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Particle Detectors

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History of Instrumentation ↔ History of Particle Physics

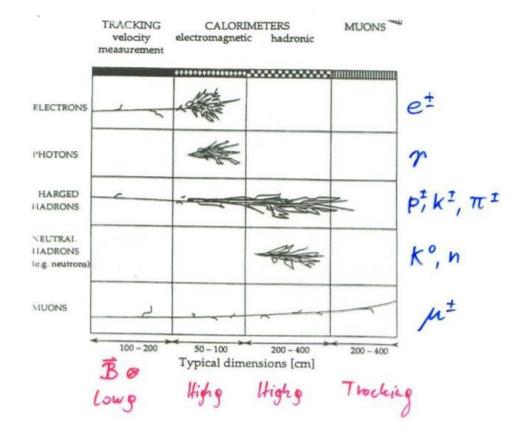
The 'Real' World of Particles

Interaction of Particles with Matter

Tracking Detectors, Calorimeters, Particle Identification

Detector Systems

We have to know the details about all interactions to design our detectors !



e^{\pm}	$m_e = 0.511 MeV$
mt	$m_e = 0.511 MeV$ $m_p = 105.7 \Pi eV \sim 200 me$ EM
r	$m_{\gamma} = 0$, $Q = 0$
$\pi^{\underline{r}}$	m _π = 139.6 MeV ~ 270 me } EM, Strong
K [±]	mk = 493.7 MeV ~ 1000 me ~ 3.5 mm
p±	mp = 938.3 MeV ~ 2000 me
Ko	mro = 497.7 MeV Q=0
n	$m_{xo} = 497.7 \text{ MeV } Q = 0$ $m_{y} = 939.6 \text{ MeV } Q = 0$ } Strong

Detector Physics

Precise knowledge of the processes leading to signals in particle detectors is necessary.

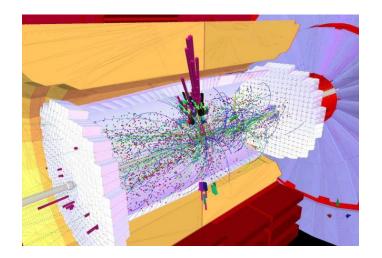
The detectors are nowadays working close to the limits of theoretically achievable measurement accuracy – even in large systems.

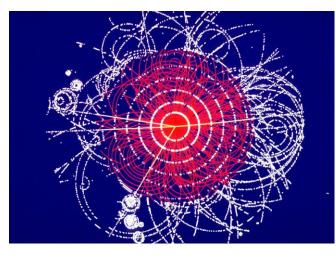
Due to available computing power, detectors can be simulated to within 5-10% of reality, based on the fundamental microphysics processes (atomic and nuclear cross-sections).

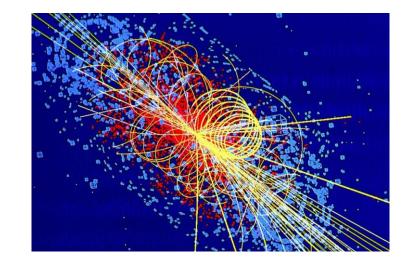
Particle Detector Simulation

CMS detector simulation GEANT

ATLAS detector simulation GEANT



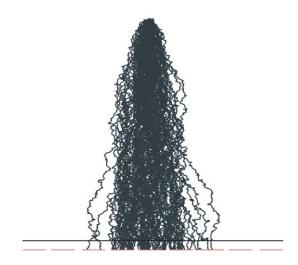


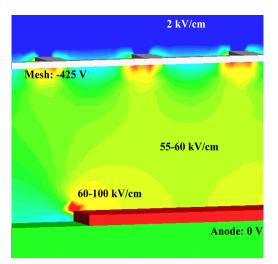


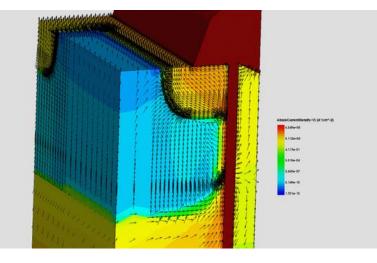
Electrons avalanche multiplication, GARFIELD++

Electric Fields in a Micromega detector, e.g. COMSOL

Silicon sensor simulation, TCAD







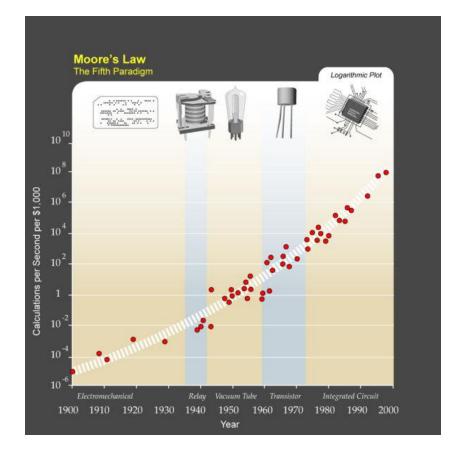
Particle Detector Simulation

I) C. Moore's Law: Computing power doubles 18 months.

II) W. Riegler's Law:

The use of brain power for solving a problem is inversely proportional to the available computing power.

 \rightarrow I) + II) = ...



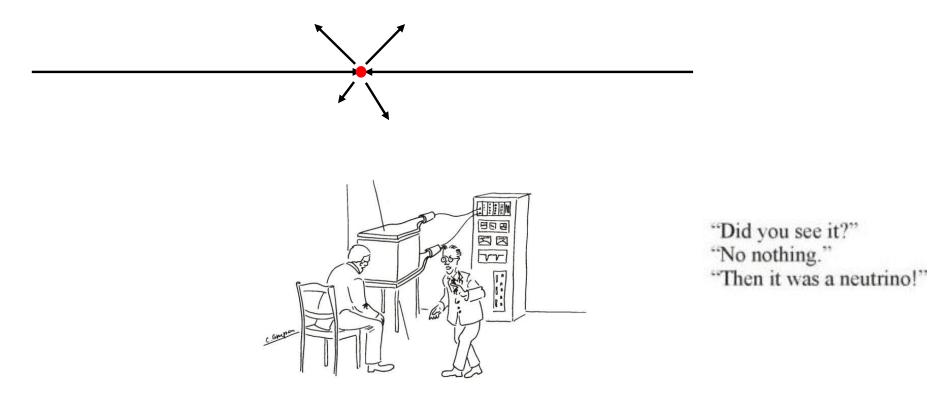
Knowing the basics of particle detectors is essential ...

Interaction of Particles with Matter

Any device that is to detect a particle must interact with it in some way \rightarrow almost ...

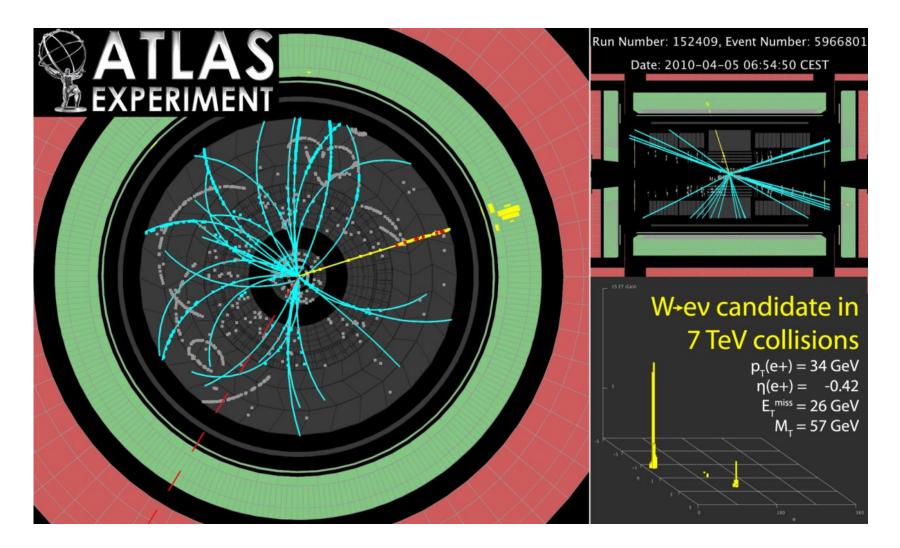
In many experiments neutrinos are measured by missing transverse momentum.

E.g. e^+e^- collider. $P_{tot}=0$, If the Σp_i of all collision products is $\neq 0 \rightarrow$ neutrino escaped.



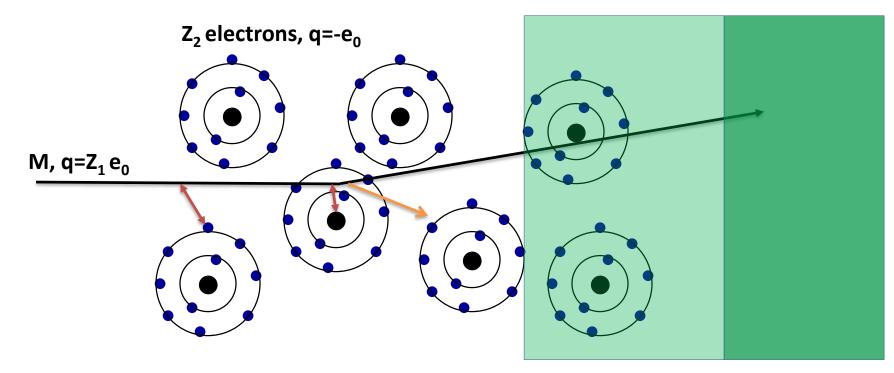
Claus Grupen, Particle Detectors, Cambridge University Press, Cambridge 1996 (455 pp. ISBN 0-521-55216-8)

Neutrinos and other invisible particles



They are seen by missing momentum vectors – if you are sure your detector is hermetic !

Electromagnetic Interaction of Particles with Matter

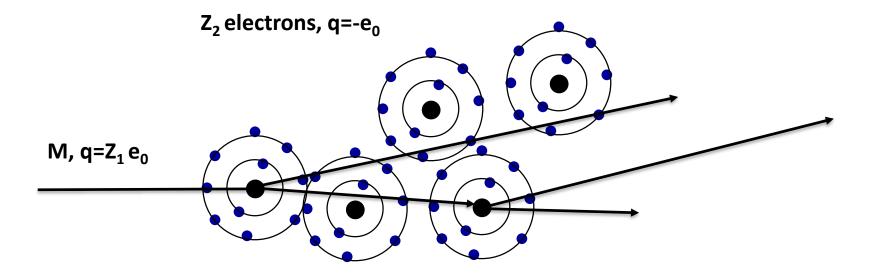


Interaction with the atomic electrons. The incoming particle loses energy and the atoms are <u>excited</u> or <u>ionized</u>.

