



The 3rd generation quarks in warped models : *LHC predictions from LEP/Tevatron anomalies*

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Outline

I) Introduction: a warped model

II) A_{FB}^t and $t\bar{t}$ cross section @ Tevatron

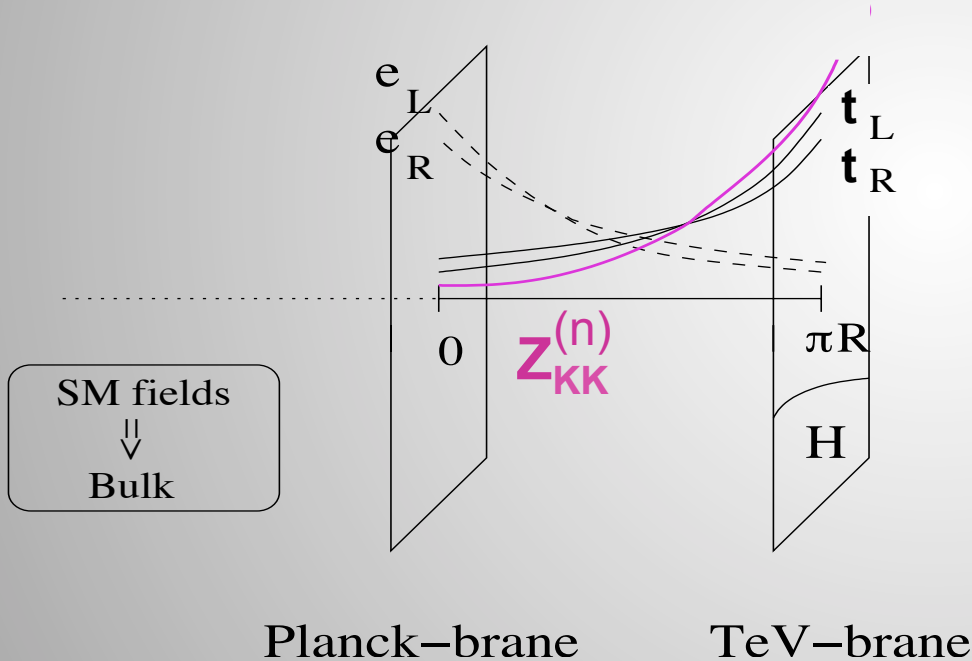
III) A_{FB}^b and EW precision tests @ LEP

IV) Constraints and predictions @ LHC

V) Conclusions

1) Introduction: a warped model

The Randall-Sundrum (RS) scenario with bulk fields:



- RS addresses the gauge *hierarchy* :

$$M_{grav} \approx TeV \approx Q_{EW}$$

Randall, Sundrum (1999)

- RS generates the mass *hierarchies* :

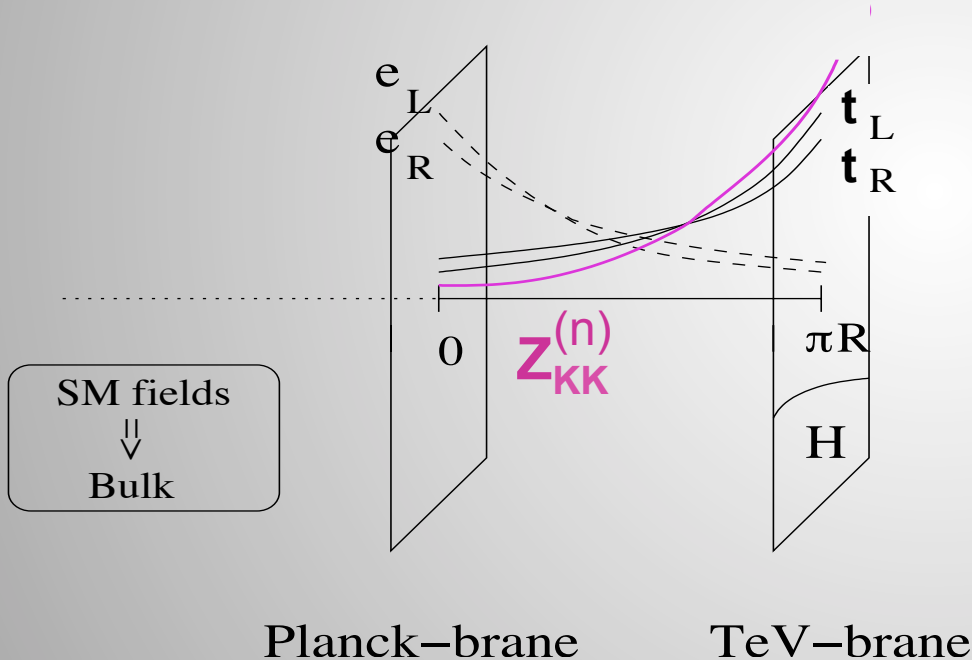
$$m_e \ll m_t$$

Gherghetta, Pomarol (2000)

...

1) Introduction: a warped model

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...

➔ New Physics effects in the heavy fermion sector !

**+ attractive features of the RS scenario with bulk fields
(= dual via AdS/CFT to composite Higgs & top models) :**

- WIMP candidates for the dark matter of universe:
a LKP stable due to a possible KK-parity (*like in UED*)
- Unification of gauge couplings (*as in ADD*) at high-energies
- Fermion mixing angles and flavor structure (*as in ADD*) \neq ***in SUSY***
- *Extra-Dimensions* =
necessary ingredients for higher-energy string theories

The EW precision constraints in warped models :

Bulk gauge bosons/fermions mix with their KK excitations

=> tree-level contributions to EW observables

Ways out to respect the constraints from EW precision data for $M_{\text{KK}} \sim \text{TeV}$:

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=> tree-level contributions to EW observables

Ways out to respect the constraints from EW precision data for $M_{\text{KK}} \sim \text{TeV}$:

~> **Gauge custodial symmetry in the bulk**

*Agashe, Delgado,
May, Sundrum (2003)*

$$\begin{array}{ccc} O(4) & & SU(2)_L \times SU(2)_R \\ \Downarrow & \approx & \Downarrow \\ O(3) & & SU(2)_V \times P_{LR} \end{array}$$

~> **Brane-localized kinetic terms for fermions/gauge fields**

Carena et al. (2002) Aguilera et al. (2003)

~> **Modification of the AdS metric in the vicinity of the IR brane**

Cabrera, Gersdorff, Quiros (2010)

« *Minimal* » representations under $SU(2)_L \times SU(2)_R \times U(1)_X$: $H=(2,2)_0$

$$\begin{pmatrix} t_{1L} & b'_L & q'_{-4/3L} \\ b_{1L} & q''_{-4/3L} & q'_{-7/3L} \end{pmatrix}_{-5/6} \quad (b_R \ q'_{-4/3R})_{-5/6} \quad \begin{pmatrix} q'_{5/3L} & t_{2L} \\ t'_L & b_{2L} \end{pmatrix}_{2/3} \quad (t_R)_{2/3}$$



“custodians”

$$SU(2)_R \longrightarrow U(1)_R$$

$$U(1)_R \times U(1)_X \longrightarrow U(1)_Y$$

$$\mathbf{W}_R^3 \quad \mathbf{B}_X \longrightarrow \mathbf{B}_Y \quad (+ \mathbf{Z}'^{KK})$$

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$$U(1)_R \times U(1)_X \longrightarrow U(1)_Y$$

$$W_R^3 \quad B_X \longrightarrow B_Y \quad (+ Z' \text{ KK})$$

Z' charges (I_{3R} isospin) and coupling ($g_{Z'} \sim 2$) \Rightarrow Zbb couplings addressing A_{FB}^b

t_R singlet: no custodian top partners \Rightarrow possible large $g^{KK} t\bar{t}$ couplings favor A_{FB}^t

II) A_{FB}^t and $t\bar{t}$ cross section @ Tevatron

A_{FB}^t at Tevatron

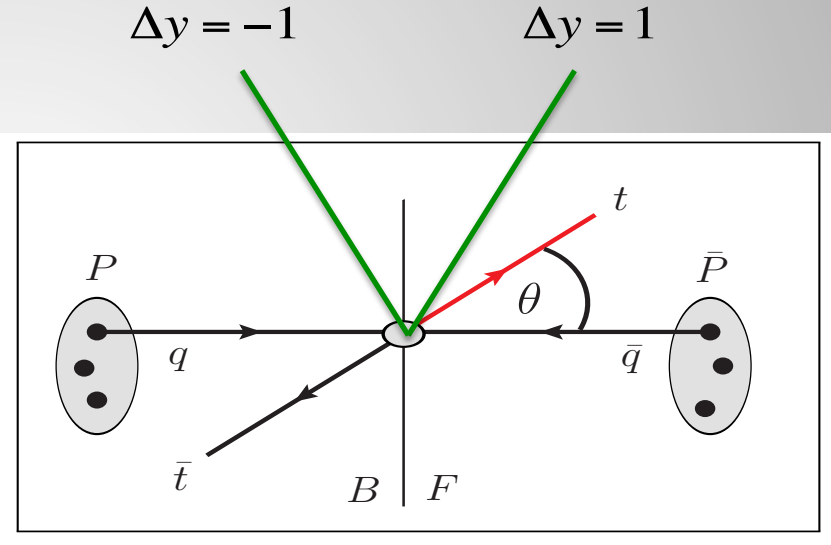
« What is the Forward-Backward asymmetry for the top quark ? »

$\neq 0$ with Parity-violating couplings

$$A_{FB}^t = \frac{\sigma^F - \sigma^B}{\sigma^F + \sigma^B} = \frac{\sigma[\cos \theta_t^* : 0 \rightarrow 1] - \sigma[\cos \theta_t^* : -1 \rightarrow 0]}{\sigma[\cos \theta_t^* : 0 \rightarrow 1] + \sigma[\cos \theta_t^* : -1 \rightarrow 0]} = \frac{\sigma[y_t > 0] - \sigma[y_t < 0]}{\sigma[y_t > 0] + \sigma[y_t < 0]}$$

($t\bar{t}$ rest frame)

