

# Hyperbolic-like Encounters of Binary Black Holes with the Numerical Relativity Code SpEC

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**FCT**

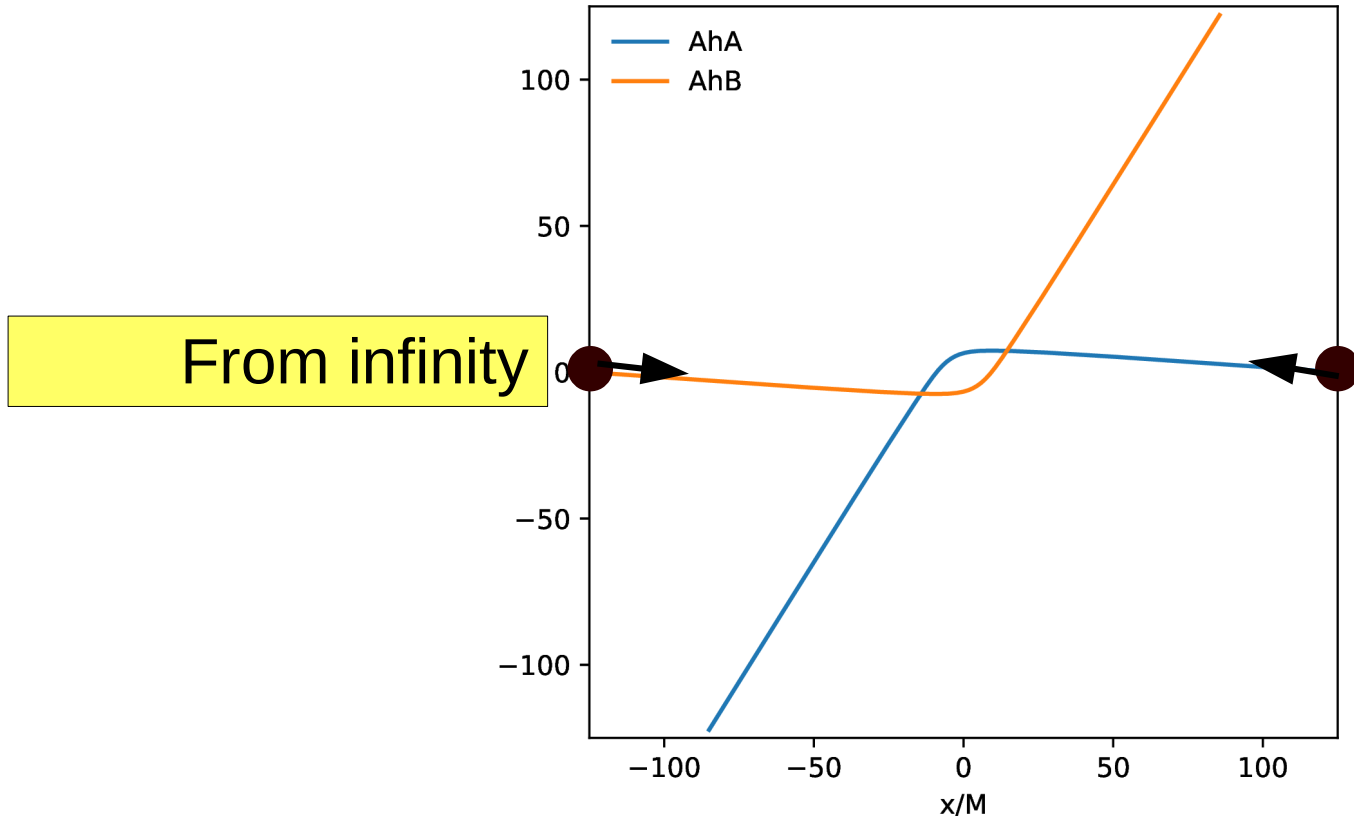
Fundação para a Ciência e a Tecnologia

MINISTÉRIO DA CIÊNCIA, TECNOLOGIA E ENSINO SUPERIOR

