

# Color-coherence in the weakly coupled picture

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Supported by the Trond Mohn Foundation BFS2018REK01



QCD challenges from pp to AA (Padova 13 - 17. Feb. 2023)

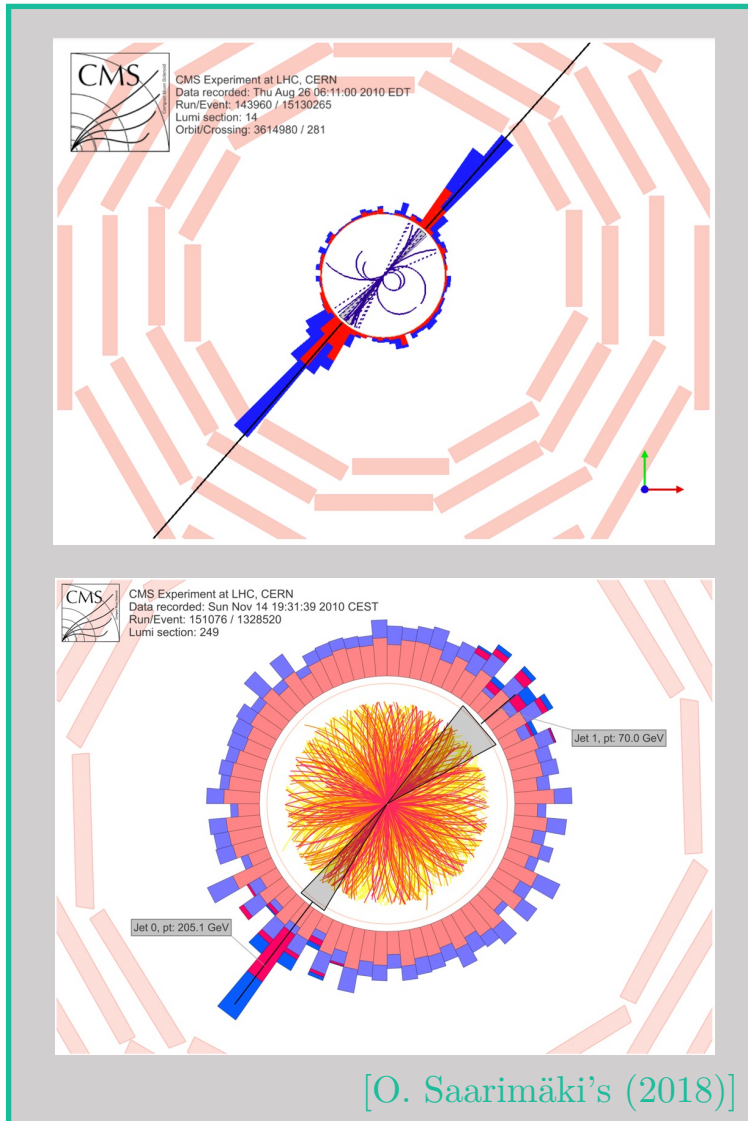
# Introduction

# What is perturbative in the medium?

pp



AA



It is perturbative!

- pQCD is valid:

$$Q_{jet} \gg \Lambda_{QCD}$$

- jet-medium int. is perturbative:

$$Q_{jet} \gg Q_{med}$$

(medium bkg. is removable)

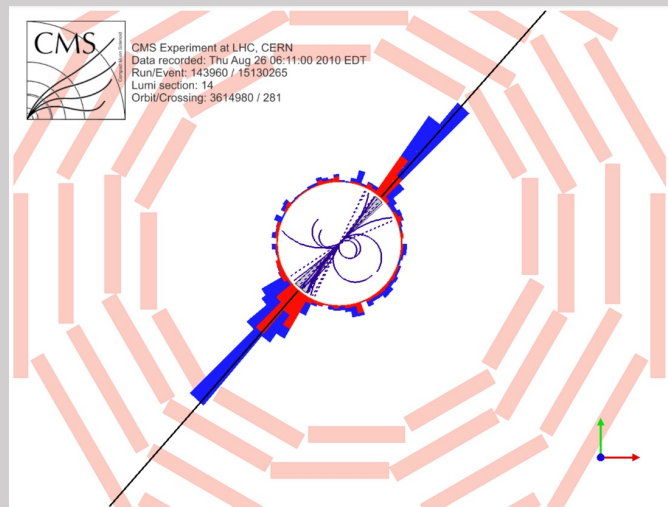
Is weakly coupled?

- medium is perturbative:

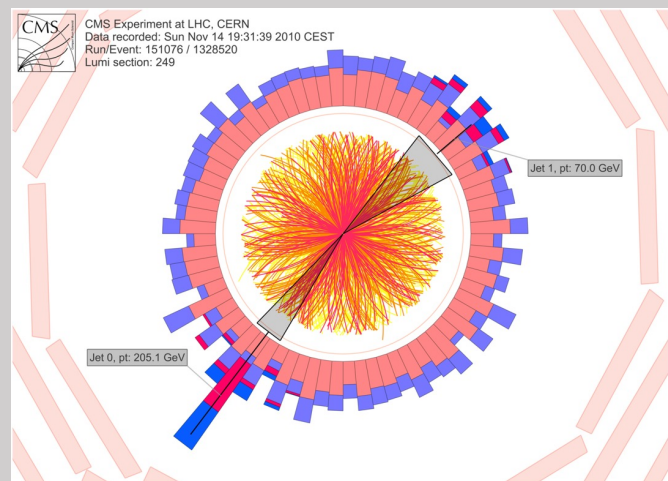
$$Q_{med} ? \gg ? \Lambda_{QCD}$$

# What is perturbative in the medium?

pp



AA



[O. Saarimäki's (2018)]

It is perturbative!

- pQCD is valid:

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[see talks from Daniel Pablos and Carlota Andres]

Is weakly coupled?

- medium is perturbative:

$$Q_{med} ? \gg ? \Lambda_{QCD}$$

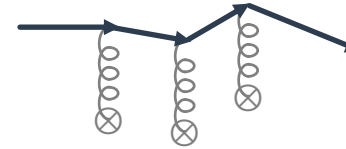
# QCD in the QGP medium

# QCD with a colored background

[Zakharov, BDMPS, GLV, Wiedemann (1996-2000)]

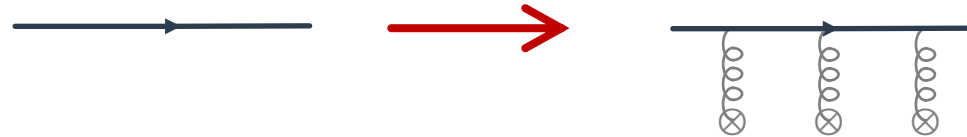
QCD with color bkg:  $\mathcal{A}(x) + \mathcal{A}_0(t, \mathbf{x})$

- Multiple scatterings

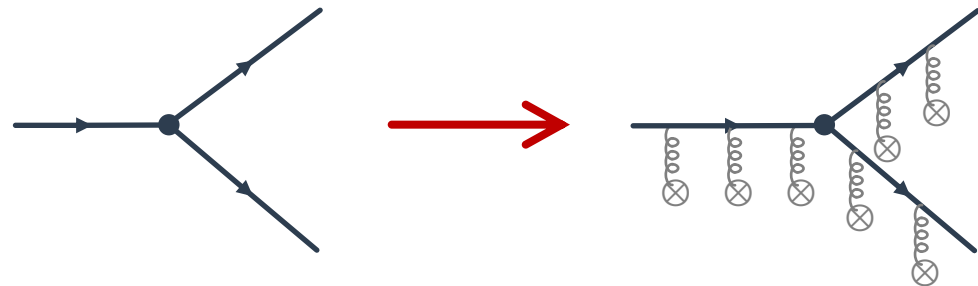


Medium Feynman rules:

- medium propagator:



- medium vertex:



- Medium average:

$$\langle \mathcal{A}_0^-(t, \mathbf{x}) \mathcal{A}_0^-(t', \mathbf{x}') \rangle_{med}$$

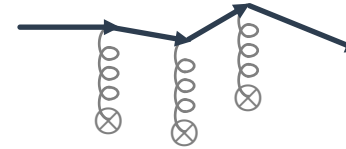
- Weakly coupled plasma ( $T \gg \Lambda_{QCD}$ ): AMY
- Random fields: BDMPSZ
- recently: idk will evaluate later

# QCD with a colored background

[Zakharov, BDMPS, GLV, Wiedemann (1996-2000)]