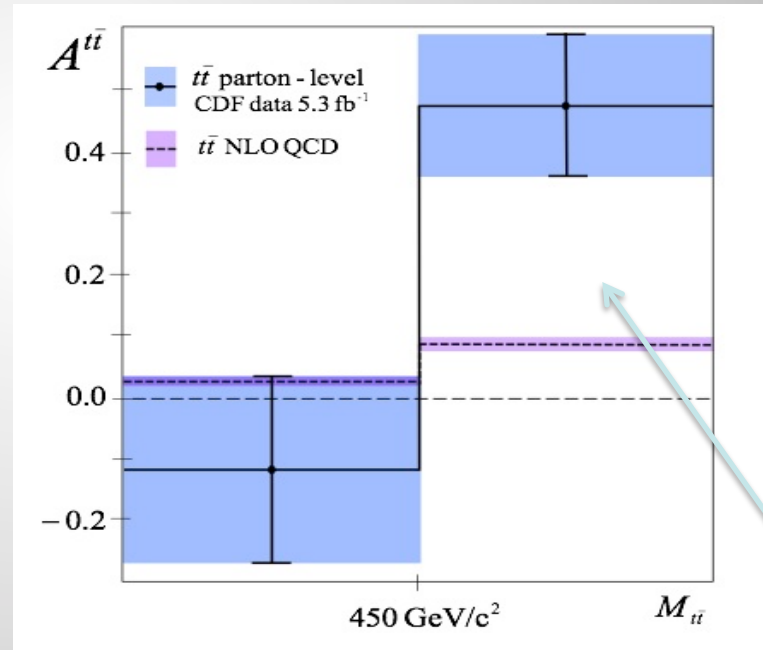
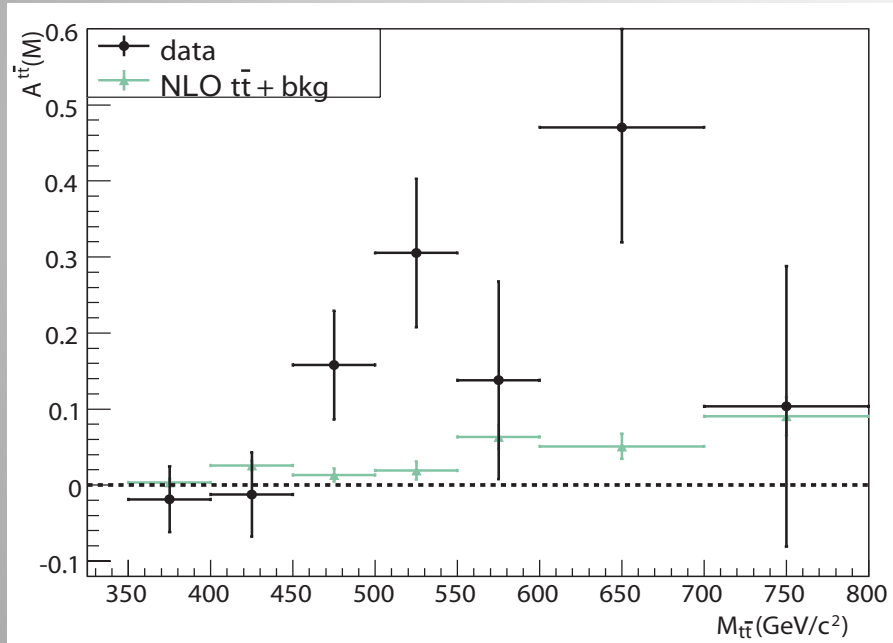
Rapidity : $y_t = \frac{1}{2} \ln[(E + p_z)/(E - p_z)] = \Delta y/2$



the data we use cause: most recent, unfolded and the only ones on rapidity dependence

01-2011 CDF in the lepton+jets channel with 5.3fb^{-1} :

$A_{\text{FB}}^t = 0.158 \pm 0.075$ (+1.3 sigma from SM prediction)

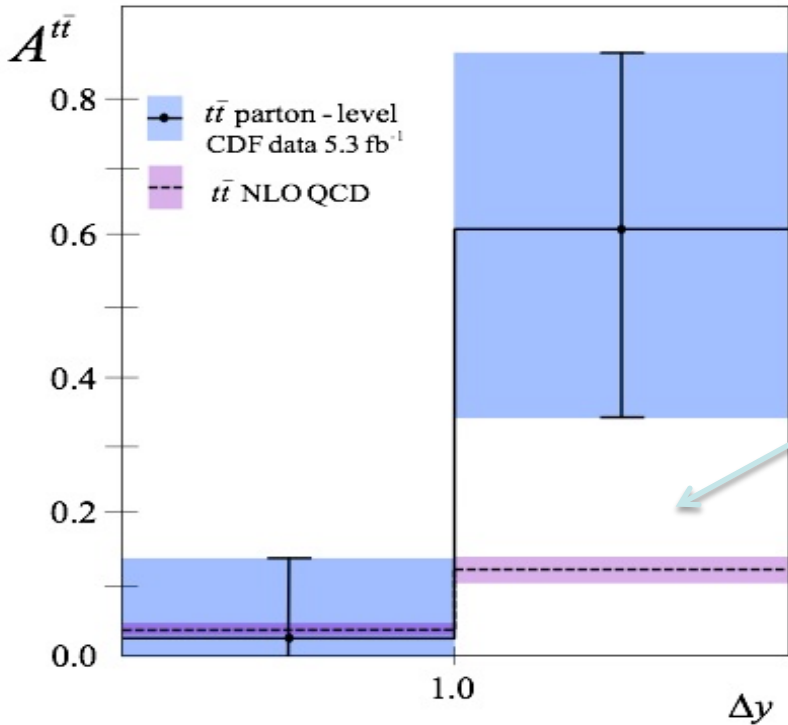


($t\bar{t}$ rest frame)

unfolding



+3.4 standard deviations from SM



+1.9 standard deviation from SM

($t\bar{t}$ rest frame, unfolded)

$$A_{\text{FB}}^{|\Delta y| < 1} = \frac{N(1 > \Delta y > 0) - N(-1 < \Delta y < 0)}{N(1 > \Delta y > 0) + N(-1 < \Delta y < 0)},$$

$$A_{\text{FB}}^{|\Delta y| > 1} = \frac{N(\Delta y > 1) - N(\Delta y < -1)}{N(\Delta y > 1) + N(\Delta y < -1)}$$

$$|\Delta y| < 3$$

A_{FB}^t in the considered warped model



+ interferences with SM
(negligible EW gauge contrib.)

A_{FB}^t non-vanishing (Parity violation)
 [

 $g_s Q(c_{t_L}) \neq g_s Q(c_{t_R})$
 $g_s Q(c_{q_L}) \neq g_s Q(c_{q_R})$
]
⇒

slightly closer to TeV-brane :
 $c_{u_L}, c_{d_L} \lesssim 0.5$
]
⇒

 $M_{KK} \sim 1.5 - 2 \text{ TeV}$
]
EW tests not so far treated in this setup

5D mass : $c k$

A_{FB}^t significant

A^t_{FB} in the considered warped model



+ interferences with SM
(negligible EW gauge contrib.)

A_{FB}^t non-vanishing (Parity violation)
 $\left[\begin{array}{l} g_s Q(c_{t_L}) \neq g_s Q(c_{t_R}) \\ g_s Q(c_{q_L}) \neq g_s Q(c_{q_R}) \end{array} \right. \Rightarrow \left. \begin{array}{l} \text{slightly closer} \\ \text{to TeV-brane :} \\ c_{u_L}, c_{d_L} \lesssim 0.5 \end{array} \right]$

A_{FB}^t significant $\Rightarrow M_{KK} \sim 1.5 - 2 \text{ TeV}$

EW tests not so far treated in this setup

We will show that EW fits are OK for :

$c_{u/d_L} \sim 0.44, c_{u/d_R} \sim 0.8, c_{c/s_L} \sim 0.6, c_{c_R} \sim 0.6,$
 $c_{s_R} \sim 0.49, c_{t/b_L} \sim 0.51, c_{b_R} \sim 0.53, c_{t_R} \sim -1.3$

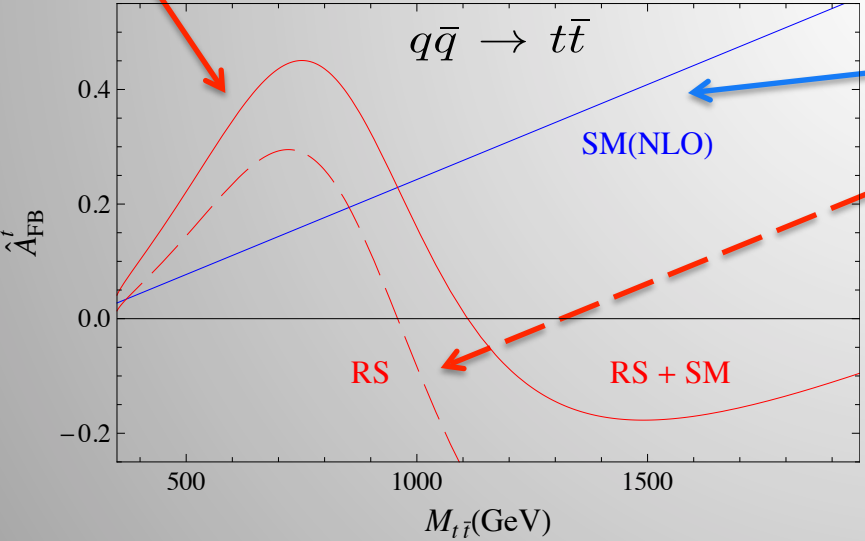
Asymmetry at parton level (neglecting 2nd/3rd generation + gluon initial state)...

$$\hat{A}_{\text{FB}}^{LO}(\hat{s}) = a_q a_t \frac{4\pi\alpha_s^2(\mu_r) \beta_t^2 |\mathcal{D}|^2 [(\hat{s} - M_{KK}^2) + 2v_q v_t \hat{s}]}{9 \hat{\sigma}_{SM-LO}^{\text{total}}(\hat{s}) + \hat{\sigma}_{RS+inter.-LO}^{\text{total}}(\hat{s})}$$

$$\left[\begin{aligned} a_q &= (Q(c_{qR}) - Q(c_{qL}))/2, \\ a_t &= (Q(c_{tR}) - Q(c_{tL}))/2, \\ v_q &= (Q(c_{qR}) + Q(c_{qL}))/2, \\ v_t &= (Q(c_{tR}) + Q(c_{tL}))/2, \end{aligned} \right.$$

$$\hat{A}_{\text{FB}}^{NLO}(\hat{s}) = \frac{(\hat{\sigma}_{SM-NLO}^F(\hat{s}) + \hat{\sigma}_{RS+inter.-LO}^F(\hat{s})) - (\hat{\sigma}_{SM-NLO}^B(\hat{s}) + \hat{\sigma}_{RS+inter.-LO}^B(\hat{s}))}{\hat{\sigma}_{SM-NLO}^{\text{total}}(\hat{s}) + \hat{\sigma}_{RS+inter.-LO}^{\text{total}}(\hat{s})}$$

$$\simeq \hat{A}_{\text{FB}}^{LO}(\hat{s}) + \hat{A}_{\text{FB}}^{SM-NLO}(\hat{s})$$