project number

DMINBNS - EXPL/FIS-AST/0735/2021

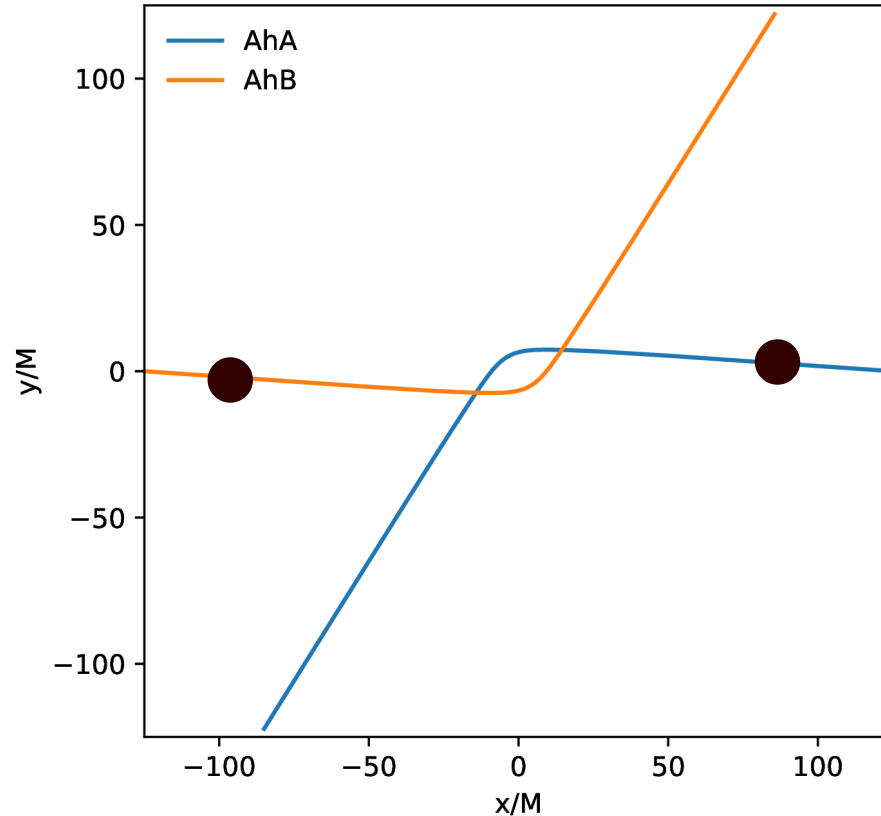
# Hyperbolic-like orbits



$$E_{\text{ADM}} = 1.02230 M$$
$$J_{\text{ADM}} = 1.78000 M^2$$

$$m_A = 0.5 M$$
$$m_B = 0.5 M$$

# Hyperbolic-like orbits

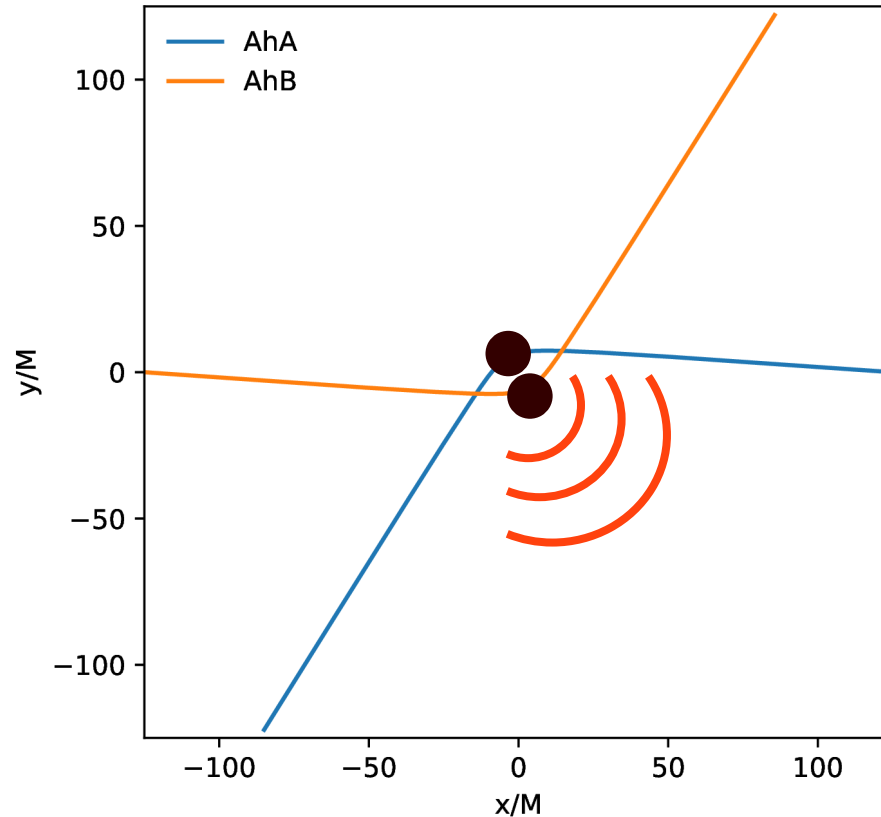


