

The LHC Higgs Cross Section Working Group

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On behalf of the LHC Higgs (Cross Section) Working Group

- Special thanks to colleagues from Theory, ATLAS and CMS -



HiggsDiscovery@10 Symposium,
June 30th 2022, Birmingham



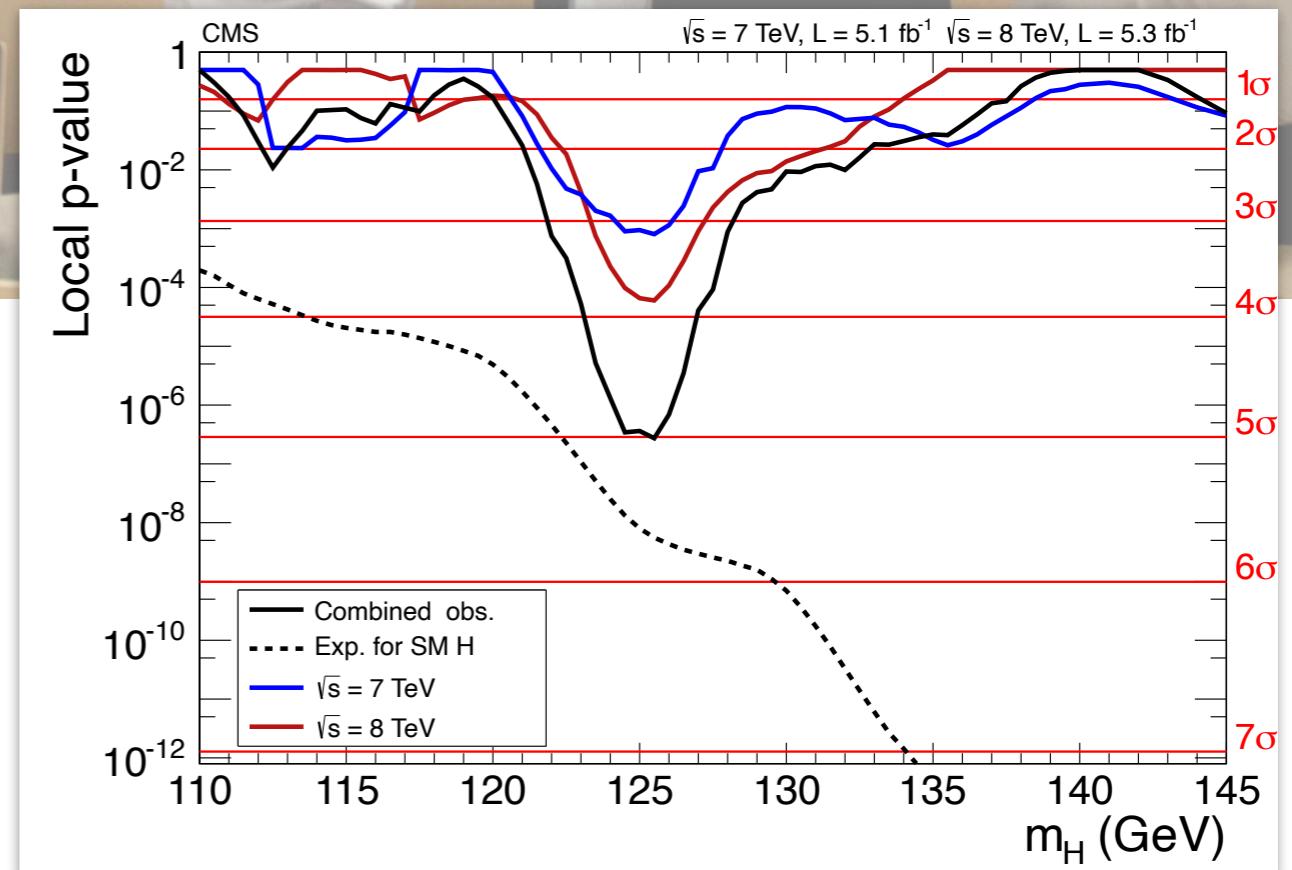
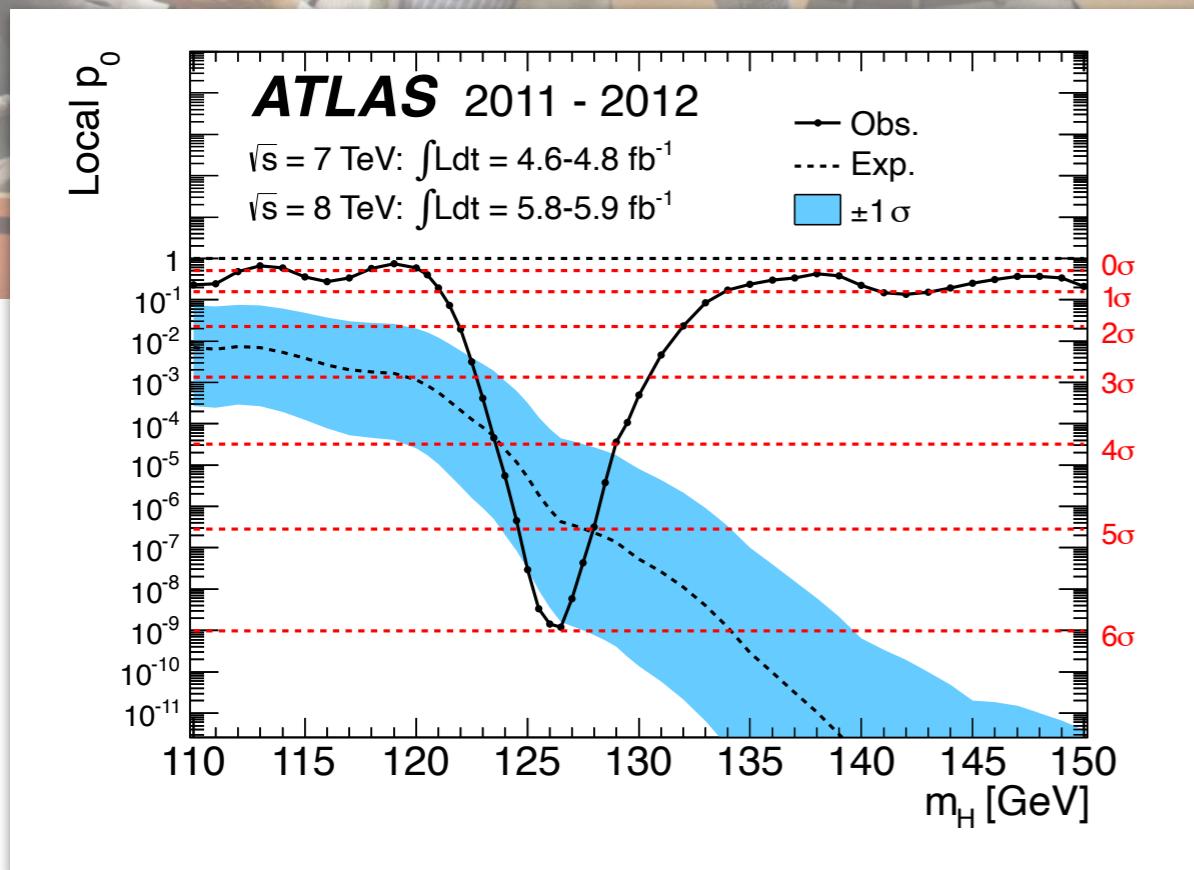
What LHCHXSWG did for July 4th 2012 discovery?

I was there!

July 4th

PLB 716 (2012) 1

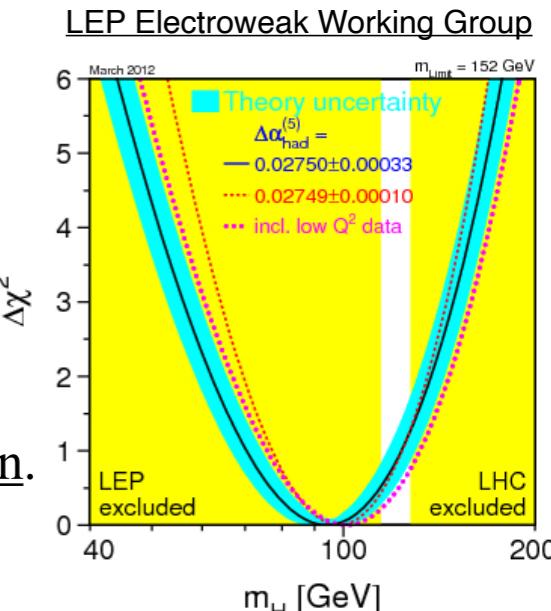
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Why LHC Higgs Cross Section Working Group ?

