

Initial stage jet momentum broadening and energy loss in tBLFQ formalism

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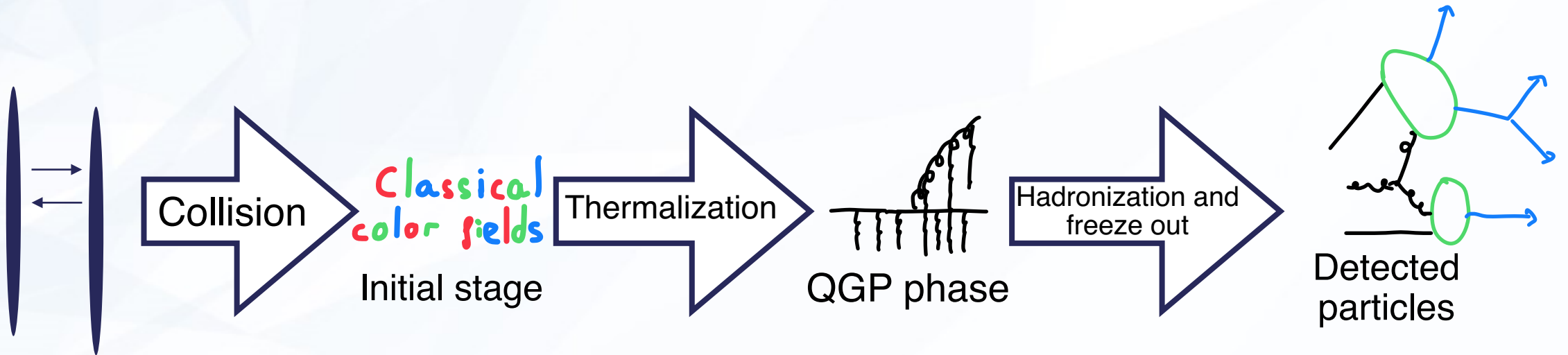
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1. Motivation of this work