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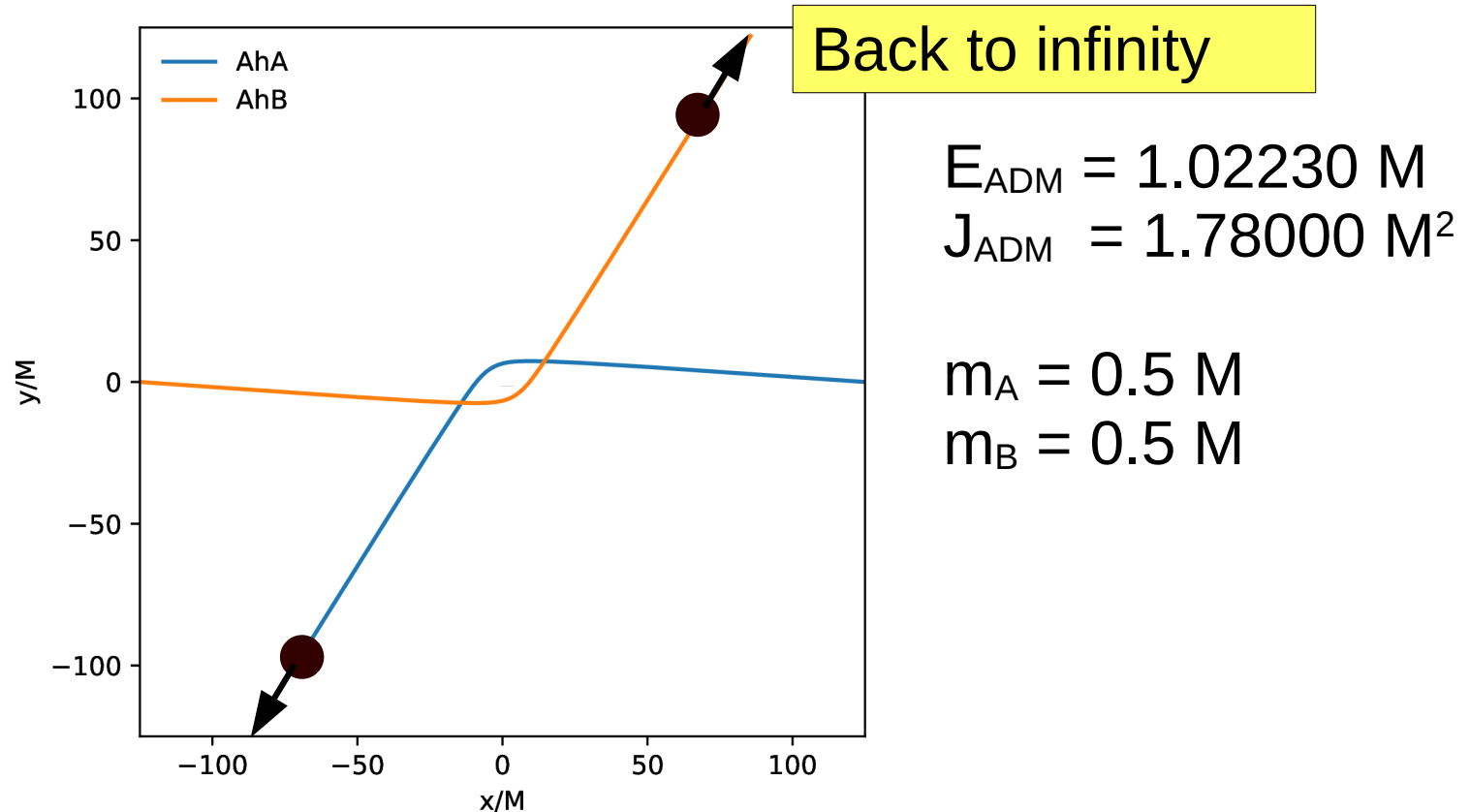


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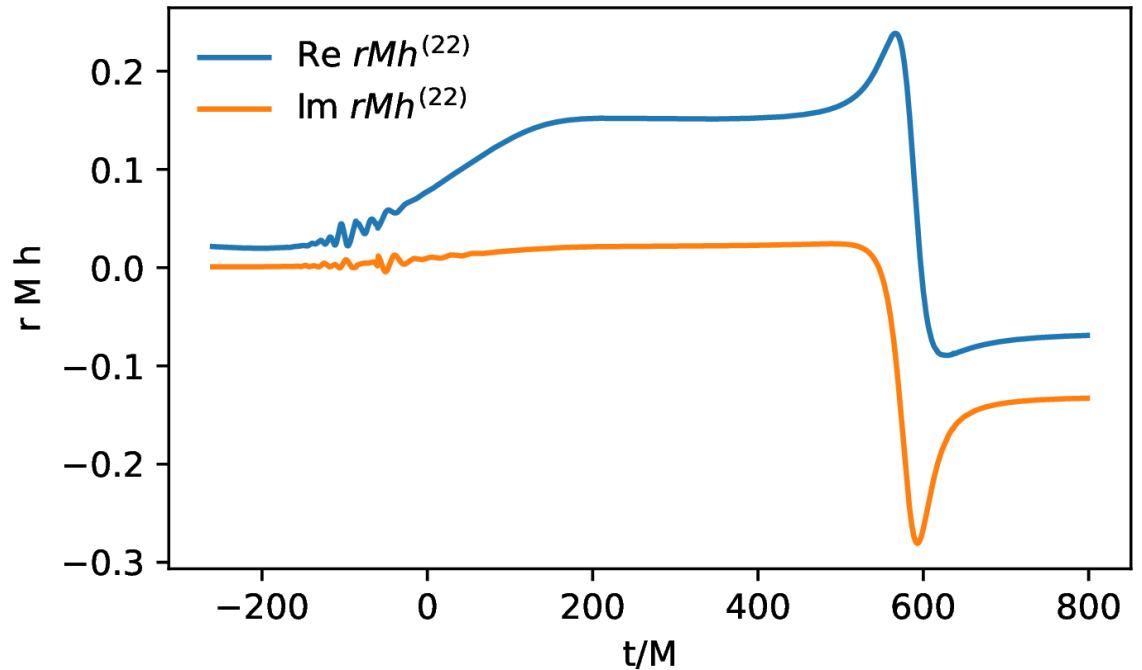
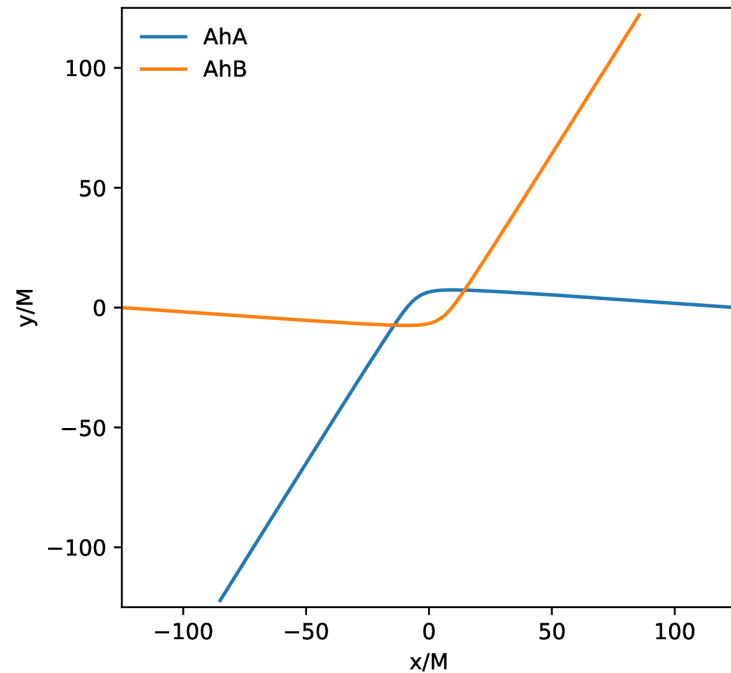
# Hyperbolic-like orbits



