



Accelerator Technology Challenges Magnets and Superconductivity PART I

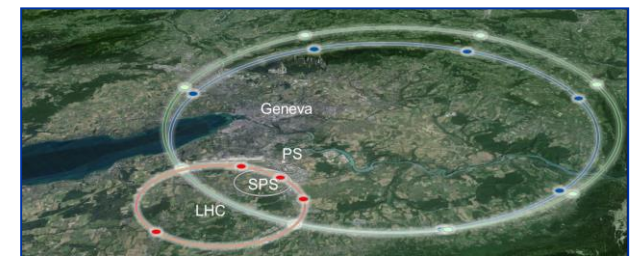
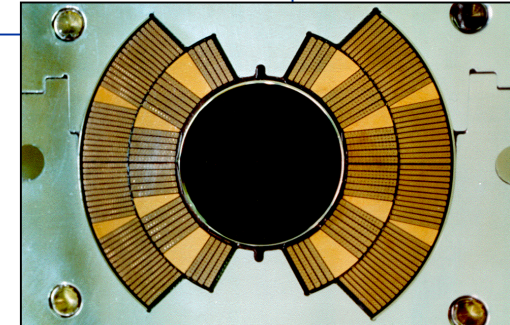
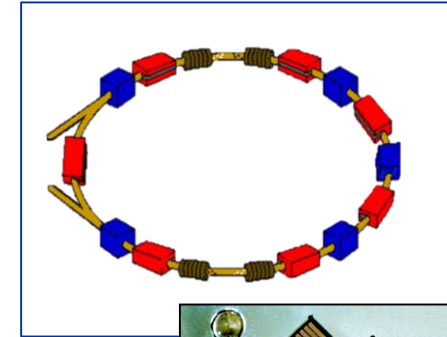
Hélène Felice

with material borrowed from P. Ferracin, E. Todesco, L. Bottura , A Devred

18/07/2022

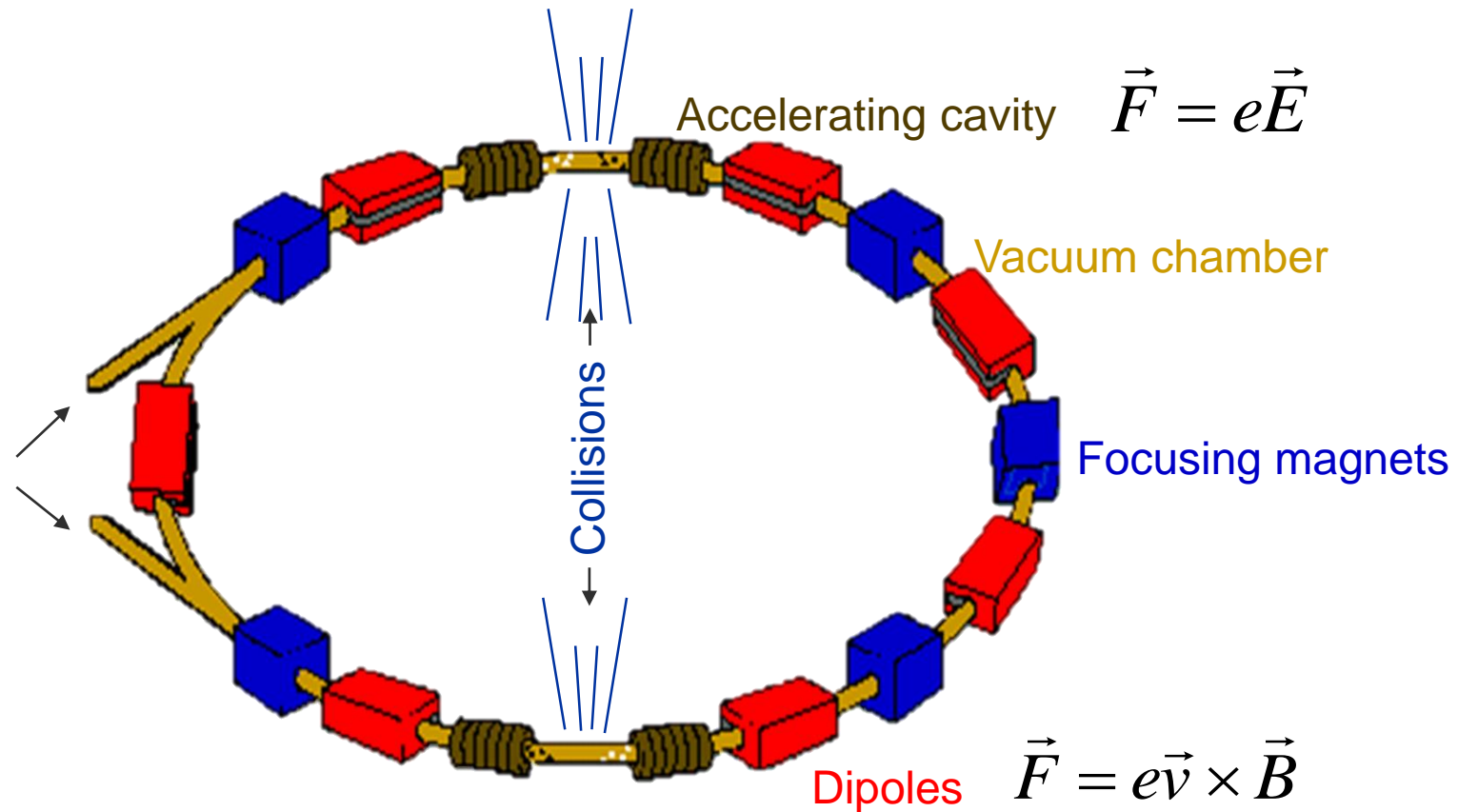
Context and Goals of the lecture

- Why do we need magnets in accelerators?
- Why do we need **Superconducting** Magnets and what is **superconductivity**?
- How do we **design** and build magnets? From the conductor to the full magnet using well known **Low Temperature Superconductors**
- Which magnets for HL-LHC?
- Beyond HL-LHC? Many challenges ahead...



Why do we need magnets in accelerators?

- Electrical field accelerates particles
- **Magnetic field** steers the particles in a closed (circular) orbit to drive particles through the same accelerating structure several times



Dipole role and relation to beam energy

$$p = eBr$$

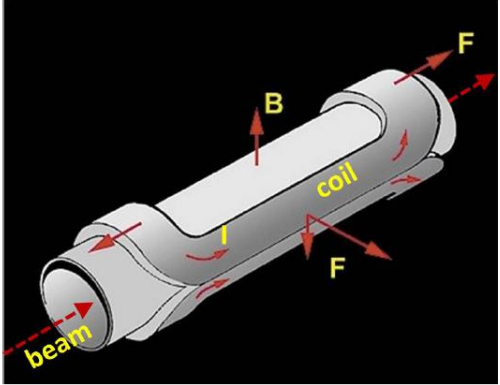
$$E[GeV] = 0.3 \times B[T] \times \rho[m]$$

- Relation between *magnetic induction* (commonly called *Field in our business*) B , curvature radius ρ and momentum p
- Particle accelerated \rightarrow energy increased \rightarrow magnetic field increased (“**synchro**”) to keep the particles on the same orbit of curvature

LHC example: curvature radius is 2800 m, field is 8.3 T, energy is 7000 GeV (i.e. 7 TeV)

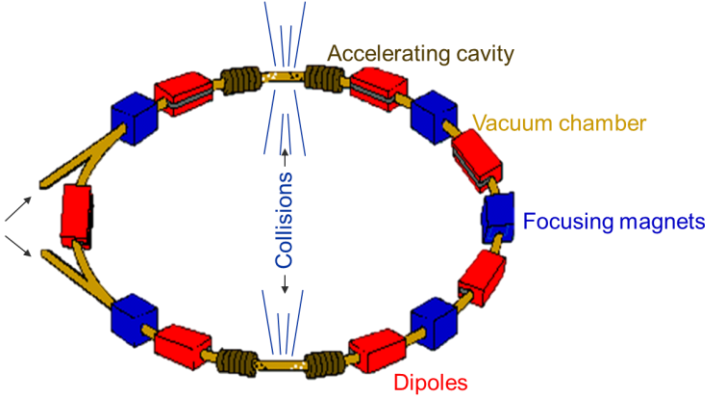
$$E[GeV] = 0.3 \cdot 8.3 \cdot 2800 = 7000$$

Dipoles in a nutshell

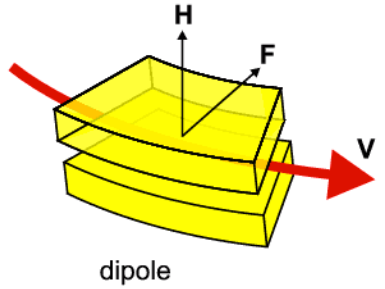
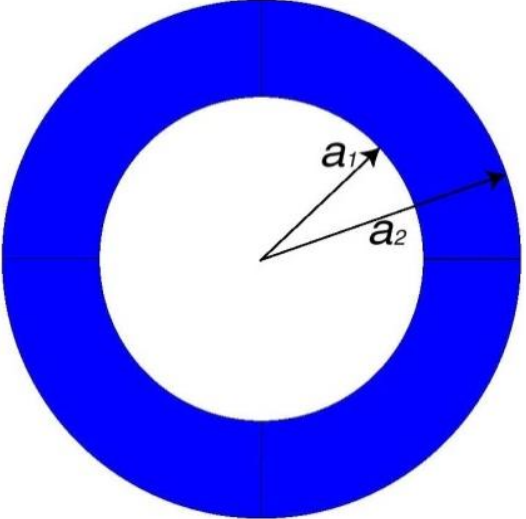


Vertical magnetic induction B_y in T produced by a current Density $J_0 \cos\theta$ (A/mm²) with a_1/a_2 inner/outer radius

$$B_y = -\frac{\mu_0 J_0}{2} (a_2 - a_1)$$



$$p = eBr$$



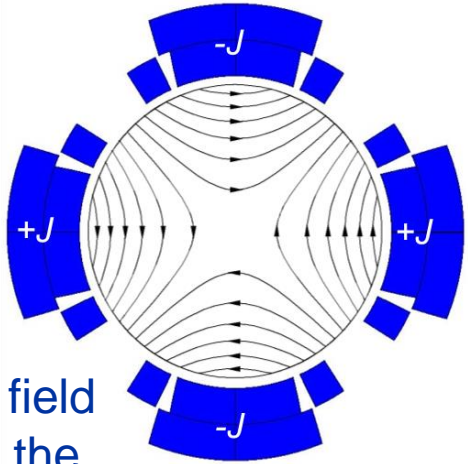
In dipoles, the larger B, the larger the steering strength

Quadrupoles in a nutshell

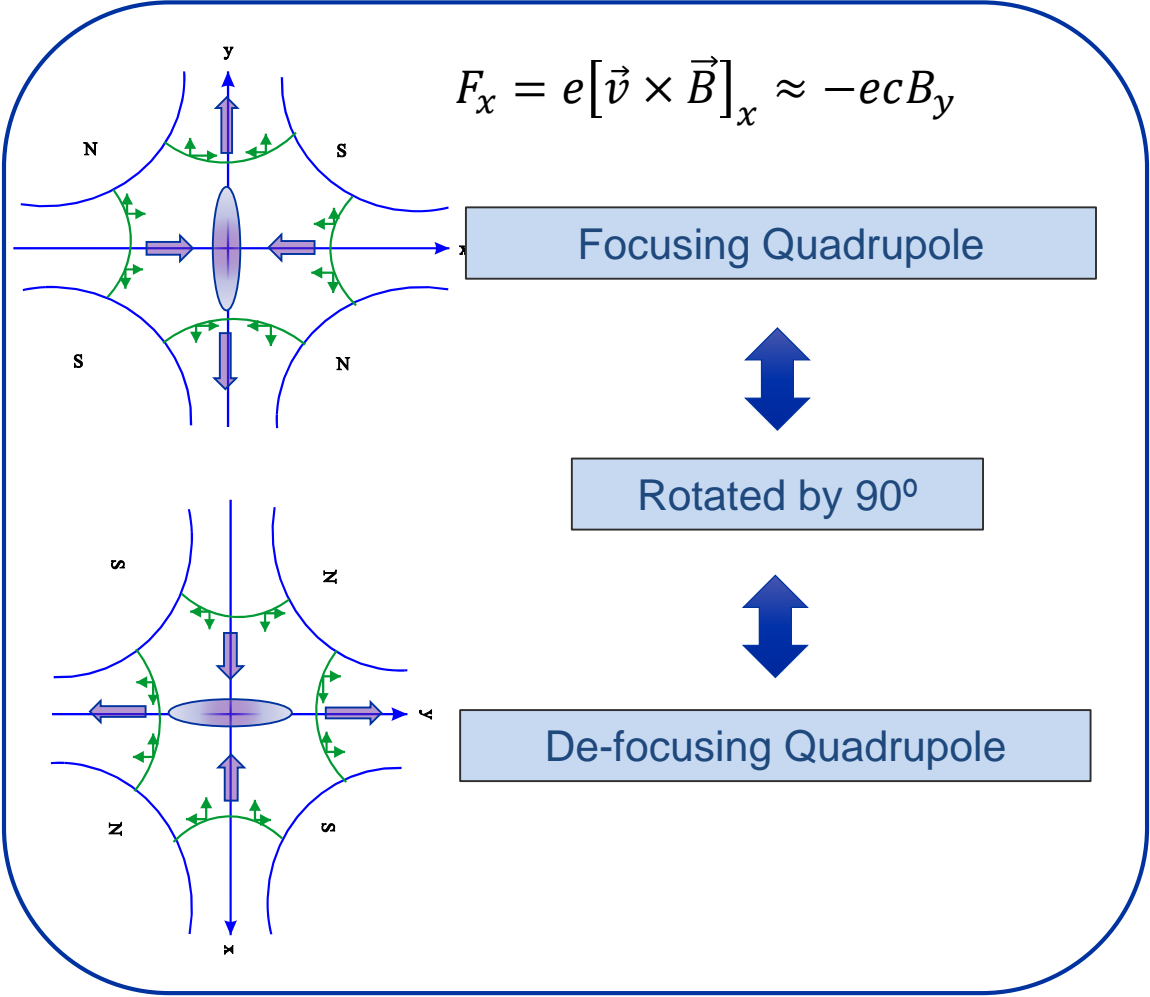
The quadrupoles focus the beam

They provide a field equal to zero in the center increasing linearly with the radius – Gradient G

$$G = \frac{B_y}{r} = -\frac{\mu_0 J_0}{2} \ln \frac{r_{out}}{r_{in}}$$



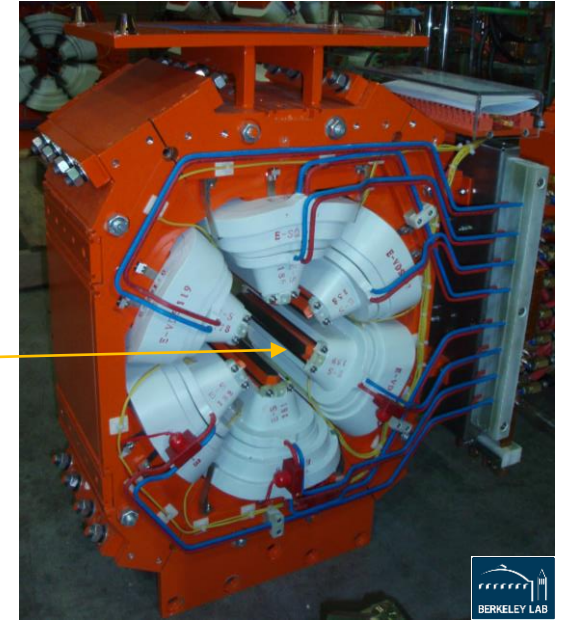
$$\begin{cases} B_y = Gx \\ B_x = Gy \end{cases}$$
 Quadrupoles provide a field which is proportional to the transverse deviation from the orbit, acting like a spring



In quads, the larger B, the larger the focusing strength

What about copper conductor?

