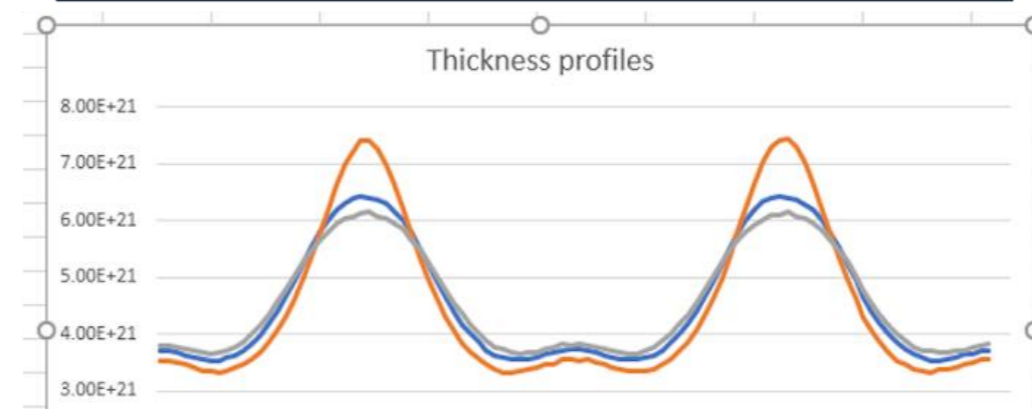
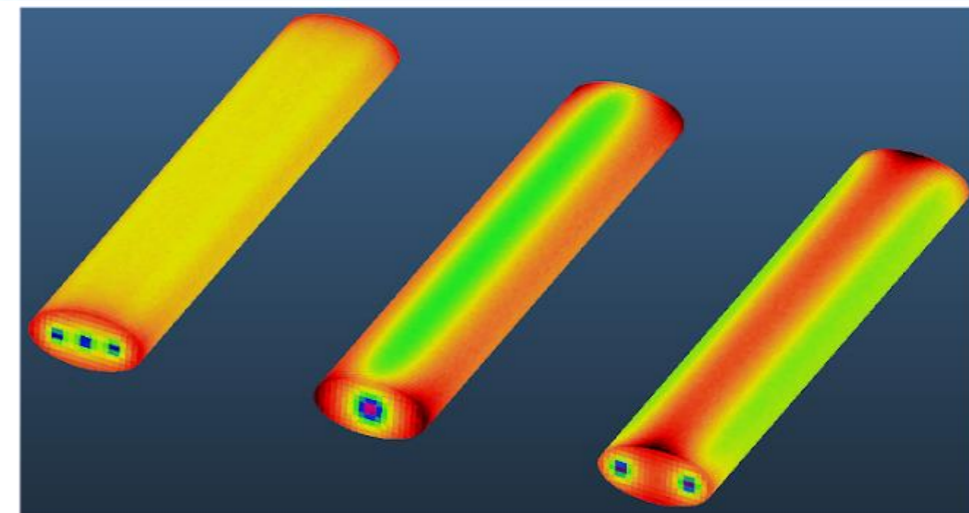
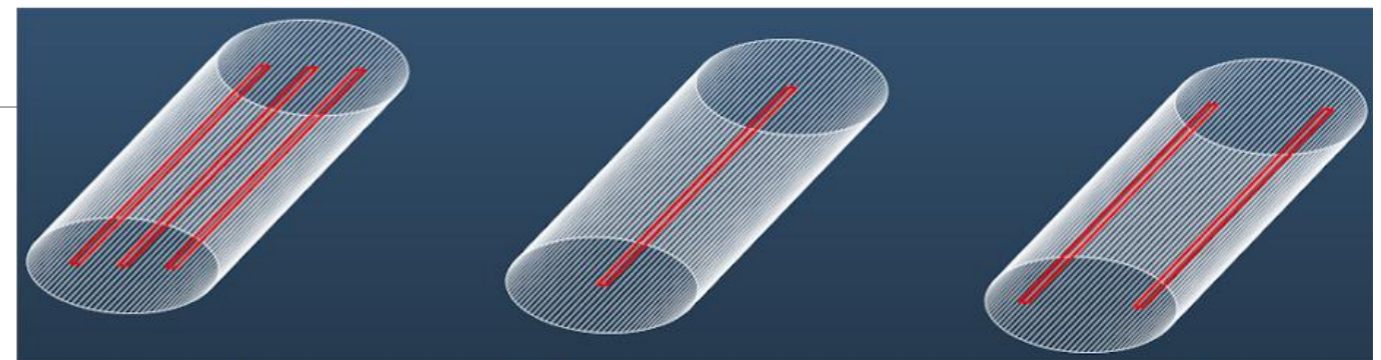
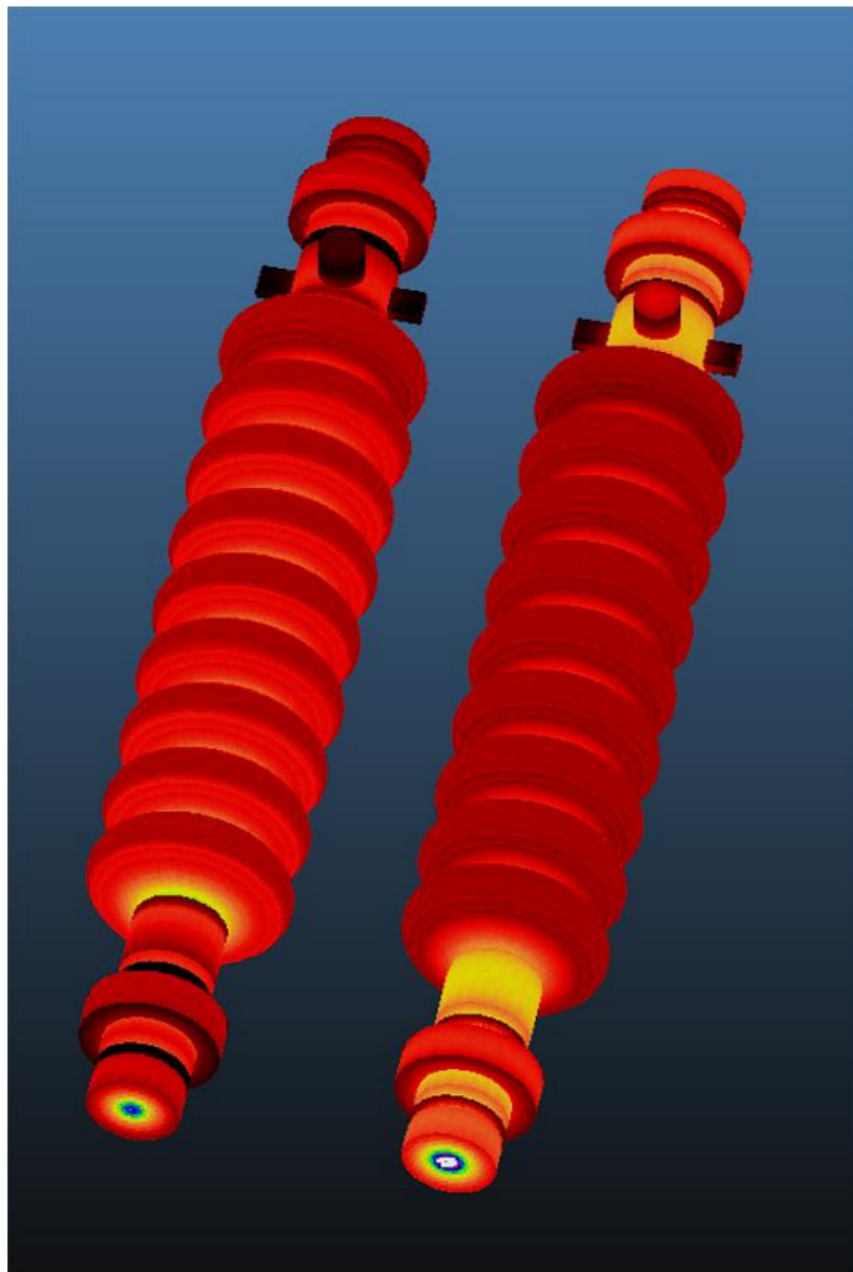
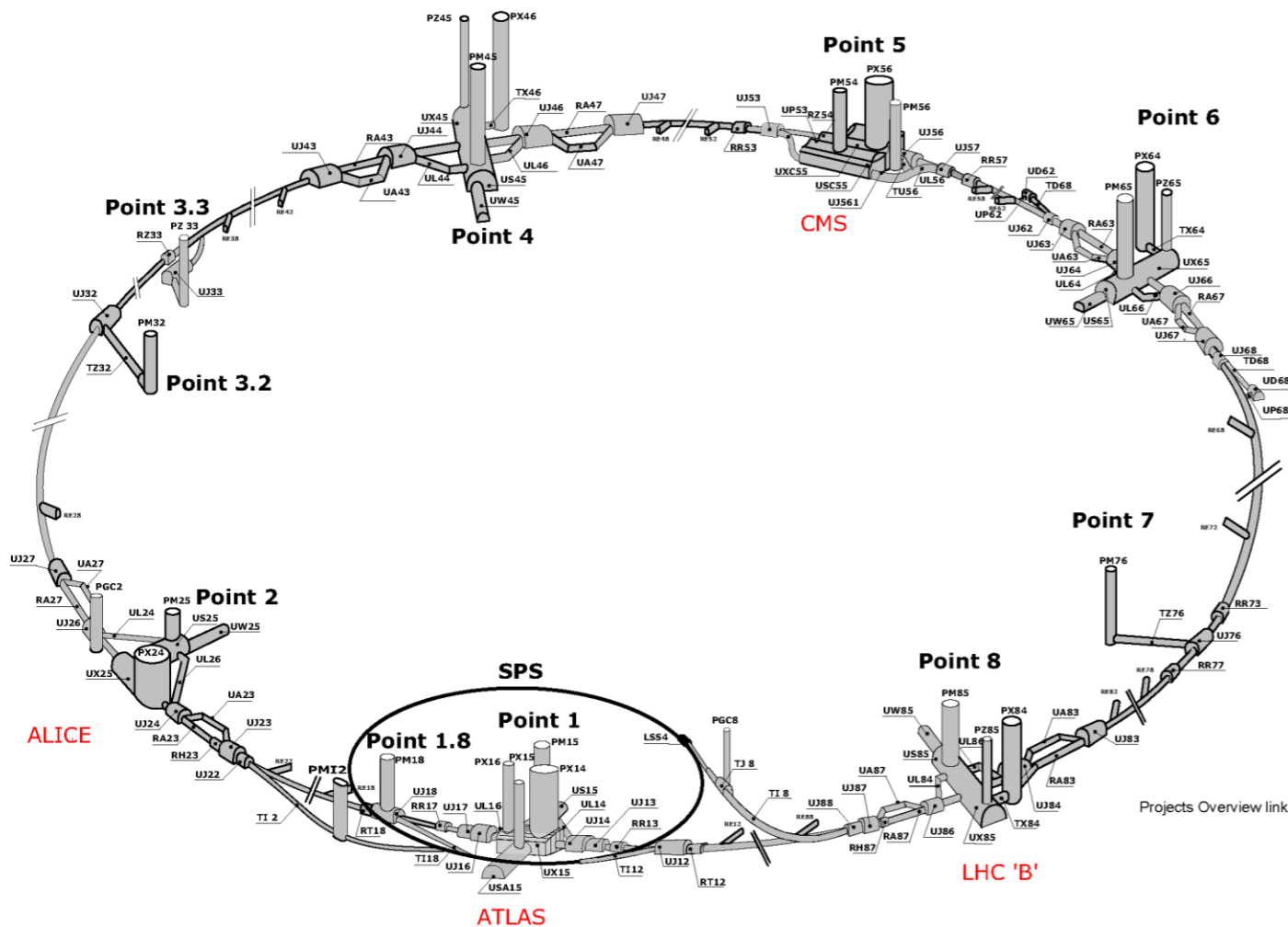


# Gas simulations with Monte Carlo methods



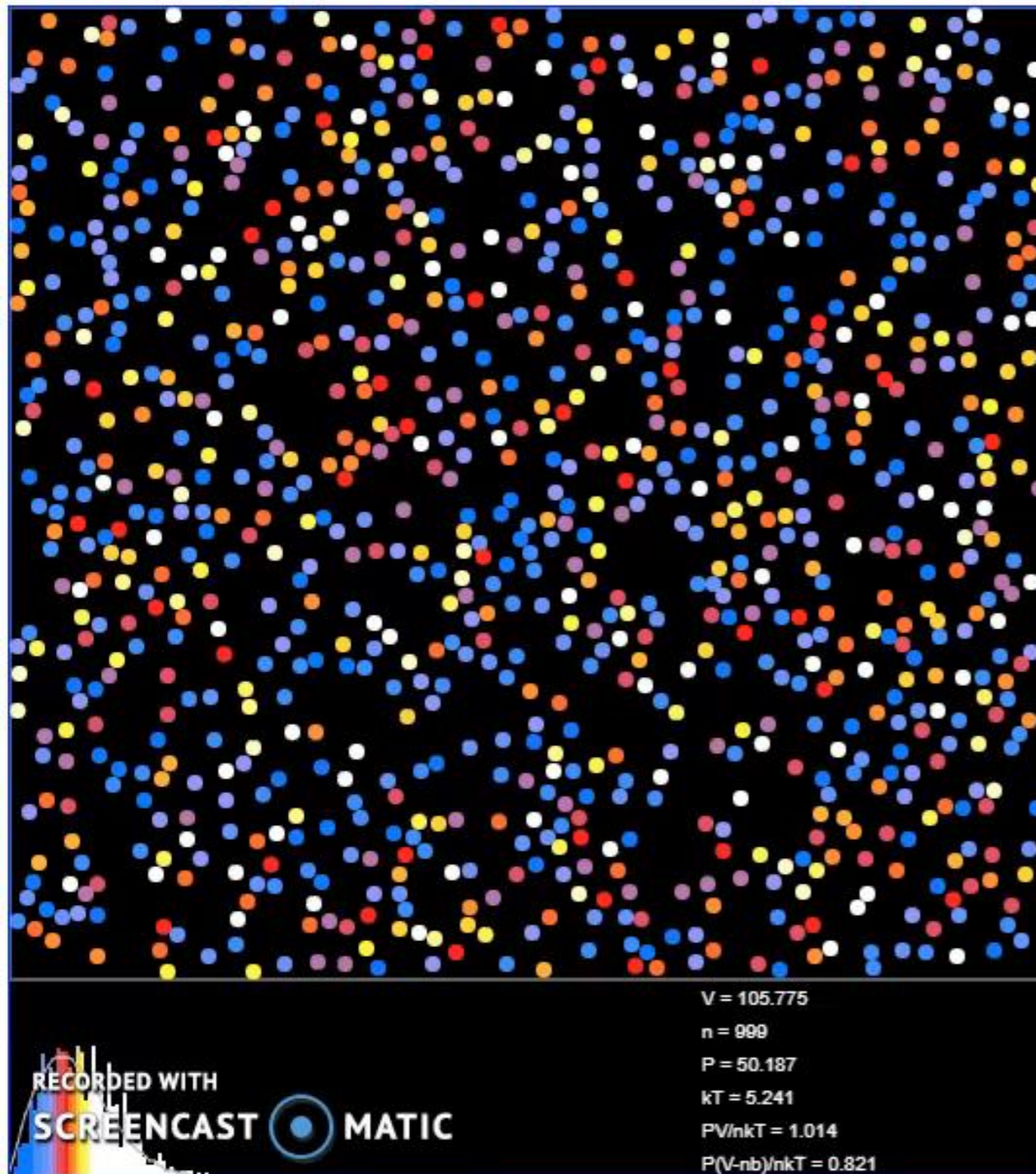
PBC workshop, CERN  
6 April 2022 - Marton Ady

