# Discovering Technicolor

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\* Sannino et al. '11, arXiv:1104.1255

CP<sup>3</sup> - Origins

Particle Physics & Origin of Mass

Planck 2011, Lisbon

### QCD & Dynamical EWSB

In QCD at  $\Lambda_{QCD}$  the interaction becomes strong and the quarks form a bound state with non-zero vev:

$$\langle 0 | \bar{u}_L u_R + \bar{d}_L d_R | 0 \rangle \neq 0, \ T_L^3 + Y_L = Y_R = Q \Rightarrow SU(2)_L \times U(1)_Y \to U(1)_{EM}$$

By redefining currents in terms of composite peudo-scalars (pions) one finds that the EW bosons acquire masses:

$$M_W^{QCD} = g f_{\pi^{\pm}}/2, \ \rho = \frac{M_W^{QCD}}{M_Z^{QCD}} \cos^{-1}(\theta_W) = 1.$$

Given the experimental value for the pion decay constant

$$f_{\pi} = 93 \,\mathrm{MeV} \quad \Rightarrow \quad M_W^{QCD} = 29 \,\mathrm{MeV!}$$

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#### Technicolor

The effective Lagrangian expansion breaks down at

$$\Lambda_{QCD} \simeq 4\pi f_{\pi} = 1.2 \,\text{GeV} \Rightarrow \Lambda_{TC} \simeq 4\pi v = 3 \,\text{TeV}, \ v = 246 \,\text{GeV}.$$

A Technicolor (TC) model able to give the right masses to the EW gauge bosons is simply "scaled up" QCD (no fundamental scalar  $\Rightarrow$  no fine-tuning!):

$$SU(N)_{TC} \times SU(3)_C \times SU(2)_L \times U(1)_Y$$
.

To generate the fermion masses an Extended Technicolor (ETC) interaction is necessary.

\* Susskind '79

#### Extended Technicolor

If the ETC gauge group gets broken at some large scale  $\Lambda_{ETC}\gg\Lambda_{TC}$ , the massive ETC gauge bosons can be integrated out.

Four fermion interactions, technifermion condensate ⇒ SM mass terms

The lowest ETC scale is determined by the heaviest mass:

$$m_t = 173 \text{ GeV} \approx \frac{\Lambda_{TC}^3}{\Lambda_{ETC}^2} \Rightarrow \Lambda_{ETC} \simeq 10 \text{ TeV}$$

Flavor changing neutral currents bounds though require  $\Lambda_{ETC}\gtrsim 10^3~{
m TeV}\dots$ 

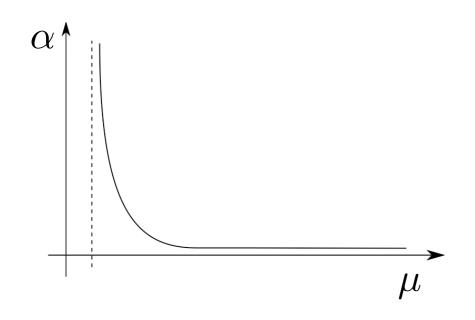
#### Fermion Mass Renormalization

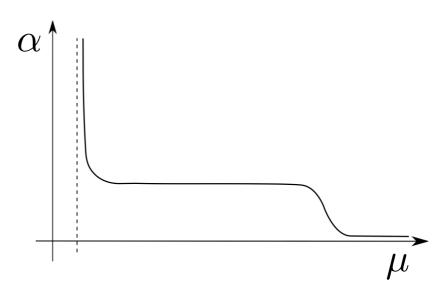
The limits on  $\Lambda_{ETC}$  from the large value of  $m_t$  and the FCNC experimental data seem to be incompatible, but that was without taking into account renormalization:

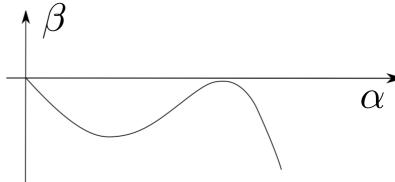
$$\gamma_m = \frac{d \log m}{d \log \mu}, \ m^3 \propto \langle \overline{Q}Q \rangle \Rightarrow \langle \overline{Q}Q \rangle_{ETC} = \langle \overline{Q}Q \rangle_{TC} \exp \left( \int_{\Lambda_{TC}}^{\Lambda_{ETC}} \frac{d\mu}{\mu} \gamma_m(\mu) \right)$$

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#### Running vs Walking TC







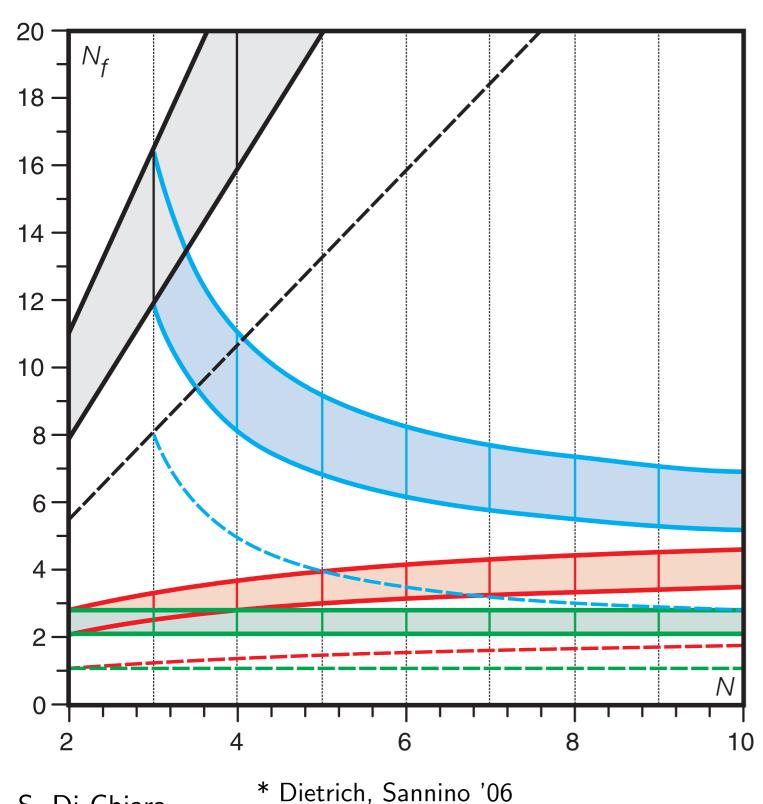
for  $\Lambda_{ETC} > \mu > \Lambda_{TC}$ :

- Running TC:  $\alpha(\mu) \propto \frac{1}{\ln \mu}, \Rightarrow \langle \overline{Q}Q \rangle_{ETC} \simeq \langle \overline{Q}Q \rangle_{TC}$
- Walking TC:  $\beta(\alpha_*) = 0 \Rightarrow \langle \overline{Q}Q \rangle_{ETC} \simeq \langle \overline{Q}Q \rangle_{TC} \left(\frac{\Lambda_{ETC}}{\Lambda_{TC}}\right)^{\gamma_m(\alpha_*)}$

A Walking TC obtains a big boost to fermion masses, while FCNC are unaffected.

