

Institute of particle and nuclear physics, Charles University in Prague

Non-zero neutrino mass effects

## Neutrino oscillations

Neutrinos produced in weak interactions $\neq$ mass eigenstates (?)


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\left|\nu_{\alpha}\right\rangle=U_{\alpha 1}^{*}\left|\nu_{1}\right\rangle+U_{\alpha 2}^{*}\left|\nu_{2}\right\rangle
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B. Pontecorvo, Sov.Phys.JETP 6 (1957) 429

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NB Neutral kaon oscillations 1957
NB Muon neutrinos not beforel 962 !
M.L. Good, Phys. Rev. I06 (1957) 59 I

Lederman, Schwarz, Steinberger

## Neutrino oscillations

## Two-level QM aproximation:



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## Neutrino oscillations

## Two-level QM aproximation:

$$
|\psi, t\rangle=e^{-i H t}\left|\nu_{e}\right\rangle \quad\left\langle\nu_{e} \mid \psi, t\right\rangle=\left\langle\nu_{e}\right| e^{-i H t}\left|\nu_{e}\right\rangle=\sum_{i=1}^{2} e^{-i E_{i} t} U_{e i} U_{e i}^{*}
$$

Survival probability:

$$
P\left(\nu_{e} \rightarrow \nu_{e}\right)=\ldots=1-\sin _{\text {mixing angle }}^{2} 2 \theta \times \sin ^{2}\left(\frac{m_{2}^{2}-m_{1}^{2}}{4 E} L\right)
$$

## Mixing in the lepton sector...

$\begin{aligned} \text { Direct analogy with quarks: } & \mathcal{L} \ni \frac{g}{\sqrt{2}} \overline{u_{L}^{\alpha}} \gamma^{\mu} V_{\alpha i} d_{L}^{i} W_{\mu}^{+}+\text {h.c. } \\ & \mathcal{L} \ni \frac{g}{\sqrt{2}} \overline{\ell_{L}^{\alpha}} \gamma^{\mu} U_{\alpha i} \nu_{L}^{i} W_{\mu}^{-}+\text {h.c. }\end{aligned}$

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$$

$$
U=\left(\begin{array}{ccc}
c_{12} c_{13} & s_{12} c_{13} & s_{13} e^{-i \delta} \\
-c_{23} s_{12}-s_{23} c_{12} s_{13} e^{i \delta} & c_{23} c_{12}-s_{23} s_{12} s_{13} e^{i \delta} & s_{23} c_{13} \\
s_{23} s_{12}-c_{23} c_{12} s_{13} e^{i \delta} & -s_{23} c_{12}-c_{23} s_{12} s_{13} e^{i \delta} & c_{23} c_{13}
\end{array}\right)
$$

## Pontecorvo - Maki - Nakagawa - Sakata matrix

3 angles, I CP phase (visible in oscillations)

## Atmospheric neutrino oscillations (1998)



## Super-Kamiokande

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## Super-Kamiokande

50,000 tons of ultrapure water, about 11,000 PMTs

## Solar neutrino puzzle

## late 1960's: Homestake mine, SD

$$
\nu+{ }^{37} C l \rightarrow{ }^{37} A r^{*}+e^{-}
$$

Ray Davis jr.


John Bahcall


Only $1 / 3$ of the predicted flux observed!

