

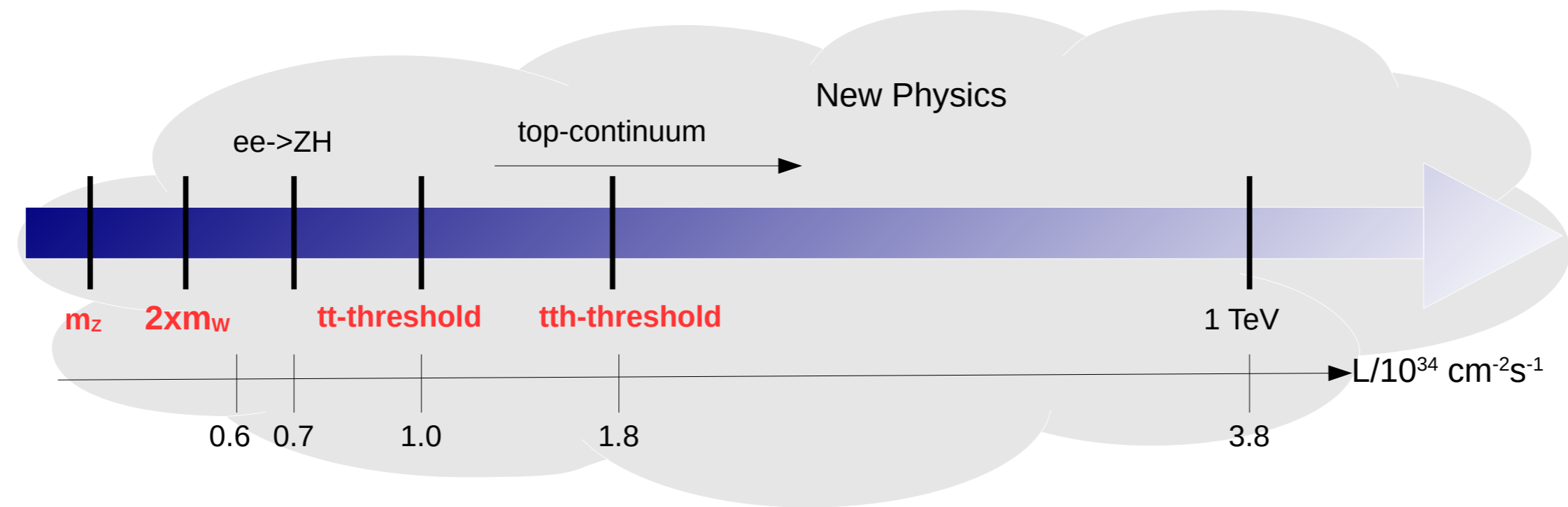
Precision electroweak capabilities of ILC

Roman Pöschl



Based on material of a number of distinguished colleagues

ECFA Higgs Study WG1 PREC Meeting – March 2022

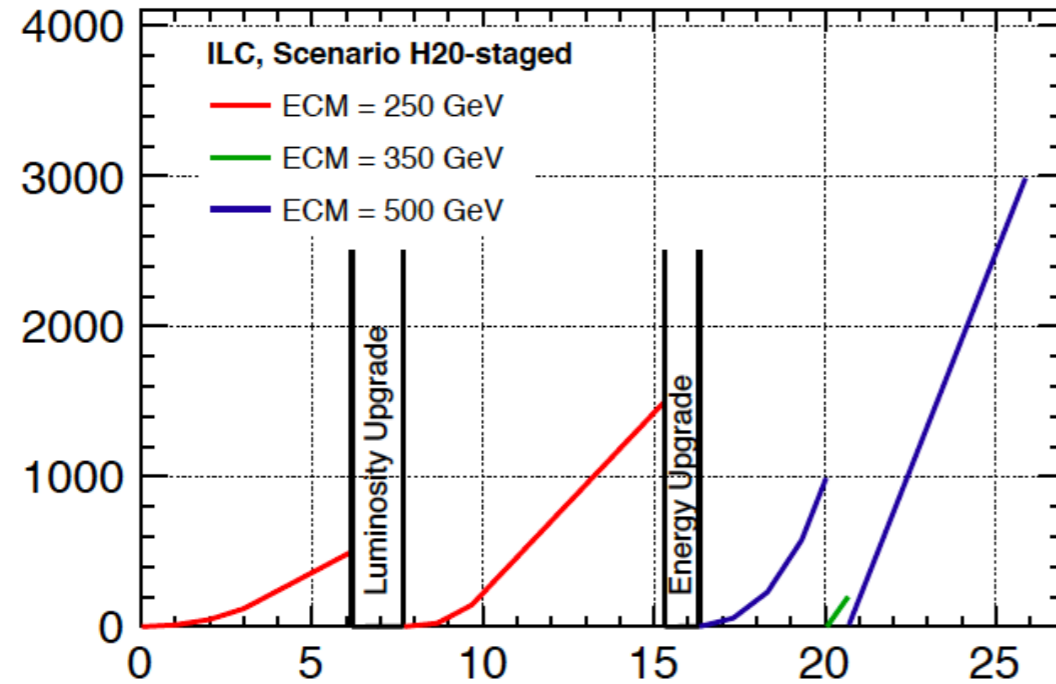


- All Standard Model particles within reach of planned e+e- colliders
- High precision tests of Standard Model over wide range to detect onset of New Physics
- Machine settings can be “tailored” for specific processes
 - Centre-of-Mass energy
 - Beam polarisation (straightforward at linear colliders)

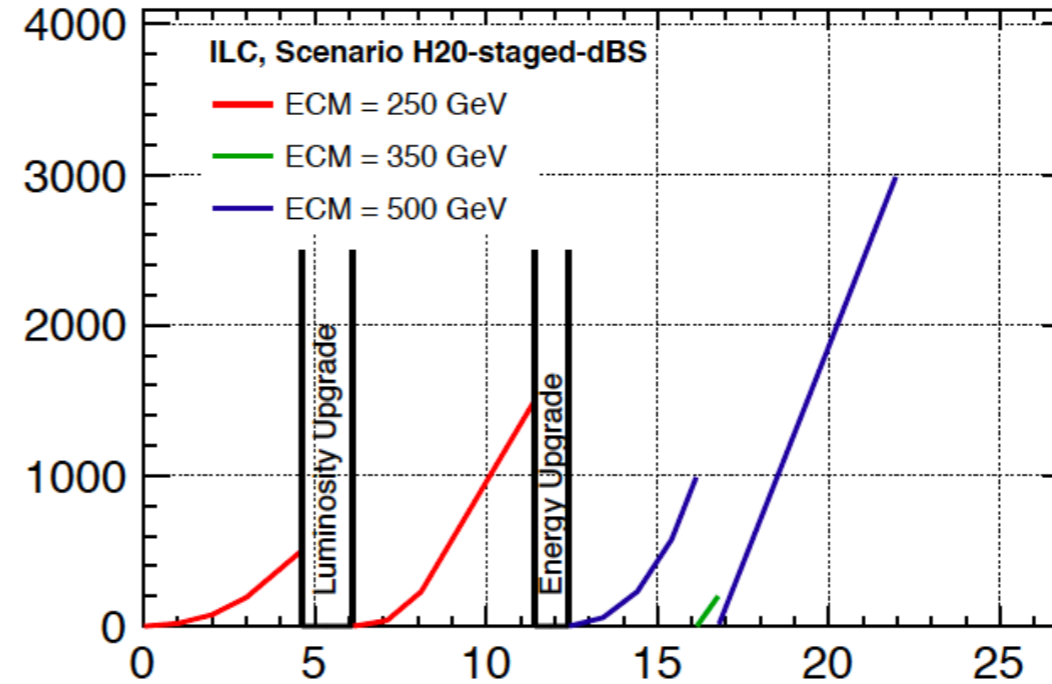
$$\sigma_{P,P'} = \frac{1}{4} [(1 - PP')(\sigma_{LR} + \sigma_{RL}) + (P - P')(\sigma_{RL} - \sigma_{LR})]$$

- **Background free** searches for BSM through beam polarisation

Integrated Luminosities [fb^{-1}]



Integrated Luminosities [fb^{-1}]



In 2019 – Revision of capabilities to run on the Z Pole - GigaZ

	$\text{sgn}(P(e^-), P(e^+)) =$				sum
	(-,+)	(+,-)	(-,-)	(+,+)	
luminosity [fb^{-1}]	40	40	10	10	
$\sigma(P_{e^-}, P_{e^+})$ [nb]	83.5	63.7	50.0	40.6	
Z events [10^9]	2.4	1.8	0.36	0.29	4.9
hadronic Z events [10^9]	1.7	1.3	0.25	0.21	3.4

- Pole running can happen before and after the luminosity upgrade
- Further details see arxiv: 1908.08212

Track momentum: $\sigma_{1/p} < 5 \times 10^{-5}/\text{GeV}$ (1/10 x LEP)

(e.g. Measurement of Z boson mass in Higgs Recoil)

Impact parameter: $\sigma_{d0} < [5 \oplus 10/(p[\text{GeV}]\sin^{3/2}\theta)] \mu\text{m}$ (1/3 x SLD)

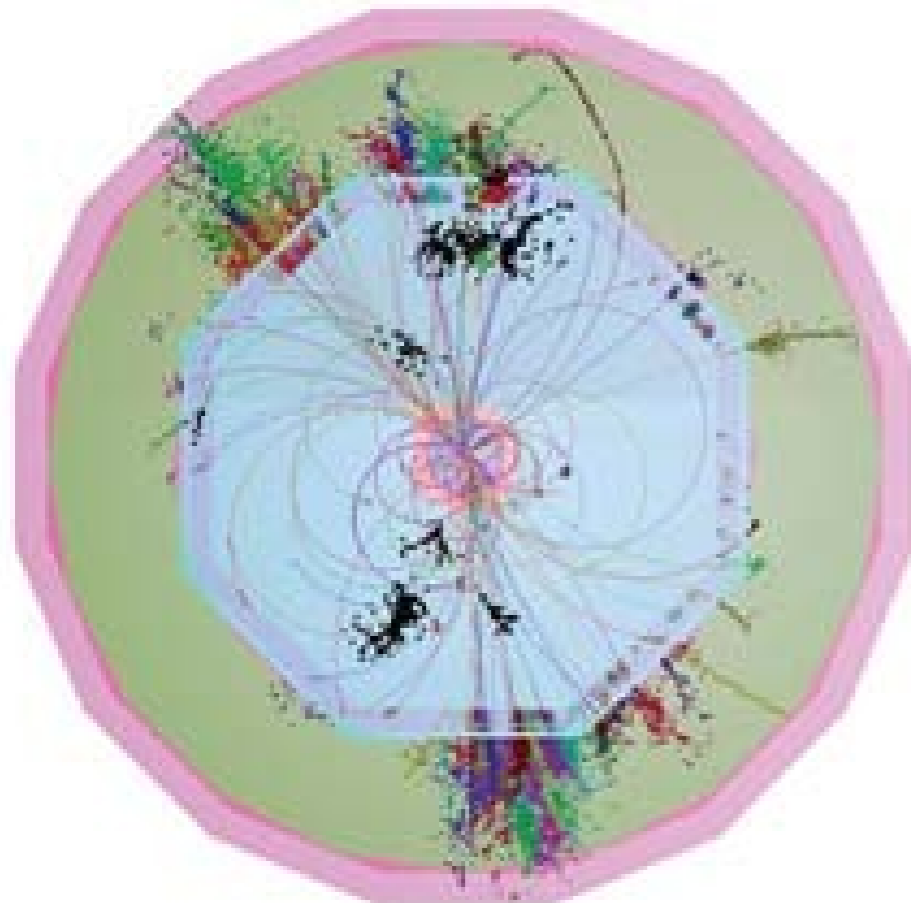
(Quark tagging c/b)

Jet energy resolution : $dE/E = 0.3/(E(\text{GeV}))^{1/2}$ (1/2 x LEP)

(W/Z masses with jets)

Hermeticity : $\theta_{\min} = 5 \text{ mrad}$

(for events with missing energy e.g. SUSY, quark charge measurement)



Final state will comprise events with a large number of charged tracks and jets(6+)

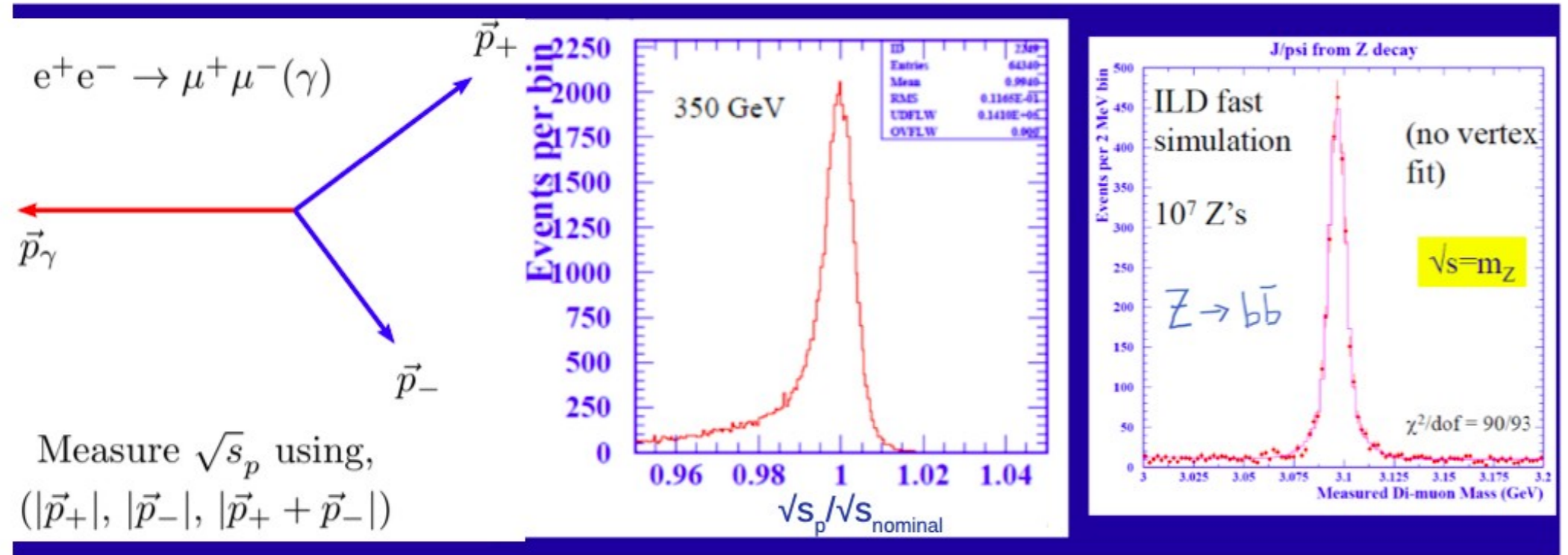
- High granularity
- Excellent momentum measurement
- High separation power for particles
- Particle Flow Detectors

Core Program				
Observable	M_H	M_t	M_W	M_X
Method	Recoil mass	Scan	Reconstruction	Scan?
Best \sqrt{s} [GeV]	250	350	250	Highest?
Current precision [MeV]	170	300	12	–
Target precision [MeV]	10	20	2	?
\sqrt{s} contribution [MeV]	3	6	0.5	?
\sqrt{s} uncertainty goal [ppm]	100	200	10	100?

Ultimate Impact/Reach				
Observable	M_W	M_Z	Γ_Z	A_{LR}
Method	Scan	Scan	Scan	Count/Scan
Best \sqrt{s} [GeV]	161	91	91	91
Current precision	12	2.1	2.3	1.9×10^{-3}
Target precision	2 MeV	0.2 MeV	0.11 MeV	3.5×10^{-5}
\sqrt{s} contribution	0.8 MeV	0.2 MeV	small	1.8×10^{-5}
\sqrt{s} uncertainty goal [ppm]	10	2	5*	10

Today

Use dilepton momenta, with $\sqrt{s}_p \equiv E_+ + E_- + |\vec{p}_{+-}|$ as \sqrt{s} estimator.



Tie detector p -scale to particle masses (know J/ψ , π^+ , p to 1.9, 1.3, 0.006 ppm)

Measure $\langle \sqrt{s} \rangle$ and luminosity spectrum with same events. Expect statistical uncertainty of 1.0 ppm on p -scale per 1.2M $J/\psi \rightarrow \mu^+\mu^-$ (4×10^9 hadronic Z's).

- excellent tracker momentum resolution - can resolve beam energy spread.
- feasible for $\mu^+\mu^-$ and e^+e^- (and ... 4l etc).

Further remarks:

- Realistic study has to take real beam energy spread and crossing angle into account
 - Ongoing
- Momentum scale can be further constrained by with K_0 and Λ using Armenteros-Podolanski Method
 - See e.g. 2012.03620
- 10ppm at $s=250$ GeV and 1ppm on Z pole seem to be in reach

W Mass from ...:

- Constrained WW reconstruction
- Hadronic mass from hadronic W decays
- Lepton endpoints: $m_W^2 = E_l(E_b - E_l)$, $E_l = E_b(1 \pm \beta_W)/2$
- Dilepton pseudo mass from constrained fit
- Polarised W scan

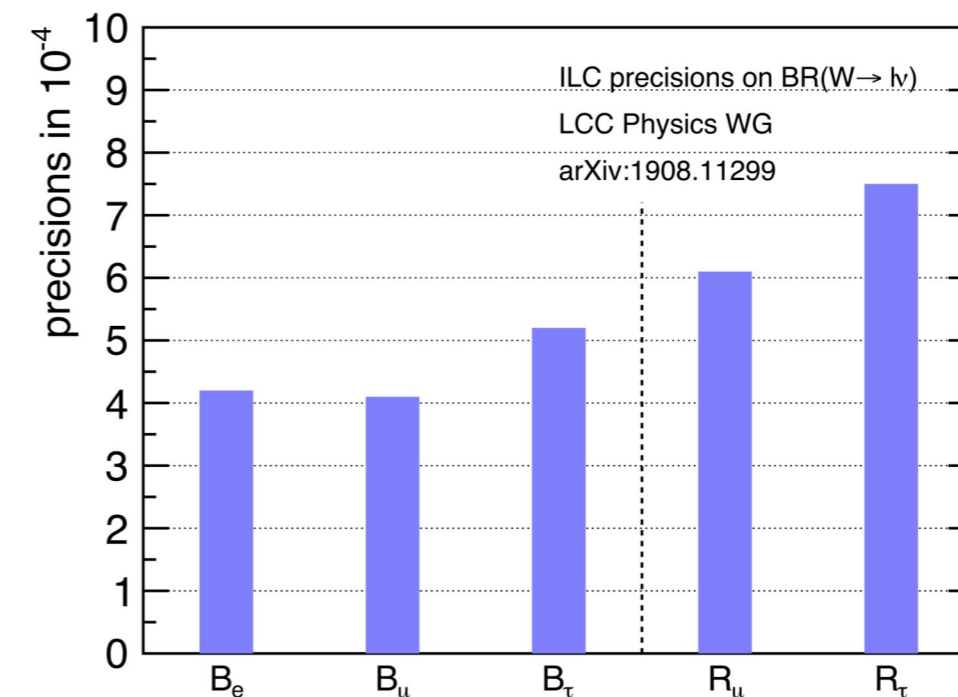
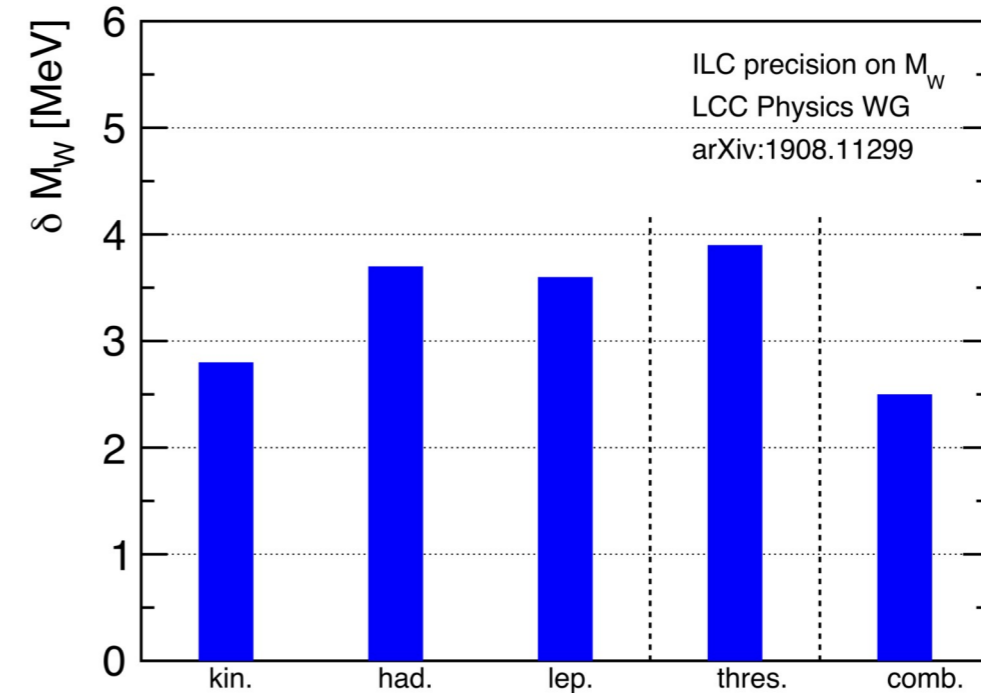
$$\Delta m_W (MeV) = 2.4(stat.) \oplus 3.2(syst.) \oplus 0.8(\sqrt{s}) \oplus \text{theory}$$

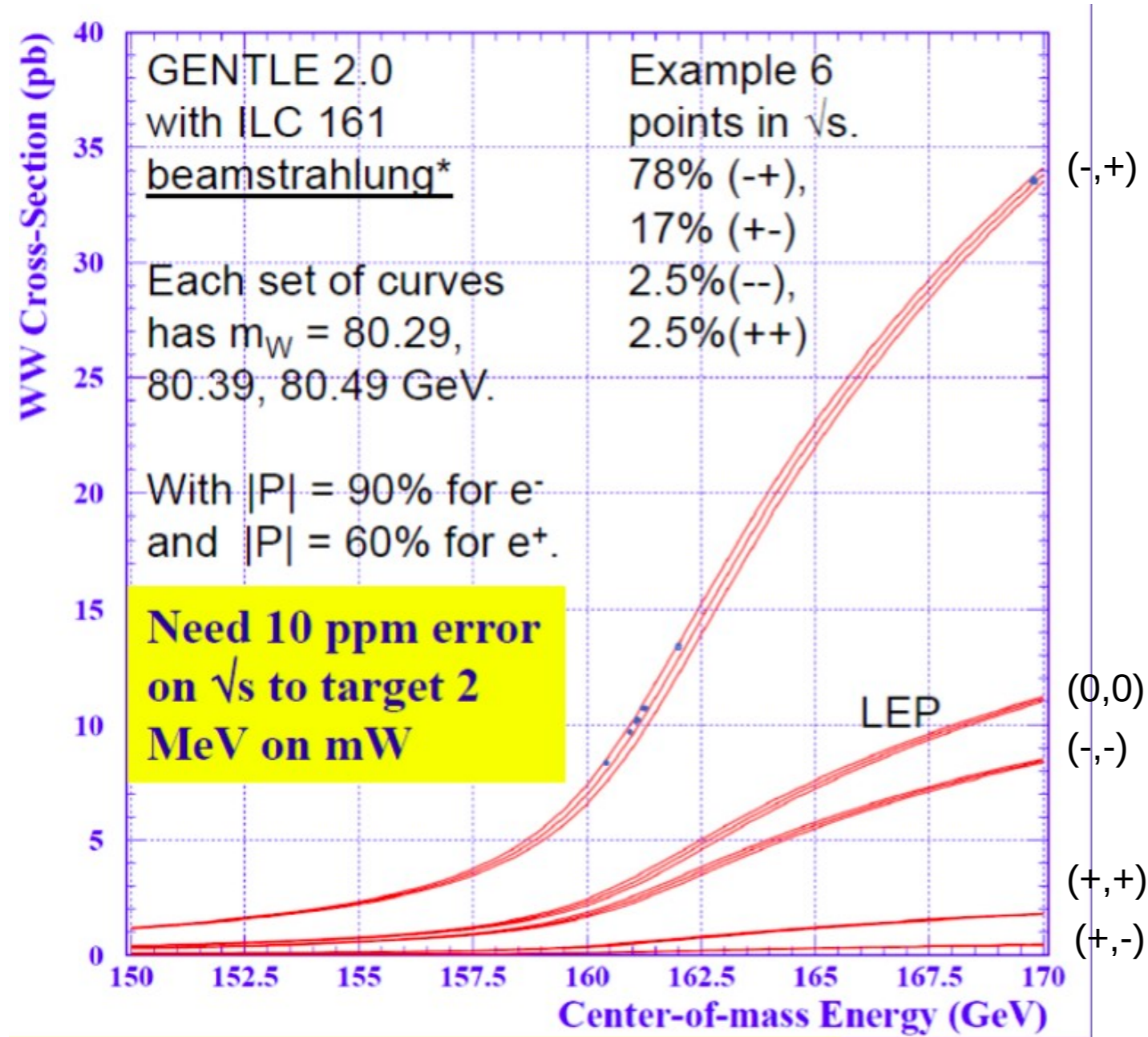
Branching ratios

From simultaneous fit to all 10 decay combinations

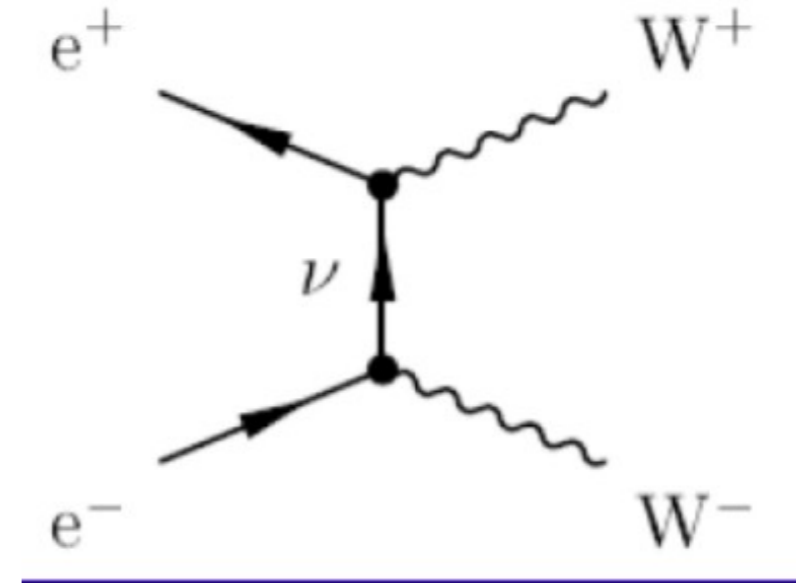
$$\Rightarrow \sigma_{tot} \text{ and } B_{e,\mu,\tau} \text{ and } B_{had} = 1 - B_e - B_\mu - B_\tau$$

