

Constraining Decaying Dark Matter with the Effective Field Theory of Large-Scale Structures

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Based on [arXiv:2203.07440](https://arxiv.org/abs/2203.07440)

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Rencontres de Blois - 24/05/2022

The S_8 tension

A tension within the Λ CDM model

S_8 parameter

$$S_8 = \sigma_8 \sqrt{\Omega_m / 0.3}$$

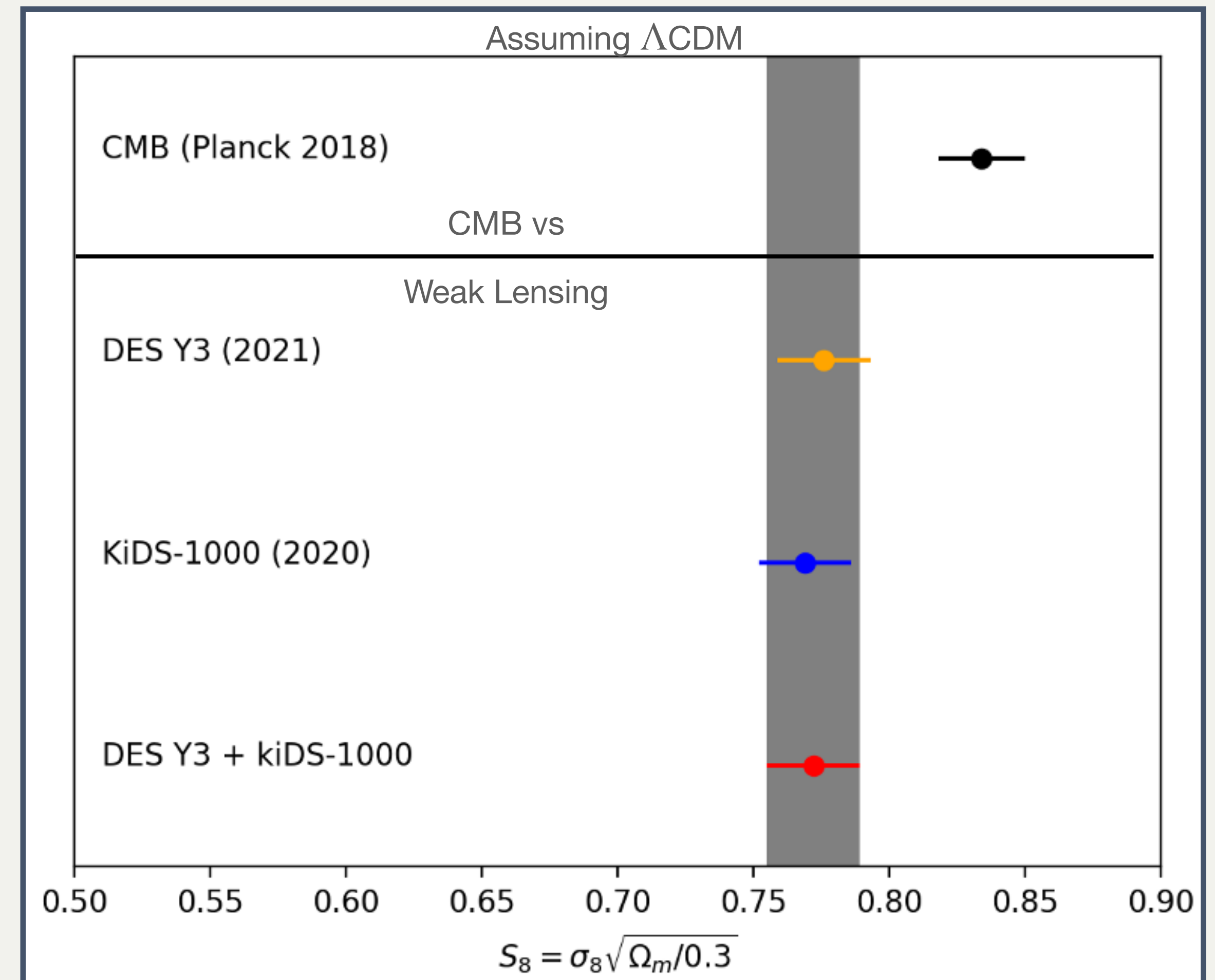
where:

$$\sigma_8^2 = \int \frac{k^3}{2\pi^2} P_m(k) W_8^2(k) d \ln(k)$$

→ $P_m(k)$ is the matter power spectrum

→ W_R is a « Window function »:

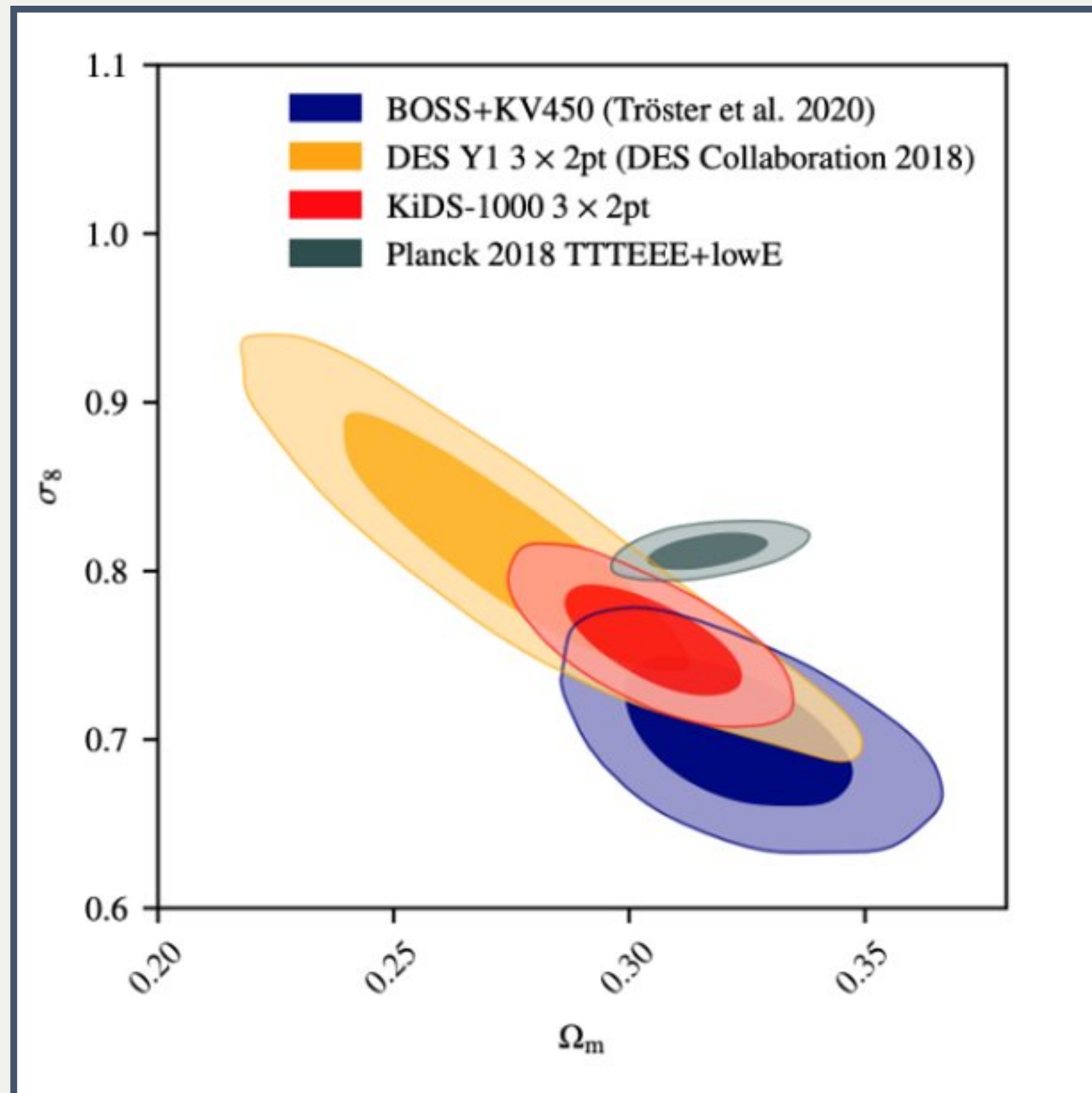
$$W_R = \frac{1}{4/3\pi R^3} \text{ for } r \leq R$$
$$W_R = 0 \text{ for } r > R$$



The σ_8 tension and the matter power spectrum

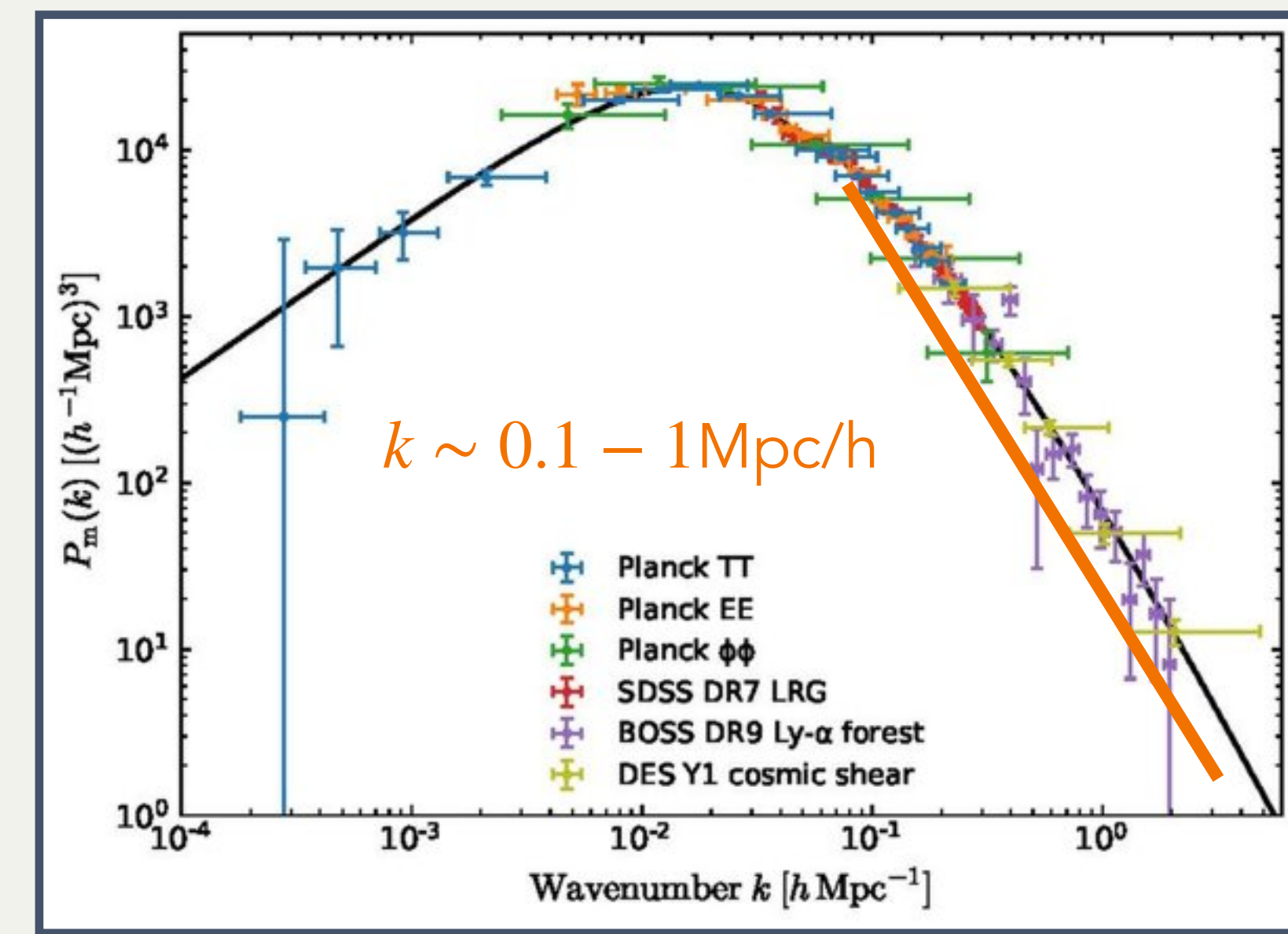
A tension within the Λ CDM model

Combining Galaxy Weak Lensing and clustering: the 3x2 statistics



σ_8 tension

$$\sigma_8 = \sqrt{\int \frac{k^3}{2\pi^2} P_m(k) W_8^2(k) d \ln(k)}$$



How to decrease power? Warm Dark Matter (excluded by Lyman alpha), Interacting Dark Matter... and decaying dark matter!

