

Antimatter in the lab

Lecture 2

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CERN

19/7/2022 10:25

Recap

Lecture 1

1. What is antimatter?

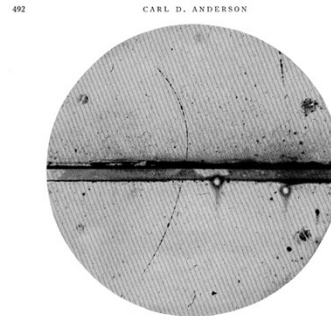


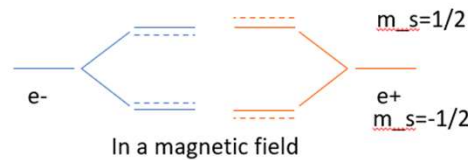
Fig. 1. A 68 million volt positron ($68 = 2 \times 34$ gaus-cm) passing through a 6 mm lead plate and emerging as a 23 million volt positron ($23 = 7.5 \times 3$ gaus-cm). The length of this latter path is at least ten times greater than the possible length of a proton path of this curvature.

$$(i\gamma^\mu \partial_\mu - m) \Psi(x, t) = 0$$

$$E = +E_p = +\sqrt{p^2 + m^2} \quad E = -E_p = -\sqrt{p^2 + m^2}$$

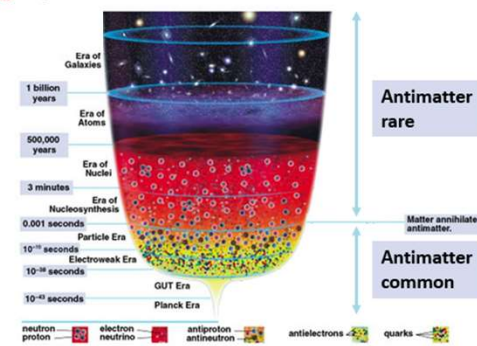
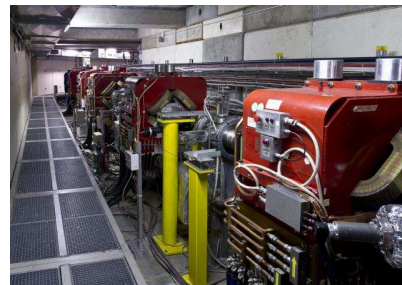
$$\Psi_1 = A \begin{pmatrix} 1 \\ 0 \\ p \\ m+E_p \end{pmatrix} e^{-ip^\mu x_\mu} \quad \Psi_3 = A \begin{pmatrix} -p \\ E_p+m \\ 0 \\ 1 \end{pmatrix} e^{-ip^\mu x_\mu}$$

2. Why study antimatter?



$$\Psi_2 = A \begin{pmatrix} 0 \\ 1 \\ 0 \\ -p \\ E_p+m \end{pmatrix} e^{-ip^\mu x_\mu} \quad \Psi_4 = A \begin{pmatrix} 0 \\ p \\ E_p+m \\ 0 \\ 1 \end{pmatrix} e^{-ip^\mu x_\mu}$$

3. How do we make antimatter at CERN?



SHOULD NOT EXIST (according to known physics)

Problem: one billion times more matter left over than expected

Figure adapted from "The Essential Cosmic Perspective", by Bennett, Voit, and Donahue

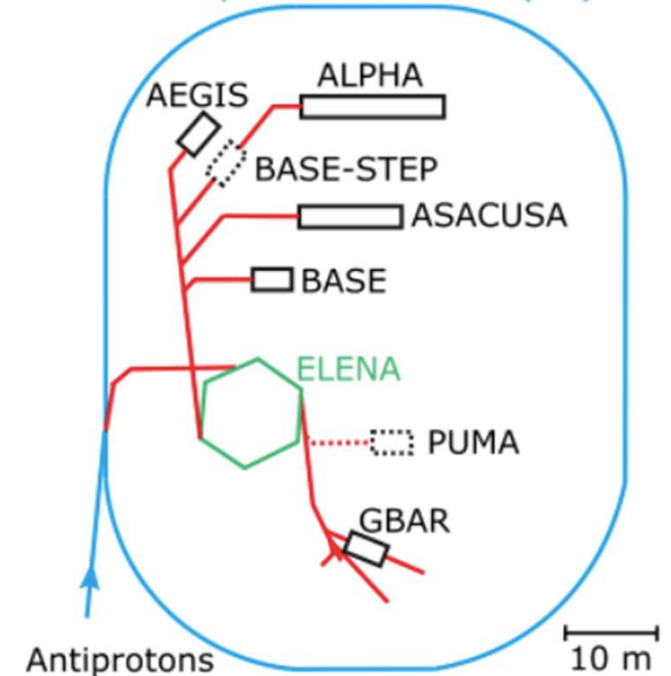
Overview

Lecture 2: Experiments at the Antimatter Factory

1. Catching and storing antimatter
2. Measurements on antiprotons
3. Spectroscopy of anti-atoms
4. Gravity and antihydrogen
5. Taking antimatter out of the lab (and into another lab..)



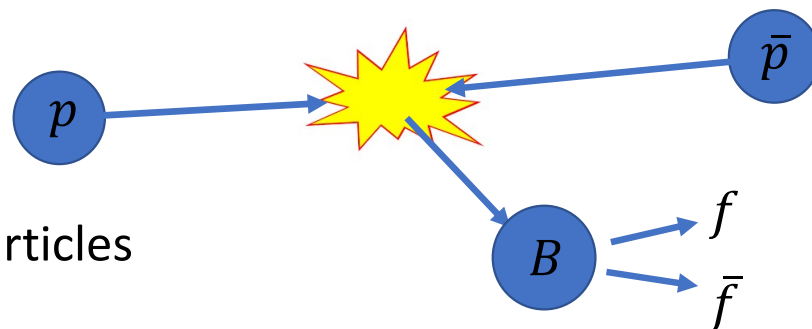
Antiproton Decelerator (AD)



Low energy physics

- High energy experiments (direct search)

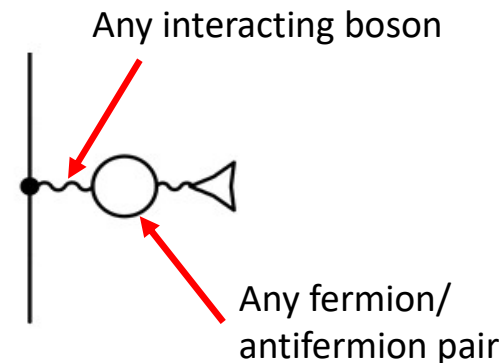
- Produce and detect new particles in high energy particle collisions
- High energies needed to make non-virtual particles



- Precision experiments: (indirect search)

$$\frac{g_{electron}}{2} = 1 + a_{QED} + a_{\mu,\tau} + a_{weak} + a_{hadrons} + a_{New\ physics}$$

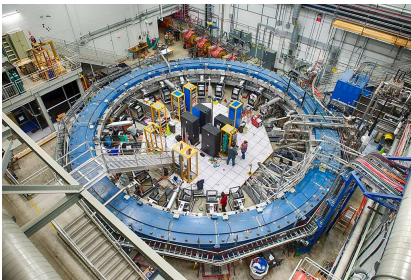
So far, all low energy CPT tests have been consistent with no CPT breaking



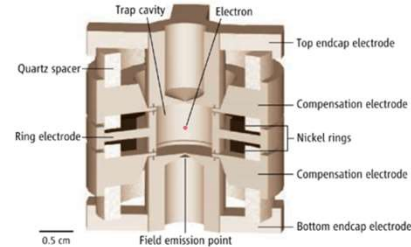
Other efforts

Many groups studying antimatter. Some notable ones are:

Positron-electron magnetic moment University of Washington/Harvard, new effort at Northwestern
Van Dyke& Dehmelt / Gabrielse



Reidar Hahn



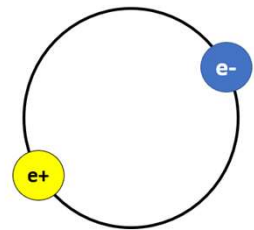
Gabrielse /Harvard

Gabrielse

Muon-antimuon magnetic moment Fermilab, formerly Brookhaven

Positronium, muonium, bound states of electrons/positron and antimuon+ electron: many groups

Kaons, B mesons, other collider searches



D. Hanneke et al. Phys. Rev. Lett. **100** (2008)

R.S. Van Dyke, Jr., P.B. Schwinberg, and H.G. Dehmelt, Phys. Rev. Lett. **59**, 26 (1987)

G.W. Bennett et al., Phys. Rev. Lett. **89**, 101804 (2002)

B. Abi et al. (Muon $g-2$ Collaboration) Phys. Rev. Lett. **126**, (2021)

Why many efforts?

Minimal Standard Model Extension (SME)

$$\mathcal{L}_{\text{lepton}}^{\text{CPT-even}} = \frac{1}{2}i(c_L)_{\mu\nu AB}\bar{L}_A\gamma^\mu\overleftrightarrow{D}^\nu L_B + \frac{1}{2}i(c_R)_{\mu\nu AB}\bar{R}_A\gamma^\mu\overleftrightarrow{D}^\nu R_B \quad (9)$$

$$\mathcal{L}_{\text{lepton}}^{\text{CPT-odd}} = -(a_L)_{\mu AB}\bar{L}_A\gamma^\mu L_B - (a_R)_{\mu AB}\bar{R}_A\gamma^\mu R_B \quad (10)$$

$$\mathcal{L}_{\text{quark}}^{\text{CPT-even}} = \frac{1}{2}i(c_Q)_{\mu\nu AB}\bar{Q}_A\gamma^\mu\overleftrightarrow{D}^\nu Q_B + \frac{1}{2}i(c_U)_{\mu\nu AB}\bar{U}_A\gamma^\mu\overleftrightarrow{D}^\nu U_B + \frac{1}{2}i(c_D)_{\mu\nu AB}\bar{D}_A\gamma^\mu\overleftrightarrow{D}^\nu D_B \quad (11)$$

$$\mathcal{L}_{\text{quark}}^{\text{CPT-odd}} = -(a_Q)_{\mu AB}\bar{Q}_A\gamma^\mu Q_B - (a_U)_{\mu AB}\bar{U}_A\gamma^\mu U_B - (a_D)_{\mu AB}\bar{D}_A\gamma^\mu D_B \quad (12)$$

$$\mathcal{L}_{\text{Yukawa}}^{\text{CPT-even}} = -\frac{1}{2}[(H_L)_{\mu\nu AB}\bar{L}_A\phi\sigma^{\mu\nu}R_B + (H_U)_{\mu\nu AB}\bar{Q}_A\phi\sigma^{\mu\nu}U_B + (H_D)_{\mu\nu AB}\bar{Q}_A\phi\sigma^{\mu\nu}D_B] + \text{h.c.} \quad (13)$$

