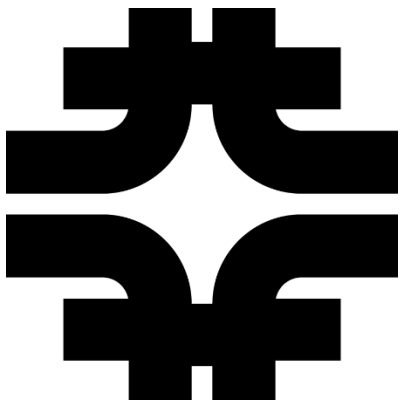
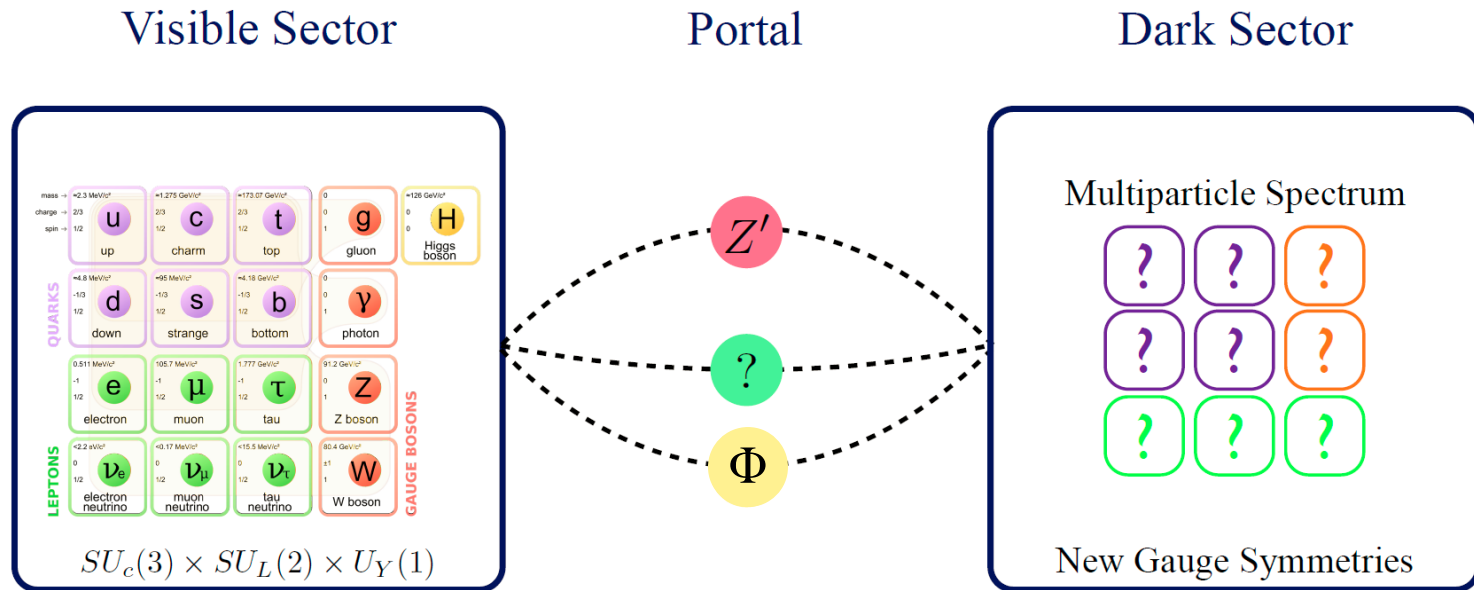


Semivisible Jets at CMS

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(Fermilab)
July 5, 2022



Hidden Sectors



- Simplest assumption: dark matter consists of a single species of weakly interacting massive particles
 - No observation of WIMPs → look for new models and phenomenology
- Dark matter may consist of multiple species of composite particles interacting via new, dark forces
 - Visible matter is mostly composite particles & has similar density to DM

Strongly Coupled Models

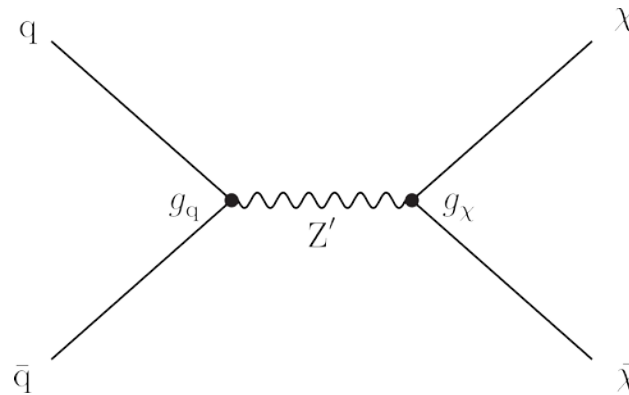
- New “dark QCD” force, $SU_{\text{dark}}(N_c^{\text{dark}})$ (carried by dark gluons) with scale Λ_{dark}
- N_f^{dark} flavors of (fermionic) dark quarks χ_i (charged under $SU_{\text{dark}}(N_c^{\text{dark}})$)
- Dark quarks *hadronize* to form dark mesons and baryons \rightarrow “dark showers”



- Some dark hadrons may be *stable* because of conserved quantities
 - Dark baryon number, dark isospin number, etc.
 - DM candidates!
- Other dark hadrons decay back to SM (through virtual mediators)
 - Leads to novel phenomenology

Production

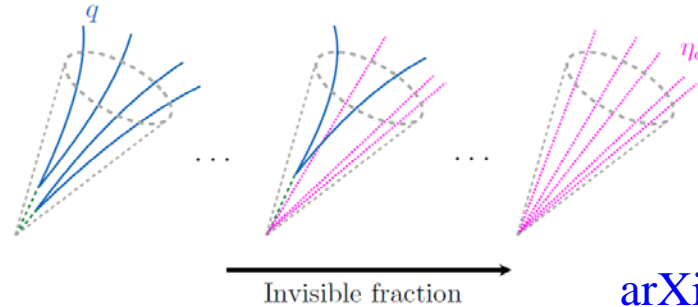
- Hidden sector couples to SM weakly via massive mediator: Z' from broken $U(1)$, vector, leptophobic, couplings g_q, g_χ



- Coupling choices aligned with LHC DM Working Group:
 - $g_q = 0.25$
 - $g_\chi = 1.0/\sqrt{(N_c^{\text{dark}} N_f^{\text{dark}})} = 0.5$
 - $B_{\text{dark}} = 47\%$, $\Gamma_{Z'}/m_{Z'} = 5.6\%$
 - Same as LHC DM models w/ $g_{\text{DM}} = 1.0$

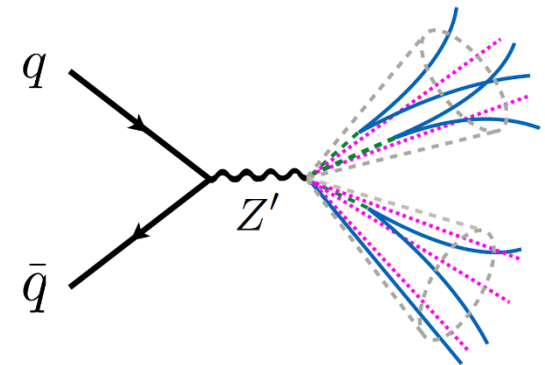
Decay

- Fraction of stable hadrons r_{inv} may vary from 0 to 1
 - Decreases w/ dark quark mass splitting, increases w/ N_f^{dark}
- Jets that contain *mix of visible and invisible particles* (prompt decays)
 - *Not covered* by existing searches for dijet resonances, $p_T^{\text{miss}} + \text{ISR}$



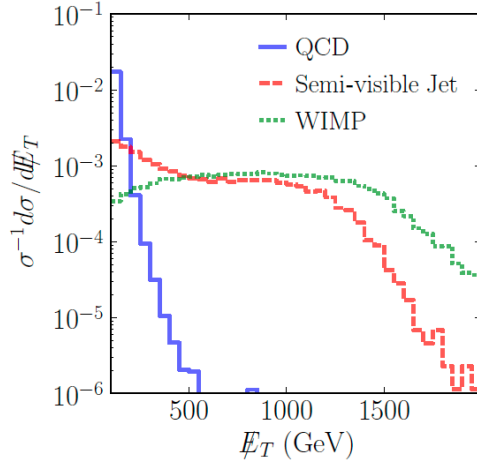
[arXiv:1707.05326](https://arxiv.org/abs/1707.05326)

- $Z' \rightarrow \chi\chi \rightarrow$ dark hadrons \rightarrow SM quarks \rightarrow SM hadrons
 - **Decay to SM** \rightarrow two high- p_T , *wide* jets
 - ρ_{dark} : democratic decay
 - π_{dark} : mass insertion decay (prefer heavy flavor)
 - $N_c^{\text{dark}} = 2, N_f^{\text{dark}} = 2, m_\chi = 1/2 m_{\text{dark}}$

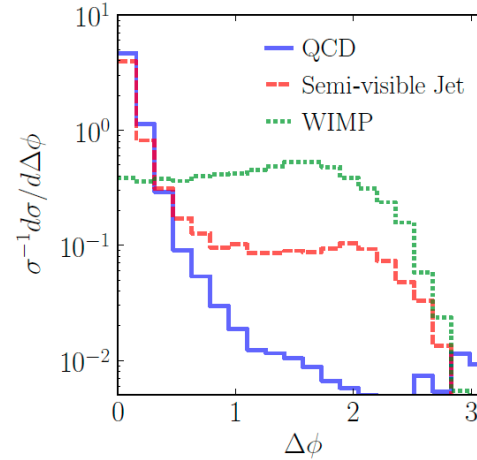


Resonant Search

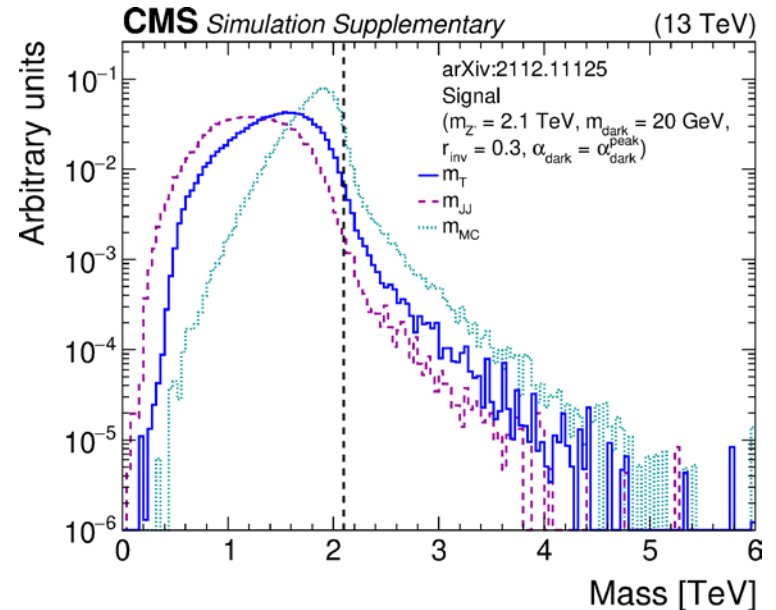
- Kinematic signature: Less missing energy than WIMPs, aligned w/ jet



[arXiv:1503.00009](https://arxiv.org/abs/1503.00009)

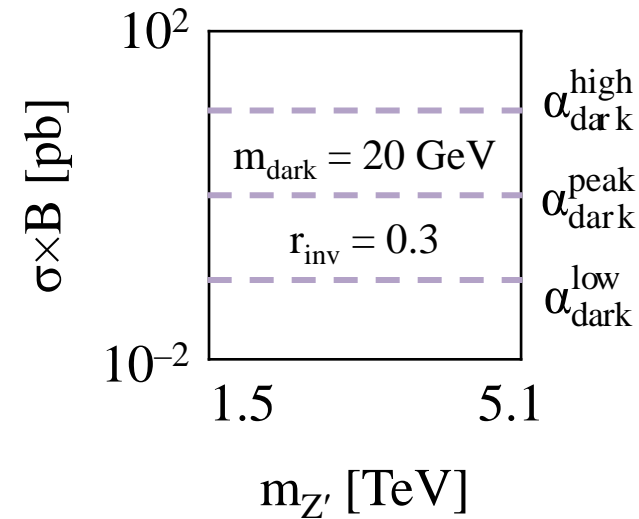
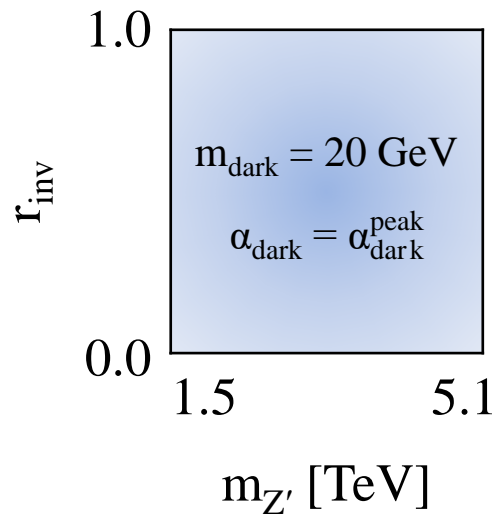
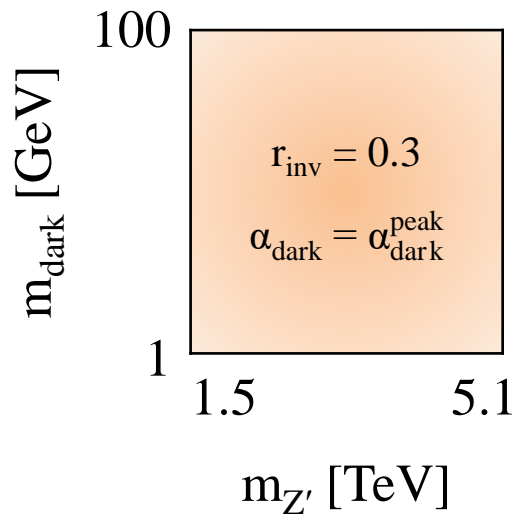


- Bump hunt in $m_T(\text{JJ}, p_T^{\text{miss}})$
 - Kinematic edge at m_Z ,
 - Better resolution than m_{JJ}
 - SM backgrounds have steeply falling distributions



Signal Models

- Parameters varied: $m_{Z'}$, m_{dark} (dark hadron mass scale), r_{inv} , α_{dark}
 - α_{dark} : running coupling of dark QCD (alternate form of scale Λ_{dark})
 - $\alpha_{\text{dark}}^{\text{peak}}$ maximizes dark hadron multiplicity (depends on m_{dark})
 - “Empirical” relationship derived from Pythia
 - Variations: $\alpha_{\text{dark}}^{\text{high}} = 3/2 \alpha_{\text{dark}}^{\text{peak}}$, $\alpha_{\text{dark}}^{\text{low}} = 1/2 \alpha_{\text{dark}}^{\text{peak}}$
- Three 2D scans ($m_{Z'}$ vs. m_{dark} , r_{inv} , α_{dark}) \rightarrow 475 points
 - Benchmark values: $m_{\text{dark}} = 20 \text{ GeV}$, $r_{\text{inv}} = 0.3$, $\alpha_{\text{dark}} = \alpha_{\text{dark}}^{\text{peak}}$
- 4D scan with same grid of values would be 8208 points



Dual Strategy

- Dark QCD theories are very complicated
 - Need to make choices about numerous parameters
 - Plus modeling of hadronization/fragmentation, etc.
- First search for jets aligned with p_T^{miss} → maximize *generality* & *sensitivity*

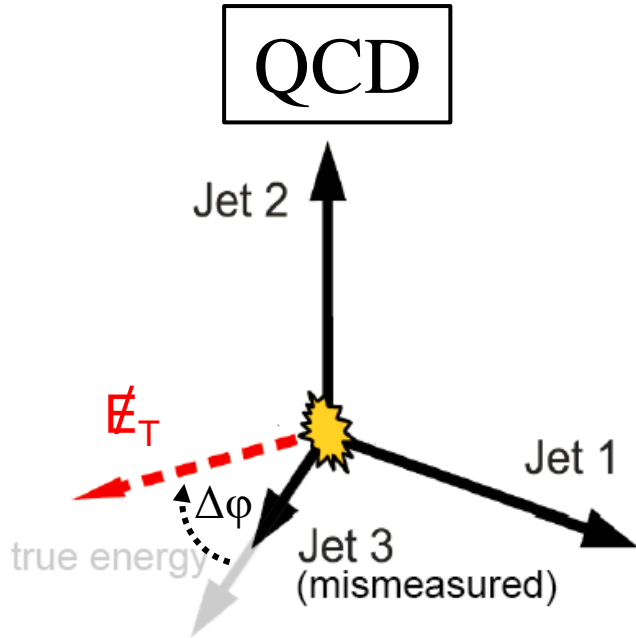
“Inclusive” search

- Use only event-level kinematic variables
- Results apply to any model with similar kinematic behavior

“BDT-based” search

- Employ machine learning for optimized semivisible jet tagger
- Assumes chosen signal models are “correct”

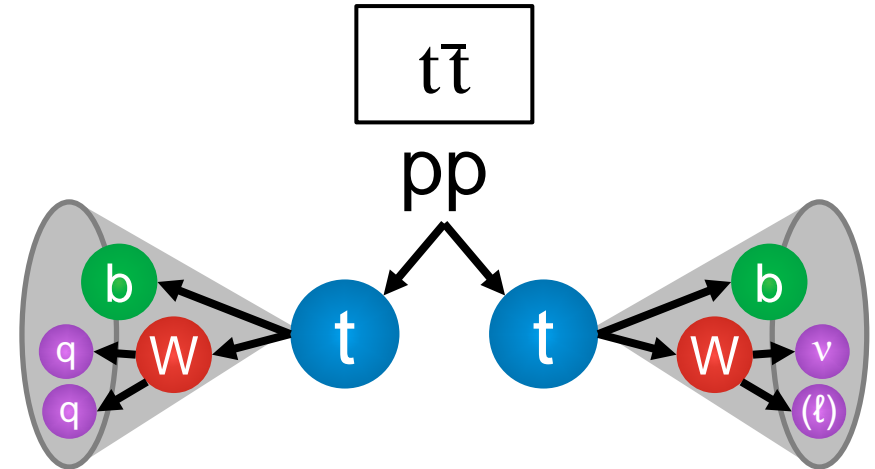
Backgrounds



- Jet mismeasurement induces \cancel{E}_T aligned with jet
- Major background

W($\ell\nu$)+jets

- Lost lepton or hadronic τ
- Less likely than $t\bar{t}$ to mimic semivisible jet, but higher σ