The effective field theory of large-scale structures (EFTofLSS)

Motivations

To constrain a model (through an MCMC), I focus on two main observables:

1. **CMB** → CMB power spectra: C_l^{TT} , C_l^{EE} , C_l^{TE} , etc.
2. **LSS** → the galaxy power spectrum: $P_g(z, k, \mu)$

In the **linear perturbation theory**, there is two popular ways to use LSS data :

1. Extract information with the full galaxy power spectrum

$$P_g(z, k, \mu) \simeq [b_1(z) + f\mu^2]^2 P_m(z, k)$$

Lack of precision

Kaiser 1987

b_1 : bias parameter, f : growth factor and $\mu = \hat{z} \cdot \hat{k}$

2. Redshift Space Distortion (RSD) information : $f\sigma_8$.

Lack of information

The effective field theory of large-scale structures (EFTofLSS)

Motivations

The galaxy power spectrum in the framework of the EFTofLSS:

$$P_g(k, \mu) \simeq [b_1 + f\mu^2]^2 P_m(k) = Z_1(\mu)^2 P_m(k)$$



$$\begin{aligned} P_g(k, \mu) = & Z_1(\mu)^2 P_{11}(k) + 2Z_1(\mu) P_{11}(k) \left(c_{\text{ct}} \frac{k^2}{k_M^2} + c_{r,1} \mu^2 \frac{k^2}{k_M^2} + c_{r,2} \mu^4 \frac{k^2}{k_M^2} \right) \\ & + 2 \int \frac{d^3q}{(2\pi)^3} Z_2(\mathbf{q}, \mathbf{k} - \mathbf{q}, \mu) P_{11}(|\mathbf{k} - \mathbf{q}|) P_{11}(q) + 6Z_1(\mu) P_{11}(k) \int \frac{d^3q}{(2\pi)^3} Z_3(\mathbf{q}, -\mathbf{q}, \mathbf{k}, \mu) P_{11}(q) \\ & + \frac{1}{\bar{n}_g} \left(c_{\epsilon,0} + c_{\epsilon,1} \frac{k^2}{k_M^2} + c_{\epsilon,2} f \mu^2 \frac{k^2}{k_M^2} \right), \end{aligned}$$

Perko et al. (2016)

$P_g(k, \mu)$ can be determined directly from $P_{11}(k) = P_m(k)$

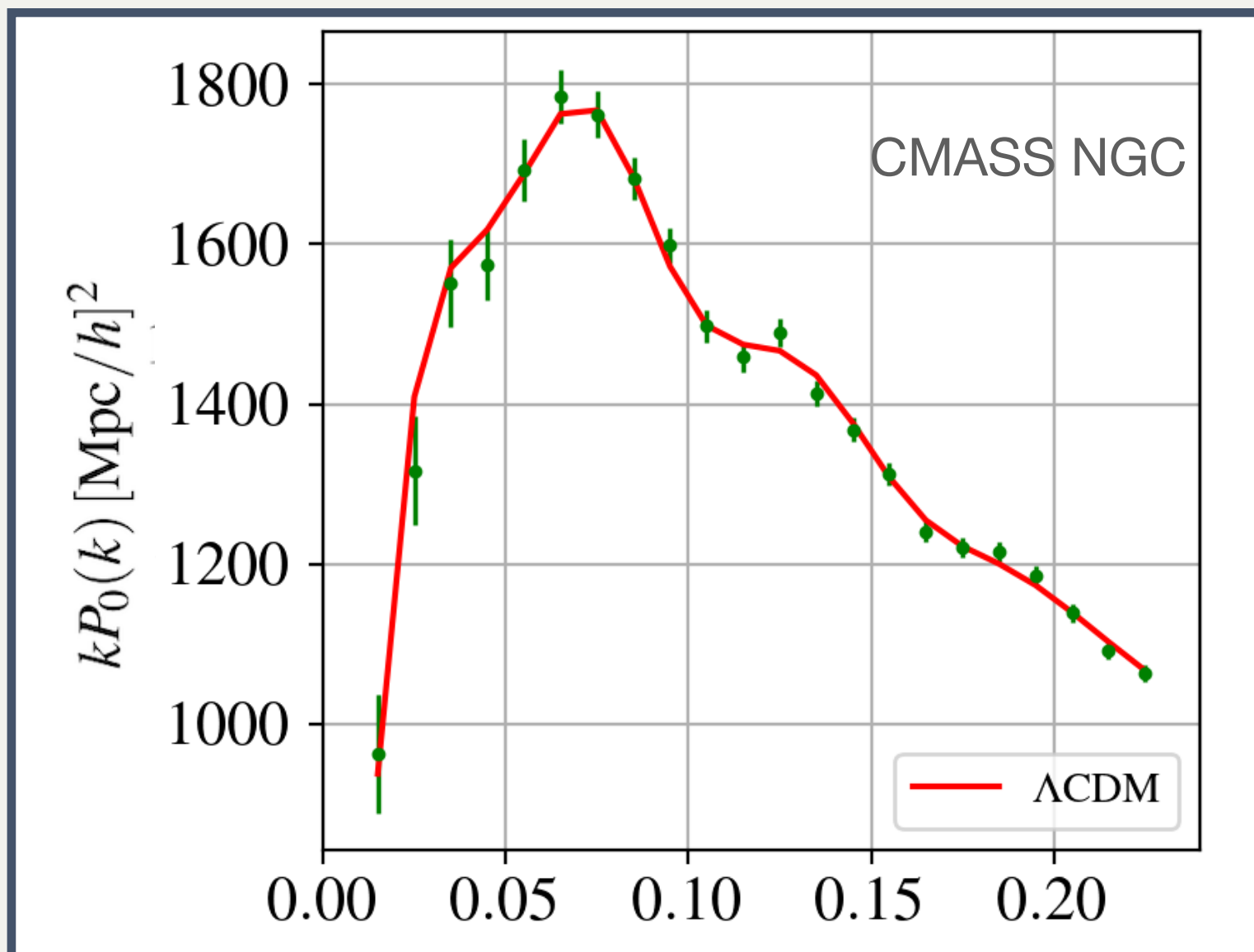
The effective field theory of large-scale structures (EFTofLSS)

BOSS data

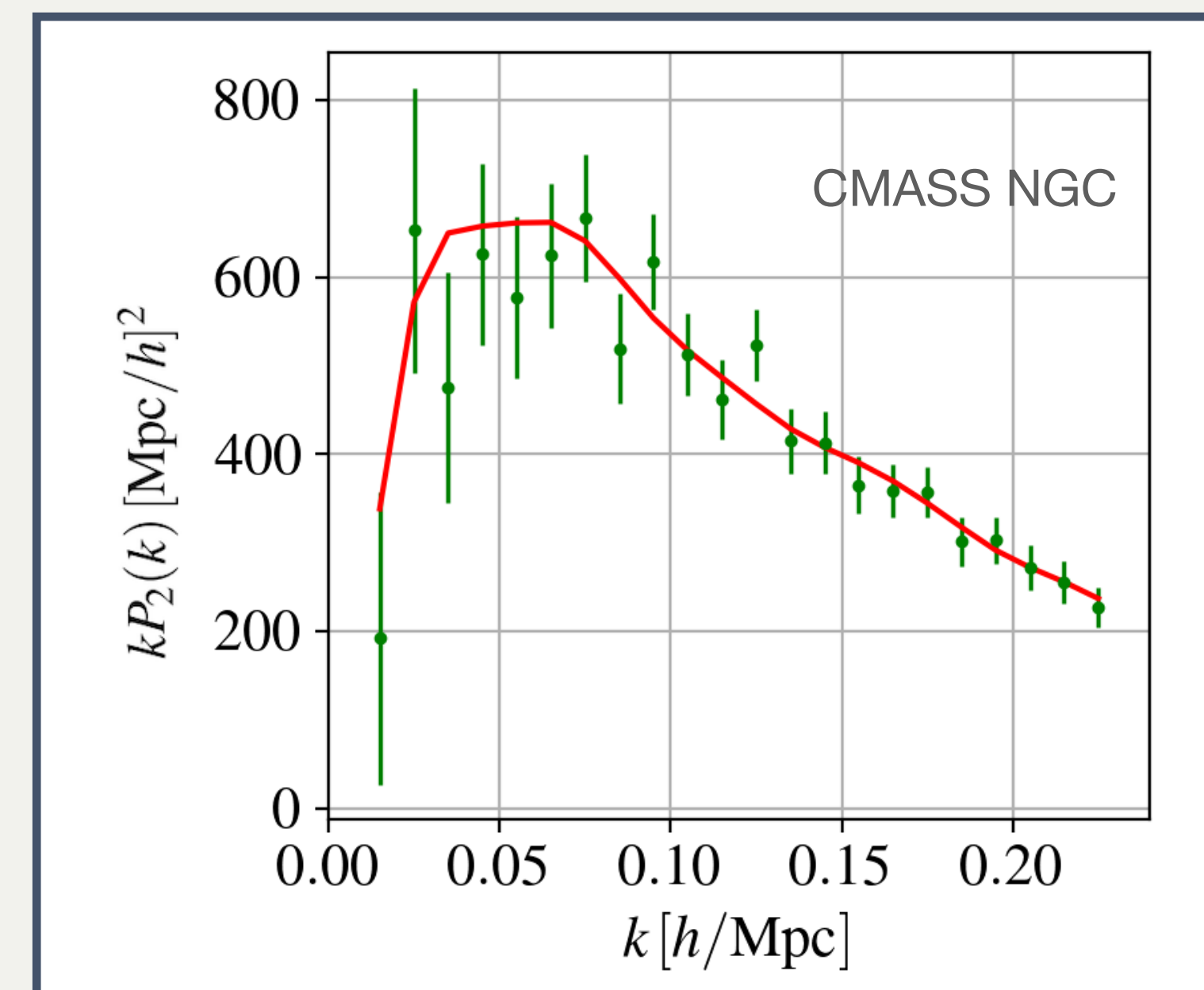
Multipoles of the galaxy power spectrum, obtained through a **Legendre** polynomials (\mathcal{L}_ℓ) decomposition:

$$P_g(z, k, \mu) = \sum_{\ell \text{ even}} \mathcal{L}_\ell(\mu) P_\ell(z, k)$$

→ two main contributions to $P_g(z, k, \mu)$ are the **monopole** ($\ell = 0$) and the **quadrupole** ($\ell = 2$).



Made with PyBird: github.com/pierrexyz/pybird



[arXiv:2203.07440](https://arxiv.org/abs/2203.07440), [arXiv:2110.07539](https://arxiv.org/abs/2110.07539)

We use 3 sky-cuts from BOSSDR12 at $z = 0.3$ and 0.6 .