## SNO (2000)



## Neutrino oscillation parameters

| Parameter | Best fit $\pm 1 \sigma$ | $2 \sigma$ range | $3 \sigma$ range |
| :--- | :--- | :--- | :--- |
| $\Delta m_{21}^{2}\left[10^{-5} \mathrm{eV}^{2}\right]$ | $7.55_{-0.16}^{+0.20}$ | $7.20-7.94$ | $7.05-8.14$ |
| $\left\|\Delta m_{31}^{2}\right\|\left[10^{-3} \mathrm{eV}^{2}\right](\mathrm{NO})$ | $2.50 \pm 0.03$ | $2.44-2.57$ | $2.41-2.60$ |
| $\left\|\Delta m_{31}^{2}\right\|\left[10^{-3} \mathrm{eV}^{2}\right](\mathrm{IO})$ | $2.42_{-0.04}^{+0.03}$ | $2.34-2.47$ | $2.31-2.51$ |
| $\sin ^{2} \theta_{12} / 10^{-1}$ | $3.20_{-0.16}^{+0.20}$ | $2.89-3.59$ | $2.73-3.79$ |
| $\theta_{12} /^{\circ}$ | $34.5_{-1.0}^{+1.2}$ | $32.5-36.8$ | $31.5-38.0$ |
| $\sin ^{2} \theta_{23} / 10^{-1}(\mathrm{NO})$ | $5.47_{-0.30}^{+0.20}$ | $4.67-5.83$ | $4.45-5.99$ |
| $\theta_{23} /^{\circ}$ | $47.7_{-1.7}^{+1.2}$ | $43.1-49.8$ | $41.8-50.7$ |
| $\sin ^{2} \theta_{23} / 10^{-1}(\mathrm{IO})$ | $5.51_{-0.30}^{+0.18}$ | $4.91-5.84$ | $4.53-5.98$ |
| $\theta_{23} /^{\circ}$ | $47.9_{-1.7}^{+1.0}$ | $44.5-48.9$ | $42.3-50.7$ |
| $\sin ^{2} \theta_{13} / 10^{-2}(\mathrm{NO})$ | $2.160_{-0.069}^{+0.083}$ | $2.03-2.34$ | $1.96-2.41$ |
| $\theta_{13} /^{\circ}$ | $8.45_{-0.14}^{+0.16}$ | $8.2-8.8$ | $8.0-8.9$ |
| $\sin ^{2} \theta_{13} / 10^{-2}$ (IO) | $2.220_{-0.076}^{+0.074}$ | $2.07-2.36$ | $1.99-2.44$ |
| $\theta_{13} /^{\circ}$ | $8.53_{-0.15}^{+0.14}$ | $8.3-8.8$ | $8.1-9.0$ |

Phys.Lett.B 782 (20I8) 633

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| :--- | :--- | :--- | :--- |
| $\delta / \pi(\mathrm{NO})$ | $1.32_{-0.15}^{+0.21}$ | $1.01-1.75$ | $0.87-1.94$ |
| $\delta /{ }^{\circ}$ | $238_{-27}^{+38}$ | $182-315$ | $157-349$ |
| $\delta / \pi(\mathrm{IO})$ | $1.56_{-0.15}^{+0.13}$ | $1.27-1.82$ | $1.12-1.94$ |
| $\delta /{ }^{\circ}$ | $281_{-27}^{+23}$ | $229-328$ | $202-349$ |

A clear laboratory signal of physics beyond the SM!

At least 2 neutrinos must be massive (though presumably very light)

Absolute neutrino mass scale
(indirect indications)

## Laboratory: beta decay spectrum



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KATRIN


$\mathrm{m}_{\mathrm{v}}<\mathrm{I} . \mathrm{I} \mathrm{eV}(90 \% \mathrm{CL})$, goal: $0.2 \mathrm{eV}(90 \% \mathrm{CL})$ after 1000 days of data taking

## Cosmology: neutrinos as a DM component

## stable + neutral + abundant

Critical density fraction in neutrinos : $\Omega_{\nu} h_{0}^{2} \sim 0.01 \times m_{\nu}[\mathrm{eV}]$
see cosmology lectures by Costas

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m_{\nu}[\mathrm{eV}] \lesssim 100 \times \Omega_{\nu} h_{0}^{2}
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Gershtein, Zeldovic 1966
R. Cowsik, J. McClelland, Phys.Rev.Lett. 29 (1972) 669-670

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Structure formation tells us that this can not be saturated!