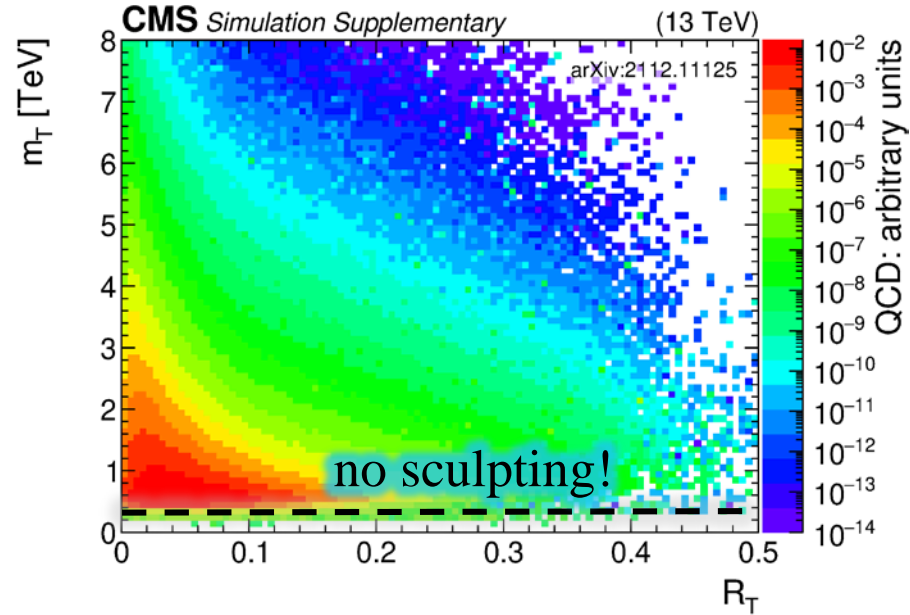
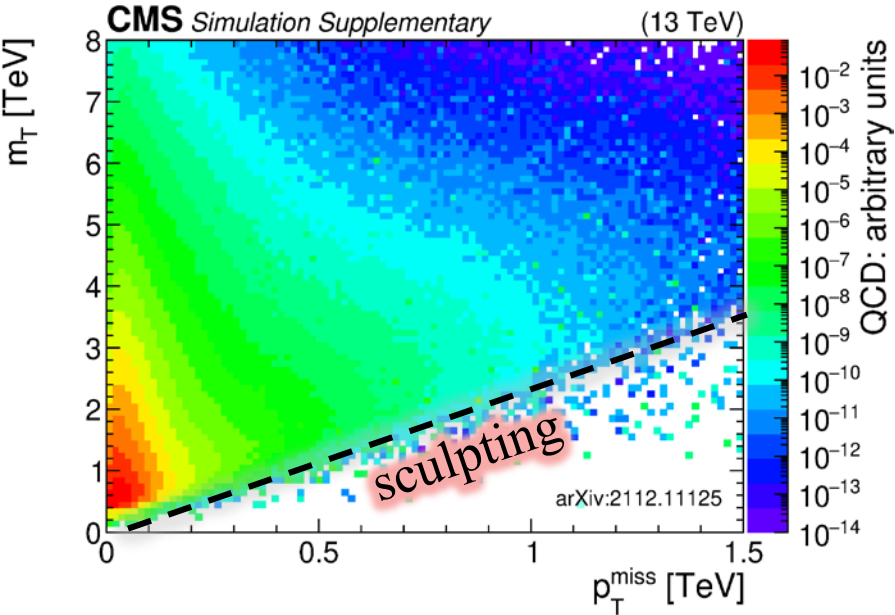


- Wide, high- p_T jets: boosted tops
- “Lost” lepton ℓ : out of acceptance, can’t veto (or hadronic τ)
- Neutrino aligned w/ wide jet: mimics semivisible jet

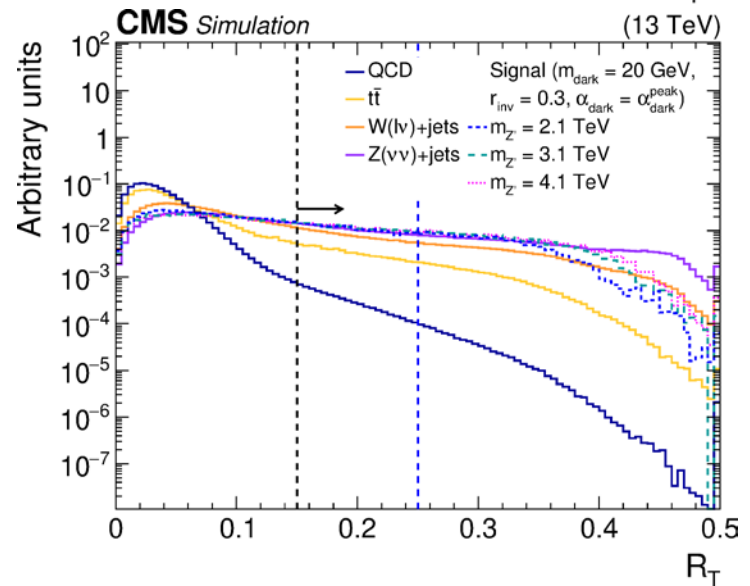
Z($\nu\nu$)+jets

- Real \cancel{E}_T from $\nu\nu$, but least likely to align with jet

Mass Sculpting

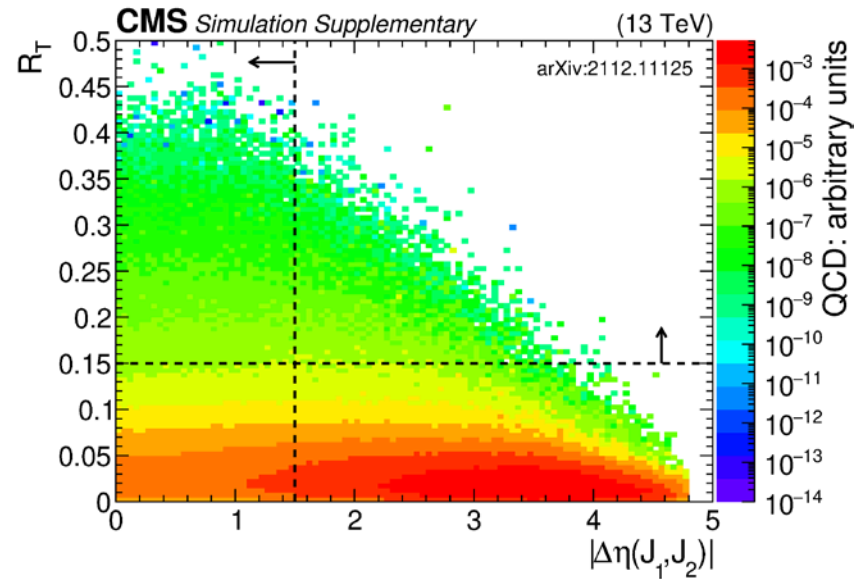
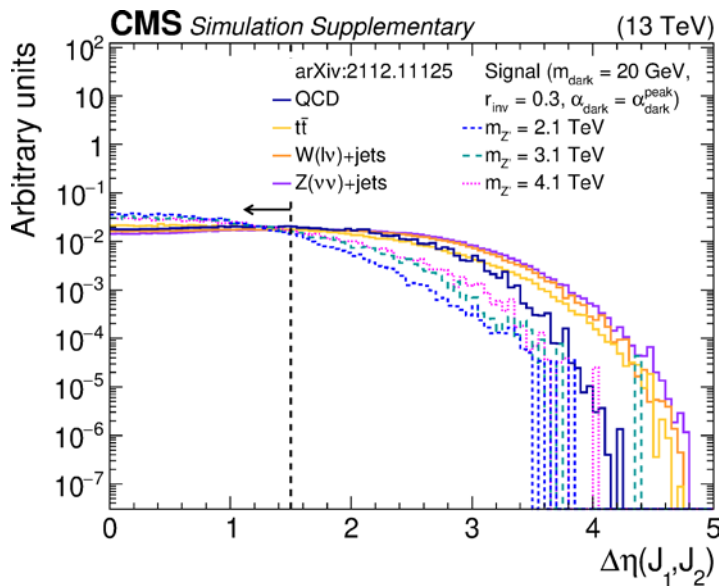
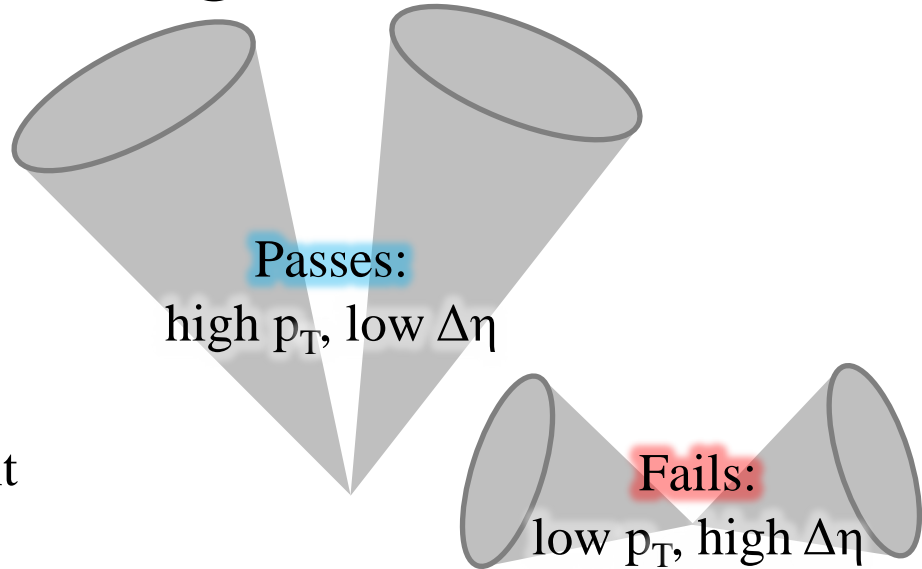


- Avoid/minimize direct cuts on m_T
ingredients: p_T^{miss} , jet p_T
 - Relative variable (“transverse ratio”):
$$R_T = p_T^{\text{miss}}/m_T$$
 - Reject QCD background without shifting m_T peak



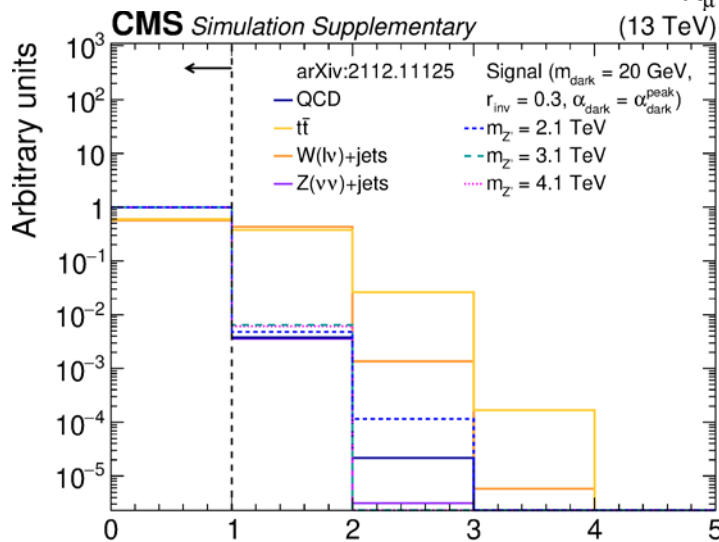
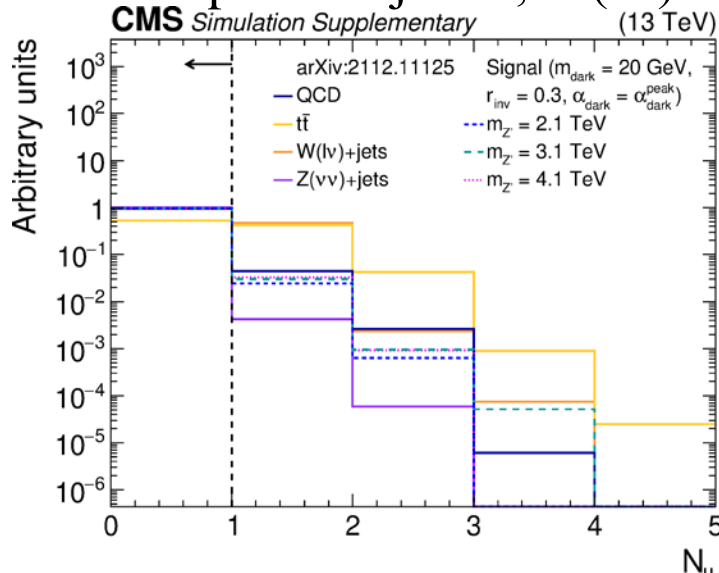
Triggering

- Trigger on jet p_T , H_T
 - Require low $\Delta\eta(J_1, J_2)$ for high efficiency
- Usually improves signal sensitivity
 - Most t -channel QCD events already rejected by R_T requirement
- $m_T > 1500$ GeV for trigger efficiency

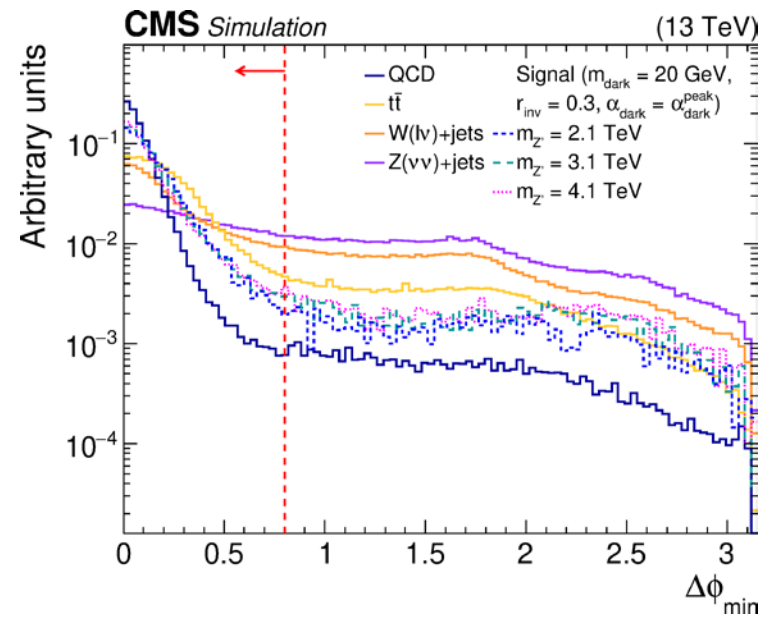


Electroweak Rejection

Veto leptons: reject $t\bar{t}$, $W(\ell\nu)$

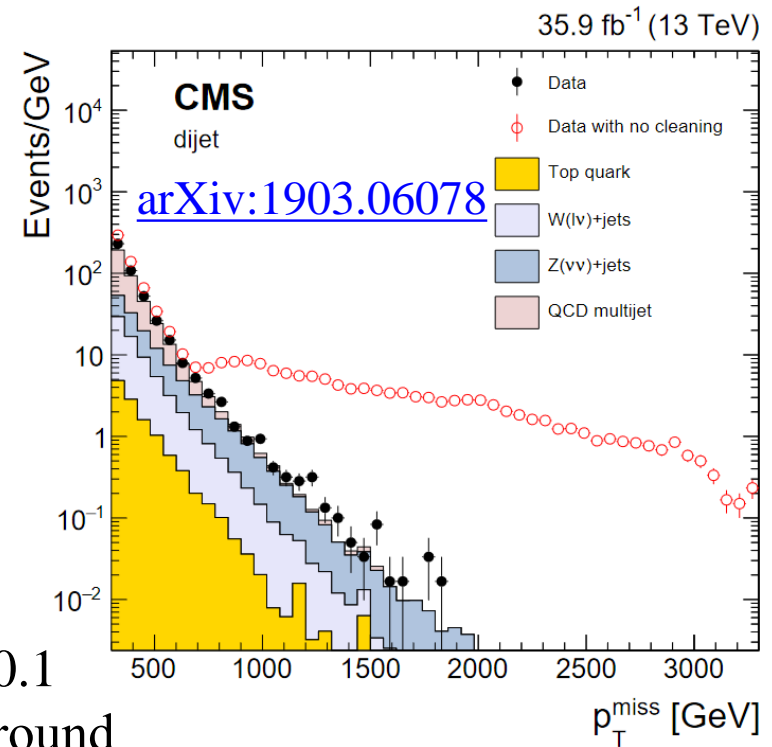


Require low $\Delta\phi_{\text{min}}(J_{1,2}, p_T^{\text{miss}})$:
Reject $t\bar{t}$, $W(\ell\nu)$, $Z(\nu\nu)$