W width: $\Delta\Gamma_W = 3.2 \text{ MeV}$

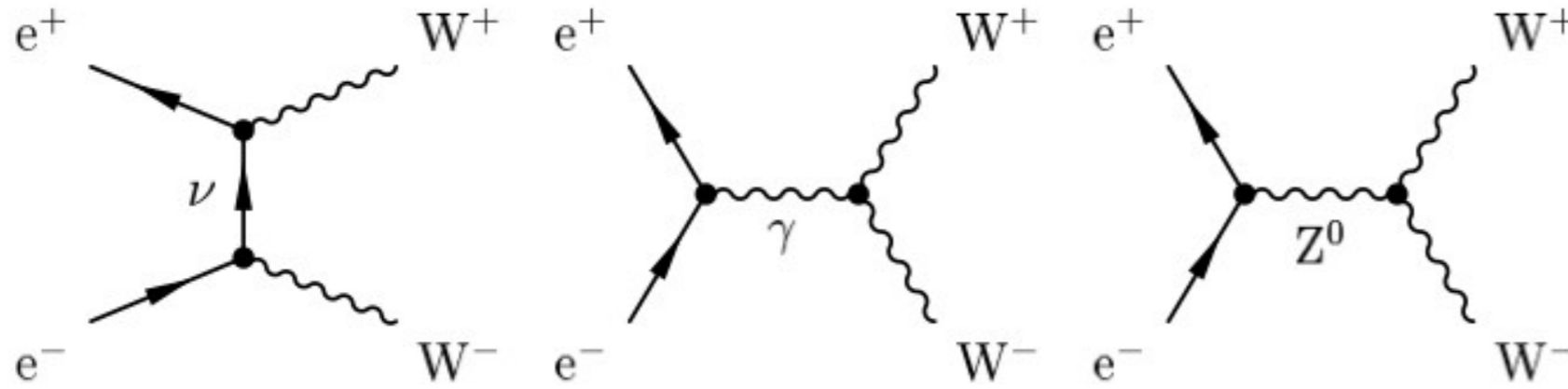




G. Wilson



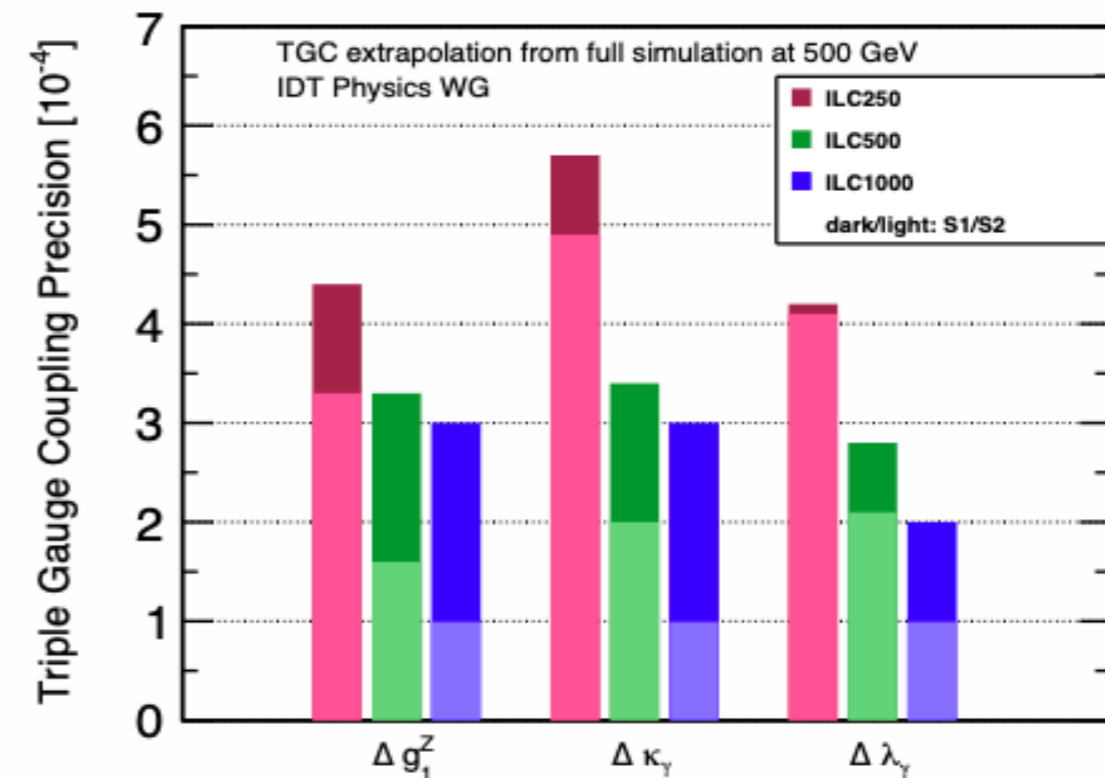
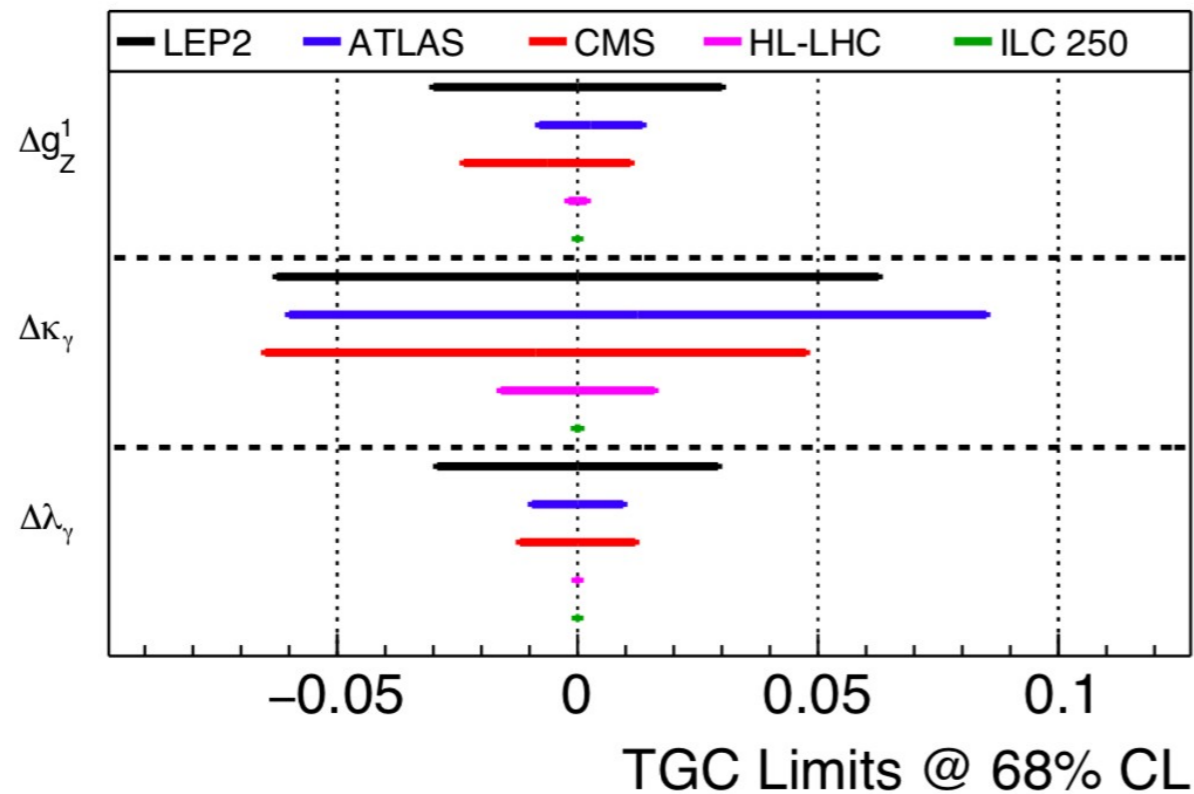
- Robust method
- Beam polarisation essential to control background
- Need extreme good control of beam energy



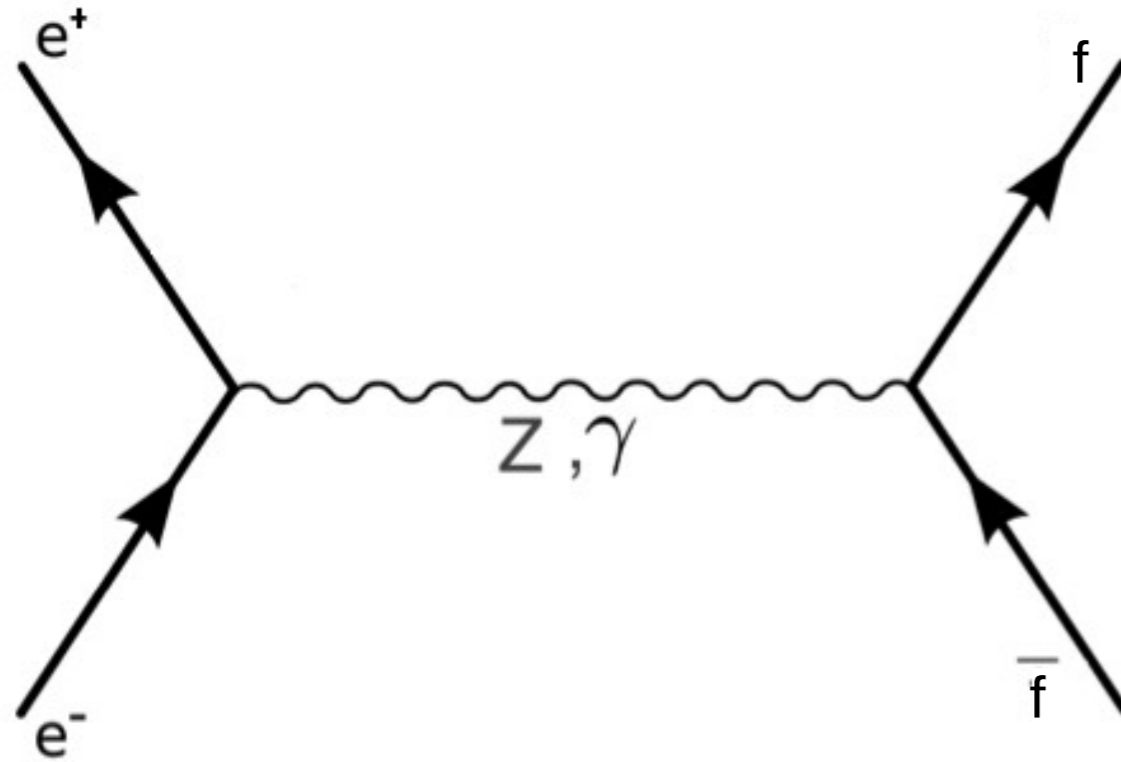
- Sensitivity to triple and quartic gauge Boson couplings (TGC and QGC)
- Observables depend strongly on beam polarisation

=> Enrich different helicity modes of W
 => Disentangling of couplings to Z and γ
 => in situ measurement of beam polarisation (and luminosity)

Limits on Triple Gauge Couplings@250 GeV



J. List, ILC Snowmass White Paper



$$\frac{d\sigma}{d\cos\theta}(e_L^- e_R^+ \rightarrow f \bar{f}) = \Sigma_{LL}(1 + \cos\theta)^2 + \Sigma_{LR}(1 - \cos\theta)^2$$

$$\frac{d\sigma}{d\cos\theta}(e_R^- e_L^+ \rightarrow f \bar{f}) = \Sigma_{RL}(1 - \cos\theta)^2 + \Sigma_{RR}(1 + \cos\theta)^2$$

*add term $\sim \sin^2\theta$ in case of non-relativistic fermions e.g. top close to threshold

- Σ_{IJ} are helicity amplitudes that contain couplings g_L, g_R (or F_V, F_A)
- $\Sigma_{IJ} \neq \Sigma_{I'J'} \Rightarrow$ (characteristic) asymmetries for each fermion
- Forward-backward in angle, general left-right in cross section
- **All four helicity amplitudes for all fermions only available with polarised beams**

Helicity amplitudes can be analysed in several ways (not mutually exclusive):

Oblique Parameters W, Z:

$$Q_{eifj} = Q_e^\gamma Q_f^\gamma + \frac{g_{e_i}^Z g_{f_j}^Z}{\sin^2 \theta_W \cos^2 \theta_W} \frac{s}{s - M_Z^2 + i\Gamma_Z M_Z} + \frac{s}{m_W^2} f_{i,j}(W, Y)$$

Contact interactions with e.g. compositeness scale Λ :

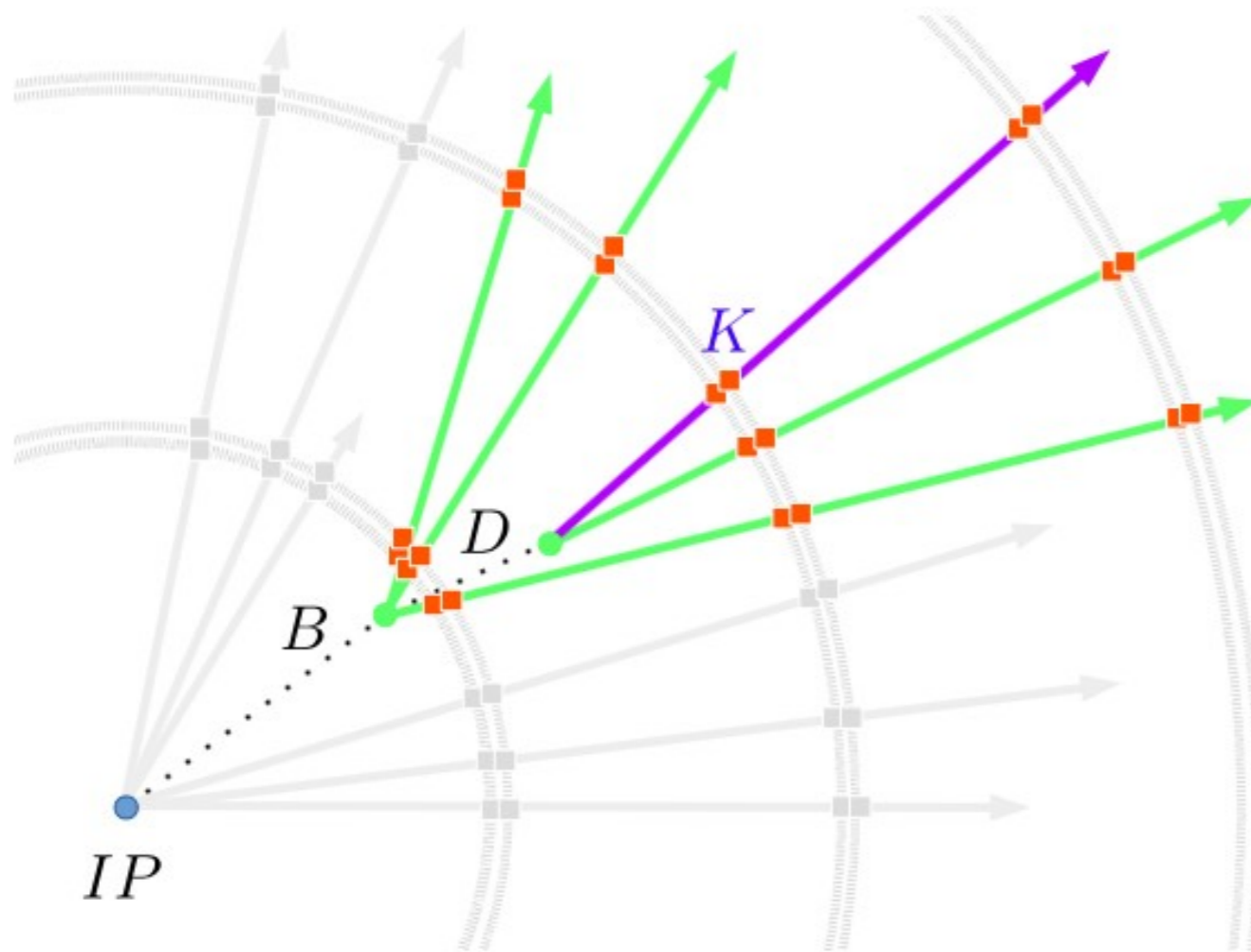
$$Q_{eifj} = Q_e^\gamma Q_f^\gamma + \frac{g_{e_i}^Z g_{f_j}^Z}{\sin^2 \theta_W \cos^2 \theta_W} \frac{s}{s - M_Z^2 + i\Gamma_Z M_Z} + \frac{g_{contact}^2}{2\Lambda^2} \eta_{eifj}$$

New propagators in concrete models of new physics:

$$Q_{eifj} = Q_e^\gamma Q_f^\gamma + \frac{g_{e_i}^Z g_{f_j}^Z}{\sin^2 \theta_W \cos^2 \theta_W} \frac{s}{s - M_Z^2 + i\Gamma_Z M_Z} + \sum \frac{g_{e_i}^{Z'} g_{f_j}^{Z'}}{\sin^2 \theta_W \cos^2 \theta_W} \frac{s}{s - M_{Z'}^2 + i\Gamma_{Z'} M_{Z'}}$$

Always with I,j being the helicities of the initial state electron e and the final state fermion f

Remark: Have to exchange g-> Q to be consistent with conventions

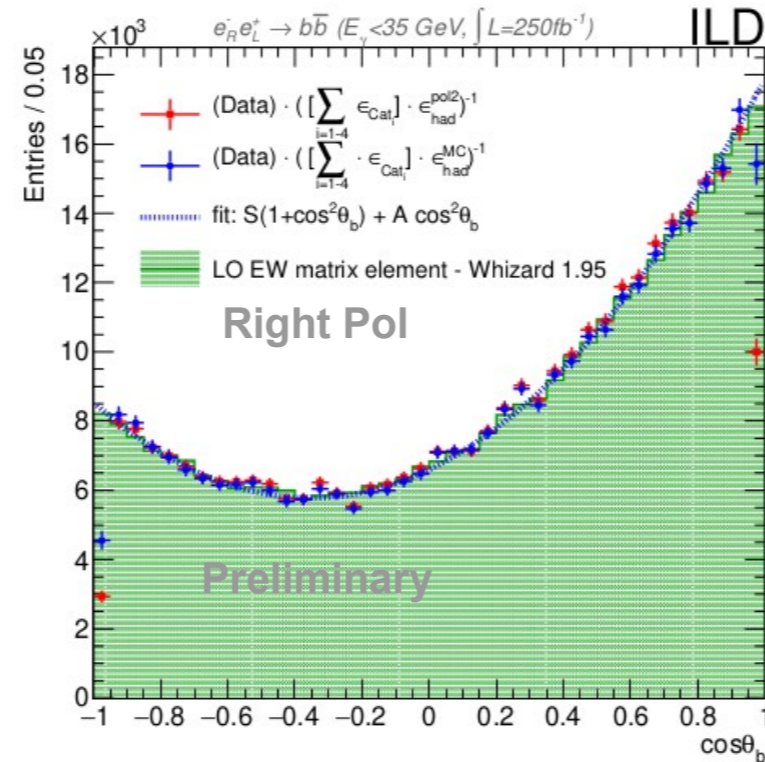
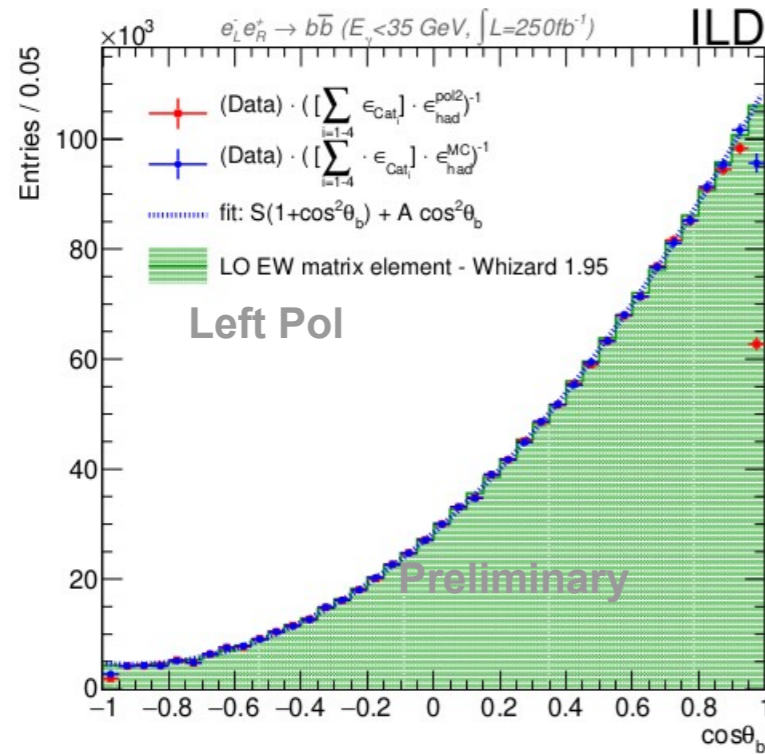


- flavor tagging
- b-quark charge measurement
 - Important for top quark studies, indispensable for $ee \rightarrow bb$
- Control of migrations:
 - Correct measurement of vertex charge
 - Requires excellent forward acceptance
 - Kaon identification by dE/dx (and more)
- ILC/ILD can base the entire measurements on double Tagging and vertex charge
 - LEP/SLC had to include single tags and semi-leptonic events

PhD thesis: S. Bilokin
 A. Irles

Full simulation study within ILD Concept allows for educated guess on uncertainties on Z-Pole

Arxiv:1709.04289, ILD Paper in progress
A. Irls, SUSY2021



Excellent agreement between predicted and reconstructed distributions

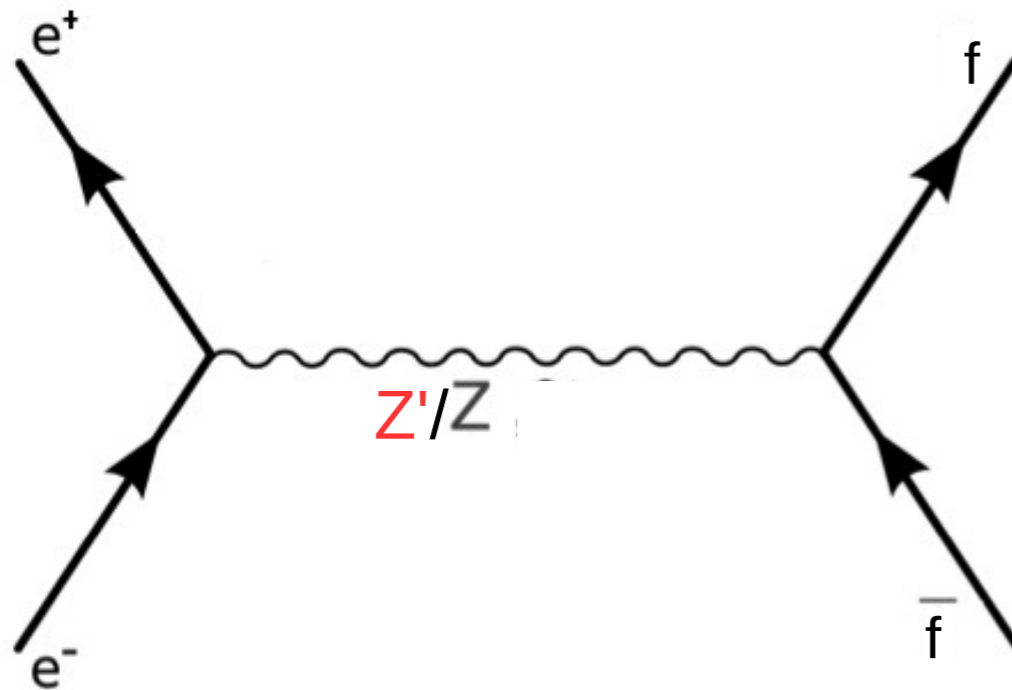
- Gap between red dots and green histogram = acceptance drop.
- Blue dots = corrected acceptance
- The fit is restricted to $|\cos\theta_b| < 0.8$
 - Minimal impact of the corrections

Systematic uncertainties under scrutiny:

- Selection and background rejection
- quark tagging/mistagging (modélisation, QCD, correlations)
- Luminosity
- Polarisation

