

Modelling the Gamma-ray Morphology of the Supernova Remnant W28

A 3D Approach

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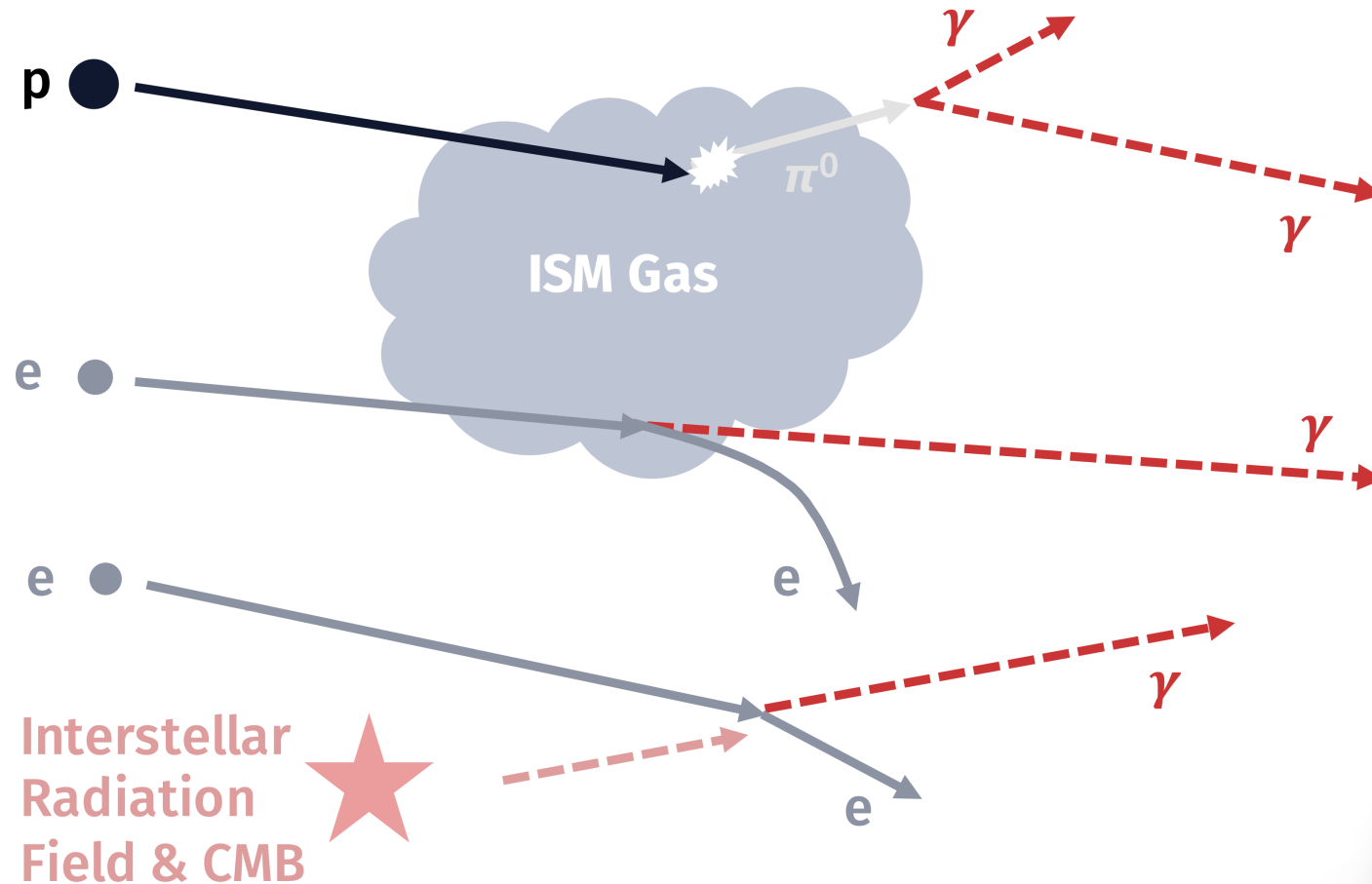


AIP 2022, Adelaide
Decembers 15th, 2022



GROUP FOR
ASTROPARTICLE
PHYSICS

Gamma-Ray Production

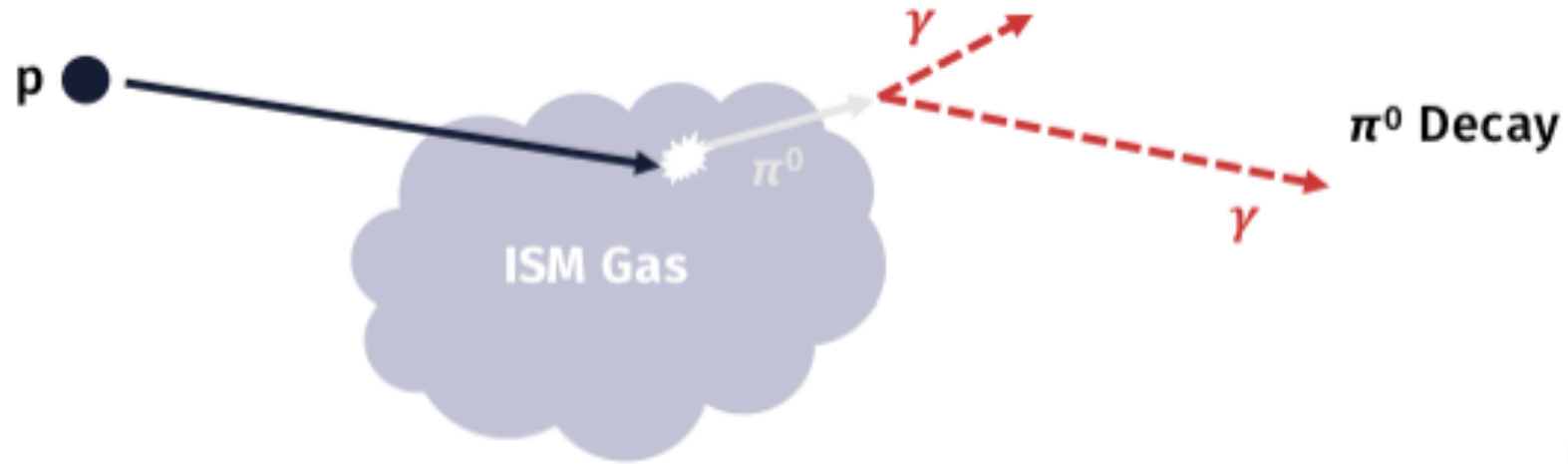


π^0 Decay

Bremsstrahlung

Inverse Compton

Modelling: Gamma-Ray Distribution



Total Number Density
(ISM)

Volume of ISM

Photons per collision

$$\Phi_{\gamma} = \frac{c n_{\text{H}} V}{4\pi D^2} \int_{E_{\gamma}}^{\infty} \sigma_{\text{pp}}(E_{\text{p}}) J_{\text{p}}(E_{\text{p}}, R, t) F_{\gamma}(E_{\text{p}}, E_{\gamma}) \frac{dE_{\text{p}}}{E_{\text{p}}}$$

Distance:
Earth - Accelerator

Cosmic-Ray Proton
Volume Distribution

Kelner et al. (2006)

Modelling: Cosmic-Ray Proton Distribution

Escaped Cosmic Rays ($E_p > E_{p,esc}$)

Steady-state solution to transport equation

$$J_p = N_0 E_p^{-\alpha} \frac{f_0}{\pi^{3/2} R_{dif}^3} \exp\left(-\frac{(R - R_{esc})^2}{R_{dif}^2}\right)$$

adapted from *Aharonian & Atoyan (1996)* to include escape at time

$$t_{esc} = t_{Sedov} \left(\frac{E_p}{E_{p,max}}\right)^{-1/\delta_p} \quad \text{Gabici et al. (2009)}$$

