14/02/23

Challenges in connecting GPDs to PDFs via exclusive heavy vector meson photoproduction in UPCs

Chris A. Flett

Université Paris-Saclay
CNRS, IJCLab,
Orsay, France

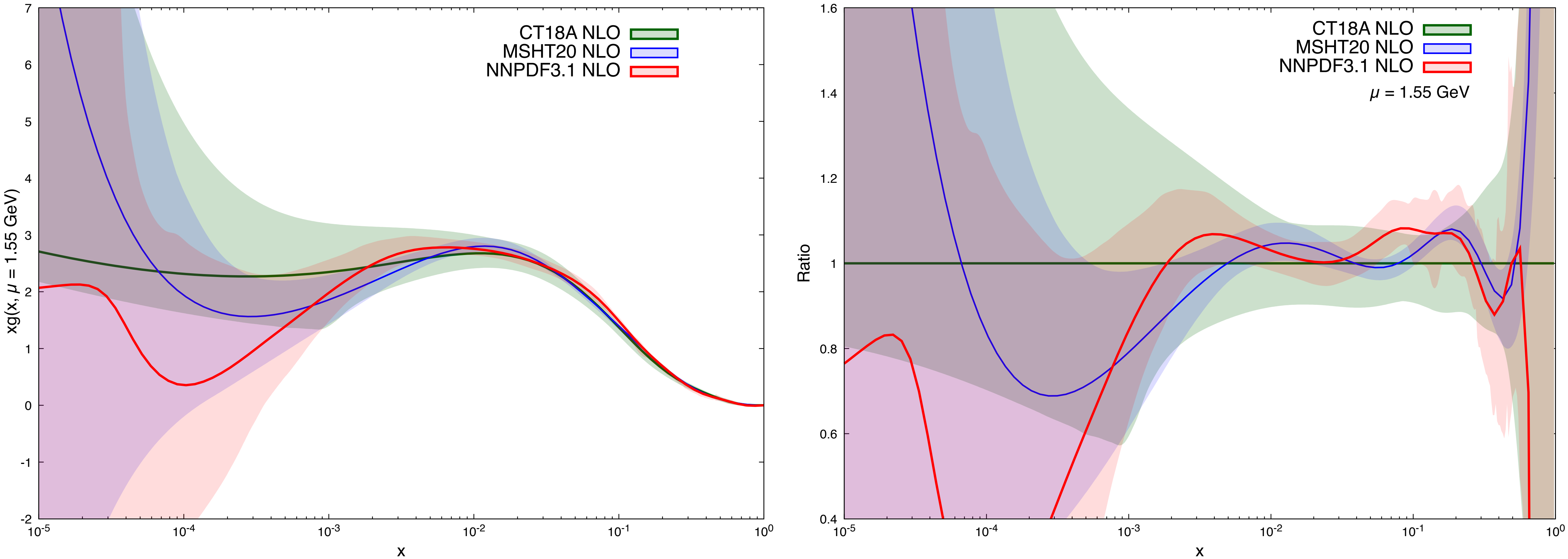
IJCLab Irène Joliot-Curie Laboratoire de Physique des 2 Infinis

Université Paris Cité

université PARIS-SACLAY

Introduction

- Inclusive processes do not well constrain small x/Regge limit domain of PDFs
- Exclusive processes offer sensitive probe of this domain but as of yet not included in global analyses PDF determination - why?
    1. Off forward kinematics imply sensitivity to *GPD* over conventional PDFs
    2. Scale dependence and stability of theoretical predictions



Introduction

- Inclusive processes do not well constrain small x/Regge limit domain of PDFs
- Exclusive processes offer sensitive probe of this domain but as of yet not included in global analyses PDF determination - why?
    1. Off forward kinematics imply sensitivity to *GPD* over conventional PDFs
    2. Scale dependence and stability of theoretical predictions

- As higher CM energies are realised at LHC, pushed towards small x domain, W ~ 1/x

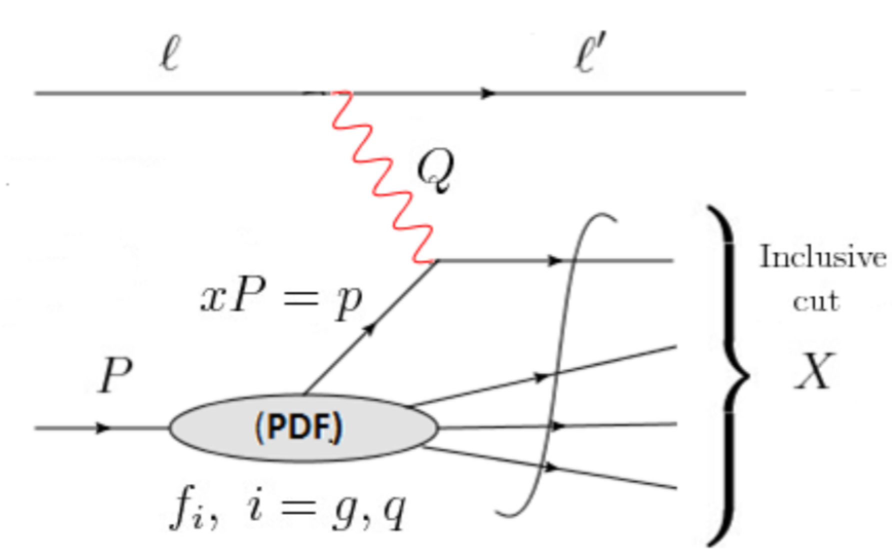
Ryskin 1993

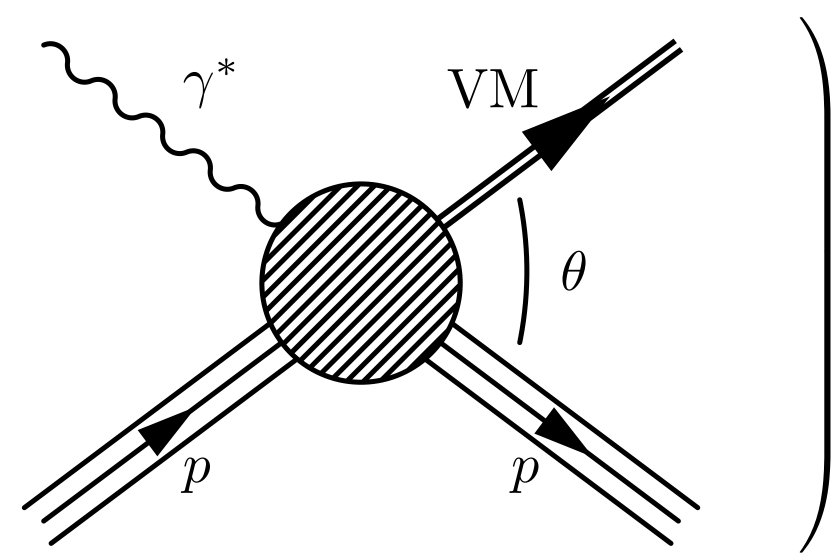
LLx exclusive J/psi production:

$$\frac{\mathrm{d}\sigma}{\mathrm{d}t}(\gamma^* p \to J/\psi p)\bigg|_{t=0} = \frac{\Gamma_{ee}^{J/\psi} M_{J/\psi}^3 \pi^3}{48\alpha_{\mathrm{em}}}\left[\frac{\alpha_s(\bar{Q}^2)}{\bar{Q}^4}\, xg(x,\bar{Q}^2)\right]^2\left(1+\frac{Q^2}{M_{J/\psi}^2}\right)$$

Inclusive - e.g. DIS included in global parton analyses

Exclusive - can we use the data?





Introduction

- Inclusive processes do not well constrain small x/Regge limit domain of PDFs
- Exclusive processes offer sensitive probe of this domain but as of yet not included in global analyses PDF determination - why?
    1. Off forward kinematics imply sensitivity to *GPD* over conventional PDFs
    2. Scale dependence and stability of theoretical predictions

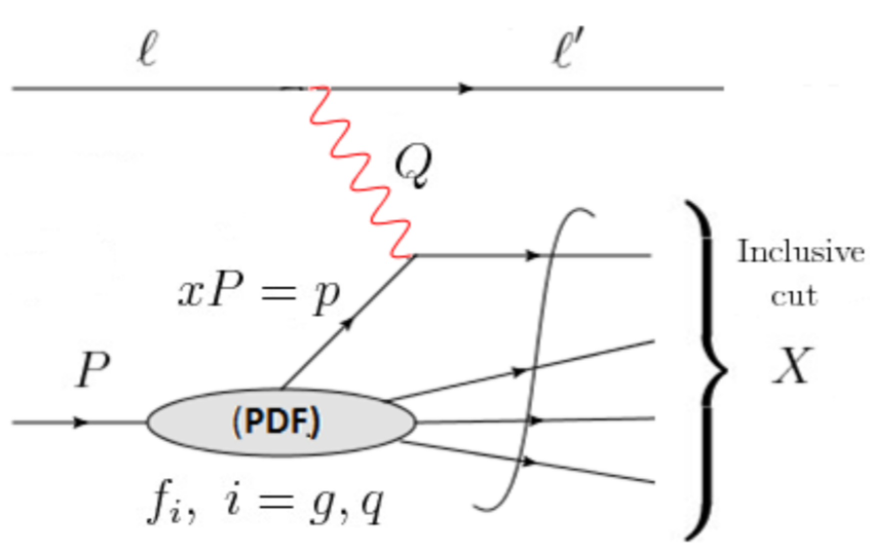
- As higher CM energies are realised at LHC, pushed towards small x domain, W ~ 1/x

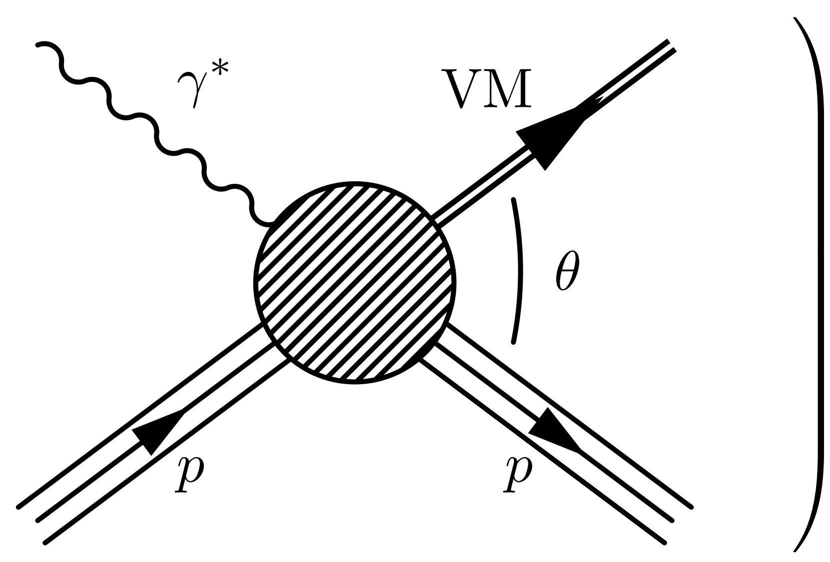
DLLA exclusive J/psi production:

$$\left.\frac{\mathrm{d}\sigma}{\mathrm{d}t}(\gamma^* p \to J/\psi p)\right|_{t=0} = \frac{\Gamma_{ee}^{J/\psi} M_{J/\psi}^3 \pi^3}{48\alpha_{\rm em}} \left[\frac{\alpha_s(\bar{Q}^2)}{\bar{Q}^4} \boxed{R_g} x g(x, \bar{Q}^2)\right]^2 \left(1 + \frac{Q^2}{M_{J/\psi}^2}\right)$$

Inclusive - e.g. DIS included in global parton analyses

Exclusive - can we use the data?

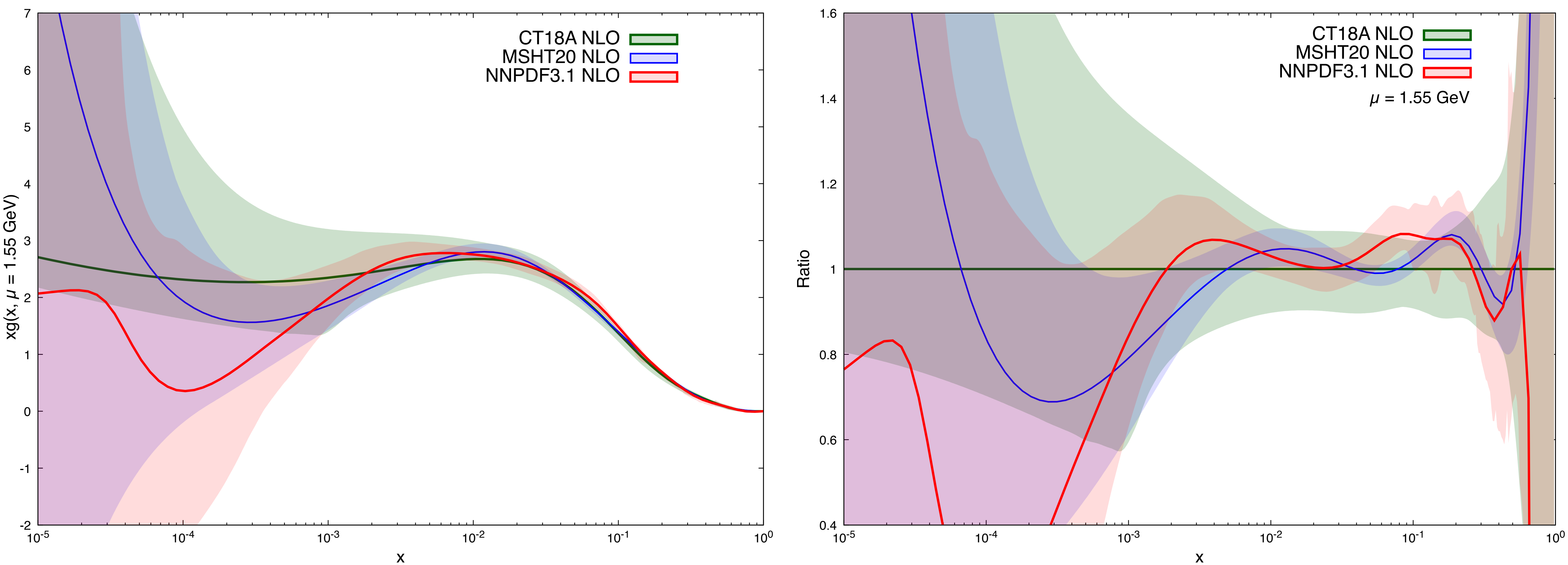




Introduction

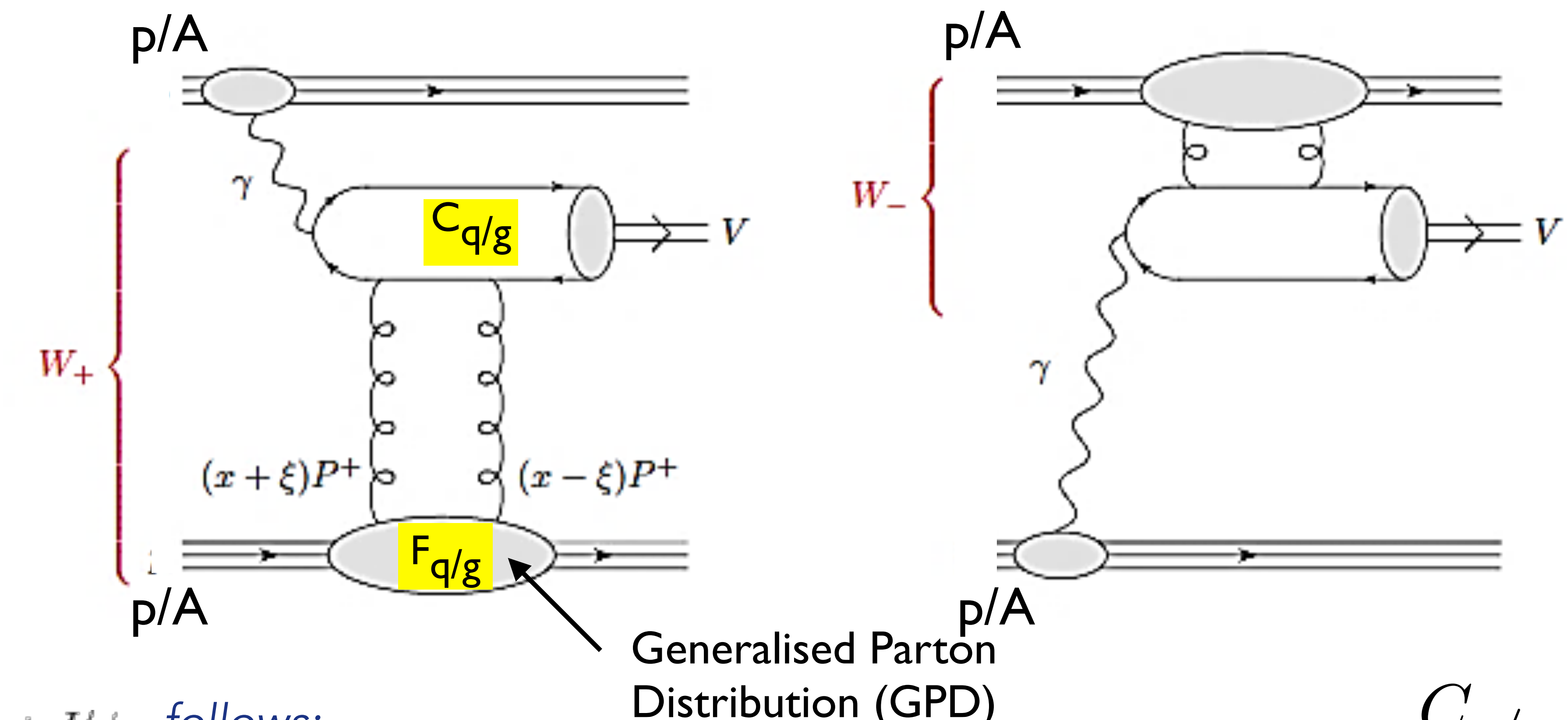
- Inclusive processes do not well constrain small x/Regge limit domain of PDFs
- Exclusive processes offer sensitive probe of this domain but as of yet not included in global analyses PDF determination - why?
    1. Off forward kinematics imply sensitivity to *GPD* over conventional PDFs
    2. Scale dependence and stability of theoretical predictions

This talk: how to counteract these problems and so allow exclusive J/psi data to probe gluon PDF down to $x \sim 3 \times 10^{-6} \quad \& \quad \mu = O(M_{J/\psi}/2)$



General Set up and Framework

Exclusive J/psi photoproduction in p+p (A+A) UPC collisions in collinear factorisation



Setup for $\gamma p \to J/\psi p$ follows:
Ivanov, Schäfer, Szymanowski, Krasnikov, 04

- Factorisation: $F_{q/g} \otimes C_{q/g} \otimes \phi^V_{Q\bar{Q}}$
- Leading zeroth order term in rel. velocity (NRQCD)
- Colour singlet exchange between hard and soft sectors

$$A \propto \int_{-1}^{1} \mathrm{d}x \left[C_g(x,\xi)F_g(x,\xi) + \sum_{q=u,d,s} C_q(x,\xi)F_q(x,\xi) \right]$$

$C_{q/g}$

Photoproduction:

- hep-ph/0401131

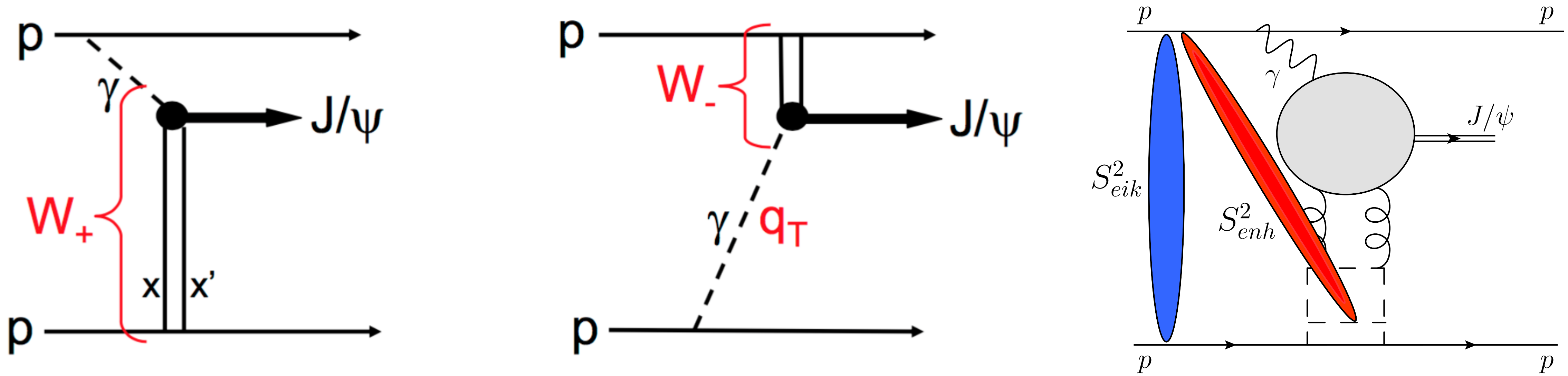
Ivanov, Schäfer, Szymanowski, Krasnikov, 04

Electroproduction:

- arXiv:1903.00171
- arXiv:2105.07657

Chen, Qiao, 19
CAF, Gracey, Jones, Teubner, 21

General Set up and assumptions



LHCb data

$$\frac{d\sigma(pp)}{dy} = S^2(W_+)\left(k_+\frac{dn}{dk_+}\right)\sigma_+(\gamma p) + S^2(W_-)\left(k_-\frac{dn}{dk_-}\right)\sigma_-(\gamma p)$$

survival probability factors

LHCb 'data'

photon flux

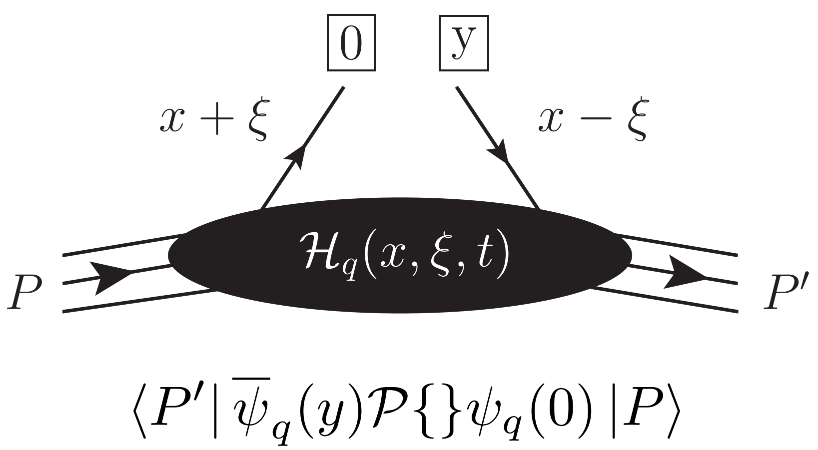
HERA gives W-

$$W^2_\pm = M_{J/\psi}\sqrt{s}e^{\pm|y|} \quad \Rightarrow x_\pm = \begin{cases} 10^{-5} \\ 0.02 \end{cases} \quad \text{at } y=4,\ \sqrt{s}{=}13\ \text{TeV}$$

