

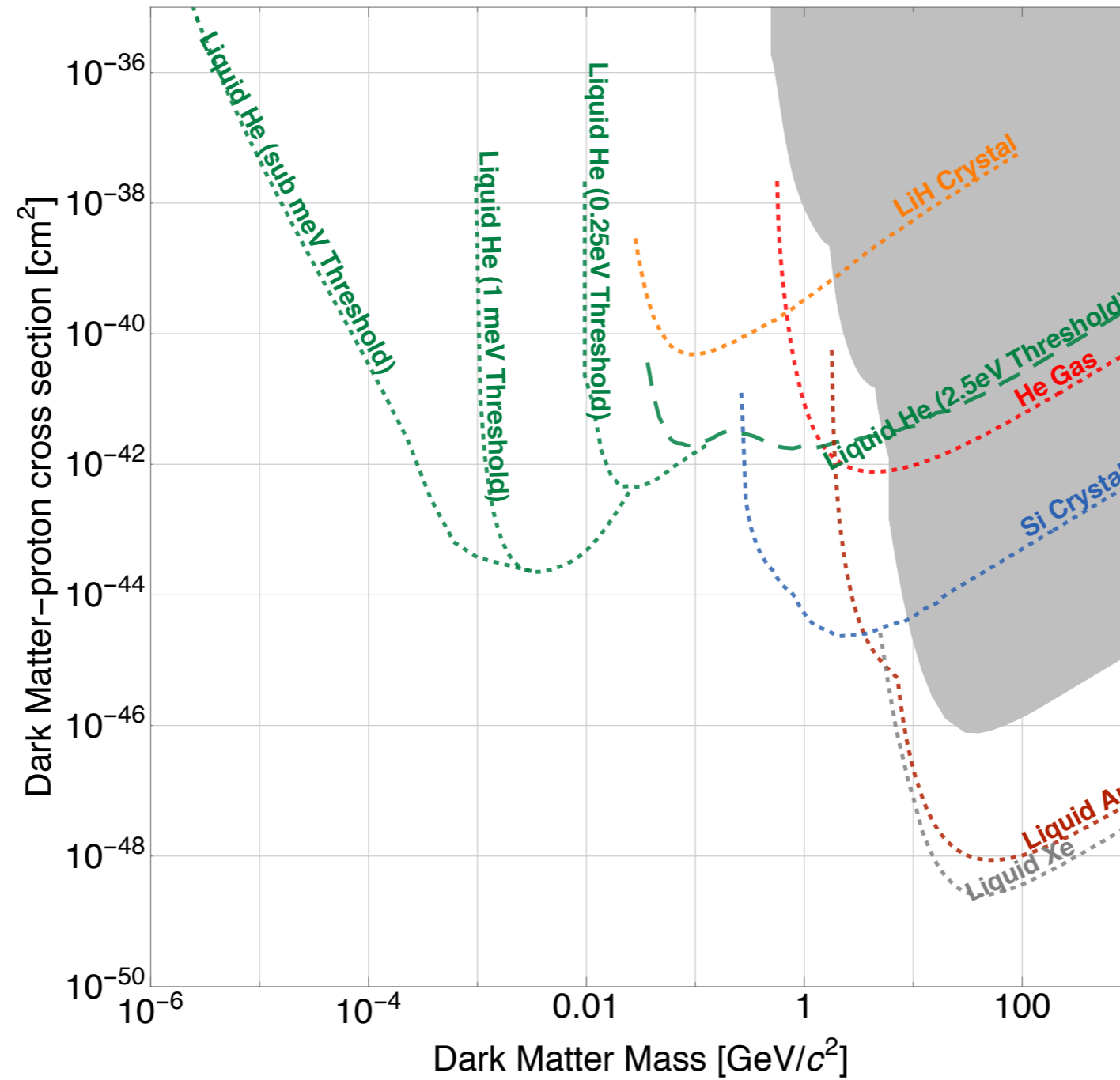
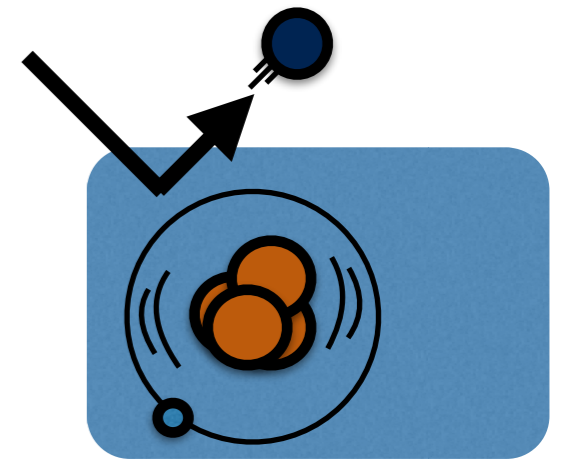
Superfluid Effective Field Theory for Dark Matter Direct Detection

Wei Xue

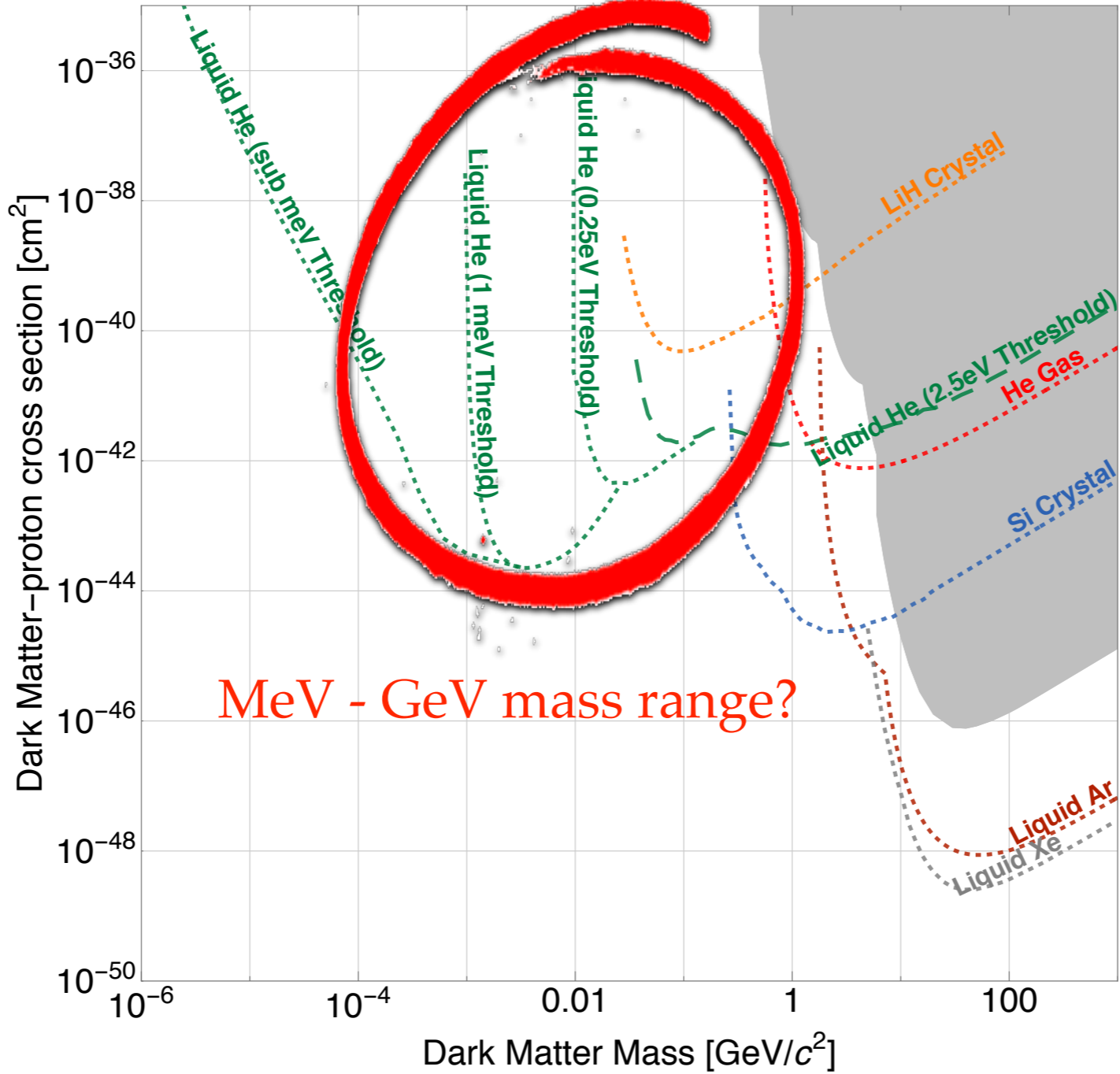
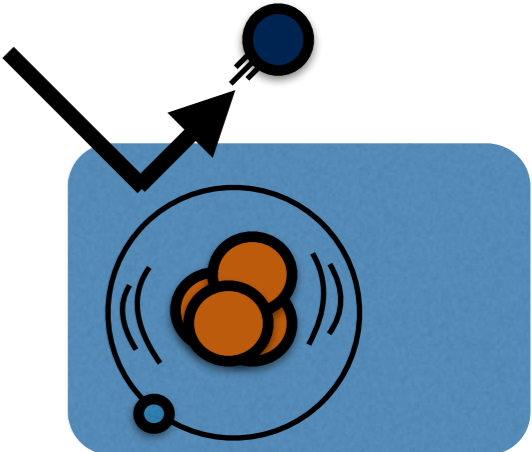
June 9, 2022
CERN-CKC workshop



Dark matter direct detection



Dark matter direct detection



Plan

- **theoretical framework** to understand the quasi-particle production and thermalization
- **simulation** to know the momentum spectrum, flux, thermalization
- a prototype **experiment** at University of Florida

arXiv: 2108.07275

Collaboration



Yoonseok Lee



Tarek Saab



Konstantin Matchev



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Jordan Smolinsky

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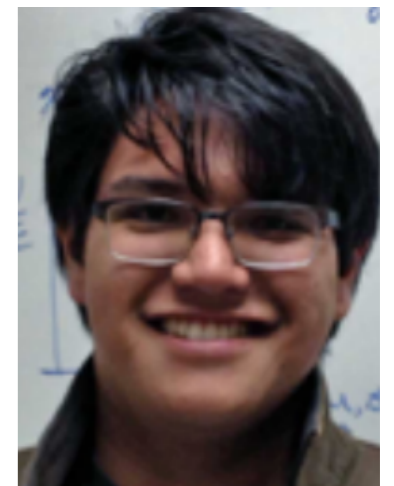
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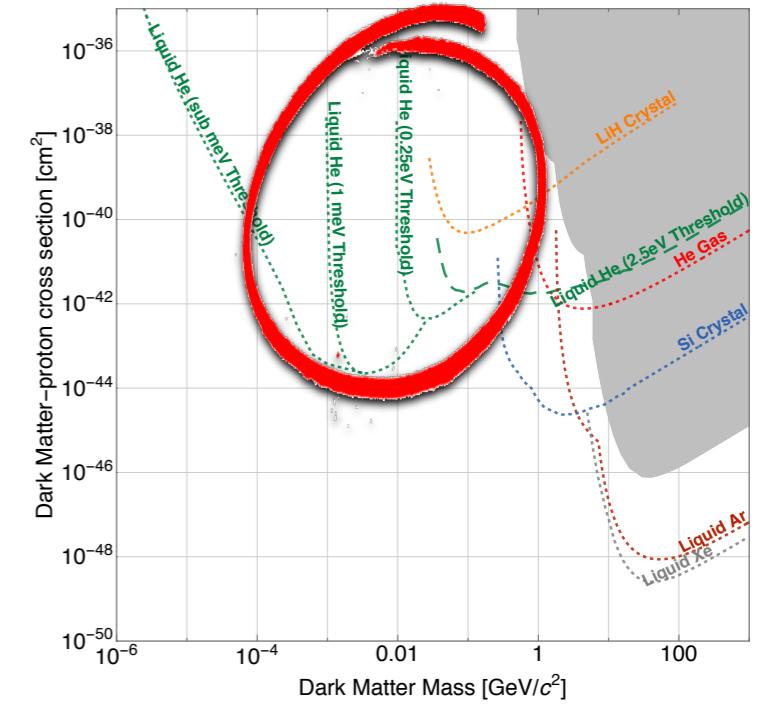


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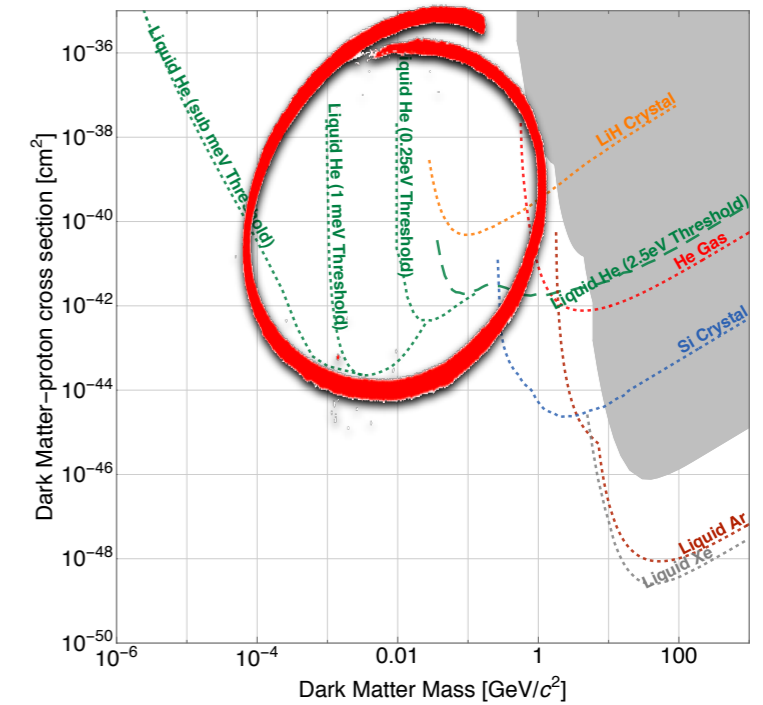
Jordan Smolinsky

Why ^4He superfluid?



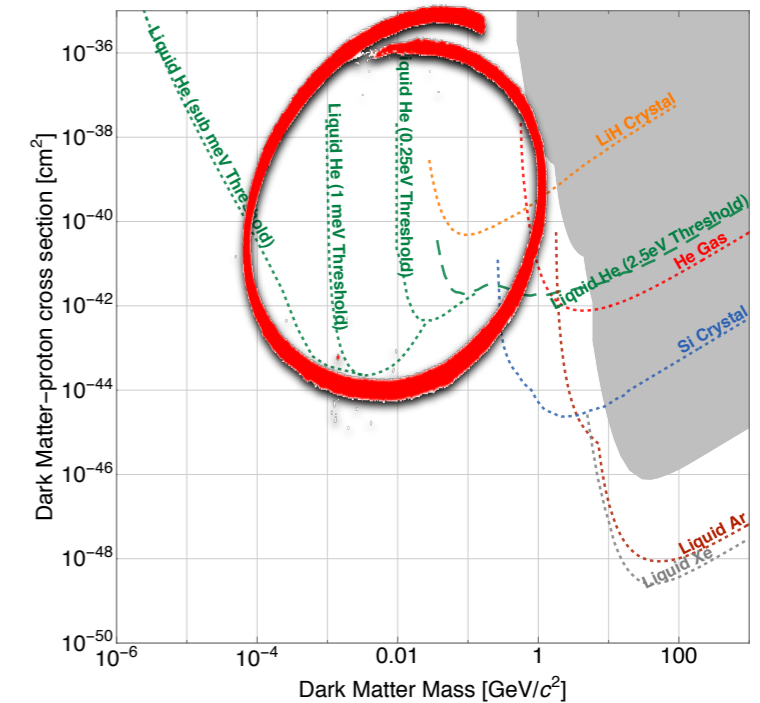
Why ^4He superfluid?

- Helium as the **second lightest element** an excellent target material for detecting light particles

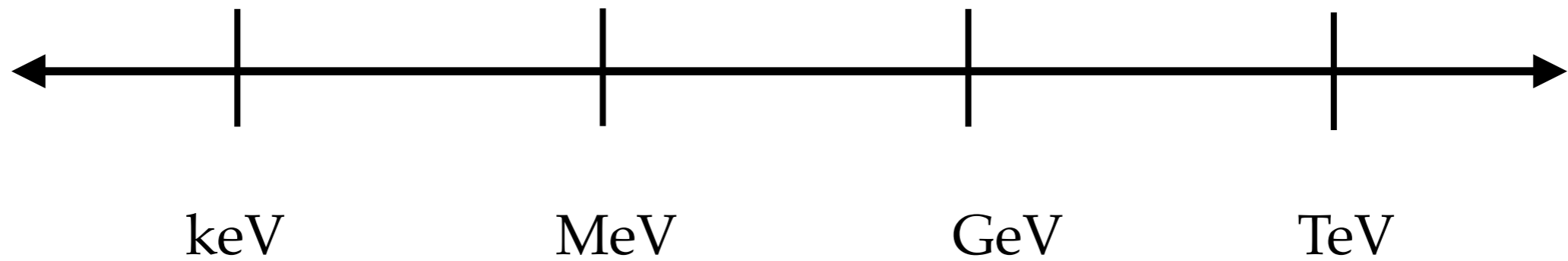


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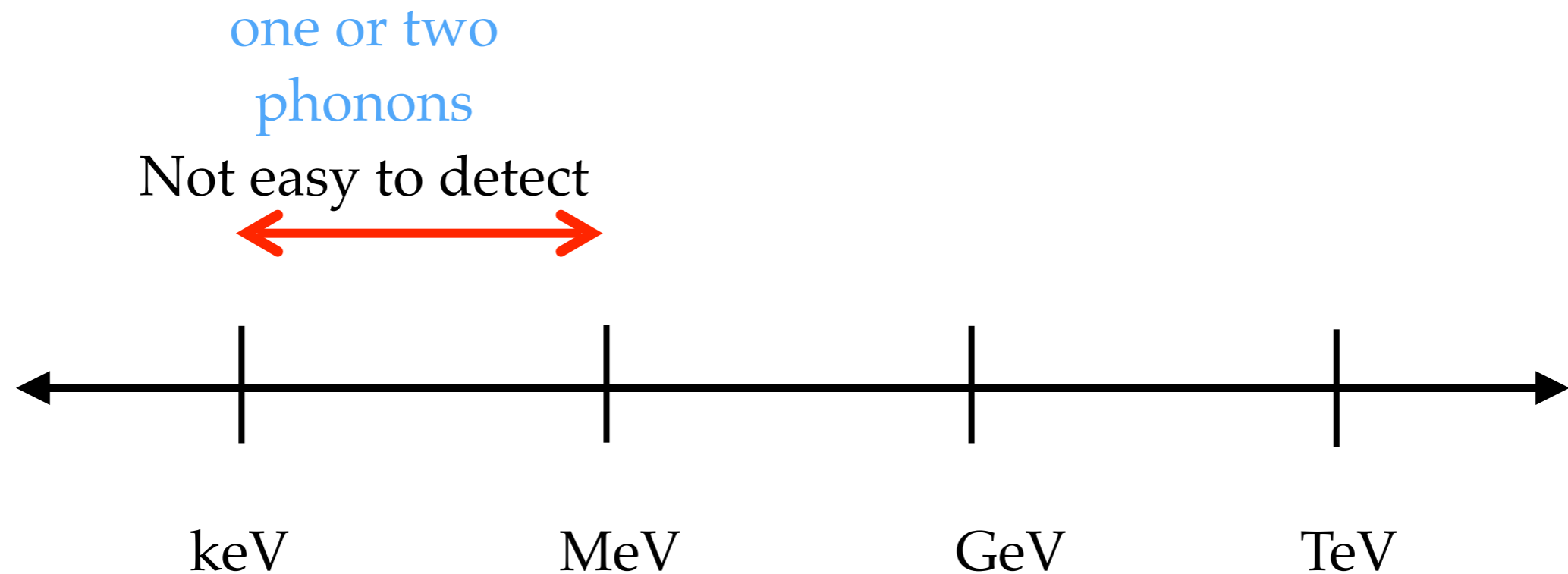
- Helium as the **second lightest element** an excellent target material for detecting light particles
- superfluid Helium will be cooled to **$\sim 0.1\text{ K}$** the system behaves as a vacuum sensitive to tiny perturbations



