

High-Energy Phenomena

Robert Thorne

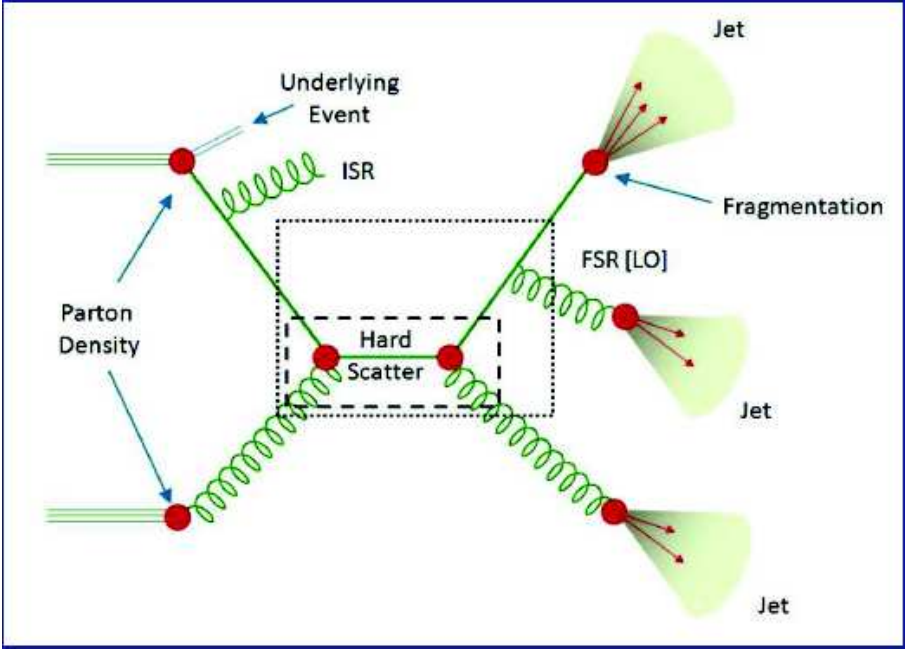
October 4th, 2011



University College London

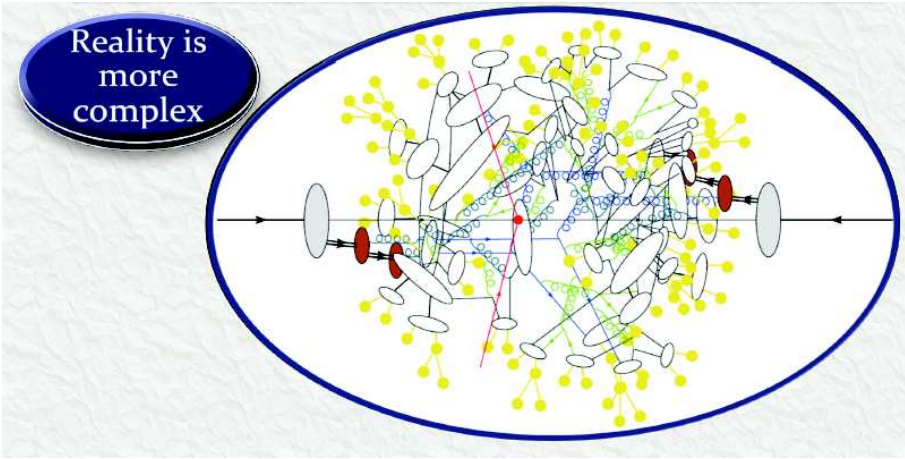
IPPP Research Associate

High energy scattering processes very complicated



Particularly in reality

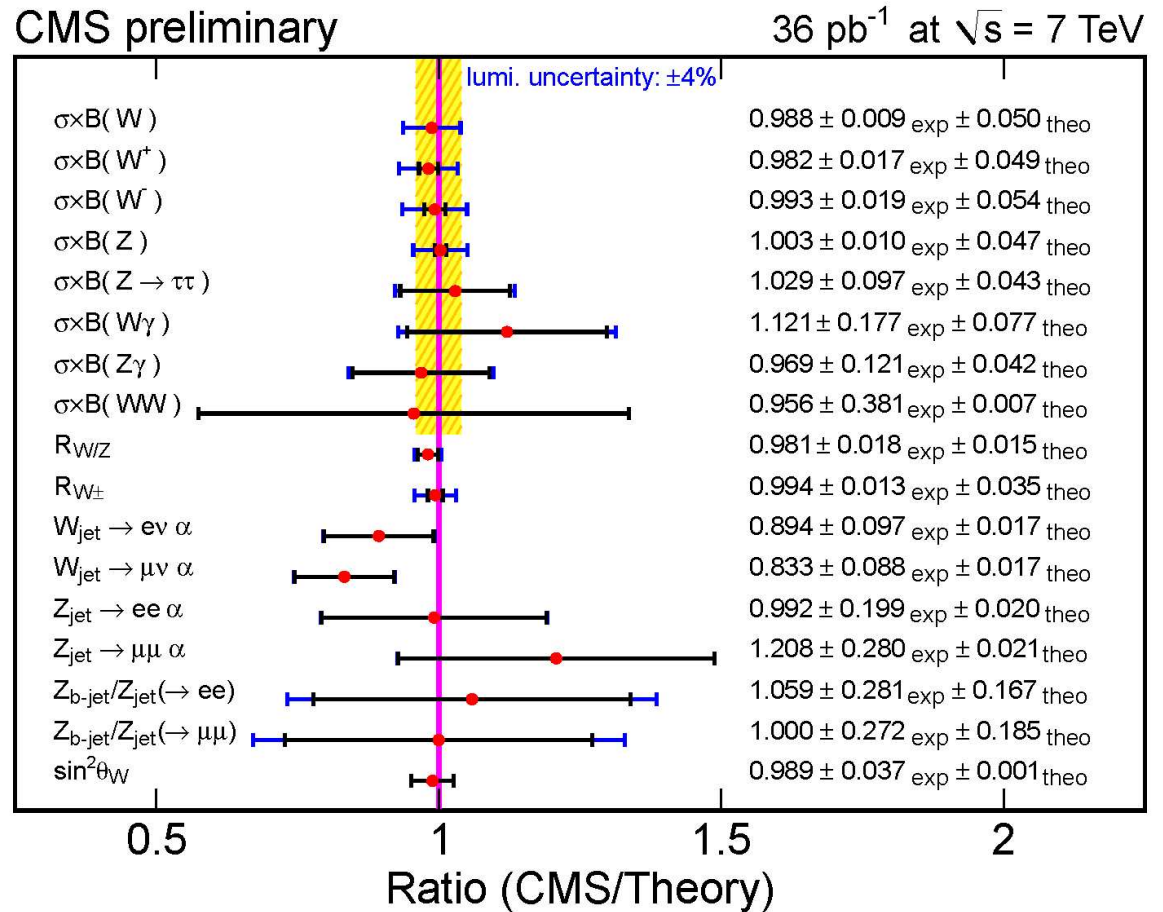
Varelas EPS-2011



Status of NLO and NNLO calculations

Start with fully inclusive quantities.

In general excellent agreement with cross sections measured at LHC.



Enormous number of processes calculated at **NLO**.

For example **MCFM** includes a wide variety in one overall framework (**Ellis, Campbell and others**).

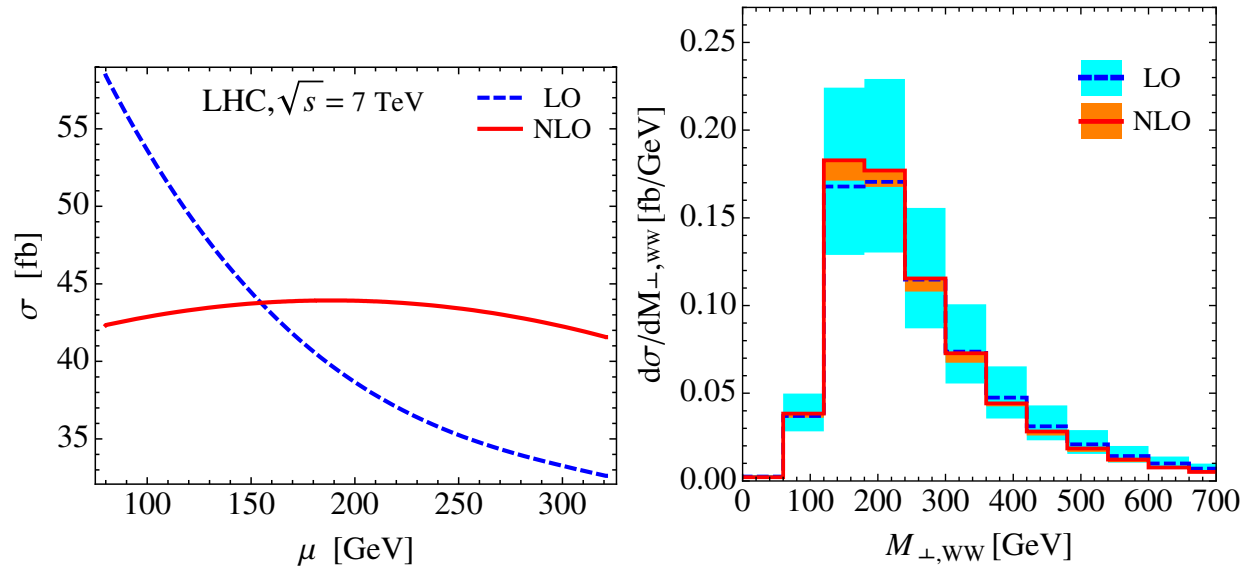
Final state	Notes	Reference	Final state	Notes	Reference
W/Z			H (gluon fusion)		
diboson (W/Z/γ)	photon fragmentation, anomalous couplings	hep-ph/0905386, arXiv:1105.0020	H+1 jet (g.f.)	effective coupling	
Wbb	massless b-quark massive b quark	hep-ph/0810489 arXiv:1011.6647	H+2 jets (g.f.)	effective coupling	hep-ph/0808194, arXiv:1001.4495
Zbb	massless b-quark	hep-ph/0008304	WH/ZH		
W/Z+1 jet			H (VBF)		hep-ph/0403194
W/Z+2 jets		hep-ph/0202176, hep-ph/0308195	Hb	5-flavour scheme	hep-ph/0204093
Wc	massive c-quark	hep-ph/0506289	t	s- and t-channel (5F), top decay included	hep-ph/0408158
Zb	5-flavour scheme	hep-ph/0312024	t	t-channel (4F)	arXiv:0903.0005, arXiv:0907.3933
Zb+jet	5-flavour scheme	hep-ph/0510362	Wt	5-flavour scheme	hep-ph/0506289
			top pairs	top decay included	

Dramatic improvement in automated calculation of **NLO** cross sections (**Hirschi et al**).

Process	μ	n_{ij}	Cross section (pb)	
			LO	NLO
a.1 $pp \rightarrow t\bar{t}$	m_{top}	5	123.76 ± 0.05	162.08 ± 0.12
a.2 $pp \rightarrow t\bar{j}$	m_{top}	5	34.78 ± 0.03	41.03 ± 0.07
a.3 $pp \rightarrow t\bar{j}j$	m_{top}	5	11.851 ± 0.006	13.71 ± 0.02
a.4 $pp \rightarrow t\bar{b}j$	$m_{top}/4$	4	25.62 ± 0.01	30.96 ± 0.06
a.5 $pp \rightarrow t\bar{b}j\bar{j}$	$m_{top}/4$	4	8.195 ± 0.002	8.91 ± 0.01
b.1 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e$	m_W	5	5072.5 ± 2.9	6146.2 ± 9.8
b.2 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e j$	m_W	5	828.4 ± 0.8	1065.3 ± 1.8
b.3 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e jj$	m_W	5	298.8 ± 0.4	300.3 ± 0.6
b.4 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^-$	m_Z	5	1007.0 ± 0.1	1170.0 ± 2.4
b.5 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- j$	m_Z	5	156.11 ± 0.03	203.0 ± 0.2
b.6 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- jj$	m_Z	5	54.24 ± 0.02	56.69 ± 0.07
c.1 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e b\bar{b}$	$m_W + 2m_b$	4	11.557 ± 0.005	22.95 ± 0.07
c.2 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e t\bar{t}$	$m_W + 2m_{top}$	5	0.009415 ± 0.000003	0.01159 ± 0.00001
c.3 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- b\bar{b}$	$m_Z + 2m_b$	4	9.459 ± 0.004	15.31 ± 0.03
c.4 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- t\bar{t}$	$m_Z + 2m_{top}$	5	0.0035131 ± 0.0000004	0.004876 ± 0.000002
c.5 $pp \rightarrow \gamma t\bar{t}$	$2m_{top}$	5	0.2906 ± 0.0001	0.4169 ± 0.0003
d.1 $pp \rightarrow W^+ W^-$	$2m_W$	4	29.976 ± 0.004	43.92 ± 0.03
d.2 $pp \rightarrow W^+ W^- j$	$2m_W$	4	11.613 ± 0.002	15.174 ± 0.008
d.3 $pp \rightarrow W^+ W^+ jj$	$2m_W$	4	0.07048 ± 0.00004	0.1377 ± 0.0005
e.1 $pp \rightarrow HW^+$	$m_W + m_H$	5	0.3428 ± 0.0003	0.4455 ± 0.0003
e.2 $pp \rightarrow HW^+ j$	$m_W + m_H$	5	0.1223 ± 0.0001	0.1501 ± 0.0002
e.3 $pp \rightarrow HZ$	$m_Z + m_H$	5	0.2781 ± 0.0001	0.3659 ± 0.0002
e.4 $pp \rightarrow HZ j$	$m_Z + m_H$	5	0.0988 ± 0.0001	0.1237 ± 0.0001
e.5 $pp \rightarrow Ht\bar{t}$	$m_{top} + m_H$	5	0.08896 ± 0.00001	0.09869 ± 0.00003
e.6 $pp \rightarrow Hb\bar{b}$	$m_b + m_H$	4	0.16510 ± 0.00009	0.2099 ± 0.0006
e.7 $pp \rightarrow Hjj$	m_H	5	1.104 ± 0.002	1.036 ± 0.002

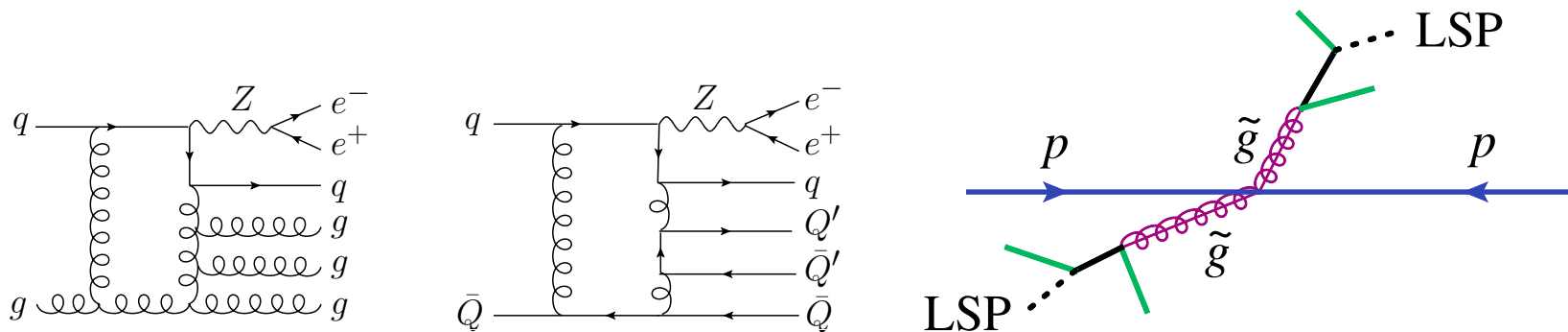
Table 2: Results for total rates, possibly within cuts, at the 7 TeV LHC, obtained with MADFKS and MADLOOP. The errors are due to the statistical uncertainty of Monte Carlo integration. See the text for details.

Enormous improvement in calculation of processes with many legs at **NLO** recently, e.g. $W^+W^- + jj$, Melia, et al.



Huge improvement in scale uncertainty, which implies the same for theory uncertainty.

And with even more final state particles $Z + jjjj$, Ita et al, ($W = jjjj$ also known). Background to gluino pair production.