# Gravitational Wave Strain

$$E_{\text{ADM}} = 1.02230 M$$

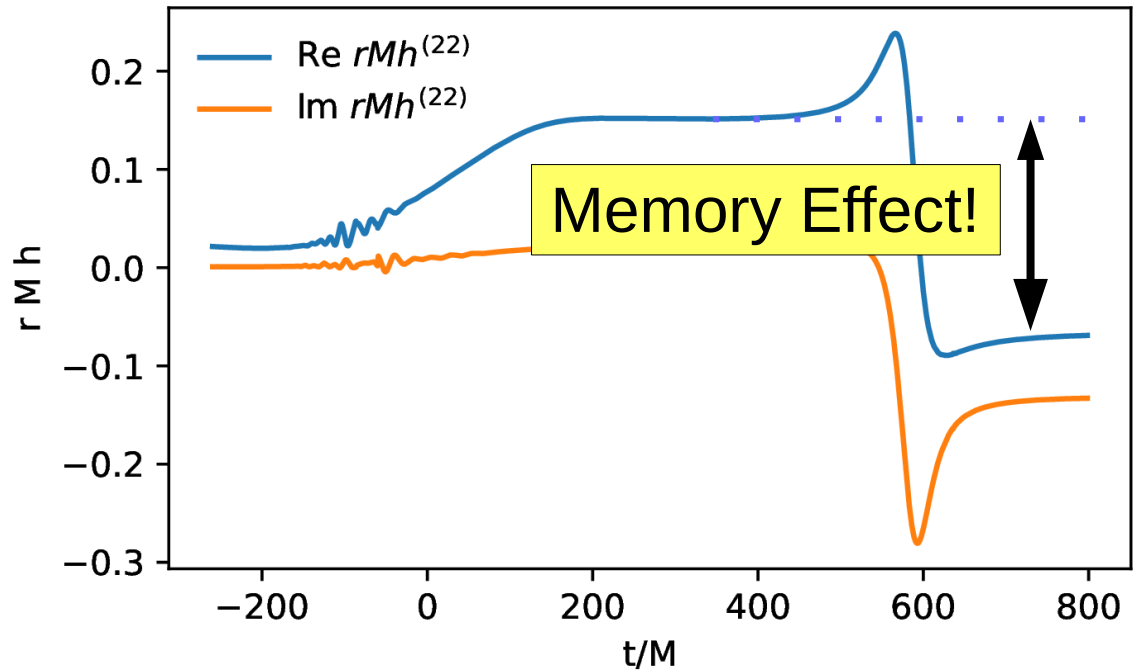
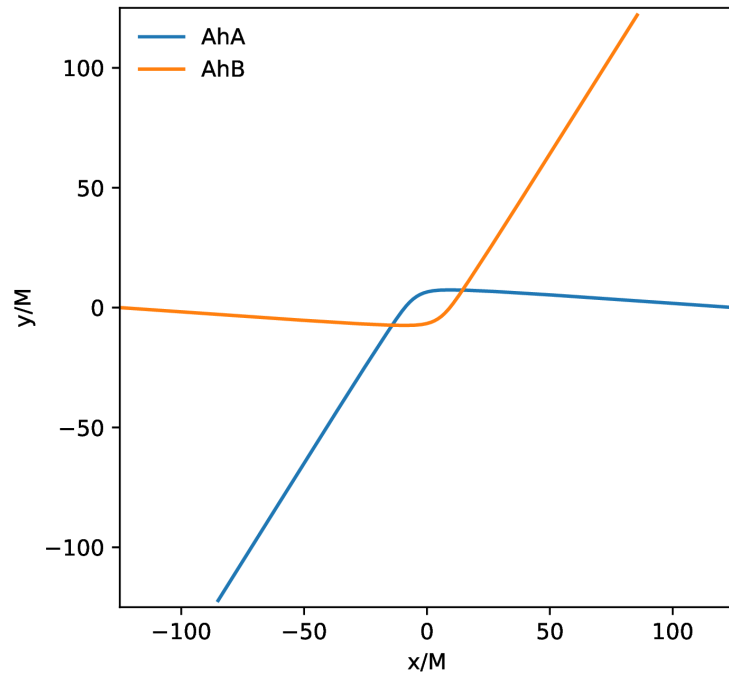
$$J_{\text{ADM}} = 1.78000 M^2$$