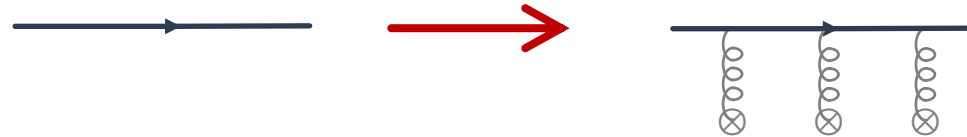
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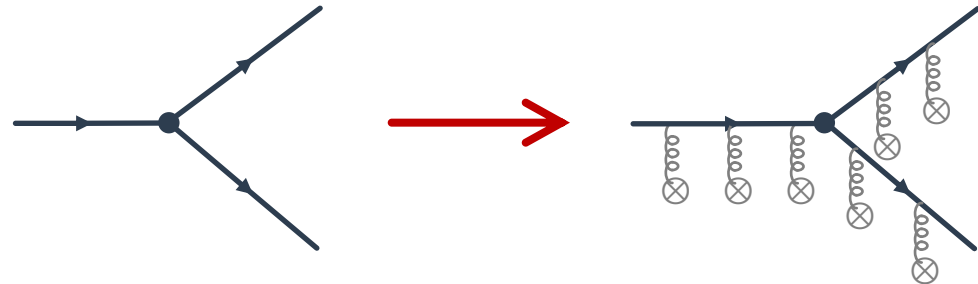


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# Color-coherence in medium

## Vacuum

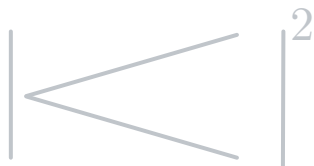
Emission:




$$\Rightarrow \frac{dI_i^{vac}}{dzd\vartheta} \approx \frac{\alpha_s}{\pi} \frac{2C_i}{z} \frac{1}{\vartheta}$$

soft & collinear divergence!

Color-conservation:



Color-coherence:



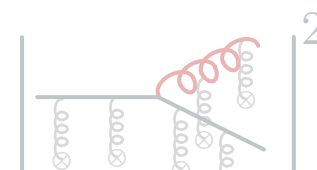
$$\Rightarrow \approx \left( \frac{dI_q^{vac}}{dzd\vartheta} + \frac{dI_{\bar{q}}^{vac}}{dzd\vartheta} \right)$$

$$\times \Theta(\vartheta_{q\bar{q}} > \vartheta_g)$$

angular-ordering!

## Medium

Medium-induced emission:



$$\Rightarrow \frac{dI_i^{med}}{dz} \approx \frac{\alpha_s}{\pi} \frac{Q_{med}}{E} \frac{2C_i}{\sqrt{z^3}}$$

soft divergence!

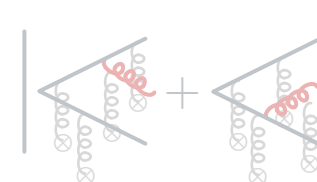
Decoherence time:



$$\Rightarrow \Theta(t_d > t)$$

resolved dipole!

Medium resolution:



$$\Rightarrow \approx \left( \frac{dI_q^{med}}{dzd\vartheta} + \frac{dI_{\bar{q}}^{med}}{dzd\vartheta} \right)$$

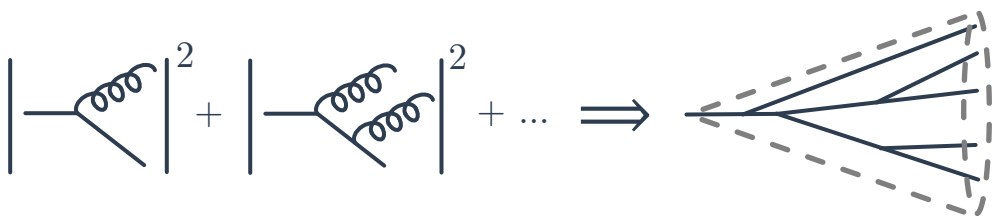
$$\times \Theta(t_f > t_d)$$



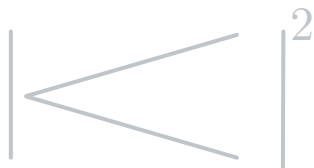
# Color-coherence in medium

## Vacuum

Resumming many emissions: collinear **jet**



Color-conservation:



Color-coherence:

$$\left| \begin{array}{c} \text{diagram 1} \\ \text{diagram 2} \end{array} \right|^2 \Rightarrow \approx \left( \frac{dI_q^{vac}}{dzd\vartheta} + \frac{dI_{\bar{q}}^{vac}}{dzd\vartheta} \right) \times \Theta(\vartheta_{q\bar{q}} > \vartheta_g)$$

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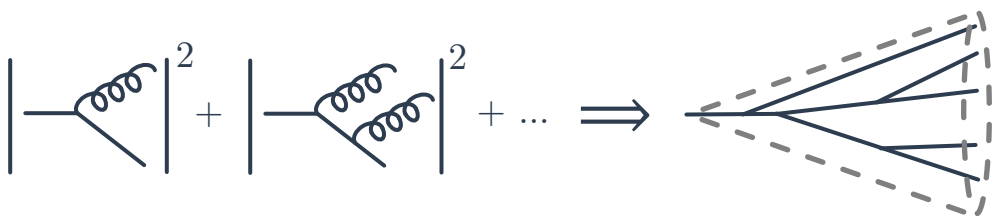
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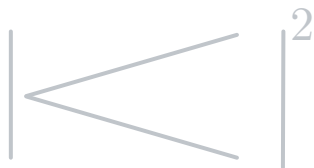
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Color-coherence:

$$\left| \begin{array}{c} \diagup \\ \text{wavy line} \\ \diagdown \end{array} + \begin{array}{c} \diagdown \\ \text{wavy line} \\ \diagup \end{array} \right|^2 \Rightarrow \approx \left( \frac{dI_q^{vac}}{dzd\vartheta} + \frac{dI_{\bar{q}}^{vac}}{dzd\vartheta} \right) \times \Theta(\vartheta_{q\bar{q}} > \vartheta_g)$$

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Medium-induced emission:

$$\left| \begin{array}{c} \text{wavy line} \\ \diagdown \\ \text{wavy line} \end{array} \right|^2 \Rightarrow \frac{dI_i^{med}}{dz} \approx \frac{\alpha_s}{\pi} \frac{Q_{med}}{E} \frac{2C_i}{\sqrt{z^3}}$$

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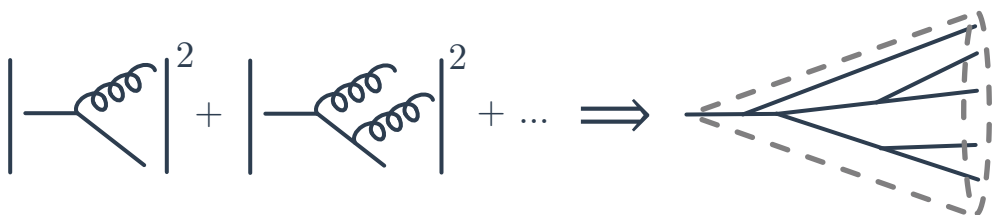
Medium resolution:

$$\left| \begin{array}{c} \diagup \\ \text{wavy line} \\ \diagdown \end{array} + \begin{array}{c} \diagdown \\ \text{wavy line} \\ \diagup \end{array} \right|^2 \Rightarrow \approx \left( \frac{dI_q^{med}}{dzd\vartheta} + \frac{dI_{\bar{q}}^{med}}{dzd\vartheta} \right) \times \Theta(t_f > t_d)$$

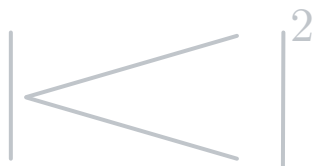
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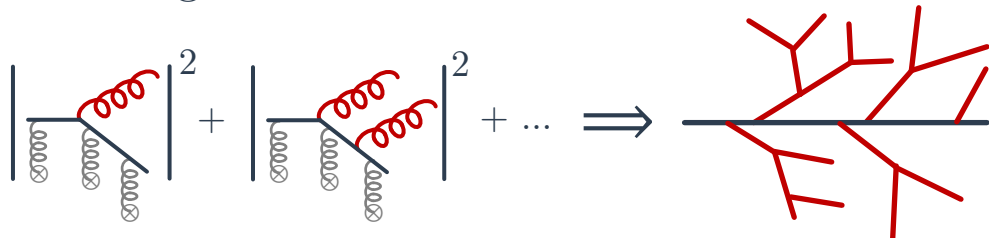
Color-coherence:

$$\left| \begin{array}{c} \diagup \\ \text{gluon} \\ \diagdown \end{array} + \begin{array}{c} \diagup \\ \text{gluon} \\ \diagdown \end{array} \right|^2 \Rightarrow \approx \left( \frac{dI_q^{vac}}{dzd\vartheta} + \frac{dI_{\bar{q}}^{vac}}{dzd\vartheta} \right) \times \Theta(\vartheta_{q\bar{q}} > \vartheta_g)$$

angular-ordering!