Interaction with the atomic nucleus. The particle is deflected (scattered) causing <u>multiple scattering</u> of the particle in the material. During this scattering a <u>Bremsstrahlung</u> photon can be emitted.

In case the particle's velocity is larger than the velocity of light in the medium, the resulting EM shockwave manifests itself as <u>Cherenkov Radiation</u>. When the particle crosses the boundary between two media, there is a probability of the order of 1% to produced and X ray photon, called <u>Transition radiation</u>.

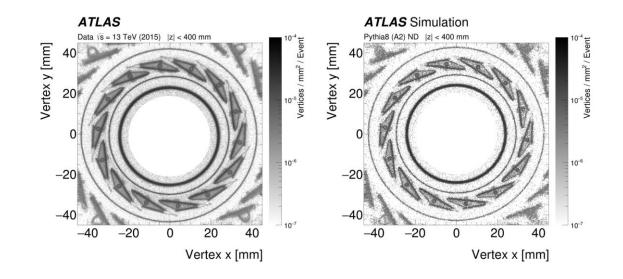
Hadronic Interaction of Particles with Matter



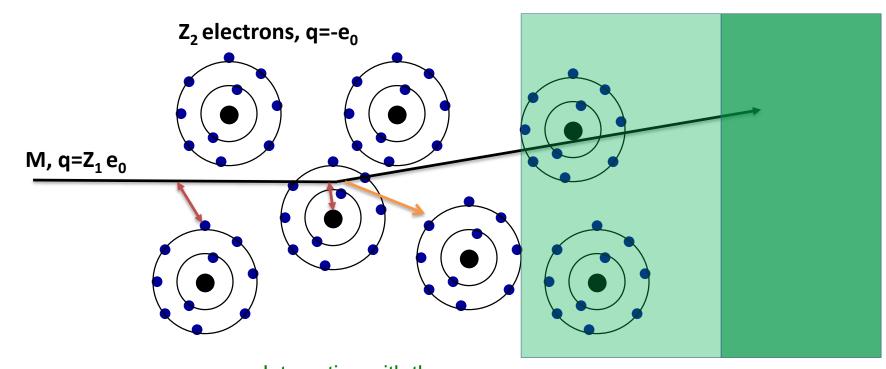
Hadronic interactions with the nuclei produce a complex sequence of secondary particles. This is at the basis of hadron calorimetry.

Hadronic interactions taking place in the trackers are of course having bad an impact on the tracker measurements !

Tracing back these secondary particles to their origin gives the place of interaction. Making a map of these points we can image our detectors !



Electromagnetic Interaction of Particles with Matter



Interaction with the atomic electrons. The incoming particle loses energy and the atoms are <u>excited</u> or <u>ionized.</u> Interaction with the atomic nucleus. The particle is deflected (scattered) causing <u>multiple scattering of</u> the particle in the material. During this scattering a <u>Bremsstrahlung</u> photon can be emitted.

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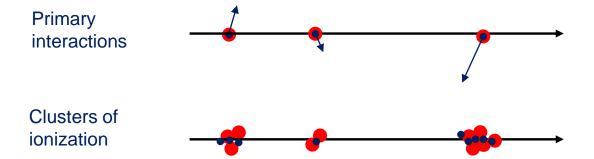
Ionization and Excitation

The charges particles leave a trail of excited and ionized atoms.

The electrons and holes produced in these interactions do themselves have sufficient energy ionize the gas or solid, but because there energy is small the loose all their energy over a very small distance, so in we get a trail of ionization-clusters along the way.

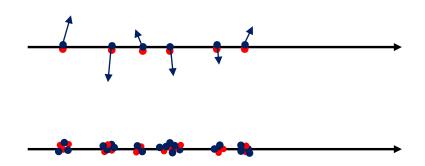
The de-excitation of the excited atoms and the movement of the electrons/holes/ions in electric field are the basis for signals in our particle detectors.

Let's make a more quantitative assessment of this ...

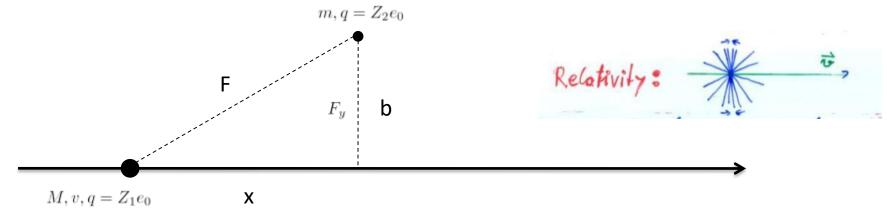


Electrons and ions in gases

Electrons and holes in solids



Ionization and Excitation



While the charged particle is passing another charged particle, the Coulomb Force is acting, resulting in momentum transfer

$$F_y = \frac{Z_1 Z_2 e_0^2}{4\pi\varepsilon_0 (b^2 + v^2 t^2)} \frac{b}{\sqrt{b^2 + v^2 t^2}} \qquad \Delta p = \int_{-\infty}^{\infty} F_y(t) dt = \frac{2Z_1 Z_2 e_0^2}{4\pi\varepsilon_0 v b}$$

The relativistic form of the transverse electric field doesn't change the momentum transfer. The transverse field is stronger, but the time of action is shorter

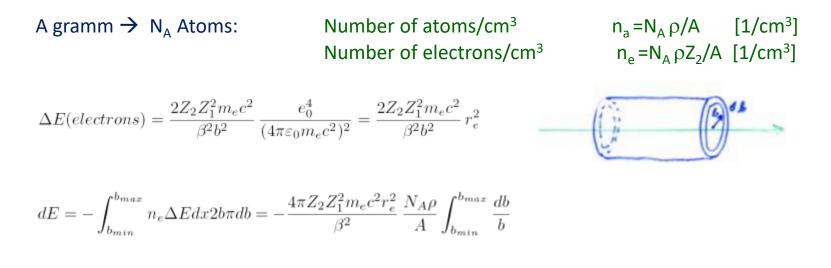
$$F_y = \frac{\gamma Z_1 Z_2 e_0^2 b}{4\pi\varepsilon_0 (b^2 + \gamma^2 v^2 t^2)^{3/2}} \qquad \Delta p = \int_{-\infty}^{\infty} F_y(t) dt = \frac{2Z_1 Z_2 e_0^2}{4\pi\varepsilon_0 v b}$$

The transferred energy is then
$$\Delta E = \frac{(\Delta p)^2}{2m} = \frac{Z_2^2}{m} \frac{2Z_1^2 e_0^4}{(4\pi\varepsilon_0)^2 v^2 b^2}$$
$$\Delta E(electrons) = Z_2 \frac{1}{m_e} \frac{2Z_1^2 e_0^4}{(4\pi\varepsilon_0)^2 v^2 b^2} \qquad \Delta E(nucleus) = \frac{Z_2^2}{2Z_2 m_p} \frac{2Z_1^2 e_0^4}{(4\pi\varepsilon_0)^2 v^2 b^2} \qquad \frac{\Delta E(electrons)}{\Delta E(nucleus)} = \frac{2m_p}{m_e} \approx 4000$$

 \rightarrow The incoming particle transfer energy only (mostly) to the atomic electrons !

Ionization and Excitation

Target material: mass A, Z₂, density ρ [g/cm³], Avogadro number N_A

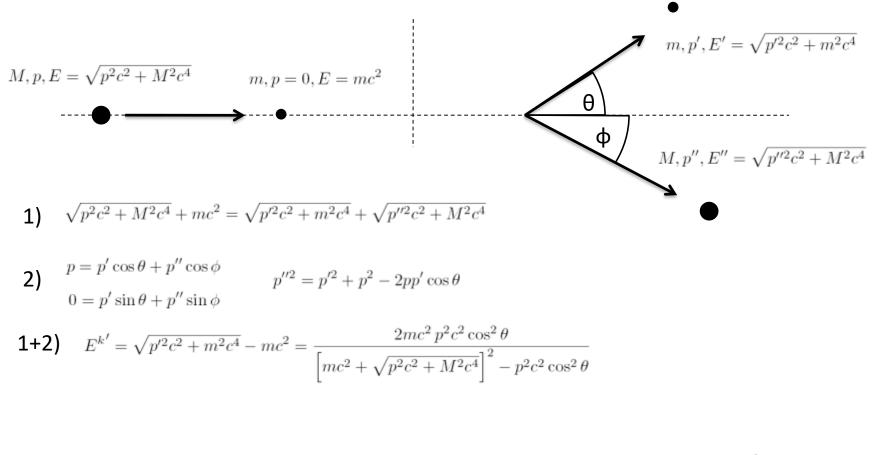


With $\Delta E(b) \rightarrow db/b = -1/2 dE/E \rightarrow E_{max} = \Delta E(b_{min}) E_{min} = \Delta E(b_{max})$

$$\frac{dE}{dx} = -2\pi r_e^2 m_e^2 c^2 \frac{Z_1^2}{\beta^2} \frac{N_A Z_2 \rho}{A} \int_{E_{min}}^{E_{max}} \frac{dE}{E} \qquad = \qquad -2\pi r_e^2 m_e^2 c^2 \frac{Z_1^2}{\beta^2} \frac{N_A Z_2 \rho}{A} \ln \frac{E_{max}}{E_{min}}$$

$$E_{min} \approx I$$
 (Ionization Energy)

Relativistic Collision Kinematics, E_{max}



$$E^{k'}_{\ max} = \frac{2mc^2p^2c^2}{(m^2 + M^2)c^4 + 2m\sqrt{p^2c^2 + M^2c^4}} = 2mc^2\beta^2\gamma^2F \qquad F = \left(1 + \frac{2m}{M}\sqrt{1 + \beta^2\gamma^2} + \frac{m^2}{M^2}\right)^{-1}$$