Previous studies and challenges on superfluid direct detection

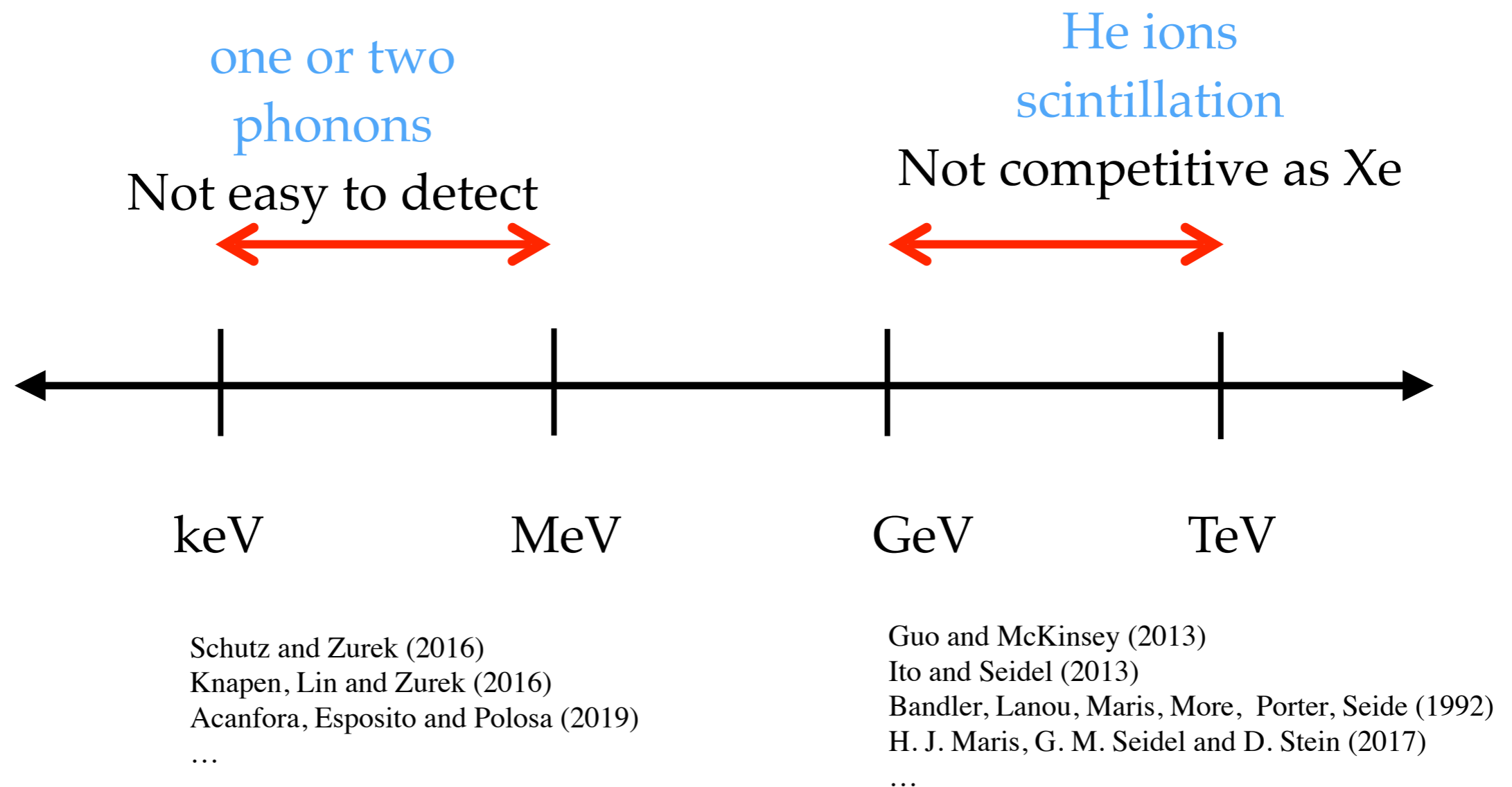


Previous studies and challenges on superfluid direct detection

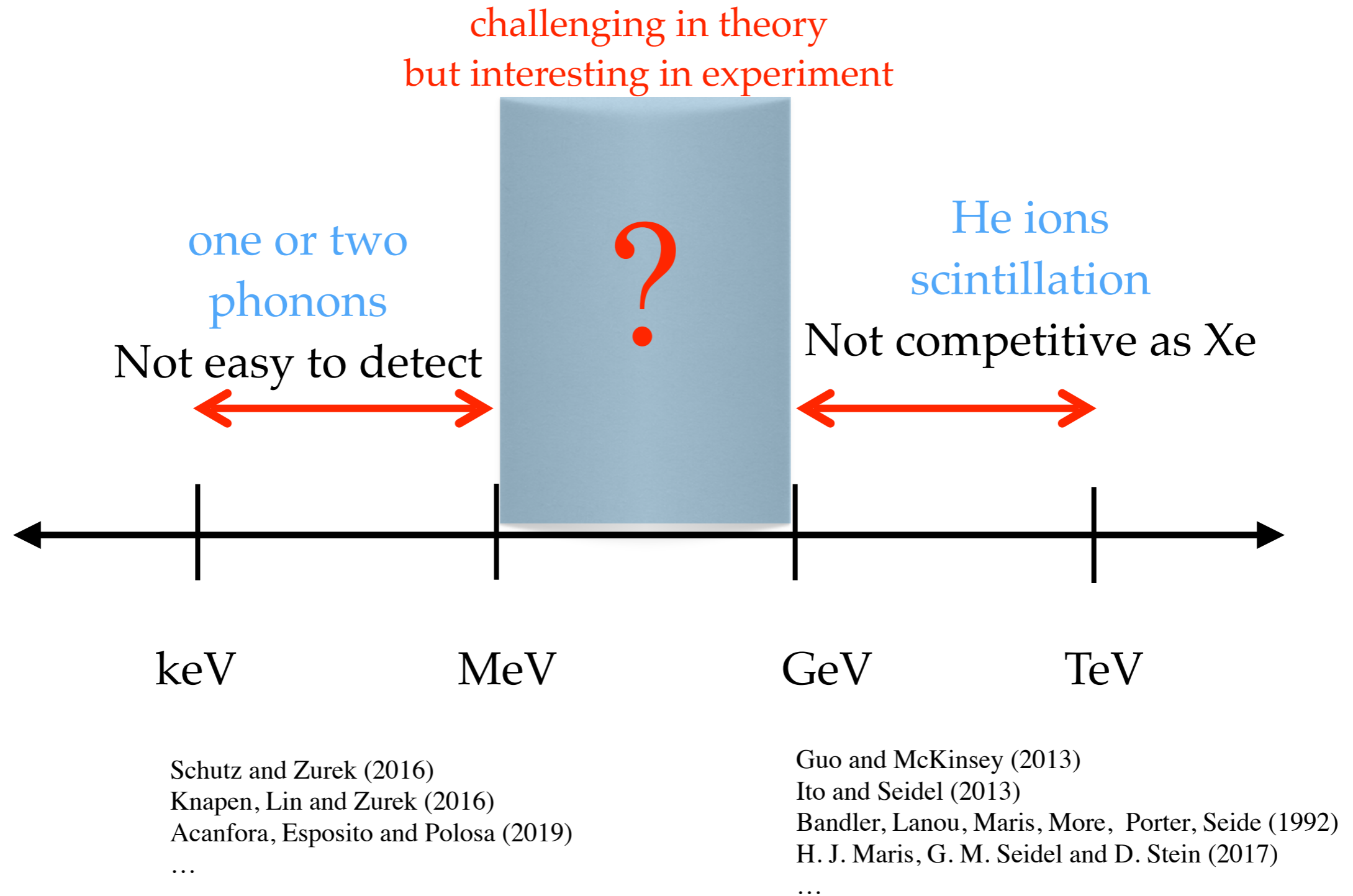


Schutz and Zurek (2016)
Knapen, Lin and Zurek (2016)
Acanfora, Esposito and Polosa (2019)
...

Previous studies and challenges on superfluid direct detection

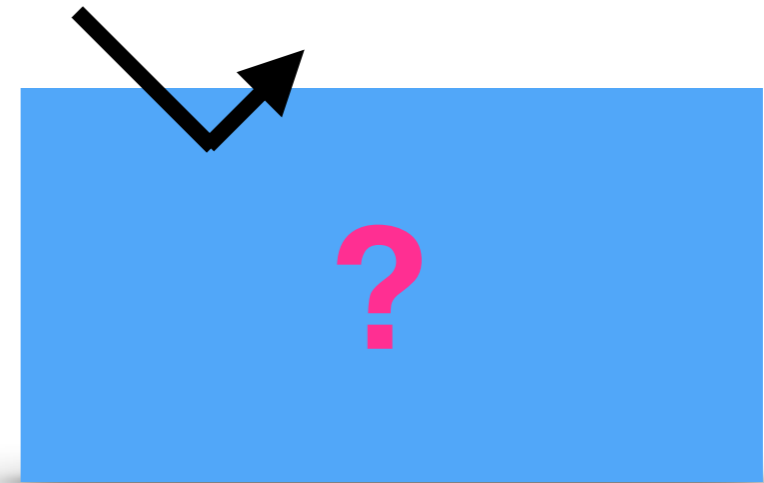


Previous studies and challenges on superfluid direct detection

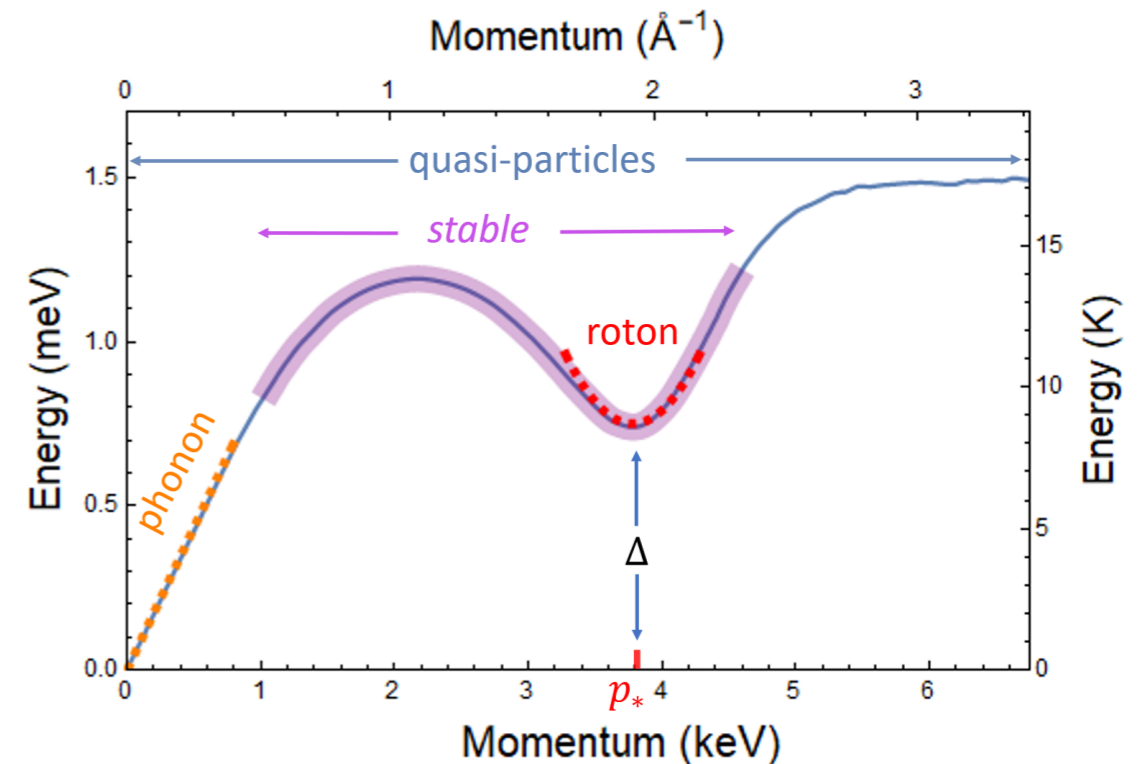


Challenges and motivations

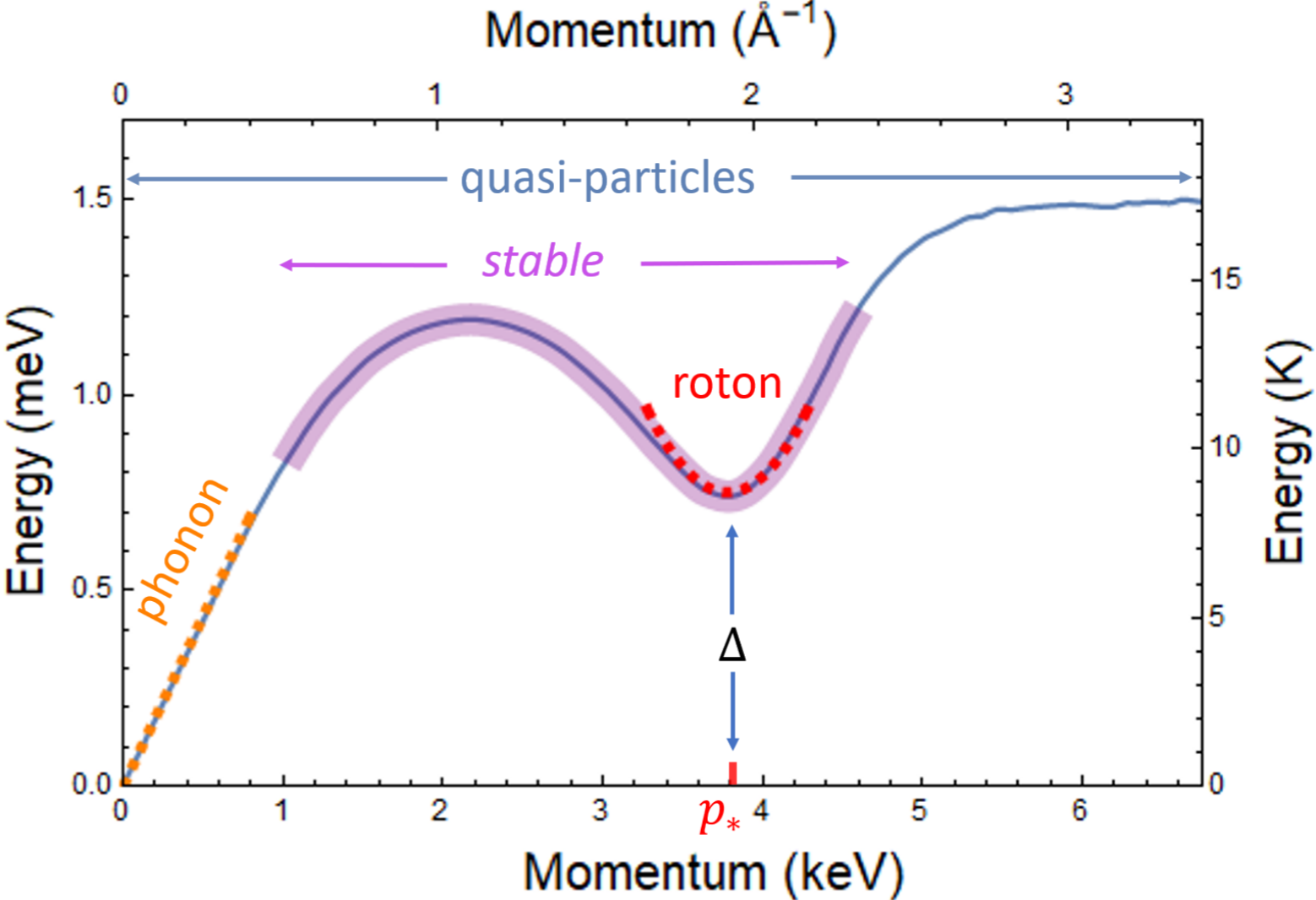
- What happens when a test particle (dark matter or neutron) scatters with the helium superfluid?



- The perturbative theory of superfluid break down $\sim \text{keV}$?
(inverse of the helium spacing)