GPDs and the Shuvaev transform

GPDs generalise PDFs: outgoing/incoming partons carry different momentum fractions

Müller 94; Radyushkin 97; Ji 97



Shuvaev: Relates GPDs to PDFs at small x under physically motivated assumptions c.f analyticity

Shuvaev 99 Martin et al. 09

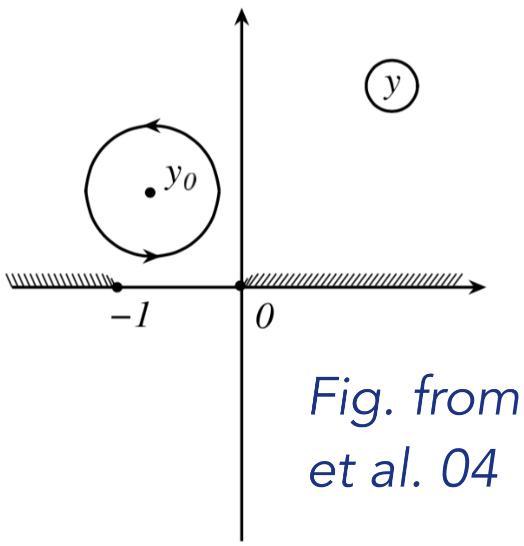


Fig. from Ivanov et al. 04

Idea: Conformal moments of GPDs = Mellin moments of PDFs
(up to corrections of O(xi^2) @ LO and O(xi) @ NLO)

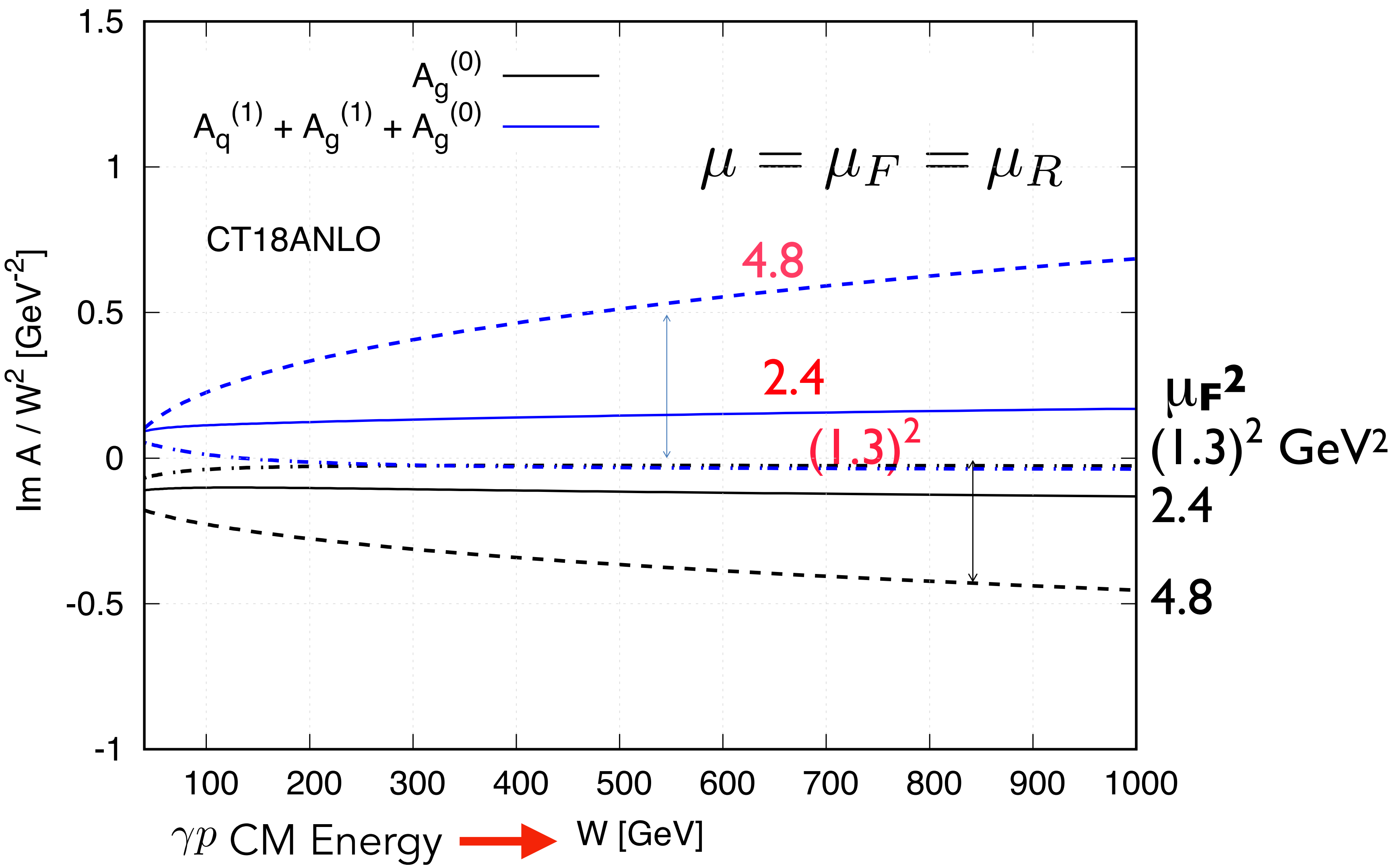
- Construct GPD grids in multidimensional parameter space x, xi/x, qsq with forward PDFs from LHAPDF
- Costly computationally due to slowly converging double integral transform
- Regge theory considerations => Shuvaev transform valid in space-like (DGLAP) region only. In time-like (ERBL) region imaginary part of coefficient function is zero

Stability of prediction I

NLO in MSbar scheme D. Ivanov, et al., hep-ph/0401131

A. Bad perturbative convergence **$|NLO_{correctn.}| > |LO|$ and**

B. Strong dependence on scale μ_F **opp. sign**



NB: Plots generated using existing global partons. Here, CT18ANLO

Can do better… resummation of logarithmically enhanced contributions at low x!

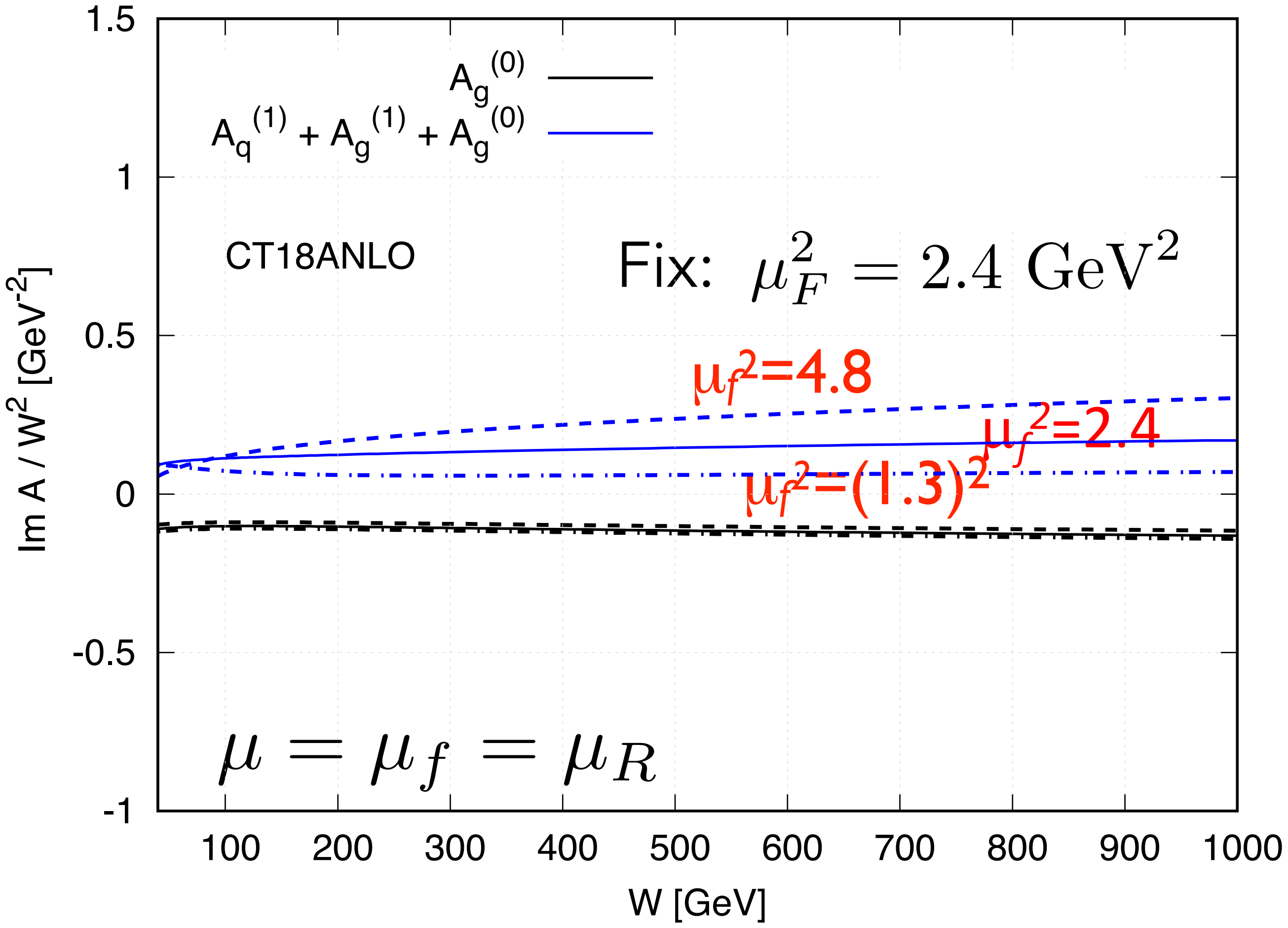
Stability of prediction II

'Scale Fixing'

`Optimal' factorisation scale $\mu_F = m$ eliminates large logs at NLO
Jones et al., 1507.06942

Resummation of $(\alpha_s \ln(1/\xi) \ln(\mu_F/m))^n$

terms into LO PDF, leaving remnant NLO coefficient and residual, μ_f, scale dependence



$$A(\mu_f) = C^{LO} \times GPD(\mu_F) + C^{NLO}(\mu_F) \times GPD(\mu_f)$$

Look for another sizeable correction that can reduce variations further
-> implementation of a `**Q0**' cut

Stability of prediction II

'Scale Fixing'

`Optimal' factorisation scale $\mu_F = m$
eliminates large logs at NLO

Jones et al., 1507.06942

Resummation of $(\alpha_S \ln(1/\xi)\ \ln(\mu_F/m))^n$

terms into LO PDF, leaving remnant
NLO coefficient
and residual, μ_f , scale dependence

NLO High-energy limit:

$$\mathcal{M} \approx \frac{-4\,i\,\pi^2\sqrt{4\pi\alpha}\,e_q(e_V^* e_\gamma)}{N_c\,\xi}\left(\frac{\langle O_1\rangle_V}{m^3}\right)^{1/2} \times$$

$$\times\left[\alpha_S(\mu_R)F^g(\xi,\xi,t) + \frac{\alpha_S^2(\mu_R)N_c}{\pi}\ln\left(\frac{m^2}{\mu_F^2}\right)\int_\xi^1 \frac{dx}{x}F^g(x,\xi,t)\right.$$

$$\left.+\frac{\alpha_S^2(\mu_R)C_F}{\pi}\ln\left(\frac{m^2}{\mu_F^2}\right)\int_\xi^1 dx\,\left(F^{q,S}(x,\xi,t) - F^{q,S}(-x,\xi,t)\right)\right]$$

$$A(\mu_f) = C^{LO} \times GPD(\mu_F) + C^{NLO}(\mu_F) \times GPD(\mu_f)$$

Look for another sizeable correction that can reduce variations further
-> implementation of a **`Q0'** cut

Stability of prediction II

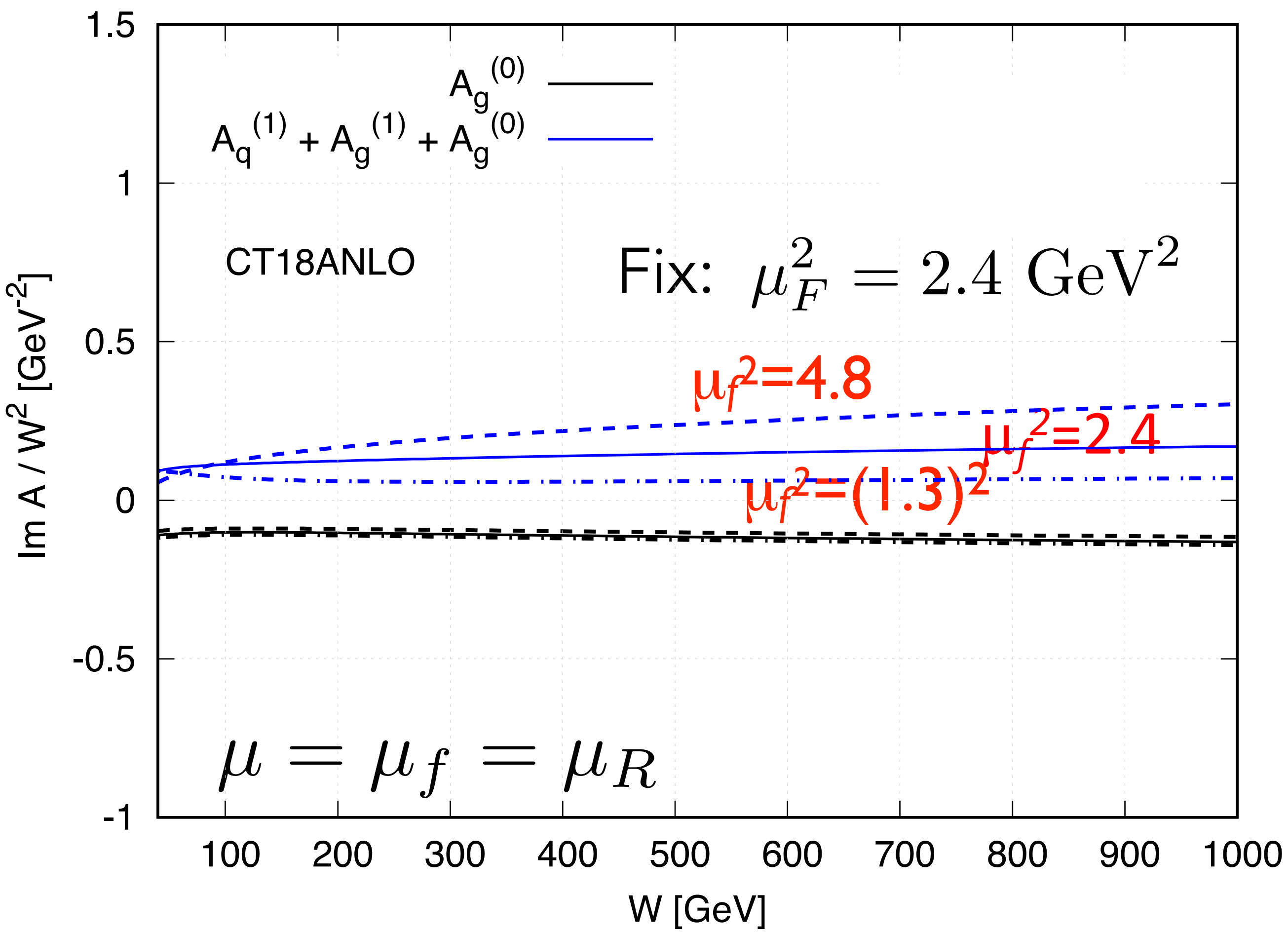
'Scale Fixing'

\`Optimal' factorisation scale $\mu_F = m$ eliminates large logs at NLO

Jones et al., 1507.06942

Resummation of $(\alpha_S \ln(1/\xi) \ln(\mu_F/m))^n$

terms into LO PDF, leaving remnant NLO coefficient and residual, μ_f, scale dependence



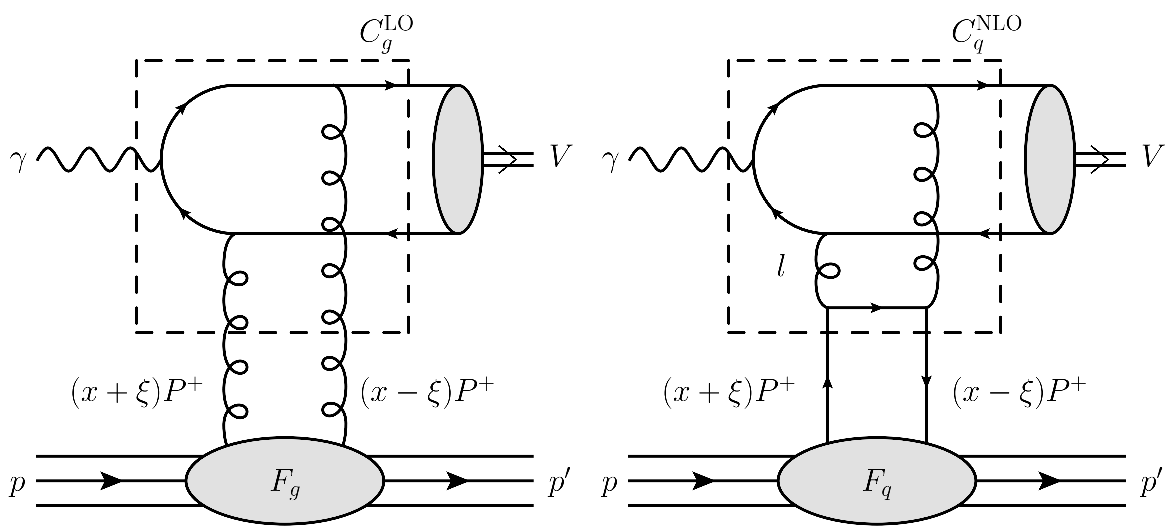
$$A(\mu_f) = C^{LO} \times GPD(\mu_F) + C^{NLO}(\mu_F) \times GPD(\mu_f)$$

Look for another sizeable correction that can reduce variations further

-> implementation of a **\`Q0'** cut

Stability of prediction III

`Q0' cut Jones et al., 1610.02272



Fundamentally ubiquitous* and typically power suppressed, but sizeable here

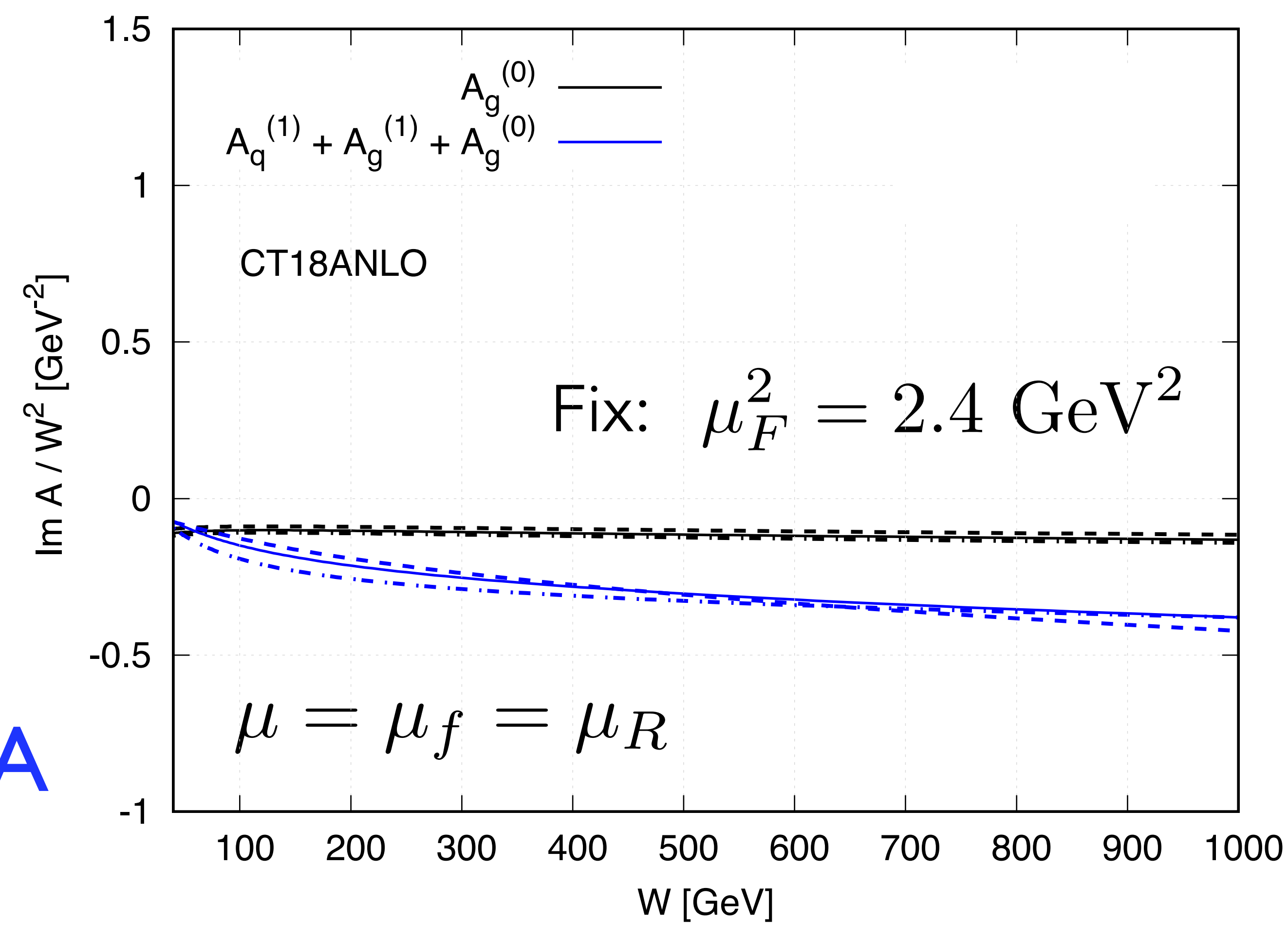
$$\mathcal{O}(Q_0^2/\mu_F^2)$$

How do these predictions compare with the data at HERA and LHCb?