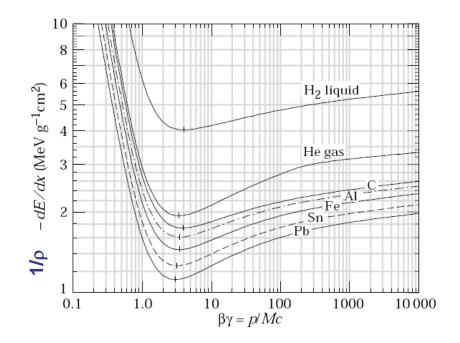
W. Riegler/CERN

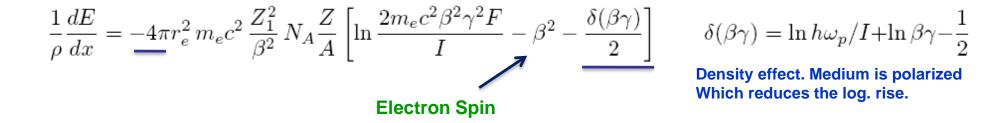
Classical Scattering on Free Electrons

$$\frac{1}{\rho}\frac{dE}{dx} = -2\pi r_e^2 m_e c^2 \frac{Z_1^2}{\beta^2} N_A \frac{Z}{A} \ln \frac{2m_e c^2 \beta^2 \gamma^2 F}{I}$$

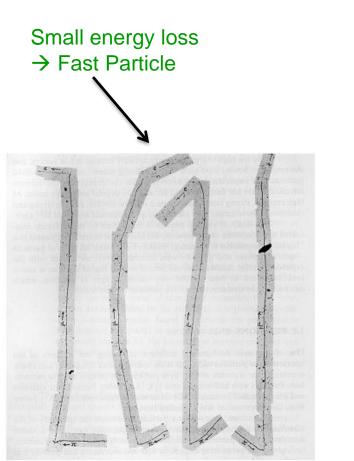
This formula is up to a factor 2 and the density effect identical to the precise QM derivation \rightarrow



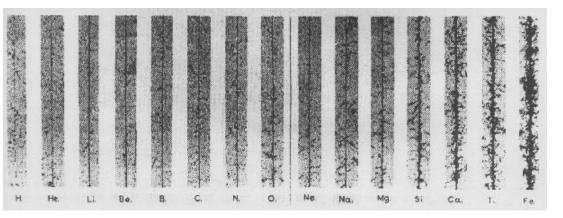




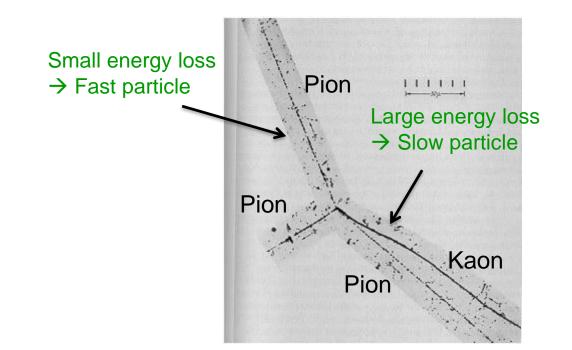
Bethe-Bloch formula



Discovery of muon and pion



Cosmis rays: dE/dx α Z²



Bethe-Bloch formula

$$\frac{1}{\rho}\frac{dE}{dx} = -4\pi r_e^2 \, m_e c^2 \, \frac{Z_1^2}{\beta^2} \, N_A \frac{Z}{A} \left[\ln \frac{2m_e c^2 \beta^2 \gamma^2 F}{I} - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right] \qquad \text{Für Z>1, I \approx16Z $^{0.9} eV}$$

For Large $\beta\gamma$ the medium is being polarized by the strong transverse fields, which reduces the rise of the energy loss \rightarrow density effect

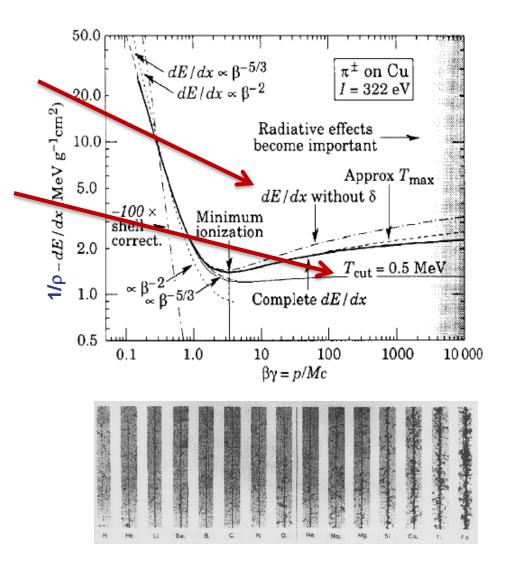
At large Energy Transfers (delta electrons) the liberated electrons can leave the material.

In reality, E_{max} must be replaced by E_{cut} and the energy loss reaches a plateau (Fermi plateau).

Characteristics of the energy loss as a function of the particle velocity ($\beta\gamma$)

The specific Energy Loss 1/p dE/dx

- first decreases as $1/\beta^2$
- increases with ln γ for β =1
- is \approx independent of M (M>>m_e)
- is proportional to Z_1^2 of the incoming particle.
- is \approx independent of the material (Z/A \approx const)
- shows a plateau at large $\beta\gamma$ (>>100)
- $dE/dx \approx 1-2 \ x \ \rho \ [g/cm^3]$ MeV/cm



Bethe-Bloch formula

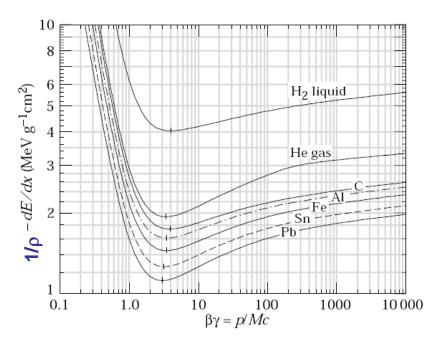
Bethe Bloch Formula, a few Numbers:

For Z \approx 0.5 A $1/\rho~dE/dx\approx$ 1.4 MeV cm $^2/g$ for ßy \approx 3

Example:

Iron: Thickness = 100 cm; ρ = 7.87 g/cm³ dE \approx 1.4 * 100* 7.87 = 1102 MeV

 \rightarrow A 1 GeV Muon can traverse 1m of Iron



This number must be multiplied with ρ [g/cm³] of the Material \rightarrow dE/dx [MeV/cm]

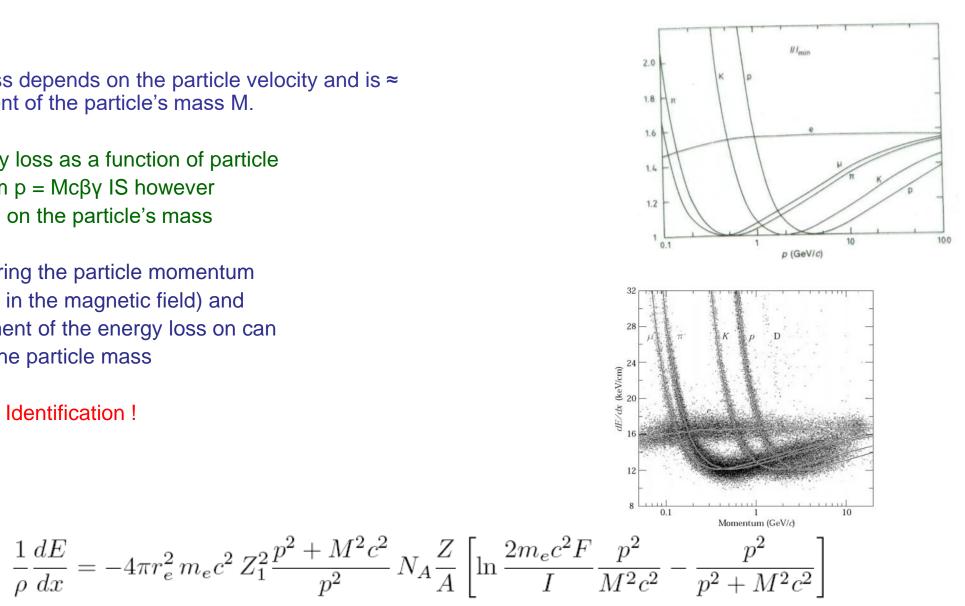
Energy loss as a function of the momentum

Energy loss depends on the particle velocity and is \approx independent of the particle's mass M.

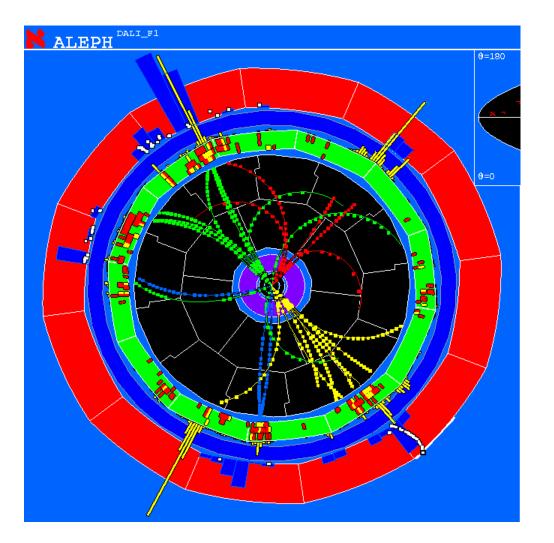
The energy loss as a function of particle momentum $p = Mc\beta \gamma$ IS however depending on the particle's mass

By measuring the particle momentum (deflection in the magnetic field) and measurement of the energy loss on can measure the particle mass

 \rightarrow Particle Identification !



Energy loss as a function of the momentum



Measure momentum by curvature of the particle track.

Find dE/dx by measuring the deposited charge along the track.

