

# Supersymmetric Left-Right models and low energy phenomenology

Avelino Vicente  
Universität Würzburg

Based on work in collaboration with  
J. Esteves, M. Hirsch, W. Porod, J. Romão and F. Staub  
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## Introduction

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- Motivation
- Left vs Right

## The model

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Lepton Flavor Violation  
in SUSY Left-Right  
models

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Summary and  
conclusions

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# Introduction

## Motivation

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- The extension must account for the **smallness of neutrino masses**

→ **Seesaw mechanism**

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- And lead to **new predictions!**

→ Seesaw: Indirect tests

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- The extension must account for the **smallness of neutrino masses**

→ Seesaw mechanism

- And lead to **new predictions!**

→ Seesaw: Indirect tests

But let us keep in mind that . . .

In addition to neutrino masses, the Standard Model has some open theoretical questions that need to be addressed. The most popular solution to these problems is **Supersymmetry**.

→ R-parity . . . conservation?

## Motivation

**R-parity** is usually introduced **by hand**, without any theoretical argument supporting it.

**Idea:** R-parity is the remnant subgroup after the breaking of a continuous  $U(1)_{B-L}$  gauge symmetry

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**Idea:** R-parity is the remnant subgroup after the breaking of a continuous  $U(1)_{B-L}$  gauge symmetry

- **Left-Right symmetry** :  $SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ 
  - ★ Restoration of parity at high energies
  - ★ Natural framework for the seesaw mechanism  $\rightarrow$  neutrino masses
  - ★ Provides technical solutions to SUSY and strong CP problems
  - ★ Gives an understanding for the  $U(1)$  charges
  - ★ Can be easily embedded in  $SO(10)$  GUTs



## Basic setup

In SUSY models, **Lepton flavor violation** is a good **indirect test** of physics at high energies.

- Flavor diagonal soft terms at the GUT scale
  - ★ mSUGRA boundary conditions :  $m_L^2 = m_E^2 = m_0^2 \mathcal{I}_3$
  
- RGE running from GUT to SUSY/EW scale
  - ★ Leptons couple to heavy fields with flavor violating couplings
  - ★ RGE running induces LFV
  - ★ Off-diagonal entries in  $m_L^2$  and  $m_E^2$  at the SUSY/EW scale
  - ★ Lepton flavor violating signatures
  
- After the heavy fields decouple no more LFV is induced
  - ★ Indirect hint of the intermediate scales

## Left vs Right

In minimal seesaw models LFV is generated **only for the left-handed sleptons**.

- ★ **Example:** Type-I seesaw.  $e^c$  only couples through the flavor diagonal charged lepton Yukawa  $Y_e$ .
- ★ No chances to observe LFV in the **right slepton sector**.

However, in a LR extended version of the seesaw,  $L^c = (e^c, \nu^c)$  couples exactly like the left-handed doublet  $L = (\nu, e)$ .

Introduction

**The model**

- How to break the LR symmetry

Lepton Flavor Violation in SUSY Left-Right models

Summary and conclusions

# The model

## How to break the LR symmetry

$$\mathbf{SU(3)}_c \times \mathbf{SU(2)}_L \times \mathbf{SU(2)}_R \times \mathbf{U(1)}_{B-L}$$



$$\mathbf{SU(3)}_c \times \mathbf{SU(2)}_L \times \mathbf{U(1)}_Y$$

Requirements:

- Automatic conservation of R-parity
- Seesaw mechanism
- Parity conservation at high energies
- Cancellation of anomalies

# Omega LR

Aulakh *et al*, Phys. Rev. Lett. 79, 2188 (1997)

Aulakh *et al*, Phys. Rev. D 58, 115007 (1998)

Besides the usual MSSM representations:

	$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)_{B-L}$	
$\Delta$	1	3	1	2	
$\Delta^c$	1	1	3	-2	$\Rightarrow f L^c \Delta^c L^c$
$\bar{\Delta}$	1	3	1	-2	$\Downarrow$
$\bar{\Delta}^c$	1	1	3	2	$f \nu_{BL} \nu^c \nu^c$
$\Omega$	1	3	1	0	RH neutrinos mass
$\Omega^c$	1	1	3	0	<b>Seesaw mechanism</b>

The  $B - L = 0$  triplets have important contributions to the **tree-level scalar potential**, allowing for **R-parity conservation**, without the necessity of higher order corrections (Kuchimanchi, Mohapatra, 1993 and Babu, Mohapatra, 2008).

# Symmetry breaking

$$\mathbf{SU(2)}_{\mathbf{R}} \times \mathbf{U(1)}_{\mathbf{B-L}}$$



$$\langle \Omega^c \rangle = \frac{v_R}{\sqrt{2}}$$

**Parity breaking scale**

$$\mathbf{U(1)}_{\mathbf{R}} \times \mathbf{U(1)}_{\mathbf{B-L}}$$



$$\langle \Delta^c \rangle = \langle \bar{\Delta}^c \rangle = \frac{v_{BL}}{\sqrt{2}}$$

**Seesaw scale**

$$\mathbf{U(1)}_{\mathbf{Y}}$$

Introduction

The model

**Lepton Flavor Violation  
in SUSY Left-Right  
models**

- Left vs Right
- $\mu^+ \rightarrow e^+ \gamma$ :  
Positron polarization  
asymmetry
- Other signatures

Summary and  
conclusions

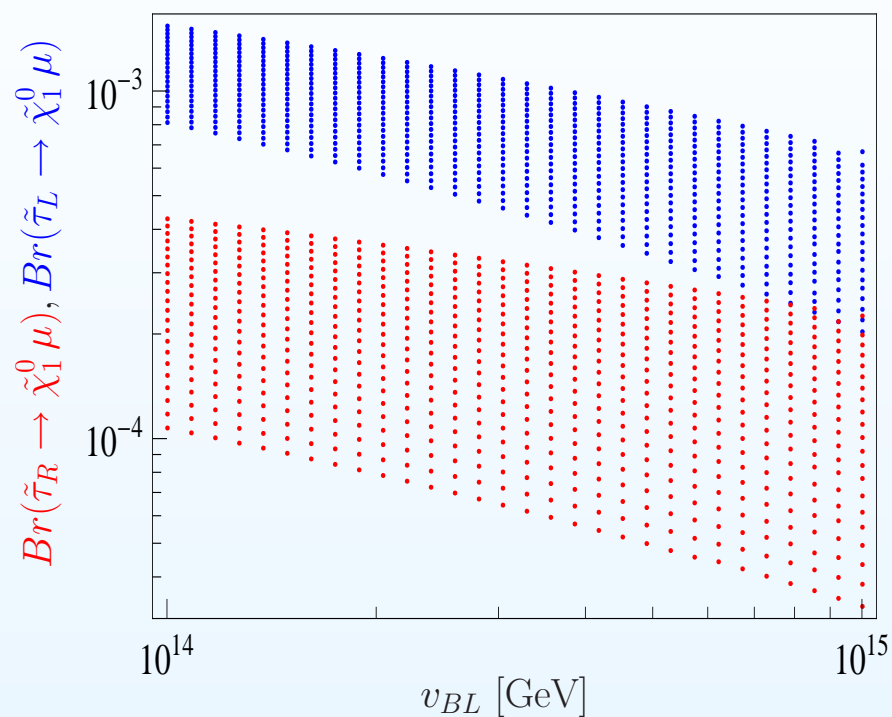
# Lepton Flavor Violation in SUSY Left-Right models

## Left vs Right

SPS3 benchmark point

$Y_\nu$  fit

$$M_S = 10^{13} \text{ GeV}, v_R \in [10^{15}, 5 \cdot 10^{15}] \text{ GeV}$$



- There are regions of parameter space with observable rates for LFV in the right-handed slepton sector
- Closer  $v_{BL} - v_R$  implies closer  $Br(\tilde{\tau}_L) - Br(\tilde{\tau}_R)$
- Is it possible to determine the ratio  $v_{BL}/v_R$ ?