$$\mathcal{L}_{\text{Higgs}}^{\text{CPT-even}} = \frac{1}{2}(k_\phi)_{\mu\nu}(D_\mu\phi)^\dagger D_\nu\phi + \text{h.c.} - \frac{1}{2}(k_\phi B)_{\mu\nu}\phi^\dagger\phi B_{\mu\nu} - \frac{1}{2}(k_\phi W)_{\mu\nu}\phi^\dagger\phi W_{\mu\nu} \quad (14)$$

$$\mathcal{L}_{\text{Higgs}}^{\text{CPT-odd}} = i(k_\phi)^\mu\phi^\dagger D_\mu\phi + \text{h.c.} \quad (15)$$

$$\mathcal{L}_{\text{gauge}}^{\text{CPT-even}} = -\frac{1}{2}(k_G)_{\kappa\lambda\mu\nu}\text{Tr}(G^{\kappa\lambda}G^{\mu\nu}) - \frac{1}{2}(k_W)_{\kappa\lambda\mu\nu}\text{Tr}(W^{\kappa\lambda}W^{\mu\nu}) - \frac{1}{4}(k_B)_{\kappa\lambda\mu\nu}B^{\kappa\lambda}B^{\mu\nu} \quad (16)$$

$$\mathcal{L}_{\text{gauge}}^{\text{CPT-odd}} = (k_3)_\alpha\epsilon^{\kappa\lambda\mu\nu}\text{Tr}(G_\lambda G_{\mu\nu} + \frac{2}{3}ig_3G_\lambda G_\mu G_\nu) + (k_2)_\alpha\epsilon^{\kappa\lambda\mu\nu}\text{Tr}(W_\lambda W_{\mu\nu} + \frac{2}{3}igW_\lambda W_\mu W_\nu) + (k_1)_\alpha\epsilon^{\kappa\lambda\mu\nu}B_\lambda B_{\mu\nu} + (k_0)_\alpha B^\alpha \quad (17)$$

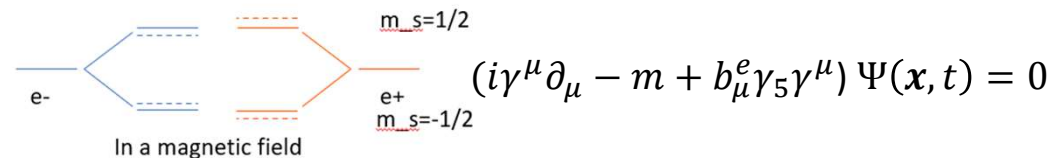
Non-minimal Standard Model Extension (SME)

18 pages to write down

Don't know a priori where to look!

CPT breaking coefficients proportional to (energy)^(-order)

Measurement	Energy scale	Fractional precision	Measurement in energy units
$K_0 - \bar{K}_0$ mass difference	Mass of two Kaons ~1 GeV	4.8×10^{-19}	4.8×10^{-19} GeV
\bar{H} 1S-2S	~2500 THz	2×10^{-12}	2×10^{-20} GeV
\bar{p} magnetic moment	Larmor frequency ~81 MHz at 1.95 T	1.5×10^{-9}	5×10^{-25} GeV

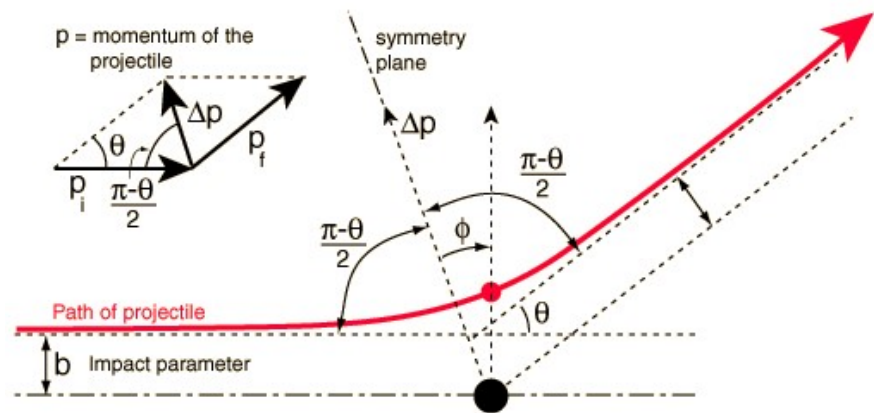
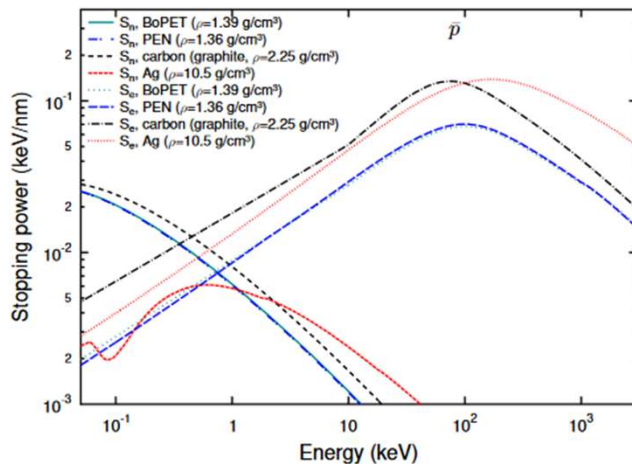
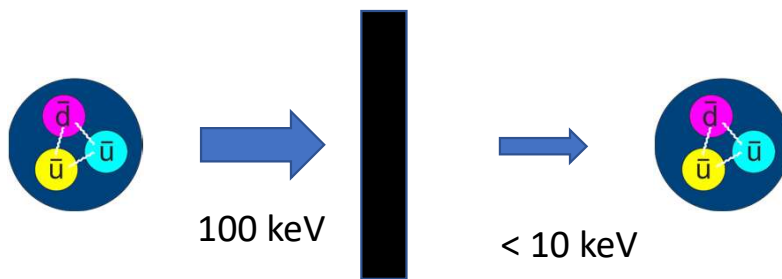


Catching and storing antimatter

Final step of slowing

Final ELENA energy 100 keV, need a final step to reach trappable energies

Degrader foil



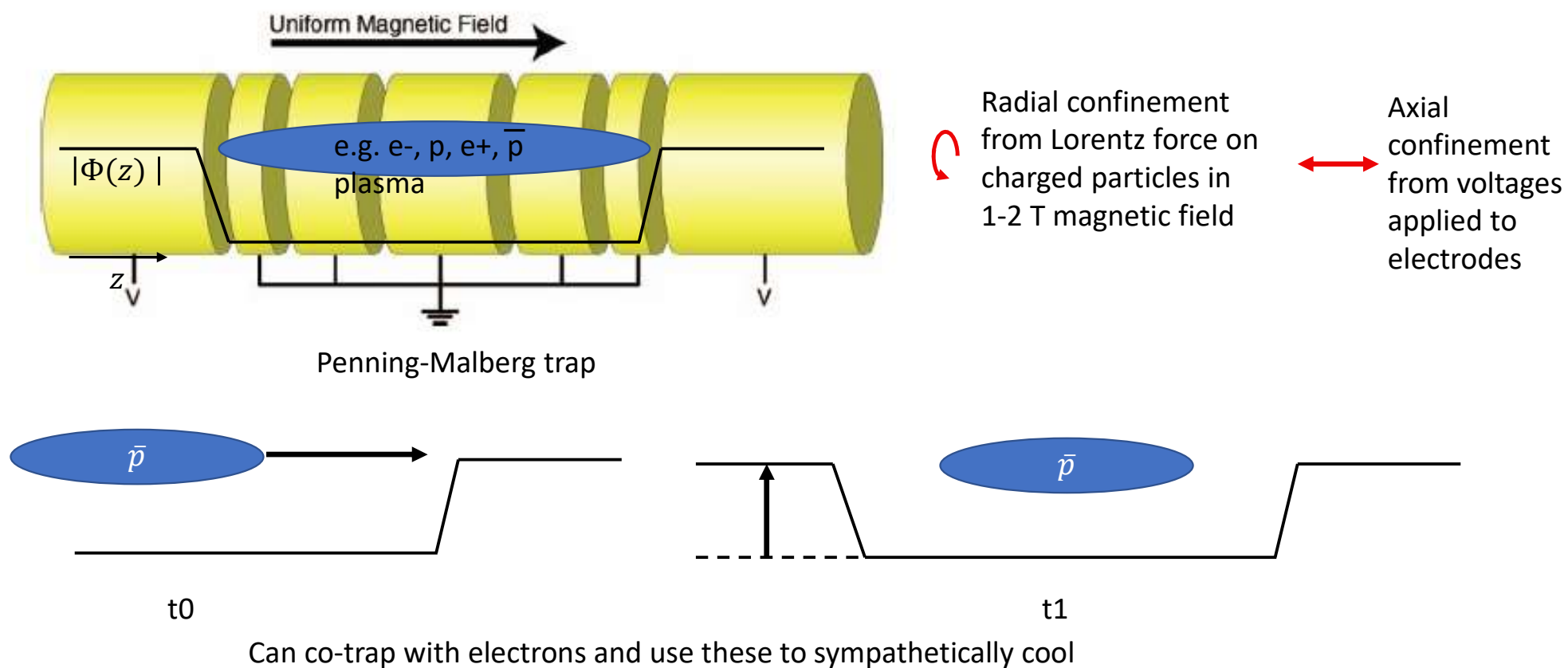
Sum of scattering from electrons and Rutherford scattering from nuclei

Up to ~50% antiprotons transmitted

J.F. Ziegler, J. Appl. Phys. **85**, 1249-1272 (1999). (Author of SRIM)
 K. Nordlund et al., Phys. Rev. A **106** (2022)

Catching antiprotons

Strong magnetic and moderate electric fields used

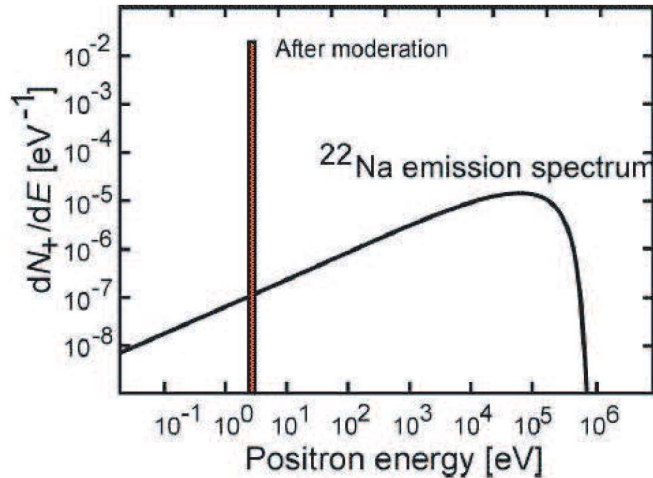


What about the positrons?