→Particle ID

Range of Particles in Matter

Particle of mass M and kinetic Energy E_0 enters matter and looses energy until it comes to rest at distance R. 50000

material

$$R(E_0) = \int_{E_0}^0 \frac{-1}{dE/dx} dE$$
$$R(\beta_0 \gamma_0) = \frac{Mc^2}{\rho} \frac{1}{Z_1^2} \frac{A}{Z} f(\beta_0 \gamma_0)$$

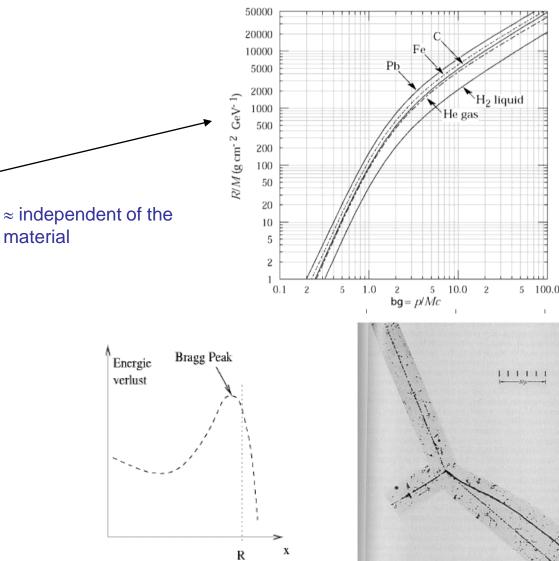
$$\frac{\rho}{Mc^2} R(\beta_0 \gamma_0) = \frac{1}{Z_1^2} \frac{A}{Z} f(\beta_0 \gamma_0)$$

Bragg Peak:

For $\beta\gamma$ >3 the energy loss is \approx constant (Fermi Plateau)

If the energy of the particle falls below $\beta\gamma$ =3 the energy loss rises as $1/\beta^2$

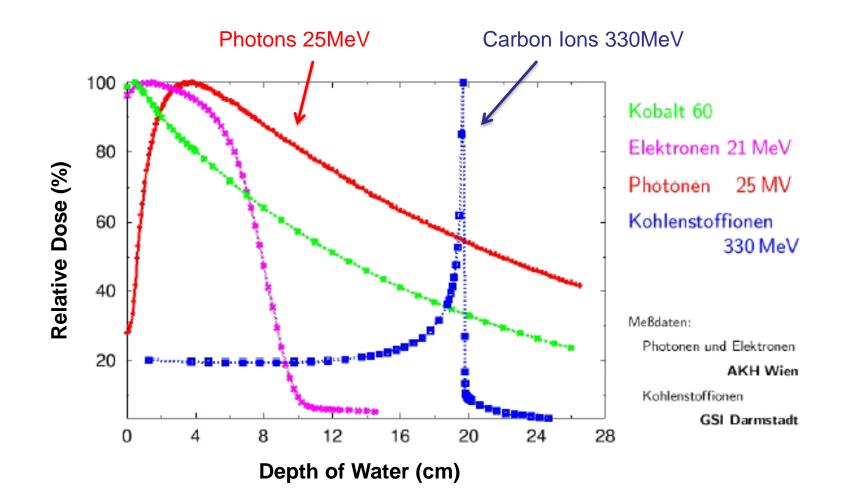
Towards the end of the track the energy loss is largest \rightarrow Cancer Therapy.



Range of Particles in Matter

Average Range:

Towards the end of the track the energy loss is largest \rightarrow Bragg Peak \rightarrow Cancer Therapy

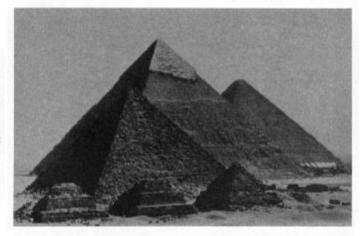


Search for Hidden Chambers in the Pyramids

The structure of the Second Pyramid of Giza is determined by cosmic-ray absorption.

Luis W. Alvarez, Jared A. Anderson, F. El Bedwei, James Burkhard, Ahmed Fakhry, Adib Girgis, Amr Goneid, Fikhny/ Hassan, Dennis Iverson, Gerald Lynch, Zenab Miligy, Ali Hilmy Moussa, Mohammed-Sharkawi, Lauren Yazolino Fig. 2 (bottom right). Cross sections of (a) the Great Pyramid of Cheops and (b) the Pyramid of Chephren, showing the known chambers: (A) Smooth limestone cap, (B) the Belzoni Chamber, (C) Belzoni's entrance, (D) Howard-Vyse's entrance, UM descending passageway, (F) ascending passageway, (G) underground chamber, (-1) Grand Gallery, (I) King's Chamber, (I) Queen's Chamber, (K) center line of the pyramid.

6 FEBRUARY 1970



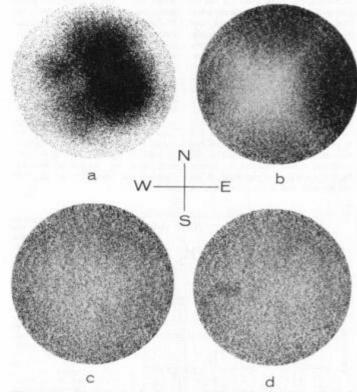
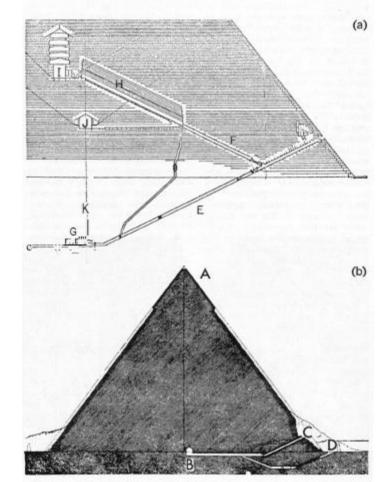


Fig. 13. Scatter plots showing the three stages in the combined analytic and visual analysis of the data and a plot with a simulated chamber, (a) Simulated "x-ray photograph" of uncorrected data. (b) Data corrected for the geometrical acceptance of the apparatus. (c) Data corrected for pyramid structure as well as geometrical acceptance. (d) Same as (c) but with simulated chamber, as in Fig. 12.

Luis Alvarez used the attenuation of muons to look for chambers in the Second Giza Pyramid → Muon Tomography

He proved that there are no chambers present.



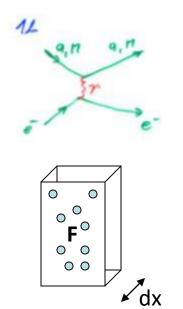
Intermezzo: Crossection

Crossection σ : Material with Atomic Mass A and density $\,\rho$ contains n Atoms/cm^3

$$n[\text{cm}^{-3}] = \frac{N_A[\text{mol}^{-1}]\,\rho[\text{g/cm}^3]}{A[\text{g/mol}]} \qquad N_A = 6.022 \times 10^{23}\,\text{mol}^{-1}$$

E.g. Atom (Sphere) with Radius R: Atomic Crossection $\sigma = R^2 \pi$

A volume with surface F and thickness dx contains N=nFdx Atoms. The total 'surface' of atoms in this volume is N σ . The relative area is $p = N \sigma/F = N_A \rho \sigma /A dx =$ Probability that an incoming particle hits an atom in dx.



What is the probability P that a particle hits an atom between distance x and x+dx ? P = probability that the particle does NOT hit an atom in the m=x/dx material layers and that the particle DOES hit an atom in the mth layer

$$P(x)dx = (1-p)^m p \approx e^{-m} p = \exp\left(-\frac{N_A\rho\sigma}{A}x\right) \frac{N_A\rho\sigma}{A}dx = \frac{1}{\lambda}\exp\left(-\frac{x}{\lambda}\right)dx \qquad \lambda = \frac{A}{N_A\rho\sigma}dx$$

 $\begin{array}{ll} \text{Mean free path} & = \int_0^\infty x P(x) dx = \int_0^\infty \frac{x}{\lambda} \, e^{-\frac{x}{\lambda}} dx = \lambda \\ \text{Average number of collisions/cm} & = \frac{1}{\lambda} = \frac{N_A \rho \sigma}{A} \end{array}$

Intermezzo: Differential Crossection



Differential Crossection:

 \rightarrow Crossection for an incoming particle of energy E to lose an energy between E' and E'+dE'

Total Crossection:

$$\sigma(E) = \int \frac{d\sigma(E, E')}{dE'} dE'$$

 $\frac{d\sigma(E,E')}{dE'}$

Probability P(E) that an incoming particle of Energy E loses an energy between E' and E'+dE' in a collision:

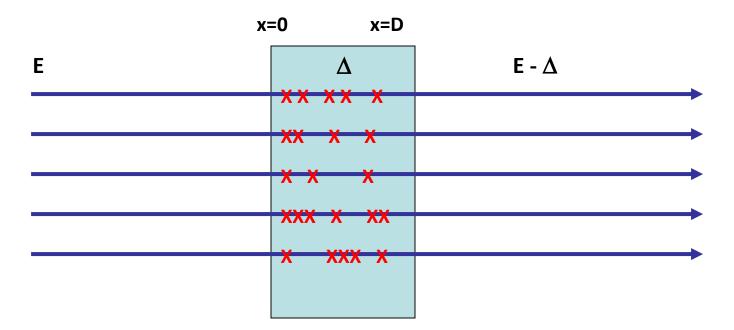
$$P(E, E')dE' = \frac{1}{\sigma(E)} \frac{d\sigma(E, E')}{dE'} dE'$$

Average number of collisions/cm causing an energy loss between E' and E'+dE' = $\frac{N_A \rho}{A} \frac{d\sigma(E, E')}{dE'}$

Average energy loss/cm:
$$\frac{dE}{dx} = -\frac{N_A \rho}{A} \int E' \frac{d\sigma(E,E')}{dE'} dE'$$

Fluctuation of Energy Loss

Up to now we have calculated the average energy loss. The energy loss is however a statistical process and will therefore fluctuate from event to event.



 $P(\Delta) = ?$ Probability that a particle loses an energy Δ when traversing a material of thickness D

We have see earlier that the probability of an interaction occuring between distance x and x+dx is exponentially distributed

$$P(x)dx = \frac{1}{\lambda} \exp\left(-\frac{x}{\lambda}\right) dx \qquad \lambda = \frac{A}{N_A \rho \sigma}$$

Probability for n Interactions in D

We first calculate the probability to find n interactions in D, knowing that the probability to find a distance x between two interactions is $P(x)dx = 1/\lambda \exp(-x/\lambda) dx$ with $\lambda = A/N_A \rho \sigma$

Probability to have no interaction between 0 und D:

$$P(x > D) = \int_D^\infty P(x_1) dx_1 = e^{-\frac{D}{\lambda}}$$

Probability to have one interaction at x_1 and no other interaction:

$$P(x_1, x_2 > D) = \int_D^\infty P(x_1) P(x_2 - x_1) dx_2 = \frac{1}{\lambda} e^{-\frac{D}{\lambda}}$$

Probability to have one interaction independently of x_1 :

$$\int_0^D P(x_1, x_2 > D) = \frac{D}{\lambda} e^{-\frac{D}{\lambda}}$$

Probability to have the first interaction at x_1 , the second at x_2 the $n^{th} \in x_n$ and no other interaction:

$$P(x_1, x_2...x_n > D) = \int_D^\infty P(x_1)P(x_2 - x_1)...P(x_n - x_{n-1})dx_n = \frac{1}{\lambda^n}e^{-\frac{D}{\lambda}}$$

