

Experience with AC dipole optics measurements at the old ESRF storage ring (2016-2018)

Andrea Franchi (ESRF, Grenoble)

Thanks to the Beam Dynamics & Diagnostics groups for the experimental campaign

FCC-ee meeting of Marc 22nd 2022

- Measuring ultra-low coupling via AC dipole and turn-by-turn (TbT) BPM data
- Simulation of beta-beating measurement via AC dipole and turn-by-turn (TbT) BPM data
- AC dipole and BPM TbT spectrum
- regarding $(1-\lambda^2)$

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Idea: replace pulsed excitation with continuous AC excitation close to the betatron tune, $d=Q-Q_{AC}$ (RHIC 1998 [*], Tevatron/RHIC 2008- [^], LHC 2009- [&],)

- thousands of TbT with no decoherence
 - efficient data cleaning
 - but some precautions & corrections to interpret data (theory not completed yet)
- } high spectral resolution

more recent: <https://www.bnl.gov/isd/documents/74582.pdf>

<https://accelconf.web.cern.ch/ipac2021/papers/wepab400.pdf>

<https://cds.cern.ch/record/2747899/files/CERN-ACC-NOTE-2020-0065.pdf>

[*] S. Peggs, C. Tang, RHIC/AP/159, 1998; M. Bai *et al.* , PRL **80**, 4673 (1998)

[^] R. Miyamoto, PhD thesis, Univ. of Texas, Austin 2008; BNL C-A/AP/#410, 2010; PRSTAB **11** 084002 (2008), X. Shen *et al.* , PRSTAB **16** 111001 (2013), ...

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Very successful on hadron machines (beating, coupling, nonlinearities). Can it work in lepton rings with radiation damping & diffusion (and high chroma @ ESRF)?

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Betatron coupling described by two CRDTs F_{xy} & F_{yx} (*)
 inferred from single-BPM x and y TBT data (i.e. without the
 evaluation of the momenta p_x and p_y which requires the use of
 pairs of BPMs thus introducing systematic errors)

$$F_{xy} = f_{1001} - f_{1010}^*$$

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PRSTAB 17 074001 (2014)

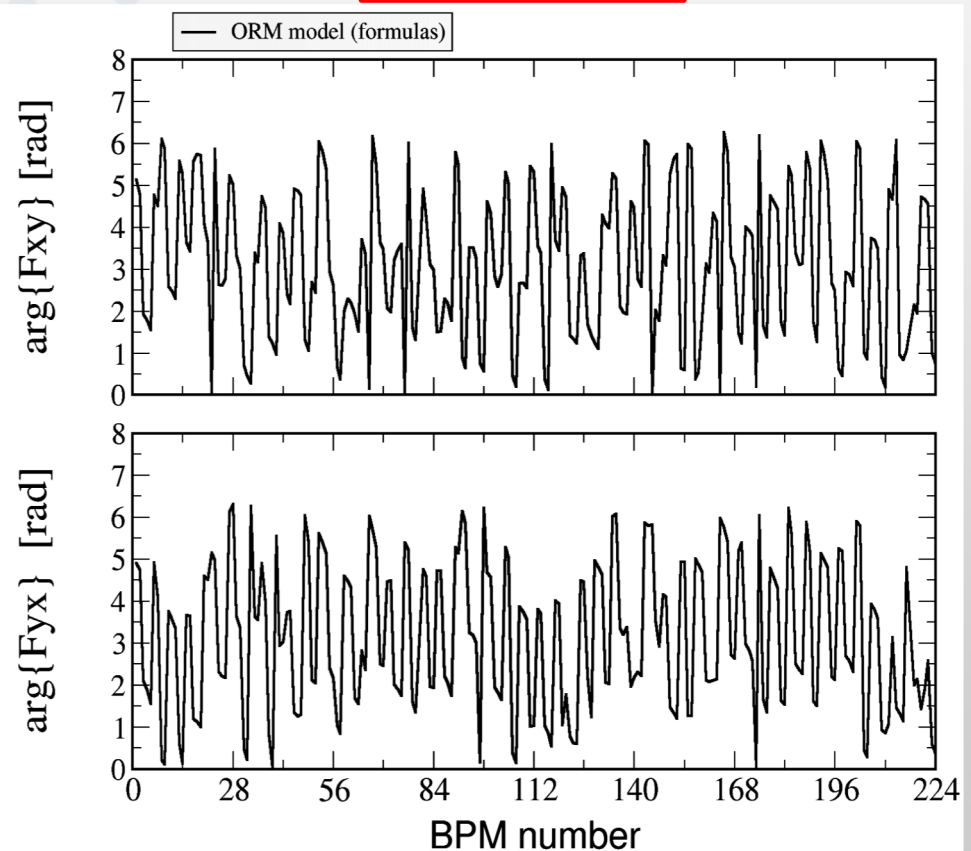
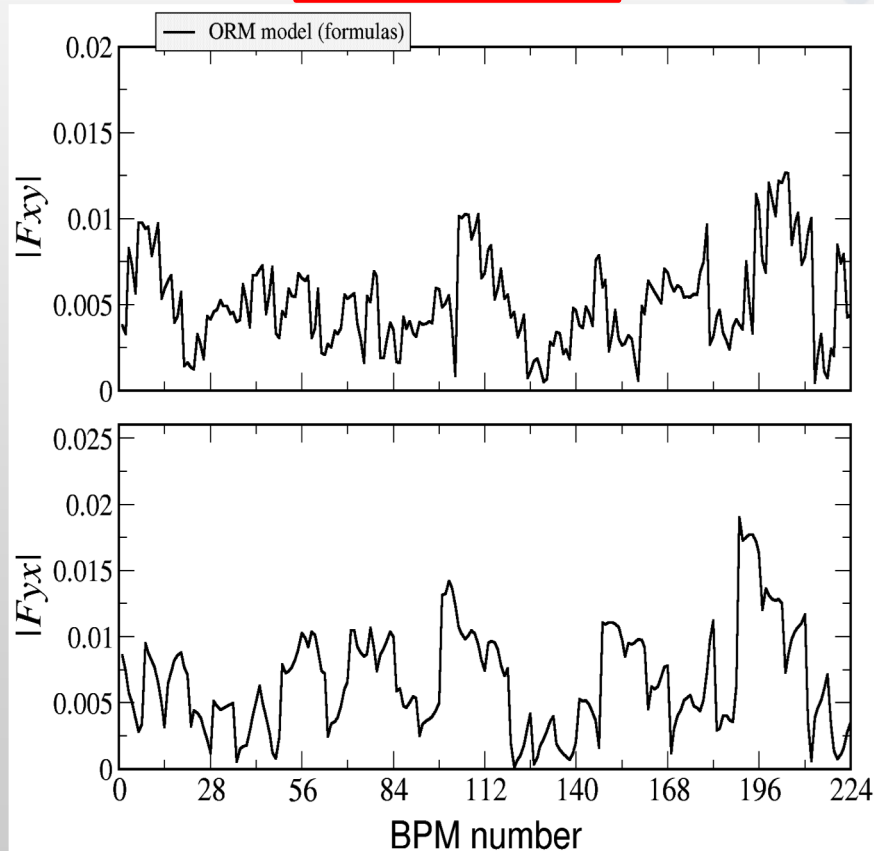
Betatron coupling described by two CRDTs F_{xy} & F_{yx} (*)

Measurement with **low chroma (0,0) & detuning sext. optics**

compare ($\epsilon_y/\epsilon_x \sim 1\text{‰}$) ORM model with TbT harmonic analysis