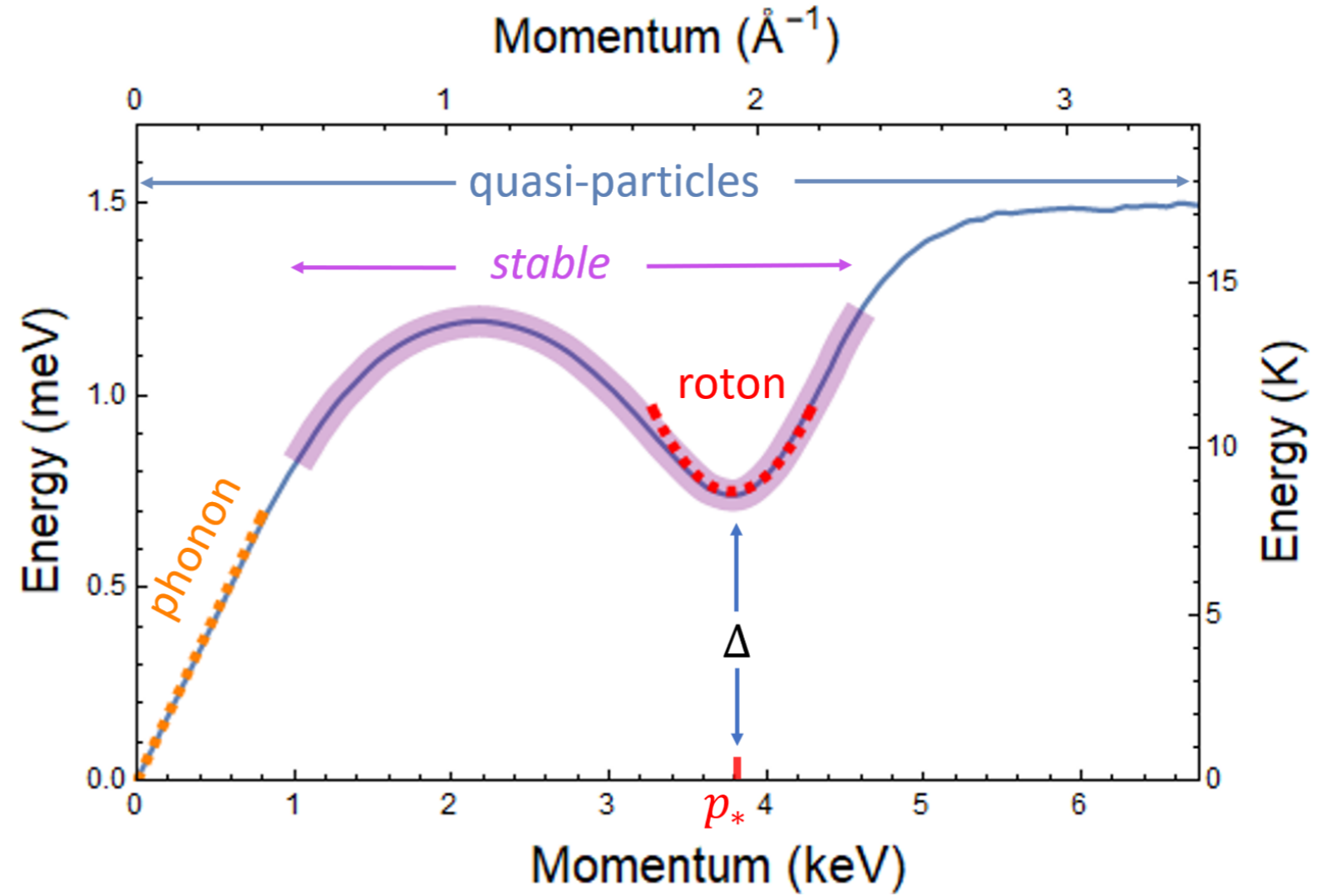


Quasi-particles



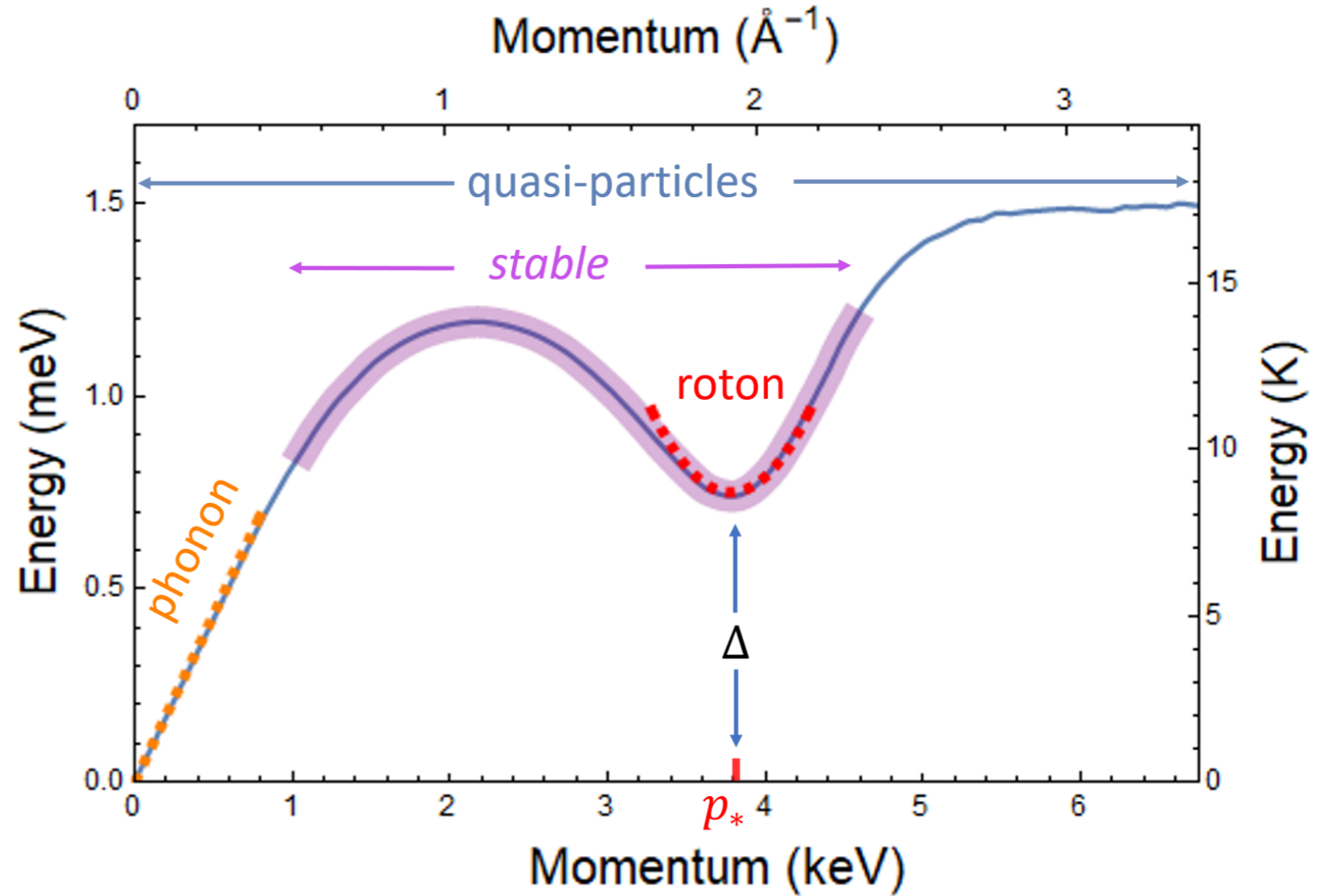
Quasi-particles

- atomic spacing $\sim \text{keV}^{-1}$



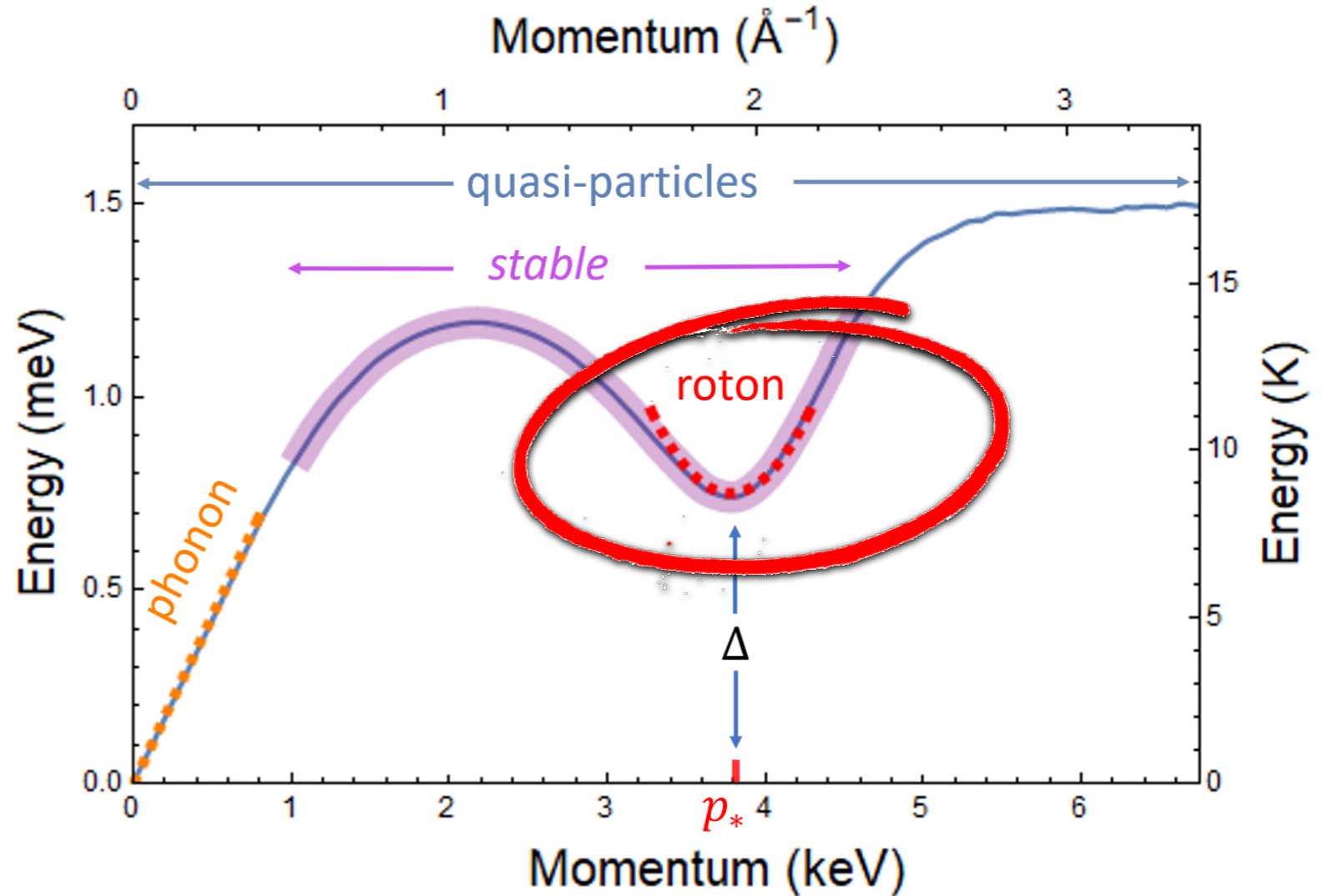
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- **phonon** $E \simeq c_s k$
- sound speed $c_s \sim 10^{-6}$
- **roton** $E_r \simeq \Delta + \frac{(p-p_*)^2}{2m_*}$

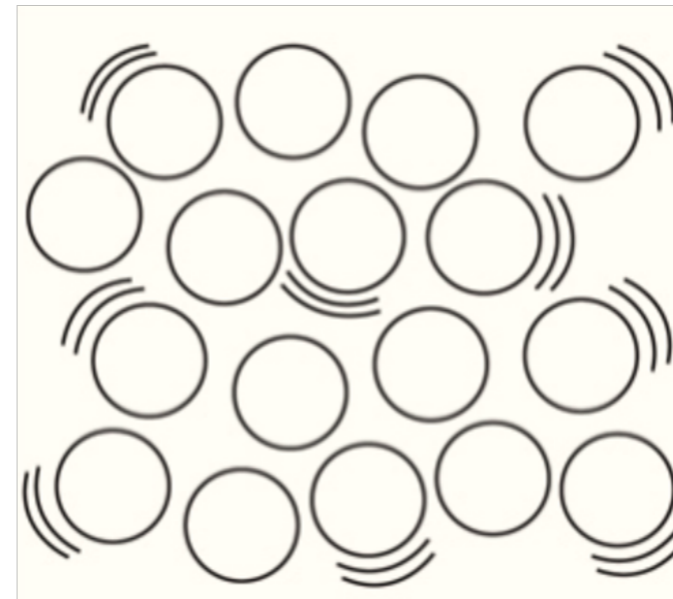
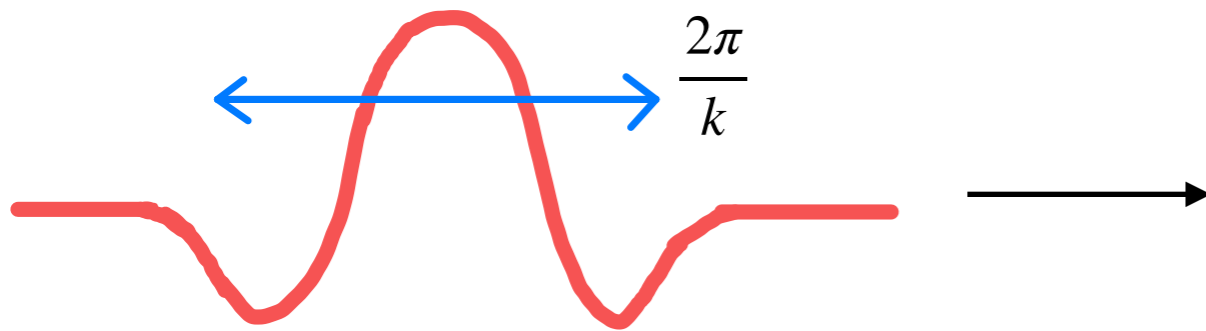


de Broglie wavelength

- atomic spacing $\lambda_a \sim \text{keV}^{-1}$

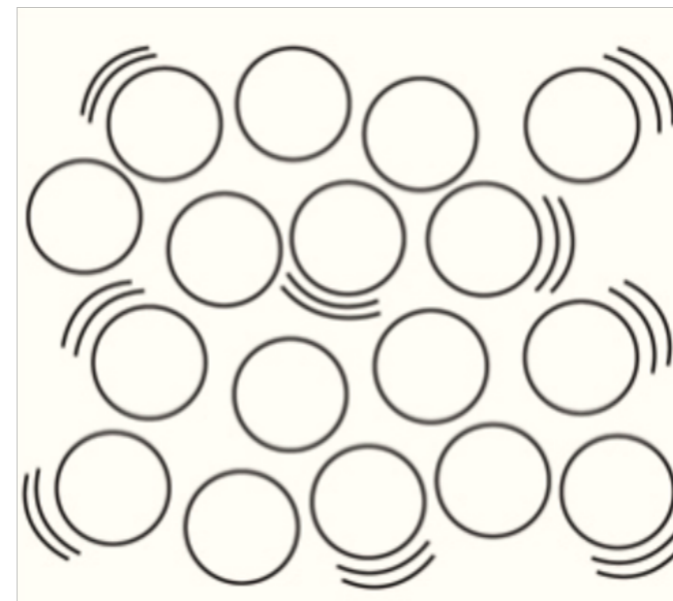
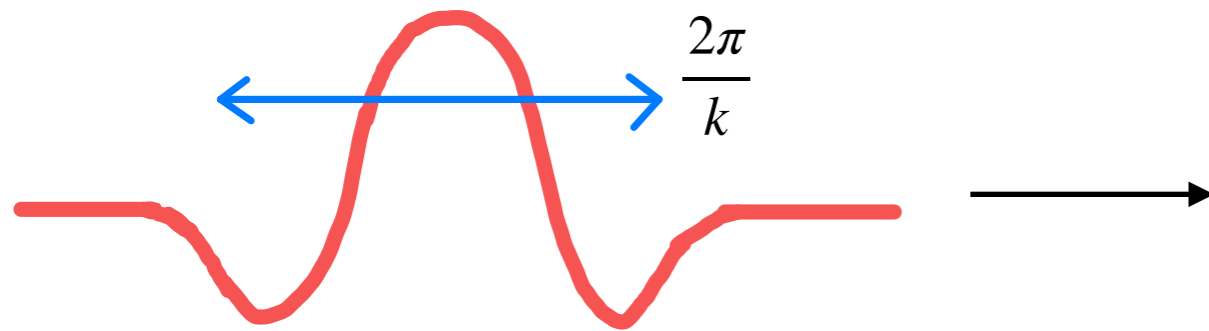
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- atomic spacing $\lambda_a \sim \text{keV}^{-1}$
- incoming particle de Broglie wavelength $\gtrsim \lambda_a$
e.g. **sub-MeV dark matter**, $v \sim 10^{-3} c$

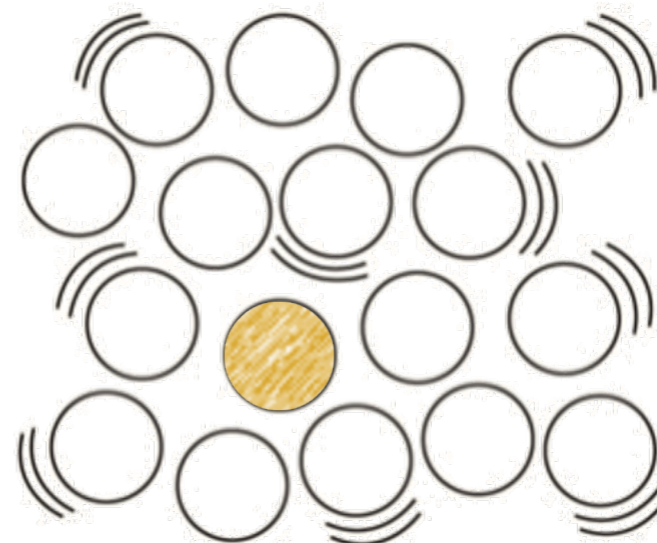
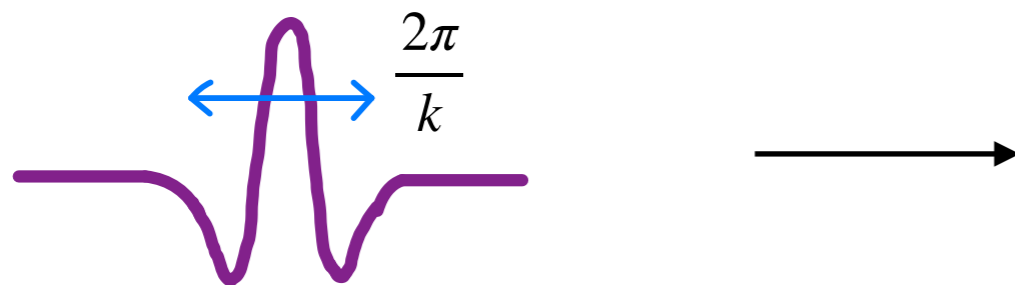