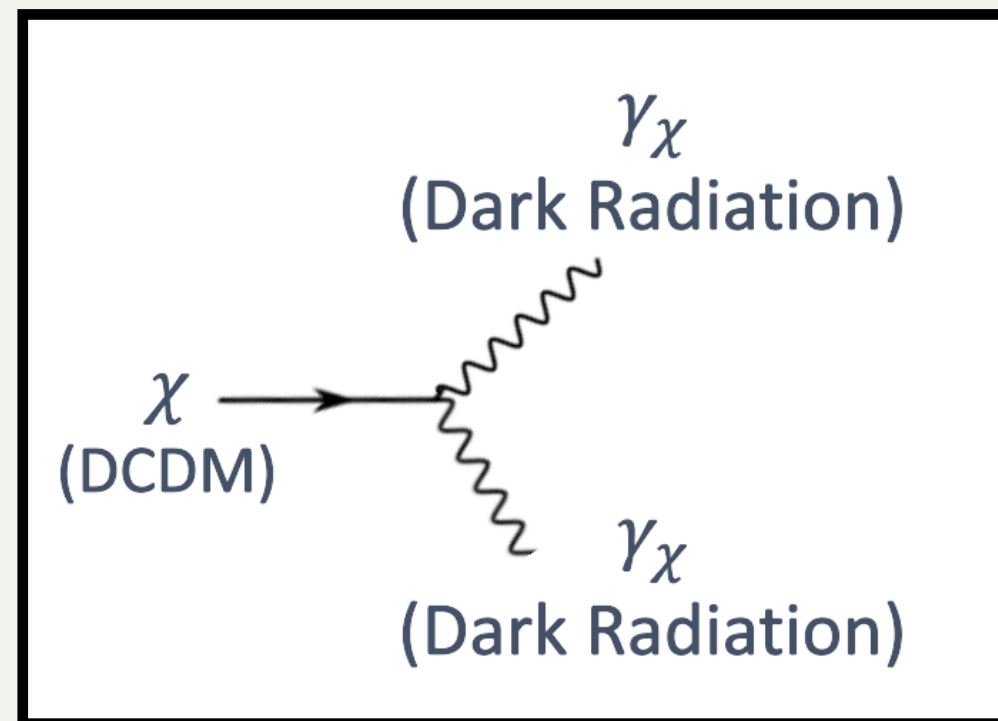
The Λ CDM \rightarrow DR model

Presentation of the model

The model

\rightarrow **Extension** to the Λ CDM model.

\rightarrow **Decay process** :

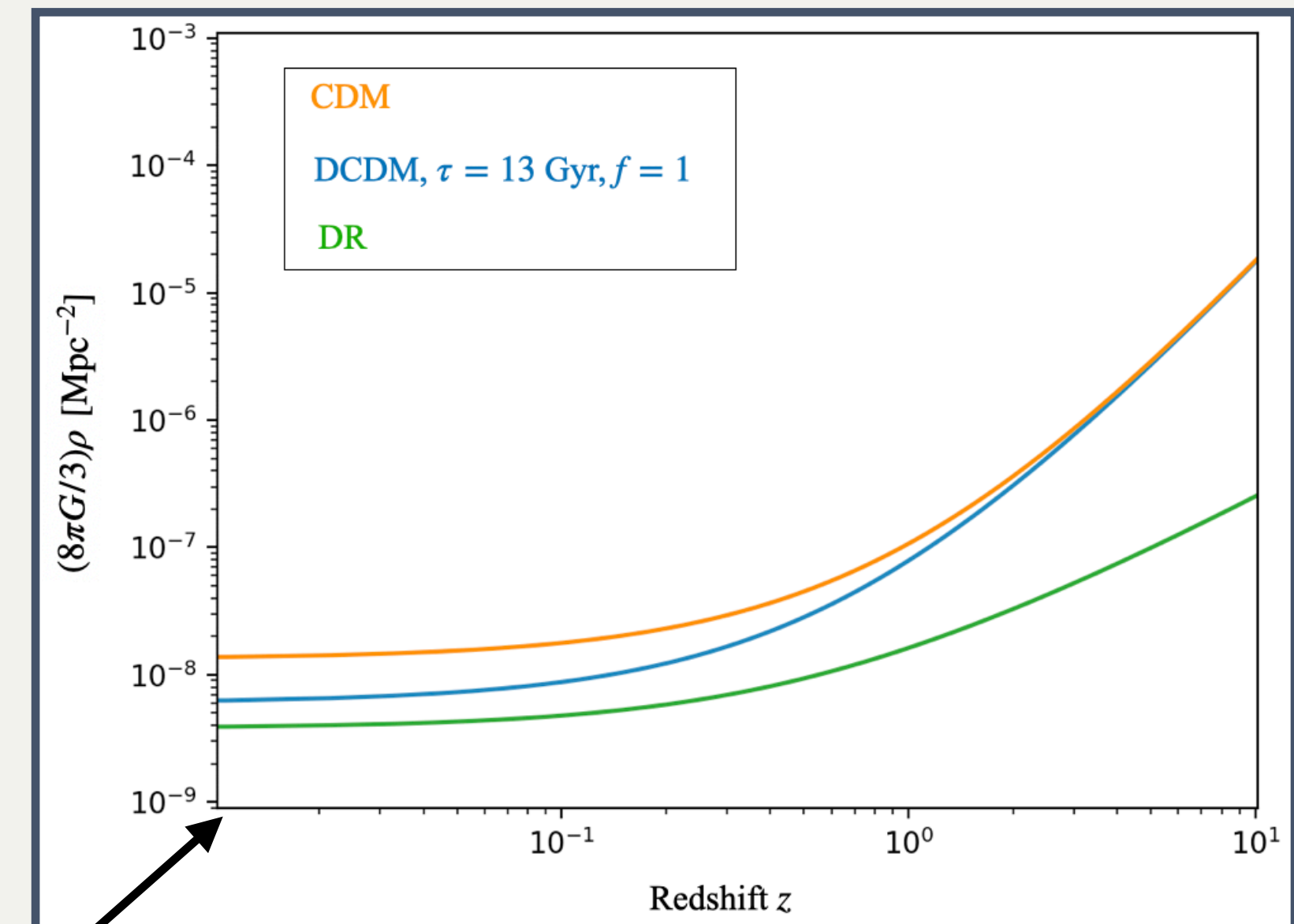


\rightarrow Λ CDM \sim Λ CDM + 2 parameters:

1. $\tau = \Gamma^{-1}$: **half-life** of the dark matter mother particle (DCDM)
2. f : **fraction** of the total CDM called DCDM is converted into Dark Radiation

Evolution of the energy densities

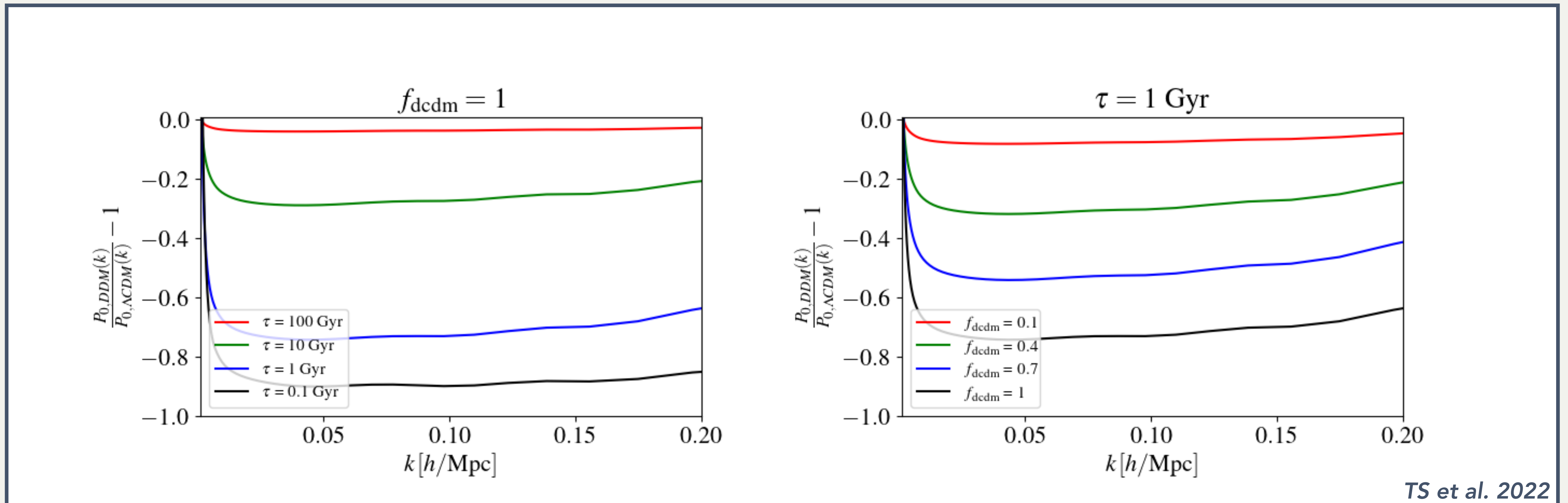
$$\begin{aligned}\dot{\bar{\rho}}_{\text{dcdm}} + 3\mathcal{H}\bar{\rho}_{\text{dcdm}} &= -a\Gamma\bar{\rho}_{\text{dcdm}} \\ \dot{\bar{\rho}}_{\text{dr}} + 4\mathcal{H}\bar{\rho}_{\text{dr}} &= a\Gamma\bar{\rho}_{\text{dcdm}}\end{aligned}$$



