

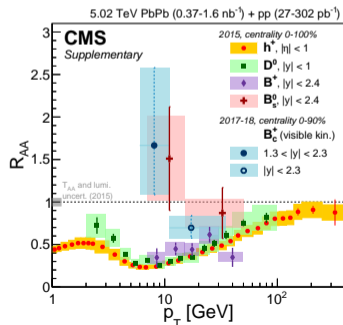
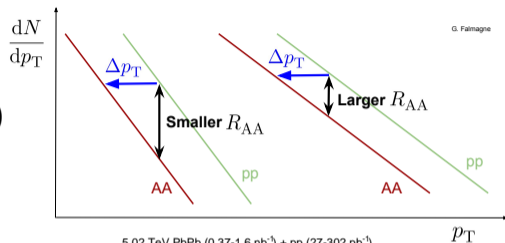
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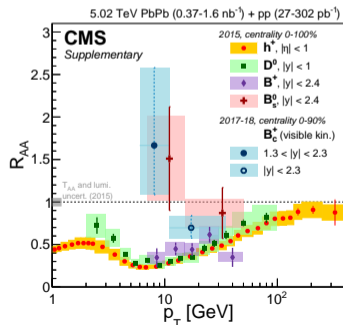
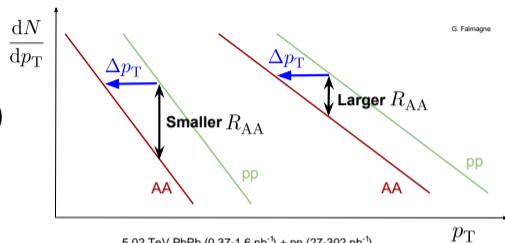
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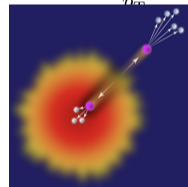
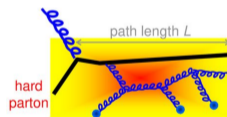
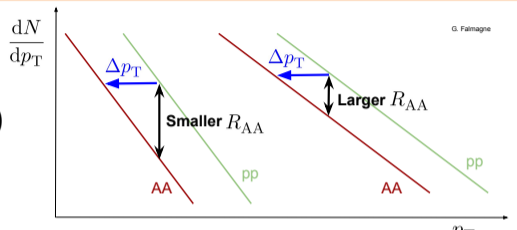
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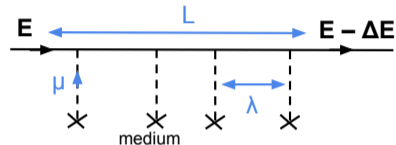
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- High- $p_T$  **hadron**  $\sim$  daughter of precursor **hard parton** traversing the QGP
- Quenching first studied with **hadrons** (RHIC), then **di-jet** asymmetry (RHIC+LHC)... but jets  $\neq$  partons (= particles)
  - Hadron 'simply' takes **momentum fraction**  $\langle z \rangle$  from parton → use hadron spectra



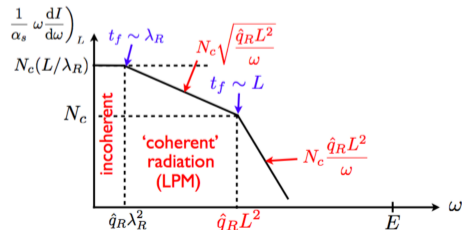
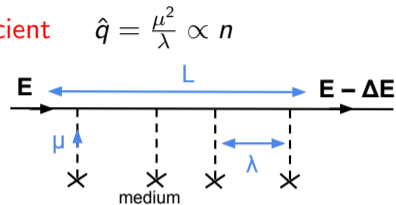
# BDMPS radiative energy loss

- QGP diffusion properties characterised by **transport coefficient**  $\hat{q} = \frac{\mu^2}{\lambda} \propto n$ 
  - Momentum kick in 1 rescattering: Debye mass  $\mu$
  - Mean free path between 2 scatterings:  $\lambda$
  - Total path length in the medium:  $L$