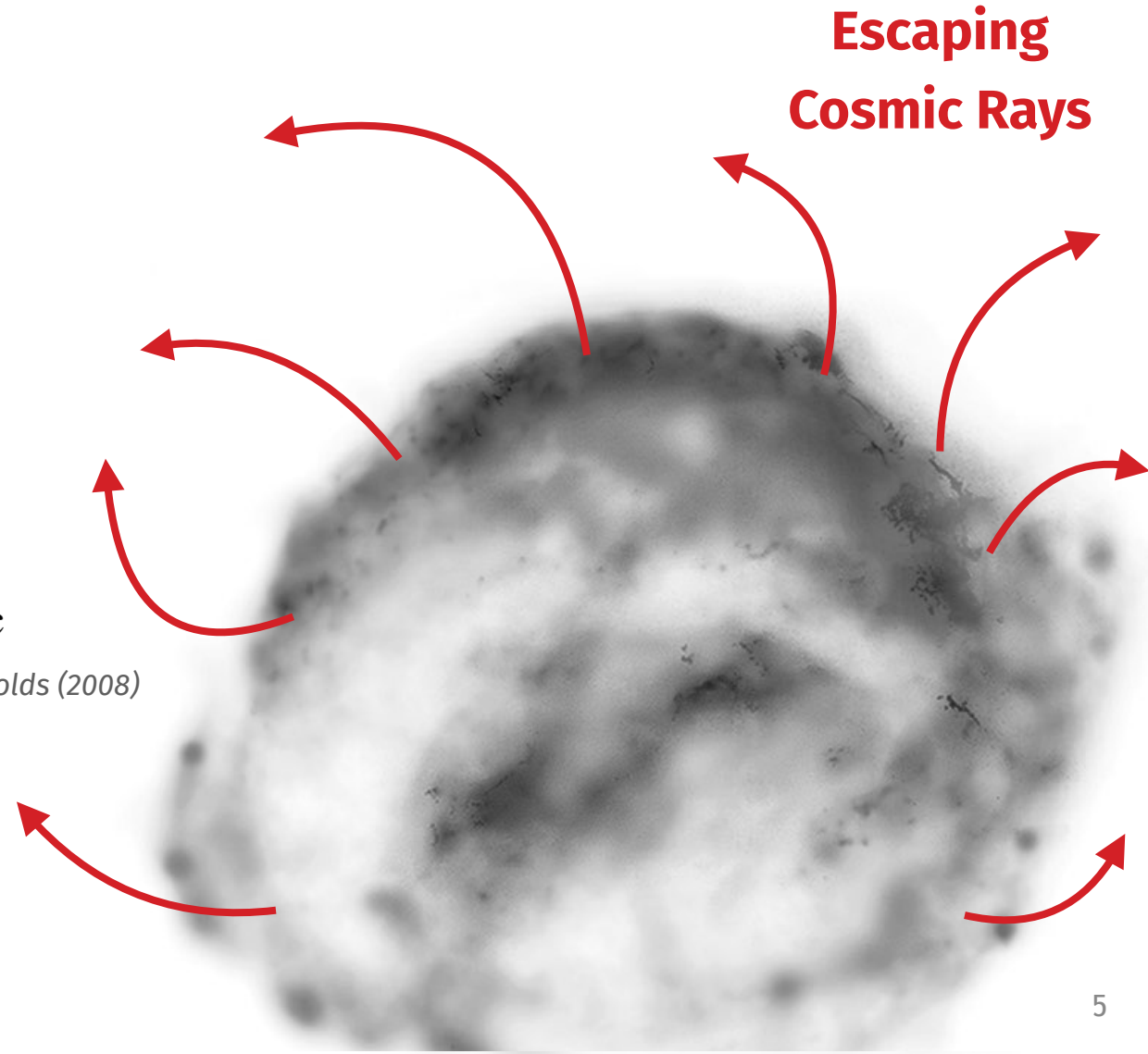
and at distance

$$R_{esc} = 0.31 \left(\frac{E_{SN}}{10^{51} \text{ erg}}\right)^{1/5} \left(\frac{n_0}{\text{cm}^{-3}}\right)^{-1/5} \left(\frac{t_{esc}}{\text{yr}}\right)^{2/5} \text{ pc} \quad \text{Reynolds (2008)}$$

with diffusion length

$$R_{dif} = \sqrt{4D(t - t_{esc})}$$

**Escaping
Cosmic Rays**



Modelling: Cosmic-Ray Proton Distribution

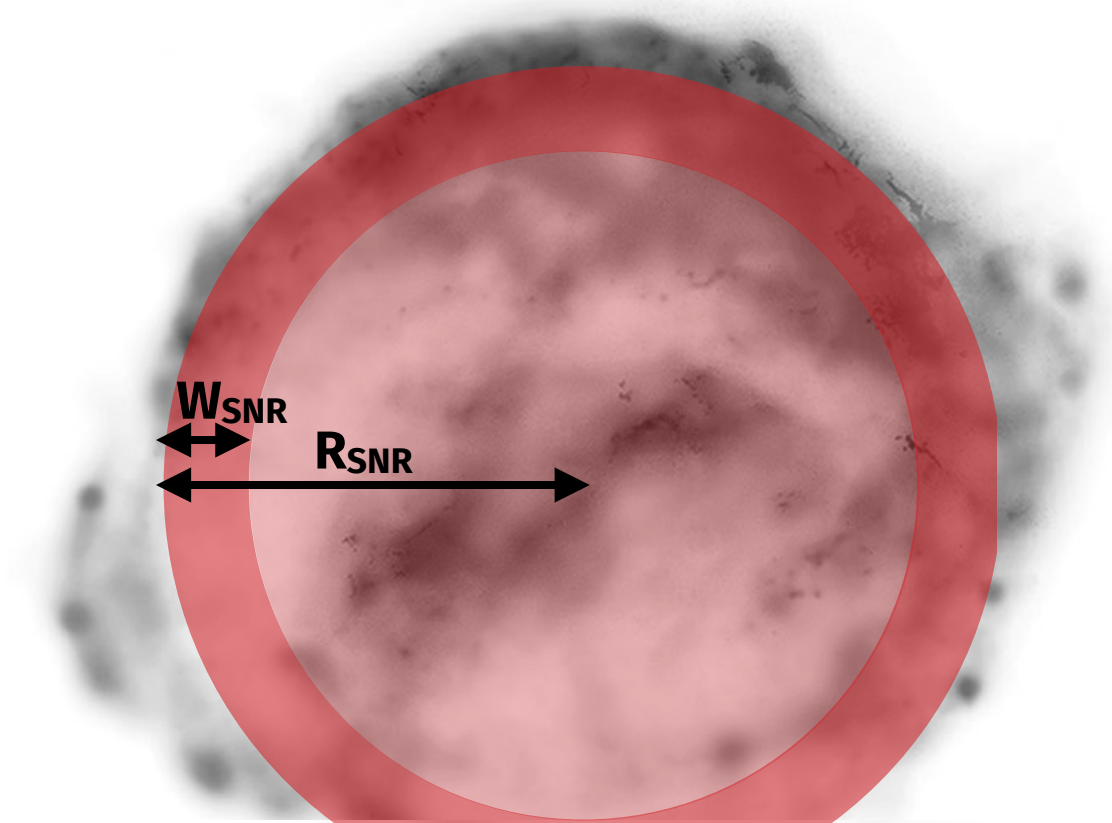
Confined Cosmic Rays ($E_p < E_{p,esc}$)

Fraction f of confined particles uniformly distributed in shell of width W_{SNR}

$$J_p = f \cdot N_0 E_p^{-\alpha} \left(\frac{4}{3} \pi R_{SNR}^3 - (R_{SNR} - W_{SNR})^3 \right)^{-1}$$

Remaining particles uniformly distributed in inner sphere

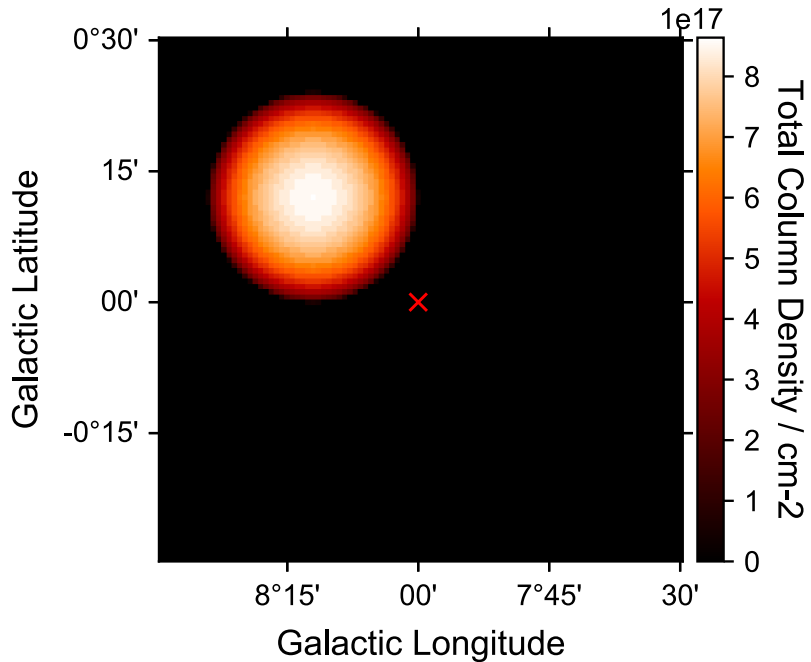
$$J_p = (1 - f) \cdot N_0 E_p^{-\alpha} \left(\frac{4}{3} \pi (R_{SNR} - W_{SNR})^3 \right)^{-1}$$



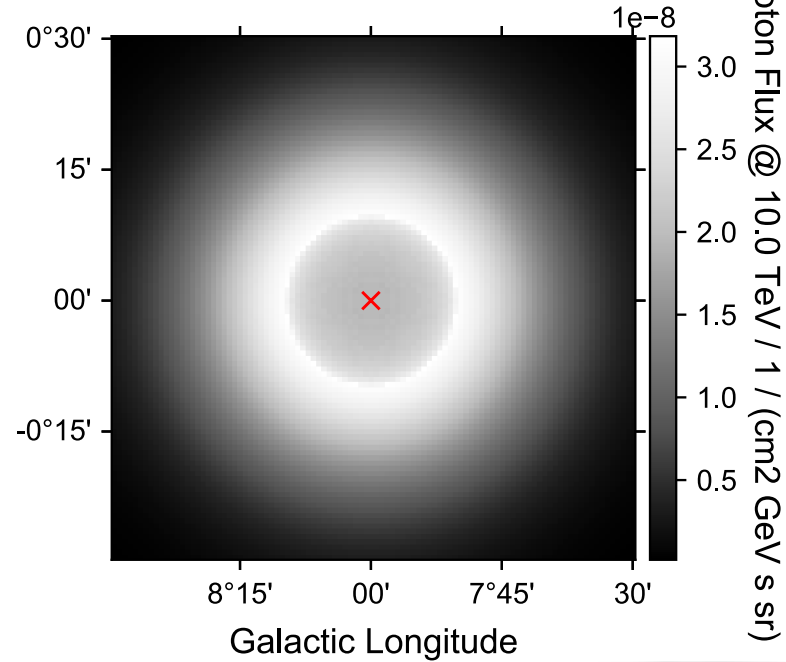
Modelling: Morphology

Modelling of cosmic-ray protons and gamma rays for a **3D** spatial grid, determined by resolution of interstellar gas measurements