# The problem



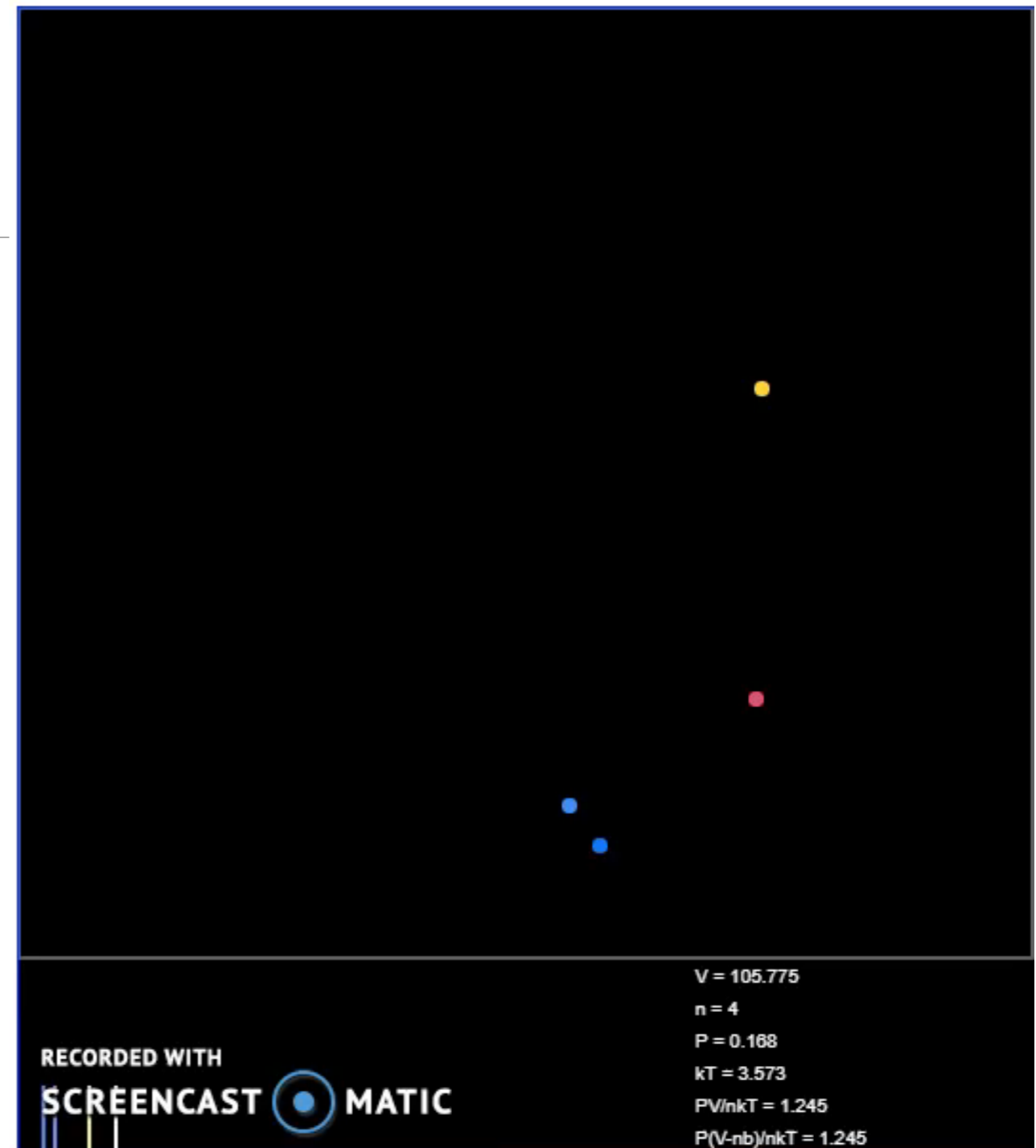
LHC: Pressure below  $1\text{E-}9$  mbar ( $0.000000\ 000001$  \* atmospheric)

## High pressure: fluid dynamics



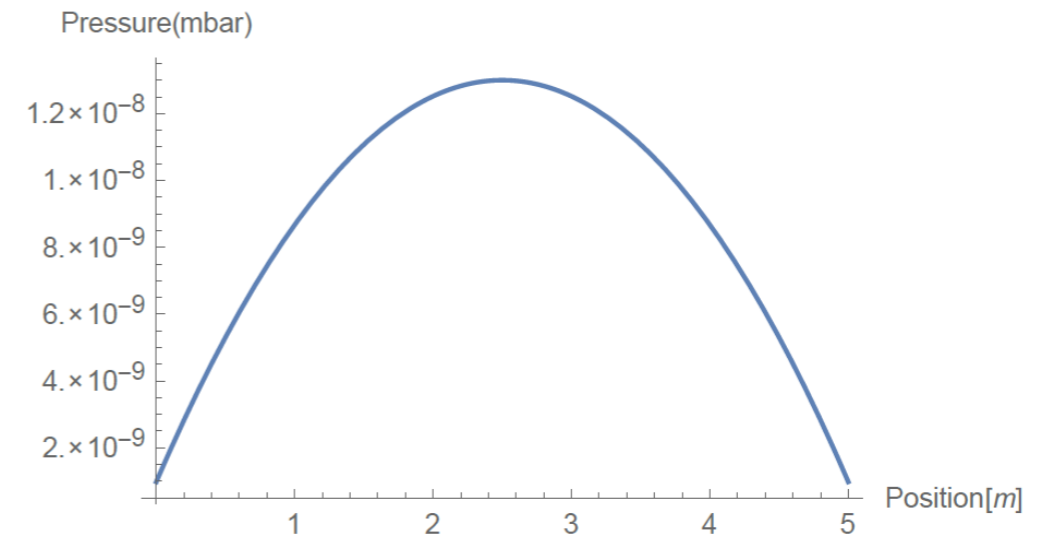
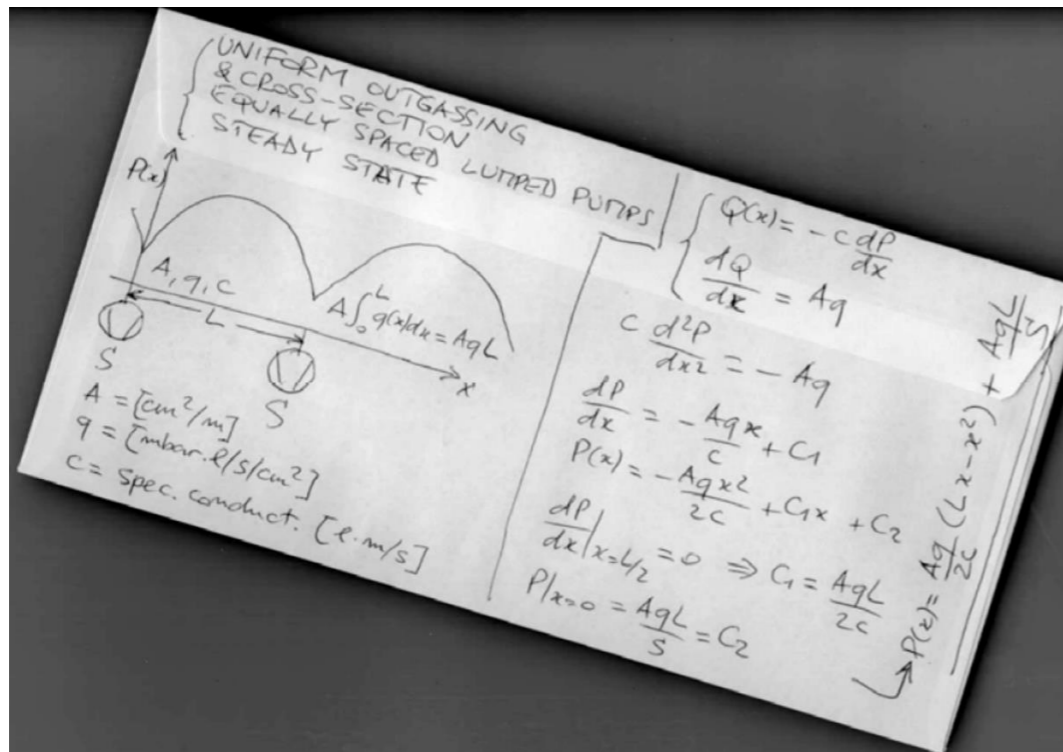
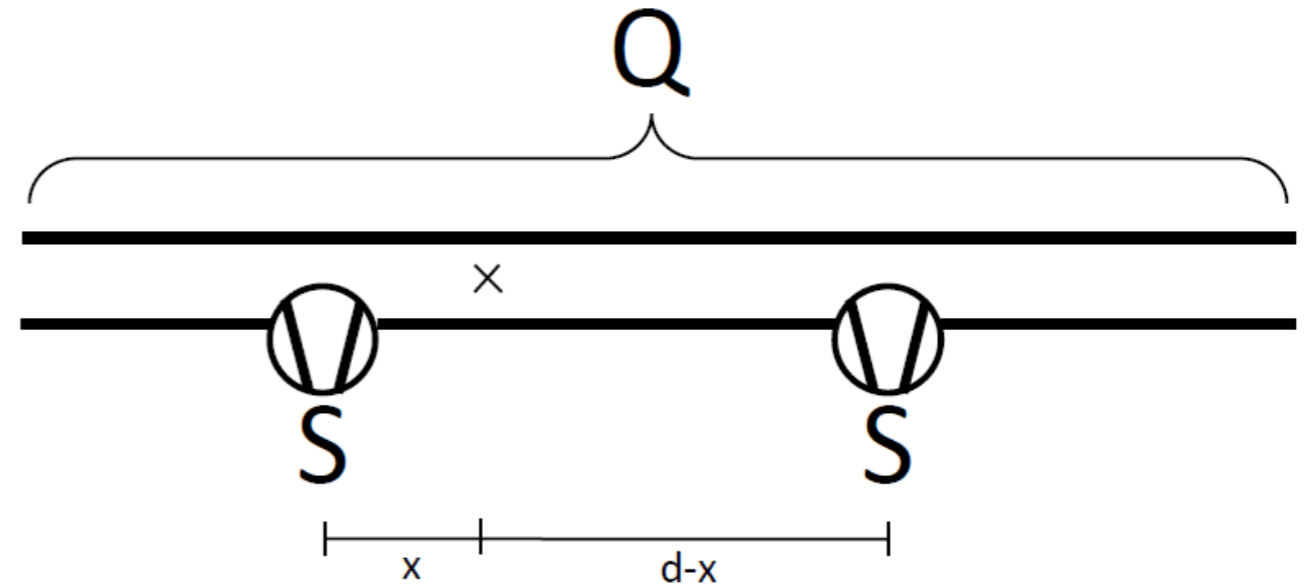
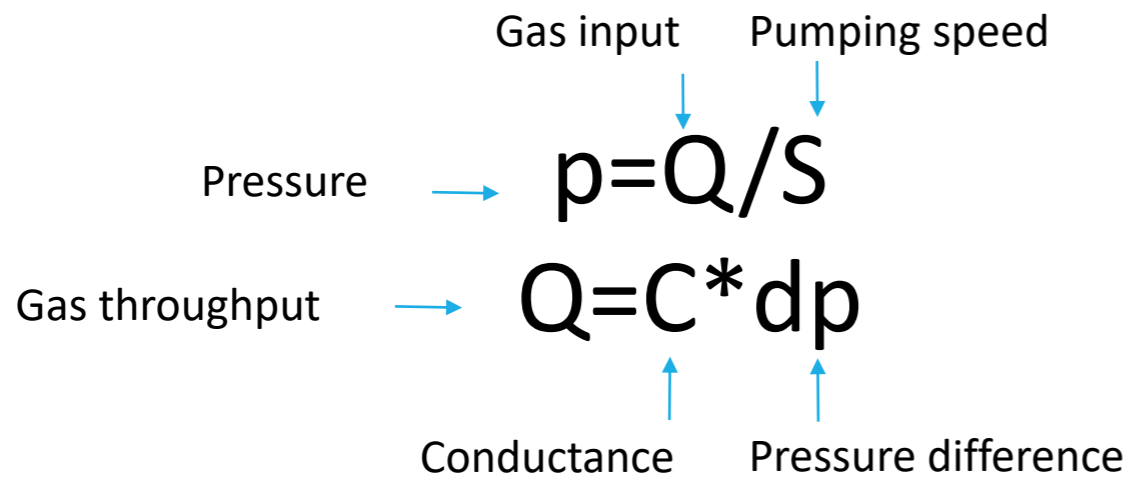
Pumping by **suction**

## High vacuum: random walk



Pumping by **capture**

# Analytic methods



# Difficulty: Conductance

Table 1.2 Equations for calculating the angular coefficients







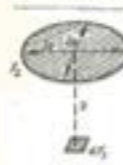
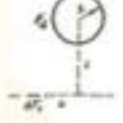