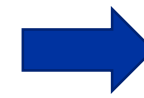
- The greater the current density J , the greater the magnetic field
- Copper can typically transport 5 to 15 A/mm² when properly cooled
- Normal conducting magnets for accelerators are made with a copper winding around a **ferromagnetic core** that greatly enhances the field
 - The shape of the pole gives the field homogeneity
 - field limited to the iron saturation around 2T
- A large number of accelerators in the world are made with **normal conducting magnets** (Cu conductor) also called **warm magnets**



- A few examples of light sources

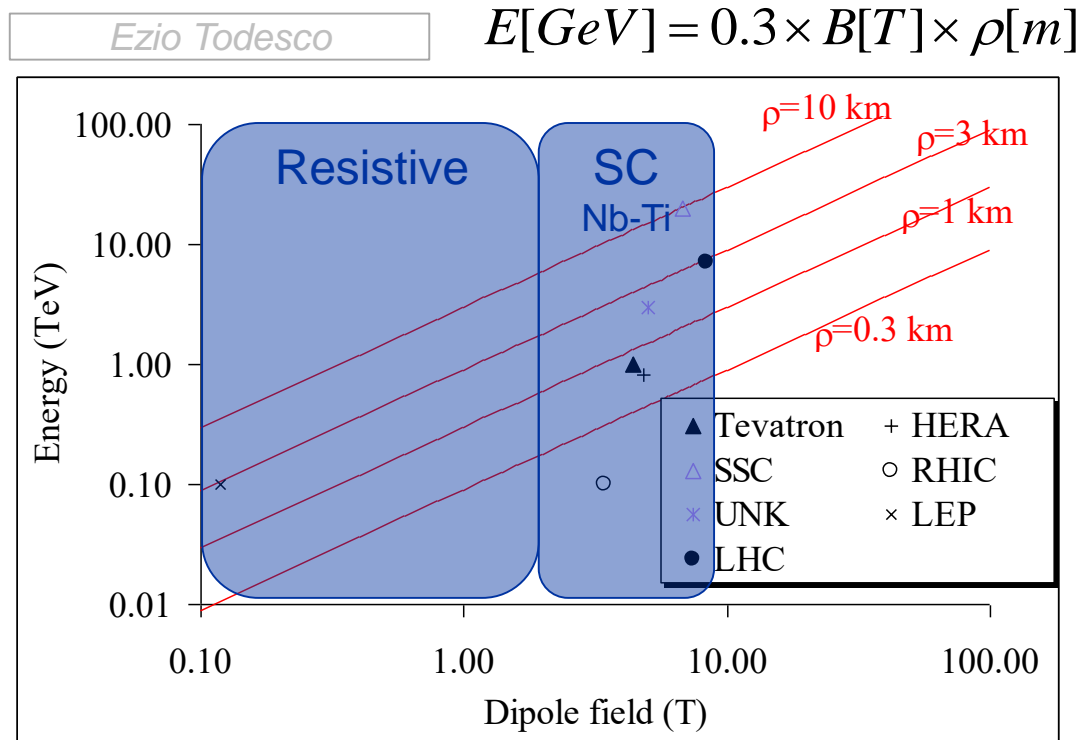


Beyond Copper conductor



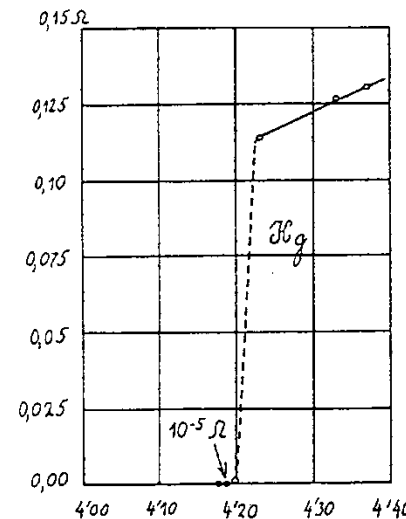
Superconductors

- LHC with 2 T would be 100 km long...
- Having 8 T magnets, we need 3 Km curvature radius to have 7 TeV
- If we had 800 T magnets, 30 m would be enough ...



In 1911, Kamerlingh Onnes discovered the **superconductivity of mercury**

- Below 4.2 K, mercury has a non measurable electric resistance => potential to transport very high current and to produce very high field
- Discovery thanks his success in **liquifying Helium** in 1908



4.2 K is called the **critical temperature Tc**:

For $T < T_c$ the material is superconducting

Superconductivity in a nutshell: discovery

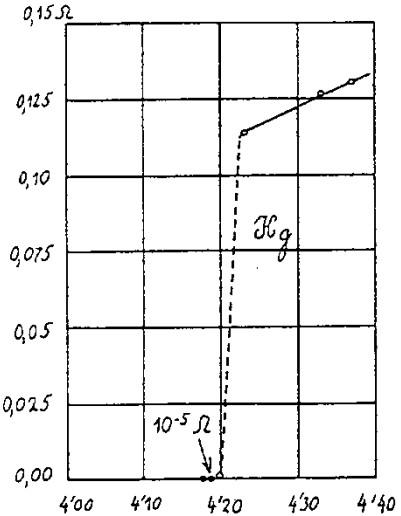


1911

40's – 80's

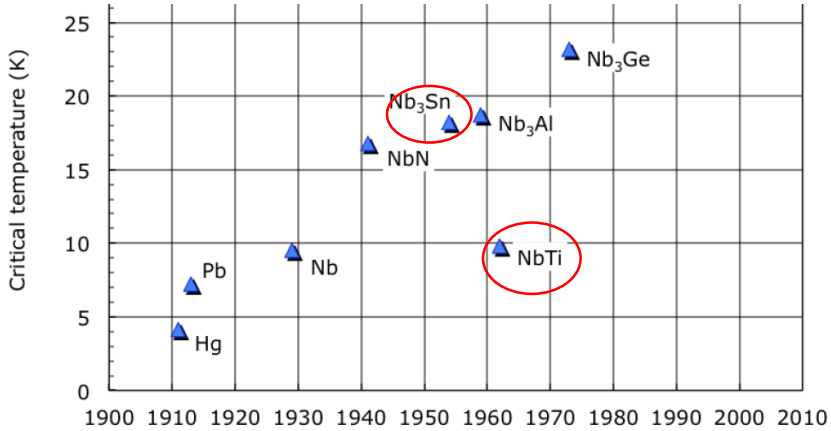
1986

LTS Low Temperature superconductors



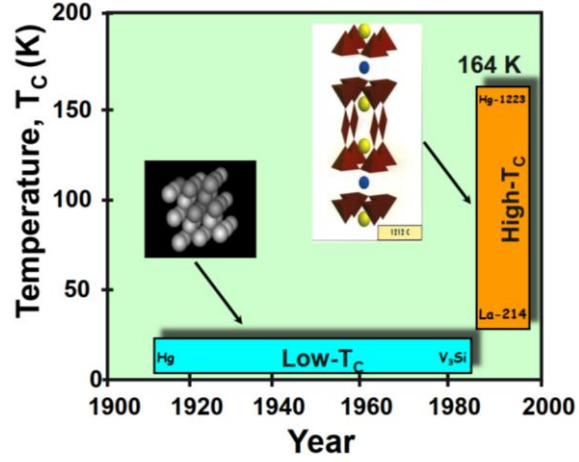
... thus the mercury at 4.2 K has entered a new state, which, owing to its particular electrical properties, can be called the state of *superconductivity*...

H. Kamerlingh-Onnes (1911)



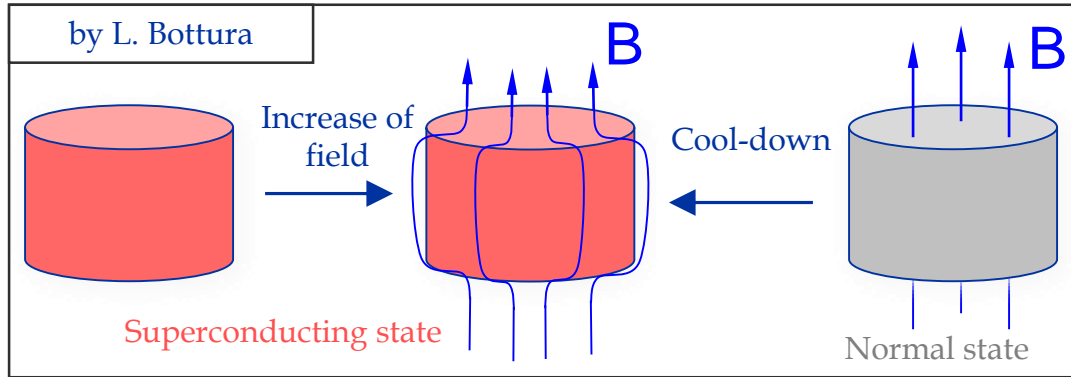
Theoretical limit around 30 K

HTS High Temperature superconductors



1987 – Nobel Prize to Bernorz and Mueller for the discovery of superconductivity in ceramic material

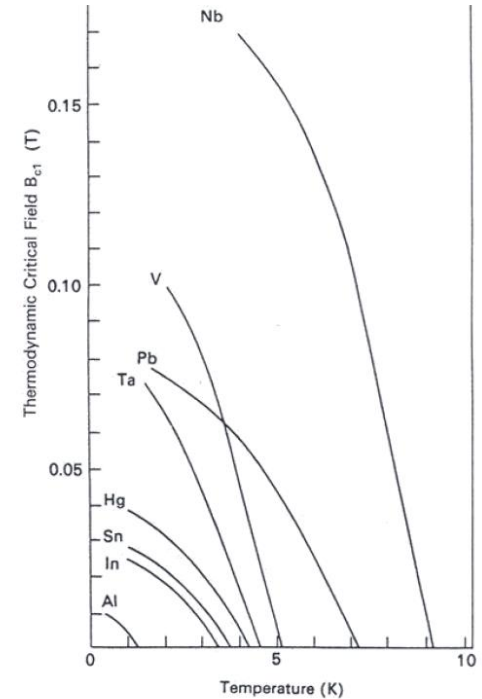
Type I superconductors



The first superconductor material demonstrate a complete field exclusion called Meissner-Ochsenfeld effect (1933)

It behaves as a perfect diamagnetic material

- for $T < T_c$
- B must be $< B_c$ called **critical field**
- If we look closely, the field penetrates over a tiny depth (~ 10 nm) called **London penetration depth λ_L**

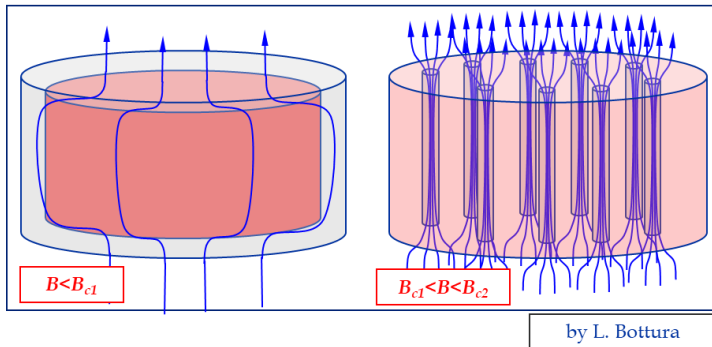


B_c is very small a few mT to barely above 100 mT

Not useful for Magnet engineers

Type II superconductors

In the 50's, discovery of a new type of superconductor
 For $B < B_{c1}$ => behaves like a type I superconductor
 For $B_{c1} < B < B_{c2}$ => **Mixed state**



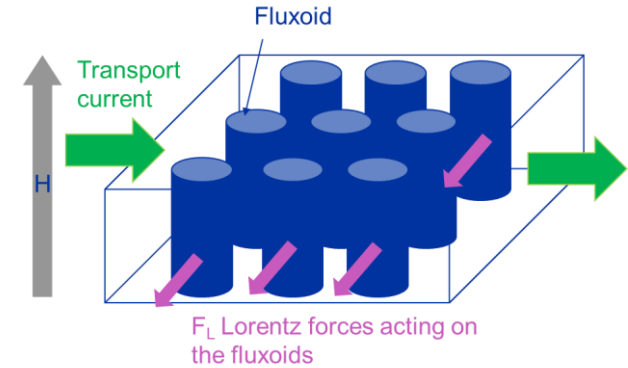
For $B_{c1} < B < B_{c2}$
 Penetration of the field as quantum of flux Φ_0 called **fluxoids**

$$\Phi_0 = h/2e = 2.07 \times 10^{-15} \text{ Wb}$$

The core of the vortex is normal conducting and is of radius ξ
 Super current are developing around each core over the London depth λ_L
 For Type II superconductor $\xi < \lambda_L$

A Lorentz force is acting on the fluxoid when a transport current flows in the SC: $F_L = J \times B$

If the fluxoids are not anchored: flux flow regime => energy dissipation (dB/dt) => loss of superconductivity

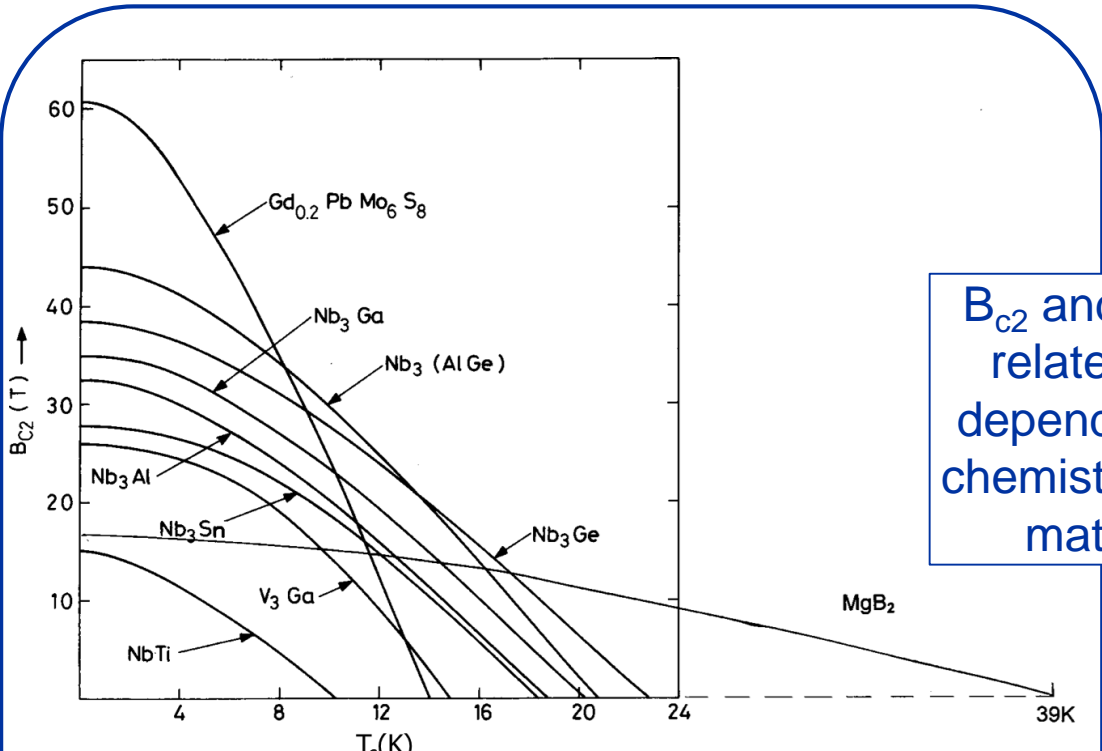


Necessity to pin the fluxoids using defect and imperfections of the material => **pinning centers** exerting a **pinning force F_p**

As long as $F_L \leq F_p$ the superconductor can carry transport current

J_c is the critical current density at which, for a given B and at a given T we have $F_p \leq F_L$

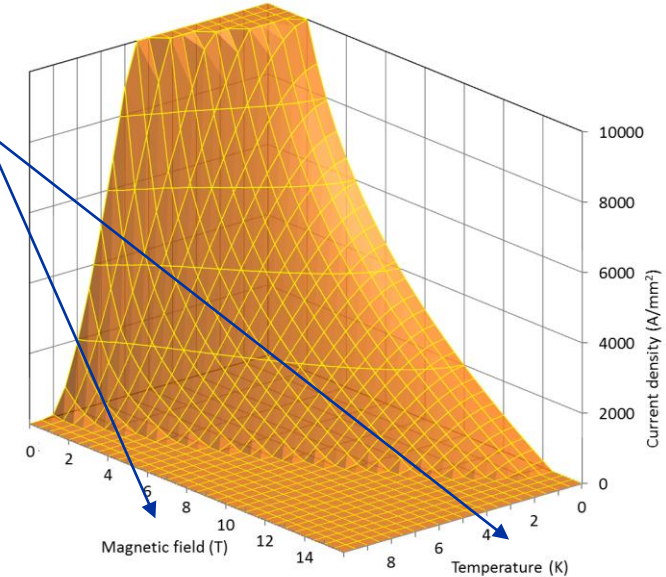
Concept of critical surface



B_{c2} and T_c are related and depend on the chemistry of the material

Important remark for magnet engineers:
Of all the metallic superconductors, only NbTi which is an alloy is ductile.
All other are brittle inter-metallic compounds

We have now 3 parameters: J_c , B_{c2} and T_c allowing to define the **critical surface** of practical superconductors - beyond: resistive state



High J_c obtained with the optimization of the conductor layout by the manufacturer

This is a dedicated field of R&D

When we talk about J_c we always specify at which field and which temperature (same for other parameters)