Preamble

- In late 2000's, a bunch of people had an idea to form TH+ATLAS+CMS forum for Higgs boson precision physics (discussions initiated by G. Passarino).
 - The Higgs boson discovery could happen earlier than expected if light Higgs boson.
 - Many theoretical progresses on Higgs physics before LHC start.
 - **Interactions between TH and EXPs for common language are very important.**
- **Access to the most advanced theory predictions for Higgs Cross Sections and Branching Ratios**
 - Experiments will coherently use the common XS&BR's based on the interaction with the TH community.
 - This will facilitate the comparison and the combination of the individual results.
(LHC Higgs Combination Group was created later.)
 - In case of a deviation from SM prediction, precise theoretical prediction are mandatory.
- **The LHC Higgs Cross Section Working Group was created in January 2010.**
 - The pre-foundation meeting was held in Torino during 23-24, November, 2009 - 1st LHC collision day !
 - The first coordinators: S. Dittmaier (TH), C. Mariotti (CMS), G. Passarino (TH), R. Tanaka (ATLAS)



LHC Higgs Cross Section Working Group



LHC Higgs XS WG CERN Reports

Handbook of LHC Higgs Cross Sections:

1. Inclusive Observables ([CERN-2011-002](#), 151 pp.)
2. Differential Distributions ([CERN-2012-002](#), 275 pp.)
3. Higgs Properties ([CERN-2013-004](#), 392 pp.)
4. Deciphering the nature of the Higgs sector ([CERN-2017-002-M](#), 869 pp.)

July 4th 2012
Higgs boson Discovery

LHC Higgs Cross Section Working Group



Run 1				Run 2					Run 3					
2009	2010	2011	2012	2013	2014	2015	2016	2017	2018	2019	2020	2021	2022	2023
Aug. TH&ATLAS& CMS proposal for joint forum for Higgs XS	Jan. Creation LHCXSWG	YR1	YR2	YR3				YR4			Nov. LHC Higgs XS WG ⇒ LHC Higgs WG			
Nov. 23-24 Torino WS @ LHC 1st pp collision	Apr. Inauguration WS in Freiburg		July 4th Higgs boson Discovery											

LHC Higgs XS WG CERN Reports

Handbook of LHC Higgs Cross Sections:

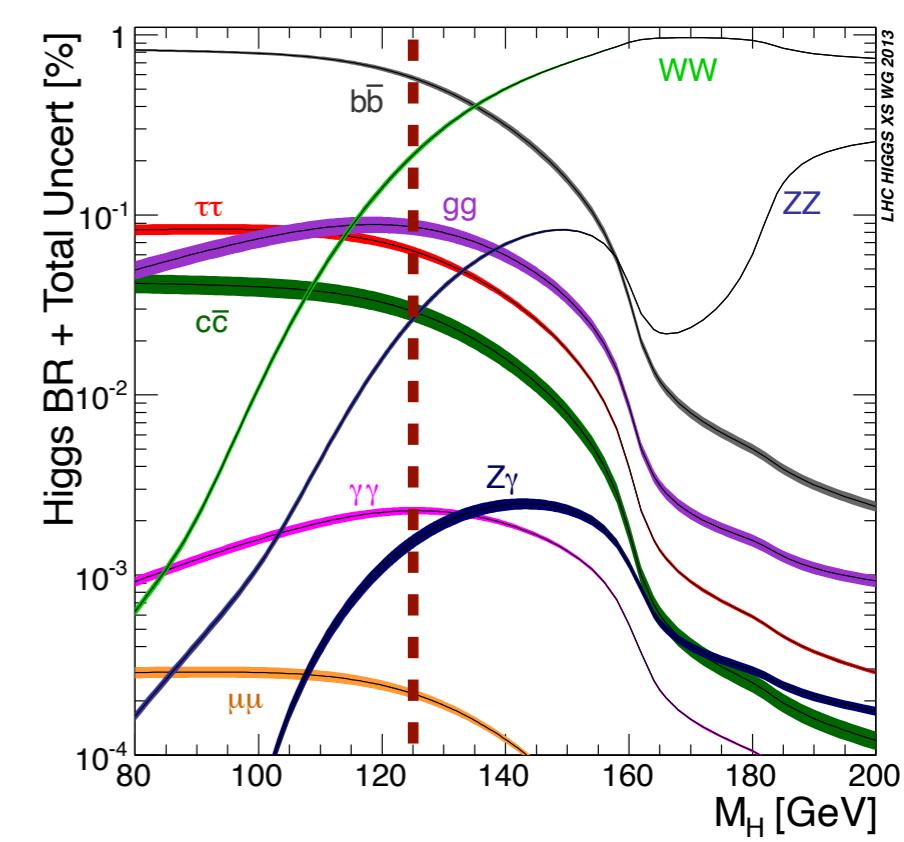
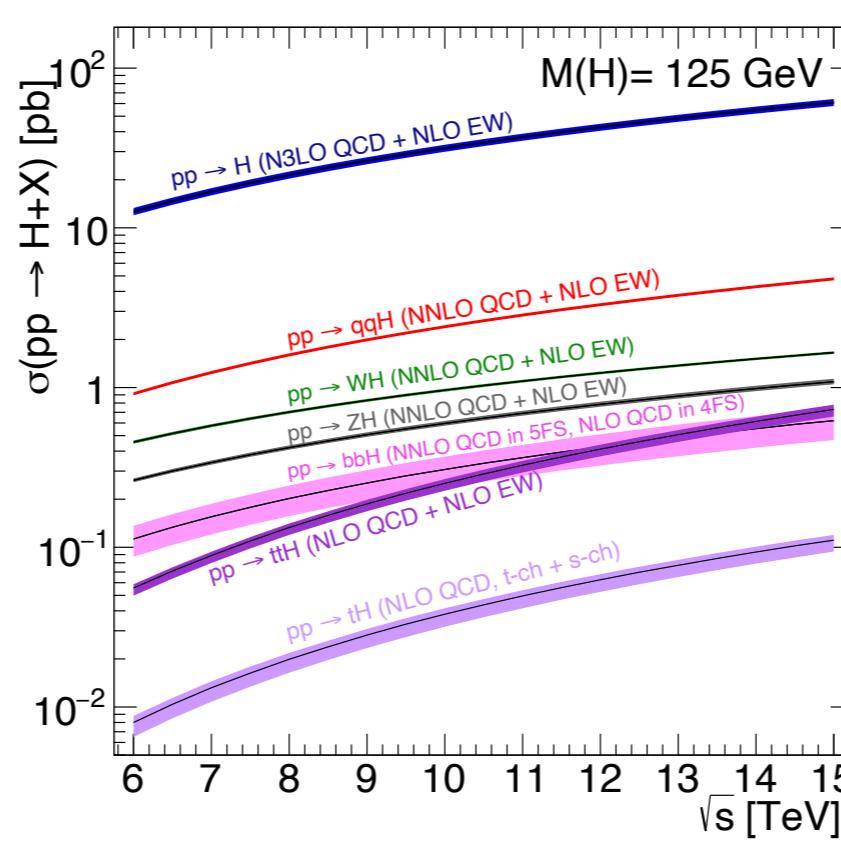
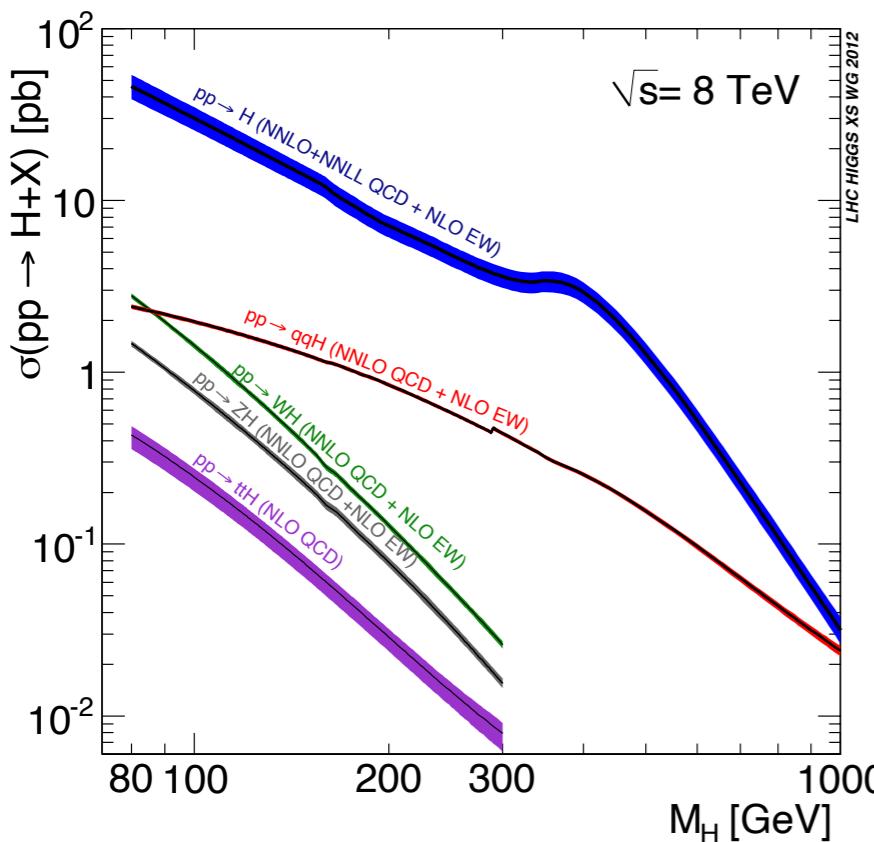
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You can safely say that it (YR4) is the "heaviest Yellow Report" ever –digital versions have no weight !
(CERN Library)

