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# UNDERSTANDING THE PROPERTIES OF THE FIREBALL WITH THE POLARIZATION SIGNATURE OF THERMAL DILEPTONS

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(TU Darmstadt)

in collaboration with B. Friman, T. Galatyuk, H. van Hees, R. Rapp, E. Speranza & J. Wambach



Quark Matter 2023, Houston



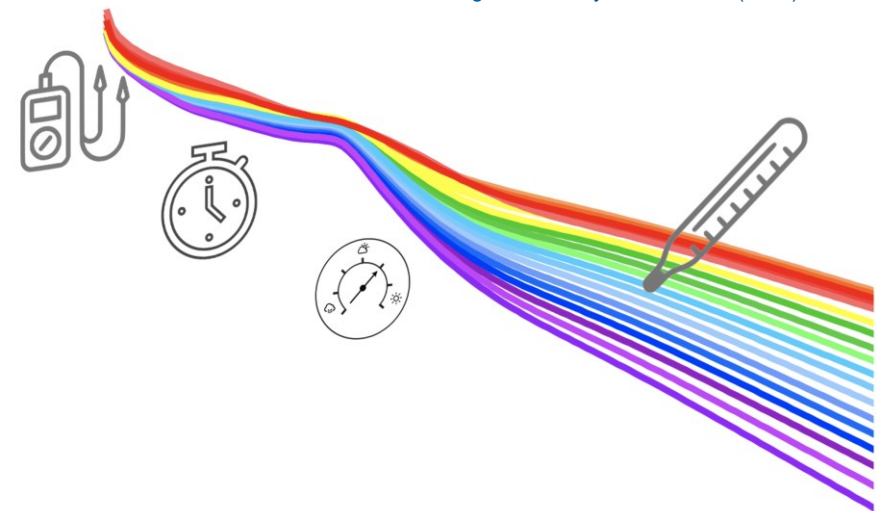
# THERMAL DILEPTON RADIATION AS MULTIMETER OF THE FIREBALL

- Lifetime via low-mass yield  
→ search for "extra radiation" due to latent heat around phase transition (& critical point?)
- Temperature via slope of invariant mass spectrum  
→ flattening of caloric curve ( $T$  vs  $\varepsilon$ ) sign for a phase transition
- Pressure anisotropies via dilepton flow  
→ access to EoS at high baryon density via multi-differential measurements
- Electric conductivity probed in the limit  $p_{ee} = 0$  MeV/c,  $M_{ee} \rightarrow 0$  MeV/c<sup>2</sup>  
→ access to transport properties of QCD matter

U. Heinz, K. Lee, Phys. Lett. B 259, 162 (1991)  
H. Barz *et al.*, Phys. Lett. B 254, 315 (1991)  
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F. Seck *et al.*, Phys. Rev. C 106 (2022), 014904  
O. Savchuk *et al.*, J. Phys G 104537 R2 (2023)

R. Chatterjee *et al.*, Phys. Rev. C 75 (2007), 054909  
T. Reichert *et al.*, Phys. Lett. B 841 (2023) 137947

G. Moore, J. Robert, arXiv:hep-ph/0607172 (2006)  
J. Atchison, R. Rapp, Nucl. Phys. A 1037 (2023) 122704  
S. Flörchinger *et al.*, Phys. Lett. B 837 (2023) 137647



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- Electric conductivity probed in the limit  $p_{ee} = 0$  MeV/c,  $M_{ee} \rightarrow 0$  MeV/c<sup>2</sup>
  - access to transport properties of QCD matter
- Spin polarization allows to distinguish different sources of thermal dileptons
  - access information on production mechanism

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E. Bratkovskaya *et al.*, Phys. Lett. B 376, 12 (1996)  
E. Speranza *et al.*, Phys. Lett. B 782, 395 (2018)  
G. Baym *et al.*, Phys. Rev. C 95, 044907 (2017)  
S. Hauksson, C. Gale, arXiv:2306.10307 [nucl-th] (2023)

## KEY QUANTITY: EM EMISSIVITY



- EM emissivity of thermal QCD matter determined by the correlator of the EM current  $\Pi_{EM}^{\mu\nu} = \langle j_{EM}^\mu j_{EM}^\nu \rangle_T$

- Dilepton emission rate given by

$$\frac{dN_{ll}}{d^4x d^4q} = \frac{\alpha^2 L(M)}{6 \pi^3 M^2} f^B(q_0; T) g_{\mu\nu} \rho_{EM}^{\mu\nu}(M, |\vec{q}|; T, \mu_B) \quad \text{with} \quad \rho_{EM}^{\mu\nu} = -2 \text{Im} \Pi_{EM}^{\mu\nu}$$

- Decomposition using standard 4D projectors for a spin-1 particle  $P_{L,T}^{\mu\nu}$

$$\rho_{EM}^{\mu\nu} = \rho_L P_L^{\mu\nu} + \rho_T P_T^{\mu\nu} \quad \text{with} \quad g_{\mu\nu} \rho_{EM}^{\mu\nu} = \rho_L + 2\rho_T$$

- Rotational symmetry of the medium broken by finite  $|\vec{q}|$

- Angular distribution of single lepton in  $\gamma^*$  rest frame depends on polarization of  $\gamma^*$ :

$$\frac{dN}{d^4x d^4q d\Omega} = \mathcal{N} (1 + \lambda_\theta \cos^2 \theta + \lambda_\varphi \sin^2 \theta \cos 2\varphi + \lambda_{\theta\varphi} \sin 2\theta \cos \varphi + \lambda_\varphi^\perp \sin^2 \theta \sin 2\varphi + \lambda_{\theta\varphi}^\perp \sin 2\theta \sin \varphi)$$

- $\lambda$  coefficients related to **difference** between longitudinal and transverse spectral function components

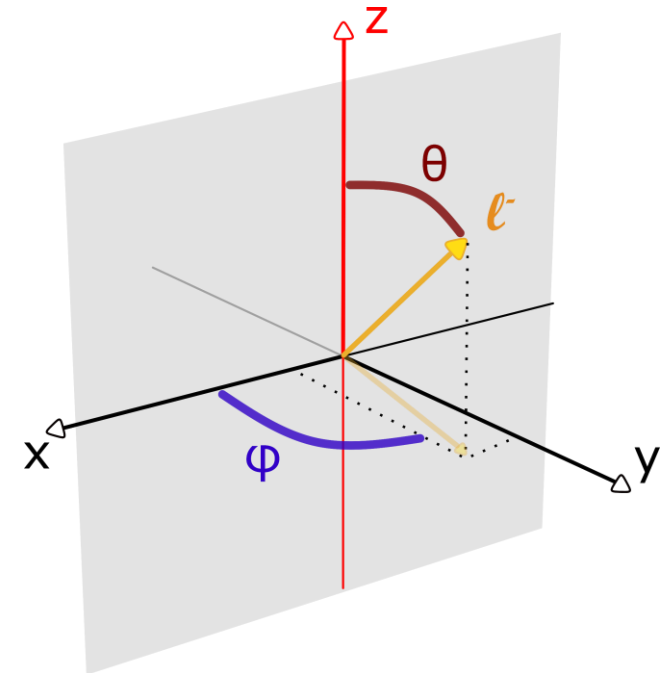
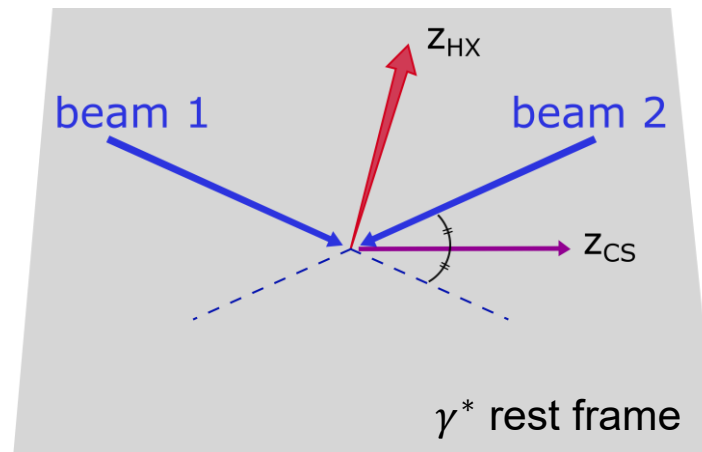
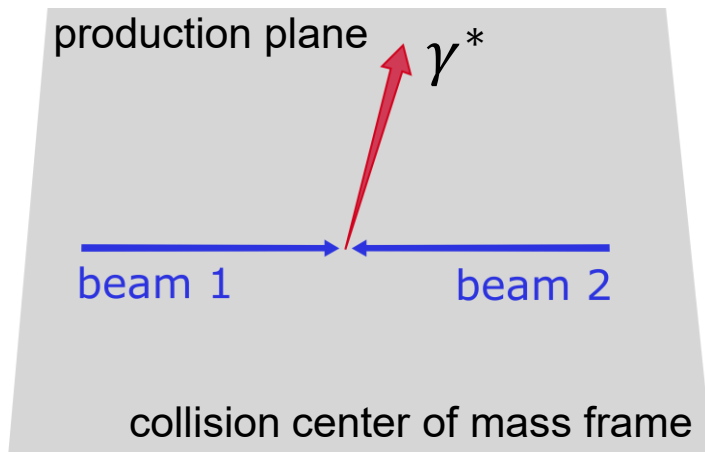
$$\rightarrow \text{for a static thermal medium in the helicity frame: } \lambda_\theta = \frac{\rho_T - \rho_L}{\rho_T + \rho_L}$$

