



# Rapidity-dependent Dynamics of the Initial State via 3D Multi-system Bayesian Calibration

Andi Mankolli  
Vanderbilt University  
(on behalf of the JETSCAPE Collaboration)



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QM23, 2-9, Sep.



SFP\_300495

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Experimental measurements at mid-rapidity have driven characterization of the quark-gluon plasma

Bayesian analyses compared mid-rapidity data to 2D initial state and hydrodynamic models

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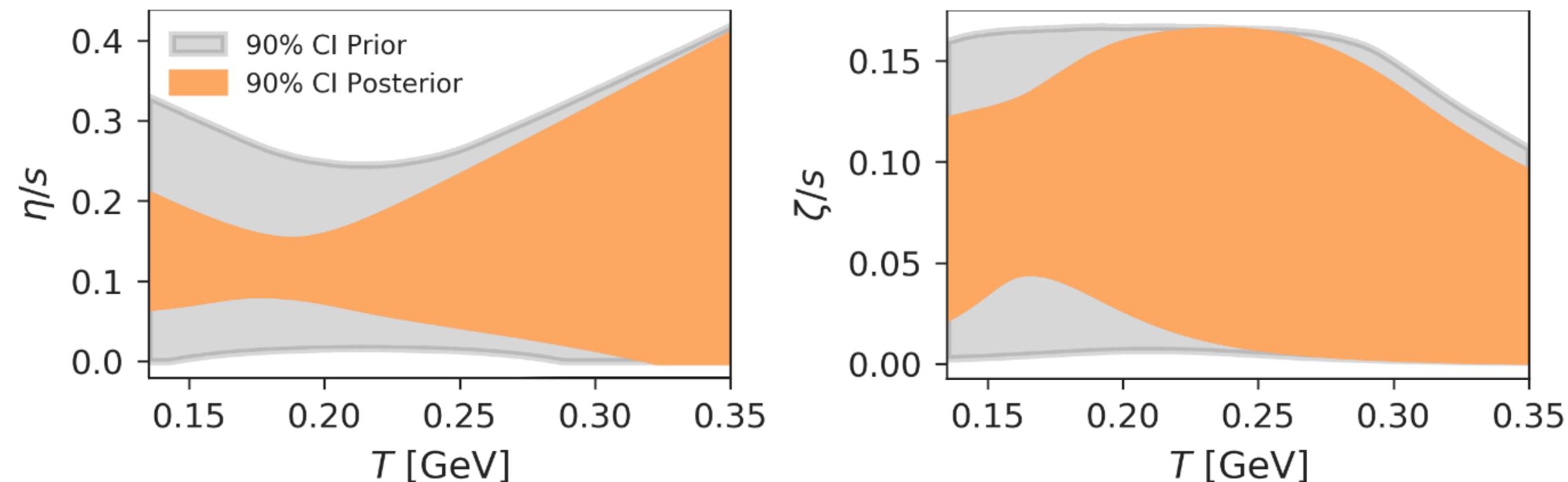
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PHYSICAL REVIEW LETTERS **126**, 242301 (2021)

Editors' Suggestion

## Phenomenological Constraints on the Transport Properties of QCD Matter with Data-Driven Model Averaging

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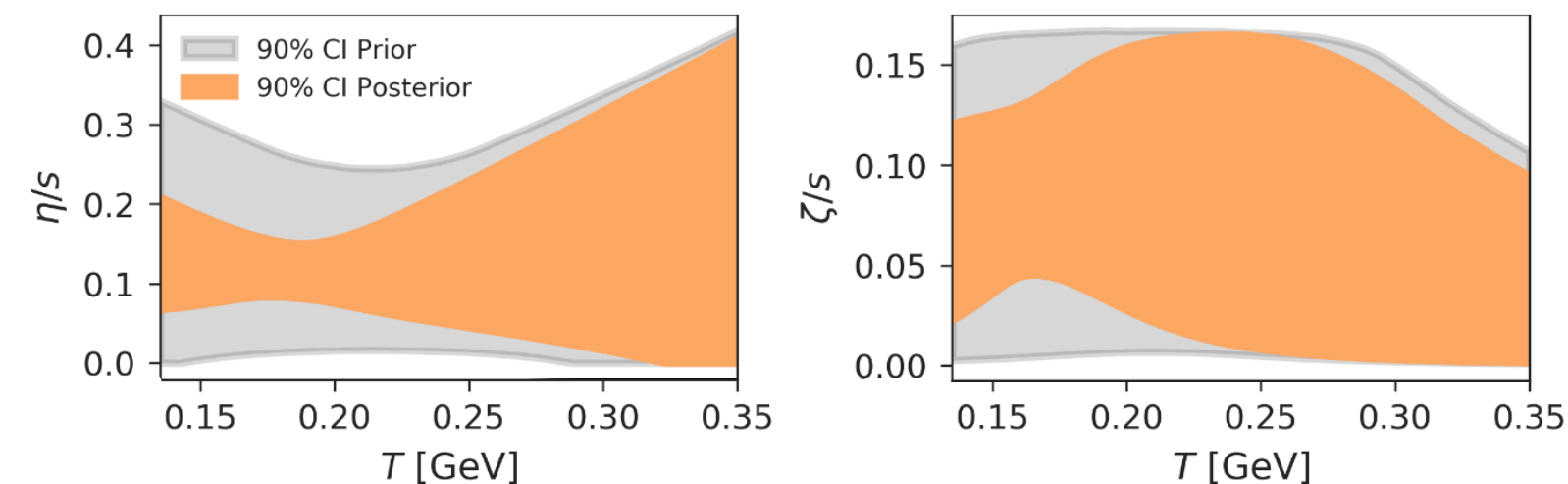
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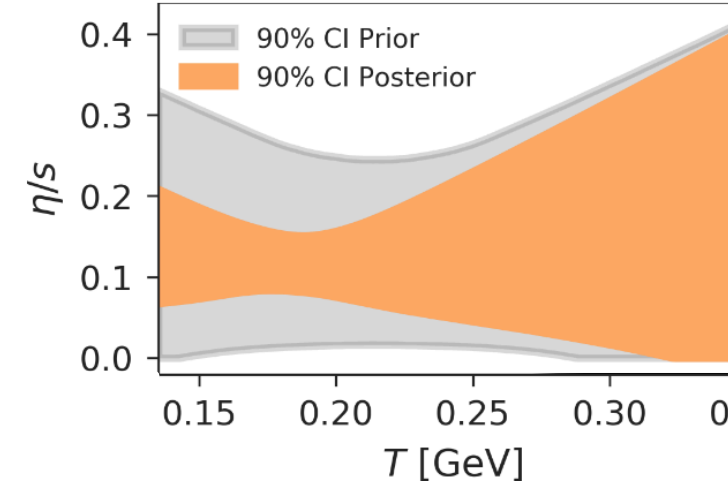
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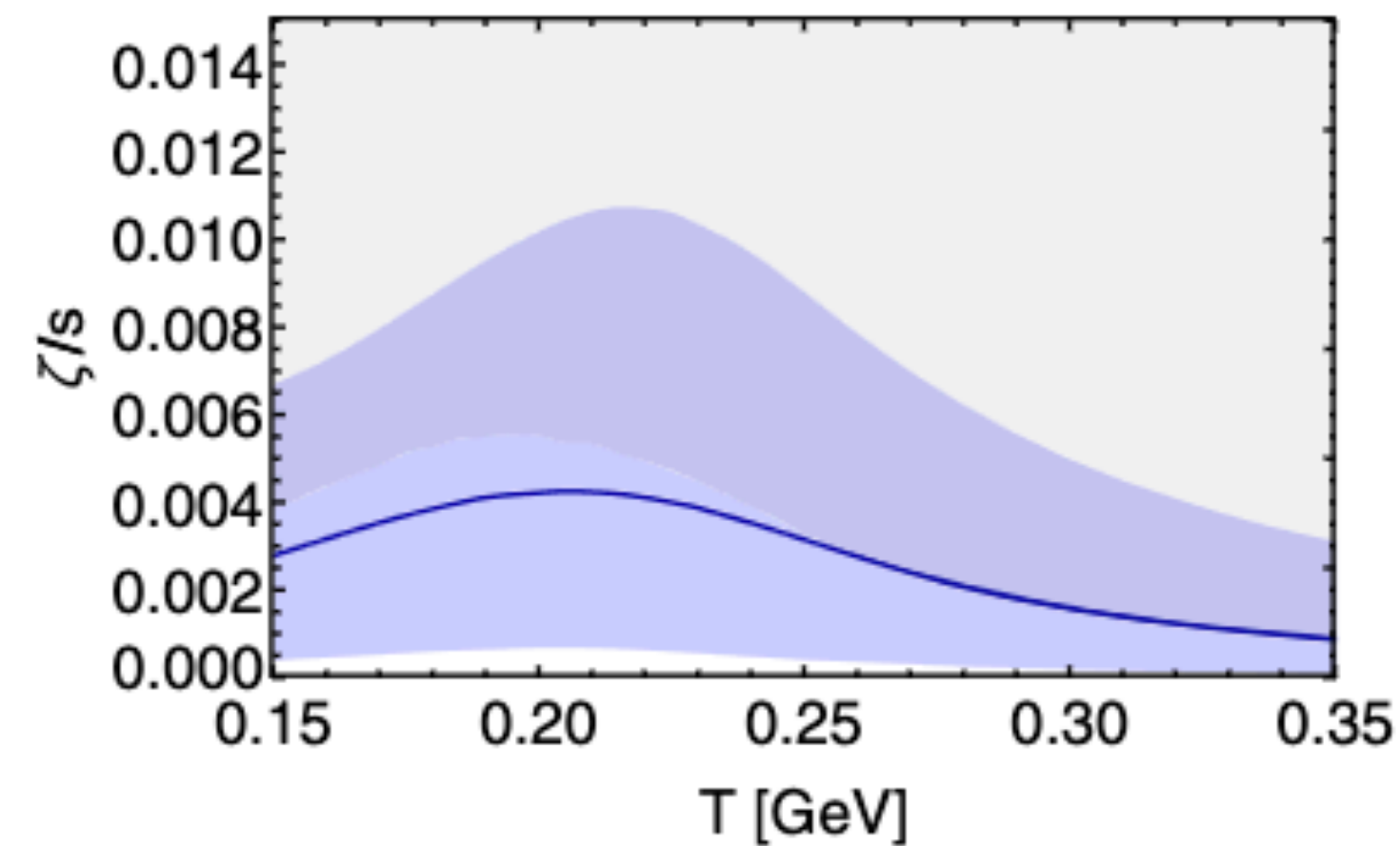
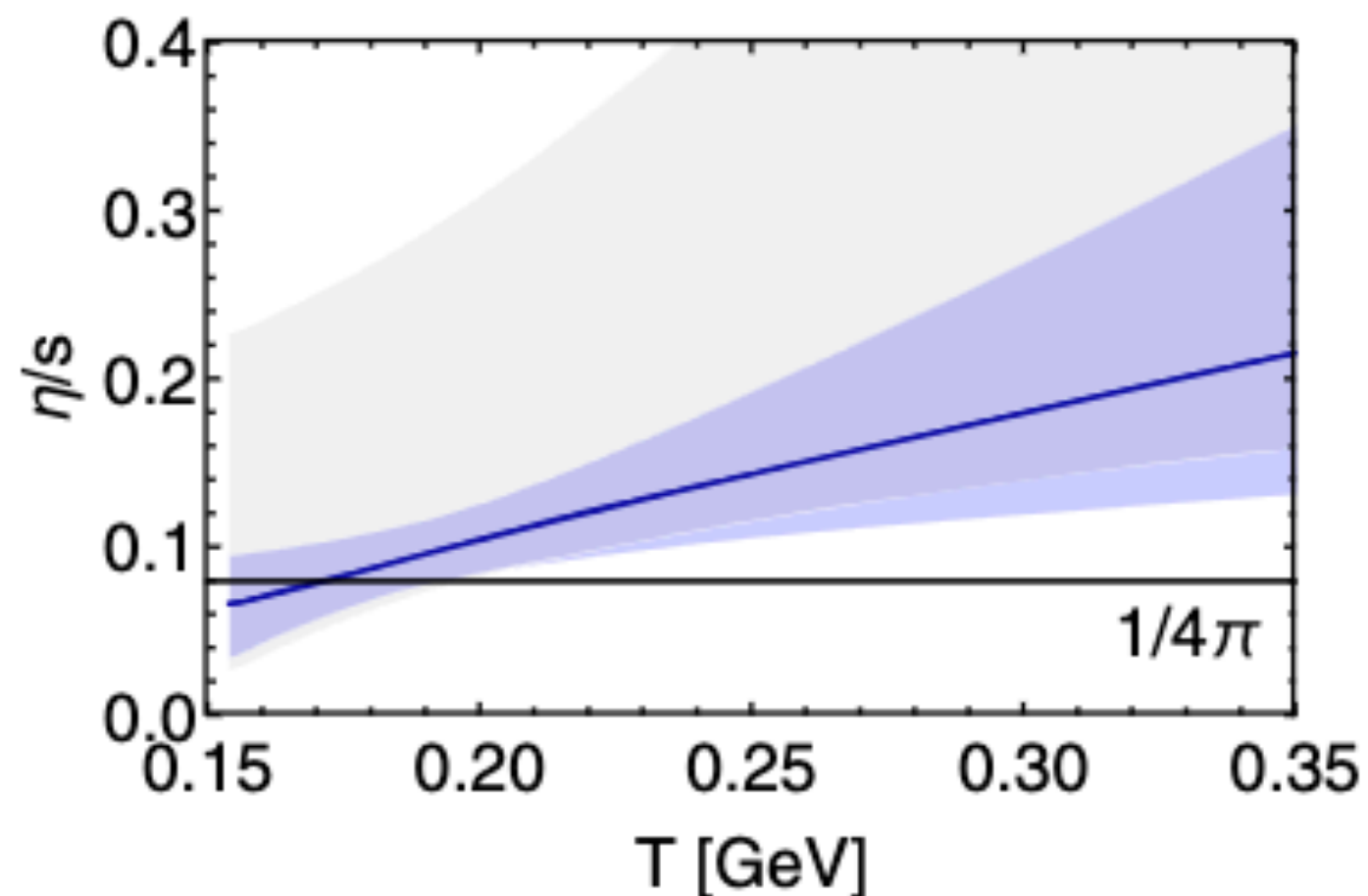
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## Transverse Momentum Differential Global Analysis of Heavy-Ion Collisions

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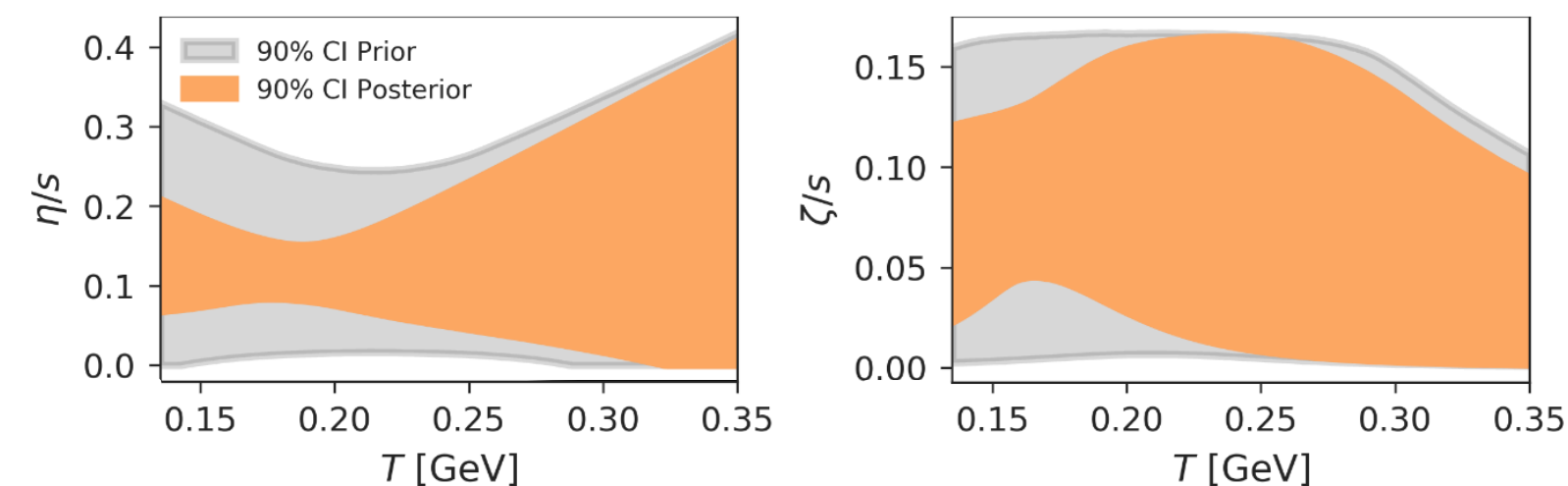
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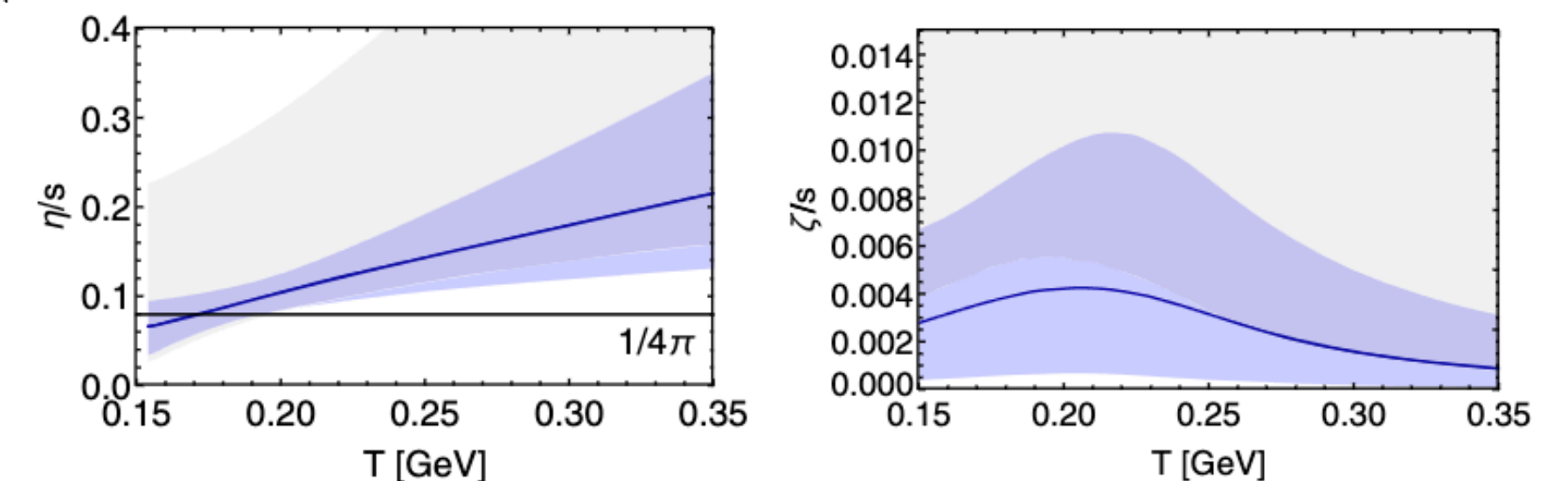
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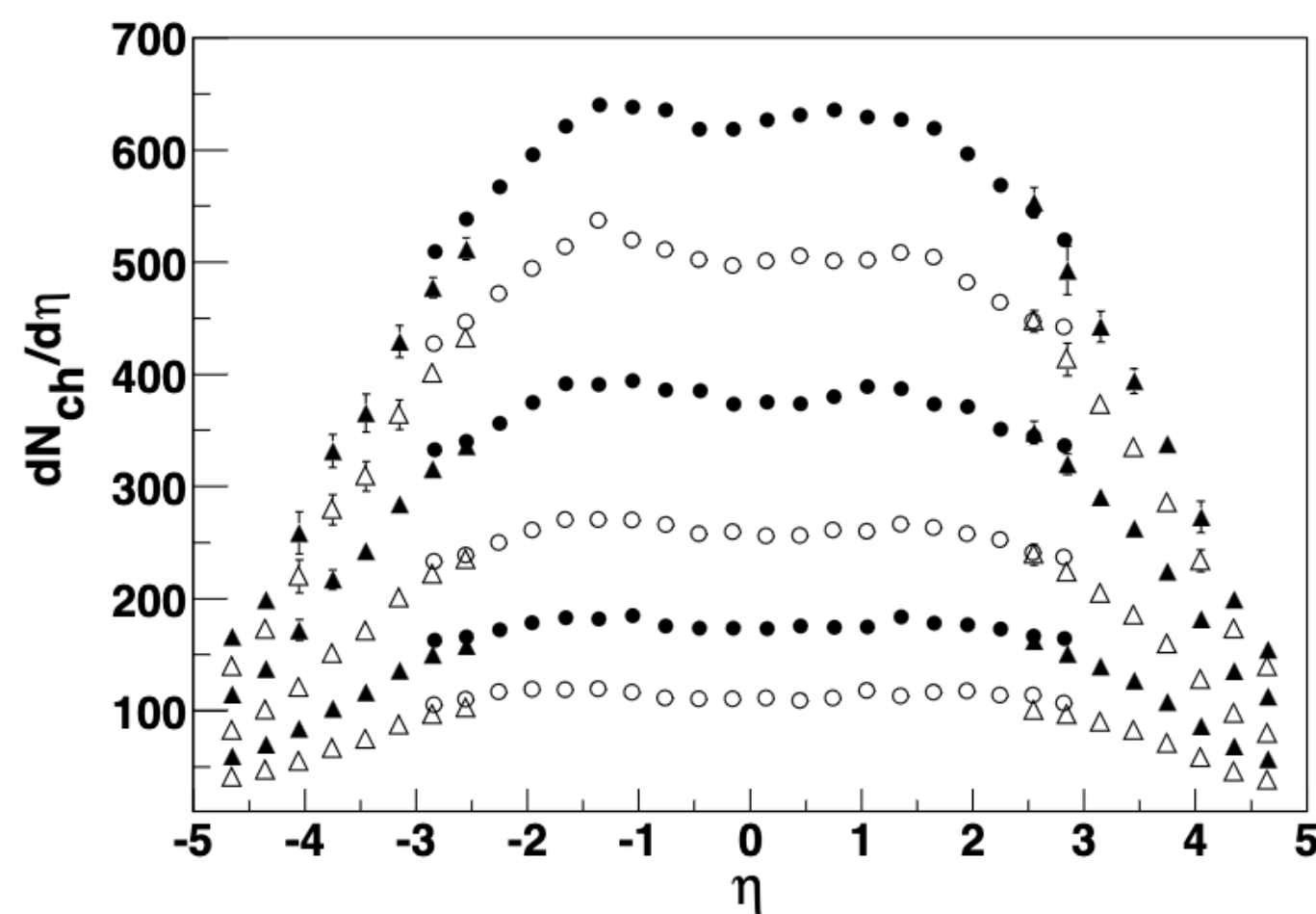