Higgs boson production XS & decay BR

- State-of-the-art Higgs XS and BR predictions with estimated theory uncertainties
- Common SM input parameters coordinated for calculation for different processes
- Mostly NNLO QCD + NLO EW production cross section
- N3LO for ggF (ATLAS and CMS adopted promptly)
- $M_H=125\text{GeV}$ was lucky to have many different decay channels

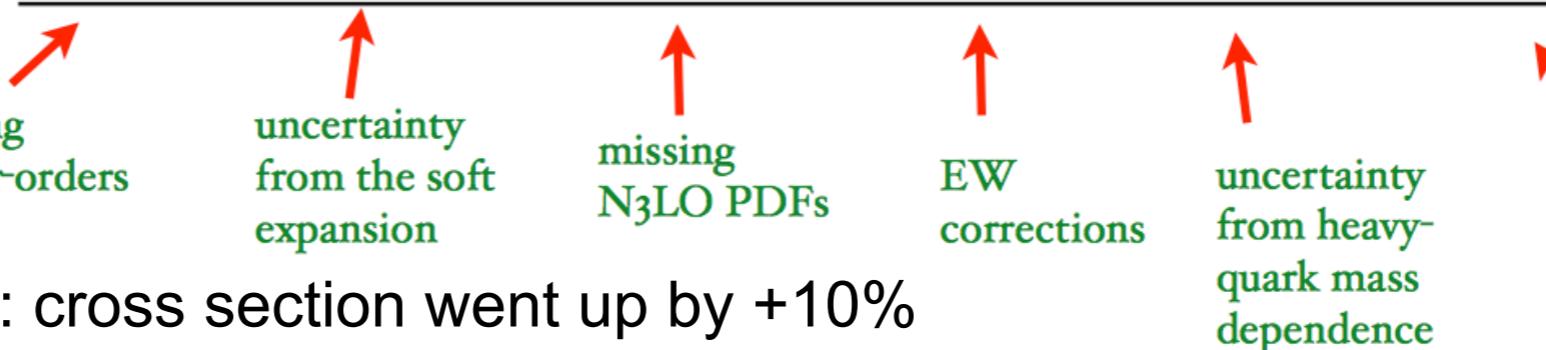
- ATLAS and CMS had common XS&BR numbers since Day-0 well before Higgs boson discovery when we did not know where it is.
- ~240k Higgs boson when Discovery, 9M in RUN-2, will produce 190M in HL-LHC (3 ab^{-1})



gg \rightarrow H gluon-gluon fusion Cross Section

- First complete N3LO calculation at hadron collider ! [\[Anastasiou:2016cez\]](#)

$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
+0.10 pb -1.15 pb	± 0.18 pb	± 0.56 pb	± 0.49 pb	± 0.40 pb	± 0.49 pb
+0.21% -2.37%	$\pm 0.37\%$	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$


 missing higher-orders
 uncertainty from the soft expansion
 missing N₃LO PDFs
 EW corrections
 uncertainty from heavy-quark mass dependence
 uncertainty in the 1/m_t included corrections

13TeV, M_H=125GeV: cross section went up by +10%

$$\sigma = 48.58 \text{ pb}^{+2.22 \text{ pb} (+4.56\%)}_{-3.27 \text{ pb} (-6.72\%)} \text{ (theory)} \pm 1.56 \text{ pb} (3.20\%) \text{ (PDF+}\alpha_s\text{)}$$

- NNLO+NNLL: $\sigma = 44.14 \text{ pb} +7.6 -8.1\% \text{ (QCD scale)} \pm 3.1\% \text{ (PDF+}\alpha_s\text{)}$

- Debates on TH QCD scale uncertainty treatment

 **TH: use Flat uncertainty: [-6.7, +4.6]@100% CL**

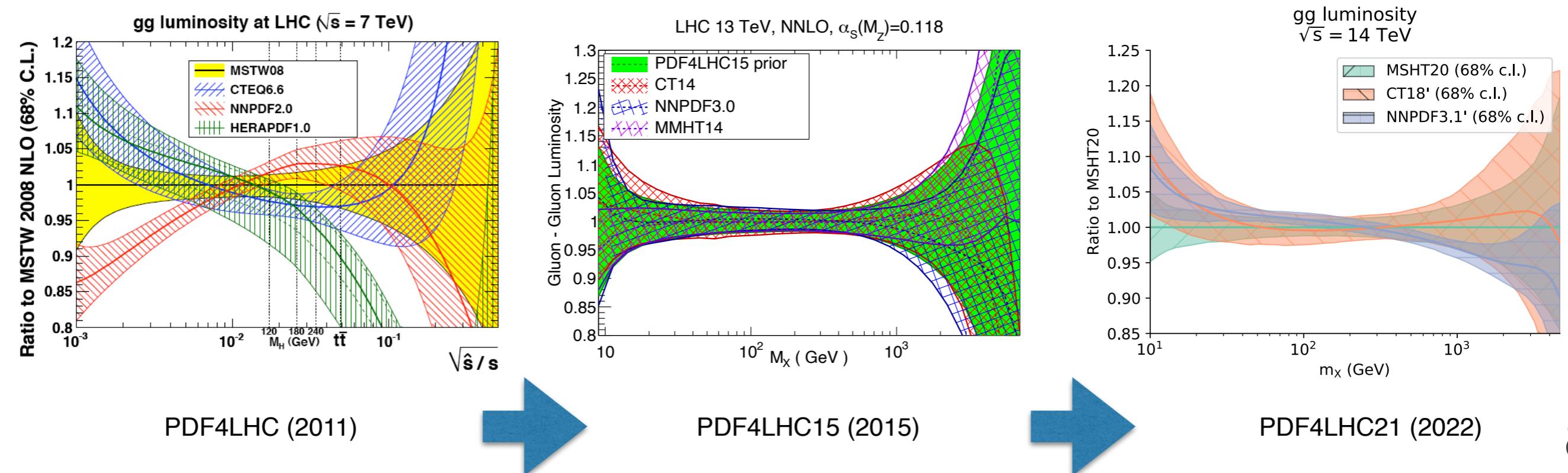
$$\rho(\theta) = \frac{1}{\sqrt{2\pi} \ln(\kappa)} \exp \left(-\frac{(\ln(\theta/\tilde{\theta}))^2}{2(\ln \kappa)^2} \right) \frac{1}{\theta}$$

 **EXP: use Gaussian uncertainty: max{neg, pos}/\sqrt{3} = ±3.9% @67% CL** $\theta=\sigma$ for $\kappa=1$

 Use this number for current workspace construction à la LHC-HCG prescription, “Procedure for the LHC Higgs boson search combination in Summer 2011”, ATL-PHYS-PUB-2011-11 CMS NOTE-2011/005

Parton Distribution Functions (PDF)

- **PDF4LHC** ([arXiv:1101.0536](#), [arXiv:1101.0538](#))
 - NLO PDF sets for Run-1: CT10, MSTW2008, NNPDF2.3
 - Uncertainty provided by the envelope of all three PDF sets and central prediction as mid-point.
- **PDF4LHC15** ([J. Phys. G: Nucl. Part. Phys. 43 \(2016\) 023001](#))
 - NNLO PDF sets for Run-2: CT14, MMHT2014, NNPDF3.0
 - Alternative PDF sets: ABM12, CJ15, HERAPDF2.0, JR14 (richness of this field !)
 - Large improvements in PDF due to inclusion of LHC data and improvements in the fitting formalisms.
 - **ggF PDF $\oplus\alpha_s$ uncertainty at $\sqrt{s}=14\text{TeV}$ for $M_H=125\text{GeV}$: $+8\text{-}7\% \rightarrow \pm 3.2\%$ (PDF $\pm 1.9\%$, $\alpha_s \pm 2.6\%$)**
 - Agreement in gg-parton luminosity was accidental.
- **New PDF4LHC21** ([arXiv:2203.05506](#))
 - NNLO PDF sets for Run-3: CT18, MSHT20, NNPDF3.1
 - **Good agreement between global PDF fits in both gg&qq-parton luminosities and reduction in uncertainties !**



Higgs boson decay width and branching ratio

Uncertainties in Branching Ratio (LHC-HCG)

1. Start with Higgs boson decay width

$$\Gamma_H = \Gamma_{\text{HDECAY}} - \Gamma_{\text{WW}} - \Gamma_{\text{ZZ}} + \Gamma_{\text{4f}}^{\text{Prophecy4f}}$$