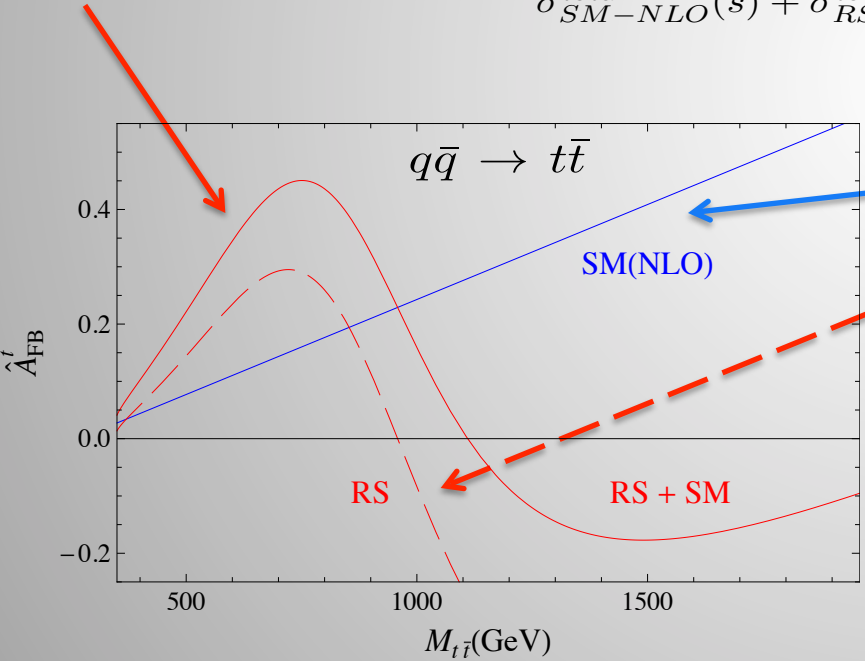


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$$\hat{A}_{\text{FB}}^{\text{NLO}}(\hat{s}) = \frac{(\hat{\sigma}_{\text{SM-NLO}}^{\text{F}}(\hat{s}) + \hat{\sigma}_{\text{RS+inter.-LO}}^{\text{F}}(\hat{s})) - (\hat{\sigma}_{\text{SM-NLO}}^{\text{B}}(\hat{s}) + \hat{\sigma}_{\text{RS+inter.-LO}}^{\text{B}}(\hat{s}))}{\hat{\sigma}_{\text{SM-NLO}}^{\text{total}}(\hat{s}) + \hat{\sigma}_{\text{RS+inter.-LO}}^{\text{total}}(\hat{s})}$$



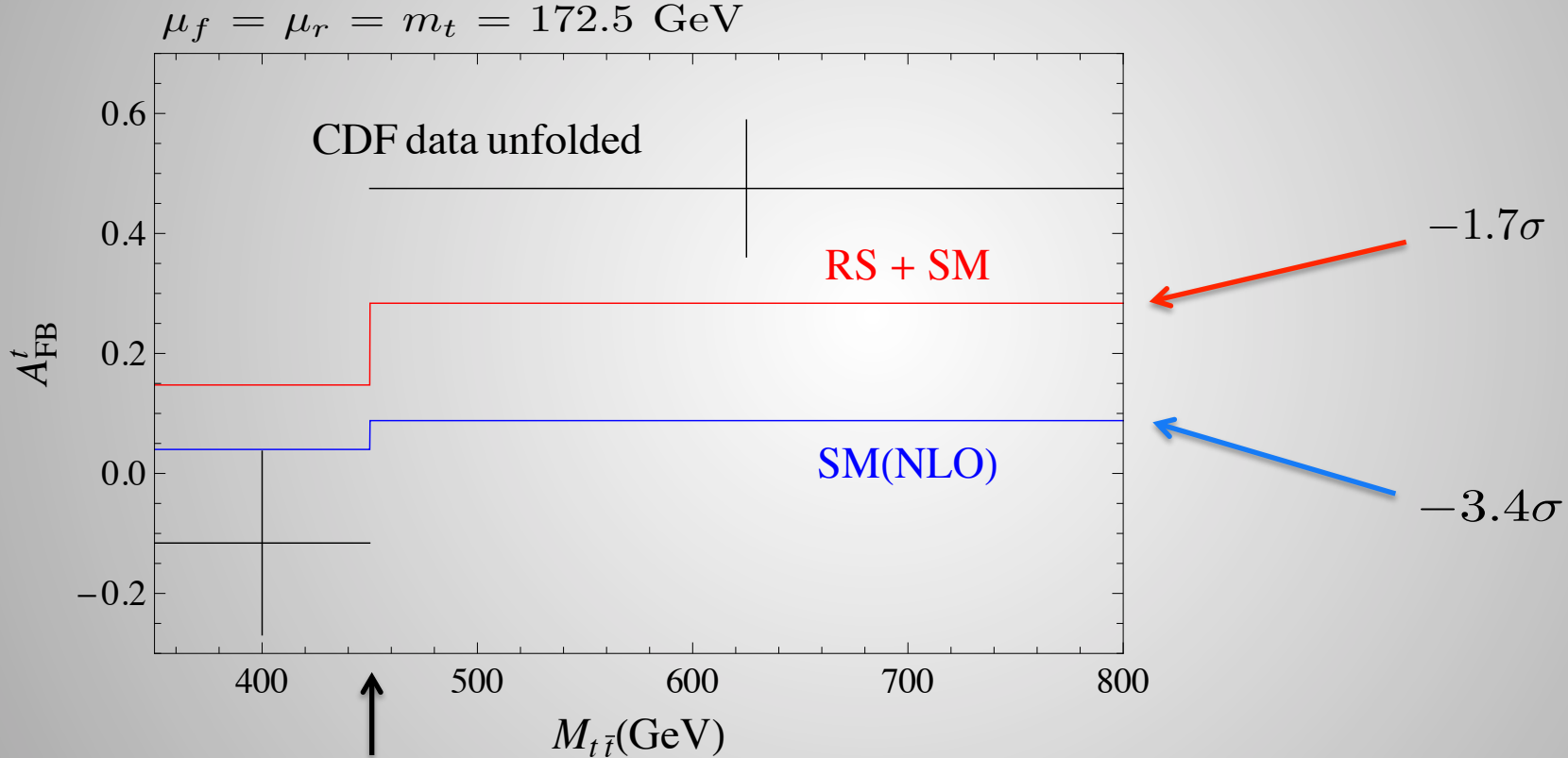
$$\simeq \hat{A}_{\text{FB}}^{\text{LO}}(\hat{s}) + \hat{A}_{\text{FB}}^{\text{SM-NLO}}(\hat{s})$$

For our parameters such that:
 $a_q a_t = -1.4 \quad v_q v_t = 0.7$

⇒ Positive $A_{\text{FB}}^{\text{LO}}$ in RS at low $M_{t\bar{t}}$
 as wanted !

Full asymmetry after convolution with MSTW-2008...

($t\bar{t}$ rest frame)



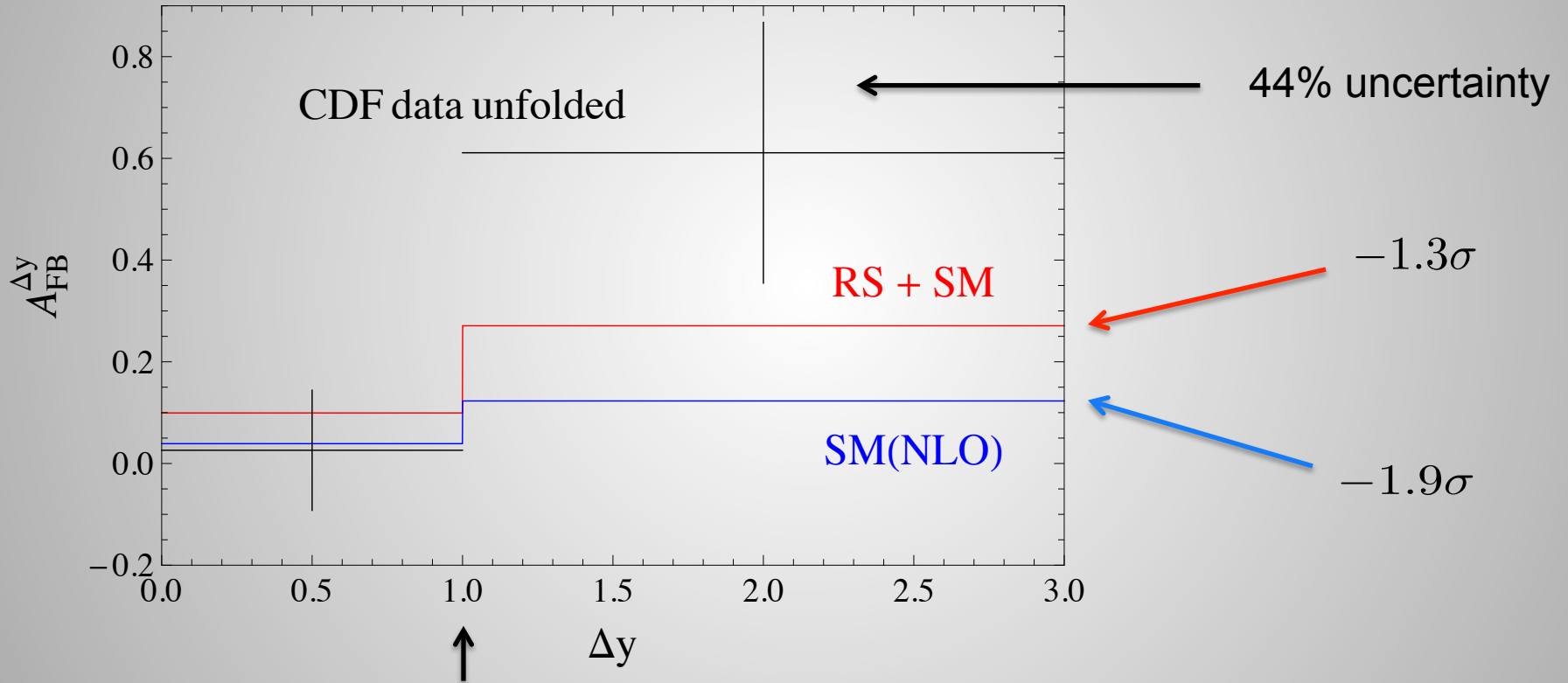
$M_{t\bar{t}} = 450 \text{ GeV}$

rest of the discrepancy : RS @ NLO ?

Full asymmetry as a function of rapidity...

($t\bar{t}$ rest frame)