In summary – from Luca Bottura

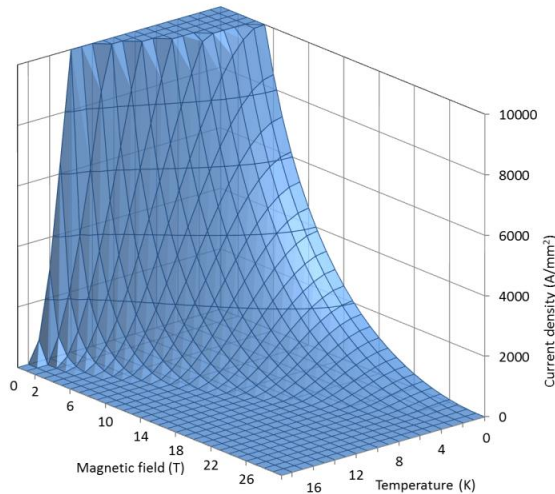
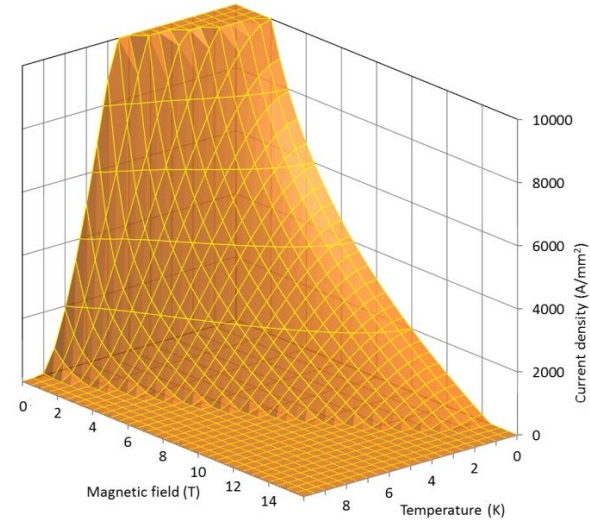
Superconductors – the bottom line

- Superconducting materials are only useful if they are **dirty** (type II - high critical field) and **messy** (strong pinning centers)
- A superconductor is such only in conditions of temperature, field and current density within the critical surface, and it is a normal-conductor above these conditions. The transition is defined by a **critical current density $J_C(B, T, \dots)$**
- The maximum current that can be carried is the **$I_C = A_{SC} \times J_C$**

Practical superconductors: NbTi and Nb₃Sn

Nb and Ti → NbTi ductile alloy

- Obtained by Extrusion + drawing
- T_c is ~ **9.2 K** at 0 T
- B_{c2} is ~ **14.5 T** at 0 K
- Firstly used in **Tevatron** (80s), then in all the other
- 1 euro per m

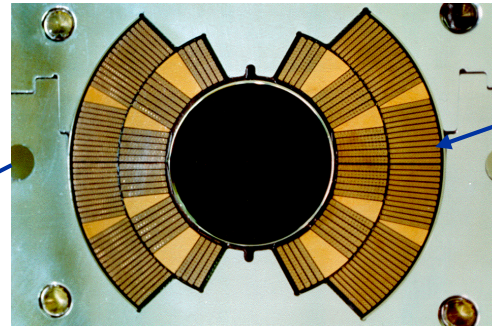
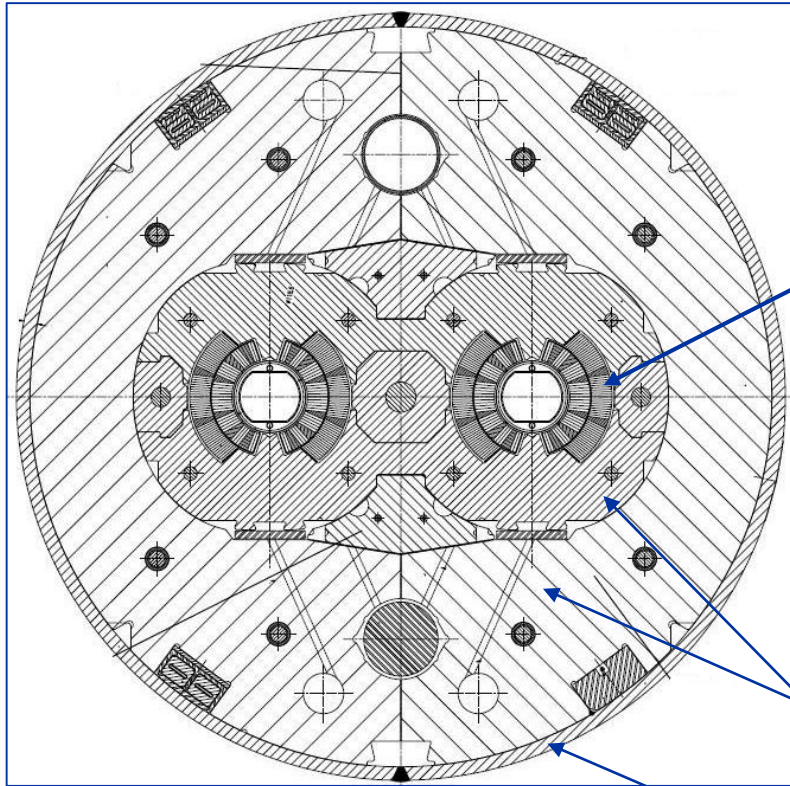


Nb and Sn → Nb₃Sn intermetallic compound

- Brittle, strain sensitive, formed at ~650°C
- T_c is ~ **18 K** at 0 T
- B_{c2} is ~ **28 T** at 0 K
- Used in **ITER**
- 5 euro per m

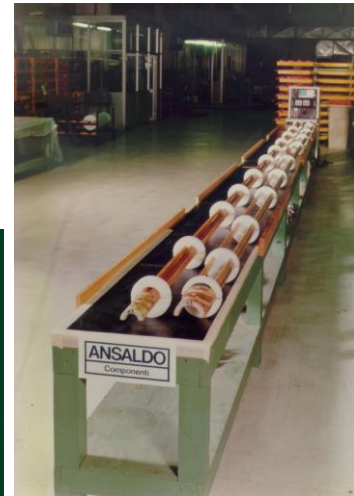
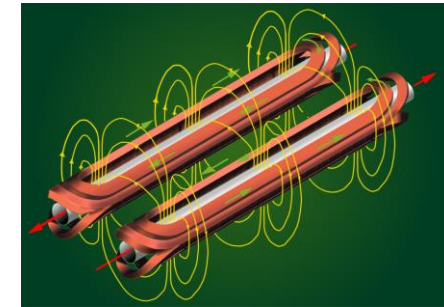
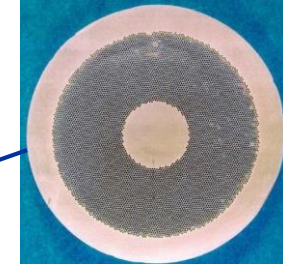
Practically, what are we talking about when we talk about accelerator magnets? A few key components

LHC Dipole



Coil cross-section

SC strand/wire



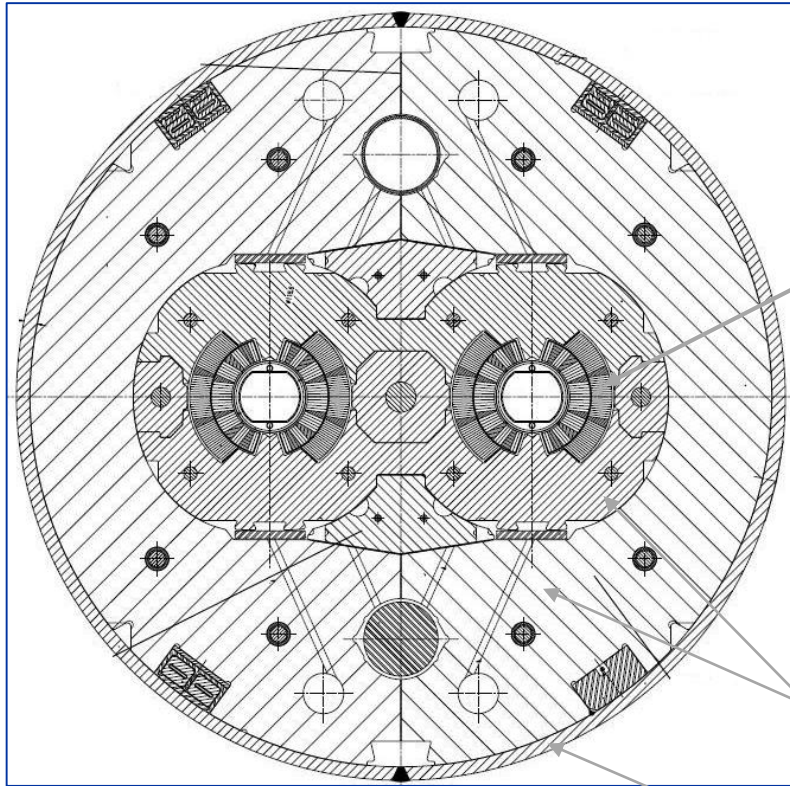
Coils

Mechanical Support structure

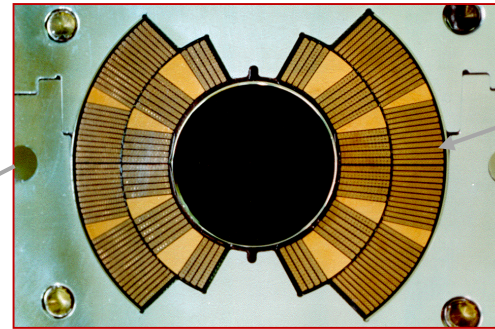
Helium Vessel

Practically, what are we talking about when we talk about accelerator magnets? A few key components

LHC Dipole

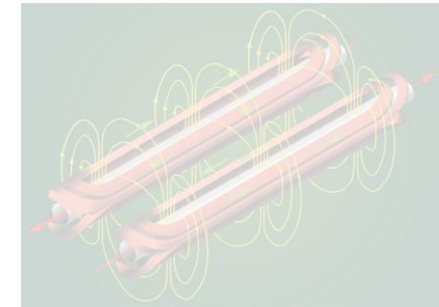
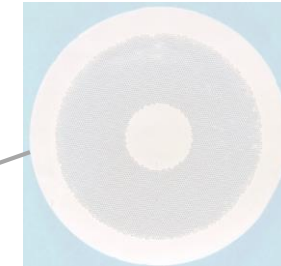


Let's start with the heart of the magnet: the coil



Coil cross-section

SC strand



Coils

Mechanical Support structure

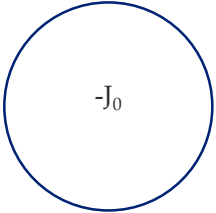
Helium Vessel

How and why do we get this strange cross-section?

Ideal dipole Field # 1: Intersecting Ellipses/Circles

Within a cylinder carrying \mathbf{j}_0 , perpendicular to the plane of the slide, the field is perpendicular to the radial direction and proportional to the distance to the centre r

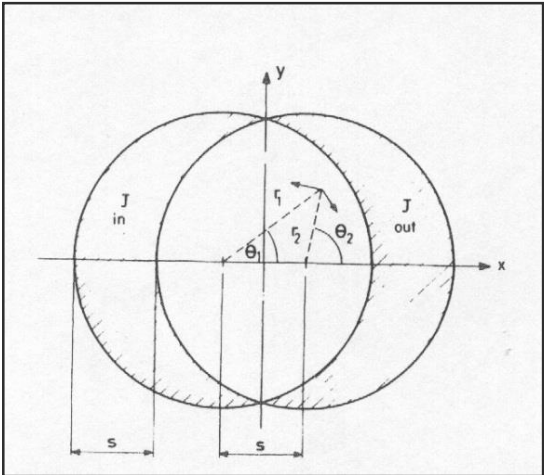
$$B = -\frac{\mu_0 j_0 r}{2}$$



Combining the effect of two intersecting cylinders

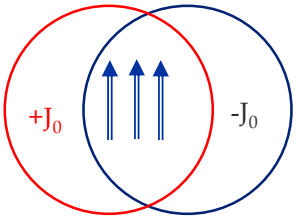
$$B_x = \frac{\mu_0 j_0 r}{2} \{-r_1 \sin \theta_1 + r_2 \sin \theta_2\} = 0$$

$$B_y = \frac{\mu_0 j_0 r}{2} \{-r_1 \cos \theta_1 + r_2 \cos \theta_2\} = -\frac{\mu_0 j_0}{2} s$$

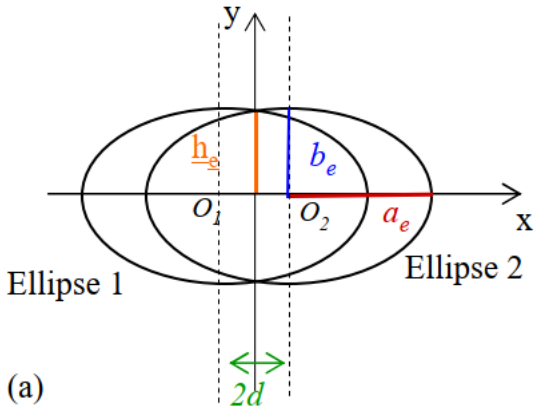


by M. Wilson

A uniform current density in the area of two **intersecting circles** produces a pure dipole



A little harder work to demonstrate similar conclusion for **intersecting ellipses**



$$\overline{B_{ellipse}} = \mu_0 J \frac{2b_e d}{a_e + b_e}$$

docnum.univ-lorraine.fr/public/INPL/2006_FELICE_H.pdf

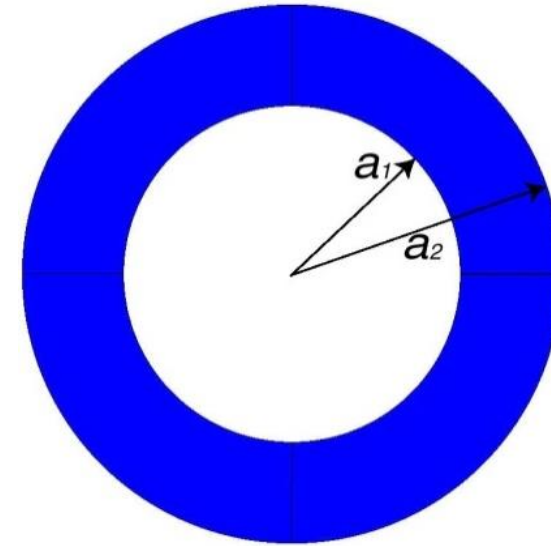
Ideal dipole Field #2: Current density distribution in $\cos\theta$

If we assume

- $J = J_0 \cos\theta$ where J_0 [A/m²] is \perp to the cross-section plane
- Inner (outer) radius of the coils = a_1 (a_2)

The generated field is a **pure dipole**

$$B_y = -\frac{\mu_0 J_0}{2} (a_2 - a_1)$$

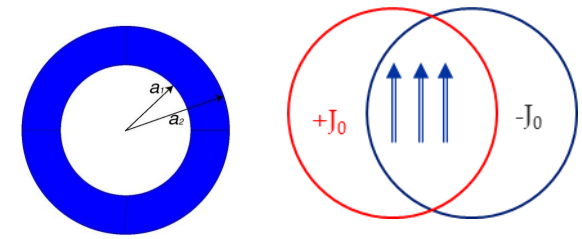


$B \propto$ current density

$B \propto$ coil width $w = a_2 - a_1$

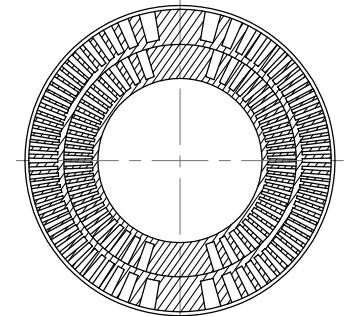
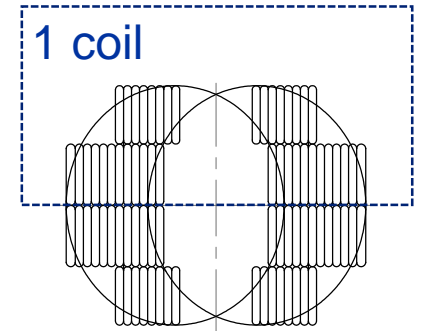
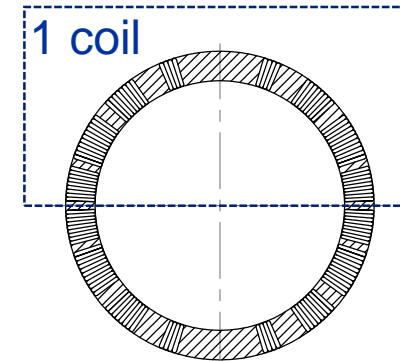
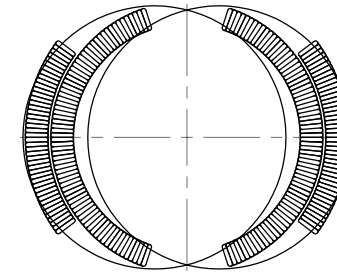
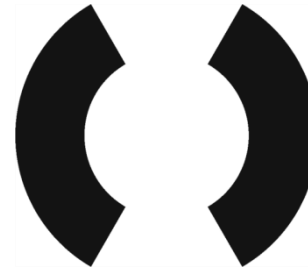
B is independent of the aperture r (not so obvious)

From ideal dipole to practical magnetic configuration



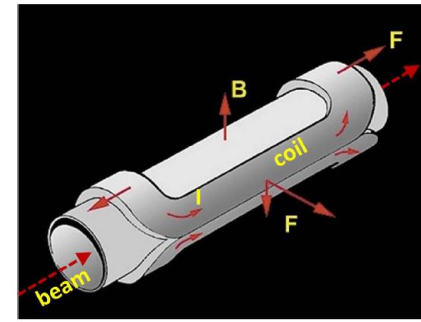
Approximation of ideal shapes

- Sector stacking of conductor
- Block approach
- Sector with wedges



Consequence: the dipole field has some imperfections
How do we assess them and how we deal with them?