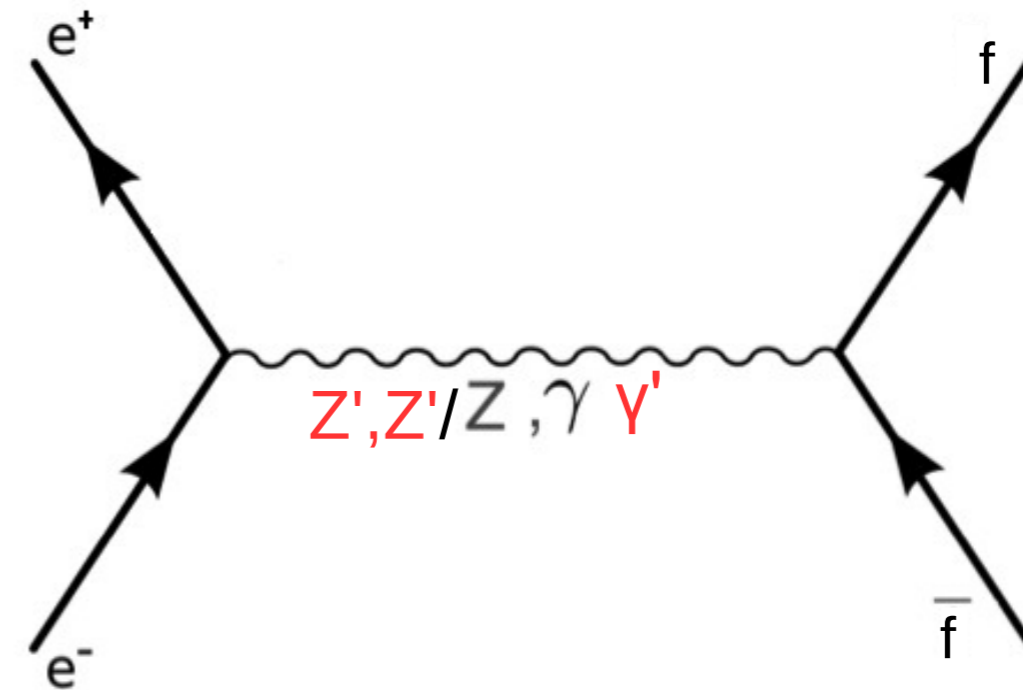
Additional complication in continuum: Rejection of ISR events – Uncertainty $\sim 5 \times 10^{-4}$ (doesn't apply on Z-pole)

On the Z-pole



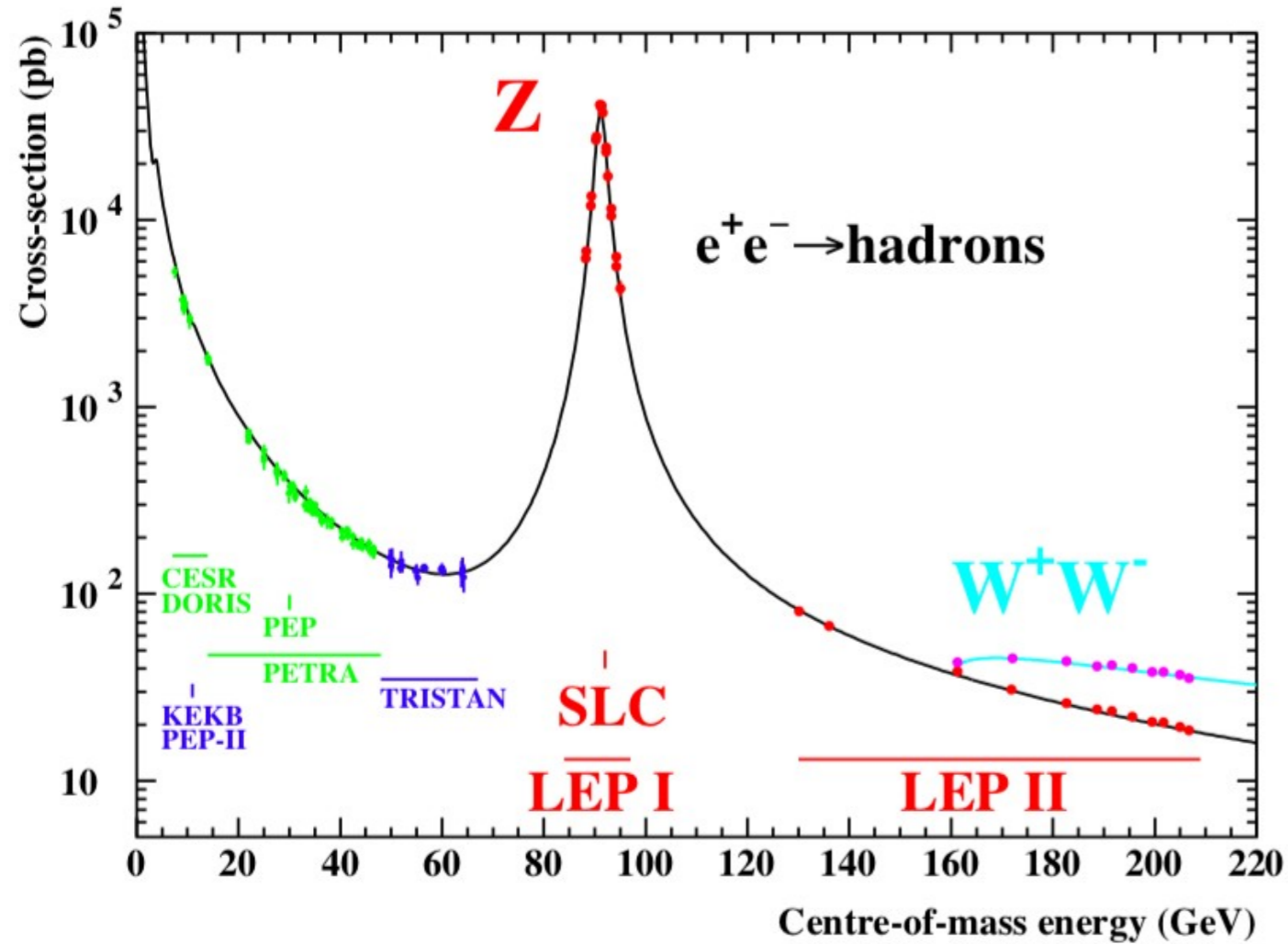
- **ILC/GigaZ with $\sim 10^9 Z$**
- Sensitivity to Z/Z' mixing
- Sensitivity to vector (and tensor?) couplings of the Z
 - the photon does not “disturb”

Above the Z-pole



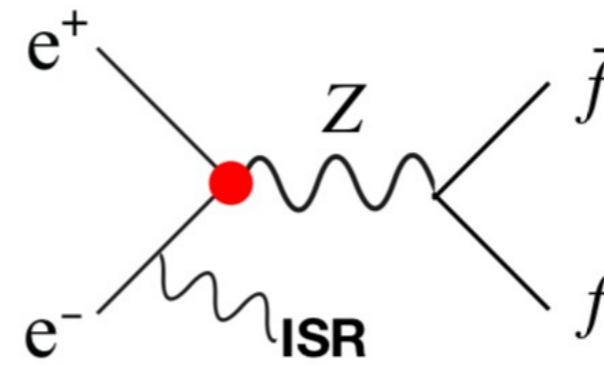
- Sensitivity to interference effects of Z and photon!!
- Measured couplings of photon and Z can be influenced by new physics effects
- Interpretation of result is greatly supported by precise input from Z pole

Running on Z pole "GigaZ"



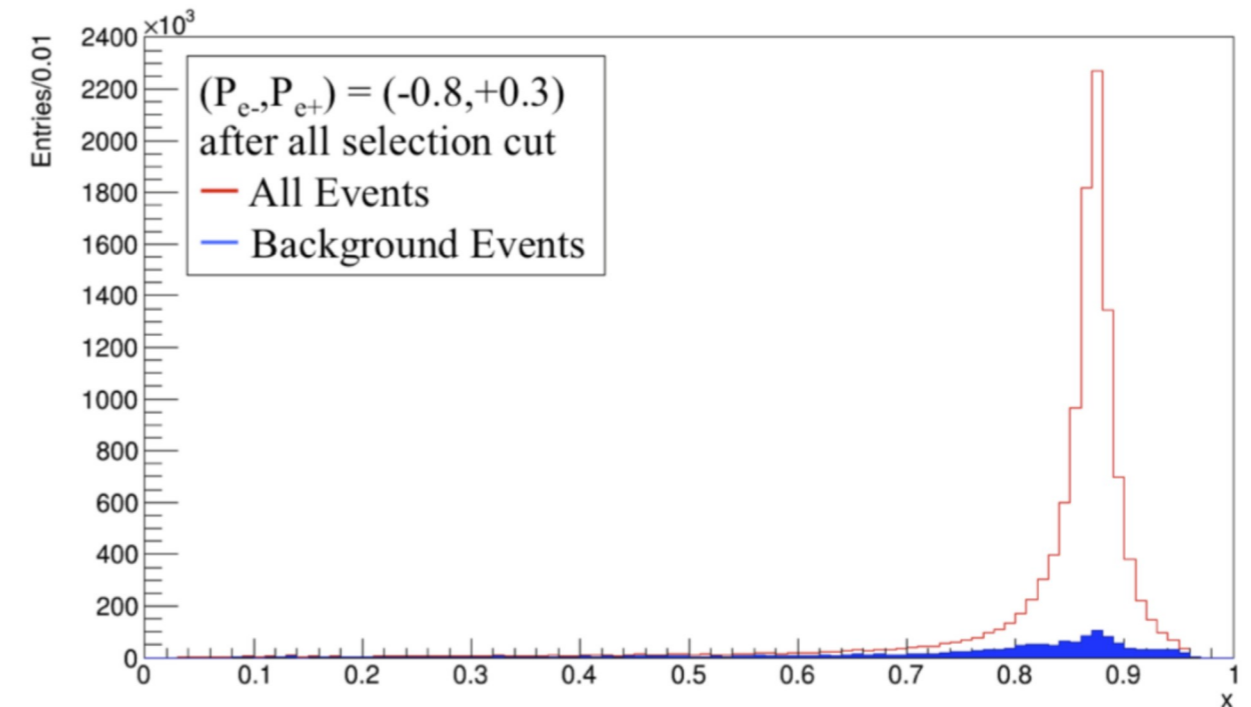
- Around 5×10^9 Z events (250xLEP)
- With beam polarisation
 $\sim 30 \times 250 = 7500$ LEP!

Radiative return at higher energies



$$m_Z^2 = \frac{1 - |\beta|}{1 + |\beta|} \cdot s$$

$$\beta = \frac{|\sin(\theta_1 + \sin \theta_2)|}{\sin \theta_1 + \sin \theta_2}$$



- $\sim 10^8$ events at 250 GeV with 2 ab^{-1}
- Beam polarisation

Partial fermion width:

$$R_f = \frac{N_f}{N_{had}} = \frac{(g_f^L)^2 + (g_f^R)^2}{\sum_{i=1}^{n_q} [(g_i^L)^2 + (g_i^R)^2]}$$

- Sensitive to sum of coupling constants
- Available at linear and circular colliders

Left-right asymmetry:

$$A_{LR} = \frac{1}{|\mathcal{P}_{eff.}|} \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R} = \mathcal{A}_e = \frac{(g_f^L)^2 - (g_f^R)^2}{(g_i^L)^2 + (g_i^R)^2} \sim 1 - 4\sin^2 \theta_{eff.}^l$$

- Direct sensitivity to Zee vertex
- Only available at linear colliders due to beam polarisation
- Circular colliders need auxiliary measurement
 - e.g. $P_T \sim A_e$

Forward-backward asymmetry:

$$A_{FB}^f = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3}{4} \mathcal{A}_e \mathcal{A}_f \quad \text{for } \mathcal{P}_e = 0.$$

- “Classical” observable to study P-violating effects in ee->ff
- Available at circular and linear colliders
- Without beam polarisation interpretation is always model dependent

Left-right-forward-backward asymmetry:

$$A_{FB,LR}^f = \frac{(\sigma_F - \sigma_B)_L - (\sigma_F - \sigma_B)_R}{(\sigma_F + \sigma_B)_L + (\sigma_L + \sigma_l)_R} = -\frac{3}{4} \mathcal{A}_f$$

- Combination of asymmetries above
- Only available linear colliders due to beam polarisation
- Direct and model independent measurement of A_f

$$\mathcal{A}_e = \frac{(g_{eL}^Z)^2 - (g_{eR}^Z)^2}{(g_{eL}^Z)^2 + (g_{eR}^Z)^2} = \frac{2g_{eV}/g_{eA}}{1 + (g_{eV}/g_{eA})^2} \quad \text{with } g_{eV}/g_{eA} = 1 - 4\sin^2\theta_{\text{eff}}^{\ell}.$$

How to determine \mathcal{A}_e ?

Left Right Asymmetry
 Requires polarised beams

$$A_{LR} = \frac{1}{|\mathcal{P}_{\text{eff}}|} \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R} = \mathcal{A}_e$$

Available at LC

Using all hadronic decays of Z!!!

Forward backward asymmetry
 Has to assume lepton universality!!!

$$A_{FB}^f = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3}{4} \mathcal{A}_e \mathcal{A}_f \quad \text{for } \mathcal{P}_e = 0.$$

Available at LC, CC

Used e.g. In EPJC (2019) 79:474
 with $f = \mu$

Final state polarisation (r,l)
 e.g. with τ

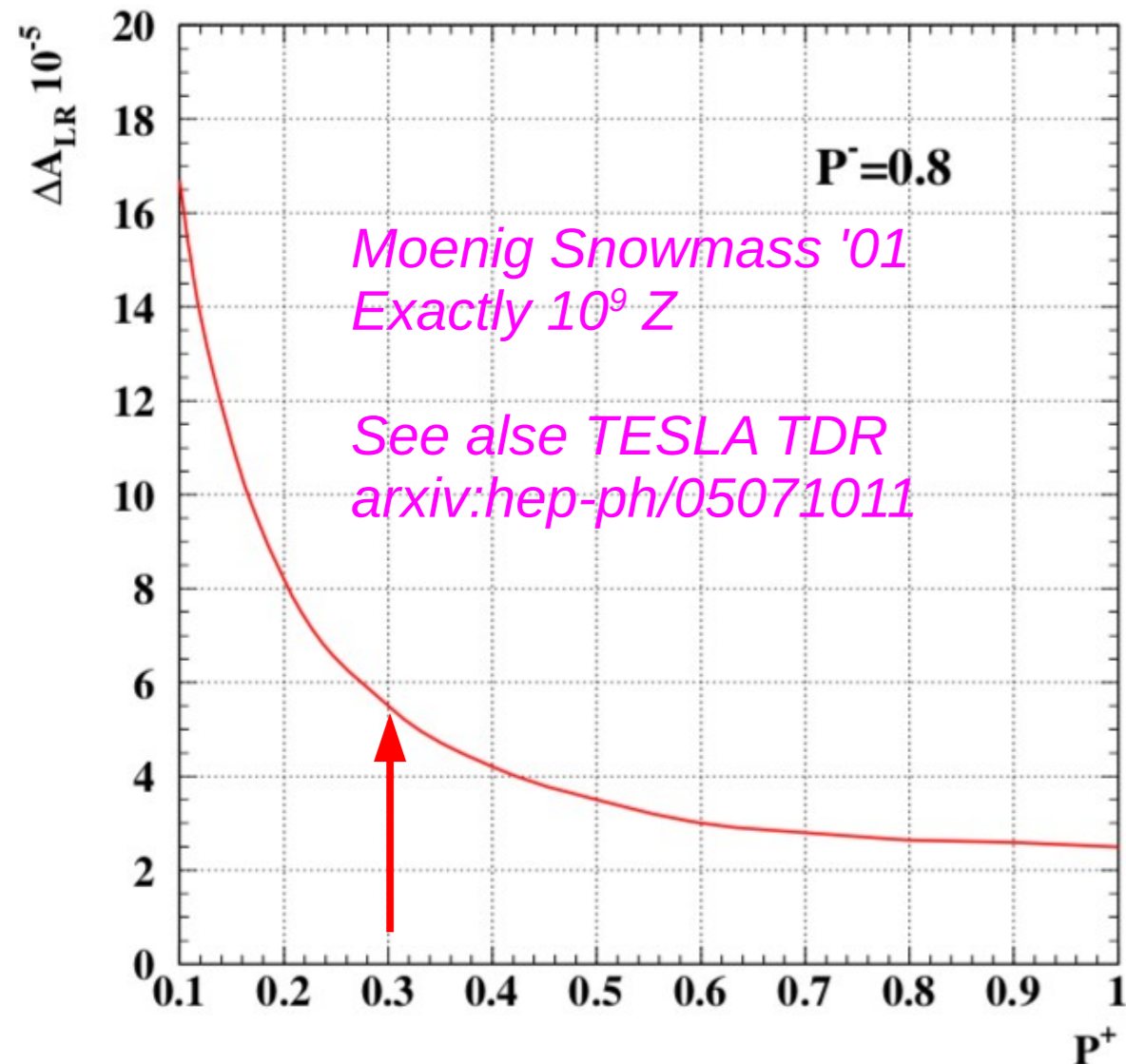
$$A_{FB}^{\text{pol}} = \frac{(\sigma_r - \sigma_l)_F - (\sigma_r - \sigma_l)_B}{(\sigma_r + \sigma_l)_F + (\sigma_r + \sigma_l)_B} = -\frac{3}{4} \mathcal{A}_e$$

Available at LC, CC

Beam polarisation is key: Remember SLC delivered most precise value of $\sin^2\theta_{\text{eff}}^{\ell}$
 despite of 30 times less lumi

Measurement of $\sin^2\theta_{\text{eff}}^{\ell}$.

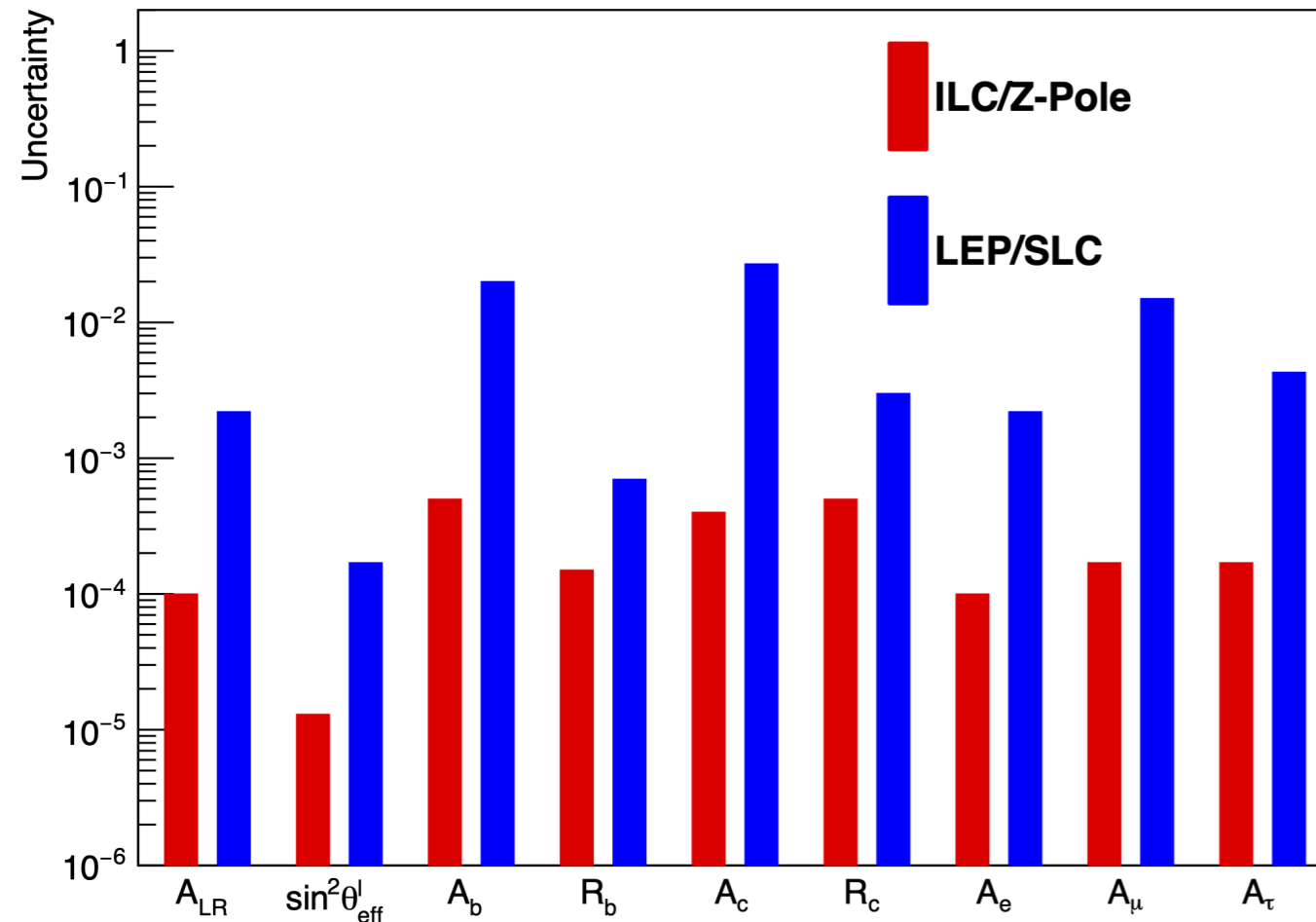
Blondel scheme:
$$A_{LR} = \sqrt{\frac{(\sigma_{++} + \sigma_{-+} - \sigma_{+-} - \sigma_{--})(-\sigma_{++} + \sigma_{-+} - \sigma_{+-} + \sigma_{--})}{(\sigma_{++} + \sigma_{-+} + \sigma_{+-} + \sigma_{--})(-\sigma_{++} + \sigma_{-+} + \sigma_{+-} - \sigma_{--})}}$$



- Blondel scheme independent of polarimeter precision
 - Assumes perfect spin flip for polarised beams
 - Residuals must be monitored by polarimeter
 - Residual uncertainty of $\Delta A_{LR} = 0.5 \times 10^{-4}$ seems possible
 - The more positron polarisation the better
 - Don't forget energy dependency ($dA_{LR}/d\sqrt{s} \sim 2 \times 10^{-5}/\text{MeV}$)
 - 1 MeV precision on \sqrt{s} seems possible (see above)
- Precision $\Delta A_{LR} = 1 \times 10^{-4}$ is a realistic assumption for GigaZ

=>
$$\delta \sin^2\theta_{\text{eff}}^{\ell} \sim 1.3 \cdot 10^{-5}$$

- Radiative return
 - Mainly limited by statistics $\Delta A_{LR} = 1.4 \times 10^{-4}$
 - Beam polarisation better than $\Delta A_{LR} = 0.5 \times 10^{-4}$ (More processes available)
 - Energy dependence much weaker than on Z-pole



- Z pole running of ILC will improve significantly precision w.r.t. LEP/SLD
- Precise measurement of $\sin^2 \theta_{\text{eff}}^l$.
 - Around 13 times better than LEP/SLD and a factor three better than current world average
- Considerable improvement of fermion asymmetries A_f
 - e.g.: arXiv: 1908.11299
 - $\Delta A_b/A_b \sim 5 \times 10^{-4}$ (compare with $\Delta A_b/A_b \sim 214 \times 10^{-4}$ today)
 - $\Delta A_c/A_c \sim (5 \oplus 5) \times 10^{-4}$ (compare with $\Delta A_c/A_c \sim 404 \times 10^{-4}$ today)
 - For completeness note that a statistical error of 10^{-4} has been assumed for A_b and 3×10^{-4} for A_c
- Main error source
 - Knowledge of beam polarisation
 - QCD corrections that dilute forward backward asymmetry (arXiv:2010.08604) not considered but about to be looked at (once more)