Heavy ion collisions

High density **quark and gluon matter** is created

Different states before reaching our detectors

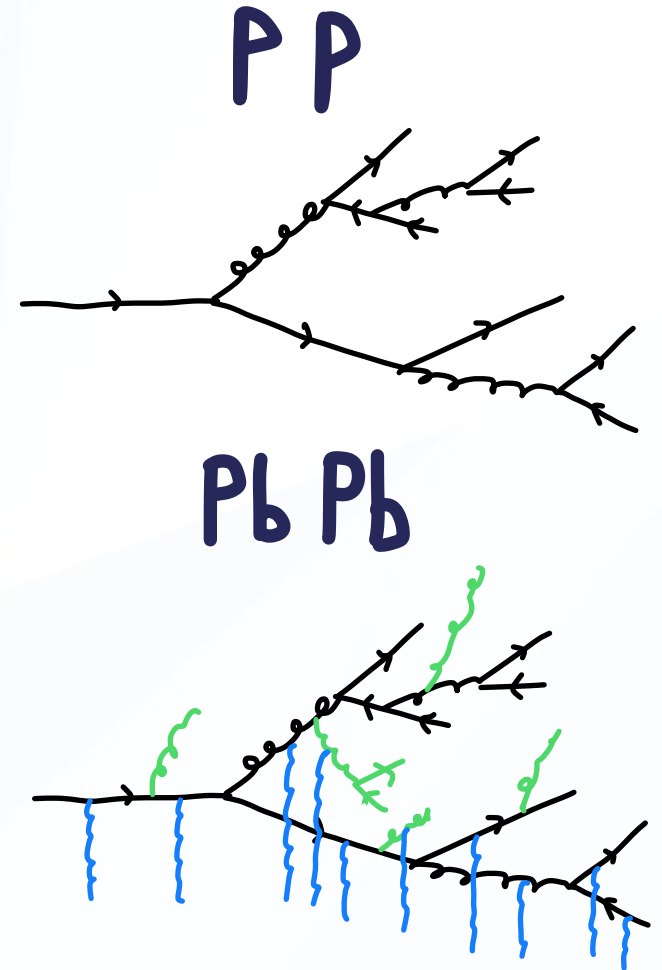


Jet quenching

Jets **probe** the different stages of nuclear matter

Jet momentum distribution and energy gets modified, **jet quenching**

$$\hat{q} = \frac{d\langle q_{\perp}^2 \rangle}{dL}$$



Jet quenching in the initial stage

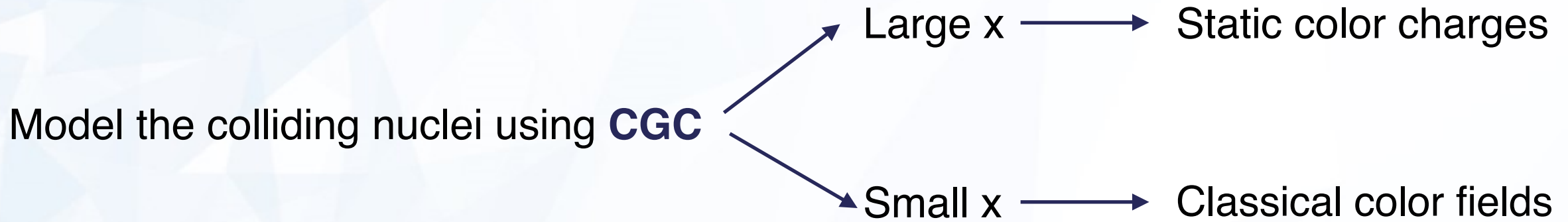
Claims that \hat{q} must be **suppressed** in the initial stage [Phys. Lett. B 803 (2020) 135318]

Classical jet analysis shows that it is in fact \hat{q} is **very large** [Phys. Lett. B 810 (2020) 135810]

Our goal: Complete **quantum treatment** of the jet in tBLFQ formalism

2. The Glasma fields

The high energy nuclei

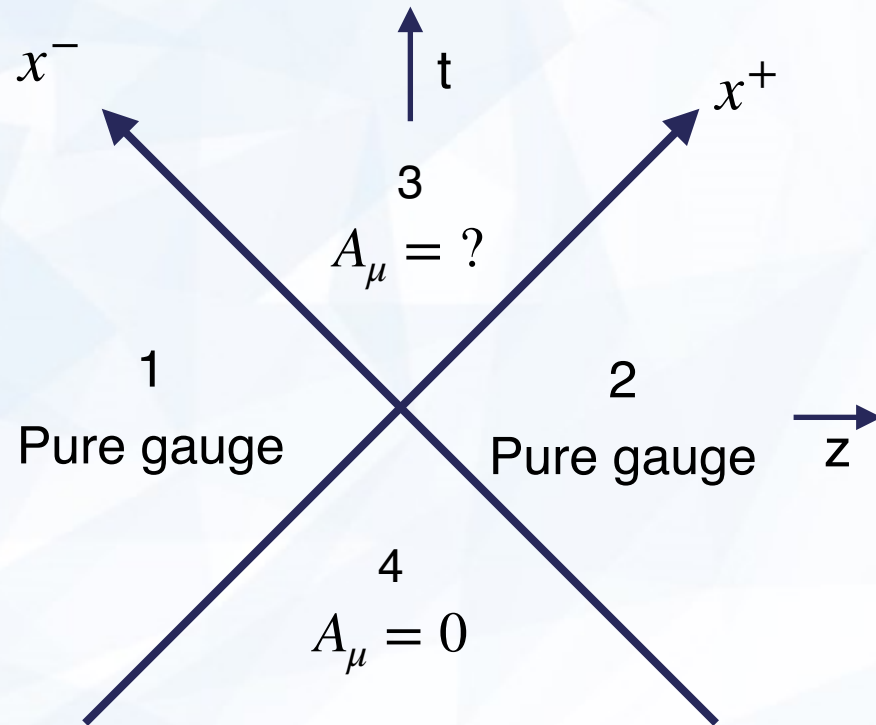


Color fields obey **classical Yang-Mills** equation $[D_\mu, F^{\mu\nu}] = J^\nu$