- Need positrons to make antihydrogen

ALPHA, AEGIS, ASACUSA

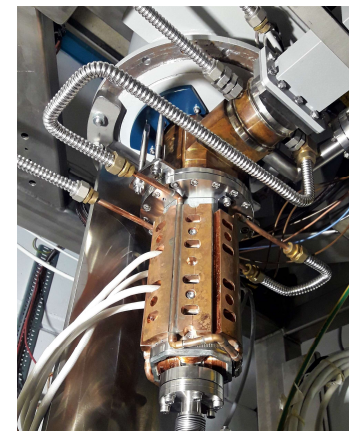
Radioactive source and moderation with frozen noble gas



(CERN/ALPHA)

~ 5 million slow
e+ per second

GBAR



(CERN/GBAR/Comini)

e- accelerated 10 MeV
onto a water-cooled
tungsten target to form
positrons by pair
production, moderated
by tungsten mesh

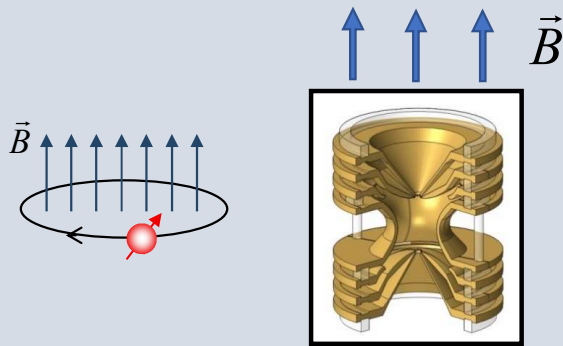
~ 40 million slow e+
per second

Measurements on antiprotons

Properties

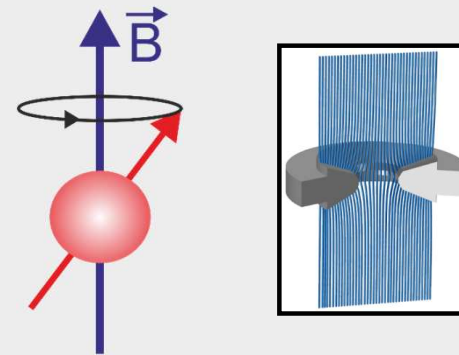
Measurements

Cyclotron Frequency



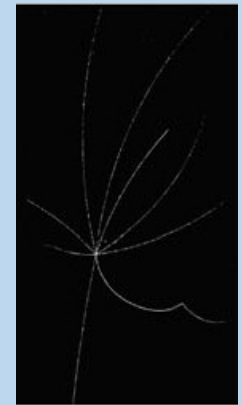
$$\omega_c = \frac{q}{m} B$$

Larmor Frequency



$$\omega_L = g \frac{e}{2m_p} B$$

Trap loss rate



CPT Tests

$$\frac{\omega_{c,\bar{p}}}{\omega_{c,p}} = \frac{q_{\bar{p}}/m_{\bar{p}}}{q_p/m_p} \text{ Charge to mass comparison}$$

$$\frac{\omega_{c,\bar{p}}}{\omega_{c,p}} (\text{Year}) \text{ Gravity, clock comparison}$$

$$\frac{\omega_L}{\omega_c} = \frac{g}{2} = \frac{\mu}{\mu_N}$$

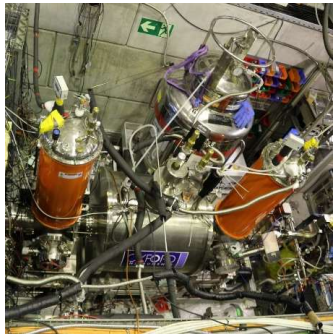
Magnetic moment

$t_{\bar{p}}$

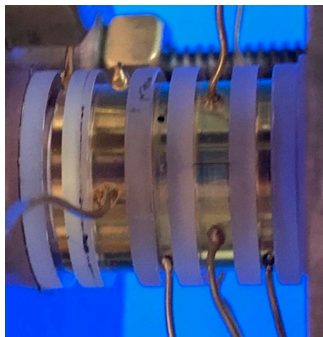
Lifetime

Frequency measurements in a Penning trap

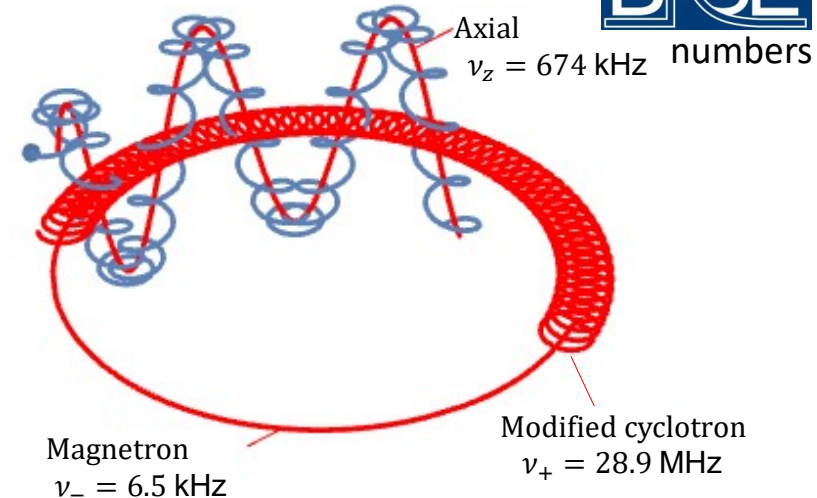
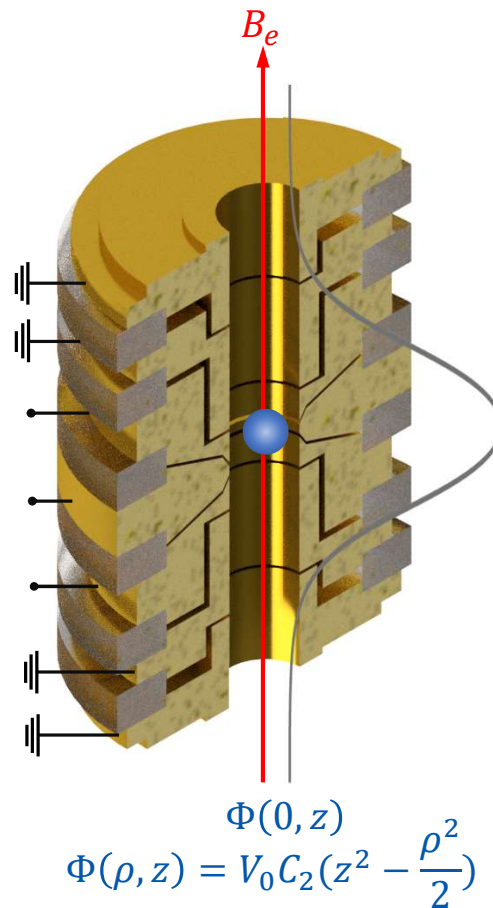
1.95 T B field from solenoid



Voltages applied to ring-shaped electrodes



A Penning trap



$$\sqrt{\nu_z^2 + \nu_+^2 + \nu_-^2} = \nu_c = \frac{q}{2\pi m} B_e$$

Orbit is sum of three normal modes

Measure frequencies and get access to charge-to-mass ratio and magnetic field

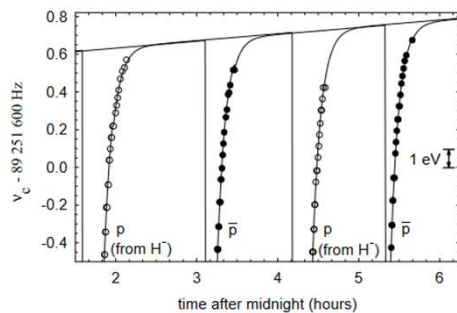
Charge-to-mass ratio comparisons

$$R = \frac{v_{c,\bar{p}}}{v_{c,H^-}} = \frac{(q/m)_{\bar{p}}}{(q/m)_{H^-}} \times \frac{B/2\pi}{B/2\pi} = \frac{(q/m)_{\bar{p}}}{(q/m)_{H^-}}$$

$$m_{H^-} = m_p \left(1 + 2 \frac{m_e}{m_p} - \frac{E_b}{m_p} - \frac{E_a}{m_p} + \frac{\alpha_{\text{pol},H^-} B_0^2}{m_p} \right)$$

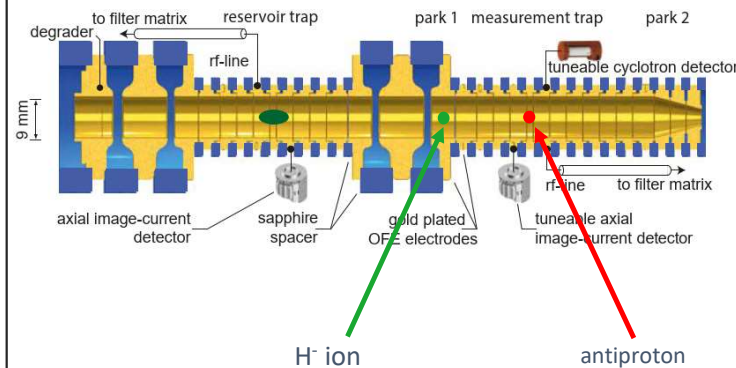
$$R_{\text{theo}} = 1.001\,089\,218\,754\,2(2)$$

Multiyear campaign performed by G. Gabrielse and collaborators at CERN's LEAR Decelerator 1990's



Single trap, 2 hrs to exchange particles, 90 ppt reached

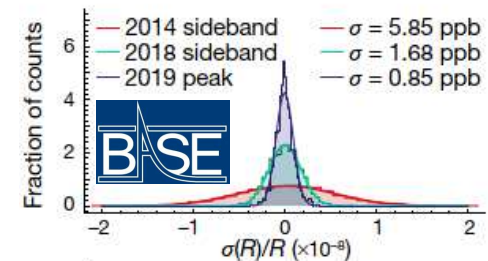
2 measurements by BASE at CERN's AD



Multi trap, 2 minutes to exchange particles,

$$\frac{(q/m)_{\bar{p}}}{(q/m)_p} = 1.000000000003(16)$$

16 ppt reached



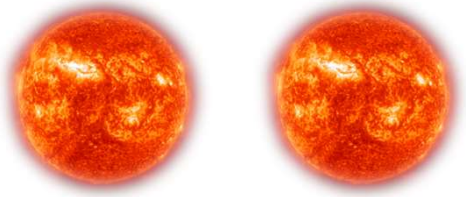
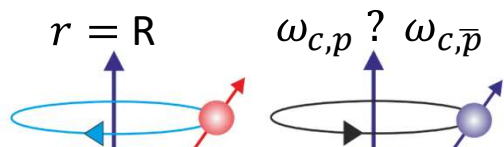
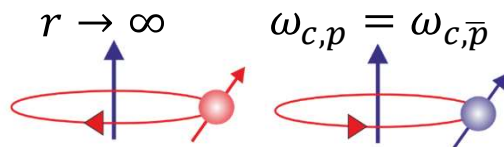
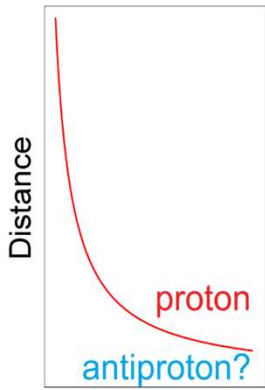
G. Gabrielse et al., Phys. Rev. Lett. **82** (1999)
M Borchert et al., Nature **601** (2022)