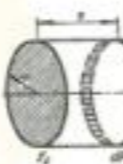
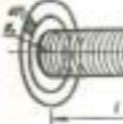
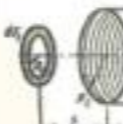
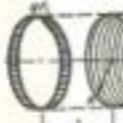
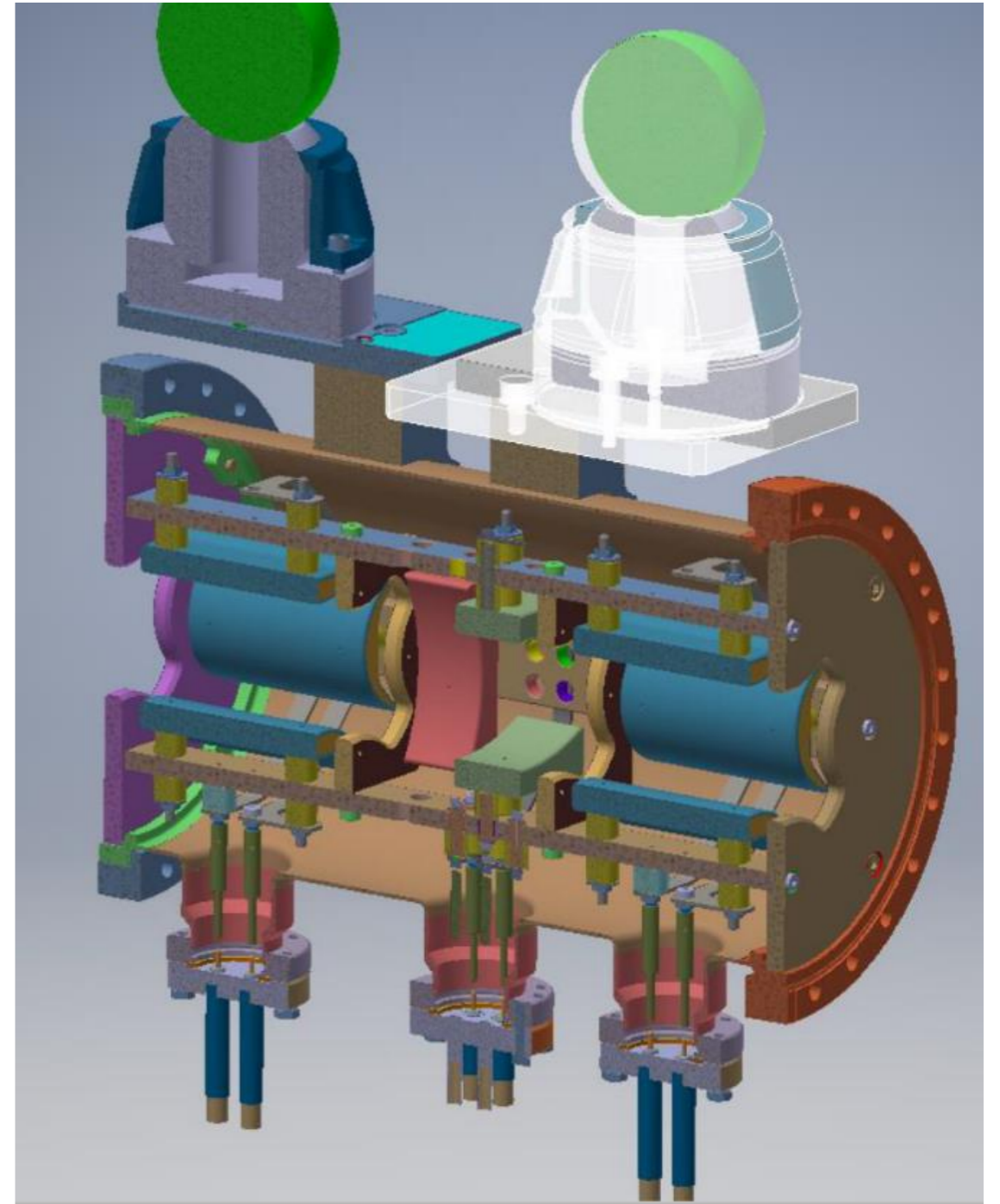
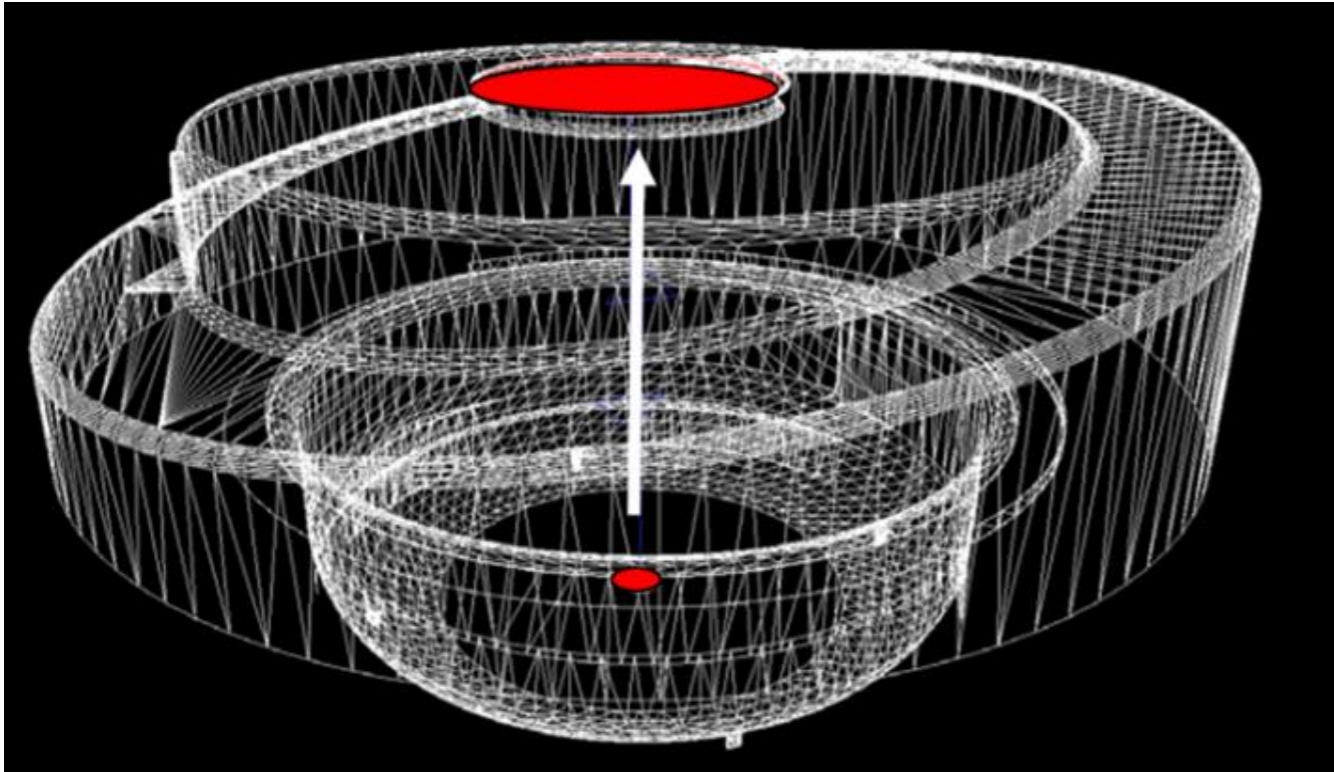
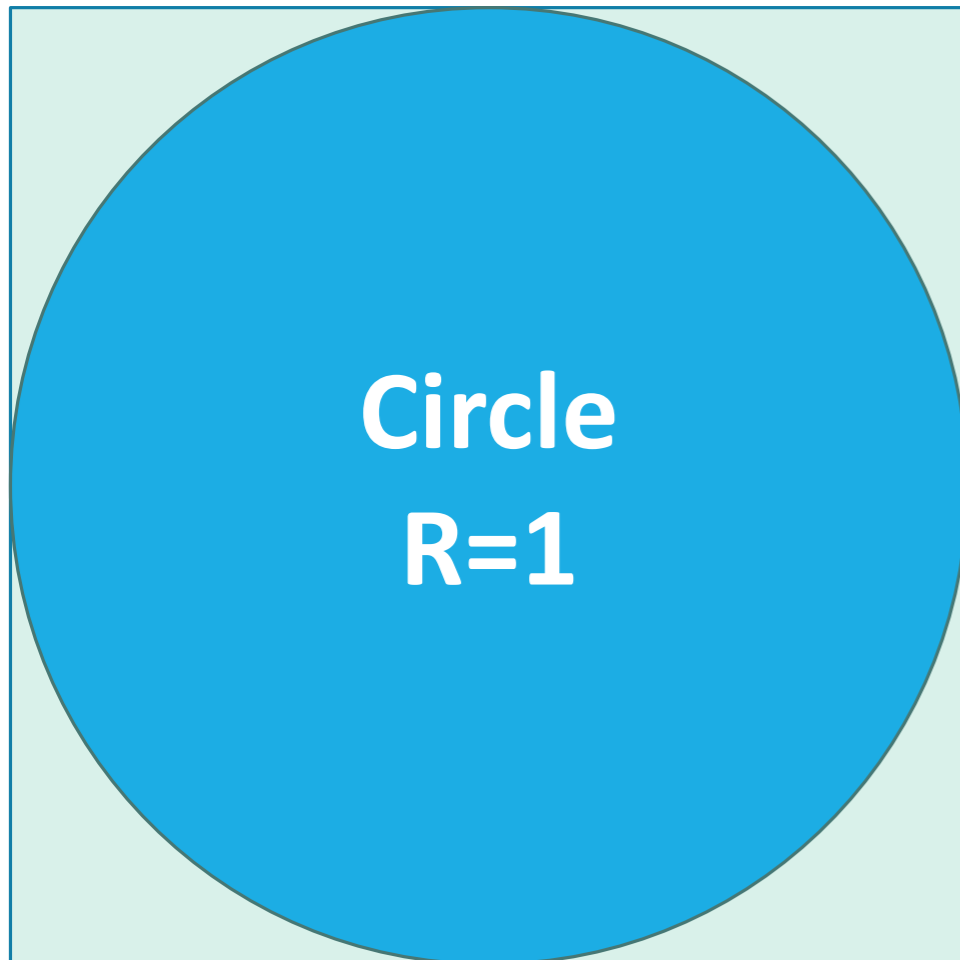
Geometric structure	Design equation	Reference
	<p>1. Two infinitesimal elements</p> <p>Two arbitrarily oriented elementary areas</p> $d\omega_{1-2} = \frac{\cos \alpha_1 \cos \alpha_2}{r^2} dA_1 dA_2$	[47]
	<p>Two strips of finite length and infinitesimal width with parallel generators</p> $d\omega_{1-2} = \frac{1}{r} \sin \alpha \operatorname{arctg} \frac{a}{r} ds$	[47]
	<p>End-face element of a channel with a square cross section, located in a corner, and a channel surface element</p> $d\omega_{1-2} = \frac{ds}{4R^2 + r^2} \left[ \operatorname{arctg} \frac{a}{\sqrt{a^2 + r^2}} + \operatorname{arctg} \frac{a\sqrt{a^2 + r^2}}{a^2 + 2r^2} \right] ds$	[47]
	<p>Two annular elements on the inside surface of a right circular cylinder</p> $d\omega_{1-2} = \frac{1}{2R} \left[ 1 - \frac{a^2 + 4R^2}{(l^2 + 4R^2)^{3/2}} \right] da$	[47]
	<p>Two annular elements on the inside surface of a right circular cone</p> $d\omega_{1-2} = \frac{\cos^2 \alpha}{2R_1 \sin \alpha} \left\{ 1 - h_1 - h_2 \frac{(R_1 - h_2)^2 + 4h_1 R_2 \sin^2 \alpha}{[h_1 - h_2]^2 + 4h_1 h_2 \sin^2 \alpha} \right\} dh_1$	[136]
	<p>Two infinitesimal elements on the inside surface of a spherical cavity</p> $d\omega_{1-2} = \frac{dA_1 dA_2}{4R^2}$	[137]

Table 1.2 (continued)

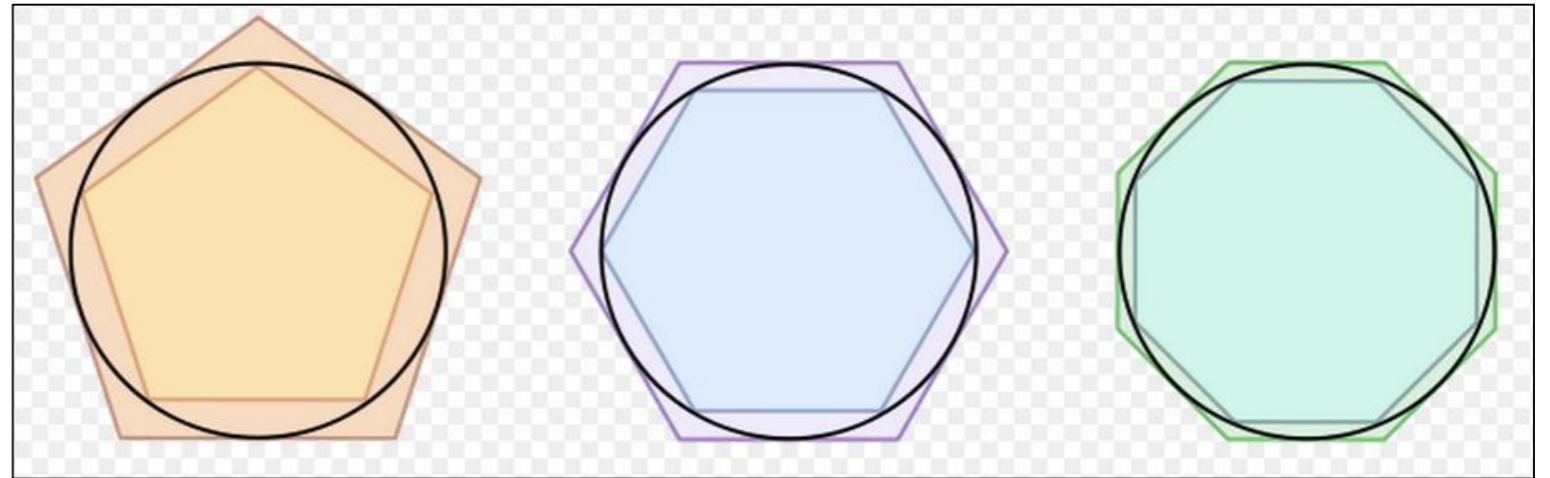
Geometric structure	Design equation	Reference
	<p>Plane element and ellipse parallel to it</p> $\omega_{1-2} = \frac{ab}{\sqrt{(l^2 + a^2)(b^2 + l^2)}}$	[47]
	<p>Elementary strip and infinite-length cylinder parallel to it</p> $\omega_{1-2} = \frac{2R}{r^2 + l^2}$	[128]
	<p>Element on the inside surface of the outer cylinder and the inside surface of the same cylinder for a space of two coaxial cylinders</p> $\omega_{1-2} = \frac{1}{2} \left[ \frac{R_2}{R_1} + \frac{R_1}{R_2} \right] + \left[ \frac{l}{R_1} \operatorname{arctg} \frac{\sqrt{R_1^2 - R_2^2}}{R_1} - \frac{1}{2} \operatorname{arctg} \frac{l^2 - 4R_1^2 - R_2^2}{4l\sqrt{R_1^2 - R_2^2}} - \frac{l^2 + 2R_1^2}{R_2\sqrt{l^2 + 4R_1^2}} \right] = \operatorname{arctg} \frac{\sqrt{(R_1^2 - R_2^2)(l^2 + 4R_1^2)}}{R_1 l}$	[129]
	<p>Annular element on the inside surface of a right circular cylinder and the end face of the cylinder</p> $\omega_{1-2} = \frac{1}{2R} \left[ \frac{r^2 + 2R^2}{\sqrt{r^2 + 4R^2}} - 1 \right] \quad \left\{ \frac{r}{R_1} - \frac{l}{R_2} \right\} = \frac{1}{R_1} \left[ \frac{r^2 + 2R_1^2}{\sqrt{r^2 + 4R_1^2}} - 1 \right] \frac{l}{R_2}$	[47]
	<p>Element of a plane ring and outside surface of a right circular cylinder</p> $\omega_{1-2} = \frac{1}{2} \left[ \frac{1}{R_1} \operatorname{arctg} \frac{R_1}{R_2} + \operatorname{arctg} \frac{R_2}{\sqrt{R_1^2 - R_2^2}} - \frac{l^2 + R_1^2 - R_2^2}{A} \right] = \operatorname{arctg} \frac{A \operatorname{tg} [(1/2) \operatorname{arccos} (R_2/R_1)]}{l^2 + R_1^2 + R_2^2 - 2R_1 R_2}$ $A = \sqrt{(l^2 + R_1^2 + R_2^2)^2 - 4R_1^2 R_2^2}$	[137]
	<p>Plane annular element and inside surface of a cylinder</p> $\omega_{1-2} = \frac{1}{2} \left[ \frac{(l^2 + r^2 + R_1^2) - R_2^2}{\sqrt{(l^2 + r^2 + R_1^2 + R_2^2)^2 - 4R_1^2 R_2^2}} - \frac{r^2 + R_1^2 - R_2^2}{\sqrt{(r^2 + R_1^2 + R_2^2)^2 - 4R_1^2 R_2^2}} \right]$	[126]
	<p>Annular cylindrical element and inside surface of a cylinder</p> $\omega_{1-2} = \frac{1}{2R} \left[ 1 + \frac{r^2 + 2R^2}{\sqrt{r^2 + 4R^2}} - \frac{l^2 + r^2 + 2R^2}{\sqrt{(l^2 + r^2 + 4R^2)}}$	[126]