\* Yamawaki et al. '86, Appelquist et al '86

# Walking in the SU(N)



Phase diagram for theories with fermions in the:

- fundamental representation (grey)
- two-index antisymmetric (blue)
- two-index symmetric (red)
- adjoint representation (green)

The S parameter for a TC model is estimated by:

$$S_{th} = \frac{1}{6\pi} \frac{N_f}{2} d(\mathbf{R}),$$
 
$$12\pi S_{ex} \le 6 @ 95\%$$
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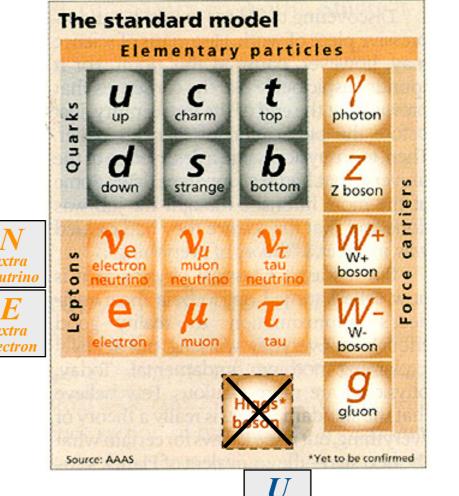
## Minimal Walking Technicolor

TC-fermions in the  $SU(2)_{TC}$  adjoint representation: a=1,2,3;

$$Q_L^a = \begin{pmatrix} U_L^a \\ D_L^a \end{pmatrix}, \ U_R^a, \ D_R^a \ .$$

Heavy leptons to cancel Witten anomaly:

$$L_L = \begin{pmatrix} N_L \\ E_L \end{pmatrix}, N_R, E_R.$$



TC-down

 $U(1)_Y$ 

 $SU(2)_L$ 

 $SU(3)_C$ 

$$Y(Q_L) = \frac{y}{2}, \qquad Y(U_R, D_R) = \left(\frac{y+1}{2}, \frac{y-1}{2}\right),$$

\* Sannino, Tuominen '04

$$Y(L_L) = -3\frac{y}{2}, \quad Y(N_R, E_R) = \left(\frac{-3y+1}{2}, \frac{-3y-1}{2}\right)$$

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## MWT Lagrangian

For  $y=\frac{1}{3}$  TC-fields have SM-like hypercharges, for y=1  $\bar{D}_R$  corresponds to a techni-gaugino. The MWT Lagrangian is

$$\mathcal{L}_{MWT} = \mathcal{L}_{SM} - \mathcal{L}_H + \mathcal{L}_{TC},$$

$$\mathcal{L}_{TC} = -\frac{1}{4} \mathcal{F}^a_{\mu\nu} \mathcal{F}^{a\mu\nu} + i \bar{Q}_L \gamma^{\mu} D_{\mu} Q_L + i \bar{U}_R \gamma^{\mu} D_{\mu} U_R + i \bar{D}_R \gamma^{\mu} D_{\mu} D_R$$

$$+ i \bar{L}_L \gamma^{\mu} D_{\mu} L_L + i \bar{E}_R \gamma^{\mu} D_{\mu} E_R + i \bar{N}_R \gamma^{\mu} D_{\mu} N_R,$$

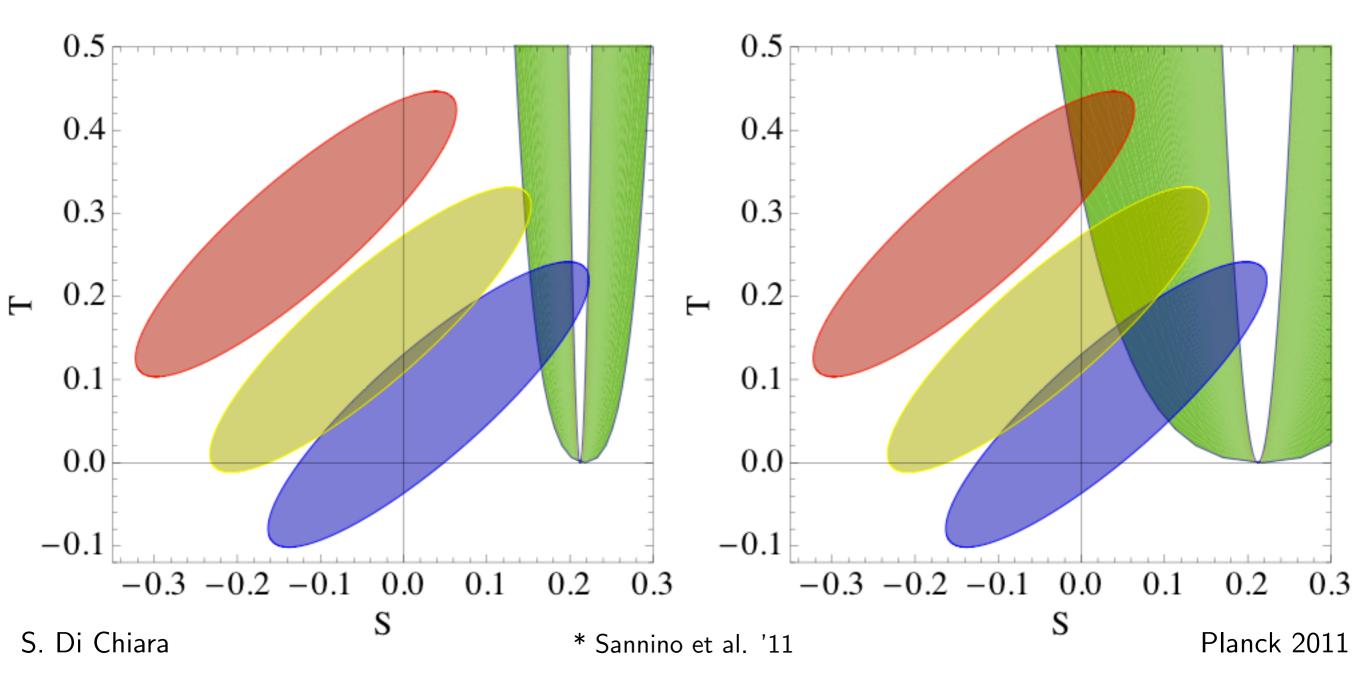
with the covariant derivatives defined by the fields' quantum numbers. The techniquarks condense and break EW:

$$\langle Q_i^{\alpha} Q_j^{\beta} \epsilon_{\alpha\beta} E^{ij} \rangle = -2 \langle \overline{U}_R U_L + \overline{D}_R D_L \rangle, \ Q = \begin{pmatrix} U_L \\ D_L \\ -i\sigma^2 U_R^* \\ -i\sigma^2 D_R^* \end{pmatrix}, \ E = \begin{pmatrix} 0 & \mathbb{I} \\ \mathbb{I} & 0 \end{pmatrix}$$

$$\langle Q_i^{\alpha} Q_j^{\beta} \epsilon_{\alpha\beta} E^{ij} \rangle \neq 0 \quad \Rightarrow \quad SU(2)_L \times U(1)_Y \to U(1)_{EM}$$

#### **S-T** Parameters

The ellipses give the S and T 90% CL region for  $M_H$ = 117 GeV (blue), 300 GeV (yellow), 1 TeV (red). MWT's S and T region (green) calculated for  $y=\frac{1}{3}$  (left panel), y=1 (right panel) and  $M_Z\leqslant M_{E,N}\leqslant 10~M_Z$ .