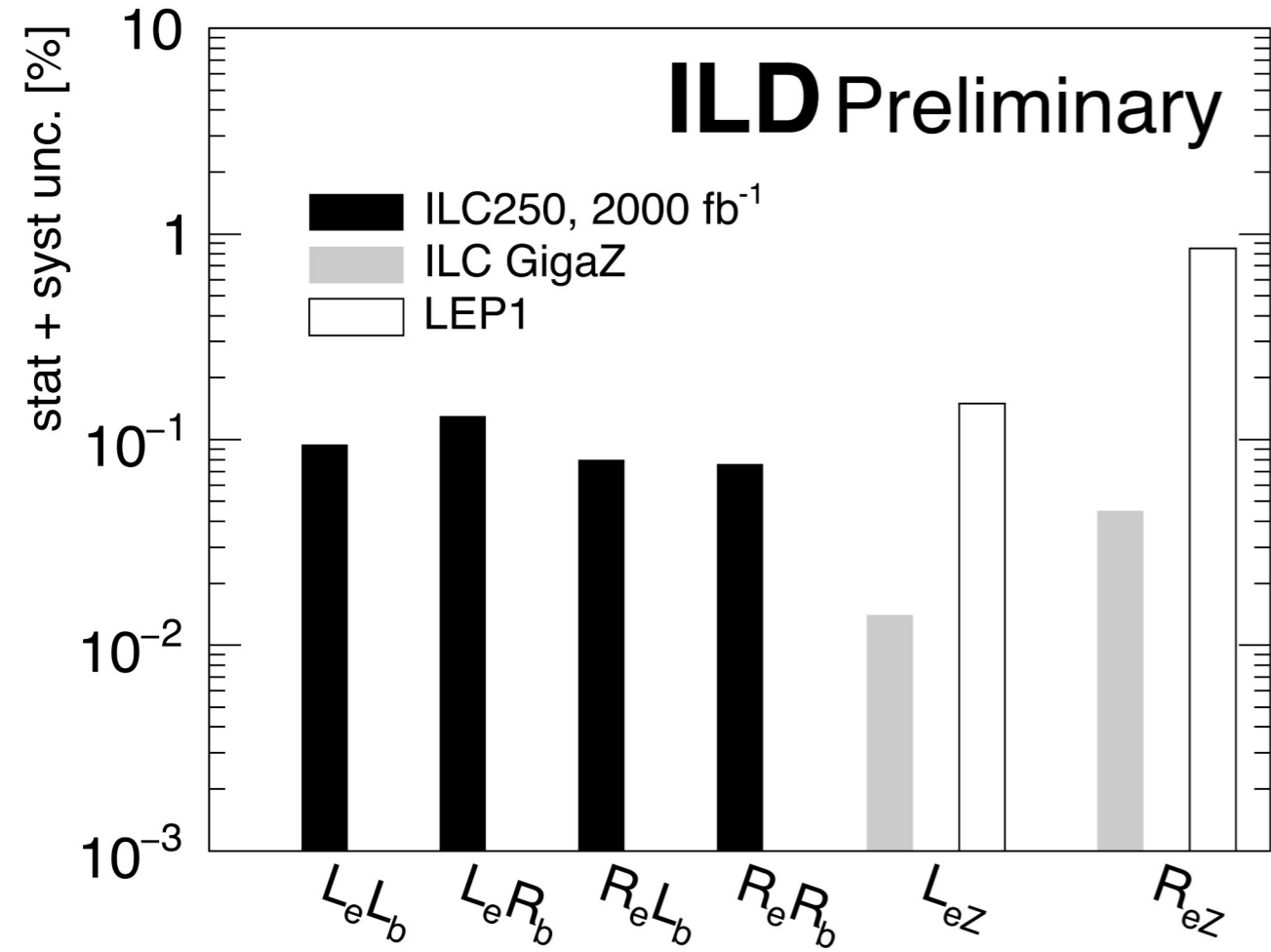


Figure: A. Irles

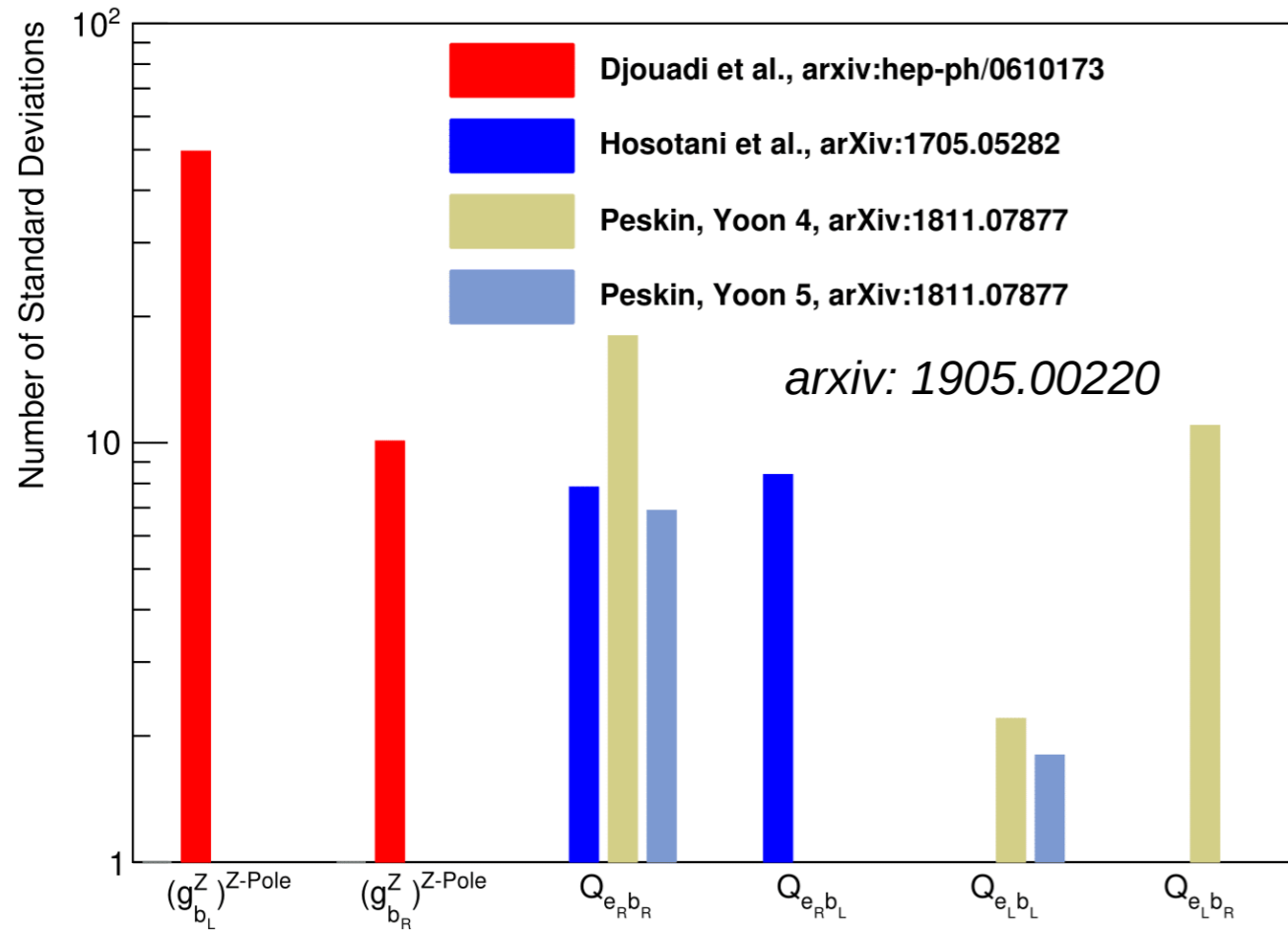
$$LeLb = Q_e Q_b + \frac{LeZLbZ}{s^2 w c^2 w} BWZ + \sum_{Z'} \frac{LeZ'LbZ'}{s^2 w c^2 w} BWZ'$$

Arrows point from the terms to labels:

- Blue arrow from $Q_e Q_b$ to ILC250
- Blue arrow from $\frac{LeZLbZ}{s^2 w c^2 w} BWZ$ to SM
- Blue arrow from $\sum_{Z'} \frac{LeZ'LbZ'}{s^2 w c^2 w} BWZ'$ to GigaZ
- Red arrow from the sum term to New resonances

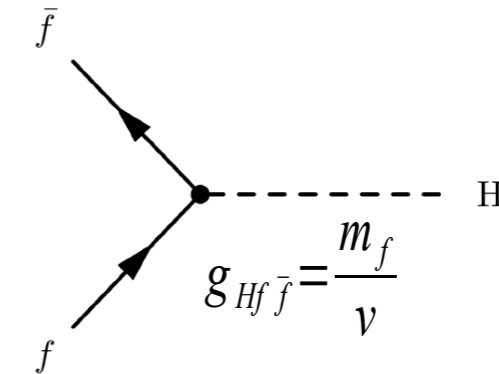
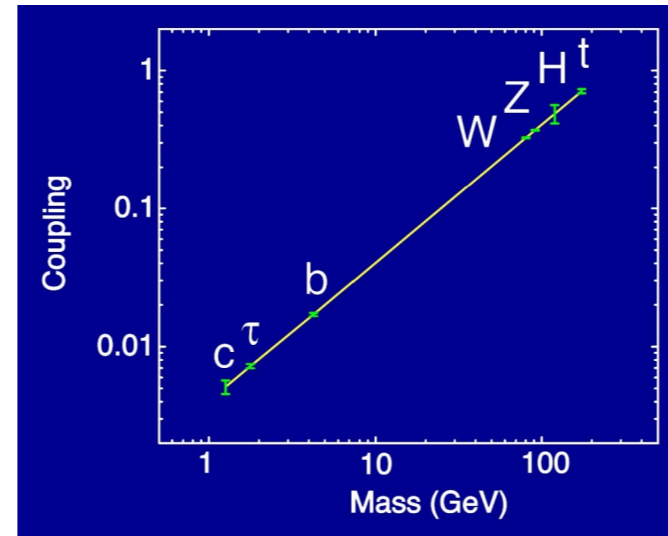
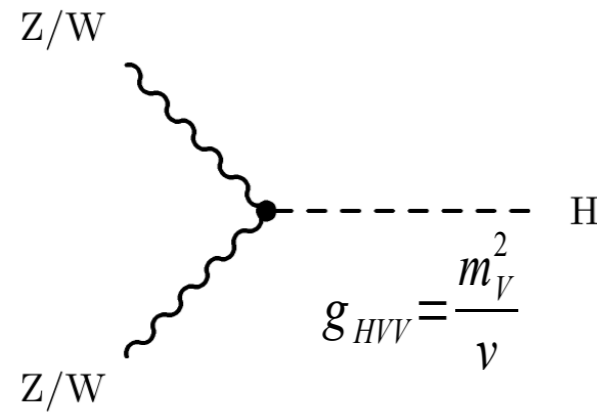
- Couplings are order of magnitude better than at LEP
 - In particular right handed couplings are much better constrained
- New physics can also influence the Zee vertex
 - in 'non top-philic' models
- **Full disentangling of helicity structure for all fermions only possible with polarised beams!!**

Example: b couplings and helicity amplitudes



- Spectacular sensitivity to new physics in Randall Sundrum Models with warped extra dimensions
 - **Complete tests only possible at LC**
 - **Discovery reach $O(10 \text{ TeV})@250 \text{ GeV}$ and $O(20 \text{ TeV})@500 \text{ GeV}$**
- Pole measurements critical input
 - Only poorly constrained by LEP
- Pole measurements will (most likely) influence also top electroweak precision program
 - (t,b) doublet

Couplings to Higgs Boson in Standard Model



Analysis using Kappa-fit:

- Simple scaling of SM-couplings
- Implies that Higgs coupling to Z in production and decay are identical
- No new operators

$$\frac{\Gamma(h \rightarrow ZZ^*)}{SM} = \kappa_Z^2, \quad \frac{\sigma(e^+e^- \rightarrow Zh)}{SM} = \kappa_Z^2$$

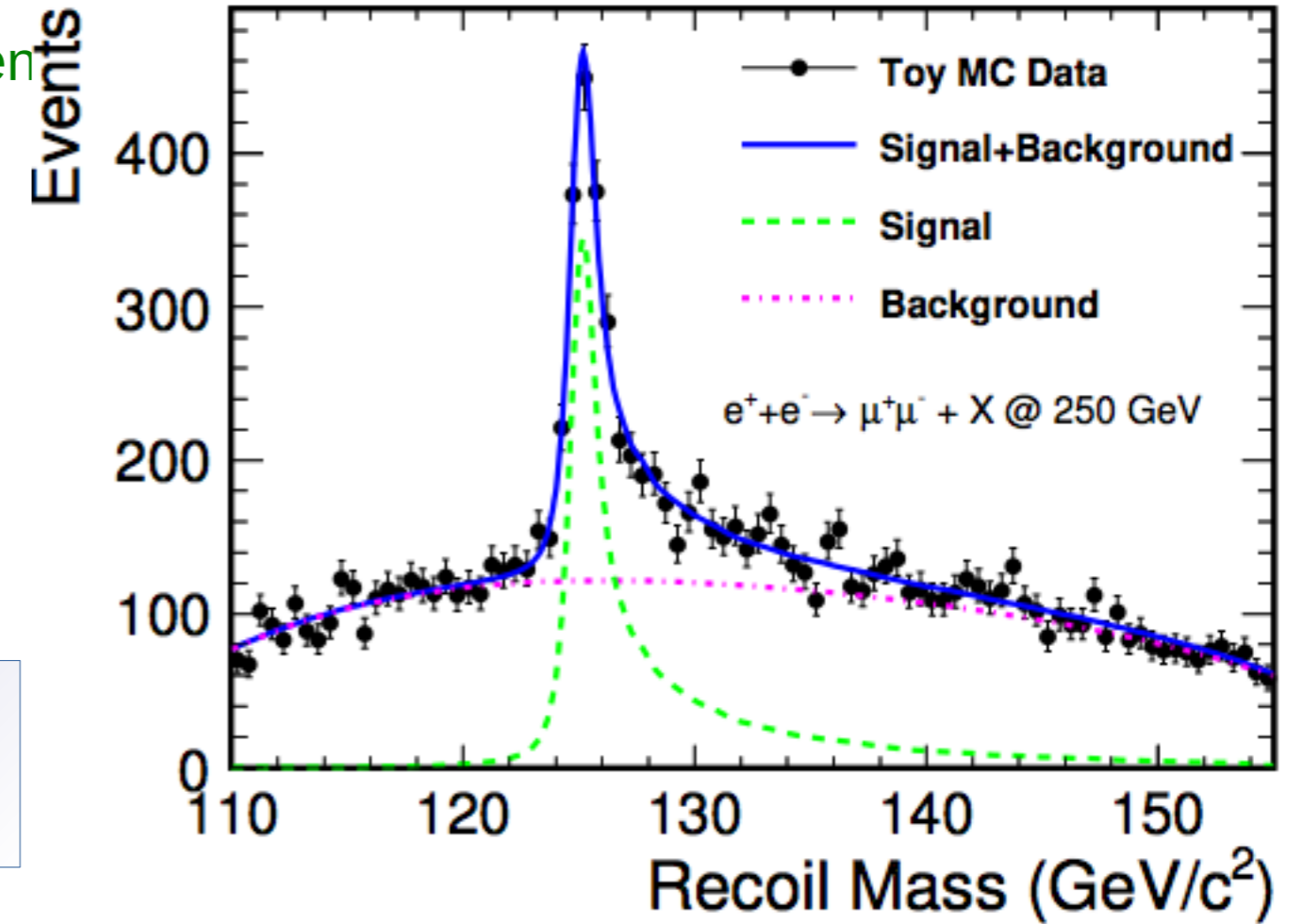
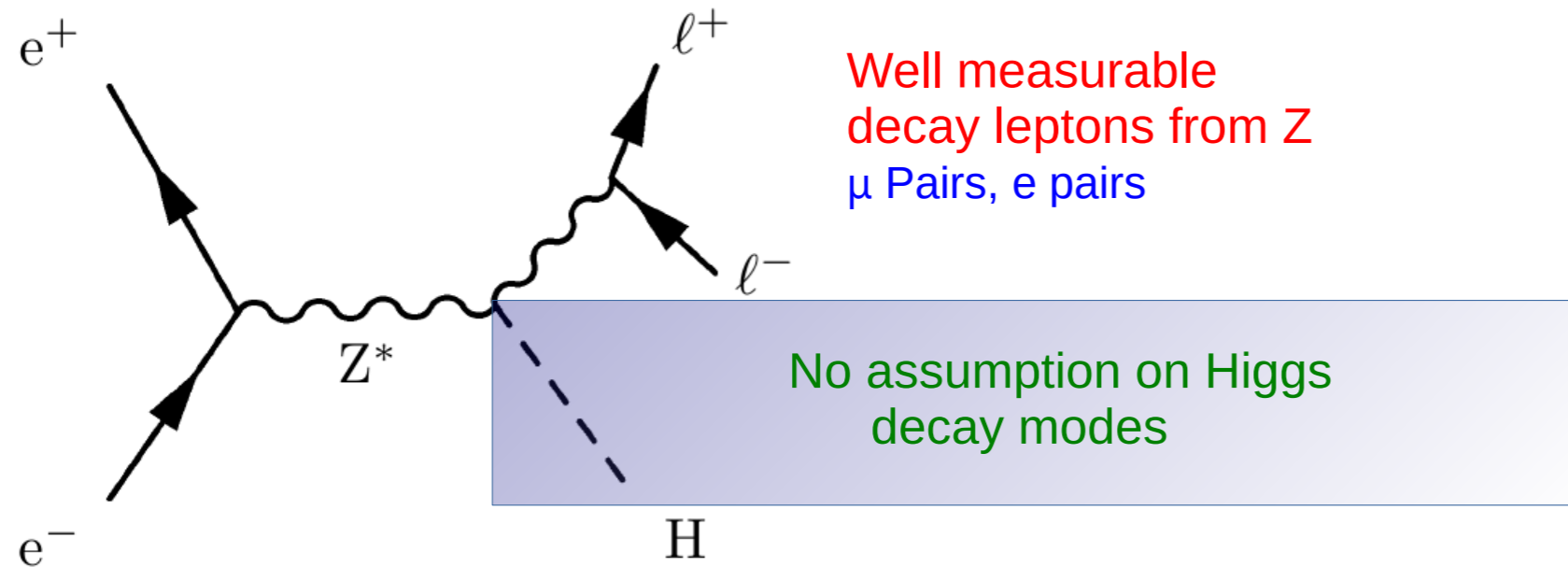
Analysis using EFT-fit:

- Introducing set of SU(2)xU(1) compatible operators
- e.g. breaks simple relation between Higgs production and decay
- Total width and Higgs to invisible as free parameters
- **Receives additional input from e.g. ee->WW and EWPO**

$$\frac{\Gamma(h \rightarrow ZZ^*)}{SM} = (1 + 2\eta_Z - 0.50\zeta_Z)$$

$$\frac{\sigma(e^+e^- \rightarrow Zh)}{SM} = (1 + 2\eta_Z + 5.7\zeta_Z)$$

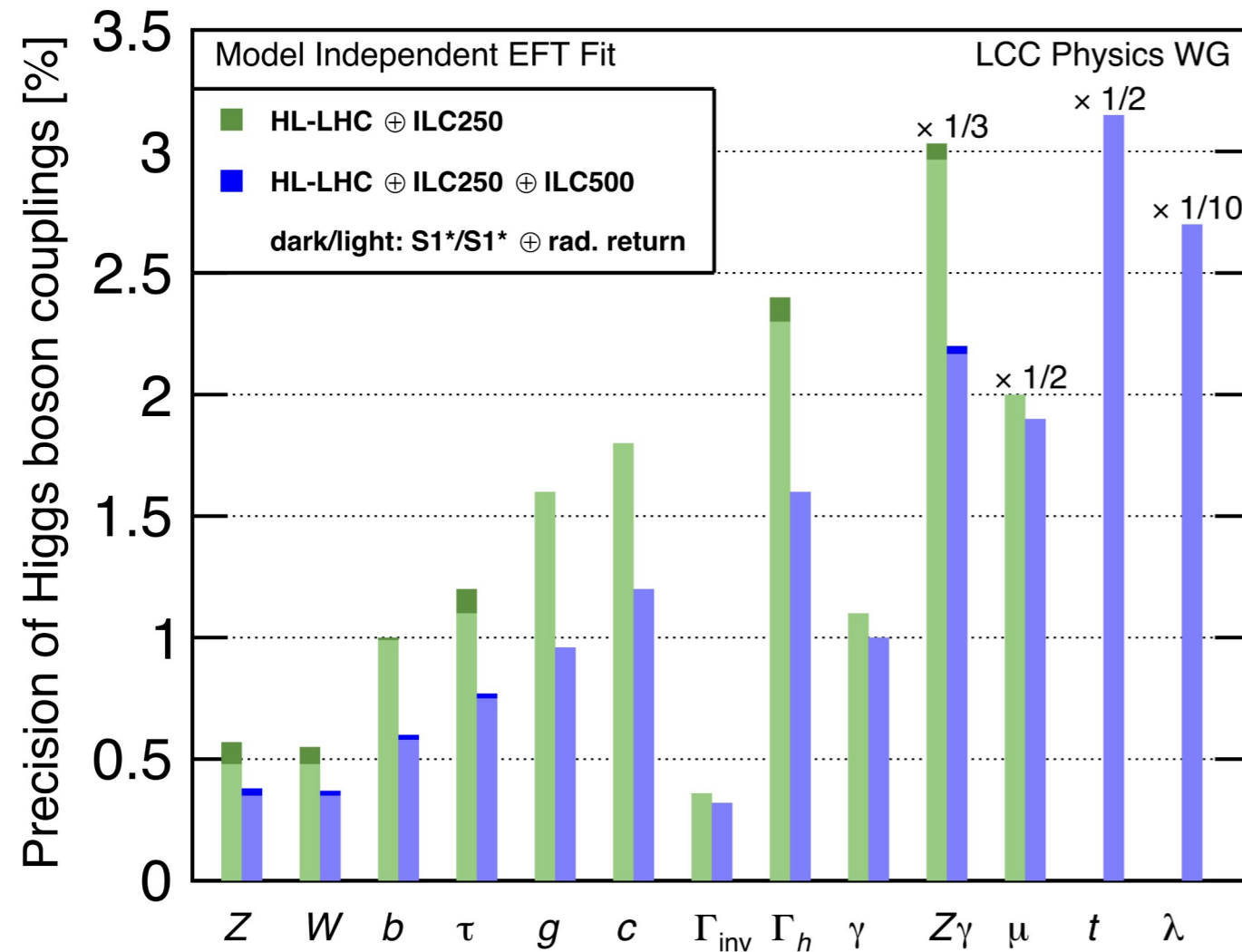
- Powerful channel for unbiased tagging of Higgs Events
- Absolute normalisation of Higgs couplings
- Sensitivity to invisible Higgs decays



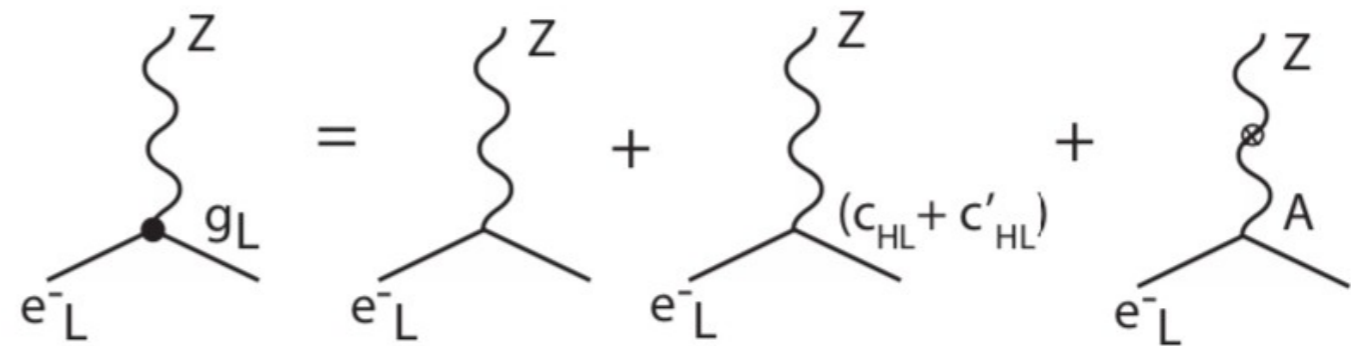
Higgs Recoil Mass: $M_h^2 = M_{recoil}^2 = s + M_Z^2 - 2 E_Z \sqrt{s}$

- Clean and sharp peak in Z recoil spectrum
- Illustrates precision that can be expected from e+e- colliders

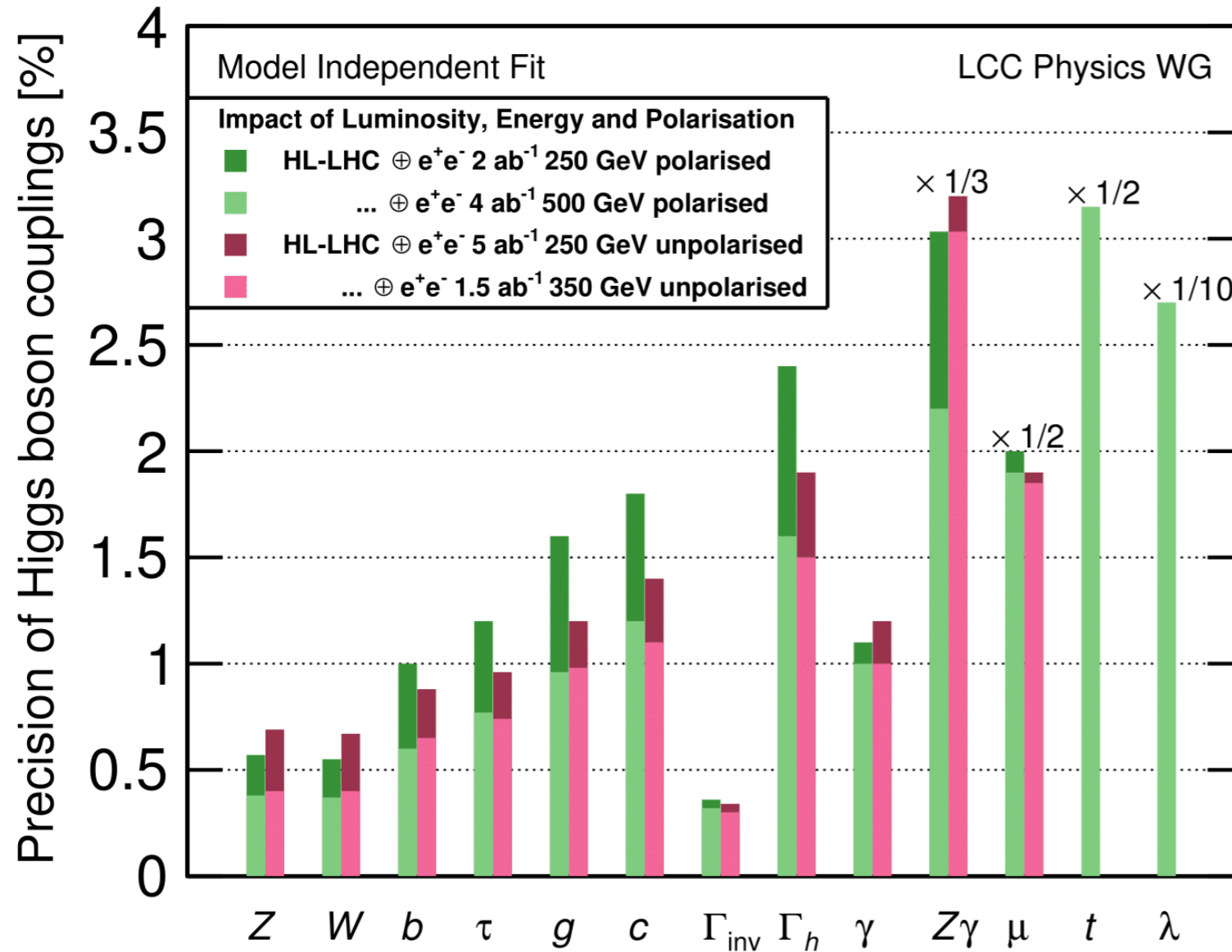
Higgs couplings in EFT using A_{LR}
(Here from radiative return events)