Gravity

Clock comparison between matter and antimatter clocks in a gravitational potential

Relies on assumptions about CPT

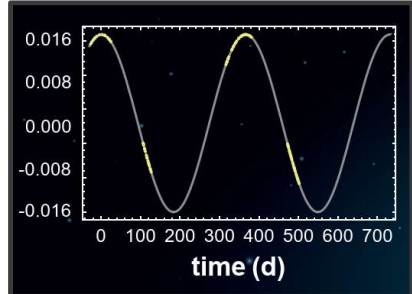
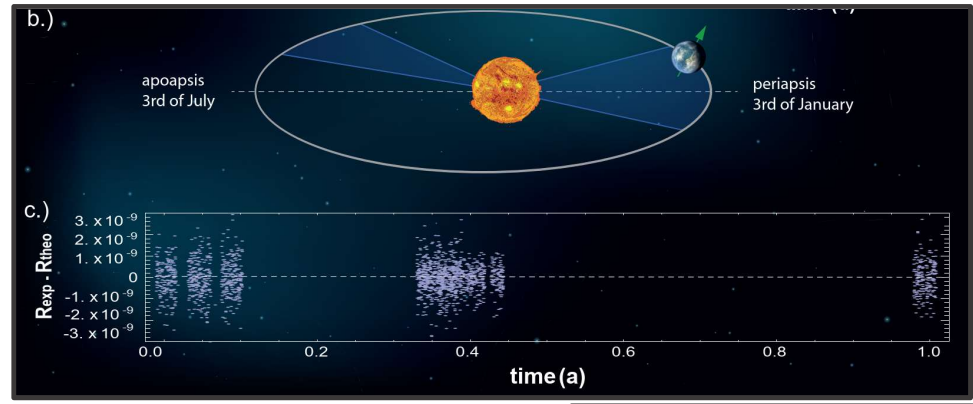
Gravitation Potential



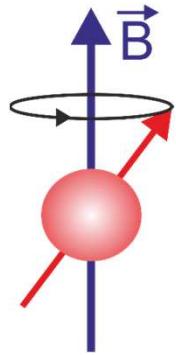
Variation in distance modulates effect

$$\frac{\Delta R(t)}{R_{avg}} = \frac{3GM_{sun}}{c^2} (\alpha_{g,D} - 1) \left(\frac{1}{O(t)} - \frac{1}{O(t_0)} \right)$$

Property	Limit
$\alpha_g - 1$	$< 1.8 * 10^{-7}$
$\alpha_{g,D} - 1$	< 0.03



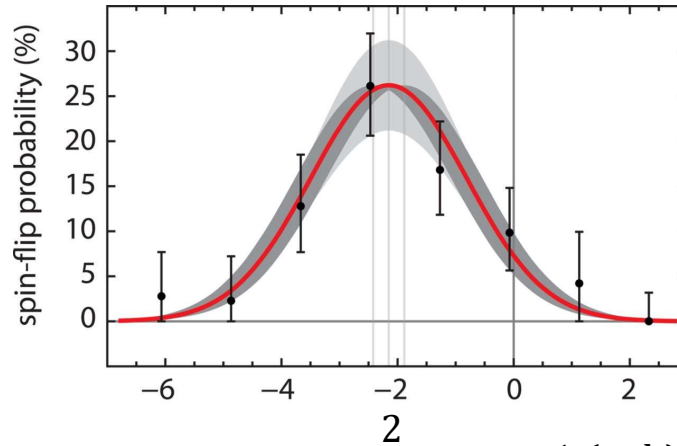
Measuring the magnetic moment



$$\omega_L = g \frac{e}{2m_p} B$$

$$\frac{g}{2} = \frac{\mu}{\mu_N} = \frac{\omega_L}{\omega_c}$$

How to measure the Larmor frequency ω_L ?



Weak radiofrequency magnetic field most likely to flip antiproton spin at ω_L

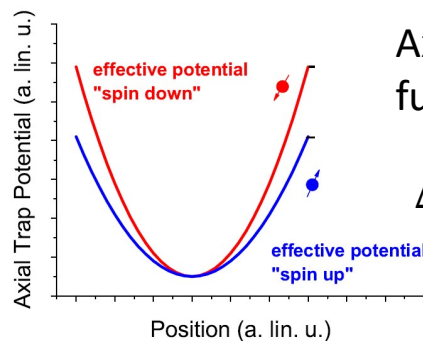
How to measure spin?

Continuous Stern-Gerlach effect

$$H_M = -(\vec{\mu}_p \cdot \vec{B})$$

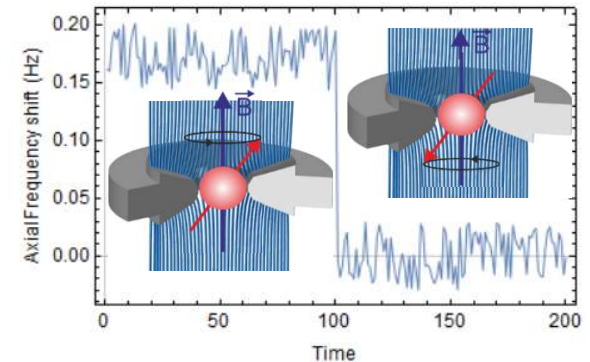
Energy of magnetic dipole in magnetic field

$$B_z = B_0 + B_2 \left(z^2 - \frac{\rho^2}{2} \right)$$



Axial frequency becomes function of spin state

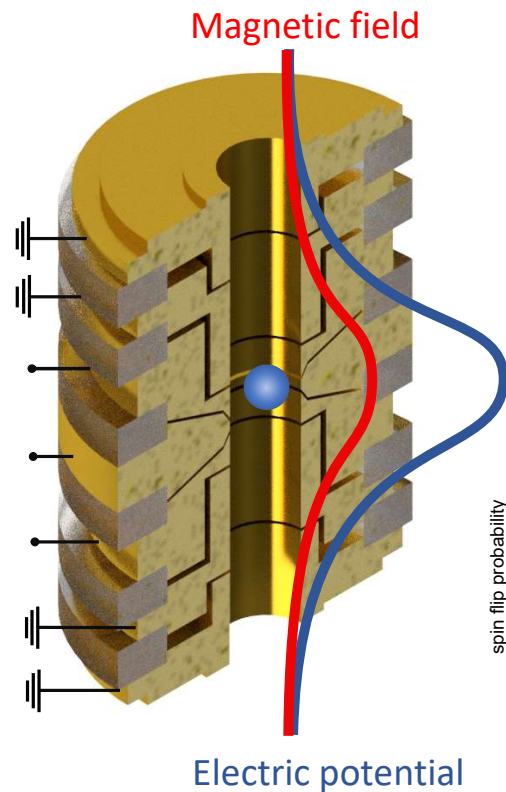
$$\Delta v_z \sim \frac{\mu_p B_2}{m_p v_z} := \alpha_p \frac{B_2}{v_z}$$



G. Schneider et al., Science. **358** 6366 (2017)

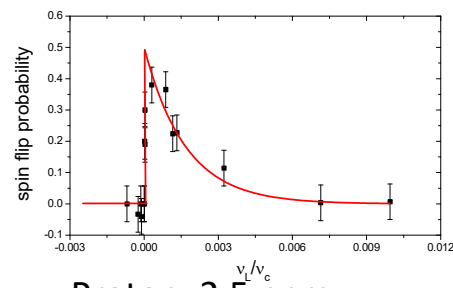
Method

Single trap method



Measure ω_L and ω_c and spin states in the same trap

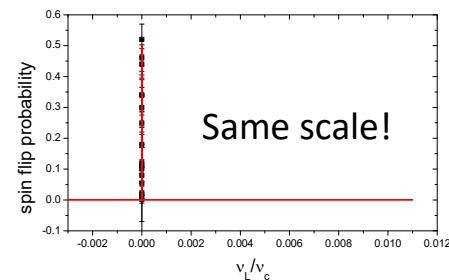
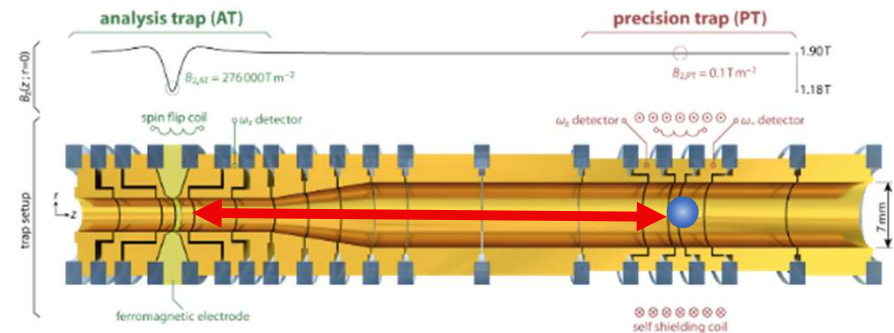
Works well for electrons, but large quadratic B field adds temperature broadening, limits measurements



Proton: 2.5 ppm
Antiproton: 0.8 ppm
Electron: 0.28 ppt
Positron: 4.3 ppt

Double trap method

Separate spin state identification from measuring ω_L and ω_c

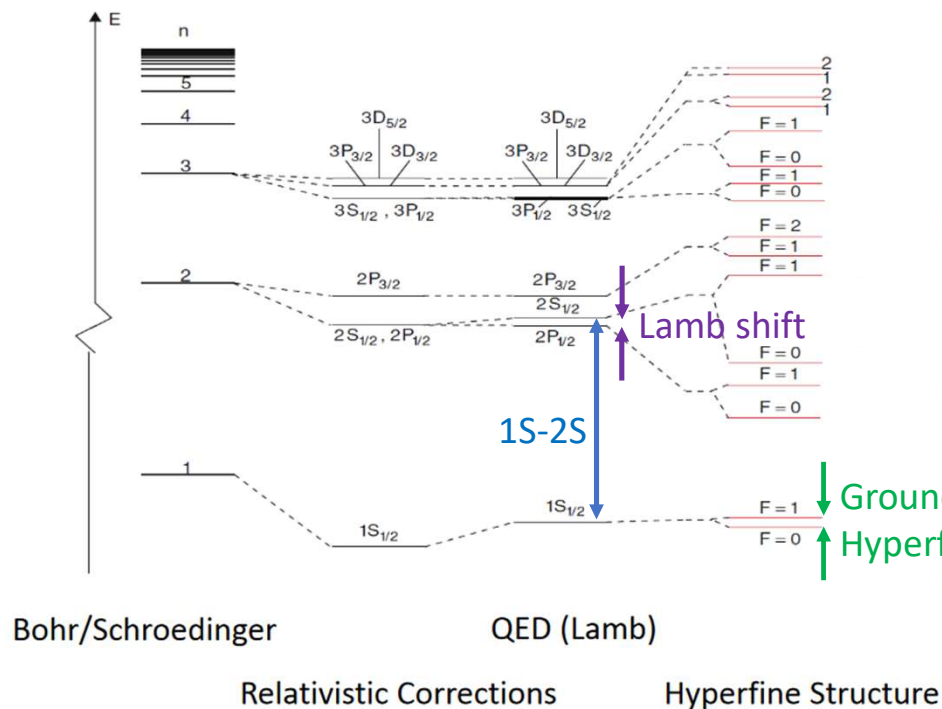


Proton: 0.3 ppb
Antiproton: 1.2 ppb

H Häffner et al., *The European Physical Journal D* **22** 2 (2003)
DiSciacca, J. & Gabrielse, G. *Phys. Rev. Lett.* **108**, 153001 (2012)
H. Nagahama et al. *Nature Communications* **8** (2017)
Hanneke et al., *Phys. Rev. Lett.* **100** (2008)
Van Dyck, R.S., Jr.; Schwinberg, P.B.; Dehmelt, H.G. *Phys. Rev. Lett.* **59** (1987)