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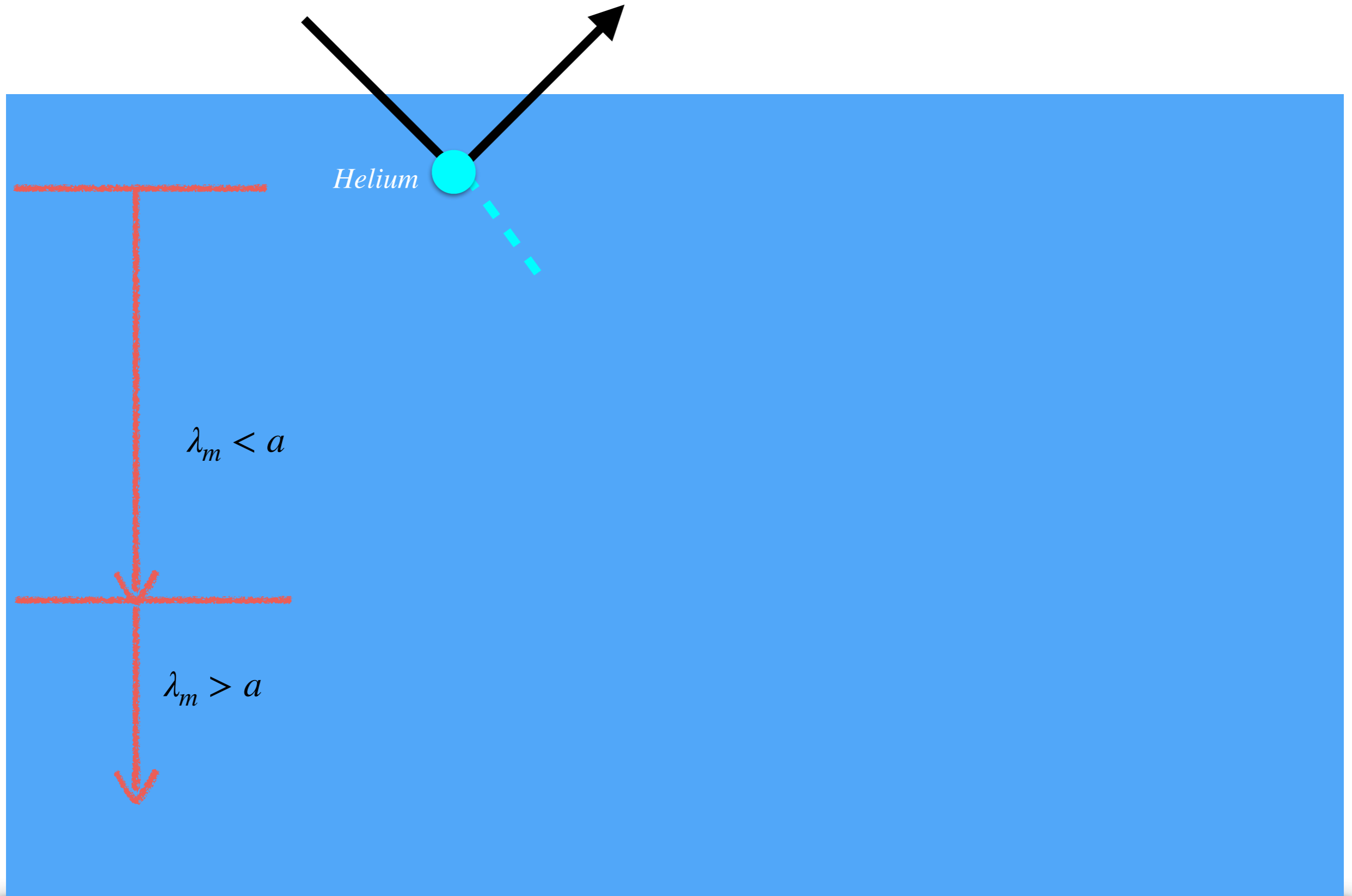
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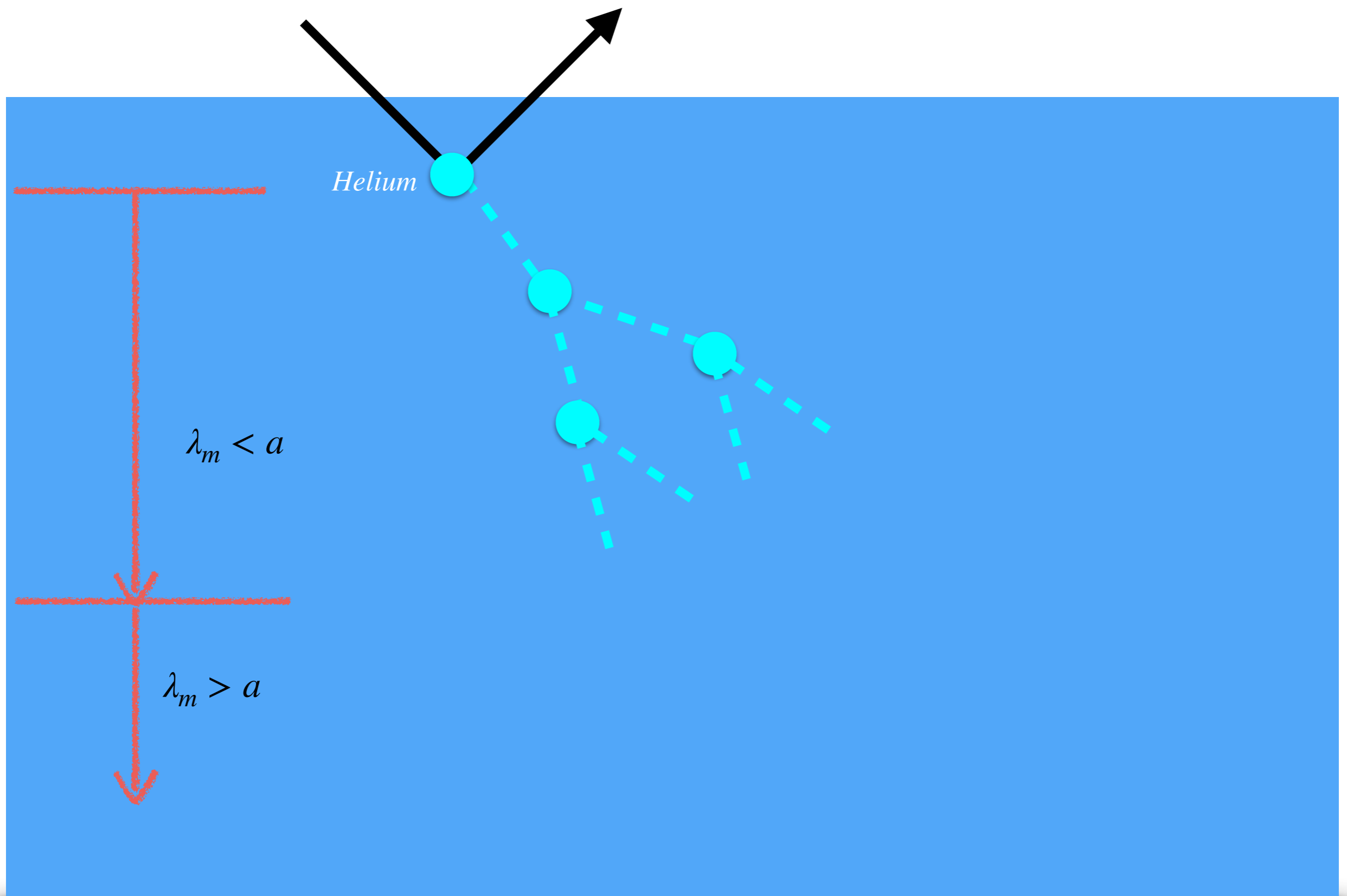
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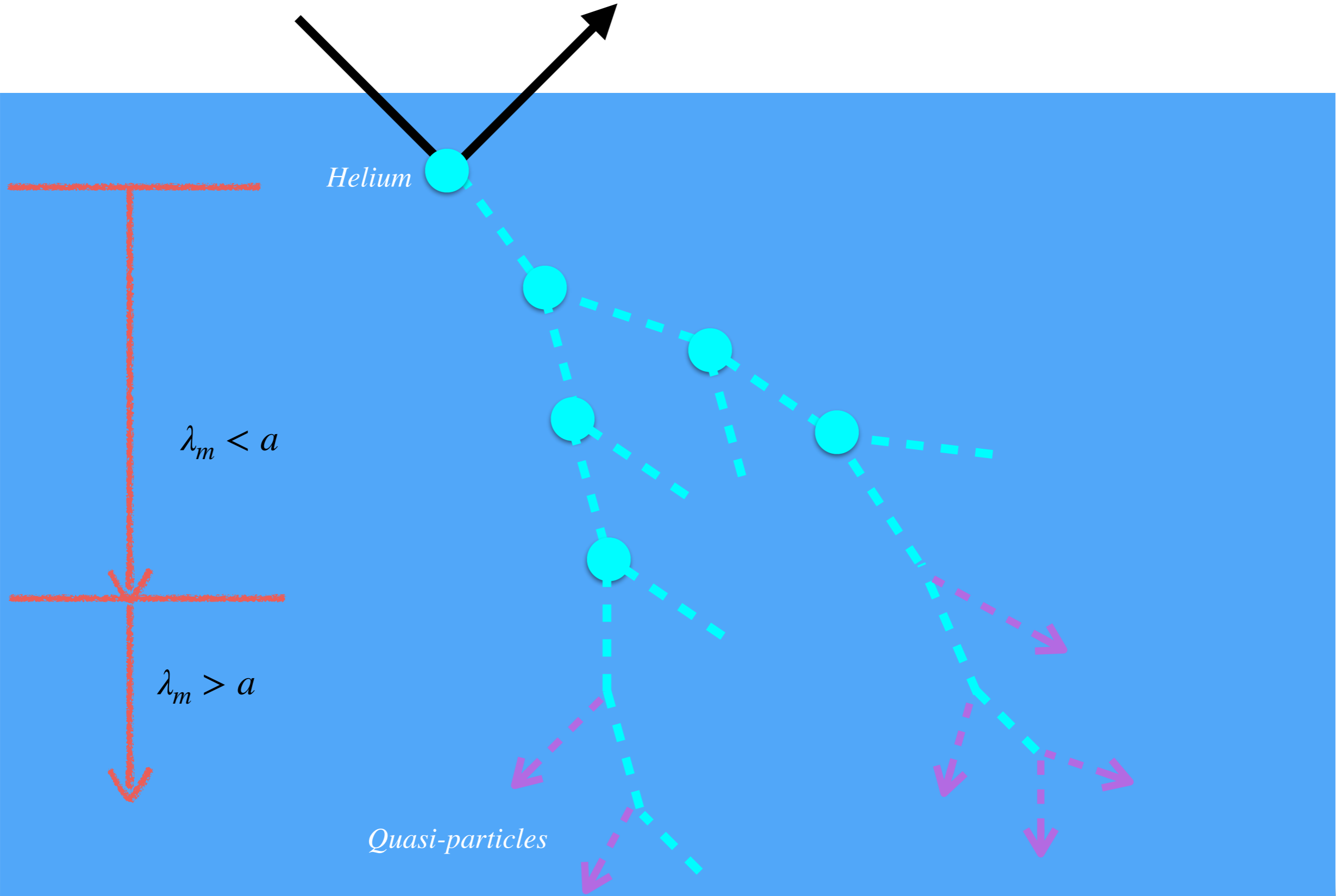
What happens after a MeV-GeV dark matter scattering?

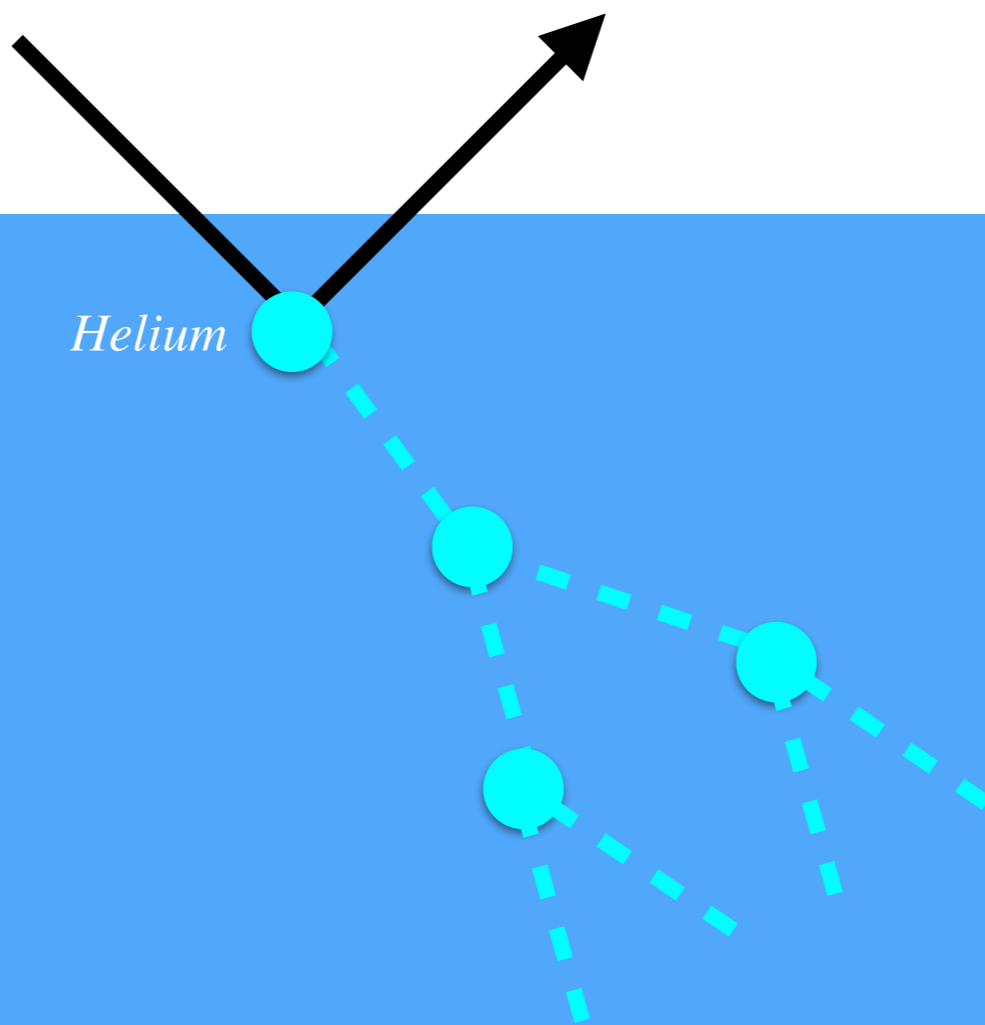


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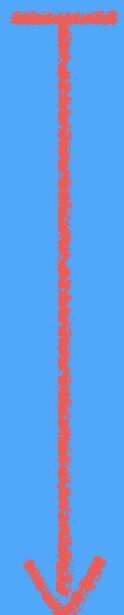
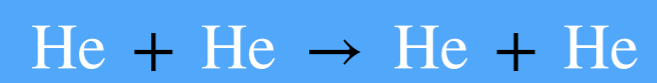


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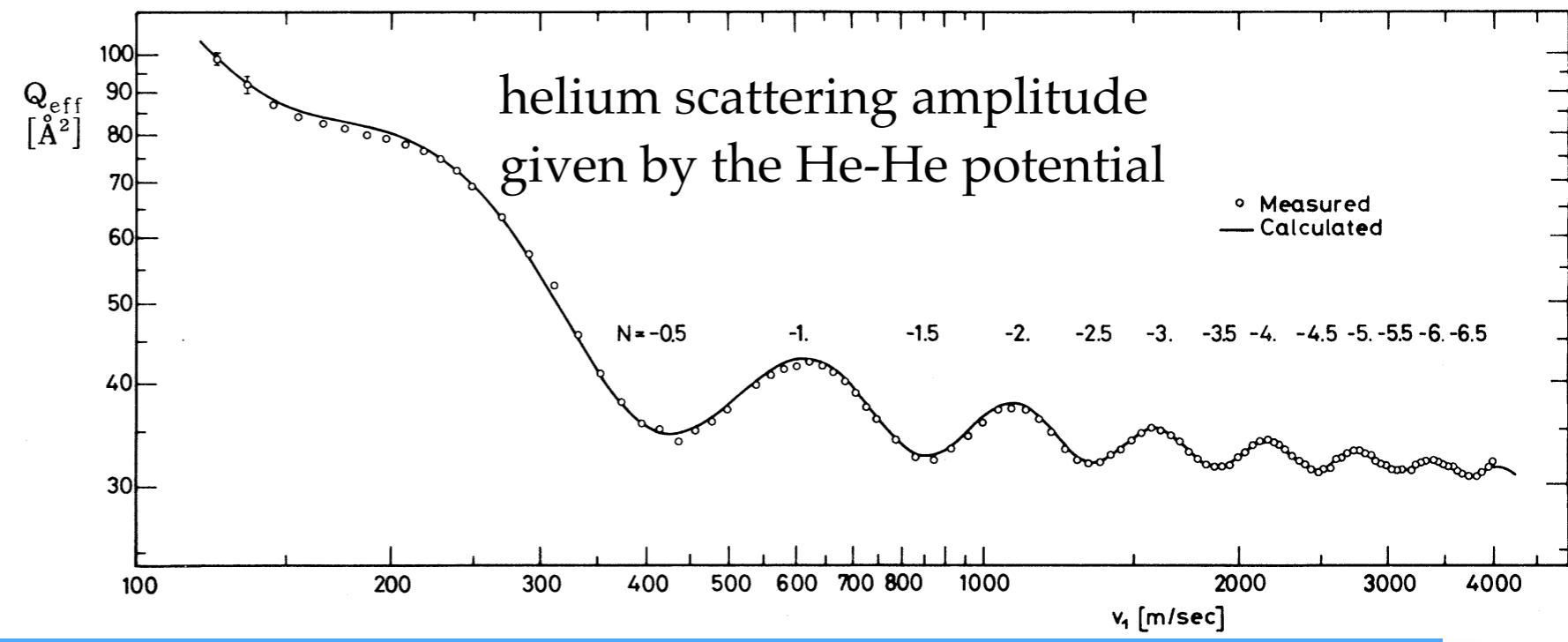
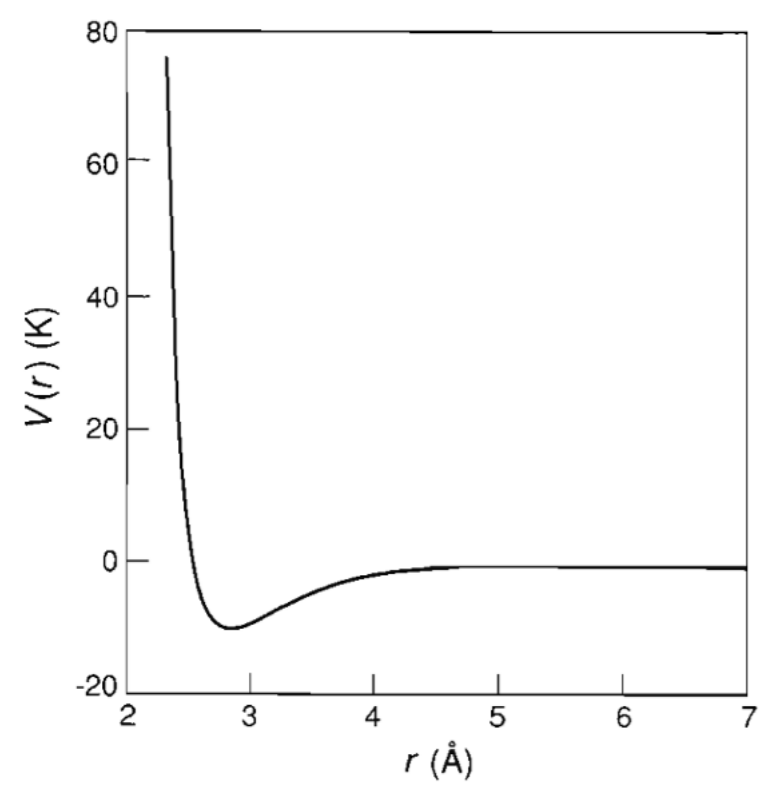


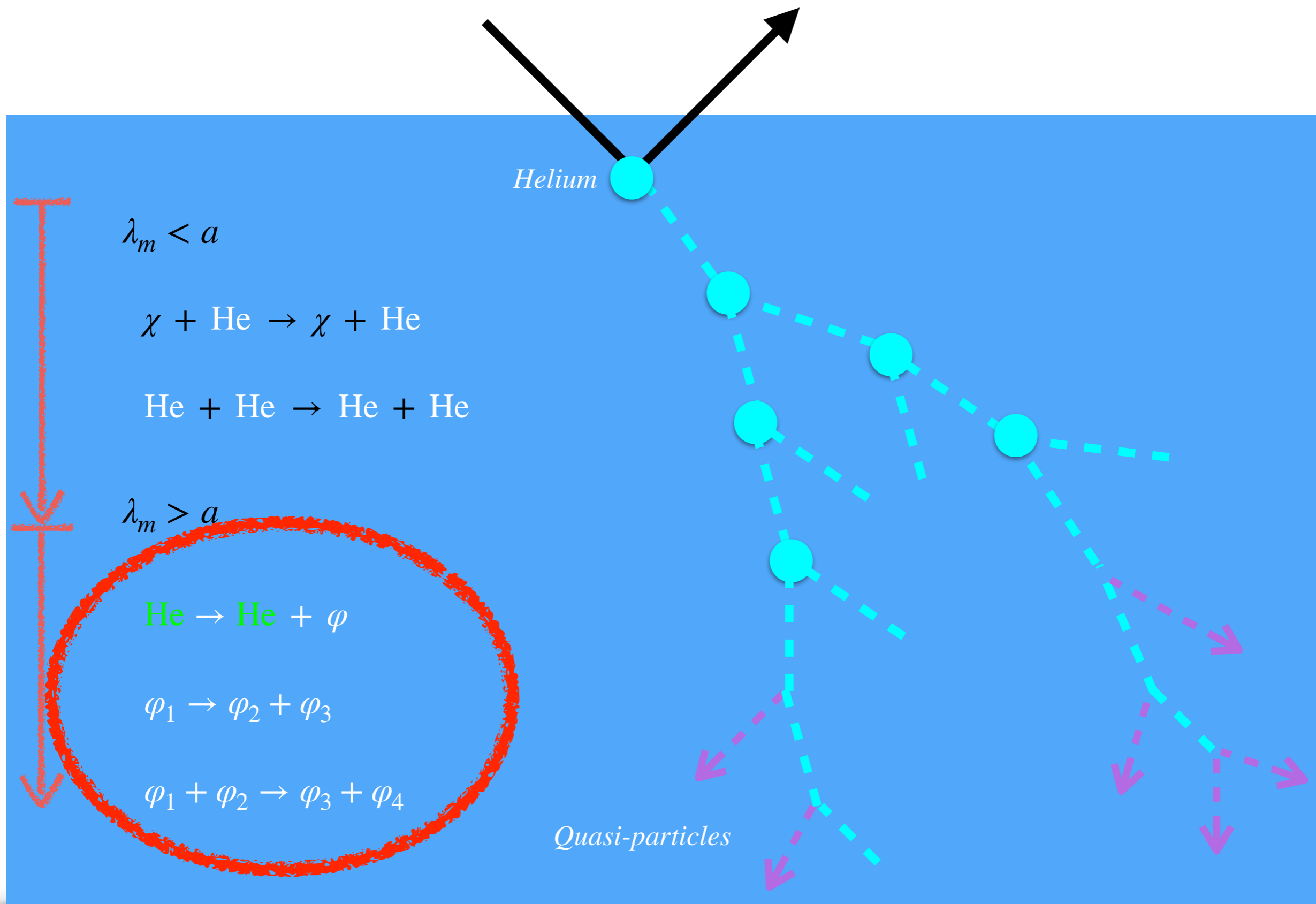


$$\lambda_m < a$$



(a) ^4He - ^4He Interaction Potential





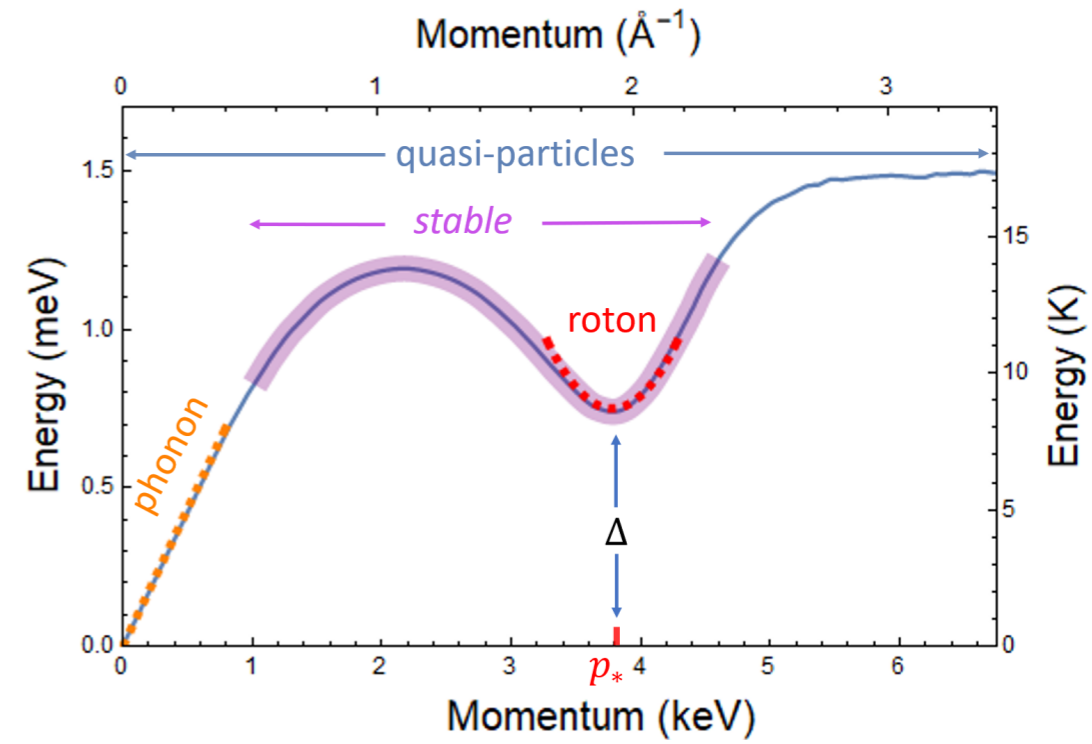
- relevant d.o.f

phonon π [0 , keV] massless goldstone mode

roton φ_r ~ keV

quasi-particles φ (0, 10 keV)

high momentum helium Φ_{He} (\gg keV)