Subtract DGLAP contribution

NLO (| ℓ^2 | < Q_0^2)

from known NLO MSbar coefficient function to avoid a double count with input GPD at Q_0.

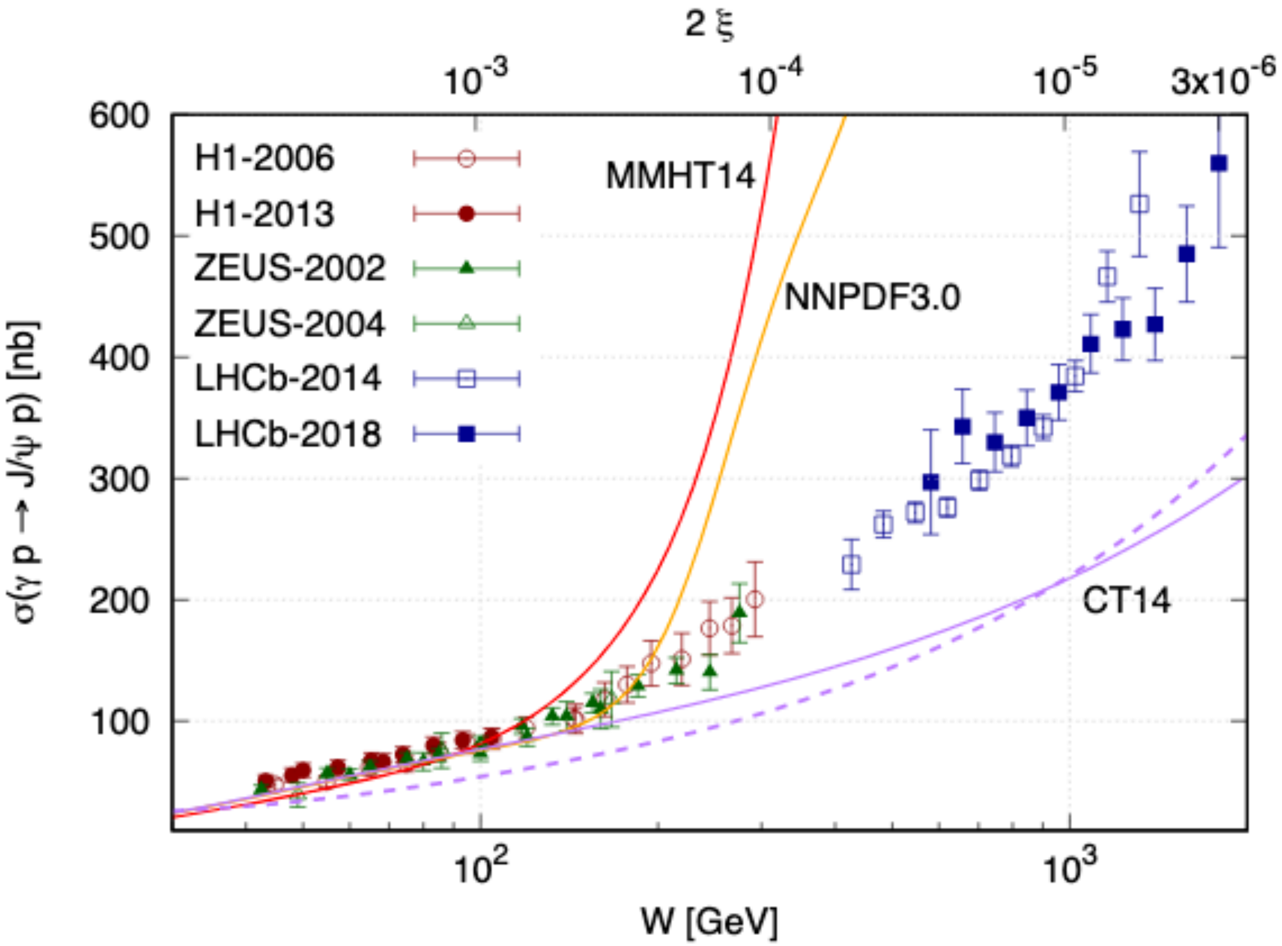


*see 1912.09304 for procedure applied to inclusive DIS and Drell-Yan production

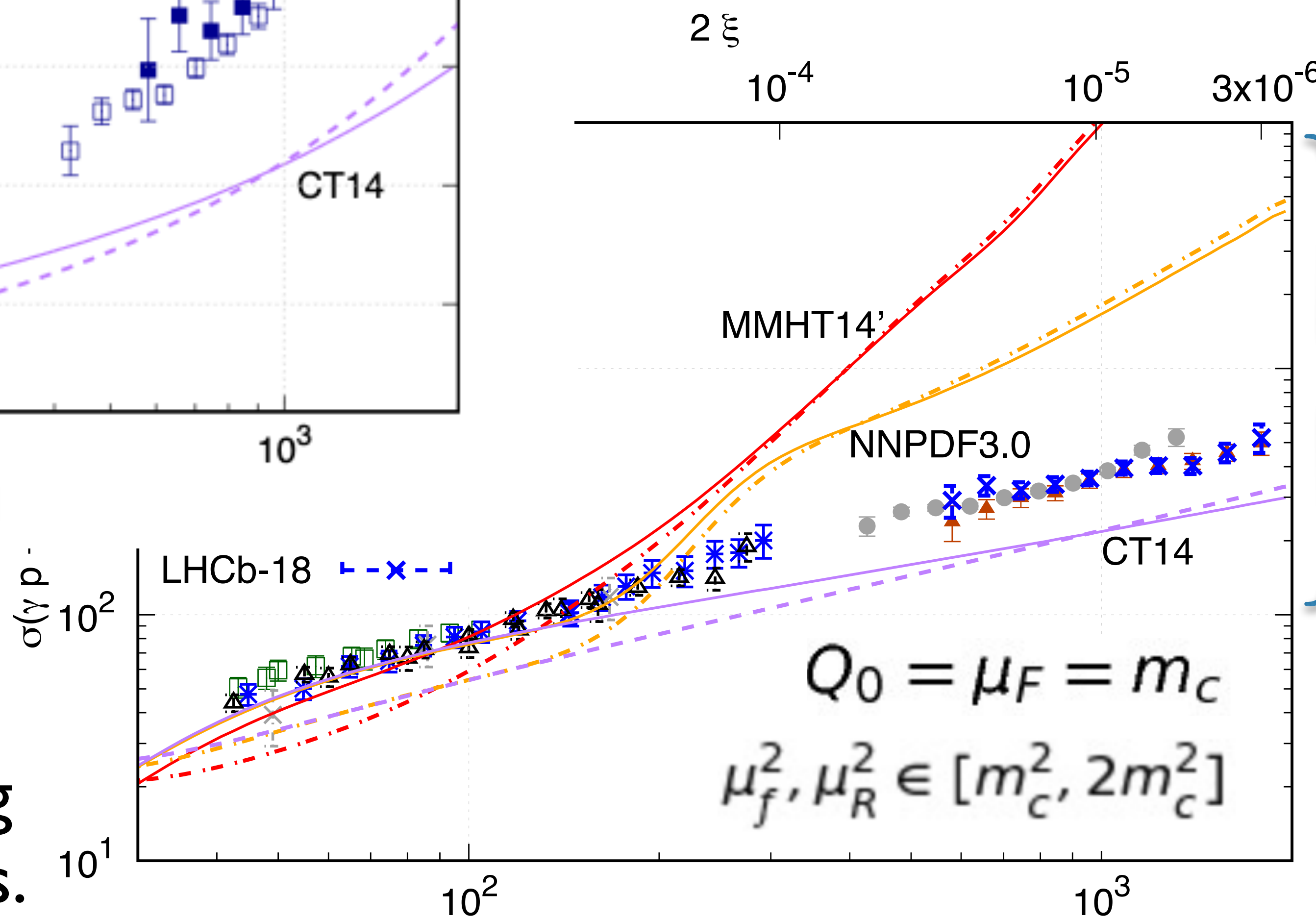
Towards the bigger picture

Plots demonstrates good scale stability of our NLO predictions in LHCb regime

Predictions at optimal scale (solid) agree better with HERA data



CAF, Jones, Martin, Ryskin, Teubner, 1907.06471 & 1908.08398



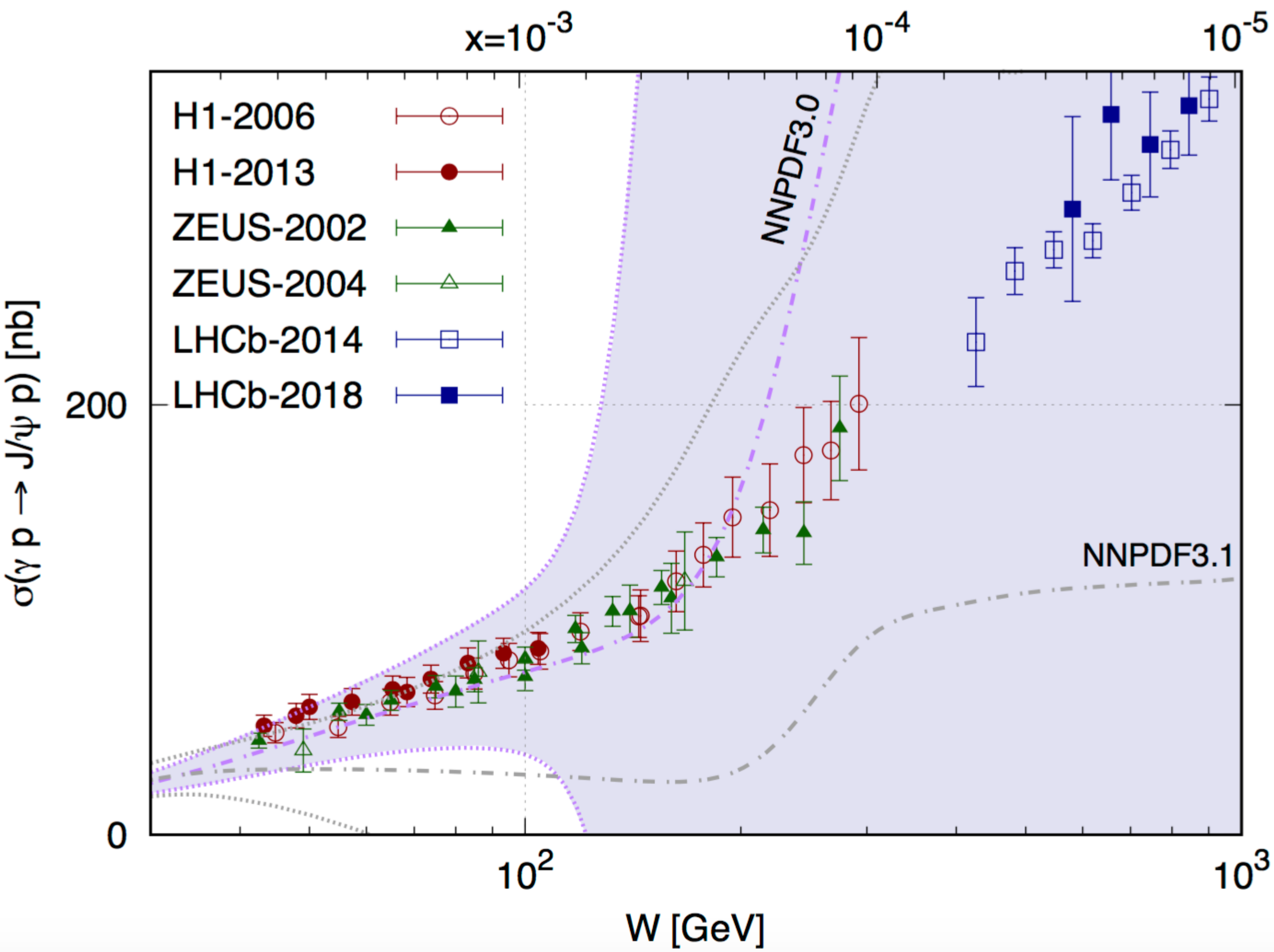
Diversity between predictions based on current global PDFs in unconstrained phase space -> important message

Repeat NB: Convoluting with existing global partons. Here, MMHT14, NNPDF3.0 & CT14

$$\frac{\mathrm{Re}\mathcal{M}}{\mathrm{Im}\mathcal{M}} \sim \frac{\pi}{2}\lambda = \frac{\pi}{2}\frac{\partial \ln \mathrm{Im}\mathcal{M}/W^2}{\partial \ln W^2} \quad \text{with} \quad \mathcal{M} \sim x^{-\lambda}$$

Error budgets: errors due to parameter variations in global fits >> experimental uncertainty and scale variations in the theoretical result

…… exclusive data now in a position to readily improve global analyses

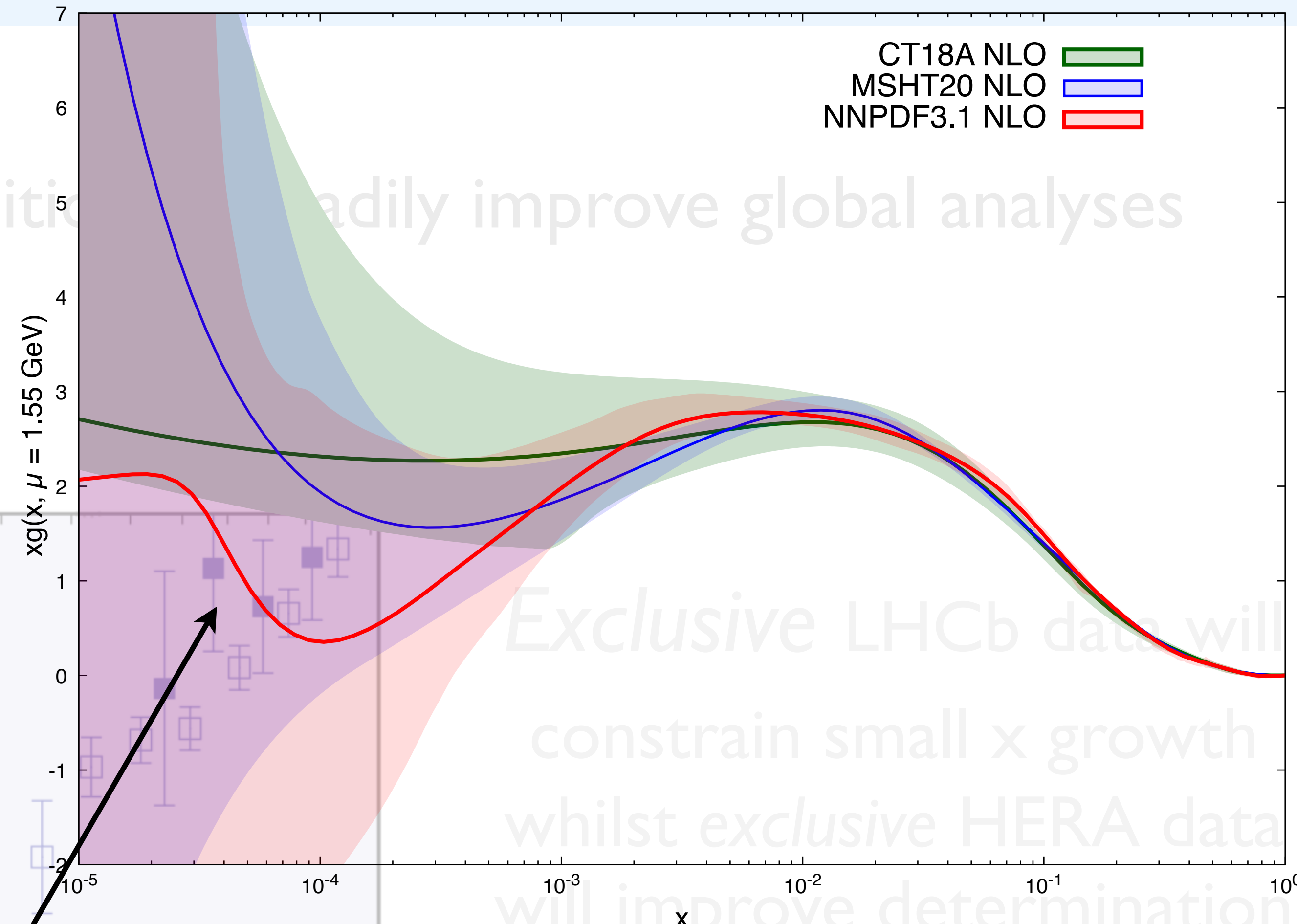


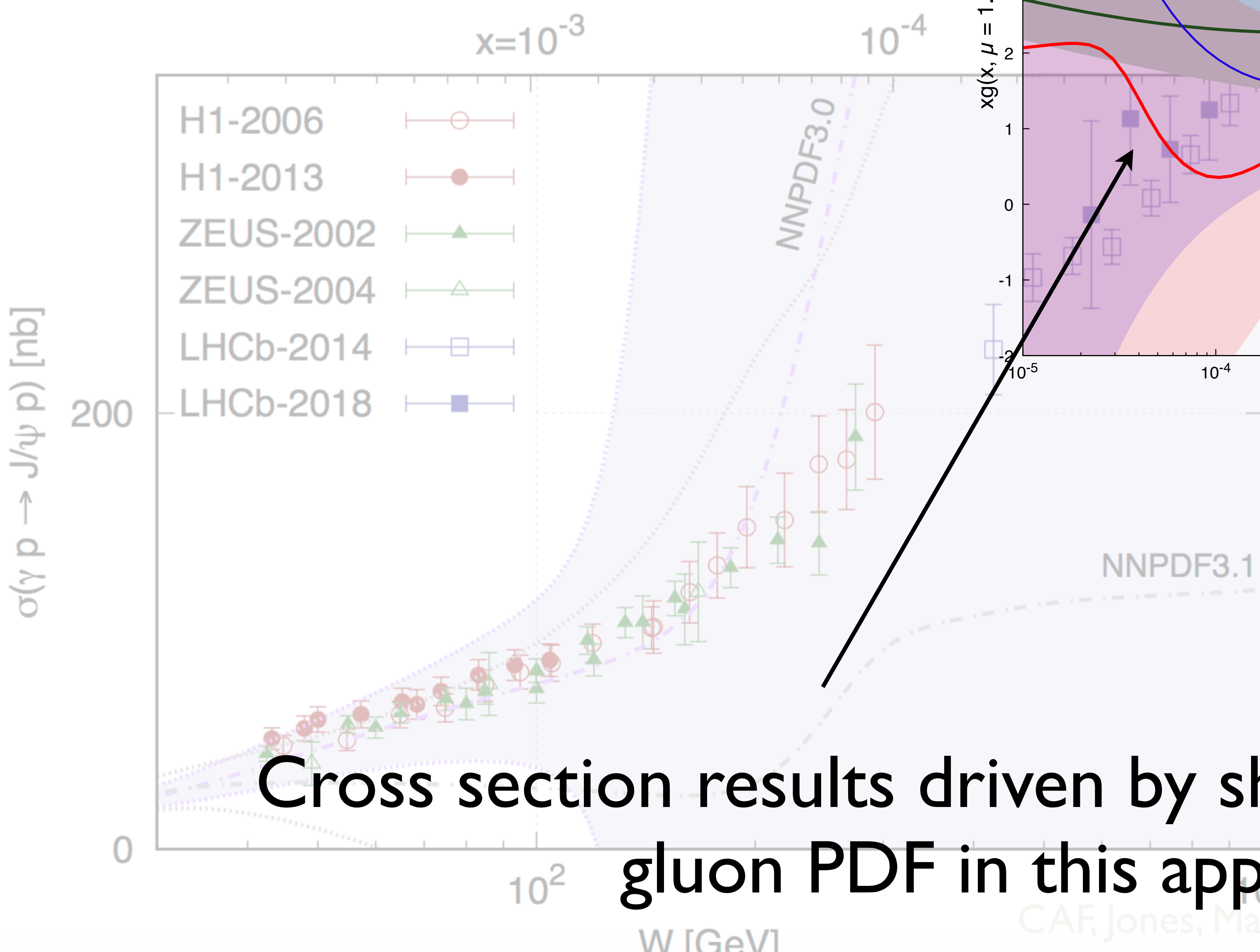
Exclusive LHCb data will constrain small x growth whilst *exclusive* HERA data will improve determination of partons in regime with data constraints already from diffractive DIS HERA data

CAF, Jones, Martin, Ryskin, Teubner, 1907.06471, 1908.08398

Error budgets: errors due to parameter variations in global fits >> experimental uncertainty and scale variations in the theoretical result