Spectroscopy of anti-atoms

(anti)hydrogen



Bohr / Schroedinger: L degeneracy

$$E_n = -\frac{mZ^2e_0^4}{2\hbar^2n^2} = -\frac{(Ze_0)^2}{2an^2} = -\frac{mc^2}{2}\alpha^2\frac{Z^2}{n^2}$$

Dirac: J degeneracy

$$\langle H_1 + H_2 \rangle_{n,j=l\pm 1/2,l} = \frac{mc^2(Z\alpha)^2}{2n^2} \frac{(Z\alpha)^2}{n^2} \left\{ \frac{3}{4} - \frac{n}{j+1/2} \right\}$$

QED: Lamb Shift

$$\Delta E_{\text{Lamb}} \approx \frac{4}{3\pi} \frac{mc^2 Z^4 \alpha^5}{n^3} \log \frac{1}{\alpha Z} \delta_{l,0}$$

↓ Ground State

↑ Hyperfine Splitting

Hyperfine Structure:

$$\Delta E_{n,1/2,0}^{\text{Hyp}} = \frac{4}{3} g_K \frac{m}{M_K} (Z\alpha)^4 \frac{mc^2}{n^3} \frac{(2I+1)}{2}$$

Analytically calculable energy levels, high precision hydrogen measurements (4.5 ppt for 1S-2S) to compare to antihydrogen

Producing antihydrogen

- 1) Recombination $\bar{p} + e^+ \rightarrow \bar{H} + \text{UV photon}$
- 2) Three body recombination $\bar{p} + e^+ + e^+ \rightarrow \bar{H} + e^+$

rate 2) \gg rate 1) typically



ATRAP

ASACUSA

ALPHA: 2.6 ± 0.2 detected \bar{H}
trapped per minute

- 3) Charge transfer $\bar{p} + \text{positronium} \rightarrow \bar{H} + e^-$



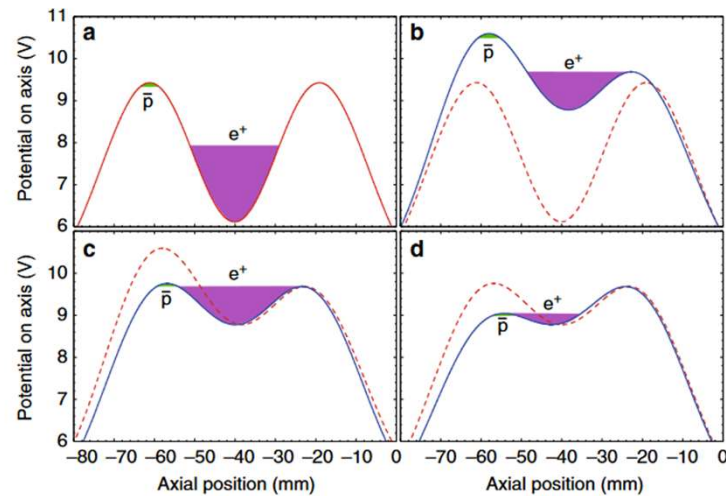
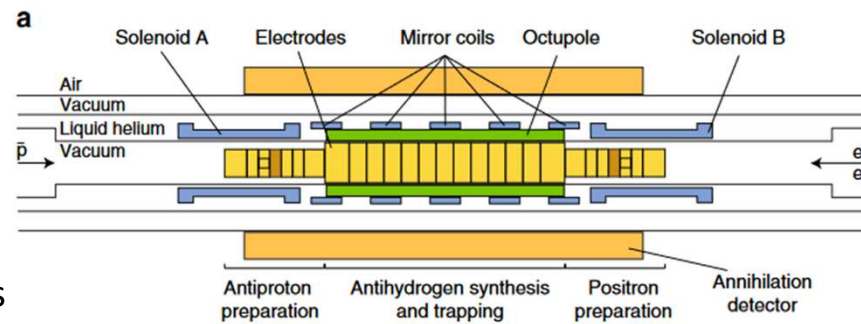
\bar{H} AEGIS EXPERIMENT

AEGIS: $0.021(5)$ \bar{H} per attempt,
 ~ 15 minutes per attempt

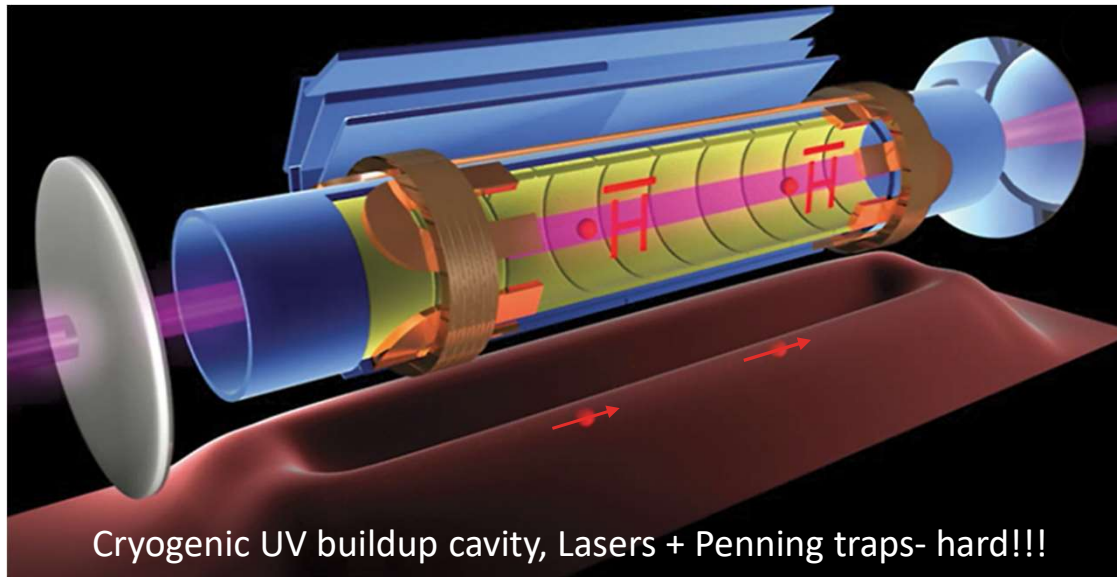
M. Ahmadi, Nature Communications **8** (2017)
C. Amsler et al., Nature Communications Physics **4** (2021)
F Robicheaux J. Phys. B: At. Mol. Opt. Phys. **41** (2008)

Antihydrogen production in ALPHA

Careful control of antiproton and positron temperatures and densities



Laser spectroscopy of Antihydrogen 1S-2S



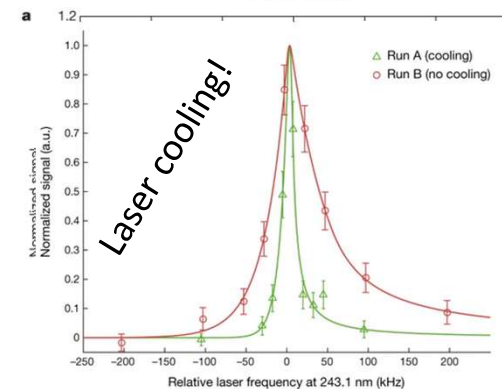
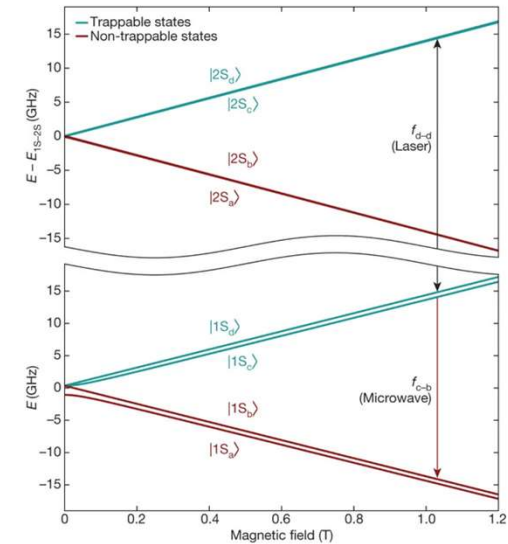
ALPHA collaboration

60 hr antihydrogen storage

$f_{\bar{d}-d} = 2,466,061,103,079.4(5.4)$ kHz (measured)

$f_{\bar{d}-d} = 2,466,061,103,080.3(0.6)$ kHz (predicted)