## Structure formation with v-dominated DM


credit: K. Heitmann, Argonne NL

## Structure formation in the $\Lambda$ CDM cosmology

$Z=28.62$
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Supercluster-size!

# Devising massive neutrinos 

 in simple extensions of the SM
## Devising neutrino masses: the Dirac option

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All other matter fields in the SM are 4-component Dirac spinors

Dirac mass terms (QED-like): $m \overline{\psi_{L}} \psi_{R}+h . c$.


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In the SM these come from the Yukawa Lagrangian (in the broken phase)

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Y_{D i j} \overline{Q_{L i}}\langle H\rangle D_{R j}+Y_{U i j} \overline{Q_{L}}\langle\tilde{H}\rangle U_{R j}+Y_{E i j} \overline{L_{L i}}\langle H\rangle E_{R j}
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How about simply adding a RH neutrino component?
This is non as trivial as it may seem...

## Charge dequantization in the SM with Dirac neutrinos

$S U(3) \times S U(2) \times U(1)$ gauge anomalies $\quad \mathcal{A}_{c} \propto \frac{1}{32 \pi^{2}} \operatorname{Tr}\left(\left\{T_{a}, T_{b}\right\} T_{c}\right) \tilde{F}_{\mu \nu}^{a} F^{b \mu \nu}$

$$
\begin{aligned}
Q_{L} & =\left(3,2, Y_{Q}\right) \\
u_{R} & =\left(3,1, Y_{U}\right) \\
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R. Foot, H. Lew, and R. Volkas, J.Phys.G G19, 361 (1993)

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Trick: just $\mathrm{SU}(2) \times \mathrm{U}(\mathrm{I})+$ Yukawas $\quad Q_{L}=\left(3,2, Y_{Q}\right)$
$\mathrm{SU}(2)^{2} \mathrm{U}(1)$ :

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$$
6 Y_{Q}+2 Y_{L}=0 \quad d_{R}=\left(3,1, Y_{D}\right)
$$

$\mathrm{U}(\mathrm{I})^{3}: \quad 12 Y_{Q}^{3}+4 Y_{L}^{3}-6 Y_{U}^{3}-6 Y_{D}^{3}-2 Y_{E}^{3}-2 Y_{N}^{3}=0 \quad L_{L}=\left(1,2, Y_{L}\right)$

$$
e_{R}=\left(1,1, Y_{E}\right)
$$



Yukawas: $\quad Y_{D i j} \overline{Q_{L i}}\langle H\rangle D_{R_{j}}+Y_{U i j}{\overline{Q_{L}}}_{i}\langle\tilde{H}\rangle U_{R_{j}}+Y_{E i j} \overline{L_{L i}}\langle H\rangle E_{R j}+Y_{N i j} \overline{L_{L i}}\langle\tilde{H}\rangle N_{R j}$

$$
\begin{array}{ll}
-Y_{Q}+Y_{D}+Y_{H}=0 & -Y_{L}+Y_{E}+Y_{H}=0 \\
-Y_{Q}+Y_{U}-Y_{H}=0 & -Y_{L}+Y_{N}-Y_{H}=0
\end{array}
$$

Solution:

$$
\begin{gathered}
Y_{Q}=+\frac{1}{6}-\frac{1}{3} Y_{N}, Y_{U}=+\frac{2}{3}-\frac{1}{3} Y_{N}, Y_{D}=-\frac{1}{3}-\frac{1}{3} Y_{N}, \\
Y_{L}=-\frac{1}{2}+Y_{N}, Y_{E}=-1+Y_{N} \quad Y_{N} \in \mathbb{R}
\end{gathered}
$$