…… exclusive data now in a positi adily improve global analyses





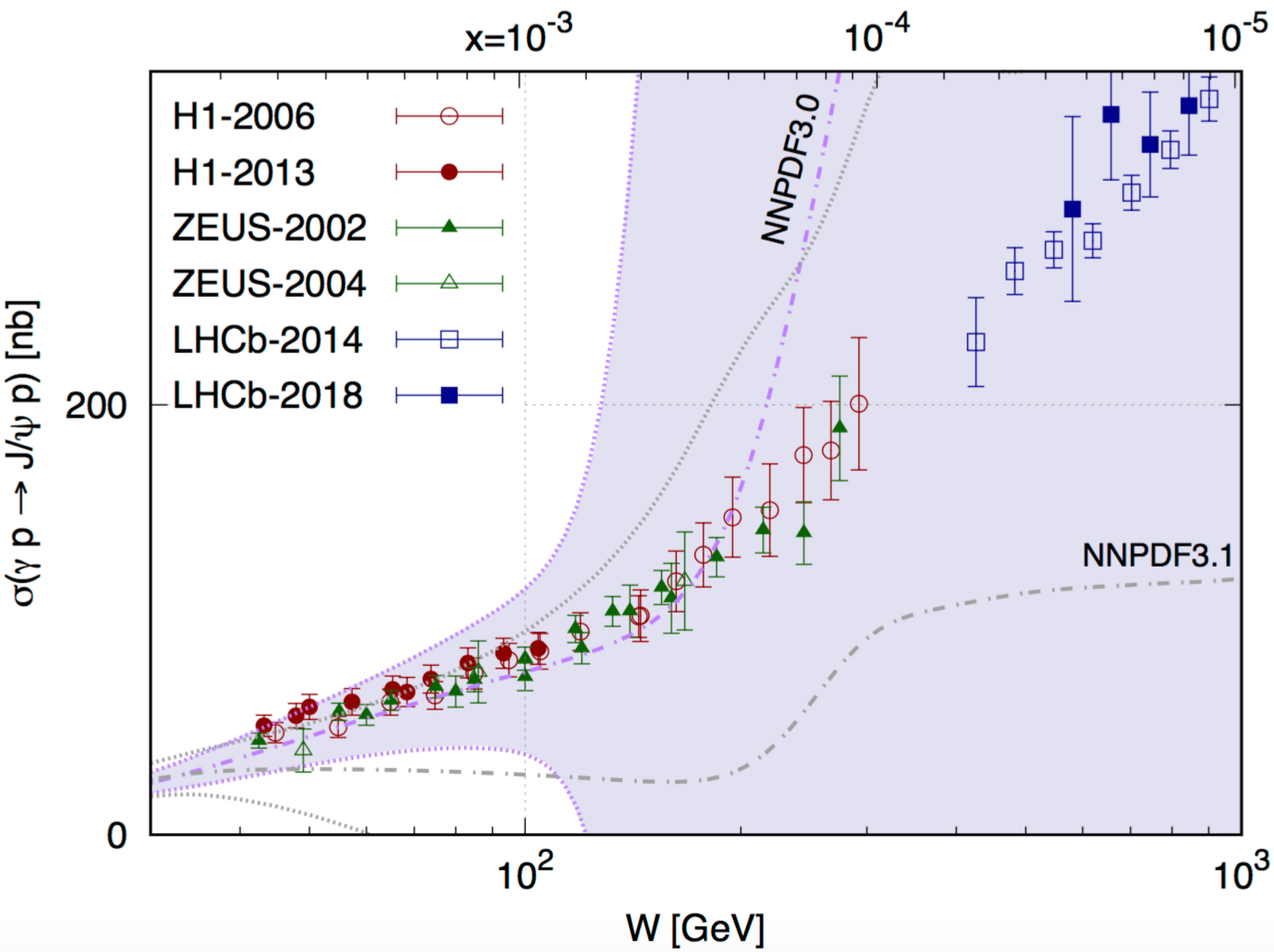
Exclusive LHCb data will constrain small x growth whilst *exclusive* HERA data will improve determination of partons in regime with data constraints already from diffractive DIS HERA data

Cross section results driven by shape/magnitude of gluon PDF in this approach

CAF, Jones, Martin, Ryskin, Teubner, 1907.06471, 1908.08398

Error budgets: errors due to parameter variations in global fits >> experimental uncertainty and scale variations in the theoretical result

…… exclusive data now in a position to readily improve global analyses



Exclusive LHCb data will constrain small x growth whilst *exclusive* HERA data will improve determination of partons in regime with data constraints already from diffractive DIS HERA data

CAF, Jones, Martin, Ryskin, Teubner, 1907.06471, 1908.08398

Extraction of low x gluon PDF via exclusive J/psi

Left

Approach 1: Fit a low x gluon PDF ansatz to the data

Right

Approach 2: Bayesian reweight current global PDF analyses

	λ	n	$\chi^2_{\rm min}$	$\chi^2_{\rm min}$/d.o.f
NNPDF3.0	0.136	0.966	44.51	1.04
MMHT14	0.136	1.082	47.00	1.09
CT14	0.132	0.946	48.25	1.12

$$xg^{\rm new}(x,\mu_0^2) \;=\; nN_0\,(1-x)\,x^{-\lambda}$$

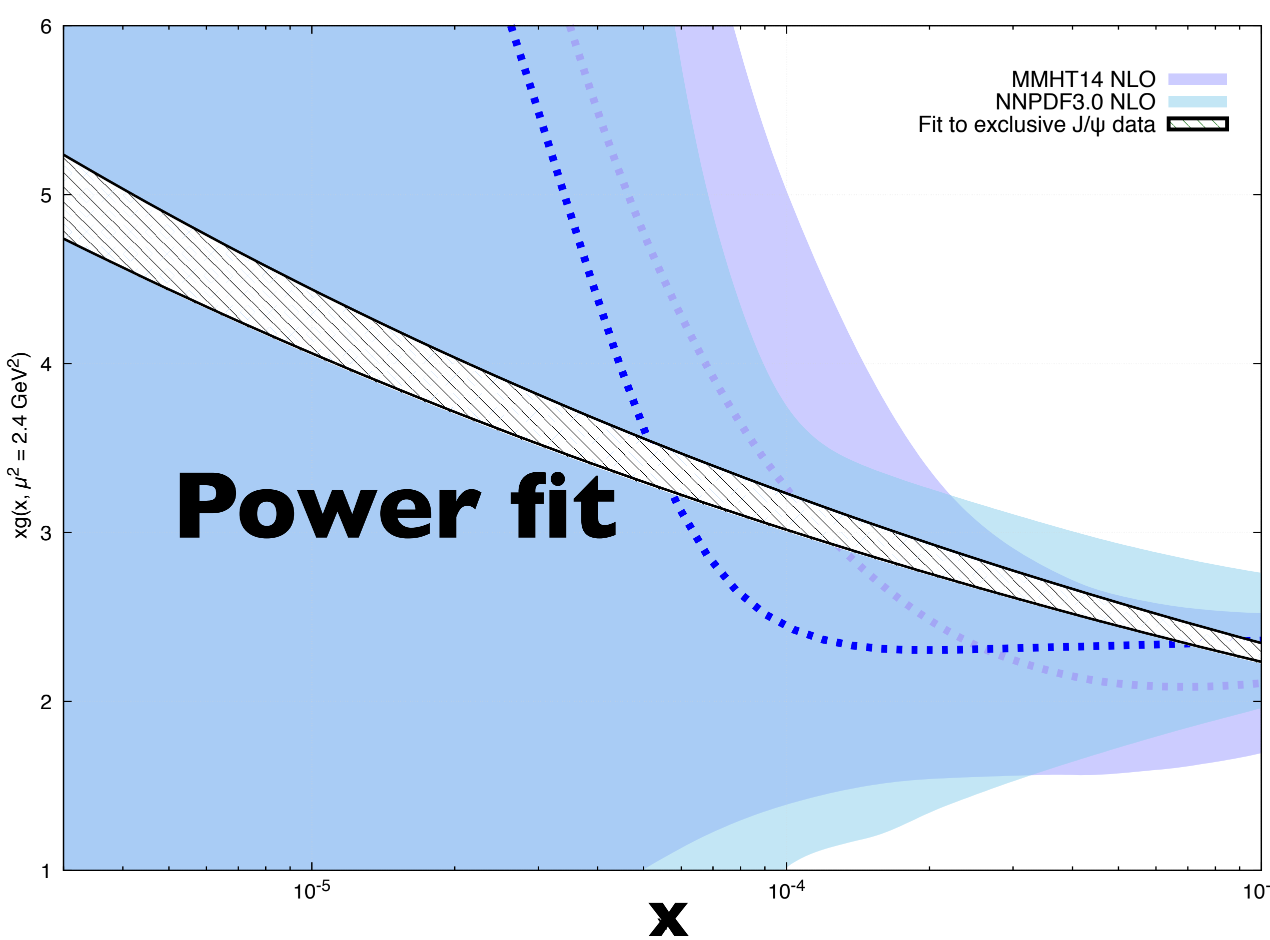
(1-x) factor for validity with b.c. of Shuvaev transform

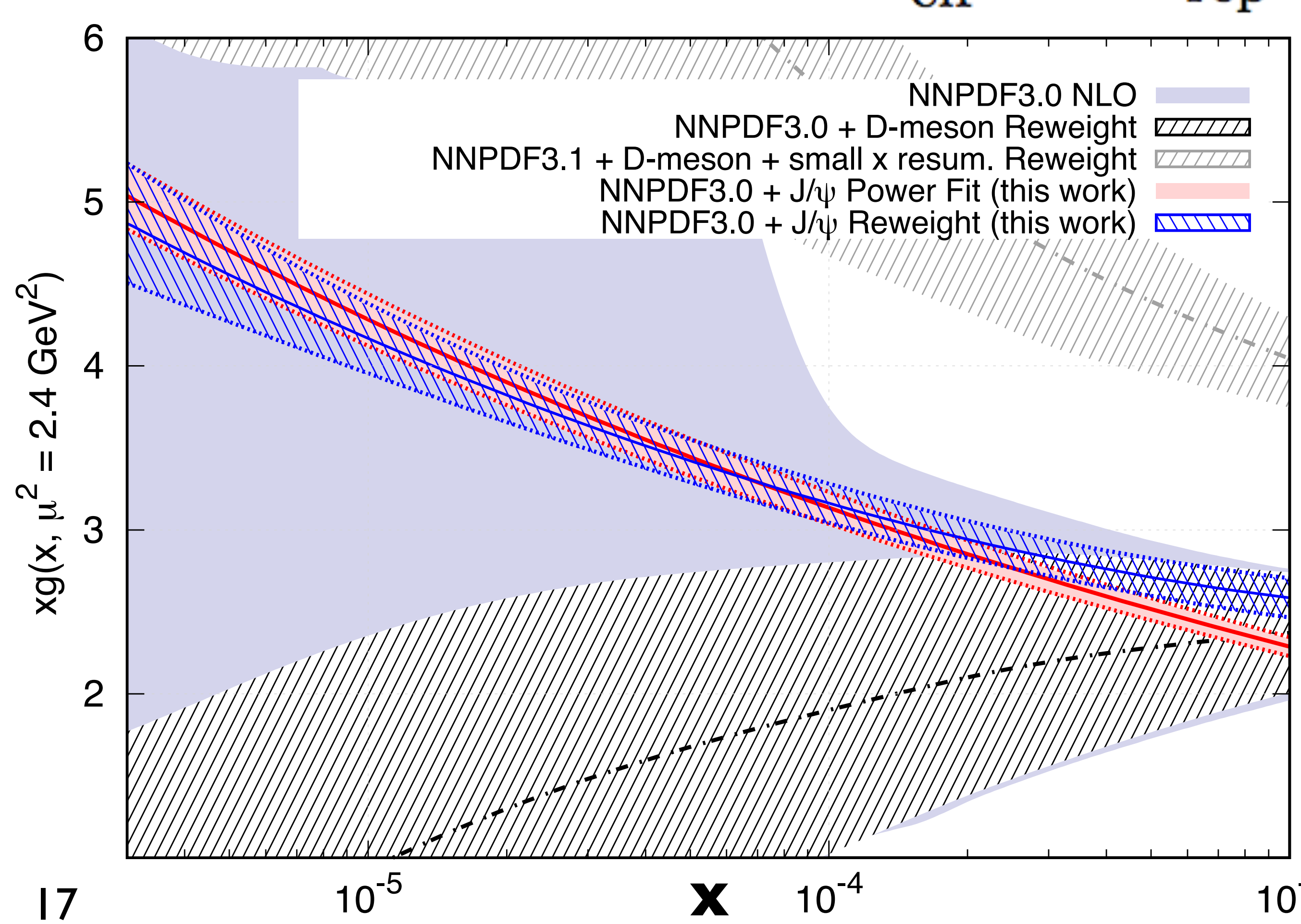
lambda = 0.136 +/- 0.006

n = 0.966 +/- 0.025

CAF, Martin, Ryskin, Teubner, 2006.13857

$N_{\rm eff} \ll N_{\rm rep}$





Left

Approach 1: Fit a low x gluon PDF ansatz to the data

Right

Approach 2: Bayesian reweight current global PDF analyses

	λ	n	$\chi^2_{\min}$	$\chi^2_{\min}$/d.o.f
NNPDF3.0	0.136	0.966	44.51	1.04
MMHT14	0.136	1.082	47.00	1.09
CT14	0.132	0.946	48.25	1.12

$$xg^{\text{new}}(x,\mu_0^2) \;=\; nN_0\,(1-x)\,x^{-\lambda}$$

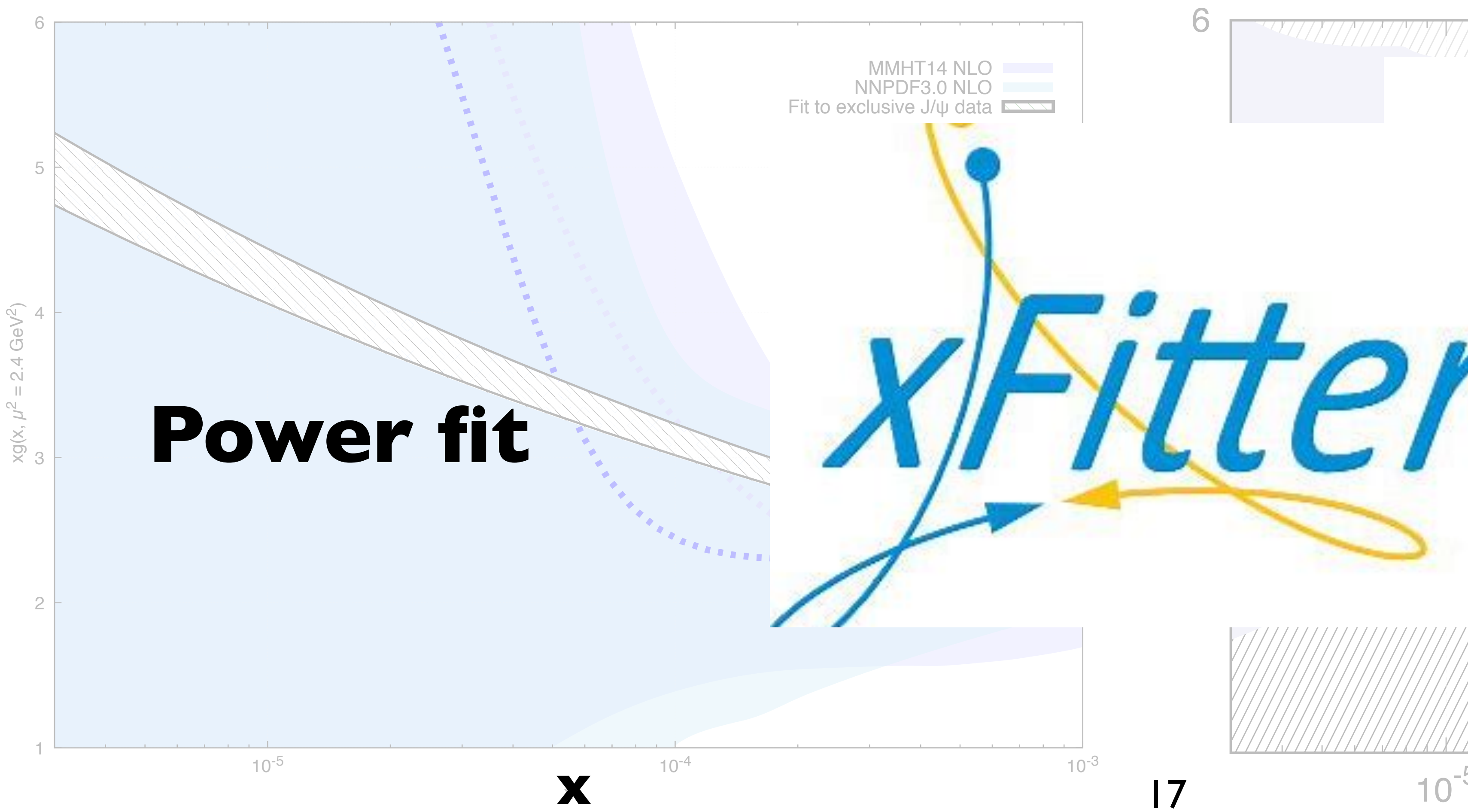
(1-x) factor for validity with b.c. of Shuvaev transform

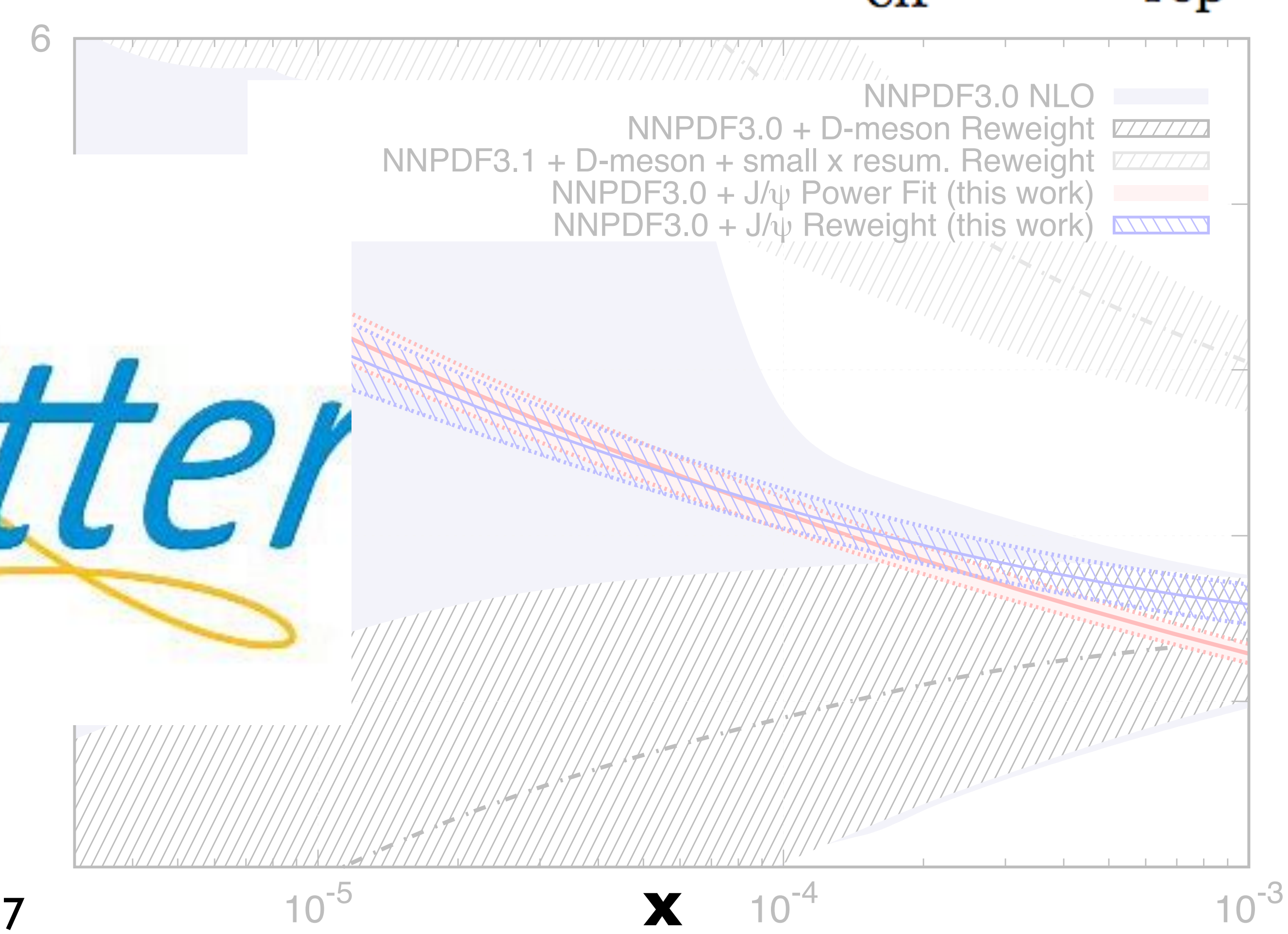
lambda = 0.136 +/- 0.006

n = 0.966 +/- 0.025

CAF, Martin, Ryskin, Teubner, 2006.13857

$N_{\text{eff}} \ll N_{\text{rep}}$





Summary

- Conventional MSbar NLO coll. fact. result unreliable and unstable
- Systematic taming via 'Q0' cut and resummation of large logarithmic contributions collectively reduce wild scale variations
- Predictions at cross section level have a good stability and central values in agreement of data within 1sigma error bands
- Large difference between predictions based on global PDFs in LHCb regime
- Reconciliation at HERA energies -> motivated a low x and low scale gluon PDF extraction via two approaches and shown to be consistent
- Upshot: In a position to finally use exclusive J/psi data in a global fitter framework. Reweighting and profiling fit exercises in progress within the xFitter framework…

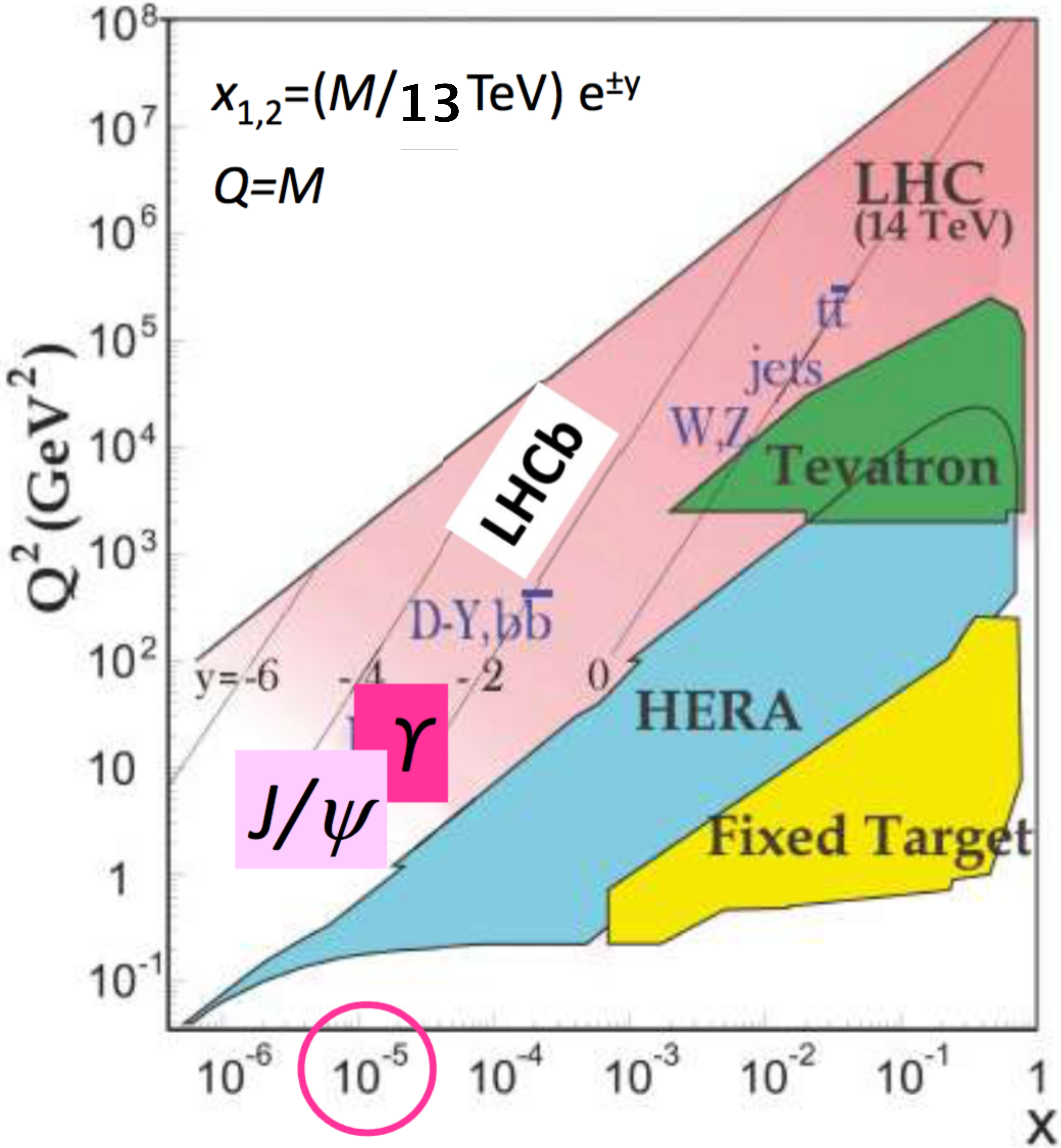
Finally..