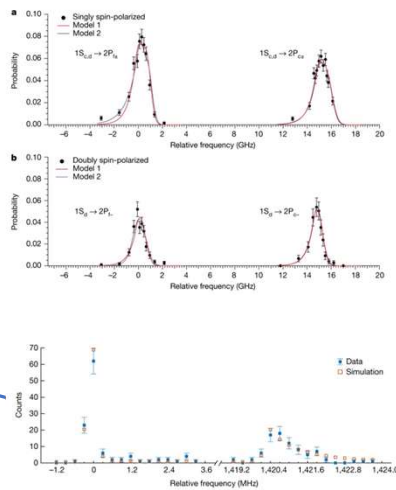
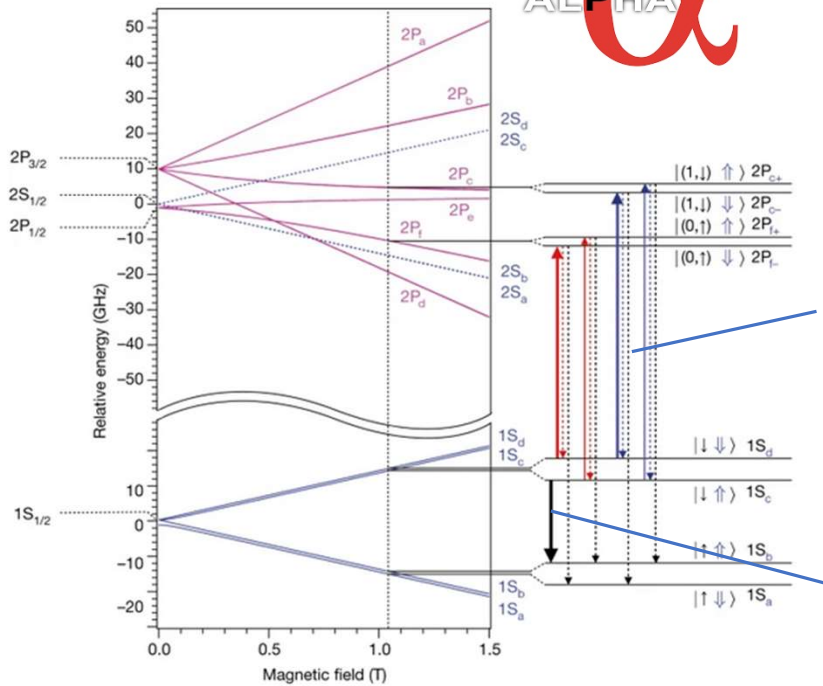
2 ppt



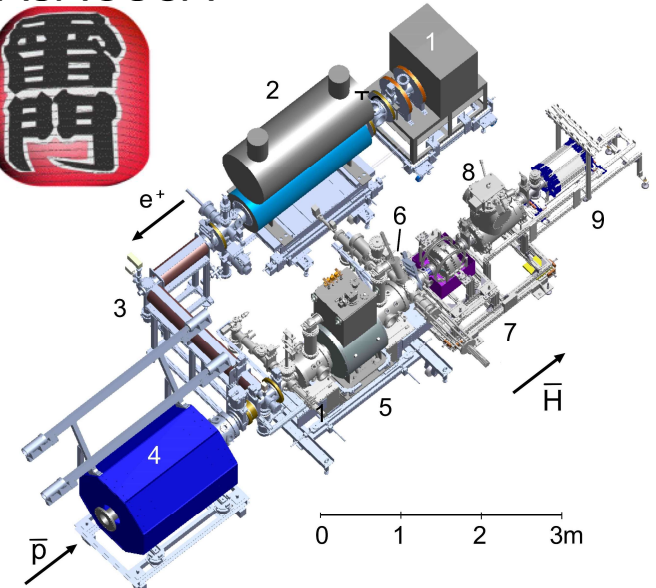
M. Ahmadi, Nature **557**, 71-75 (2018) C. J Baker, Nature **592**, 35-42 (2021)

RF spectroscopy hyperfine splitting

ALPHA



ASACUSA



$\Delta\nu = 1420405748.4(3.4)(1.6) \text{ Hz}$
 - 2.7 ppb in Hydrogen

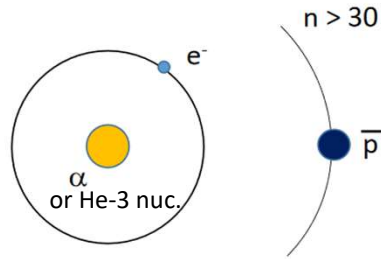
Lamb shift $2S_{1/2} - 2P_{1/2}$ \vec{H} $0.99 \pm 0.11 \text{ GHz}$, \vec{H} $0.9098717(32) \text{ GHz}$
 Ground state splitting: \vec{H} $1,420.4 \pm 0.5 \text{ MHz}$, \vec{H} $1\ 420\ 405.751\ 766\ 7(9)$

M. Ahmadi, Nature **548**, 66-69 (2017)
 M. Ahmadi, Nature **578**, 375-380 (2020)
 ASACUSA Collaboration. Report No. SPSC-P-307 Add. 1 CERN-SPSC-2005-002 (2005)
 N. Ramsey, Hyp. Interactions **81** (1993)

Antiprotonic helium



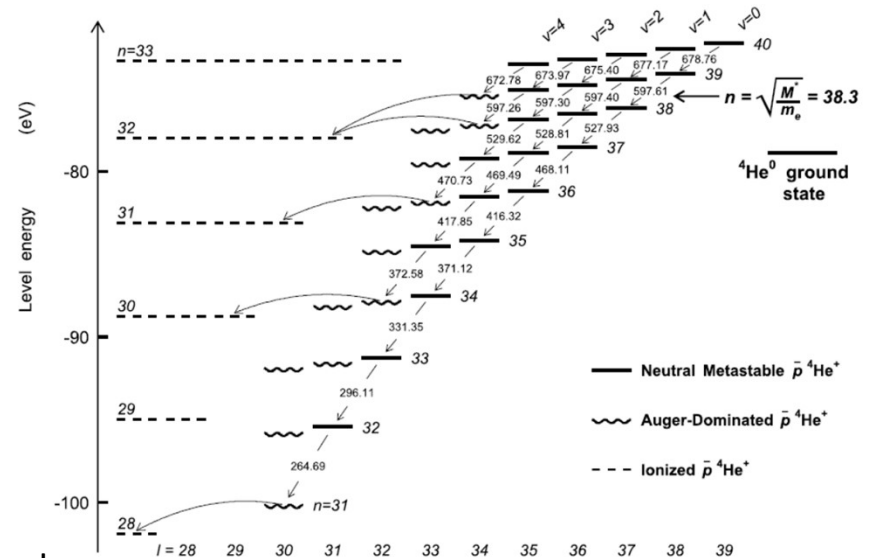
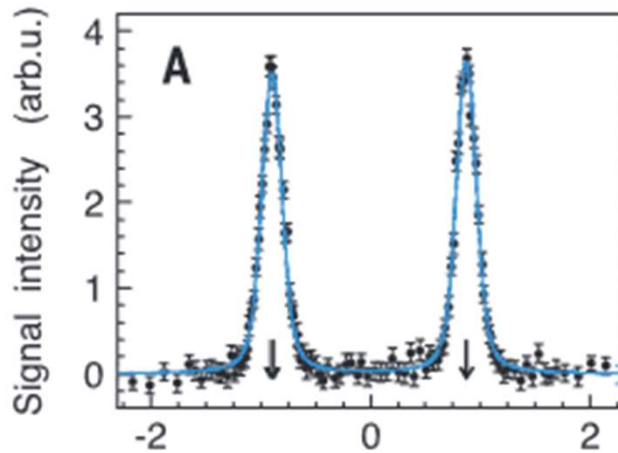
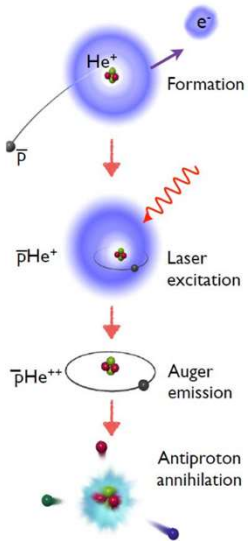
Antiprotonic Helium



$$E_n = -hcR \frac{Z^2}{n^2} \quad R = R_\infty \frac{m_{\bar{p}}}{m_e} \frac{1}{\left(\frac{m_{\bar{p}}}{m_e} + 1\right)}$$

Ground state lifetime: 100 ns
Lifetime $n \sim 38 \sim 1-2 \text{ us}$ or $\sim \text{ns}$

Measure energy levels, determine $\frac{m_{\bar{p}}}{m_e}$

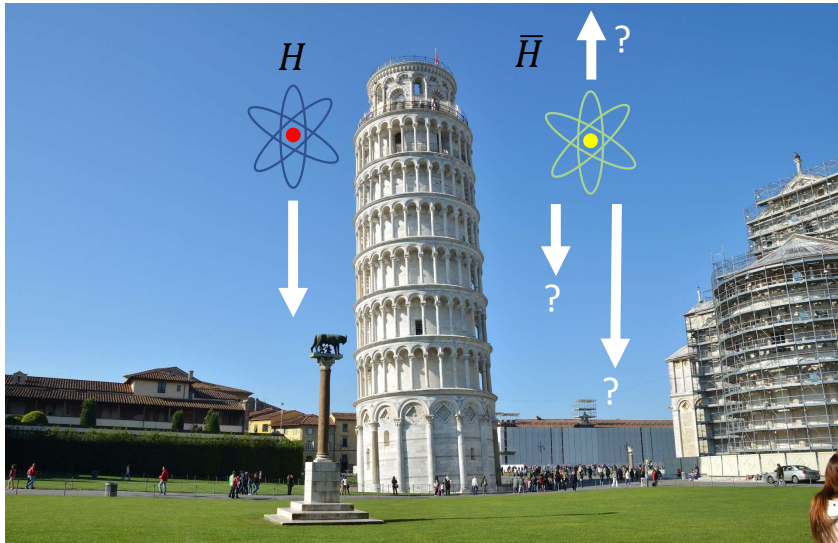


Laser resonance leads to electron ejection and rapid $\bar{p}\text{He}^{2+}$ decay emitting pions, detected via Cherenkov detectors

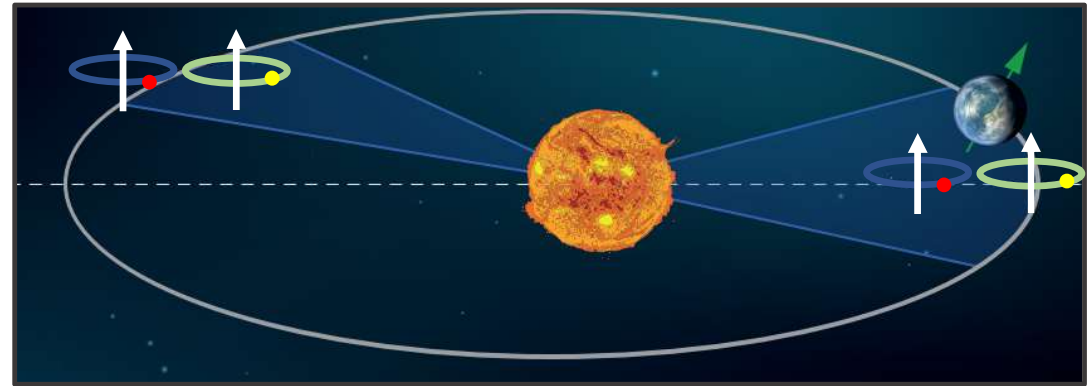
M. Hori et al., Science 354, 610 (2016)