2. Categorize PU(α_s , m_b , m_c , m_t) and THU

Separate treatment of PU($\Delta\alpha_s$, Δm_q) and THU

3. Convert to BR (correlations are taken into)

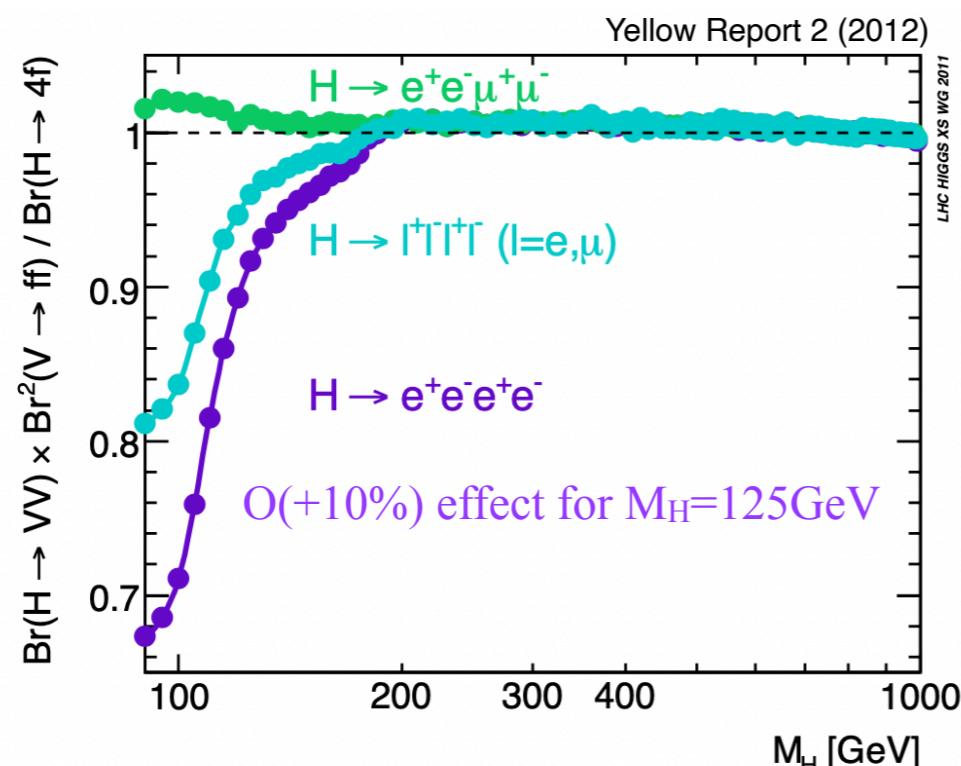
Partial cancellation for $H \rightarrow bb, cc$ but not for gg !

$$BR(H \rightarrow VV) = \frac{\Gamma_{VV}}{\Gamma_{\text{tot}}} = \frac{\Gamma_{VV}}{\Gamma_{ff} + \Gamma_{gg} + \Gamma_{VV}}$$

$$\Gamma_{ff} : \Gamma_{VV} \simeq 3 : 1 \text{ (dominated by } \Gamma_{bb})$$

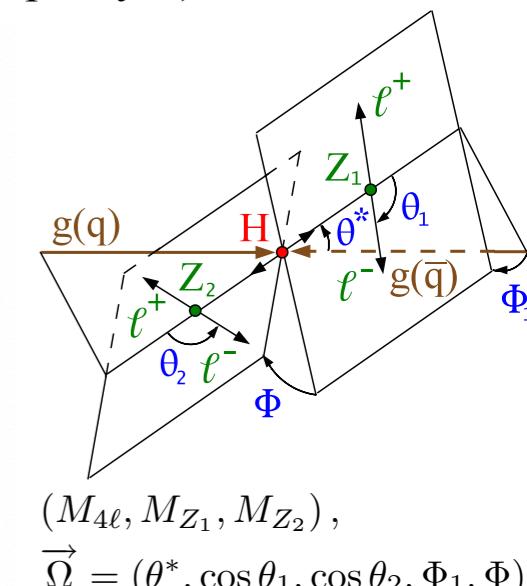
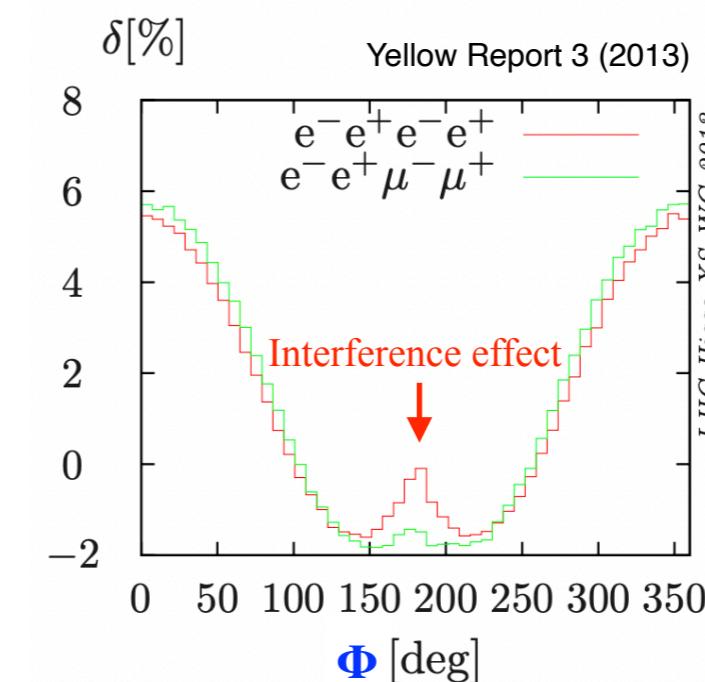
Precise $H \rightarrow 4f$ BR estimation and Monte Carlo at NLO EW

Interference effect in $H \rightarrow ZZ^* \rightarrow e^+e^-e^+e^-$, $\mu^+\mu^-\mu^+\mu^-$



$M_H=126\text{GeV}$	Decay width uncertainty				
Decay	$\Delta\alpha_s$	Δm_b	Δm_c	Δm_t	THU
$H \rightarrow bb$	$\pm 2.3\%$	$\pm 3.3\%$	$\pm 0.0\%$	$\pm 0.0\%$	$\pm 2.0\%$
$H \rightarrow cc$	$\pm 7.1\%$	-0.1%	$\pm 6.2\%$	$\pm 0.1\%$	$\pm 2.0\%$
$H \rightarrow \tau\tau$	$\pm 0.0\%$	$\pm 0.0\%$	$\pm 0.0\%$	$\pm 0.1\%$	$\pm 2.0\%$
$H \rightarrow \mu\mu$	$\pm 0.0\%$	$\pm 0.0\%$	$\pm 0.1\%$	$\pm 0.1\%$	$\pm 2.0\%$
$H \rightarrow gg$	$\pm 4.2\%$	-0.1%	$\pm 0.0\%$	$\mp 0.2\%$	$\pm 3.0\%$
$H \rightarrow \gamma\gamma$	$\pm 0.0\%$	$\pm 0.0\%$	$\pm 0.0\%$	$\pm 0.1\%$	$\pm 1.0\%$
$H \rightarrow Z\gamma$	$\pm 0.0\%$	$\pm 0.0\%$	$\pm 0.1\%$	$\pm 0.1\%$	$\pm 5.0\%$
$H \rightarrow WW$	$\pm 0.0\%$	$\pm 0.0\%$	$\pm 0.0\%$	$\pm 0.0\%$	$\pm 0.5\%$
$H \rightarrow ZZ$	$\pm 0.0\%$	$\pm 0.0\%$	$\pm 0.0\%$	$\pm 0.0\%$	$\pm 0.5\%$

Precise $H \rightarrow 4f$ Monte Carlo (Prophecy4f) at NLO EW



Challenges beyond Yellow Report 4 - selected topics

ggF

- N3LO differential distributions
- Reduction of ggF in VBF category
- Boosted Higgs XS