Proposals for discussion

- Alternate small-x resummation
- Ratios of UPC cross sections with various colliding species - utility of possible O-O UPCs
- General comments on photon fluxes in UPCs
- Impact of non-relativistic corrections on charmonium wave function - need for uniform consensus on their relevancy

Thank you

Kinematic coverage

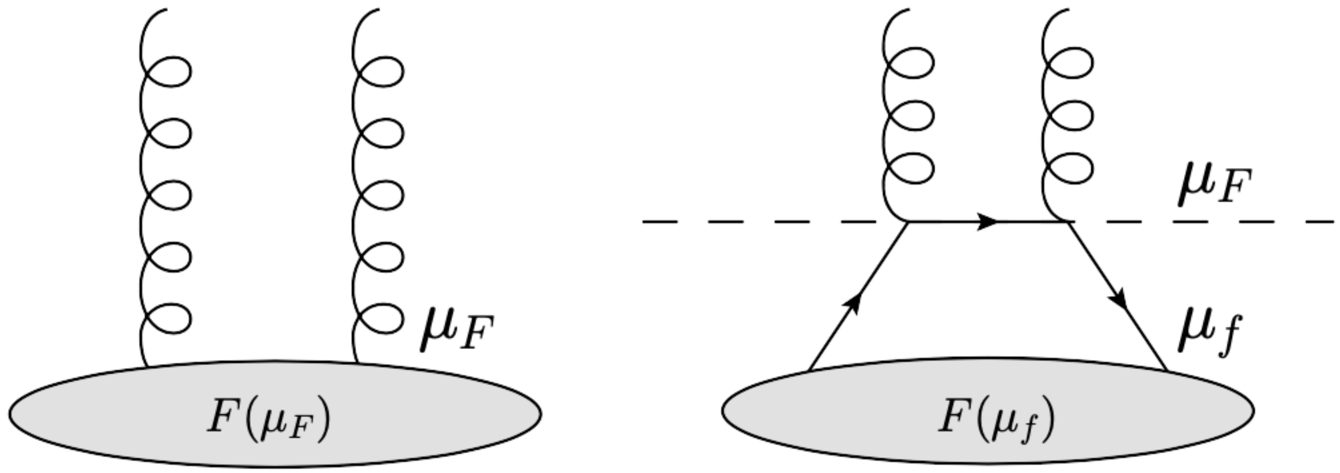


LHCb with $2 < y < 4.5$ can probe gluon down to $x \sim 10^{-5}$

exclusive J/ψ, Υ
[$Q=M_V/2$ (scale)]

Why are these LHCb data not used in global PDF fits ??

Treatment of double logarithmic contribution



Ideology: Use scale shifting to find optimal scale that removes the largest contribution from the NLO correction *

At fact. scale. μ_f , quark contribution is part of NLO hard matrix element

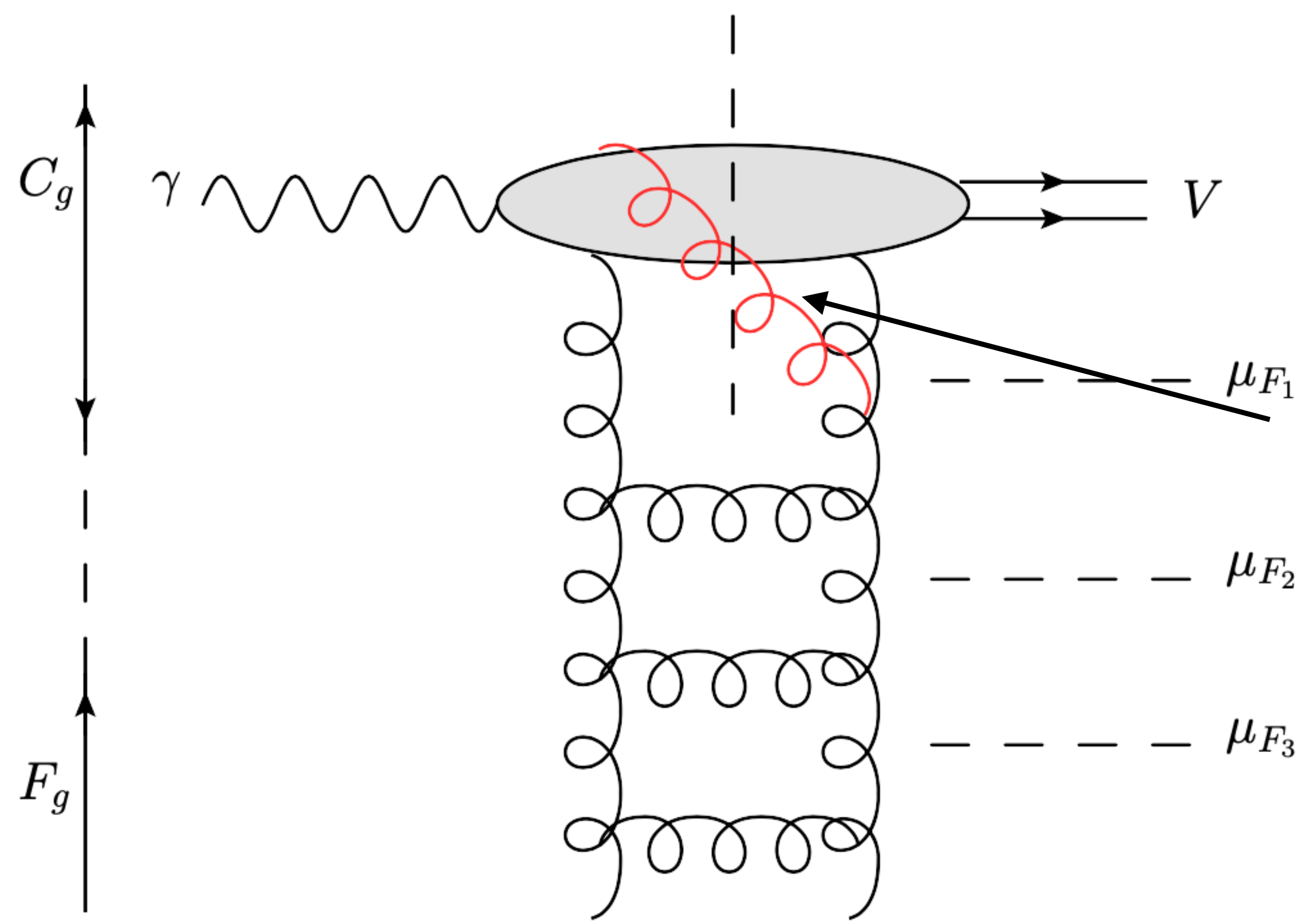
At fact. scale μ_F, absorbed quark contribution into LO result

Effect of scale change driven by (generalised, skewed) DGLAP evolution:

$$A^{(0)}(\mu_f) = \left(C^{(0)} + \frac{\alpha_s}{2\pi} \ln\left(\frac{\mu_f^2}{\mu_F^2}\right) C^{(0)} \otimes V \right) \otimes F(\mu_F)$$

* At small xi, this is the double logarithmic contribution ~ln(1/xi) ln(muF^2/mc^2)

Treatment of double logarithmic contribution



The red gluon cannot be resummed in this scale shifting approach and so will always be treated as part of the higher order correction

Choice muF = mc ‘resums’ the gluon ladder contributions, enhanced by this double logarithmic contribution. They are intrinsically resummed within the kt factorisation framework* and here by judicious choice of factorisation scale

* But kt fact. framework treats only a *subset* of NLO corrections, those belonging to equivalence class of gluon-ladder diagrams

Shuvaev Transform

Full Transform:

$$\mathcal{H}_q(x,\xi) = \int_{-1}^{1} \mathrm{d}x' \left[\frac{2}{\pi} \mathrm{Im} \int_0^1 \frac{\mathrm{d}s}{y(s)\sqrt{1-y(s)x'}} \right] \frac{\mathrm{d}}{\mathrm{d}x'} \left(\frac{q(x')}{|x'|} \right),$$

$$\mathcal{H}_g(x,\xi) = \int_{-1}^{1} \mathrm{d}x' \left[\frac{2}{\pi} \mathrm{Im} \int_0^1 \frac{\mathrm{d}s(x+\xi(1-2s))}{y(s)\sqrt{1-y(s)x'}} \right] \frac{\mathrm{d}}{\mathrm{d}x'} \left(\frac{g(x')}{|x'|} \right),$$

$$y(s) = \frac{4s(1-s)}{x+\xi(1-2s)}.$$

[Shuvaev et. al 1999]

Shuvaev Transform cont.

The conformal moments H_i^N of the GPDs are given by

$$H_i^N \equiv \int_{-1}^{1} \mathrm{d}x R_{N,i}(x_1, x_2) H_i(x,\xi), \qquad i = q, g,$$

Ohrndorf, 82

The conformal moments are polynomials in even powers of ξ,

$$H_i^N = \sum_{k=0}^{\lfloor (N+1)/2 \rfloor} c_{k,i}^N \xi^{2k} = c_{0,i}^N + c_{1,i}^N \xi^2 + c_{2,i}^N \xi^4 + \ldots, \qquad , \; c_{0,i}^N = f_i^N$$

Leading term is Mellin moment of PDF

- Provided inverse exists then can relate GPDs to PDFs with suppression of order xi (i.e. good low x approx)

Shuvaev Transform cont.

Widely debated, certain conditions needing upheld, e.g lack of singularities in Re N > 1 plane

e.g Diehl, Kugler, 08

Regge theory considerations => condition met Martin, Nockles, Ryskin, Teubner, 09

- Can check in physically motivated ansatz, e.g MSTW2008 global partons input parametrisation

Martin, Stirling,Thorne, Watt, 09

$$xg(x, Q_0^2) = A_g x^{\delta_g}(1-x)^{\eta_g}(1+\epsilon_g\sqrt{x}+\gamma_g x) + A_{g'} x^{\delta_{g'}}(1-x)^{\eta_{g'}}.$$

Expand about x ~ 0

$$xg(x, Q_0^2) = A_g x^{\delta_g} + A_{g'} x^{\delta_{g'}} + \ldots,$$

Mellin transform:

$$\begin{aligned} xg^N(Q_0^2) &= \int_0^1 \mathrm{d}x x^{N-1}(A_g x^{\delta_g} + A_{g'} x^{\delta_{g'}}) + \ldots \\ &= \frac{A_g}{N+\delta_g} + \frac{A_{g'}}{N+\delta_{g'}} + \ldots, \end{aligned}$$

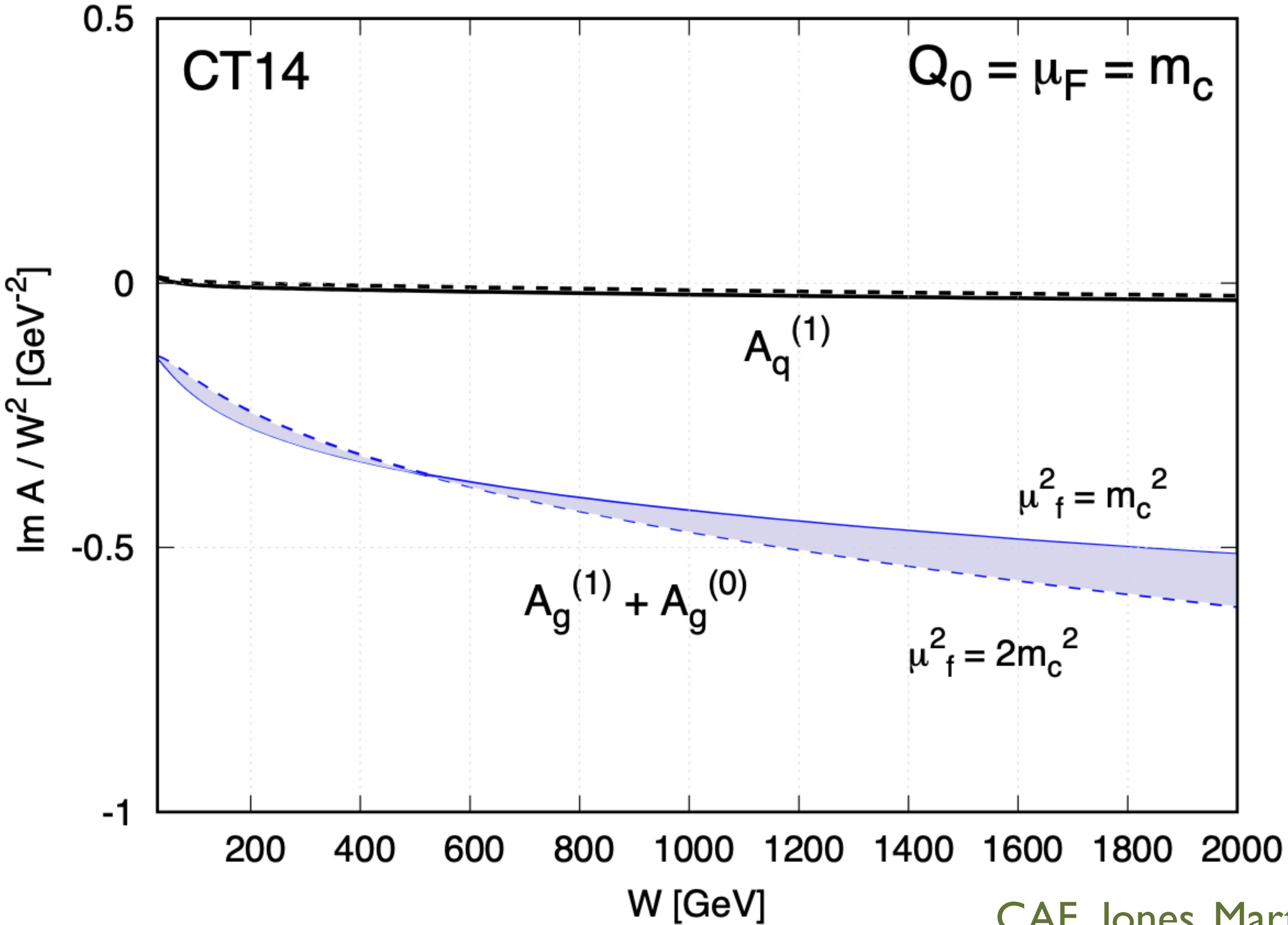
Fits to data (including 1sig. errors) suggest $\delta_g > -1$ and $\delta_{g'} > -1$

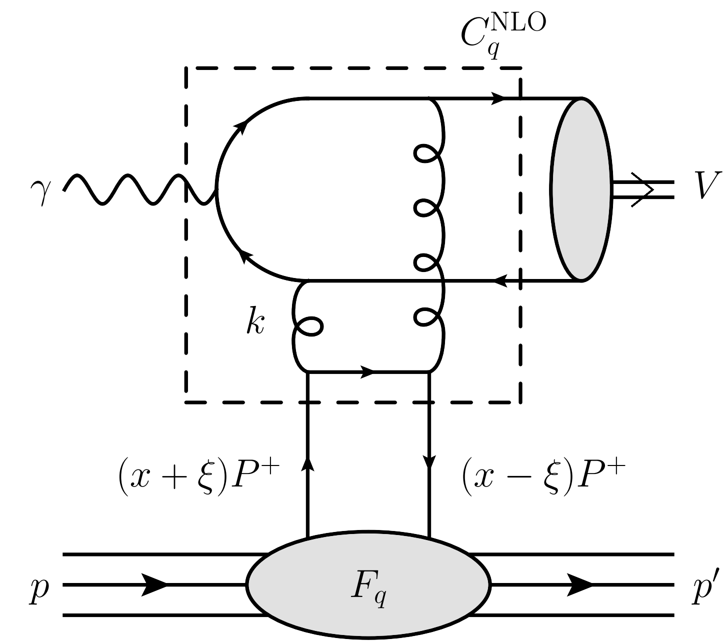
- Shuvaev transform describes HVM and GDVCS data well

Kumericki, Muller, 10

Interplay of quark and gluons at NLO (tamed)

After Q_o subtraction:



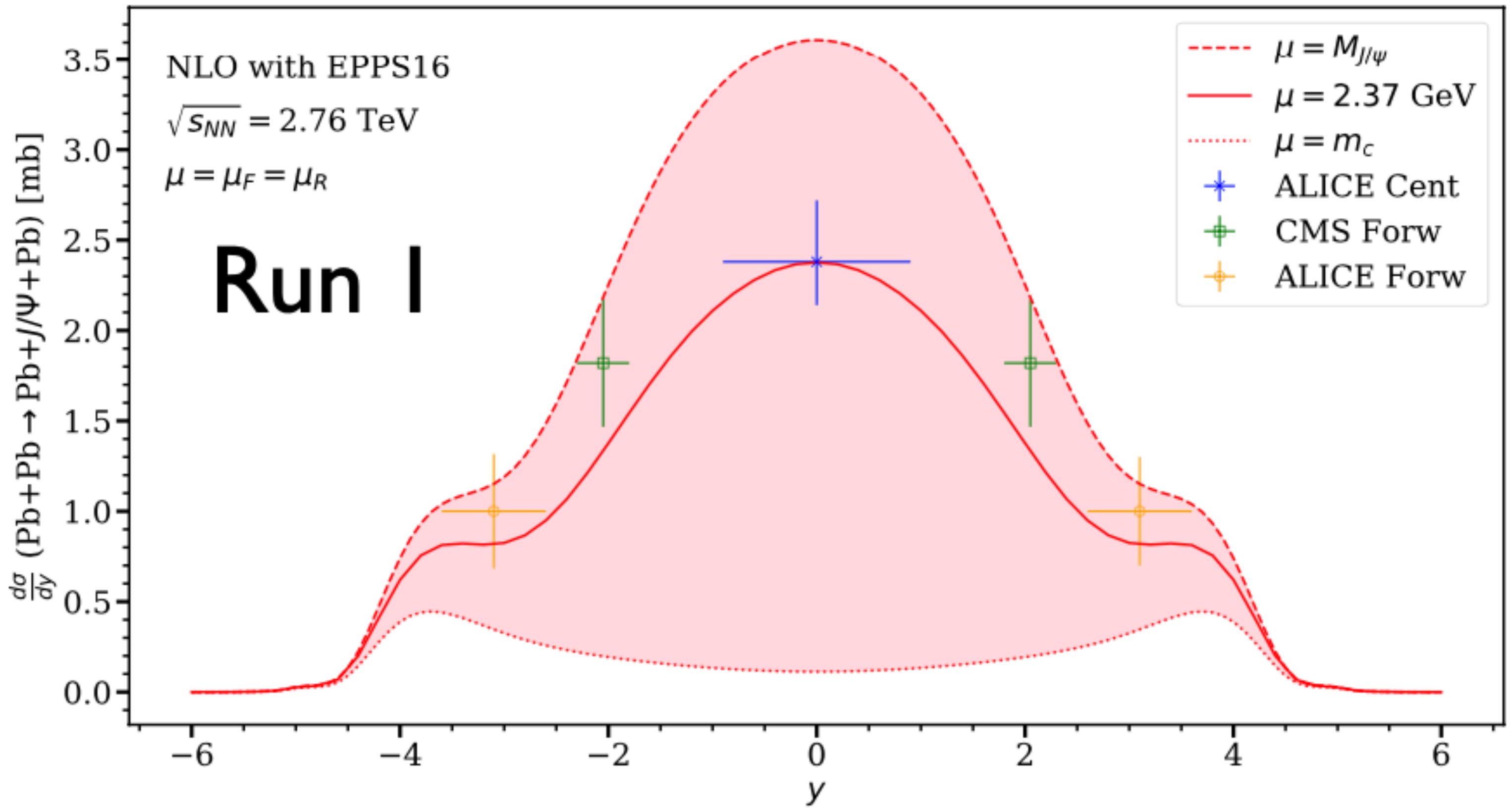


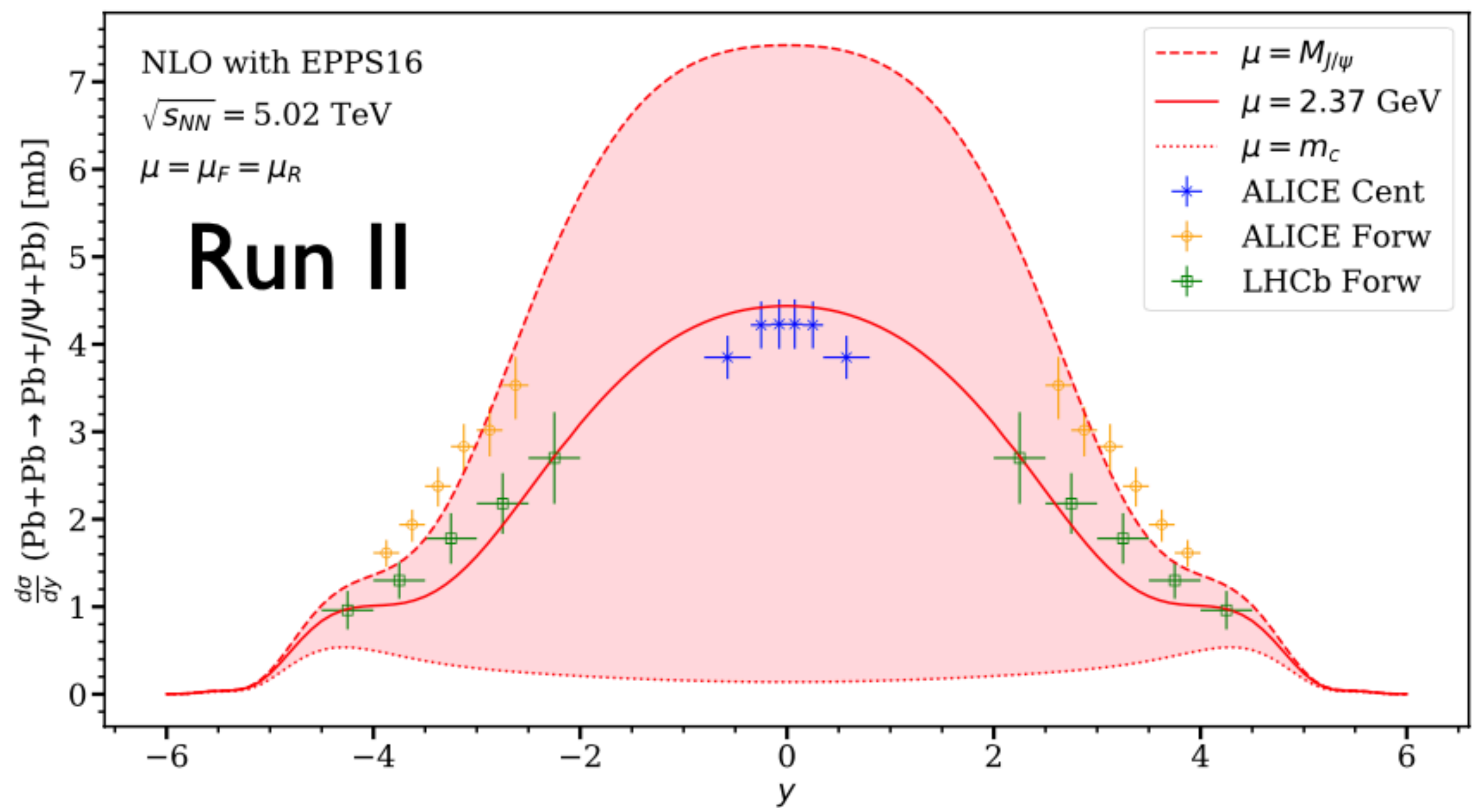
CAF, Jones, Martin, Ryskin, Teubner, 1908.08398