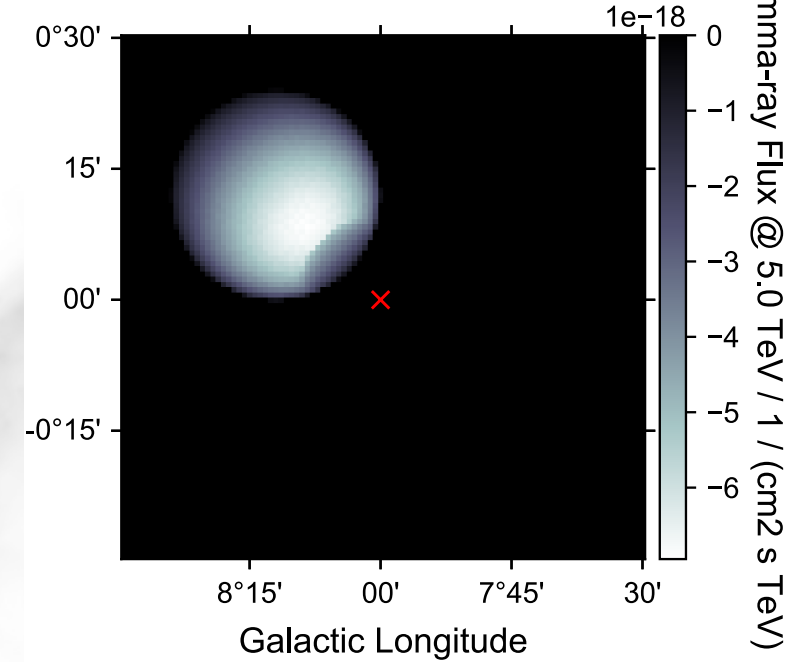
Interstellar Gas



Proton Flux @ 30 TeV



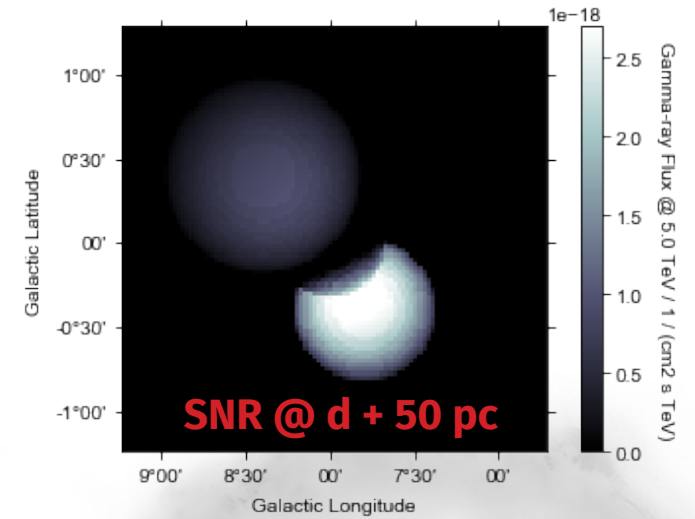
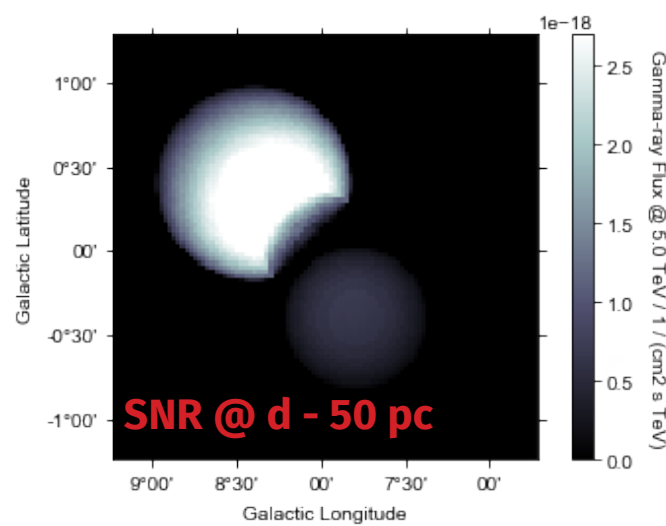
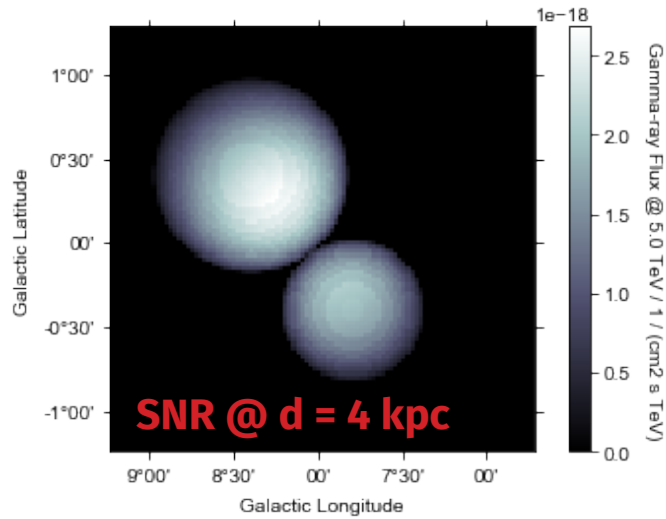
Gamma Flux @ 5 TeV



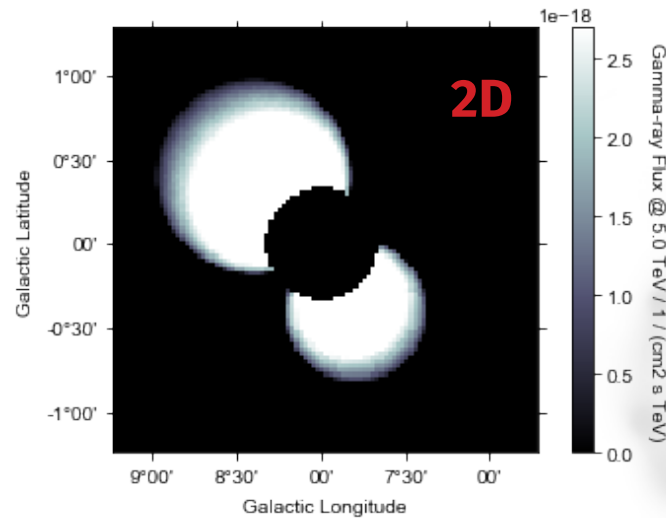
(Note: All distributions here integrated over z-axis for illustration.)

Gamma-Ray Morphology: Importance of 3D

3D



Example:
Gas clouds with
different distances
to Earth

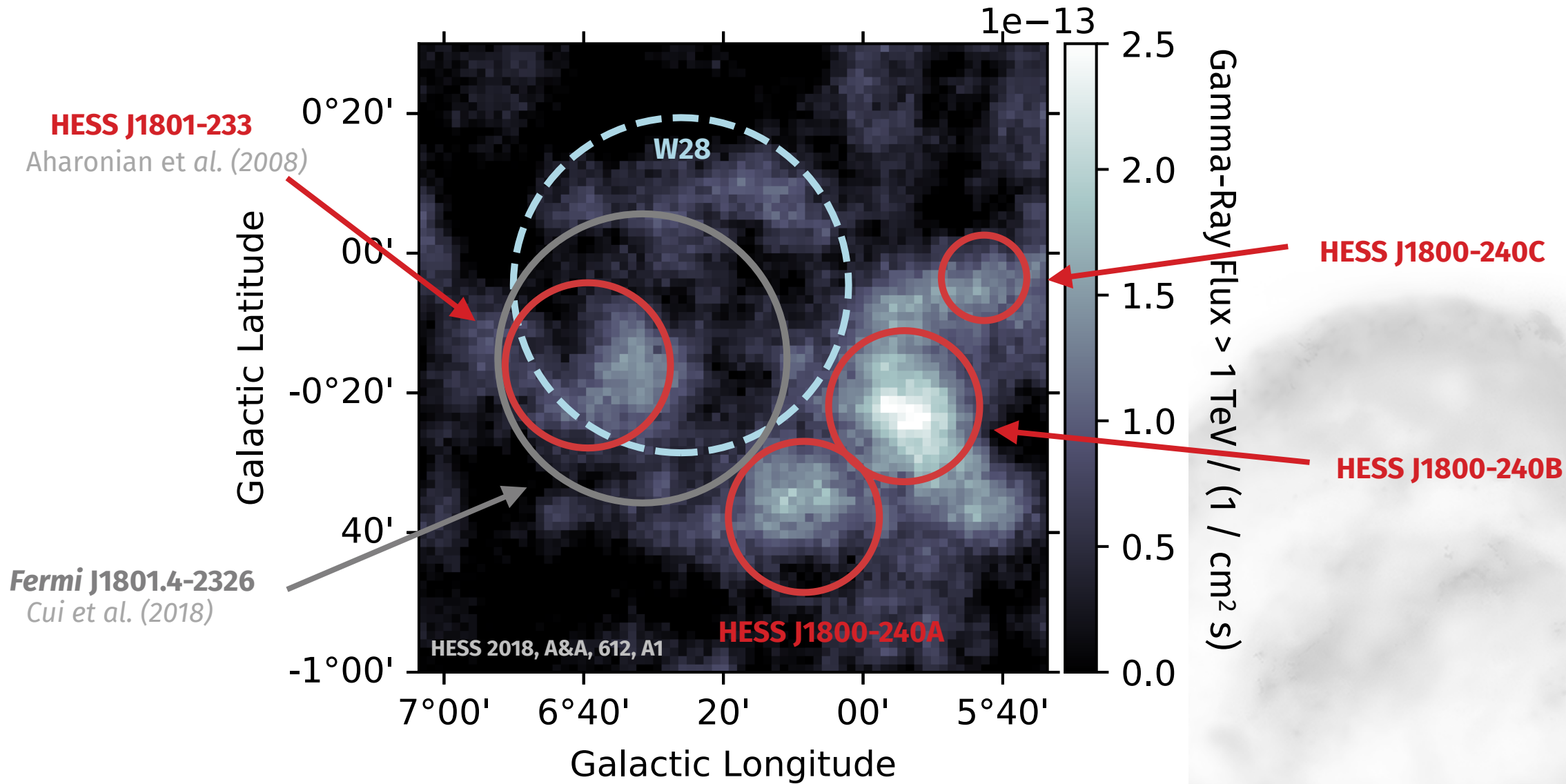


- Python framework for modelling **part**icles (protons, gamma rays and neutrinos) in the **ISM**
- Modular and user-friendly structure
- Hosted on GitHub
(to be released together with publication)
- Novel modelling of morphology
- Novel modelling in 3D
- Notebooks available with examples and reproduction of plots from
 - *Aharonian and Atoyan (1996) A&A 309*
 - *Kelner et al. (2006) Phys Rev D 79*
 - *Mitchell, Einecke et al. (2021) MNRAS 503*
 - *Feijen, Einecke et al. (2022) MNRAS 511*