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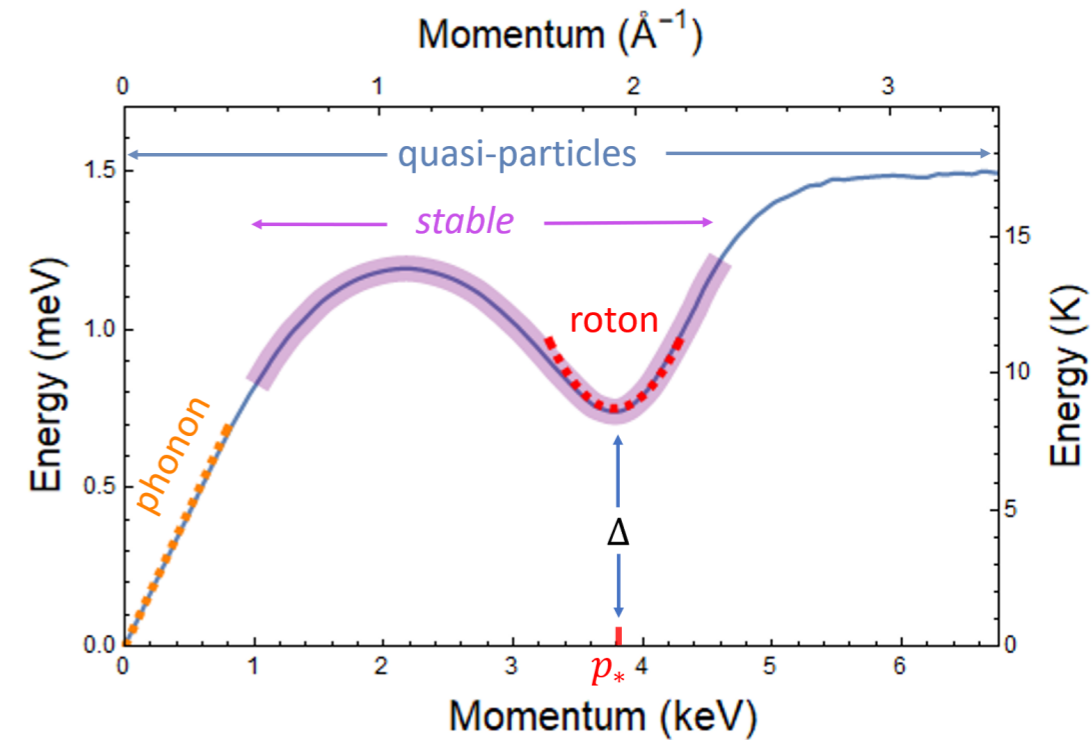
roton $\varphi_r \sim \text{keV}$

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- cutoff $\Lambda \sim \text{keV}$

atomic spacing $\sim (\text{keV})^{-1}$



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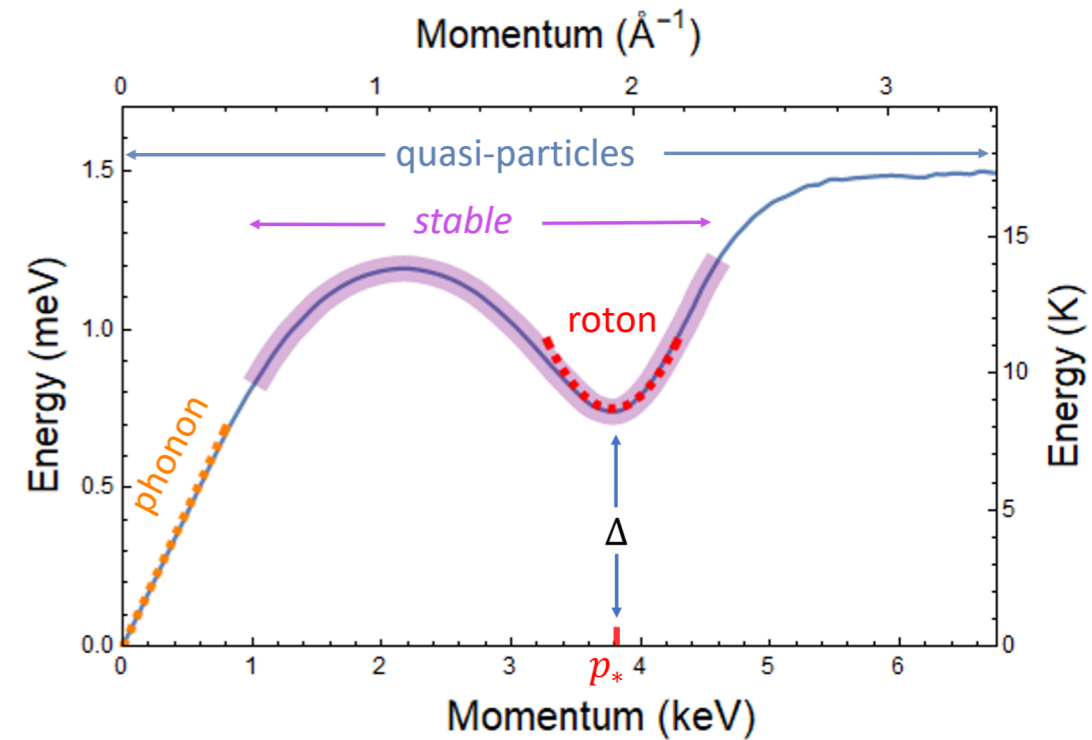
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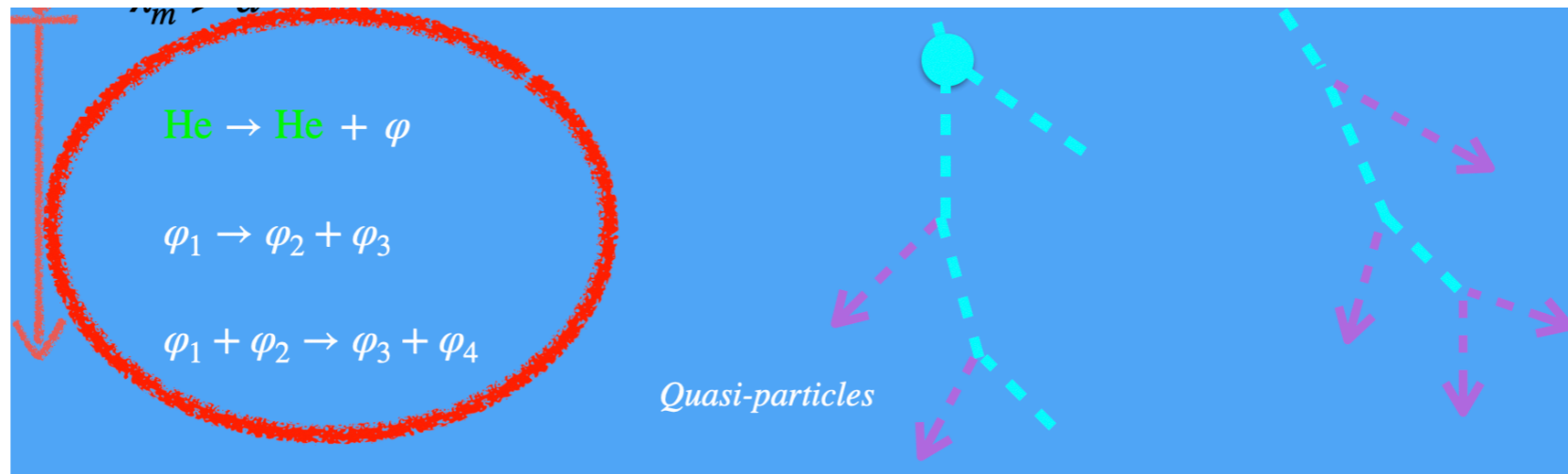
- processes

quasi-particle Helium interactions to study quasi-particle **production**

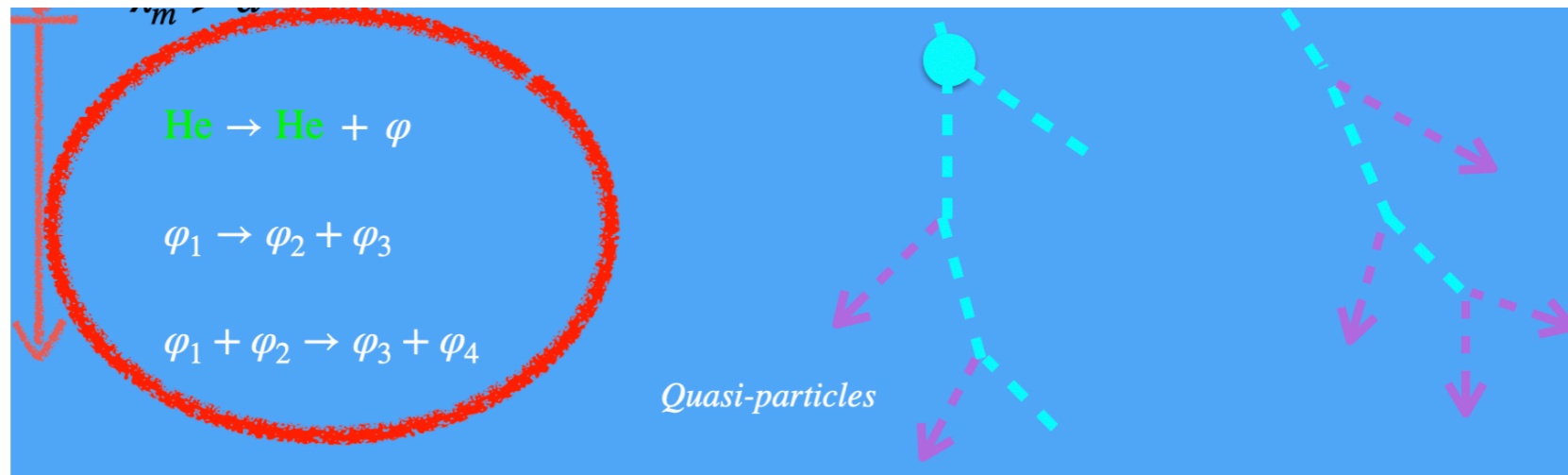
quasi-particle self interactions to understand **thermalization**



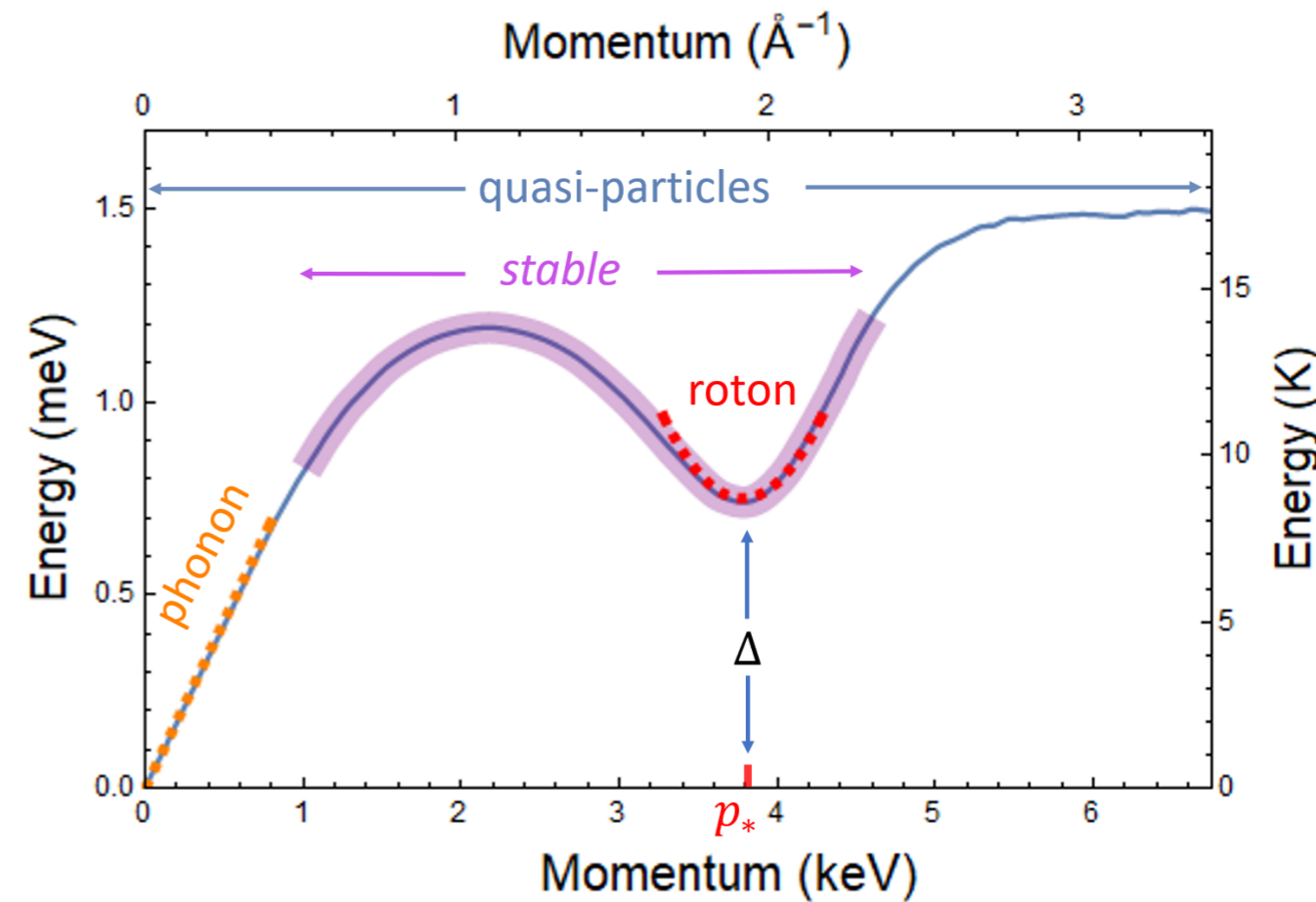
Why it is challenging?



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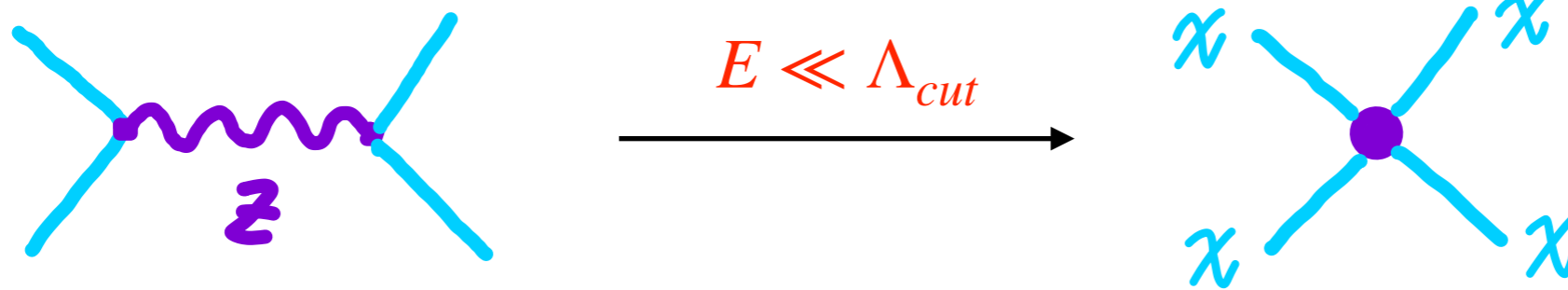
- inverse atomic spacing $\Lambda_{cut} \sim \text{keV}$
- rotons, quasi-particles and heliums
momentum $p \gtrsim \Lambda_{cut}$



Effective field theory

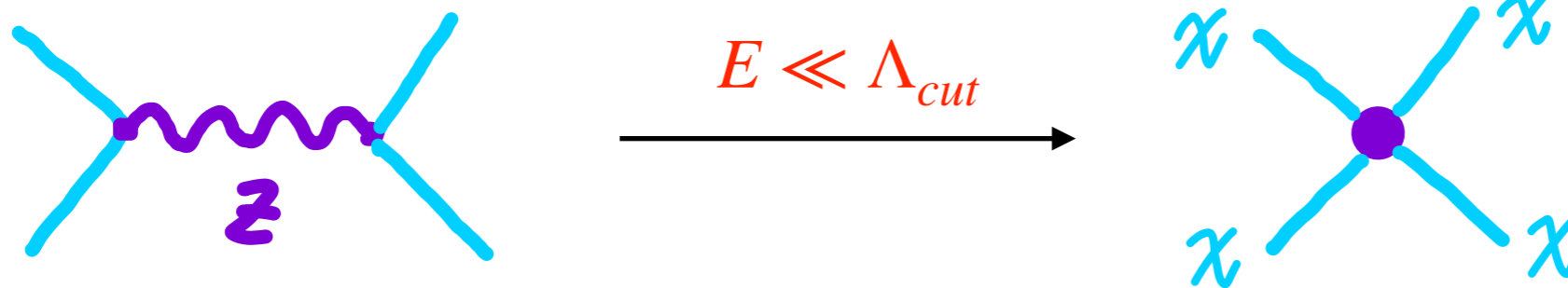
Effective field theory

- find the relevant **degrees of freedom** and **symmetry**
- four-fermion interactions