## POLARIZATION FRAME

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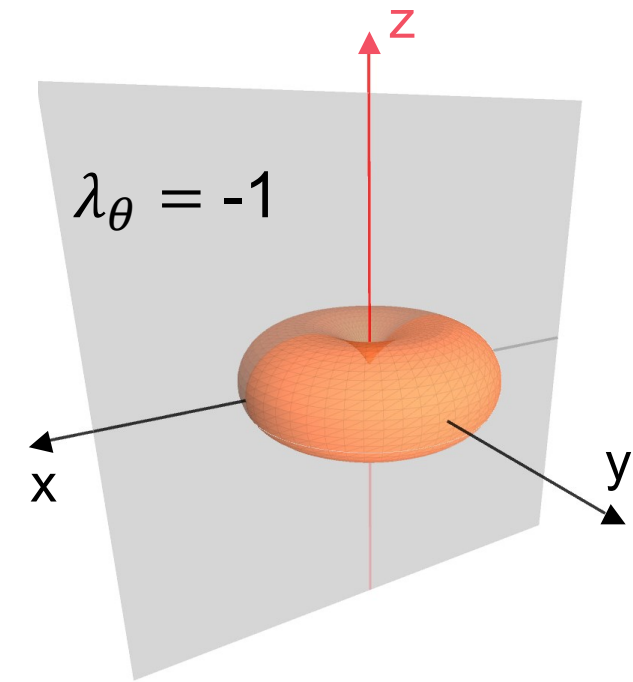
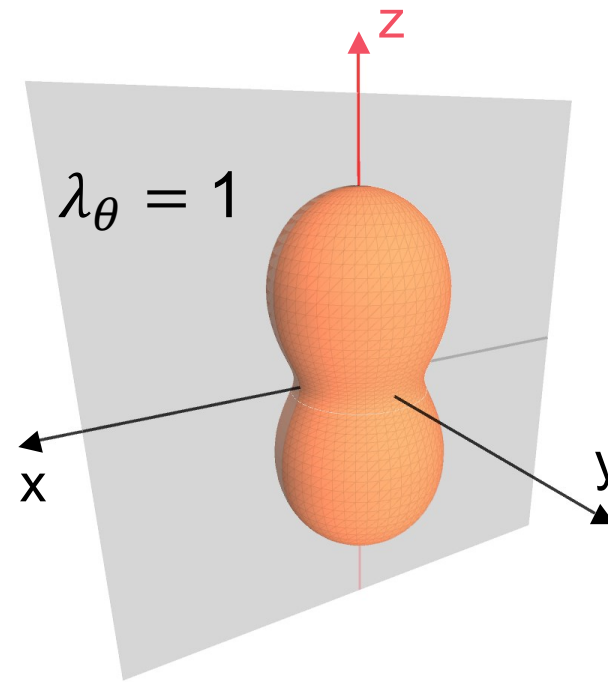
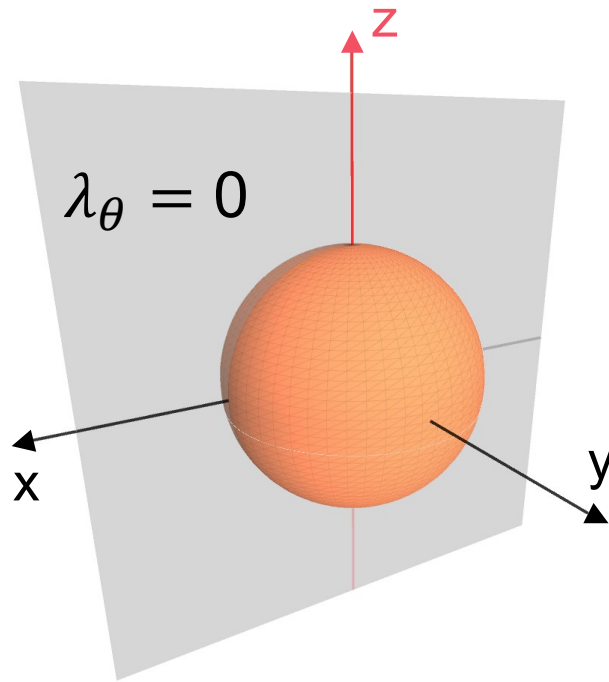
- Experiments have chosen different polarization axes for their measurements, e. g. Helicity frame (HX), Collins-Soper frame (CS) or Gottfried-Jackson frame (GJ)
- Anisotropy coefficients in different frames related via rotations



## STATIC THERMAL MEDIUM

- Rotational symmetry only broken by virtual photon's momentum direction
- In the helicity frame HX the only non-zero coefficient is  $\lambda_\theta = \frac{\rho_T - \rho_L}{\rho_T + \rho_L}$

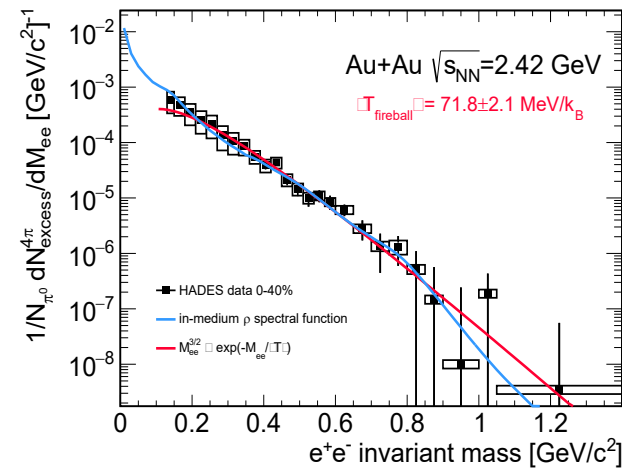
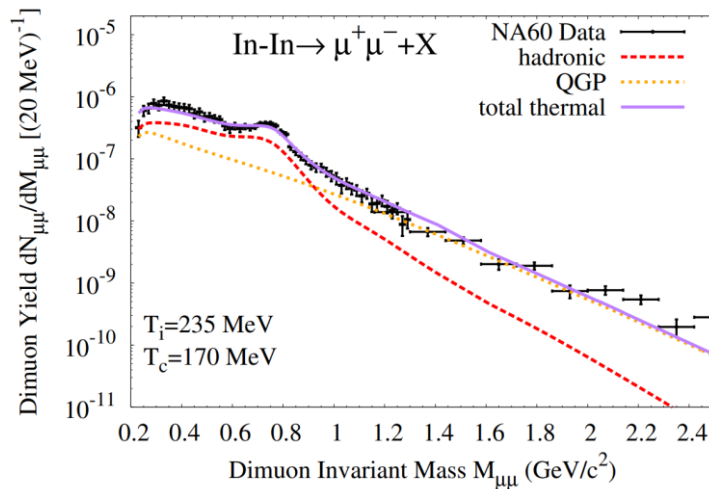
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- Employ in-medium spectral functions that give fair description of available dilepton data

E. Speranza *et al.*, Phys. Lett. B 782, 395 (2018)  
G. Baym *et al.*, Phys. Rev. C 95, 044907 (2017)



NA60 coll., Phys. Rev. Lett. 96, 162302 (2006)  
R. Rapp, H. van Hees, Phys. Lett. B 753, 586 (2016)

HADES coll., Nature Phys. 15(2019) 1040  
T. Galatyuk *et al.*, Eur. Phys. J. A 52, 131 (2016)

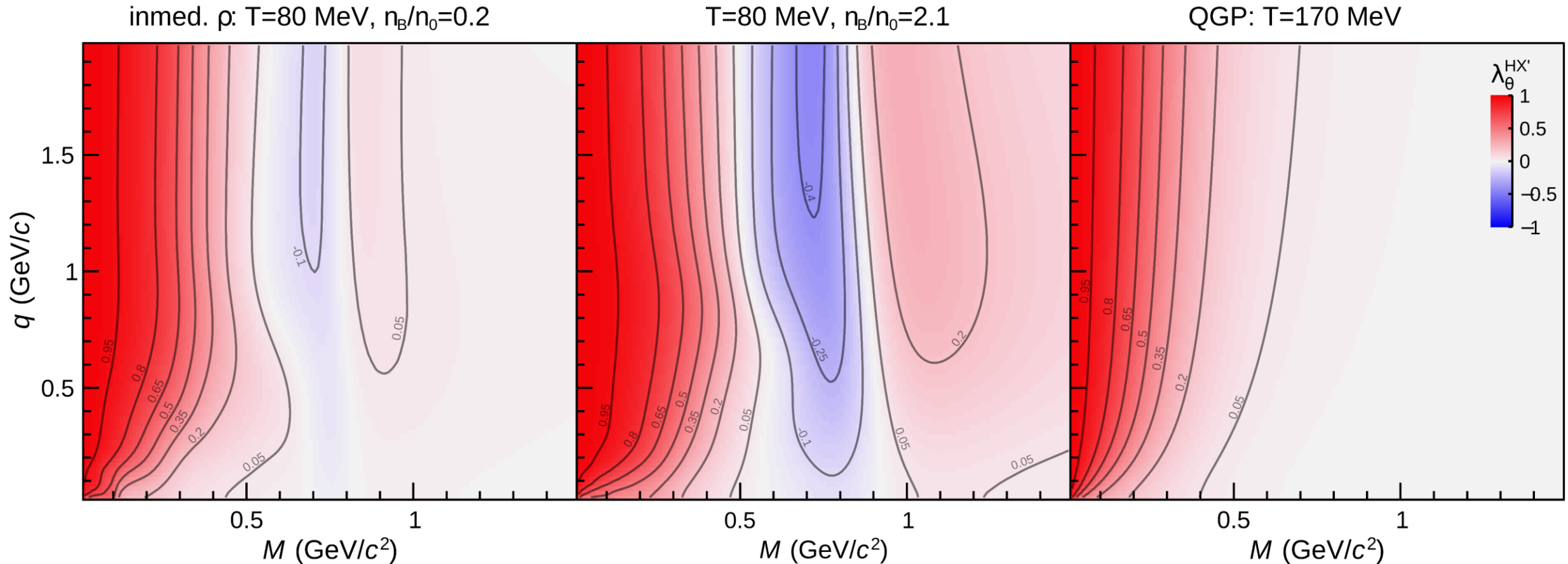
- Hadronic emission with in-medium  $\rho$ -meson spectral function calculated from hadronic many-body theory based on effective Lagrangians
- QGP emission based on perturbative  $q\bar{q}$  annihilation with a low-energy transport peak constrained by IQCD data

R. Rapp, J. Wambach, Eur. Phys. J. A 6, 415 (1999)  
R. Rapp, G. Chanfray, J. Wambach, Nucl. Phys. A 617, 472 (1997)

R. Rapp, Adv. High Energy Phys. 2013, 148253 (2013)

# POLARIZATION IN STATIC MEDIUM

- Strong dependence on mass, momentum and baryon density for hadronic medium
- Rather small polarization for QGP except for  $M_{ee} < 0.5 \text{ GeV}/c^2$  approaching the photon point



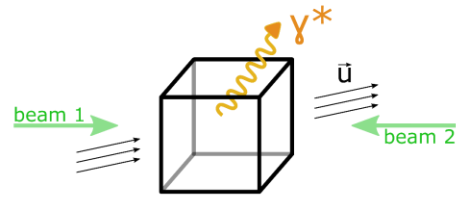
F. Seck et al., submitted



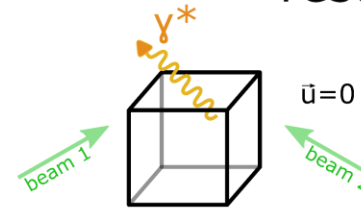
## POLARIZATION IN MOVING MEDIUM

- Helicity frames (HX') of individual local fluid cells misaligned
- Transform polarization coefficients from each cell into a global frame accessible to experiment: HX, CS, ...
- Integration over kinematic bins with yield-weighted mean

center of mass frame  
of the collision  
"lab"