Instrumental Backgrounds

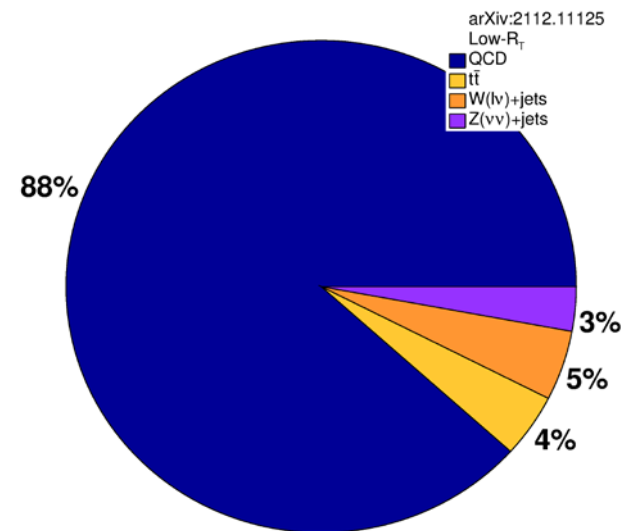
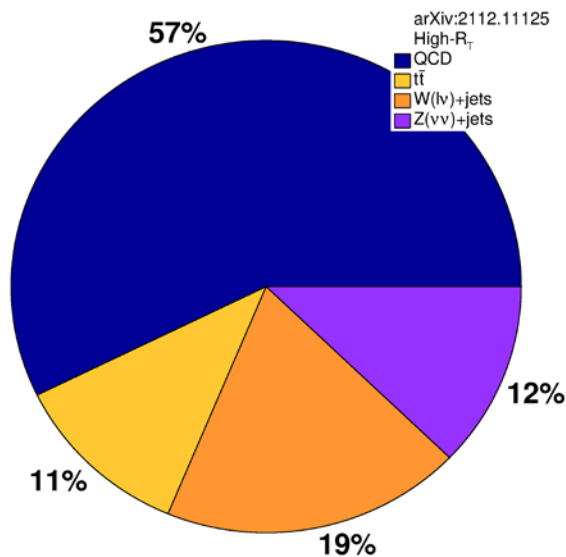
- Centrally-maintained filters reject *most* instrumental sources of artificial high- p_T^{miss} events
 - But low- $\Delta\phi$ region ignored by almost all analyses: filters not tuned here
- Major source of jet mismeasurement: nonfunctional ECAL readout channels (“dead” or “hot” cells)
 - Custom filter vetoing events w/ narrow (AK4) jets w/ $\Delta R(j_{1,2}, \text{nonfunctional}) < 0.1$
 - reject additional 40% of QCD background
 - Signal efficiency 95%
- Misreconstructed jets near barrel-endcap gap in ECAL
 - Appear at high p_T^{miss} and high m_T
 - Veto events w/ $p_T(j_1) > 1000$ GeV and $f_\gamma(j_1) > 0.7$



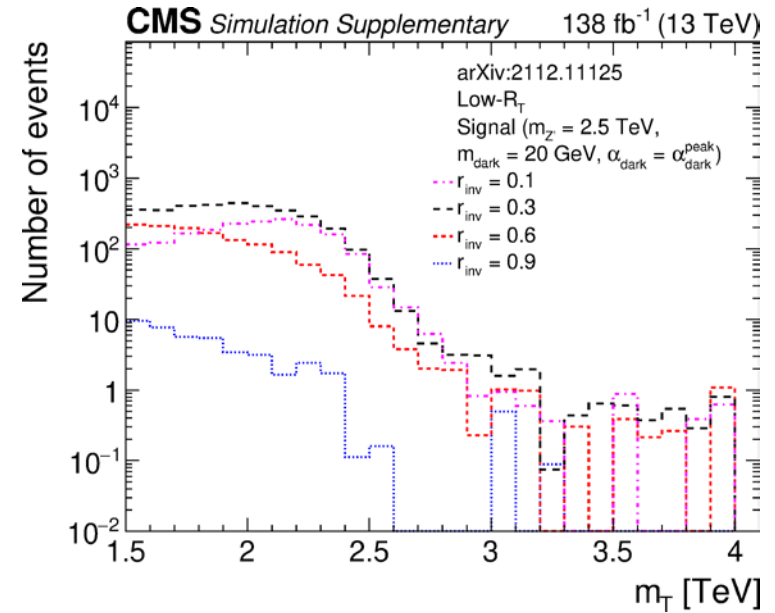
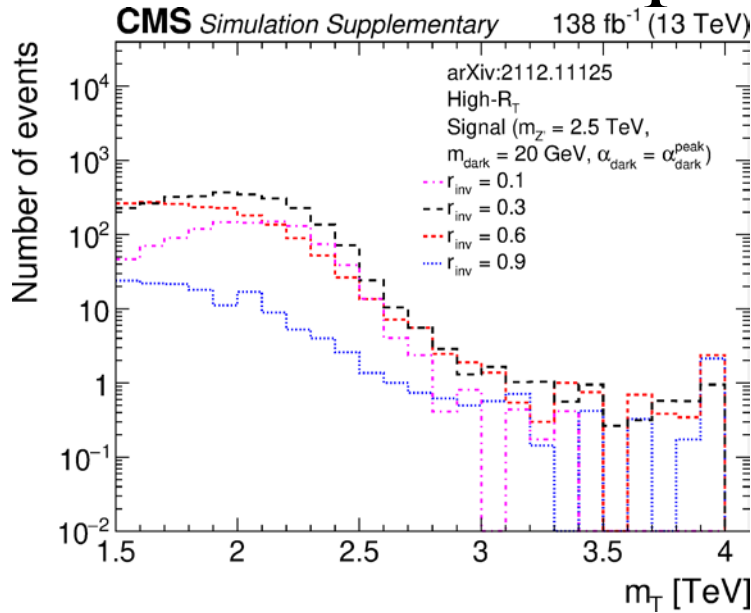
Inclusive Signal Regions

- With all inclusive selection requirements applied:
- If only one signal region were defined, high- R_T ($R_T > 0.25$) would have optimal significance
- Adding separate region low- R_T ($0.15 < R_T < 0.25$) improves expected performance

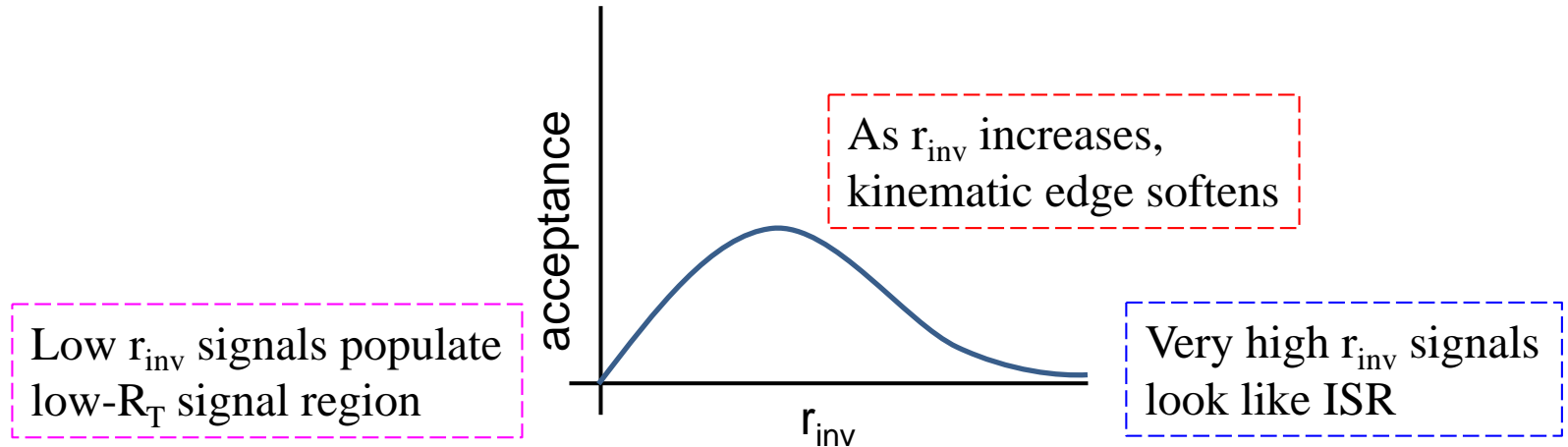
Process	Efficiency [%]
QCD	0.000016
$t\bar{t}$	0.0060
$W(\ell\nu)+\text{jets}$	0.0029
$Z(\nu\nu)+\text{jets}$	0.0085
signal	~ 17



m_T Variations

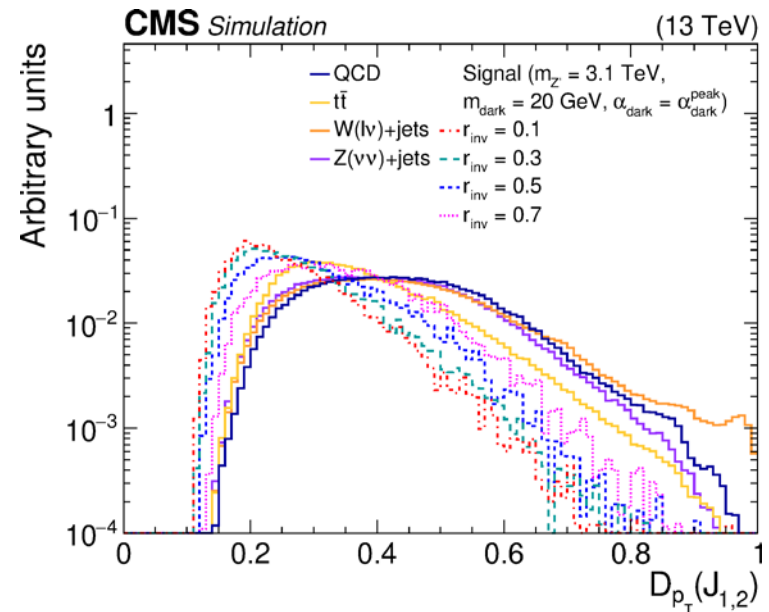
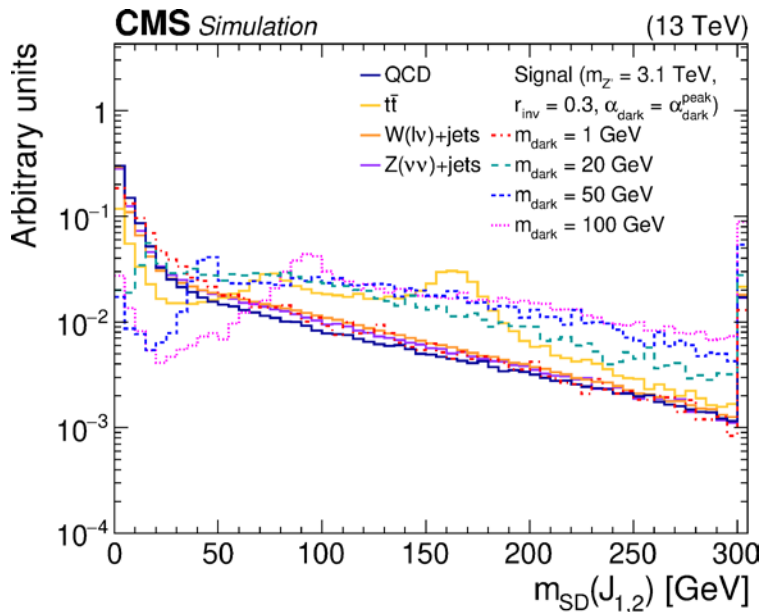


- r_{inv} has largest impact on signal mass distributions
 - α_{dark} has minor impact; m_{dark} has very little impact



Tagging Semivisible Jets

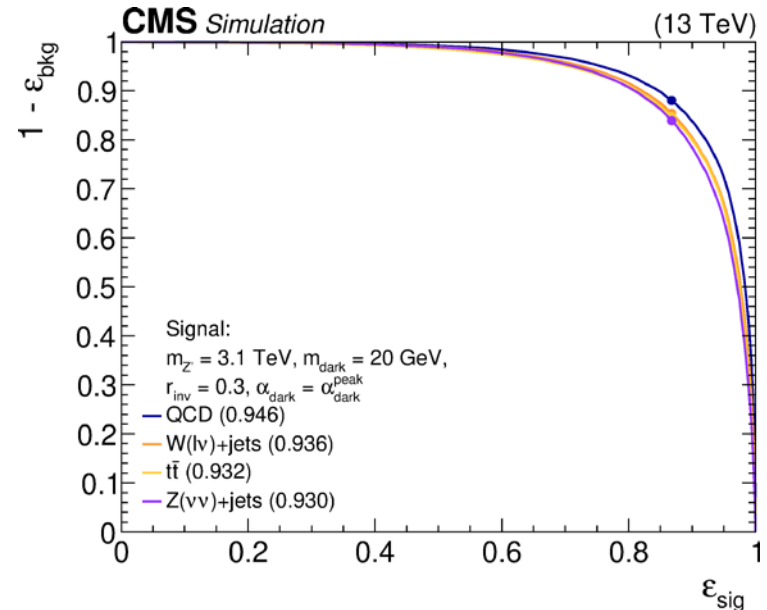
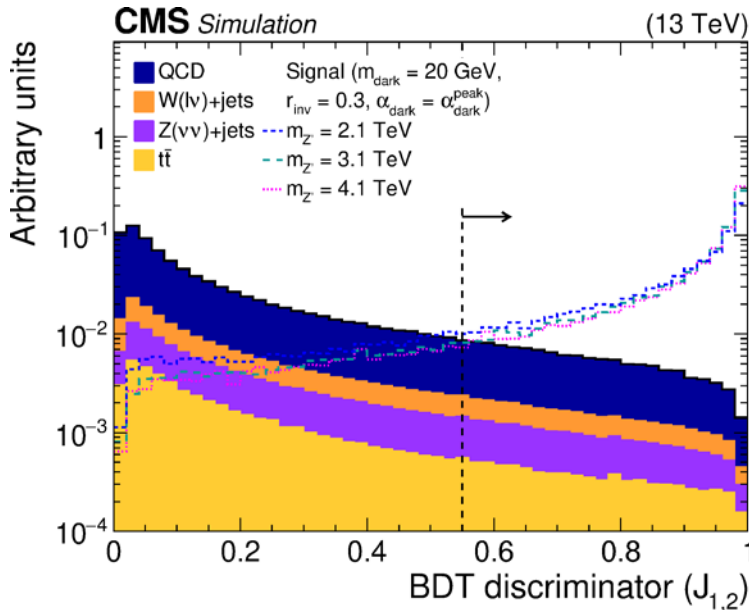
- Various jet substructure variables (& $\Delta\phi(J, p_T^{\text{miss}})$) can weakly discriminate between semivisible jets and SM background jets
 - Heavy object tagging: $m_{\text{SD}}, \tau_{21}, \tau_{32}, N_2^{(1)}, N_3^{(1)}$
 - Quark-gluon discrimination: $D_{p_T}, \sigma_{\text{major}}, \sigma_{\text{minor}}, \text{girth}$
 - Flavor (energy fractions): $f_\gamma, f_{h^\pm}, f_{h^0}, f_e, f_\mu$
- Combine useful variables into a BDT for strong discrimination!
 - Background: equal mix of QCD and $t\bar{t}$; signal: mix of many models
 - Reweight background jet p_T spectrum to match signal: avoid sculpting



Tagger Performance

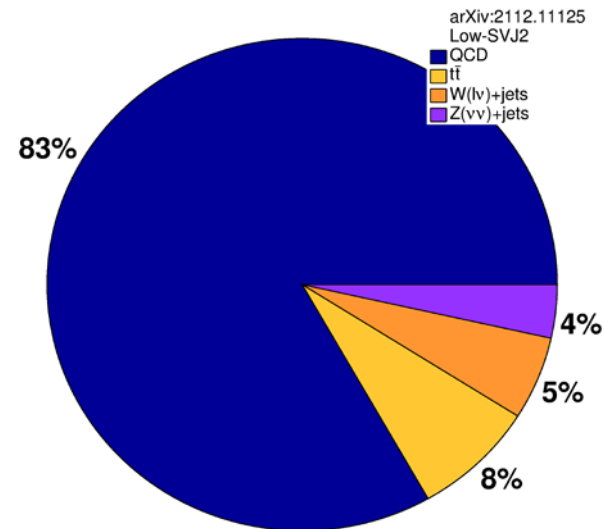
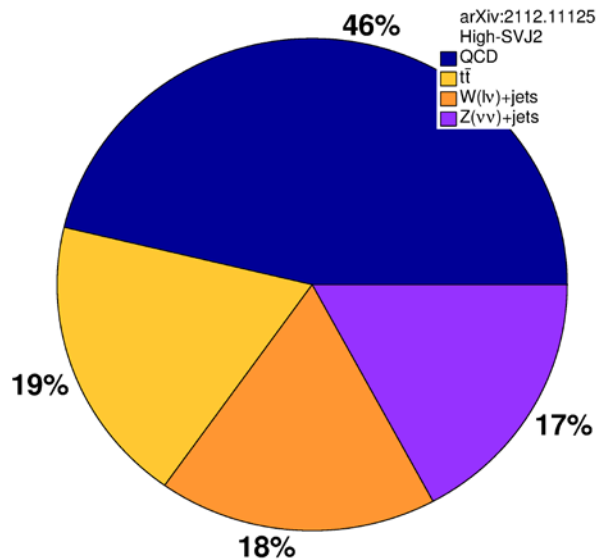
$m_{Z'} = 3.1 \text{ TeV}, m_{\text{dark}} = 20 \text{ GeV},$ $r_{\text{inv}} = 0.3, \alpha_{\text{dark}} = \alpha_{\text{dark}}^{\text{peak}}$			
	Acc (WP = 0.5)	AUC	$1/\epsilon_B$ ($\epsilon_S = 0.3$)
QCD	0.881	0.947	651.4
$t\bar{t}$	0.881	0.931	270.6
$W(\ell\nu)+\text{jets}$	0.881	0.936	441.5
$Z(\nu\nu)+\text{jets}$	0.881	0.930	420.7

- Strong and consistent performance
 - Training on only QCD ($t\bar{t}$) caused misclassification of $t\bar{t}$ (QCD) jets at rate of 10–20%
 - Some inefficiency for signals with high or low m_{dark}
- Working point 0.55 chosen based on background estimation



BDT-based Signal Regions

- Start from inclusive signal regions (high- R_T , low- R_T)
- Require both leading wide jets to be tagged as semivisible
 - high-SVJ2, low-SVJ2 regions: strict subsets of inclusive regions
- Reduce background by factor ~ 60 while preserving signal