Probability for *n* interactions independently of $x_1, x_2...x_n$

$$\int_{0}^{D} \int_{0}^{x_{n-1}} \int_{0}^{x_{n-1}} \dots \int_{0}^{x_{1}} P(x_{1}, x_{2}..., x_{n} > D) dx_{1}...dx_{n-1} = \frac{1}{n!} \left(\frac{D}{\lambda}\right)^{n} e^{-\frac{D}{\lambda}}$$

Probability for n Interactions in D

For an interaction with a mean free path of λ , the probability for n interactions on a distance D is given by

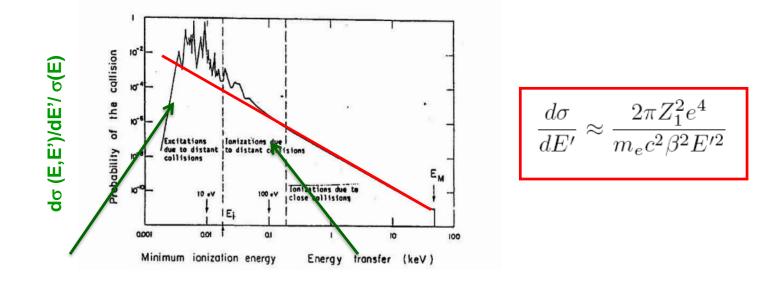
$$P(n) = \frac{1}{n!} \left(\frac{D}{\lambda}\right)^n e^{-\frac{D}{\lambda}} = \frac{\overline{n}^n}{n!} e^{-\overline{n}} \qquad \overline{n} = \frac{D}{\lambda} \qquad \lambda = \frac{A}{N_A \rho \sigma}$$

 \rightarrow Poisson Distribution !

$$\begin{split} f(E) &= \frac{1}{\sigma} \frac{d\sigma}{dE} \\ p(E) &= P(1)f(E) + P(2) \int_0^E f(E-E')f(E')dE' + P(3) \int_0^E \int_0^{E'} f(E-E'-E'')f(E'')f(E')dE''dE' + \dots \\ F(s) &= \mathcal{L}\left[f(E)\right] = \int_0^\infty f(E)e^{-sE}dE \\ \mathcal{L}\left[p(E)\right] &= P(1)F(s) + P(2)F(s)^2 + P(3)F(s)^3 + \dots \\ &= \sum_{n=1}^\infty P(n)F(s)^n = \sum_{n=1}^\infty \frac{\overline{n}^n F^n}{n!} e^{-\overline{n}} = e^{\overline{n}(F(s)-1)} - 1 \approx e^{\overline{n}(F(s)-1)} \\ p(E) &= \mathcal{L}^{-1}\left[e^{\overline{n}(F(s)-1)}\right] = \frac{1}{2\pi i} \int_{\sigma-i\infty}^{\sigma+i\infty} e^{\overline{n}(F(s)-1)+sE} ds \end{split}$$

Fluctuations of the Energy Loss

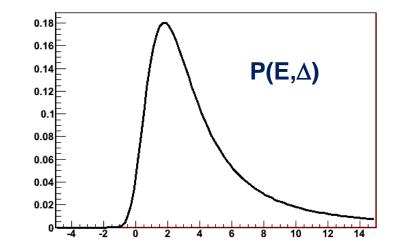
Probability f(E) for loosing energy between E' and E'+dE' in a single interaction is given by the differential crossection $d\sigma$ (E,E')/dE'/ σ (E) which is given by the Rutherford crossection at large energy transfers



Excitation and ionization

$$p(x) = \frac{1}{2\pi i} \int_{c-i\infty}^{c+i\infty} \exp(s\log s + xs) \, ds.$$
$$= \frac{1}{\pi} \int_{0}^{\infty} \exp(-t\log t - xt) \sin(\pi t) \, dt.$$
$$x = \frac{E}{\overline{n}\epsilon} + C_{\gamma} - 1 - \ln \overline{n} \qquad \overline{n} = \frac{N_A \rho Z_2 k D}{A\epsilon}$$
$$\ln \epsilon = \ln \frac{I^2}{E_{max}} + 2\beta^2$$

Scattering on free electrons



Landau Distribution

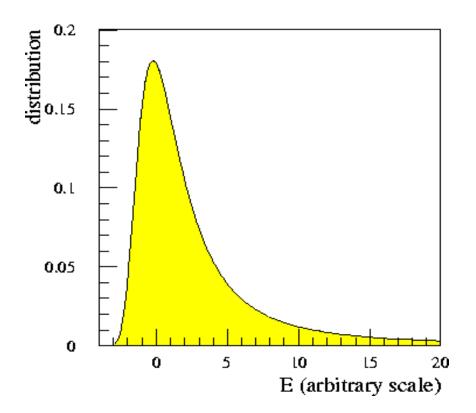
 $P(\Delta)$: Probability for energy loss Δ in matter of thickness D.

Landau distribution is very asymmetric.

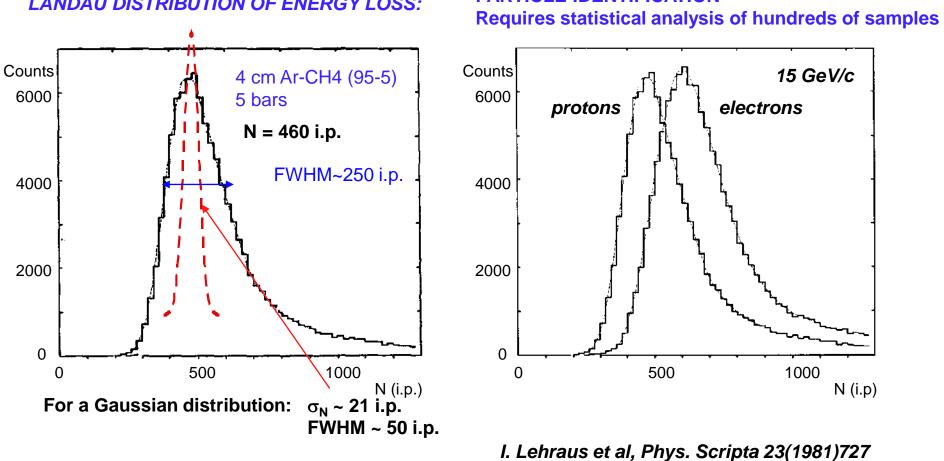
Average and most probable energy loss must be distinguished !

Measured Energy Loss is usually smaller that the real energy loss:

3 GeV Pion: $E'_{max} = 450 MeV \rightarrow A 450$ MeV Electron usually leaves the detector.



Landau Distribution

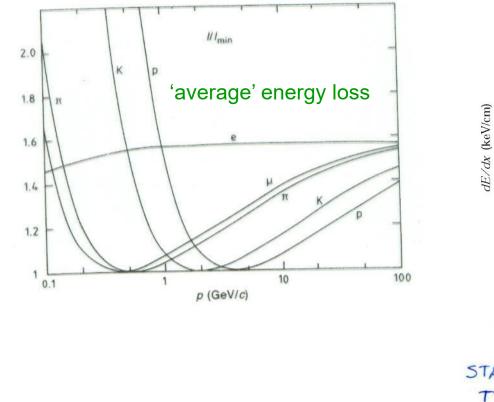


PARTICLE IDENTIFICATION LANDAU DISTRIBUTION OF ENERGY LOSS:

Particle Identification

Measured energy loss

1.0



32 28 24 20 20 20 20 20 16 12 8 0.1 10 Momentum (GeV/c) BLUE => PIONS BLACK => NO ID POSSIBLE RED => KAONS GREEN => PROTONS MAGENTA => ELECTRONS dE/dx vs. Rigidity (~ 50 HIJING Events) 4.0e-06 STAR TPC 3.5e-06 3.0e-06 2.5e-06 2.0e-06

0.5

Rigidity

1.5e-06

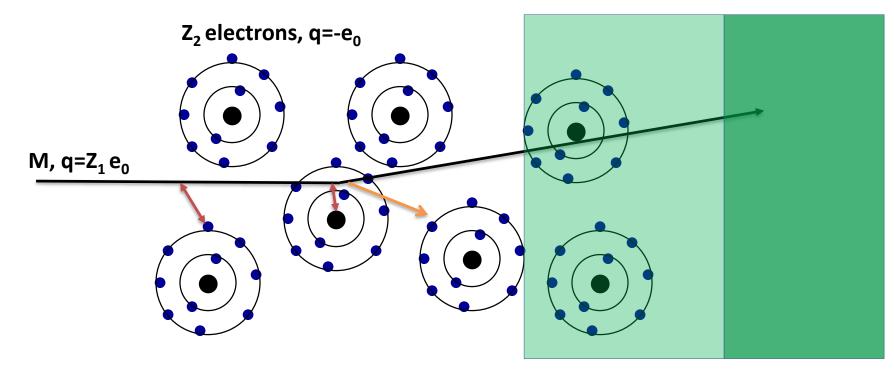
1.0e-06

5.0e-07

In certain momentum ranges, particles can be identified by measuring the energy loss.



Electromagnetic Interaction of Particles with Matter

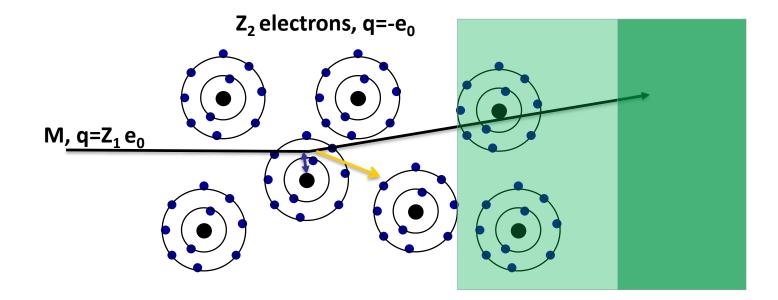


Interaction with the atomic electrons. The incoming particle loses energy and the atoms are <u>excited</u> or <u>ionized</u>.

Interaction with the atomic nucleus. The particle is deflected (scattered) causing <u>multiple scattering</u> of the particle in the material. During this scattering a <u>Bremsstrahlung</u> photon can be emitted. In case the particle's velocity is larger than the velocity of light in the medium, the resulting EM shockwave manifests itself as <u>Cherenkov Radiation</u>. When the particle crosses the boundary between two media, there is a probability of the order of 1% to produced and X ray photon, called <u>Transition radiation</u>.

Bremsstrahlung

A charged particle of mass M and charge $q=Z_1e$ is deflected by a nucleus of charge Ze which is partially 'shielded' by the electrons. During this deflection the charge is 'accelerated' and it therefore radiated \rightarrow Bremsstrahlung.