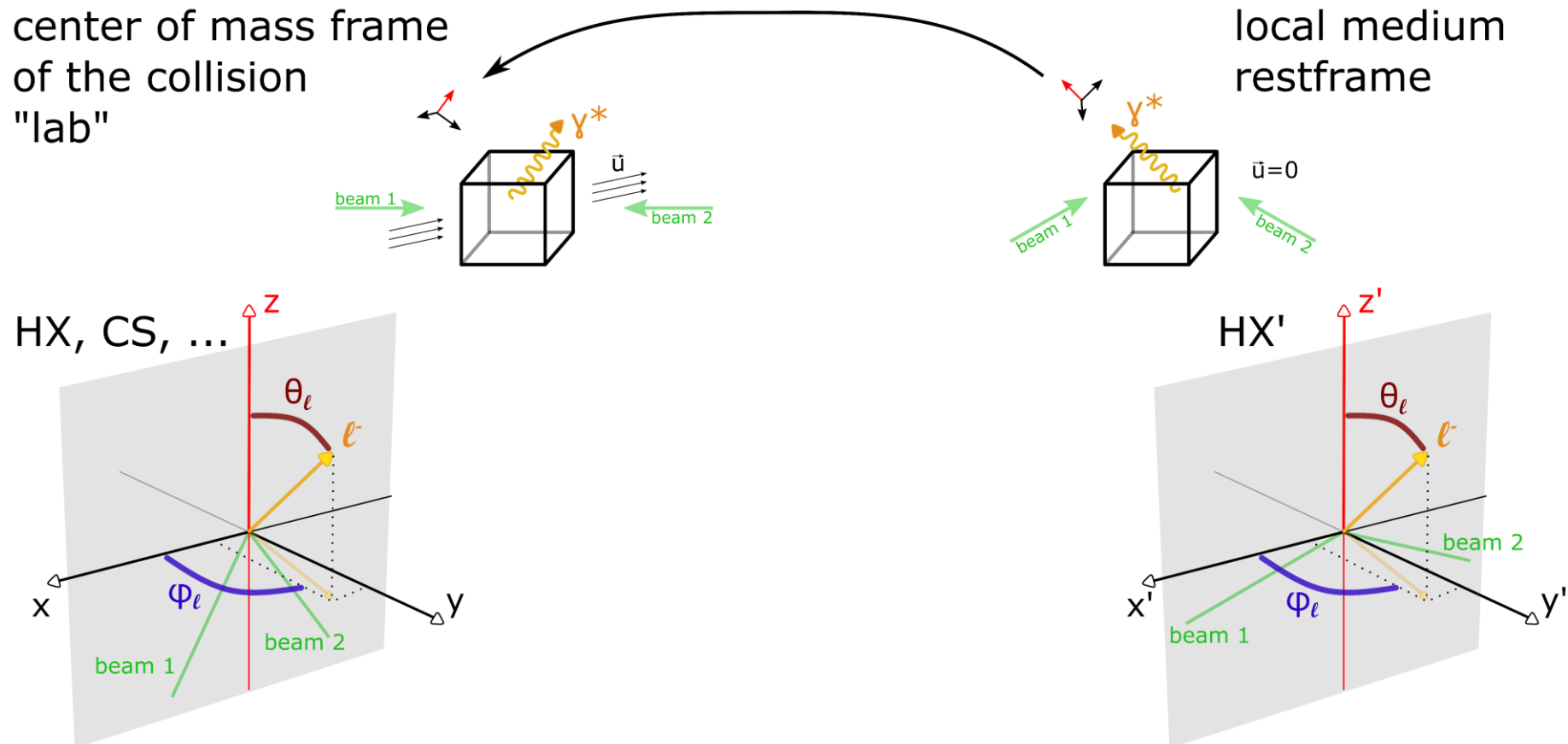


local medium  
restframe



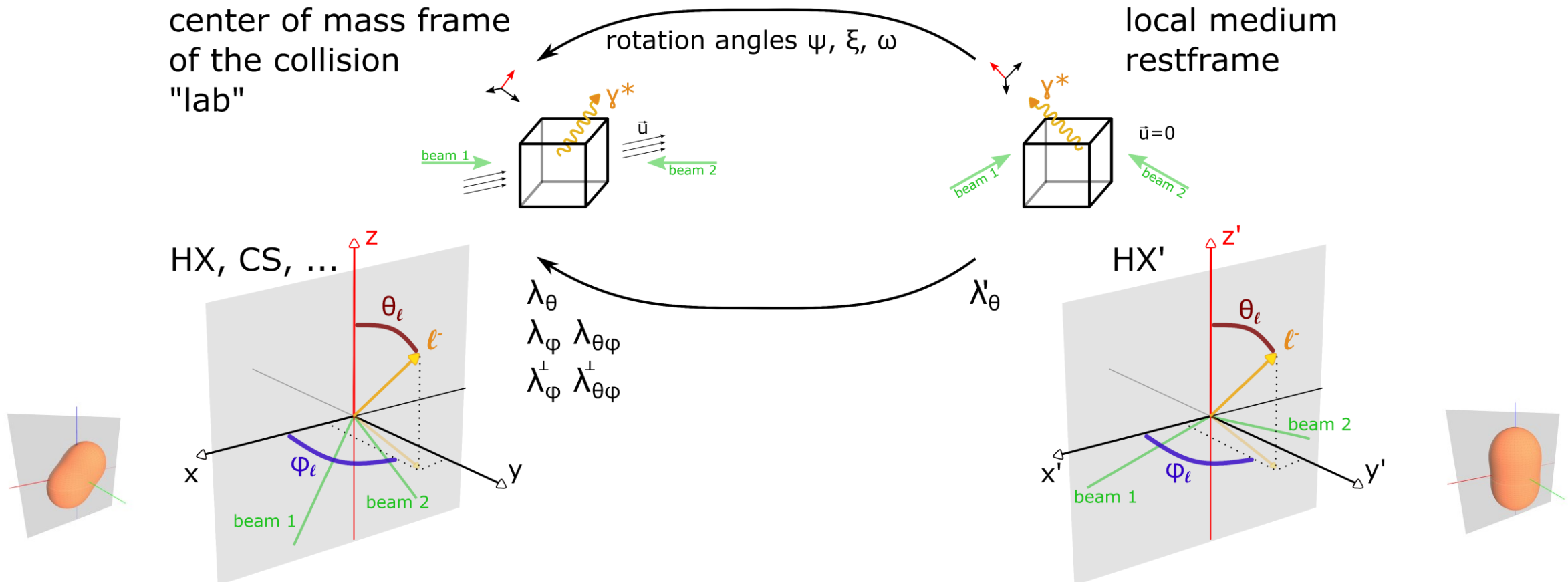
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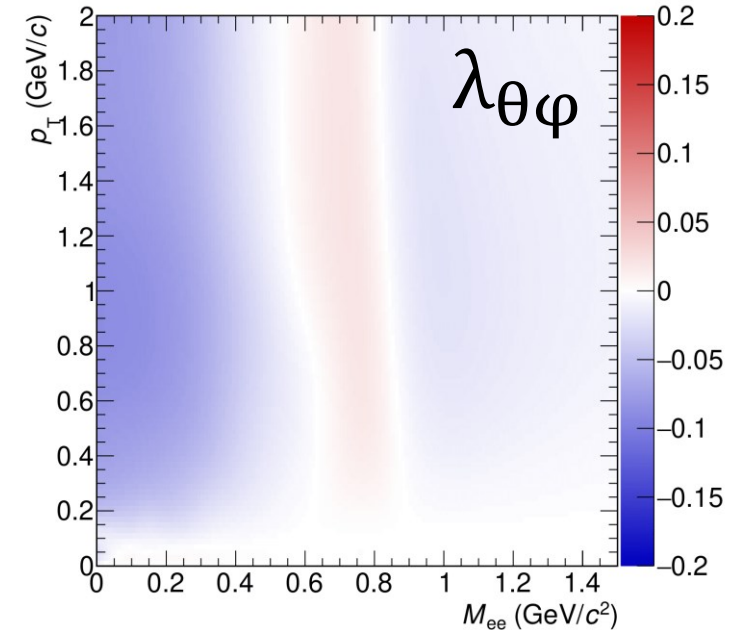
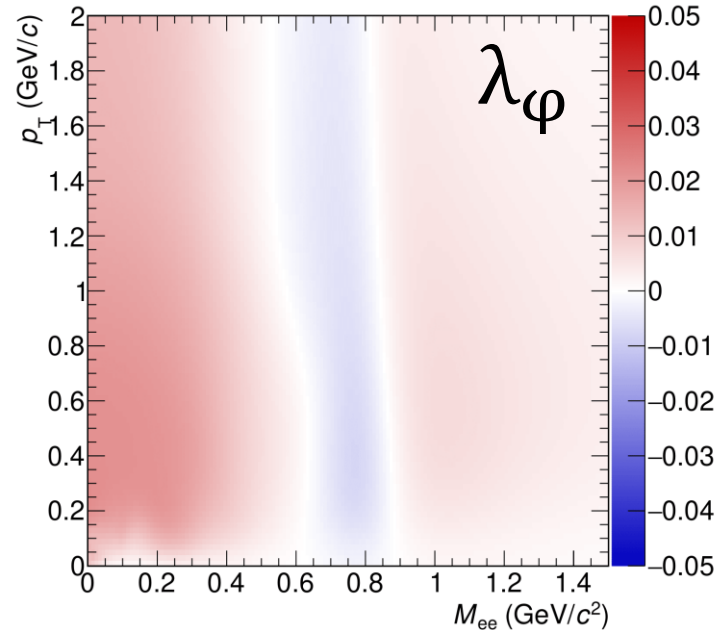
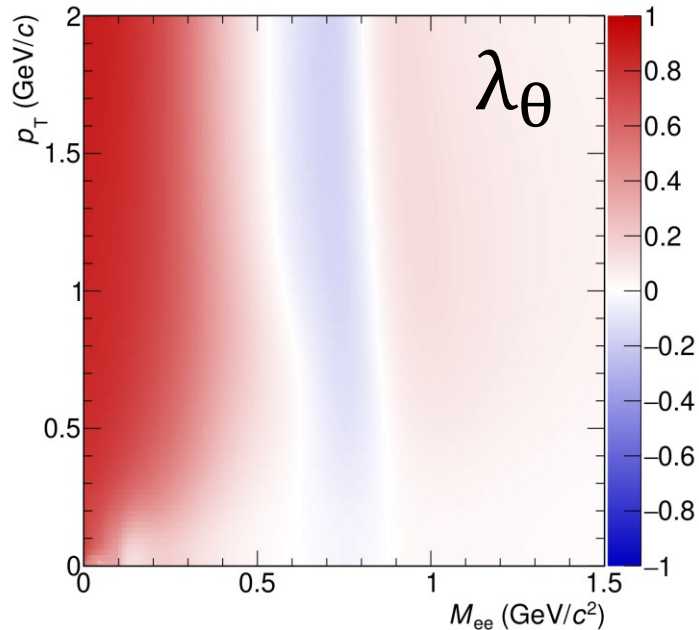


