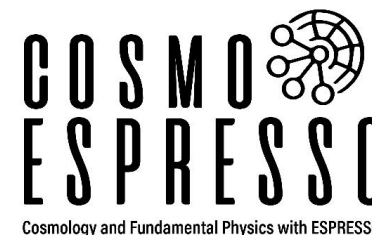
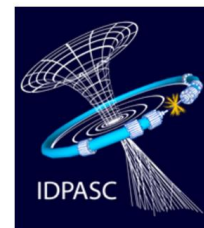


Generalizing models with variations of the fine-structure constant driven by scalar fields: extended Bekenstein model coupled to the dark sector

João Freitas Dias

PhD Supervisor: C. J. A. P. Martins



Motivation

Beyond Λ CDM



Scalar fields

Alternative description of DE

Consistent theories of
variable fundamental
constants

Original Bekenstein Model

Is the fine-structure constant really a constant?

$$e = e_0 \epsilon(X^\mu)$$

$$\epsilon A_\mu \rightarrow \epsilon A_\mu + \partial_\mu \chi$$

$$\mathcal{L}_{EM} \propto \epsilon^{-2} f_{\mu\nu} f^{\mu\nu}$$



$$\alpha = \alpha_0 \epsilon^2$$

Original vs Generalized Bekenstein Model

$$\mathcal{L}_{EM} \propto \epsilon^{-2} f_{\mu\nu} f^{\mu\nu}$$

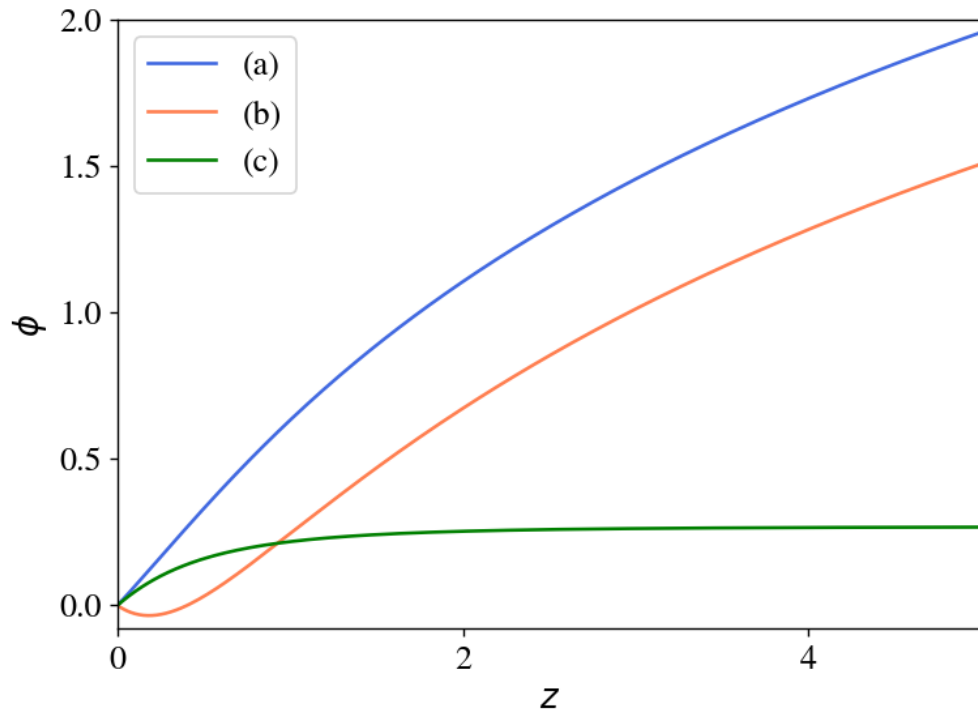


$$\mathcal{L}_{EM} \propto B_F(\phi) f_{\mu\nu} f^{\mu\nu}$$

$$S = \int d^4x \sqrt{-g} [\mathcal{L}_G + \mathcal{L}_M + \epsilon^{-2} \mathcal{L}_{EM} + \mathcal{L}_\epsilon]$$