## Low Energy Lagrangian

Low energy Lagrangian:

$$\mathcal{L}_{\mathrm{Higgs}} = \frac{1}{2} \mathrm{Tr} \left[ D_{\mu} M D^{\mu} M^{\dagger} \right] - \mathcal{V}(M) + \mathcal{L}_{\mathrm{ETC}} ,$$

where the potential reads

$$\mathcal{V}(M) = -\frac{m_M^2}{2} \text{Tr}[MM^{\dagger}] + \frac{\lambda}{4} \text{Tr} \left[ MM^{\dagger} \right]^2 + \lambda' \text{Tr} \left[ MM^{\dagger}MM^{\dagger} \right]$$
$$- 2\lambda'' \left[ \text{Det}(M) + \text{Det}(M^{\dagger}) \right] ,$$

$$M_{ij} \sim Q_i Q_j$$
 with  $i, j = 1 \dots 4$ ,  $\langle M \rangle = \frac{v}{2} E$ .

M transforms under the full SU(4) group according to

$$M \to u M u^T$$
, with  $u \in SU(4)$ .

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#### Composite Vector Bosons

Composite vector bosons described by the four-dimensional traceless Hermitian matrix:

$$A^{\mu} = A^{a\mu} T^a ,$$

where  $T^a$  are the SU(4) generators. Under an arbitrary SU(4) transformation,  $A^\mu$  transforms like

$$A^{\mu} \rightarrow u A^{\mu} u^{\dagger}$$
, where  $u \in SU(4)$ .

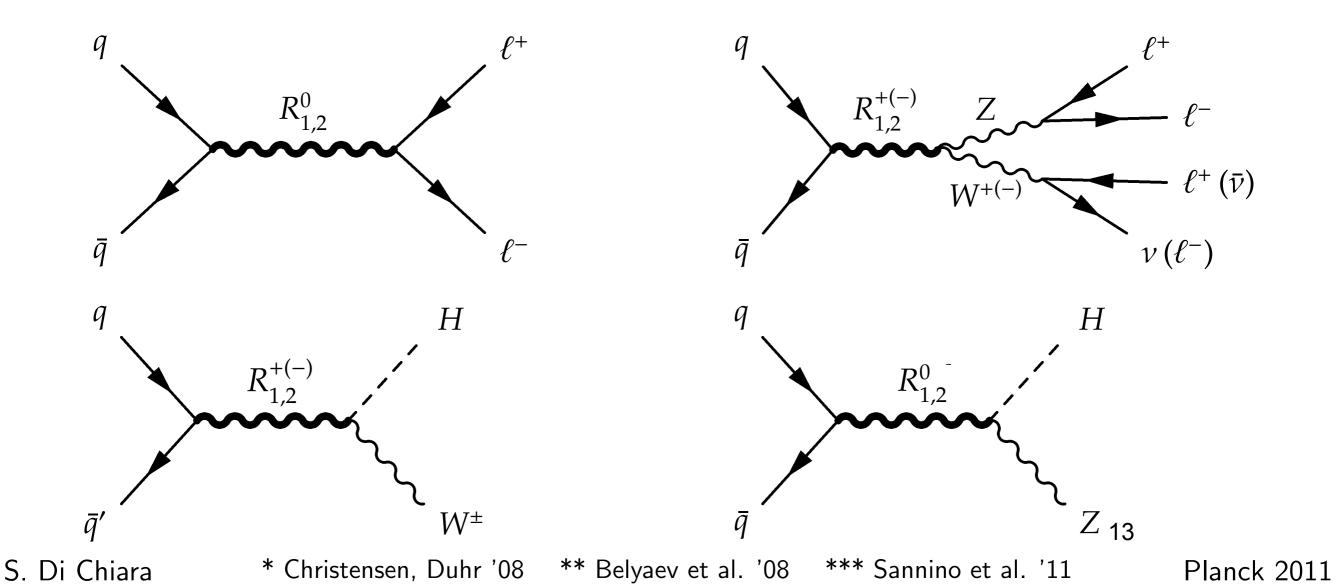
The techniquark content is expressed by the bilinears:

$$A_i^{\mu,j} \sim Q_i^{\alpha} \sigma^{\mu}_{\alpha\dot{\beta}} \bar{Q}^{\dot{\beta},j} - \frac{1}{4} \delta_i^j Q_k^{\alpha} \sigma^{\mu}_{\alpha\dot{\beta}} \bar{Q}^{\dot{\beta},k} .$$

#### LHC Phenomenology

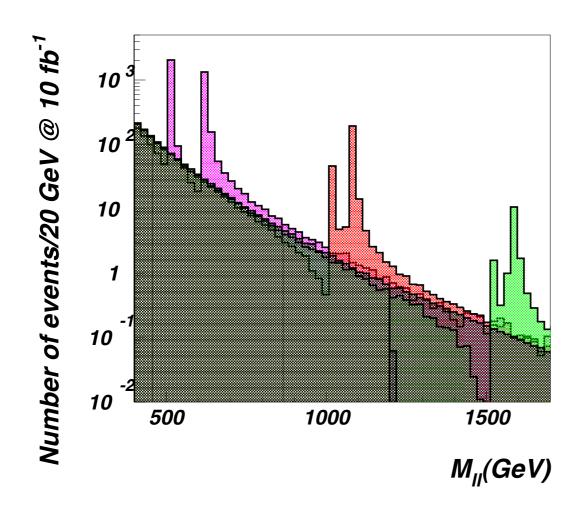
Effective Lagrangian implemented in Madgraph through FeynRules, and following processes studied for  $\sqrt{s}=7$  TeV:

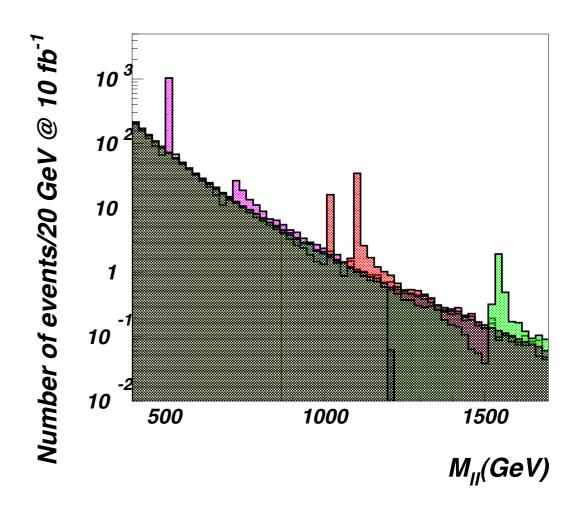
- Heavy vector boson  $(R_{1,2})$  production
- Associated composite Higgs production with  $W^{\pm}, Z$



#### Drell-Yan Process

Invariant mass distribution  $M_{\ell\ell}$  for  $pp \to R_{1,2} \to \ell^+\ell^-$  signal and background processes given by  $\tilde{g}=2$  (left),  $\tilde{g}=3$  (right), and  $M_A=0.5$  TeV (purple), 1 TeV (red), 1.5 TeV (green).  $R_1(R_2)$  is the lighter (heavier) vector meson.  $\tilde{g}=$  composite vector bosons self-coupling;  $M_A=$  axial-vector boson mass.