## RESULTS FOR AR+KCL COLLISIONS AT SIS18 ENERGIES

- HADES measured polarization coefficient  $\lambda_\theta$  of excess radiation in the HX frame in Ar+KCl collisions at 1.76 AGeV beam energy
- Space-time evolution via coarse-grained UrQMD
- Polarization largely survives evolution of the expanding medium

HADES coll., Phys. Rev. C 84, 014902 (2011)

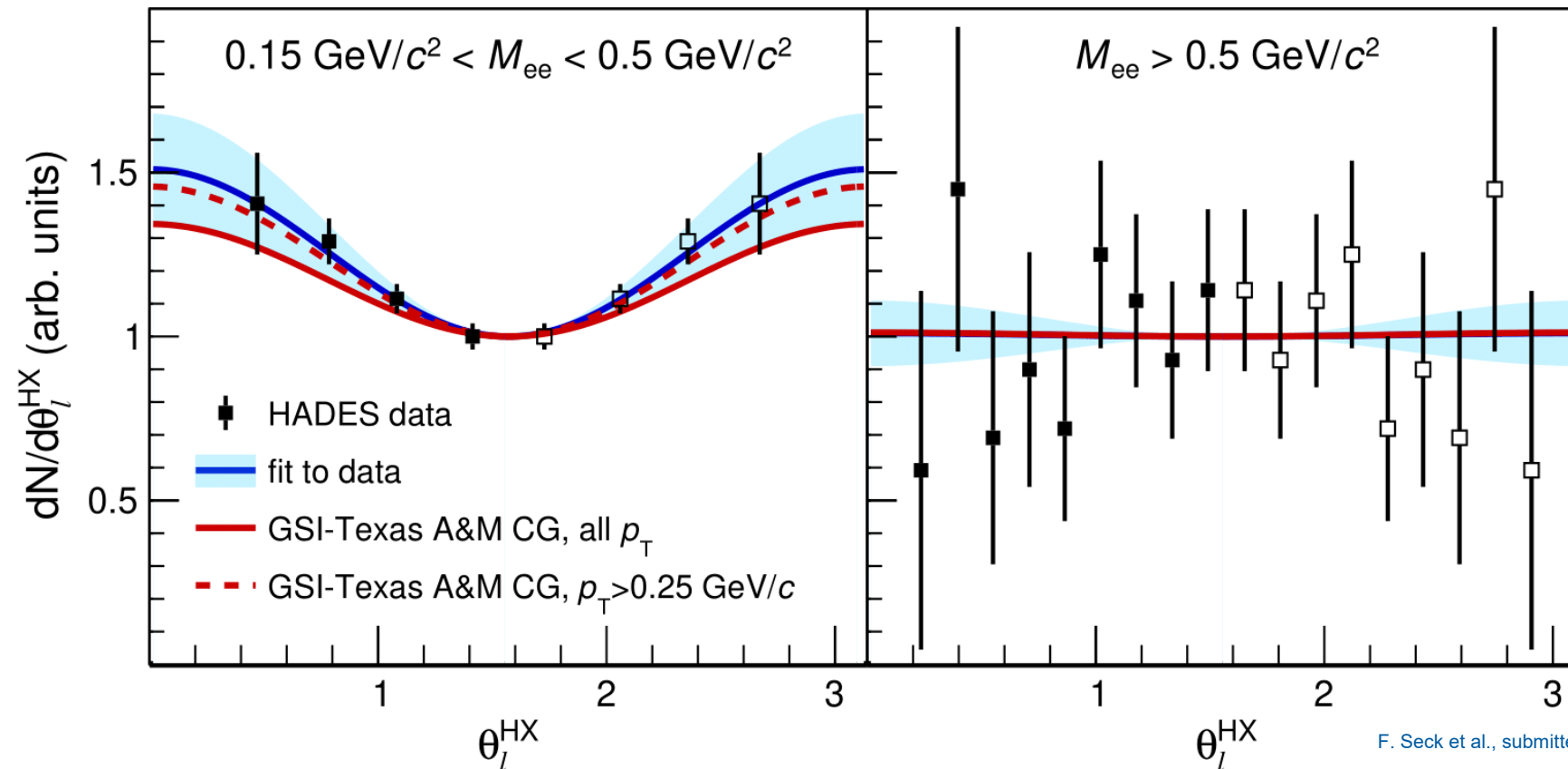
T. Galatyuk *et al.*, Eur. Phys. J. A 52, 131 (2016)



## COMPARISON TO HADES DATA

- Good agreement between data and theory
- **Best fit** to data gives  $\lambda_\theta = 0.51 \pm 0.17$  and  $\lambda_\theta = 0.01 \pm 0.10$  in the two mass windows
- **Calculation** result gives  $\lambda_\theta = 0.34$  and  $\lambda_\theta = 0.01$  respectively

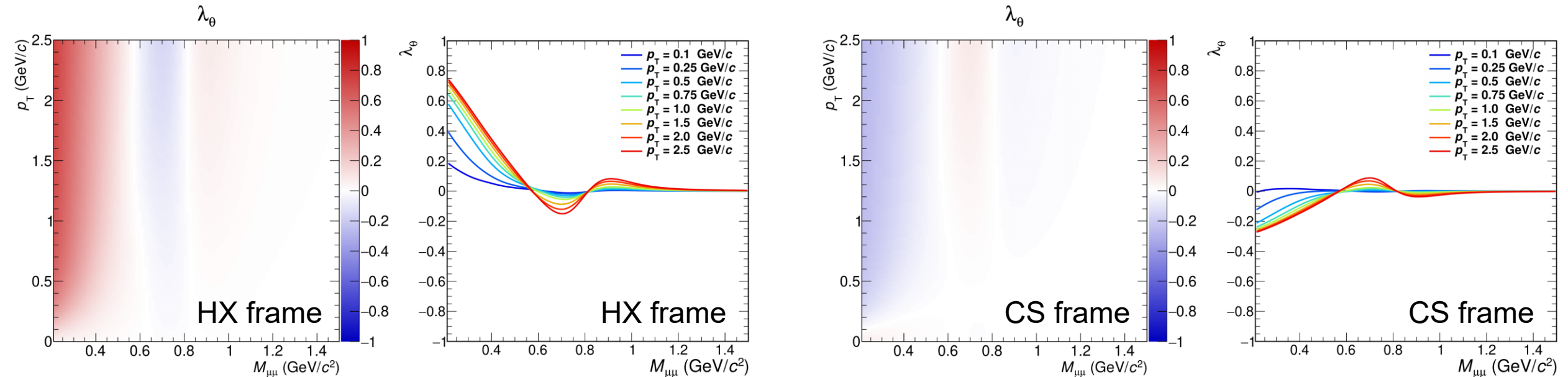
data points: HADES coll., Phys. Rev. C 84, 014902 (2011)



# RESULTS FOR IN+IN COLLISIONS AT SPS ENERGIES

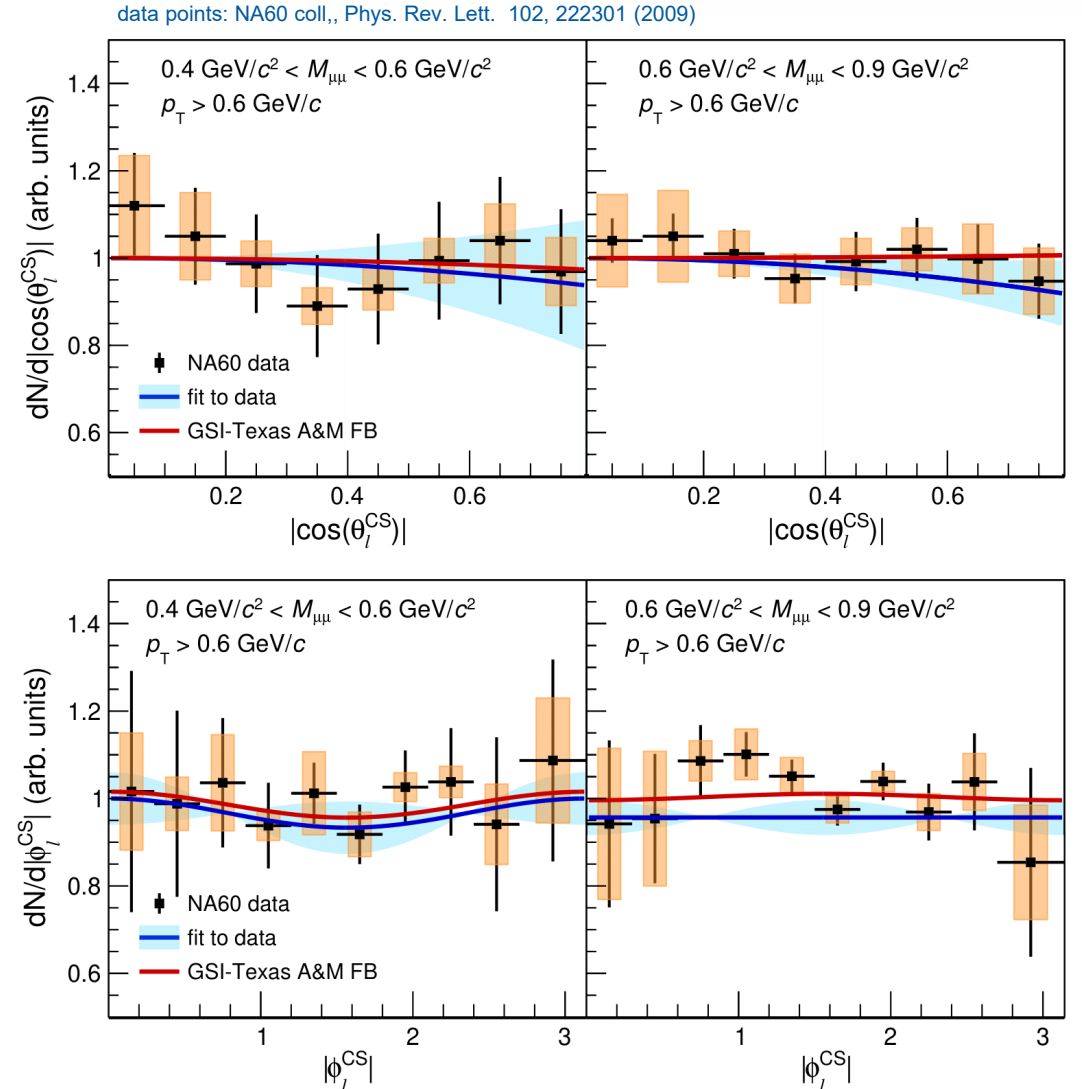
- NA60 measured polarization coefficients  $\lambda_\theta$ ,  $\lambda_\varphi$  and  $\lambda_{\theta\varphi}$  of excess radiation in the CS frame in In+In collisions at 158 AGeV beam energy
- Space-time evolution via isentropic fireball model with transition from QGP to hadronic rates at  $T=170$  MeV
- Strong dependence on the polarization frame as function of mass and momentum