$$S = \int d^4x \sqrt{-g} \left[-\frac{1}{2} M_{pl}^2 R + \frac{1}{2} M_*^2 \partial_\mu \phi \partial^\mu \phi - M_{pl}^2 \Lambda_0 B_\Lambda(\phi) - \frac{1}{4} B_F(\phi) F_{\mu\nu} F^{\mu\nu} + \bar{\psi} (i\gamma^\mu D_\mu - m_\psi B_\psi(\phi)) \psi + \bar{\chi} (i\gamma^\mu D_\mu - M_\chi B_\chi(\phi)) \chi + V(\phi) \right]$$

Generalized Bekenstein Model



$$\left(\frac{H}{H_0}\right)^2 = (\zeta_b \Omega_b + \zeta_\chi \Omega_\chi) \left(\frac{a_0}{a}\right)^3 + \zeta_\Lambda \Omega_\Lambda$$

$$\ddot{\phi} + 3H\dot{\phi} = -3H_0\omega \left[\zeta_m \Omega_m \left(\frac{a_0}{a}\right)^3 + \zeta_\Lambda \Omega_\Lambda \right]$$

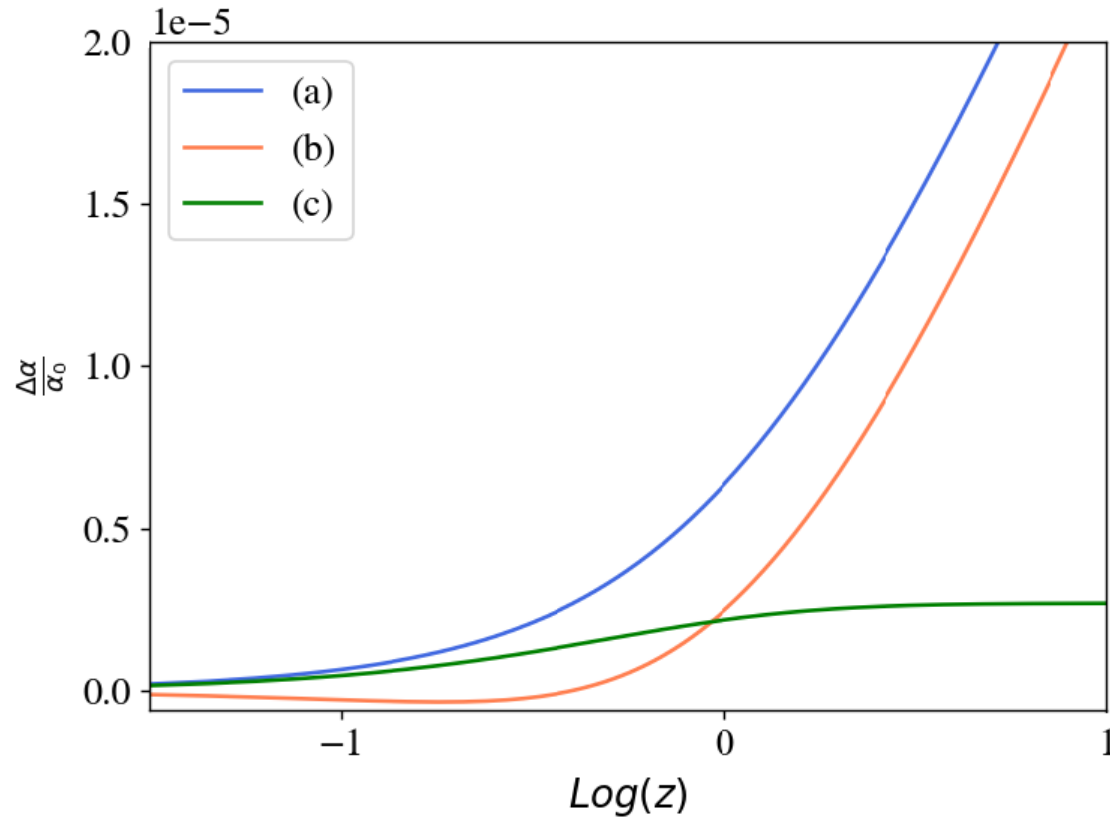
$$\zeta_m \Omega_m = \zeta_b \Omega_b + \zeta_\chi \Omega_\chi$$