AMPLITUDE

PHASE



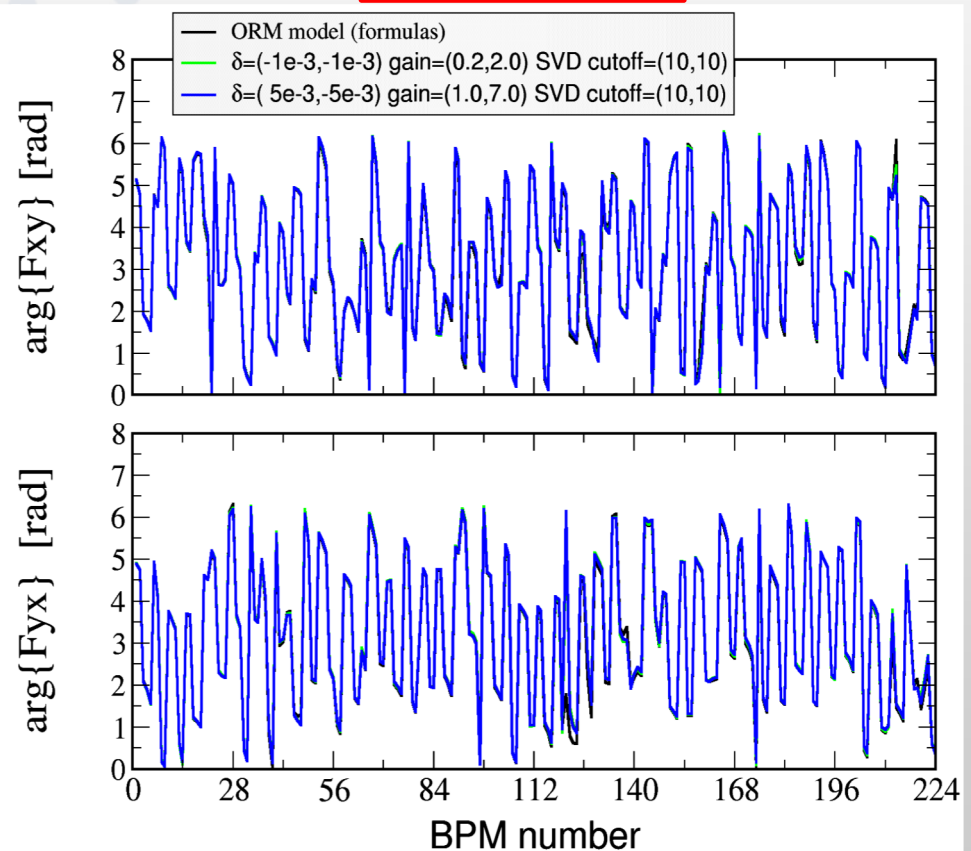
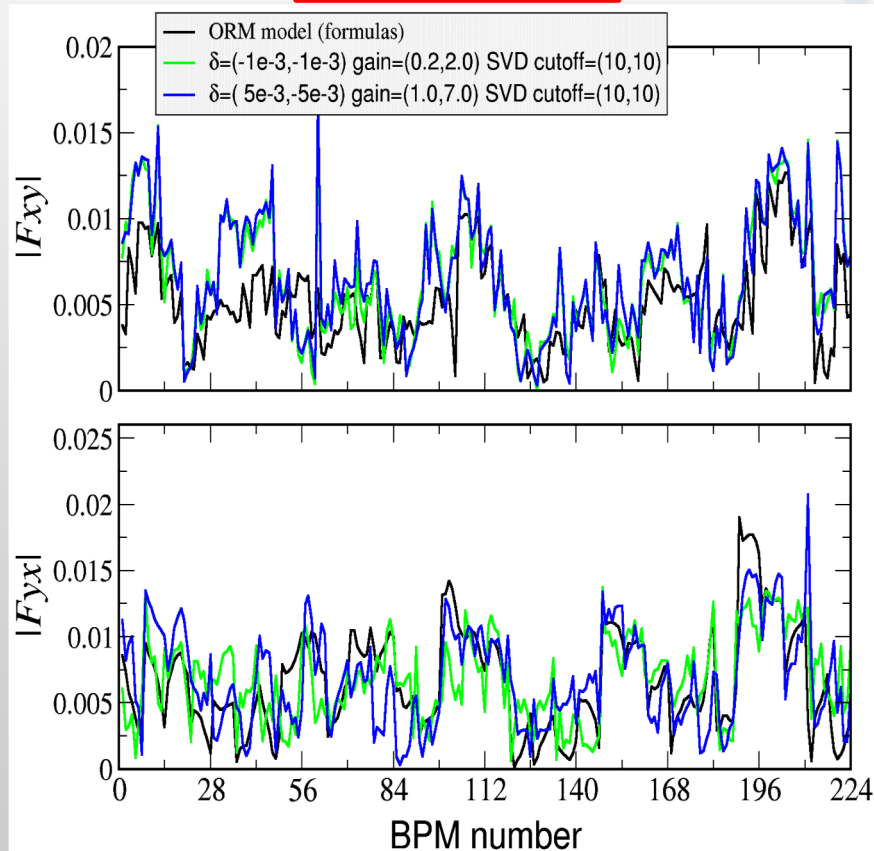
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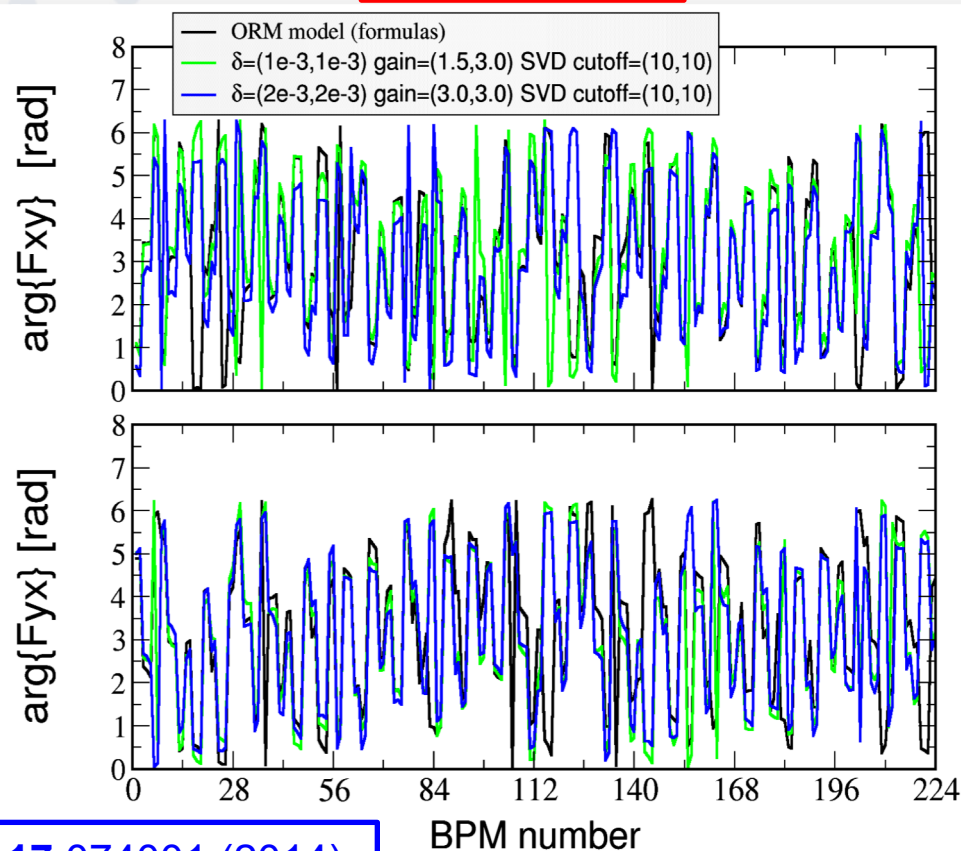
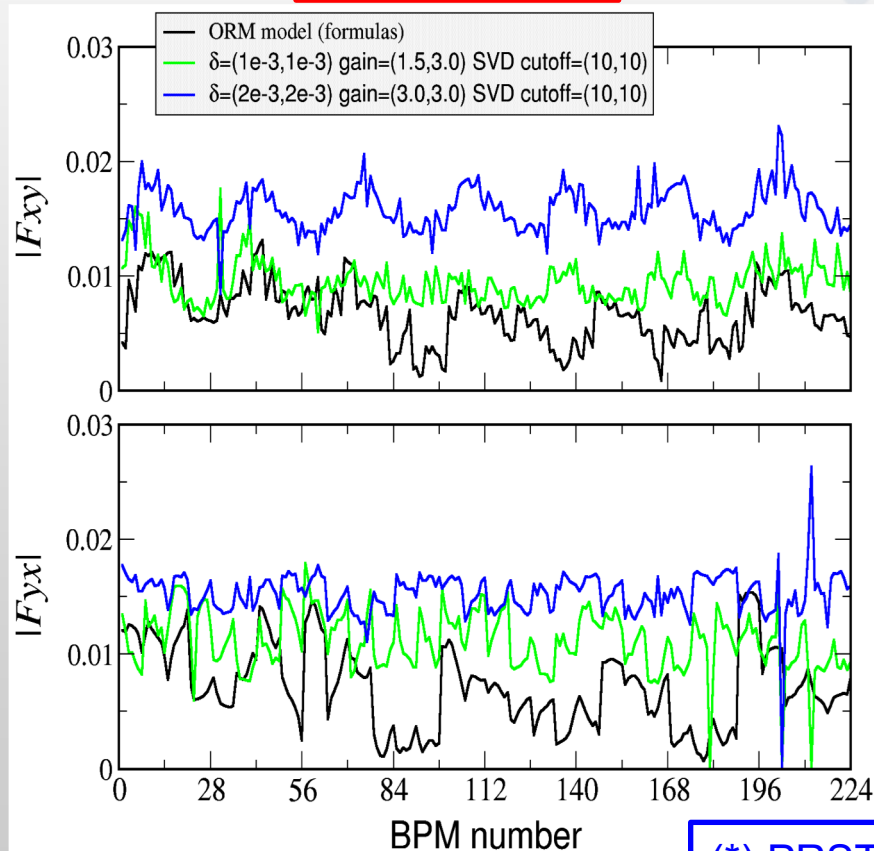
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Measurement with **large chroma (8,13) operational optics**