Background Estimation

- Estimate smoothly-falling SM backgrounds via analytic fit to m_T data
- Primary fit function:

$$x = m_T / \sqrt{s}$$

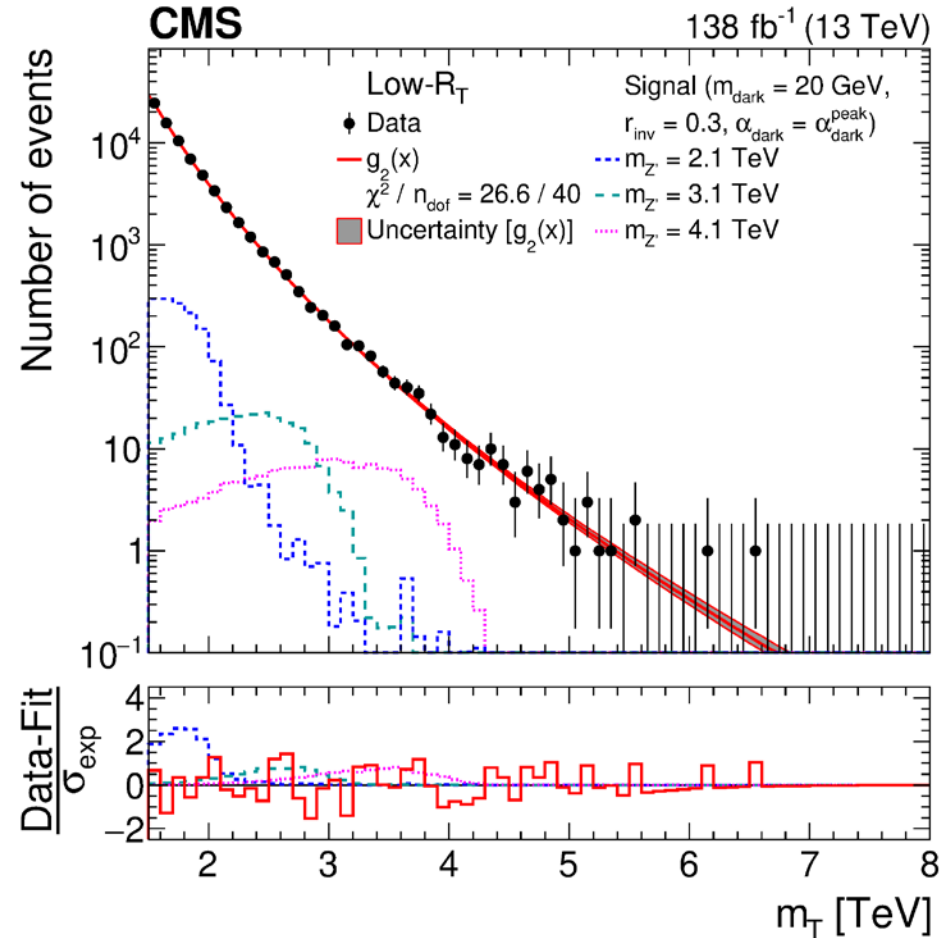
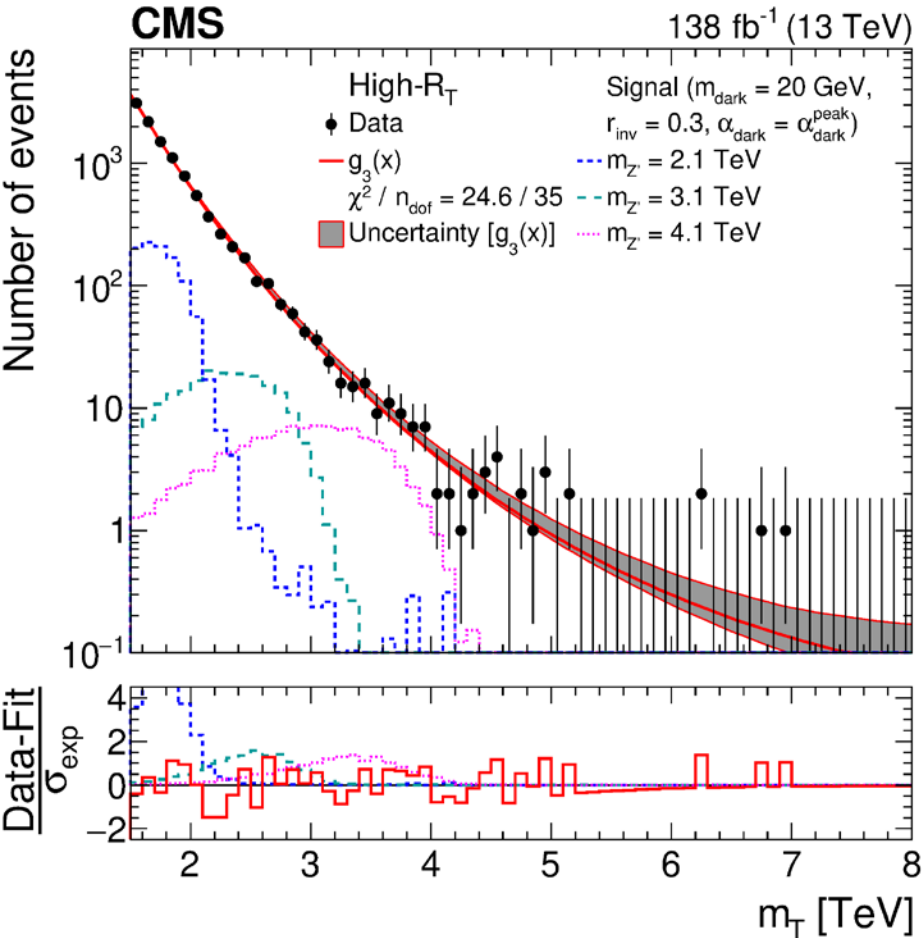
$$g(x) = \exp(p_1 x) x^{p_2(1+p_3 \log(x)(1+p_4 \log(x)(\dots)))}$$

- Perform fits varying sign and magnitude of initial parameter values (necessary to escape false minima)
- Optimal # parameters for each signal region determined w/ Fisher test
- Several secondary functions (from other resonant searches) employed for bias studies:
 - Ensure that chosen function can fit different possible data distributions
 - Generate toy data with secondary functions, fit w/ primary function
 - $b = (\sigma_{\text{ext}} - \sigma_{\text{inj}}) / \varepsilon_{\sigma_{\text{ext}}}$ should be normally distributed ($\mu = 0, \sigma = 1$)
 - $|\langle b \rangle| \leq 0.5$ in all cases \rightarrow fits are sufficiently unbiased

Optimal # Parameters

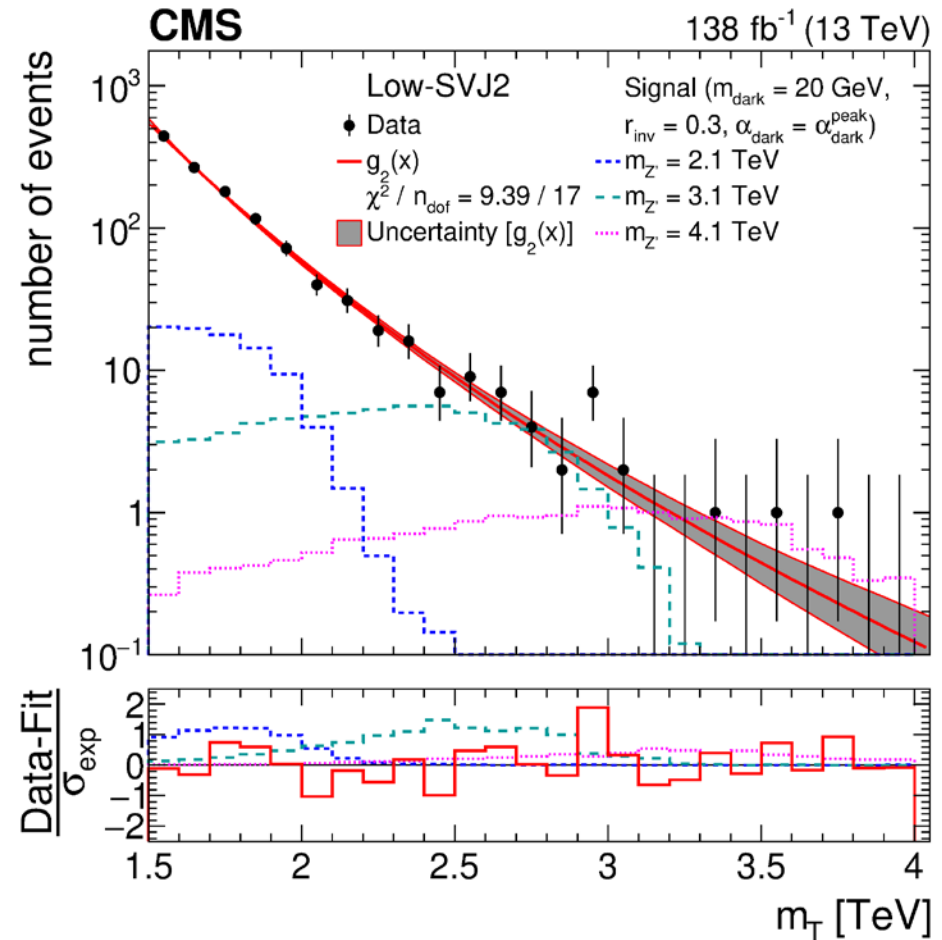
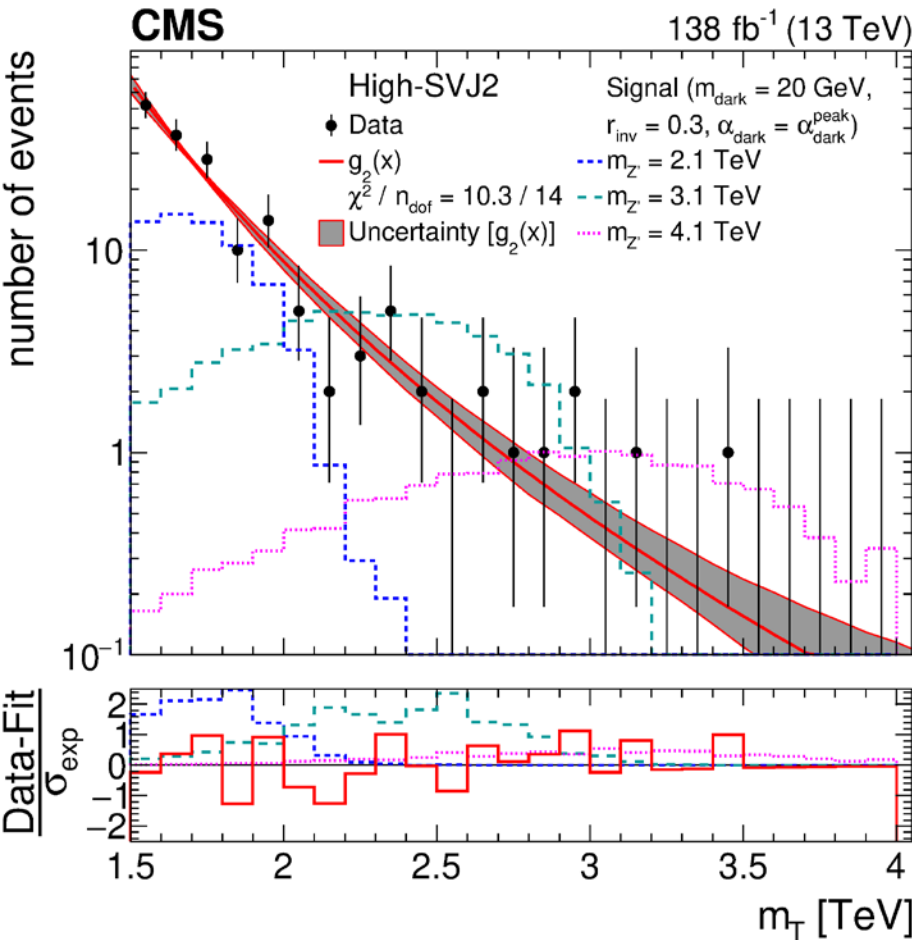
region	$g(x)$
high- R_T	3
low- R_T	2
high-SVJ2	2
low-SVJ2	2

Background Fits (inclusive)



- No significant deviations from SM
 - Small pulls, few if any cases of several contiguous pulls > 0
- Signals shown w/ cross section at observed limit

Background Fits (BDT-based)

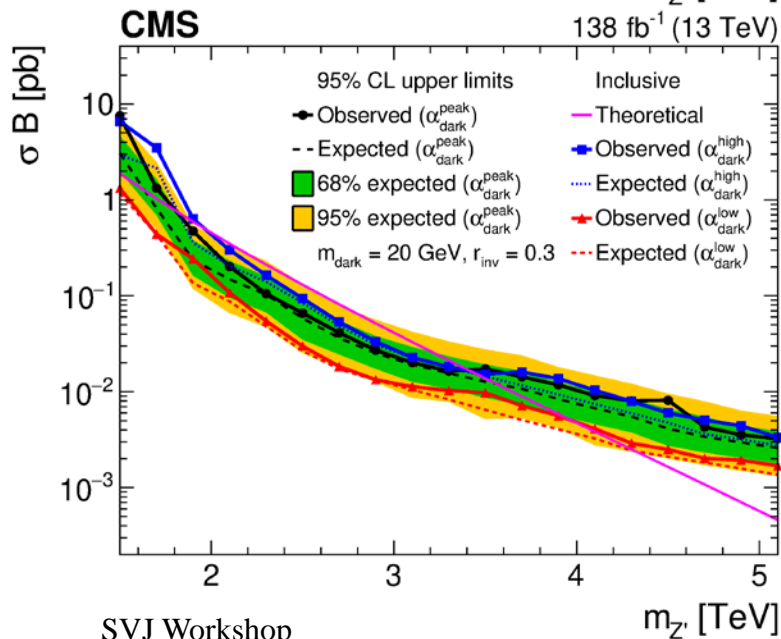
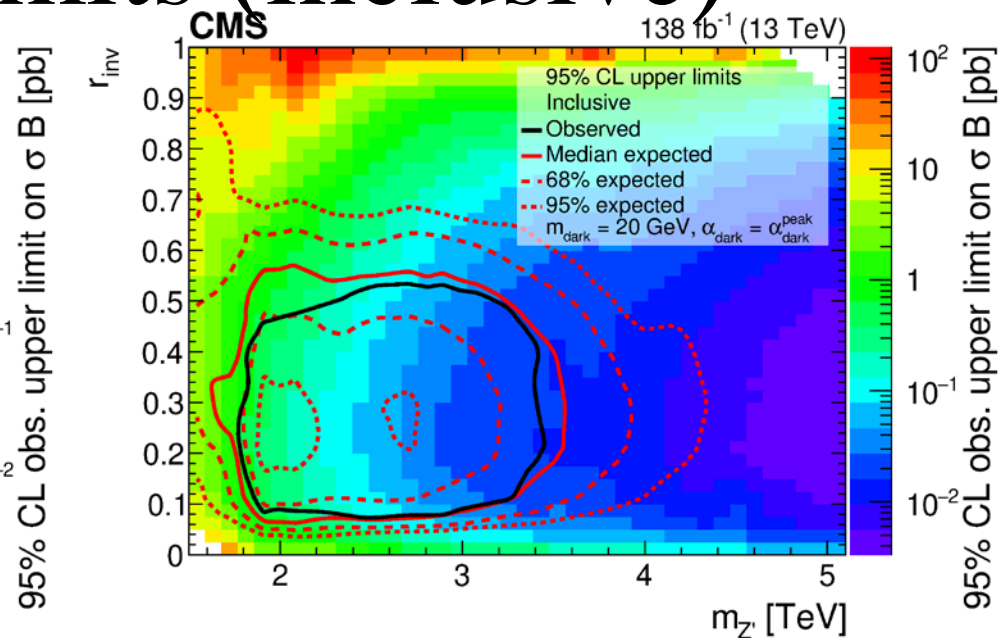
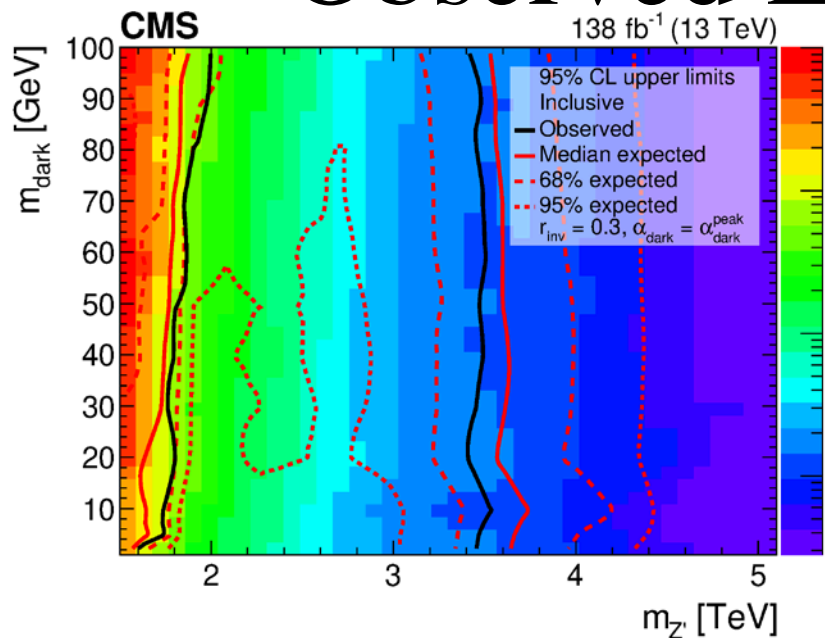


- No significant deviations from SM
 - Small pulls, few if any cases of several contiguous pulls > 0
- Signals shown w/ cross section at observed limit

Systematic Uncertainties

- Signal:
 - Experimental: (uncorrelated between years of data-taking)
 - Luminosity, trigger efficiency, **jet energy corrections** (up to 12%), jet energy resolution, pileup, statistical uncertainties in simulated samples
 - Theoretical: (correlated between years of data-taking)
 - PDFs, renormalization/factorization scale, parton shower modeling (ISR/FSR), **jet energy scale/composition** (up to 21%)
- Background:
 - Fit parameters: freely floating, uncertainties arise from statistical uncertainty in data
 - **Fit normalizations**: also freely floating, can change by up to 10%
→ *most impactful uncertainty*