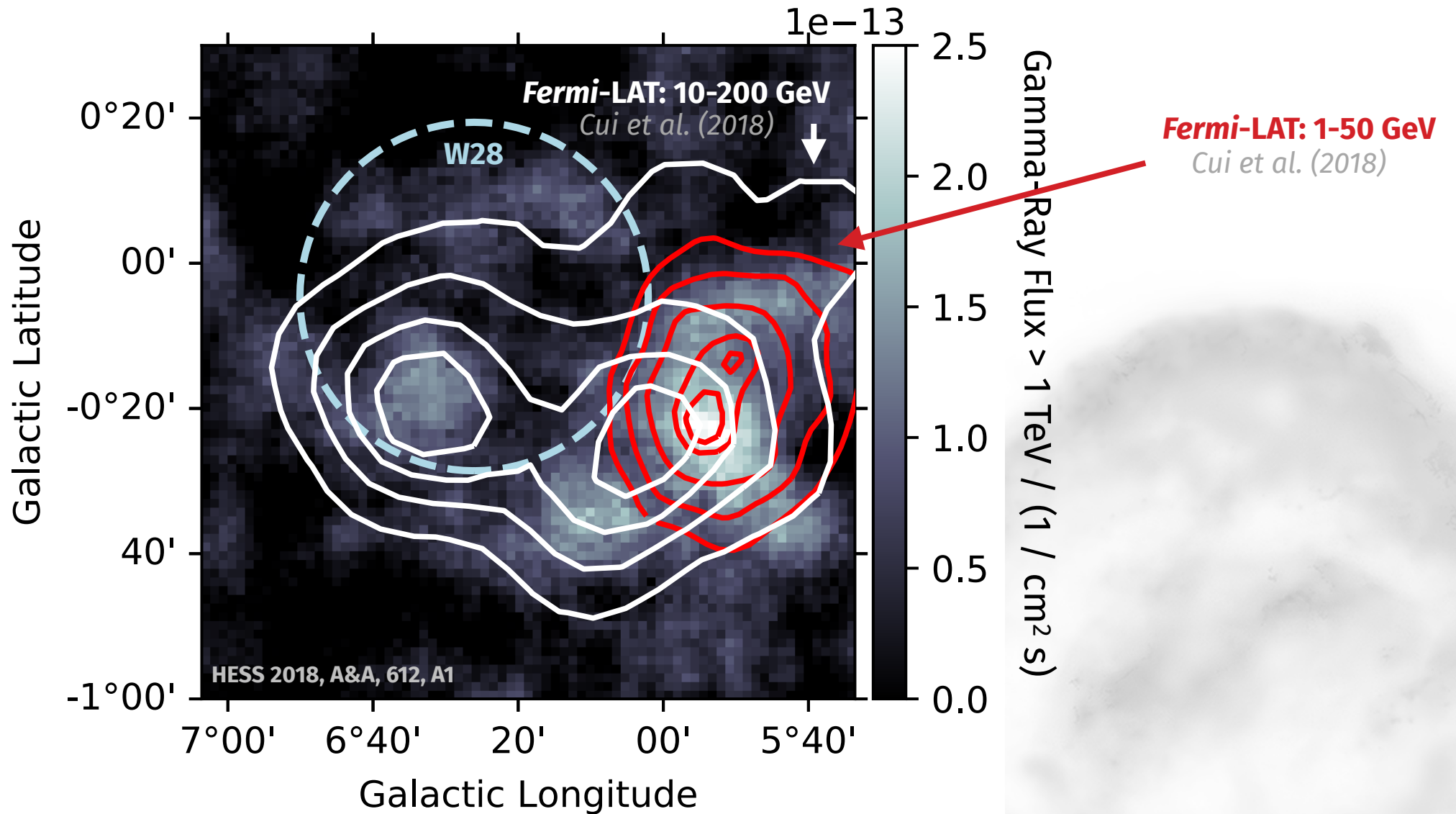


Thursday 3pm: Ryan Burley, *Gamma-ray and Neutrino Emission from SNRs and Molecular Clouds*

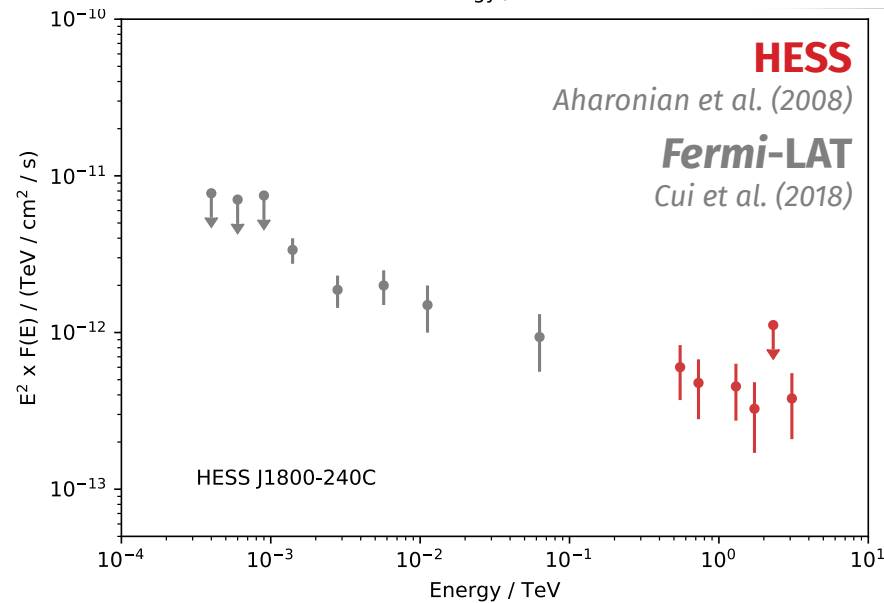
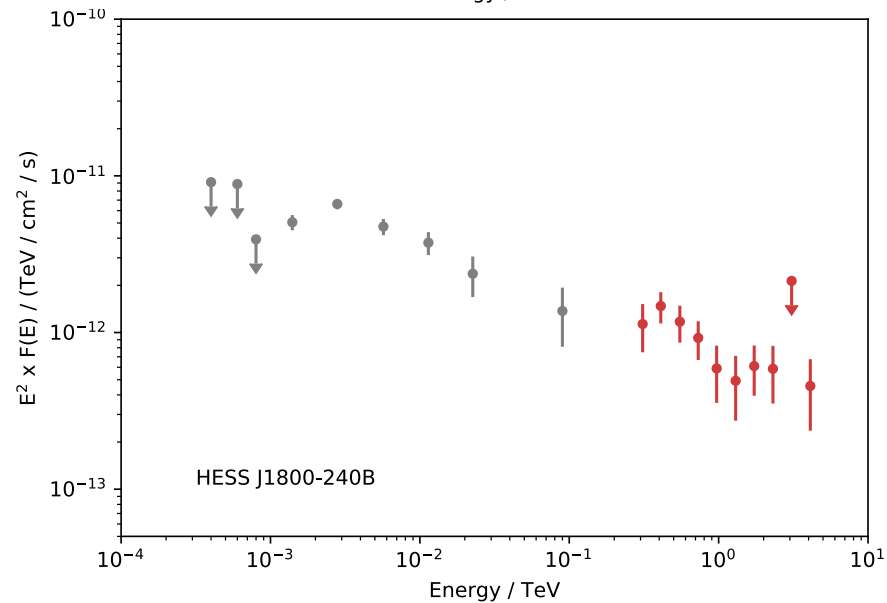
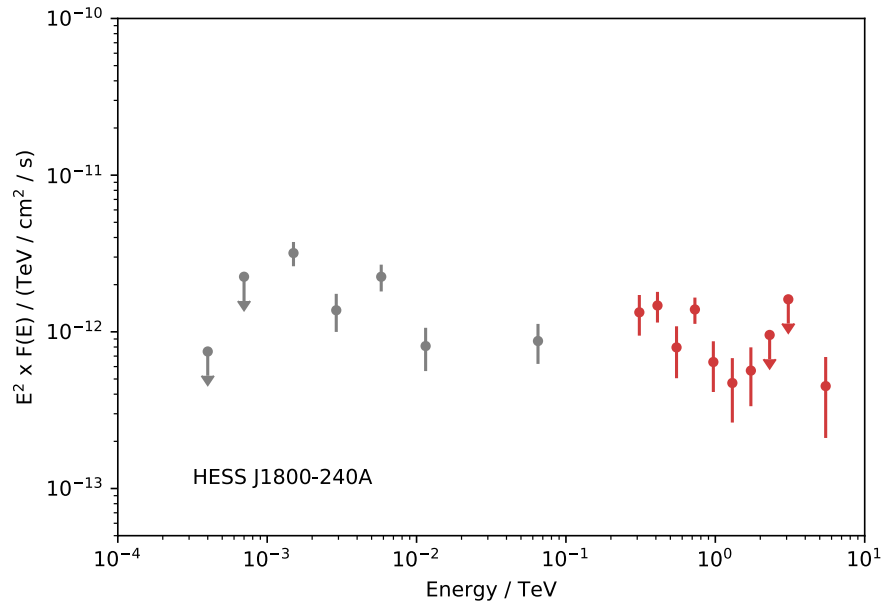
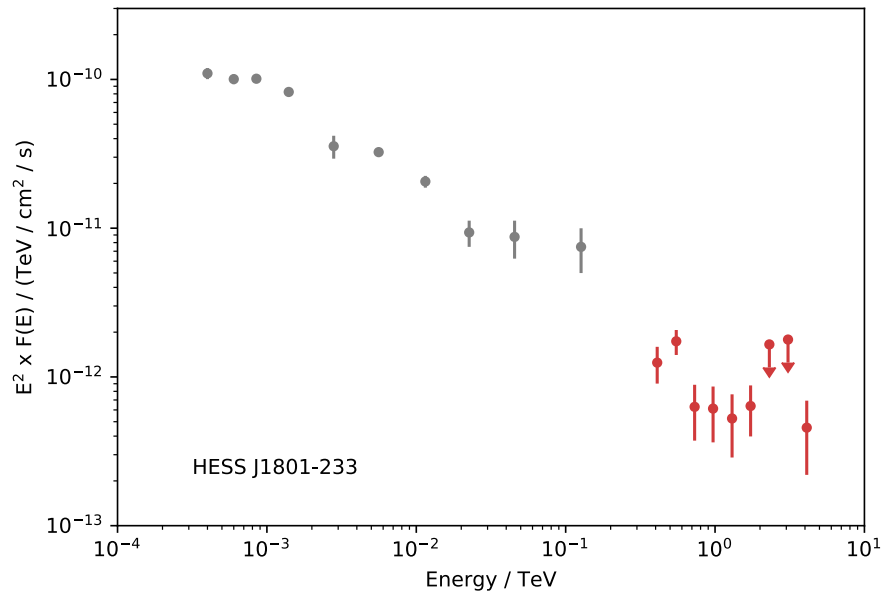
Measurement: Gamma-ray Distribution towards W28