## Medium

wide-angle medium **cascade**



Decoherence time:



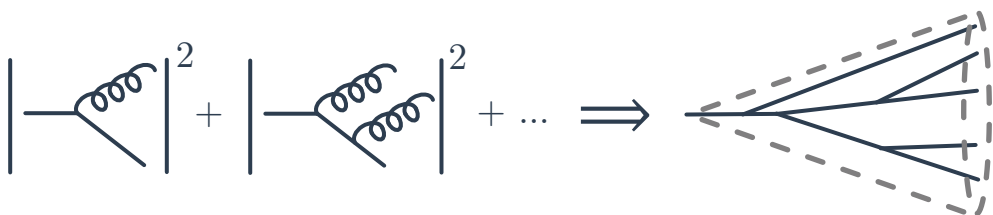
Medium resolution:

$$\left| \begin{array}{c} \diagup \\ \text{gluon} \\ \diagdown \end{array} + \begin{array}{c} \diagup \\ \text{gluon} \\ \diagdown \end{array} \right|^2 \Rightarrow \approx \left( \frac{dI_q^{med}}{dzd\vartheta} + \frac{dI_{\bar{q}}^{med}}{dzd\vartheta} \right) \times \Theta(t_f > t_d)$$

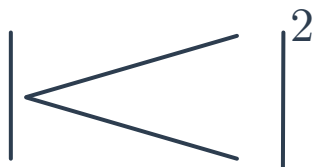
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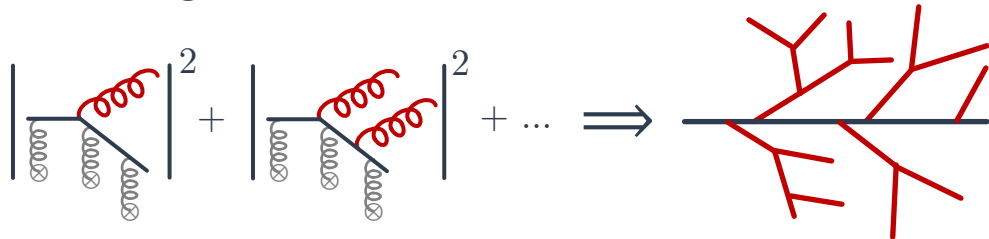
Color-coherence:

$$\left| \begin{array}{c} \diagup \\ \text{curly} \\ \diagdown \end{array} + \begin{array}{c} \diagup \\ \text{curly} \\ \diagdown \end{array} \right|^2 \Rightarrow \approx \left( \frac{dI_q^{vac}}{dzd\vartheta} + \frac{dI_{\bar{q}}^{vac}}{dzd\vartheta} \right) \times \Theta(\vartheta_{q\bar{q}} > \vartheta_g)$$

angular-ordering!

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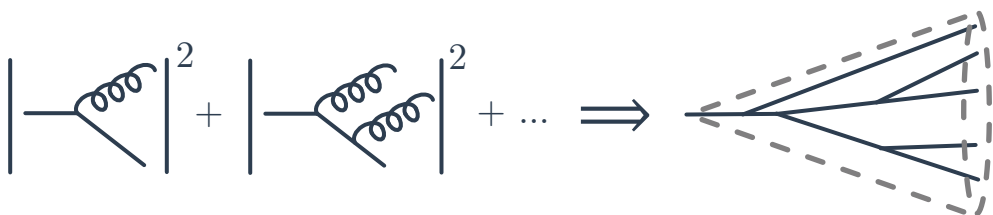
Medium resolution:

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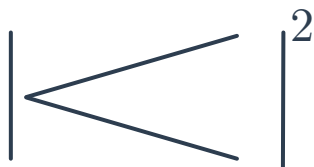
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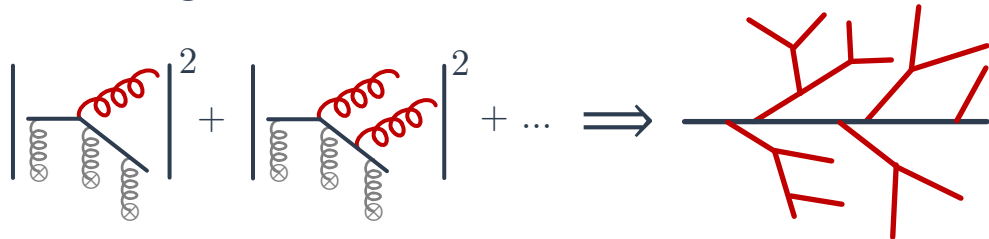
Color-coherence:

$$\left| \begin{array}{c} \diagup \\ \text{wavy line} \\ \diagdown \end{array} + \begin{array}{c} \diagdown \\ \text{wavy line} \\ \diagup \end{array} \right|^2 \Rightarrow \approx \left( \frac{dI_q^{vac}}{dzd\vartheta} + \frac{dI_{\bar{q}}^{vac}}{dzd\vartheta} \right) \times \Theta(\vartheta_{q\bar{q}} > \vartheta_g)$$

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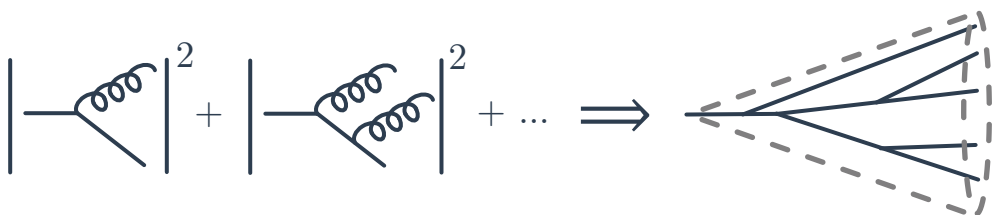
Medium resolution:

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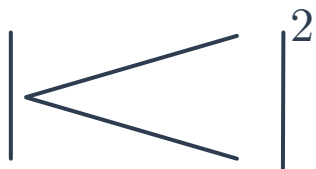
# Color-coherence in medium

## Vacuum

Resumming many emissions: collinear **jet**



Color-conservation:



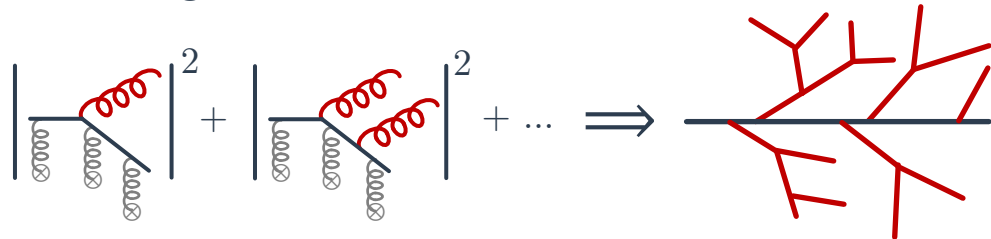
Color-coherence:

$$\left| \begin{array}{c} \diagup \\ \text{gluon} \\ \diagdown \end{array} + \begin{array}{c} \diagup \\ \text{gluon} \\ \diagdown \end{array} \right|^2 \Rightarrow \approx \left( \frac{dI_q^{vac}}{dzd\vartheta} + \frac{dI_{\bar{q}}^{vac}}{dzd\vartheta} \right) \times \Theta(\vartheta_{q\bar{q}} > \vartheta_g)$$

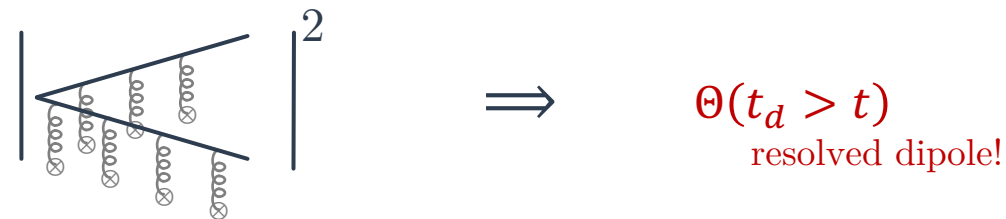
angular-ordering!