Bremsstrahlung, Classical

9= 2-1 e q,M $\frac{de'}{d\Omega} = \left(\frac{2\bar{z}_1\bar{z}_2e^2}{4\pi\epsilon_0 P\cdot V}\right)^2 \frac{1}{(2\sin 2)^4}$ D - Mur " Rukaford Scattering" Written in Terms of Monechin Transfer Q: 2p= (1-coo) $\frac{de'}{AQ} = 8\pi \left(\frac{3}{4\pi\epsilon}\frac{e^2}{Ac}\right)^2 \cdot \frac{1}{Q^3}$ \vec{p} \vec{p}' $Q = |\vec{p} - \vec{p}'|$ $\frac{dI}{dW} \sim \frac{2}{3\pi} \frac{2^2 e^2}{M^2 c^3} \frac{1}{4\pi c} Q^2 Radiated Energy between <math>\vec{w}, w + dw$ Jaw Stade . de , when - Th dE = NAS. $\frac{dE}{dx} = \frac{N_{A}g}{A} \cdot \frac{16}{3} d \cdot 2^{2} \cdot \left(\frac{2^{2}e^{2}}{4\pi\epsilon_{0}} \operatorname{Mcz}\right)^{2} \cdot E \cdot \ln \frac{R_{max}}{R}$ L= e 1

A charged particle of mass M and charge $q=Z_1e$ is deflected by a nucleus of Charge Ze.

Because of the acceleration the particle radiated EM waves \rightarrow energy loss.

Coulomb-Scattering (Rutherford Scattering) describes the deflection of the particle.

Maxwell's Equations describe the radiated energy for a given momentum transfer.

 \rightarrow dE/dx

Bremsstrahlung, QM

26 Brenssluchlung Q.M. Q.M. E. q=Z_ae, E+Mc1>> 137Mc1 Z=3 > Aigle Relativistic: Z $\frac{d \sigma'(E_{I}E')}{AE'} = 4 \mathcal{L} \mathcal{Z}^{2} \mathcal{Z}^{4}_{n} \left(\frac{1}{4\pi \epsilon_{o}} \frac{e^{2}}{Mc^{4}} \right)^{2} \frac{1}{E'} \mp (E, E')$ $\overline{\mp}(E,E') = \left[1 + \left(1 - \frac{E'}{E+Mcs}\right)^2 - \frac{2}{3}\left(1 - \frac{E'}{E+Mcs}\right)\right] \ln 183 \frac{1}{2} + \frac{1}{4}\left(1 - \frac{E'}{E+Mcs}\right)$ $\frac{dE}{dx} = -\frac{N_{A}g}{A} \int E' \frac{de'}{dt'} dt' - 42 Z' Z_{4}^{4} \left(\frac{1}{4\pi\epsilon_{0}} \frac{e^{1}}{\pi\epsilon_{0}}\right)^{2} E \left[l_{4} 183 Z^{\frac{1}{3}} + \frac{1}{18} \right]$ $\frac{dE}{dx} = -\frac{N_A g}{A} 4d z^* z^* \left(\frac{1}{4\pi\epsilon_o} \frac{e^2}{hc^*}\right)^2 E ln(183z^{-\frac{2}{3}})$

$$E(x) = E_0 e^{-\frac{x}{x_0}} \qquad X_0 = \frac{A}{42 N_A g Z^2 (\frac{1}{4\pi \epsilon_0} \frac{e^2}{nc^2})^2 \ln 183 Z^{-\frac{2}{3}}}$$
$$X_0 = Rodiction length$$

Proportional to Z²/A of the Material.

Proportional to Z₁⁴ of the incoming particle.

Proportional to ρ of the material.

Proportional 1/M² of the incoming particle.

Proportional to the Energy of the Incoming particle \rightarrow

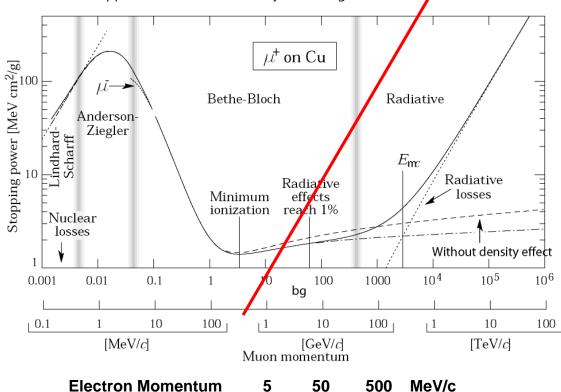
E(x)=Exp(-x/X₀) – 'Radiation Length'

 $X_0 \propto M^2 A / (\rho Z_1^4 Z^2)$

 X_0 : Distance where the Energy E_0 of the incoming particle decreases $E_0Exp(-1)=0.37E_0$.

Critical Energy

such as copper to about 1% accuracy for energies between about 6 MeV and 6 GeV



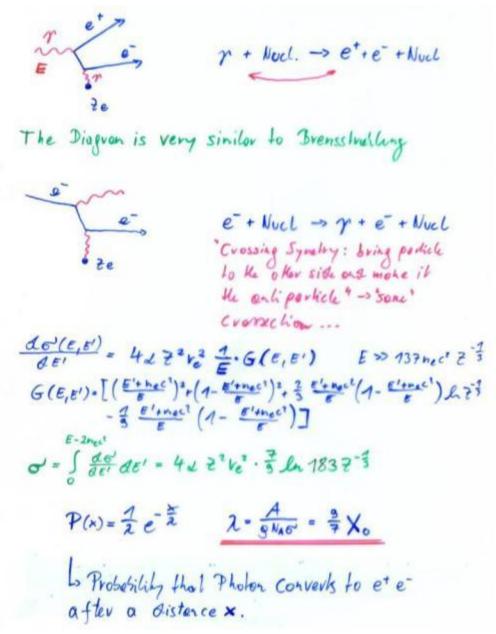
For the muon, the second lightest particle after the electron, the critical energy is at 400GeV.

The EM Bremsstrahlung is therefore only relevant for electrons at energies of past and present detectors.

Critical Energy: If dE/dx (Ionization) = dE/dx (Bremsstrahlung)

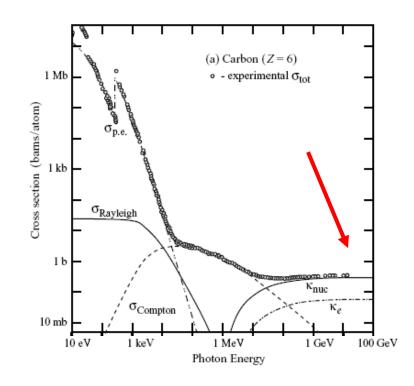
Myon in Copper: $p \approx 400 \text{GeV}$ Electron in Copper: $p \approx 20 \text{MeV}$

Pair Production, QM

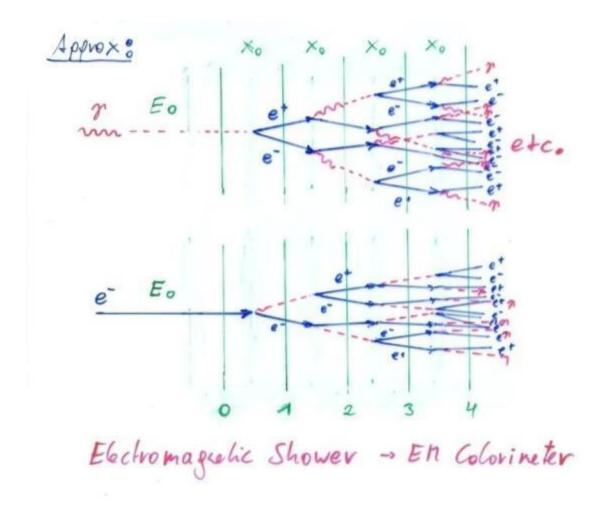


For $E\gamma > m_e c^2 = 0.5 MeV$: $\lambda = 9/7 X_0$

Average distance a high energy photon has to travel before it converts into an $e^+ e^-$ pair is equal to 9/7 of the distance that a high energy electron has to travel before reducing it's energy from E₀ to E₀*Exp(-1) by photon radiation.



Bremsstrahlung + Pair Production → EM Shower



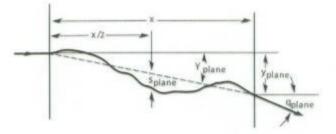
Statistical (quite complex) analysis of multiple collisions gives:

Probability that a particle is defected by an angle θ after travelling a distance x in the material is given by a Gaussian distribution with sigma of:

$$\Theta_0 = \frac{0.0136}{\beta cp [\text{GeV/c}]} Z_1 \sqrt{\frac{x}{X_0}}$$

X₀... Radiation length of the material

- Z_1 ... Charge of the particle
- p... Momentum of the particle



Magnetic Spectrometer: A charged particle describes a circle in a magnetic field:

$$\vec{B} \otimes L = R \cdot \Theta$$

$$L = R \cdot \Theta$$

$$S = R(1 - 60 \frac{\alpha}{2}) \sim R = \frac{\theta^2}{8} = \frac{L^2}{8R} \rightarrow R = \frac{L^2}{85}$$

$$\Delta p = 0.3 \text{ B } \Delta R = 0.3 \text{ B } \frac{L^2}{85^2} \Delta S$$

$$\Delta s = \frac{6L}{1N^2} \quad 6L = 0.3 \text{ B } \frac{L^2}{85^2} \Delta S$$