R. Foot, H. Lew, and R. Volkas, J.Phys.G G19, 361 (1993)

## Charge dequantization in the SM with Dirac neutrinos

Symmetry argument: $B$ and $L$ anomalies in the SM

$$
\begin{gathered}
\operatorname{Tr}(\{Y, Y\} L)=\operatorname{Tr}(\{Y, Y\} B)=-\frac{1}{2} \quad \operatorname{Tr}\left(\left\{T_{L}^{3}, T_{L}^{3}\right\} L\right)=\operatorname{Tr}\left(\left\{T_{L}^{3}, T_{L}^{3}\right\} B\right)=\frac{1}{2} \\
\operatorname{Tr}(\{Y, Y\}(B-L))=0, \operatorname{Tr}\left(\left\{T_{L}^{3}, T_{L}^{3}\right\}(B-L)\right)=0, \ldots, \operatorname{Tr}(B-L)^{3} \neq 0
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With 3 RH neutrinos:

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Experimentally (neutron neutrality): $|\varepsilon|<10^{-21}$

## Another interesting feature of $B-L . .$.

$$
\begin{array}{cccc} 
& T_{L}^{3} & Y & Q \\
\binom{u}{d}_{L} & +\frac{1}{2} & +\frac{1}{2} & +\frac{1}{6} \\
+\frac{2}{3} \\
u_{R} & 0 & +\frac{1}{3} \\
d_{R} & 0 & -\frac{2}{3} & +\frac{2}{3} \\
& & & -\frac{1}{3} \\
\binom{\nu_{e}}{e}_{L} & +\frac{1}{2} & -\frac{1}{2} & 0 \\
& -\frac{1}{2} & & -1 \\
\nu_{R} & 0 & 0 & 0 \\
e_{R} & 0 & -1 & -1
\end{array}
$$

## Another interesting feature of $B-L . .$.

$$
\begin{aligned}
& T_{L}^{3} \quad Y \quad Q \quad(B-L) / 2 \\
& \begin{array}{llll}
\binom{u}{d}_{L} & \begin{array}{lll}
+\frac{1}{2} & +\frac{1}{6} & +\frac{2}{3} \\
-\frac{1}{2}
\end{array} & \begin{array}{l}
-\frac{1}{3}
\end{array}
\end{array} \\
& +\frac{1}{6} \\
& u_{R} \\
& 0 \quad+\frac{2}{3} \\
& +\frac{2}{3} \\
& d_{R} \\
& 0 \quad-\frac{1}{3} \\
& -\frac{1}{3} \\
& +\frac{1}{6} \\
& \begin{array}{ccccc}
\binom{\nu_{e}}{e}_{L} & \begin{array}{c}
+\frac{1}{2} \\
-\frac{1}{2}
\end{array} & -\frac{1}{2} & 0 & -1
\end{array} \\
& \nu_{R} \\
& 0 \quad 0 \\
& 0 \begin{array}{lll}
0 & -1 & -1
\end{array} \\
& -\frac{1}{2}
\end{aligned}
$$

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$$
\begin{array}{ccccc} 
& T_{L}^{3} & Y & Q & (B-L) / 2 \\
\binom{u}{d}_{L} & \begin{array}{c}
+\frac{1}{2} \\
-\frac{1}{2}
\end{array} & \boxed{+\frac{1}{6}} & \begin{array}{c}
+\frac{2}{3} \\
-\frac{1}{3}
\end{array} & \boxed{+\frac{1}{6}} \\
u_{R} & 0 & +\frac{2}{3} & +\frac{2}{3} & \\
d_{R} & 0 & -\frac{1}{3} & -\frac{1}{3} & +\frac{1}{6} \\
\binom{\nu_{e}}{e}_{L} & -\frac{1}{2} & -\frac{1}{2} & -\frac{1}{2} & 0 \\
\nu_{R} & 0 & 0 & 0 & -1 \\
e_{R} & 0 & -1 & -1 & -\frac{1}{2} \\
\hline
\end{array}
$$