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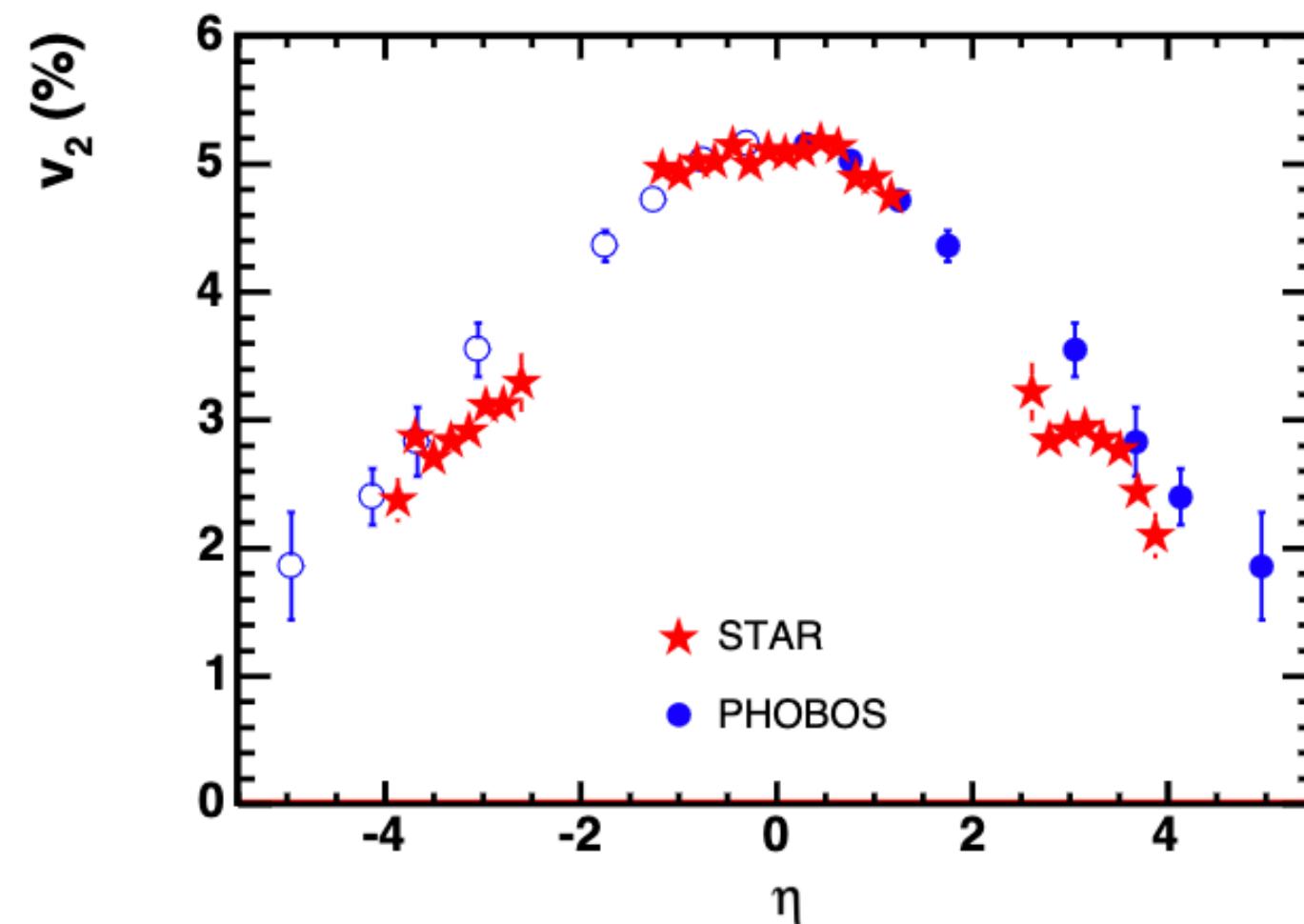
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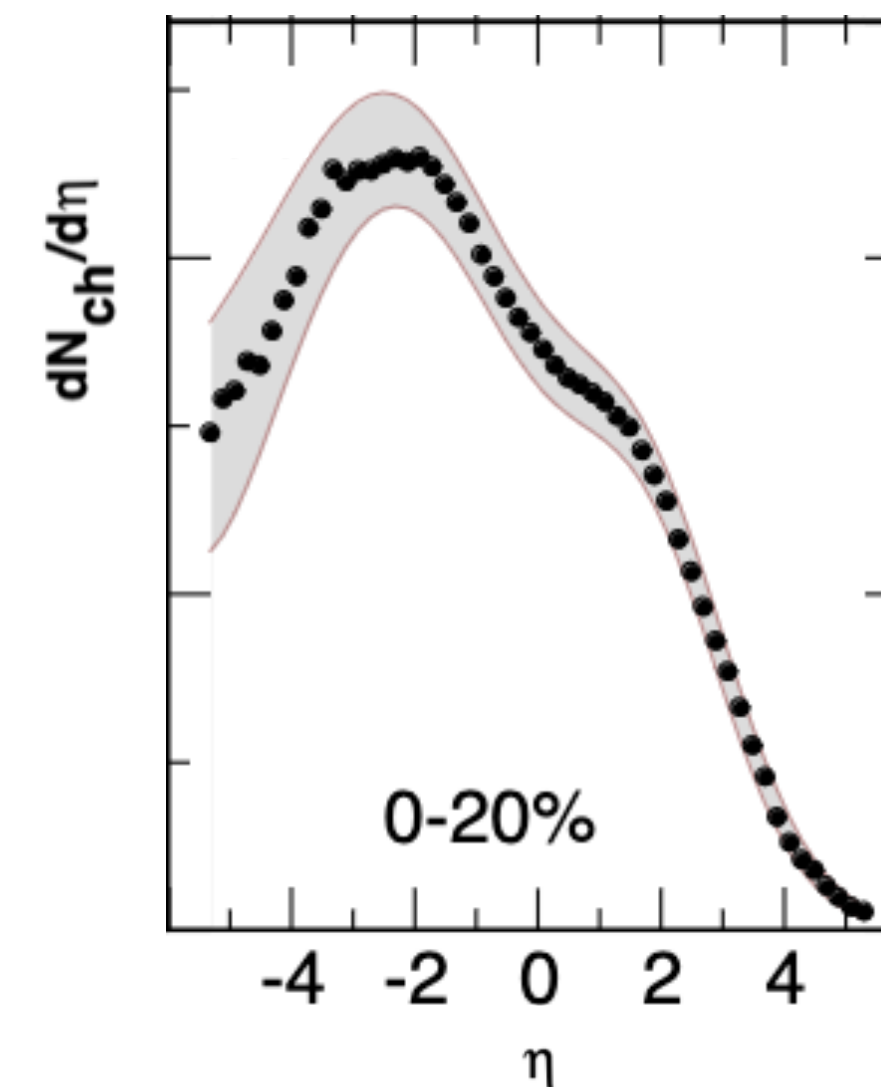
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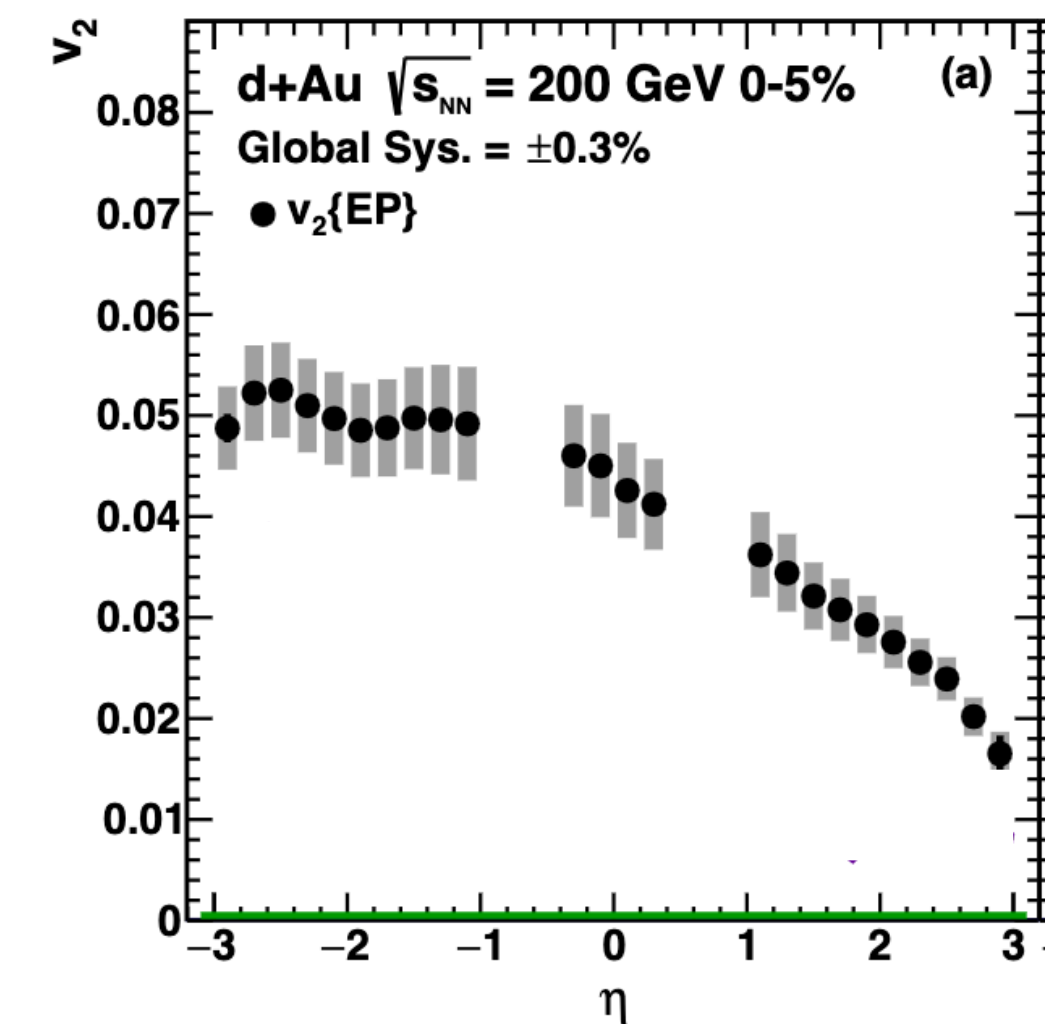
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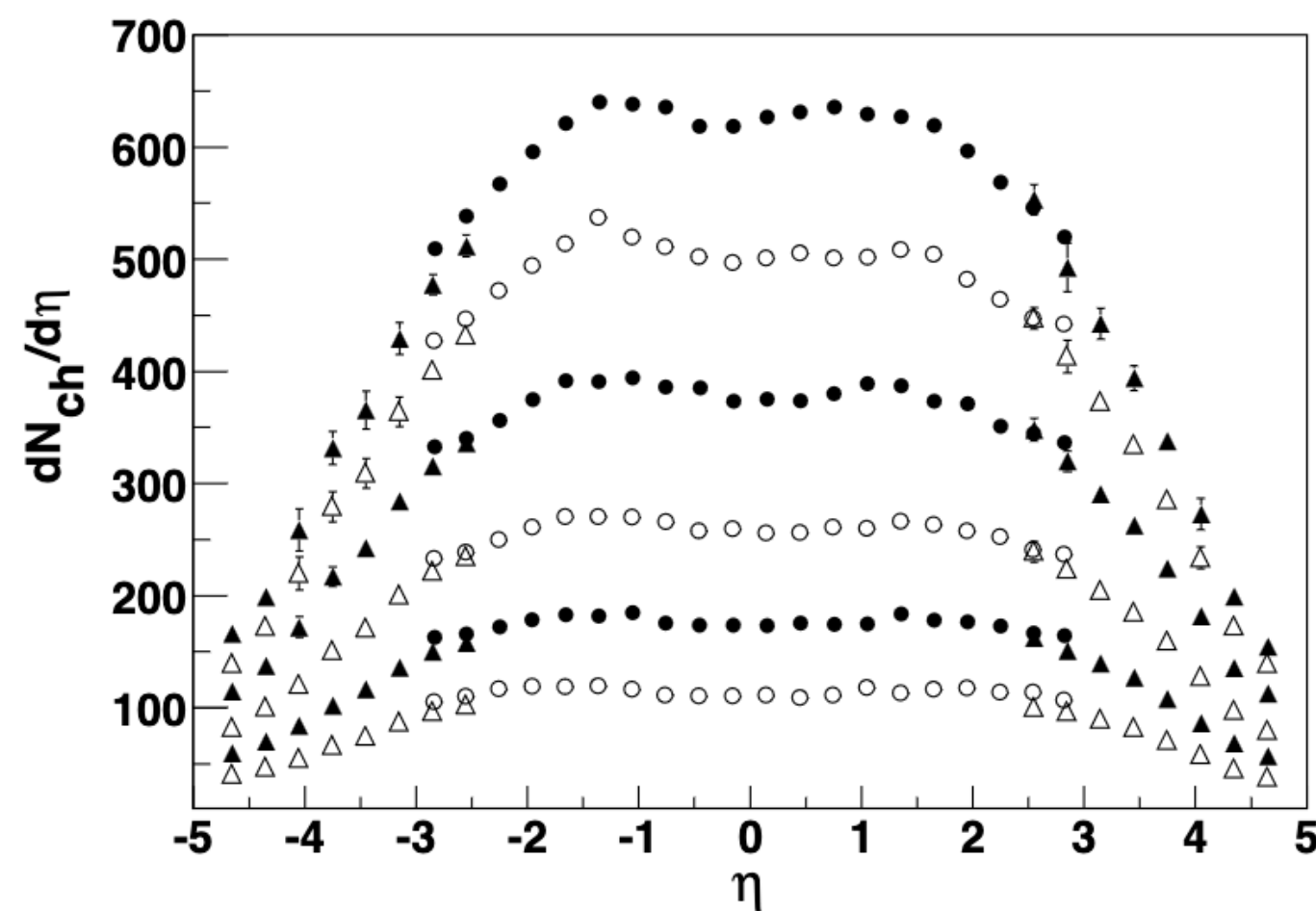


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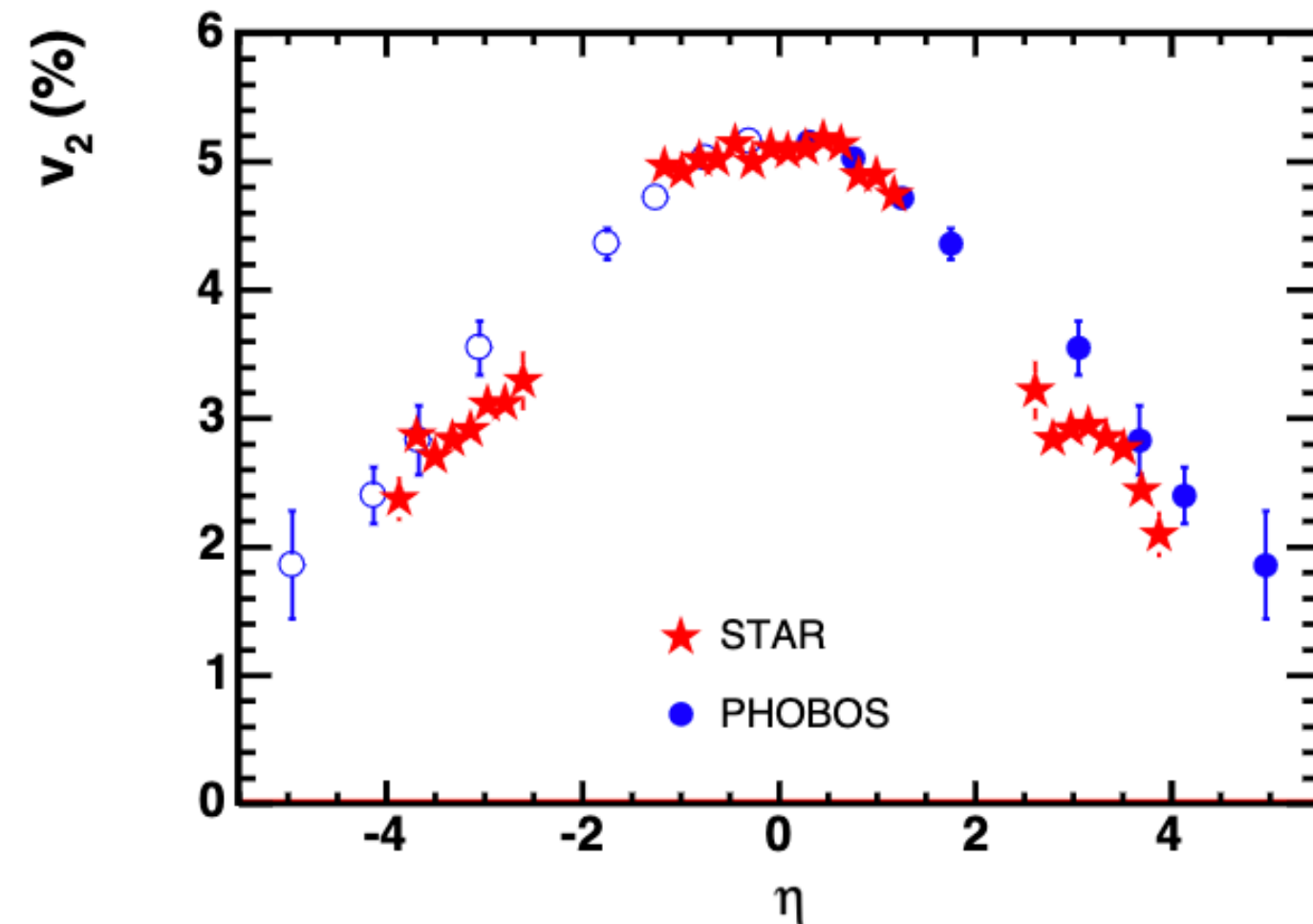
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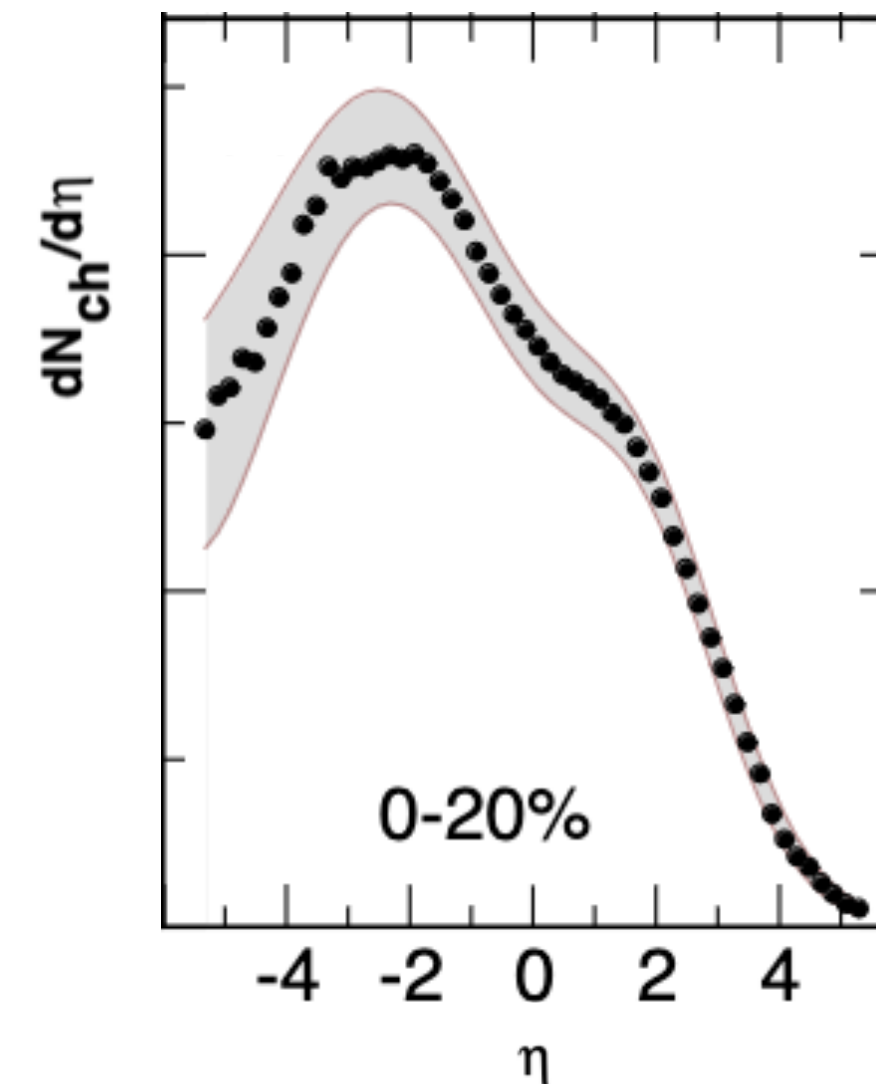
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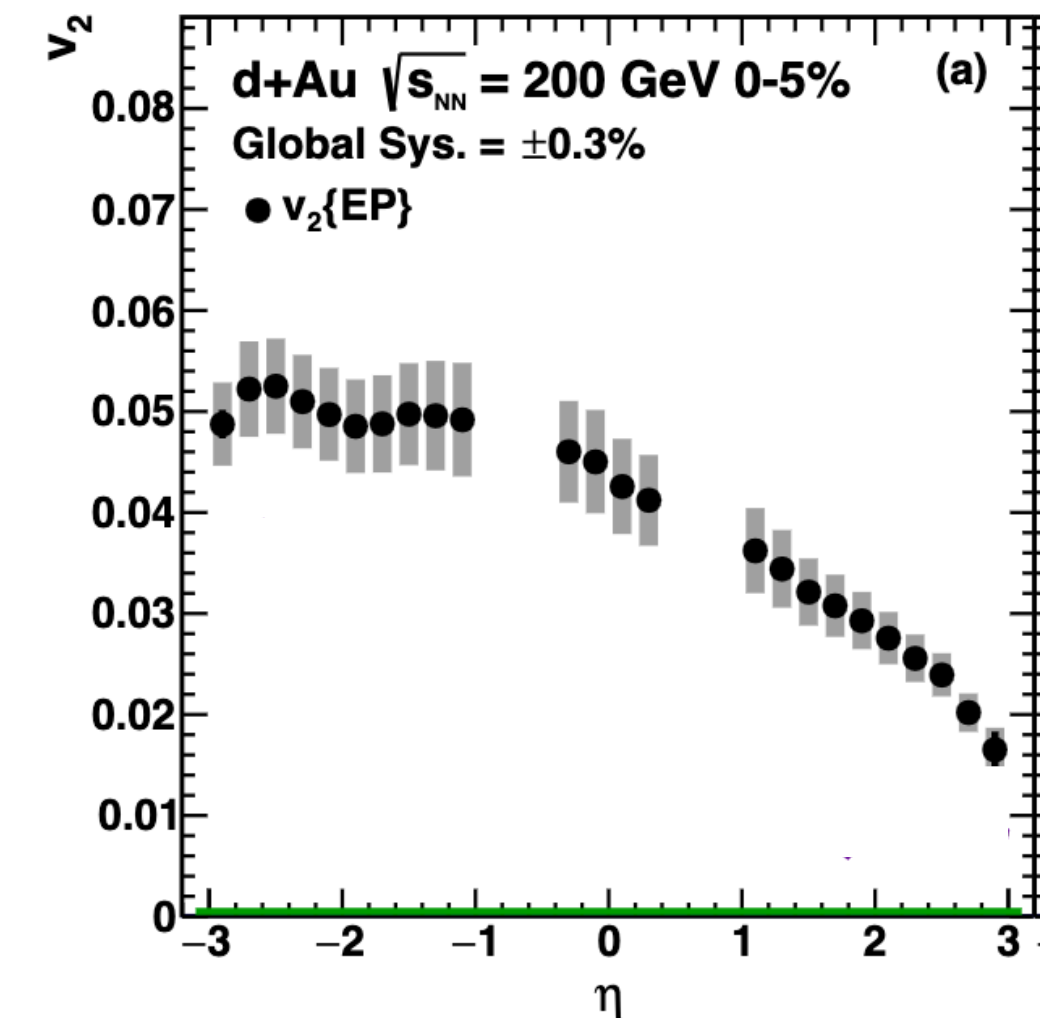
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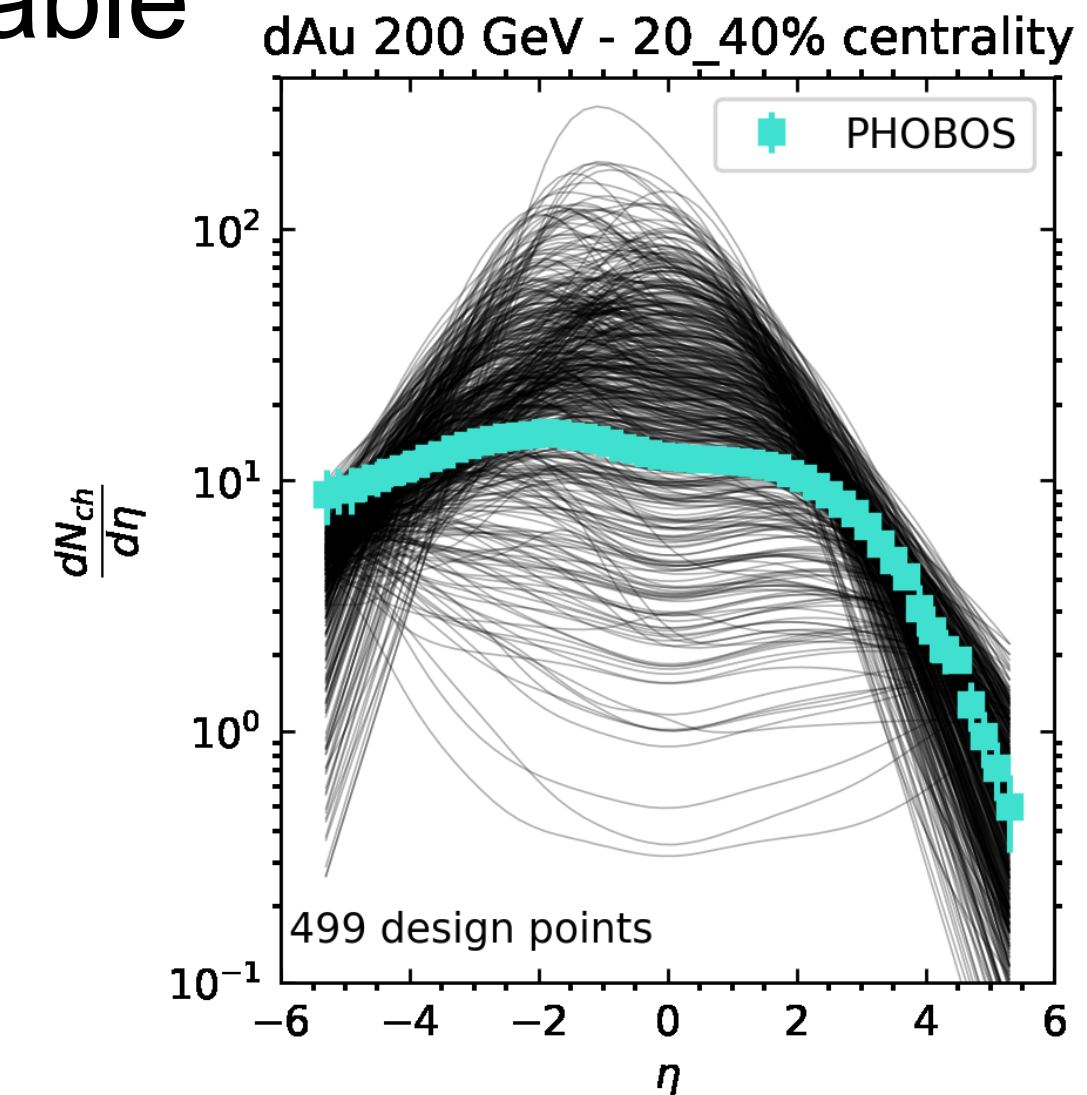
**A 3D model in a Bayesian analysis can utilize the wealth of our experimental knowledge at forward/backward rapidities**



# Constraining QGP Models: Bayesian Analyses

Observable  
Prior

$$\underset{\substack{\uparrow \\ \text{Posterior}}}{P(\vec{\theta}|\vec{x})} \propto \underset{\substack{\uparrow \\ \text{Parameter prior}}}{P(\vec{\theta})} \underset{\substack{\uparrow \\ \text{Likelihood of the parameters given the data}}}{P(\vec{x}|\vec{\theta})}$$

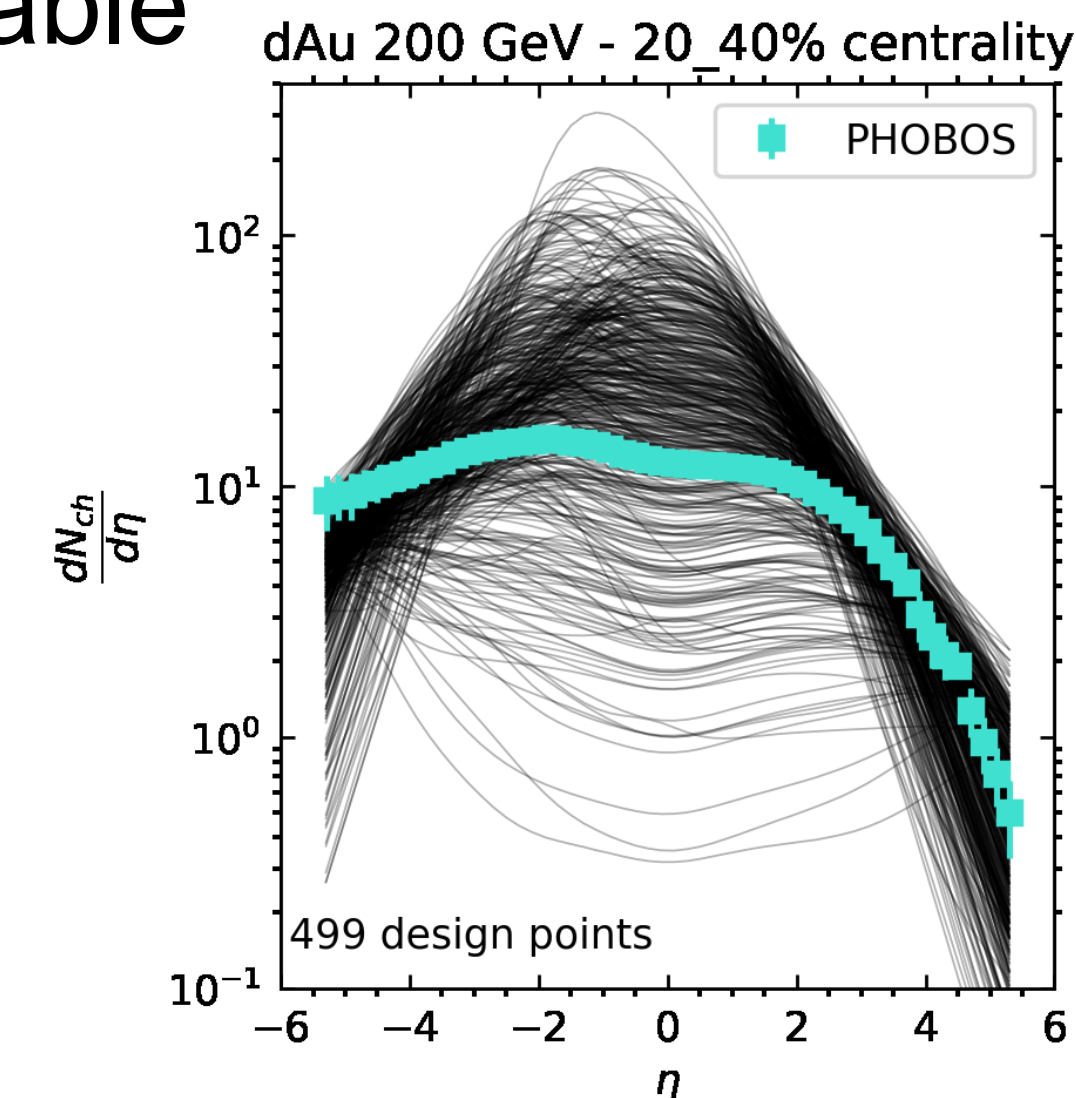


We gain new insight by:

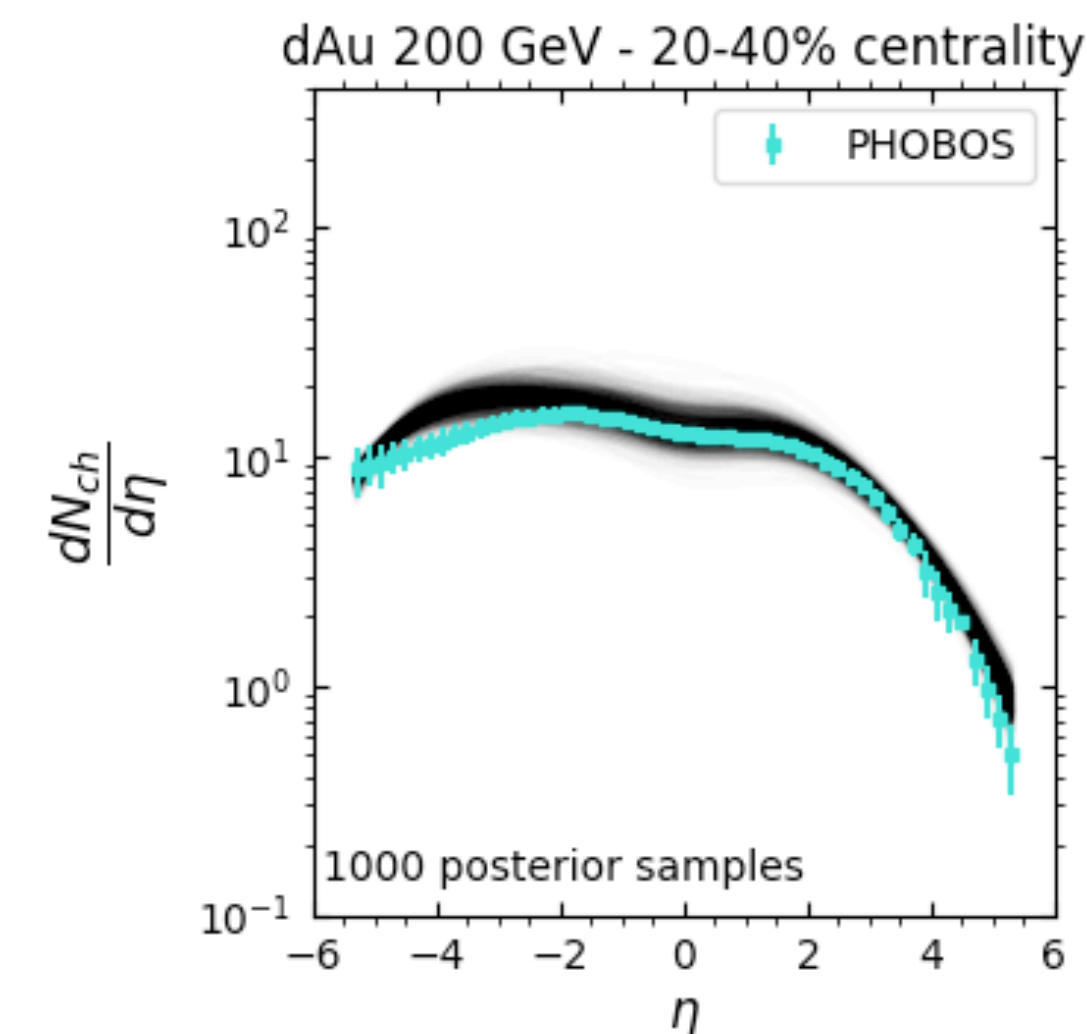
- Taking more (precise) measurements
- Calibrating new models that can describe previously measured data

# Constraining QGP Models: Bayesian Analyses

Observable  
Prior



Observable  
Posterior



Likelihood of the  
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$$P(\vec{\theta} | \vec{x}) \propto P(\vec{x} | \vec{\theta}) P(\vec{\theta})$$