Effect of gravity on antihydrogen

Types of measurement



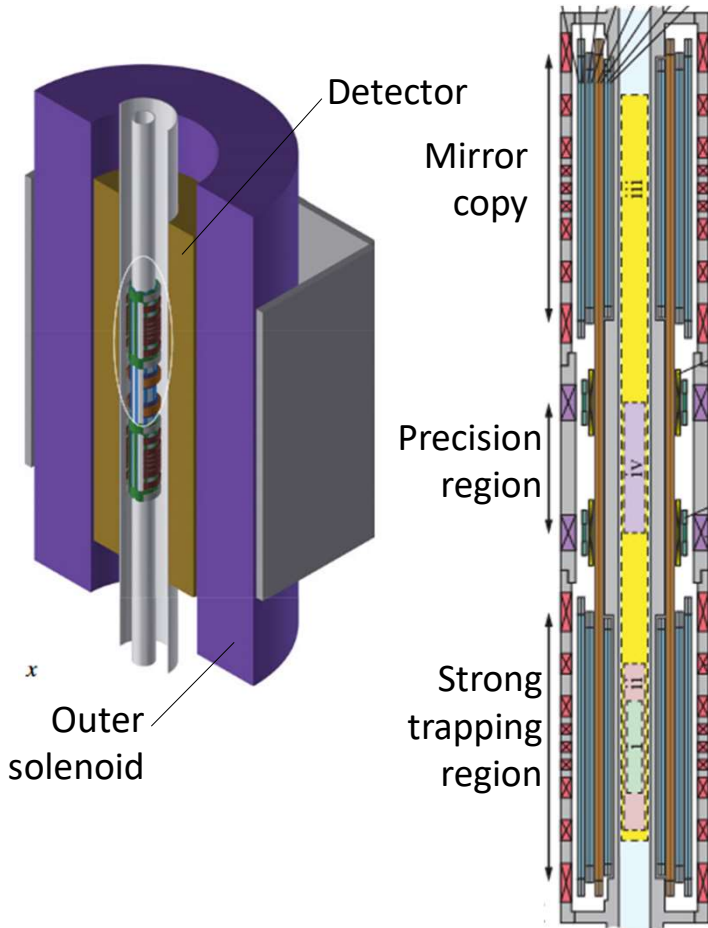
Freefall



Clock comparison

High precision needed- If proton is any guide, antiquark masses only ~1% of the antiproton

ALPHA-g

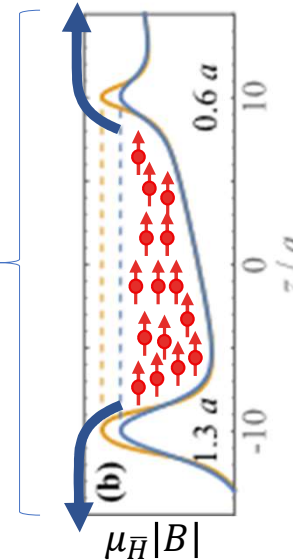


Mirror copy of lower region to keep fields symmetric

Region optimized for gravity measurement

Region optimized for \bar{H}

$$V = \mu_{\bar{H}}|B| - m_{\bar{H}}gh$$



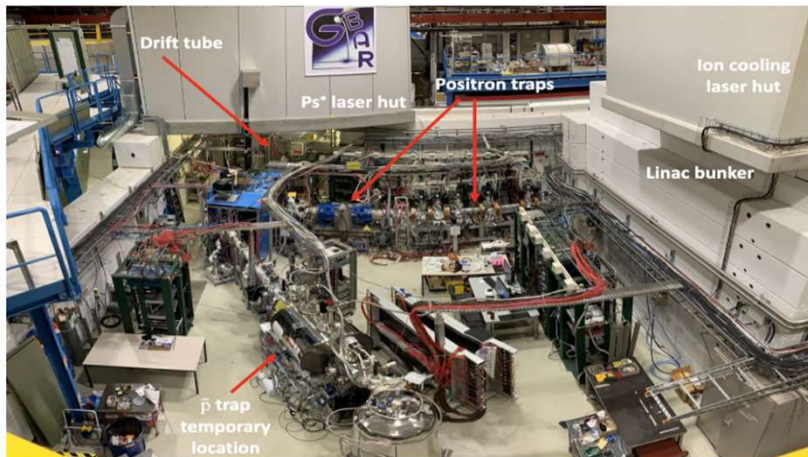
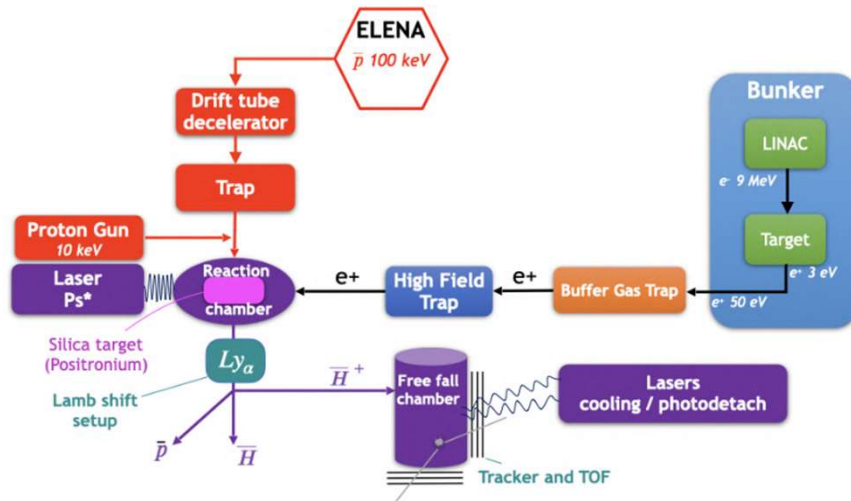
Slowly ramp magnetic fields until equal numbers escape up and down, Infer $m_{\bar{H}}$

Colder the better!
Initially <0.54 mK
With laser cooling
Initially <0.05 mK

Target 5-1% measurement on $m_{\bar{H}}$

W. A. Bertsche, Phil. Trans. R. Soc. A **376** (2018)
C. So et al., IEEE Trans. Appl. Super. **30** 4 (2020)

GBAR



1. Make \bar{H}^+ by reacting \bar{H} with positronium
2. Sympathetically laser cool \bar{H}^+ with Be^+ to $20 \mu\text{K}$
3. Photoionise \bar{H}^+ to \bar{H}
4. Drop and measure effect of gravity

Initial goal 1%, final goal 0.1% with quantum measurement

Also, long term possibility to produce \bar{H}_2^+ molecules and do antimolecular spectroscopy!

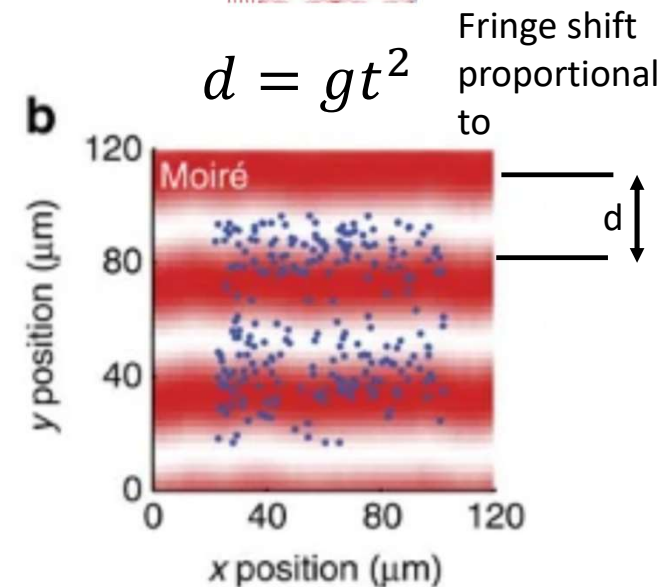
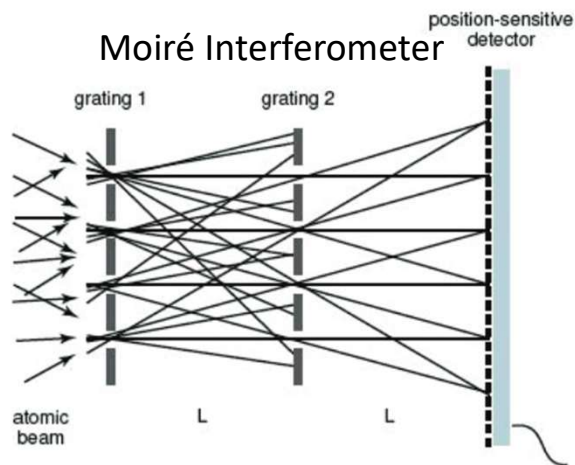
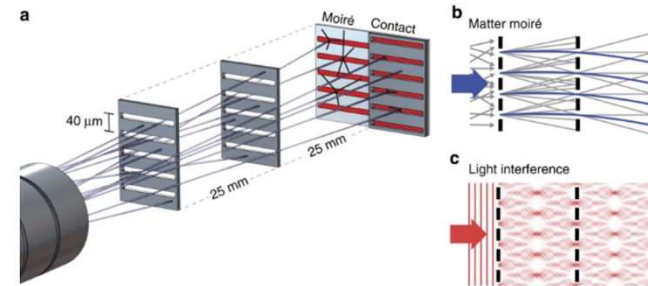
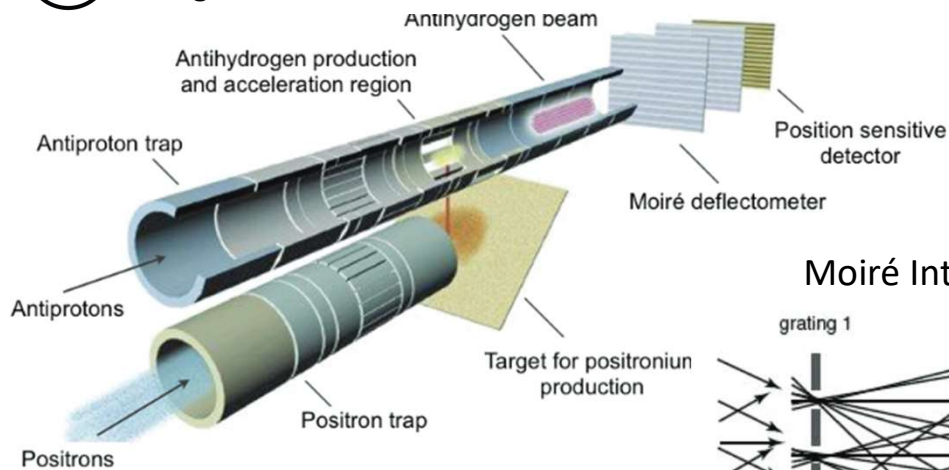


D. P. van der Werf, Antimatter and Gravity (WAG 2013) **30** (2014)
GBAR status report CERN-SPSC-2022-003 / SPSC-SR-302 (2022)

AEgIS

Use beam of \bar{H} for gravity measurement

\bar{H} AEgIS EXPERIMENT



First used to measure force on antiprotons
 $530 \pm 50 \text{ aN (stat.)} \pm 350 \text{ aN (syst.)}$ in 2014
 Next antihydrogen \rightarrow 100 mK required, 1% accuracy sought