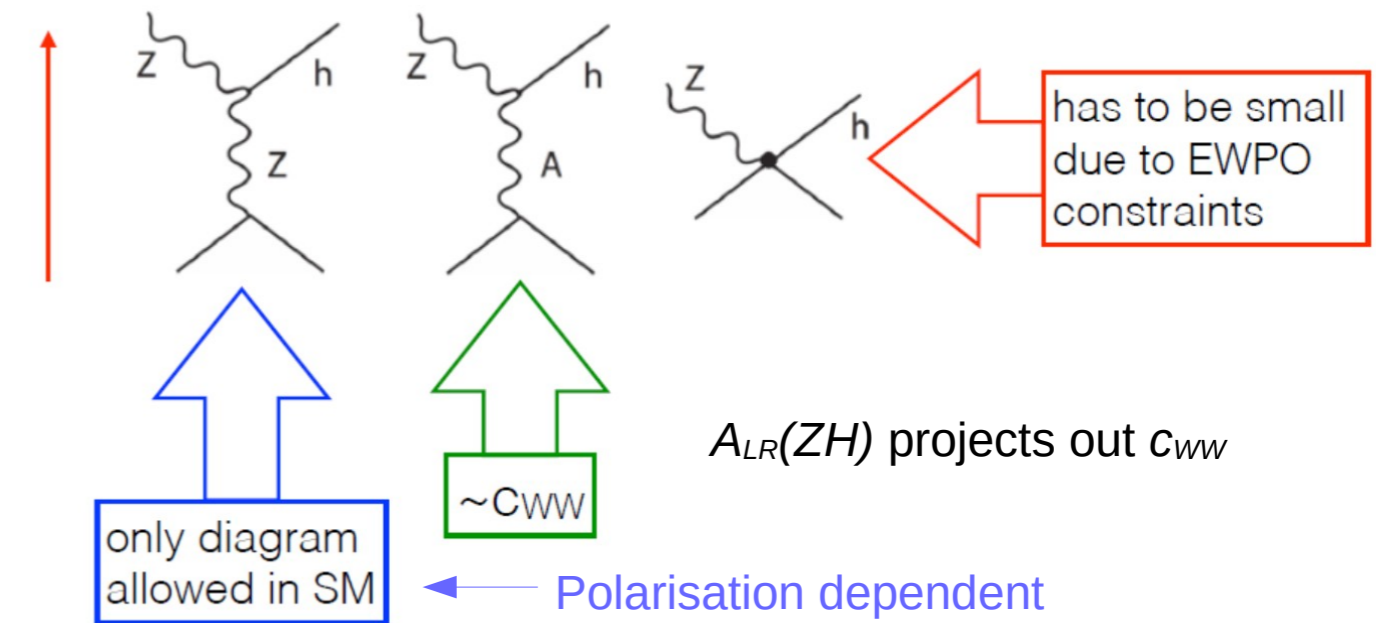
Corrections to Zee-vertex due to additional terms in EFT



- Model independent, clean A_e from A_{LR} and Γ_e from R_e to constrain EFT fit
 - (again) No assumption of Lepton Universality
- Mild but visible improvement on some Higgs couplings at 250 GeV
 - Effect stronger in fit presented in 1905.03764 (see backup and talk by G. Durieux)



- EFT adds additional spin structure to ZH production cross section (see backup)

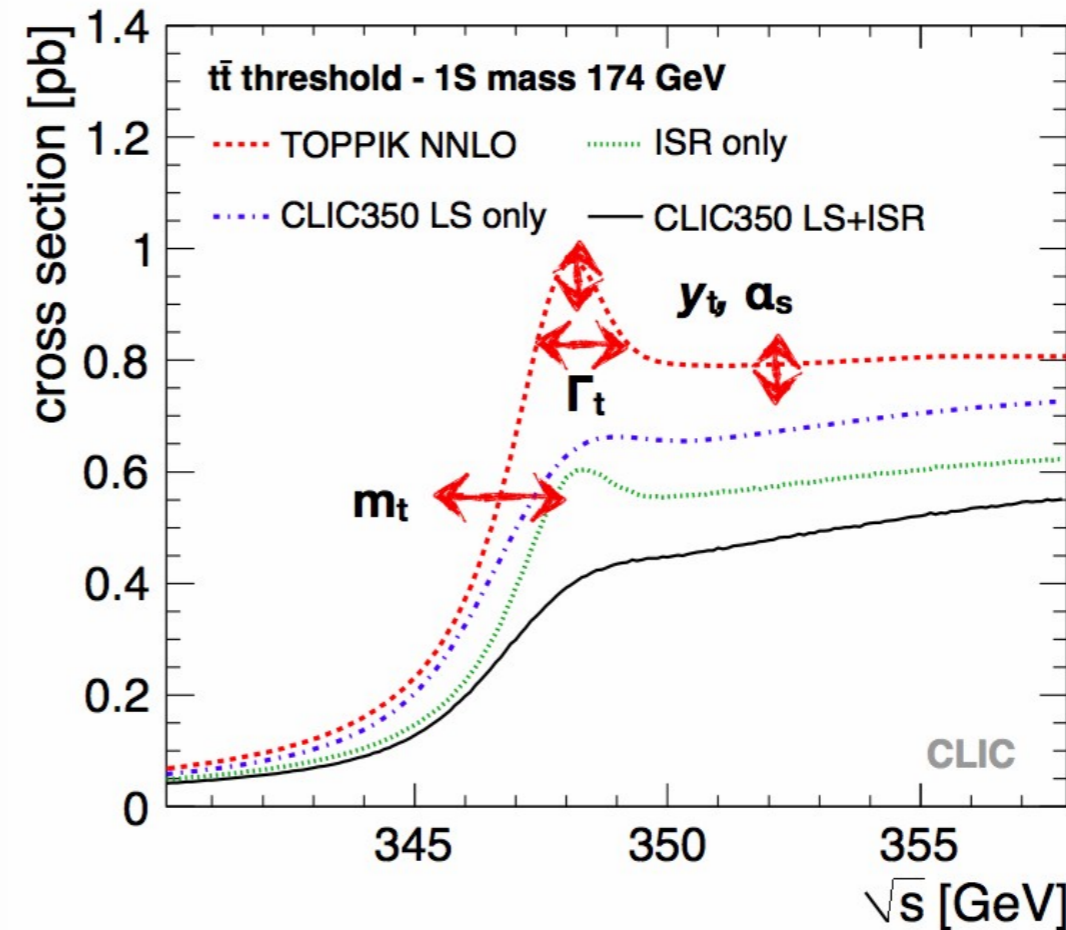
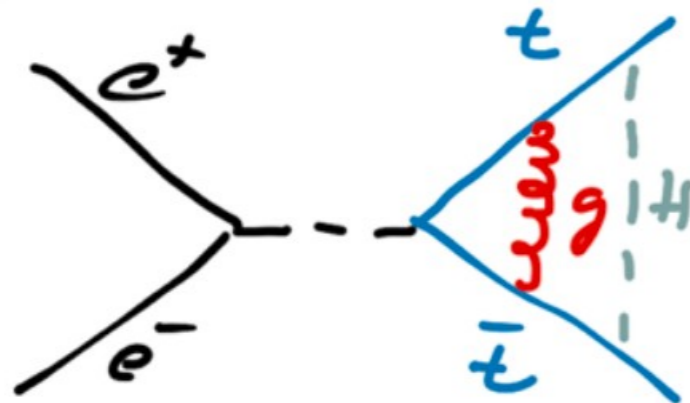


- Precision for 2 ab^{-1} polarised = 5 ab^{-1} unpolarised

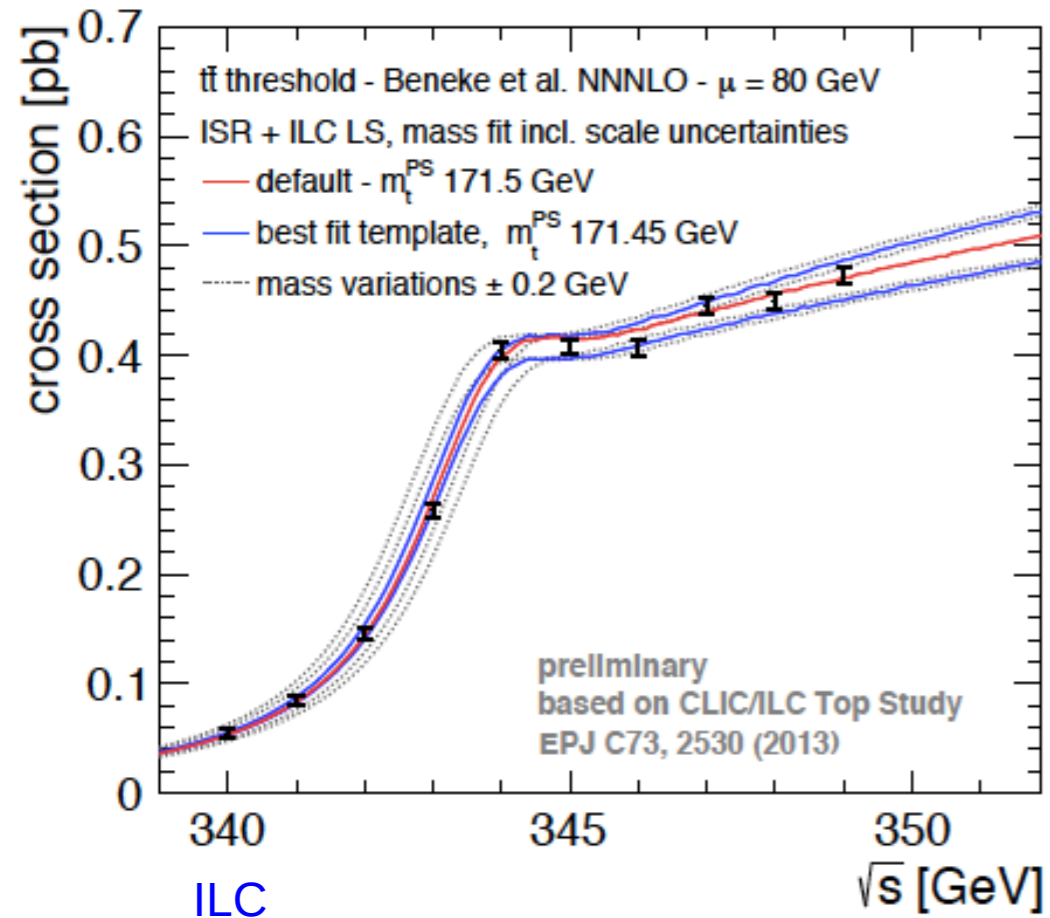
Small size of $t\bar{t}$ “bound state” at threshold ideal premise for precision physics

Cross section around threshold is affected by several properties of the top quark and by QCD

- Top mass, width Yukawa coupling
- Strong coupling constant

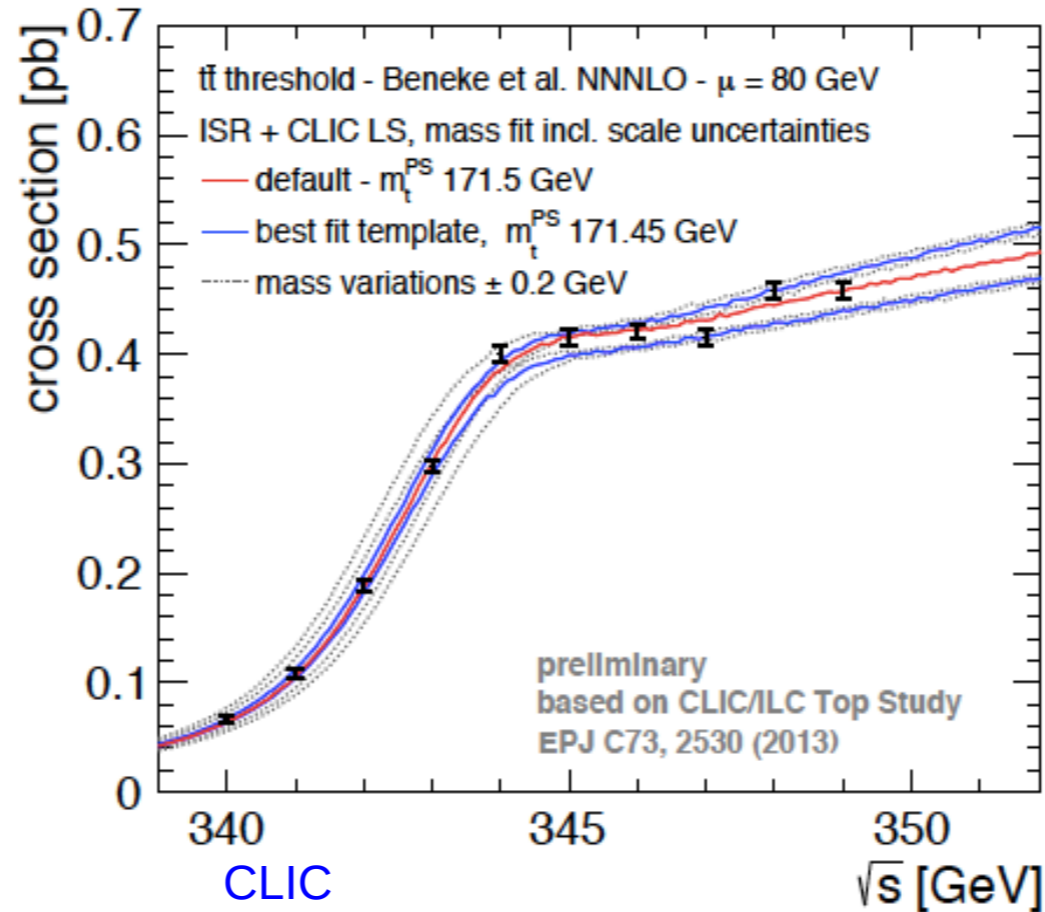


- Effects of some parameters are correlated:
- Dependence on Yukawa coupling rather weak,
- Precise external α_s helps



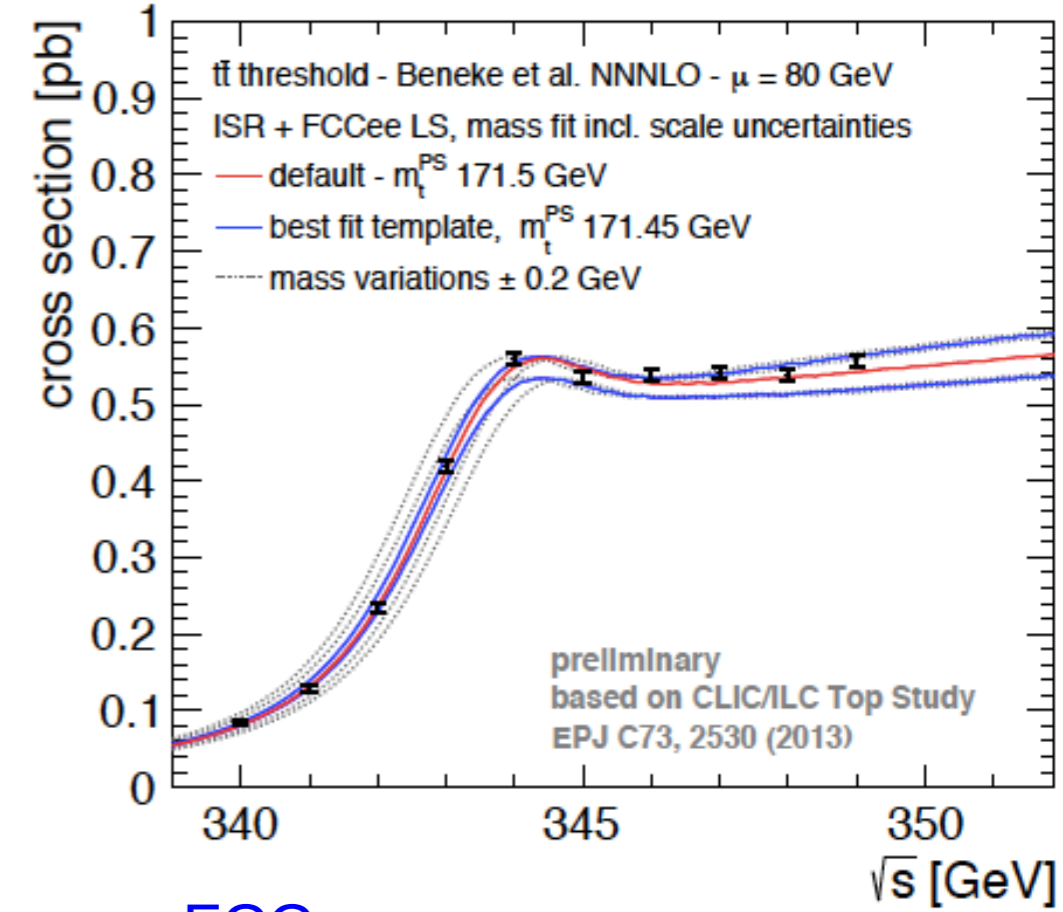
Fit uncertainty:
 28.5 MeV (18 MeV stat)

Scale uncertainty:
 40 MeV



Fit uncertainty:
 31 MeV (21 MeV stat)

Scale uncertainty:
 42 MeV

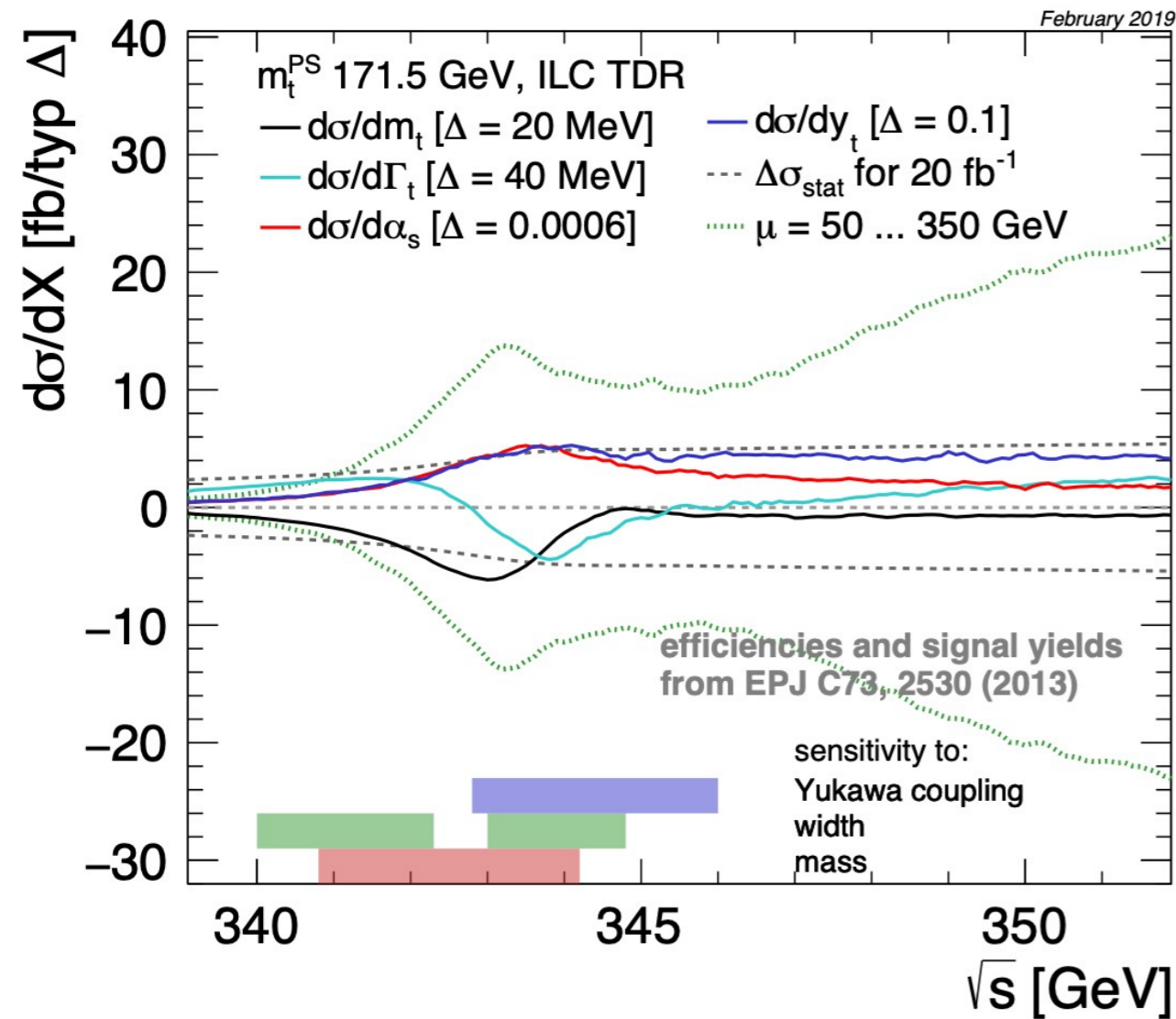


FCC-ee

Fit uncertainty:
 27 MeV (15 MeV stat)

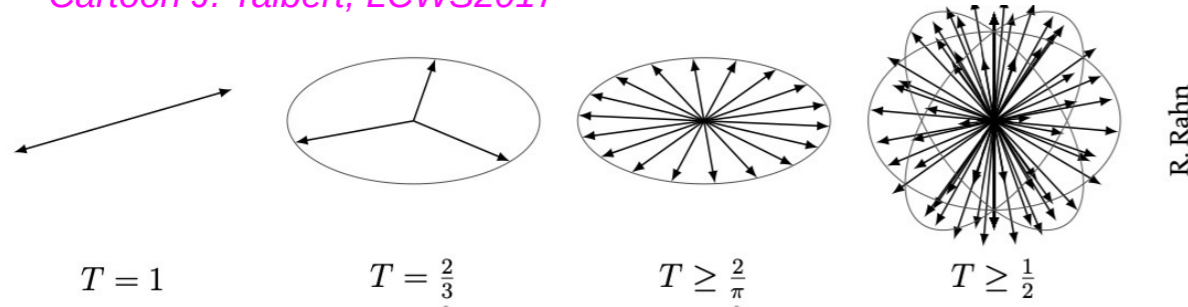
Scale uncertainty:
 40 MeV

Sensitivity and error breakdown



error source	$\Delta m_t^{\text{PS}} [\text{MeV}]$
stat. error (200 fb^{-1})	13
theory (NNNLO scale variations, PS scheme)	40
parametric (α_s , current WA)	35
non-resonant contributions (such as single top)	< 40
residual background / selection efficiency	10 – 20
luminosity spectrum uncertainty	< 10
beam energy uncertainty	< 17
combined theory & parametric	30 – 50
combined experimental & backgrounds	25 - 50
total (stat. + syst.)	40 – 75