# Gravitational Wave Strain

$$E_{\text{ADM}} = 1.02230 M$$

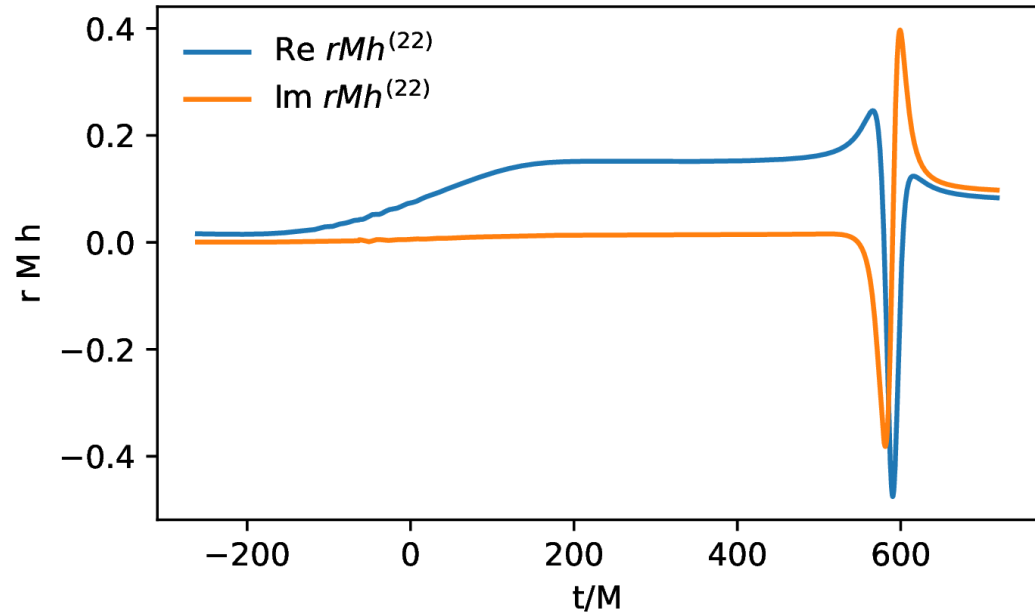
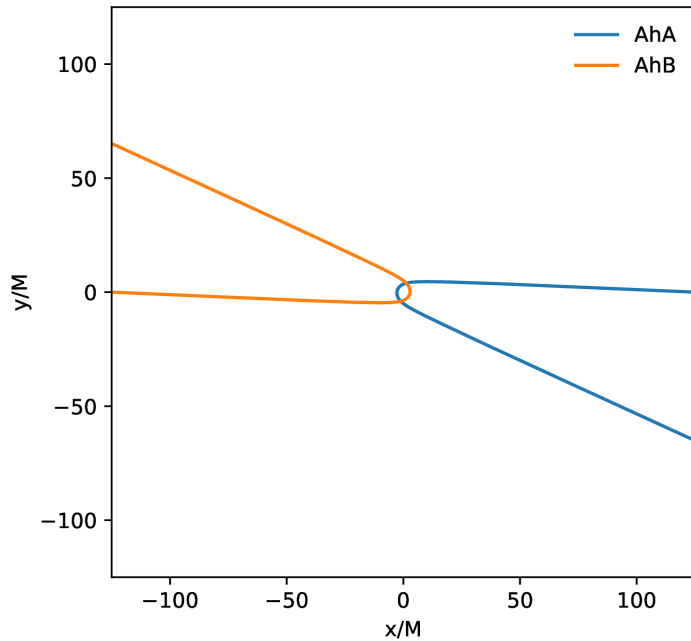
$$J_{\text{ADM}} = 1.78000 M^2$$



# Gravitational Wave Strain

$$E_{\text{ADM}} = 1.02230 M$$

$$J_{\text{ADM}} = 1.10304 M^2$$



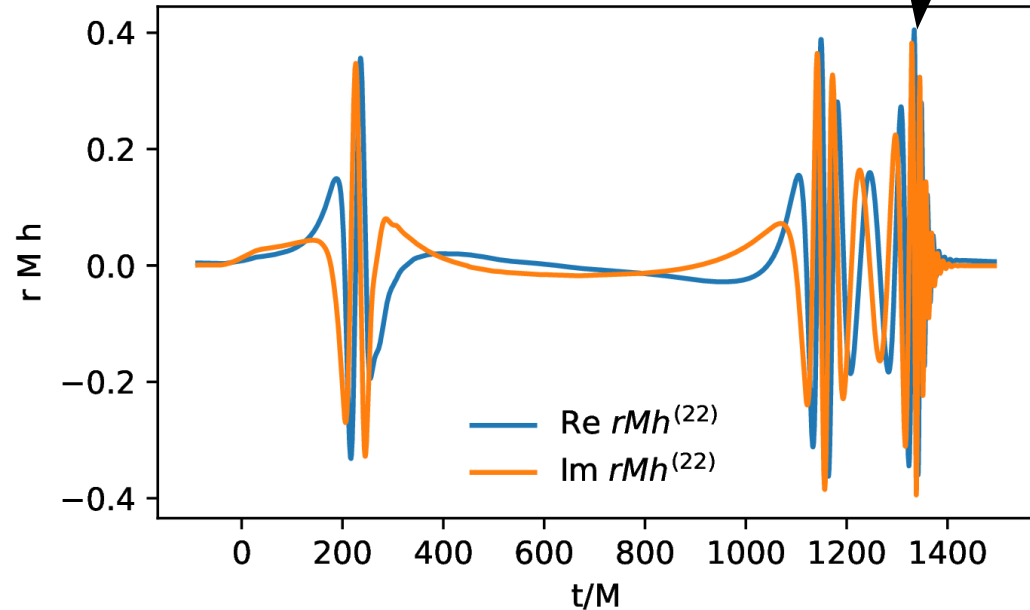
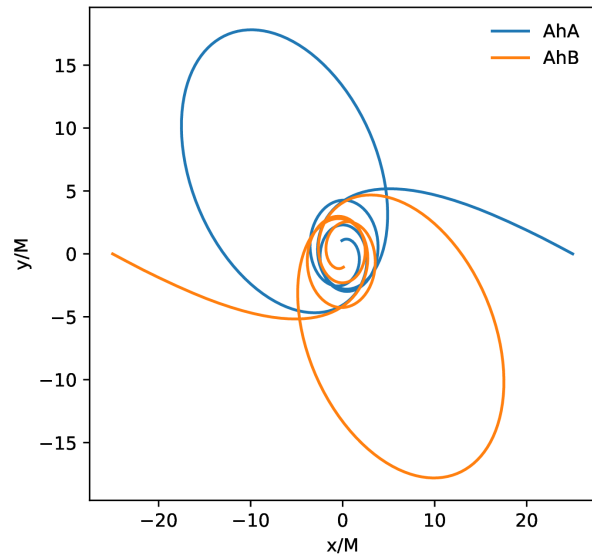