$$\mu_f = \mu_r = m_t = 172.5 \text{ GeV}$$

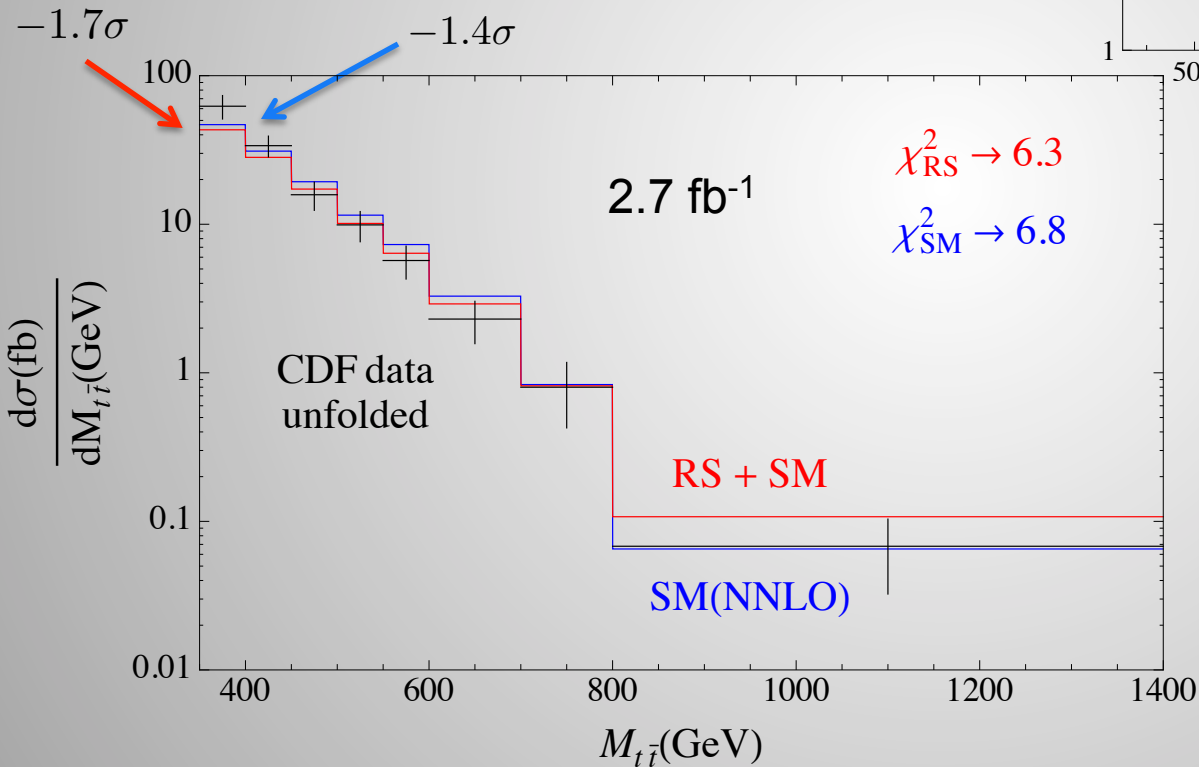
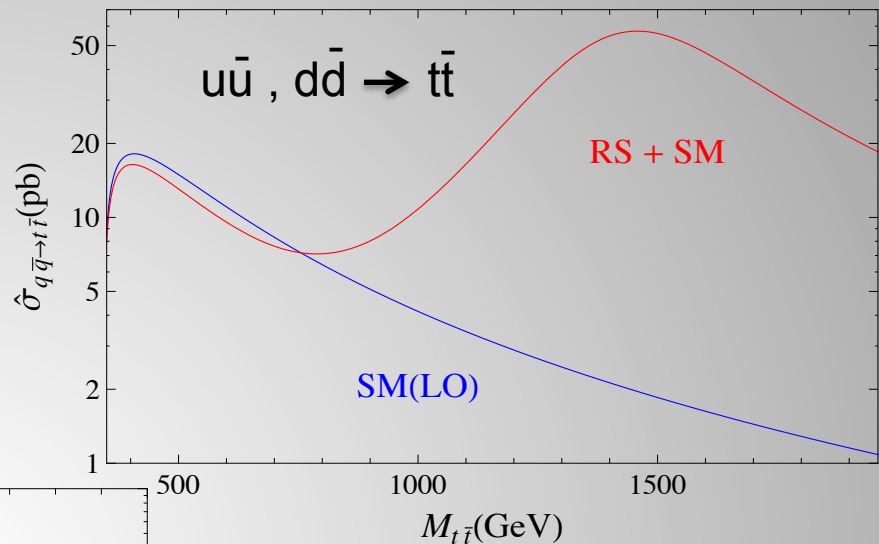


$\Delta y = 1$

additional positive test of the model

One must take care of the differential $t\bar{t}$ production cross section in good agreement with the SM...

$$\frac{d\sigma_{SM-NNLO}}{dM_{t\bar{t}}} \left(1 + \frac{d\sigma_{RS+inter.-LO}}{dM_{t\bar{t}}} / \frac{d\sigma_{SM.-LO}}{dM_{t\bar{t}}} \right)$$



$$\chi_{RS}^2 \rightarrow 6.3$$

$$\chi_{SM}^2 \rightarrow 6.8$$

In SM :

$$\chi_{SM}^2 / d.o.f. = 6.8 / 8$$

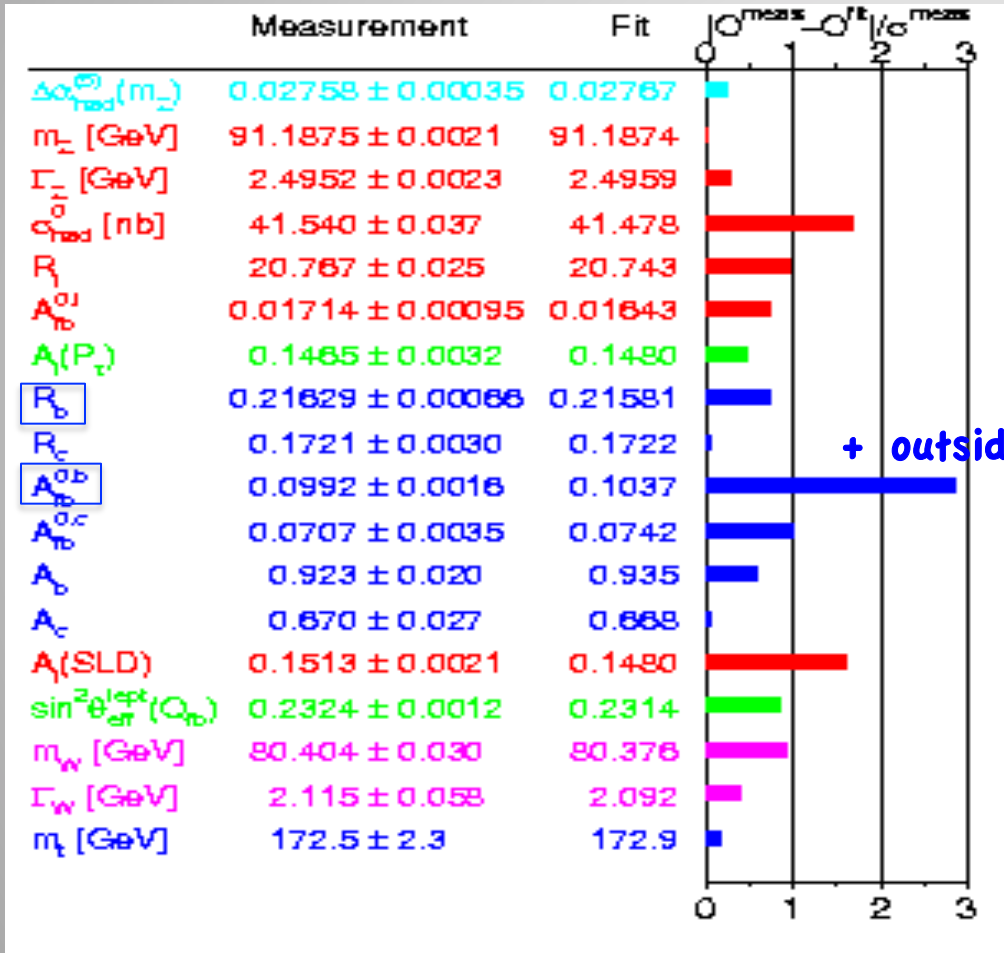
In RS :

$$\chi_{RS}^2 / d.o.f. = 6.3 / 8$$

$$m_t = 175 \text{ GeV}$$

$$\mu_f = \mu_r = m_t$$

III) A_{FB}^b and EW precision tests @ LEP



A_{FB}^b : a NP effect in the b sector ?

$$A_{FB}^b(p\hat{o}le) \equiv \frac{\int_0^{+1} \sigma_{\theta} d \cos \theta - \int_{-1}^0 \sigma_{\theta} d \cos \theta}{\sigma_0(e^+e^- \rightarrow \gamma / Z \rightarrow b\bar{b})}$$

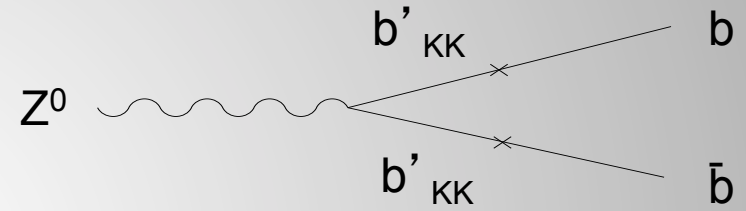
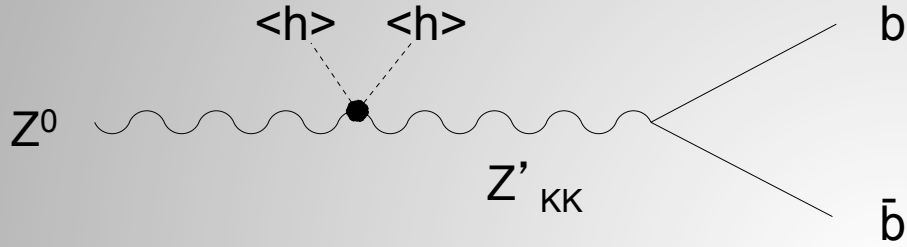
$$= \frac{3(Q_Z^{eL})^2 - (Q_Z^{eR})^2}{4(Q_Z^{eL})^2 + (Q_Z^{eR})^2} \frac{(Q_Z^{bL})^2 - (Q_Z^{bR})^2}{(Q_Z^{bL})^2 + (Q_Z^{bR})^2}$$

+ outside Z pôle !

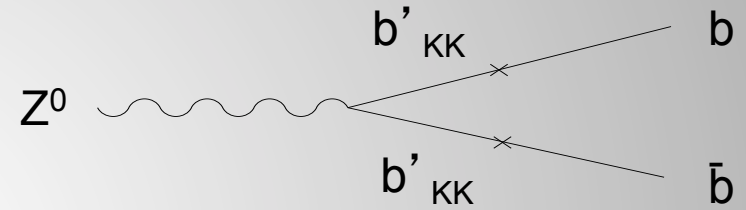
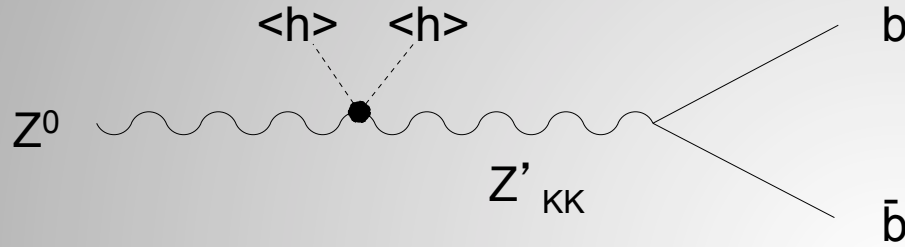
$$R_b \equiv \frac{\Gamma(Z \rightarrow b\bar{b})}{\Gamma(Z \rightarrow hadrons)}$$

$$= \frac{(Q_Z^{bL})^2 + (Q_Z^{bR})^2}{\sum_{q \neq t} [(Q_Z^{qL})^2 + (Q_Z^{qR})^2]}$$

Interpretation in a generic extra-dimensional model...
(difficult in SUSY)



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(difficult in SUSY)



$$\left| \delta Q_Z^{f_l} \right| \approx 1\%_{00} \ll \left| \delta Q_Z^{b_{L/R}} \right| \approx |-1.5/30\%|$$

$$m_{b'}(c_{t_R}) \ll m_{f'}(c_{\text{light}})$$

$$\text{Coupling } Z_{KK} f_l \bar{f}_l \ll \text{Coupling } Z_{KK} b \bar{b}$$

$$m_t(c_{t_R}) \uparrow \Rightarrow m_{b'}(c_{t_R}) \downarrow$$



'natural' conditions within the RS model

Summary of the EW observables...