Cartoon J. Talbert, LCWS2017

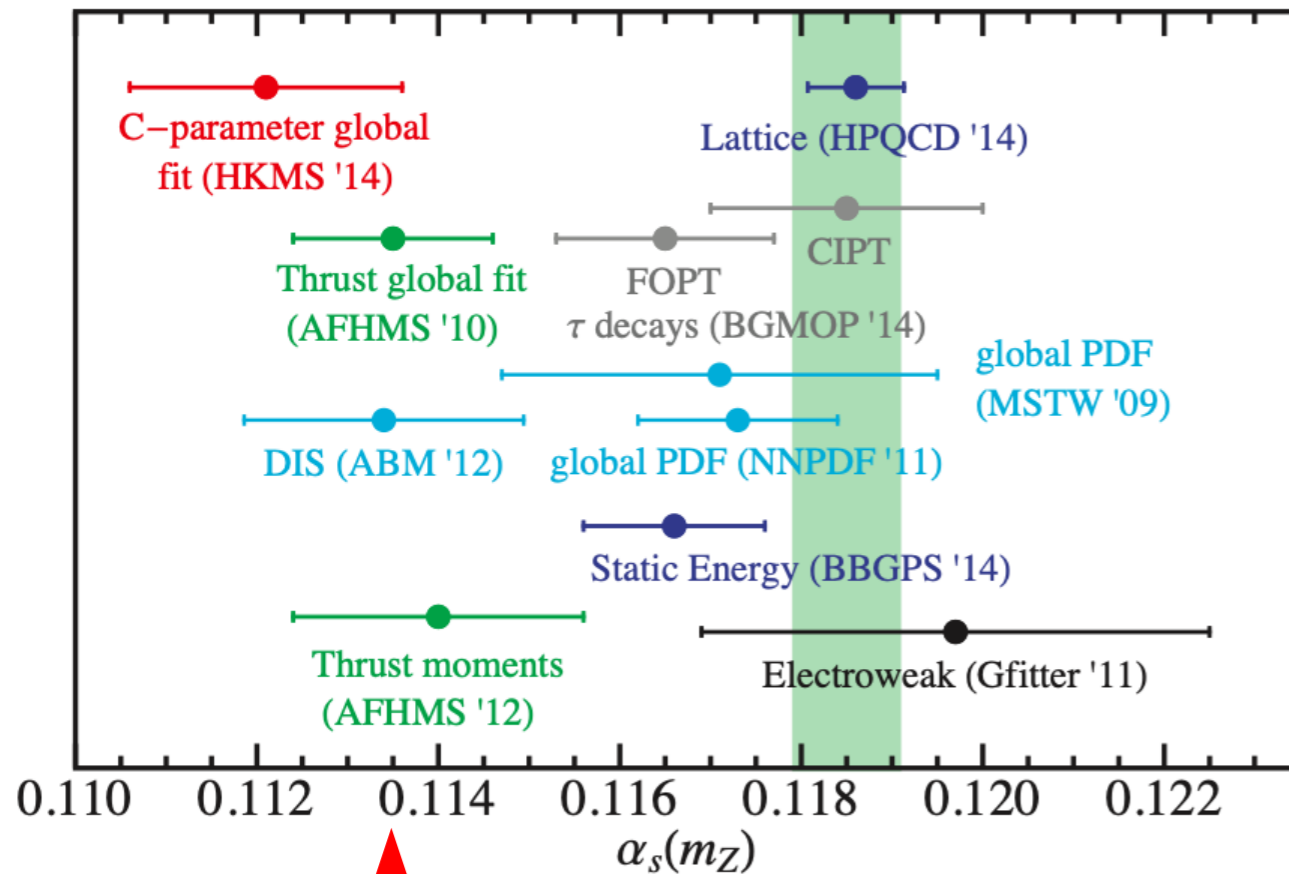


R. Rahn

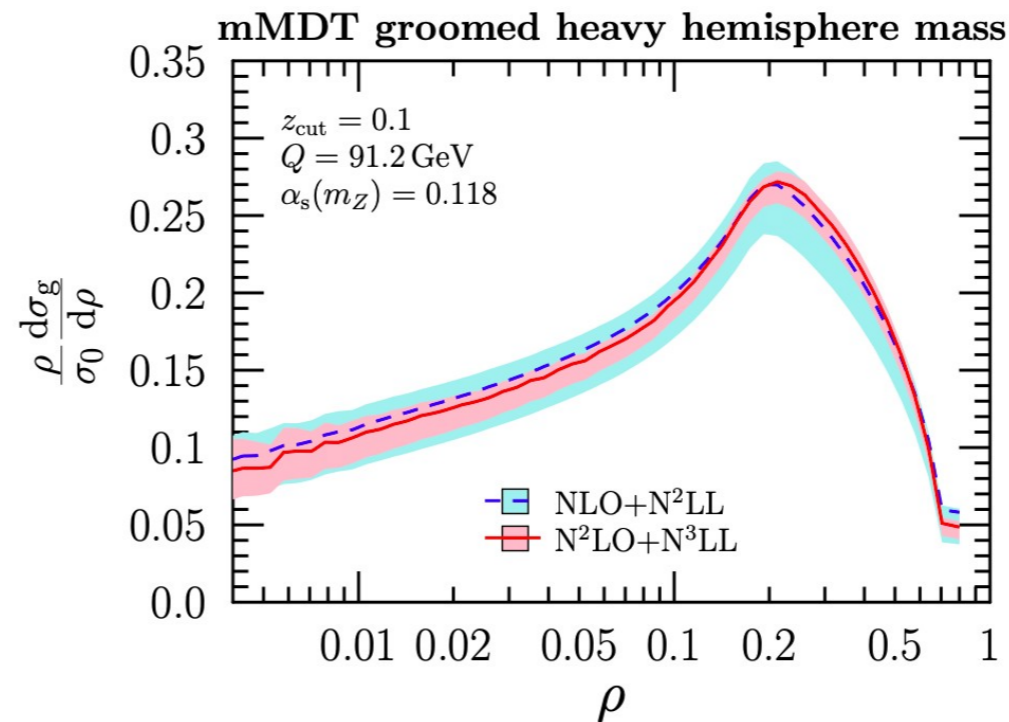
Here brief summary see upcoming ILC Snowmass White Paper for more details

- Significant discrepancy between α_s from lattice calculations (most precise) and QCD event shape variables
 - Most “recent” e+e- input from LEP
- Event shape variable are subject to non-perturbative effects
 - “Power corrections” caused by soft radiation within a jet
- How to take handle effects into account?
 - Handling with Soft Collinear Effective Theories and/or
 - “Jet Grooming”, i.e. removing soft parts from jet

From arxiv:1501.04111



Event shape observables



- Stable perturbative series after grooming
- Excellent premise for extracting α_s



- **ILC is electroweak precision machine**
 - Electroweak parameters are limited by systematics, not statistics
 - High precision measurements of $M_{Z'}$, $\Gamma_{Z'}$, $M_{W'}$, $\Gamma_{W'}$, M_t and $\sin^2 \theta_{\text{eff}}^\ell$.
- **ILC can (should) be run on the Z-pole**
 - Electroweak precision observables deliver decisive input for interpretation at higher energies
- **Full exploitation of physics potential by large energy coverage and polarised beams**
 - Clean model independent measurements due to beam polarisation
 - Tests of lepton universality
 - Measurement of patterns for indirect discovery of new physics
 - Spectacular mass reach for new physics already at 250 GeV demonstrated
 - Flexibility of beam energy allows for systematic tracing of the onset of new physics

Main challenge at future machines will be the control of systematic errors

- Experimentally (non exhaustive list)
 - Vertex charge and particle ID
 - PFO for final state jets
 - Beam energy and polarisation
- Theoretically (not discussed)
 - Need at least NLO electroweak predictions (and MC programs) for correct interpretation of results
 - α_s



1. Can m_W be measured well at center-of-mass energies above ZH production threshold? For ILC this needs a more detailed look with a full kinematic fit to $qq\nu$ events including effects of luminosity spectrum. These events have m_W information from both W's.

Acceptance?

1b. Is it really necessary to use the WW threshold for theoretical reasons?

2. Ultimate precision on center-of-mass energy using radiative return events especially in case momentum-scale systematics dominate \sqrt{s} . Important for Higgs mass, top mass, and W mass.

3. Detector requirements for Z pole observables.

Forward acceptance for $e^+e^- \rightarrow q\bar{q}$ is very important.

4. Can the background be controlled well enough

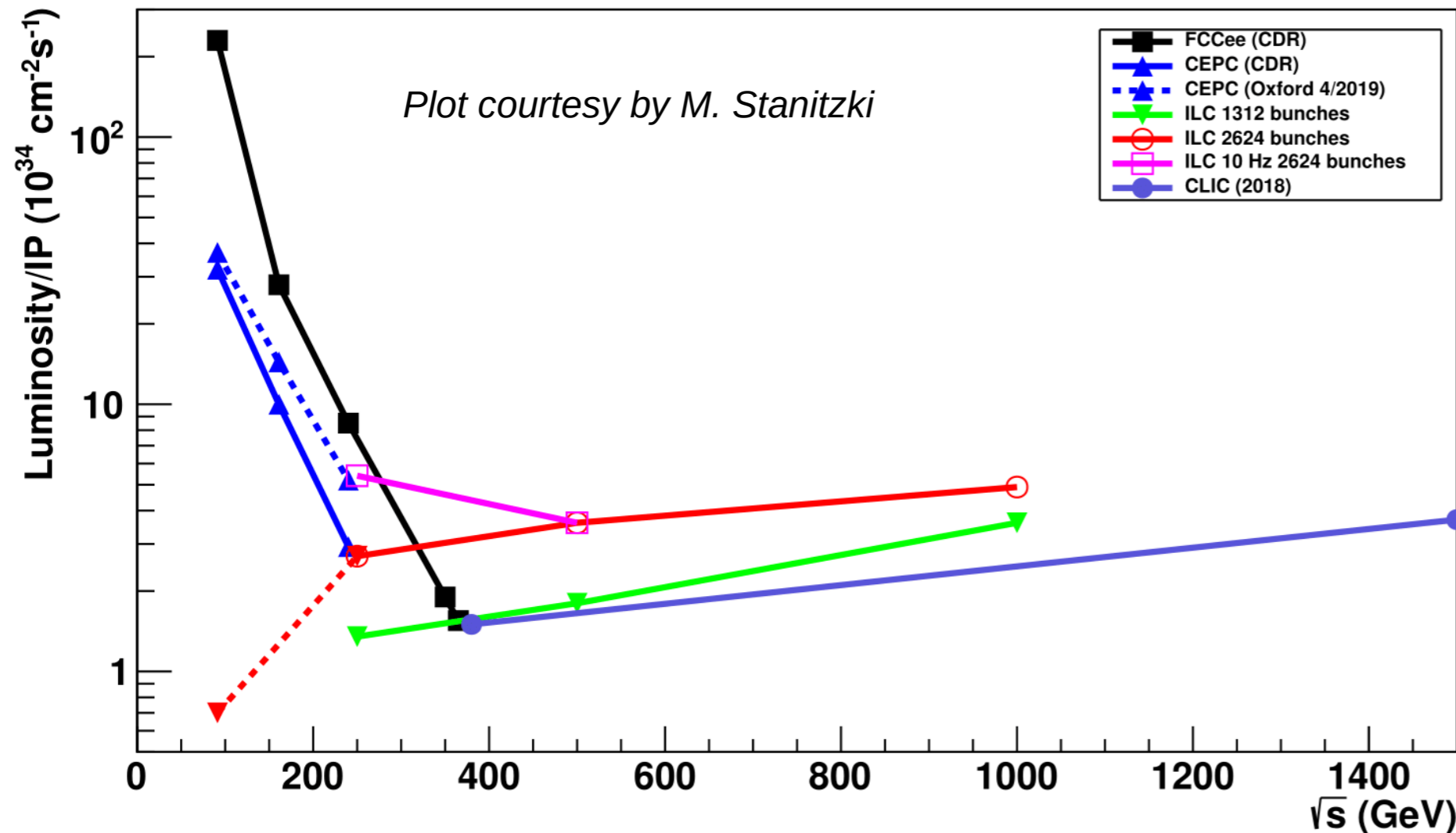
for m_W from threshold measurements. Especially for 4-jet case, and without both beams being polarized.

5. Can $\gamma\gamma \rightarrow$ hadrons background be controlled at the Z peak?

Backup

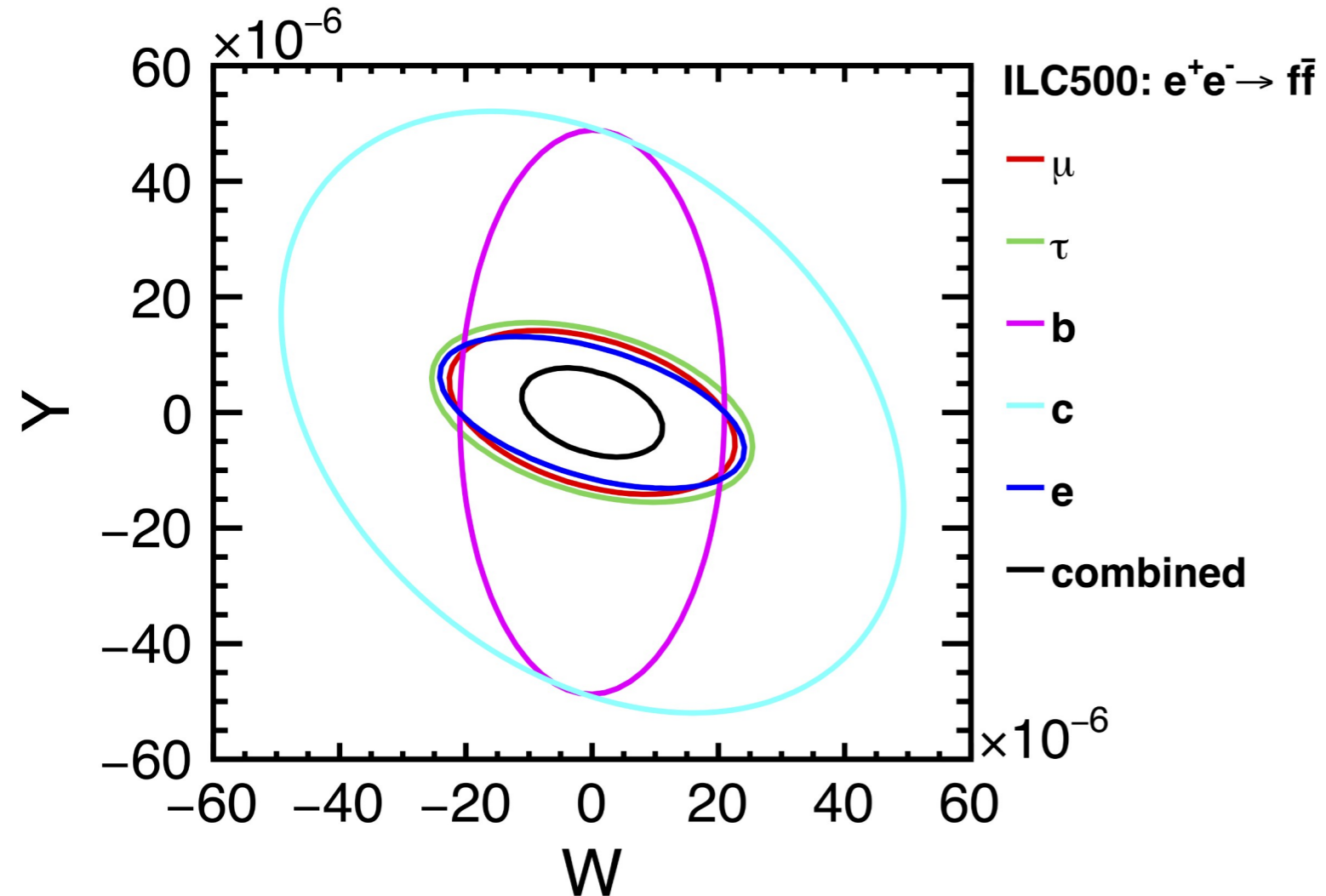
e+e- Higgs Factory Luminosity Comparisons

Updated 15/04/2019



- High energies ~above tt-threshold
Domain of linear colliders
- Low energies e.g. Z-pole
Domain of circular machines
 - However, see later ...
- Transition region, i.e. HZ threshold
... not so clear
Comparable numbers for all proposals
- Linear colliders are more versatile to test chiral theory due to polarised beams
- Detailed design parameters see backup

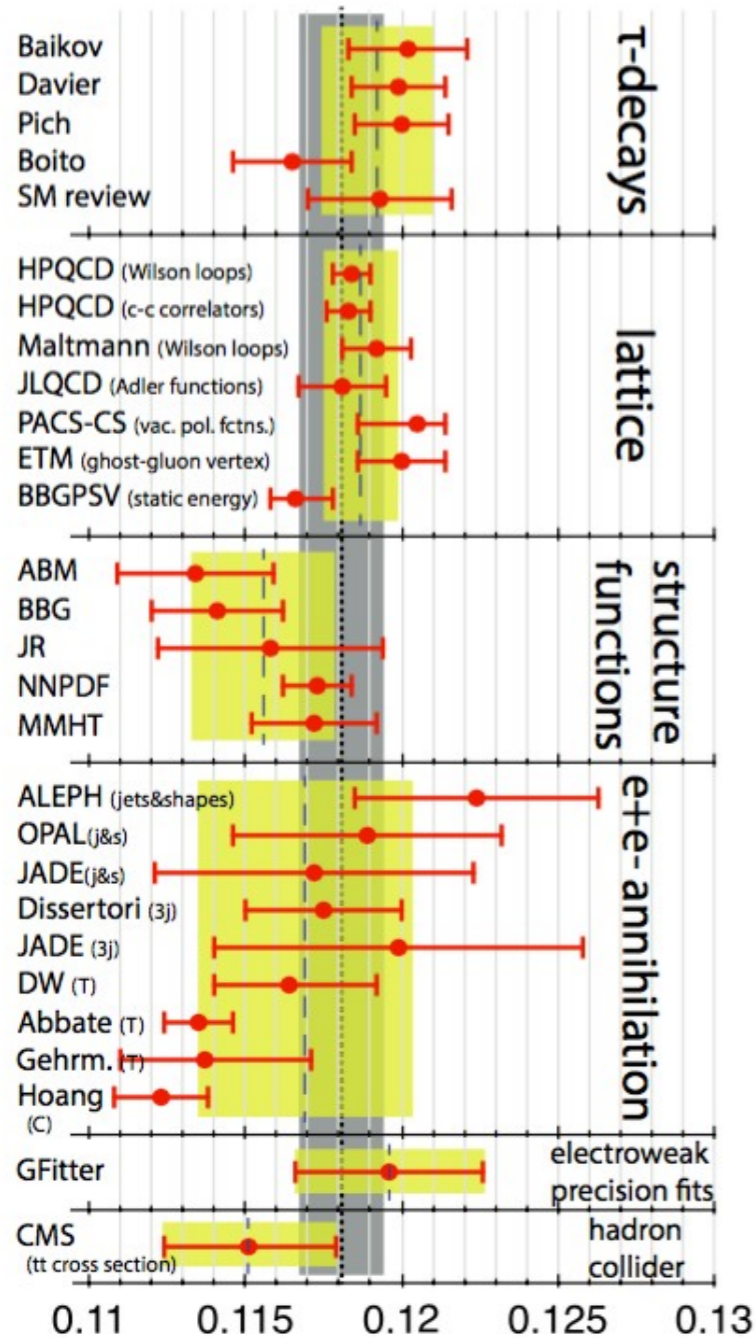
Contributions for different fermion species



\sqrt{s}	ΔW	ΔY	ρ
HL-LHC	15×10^{-5}	20×10^{-5}	-0.97
ILC250	3.4×10^{-5}	2.4×10^{-5}	-0.34
ILC500	1.1×10^{-5}	0.78×10^{-5}	-0.35
ILC1000	0.39×10^{-5}	0.27×10^{-5}	-0.38
500 GeV, no beam pol.	2.0×10^{-5}	1.2×10^{-5}	-0.78

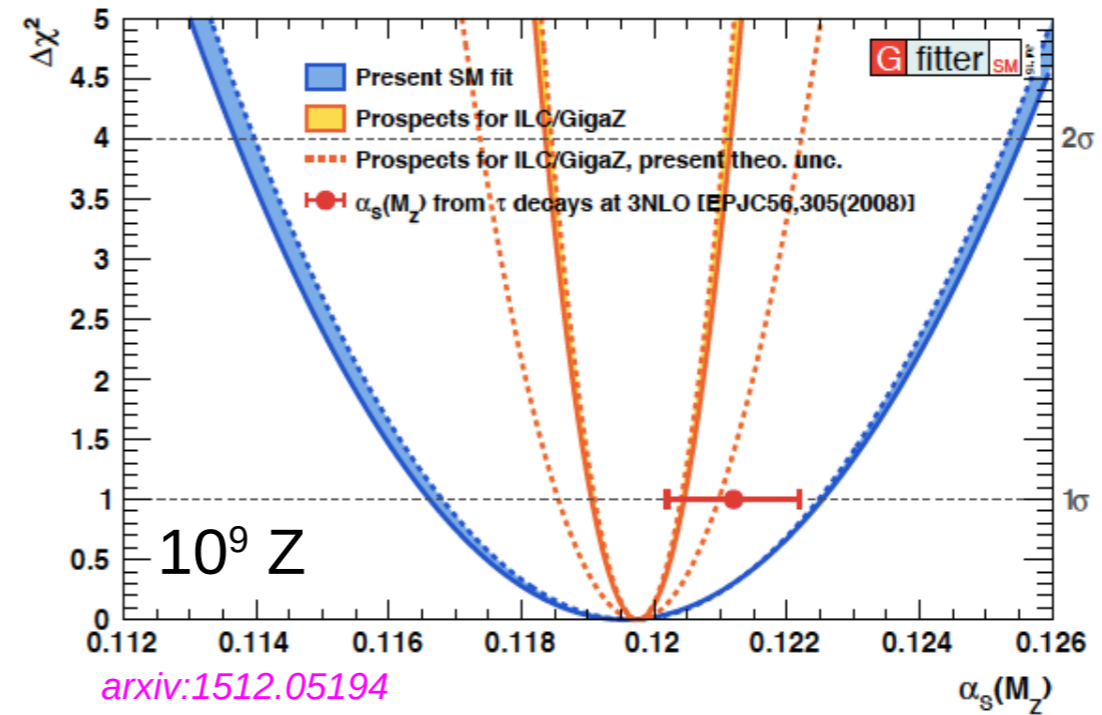
- Beam polarisation essential to disentangle effects from W and Y
- ILC250 outperforms LHC
- ILC500 and above outperforms e^+e^- machines w/o polarisation (at 4ab^{-1})

Current status



Dominated by lattice QCD

Prospects Z-running



Slide made in 2016!

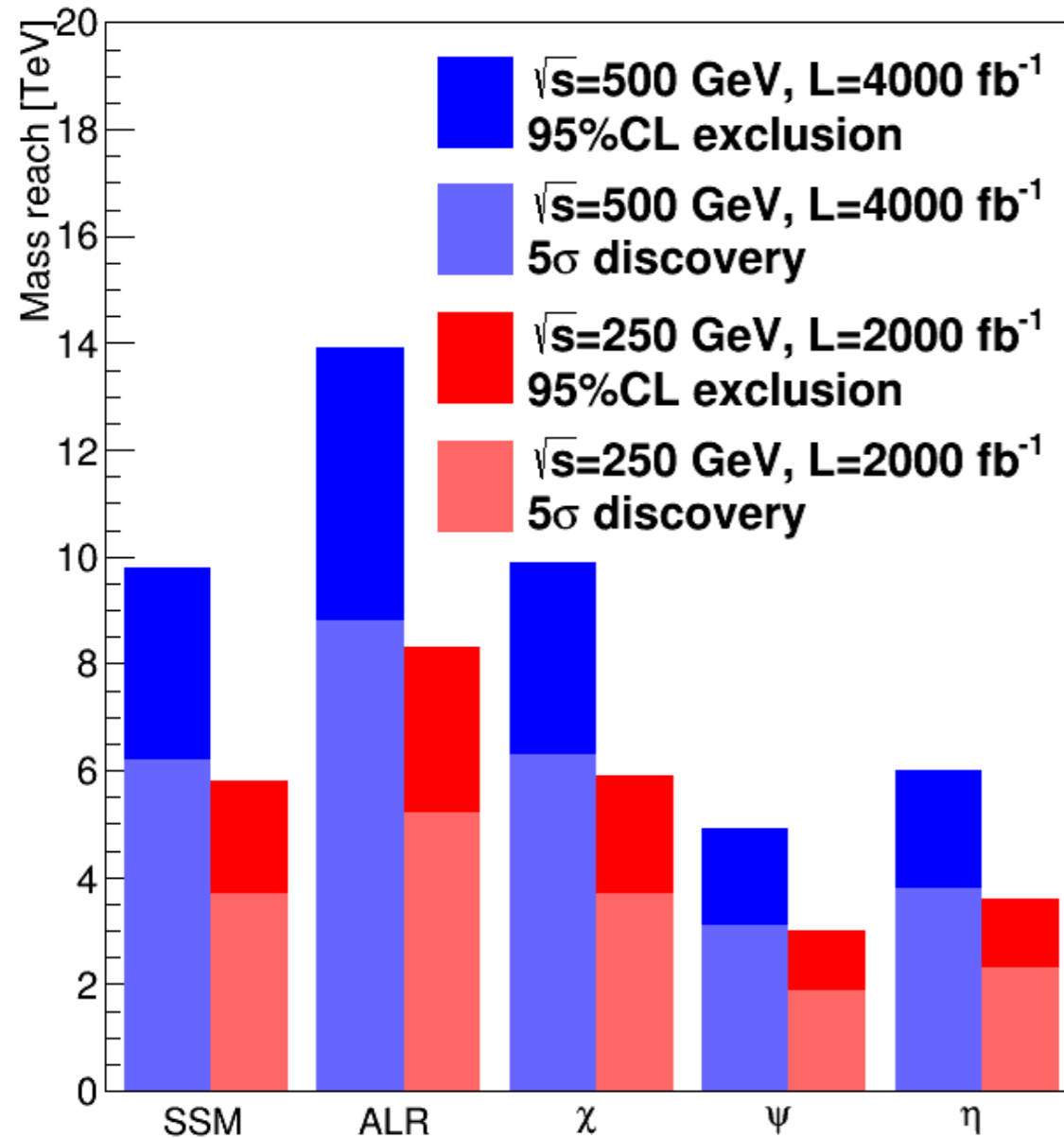
Electroweak fit with updated EWPO and theory uncertainties