# Dynamical Capture

$$E_{\text{ADM}} = 1.00052 M$$

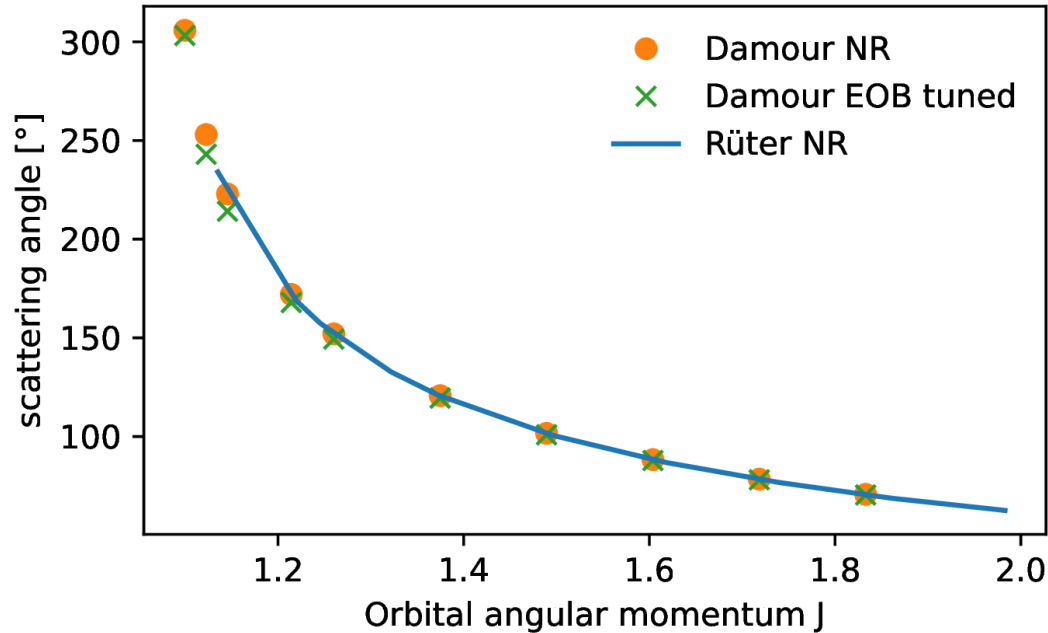
$$J_{\text{ADM}} = 1.007 M^2$$

Merger  
+ Ringdown



# Scattering Angles

$E=1.0226 M$

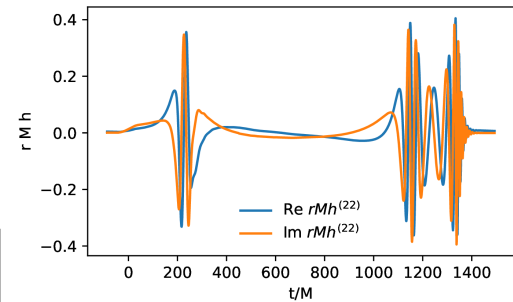
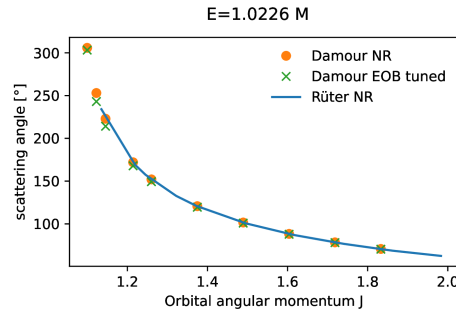
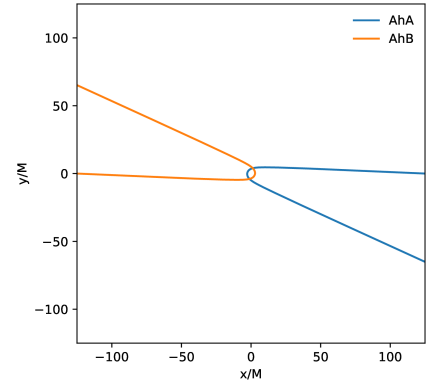