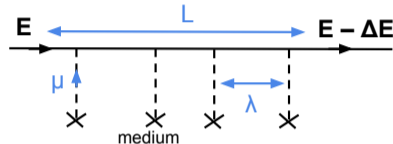
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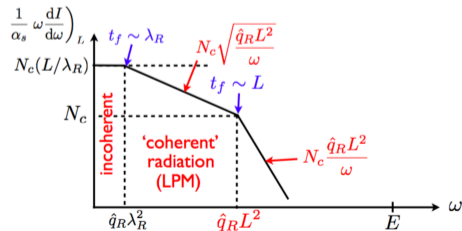
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- Integrating the energy spectrum of emitted gluons  
→ BDMPS **mean energy loss**:

$$\varepsilon \sim \frac{\alpha_S C_R}{4} \hat{q} L^2$$

- Hypotheses:  $\varepsilon \ll E$ , and  $L \gg \lambda$

→ = small fractional energy loss & large medium





# Hadron suppression from parton energy loss

- Model describing *only* BDMPS radiative energy loss of partons (Arleo, PRL119, 2017)
- Using quenching weight  $P(\varepsilon)$ :

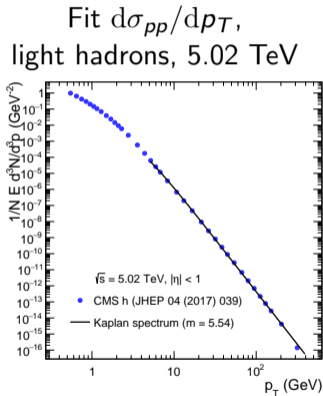
$$\frac{d\sigma_{AA}^{q/g}}{dp_T}(p_T) = A^2 \int d\varepsilon P(\varepsilon) \frac{d\sigma_{pp}^{q/g}}{dp_T}(p_T + \varepsilon)$$

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- Hadron takes fraction  $\langle z \rangle$  of parton momentum (smooth FF assumed)
- Scaleless  $\bar{P}$ , with free parameter  $\langle \varepsilon \rangle$ :  $P(\varepsilon) = \frac{1}{\langle \varepsilon \rangle} \bar{P}\left(\frac{\varepsilon}{\langle \varepsilon \rangle}\right)$
- Fit high- $p_T$  pp cross section  $d\sigma/dp_T \sim p_T^{-n}$  (depending on hadron species)



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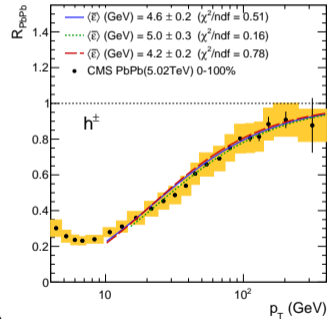
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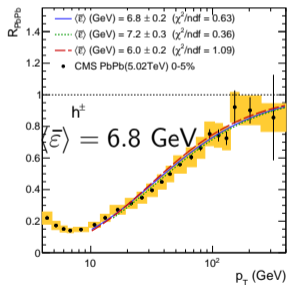
$$\rightarrow R_{AA}(p_T) = \int_0^\infty dx \frac{\bar{P}(x)}{\left(1 + x \frac{\langle z \rangle \langle \varepsilon \rangle}{p_T}\right)^n} \simeq \int_0^\infty dx \exp\left(-x n \frac{\langle z \rangle \langle \varepsilon \rangle}{p_T}\right) \bar{P}(x)$$