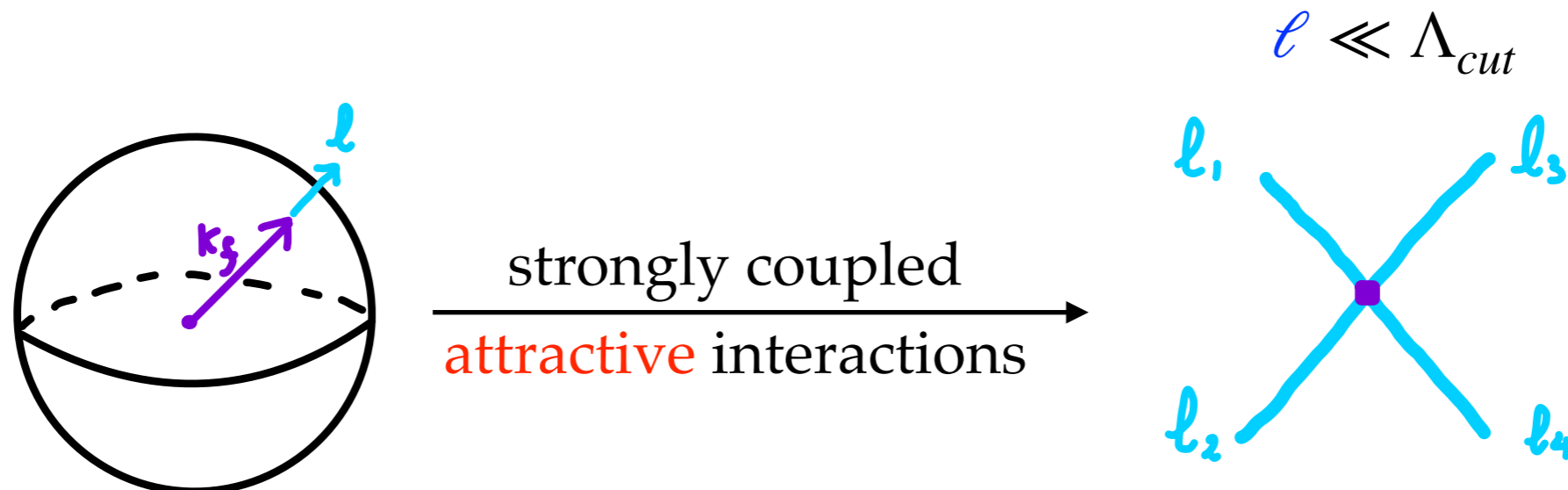


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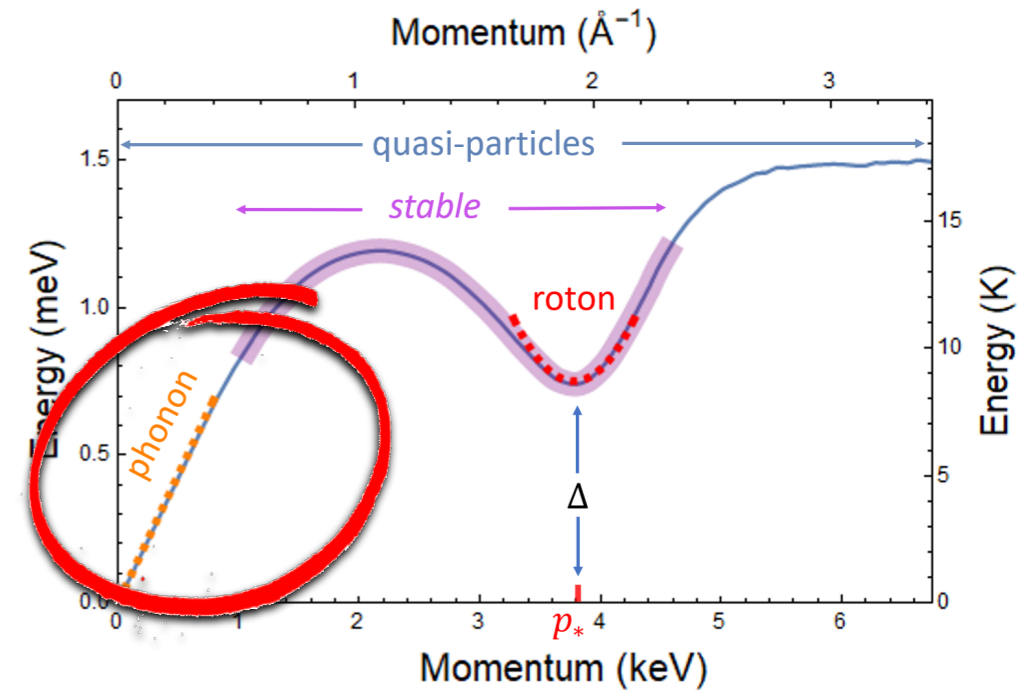


- BCS theory
perturbation around Fermi surface [J. Polchinski, 1999]



Phonons π ($p \ll \Lambda$ ($\sim \text{keV}$))

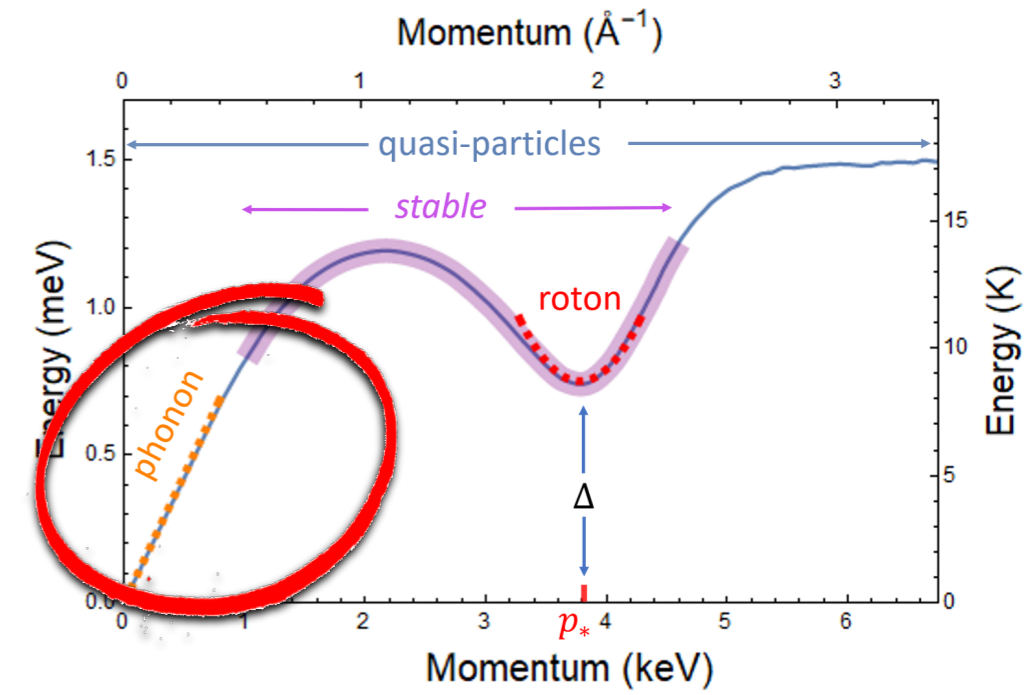
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- Similar to [chiral perturbation theory](#) (pions)
Effective quantum action method [D. Son, 2002]



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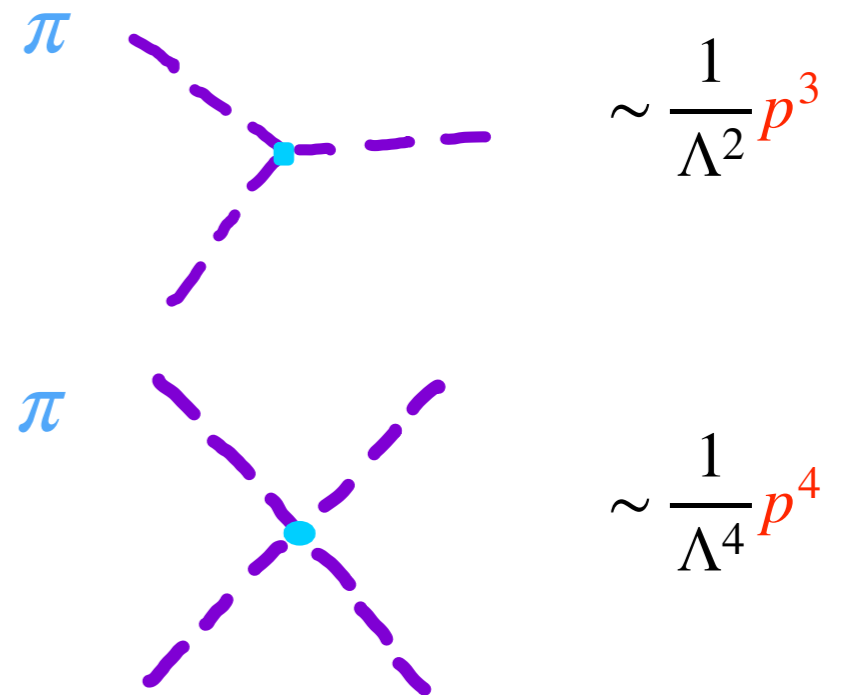
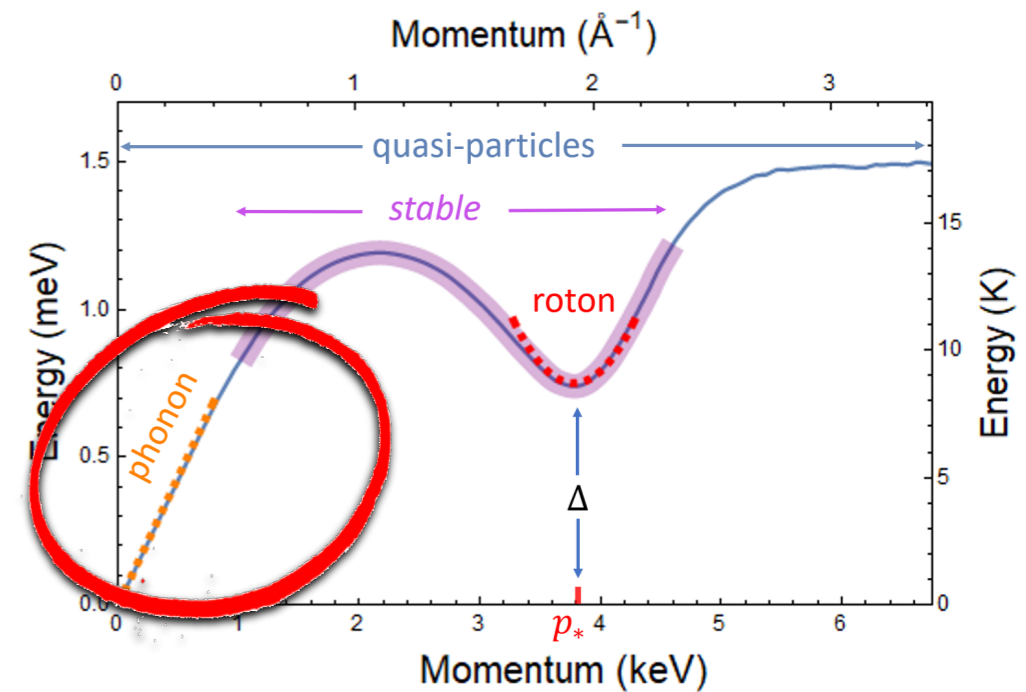
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Effective quantum action method [D. Son, 2002]

- or Power counting method

$$[p] = 1, \quad [t] = -1, \quad [x] = -1, \quad [\pi] = 1$$

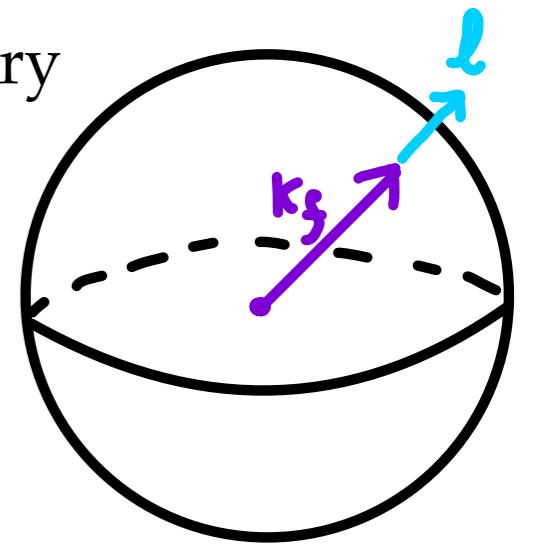
phonon interactions

$$\mathcal{L}_{\text{ph}} = -\frac{c_s^{3/2}}{2\Lambda^2} \dot{\pi} \partial_i \pi \partial_i \pi + \frac{g_3 c_s^{-1/2}}{6\Lambda^2} \dot{\pi}^3 + \mathcal{O}(\pi^4)$$



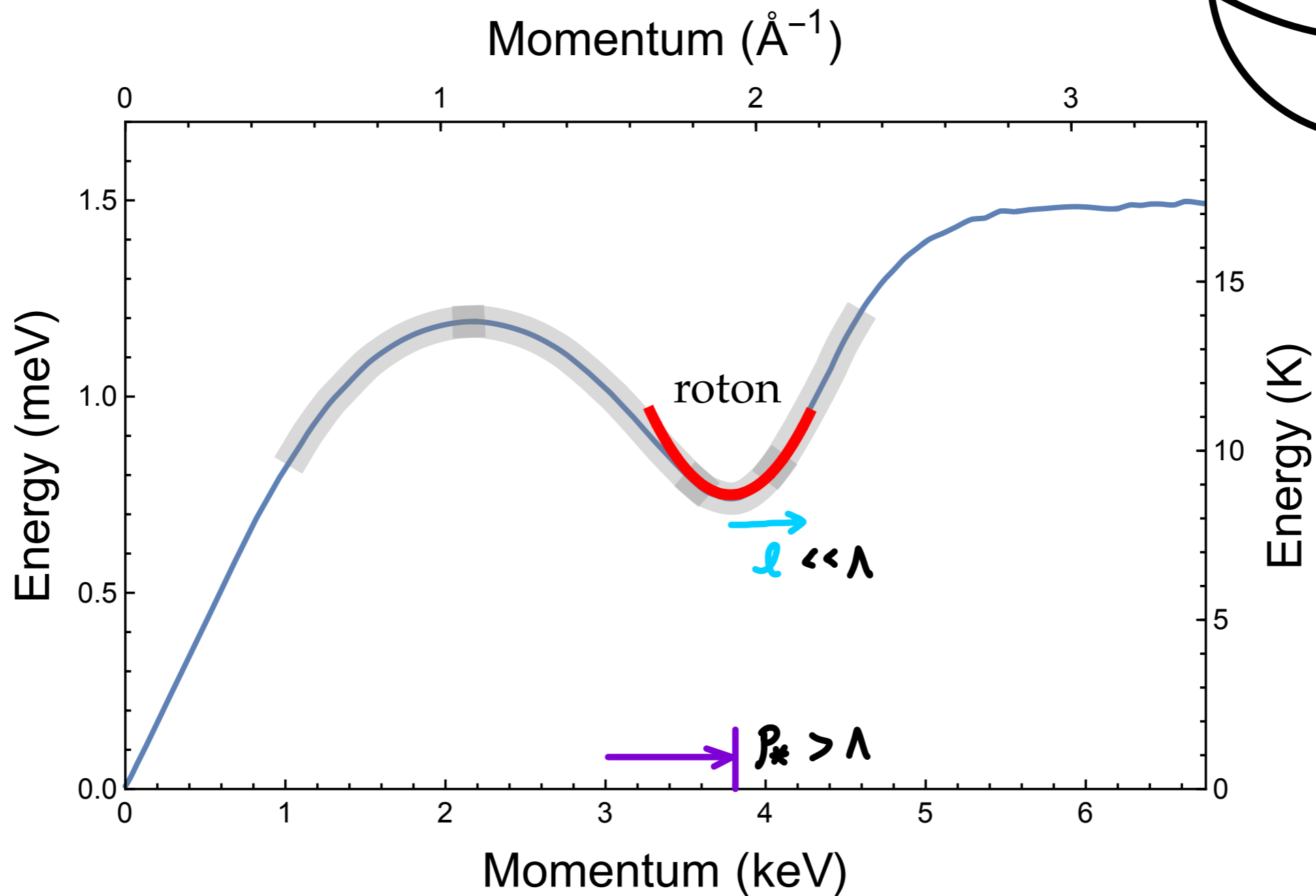
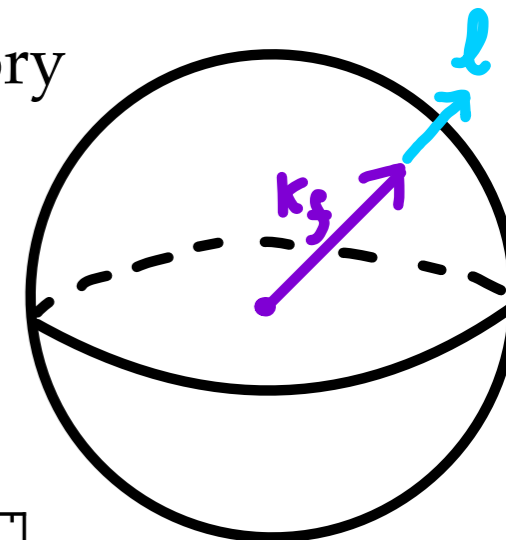
Roton effective field theory