STXS & Fiducial/Differential XS

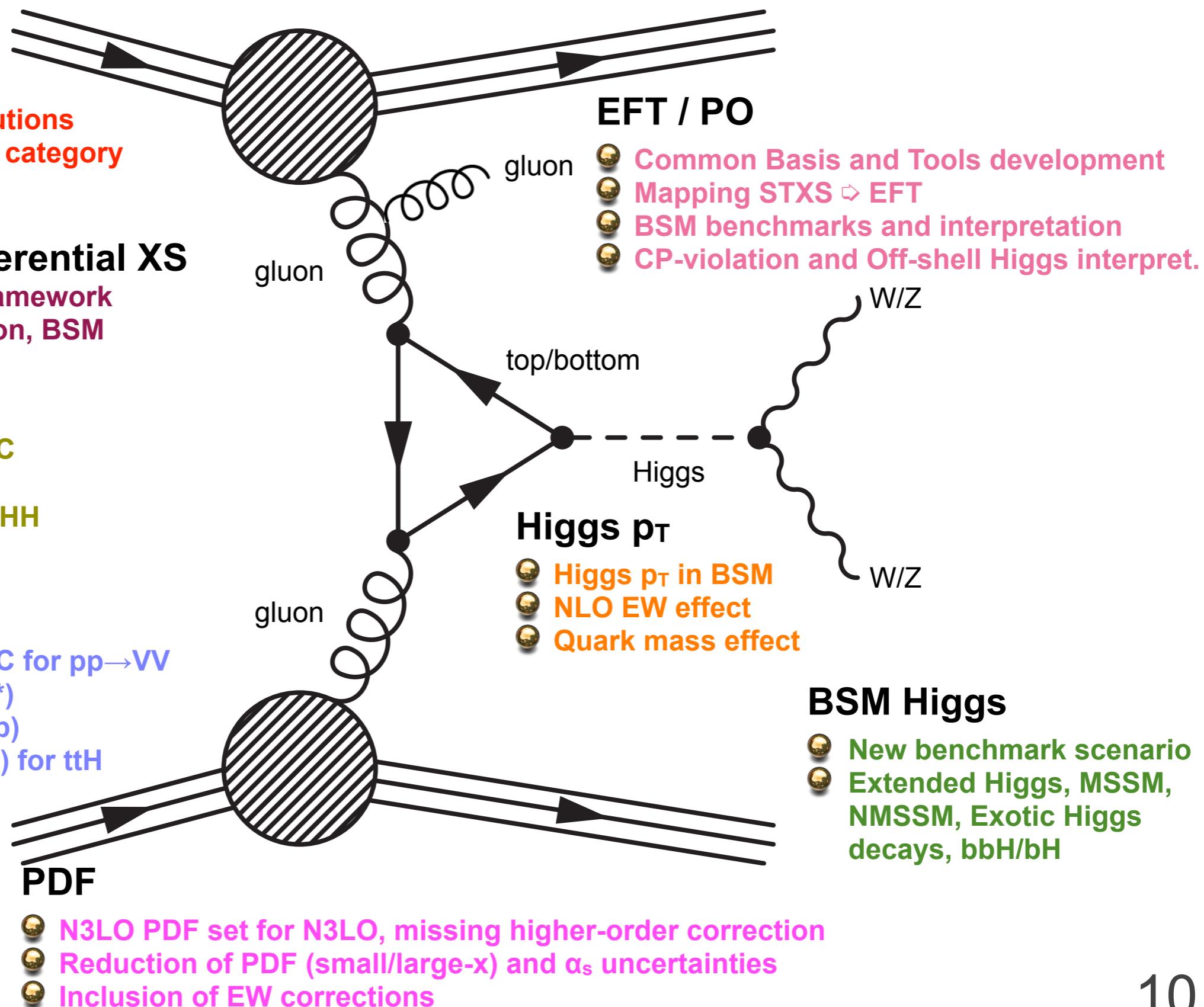
- Uncertainties in STXS framework
- STXS bins for CP-violation, BSM

(N)NLO MC

- NNLO QCD + NLO EW MC
- $\Delta\phi_{jj}$ in H+2-jets MC
- NLO MC for $gg \rightarrow VV, ZH, HH$
- PS Uncertainties

SM Backgrounds

- NNLO QCD + NLO EW MC for $pp \rightarrow VV$
(include off-shell, ex Z^*Z^*)
- V+HF modeling for VH(bb)
- ttbar+V/HF+jets (ttbb, ttV) for ttH



Higgs signal-strength

LO κ -framework

$$\mu = \frac{\sigma \cdot \text{BR}}{(\sigma \cdot \text{BR})_{\text{SM}}}$$

$$\mu = \frac{(\sigma \cdot \text{BR})(gg \rightarrow H \rightarrow \gamma\gamma)}{\{\sigma(gg \rightarrow H) \cdot \text{BR}(H \rightarrow \gamma\gamma)\}_{\text{SM}}} = \frac{\kappa_g^2 \cdot \kappa_\gamma^2}{\kappa_H^2}$$

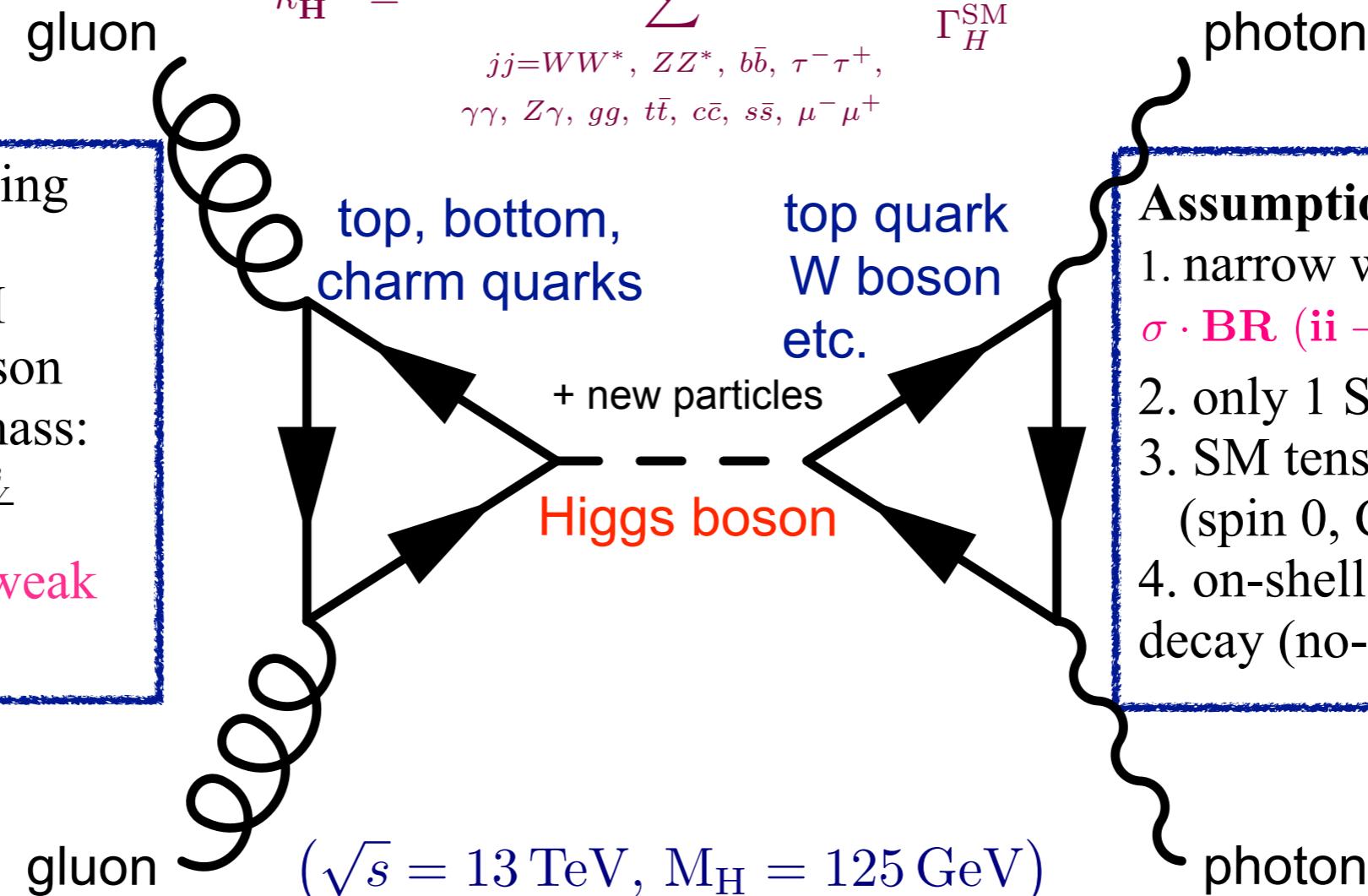
$$\kappa_H^2 = \sum_{jj=WW^*, ZZ^*, b\bar{b}, \tau^-\tau^+, \gamma\gamma, Z\gamma, gg, t\bar{t}, c\bar{c}, s\bar{s}, \mu^-\mu^+} \frac{\kappa_j^2 \Gamma_{jj}^{\text{SM}}}{\Gamma_H^{\text{SM}}}$$

- Measure with coupling scale factors κ_i .

- The coupling of SM particles to Higgs boson scales with particle mass:

$$g_F = \sqrt{2} \frac{m_f}{v}, g_V = 2 \frac{m_V^2}{v}$$

- Holds up to electroweak effects of $O(5\text{-}10\%)$.