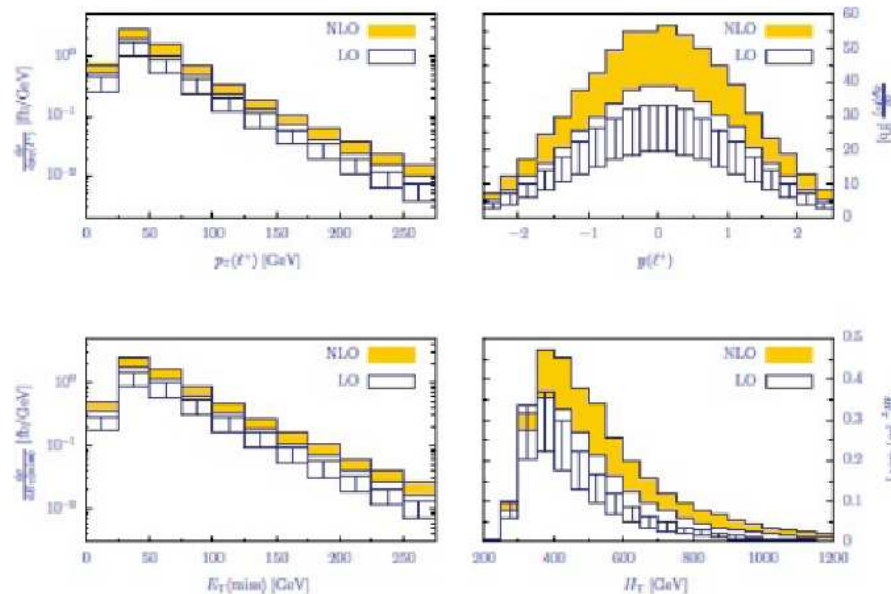


Sometimes at **NLO** little improvement in uncertainty, essentially because part of **NLO** is really **LO**.

For example Melnikov, Schulze and Scharf

The process $t\bar{t} + \gamma$ is an interesting SM signal

- We calculated $pp \rightarrow t\bar{t} + \gamma \rightarrow b\bar{b} \ell\nu jj + \gamma$ at NLO QCD



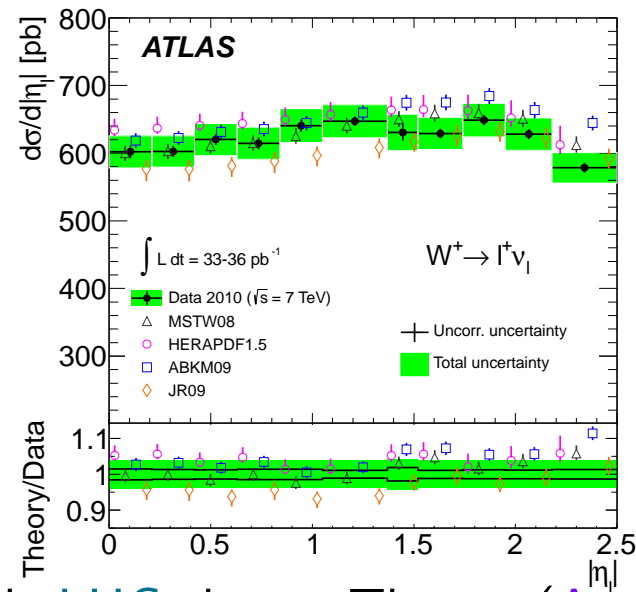
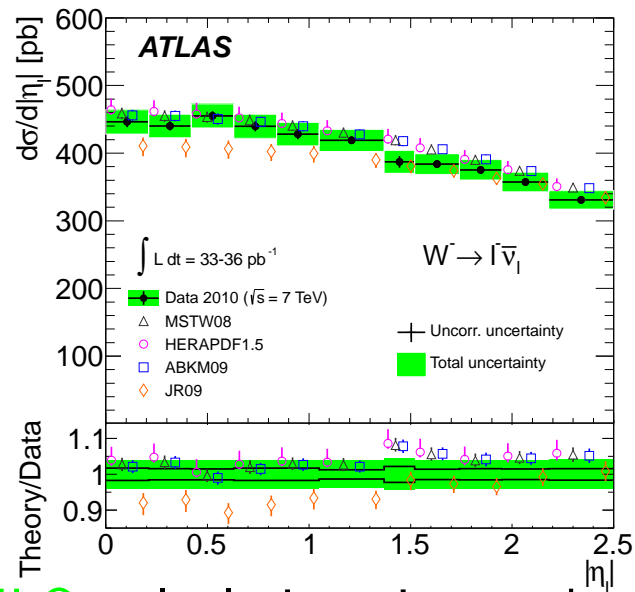
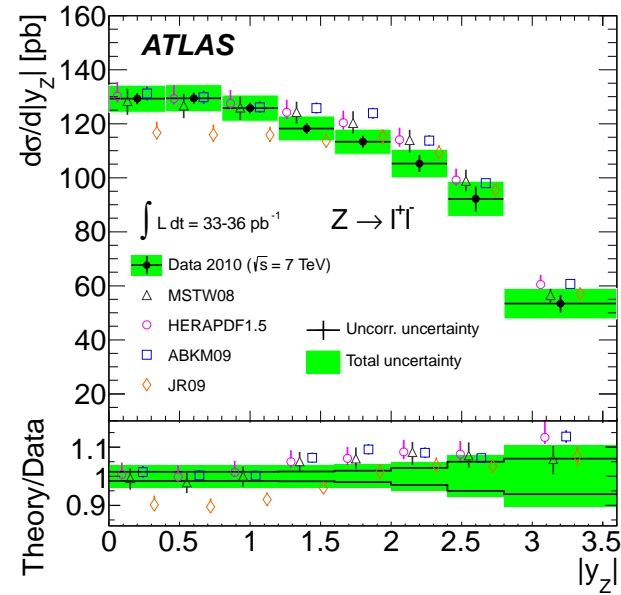
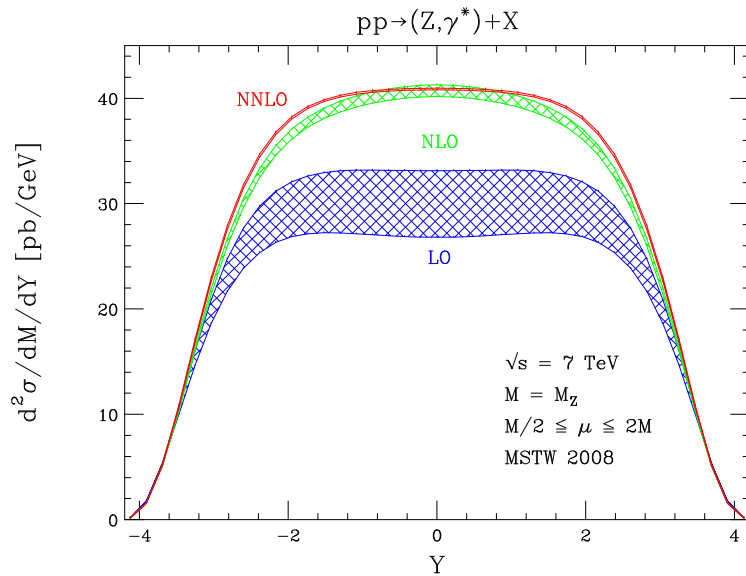
$$\sigma_{t\bar{t}\gamma}^{\text{LO}} = 74.5^{+24.0}_{-16.9} \text{ fb}$$

$$\sigma_{t\bar{t}\gamma}^{\text{NLO}} = 138^{+30}_{-23} \text{ fb}$$

$$\sigma_{t\bar{t}\gamma}^{\text{decay}} = 56\% \sigma_{t\bar{t}\gamma}^{\text{tot}}$$

- large K-factor \Rightarrow extra phase space for additional jet
- no reduction of scale dependence \Rightarrow opening up of q - g channel at NLO

Progress at NNLO. Some final states known for LHC – W, Z, Higgs, ..



NNLO calculations in good agreement with LHC data. Theory (Anastasiou *et al*) uncertainty now tiny. Noticeable differences from PDF versions.

More complicated Final States.

$e^+e^- \rightarrow 3 \text{ jets at NNLO}$

Method thoroughly tried and tested for partons only in the final state

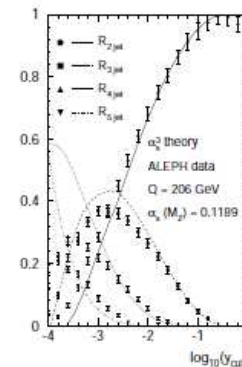
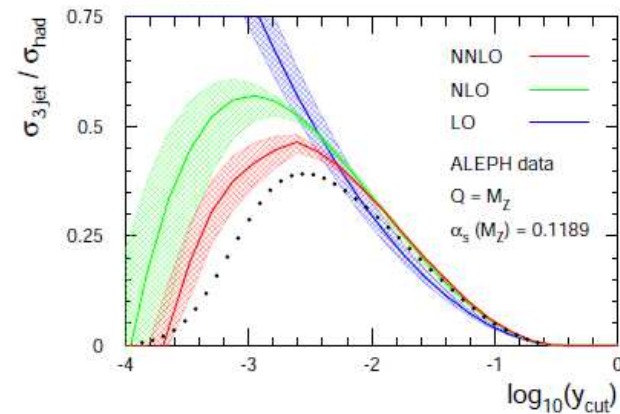
Gehrmann-De Ridder, Gehrmann, Heinrich, NG (07)

- ✓ NNLO corrections to jet rate small
- ✓ stable perturbative prediction
- ✓ resummation not needed
- ✓ theory error below 2%
- ✓ small hadronisation corrections
- ✓ α_s extraction from jet rates

Dissertori, Gehrmann-De Ridder,
Gehrmann, Heinrich, Stenzel, NG (09)

- ✓ fit at $y_{cut} = 0.02$
- ✓ consistent results at other y_{cut}

$$\alpha_s(M_Z) = 0.1175 \pm 0.0020(\text{exp}) \pm 0.0015(\text{th})$$



Glover St Andrews 2011.

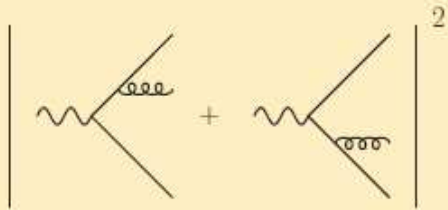
More Inclusive – Monte Carlos

Enormous recent progress in merging fixed order calculations with Monte Carlo generators.

(NLO)ME vs. PS

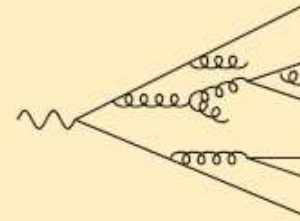
Approaches to real emission corrections

(NLO) Matrix Element



- + **Exact** to fixed order
- Perturbative series breaks down due to **large logarithms**

Parton Shower



- + Resums logarithms to **all orders**
- Only **approximation** to real emission ME

Combine Advantages \Rightarrow ME \otimes PS, NLO \otimes PS, MENLOPS

- avoid double-counting by dividing phase space $\Rightarrow Q_{\text{cut}}$
- **ME** to describe **hard radiation**, **PS** for **intrajet evolution**

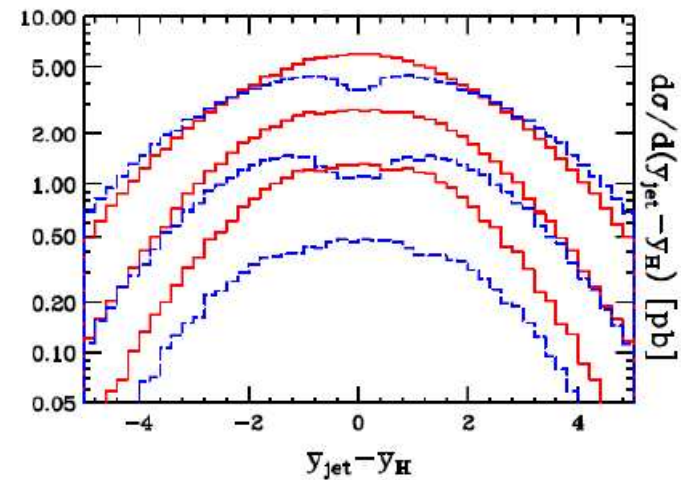
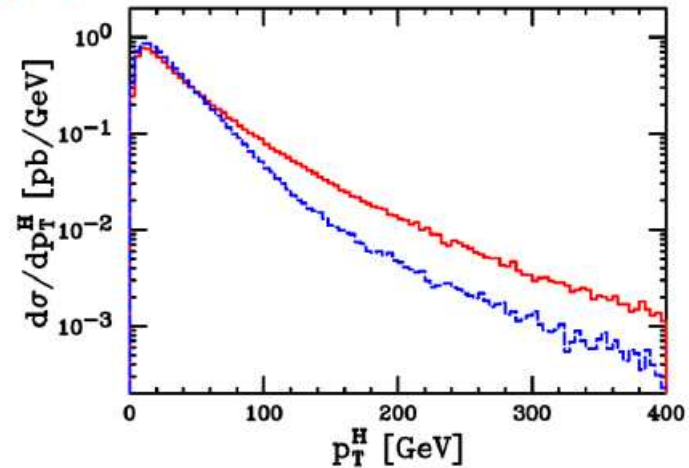
Schönherr St Andrews 2011.

Different Approaches

- The two approaches are the same to NLO.
- Differ in the subleading terms.
- In particular at large p_T

$$d\sigma \approx R(v, r) d\Phi_v d\Phi_r \quad \text{MC@NLO}$$

$$d\sigma \approx \frac{\bar{B}(v)}{B(v)} R(v, r) d\Phi_v d\Phi_r \quad \text{POWHEG}$$



JHEP 0904:002,2009 Alwall et. al.

Forum 6th September

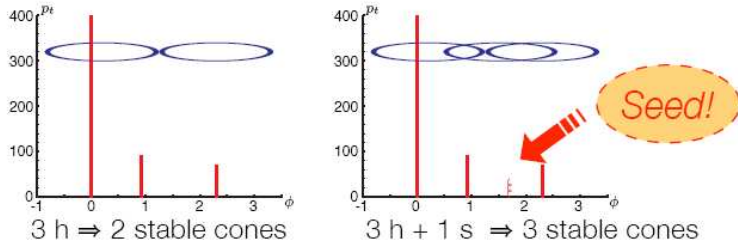
Richardson Cosener's House 2011

Developments in Perturbative QCD - Jets.

Long known that initial cone-based jet algorithms are generally infrared unsafe

Mid-point algorithm

Soyez



Real life does not have infinities, but pert. infinity leaves a real-life trace

$$\alpha_s^2 + \alpha_s^3 + \alpha_s^4 \times \infty \rightarrow \alpha_s^2 + \alpha_s^3 + \alpha_s^4 \times \ln p_t/\Lambda \rightarrow \alpha_s^2 + \underbrace{\alpha_s^3 + \alpha_s^3}_{\text{BOTH WASTED}}$$

with quantitative finite consequences. “anti- k_t algorithm” combines all soft partons within “cone” with hard parton to produce cone-like jet definition.