Quark contribution separated from hard scattering by at least *one* step of DGLAP evolution and is therefore removed after imposition of Q_o subtraction

⟶ Gluon driven again like at LO

Scale dependence at NLO

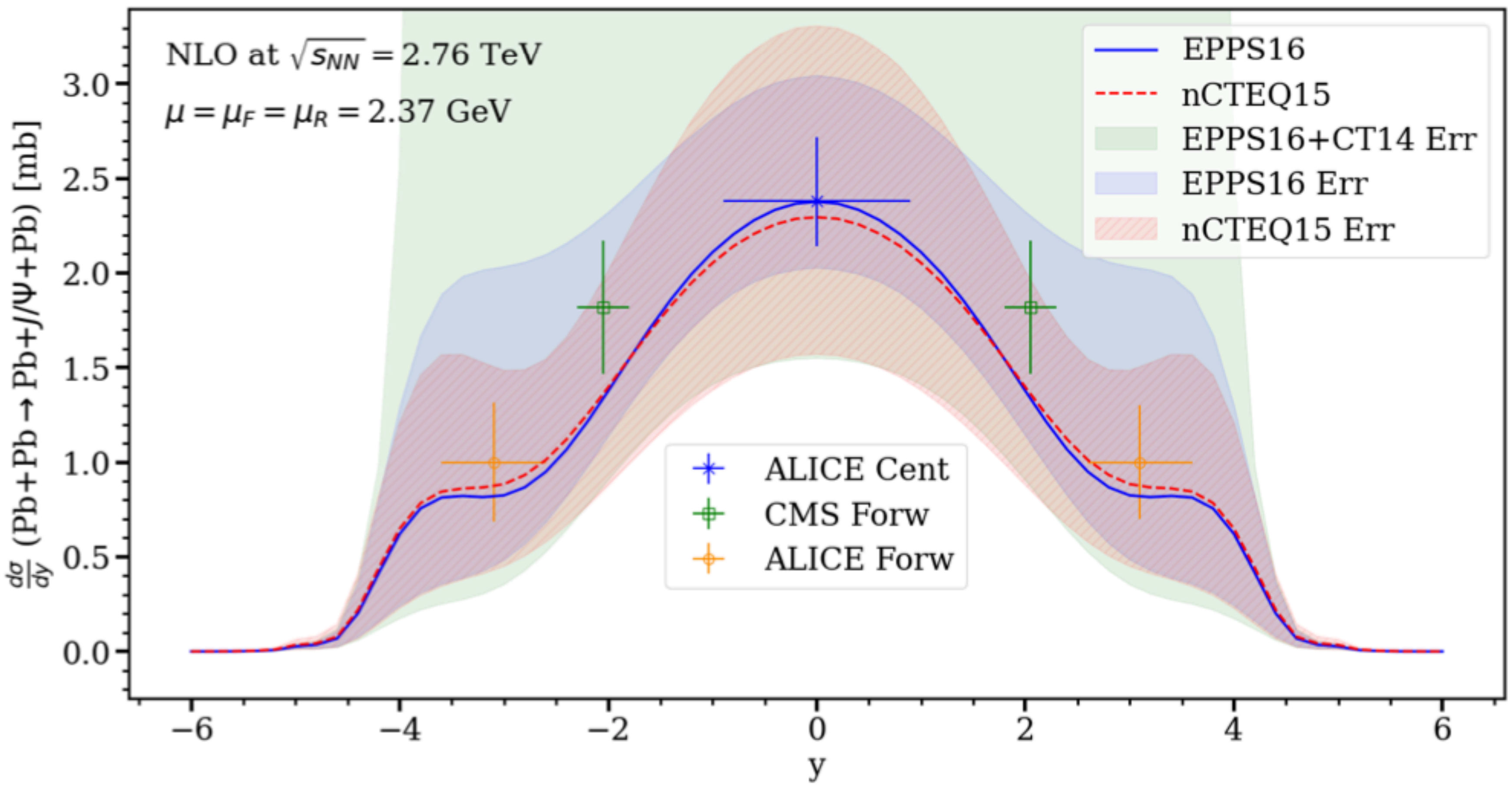


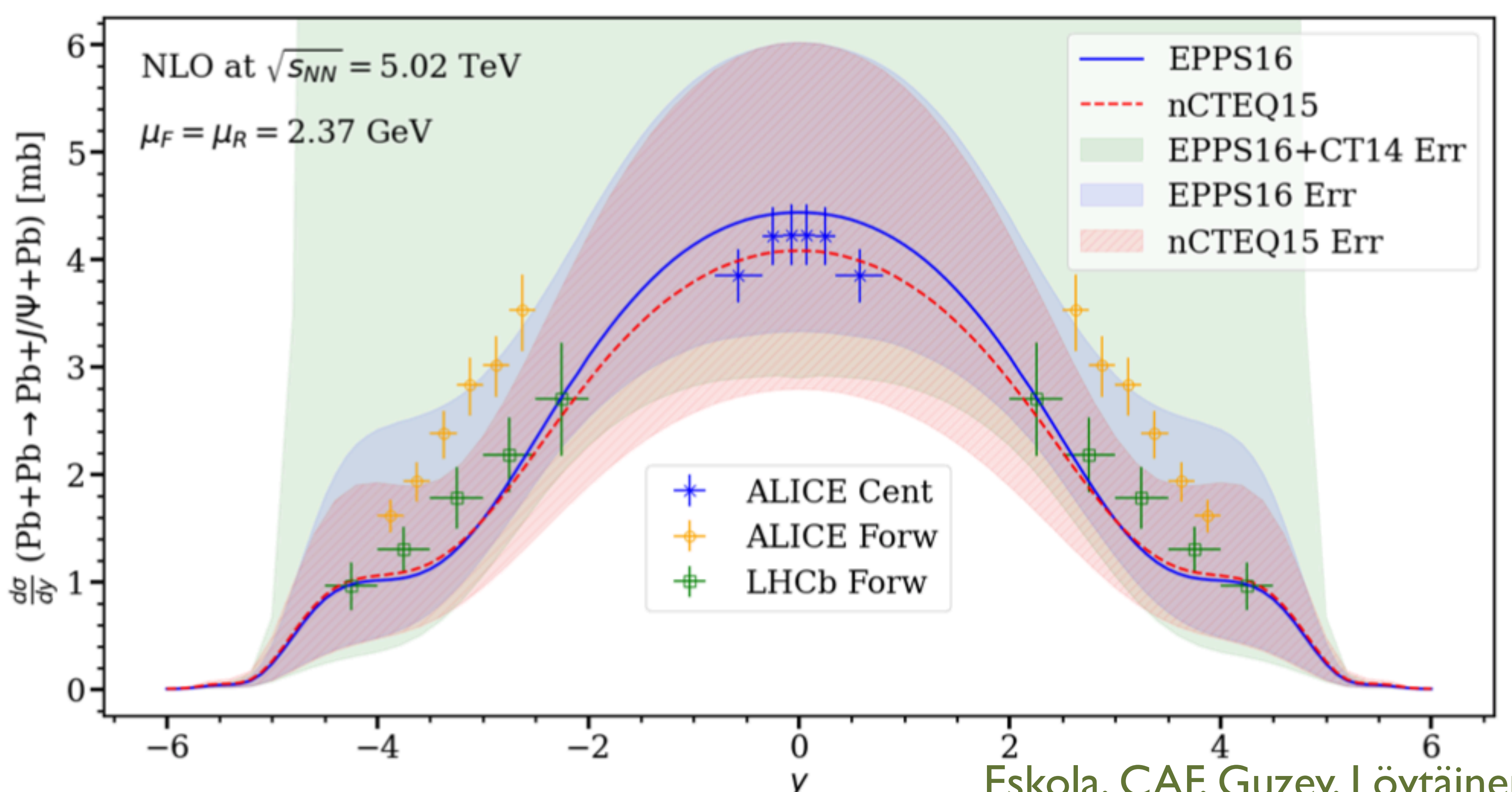


- Scale dependence large (!) (worsens at NLO)
- 'Optimal scale': fitted to reproduce the data at both Run I and Run II energies
- Large scale variation consistent with results in hep-ph/0401131

Eskola, CAF, Guzey, Löytäinen, Paukkunen 2203.11613, 2210.16048

Comparison with data



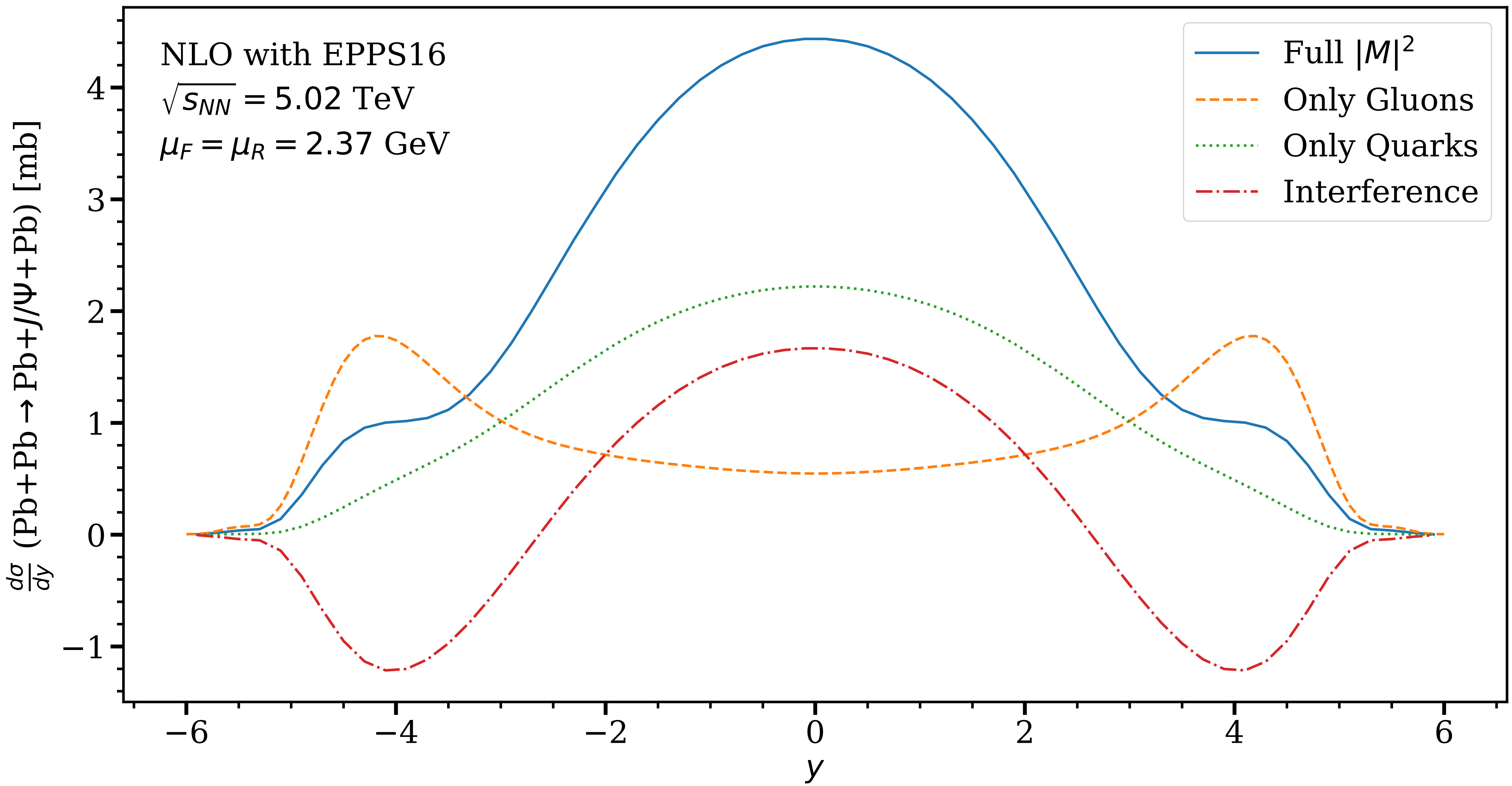


- Nuclear uncertainties encompass available data both at Run I and Run II energies nicely
- Free proton uncertainties large and dominated by single error set
- Tension between Run II ALICE and LHCb data at forward rapidities (now resolved through updated LHCb analysis)

Eskola, CAF, Guzey, Löytäinen, Paukkunen 2203.11613, 2210.16048

Interplay of quark and gluon at NLO (conventional)

Conventional NLO Pb + Pb -> Pb + J/psi + Pb



Quark contribution dominant at mid-rapidity (!)

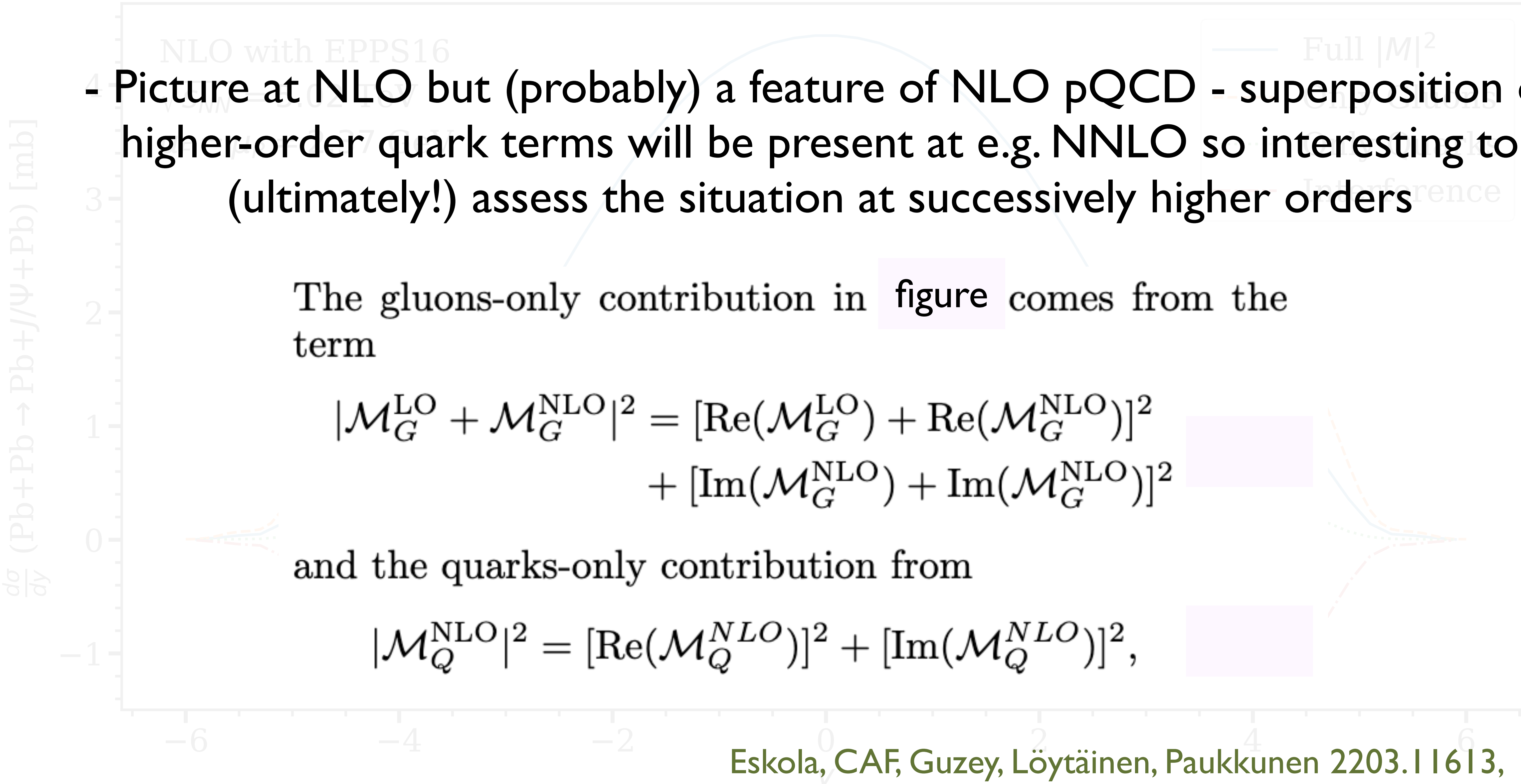
Structure of amplitude detailed, interplaying between photoproduction cross section, photon flux, form factor and $W_{\pm}$ components

Key: Cancellation of LO and NLO gluon amplitudes due to opp. signs

Eskola, CAF, Guzey, Löytäinen, Paukkunen 2203.11613, 2210.16048

Interplay of quark and gluon at NLO

Conventional NLO Pb + Pb -> Pb + J/psi + Pb



- Picture at NLO but (probably) a feature of NLO pQCD - superposition of higher-order quark terms will be present at e.g. NNLO so interesting to (ultimately!) assess the situation at successively higher orders

The gluons-only contribution in figure comes from the term

$$|\mathcal{M}_G^{\rm LO} + \mathcal{M}_G^{\rm NLO}|^2 = [\mathrm{Re}(\mathcal{M}_G^{\rm LO}) + \mathrm{Re}(\mathcal{M}_G^{\rm NLO})]^2 + [\mathrm{Im}(\mathcal{M}_G^{\rm NLO}) + \mathrm{Im}(\mathcal{M}_G^{\rm NLO})]^2$$

and the quarks-only contribution from

$$|\mathcal{M}_Q^{\rm NLO}|^2 = [\mathrm{Re}(\mathcal{M}_Q^{NLO})]^2 + [\mathrm{Im}(\mathcal{M}_Q^{NLO})]^2,$$

Eskola, CAF, Guzey, Löytäinen, Paukkunen 2203.11613, 2210.16048

Quark contribution dominant at mid-rapidity (!)