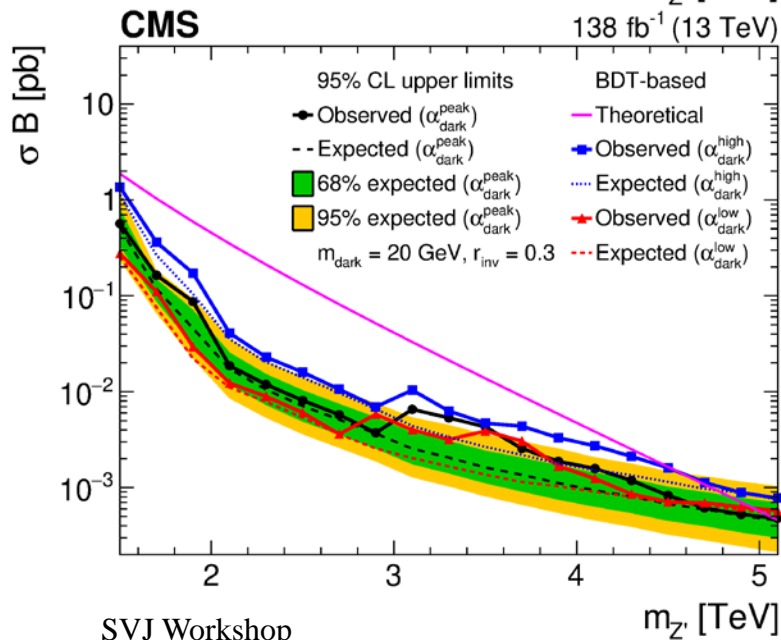
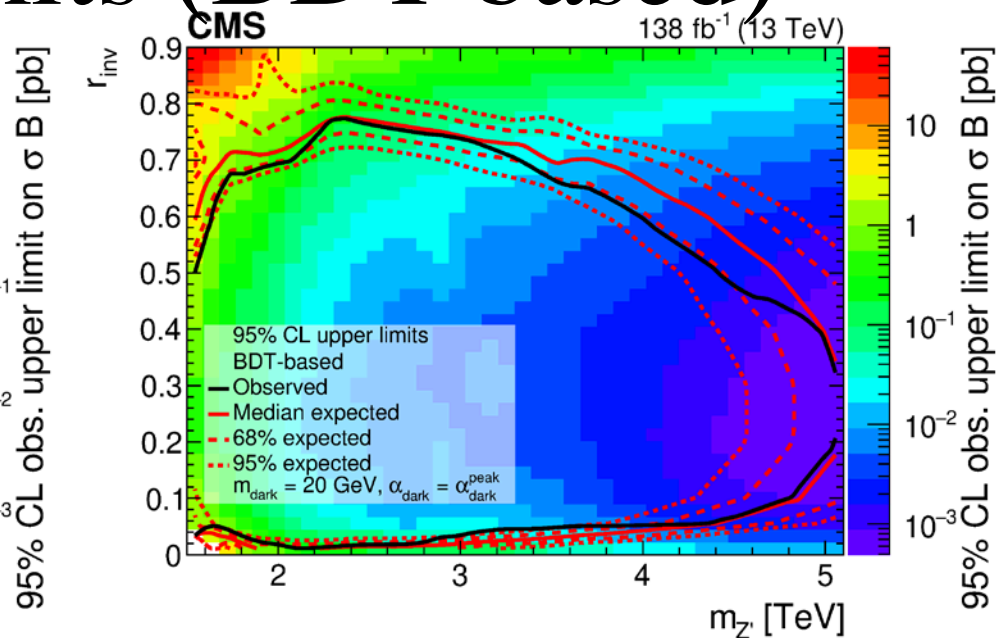
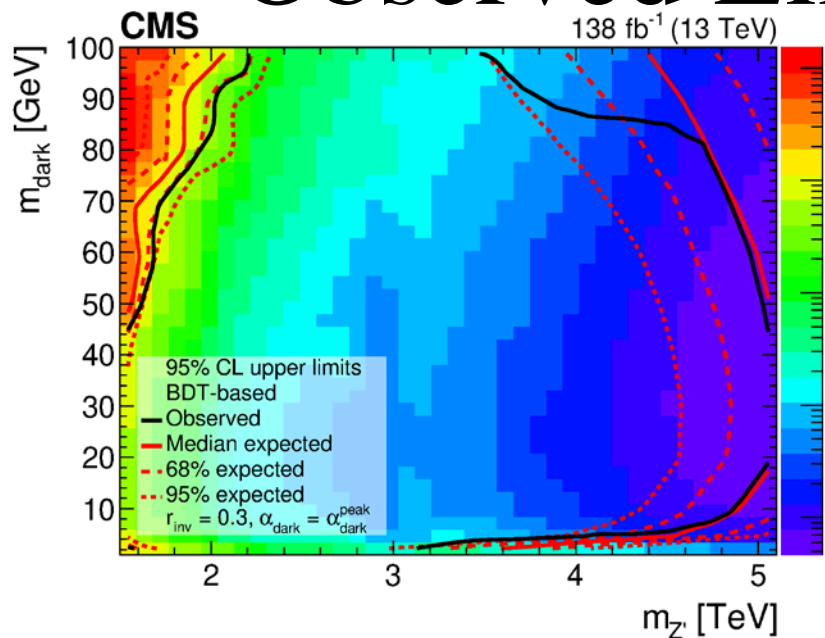
Observed Limits (inclusive)



Observed (expected) exclusions:

- $1.5 < m_{Z'} < 4.0 \text{ TeV}$ ($1.5 < m_{Z'} < 4.3 \text{ TeV}$)
- Depending on $m_{Z'}$:
 - $0.07 < r_{inv} < 0.53$ ($0.06 < r_{inv} < 0.57$)
 - All m_{dark}, α_{dark} variations

Observed Limits (BDT-based)

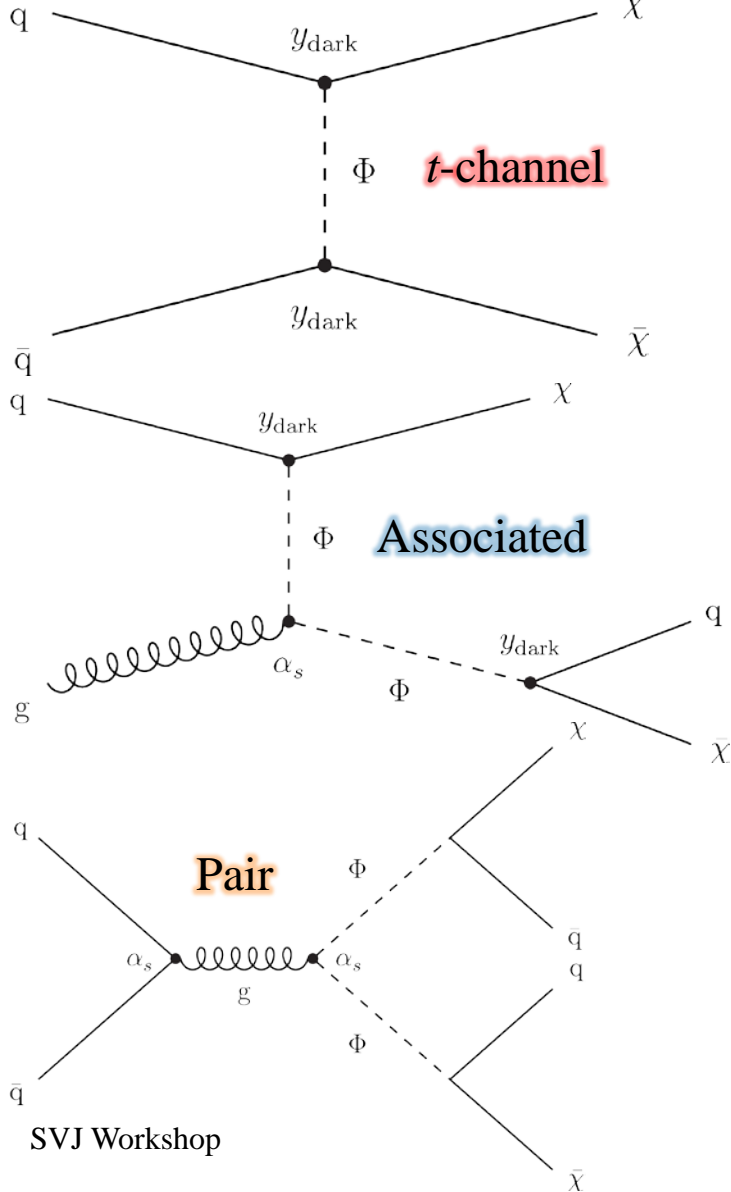


Observed (expected) exclusions:

- $1.5 < m_{Z'} < 5.1 \text{ TeV}$ ($1.5 < m_{Z'} < 5.1 \text{ TeV}$)
- Depending on $m_{Z'}$:
 - $0.01 < r_{\text{inv}} < 0.77$ ($0.01 < r_{\text{inv}} < 0.78$)
 - All $m_{\text{dark}}, \alpha_{\text{dark}}$ variations
- Signal parameters excluded for wider range in $m_{Z'}$ vs. inclusive search

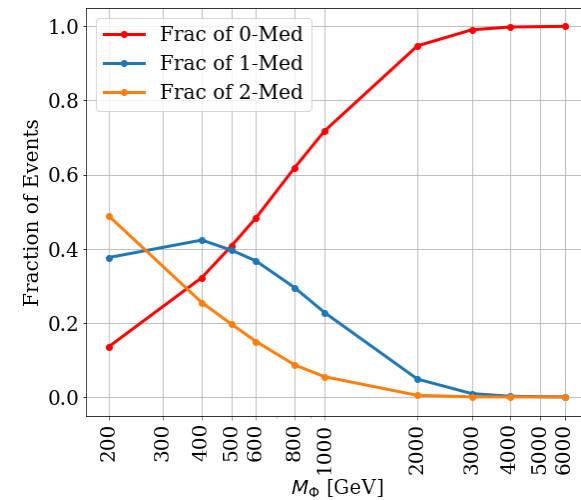
Future Semivisible Jet Searches

- Bifundamental mediator

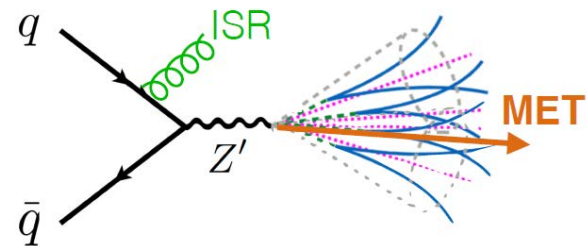


- Challenges:

- Additional parameter y_{dark}
- Non-resonant diagrams dominate as mediator mass increases

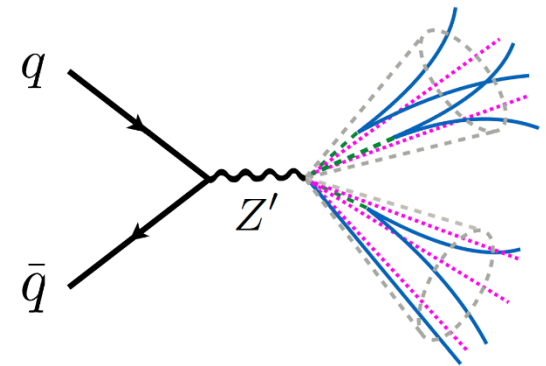


- Low-mass Z' mediators (boosted)



Conclusions

- CMS search directly excludes a large portion of semivisible jet model space for the first time
 - Sensitivity to a broad range of $m_{Z'}$, m_{dark} , r_{inv} values
- Dual strategy provides both generality and sensitivity
 - Inclusive search can be reinterpreted for any kinematically similar signal
 - BDT-based search improves background rejection by almost two orders of magnitude (first SVJ tagger applied to data)
- Ongoing search program targets different mediators, regions of model space
 - Will employ new techniques such as autoencoders to increase sensitivity and reinterpretability even further
 - Run 3 plans developing: opportunities to improve triggers, etc.
- Stay tuned for more SVJ results from CMS!



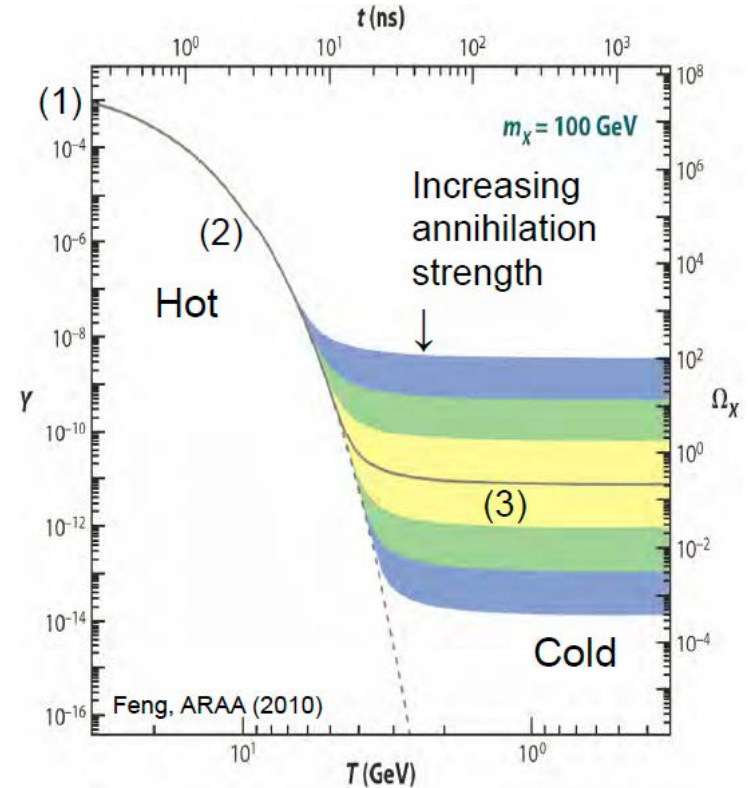
Backup

Strongly-Coupled Hidden Sector References

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Dark Matter Relic Abundance

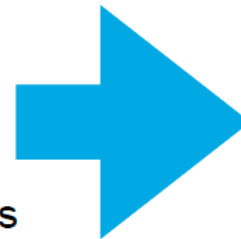
- Dark matter production, annihilation at equilibrium in early universe
- Universe expands and cools: stops DM production, then annihilation
- WIMPs imply fixed DM abundance (bottom)



$$\Omega_{\text{DM}} h^2 = 0.12$$

$$\Omega_{\text{DM}} h^2 = \frac{0.2 \times 10^{-9} \text{GeV}^{-2}}{\langle \sigma v \rangle}$$

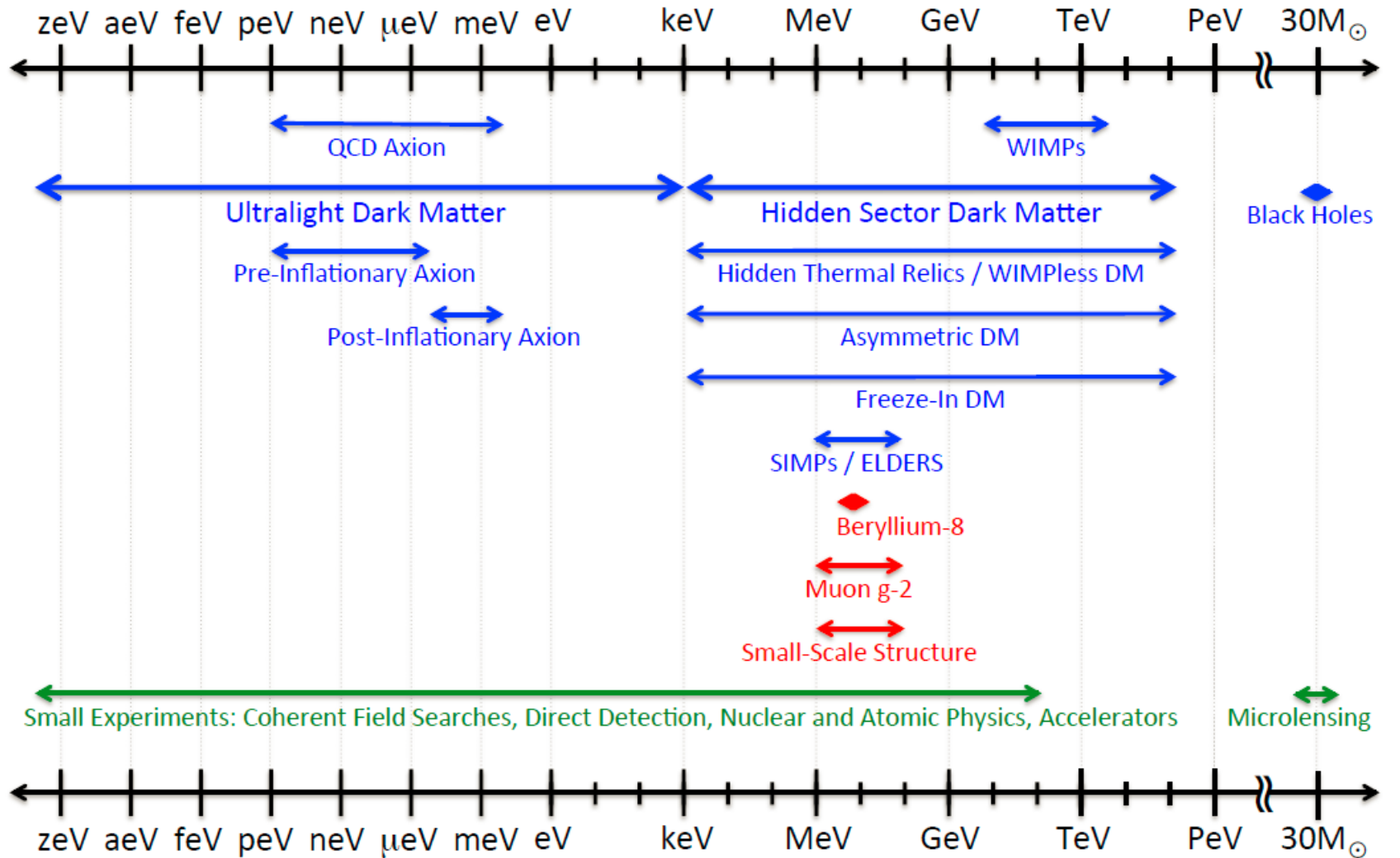
$$\langle \sigma v \rangle \sim 10^{-9} \text{GeV}^{-2} \quad (\text{weak cross section})$$