Observable	SM	RS
$A_{FB}^b(m_Z)$	2.7σ	1.2σ
R_b	0.8σ	1.2σ
$A_{FB}^c(m_Z)$	0.9σ	0.9σ
R_c	0.0σ	0.5σ
$A_{FB}^s(m_Z)$	0.6σ	0.2σ
$\Gamma_{\text{had}}(Z)$	1.3σ	1.0σ
$\Gamma_{\text{tot}}(W)$	0.2σ	0.2σ
$\langle Q_{FB} \rangle$	1.1σ	0.1σ
$C_{1u} + C_{1d}$	0.2σ	0.8σ
$C_{1u} - C_{1d}$	1.1σ	0.1σ
$\chi^2/d.o.f.$	25.3/17	19.8/17

no more A_{FB}^b anomaly
at the Z^0 pole

still fits well

whole fit improved

+ Zuu/Zdd OK from
Tevatron Run I & II
& HERA (H1,ZEUS)

IV) Constraints and predictions @ LHC

Comparison of the $t\bar{t}$ cross section $\sigma_{t\bar{t}}$

in RS+SM

NNLO
(HATHOR)

$$\mu_F = \mu_R = m_t = 173 \text{ GeV}$$

$$\sqrt{s} = 7 \text{ TeV}$$

$$\mathcal{L} = 35 \text{ pb}^{-1}$$

$$\sigma(pp \rightarrow t\bar{t}) \text{ at } -0.86\sigma$$

SM at -0.81σ

from the ATLAS measurement, $180 \pm 18.5 \text{ pb}$

$$\sigma(pp \rightarrow t\bar{t}) \text{ at } +0.36\sigma$$

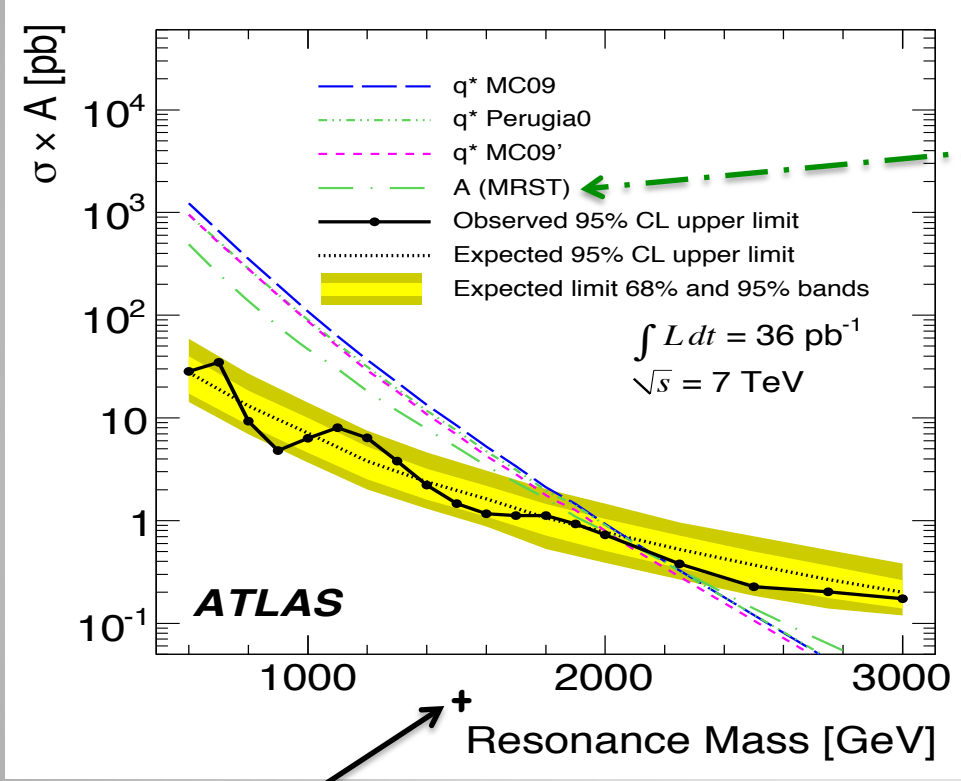
SM at $+0.31\sigma$

from the CMS measurement, $158 \pm 19 \text{ pb}$



OK as major contribution from the gg initial state

Constraints from dijets



Axiguon - $SU(3)_L \times SU(3)_R$

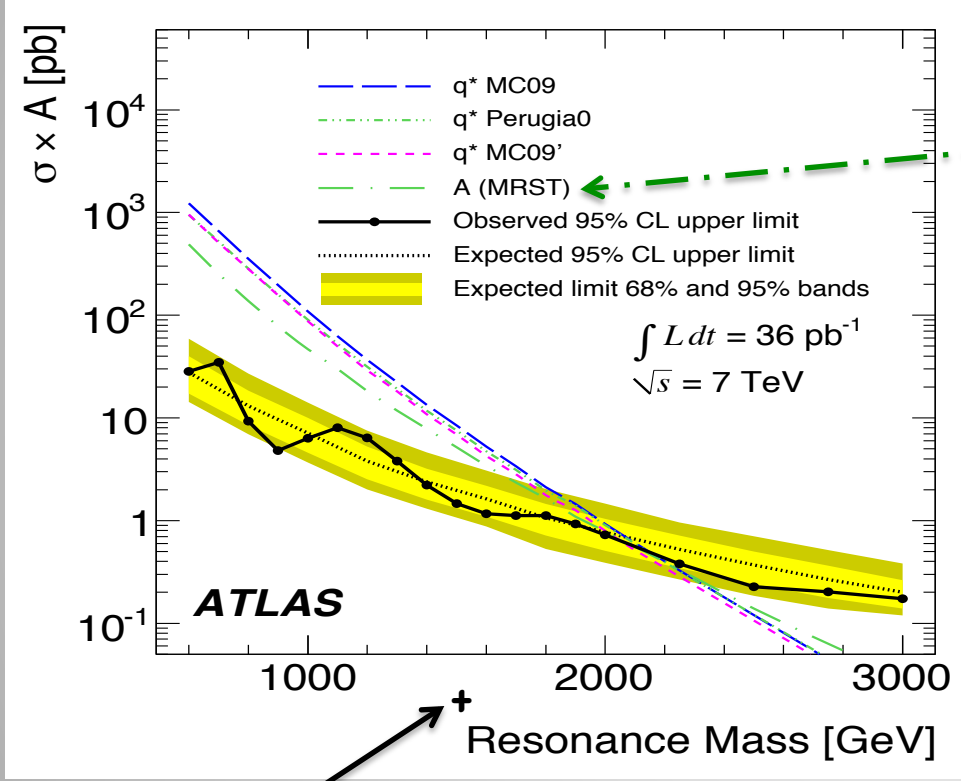
Frampton et al. (1987)
Bagger et al. (1987)

- ★ now including the width effect between $0.7 M_{KK}$ and $1.3 M_{KK}$
- ★ we have also checked the angular distribution constraints



we've computed the ratio $RS/Axiguon$
 $\Rightarrow KK$ gluon exchange @ 0.023 pb

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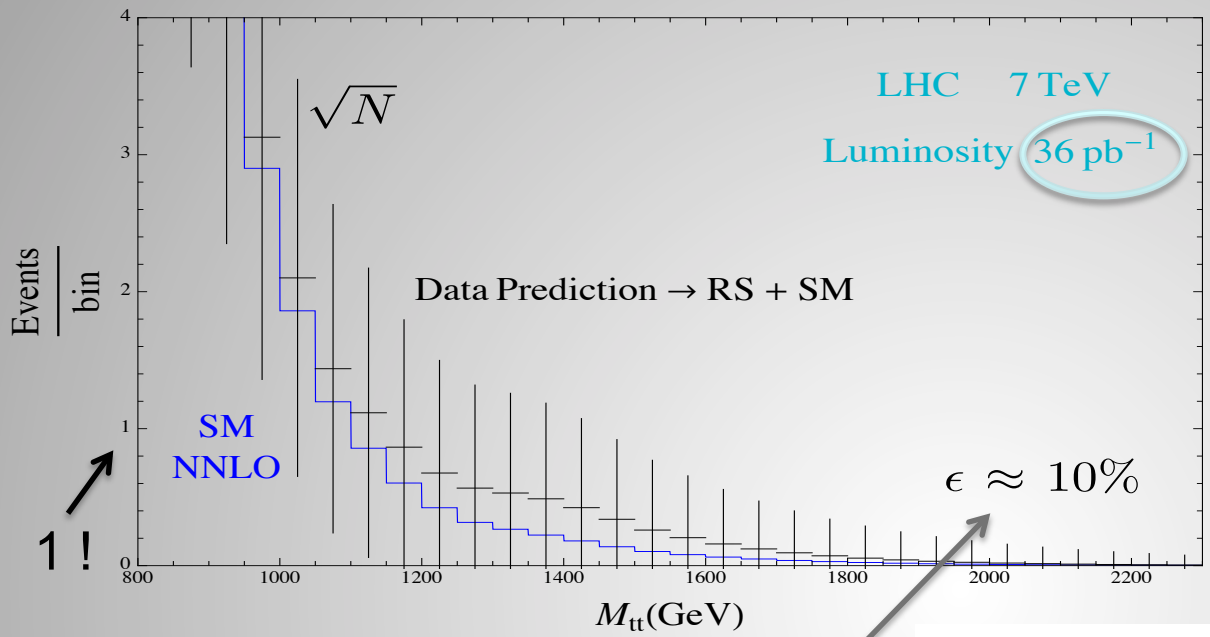
Coupling $g^{(1)tt} > g^{(1)qq}$



RS addresses A_{FB}^t
 + passes dijet bounds

we've computed the ratio RS/Axigluon
 $\Rightarrow KK$ gluon exchange @ 0.023 pb

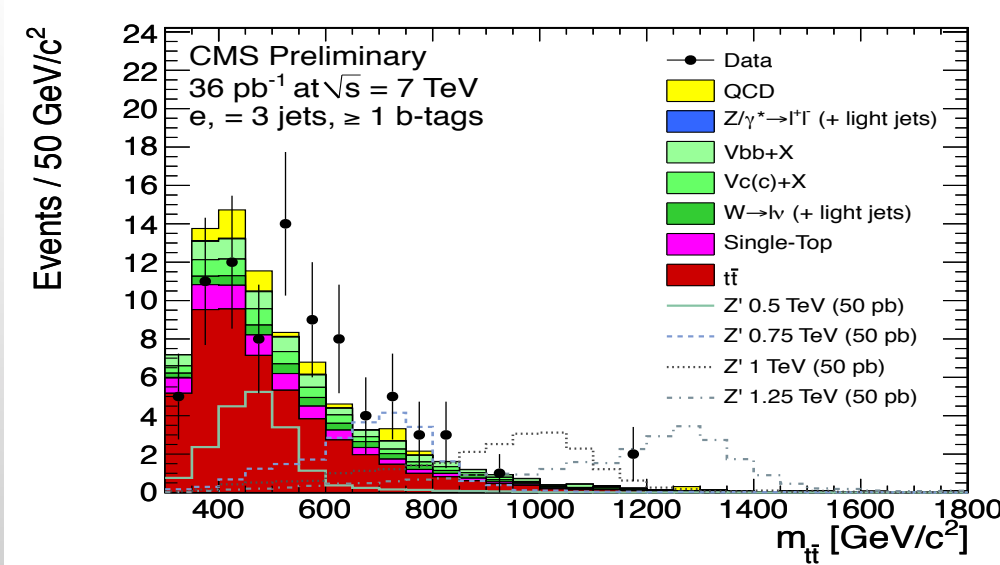
Predictions on the $M_{t\bar{t}}$ distribution at LHC