↓ LC gauge

Transverse **pure gauge** fields

Initial condition of the Glasma



Natural to use **Fock-Swinger gauge**

$$A_\tau = \frac{x^+ A^- + x^- A^+}{\tau} = 0$$

Imposing **boost invariance**

$$A_i^{(3)}(\tau = 0) = A_i^{(1)} + A_i^{(2)}$$

$$A^\eta(\tau = 0) = \frac{ig}{2} [A_i^{(1)}, A_i^{(2)}]$$

[Phys. Rev. D **52**, 6231]

Evolution of the Glasma fields

The Glasma fields evolve according to **free Young-Mills** $[D_\mu, F^{\mu\nu}] = 0$

Solved numerically we use **real-time lattice gauge theory**

Gauge fields

$$A_\mu(x)$$

Exponentiation

$$\longrightarrow U[c] = \mathcal{P} \exp\left(-ig \int_c dx^\mu A_\mu(x)\right)$$

Wilson lines

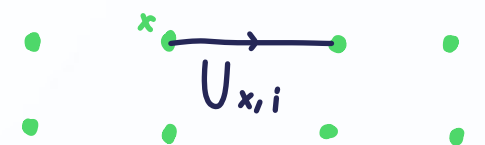


$$U[c]$$

Discretization

$$\longrightarrow U_{x,\mu} \approx \left(ig a^\mu A_\mu\left(x + \frac{a^\mu}{2}\right)\right)$$

Gauge links



3. The tBLFQ formalism

time-dependent Basis Light Front Quantization

Construction of the jet wave-function

Exploit the QFT \leftrightarrow QM isomorphism in **LC quantization**

Construct the eigenstates of
the Hamiltonian using BLFQ

[Phys. Rev. C 81, 035205]



Make the states evolve under
the action of the external field

$$|\psi; x^+\rangle_I = T_+ e^{-\frac{i}{2} \int_0^{x^+} V_I} |\psi; 0\rangle_I$$

[Phys. Rev. D 88 (2013) 065014]

Successfully applied to $|q\rangle$ and $|q\rangle + |qg\rangle$ evolution in a MV field

[Phys. Rev. D 101 (2020), 076016]

[Phys. Rev. D 104 (2021), 056014]