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$$
\begin{align*}
& T_{L}^{3} \quad Y \\
& Q \\
& (B-L) / 2 \\
& \begin{array}{ll}
\binom{u}{d}_{L} & \begin{array}{l}
+\frac{1}{2} \\
-\frac{1}{2}
\end{array}
\end{array}  \tag{1}\\
& +\frac{2}{3} \\
& -\frac{1}{3} \\
& +\frac{1}{6}  \tag{0}\\
& u_{R} \\
& d_{R} \\
& +\frac{2}{3} \\
& -\frac{1}{3} \\
& +\frac{1}{6} \\
& +\frac{1}{2} \\
& -\frac{1}{2} \\
& \binom{\nu_{e}}{e}_{L} \quad \begin{array}{c}
+\frac{1}{2} \\
-\frac{1}{2}
\end{array} \quad \begin{array}{|c|}
\hline \frac{1}{2}
\end{array} \begin{array}{c}
0 \\
-1
\end{array} \\
& \begin{array}{l}
\nu_{R} \\
e_{R}
\end{array} \\
& \begin{array}{l}
+\frac{1}{2} \\
-\frac{1}{2}
\end{array}
\end{align*}
$$

## Another interesting feature of $B-L \ldots$

$$
\begin{align*}
& T_{L}^{3} \quad Y \\
& \begin{array}{ll}
\binom{u}{d}_{L} & \begin{array}{l}
+\frac{1}{2} \\
-\frac{1}{2}
\end{array}
\end{array}  \tag{0}\\
& +\frac{1}{6} \\
& +\frac{2}{3} \\
& -\frac{1}{3} \\
& (B-L) / 2 \\
& Q \\
& +\frac{1}{6} \\
& +\frac{2}{3} \\
& -\frac{1}{3} \\
& +\frac{1}{6} \\
& +\frac{1}{2} \\
& -\frac{1}{2} \\
& \binom{\nu_{e}}{e}_{L} \quad \begin{array}{c}
+\frac{1}{2} \\
-\frac{1}{2}
\end{array} \begin{array}{|}
-\frac{1}{2} & \begin{array}{c}
0 \\
-1
\end{array} & \boxed{-\frac{1}{2}}
\end{array}  \tag{0}\\
& \begin{array}{c}
\nu_{R} \\
e_{R}
\end{array} \\
& \text { T33-like } \\
& \text { generator } \\
& \text { for RH fields! } \\
& +\frac{1}{2} \\
& -\frac{1}{2}
\end{align*}
$$

## Another interesting feature of $B-L \ldots$

$$
\begin{align*}
& T_{L}^{3} \quad Y \quad Q \quad(B-L) / 2 \\
& \binom{u}{d}_{L} \quad \begin{array}{l}
+\frac{1}{2} \\
-\frac{1}{2}
\end{array}++\frac{1}{6} \quad \begin{array}{l}
+\frac{2}{3} \\
-\frac{1}{3}
\end{array} \quad++\frac{1}{6}  \tag{0}\\
& \text { T3-like } \\
& \text { generator } \\
& \text { for RH fields! } \\
& +\frac{1}{2} \\
& -\frac{1}{2} \\
& +\frac{1}{2} \\
& -\frac{1}{2}
\end{align*}
$$

## Majorana spinors

## E. Majorana 1937:

Neutral spinor can be massive even with 2 components only!!!

E. Majorana

## Majorana spinors

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## RH neutrino is a full $\operatorname{SU}(3) \times S U(2)$ singlet

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\mathcal{L} \ni \bar{L}_{L} Y_{\nu} N_{R} \tilde{H}+\frac{1}{2} N_{R}^{T} C M_{R} N_{R}+h . c .
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$$

If we engage this, the $\mathbf{N}_{\mathbf{R}}$ hypercharge must be zero!
Charge quantization through anomalies restored!