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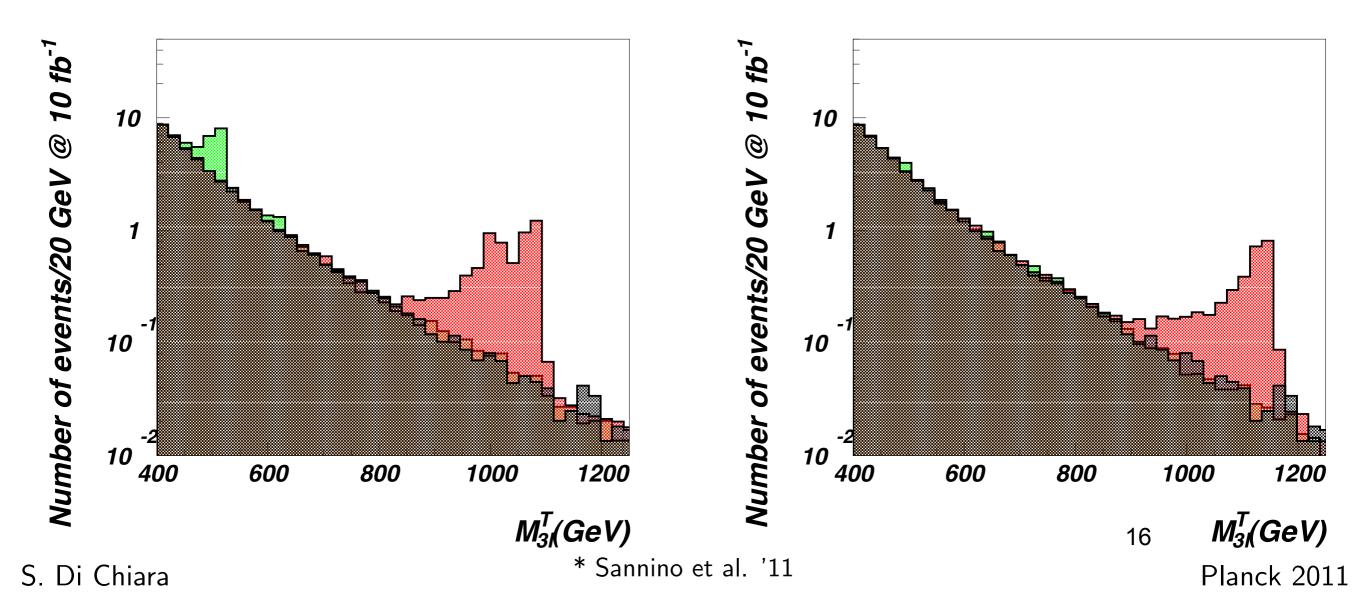
## Vector Resonance Signals

 $pp \to R_{1,2} \to \ell^+\ell^-$ . Signal and background cross sections for  $\tilde{g}=2,3,4$ , and required luminosity for  $3\sigma$  and  $5\sigma$  signals.

ğ	$M_A$	$M_{R_{1,2}}$	$\sigma_S$ (fb)	$\sigma_B$ (fb)	$\mathscr{L}(\mathrm{fb}^{-1})$ for $3\sigma$	$\mathscr{L}(\mathrm{fb}^{-1})$ for $5\sigma$
2	500	$M_1 = 517$	194	3.43	0.012	0.038
2	500	$M_2 = 623$	118	1.34	0.019	0.056
2	1000	$M_1 = 1027$	4.57	$9.17 \cdot 10^{-2}$	0.53	1.8
2	1000	$M_2 = 1083$	16.4	$5.60 \cdot 10^{-2}$	0.13	0.39
2	1500	$M_1 = 1526$	0.133	$5.91 \cdot 10^{-3}$	26	67
2	1500	$M_2 = 1546$	0.776	$2.81 \cdot 10^{-3}$	2.7	8.2
3	500	$M_1 = 507$	93.5	3.71	0.037	0.090
3	500	$M_2 = 715$	0.447	0.649	39	81
3	1000	$M_1 = 1013$	1.32	$8.81 \cdot 10^{-2}$	2.7	7.4
3	1000	$M_2 = 1097$	2.94	$5.15 \cdot 10^{-2}$	0.79	2.5
3	1500	$M_1 = 1514$	$3.19 \cdot 10^{-3}$	$5.63 \cdot 10^{-3}$	6300	14000
3	1500	$M_2 = 1586$	0.120	$3.94 \cdot 10^{-3}$	29	68
4	500	$M_1 = 504$	34.6	3.85	0.12	0.34
4	500	$M_2 = 836$	0.0	0.649	_	_
4	1000	$M_1 = 1007$	0.234	$8.98 \cdot 10^{-2}$	30	85
4	1000	$M_2 = 1148$	0.0	$5.15 \cdot 10^{-2}$	-	_
4	1500	$M_1 = 1509$	$1.31 \cdot 10^{-3}$	$3.94 \cdot 10^{-3}$	25000	57000
4	1500	$M_2 = 1533$	$1.43 \cdot 10^{-2}$	$3.94 \cdot 10^{-3}$	435	1200