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wide-angle medium **cascade**



Decoherence time:

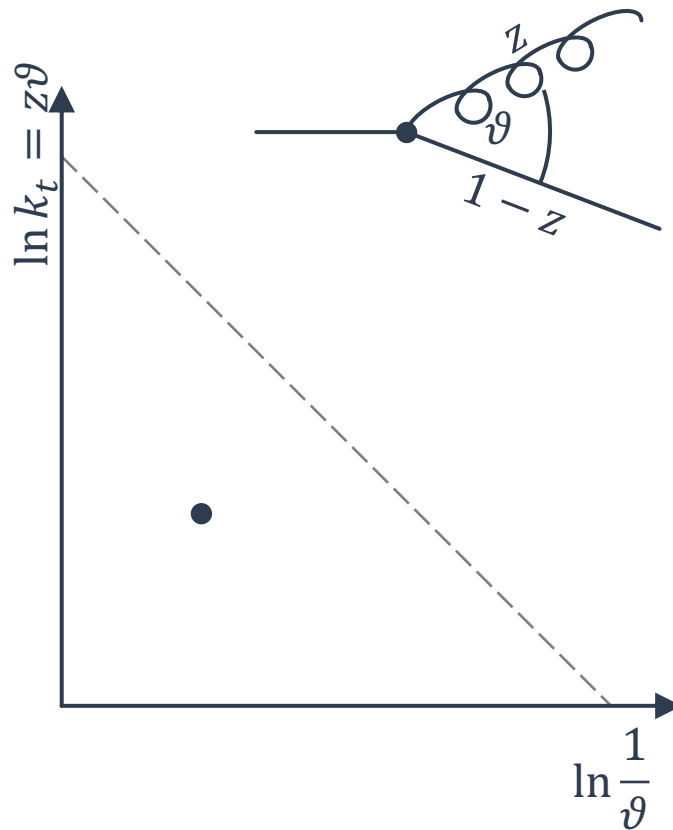


Medium resolution:

$$\left| \begin{array}{c} \diagup \\ \text{gluon} \\ \diagdown \end{array} + \begin{array}{c} \diagup \\ \text{gluon} \\ \diagdown \end{array} \right|^2 \Rightarrow \approx \left( \frac{dI_q^{med}}{dzd\vartheta} + \frac{dI_{\bar{q}}^{med}}{dzd\vartheta} \right) \times \Theta(t_f > t_d)$$

# Color-coherence in medium

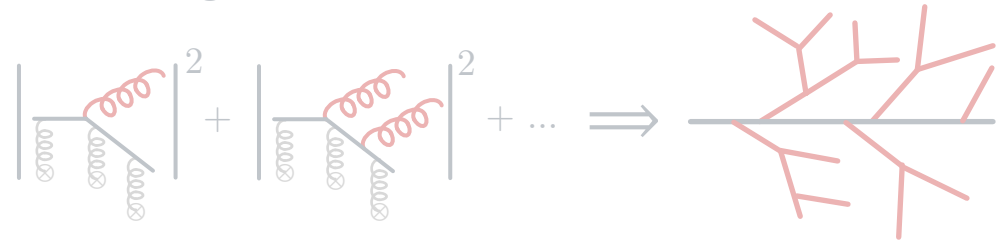
Vacuum



angular-ordering!

Medium

wide-angle medium cascade



Decoherence time:

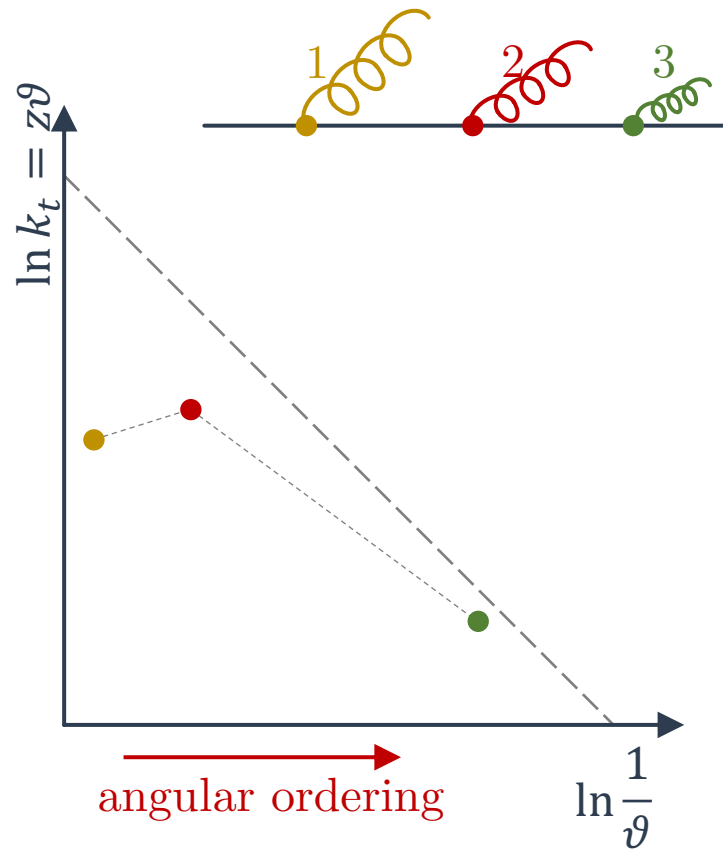


Medium resolution:

$$| \text{splitting} |^2 \Rightarrow \approx \left( \frac{dI_q^{med}}{dzd\vartheta} + \frac{dI_{\bar{q}}^{med}}{dzd\vartheta} \right) \times \Theta(t_f > t_d)$$

# Color-coherence in medium

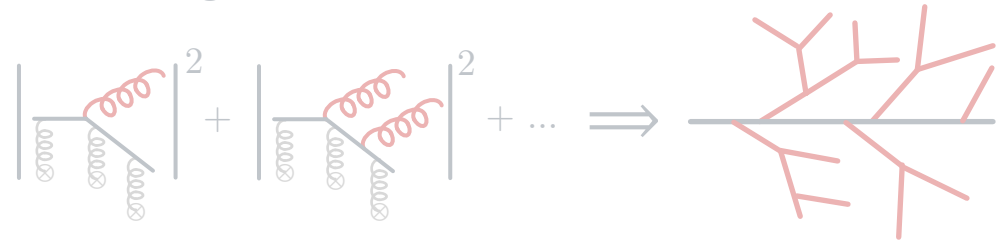
## Vacuum



angular-ordering!

## Medium

wide-angle medium cascade



Decoherence time:



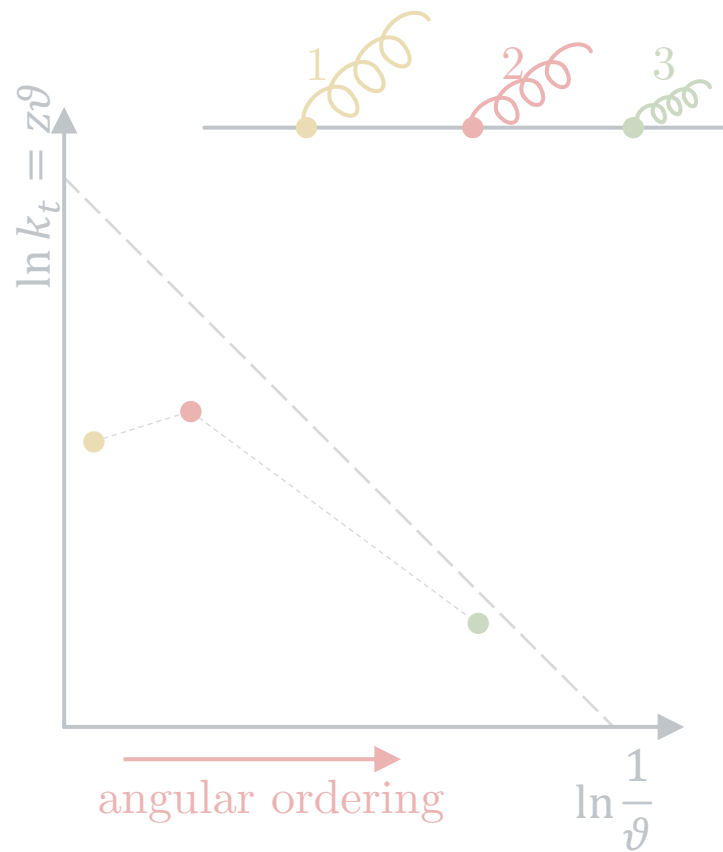
Medium resolution:

$\approx \left( \frac{dI_q^{med}}{dzd\vartheta} + \frac{dI_{\bar{q}}^{med}}{dzd\vartheta} \right)$   
 $\times \Theta(t_f > t_d)$

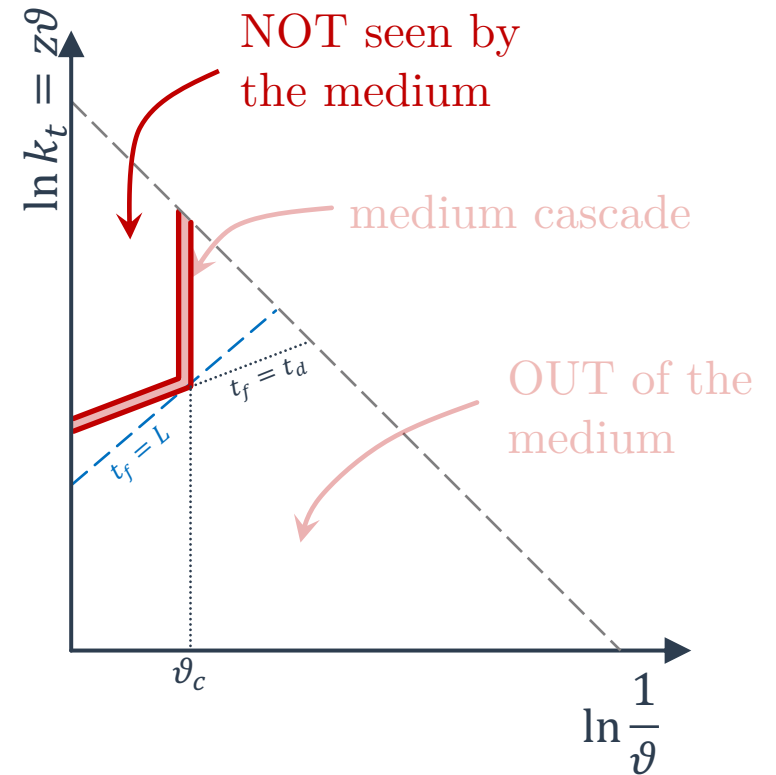


# Color-coherence in medium

Vacuum



Medium



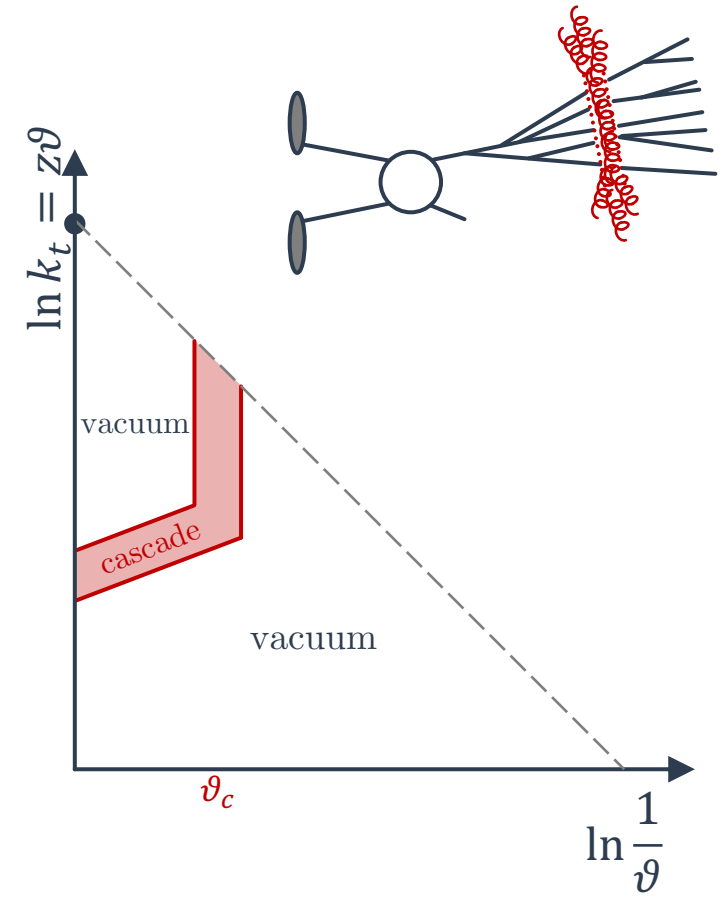
# Factorized picture of jet evolution in medium

[Blaizot,Dominguez,Iancu,Mehtar-Tani]

[Mehtar-Tani,Salgado,Tywoniuk]

[Caucal,Iancu,Mueller,Soyez]

1. Hard scattering is unaffected\*
2. Vacuum parton shower is unaffected
3. Switching at:  $L > t_d = t_f$
4. Cascade of medium-induced emissions
5. Vacuum parton shower is unaffected#



# Testing color-coherence and the factorized picture

# How to test color-coherence?

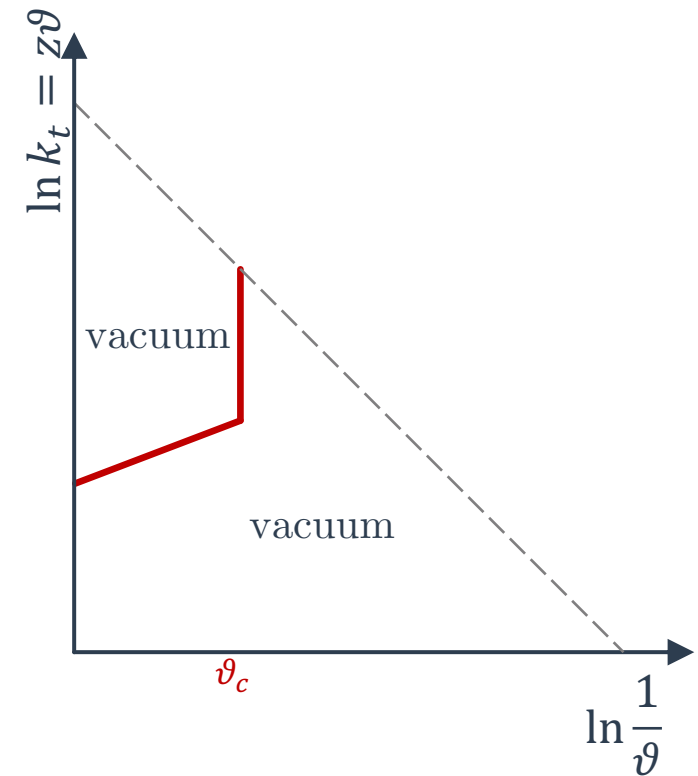
[see Martha Verweij's talk]

$R_{AA}$  measurements (**with bkg subtraction!**):

- small  $R$  - dependence of  $R_{AA}$
- high  $p_T$  - dependence of  $R_{AA}$
- big centrality ( $L$ ) dependence of  $R_{AA}$

Jet substructure:

- **Dynamical grooming**, SoftDrop
- $R_{AA}$  vs. substructure



# How to test color-coherence?

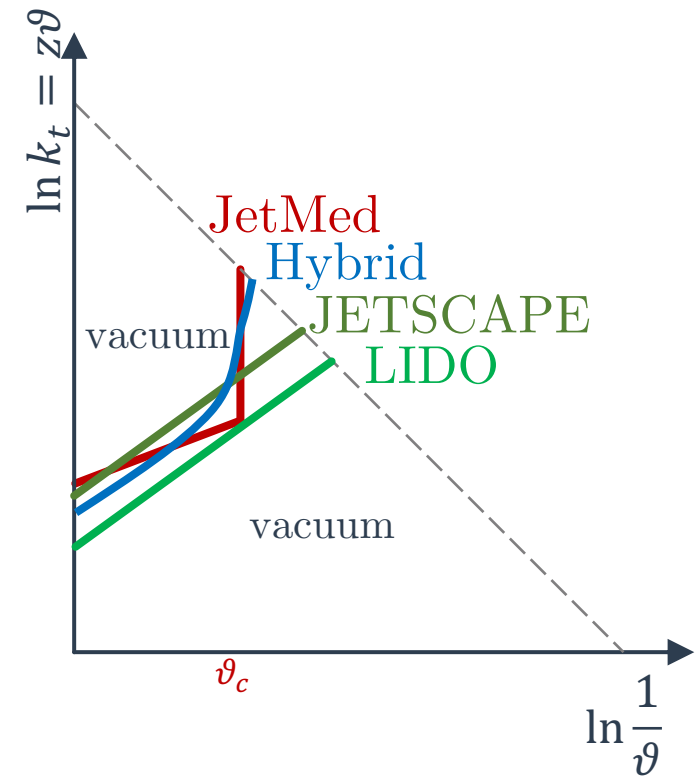
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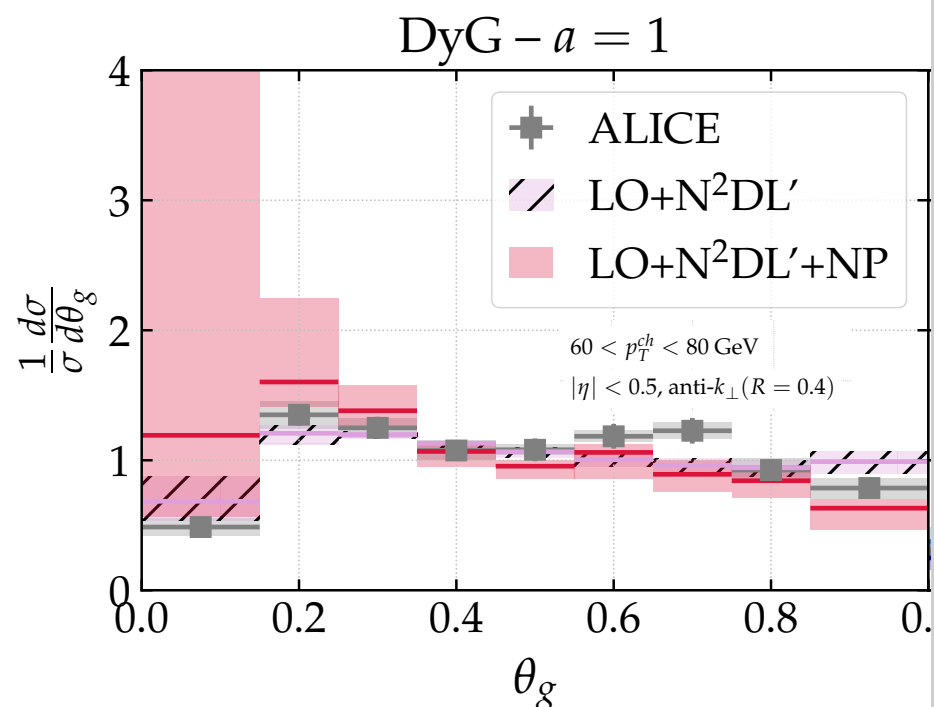


# Angle of the hardest branching

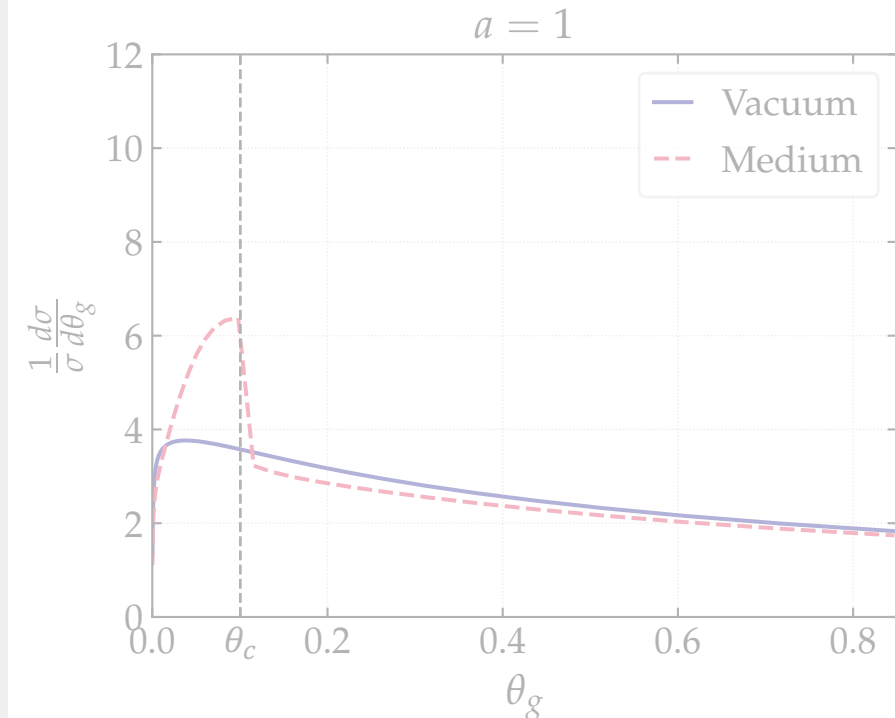
[Caucal,Soto-Ontoso,Takacs]

Precise pQCD calculation in pp  
[arXiv:2103.06566]

Changes in AA  
[arXiv:2111.14768]



[ALICE 2204.10246]



[Caucal,Soto-Ontoso,Takacs]

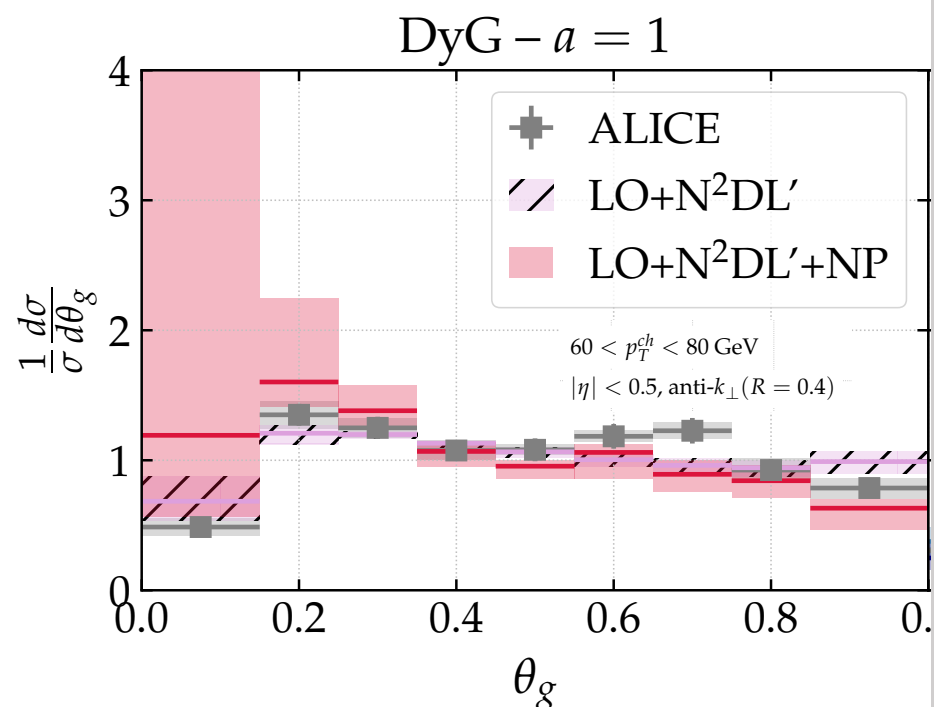
huge enhancement around  $\vartheta_c$ !