$$\Omega_{\text{DM}} \sim 0.2$$

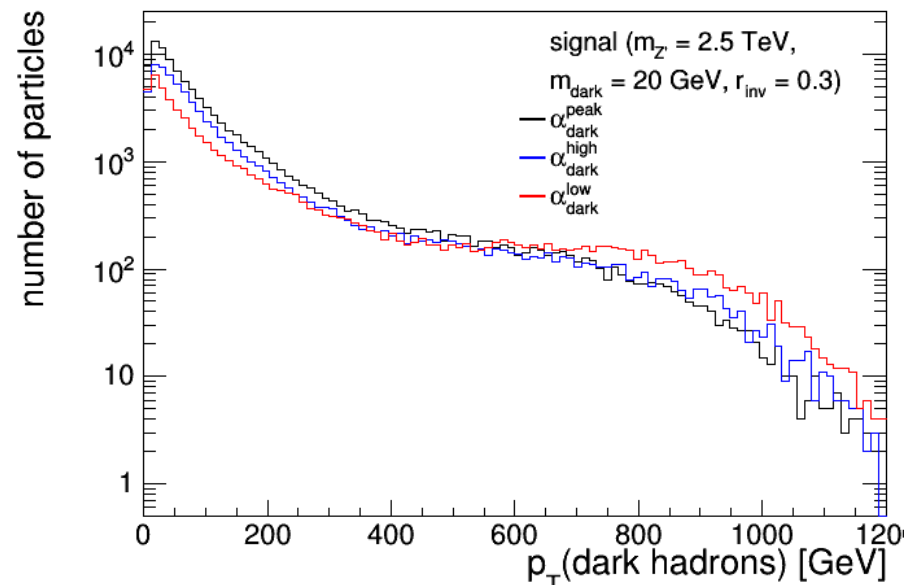
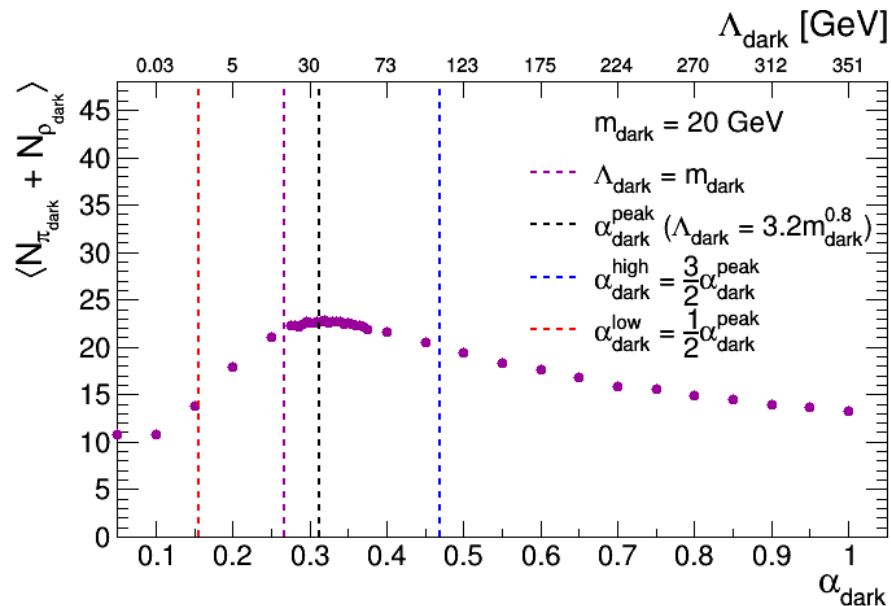
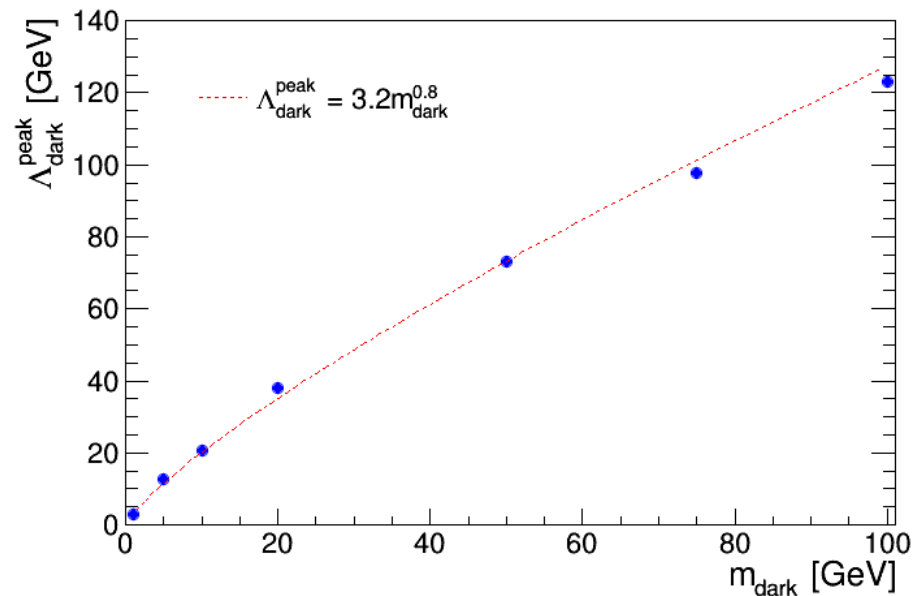
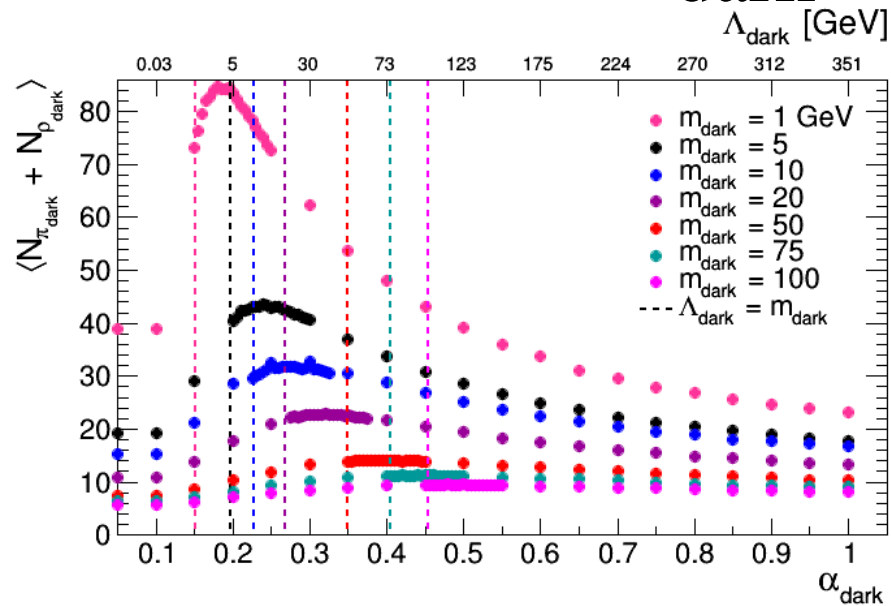
Dark Matter Landscape

Dark Sector Candidates, Anomalies, and Search Techniques

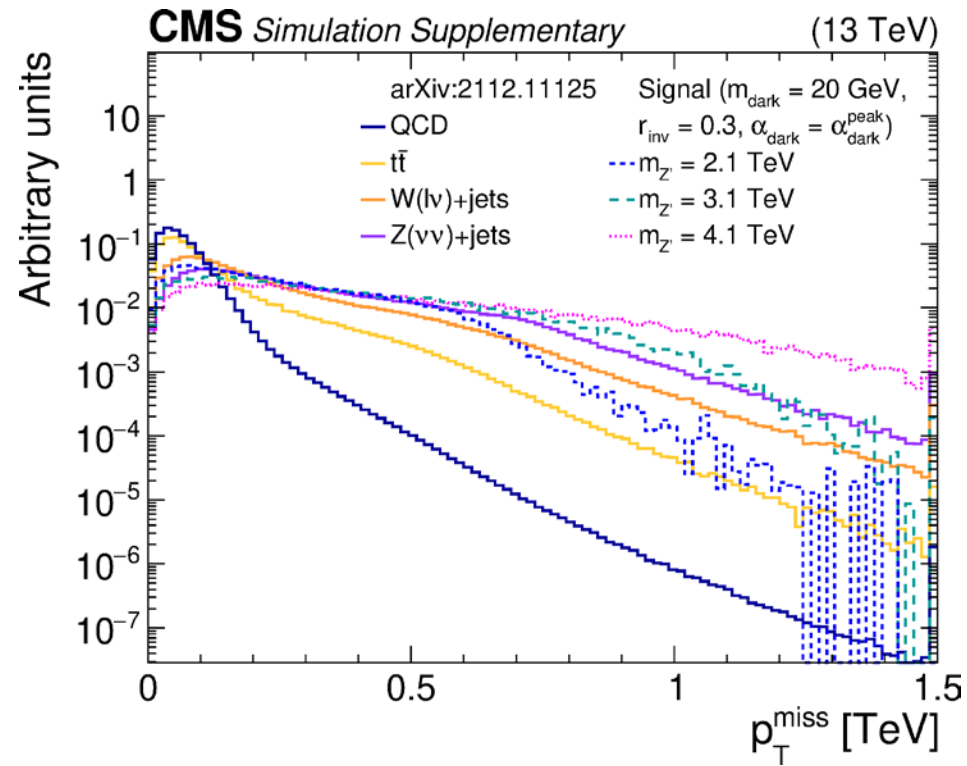
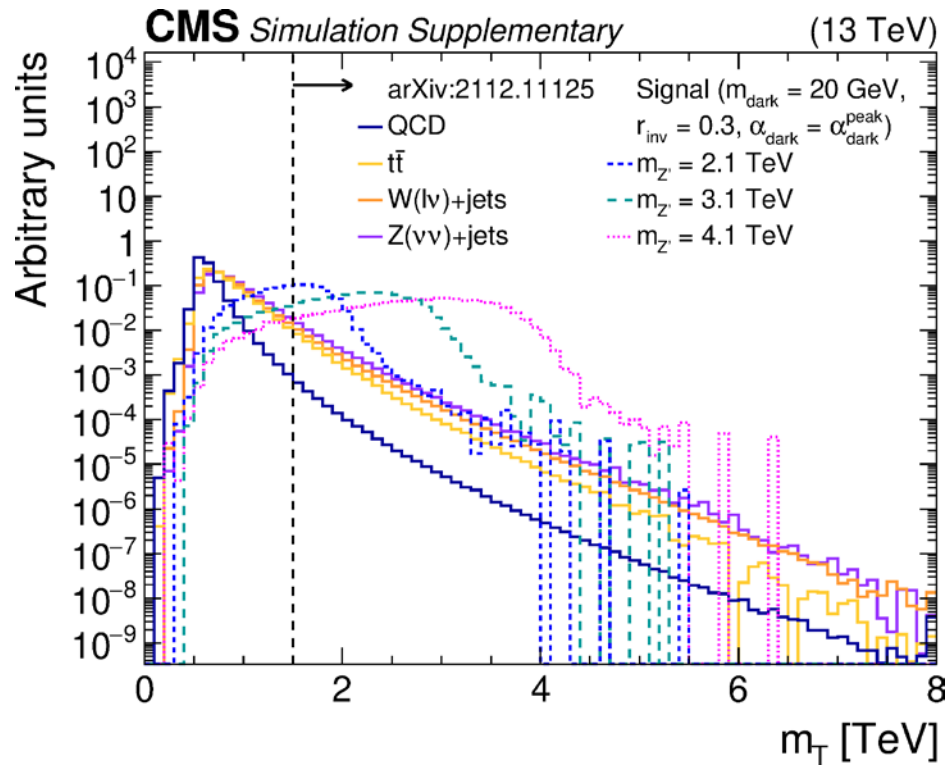


[arXiv:1707.04591](https://arxiv.org/abs/1707.04591), [G. Landsberg](#)

α_{dark} variations



Semivisible Jet Kinematics



Event Selection

Preselection

- $N_J \geq 2$
- $p_T(J_1, J_2) > 200 \text{ GeV}, |\eta(J_1, J_2)| < 2.4,$
- $J_{1,2}$ pass noise rejection
- $R_T \equiv p_T^{\text{miss}}/m_T > 0.15$
- $\Delta\eta(J_1, J_2) < 1.5$
- $m_T > 1500 \text{ GeV}$
- e/μ veto ($p_T > 10 \text{ GeV}, |\eta| < 2.4$)
- p_T^{miss} filters
- Custom dead ECAL cell filter: veto events w/ $\Delta R(j_{1,2}, c_{\text{nonfunctional}}) < 0.1$
- Inactive HCAL filter (2018 only): veto events w/ $p_T(j) > 30 \text{ GeV},$
 $-3.05 < \eta(j) < -1.35,$
 $-1.62 < \varphi(j) < -0.82$

Signal topology

Data quality

Reject QCD

Trigger efficiency

Reject $t\bar{t}, W(\ell\nu)$

Data quality

Final Selection

- Gap jet filter: veto events w/ $p_T(j_1) > 1000 \text{ GeV}, f_y(j_1) > 0.7$
- $\Delta\phi_{\text{min}}(J_{1,2}, p_T^{\text{miss}}) < 0.80$

Data quality

Reject $t\bar{t}, W(\ell\nu), Z(\nu\nu)$

Control Regions

Single Muon

- $N_J \geq 2$
- $p_T(J_1, J_2) > 200 \text{ GeV}$, $|\eta(J_1, J_2)| < 2.4$, $J_{1,2}$ pass noise rejection
- $R_T \equiv p_T^{\text{miss}}/m_T > 0.15$
- $\Delta\eta(J_1, J_2) < 1.5$
- e veto ($p_T > 10 \text{ GeV}$, $|\eta| < 2.4$)
- $N_\mu \geq 1$ ($p_T > 50 \text{ GeV}$, $|\eta| < 2.4$, medium ID, $I_{\text{mini}} < 0.2$, HLT match)

- Used for trigger efficiency measurement
- Corresponding Single Muon High- $\Delta\eta$ region used for CR trigger efficiency measurement

- Used for data quality studies
 - Statistically limited, but otherwise kinematically similar to signal region
- $\Delta\eta$ range maximizes data yield (in fully efficient region, $m_T > 1850 \text{ GeV}$)
 - $1500 < m_T < 1850 \text{ GeV}$ can be used w/ trigger efficiency correction applied

High- $\Delta\eta$

Preselection, except:

- $1.5 < \Delta\eta(J_1, J_2) < 2.2$
- $m_T > 1850 \text{ GeV}$

Cutflows

Selection	QCD	t \bar{t}	W+jets	Z+jets	$r_{\text{inv}} = 0.3$
$p_{\text{T}}(J_{1,2}) > 200 \text{ GeV}, \eta(J_{1,2}) < 2.4$	1.2	6.4	2.0	1.3	83.5
$R_{\text{T}} > 0.15$	1.3	12.1	18.5	34.6	39.7
$\Delta\eta(J_1, J_2) < 1.5$	94.9	88.0	85.1	78.8	80.0
$m_{\text{T}} > 1.5 \text{ TeV}$	0.20	3.1	4.0	5.6	81.8
$N_{\mu} = 0$	93.0	62.0	66.0	99.5	96.8
$N_{\text{e}} = 0$	99.6	59.8	57.3	99.6	99.4
$p_{\text{T}}^{\text{miss}}$ filters	99.5	99.9	99.9	99.9	99.8
$\Delta R(j_{1,2}, c_{\text{nonfunctional}}) > 0.1$	60.6	95.1	95.2	95.6	95.2
veto $f_{\gamma}(j_1) > 0.7$ & $p_{\text{T}}(j_1) > 1.0 \text{ TeV}$	99.7	99.7	99.6	99.7	99.7
$\Delta\phi_{\text{min}} < 0.8$	94.8	81.7	61.8	44.7	87.7
Efficiency [%]	1.6e-05	0.0060	0.0029	0.0085	17
high- R_{T}	9.0	29.5	38.8	39.1	45.2
low- R_{T}	91.0	70.5	61.2	60.9	54.8
high-SVJ2	0.093	0.62	0.46	0.69	34.6
low-SVJ2	1.1	1.7	0.92	0.94	42.3

Variable Definitions

- **Girth:** $g = \sum_i \frac{p_{T,i}}{p_{T,\text{jet}}} r_i$

- **Major/minor axes:**

$$\mathcal{M} = \begin{bmatrix} \sum_i p_{T,i}^2 \Delta \eta_i^2 & -\sum_i p_{T,i}^2 \Delta \eta_i \Delta \phi_i \\ -\sum_i p_{T,i}^2 \Delta \eta_i \Delta \phi_i & \sum_i p_{T,i}^2 \Delta \phi_i^2 \end{bmatrix}$$

$$\sigma_{\text{major}} = \sqrt{\lambda_1 / \sum_i p_{T,i}^2}$$

$$\sigma_{\text{minor}} = \sqrt{\lambda_2 / \sum_i p_{T,i}^2}$$

- **$p_T \mathbf{D}$:** $p_T \mathbf{D} = \frac{\sqrt{\sum_i p_{T,i}^2}}{\sum_i p_{T,i}}$

- **Nsubjettiness:** $\tau_{21} = \tau_2 / \tau_1$, $\tau_{32} = \tau_3 / \tau_2$

$$\tau_N^{(\beta)} = \frac{1}{\sum_k p_{T,k} R_0} \sum_k p_{T,k} \min\{\Delta R_{1,k}^{(\beta)}, \Delta R_{2,k}^{(\beta)}, \dots, \Delta R_{N,k}^{(\beta)}\}$$