# The idea: Monte Carlo method



Area=3.14

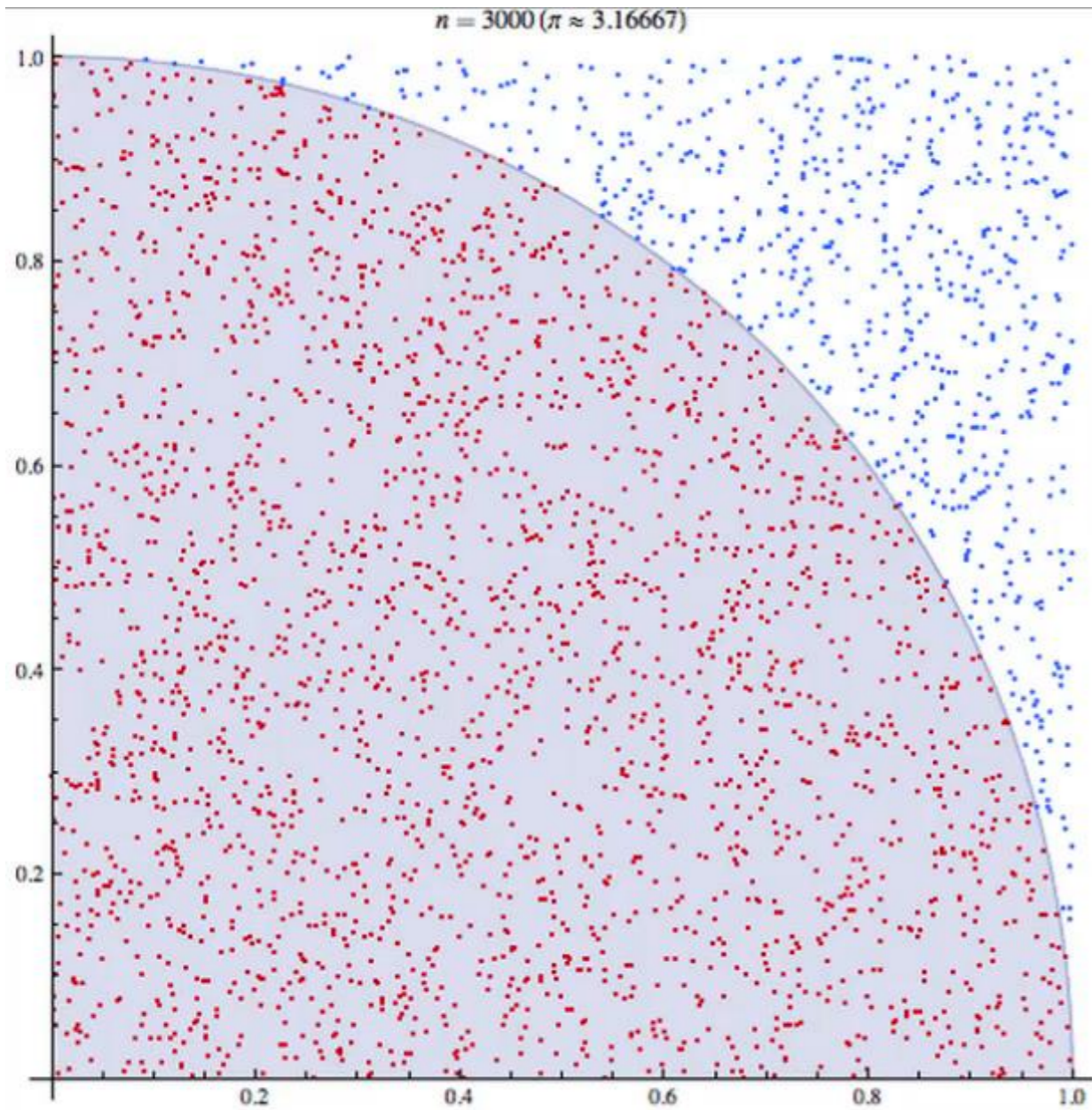


$$\pi = \frac{4}{1 + \frac{1^2}{2 + \frac{3^2}{2 + \frac{5^2}{2 + \frac{7^2}{2 + \frac{9^2}{2 + \dots}}}}}}$$

$$\frac{1}{\pi} = \frac{2\sqrt{2}}{9801} \sum_{k=0}^{\infty} \frac{(4k)!(1103 + 26390k)}{(k!)^4 396^{4k}}$$

$$\frac{2}{\pi} = \frac{\sqrt{2}}{2} \cdot \frac{\sqrt{2 + \sqrt{2}}}{2} \cdot \frac{\sqrt{2 + \sqrt{2 + \sqrt{2}}}}{2} \dots$$

# Monte Carlo



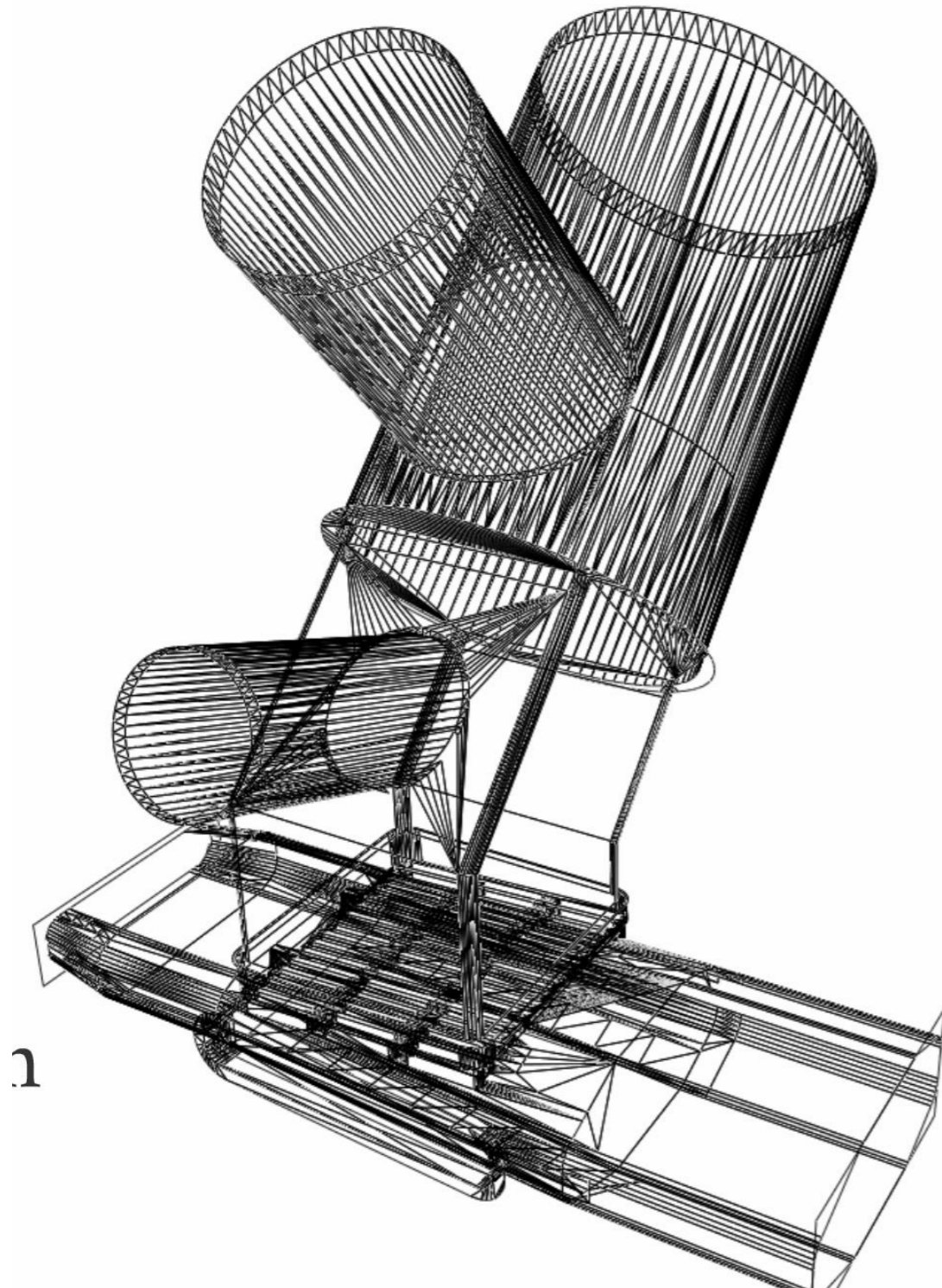
$$\frac{\text{points inside}}{\text{all points}} \sim \frac{\text{circle area}}{\text{square area}} = \frac{\pi}{4}$$



# Monte Carlo simulations

Geometry: polygons

Gas input:

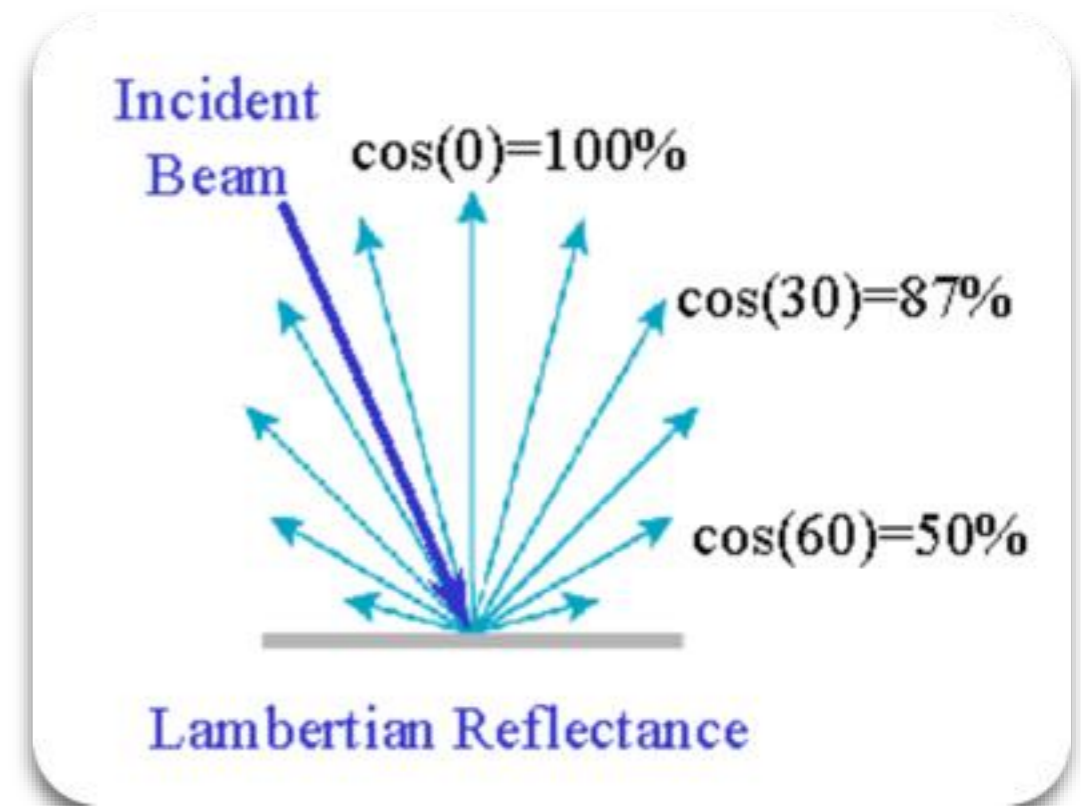
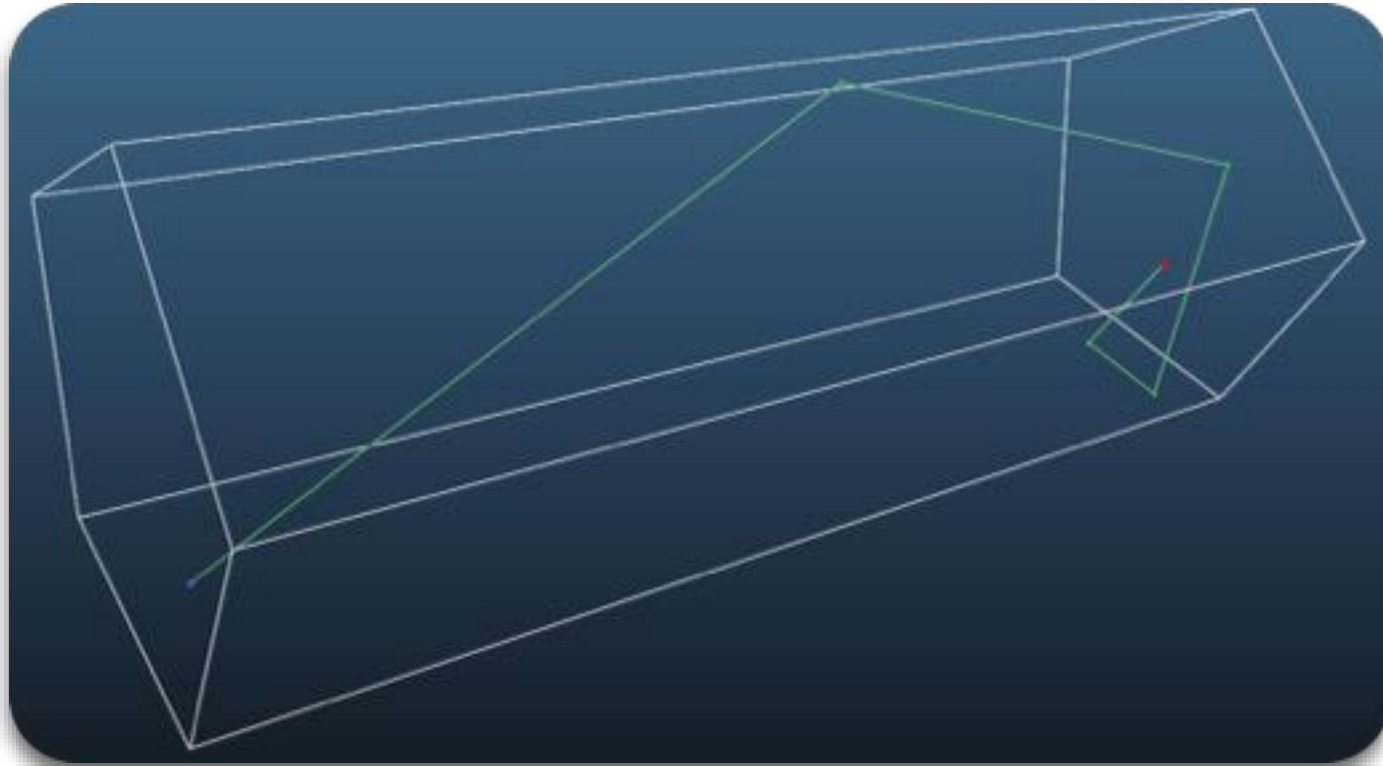


$$pV=NkT$$

$$1 \text{ Pa} \cdot \text{m}^3/\text{s} = 2.4 \cdot 10^{20} \text{ molecules/s}$$