Damour NR:  
Damour et al.  
PRD 89, 081503 (2014)

Damour EOB tuned:  
Nagar et al.  
PRD 103, 064013 (2021)

# Summary

- We perform simulations of hyperbolic-like black hole encounters
- We extract the strain wave form
- Binary can become bound
- We extract the scattering angles

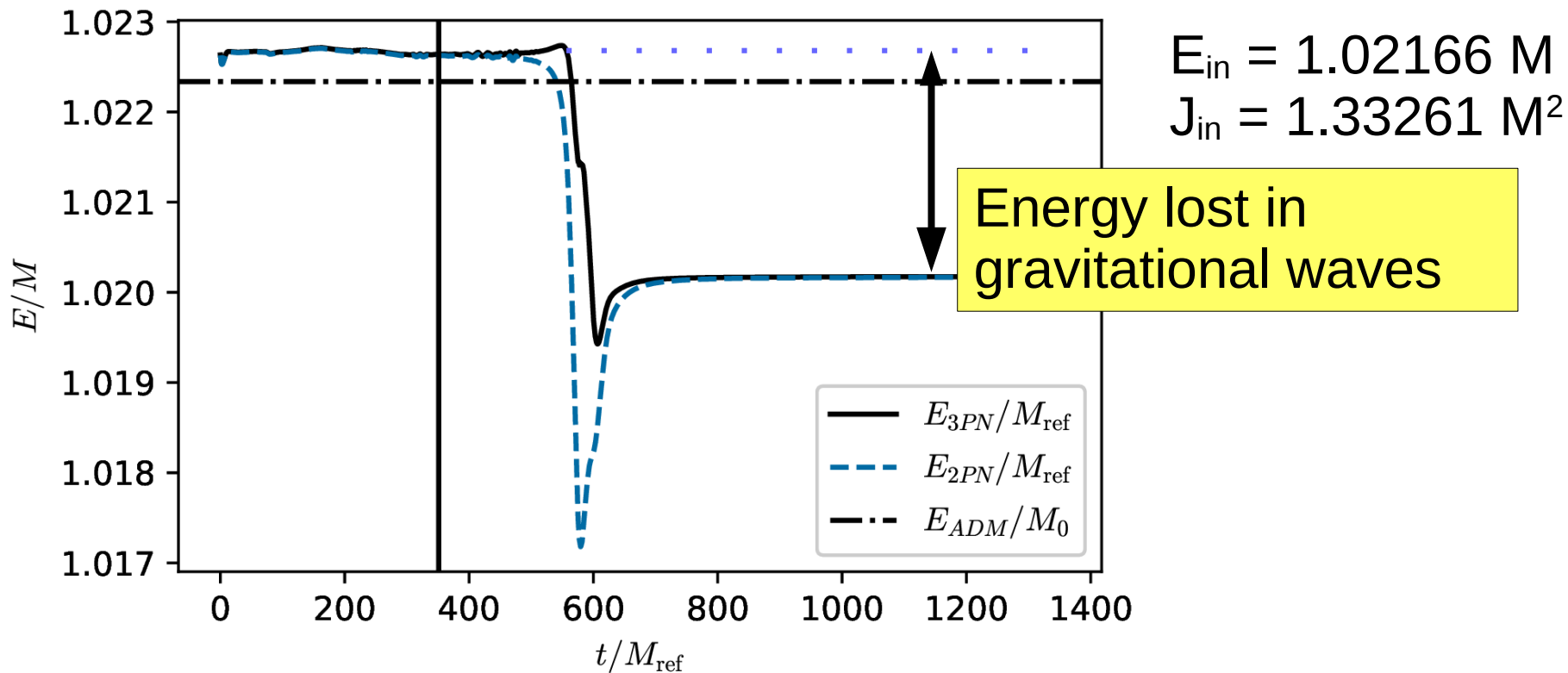


# Bonus: Computation of $E_{\text{orb}}$ and $J_{\text{orb}}$

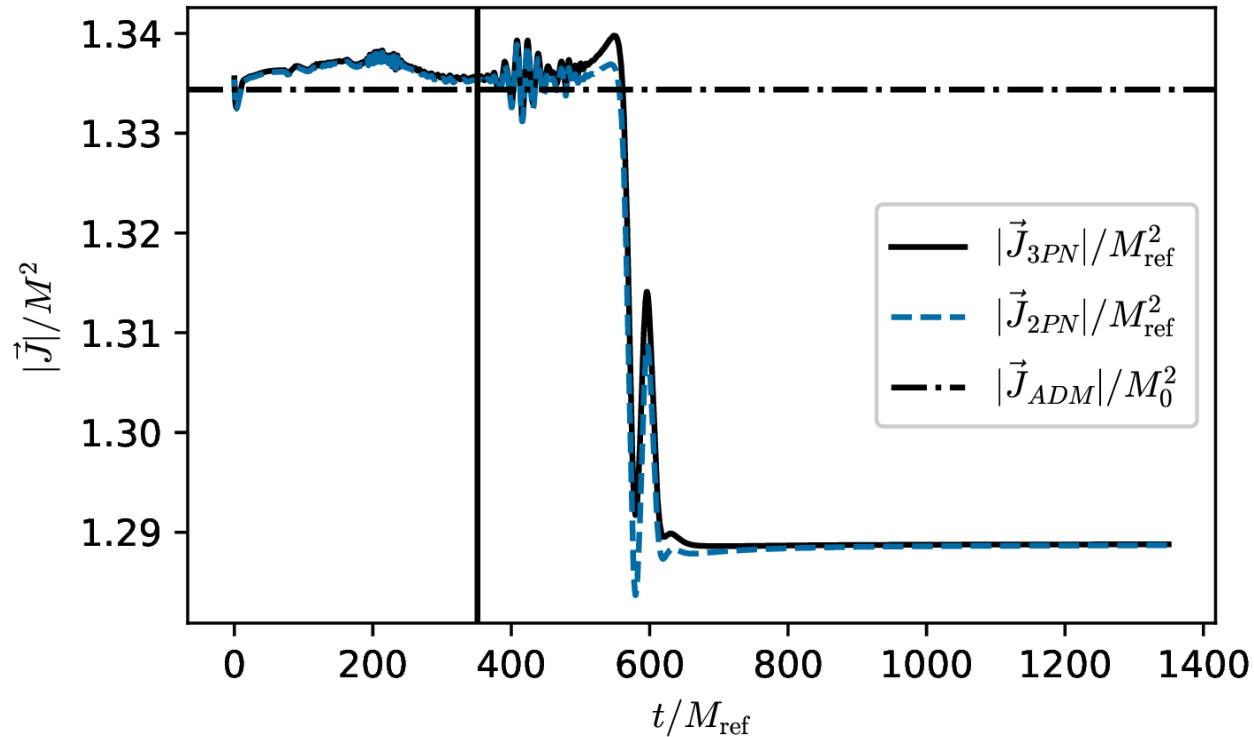
- Coevolve harmonic coordinates  $X^\mu$   
[Prayush Kumar]
- Use PN expressions for orbits in harmonic coordinates [Memmesheimer *et al.* - PRD **70** 104011 (2004)]