Structure of amplitude detailed, interplaying between photoproduction cross section, photon flux, form factor and $W_\pm$ components

Key: Cancellation of LO and NLO gluon amplitudes due to opp. signs

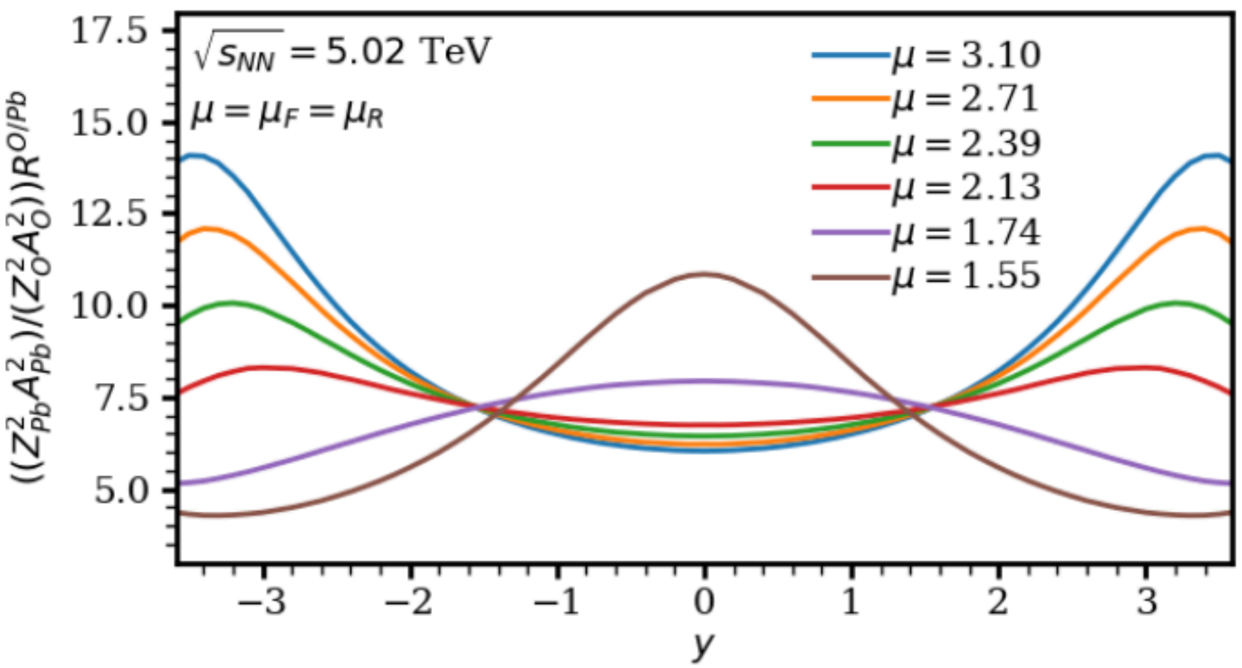
Slide made by V. Guzey

Reduction of uncertainties using O/Pb ratio

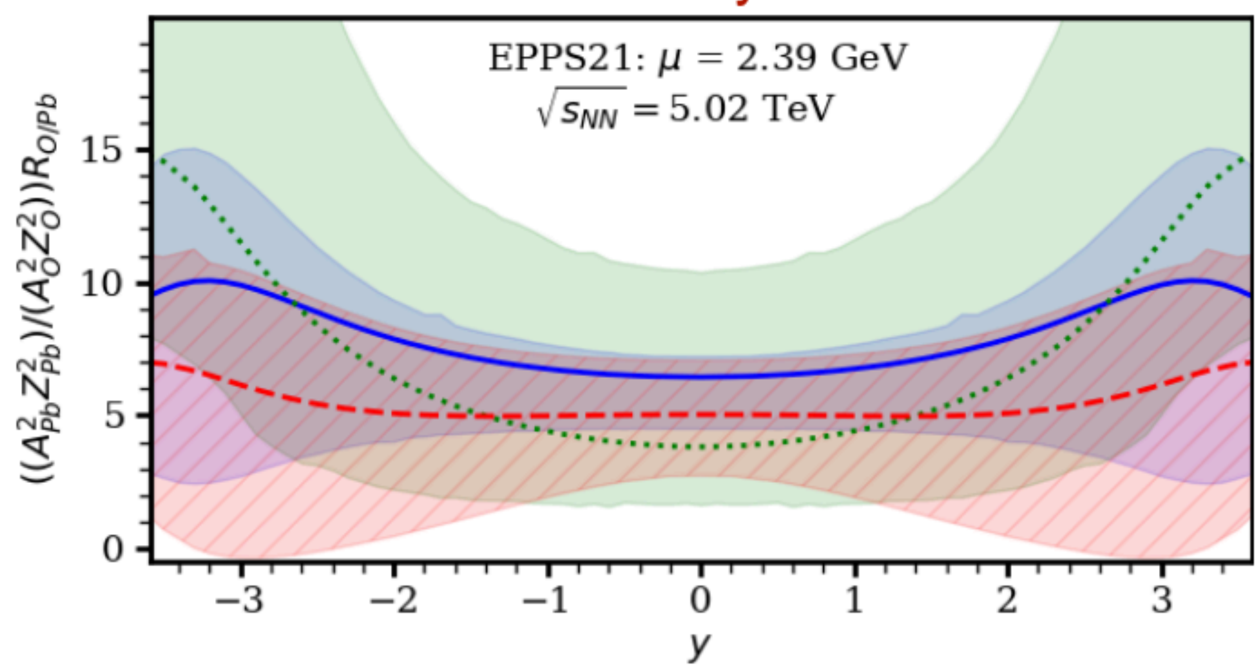
- One can reduce the significant scale μ_F and nPDF uncertainties by considering the ratio of oxygen to lead UPC cross sections:

$$R^{\mathrm{O/Pb}} = \left(\frac{208 Z_{\mathrm{Pb}}}{16 Z_{\mathrm{O}}}\right)^2 \frac{d\sigma(\mathrm{O}+\mathrm{O}\to\mathrm{O}+J/\psi+\mathrm{O})/dy}{d\sigma(\mathrm{Pb}+\mathrm{Pb}\to\mathrm{Pb}+J/\psi+\mathrm{Pb})/dy}$$

Scale uncertainty of R



nPDF uncertainty of R



- Hard scattering coefficient functions for O and Pb are the same → the scale dependence comes from nPDFs → reduced by factor of 10 compared to individual UPC cross sections.

- Reduction of nPDF uncertainties is even larger due to additional partial cancellation of uncertainties associated with proton PDFs.

Eskola, CAF, Guzey, Löytäinen, Paukkunen 2203.11613, 2210.16048

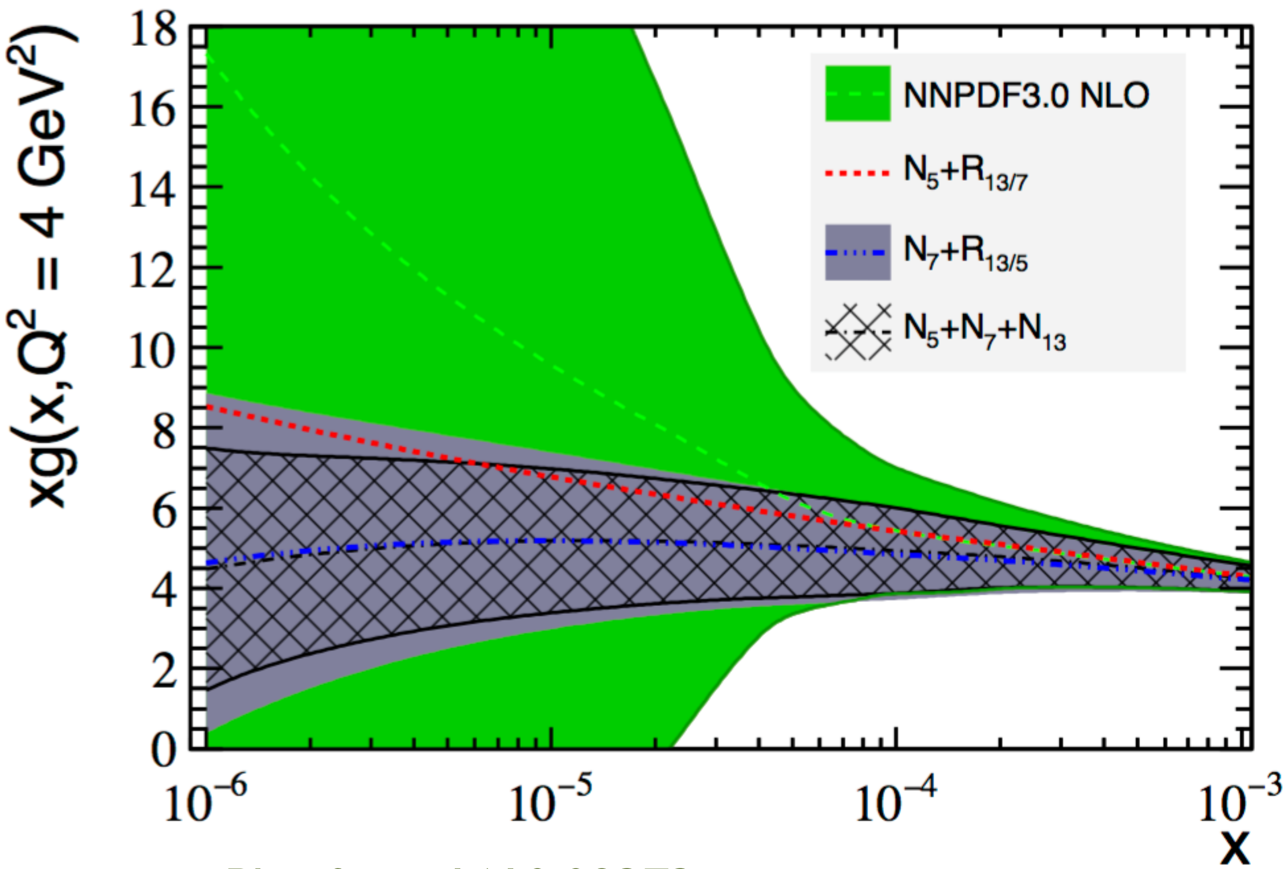
Constraints from inclusive D meson production data

Idea: Construct ratios of observables in y and p_t bins to combat various uncertainties

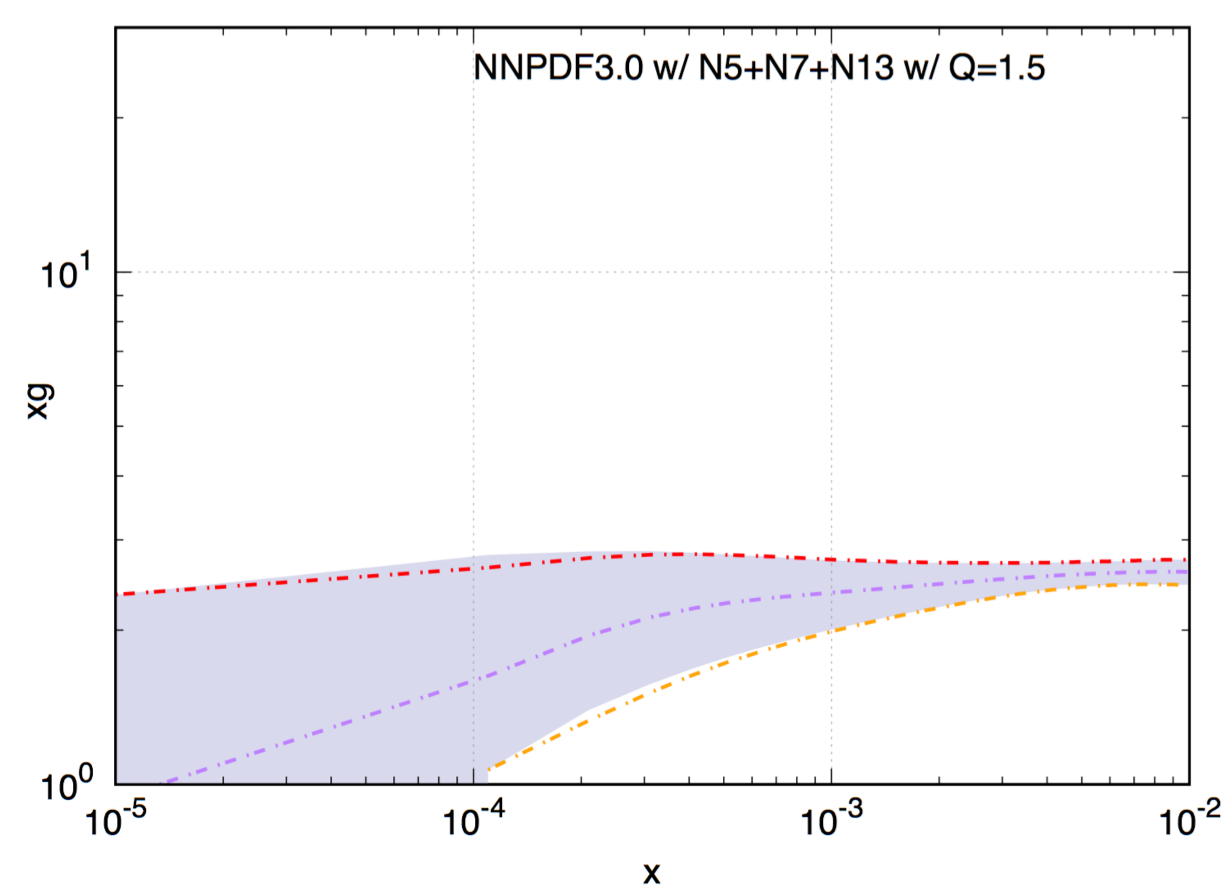
$$N_X^{ij} = \frac{d^2\sigma(\mathrm{X\ TeV})}{dy_i^D d(p_T^D)_j} \Bigg/ \frac{d^2\sigma(\mathrm{X\ TeV})}{dy_{\mathrm{ref}}^D d(p_T^D)_j}$$

$$R_{13/X}^{ij} = \frac{d^2\sigma(13\ \mathrm{TeV})}{dy_i^D d(p_T^D)_j} \Bigg/ \frac{d^2\sigma(\mathrm{X\ TeV})}{dy_{\mathrm{i}}^D d(p_T^D)_j}$$

→ find decreasing gluon at the lowest x they may probe



Plot from 1610.09373



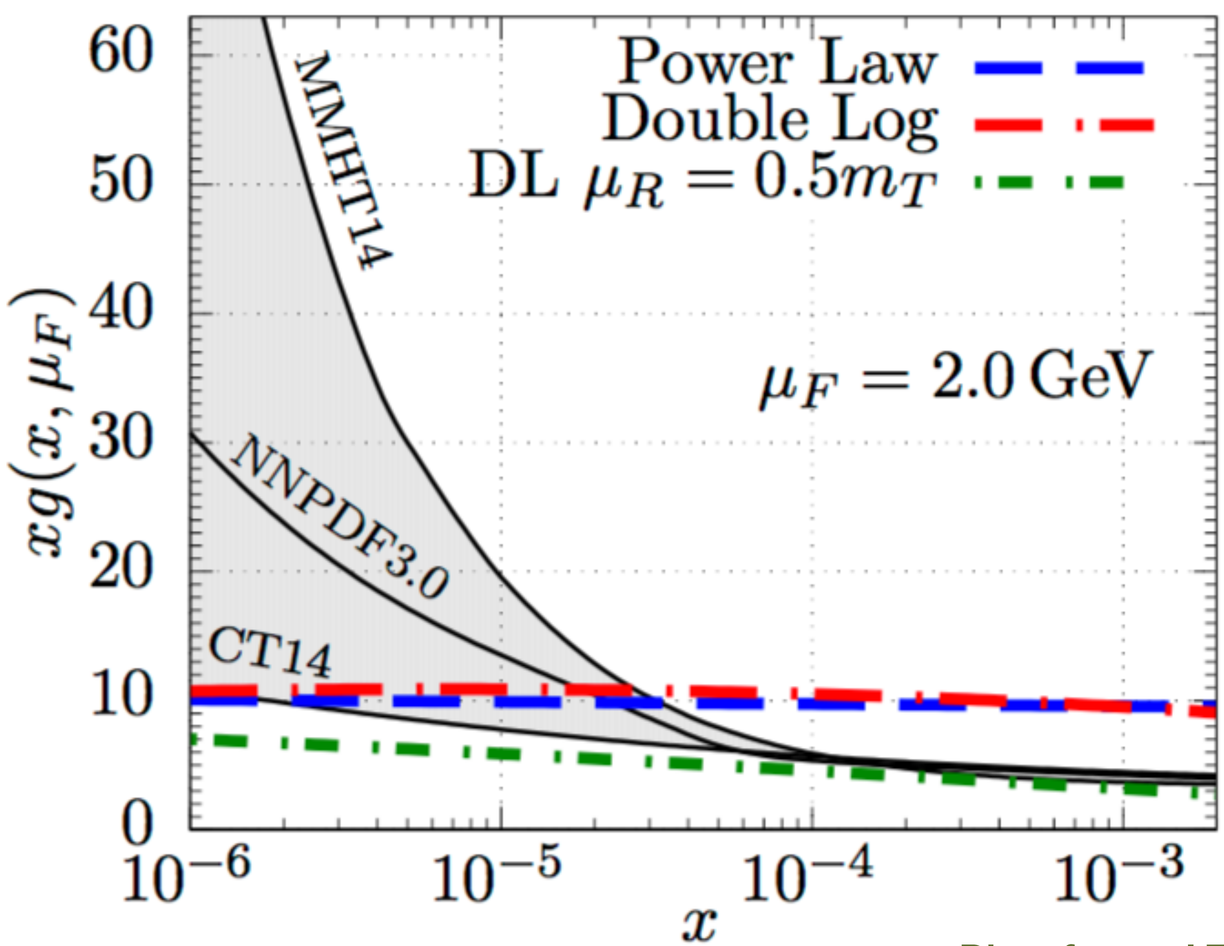
Tension with the J/psi data

We need a much harder gluon at low x to describe the exclusive J/psi LHCb data.

What's the reconciliation?

Indications of **inconsistencies** in the inclusive D experimental measurement

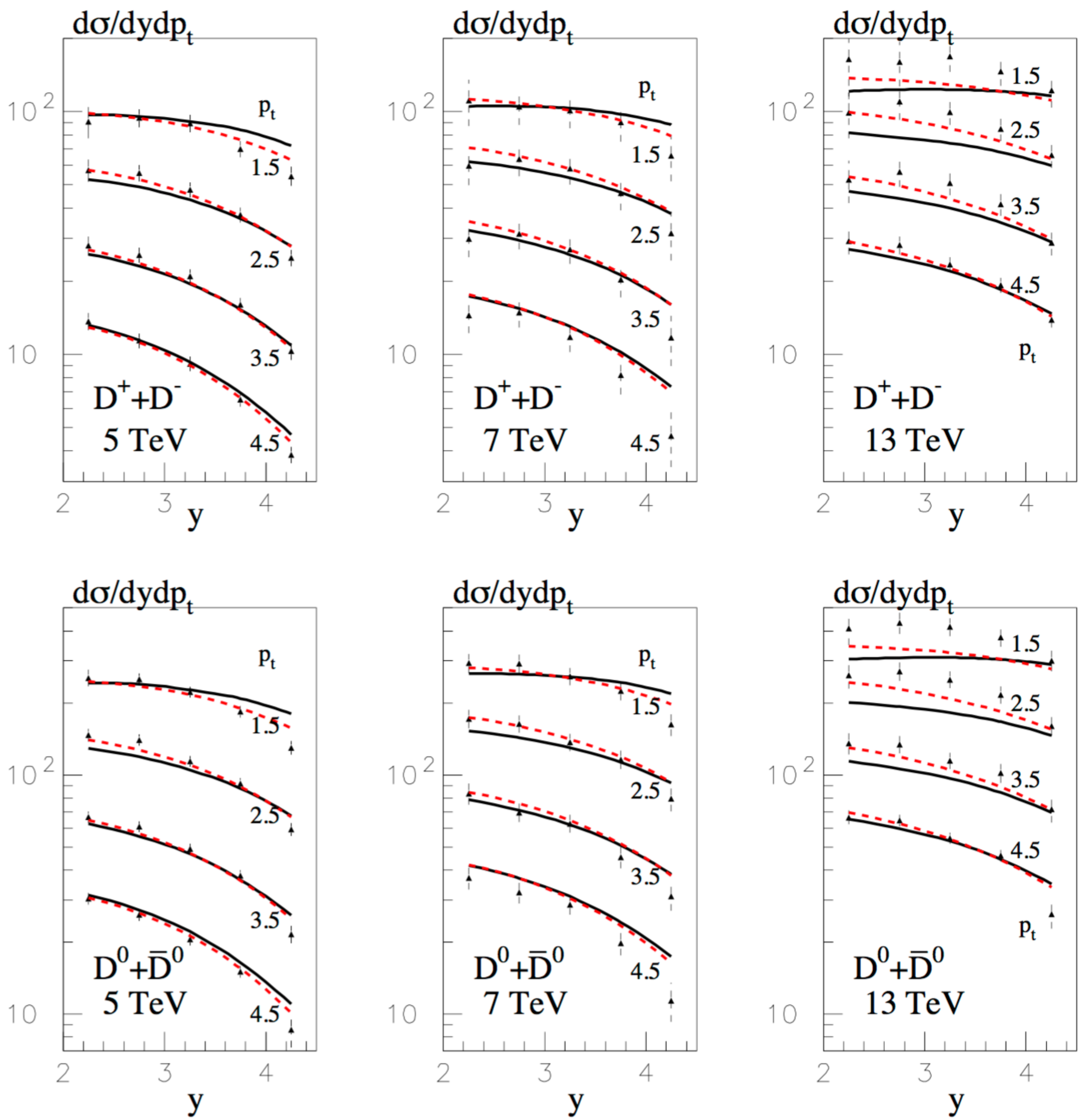
$$xg(x) = N\left(\frac{x}{x_0}\right)^{-\lambda}$$



Plot from 1712.06834

$$xg(x,\mu^2) \;=\; N^{\rm DL}\left(\frac{x}{x_0}\right)^{-a}\left(\frac{\mu^2}{Q_0^2}\right)^{b}\exp\left[\sqrt{16(N_c/\beta_0)\ln(1/x)\ln(G)}\right]$$

Rapidity and energy dependence of open charm cross section



Plot from 1712.06834

- Need *slower* increasing gluon with decreasing x to describe rapidity dependence
- Need *faster* increasing gluon with decreasing x to describe energy dependence

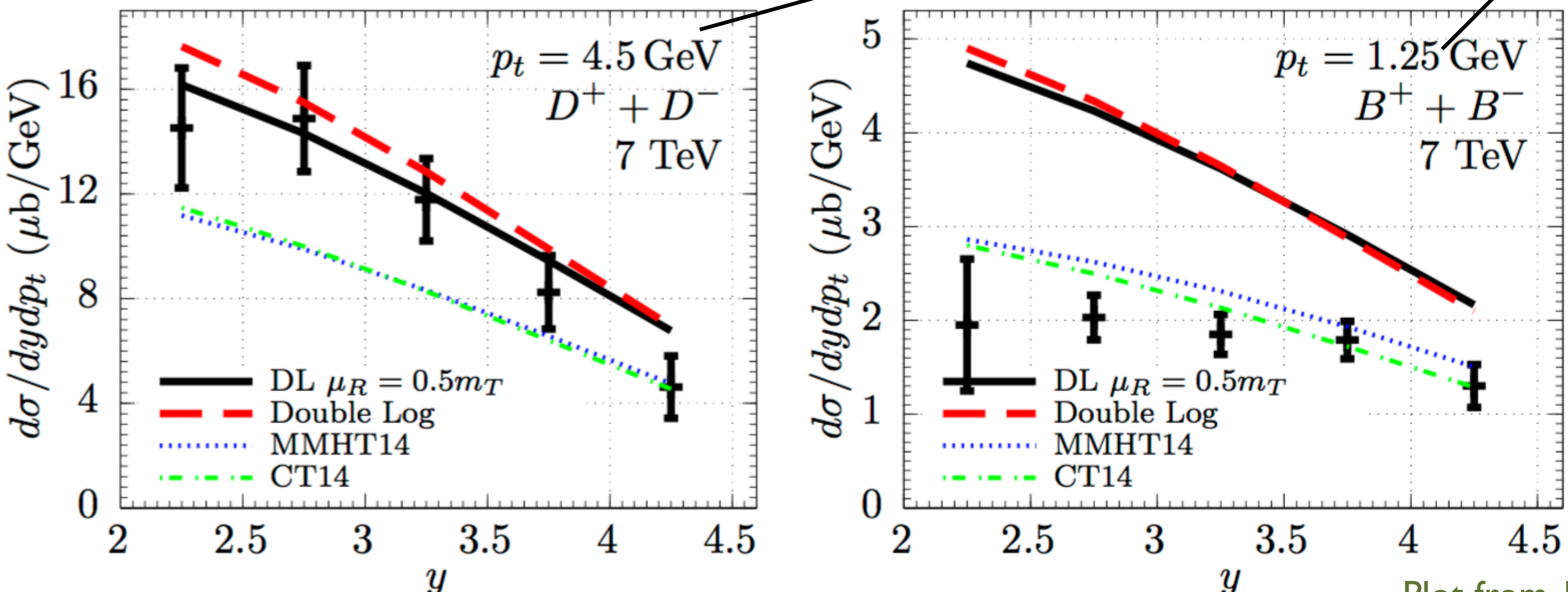
y ~ ln(1/x) !!

dash	Q_0=1 GeV and $\mu_F = \mu_R = 0.85 m_T$
solid	$\mu_f = \mu_R = 0.5 m_T$ and Q_0=0.5 GeV

Open beauty results

B sector has something to say…

p_t chosen to sample gluon at same factorisation scale and x



Plot from 1712.06834

Gluon found through fit to D meson data fails to describe the B meson distribution

Should we really trust the decreasing nature of the low scale, low x gluon obtained via fit to LHCb open charm data?