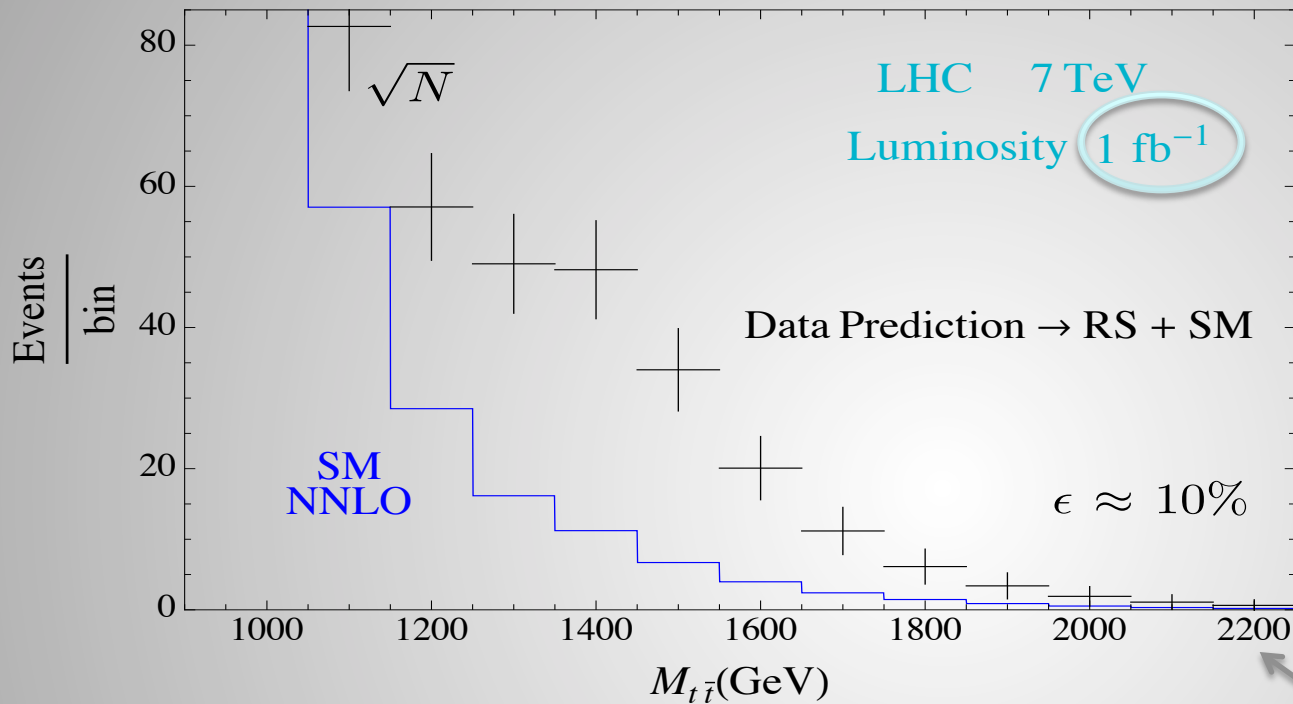
compatible

$t\bar{t}$ reconstruction efficiency taken

$$\mu_f = \mu_r = m_t = 173 \text{ GeV}$$



What does the RS model predicts at the expected luminosity of 1 fb^{-1} ?



..a KK gluon resonance

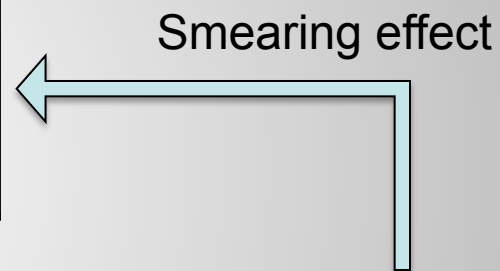
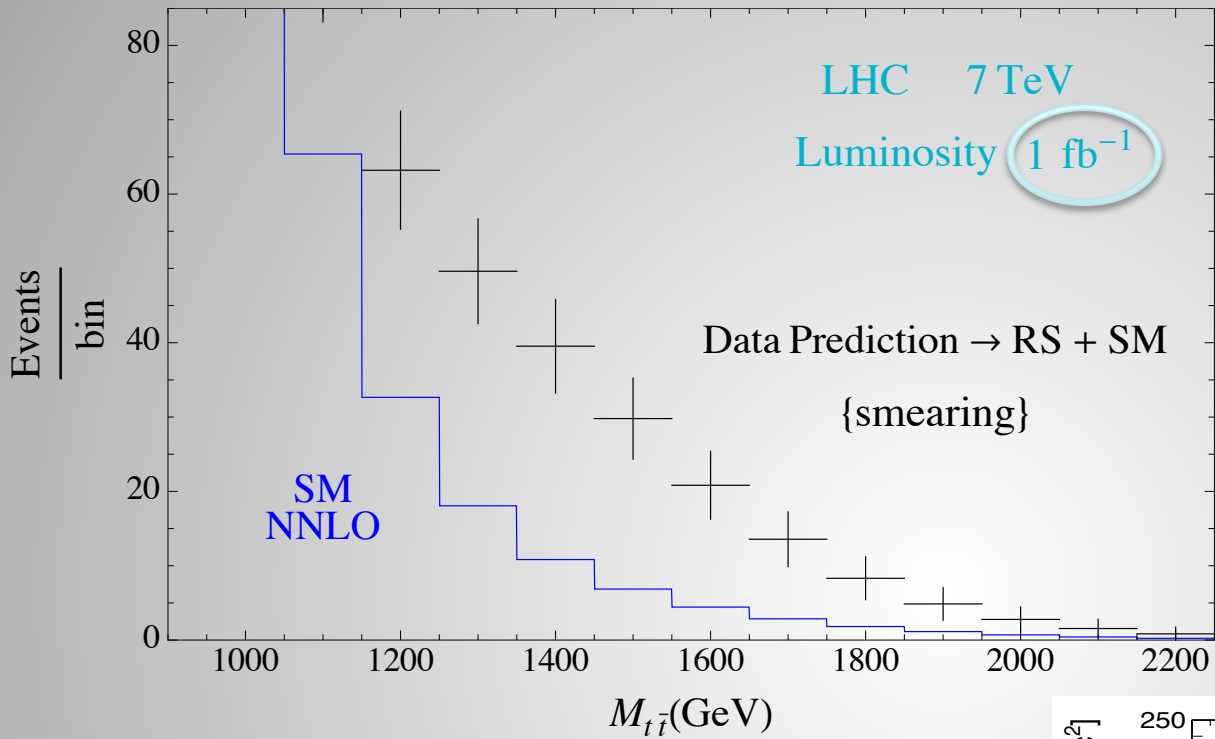
$$\Gamma_{g^{(1)}} \simeq 40\% M_{KK}$$

assuming 100 GeV bin resolutions

integration of the cross section e.g. over $[1050, 1750]$ GeV

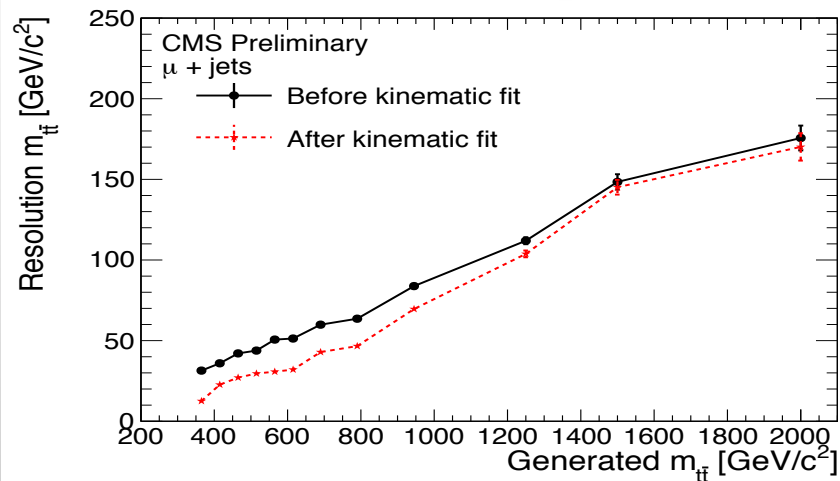
$$\rightarrow \text{Signal} / \sqrt{\text{Background}} \simeq 13.9$$

An excess should be clearly visible.



$$\text{Signal} / \sqrt{\text{Background}} \cong 12.7$$

A great excess even simulating the $M_{t\bar{t}}$ experimental resolution:



V) Conclusions

- ☀ The ‘warped paradigm’, with theoretical motivations, predicts deviations from SM in the 3rd generation sector => $A_{FB}^b, A_{FB}^t = \text{early indications ?}$
- ☀ We suggest a geometrical RS realization addressing both A_{FB}^b and A_{FB}^t .
- ☀ The several constraints on the parameter space render this RS scenario quite **predictive on the effects in the $t\bar{t}$ invariant mass distribution @ LHC.**
- ☀ One must wait for more data (Tevatron, LHC) in order to discriminate between the main A_{FB}^t interpretations: Z/W’, KK gluon, Axigluon, stop...
- ☀ This RS model addressing A_{FB}^b, A_{FB}^t predicts a **KK gluon resonance**
 \neq
Other RS models usually with light **custodians copiously producible**
(‘no-lose signal’ theorem in warped pheno. @ LHC)

Back up

Some useful formula's...

$$\cos \theta_t^* = \sqrt{1 + \frac{4m_t^2}{\hat{s} - 4m_t^2}} \tanh y_t$$

$$\frac{1}{\mathcal{D}} = \hat{s} - M_{KK}^2 + i \frac{\hat{s}}{M_{KK}^2} \sum_q \Gamma_{KK}^{g(1) \rightarrow q\bar{q}} M_{KK} \frac{\beta_q [v_q^2 (3 - \beta_q^2)]/2 + a_q^2 \beta_q^2}{v_q^2 + a_q^2}$$

$$\beta_t = \sqrt{1 - 4m_t^2/\hat{s}}$$

$$\sqrt{\hat{s}_0} \simeq \frac{M_{KK}}{(1 + \Gamma_{KK}^2/M_{KK}^2)^{1/4}}$$

$$\frac{d\hat{\sigma}_{RS-LO}}{d \cos \theta_t^*}(\hat{s}) = \frac{\pi \alpha_s^2(\mu_r) \beta_t}{9\hat{s}} \times$$

$$\hat{s}^2 |\mathcal{D}|^2 \left[8v_q v_t a_q a_t \beta_t \cos \theta^* + (a_q^2 + v_q^2) (v_t^2 (2 - \beta_t^2 \sin^2 \theta^*) + a_t^2 \beta_t^2 (1 + \cos^2 \theta^*)) \right]$$

$$\frac{d\hat{\sigma}_{inter.-LO}}{d \cos \theta_t^*}(\hat{s}) = \frac{\pi \alpha_s^2(\mu_r) \beta_t}{9\hat{s}} 4\hat{s} \text{Re}(\mathcal{D}) \left[v_q v_t \left(1 - \frac{1}{2} \beta_t^2 \sin^2 \theta^* \right) + a_q a_t \beta_t \cos \theta^* \right]$$

$$\left(\frac{d\hat{\sigma}_{SM-LO}}{d \cos \theta_t^*}(\hat{s}) \Big|_{q\bar{q}} = \frac{\pi \alpha_s^2(\mu_r) \beta_t}{9\hat{s}} \left\{ 2 - \beta_t^2 \sin^2 \theta^* \right\} \right)$$