Fit  $R_{PbPb}(p_T)$ ,  
light hadrons

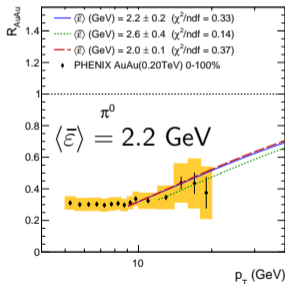


# Fits of $R_{AA}(p_T)$

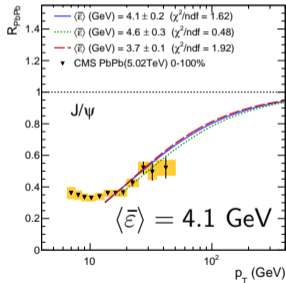
- Fit mean energy loss  $\langle \bar{\epsilon} \rangle = \langle z \rangle \langle \epsilon \rangle$  from many  $R_{AA}(p_T)$  measurements
- $p_T > 7$  to 13 GeV, depending on system (varied for **systematic** on  $\langle \bar{\epsilon} \rangle$ )
- $\langle \bar{\epsilon} \rangle$  uncertainties: from **correlated and uncorrelated** (vs  $p_T$  bins) measurement uncert.



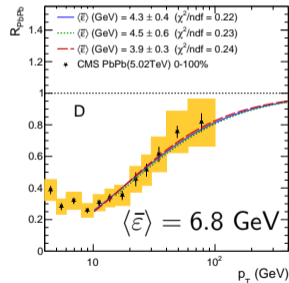
$h^\pm$  5.02 TeV  
0-5% centr.



$\pi^0$  RHIC  
AuAu 200 GeV



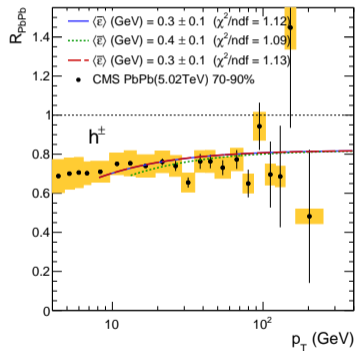
prompt  $J/\psi$   
5.02 TeV



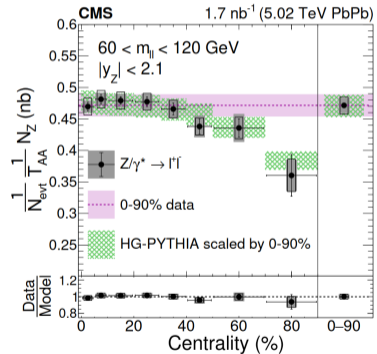
$D$   
5.02 TeV

# Bias in peripheral collisions

- Event-selection and **geometry bias** set forth by Loizides and Morsch (PLB773 (2017))
- Multiply the  $R_{AA}$  model by their correction factors, relevant for **centralities  $> 50\%$**



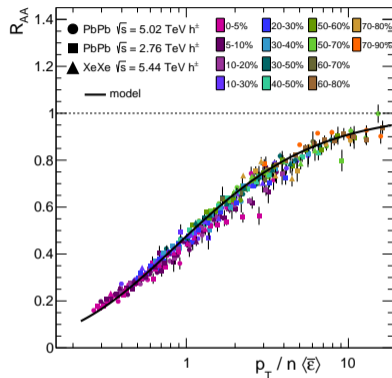
- Goes **up to 18% in 70-90%** centr. PbPb collisions



- Obvious in electroweak probes apparent suppression

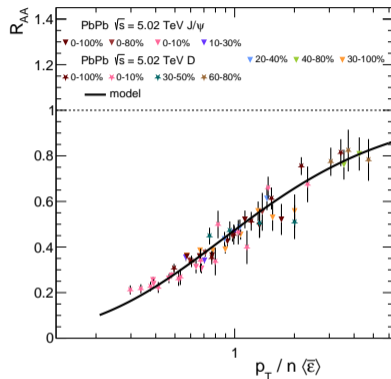
# Universal high- $p_T$ shape: $R_{AA}(p_T, \langle \bar{\epsilon} \rangle) \simeq R_{AA}(p_T / \langle \bar{\epsilon} \rangle)$