Measurement: Gamma-ray Distribution towards W28



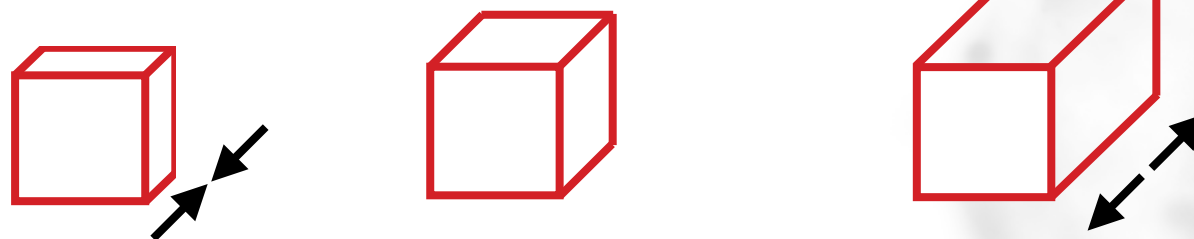
Measurement: Gamma-ray Distribution towards W28



Measurement: Gas Distribution

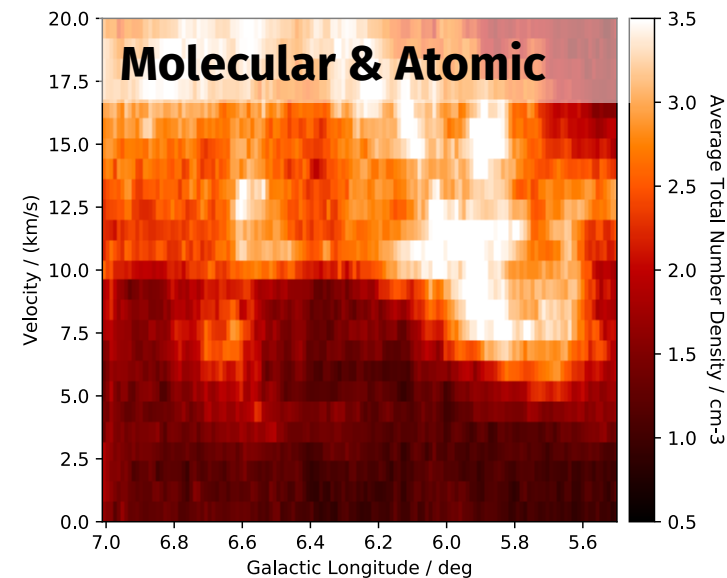
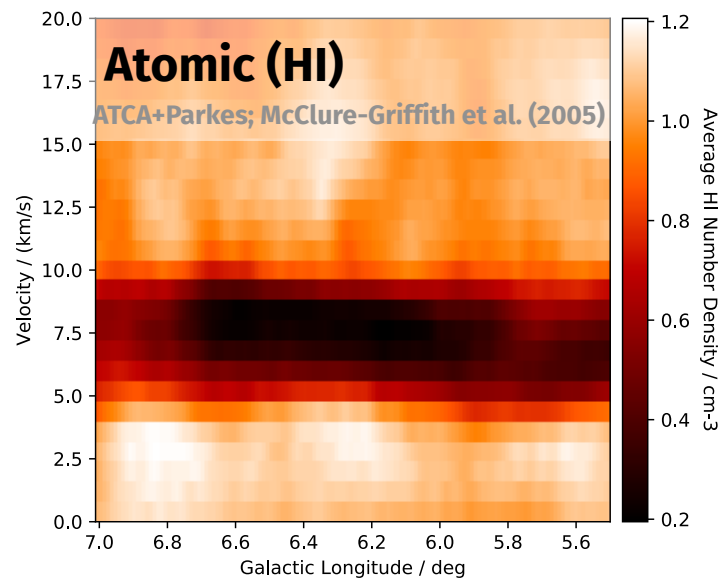
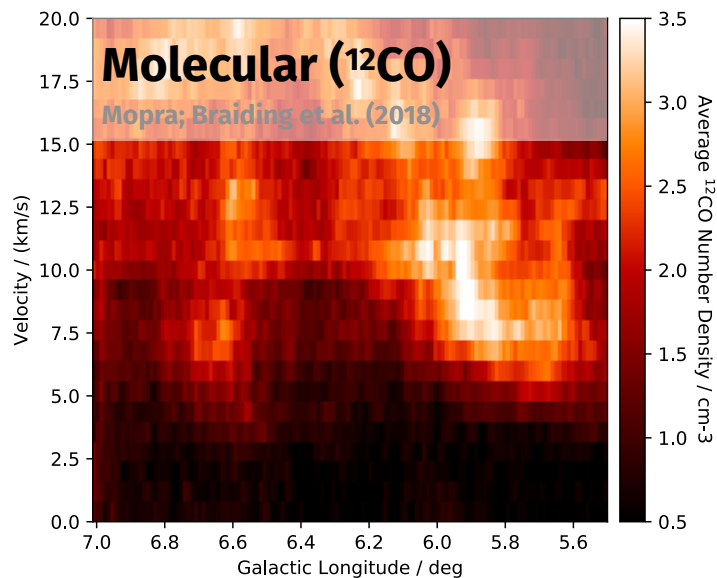
Challenges

- Measurement of line-of-sight Doppler velocities instead of physical distance
- Model of Galaxy's rotation translates these velocities to distances, but ...
 - ... often it has two solutions ('near' and 'far' distance)
 - ... it does not consider local velocities of the gas
 - ... it has rather large uncertainties (for our application)
- Iterative approach:
 - Location of centre of 3D gas distribution
 - Compress / stretch distance dimension of 3D gas distribution

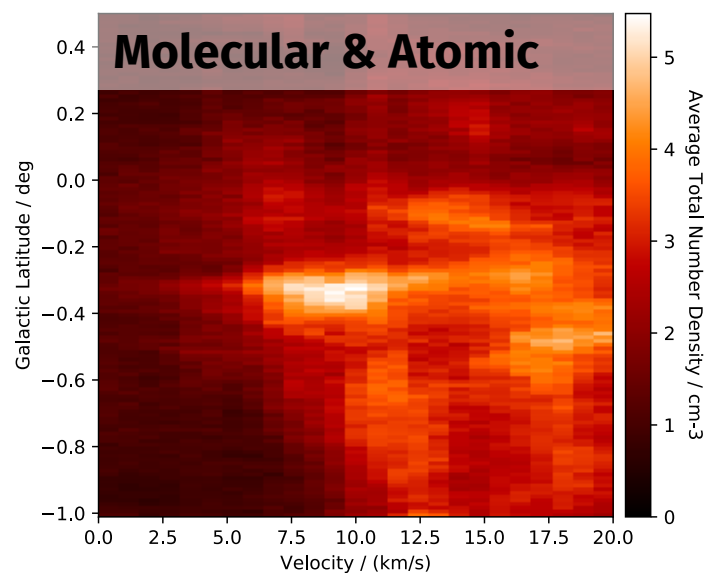
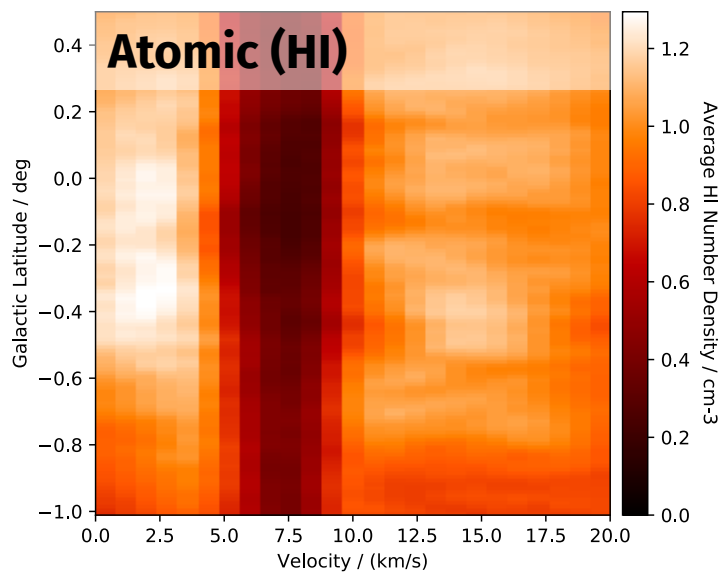
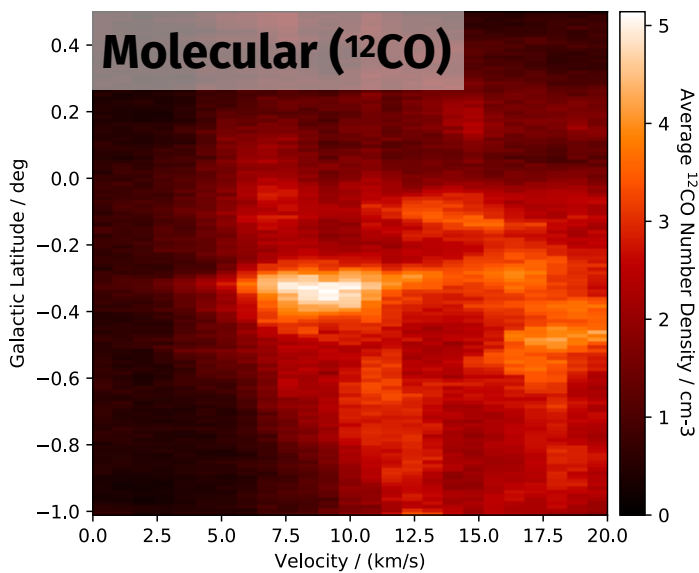