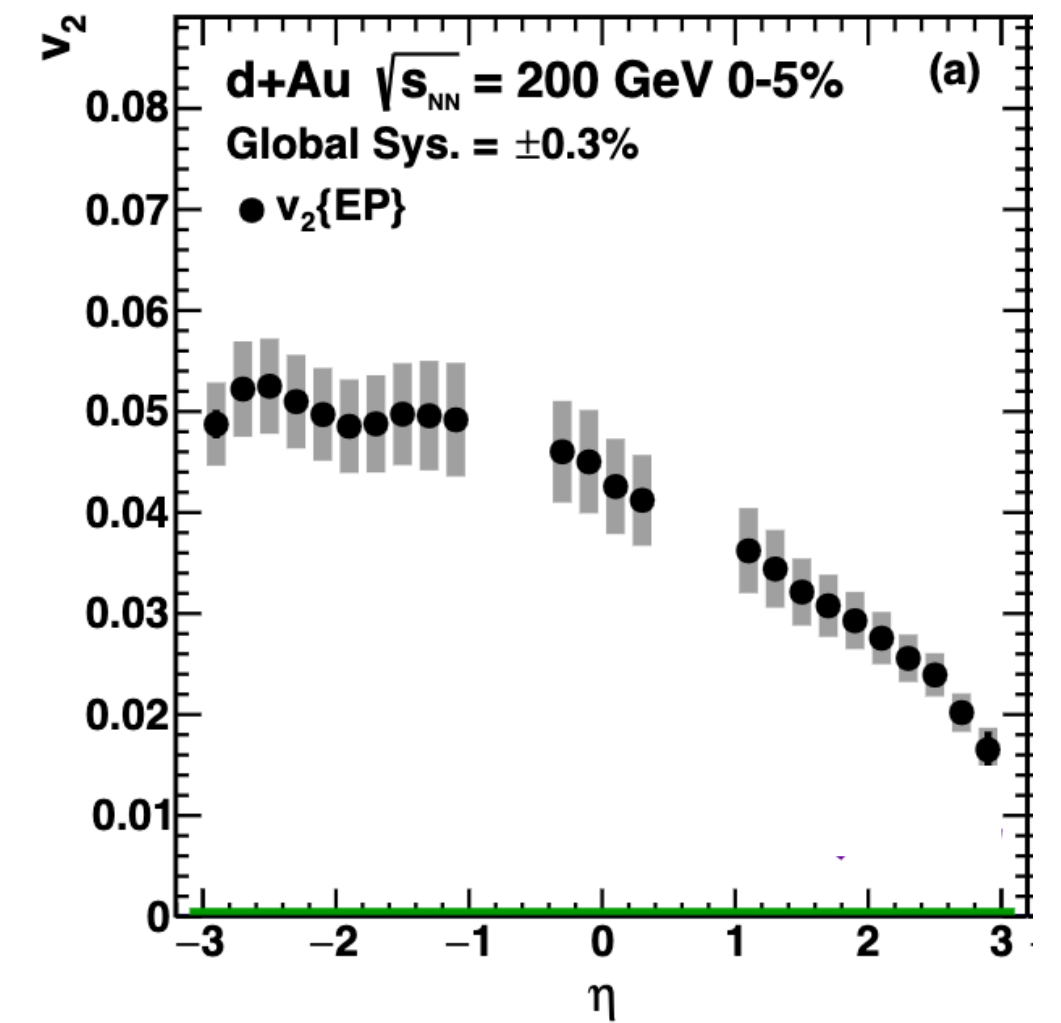
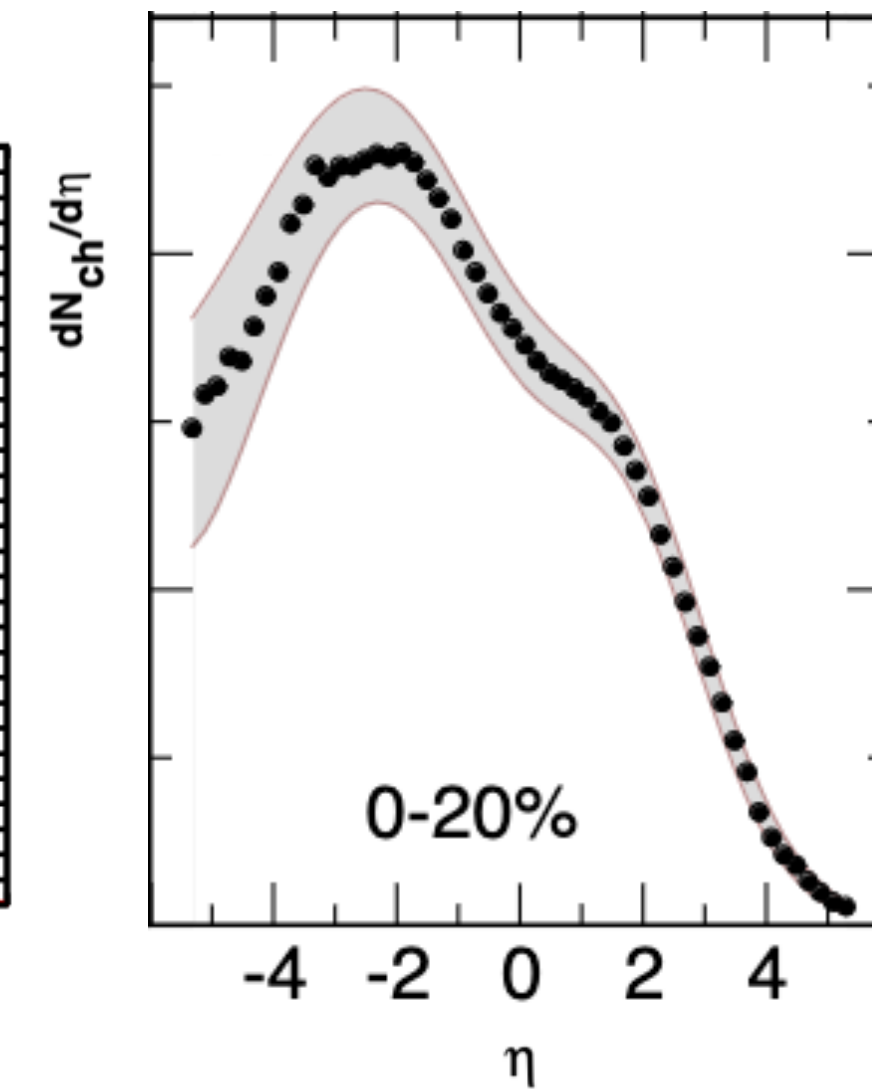
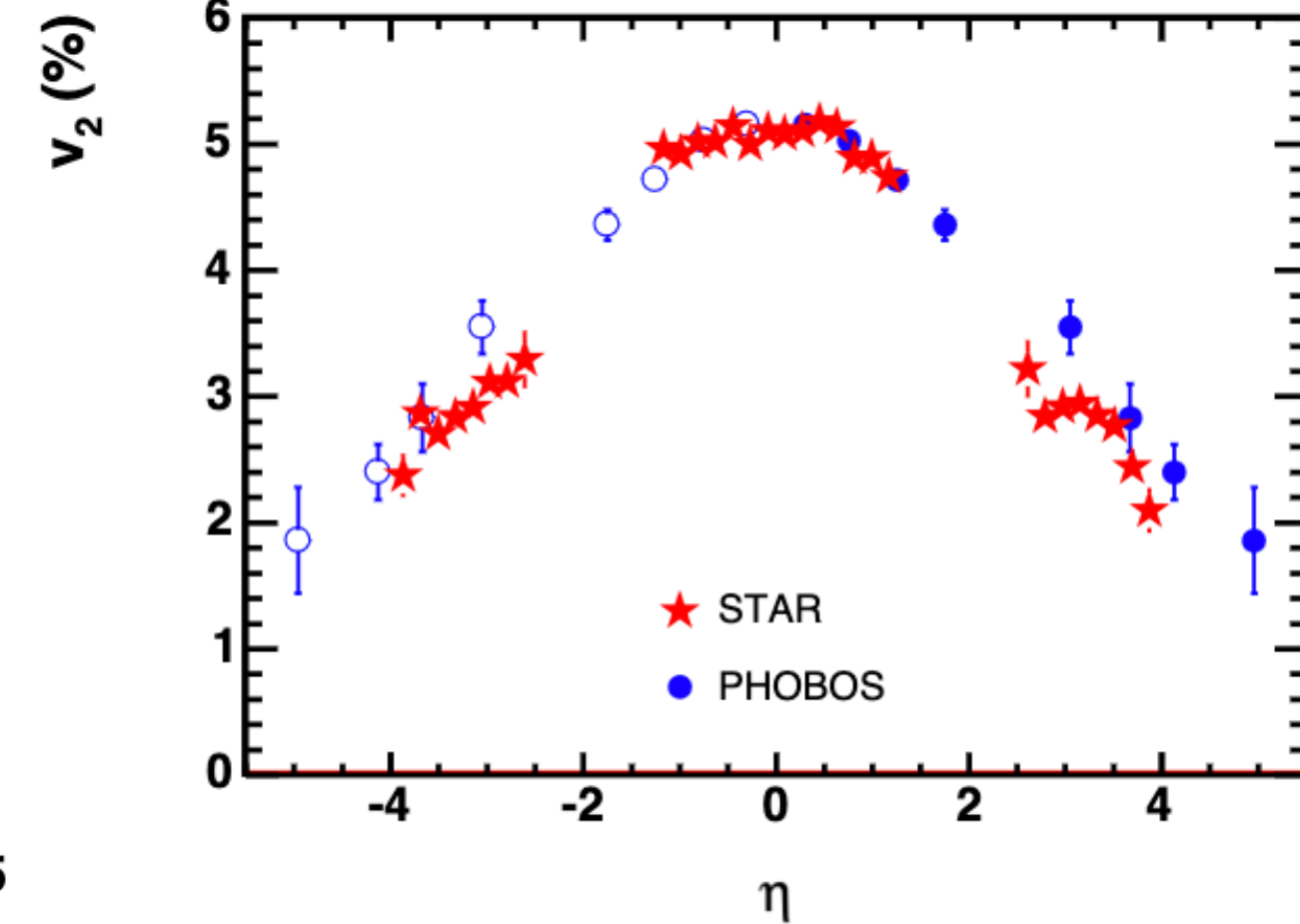
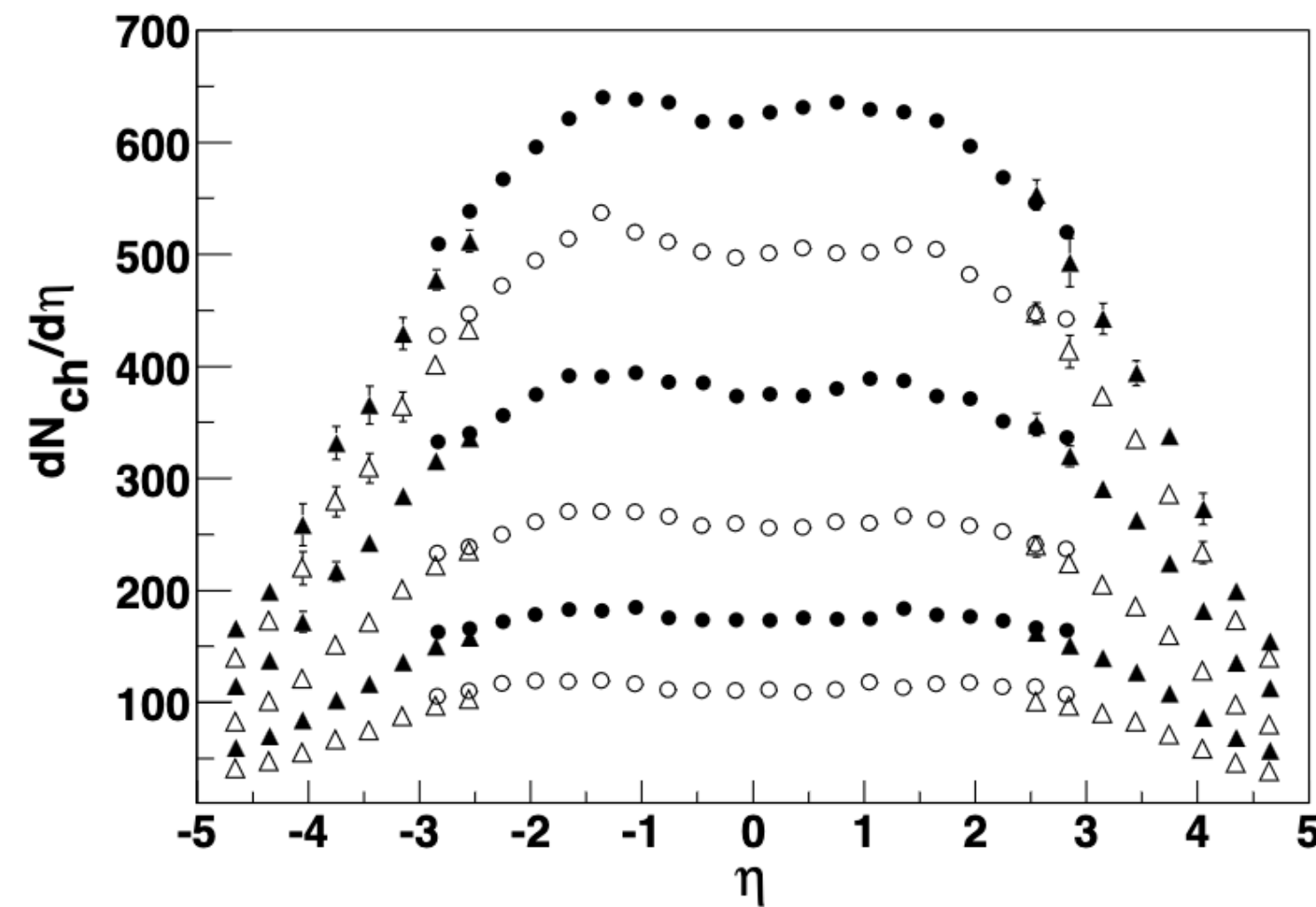
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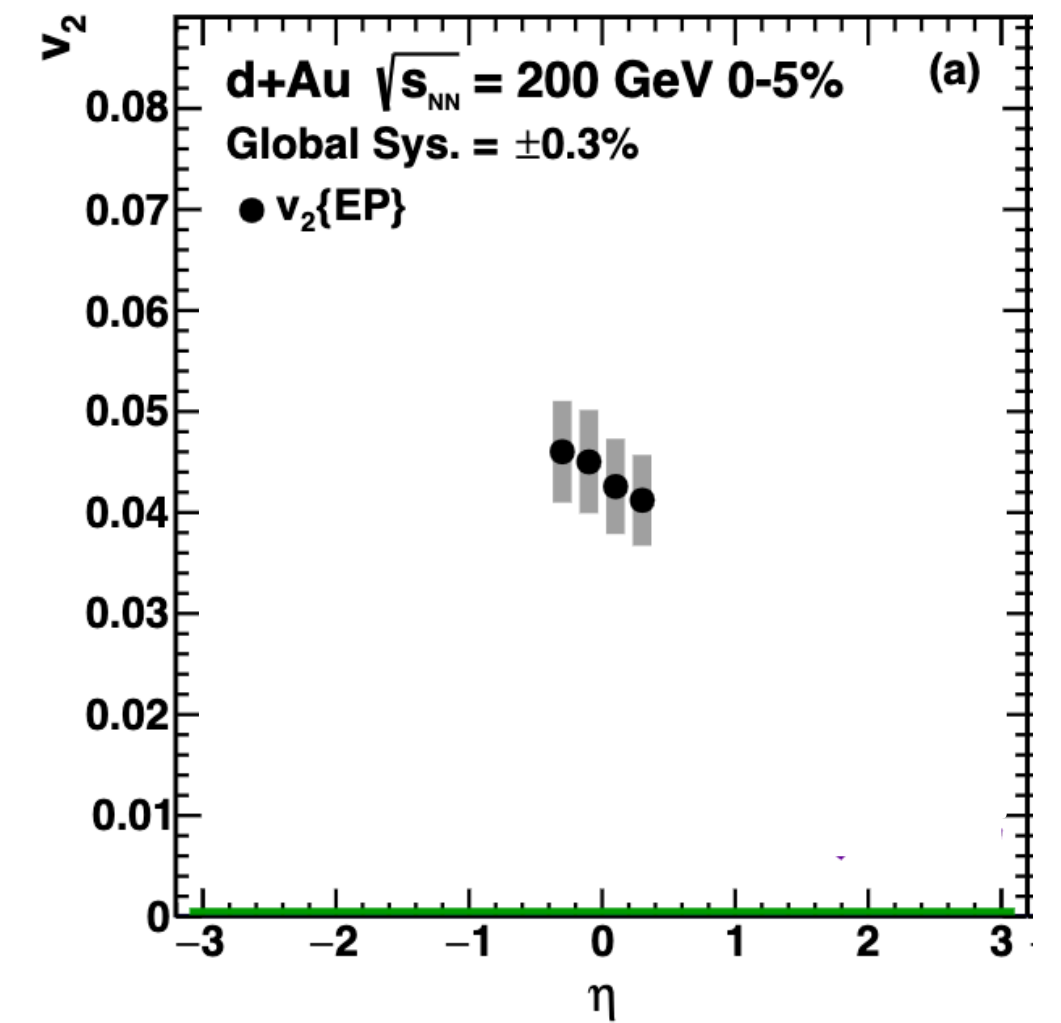
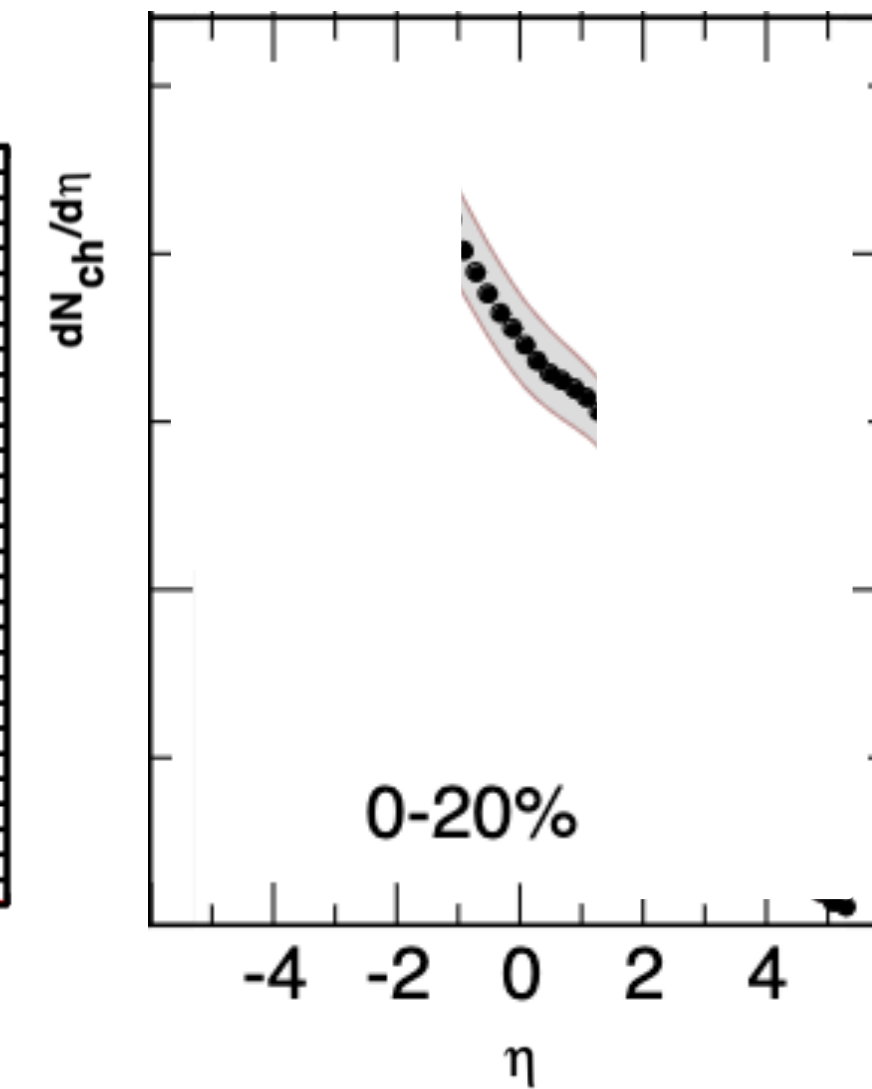
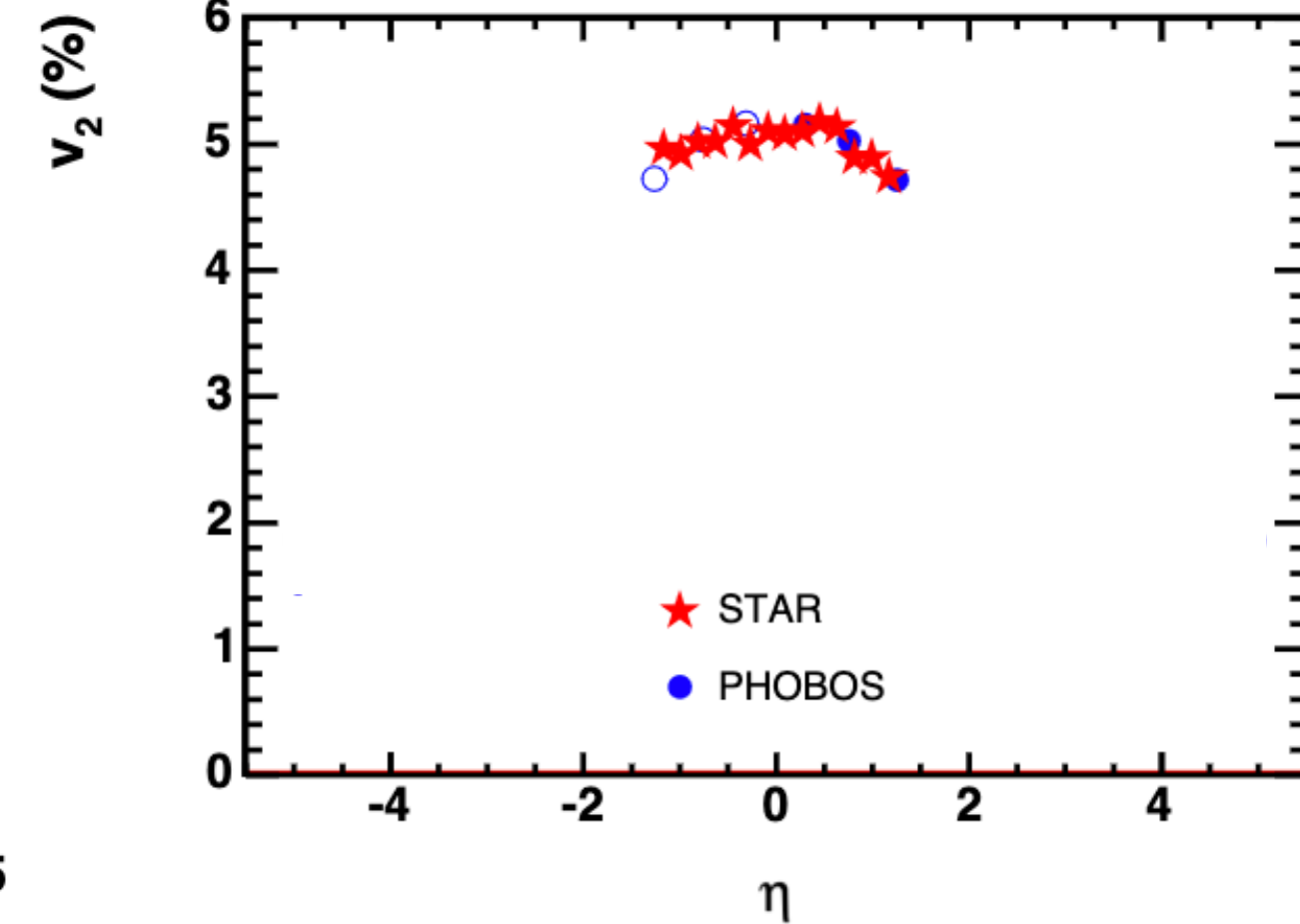
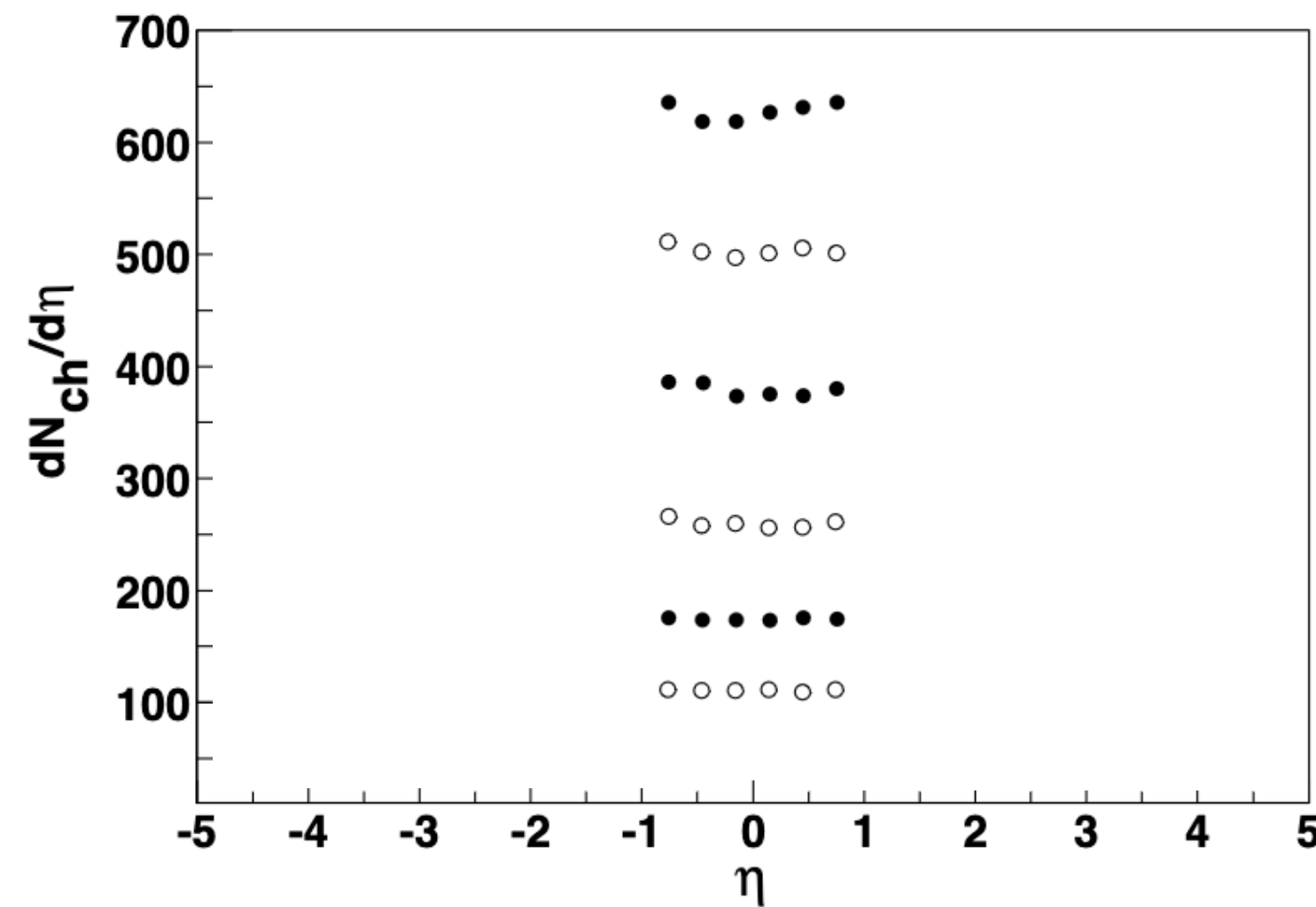
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# 3D Model Constrained on Data at Mid-rapidity