Let's start with the 2D field representation: complex formalism



x and y perpendicular to the beam (transverse coordinates), z along the beam

Flux conservation – Maxwell Gauss

$$\nabla \cdot \mathbf{B} = \frac{\partial B_x}{\partial x} + \frac{\partial B_y}{\partial y} + \frac{\partial B_z}{\partial z} = 0$$

In presence of a constant axial field (here = 0)

$$\frac{\partial B_z}{\partial z} = 0$$

$$\frac{\partial B_x}{\partial x} + \frac{\partial B_y}{\partial y} = 0$$

Maxwell Ampere's law

$$\nabla \times \mathbf{B} = \mu_0 \mathbf{J} + \mu_0 \epsilon_0 \frac{\partial \mathbf{E}}{\partial t}$$

In absence of current and varying electrical field

$$\nabla \times \mathbf{B} = \left(\frac{\partial B_y}{\partial z} - \frac{\partial B_z}{\partial y}, \frac{\partial B_z}{\partial x} - \frac{\partial B_x}{\partial z}, \frac{\partial B_x}{\partial y} - \frac{\partial B_y}{\partial x} \right) = 0$$

$$\frac{\partial B_x}{\partial y} - \frac{\partial B_y}{\partial x} = 0$$

Cauchy Riemann conditions

$$\begin{cases} \frac{\partial f_x}{\partial x} - \frac{\partial f_y}{\partial y} = 0 \\ \frac{\partial f_x}{\partial y} + \frac{\partial f_y}{\partial x} = 0 \end{cases}$$

\mathbf{B} can be written as an analytic function

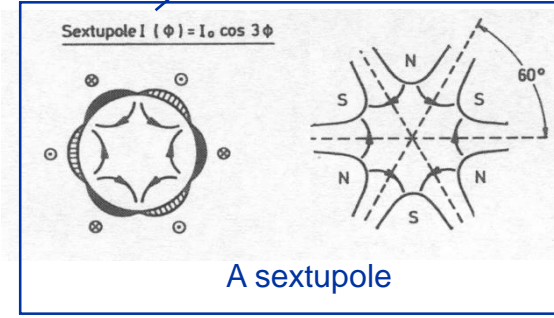
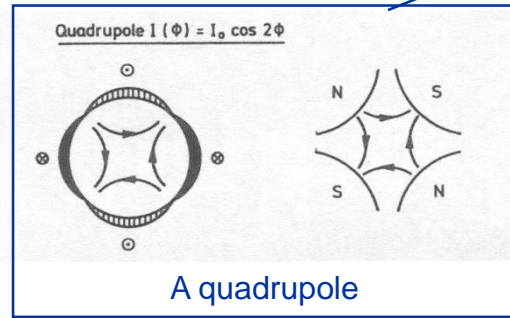
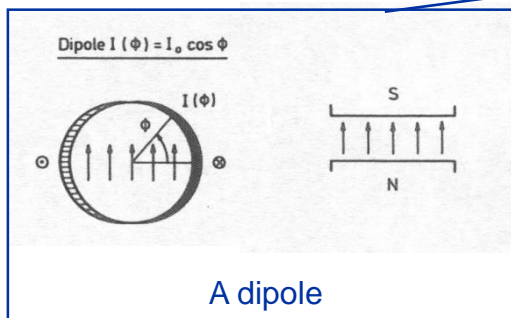
$$B_y(x, y) + iB_x(x, y)$$

Definition of field harmonics in 2D

\mathbf{B} as an analytic function can be expressed as a series expansion with (x,y) in domain D (aperture of the magnet)

$$B_y(x, y) + iB_x(x, y) = \sum_{n=1}^{\infty} C_n (x + iy)^{n-1} = \sum_{n=1}^{\infty} (B_n + iA_n) (x + iy)^{n-1}$$

$$B_y(x, y) + iB_x(x, y) = \sum_{n=1}^{\infty} C_n (x + iy)^{n-1} = C_1 + C_2(x + iy) + \dots$$



from P. Schmuser et al, pg. 50

Each coefficient corresponds to a “pure” multipolar field

Definition of field harmonics in 2D

$$B_y(x, y) + iB_x(x, y) = \sum_{n=1}^{\infty} C_n (x + iy)^{n-1} = \sum_{n=1}^{\infty} (B_n + iA_n) (x + iy)^{n-1}$$

The field harmonics are rewritten as (EU notation)

$$B_y + iB_x = 10^{-4} B_1 \sum_{n=1}^{\infty} (b_n + ia_n) \left(\frac{x + iy}{R_{ref}} \right)^{n-1}$$

We **factorize** 10^{-4} since the deviations from ideal field are $\sim 0.01\%$

Factorization of **the main component** (B_1 for dipoles, B_2 for quadrupoles)

Reference radius R_{ref} to have dimensionless coefficients

The coefficients b_n, a_n are called **normalized multipoles**: b_n are the normal, a_n are the skew (adimensional)

!! US notation is different from EU notation $b_2^{US} = b_3^{EU}$

Now that we have the tools: how do we go from ideal to practical coil cross sections?

For symmetry reasons only certain harmonics are «allowed»

In a dipole B_{2n+1} are allowed: B_3, B_5, \dots

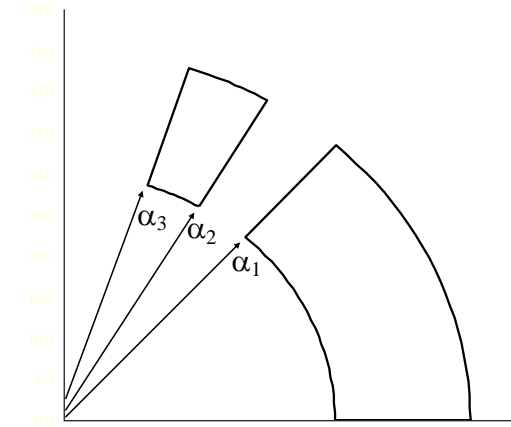
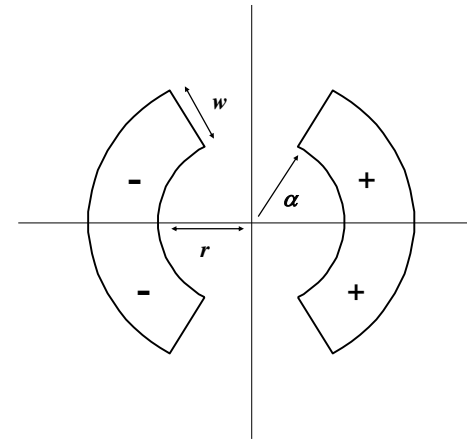
Multipoles for a sector coil can be expressed for $n > 2$

$$B_n = -\frac{j\mu_0 R_{ref}^{n-1}}{\pi} \frac{2 \sin(\alpha n)}{n} \frac{(r+w)^{2-n} - r^{2-n}}{2-n}$$

Multipoles can be made equal to zero

$$B_3 = \frac{\mu_0 j R_{ref}^2}{\pi} \frac{\sin 3\alpha_3 - \sin 3\alpha_2 + \sin 3\alpha_1}{3} \left(\frac{1}{r} - \frac{1}{r+w} \right)$$

$$B_5 = \frac{\mu_0 j R_{ref}^4}{\pi} \frac{\sin 5\alpha_3 - \sin 5\alpha_2 + \sin 5\alpha_1}{5} \left(\frac{1}{r^3} - \frac{1}{(r+w)^3} \right)$$

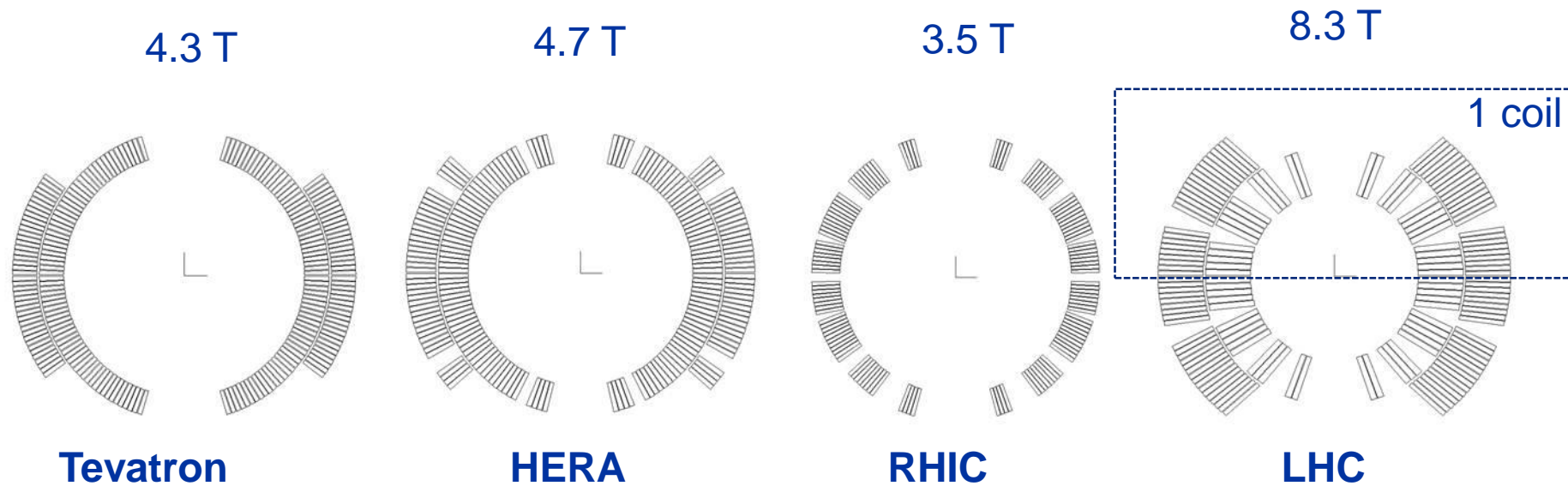


Equations to set to zero B_3 and B_5

$$\begin{cases} \sin(3\alpha_3) - \sin(3\alpha_2) + \sin(3\alpha_1) = 0 \\ \sin(5\alpha_3) - \sin(5\alpha_2) + \sin(5\alpha_1) = 0 \end{cases}$$

$(48^\circ, 60^\circ, 72^\circ)$ or $(36^\circ, 44^\circ, 64^\circ)$ are solutions

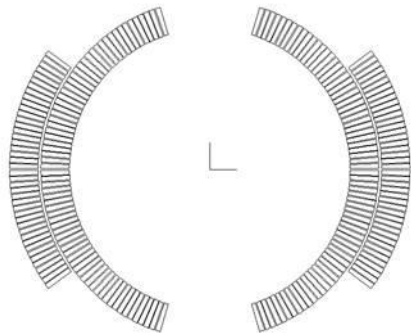
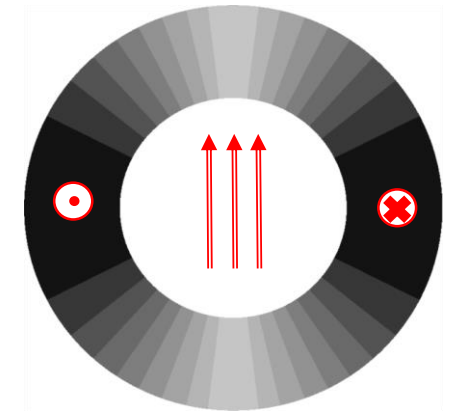
Coil cross sections (to scale) of the four superconducting colliders



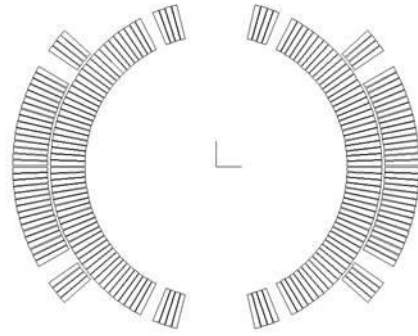
	Nominal		
	Temp. (K)	Field (T)	Margin
Tevatron	4.6	4.3	4%
Hera	4.6	4.7	23%
RHIC	4.5	3.5	30%
LHC	1.9	8.3	14%

Increased coil complexity (nested layers, wedges and coil blocks) to achieve higher efficiency and improved field homogeneity

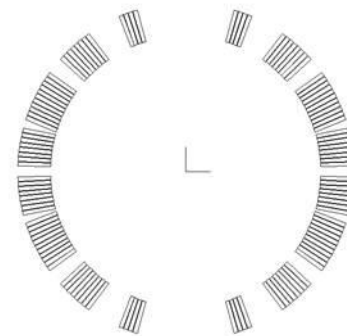
Coil cross sections (to scale) of the four superconducting colliders



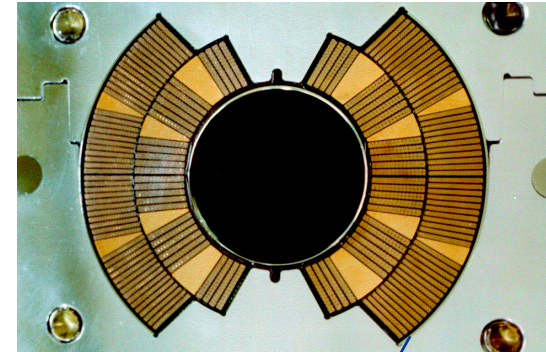
Tevatron



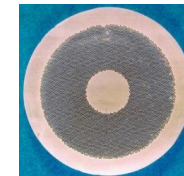
HERA



RHIC



LHC



strand

cable

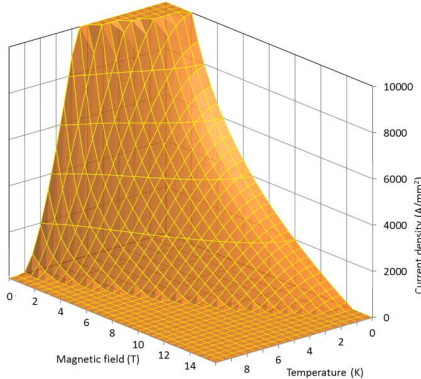


Now that we know how to design magnetically a cross-section, let's take a look at the conductor itself

Practical superconductors: strand

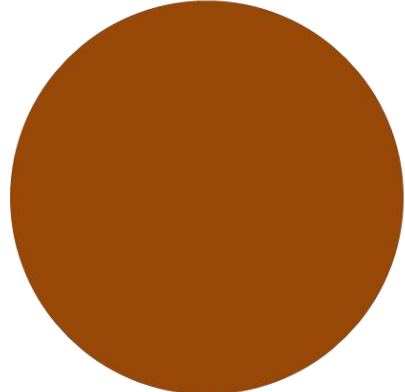
Focus on LTS since all existing accelerator magnets are made of LTS so far

A word on HTS tomorrow



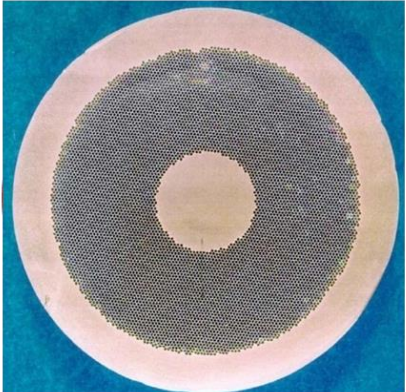
LTS STRANDS

Cu



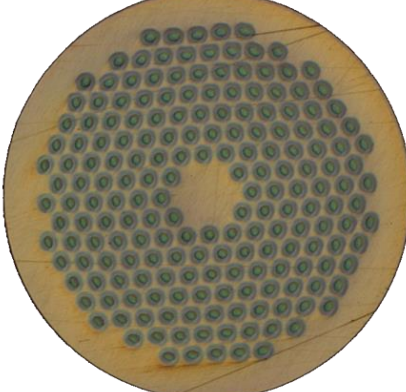
$J_e \sim 5 \text{ A/mm}^2$
 $I \sim 3 \text{ A}$
 $B = 2 \text{ T}$

Nb-Ti



$J_e \sim 600-700 \text{ A/mm}^2$
 $I \sim 300-400 \text{ A}$
 $B = 8-9 \text{ T}$

Nb₃Sn

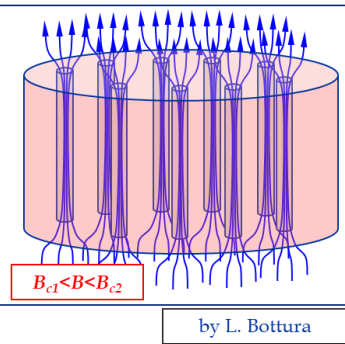


$J_e \sim 600-700 \text{ A/mm}^2$
 $I \sim 300-400 \text{ A}$
 $B = 12-16 \text{ T}$



- Multifilamentary structure: Why?
- Presence of Cu: Why?
- Any other detail?