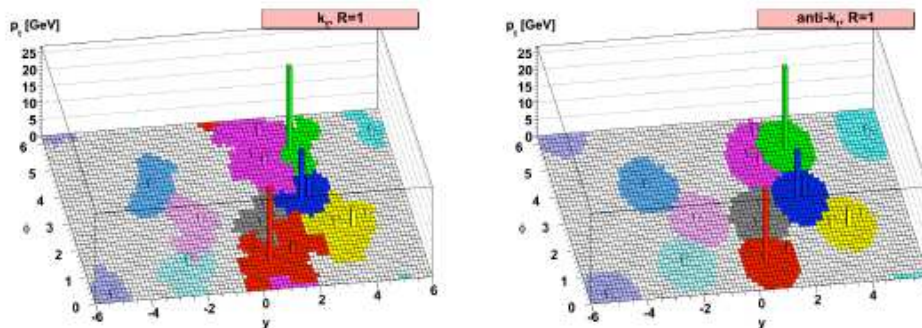
Come back to recombination-type algorithms:

Soyez

$$d_{ij} = \min(k_{t,i}^{2p}, k_{t,j}^{2p}) (\Delta\phi_{ij}^2 + \Delta\eta_{ij}^2)$$

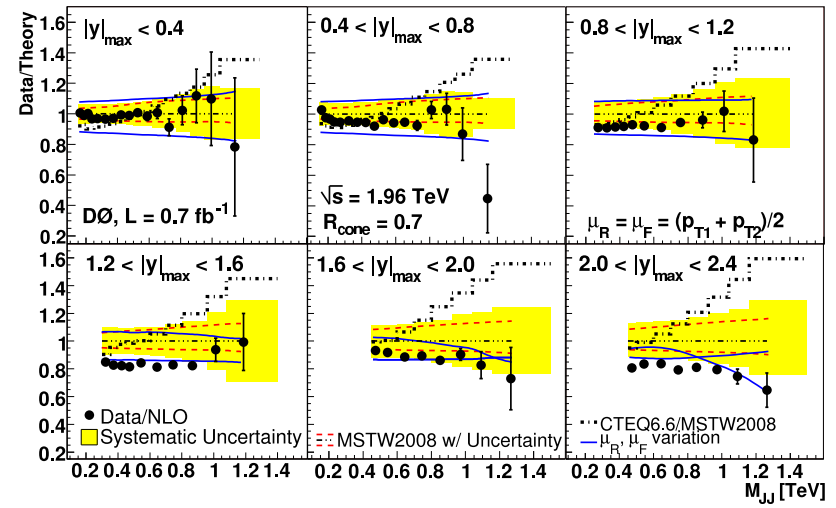
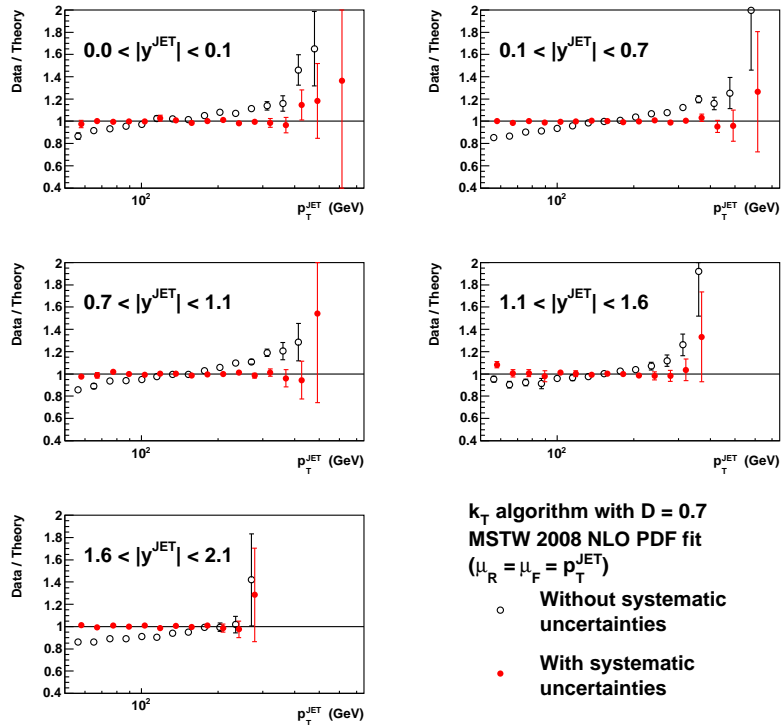
- $p = 1$: k_t algorithm
- $p = 0$: Aachen/Cambridge algorithm
- $p = -1$: anti- k_t algorithm [M.Cacciari, G.Salam, G.S., JHEP 04 (08) 063]

Hard event + homogeneous soft background



Jet production – Inclusive, Dijets and Three-Jets.

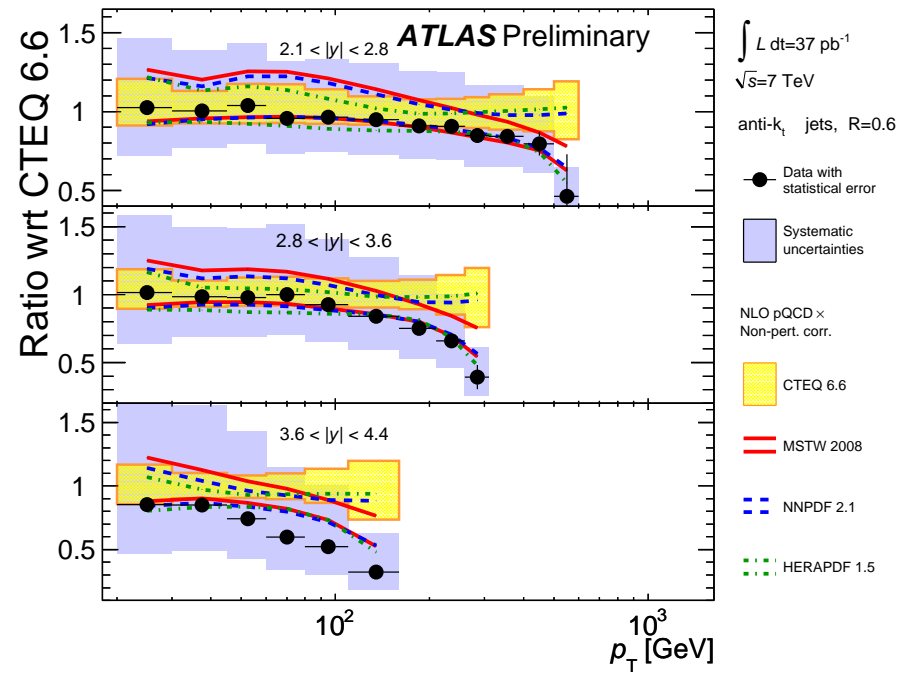
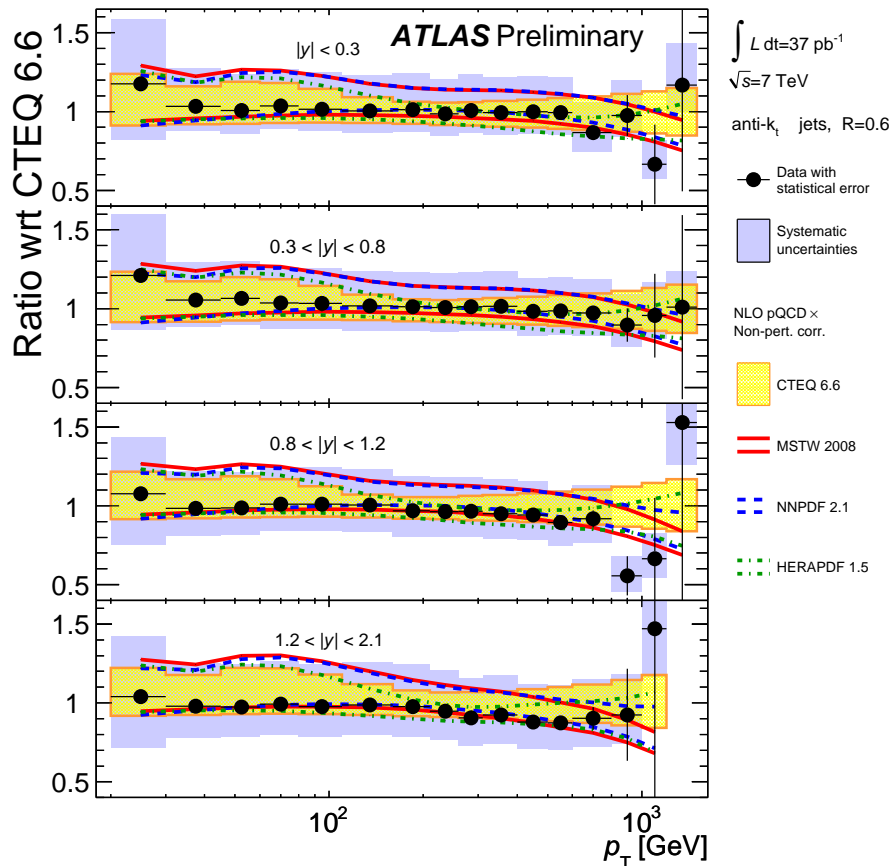
CDF Run II inclusive jet data, $\chi^2 = 56$ for 76 pts.



Easy to get excellent agreement with **Tevatron** inclusive jets.

A bit harder with dijets. Problems with theory at high M_{JJ} and y . Related to choice of scale of function of p_T ?

Recent results from **D0** on three jets cross sections discriminate between PDFs. See backup.

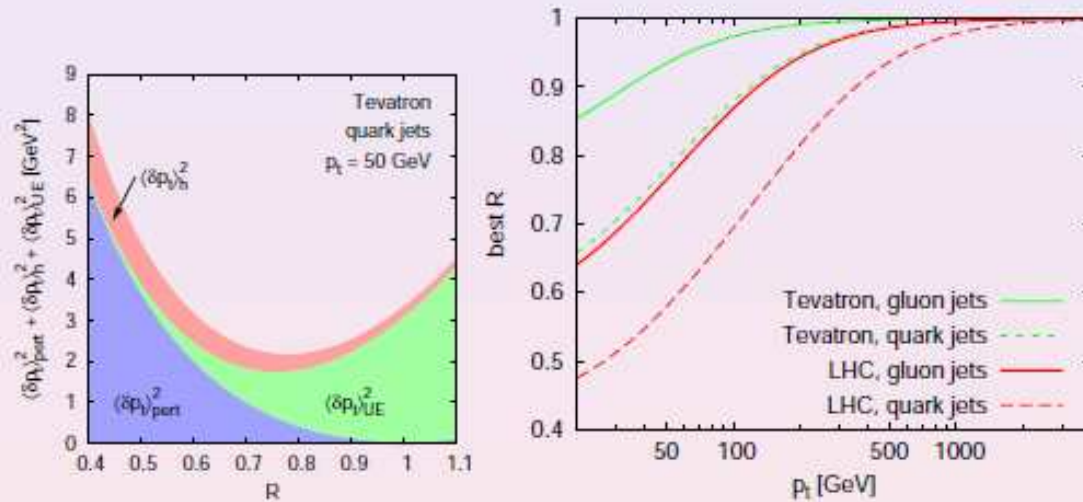


Jets at LHC Starting to discriminate between PDFs and test QCD, but size of correlated errors makes comparison to the PDFs by eye very difficult.

Possible problems with NLO calculations at high p_T and y even for inclusive jets. Full NNLO desirable.

Knowing R dependence gives rise to concept of optimal R values. Based on minimising

$$\langle \delta p_t^2 \rangle = \langle \delta p_t \rangle_h^2 + \langle \delta p_t \rangle_{UE}^2 + \langle \delta p_t \rangle_{PT}^2$$

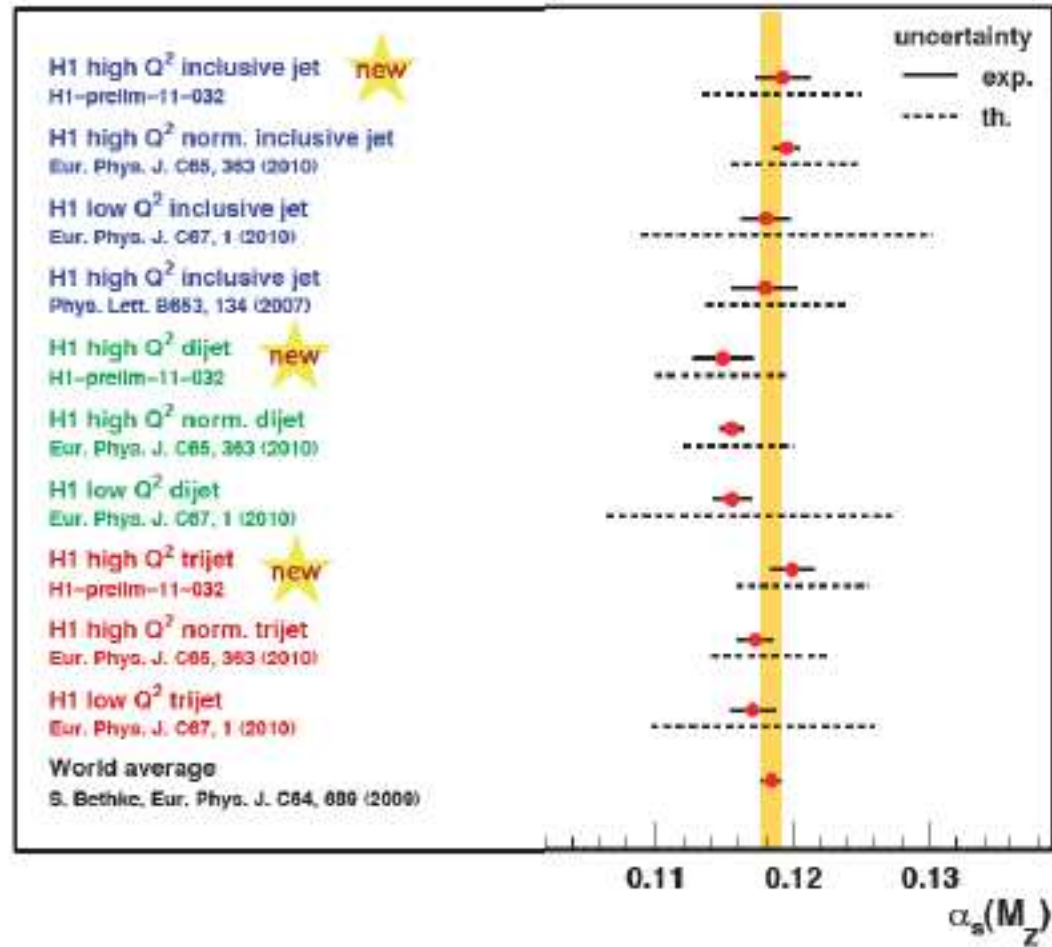


At high p_t one should use a larger R - minimises perturbative effect. Likewise for gluon jets a larger R is suggested. For LHC smaller R values than Tevatron.

Dasgupta

Different considerations require different values of R for jets. However, currently ATLAS and CMS use $R = 0.4, 0.6$ and $R = 0.5, 0.7$ respectively. A common value would be nice.

HERA Jets



Measurement of jets at HERA leads to many measurements of α_s . All in agreement with world average. Limited by theory uncertainty due to NLO calculation.

Potential Improvements Using LHeC

case	cut [Q^2 in GeV^2]	α_S	\pm uncertainty	relative precision in %
HERA only (14p)	$Q^2 > 3.5$	0.11529	0.002238	1.94
HERA+jets (14p)	$Q^2 > 3.5$	0.12203	0.000995	0.82
LHeC only (14p)	$Q^2 > 3.5$	0.11680	0.000180	0.15
LHeC only (10p)	$Q^2 > 3.5$	0.11796	0.000199	0.17
LHeC only (14p)	$Q^2 > 20.$	0.11602	0.000292	0.25
LHeC+HERA (10p)	$Q^2 > 3.5$	0.11769	0.000132	0.11
LHeC+HERA (10p)	$Q^2 > 7.0$	0.11831	0.000238	0.20
LHeC+HERA (10p)	$Q^2 > 10.$	0.11839	0.000304	0.26

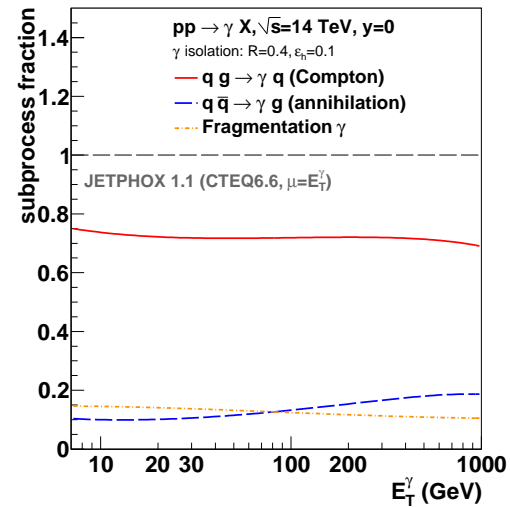
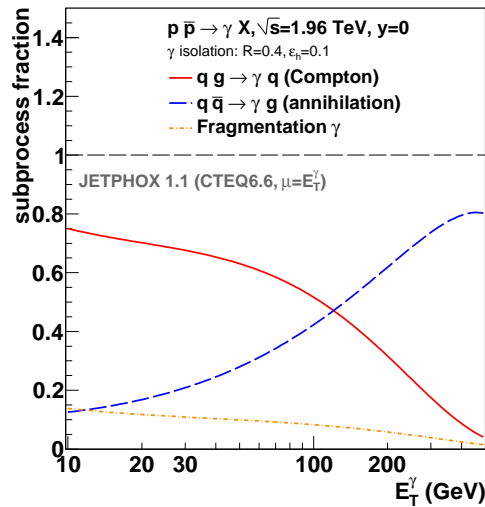
Table 4.4: Results of NLO QCD fits to HERA data (top, without and with jets) to the simulated LHeC data alone and to their combination. Here 10p or 14p denotes two different sets of parametrisations, one, with 10 parameters, the minimum parameter set used in [37] and the other one with four extra parameters

Klein/Radescu

Can get enormous improvement in experimental error on $\alpha_S(M_Z^2)$ from evolution of structure functions and other processes, including jets.