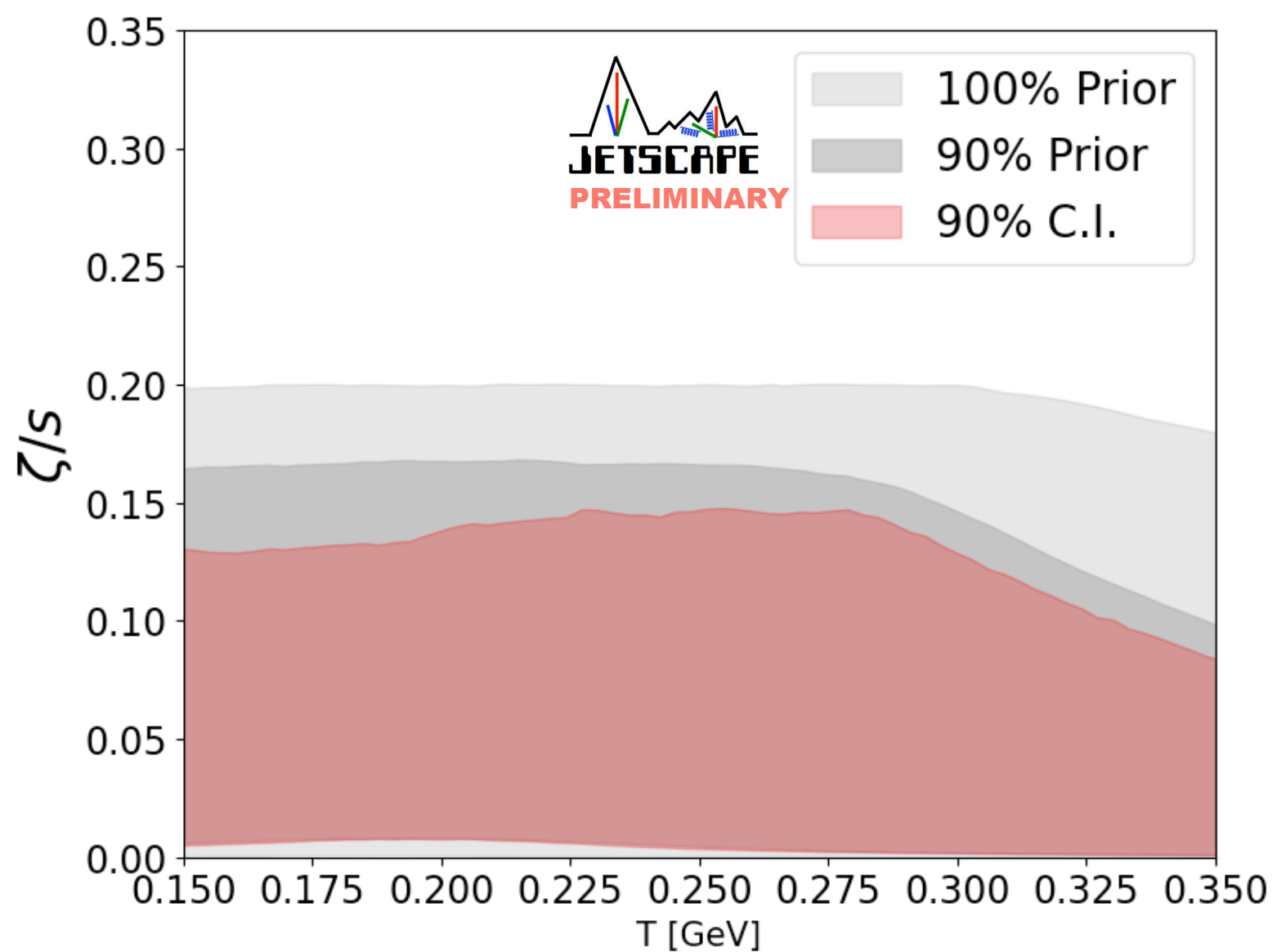
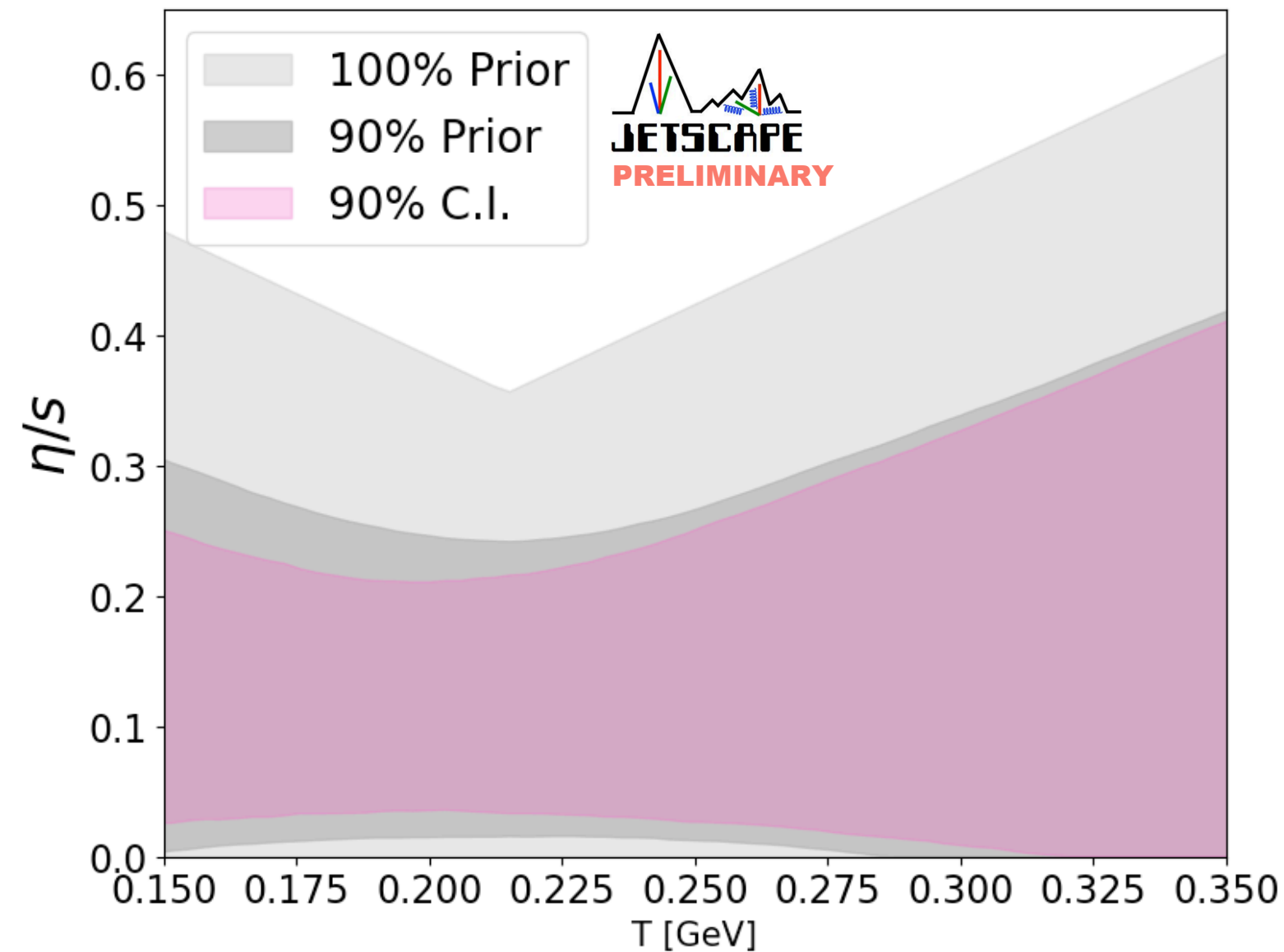


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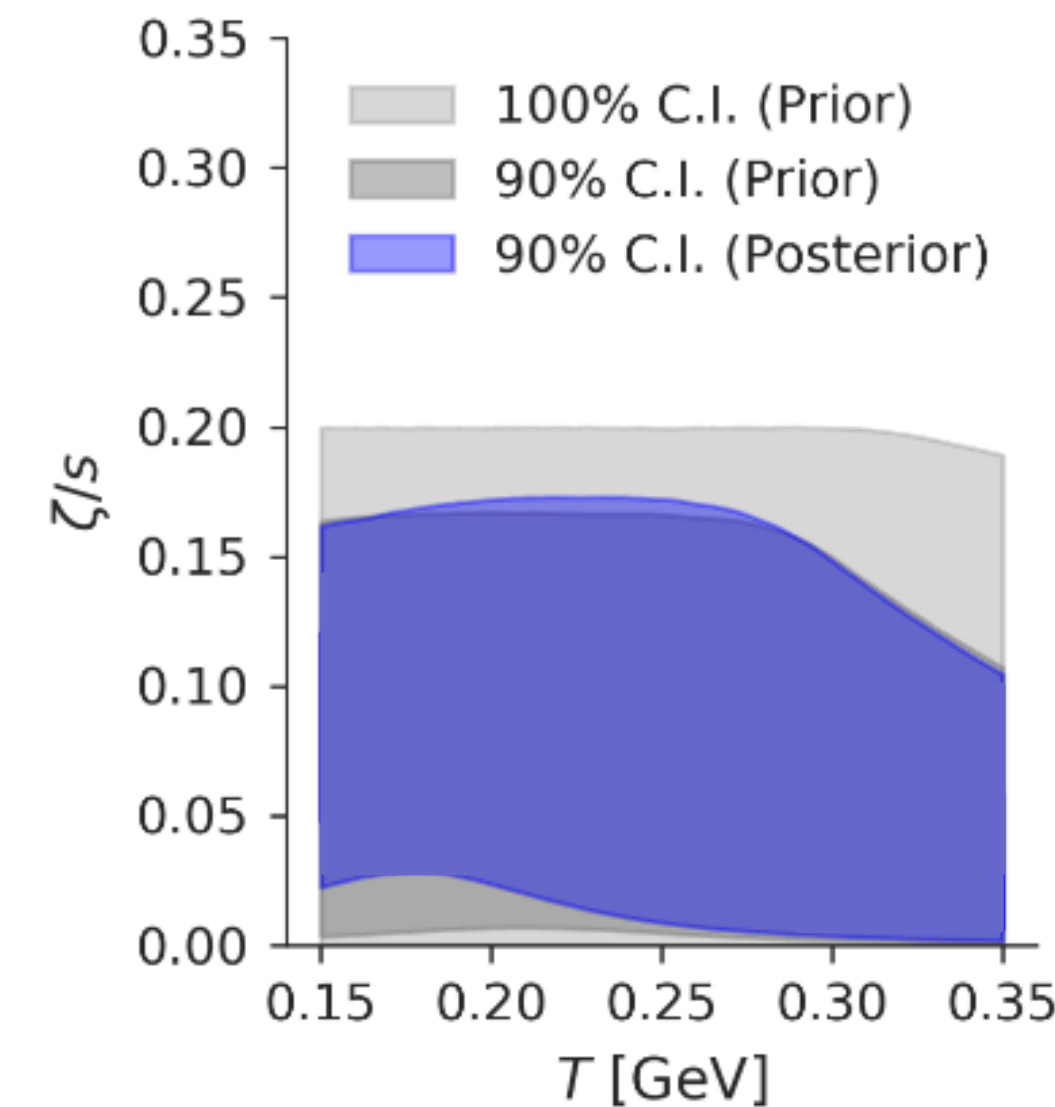
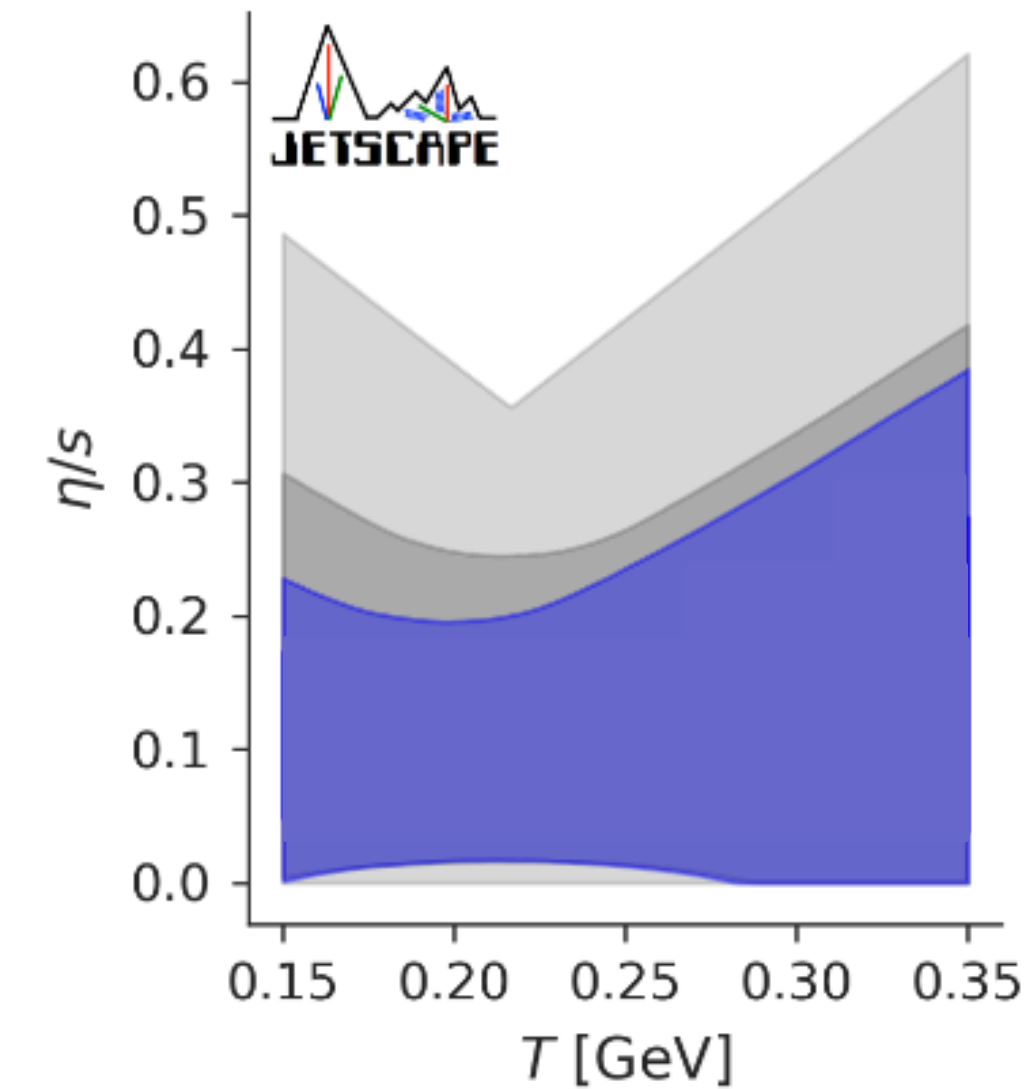
# Constraints using only mid-rapidity measurements

***This analysis***  
using only  
mid-rapidity  
measurements



Consistent  
constraints  
with previous  
analyses

**JETSCAPE 2D  
calibration using  
only RHIC data at  
mid-rapidity**

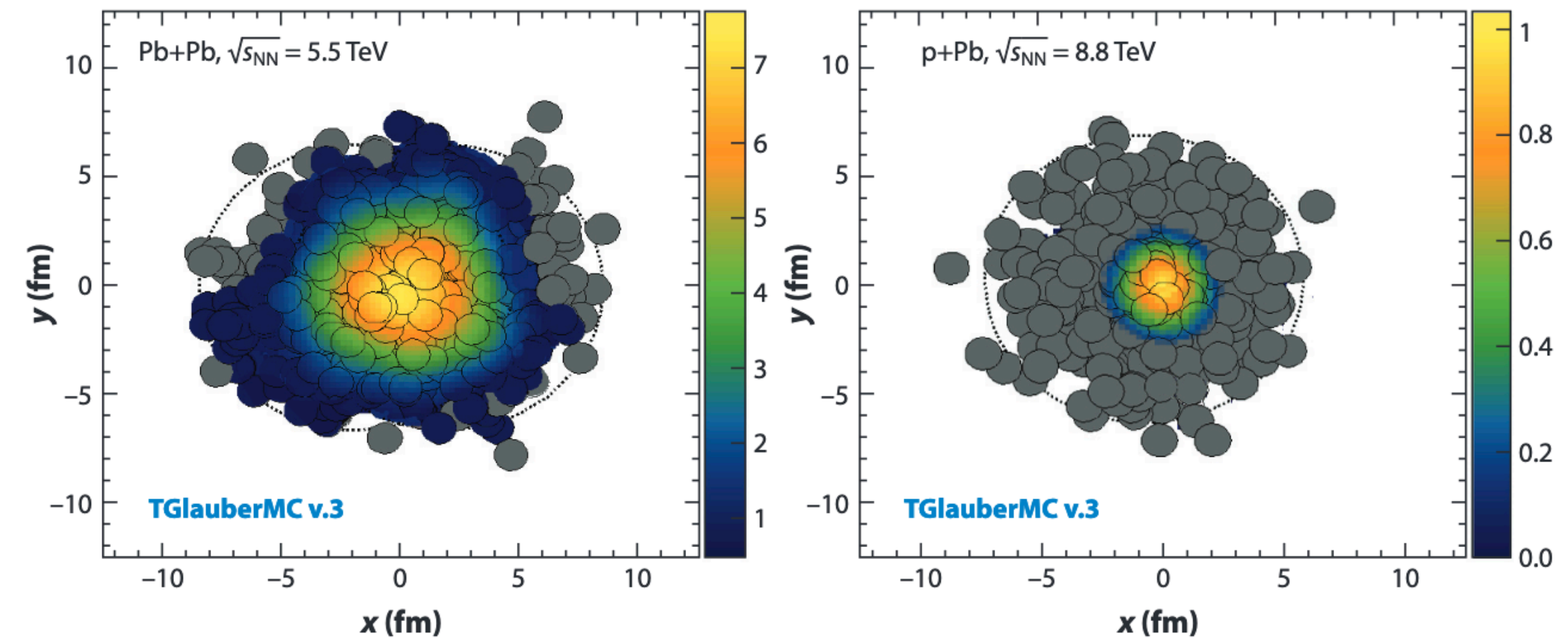


# The Model: 3D Initial State and Hydrodynamics

- 3D Monte Carlo Glauber Model
- Valence quark hot spots
- Energy deposited along the decelerating string connecting two colliding participants
- Collision-by-collision fluctuating rapidity loss

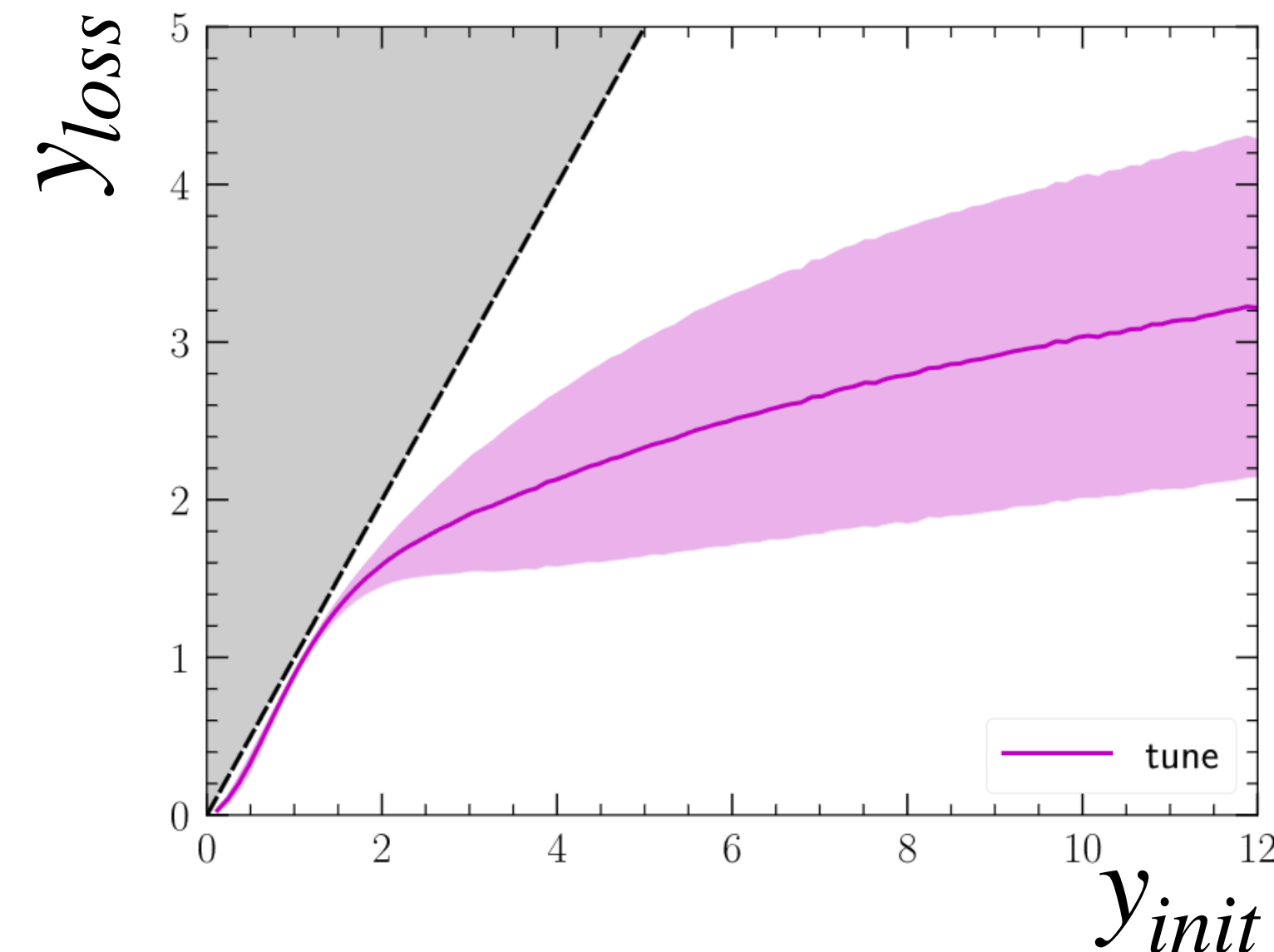
See talks by B. Schenke and Chun Shen 9/5 !

## 2D Glauber density profiles



Ann. Rev. Nucl. Part. Sci. 57 (2007)

## Parametrization of rapidity loss function



Schenke, Shen, Zhao.

Phys. Rev. C 105, 064905  
(2022)

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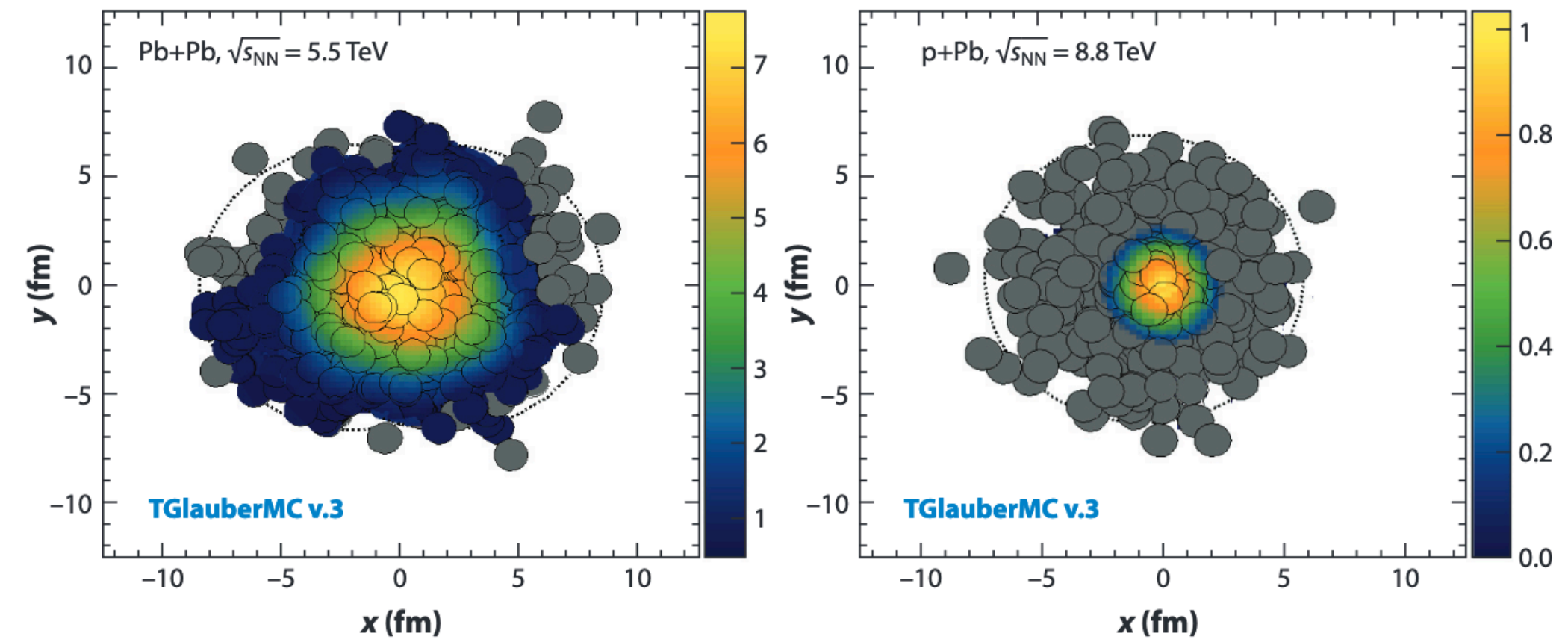