compare ($\epsilon_y/\epsilon_x \sim 1\%$) ORM model with TbT harmonic analysis

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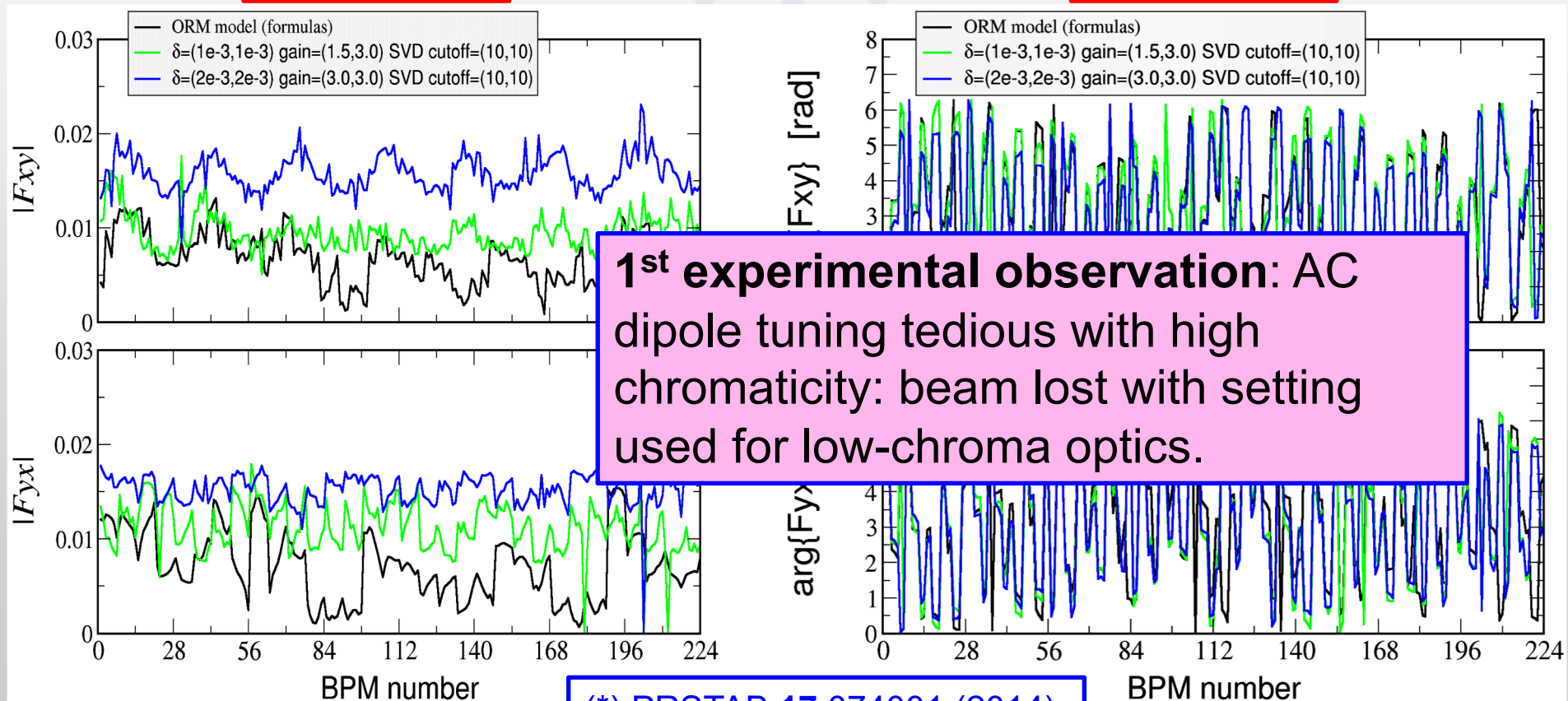
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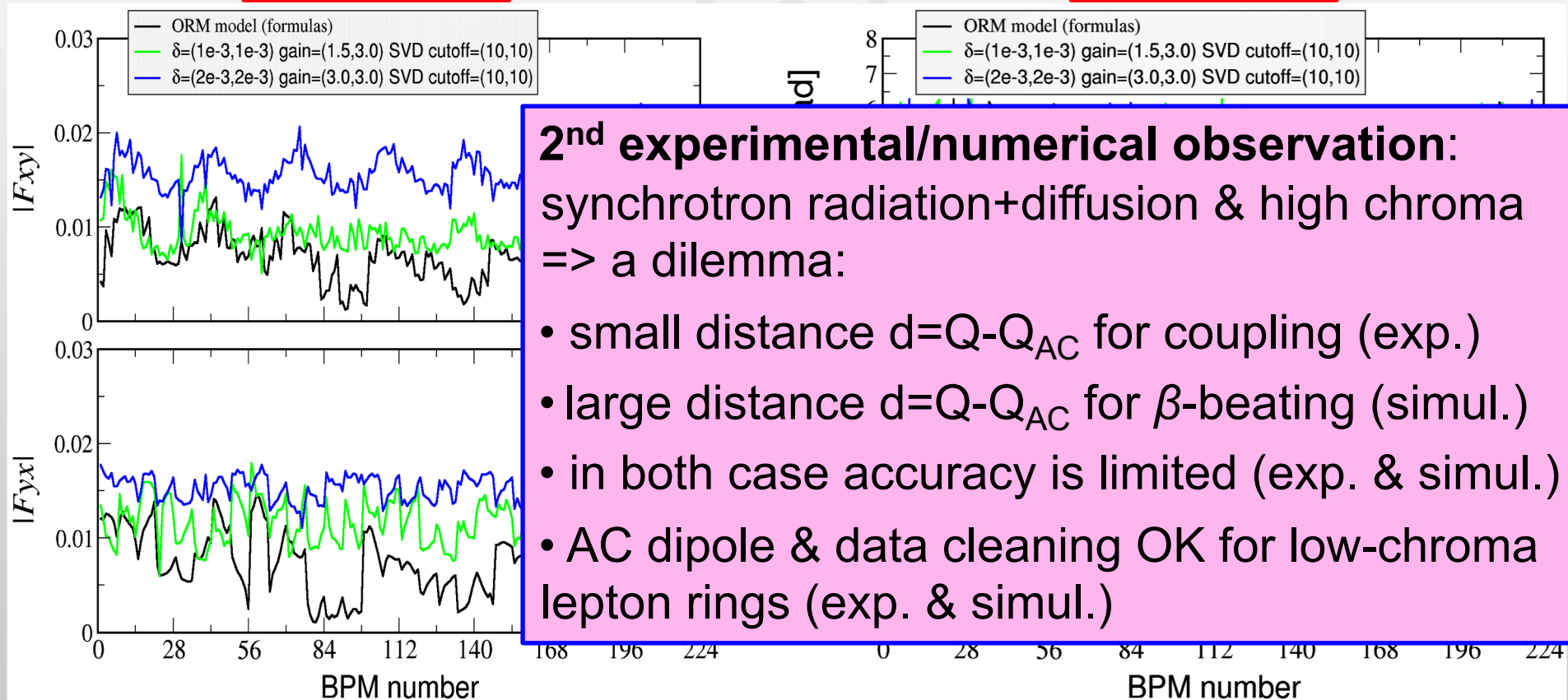
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compare ($\epsilon_y/\epsilon_x \sim 1\text{‰}$) ORM model with TbT harmonic analysis

AMPLITUDE

PHASE



2nd experimental/numerical observation:
 synchrotron radiation+diffusion & high chroma
 => a dilemma:

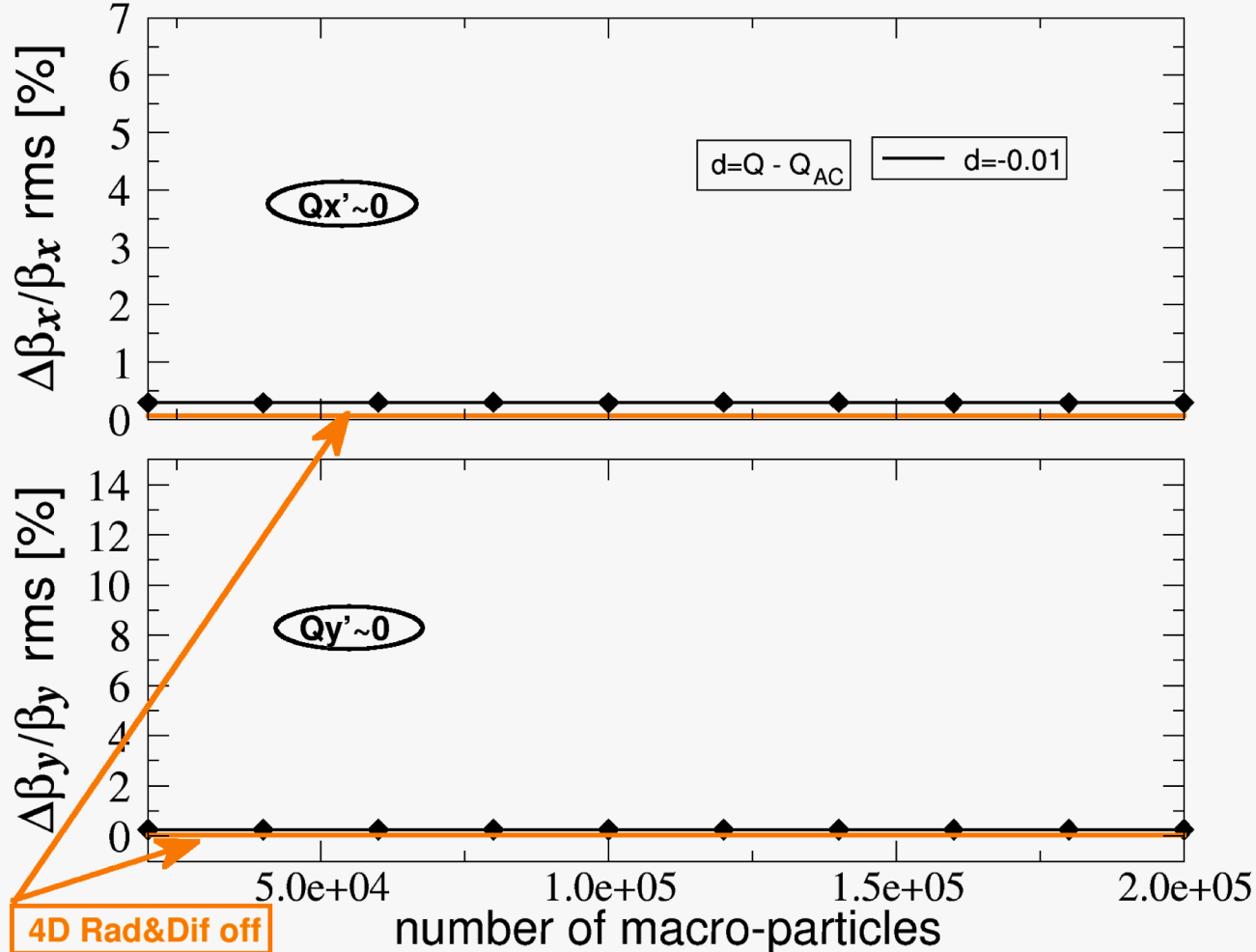
- small distance $d=Q-Q_{AC}$ for coupling (exp.)
- large distance $d=Q-Q_{AC}$ for β -beating (simul.)
- in both case accuracy is limited (exp. & simul.)
- AC dipole & data cleaning OK for low-chroma lepton rings (exp. & simul.)