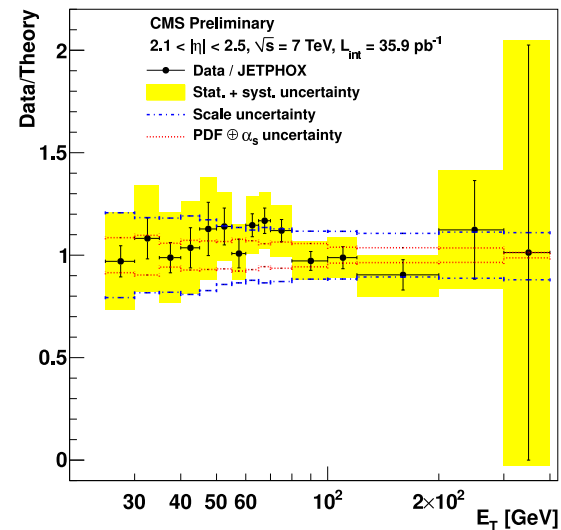
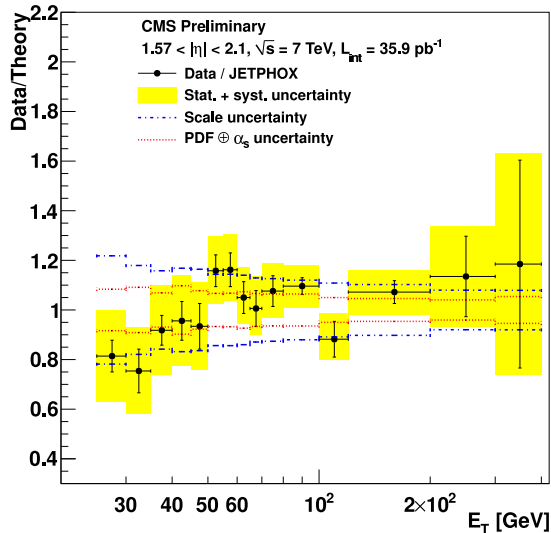
However, must remember that there is always a theory uncertainty, and it will be a great challenge to QCD theory to make the most of such results. Some current limitations, e.g. charm mass uncertainty, would be automatically improved by LHeC itself.

Prompt Photons



Ichou, d'Enterria

Much better sensitivity to gluons at the LHC than Tevatron from prompt photon production, and much safer than fixed target experiments where nonperturbative corrections very large. Important discriminator in principle. Photon isolation necessary.



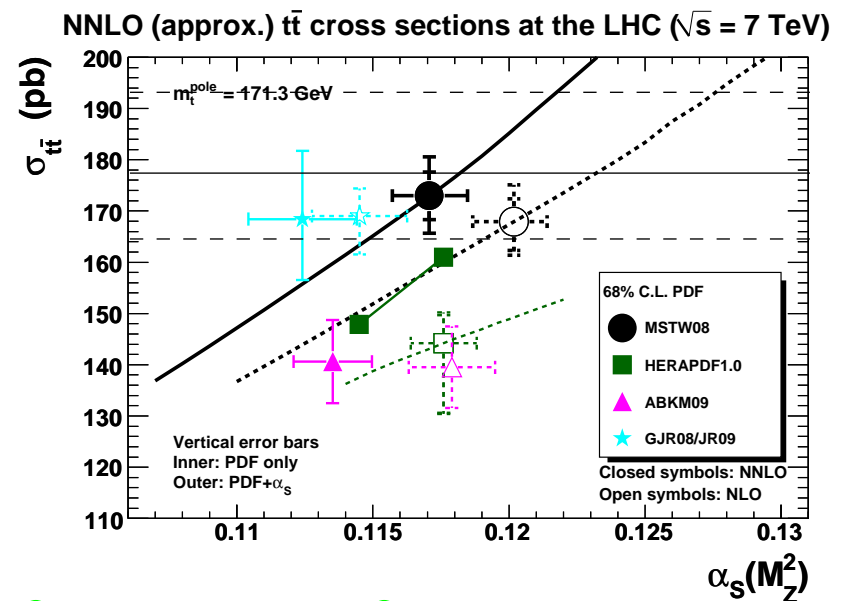
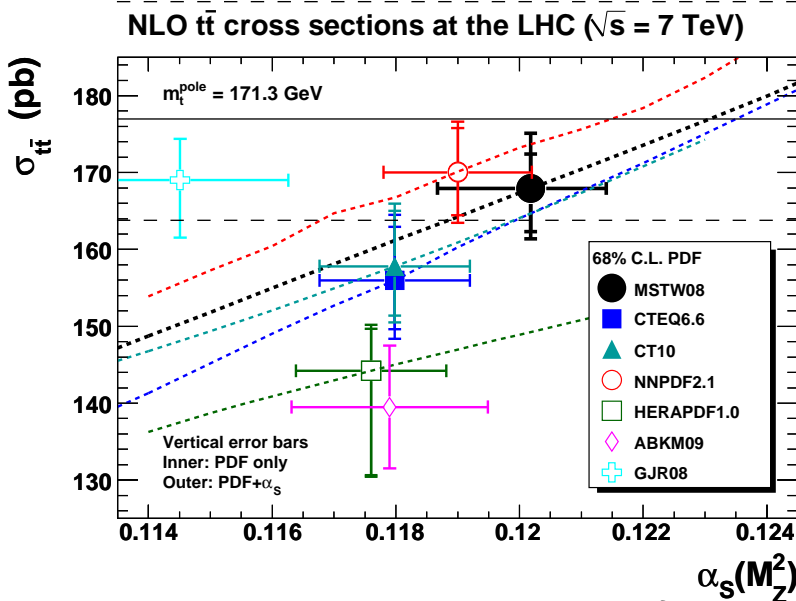
Top-antitop Cross-section Inclusive cross-section known approximately to NNLO

Intrinsic theory uncertainty not very large – for example, recent NNLL calculation by Beneke et al.

Data getting precise. Main uncertainty in choice of PDFs, not in individual uncertainty but choice of set. Correlated to Higgs predictions.

Plots by G. Watt – modified by RST ATLAS preliminary combined $\sigma_{t\bar{t}} = 176_{-13}^{+16}$ pb.

		Tevatron	LHC ($\sqrt{s} = 7$ TeV)	LHC ($\sqrt{s} = 14$ TeV)
NNLO ^{IP1} _{app}	(Ref. [41])	$7.08_{-0.24}^{+0.20}$	163_{-5}^{+7}	920_{-39}^{+60}
NNLO ^{IP1} _{SCHEP}	(Ref. [42])	$6.63_{-0.27}^{+0.00}$	155_{-2}^{+3}	851_{-5}^{+25}
NNLO ^{P1M} _{SCHEP}	(Ref. [38])	$6.62_{-0.40}^{+0.05}$	155_{-8}^{+8}	860_{-43}^{+46}
NNLL ^{IP1} _{SCHEP}	(Ref. [42])	$6.55_{-0.14}^{+0.16}$	150_{-7}^{+7}	824_{-44}^{+41}
NNLL ^{P1M} _{SCHEP}	(Ref. [38])	$6.46_{-0.19}^{+0.18}$	147_{-6}^{+7}	811_{-42}^{+45}
NNLL ₂	this work	$7.22_{-0.47}^{+0.31}$	163_{-8}^{+7}	896_{-37}^{+40}



Differences between groups significant at NLO, and at NNLO.

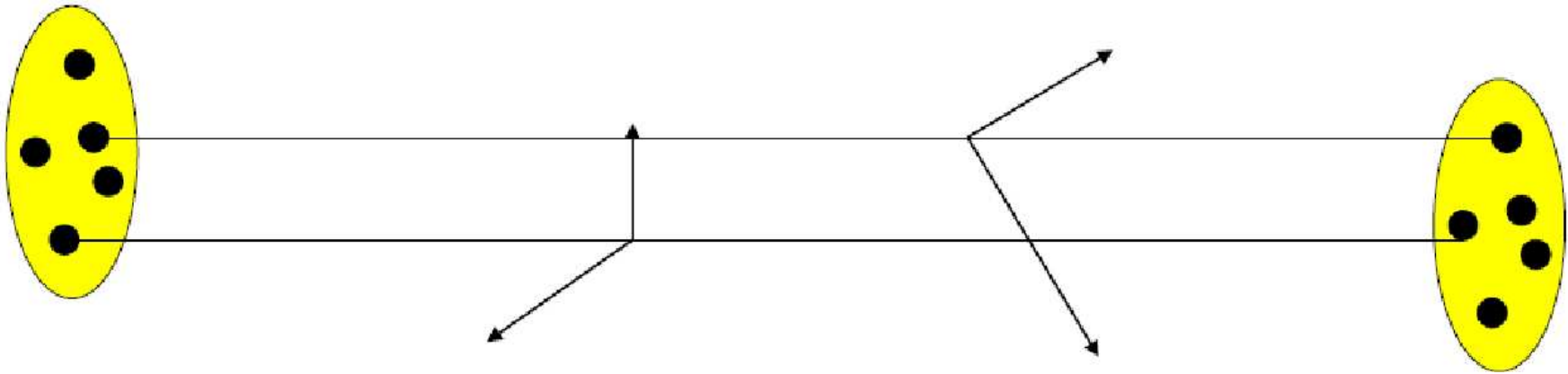
Multiparton Interactions

If the interactions occur independently they should follow Poissonian statistics.

$$P_n = \frac{\langle n \rangle^n}{n!} \exp - \langle n \rangle$$

But we must also consider energy-momentum conservation, which suppresses large numbers of scatterings.

Also need to model the spatial distribution on partons.



The cross-section can then be regulated either by a cut-off $p_{T,\min}$ or smoothing parameter p_{T0} , e.g. $\frac{d\sigma}{dp_T^2} \propto \frac{\alpha_S^2(p_T^2 + p_{T0}^2)}{(p_T^2 + p_{T0}^2)^2}$, either usually about 2GeV for the best tune.

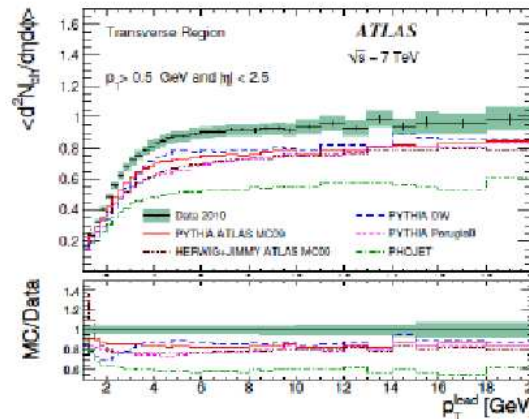
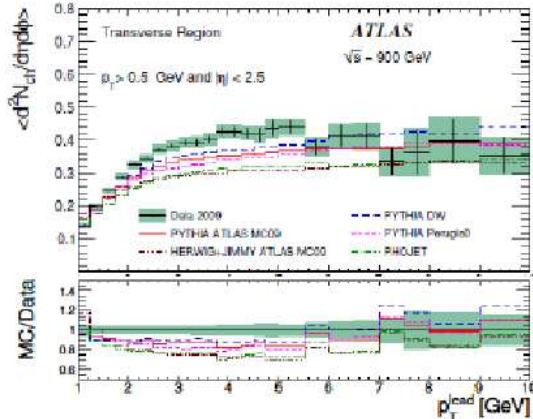
Typically about 2-3 interactions per event at the Tevatron and 4-5 at the LHC.

ATLAS underlying event results

Leading charged track N_{ch} and $\sum p_T$, $p_T > 500$ MeV (arXiv:1012.0791)

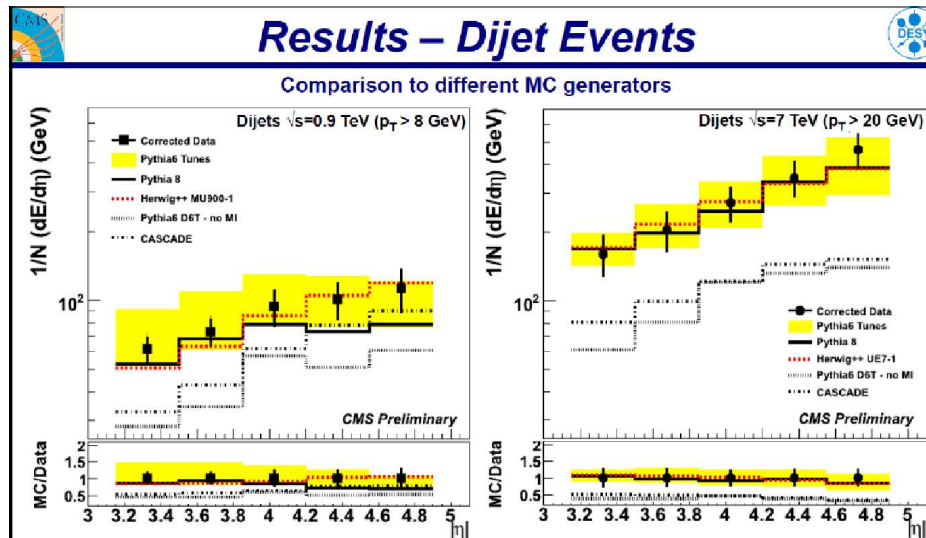
900 GeV

7 TeV



Comparison to CMS data after retuning

Buckley SM@LHC

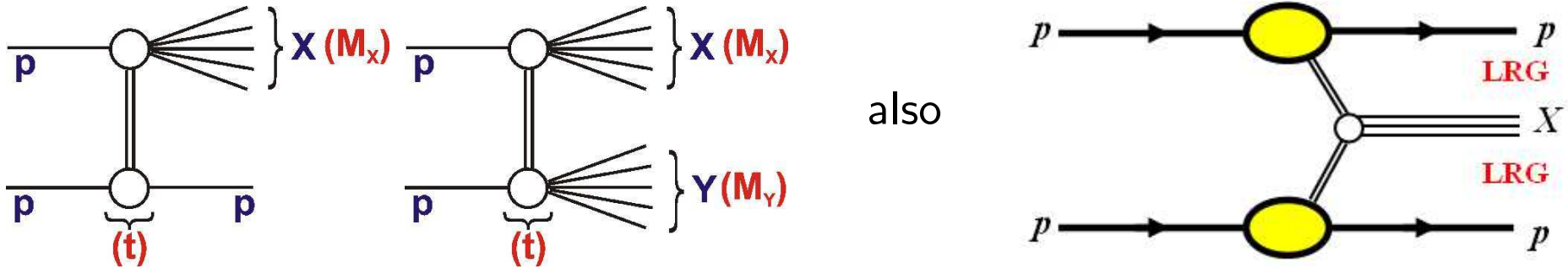


Knutson DIS2011

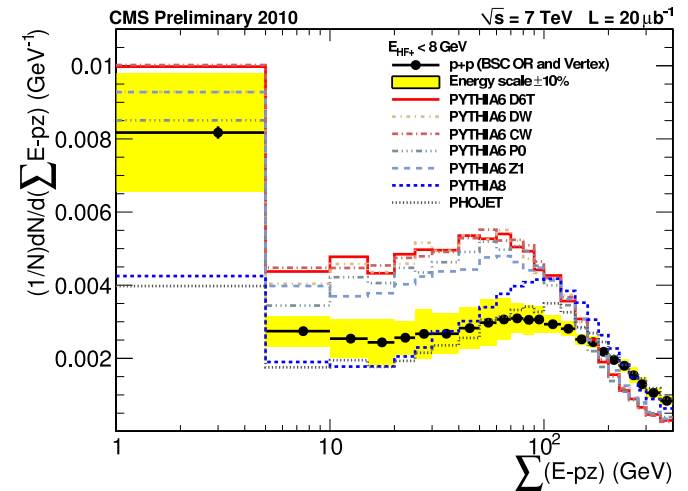
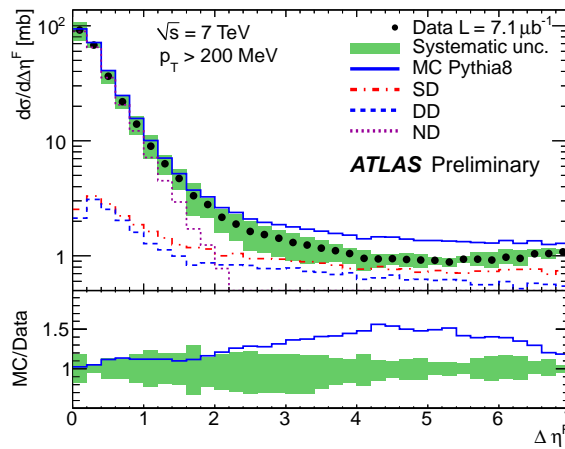
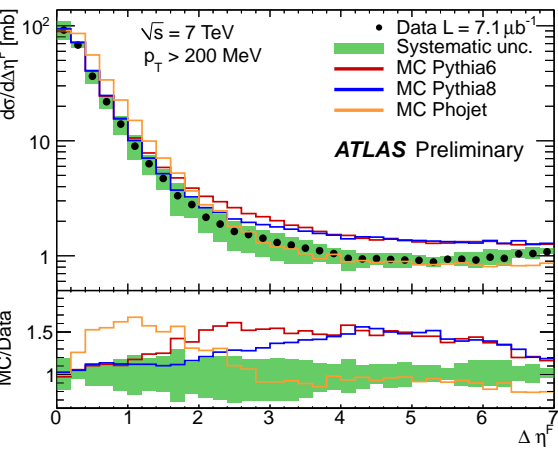
Large contribution from multiple interactions. Improved theory important here. There have been some recent developments

Diffraction at the LHC

Potentially either single or double diffraction can occur (and central exclusive production). Accompanied by large rapidity gaps.