## Seesaw mechanism

P. Minkowski, Phys. Lett. B67, 42 I (1977)

$$
\begin{gathered}
\mathcal{L} \ni \bar{\nu}_{L} m_{D} N_{R}+\frac{1}{2} M_{R} N_{R}^{T} C N_{R}+h . c .=\frac{1}{2} n_{L}^{T} C \mathcal{M} n_{L}+h . c . \\
\mathcal{M}=\left(\begin{array}{cc}
0 & m_{D} \\
m_{D} & M_{R}
\end{array}\right) \quad n_{L}=\binom{\nu_{L}}{\left(N_{R}\right)^{C}}
\end{gathered}
$$

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\begin{gathered}
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m_{D} & M_{R}
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\end{gathered}
$$

Suppose $m_{D} \ll M_{R}$ :
$m_{1}=-\frac{m_{D}^{2}}{M_{R}}$
$n_{1} \propto \nu_{L}+\mathcal{O}\left(\frac{m_{D}}{M_{R}}\right)\left(N_{R}\right)^{c}$
$m_{2}=M_{R}$

$$
n_{2} \propto\left(N_{R}\right)^{c}+\mathcal{O}\left(\frac{m_{D}}{M_{R}}\right) \nu_{L}
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$$
n_{2} \propto\left(N_{R}\right)^{c}+\mathcal{O}\left(\frac{m_{D}}{M_{R}}\right) \nu_{L}
$$



## Neutrino masses are naturally suppressed if $M_{R}$ is large!

NB the argument is not water-tight (Yukawas self-renormalize)
$M_{R} \sim 10^{12-14} \mathrm{GeV}$

Lepton number violation (?)

## $L$ and $B$ are not sacred in the SM anyway...

## Renormalizable case: anomalous global symmetries

- Instantons (at zeroT) cause $9 q+3 l \leftrightarrow \emptyset$


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Non-renormalizable (effective) case: L broken explicitly at d=5

$$
\begin{aligned}
& \mathcal{L}_{5} \sim \frac{c}{\Lambda}\left(L^{T} i \sigma_{2} H\right) C\left(H^{T} i \sigma_{2} L\right) \quad \text { Weinberg's operator } \\
& \text { S.Weinberg, PRL43, I } 566 \text { (I979) }
\end{aligned}
$$

## PMNS mixing in the Majorana case

## Maiorana mass

$$
\frac{1}{2} m \psi_{L}^{T} C \psi_{L}+h . c .
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$$
\begin{gathered}
\text { Charged currents: } \mathcal{L} \ni \frac{g}{\sqrt{2}} \overline{\ell_{L}^{\alpha}} \gamma^{\mu} U_{\alpha i} \nu_{L}^{i} W_{\mu}^{-}+h . c . \\
U=\left(\begin{array}{ccc}
c_{12} c_{13} & s_{12} c_{13} & s_{13} e^{-i \delta} \\
-s_{12} c_{23}-c_{12} s_{23} s_{13} e^{i \delta} & c_{12} c_{23}-s_{12} s_{23} s_{13} e^{i \delta} & s_{23} c_{13} \\
s_{12} s_{23}-c_{12} c_{23} s_{13} e^{i \delta} & -c_{12} s_{23}-s_{12} c_{23} s_{13} e^{i \delta} & c_{23} c_{13}
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s_{12} s_{23}-c_{12} c_{23} s_{13} e^{i \delta} & -c_{12} s_{23}-s_{12} c_{23} s_{13} e^{i \delta} & c_{23} c_{13}
\end{array}\right)\left(\begin{array}{c}
1 \\
e^{i \alpha_{1}} \\
\\
\\
e^{i \alpha_{2}}
\end{array}\right)
\end{gathered}
$$

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1 \\
\\
e^{i \alpha_{1}} \\
\\
\\
e^{i \alpha_{2}}
\end{array}\right)
\end{gathered}
$$

3 physical CP phases (I Dirac, 2 Majorana)!