Multi-filamentary wire: fighting flux jumps



Let's remember that in a Type II superconductor submitted to an external magnetic field, the flux penetrates by quantum of flux called fluxoids

If the superconductor is subjected to a thermal disturbance, J_c will change

Thermal disturbance $\Rightarrow dJ_c/dt \Rightarrow dB/dt \Rightarrow E$ electrical field $\Rightarrow E \cdot J_c$ power dissipation

Reorganization of fluxoids called **flux jump**

Some criteria exist to evaluate the critical size of the superconductor

In the case of a slab of superconductor of thickness $2a$, according to the adiabatic criteria, the half size of the slab should be

$$a \leq \sqrt{\frac{3\gamma C(\theta_c - \theta_0)}{\mu_0 j_c^2}}$$

where j_c is the critical current density [$A m^{-2}$], γ is the density [$kg m^{-3}$], C is the specific heat [$J kg^{-1}$], and θ_c is the critical temperature.

- \Rightarrow **The higher J_c , the higher risk of flux jump (low field)**
- \Rightarrow **Incentive to reduce the SC filament size $< 50 \mu m$**

Multi-filamentary wire: dealing with magnetization

The current distribution in a Type II superconductor is given by the **Bean Critical state** (1962)

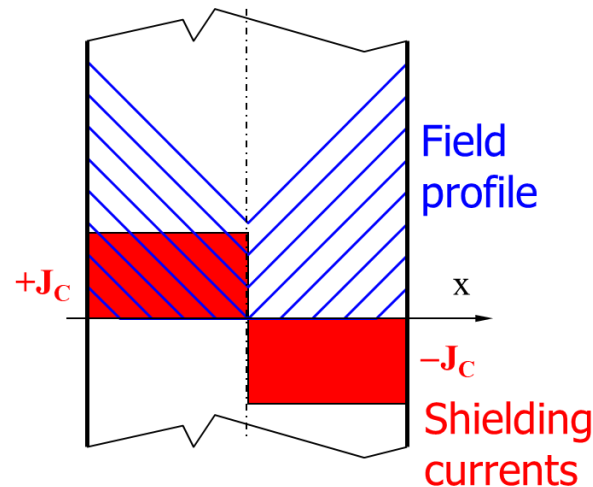
The local current density is either null or equal to J_c

When a filament is in a varying B_{ext} , shielding currents are developing starting from the outer surface of the filament.

Based on Bean's model, the current density is J_c

They **do not decay** when B_{ex} is held constant

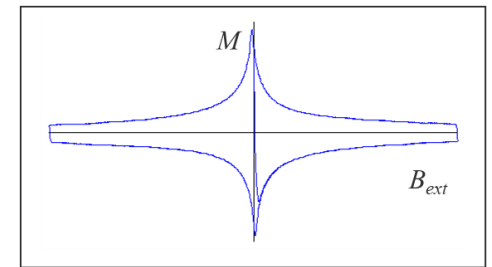
→ Shielding / persistent currents



The shielding currents are producing a magnetic moment

A **magnetization** can be defined and causes:

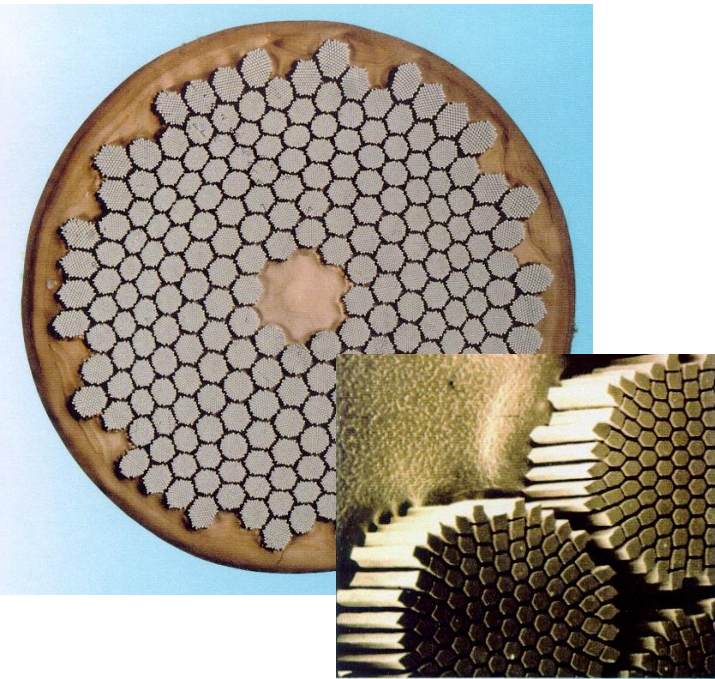
- Field distortion
- losses



This magnetization is proportional to J_c and to the filament size

⇒ **Incentive to reduce the SC filament size as much as possible (6-7 μm in LHC)**

Multifilament wire: inter-filament coupling



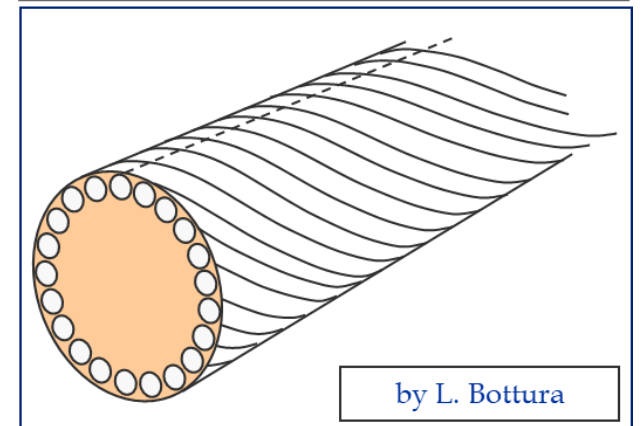
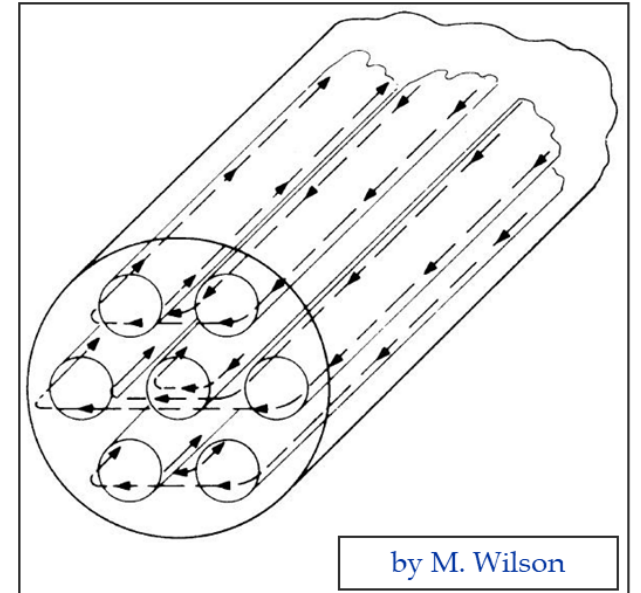
Wire composed of very small filaments

When a multi-filamentary wire is subjected to a time varying magnetic field, **current loops** are generated between filaments => **inter-filament coupling**

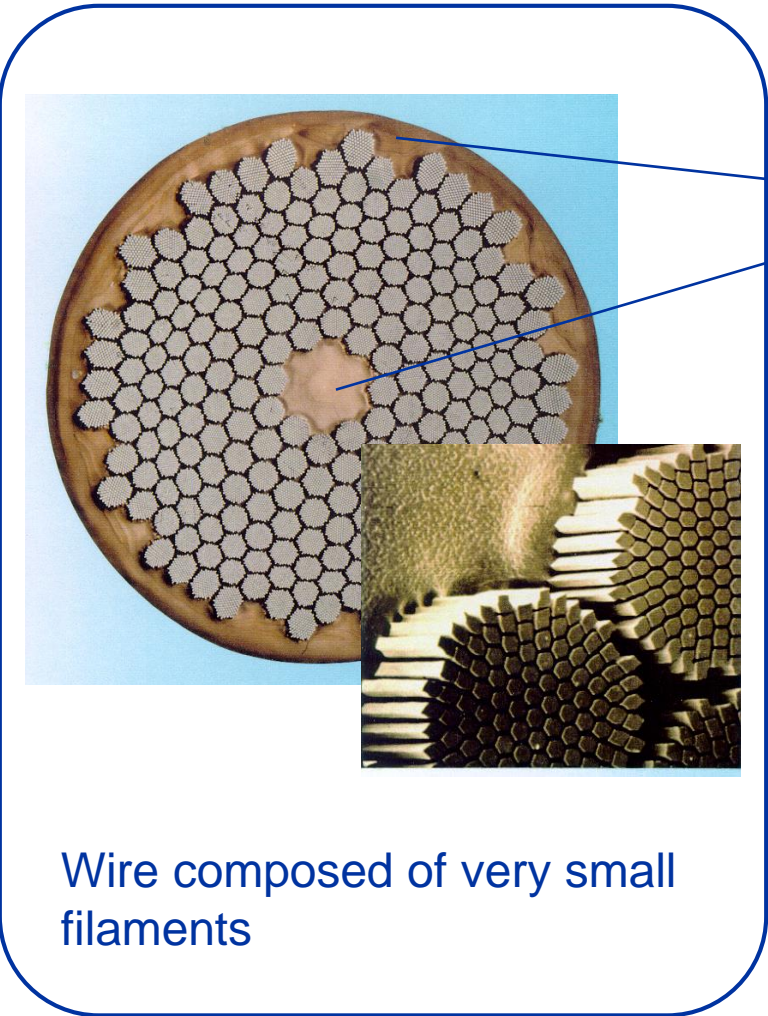
- If filaments are straight, large loops with large currents → **ac losses**
- If the strands are magnetically coupled the **effective filament size** is larger → **flux jumps**

To reduce these effects, filaments are **twisted**

- twist pitch of the order of 20-30 times of the wire diameter.



Multifilament wire: presence of a stabilizer (Cu)

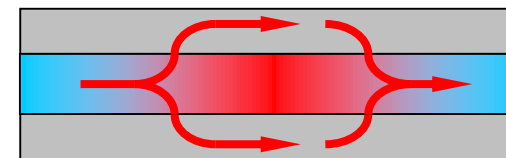


When $T > T_c$, the resistivity of superconducting materials (in normal state) is very high

$$\rho_{\text{NbTi},n} \sim 5 \cdot 10^{-7} \text{ } \Omega \cdot \text{m} \text{ whereas } \rho_{\text{Cu}} \sim 1.7 \cdot 10^{-8} \text{ } \Omega \cdot \text{m}$$

If the SC becomes normal, its temperature will rise very quickly (ms) by Joule heating

Embedding the SC in a **low resistivity matrix** such as copper, allows the current to flow in the matrix in case of quench (transition to normal state)

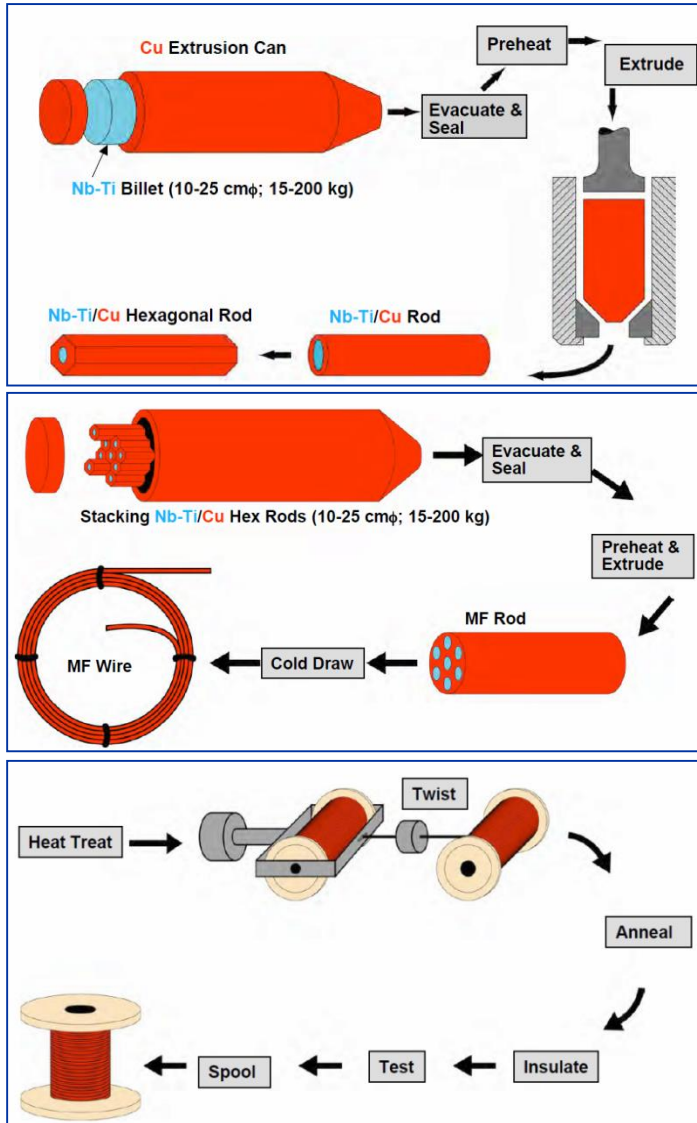


by L. Bottura

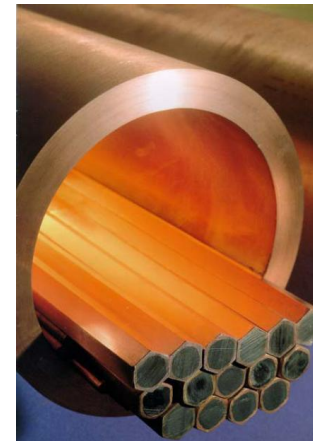
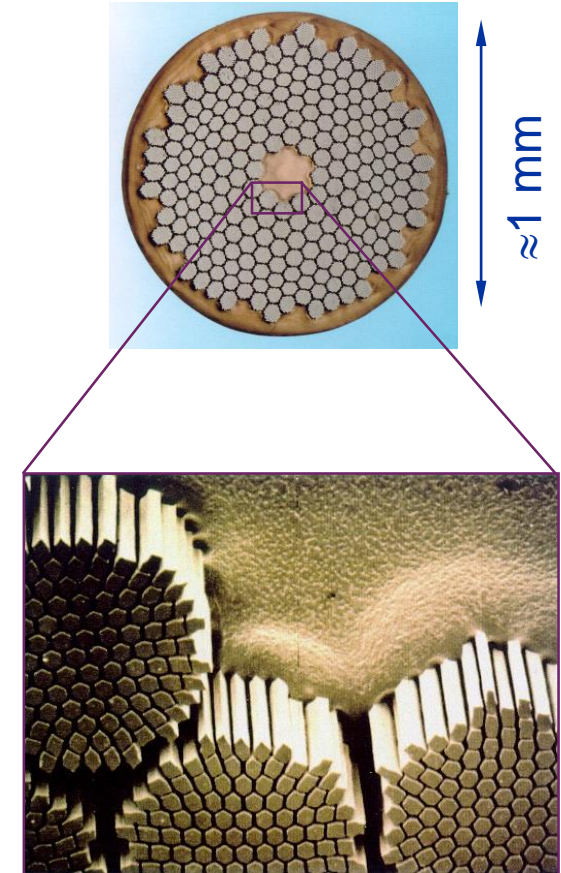
Depending on the perturbation inducing the quench:

- Either the SC can recover
- Or the current flow through the matrix will allow gaining time to protect the magnet system (see later)