- Measuring ultra-low coupling via AC dipole and turn-by-turn (TbT) BPM data
- **Simulation of beta-beating measurement via AC dipole and turn-by-turn (TbT) BPM data**
- AC dipole and BPM TbT spectrum
- regarding $(1-\lambda^2)$

low (0,0) Vs high (8,13) chroma sextupole optics

Artificial β -beating from multiparticle & leptonic nature of the beam

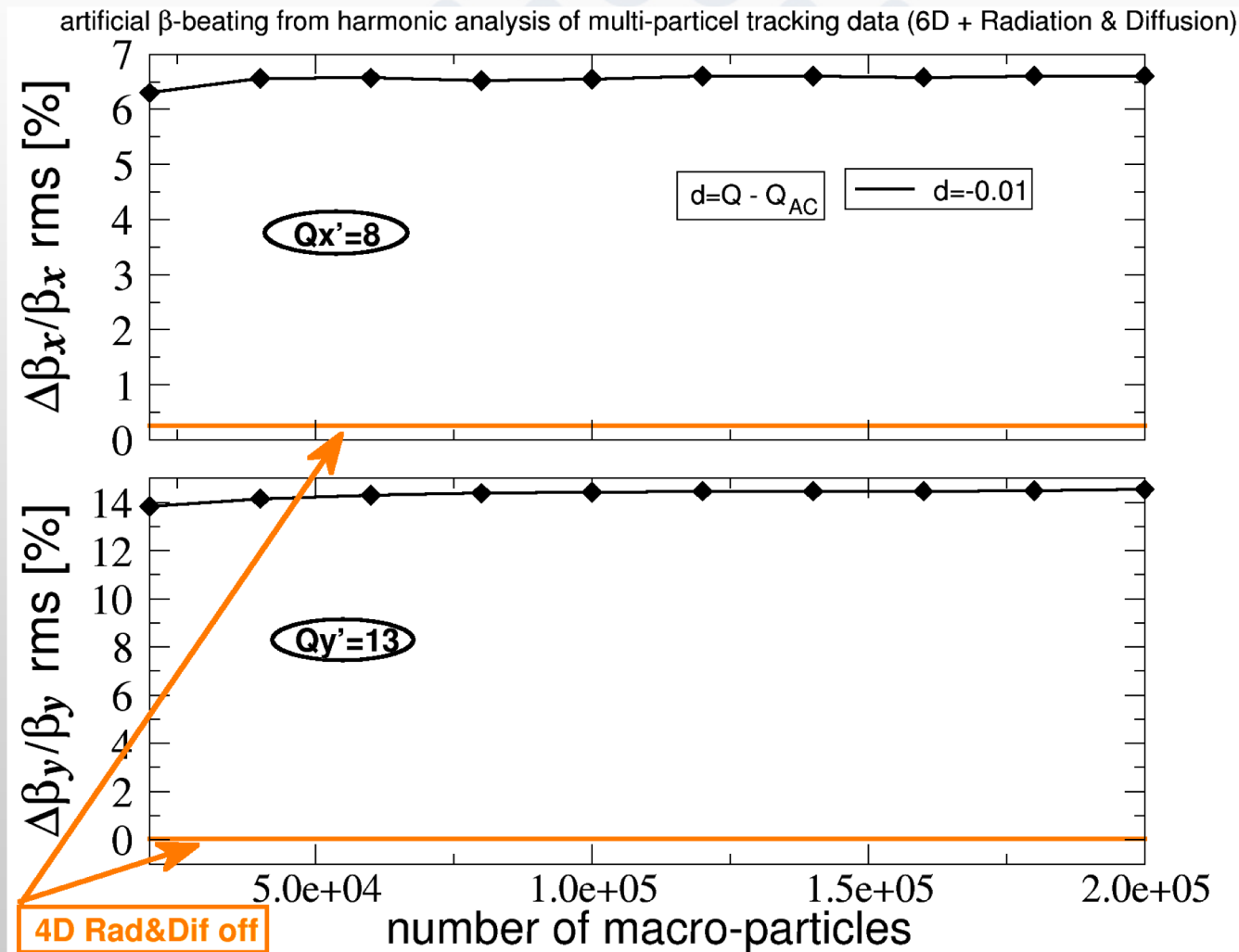
artificial β -beating from harmonic analysis of multi-particle tracking data (6D + Radiation & Diffusion)



Low chroma & detuning

low (0,0) Vs high (8,13) chroma sextupole optics

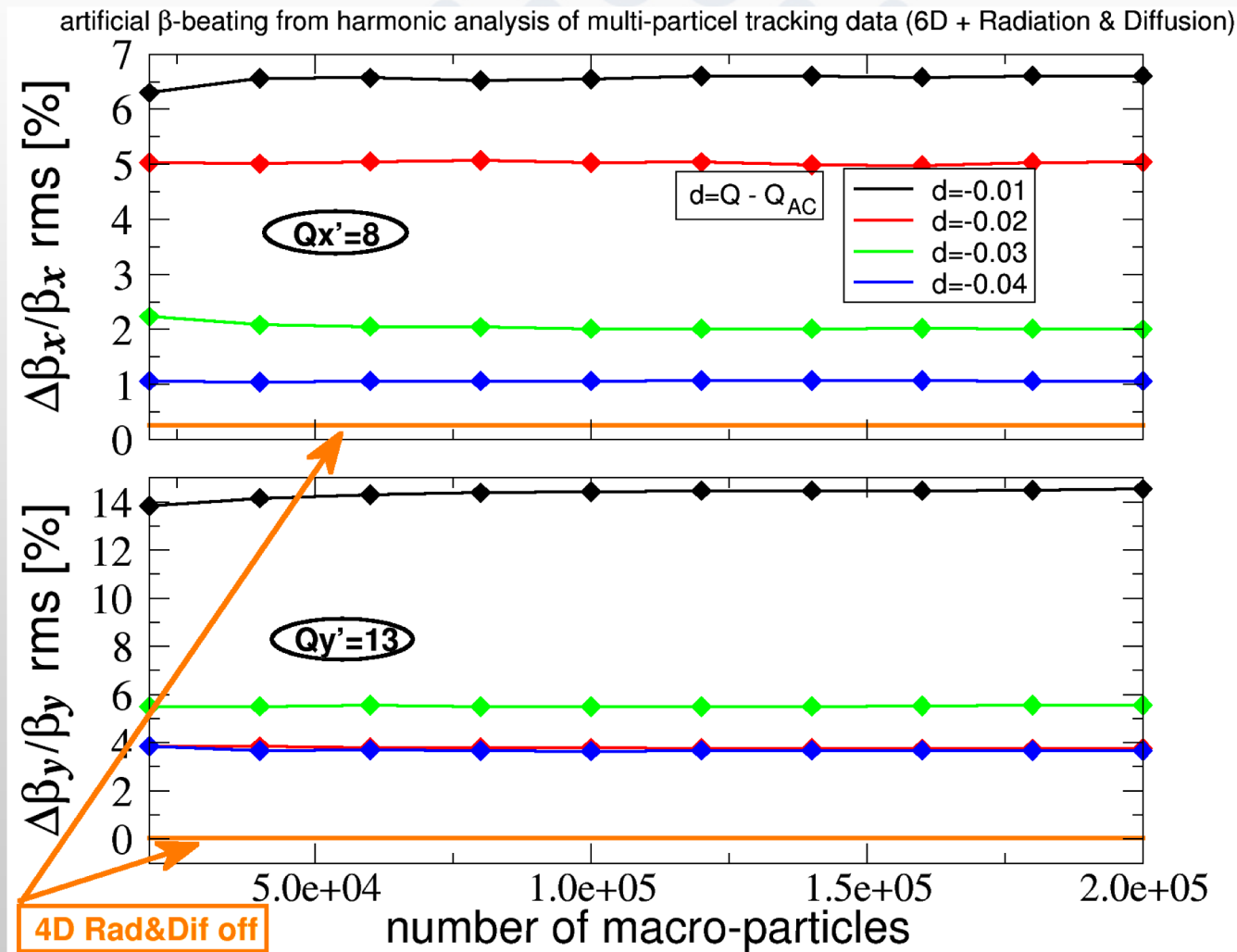
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High chroma & detuning