- 62 fits to measured  $R_{AA}(p_T)$ , all consistent with model at high  $p_T$ !
  - 3 particles: light hadrons (and  $\pi^0$ ),  $J/\psi$ ,  $D$
  - 4 energies: 0.2, 2.76, 5.02, 5.44 TeV
  - 4 experiments: CMS, ALICE, ATLAS, PHENIX
  - Many centrality classes + pp spectrum
- ➔ Scaling of  $R_{AA}(\text{hadrons})$  for  $p_T \gtrsim 8 - 10$  GeV



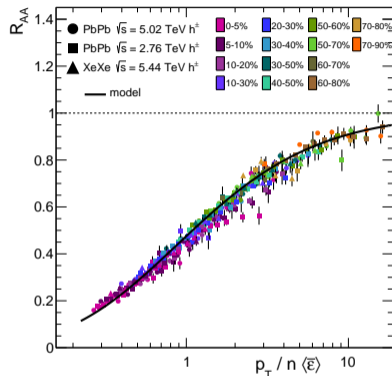
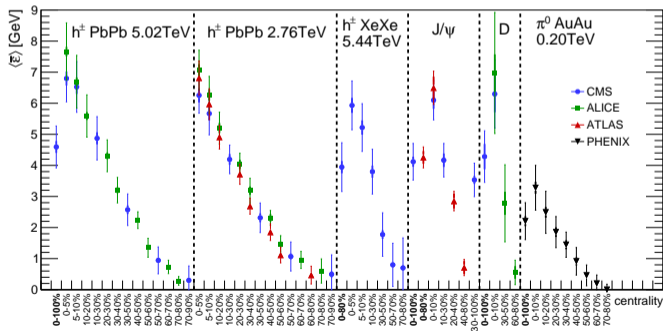
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- Fitted mean energy loss  $\langle \bar{\epsilon} \rangle$  is related to medium geometry ( $L$  and transverse area  $A_T$ ),  $\hat{q}$ , and expansion dynamics



# Energy loss vs medium geometry+density

- Salgado & Wiedemann [PRL89 \(2003\)](#) model the **decreasing medium density** with

$$\hat{q} \propto \hat{q}_0 \left( \frac{\tau_0}{\tau} \right)^\alpha$$

- $\hat{q}_0 \propto n \propto \left( \frac{dN_{ch}}{dy} \Big|_{y=0} \right) / A_\perp \tau_0$  (Bjorken estimate)
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- Equivalent transport coefficient in static medium:

$$\langle \hat{q} \rangle = \frac{2}{L^2} \int_{\tau_0}^{\tau_0+L} d\tau (\tau - \tau_0) \times \hat{q}_0 \left( \frac{\tau_0}{\tau} \right)^\alpha \simeq \frac{2}{2-\alpha} \hat{q}_0 \left( \frac{\tau_0}{L} \right)^\alpha$$

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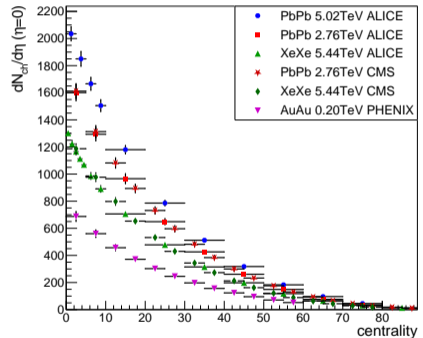
$$\rightarrow \varepsilon \propto \langle \hat{q} \rangle L^2 \propto \tau_0^{\alpha-1} \frac{\frac{dN_{ch}}{dy} \Big|_{y=0}}{A_T} \times L^{2-\alpha}$$

# Medium geometry and density

$$\varepsilon \propto \tau_0^{\alpha-1} \frac{\left. \frac{dN_{ch}}{dy} \right|_{y=0}}{A_T} \times L^{2-\alpha}$$