3. Gauge transformation of the Glasma fields

Need to gauge transform the Glasma fields

The Glasma and jet evolution have different natural gauges

Glasma
↓
Temporal gauge

Jet
↓
LC gauge

To use tBLFQ we need to **gauge transform** the Glasma gauge links to LC gauge

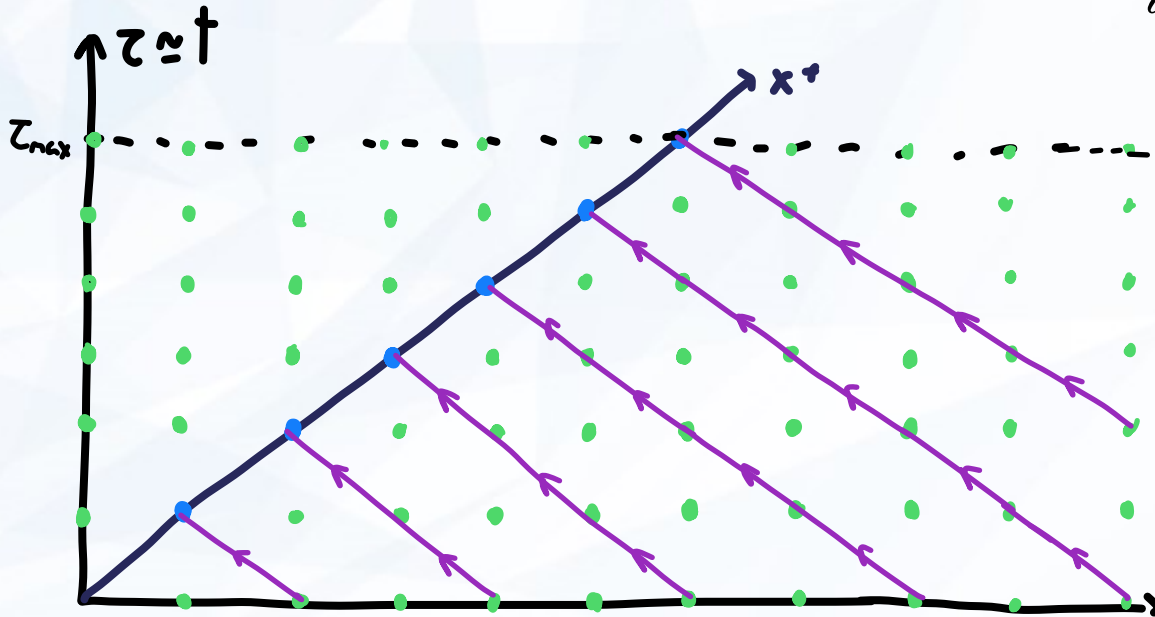
Gauge transformation operator

$$\mathcal{U}_{LC}^\dagger(x_{LC}) = P \exp \left\{ ig \int_{-\infty}^0 dx^- A_{temp}^+(x^+, x^-, y, z) \right\} \xrightarrow{\text{Discretizing}}$$

$$\mathcal{U}_{LC}^\dagger(x^+, y, z) = \prod_k \mathcal{U}_{LC}^\dagger(x^+, x_k^-, y, z)$$

where

$$\mathcal{U}_{LC}^\dagger(x^+, x_k^-, y, z) = \exp \left\{ \frac{za}{\tau^2} A_\eta^{latt}(x^+, x^-, y, z) \right\} U_x(x^+, x^-, y, z)$$