Virtual / Physical particle ratio

## Reflection

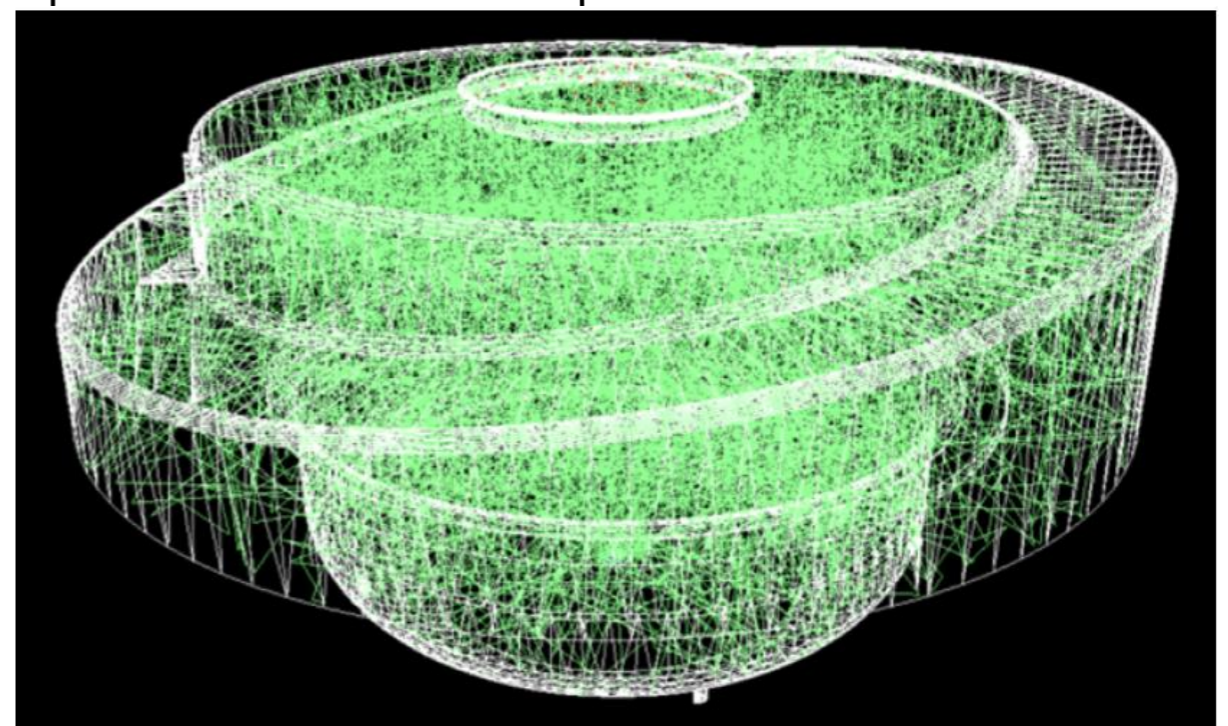
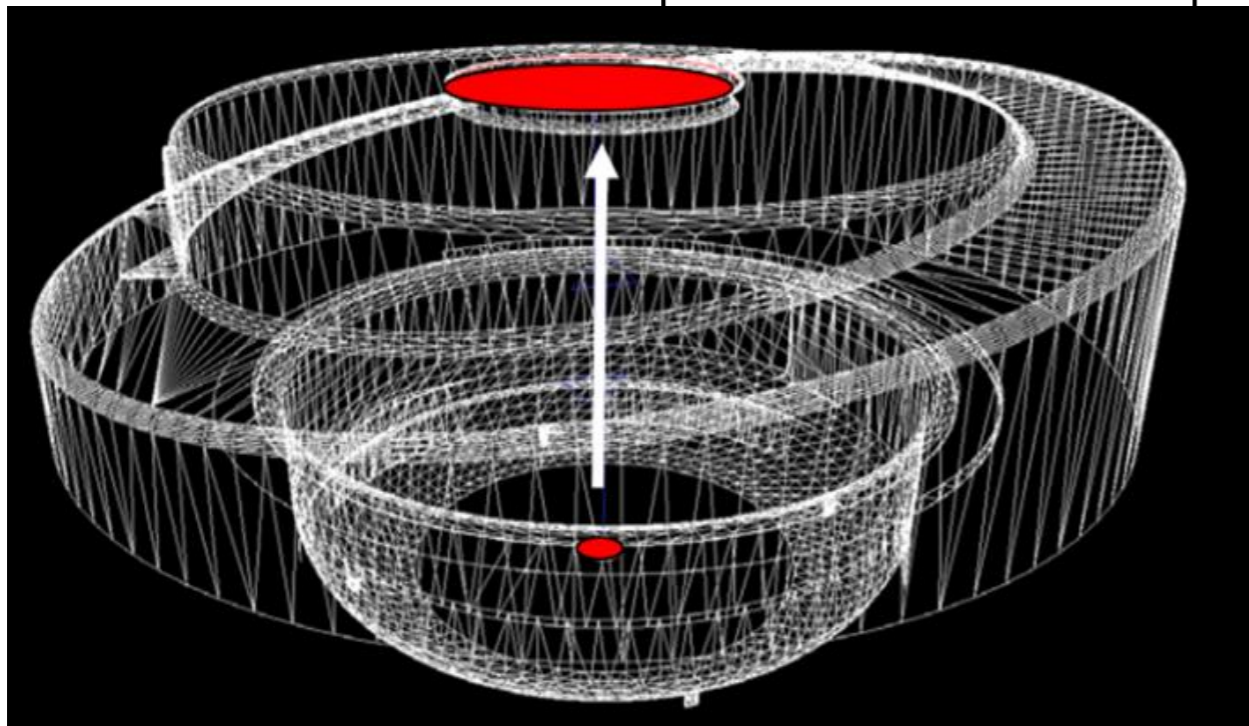
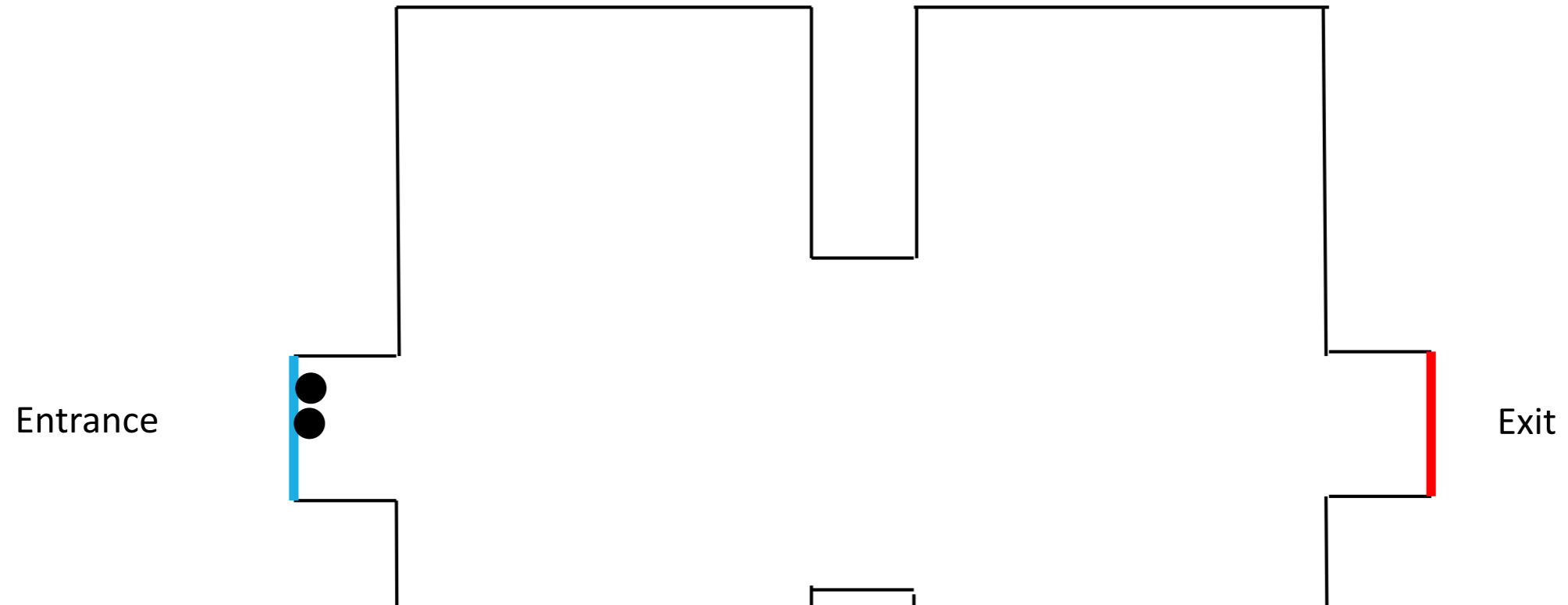


## Pumping / absorption



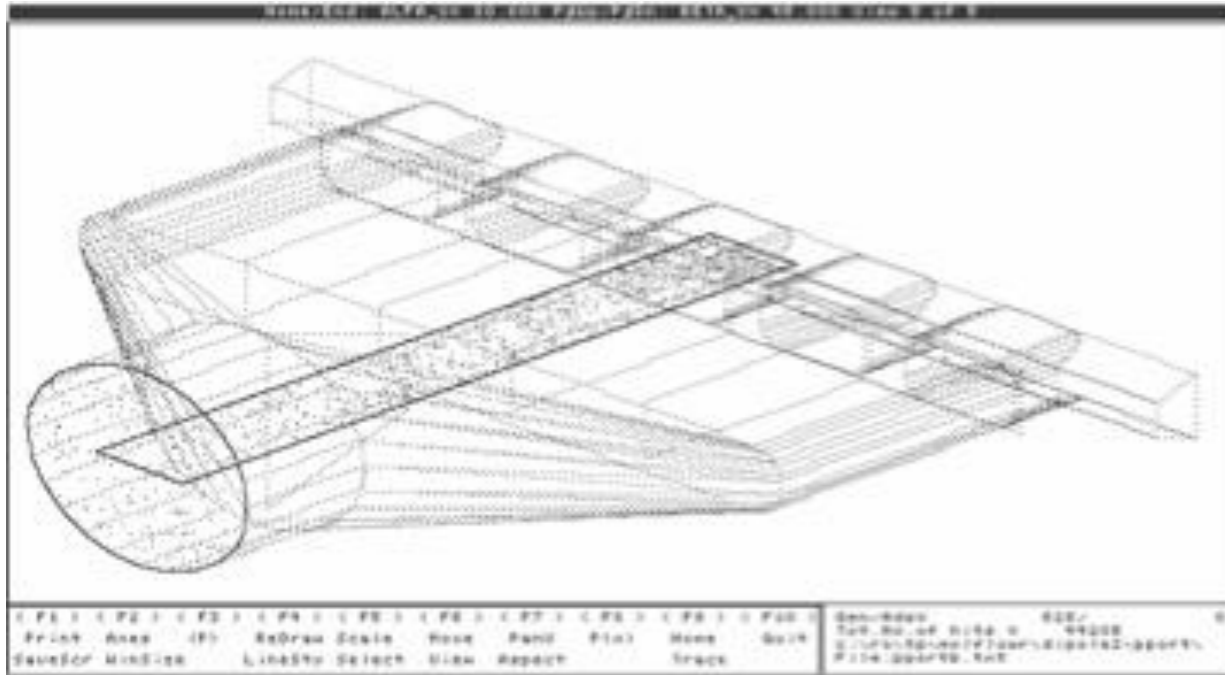
$$S \text{ [m}^3\text{/s]} = \text{sticking [0..1]} * 1/4 * A \text{ [m}^2\text{]} * v_{\text{avg}} \text{ [m/s]}$$

# Monte Carlo

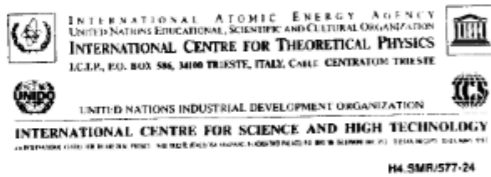
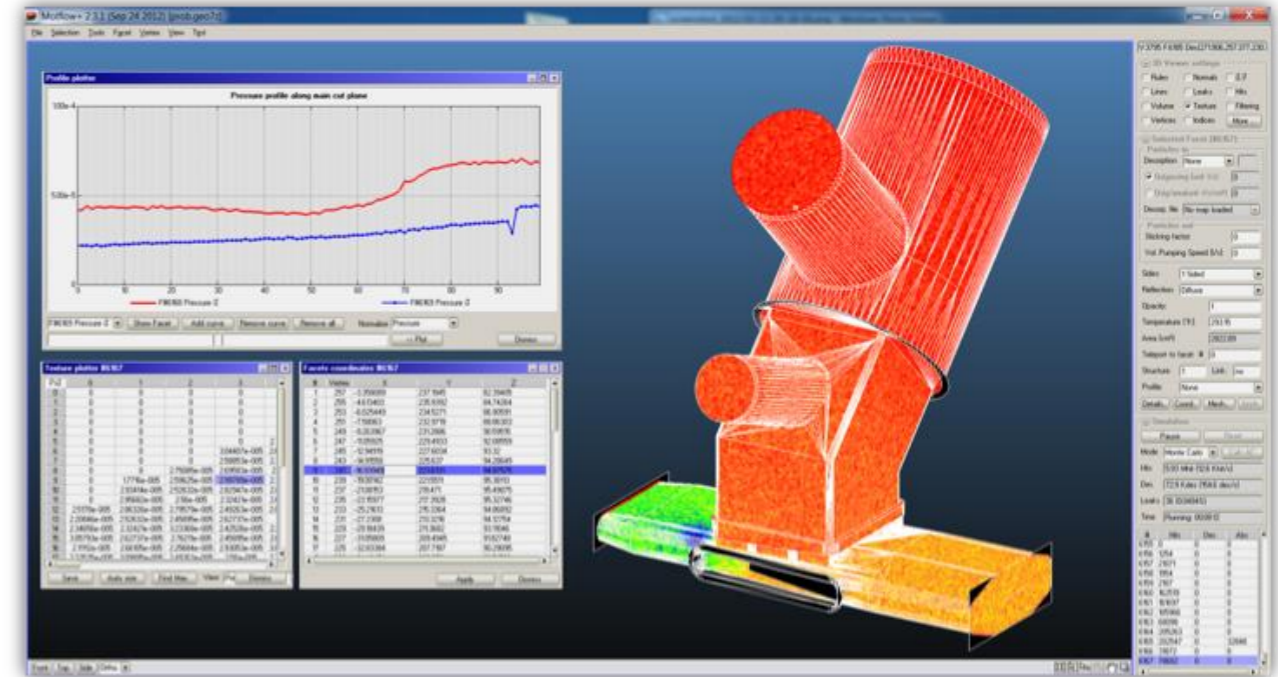


# Molflow (1990)

Roberto Kersevan



# Molflow+ (2008-)



SEM-95/7

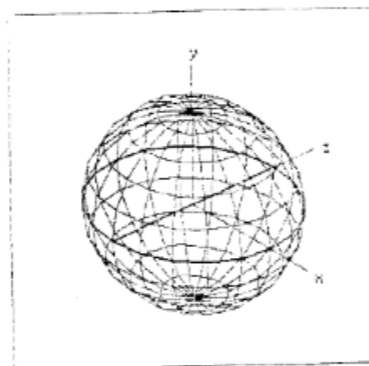
School on  
"Use of Synchrotron Radiation in Science and Technology"  
14 October - 8 November 1991