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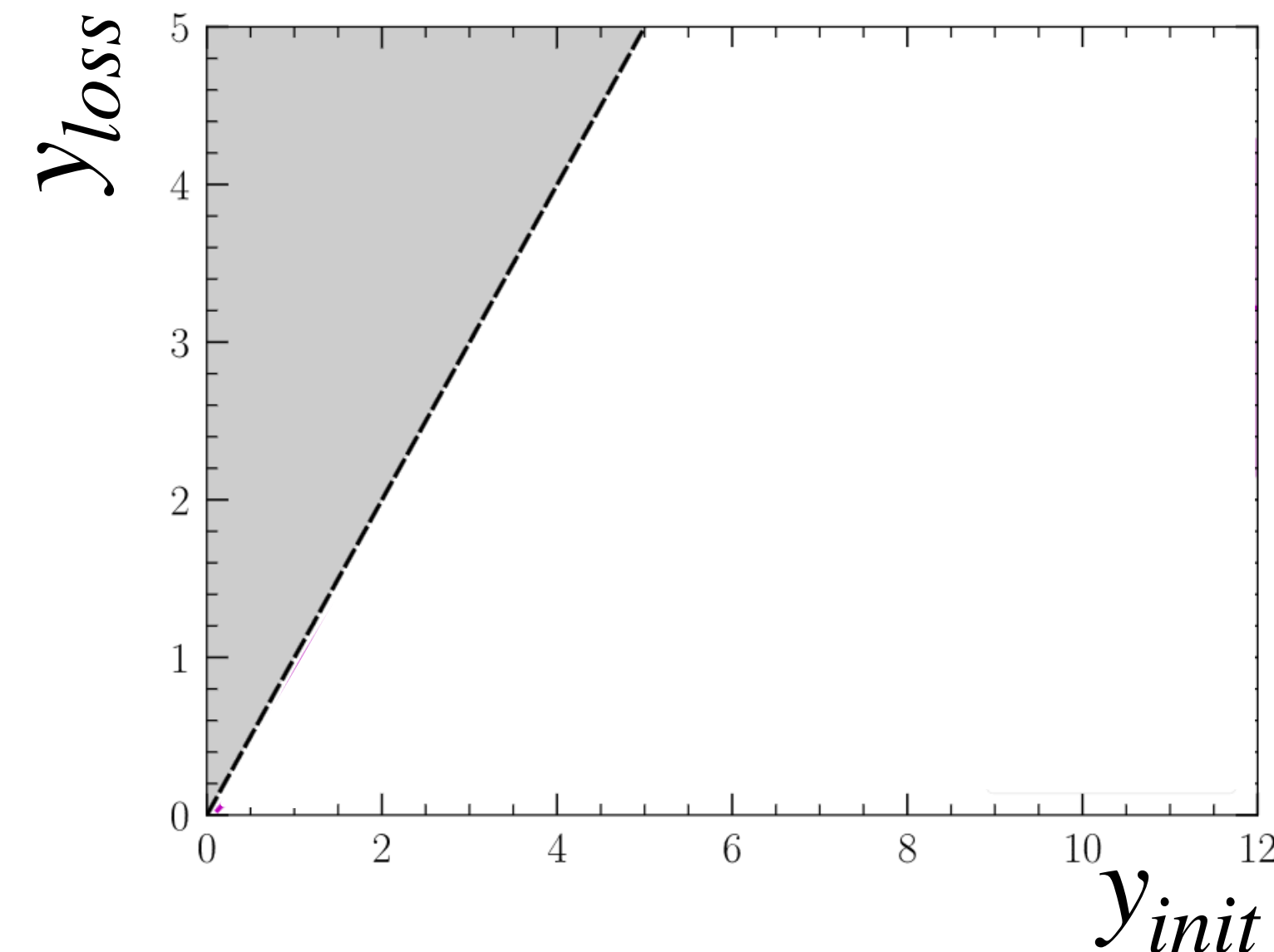
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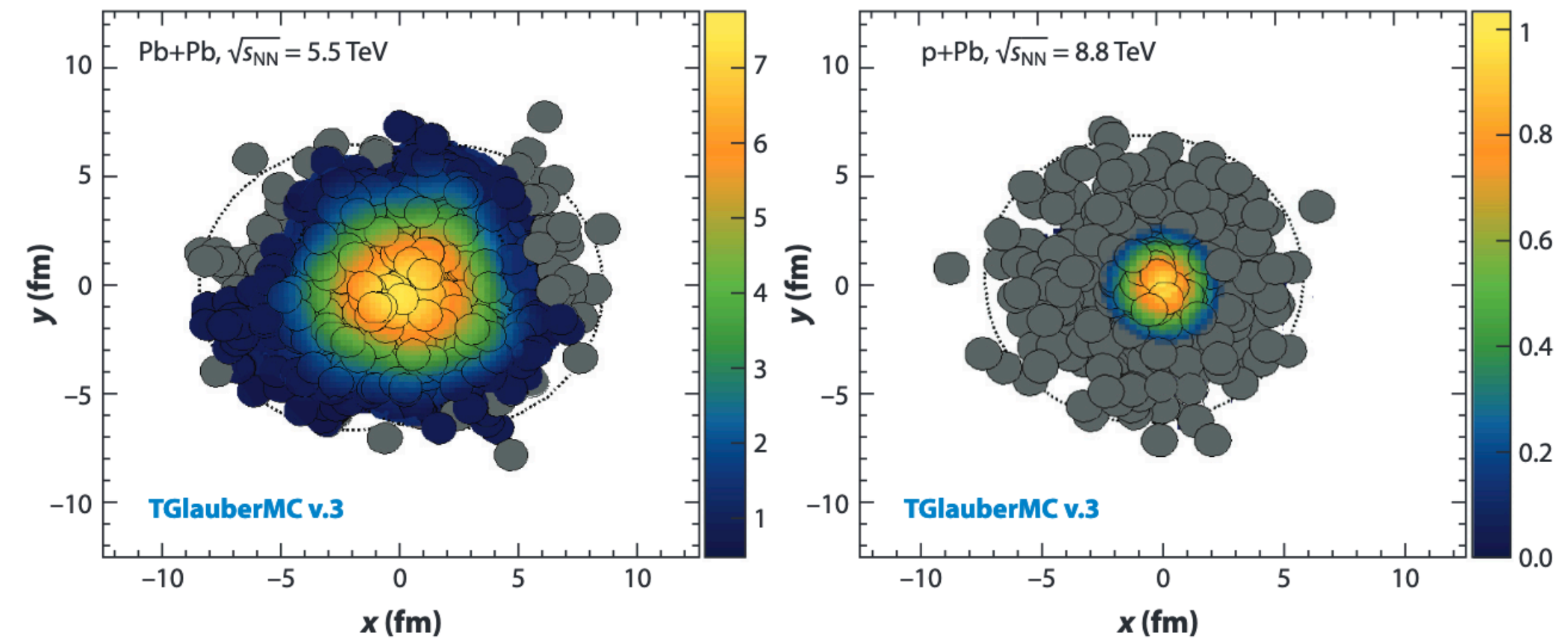
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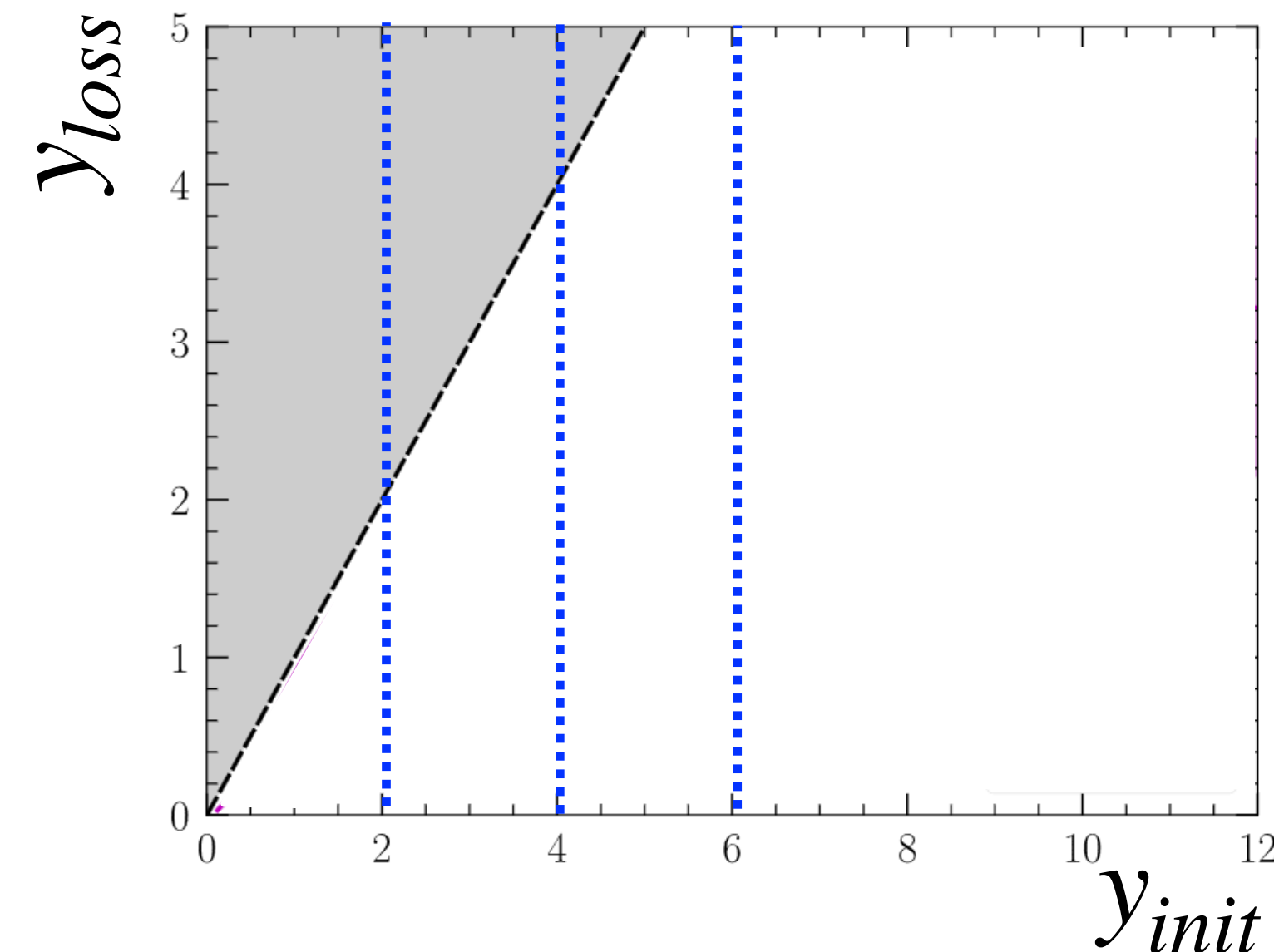
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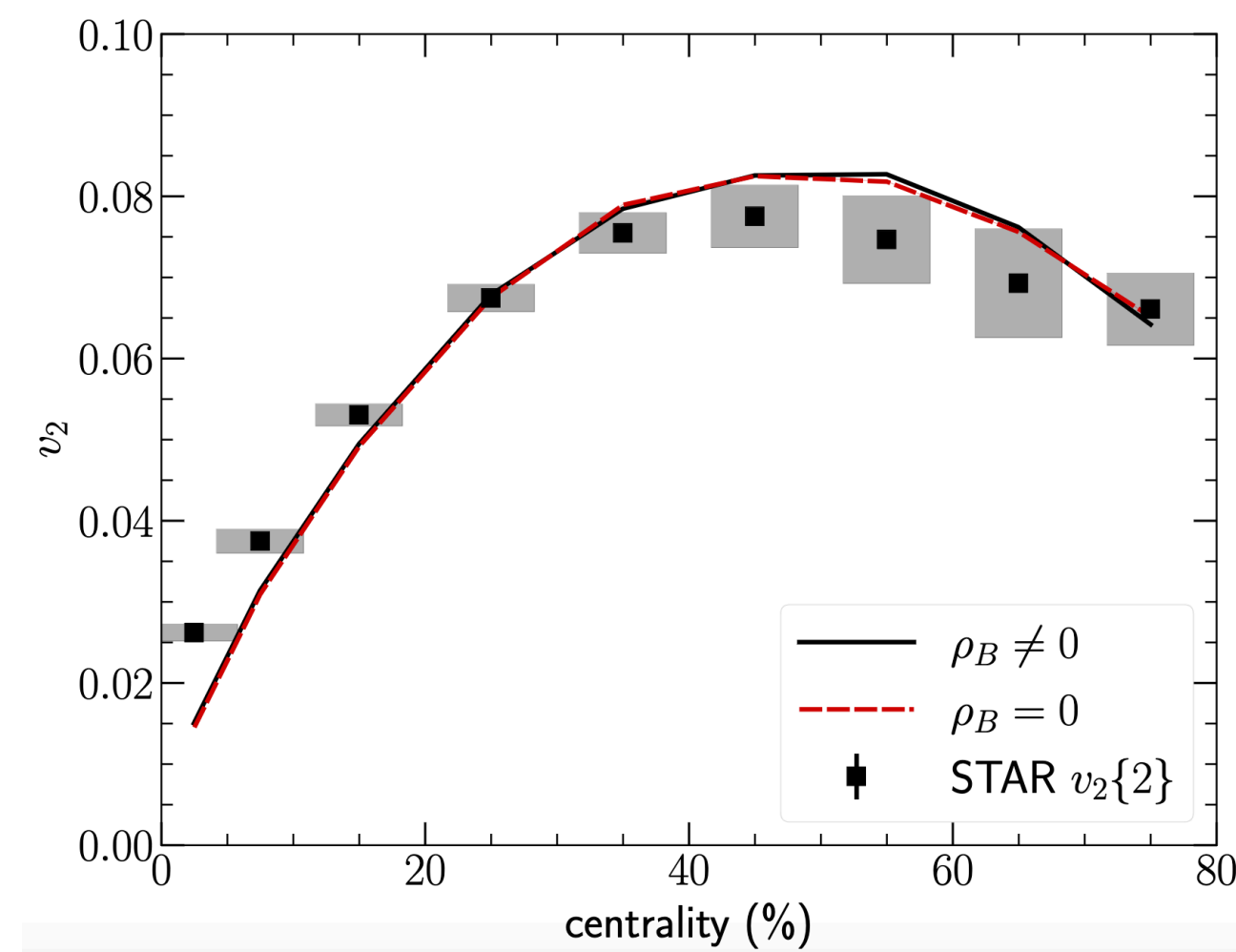
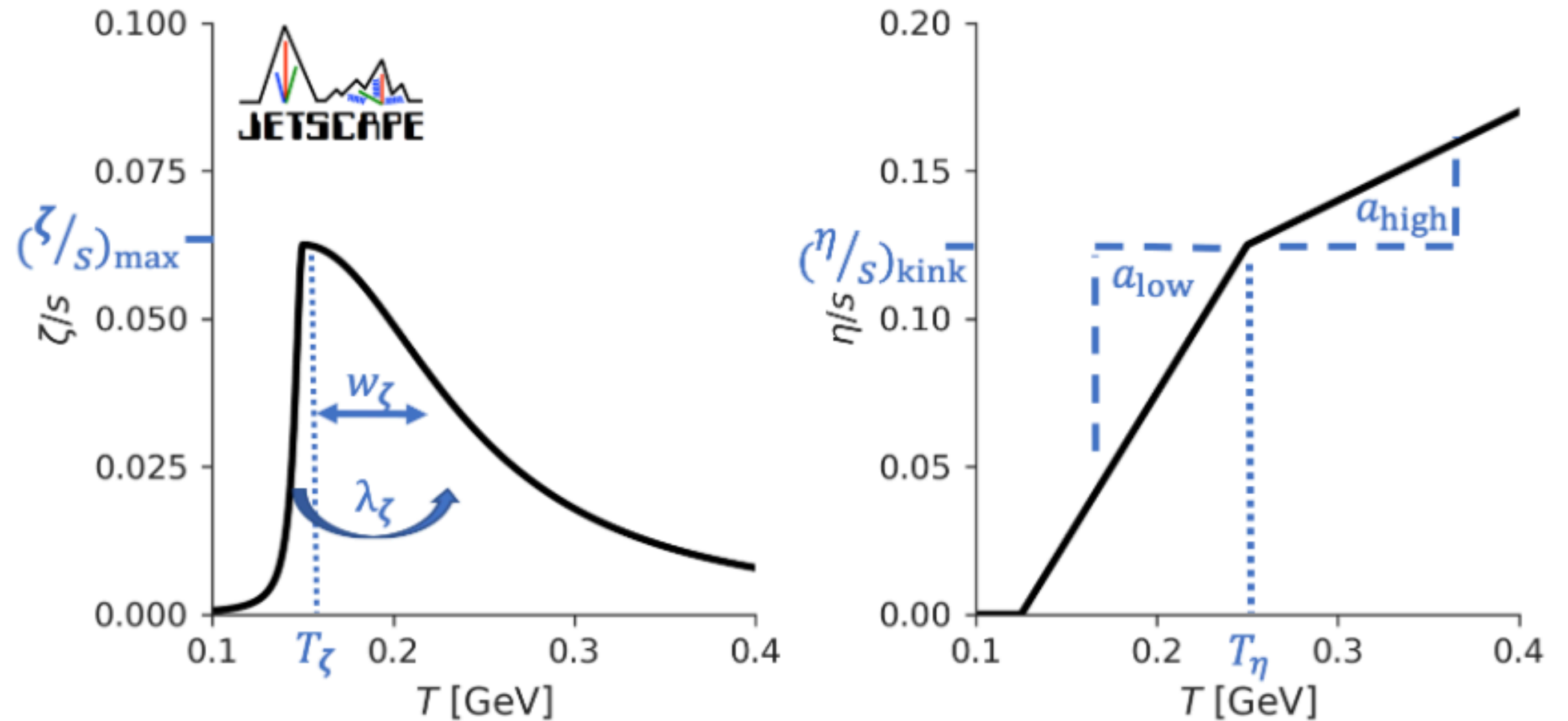
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# The Model: Hydrodynamics and Hadronic Transport

- (3+1)D Viscous Hydrodynamics
  - Shear and bulk viscosities parametrized as in previous JETSCAPE analyses
- Grad viscous corrections model
- UrQMD to perform hadronic scatterings and decays
- Take  $\rho_b = 0$  (effect on  $v_2$  negligible)

Parametrization of viscosity







Ref: Chun Shen



# Model Calculations and the Analysis

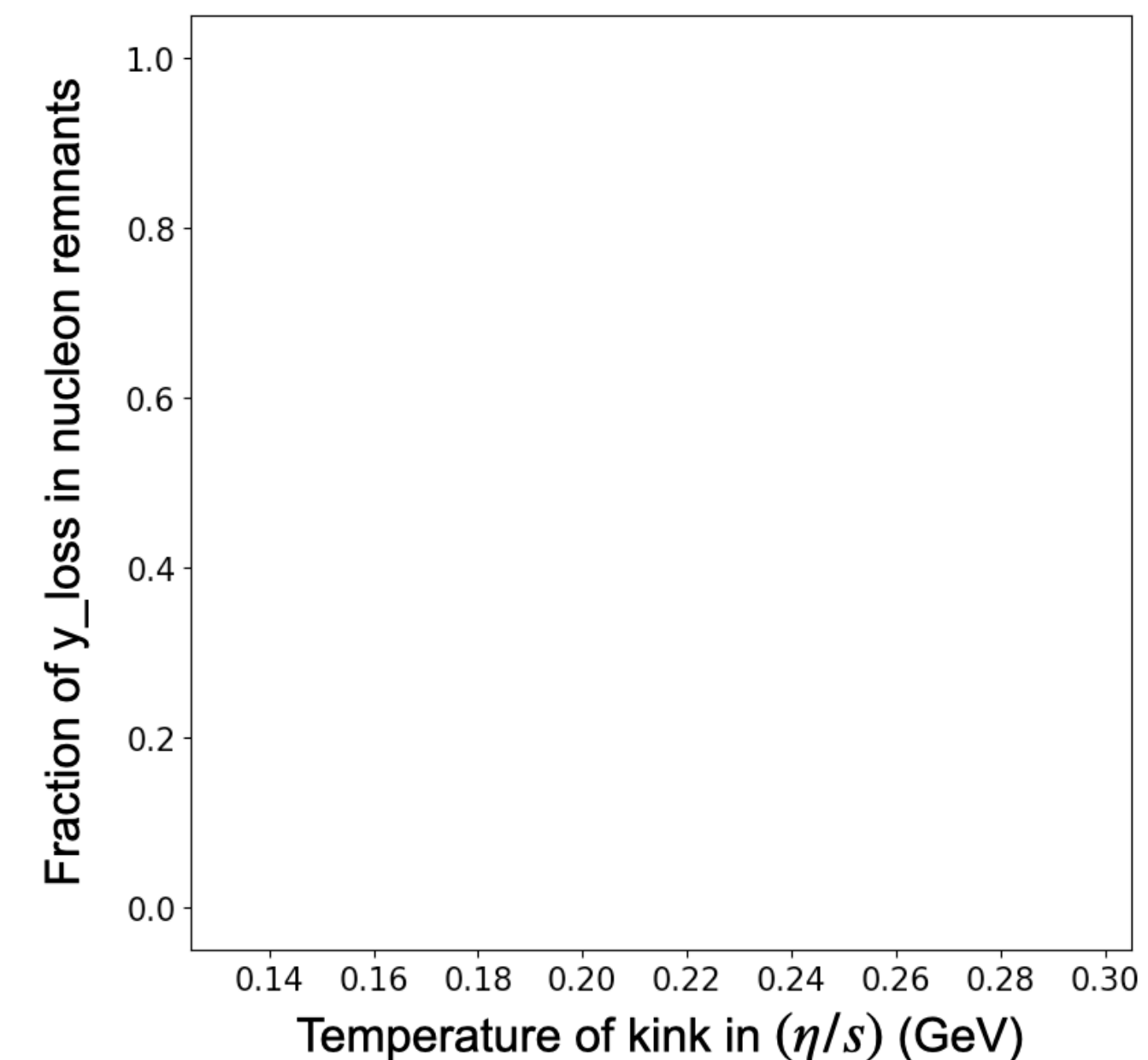
- Used the following experimental data from RHIC collisions at 200 GeV:

	<i>AuAu</i>	<i>dAu</i>
$dN_{ch}/d\eta$		
$v_2$		

- Ran simulations across multiple HPC centers through ACCESS (NSF)
- Multivariate-normal distribution used as likelihood function

- Trained a Gaussian process emulator to interpolate between design points:

Sample 2D parameter space (500 design points)



$$P(Y_{exp}|\theta) \propto \left( -[Y_{exp} - Y_{sim}(\theta)]^T [\Sigma_{exp} + \Sigma_{sim}(\theta)]^{-1} [Y_{exp} - Y_{sim}(\theta)] \right)$$





Covariance matrix of uncertainties

Difference between prediction and data



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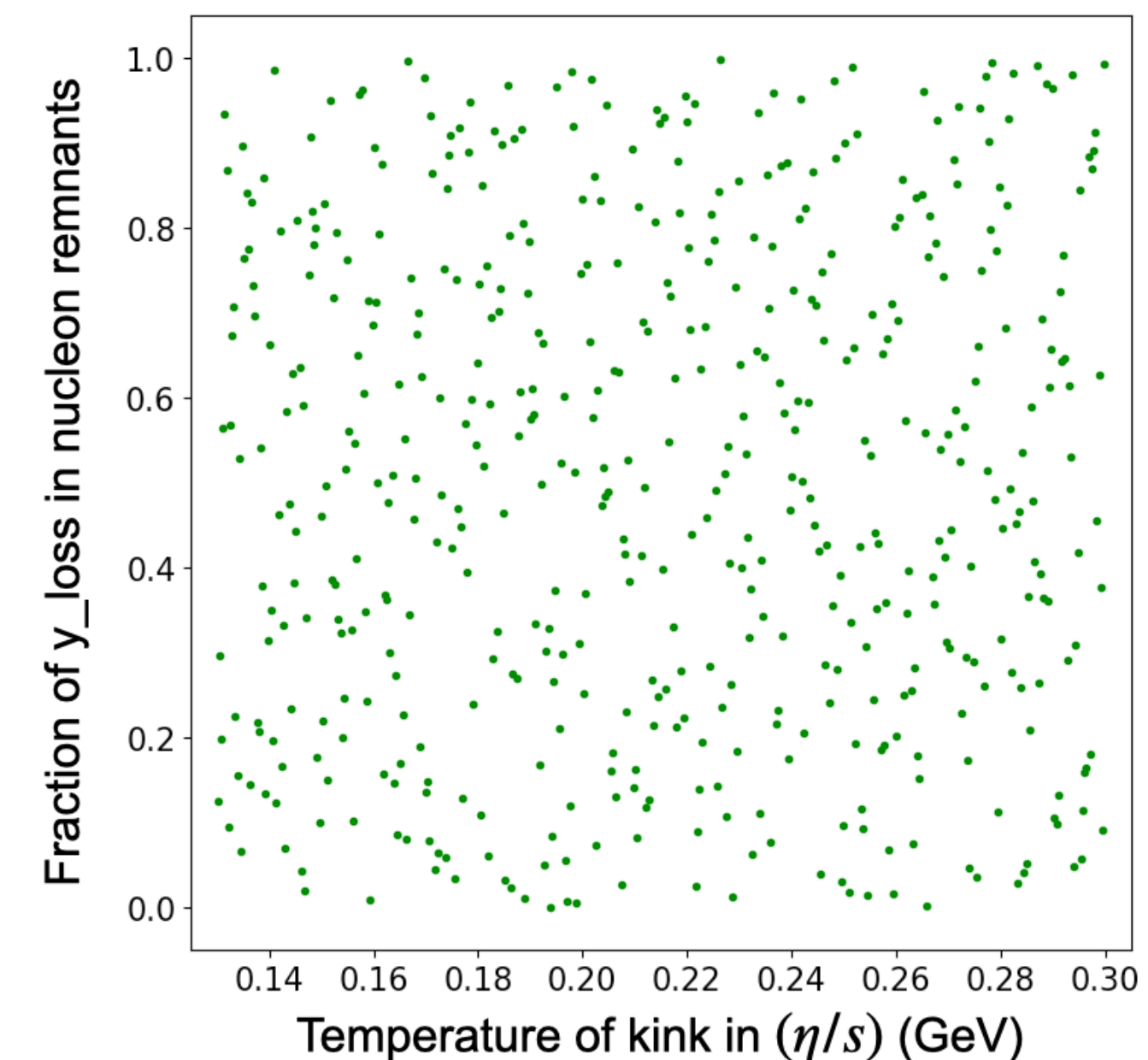
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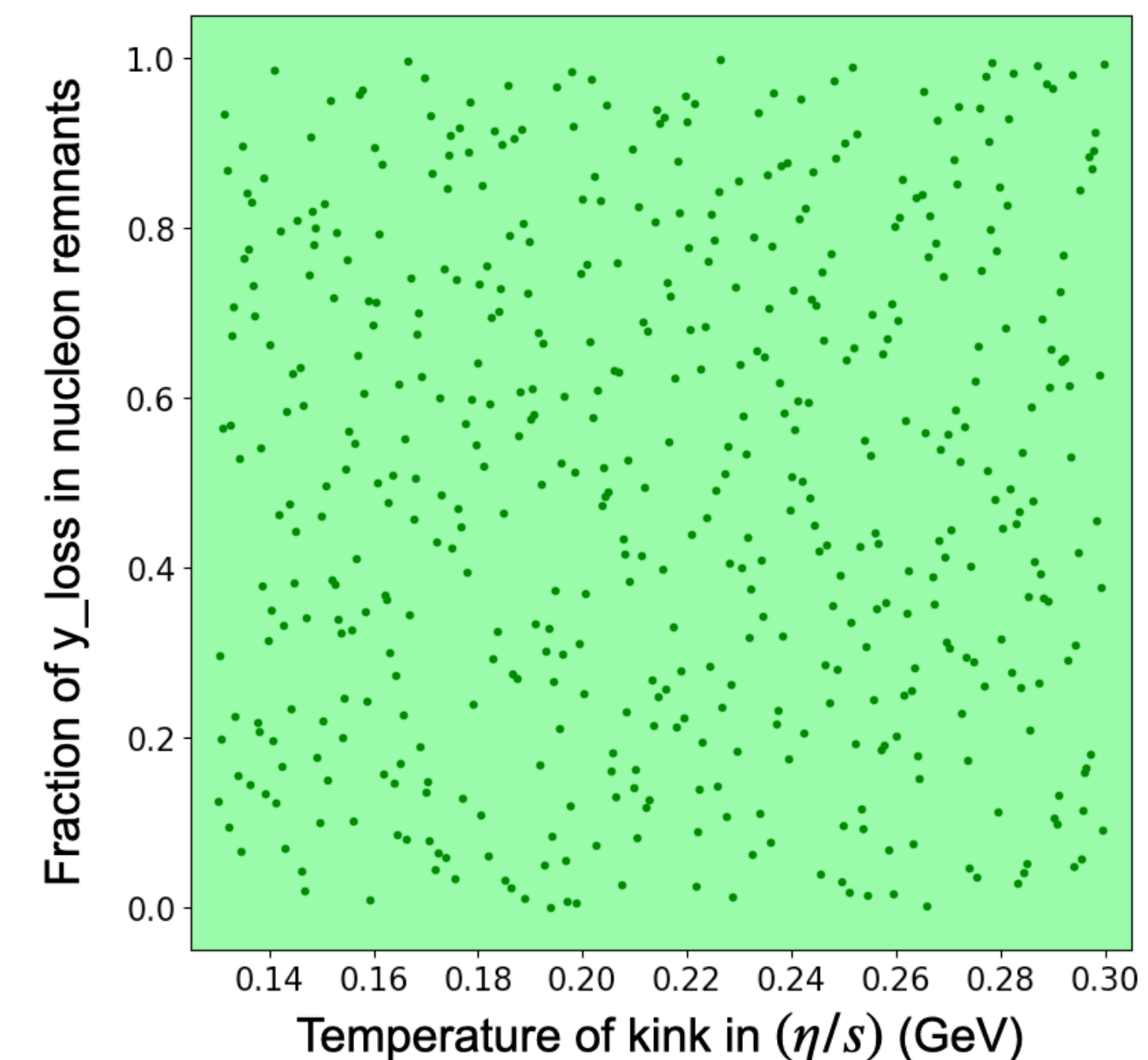
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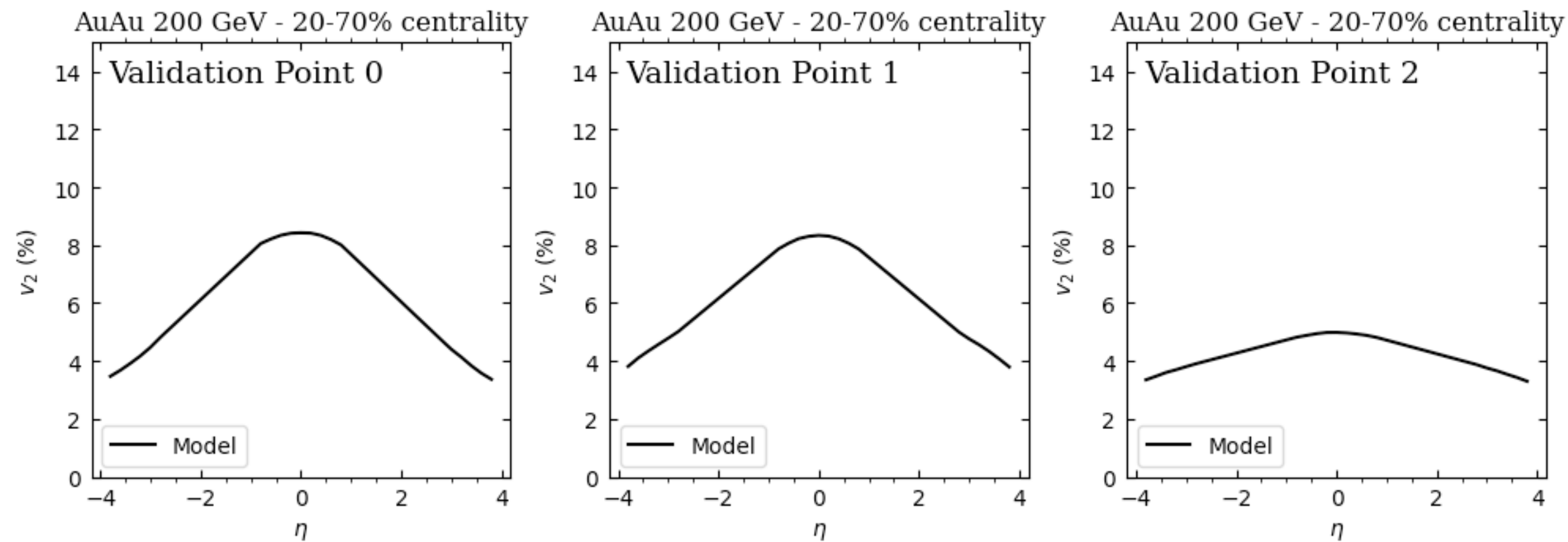
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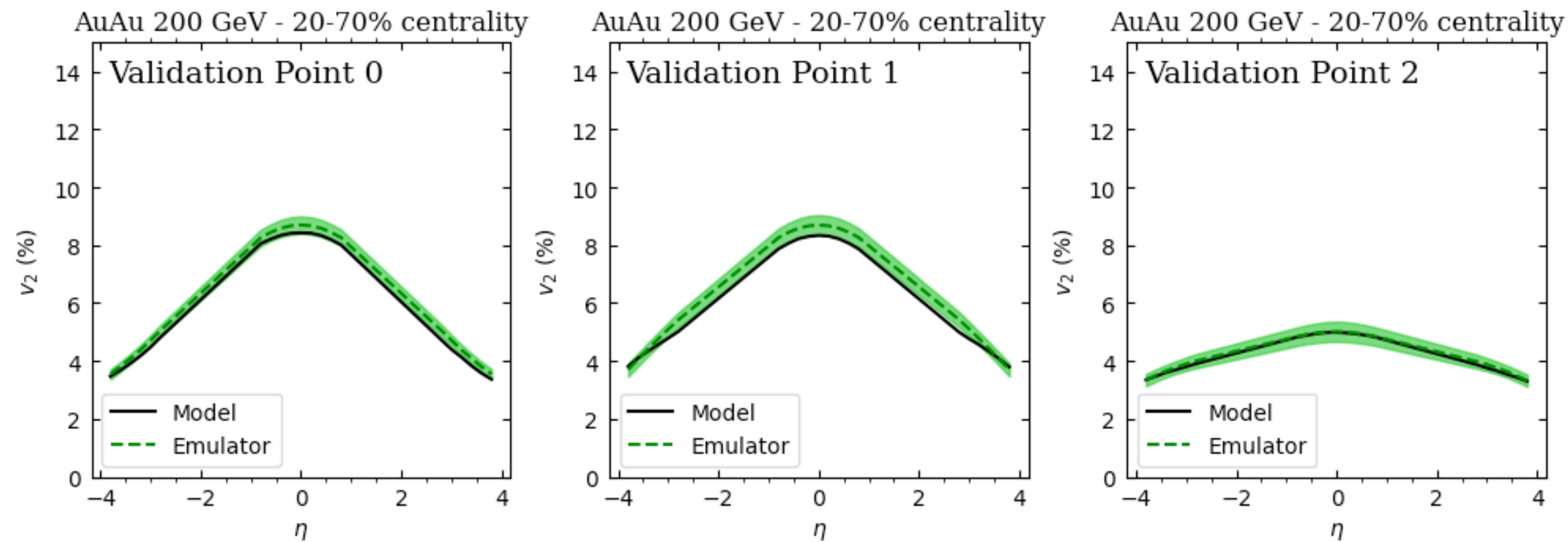
# Emulating the Model and Validating the Analysis