Fabrication of NbTi wire



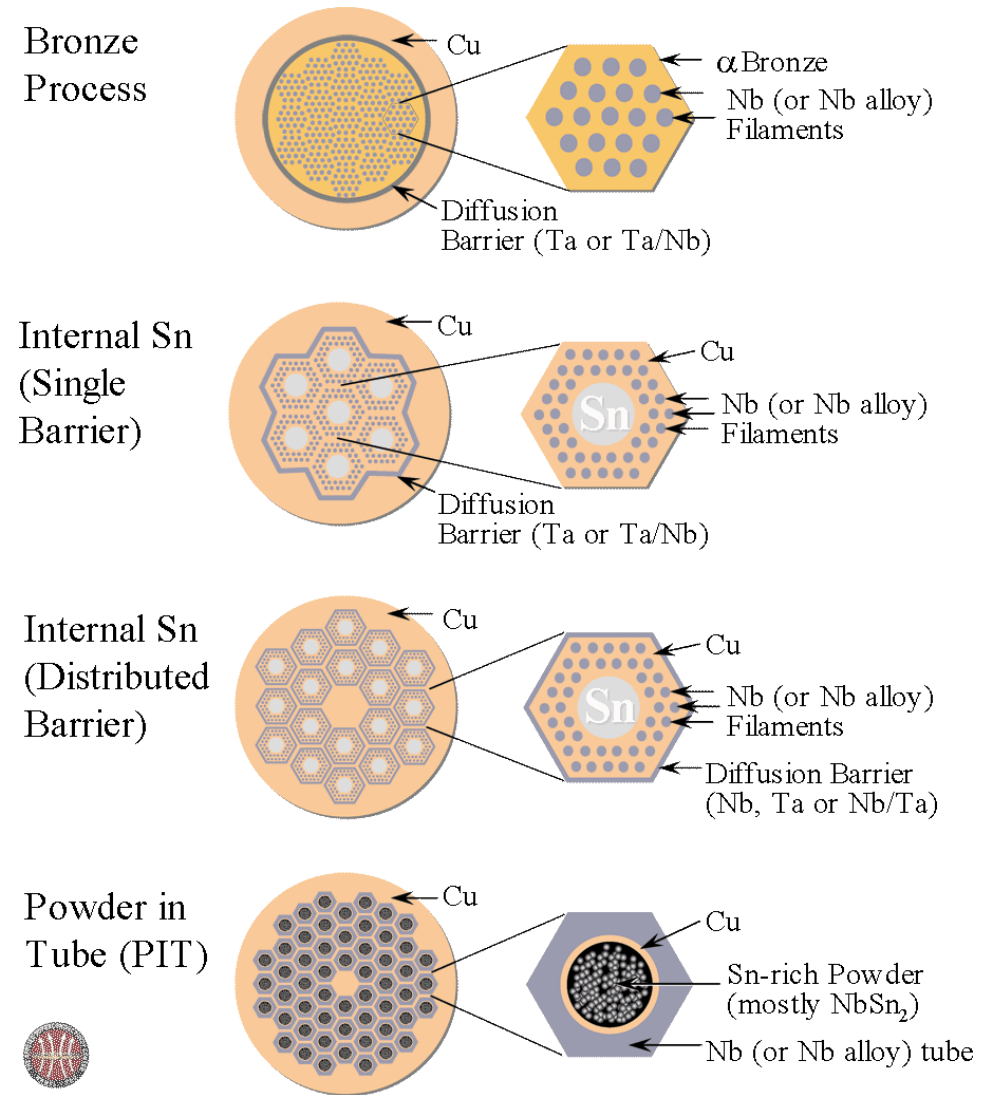
- Nb-Ti ingots in Cu can
 - 200 mm ϕ , 750 mm long
- Becomes Monofilament rods are stacked to form a multifilament billet
 - then extruded and drawn down
- Heat treatments are applied to produce pinning centers (precipitates).
- When the number of filaments is very large, multifilament rods can be re-stacked (double stacking process)



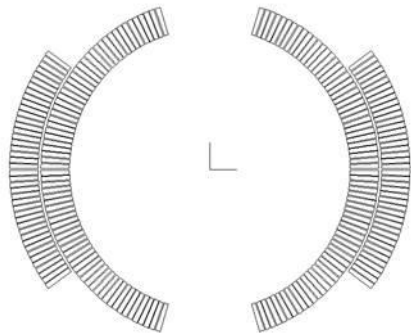
Fabrication of Nb₃Sn wire

- Nb₃Sn is brittle and cannot be drawn in final form.
- The precursors of Nb and Sn are drawn
- The wire must heat-treated to ≈650 C for several hours, to form the Nb₃Sn phase

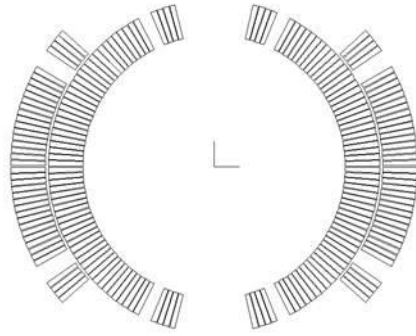
We will see later that the heat treatment occurs after the full coil fabrication



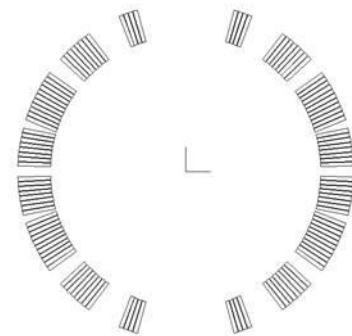
Coil cross sections (to scale) of the four superconducting colliders



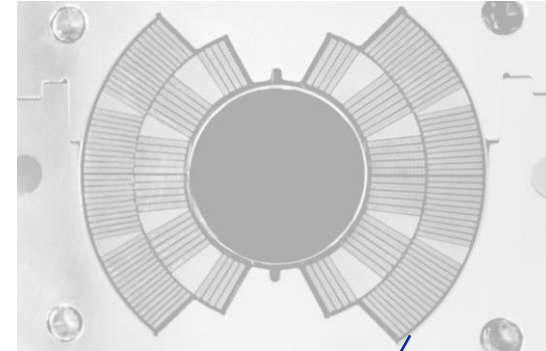
Tevatron



HERA

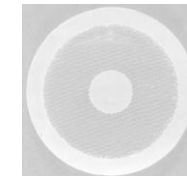


RHIC



LHC

Now that we know how to design magnetically a cross-section, let's take a look at the conductor itself



strand



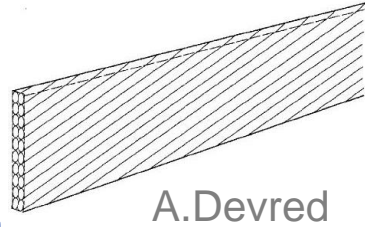
cable

From the strand to the cable

[Link to seminar](#)

Why a cable?:

- To lower the inductance
- To ease coil wind- ability
- Allow current redistribution



Rutherford cable made of two layers of multifilamentary strands: rectangular or trapezoidal

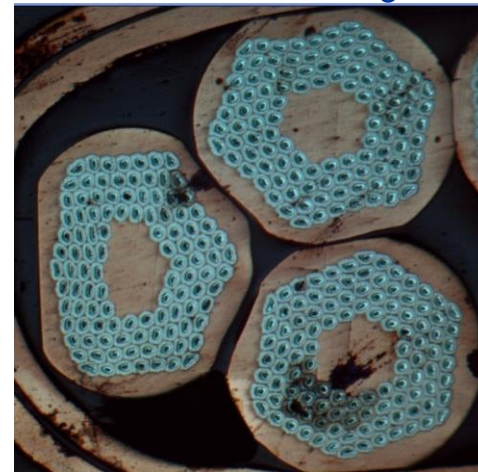


J. Fleiter – cabling machine Bldg 163 - CERN

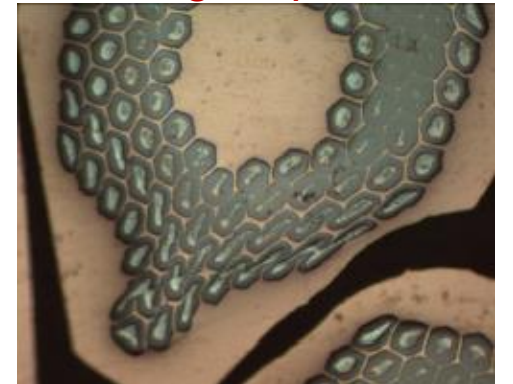


Cable must be compacted enough to insure enough mechanical stability for winding
But too much compaction can lead to edges deformation:

- reduction of the filament cross-sectional area (Nb-Ti)
- breakage of reaction barrier with incomplete tin reaction (Nb_3Sn)



Could affect magnet performance



Characterization of the critical surface

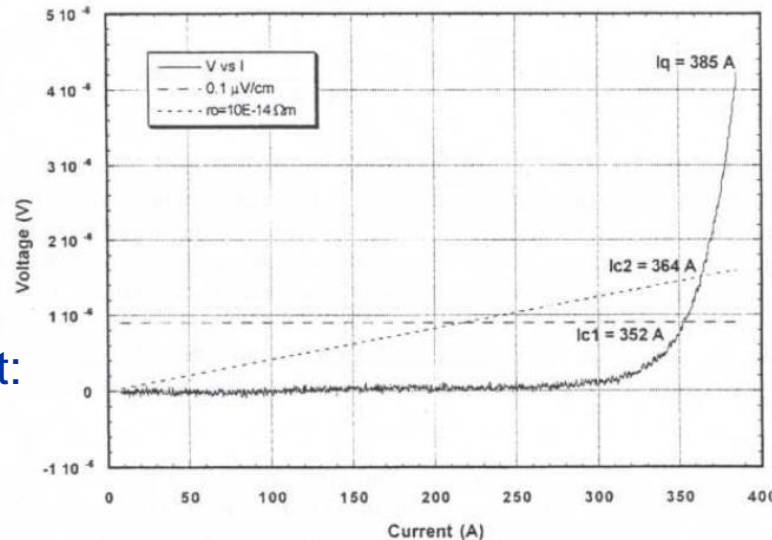
Electrical characterization of a SC strand looking at its Voltage vs current curve

“Self standing” strand

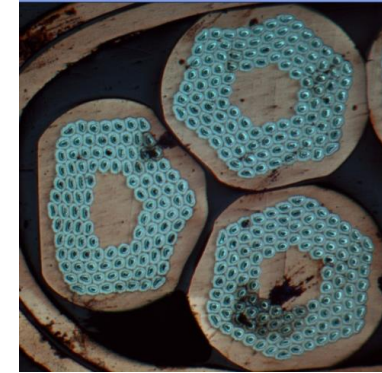
Versailles project on Advanced MAterials and Standards (VAMAS)



Standardized procedure and mandrel material to mount the wire sample (called Short Sample)



Criteria to define the critical current:
 I_c is defined as the current where
 $\rho_{SC} = 10^{-14} \Omega\text{m}$ or $E = 0.1 \mu\text{V/cm}$.
 Definition of I_c (B,T) for a **virgin strand**



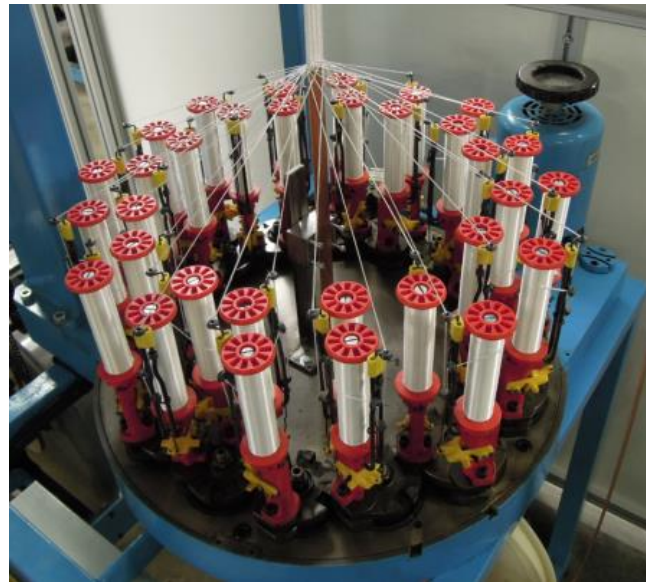
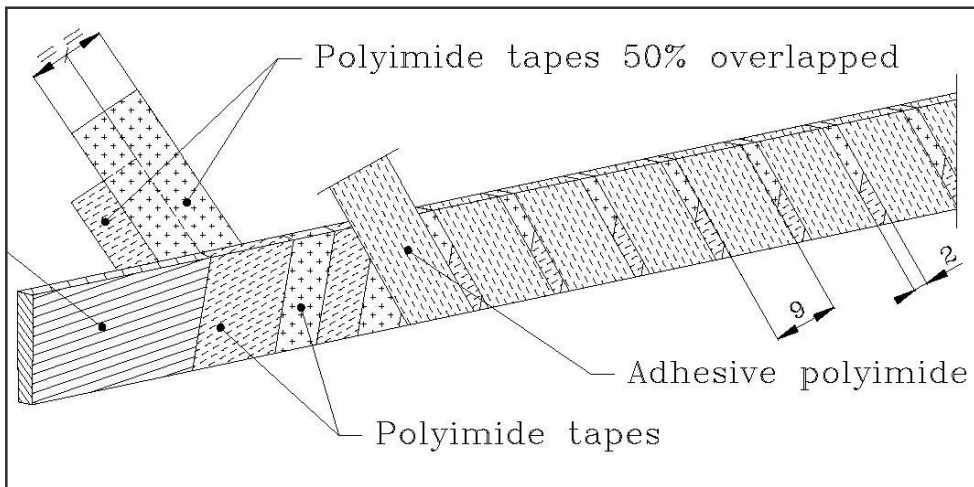
Cable I_c

Cabling can induce I_c degradation due to high compaction during cabling
 => **Extracted strands (XS)** from cables are also measured to quantify the possible degradation (typically a few %)

$$I_{c\text{-cable}} = n_{\text{strand}} \times I_{c\text{XS}}$$

Cable Insulation

- Good **dielectric properties** to withstand turn-to-turn V after a quench
- Good **mechanical properties** to withstand high stress conditions
- **Porosity** to allow penetration of helium (or epoxy)
- **Radiation hardness**
- In Nb-Ti magnets overlapped layers of **polyimide**
- In Nb₃Sn magnets, **fiber-glass** braided or as tape/sleeve.
- Typically the insulation thickness: 100 and 200 μm .

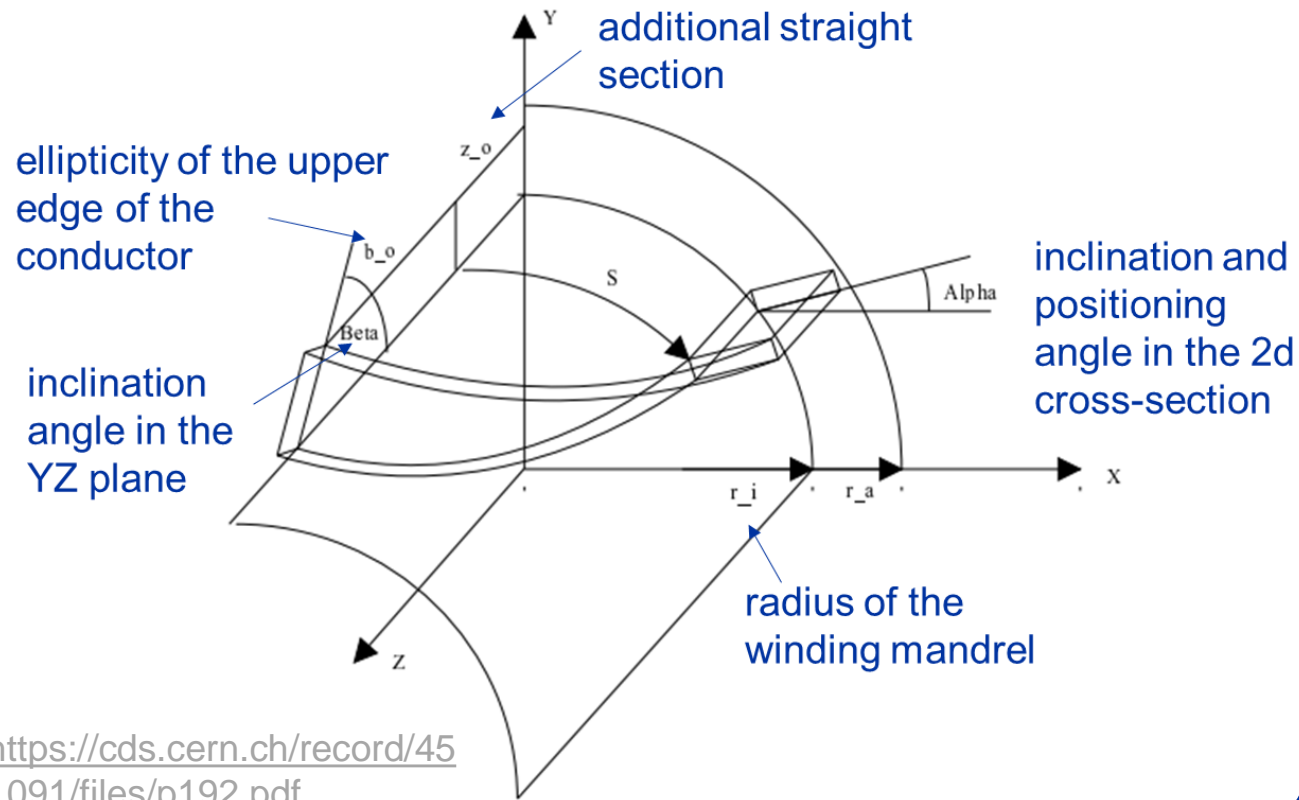


Mastering the thickness of the insulation within a few microns is key due to the large number of turns

3D coil end design

So far, we have only discussed 2D design but we need to address the 3D. End design is important as the particle sees the integrated field over the magnet length!