NA60 coll., Phys. Rev. Lett. 96, 162302 (2006)  
R. Rapp, H. van Hees, Phys. Lett. B 753, 586 (2016)



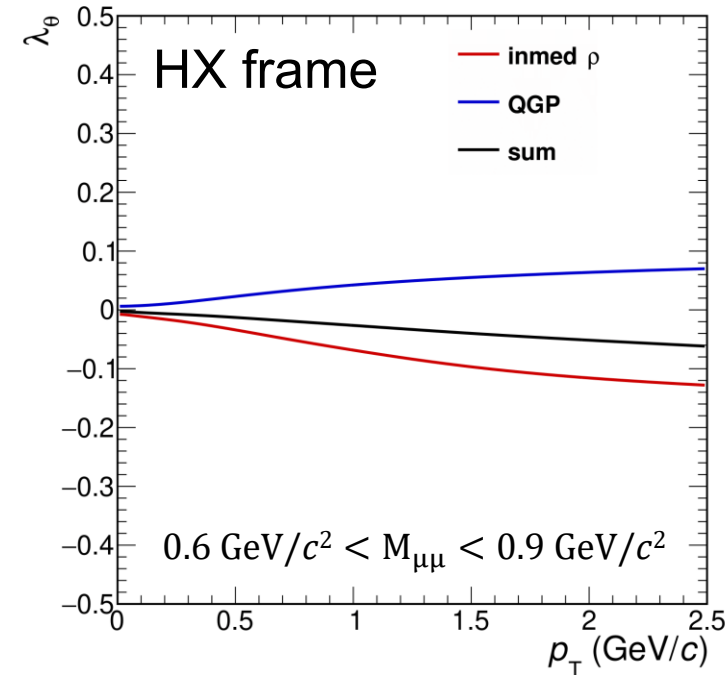
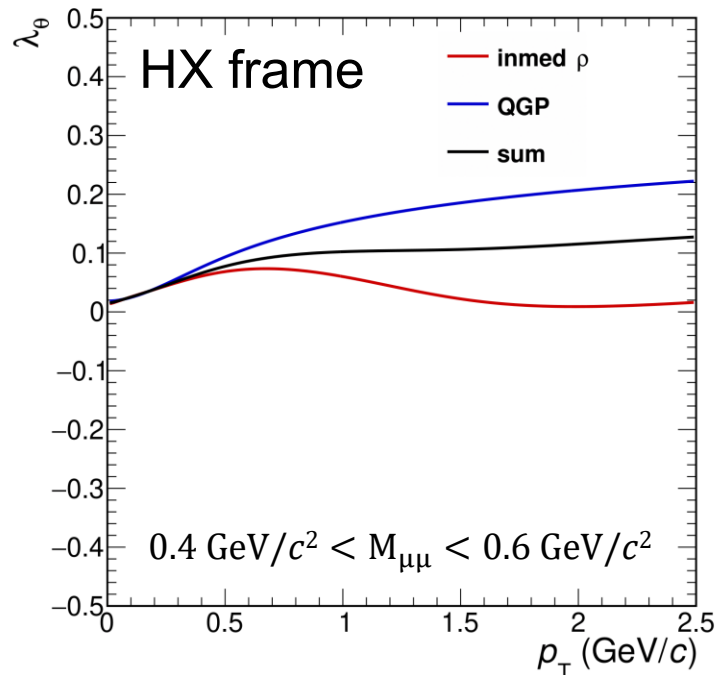
## COMPARISON TO NA60 DATA

- Good agreement between data and theory  
→ size and trend
- Near absence of a net polarization
  - not related to thermal isotropy arguments
  - thermal properties of the EM spectral function
- **Best fit** to data gives  $\lambda_\theta = -0.10 \pm 0.24$  and  $\lambda_\theta = -0.13 \pm 0.12$  in the two mass windows
- **Calculation** results in  $\lambda_\theta = -0.04$  and  $\lambda_\theta = 0.01$  respectively
- **Best fit** to data gives  $\lambda_\phi = 0.05 \pm 0.09$  and  $\lambda_\phi = 0.00 \pm 0.06$  in the two mass windows
- **Calculation** results in  $\lambda_\phi = 0.04$  and  $\lambda_\phi = -0.01$  respectively
- **Best fit** to data and **calculation** consistent with  $\lambda_{\theta\phi} = 0$  in both mass windows



## PROSPECT OF DISENTANGLING HADRONIC AND PARTONIC SOURCES

- Polarization observables will play an increasingly important role in exploring the mechanisms underlying EM emission spectra in heavy-ion collisions
- Multidifferential measurements of the virtual photon polarization → large datasets needed
  - HADES, STAR and ALICE
  - future high-rate experiments CBM, NA60+ and ALICE3





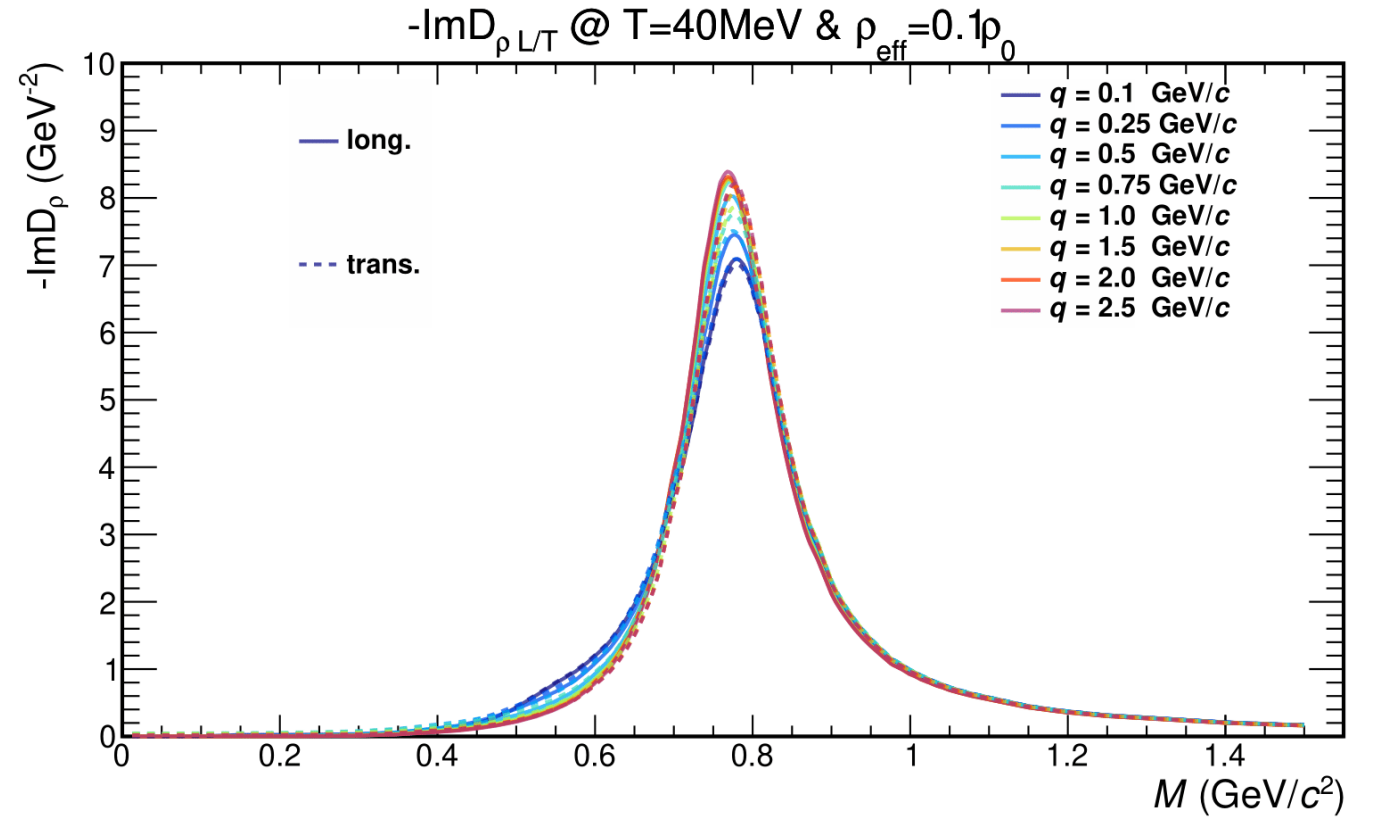
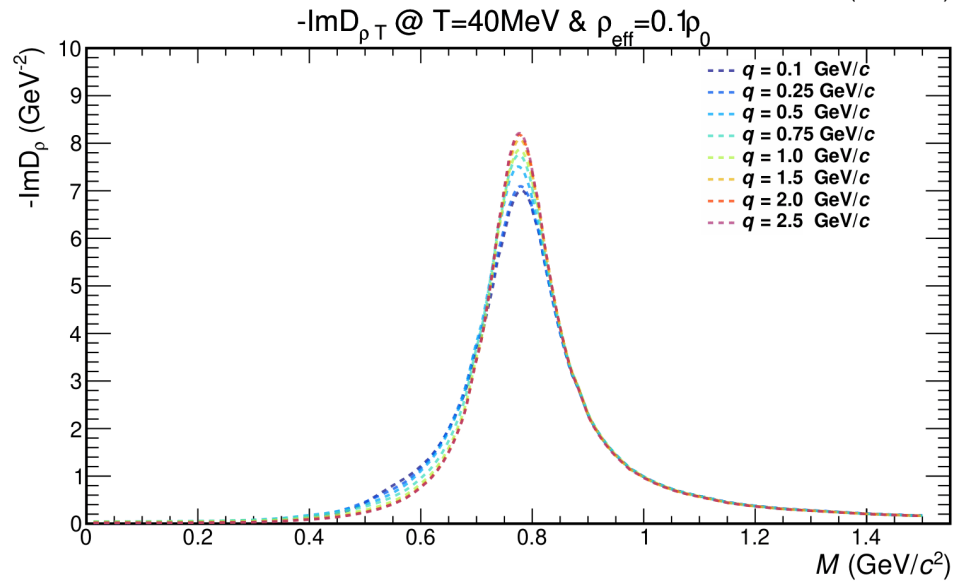
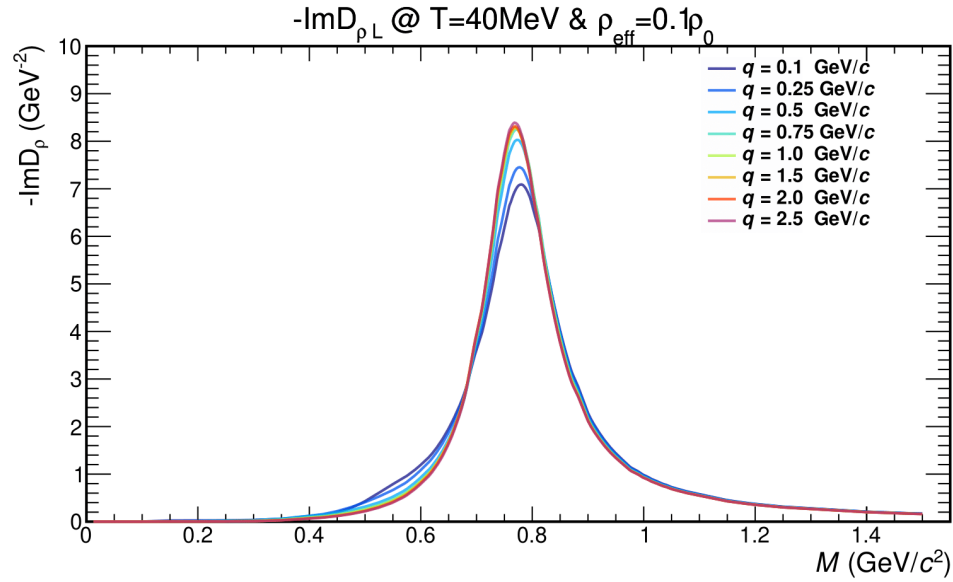
## SUMMARY