BCS theory



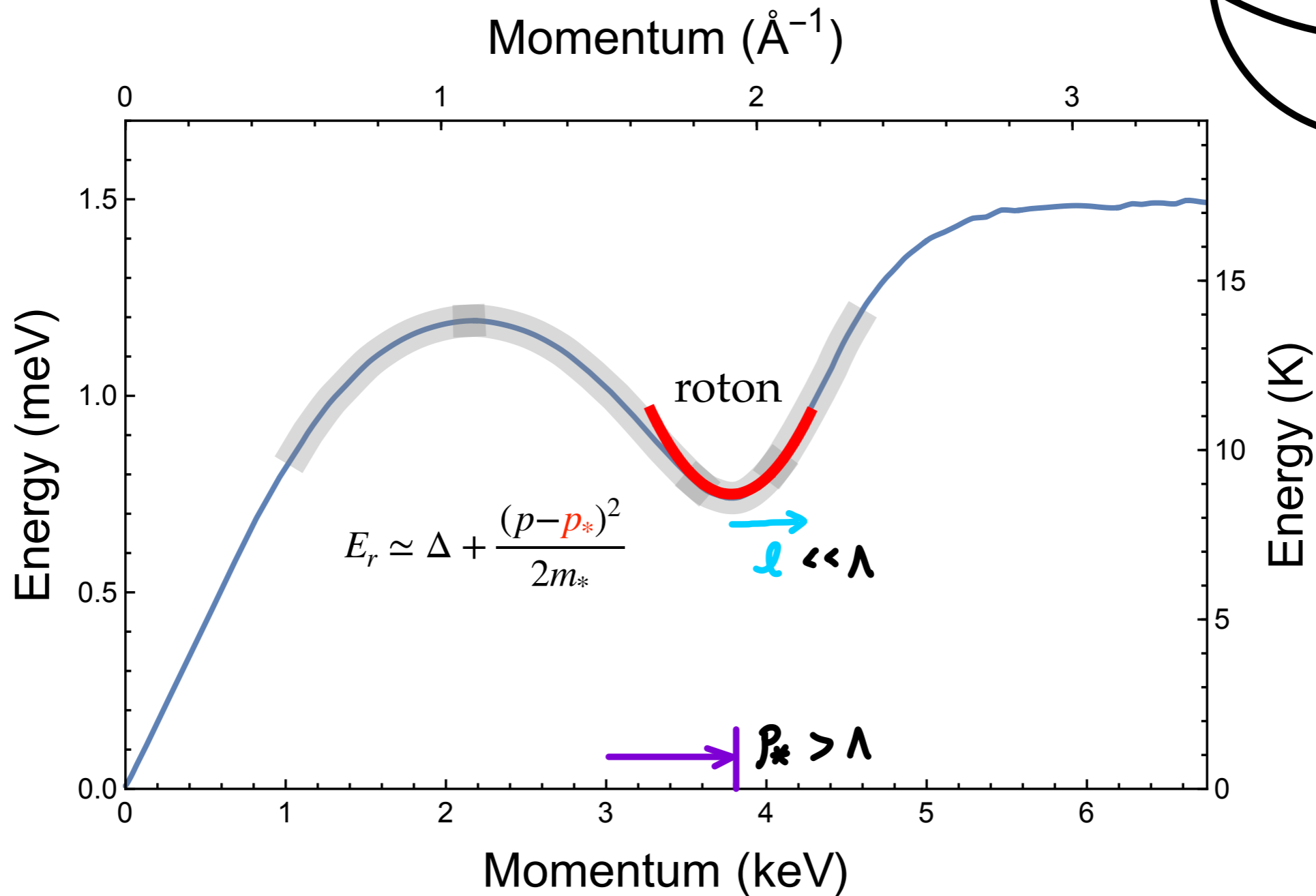
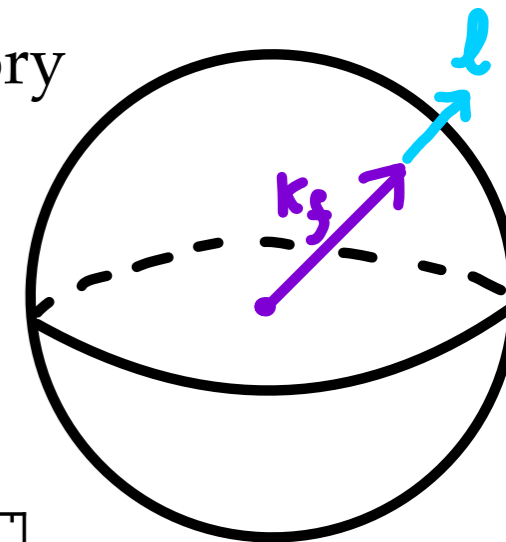
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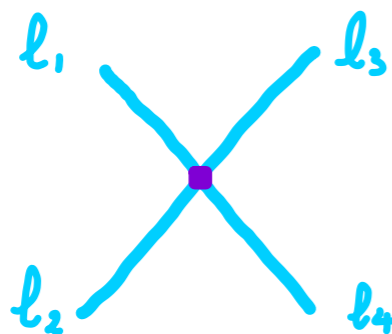
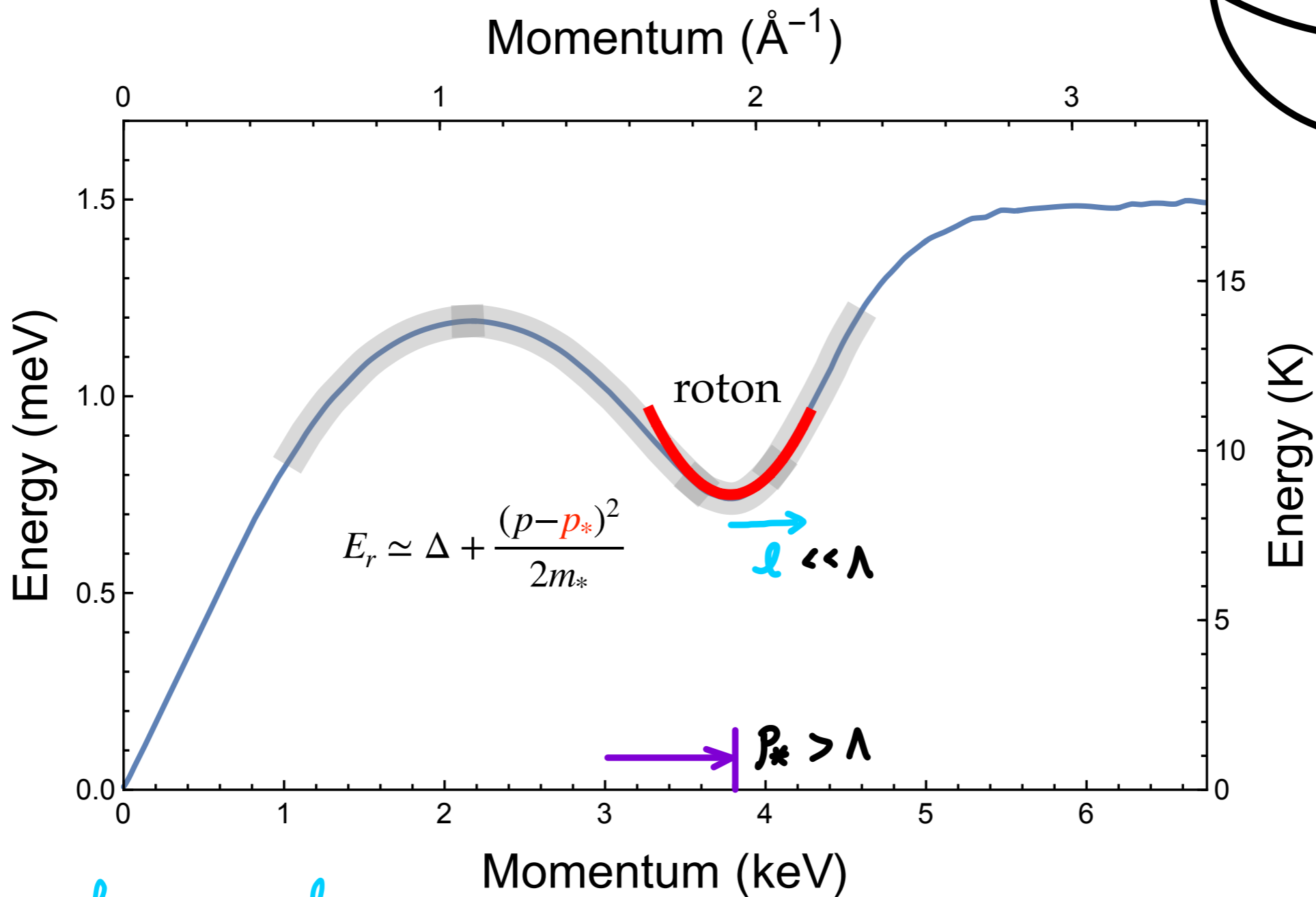
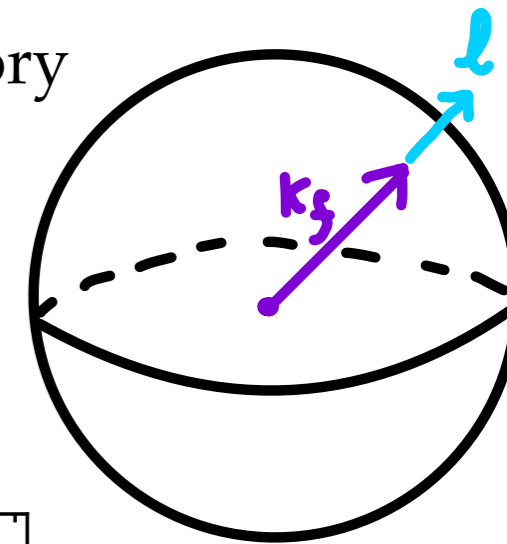
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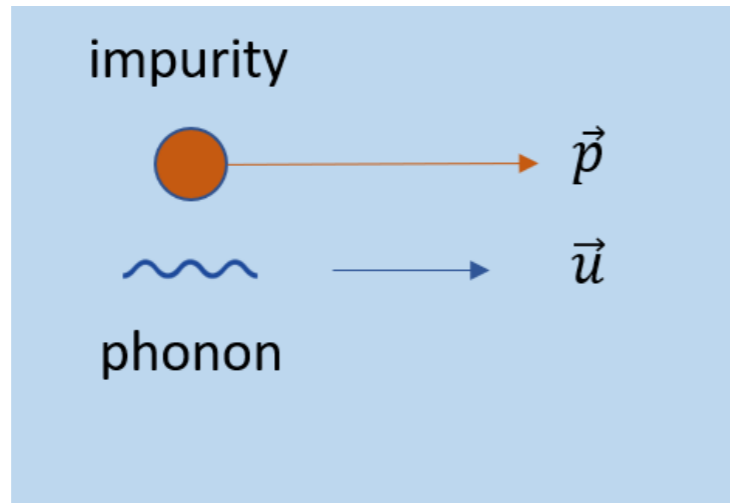
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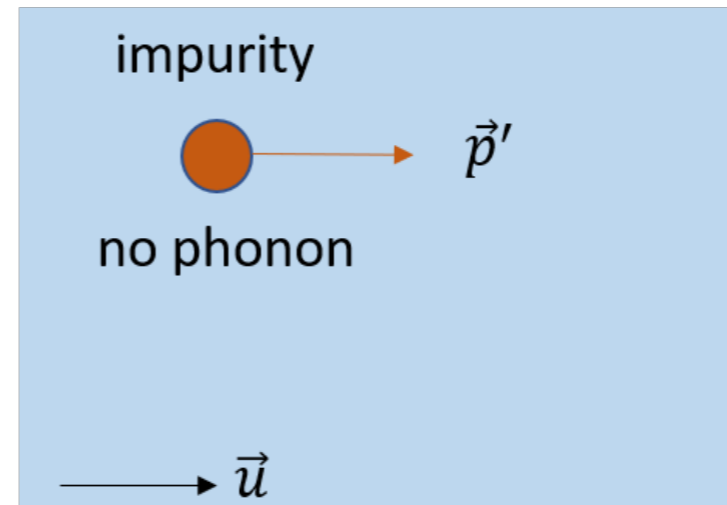


$\lambda_r \simeq 0.93$ consistent with data

Roton and phonon interactions

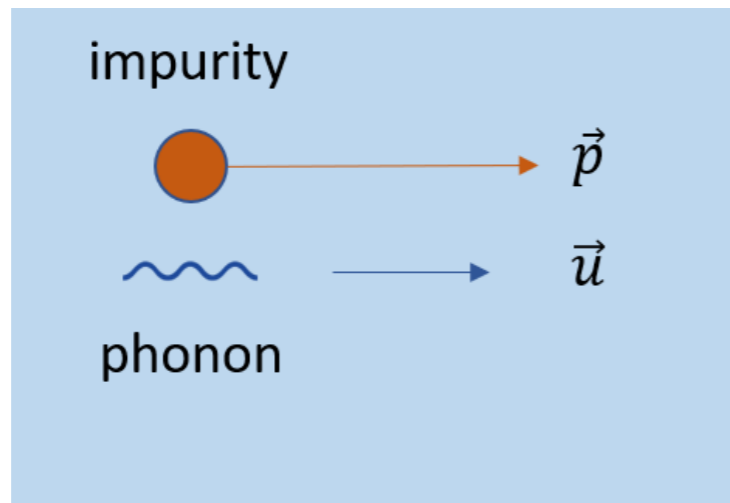


Lab frame

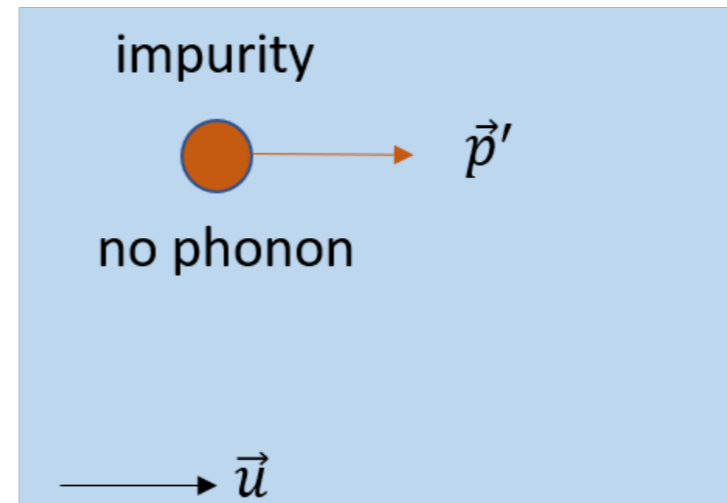


Boosted frame

Roton and phonon interactions



Lab frame

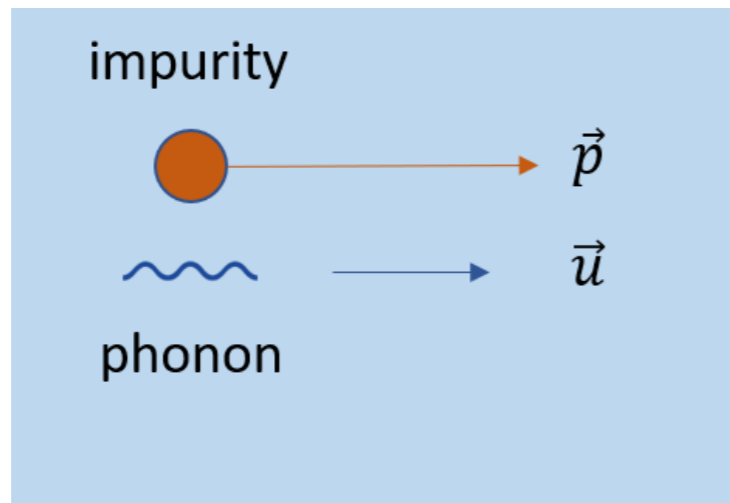


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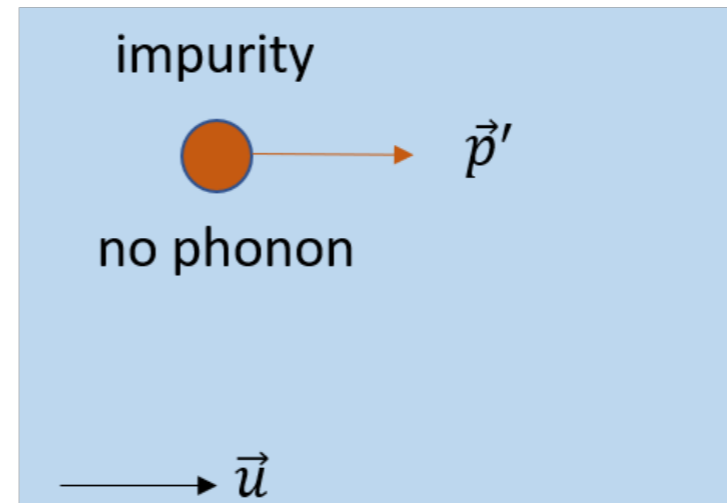
- **roton** (as impurity) and phonon interactions

$$V_{\text{ph-r}} = \epsilon_{\text{boost}} - \epsilon_{\text{lab}} + \mathbf{p} \cdot \mathbf{u}$$

Roton and phonon interactions



Lab frame



Boosted frame

- **roton** (as impurity) and phonon interactions

$$V_{\text{ph-r}} = \epsilon_{\text{boost}} - \epsilon_{\text{lab}} + \mathbf{p} \cdot \mathbf{u}$$

- This method can be applied to **dark matter, quasiparticles**, etc.

Helium atom Φ_{He} ($p \gg \text{keV}$)

- U(1) symmetry $\Phi_{\text{He}} \rightarrow e^{i\alpha} \Phi_{\text{He}}$

effective field theory breaks down? $p \gg \Lambda$

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- **Similar to** Heavy quark effective theory

$$\mathbf{p} = m_Q \mathbf{v} + \mathbf{k} \quad , \quad \Lambda/m_Q \ll 1$$

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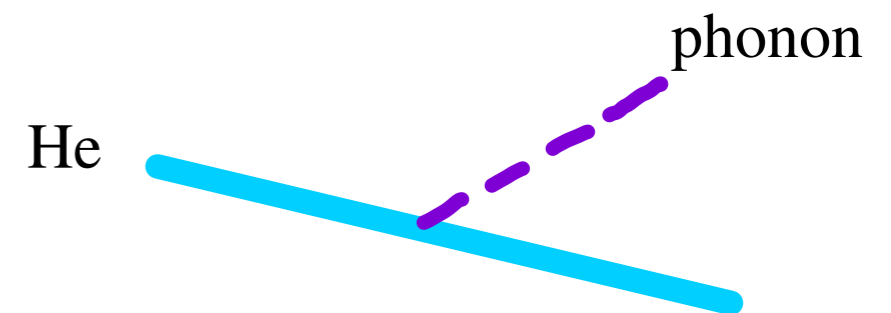
- Helium currents $J_{\text{He}}^0, J_{\text{He}}^i$

$$J_{\text{He}}^0 = \Phi^\dagger \Phi, \quad J_{\text{He}}^i = v^i \Phi^\dagger \Phi$$

Phonon currents J^0, J^i

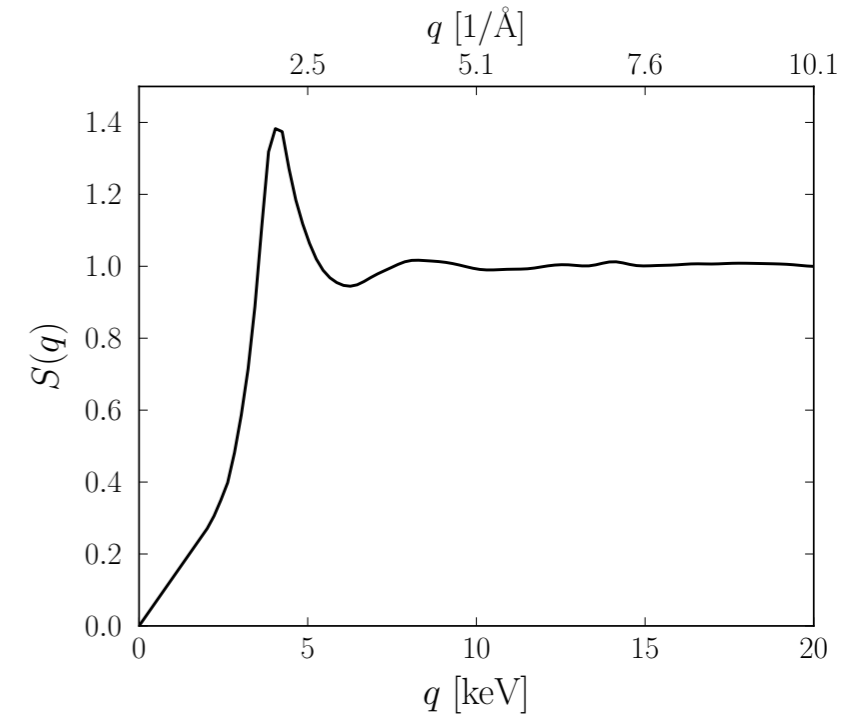
$$J^0 = (\sqrt{\rho}/m_{\text{He}} c_s) \dot{\pi} + \dots,$$

$$\mathcal{L}_{JJ} = \lambda_1 \frac{1}{m_{\text{He}} \Lambda} J^0 J_{\text{He}}^0 + \lambda_2 \frac{m_{\text{He}}}{\Lambda^3} J^i J_{\text{He}}^i$$



He \rightarrow He + quasi-particle from measurement

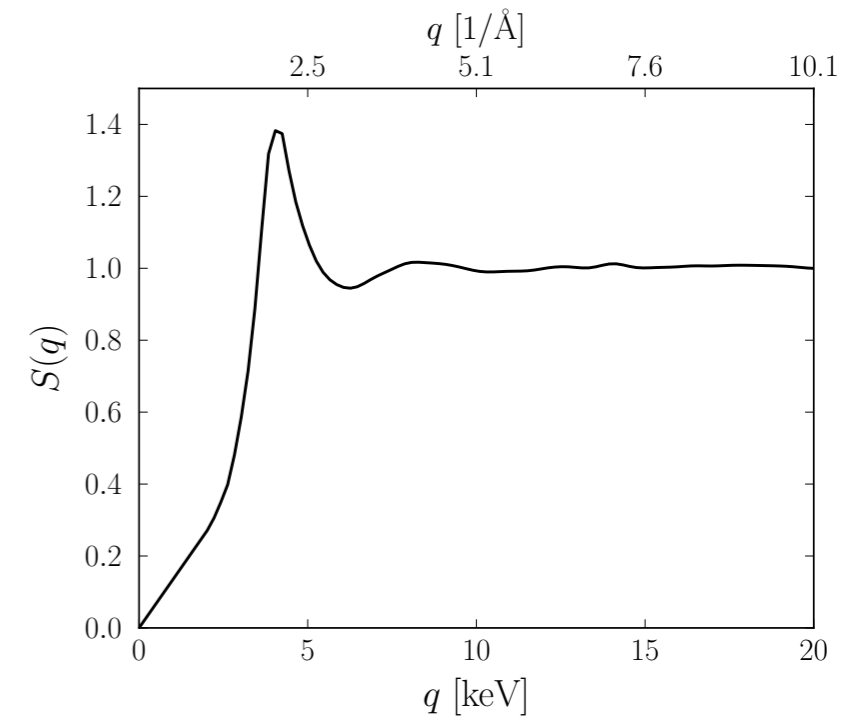
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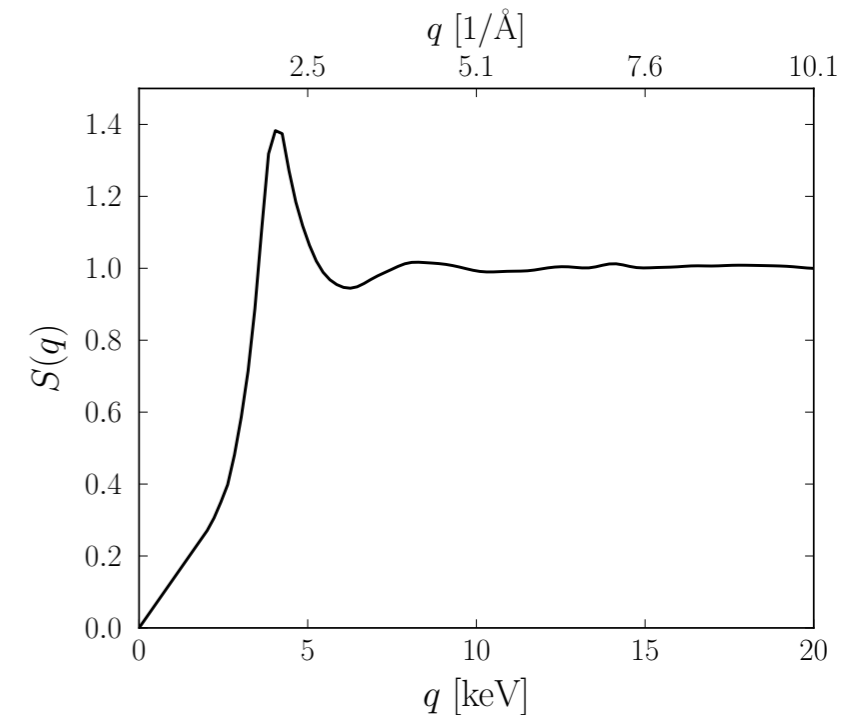
\Rightarrow HEP language, $S(q) = |\langle vac | j_0 | \varphi \rangle|^2$
Current conservation, we can know $|\langle vac | j_i | \varphi \rangle|^2$