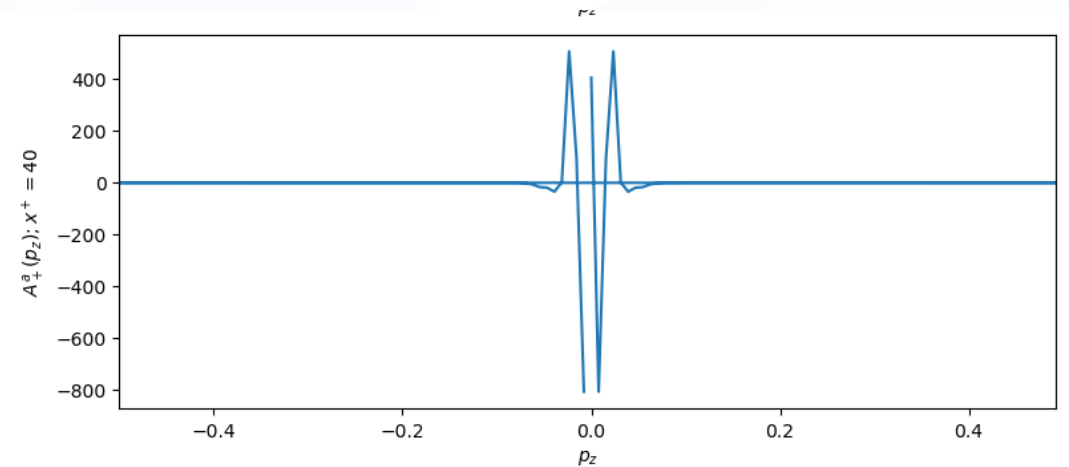
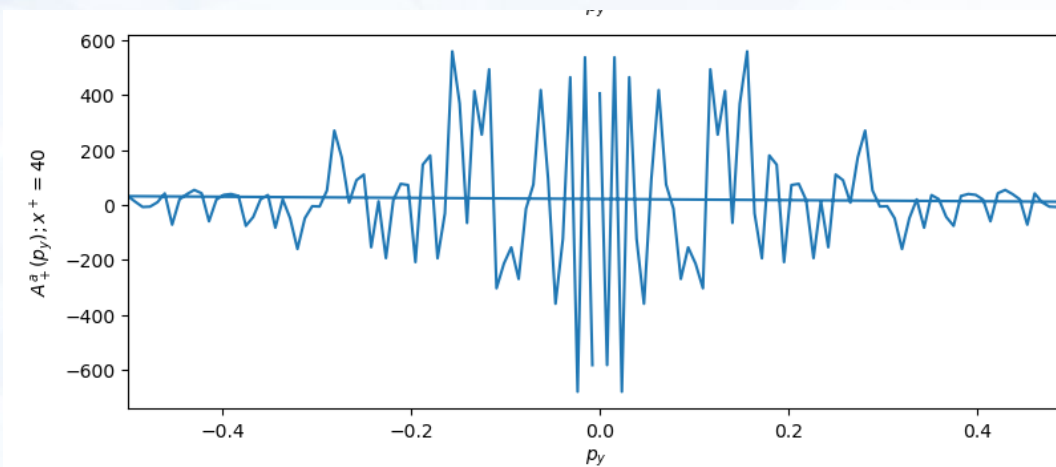
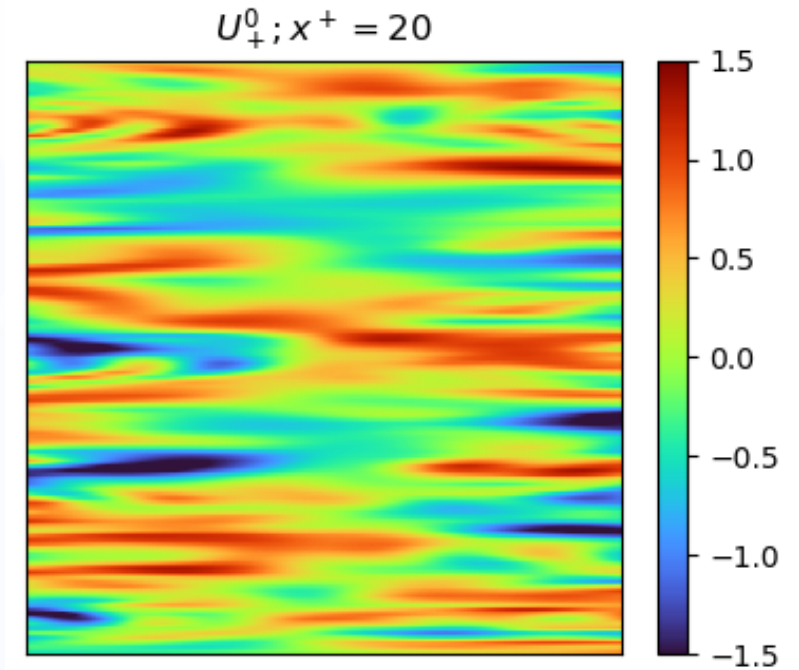


Only z dependence we are considering, restricted to jets at approximately mid-rapidity

Gauge transformation of the fields

$$U(x, y) \rightarrow U(x)U(x, y)U^\dagger(y) \longrightarrow U_{x, \hat{\mu}} \rightarrow \mathcal{U}_{x+\mu} U_{x, \hat{\mu}} \mathcal{U}_x$$

Transform U_+ link over the x^+ axis
 (perp components subeikonal)



4. Outlook

Future work



Adapt the jet evolution code to suit our analysis



Initialize the wave-package in such a way that it is insensitive to boundary conditions



Get results for both jet momentum broadening and energy loss



Compare our results to classical analysis and experimental data and check the validity of our approximations