Measurement: Gas Distribution towards W28

Averaged over
Latitudes -1.0° to 0.5°

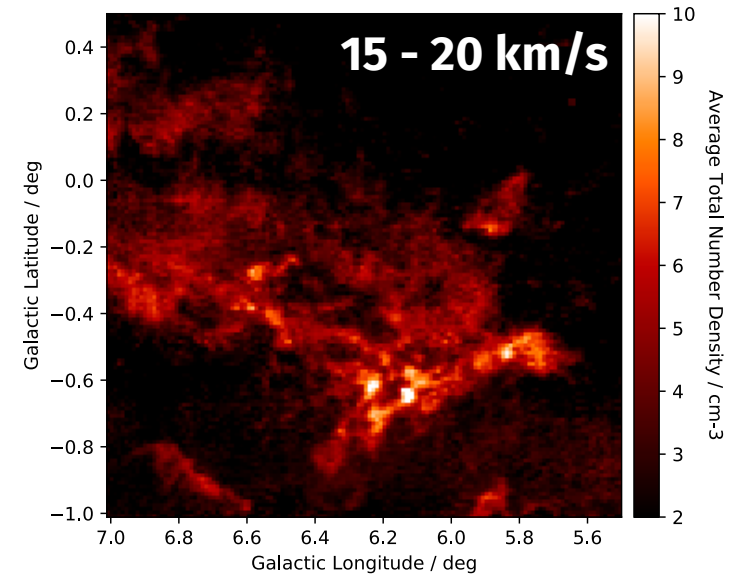
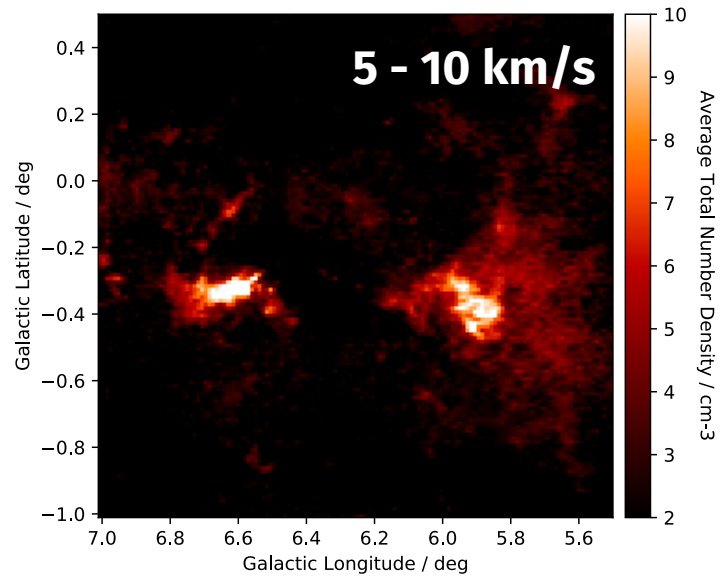
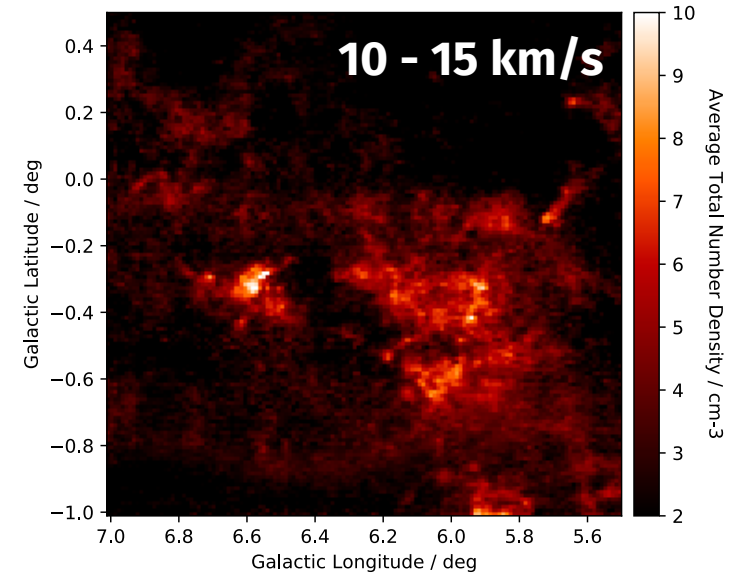
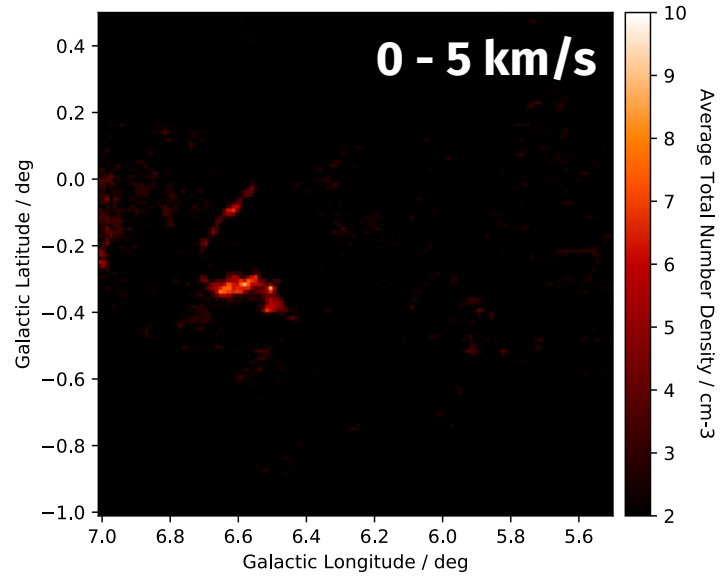


Averaged over
Longitudes 5.5° to 7.0°



Measurement: Gas Distribution towards W28

**ATOMIC & MOLECULAR
Averaged over Velocities**



Model Parameters

Grid search

- Spectral index α : 2.0, 2.2
- Diffusion suppression factor $\chi_{\text{diffusion}}$: 0.01, 0.1, 1
- Index of diffusion coefficient $\delta_{\text{diffusion}}$: 0.3, 0.5, 0.7
- Ambient magnetic field B: 10, 50, 100 μG
- Energy dependence of escape δ_p : 1.4, 2.5
- $E_{p,\text{max}}$: 1 PeV

- Total ejected kin. energy of SN E_{SN} : $1e^{51}$, $2.5e^{51}$, $5e^{51}$ erg
- η ($W_p = \eta E_{\text{SN}}$): 0.3, 0.35, 0.4, 0.45, 0.5
- Ambient hydrogen number density n_0 : 10, 20, 30 cm^{-3}
(n_0 of 10 cm^{-3} belongs to E_{SN} of $1e^{51}$ erg etc.)
- Mass of SN ejecta M_{ej} : 1, 5, 10 M_{sol}

- Velocity centre: 11, 13, 15 km/s
- Velocity range (around centre): ± 5 , ± 10 km/s

Fixed parameters:

- SNR age: 37 kyr
- SNR distance: 1.9 kpc
- $n_0 = 10 * E_{\text{SN}}$ [$1e^{51}$ erg]
- Shell width of confined particles: 3.7 pc
- Fraction of confined particles in shell: 68%

Additional constraint:

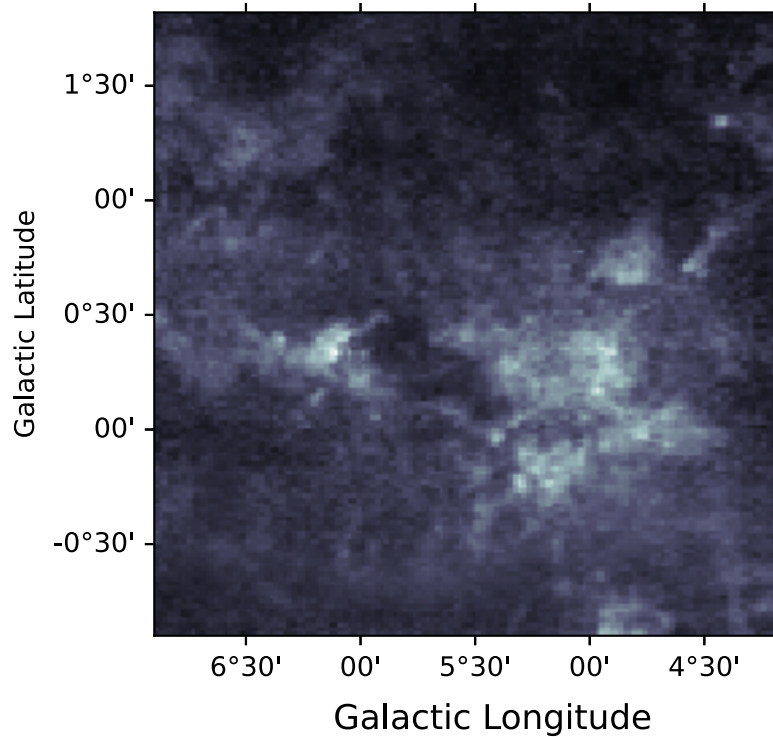
$$E_{\text{esc}} < 1 \text{ TeV}$$

(based on *Fermi*-LAT measurements,
low-energy particles must have escaped already)