Coordinate system of the coil end



<https://cds.cern.ch/record/451091/files/p192.pdf>

End design optimization

- Minimizing peak field in the ends
- Field quality

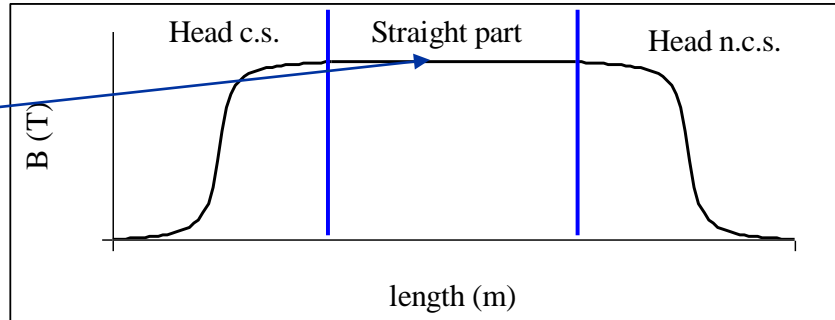
CAD design of the end parts:

physical parts around which the ends are wound

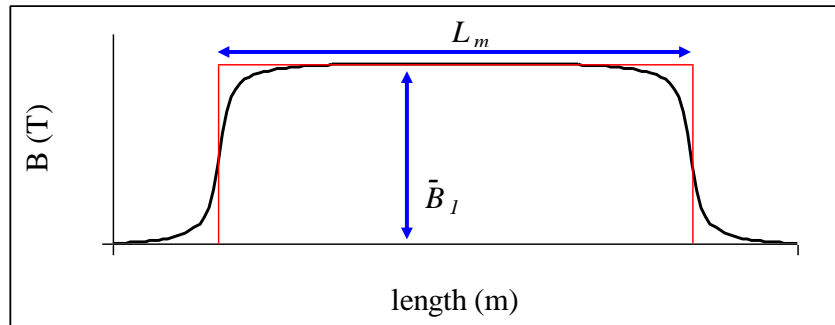
Field quality in 3D

The particle sees the integrated field over the magnet length
 Concept of **integrated main component value**

$$\bar{B}_1 \equiv \frac{\int_{sp} B_1(s) ds}{\int_{sp} ds}$$



$$L_m \equiv \frac{\int B_1(s) ds}{\bar{B}_1}$$

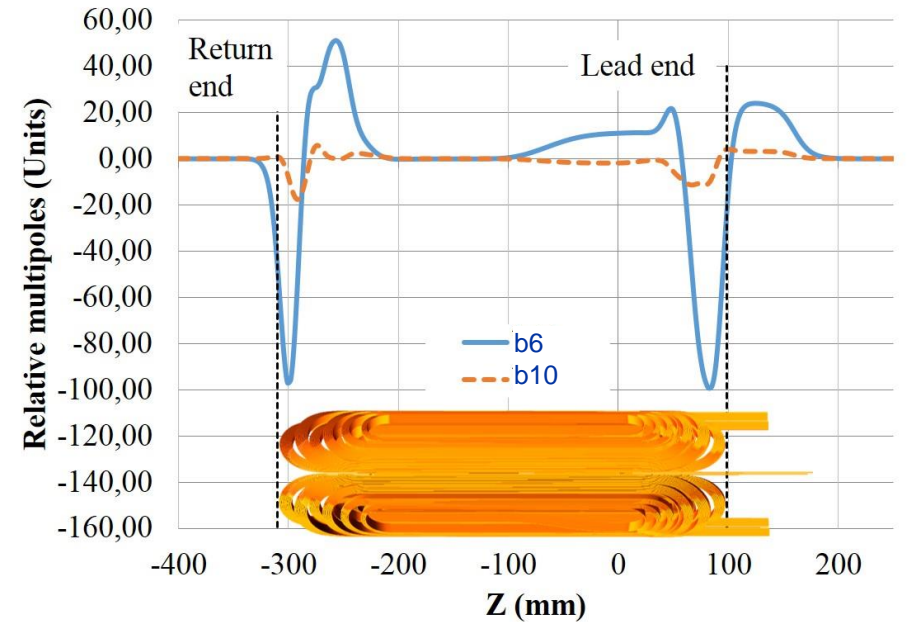


$$\bar{a}_n \equiv \frac{\int B_1(s) a_n(s) ds}{\int B_1(s) ds}$$

$$\bar{b}_n \equiv \frac{\int B_1(s) b_n(s) ds}{\int B_1(s) ds}$$

Concept of **integrated multipoles**

Example of the MQYYM quadrupole
 Coil ends have been designed so that b_6 and b_{10} integrate to zero

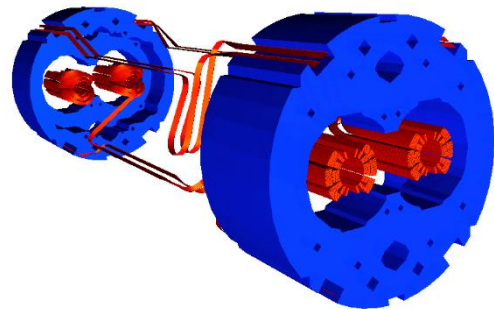


M. Segreti

Simulation and magnetic field computation

ROXIE: Routine for the Optimization of Magnet X-sections, Inverse Field Computation and Coil End Design

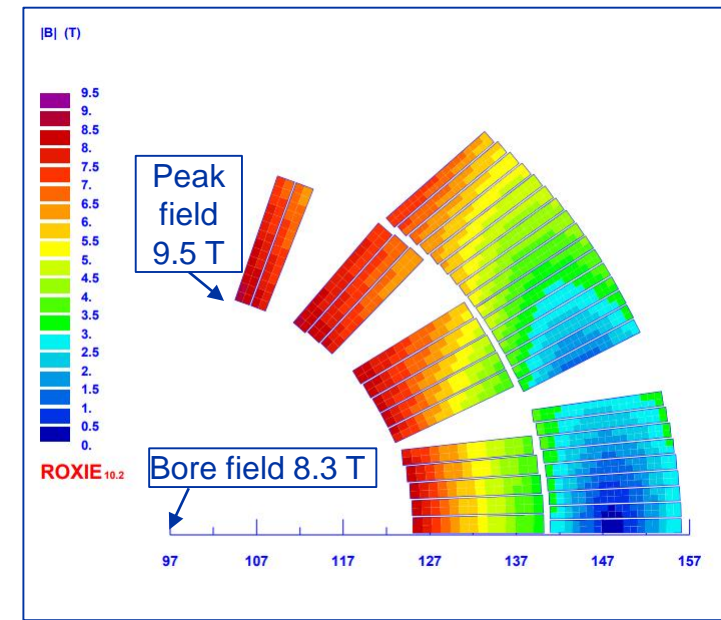
- Developed by S. Russenschuck at CERN
- Specific to superconducting accelerator magnet design
- coil geometry, iron geometry, and coil ends
- Several routines for optimization
- Evaluation of field quality, including iron saturation (BEM-FEM methods) and persistent currents



[Roxie CERN webpage](#)

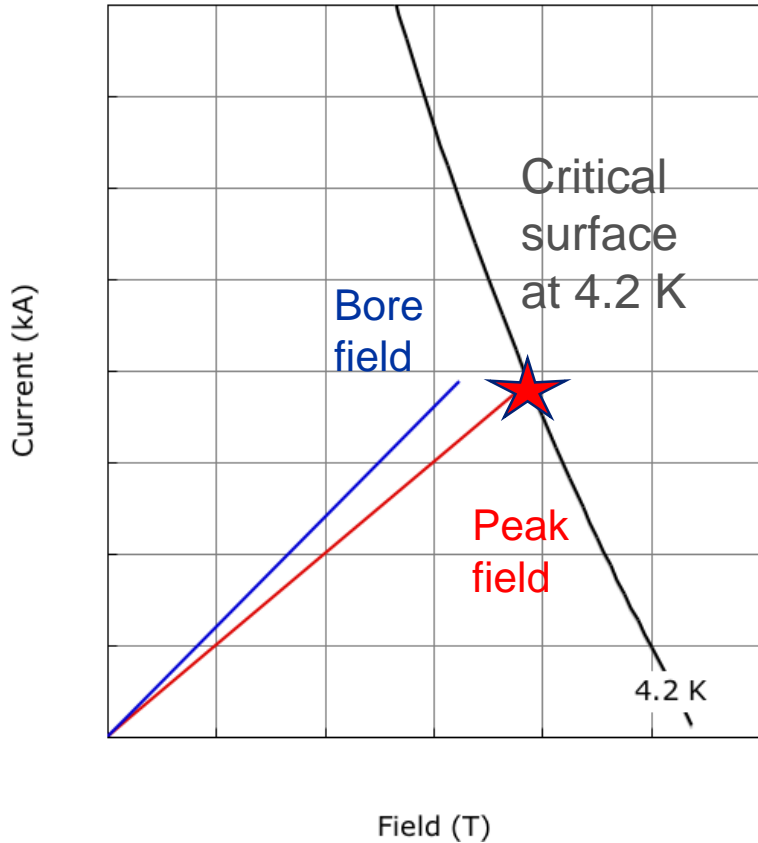
ROXIE Cross section of LHC dipole

- Peak field : maximum field in the coil
- Bore field : field at the center of the aperture

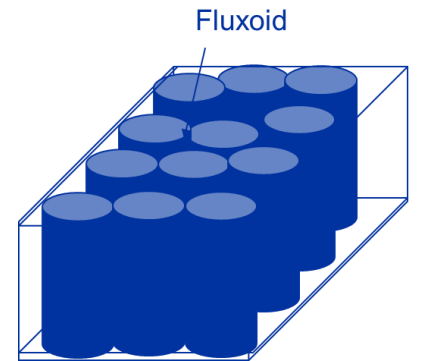
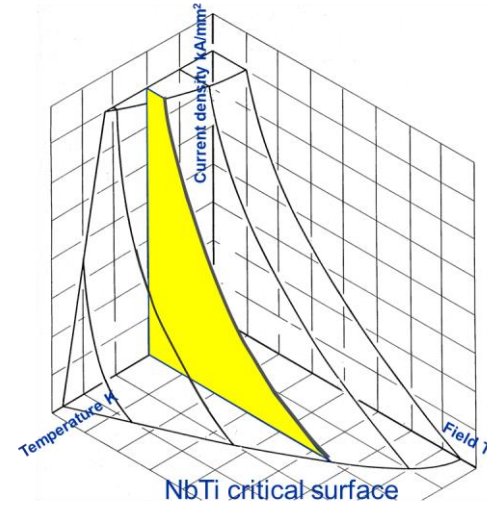


[LHC Design Report - CERN Document Server](#)

Concept of load line and quench



- The peak field as the function of the field defines the **magnet load line**
- The maximum magnet performance is obtained when the load line reaches the critical surface. Beyond that point the superconductor becomes resistive
- ⇒ this the **quench** :transition from SC to normal material
- A similar bore field load line can be plotted



SC fully penetrated and the normal cores of the fluxoids are covering the material
 => fully resistive

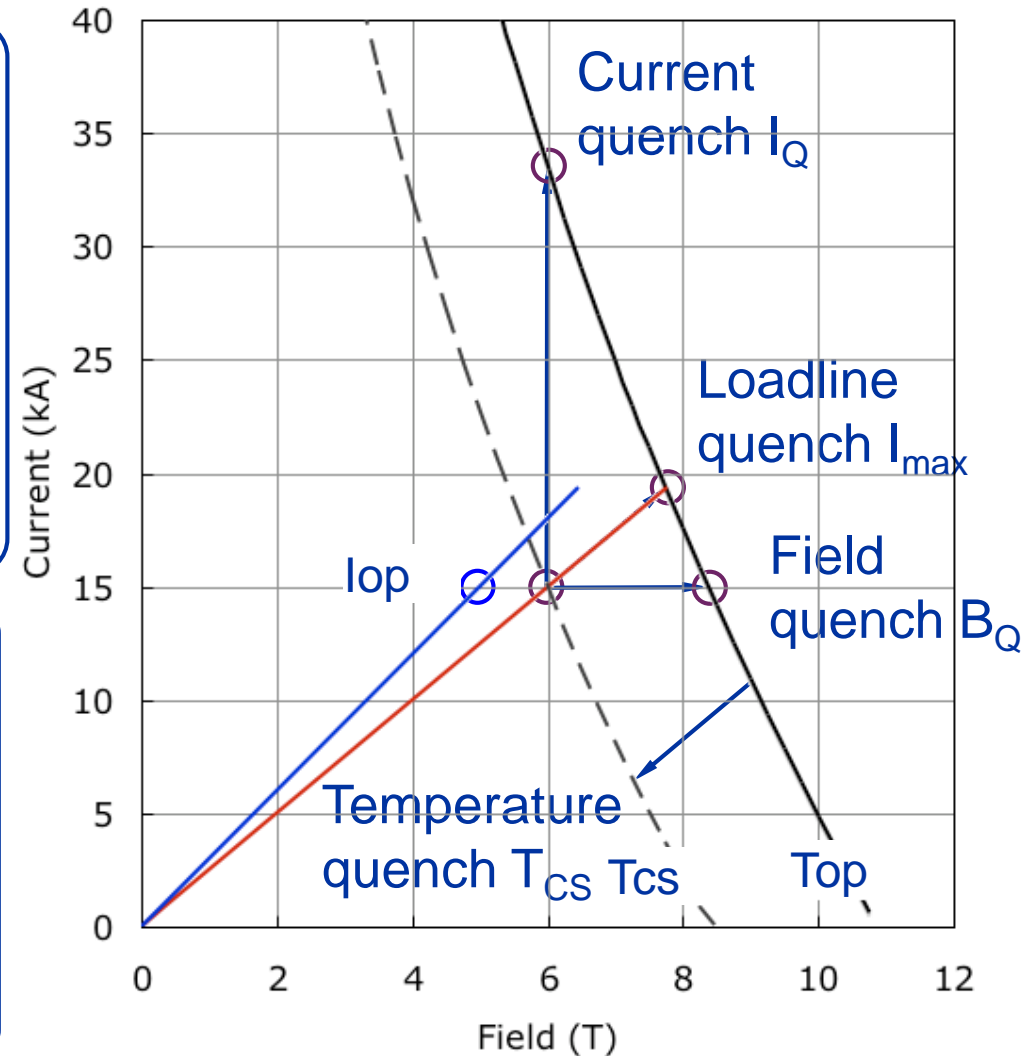
Margins in SC magnets

- Among magnet engineers, a commonly used concept is the **loadline margin**
- The concept is always criticized (not physical) but never replaced: the success of a magnet judged on its ability of reaching the max performance

E. Todesco

$$LL\ margin = 1 - \frac{I_{op}}{I_{max}}$$

- A more physical margin is the **temperature margin**: $T_{CS} - T_{op}$
- How much can we heat locally to reach the critical surface (at the operational current density and field)?

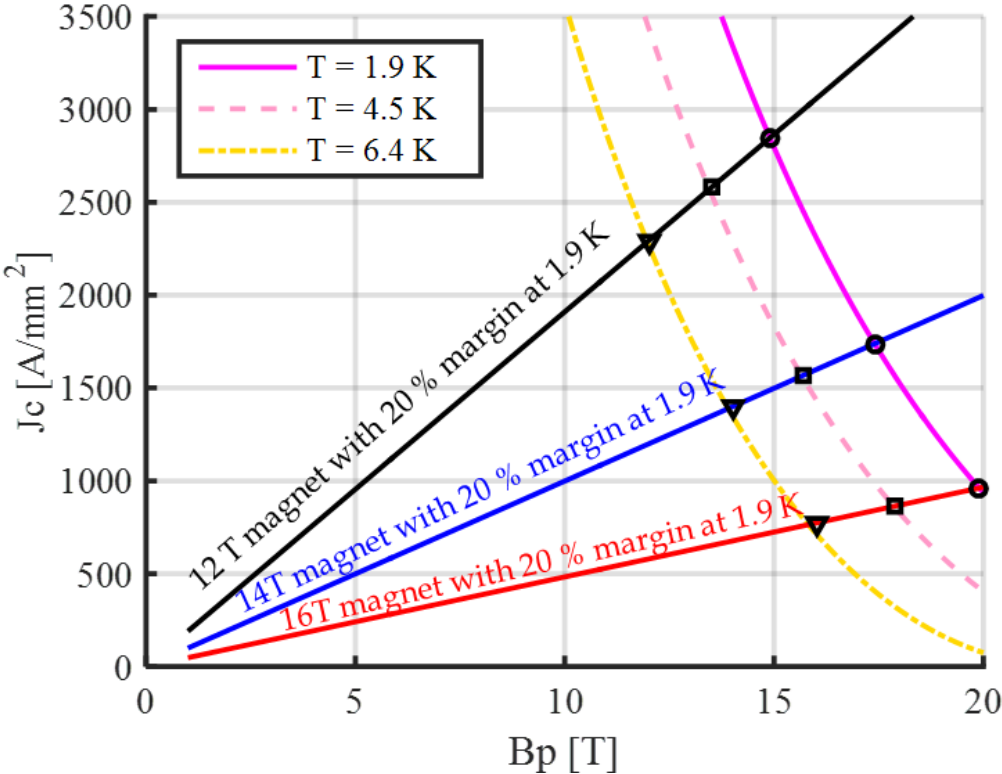


Consideration on margins for NbTi and Nb₃Sn

For Nb₃Sn and Nb-Ti the temperature margin depends only on the loadline margin and very weakly on the field.