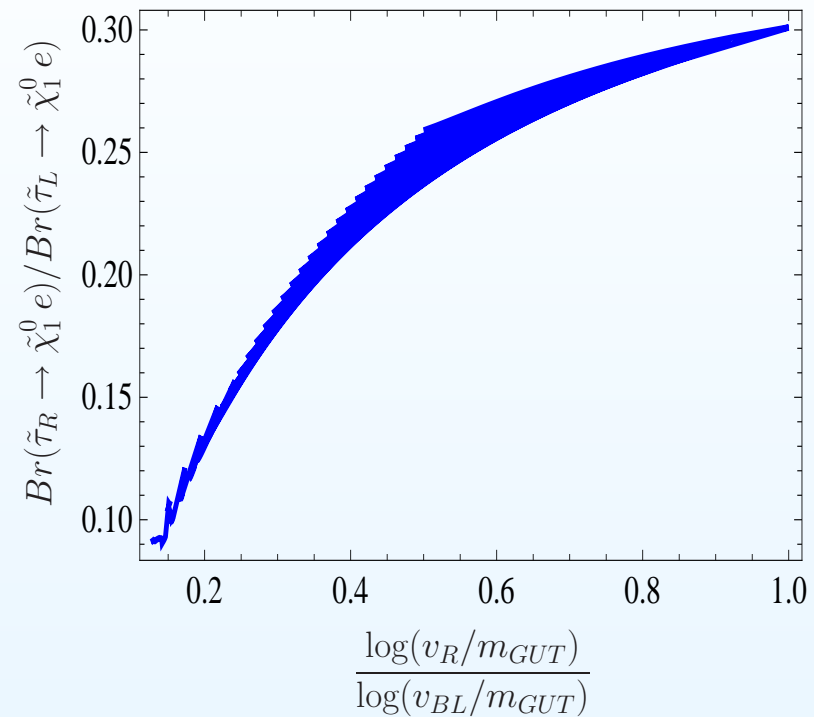
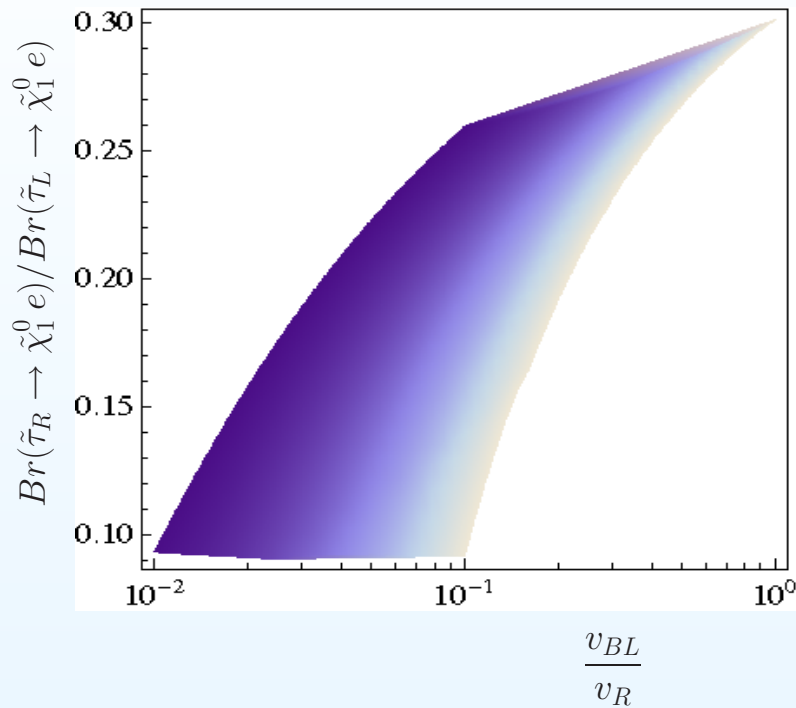


## Left vs Right

SPS3 benchmark point

$Y_\nu$  fit

$$M_S = 10^{13} \text{ GeV}, v_{BL} \in [10^{14}, 10^{15}] \text{ GeV}, v_R \in [10^{15}, 10^{16}] \text{ GeV}$$



- By measuring **left- and right-handed LFV** the ratio  $v_{BL}/v_R$  can be constrained
- However, there is a slight dependence on  $M_S$  and  $m_{GUT}$
- More information (e.g. other LFV decays) is required

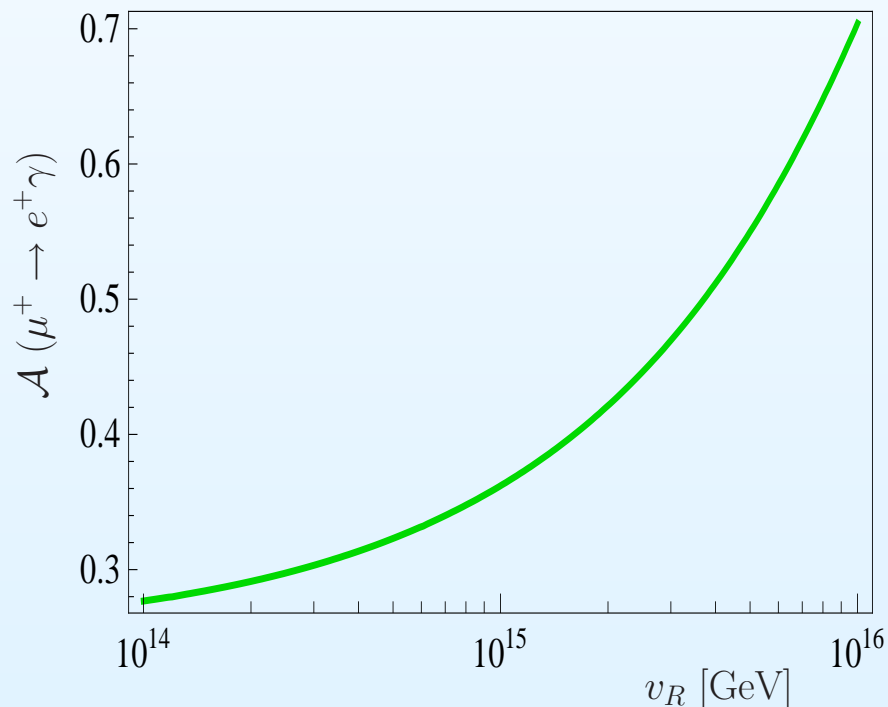
## $\mu^+ \rightarrow e^+ \gamma$ : Positron polarization asymmetry

$$\mathcal{L}_{eff} = e \frac{m_i}{2} \bar{l}_i \sigma_{\mu\nu} F^{\mu\nu} (A_L^{ij} P_L + A_R^{ij} P_R) l_j + h.c.$$

### Positron polarization asymmetry

$$\mathcal{A}(\mu^+ \rightarrow e^+ \gamma) = \frac{|A_L|^2 - |A_R|^2}{|A_L|^2 + |A_R|^2}$$