Extraction of low x gluon PDF via exclusive J/psi

Left

on PDF ansatz to the data

eight current global PDF analyses

= 0.136 +/- 0.006

0.966 +/- 0.025

Reweighted gluon PDF extractions via exclusive J/psi data and inclusive D meson production differ:

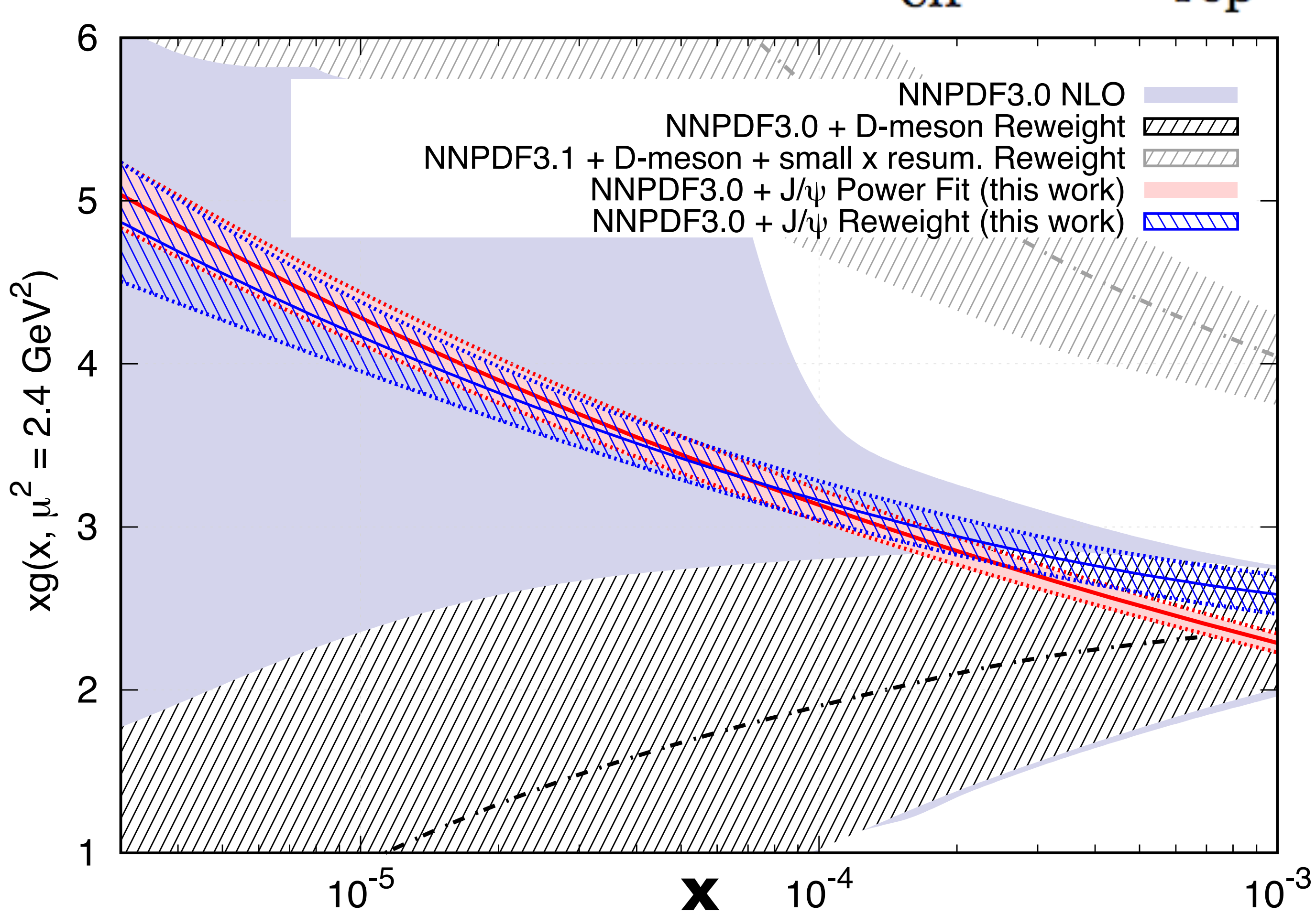
- Experimental inconsistencies in measurement of inclusive D meson production (?) (rapidity detection efficiency and self inconsistency with inclusive B meson detection) ,

  Oliveira, Martin, Ryskin, 1712.06834

- etac hadroproduction (conventional inclusive mode) favours harder gluon than that obtained from inclusive D meson production,

  Lansberg, Ozcelik, 2012.00702

$N_{\text{eff}} \ll N_{\text{rep}}$



General Set up and Framework

ccbar->J/psi:

- Effective field theory for production of heavy quarkonium [Bodwin et al. 1995]

$$\sigma_V = \sigma_{q\bar{q}} \cdot \langle O \rangle_V$$

- Relativistic corrections systematically computed by expanding matrix elements in powers of r:

$$\mathcal{M}[J/\psi] \propto (\mathcal{A}_\rho + \mathcal{B}_{\rho\sigma} r^\sigma + \mathcal{C}_{\rho\sigma\tau} r^\sigma r^\tau + \ldots)\epsilon^\rho_{J/\psi} \qquad r^\mu = q_1^\mu - q_2^\mu$$

$\mathcal{A}$, $\mathcal{B}$, $\mathcal{C}$ - matrix elements $\quad \epsilon^\rho_{J/\psi}$ - J/ψ polarization

- We will compute to leading order in relative quark velocity v, for J/ψ:

$$\mathcal{M}[J/\psi] = \left(\frac{\langle O_1 \rangle_{J/\psi}}{2N_c m_C}\right)^{\frac{1}{2}} \mathcal{A}_\rho \epsilon^\rho_{J/\psi} \qquad \langle O_1 \rangle_{J/\psi} \equiv \langle O_1(^3S_1) \rangle_{J/\psi}$$

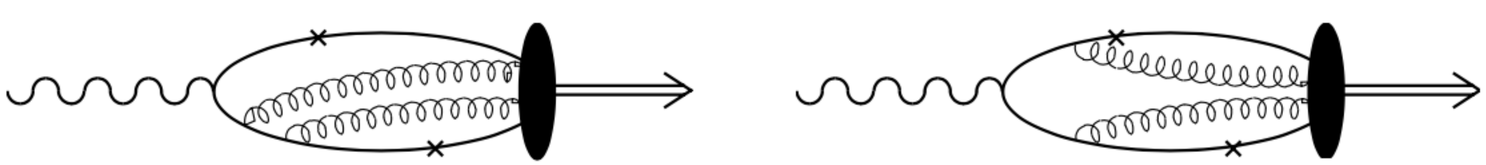
$$\mathcal{O}_1(^3S_1) = \psi^\dagger \boldsymbol{\sigma} \chi \cdot \chi^\dagger \boldsymbol{\sigma} \psi$$

- Compute $\Gamma_{ee} \propto \langle O_1 \rangle_{J/\psi}$
  - Extract $\langle O_1 \rangle_{J/\psi}$ from measurement of Γ_{ee}

$$\langle O_1 \rangle_V = \frac{N_c}{2\pi} |R_S(0)|^2 + \mathcal{O}(v^2)$$

- Leading zeroth order term in rel. velocity (NRQCD)
- First non-vanishing O(v^2) relativistic correction small AFTER additional ccbar+gg Fock state component considered for gauge invariance

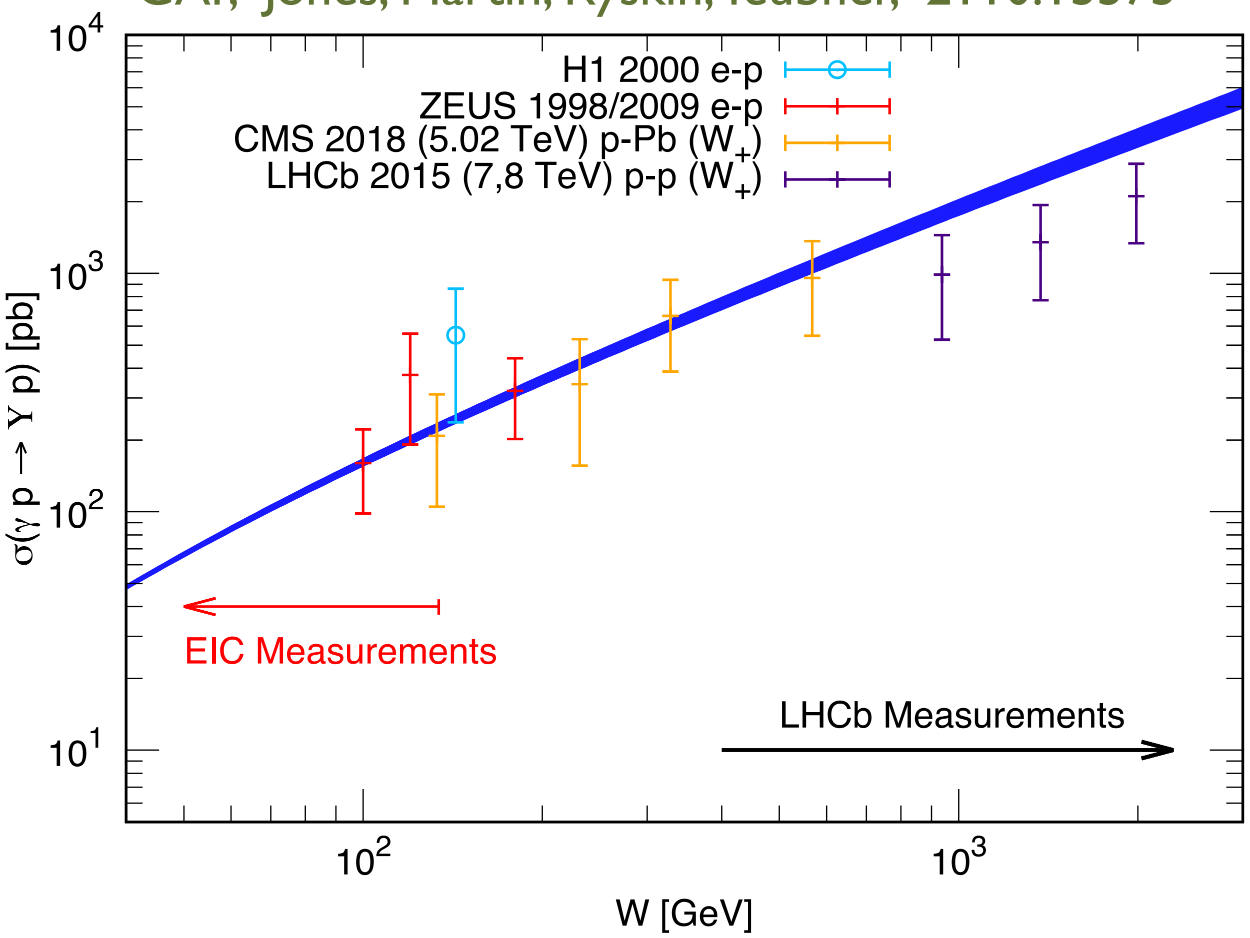
Hoodbhoy 97



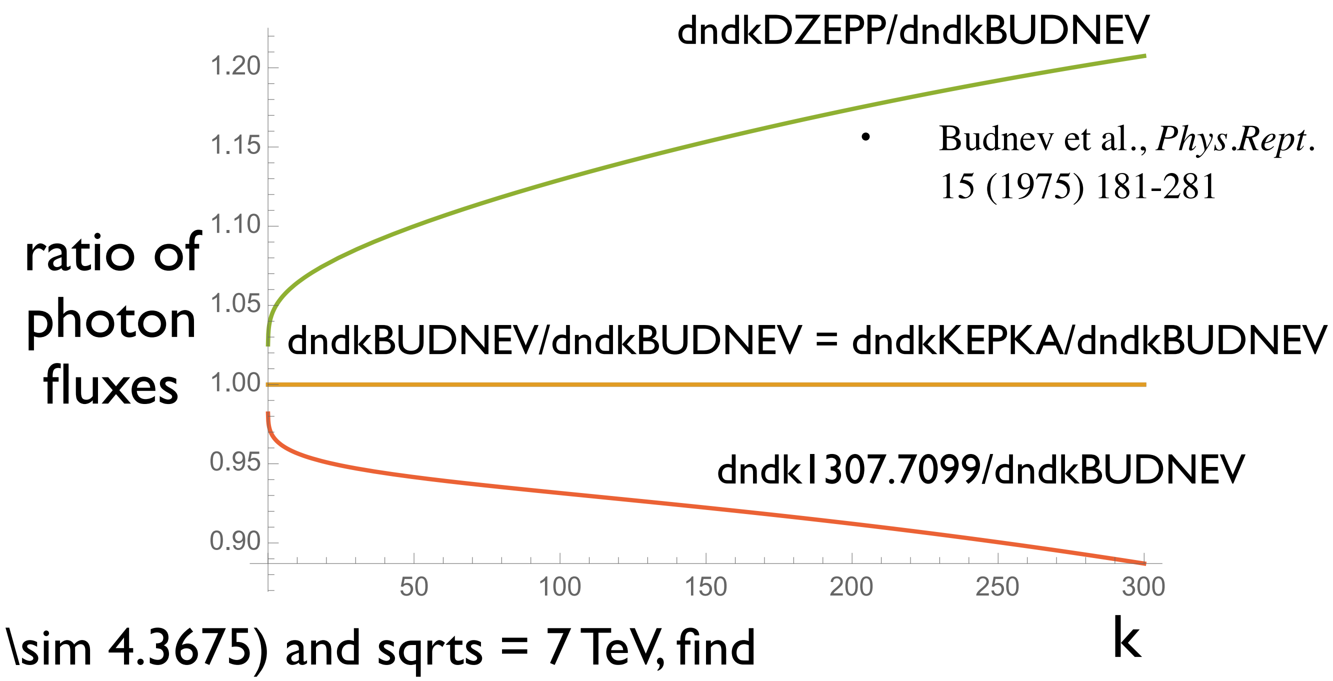
- O(6%) cross section correction factor proportional to derivative of *square* of J/psi w.f. at origin (and affecting normalisation only and not energy dependence)

Other results in UPC: Photon flux in Upsilon photoprod. in pp

CAF, Jones, Martin, Ryskin, Teubner, 2110.15575



-DGLAP evolve gluon PDF obtained from fit to J/psi data to scale of Upsilon photoproduction and use as input to make cross-section prediction (blue band)



• Budnev et al., *Phys.Rept*. 15 (1975) 181-281

For J/psi rapidity at border of LHCb acceptance (y \sim 4.3675) and sqrts = 7 TeV, find

(ss1307.7099*flux1307.7099)/(ssBudnev*fluxBudnev)= 0.94901

~ 5% effect

For J/psi rapidity *outside* border of LHCb acceptance (y \sim 5.125) and sqrts = 7 TeV, find

(ss1307.7099*flux1307.7099)/(ssBudnev*fluxBudnev)= 1.24832

~ 25% effect

Upsilon photoproduction photon energies will be larger so discrepancy between fluxes (and survival factors) will be larger and we enter the region where the approximation of 1307.7099 flux breaks down at much lower rapidities and, importantly, within the acceptance of LHCb

=> use Budnev flux (without negligence of O(x) terms)

=> large W unfolded photoproduction LHCb data should be shifted upwards

Sensitivity to the MSbar gluon PDF

- Remain in MSbar scheme with Q0 subtracted coefficient functions to NLO accuracy
- Subtraction does not affect IR or UV divergence renormalisation procedures
- Soft singularity at l=0 is removed after subtracting off the LO part of the NLO coefficient function before integral over loop momentum from 0 to Q0 is performed

$$\Delta \mathrm{Im}\mathcal{M}^q = \frac{\alpha_s^2}{2\pi}\int_\xi^1 dx\,(F_q(x,\xi,m_c) - F_q(-x,\xi,m_c))\left(\int_0^{Q_0^2}(M_a^q + M_b^q)\frac{2\pi m_c^4}{\hat{s}^2}dl^2\right)$$

- Precisely this FINITE contribution that is subtracted from full MSbar coefficient functions to avoid double counting inherent within MSbar scheme (subtraction fundamentally ubiquitous but numerically relevant for low scale processes only*)

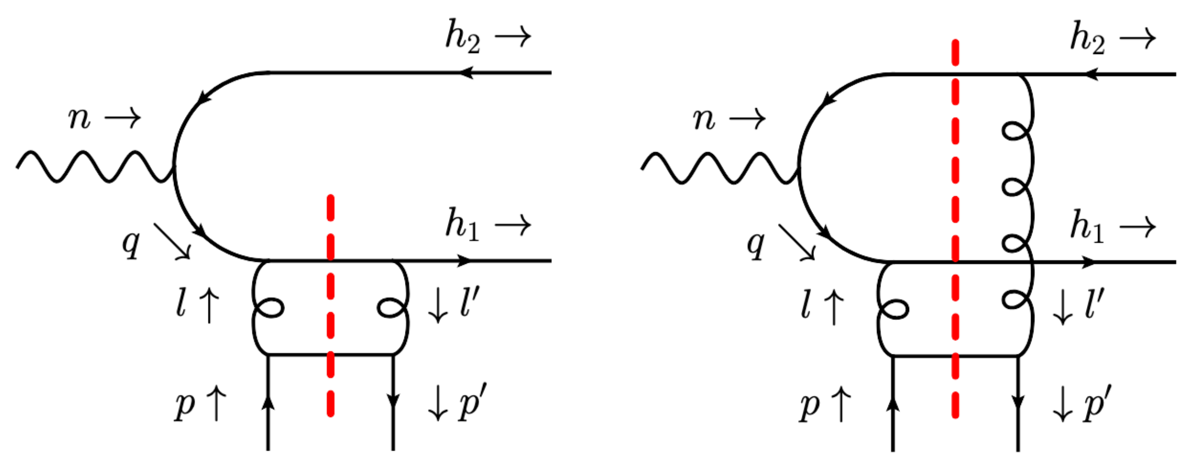
---

*see 1912.09304 for procedure applied to inclusive DIS and Drell-Yan production

Sensitivity to the MSbar gluon PDF

$$\Delta \mathrm{Im}\mathcal{M}^q = \frac{\alpha_s^2}{2\pi}\int_\xi^1 dx\,(F_q(x,\xi,m_c) - F_q(-x,\xi,m_c))\left(\int_0^{Q_0^2}(M_a^q + M_b^q)\frac{2\pi m_c^4}{\hat{s}^2}dl^2\right)$$

- Precisely this FINITE contribution that is subtracted from full MSbar coefficient functions to avoid double counting inherent within MSbar scheme (subtraction fundamentally ubiquitous but numerically relevant for low scale processes only)



- NLO diagrams for quark and gluon channel considered. Contain both LO and NLO contributions. Subtract off LO contribution (part given by LO (generalised) DGLAP evolution P_LO x C^0, see previous) before integration over l is performed, cancelling soft singularity dl^2/l^2.

Higher twist contributions

- Absorptive corrections, which provide the saturation, are described by higher-twist operators and formally not known within the collinear factorisation approach.
- The relative size of the contribution of the next twist absorptive correction is driven by parameter:

$$c = \alpha_s \frac{xg(x)}{R^2 \mu_0^2}$$

- Factor appearing in GLR equation (Phys. Rept. 100 (1983) 1–150) provides non-linear terms through computation of so-called 'fan' diagrams in pQCD that tame (linear) BFKL evolution

- Semi-quantitative estimate based on this scaling gives higher-twist term of O(few percent*). Details in 2006.13857.

---

*If one takes into consideration the colour factor calculated assuming that the low x gluon is emitted by the valence quark in the proton, then there is an additional factor of 81/16 which enhances the estimate to ~6.5%. However, the point is that the higher-twist contribution may be relatively small and that, together with the additional factor of alphas from <v2> \sim alphas, all the parametric dependence is included in the GLR factor c.

Alternate small x resummation

- By fixing the scale in the way described previously, we may miss terms containing a large ln(1/xi) not enhanced by a logarithm depending on the factorisation scale, previously considered $(\alpha_S \ln(1/\xi)\ \ln(\mu_{F/m}))^n$
- Can also consider terms $(\alpha_S \ln(1/\xi))^n$:

$$\mathcal{I}m\mathcal{M}^g \sim H^g(\xi,\xi) + \int_\xi^1 \frac{dx}{x} H^g(x,\xi) \sum_{n=1} C_n(L) \frac{\bar{\alpha}_s^n}{(n-1)!} \log^{n-1} \frac{x}{\xi}$$

$$A \sim 1 + z \ln\left(\frac{m^2}{\mu_F^2}\right) + z^2 \left[\frac{\pi^2}{6} + \frac{1}{2}\ln^2\left(\frac{m^2}{\mu_F^2}\right)\right] + \ldots, \quad z^n \sim \alpha_s^n \ln^n(1/\xi)$$

1601.07338

$$a) \quad (\mu_F = M_V): \quad 1 - 1.39\, z + 2.61\, z^2 + 0.481\, z^3 - 4.96\, z^4 + \ldots$$
$$b) \quad (\mu_F = M_V/2): \quad 1 + 0.\, z + 1.64\, z^2 + 3.21\, z^3 + 1.08\, z^4 + \ldots .$$

- **To investigate:** Supplement the fixed order NLO code with the resummed coefficients (with and without a Q0 subtraction)