Legend: $\zeta_F = 10^{-5}$ and (a) $\zeta_m = 1, \zeta_\Lambda = 0$. (b) $\zeta_m = 1, \zeta_\Lambda = -2$, (c) $\zeta_m = 0, \zeta_\Lambda = 1$.

$$B_i(\Delta\phi) = 1 + \zeta_i \Delta\phi$$

Bekenstein Model

Variation of the fine-structure constant



$$\alpha = \frac{\alpha_0}{B_F(\phi)}$$

$$\frac{\Delta\alpha}{\alpha}(z) = \frac{\alpha - \alpha_0}{\alpha_0} \sim -\zeta_F \Delta\phi$$

$$\frac{1}{H_0} \left(\frac{\dot{\alpha}}{\alpha} \right)_0 \sim -\zeta_F \phi'_0$$

Legend: $\zeta_F = 10^{-5}$ and (a) $\zeta_m = 1, \zeta_\Lambda = 0$. (b) $\zeta_m = 1, \zeta_\Lambda = -2$, (c) $\zeta_m = 0, \zeta_\Lambda = 1$.

Local Constraints

Atomic clocks: $\frac{1}{H_0} \left(\frac{\dot{\alpha}}{\alpha} \right)_0 = (1.4 \pm 1.5) \times 10^{-8}$

Lange *et al.* (2021)

Oklo: $\frac{\Delta\alpha}{\alpha}(z = 0.14) = (0.5 \pm 6.1) \times 10^{-8}$

Petrov *et al.* (2006)

$$\eta = 2 \frac{a_1 - a_2}{a_1 + a_2}$$

$$\eta \sim 1.45 \times 10^{-2} \zeta_b \zeta_F$$

MICROSCOPE: $\eta = (-0.1 \pm 1.3) \times 10^{-14}$

Touboul *et al.* (2019)

Cosmological Constraints

Quasar spectra: $\frac{\Delta\alpha}{\alpha} = -0.64 \pm 0.65 \text{ ppm}$ [1]



Webb: $\frac{\Delta\alpha}{\alpha} (0.2 < z < 4.2) = -2.16 \pm 0.86 \text{ ppm}$

Webb *et al.* (2011)

Set of 21 different measurements ($1.02 < z < 2.31$)

Agafonova *et al.* (2011), Molaro *et al.* (2013), Evans *et al.* (2014), Songaila and Cowie (2014), Murphy *et al.* (2016), Bainbridge and Webb *et al.* (2016), Kotus *et al.* (2017)

ESPRESSO: $\frac{\Delta\alpha}{\alpha} = 1.3 \pm 1.3_{stat} \pm 0.4_{sys} \text{ ppm}$

Murphy *et al.* (2021)