- **Multiplicities** from measurements

Multiplicity at central rapidity

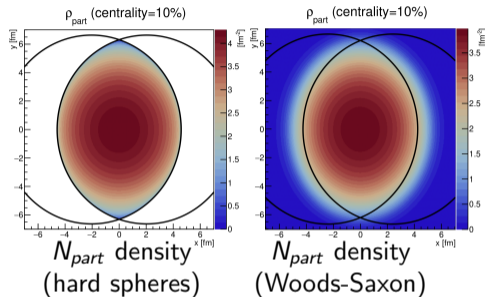


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- **Multiplicities** from measurements
- Path length  $L$  and area  $A_T$  through 4 Glauber models:
  - MC Glauber from  
Loizides, Kamin, d'Enterria, PRC97 (2018)
  - 1 pure hard sphere nuclei: **constant QGP density**, fully analytic
  - 2 **custom optical Glauber**: hard spheres or Woods-Saxon  
→  $L$  less straightforward there:

$$\langle L \rangle = \frac{\int L(\vec{s}, \phi) \rho_{coll} d\vec{s} d\phi}{2\pi \int \rho_{coll} d\vec{s}}$$

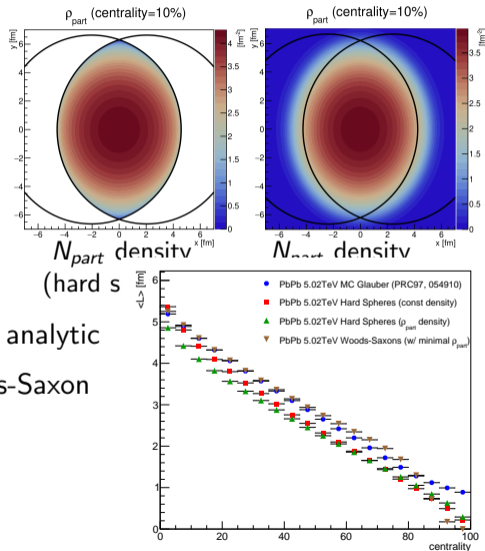


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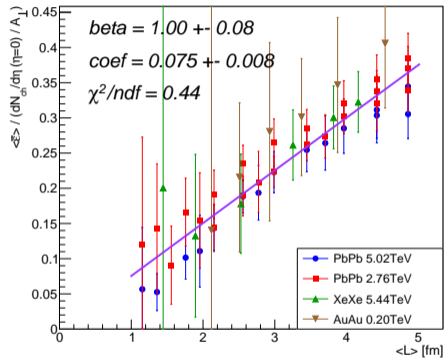
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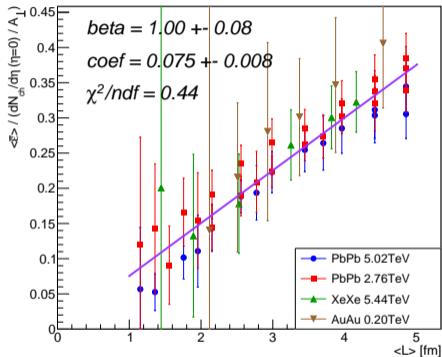
# Fitting energy loss VS medium geometry

Fit of  $\beta = 2 - \alpha$



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example of hard-spheres Glauber

small dispersion of  $\beta$  with  $\neq$  Glauber models

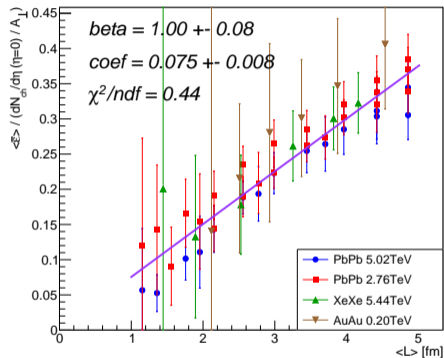
$\rightarrow \Delta\alpha = 0.03$

$\rightarrow$  Multiple systems scale!  $\rightarrow \alpha = 1.00 \pm 0.09$ , compatible with Bjorken expansion ( $\alpha = 1$ )