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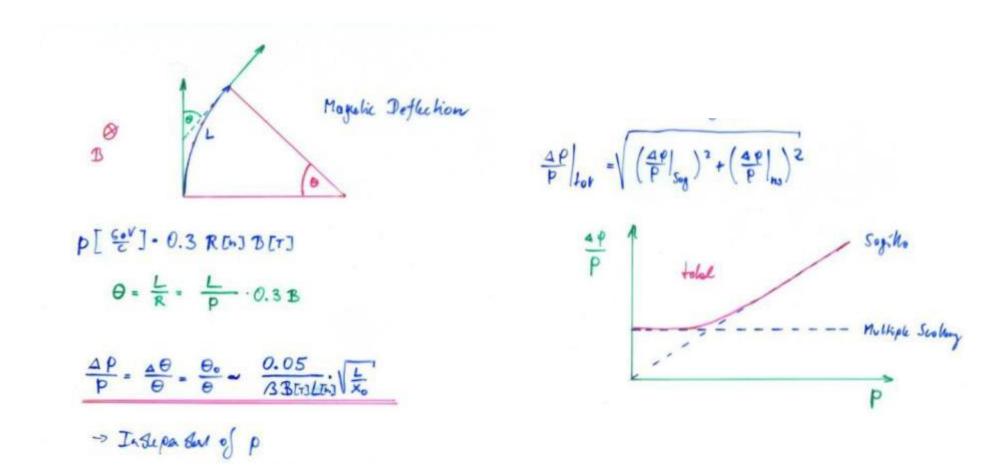
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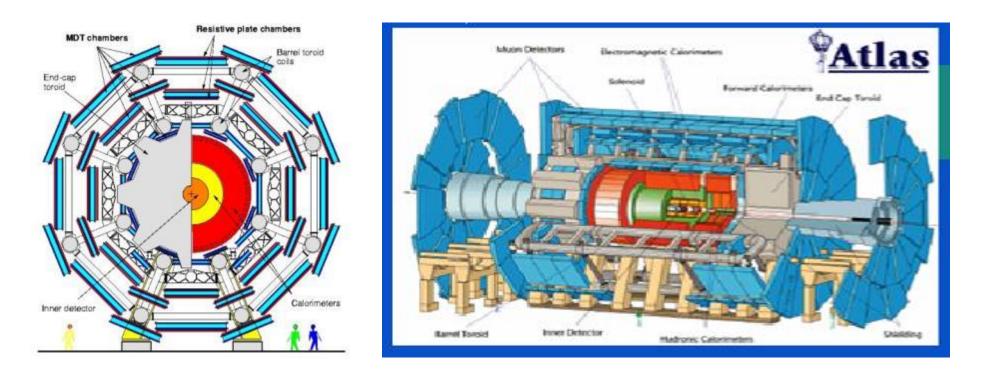
$$\vec{\Delta} s = \frac{6L}{1N^2} \quad 8L = 0.3 \text{ B } \frac{L^2}{10^2} \text{ B }$$

Limit → Multiple Scattering



ATLAS Muon Spectrometer: N=3, sig=50µm, P=1TeV, L=5m, B=0.4T

 $\Delta p/p \sim 8\%$ for the most energetic muons at LHC



Cherenkov Radiation

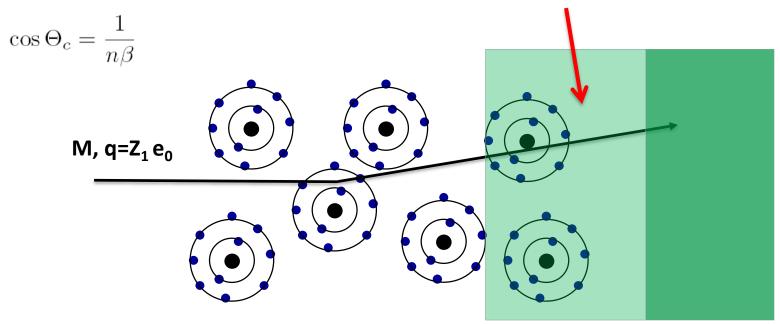
If we describe the passage of a charged particle through material of dielectric permittivity ε (using Maxwell's equations) the differential energy cross-section is >0 if the velocity of the particle is larger than the velocity of light in the medium is

$$\frac{d\sigma}{dE} = \frac{\alpha}{\beta^2 \pi} \frac{A}{N_A \rho Z_2 \hbar c} \left(\beta^2 - \frac{1}{\epsilon_1} \right) \quad \rightarrow \quad \frac{N_A \rho Z_2}{A} \frac{d\sigma}{d\omega} \frac{d\omega}{dE} = \frac{\alpha}{c} \left(1 - \frac{1}{\beta^2 n^2} \right) \qquad n = \sqrt{\epsilon_1} \qquad E = \hbar \omega$$

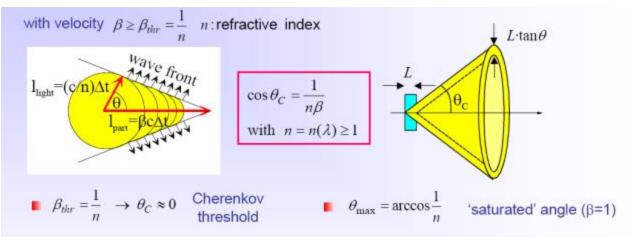
$$\frac{dE}{dx d\omega} \frac{1}{\hbar} = \frac{\alpha}{c} \left(1 - \frac{1}{\beta^2 n^2} \right) \qquad \rightarrow \qquad \frac{dN}{dx d\lambda} = \frac{2\pi \alpha}{\lambda^2} \left(1 - \frac{1}{\beta^2 n^2} \right) \qquad \omega = \frac{2\pi c}{\lambda}$$

N is the number of Cherenkov Photons emitted per cm of material. The expression is in addition proportional to Z_1^2 of the incoming particle.

The radiation is emitted at the characteristic angle θ_c , that is related to the refractive index n and the particle velocity by



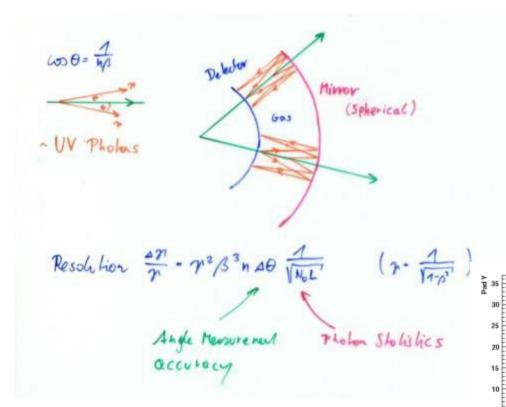
Cherenkov Radiation



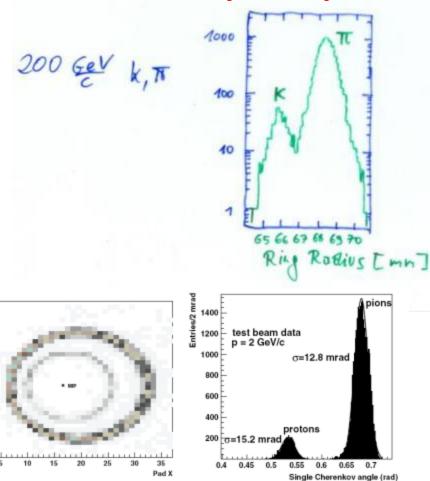
If the velocity of a chargest particle is lorger than the velocity of light in He we sign to > = (n ... Reprective Index of Makriel) it emits Grenkov' radiotion at a characteritic orghe of coste = This (B= 2) $\frac{dN}{Ax} \sim 2\pi d Z_{\eta}^{2} \left(1 - \frac{\Lambda}{\beta^{2}n^{2}}\right) \frac{\lambda_{2} - \lambda_{\eta}}{\lambda_{2} \cdot \lambda_{\eta}}$ = Number of emille Photons / largh with 2 between 29 and 2 Wik 2, - 400mm 2,= 700 mm aN = 430 (1 - 1) [1]

Maleriel	n-1	B Haranhold	7 threshold
solid Sodium	3.22	0.24	1.029
lead gloss	0.67	0.60	1.25
water	0.33	0.75	1.52
silica aerogel	0.025-0.075	0.93-0.976	2.7 - 4.6
air	2.93-10-4	0.9957	41.2
He	3.3.10-5	0.99997	123

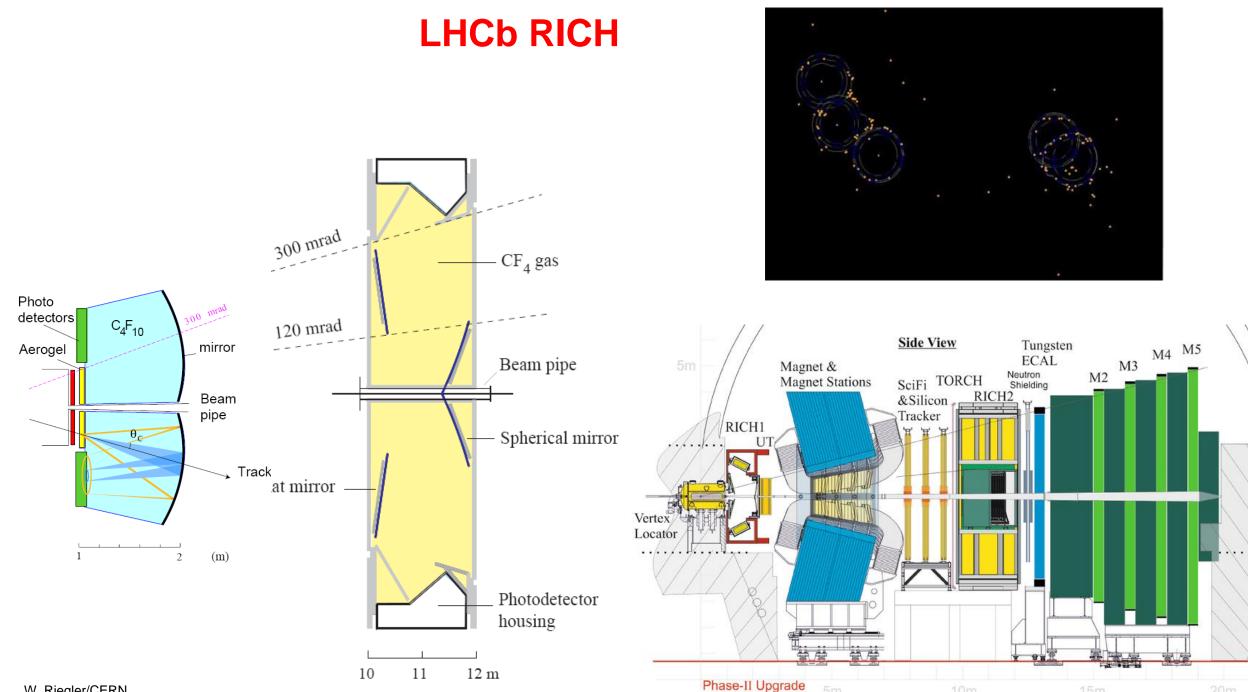
Ring Imaging Cherenkov Detector (RICH)