For a given a material and an operational temperature, load line margin and temperature margin are equivalent

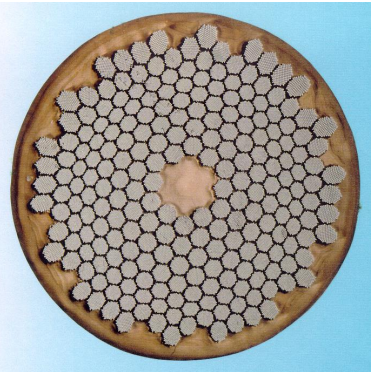
For a given LL margin, Nb₃Sn T margin is about 2.5 times greater than NbTi T margin



E. Todesco, S. Izquierdo Bermudez

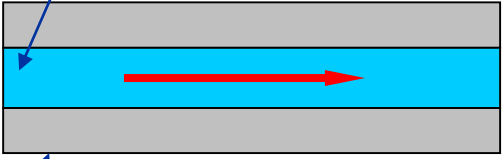
Temperature margins at 20% on loadline		
Operational temperature	1.9 K	4.2 K
Nb-Ti	2.1 K	1.2 K
Nb ₃ Sn	4.5 K	3.0 K

Quench phenomenon : a few more details

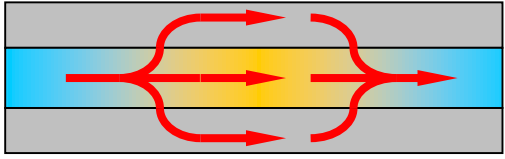


Stabilizer

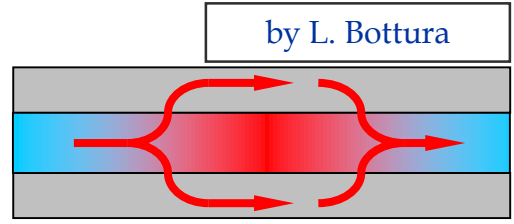
Superconductor



$T < T_{CS}$

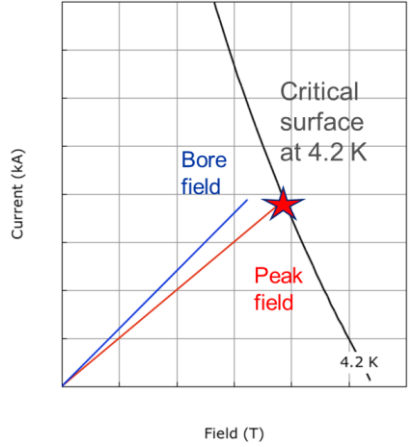


$T_{CS} < T < T_c$
Current Sharing



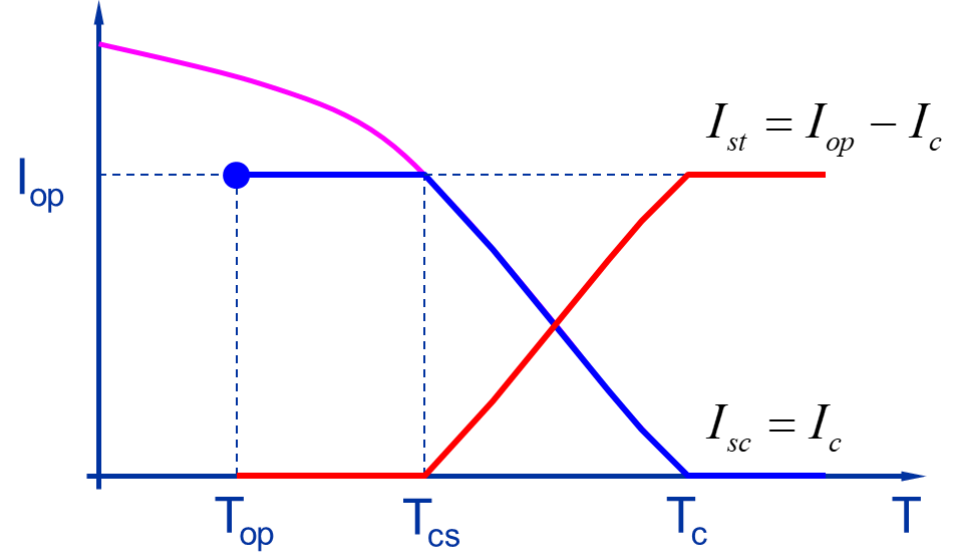
$T_c < T$
Quench

by L. Bottura



When any margin of the magnet is «eaten»

- the current starts to flow in the stabilizer
- If the temperature keeps rising, the current will ONLY flow in the stabilizer – without sufficient cooling, the transition is irreversible: it is a **quench**



Quench phenomenon and concept of protection

$$C \frac{\partial T}{\partial t} = q_{ext}''' + q_J''' + \frac{\partial}{\partial x} \left(k \frac{\partial T}{\partial x} \right) - \frac{wh}{A} (T - T_{he})$$

Heat capacity Heat source Joule heat Conduction cooling

along the conductor

generation

CAUSES

Mechanical events

- Frictional motion
- Epoxy cracking

Electromagnetic events

- Flux-jumps ,AC loss

Nuclear events

- Particle showers

Thermal events
such as Degraded
cooling

When the current starts
to flow in the stabilizer

by L. Bottura

But in fact: what is the problem?

Stored energy in the magnet

$$E_m = \int_V \frac{B^2}{2\mu_0} dv = \frac{1}{2} LI^2$$

LHC dipole : 7 MJ

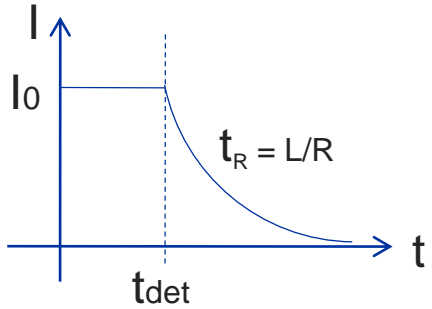
A 20 ton truck at 100 km/h: 7.7 MJ

This energy has to be removed and/or dissipated in the magnet :

- To minimize the rise of temperature
- To minimize gradient of temperature inside the coil (homogeneous distribution)

=> Concept of **quench Protection**

How to protect a magnet against quench?



- 1) When the quench starts, a resistive voltage starts to grow
- 2) Detection of that voltage (threshold at about 100 mV)
- 3) Triggering of the protection
- 4) Current decay in L/R , the quicker the decay the lower the temperature in the coil (0.1 to 0.5 s)

$$\gamma C_p(T) dT = \rho J(t)^2 dt$$

$$\int_0^{\infty} I(t)^2 dt = A_{tot} A_{Cu} \int_{T_0}^{T_{max}} \frac{\sum_k \gamma_k v_k C_{p,k}}{\rho_{Cu}(T, B)} dT$$



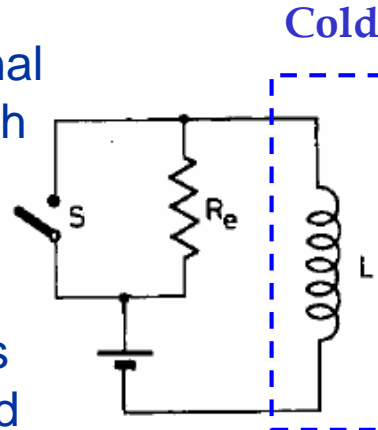
Increase the R



Cut the power supply

By adding an external resistor in series with the magnet: **dump resistor**

Part of the energy is extracted, dissipated outside the magnet



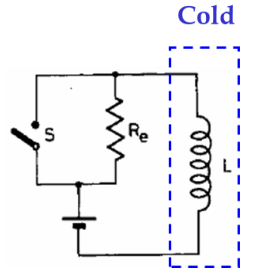
M.K. Wilson,
Superconducting Magnets

By heating up the coil, using heating elements on top of the coils called **quench heater or protection heaters**

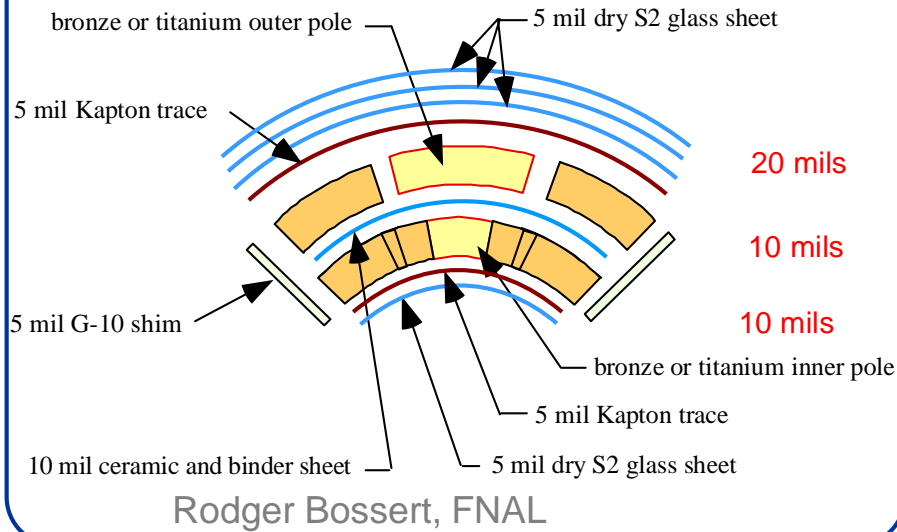


Protection: always watch the dielectric strength

- The energy extraction triggers **high voltage at the magnet terminals** – usual limit set to 1 kV
- **Internal voltages** are developing due to the magnet inductance



Importance of the design of a proper dielectric insulation in the coil



Importance of the electrical QA tests

Hipot

- Look for leakage current between coil and magnet components under high DC voltage
- Verify that the coil sustains the required voltage limits without breakout

Impulse test

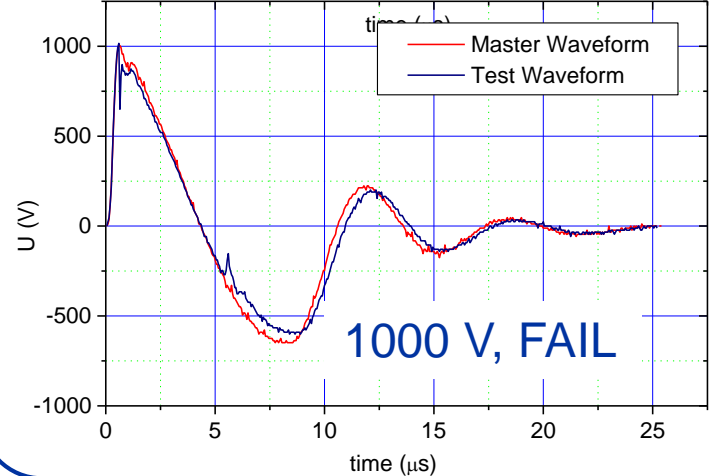
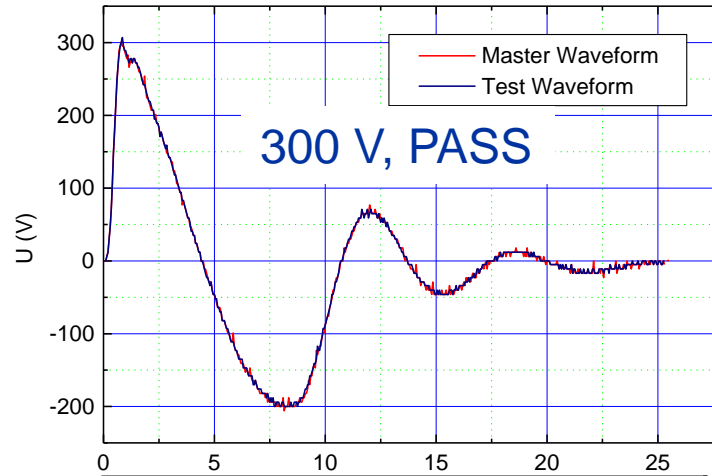
- Look for turn-to turn shorts and insulation breakdown and coil to coil parts

$$f = \frac{1}{2\pi} \sqrt{\frac{1}{LC} - \frac{R^2}{4L^2}}$$

Examples of dielectric failure

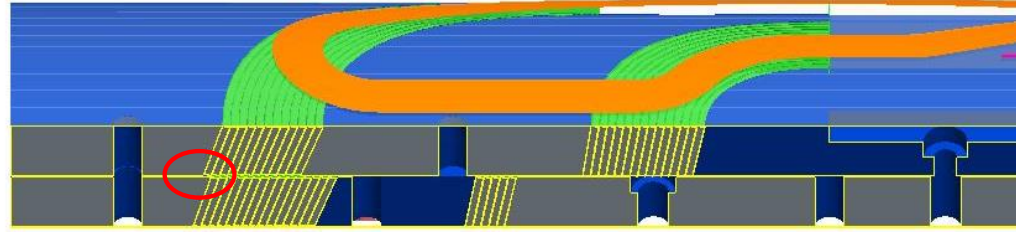
Diagnosed before test

$$f = \frac{1}{2\pi} \sqrt{\frac{1}{LC} - \frac{R^2}{4L^2}}$$



Coil not used in a magnet

Not diagnosed (occured during test) with tragic consequence

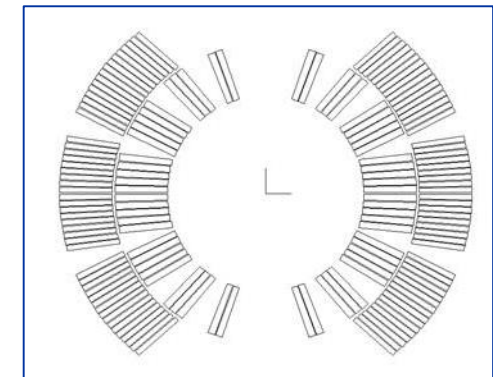
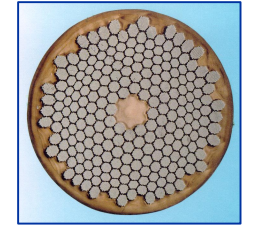
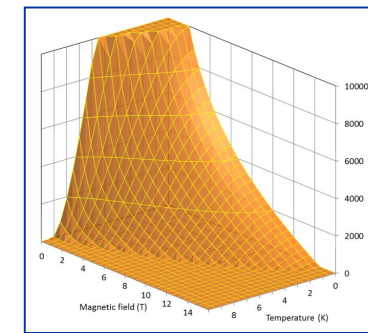


S. Caspi, R. Hafalia

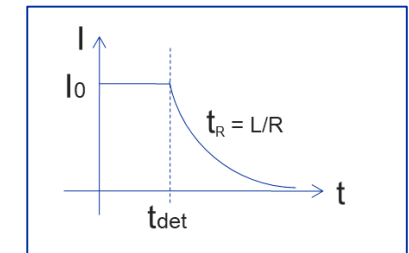


Summary of Part I

- We need superconducting magnets to bend high energy particle beams
- We need complex conductor: stabilizer, subdivision, twisting, cabling... => practical superconductors
- Superconductor operation is limited by a critical surface (B, I and T) beyond which the superconductor quenches = becomes highly resistive
- We have Ideal field distributions which we approximate
 - 2D and 3D design tools
 - Field homogeneity
 - Margins
- Large magnetic stored energy in the magnets: we need to protect them in case of quench



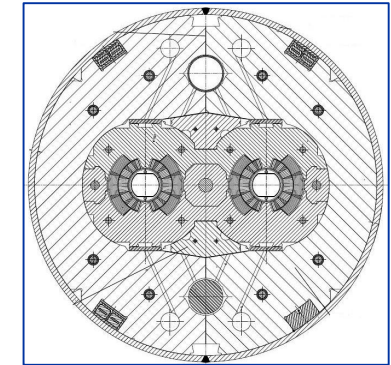
$$E_m = \int_V \frac{B^2}{2\mu_0} dv = \frac{1}{2} LI^2$$



Teaser of part II

We will take a look at:

- The **coil manufacturing**
- **the support structure** in which the coils are assembled
- The cold test and the concept of **training**



This should complete the overview of the magnet technology main concepts.

Then:

- HL-LHC at a glance with its zoo of magnets and associated challenges
- Beyond HL-LHC... what's next?