SPS3 benchmark point,  $Y_\nu$  fit,  $v_{BL} = 10^{14}$  GeV



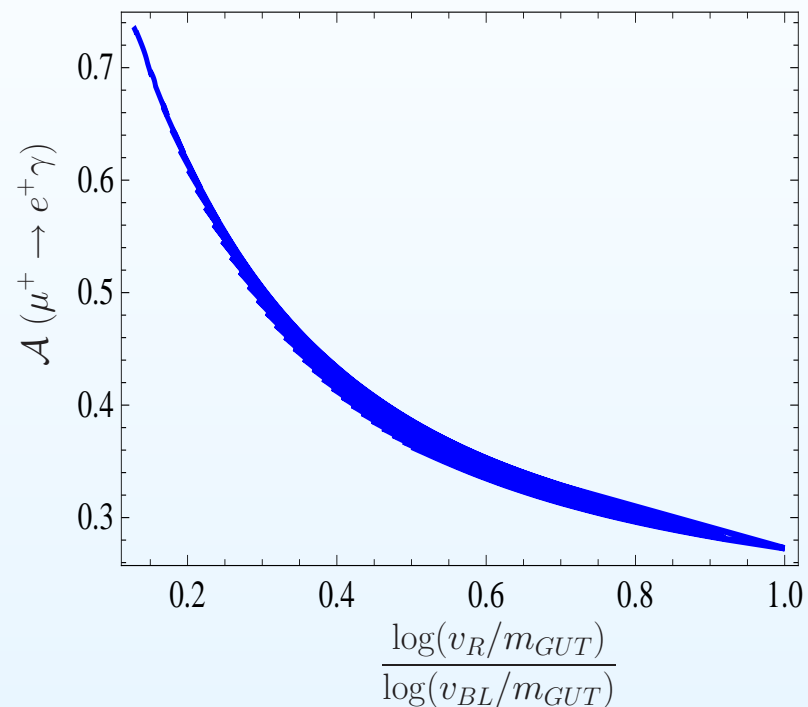
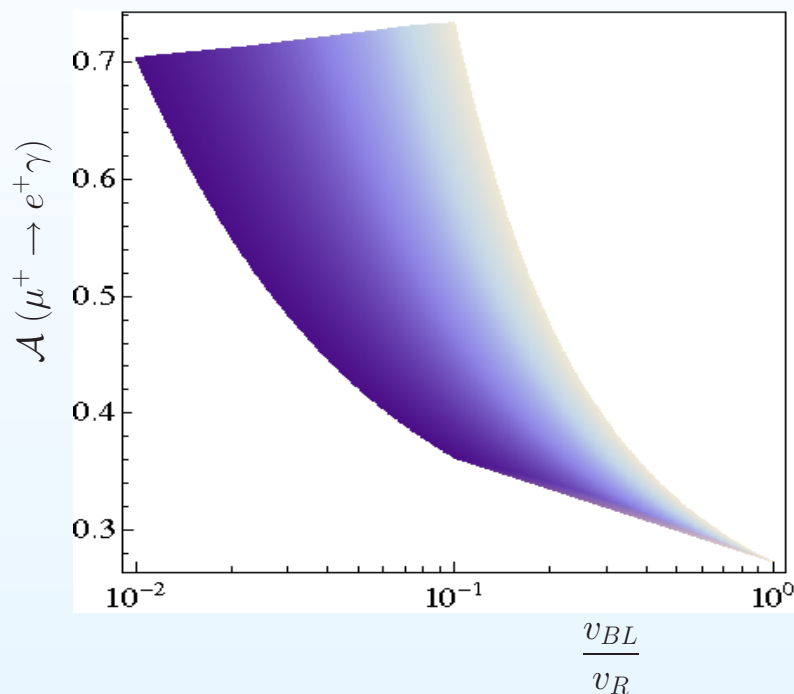
- In minimal seesaw models  $\mathcal{A} \simeq 1$  is expected
- In this case large departures from  $\mathcal{A} = 1$  can be found
- This observable is very sensitive to the high energy scales

## Left vs Right

SPS3 benchmark point

$Y_\nu$  fit

$$M_S = 10^{13} \text{ GeV}, v_{BL} \in [10^{14}, 10^{15}] \text{ GeV}, v_R \in [10^{15}, 10^{16}] \text{ GeV}$$



- The polarization asymmetry is strongly dependent on the ratio  $v_{BL}/v_R$
- Again, there is a slight dependence on  $M_S$  and  $m_{GUT}$

## Other signatures

Other things to look at:

- Impact on the SUSY spectrum
  - ★ Main changes from the standard expectation
  - ★ Invariant sparticle mass combinations
- Dark matter relic density
- Other low-energy lepton flavor violating processes  
( $\mu \rightarrow 3e \dots$ )
- CP Violation and flavor physics

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Summary and  
conclusions

# Summary and conclusions

## Summary

- ★ SUSY Left-Right models are well motivated extensions of the MSSM, with automatic R-parity conservation and seesaw mechanism.
- ★ Assuming flavor blind soft terms at the GUT scale, lepton flavor violating entries are generated at the SUSY scale due to RGE running. This makes LFV a window to the high energy scales.
- ★ Contrary to minimal seesaw implementations, there are regions of parameter space where LFV is also observable in the R sector. Such observation would clearly point to an underlying Left-Right symmetry.
- ★ In addition, by comparing LFV in L and R sectors one can constrain the ratio  $v_{BL}/v_R$ , providing valuable information about the symmetry breaking pattern.
- ★ Many distinctive features not present in the standard mSUGRA scenarios. More observables to study!

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Backup slides

**Backup slides**

## Neutrino data

Parameter	Best fit	$2\sigma$	$3\sigma$
$\Delta m_{21}^2$ [ $10^{-5}\text{eV}^2$ ]	$7.59^{+0.23}_{-0.18}$	7.22–8.03	7.02–8.27
$ \Delta m_{31}^2 $ [ $10^{-3}\text{eV}^2$ ]	$2.40^{+0.12}_{-0.11}$	2.18–2.64	2.07–2.75
$\sin^2 \theta_{12}$	$0.318^{+0.019}_{-0.016}$	0.29–0.36	0.27–0.38
$\sin^2 \theta_{23}$	$0.50^{+0.07}_{-0.06}$	0.39–0.63	0.36–0.67
$\sin^2 \theta_{13}$	$0.013^{+0.013}_{-0.009}$	$\leq 0.039$	$\leq 0.053$

Taken from Schwetz *et al*, New J. Phys. 10 (2008) 113011 [*arXiv:0808.2016v3*]

- Hierarchy between atmospheric and solar mass scales
- Two large mixing angles
- One small (maybe zero?) mixing angle



## CMSSM benchmark points

Point	$m_0$	$M_{1/2}$	$A_0$	$\tan \beta$	$sign(\mu)$
SPS1a'	70 GeV	250 GeV	-300 GeV	10	+
SPS3	90 GeV	400 GeV	0 GeV	10	+
SPS4	400 GeV	300 GeV	0 GeV	50	+
SPS5	150 GeV	300 GeV	-1000 GeV	5	+
SU4	200 GeV	160 GeV	-400 GeV	10	+
Om1	280 GeV	250 GeV	-500 GeV	10	+
LM1	60 GeV	250 GeV	0 GeV	10	+

## LR models - Case 1: Doublet models

R. N. Mohapatra and G. Senjanovic, Phys. Rev. D 12, 1502 (1975)

In the **first LR models** doublets were chosen to break the LR symmetry.

	$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)_{B-L}$
$\chi$	1	2	1	1
$\chi^c$	1	1	2	-1

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**However ...**

- R-parity gets broken unless additional discrete symmetries are imposed by hand
- There is no seesaw mechanism

## LR models - Case 2: MSUSYLR

M. Cvetič and J. C. Pati, Phys. Lett. 135, 57 (1984)

The so-called **Minimal SUSY Left-Right** (MSUSYLR) model breaks the LR symmetry with **triplets** instead of doublets.