However, not so easy to define experimentally. **ATLAS** use a large forward rapidity gap definition and **CMS** base the definition on energy in forward detectors and/or $\Sigma E - p_z \propto$ Pomeron energy (with option of additional $\Delta\eta \sim 2$).



LHC and Parton x

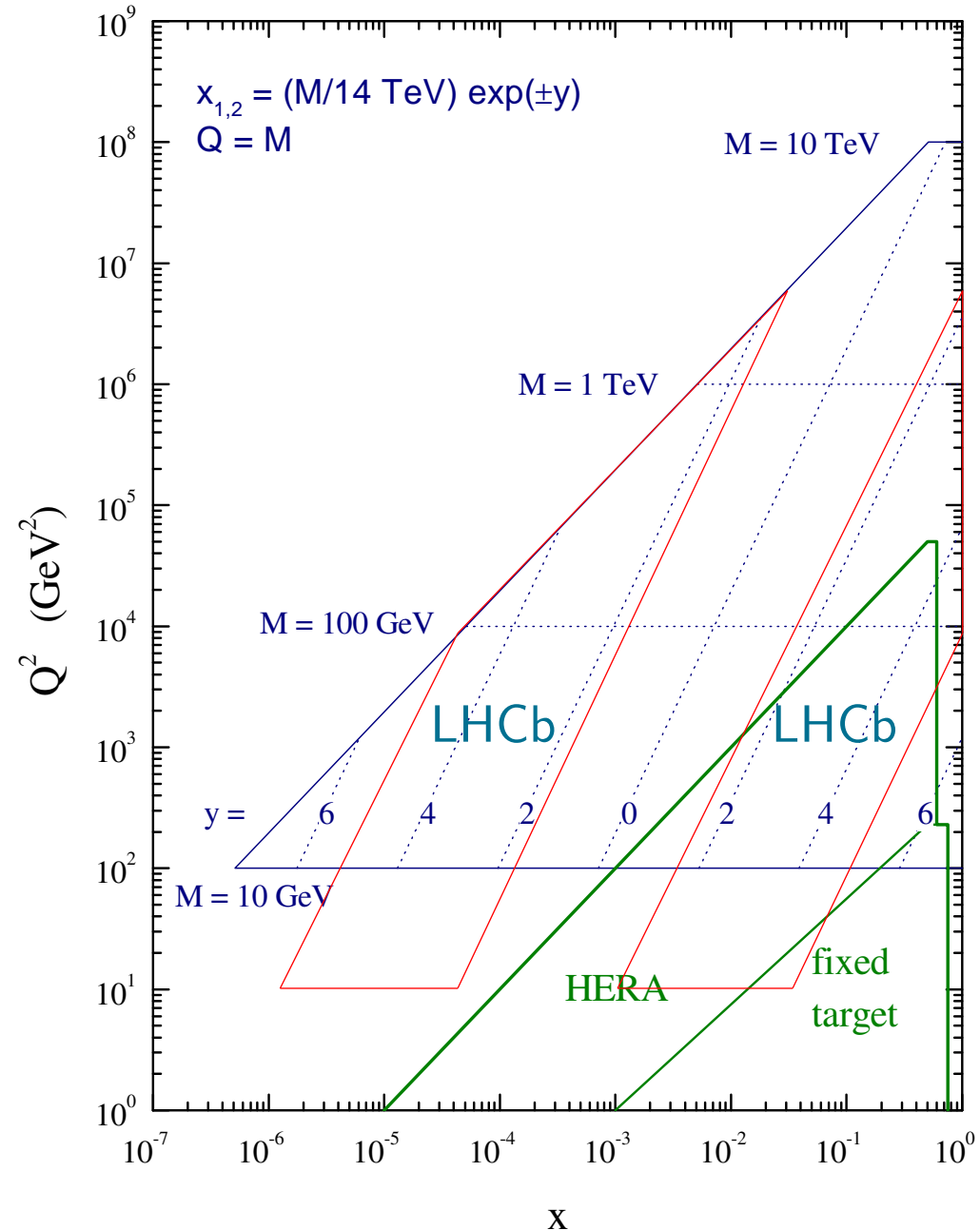
The kinematic range for particle production at the LHC is shown.

$$x_{1,2} = x_0 \exp(\pm y), \quad x_0 = \frac{M}{\sqrt{s}}.$$

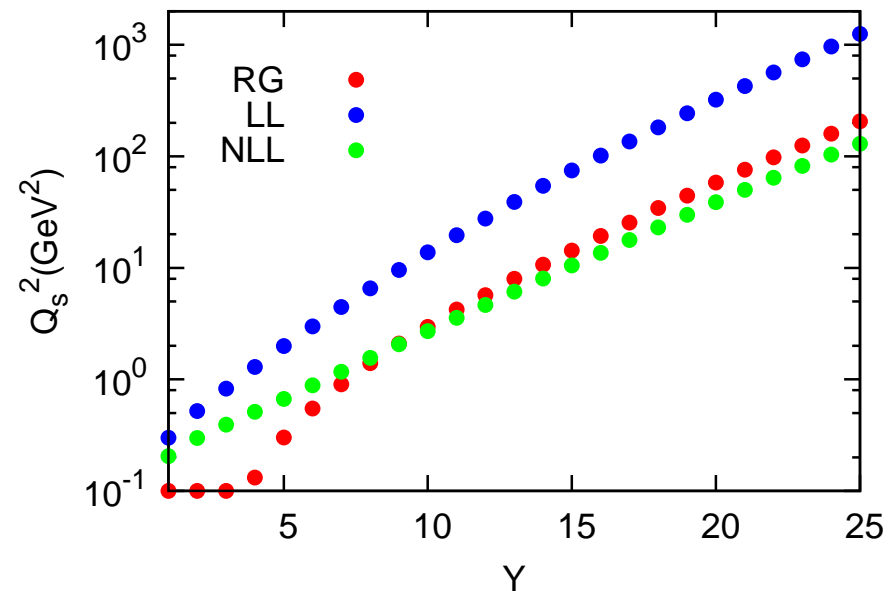
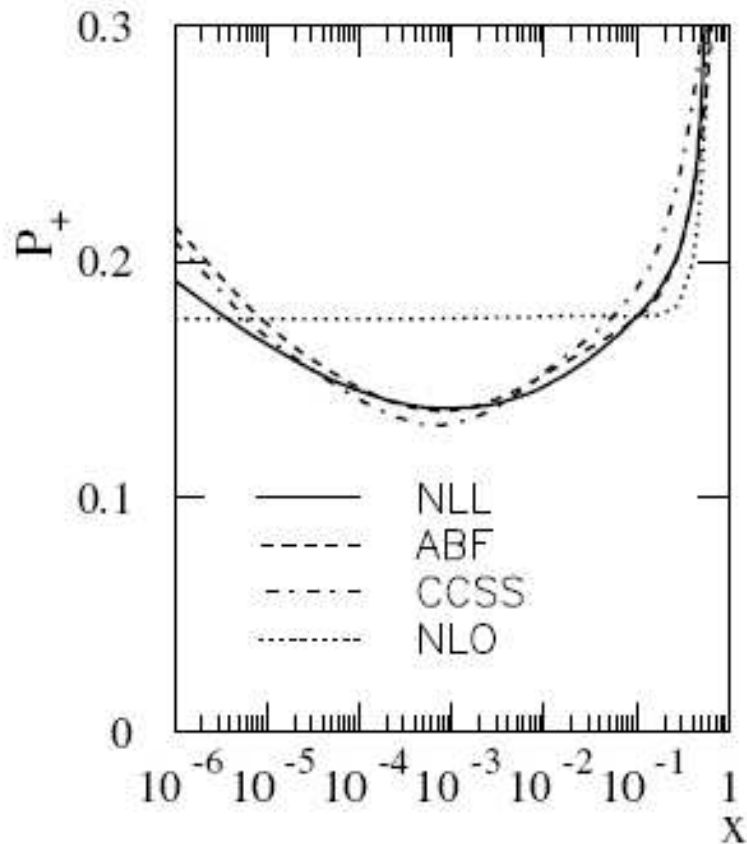
Smallish $x \sim 0.001 - 0.01$ parton distributions therefore vital for understanding the standard production processes at the LHC, and must trust QCD evolution from lower scales.

However, even smaller (and higher) x required when one moves away from zero rapidity, e.g. when calculating total cross-sections.

LHC parton kinematics



Some fits to new combined [HERA](#) structure function data using saturation inspired models. Seems fairly successful. But not necessary.



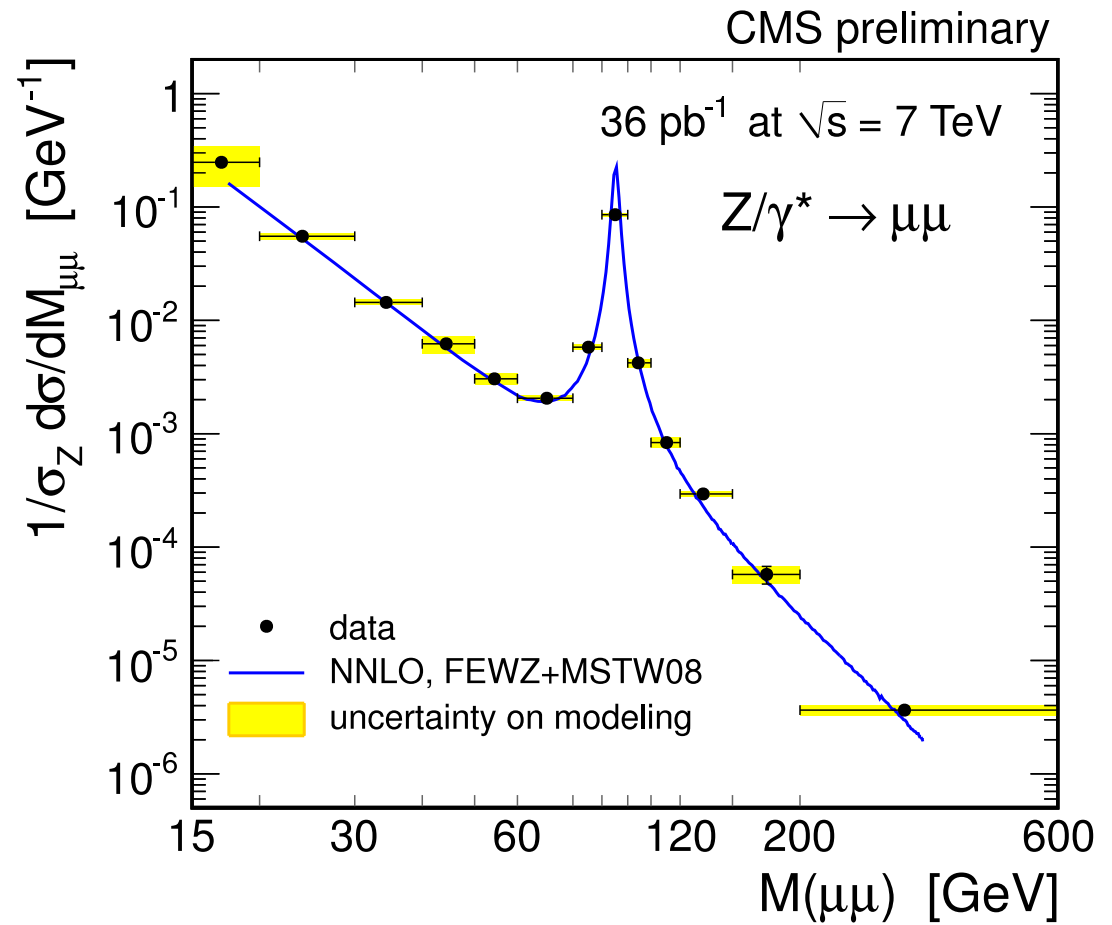
Agreed among all groups that full resummation of small- x logarithms leads to dip in splitting functions at fairly small x before rise at very small x .

Actually delays saturation compared to more naive calculations [Avsar et al.](#) Full resummation perhaps important before saturation for nucleon colliders.

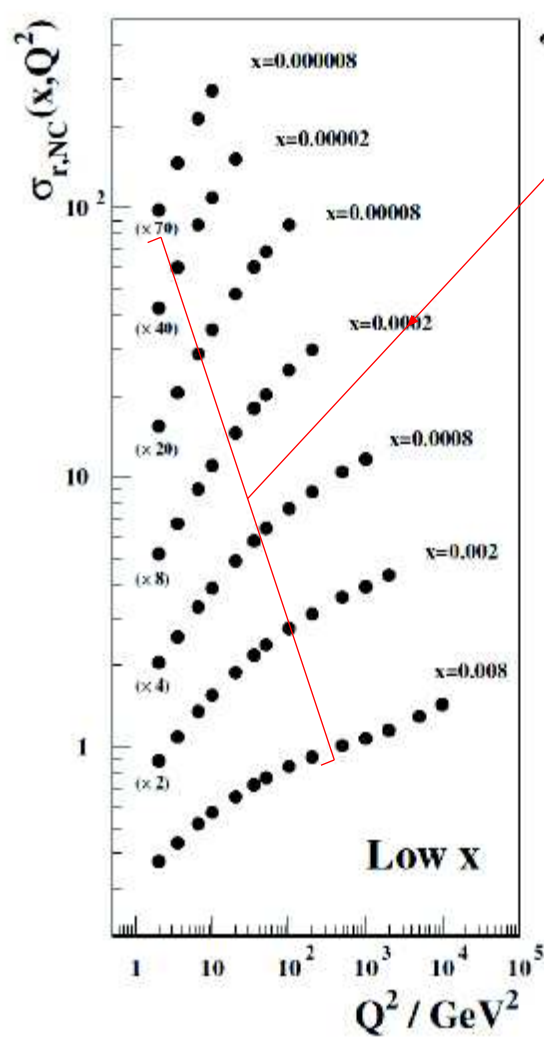
Small- x effects could be seen in low-mass Drell-Yan at LHC.

Good agreement with NNLO from CMS

Probably want lowest mass and high rapidity \rightarrow LHCb. Investigate in detail here.



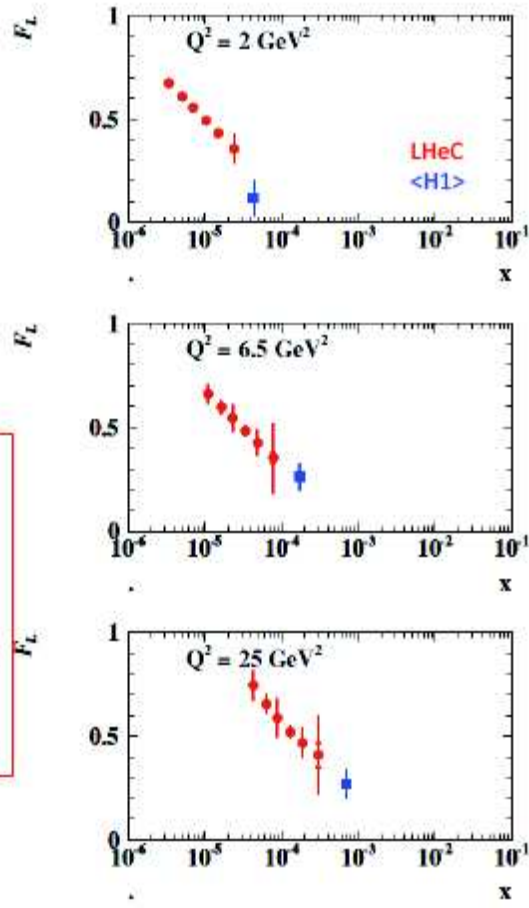
Perfect place to investigate this would be LHeC – (Klein CERN)



Gluon input

Hera limit with much larger errors

F_2 and F_L crucial to discover gluon saturation in ep in DIS region



Likely to see evidence of resummation and/or saturation (even in proton collisions). Might be difficult to disentangle the two.

Summary

We are obtaining a very complete set of processes calculated at **NLO**, and there is a move to automation. A few of the most standard processes are known at **NNLO** along with distributions. Threshold resummations often provide approximations to full **NNLO**. Full **NNLO** for hadronic jet rate and top cross section a priority.