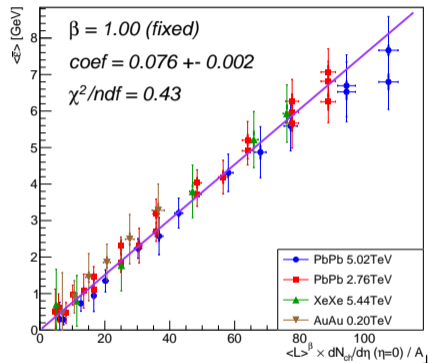


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Resulting energy loss scaling



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$$\langle z \rangle \langle \epsilon \rangle = (0.26 \pm 0.03) \frac{\alpha_S C_R}{2} \frac{dN_{ch}}{d\eta} \frac{\langle L \rangle^{1.00 \pm 0.09}}{A_T} \text{ [GeV]}$$

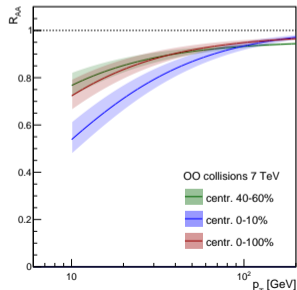
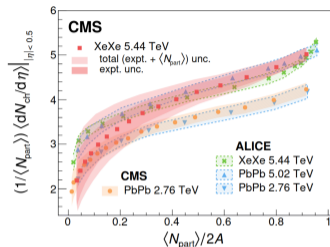
(no  $\tau_0$  dependence due to  $\alpha \simeq 1$ )

# Predictions of $R_{AA}(p_T)$ at high- $p_T$ in various systems

- Knowing  $dN_{\text{ch}}/d\eta$  + hypothesis on  $\langle z \rangle$  and  $C_R$   
 → can predict  $\langle \bar{\epsilon} \rangle$  in any system! → gives  $R_{AA}(p_T)$
- Uncertainty on  $\langle \bar{\epsilon} \rangle$  from fit (considering fully correlated energy loss values, overestimated for now)
- Calculations: ALICE  $R_{AA}(J/\psi)$  measurement in PbPb 5 TeV:
  - Similar  $C_R$  (gluon-dominated) and  $\langle z \rangle$  than  $h^\pm$  assumed + 20% uncertainty
  - Smaller multiplicity for  $2.5 < |\eta| < 4$  (+ uncertainty)

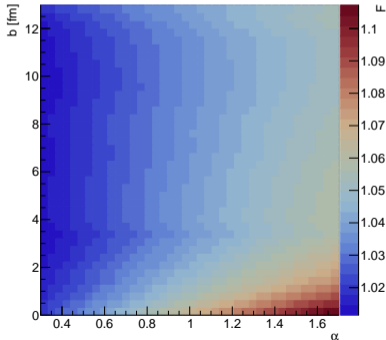
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- Predictions:  **$R_{AA}(h^\pm)$  in OO collisions at 7 TeV**
  - Multiplicity extrapolated from PbPb and XeXe measurements + 6% uncertainty
  - $L$  and  $A_T$  as in other systems
- pPb collisions? Formalism breaks, but predicts  $R_{pPb} \gtrsim 0.8 - 0.9$



# Checks of formalism

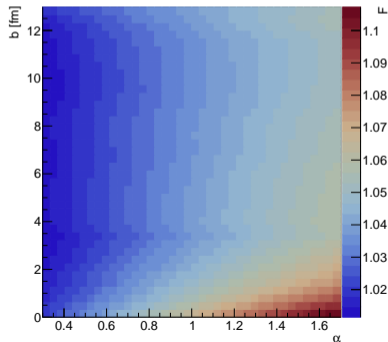
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→ Similar results from two models with hard spheres



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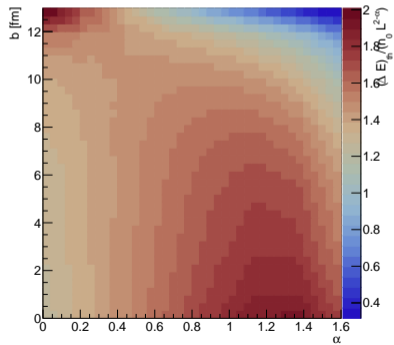
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→ Similar results from two models with hard spheres