$$\delta \alpha_s(M_Z) \sim 0.0007 \text{ for } 10^9 Z$$

$$\delta \alpha_s(M_Z) \sim 0.0003(16) \text{ for } 10^{12} Z$$

Prospects Lattice

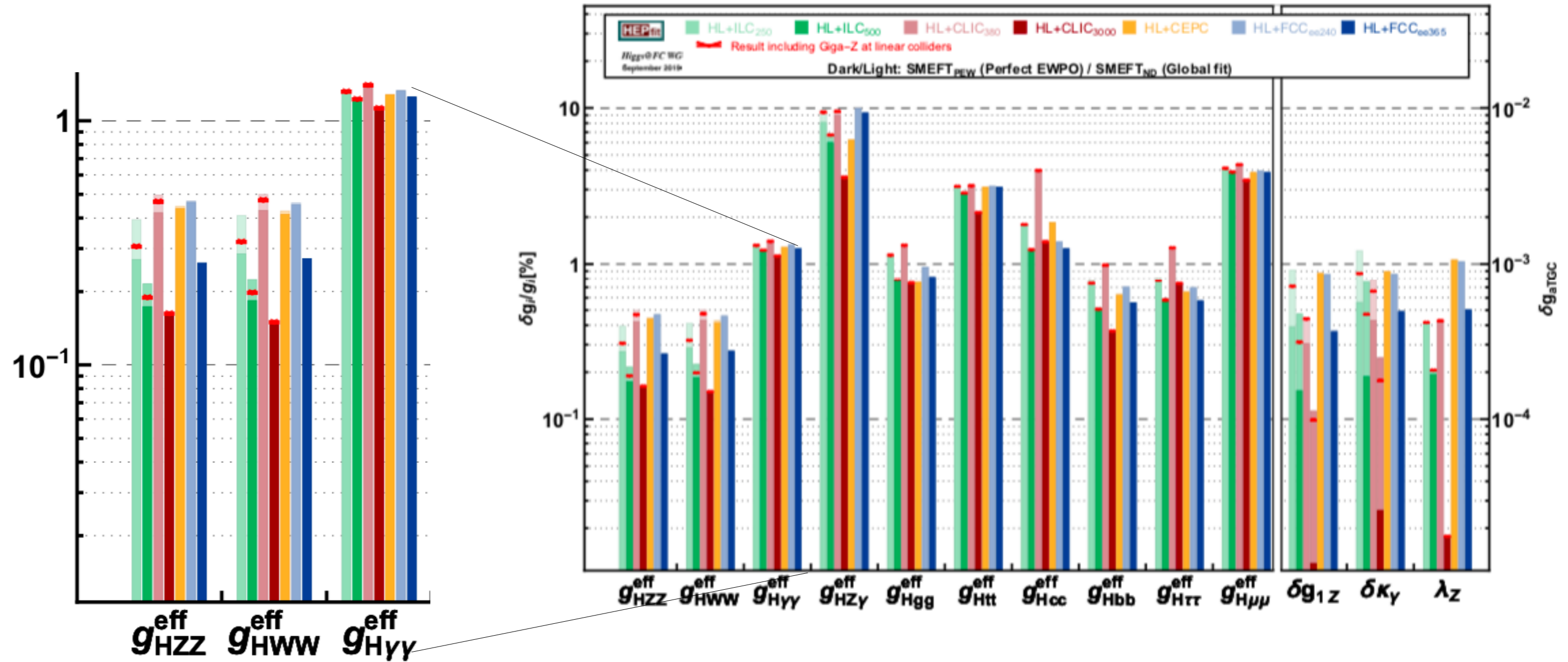
$$\delta \alpha_s(M_Z) \sim 0.0003$$

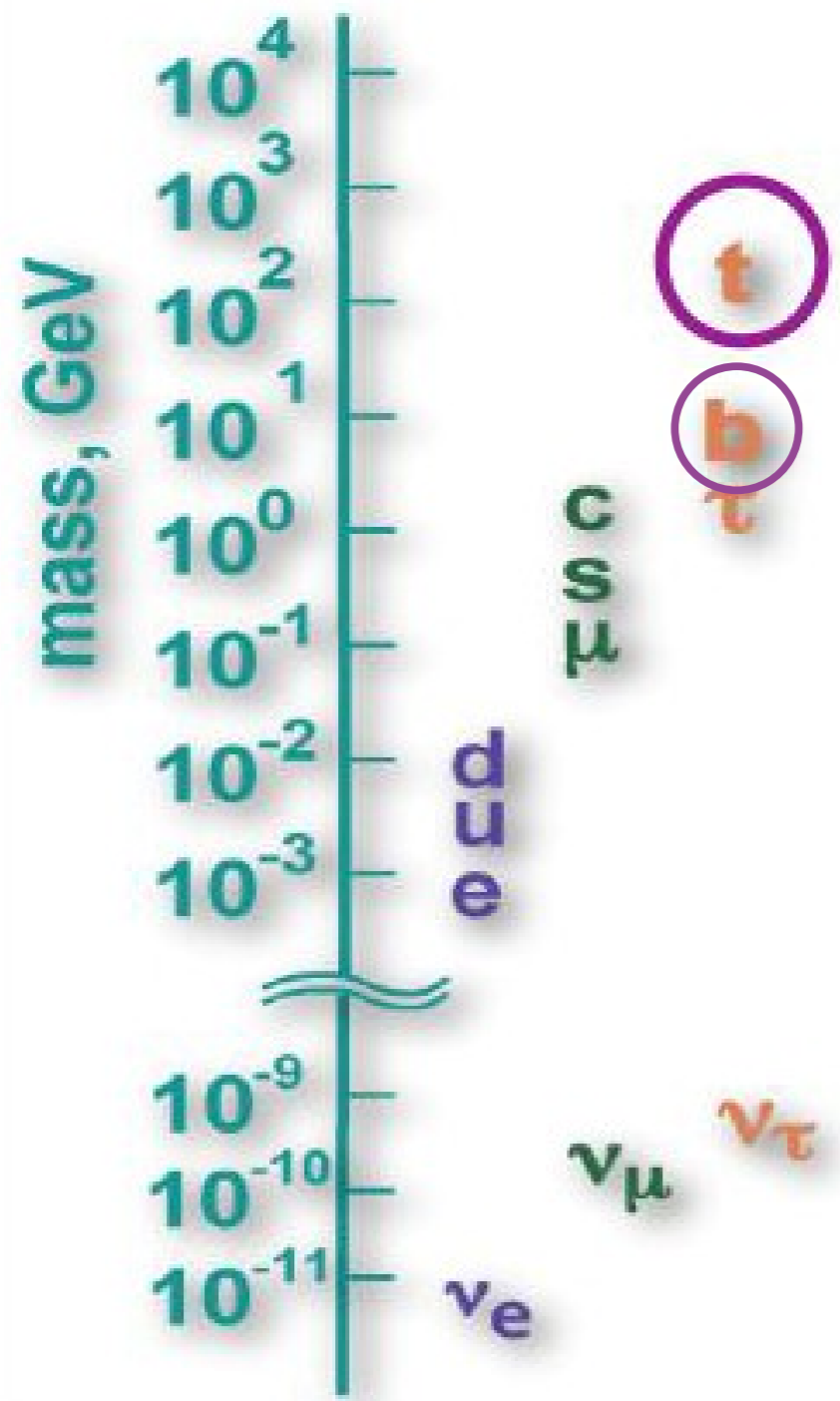
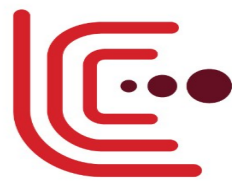


- SSM is “carbon” copy of SM Z and used as common metric in generic Z' searches
- ALR introduces an “ad hoc” $SU(2)_R$ and a Z' with orthogonal couplings to the fermions
- χ, ψ, η are linear combinations of bosons appearing in Grand Unified Theories with couplings orthogonal to the SM Z

Typical mass reach 5-10 TeV

- Reach shown for e, μ, τ
- Adding quarks would improve limits





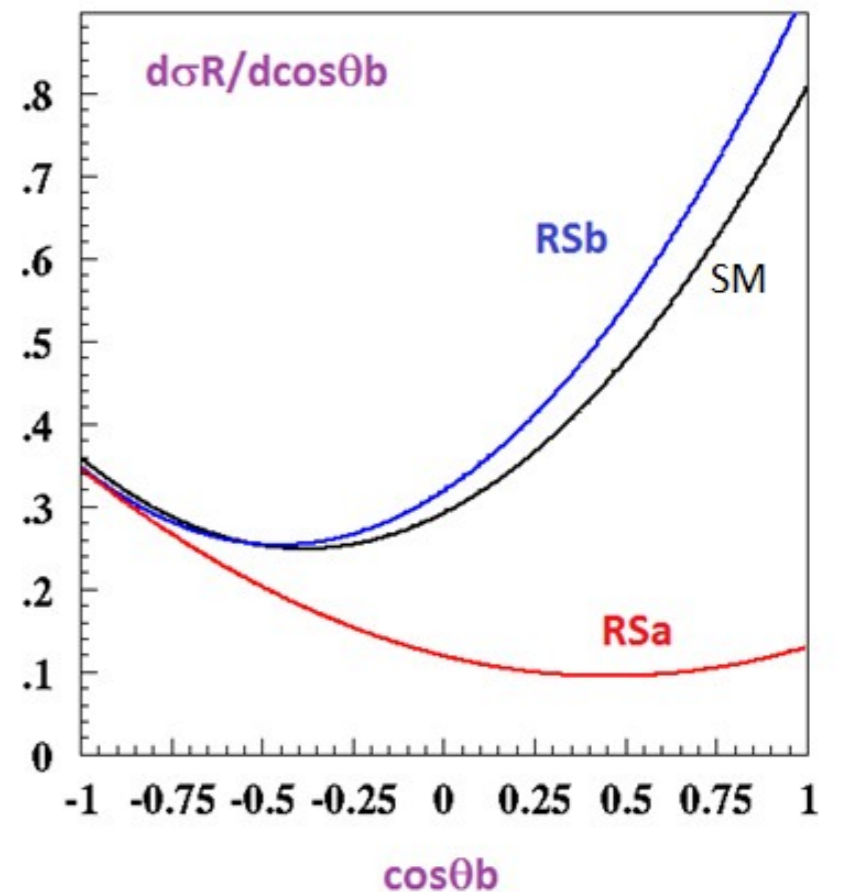
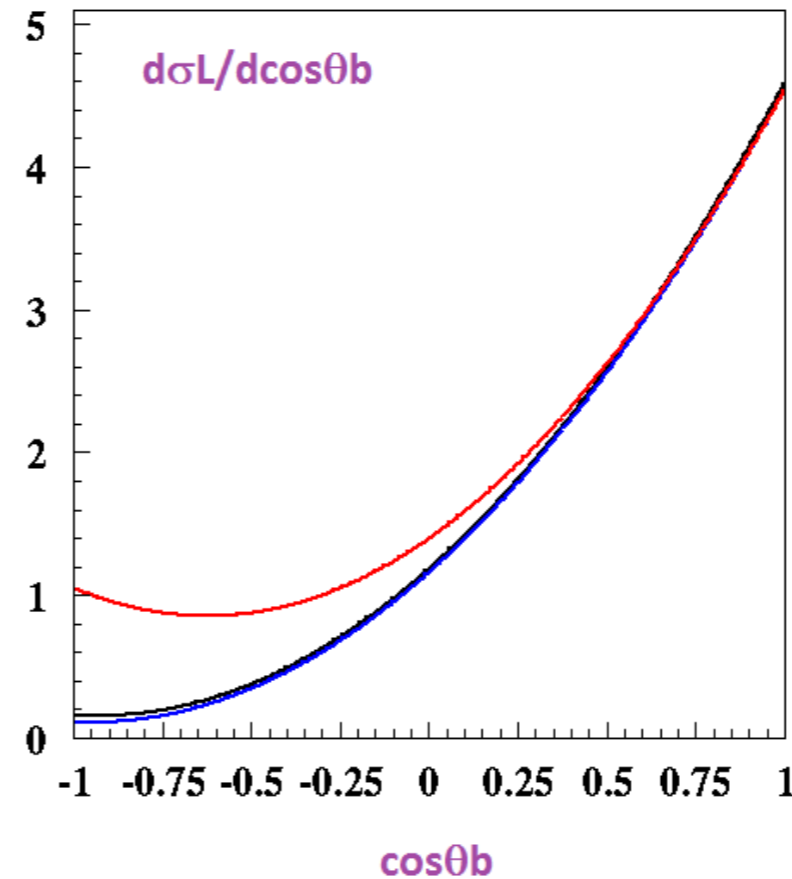
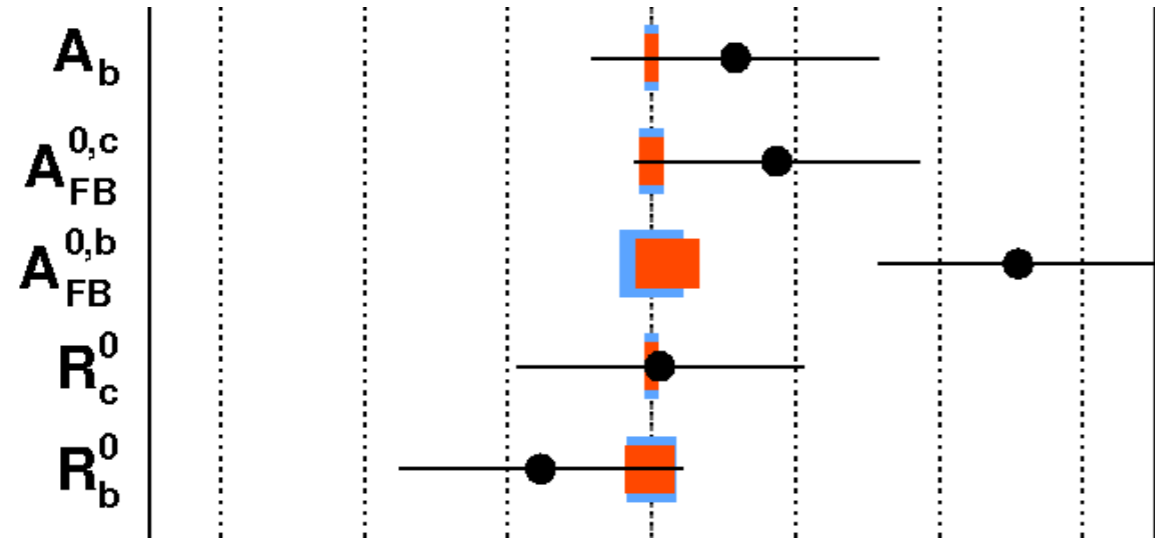
- SM does not provides no explanation for mass spectrum of fermions (and gauge bosons)
- Fermion mass generation closely related to the origin electroweak symmetry breaking
- Expect residual effects for particles with masses closest to symmetry breaking scale

$$\begin{pmatrix} t \\ b \end{pmatrix}_L$$

Strong motivation to study chiral structure of heavy quark vertices in high energy e+e- collisions

$\sim 3\sigma$ in heavy quark observable A_{FB}^b

$ee \rightarrow bb @ 250 \text{ GeV}$



- Is tension due to underestimation of errors or due to new physics?

- High precision e^+e^- collider will give final word on anomaly

- In case it will persist polarised beams will allow for discrimination between effects on left and right handed couplings

- Randall Sundrum Models generate basically automatically a symmetry group of type $SU(2)_R$

Randall Sundrum Models Djouadi/Richard '06

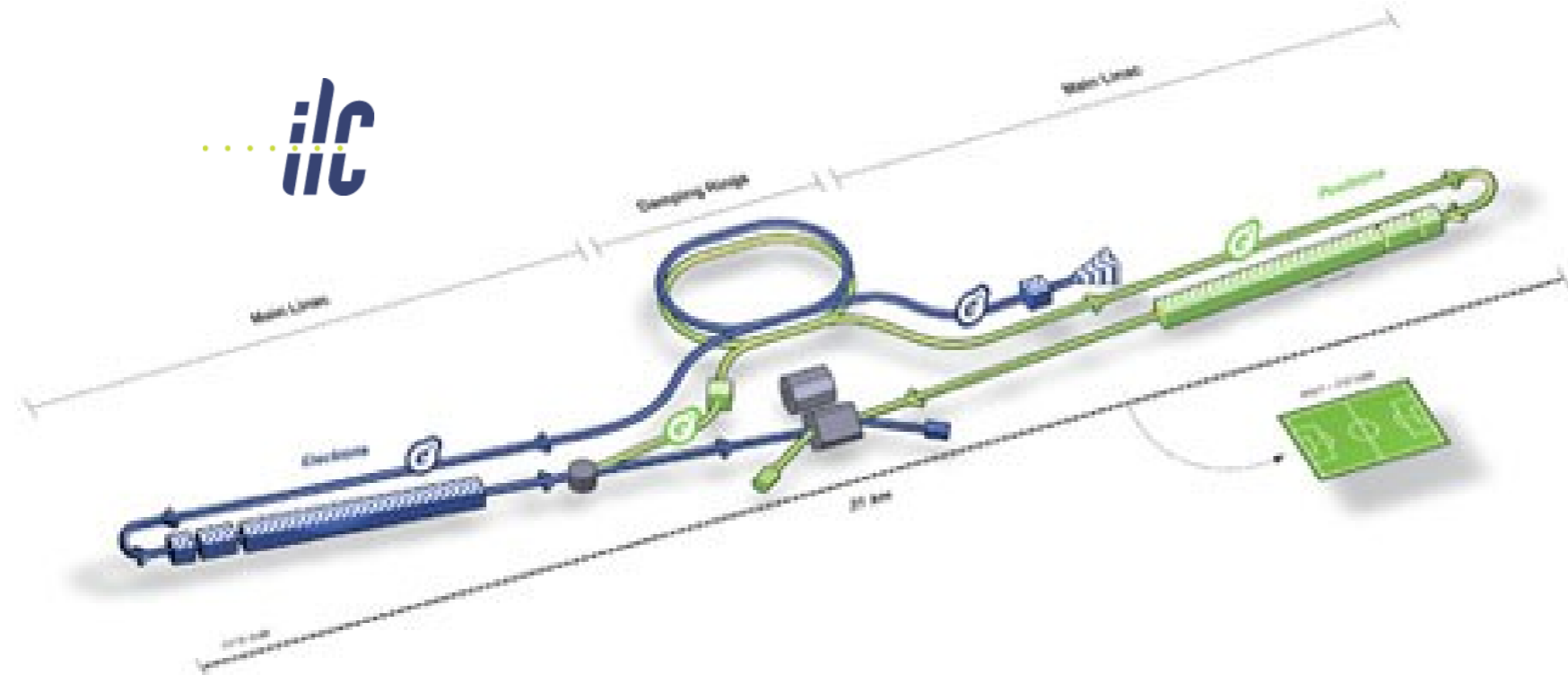
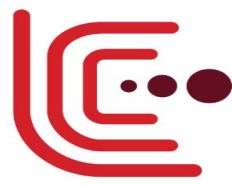
	\sqrt{s}	beam polarisation	$\int L dt$ for Higgs	R&D phase	
ILC	0.1 - 1 TeV	e-: 80% e+: 30%	2000 fb-1 @ 250 GeV 200 fb-1 @ 350 GeV 4000 fb-1 @ 500 GeV	TDR completed in 2013	Details see talk by Y. Okada
CLIC	0.35 - 3 TeV	e-: (80%) e+: 0%	1000 fb-1 @ 380 GeV 2500 fb-1 @ 1.5 TeV 5000 fb-1 @ 3 TeV	CDR completed in 2012	
CEPC	90 - 240 GeV	e-: 0% e+: 0%	5600 fb-1 @ 240 GeV	CDR completed in 2018	Details see talk by M. Ruan
FCC-ee	90 - 350 GeV	e-: 0% e+: 0%	5000 fb-1 @ 250 GeV 1700 fb-1 @ 350 GeV	CDR completed in Jan 2019	

Table courtesy of J. Brau

Open questions



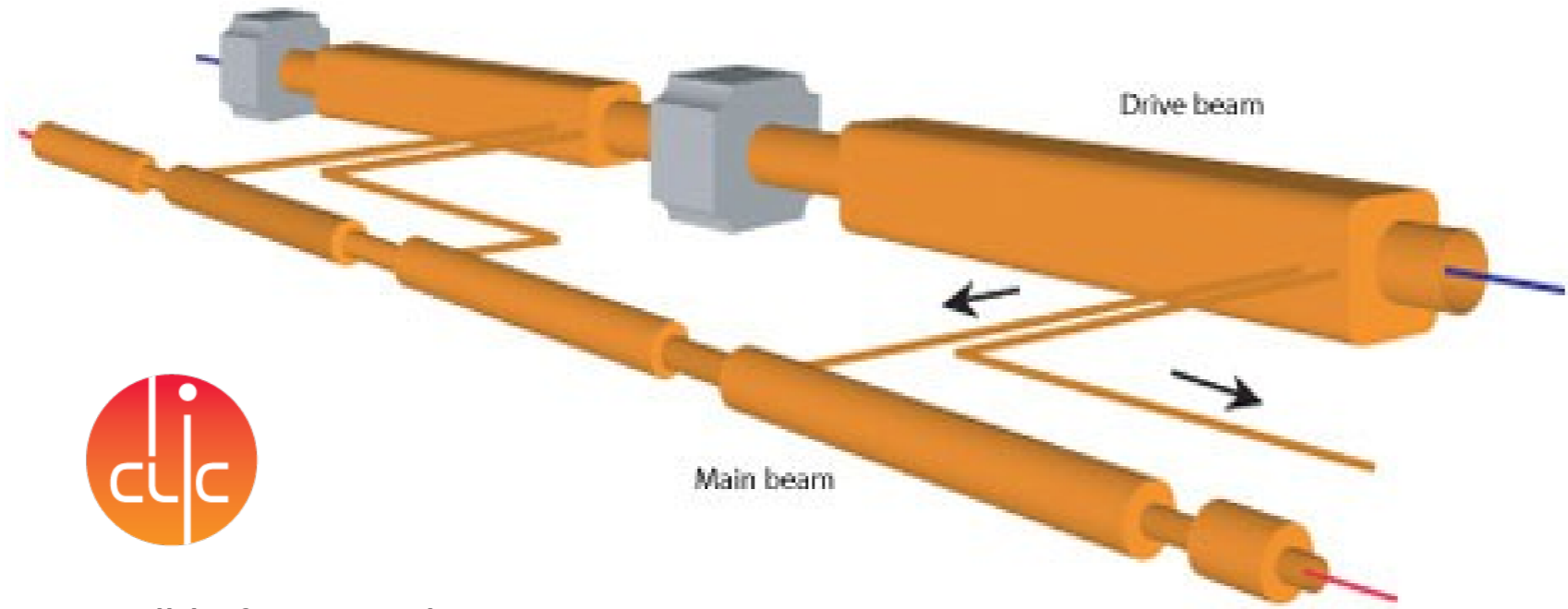
Linear Electron-Positron Colliders



Energy: 0.1 - 1 TeV
Electron (and positron) polarisation
TDR in 2013
+ DBD for detectors
 Footprint 31 km

Initial Energy 250 GeV – Footprint ~20km

Japanese Government expressed its interest in project in March 2019



Energy: 0.4 - 3 TeV
CDR in 2012
 Footprint 48km
 Initial Energy 380 GeV

EFT: Two distinct observations

Observables at fixed mass m
(e.g. Z pole of Higgs decays)

$$\frac{\sigma}{\sigma_{SM}} \approx \left| 1 + \frac{c_6 m^2}{\Lambda^2} \right|^2$$

Increasing UV scales probed in EFT
achieved solely by increasing the
measurement precision

$$c_6 \sim (g^*)^2$$

Typical experimental precision 0.1-1%

High energy tails of distributions
(e.g. Drell-Yan Productions)

$$\frac{\sigma}{\sigma_{SM}} \approx \left| 1 + \frac{c_6 E^2}{\Lambda^2} \right|^2$$

Increasing UV scales probed in EFT
achieved solely by increasing the
energy scale of measurement precision

Typical experimental precision 10%

- Polarized beams play a crucial role in disentangling the two spin structures

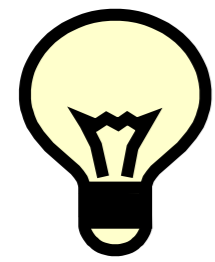
$$\sigma = \frac{2}{3} \frac{\pi \alpha_w^2}{c_w^4} \frac{m_Z^2}{(s - m_Z^2)} \frac{2k_Z}{\sqrt{s}} \left(2 + \frac{E_Z^2}{m_Z^2}\right) \cdot Q_Z^2 \cdot \left[1 + 2a + 2 \frac{3\sqrt{s}E_Z/m_Z^2}{(2 + E_Z^2/m_Z^2)} b\right]$$

The **a** and **b** coefficients depend on beam polarization:

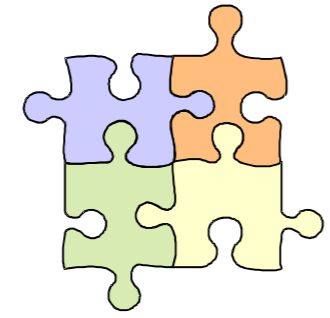
$$e_L^- e_R^+ \quad \begin{aligned} Q_{ZL} &= \left(\frac{1}{2} - s_w^2\right), & a_L &= -c_H \\ b_L &= c_w^2 \left(1 + \frac{s_w^2}{1/2 - s_w^2} \frac{s - m_Z^2}{s}\right) (8c_{WW}) \end{aligned}$$

$$e_R^- e_L^+ \quad \begin{aligned} Q_{ZR} &= (-s_w^2), & a_R &= -c_H \\ b_R &= c_w^2 \left(1 - \frac{s - m_Z^2}{s}\right) (8c_{WW}) \end{aligned}$$

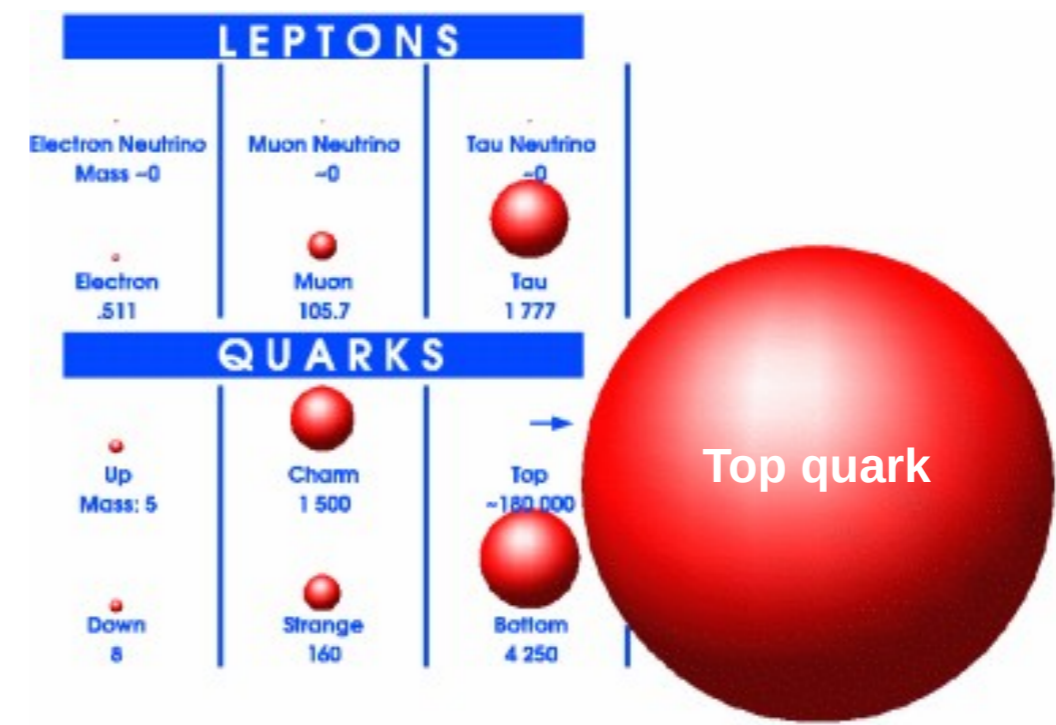
- Angular distributions in $e^+e^- \rightarrow hZ$ can also be used, but have weaker analyzing power and require more luminosity to achieve the same result



Elementary Scalar?