$$\rightarrow E_{\text{orb}}(X^\mu, V^\mu) \quad J_{\text{orb}}(X^\mu, V^\mu)$$

# Bonus: Orbital Energy

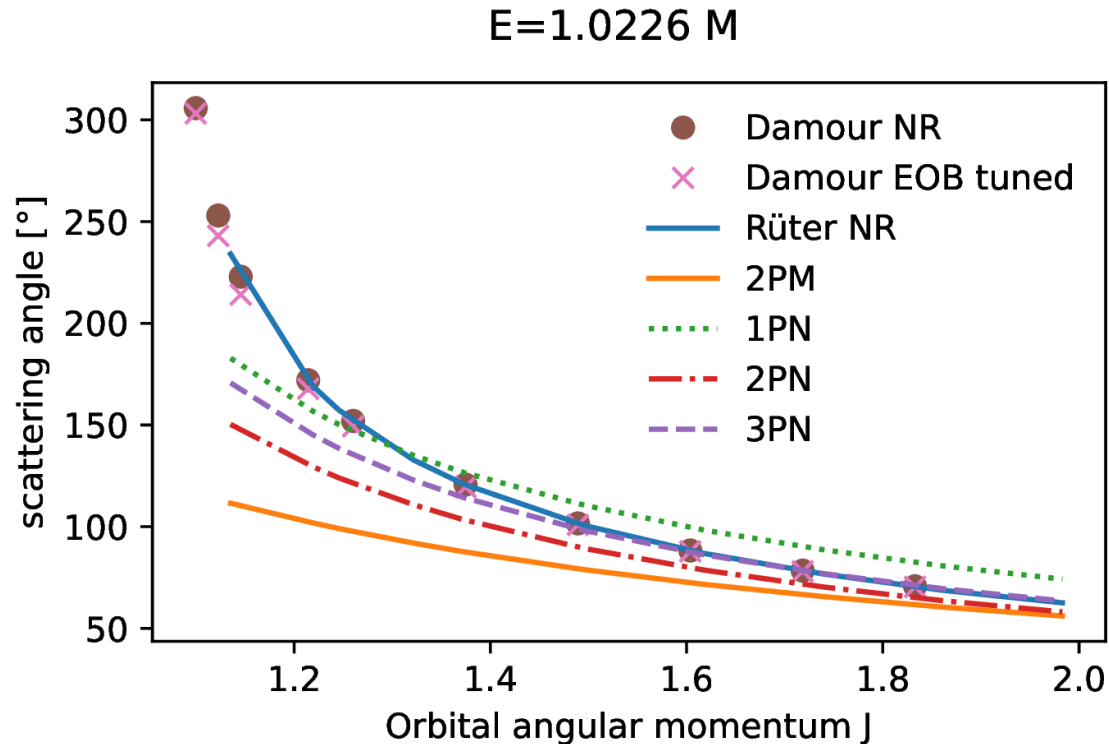


# Bonus: Orbital Angular Momentum



$$E_{\text{in}} = 1.02166 M$$
$$J_{\text{in}} = 1.33261 M^2$$

# Bonus: Scattering Angles



Damour NR:  
Damour et al.  
PRD 89, 081503 (2014)

Damour EOB tuned:  
Nagar et al.  
PRD 103, 064013 (2021)

PN:  
Scattering angle from  
quasi-Keplerian orbits  
derived in  
[Memmesheimer et al.  
PRD 70, 104011 (2004)]