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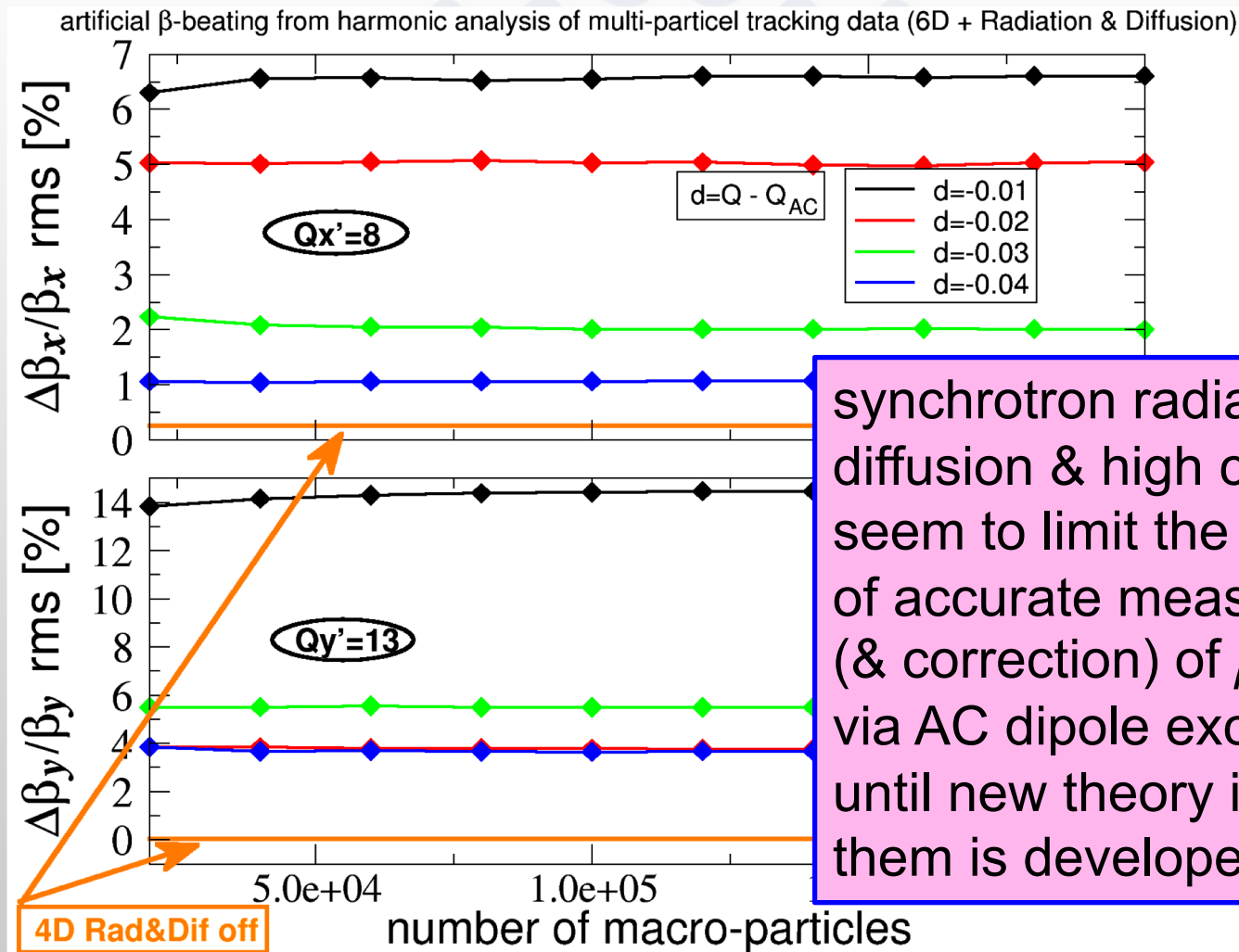
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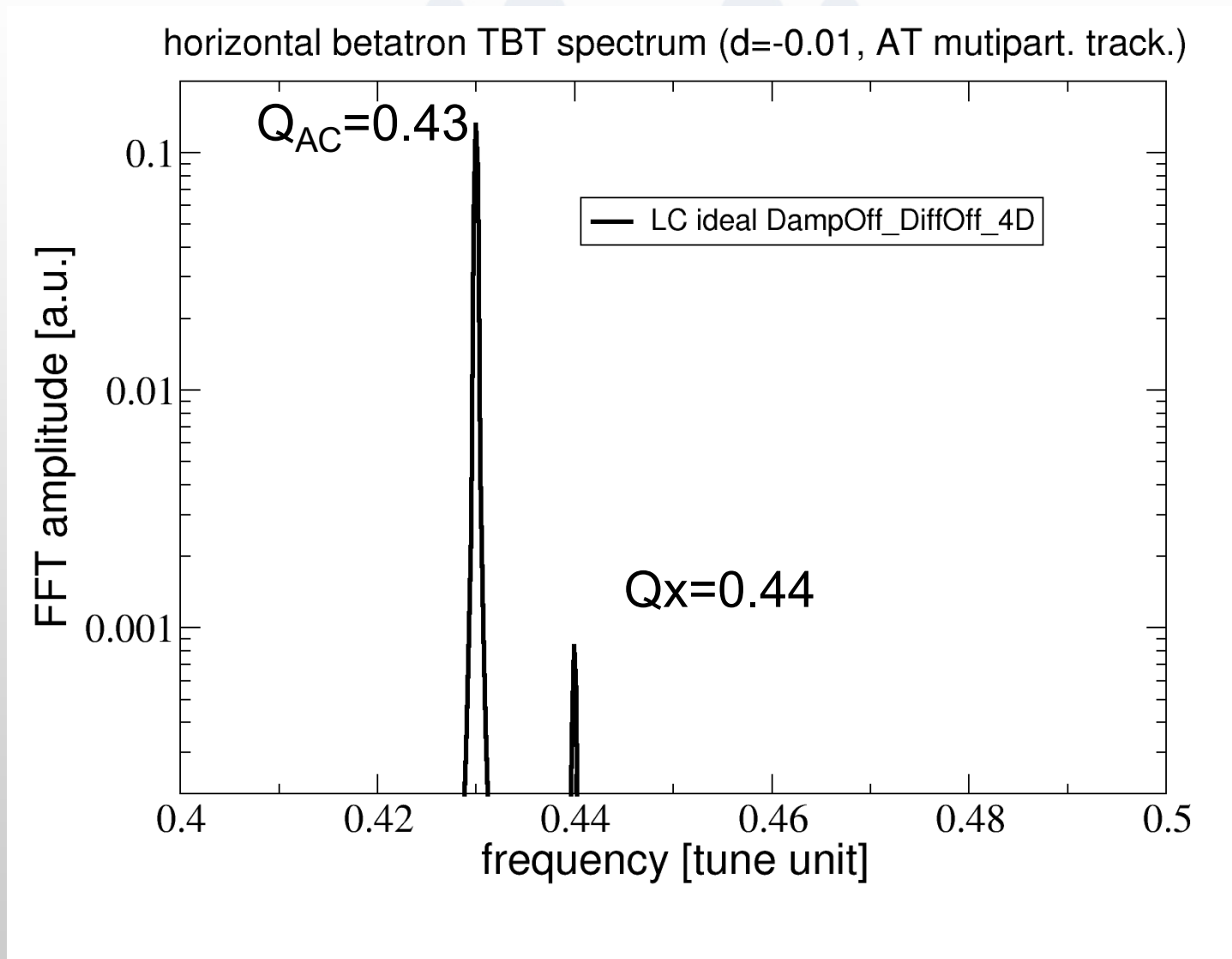
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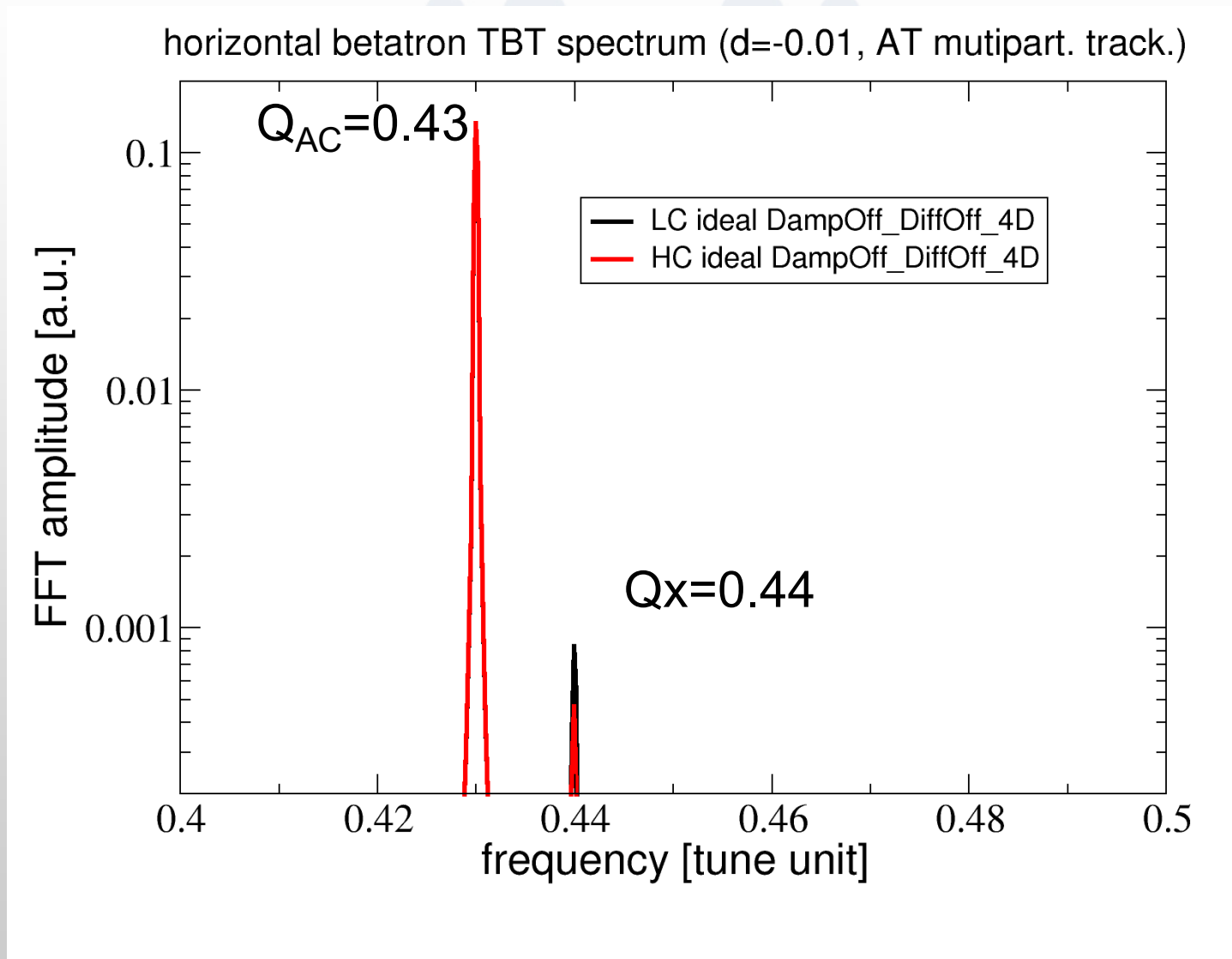
synchrotron radiation and diffusion & high chroma seem to limit the possibility of accurate measurement (& correction) of β -beating via AC dipole excitation ... until new theory including them is developed