Simulation

Modified CLASS

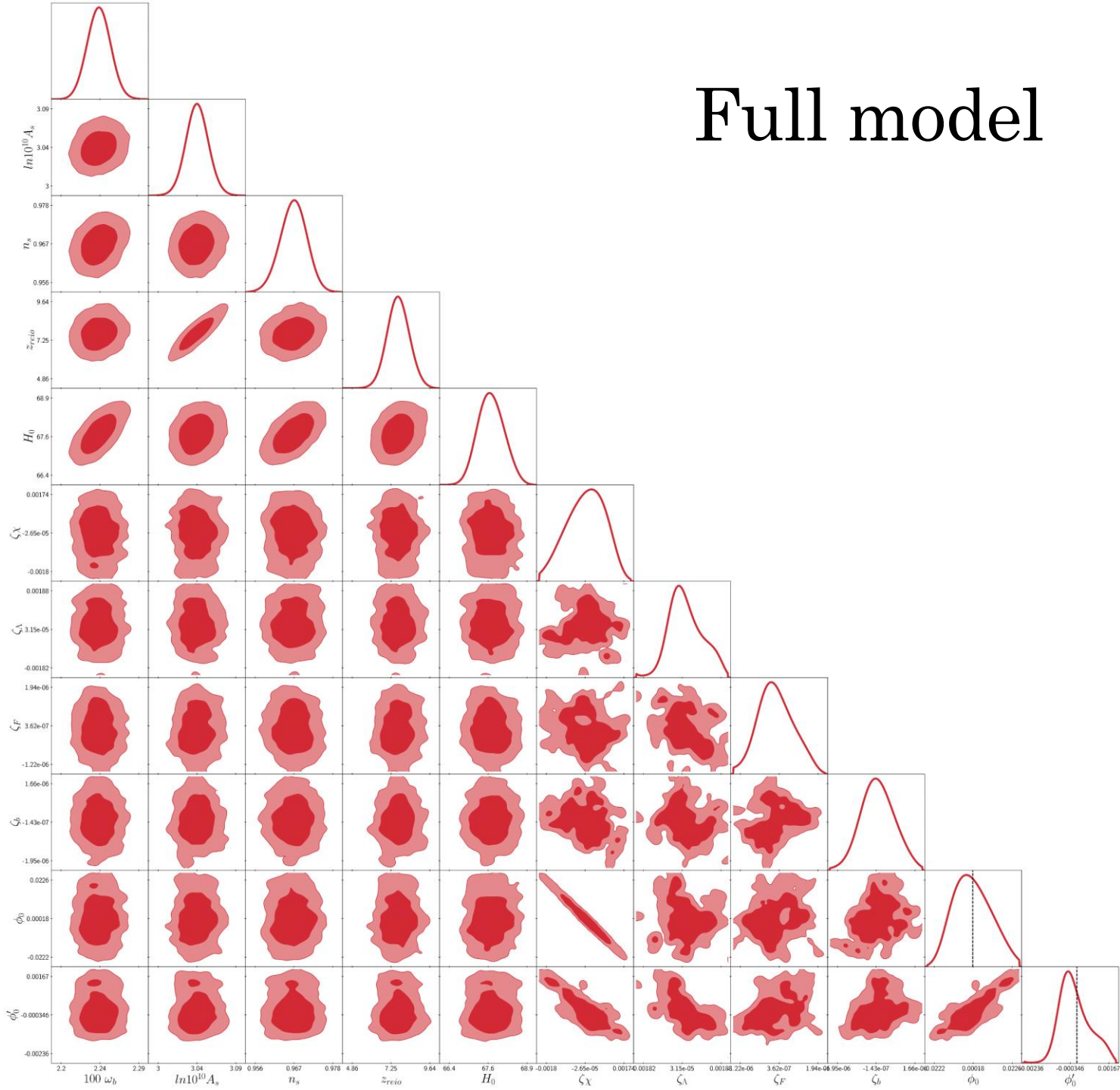


MCMC

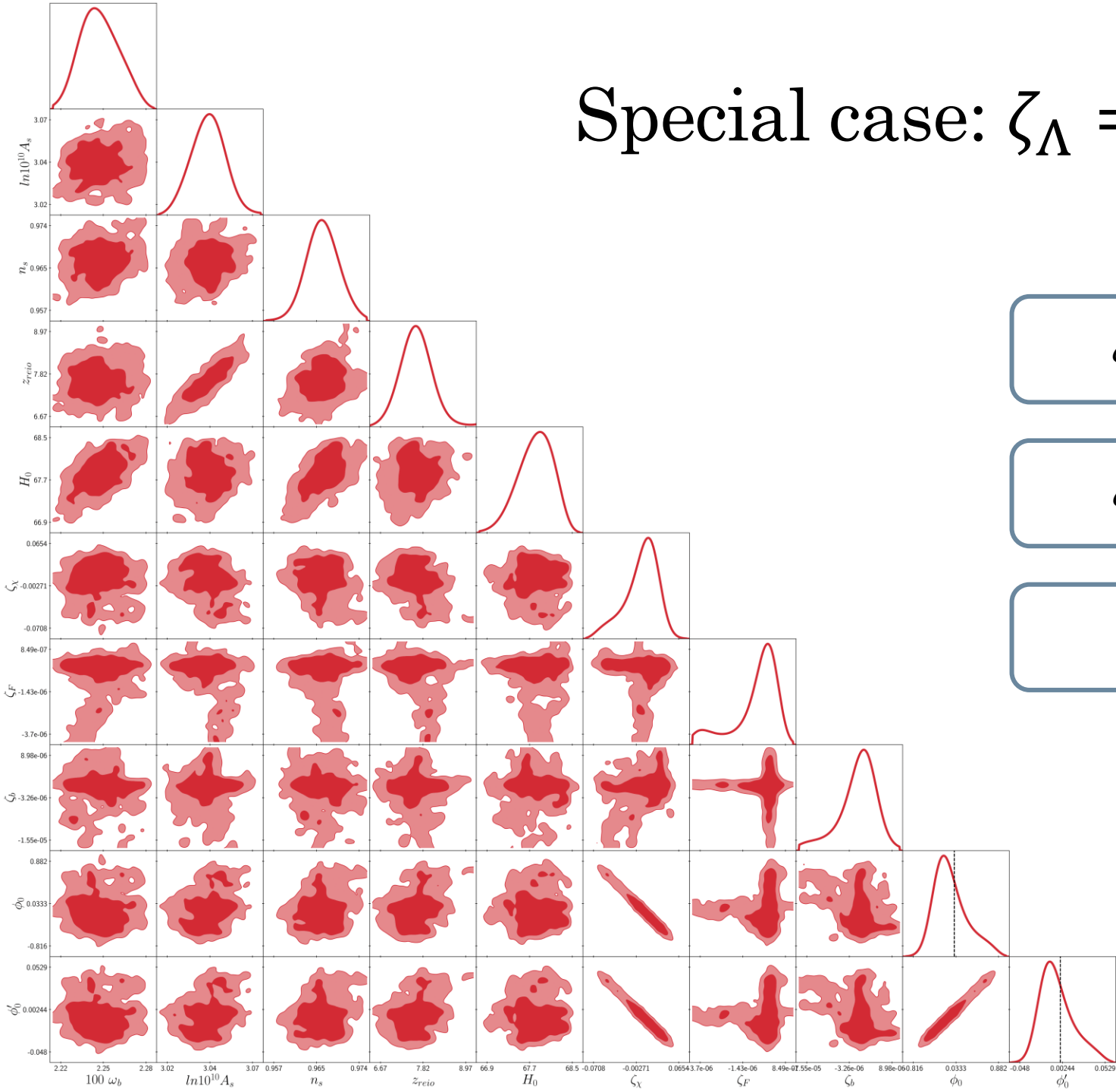
Other data sets: Planck, BAO, Pantheon.

Planck VI (2018), Alam *et al.* (2016). Riess *et al.* (2017)

Full model



Special case: $\zeta_\Lambda = 0$



$$\zeta_F = -0.51_{-0.12}^{+0.92} \text{ ppm}$$

$$\zeta_b = -0.78_{-2.84}^{+3.99} \text{ ppm}$$

$$\zeta_\chi = -0.0059_{-0.014}^{+0.036}$$

Conclusion and Outlook

- Couplings of order one are excluded
- Look at other special cases: $\zeta_m = 0$, $\zeta_\Lambda = \zeta_\chi$
- Explore other models (e.g. rolling tachyon)