- **Energy correlation functions:**

$$v e_n^{(\beta)} = \sum_{1 \leq i_1 < \dots < i_n \leq n_{\text{const.}}} z_{i_1} \dots z_{i_n} \prod_{m=1}^v \min_{s < t \in \{i_1, \dots, i_n\}}^{(m)} \left\{ \theta_{st}^\beta \right\}$$

$$N_2^{(1)} = \frac{2e_3^{(1)}}{\left(1e_2^{(1)}\right)^2}$$

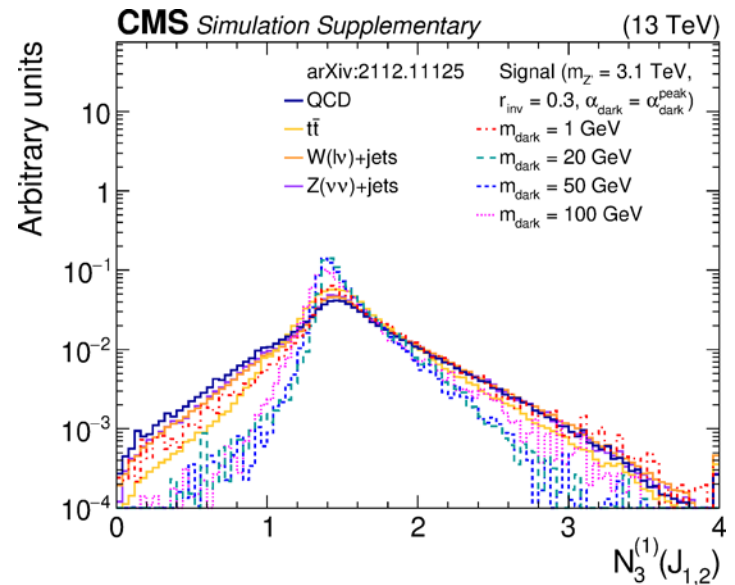
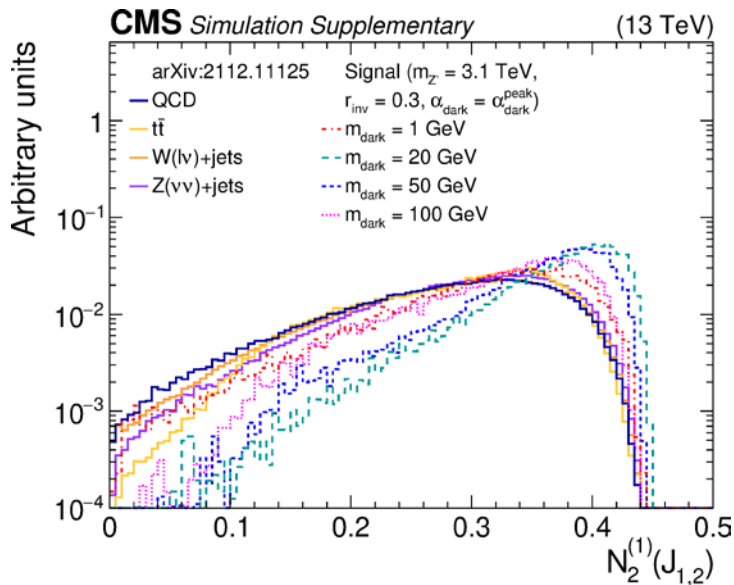
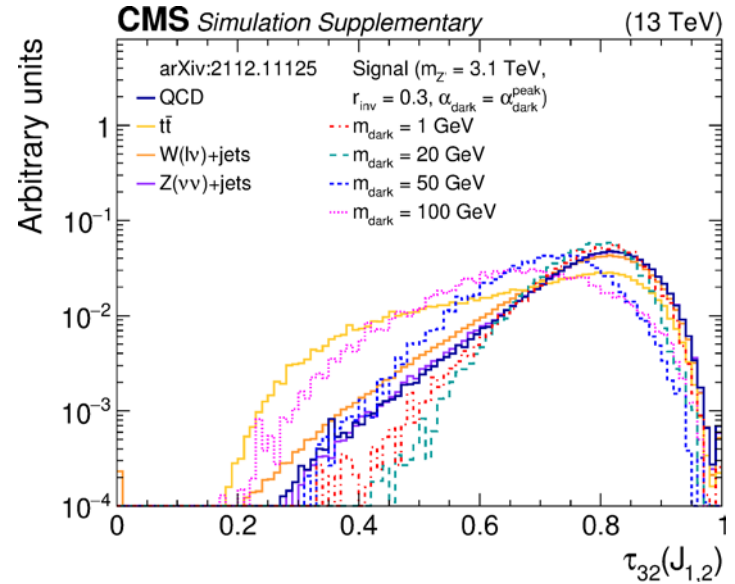
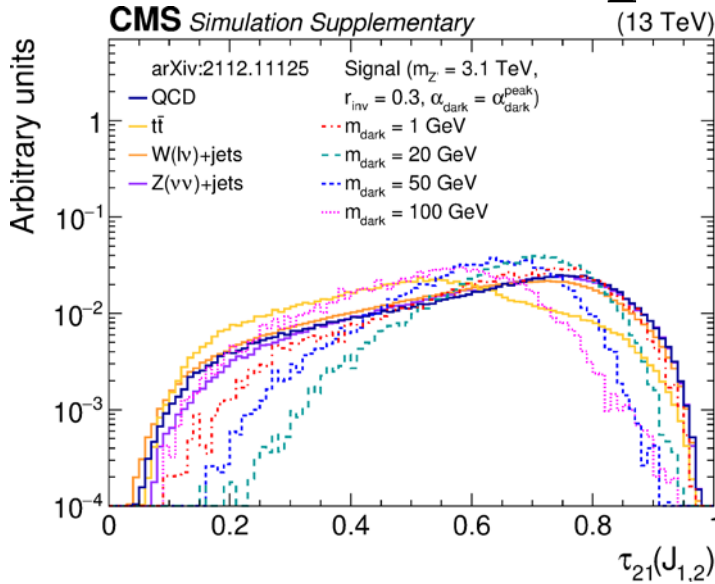
$$N_3^{(1)} = \frac{2e_4^{(1)}}{\left(1e_3^{(1)}\right)^2}$$

$$\begin{aligned} m_{\text{T}}^2 &= [E_{\text{T,JJ}} + E_{\text{T}}^{\text{miss}}]^2 - [\vec{p}_{\text{T,JJ}} + \vec{p}_{\text{T}}^{\text{miss}}]^2 \\ &= m_{\text{JJ}}^2 + 2p_{\text{T}}^{\text{miss}} \left[\sqrt{m_{\text{JJ}}^2 + p_{\text{T,JJ}}^2} - p_{\text{T,JJ}} \cos(\phi_{\text{JJ,miss}}) \right] \end{aligned}$$

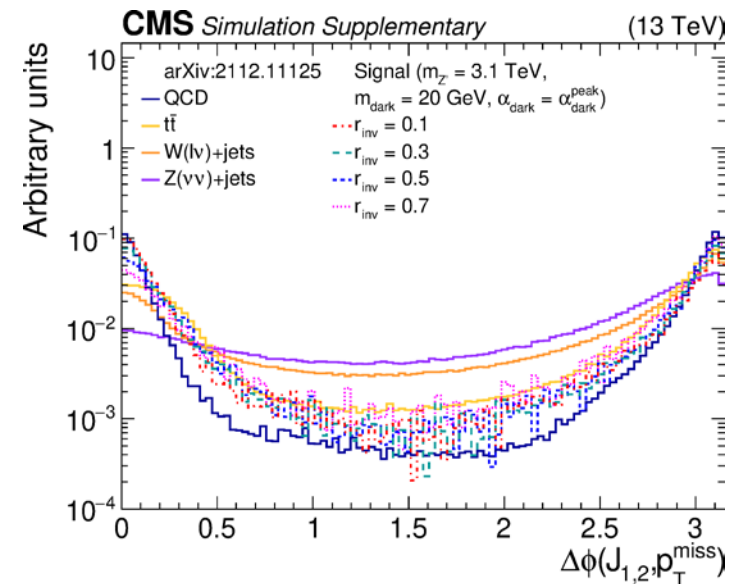
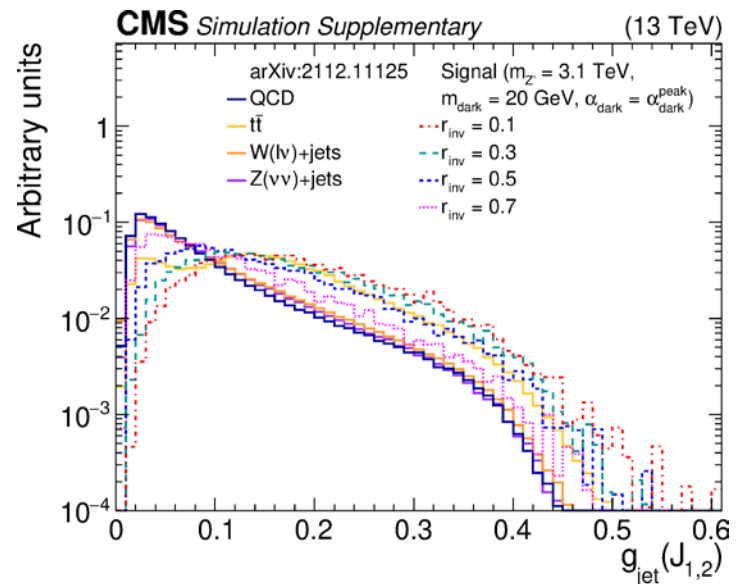
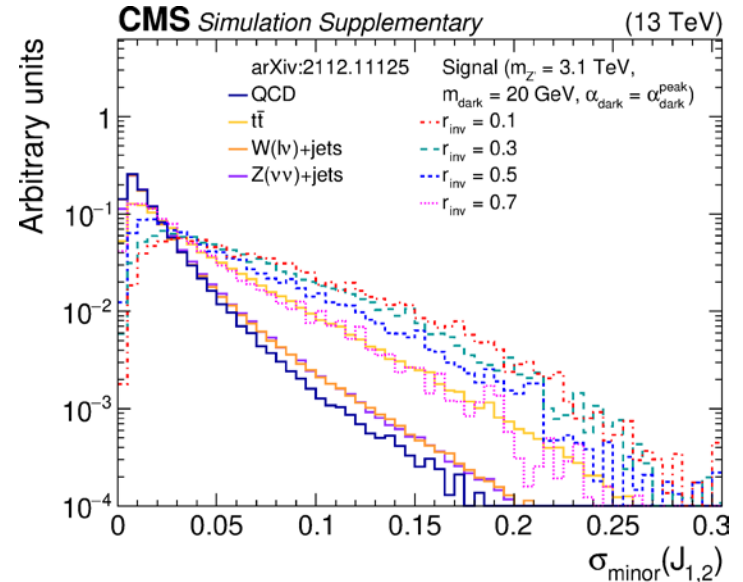
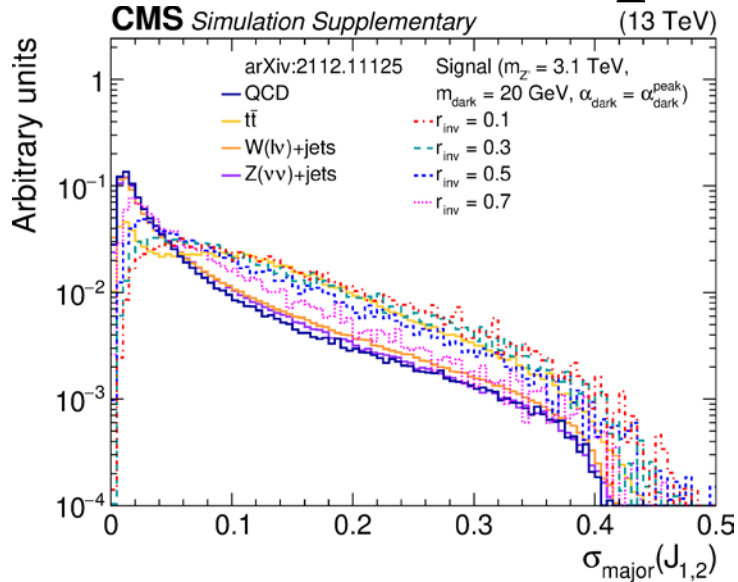
Soft Drop Mass

- Start w/ jet clustered by anti- k_t algorithm w/ $R = 0.8$
- Recluster jet constituents w/ Cambridge-Aachen algorithm
 - Undo clustering one step at a time
 - Get two subjets j_1, j_2
 - Check condition: $\frac{\min(p_{Tj1}, p_{Tj2})}{p_{Tj1} + p_{Tj2}} > z_{\text{cut}} \times \left(\frac{\Delta R_{12}}{R_0}\right)^\beta$
 - If met, then keep whole jet and stop
 - If not met, keep higher p_T subjet and repeat
- CMS uses $z_{\text{cut}} = 0.1, \beta = 0$
- See [arXiv:1402.2657](https://arxiv.org/abs/1402.2657)
- Effect: drop soft constituents (at wide angles)
→ remove ISR, underlying event, pileup
- Mass calculation: find invariant mass from softdrop subjet 4-vectors

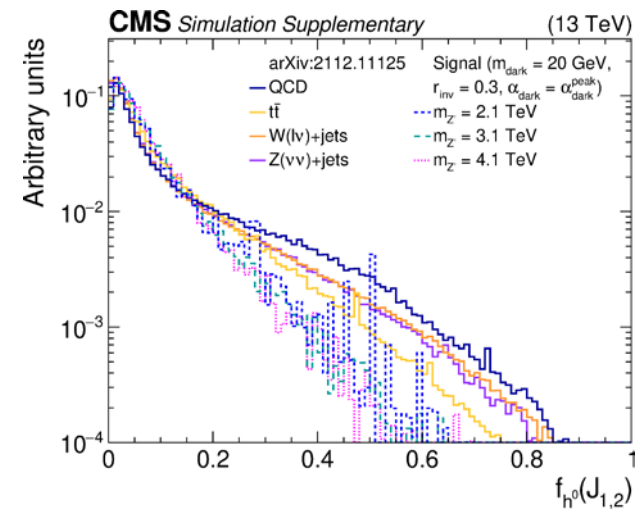
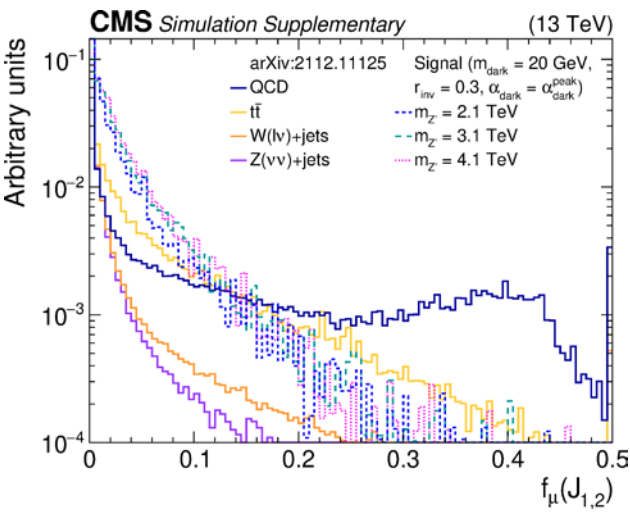
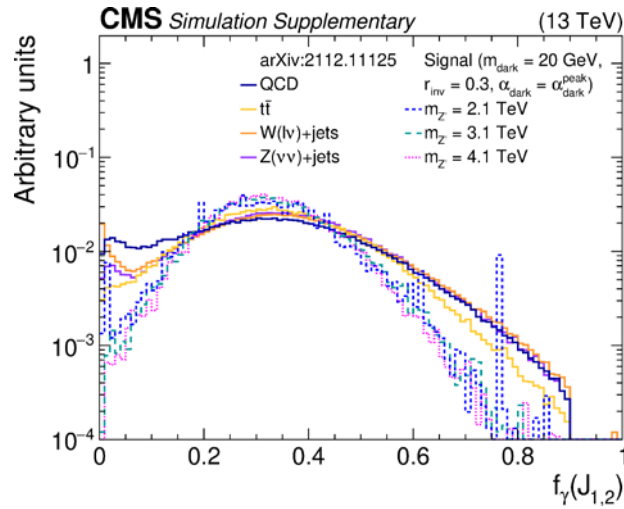
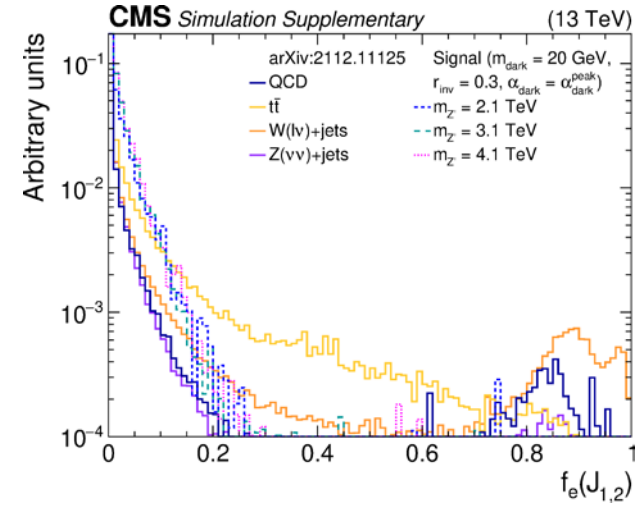
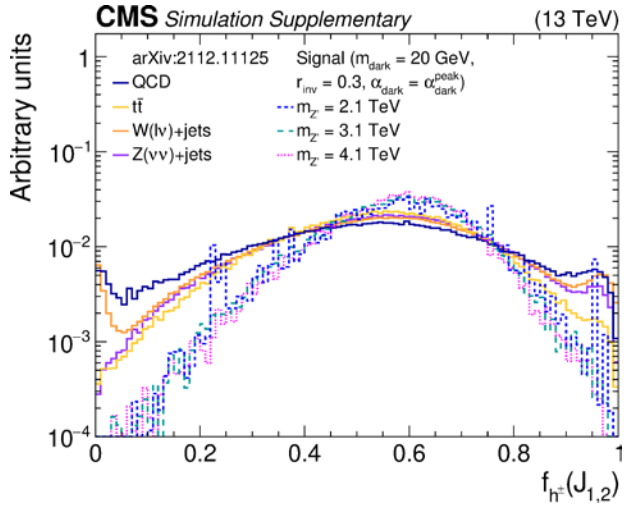
BDT Input Variables (1)