	$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)_{B-L}$
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RH neutrinos mass  
**Seesaw mechanism**

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					RH neutrinos mass
					<b>Seesaw mechanism</b>

**However ...**

- A detailed analysis of the scalar potential shows that **R-parity gets broken by  $\langle \tilde{\nu}^c \rangle \neq 0$** . Kuchimanchi, Mohapatra, PRD 48, 4352 (1993).  
 → This is **controversial** : 1-loop corrections must be taken very seriously.

## Omega LR: Superpotential and soft terms

$$\begin{aligned}
 \mathcal{W} &= Y_Q Q \Phi Q^c + Y_L L \Phi L^c - \frac{\mu}{2} \Phi \Phi + f L \Delta L + f^* L^c \Delta^c L^c \\
 &+ a \Delta \Omega \bar{\Delta} + a^* \Delta^c \Omega^c \bar{\Delta}^c + \alpha \Omega \Phi \Phi + \alpha^* \Omega^c \Phi \Phi \\
 &+ M_\Delta \Delta \bar{\Delta} + M_\Delta^* \Delta^c \bar{\Delta}^c + M_\Omega \Omega \Omega + M_\Omega^* \Omega^c \Omega^c
 \end{aligned}$$

$$\begin{aligned}
 -\mathcal{L}_{soft} &= m_Q^2 \tilde{Q}^\dagger \tilde{Q} + m_{Q^c}^2 \tilde{Q}^{c\dagger} \tilde{Q}^c + m_L^2 \tilde{L}^\dagger \tilde{L} + m_{L^c}^2 \tilde{L}^{c\dagger} \tilde{L}^c \\
 &+ m_\Delta^2 \Delta^\dagger \Delta + m_{\Delta}^2 \bar{\Delta}^\dagger \bar{\Delta} + m_{\Delta^c}^2 \Delta^{c\dagger} \Delta^c + m_{\Delta^c}^2 \bar{\Delta}^{c\dagger} \bar{\Delta}^c \\
 &+ m_\Phi^2 \Phi^\dagger \Phi + m_\Omega^2 \Omega^\dagger \Omega + m_{\Omega^c}^2 \Omega^{c\dagger} \Omega^c \\
 &+ \frac{1}{2} [M_1 \tilde{B}^0 \tilde{B}^0 + M_2 (\tilde{W}_L \tilde{W}_L + \tilde{W}_R \tilde{W}_R) + M_3 \tilde{g} \tilde{g} + h.c.] \\
 &+ [T_Q \tilde{Q} \Phi \tilde{Q}^c + T_L \tilde{L} \Phi \tilde{L}^c + T_f \tilde{L} \Delta \tilde{L} + T_f^* \tilde{L}^c \Delta^c \tilde{L}^c + T_a \Delta \Omega \bar{\Delta} \\
 &+ T_a^* \Delta^c \Omega^c \bar{\Delta}^c + T_\alpha \Omega \Phi \Phi + T_\alpha^* \Omega^c \Phi \Phi + B_\mu \Phi \Phi \\
 &+ B_{M_\Delta} \Delta \bar{\Delta} + B_{M_\Delta}^* \Delta^c \bar{\Delta}^c + B_{M_\Omega} \Omega \Omega + B_{M_\Omega}^* \Omega^c \Omega^c + h.c.]
 \end{aligned}$$

## A comment on bidoublets

In LR models the MSSM Higgses are introduced as **bidoublets**

$$\Phi = \begin{bmatrix} H_d^0 & H_u^+ \\ H_d^- & H_u^0 \end{bmatrix} : (2, 2, 0) \text{ under } SU(2)_L \times SU(2)_R \times U(1)_{B-L}$$

However, at least **two bidoublets** are needed to produce a non-trivial  $V_{CKM}$  at tree-level.

$$Y_Q^{(i)} Q \Phi_i Q^c \Rightarrow \text{The misalignment } Y_Q^{(1)} - Y_Q^{(2)} \text{ generates } V_{CKM}$$

At the  $v_R$  scale one of these two bidoublets decouples while the orthogonal combination leads to the MSSM two Higgs doublets. Therefore, the **low-energy Yukawa parameters** are rotations of the original ones. In the leptonic sector:

$$\begin{aligned} Y_e &= Y_L^1 \cos \theta_1 - Y_L^2 \sin \theta_1 \\ Y_\nu &= -Y_L^1 \cos \theta_2 + Y_L^2 \sin \theta_2 \end{aligned}$$



# Renormalization Group Equations

- From the GUT scale to the  $v_R$  scale

$$\begin{aligned}
 16\pi^2 \frac{d}{dt} m_L^2 &= 6 f f^\dagger m_L^2 + 12 f m_L^2 f^\dagger + 6 m_L^2 f f^\dagger + 12 m_{\Delta}^2 f f^\dagger \\
 &+ 2 Y_L^{(k)} Y_L^{(k)\dagger} m_L^2 + 2 m_L^2 Y_L^{(k)} Y_L^{(k)\dagger} + 4 Y_L^{(k)} m_{L^c}^2 Y_L^{(k)\dagger} \\
 &+ 4 (m_{\Phi}^2)_{mn} Y_L^{(m)} Y_L^{(n)\dagger} + 12 T_f T_f^\dagger + 4 T_L^{(k)} T_L^{(k)\dagger} \\
 &- (3g_{BL}^2 |M_1|^2 + 6g_2^2 |M_2|^2 + \frac{3}{2} g_{BL}^2 S_1) \mathcal{I}_3
 \end{aligned}$$

$$\begin{aligned}
 16\pi^2 \frac{d}{dt} m_{L^c}^2 &= 6 f^\dagger f m_{L^c}^2 + 12 f^\dagger m_{L^c}^2 f + 6 m_{L^c}^2 f^\dagger f + 12 m_{\Delta^c}^2 f^\dagger f \\
 &+ 2 Y_L^{(k)\dagger} Y_L^{(k)} m_{L^c}^2 + 2 m_{L^c}^2 Y_L^{(k)\dagger} Y_L^{(k)} + 4 Y_L^{(k)\dagger} m_L^2 Y_L^{(k)} \\
 &+ 4 (m_{\Phi}^2)_{mn} Y_L^{(m)\dagger} Y_L^{(n)} + 12 T_f^\dagger T_f + 4 T_L^{(k)\dagger} T_L^{(k)} \\
 &- (3g_{BL}^2 |M_1|^2 + 6g_2^2 |M_2|^2 - \frac{3}{2} g_{BL}^2 S_1) \mathcal{I}_3
 \end{aligned}$$

# Renormalization Group Equations

- From the  $v_R$  scale to the  $v_{BL}$  scale

$$\begin{aligned}
 16\pi^2 \frac{d}{dt} m_L^2 &= 2Y_e m_{\tilde{e}^c}^2 Y_e^\dagger + 2m_{H_d}^2 Y_e Y_e^\dagger + 2m_{H_u}^2 Y_\nu Y_\nu^\dagger + m_L^2 Y_e Y_e^\dagger \\
 &+ Y_e Y_e^\dagger m_L^2 + m_L^2 Y_\nu Y_\nu^\dagger + Y_\nu Y_\nu^\dagger m_L^2 + 2Y_\nu m_{\tilde{\nu}^c}^2 Y_\nu^\dagger \\
 &+ 2T_e T_e^\dagger + 2T_\nu T_\nu^\dagger - (3g_{BL}^2 |M_1|^2 + 6g_L^2 |M_L|^2 + \frac{3}{4}g_{BL}^2 S_2) \mathcal{I}_3
 \end{aligned}$$

$$\begin{aligned}
 16\pi^2 \frac{d}{dt} m_{\tilde{e}^c}^2 &= 2Y_e^\dagger Y_e m_{\tilde{e}^c}^2 + 2m_{\tilde{e}^c}^2 Y_e^\dagger Y_e + 4m_{H_d}^2 Y_e^\dagger Y_e + 4Y_e^\dagger m_L^2 Y_e \\
 &+ 4T_e^\dagger T_e - (3g_{BL}^2 |M_1|^2 + 2g_R^2 |M_R|^2 - \frac{3}{4}g_{BL}^2 S_2 - \frac{1}{2}g_R^2 S_3) \mathcal{I}_3
 \end{aligned}$$