The Λ CDM \rightarrow DR model

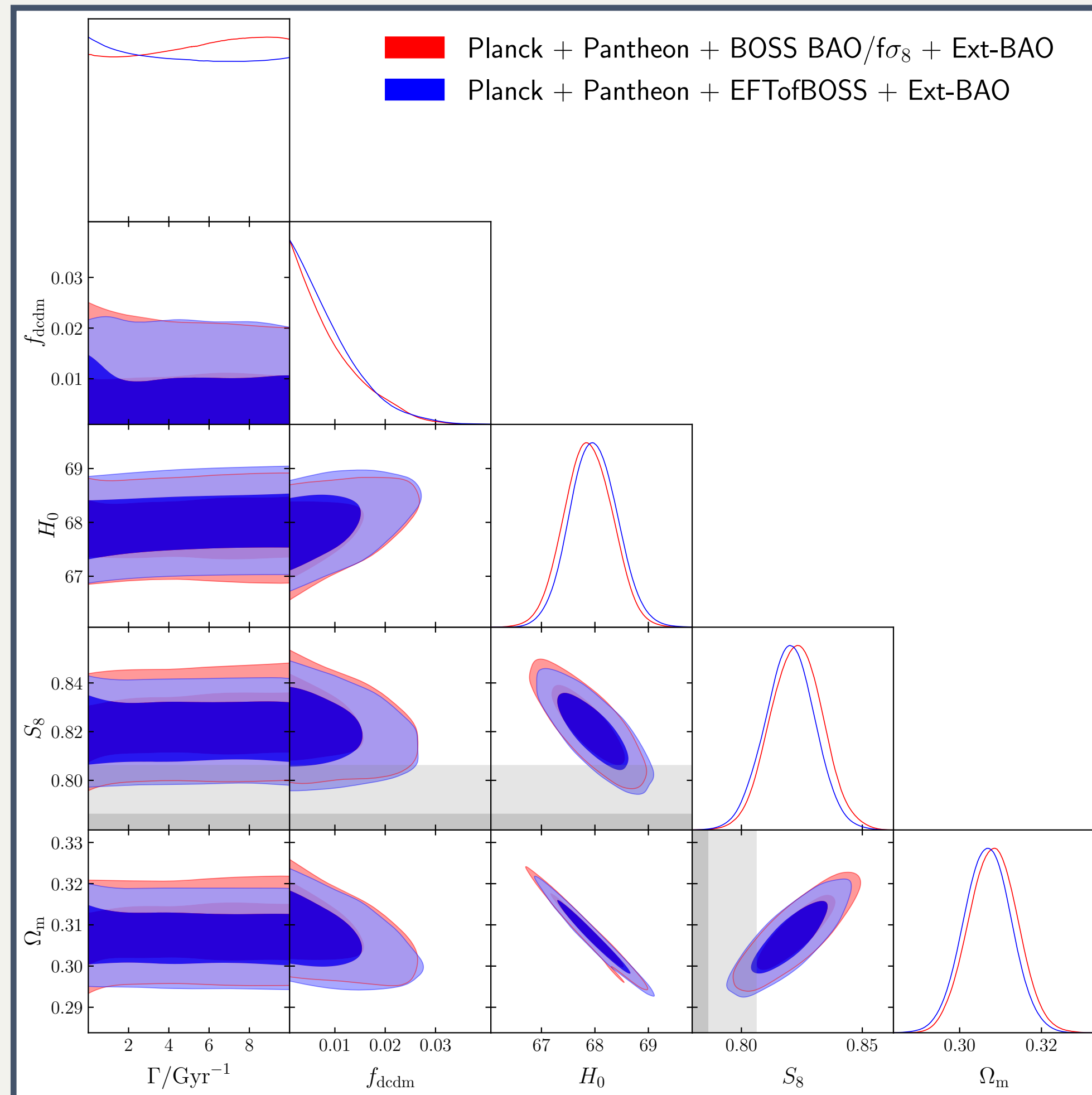
Results: galaxy power spectrum

- \rightarrow At level of perturbations in the synchronous gauge co-moving with Λ CDM: Λ CDM perturbations are unchanged! We consider homogeneous decays.
- \rightarrow The effect is dominated by the decrease of Ω_m at the **background** (effect of daughter radiation is minor).



The Λ CDM \rightarrow DR model

Results: constraints



3 main results

Planck+Pantheon+BAO/ $f\sigma_8$ or EFTofBOSS

1. We derive the most up-to-date constraints
 - $\tau > 250.0 \text{ Gyr}$ for $f = 1$
 - $f < 0.0216$ for $\tau < t_u$
2. EFTofLSS does not improve the constraints over BAO/ $f\sigma_8$
3. This model **does not resolve** the S_8 tension

TS et al. 2022, arXiv:2203.07440

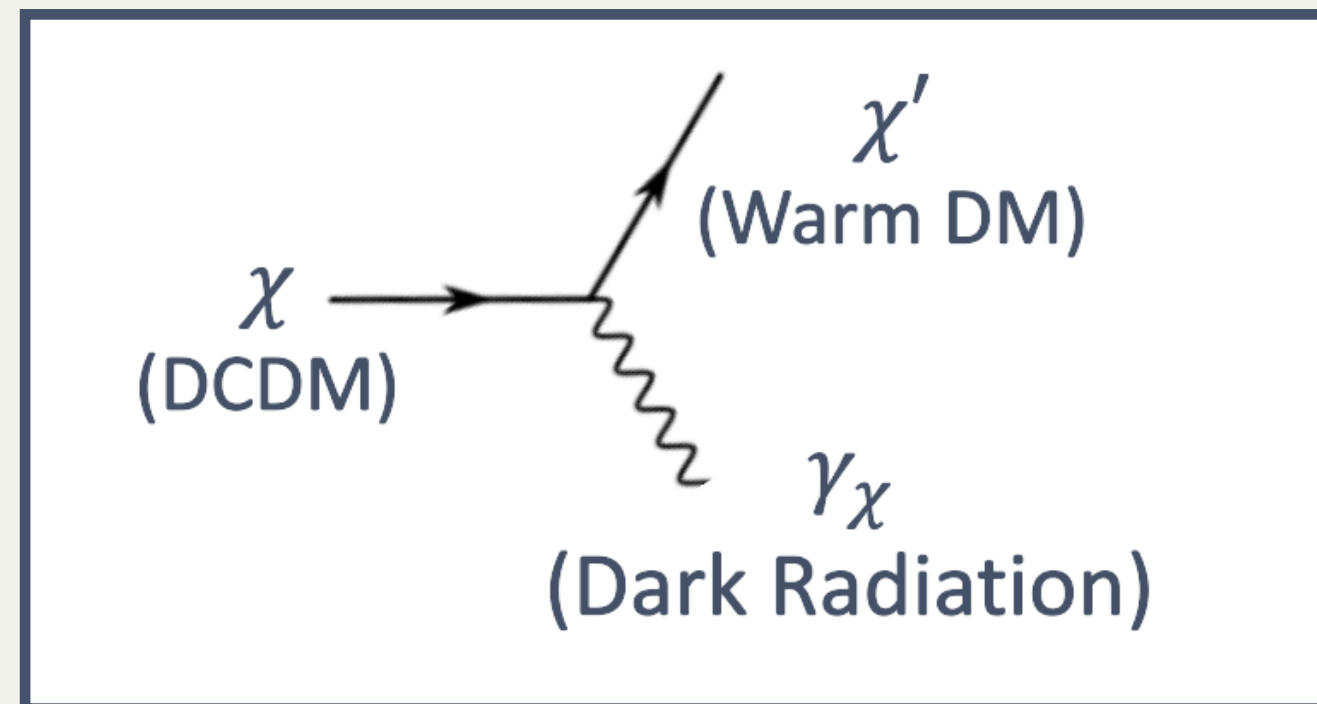
The DCDM \rightarrow WDM+DR model

Presentation of the model

The model

\rightarrow **Extension** to the Λ CDM model.

\rightarrow **Decay process** :



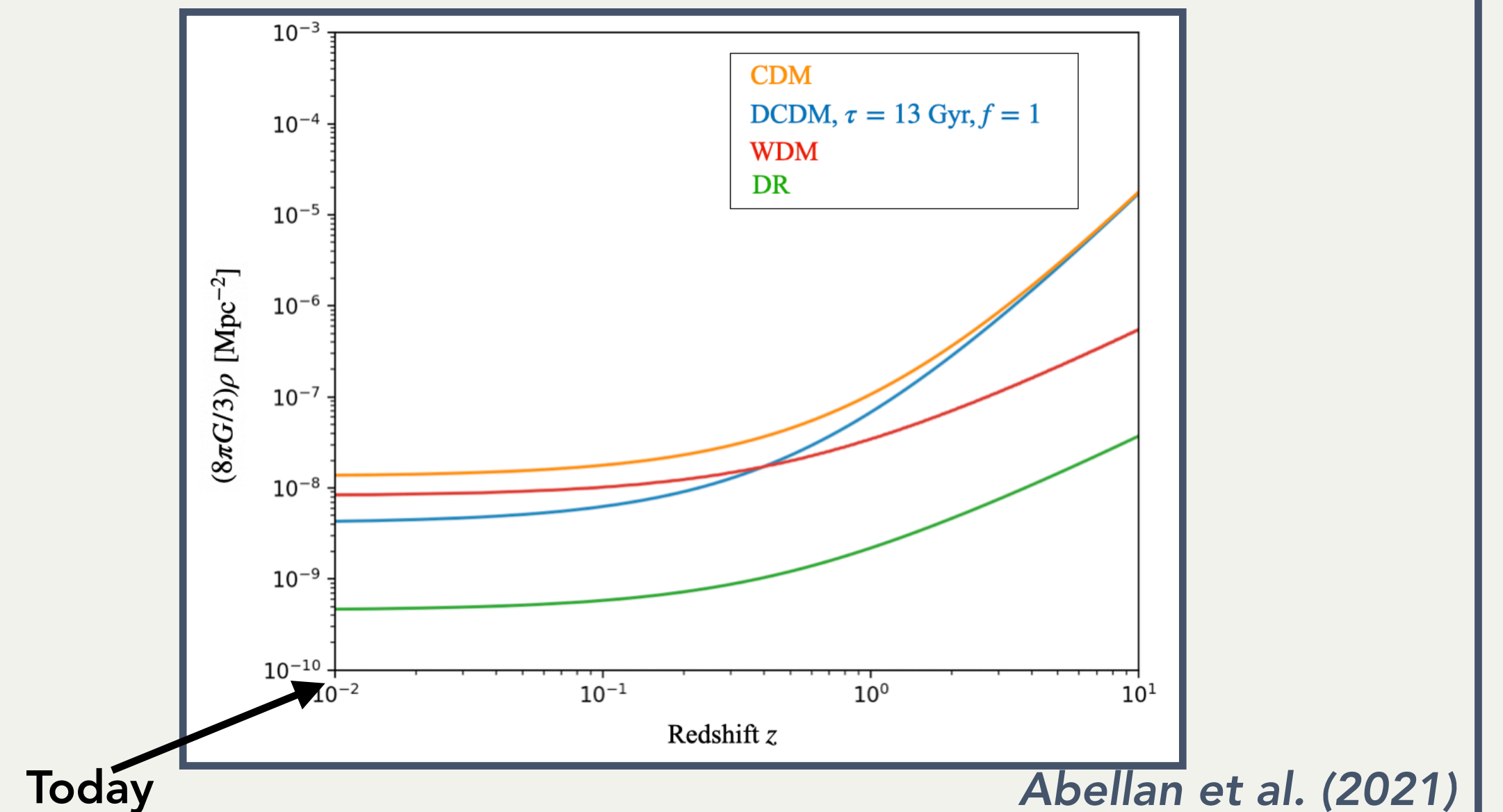
\rightarrow DCDM \sim Λ CDM + 2 parameters:

1. $\tau = \Gamma^{-1}$: **half-life** of the dark matter mother particle (DCDM)
2. ε : **fraction** of the rest mass energy of the DCDM converted into Dark Radiation

Evolution of the energy densities

$$\begin{aligned} \dot{\bar{\rho}}_{\text{dcdm}} + 3\mathcal{H}\bar{\rho}_{\text{dcdm}} &= -a\Gamma\bar{\rho}_{\text{dcdm}} \\ \dot{\bar{\rho}}_{\text{dr}} + 4\mathcal{H}\bar{\rho}_{\text{dr}} &= \varepsilon\Gamma a\bar{\rho}_{\text{dcdm}} \\ \dot{\bar{\rho}}_{\text{wdm}} + 3(1+w)\mathcal{H}\bar{\rho}_{\text{wdm}} &= (1-\varepsilon)a\Gamma\bar{\rho}_{\text{dcdm}} \end{aligned}$$