Molflow  
User's Guide

R. Kersevan  
Sincrotrone Trieste  
Trieste, Italy

## MOLFLOW User's Guide

Roberto Kersevan



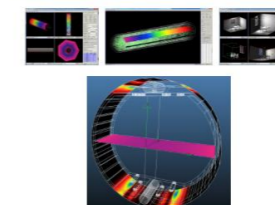
September 1991

SINCROTRONE TRIESTE



molflow

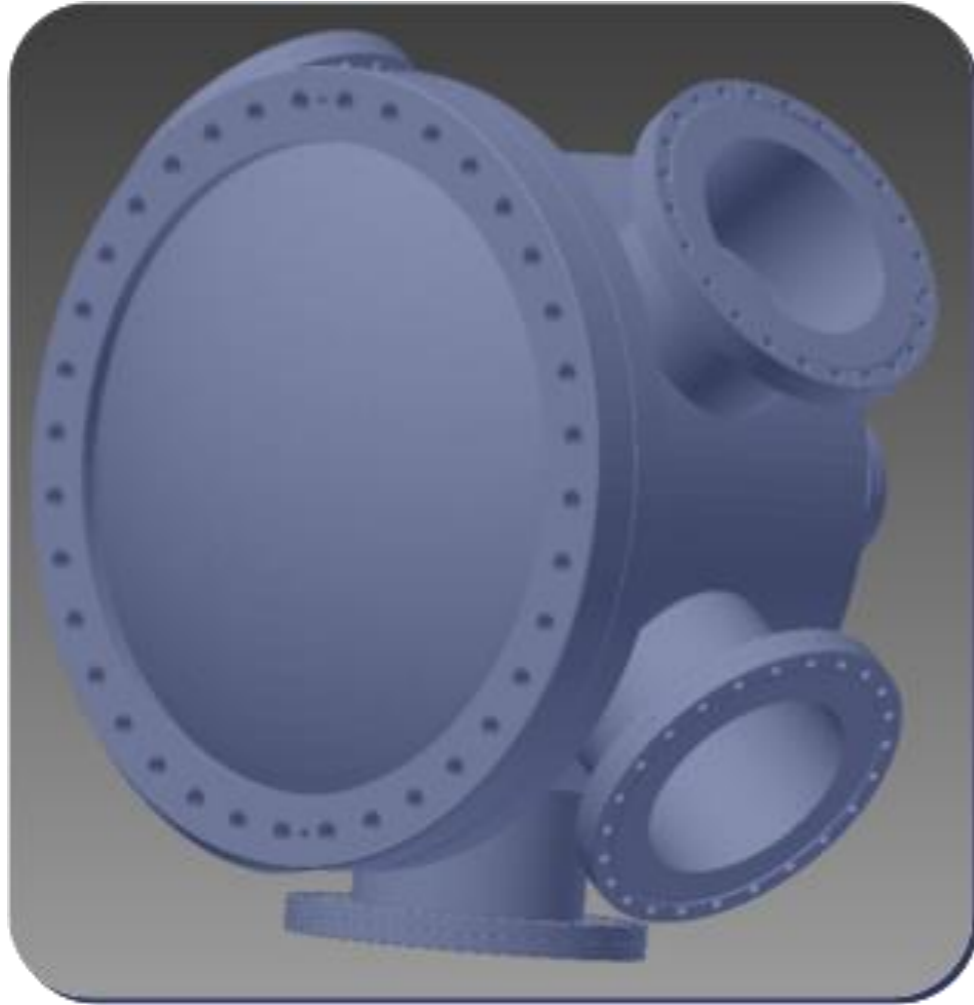
Google Search I'm Feeling Lucky



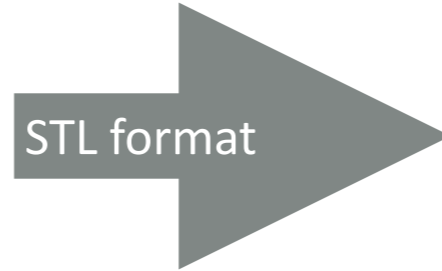
# WORKING WITH MOLFLOW

Step 1: creating geometry

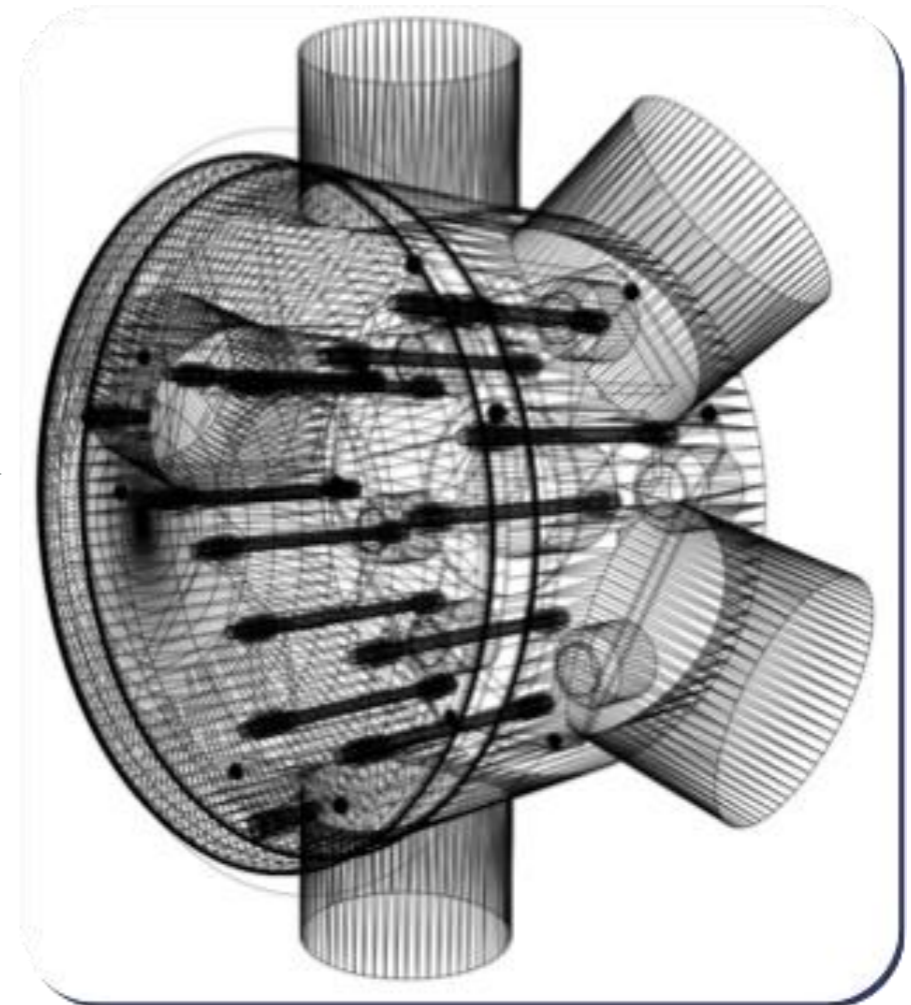
CAD



STL format



Molflow+



## Step 2: adding physics

Molflow+ 2.6.39 64-bit (Feb 22 2017) [simple\_geo.zip]

File Selection Tools Facet Vertex View Test Time

The screenshot displays the Molflow+ software interface with four viewports and a right-hand panel. The top-left viewport shows a perspective view of a vacuum chamber with a red circle highlighting a specific facet. The top-right viewport shows an orthographic view of the chamber's cross-section. The bottom-left viewport shows another perspective view of the chamber. The bottom-right viewport shows an orthographic view of the chamber's side profile. The right-hand panel, titled 'Profile plotter', contains various settings and simulation results.

Profile plotter [V:228 F:139 Dim:(5,4,18) Area:216.18]

3D Viewer settings

- Rules
- Normals
- $\vec{u}, \vec{v}$
- Lines
- Leaks
- Hits
- Volume
- Texture
- Vertices
- Indices

Selected Facet (3 selected)

Particles in

Description ...

- Outgassing (mbar<sup>l</sup>/s):
- Outg/area(mbar<sup>l</sup>/s/cm<sup>2</sup>):

Particles out

Sticking factor: ...

Pumping Speed (l/s): ...

Sides: 1 Sided

Opacity: 1

Temperature (°K): 293.15

Sum Area (cm<sup>2</sup>): 13.90576475

Profile: None

<< Adv Details... Coord... Apply

Shortcuts

Simulation

<< Sim Resume Reset

- Auto update scene Update

Hits 182.76 Mhit (3.2 Mhit/s)

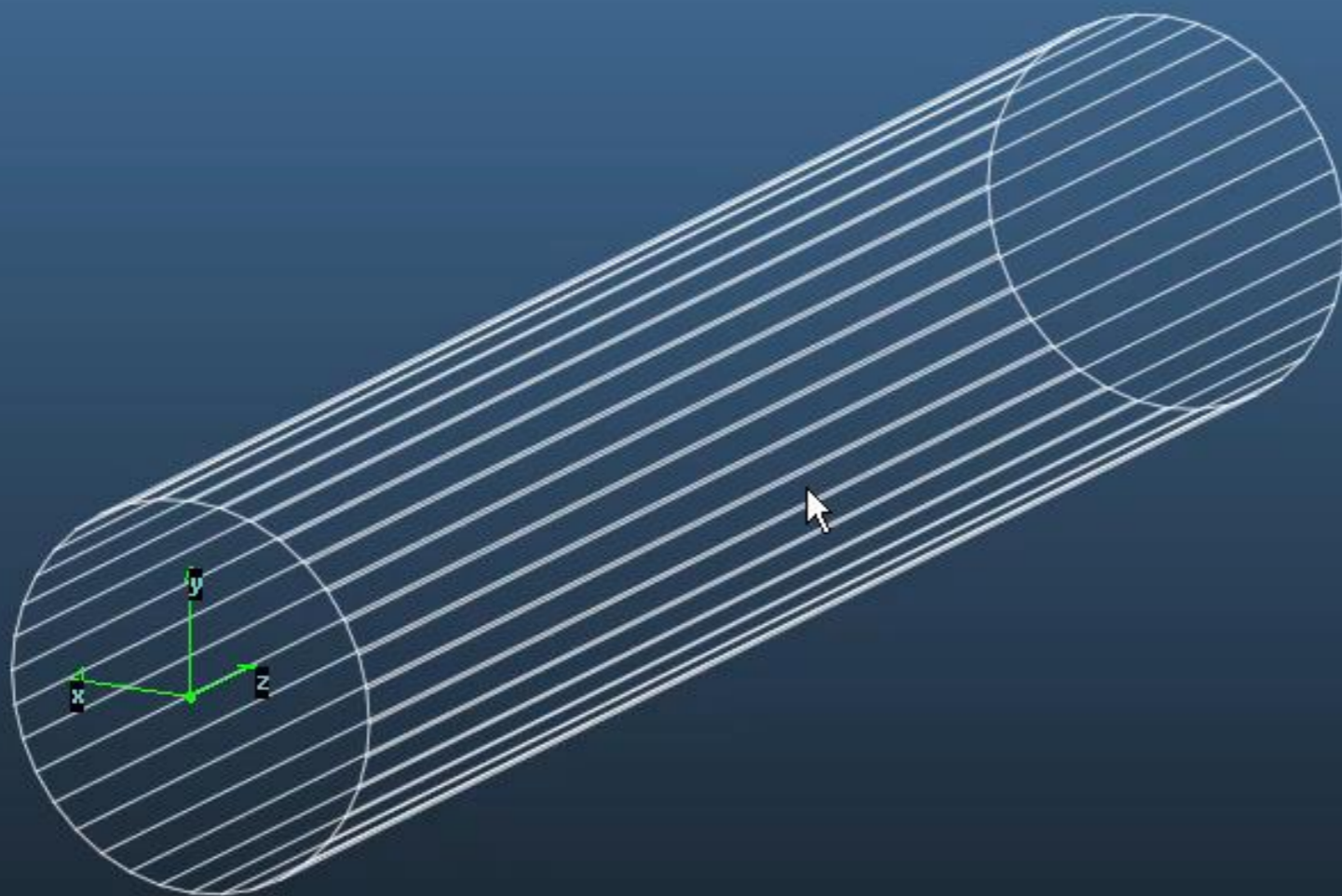
Des. 2.02 Mdes (34.9 Kdes/s)

Leaks None

Time Stopped: 00:00:58

#	Hits	Des	Abs
67	6261377	0	0
68	6280336	0	0
69	6291972	0	0

Trans. Prob. Divide by 0



V:72 F:38 Dim:(2,2,10) Area:69.0035

**3D Viewer settings**

Rules     Normals      $\vec{u}, \vec{v}$   
 Lines     Leaks     Hits  
 Volume     Texture     FacetIDs  
 Indices     VertexIDs

<< View

**Selected Facet (none)**

Particles in

Description

Outgassing (mbar<sup>3</sup>/s):   
 Outg/area(mbar<sup>3</sup>/s/cm<sup>2</sup>):

Particles out

Sticking factor:

Pumping Speed (l/s):

Sides:

Opacity:

Temperature (°K):

Sum Area (cm<sup>2</sup>):

Profile:

<< Adv    Details...    Coord.    Apply

**Shortcuts**

**Simulation**

<< Sim    Begin    Reset

Auto update scene    Update

Hits

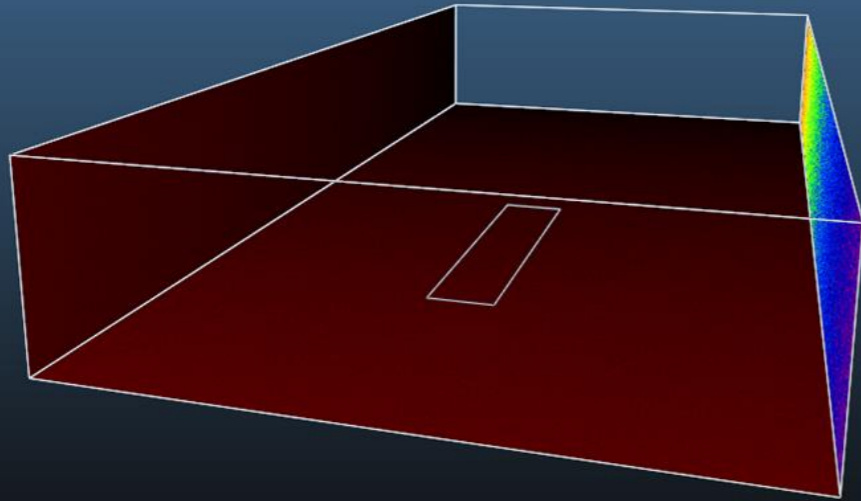
Des.