- Model assumes same rules for **single-particle quantities VS average over active area and centrality**

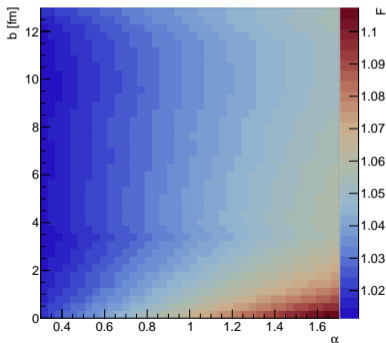
→ significant influence, to be studied



# Checks of formalism

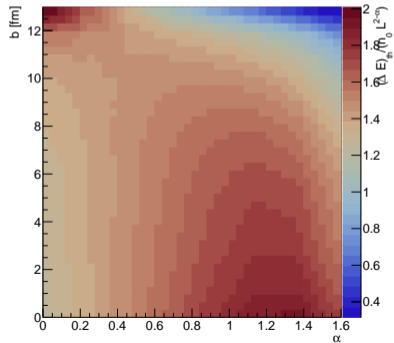
- Small influence of **inhomogeneity** on energy loss (constant VS  $N_{\text{part}}$  QGP density)

→ Similar results from two models with hard spheres



- Model assumes same rules for **single-particle quantities VS average over active area and centrality**

→ significant influence, to be studied



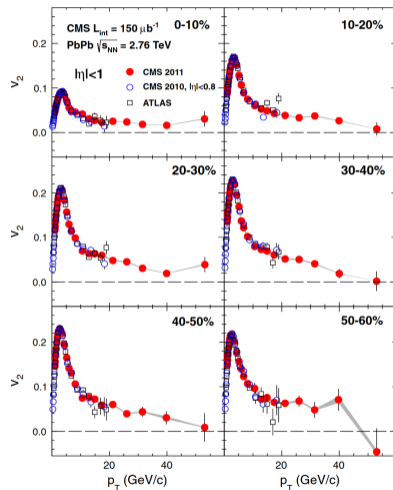
- Only one parton nature assumed now

→ possible small impact of **quark/gluon mix** on  $R_{AA}(p_T)$  scaling (to be checked)

- Influence of  $\log(E)$  corrections on  $R_{AA}(p_T)$  scaling?

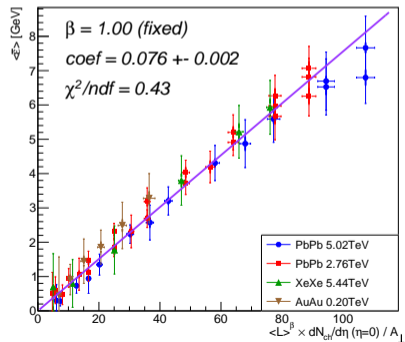
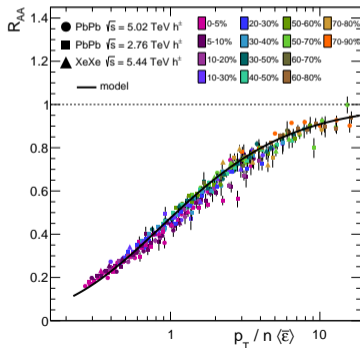
$v_2$ 

- $L$  depends on  $\varphi$   $\rightarrow$  path-length dependence of energy loss
- Formalism of custom Glauber model gives energy loss of particles produced at various  $\varphi$  angles
  - $\rightarrow$   $\varphi$  dependence of suppression from energy loss
  - $\rightarrow R_{AA}(\varphi)$
  - $\rightarrow$  Possible to predict  $v_2$  of hadrons at  $p_T \gtrsim 10$  GeV (to be done)
- Convergence of  $v_2$  for all species at high  $p_T$ ?