## RGEs: Approximated expressions

- **From the GUT scale to the  $v_R$  scale**

$$\Delta m_L^2 = -\frac{1}{4\pi^2} \left( 3ff^\dagger + Y_L^{(k)} Y_L^{(k)\dagger} \right) (3m_0^2 + A_0^2) \ln \left( \frac{m_{GUT}}{v_R} \right)$$

$$\Delta m_{Lc}^2 = -\frac{1}{4\pi^2} \left( 3f^\dagger f + Y_L^{(k)\dagger} Y_L^{(k)} \right) (3m_0^2 + A_0^2) \ln \left( \frac{m_{GUT}}{v_R} \right)$$

- **From the  $v_R$  scale to the  $v_{BL}$  scale**

$$\Delta m_L^2 \sim -\frac{1}{8\pi^2} Y_\nu Y_\nu^\dagger (3m_L^2|_{v_R} + A_e^2|_{v_R}) \ln \left( \frac{v_R}{v_{BL}} \right)$$

$$\Delta m_{ec}^2 \sim 0$$

## Basic setup

J. N. Esteves, M. Hirsch, J.C. Romão, W. Porod, F. Staub and A. Vicente  
JHEP 12, 077 (2010)

- mSUGRA boundary conditions
- 2-loop RGEs

- ★ Analytical computation with *Sarah*

F. Staub, Comput. Phys. Commun. 181, 1077 (2010)

- ★ Numerical implementation with *SPheno*

W. Porod, Comput. Phys. Commun. 153, 275 (2003)

- Threshold corrections at intermediate scales
- Two types of fit to neutrino oscillation parameters
  - ★  $Y_\nu$  fit : Flavor in  $Y_\nu LH_u \nu^c \supset Y_L L \Phi L^c$
  - ★  $f$  fit : Flavor in  $f L \Delta L$

## Left vs Right: types of fit

$Y_\nu$  fit

f fit

**GUT scale** :  $m_L^2 = m_E^2 = m_0^2 \mathcal{I}_3$



**$\nu_R$  scale** :  $m_L^2 = m_E^2$   
**due to parity conservation**  
off-diagonal  $m_E^2$  stop running



**$\nu_{BL}$  scale** :  $m_L^2 \neq m_E^2$   
off-diagonal  $m_L^2$  stop running



**SUSY scale** :  $m_L^2 \neq m_E^2$

**GUT scale** :  $m_L^2 = m_E^2 = m_0^2 \mathcal{I}_3$



**$\nu_R$  scale** :  $m_L^2 = m_E^2$   
**due to parity conservation**  
off-diagonal  $m_E^2$  and  $m_L^2$  stop running



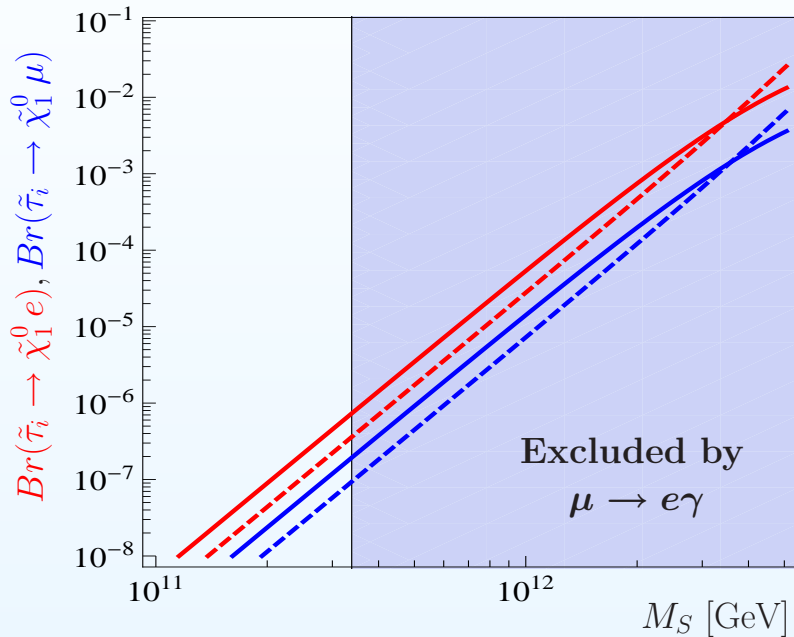
**SUSY scale** :  $m_L^2 \neq m_E^2$

- ★ Large LFV entries in both sectors.
- ★ In case of the  $Y_\nu$  fit, the L-R difference is sensitive to the  $\nu_{BL} - \nu_R$  difference.

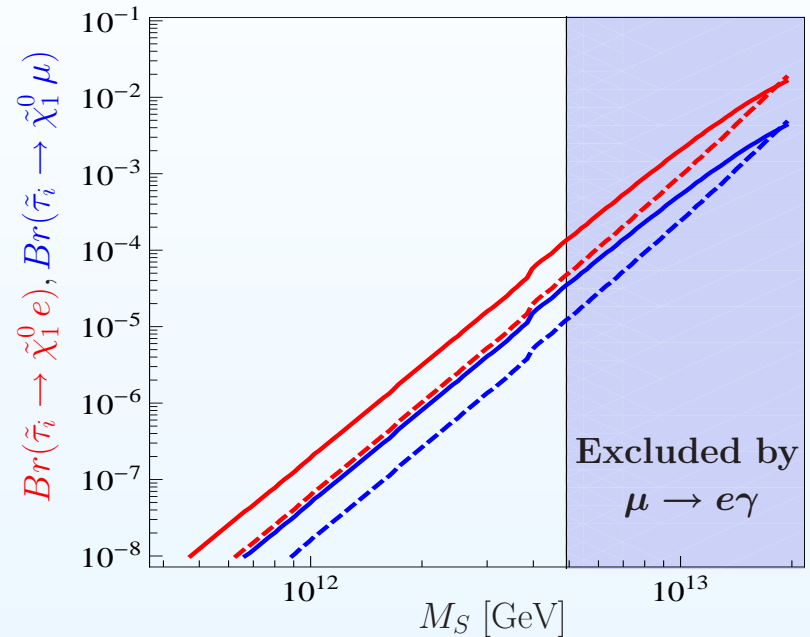
# Seesaw scale determination

$$v_{BL} = 10^{15} \text{ GeV}, v_R = 5 \cdot 10^{15} \text{ GeV} \quad Y_\nu \text{ fit}$$

SPS1a'



SPS3



$$m_\nu = -\frac{v_u^2}{2} Y_\nu^T \cdot M_R^{-1} \cdot Y_\nu$$

The absolute value of LFV BR's is linked to the Seesaw scale.