- Polarization properties of virtual photons from electromagnetic spectral functions of QCD matter
  - Sensitive to difference of longitudinal and transverse components of the spectral function
- Polarization of hadronic matter transits from transverse at low masses into longitudinal in the  $\rho$ -meson mass region
  - Less pronounced structure at high temperatures and low baryon density
  - More closely resembles polarization of QGP emission
- Transformations from the thermal frame into angular variables observable in the lab frame
  - Good agreement between our predictions and both HADES and NA60 data
- Polarization observables to play an increasingly important role in exploring the mechanisms underlying EM emission
  - Multidifferential measurements: HADES, STAR, ALICE, CBM, NA60+ and ALICE3

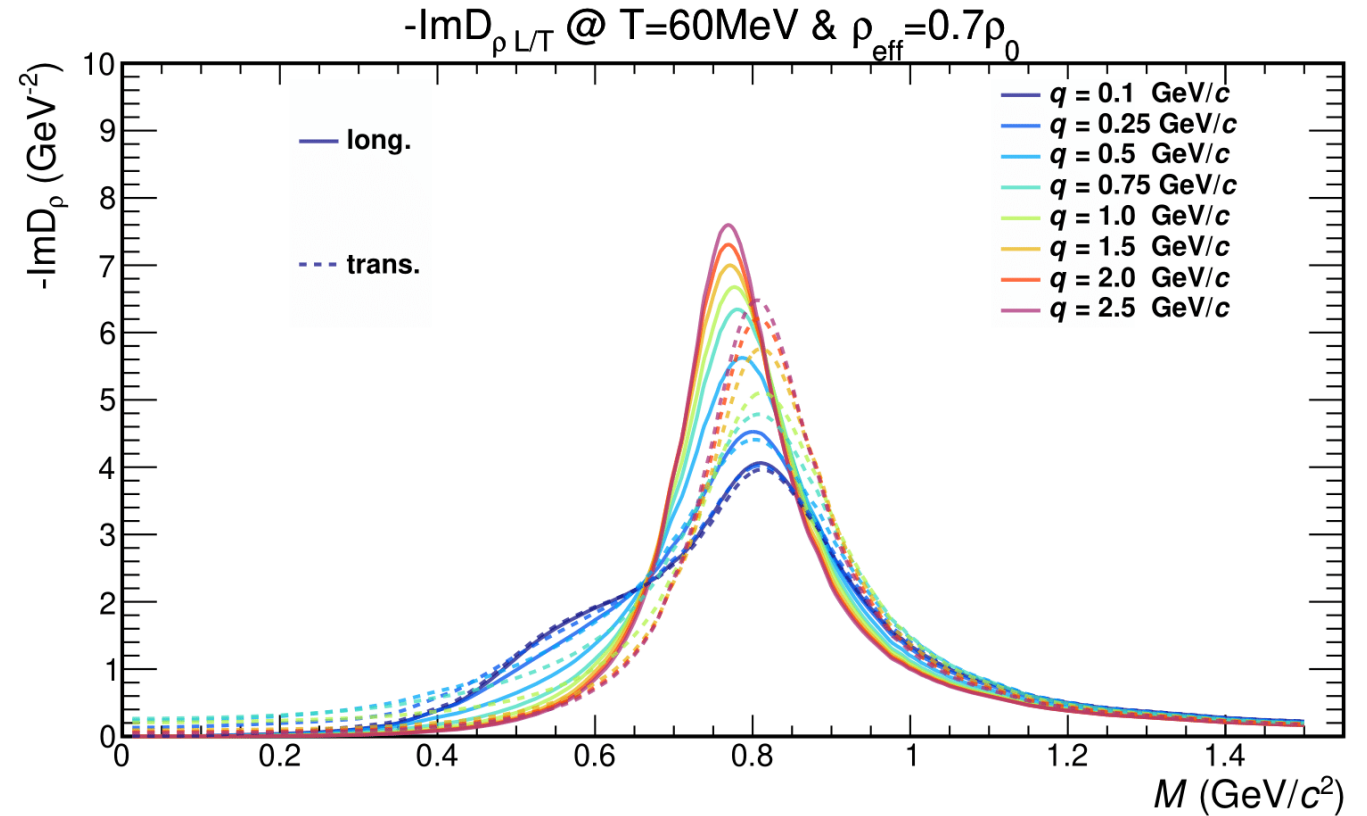
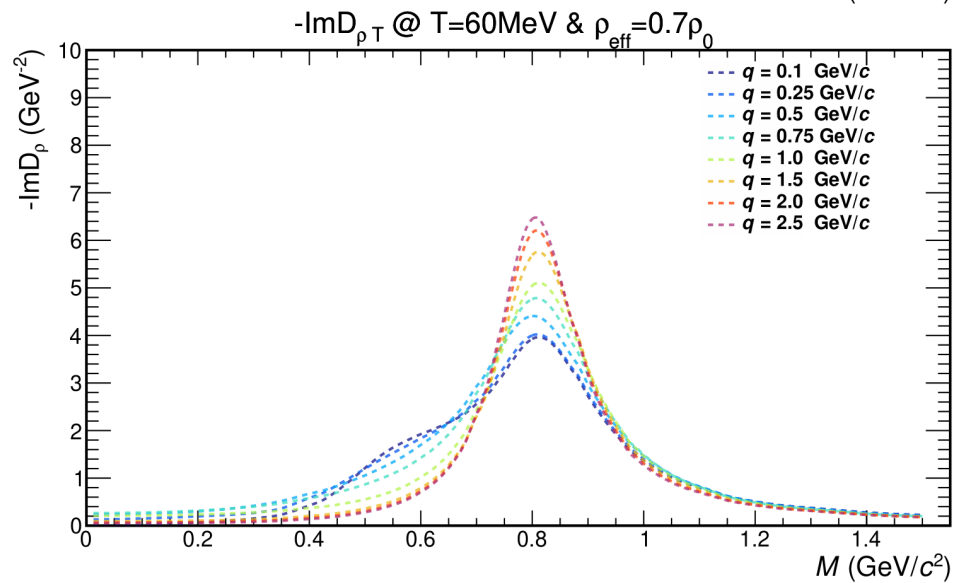
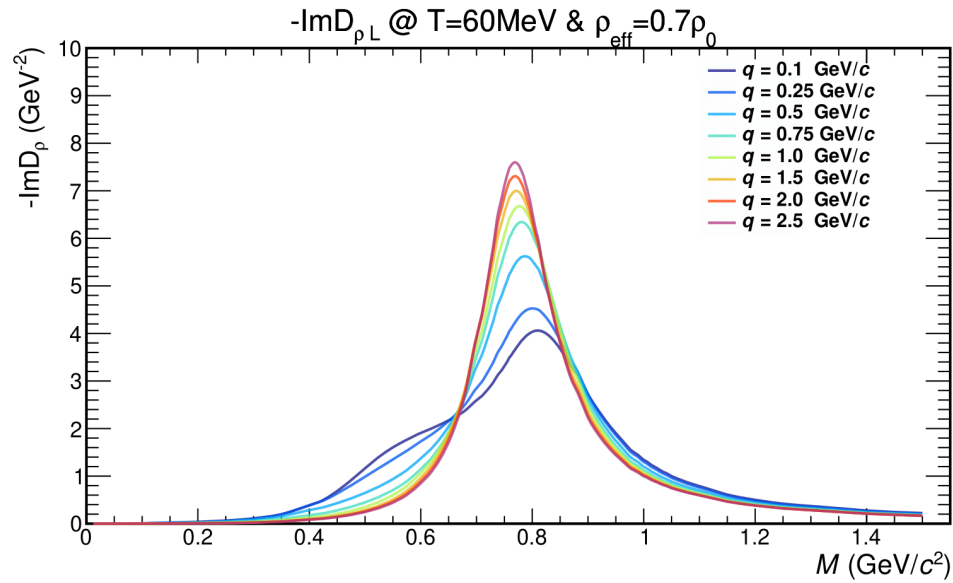