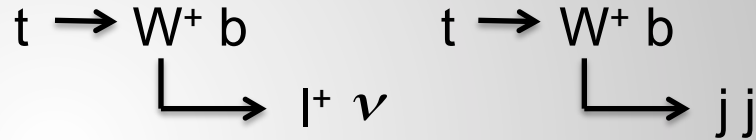
« How is A_{FB}^t measured at Tevatron in lepton+jet channels ? »

$$\Delta y = y_t - y_{\bar{t}} \quad y_t = (y_t - y_{\bar{t}})/2$$

$$\Delta y = q(y_l - y_h) = q\Delta y_{lh}$$



in the laboratory frame

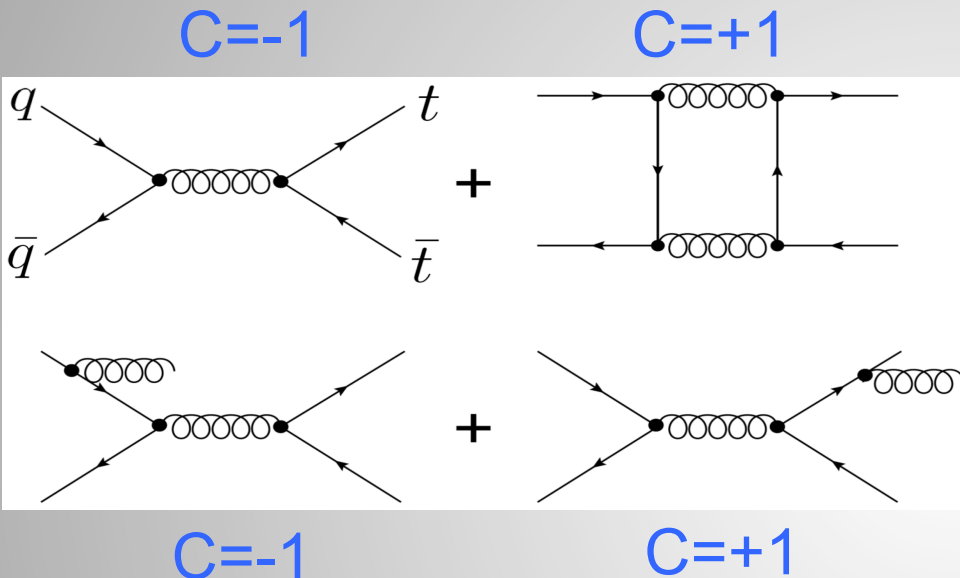


$$A_{\text{FB}}^t = \frac{N(\Delta y > 0) - N(\Delta y < 0)}{N(\Delta y > 0) + N(\Delta y < 0)} = \frac{N(q\Delta y_{lh} > 0) - N(q\Delta y_{lh} < 0)}{N(q\Delta y_{lh} > 0) + N(q\Delta y_{lh} < 0)}$$

Other asymmetries...

$$A_{\text{FB}}^{p\bar{p}} = \frac{\sigma[y_t^{p\bar{p}} > 0] - \sigma[y_t^{p\bar{p}} < 0]}{\sigma[y_t^{p\bar{p}} > 0] + \sigma[y_t^{p\bar{p}} < 0]} \quad A_C^t = \frac{\sigma_t[y_t > 0] - \sigma_{\bar{t}}[y_t > 0]}{\sigma_t[y_t > 0] + \sigma_{\bar{t}}[y_t > 0]} \quad A_C^t = A_{\text{FB}}^t \Rightarrow CP$$

Standard Model (QCD) contribution to A_{FB}^t



$$A_{FB}^{SM} = \frac{\sigma_{SM-NLO}^F - \sigma_{SM-NLO}^B}{\sigma_{SM-NLO}^F + \sigma_{SM-NLO}^B}$$

(vanishing at LO)

MCFM for SM ($m_t=172.5\text{GeV}$, PDF=CTEQ) @ NLO : $A_{FB}^t = 0.058 \pm 0.009$


Ahrens *et al.* (2010) obtain ($m_t=173.1\text{GeV}$, PDF=MSTW) :

@ NLO : $A_{FB}^t = 0.067^{+0.006}_{-0.004}$ @ NNLO-approx : $A_{FB}^t = 0.064^{+0.009}_{-0.007}$ $0.2 < \mu_f / \text{TeV} < 0.8$

=> $A_{FB}^t [M_{tt} > 450\text{GeV}]$ anomaly probably not fully explained by QCD errors ~ 0.01

Measurements of A_{FB}^t at Tevatron

now 5.1fb⁻¹: see F.Badaud's talk

07-2010 D0 in the lepton+jets channel with **(0.9fb⁻¹ then) 4.3fb⁻¹** 
(*ttbar frame, not unfolded = no subtracting bckgrd & effic. + no ttbar level*) :
 $A_{FB}^t = 0.08 \pm 0.04 \pm 0.01$ (+1.7 sigma from SM prediction)

03-2009 CDF in the lepton+jets channel with **(1.9fb⁻¹ then) 3.1fb⁻¹**
(*lab frame, unfolded*) :
 $A_{FB}^t = 0.193 \pm 0.065 \pm 0.024$ (+2.1 sigma from SM prediction)

01-2011 CDF in the dilepton channel with **5.1fb⁻¹**
(*lab frame, unfolded*) :
 $A_{FB}^t = 0.42 \pm 0.15 \pm 0.05$ (+2.3 sigma from SM prediction)
(large error => +1.7 sigma from lept.+jets channel)
(*lab frame, not unfolded*) :

$A_{FB}^t (M_{tt} < 450 \text{ GeV}) = 0.104 \pm 0.066$ (+1.6 sigma from SM prediction)

$A_{FB}^t (M_{tt} > 450 \text{ GeV}) = 0.212 \pm 0.096$ (+2.6 sigma from SM prediction)

The way to compute it...

$$A_{\text{FB}}^t = \frac{(\sigma_{SM}^F + \sigma_{RS}^F + \sigma_{inter.}^F) - (\sigma_{SM}^B + \sigma_{RS}^B + \sigma_{inter.}^B)}{(\sigma_{SM}^F + \sigma_{RS}^F + \sigma_{inter.}^F) + (\sigma_{SM}^B + \sigma_{RS}^B + \sigma_{inter.}^B)}$$

$$\Leftrightarrow A_{\text{FB}}^t = A_{\text{FB}}^{RS} \times R + A_{\text{FB}}^{SM} \times (1 - R)$$

Cao et al. (2010)

with

$$A_{\text{FB}}^{RS} = \frac{(\sigma_{RS-LO}^F + \sigma_{inter.-LO}^F) - (\sigma_{RS-LO}^B + \sigma_{inter.-LO}^B)}{(\sigma_{RS-LO}^F + \sigma_{inter.-LO}^F) + (\sigma_{RS-LO}^B + \sigma_{inter.-LO}^B)}$$

$$R = \frac{\sigma_{RS-LO}^{\text{total}} + \sigma_{inter.-LO}^{\text{total}}}{\sigma_{SM-LO}^{\text{total}} + \sigma_{RS-LO}^{\text{total}} + \sigma_{inter.-LO}^{\text{total}}}$$

ex: $\sigma_{RS-LO}^F = \sigma_{RS-LO}[\cos \theta_t^* : 0 \rightarrow 1] =$

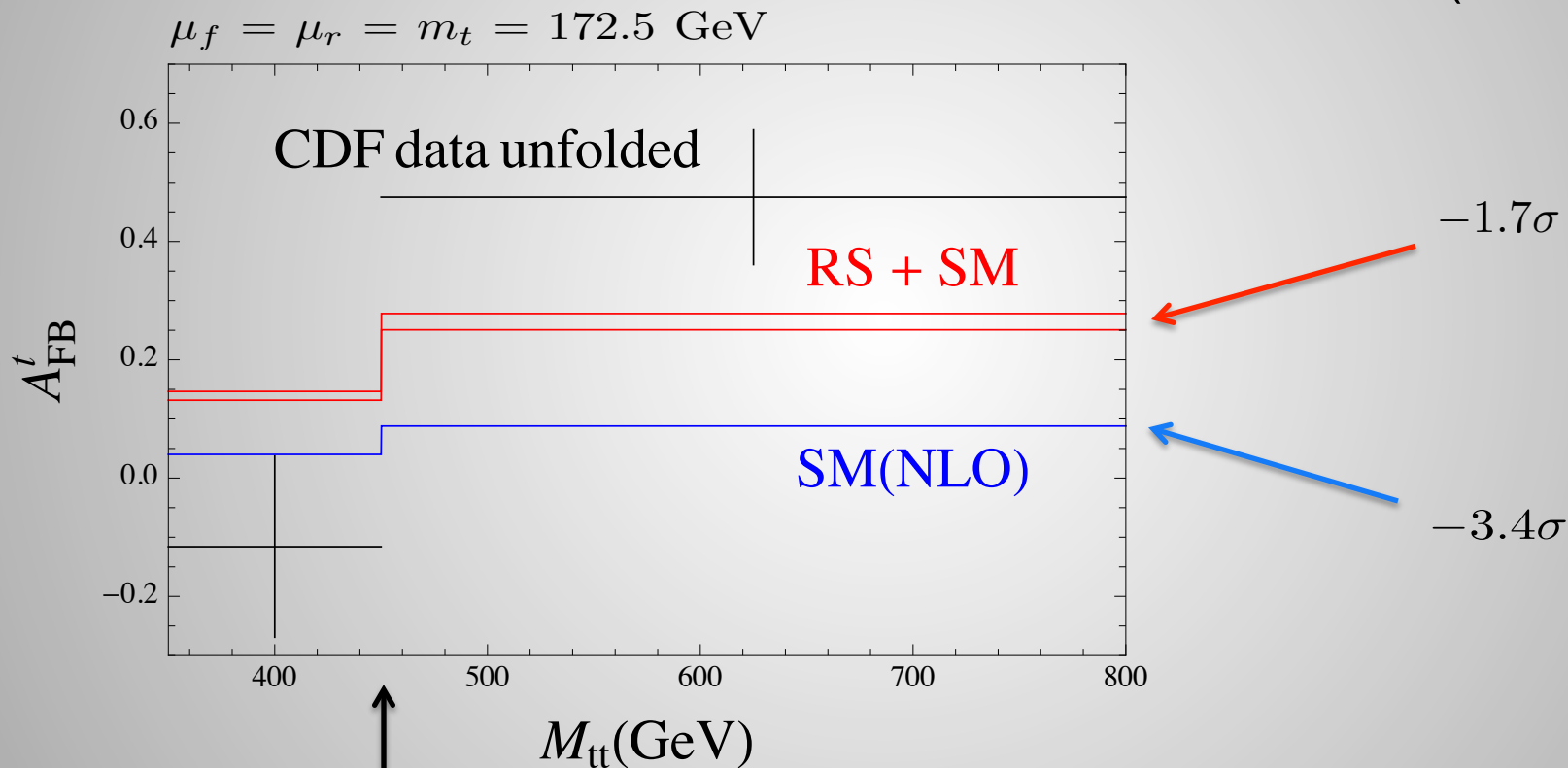
$$\sum_{ij} \int_{\tau_{min}}^{\tau_{max}} d\tau \left[\int_0^1 d \cos \theta_t^* \left(\frac{d\hat{\sigma}_{RS-LO}}{d \cos \theta_t^*}(\tau s) \right)_{ij} \right] \left\{ \int_{\tau}^1 \frac{dx}{x} f_i(x, \mu_f) f_j\left(\frac{\tau}{x}, \mu_f\right) \right\}$$

$$\tau_{min/max} = \hat{s}_{min/max}/s$$

MSTW-2008-NLO

Looking at the effect of MSTW uncertainties [*@ 90% C.L.*]...