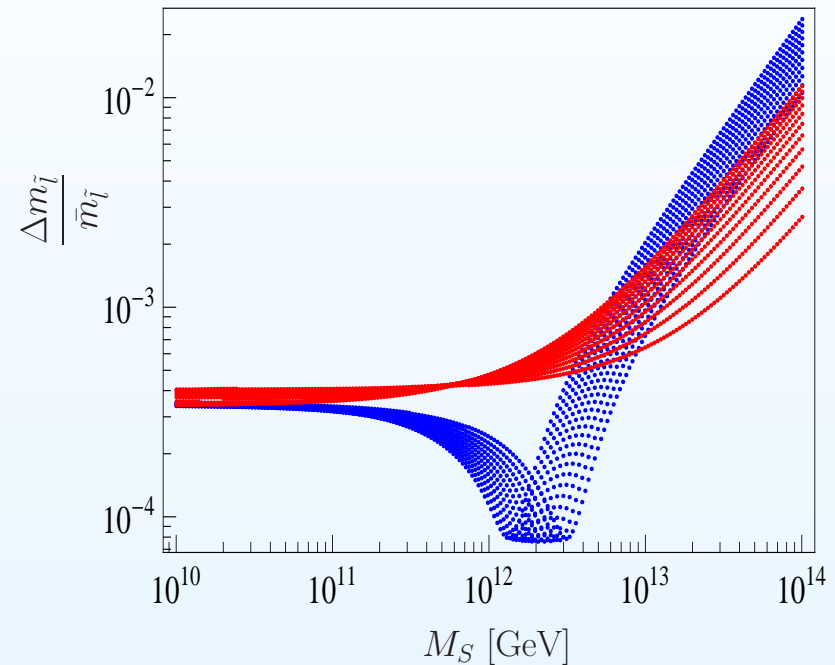
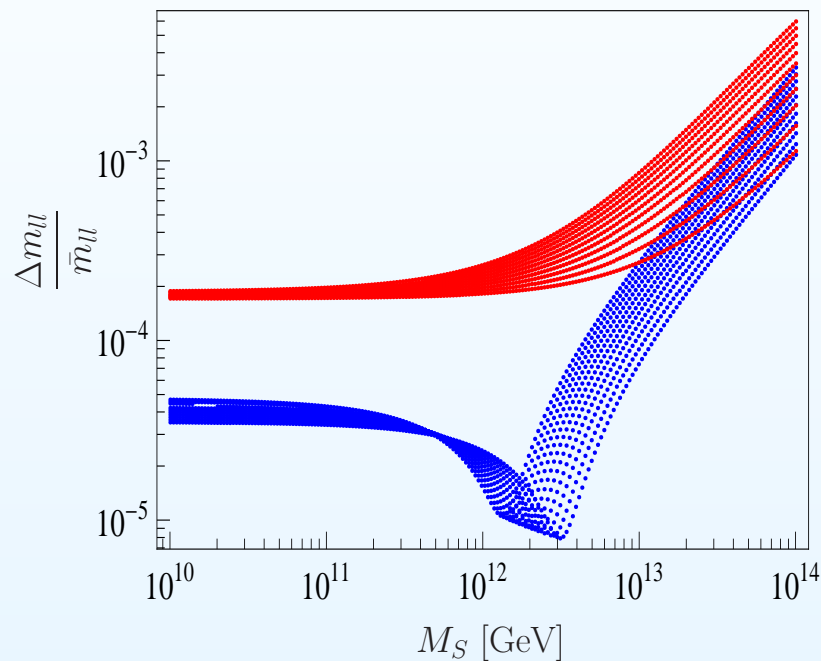
# $\tilde{e} - \tilde{\mu}$ mass splitting

SPS3 benchmark point

$Y_\nu$  fit

$v_{BL} = 10^{15}$  GeV,  $v_R \in [10^{15}, 10^{16}]$  GeV

$$\tilde{\chi}_2^0 \rightarrow \tilde{l}^\pm l^\mp \rightarrow \tilde{\chi}_1^0 l^\pm l^\mp$$



- Sizeable splittings  $m_{\tilde{e}} - m_{\tilde{\mu}}$  are produced by RGE running in the **L** and **R** sectors.
- Sensitivities around  $10^{-4}$  can be reached at the LHC for both observables (Allanach et al. PRD 77 (2008) 076006).
- Deviations from the mSUGRA prediction ( $m_{\tilde{e}} \simeq m_{\tilde{\mu}}$ ) are measurable.

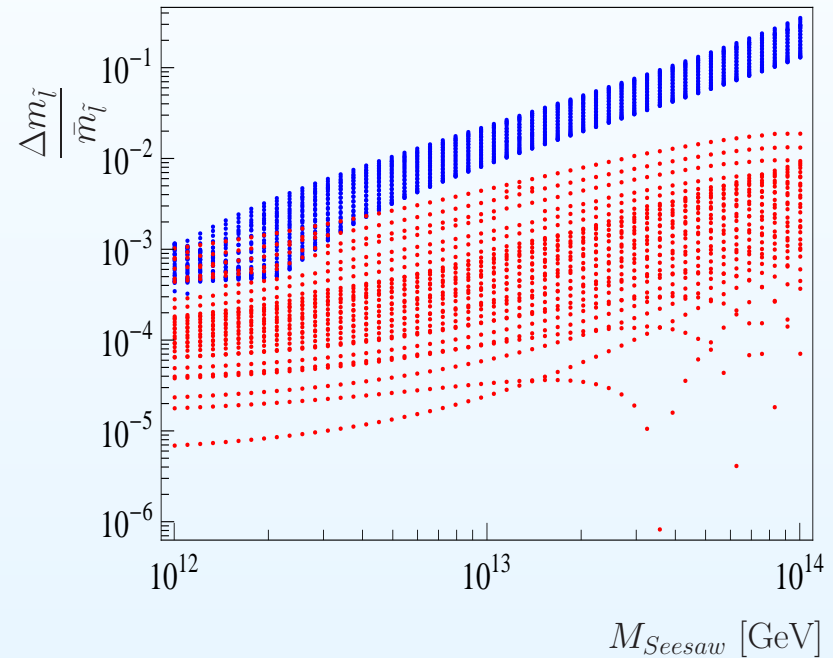
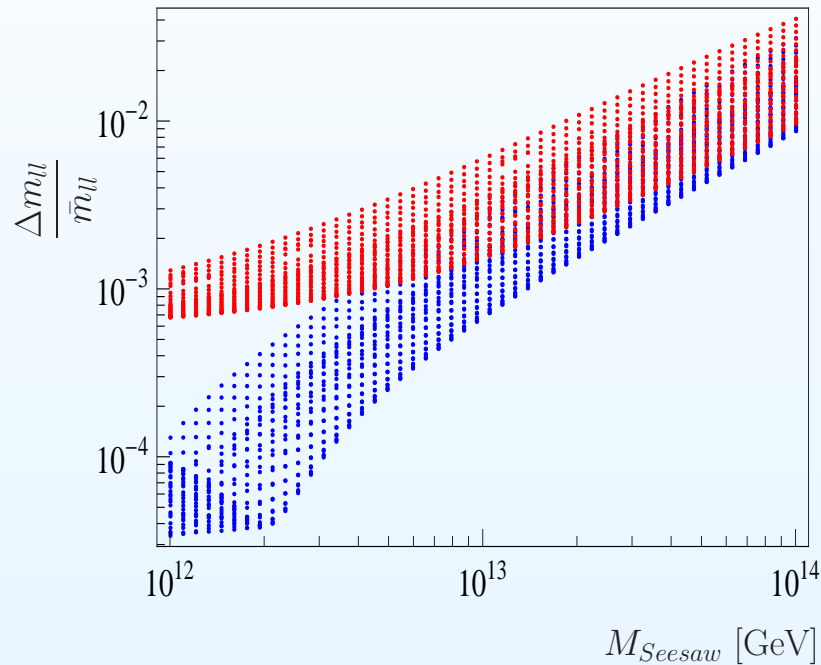
# $\tilde{e} - \tilde{\mu}$ mass splitting