# BACKUP

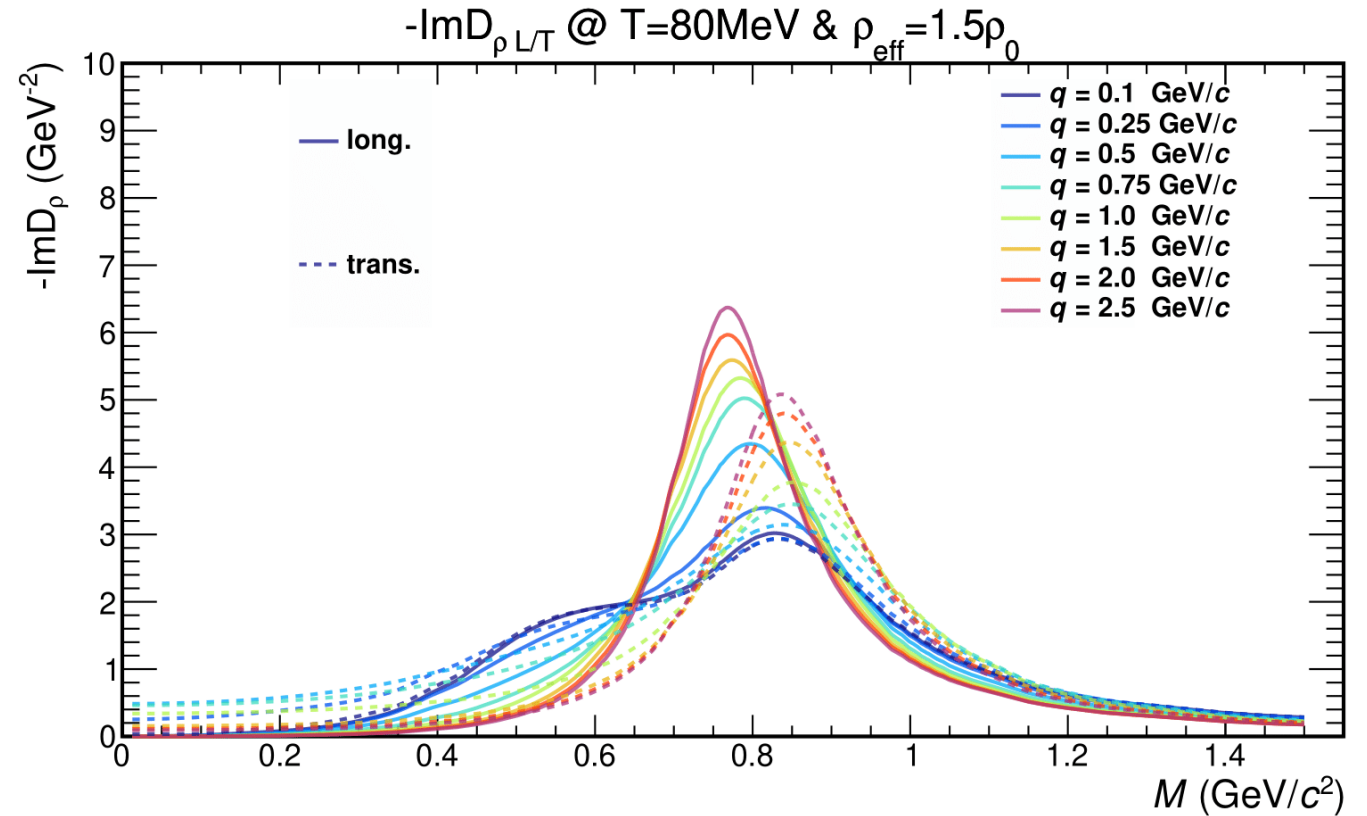
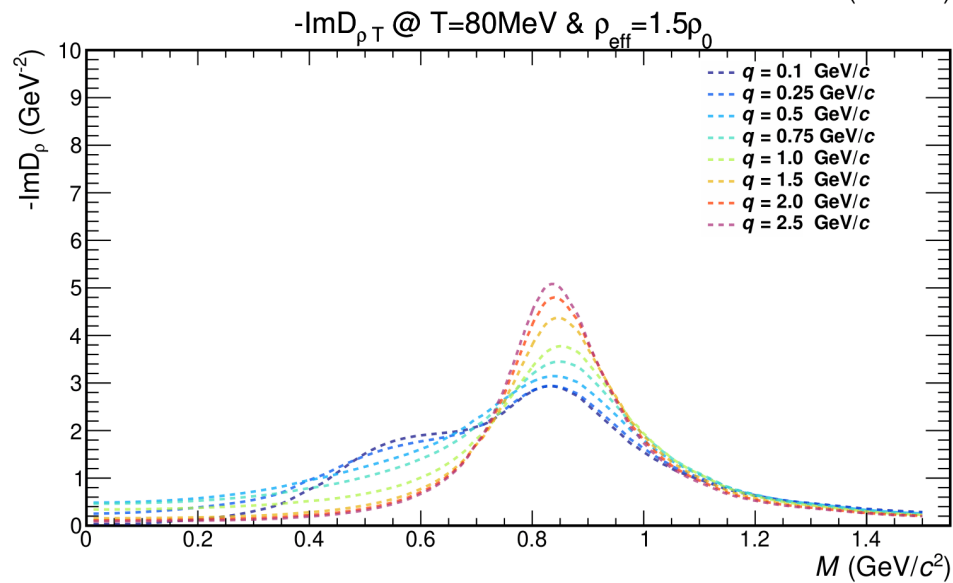
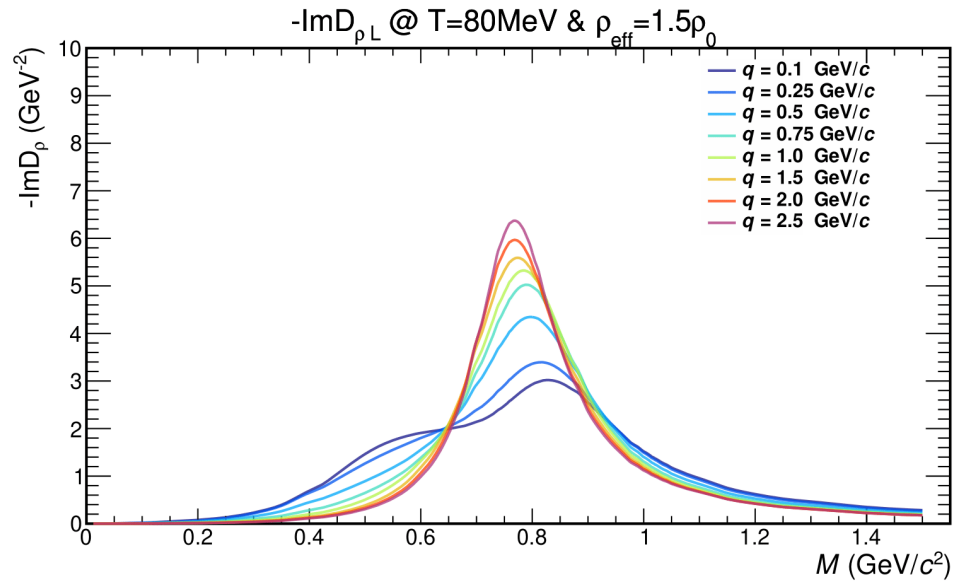
# SPECTRAL FUNCTION COMPONENTS: LOW TEMPERATURE & LOW DENSITY



# SPECTRAL FUNCTION COMPONENTS: MID TEMPERATURE & MID DENSITY



# SPECTRAL FUNCTION COMPONENTS: HIGH TEMPERATURE & HIGH DENSITY



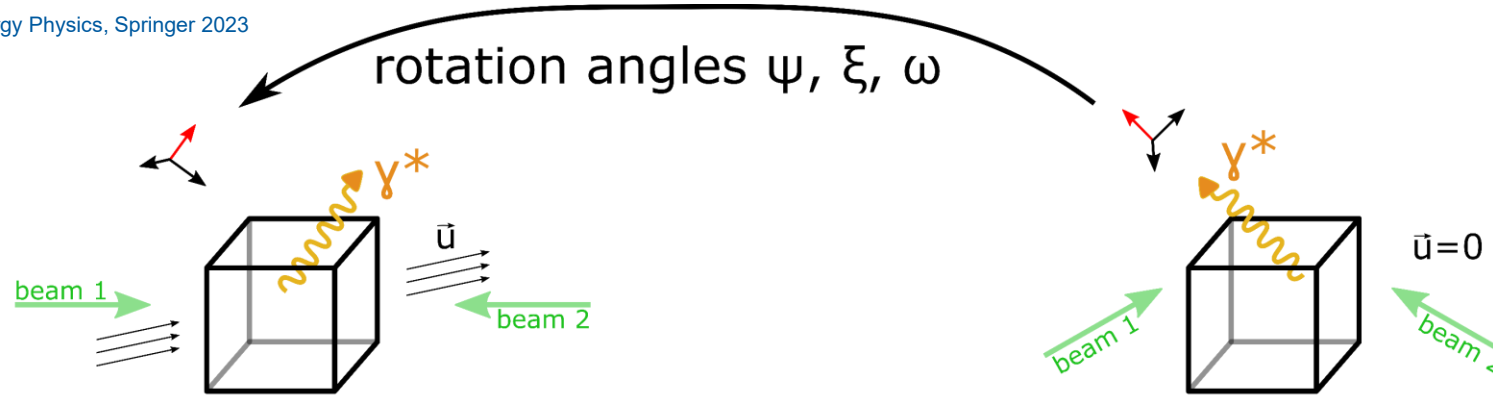
# VIRTUAL PHOTON POLARIZATION

based on: P. Faccioli, Particle Polarization in High Energy Physics, Springer 2023