with $w = \bar{P}_{\text{wdm}}/\bar{\rho}_{\text{wdm}}$



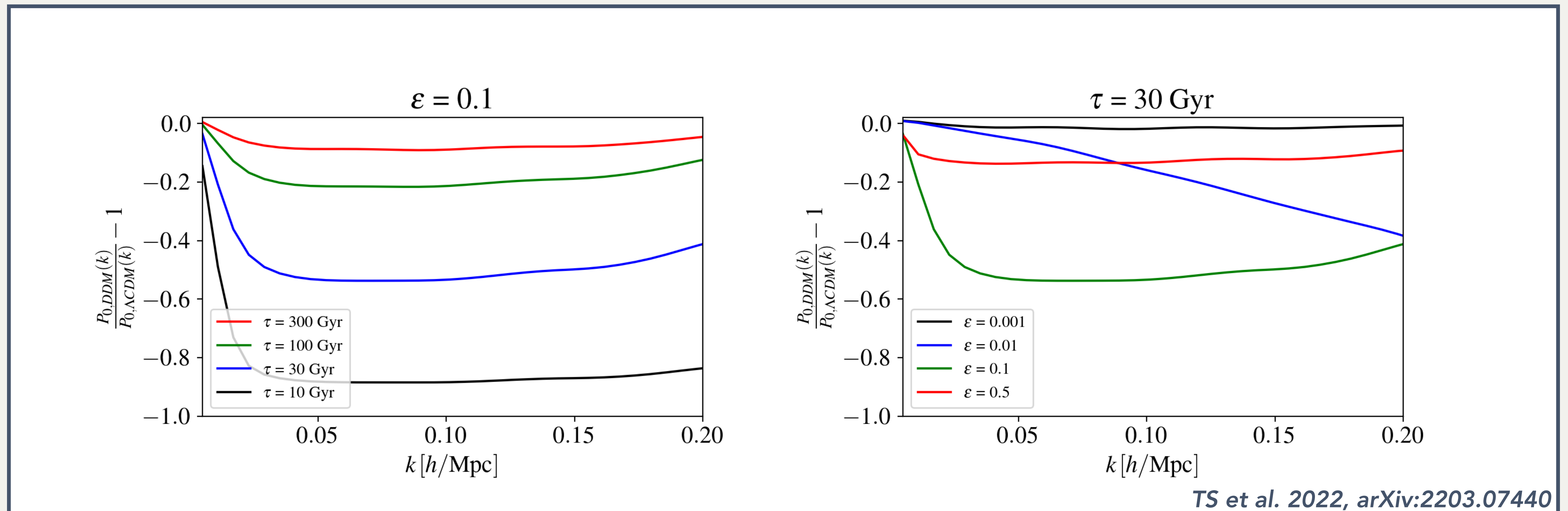
The Λ CDM \rightarrow WDM+DR model

Results: galaxy power spectrum

\rightarrow The effect **is not** dominated by a background effect

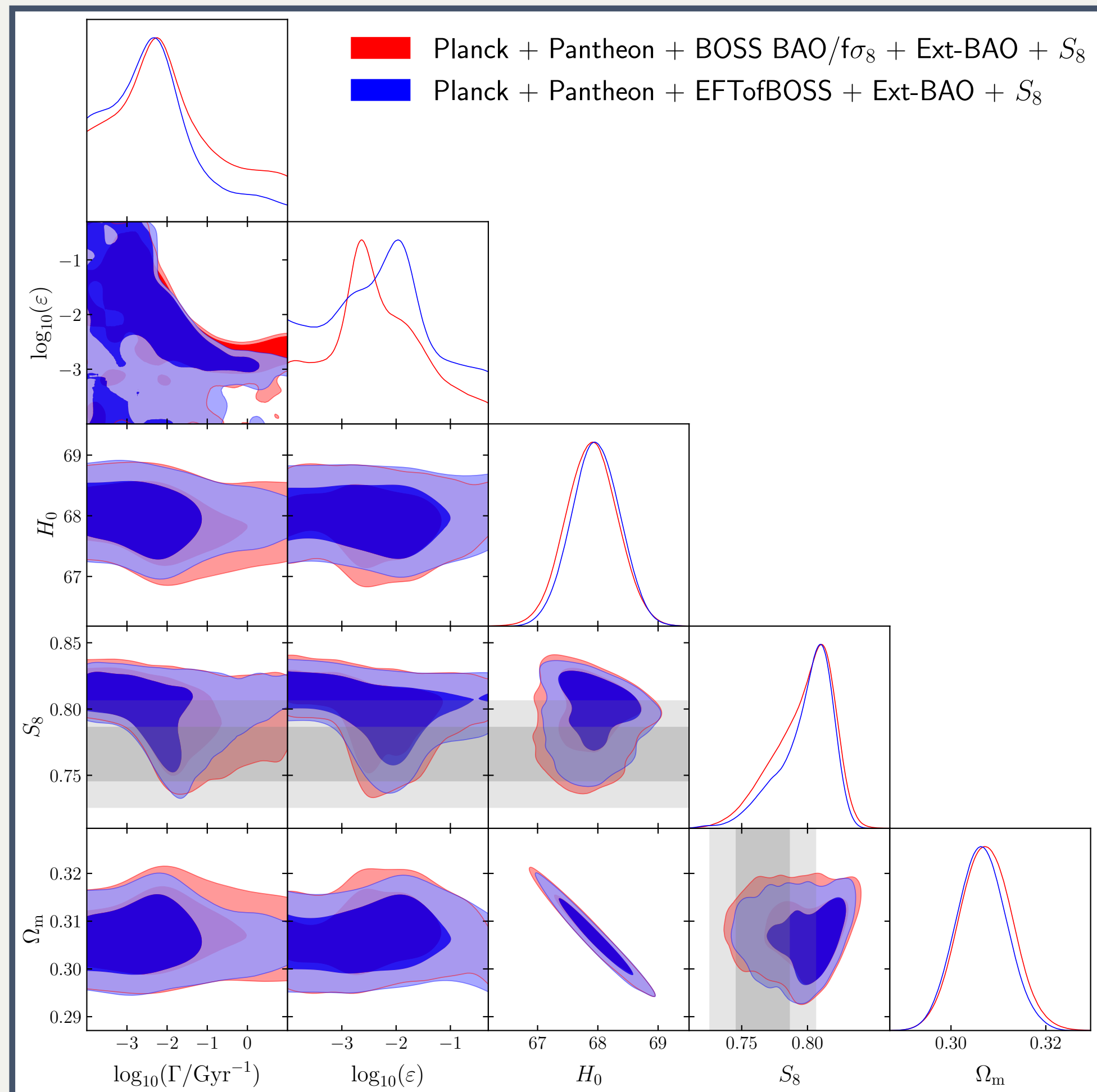
\rightarrow WDM perturbed continuity equation :

$$\dot{\delta}_{\text{wdm}} = -3\mathcal{H}(c_s^2 - \omega)\delta_{\text{wdm}} - (1 + \omega)\left(\theta_{\text{wdm}} + \frac{\dot{h}}{2}\right) + (1 - \epsilon)a\Gamma\frac{\bar{\rho}_{\text{dcdm}}}{\bar{\rho}_{\text{wdm}}}(\delta_{\text{dcdm}} - \delta_{\text{wdm}})$$



The Λ CDM \rightarrow WDM+DR model

Results: constraints



TS et al. 2022, arXiv:2203.07440

3 main results

Planck+Pantheon+BAO/ $f\sigma_8$ or EFTofBOSS

1. This model **could resolve** the S_8 tension!
2.8 σ for Λ CDM \rightarrow 1.5 σ for Λ CDM \rightarrow WDM+DR
2. The EFTofBOSS data **improve the constraints** on τ :
1.61 < $\log_{10}(\tau/\text{Gyr})$ < 3.71 with EFTofBOSS
1.31 < $\log_{10}(\tau/\text{Gyr})$ < 3.82 without EFTofBOSS
3. It changes the **bestfit**:

$$\tau = 43 \text{ Gyr} \rightarrow \tau = 120 \text{ Gyr}$$
$$\epsilon = 0.6 \% \rightarrow \epsilon = 1.2 \%$$

Conclusions and Perspectives

Main results

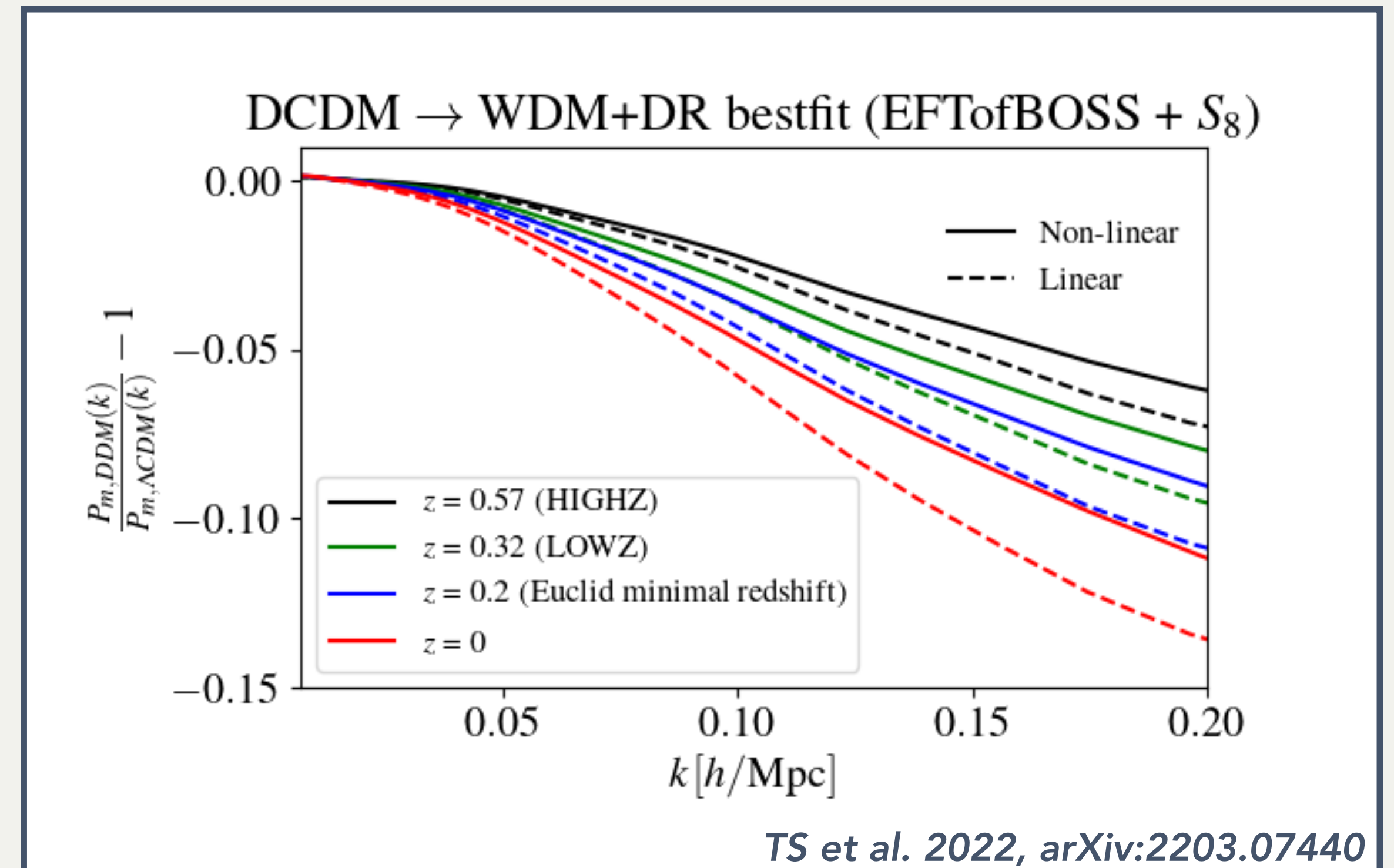
→ EFTofLSS can have **constraining power** on alternative models to Λ CDM.