- Gaussian Process Emulator: Fast surrogate for slow model



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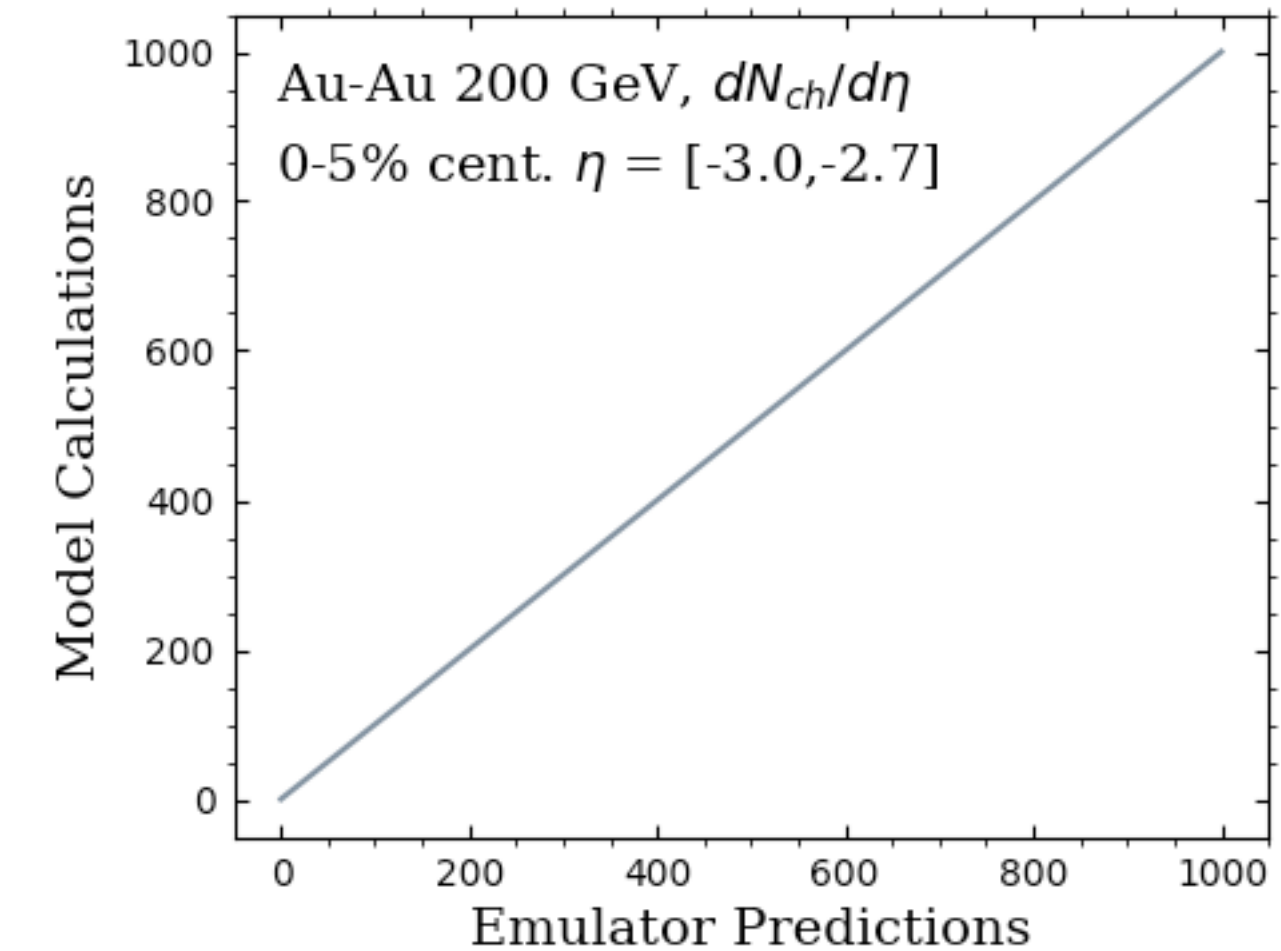
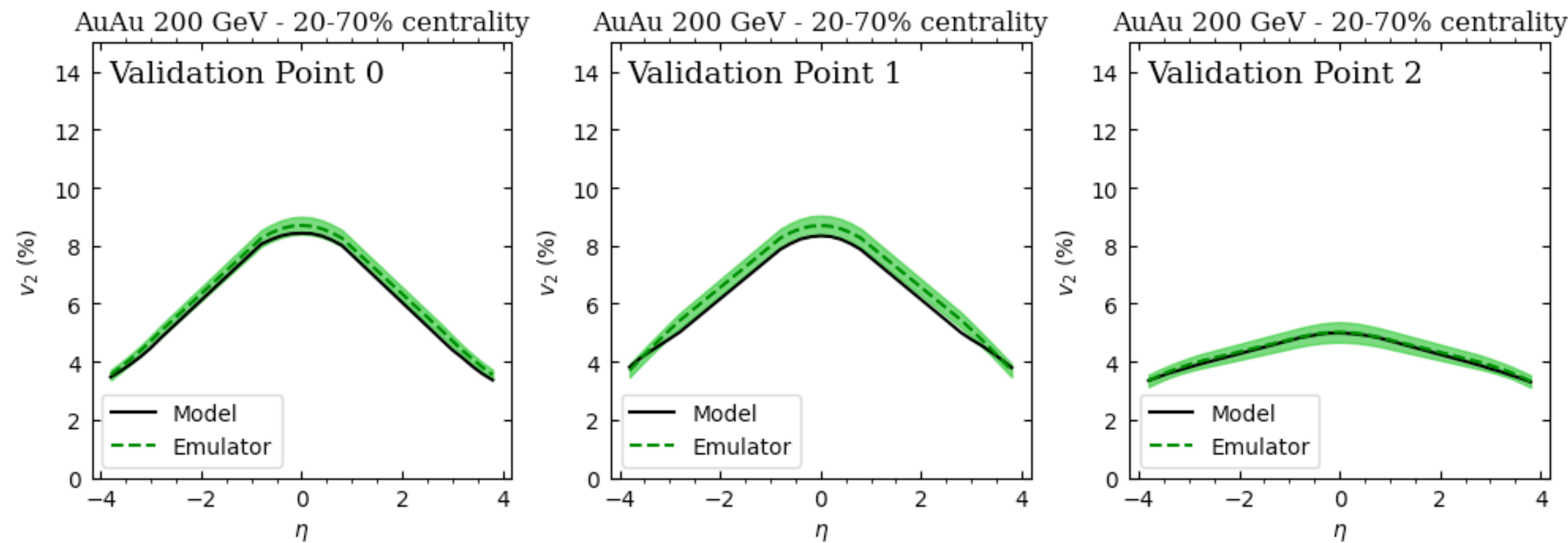
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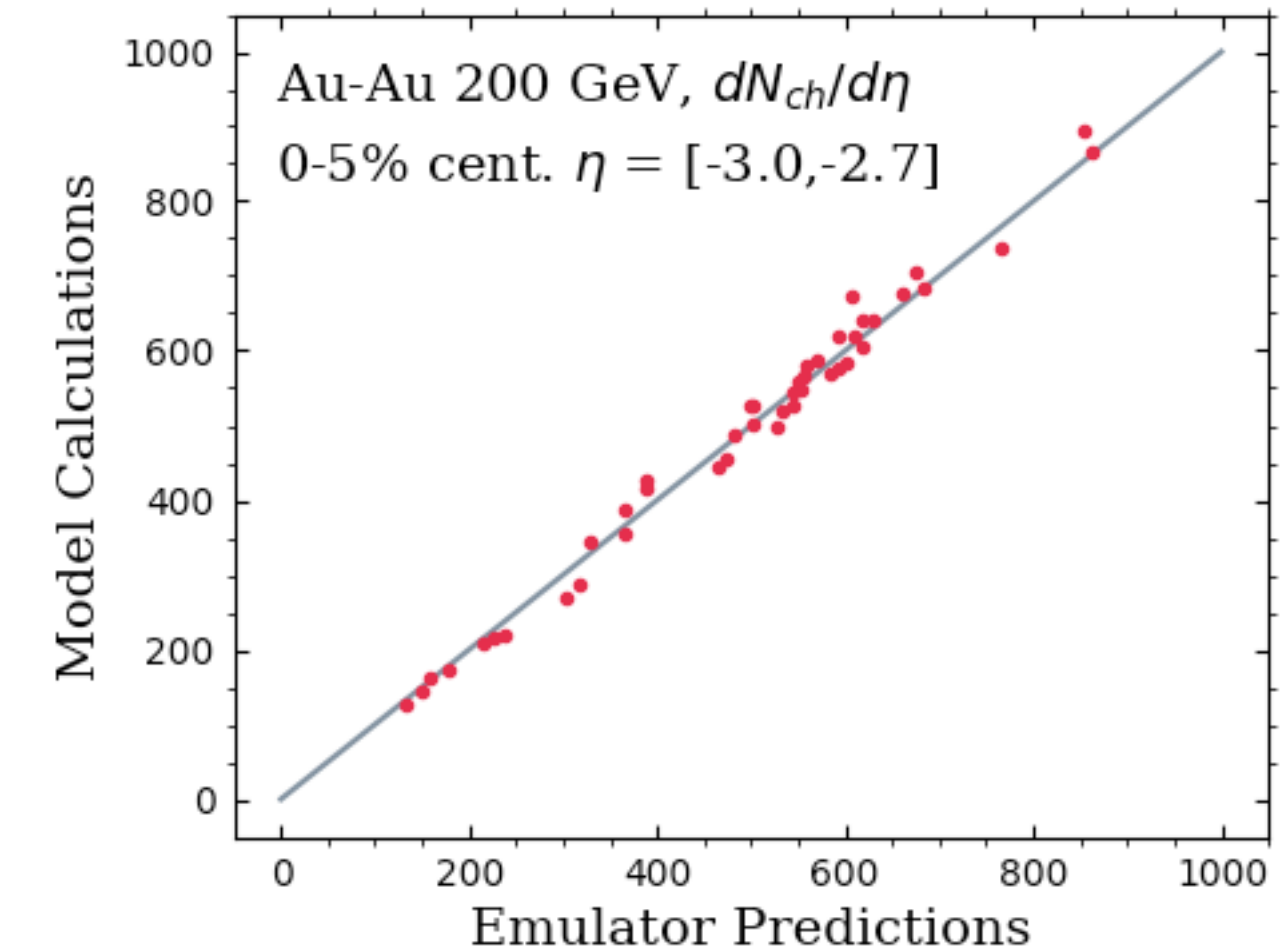
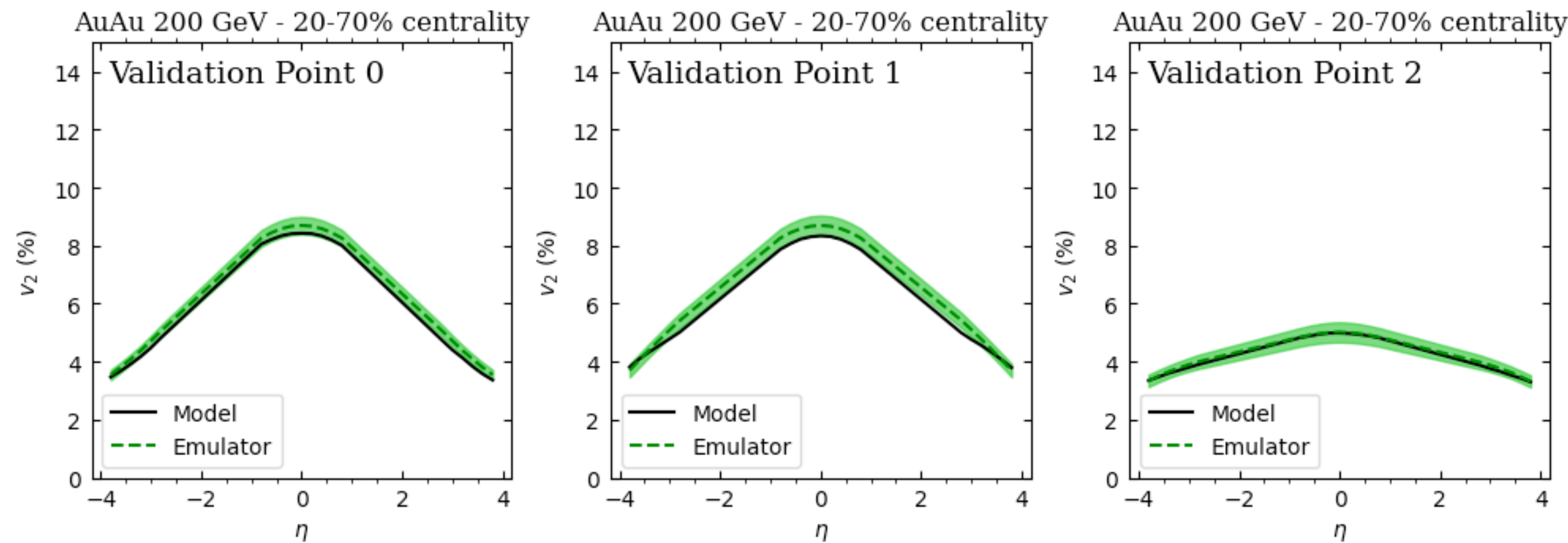
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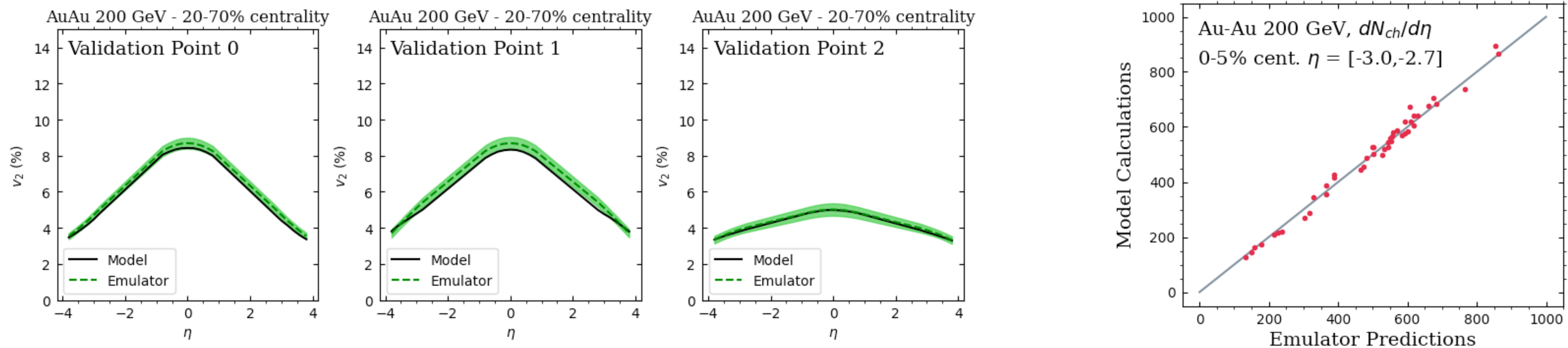
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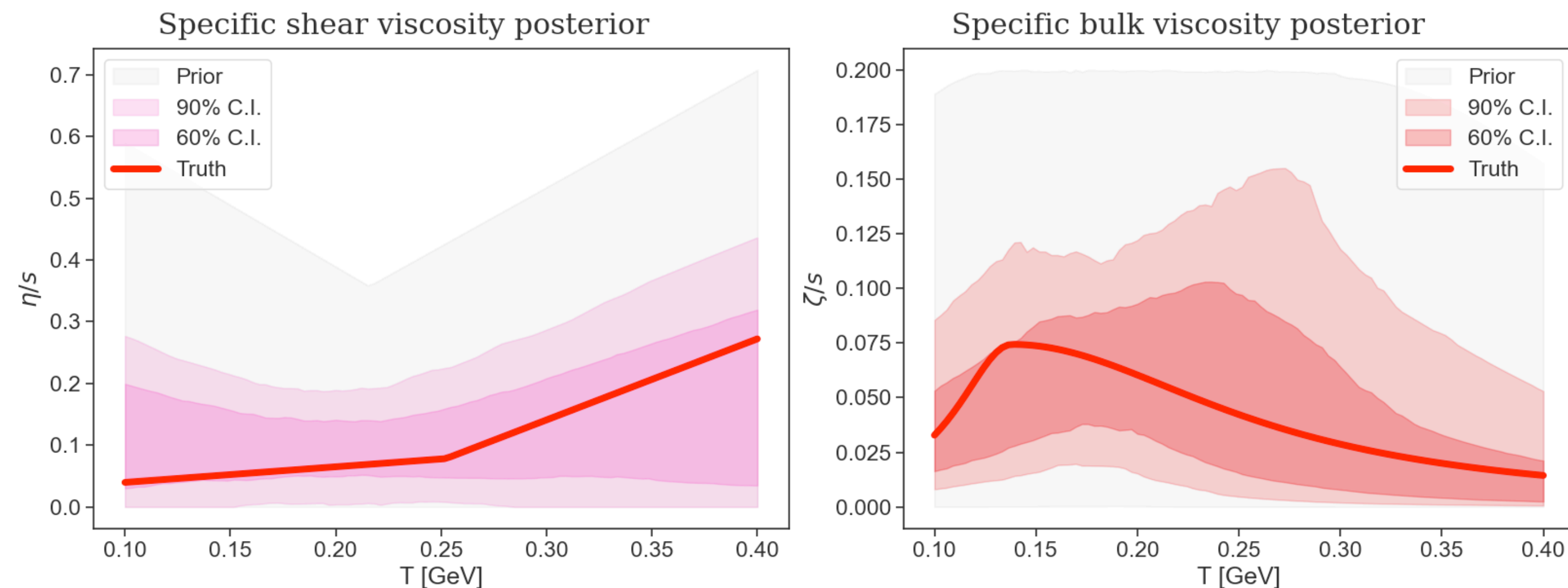


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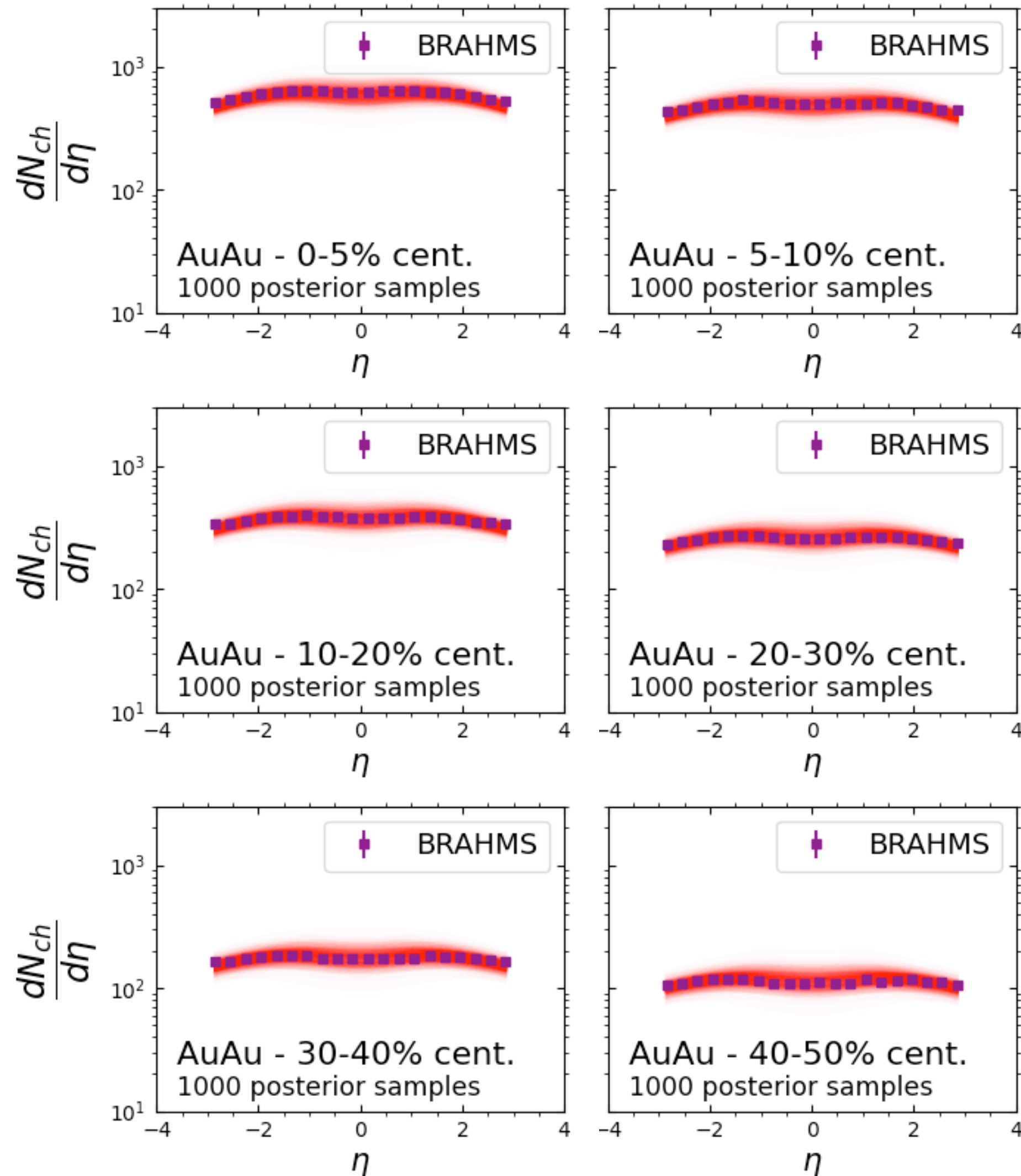
## Closure test with the viscosity parameters