Recently (very in one case) lost two high-energy colliders, **HERA** and the **Tevatron**, but many final results to come out still, from both.

Many interesting results appearing at the **LHC**, extending the kinematic range and starting to distinguish between PDFs, and test **QCD**. Generally need at least **NLO**. Monte Carlos interfaced to **NLO** or large multiplicity matrix elements much more. Differences to be understood better.

Just about everything can be described by a Monte Carlo tune, but not necessarily simultaneously. More investigation on universality desirable. More systematic investigation of Monte Carlo errors a next step?

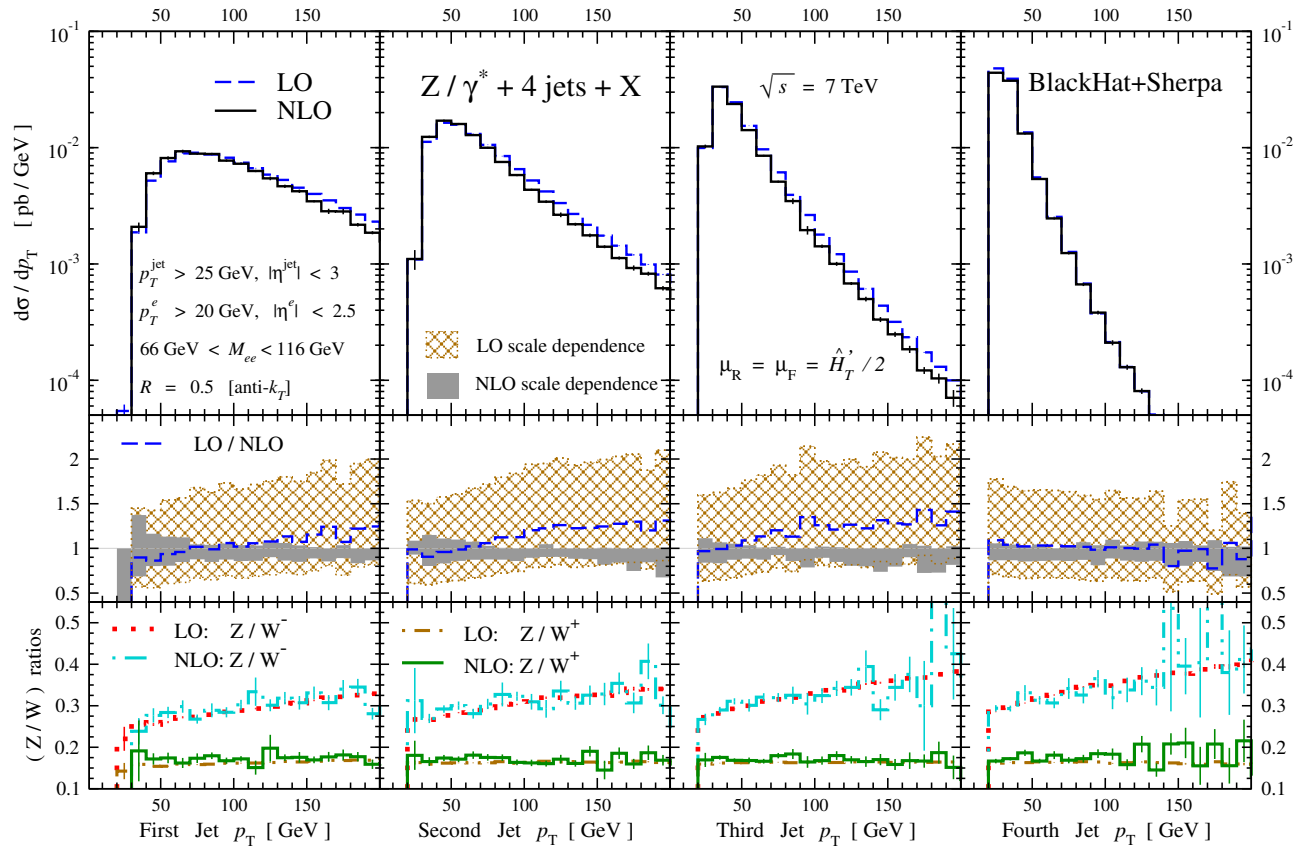
The **LHC** may address long-standing issues in perturbative **QCD**, like small- x resummation, saturation, and improve determinations of $\alpha_S(M_Z^2)$. Proposed lepton-proton colliders, e.g. **LHeC** would be a clean probe of these.

Backup Slides

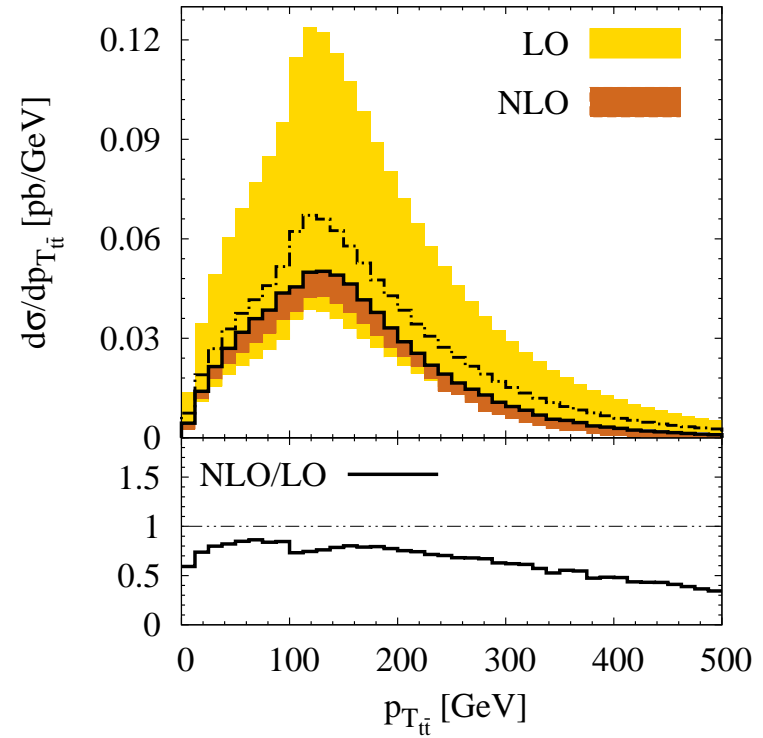
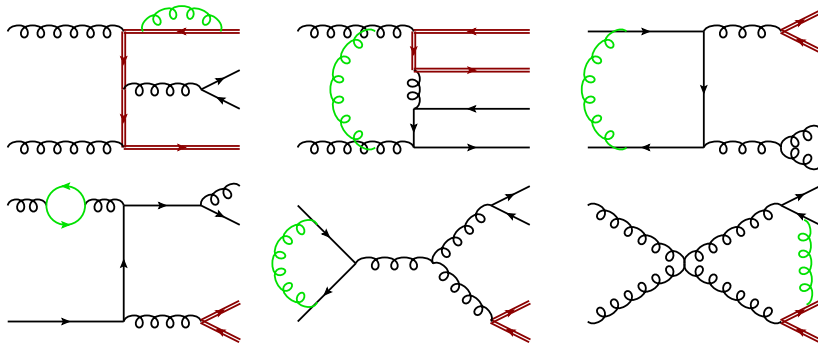
NLO Corrections.

And with even more final state particles $Z + jjjj$, Ita et al, ($W = jjjj$ also known).

Scale uncertainty much reduced.



Another example, $t\bar{t} + jj$, Bevilacqua et al



Progress at NNLO.

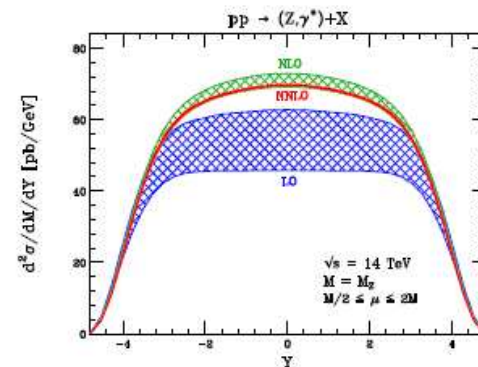
NNLO calculations for $2 \rightarrow 2$ processes

$$d\sigma = \sum_{i,j} \int \frac{d\xi_1}{\xi_1} \frac{d\xi_2}{\xi_2} f_i(\xi_1, \mu_F^2) f_j(\xi_2, \mu_F^2) d\hat{\sigma}_{ij}(\alpha_s(\mu_R), \mu_R, \mu_F)$$

$$d\hat{\sigma}_{ij} = d\hat{\sigma}_{ij}^{LO} + \left(\frac{\alpha_s(\mu_R)}{2\pi} \right) d\hat{\sigma}_{ij}^{NLO} + \left(\frac{\alpha_s(\mu_R)}{2\pi} \right)^2 d\hat{\sigma}_{ij}^{NNLO} + \mathcal{O}(\alpha_s^3)$$

Processes of interest

- ✓ $pp \rightarrow 2 \text{ jets}$
- ✓ $pp \rightarrow \gamma + \text{jets}$
- ✓ $pp \rightarrow \gamma\gamma$
- ✓ $pp \rightarrow V + \text{jet}$
- ✓ $pp \rightarrow t\bar{t}$
- ✓ $pp \rightarrow VV$
- ✓ $pp \rightarrow H + \text{jet}$
- ✓ ...



Massively reduced theoretical error

Anastasiou, Dixon, Melnikov, Petriello (04)

Glover St Andrews 2011.

Applications to LHC processes

- ✓ All relevant matrix elements for $pp \rightarrow 2 \text{ jet}$ and $pp \rightarrow V + 1 \text{ jet}$ processes available for some time
- ✓ Can expect to have parton-level NNLO predictions for $pp \rightarrow 2 \text{ jet}$ and $pp \rightarrow V + 1 \text{ jet}$ in next couple of years
- ✓ Hope for significant reduction in theory (renormalisation scale/factorisation scale) dependence
- ✓ LHC already has increased dynamic range for jet studies - rapidity, transverse energy.
- ✓ Combined with excellent experimental jet energy scale uncertainty, there is the opportunity for improved measurements of
 - ✓ Parton distributions
 - ✓ Strong coupling
 - ✓ Internal structure of the jet
 - ✓ Rapidity gaps between the jets

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NLO Monte Carlos

Available processes*

Process	POWHEG			MC@NLO	
	POWHEG-BOX	HERWIG++	SHERPA	MC@NLO	aMC@NLO
$e^+e^- \rightarrow jj$	X	✓	✓	X	X
DIS	X	✓	✓	✓	X
$pp \rightarrow W/Z$	✓	✓	✓	✓	X
$pp \rightarrow H$ (GF)	✓	✓	✓	✓	X
$pp \rightarrow V + H$	X	✓	✓	✓	X
$pp \rightarrow VV$	X	✓	✓	✓	X
VBF	✓	✓	in prep.	X	X
$pp \rightarrow Q\bar{Q}$	✓	X	X	✓	X
$pp \rightarrow Q\bar{Q} + j$	✓	X	X	X	X
single-top	✓	X	X	✓	X
$pp \rightarrow V + j$	✓	X	in prep.	X	X
$pp \rightarrow V + jj$	in prep.	X	in prep.	X	X
$pp \rightarrow H + j$ (GF)	X	X	in prep.	X	X
$pp \rightarrow H + t\bar{t}$	✓	X	X	X	✓
$pp \rightarrow W^+W^+jj$	✓	X	X	X	X
$pp \rightarrow V + b\bar{b}$	✓	X	in prep.	X	✓
diphotons	?	✓	in prep.	X	X
dijets	✓	X	in prep.	X	X

*Table includes SM processes presented so far. Automated codes and toolkits can, in principle, be used for any process.

Schönherr St Andrews 2011.

Pros and Cons

POWHEG

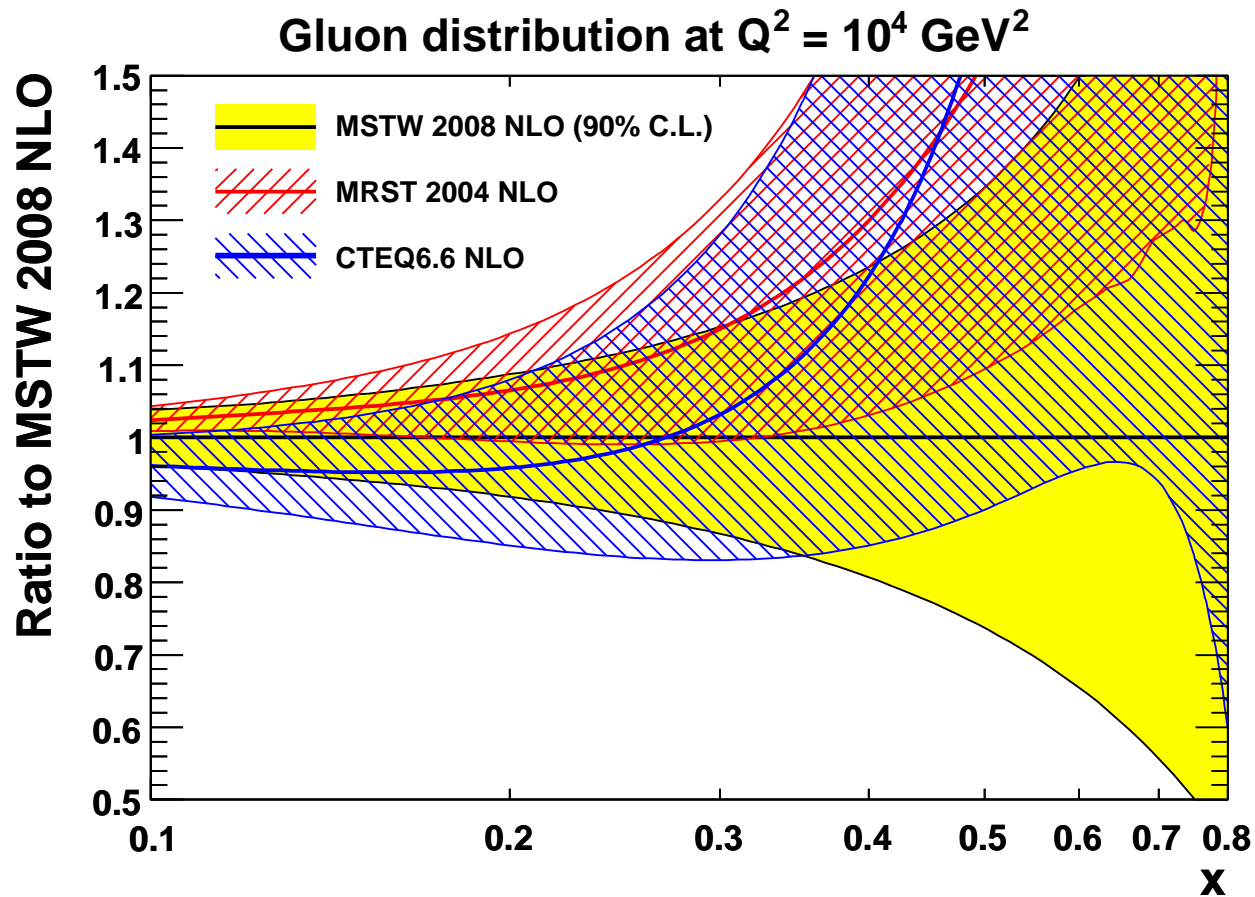
- Positive weights.
- Implementation doesn't depend on the shower algorithm.
- Needs changes to shower algorithm for non- p_T ordered showers.
- Differs from shower and NLO results, but changes can be made to give NLO result at large p_T .