- Measuring ultra-low coupling via AC dipole and turn-by-turn (TbT) BPM data
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- **AC dipole and BPM TbT spectrum**
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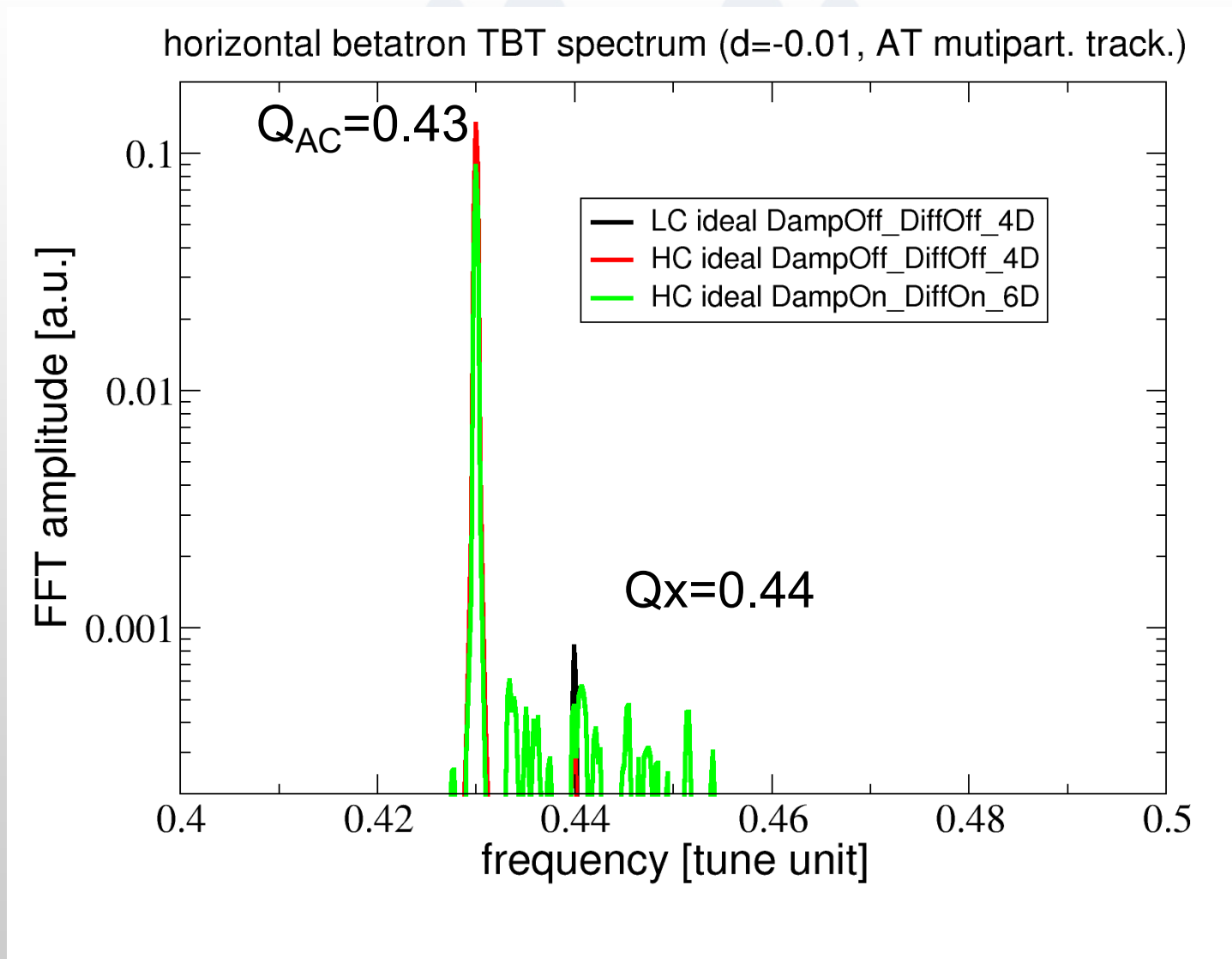
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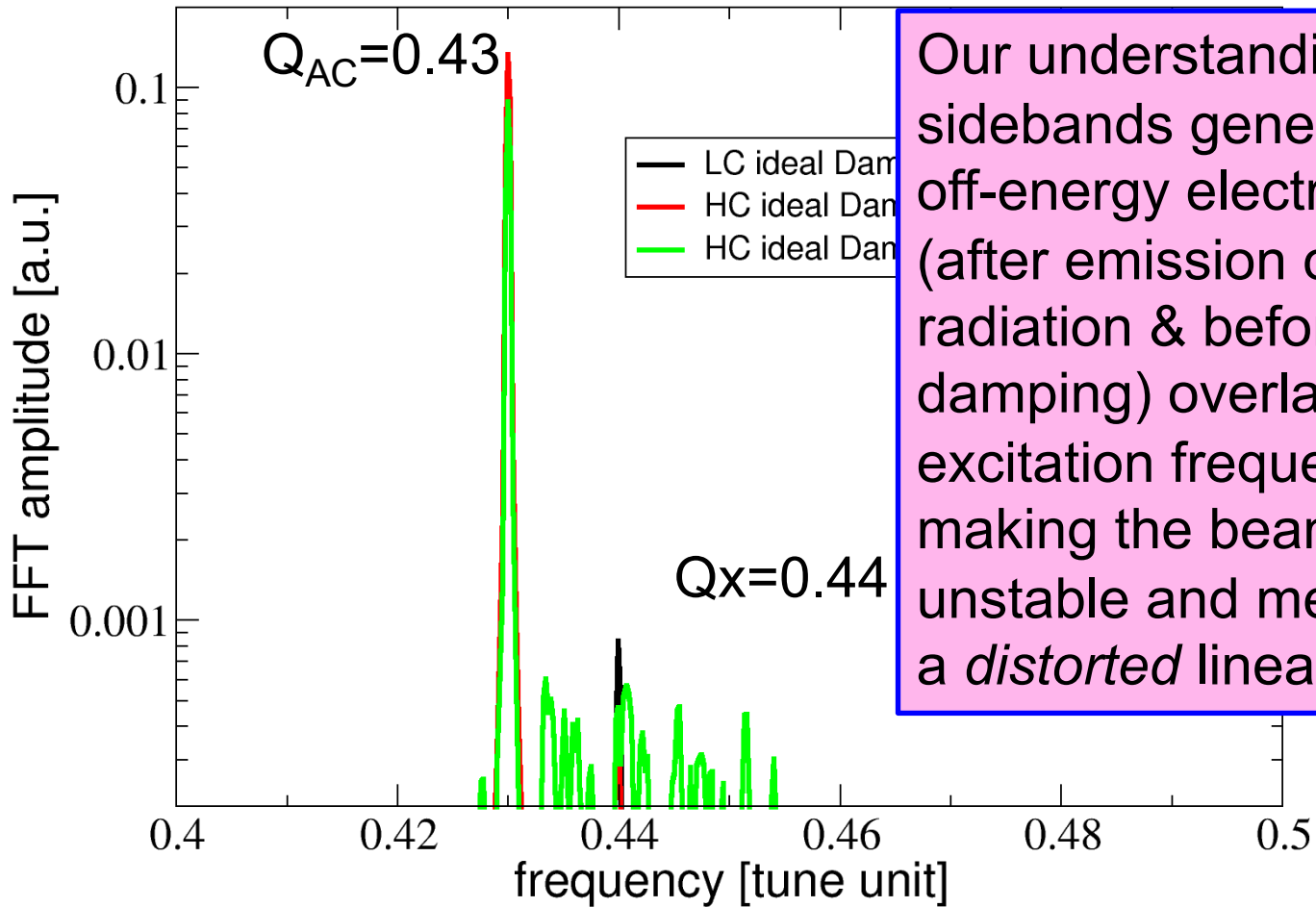


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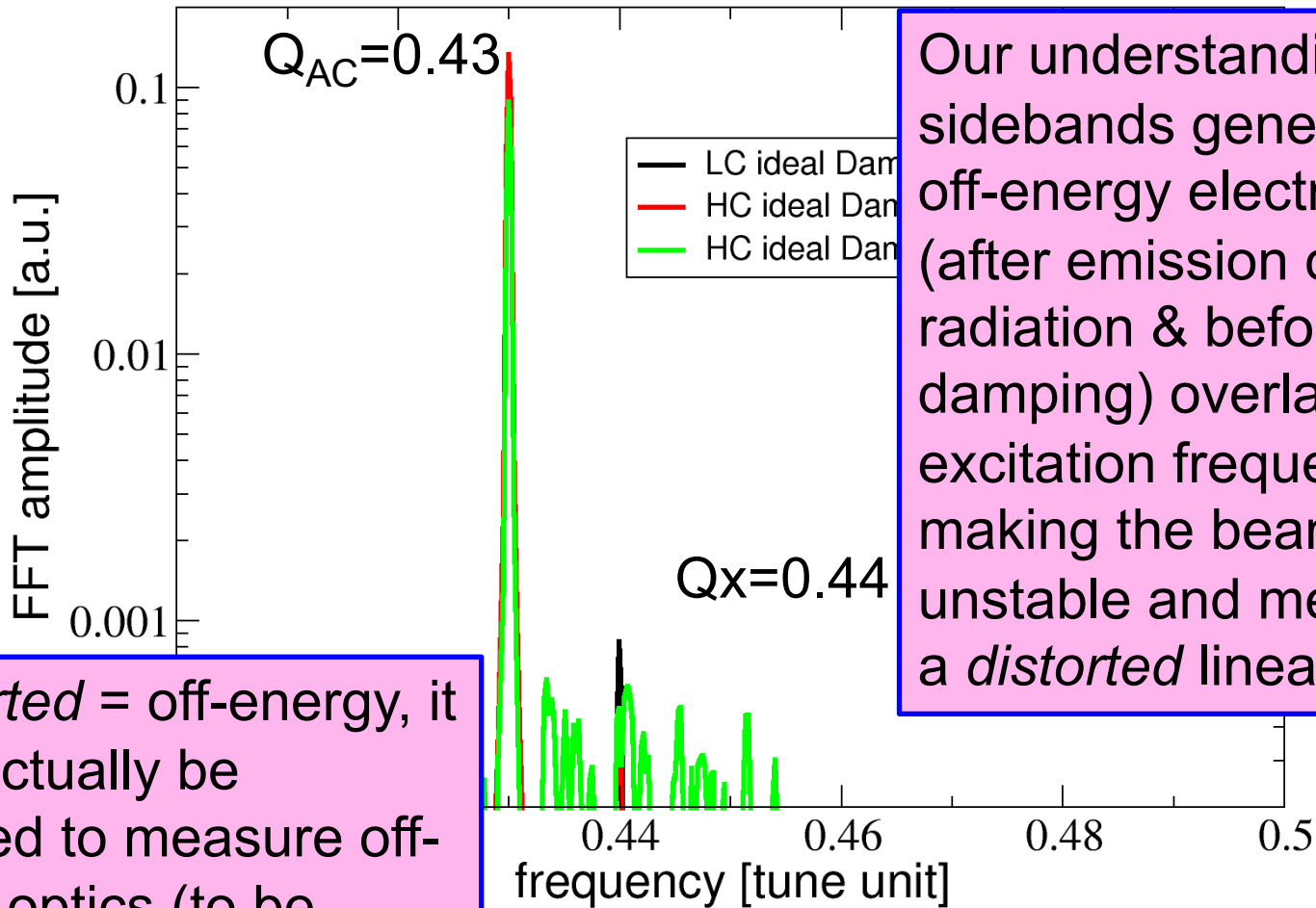
horizontal betatron TBT spectrum (d=-0.01, AT mutipart. track.)