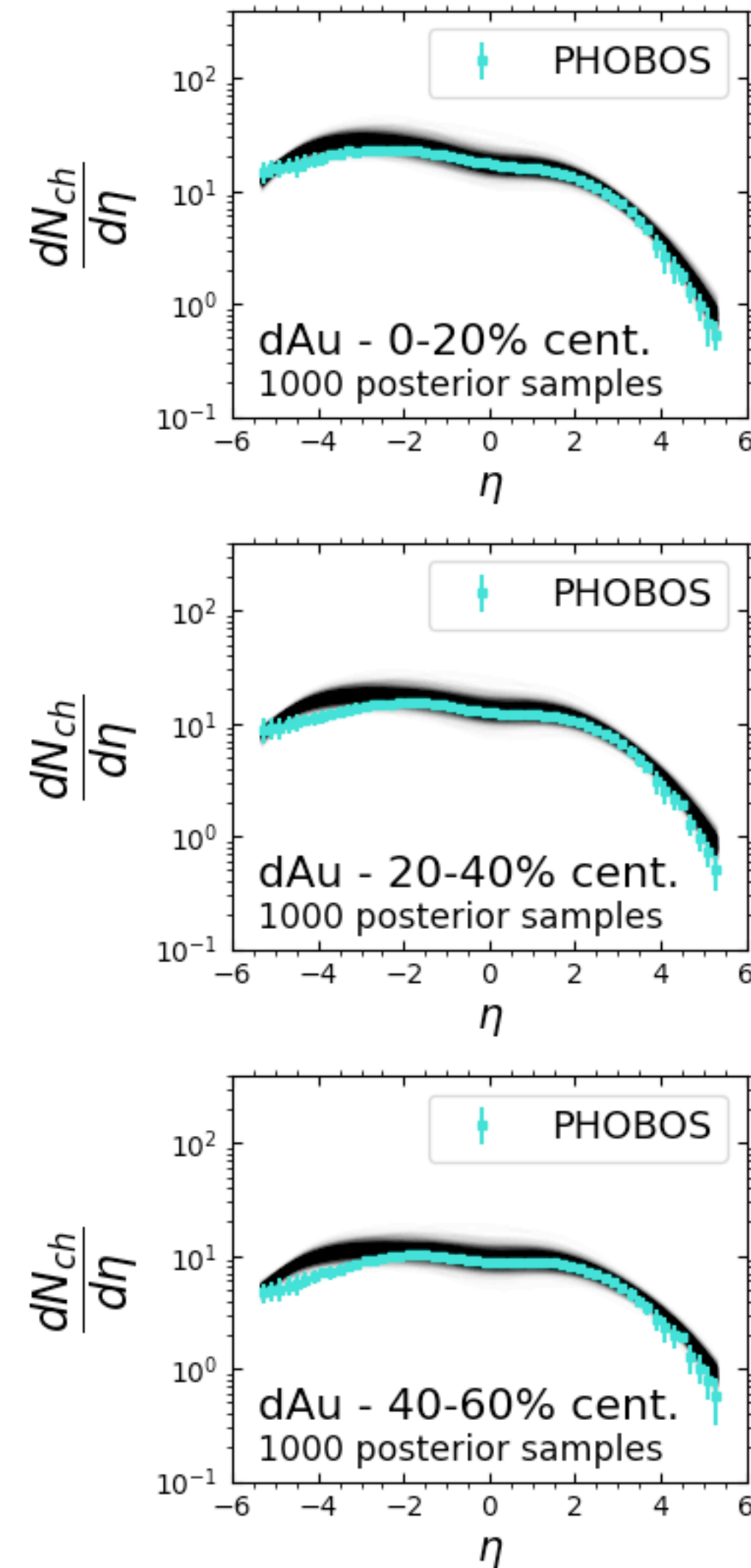


# Comparing with Experimental Data

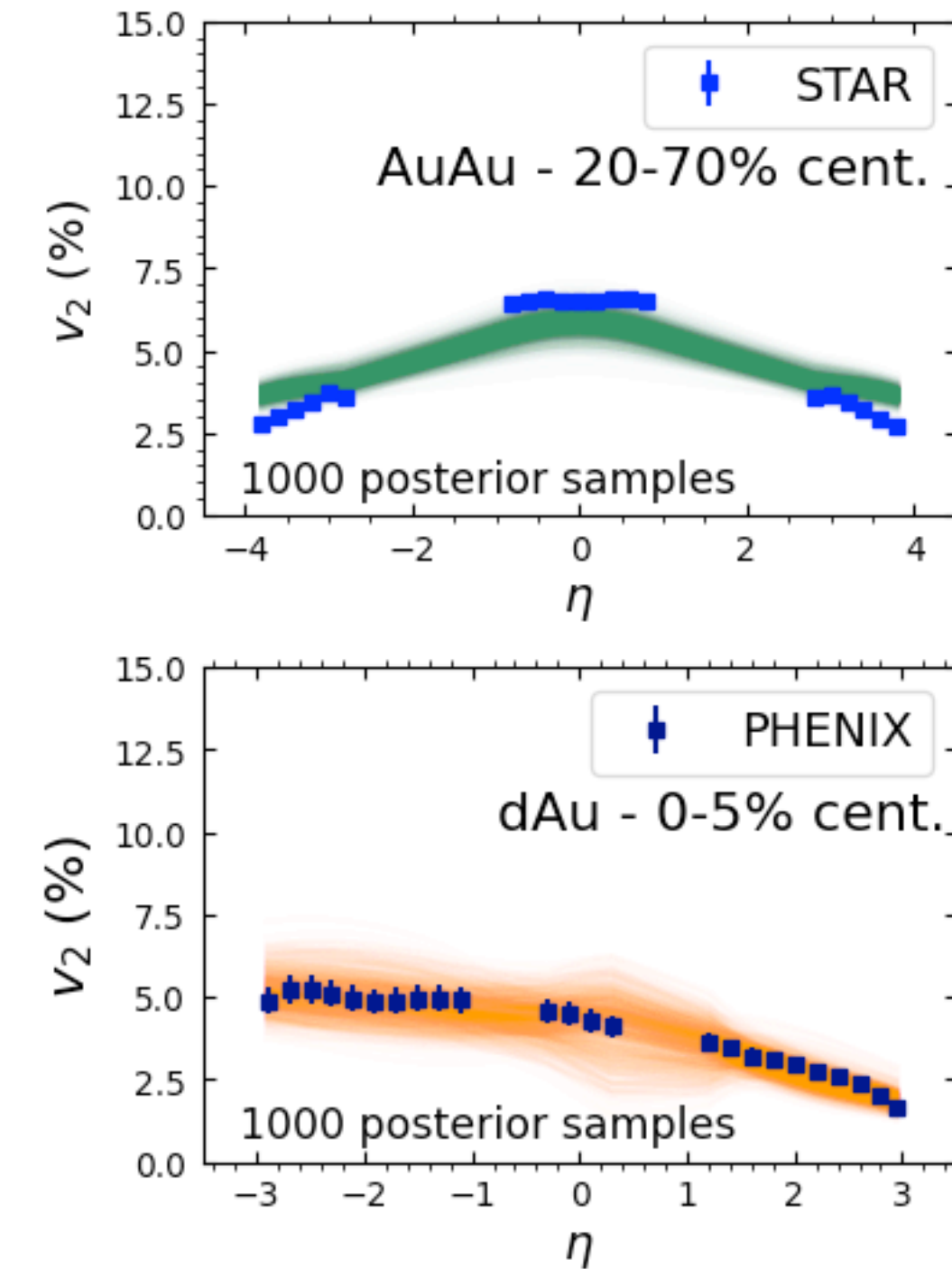
## Multiplicity in Au-Au



## Multiplicity in d-Au

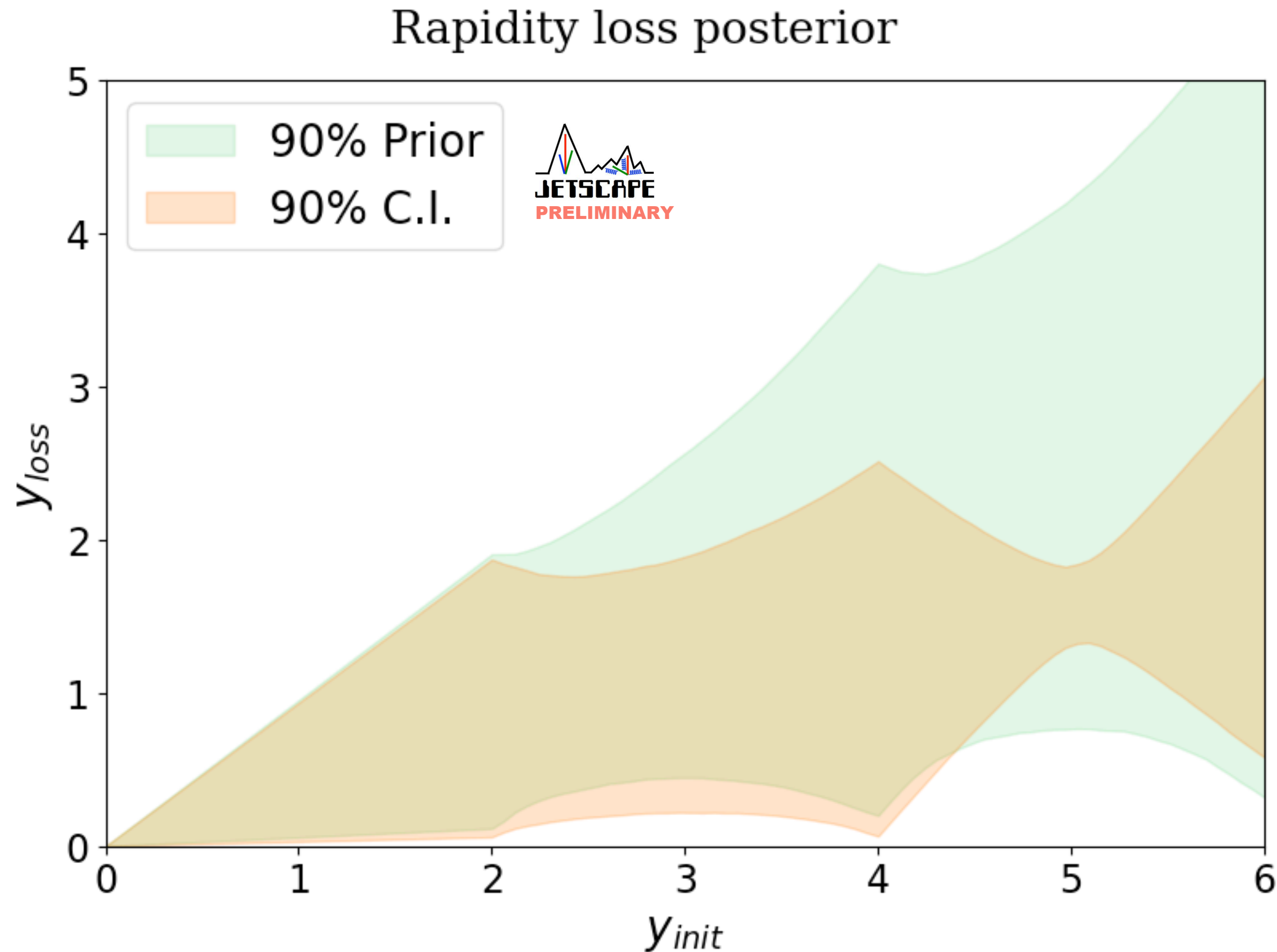


## Flow in Au-Au and d-Au



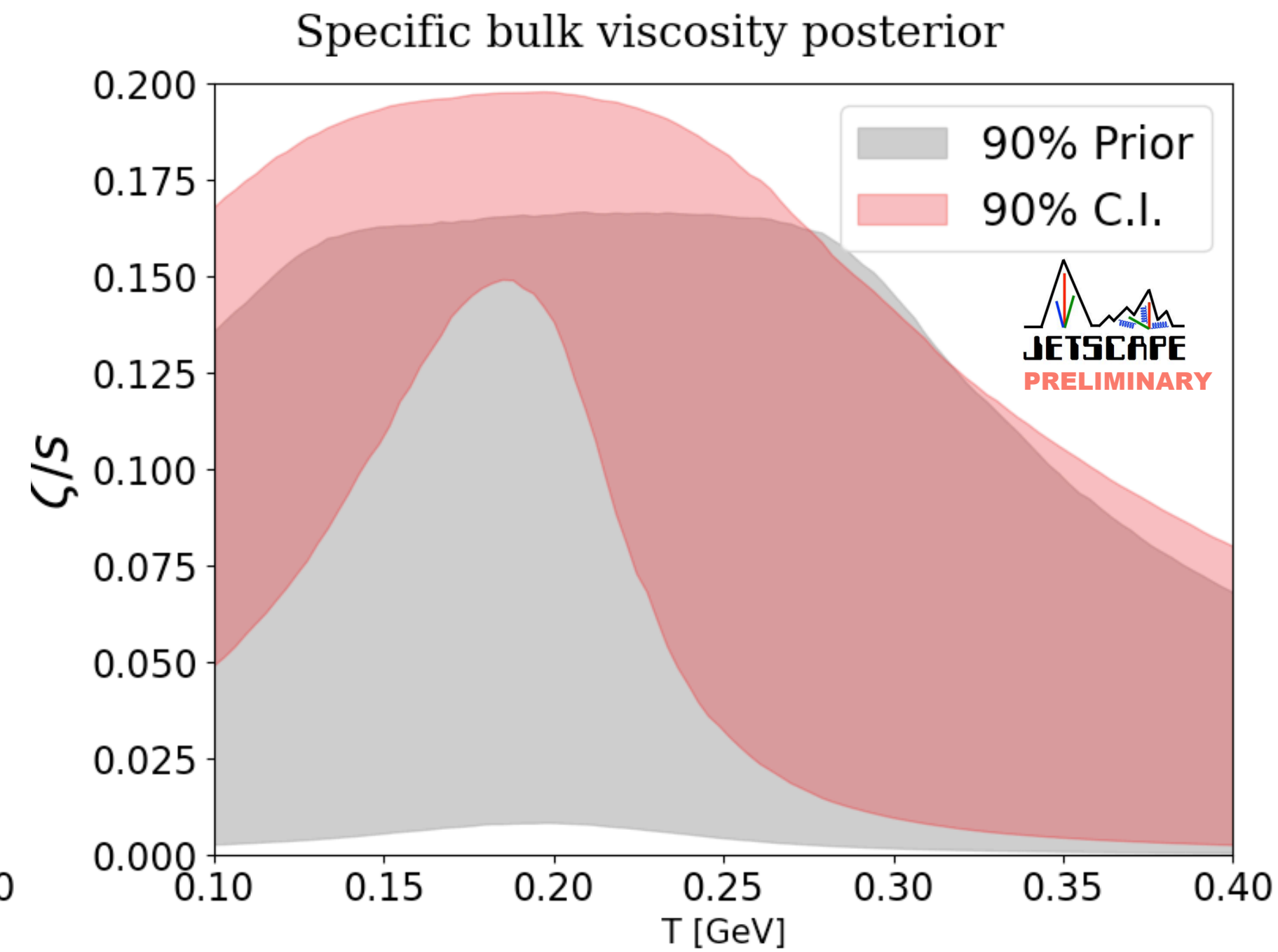
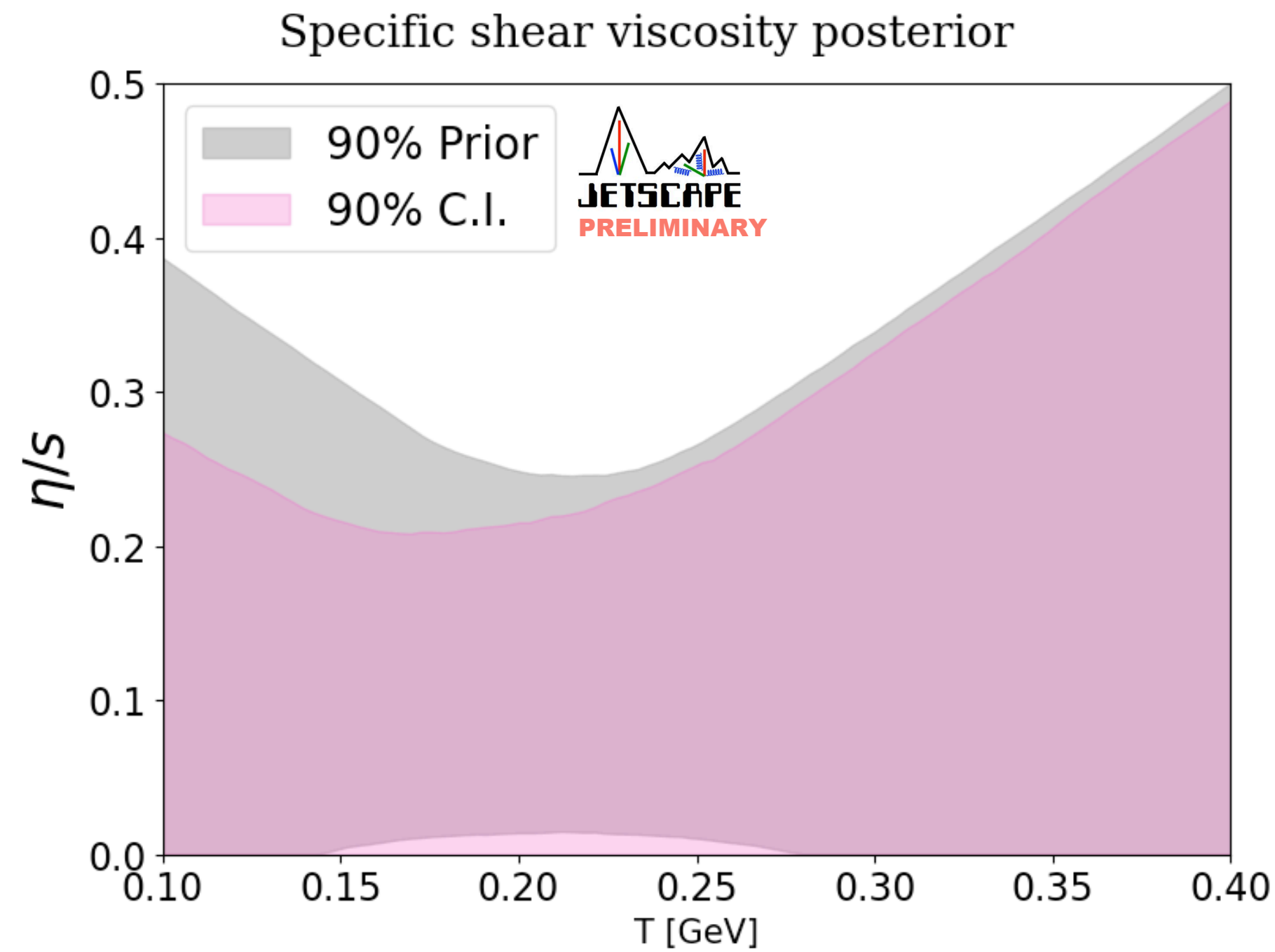
Good agreement with data across systems, observables, pseudorapidity, centrality, and experiment

# Parameter Posteriors - Rapidity Loss

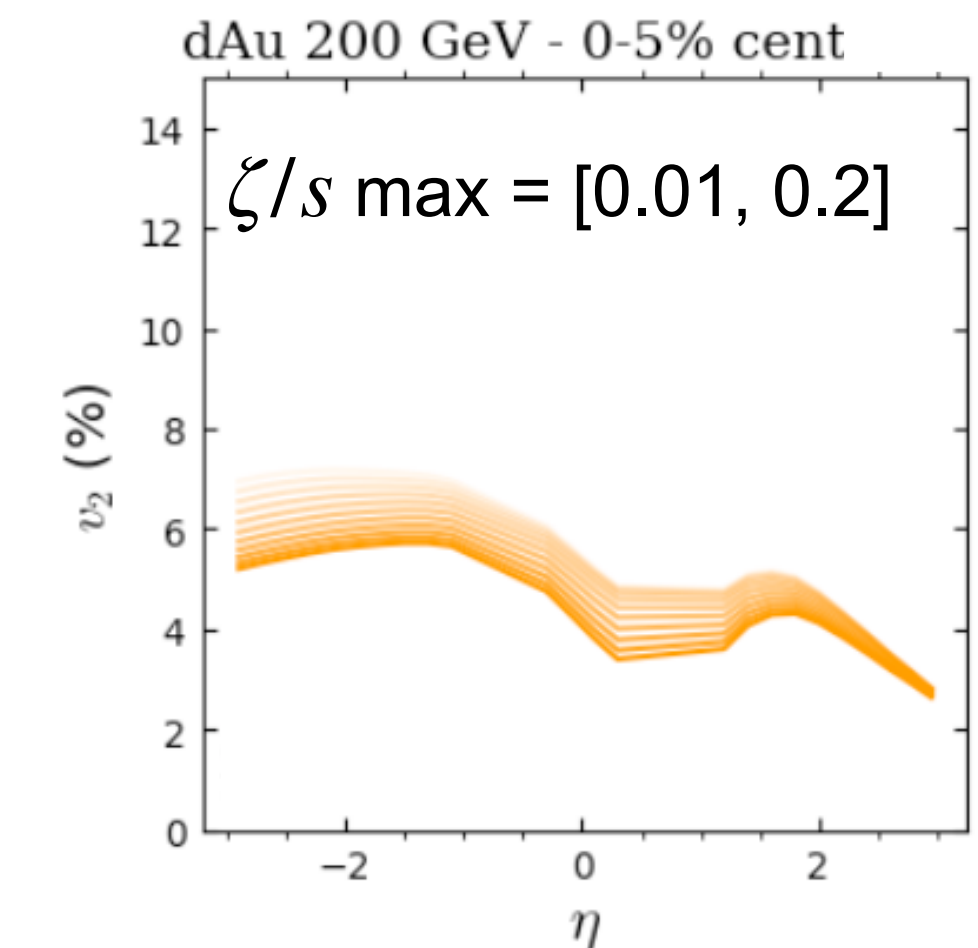
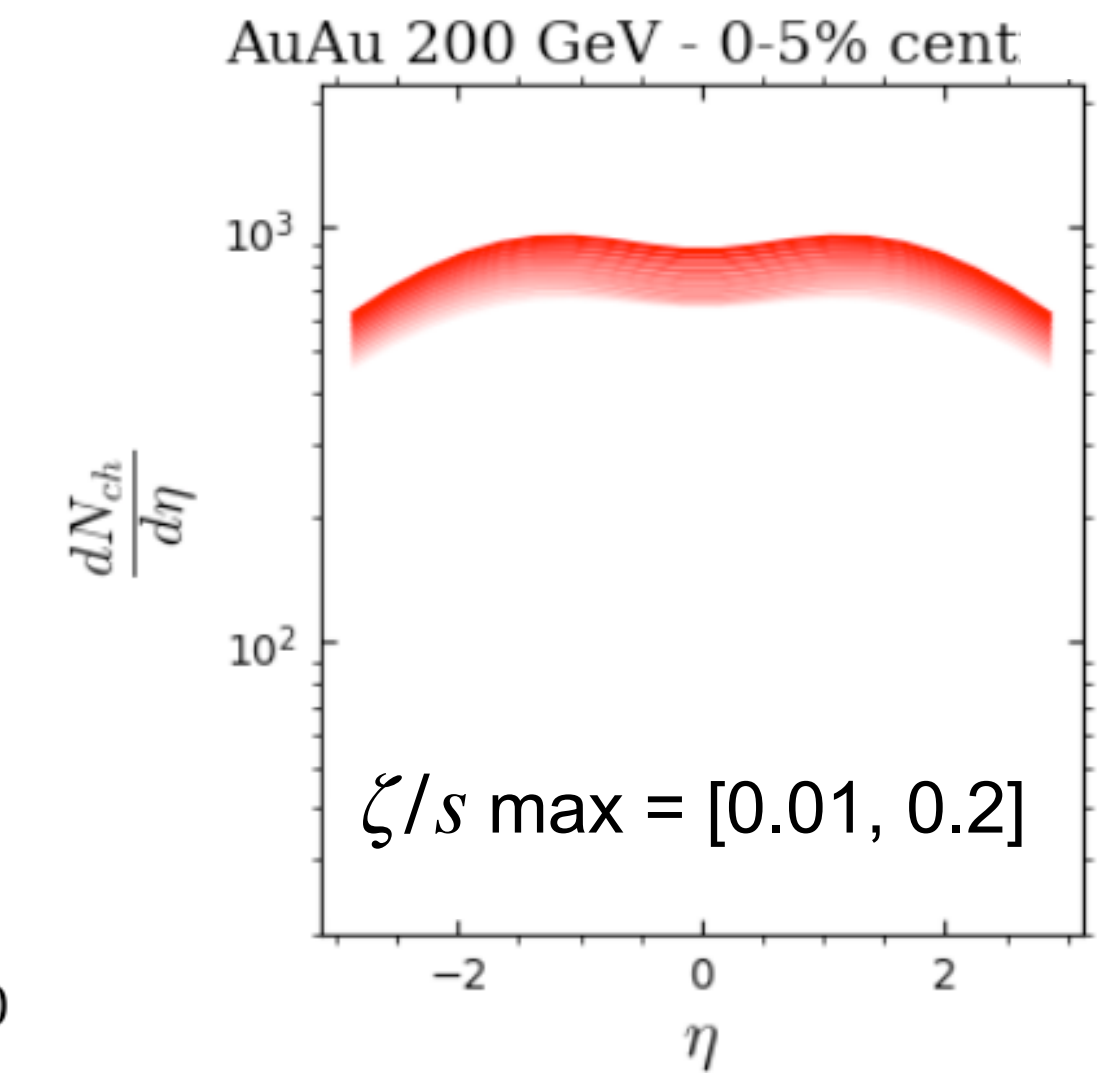


- Initial state energy deposition well constrained, particularly around 5 units of incoming rapidity
- Comparison with data from systems at lower energies may provide stronger constraints in the lower incoming rapidity region

# Parameter Posteriors - Viscosity



Sensitivity of observables to the max of the bulk viscosity

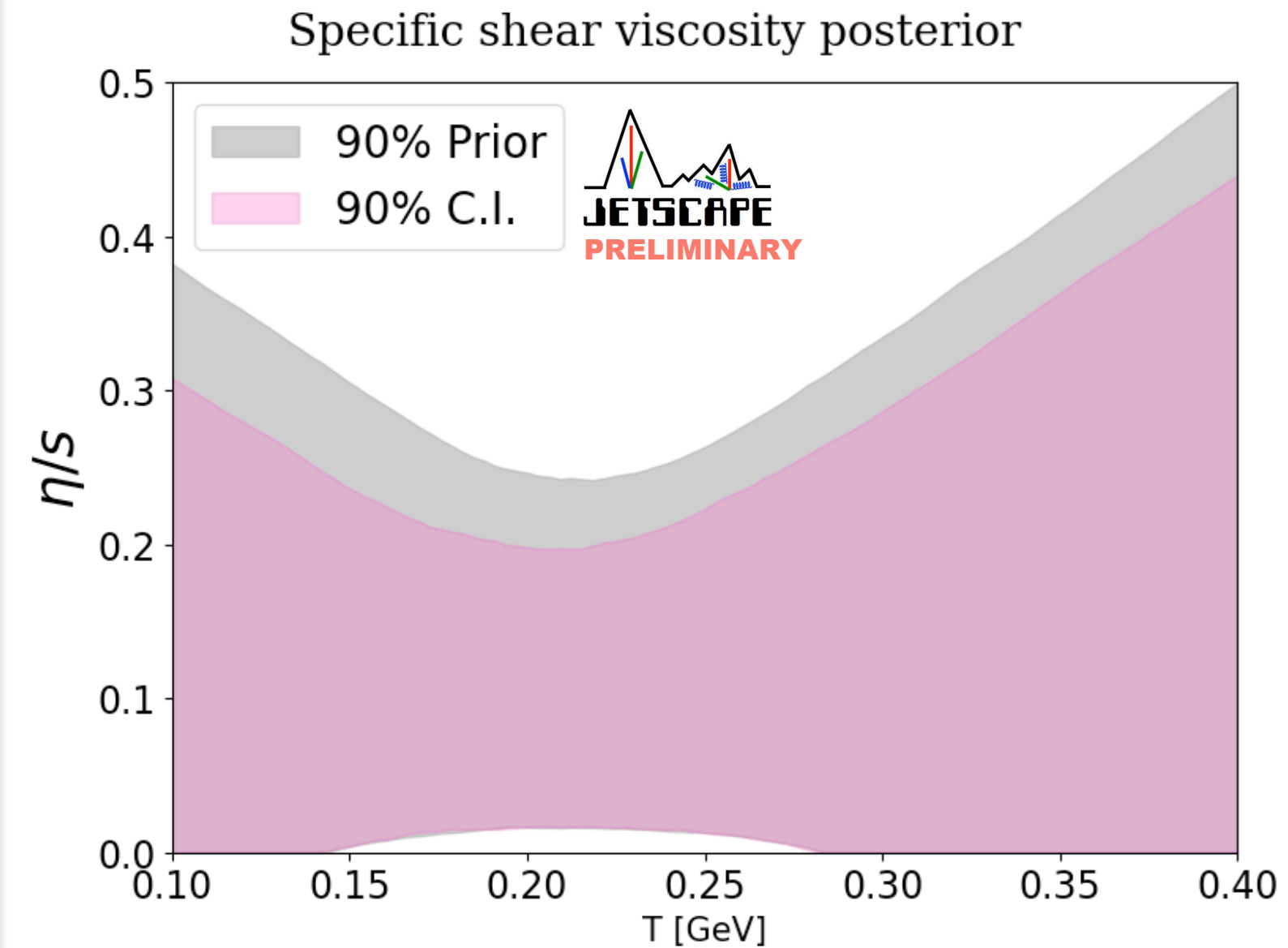
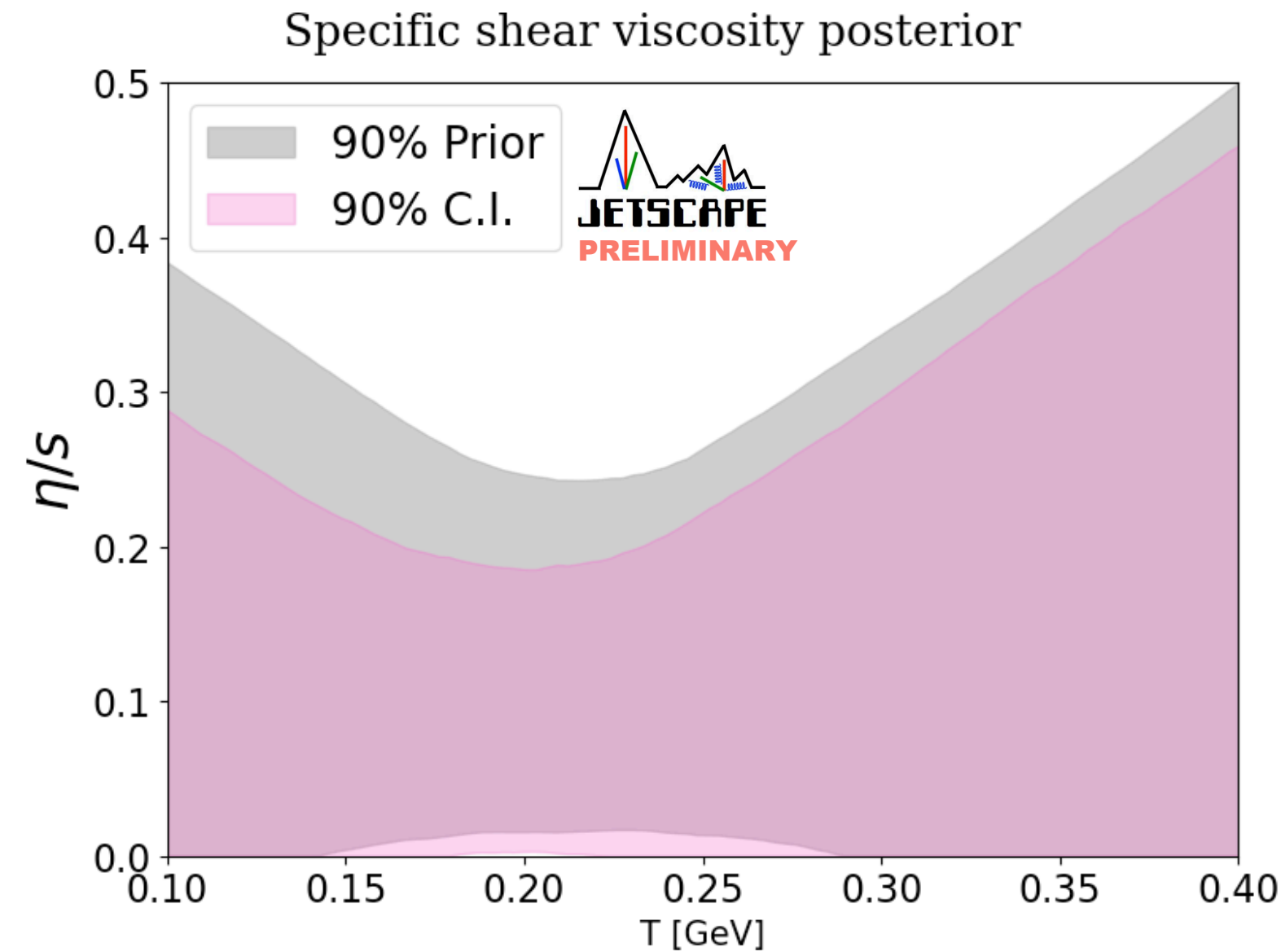


- Strong constraints showing a large bulk viscosity
- Weak constraints on the shear viscosity