S. Aghion et al., *Nature Communications* **5** 4538 (2014)
 P. Scampoli et al., *Modern Physics Letters A* **29** 17 (2014)
 A. Kellerbauer et al., *NIM B* **226** 3 (2008)

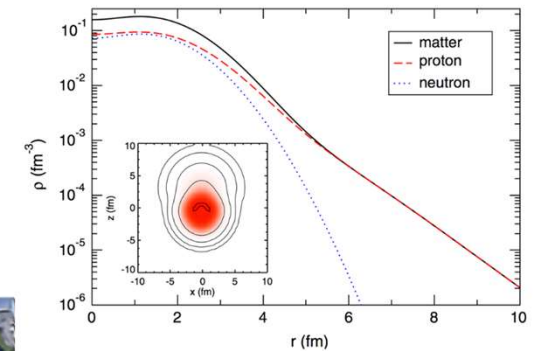
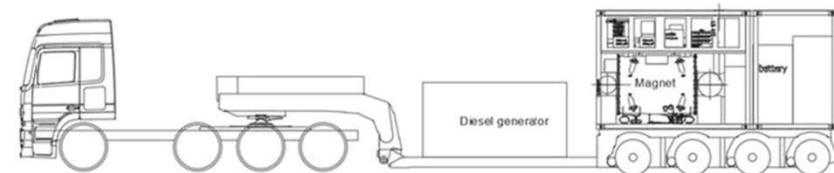
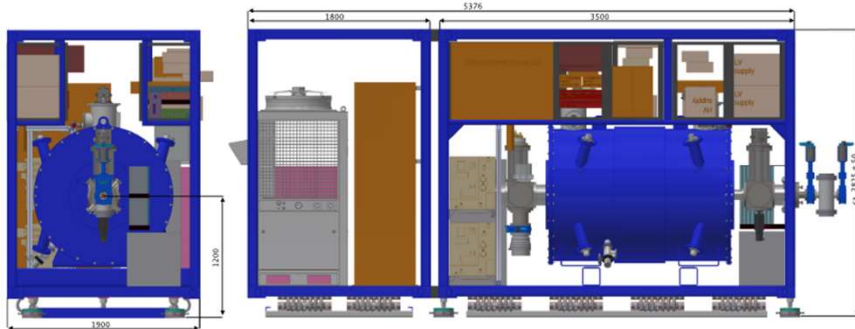
Taking antimatter out of the lab

PUMA

Take 10^9 antiprotons from the antimatter factory to ISOLDE

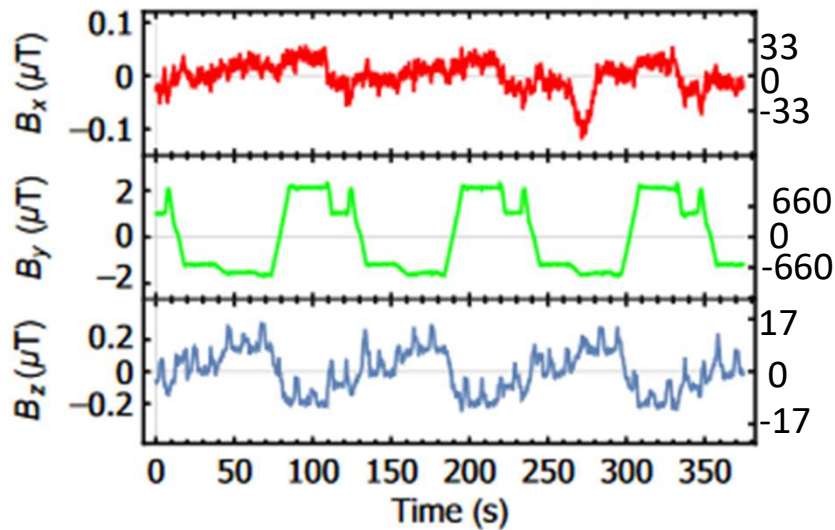
Some nuclei at the limits of $N > Z$ have a neutron halo where one or more neutrons are found far outside the nucleus.

Others have neutron skins, where the density of neutrons is larger than protons at the nuclear surface – antiproton annihilation study these effects



BASE-STEP

BASE trying to measure frequencies to parts-per-trillion level



Magnetic field fluctuating in the background up to one million times more strongly

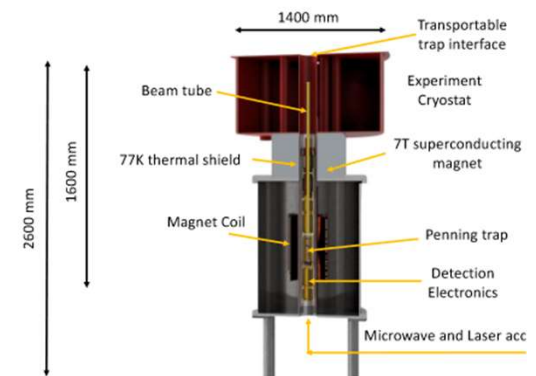
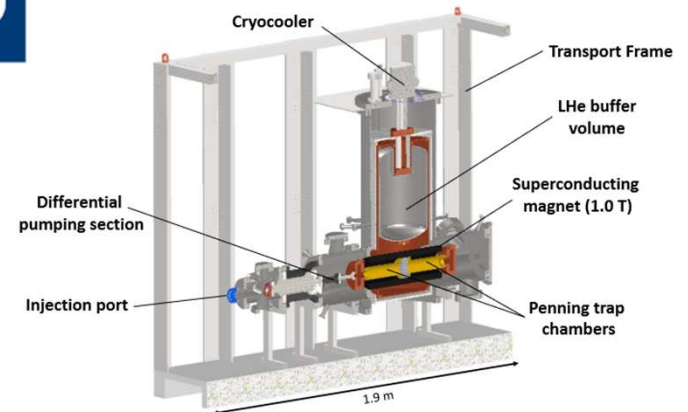
Hard to push the limits in this environment



Take the antimatter somewhere quiet

Fractional magnetic field fluctuations (ppb)

Inject into a separate magnet in a quiet lab



Should we be worried?

EXPRESS 

Antimatter bombs: Could antimatter weaponry wipe out all life on Earth? Expert weighs in Wed 21 Jul 2021

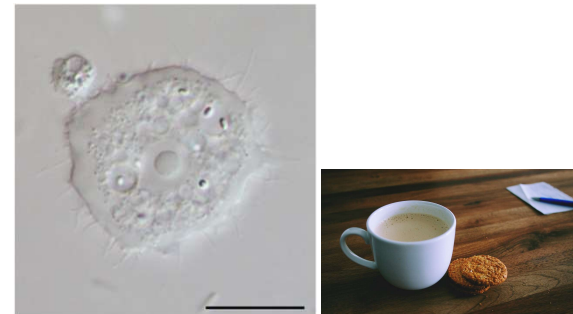
NO!

Professor Robson said: "The idea you can produce masses of antimatter and make a bomb from it or something is not realistic. It's not something anyone needs to worry about."

One billion antiprotons annihilating

$$E = mc^2 = (2 \times 1 \times 10^9 \times 1.6 \times 10^{-27})c^2 = 1 \text{ nJ}$$

1nJ can heat 3 picogram of water from 20->100 °C



About enough to make an espresso for an amoeba

(2015). "An update on *Acanthamoeba* keratitis: diagnosis, pathogenesis and treatment". *Parasite* **22**: 10.

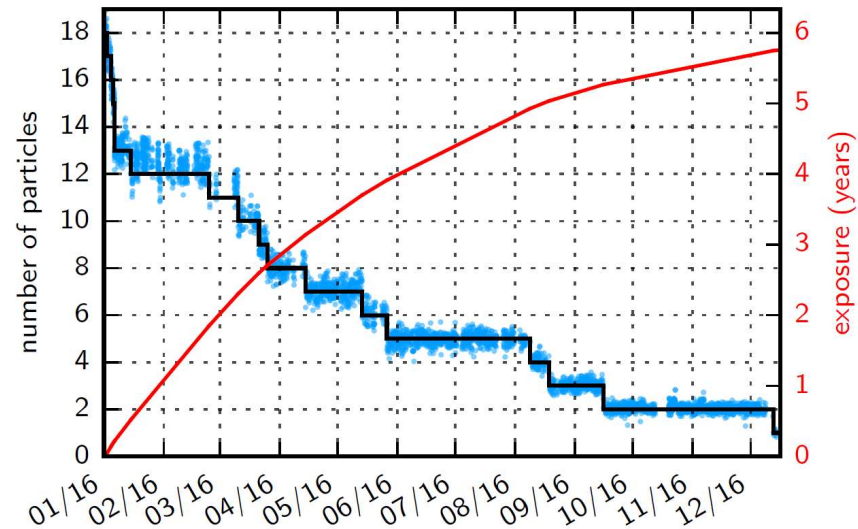
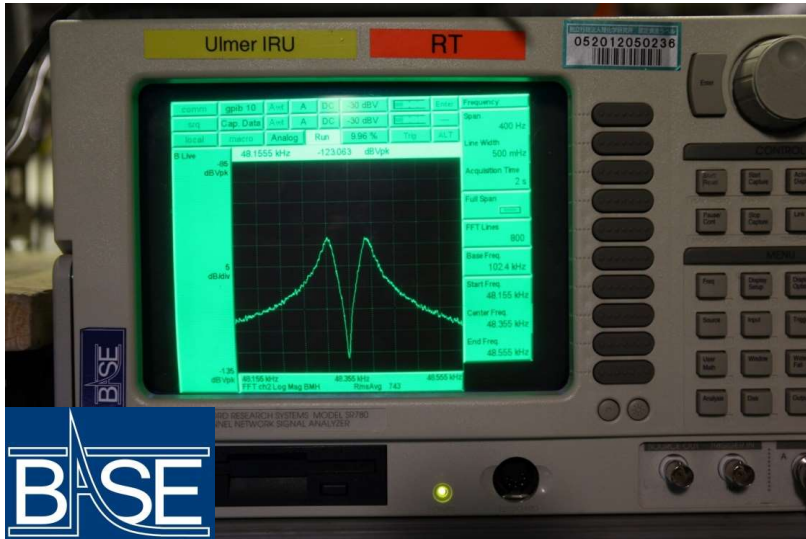
Thank you

Thanks to Stefan Ulmer, Christian Smorra & Andi Mooser for providing slides and materials for these lectures

And thank you for listening

Storing antiprotons

BASE holds record for antiprotons stored from 03.11.2015 – 22.12.2016



- Storage of antiprotons for more than one year: **405.5 days**
- Extraction of single particles by a potential tweezer scheme

Inversion of the baryon asymmetry:

Antibaryon density: $\sim 10^8/\text{cm}^3$ $V < (50 \mu\text{m})^3$

Baryon density: $\sim 1 / \text{cm}^3$ $p < 10^{-16}$ Pa

C. Smorra et al., Int. J. Mass Spectr. **389**, 10 (2015).

S. Sellner et al., New J. Phys. 19, 083023 (2017).