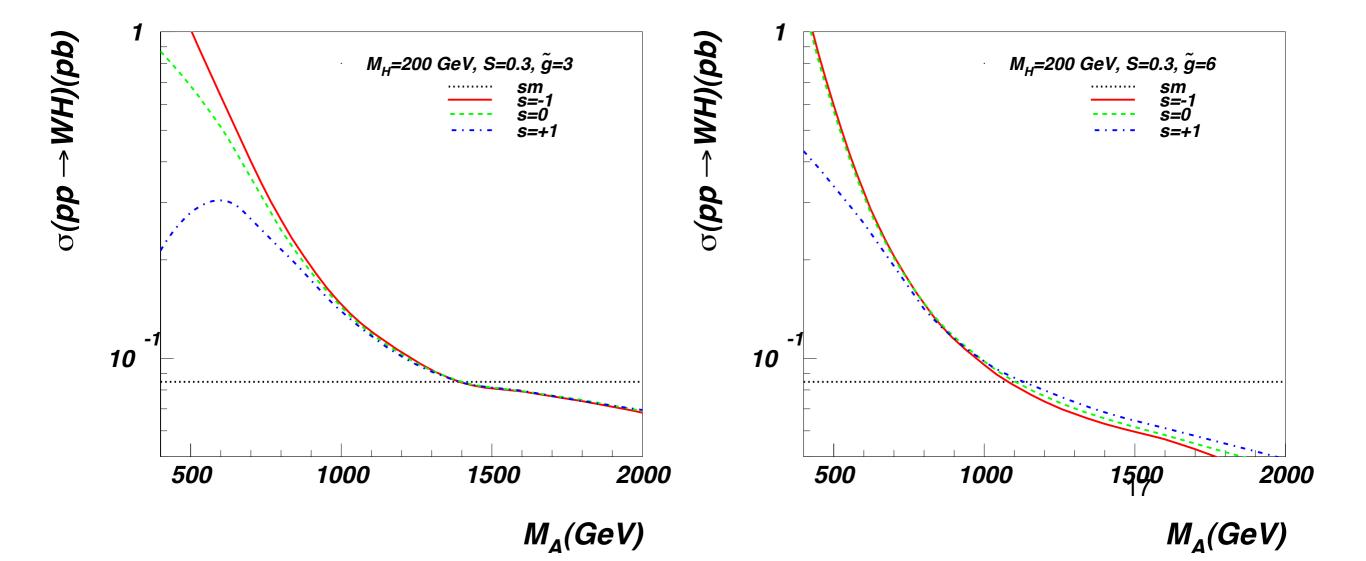
## Three Leptons+Missing Et

Transverse mass distribution  $M_{3\ell}^T$  for  $pp \to R_{1,2}^\pm \to ZW^\pm \to \ell\ell\ell\nu$  signal and background processes, calculated with  $\tilde{g}=2$  (left), 4 (right), and  $M_A=0.5$  TeV (green), 1 TeV (red). The  $R_{1,2}$  coupling to  $W^\pm,Z$  is enhanced for large values of  $\tilde{g}$ , balancing the suppression coming from the quark- $R_{1,2}$  couplings.



### Composite Higgs Production

The cross section for  $pp \to WH$  production at 7 TeV versus  $M_A$  for S=0.3, s=(+1,0,1) and  $\tilde{g}=3$  (left) and  $\tilde{g}=6$  (right). The dotted line at the bottom indicates the SM cross section level. The resonant production of heavy vectors can enhance HW and ZH production by a factor 10.



#### Conclusions

- Technicolor solves fine tuning
- Walking dynamics allow to satisfy experimental constraints
- MWT viable model with interesting LHC phenomenology
- Dark matter, inflation, unification, can all be accommodated within Technicolor

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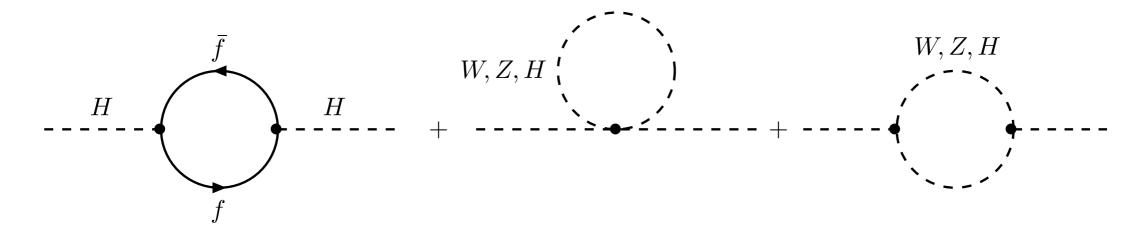
# Backup Slides

## SM Fine Tuning

SM Higgs mass at one loop:

$$M_H^2 = (M_H^0)^2 + \Delta M_H^2, (M_H^0)^2 = \frac{\lambda v^2}{2},$$

$$\Delta M_H^2 = \frac{3\Lambda^2}{8\pi^2 v^2} \left( M_H^2 - 4m_t^2 + 2M_W^2 + M_Z^2 \right) + O\left(\log \frac{\Lambda^2}{v^2}\right) =$$



If  $\Lambda=2.4\times 10^{18}$  GeV (Planck scale)  $\Rightarrow \frac{\Delta M_H^2}{M_H^2}\simeq 10^{32}$ :  $\lambda$  has to be determined up to the 32nd digit to miraculously cancel the quantum correction . . .

## One Family ETC

A toy ETC model: each entire family belongs to a single ETC fermion.

$$SU(N_{ETC}) \times SU(3)_C \times SU(2)_W \times U(1)_Y$$
:

$$Q_L = (N_{ETC}, 3, 2)_{1/6}$$
  $L_L = (N_{ETC}, 1, 2)_{-1/2}$   
 $U_R = (N_{ETC}, 3, 1)_{2/3}$   $E_R = (N_{ETC}, 1, 1)_{-1}$   
 $D_R = (N_{ETC}, 3, 1)_{-1/3}$   $N_R = (N_{ETC}, 1, 1)_0$ 

The lowest ETC scale is determined by the heaviest mass:

$$m_t = 173 \text{GeV} \Rightarrow \Lambda_{ETC} \simeq 10 \,\text{TeV}$$

Because of global symmetry breaking there are also massless NGB

$$SU(8)_L \times SU(8)_R \rightarrow SU(8)_V \Rightarrow 60 \,\mathrm{NGB}$$

$$SU(N_{TC}+3)$$

$$\Lambda_1 \qquad \downarrow \qquad m_1 \approx \frac{\Lambda_{TC}^3}{\Lambda_1^2}$$

$$SU(N_{TC}+2)$$

$$\Lambda_2 \qquad \downarrow \qquad m_2 \approx \frac{\Lambda_{TC}^3}{\Lambda_2^2}$$

$$SU(N_{TC}+1)$$

$$\Lambda_3 \qquad \downarrow \qquad m_3 \approx \frac{\Lambda_{TC}^3}{\Lambda_3^2}$$

$$SU(N_{TC})$$

#### pNGB Masses

Without specifying an ETC one can write down the most general ETC sector:

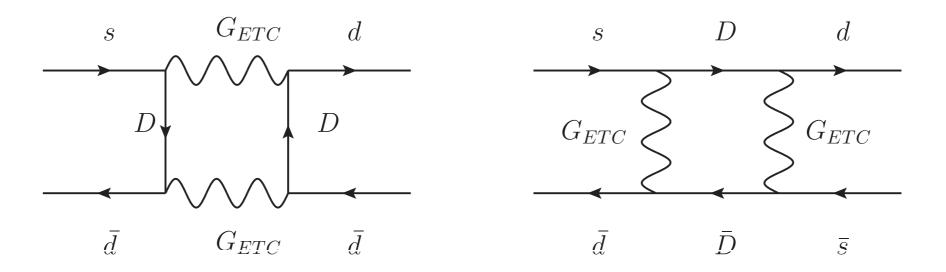
$$\mathcal{L}_{ETC} = \alpha_{ab} \frac{\bar{Q}_L T^a Q_R \bar{Q}_R T^b Q_L}{\Lambda_{ETC}^2} + \beta_{ab} \frac{\bar{Q}_L T^a Q_R \bar{\psi}_R T^b \psi_L}{\Lambda_{ETC}^2} + \gamma_{ab} \frac{\bar{\psi}_L T^a \psi_R \bar{\psi}_R T^b \psi_L}{\Lambda_{ETC}^2}$$