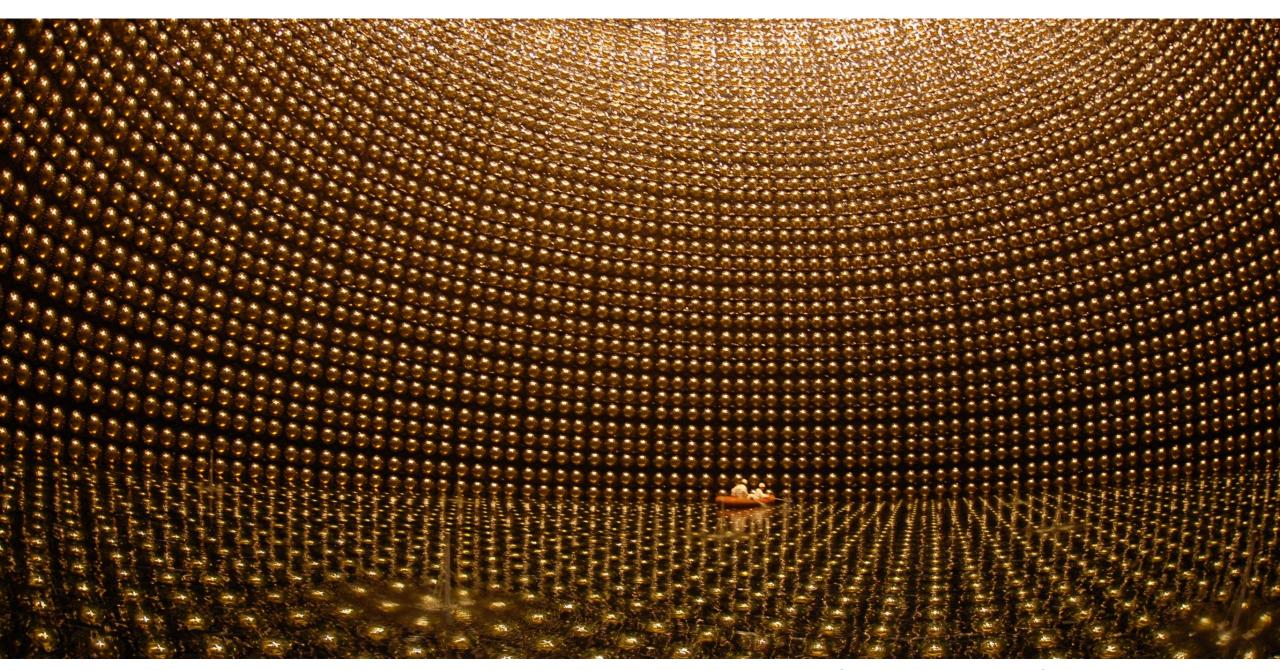


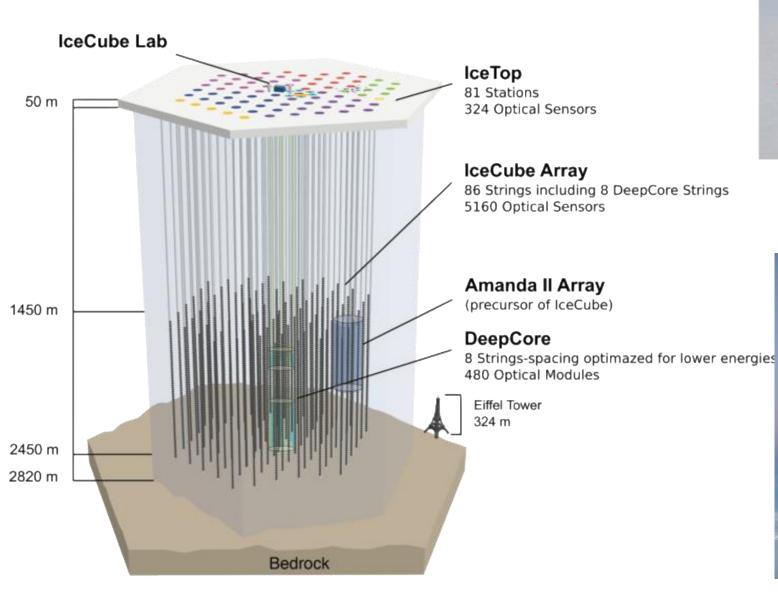
medium	n	$\theta_{max} \; (deg.)$	$N_{ph} (eV^{-1} cm^{-1})$
air*	1.000283	1.36	0.208
isobutane*	1.00127	2.89	0.941
water	1.33	41.2	160.8
quartz	1.46	46.7	196.4

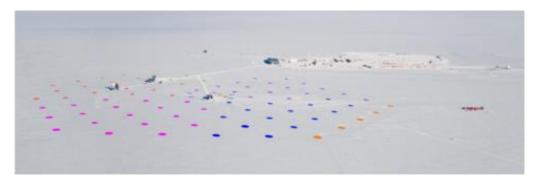


There are only 'a few' photons per event →one needs highly sensitive photon detectors to measure the rings !







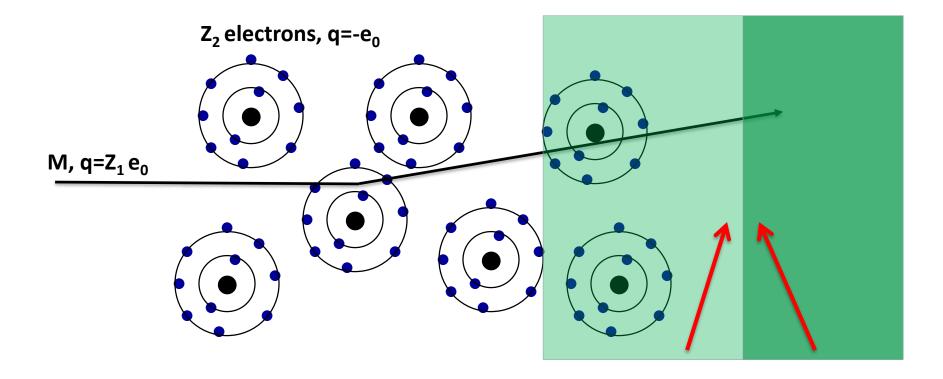


IceCube Aerial View



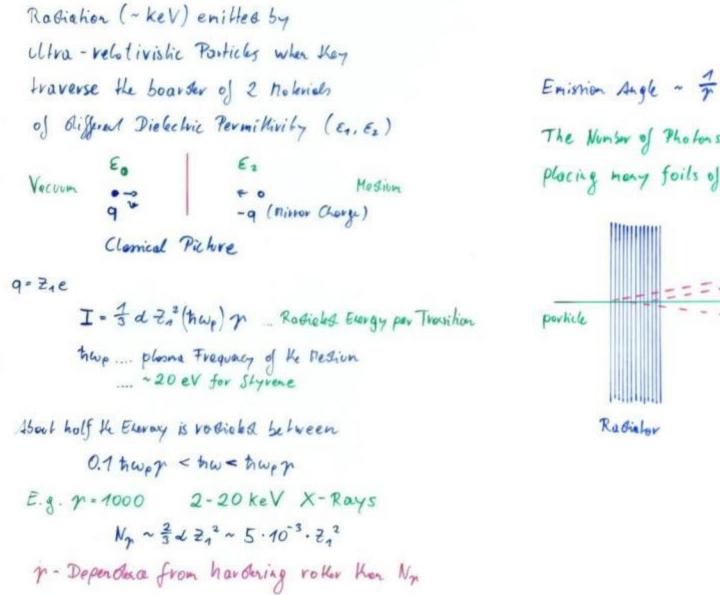
IceCube Cherekov Detector

Transition Radiation



When the particle crosses the boundary between two media, there is a probability of the order of 1% to produced and X ray photon, called <u>Transition radiation</u>.

Transition Radiation



The Number of Photons can be increased by placing many foils of Noterial. X-Rays porticle

Delebor

Radialar

Electromagnetic Interaction of Particles with Matter

Ionization and Excitation:

Charged particles traversing material are exciting and ionizing the atoms.

The average energy loss of the incoming particle by this process is to a good approximation described by the Bethe Bloch formula.

The energy loss fluctuation is well approximated by the Landau distribution.

Multiple Scattering and Bremsstrahlung:

The incoming particles are scattering off the atomic nuclei which are partially shielded by the atomic electrons.

Measuring the particle momentum by deflection of the particle trajectory in the magnetic field, this scattering imposes a lower limit on the momentum resolution of the spectrometer.

The deflection of the particle on the nucleus results in an acceleration that causes emission of Bremsstrahlungs-Photons. These photons in turn produced e+e- pairs in the vicinity of the nucleus, which causes an EM cascade. This effect depends on the 2nd power of the particle mass, so it is only relevant for electrons.

Electromagnetic Interaction of Particles with Matter

Cherenkov Radiation:

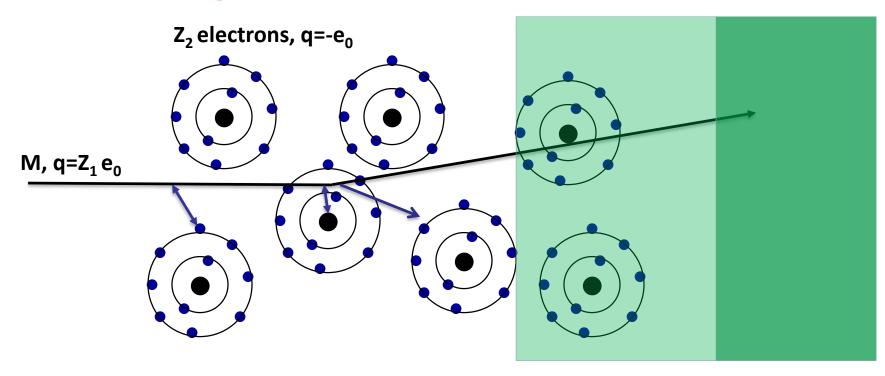
If a particle propagates in a material with a velocity larger than the speed of light in this material, Cherenkov radiation is emitted at a characteristic angle that depends on the particle velocity and the refractive index of the material.

Transition Radiation:

If a charged particle is crossing the boundary between two materials of different dielectric permittivity, there is a certain probability for emission of an X-ray photon.

 \rightarrow The strong interaction of an incoming particle with matter is a process which is important for Hadron calorimetry and will be discussed later.

Electromagnetic Interaction of Particles with Matter



Now that we know all the Interactions we can talk about Detectors !

Interaction with the atomic electrons. The incoming particle loses energy and the atoms are <u>excited</u> or <u>ionized.</u>

Interaction with the atomic nucleus. The particle is deflected (scattered) causing <u>multiple scattering</u> of the particle in the material. During this scattering a <u>Bremsstrahlung</u> photon can be emitted. In case the particle's velocity is larger than the velocity of light in the medium, the resulting EM shockwave manifests itself as <u>Cherenkov Radiation</u>. When the particle crosses the boundary between two media, there is a probability of the order of 1% to produced and X ray photon, called <u>Transition radiation</u>.

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