→ We derive strong constraints on DCDM → DR model:

$$f < 0.0216$$
$$\tau > 250.0 \text{ Gyr}$$

→ The DCDM → WDM+DR model resolve the S_8 tension and could be probed further with next generation LSS surveys:

$$\tau = 120 \text{ Gyr} \ \& \ \varepsilon = 1.2 \%$$



Thanks for your attention

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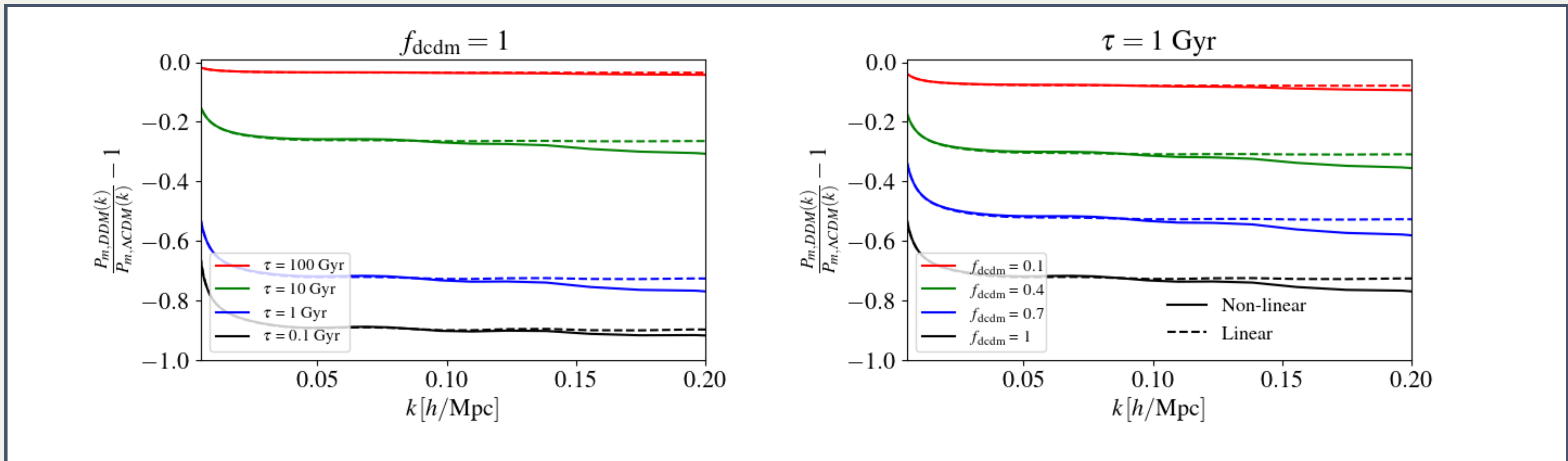
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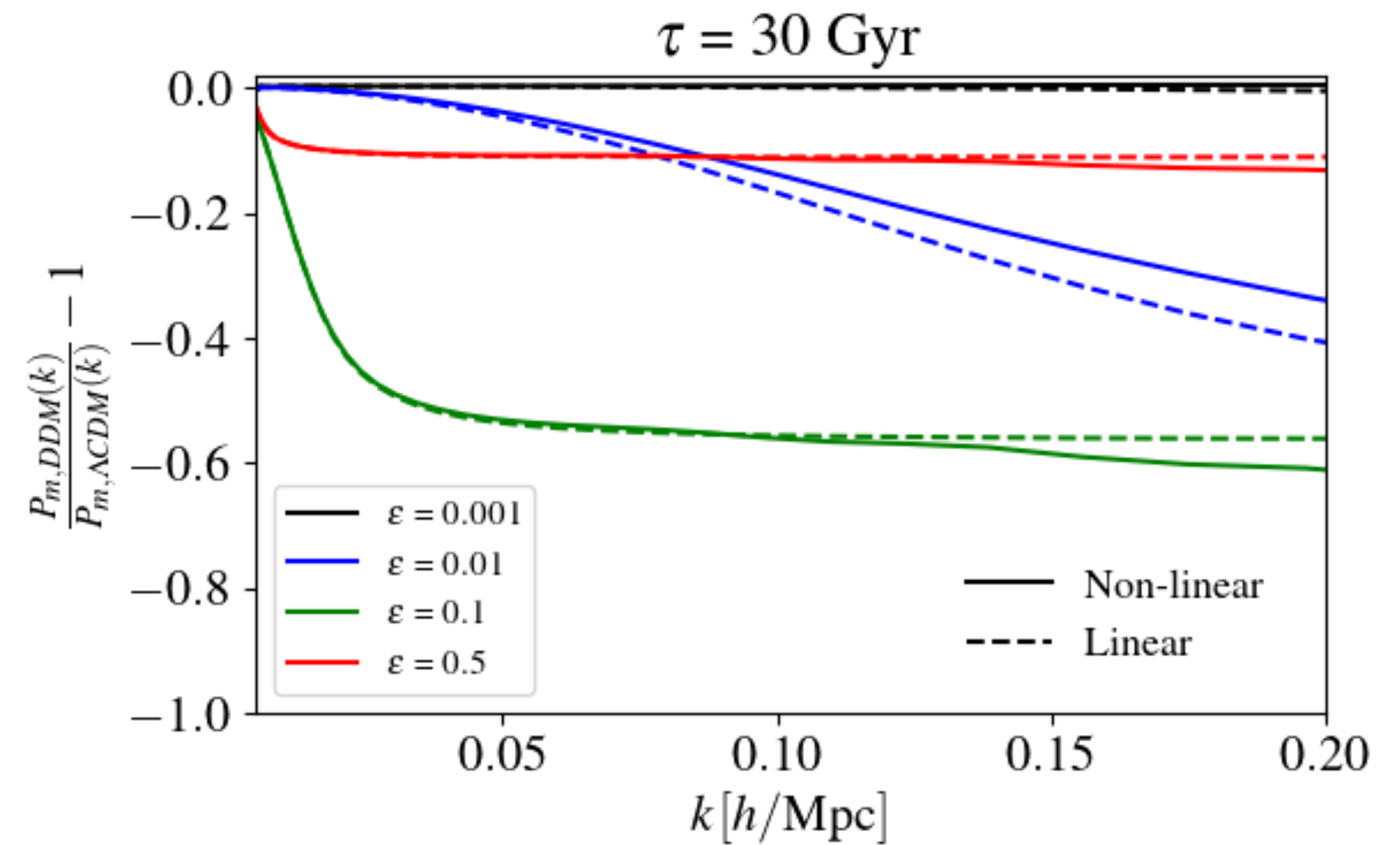
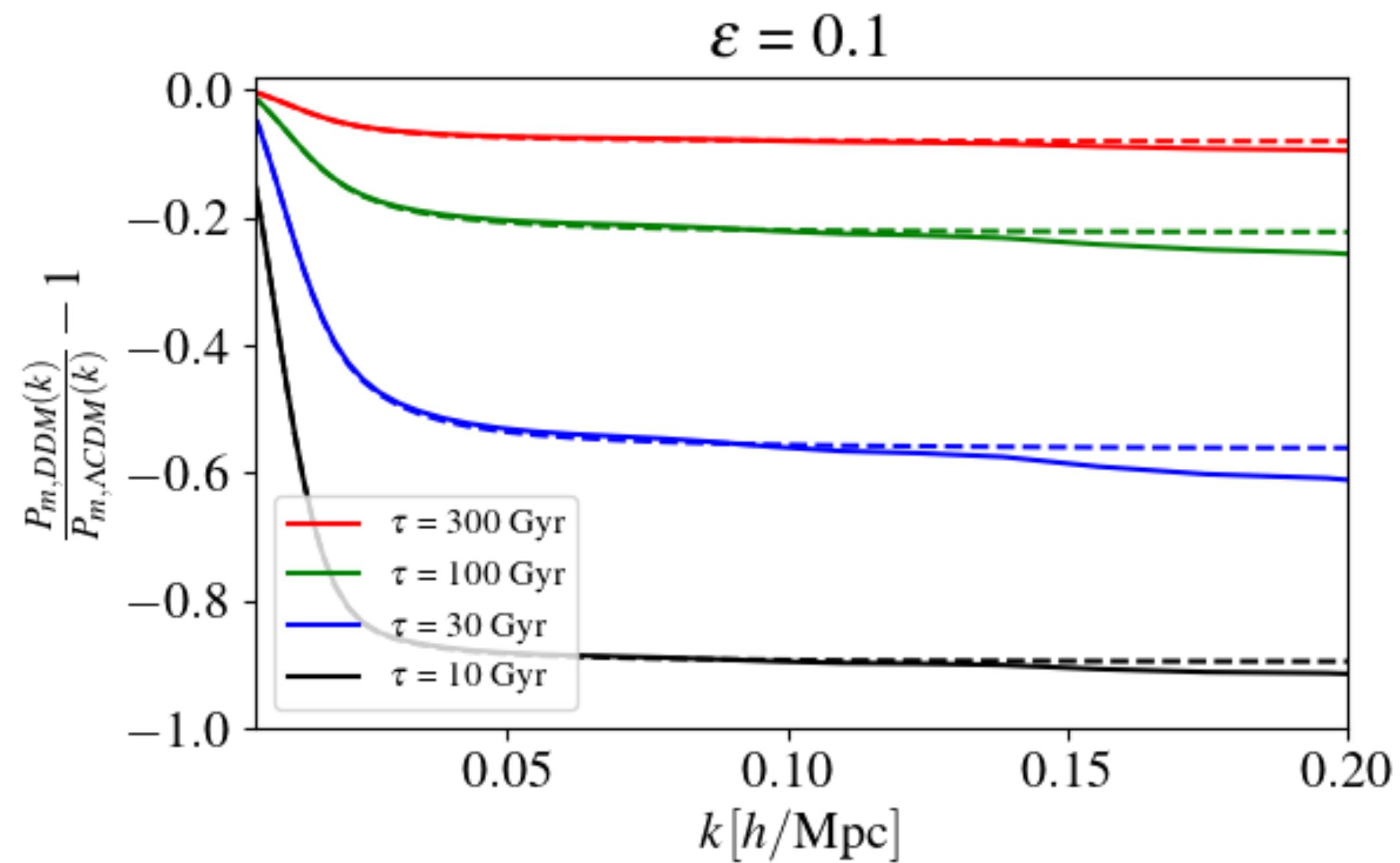
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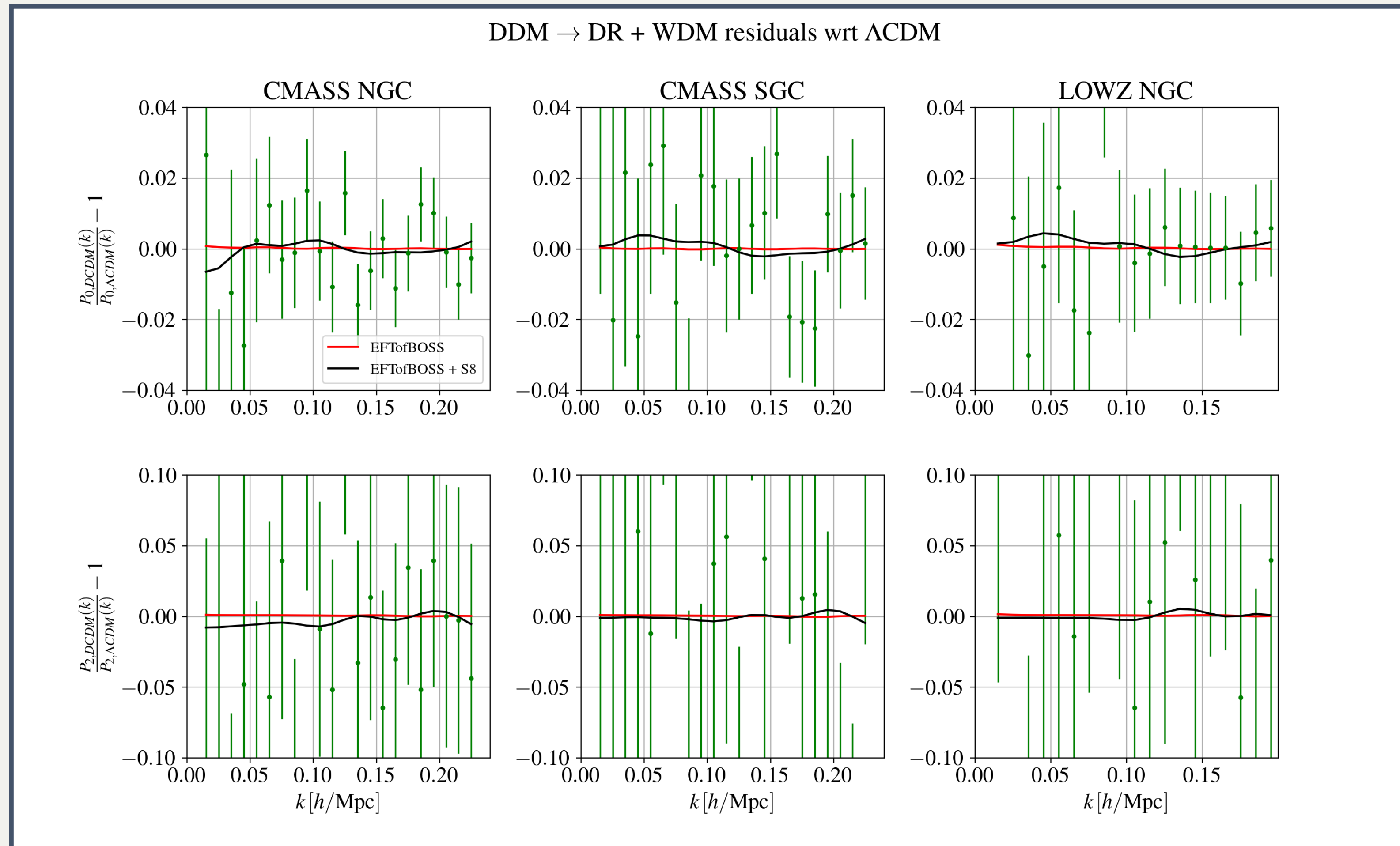
Backup I: Λ CDM \rightarrow DR matter power spectrum