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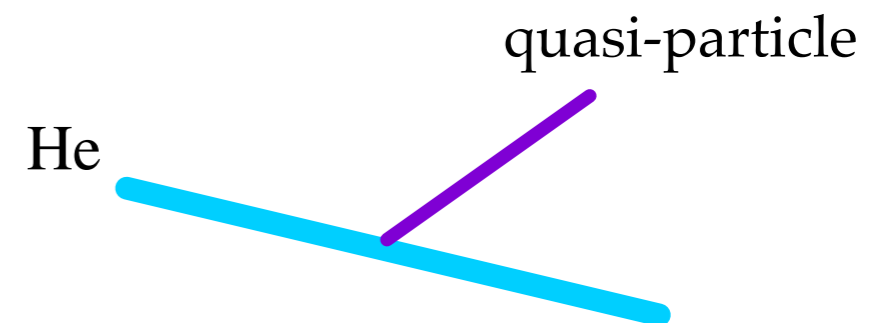
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- Helium decay to a quasi-particle,

$$\mathcal{L}_{JJ} = \lambda_1 \frac{1}{m_{\text{He}} \Lambda} J^0 J_{\text{He}}^0 + \lambda_2 \frac{m_{\text{He}}}{\Lambda^3} J^i J_{\text{He}}^i$$

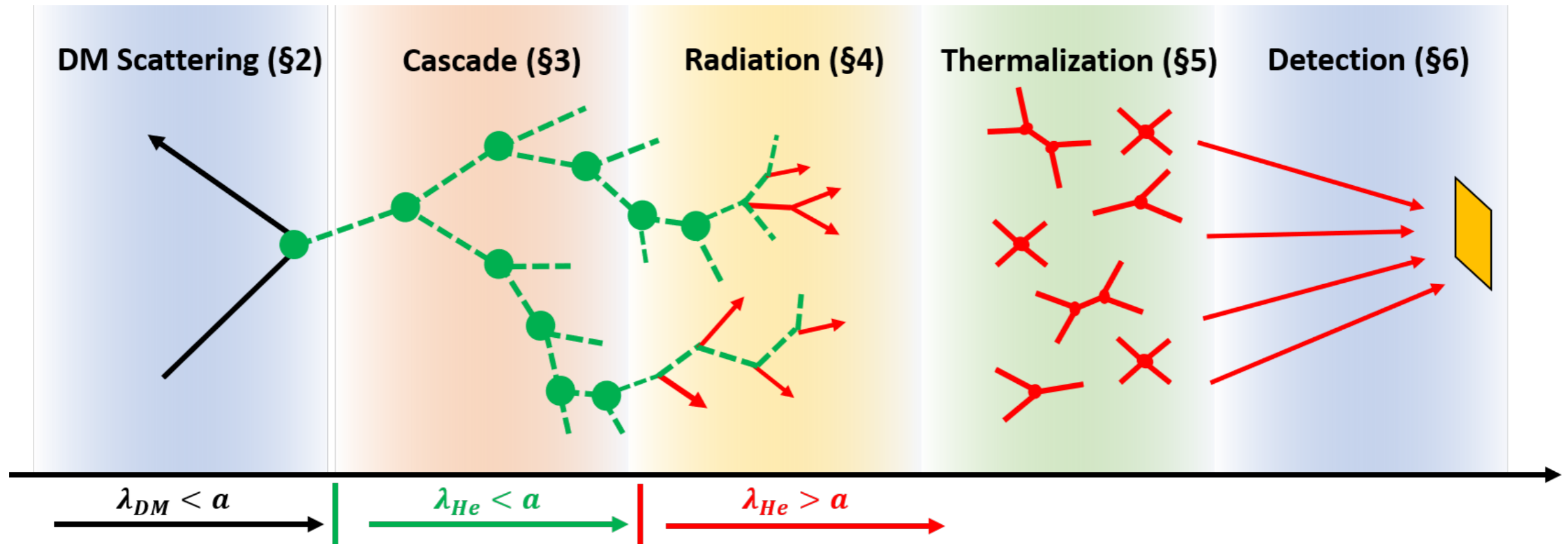
$$\text{amplitude } \mathcal{M} \propto \lambda_1 J_{\text{He}}^0 \langle vac | J^0 | \varphi \rangle + \lambda_2 J_{\text{He}}^i \langle vac | J^i | \varphi \rangle$$



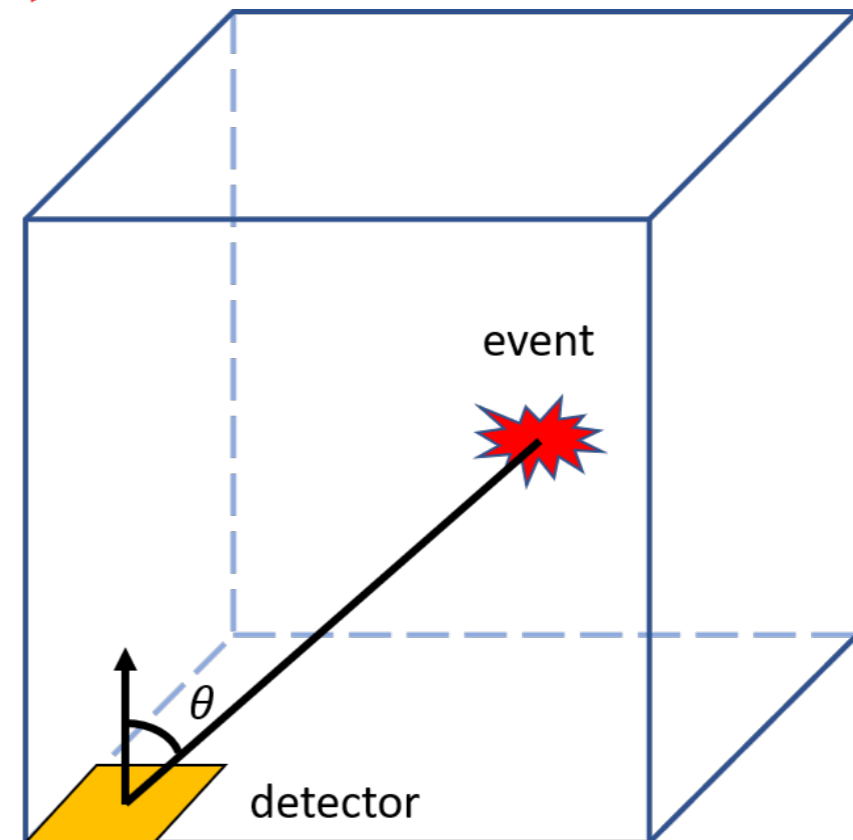
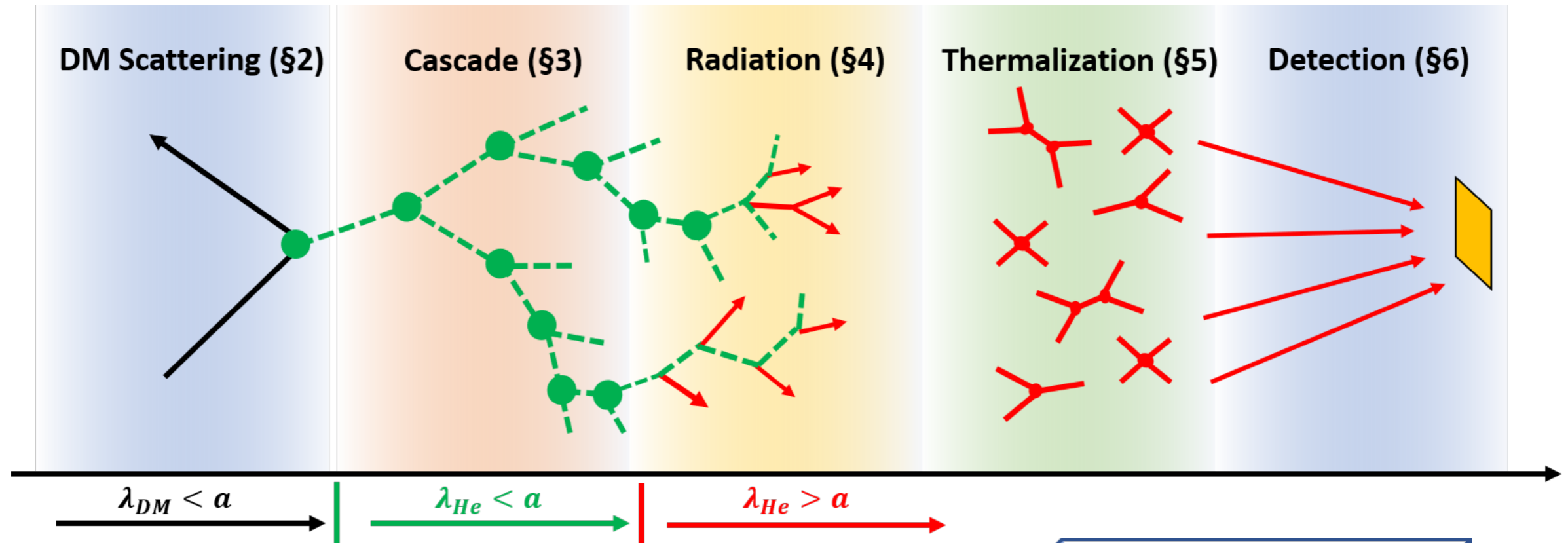
Rate summary

Process	Diagram	Result
Phonon decay $\pi \rightarrow \pi + \pi$		$\Gamma = \frac{(u+1)^2 c_s p^5}{120\pi\Lambda^4}$
Phonon self-scattering $\pi + \pi \rightarrow \pi + \pi$		$\langle \sigma \Delta v \rangle_\theta \simeq \frac{(2u+2)^2 c_s p_1^4}{96^2 \gamma \pi \Lambda^6}$
Roton self-scattering $\varphi_r + \varphi_r \rightarrow \varphi_r + \varphi_r$		$\sigma = \frac{2\lambda_r^2}{ \mathbf{v}_1 - \mathbf{v}_2 \cos \frac{\theta}{2} m_* p_*}$
Roton-phonon scattering $\pi + \varphi_r \rightarrow \pi + \varphi_r$		$\langle \sigma \rangle_\Omega = \frac{1}{4\pi} \left[\frac{1}{25\Lambda^8} \frac{p_*^4 k^4}{m_*^2 c_s^2} + \frac{2432 + 45\pi^2}{11520\Lambda^8} p_*^2 k^4 + \frac{2y_4}{9\Lambda^7} \frac{p_*^2 k^4}{m_* c_s} + \frac{y_4^2}{\Lambda^6} k^4 \right]$
Helium emits quasiparticles $\text{He} \rightarrow \text{He} + \varphi$		$\Gamma_m = \frac{2\pi\rho}{m_{\text{He}}} \int \frac{d^3k}{(2\pi)^3} \left(\frac{\lambda_1}{m_{\text{He}}\Lambda} + \frac{\lambda_2 m_{\text{He}} \mathbf{v}_{\text{He}} \cdot \mathbf{k}\omega}{\Lambda^3 k^2} \right)^2 S(\mathbf{k}, \omega)$ Single emission: $S(\mathbf{k}, \omega) \rightarrow S(k)\delta(E_i - E_f - \omega)$
DM emits quasiparticles $\text{DM} \rightarrow \text{DM} + \varphi$		$\Gamma_s = \frac{\rho}{2\pi m_{\text{He}} v_{\text{DM}}} \left(\frac{\lambda}{m_\sigma^2} \right)^2 \int k S(k) dk$ $\Gamma_m = \frac{2\pi\rho}{m_{\text{He}}} \left(\frac{\lambda}{m_\sigma^2} \right)^2 \int \frac{d^3k}{(2\pi)^3} S(\mathbf{k}, \omega)$

Thermalization and Detection

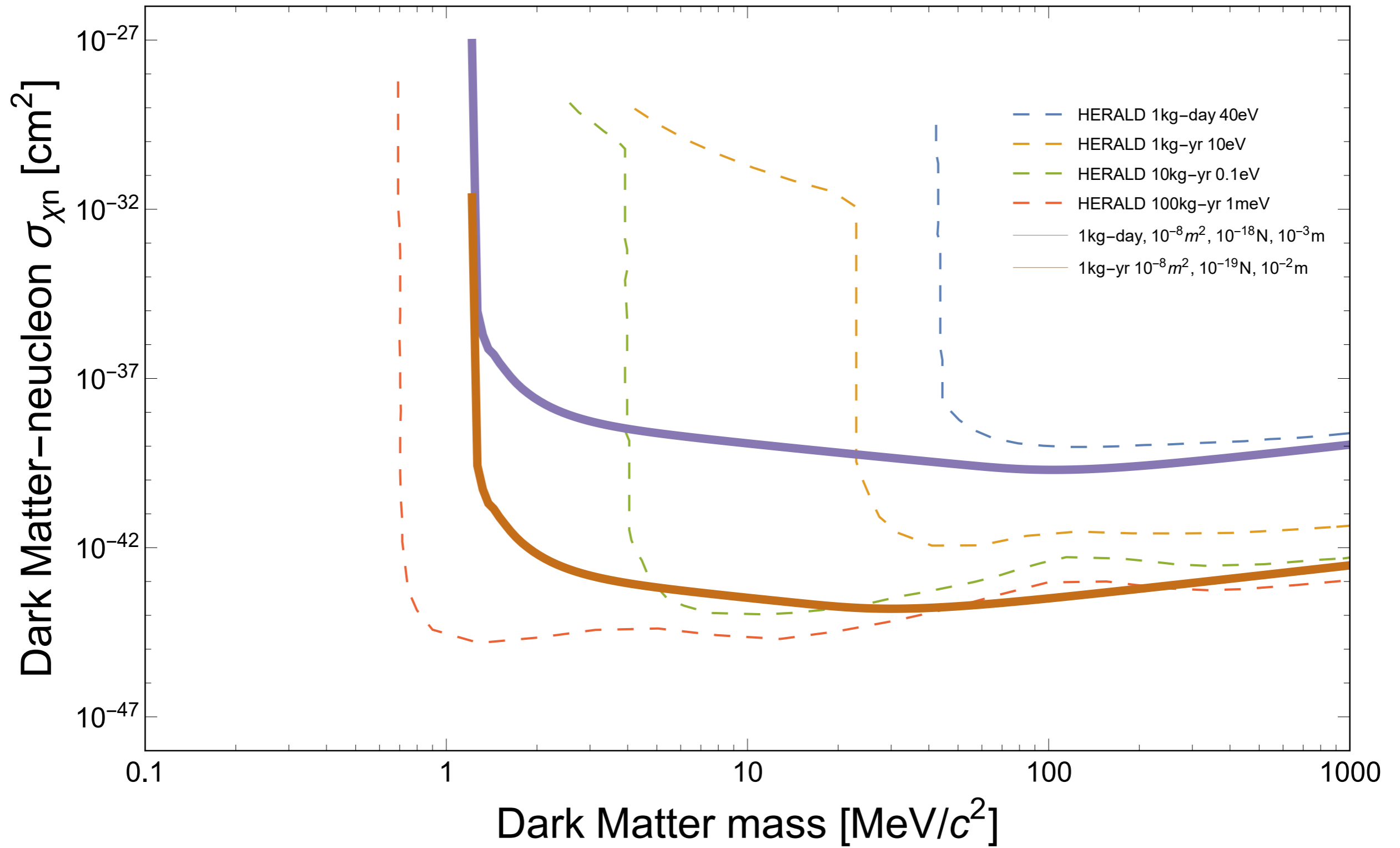


Thermalization and Detection



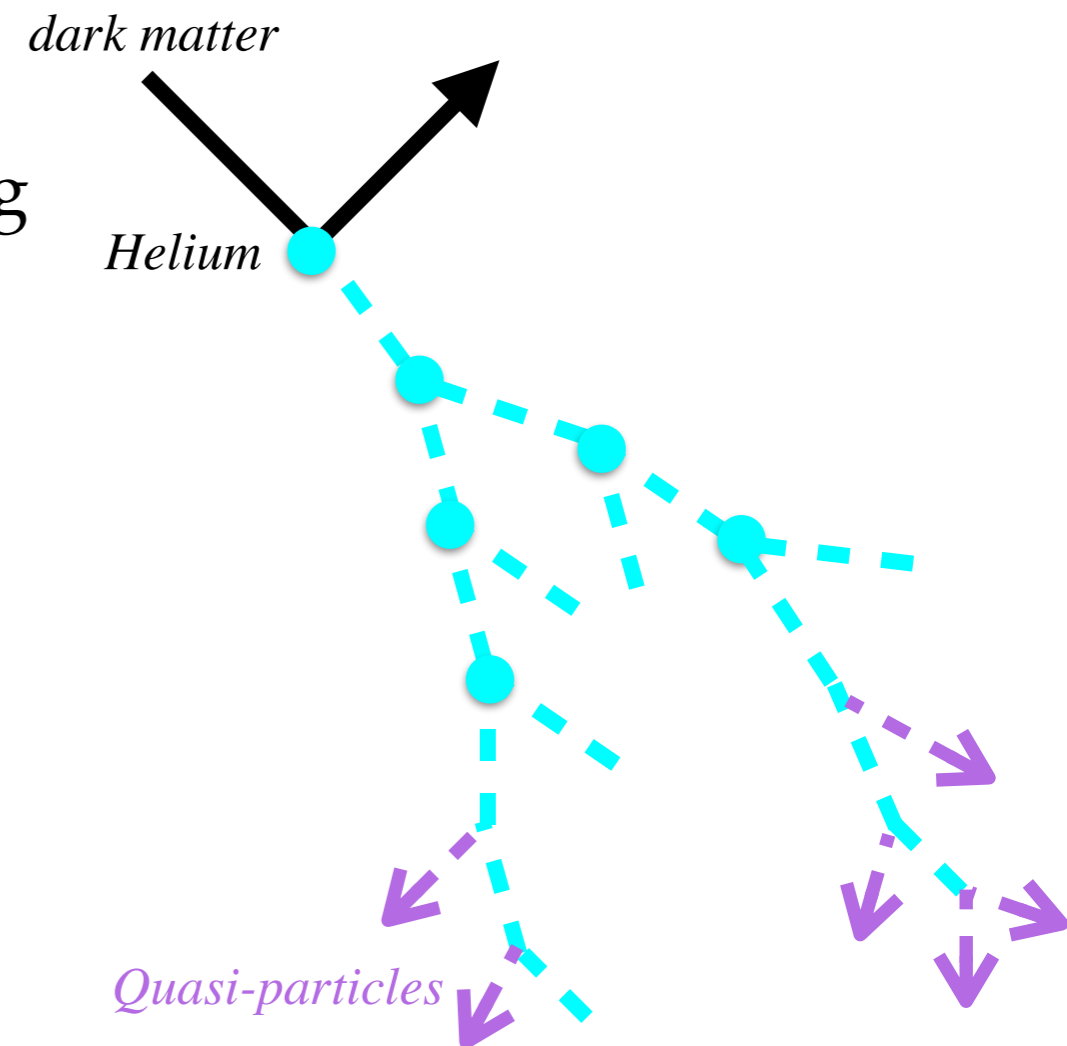
- Nano-mechanical Resonator Detector
dimension $(10 \sim 100) \mu m \times (10 \sim 100) \mu m$
force sensitivity $10^{-18} \text{ N} \sim 10^{-21} \text{ N}$

Reach Plots



Summary and future works

- MeV - GeV dark matter
theoretically and experimentally interesting
- effective field theory
quasi-particle interactions



Summary and future works

- MeV - GeV dark matter
theoretically and experimentally interesting
- effective field theory
quasi-particle interactions
- to do
 - simulations
 - experiment at UF