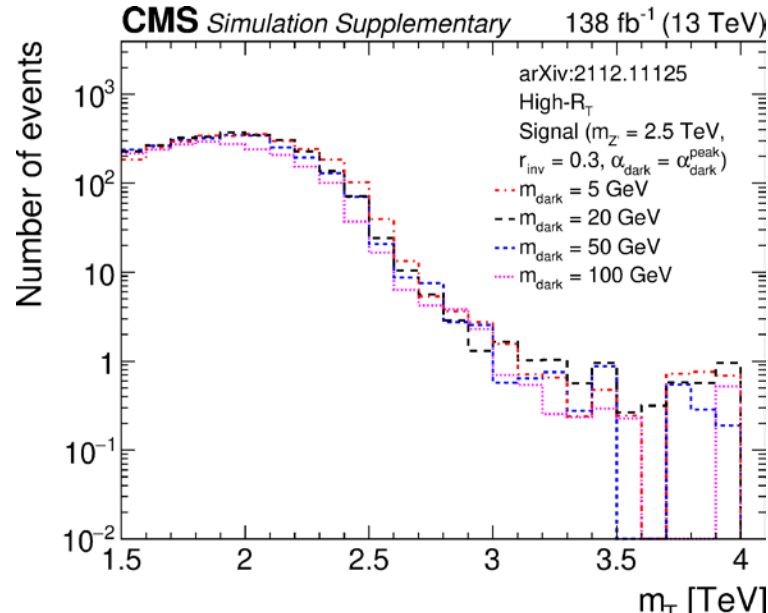
BDT Input Variables (2)



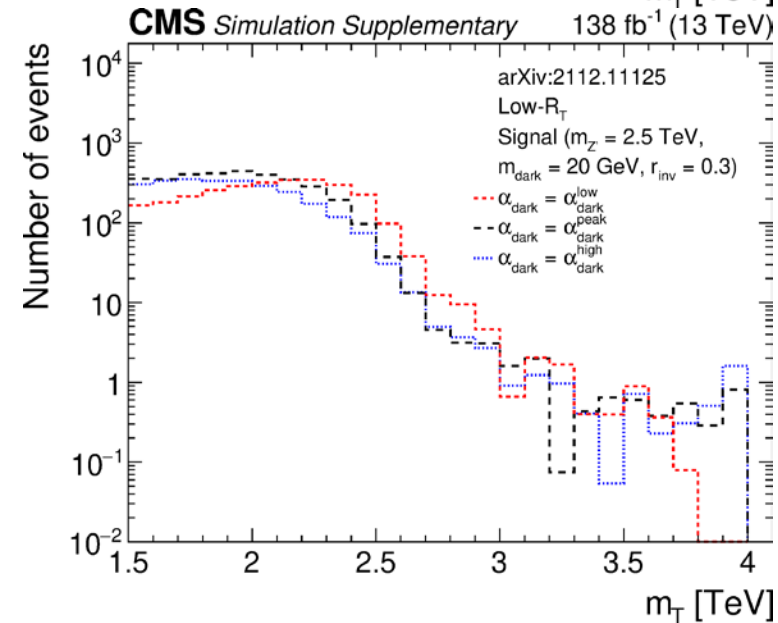
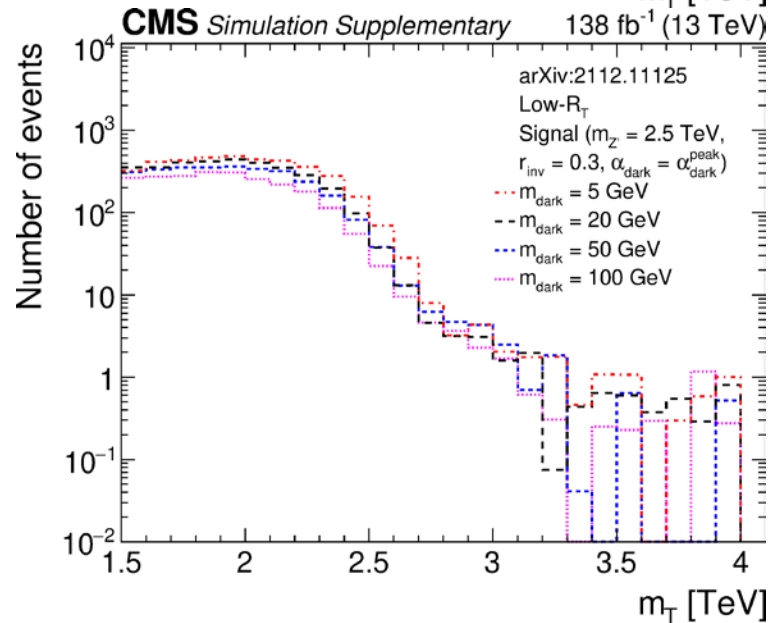
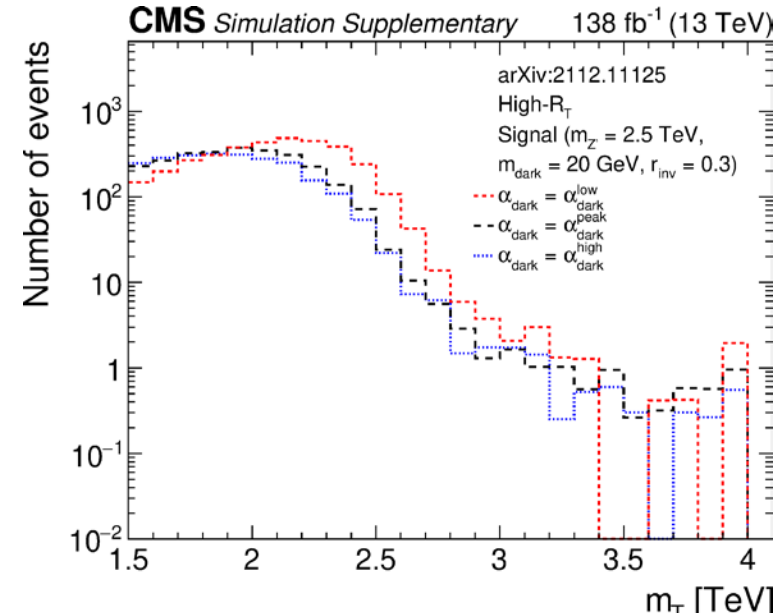
BDT Input Variables (3)



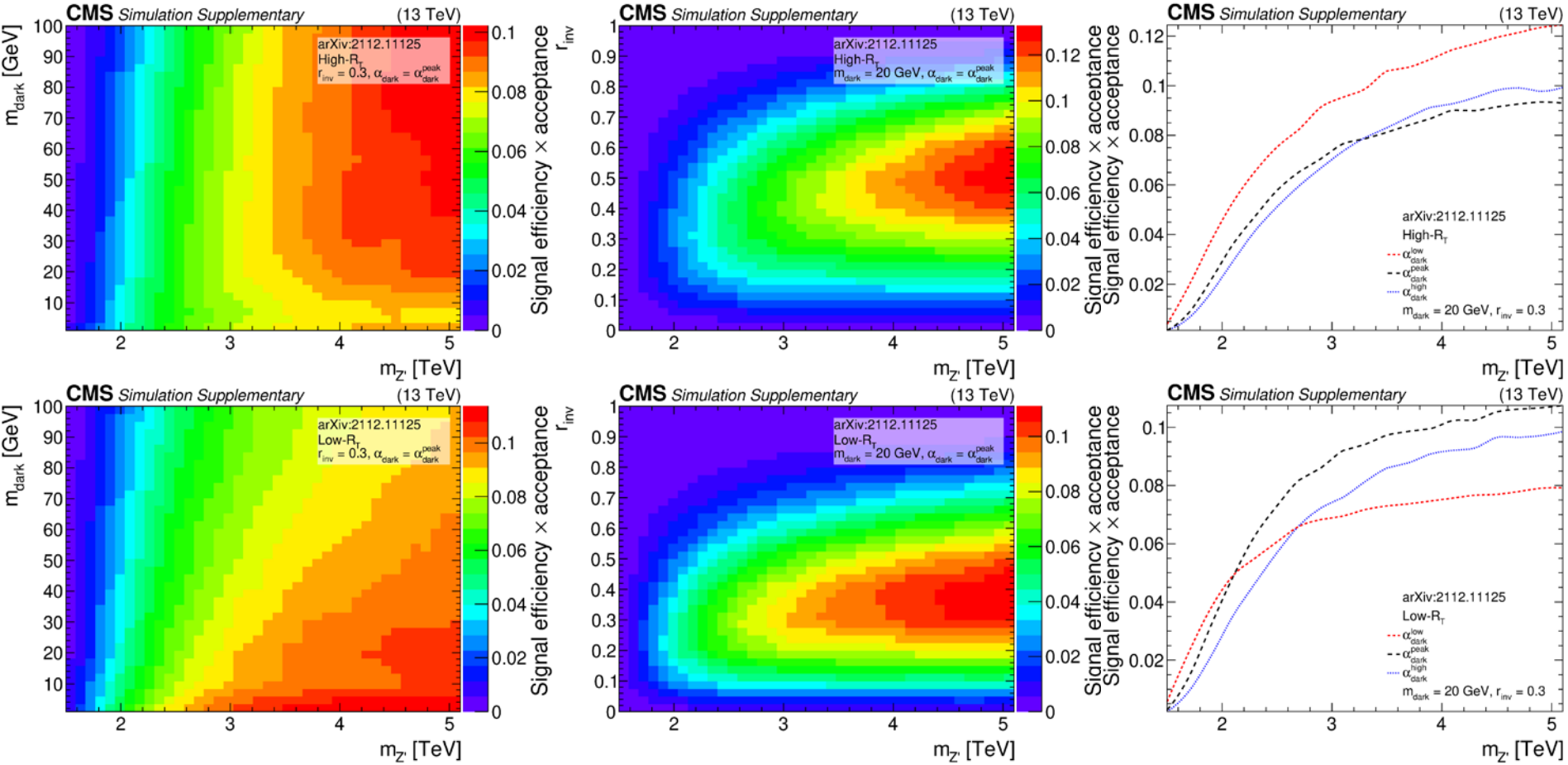
More m_T Variations



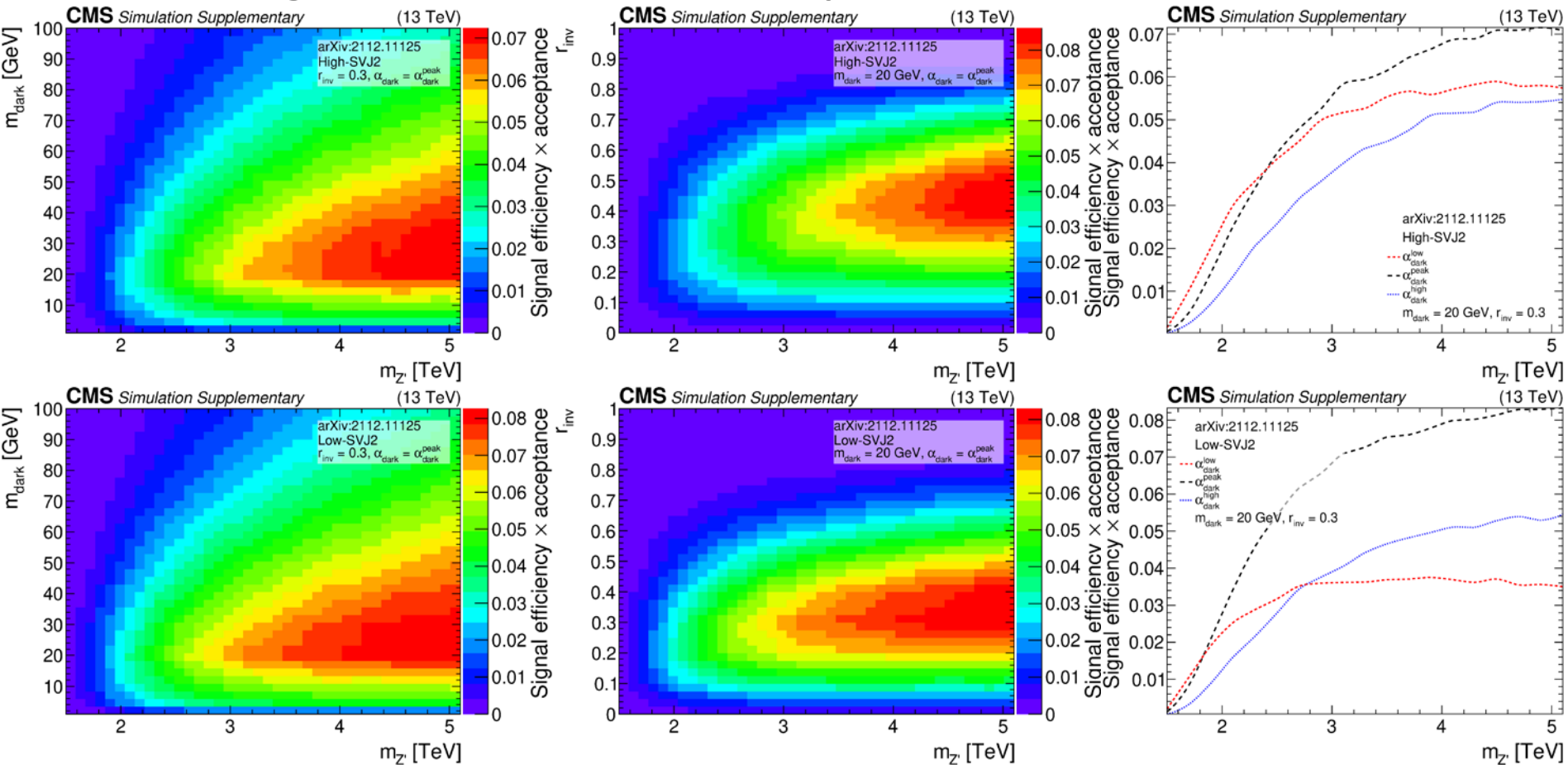
- α_{dark} has non-trivial impact
- m_{dark} has very little impact



Signal Efficiency (inclusive)



Signal Efficiency (BDT-based)



Secondary Functions

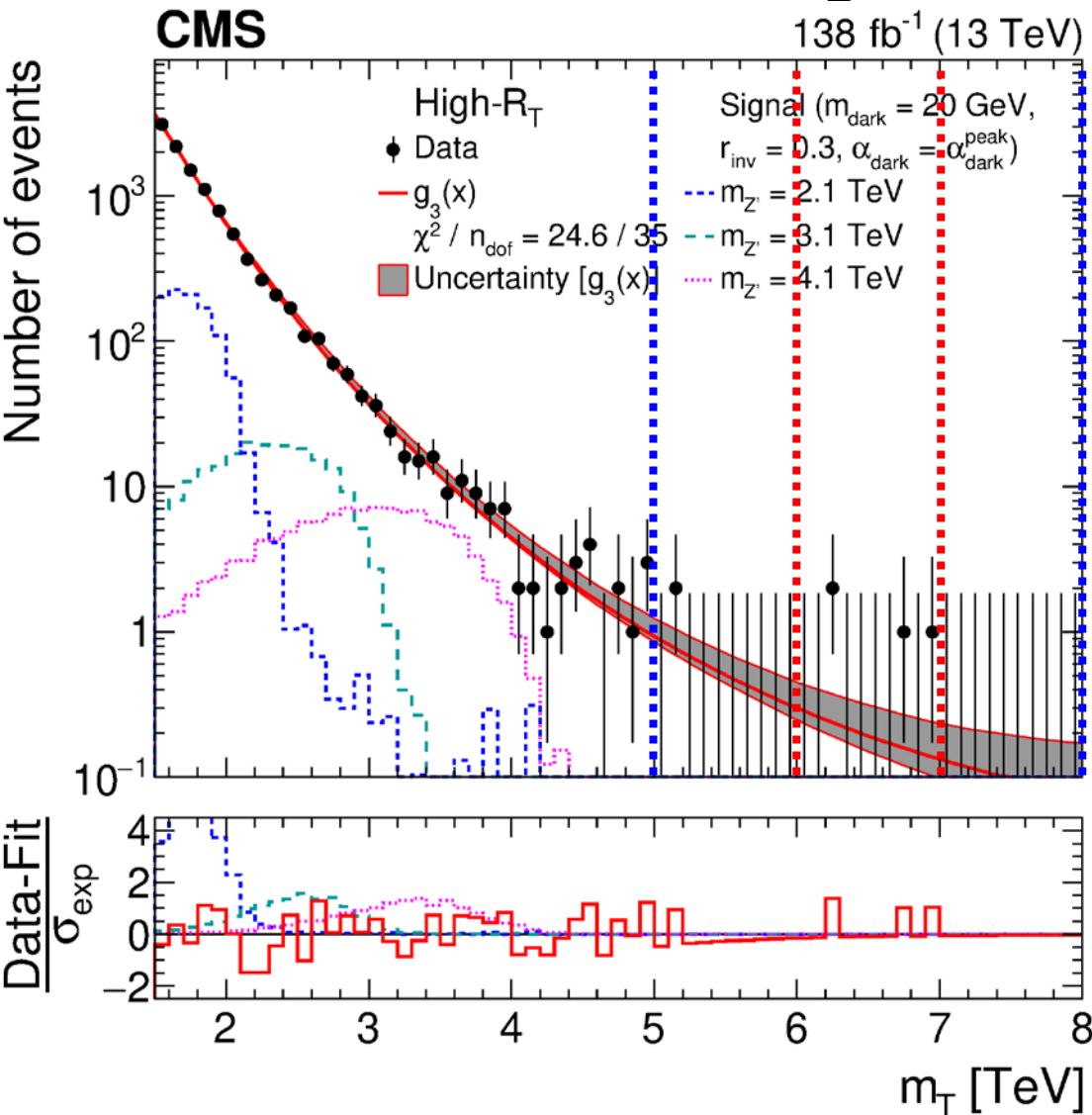
$$x = m_T / \sqrt{s}$$

$$f(x) = (1 - x)^{p_1} (x)^{p_2 + p_3 \log(x)}$$

$$h(x) = (x)^{-p_1} \exp(-p_2 x - p_3 x^2)$$

- $f(x)$ from CMS dijet searches e.g. [arXiv:1911.03947](https://arxiv.org/abs/1911.03947)
- $h(x)$ from UA2 dijet searches: [Z. Phys. C **49** \(1991\) 17](#), [Nucl. Phys. B **400** \(1993\) 3](#)

High- R_T Tail Counts



m_T [TeV]	Obs.	Pred.	
5–8	6	8.4	+2.1
			-1.4
6–7	4	2.0	+0.6
			-0.4

- Predicted counts and uncertainties obtained from integrating background fit