MC@NLO

- Negative weights
- Implementation depends on the specific shower algorithm used.
- No changes to parton shower.
- Reduces to the exact shower result at low p_T and NLO result at high p_T

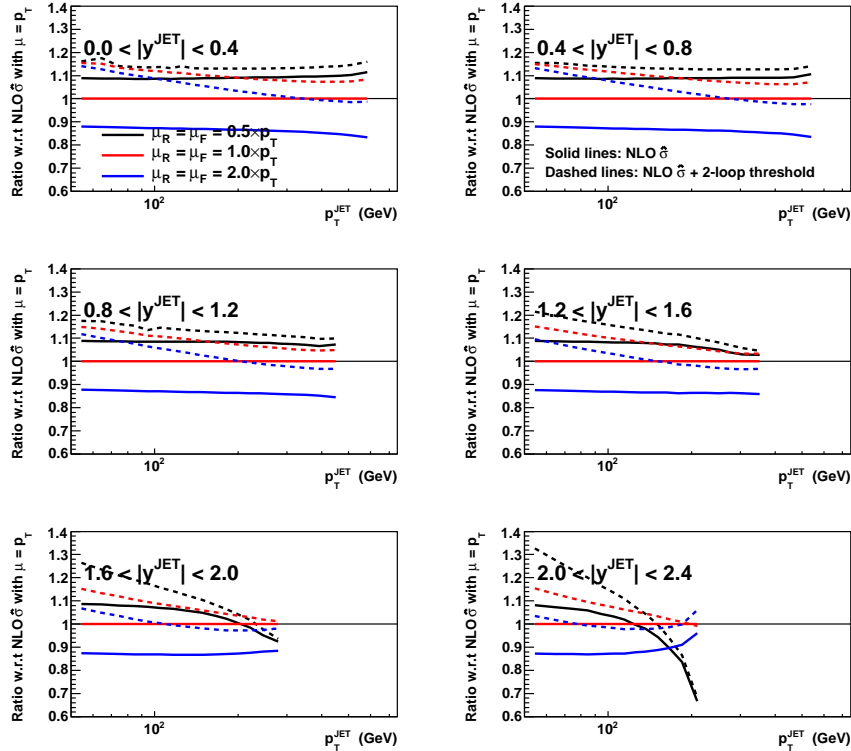
Richardson Cosener's House 2011

From personal experience, fitting to Run II **Tevatron** high- E_T jet data, with improved jet algorithms (k_T algorithm for **CDF**) results in a significant change in the gluon.

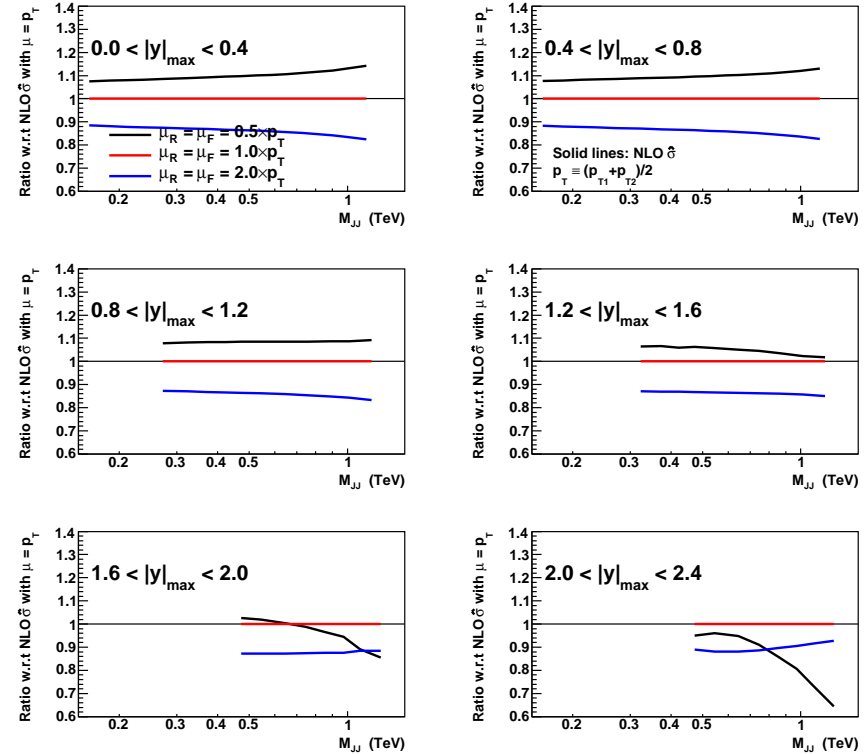


Due to improvements in algorithms?

$\text{D}\phi$ Run II inclusive jet data (cone, $R = 0.7$) (Ratio w.r.t. NLO $\hat{\sigma}$ with $\mu = p_T$ using MSTW08 NNLO PDFs)



$\text{D}\phi$ Run II dijet data (cone, $R = 0.7$) (Ratio w.r.t. NLO $\hat{\sigma}$ with $\mu = p_T$ using MSTW08 NNLO PDFs)

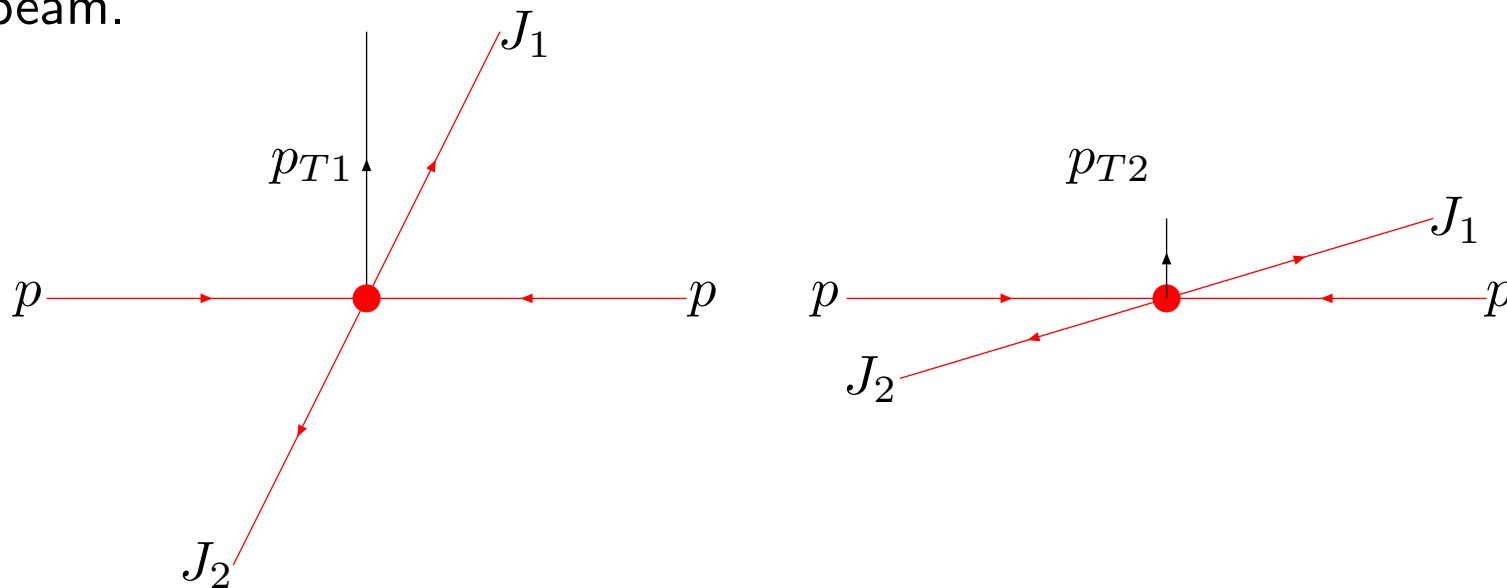


Shape of corrections as function of p_T at NLO and also at approx. NNLO in inclusive case. Problem at highest p_T and rapidity even for inclusive jets.

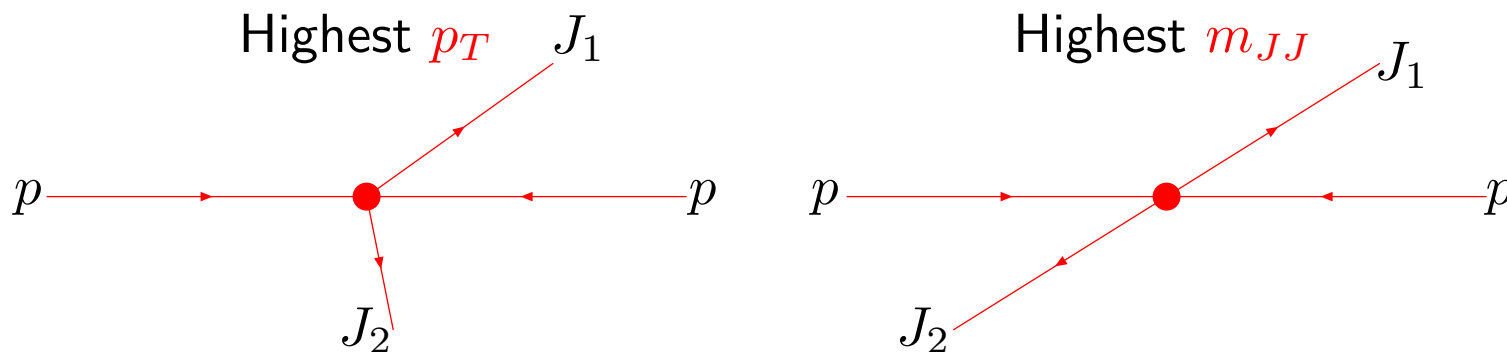
NNLO uses threshold (Kidonakis and Owens) approx. for Tevatron jets (see also de Florian and Vogelsang).

NNLO approximation aids stability – always worst at high- p_T i.e. high- x . Includes large $\ln(p_T/\mu)$ terms predicted by renormalisation group.

Consider two dijet processes with similar energy jets, but with one at much smaller angle to beam.

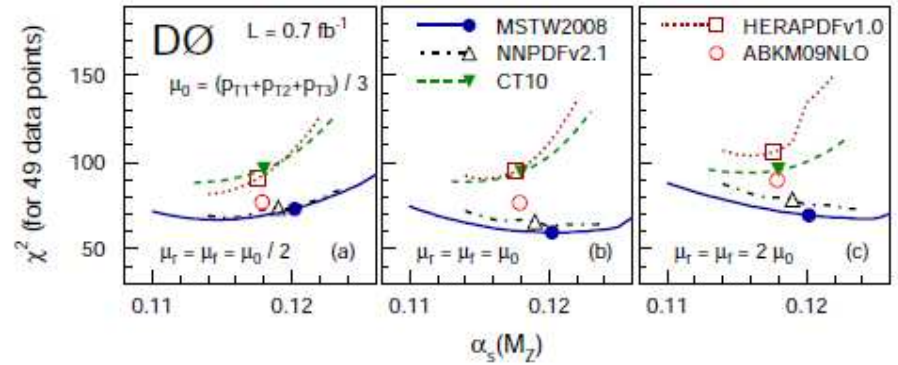
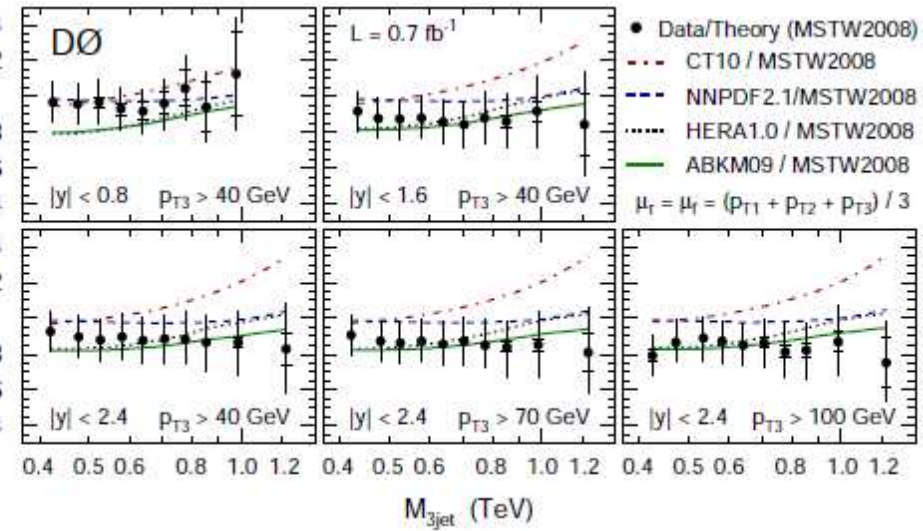


Generally use scale based entirely on p_T . Is the second event really that much less hard than the first?



In first case one x very large other quite small, in second both x values very large. In both cases p_T not too large.

Recent results from D0 on three jets cross sections.



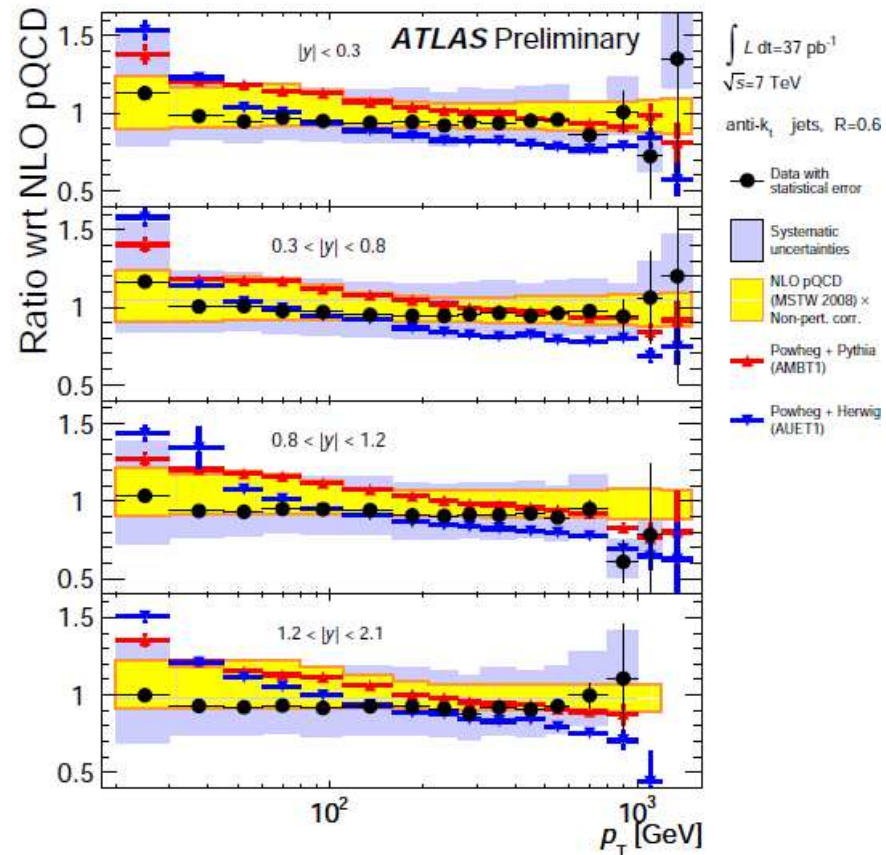
Seems like an excellent way to present significance of results. Groups can then study effects on central values uncertainties (consistency) *etc.*

TABLE II: χ^2 values between data and theory for different PDF parametrizations in the order of decreasing χ^2 , for all 49 data points.

PDF set	Default $\alpha_s(M_Z)$	χ^2 at $\mu_r = \mu_f = \mu_0$ for default $\alpha_s(M_Z)$	χ^2_{minimum}
HERAPDFv1.0	0.1176	95.1	81.7
CT10	0.1180	94.5	88.2
ABKM09NLO	0.1179	76.5	76.5
NNPDFv2.1	0.1190	65.9	63.3
MSTW2008NLO	0.1202	59.5	59.5

Inclusive Jets: NLOJET++ vs. PowHeg

- A significant difference between NLOJET++, PowHeg+Pythia and PowHeg+Herwig was observed
- NLO Matrix Element in good agreement between NLOJET++ and PowHeg
- Indication of uncertainties due to non-perturbative effects?



However, use of **POWHEG** leads to a big variation compared to standard **NLO**, and a big variation depending on Monte Carlo tune.

Implications for PDFs.

Values of $\alpha_S(M_Z^2)$ from PDF fits.

Converging on general agreement that the **NNLO** values of α_S are **0.0002 – 0.0003** smaller than the **NLO** values of α_S ?

MSTW08 – $\alpha_S(M_Z^2) = 0.1202 \rightarrow 0.1171$.

ABKM09 – $\alpha_S(M_Z^2) = 0.1179 \rightarrow 0.1135$.

GJR/JR – $\alpha_S(M_Z^2) = 0.1145 \rightarrow 0.1124$.