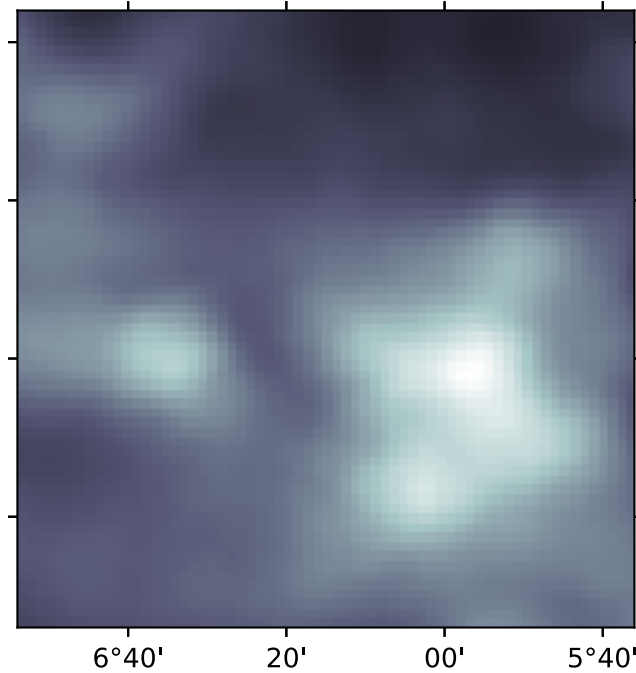
Results

PRELIMINARY

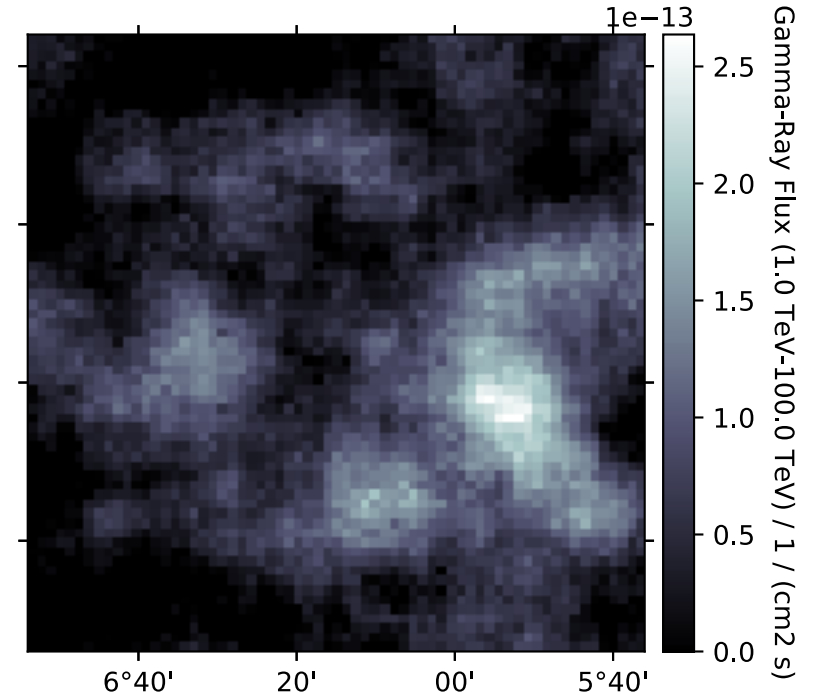
Model: > 1 TeV



**Model: > 1 TeV
(Oversampled)**



**HESS: > 1 TeV
(Oversampled)**



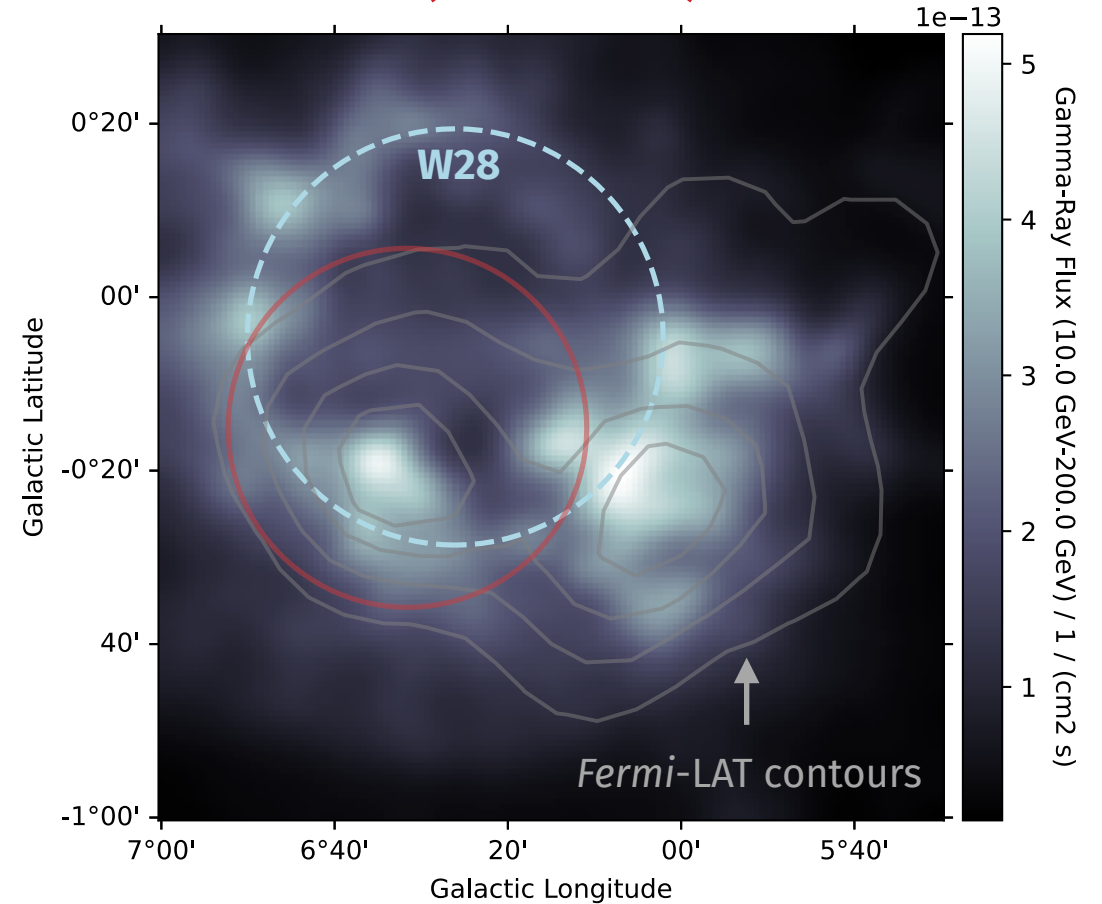
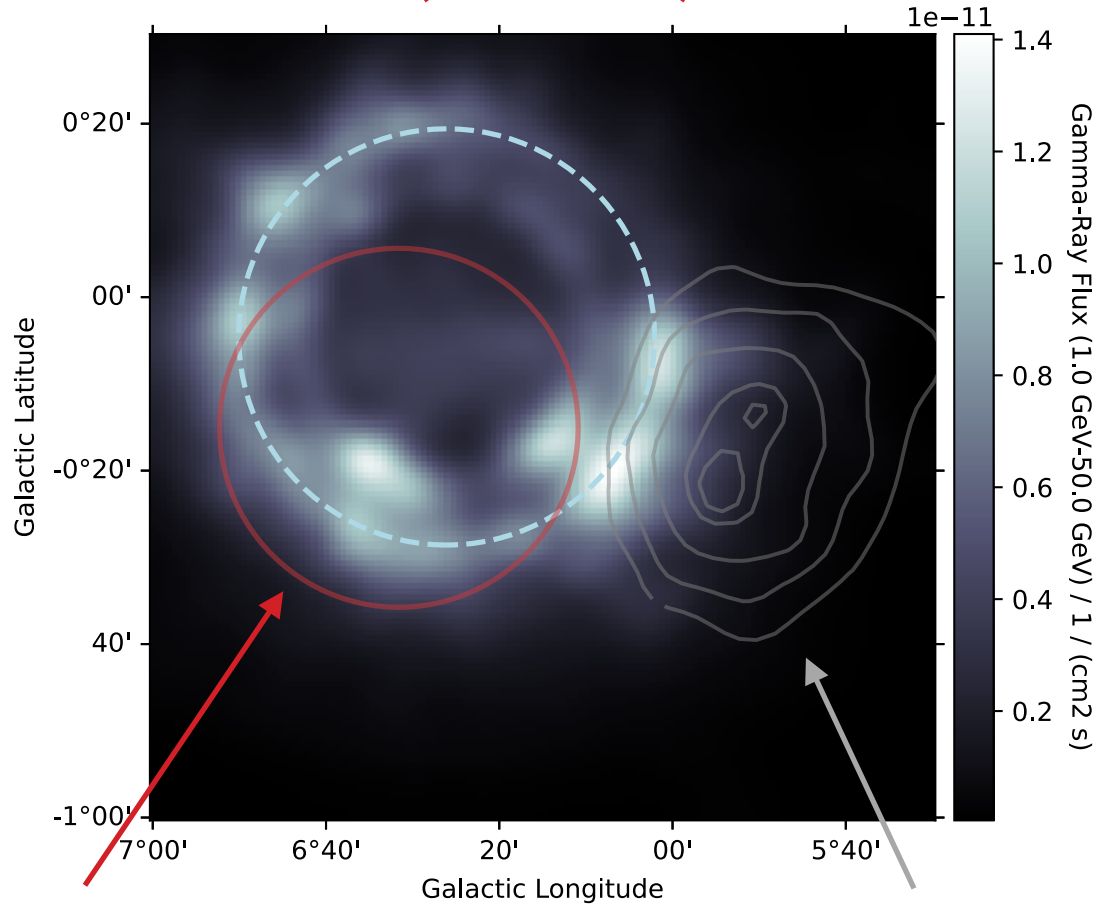
- α : 2.2, $\chi_{\text{diffusion}}$: 0.1, $\delta_{\text{diffusion}}$: 0.5, B: 100 μG , δ_p : 2.5, E_{SN} : $5e51$ erg, n_0 : 50 cm^{-3} , M_{ej} : 10 M_{sol}
- Velocity: 8 - 18 km/s