Assumptions

1. narrow width approx. $\sigma \cdot \text{BR} (ii \rightarrow H \rightarrow ff) = \frac{\sigma_{ii} \cdot \Gamma_{ff}}{\Gamma_H}$
2. only 1 SM-like Higgs
3. SM tensor structure (spin 0, CP-even)
4. on-shell production and decay (no-sense for offshell).

$$\begin{aligned} \kappa_g^2(\kappa_t, \kappa_b, \kappa_c) &= 1.040\kappa_t^2 + 0.002\kappa_b^2 + 0.00002\kappa_c^2 \\ &- 0.038\kappa_t\kappa_b - 0.005\kappa_t\kappa_c + 0.0004\kappa_b\kappa_c \end{aligned}$$

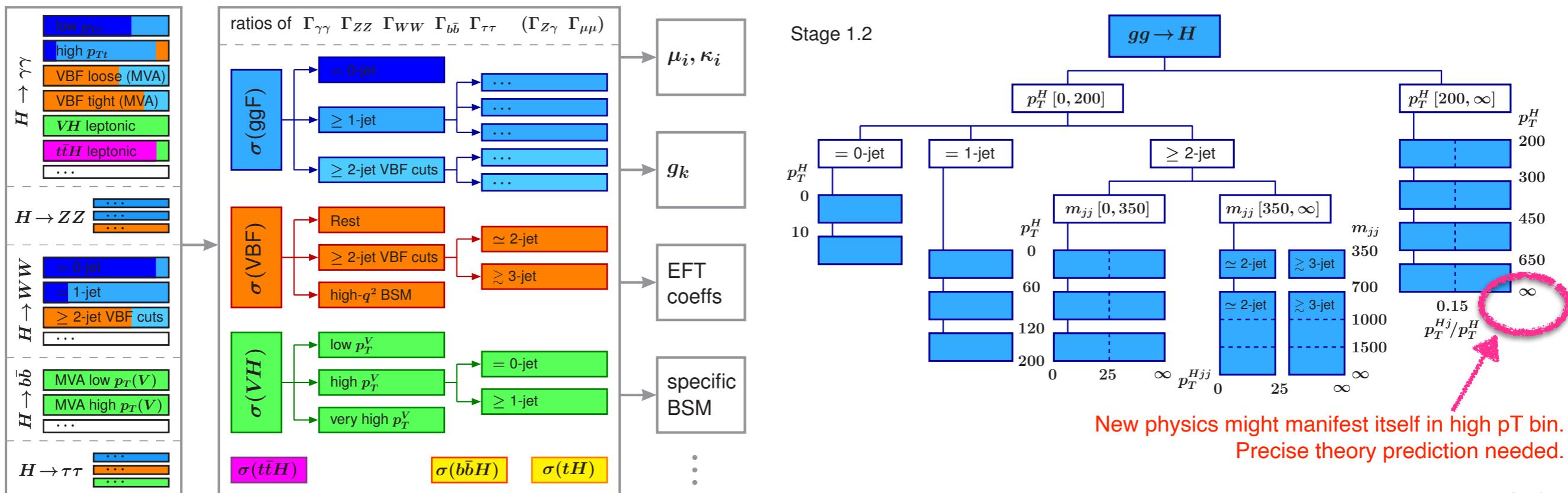
$$\kappa_\gamma^2(\kappa_W, \kappa_t) \simeq |1.26\kappa_W - 0.27\kappa_t|^2$$

Destructive interference in both $gg \rightarrow H$ (top-bottom) and $H \rightarrow \gamma\gamma$ (W-top) loops.

Simplified Template Cross Section (STXS)

- ➊ Divide phase space into simplified “bins”
- ➋ Maximise the measurement precision and the sensitivity to BSM contributions
- ➌ Production cross sections times BR measured in mutually exclusive phase space regions
- ➍ Based on production properties → allows combination of various decay modes
- ➎ Facilitates to compare/combine ATLAS+CMS results and to interpret theory models.
- ➏ Interpretation via Effective Field Theory (EFT)

- ➐ Fiducial Cross Section measurements in model-independent way.



Off-shell Higgs Boson Production and Interference

Kauer-Passarino-Caola-Melnikov Effect

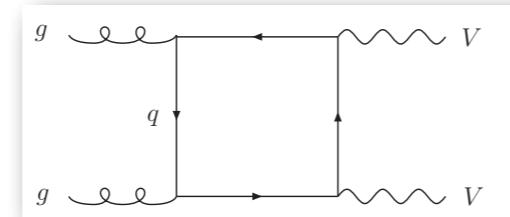
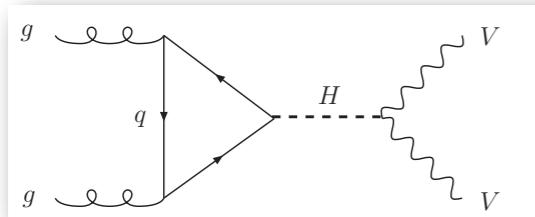
Total $gg \rightarrow H \rightarrow VV^*$ receives an $O(10\%)$ off-shell correction

On-shell signal cross section is proportional to $1/\Gamma_H$

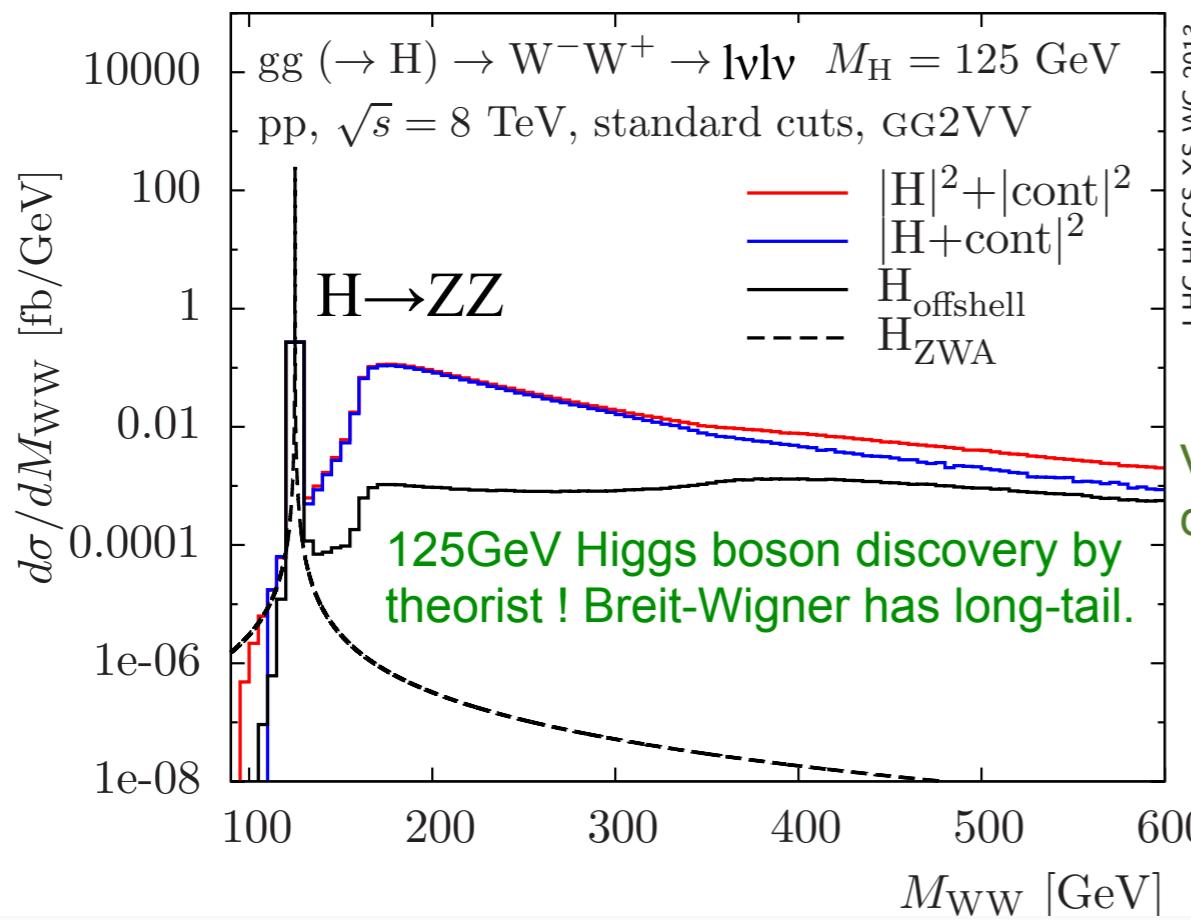
Off-shell signal cross section is independent of Γ_H

$\mu_{\text{off-shell}}/\mu_{\text{on-shell}}$ gives the information on Γ_H !