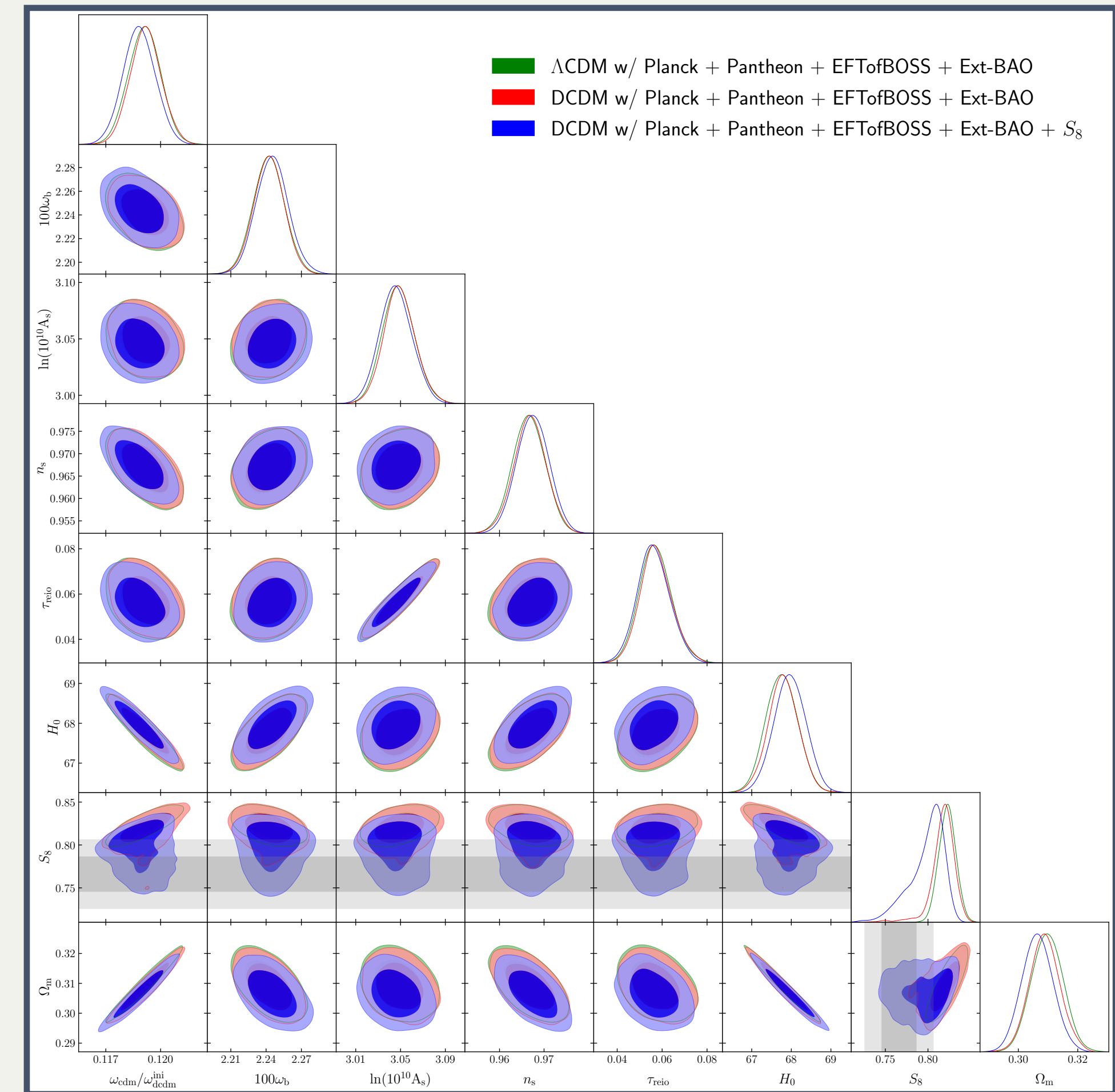
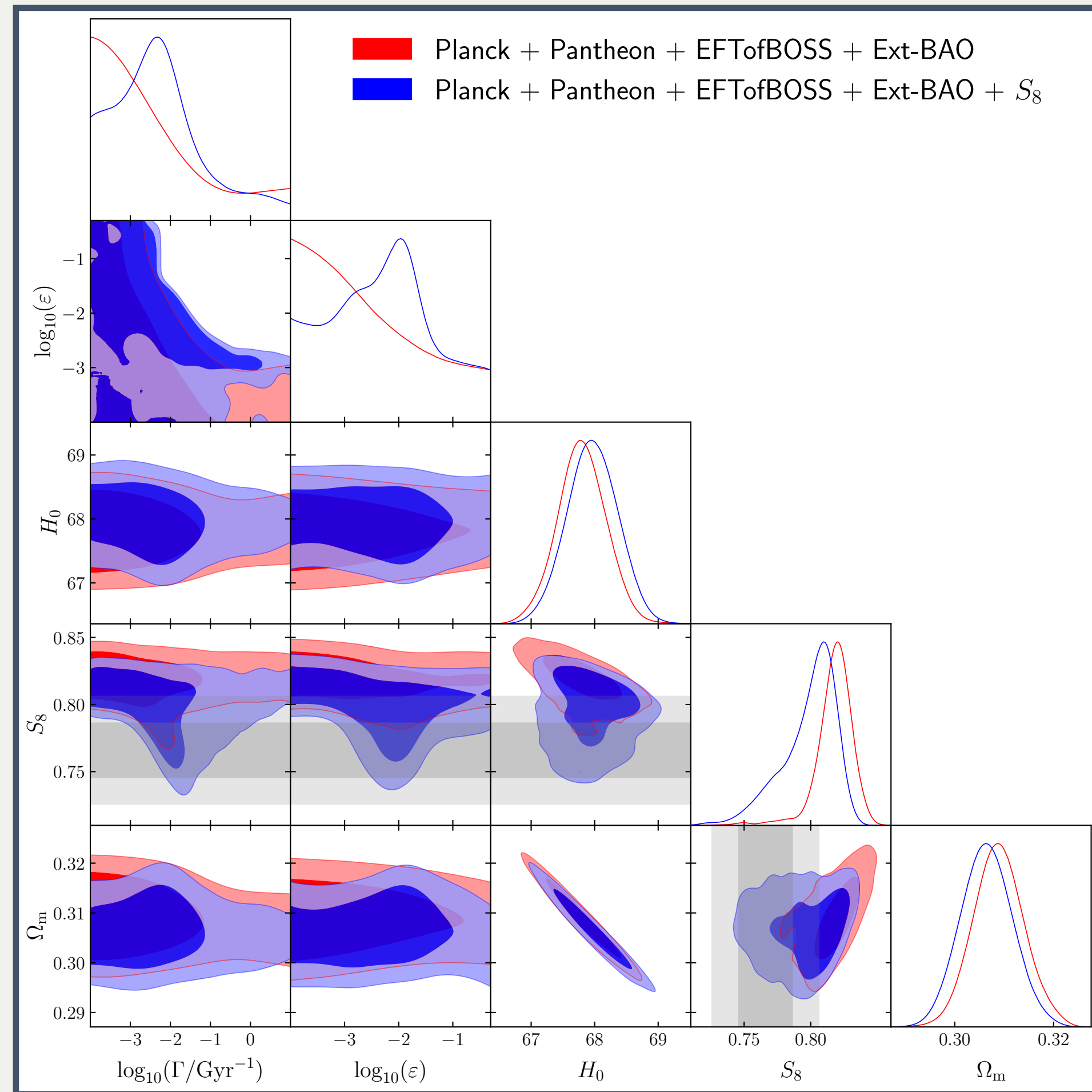
Backup II: DCDM \rightarrow WDM+DR matter power spectrum



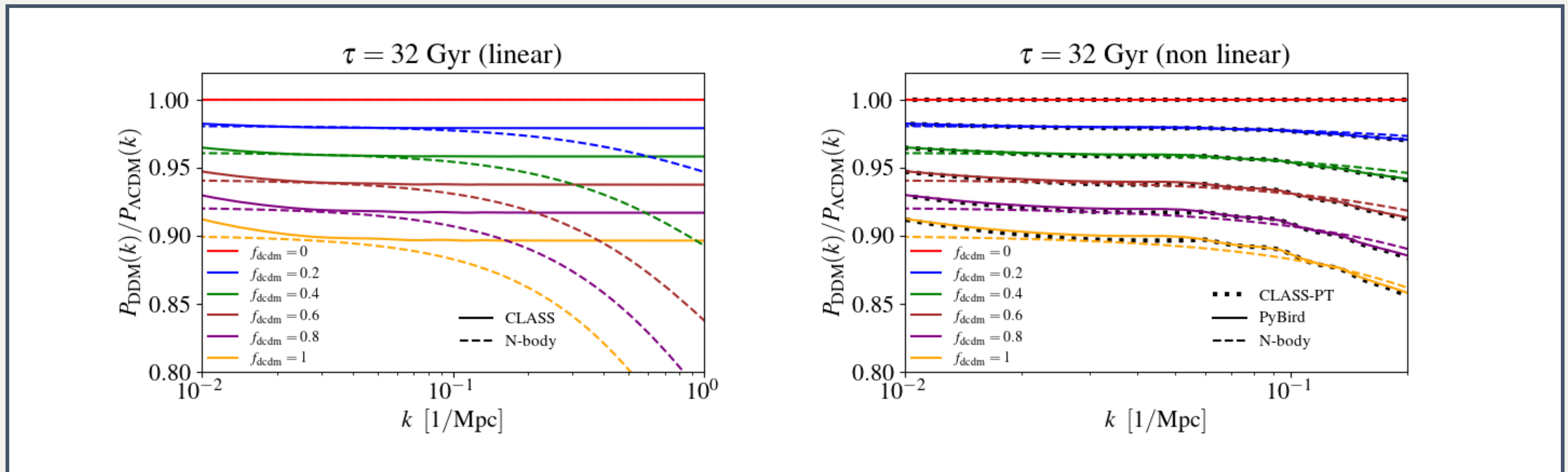
Backup III: Λ CDM \rightarrow WDM+DR bestfit power spectrum