The first terms generate masses for the uneaten NGB. These can be estimated by:

$$\bar{Q}_R Q_L \to \Lambda_{TC}^3 \Sigma$$
,  $\Sigma \equiv \exp(i\pi^c \tilde{T}^c / F_T)$ ,  $\tilde{T} \in \mathcal{G}_{ETC}$ 

$$(M_{PNGB}^{cd})^2 \simeq \frac{\alpha_{ab}\Lambda_{TC}^6}{\Lambda_{ETC}^2 F_T^2} \text{Tr}([\tilde{T}^c, T^a][T^b, \tilde{T}^d]) \Rightarrow M_{PNGB} = O\left(\frac{\Lambda_{TC}^2}{\Lambda_{ETC}}\right)$$

#### **FCNC**



The second terms generate masses for the SM fermions, while the third terms are responsible for Flavor Changing Neutral Currents (FCNC):

$$\mathcal{L}_{\Delta S=2} = \gamma_{sd} \frac{(\bar{s}\gamma^5 d)(\bar{s}\gamma^5 d)}{\Lambda_{ETC}^2} + hc, \, \gamma_{sd} \sim \sin^2 \theta_c \simeq 10^{-2}.$$

Measured value of the neutral kaon mass splitting determines tight bound on ETC scale:

$$\frac{\Delta m^2}{m_K^2} \simeq \gamma_{sd} \frac{f_K^2 m_K^2}{\Lambda_{ETC}^2} \lesssim 10^{-14} \Rightarrow \Lambda_{ETC} \gtrsim 10^3 \text{ TeV} \,.$$

### Walking TC

Look for Walking TC ( $\beta(\alpha_*) = 0$ ) in theory space (Representation (R), Number of colors (N), Number of flavors  $(N_f)$ ) by studying

$$\beta(g) = -\beta_0 \frac{\alpha^2}{4\pi} - \beta_1 \frac{\alpha^3}{(4\pi)^2}, \ \alpha_* = -4\pi \frac{\beta_0}{\beta_1}, \ \beta_0 = \frac{11}{3} C_2(G) - \frac{4}{3} T(R),$$

$$\beta_1 = \frac{34}{3} C_2^2(G) - \frac{20}{3} C_2(G) T(R) - 4C_2(R) T(R).$$

The conformal window is defined by requiring asymptotic freedom, existence of a Banks-Zaks fixed point, and conformality to arise before chiral symmetry breaking:

$$\beta_{0} > 0 \implies N_{f} > \frac{11}{4} \frac{d(G)C_{2}(G)}{d(R)C_{2}(R)},$$

$$\beta_{1} < 0 \implies N_{f} < \frac{d(G)C_{2}(G)}{d(R)C_{2}(R)} \frac{17C_{2}(G)}{10C_{2}(G) + 6C_{2}(R)}$$

$$\alpha_{*} < \alpha_{c} \implies N_{f} > \frac{d(G)C_{2}(G)}{d(R)C_{2}(R)} \frac{17C_{2}(G) + 66C_{2}(R)}{10C_{2}(G) + 30C_{2}(R)}.$$
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#### TC Models

#### Walking Technicolor candidate models:

• Fundamental:

$$12\pi S(N = 3, N_f = 12) = 36,$$
  
$$12\pi S(N = 2, N_f = 8) = 16$$

Adjoint:

$$12\pi S(N=2, N_f=2) = 6,$$
  
 $12\pi S(N=3, N_f=2) = 16$ 

• 2 I. Symmetric:

$$12\pi S(N = 2, N_f = 2) = 6,$$
  
$$12\pi S(N = 3, N_f = 2) = 12$$

• 2 I. Antisymmetric:

$$12\pi S(N=3, N_f=12) = 36$$

Alternatives to reduce S:

- Custodial TC (S=0)
- Partially Gauged TC
- Split TC

The best (fully gauged) Walk-ing TC candidates are:

$$\bullet \text{ Adj}, N = 2, N_f = 2$$

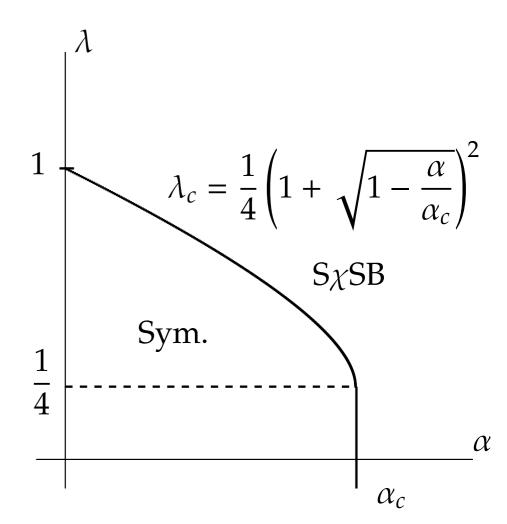
• 2-IS, 
$$N = 3, N_f = 2$$

### Ideal Walking

A strong ETC sector increases the value of the fermion mass anomalous dimension. In gauged Nambu-Jona-Lasinio (gNJL):

$$\mathcal{L}_{gNJL} = \mathcal{L}_{TC} + \frac{16\pi^2\lambda}{d[r]N_f\Lambda_{ETC}^2} \bar{\psi}_L \psi_R \bar{\psi}_R \psi_L \Rightarrow$$

$$\gamma_m(\lambda) = 1 - \omega + 2\omega \frac{\lambda}{\lambda_c}, \, \omega \equiv \sqrt{1 - \frac{\alpha}{\alpha_c}}$$