Leaks

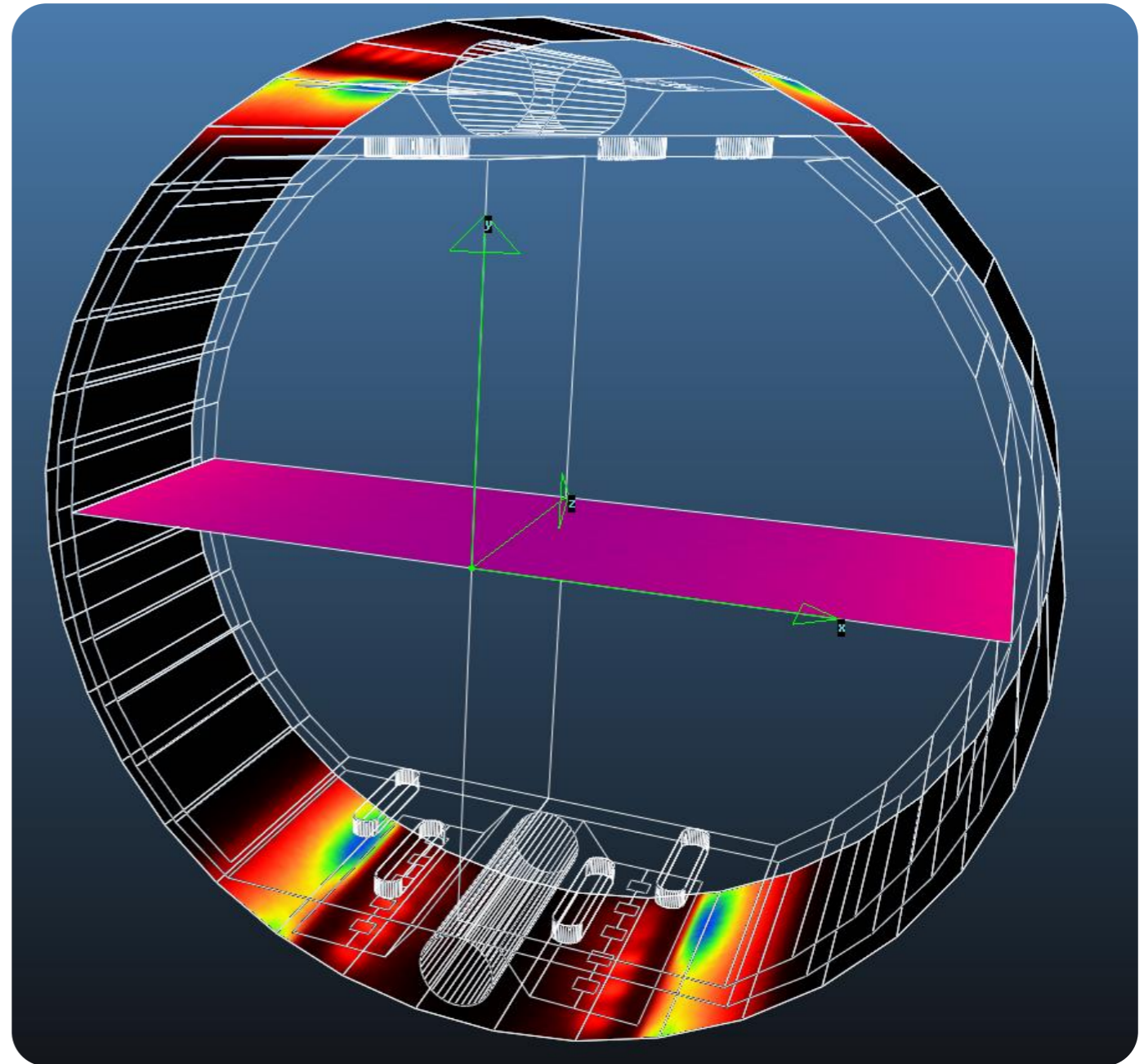
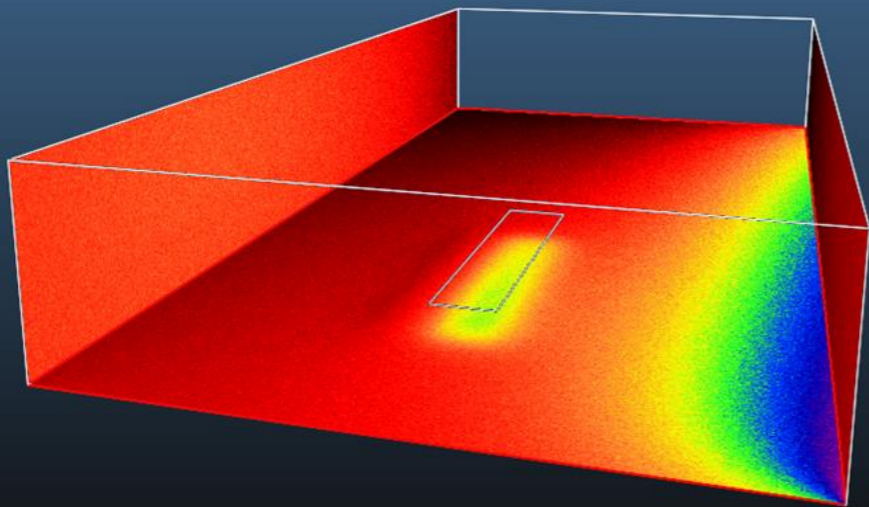
Time