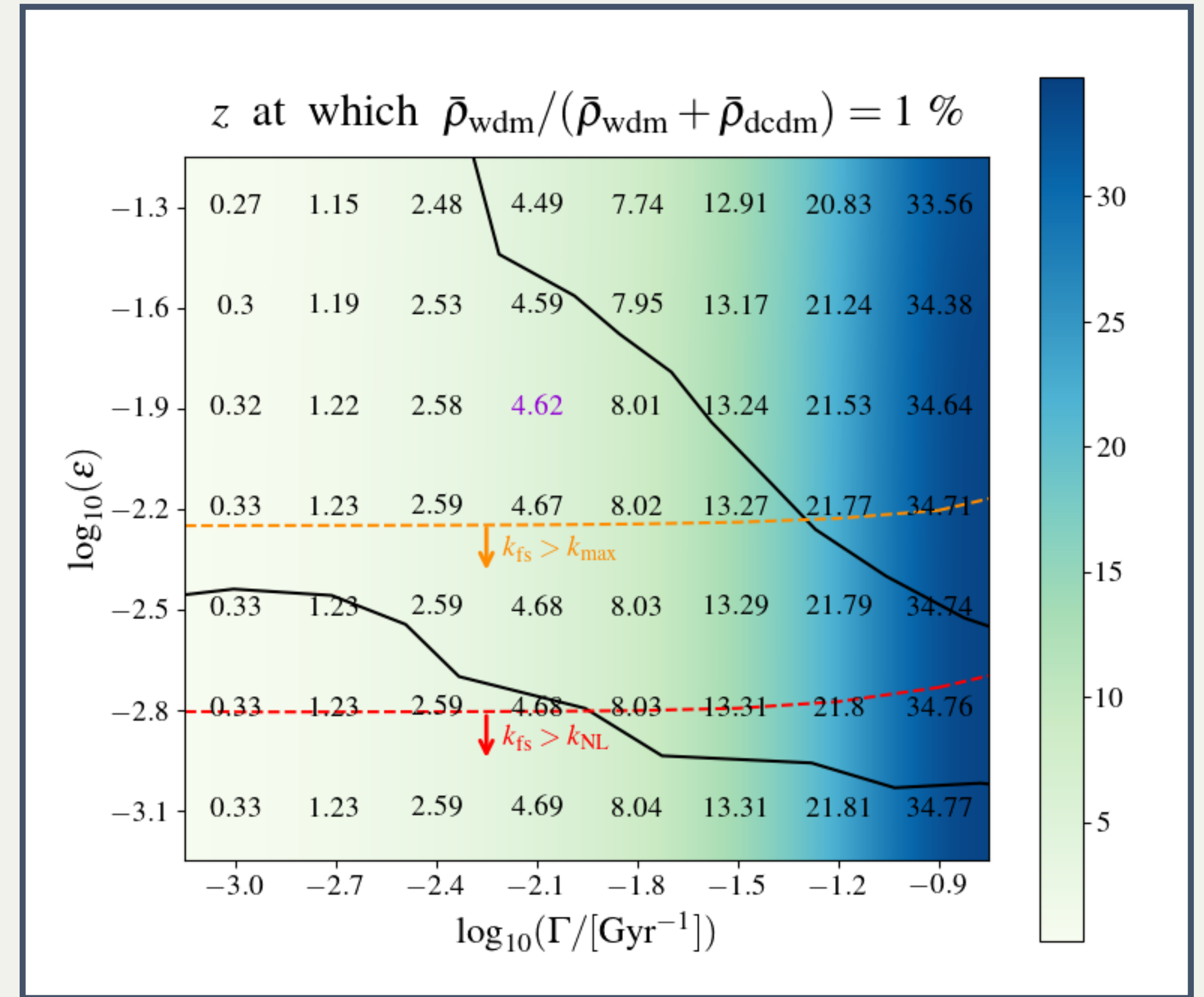
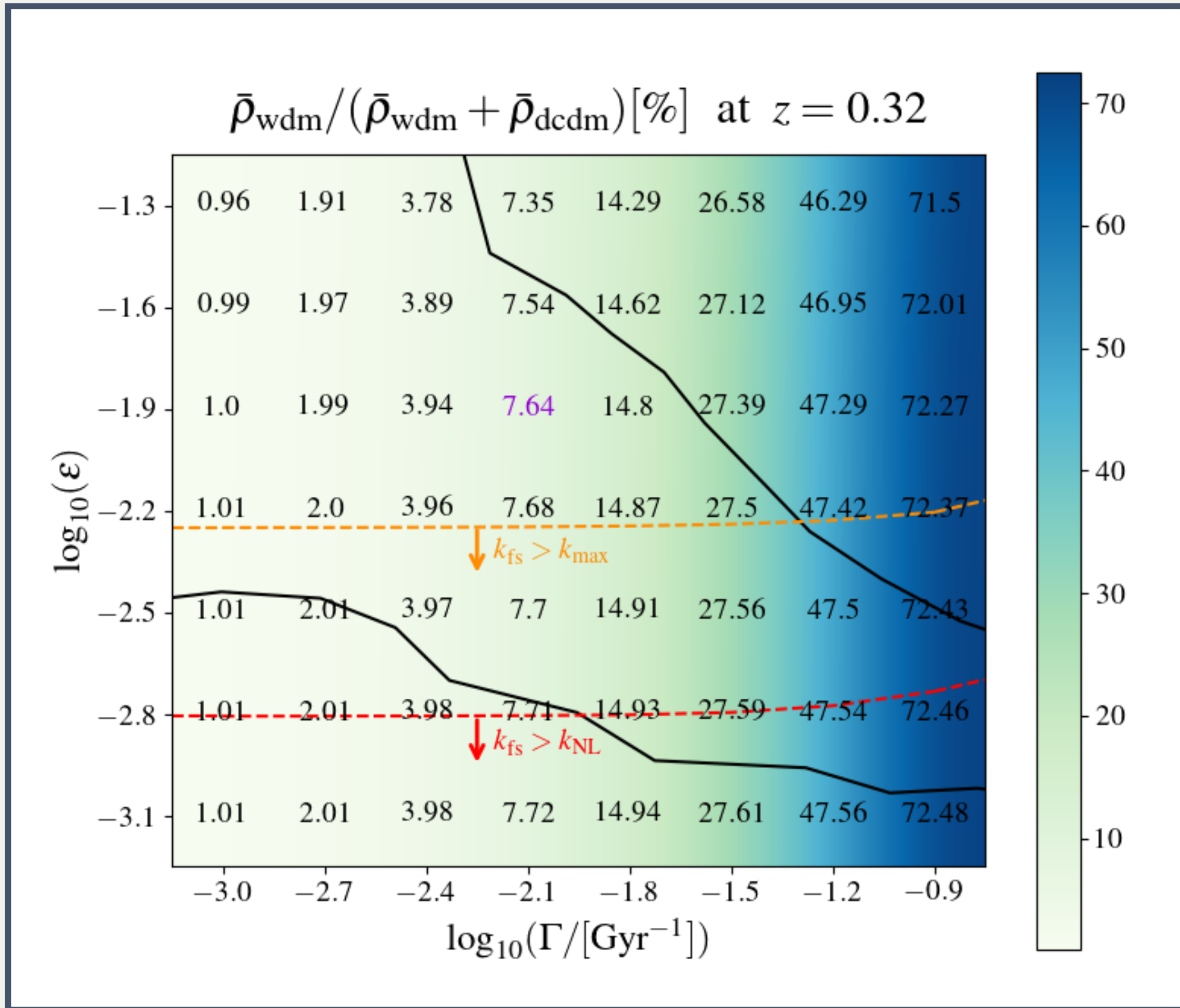
Backup IV: the Λ CDM \rightarrow WDM+DR model and the S_8 tension



Backup V: EFTofLSS vs N-body simulations (DCDM \rightarrow DR model)



Backup VI: validity of the EFTofLSS for the Λ CDM \rightarrow WDM+DR model



Backup VII: EFTofLSS parameters

$$\begin{aligned}
 P(k, \mu) &= Z_1(\mu)^2 P_{11}(k) \\
 &+ 2 \int \frac{d^3q}{(2\pi)^3} Z_2(\mathbf{q}, \mathbf{k} - \mathbf{q}, \mu)^2 P_{11}(|\mathbf{k} - \mathbf{q}|) P_{11}(q) + 6Z_1(\mu) P_{11}(k) \int \frac{d^3q}{(2\pi)^3} Z_3(\mathbf{q}, -\mathbf{q}, \mathbf{k}, \mu) P_{11}(q) \\
 &+ 2Z_1(\mu) P_{11}(k) \left(c_{ct} \frac{k^2}{k_M^2} + c_{r,1} \mu \frac{k^2}{k_M^2} + c_{r,2} \mu^2 \frac{k^2}{k_M^2} \right) + \frac{1}{\bar{n}_g} \left(c_{\epsilon,0} + c_{\epsilon,1} \frac{k^2}{k_M^2} + c_{\epsilon,2} f \mu^2 \frac{k^2}{k_M^2} \right), \quad (10)
 \end{aligned}$$


with


$$\begin{aligned}
 Z_1(\mathbf{q}_1) &= K_1(\mathbf{q}_1) + f\mu_1^2 G_1(\mathbf{q}_1) = b_1 + f\mu_1^2, \\
 Z_2(\mathbf{q}_1, \mathbf{q}_2, \mu) &= K_2(\mathbf{q}_1, \mathbf{q}_2) + f\mu_{12}^2 G_2(\mathbf{q}_1, \mathbf{q}_2) + \frac{1}{2} f\mu q \left(\frac{\mu_2}{q_2} G_1(\mathbf{q}_2) Z_1(\mathbf{q}_1) + \text{perm.} \right), \\
 Z_3(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3, \mu) &= K_3(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3) + f\mu_{123}^2 G_3(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3) \\
 &+ \frac{1}{3} f\mu q \left(\frac{\mu_3}{q_3} G_1(\mathbf{q}_3) Z_2(\mathbf{q}_1, \mathbf{q}_2, \mu_{123}) + \frac{\mu_{23}}{q_{23}} G_2(\mathbf{q}_2, \mathbf{q}_3) Z_1(\mathbf{q}_1) + \text{cyc.} \right),
 \end{aligned}$$

with

$$\begin{aligned}
 K_1 &= b_1, \\
 K_2(\mathbf{q}_1, \mathbf{q}_2) &= b_1 \frac{\mathbf{q}_1 \cdot \mathbf{q}_2}{q_1^2} + b_2 \left(F_2(\mathbf{q}_1, \mathbf{q}_2) - \frac{\mathbf{q}_1 \cdot \mathbf{q}_2}{q_1^2} \right) + b_4 + \text{perm.}, \\
 K_3(k, q) &= \frac{b_1}{504k^2q^3} \left(-38k^5q + 48k^3q^3 - 18kq^5 + 9(k^2 - q^2)^3 \log \left[\frac{k-q}{k+q} \right] \right) \\
 &+ \frac{b_3}{756k^3q^5} \left(2kq(k^2 + q^2)(3k^4 - 14k^2q^2 + 3q^4) + 3(k^2 - q^2)^4 \log \left[\frac{k-q}{k+q} \right] \right)
 \end{aligned}$$

10 parameters

 **4 parameters** b_i ($i = 1, 2, 3, 4$) to describe the **galaxy bias** which arises from the one-loop contributions.

 **3 parameters** corresponding to **counterterms** (c_{ct} linear combination of a higher derivative bias and the dark matter sound speed, while $c_{r,1}$ and $c_{r,2}$ are the redshift-space counterterms).

 **3 parameters** which describe **stochastic** terms.