# Conclusion

- Universal  $R_{AA}(p_T)$  behaviour of hadrons from radiative energy loss
- Extracted energy loss values scale  $\propto$  variable describing medium density and geometry  
 $\rightarrow$  Path length dependence  $\langle \varepsilon \rangle \propto \langle L \rangle^1$  consistent with Bjorken (longitudinal) expansion
- All measured systems (PbPb, XeXe, AuAu, 0.2 to 5 TeV) consistent with both scalings





**BACKUP**

# List of measurements

Particle	System	$\sqrt{s_{NN}}$	experiment	already in Ref. [2]?	pp fit and centrality classes	Kinematic range
Light charged hadrons $h^\pm$	PbPb	2.76 TeV	CMS	yes	pp, 0-5%, 5-10%, 10-30%, 30-50%, 50-70%, 70-90%	$ \eta  < 1$ , $p_\perp < 103$ GeV
			ATLAS	no	0-5%, 5-10%, 10-20%, 20-30%, 30-40%, 40-50%, 50-60%, 60-80%	$ \eta  < 2$ , from $p_\perp < 95$ GeV to $p_\perp < 150$ GeV
		ALICE	no	0-5%, 5-10%, 10-20%, 20-30%, 30-40%, 40-50%, 50-60%, 60-70%, 70-80%	$ \eta  < 0.8$ , $p_\perp < 50$ GeV	
	XeXe	5.44 TeV	ALICE	no	0-5%, 5-10%, 10-20%, 20-30%, 30-40%, 40-50%, 50-60%, 60-70%, 70-80%	$ \eta  < 0.8$ , $p_\perp < 50$ GeV
			CMS	yes	pp, 0-5%, 5-10%, 10-30%, 30-50%, 50-70%, 70-90%, 0-100%	$ \eta  < 1$ , $p_\perp < 400$ GeV (250 GeV for centr.> 70%)
$\pi^0$	AuAu	0.20 TeV	PHENIX	no	pp	$ y  < 0.35$ , $p_\perp < 25$ GeV
					0-10%, 10-20%, 20-30%, 30-40%, 40-50%, 50-60%	$ y  < 0.35$ , $p_\perp < 20$ GeV
$D^0$	PbPb	5.02 TeV	CMS	yes (except pp)	pp, 0-10%, 0-100%	$ y  < 1$ , $p_\perp < 100$ GeV
			ALICE	no	0-10%, 30-50%, 60-80%	$ y  < 0.5$ , $p_\perp < 50$ GeV (35 GeV for centr.> 50%)
$J/\psi$	PbPb	5.02 TeV	CMS	no (except 0-100%)	pp, 0-10%, 10-30%, 30-100%, 0-100%	$ y  < 2.4$ , $p_\perp < 30$ GeV (50 GeV for centr. 0-100%)
			ATLAS	no	0-10%, 20-40%, 40-80%, 0-80%	$ y  < 2$ , $p_\perp < 40$ GeV

# Energy loss in proton-lead collisions?

- The geometric formalism developed for the  $\varepsilon \propto \frac{dN_{ch}}{dy} \Big|_{y=0} \times L^\beta$  scaling might not be transferable to p-Pb collisions (and the hypothesis  $\Delta E \ll E$  breaks)
- However, taking the numerical values from the scaling to measurements, and these ingredients:
  - path length  $\langle L \rangle \sim r_0 \simeq 1$  fm
  - transverse area  $\langle A_T \rangle = \pi r_0^2 \simeq \pi(1 \text{ fm})^2$
  - Measured average multiplicity  $\sim 22$  in p-Pb collisions at 8.16 TeV
  - $\langle z \rangle \langle \varepsilon \rangle = 0.5$  GeV
  - Similar to energy loss in PbPb 5.02 TeV at centralities 60-80%
  - $R_{pA} \simeq 0.8 - 0.9$  at  $p_T = 10$  GeV
  - Comparable or smaller than cold nuclear matter effects (and formalism might not be valid)