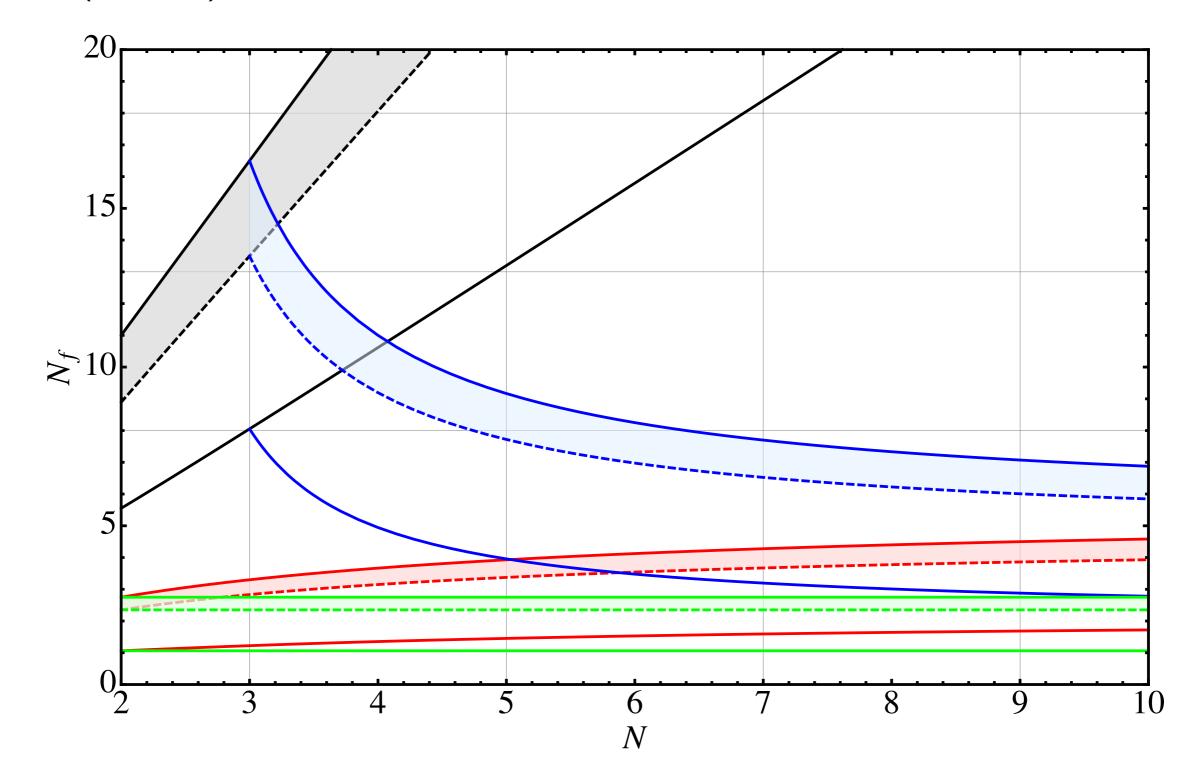


Assuming  $\lambda = \lambda_c = 0.75$  one gets  $\gamma_m(\lambda = \lambda_c) = 1 + \omega = 1.73 \Rightarrow$ By using dimensional analysis  $m_t = 172 \, \mathrm{GeV}$  for  $\Lambda_{ETC} \approx 10^7 \, \mathrm{TeV!}$ 

An accurate estimate of  $\Lambda_{TC}$  and  $\langle \bar{T}T \rangle_{TC}$  is needed to determine  $\Lambda_{ETC}$ .

### Phase Diagram with 4F Interaction

Phase diagram for SU(N) representations with chiral symmetry breaking (dashed) line determined for  $\lambda_c=0.75$ 



#### ETC Scalar Sector

In order to give masses to the 6 uneaten Goldstone bosons we add the following term which is generated in the ETC sector:

$$\mathcal{L}_{\rm ETC} \supset \frac{m_{\rm ETC}^2}{4} \, {\rm Tr} \left[ MBM^\dagger B + MM^\dagger \right] \; ,$$
 
$$M_{pNGB}^2 = m_{\rm ETC}^2 \; .$$

# MWT Gauge Sector

The minimal kinetic Lagrangian is:

$$\mathcal{L}_{\text{kinetic}} = -\frac{1}{2} \text{Tr} \left[ \widetilde{W}_{\mu\nu} \widetilde{W}^{\mu\nu} \right] - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} - \frac{1}{2} \text{Tr} \left[ F_{\mu\nu} F^{\mu\nu} \right] + m^2 \text{Tr} \left[ C_{\mu} C^{\mu} \right] ,$$

where  $\widetilde{W}_{\mu\nu}$  and  $B_{\mu\nu}$  are the EW elementary field strength tensors, and

$$F_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu} - i\tilde{g}\left[A_{\mu}, A_{\nu}\right] .$$

The vector field  $C_{\mu}$  is defined by

$$C_{\mu} \equiv A_{\mu} - \frac{g}{\tilde{g}} G_{\mu},$$

with  $G_{\mu}$  given by

$$G_{\mu} = g W_{\mu}^{a} L^{a} + g' B_{\mu} Y.$$

## Vector-Scalar Couplings

The  $C_{\mu}$  fields couple with M via gauge invariant operator:

$$\mathcal{L}_{\mathrm{M-C}} = \tilde{g}^{2} r_{1} \operatorname{Tr} \left[ C_{\mu} C^{\mu} M M^{\dagger} \right] + \tilde{g}^{2} r_{2} \operatorname{Tr} \left[ C_{\mu} M C^{\mu T} M^{\dagger} \right]$$

$$+ i \tilde{g} \frac{r_{3}}{2} \operatorname{Tr} \left[ C_{\mu} \left( M (D^{\mu} M)^{\dagger} - (D^{\mu} M) M^{\dagger} \right) \right]$$

$$+ \tilde{g}^{2} s \operatorname{Tr} \left[ C_{\mu} C^{\mu} \right] \operatorname{Tr} \left[ M M^{\dagger} \right].$$

The dimensionless parameters  $r_1$ ,  $r_2$ ,  $r_3$ , s express interaction strength in units of  $\tilde{g}$ , and are therefore expected to be of order one.

The fermions are coupled to the low energy effective Higgs through effective SM Yukawa interactions.

## Weinberg Sum Rules

The free parameters of the low energy spectrum are:  $r_1, r_2, r_3, s, M_A, M_H$ ,  $\tilde{g}$ , with A referring to the axial-vector meson. Three of these parameters can in principle be eliminated by using the constraints from the S parameter and the Weinberg Sum Rules (WSR).

The 1st and 2nd WSR are obtained from the vector and axial-vector two-point correlation functions, by assuming partial conservation of the axial current and they read

$$F_V^2 - F_A^2 = F_\pi^2$$
,  $F_V^2 M_V^2 - F_A^2 M_A^2 = a \frac{8\pi^2}{d(R)} F_\pi^4$ ,