Our understanding:
sidebands generated by
off-energy electrons
(after emission of synchr.
radiation & before long.
damping) overlap the AC
excitation frequency, thus
making the beam
unstable and measuring
a *distorted* linear optics

low (0,0) Vs high (8,13) chroma sextupole optics

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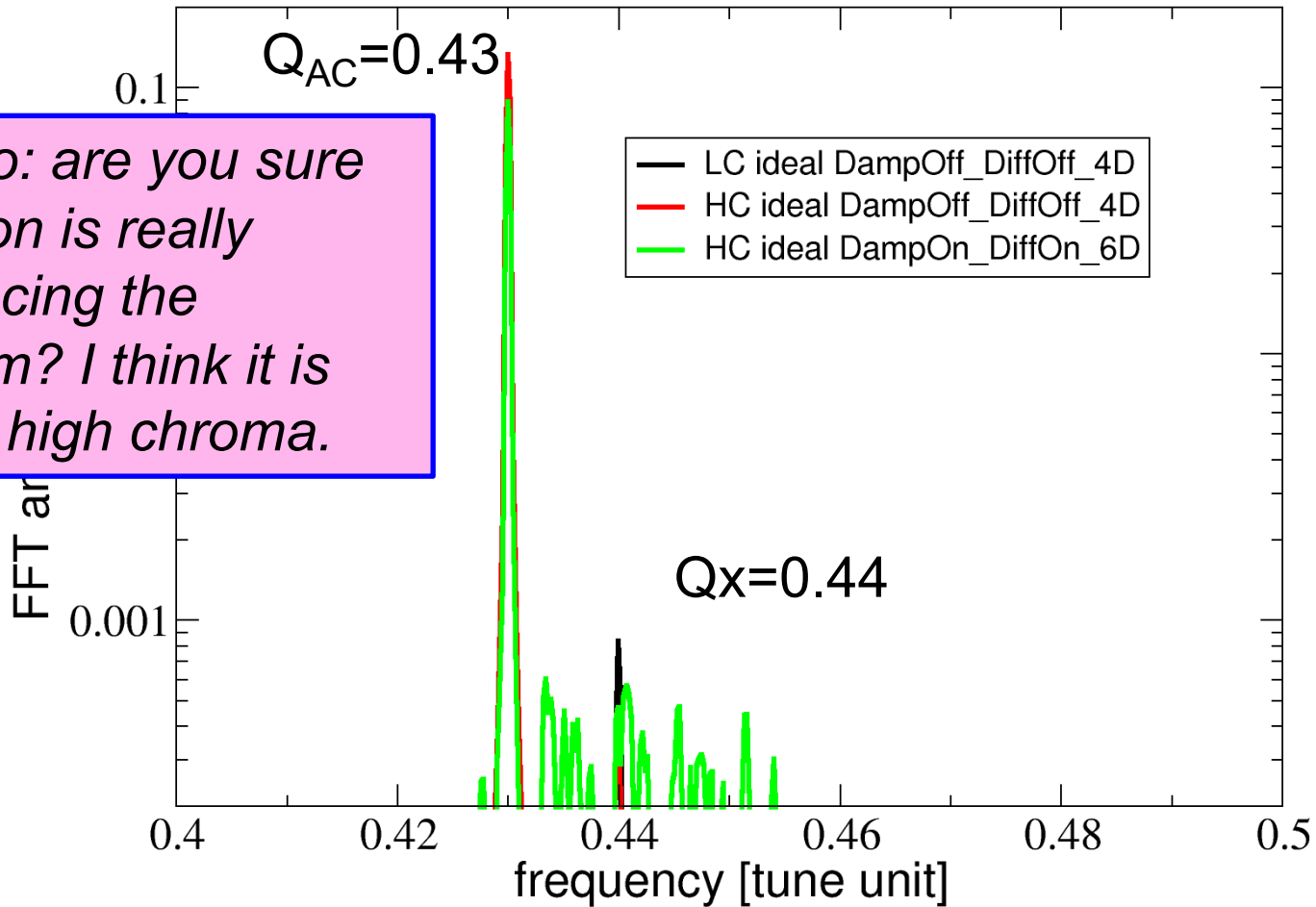


Our understanding:
sidebands generated by off-energy electrons (after emission of synchr. radiation & before long. damping) overlap the AC excitation frequency, thus making the beam unstable and measuring a *distorted* linear optics

If *distorted* = off-energy, it could actually be exploited to measure off-energy optics (to be simulated yet)

low (0,0) Vs high (8,13) chroma sextupole optics

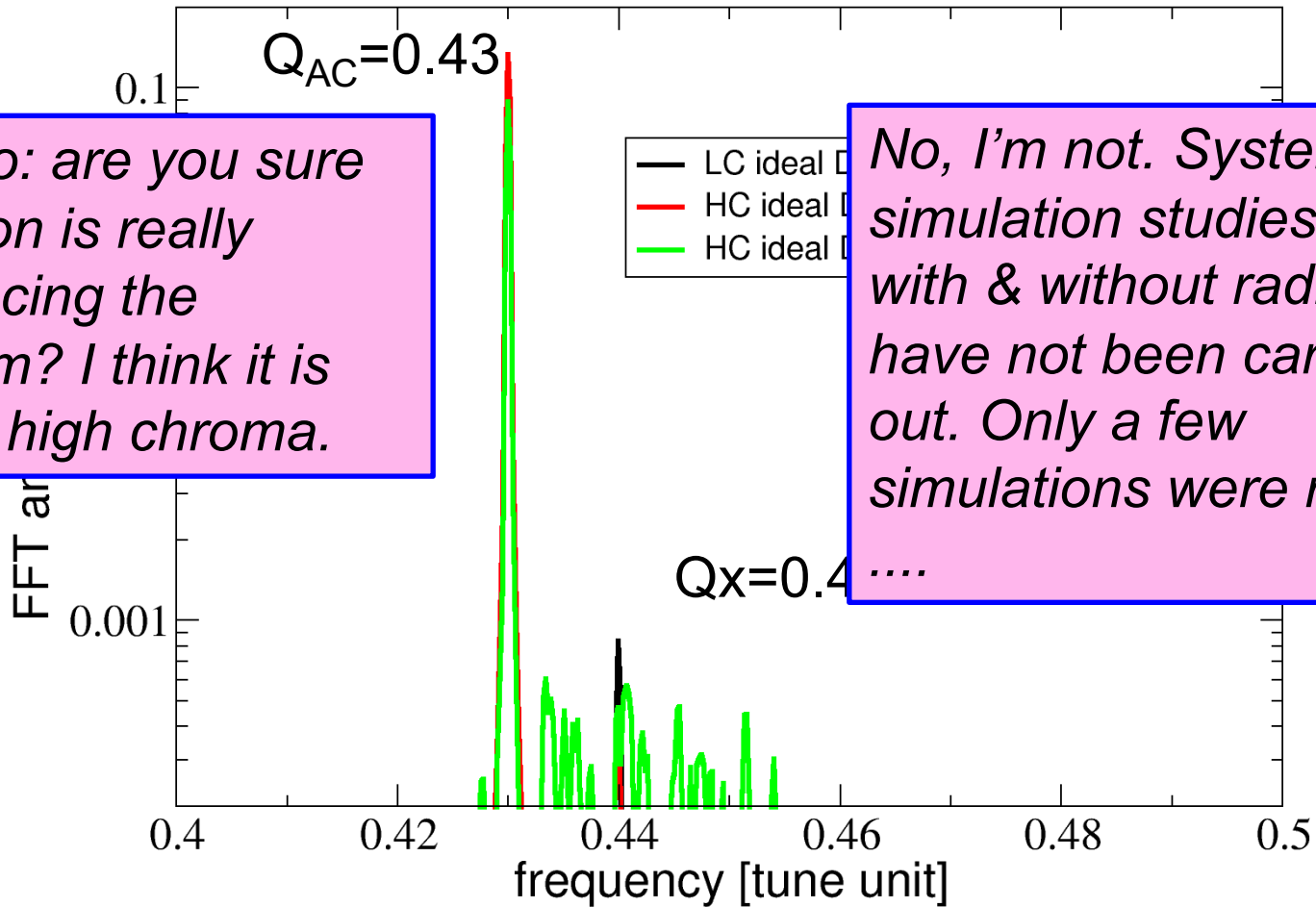
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Rogelio: are you sure radiation is really introducing the problem? I think it is mostly high chroma.