Results

PRELIMINARY

**Model: 1 - 50 GeV
(Smoothed)**

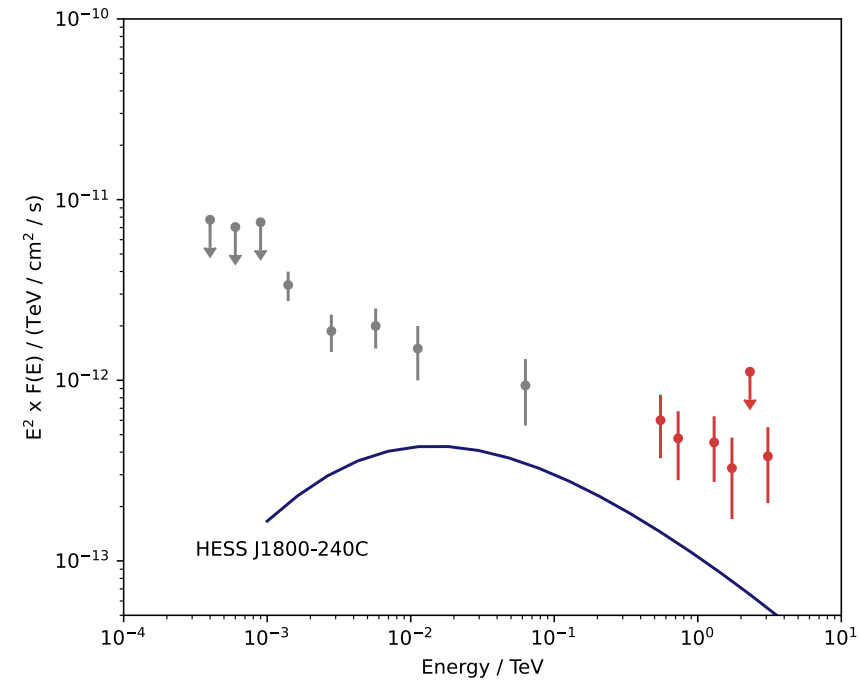
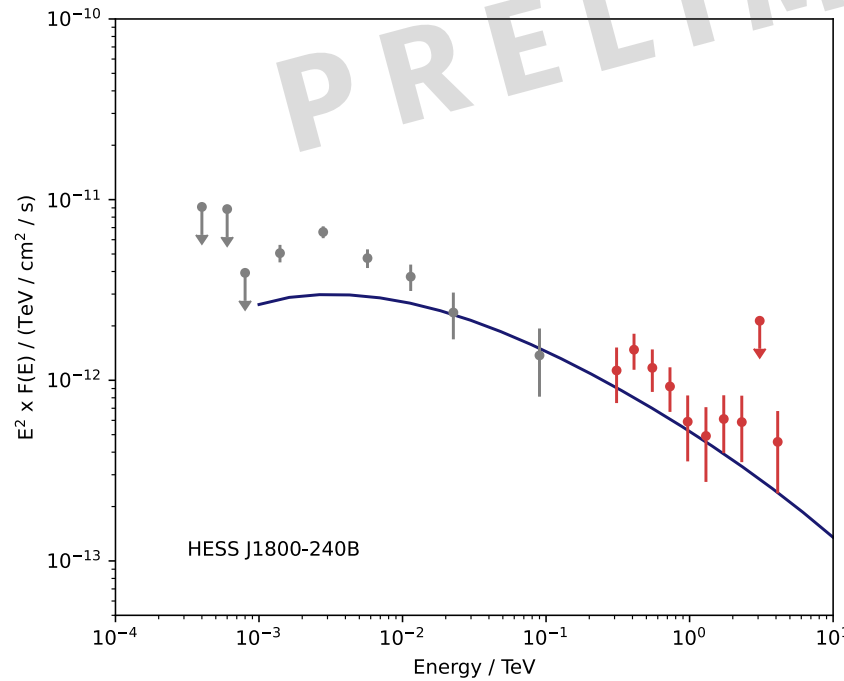
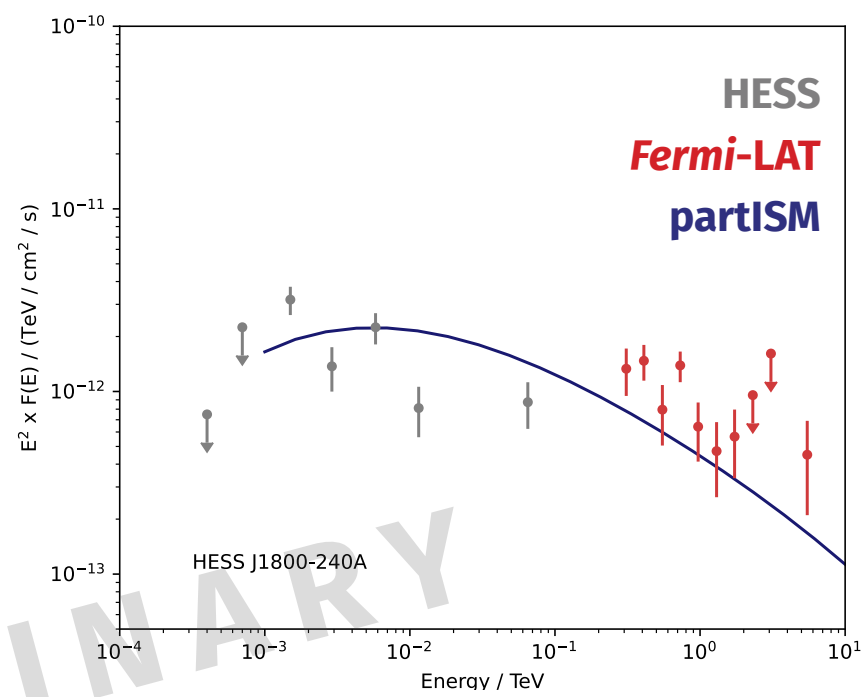
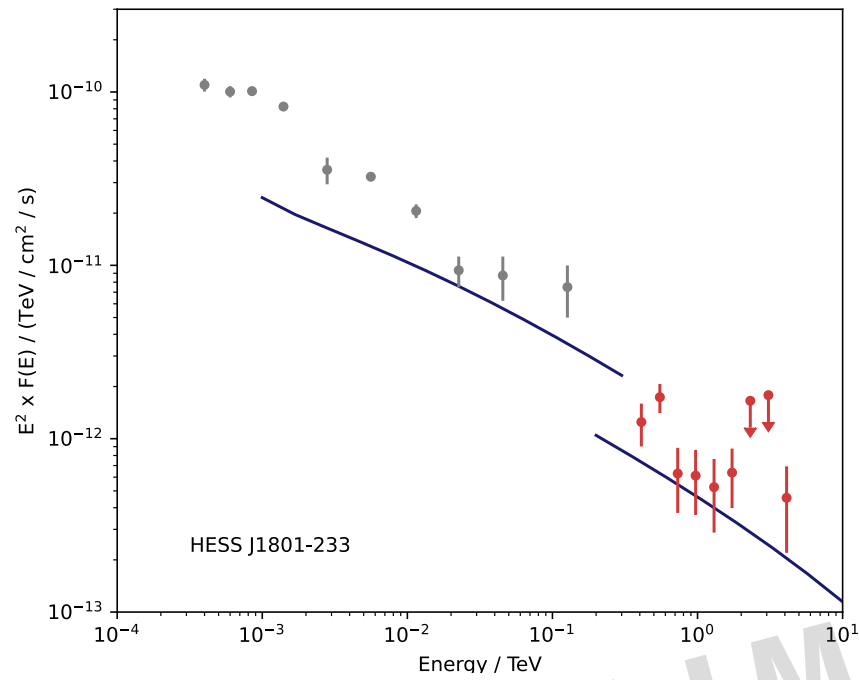
**Model: 10 - 200 GeV
(Smoothed)**



Extraction region
for *Fermi*-LAT spectrum

Fermi-LAT contours
(BUT ONLY FOR SMALL SKY REGION)

Results



PRELIMINARY

Conclusion

- To understand particle accelerators and their environments, we need to be able to reproduce their gamma-ray spectra **and** their morphologies
- New software framework to model **particles** (protons, gamma rays, neutrinos) in the **ISM**
 - 3D models: Morphologies & spectra
 - Computation time allows constraining model parameters for more computationally expensive models
- First model of morphology of SNR W28
 - Very promising results
 - New insights into SNR and its environment
- Demonstrated importance of modelling in 3D
- Modelling gamma-ray distribution and matching observations can constrain gas distribution