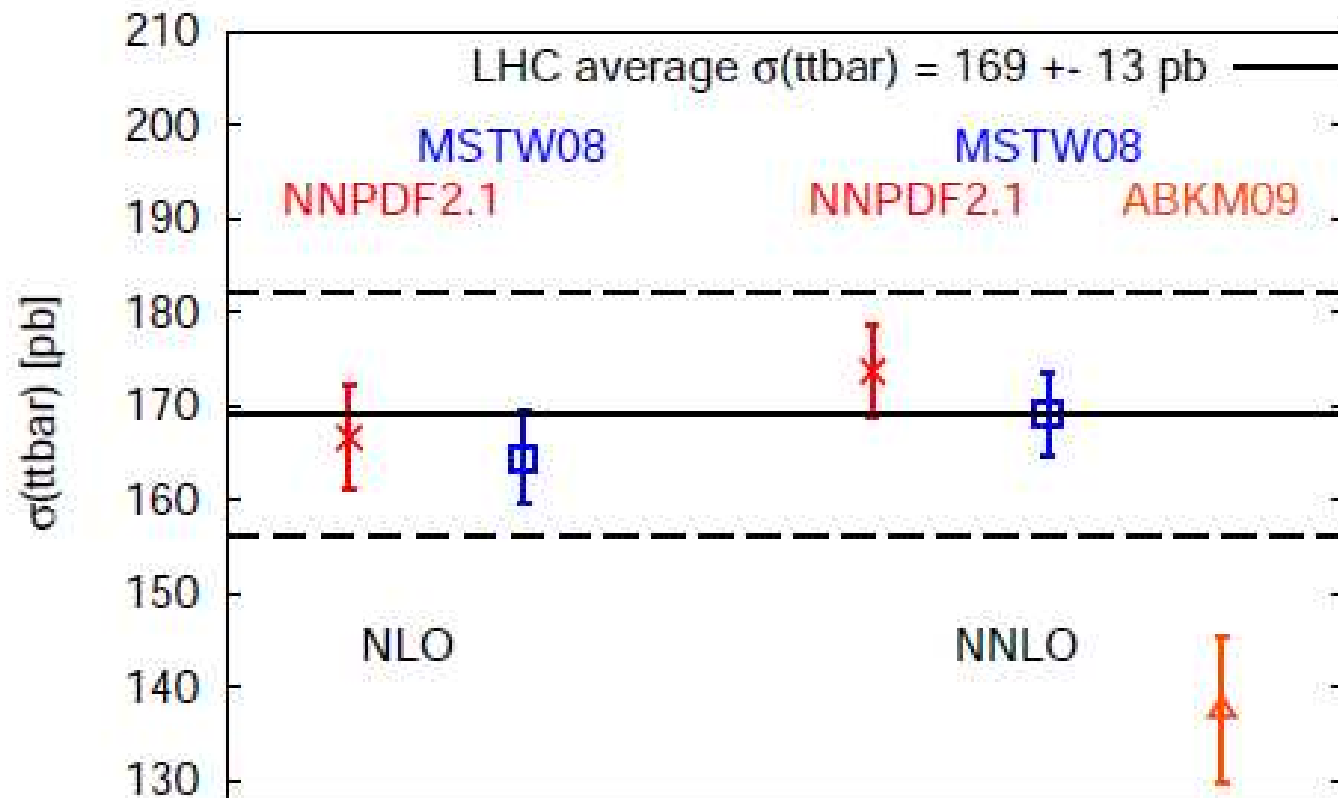
NNPDF2.1 – $\alpha_S(M_Z^2) = 0.1191 \rightarrow 0.1174$ (prelim).

CT10.1 – $\alpha_S(M_Z^2) = 0.1196 \rightarrow 0.1180$ (both prelim – PDF4LHC, DESY July).

HERAPDF1.6 – $\alpha_S(M_Z^2) = 0.1202$ at **NLO** and general preference for ~ 0.1176 at **NNLO**.

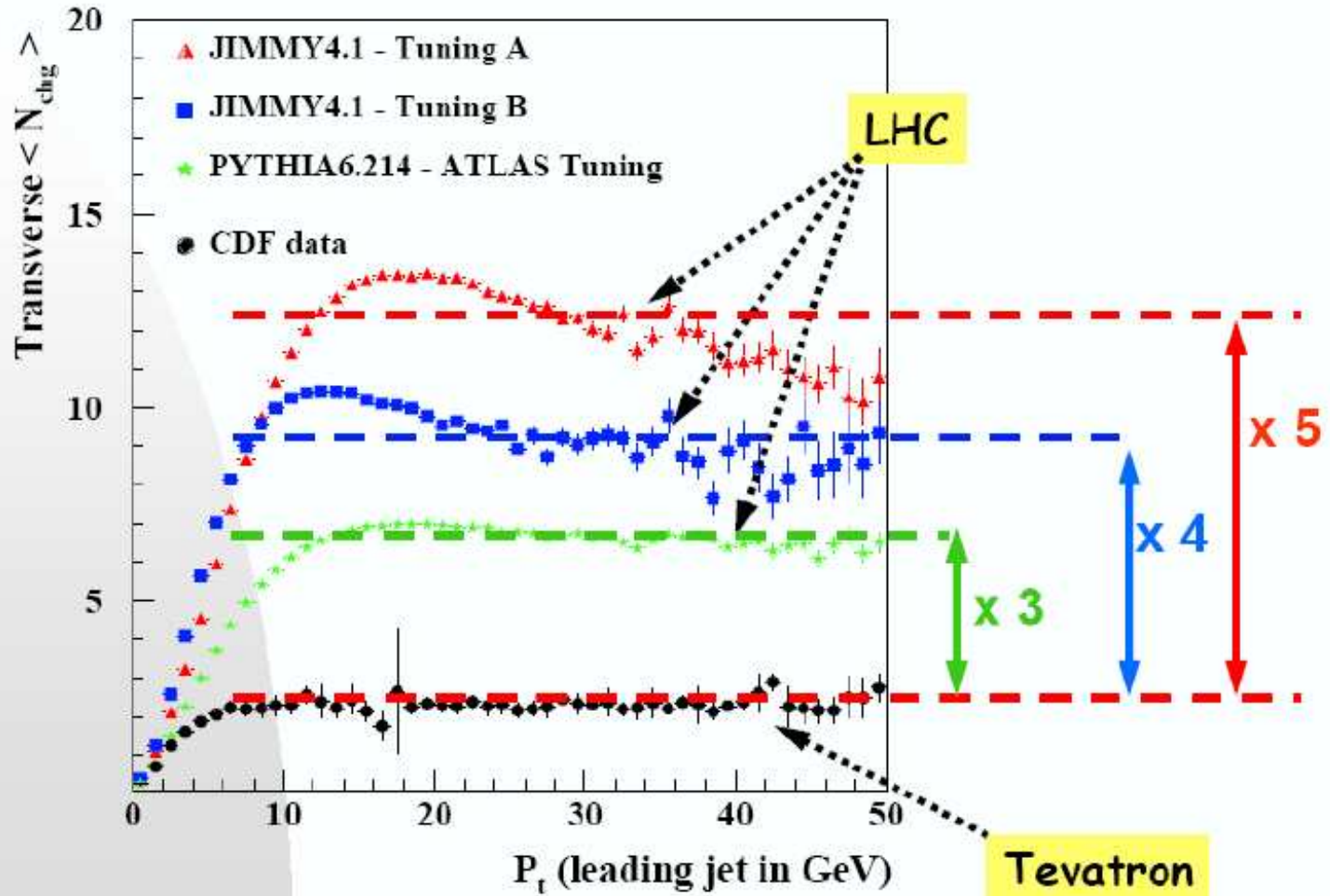
Central values differ far more than **NLO** \rightarrow **NNLO** trend.

LHC 7 TeV, HATHOR, $m_t = 172$ GeV



NNPDF NNLO prediction slightly bigger than MSTW, but use $\alpha_S = 0.119$ – not preferred value? General very good agreement

LHC predictions: JIMMY4.1 Tunings A and B vs. PYTHIA6.214 – ATLAS Tuning (DC2)

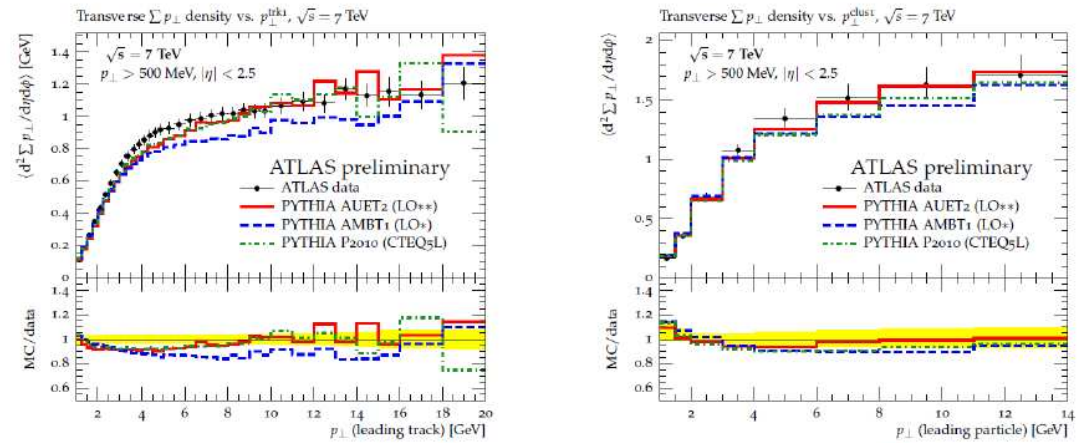


A. M. Moraes

Minimum-bias and the Underlying Event at the LHC

5th November 2004

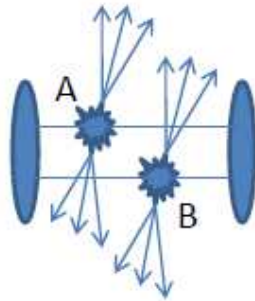
NEW PYTHIA 6 TUNE TO ATLAS DATA: AUET2



- Improvement w.r.t. AMBT1, “turn-over region” undershot
- Similar agreement for track- and calorimeter based UE measurements

However, to be more theoretically correct multi-parton distribution functions should be used.

Cross Section for DPS



Assuming only the factorisation of the hard processes A and B, the DPS cross section may be written as:

$$\sigma_D^{(A,B)} = \frac{m}{2} \sum_{i,j,k,l} \int \overbrace{\Gamma_n^{ik}(x_1, x_2, \mathbf{b}; Q_A, Q_B) \Gamma_n^{jl}(x'_1, x'_2, \mathbf{b}; Q_A, Q_B)}^{\text{Two-parton generalised PDF (2pGPD)}} \times \underbrace{\hat{\sigma}_U^A(x_1, x'_1) \hat{\sigma}_{kl}^B(x_2, x'_2)}_{\text{Parton level cross sections}} dx_1 dx'_1 dx_2 dx'_2 d^2 \mathbf{b}$$

The vector \mathbf{b} in the 2pGPDs corresponds to the vector separation in transverse space between the two partons described by the 2pGPD.

DPS differs from SPS in that the cross section may not naturally be expressed in terms of PDFs depending only on x arguments. The 2pGPDs in the DPS cross section must share a common \mathbf{b} in order that both pairs of partons can meet and interact – one cannot integrate independently over the transverse separation arguments of each PDF and obtain PDFs depending only on x arguments, as one can in the SPS case.

4

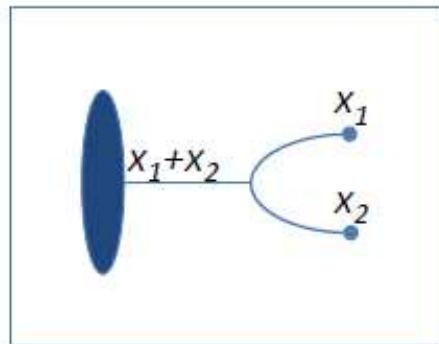
Gaunt St Andrews 2011

Pictorial Representation of the dDGLAP equation

$$\frac{dD_h^{j_1 j_2}(x_1, x_2; t)}{dt} = \frac{\alpha_s(t)}{2\pi} \left[\sum_{j'_1} \int_{x_1}^{1-x_2} \frac{dx'_1}{x'_1} D_h^{j'_1 j_2}(x'_1, x_2; t) P_{j'_1 \rightarrow j_1} \left(\frac{x_1}{x'_1} \right) \right. \\ \left. + \sum_{j'_2} \int_{x_2}^{1-x_1} \frac{dx'_2}{x'_2} D_h^{j_1 j'_2}(x_1, x'_2; t) P_{j'_2 \rightarrow j_2} \left(\frac{x_2}{x'_2} \right) \right]$$

$$\left[+ \sum_{j'} D_h^{j'}(x_1 + x_2; t) \frac{1}{x_1 + x_2} P_{j' \rightarrow j_1 j_2} \left(\frac{x_1}{x_1 + x_2} \right) \right]$$

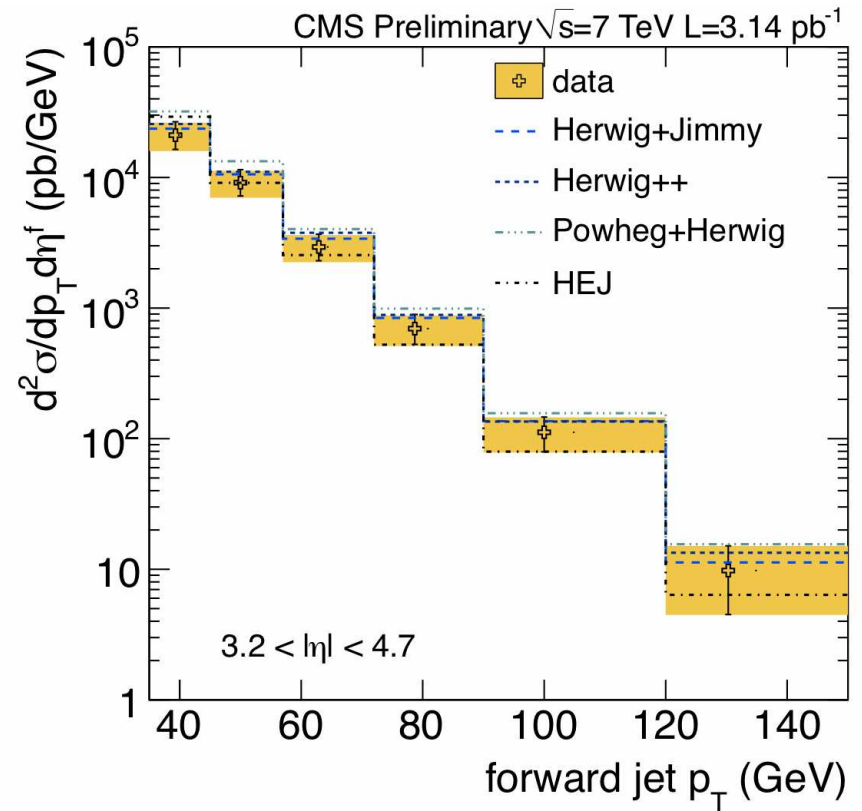
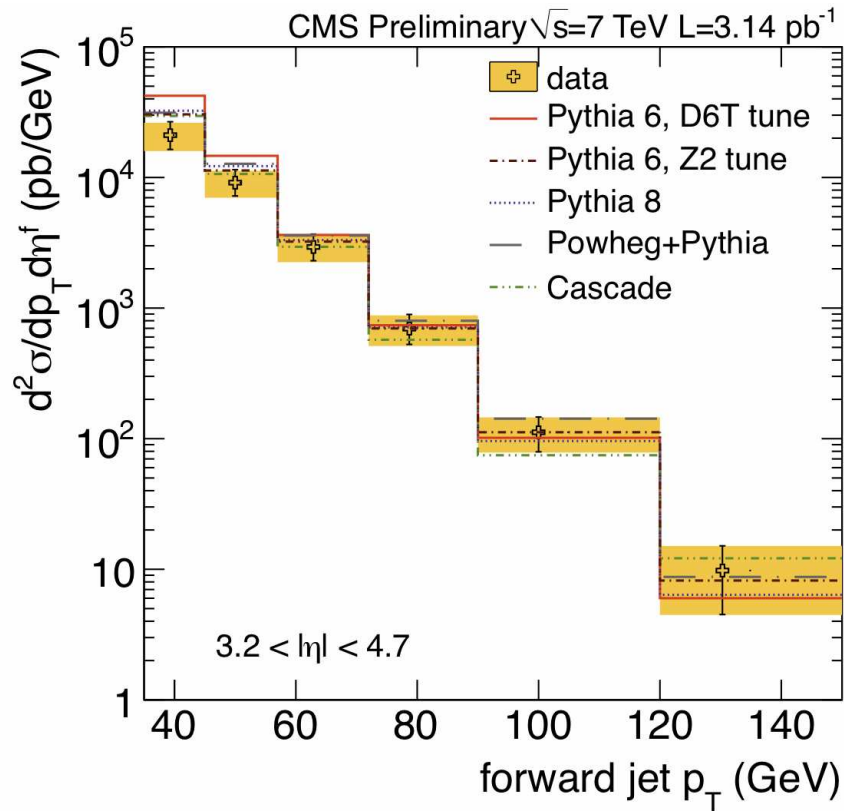
'sPDF feed' term



Gaunt St Andrews 2011

Production of one central jet and one forward jet.

Guaranteed imbalance of partons, one at small x .



Some fits to new combined HERA structure function data using saturation inspired models [Albacete et al.](#)

Seems fairly successful, as before. But not necessary.