# Angle of the hardest branching

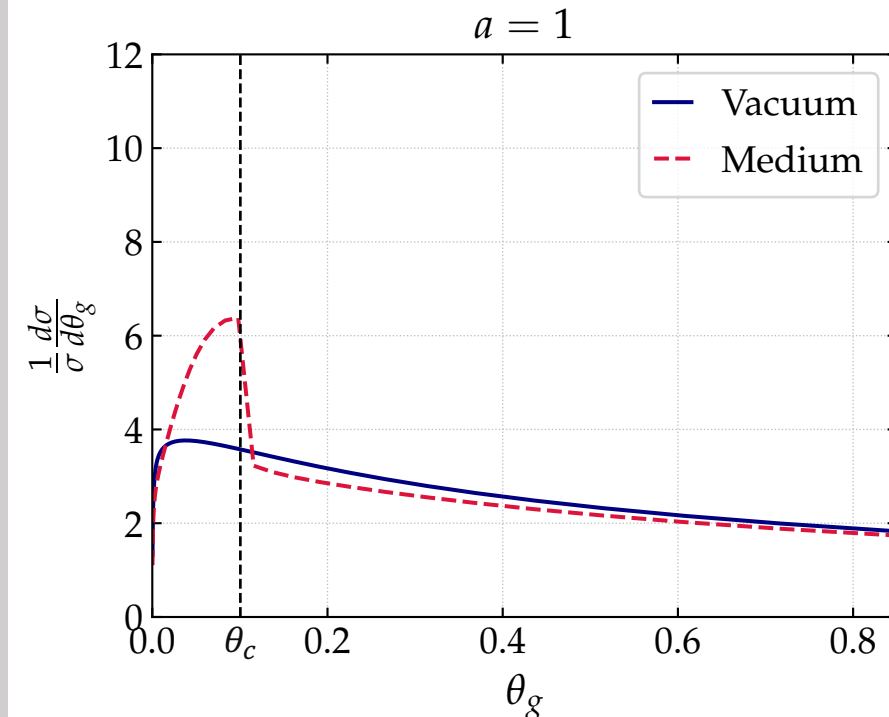
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[ALICE 2204.10246]



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# Is $\vartheta_c$ really measurable?

[Caucal,Soto-Ontoso,Takacs,arXiv:2111.14768]

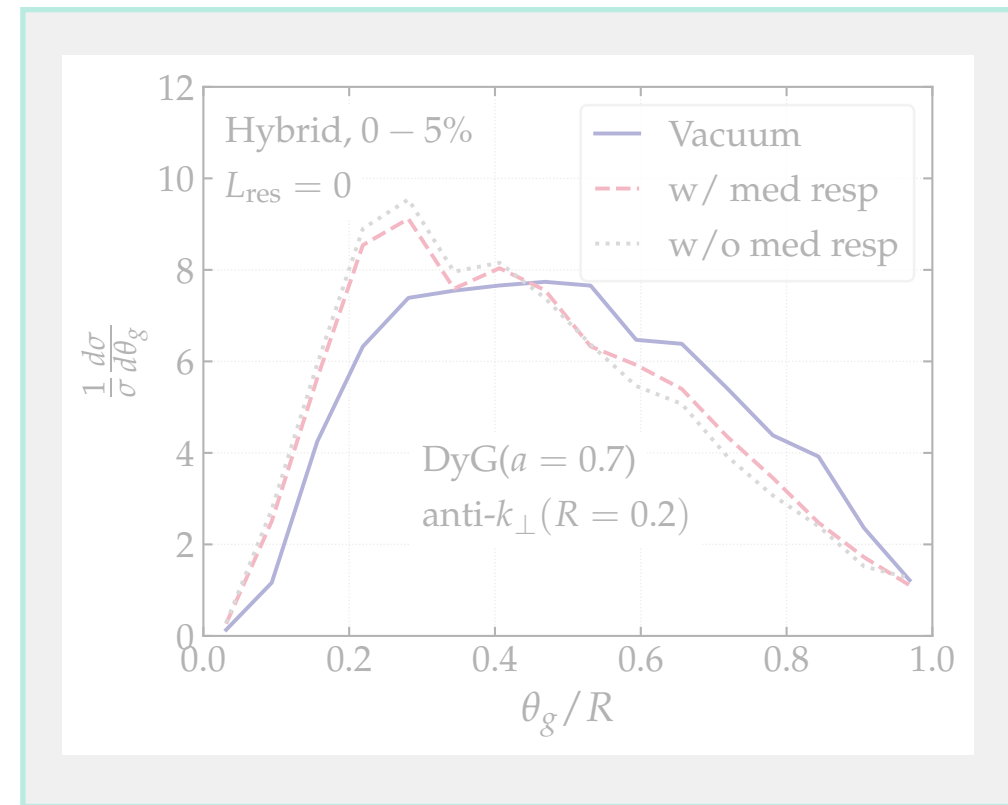
- HI event generator study:

**JetMed** [Caucal,Iancu,Soyez]

**Jewel** [Zapp,Krauss,Wiedemann]

**Hybrid** [Casalderrey-S,Milhano,Pablos,Rajagopal]

- Non-perturbative physics:
  - Fluctuating background
  - Medium response
  - Hadronization



Enhancement remains!

Best chance to measure  $\vartheta_c$ :

- $R = 0.2$ , DyG  $a = 0.2$



# Is $\vartheta_c$ really measurable?

[Caucal,Soto-Ontoso,Takacs,arXiv:2111.14768]

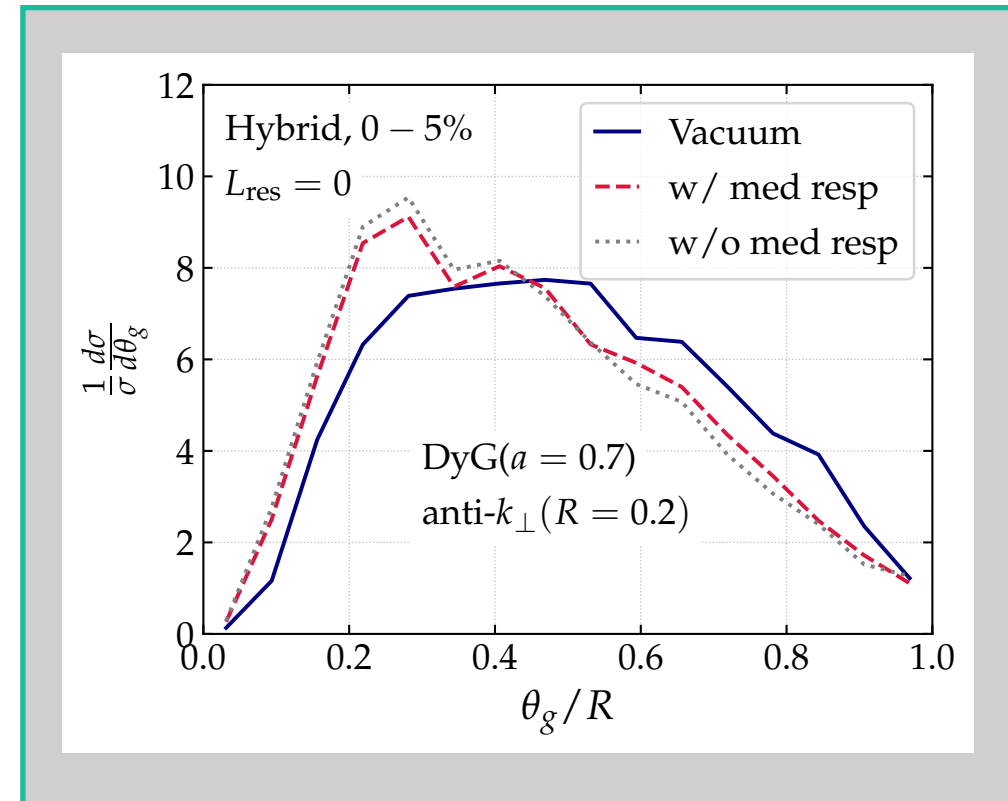
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# Summary

# Summary

- What is **perturbative**, and what is **weakly coupled**.
- **Color-coherence** results in **angular ordering** in vacuum.
- In medium, color-connections gets **resolved** and **decohere**

$\Rightarrow$  **Factorized picture** of jet energy loss

- Testing the factorized picture
- **Dynamical grooming** to measure  $\vartheta_c$

Thank you for the attention!