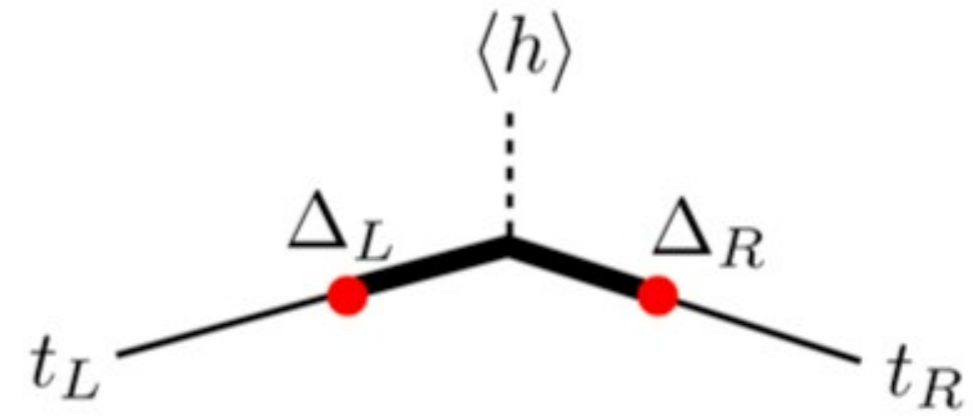
Composite object?



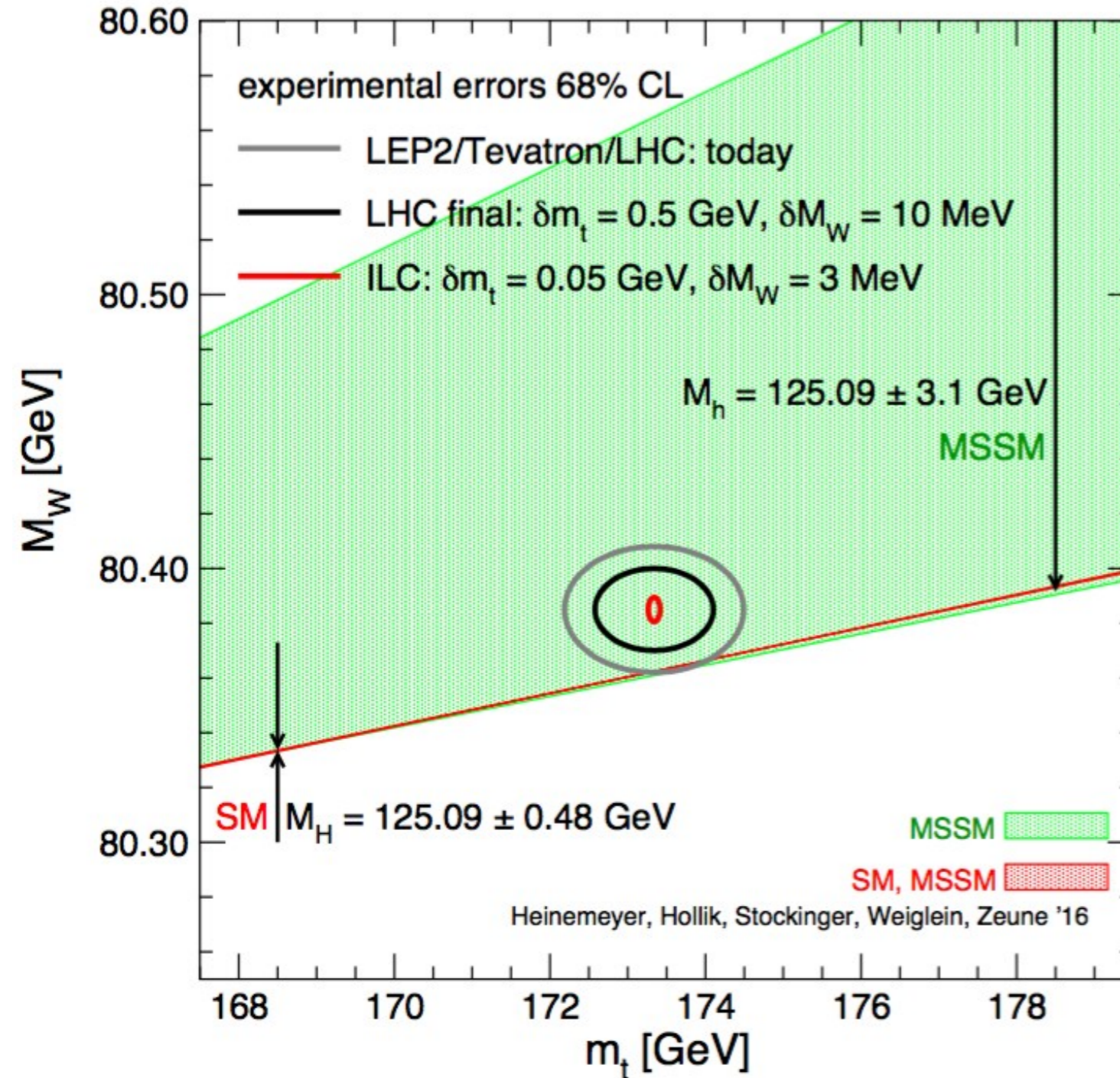
- Higgs and top quark are intimately coupled!
Top Yukawa coupling $O(1)$!
=> Top mass important SM Parameter

- New physics by compositeness?
Higgs and top composite objects?

- e+e- collider perfectly suited to decipher both particles

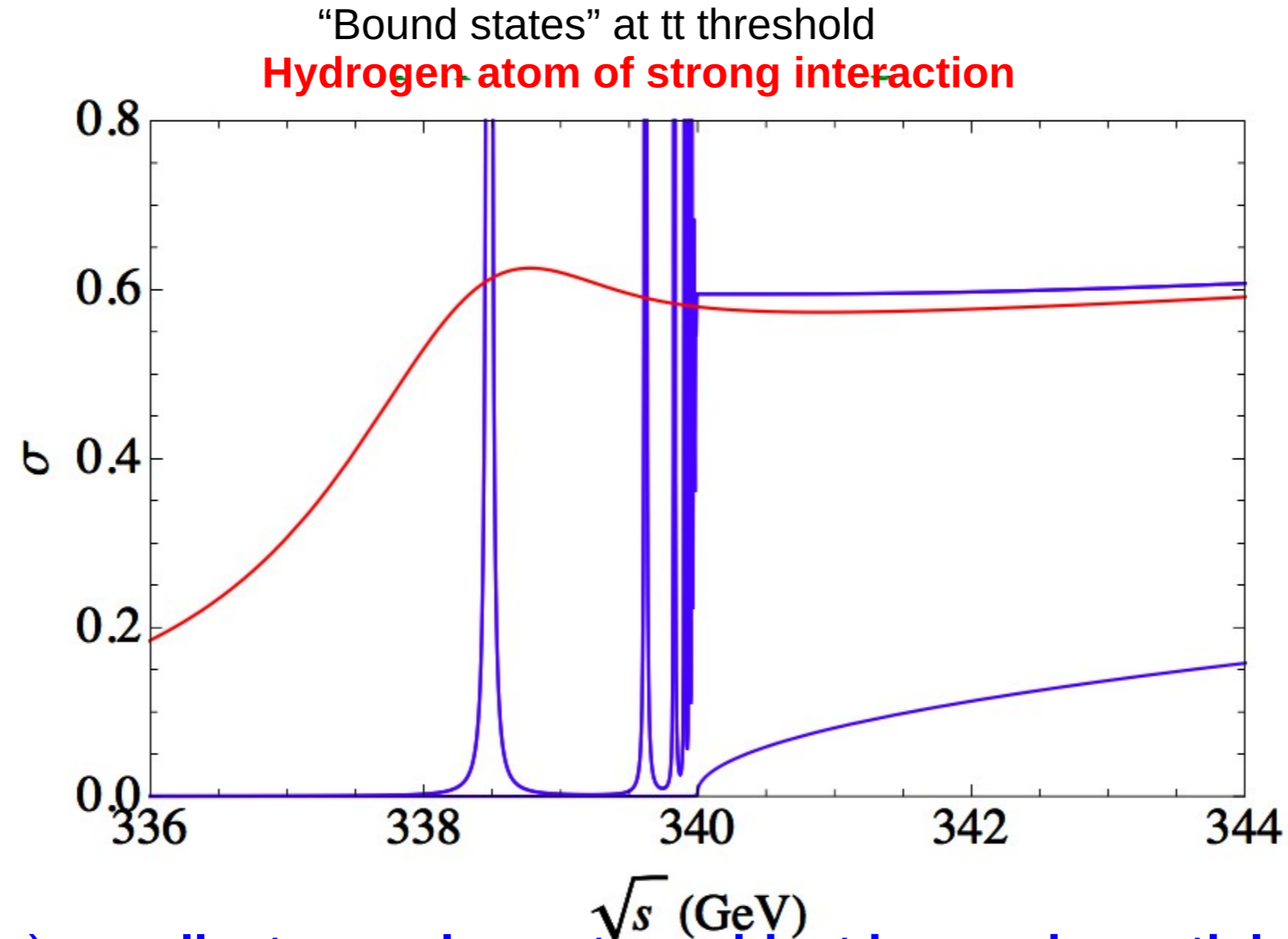


Courtesy of S. Rychkov



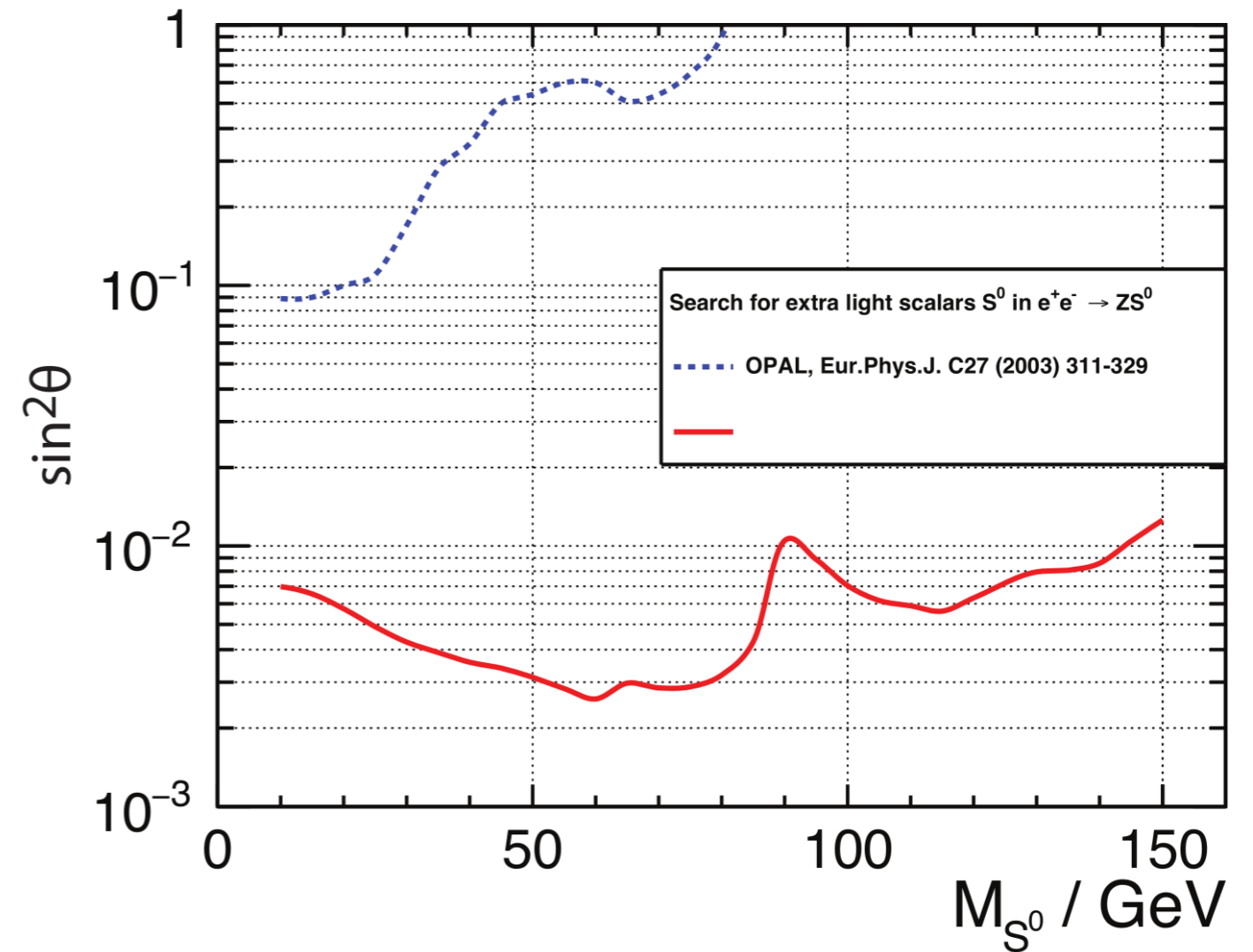
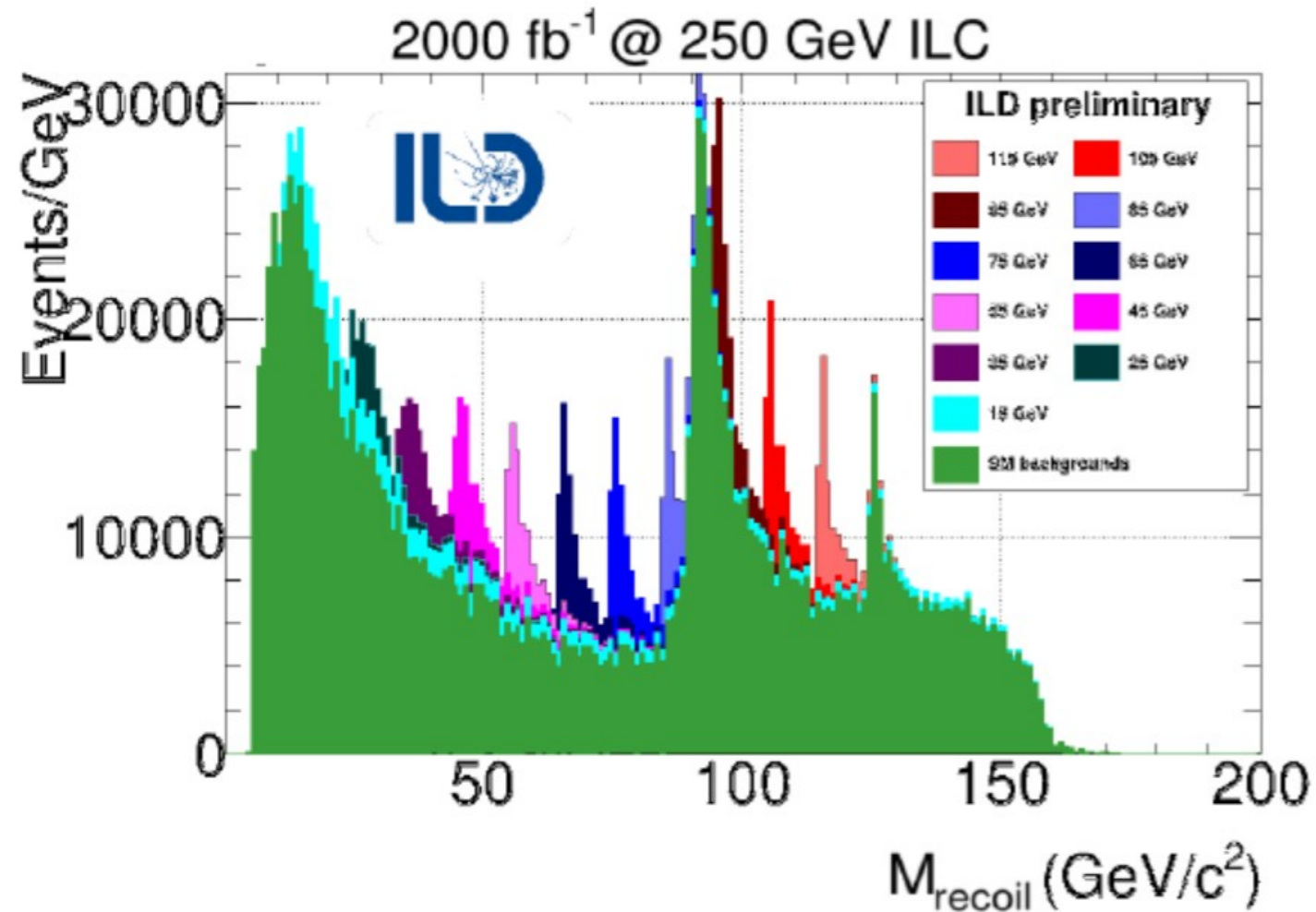
- Precise Top (and W) mass crucial to test compatibility of measured Higgs mass
- SM might not be sufficient to explain Higgs mass
- LHC may not reach sufficient discriminative power
- A lepton collider will for sure

Top pair production at threshold



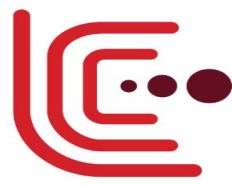
- Size $O(10^{-17}\text{m})$, **smallest non-elementary object known in particle physics**
 Small scale \Rightarrow Free of confinement effects \Rightarrow Ideal premise for precision calculations
 Measurement of (a hypothetical) 1^3S_1 State
- **Decay of top quark smears out resonances in a well defined way**

Light scalar may be missing piece to trigger first order 1st transition and/or the being the radion in extra dimension theories

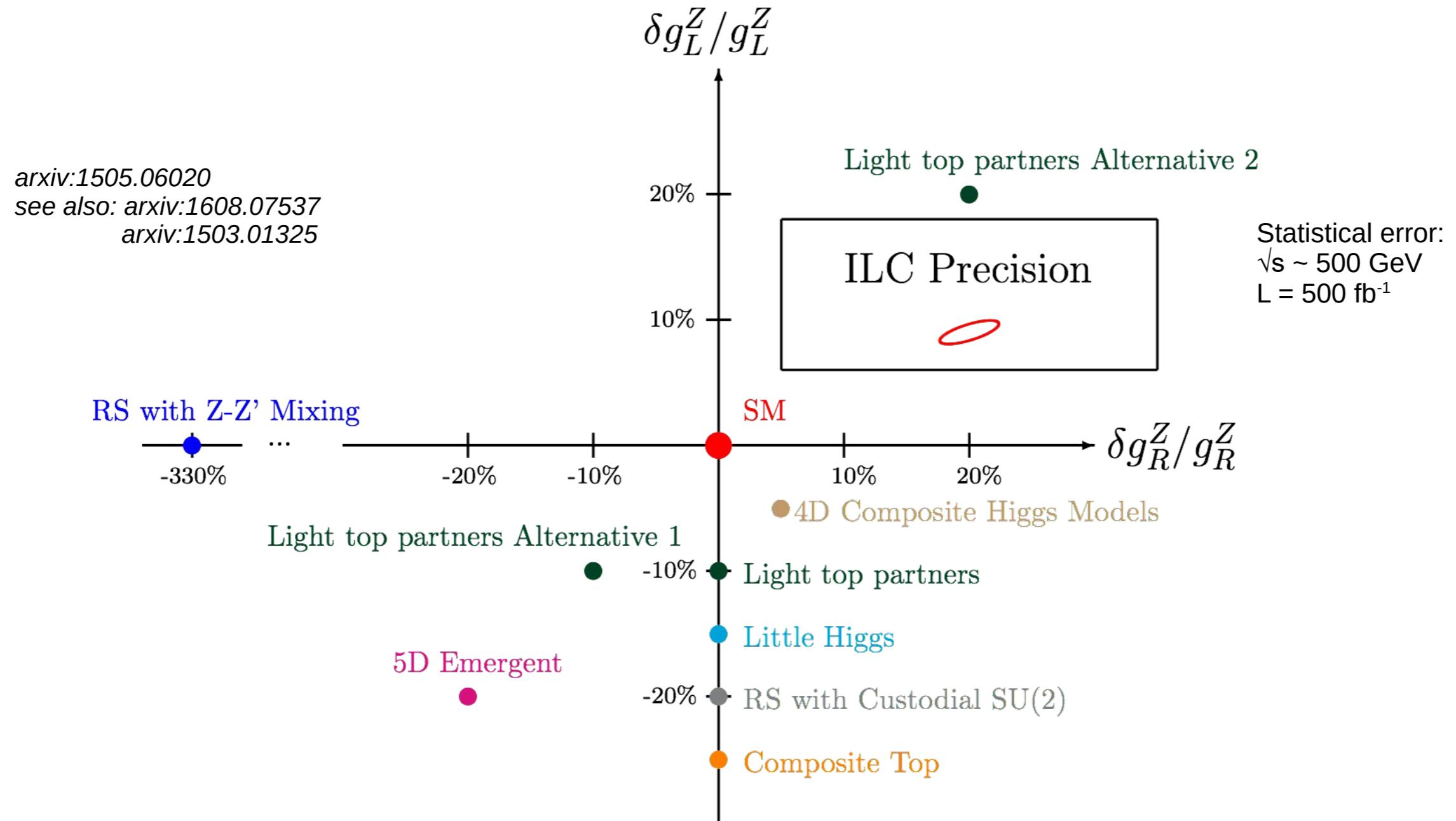


- New resonances cleanly distinguishable for large range of masses
- Sensitivity to mixing angle θ_h down to 10^{-2} (taking all relevant backgrounds into account)
- New scalar would count as “Feebly interacting Particle” (FIPS)

Electroweak top couplings

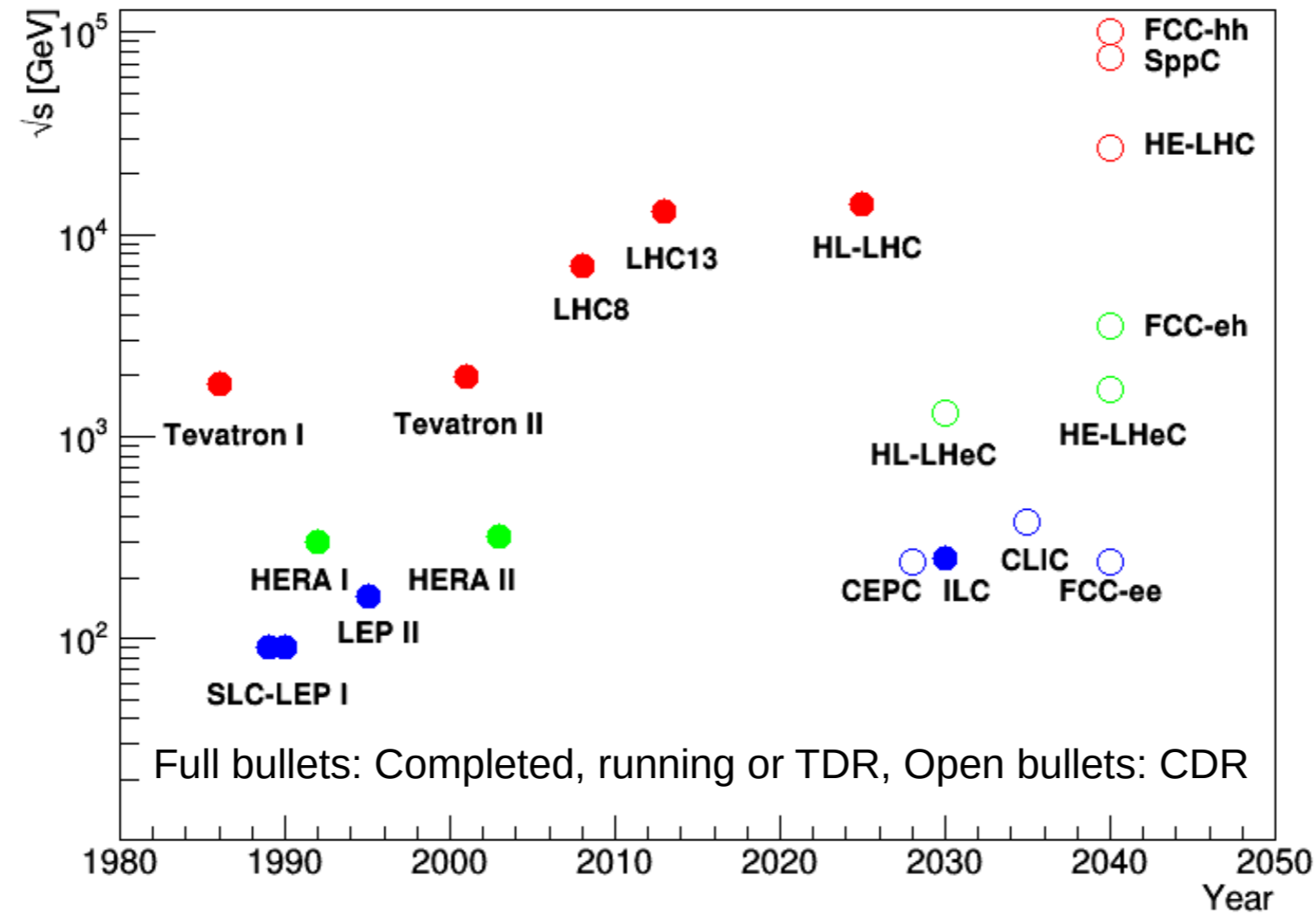


Top is primary candidate to be a messenger new physics in many BSM models



Precision expected for top quark couplings will allow to distinguish between models

Remark: All presented models are compatible with LEP elw. precision data



- ILC is the only machine that can be built now
 - European XFEL gives credibility for construction