SPS1a' benchmark point

$Y_\nu$  fit

$$v_{BL} = 10^{15} \text{ GeV}, v_R \in [10^{15}, 10^{16}] \text{ GeV}$$

$$\tilde{\chi}_2^0 \rightarrow \tilde{l}^\pm l^\mp \rightarrow \tilde{\chi}_1^0 l^\pm l^\mp$$

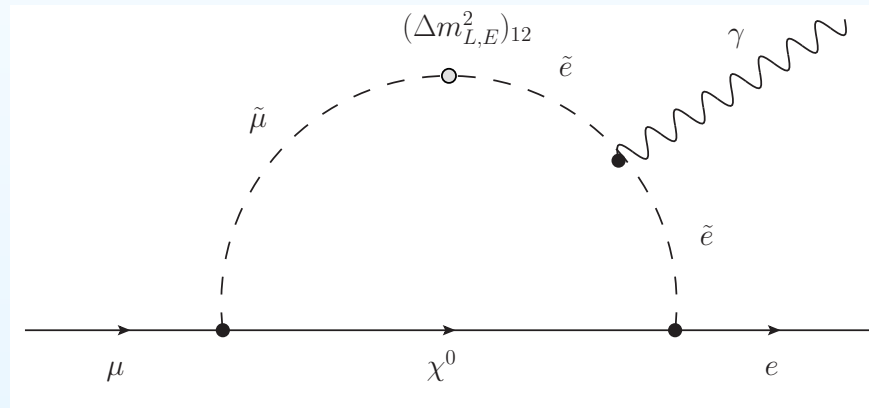
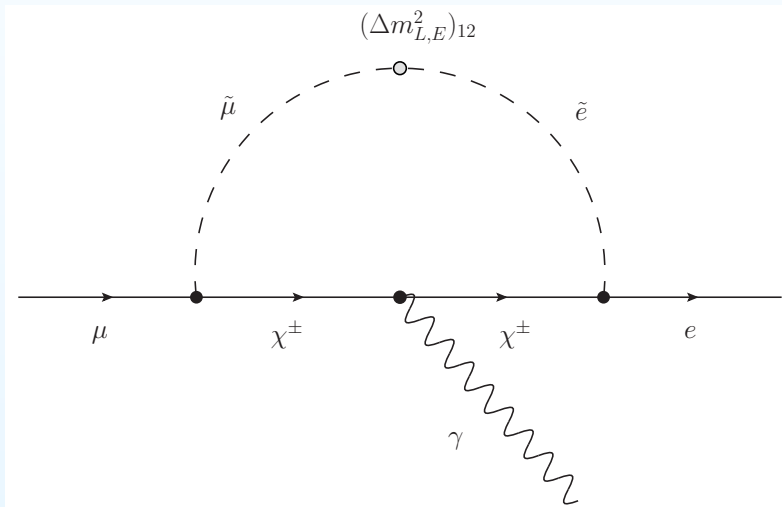


Large splittings  $m_{\tilde{e}} - m_{\tilde{\mu}}$  are produced by RGE running in the **L** and **R** sectors.



$$\underline{l_i \rightarrow l_j \gamma}$$

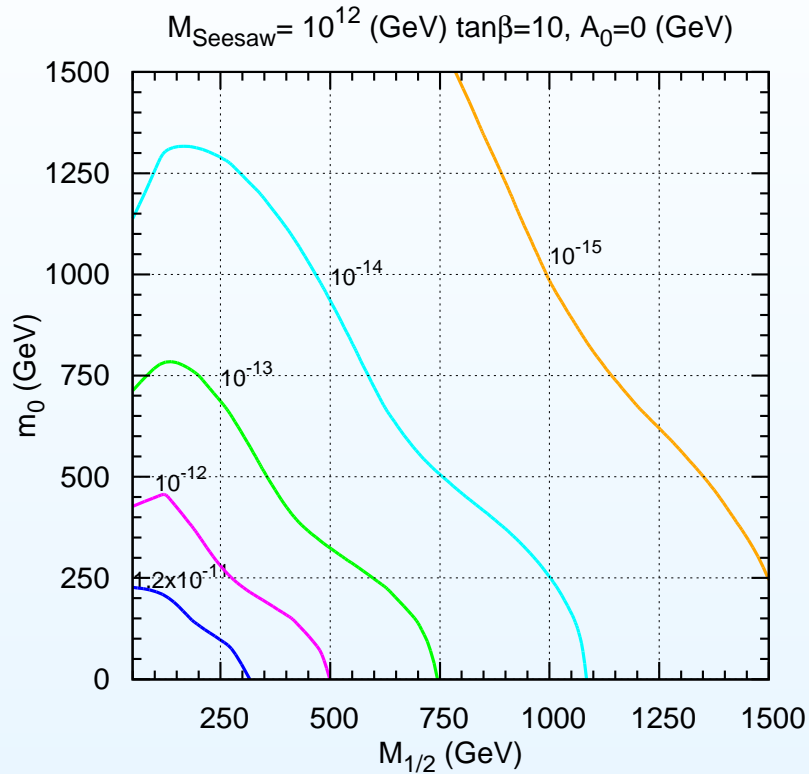
$l_i \rightarrow l_j \gamma$  processes are enhanced by **off-diagonal  $\Delta m_L^2$  and  $\Delta m_E^2$** . For example, in the case of  $\mu \rightarrow e \gamma$ :



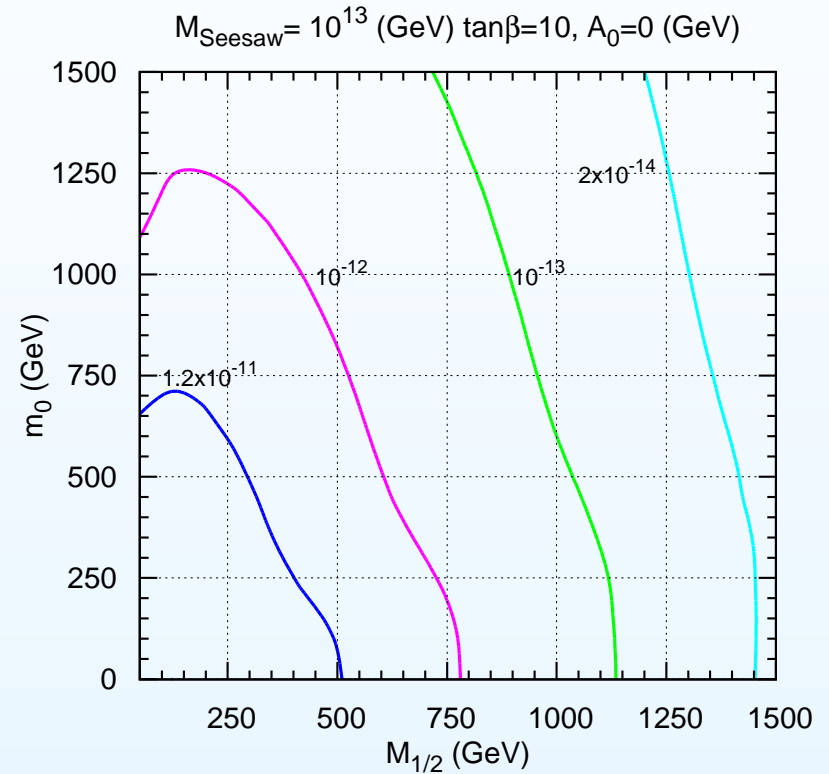
$$Br(\mu \rightarrow e \gamma) \propto \Delta(m_{L,E}^2)_{12}^2$$