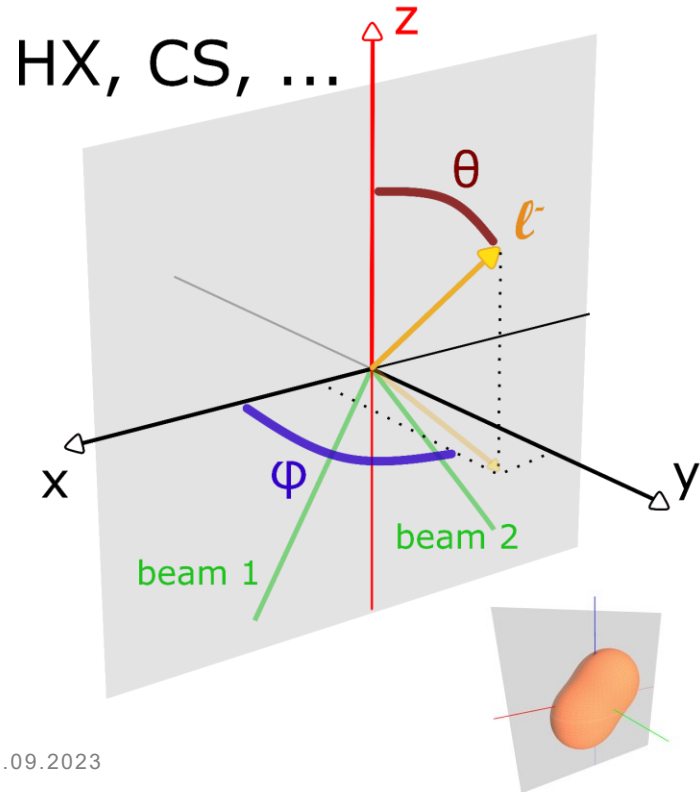
- $\psi$  -- rotation around  $z'$ -axis: rotated y-axis perpendicular to final z-axis
- $\xi$  -- rotation around new  $y''$ -axis: align initial and final z-axes
- $\omega$  -- rotation around z-axis: give x- and y-axes their orientation



center-of-mass  
frame of the collision  
"lab"



local fluid  
rest frame



$$\lambda_\theta = \frac{\lambda'_\theta}{1 + \Lambda} \left( 1 - \frac{3}{2} \sin^2 \xi \right)$$

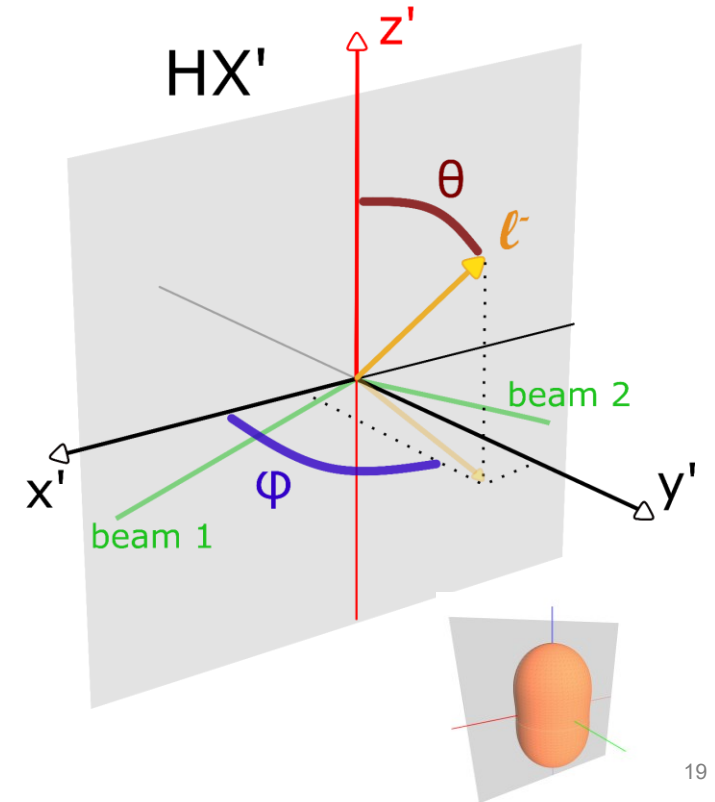
$$\Lambda = \frac{1}{2} \lambda'_\theta \sin^2 \xi$$

$$\lambda_\phi = \frac{\lambda'_\theta}{1 + \Lambda} \left( \frac{1}{2} \sin^2 \xi \cos 2\omega \right)$$

$$\lambda_{\theta\phi} = \frac{\lambda'_\theta}{1 + \Lambda} \left( -\frac{1}{2} \sin 2\xi \cos \omega \right)$$

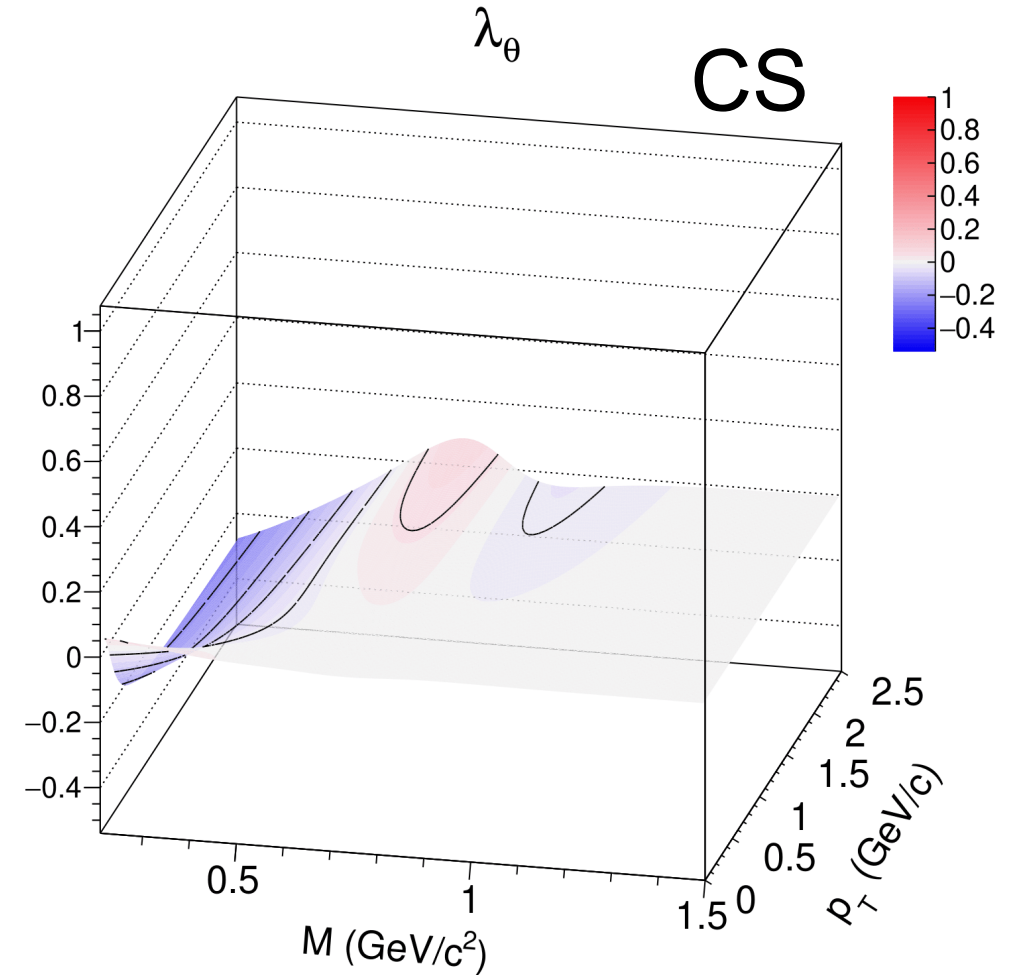
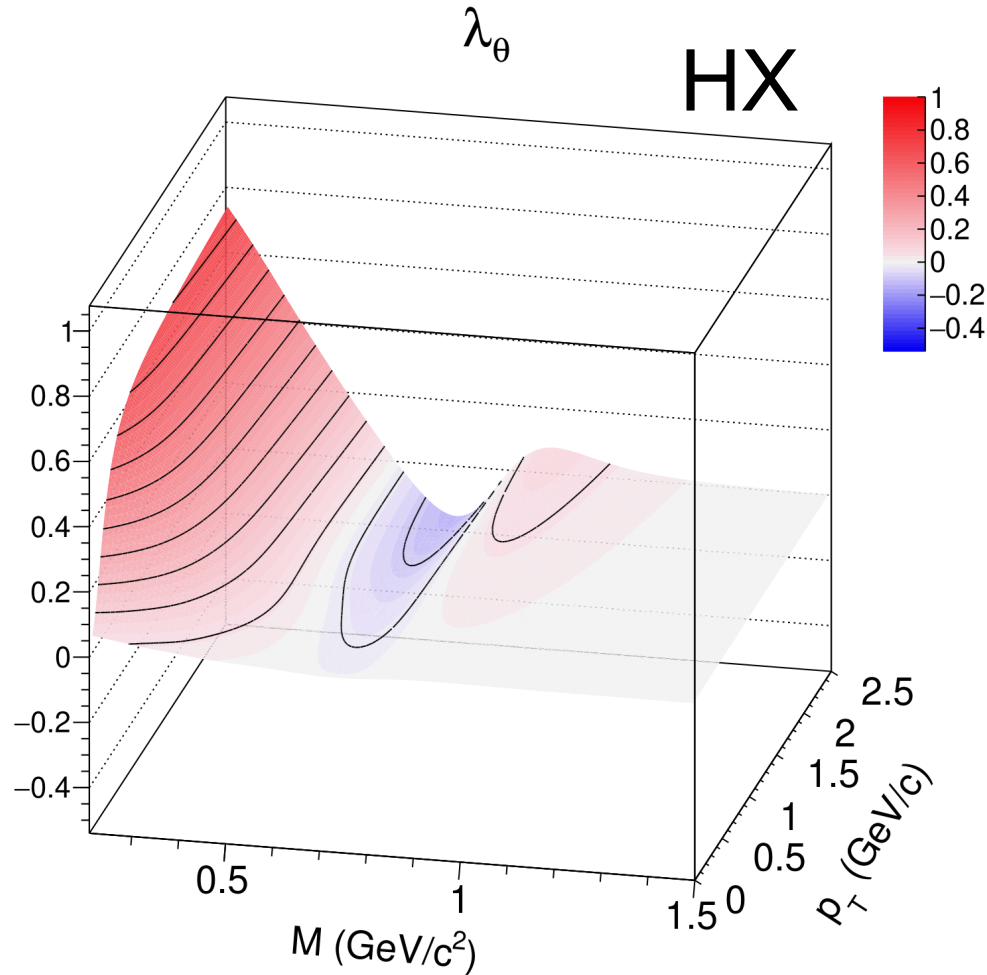
$$\lambda_\phi^\perp = \frac{\lambda'_\theta}{1 + \Lambda} \left( -\frac{1}{2} \sin^2 \xi \sin 2\omega \right)$$

$$\lambda_{\theta\phi}^\perp = \frac{\lambda'_\theta}{1 + \Lambda} \left( \frac{1}{2} \sin 2\xi \sin \omega \right)$$



# RESULTS FOR IN+IN COLLISIONS IN SPS ENERGY REGIME: LAMBDA THETA

- Strong dependence on the polarization frame as function of mass and momentum



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- Polarization observables will play an increasingly important role in exploring the mechanisms underlying EM emission spectra in heavy-ion collisions