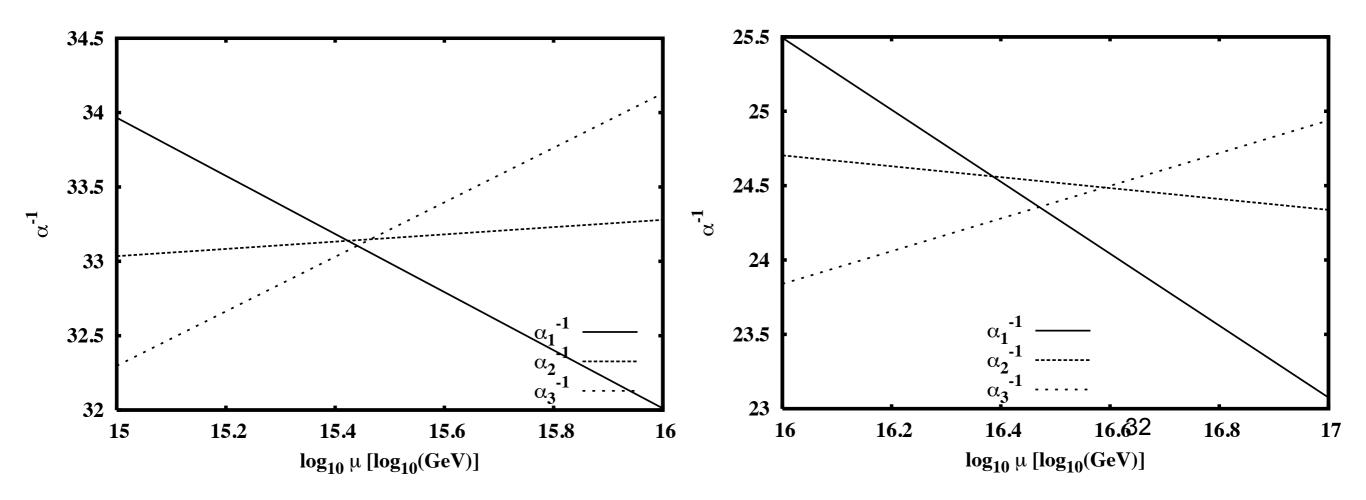
where a is expected to be positive and  $\mathcal{O}(1)$  for a walking theory and 0 for a running one.

#### Unification in MWT

Unification ingredients for MWT:

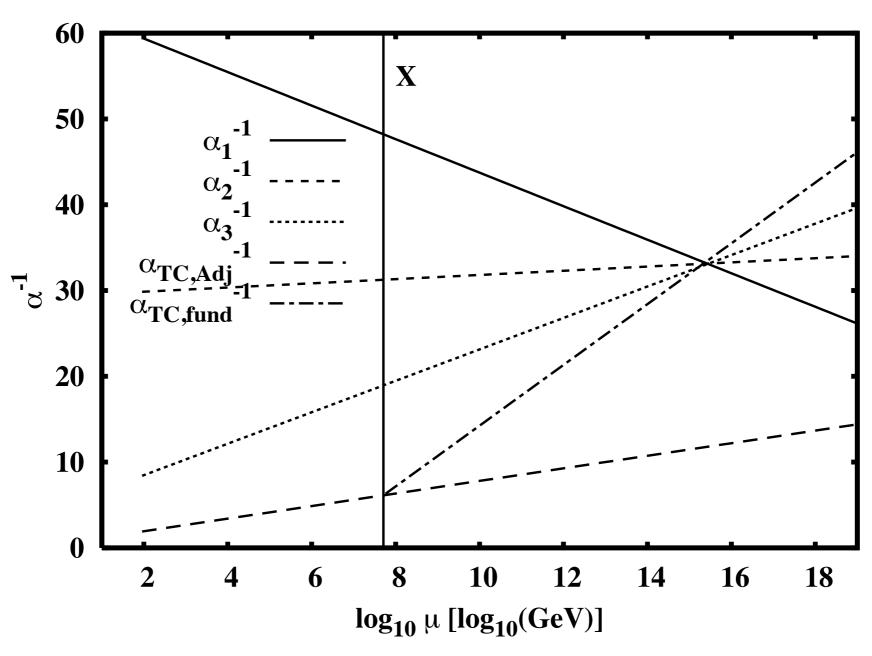
- ullet Make  $g_{TC}$  run at scale X by embedding  $SU(2)_{Adj}$  in  $SU(3)_F$
- Delay unification  $(M_{GUT} \gg v)$  to avoid the experimental bounds on the proton decay by adding a wino and a bino

Unification of  $g_Y, g_L, g_s$  in uMWT (left) and MSSM (right)



## uMVT Gauge Unification

Unification of gauge couplings in the uMWT:



#### Bosonic Technicolor

By supersymmetrizing the theory and taking the limit of scalars much heavier than their fermion superpartners, one finds that the theory is not fine tuned:

$$m_{\tilde{f}} \gg m_f \Rightarrow \Delta m_{\tilde{f}}^2 \propto \frac{y}{16\pi^2} m_{\tilde{f}}^2 \left( 1 - \log \frac{m_{\tilde{f}}^2}{\mu^2} \right) \Rightarrow \frac{\Delta M_H^2}{M_H^2} = O(1)$$

In the same limit the FCNC generated by scalars are suppressed.

#### From MWT to N=4 SUSY

MWT Minimal S-partners N=1 Multiplets N=4

$$G_{\mu}$$

$$\bar{D}_R$$

$$\bar{U}_R$$

$$U_L$$

$$D_L$$

$$G_{\mu}$$
 $\bar{D}_{R}$ 

$$egin{array}{ccc} ar{ar{U}}_R & ilde{ar{U}}_R \ U_L & ilde{U}_L \ D_L & ilde{D}_L \ \end{array}$$

$$\Phi_3$$
 $\Phi_1$ 
 $\Phi_2$ 

$$egin{bmatrix} V \ \Phi_3 \ \Phi_1 \ \Phi_2 \end{bmatrix}$$

Superpotential for SU(N)  $\mathcal{N}=4$  Super Yang-Mills (4SYM):

$$f(\Phi) = -\frac{g}{3\sqrt{2}} \epsilon_{ijk} f^{abc} \Phi_i^a \Phi_j^b \Phi_k^c, \ i = 1, 2, 3; a = 1, \dots, N^2 - 1;$$

# Minimal Super Conformal TC

	Superfield	$\mathrm{SU}(2)_{\mathrm{TC}}$	$\mathrm{SU}(3)_{\mathrm{c}}$	$\mathrm{SU}(2)_{\mathrm{L}}$	$U(1)_{Y}$
	$\Phi_L$	Adj	1		1/2
$\mathcal{N}=4$	$\Phi_3$	Adj	1	1	-1
	V	Adj	1	1	0
	$_{4^{ ext{th}}}$ $\Lambda_L$	1	1		-3/2
Lepton Fa	7. 7	1	1	1	1
_	E	1	1	1	2
	H	1	1		1/2
	H'	1	1		-1/2

### MSCT Superpotential

- Spectrum: 4SYM + lepton 4th superfamily + MSSM
- Gauge group:  $SU(2)_{TC} \times SU(3)_C \times SU(2)_L \times U(1)_Y$

$$f(\Phi)_{TC} = -\frac{g_{TC}}{3\sqrt{2}} \epsilon_{ijk} \epsilon^{abc} \Phi_i^a \Phi_j^b \Phi_k^c + y_U \epsilon_{ij3} \Phi_i^a H_j \Phi_3^a + y_N \epsilon_{ij3} \Lambda_i H_j N + y_E \epsilon_{ij3} \Lambda_i H_j' E + y_R \Phi_3^a \Phi_3^a E.$$

MSCT represents a possible UV completion of MWT.