$$\underline{l_i \rightarrow l_j \gamma}$$

$$\mu \rightarrow e \gamma$$



$$M_{\text{Seesaw}} = 10^{12} \text{ GeV}$$



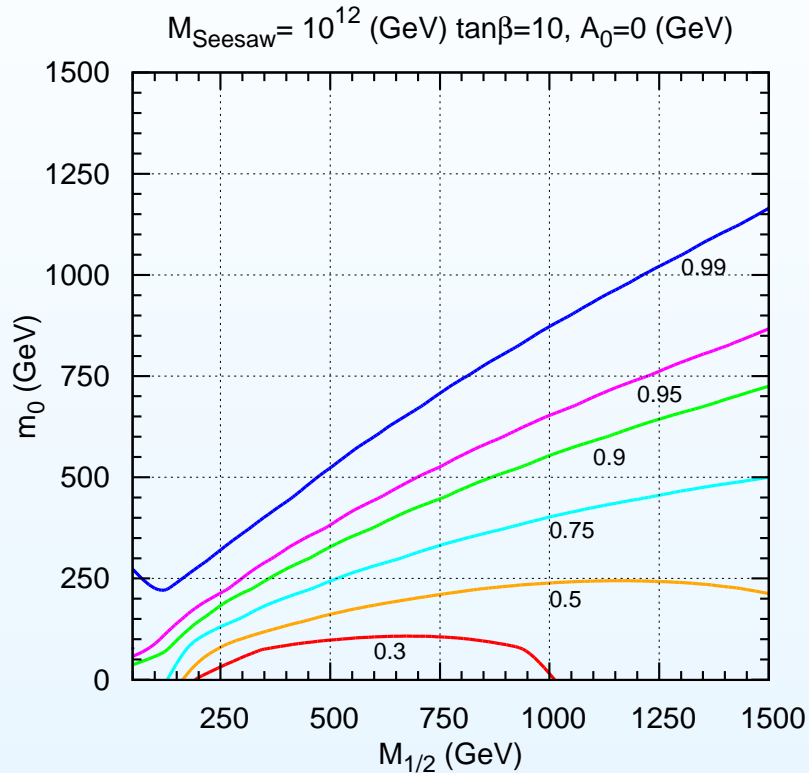
$$M_{\text{Seesaw}} = 10^{13} \text{ GeV}$$

Non-negligible right-handed contribution

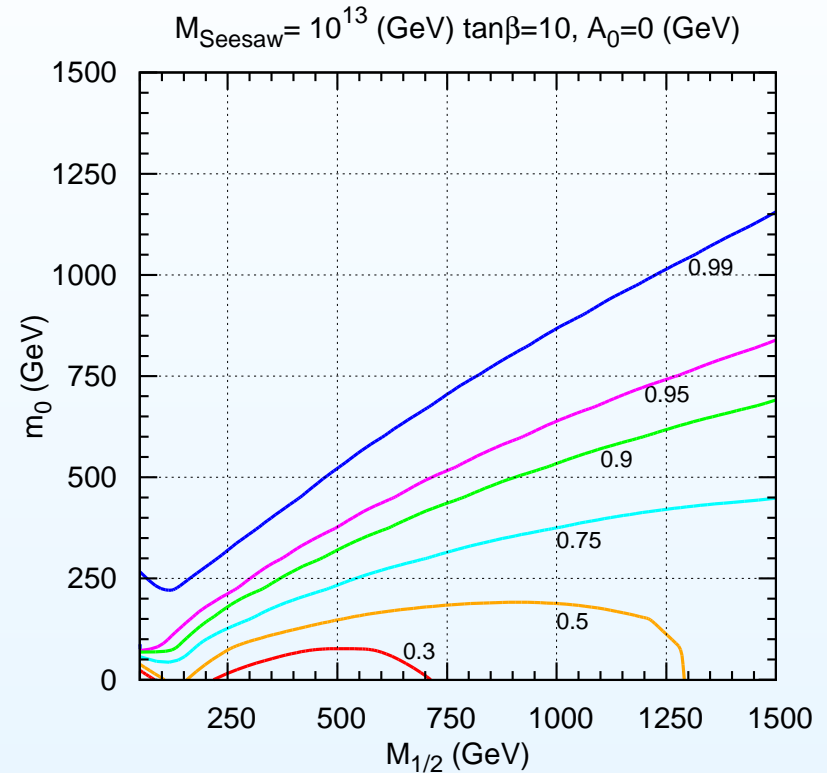
$\Rightarrow$  Larger Br's w.r.t. standard seesaw

$$\underline{\mathcal{A}(\mu^+ \rightarrow e^+ \gamma)}$$

$$\mathcal{A}(\mu^+ \rightarrow e^+ \gamma)$$



$$M_{\text{Seesaw}} = 10^{12} \text{ GeV}$$



$$M_{\text{Seesaw}} = 10^{13} \text{ GeV}$$

Strong dependence on  $m_0$  due to slepton masses

- Large  $m_0$ : Comparable **L** and **R** slepton masses, LFV in the **L** sector dominates
- Small  $m_0$ : Lighter **R** sleptons compensate the additional LFV in the **L** sector

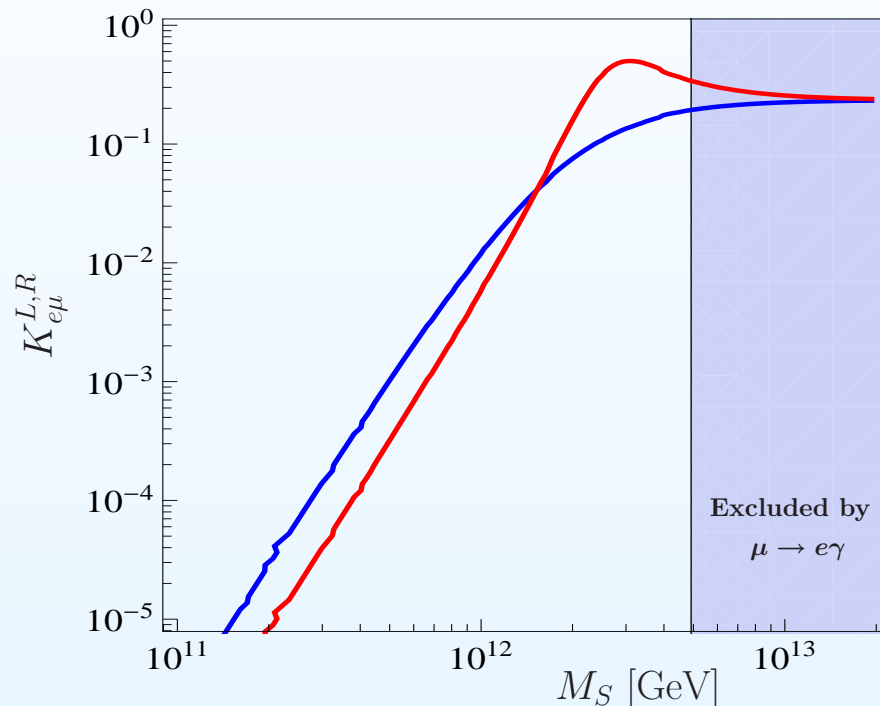
# $\tilde{\chi}_2^0$ decays and LFV

SPS3 benchmark point

$f$  fit

$$v_{BL} = 10^{15} \text{ GeV}, v_R = 5 \cdot 10^{15} \text{ GeV}$$

$$\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 l_i l_j \text{ with } i \neq j$$



$K_{e\mu}$  defined as

$$\frac{Br(\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 e\mu)}{Br(\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 ee) + Br(\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \mu\mu)}$$

If the intermediate L and R sleptons are on-shell (as in SPS3) one can distinguish between  $K_{e\mu}^L$  and  $K_{e\mu}^R$  and find LFV in both sectors

This signal can be discovered at the LHC if  $K_{e\mu} \geq 0.04$

See Andreev et al., Phys. Atom. Nucl. 70 (2007) 1717