low (0,0) Vs high (8,13) chroma sextupole optics

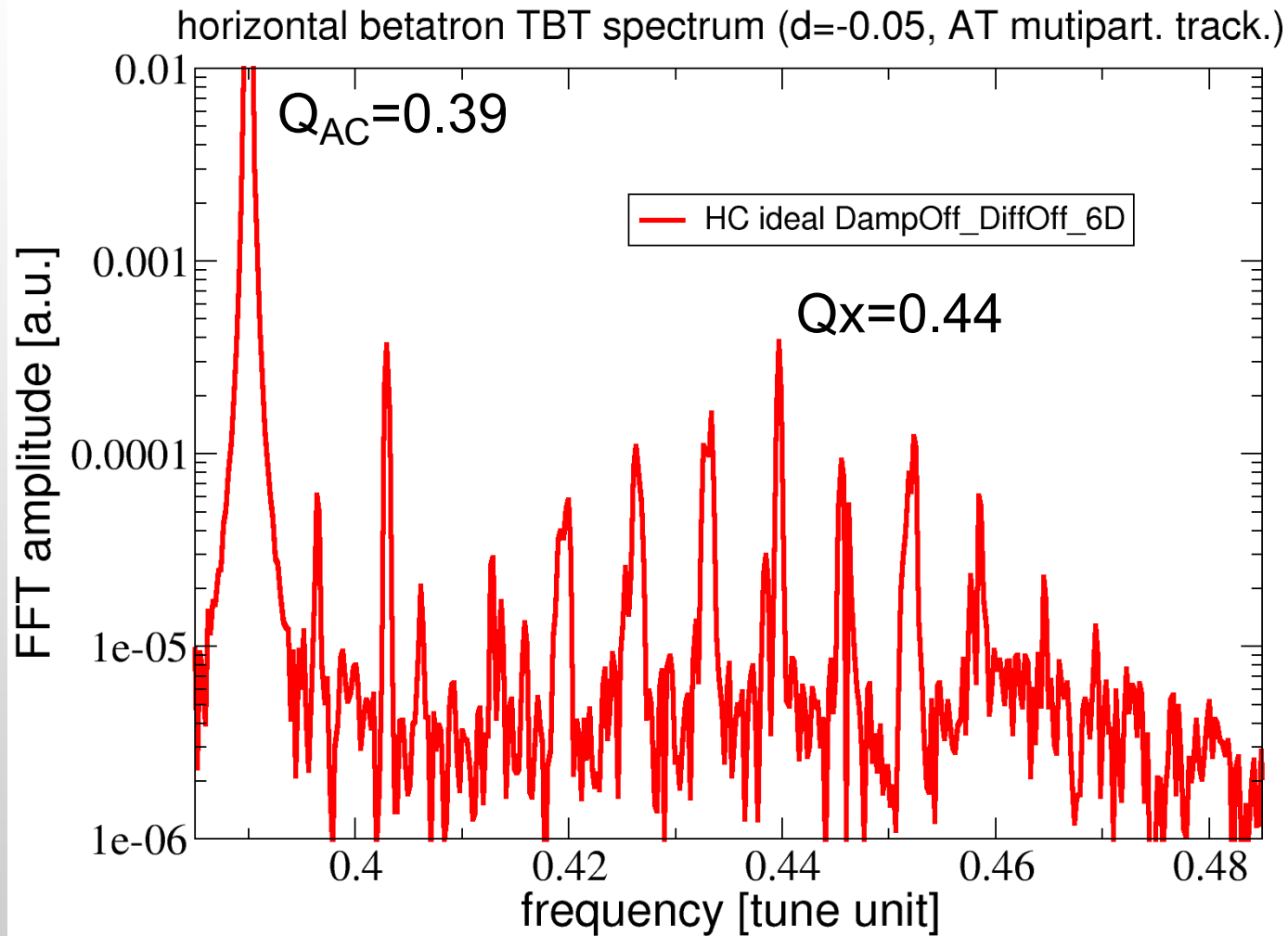
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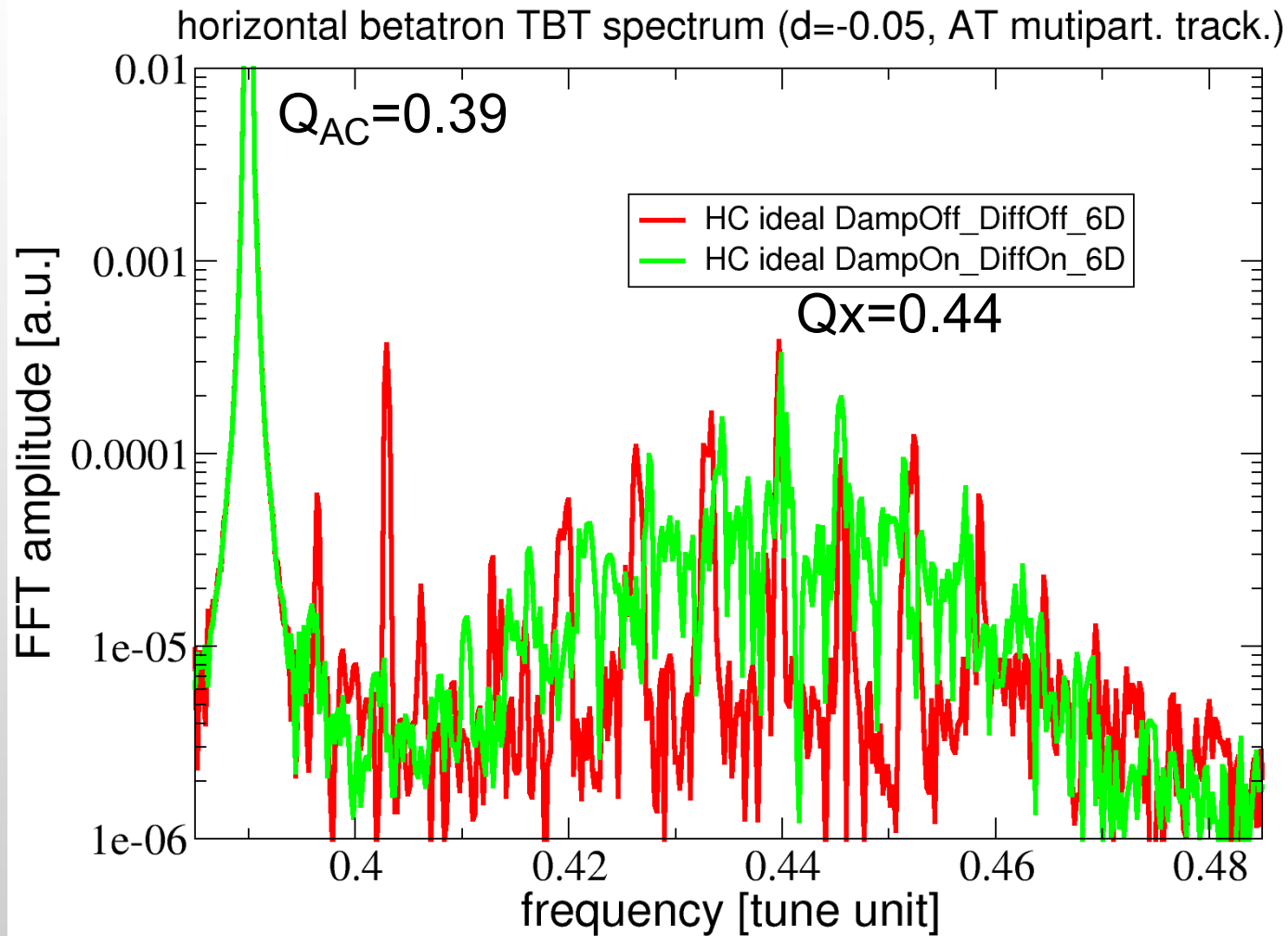
Rogelio: are you sure radiation is really introducing the problem? I think it is mostly high chroma.

No, I'm not. Systematic simulation studies 6D with & without radiation have not been carried out. Only a few simulations were run

high (8,13) chroma sextupole optics: RAD OFF & ON



high (8,13) chroma sextupole optics: RAD OFF & ON



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- **regarding $(1-\lambda^2)$**

The measurable *driven* optical parameters are computed from the measured phase advance & model functions via the λ parameter

$$\lambda_h = \frac{\sin[\pi(\nu_{x,h} - \nu_x)]}{\sin[\pi(\nu_{x,h} + \nu_x)]}$$

$$\Psi_x(\bar{s}_2, \bar{s}_1) = \psi_x(\bar{s}_2, \bar{s}_1) - \pi\nu_x \text{sgn}(\bar{s}_2 - \bar{s}_1)$$

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$$\tan[\Psi_{x,h}(\bar{s}, \bar{s}_h)] = \frac{1 + \lambda_h}{1 - \lambda_h} \tan[\Psi_x(\bar{s}, \bar{s}_h)]$$

$$\beta_{x,h}(\bar{s}) = \frac{1 + \lambda_h^2 - 2\lambda_h \cos[2\Psi_x(\bar{s}, \bar{s}_h)]}{1 - \lambda_h^2} \beta_x(\bar{s}) \quad A_{x,h} = \frac{\theta_h}{4 \sin(\pi\delta_h)} \sqrt{\beta_x(\bar{s}_h)(1 - \lambda_h^2)}$$

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see Ryoichi Miyamoto's PhD thesis, notes and papers

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hypothesis: $\lambda \ll 1$

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hypothesis: $\lambda \ll 1$

hypothesis not really met @ESRF:

$$v=(36.44, 13.39)$$

$$d=v_{x,h}-v_x=0.01 \Rightarrow \lambda_x=0.09$$

$$d=v_{x,h}-v_x=0.03 \Rightarrow \lambda_x=0.34$$

$$\Psi_x(\bar{s}_2, \bar{s}_1) = \psi_x(\bar{s}_2, \bar{s}_1) - \pi\nu_x s$$

$$\tan[\Psi_{x,h}(\bar{s}, \bar{s}_h)] = \frac{1 + \lambda_h}{1 - \lambda_h} \tan[\Psi_x(\bar{s}, \bar{s}_h)]$$

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$$\lambda_h = \frac{\sin[\pi(\nu_{x,h} - \nu_x)]}{\sin[\pi(\nu_{x,h} + \nu_x)]}$$

hypothesis: $\lambda \ll 1$

$(1-\lambda^2)$ artificially introduced to retrieve the same C-S relations between β, α & γ , though it is not needed.

$$\Psi_x(\bar{s}_2, \bar{s}_1) = \psi_x(\bar{s}_2, \bar{s}_1) - \pi\nu_x s$$

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see Ryoichi Miyamoto's PhD thesis, notes and papers

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$$\lambda_h = \frac{\sin[\pi(\nu_{x,h} - \nu_x)]}{\sin[\pi(\nu_{x,h} + \nu_x)]}$$

hypothesis: $\lambda \ll 1$

$(1-\lambda^2)$ removed for all analysis @ ESRF, both in simulations & measurement to retrieve good matching with model and measured linear optics

$$\Psi_x(\bar{s}_2, \bar{s}_1) = \psi_x(\bar{s}_2, \bar{s}_1) - \pi\nu_x s$$

$$\tan[\Psi_{x,h}(\bar{s}, \bar{s}_h)] = \frac{1 + \lambda_h}{1 - \lambda_h} \tan[\Psi_x(\bar{s}, \bar{s}_h)]$$

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- Simulations and measurement @ the old ESRF storage ring revealed problems in using AC dipole TbT data along with large chromaticity & synchrotron radiation.
- Sources of pollution (large chroma Vs synch. rad.) have not yet been disentangled and quantified individually. This is feasible in simulations, though not experimentally.
- A light source with robust linear modelling via ORM and TbT BPM data (with MAF filter & AC dipole) could be used as playground for an experimental campaign. PETRA looks a good candidate!!