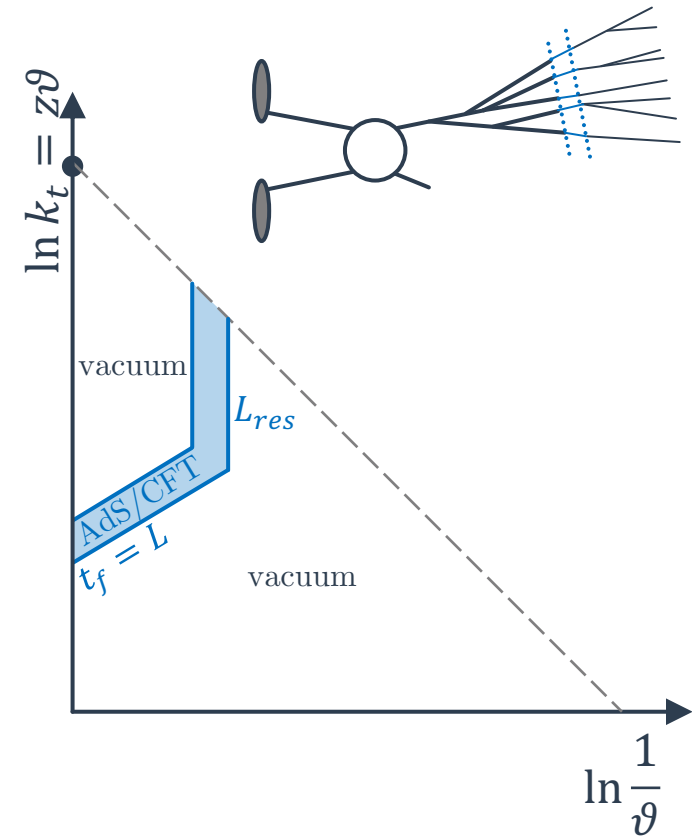


# Other models and recent progression

# Color-coherence in Hybrid

[Casalderrey-S,Milhano,Pablos,Rajagopal]

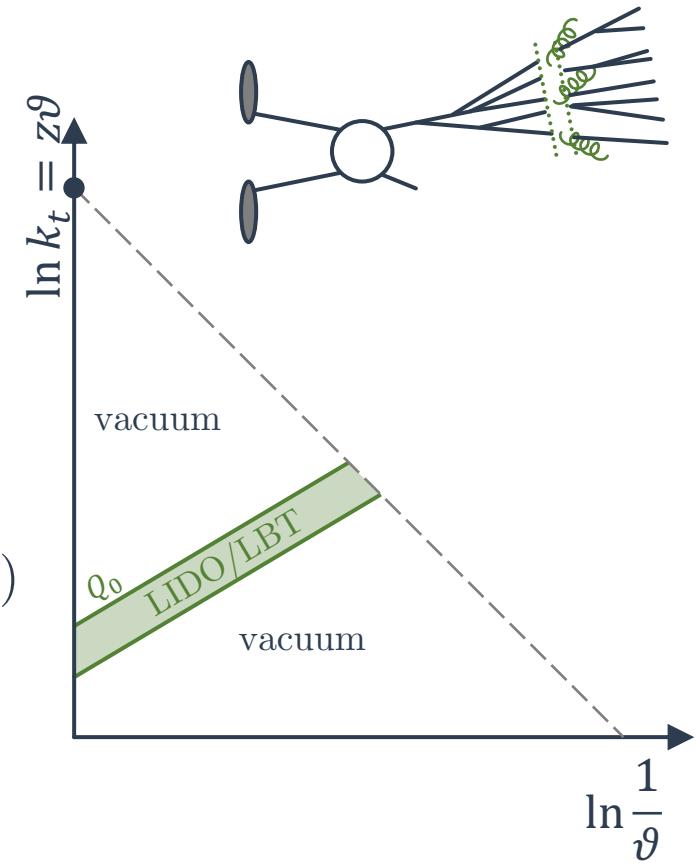
1. Hard scattering from Pythia8
2. Vacuum parton shower is unaffected
3. Switching scale: formation time & dipole size
4.  $\text{AdS/CFT}$  energy-loss
5. Vacuum parton shower the rest



# Color-coherence in LIDO

[Ke, Wang]

1. Hard scattering from Pythia8
2. Vacuum parton shower is unaffected
3. Switching scale in virtuality
4. LIDO/LBT (LO QCD  $2 \rightarrow 2$ , and  $1 \rightarrow 2$  higher-twist)
5. Vacuum parton shower the rest

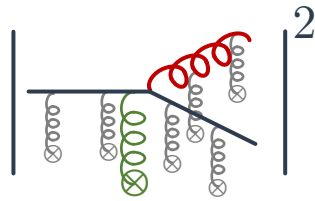


# Recent improvements: soft + hard scatterings

[Opacity expansion: Gyulassy, Levai, Vitev, Wiedeman, Higher-twist: Wang, Majumder]

[IOE formalism: Barata, Isaksen, Mehtar-Tani, Soto-Ontoso, Takacs, Tywoniuk]

Emission in medium:

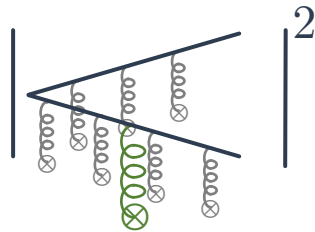


$\Rightarrow$

$$\frac{dI_i^{med}}{dz} = \int d\vartheta \frac{dI}{dzd\vartheta} \approx \frac{\alpha_s}{\pi} \sqrt{\frac{\hat{q}L^2}{4E}} \frac{2C_i}{\sqrt{z^3}} [1 + \mathcal{O}(1^{st} \text{ opacity})]$$

small modification of the cascade!

Decoherence time (destroying color-connections):

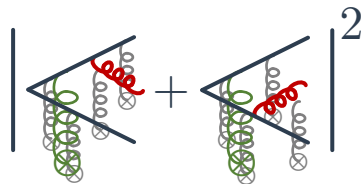


$\Rightarrow$

$$\Delta^{med}(t) = \Theta(t_d > t) [1 + \mathcal{O}(1^{st} \text{ opacity})]$$

modification of coherence!

Angular ordering:



$\Rightarrow$

$$\frac{dI_{q\bar{q}}^{med}}{dzd\vartheta} \approx ?$$

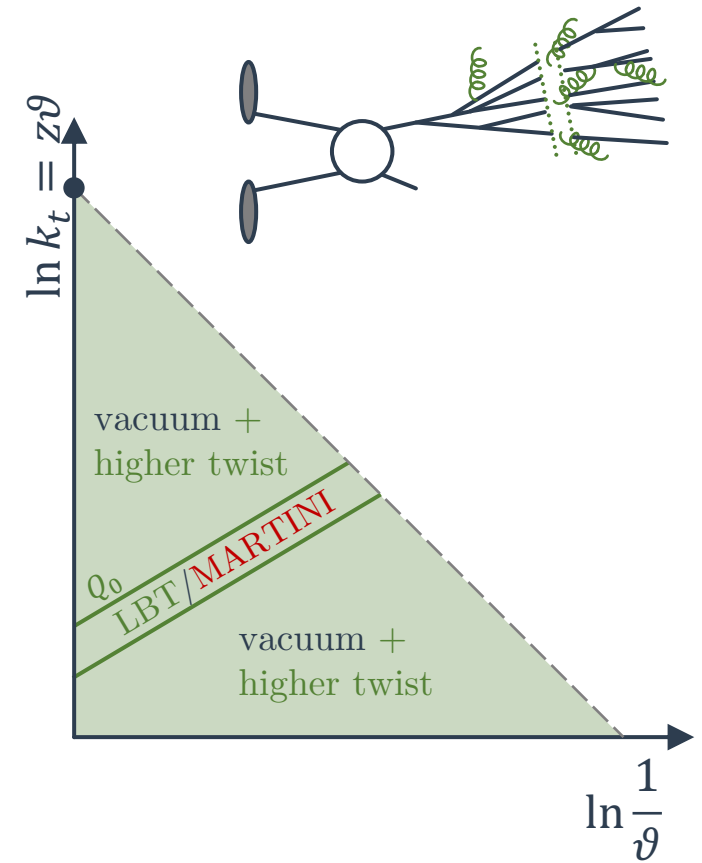
work in progress!



# Color-coherence in OLD JETSCAPE

[Kumar et al, 2204.01163]

1. Hard scattering from Pythia8
2. **MATTER** (vacuum + higher-twist splittings)
3. Switching scale in virtuality
4. **LBT** (LO QCD  $2 \rightarrow 2$ , and  $1 \rightarrow 2$  higher-twist)
- MARTINI** (LO HTL  $2 \rightarrow 2$ , and  $1 \rightarrow 2$  splittings)
5. **MATTER** (vacuum + higher-twist splittings)



# Color-coherence in NEW JETSCAPE

[Kumar et al, 2301.02485]

1. Hard scattering from Pythia8
2. MATTER (vacuum + ~~higher-twist~~ splittings)
3. Switching scale in virtuality
4. **LBT** (LO QCD  $2 \rightarrow 2$ , and  $1 \rightarrow 2$  higher-twist)  
**MARTINI** (LO HTL  $2 \rightarrow 2$ , and  $1 \rightarrow 2$  splittings)
5. **MATTER** (vacuum + higher-twist splittings)