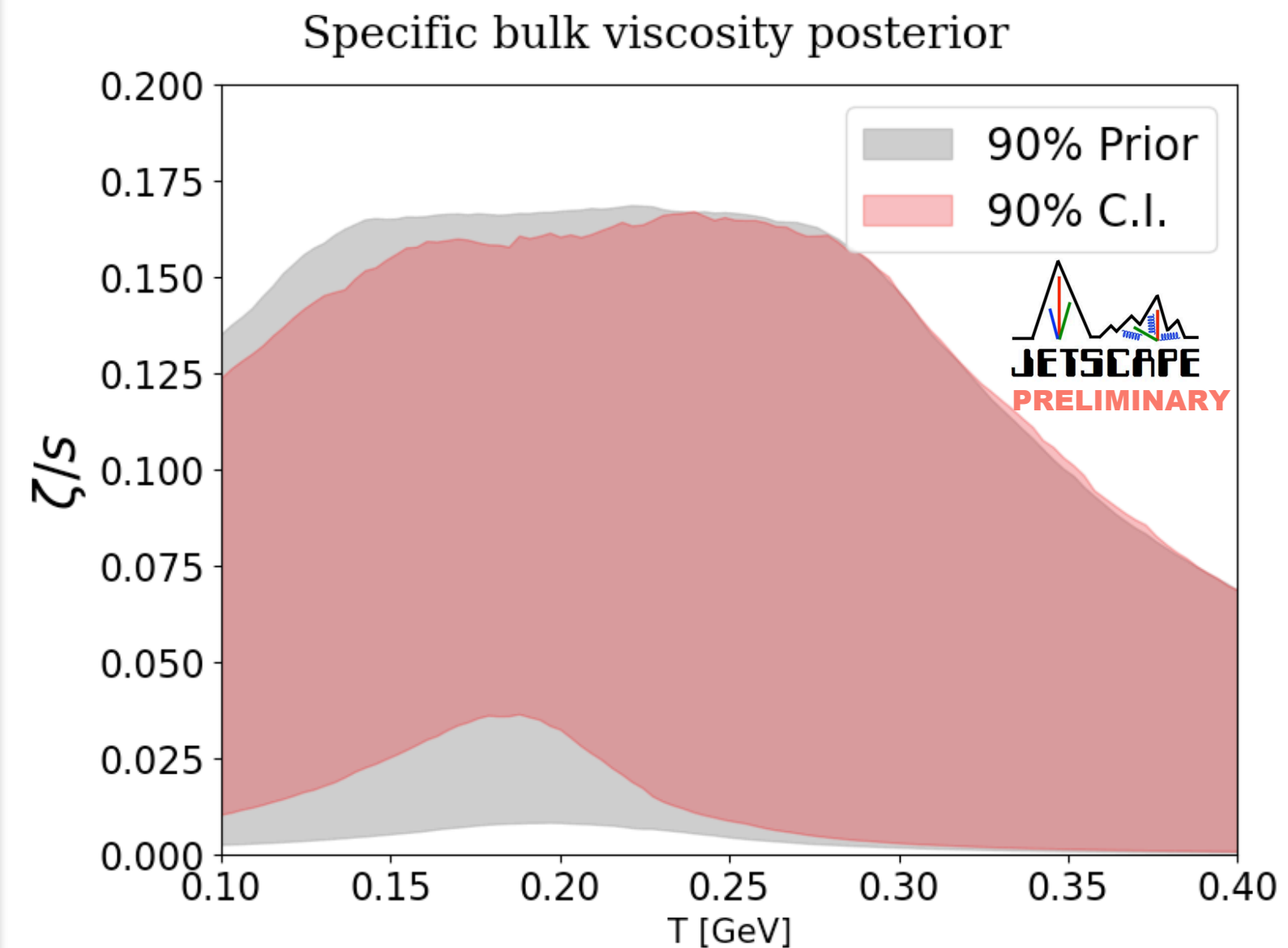
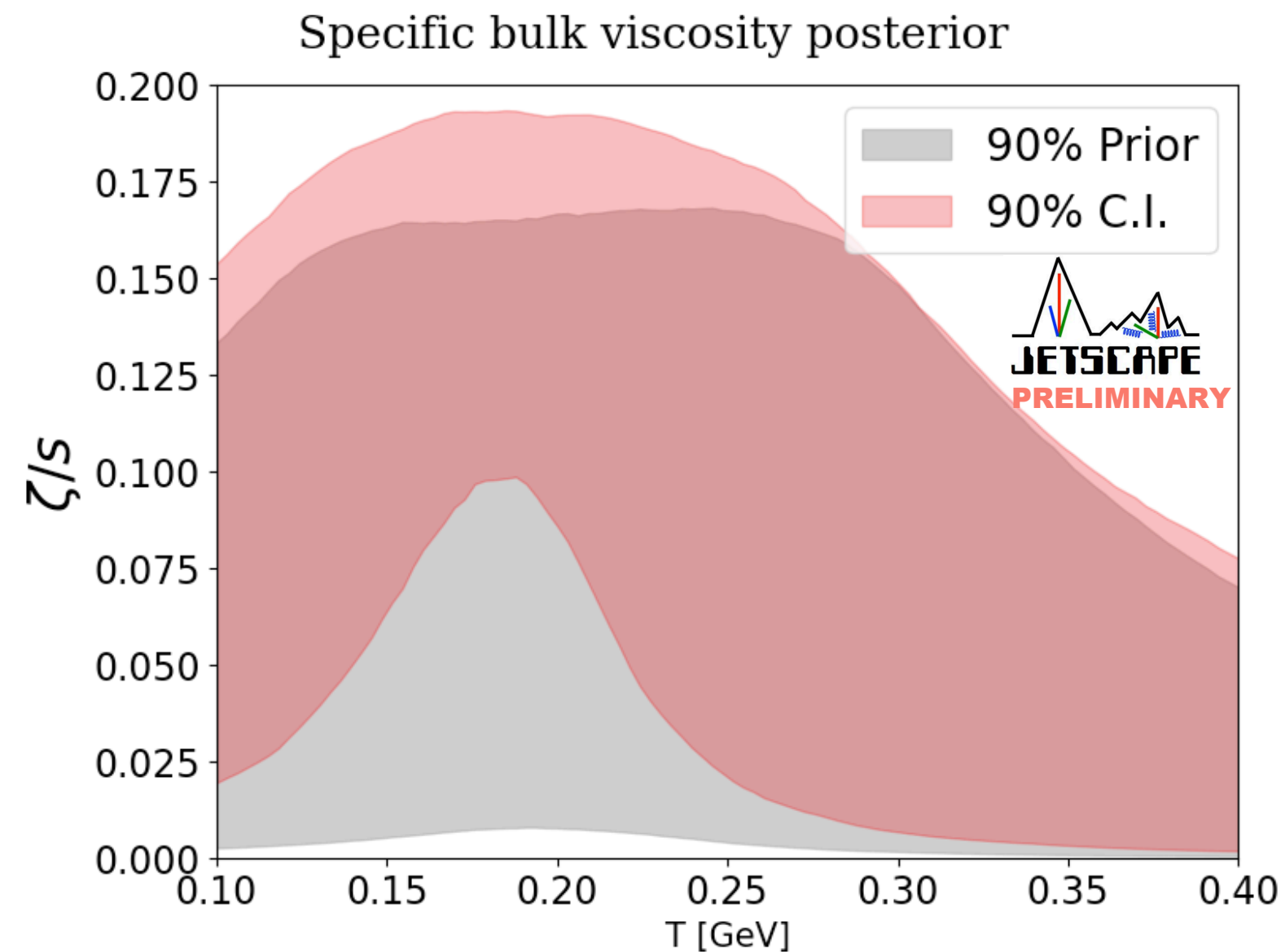
# Au-Au vs d-Au constraints

Constrained  
on ***Au-Au***  
***only***



Constrained  
on ***d-Au***  
***only***

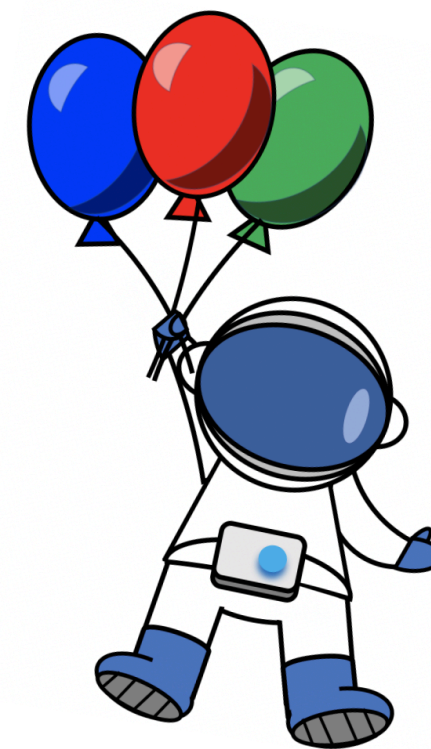
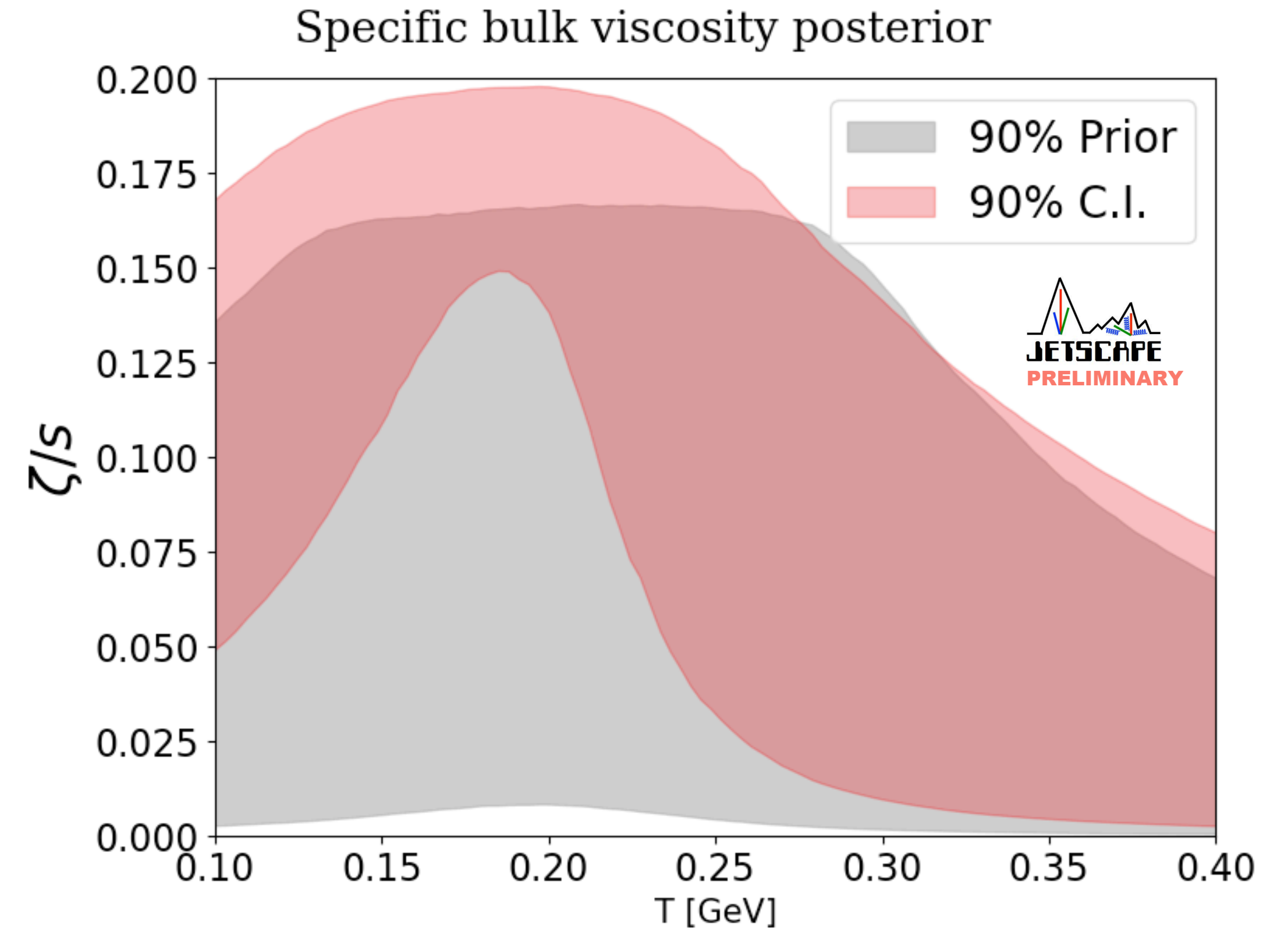
Stronger  
constraints  
provided on  
bulk viscosity  
by Au-Au  
measurements



Slight  
preference  
for  $\zeta/s \neq 0$   
in d-Au also

# Conclusions and Outlook

- Successfully describe data across pseudo-rapidity for large and small systems at 200 GeV
- Multiplicity and flow measurements at forward rapidities indicate a large bulk viscosity
- **Stay tuned** for 3D calibration using broader set of experimental data



# THANK YOU!





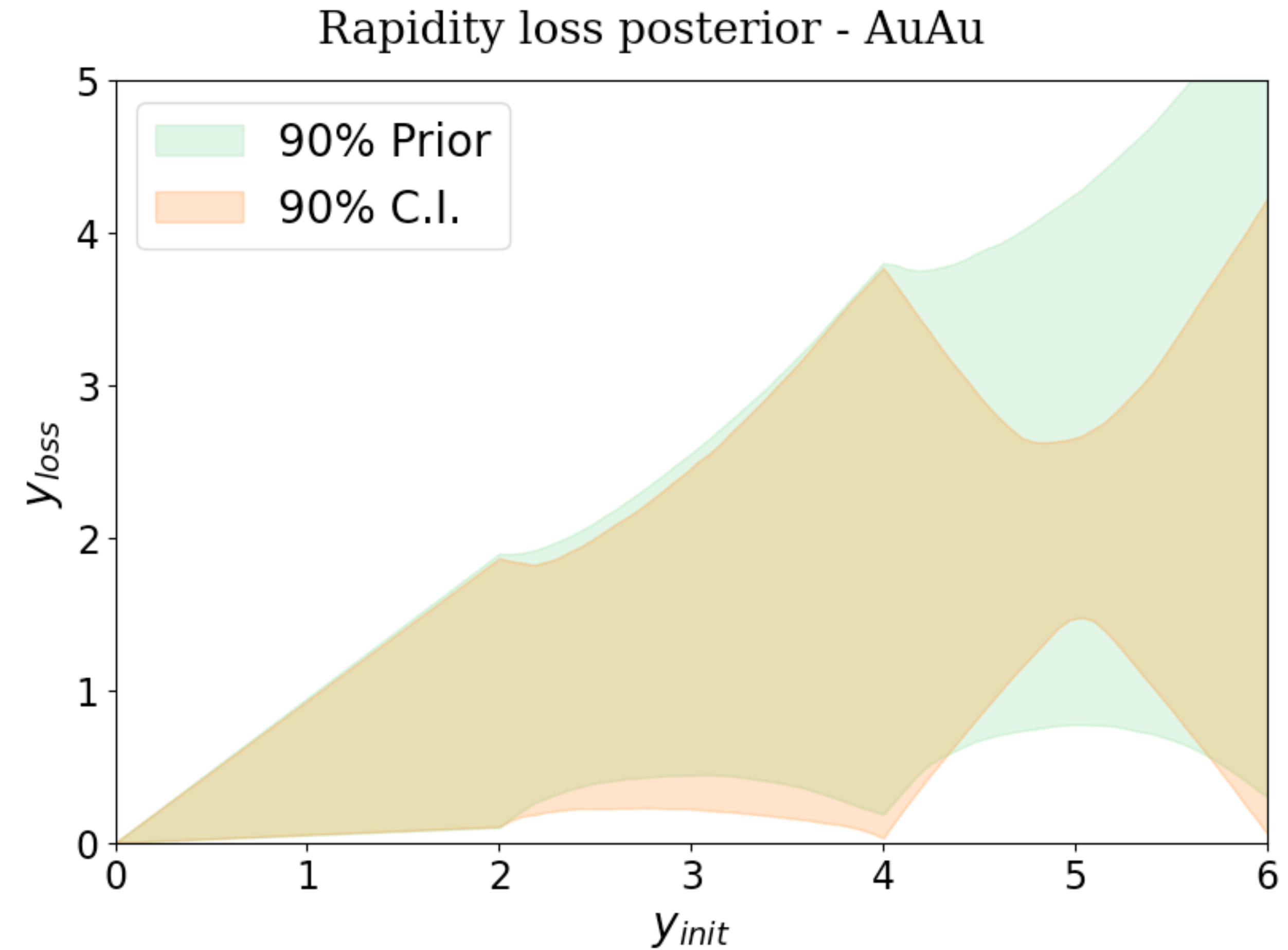
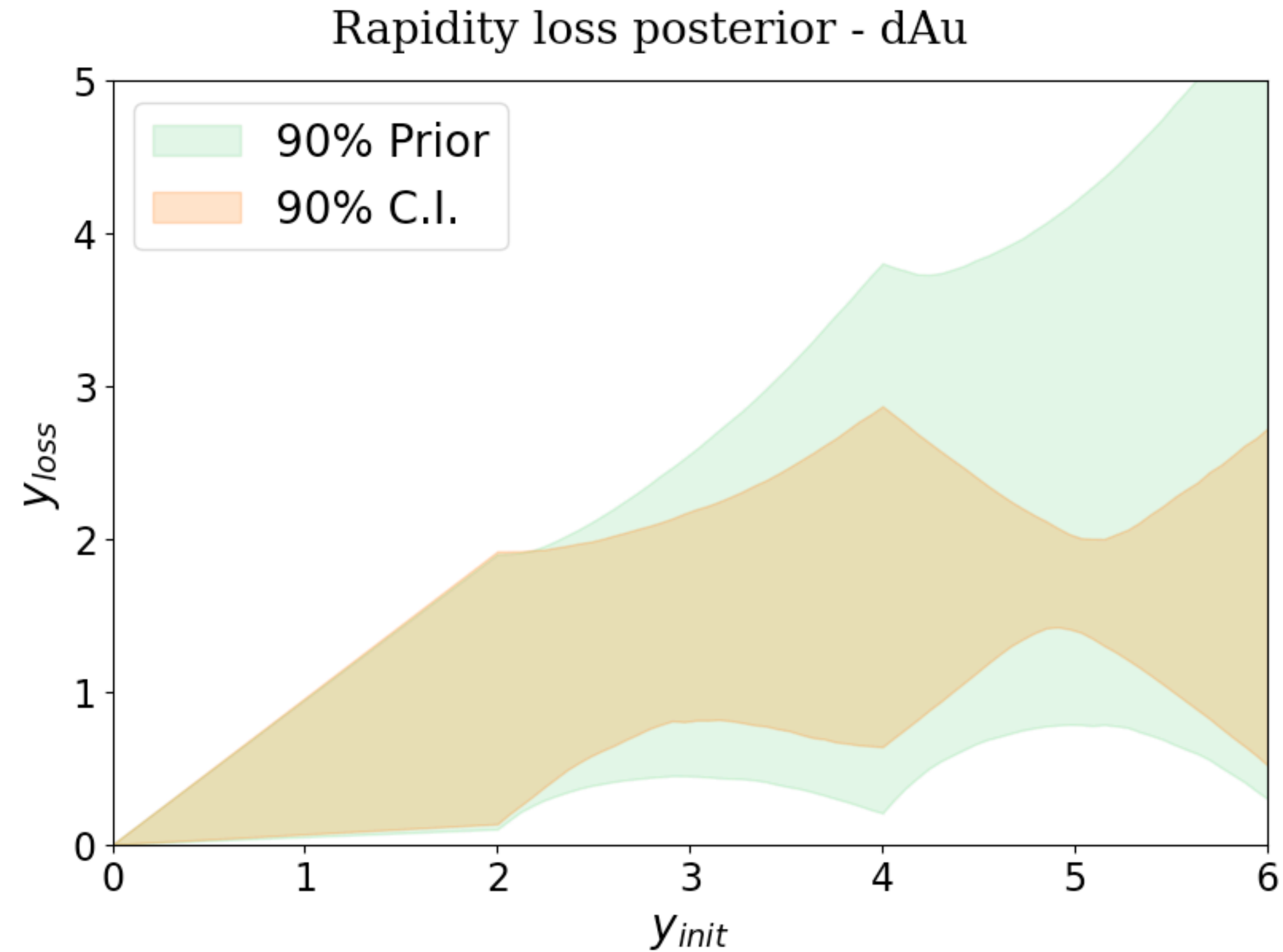
# Acknowledgements

## JETSCAPE COLLABORATION



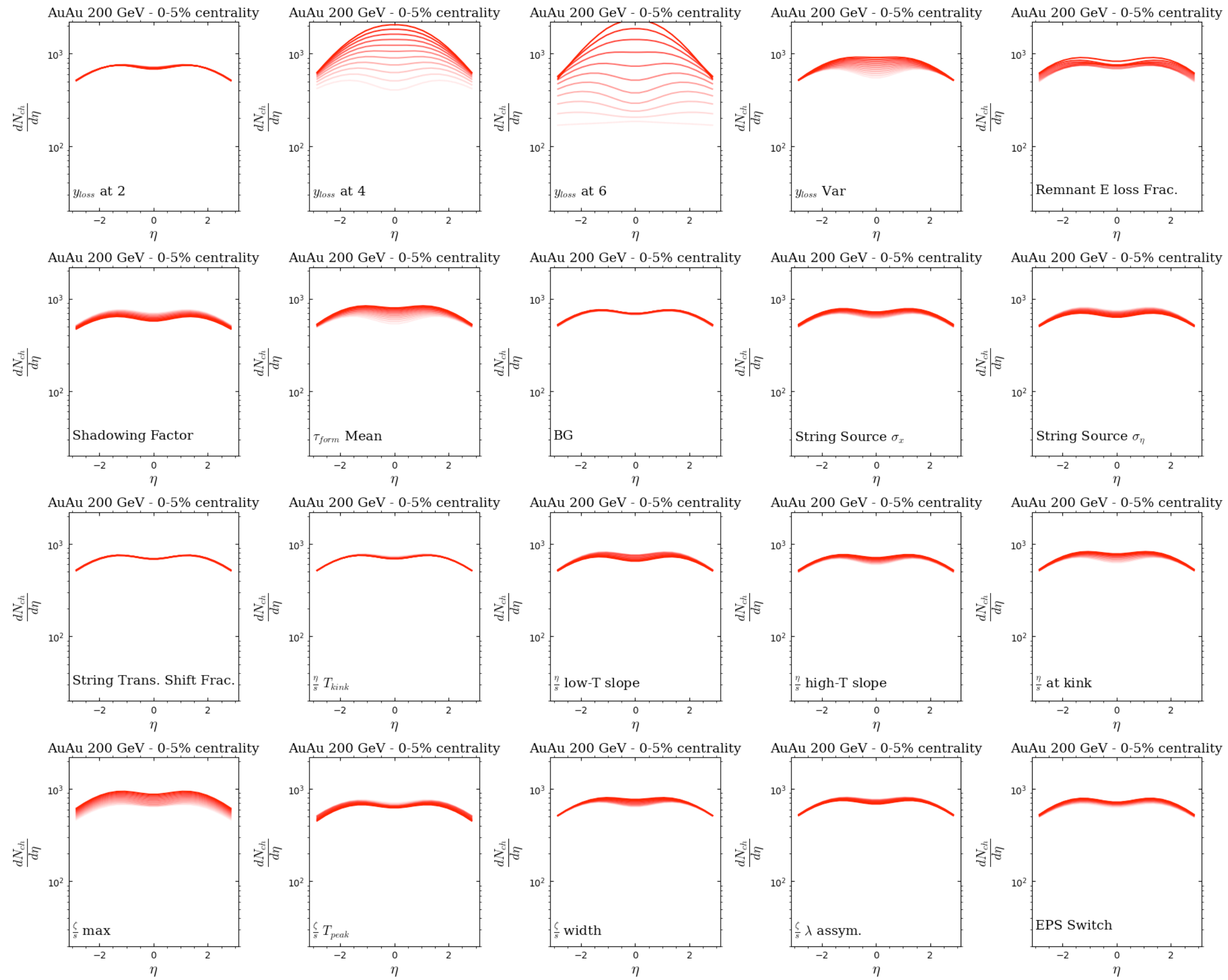


# Constraints on rapidity loss from dAu or AuAu only



# Sensitivity of AuAu $dN_{ch}/d\eta$ to parameters

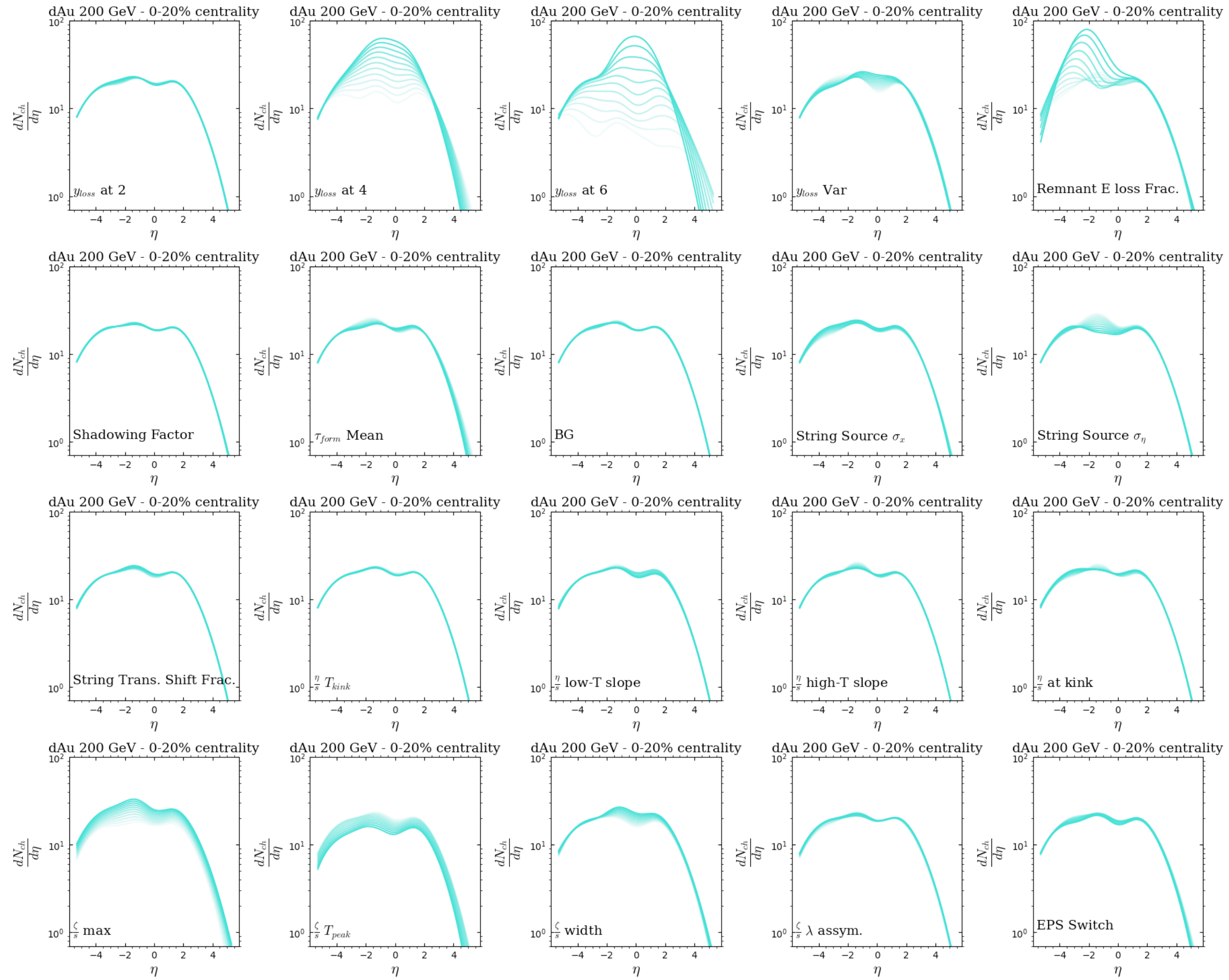
Sensitivity to Parameters





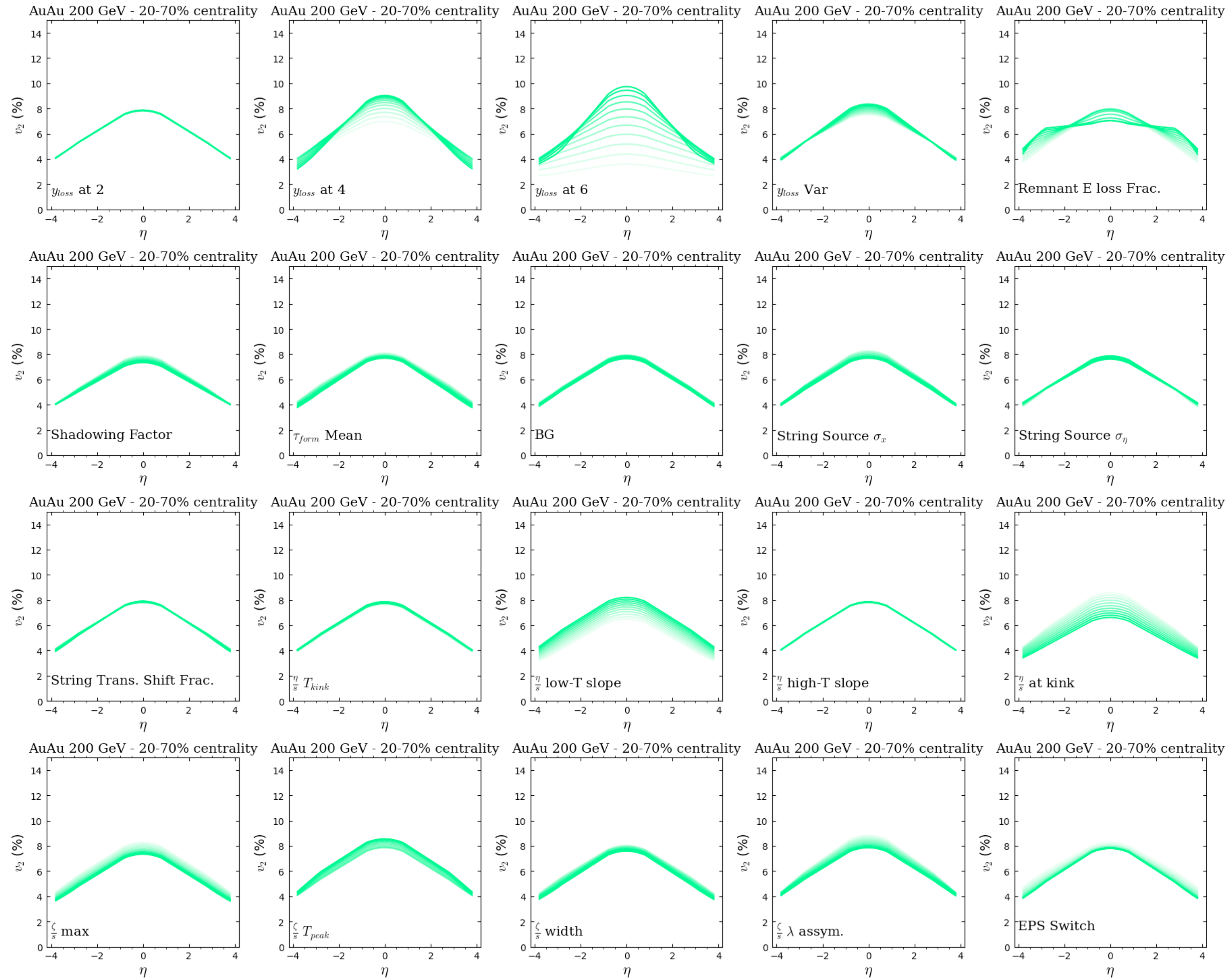
# Sensitivity of dAu $dN_{ch}/d\eta$ to parameters

Sensitivity to Parameters



# Sensitivity of AuAu $v_2$ to parameters

Sensitivity to Parameters





# Sensitivity of dAu $v_2$ to parameters

Sensitivity to Parameters