Negative signal-background interference effect

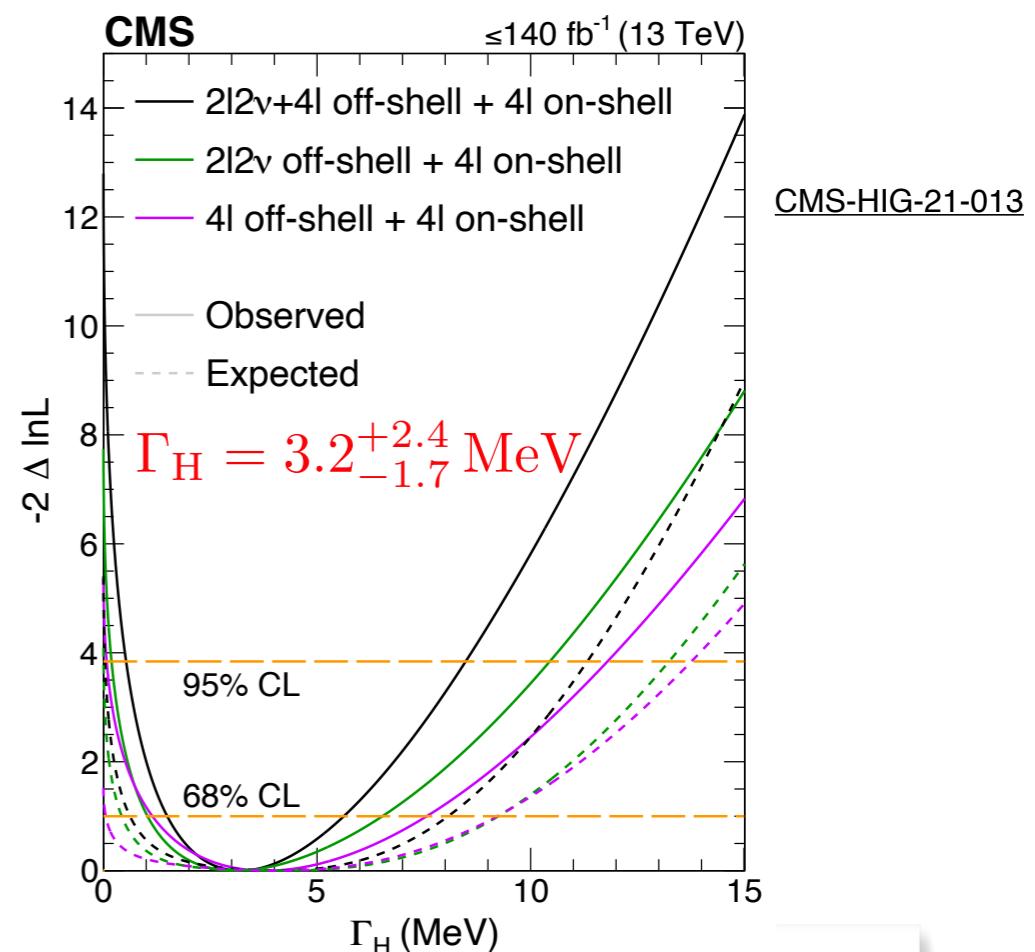
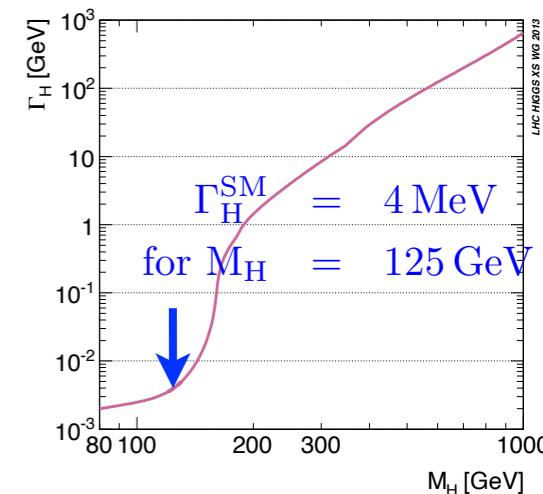


Yellow Report 3 (2013)



$$\sigma_{gg \rightarrow H \rightarrow VV}^{\text{on-shell}} \sim \frac{g_{Hgg}^2 g_{HVV}^2}{m_H \Gamma_H}$$

$$\sigma_{gg \rightarrow H \rightarrow VV}^{\text{off-shell}} \sim \frac{g_{Hgg}^2 g_{HVV}^2}{m_{VV}^2}$$

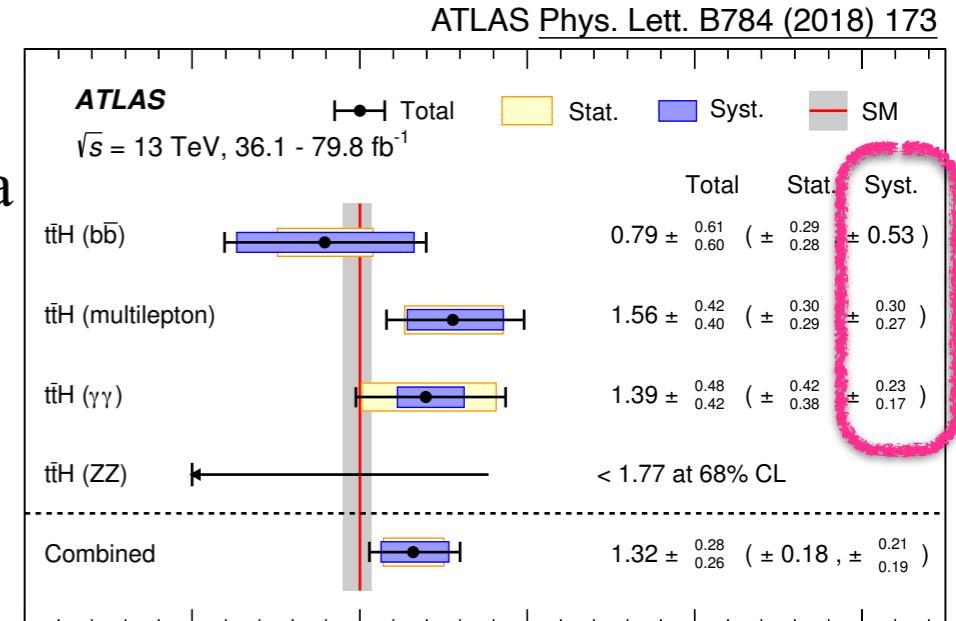
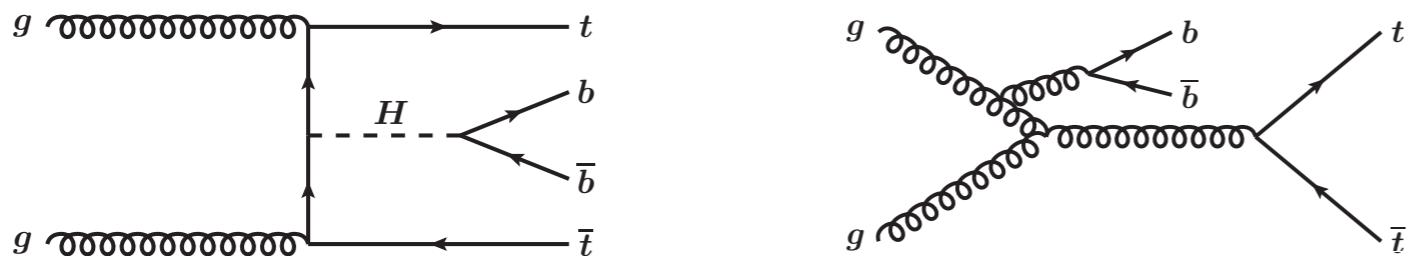


Large theoretical uncertainties in kinematical distributions due to QCD, PDF and EW corrections of $O(20-30\%)$ at high-mass.

Off-shell Sensitive to new physics \Rightarrow EFT interpretation

ttH($H \rightarrow bb$)

- ttH is a very important channel to measure Higgs-Yukawa coupling, spin/CP
- Overwhelming and irreducible backgrounds
 - ttbb in ttH($H \rightarrow bb$)
 - ttW in ttH(multi-lepton)



ATLAS arXiv:2111.06712

Uncertainty source	$\Delta\mu$	
Process modelling		
$t\bar{t}H$ modelling	+0.13	-0.05
$t\bar{t} + \geq 1b$ modelling	+0.21	-0.20
$t\bar{t} + \geq 1b$ NLO matching	+0.12	-0.12
$t\bar{t} + \geq 1b$ fractions	+0.10	-0.11
$t\bar{t} + \geq 1b$ FSR	+0.09	-0.08
$t\bar{t} + \geq 1b$ PS & hadronisation	+0.04	-0.04
$t\bar{t} + \geq 1b$ p_T^{bb} shape	+0.04	-0.04
$t\bar{t} + \geq 1b$ ISR	+0.03	-0.04
$t\bar{t} + \geq 1c$ modelling	+0.03	-0.04
$t\bar{t} + \text{light}$ modelling	+0.03	-0.03
tW modelling	+0.08	-0.07
Background-model statistical uncertainty	+0.04	-0.05
b -tagging efficiency and mis-tag rates		
b -tagging efficiency	+0.03	-0.02
c -mis-tag rates	+0.03	-0.03
l -mis-tag rates	+0.02	-0.02
Jet energy scale and resolution		
b -jet energy scale	+0.00	-0.01
Jet energy scale (flavour)	+0.01	-0.01
Jet energy scale (pile-up)	+0.00	-0.01
Jet energy scale (remaining)	+0.01	-0.01
Jet energy resolution	+0.02	-0.02
Luminosity	+0.01	-0.00
Other sources	+0.03	-0.03
Total systematic uncertainty	+0.30	-0.28
$t\bar{t} + \geq 1b$ normalisation	+0.04	-0.07
Total statistical uncertainty	+0.20	-0.20
Total uncertainty	+0.36	-0.34