## L violation in neutrinoless double beta decay

## Double beta decay


"Standard" double beta decay: $\quad 2 n \rightarrow 2 p^{+}+2 e^{-}+2 \bar{\nu}$

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Isotopes: ${ }^{48} \mathrm{Ca},{ }^{76} \mathrm{Ge},{ }^{82 \mathrm{Se},}{ }^{96} \mathrm{Zr},{ }^{100 \mathrm{Mo},}{ }^{116} \mathrm{Cd},{ }^{130} \mathrm{Te},{ }^{136} \mathrm{Xe},{ }^{150 \mathrm{Nd}}$

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## Neutrinoless double beta decay - lifetime estimates

## Diagrammatics:



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Figures from Chakrabortty et al., 2012

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Heavy neutrinos also feel gauge interactions!


Figures from Chakrabortty et al., 2012

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Diagrammatics:

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Figures from Chakrabortty et al., 2012

## Neutrinoless double beta decay - lifetime estimates

Diagrammatics:

$\mathcal{A} \propto g^{4} \frac{\langle m\rangle}{q^{2}}$

Heavy neutrinos also feel gauge interactions!

$\mathcal{A} \propto g^{4} \sum_{i} F^{2} \frac{\kappa}{M_{i}}$

## Is this a test of the Majorana nature of neutrinos?

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That actually does not make a difference...

J. Schechter, J. F. W. Valle, PRD 1982 Takasugi, PLB 1984

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Takasugi, PLB 1984

If neutrinoless double beta decay is seen, neutrinos are inevitably Majorana...

## L violation in cosmology (?)

## The $\eta_{B}$ issue of the $S M$

## Baryon to photon \# density:

$$
\frac{n_{B}}{n_{\gamma}} \equiv \eta_{B}=(6.1 \pm 0.3) \times 10^{-10}
$$



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$$

This is actually a huge number!

Symmetric initial conditions: (+ Standard model)

$$
\eta_{\mathrm{SM}} \approx 10^{-18}
$$



## Cooking up a primordial baryon asymmetry

# Cooking up a primordial baryon asymmetry 

## I967: Sacharov's baryogenesis conditions



## Cooking up a primordial baryon asymmetry

## I 967: Sacharov's baryogenesis conditions

- Baryon number violation
- $\quad \mathrm{C}$ and CP violation

- Departure from thermal equilibrium


## Cooking up a primordial baryon asymmetry

## 1967: Sacharov's baryogenesis conditions

- Baryon number violation this is clear...
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## Cooking up a primordial baryon asymmetry

## 1967: Sacharov's baryogenesis conditions

- Baryon number violation this is clear...
- $C$ and $C P$ violation
 $\Gamma(X \rightarrow Y+B)=\Gamma(\bar{X} \rightarrow \bar{Y}+\bar{B})$
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## All this is there in the Standard Model (!)

## B+L generation during the EW phase transition?

Assume that "bubbles" grow below the EWPT critical temperature...


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Bubbles do not form for $\mathrm{m}_{\mathrm{H}}=125 \mathrm{GeV}$, not enough CPV in the SM !!!

## Baryogenesis through leptogenesis

 (are we here thanks to Majorana neutrinos?)
## Baryogenesis through leptogenesis

Perturbative LNV + nonperturbative BNV enough for baryogenesis
Fukugita, Yanagida, PLBI74, I 986

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2) Sphalerons provide $L$ to $B$ transitions before EWPT

Kuzmin, Rubakov, Shaposhnikov, PLBI55, I985

## Baryogenesis through leptogenesis



CP asymmetry:

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\epsilon_{1} \approx-\frac{3}{8 \pi} \frac{1}{\left(Y_{N} Y_{N}^{\dagger}\right)_{11}} \sum_{i=2,3} \operatorname{Im}\left[\left(Y_{N} Y_{N}^{\dagger}\right)_{1 i}^{2}\right] \frac{M_{1}}{M_{i}}
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Davidson-Ibarra bound:
S. Davidson and A. Ibarra, Phys. Lett. B535, 25 (2002)

$$
\left|\epsilon_{1}\right| \leq \frac{3}{16 \pi} \frac{M_{1}\left(m_{3}-m_{2}\right)}{v^{2}}
$$

$$
M_{1} \gtrsim 10^{9} \mathrm{GeV}
$$