#	Hits	Des	Abs
1	0	0	0
2	0	0	0
3	0	0	0
4	0	0	0

Isothermal mode

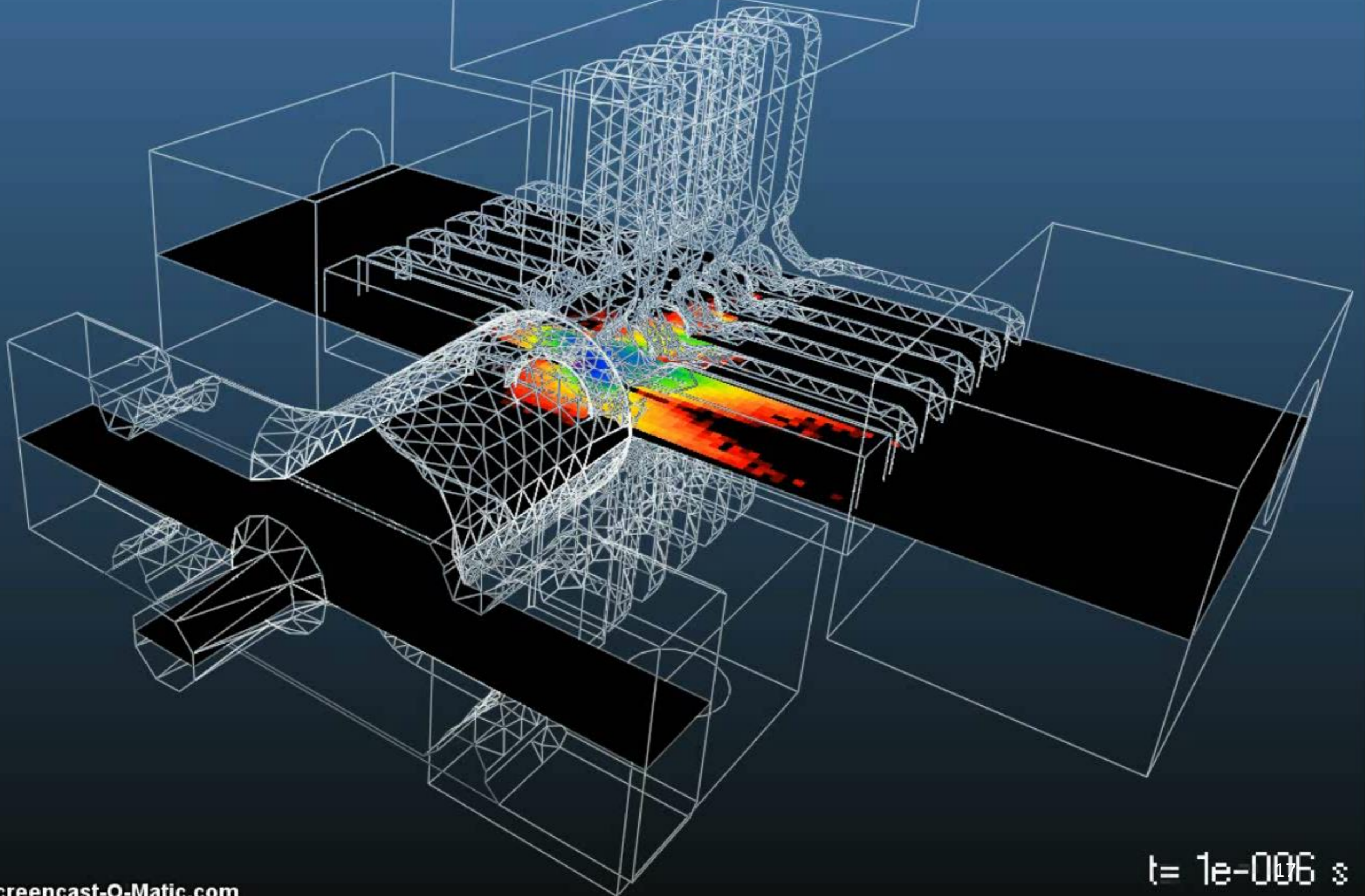


Non-isothermal mode

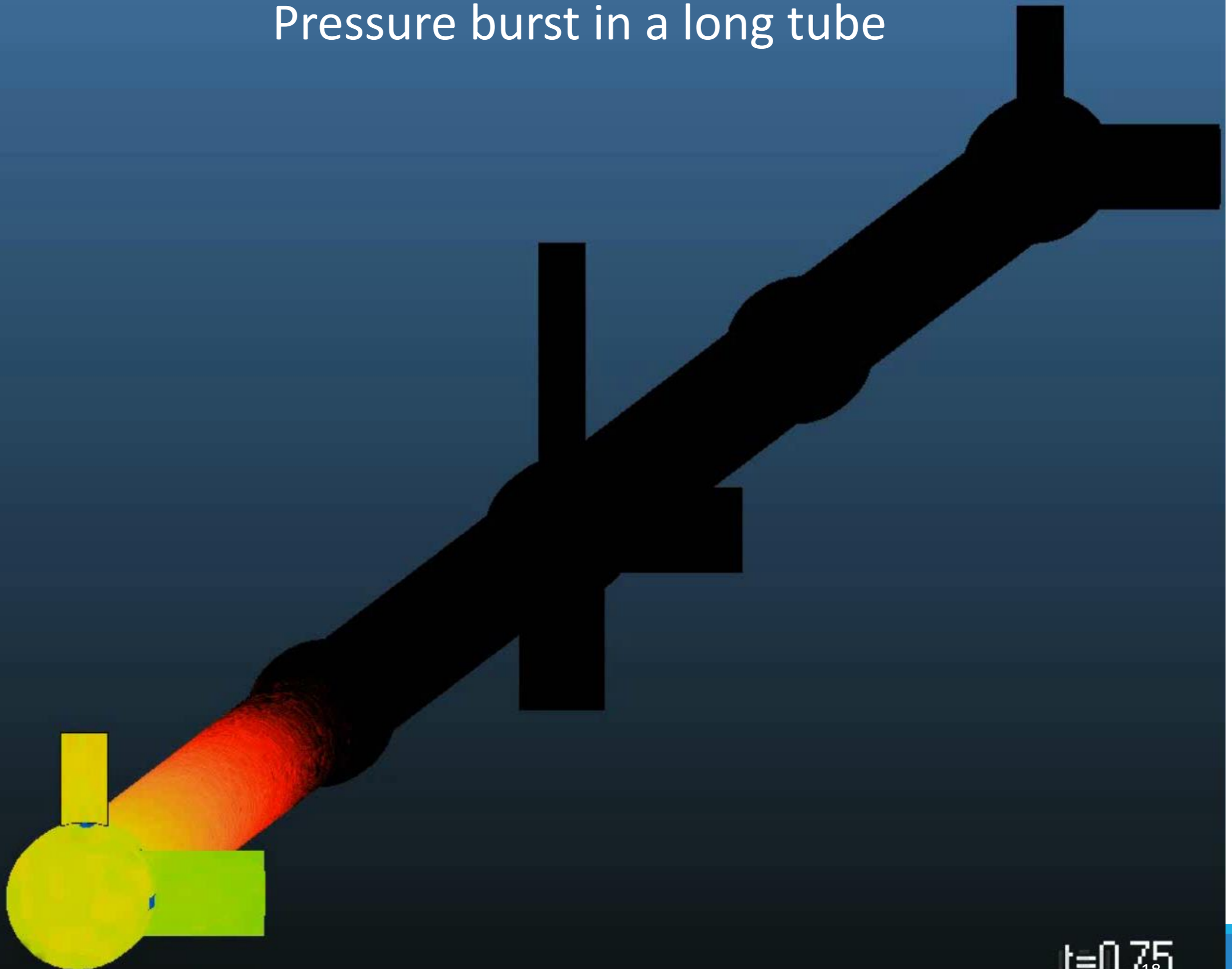




# Electric breakdown in an accelerator cavity

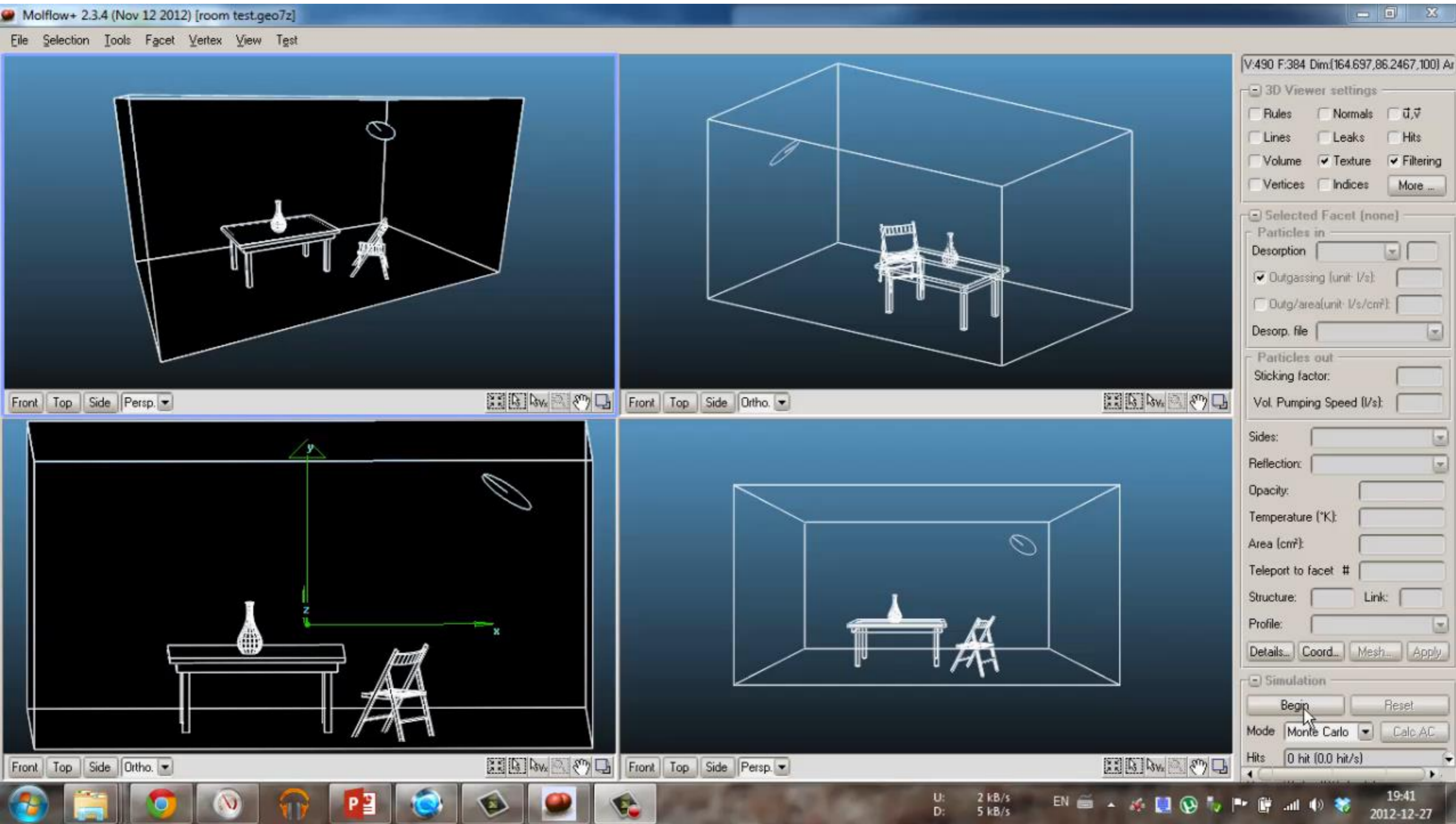


# Pressure burst in a long tube



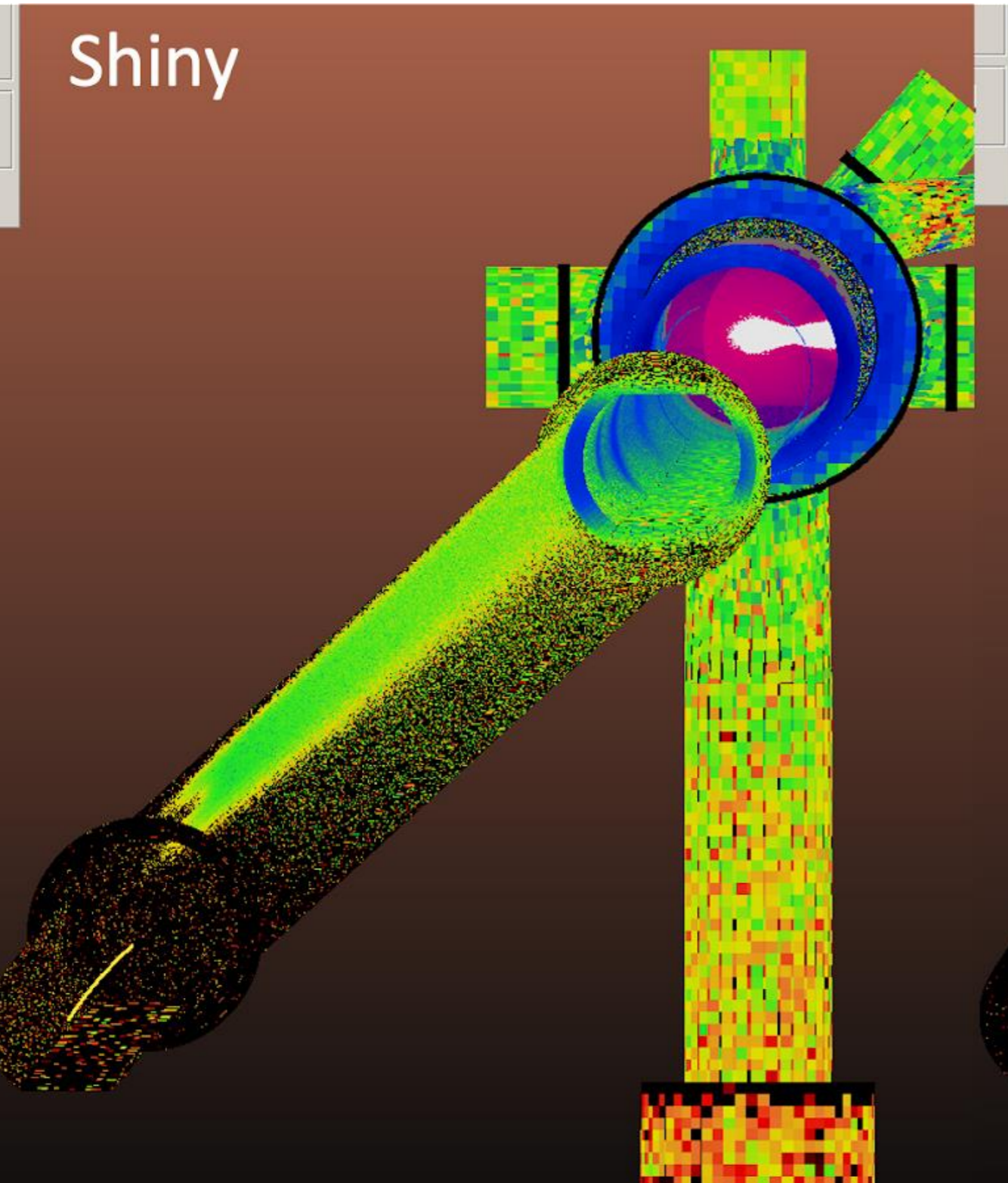
$t=0.75$   
18

# Simulation of light

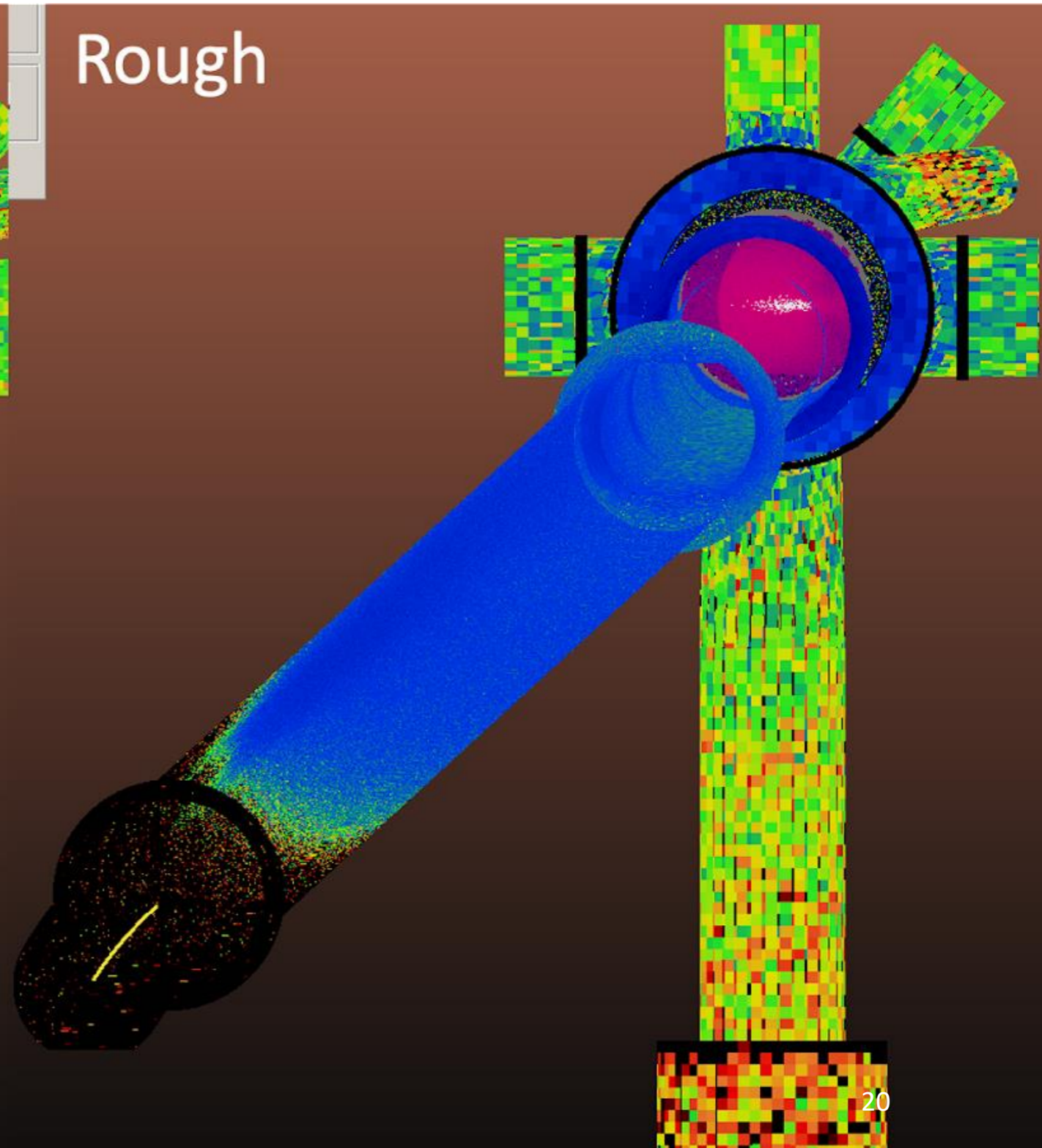


# Synrad+: Synchrotron radiation simulations

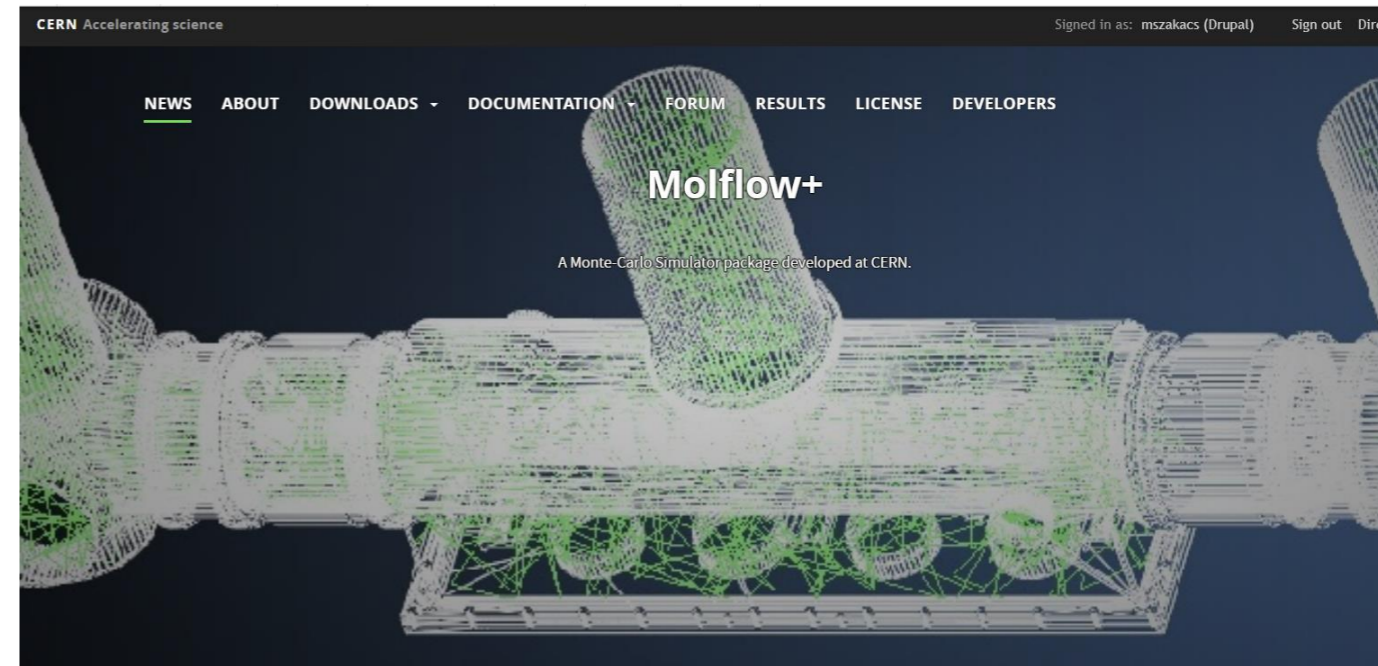
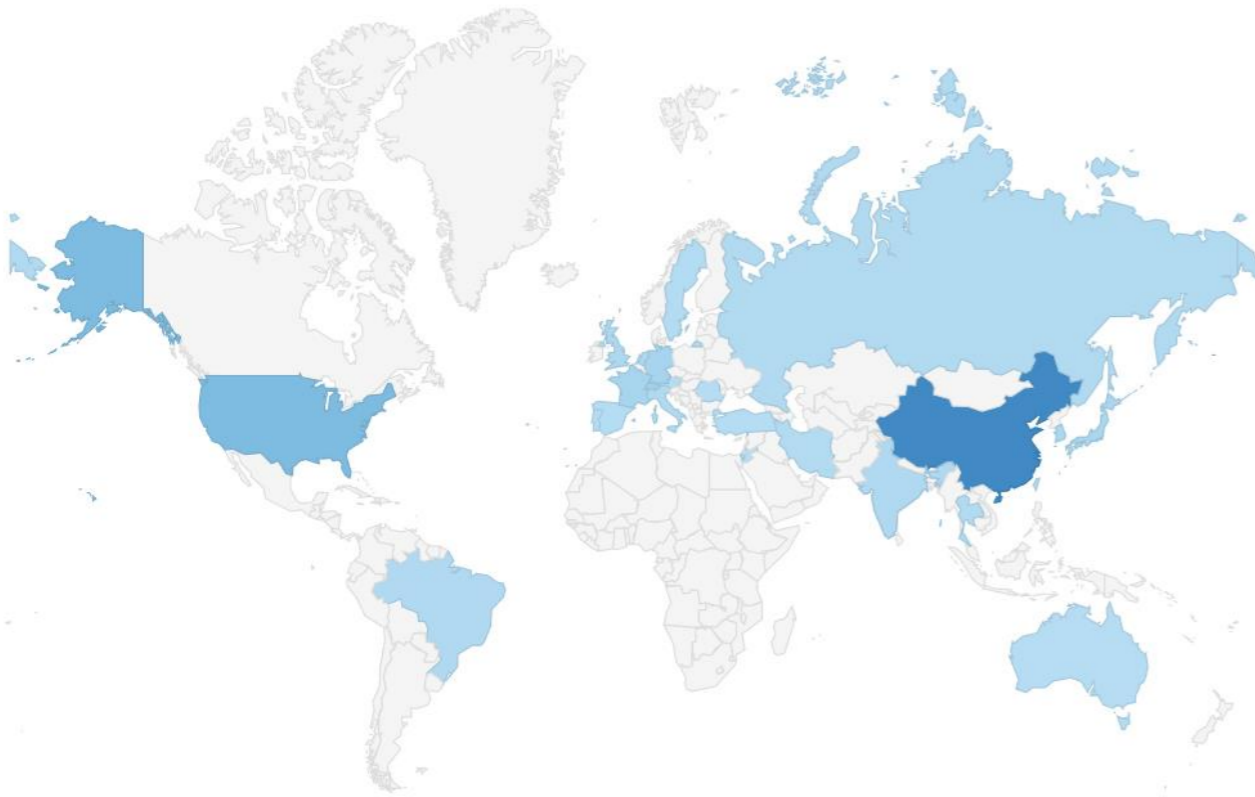
Shiny






Rough



<https://molflow.web.cern.ch/>



Country ?	Acquisition		
	Users ? ↓	New Users ?	Sessions ?
	<b>4,983</b> % of Total: 100.00% (4,983)	<b>4,908</b> % of Total: 100.12% (4,902)	<b>9,107</b> % of Total: 100.00% (9,107)
1. 🇨🇳 China	<b>2,575 (50.98%)</b>	<b>2,551 (51.98%)</b>	<b>3,508 (38.52%)</b>
2. 🇺🇸 United States	<b>702 (13.90%)</b>	<b>684 (13.94%)</b>	<b>1,067 (11.72%)</b>
3. 🇩🇪 Germany	<b>215 (4.26%)</b>	<b>209 (4.26%)</b>	<b>513 (5.63%)</b>
4. 🇯🇵 Japan	<b>205 (4.06%)</b>	<b>192 (3.91%)</b>	<b>590 (6.48%)</b>
5. 🇨🇭 Switzerland	<b>194 (3.84%)</b>	<b>172 (3.50%)</b>	<b>641 (7.04%)</b>
6. 🇰🇷 South Korea	<b>173 (3.43%)</b>	<b>170 (3.46%)</b>	<b>334 (3.67%)</b>
7. 🇫🇷 France	<b>136 (2.69%)</b>	<b>121 (2.47%)</b>	<b>447 (4.91%)</b>
8. 🇮🇷 Iran	<b>111 (2.20%)</b>	<b>112 (2.28%)</b>	<b>157 (1.72%)</b>
9. 🇷🇺 Russia	<b>79 (1.56%)</b>	<b>73 (1.49%)</b>	<b>201 (2.21%)</b>
10. 🇮🇳 India	<b>77 (1.52%)</b>	<b>73 (1.49%)</b>	<b>222 (2.44%)</b>

MacOS	Windows	Linux
		
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[Instructions](#)

[Instructions](#)

[Debian Instructions<sup>1</sup>](#)  
[Fedora Instructions<sup>2</sup>](#)

### Introduction to Monte Carlo simulations

If you're new to these Monte Carlo tools, this presentation is a good overview of the special physics at very low pressures, how it's related to Monte Carlo simulations, and how Molflow actually works.

- Short explanation of the high vacuum physics
- The Monte Carlo method
- History of Molflow and Synrad
- Typical Molflow workflow