- Uncertainty in $t\bar{t} + \geq 1b$ modeling:
 - NLO matching, b-fractions, FSR, PS & Hadronisation, etc.
- ttbb process is theoretically challenging for correct modeling
 - Traditionally in 5FS, recently moving towards 4FS
 - Significant differences among existing theory predictions
- ATLAS+CMS joint efforts in LHC Higgs WG
 - Adopt common ttbb treatment
 - In view of a full Run 2 ttH($H \rightarrow bb$) combination

Tools for Higgs Analysis

ggF

iHixs	(N3LO QCD+NLO EW)
HIGLU	(NNLO QCD+NLO EW)
FeHiPro	(NNLO QCD+NLO EW)
HNNLO, HRes	(NNLO+NNLL QCD)
RGHiggs	(NNLO+NNNLL QCD)
SusHi, aMC SusHi	(N3LO/NLO QCD)
ggHiggs	(N3LO QCD)
TROLL	(N3LL' QCD)

VBF

VV2H	(NLO QCD)
VBFNLO	(NLO QCD)
HAWK	(NLO QCD+EW)
VBF@NNLO	(NNLO QCD)
HJets	(NLO QCD)
proVBFH	(NNLO QCD)

WH/ZH

V2HV	(NLO QCD)
HAWK	(NLO QCD+EW)
VH@NNLO	(NNLO)

ttH

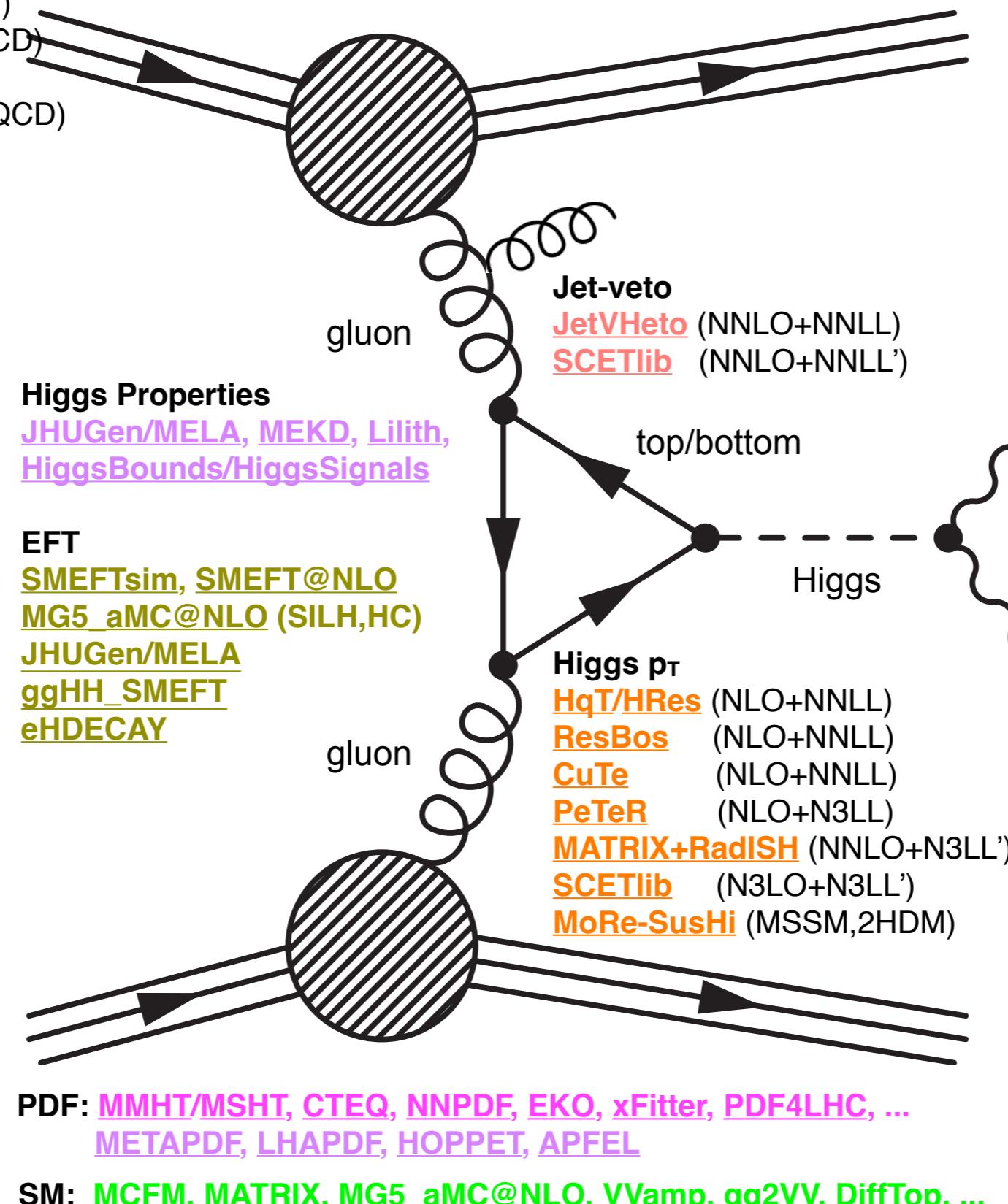
HQQ	(LO QCD)
POWHEL	(NLO QCD)

bbH

bbh@NNLO	(NNLO QCD)
bbhFONLL	(NLO+NNLL QCD)
bbX	(NLO+NNLL QCD)

HH

HPAIR	(NLO QCD)
ggHH	(NLO QCD)
proVBFHH	(NNLO QCD)



NNLO+PS MC
[NNLOPS \(MiNLO'+reweighting\)](#)
[MiNNLO](#)
[GenEvA](#)

NLO+PS MC (Multi-purpose)
[POWHEG-BOX](#)
[MadGraph5_aMC@NLO](#)
[SHERPA MEPS@NLO](#)
[PYTHIA8 UNLOPS](#)
[HERWIG7 Matchbox](#)

NLO ME/Automated NLO
[MCFM, MG5_aMC@NLO,](#)
[Recola, GoSam, HELAC,](#)
[OpenLoops, BlackHat, etc.](#)

W/Z

Higgs Decay
[HDECAY](#) (NLO++)
[Prophecy4f](#) (NLO QCD+EW)
[Hto4I](#) (NLO QCD+EW)

W/Z

MSSM/2HDM
[FeynHiggs, CPSuperH](#)
[SusHi+2HDMC](#)
[HIGLU+HDECAY](#)
[2HDECAY](#)

NMSSM
[NMSSMCALC](#) (EW),
[NMSSMTools, FlexibleSUSY,](#)
[SOFTSUSY, SPheno](#)

+ many codes for BSM physics

Summary and Prospects

- ➊ The LHC Higgs Cross Section Working Group brought together the TH and EXP communities working on the Higgs physics.
 - ➊ Enabled the success for fruitful collaboration between EXP and TH.
 - ➋ The LHC Higgs Cross Section Working Group provided the state-of-the-art Higgs XS&BR since the beginning.
 - ➌ Enabled early determination of the nature of “Higgs-like” particle.
 - ➍ Attempts were made for proper theory paper citation as it is fundamental (managed by ATLAS&CMS).

The LHC Higgs Combination Group
(ATLAS+CMS)

“Procedure for the LHC Higgs boson search combination in Summer 2011”

[ATL-PHYS-PUB-2011-11, CMS NOTE-2011/005](#)

Acknowledgements

We would like to thank the ATLAS statistics forum and CMS statistics committee for their extremely valuable and continuous feedback and for the guiding suggestions and corrections. We would like to acknowledge the role of the LHC Higgs Cross Section group that helped settle a number of non-trivial questions on correlations of theoretical errors for exclusive final states of Higgs boson production in association with jets. The prompt response of the group on the request to produce SM Higgs boson production cross sections and branching ratios for the fine grid of Higgs boson mass points needed for the combination was simply spectacular. We would also like to thank the ATLAS and CMS Higgs working groups for their close involvement in the overall effort and for preparing analysis Workspaces for performing technical exercises as reported in this document.

- ➊ Collaboration between EXP and TH is even more necessary now to find any hints for BSM physics.
 - ➊ Restarting the construction of a common language, silence of nature is only a pause.