(*ttbar* frame)



$M_{\text{tt}} = 450 \text{ GeV}$

no significant dependence as well on μ_f, μ_r and m_t

$$1/(t - M_{KK}^2) \quad -t \leq M_{KK}^2 \quad t = -M_{jj}^2/2 \quad M_{jj} = \sqrt{2}M_{KK} \sim 2 \text{ TeV}$$

$$\cos \theta^* = 0$$

KK gluon produces less than 10% deviation

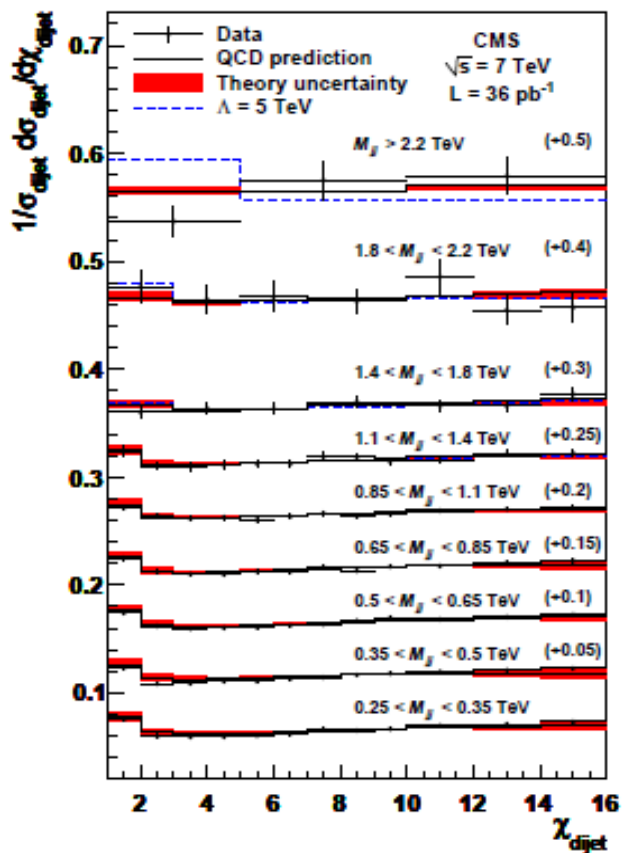
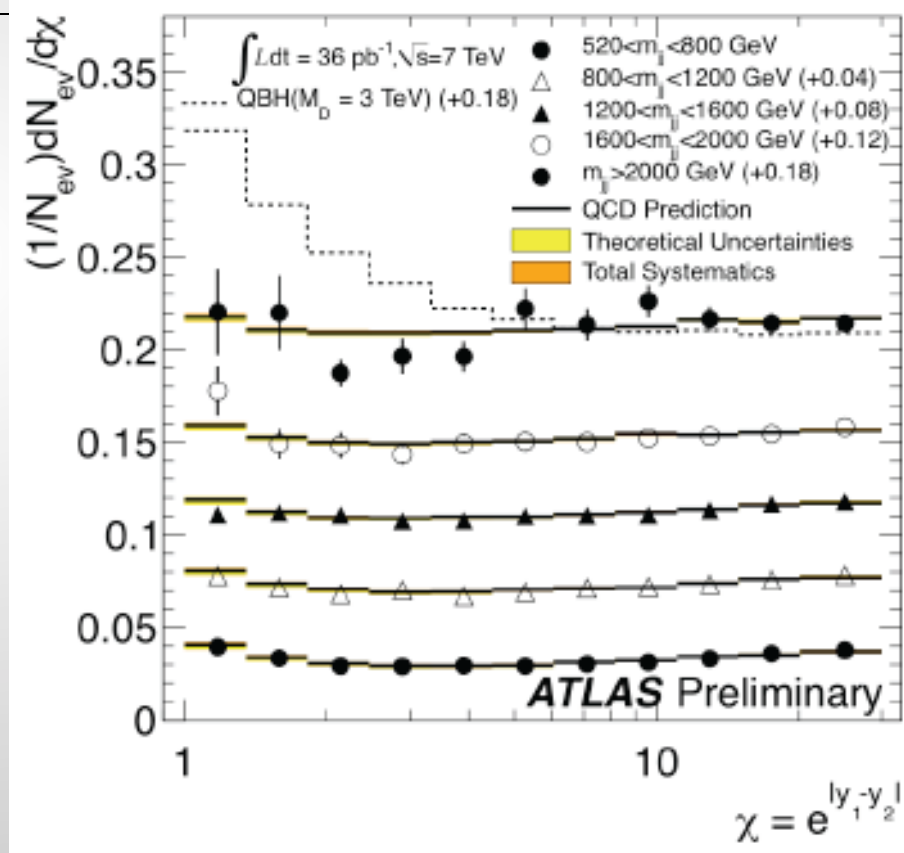


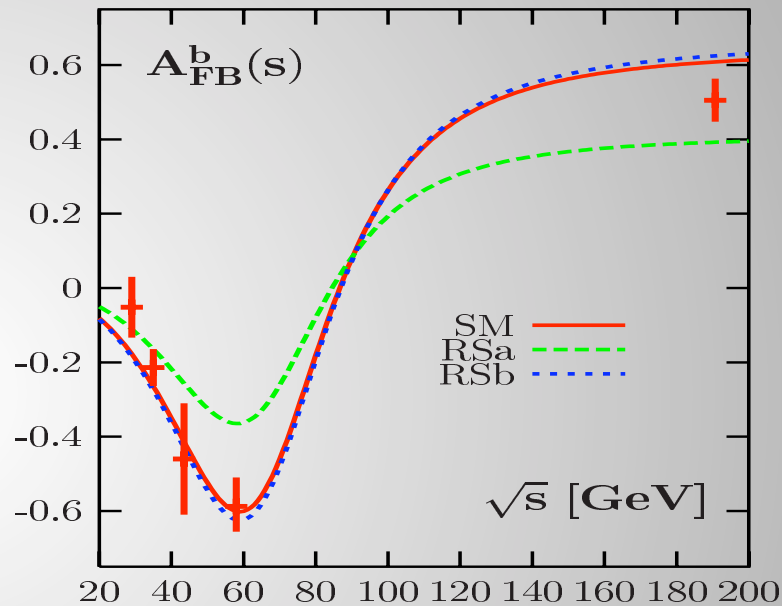
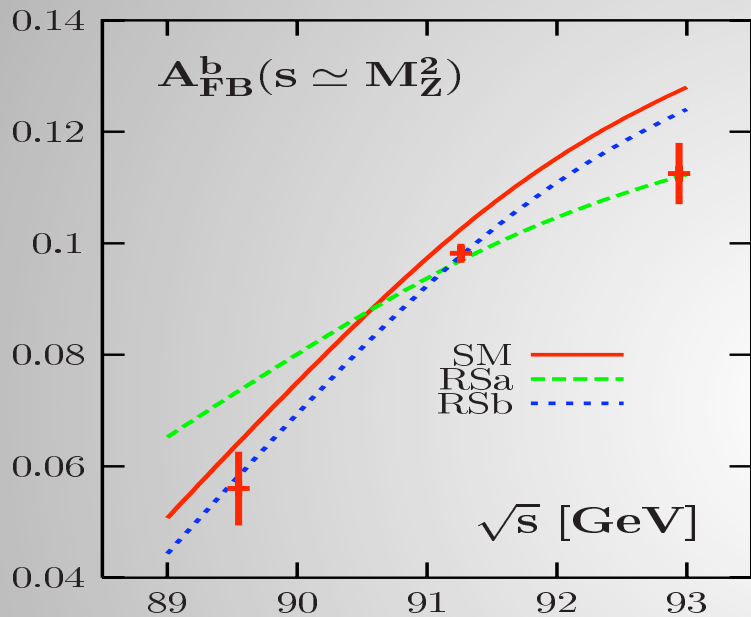
Figure 1: Normalized dijet angular distributions in several M_{jj} ranges, shifted vertically by the additive amounts given in parentheses in the figure for clarity. The data points include statistical and systematic uncertainties. The results are compared with the predictions of pQCD at NLO (solid histogram) and with the predictions including a contact interaction term of compositeness scale $\Lambda = 5 \text{ TeV}$ (dashed histogram). The shaded band shows the effect on the NLO pQCD predictions due to μ_r and μ_f scale variations and PDF uncertainties, as well as the uncertainties from the non-perturbative corrections added in quadrature.



ATLAS Preliminary

$$\chi = e^{ly-y_2}$$

Global A_{FB}^b fit @ and off the Z pôle :




SM : $\chi^2 = 24$ RSa : $\chi^2 = 20$ RSb : $\chi^2 = 14$

b_R under $SU(2)_L \times SU(2)_R \times U(1)_X$:

$$\begin{cases} Q_X = (B-L)/2 \Rightarrow I_R^3 = -1/2 & \text{RSa} \\ Q_X = -5/6 \Rightarrow I_R^3 = +1/2 & \text{RSb} \end{cases}$$

What about the **whole** integrated top quark **asymmetry** and **cross section** ?

☺ **Tevatron data** [5] : 0.158 ± 0.075 [5] CDF Collaboration
SM [NLO] [5] : $0.058 \pm 0.009 (-1.33\sigma)$ arXiv:1101.0034
RS+SM : $0.189 \pm 0.010 (+0.42\sigma)$  improves

☺ Theoretical (HATHOR): $\sigma(p\bar{p} \rightarrow t\bar{t}) = 6.62 \pm 1 \text{ pb}$
 $\mu_R = \mu_F = m_t = 172.5 \text{ GeV}$
MSTW PDF NNLO

Experimental (Tevatron): $7.50 \pm 0.48 \text{ pb}$ CDF Collaboration, Note 9913,
Run II, October 2009.

 OK as heavy KK gluon with broad resonance